12th International Conference on the Exact Renormalization Group 2024 (ERG2024)

# Strangeness neutrality and QCD phase structure from FRG

Rui Wen

University of Chinese Academy of Sciences



2024.09.25

Based on: W.-j. Fu, C. Huang, J. M. Pawlowski, F. Rennecke, R. Wen, S. Yin. (2024) in preparation

fQCD collaboration: J. Braun, Y.-r. Chen, W.-j. Fu, F. Gao, F. Ihssen, A. Geissel, C. Huang,Y. Lu, J. M. Pawlowski, F. Rennecke, F. R. Sattler, B. Schallmo, J. Stoll, Y.-y. Tan, S. T<sup>..</sup>opfel, J. Turnwald, R. Wen, J. Wessely, N. Wink, S. Yin, P.-w. Zheng and N. Zorbach, (2024).

## Outline

- Introduction
- The 2+1 flavor QCD Theory within FRG
- Numerical results
- Gluon propagator; quarks and mesons mass; chiral condensates
- QCD phase structure
- B-S Correlation
- Summary

## Introduction



Adam Bzdak, Shinichi Esumi et.al. Phys.Rept. 853 (2020) 1-87



STAR Collaboration, XQCD2024

## Introduction



Wei-jie's talk

### The 2+1 flavor QCD Theory within FRG

$$\partial_{t}\Gamma_{k}[\Phi] = \underbrace{\frac{1}{2}}_{Q_{\mu}} \underbrace{\sum_{\alpha} (\partial_{\mu} \sigma^{\alpha}) - (\nabla \sigma)}_{Q_{\mu}} - (\nabla \sigma) + \frac{1}{2\xi}}_{Q_{\mu}} \underbrace{\sum_{\alpha} (\partial_{\mu} \sigma^{\alpha}) - (\nabla \sigma)}_{Q_{\mu}} - (\nabla \sigma) + \frac{1}{2\xi}}_{Q_{\mu}} \underbrace{\sum_{\alpha} (\partial_{\mu} \sigma^{\alpha}) - (\nabla \sigma)}_{Q_{\mu}} - (\nabla \sigma) + \frac{1}{2\xi}}_{Q_{\mu}} \underbrace{\sum_{\alpha} (\partial_{\mu} \sigma^{\alpha}) - (\nabla \sigma)}_{Q_{\mu}} + \frac{1}{2\xi}} \underbrace{\sum_{\alpha} (\partial_{\mu} \sigma^{\alpha}) - (\nabla \sigma)}_{Q_$$

#### The flow equations



#### The flow equations

propagators :





## Dynamical hadronization

The scale dependent meson fields:

 $\langle \partial_t \hat{\phi}_k \rangle = \left[ (\bar{q} \dot{A}_k^{\frac{1}{2}} T_a \dot{A}_k^{\frac{1}{2}} q) + (\bar{q} \dot{A}_k^{\frac{1}{2}} i \gamma_5 T_a \dot{A}_k^{\frac{1}{2}} q) \right] + \dot{B}_k \Sigma$   $\begin{pmatrix} \dot{A}_{l,k} & 0 & 0 \end{pmatrix}$ 

$$\dot{oldsymbol{A}}_k = \left(egin{array}{ccc} 0 & \dot{A}_{l,k} & 0 \ 0 & 0 & \dot{A}_{s,k} \end{array}
ight)$$

The Wetterich equation with dynamical hadronization:

$$\partial_t \Gamma_k[\Phi] + \int \langle \partial_t \hat{\phi}_{k,i} \rangle \left( \frac{\delta \Gamma_k[\Phi]}{\delta \phi_i} + c_\sigma \delta_{i\sigma} \right)$$
$$= \frac{1}{2} \operatorname{Tr} \left( G_k[\Phi] \partial_t R_k \right) + \operatorname{Tr} \left( G_{\phi \Phi_j}[\Phi] \frac{\delta \langle \partial_t \hat{\phi}_k \rangle}{\delta \Phi_j} R_\phi \right)$$

With the fully hadronized condition:

$$\lambda_q \equiv 0, \quad \forall k$$

We get the hadronization functions :

$$\dot{A}_{l,k} = -\frac{1}{h_{l,k}} \operatorname{Flow}_{(\bar{q}T^Lq)(\bar{q}T^Lq)}^{(4)} \qquad \partial_t h_{l,k} = -\frac{1}{\sigma_l} \frac{\delta \tilde{U}(\Sigma)}{\delta \sigma_l} \dot{A}_{l,k} + \frac{1}{\sigma_l} \operatorname{Re}(\operatorname{Flow}_{(\bar{q}T^lq)}^{(2)}),$$
$$\dot{A}_{s,k} = -\frac{1}{h_{s,k}} \operatorname{Flow}_{(\bar{q}T^Sq)(\bar{q}T^Sq)}^{(4)} \qquad \partial_t h_{s,k} = -\frac{1}{\sigma_s} \frac{\delta \tilde{U}(\Sigma)}{\delta \sigma_s} \dot{A}_{s,k} + \frac{1}{\sigma_s} \operatorname{Re}(\operatorname{Flow}_{(\bar{q}T^sq)}^{(2)}).$$

 $\partial_t$ 





Gies, Wetterich , PRD 65 (2002) 065001; 69 (2004) 025001 Pawlowski, AP 322 (2007) 2831 Flörchinger, Wetterich, PLB 680 (2009) 371

#### The Gluon Propagator at T=0 and Finite T



W-j Fu, J.M. Pawlowski, F. Rennecke, Phys.Rev.D 101 (2020) 5, 054032

#### Quarks and Mesons Masses



$$\begin{split} \Lambda &= 20 {\rm GeV} & m_{l,k=IR} = 333 \; {\rm MeV} & m_{\pi} = 142 \; {\rm MeV} & m_{\sigma} = 628 \; {\rm MeV} \\ m_{u} &= m_{d} = m_{l} & m_{s,k=IR} = 438 \; {\rm MeV} & m_{K} = 481 \; {\rm MeV} & m_{\eta} = 527 \; {\rm MeV} \\ m_{s,k=\Lambda}/m_{l,k=\Lambda} = 27.4 & m_{\eta\prime} = 946 \; {\rm MeV} \\ \end{split}$$

## The mixing angles between light-strange (LS) basis and physical basis

Hessian matrix

$$H_{ij} = \frac{\partial^2 \tilde{U}_k(\Sigma, \Sigma^{\dagger})}{\partial \phi_i \partial \phi_j}$$

Because the nonvanishing nondiagonal element  $H_{s/p,ls}$ 

$$\begin{pmatrix} f_0 \\ \sigma \end{pmatrix} = \begin{pmatrix} \cos \varphi_s & -\sin \varphi_s \\ \sin \varphi_s & \cos \varphi_s \end{pmatrix} \begin{pmatrix} \sigma_l \\ \sigma_s \end{pmatrix}$$
$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos \varphi_p & -\sin \varphi_p \\ \sin \varphi_p & \cos \varphi_p \end{pmatrix} \begin{pmatrix} \eta_l \\ \eta_s \end{pmatrix}$$

The mixing angles

$$\varphi_{s/p} = \frac{1}{2} \arctan\left(\frac{2H_{s/p,ls}}{H_{s/p,ss} - H_{s/p,ll}}\right)$$





Wuppertal-Budapest Collaboration: JHEP 09 (2010) 073

## Phase diagram with $\mu_s = 0$



 $\frac{T_c(\mu_B)}{T_c} = 1 - \kappa_2 \left(\frac{\mu_B}{T_c}\right)^2 + \kappa_4 \left(\frac{\mu_B}{T_c}\right)^4 + \cdots$ 

 $\kappa_2(\mu_s = 0) = 0.0148(2)$ 

$$\begin{split} \kappa_2 &= 0.015(1) \\ \text{H. T. Ding, et.al. arXiv:2403.09390} \\ \kappa_2 &= 0.0153 \pm 0.0018 \\ \text{S. Borsanyi, et.al. Phys. Rev. Lett. 125,} \\ 052001 (2020), \end{split}$$

 $(T_{CEP} = 102 MeV, \mu_B = 649 MeV), \mu_s = 0$ 

 $(T, \mu_B)_{CEP} = (107, 635) MeV$ fRG: W-j Fu, Pawlowski, Rennecke, PRD 101 (2020), 054032  $(T, \mu_B)_{CEP} = (109, 610) MeV$ DSE (fRG): Gao, Pawlowski, PLB 820 (2021) 136584  $(T, \mu_B)_{CEP} = (112, 636) MeV$ DSE: Gunkel, Fischer, PRD 104 (2021) 5, 054022

## Phase diagram with $\mu_s = 0$ and $n_s = 0$





$$T_{CEP} = 102 MeV, \mu_B = 649 MeV), \mu_s = 0$$
  
 $T_{CEP} = 97 MeV, \mu_B = 680 MeV), n_s = 0$ 

 $\kappa_2^B(n_S=0)/\kappa_2^B(\mu_S=0) = 0.893(35)$ H. T. Ding, et.al. arXiv:2403.09390

## The 2nd order susceptibilities



$$\chi^{BQS}_{ijk} = \frac{\partial^{i+j+k}}{\partial \hat{\mu}^i_B \partial \hat{\mu}^j_Q \partial \hat{\mu}^k_S} \frac{p}{T^4}$$



## Summary

- We build the 2+1 flavor QCD theory within FRG approach. The light and reduced chiral condensate are in good agreement with the Lattice results.
- The curvature of the phase boundary  $\kappa_2(n_s=0)/\kappa_2(\mu_s=0)=0.91(2)$

and the  $\mu_{B,CEP}(n_S = 0)$  is slightly larger than  $\mu_{B,CEP}(\mu_S = 0)$ .

• The 2nd order baryon-strangeness correlation functions are monotonic changed with the collision energy.

## Thanks for your attention