

Precise predictions for the trilinear Higgs coupling in arbitrary models

Based on

arXiv:2305.03015 in collaboration with Henning Bahl, Martin Gabelmann and Georg Weiglein

Johannes Braathen

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Why study the trilinear Higgs coupling?

Probing the Higgs potential:

Since the Higgs discovery, the existence of the Higgs potential is confirmed, but at the moment we only know:

→ the location of the EW minimum:

$$v = 246 \text{ GeV}$$

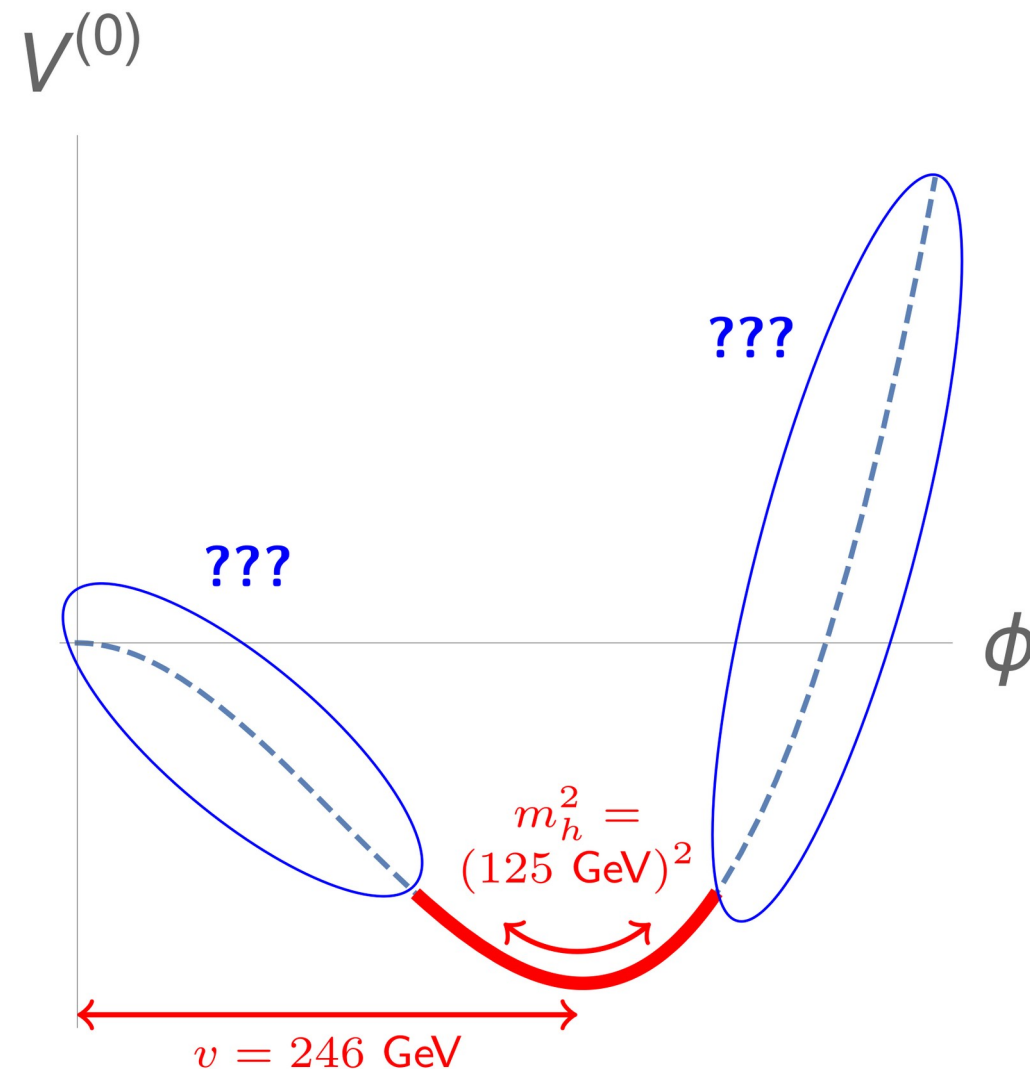
→ the curvature of the potential around the EW minimum:

$$m_h = 125 \text{ GeV}$$

However we still don't know the **shape** of the potential, away from EW minimum → depends on λ_{hhh}

λ_{hhh} determines the nature of the EWPT!

⇒ deviation of λ_{hhh} from its SM prediction typically needed to have a strongly first-order EWPT → necessary for EWBG [Grojean, Servant, Wells '04], [Kanemura, Okada, Senaha '04]



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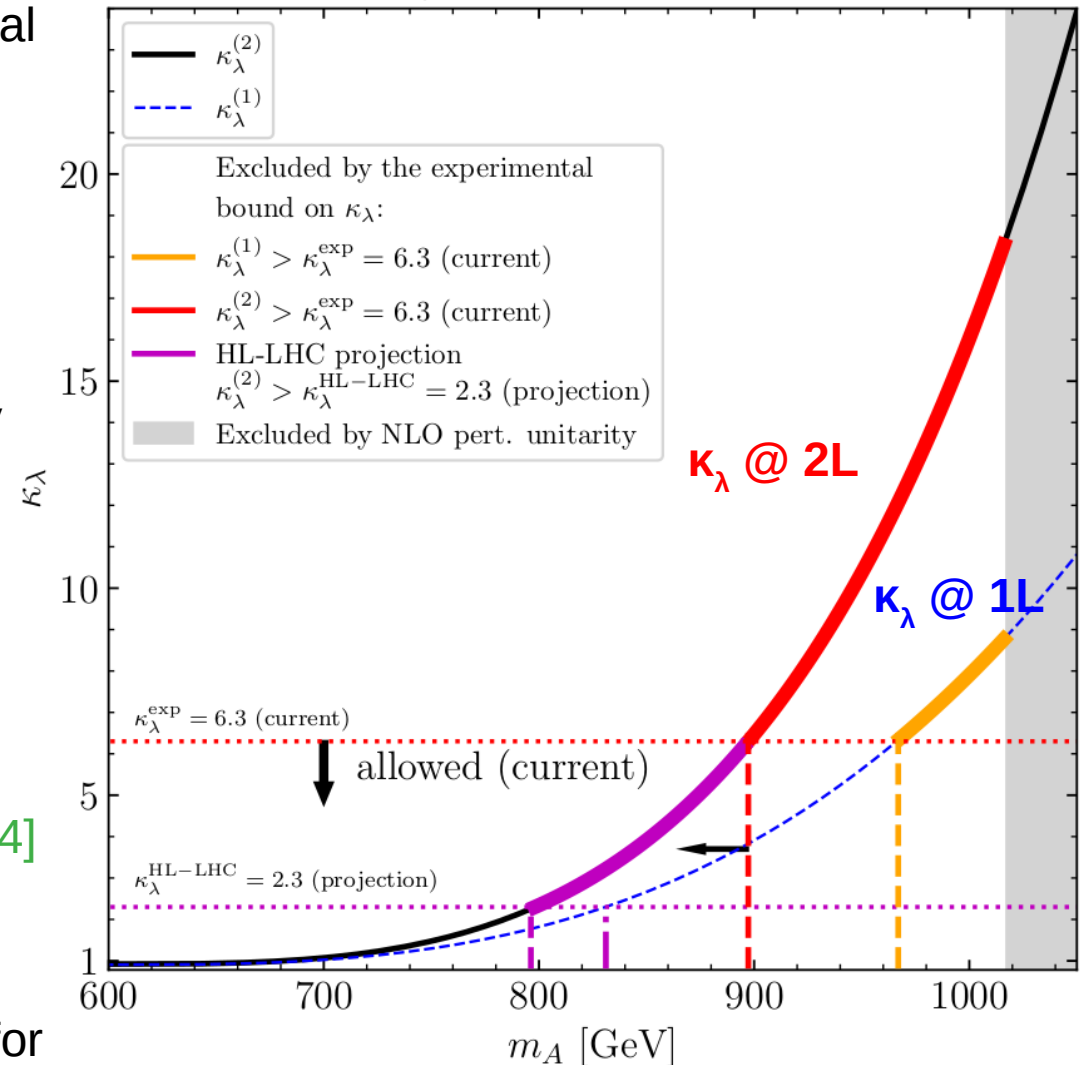
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Comparing latest exp. bounds $-0.4 < \kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM} < 6.3$ [ATLAS-CONF-2022-050] with precise theory predictions for λ_{hhh} provides a **powerful new tool to constrain BSM models**

2HDM type I, $\alpha = \beta - \pi/2$, $m_A = m_{H^\pm}$, $M = m_H = 600 \text{ GeV}$, $\tan \beta = 2$



[Bahl, JB, Weiglein *Phys.Rev.Lett.* '22]

Computing λ_{hhh} in BSM theories

- Calculations of λ_{hhh} are important, and receive increasing attention

- More and more model specific results at 1L

SM + singlet [Kanemura et al. '16]; *2HDMs* [Kanemura et al. '04], [Basler et al. '17]; *N2HDM (2HDM + singlet)* [Basler et al. '19]; *triplet extensions* [Aoki et al. '12], [Chiang et al. '18]; *MSSM* [Hollik, Penaranda '04]; *NMSSM* [Dao et al. '13]; *models with classical scale invariance* [Hashino, Kanemura, Orikasa '16], etc.

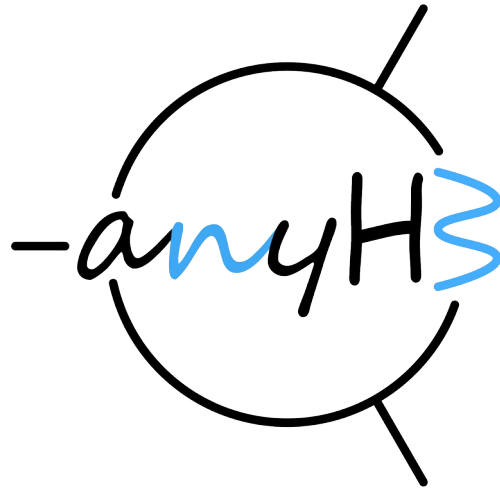
... and at 2L

SM + singlet [JB, Kanemura '19]; *2HDMs* [Senaha '18], [JB, Kanemura '19]; *MSSM* [Brucherseifer et al. '13]; *NMSSM* [Dao et al. '15], [Borschensky et al '22]; *models with classical scale invariance* [JB, Kanemura, Shimoda '20], etc.

but many more models to investigate!

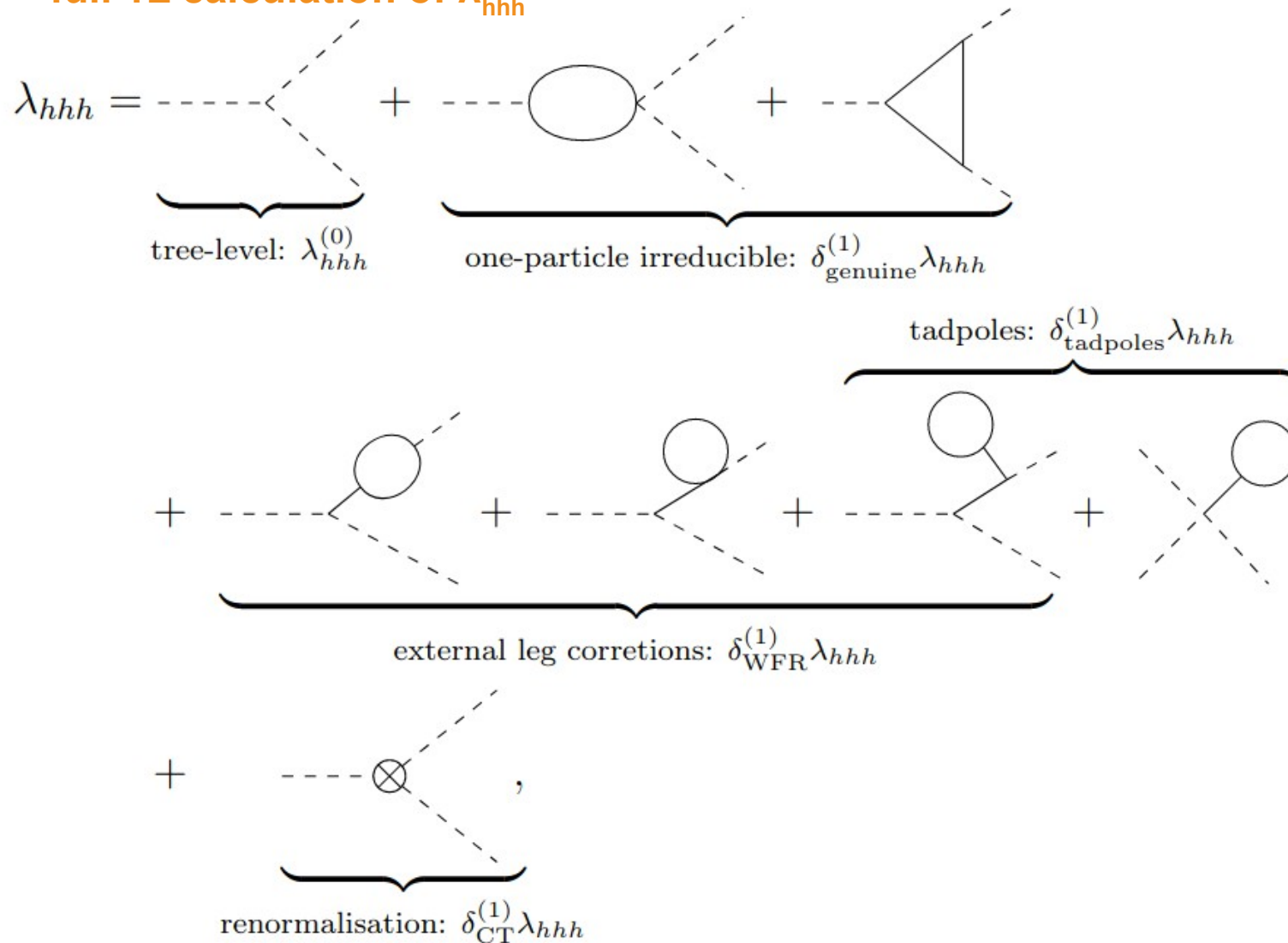
- For many (pseudo-)observables, automated tools exist
- What about for the trilinear Higgs coupling?
 - none so far
 - **anyH3** [Bahl, JB, Gabelmann, Weiglein 2305.03015]

Generic predictions for λ_{hhh}



Computing λ_{hhh} in general renormalisable theories: ingredients

anyH3 \rightarrow full 1L calculation of λ_{hhh}



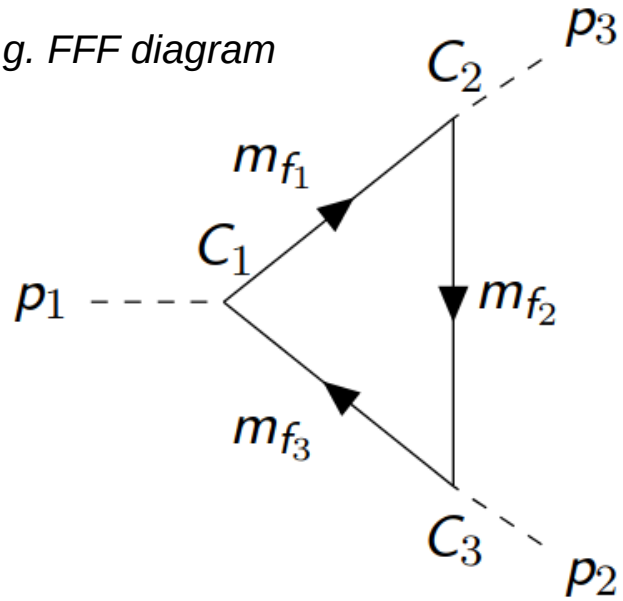
- Solid lines:
 - scalars,
 - fermions,
 - gauge/vector bosons,
 - ghosts

- Restrictions on particles and/or topologies possible

Computing λ_{hhh} in general renormalisable theories: method

Our method: we derive and implement analytic results for **generic diagrams**, i.e. assuming generic

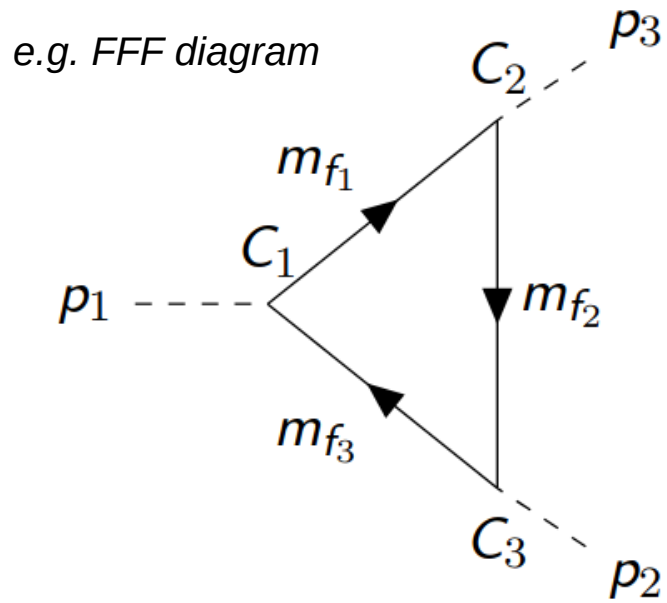
e.g. FFF diagram



- › Couplings $C_i = C_i^L P_L + C_i^R P_R$, where $P_{L,R} \equiv \frac{1}{2}(1 \mp \gamma_5)$
- › Masses on the internal lines m_{f_i} , $i=1,2,3$
- › External momenta p_i , $i=1,2,3$

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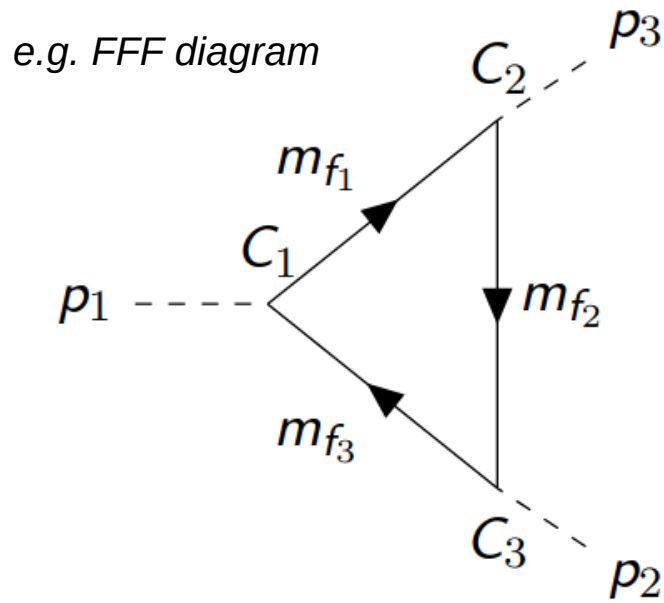
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- › Masses on the internal lines m_{fi} , $i=1,2,3$
- › External momenta p_i , $i=1,2,3$

$$\begin{aligned}
 &= 2\mathbf{B0}(p_3^2, m_2^2, m_3^2)(C_1^L(C_2^L C_3^R m_{f_1} + C_2^R C_3^R m_{f_2} + C_2^R C_3^L m_{f_3}) + C_1^R(C_2^R C_3^L m_{f_1} + \\
 &C_2^L C_3^L m_{f_2} + C_2^L C_3^R m_{f_3})) + m_{f_1} \mathbf{C0}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((C_1^L C_2^L C_3^R + \\
 &C_1^R C_2^R C_3^L)(p_1^2 + p_2^2 - p_3^2) + 2(C_1^L C_2^L C_3^L + C_1^R C_2^R C_3^R)m_{f_2} m_{f_3} + \\
 &2m_{f_1}(C_1^L(C_2^L C_3^R m_{f_1} + C_2^R C_3^R m_{f_2} + C_2^R C_3^L m_{f_3}) + C_1^R(C_2^R C_3^L m_{f_1} + C_2^L C_3^L m_{f_2} + \\
 &C_2^L C_3^R m_{f_3}))) + \mathbf{C1}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)(2p_2^2(C_1^L C_3^R(C_2^L m_{f_1} + C_2^R m_{f_2}) + \\
 &C_1^R C_3^L(C_2^R m_{f_1} + C_2^L m_{f_2})) + (p_1^2 + p_2^2 - p_3^2)((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)m_{f_1} + \\
 &(C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f_3})) + \mathbf{C2}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)((p_1^2 + p_2^2 - \\
 &p_3^2)(C_1^L C_3^R(C_2^L m_{f_1} + C_2^R m_{f_2}) + C_1^R C_3^L(C_2^R m_{f_1} + C_2^L m_{f_2})) + 2p_1^2((C_1^L C_2^L C_3^R + \\
 &C_1^R C_2^R C_3^L)m_{f_1} + (C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f_3}))
 \end{aligned}$$

(**B0**, **C0**, **C1**, **C2**: loop functions)

Computing λ_{hhh} in general renormalisable theories: method

Our method: we derive and implement analytic results for **generic diagrams**, i.e. assuming generic



- › Couplings $C_i = C_i^L P_L + C_i^R P_R$, where $P_{L,R} \equiv \frac{1}{2}(1 \mp \gamma_5)$
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 &2m_{f_1}(C_1^L(C_2^L C_3^R m_{f_1} + C_2^R C_3^R m_{f_2} + C_2^R C_3^L m_{f_3}) + C_1^R(C_2^R C_3^L m_{f_1} + C_2^L C_3^L m_{f_2} + \\
 &C_2^L C_3^R m_{f_3}))) + \mathbf{C1}(p_2^2, p_3^2, p_1^2, m_1^2, m_3^2, m_2^2)(2p_2^2(C_1^L C_3^R(C_2^L m_{f_1} + C_2^R m_{f_2}) + \\
 &C_1^R C_3^L(C_2^R m_{f_1} + C_2^L m_{f_2})) + (p_1^2 + p_2^2 - p_3^2)((C_1^L C_2^L C_3^R + C_1^R C_2^R C_3^L)m_{f_1} + \\
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 &C_1^R C_2^R C_3^L)m_{f_1} + (C_1^L C_2^R C_3^L + C_1^R C_2^L C_3^R)m_{f_3}))
 \end{aligned}$$

For evaluation:

- › Apply to concrete (B)SM model, using inputs in UFO format [Degrande et al., '11], [Darmé et al. '23]
- › Evaluate loop functions via COLLIER [Denner et al '16] interface, pyCollier
- › All included in public tool anyH3 [Bahl, JB, Gabelmann, Weiglein '23]

(B0, C0, C1, C2: loop functions)

Flexible choice of renormalisation schemes

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \text{---} \otimes \text{---} = ?$$

➤ **1L calculation** → renormalisation of all parameters entering λ_{hhh} at tree-level

➤ In general:

$$(\lambda_{hhh}^{(0)})^{\text{BSM}} = (\lambda_{hhh}^{(0)})^{\text{BSM}} \left(\underbrace{m_h \simeq 125 \text{ GeV}, v \simeq 246 \text{ GeV}}_{\text{SM sector}}, \underbrace{m_{\Phi_i}}_{\text{BSM}}, \underbrace{\alpha_i}_{\text{BSM}}, \underbrace{v_i}_{\text{BSM}}, \underbrace{g_i}_{\text{indep.}} \right)$$

masses
mixing angles
VEVs
BSM coups.

➤ Most automated codes: $\overline{\text{MS}}/\overline{\text{DR}}$ only

➤ **anyH3**: much more flexibility, following **user choice**:

- **SM sector** (m_h, v): fully OS or $\overline{\text{MS}}/\overline{\text{DR}}$
- **BSM masses**: OS or $\overline{\text{MS}}/\overline{\text{DR}}$
- **Additional couplings/vevs/mixings**: by default $\overline{\text{MS}}$, but **user-defined ren. conditions** also possible!

$$\delta_{\text{CT}}^{(1)} \lambda_{hhh} = \sum_x \left(\frac{\partial}{\partial x} (\lambda_{hhh}^{(0)})^{\text{BSM}} \right) \delta^{\text{CT}} x, \quad \text{with } x \in \{m_h, v, m_{\Phi_i}, v_i, \alpha_i, g_i, \text{etc.}\}$$

Renormalised in $\overline{\text{MS}}$, OS, in custom schemes, etc.

Example results from anyH3

A cross-check: the decoupling limit

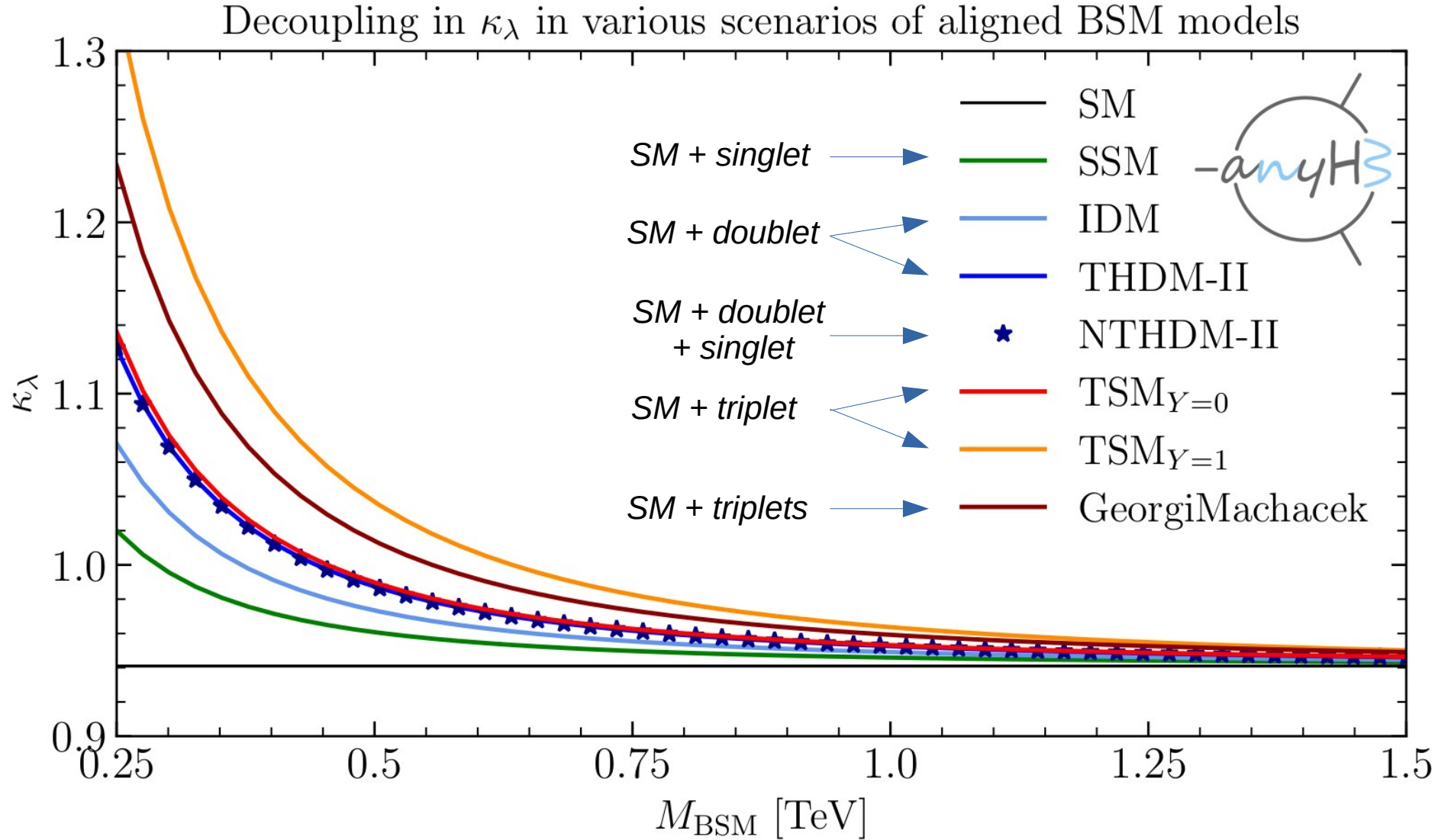
- Consider the decoupling limit in several BSM models

$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda} v^2$$

\mathcal{M} : BSM mass scale
 $\tilde{\lambda}$: Quartic couplings

- Increase BSM mass scale
 $\mathcal{M} \rightarrow \infty$

- BSM corrections to should vanish (c.f. decoupling theorem [Appelquist, Carrazone '75])



New results I: non-decoupling effects in various BSM models

- Consider the non-decoupling limit in several BSM models

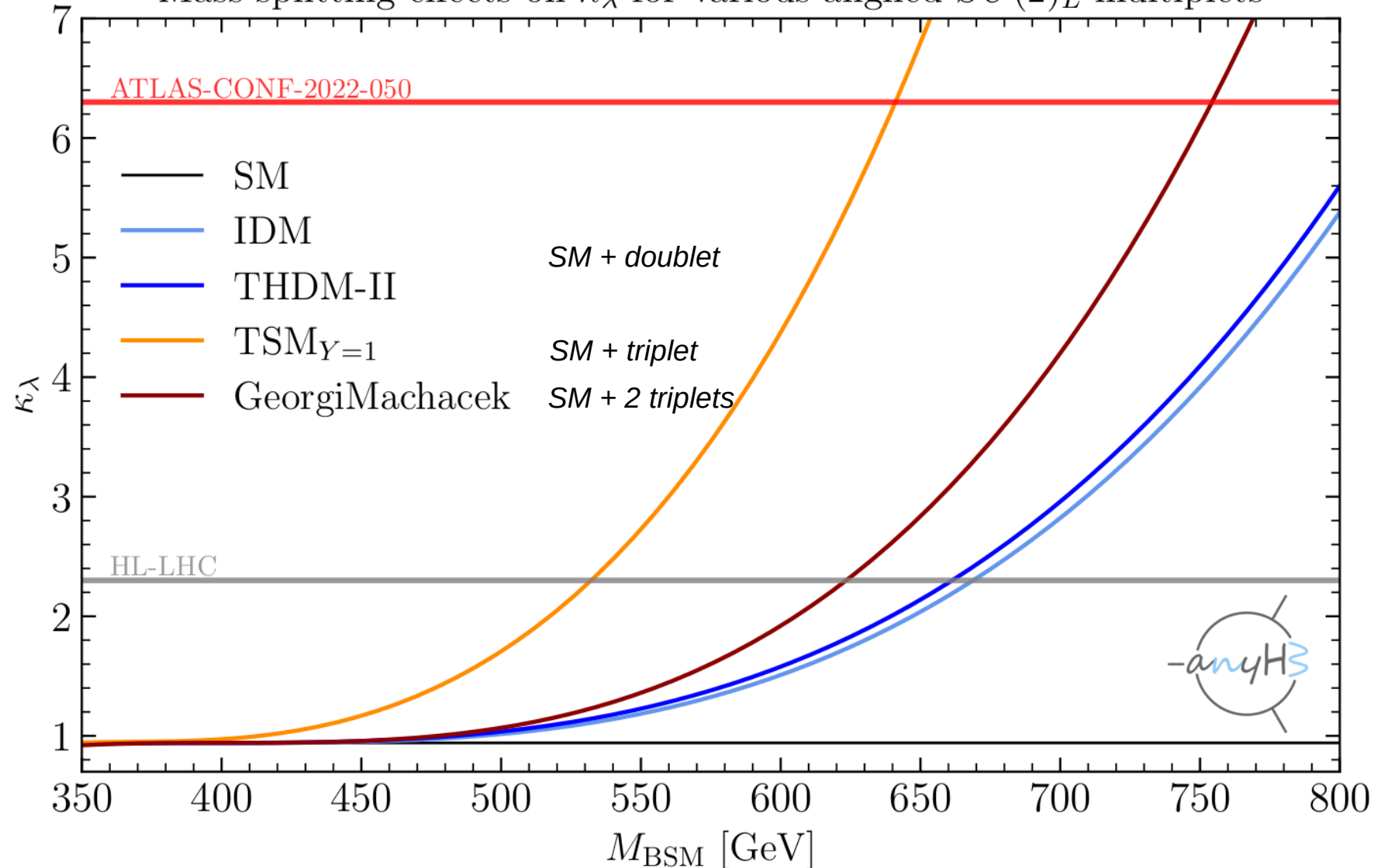
$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda} v^2$$

- Increase M_{BSM} , keeping \mathcal{M} fixed
 - large mass splittings
 - **large BSM effects!**

- Perturbative unitarity checked with anyPerturbativeUnitarity

- Constraints on BSM parameter space!**

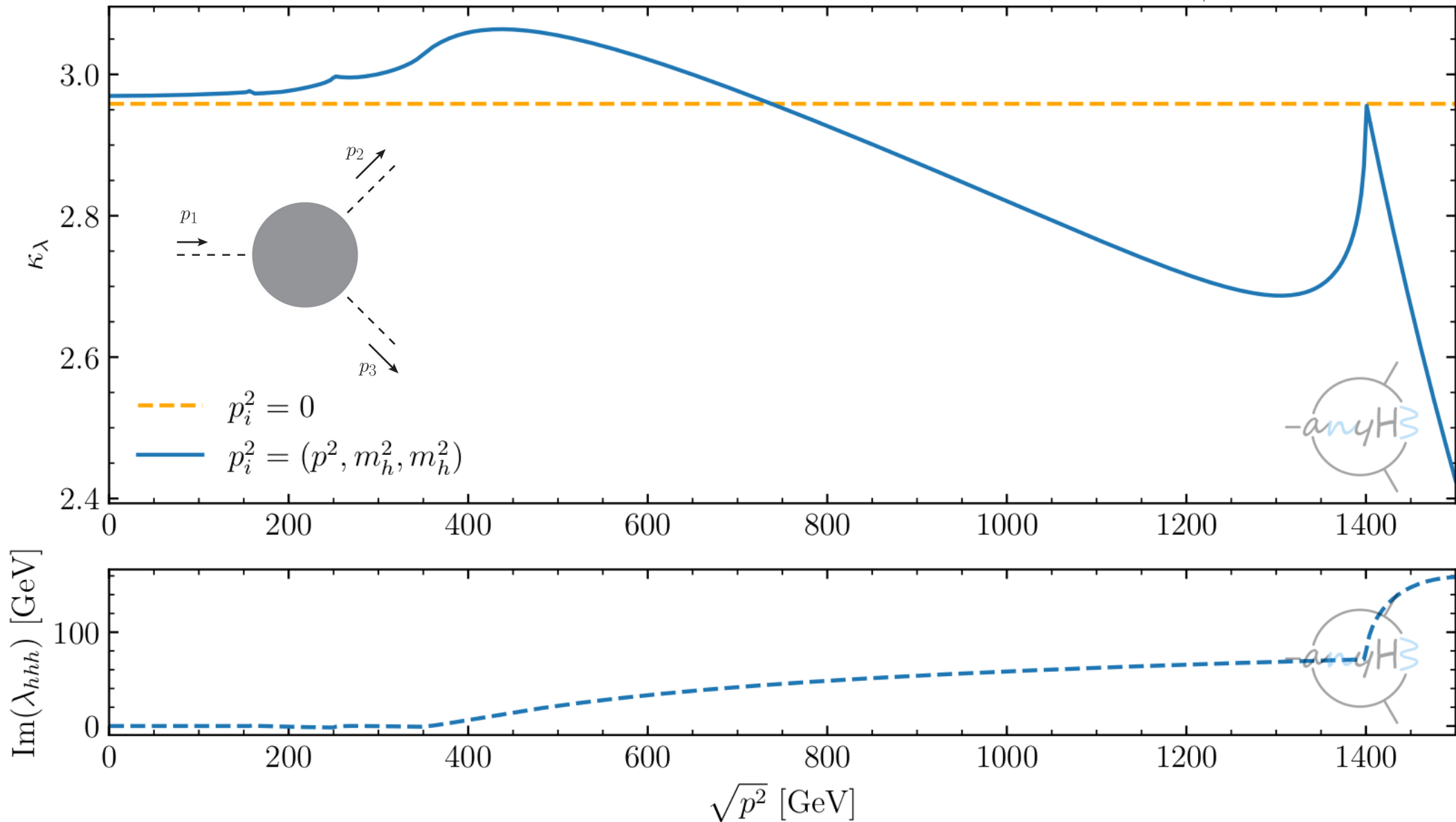
Mass-splitting effects on κ_λ for various aligned $SU(2)_L$ multiplets



Here: scenarios with lightest BSM scalar mass + BSM mass param. at 400 GeV; other BSM scalar masses = M_{BSM}

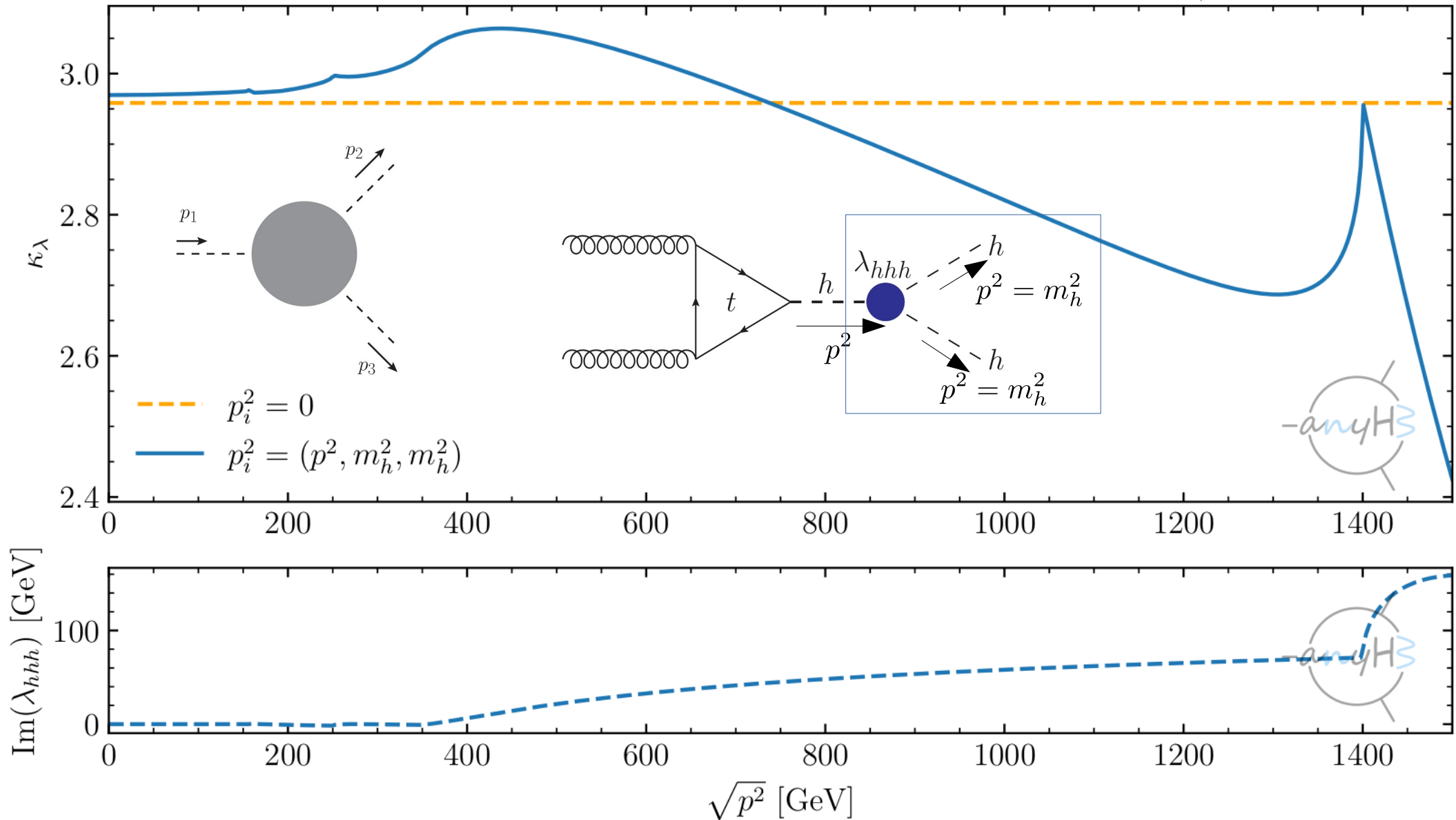
New results II: momentum dependence in the 2HDM

THDM-I: $m_H = M = 400 \text{ GeV}$, $m_A = m_{H^\pm} = 700 \text{ GeV}$, $t_\beta = 2$



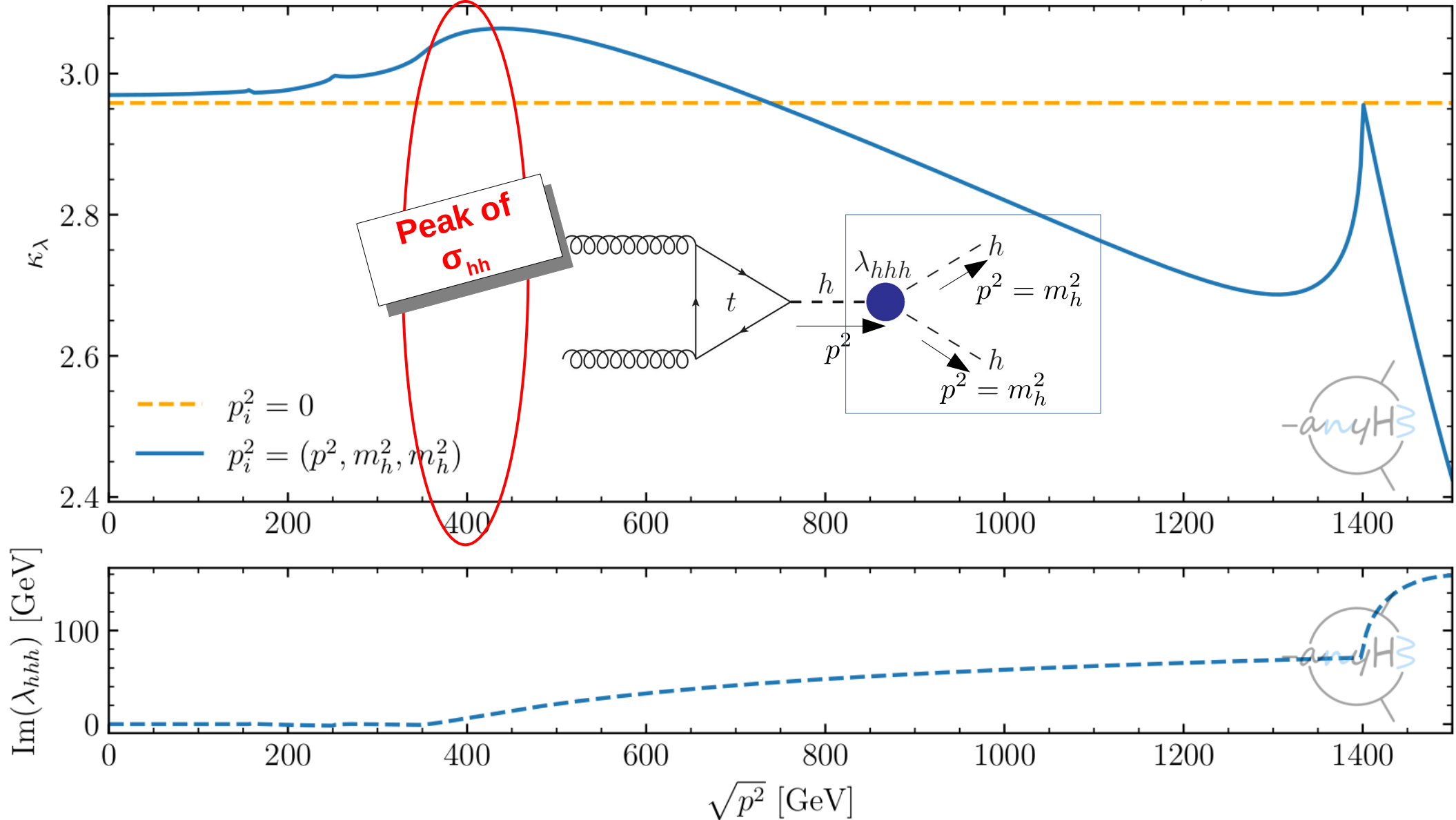
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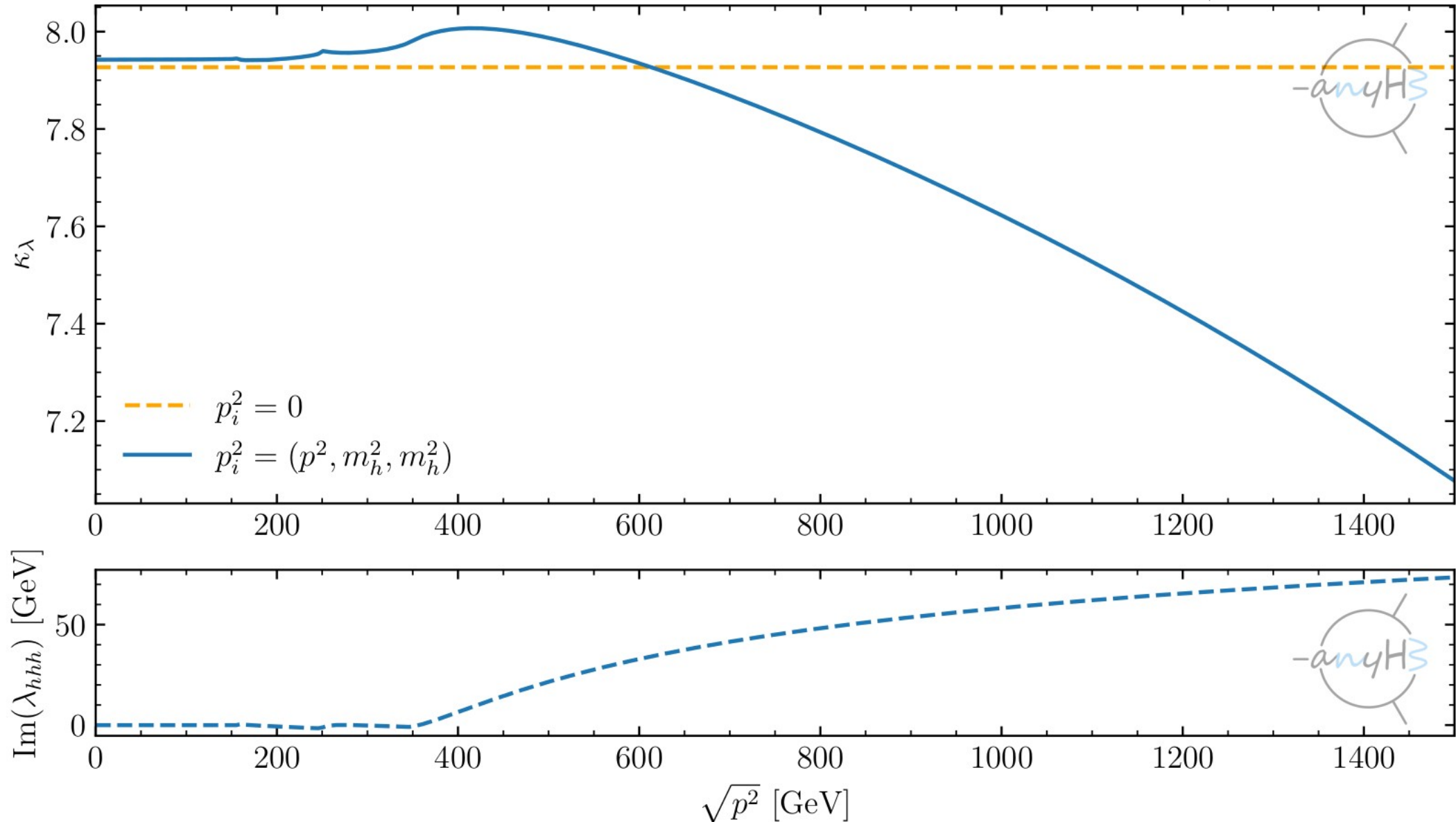
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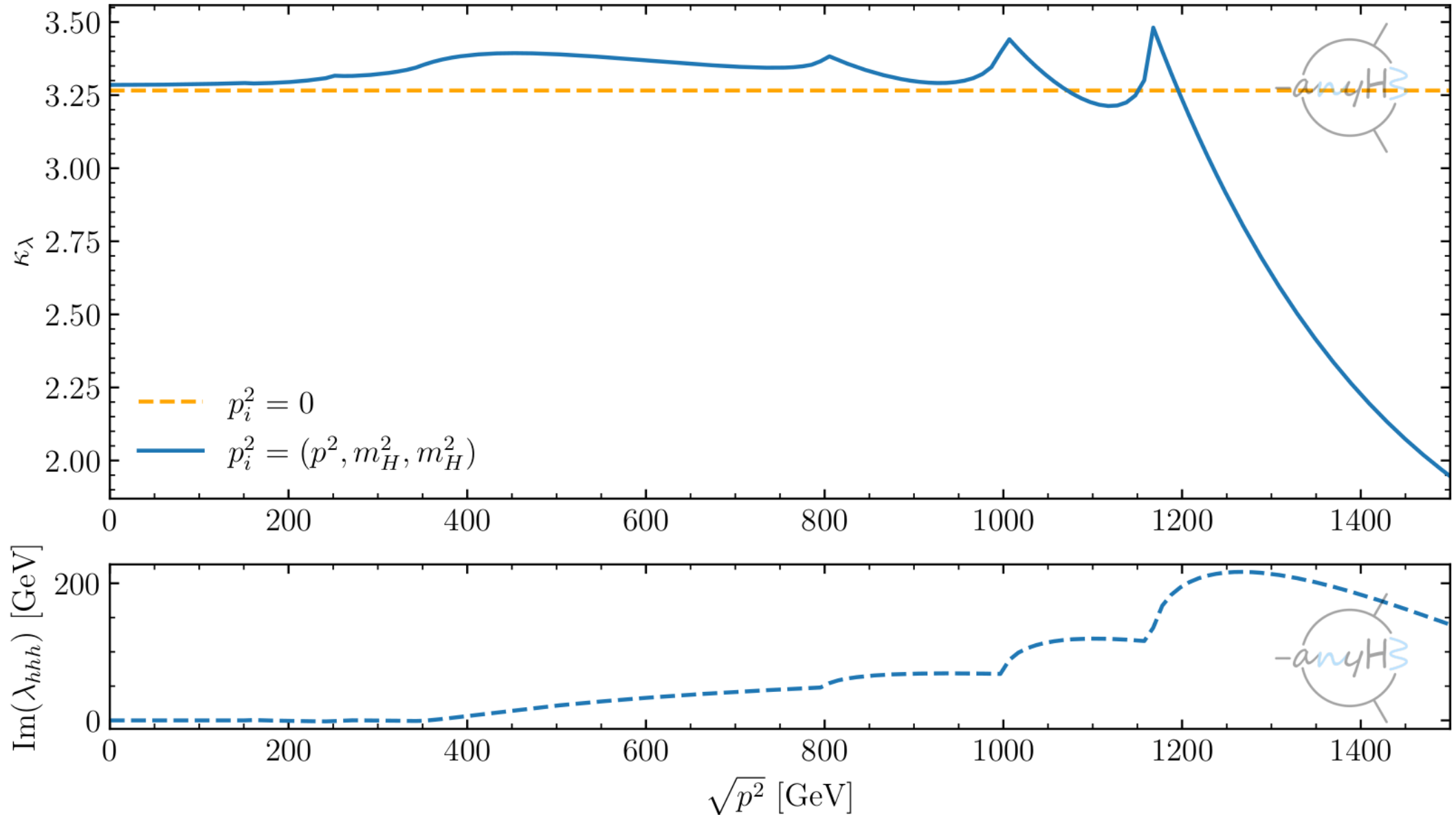
New results II': momentum dependence in the 2HDM

THDM-I: $m_H = M = 600 \text{ GeV}$, $m_A = m_{H^\pm} = 1000 \text{ GeV}$, $t_\beta = 2$



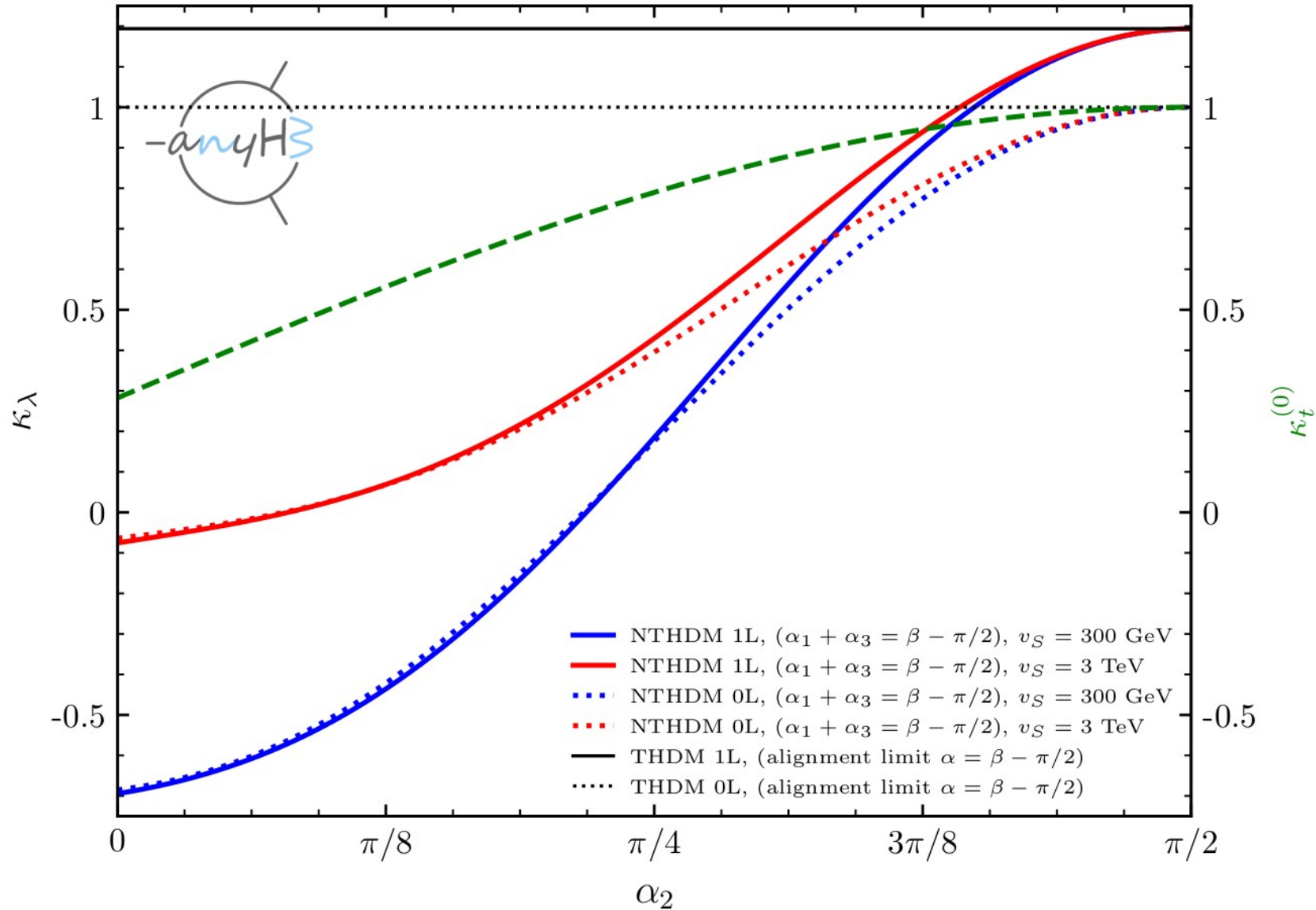
New results III: momentum dependence in a $Y=1$ triplet extension

$Y = 1$ triplet model: $m_{D^{++}} = 400 \text{ GeV}$, $m_{D^\pm} = 500 \text{ GeV}$, $\lambda_4 = 4$



New results IV: an example in the N2HDM

NTHDM: $m_{h_2} = 125.1$ GeV, $m_{h_1} = m_{h_3} = m_A = m_{H^\pm} = 300$ GeV, $\tilde{\mu} = 100$ GeV, $t_\beta = 2$



- N2HDM = 2HDM + real singlet
- CP-even sector: 3 states h_1, h_2, h_3 , with 3 mixing angles $\alpha_1, \alpha_2, \alpha_3$
- Here $\alpha_2 \rightarrow \pi/2 \rightarrow$ recover 2HDM (itself in alignment limit)
- We can study e.g. the relative sign of κ_λ and $\kappa_t \rightarrow$ affects double-Higgs production
- κ_t too far away from 1 excluded

Summary

- λ_{hhh} plays a crucial role to understand the **shape of the Higgs potential**, and probe indirectly **signs of New Physics**
- **Python package anyH3 allows calculation of λ_{hhh} for arbitrary renormalisable theories** with
 - Full 1L effects including p^2 dependence
 - Highly flexible choices of renormalisation schemes → predefined or by user
- Uses **UFO** model inputs (generated with SARAH, FeynRules or using custom ones)
- Analytical results (Python, Mathematica); fast numerical results (with caching): SM → O(0.2s); MSSM → O(0.5s); handles inputs for numerical evaluation in SLHA format (example in backup)
- Part of wider **anyBSM framework**, under development
- Currently 14 models included, easy inclusion of further models → **new ideas/requests welcome!**

**Get started at <https://gitlab.com/anybsm/anybsm>
or directly in terminal with**
`pip install anyBSM !`

Thank you very much for your attention!

Contact

DESY. Deutsches
Elektronen-Synchrotron

Johannes Braathen
DESY Theory group

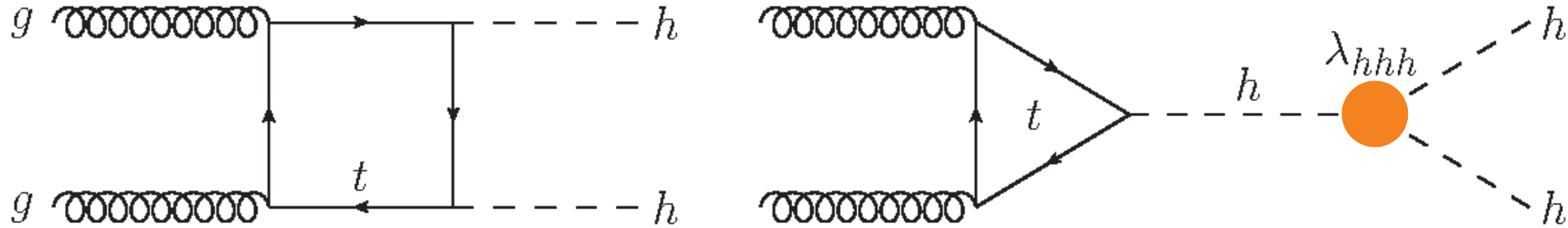
www.desy.de

johannes.braathen@desy.de

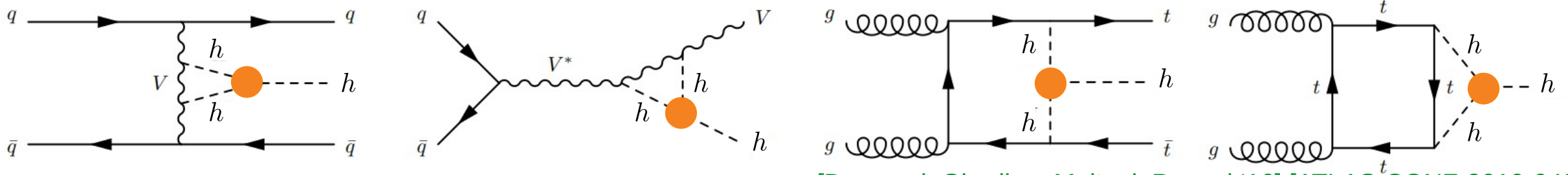
Backup

Experimental probes of λ_{hhh}

- **Double-Higgs production** $\rightarrow \lambda_{hhh}$ enters at leading order (LO) \rightarrow **most direct probe!**

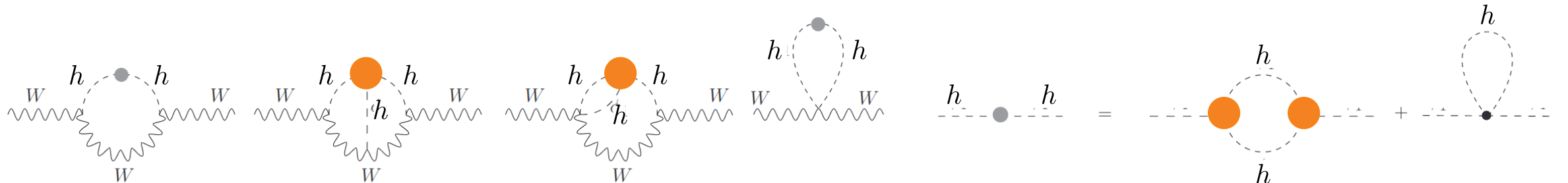


- **Single-Higgs production** $\rightarrow \lambda_{hhh}$ enters at NLO



[Degrassi, Giardino, Maltoni, Pagani '16] [ATLAS-CONF-2019-049]

- **Electroweak Precision Observables (EWPOs)** $\rightarrow \lambda_{hhh}$ enters at NNLO



[Degrassi, Fedele, Giardino '17]

Accessing λ_{hhh} via double-Higgs production

- Double-Higgs production $\rightarrow \lambda_{hhh}$ enters at LO \rightarrow most direct probe of λ_{hhh}

Recent results from ATLAS hh-searches [ATLAS-CONF-2022-050] yield the limits:

$$-0.4 < \kappa_\lambda < 6.3 \text{ at 95\% C.L.}$$

\rightarrow factor ~ 2 improvement compared to

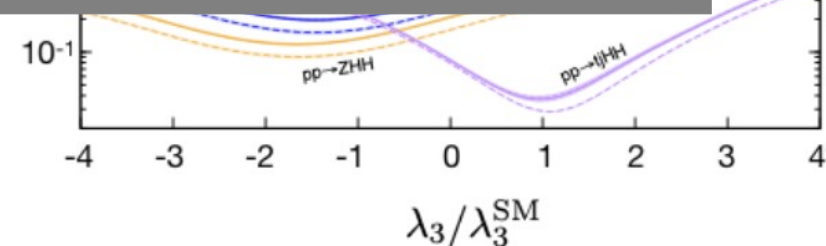
pre-2021 best ATLAS limits (from single-h prod.)

$$-3.2 < \kappa_\lambda < 11.9 \text{ at 95\% C.L. [ATLAS-PHYS-PUB-2019-009]}$$

(CMS recently gave $-1.2 < \kappa_\lambda < 6.5$ at 95% C.L. [CMS '22])

\rightarrow Can κ_λ now be used to constrain the parameter space of BSM models?

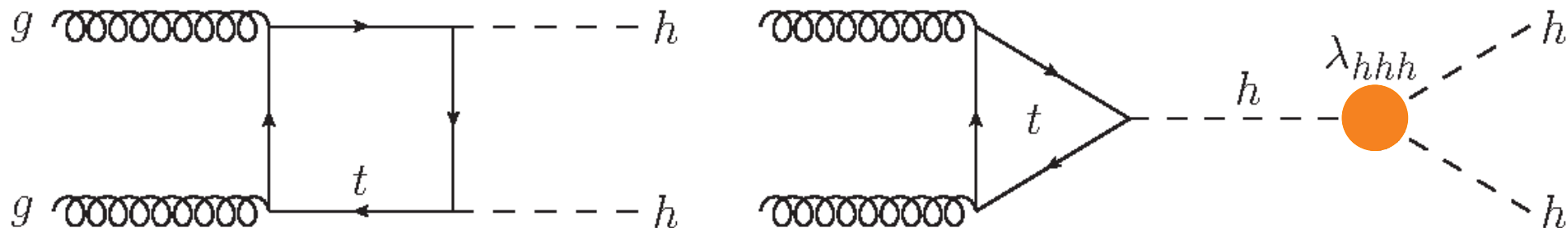
- κ_λ as an effective coupling $\rightarrow \mathcal{L} \supset -\kappa_\lambda \times \frac{\partial \ln v_h}{v^2} \cdot h^3 + \dots$



[Frederix et al., '14]

Accessing λ_{hhh} experimentally

- Double-Higgs production $\rightarrow \lambda_{hhh}$ enters at LO \rightarrow **most direct probe of λ_{hhh}**



- Box and triangle diagrams **interfere destructively**

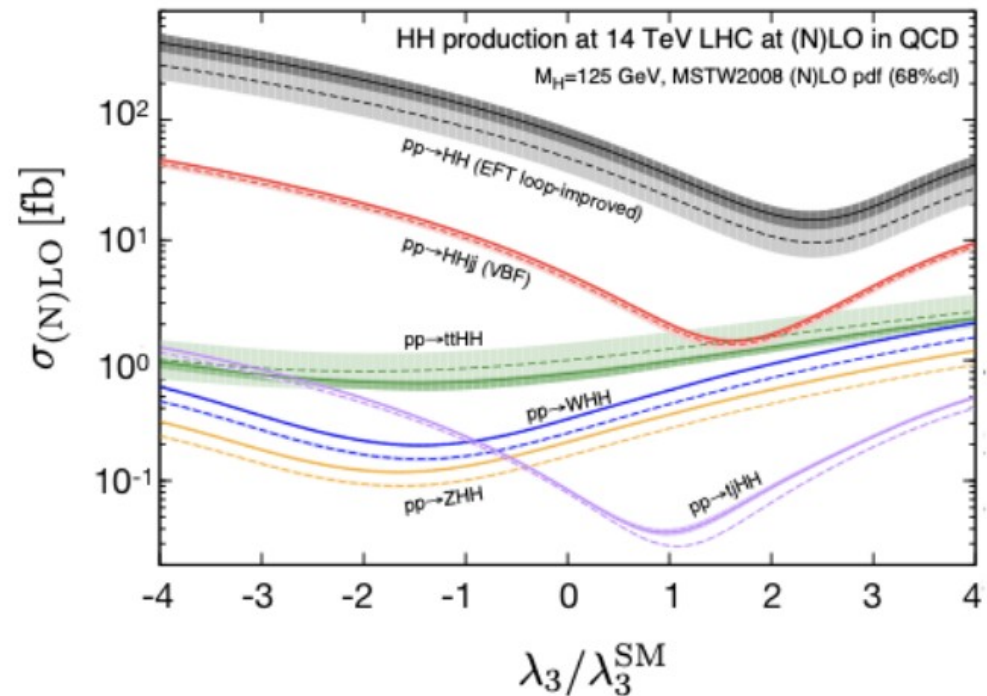
\rightarrow small prediction in SM

\rightarrow BSM deviation in λ_{hhh} can **significantly alter double-Higgs production!**

- Upper limit on double-Higgs production cross-section

\rightarrow **limits on $\kappa_\lambda \equiv \lambda_{hhh}/(\lambda_{hhh}^{(0)})^{SM}$**

- κ_λ as an effective coupling $\rightarrow \mathcal{L} \supset -\kappa_\lambda \times \frac{3m_h^2}{v^2} \cdot h^3 + \dots$



Constraining BSM models with λ_{hhh} – details

Latest experimental bounds

$$-0.4 < \kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})_{SM} < 6.3$$

[ATLAS-CONF-2022-050]

Comparing these bounds with **precise theory predictions** for λ_{hhh} provides a **powerful new way of constraining BSM models**

Assumptions for the extraction of bounds on κ_λ :

- Other couplings of 125-GeV Higgs are SM-like
- Deviation in di-Higgs production cross-section only due to deviation in κ_λ

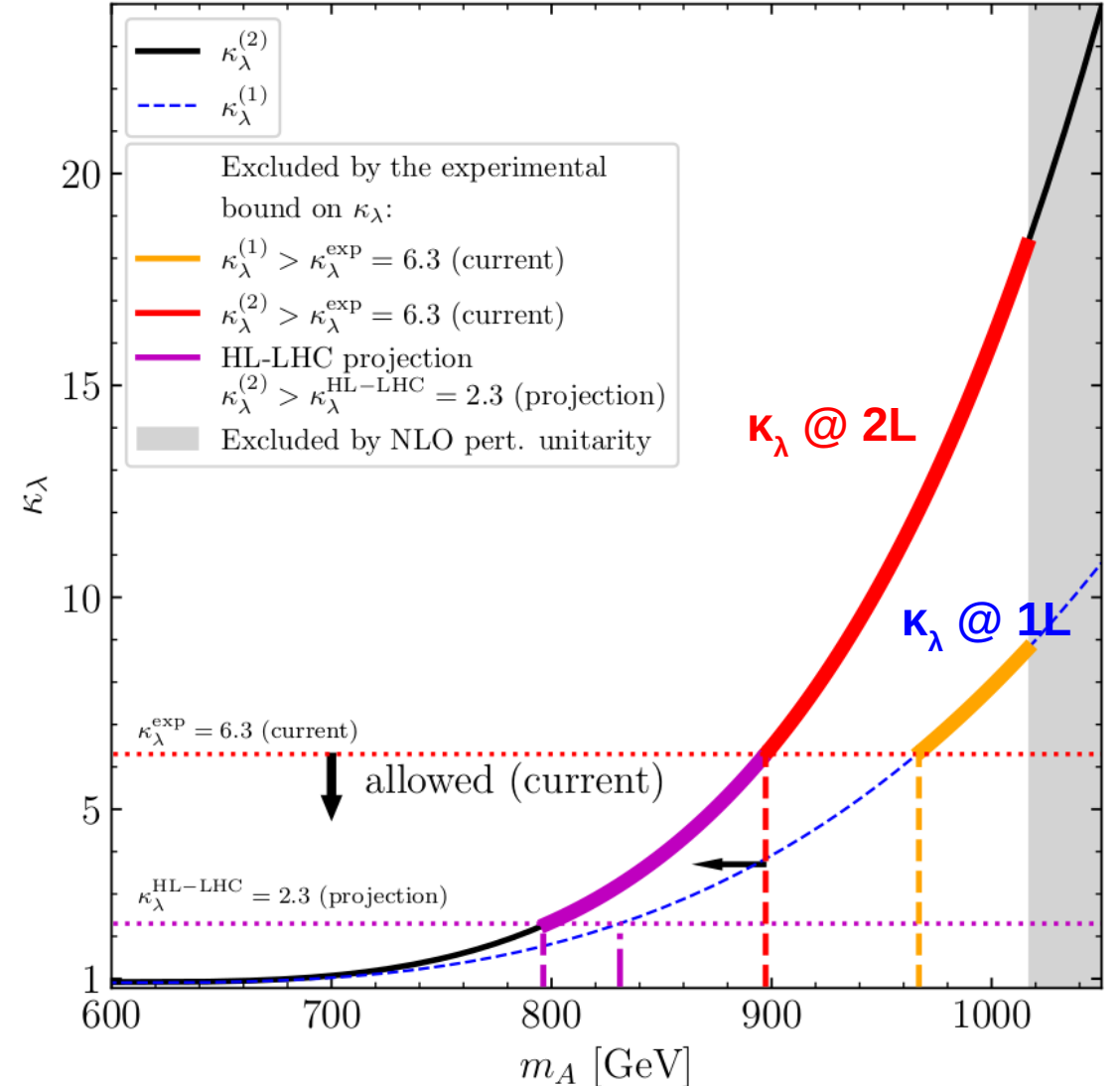
- true for many BSM models, e.g. with **alignment**
- couplings of 125-GeV Higgs SM-like at tree level

E.g. for an aligned 2HDM scenario

[Bahl, JB, Weiglein *Phys.Rev.Lett.* '22]

[Bahl, JB, Weiglein *Phys.Rev.Lett.* '22]

2HDM type I, $\alpha = \beta - \pi/2$, $m_A = m_{H^\pm}$, $M = m_H = 600$ GeV, $\tan \beta = 2$



Future determination of λ_{hhh}

Expected sensitivities in literature, assuming $\lambda_{hhh} = (\lambda_{hhh})^{SM}$

di-Higgs exclusive result

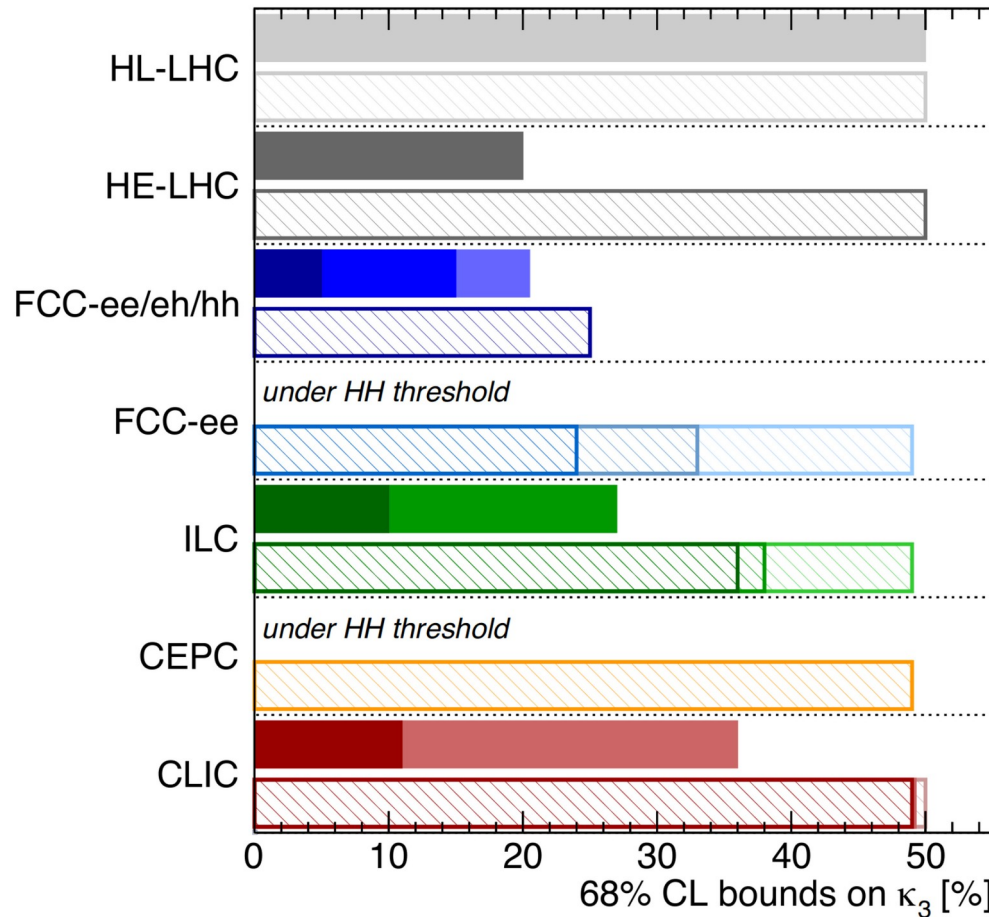
Higgs@FC WG September 2019

di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50% (47%)
HE-LHC [10-20]%	HE-LHC 50% (40%)
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25% (18%)
LE-FCC 15%	LE-FCC n.a.
FCC-eh ₃₅₀₀ -17+24%	FCC-eh ₃₅₀₀ n.a.
	FCC-ee ^{4IP} ₃₆₅ 24% (14%)
	FCC-ee ₃₆₅ 33% (19%)
	FCC-ee ₂₄₀ 49% (19%)
ILC ₁₀₀₀ 10%	ILC ₁₀₀₀ 36% (25%)
ILC ₅₀₀ 27%	ILC ₅₀₀ 38% (27%)
	ILC ₂₅₀ 49% (29%)
	CEPC 49% (17%)
CLIC ₃₀₀₀ -7+11%	CLIC ₃₀₀₀ 49% (35%)
CLIC ₁₅₀₀ 36%	CLIC ₁₅₀₀ 49% (41%)
	CLIC ₃₈₀ 50% (46%)

All future colliders combined with HL-LHC

single-Higgs exclusive

single-Higgs global



Plot taken from
[de Blas et al., 1905.03764]

see also [Cepeda et al., 1902.00134], [Di Vita et al.1711.03978], [Fujii et al. 1506.05992, 1710.07621, 1908.11299], [Roloff et al., 1901.05897], [Chang et al. 1804.07130,1908.00753], etc.

Future determination of λ_{hhh}

Higgs production cross-sections (here double Higgs production) depend on λ_{hhh}

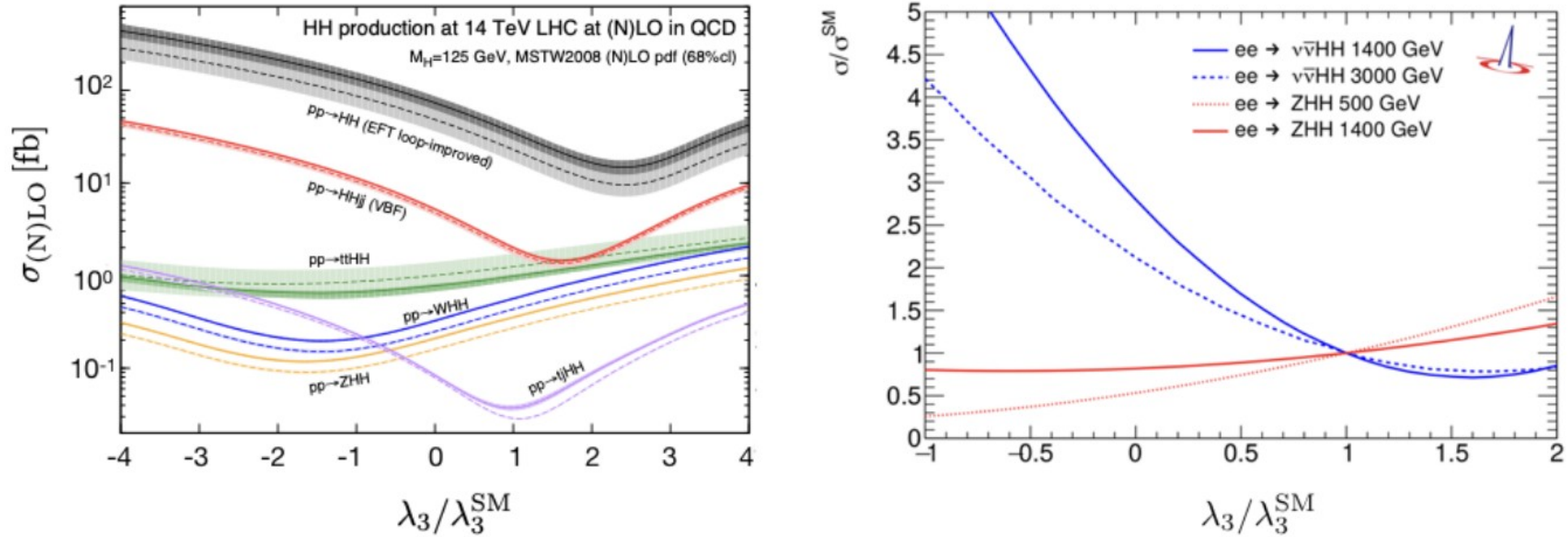


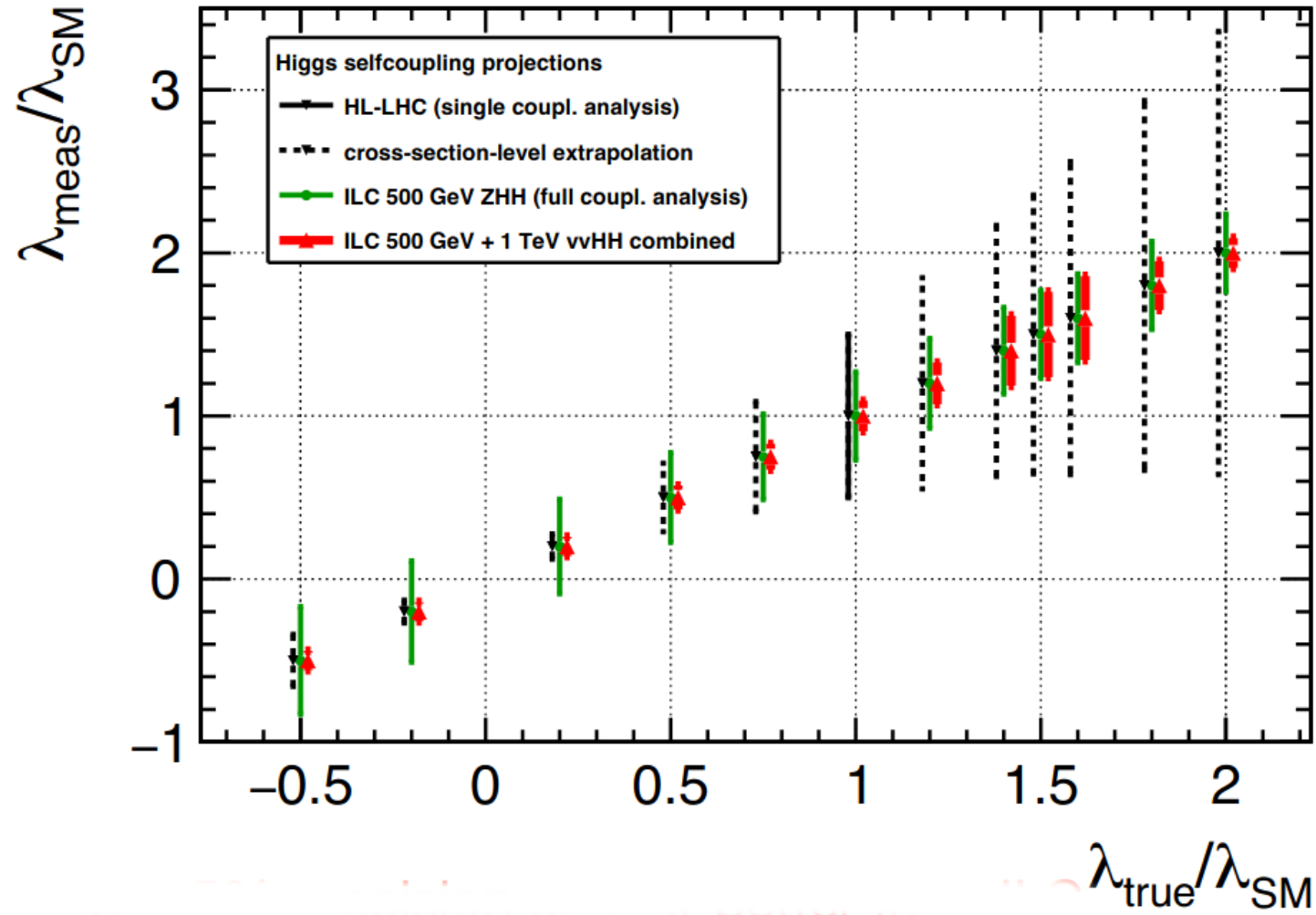
Figure 10. Double Higgs production at hadron (left) [65] and lepton (right) [66] colliders as a function of the modified Higgs cubic self-coupling. See Table 18 for the SM rates. At lepton colliders, the production cross sections do depend on the polarisation but this dependence drops out in the ratios to the SM rates (beam spectrum and QED ISR effects have been included).

Plots taken from
[de Blas et al., 1905.03764]

[Frederix et al.,
1401.7340]

Future determination of λ_{hhh}

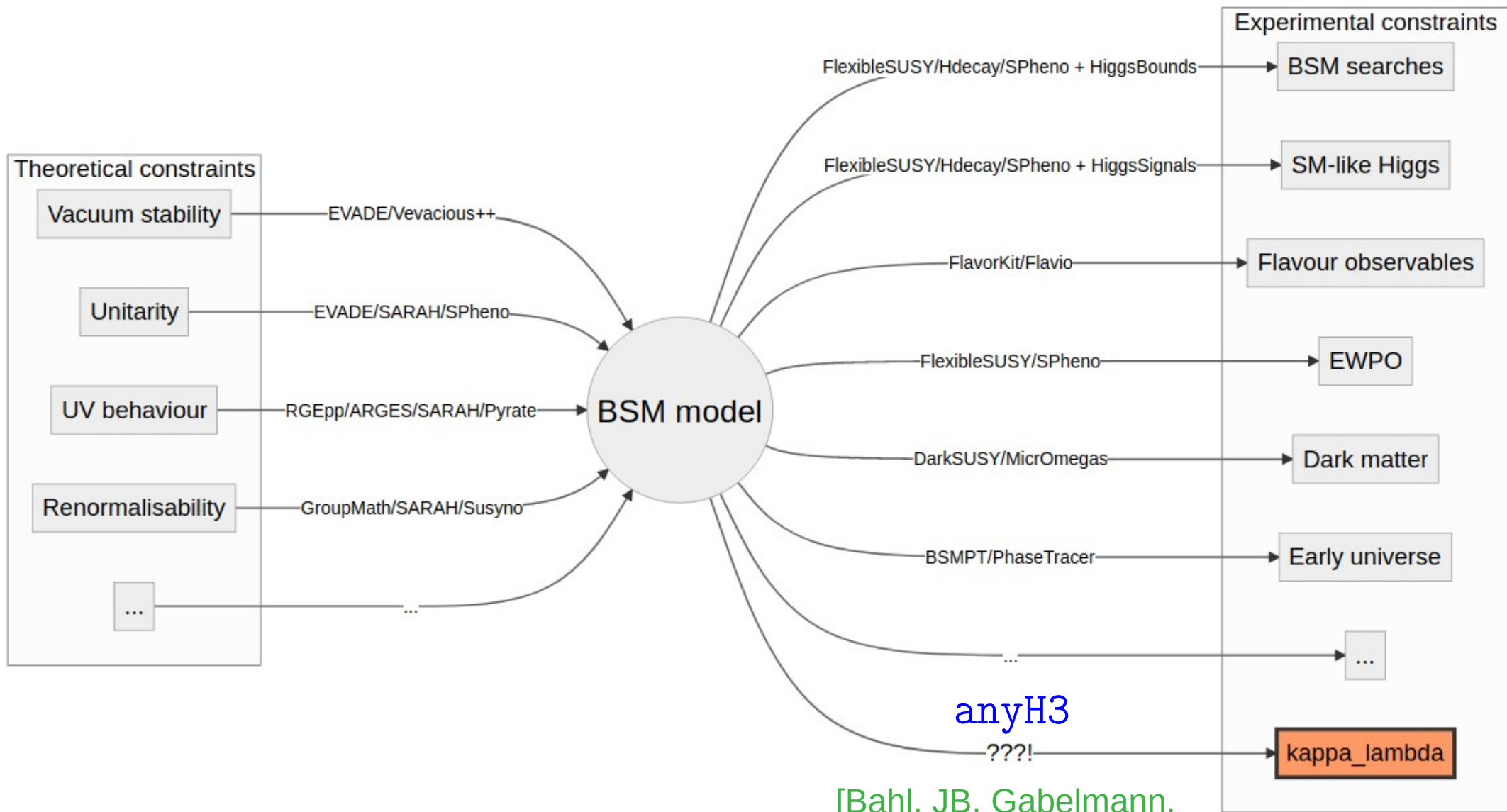
Achieved accuracy actually depends on the value of λ_{hhh}



[J. List et al. '21]

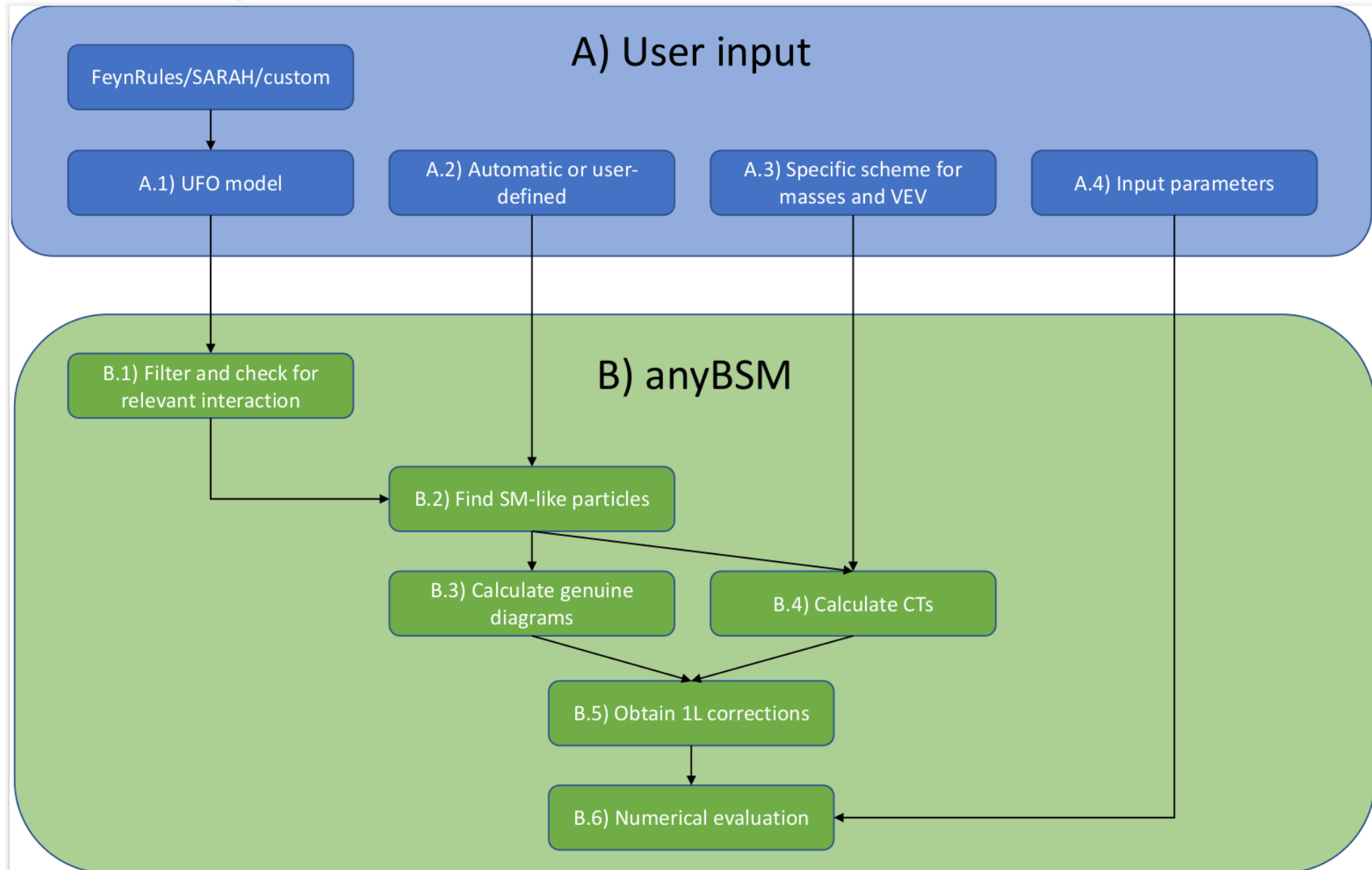
See also [Dürig, DESY-THESIS-2016-027]

λ_{hhh} within the landscape of automated tools



[Bahl, JB, Gabelmann,
Weiglein 2305.03015]

Workflow of anyH3



(Default) Renormalization choice of $(v^{\text{SM}})^{\text{OS}}$ and $(m_i^2)^{\text{OS}}$

> $v^{\text{OS}} \equiv \frac{2M_W^{\text{OS}}}{e} \sqrt{1 - \frac{M_W^{2\text{OS}}}{M_Z^{2\text{OS}}}}$ with

- $\delta^{(1)} M_V^{2\text{OS}} = \frac{\Pi_V^{(1),T}}{M_V^{2\text{OS}}}(p^2 = M_V^{2\text{OS}})$, $V = W, Z$
- $\delta^{(1)} e^{\text{OS}} = \frac{1}{2} \dot{\Pi}_\gamma(p^2 = 0) + \text{sign}(\sin \theta_W) \frac{\sin \theta_W}{M_Z^2 \cos \theta_W} \Pi_{\gamma Z}(p^2 = 0)$

> attention (i): $\rho^{\text{tree-level}} \neq 1 \rightarrow$ further CTs needed (depends on the model)
 \rightarrow ability to define *custom* renormalisation conditions

> scalar masses: $m_i^{\text{OS}} = m_i^{\text{pole}}$

- $\delta^{\text{OS}} m_i^2 = -\widetilde{\text{Re}} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$
- $\delta^{\text{OS}} Z_i = \widetilde{\text{Re}} \frac{\partial}{\partial p^2} \Sigma_{h_i}^{(1)}|_{p^2=m_i^2}$

> attention (ii): scalar mixing may also require further CTs/tree-level relations

All bosonic one- & two-point functions and their derivatives for general QFTs are required for flexible OS renormalisation.

Features of anyH3, so far

- Import/conversion of any UFO model
- Definition of renormalisation schemes

schemes.yml:

```
default_scheme: OSalignment
```

Example for 2HDM

```
renormalization_schemes:
```

```
MS:
```

```
  description: all (B)SM parameters MS
```

```
  SM_names:
```

```
    Higgs-Boson: h1
```

```
  VEV_counterterm: MS
```

```
  mass_counterterms:
```

```
    h1: MS
```

```
    h2: MS
```

```
OSalignment:
```

```
  description:  $\overline{\mathrm{MS}}$  mixing angles  
and OS masses i.e. fully on-shell  $\lambda_{hhh}$  for  $\sin{\beta-\alpha}=1$ 
```

```
  SM_names:
```

```
    Higgs-Boson: h1
```

```
  VEV_counterterm: OS
```

```
  mass_counterterms:
```

```
    h1: OS
```

```
    h2: OS
```

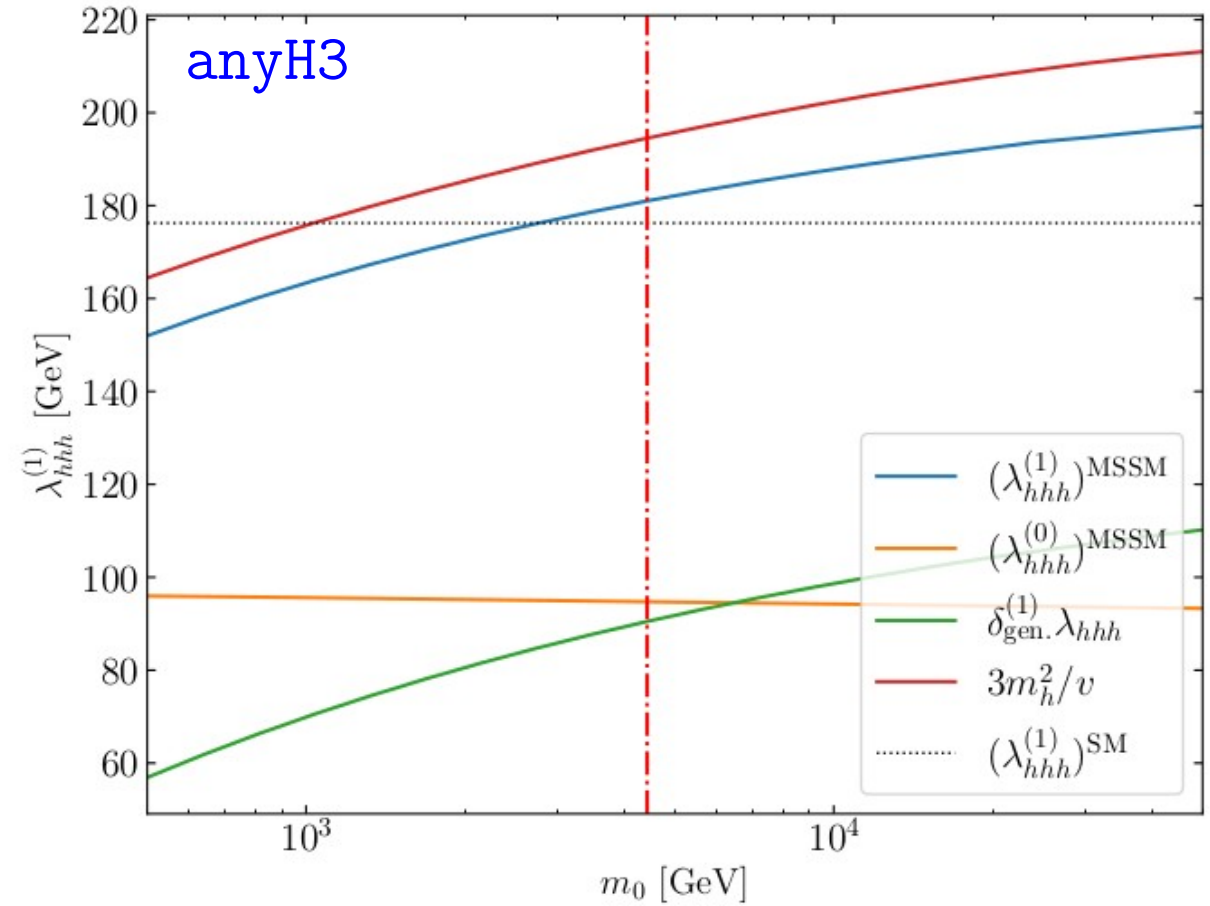
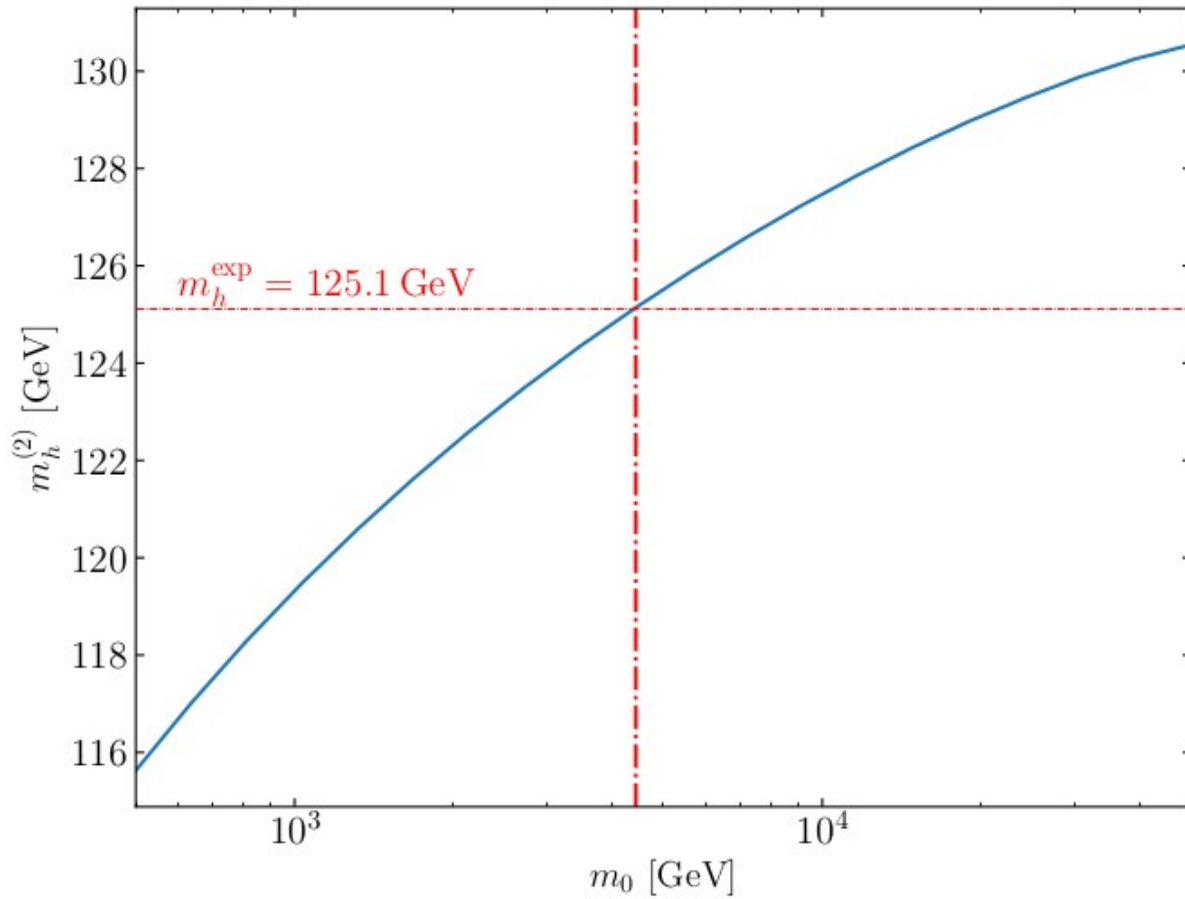
```
OS:
```

```
  description: OS conditions for scalar masses as well
```

- Analytical / numerical / LaTeX outputs
- Restrictions on topologies or on considered particles possible
- **3 user interfaces:**
 - Python library
 - Command line
 - Mathematica interface
- **Perturbative unitarity checks** available (at tree level and in high-energy limit for now)
- Can be used together with a spectrum generator and **handles SLHA format**
- Efficient **caching** available
- Etc.

New results V: full one-loop calculation of λ_{hhh} in the MSSM

CMSSM, $m_0 = m_{1/2} = -A_0$, $\tan\beta = 10$, $\text{sgn}(\mu) = 1$, with m_h computed at 2L in SPheno



- ▶ Example for a very simple version of the constrained MSSM → BSM parameters m_0 , $m_{1/2}$, A_0 , $\text{sgn}(\mu)$, $\tan\beta$
- ▶ For each point, M_h computed at 2L with SPheno, and SLHA output of SPheno used as input of anyH3