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Bernhard Manfred Gruber CERN, CASUS, HZDR, TU Dresden

LLAMA: A Low-Level Abstraction of Memory Access Memory layout optimization and efficient interconversion of data structures for heterogeneous architectures 23rd Gentner Day @ CERN // April 26th, 2023

Performance, latency and power gap



Google: 62.7% energy spent on data movement [3]



1300-2600



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Slide 2



64b DRAM

Growth by hardware diversity





Image from [5]



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Problems and challenges

Many programs are memory bound, or will soon become

Performance relies on maximizing data throughput, data locality, efficient parallel access Optimizations depend on full control over data layout and memory access Efficiently using modern hardware requires respecting its internal structure

Compute and memory hardware is increasingly heterogeneous

Porting to new architectures is expensive

Performance portability is challenging

Different hardware requires different data layouts and access patterns

Different data layouts require different indexing syntax

Changing data layout requires rewriting code

data[i].x
data.x[i]
data[i/8].x[i%8]

Indexing different data layouts. Here: AoS, SoA and AoSoA8





Related work – taxonomy





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No wholistic solution, combining all these optimizations techniques



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Case study: HEP analysis

High-Energy-Physics (HEP) analyzes energetic particle collisions

Stored as events, 1 event = data of one collision inside a detector Estimate: ~15k high-energy/nuclear physicists working in this field

B2HHH decay with LHCb Open Data [6,7] and ROOT [8]

Simple, but representative analysis

- "Real" analyses: more data/observables
- Standard workflow: read events, filters/cuts, compute, histograms
- IO (network + disk) and memory bound

Only study in-memory data layouts, no IO Baseline: SoA multi blob layout









Slide 8







Images © CERN

Generate insight

Event
loop

Filters and cuts

Comp. observable Fill hist.

#pragma omp parallel for for(size_t i = 0; i < n; i++) {</pre> Instrumentation to auto&& event = view[i]; the rescue! Count accesses to fields if(event(H1isMuon{})) continue; if(event(H2isMuon{})) continue; if(event(H3isMuon{})) continue; if(event(H1ProbK{}) < probKCut) continue;</pre> if(event(H2ProbK{}) < probKCut) continue;</pre> if(event(H3ProbK{}) < probKCut) continue;</pre> if(event(H1ProbPi{}) > probPiCut) continue; if(event(H2ProbPi{}) > probPiCut) continue; if(event(H3ProbPi{}) > probPiCut) continue; // compute bmass ... hists[omp get thread num()].Fill(bmass); } Memory layout optimization [...] of data structures for heterogeneous architectures FECHNISCHE UNIVERSITÄT Bernhard Manfred Gruber

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2 LOCS in LLAMA

Slide 9

How often is which

Depends on filters ...

data touched?









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Slide 10

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SYSTEMS LINDERSTANDIN

Data reduction

H[1-3]isMuon are int32, but only store 0 or 1

Pack into 1 bit each

Reduce the FP precision

Exponent: look at min/max value Mantissa: domain knowledge, theory, ... Our use case: 6 exp. and 16 man. bits

But: bit-packing introduces overhead

Changing data types usually faster Uses dedicated hardware instructions

Also: Runtime not the only concern

Data size matters especially for storage

Analysis result with different mantissa bits



Slide 11





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The optimal layout

Using pure data layout

Separate H[1-3]isMuon into AoS Separate H[1-2]PropK into AoS

With data reduction

Pack H[1-3]isMuon into 1 bit each Change type of H[1-2]PropK to float Bitpack the rest

Blob: 0	0 H1isMuon	0 H2isMuon	0 H3isMuon	1 H1isMuon	1 H2isMuon	1 H3isMuon	2 H1isMuon	2 H2isMuon
D 100. 0	2 H3isMuon							

Blob: 1	0 H1ProbK	0 H2ProbK	1 H1ProbK	1 H2ProbK					
	2 H1ProbK	2 H2ProbK							

	0 H1PX	0 H1PY	0 H1PZ	0 H1ProbPi
	0 H2PX	0 H2PY	0 H2PZ	0 H2ProbPi
	0 H3PX	0 H1PY 0 H1PZ 0 0 H2PY 0 H2PZ 0 0 H3PY 0 H3PZ 0 1 H1PX 1 H1PY 0 1 H1PX 1 H1PY 0 1 H3PX 1 H3PY 0 1 H3ProbPi 2 H1PX 0 2 H1ProbPi 2 H2PX 0 2 H3ProbPi 2 H3PX 0	0 H3ProbK	
	0 H3ProbPi	1 H1PX	1 H1PY	1 H1PZ
Blob: 2	1 H1ProbPi	1 H2PX	1 H2PY	1 H2PZ
	1 H2ProbPi	1 H3PX	1 H3PY	1 H3PZ
	1 H3ProbK	1 H3ProbPi	2 H1PX	2 H1PY
	2 H1PZ	2 H1ProbPi	2 H2PX	2 H2PY
	2 H2PZ	2 H2ProbPi	2 H3PX	2 H3PY
	2 H3PZ	2 H3ProbK	2 H3ProbPi	

Blob: 0 ZisM

D1 1

B100: 1	0 H1F	Probk		o H2	2Prob	<	1	H1Pro	bK	1	H2	Prob	<	2	H1P	robK		2 H2I	Prob	ĸ						
	0 _I H1P	Х	0 H1PY		0 H	1PZ	0	H1Prol	bPi	0 H	2PX		0 H2	2PY	0 H	12PjZ	z	0 H2Pro	bPi	0 _. H3F	Х	0 H3PY		0 H3	PZ	3Pro
Blob: 2	0 H3Pro	bK 0	H3Prob	Pi	1 H	1PX	1	H1PY		1 H1P	Z	1 H	1Pro	bPi	1 H2	PX		1 H2PY		1 H2PZ	1	H2Prob	Pi	1 H3	PX	H3P
Dicci 2	1 H3PY	1	H3PZ	1	H3Prc	bK1	H3Pr	obPi	2	2 H1PX		2 H1	IPY		2 H1	PZ	2	H1Probl	Pi 2	H2PX	2	H2PY	:	2 _. H2PZ	H2P	robF
	H2Prob	2 H3	PX	21	H3PY		2 H3	P7	21	H3Probl	(2 H	3Pro	bPi													

Layout visualization of 3 events 1 LOC with LLAMA





Benchmark





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HEP analysis case study: Summary

LLAMA can visualize layouts, trace access counts and heatmaps

Helps to understand your data, data layouts and access pattern

LLAMA's mappings are versatile

Combine them into custom layouts, including user-defined mappings

Reducing precision/bits can vastly accelerate programs and reduce storage

LLAMA can greatly help with precision studies

Future work

Data only read once: customize access using streaming instructions

Outlook

Within ROOT, for long-running analyses: JIT-compile with a better layout after a while

Convert to LLAMA Instrument Design layout Reduce data Customize access











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Summary and conclusions

Programs are increasingly memory bound, regarding throughput, latency and power

Compute and memory hardware becomes increasingly diverse

There is no wholistic, generic and portable solution for memory-related optimizations

LLAMA is a novel abstraction to fill this gap, it ...

... addresses: data layout, mem. access, data reduction, SIMD, layout-aware copy, instrum., and layout vis.

- Largely decoupled, algorithmically transparent and fully user-extensible
- Coherently integrated into a concise and well-designed API

... supports fast data layout exploration and rapid porting to new architectures with minimal code changes

... facilitates systematic data layout engineering with instrumentation and performance metrics

... allows for hardware specific tuning using memory accessors and SIMD







Thank you, questions?

Scientific publications

- B. M. Gruber, G. Amadio, J. Blomer, A. Matthes, R. Widera, M. Bussmann, "<u>LLAMA: The low-level</u> <u>abstraction for memory access</u>", Software: Practice and Experience 53 (1), 115-141, 2022.
- B. M. Gruber, G. Amadio, S. Hageböck, "<u>Challenges</u> and opportunities integrating LLAMA into AdePT", Proceedings to the 21st International Workshop on Advanced Computing and Analysis Techniques in Physics Research (ACAT22), 2023.
- B. M. Gruber, "<u>Updates on the Low-Level</u> <u>Abstraction of Memory Access</u>", Proceedings to the 21st International Workshop on Advanced Computing and Analysis Techniques in Physics Research (ACAT22), 2023.
- J. Stephan, ..., **B. M. Gruber** et al., "Performance portability with alpaka," unpublished, 2023.

GitHub: <u>https://github.com/alpaka-group/llama</u>

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- [7] LHCb collaboration. Matter Antimatter Differences (B meson decays to three hadrons) Project Notebook. 2017. doi: 10.7483/OPENDATA.LHCB.K6BL.RF22. url: http://opendata.cern.ch/record/4902 (visited on 2023-04-19).
- [8] Rene Brun and Fons Rademakers. "ROOT—an object oriented data analysis framework". In: Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 389.1-2 (1997), pp. 81–86.





Backup slides



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Example – N-body simulation 1/3

```
using FP = float;
constexpr FP timestep = 0.0001, eps2 = 0.01;
constexpr int steps = 5, problemSize = 64 * 1024;
namespace tag {
  struct Pos{}; struct Vel{}; struct X{}; struct Y{};
  struct Z{}; struct Mass{};
using V3 = llama::Record<
  llama::Field<tag::X, FP>,
  llama::Field<tag::Y, FP>,
  llama::Field<tag::Z, FP>>;
using Particle = llama::Record<</pre>
  llama::Field<tag::Pos, V3>,
  llama::Field<tag::Vel, V3>,
  llama::Field<tag::Mass, FP>>;
```





Example – N-body simulation 2/3

```
void pPInteraction(auto&& pi, auto&& pj) {
  auto dist = pi(tag::Pos{}) - pj(tag::Pos{});
  dist *= dist;
  const auto distSqr = eps2 +
                       dist(tag::X{}) + dist(tag::Y{}) + dist(tag::Z{});
  const auto distSixth = distSqr * distSqr * distSqr;
  const auto invDistCube = FP{1} / sqrt(distSixth);
  const auto sts = (pj(tag::Mass{}) * timestep) * invDistCube;
  pi(tag::Vel{}) += dist * sts;
void update(auto& particles) {
  LLAMA INDEPENDENT DATA
  for(std::size t i = 0; i < problemSize; i++) {</pre>
    illama::One<Particle> pi = particles(i);
    for(std::size_t j = 0; j < problemSize; ++j)</pre>
      pPInteraction(pi, particles(j));
    particles(i)(tag::Vel{}) = pi(tag::Vel{});
```





Example – N-body simulation 3/3

```
void move(auto& particles) {
  LLAMA INDEPENDENT DATA
  for(std::size t i = 0; i < problemSize; i++)</pre>
    particles(i)(tag::Pos{}) += particles(i)(tag::Vel{}) * timestep;
int main() {
  using ArrayExtents = llama::ArrayExtentsDynamic<std::size t, 1>;
                                                                                 Change mapping
  using Mapping = llama::mapping::AoS<ArrayExtents, Particle>; // !!!
                                                                                 with this line
  auto mapping = Mapping{ArrayExtents{problemSize}};
  auto view = llama::allocViewUninitialized(mapping); // !!!
  for(auto&& p : view) {
                                                              Set custom blob
    p(tag::Pos{}, tag::X{}) = random();
                                                              alloc. or accessor
    // ...
                                                              on this line
    p(tag::Mass{}) = random();
  for(std::size t s = 0; s < steps; ++s) {</pre>
    update(view);
    move(view);
             Memory layout optimization [...] of data structures for heterogeneous architectures
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```

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Slide 22

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Mapping example: AoS implementation

```
template<typename TArrayExtents, typename TRecordDim, bool AlignAndPad = true,
 typename TLinearizeArrayDimsFunctor = LinearizeArrayDimsCpp,
 template<typename> typename FlattenRecordDim = FlattenRecordDimInOrder>
struct AoS : MappingBase<TArrayExtents, TRecordDim> {
 private:
    using Base = MappingBase<TArrayExtents, TRecordDim>;
    using size type = typename Base::size type;
 public:
    inline static constexpr bool alignAndPad = AlignAndPad;
    using LinearizeArrayDimsFunctor = TLinearizeArrayDimsFunctor;
    using Flattener = FlattenRecordDim<TRecordDim>;
    inline static constexpr std::size t blobCount = 1;
    using Base::Base;
    LLAMA FN HOST ACC INLINE constexpr auto blobSize(size type) const -> size type {
     return LinearizeArrayDimsFunctor{}.size(Base::extents())
       * flatSizeOf<typename Flattener::FlatRecordDim, AlignAndPad>;
    template<std::size t... RecordCoords>
    LLAMA_FN_HOST_ACC_INLINE constexpr auto blobNrAndOffset(
     typename Base::ArrayIndex ai,
      RecordCoord<RecordCoords...> = {}) const -> NrAndOffset<size type> {
      constexpr std::size t flatFieldIndex = Flattener::template flatIndex<RecordCoords...>;
      const auto offset = LinearizeArrayDimsFunctor{}(ai, Base::extents())
        * static cast<size type>(flatSizeOf<typename Flattener::FlatRecordDim, AlignAndPad>)
        + static cast<size type>(flatOffsetOf<typename Flattener::FlatRecordDim, flatFieldIndex,
                                                                                 AlianAndPad>):
      return {size_type{0}, offset};
```

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};

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LHCB B2HHH analysis layout 4 definition

```
using Mapping = llama::mapping::Split<</pre>
    llama::ArrayExtentsDynamic<RE::NTupleSize t, 1>,
    RecordDim,
    mp_list<mp_list<H1isMuon>, mp_list<H2isMuon>, mp_list<H3isMuon>>,
    llama::mapping::AlignedAoS,
    llama::mapping::BindSplit<</pre>
        mp list<mp list<H1ProbK>, mp list<H2ProbK>>,
        illama::mapping::AlignedAoS,
        illama::mapping::AlignedAoS,
        true>::fn,
    true>;
```







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LHCB B2HHH analysis layout 8 definition

```
using Mapping = llama::mapping::Split<
    llama::ArrayExtentsDynamic<RE::NTupleSize_t, 1>,
    RecordDim,
    mp_list<mp_list<H1isMuon>, mp_list<H2isMuon>, mp_list<H3isMuon>>,
    llama::mapping::BindBitPackedIntAoS<llama::Constant<1>, llama::mapping::SignBit::Discard>::fn,
    llama::mapping::BindSplit<
        mp_list<mp_list<H1ProbK>, mp_list<H2ProbK>>,
        llama::mapping::BindChangeType<llama::mapping::BindAoS<>::fn, mp_list<mp_list<double, float>>>::fn,
        llama::mapping::BindBitPackedFloatAoS<llama::Constant<6>, llama::Constant<16>>::template fn,
        true>;;
```





Case study: AdePT



Significant compute workload in High Energy Physics (HEP): particle transport simulation

Traditional codes (Geant4) and CPU based

New: Accelerated demonstrator of electromagnetic Particle Transport (AdePT)

C++/CUDA prototype for offloading electromagnetic (EM) physics to GPUs using <u>VecGeom</u> and <u>G4HepEm</u> GitHub: <u>https://github.com/apt-sim/AdePT</u>

Profiling showed: bound by memory access

Ideal testbed for LLAMA!



More on AdePT:

Talk and proceedings at ACAT21: "Offloading electromagnetic shower transport to GPUs: the AdePT project" Talk at 27th Geant4 Collaboration meeting: "AdePT status report and discussion"





AdePT track data structure

Single sparse buffer

New: Double dense buffers



active	next
track #0	track #0
track #1	track #1
track #2	track #2
track #3	track #3
track #4	track #4
track #5	track #5
track #6	track #6
track #7	track #7

#

5

Drawback: copies more memory

wrapped after 64B

0 RngState												
0 R	IngState	0 Energy	0 NumlALeft.0??	0 NumIALeft,?1?	0 NumIALeft,?2?	0 InitialRange	0 DynamicRangeFactor					
0 TlimitMin		0 Pos			0 Dir		0 NavState					
0 NavState				1 RngState								
	1 RngState		1 Energy	1 NumIALeft,0??	1 NumlALeft, 717	1 NumlALeft,?2?	1 InitialRange					
1 DynamicRangeFactor	1 TlimitMin		1 Pos			1 Dir						
1 NavState				2 Rn	gState							
	2 Rn	gState		2 Energy	2 NumIALeft 0??	2 NumlALeft,?1?	2 NumIALeft,?2?					
2 InitialRange	2 DynamicRangeFactor	2 TlimitMin		2 Pos		2	Dir					
2 Dir	2 NavState				3 RngState							
		3 RngState			3 Energy	3 NumlALeft,0??	3 NumIALeft,?1?					
3 NumlALeft,?2?	3 InitialRange	3 DynamicRangeFactor	3 TlimitMin		3 Pos		3 Dir , , , , , , , , , , , , , , , , , , ,					
and the second second	3 Pir	3 NavState	- 1 - 1		4 Rn	gState						
		4 Rng	State			4 Energy	4 NumIALeft,0??					
4 NumlALeft,?1?	4 NumlALeft,?2?	4 InitialRange	4 DynamicRangeFactor	4 TlimitMin		4 Pos						
	4 Pir		4 NavState			5 RngState						
			5 RngState				5 Energy					
5 NumIALeft.0??	5 NumlALeft,?1?	5 NumIALeft,?2?	5 InitialRange	5 DynamicRangeFactor	5 TlimitMin	51	Pos					
5 Pos		5 Dir		5 NavState		6 Rn	gState					
			6 Rng	gState								
6 Energy	6 NumlALeft,0??	6 NumIALeft,?1?	6 NumIALeft,?2?	6 InitialRange	6 DynamicRangeFactor	6 TlimitMin	6 Pos					
	6 Pos		6 Dir		6 NavState		7 RngState					
			7 Rng	gState								
7 RngState	7 Energy	7 NumIALeft,0??	7 NumlALeft ?1?	7 NumIALeft,?2?	7 (nitialRange	7 DynamicRangeFactor	7 TlimitMin					
	7 Pos			7 Dir		7 NavState						
			8 Rn(gstate								
88	ingState	8 Energy	8 NumIALeft,077	8 NumiALett,717	8 NumIALeft,727	8 InitialRange	8 DynamicRangeFactor					
s rimitinin		81905			s bir		a navState					
a Navstate				9 KingState			A 10% 10 000					
	9 KingState		9 Energy	9 NumiALeft,0??	9 NumiALeft,?1?	9 NumiALeft,?2?	9 initialRange					
9 DynamicRangeFactor	y nimitMin		9 105			a Dir						

Layout visualization: 1 LOC with LLAMA



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Benchmark & Instrumentation

AdePT on NVIDIA V100



Changing layout is changing 1 LOC, recompile, rerun



Heatmaps only: Single sparse buffer



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Slide 28





Runtime [s]

Instrumentation





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Adept: Summary and conclusions

Memory layout and access pattern must fit together

SoA is not a silver bullet, requires dense access pattern AoS works substantially better with sparse and random access

Memory access visualization gives crucial insights for further optimization

Split and regroup data structs based on access pattern Based on instrumentation results, the AdePT team can now engineer better layouts

LLAMA caused slight abstraction overhead

Different inlining decisions and register allocation Compile time increased for incremental build by 27% (1.cpp, 3.cu files)

Invasive code changes necessary around your data structure

Benchmark has 1336 LoCs (cloc), LLAMA integration: 178 ins. 226 del. (git) But: porting to the next architecture may now just be a single line switch!





AdePT: Track before/after LLAMA integration

```
struct Track {
   RanluxppDouble rngState;
   double energy;
   double numIALeft[3];
   double initialRange;
   double dynamicRangeFactor;
   double tlimitMin;
   vecgeom::Vector3D<Precision> pos;
   vecgeom::NavStateIndex navState;
```

```
__device__ void InitAsSecondary(
    const Track &parent) {
```

```
// ...
this->pos = parent.pos;
this->navState = parent.navState;
}
```

```
struct RngState {}; struct Energy {}; // ...
using Track = llama::Record<
    llama::Field<RngState, RanluxppDouble>,
    llama::Field<Energy, double>,
    llama::Field<NumIALeft, double[3]>,
    llama::Field<InitialRange, double>,
    llama::Field<DynamicRangeFactor, double>,
    llama::Field<TlimitMin, double>,
    llama::Field<Pos, vecgeom::Vector3D<vecgeom::Precision>>,
    llama::Field<Dir, vecgeom::Vector3D<vecgeom::Precision>>,
    llama::Field<NavState, vecgeom::NavStateIndex>>;
```



};

