

A Taste of Nuclear Structure from an Experimental Point of View (in two lectures)

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Plan of Action

Keep it simple and give a flavour of WHY/WHAT/HOW of nuclear structure.

- Back to basics: what is a nucleus? nucleus as a quantum system, single-particle and collective structure, exotic nuclei – not comprehensive, just a flavour!
- What characterises a nucleus and how do we study them? nuclear properties, nuclear reactions, historical context, stable and exotic ion beams.
- Case study: some recent example measurements from ISOLDE@CERN – will push the boundaries of nuclear structure into other areas
- Perspectives.

A - taking an experimental, intuitive, pedagogical, heuristic approach – with lots of "cartoon" explanations!





What is a nucleus?

- Protons (charged) and neutrons; *nucleons*.
- Electrostatic repulsion vs strong attraction.
- Nucleon incompressibility, r=1.2A^{1/3} fm.
- Looks static, dull and uninteresting.
- Quantum mechanics makes it much more dynamic see next.
- N-N binding force that depends on separation, spin orientation, and relative momentum with tensor, non-central and exchange contributions.
- In-medium effects make things even more complex with three-body forces and higher order contributions.









Sean J Freeman | Nuclear Structure Experiment

 N_3

Challenges in nuclear structure

- Describe a many-body system using quantum mechanics where particles interact via a complicated force.
- In principle, could operate like solving hydrogen atom. *Ab-initio Models*: write down the Schrödinger equation for each nucleon including interactions with all other nucleons using nucleon-nucleon interaction – complex coupled equations.
- Calculations beyond A=12 become difficult; with a good form of the N-N force:
 - ⁴He takes ~1 cpu-hour ⁸Be takes ~300 cpu-hour ¹²C takes ~70,000 cpu-hour (8 years!)
- In principle, could operate like solid-state physics and use statistical mechanics, but not enough 300 particles rather than 10²³!
- Some analogy with a liquid droplet, can approach macroscopically.





Mean-field approaches to single-particle structure

- *Mean-field potential*: assume that all the interactions with all the other nucleons averages out to some potential that only depends on the coordinates of the nucleon in question. Schrödinger equation separates into single nucleon equations.
- *Hartree-Foch* is one theoretical tool but you can guess the general form!
- The *nuclear shell-model* uses a simple approach with a harmonic oscillator potential with a *spin-orbit interaction* could use anything that is a complete basis set!
- *Spin-orbit interaction* is a famous addition from 75 years ago that "fixes" the magic numbers.
- Run the now easy quantum mechanics and get levels in the well...

Example of potentials for a neutron bound to a ¹¹²Sn nucleus





Magic numbers



Nucleons as fermions fill single-particle levels...clumping of levels causes

(STABLE) Magic numbers 2, 8, 20, 28, 50, 82 and 126

But starting to these disappear and new ones appear away from stability.





(168)

Independent-particle model:

Single-nucleon wavefunctions characterised by: *n*, *l*, and *j* quantum numbers.

Nuclear wavefunction constructed using products of single-nucleon wavefunctions coupled to give the right spin and appropriately anti-symmetrised.

BUT – extremely limited success in describing experimental data. *Essentially just spin-parities of a few nuclei around closed shells along the line of stability.*





Beware the residual interaction:

The nucleus is made up of A nucleons:

Depends only on coordinates of one nucleon, i one-body operator t

Limit to two-body interaction - ignoring 3body forces already!

 $\hat{H}\Psi = \left| -\frac{\hbar^2}{2m} \sum_{i}^{A} \nabla_i^2 + \sum_{ij} V_{ij} \right| \Psi = E\Psi$

Invent an AVERAGE or MEAN-FIELD POTENTIAL:

$$\hat{H}\Psi = \left[\sum_{i}^{A} \left(-\frac{\hbar^2}{2m}\nabla_i^2 + U(r_i)\right) + \left(\sum_{ij} V_{ij} - \sum_{i}^{A} U(r_i)\right)\right]\Psi = E\Psi$$

KE plus mean-field potential are one-body operators generates IPM configurations as a basis set the residual interaction, contains the two-body terms that mixes the basis sets. Depends on the motion of nucleons i and j, i.e. the associated single-particle quantum numbers, and builds "correlations" between nucleons. Scatters from below Fermi surface to above (later!).

You <u>cannot</u> ignore the residual interaction – nuclear shell model uses phenomenological residual interactions and matrix diagonalization to solve the problem – results are admixtures of independent-particle configurations.



Expectations in very exotic nuclei:



When adding nucleons can expect the system to become less well bound; final nucleons can wander more: surface becomes more diffuse.

$$V_{so} = -V_0rac{1}{r}rac{\partial U(r)}{\partial r}\ell.{f s}$$

Changes in diffuseness of mean-field potential near neutron drip line may influence spin-orbit interaction:

Nuclei with neutron haloes have been observed!

Nuclear Shell Structure



J.Dobaczewski et al. Prog.Part.Nucl.Phys. 59 432 (2007)



Shell evolution

In IPM, protons and neutrons fill the levels according to Pauli, e.g. stable mid-shell nucleus with N>Z.



- Potentials around 50 MeV deep (nucleon scattering).
- Energy in N-N residual interactions
- << 7 MeV (binding energy per nucleon).
- Residual interactions scatter nucleons from orbitals around the Fermi level.

- Different isotopes have different N/Z
- Fermi surfaces sample different single-particle orbitals.
- Correlations between nucleons depend on their orbitals, expect to different nuclear structure in different nuclei.



from Rev. Mod. Phys. 92, 015002 (2020)

- Expect changes in shell structure of protons/neutrons as you move along a chain of isotones/isotopes sometimes enough to create or destroy magic numbers
- Expect differences in the overall effect of residual interactions when you excite nucleons within a nucleus.



Shell evolution

As chains of isotopes and exotic nuclei are probed, beginning to see examples of phenomena.

h_{9/2}

7_{11/2}

 $g_{7/2}$

g_{9/2}

Proton states in Sb isotopes probed by gently adding a proton to Sn targets in a *transfer reaction*.



Other examples of new magic numbers starting to emerge e.g. N=32 and N=34 in calcium isotopes.

²⁵O produced in single-neutron *knockout reaction* from ²⁶O. Ground-state mass reconstructed from the reaction products; difference with ²⁴O tells you the $d_{3/2}$ energy.



from Rev. Mod. Phys. 92, 015002 (2020)

Prompted discussions of what makes a magic number and what quantities characterise them?



Collectivity and nuclear shape

For a nucleus corresponding to a shell closure, large jump from Fermi level to the next empty orbital – effect of residual interactions low and IPM works (a little) better.

Going away from a closed shell, with increasing numbers of (valence) nucleons outside the shell, the correlations between them increase and can have macroscopic effects on the nuclear structure, distorting the surface.

Distortions of the nuclear surface described by a spherical harmonic expansion – good angular momentum:

$$R(\theta,\phi) = c(\alpha_{\lambda\mu})R_0 \left[1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda\mu} Y_{\lambda\mu}(\theta,\phi)\right]$$

Excitations can arise if the shape changes with time – NUCLEAR VIBRATIONS.

Permanent distortions lead to NUCLEAR SHAPE and excitations can arise from ROTATIONS of that shape.

Coherence in the admixtures of single-particle configurations can greatly increase some observables – e.g. electrostatic moments, e/m transition rates... Example: quadrupole shapes

$$Q_0 = Z \left[3\langle z^2 \rangle - \langle r^2 \rangle \right]$$

$$z^2 \rangle > \frac{1}{3} \langle r^2 \rangle \qquad \frac{3 \langle z^2 \rangle = \langle r^2 \rangle}{\langle x^2 \rangle = \langle y^2 \rangle = \langle z^2 \rangle} \quad \langle z^2 \rangle < \frac{1}{3} \langle r^2 \rangle$$



Given the nucleus has a charge – distortion results in electromagnetic moments, which can be probed experimentally in some nuclear reactions or by their effect on electron levels in the associated atom/ion (see later!).



Vibrations and rotations

Harmonic vibrators give equally spaced energy levels. Rotational levels proportional to I(I+1) – gaps between them as I. e/m transition strengths between levels (deduced by measuring the lifetime of the excited state) are also characteristic.







Shape evolution and coexistence

We saw that the effect of residual interactions changes along chains of isotopes/isotones and within excited states in the same nucleus – these also drive evolution in nuclear shape. You need to access particular (N,Z) to study certain shapes.

EXAMPLE: octupole or pear-shaped deformation related to correlations induced by a Y_3 operator, strong between orbitals of opposite parity and ΔJ , $\Delta L = 3$ close to the Fermi level.





EXAMPLE: spherical, oblate and prolate shapes exist as different excited states in the same nucleus¹⁸⁶Pb.

A.Andreyev et al., Nature 405, 430 (2000)

Pause for thought:

- nuclei = a complex, many-body problem bound with complicated strong force.
- relatively simple structures emerge from this complexity.
- correlations between nucleons are very important.
- nuclear structure has microscopic (single-particle) and macroscopic (collective) features.
- the only bound system of two different fermions the proton/neutron Fermi surfaces sample different single-particle orbitals and the resulting correlations support different structures.
- leads to an evolution of shell structure, nuclear shape and shape coexistence.
- expectation of strange effects in the most exotic, least bound systems near the proton and neutron driplines.

- How can we understand the forces binding nuclei?
- How do these forces lead to the microscopic structure of nuclei?
- How do macroscopic structures arise in nuclei?
- What are the limiting conditions for the nuclear binding and what phenomena emerge at the limits?
- What impact does nuclear structure have on other areas such as the origin of the chemical elements and fundamental physics?

Nuclei far from the line of stability hold the keys to answering these questions.

How do we access and study exotic nuclei?.



What characterizes a nucleus?

Some examples of relevant quantities....









decay properties: mode, lifetime, BR..

spin-parity



....in principle, for the ground state and excited states.



Historical perspective

(i) Early Years: discoveries of radioactivity, nucleus, nuclear reactions, protons and neutrons, isotopes – using mainly decay.

(ii) Neutrons: from reactions initiated by radioactivity, then fission, then accelerators.

(iii) Light-ion accelerators: explosion of small machines for protons, deuterons and alphas for elastic/inelastic scattering, compound nucleus, transfer, with increasing energy allows spallation etc.

(iv) Heavy-ion accelerators: Coulomb excitation, fusion evaporation, with increasing energy projectile fragmentation

(v) Radioactive ion beam facilities: early work on spallation and fragmentation harnessed for production of beams of exotic nuclei used to induce secondary nuclear reactions.





Radioactive Ion Beam Facilities

- Most isotopes predicted to exist are not known.
- Many known exotic isotopes have only rudimentary studies.
- The proton drip line has been reached in many cases; the neutron drip line is largely unknown.

Requires:

- i. high-intensity exotic nuclei for direct study.
- ii. high-energy exotic beams to initiate secondary reactions

Two main types of facility have emerged.



from "The Discovery of Isotopes" Michael Thoennessen



















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As an example of an ISOL facility and a slightly deeper dive into the experiments in nuclear structure and the physics that can be addressed....will stray into other scientific areas in the process!

Still high-level view – presenting work of a vast array of scientific, engineering and technical experts.



The CERN accelerator complex Complexe des accélérateurs du CERN



 \downarrow H⁻ (hydrogen anions) \downarrow p (protons) \downarrow ions \downarrow RIBs (Radioactive Ion Beams) \downarrow n (neutrons) \downarrow p (antiprotons) \downarrow e⁻ (electrons) \downarrow μ (muons)

LHC - Large Hadron Collider // SPS - Super Proton Synchrotron // PS - Proton Synchrotron // AD - Antiproton Decelerator // CLEAR - CERN Linear Electron Accelerator for Research // AWAKE - Advanced WAKefield Experiment // ISOLDE - Isotope Separator OnLine // REX/HIE-ISOLDE - Radioactive EXperiment/High Intensity and Energy ISOLDE // MEDICIS // LEIR - Low Energy Ion Ring // LINAC - LINear ACcelerator //

n_TOF - Neutrons Time Of Flight // HiRadMat - High-Radiation to Materials // Neutrino Platform

ISOL with GeV Protons





Isotope Production with GeV protons and over 50 years of experience

 Over 20 target materials – carbides, oxides, solid metals, molten metals and molten salts – operated at high temperature.



Research with radioactive beams at ISOLDE



Low-energy installations



MEDICIS

HIE-ISOLDE completed 2018





Some recent science highlights from ISOLDE: a quick stroll through fundamental science, nuclear physics to condensed matter...

Difficult to be representative of the overall science programme – spoilt for choice!





Electric dipole moment searches

Searching for effects of EDM in atomic energy levels provides a precision method to test fundamental physics..

Polarisation of molecules of heavy elements amplifies the interaction with external electric fields by factors of up to 10⁶ and are less sensitive to problematic systematic effects.

<u>Static</u> nuclear octupole deformation of the heavy element can add an additional enhancement via the atomic Schiff moment.

Where do octupole nuclei lie away from stability and what signatures?

Molecular spectroscopy of heavy molecules?



Stable octupole shape versus octupole vibration?

Circumstantial evidence existed for some time that certain nuclei show octupole distortion...but observables (interleaved parity bands in even-even; parity doublets in odd-A; enhanced E1) are indirect



ISOLDE Coulomb excitation establish direct evidence for stable octupole deformation in ²²⁴Ra via measurements of transition matrix elements – neighboring odd isotopes would have enhanced EDM's. ²²⁰Rn appears to how dynamic octupole vibration – ^{219,221}Rn unlikely to have enhancement.

REX-ISOLDE 2.8 MeV/u







Nature 497, 199 (2013)



Sparse data on stable pear shapes extended to show the boundaries of this region:

- ²²²Ra has patterns of transitions and matrix elements consistent with stable octupole shape.
- ²²⁸Ra is exhibits octupole vibration.

PRL 124, 042503 (2020)

HIE-ISOLDE 4.3 MeV/u

33



CRIS. Spectroscopy of Radioactive RaF

Multiple laser beams stepwise excite a neutral radioactive atom/molecule to ionization continuum.

Tuning the frequency of one laser as the ion yield is monitored enables the molecular levels to be mapped out.

Nature 581, 396 (2020)



Fig. 3 | **Vibronic spectra measured for different isotopologues of RaF.** Measured vibronic absorption spectra for the $A^2\Pi_{1/2} \leftarrow X^2\Sigma^*$ transition are shown for the isotopologues ²²³RaF, ²²⁴RaF, ²²⁵RaF, ²²⁶RaF and ²²⁸RaF. Wavenumber values are relative to the transition (0, 0) of ²²⁶RaF. ISOLDE experiments established low-lying electronic structures of RaF with nuclear octupole deformation giving evidence for their suitability for laser cooling, a pivotal step to precision measurements for EDM searches.

Recently followed up by AcF measurements during "winter physics" in 2022.

PHYSICS TODAY

11 Jun 2020 in Research & Technology

Spectroscopy of molecules with unstable nuclei

physicsworld

ATOMIC AND MOLECULAR RESEARCH UPDATE

Exotic radioactive molecules could reveal physics beyond the Standard Model ^{05 Jun 2020}







ISOLDE Solenoidal Spectrometer

Direct reactions: e.g. addition of neutron to a nucleus (d,p) without excitation of other degrees of freedom probe single-particle strength distributions.

Stable species: deuteron beam on target – CM with small velocity.

Unstable species: heavy beam on deuterated target - CM with large velocity, creating kinematic issues for measuring outgoing proton.

Helical orbit spectrometer principle

Target on the field axis + array of Si detectors.

MEASURE: position z, cyclotron period T_{cvc} and energy E_p of emitted protons from transfer reaction







4T superconducting (former MRI) solenoid from UQ hospital, Brisbane to ISOLDE in 2017



No kinematic compression of the Q-value spectrum – excellent resolution without need for y rays.







First ISS Physics (CERN Run 2) 2018 – with HELIOS Si array.

(i) Terra incognita Z<82 N>126

Study excited states in ²⁰⁷Hg for the first time using transfer reactions, ²⁰⁶Hg(d,p)@7.4 MeV/A, 5x10⁵ pps, 165 μg/cm²,140-keV FWHM.





Energy (MeV)

2492

3917+4042

 θ_{CM} (deg)

2257

3201

 $\ell = 2$

(ii) Single-particle evolution driving shape changes

1434

2868

 $\ell = 3$

4352

Si recoil

detector

Map single-particle trends close to abrupt shape change in ³⁰Mg: ²⁸Mg(d,p)@9.47 MeV/A, 10⁶ pps, 80 and 120 μg/cm², 150-keV FHWM.

MANCHESTER

The University of Manchester



Tests of shell models tuned for the Island of Inversion and highlights the role of geometry of the binding potential on behaviour of orbitals close to threshold.

> MacGregor et al. PRC Letts 104, L051301 (2021)



Transfer-induced fission:



Proof of principle experiment using the HELIOS@ANL ²³⁸U(d,pf) 8.6 MeV/u

Accepted PRL 2023



CHALMERS

ISOLDE: MWPC coupled to solar-cell array being developed to study transfer-induced fission









Indium – from one extreme to the other – two back-to-back ISOLDE PRL's in July



Isomeric Excitation Energy for ⁹⁹In^m from Mass Spectrometry Reveals Constant Trend Next to Doubly Magic ¹⁰⁰Sn



- Precision measurement of ground and isomeric state using <u>ISOLTRAP.</u>
- Excitation of isomer extremely constant across In
- In contrast to measurements of magnetic moment, which increases near N=50 - also ISOLDE experiment from 2022!
- Very difficult to reproduce with modern calculations and may point to missing physics.



¹³³In: A Rosetta Stone for Decays of *r*-Process Nuclei

- Measured β decays from ground and isomeric levels using ISOLDE DECAY STATION.
- Decays populate just a few unbound levels in ¹³³Sn.
- Measured resonance properties that are critical for benchmarking models of the *astrophysical r process* that manufactures many of the heavy chemical elements.

Good example of versatility of ISOLDE – <u>precision</u> studies of <u>both</u> neutron-rich and neutron-deficient exotic isotopes separated by 34 neutrons!

Towards a nuclear clock...

For 60 years, atomic clocks have been used with a precision of 1s in 300 million years. Based on the frequency of a transition between two atomic levels in cold ¹³³Cs atoms.

> If you can find two nuclear levels with separation corresponding to optical photons, the nuclear clock would be much more precise as less sensitive to external perturbations.

²²⁹Th isomer is currently the best candidate for a nuclear clock, with a first excited state at only around 8 eV from the ground state and a long half life

Experiment at ISOLDE: ^{229m}Th ions produced using β -decay of a ²²⁹Fr - ²²⁹Ra beam implanted into CaF₂ and MgF₂ crystals. Radiative decays of ²²⁹Th observed for the first time giving precise measurement of transition energy (essential for laser excitation of the clock) and confirmed "long" lifetime of ^{229m}Th state



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148

150

152

154





Vacancy centres in diamond as potential qubits

Diamond has excellent optical/mechanical properties for integrating into photonic circuits and quantum info tech – refractive index, transmission window, band gap, high Young's modulus etc.

Optically active crystal defects "color centres" can exhibit stable single-photon fluorescence, combined with nanophotonic circuits, could act as qubits - those created by nitrogen are well studied.

Implantation of radioactive ¹²¹Sn into diamond at ISOLDE allows β "emission channeling" to study the lattice site location – measure intensity of β as a function of angle to lattice direction and model the results.



Experiments revealed that Sn vacancy centres are very promising candidates for single-photon emission due to their excellent optical properties and a very simple structural formation mechanism.





Perspectives

- The study of the nuclear many-body problem, effectively "nuclear structure", is a tricky and difficult problem.
- It is (endlessly!) fascinating how the nucleus can exhibit such different behaviour and how simplicity emerges from such a complex system.
- The study of exotic nuclei is giving new impetus to these challenges and the start of several new facilities – FRIB (USA), FAIR (Germany), RAON (Korea), SPES (Italy)... and improvements to others GANIL (France), ISOLDE (CERN), RIKEN (Japan) – make it an exciting time for nuclear structure.
- More and more nuclear structure and the techniques used to study the nucleus are becoming important for other areas of study from fundamental forces through to condensed matter physics.







home.cern

Large Shape Staggering in Neutron-Deficient Bi Isotopes



In-source laser spectroscopy – wavelengths of ionising lasers scanned as yields deduced by measurements of α decay, mapping out the atomic hyperfine structure.

Deduce changes in mean-square charge radii via the isotope shifts.

Spectacular changes in radius in Bi isotopes due to rapidly changing gs shapes.

Only second example of such dramatic changes – Hg isotopes studied at ISOLDE 50 years ago.



PRL 127, 192501 (2021)





ISS Science Programme: (d,p) studies



Third ISS Physics (CERN Run 2) 2022 – with ISS Si array.





- ⁶⁸Ni ~2 x 10⁴ pps @ 6.0 MeV/*u*
- N = 50 shell gap approaching ⁷⁸Ni

• Intruder configurations leading to shape coexistence



GANIL experiment (2010, unpublished, M. Moukkamad et al.) $E_{beam} = 25.14 \text{ MeV}/u; CD_2 \text{ Target} : 2.6 \text{ mg/cm}^2$

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