

# The Composite Two Higgs Doublet Model

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# Introduction

The main question for the **LHC**:  
What is the **Nature** of **EWSB** ?

## Introduction

The main question for the **LHC**:  
What is the **Nature** of **EWSB** ?

The answers from **LEP**:

- If strong-sector,  $\hat{S}$  must be **tuned**
- Higgs model is **fine** for a **light** Higgs
- Not light enough though, **SUSY** in trouble  
(need for more complicated/tuned versions)

# Introduction

One possible interpretation:

**EWPT**

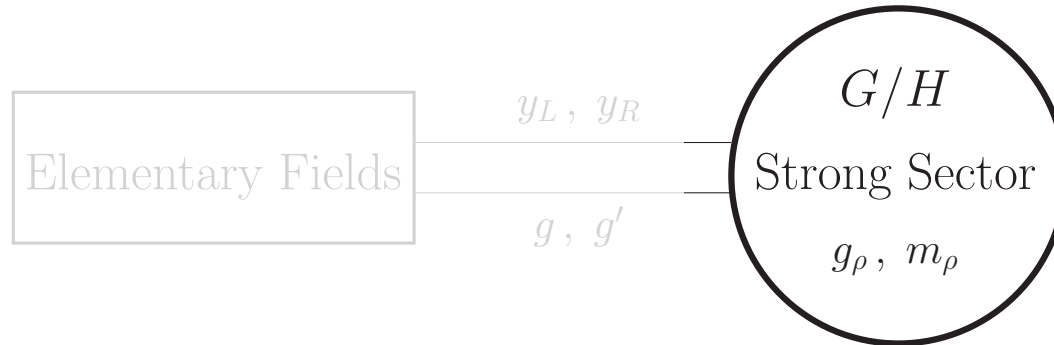


**Hierarchy Problem**



The **Higgs exists**, but it is **Composite**

# The PNGB Higgs



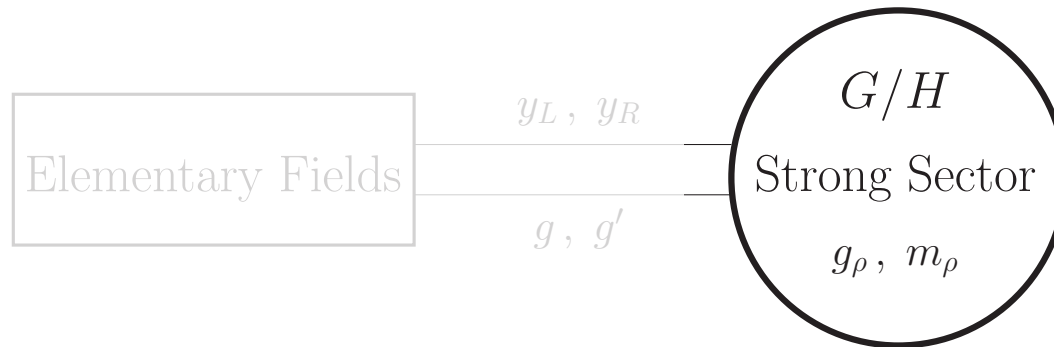
$$H \supset SO(4)$$

Constraints (from  $\rho=1$ ) on  $G/H$ :

$$G/H \supset 4$$

	$G$	$H$	$N_G$	NGB's rep. $[H] = \text{rep.}[\text{SU}(2) \times \text{SU}(2)]$
<b>MCHM</b>	$\rightarrow$ SO(5)	SO(4)	4	$4 = (2, 2)$
	SO(6)	SO(5)	5	$5 = (1, 1) + (2, 2)$
<b>CTHDM</b>	$\rightarrow$ SO(6)	$SO(4) \times SO(2)$	8	$4_{+2} + \bar{4}_{-2} = 2 \times (2, 2)$
	$\rightarrow$ SO(7)	SO(6)	6	$6 = 2 \times (1, 1) + (2, 2)$
	$\rightarrow$ SO(7)	$G_2$	7	$7 = (1, 3) + (2, 2)$
	$\rightarrow$ SO(7)	$SO(5) \times SO(2)$	10	$10_0 = (3, 1) + (1, 3) + (2, 2)$
	$\rightarrow$ SO(7)	$[SO(3)]^3$	12	$(2, 2, 3) = 3 \times (2, 2)$
	$\rightarrow$ Sp(6)	$Sp(4) \times SU(2)$	8	$(4, 2) = 2 \times (2, 2), (2, 2) + 2 \times (2, 1)$
<b>Georgi-Kaplan</b>	$\rightarrow$ SU(5)	$SU(4) \times U(1)$	8	$4_{-5} + \bar{4}_{+5} = 2 \times (2, 2)$
	$\rightarrow$ SU(5)	SO(5)	14	$14 = (3, 3) + (2, 2) + (1, 1)$

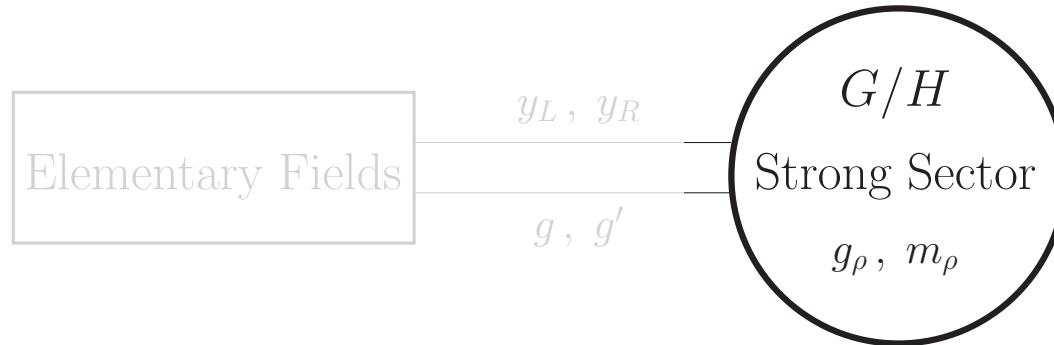
# The PNGB Higgs



Adopt the simplest description of the Strong Sector:

$$\begin{array}{ll} \text{One Coupling: } & g_\rho \\ \text{One Mass: } & m_\rho \end{array} \quad \sim \quad \begin{array}{ll} \text{Large-}N: & g_\rho \sim 4\pi/\sqrt{N} \\ \text{Explicit Realization: } & 5d \end{array}$$

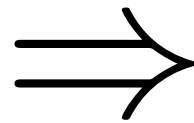
# The PNGB Higgs



Adopt the simplest description of the Strong Sector:

One Coupling:  $g_\rho$

One Mass:  $m_\rho$

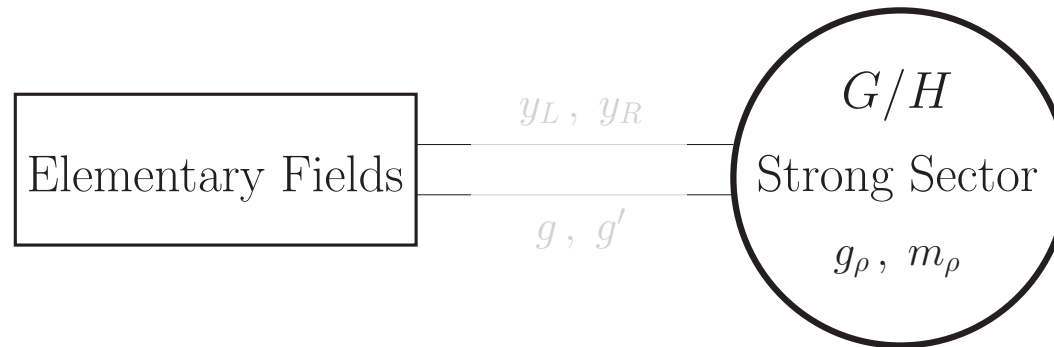


**Tuning:**

$$f = \frac{m_\rho}{g_\rho}$$
$$\xi = \frac{v^2}{f^2} < 1$$

$$m_\rho = \frac{g_\rho}{\sqrt{\xi}} v$$

# The PNGB Higgs

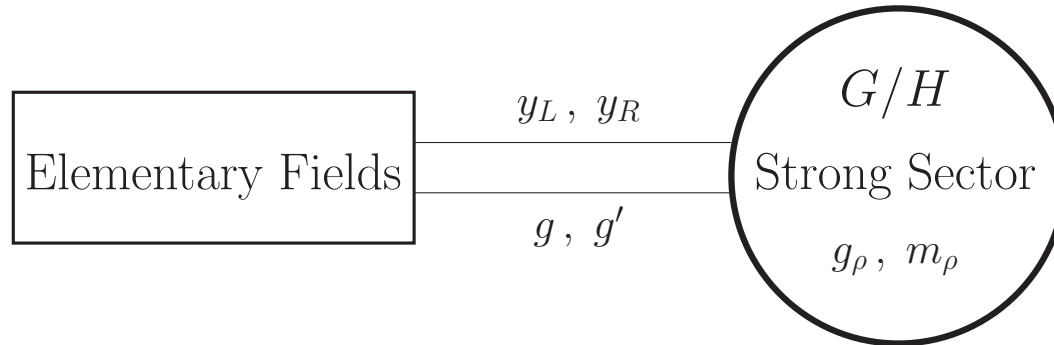


**SM** fermions and gauge fields are elementary d.o.f.

Not the  $t_R$ , it might be **totally composite**



# The PNGB Higgs

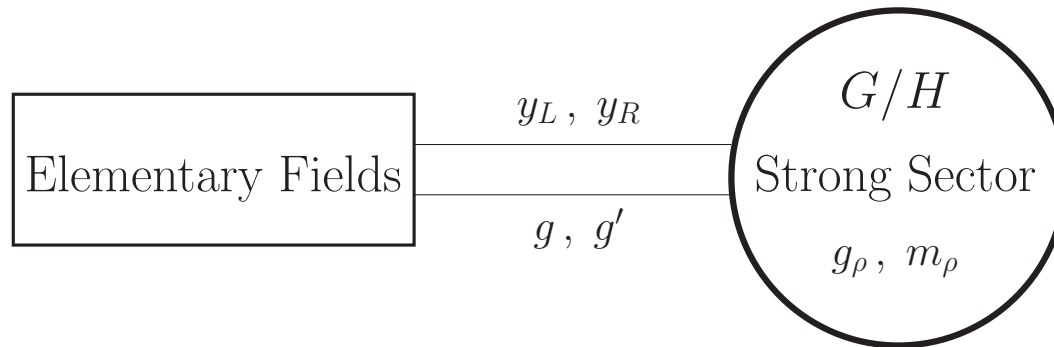


Elementary-Composite Couplings:

$$g_{SM} \cdot \Psi_{SM} \cdot \mathcal{O} = \begin{cases} g A_\mu J^\mu \\ y_{L,R} f_{L,R} \mathcal{O}_{L,R} \end{cases}$$

We adopt **partial compositeness** for fermions

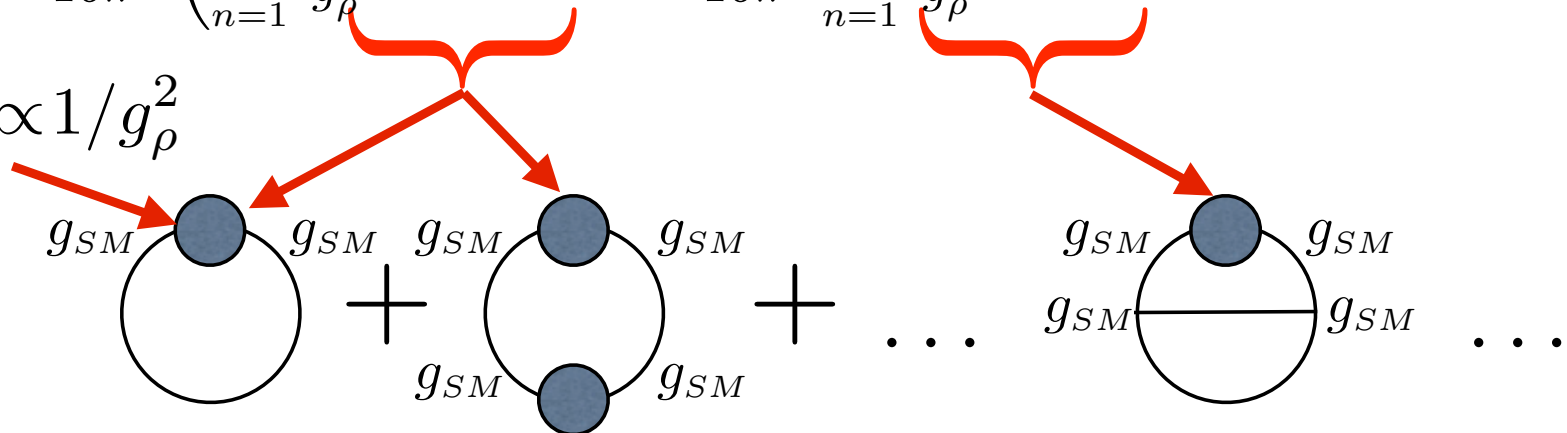
# The PNGB Higgs



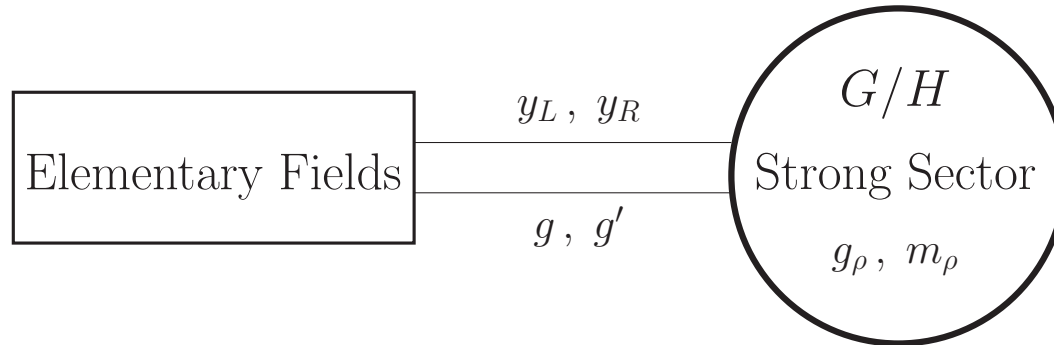
We also assume  $g_{SM}$  is the only  $G$  source

$$V(\Pi) = \frac{m_\rho^4}{16\pi^2} \left( \sum_{n=1}^{\infty} \frac{g_{SM}^{2n}}{g_\rho^{2n}} F_{1n}(\Pi/f) + \frac{g_\rho^2}{16\pi^2} \sum_{n=1}^{\infty} \frac{g_{SM}^{2n}}{g_\rho^{2n}} F_{2n}(\Pi/f) + \text{higher loops} \right)$$

$$\langle \mathcal{O}\mathcal{O} \rangle \propto 1/g_\rho^2$$



# The PNGB Higgs



We also assume  $g_{SM}$  is the only  $G$  source

$$V(\Pi) = \frac{m_\rho^4}{16\pi^2} \left( \sum_{n=1}^{\infty} \frac{g_{SM}^{2n}}{g_\rho^{2n}} F_{1n}(\Pi/f) + \frac{g_\rho^2}{16\pi^2} \sum_{n=1}^{\infty} \frac{g_{SM}^{2n}}{g_\rho^{2n}} F_{2n}(\Pi/f) + \text{higher loops} \right)$$

Spurion power-counting will **fix** the  $F$ 's:

Higgs potential **strongly constrained**

# EW Precision Observables

Tree-Level contribution to  $\widehat{S}$ :

$$\widehat{S} \sim \frac{m_W^2}{m_\rho^2} \sim \frac{g^2 v^2}{g_\rho^2 f^2} \quad \rightarrow \quad \xi \equiv \frac{v^2}{f^2} \lesssim 0.01 g_\rho^2$$

**Best case:**  $\mathcal{O}_L = (2, 2)_{2/3}$ ,  $\mathcal{O}_R = (1, 1)_{2/3}$

$$\frac{\delta g_b}{g_b} \sim \frac{y_L^2}{g_\rho^2} \xi \quad \widehat{T} \sim \frac{N_c y_L^4}{16\pi^2 g_\rho^2} \xi$$

**Extra pressure** from  $\delta g_b$ :

$$Y_t \simeq y_L y_R / g_\rho \quad \begin{cases} y_L \sim Y_t \\ y_R \sim g_\rho \end{cases}$$

## EW Precision Observables

**Avoided** by  $P_{LR}$  symmetry:  $L \leftrightarrow R$   
 $b_L \rightarrow b_L$

$$\bar{b}_L i \cancel{D} b_L + \bar{b}_L [\delta_L \cancel{L} + \delta_R \cancel{R} + \delta_X \cancel{X}] b_L$$

$P_{LR}$  plus unbroken sym.  $\rightarrow \delta_L = \delta_R = \delta_X = 0$

Do we really need **another** symmetry ?

# EW Precision Observables

**NO,  $P_{LR}$  is accidental !**

Use the  $SO(4)/SO(3)$  symmetry:

$$(y_L)_A q_L \mathcal{O}_L^A \equiv Q_A \mathcal{O}_L^A$$

$$\psi_i = Q_A U_{Ai}^*$$

$$\eta = Q_A U_{A4}^*$$

$$\mathcal{O}_1 = \bar{\psi} \bar{\sigma}^\mu (\partial_\mu + \mathcal{E}_\mu) \psi$$

$$\mathcal{O}_2 = \bar{\eta} \bar{\sigma}^\mu \partial_\mu \eta$$

$$\mathcal{O}_3 = \bar{\psi}_i \bar{\sigma}^\mu \eta \mathcal{D}_{i\mu}$$

$$\mathcal{O}_4 = \bar{\psi}_i \bar{\sigma}^\mu \psi_j \mathcal{D}_{k\mu} \epsilon_{ijk}$$

Can this term emerge with the full symmetry ?

## EW Precision Observables

**NO,  $P_{LR}$  is accidental !**

Use now the full  $SO(5)/SO(4)$

With  $\mathcal{O}_L = \mathfrak{5}_{2/3}$ :

$$\psi_i = Q_A U_{Ai}^* \quad \eta = Q_A U_{A5}^*$$

cannot use the  $\epsilon$  tensor !

**Reduction** of  $\delta g_b / g_b$  allows larger  $y_L \sim \sqrt{Y_t g_\rho}$ .

# Two Composite Higgses

Two **guidelines** for model-building:

- Custodial  $SO(3)_c$  can be broken by the VEVs
- Second Higgs is a possible new source of FCNC



## Two Composite Higgses

$$\begin{array}{l}
 \text{SO}(3)_c: \\
 \Phi^{\hat{1}} = (0, 0, 0, v_4^{\hat{1}}) \\
 \Phi^{\hat{2}} = (0, 0, v_3^{\hat{2}}, v_4^{\hat{2}})
 \end{array}
 \quad
 \begin{array}{l}
 H^{\hat{1}} = \begin{pmatrix} 0 \\ v_4^{\hat{1}} \end{pmatrix} \\
 H^{\hat{2}} = \begin{pmatrix} 0 \\ v_4^{\hat{2}} - i v_3^{\hat{2}} \end{pmatrix}
 \end{array}$$

$$\frac{c_T}{f^2} \left( \Phi^{\hat{1}} \cdot \overleftrightarrow{D}_\mu \Phi^{\hat{2}} \right)^2 \quad \longrightarrow \quad \hat{T} = 2c_T \frac{(v_4^{\hat{1}})^2 (v_3^{\hat{2}})^2}{f^2 [(v_4^{\hat{1}})^2 + (v_4^{\hat{2}})^2 + (v_3^{\hat{2}})^2]} \sim \frac{c_T}{2} \frac{v^2}{f^2}$$

$$\text{SO}(4) \rightarrow \text{SO}(2)_c \text{ triggered by: } v_4^{\hat{1}} v_3^{\hat{2}} \propto \text{Im} (H^{\hat{1}\dagger} H^{\hat{2}})$$

## Two Composite Higgses

**Three ways** to control  $\hat{T}$ :

$$C_1 \in SO(4) : (\phi_1, \phi_2, \phi_3, \phi_4) \rightarrow (-\phi_1, \phi_2, -\phi_3, \phi_4)$$

(or,  $H \rightarrow H^*$ )

## Two Composite Higgses

**Three ways** to control  $\hat{T}$ :

$$C_1 \in SO(4) : (\phi_1, \phi_2, \phi_3, \phi_4) \rightarrow (-\phi_1, \phi_2, -\phi_3, \phi_4)$$

(or,  $H \rightarrow H^*$ )

Acts like  $C$ , also on the EW bosons

$C$  is broken by fermions, **we impose**  $C_1 P \equiv CP$

## Two Composite Higgses

**Three ways** to control  $\hat{T}$ :

$$C_2 : \begin{aligned} \Phi^{\hat{1}} &\rightarrow \Phi^{\hat{1}} \\ \Phi^{\hat{2}} &\rightarrow -\Phi^{\hat{2}} \end{aligned}$$

$$C_2 = P_6 \text{ in } SO(6)/SO(4) \times SO(2)$$

Accidental  $C_2$  in 2-der.  $\sigma$ -model

If unbroken,  $C_2$  leads to **Inert Higgs**

# Two Composite Higgses

**Three ways** to control  $\hat{T}$ :

**Extended Custodial:**

$$\Phi_{\hat{1}} \rightarrow L\Phi_{\hat{1}}R_1^\dagger$$

$$\Phi_{\hat{2}} \rightarrow L\Phi_{\hat{2}}R_2^\dagger$$

$SO(3)_c$  **is preserved** by the VEV

Mechanism at work in the ren.THDM

Realized in  $Sp(6)/SU(2) \times Sp(4)$

# Two Composite Higgses

## Higgs-Mediated **FCNC**:

**Renormalizable** effects:

$$\bar{q}_L (Y_1^u \tilde{H}_1 + Y_2^u \tilde{H}_2) u_R + \bar{q}_L (Y_1^d H_1 + Y_2^d H_2) d_R$$

**Solution** is restore MFV by:

**i) Symmetry:**  $C_2$  

type	$u_R$	$d_R$	$e_R$
I	+	+	+
II	+	-	-
X	+	+	-
Y	+	-	+

**ii) Ansatz:** (uv-motivated)  $Y_1^u \propto Y_2^u, Y_1^d \propto Y_2^d$ ;  
(type-III)

# Two Composite Higgses

## Higgs-Mediated **FCNC**:

Effects of **compositeness**: (for 1 or 2 Higgses)

$$\bar{q}_L (Y_1^u \tilde{H} + Y_3^u \tilde{H} H^\dagger H / f^2 + \dots) u_R$$

**Solution** is again MFV: (**Agashe-Contino**)

$$\bar{q}_L (Y_1^u \tilde{H} F_u (H^\dagger H / f^2)) u_R$$

Enforced by  $G$  **selection rules**

# Two Composite Higgses

## Higgs-Mediated **FCNC**:

$$\mathcal{L}_{\text{mix}} = (\bar{f}_L)_{\bar{\alpha}} (y_L^{\bar{\alpha}})^{I_{f_L}} \mathcal{O}_{I_{f_L}} + (\bar{f}_R) (y_R)^{I_{f_R}} \mathcal{O}_{I_{f_R}}$$

$$\Psi_L^{I_{f_L}} = (f_L)_{\bar{\alpha}} (y_L^*{}^{\bar{\alpha}})^{I_{f_L}} / g_\rho \quad \Psi_R^{I_{f_R}} = (f_R) (y_R^*)^{I_{f_R}} / g_\rho$$

$U^\dagger \Psi$  transforms as in  $H$ .

$$\text{SO}(5)/\text{SO}(4), \quad \{\mathbf{5}, \mathbf{5}\} \quad \longrightarrow \quad 2 - 1 = 1$$

$$\text{SO}(6)/\text{SO}(4) \times \text{SO}(2), \quad \{\mathbf{20}, \mathbf{1}\} \quad \longrightarrow \quad 1$$

$$\text{SO}(6)/\text{SO}(4) \times \text{SO}(2), \quad \{\mathbf{6}, \mathbf{6}\} \quad \longrightarrow \quad 3 - 1 = \cancel{2} \xrightarrow{C_2} 1$$



# Explicit Models

$$\text{SO}(6)/\text{SO}(4) \times \text{SO}(2)$$

Two doublets:  $\Phi^\alpha = \{\Phi^{\hat{1}}, \Phi^{\hat{2}}\}$

$$(U^{\mathbf{6}})^I_{\bar{I}} = \left(e^{i\frac{\Pi}{f}}\right)^I_{\bar{I}}, \quad \Pi = T_\alpha^i \Phi_i^\alpha = \frac{i}{\sqrt{2}} \left( \begin{array}{c|cc} 0_{4 \times 4} & \Phi^{\hat{1}} & \Phi^{\hat{2}} \\ \hline -\Phi^{\hat{1}} & & \\ -\Phi^{\hat{2}} & & 0_{2 \times 2} \end{array} \right)$$

$$U^{\mathbf{6}} \rightarrow \mathcal{C}_{1,2}^{\mathbf{6}} \cdot U^{\mathbf{6}} \cdot \mathcal{C}_{1,2}^{\mathbf{6}} \quad \text{with} \quad \mathcal{C}_1^{\mathbf{6}} = \text{diag}(-1, 1, -1, 1, 1, 1), \quad \mathcal{C}_2^{\mathbf{6}} = \left( \begin{array}{c|cc} 1_{4 \times 4} & 0 & 0 \\ \hline 0 & & \\ 0 & & \sigma_3 \end{array} \right)$$

## Explicit Models

$$L_{\text{mix}} = (\bar{q}_L)_{\bar{\alpha}} (y_L^{\bar{\alpha}})^{I_Q} Q_{I_Q} + (\bar{t}_R) (y_R)^{I_T} T_{I_T} + \text{h.c.}$$

$$\begin{aligned} (\Upsilon_L)^{I_Q J_Q} &= (y_L^*_{\bar{\alpha}})^{I_Q} (y_L^{\bar{\alpha}})^{J_Q}, & \rightarrow & & (\bar{\Upsilon}_L)^{\bar{I} \bar{J}} &\equiv (U^{\text{r}Q\dagger})^{\bar{I}}_I (U^{\text{r}Q\dagger})^{\bar{J}}_J (\Upsilon_L)^{IJ} \\ (\Upsilon_R)^{I_T J_T} &= (y_R^*)^{I_T} (y_R)^{J_T}. & & & (\bar{\Upsilon}_R)^{\bar{I} \bar{J}} &\equiv (U^{\text{r}T\dagger})^{\bar{I}}_I (U^{\text{r}T\dagger})^{\bar{J}}_J (\Upsilon_R)^{IJ} \end{aligned}$$

$$V = \frac{m_\rho^4}{16\pi^2} \sum_{n_L, n_R} \frac{1}{(g_\rho^2)^{n_L + n_R}} \sum_{\delta} c_\delta^{n_L, n_R} \mathcal{I}_{n_L, n_R}^\delta$$

The potential terms are H-invariants made of  $\bar{\Upsilon}$ .

## Explicit Models

$$\text{Model } \mathbf{A} : \{r_Q, r_T\} = \{2\mathbf{0}', \mathbf{1}\}$$

$$2\mathbf{0}' = (\mathbf{9}, \mathbf{1}) \oplus (\mathbf{4}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{1})$$

- we impose  $C_1 P$  to align the VEVs
- **unique** generalized Yukawa
- **multiple**  $q_L$  embedding (pick one)

# Explicit Models

$$\text{Model } \mathbf{A} : \{ \mathbf{r}_Q, \mathbf{r}_T \} = \{ \mathbf{20}', \mathbf{1} \}$$

$$\mathbf{20}' = (\mathbf{9}, \mathbf{1}) \oplus (\mathbf{4}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{2}) \oplus (\mathbf{1}, \mathbf{1})$$

**accidental symmetries !**

		Intrinsic Parity		Residual $SO(4)$
		$C_2$	$C_1P$	
$y_L^2$	$\mathcal{I}_1^1 = \delta_{ij}\delta_{kl}(\bar{\Upsilon}_L^{\mathbf{20}'})^{ijkl}$	+	+	✓
	$\mathcal{I}_1^2 = \delta_{ik}\delta_{jl}(\bar{\Upsilon}_L^{\mathbf{20}'})^{ijkl}$	+	+	✓
	$\mathcal{I}_1^3 = \delta_{\alpha\gamma}\delta_{\beta\delta}(\bar{\Upsilon}_L^{\mathbf{20}'})^{\alpha\beta\gamma\delta}$	+	+	✓
	$\mathcal{I}_1^4 = \epsilon_{\alpha\gamma}\delta_{\beta\delta}(\bar{\Upsilon}_L^{\mathbf{20}'})^{\alpha\beta\gamma\delta}$	-	-	×
	$\mathcal{I}_1^5 = \epsilon_{\alpha\gamma}\delta_{ij}(\bar{\Upsilon}_L^{\mathbf{20}'})^{i\alpha j\beta}$	-	-	×

## Explicit Models

Model **A** :  $\{r_Q, r_T\} = \{20', 1\}$

- accidental  $C_2$  and  $SO(4)$  in the potential
- accidental  $C_2$  in the top Yukawa
- **broken**  $C_2$  in the other Yukawas



**Almost Inert Higgs**

# Explicit Models

**Model A** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{\mathbf{20}', \mathbf{1}\}$

Operator	$\mathcal{I}_1^1$	$\mathcal{I}_1^2$	$\mathcal{I}_1^3$
$\frac{1}{16\pi^2} \times$	$y_L^2$	$-\frac{5}{2}y_L^2$	$y_L^2$
$m_{11}^2/f^2$	1	1	1
$m_{22}^2/f^2$	0	0	$\frac{1}{2}$
$\lambda_1$	$-\frac{2}{3}$	$-\frac{11}{30}$	$-\frac{2}{3}$
$\lambda_2$	0	0	$-\frac{1}{12}$
$\lambda_3$	0	$-\frac{1}{10}$	$-\frac{1}{4}$
$\lambda_4$	$-\frac{2}{3}$	$-\frac{4}{15}$	$-\frac{1}{2}$
$\tilde{\lambda}_4$	0	0	0

From the “**explicit**” potential:

- check that it is **tunable**  $\left(\frac{v}{f} < 1\right)$
- derive constraints on the spectrum

$$m_h^2 \sim \frac{N_c}{16\pi^2} y_L^2 g_\rho^2 v^2 \sim (100 \text{ GeV})^2 \left(\frac{y_L}{1}\right)^2 \left(\frac{3}{N}\right)$$

$$m_{H_2}^2 \sim \frac{N_c}{16\pi^2} y_L^2 g_\rho^2 f^2 \sim (200 \text{ GeV})^2 \left(\frac{y_L}{1}\right)^2 \left(\frac{3}{N}\right) \left(\frac{0.25}{\xi}\right)$$

# Explicit Models

**Model A** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{20', 1\}$

Operator	$\mathcal{I}_1^1$	$\mathcal{I}_1^2$	$\mathcal{I}_1^3$
$\frac{1}{16\pi^2} \times$	$y_L^2$	$-\frac{5}{2}y_L^2$	$y_L^2$
$m_{11}^2/f^2$	1	1	1
$m_{22}^2/f^2$	0	0	$\frac{1}{2}$
$\lambda_1$	$-\frac{2}{3}$	$-\frac{11}{30}$	$-\frac{2}{3}$
$\lambda_2$	0	0	$-\frac{1}{12}$
$\lambda_3$	0	$-\frac{1}{10}$	$-\frac{1}{4}$
$\lambda_4$	$-\frac{2}{3}$	$-\frac{4}{15}$	$-\frac{1}{2}$
$\tilde{\lambda}_4$	0	0	0

From the “**explicit**” potential:

- check that it is **tunable** ( $\frac{v}{f} < 1$ )
- derive constraints on the spectrum

$$\frac{m_H^2 - m_{H^a}^2}{m_H^2} \simeq \frac{m_h^2}{3m_H^2} + \frac{2}{3}\xi \sim \xi$$

$$\left| \frac{m_{H^\pm} - m_A}{m_T} \right|_{\text{gauge}} \sim \left( \frac{v}{f} \right)^2 \left( \frac{g'}{y_L} \right)^2 \simeq 0.03 \left( \frac{1}{y_L} \right)^2 \left( \frac{\xi}{0.25} \right)$$

## Explicit Models

Model **B** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{\mathbf{6}, \mathbf{6}\}$

$$\mathbf{6} = (4, 1) \oplus (1, 2)$$

- we impose  $C_2$
- **unique** Yukawa because of  $C_2$
- **unique** embedding (again,  $C_2$ )
- gives the **Composite Inert Higgs**



## Explicit Models

Model **B** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{\mathbf{6}, \mathbf{6}\}$

Peculiarities of the potential:

- **not tunable** at the **LO**
- accidental  $C_1P$  at **NLO**
- accidental  $SO(4)$  at **LO**

# Explicit Models

**Model B** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{\mathbf{6}, \mathbf{6}\}$

**Spectrum:**

$$m_h^2 = Y_t^2 \frac{g_\rho^2}{16\pi^2} v^2 \sim (100 \text{ GeV})^2 \left(\frac{3}{N}\right)$$

$$m_{H_2}^2 \sim N_c \frac{g_\rho Y_t}{16\pi^2} m_\rho^2 \simeq (500 \text{ GeV})^2 \sqrt{\frac{3}{N}} \left(\frac{m_\rho}{2 \text{ TeV}}\right)^2$$

$$m_H^2 \simeq \left(1 - \frac{\xi}{6}\right) m_{H^a}^2$$

# Explicit Models

**Model B** :  $\{\mathbf{r}_Q, \mathbf{r}_T\} = \{\mathbf{6}, \mathbf{6}\}$

**Spectrum:**

$$\left| \frac{m_{H^\pm} - m_A}{m_{H^\pm}} \right|_{\text{NLO}} \sim \left( \frac{v}{f} \right)^2 \frac{Y_t}{g_\rho} \simeq 0.03 \sqrt{\frac{N}{3}} \left( \frac{\xi}{0.25} \right)$$

## Conclusions

Realistic composite THDM are easily constructed

Our examples have **peculiar** phenomenology,  
because of the many **accidental symmetries**

Some progresses on the **general understanding**  
of the scenario, **better use** of symmetries

# Two Composite Higgses

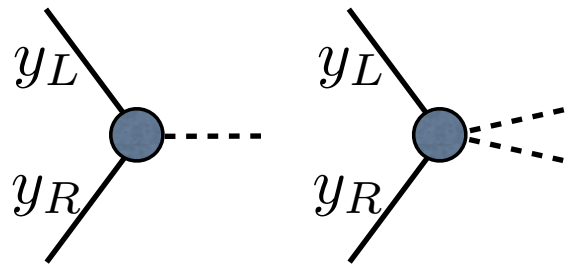
## Higgs-Mediated **FCNC**:

Effects of **compositeness**: (for 1 or 2 Higgses)

$$\bar{q}_L (Y_1^u \tilde{H} + Y_3^u \tilde{H} H^\dagger H / f^2 + \dots) u_R$$

These operators are generated by

$$\mathcal{L}_{\text{mix}} = (\bar{f}_L)_{\bar{\alpha}} (y_L^{\bar{\alpha}})^{I_{f_L}} \mathcal{O}_{I_{f_L}} + (\bar{f}_R) (y_R)^{I_{f_R}} \mathcal{O}_{I_{f_R}}$$


$$Y_{1,3}^{ij} = \frac{y_L^i y_R^j}{g_\rho} \times a_{1,3}^{ij} = g_\rho \frac{y_L^i}{g_\rho} \frac{y_R^j}{g_\rho} \times a_{1,3}^{ij}$$

# Two Composite Higgses

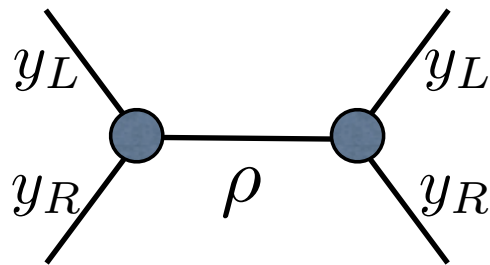
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Effects of **compositeness**: (for 1 or 2 Higgses)

$$\bar{q}_L (Y_1^u \tilde{H} + Y_3^u \tilde{H} H^\dagger H / f^2 + \dots) u_R$$

$$\Delta S = 2 \text{ transitions: } \epsilon_L^i \epsilon_R^j \epsilon_L^k \epsilon_R^\ell \frac{g_\rho^2}{m_h^2} \frac{v^4}{f^4} \left( \bar{f}_L^i f_R^j \bar{f}_L^k f_R^\ell \right)$$

v.s. resonance effects:



$$\epsilon_L^i \epsilon_R^j \epsilon_L^k \epsilon_R^\ell \frac{g_\rho^2}{m_\rho^2} \left( \bar{f}_L^i f_R^j \bar{f}_L^k f_R^\ell \right)$$