Nuclear Reactions 3 & 4 Cross Section Measurements

Claudia Lederer-Woods University of Edinburgh, UK



European Research Council Established by the European Commission





Nuclear Reactions 3 & 4 (Direct) Cross Section Measurements (for Astrophysics)

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Outline

- Introduction
- Charged Particle Induced Reaction Measurements
 - stable beams (example LUNA)
 - radioactive beams (examples ISOLDE and GSI)
- Neutron Induced Reaction Measurements
 - radiative capture
 - n,cp

Acknowledgements: Material partly from Colleagues of the NP Edinburgh Group (M. Aliotta, PJ Woods, A. Murphy, C.G. Bruno, ...) and n_TOF Collaboration

Introduction

Nuclear Reactions

- collision process between projectile p and target nuclei T: $p+T \rightarrow e+R$ or T(p,e)R
- ejectile (e) and recoil (R) may be the same as p and T (scattering)
- Examples
 - Elastic Scattering: $p + T \rightarrow p + T$
 - Inelastic Scattering: $p + T \rightarrow p + T^* \rightarrow p + T+\gamma$
 - Radiative Capture: $p + T \rightarrow R^* \rightarrow R + \gamma$

Nuclear Reactions

• Energy conservation:

E.... kinetic energy

• Q-value of a reaction: $Q = m_p c^2 + m_T c^2 - m_e c^2 - m_R c^2$

Q>0 exothermic (energy is released) Q<0 endothermic (energy is required)

• Threshold energy (lab) for projectile p reacting with stationary target T:

 $E_{th} = (-Q)x(1+m_p/m_T)$

Nuclear Reaction Cross Section

- cross section σ = quantitative measure of probability for a reaction to occur
- Dimension: area Unit: barn (b) = 10⁻²⁴ cm²
- cross sections are energy (i.e. velocity) dependent
- In general: not possible to determine reaction cross section from first principles

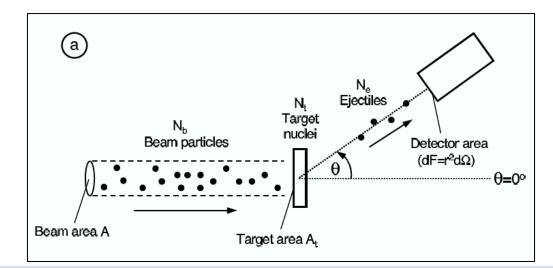
$$\sigma = \frac{N_e/t}{(N_b/tA)N_t}$$

• Differential cross section:

$$\frac{d\sigma}{d\Omega} = \frac{N_e^{d\Omega}/t}{(N_b/tA)N_t} \frac{1}{d\Omega}$$

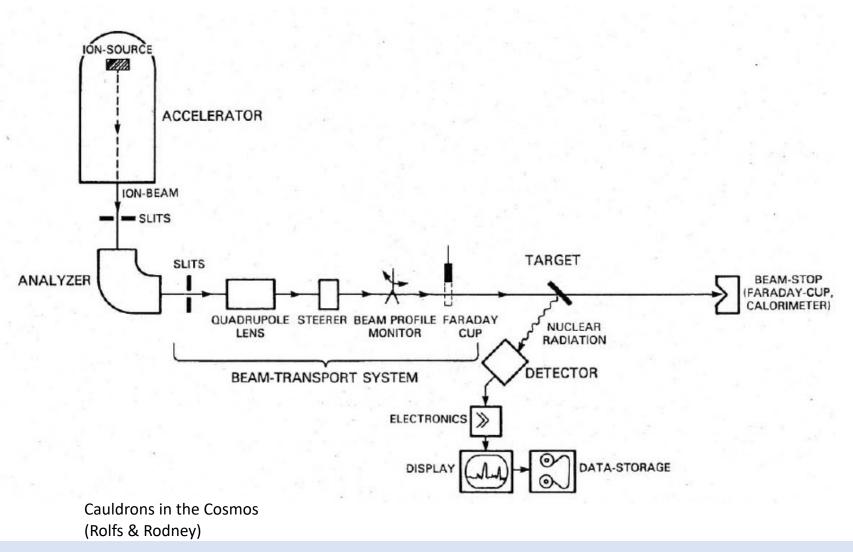
and
$$\sigma = \int \frac{d\sigma}{d\Omega} d\Omega$$

N_e/t... Number of reactions per time N_b/tA... Number of beam particles per time per area N_t... Number of target nuclei in the beam



Reactions with Ion Beams

Schematic Layout for Nuclear Reaction Experiments



Beam Requirements and Properties

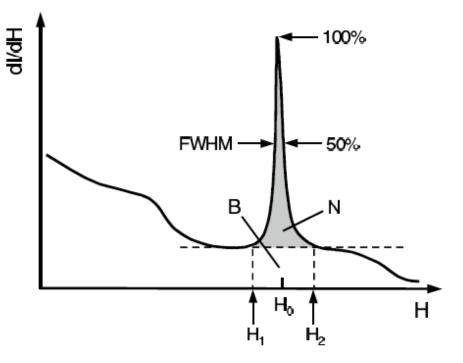
- high intensity
 - for stable nuclei, μA-mA currents are possible, corresponding to ~ 10¹²-10¹⁵ particles per second (pps)
 - for unstable nuclei, intensities vary greatly depending on isotope (10³-10⁶ pps)
- low energy spread
 - ideally $\Delta E \leq 1 \text{keV}$
- easily adjustable energy
 - few keV steps often required
- well collimated
- high purity
- small spot size on target
 - better definition of interaction point
- good absolute energy calibration

Target Requirements and Properties

- high purity
 - avoid background reactions on contaminants
- known and stable stoichiometry (for compound targets)
- appropriate and uniform thickness
 - thin enough to let beam pass through (transmission targets)
 - thick enough to stop the beam (beam-stop targets)
 - anywhere in between
- for solid targets
 - evaporated, sputtered, implanted
 - with or without backing
 - allow for water-cooling if high beam intensities are used
- for gas target
 - extended, or jet-like
 - with or without containment windows
 - recirculation (especially for expensive gases)

Detector Requirements and Properties

- nuclear reactions are studied by measuring reaction products
 - mostly protons, neutrons, α particles, or γ rays
- different types of radiation interact in different ways with
- type of detector used will depend on radiation to be measured
- electric signal produced in detector with amplitude proportional to energy deposited by radiation
- high efficiency
- good energy resolution R=FWHM/H₀
- good solid angle coverage



Reactions with Ion Beams Yield measurements and Cross Section

Reaction Yield

$$Yield = \frac{total number of reactions}{total number of incident particles}$$

yield vs bombarding energy = *yield curve* or *excitation function*

Yield over slice of target with thickness Δx , assuming σ and stopping power ε constant (energy lost by beam small) $\Delta Y = \frac{N_R}{\Delta x} = \sigma n \Delta x$

$$\Delta I = \frac{1}{N_B} = 0 \, n \Delta x$$

With stopping power $\varepsilon(E) = -1/n x dE/dx$ and particles per volume n

Total yield from integration over all target slices:

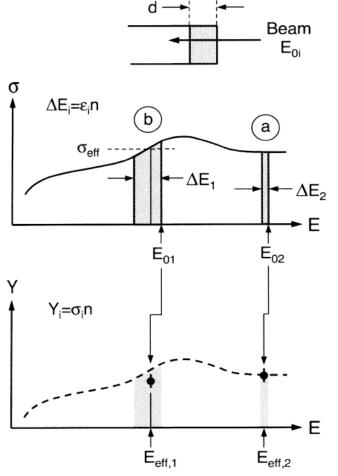
$$Y(E_0) = \int \sigma(x)n(x)dx = \int \sigma(x)n(x)dx \frac{dE(x)}{dx} \frac{dx}{dE(x)}$$
$$Y(E_0) = \int_{E_0 - \Delta E}^{E_0} \frac{\sigma(E)}{\varepsilon(E)} dE \qquad \text{where } \Delta E \text{ is the energy lost by the beam over the target thickness}$$

for non-resonant reactions or for broad resonances

<u>cross section</u> and <u>stopping power $\varepsilon(E)$ </u> are almost <u>constant</u> within small energy region

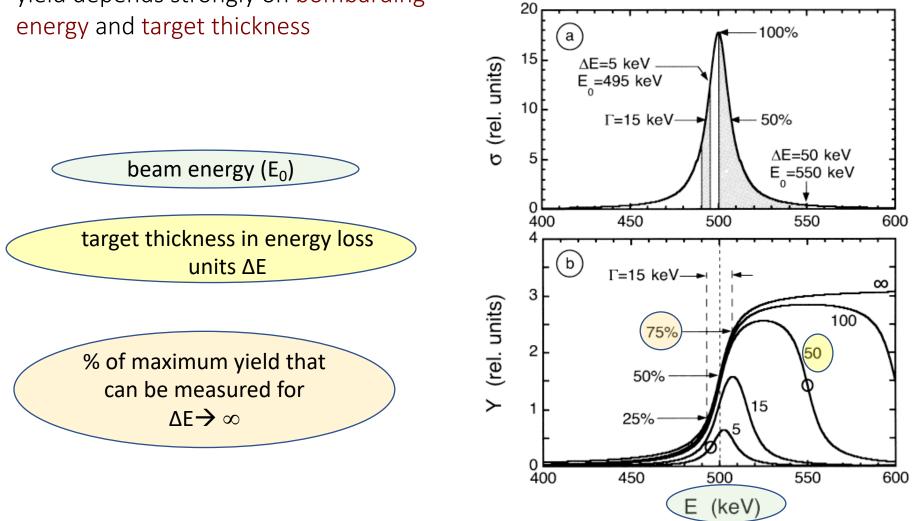
$$Y(\mathsf{E}_{0}) = \int_{\mathsf{E}_{0}-\Delta\mathsf{E}}^{\mathsf{E}_{0}} \frac{\sigma(\mathsf{E})}{\varepsilon(\mathsf{E})} d\mathsf{E} = \frac{\sigma(\mathsf{E}_{eff})}{\varepsilon(\mathsf{E}_{0})} \Delta\mathsf{E}(\mathsf{E}_{0})$$

E_{eff} energy at which the cross section, evaluated at this energy, equals the cross section averaged over the target thickness; energy at which 50% of total yield is obtained



Iliadis, 2007

for <u>resonant reactions</u>: yield depends strongly on bombarding energy and target thickness



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16

for resonant reactions:

yield depends strongly on bombarding energy and target thickness

thin target thickness $\Delta E \ll \Gamma$

yield curve resembles cross section curve

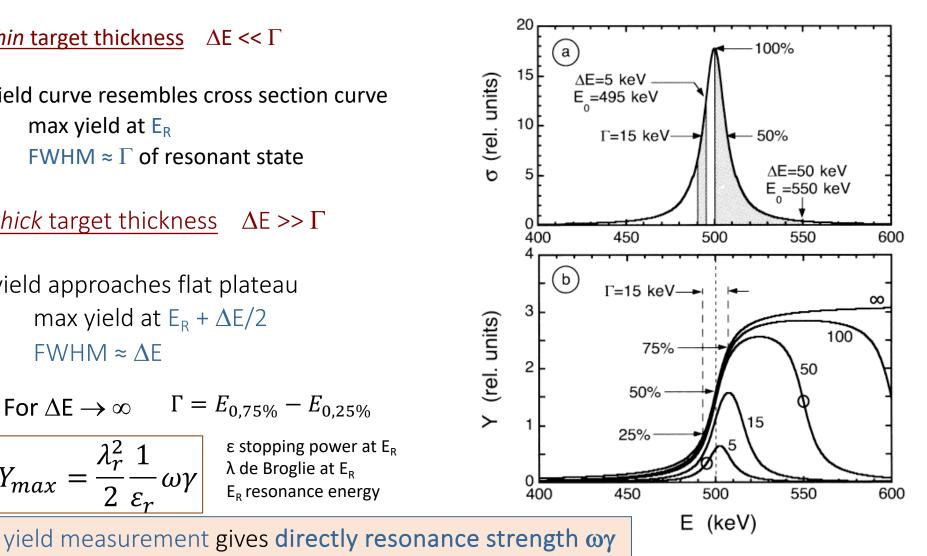
- max yield at E_R
- FWHM $\approx \Gamma$ of resonant state

thick target thickness $\Delta E >> \Gamma$

yield approaches flat plateau

- max yield at $E_{R} + \Delta E/2$
- FWHM $\approx \Lambda F$

For
$$\Delta E \rightarrow \infty$$
 $\Gamma = E_{0,75\%} - E_{0,25\%}$
 $Y_{max} = \frac{\lambda_r^2}{2} \frac{1}{\varepsilon_r} \omega \gamma$
 ϵ stopping power at E_R
 λ de Broglie at E_R
 E_R resonance energy



Reactions with Stable Ion Beams

Quiescent burning stages of stellar evolution



- Nuclear reactions in stable (quiescent) burning phases of stars happen energies below the Coulomb Barrier due to low the temperature $T \simeq 10^6 10^8 \text{ K}$
- $\Rightarrow E_0 \sim 100 \text{ keV} << E_{coul} \Rightarrow \text{ tunnel effect}$
- \Rightarrow 10⁻¹⁸ barn < σ < 10⁻⁹ barn

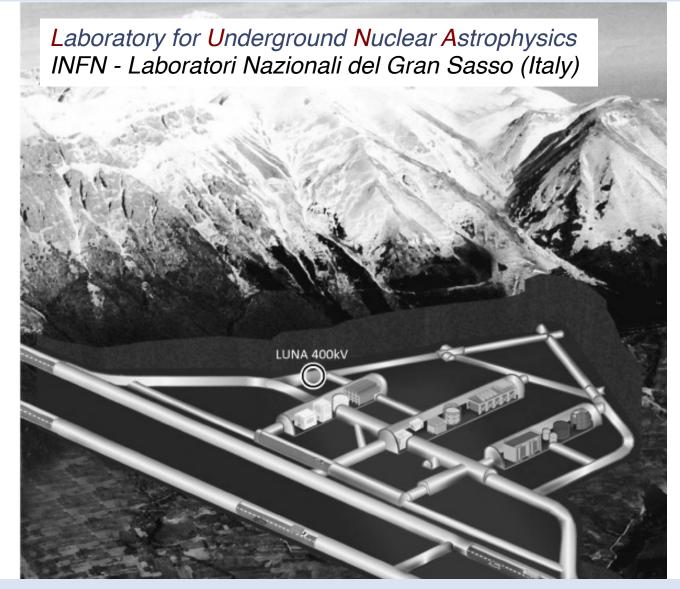
⇒ average interaction time $\tau \sim \langle \sigma v \rangle^{-1} \sim 10^9$ y, hence unstable species <u>DO NOT</u> play significant role

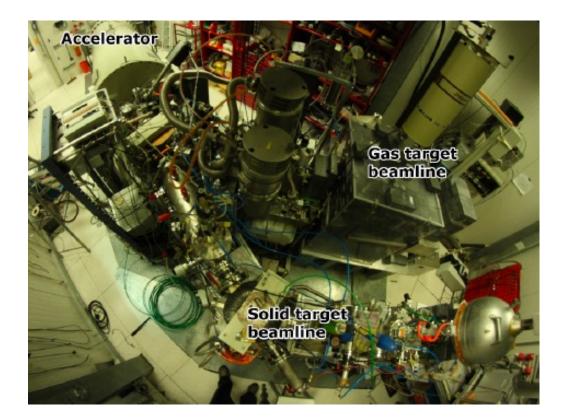
- Low count rates (and poor signal-to-noise ratios) require
 - \Rightarrow long measurements
 - \Rightarrow ultra pure targets
 - \Rightarrow high beam intensities
 - \Rightarrow high detection efficiency

 \Rightarrow reducing natural background

Measurements underground

¹⁷O(p,α) Cross Section at LUNA

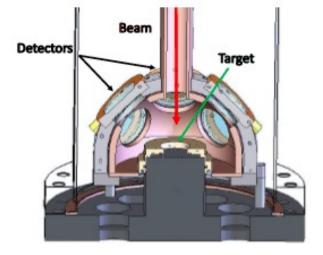


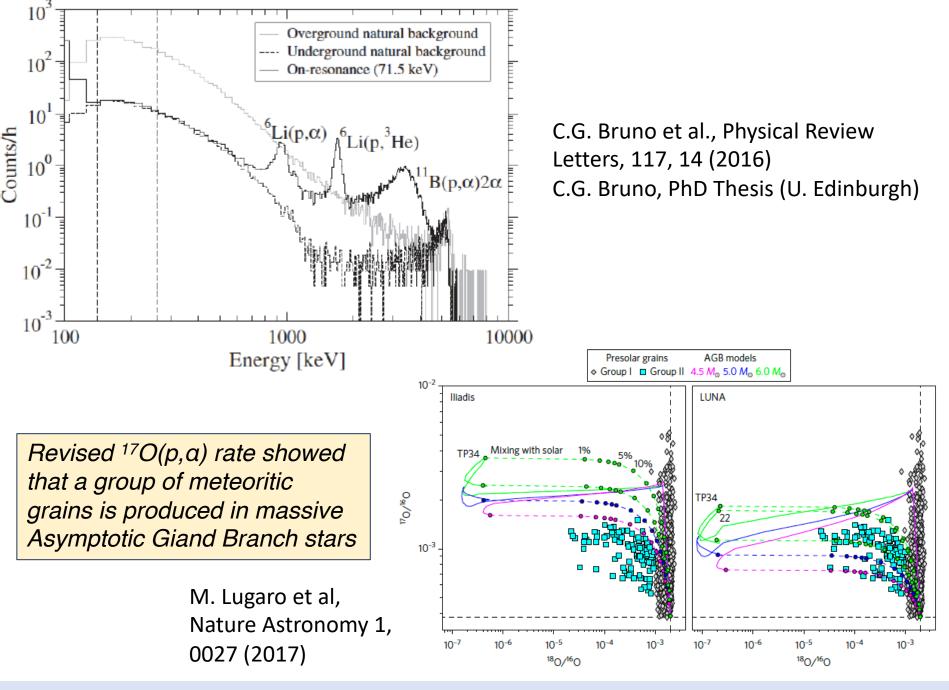


- typical beam intensities 100-200 μA
- expected alpha particle energy E ~ 200 keV (from 70 keV resonance in ¹⁷O(p,a)¹⁴N)
- protective aluminized Mylar foils before each detector

C.G. Bruno et al., Physical Review Letters, 117, 14 (2016) C.G. Bruno, PhD Thesis (U. Edinburgh)







Reactions with Radioactive Ion Beams

Explosive burning stages of stellar evolution

- Nuclear reactions in explosive environments (T[~] GK) typically happen at higher energies (near Coulomb barrier) → higher cross sections
- Reactions on protons and alphas: Measurements in Inverse Kinematics

<u>CHALLENGES</u> unstable nuclei \Rightarrow short half-lives

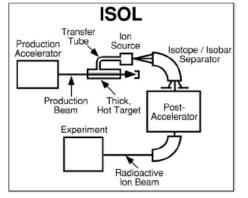
 \Rightarrow low beam currents

REQUIREMENTS

- \Rightarrow Radioactive Ion Beam facilities
- ⇒ produce and accelerate ions of interest
- \Rightarrow dedicated detection systems

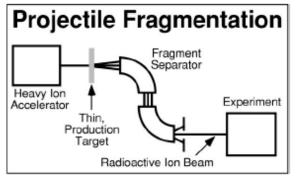
Radioactive Ion Beam Production

- Off-Line Production and subsequent installation in accelerator (limited to longlived isotopes)
- ISOL Technique



- excellent quality (small emittance)
- limited number of species and half lives

• In-Flight / fragmentation



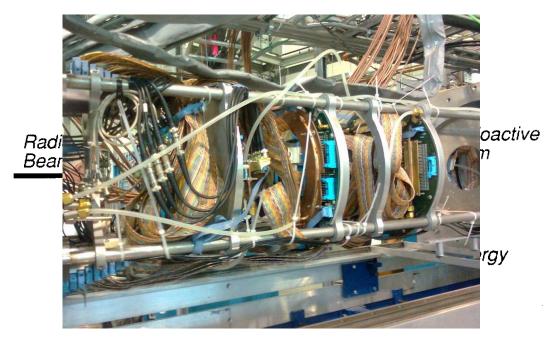
- independent of chemical properties
- small half lives possible
- larger beam spot, poorer emittance
- energies generally too high for nuclear astrophysical studies

Smith and Rehm, Annu. Rev. Nucl. Part. Sci. 2001. 51:91–130

mainly $X(p,\alpha)Y$ and $X(\alpha,p)Y$

light-heavy nuclei coincidence

silicon strip detector arrays \Rightarrow large solid angle coverage (e.g.TUDA at TRIUMF)



- Coincident detection of heavy recoil and light ion (i.e. proton, alpha)
- High segmentation of detectors for accurate determination of kinematics
- If possible dE-E particle identification

⁴⁴Ti(α,p) Cross Section at REX-ISOLDE

- Important destruction reaction of cosmic γray emitter ⁴⁴Ti
- ⁴⁴Ti from highly irradiated components of the SINQ spallation neutrons source (PSI)
- Detection of Proton using ΔE-E technique
- $\Delta E = \text{fraction of energy lost in thin}$ detector $\sim MZ^2/E_{\text{ini}}$

(p,p)

10

8

6

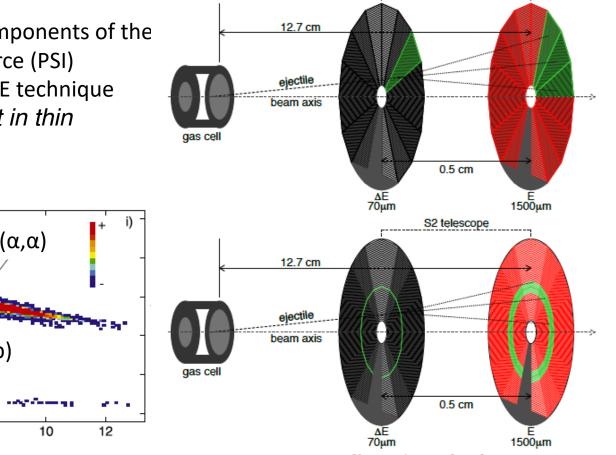
2

0

0

2

ΔE[MeV]



S2 telescope

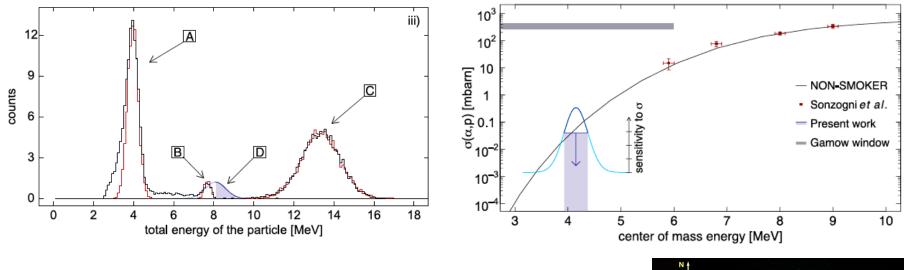
V. Margerin et al. Physics Letters B 731 (2014) 358–361 ; V. Margerin, PhD Thesis (U. Edinburgh)

(p,p)

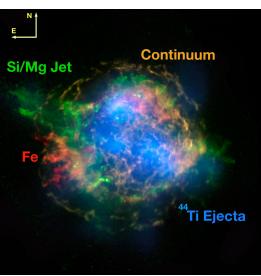
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E [MeV]

⁴⁴Ti(α,p) Cross Section at REX-ISOLDE



- No signal above background
- Upper limit suggests lower destruction rate



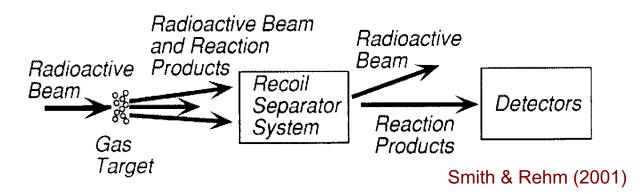
V. Margerin et al. Physics Letters B 731 (2014) 358–361 ; V. Margerin, PhD Thesis (U. Edinburgh)

RADIATIVE CAPTURE

1. <u>heavy recoil detection</u> $X(p,\gamma)Y$ among the most common reactions in nuclear astrophysics

 $\begin{array}{ll} \mbox{inverse kinematics} & \Rightarrow \mbox{ forward peaked emission ($\theta ~ 1^{\circ}$)} \\ & \Rightarrow \mbox{ detection efficiency ~ 100\%} \end{array}$

BUT: high suppression factors required (10¹⁰-10¹⁵)



2. <u> γ -ray detection</u> low efficiency $\Rightarrow ~ 4\pi$ coverage needed

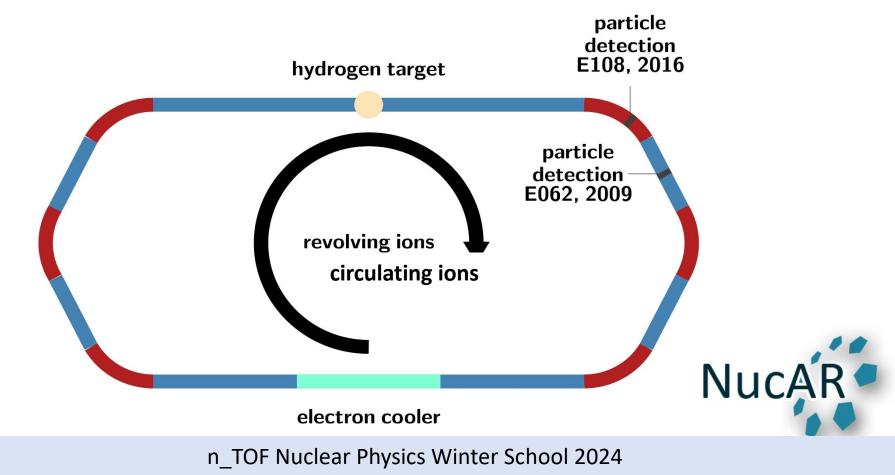
 $\gamma\text{-ray}$ background induced by $\beta^{\scriptscriptstyle +}$ beam decay

3. **delayed decay measurement** for example: ¹⁹Ne(p, γ)²⁰Na(β ⁺)²⁰Ne^{*}(α)¹⁶O

REACTION MEASUREMENTS AT ION STORAGE RINGS

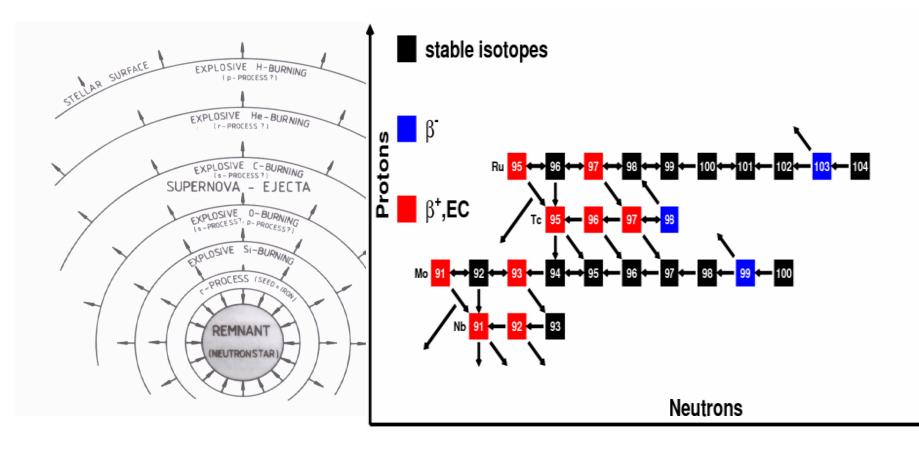
Advantages of using inverse kinematics in storage rings:

- 1. Heavy isotope can be radioactive or stable
- 2. Gas/jet target and beam species are pure

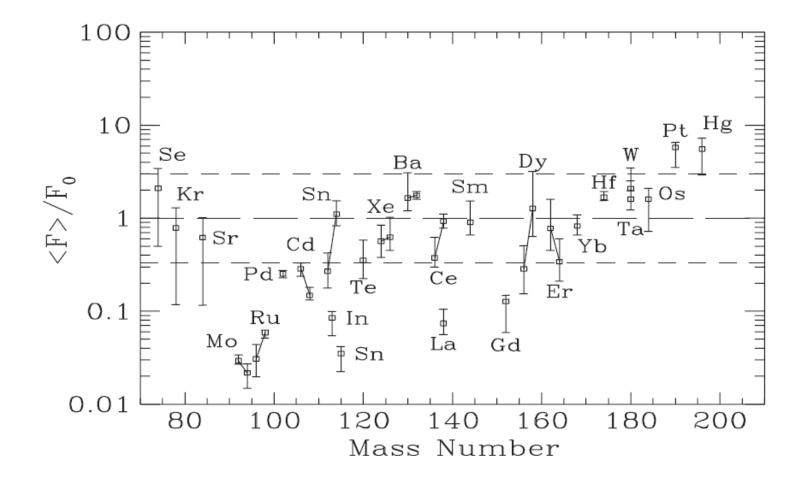


Puzzle of the origin of certain highly abundant p-nuclei

eg ^{92,94}Mo and ⁹⁶Ru

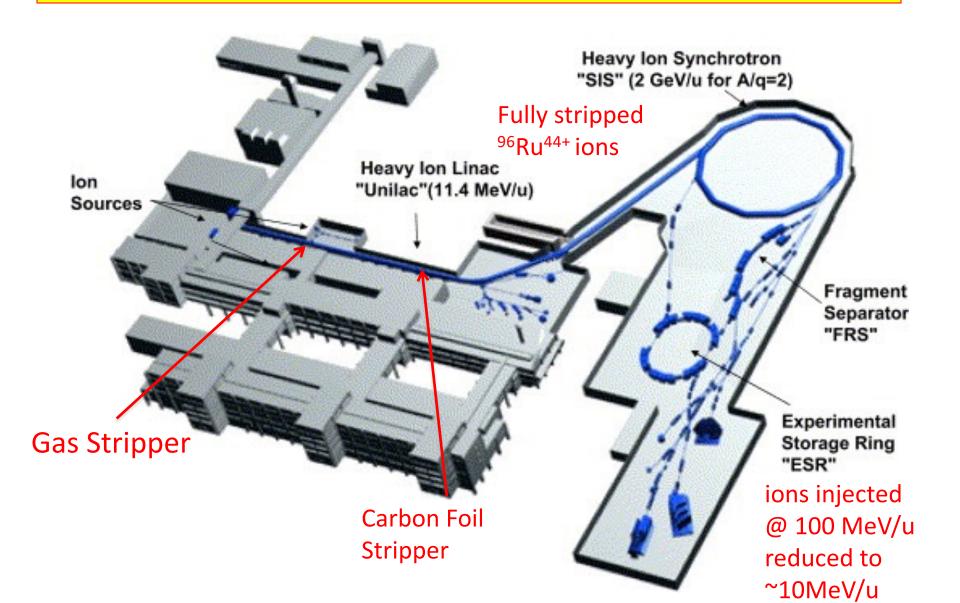


Predicted p-process abundances compared to observations

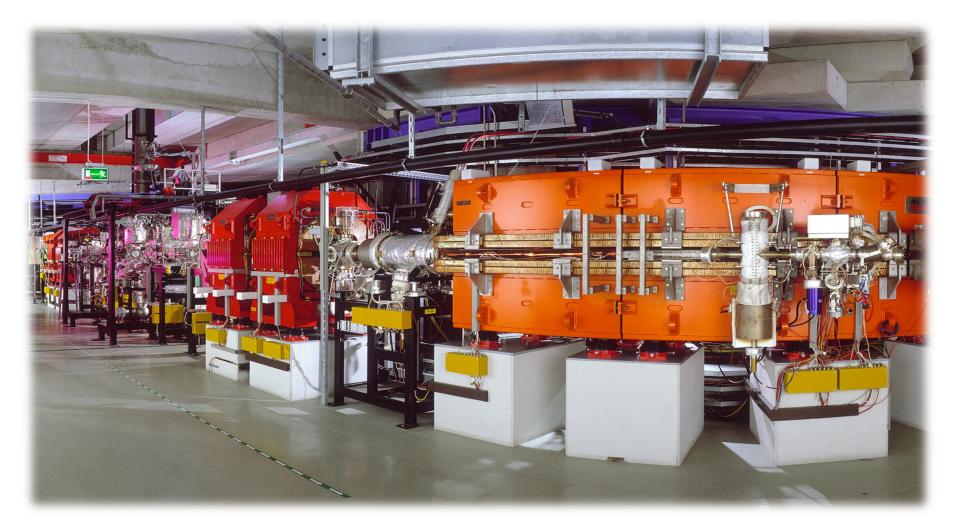


Arnould & Goriely Phys. Rep. 384,1 (2003)

Study of ⁹⁶Ru(p,γ)⁹⁷Rh reaction with decelerated beams using the ESR storage ring at GSI

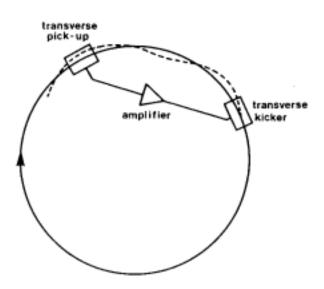


Ions cooled and decelerated to ~10 MeV/u in ESR



Stochastic Cooling

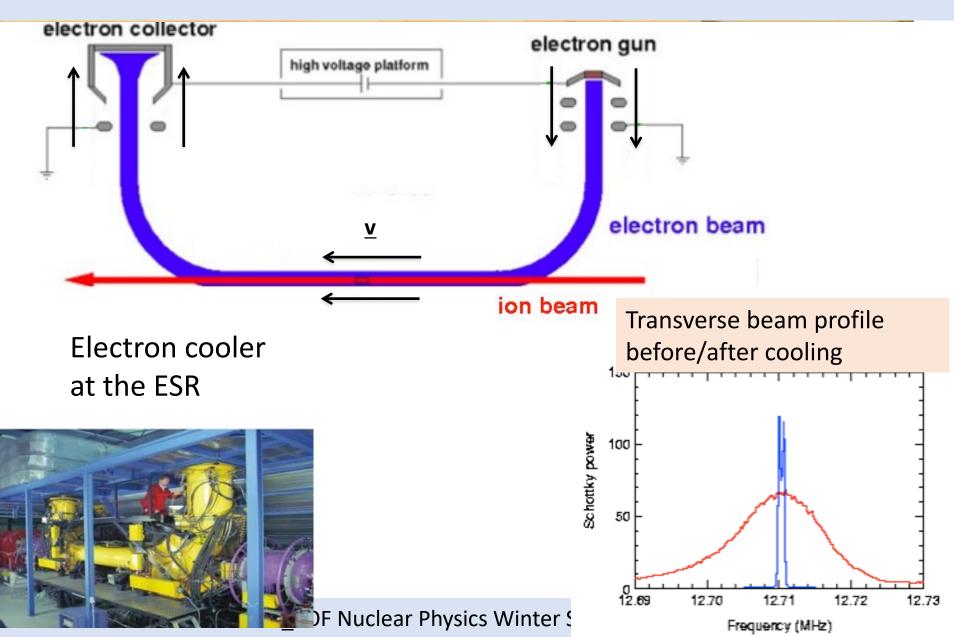
- Used for fast pre-cooling of hot fragment beams.
- Simon Van der Meer shared Nobel prize with Carlo Rubbia (1984).



Demonstration of Stochastic cooling for a single ion.

Taken from Simon Van der Meer Nobel prize lecture, 1984

Electron Cooling of the Beam

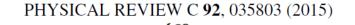




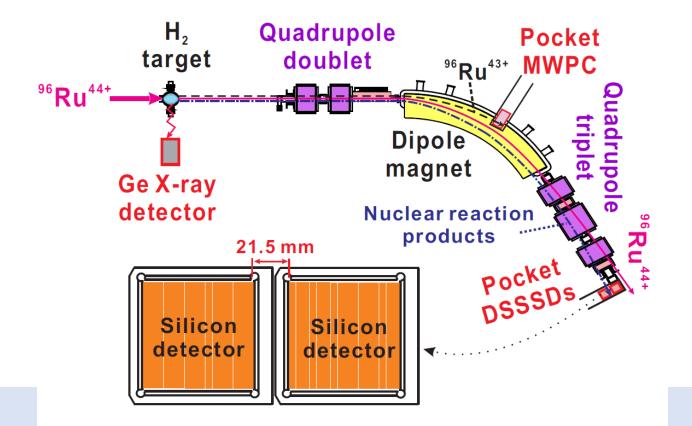
search and discovery

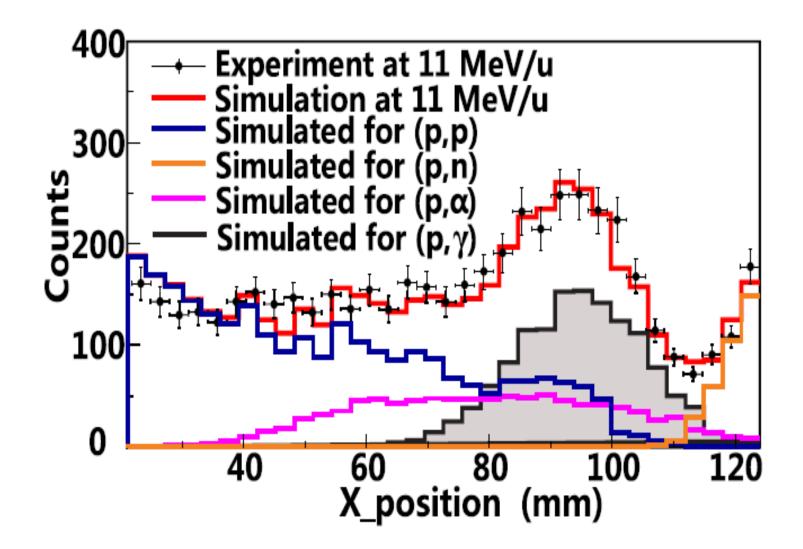
Physics Today 68, 11, 12 (2015)

Particle storage ring enables a role reversal in proton capture



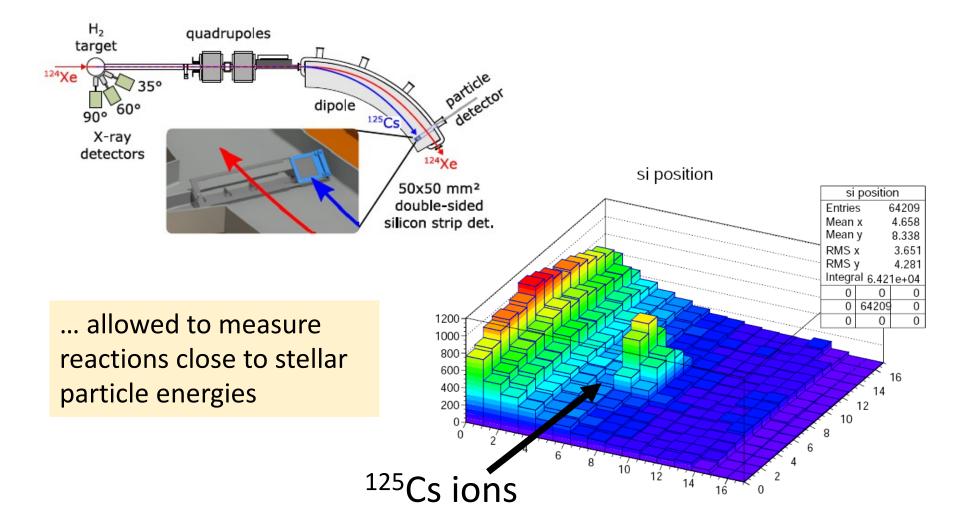
First measurement of the 96 Ru (p,γ) Rh cross section for the p process with a storage ring





¹²⁴Xe(p,γ)¹²⁵Cs particle detectors in Ultra High Vacuum

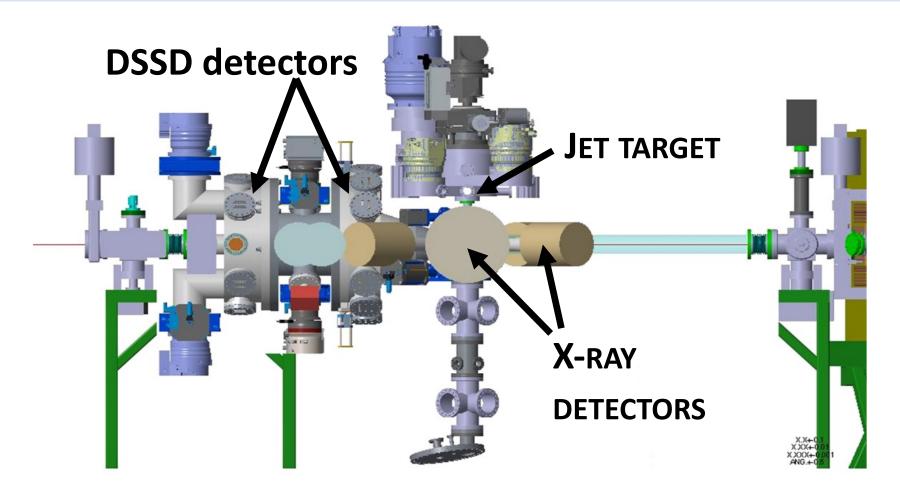
J. Glorius et al., Phys. Rev. Lett. 122, 092701 (2019)



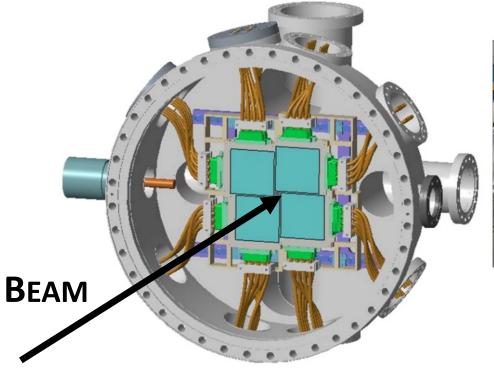
Measurements at Stellar Energies

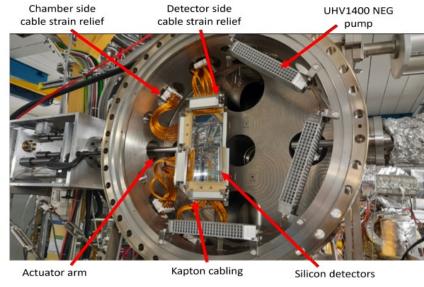


NUCLEAR ASTROPHYSICAL REACTION STUDIES USING THE CRYRING ARRAY FOR REACTION MEASUREMENTS (CARME)



C. Bruno et al., NIMA <u>Volume 1048</u>, (2023), 168007 J. Marsh, PhD Thesis (U. Edinburgh 2023)





J. Marsh, PhD Thesis (U. Edinburgh 2023)

This system will be used for **high resolution** charge particle reaction studies for nuclear astrophysics including:

- I. Direct astrophysical reaction measurements e.g. $(p,\alpha),(\alpha,p)$
- II. Indirect reactions probing key resonance properties e.g. (d,p)

First nuclear astro measurement scheduled for Feb 2023 (Ultra-high resolution study of the ${}^{15}O(\alpha,\alpha){}^{15}O$, PIs Bruno & Woods)

Reactions with Neutron Beams

FEATURES \Rightarrow no Coulomb barrier

⇒ neutrons to not lose energy in target – either transmitted or absorbed/scattered

$\frac{CHALLENGES}{reaction partners} \implies free neutrons unstable, hence stable or long-lived$

- \Rightarrow neutron energy cannot be 'tuned' in accelerator
- \Rightarrow background from scattered neutrons

<u>**REQUIREMENTS</u> \Rightarrow Intense neutron source**</u>

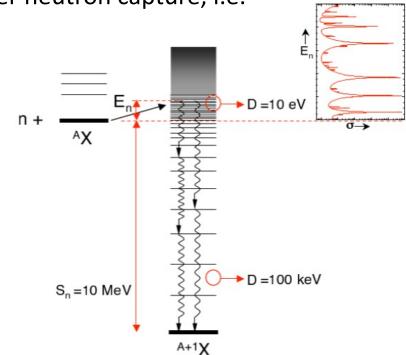
 \Rightarrow 'white' neutron spectrum or spectrum with the

'right' energy for the application

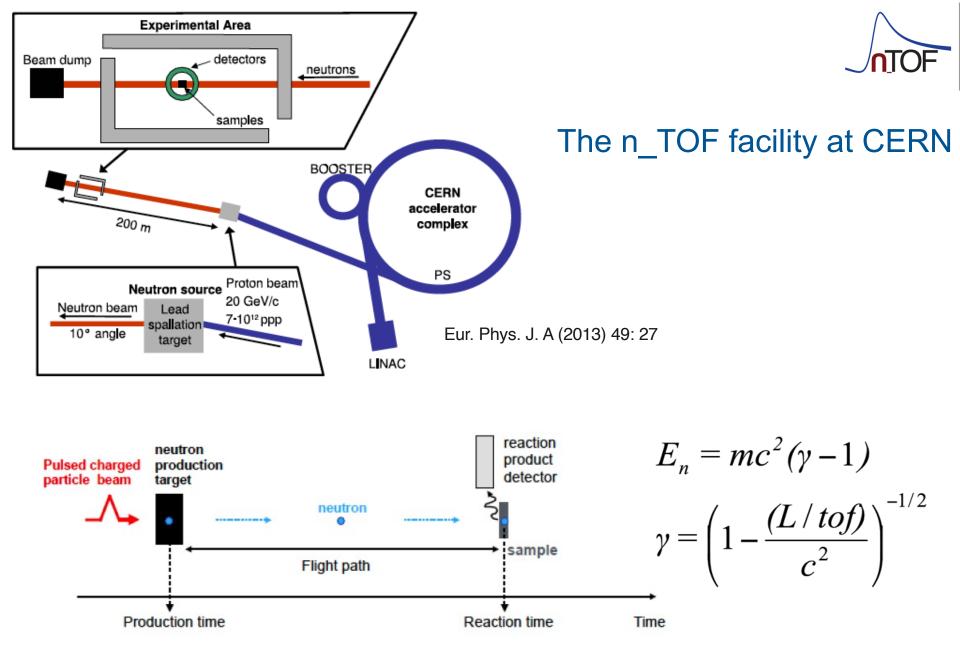
 \Rightarrow detection system insensitive to neutrons

Time-of-Flight technique

- applicable to all stable and long-lived nuclei
- need <u>pulsed neutron source</u> for E_n determination via ToF
- measurement of prompt emission after neutron capture, i.e.
 prompt γ-rays or p,α, etc
- measurement of resonance properties
- main background: neutrons scattered from the target: → need γ-ray detectors insensitive to neutron reaction



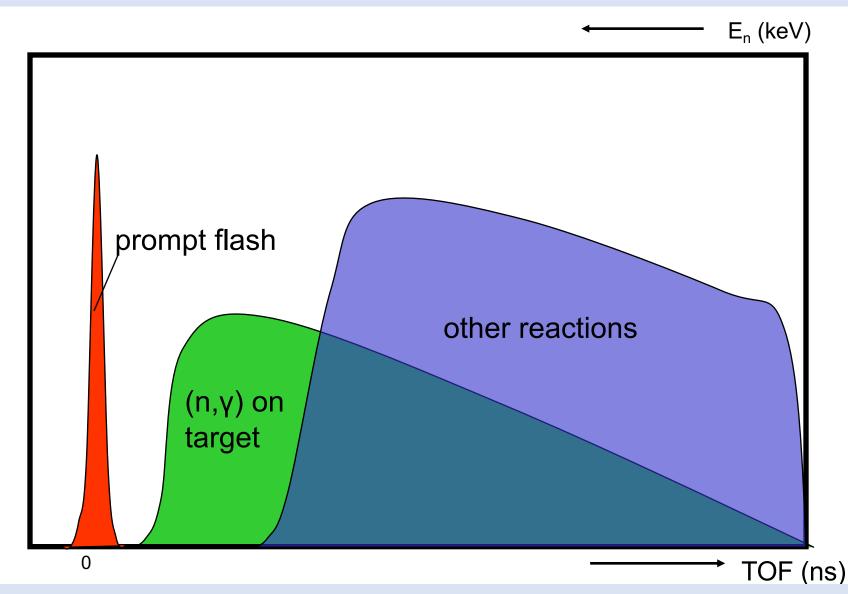
compound neutron capture reaction



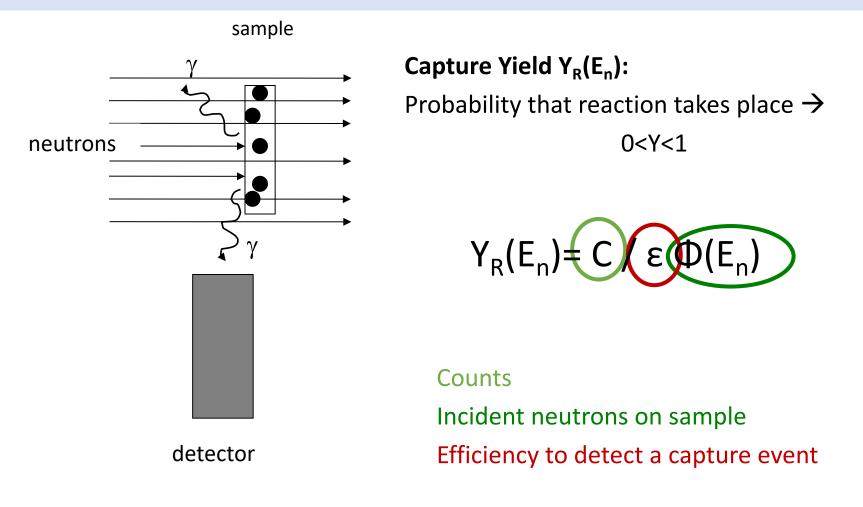
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46

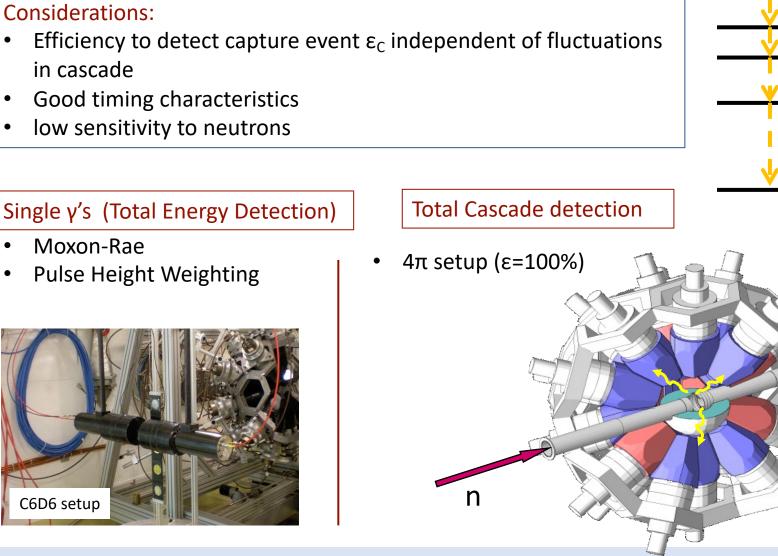
Schematic TOF Spectrum



Radiative Neutron Capture Yield



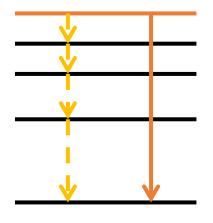
 γ -ray Detection



n_TOF Nuclear Physics Winter School 2024

BaF₂ array

Total Energy Detection



For γ -detection efficiency ε_{γ} proportional to γ -ray energy E_{γ} and small detection efficiency the cascade efficiency ε_{c} is proportional to the excitation energy E_{c} of the nucleus:

$$\varepsilon_{\gamma} = kE_{\gamma} \implies \varepsilon_{c} = 1 - \prod_{i} \left[(1 - \varepsilon_{\gamma,i}) \right]$$
$$\implies \varepsilon_{C} \approx \sum_{i} \varepsilon_{\gamma,i} = \sum_{i} k E_{\gamma,i} = kE_{c}$$

1) Design detector with $\varepsilon_{\gamma} = kE_{\gamma}$ (Moxon-Rae Detectors)

2) Manipulate signals a posteriori to achieve proportionality (Pulse Height Weighting Technique)

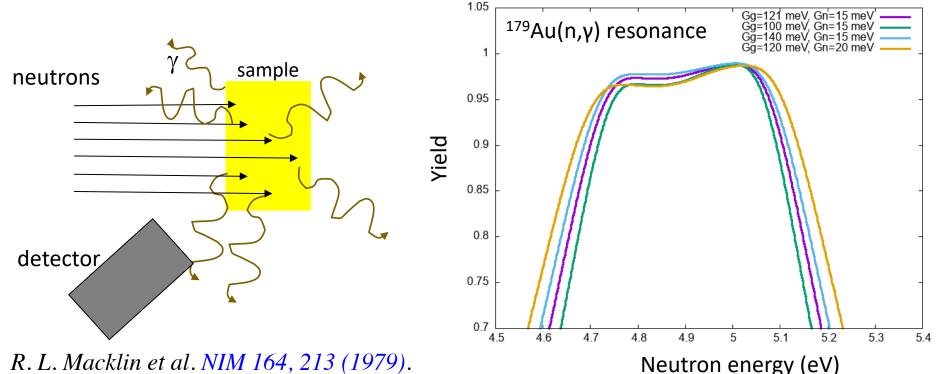
R. L. Macklin and R. H. Gibbons, Phys. Rev. 159, 1007 (1967). *U. Abbondanno and the n_TOF Collaboration, NIM A* 521, 454 (2004).

Neutrons incident on sample - Neutron flux φ

Determination of $\Phi(E_n)$ using a reaction(s) with a well known cross section.

In some cases, Φ at a particular energy can be determined with high accuray using the **Saturated Resonance technique:**

- \rightarrow Find resonance with capture >> scattering and large cross section
- ightarrow make target thick enough so no neutron is transmitted
- ightarrow Close to 100% of neutrons react and cause a gamma cascade



Neutron Capture Resonances

for a single isolated resonance:

resonant cross section given by Breit-Wigner expression

 $\sigma(E) = \pi \lambda^2 \frac{2J+1}{(2J_n+1)(2J_T+1)} \frac{\Gamma_{\gamma} \Gamma_n}{(E-E_R)^2 + (\Gamma_{TOT}/2)^2}$ geometrical factor strongly energy-dependent term $\propto 1/E$ Γ_n = partial width for decay via emission of neutron spin factor g = probability of compound formation via neutron J = spin of Resonance Γ_{v} = partial width for decay via emission γ -ray J_n = spin of neutron (1/2) = probability of compound decay via y-emission J_{T} = spin of target Γ = total width of compound's excited state $=\Gamma_n + \Gamma_{\gamma} + \dots$ E_{R} = resonance energy

Neutron Capture Resonances

Assuming
$$\sigma_{TOT} \sigma_{\gamma} + \sigma_n$$

$$\sigma_{n\gamma}(E) = \pi \lambda^2 g \frac{\Gamma_{\gamma} \Gamma_n}{(E - E_R)^2 + (\Gamma_{TOT}/2)^2}$$

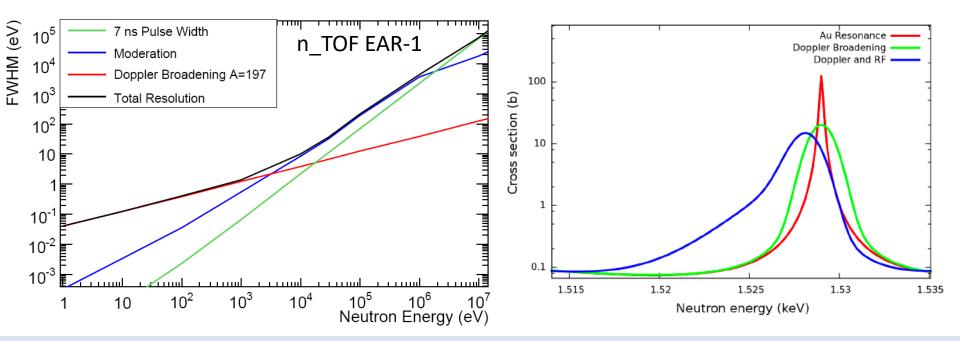
$$\sigma_{0\gamma} = \sigma(E_R) = \pi \lambda^2 g \frac{\Gamma_{\gamma} \Gamma_n}{(\Gamma_{TOT}/2)^2} = \sigma_0 \frac{\Gamma_{\gamma}}{\Gamma_{TOT}}$$

$$\sigma_0 = \sigma_{TOT}(E_R) = 4\pi \lambda^2 g \frac{\Gamma_n}{\Gamma_{TOT}}$$

Very good resolution: all resonance parameters (E_R , J, Γ_γ , Γ_n) from capture and total cross section measurement

Resolution Broadening

- Pulse width
- Neutron production target + moderator
- Doppler broadening
- flight path length
- Data acquisition



Area Analysis

However $\Gamma_{exp} >> \Gamma_{nat}$ in most cases \rightarrow Analysis yields the **Resonance Area**

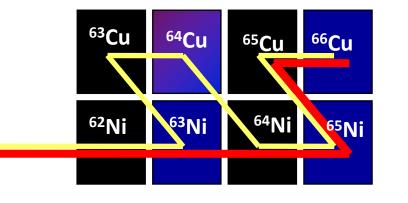
$$A_{capture} \propto ng\Gamma_{\gamma}\Gamma_{n}/\Gamma_{TOT}$$

Can extract resonance parameters when combined with transmission measurement with a thin and thick sample:

$$A_{transmission,thick} \propto \sqrt{ng\Gamma_n\Gamma_{TOT}}$$

 $A_{transmission,thin} \propto ng\Gamma_n$

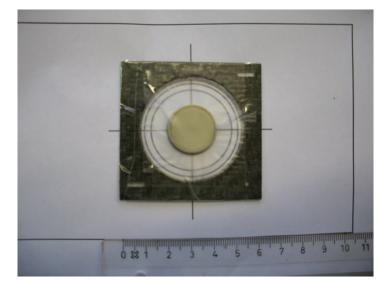
thin... T~1 thick... T~0 n... areal density

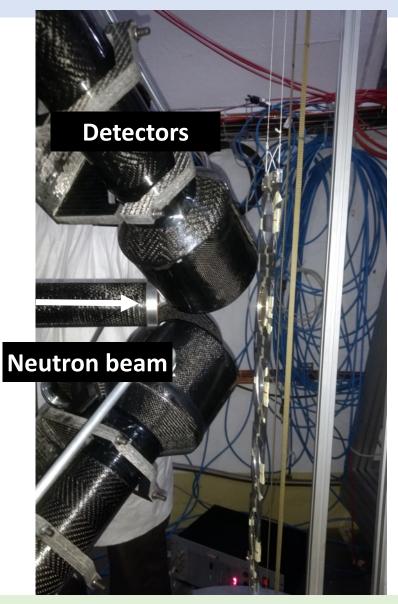


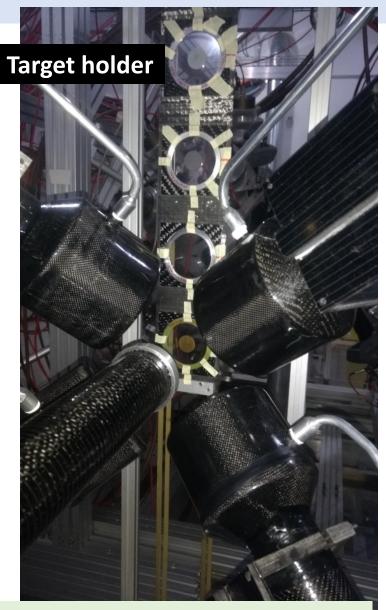
Measurement of ⁶²Ni(n,γ) and branching point ⁶³Ni(n,γ) at stellar energies at n_TOF

⁶³Ni is **radioactive** $(t_{1/2} \sim 100 \text{ y}) \rightarrow$ need to produce a radioactive target

- irradiation of ⁶²Ni at ILL thermal reactor (high cross sections and neutron flux)
- chemical separation of contaminantsat
 PSI (other elements)
- \rightarrow resulting target: ~100 mg ⁶³Ni, 900 mg ⁶²Ni

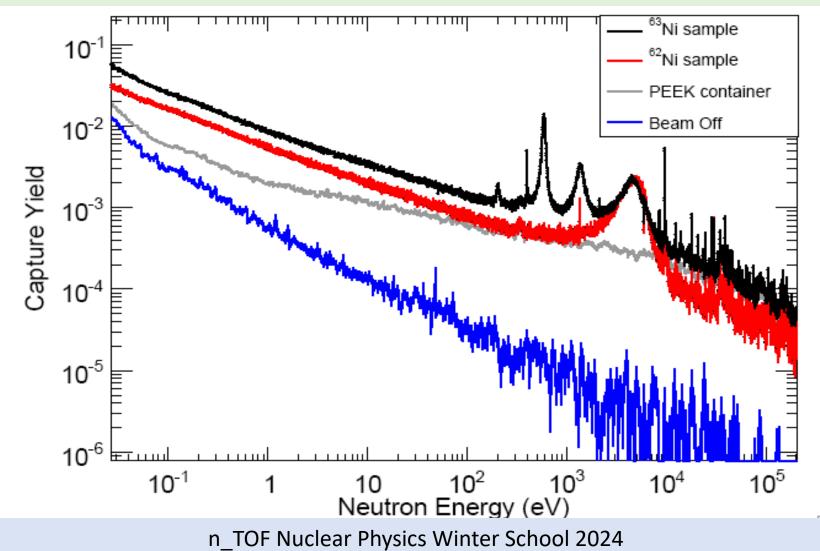


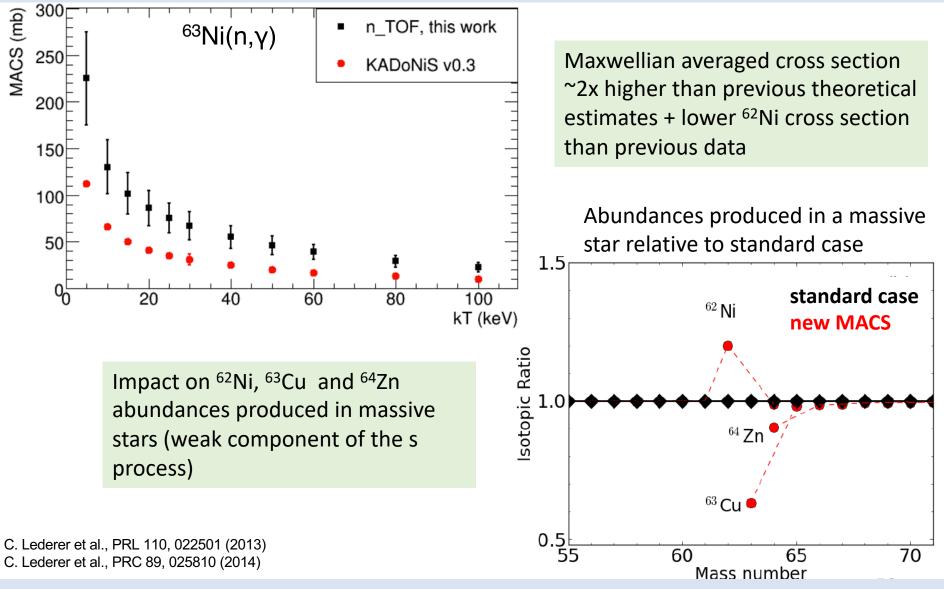


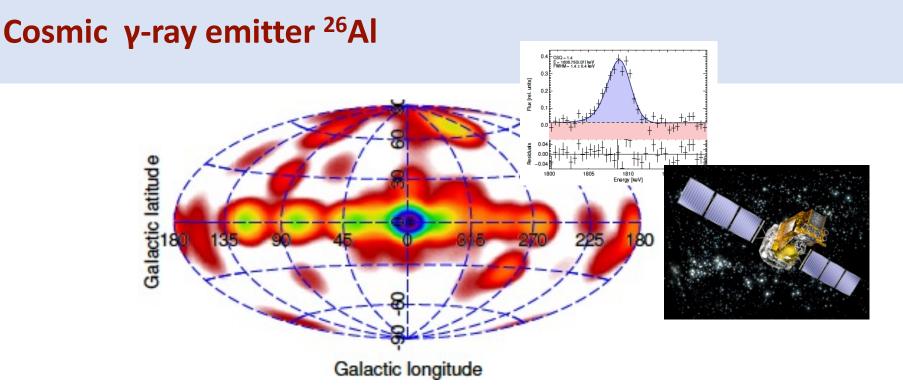


Setup for prompt y-ray detection using scintillation detectors with low neutron sensitivity

Typical neutron time-of-flight spectrum: neutron energy resolution $\Delta E/E^{-3}$ at 1 keV \rightarrow can access individual states for high A







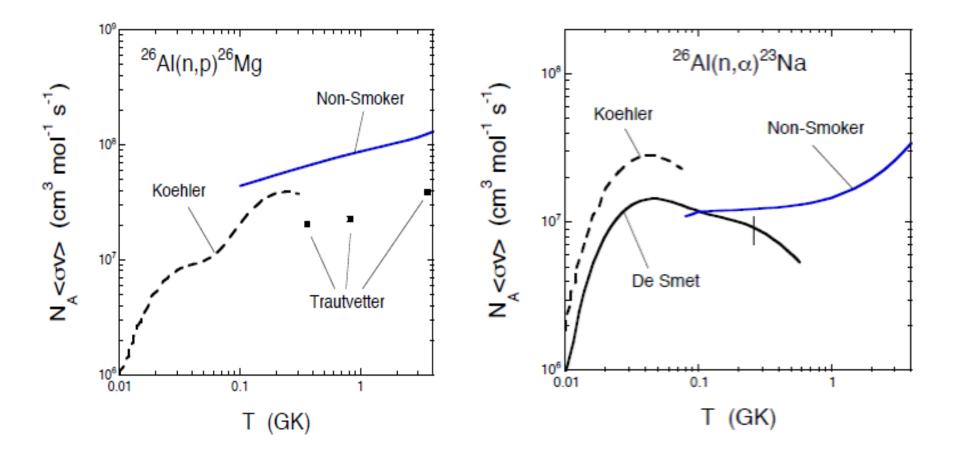
Main Origin of ²⁶Al in massive stars (Diehl et al, Nature 439 (2006))

Mainly produced in

- convective hydrogen burning in Wolf-Rayet stars followed by ejection by stellar wind
- convective Carbon shell burning followed by ejection from core collapse supernova
- explosive Ne/C burning in core collapse phase of supernova

Key uncertainties for theoretical predictions of abundances: ²⁶Al(n,p) and ²⁶Al(n,a) reaction rates [Iliadis et al., Astrophys. J. Supp. 193, 16 (2011)]

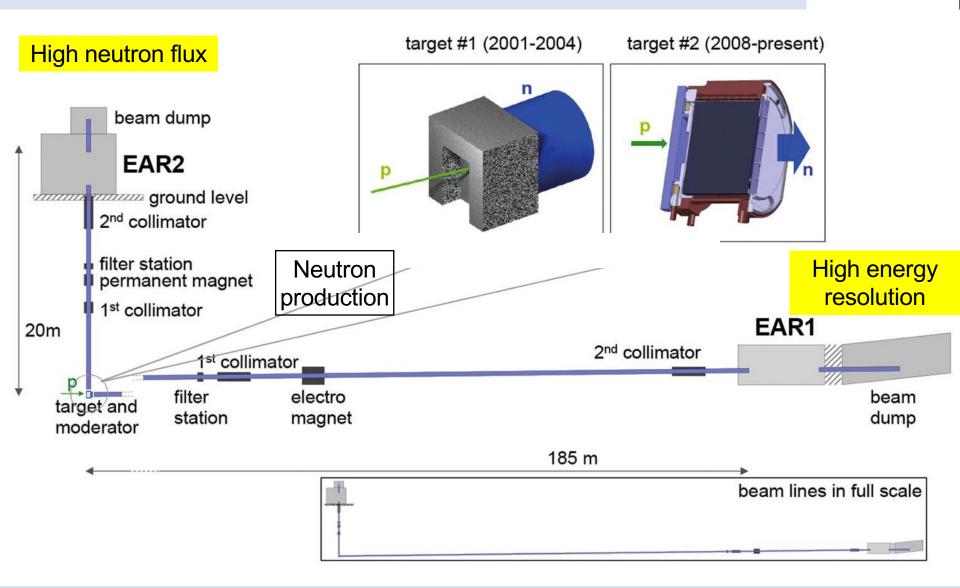
²⁶Al +n reactivities from previous measurements



C Iliadis et al., Ast. J. Supp. 193, 16 (2011)

n_TOF EAR-2





²⁶Al(n,p) and ²⁶Al(n,α)

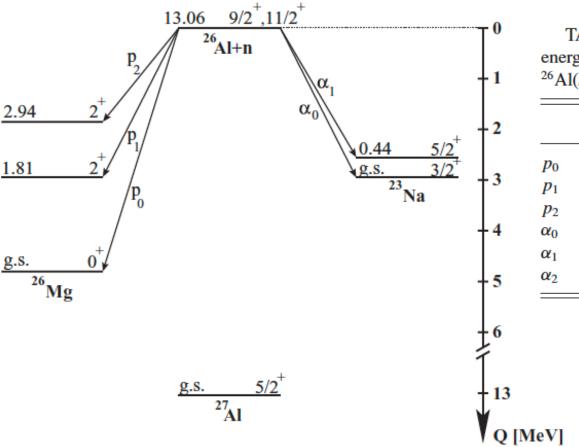


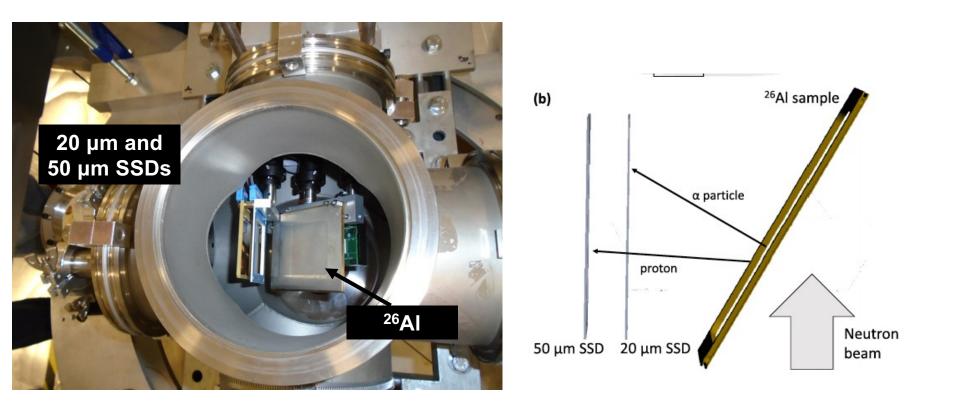
TABLE I. Q values and corresponding ejectile energies for the possible ${}^{26}\text{Al}(n, \alpha_i){}^{23}\text{Na}$ and ${}^{26}\text{Al}(n, p_i){}^{26}\text{Mg}$ reactions.

	Q value (MeV)	E (MeV)
p_0	4.78	4.60
p_1	2.98	2.87
p_2	1.85	1.78
α_0	2.97	2.53
α_1	2.53	2.16
α_2	0.89	0.76

de SMET et al PHYSICAL REVIEW C 76, 045804 (2007)

Silicon Strip Detection Setup: ΔE - E Technique

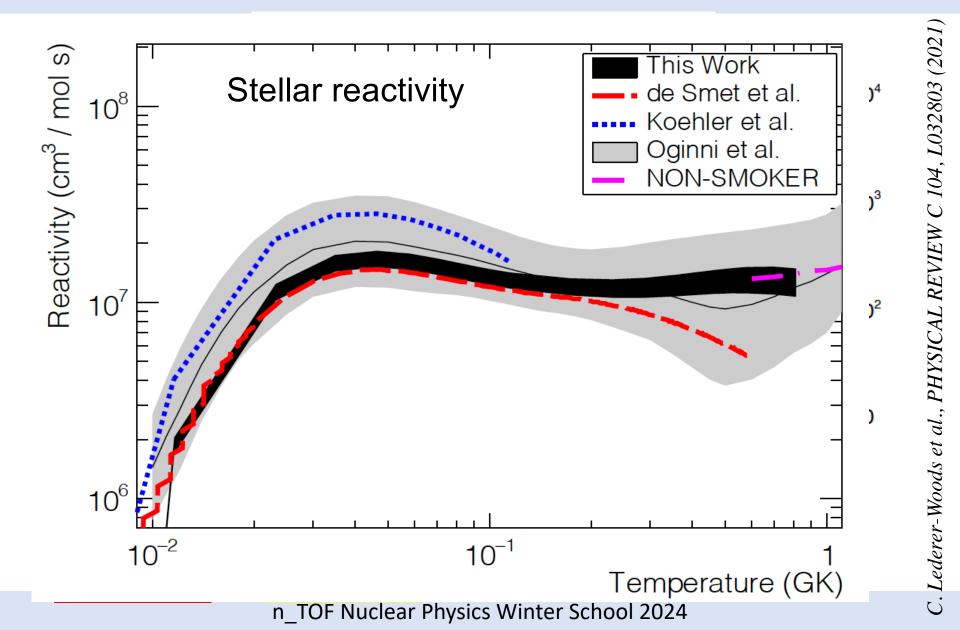




²⁶Al Target (JRC GELINA): 2.6 10¹⁷ atoms

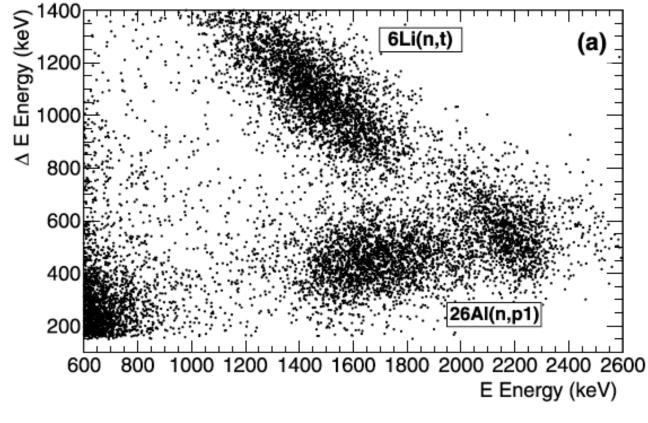
²⁶Al(n, α) measured at n_TOF / GELINA





ΔE – E Spectra



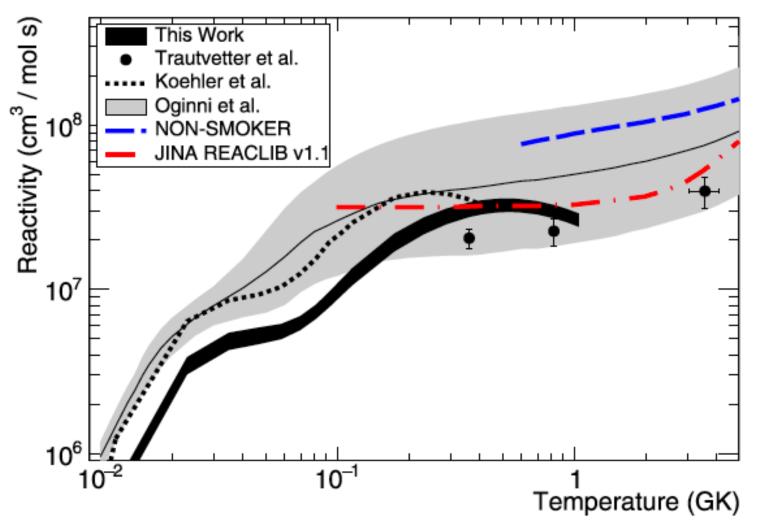


Thick Detector

n_TOF Nuclear Physics Winter School 2024

Thin Detector



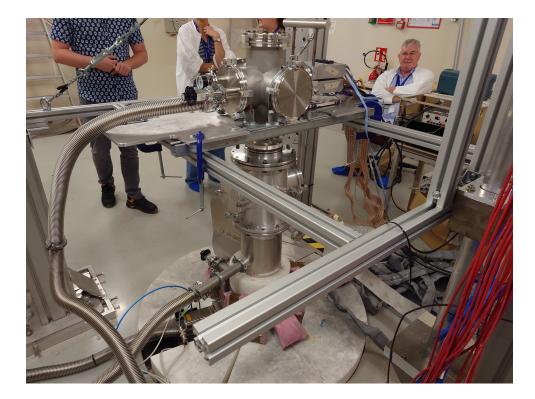


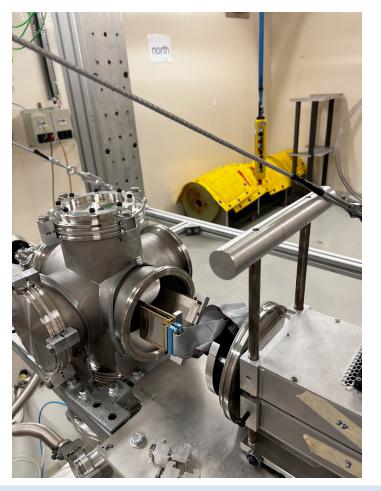
C. Lederer-Woods et al., PHYSICAL REVIEW C 104, L022803 (2021)

New Run at for high neutron energy 2023



... taking advantage of higher flux which allows use of better collimated neutron beam





THE END