

μTRISTAN

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Based on 2201.06664, Yu Hamada (KEK), RK, Ryutaro Matsudo (KEK -> NTU), Hiromasa Takaura (KEK -> YITP), Mitsuhiro Yoshida (KEK)

2210.11083, Yu Hamada (KEK), RK, Ryutaro Matsudo (KEK -> NTU), Hiromasa Takaura (KEK -> YITP)

2304.14020, Kåre Fridell (KEK/Florida State U.), RK, Ryoto Takai (KEK/Sokendai)

Also, study in progress with Koji Nakamura (KEK), Sayuka Kita (Tsukuba U.), Toshiaki Kaji (Waseda U.), Taiki Yoshida (Waseda U.), Kohei Yorita (Waseda U.)

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Clearly, we need next generation colliders.

1. We must investigate **the form of the Higgs potential** by the observation of self-interactions.
2. We must check the possibility that one can actually produce **dark matter** artificially.
3. We must look for **new physics** at least up to about 10TeV (~ a loop factor higher than the EW scale).

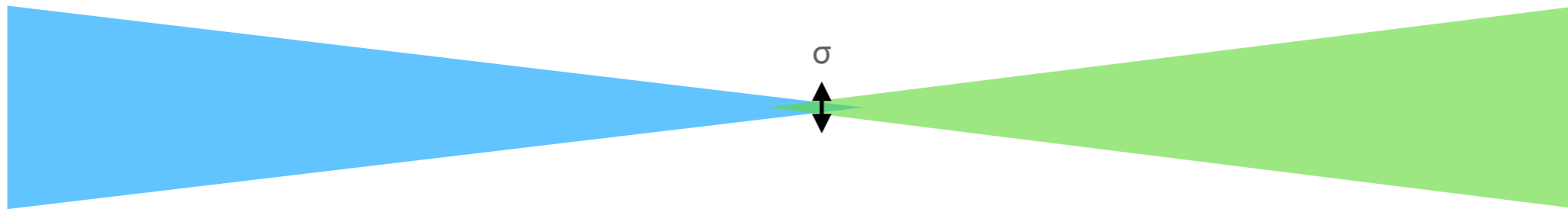
We cannot stop here.

Today, I talk about possibly a realistic scenario of μ^+ based colliders.

As you know, the most important (difficult) part of muon colliders is to obtain enough **luminosity** for particle physics.

Luminosity

$$\mathcal{L} = \frac{N_{\text{beam1}} N_{\text{beam2}}}{4\pi\sigma_x\sigma_y} f_{\text{rep}}$$



We need a large number of muons and/or narrow beams.

As a reference,

$N_{\text{beam}}=10^{10}$ (1.6nC) / bunch

$\sigma=1\mu\text{m}$

$f_{\text{rep}}=1\text{MHz}$



$\sim 8 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1} \sim 25 \text{ fb}^{-1}/\text{year}$

We want ab^{-1} level luminosity for physics
(HL-LHC, ILC)

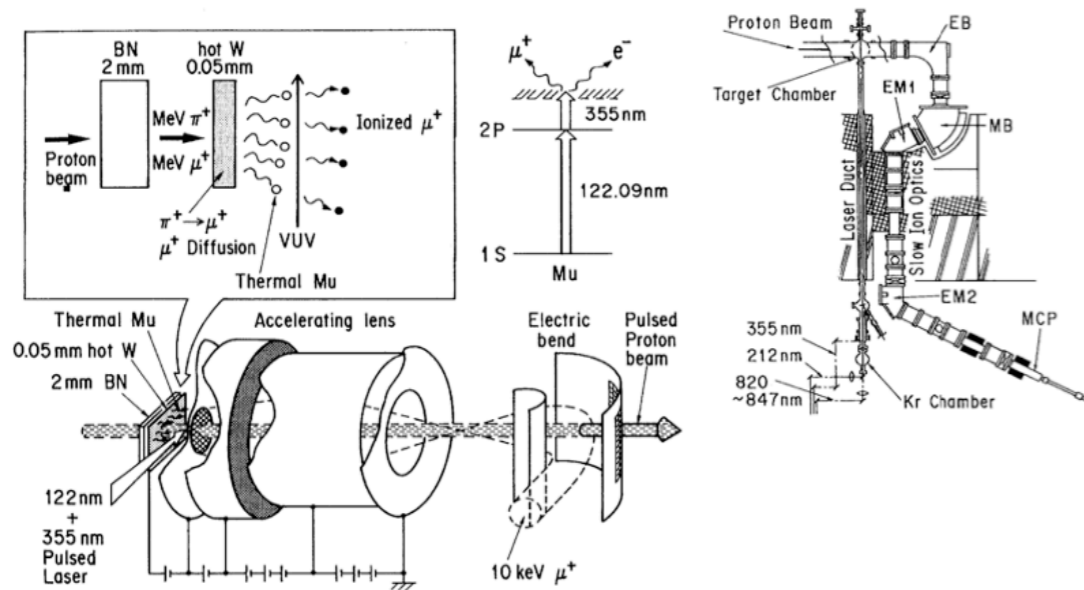
σ is the most difficult part. The **cooling** is the key.

Muon cooling

There is a rather mature(?) technology works for μ^+ .

Ultracold muon technology

[K.Nagamine et al. 1995]



This has been the key technology for the J-PARC muon g-2/EDM experiment.

ミュオンg-2/EDMと極冷ミュオンビーム

J-PARCで行う新しいミュオンg-2/EDM精密測定

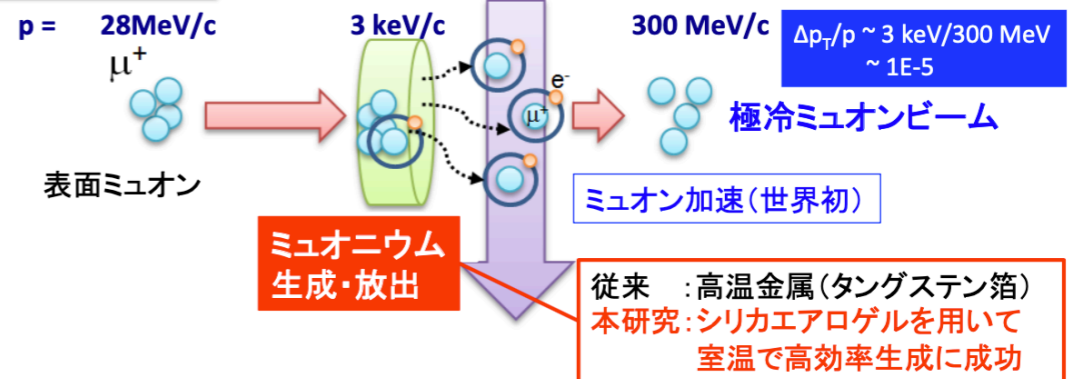
www.g-2.kek.jp

- BNLが報告した標準模型からのズレ(3 σ)の検証(0.1ppm)
- 全く新しいコンセプトで主要系統誤差要因を払拭
 - ゼロ電場
 - コンパクトな蓄積磁石(0.7 m \ll 14 m)
- 通常に比べてエミッタンスが1/1000程度小さいミュオンビーム (極冷ミュオンビーム)が必須

ミュオニウムMu (μ^+e^-)のレーザー共鳴イオン化

Nagamine et al. PRL 74 (1995)
P. Bakule et al. INM B266(2008)

Laser
122nm, 355nm

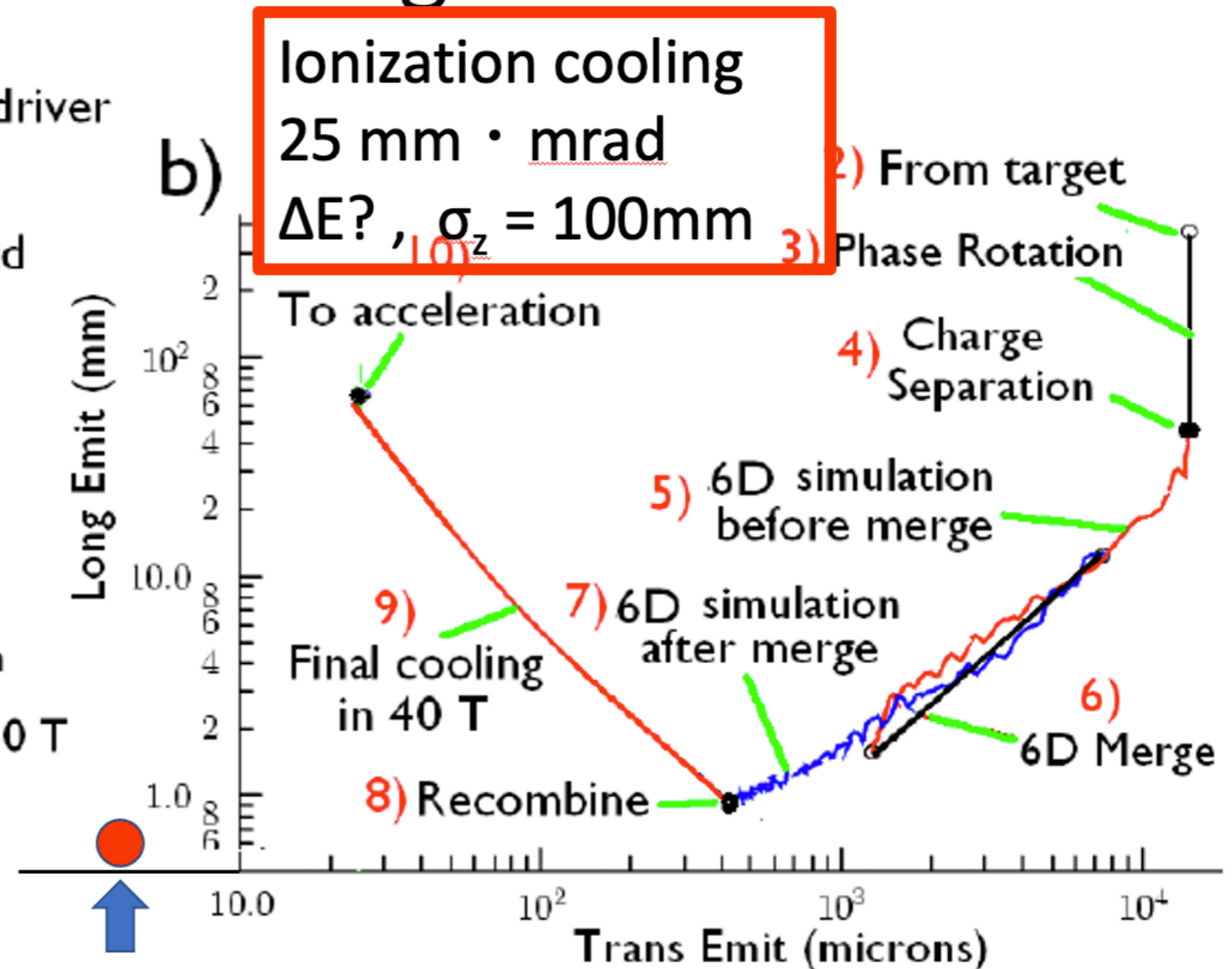
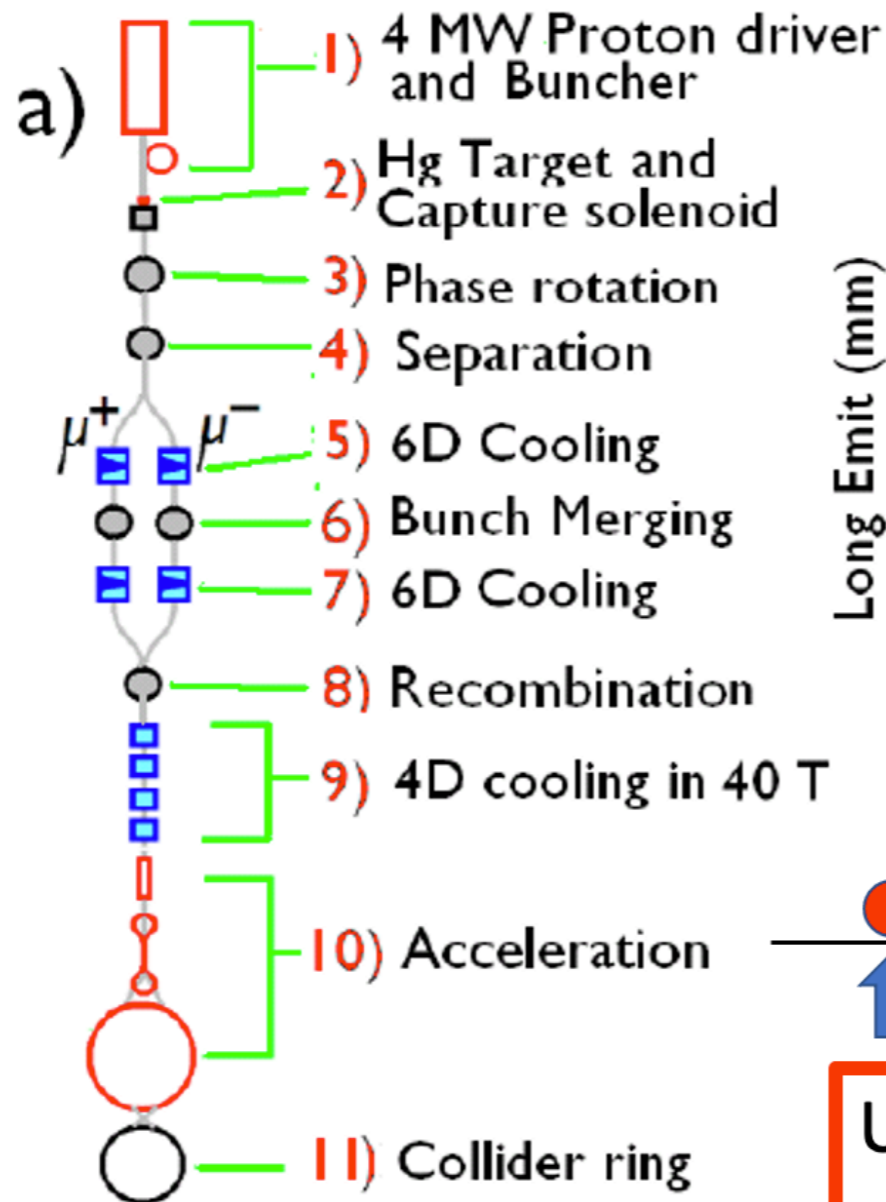


Looks like a low-emittance μ^+ beam is already there!

Mibe-san's slide

Also, polarized beam is possible. (non-trivial though)

Emittance : Ionization cooling vs Ultra Cold



Ultra Cold μ^+
 $< 5 \text{ mm} \cdot \text{mrad}$
 $\Delta E = 1 \text{ eV}$, $\sigma_z = 1 \text{ mm}$

μ TRISTAN

$\mu^+e^-/\mu^+\mu^+$ collider with 1 TeV μ^+ beam.

PTEP

Prog. Theor. Exp. Phys. **2022** 053B02(16 pages)
DOI: 10.1093/ptep/ptac059

30 GeV e^- / 1 TeV μ^+ : Higgs factory, $\sqrt{s}=346\text{ GeV}$
1 TeV μ^+ / 1 TeV μ^+ : new physics search, $\sqrt{s}=2\text{ TeV}$

μ TRISTAN

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The ultra-cold muon technology developed for the muon $g-2$ experiment provides a low-emittance μ^+ beam which can be accelerated and used for experiments. We consider the possibility of new collider experiments by μ^+ beam up to 1 TeV. Allowing the μ^+ beam to collide with a high-intensity TRISTAN energy, $E_{e^-} = 30\text{ GeV}$, in a storage ring with the same size as TRISTAN (circumference of 3 km), one can realize a collider experiment with the center-of-mass energy $\sqrt{s} = 346\text{ GeV}$, which allows the production of Higgs bosons through vector boson fusion processes. We estimate the deliverable luminosity with existing accelerator technology. $\mu^+\mu^+$ colliders up to $\sqrt{s} = 2\text{ TeV}$ are also possible using the same technology. $\mu^+\mu^+$ colliders up to $\sqrt{s} = 2\text{ TeV}$ are also possible using the same technology. $\mu^+\mu^+$ colliders up to $\sqrt{s} = 2\text{ TeV}$ are also possible using the same technology.

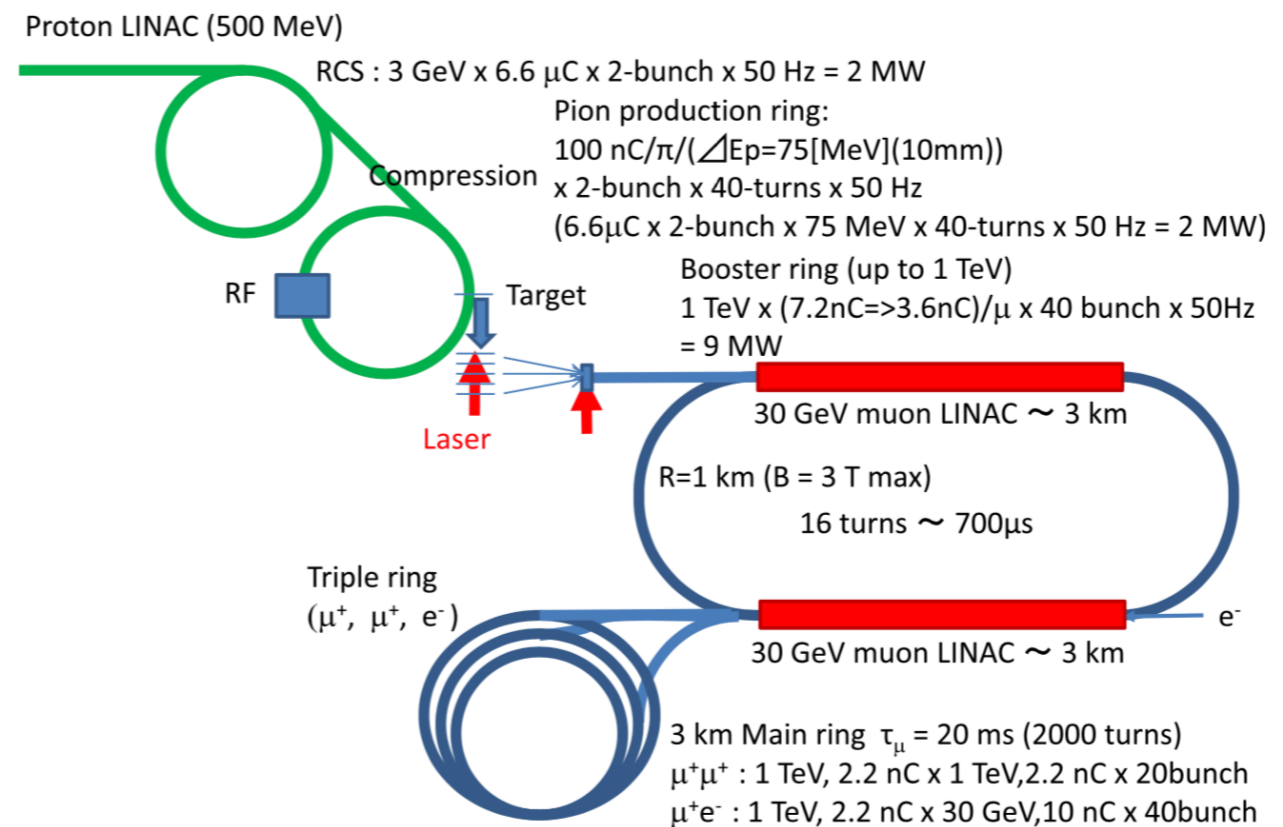


Fig. 1. Conceptual design of the $\mu^+e^-/\mu^+\mu^+$ collider.

How many cold muons?

1/(20ms) where 20ms is the lifetime of the 1TeV muon

J-PARC like proton driver: $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$ realistic

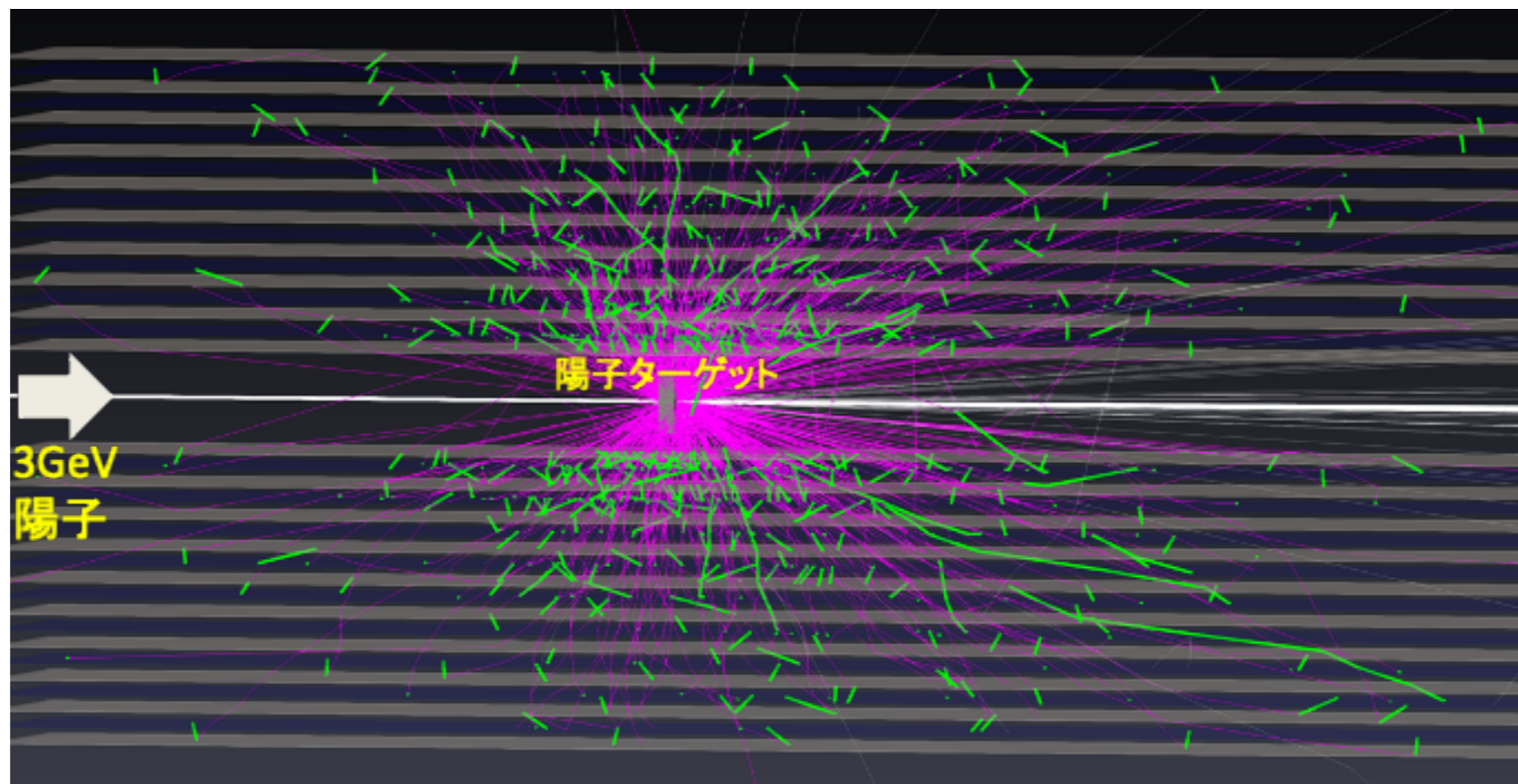
pion production target: 40 hits/bunch 0.016 π^+ /proton $2.6 \times 10^{15} \pi^+$ /s maybe realistic

pion stopping target: 0.5 stopping efficiency * 0.07 muons/ π^+ $9 \times 10^{13} \mu^+$ /s maybe challenging

10^5 larger than J-PARC MLF.

Super muon factory!

simulation: (in progress)



pink: pion
green: muon

Luminosity?

J-PARC like proton driver: $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$
 pion production target: 40 hits/bunch 0.016 π^+ /proton $2.6 \times 10^{15} \pi^+$ /s
 pion stopping target: 0.5 stopping efficiency * 0.07 muons/ π^+ $9 \times 10^{13} \mu^+$ /s

$6.6 \mu\text{C} \times 2 \times 0.016 \times 0.5 \times 0.07 \sim 7 \text{ nC} / \text{bunch} \sim 4 \times 10^{10} \text{ muons/bunch}$

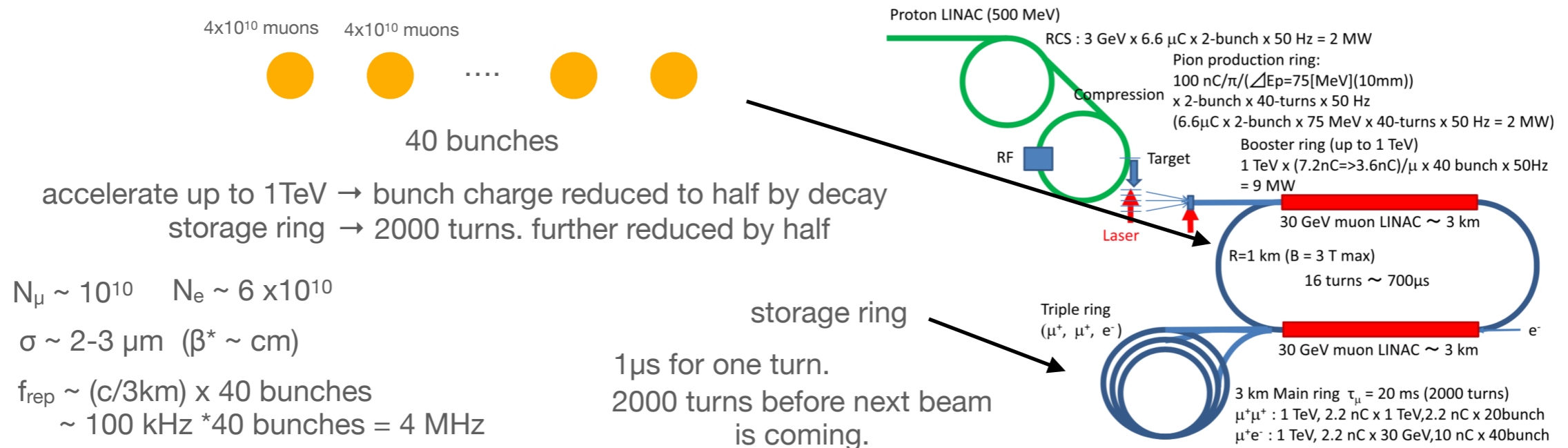
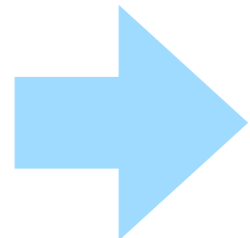


Fig. 1. Conceptual design of the $\mu^+e^-/\mu^+\mu^+$ collider.



$$\mathcal{L}_{\mu^+e^-} = 4.6 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}.$$

$$\mathcal{L}_{\mu^+\mu^+} = 5.7 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}.$$

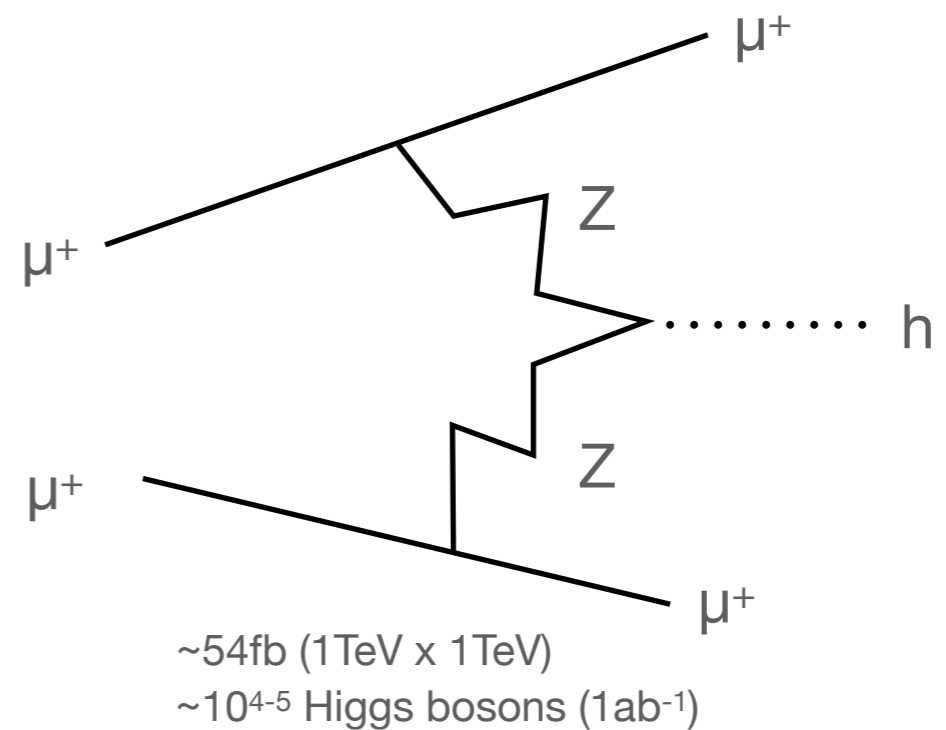
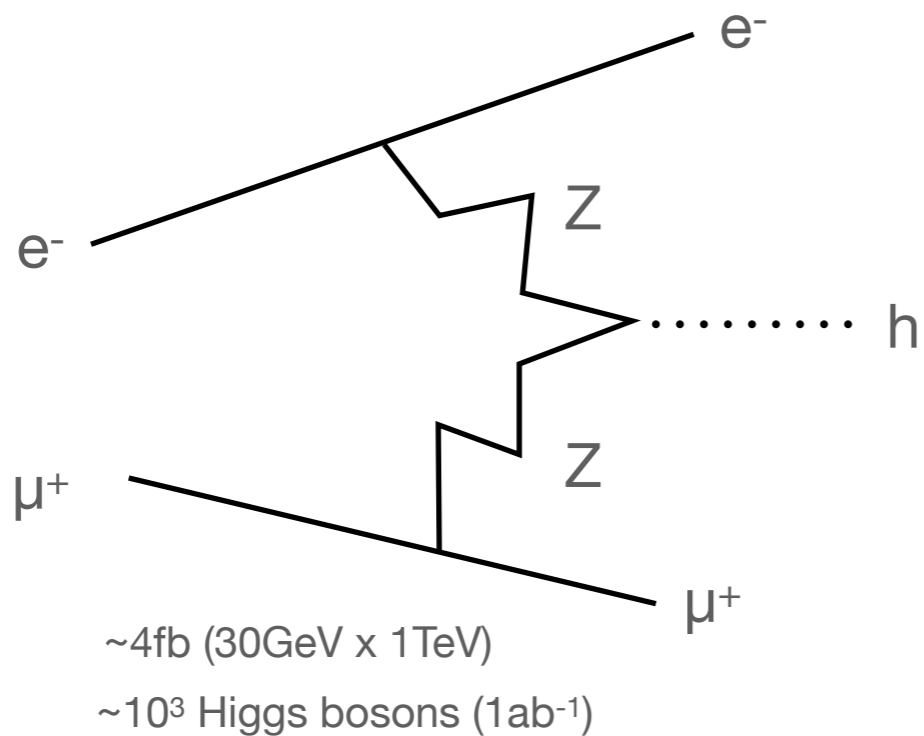
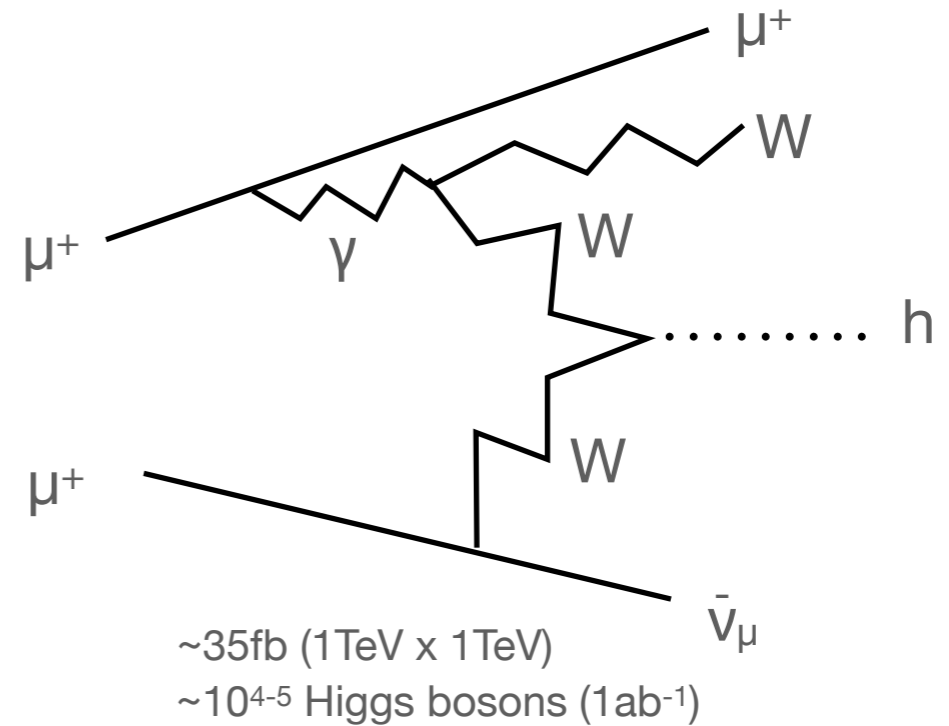
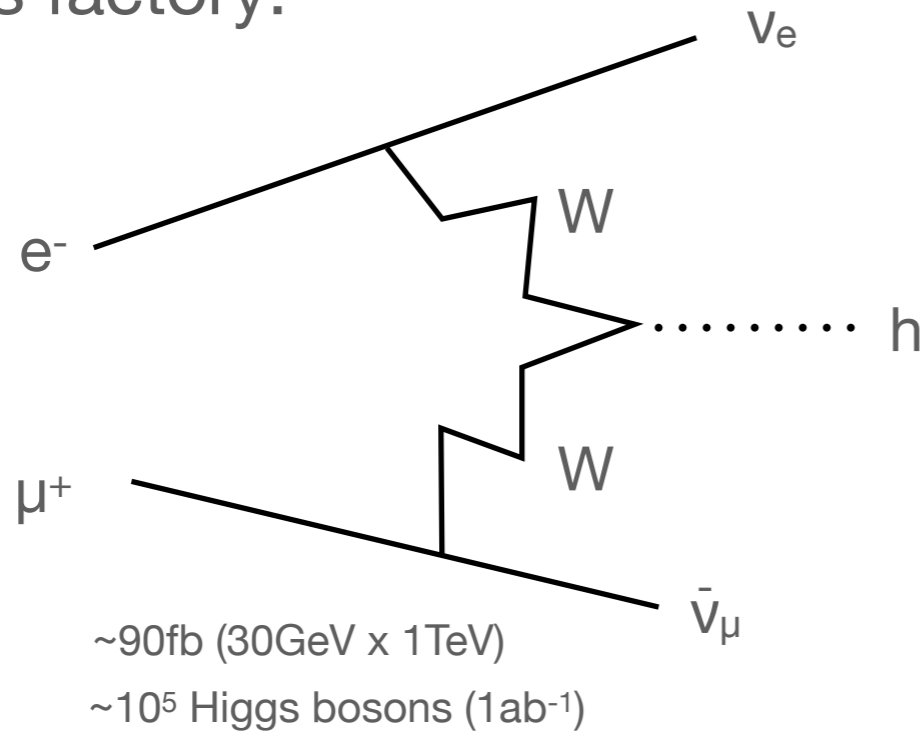
(β^* may be much smaller?)

ab^{-1} level for 10yrs running.

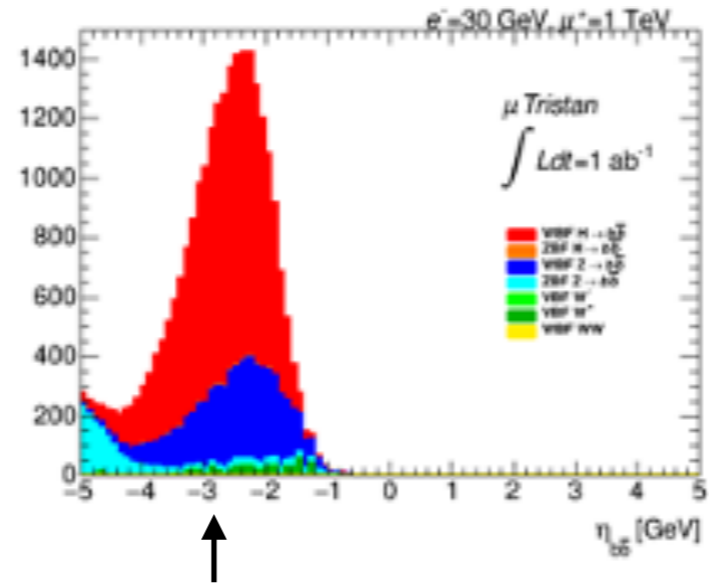
not bad.

What can we do at μ TRISTAN?

Higgs factory:

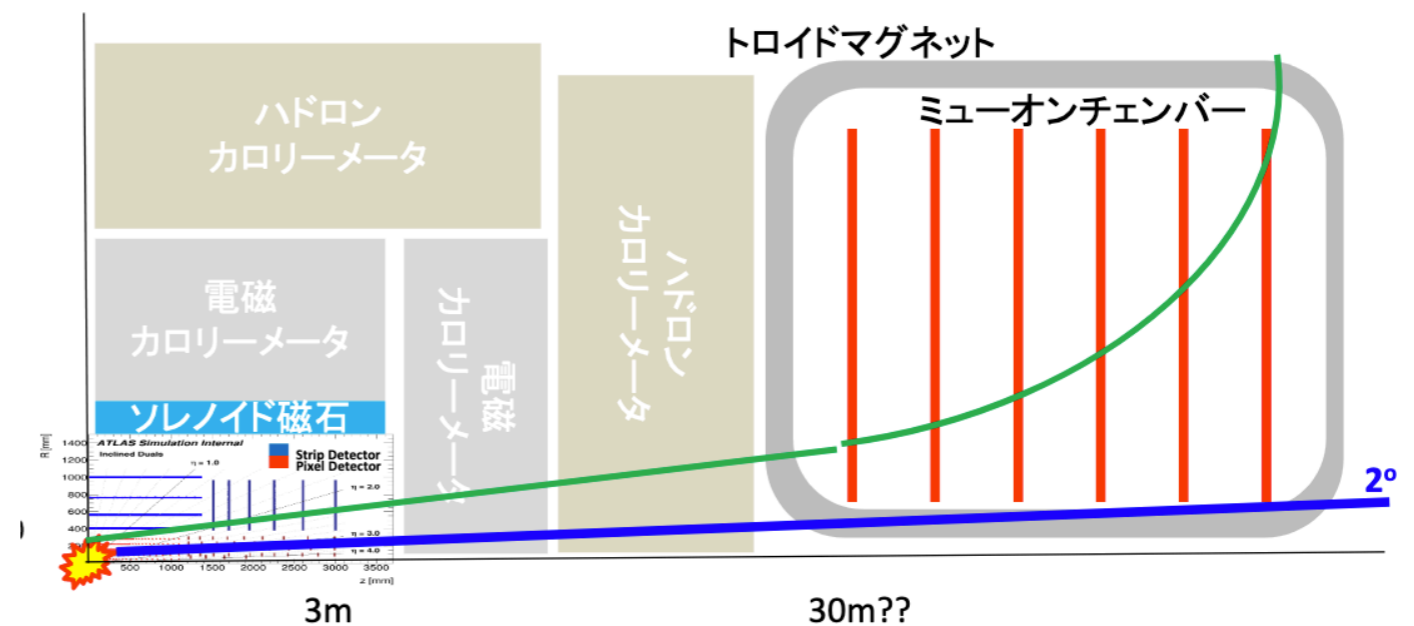
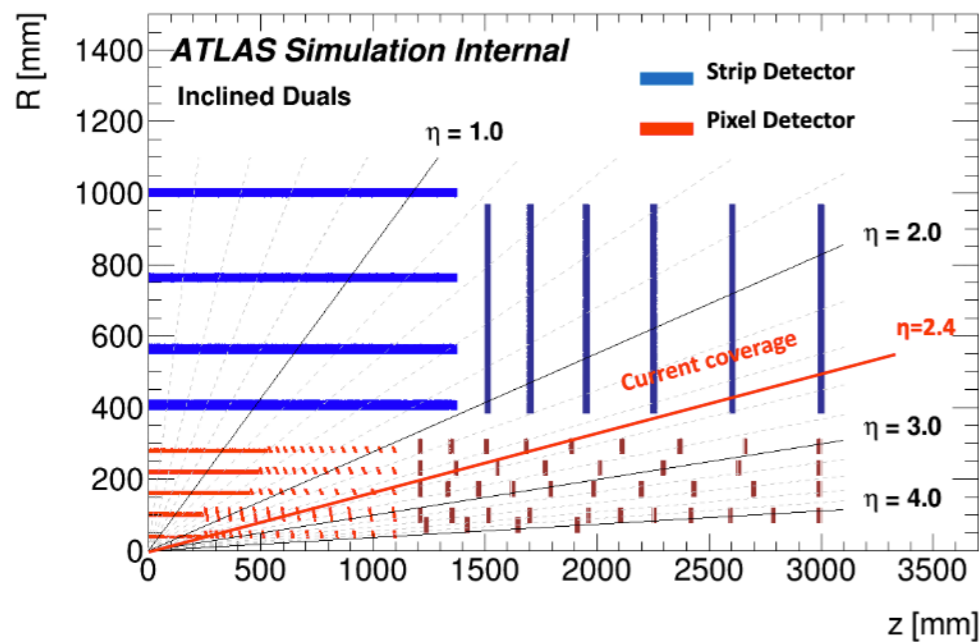


μ^+e^- : Very asymmetric



All the particles go to the direction of the muon.

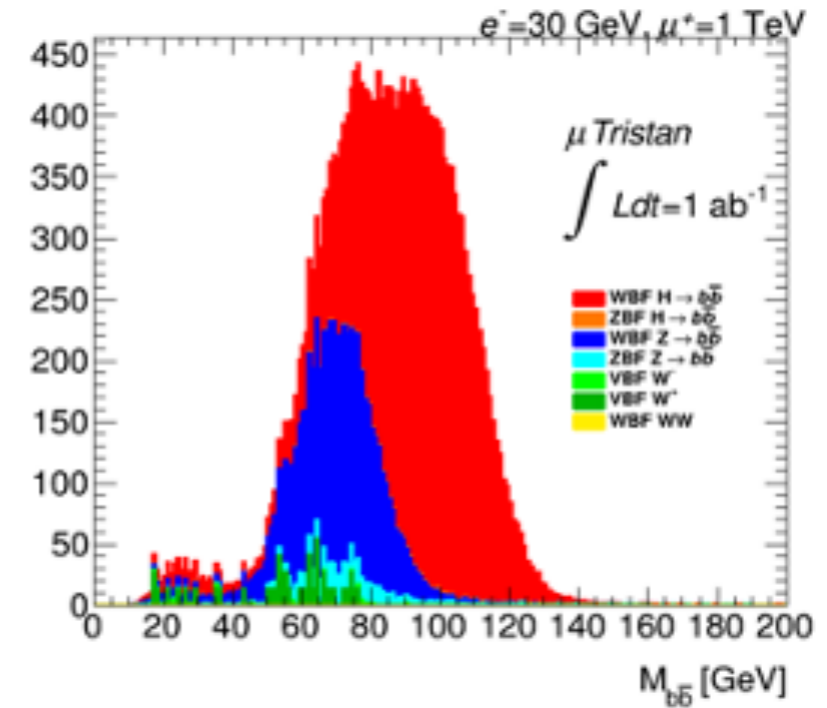
We need a coverage of $\eta \sim -4$ (2°), which is the same level as the design of the ATLAS at HL-LHC.



Higgs coupling

Study in progress in collaboration with Koji Nakamura and Sayuka Kita.

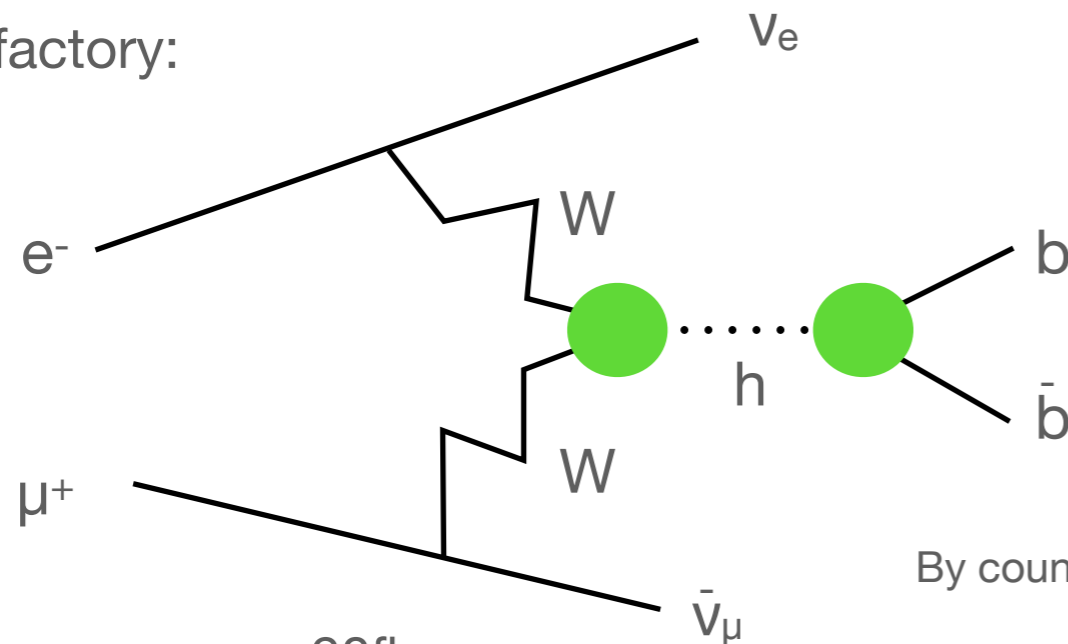
simulation with the ATLAS detector for HL-LHC



acceptance $\sim 23\%$

(This should improve a lot with a detector designed for this collider.)

Higgs factory:



$\sim 90\text{fb}$

$\sim 10^5$ Higgs bosons

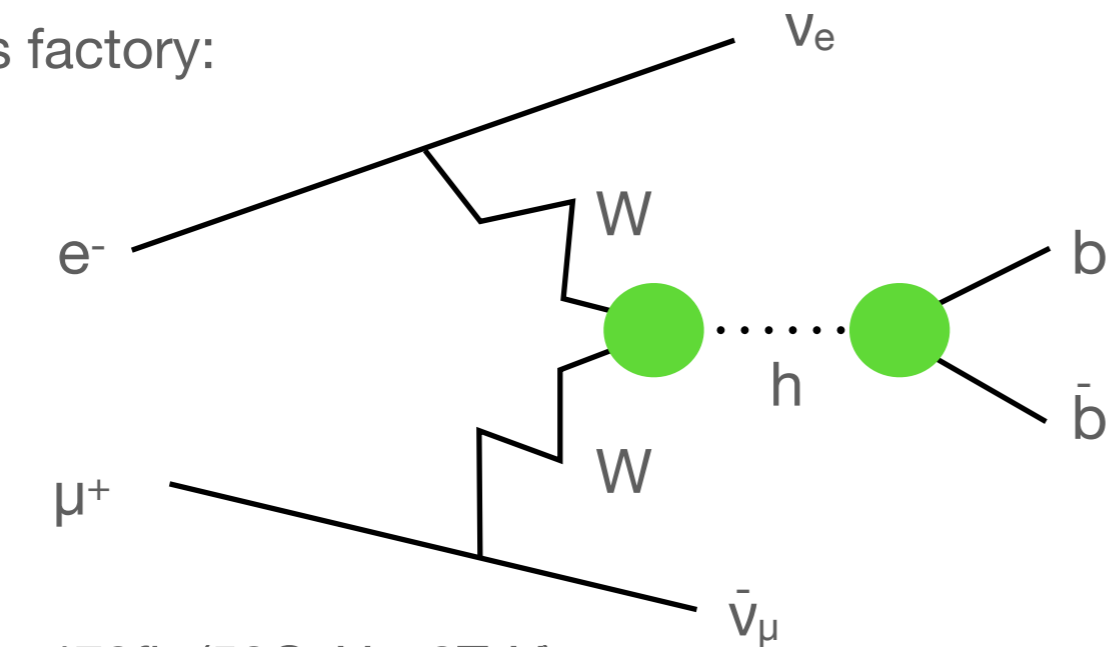
By counting the number of events and compare with the SM prediction

$$\begin{aligned} \Delta(\kappa_W + \kappa_b - \kappa_H)_{\text{stat}} &= \frac{1}{2} \frac{1}{\sqrt{N(\text{WBF}) \times \text{Br}(h \rightarrow b\bar{b}) \times \text{efficiency}}} \\ &= 3.1 \times 10^{-3} \times \left(\frac{\text{integrated luminosity}}{1.0 \text{ ab}^{-1}} \right)^{-1/2} \left(\frac{\text{efficiency}}{0.5} \right)^{-1/2} \end{aligned}$$

sub percent level measurements.

Higher energy? μ Tevatron?

Higgs factory:



$\sim 472 \text{ fb}$ ($50 \text{ GeV} \times 3 \text{ TeV}$)

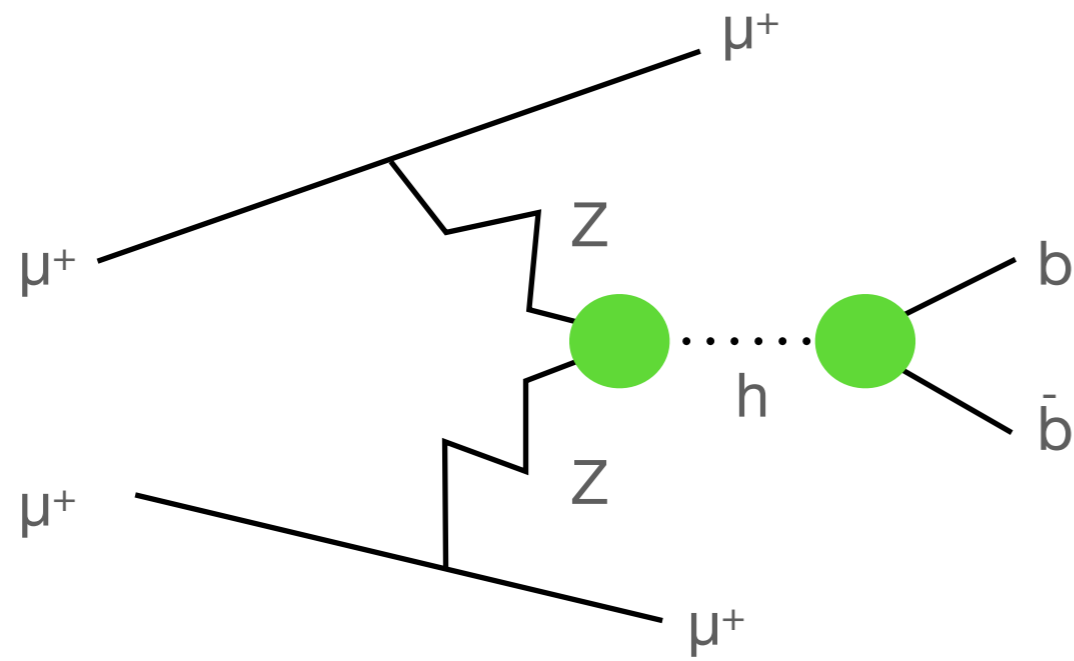
$\sim 5 \times 10^5$ Higgs bosons (ab^{-1})

50 GeV electron + 3 TeV muon at a **6 km** ring

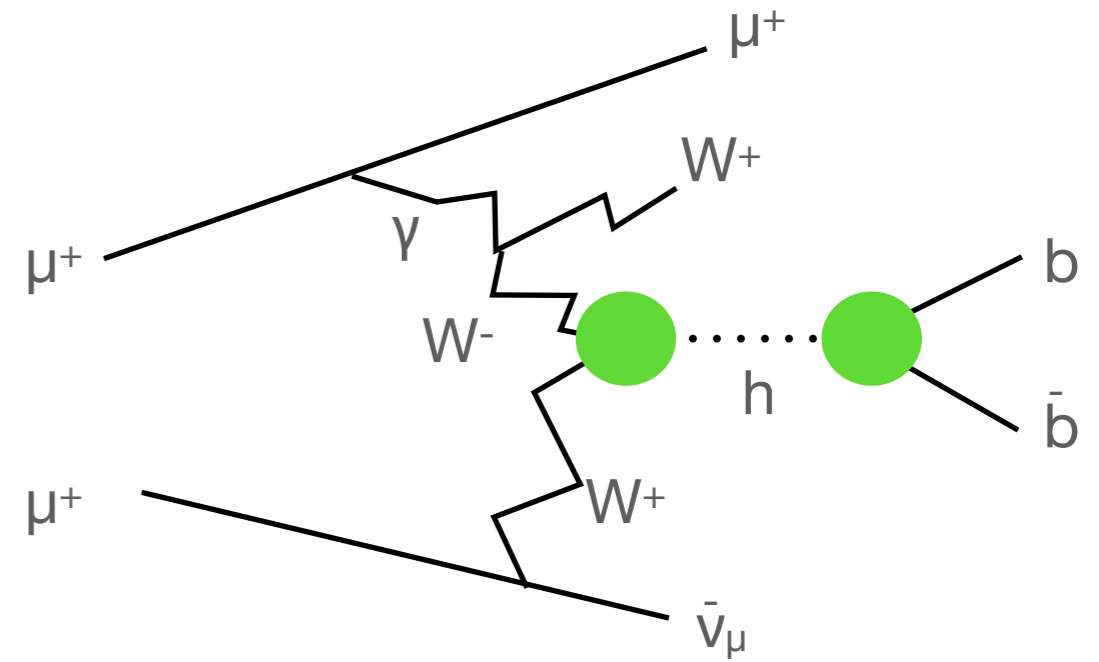
$$\sqrt{s} = 775 \text{ GeV}$$

hh production: 89 events/ ab^{-1} (maybe we need more for coupling measurements)

Higgs production@ $\mu^+\mu^+$



$\sim 54\text{fb}@2\text{TeV}$ final state all visible



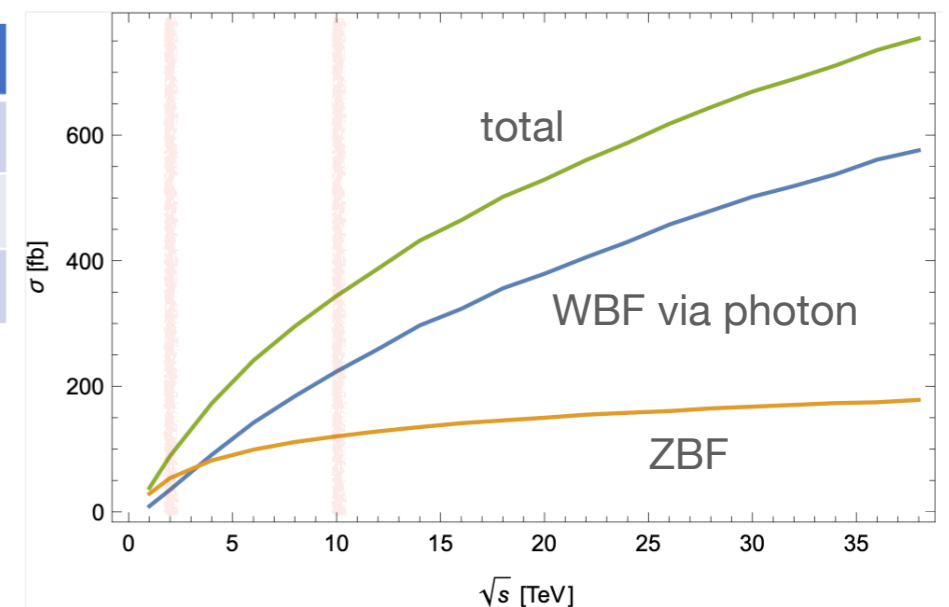
$\sim 35\text{fb}@2\text{TeV}$

gets more important at high energy



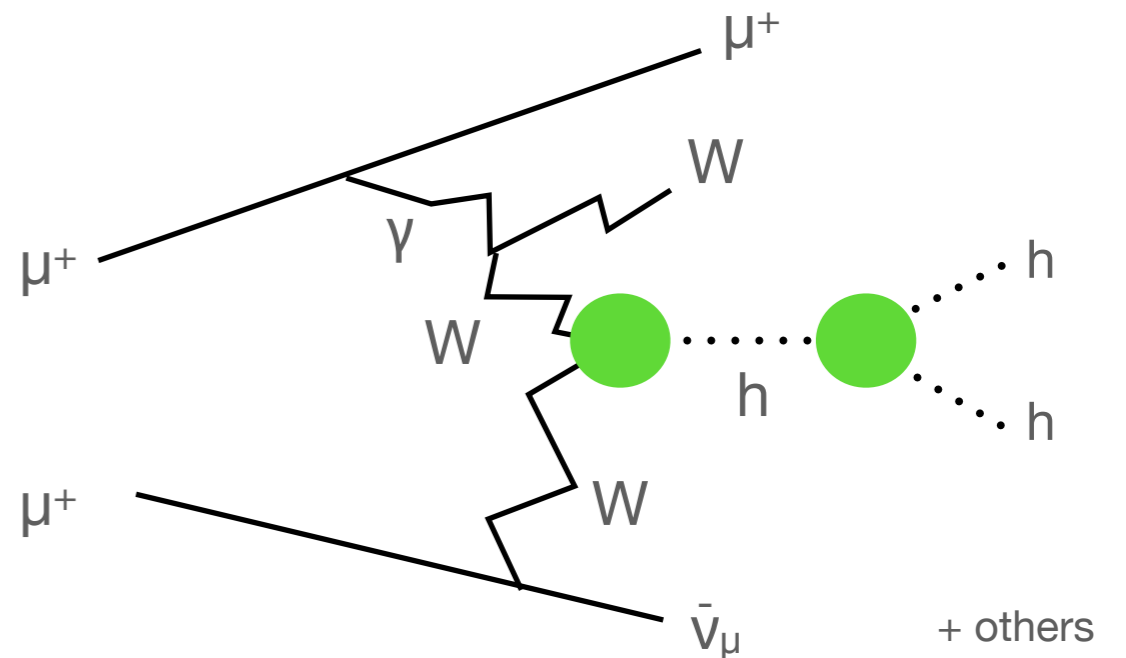
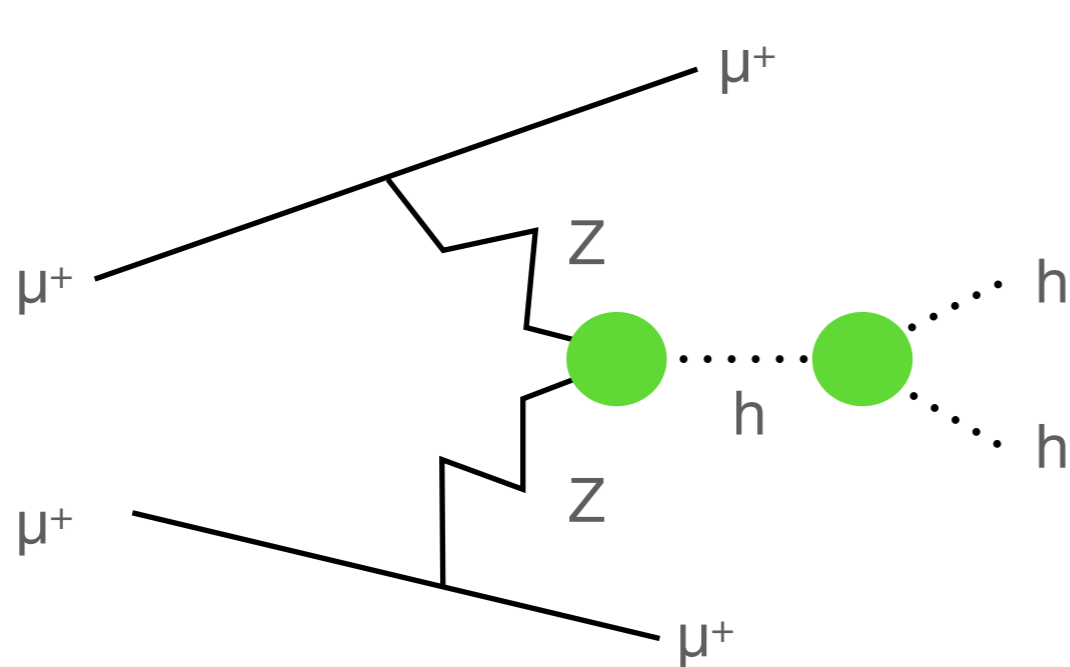
\sqrt{s} [TeV]	ZBF [fb]	Photon emission [fb]
2	54	35
10	121	224
20	150	376

about a factor of two smaller than $\mu^+\mu^-$
(not too bad?)



maybe we should plan 5-10TeV colliders.

Higgs production@ $\mu^+\mu^+$

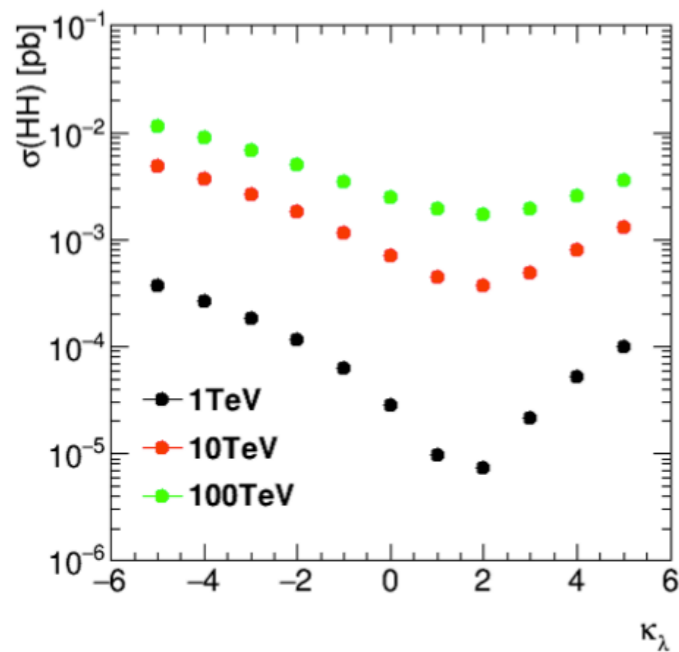


about 1/3 of $\mu^+\mu^-$

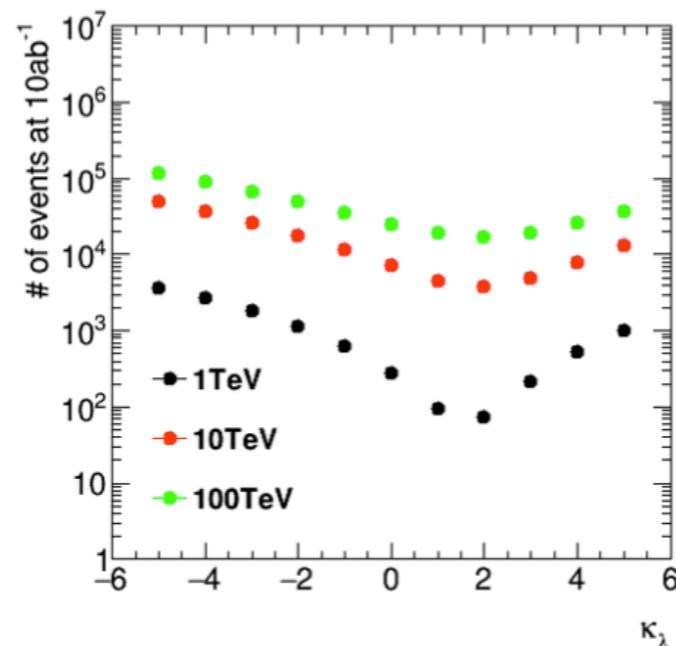
\sqrt{s} [TeV]	ZBF [fb]	Photon emission [fb]
2	0.075	0.010
10	0.62	0.30
20	1.1	0.75

ZBF:

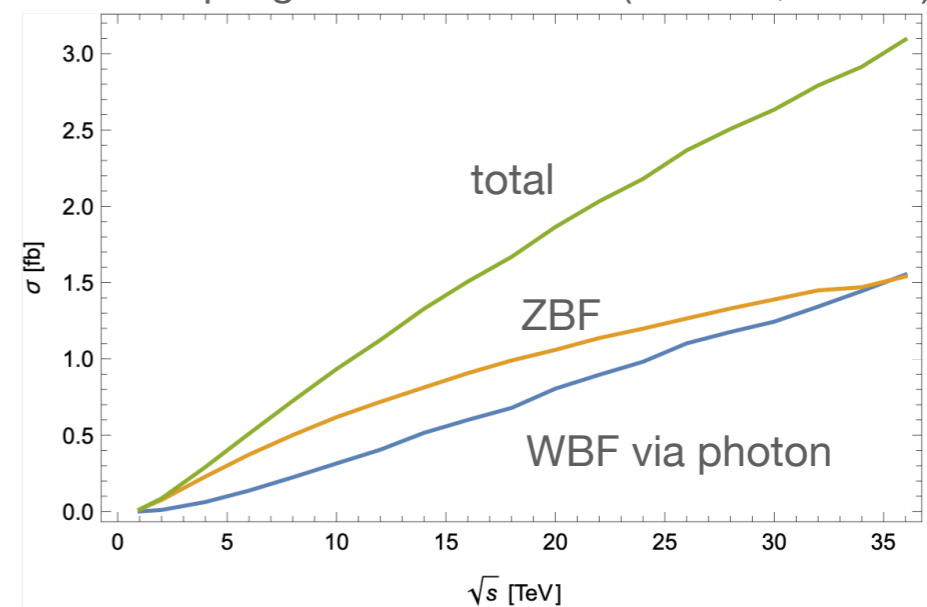
Cross section



of Events in 10ab⁻¹

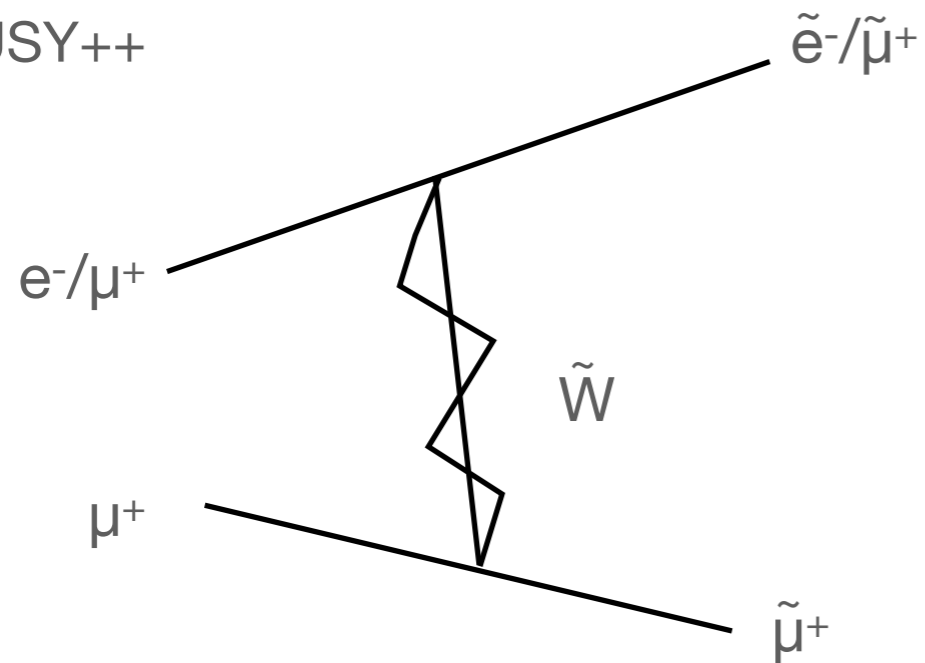


hhh coupling at 5-10% level? (@10TeV, 10ab⁻¹)



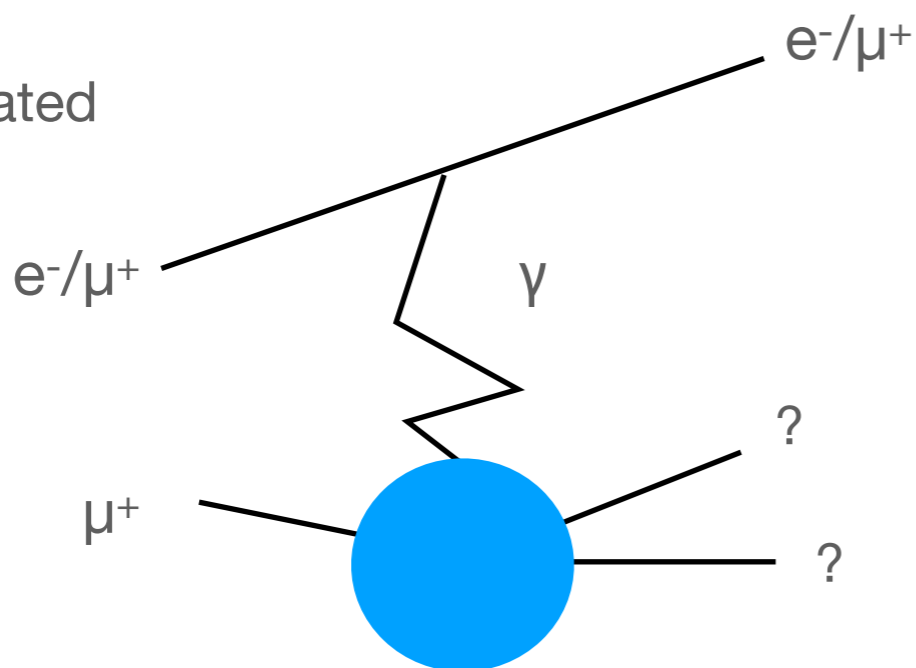
New physics?

SUSY₊₊

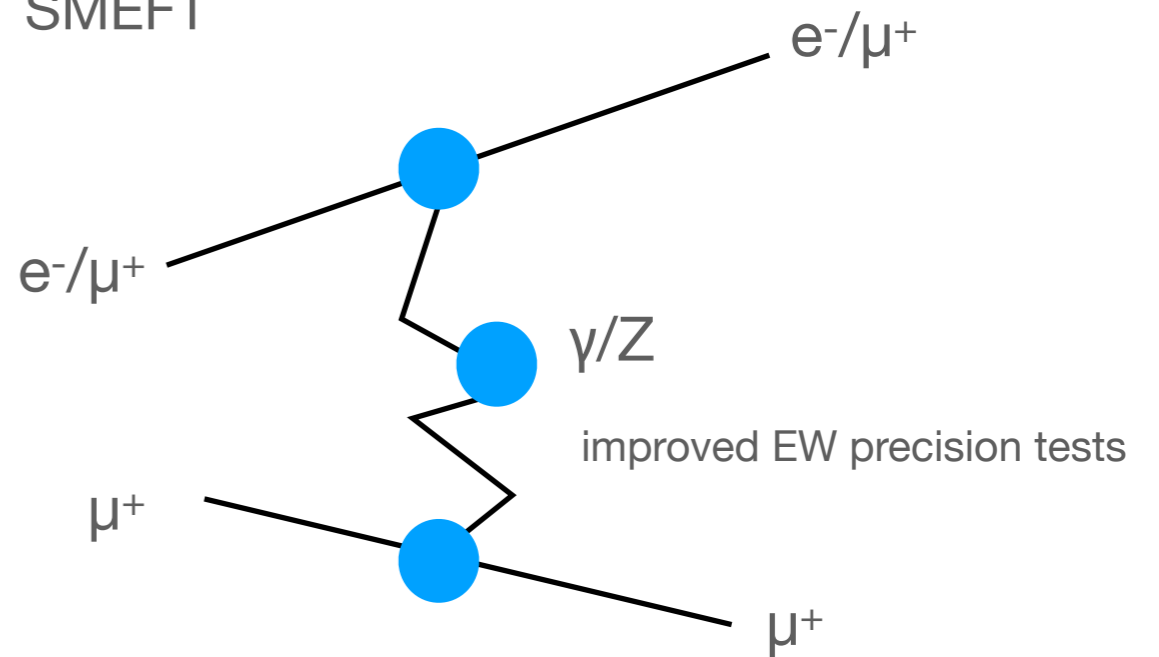


TeV mass new particles

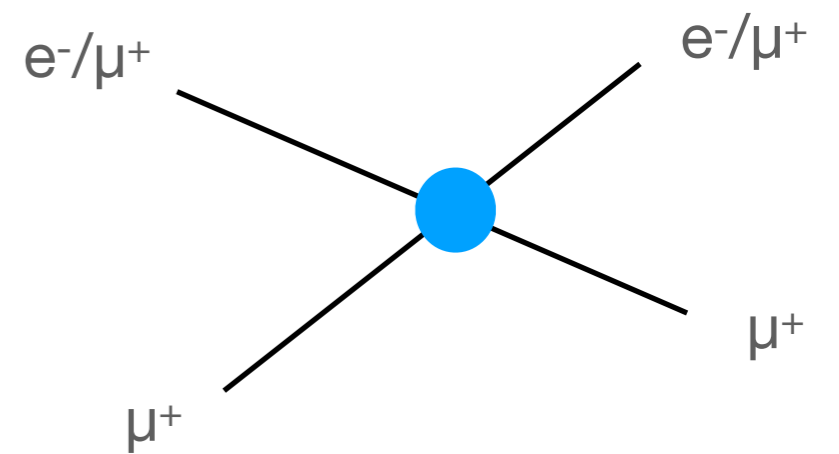
$g-2$ motivated



SMEFT



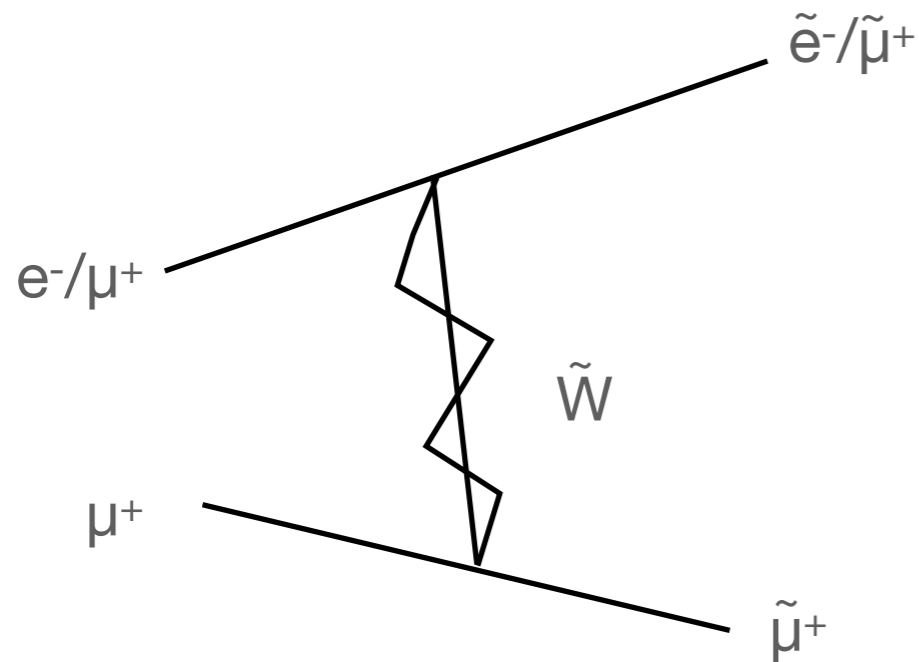
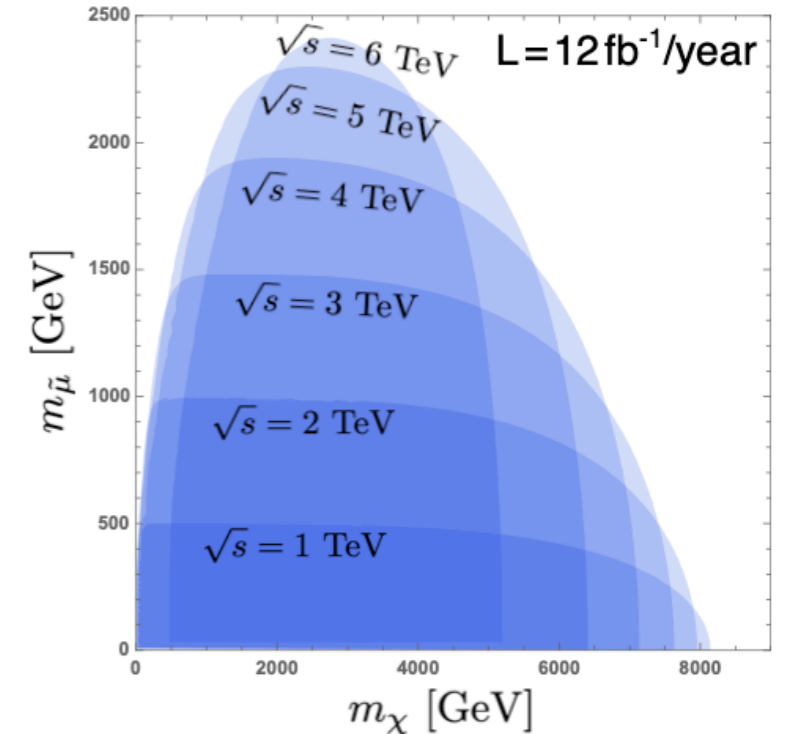
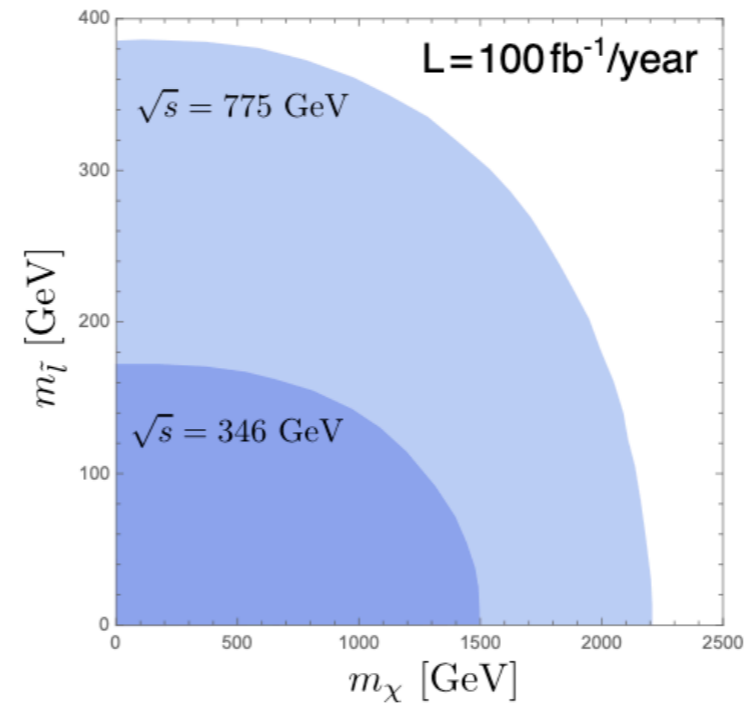
improved EW precision tests



probe 100TeV scale physics!?

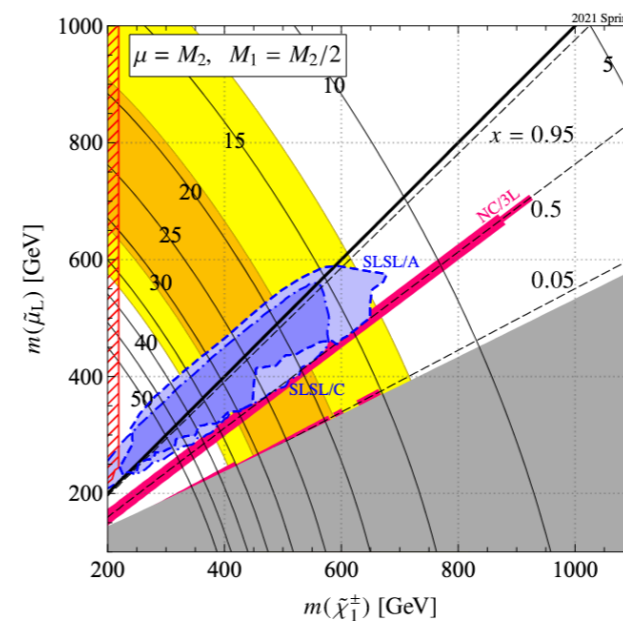
Supersymmetry

Regions for $N_{\text{event/year}} > 100$.

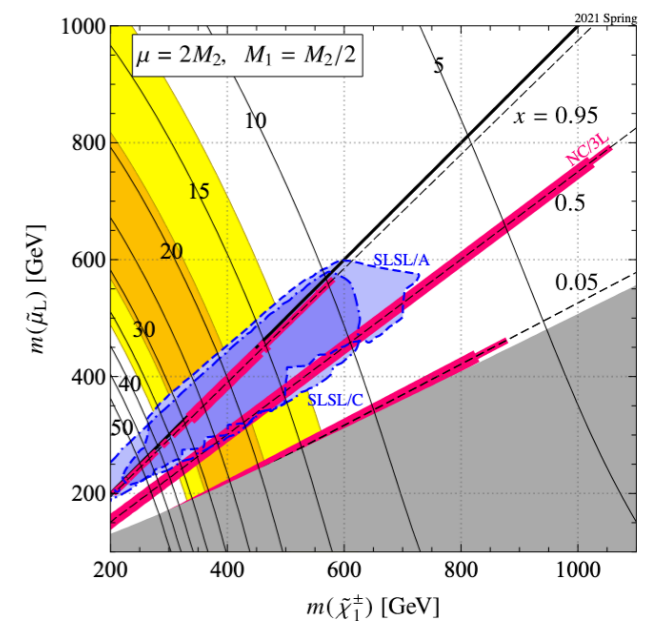


Scalar muons up to TeV even for very heavy gauginos.
Almost completely cover the muon $g-2$ motivated region.

[Endo, Hamaguchi, Iwamoto, Kitahara '21]



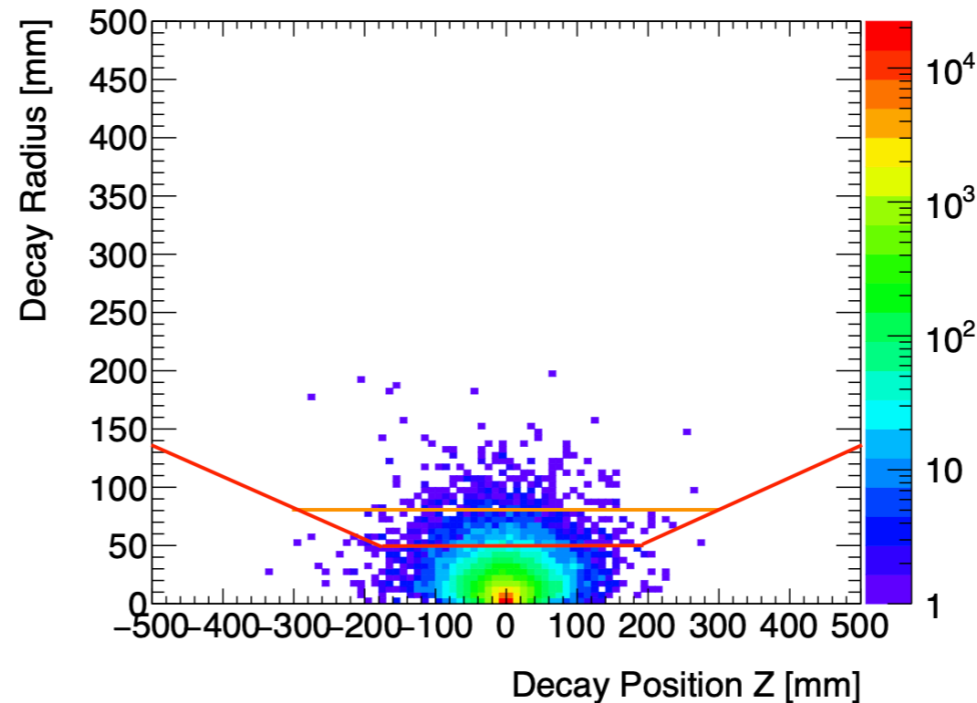
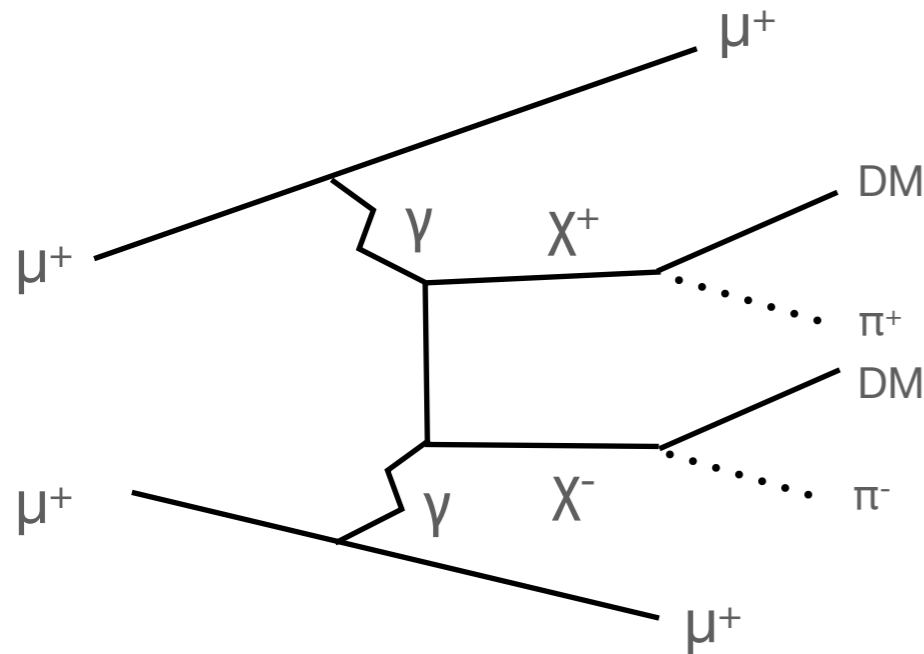
(A) $\mu = M_2, M_1 = M_2/2$.



(B) $\mu = 2M_2, M_1 = M_2/2$.

DM search

$\sqrt{s} = 10 \text{ TeV}$, 質量 1 TeV Higgsino の崩壊マップ



崩壊半径

• Case A > 80 mm

• Case B > 50 mm

$|\eta| < 2.0$

を再構成できると仮定

of expected events @ 1 ab^{-1}

	R > 50 mm	R > 80 mm
$\sigma = 124.7 \text{ ab}$ $\mu^+\mu^+ \rightarrow \chi^+\chi^-\mu^+\mu^+$ (2 muons + at least 1 chargino)	2.4	0.5

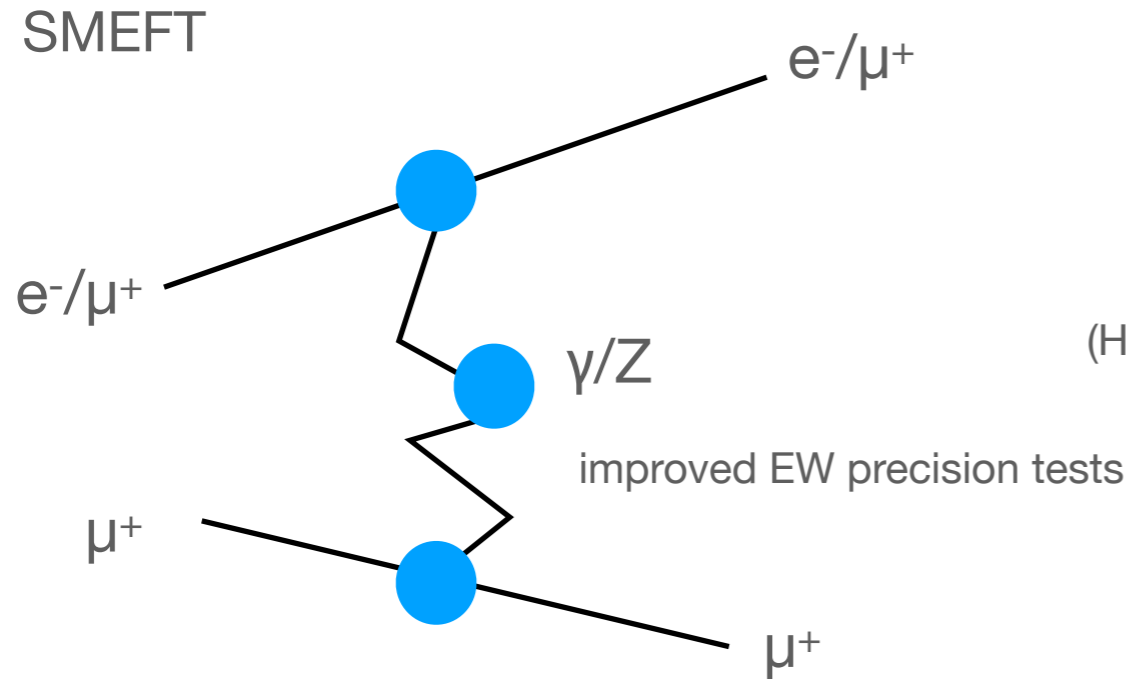
assumed a muon system which can detect forward muons ($|\eta| < 6$)

Looks like 1TeV Higgsino is within the reach.

(@10TeV machine)

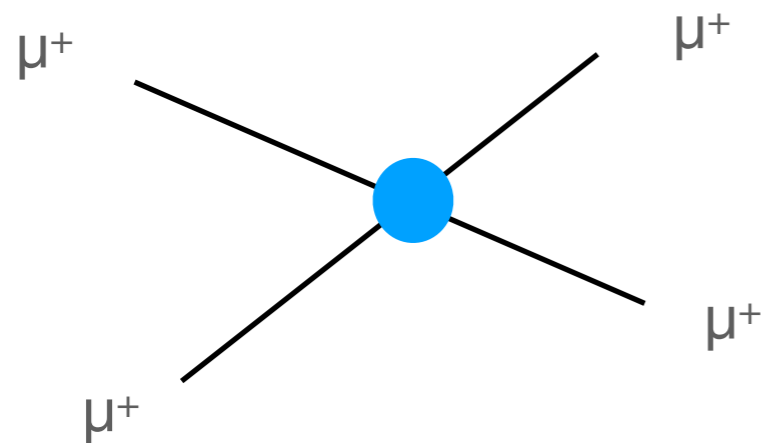
Indirect searches

Basically the SM process has peak at the forward region, while interference with new physics (dim-6 operators) give events in the central region.



		RR	RL	LR	LL
S T (H current)(L current)	C_{HWB}	6.9 TeV	24 TeV	26 TeV	6.9 TeV
	C_{HD}	6.8 TeV	9.0 TeV	14 TeV	6.8 TeV
	$C_{H\ell}^{(1)}$	15 TeV	0	20 TeV	15 TeV
	$C_{H\ell}^{(3)}$	20 TeV	18 TeV	35 TeV	20 TeV
	C_{He}	16 TeV	19 TeV	0	16 TeV
4-fermi	$C_{\ell\ell}$	9.6 TeV	13 TeV	43 TeV	9.6 TeV
	$C_{\ell\ell}''$	0	0	47 TeV	0
	$C_{e\mu}$	0	66 TeV	0	0
	$C_{\ell e}$	0	0	0	44 TeV
	$C_{ee\mu\mu}$				
	$C_{\ell e}$	44 TeV	0	0	0
	$C_{\mu\mu ee}$				

Table 2: Constraints on SMEFT operators at two-sigma level. $E_e = 30$ GeV and $E_\mu = 1$ TeV, which amounts to $\sqrt{s} = 346$ GeV. The bin size for Θ_e is taken as 1° . We require both muon and electron to go into the range of $15.4^\circ \lesssim \Theta \lesssim 178^\circ$, corresponding to $\eta_{max} = 2$ for the muon beam side and $\eta_{max} = 4$ for the electron beam side. As a result, the angle range of the electron is $62.8^\circ \lesssim \Theta_e \lesssim 178^\circ$.

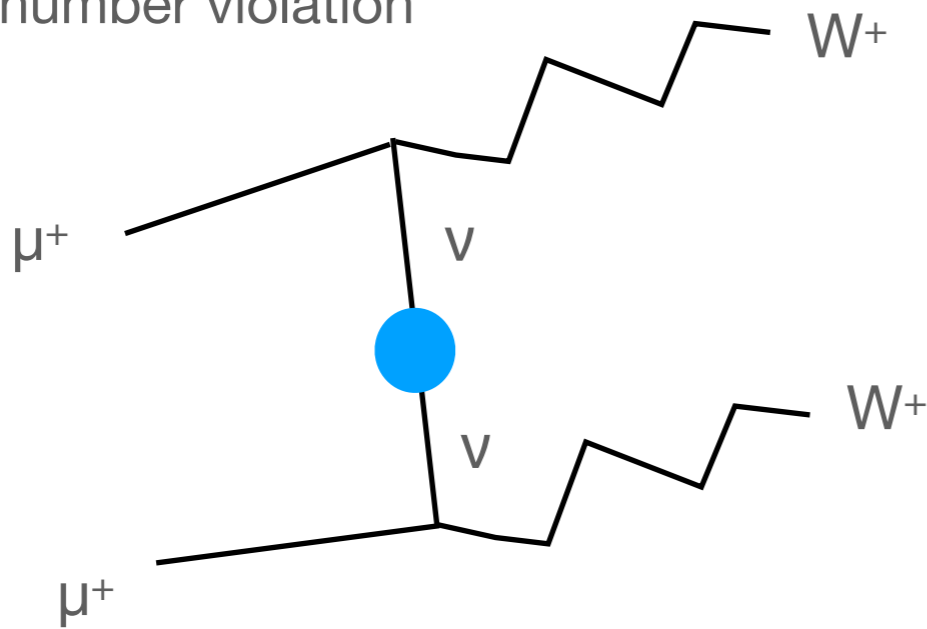


		RR	LL	RL
S T (H current)(L current)	C_{HWB}	10 TeV	9.4 TeV	2.3 TeV
	C_{HD}	5.5 TeV	3.5 TeV	2.3 TeV
	$C_{H\ell}^{(1)}$	8.0 TeV	0	4.9 TeV
	$C_{H\ell}^{(3)}$	14 TeV	7.0 TeV	6.7 TeV
	C_{He}	0	7.5 TeV	5.3 TeV
4-fermi	$C_{\ell\ell}$	7.7 TeV	5.0 TeV	3.3 TeV
	$C_{\mu\mu\mu\mu}$	100 TeV	0	0
	$C_{ee\mu\mu}$	0	100 TeV	0
	$C_{\ell e}$	0	0	46 TeV

Table 1: Constraints on SMEFT operators at 2-sigma level. $\sqrt{s} = 2$ TeV. The bin size for θ is taken as 1° and each bin covers the range $\theta_i - 0.5^\circ < \theta < \theta_i + 0.5^\circ$. The considered range of θ_i is $16^\circ \leq \theta_i \leq 164^\circ$.

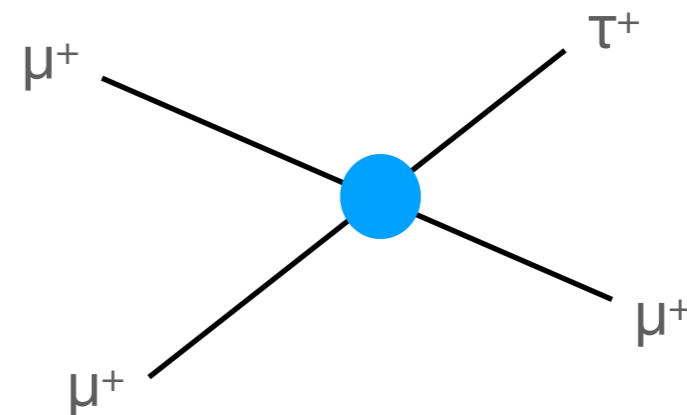
Lepton number/flavor violation?

lepton number violation

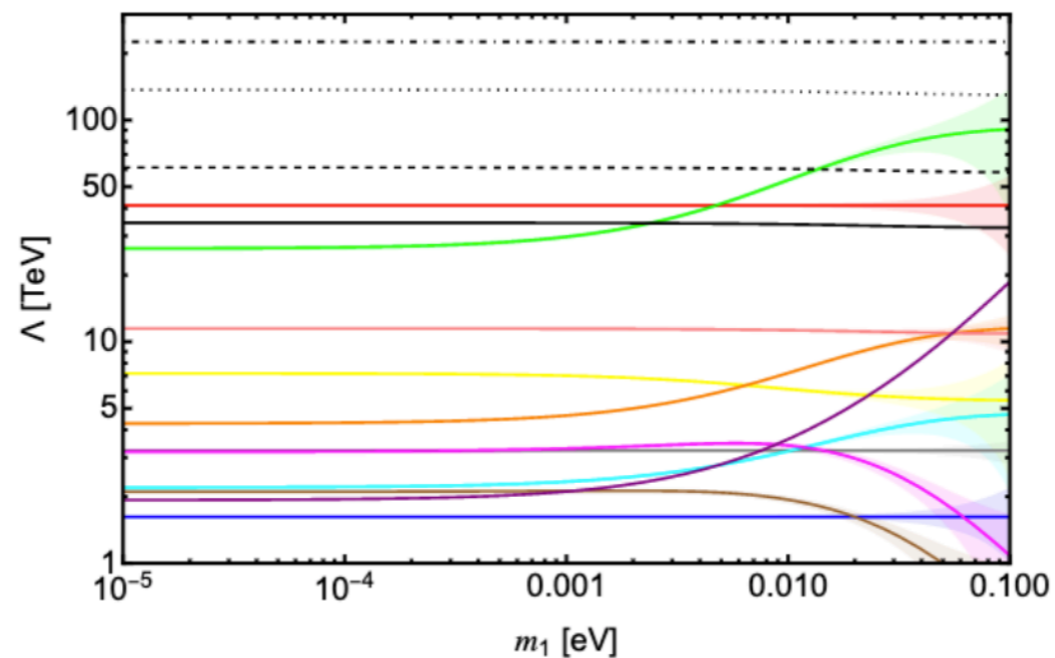


lepton flavor violation

[Fridell, RK and Takai '23]



Can be better than rare decays!



comparison with $\mu \rightarrow 3e$ decay
type-II seesaw model

- $\mu \rightarrow e\gamma$
- $\mu \rightarrow 3e$
- $\tau \rightarrow e\gamma$
- $\tau \rightarrow \mu\gamma$
- $\tau \rightarrow 3e$
- $\tau^- \rightarrow \mu^+ \mu^- e^-$
- $\tau^- \rightarrow e^+ \mu^- \mu^-$
- $\tau^- \rightarrow e^+ e^- \mu^-$
- $\tau^- \rightarrow \mu^+ e^- e^-$
- $\tau \rightarrow 3\mu$
- $M \rightarrow \bar{M}$
- 100 events (2 TeV, 1 ab^{-1})
- - - - 10 events (2 TeV, 1 ab^{-1})
- ⋯⋯⋯ 100 events (10 TeV, 10 ab^{-1})
- ⋯⋯⋯ elastic (2 TeV, 1 ab^{-1})

Summary

We are not satisfied with the current understanding of particle physics. Too much unknowns. Full of mysteries.

μ^+ may have a chance. Interesting to consider a km size experiment as a relatively near future project.

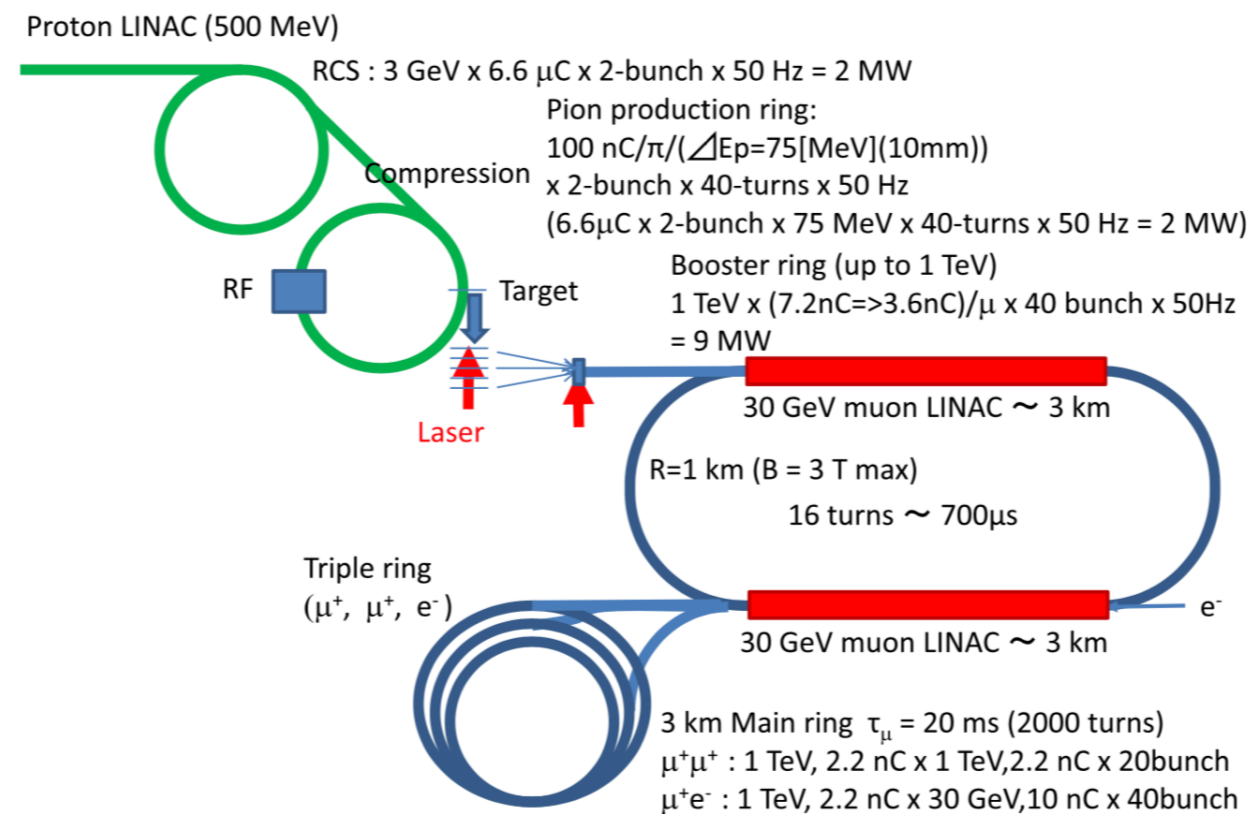


Fig. 1. Conceptual design of the $\mu^+e^-/\mu^+\mu^+$ collider.