



PTA gravitational waves and JWST early galaxies:  
from Primordial Black Holes to Axion Clusters

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21 December 2023

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# 2023 was a great year for cosmo!



[Gouttenoire, ST,  
Valogiannis,  
Vanvlasselaer ]  
2307.01457

# Spoiler Alert: HST has restricted New Physics!

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## N SERIES HOW TO RUIN CHRISTMAS



# Outline

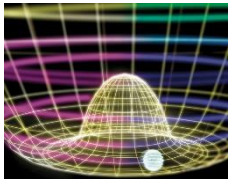
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## I. Observations



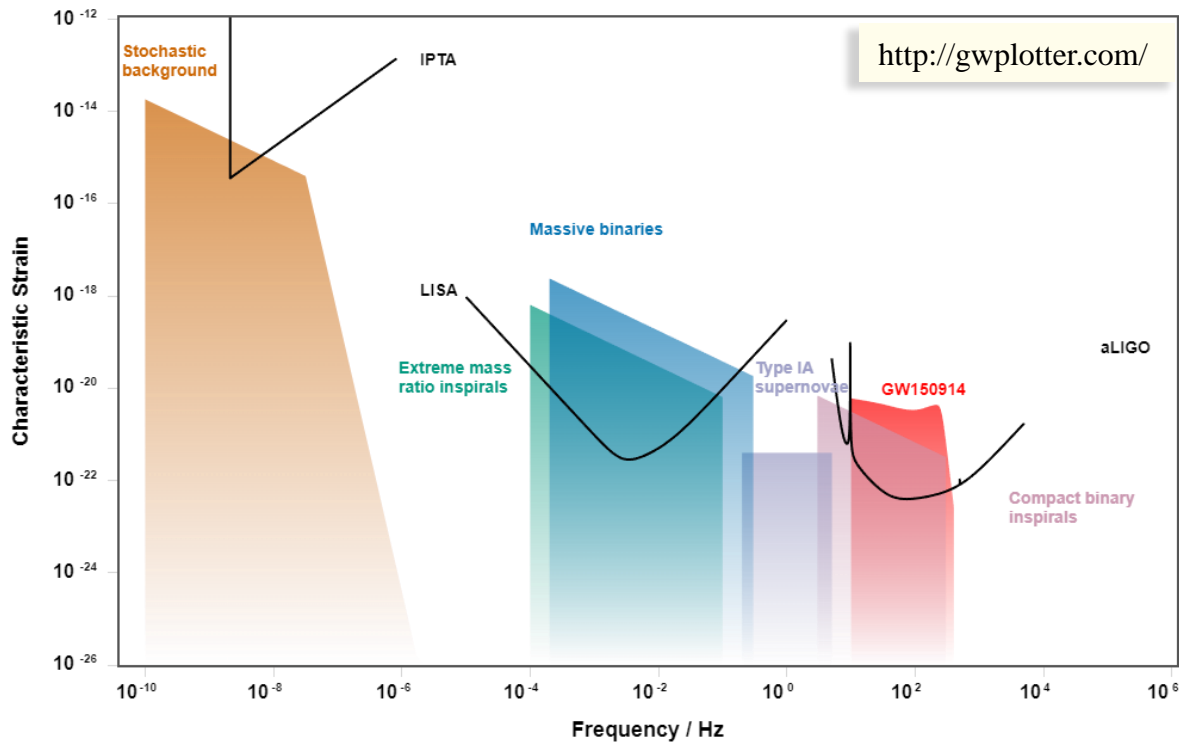
## II. Primordial Black Holes



## III. Axion Clusters

# Observations of Gravitational Waves (GWs)

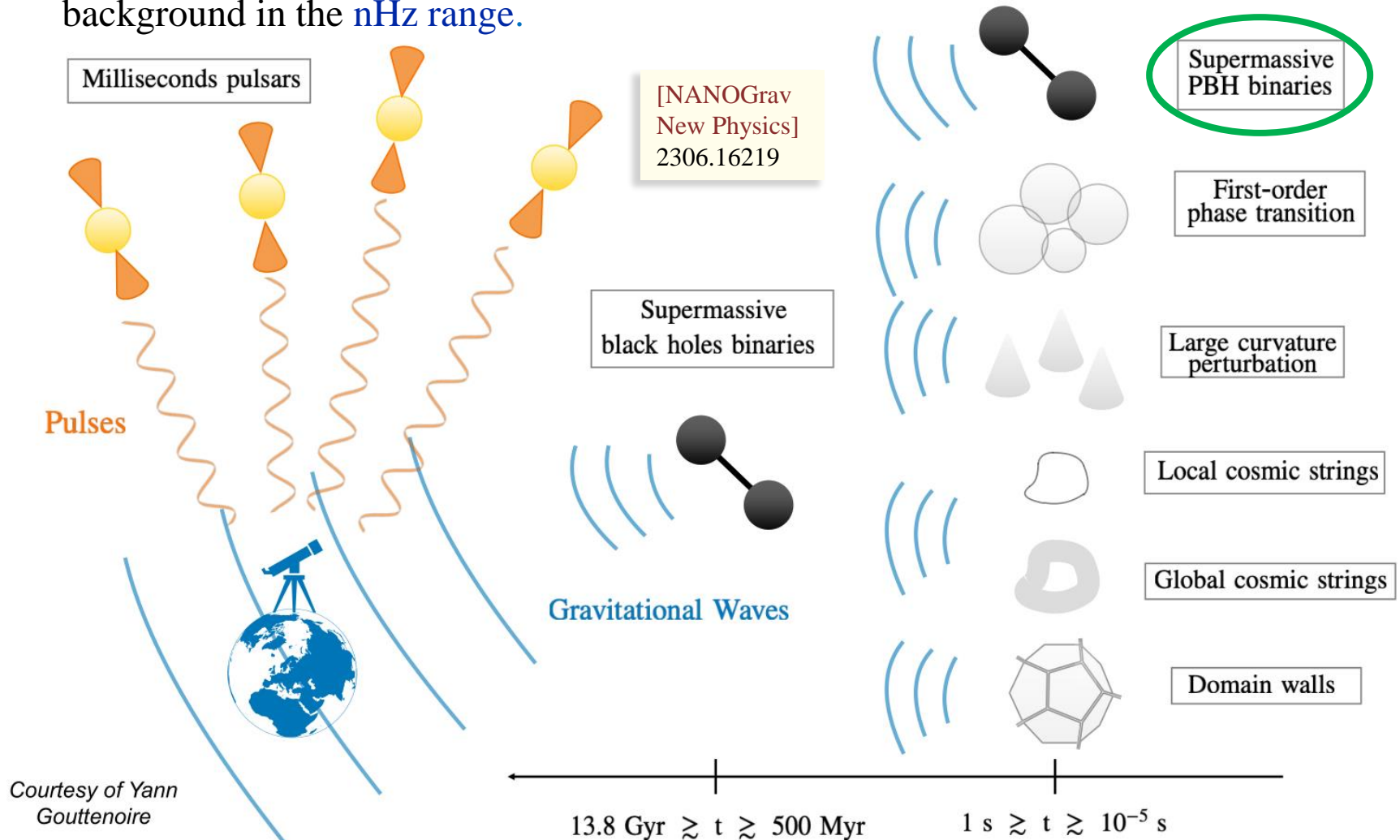
➤ GWs offer a new lens into the dynamics of the early universe.





# Pulsar Timing Arrays (PTAs)

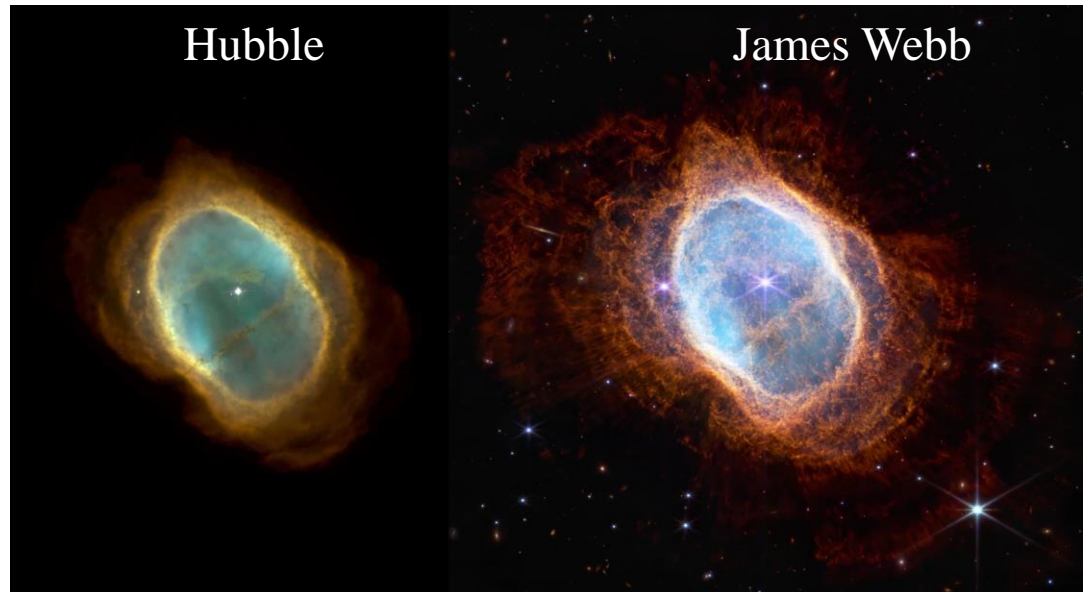
- The NANOGrav combined with 4 PTA collaborations have recently released evidence for the **existence** of a stochastic Gravitational Wave (GW) background in the **nHz range**.



# James Webb Space Telescope

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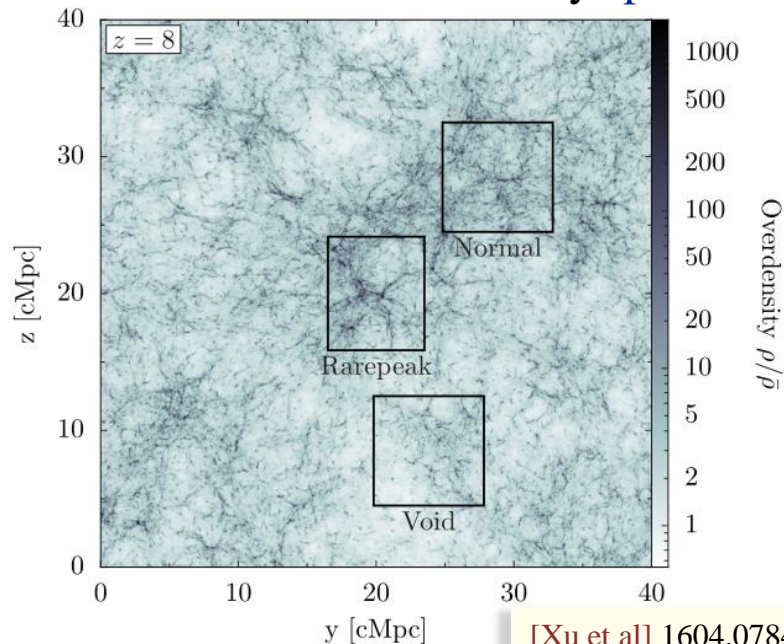
- JWST launched and it is already **collecting data!**



[STSI/NASA, ESA, CSA, STScI, Webb ERO] Southern Ring Nebula

# JWST Early Massive Galaxies

- Initial observations (e.g. JADES & CEERs surveys) have reported **photometric** evidence of massive galaxies at unexpectedly **high redshifts**  $7 < z < 12$ . A large subset of them has been recently **spectroscopically** confirmed.



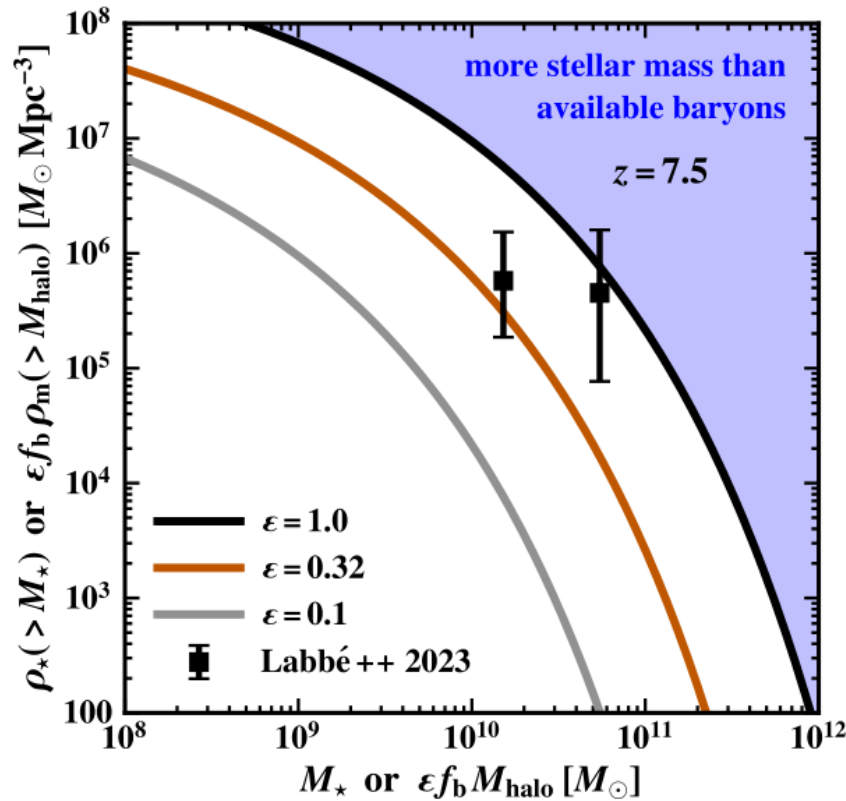
[Adams et al] 2207.11217, [Finkelstein et al] 2211.05792, [Naidu et al] 2207.09434

- Large cosmological hydrodynamical simulation demonstrated **compatibility** with existing models of galaxy formation.

[Keller et al] 2212.12804  
[McCaffrey et al] 2304.13755



# JWST Early Massive Galaxies: $\Lambda$ CDM tension?



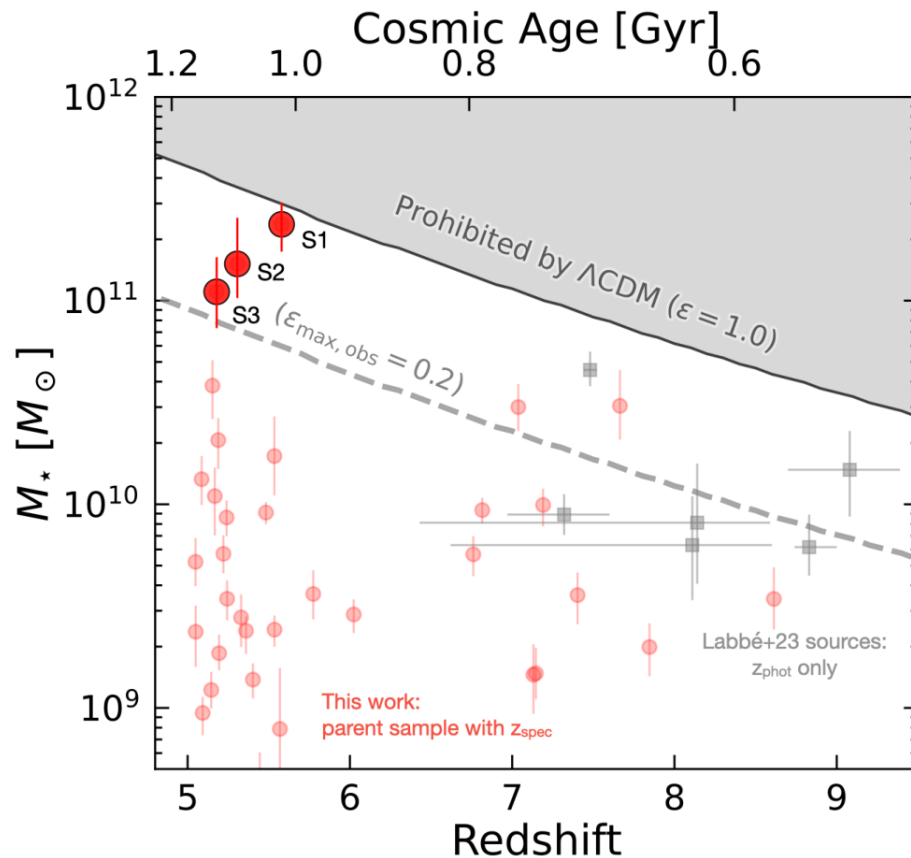
- The status of extreme galaxy candidates with stellar mass as high as  $10^{11} M_\odot$  still remains under **investigation**.

[Labbe et al] 2207.12446

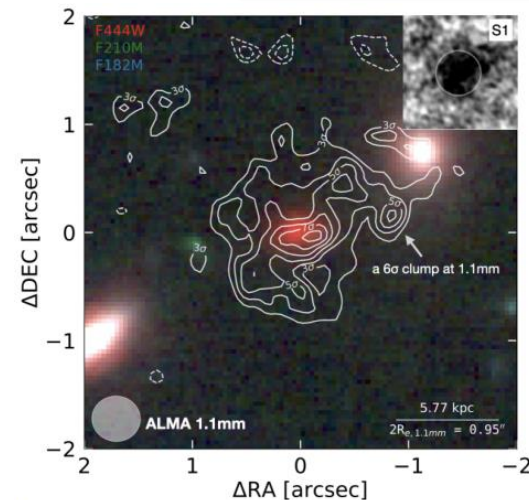
- If those results hold under spectroscopic scrutiny, they would pose a **challenge** to  $\Lambda$ CDM itself. For  $\epsilon = 0.1$ , the current tension amounts to **2.5-3 $\sigma$**  confidence level.

[Boylan-Kolchin ] 2208.01611 [Lovell et al ] 208.10479 [Wang, Liu,Lu] 2311.02866

# JWST Early Massive Galaxies: $\Lambda$ CDM tension?



➤ A sample of 36 galaxies with **robust** spectroscopic redshifts at  $z \sim 5-9$  was announced by FRESCO survey. [Xiao et al] 2309.02492



# Outline

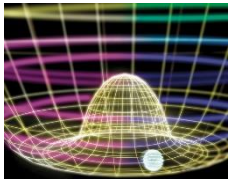
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I. Observations



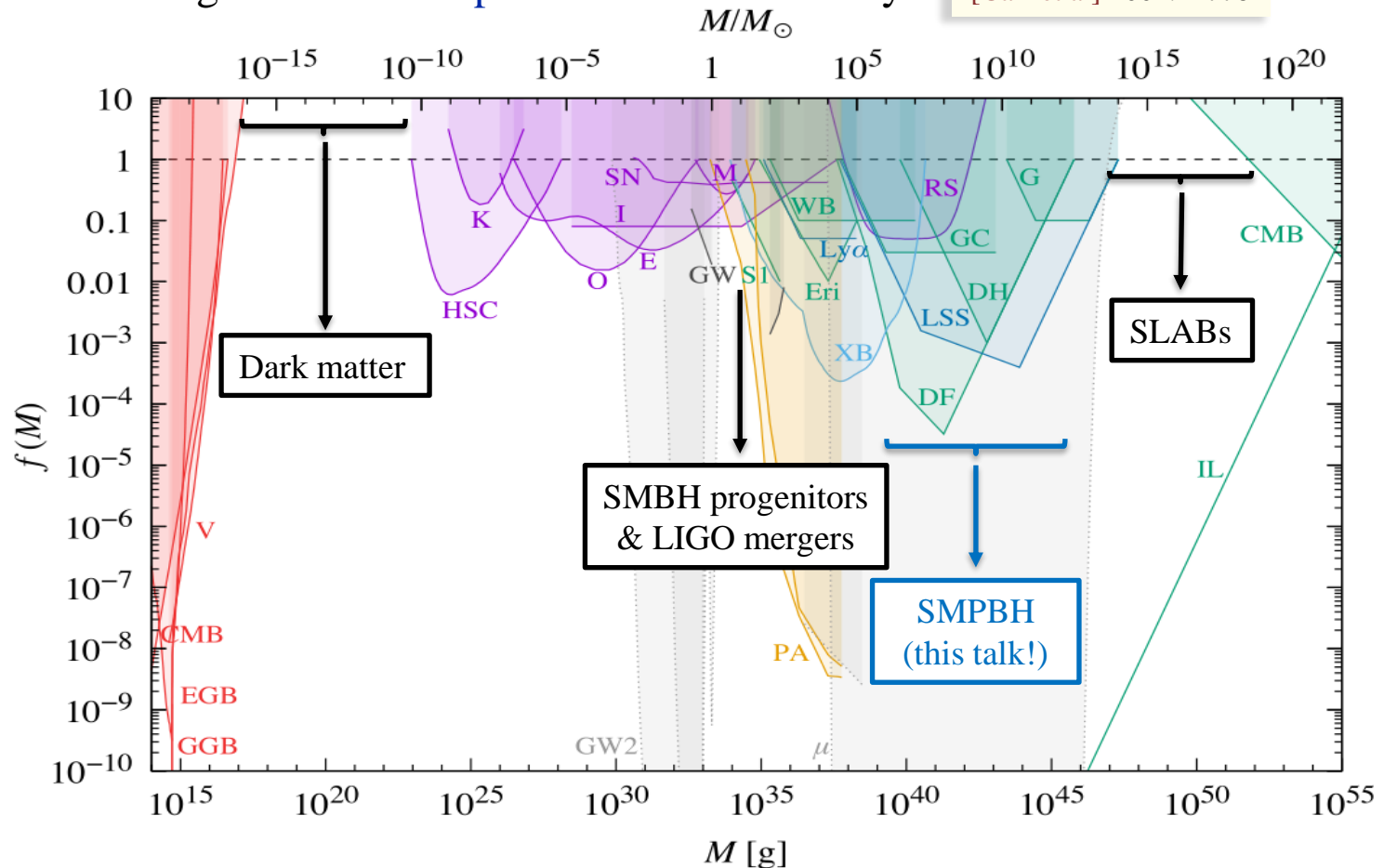
**II. Primordial Black Holes**



III. Axion Clusters

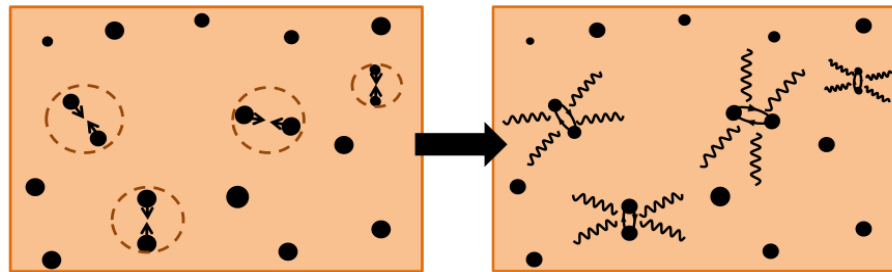
# Primordial Black Holes (PBHs)

- PBHs emerge as one of the most long-studied scenarios, capable of leaving distinctive **imprints** on cosmic history. [Carr et al] 2002.12778



# Early-Universe PBH binaries formation

- Immediately after their formation, PBHs are sparsely distributed in space.
- The mean separation between PBHs,  $\bar{l}_{\text{PBH}}(t) \propto t^{1/2}$ , falls below the Hubble distance  $H^{-1} \propto t$  before matter-radiation equality.
- A pair of PBH **decouples** from the expansion of the Universe and becomes gravitationally **bound** when  $M_{\text{PBH}} R^{-3} > \rho(z_{\text{dec}})$ .



[Sasaki et al]  
[1801.05235]

- The two PBHs will orbit around each other and gradually shrink by gravitational radiation (*inspiral*). At later times when they are close enough they *merge* and eventually settle down to a stable form (*ring-down*).



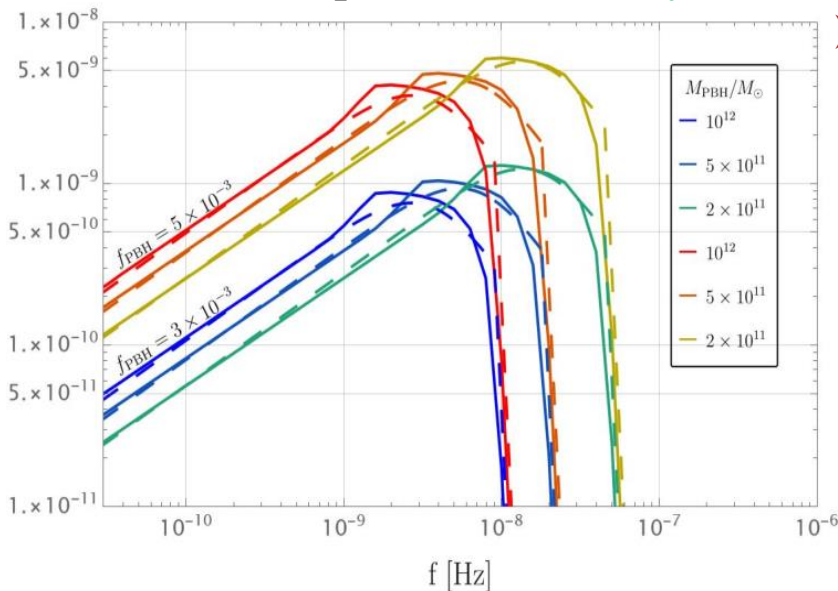
# Gravitational Waves from PBH Mergers

- The energy density of the stochastic GWs from PBH binaries reads

$$\Omega_{\text{GW}} h^2 = \frac{f}{\rho_c/h^2} \int_0^\infty dz \frac{\mathcal{R}(z)}{(1+z)H(z)} \frac{dE_{\text{GW}}(f')}{df'} \Big|_{f'=(1+z)f}$$

[LIGO] 1602.03847

- We perform a full **Bayesian** analysis of the PTA signals.



- We include as priors:

[PTArcade] 2306.16377

- 1) Environmental effects:** At low frequencies, the assumption of GW-driven energy loss breaks down due to **interactions with the environment**.
- 2) Continuous signal:** At high frequencies, the number of sources per frequency bins can become  $N(f, \Delta f) < 1$ , and the assumption of a smooth distribution of sources breaks down.

# Isocurvature Perturbations: Poisson vs Seed

➤ On large scales, we expect  $\rho_{\text{PBH}}$  to follow the adiabatic perturbations  $\delta_{\text{ad}}$ . However, on small enough scales, due to the **discrete** nature of PBHs an **isocurvature** component  $\delta_{\text{PBH}}^0$  is generated. For a Poissonian gas of PBH the variance is  $\langle |\delta_{\text{PBH}}^0(k)|^2 \rangle = (\bar{n}_{\text{PBH}})^{-1} = \frac{M_{\text{PBH}}}{f_{\text{PBH}} \rho_{\text{DM}}}$ .

➤ PBH bind gravitationally regions of mass  $\tilde{M}$  via two mechanisms:

[Carr, Silk] 1801.00672

1. **Poisson Effect:** If  $f_{\text{PBH}} > \frac{M_{\text{PBH}}}{\tilde{M}}$  then the Poisson-distributed locations of the PBH introduce a **shot noise** in  $\rho_{\text{DM}}$ , i.e.

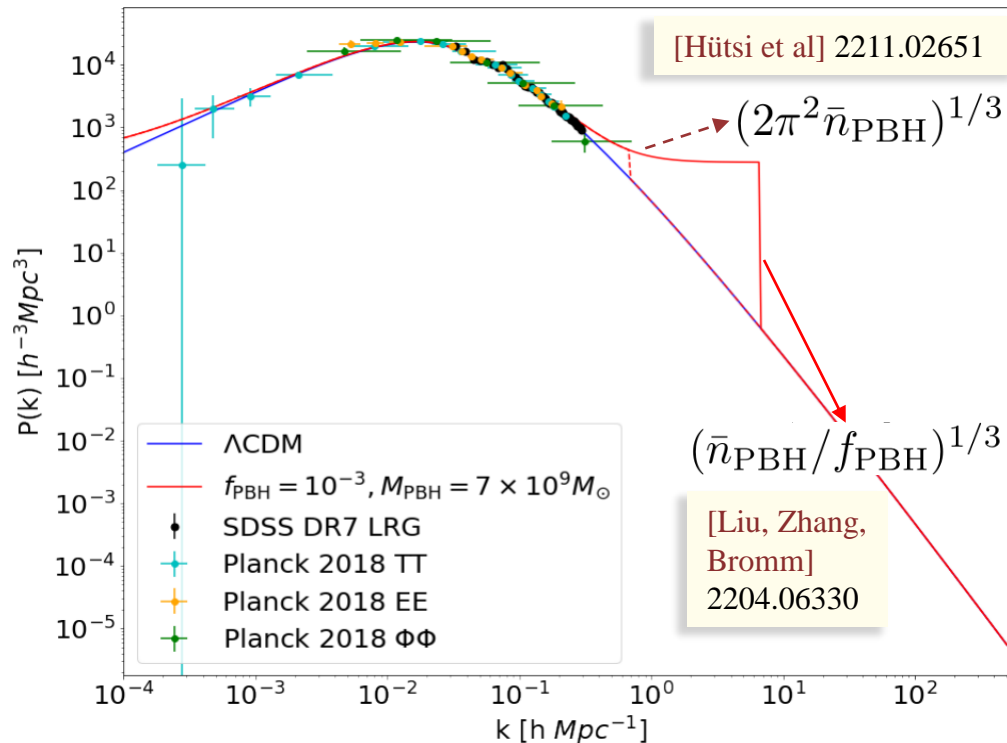
$$\delta_{\text{DM}}^0 = \delta_{\text{ad}}^0 + f_{\text{PBH}} \delta_{\text{PBH}}^0 \approx \sqrt{\frac{f_{\text{PBH}} M_{\text{PBH}}}{\tilde{M}}}$$

[Afshordi, McDonald, Spergel] astro-ph/0302035  
[Inma, Ali-Haimoud] 1907.08129

2. **Seed Effect:** If  $f_{\text{PBH}} < \frac{M_{\text{PBH}}}{\tilde{M}}$ , evolve in **isolation**. They generate

$$\delta_{\text{PBH}}^0 = \frac{M_{\text{PBH}}}{\tilde{M}}, \text{ which grow linearly and thus } \tilde{M} \approx \frac{z}{z_{\text{eq}}} M_{\text{PBH}}.$$

# Matter Power Spectrum (Poisson effect)



➤ The isocurvature perturbations induce modification of the matter-power spectrum:

$$P(k) = P_{ad}(k) + P_{iso}(k) ,$$

$$P_{iso}(k) \simeq \begin{cases} \frac{(f_{PBH} D(0))^2}{\bar{n}_{PBH}} , & \text{if } k \leq k_{cut} \\ 0 , & \text{otherwise} \end{cases}$$

where  $D(0) \approx a/a_{eq}$  (at late times) is the growth factor.

# Accelerated Galaxy Formation and JWST

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- 1. Poisson Effect:** We use modified **Press-Schechter (PS)** formalism to compute the halo mass function  $n(M_h, z)$ . Then the expected number density of galaxies is given by

$$n_{\text{gal}}(M_{\star} \geq M_{\star}^{\text{obs}}) = \int_{M_h^{\text{cut}}}^{\infty} \frac{dn(z_{\text{obs}}, M_h)}{dM_h} dM_h .$$

[Sheth & Tormen]  
[astro-ph/9901122]

The JWST signature can be expressed as  $n_{\text{gal}}(M_{\star} \geq 10^{10.8} M_{\odot}) \simeq 10^{-5} \text{Mpc}^{-3}$  at  $z_{\text{obs}} \sim 8$ .

- 2. Seed Effect:** Due to its highly non-linear nature, this effect can be examined properly only using **simulations**. We can still determine the part of the parameter space compatible with JWST by requiring:  
i)  $f_{\text{PBH}} < M_{\text{PBH}}/\tilde{M}$ , ii)  $\bar{n}_{\text{PBH}} \geq 10^{-5} \text{Mpc}^{-3}$ , iii)  $\tilde{M}(M_{\text{PBH}}, z_{\text{obs}}) \geq M_h(M_{\star} \sim 10^{11} M_{\odot})$ .

[Liu, Zhang, Bromm] 2204.06330

# Observational Constraints

- **CMB  $\mu$  distortion:** The PBH formation from large-amplitude Gaussian primordial fluctuations leaves imprints in the CMB, strictly **constraint** by COBE/FIRAS.

[Nakama et al]  
1609.02245

Large **non-Gaussianities (NGs)** : 
$$P(\zeta) = \frac{1}{2\sqrt{2}\tilde{\sigma}\Gamma(1+1/p)} \exp\left[-\left(\frac{|\zeta|}{\sqrt{2}\tilde{\sigma}}\right)^p\right]$$
  $p = 2$ : Gaussian

- **Large-scale structure (LSS):** The non-observation of different types of **cosmic structures** can be used to constrain population of PBHs.

$$\tilde{M} < \begin{cases} 10^{10} M_{\odot} & \text{at } z \sim 7 \text{ (dwarf galaxies)} \\ 10^{12} M_{\odot} & \text{at } z \sim 3 \text{ (MW-type galaxies)} \\ 10^{14} M_{\odot} & \text{at } z \sim 1 \text{ (galaxy clusters)} \end{cases}$$

[Carr et al]  
1801.00672



[Ivanov, Toomey, ST] TBA

- **Lyman- $\alpha$  forest:** sensitive to modifications to the PS at scales  $0.1 < k \text{ Mpc} < 10$ . The most recent **bounds** yield  $f_{\text{PBH}} M_{\text{PBH}} < 170 M_{\odot}$  ( $M_{\text{PBH}} < 10^5 M_{\odot}$ ).

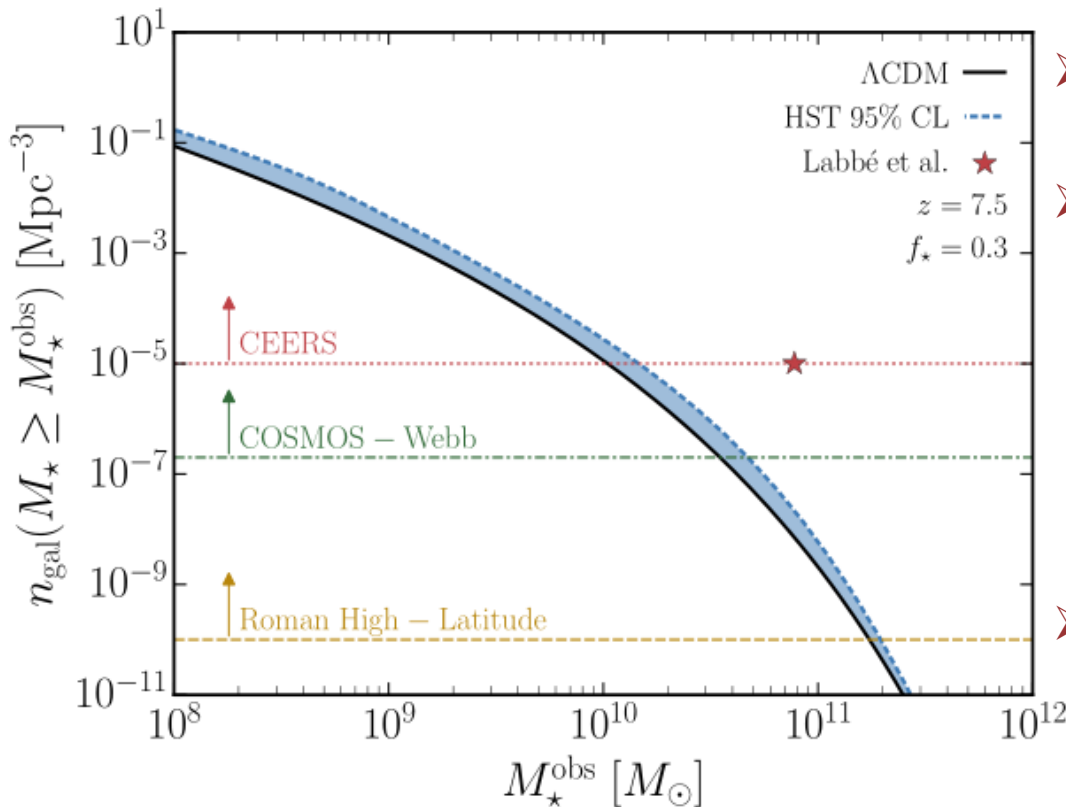
[Murgia et al] 1903.10509

improve the Ly- $\alpha$  bound!



# Ultraviolet Luminosity Function (UV LF)

Novel!



- Young massive stars emit in the **ultraviolet**.
- The Hubble Space Telescope (HST) has already **probed** the range  $7 < z < 10$  via the **UV LF**:

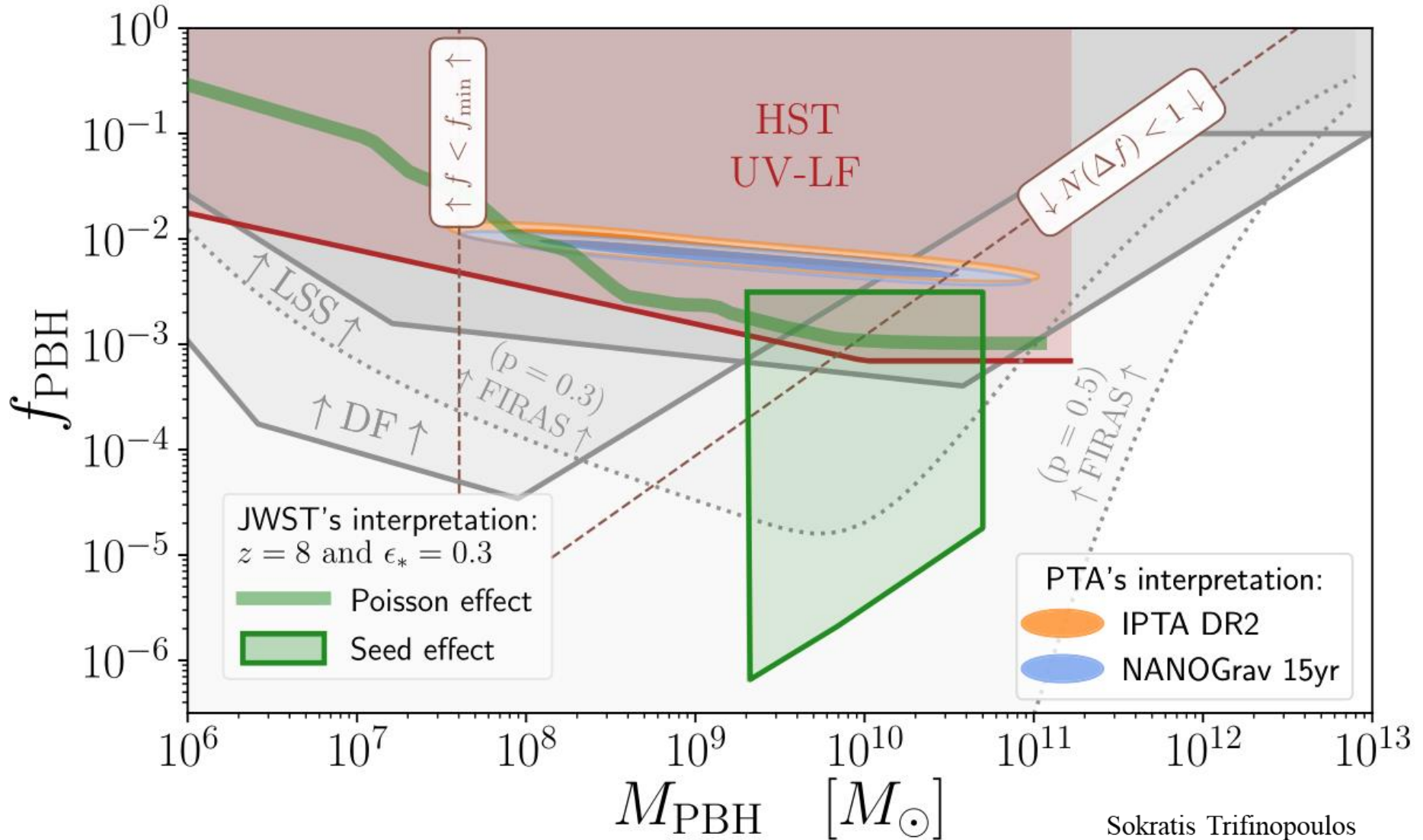
$$\Phi_{\text{UV}} = \underbrace{\frac{dn}{dM_{\text{h}}}}_{\text{cosmology}} \times \underbrace{\frac{dM_{\text{h}}}{dM_{\text{UV}}}}_{\text{astrophysics}}$$

- A cosmological solution to the JWST anomaly is **disfavored**.

[Sabti, Munoz, Kamionkowski] 2305.07049,  
 [Sabti, Munoz, Blas] 2110.13161

# PBH parameter space

[Gouttenoire, ST, Valogiannis,  
Vanvlasselaer ] 2307.01457



# Outline

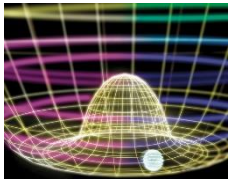
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## I. Observations



## II. Primordial Black Holes



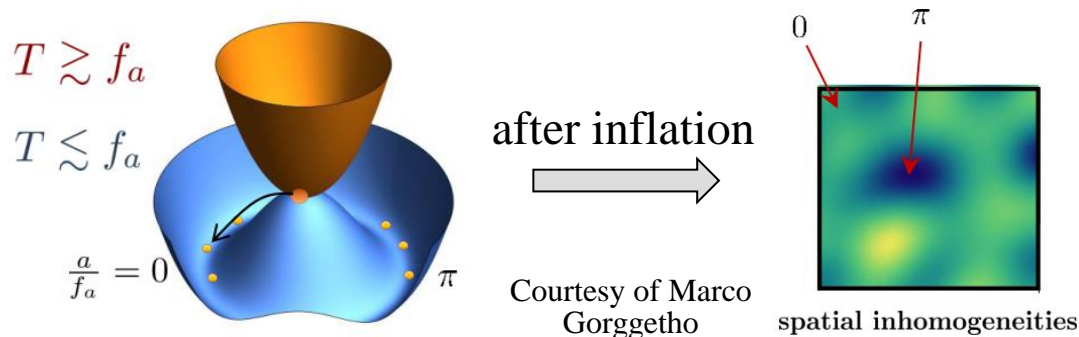
## III. Axion Clusters



[Gorghetto, Foster ST, Valogiannis ] TBA

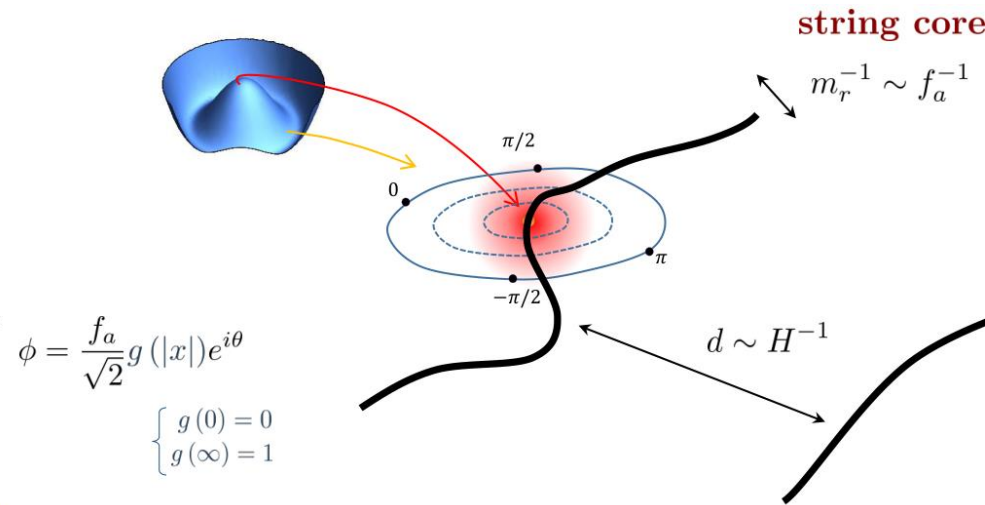
# Post-inflationary axions

- **Axion:** Goldstone boson of a spontaneously broken global  $U(1)_{\text{PQ}}$  symmetry at scale  $f_a$ :  $\varphi = \frac{1}{\sqrt{2}}(r + f_a)e^{i\frac{a}{f_a}}$ .
- $U(1)_{\text{PQ}}$  is also explicitly broken at scale  $\Lambda \ll f_a$  by non-perturbative effects that generate a periodic potential and the **axion mass**  $m_a \approx \Lambda^2/f_a$ .
- The initial conditions for the axion field are inhomogeneous if  $T_{\text{RH}} > f_a$  (**thermal** fluctuations) or  $H_I > f_a$  (**quantum** inflationary fluctuations):



# Axion Strings

➤ The e.o.m. of  $\varphi$  admit in this case non-trivial solutions: **axion strings**.

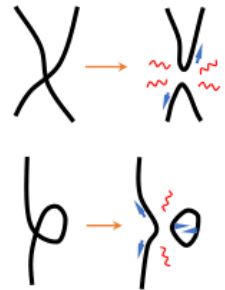


[Gorghetto, Hardy, Nicolaescu] 2101.11007

➤ The strings contain energy which is proportional to

$$\mu = \pi f_a^2 \log \frac{m_r}{H}.$$

➤ When they interact with other strings they can release energy in the form of **axion radiation**.



➤ The string network reaches an **attractor** solution (scaling regime), in which the number of strings per Hubble patch remains constant.



# Isocurvature perturbations: Axion Clusters

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- The scaling regime is maintained by axion radiation and **GW energy emission**.
- When the Hubble scale is  $H_* \sim m_a$ , **domain walls** bounded by the strings form and subsequently **annihilate** rendering the network unstable.
- Inhomogeneities in the axion field develop during this period that lead to the **formation of ACs** of mass  $M_{AC} \propto \rho_a k_*^{-3}$ , where  $k_* \propto f_{AC}^{1/4} m_a^{1/2}$ .

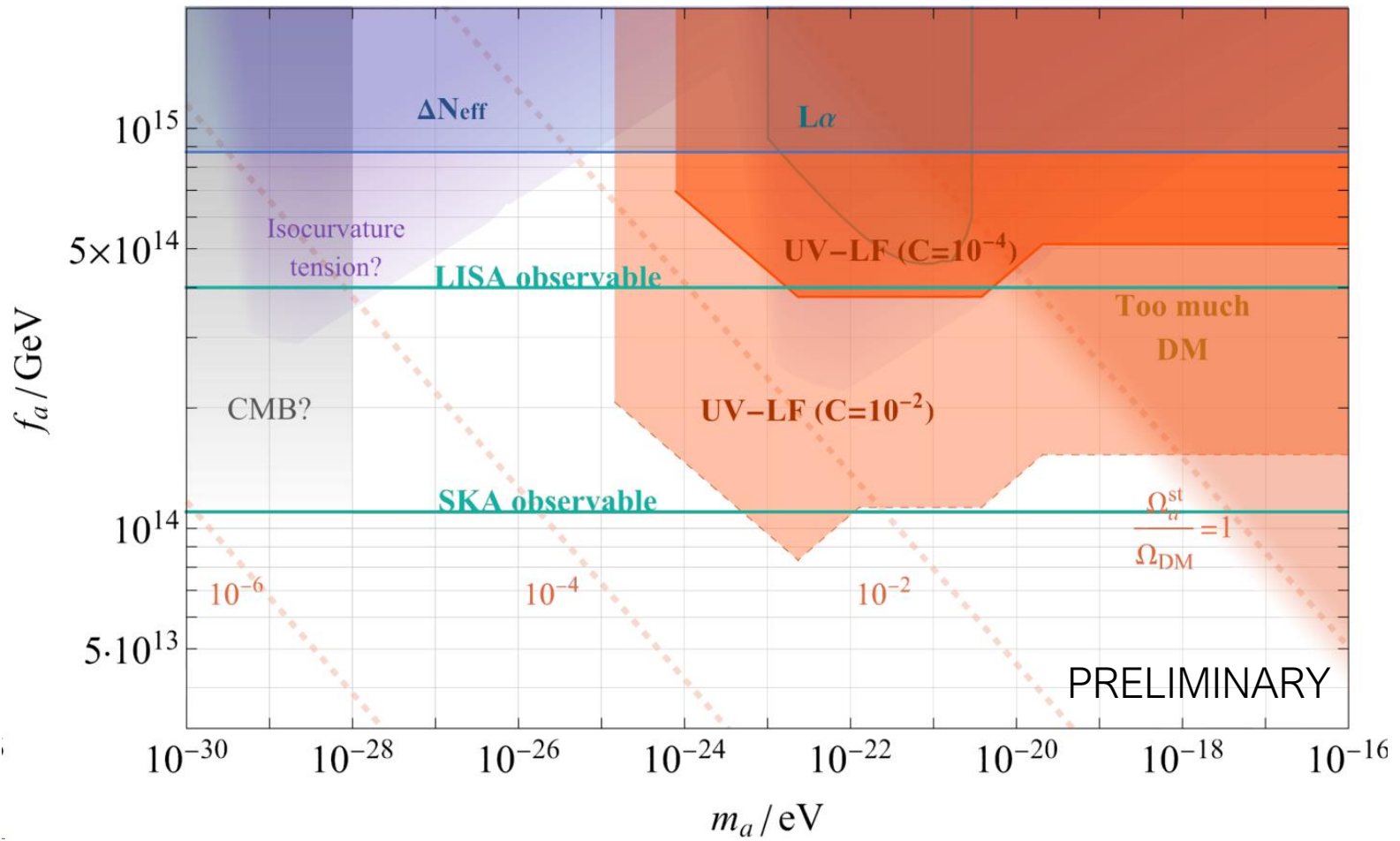
- They correspond to **isocurvature perturbations** of the form:

$$P_{\text{iso}}(k) \simeq \begin{cases} 2\pi^2 C (f_{AC} D(0))^2 / k_*^3, & \text{if } k \leq k_* \\ 0, & \text{otherwise} \end{cases}$$

[Buschmann, Foster,  
Safdi] 1906.00967  
[O'Hare, Perobon,  
Redondo, Wong]  
2112.05117

- Similarly to PBH, **LSS constraints** are imposed due to the accelerated structure formation induced by the AC seeds.

# Ultra-light axion parameter space



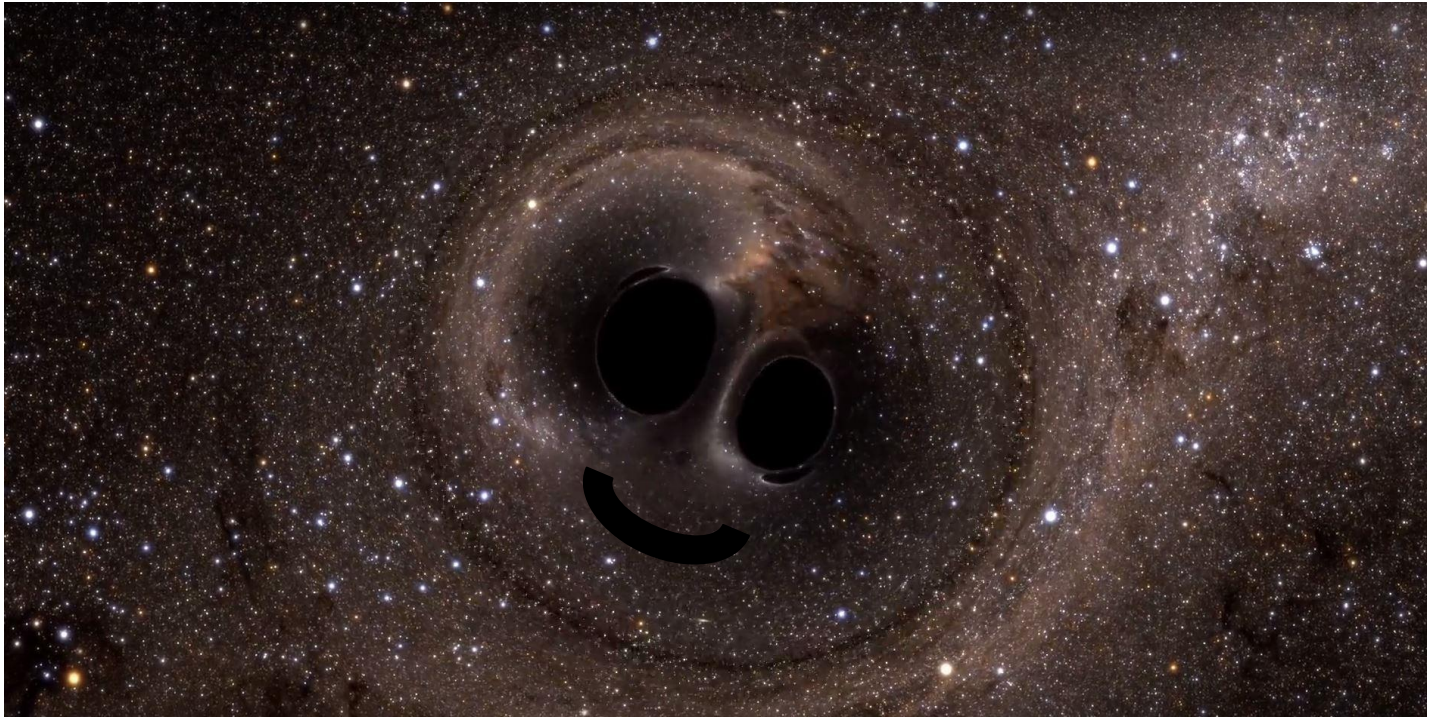
# Conclusions & Future Outlook

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- We explore for the first time a common explanation of the **PTA gravitational waves** signal and the **JWST early galaxies** observations.
- The PBH populations needed to source the PTA GW signal are partly excluded by **LSS** and decisively excluded by the **UV LF** constraint.
- The PBH and ACs interpretations of the JWST extreme galaxies with the **Poisson** effect is excluded due to **UV LF**, while the one based on PBH **seed** effect is in principle still viable for  $f_{\text{PBH}} < 10^{-3}$  (needs very large NGs).
- A **spectroscopic** analysis will provide the final verdict on whether the JWST observations constitute a  $\Lambda$ CDM anomaly.
- Future increase in observation time of PTAs and in number of detected pulsars might facilitate the resolution of **individual sources** at larger frequencies and thus enable the more careful examination of NP scenarios.

**Thank you!!!!**

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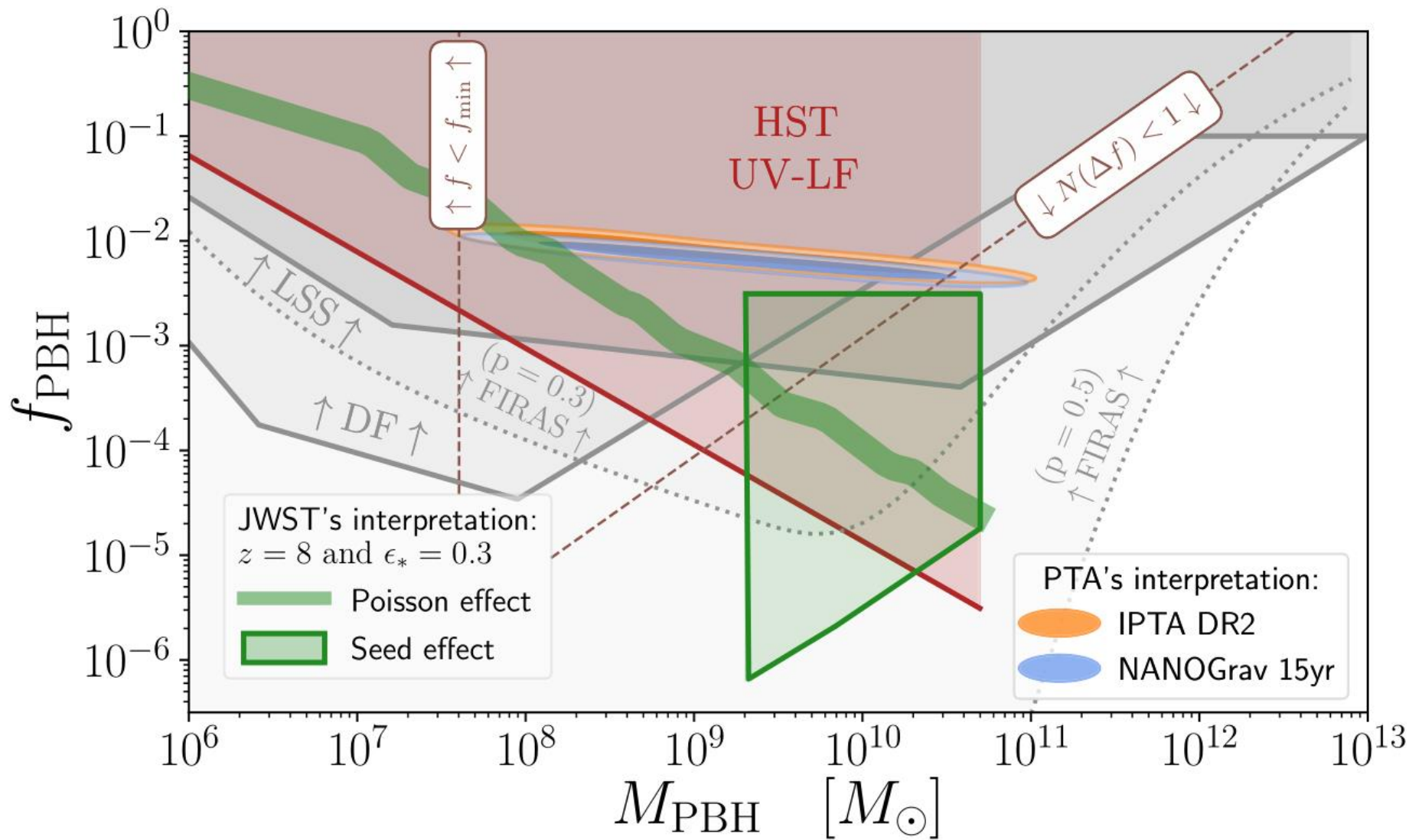


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# Backup slides



# PBH parameter space



# Spectroscopy vs Photometry

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Method	Advantages	Disadvantages
<u>Spectroscopy</u> : record the intensity of dispersed light vs wavelength.	<ul style="list-style-type: none"><li>✓ excellent discrimination between wavelengths</li><li>✓ individual spectral features</li></ul>	<ul style="list-style-type: none"><li>✗ difficult to obtain multiple spectra due to wide range of spreading over the detector</li></ul>
<u>Photometry</u> : record images of the source light after allowing it to pass through colored filters.	<ul style="list-style-type: none"><li>✓ better signal-to-noise ratios (fainter objects reachable)</li><li>✓ examine thousands of sources simultaneously</li></ul>	<ul style="list-style-type: none"><li>✗ effective wavelength resolution is limited by the filter bandpass</li><li>✗ no individual spectral features</li></ul>

# GW Energy Density Spectrum

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- We employ a power broken-law and we truncate the frequency at the end of the ring-down phase:

$$\Omega_{\text{GW}} h^2 \simeq \Omega_{\text{peak}} S(f) \Theta(2f_{\text{peak}} - f), \quad S(f) = \frac{f_{\text{peak}}^b f^a}{\left( b f^{\frac{a+b}{c}} + a f_{\text{peak}}^{\frac{a+b}{c}} \right)^c}$$

- The peak amplitude and frequencies are:

$$\Omega_{\text{peak}} \simeq 0.05 f_{\text{PBH}}^3 \left( 1.5 \frac{M_{\text{PBH}}}{10^{12} M_{\odot}} \right)^{-0.3}, \quad f_{\text{peak}} \simeq 5000 M_{\odot} / M_{\text{PBH}}$$

- Due to environmental effects, we discard frequencies below:

$$f_{\text{min}} = \left( \frac{T_{\text{max}}}{\delta_2} \right)^{-\frac{3}{8}},$$

and to ensure that the signal is stochastic, high frequencies that yield

$$N(f, \Delta f) = \int_{f_0 - \Delta f/2}^{f_0 + \Delta f/2} \frac{df}{f} \int_0^{\infty} dz \frac{4\pi d_c^2(z)}{H(z)} R(z) \tau_{r, <} < 1$$

# CMB $\mu$ distortion

- PBH form when large-amplitude primordial fluctuations  $\zeta$  undergo spherical gravitational collapse upon horizon reentry. We may parametrize the  $\zeta$  PDF as:

$$P(\zeta) = \frac{1}{2\sqrt{2}\tilde{\sigma}\Gamma(1+1/p)} \exp\left[-\left(\frac{|\zeta|}{\sqrt{2}\tilde{\sigma}}\right)^p\right]$$

$p = 2$ : Gaussian  $\leftarrow$

[Nakama Suyama, Yokoyama] 1609.02245  
[Hooper, Ireland, Krnjaic, Stebbins] 2308.00756

- Fluctuations that dissipate via Silk damping during the photon diffusion scale,  $5 \times 10^4 < z < 2 \times 10^6$ , **inject energy** in the photon bath and modify the number of photons w.r.t. the black-body equilibrium.

- Let us consider a sharp feature  $\Delta\mathcal{P}_\zeta = 2\pi^2\sigma^2k^{-2}\delta(k - k_\delta)$ , the weighted total energy release  $\mu$  is strictly **constrained** by COBE/FIRAS:

$$\mu \simeq 2.2\sigma^2 \left[ \exp\left(-\frac{\hat{k}_\delta}{5400}\right) - \exp\left(-\left[\frac{\hat{k}_\delta}{31.6}\right]^2\right) \right] < 4.7 \times 10^{-5}$$

Solution: Large NGs  $p < 0.3$

[Chubla, Erickcek, Ben-Dayan] 1203.2681