

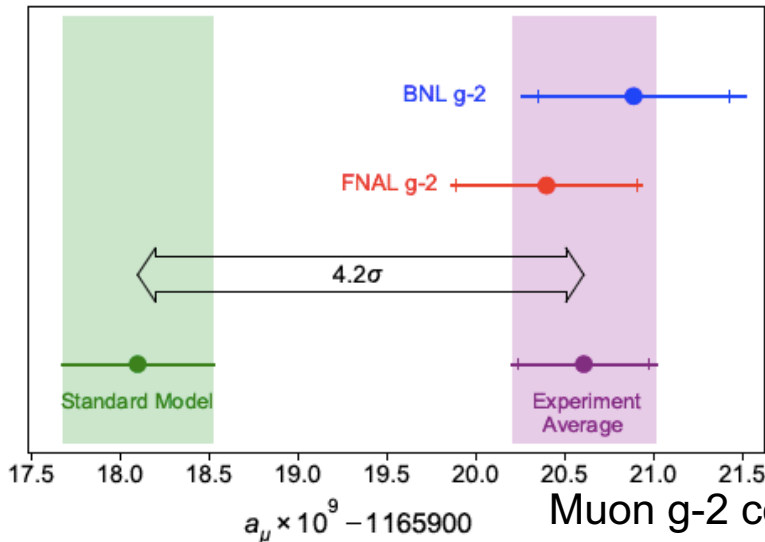
Large $SU(2)$ multiplet scalars providing sizable muon $g-2$ and its phenomenology

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Based on TN, H.Okada, arXiv: 2208.08704

1. Introduction

Muon anomalous dipole magnetic moment (muon g-2)



Muon g-2 collaboration, PRL126 (2021)

$$a_\mu^{BNL} = (11659208.9 \pm 5.4 \pm 3.3) \times 10^{-10}$$

$$a_\mu^{FNAL} = (11659204.0 \pm 5.1 \pm 1.9) \times 10^{-10}$$

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10}$$

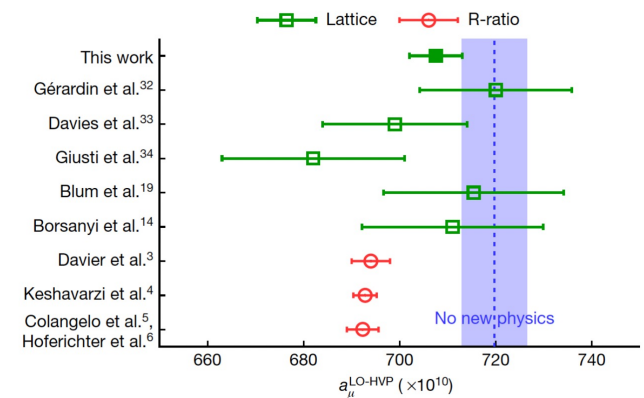
Combined result (4.2 σ deviation)

In fact, it is controversial

Estimation of HVP by Lattice groups: (e.g. BMWc)

Recent $e^+ e^- \rightarrow \pi^+ \pi^-$ measurement :

(CMD3- Collaboration 2302.08834)



Borsanyi et al (BMWc), Nature 2021

⇒ They make SM prediction closer to experimental values ($\sim 1.5\sigma$)

In any case the muon g-2 is good hint/test of new physics

1. Introduction

A simple extension of the SM

 Adding $SU(2)_L$ multiplet scalar/vector-like fermion(VLF)

◆ Extending field contents

◆ Simple extension but rich possibilities in phenomenology

- Generating neutrino masses
- New scalar with VEV → Higgs physics, electroweak precision test
- Explaining experimental anomalies: **muon g-2** etc.
- Collider physics
- Etc.

2. A model

Structure of the model

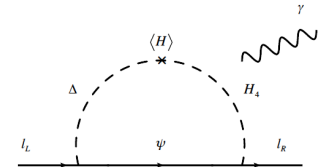
(TN, H.Okada, arXiv: 2208.08704)

	L_{L_i}	e_{R_i}	ψ	H	Δ	H_4
$SU(2)_L$	2	1	4	2	3	4
$U(1)_Y$	$-\frac{1}{2}$	-1	$\frac{1}{2}$	$\frac{1}{2}$	1	$\frac{3}{2}$

New vector-like fermion(VLF) **New scalars**

- ❖ Introduction of Higgs triplet Δ : neutrino mass from type-II seesaw
- ❖ Quartet VLF ψ and scalar H_4 to get muon g-2 with Δ

 Without chiral suppression



Muon g-2 is also enhanced by multiply charged scalars/fermions contributions

- ❖ General 2HDM is simple to get large muon g-2 but FCNC in quark sector
- ❖ Extra doublet for ψ also work but we have unwanted term $\bar{L}_L \psi_L^c$

Phenomenological consequences: LFV, collider physics

2. A model

New Lagrangian of the model

$$-\mathcal{L}_\ell = y_{\ell_{ii}} \bar{L}_{L_i} H e_{R_i} + y_{\nu_{ij}} \bar{L}_{L_i} \Delta^\dagger L_{L_j}^c + y_{D_i} [\bar{L}_{L_i} \Delta^\dagger \psi_R] + f_i [\bar{\psi}_L H_4 e_{R_i}] \\ + g_L [\bar{\psi}_L^c \Delta^\dagger \psi_L] + g_R [\bar{\psi}_R^c \Delta^\dagger \psi_R] + M_\psi \bar{\psi}_L \psi_R + \text{h.c.},$$


$$V = -\mu_H^2 H^\dagger H + \mu_\Delta^2 \text{Tr}[\Delta^\dagger \Delta] + \mu_{H_4}^2 H_4^\dagger H_4 + \lambda_H (H^\dagger H)^2 \\ + (\text{trivial quartet terms including } \Delta \text{ and } H_4) + V_{\text{non-trivial}},$$

$$V_{\text{non-trivial}} = \mu_1 [H^\dagger \Delta^\dagger H_4 + \text{h.c.}] + \mu_2 [H^T \Delta^\dagger H] + \sum \lambda_{H_4 H}^i [H_4^\dagger H H H]_i + \text{h.c.},$$

Fields by components

$$H = (h^+, \tilde{h}^0) \quad H_4 = (\phi_4^{++++}, \phi_4^{+++}, \phi_4^{++}, \phi_4^0)^T, \\ \Delta = \begin{pmatrix} \frac{\delta^+}{\sqrt{2}} & \delta^{++} \\ \delta^0 & -\frac{\delta^+}{\sqrt{2}} \end{pmatrix} \quad \psi_{L(R)} = (\psi^{++}, \psi^+, \psi^0, \psi^-)_{L(R)}^T,$$

Neutral components will develop VEVs $\langle H_4 \rangle = v_4 / \sqrt{2}$ $\langle \Delta \rangle = v_\Delta / \sqrt{2}$

 Constraints from ρ -parameter : $\rho = \frac{v_h^2 + 2v_\Delta^2 + 6v_4^2}{v_h^2 + 4v_\Delta^2 + 9v_4^2}$ $v_X \lesssim 1.55 \text{ GeV}$
 $v_x \equiv v_\Delta = v_4$

2. A model

Masses of new scalar particles

Mass eigenstates (in approximation):

$$\begin{pmatrix} \delta^\pm \\ \phi_4^\pm \end{pmatrix} = \begin{pmatrix} c_\alpha & s_\alpha \\ -s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} H_1^\pm \\ H_2^\pm \end{pmatrix}, \quad \text{Singly charged} \quad H^{\pm\pm\pm} \quad \text{Triply charged}$$
$$\begin{pmatrix} \delta^{\pm\pm} \\ \phi_4^{\pm\pm} \end{pmatrix} = \begin{pmatrix} c_\beta & s_\beta \\ -s_\beta & c_\beta \end{pmatrix} \begin{pmatrix} H_1^{\pm\pm} \\ H_2^{\pm\pm} \end{pmatrix}, \quad \text{Doubly charged}$$
$$\begin{pmatrix} \delta^0 \\ \phi_4^0 \end{pmatrix} = \begin{pmatrix} c_\gamma & s_\gamma \\ -s_\gamma & c_\gamma \end{pmatrix} \begin{pmatrix} H_1^0 \\ H_2^0 \end{pmatrix}, \quad \text{Neutral}$$
$$\tan(2\{\alpha, \beta, \gamma\}) = \frac{2\Delta M_{\{+,++,0\}}^2}{\mu_\Delta^2 - \mu_{H_4}^2}$$

H-H₄ and H-Δ mixing is negligibly small due to small VEVs of H₄ and Δ

Masses:

$$m_{\{H_1^+, H_1^{++}, H_1^0\}}^2 = \frac{1}{2}(\mu_{H_4}^2 + \mu_\Delta^2) - \frac{1}{2}\sqrt{(\mu_{H_4}^2 - \mu_\Delta^2)^2 + 4\Delta M_{\{+,++,0\}}^4}, \quad m_{H^{+++}} = \mu_{H_4}$$
$$m_{\{H_2^+, H_2^{++}, H_2^0\}}^2 = \frac{1}{2}(\mu_{H_4}^2 + \mu_\Delta^2) + \frac{1}{2}\sqrt{(\mu_{H_4}^2 - \mu_\Delta^2)^2 + 4\Delta M_{\{+,++,0\}}^4},$$
$$\Delta M_{\{+,++,0\}}^2 = \left\{ \frac{\sqrt{3}\mu_1 v_h}{3}, \frac{\sqrt{6}\mu_1 v_h}{3}, \mu_1 v_h \right\}$$

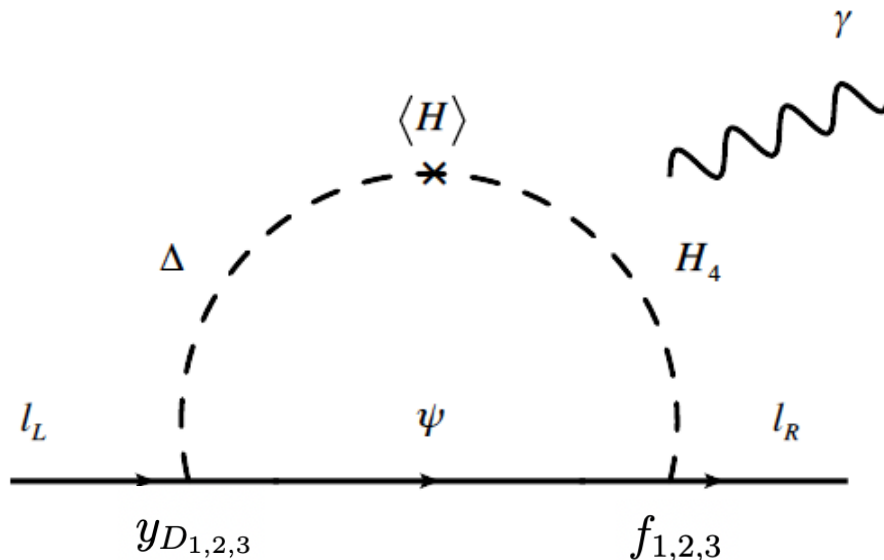
3. Phenomenology of the model

Muon g-2 and LFV processes

Relevant Lagrangian

$$\begin{aligned}
 & f_i [\overline{\psi}_L H_4 e_{R_i}] + y_{D_i} [\overline{L}_{L_i} \Delta^\dagger \psi_R] + h.c. \\
 & = f_i [\overline{\psi}_L^0 \phi_4^+ + \overline{\psi}_L^{++} \phi_4^{+++} + \overline{\psi}_L^+ \phi_4^{++} + \overline{\psi}_L^- \phi_4^0] e_{R_i} \\
 & + \frac{y_{D_i}}{3} [\overline{e}_{L_i} (\sqrt{3} \delta^{0*} \psi_R^- + 3 \delta^{--} \psi_R^+ + \sqrt{6} \delta^- \psi_R^0) + \overline{\nu}_{L_i} (\sqrt{3} \delta^{0*} \psi_R^0 + 3 \delta^{--} \psi_R^{++} + \sqrt{6} \delta^- \psi_R^+)].
 \end{aligned}$$

One-loop diagram inducing muon g-2 and LFVs $l \rightarrow l' \gamma$



Dominant contribution

3. Phenomenology

Muon g-2 and LFV processes

Analytic formula

$$\text{Muon } g-2 : \quad \Delta a_\mu \approx -\frac{m_\mu}{(4\pi)^2} [a_{L22} + a_{R22}]$$

$$\text{LFV decay :} \quad \text{BR}(\ell_i \rightarrow \ell_j \gamma) = \frac{48\pi^3 \alpha_{\text{em}} C_{ij}}{(4\pi)^4 G_{\text{F}}^2 m_{\ell_i}^2} (|a_{R_{ij}}|^2 + |a_{L_{ij}}|^2)$$

Amplitudes:

$$a_{R_{ji}} = -y_{D_j} f_i (-1)^{k-1} \left[\frac{\sqrt{6} s_\alpha c_\alpha}{3} D_a F(m_{c_k}, D_a) + M_\psi \left(s_\beta c_\beta (F(m_{d_k}, M_\psi) - G(m_{d_k}, M_\psi)) + \frac{s_\gamma c_\gamma}{\sqrt{3}} G(m_{h_k}, M_\psi) \right) \right],$$
$$a_{L_{ji}} = -f_j^\dagger y_{D_i}^\dagger (-1)^{k-1} \left[\frac{\sqrt{6} s_\alpha c_\alpha}{3} D_a F(m_{c_k}, D_a) + M_\psi \left(s_\beta c_\beta (F(m_{d_k}, M_\psi) - G(m_{d_k}, M_\psi)) + \frac{s_\gamma c_\gamma}{\sqrt{3}} G(m_{h_k}, M_\psi) \right) \right],$$
$$F(m_a, m_b) \approx \frac{m_a^4 - m_b^4 + 2m_a^2 m_b^2 \ln\left(\frac{m_b^2}{m_a^2}\right)}{2(m_a^2 - m_b^2)^3},$$
$$G(m_a, m_b) \approx -\frac{3m_a^4 + m_b^4 - 4m_a^2 m_b^2 + 2m_a^4 \ln\left(\frac{m_b^2}{m_a^2}\right)}{2(m_a^2 - m_b^2)^3}$$

3. Phenomenology

Neutrino mass generation

We have type-II seesaw and inverse seesaw contributions

$$M_N = \begin{bmatrix} m_\nu^{(II)} & m_D & 0 \\ m_D^T & m_R & M_\psi \\ 0 & M_\psi & m_L \end{bmatrix} \quad \text{Basis is } (\nu_L^c, \psi_R, \psi_L^c)^T$$
$$\left(\begin{aligned} -\mathcal{L}_\ell = & y_{\ell ii} \bar{L}_{L_i} H e_{R_i} + y_{\nu ij} \bar{L}_{L_i} \Delta^\dagger L_{L_j}^c + y_{D_i} [\bar{L}_{L_i} \Delta^\dagger \psi_R] + f_i [\bar{\psi}_L H_4 e_{R_i}] \\ & + g_L [\bar{\psi}_L^c \Delta^\dagger \psi_L] + g_R [\bar{\psi}_R^c \Delta^\dagger \psi_R] + M_\psi \bar{\psi}_L \psi_R + \text{h.c.}, \end{aligned} \right)$$

$$m_\nu^{(II)} \equiv y_\nu v_\Delta, \quad m_D \equiv y_D v_\Delta / \sqrt{3}, \quad m_R \equiv 2g_R v_\Delta / 3, \quad \text{and} \quad m_L \equiv 2g_L v_\Delta / 3$$



$$m_\nu \approx m_\nu^{(II)} + \frac{m_D m_D^T m_L}{M_\psi^2}$$

3. Phenomenology

Numerical analysis

Scanning free parameters

$$M_\psi \supset [10^3, 10^5] \text{ GeV}, \quad m \supset [0.01, 10] \text{ GeV}, \quad \mu_{H_4} = 1.2M_\psi, \quad \mu_\Delta = 0.8M_\psi, \\ \mu_1 \supset [100, \mu_{H_4}] \text{ GeV}, \quad \{|f_2|, |y_{D_2}|\} \supset [0.1, 2.0], \quad \{|f_{1,3}|, |y_{D_{1,3}}|\} \supset [10^{-5}, 0.1],$$

Searching solution to explain muon g-2

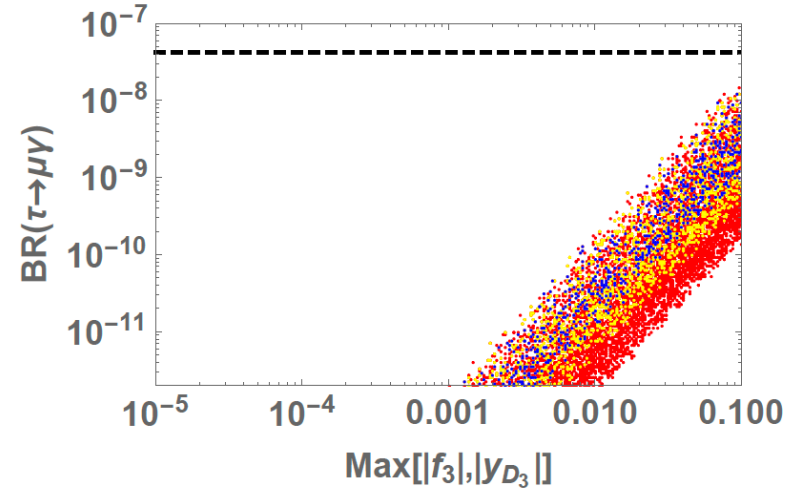
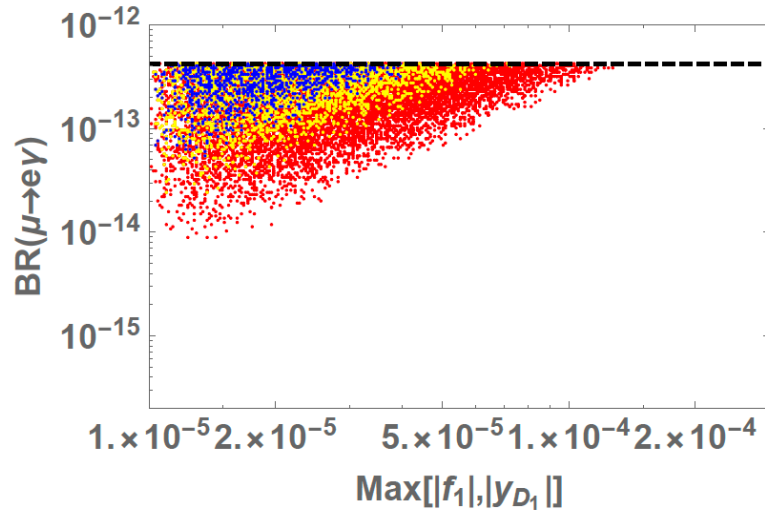
Constraints:

$$\text{BR}(\mu \rightarrow e\gamma) \leq 4.2 \times 10^{-13}, \quad \text{BR}(\tau \rightarrow \mu\gamma) \leq 4.4 \times 10^{-8}, \quad \text{BR}(\tau \rightarrow e\gamma) \leq 3.3 \times 10^{-8}$$

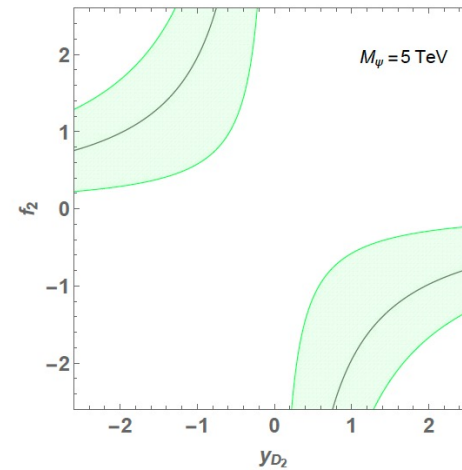
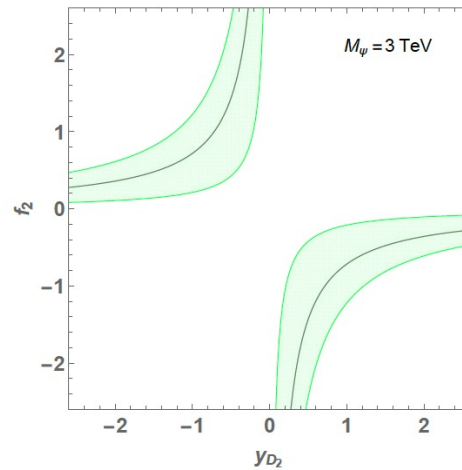
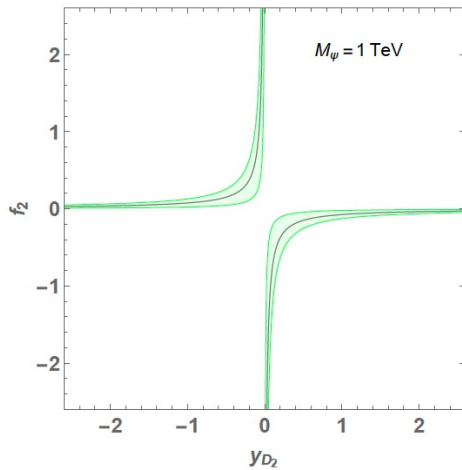
A. M. Baldini *et al.* [MEG], Eur. Phys. J. C **76** (2016) no.8, 434 doi:10.1140/epjc/s10052-016-4271-x [arXiv:1605.05081 [hep-ex]].

3. Phenomenology

Muon g-2, $\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, and parameters



Blue: 1 σ , Yellow: 2 σ , Red: 3 σ for $\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.1 \pm 5.9) \times 10^{-10}$



Region giving 3 σ of muon g-2 fixing some parameters

$$\mu_1 = \mu_{H_4} = 1.2M_\psi, \mu_\Delta = 0.8M_\psi, m = 10 \text{ GeV and } y_{D_{1,3}} = f_{1,3} = 0$$

3. Phenomenology

Multi-charged particle signature at the LHC

$$pp \rightarrow Z / \gamma \rightarrow \psi^{++} \psi^{--}, H^{+++} H^{---}$$

Width of dominant decay channel (assuming mass relation)

$$\Gamma(H^{+++} \rightarrow \ell^+ \psi^{+++}) = \frac{f_\ell^2}{16\pi} m_{H^{+++}} \left(1 - \frac{M_\psi^2}{m_{H^{+++}}^2} \right)^2$$

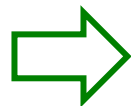
$$\Gamma(\psi^{++} \rightarrow \nu_\ell \delta^{++}) = \frac{y_\ell^2}{8\pi} M_\psi.$$

Decay chain at the experiments

$$\psi^{++} \overline{\psi^{++}} \rightarrow \nu \bar{\nu} \delta^{++} \delta^{--} \rightarrow \nu \bar{\nu} W^+ W^+ W^- W^-,$$

$$H^{+++} H^{---} \rightarrow \ell^+ \ell^- \psi^{++} \overline{\psi^{++}} \rightarrow \ell^+ \ell^- \nu \bar{\nu} \delta^{++} \delta^{--} \rightarrow \ell^+ \ell^- \nu \bar{\nu} W^+ W^+ W^- W^-,$$

Signal events

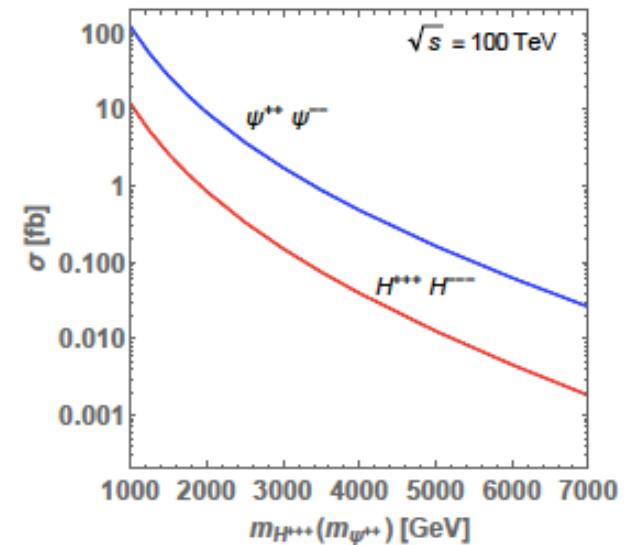
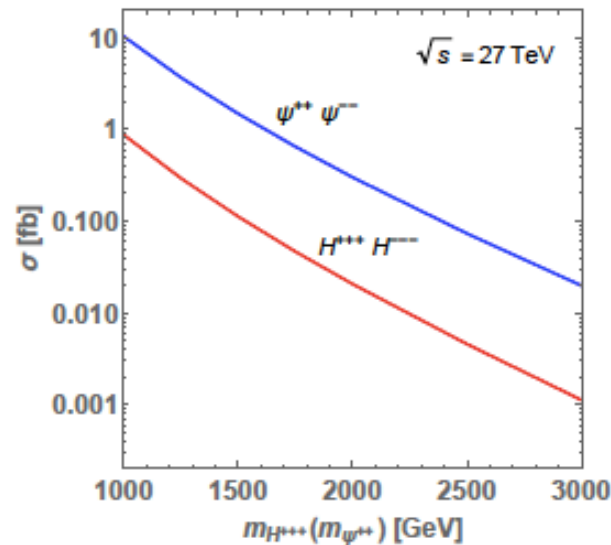
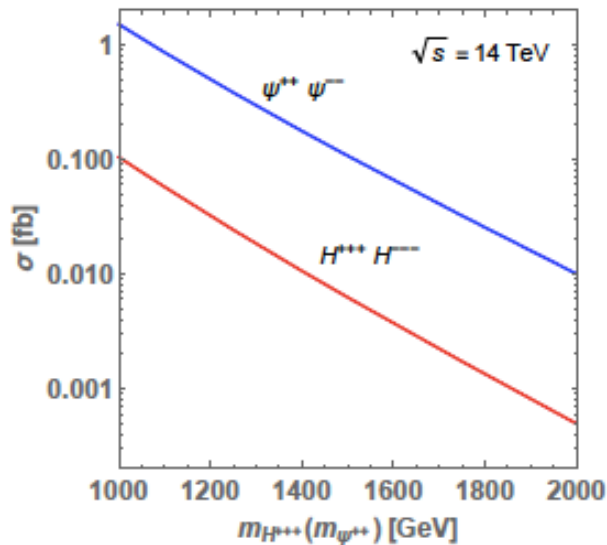


$$\text{Signal 1: } \ell^\pm \ell^\pm 4j \cancel{E}_T,$$

$$\text{Signal 2: } \ell^\pm \ell^\pm \ell^\pm \ell^\mp 4j \cancel{E}_T$$

3. Phenomenology

Signal cross sections



Backgrounds

$$pp \rightarrow \{ZZZ, ZW^+W^-, ZZW^\pm, ZZZZ, W^+W^-W^+W^-, ZZW^+W^-, ZZZW^\pm\}$$

$$\sigma(pp \rightarrow ZZZ) = 10.3 \text{ fb}, \quad \sigma(pp \rightarrow ZW^+W^-) = 9.44 \text{ fb}, \quad \sigma(pp \rightarrow ZZW^+) = 19.9 \text{ fb}$$

$$\sigma(pp \rightarrow ZZW^-) = 10.4 \text{ fb}, \quad \sigma(pp \rightarrow ZZZZ) = 1.95 \times 10^{-2} \text{ fb},$$

$$\sigma(pp \rightarrow W^+W^-W^+W^-) = 0.571 \text{ fb}, \quad \sigma(pp \rightarrow ZZW^+W^-) = 0.436 \text{ fb},$$

$$\sigma(pp \rightarrow ZZZW^+) = 4.21 \times 10^{-2} \text{ fb}, \quad \sigma(pp \rightarrow ZZZW^-) = 1.87 \times 10^{-2} \text{ fb}, \quad \sqrt{s} = 14 \text{ TeV}$$

We generate events by MADGRAPH5 with Pythia8 and Delphes

3. Phenomenology

Numerical simulation choosing signal : $\ell^\pm \ell^\pm +$ at least 3 jets

Number of events before and after kinematical cuts for event selection of $\ell^- \ell^- +$ jets

	N_{signal}	N_{ZZZZ}	N_{ZW+W-}	N_{ZZW^\pm}	N_{4Z}	N_{2W+W-}	N_{ZZW+W-}	N_{ZZZW^\pm}	S
Without cuts	33.4	7.83	13.6	53.5	0.0819	10.3	3.02	0.313	3.36
With cuts	26.0	0.824	3.02	4.58	0.0164	2.27	0.820	0.0572	6.04

$$M_\psi = 1000 \text{ GeV}$$

$$M_\delta = 500 \text{ GeV}$$

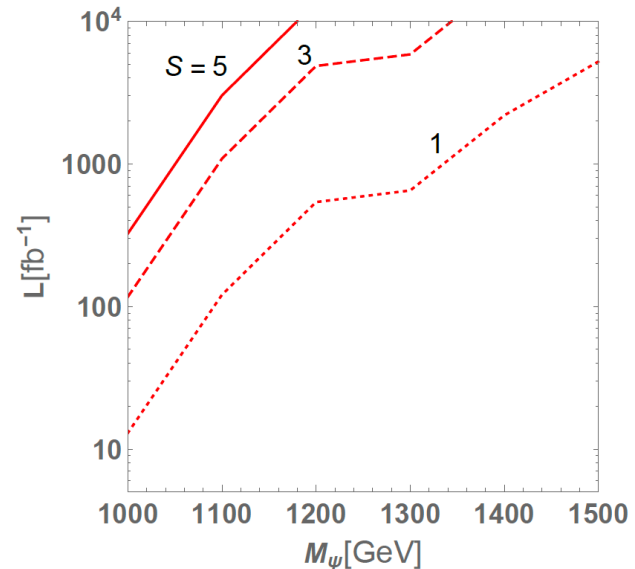
$$\sqrt{s} = 14 \text{ TeV}$$

Kinematical cuts : $p_T(\ell_1^\pm) > 100 \text{ GeV}$, $\cancel{E}_T > 100 \text{ GeV}$

$$L = 1 \text{ ab}^{-1}$$

Required luminosity to test the signal :

$$S = \sqrt{2 \left[(N_S + N_{BG}) \ln \left(1 + \frac{N_S}{N_{BG}} \right) - N_S \right]}$$



Further kinematical cuts would improve significance

Summary

Extension of the SM with extra $SU(2)_L$ multiplets

- ✓ Neutrino mass generation (mainly type-II seesaw)
- ✓ Muon $g-2$ without chiral suppression
- ✓ Multiply charged particles
- ✓ Small mixing between new scalar and SM Higgs
 - Due to small VEVs of large multiplet scalars

□ Phenomenology

- ✓ Muon $g-2$ and LFV
- ✓ Collider physics

possible signatures at the (HL-)LHC

We can have signatures at future collider experiments

Appendix

VEVs of scalar fields

$$\frac{\partial V}{\partial v_h} = \frac{\partial V}{\partial v_\Delta} = \frac{\partial V}{\partial v_4} = 0.$$



$$v_h \simeq \sqrt{\frac{\mu_H^2}{\lambda_H}}, \quad v_\Delta \simeq \frac{1}{\mu_\Delta^2} \left(\frac{1}{3} \sqrt{\frac{3}{2}} \mu_1 v_4 v_h + \mu_2 v_h^2 \right), \quad v_4 \simeq \frac{1}{3} \sqrt{\frac{3}{2}} \frac{\mu_1 v_\Delta v_h}{\mu_{H_4}^2}.$$

Small VEVs for triplet and quartet can be naturally achieved

Signal and BG distributions

