Probing the odderon through η_c production in diffractive collisions at the EIC

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Benić, Horvatić, Kaushik, Vivoda, in preparation

QCD Evolution, Orsay, May 27, 2023



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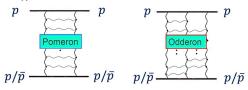
Odderon

C-odd counterpart of the C-even pomeron: a colour-neutral t-channel strong exchange.

• First suggested as mechanism to explain differences in pp vs $p\bar{p}$ elastic cross-sections

Łukaszuk, Nicolescu, LNC 8 (1973) 40

 At lowest order in QCD, exchange of three gluons in a colour singlet state: d^{abc}A^a_μA^b_μA^c_λ



https://blog.hip.fi/the-discovery-of-the-odderon/

• Recent results by TOTEM and D0 indicate a non-zero odderon TOTEM, D0, PRL 127 (2021) 6, 062003

How do we understand it in a perturbative QCD framework?

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Exclusive η_c **production:** $ep \rightarrow e + p + \eta_c$

Production of C-even mesons in ep collisions offer a clean environment to probe the odderon

- η_c has been suggested as a golden probe: η_c has C = +1, photon has C = -1, therefore strong exchange should have C = -1.
- Charm quark production ensures sensitivity to gluon content of proton.
- So far no exclusive measurements of η_c production. Could be measured at the Electron-Ion Collider.

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Exclusive η_c **production:** $ep \rightarrow e + p + \eta_c$

Lots of work done on this probe: Czyzewski, Kwiecinski, Motyka, Sadzikowski, PLB 398 (1997) 400 [Erratum PLB 411 (1997) 402] Engel, Ivanov, Kirschner, and Szymanowski, EPJC 4 (1998) 93 Bartels, Braun, Colferai, Vacca, EPJC 20 (2001) 323 Ma, NPA 727 (2003) 333 Goncalves, NPA 902 (2013) 32 Dumitru, Stebel, PRD 99 (2019) 094038

- Studies so far focussed on dilute regime, moderate-*x*, gluon density not too large
- Newer calculations sugggest far smaller differential cross-sections than older calculations: dσ/d|t| ~ O(fb/GeV²) vs O(pb/GeV²)

In this work:

- We focussed on the dense regime, small-x, where gluon density is larger and saturation effects may be relevant
- We considered nuclear targets as well, which can be studied at the EIC and which again offer a dense gluon environment

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Odderon in a CGC framework

Small-x regime, dense target \implies Colour-Glass condensate framework

• Gluon distributions are given through correlators of Wilson lines

$$V(\mathbf{z}_{\perp}) = \mathcal{P} \exp\left\{ ig \int dz^{-} A^{+}(z^{-}, \mathbf{z}_{\perp})
ight\}$$

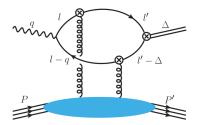
• Odderon is the imaginary parton of the dipole distribution,

$$\mathcal{O}(\mathbf{x}_{\perp},\mathbf{y}_{\perp})\equiv-rac{1}{2iN_{c}}\mathrm{tr}\langle V(\mathbf{x}_{\perp})V^{\dagger}(\mathbf{y}_{\perp})-V(\mathbf{y}_{\perp})V^{\dagger}(\mathbf{x}_{\perp})
angle$$

 Energy evolution given by JIMWLK equations, reduces to coupled BK equations for the odderon and the pomeron in the large N_c limit

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Calculating η_c production in a CGC framework



$$\mathcal{S}_{\lambda} = (eq_c) \int_{ll'} \operatorname{Tr} \left[S(l) \notin (\lambda, q) S(l-q) \tau (l-q, l'-\Delta) S(l'-\Delta) (i\gamma_5) S(l') \tau (l', l) \right]$$

• CGC vertex: $\tau(\boldsymbol{p}, \boldsymbol{p}') = (2\pi)\delta(\boldsymbol{p}^- - \boldsymbol{p}'^-)\gamma^- \operatorname{sgn}(\boldsymbol{p}^-) \int_{\boldsymbol{z}_\perp} e^{-i(\boldsymbol{p}_\perp - \boldsymbol{p}'_\perp) \cdot \boldsymbol{z}_\perp} V^{\operatorname{sgn}(\boldsymbol{p}^-)}(\boldsymbol{z}_\perp)$

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Calculating η_c production in a CGC framework

After some algebra,

$$\begin{split} \langle \mathcal{S}_{\lambda} \rangle &= - \left\langle \mathcal{M}_{\lambda} \right\rangle (2\pi) \delta(q^{-} - \Delta^{-}) \\ \langle \mathcal{M}_{\lambda} \rangle &= (eq_{c}) \int_{\mathbf{r}_{\perp}} \int_{ll'} (2\pi) \delta(l^{-} - l'^{-}) \theta(l^{-}) \theta(q^{-} - l^{-}) \mathrm{e}^{-\mathrm{i}(l'_{\perp} - l_{\perp} - \frac{1}{2} \Delta_{\perp}) \cdot \mathbf{r}_{\perp}} \\ &\times (-\mathrm{i} N_{c}) \mathcal{O}(\mathbf{r}_{\perp}, \Delta_{\perp}) \mathrm{tr} \left[S(l) \notin (\lambda, q) S(l - q) \gamma^{-} S(l' - \Delta) (\mathrm{i} \gamma_{5}) S(l') \gamma^{-} \right] , \\ \mathbf{r}_{\perp} &= \mathbf{x}_{\perp} - \mathbf{y}_{\perp}, \qquad \mathbf{b}_{\perp} = \frac{\mathbf{x}_{\perp} + \mathbf{y}_{\perp}}{2} \end{split}$$

General features of amplitude:

• Longitudinal polarisation $\lambda = 0$ decouples, only transverse photon $\lambda = \pm 1$ contributes

$$\langle \mathcal{M}_{\lambda}
angle = q^{-} \mathrm{e}^{\mathrm{i} \lambda \phi_{\Delta}} \lambda \langle \mathcal{M}
angle$$

• Amplitude proportional to m_c : γ splits into a spin 1 $q\bar{q}$ state which transitions to an spin 0 meson - need a spin flip provided by m_c

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Accounting for small-x effects: BK equation

The Balitsky-Kovchegov equation describes the small-*x* evolution of the dipole distribution:

$$\frac{\partial \mathcal{D}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp})}{\partial Y} = \frac{\alpha_{5} N_{c}}{2\pi^{2}} \int_{\mathbf{r}_{1\perp}} \frac{\mathbf{r}_{\perp}^{2}}{\mathbf{r}_{1\perp}^{2} \mathbf{r}_{2\perp}^{2}} \left[\mathcal{D}(\mathbf{r}_{1\perp}, \mathbf{b}_{1\perp}) \mathcal{D}(\mathbf{r}_{2\perp}, \mathbf{b}_{2\perp}) - \mathcal{D}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \right]$$
$$\mathbf{r}_{2\perp} = \mathbf{r}_{\perp} - \mathbf{r}_{1\perp}$$
$$\mathcal{D}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \equiv \frac{1}{N_{c}} \operatorname{tr} \left\langle V\left(\mathbf{b}_{\perp} + \frac{\mathbf{r}_{\perp}}{2}\right) V^{\dagger}\left(\mathbf{b}_{\perp} - \frac{\mathbf{r}_{\perp}}{2}\right) \right\rangle = 1 - \mathcal{N}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) + i \mathcal{O}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp})$$

BK nonlocal in \boldsymbol{b}_{\perp} : $\boldsymbol{b}_{1\perp} = \boldsymbol{b}_{\perp} + (\boldsymbol{r}_{\perp} - \boldsymbol{r}_{1\perp})/2$, $\boldsymbol{b}_{2\perp} = \boldsymbol{b}_{\perp} - \boldsymbol{r}_{1\perp}/2$ and Odderon explicitly depends on \boldsymbol{b}_{\perp}

- In principle, we need to solve the fully impact parameter dependent BK
- In practice, we treat impact parameter b_{\perp} as an external parameter Lappi, Mäntysaari, PRD 88 (2013) 114020

$$\mathbf{r}_{1\perp},\,\mathbf{r}_{2\perp}<<\mathbf{b}_{\perp}$$

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BK equation

$$\begin{aligned} \frac{\partial \mathcal{N}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp})}{\partial Y} &= \int_{\mathbf{r}_{1\perp}} \mathcal{K}_{\mathrm{Bal}}(\mathbf{r}_{\perp}, \mathbf{r}_{1\perp}, \mathbf{r}_{2\perp}) \left[\mathcal{N}(\mathbf{r}_{1\perp}, \mathbf{b}_{\perp}) + \mathcal{N}(\mathbf{r}_{2\perp}, \mathbf{b}_{\perp}) - \mathcal{N}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \right] \\ &+ \mathcal{N}(\mathbf{r}_{1\perp}, \mathbf{b}_{\perp}) \mathcal{N}(\mathbf{r}_{2\perp}, \mathbf{b}_{\perp}) - \mathcal{O}(\mathbf{r}_{1\perp}, \mathbf{b}_{\perp}) \mathcal{O}(\mathbf{r}_{2\perp}, \mathbf{b}_{\perp}) \right] ,\\ \frac{\partial \mathcal{O}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp})}{\partial Y} &= \int_{\mathbf{r}_{1\perp}} \mathcal{K}_{\mathrm{Bal}}(\mathbf{r}_{\perp}, \mathbf{r}_{1\perp}, \mathbf{r}_{2\perp}) \left[\mathcal{O}(\mathbf{r}_{1\perp}, \mathbf{b}_{\perp}) + \mathcal{O}(\mathbf{r}_{2\perp}, \mathbf{b}_{\perp}) - \mathcal{O}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) - \mathcal{O}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \right] . \end{aligned}$$

• Odderon and pomeron evolution coupled by nonlinear terms

Small r_{\perp} limit: system decouples, odderon exponentially suppressed

 $\mathcal{O} \sim \exp(-cY)$

Large r_{\perp} limit: $\mathcal{N}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \rightarrow 1$, nonlinear terms result in exponential suppression

$$\mathcal{O} \sim \exp(-cY)$$

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Initial conditions

For pomeron, we use a fit to HERA data,

$$\mathcal{N}(\mathbf{r}_{\perp}, \boldsymbol{b}_{\perp}) = 1 - \exp\left[-\frac{1}{4}\mathbf{r}_{\perp}^{2}AT_{A}(\boldsymbol{b}_{\perp})\frac{\sigma_{0}}{2}Q_{S,0}^{2}\log\left(\frac{1}{r_{\perp}\Lambda_{\rm QCD}} + \boldsymbol{e}_{c}\mathrm{e}\right)\right]$$

Lappi, Mäntysaari, PRD 88 (2013) 114020 Woods-Saxon transverse profile:

$$T_{A}(\boldsymbol{b}_{\perp}) = \int_{-\infty}^{\infty} \mathrm{d}z \frac{n_{A}}{1 + \exp\left[\frac{\sqrt{\boldsymbol{b}_{\perp}^{2} + z^{2}} - R_{A}}{d}\right]}$$

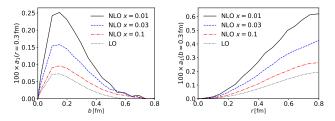
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Initial conditions

For odderon, depending on the target,

 DMP: For proton, we use a recent light-front NLO calculation of the odderon by Dumitru, Mäntysaari and Paatelainen Dumitru, Mäntysaari, Paatelainen, PRD 107 (2023) 1, L011501



- Initial x = 0.01 (black curve)
- Odderon peak lies well within the proton $\sim~0.25 imes R_p$

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Initial conditions

2. JV: For nuclear targets, we adopt the Jeon-Venugopalan model with impact parameter dependence introduced

$$W[\rho] = \exp\left[-\int_{\mathbf{x}_{\perp}} \left(\frac{\delta_{ab}\rho^{a}\rho^{b}}{2\mu^{2}} - \frac{d_{abc}\rho^{a}\rho^{b}\rho^{c}}{\kappa}\right)\right]$$

Jeon, Venugopalan, PRD 71 (2005) 125003

$$\begin{split} \mathcal{O}(\mathbf{r}_{\perp}, \boldsymbol{b}_{\perp}) &= \frac{\lambda}{8} \left[R_A \frac{\mathrm{d} \mathcal{T}_A(\boldsymbol{b}_{\perp})}{\mathrm{d} \boldsymbol{b}_{\perp}} A^{2/3} \frac{\sigma_0}{2} \right] A^{1/2} (Q_{5,0}^3 r_{\perp}^3) (\hat{\boldsymbol{r}}_{\perp} \cdot \hat{\boldsymbol{b}}_{\perp}) \log \left(\frac{1}{r_{\perp} \Lambda_{\rm QCD}} + \boldsymbol{e}_c \mathbf{e} \right) \\ & \exp \left[-\frac{1}{4} \mathbf{r}_{\perp}^2 A \mathcal{T}_A(\boldsymbol{b}_{\perp}) \frac{\sigma_0}{2} Q_{5,0}^2 \log \left(\frac{1}{r_{\perp} \Lambda_{\rm QCD}} + \boldsymbol{e}_c \mathbf{e} \right) \right] \,, \end{split}$$

•
$$\lambda_{\rm JV} = -\frac{3}{16} \frac{N_c^2 - 4}{(N_c^2 - 1)^2} \frac{Q_{5,0}^3 A^{1/2} R_A^3}{\alpha_5^3 A^2}$$

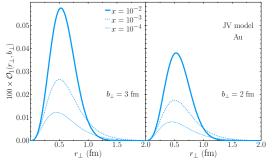
• We also explore different strengths for λ

Solutions of BK evolution

Negligible higher harmonics induced in the odderon by non-linear terms

Yao, Hagiwara, Hatta PLB 790 (2019) 361 Motyka, PLB 637 (2006) 185

 $\mathcal{O}(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) = \mathcal{O}_1(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \cos(\phi_{rb}) + \mathcal{O}_3(\mathbf{r}_{\perp}, \mathbf{b}_{\perp}) \cos(3\phi_{rb}) + \dots$

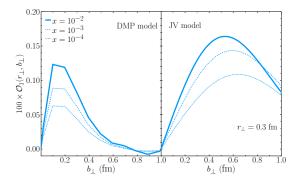


- Odderon decreases significantly with evolution
- Peak position around $r_{\perp} \sim Q_S$. Changes slowly with evolution

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Odderon through η_c at EIC

Solutions of BK evolution



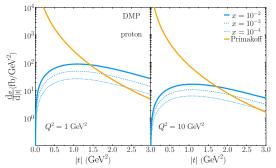
 Peak position dictated by ^{dT_A(**b**_⊥)}/_{db} in JV model, close to the edge of the system, increases slowly with evolution → Gluon radius ↑ as x ↓

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Results: $ep \rightarrow e + \eta_c + p$ with DMP odderon

Important QED background: Primakoff process. Photon (C = -1) from proton can also

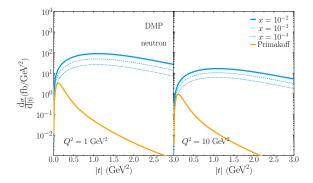
result in η_c . Can be calculated from well known electromagnetic charge form factor.



- Odderon contribution has rather small slope in |t|
 → proton can remain intact at large momentum transfers if three gluons in the
 odderon couple to different quarks.
- Primakoff contribution dominates at small |t|. Need $|t| \gtrsim 1.5$ to access odderon.
- Similar to earlier results in the dilute regime by Dumitru and Stebel Dumitru, Stebel, PRD 99 (2019) 094038

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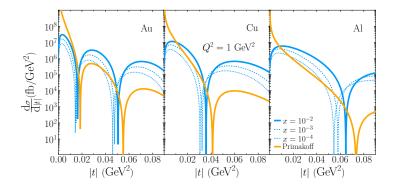
Results: $en \rightarrow e + \eta_c + n$ with DMP odderon



- Primakoff contribution negligible
- Odderon accesible even at low momentum transfers

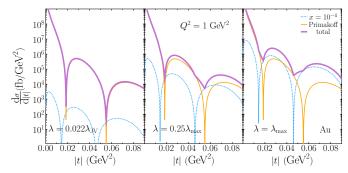
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Results: $eA \rightarrow e + \eta_c + A$ with JV odderon



- Diffractive patterns of geometric origin (c.f. leading twist estimates)
- Multiple scattering effects → diffractive dips shifted to smaller |t| w.r.t Primakoff case
- Shifts more pronounced as $x \downarrow$ or $|t| \uparrow$

Results: $eA \rightarrow e + \eta_c + A$ with JV odderon



Scenarios:

- **1.** JV coupling inspired by DMP: Cross-section dominated by Primakoff component. Odderon too small to produce visible effect.
- 2. Odderon component still lower than Primakoff, but difference in diffractive pattern "fills out" Primakoff dips.
- **3.** Odderon component larger than Primakoof. Diffractive pattern would be shifted wrt the known pattern from nuclear charge form factors.

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Conclusions

For proton target:

- Isolating odderon requires large momentum transfer $|t|\gtrsim 1.5$ -3 GeV² for $x\sim 10^{-2}-10^{-4}$.
- Similar to conclusions drawn for the dilute regime.
- Small-x evolution does not alter |t| slope, but cross-section reduces in magnitude.

For neutron target:

- Negligible Primakoff component. Can probe odderon at low |t|.
- Could be performed with deuteron or He³ targets with spectator proton tagging in the near forward direction.

For nuclear targets:

- Saturation effects in Odderon distribution distort diffractive pattern w.r.t known QED contributions!
- Effect ~ few percent and accumulates for small-x/large momentum transfers.

Thank you!

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Leading twist estimates

• Odderon:

$$\frac{d\sigma}{d|t|} \simeq \frac{9\pi q_c^2 \alpha \alpha_S^6 A^2 C_{3F}^2 \mathcal{R}_{\mathcal{P}}^2(0)}{4N_c m_c^5} \frac{|t| \mathcal{T}_A^2(\sqrt{|t|})}{m_c^4}$$

• QED (Primakoff):

$$\frac{\mathrm{d}\sigma}{\mathrm{d}|t|} \simeq \frac{\pi q_c^4 \alpha^3 Z^2 N_c \mathcal{R}_{\mathcal{P}}^2(0)}{m_c^5} \frac{\mathcal{T}_A^2(\sqrt{|t|})}{|t|}$$

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