

# **Beam-Based Alignment in the FCC-ee**

**Jacqueline Keintzel**

**Acknowledgements: Michael Benedikt, Tor Raubenheimer,  
Rogelio Tomas, Leon van Riesen-Haupt, Frank Zimmermann**

**Optics Tuning for Future Colliders Workshop**

**CERN, Geneva, Switzerland**

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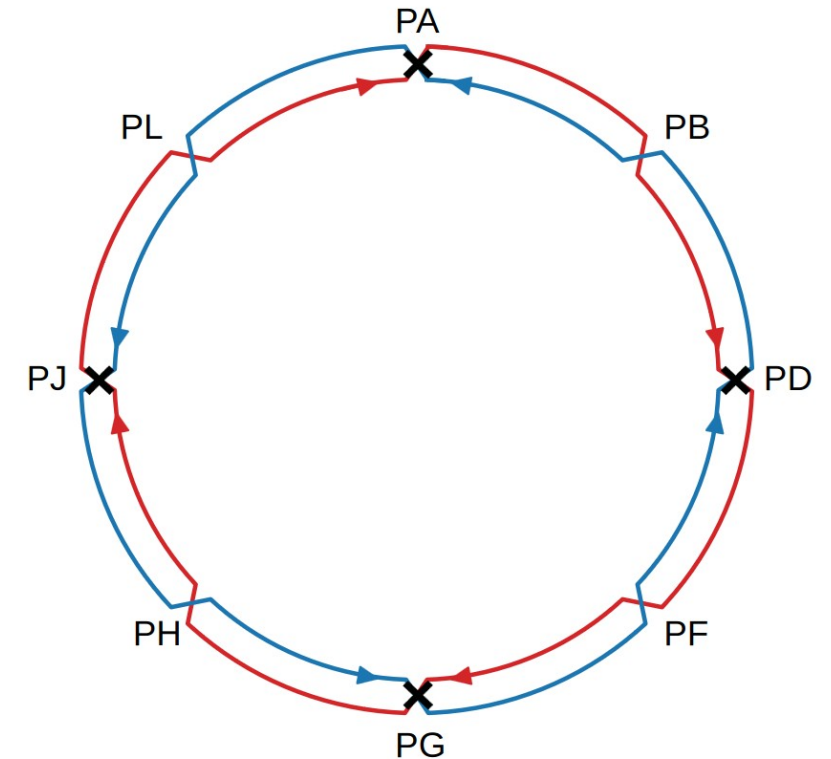
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**FCCIS – The Future Circular Collider Innovation Study.**  
This INFRADEV Research and Innovation Action project receives funding from the European Union's H2020 Framework Programme under grant agreement no. 951754.

# Overview FCC-ee

- 4-fold superperiodicity, super-symmetry and possible Interaction Points (IPs)
- Designed for high precision physics experiments
  - Center-of-mass energy ( $E_{\text{CM}}$ ) and boost determination
    - → ECM calibration, polarization and monochromatization
- Well controlled orbit and optics
  - → Optics tuning team



# Achieving the Design Values

- Mechanical alignment
- Orbit and optics measurements
- Beam based alignment
- Optics and emittance tuning

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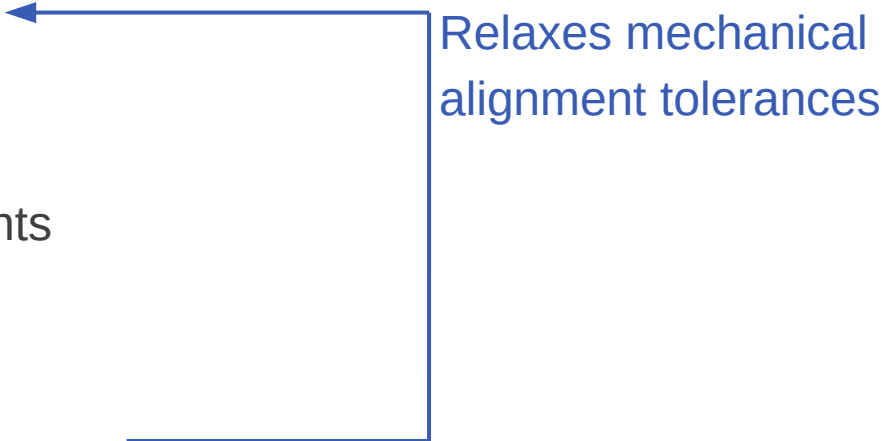
Challenging and time consuming for ~ 100 km circular machine

Extrapolation:  
25 teams in 4 months for main components

Talk: H. Mainaud Durand

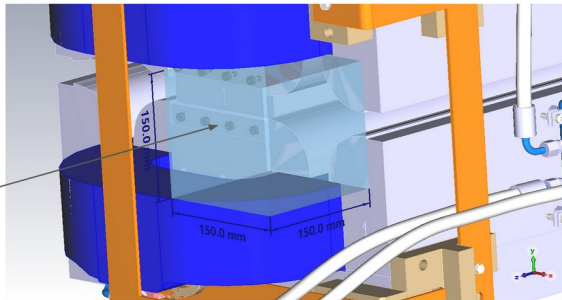
Idea/Goal:  
Relax mechanical alignment tolerances and use beam for alignment

# Achieving the Design Values

- Mechanical alignment
  - Orbit and optics measurements
  - **Beam based alignment**
  - Optics and emittance tuning
- 
- Relaxes mechanical alignment tolerances
- The diagram consists of a blue line that starts from the right side of the 'Beam based alignment' bullet point, extends horizontally to the right, then turns 90 degrees upwards, and finally turns 90 degrees to the left, ending with an arrowhead pointing towards the 'Mechanical alignment' bullet point.

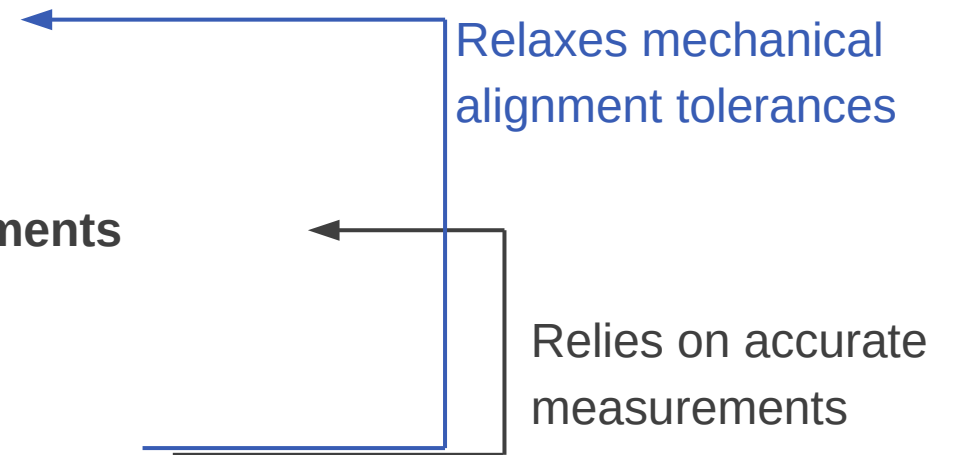
# Achieving the Design Values

Beam based measurements depend on precision of beam instrumentations (BPMs, etc.)

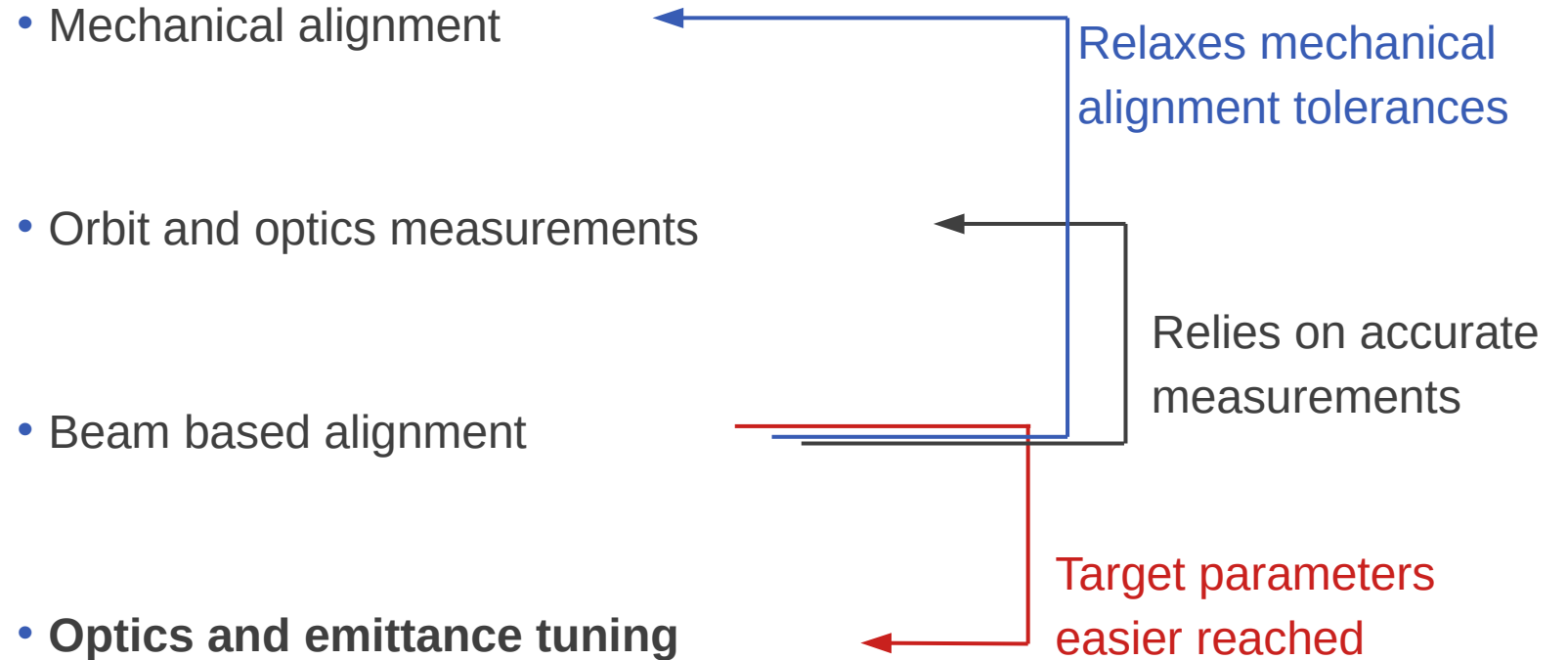


Courtesy: M. Wendt

- Mechanical alignment
- **Orbit and optics measurements**
- **Beam based alignment**
- Optics and emittance tuning

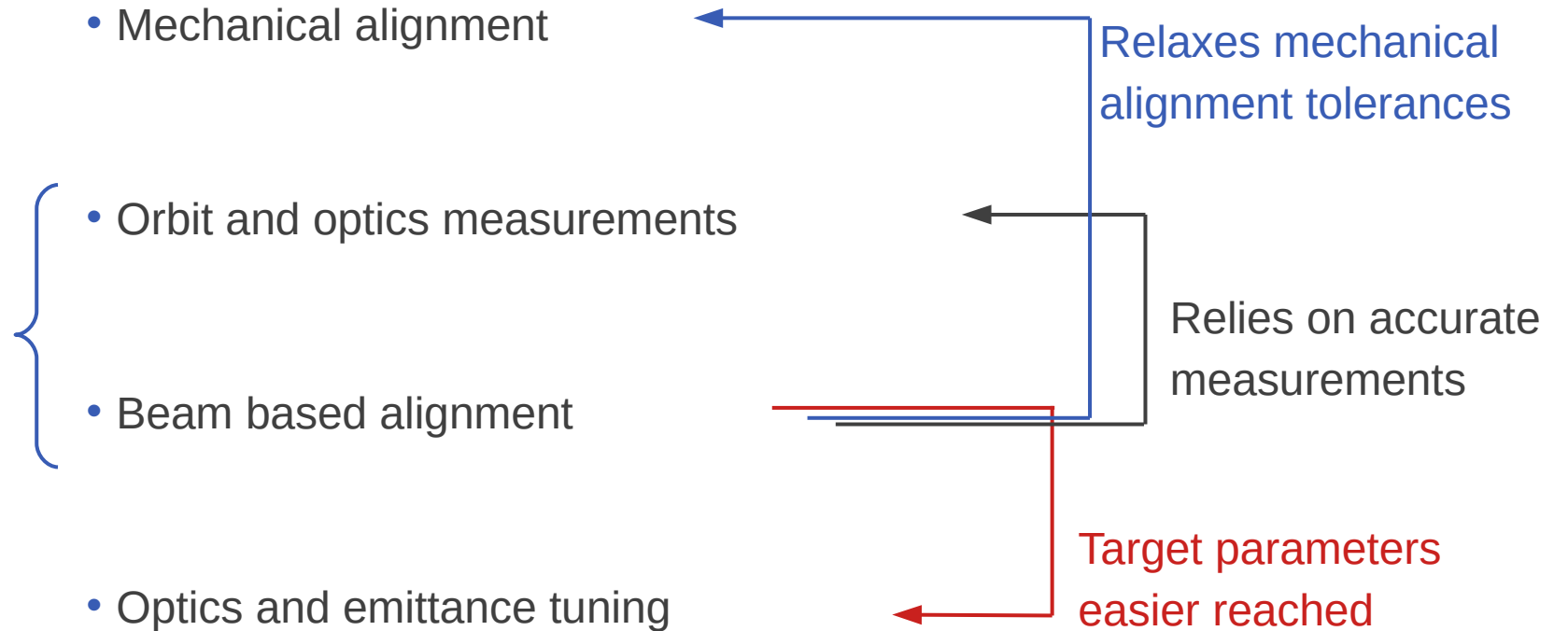


# Achieving the Design Values



# Achieving the Design Values

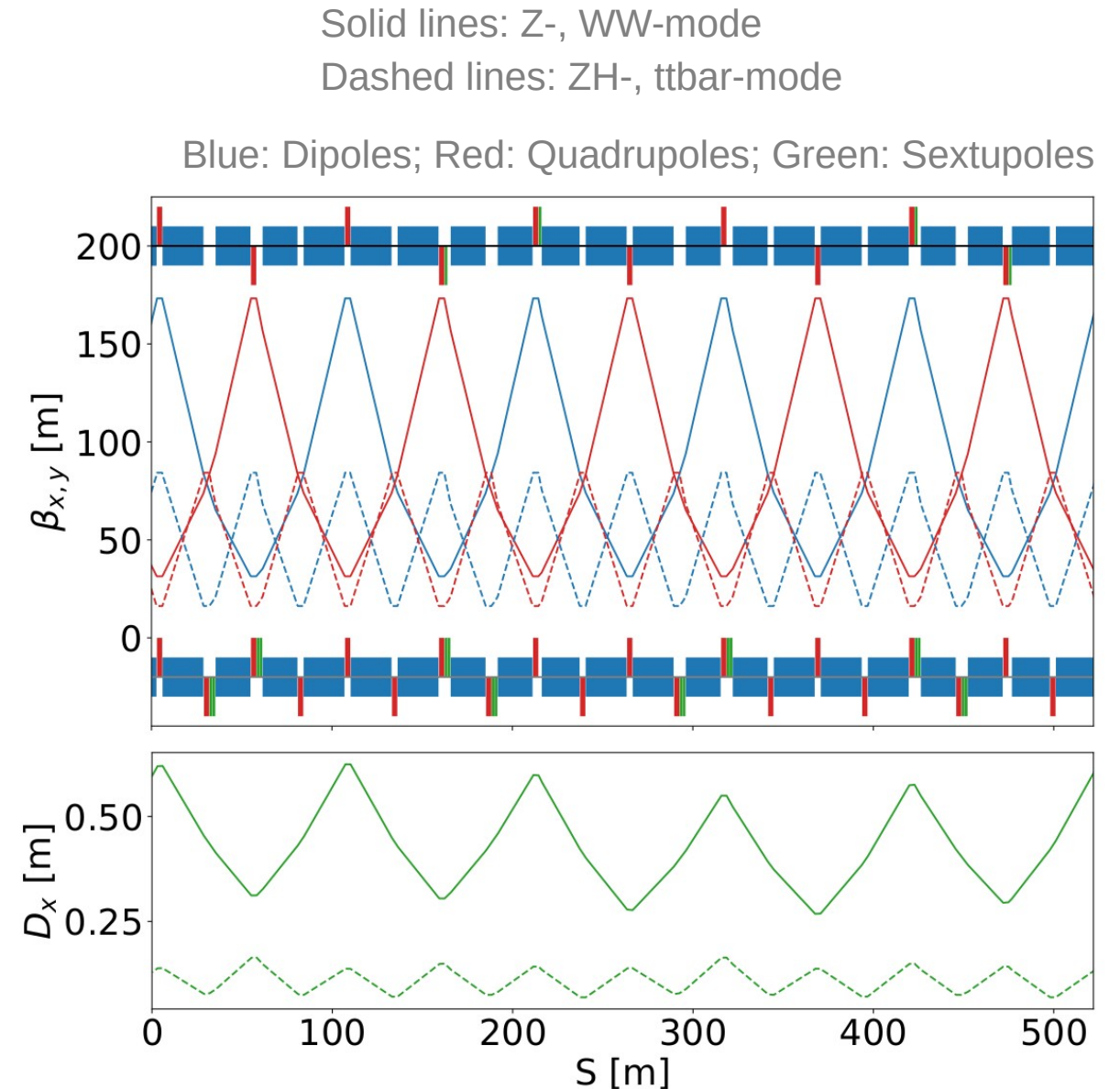
Explored here with  
focus on the arcs for  
the Z-lattice





# Arc Lattice

- Periodic FODO-cell structure
- Make up about 80 % of the FCC-ee lattice
- Dipole lengths: 20 - 30 m
- Quadrupole lengths: 2.9 m or 1.8 m
- Placement and number of orbit correctors and BPMs to be decided



# Short Straight Section

## Arc Sextupoles (S.)

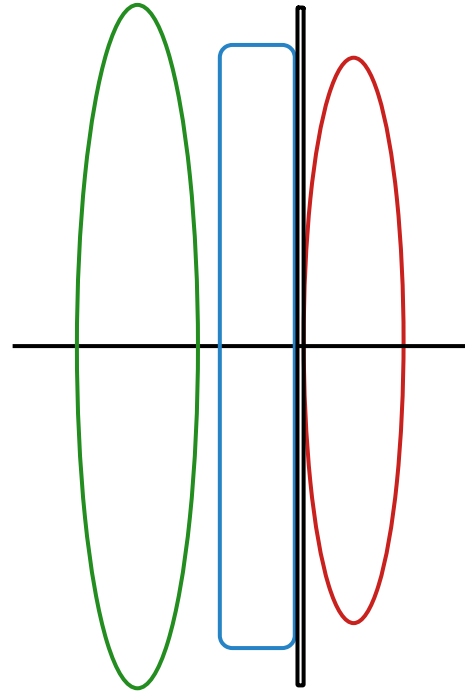
- ~ 600 elements installed
- Non-interleaved scheme
- Strong impact on optics
- More critical than quadrupoles

## Orbit correctors (C.)

- ~ 1500 elements installed
- 10 cm length
- Individual H and V trim
- Here: no strength limit

## BPM

- ~ 1500 elements installed
- H and V measurement
- Here: 0 m length



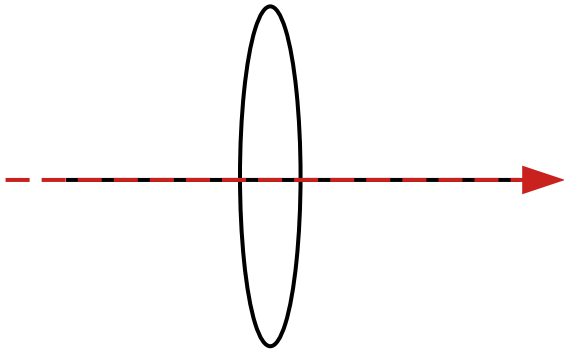
## Arc quadrupole (Q.)

- ~ 1500 arc quadrupoles
- In series with other quadrupoles of same type
- Additional individually powered trim circuit installed

# Principle of Beam Based Alignment

**Goal for FCC-ee: 10  $\mu\text{m}$  residual alignment for arc quadrupoles and sextupoles**

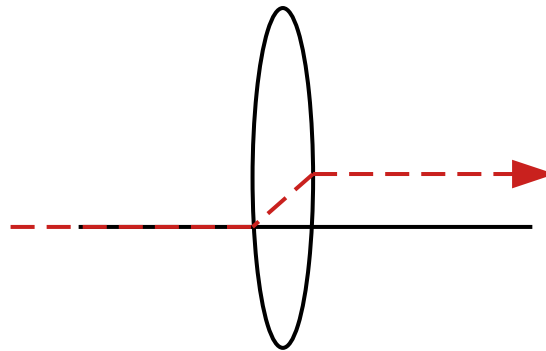
Example: quadrupole with transverse offset



## Aligned quadrupole

Beam passed through center

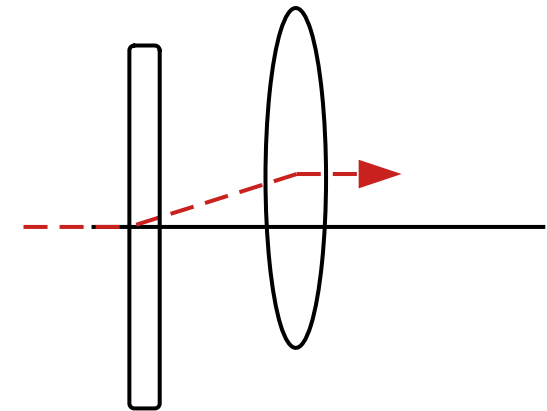
Quadrupole modulation does not change orbit



## Misaligned quadrupole

- Beam does not pass through center
- Leads to dipole kick due to feed-down
- Orbit offset propagates to other elements

Quadrupole modulation changes orbit



## Misaligned quadrupole and adjusted orbit kicker

- Beam passes through center again
- No feed-down from this quadrupole
- Orbit offset propagates to other elements

Quadrupole modulation does not change orbit

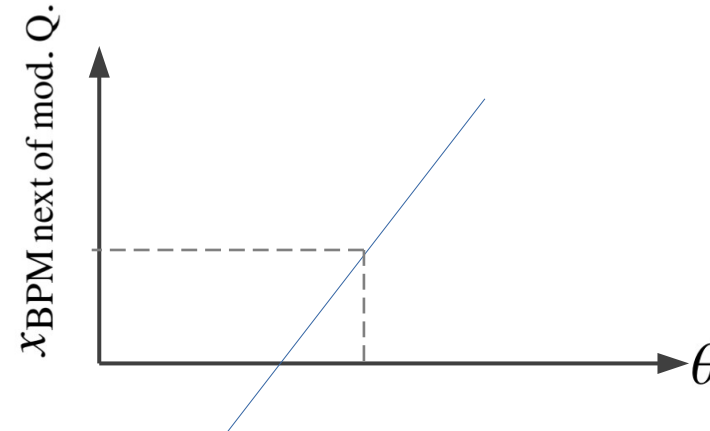
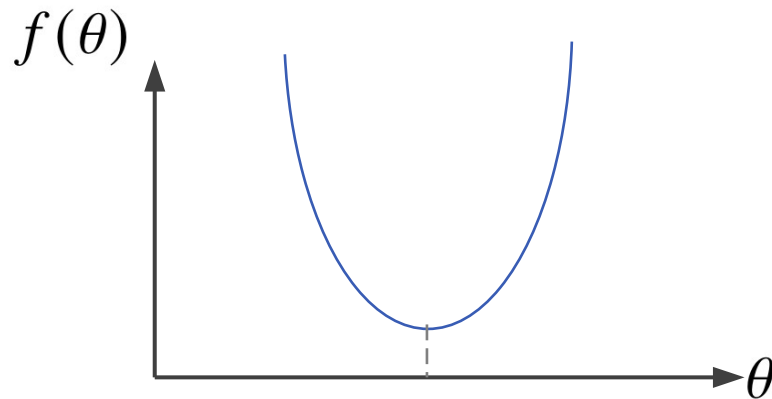
# Cost Function Quadrupole Offset

$$\underbrace{f(\theta)} = \frac{1}{N_{\text{BPM}}} \sum_{\text{BPM}} \underbrace{(x(\theta, +\Delta k_1) - x(\theta, -\Delta k_1))}_{\text{Orbit offset from positive quadrupole modulation}} \underbrace{)}_{\text{Orbit offset from negative quadrupole modulation}}^2$$

Cost function for one generated orbit

Orbit offset from positive quadrupole modulation

Orbit offset from negative quadrupole modulation

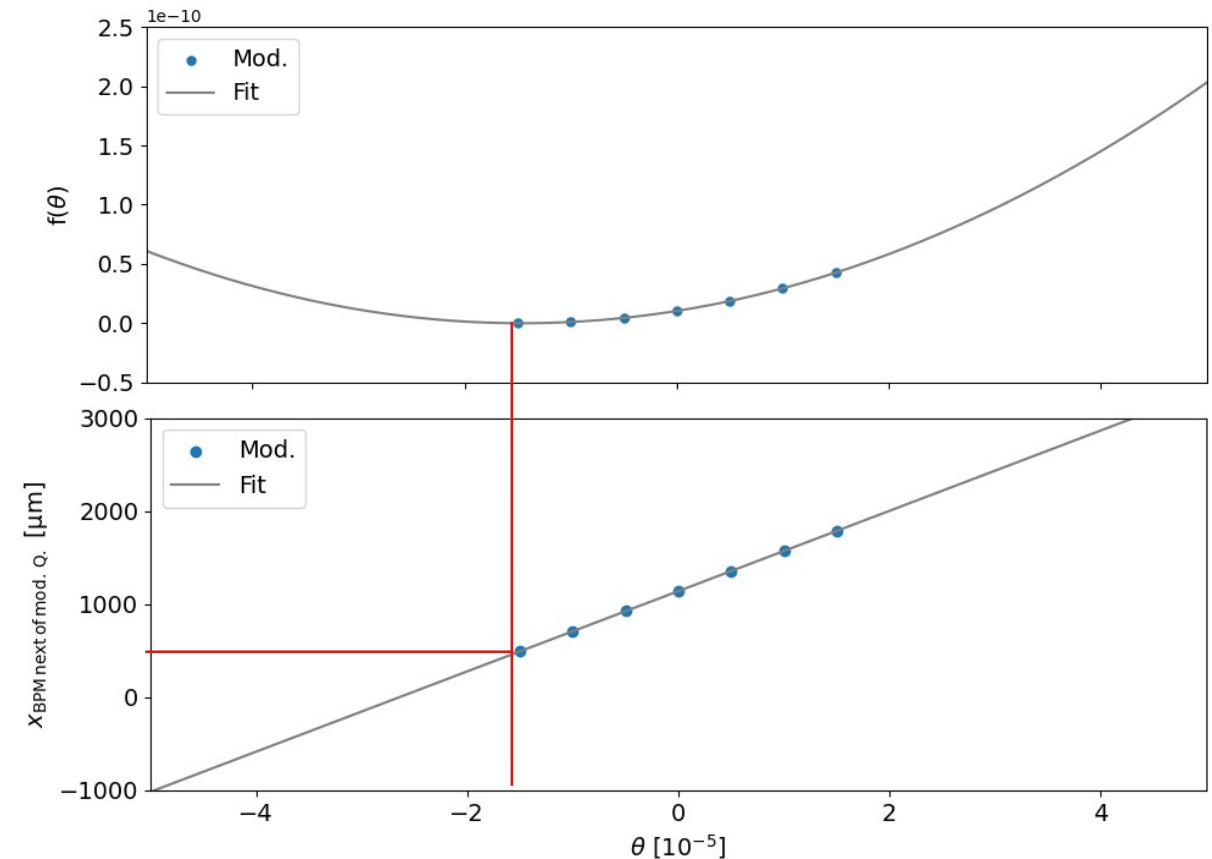


# Single Quadrupole

- $\Delta x = \Delta y = 500 \mu\text{m}$
- Propagating orbit bump
- Measured:
- $\Delta x = 491 \mu\text{m}$
- $\Delta y = 523 \mu\text{m}$

What happens if all quadrupoles are misaligned?

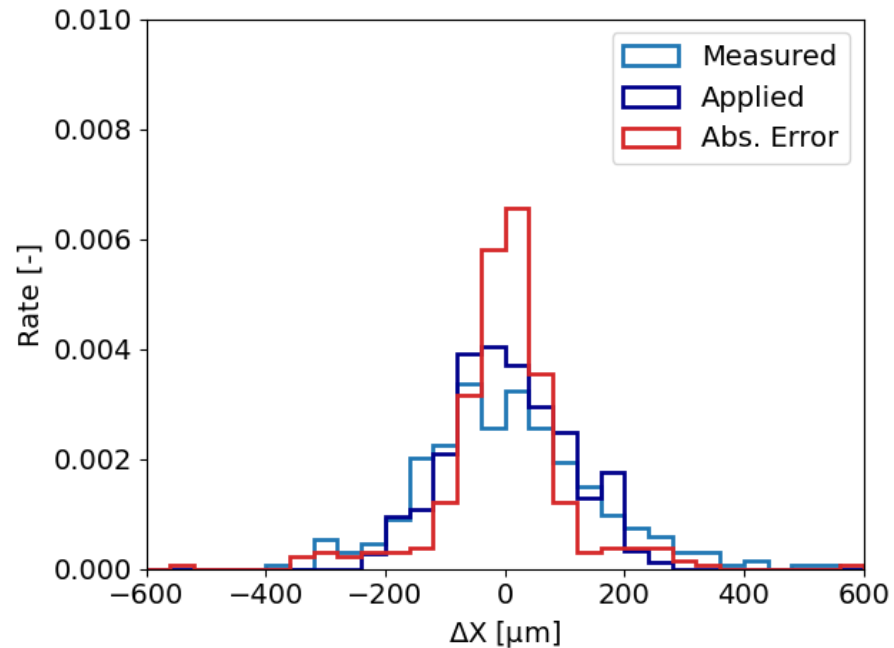
- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}, 2.4 \text{ mm}$
- No synchrotron radiation and sextupoles off
- One misaligned quadrupole



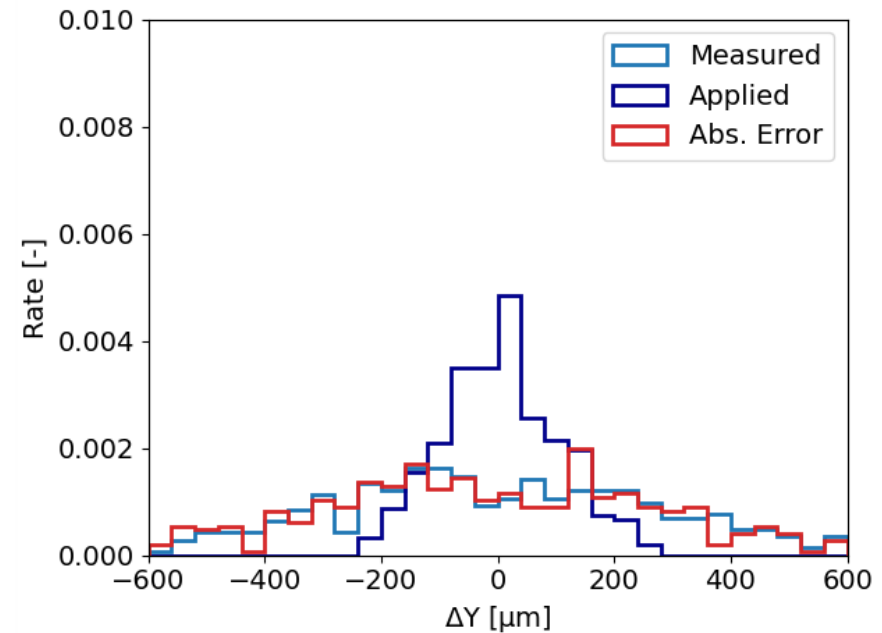
# All Quadrupoles

- $\Delta x = \Delta y = \text{Gauss}(0, 100 \mu\text{m})$
- Propagating orbit bump

- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}, 2.4 \text{ mm}$
- No synchrotron radiation and sextupoles off
- All quadrupoles misaligned



Errors mainly up to  $\pm 100 \mu\text{m}$   
Outliers up to  $\pm 2000 \mu\text{m}$   
 $\sim \text{Gauss}(0, 117 \mu\text{m})$

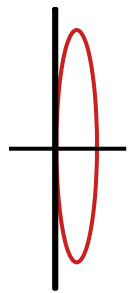


Large errors in measurements  
Outliers up to  $\pm 1400 \mu\text{m}$   
 $\sim \text{Gauss}(0, 278 \mu\text{m})$

# Error Sources and Solutions

## Initial Angle

- Here: BPM at beginning of Q.

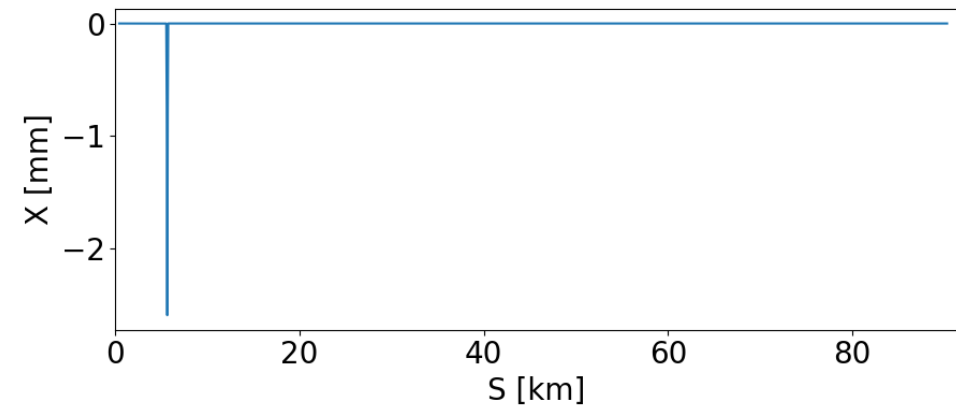

$$\begin{pmatrix} u(s) \\ u'(s) \end{pmatrix} = \mathbf{M} \begin{pmatrix} u(0) \\ u'(0) \end{pmatrix}$$

For example:  $u' = 100 \mu\text{rad}$   
→  $\Delta u$  over  $L \sim 2.9 = \sim 290 \mu\text{m}$   
→ Apply small kicks or include  $u'$

- Solution:
- Include/limit angle in offset measurement
- Assumption: Measuring at BPM

## Orbit Bump

- Here: Propagating bump
- → Feed-down effect from all Q.

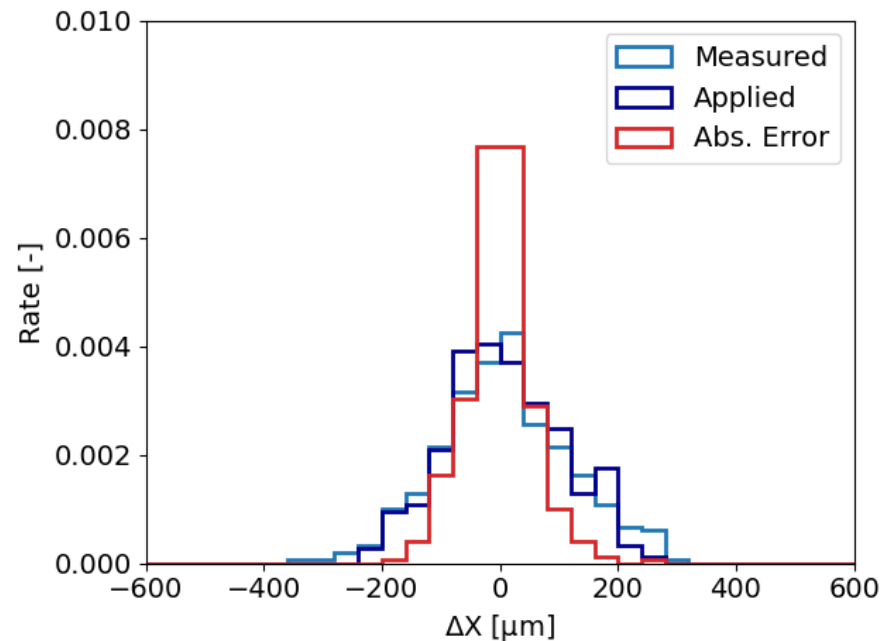


- Solution:
- Closed orbit bump (COB) around mod. Q.

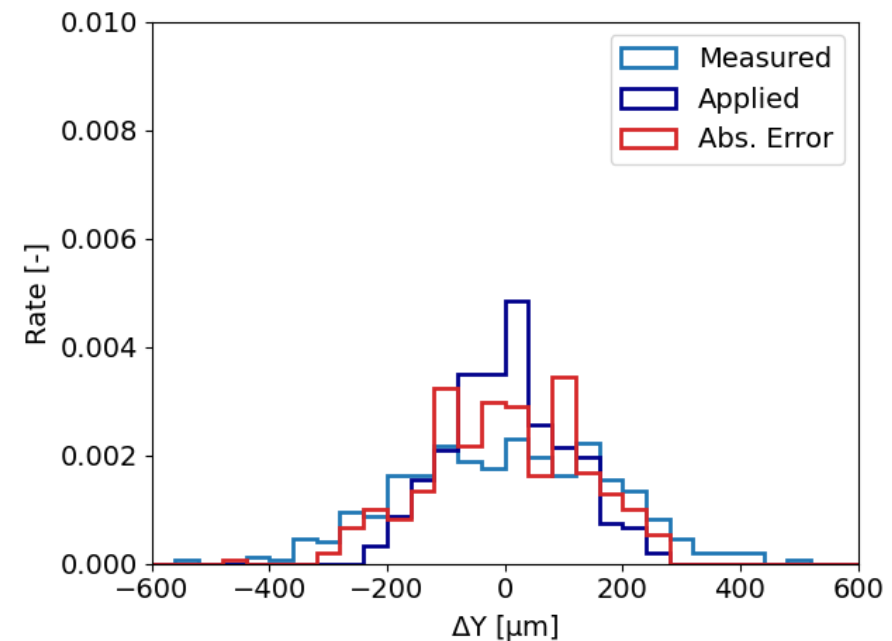
# + Closed Orbit Bump

- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}$ , 2.4 mm
- No synchrotron radiation and sextupoles off
- All quadrupoles misaligned

- $\Delta x = \Delta y = \text{Gauss}(0, 100 \mu\text{m})$
- **COB** ( $u' \sim 10 \mu\text{rad}$ ) and including angle



No severe outliers  
~ **Gauss(0, 55  $\mu\text{m}$ )**



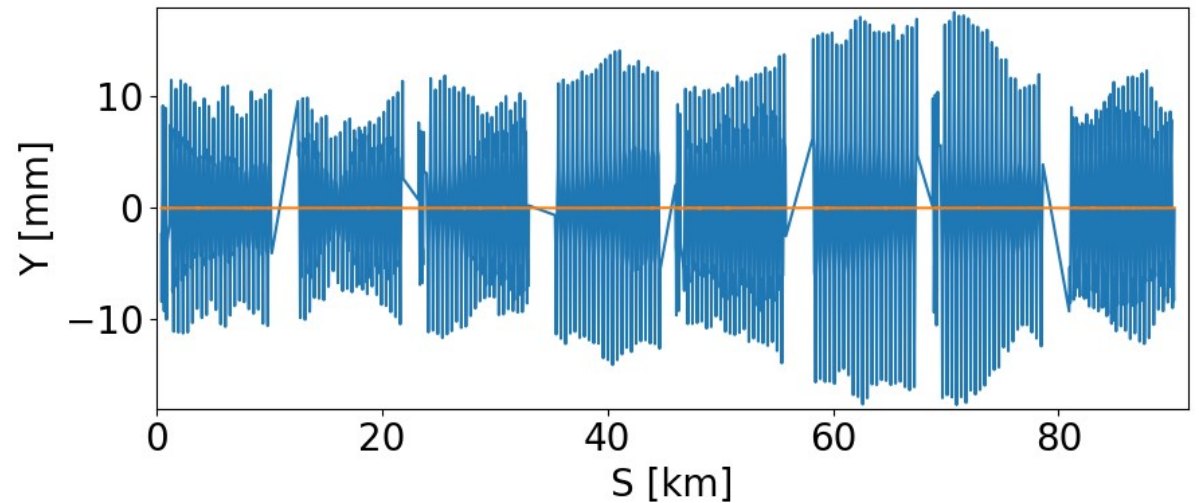
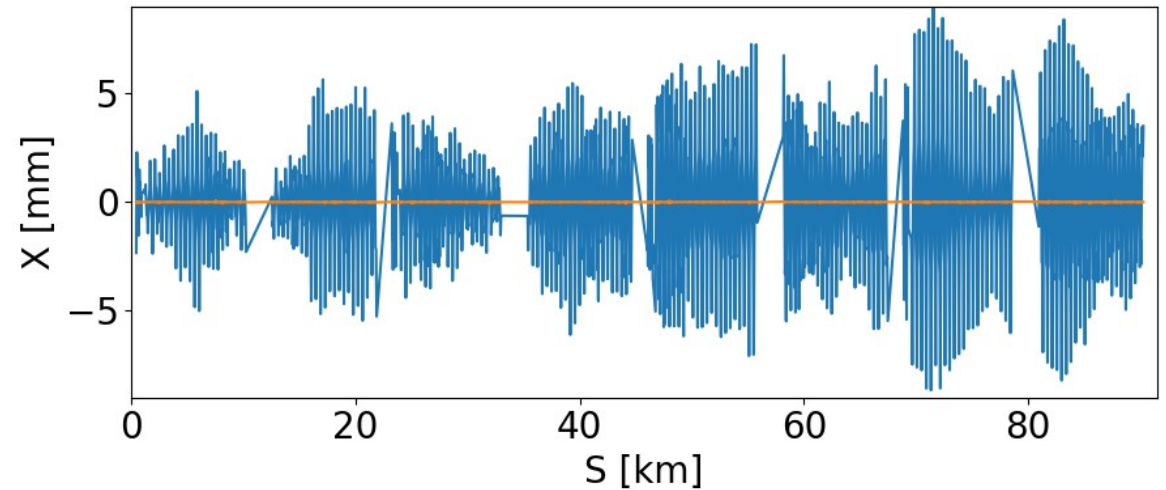
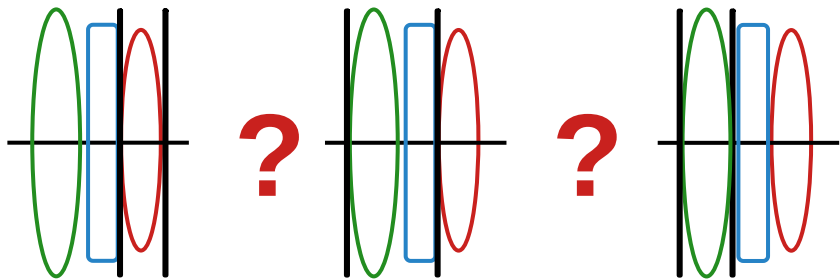
Only 2 severe outliers (not shown here)  
~ **Gauss(0, 130  $\mu\text{m}$ )**



# Controlling Initial Angles

## Initial Angle

- Initial angles/orbits must be corrected
- → Assume MICADO with all orbit kickers
- RMS  $X = Y \sim 10 \mu\text{m}$
- How can we measure  $u'$  at each BPM
- → Could require more ( $\sim$ factor 2) more BPMs!

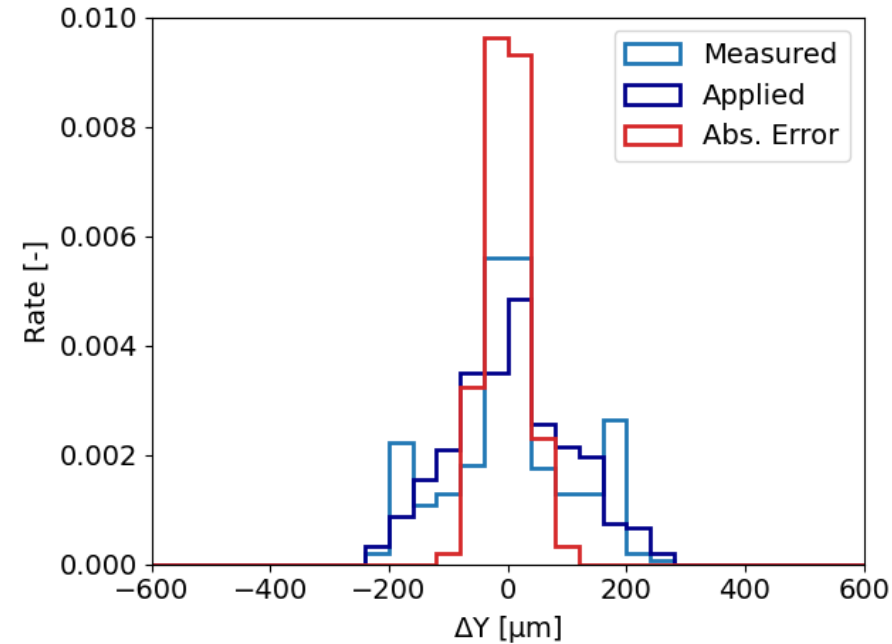
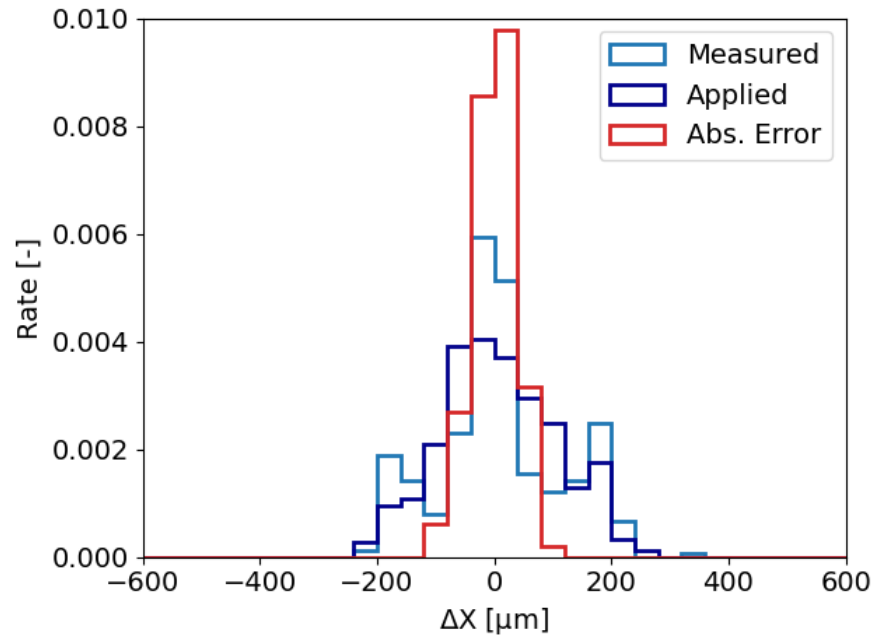


Blue: before correction; Orange: after correction

# + Orbit Correction

- $\Delta x = \Delta y = \text{Gauss}(0, 100 \mu\text{m})$
- COB ( $u' \sim 10 \mu\text{rad}$ ), including angle and **orbit correction**

- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}, 2.4 \text{ mm}$
- No synchrotron radiation and sextupoles off
- All quadrupoles misaligned

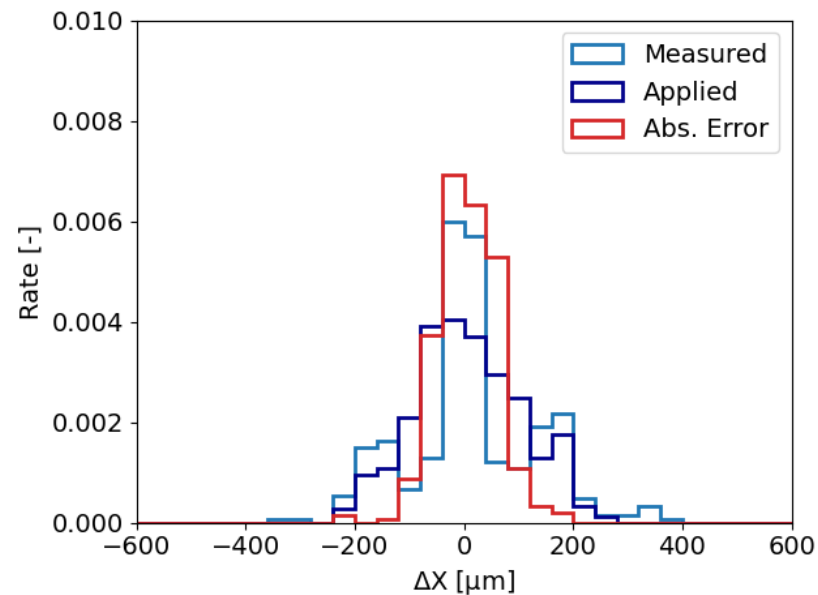


Resulting alignment:  $\sim \text{Gauss}(0, 35 \mu\text{m})$

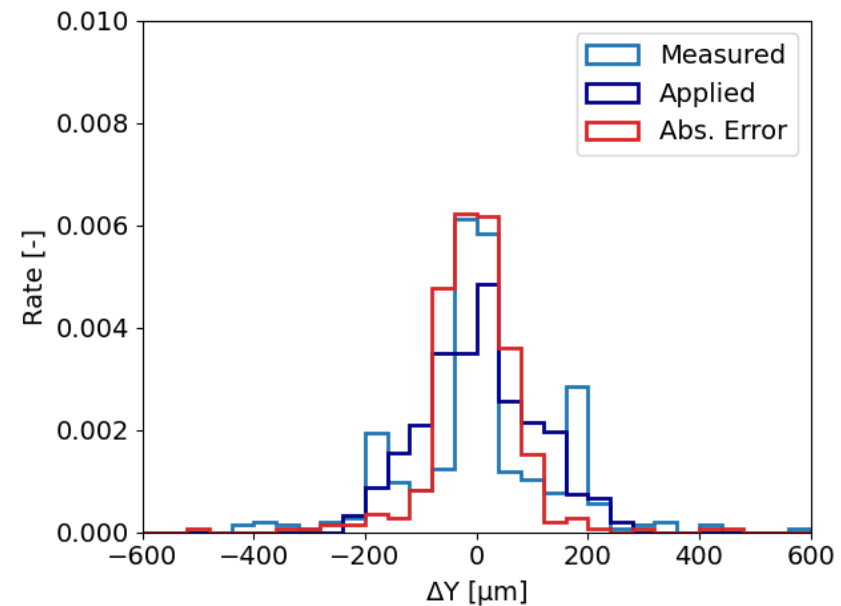
# + BPM Resolution

- $\Delta x = \Delta y = \text{Gauss}(0, 100 \mu\text{m})$
- COB ( $u' \sim 10 \mu\text{rad}$ ), including angle, orbit correction and **1  $\mu\text{m}$  BPM resolution**

- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}, 2.4 \text{ mm}$
- No synchrotron radiation and sextupoles off
- All quadrupoles misaligned



Resulting error: ~Gauss(0, 56  $\mu\text{m}$ )



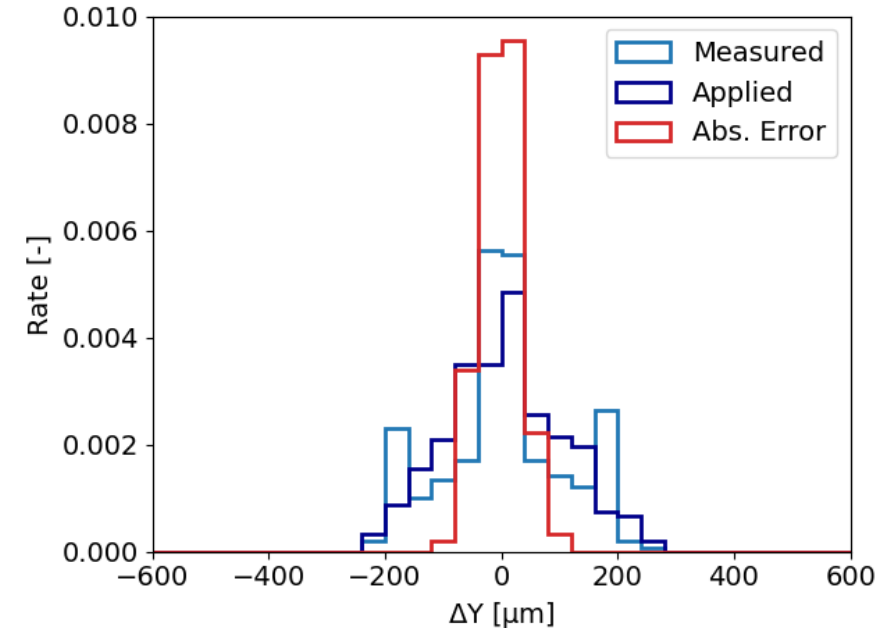
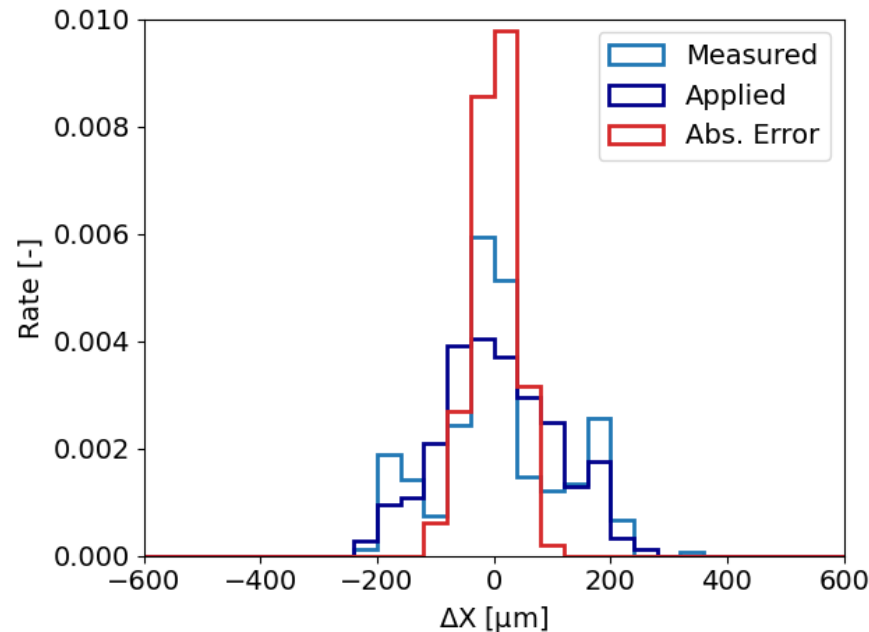
Resulting error: ~Gauss(0, 83  $\mu\text{m}$ )

**1  $\mu\text{m}$  BPM resolution increases errors by factor 2-3 → Better resolution required**

# + BPM Resolution

- $\Delta x = \Delta y = \text{Gauss}(0, 100 \mu\text{m})$
- COB ( $u' \sim 10 \mu\text{rad}$ ), including angle, orbit correction and **0.05  $\mu\text{m}$  BPM resolution**

- Relaxed Z- lattice with  $\beta_{x,y}^* = 27 \text{ cm}, 2.4 \text{ mm}$
- No synchrotron radiation and sextupoles off
- All quadrupoles misaligned



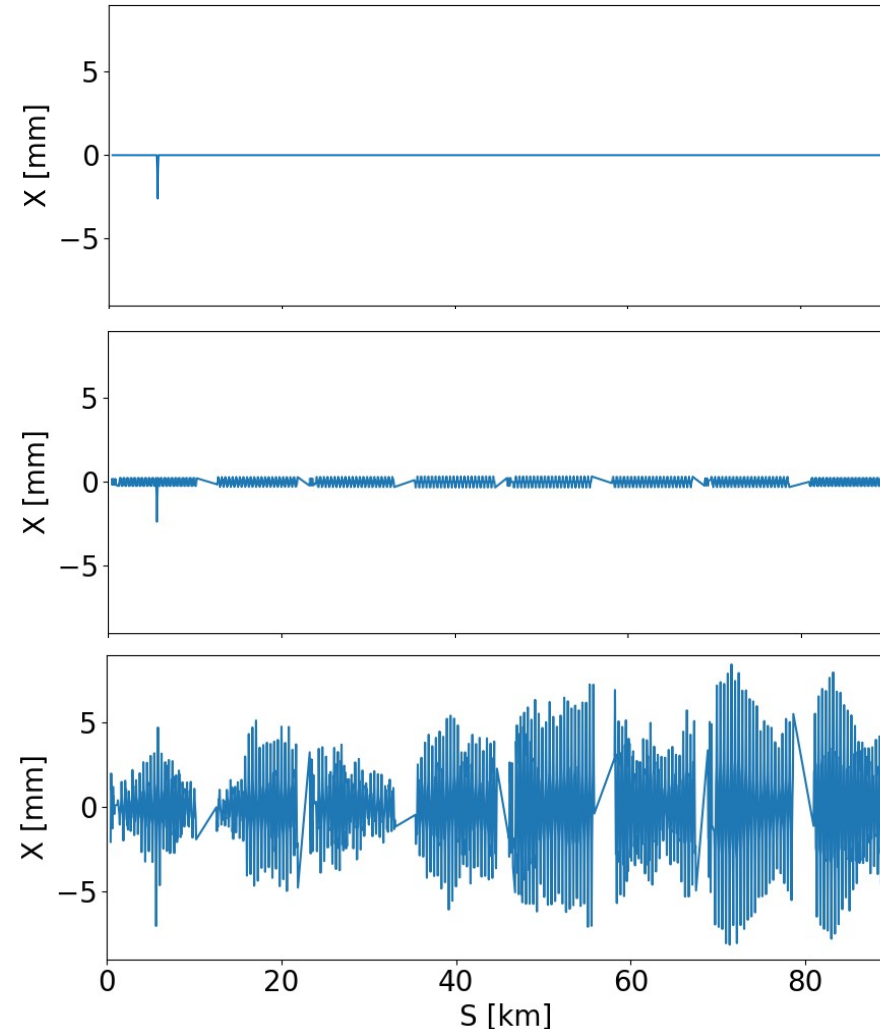
Resulting alignment: ~Gauss(0, 35  $\mu\text{m}$ )

**BUT: vertically few outliers (not shown here)**

# Orbit Bumps

## Orbit Bump

- Model orbit bump not closed with errors
- How can we close it?
- → What is the introduced error?
- Orbit change at modulated quadrupole only from COB and not propagated feed-down from other elements



Designed COB  
with 2 kicker  
magnets, 180°  
apart

No longer closed  
when quadrupole is  
modulated

Feeddown effects  
from all misaligned  
elements

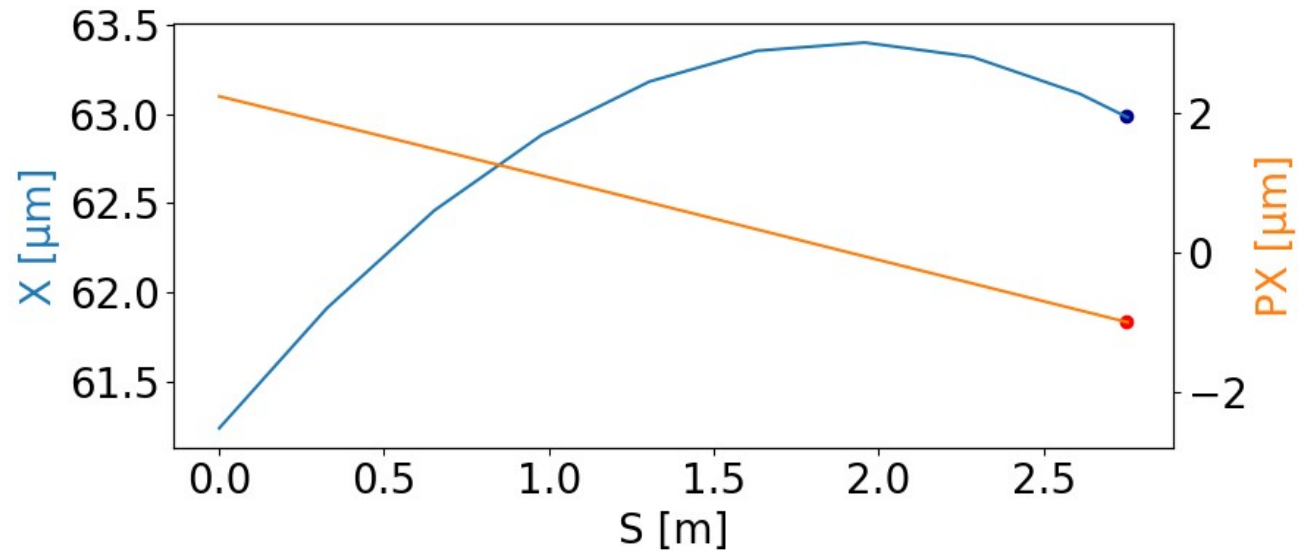
# Orbit Through Magnet

## No Misalignment

- Quadrupole sliced in 10 slices
- X, PX measured at beginning
- Dots: Propagated with transfer matrix

$$\begin{pmatrix} u(s) \\ u'(s) \end{pmatrix} = \mathbf{M} \begin{pmatrix} u(0) \\ u'(0) \end{pmatrix}$$

$$\mathbf{M}_{f. qu.} = \begin{pmatrix} \cos(\sqrt{k_1}l) & \frac{1}{\sqrt{k_1}} \sin(\sqrt{k_1}l) \\ -\sqrt{k_1} \sin(\sqrt{k_1}l) & \cos(\sqrt{k_1}l) \end{pmatrix}$$



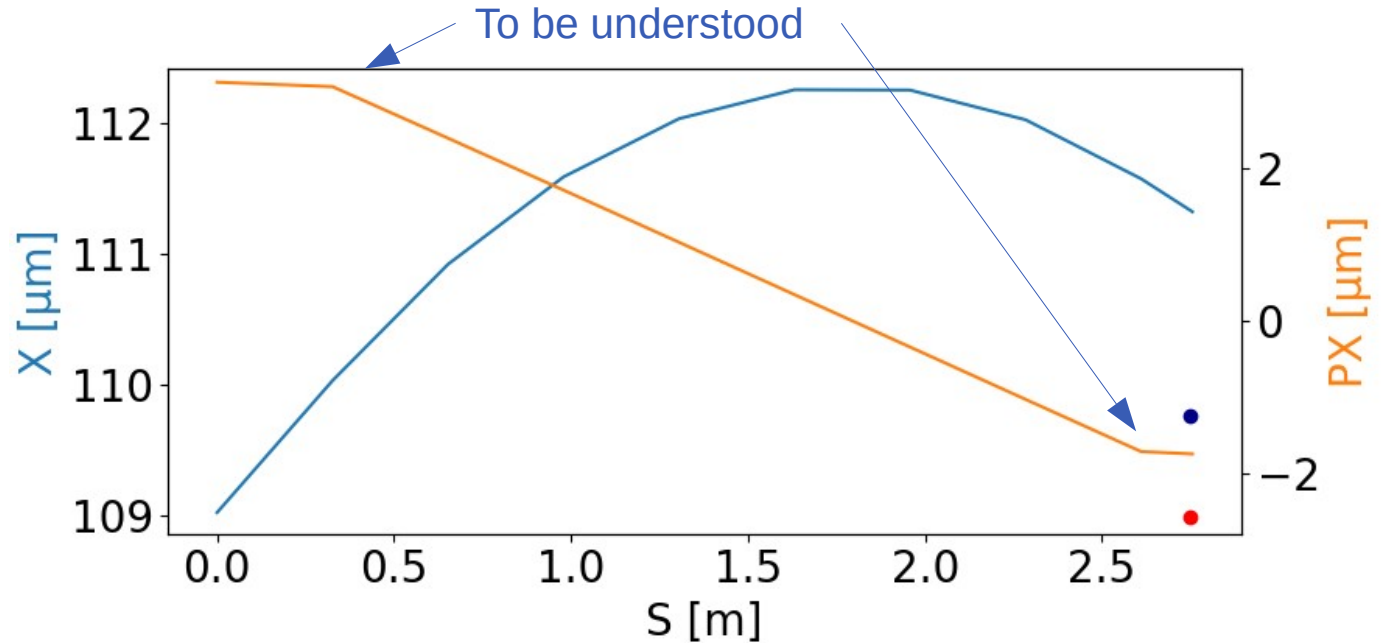
# Orbit Through Magnet

## Misalignment of 1 Quadrupole

- Quadrupole sliced in 10 slices
- X, PX measured at beginning
- Dots: Propagated with transfer matrix

$$\begin{pmatrix} u(s) \\ u'(s) \end{pmatrix} = \mathbf{M} \begin{pmatrix} u(0) \\ u'(0) \end{pmatrix}$$

$$\mathbf{M}_{f. qu.} = \begin{pmatrix} \cos(\sqrt{k_1}l) & \frac{1}{\sqrt{k_1}} \sin(\sqrt{k_1}l) \\ -\sqrt{k_1} \sin(\sqrt{k_1}l) & \cos(\sqrt{k_1}l) \end{pmatrix}$$



Feeddown: dipole field created by misaligned quadrupole

→ Strength of dipole component proportional to offset

→ **Aim: Explore comparing propagated and measured X, PX to directly extract the transverse offset**

→ Will require ~ 2 BPMs per short straight section

# Summary

- Requirements for BPMs presently being defined for optics measurements and beam-based alignment
  - $\sim 2 \mu\text{m}$  resolution in turn-by-turn mode
  - $\ll 1 \mu\text{m}$  in closed orbit mode
  - $\sim 2$  BPMs for short straight section necessary?
- First beam-based alignment techniques explored for arc quadrupoles without radiation and sextupoles
- Outlook:
  - Aim achieving **10  $\mu\text{m}$  after beam-based alignment** with misalignment and multipole errors in all elements
  - Techniques for monitoring possible element drifts, also in squeezed optics

Orbit bump	Initial $u'$ [y/n]	BPM Res. [ $\mu\text{m}$ ]	H/V [ $\mu\text{m}$ ]
Open	n	0	117/278
COB	y	0	55/130
+ orbit cor.	y	0	35/35
+ orbit cor.	y	1	56/83
+ orbit cor.	y	0.05	35/35



**Thank you!**

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in the  
FCC-ee**

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# Bunch Parameters

Parameter		FCC-Z	FCC-ttbar
Bunch intensity [ $10^{11}$ ]	Low-intensity pilot	~0.1	~0.1
	High-intensity non-colliding	1.51	1.55
	High-intensity colliding	1.51	1.55
Bunch length [mm]	Low-intensity pilot	< 5.6	< 1.81
	High-intensity non-colliding	5.6	1.81
	High-intensity colliding	12.7	2.17
Number of bunches [-]	Low-intensity pilot	~200	-
	High-intensity non-colliding	A few	-
	High-intensity colliding	15880	60

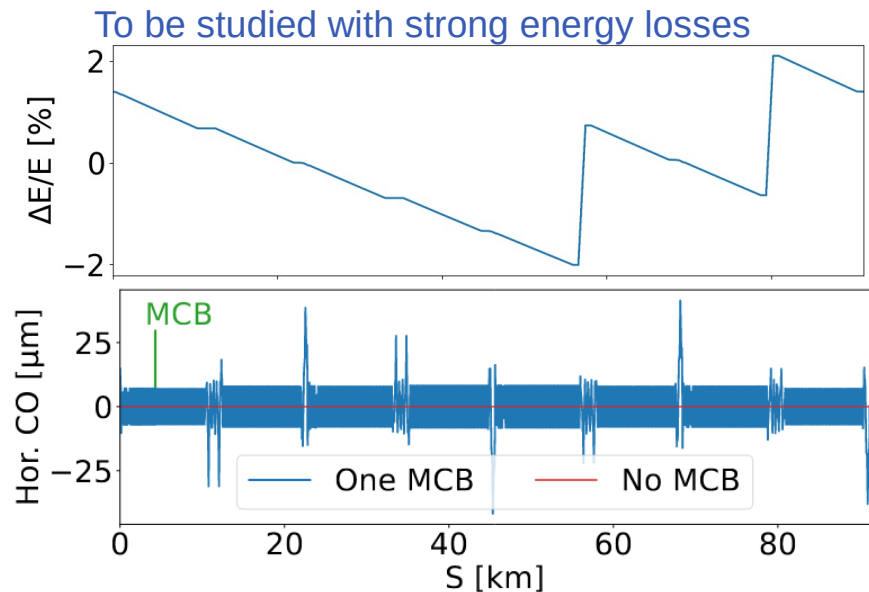
For energy calibration: 100-200 bunches with low-intensity at Z-pole

→ Optics measurements and corrections: Could correspond to measurements with e.g. ~ 20 bunches each with  $10^{11}$

# Optics Measurements

## Record orbit over several turns

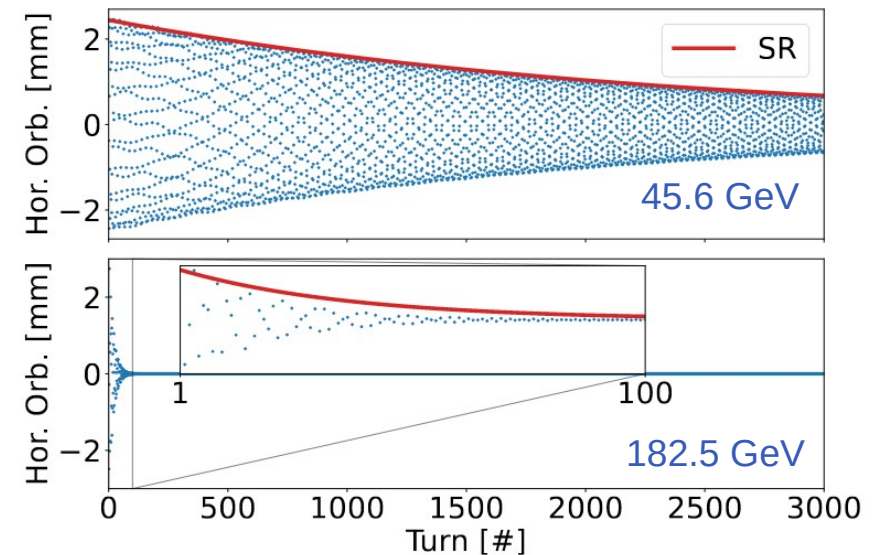
- Used for orbit measurements
- Orbit response matrix measurements



Higher BPM resolution:  $< 1 \mu\text{m}$

## Turn-by-turn measurements

- And bunch-by-bunch measurements
- Measurement of frequency spectrum



Poorer BPM resolution:  $< 10 \mu\text{m}$

# Turn-by-Turn BPM Resolution

- Goal: Phase advance error wrt model  $< 1 \times 10^{-3}$

- Z- lattice  
- No synchrotron radiation and sextupoles off

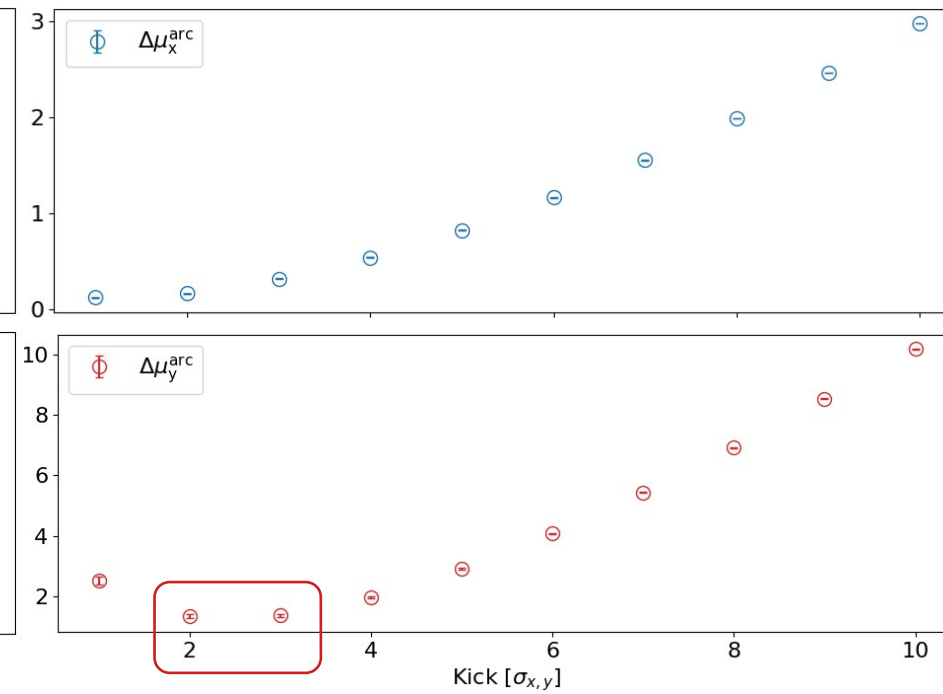
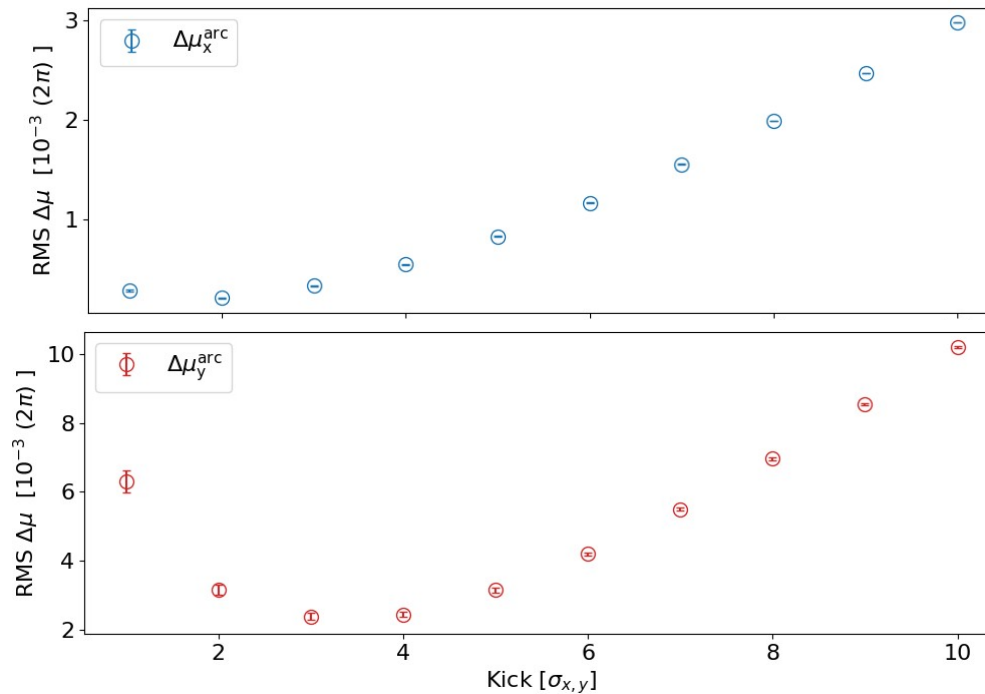
- Phase advance errors depends on BPM resolution and applied kick strength

BPM resolution: 5  $\mu\text{m}$

BPM resolution: 2  $\mu\text{m}$

Horizontal

Vertical



Phase advance error goal only achievable with high resolution BPMs ( $\sim 2 \mu\text{m}$ )