

New light on light dark sectors



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Xmas Theoretical Physics Workshop

National and Kapodistrian University of Athens

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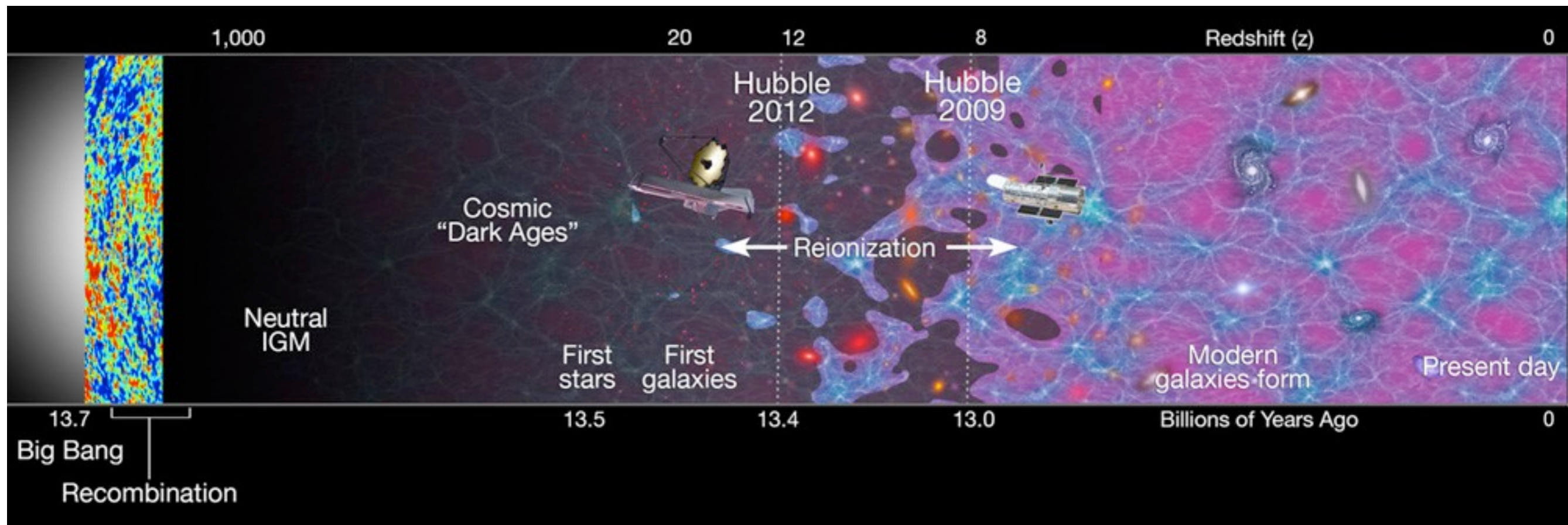
European Research Council
Established by the European Commission

FWF

Der Wissenschaftsfonds.

Cosmic history

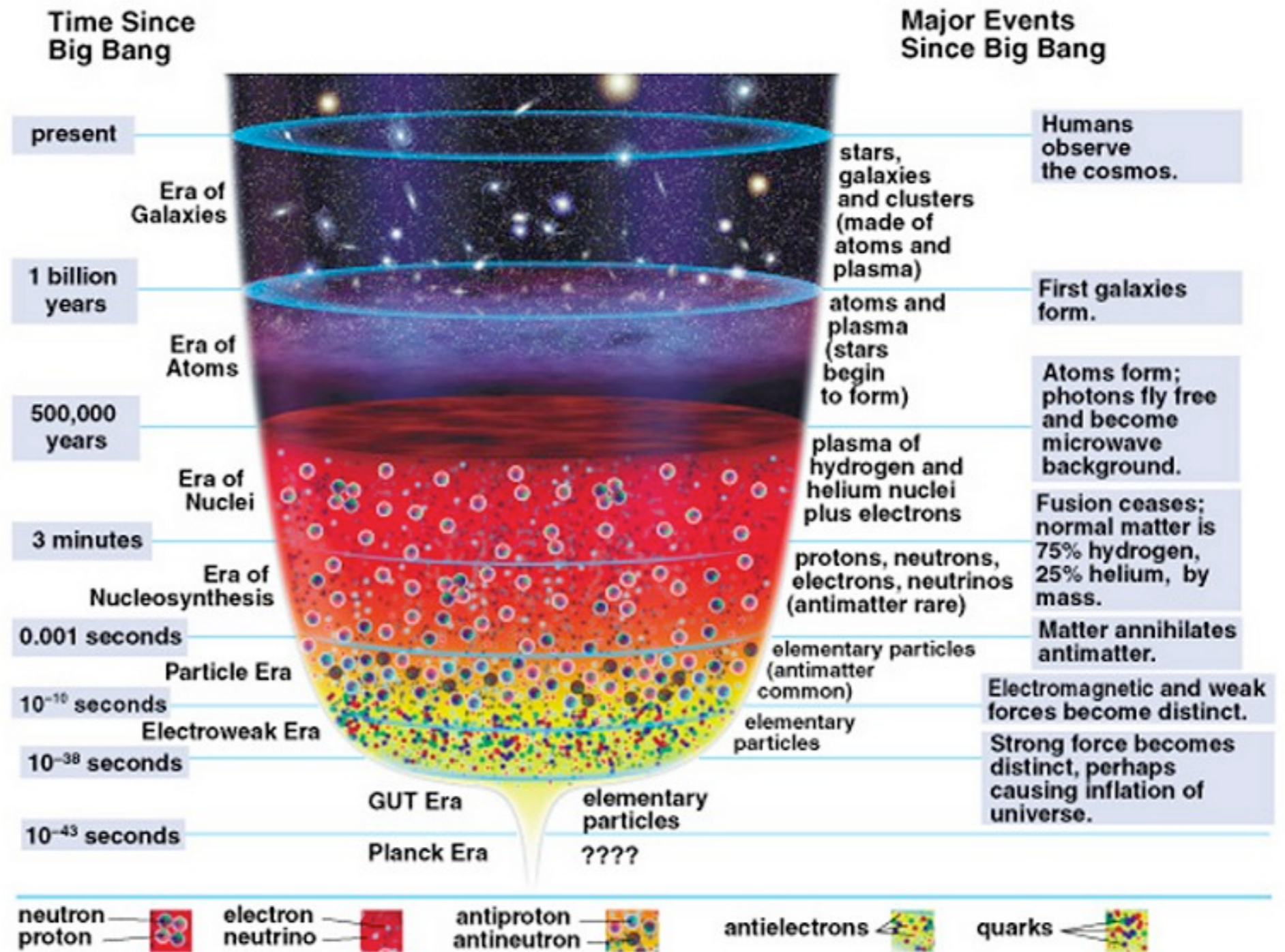
An astronomer's view:



All evidence for Dark Matter (DM) comes from astronomical and cosmological observations, existence is inferred from gravity alone.

Cosmic history

A particle physicist's view



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Our “New Physics Laboratory”

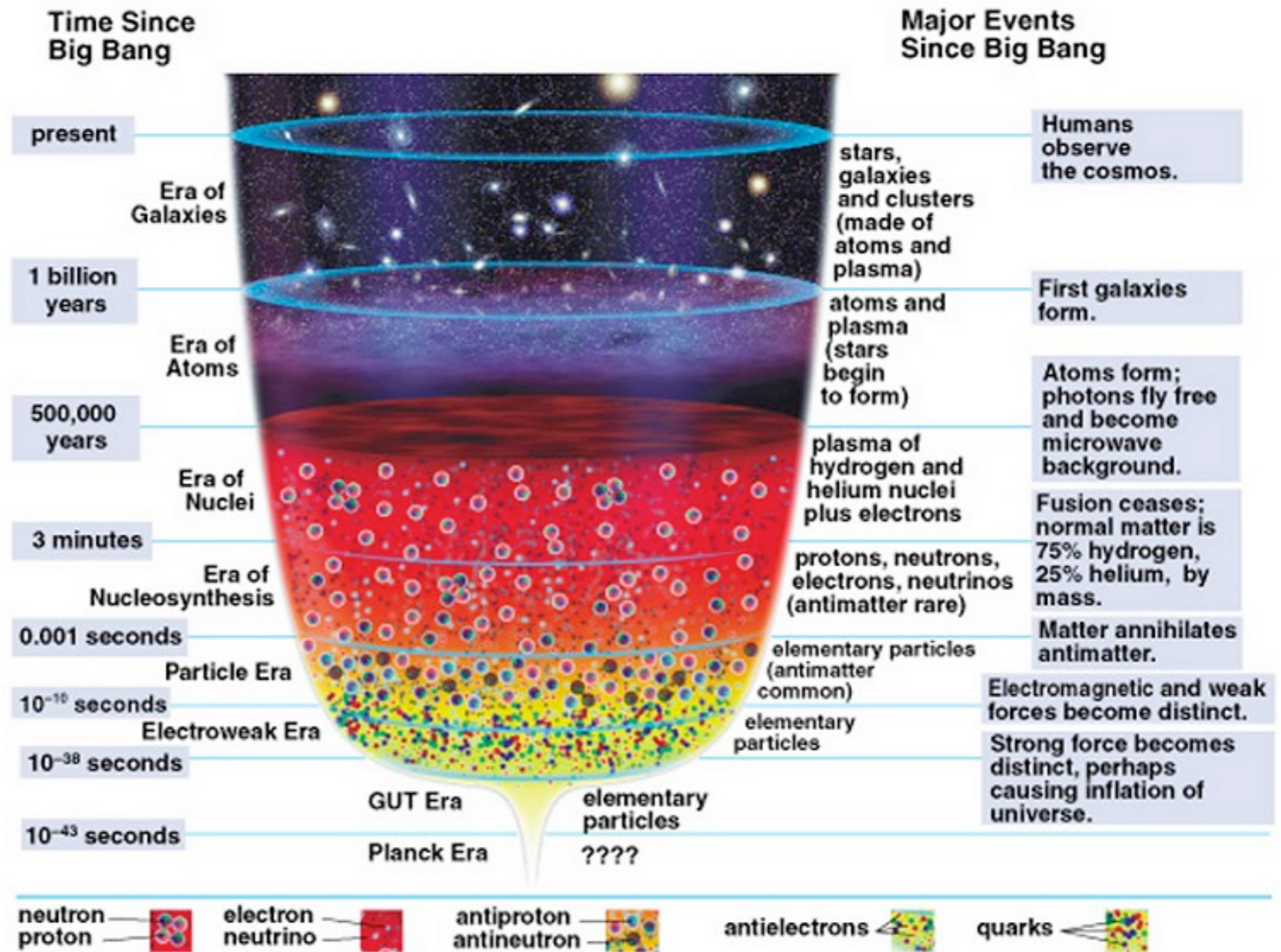
A particle physicist's view

experimental searches
stellar astrophysics

21cm cosmology

cosmic microwave
background

primordial
nucleosynthesis
dark matter genesis
Baryogenesis



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Outline

one central piece of evidence of dark matter and potential solutions

1. showcase of a dark sector below the GeV mass scale

“photon portal” (experiments, astrophysics, cosmology)

[arXiv:1811.04095](https://arxiv.org/abs/1811.04095)

[arXiv:2001.06042](https://arxiv.org/abs/2001.06042)

[arXiv:1908.00553](https://arxiv.org/abs/1908.00553)

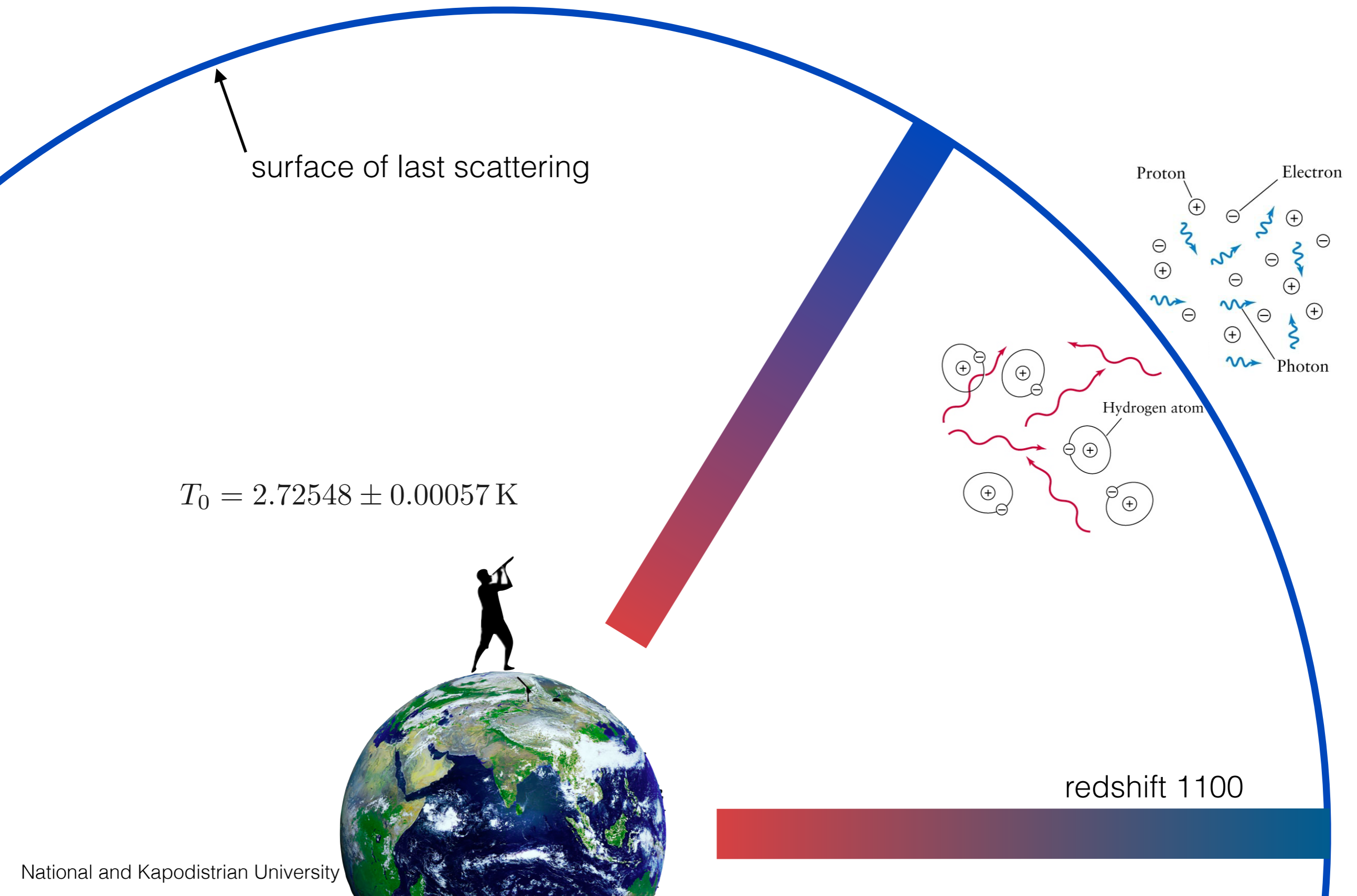
[arXiv:2303.13643](https://arxiv.org/abs/2303.13643)

2. brief remarks on MeV - scale thermal dark matter freeze-out

[arXiv:2205.05714](https://arxiv.org/abs/2205.05714)

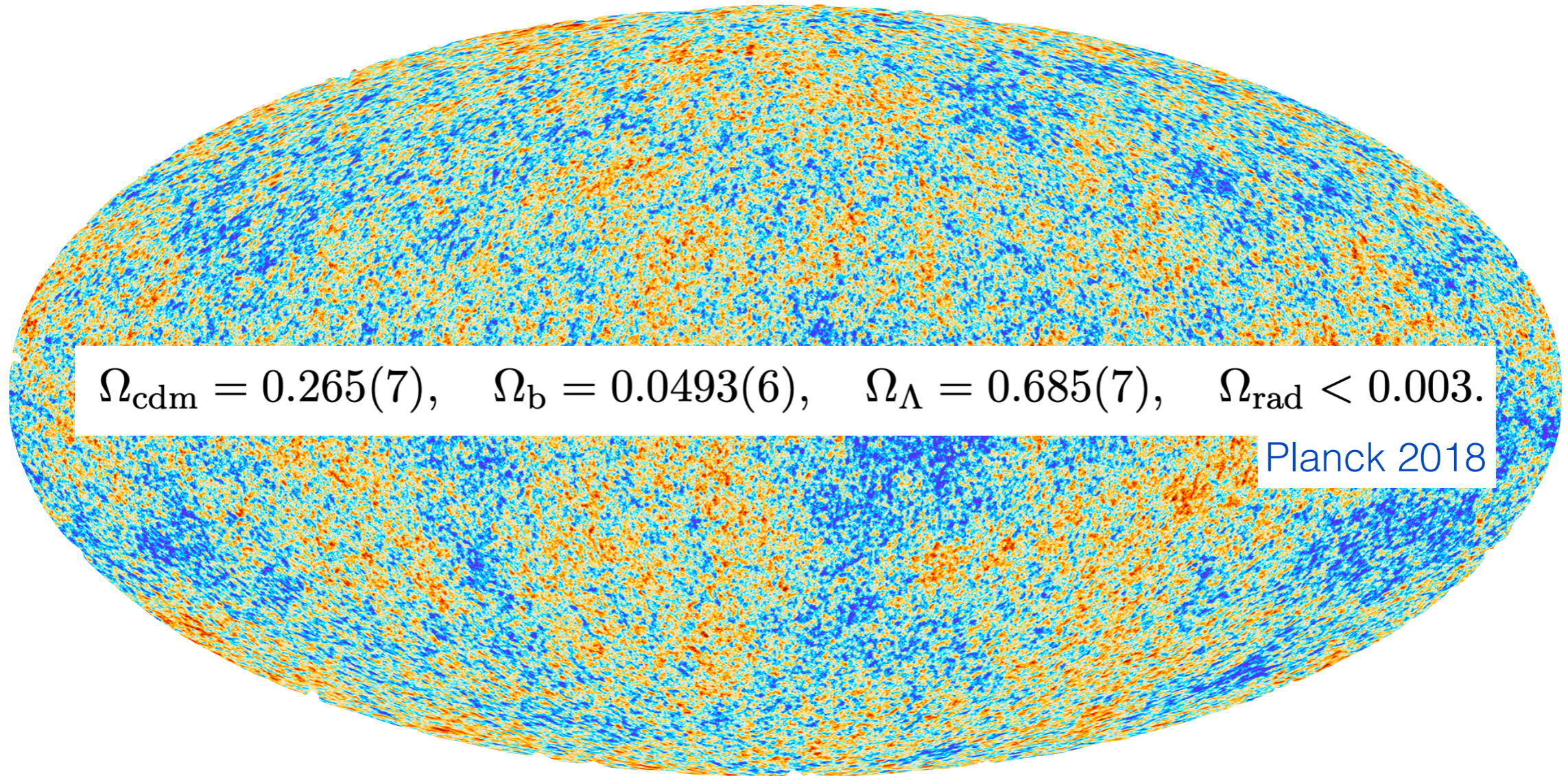
[arXiv:2310.06611](https://arxiv.org/abs/2310.06611)

Cosmic Microwave Background (Gpc)



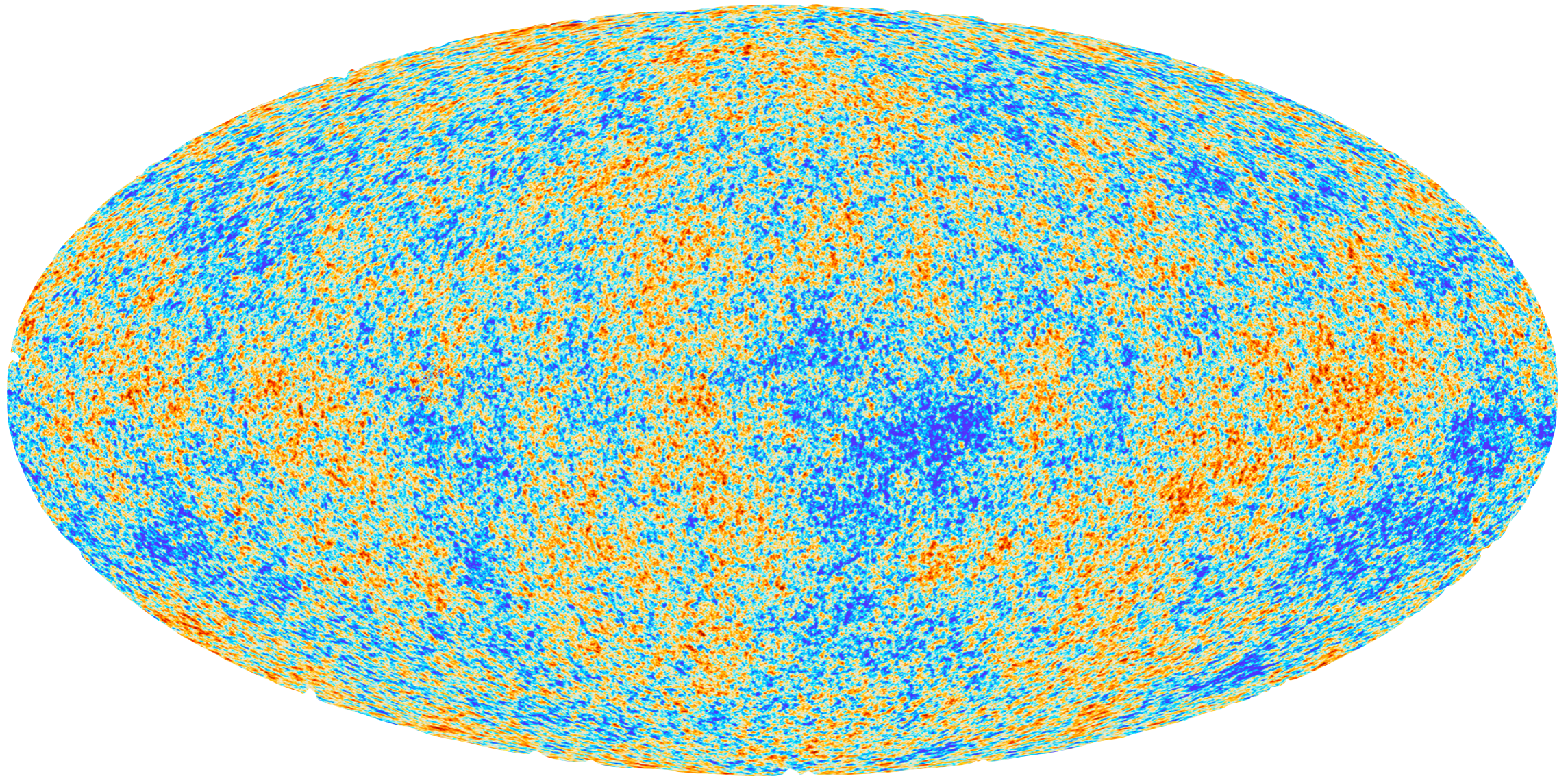
Dark Matter is key...

... in explaining the observations of the CMB (linear theory)



Dark Matter is key...

... in explaining the observations of the
cosmic microwave background

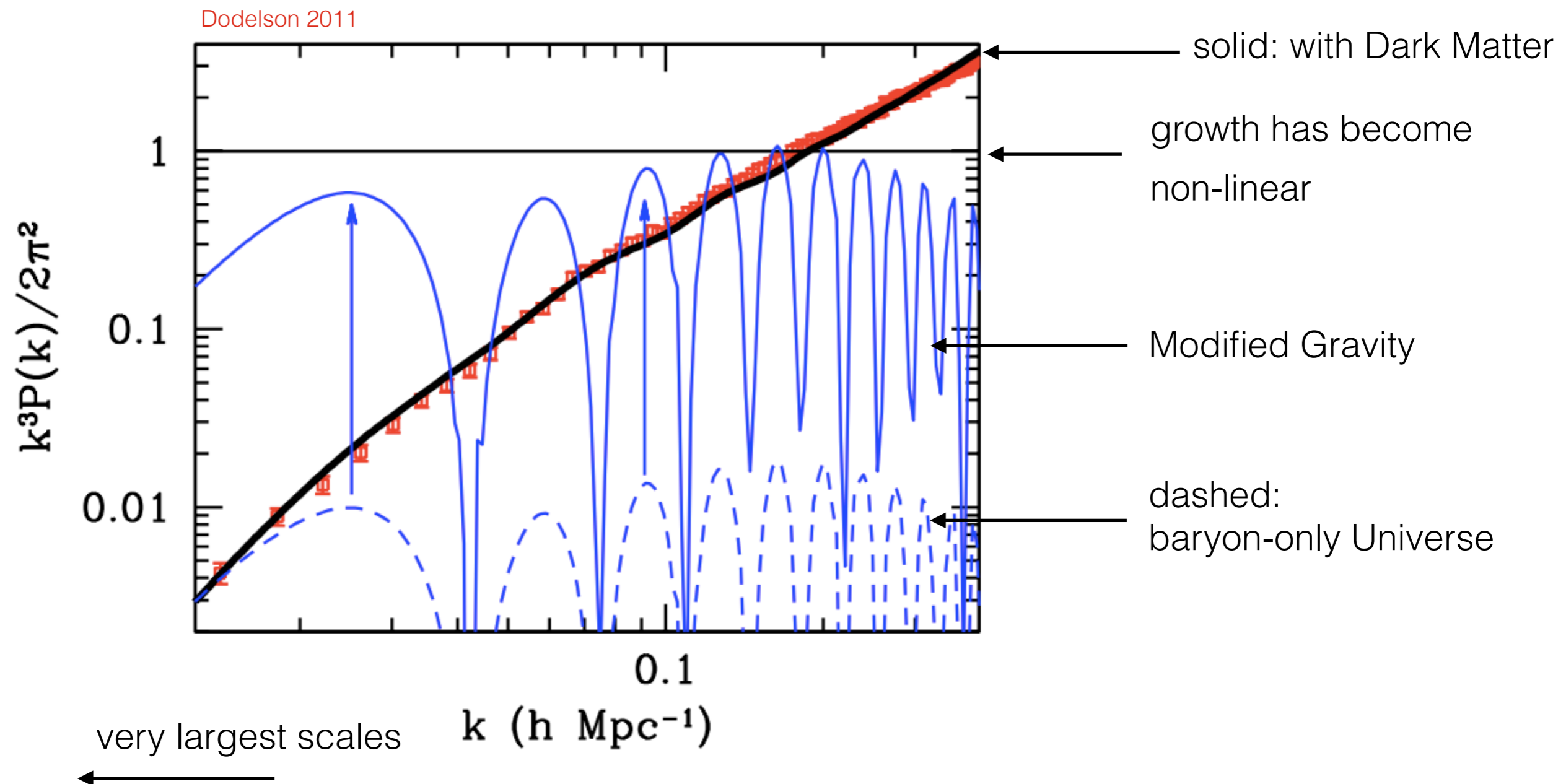


... in the formation of large scale structure
such as galaxies and clusters of galaxies

Dark Matter assisted growth

Growth of structure is quantified by the power spectrum

$$\frac{k^3 P(k)}{2\pi^2} = \left(\frac{\delta\rho}{\rho} \right)_k^2$$



OK, the Dark Matter is there.

What can it be?

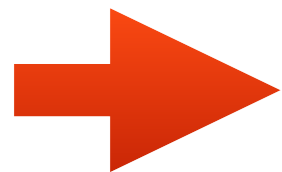
Modified Gravity?

successes on Galaxy scales,
but fails elsewhere

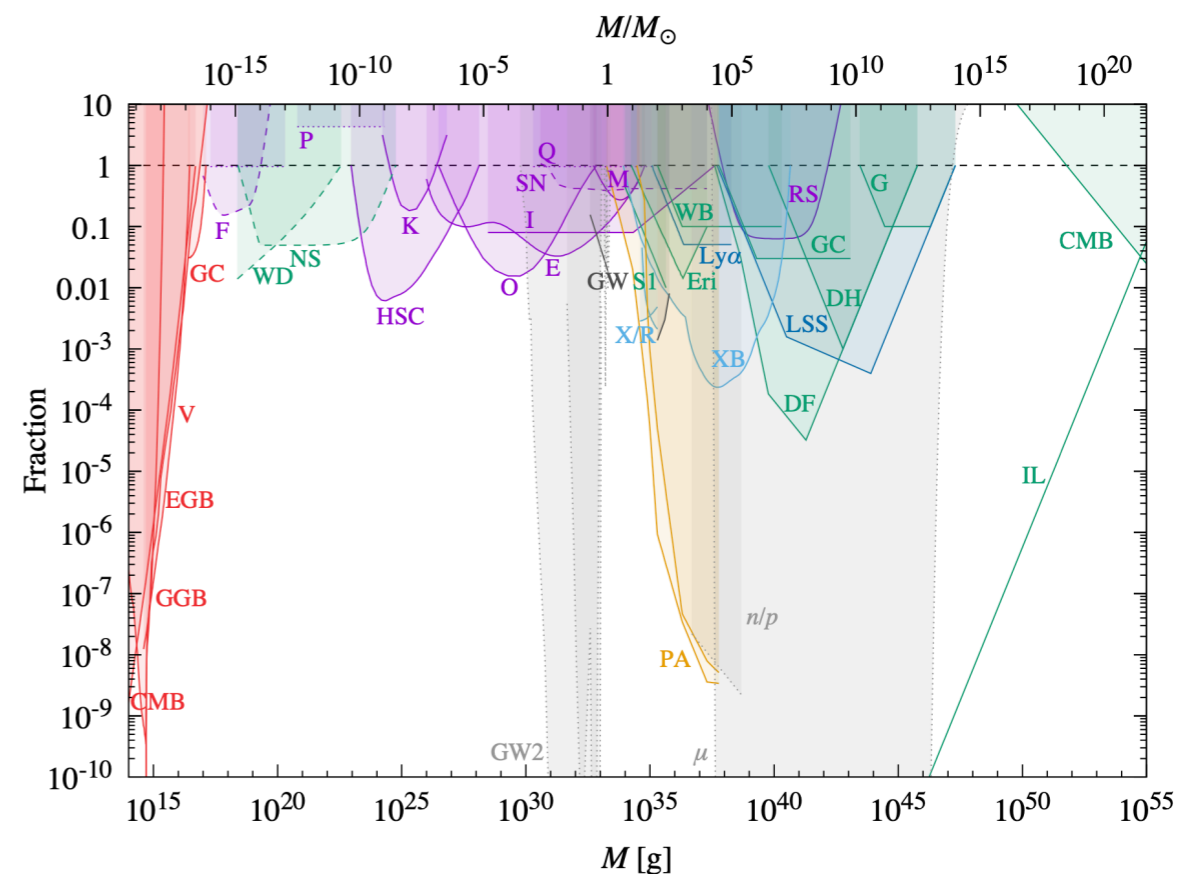
Primordial Black holes?

asteroid mass black holes may
still make up 100% of DM

New particle(s) of nature?



our best bet. This talk.



The missing mass - what is it?

New particle(s) of nature?

electroweak scale
WIMPs, GeV-scale DM

axion, ALPs

keV sterile neutrinos

gravitinos

other super-WIMPs such
as Dark Photons



A model beloved for its
inner beauty

$$\begin{aligned}
\frac{1}{e} \mathcal{L}_{\text{sugra}} = & -\frac{M_P^2}{2} R + g_{ij^*} \tilde{\mathcal{D}}_\mu \phi^i \tilde{\mathcal{D}}^\mu \phi^{*j} - \frac{1}{2} g^2 [(\text{Re}f)^{-1}]^{ab} D_{(a)} D_{(b)} \\
& + ig_{ij^*} \bar{\chi}_L^j \gamma^\mu \tilde{\mathcal{D}}_\mu \chi_L^i + \varepsilon^{\mu\nu\rho\sigma} \bar{\psi}_{L\mu} \gamma_\nu \tilde{\mathcal{D}}_\rho \psi_{L\sigma} \\
& - \frac{1}{4} \text{Re}f_{ab} F_{\mu\nu}^{(a)} F^{\mu\nu(b)} + \frac{1}{8} \varepsilon^{\mu\nu\rho\sigma} \text{Im}f_{ab} F_{\mu\nu}^{(a)} F_{\rho\sigma}^{(b)} \\
& + \frac{i}{2} \text{Re}f_{ab} \bar{\lambda}^a \gamma^\mu \tilde{\mathcal{D}}_\mu \lambda^b - e^{-1} \frac{1}{2} \text{Im}f_{ab} \tilde{\mathcal{D}}_\mu [e \bar{\lambda}_R^a \gamma^\mu \lambda_R^b] \\
& + \left[-\sqrt{2} g \partial_i D_{(a)} \bar{\lambda}^a \chi_L^i + \frac{1}{4} \sqrt{2} g [(\text{Re}f)^{-1}]^{ab} \partial_i f_{bc} D_{(a)} \bar{\lambda}^c \chi_L^i \right. \\
& + \frac{i}{16} \sqrt{2} \partial_i f_{ab} \bar{\lambda}^a [\gamma^\mu, \gamma^\nu] \chi_L^i F_{\mu\nu}^{(b)} - \frac{1}{2M_P} g D_{(a)} \bar{\lambda}_R^a \gamma^\mu \psi_\mu \\
& \left. - \frac{i}{2M_P} \sqrt{2} g_{ij^*} \tilde{\mathcal{D}}_\mu \phi^{*j} \bar{\psi}_\nu \gamma^\mu \gamma^\nu \chi_L^i + \text{h.c.} \right] \\
& - \frac{i}{8M_P} \text{Re}f_{ab} \bar{\psi}_\mu [\gamma^m, \gamma^n] \gamma^\mu \lambda^a F_{mn}^{(b)} \\
& - e^{K/2M_P^2} \left[\frac{1}{4M_P^2} W^* \bar{\psi}_{R\mu} [\gamma^\mu, \gamma^\nu] \psi_{L\nu} - \frac{1}{2M_P} \sqrt{2} D_i W \bar{\psi}_\mu \gamma^\mu \chi_L^i \right. \\
& \left. + \frac{1}{2} \mathcal{D}_i D_j W \bar{\chi}_L^i \chi_L^j + \frac{1}{4} g^{ij^*} D_{j^*} W^* \partial_i f_{ab} \bar{\lambda}_R^a \lambda_L^b + \text{h.c.} \right] \\
& - e^{K/M_P^2} \left[g^{ij^*} (D_i W)(D_{j^*} W^*) - 3 \frac{|W|^2}{M_P^2} \right] + \mathcal{O}(M_P^{-2}),
\end{aligned}$$

Supergravity

A model beloved for its
outer beauty

$$\mathcal{L} = \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 - \lambda S^2(H^\dagger H)$$

Higgs portal

A model beloved for its
outer beauty

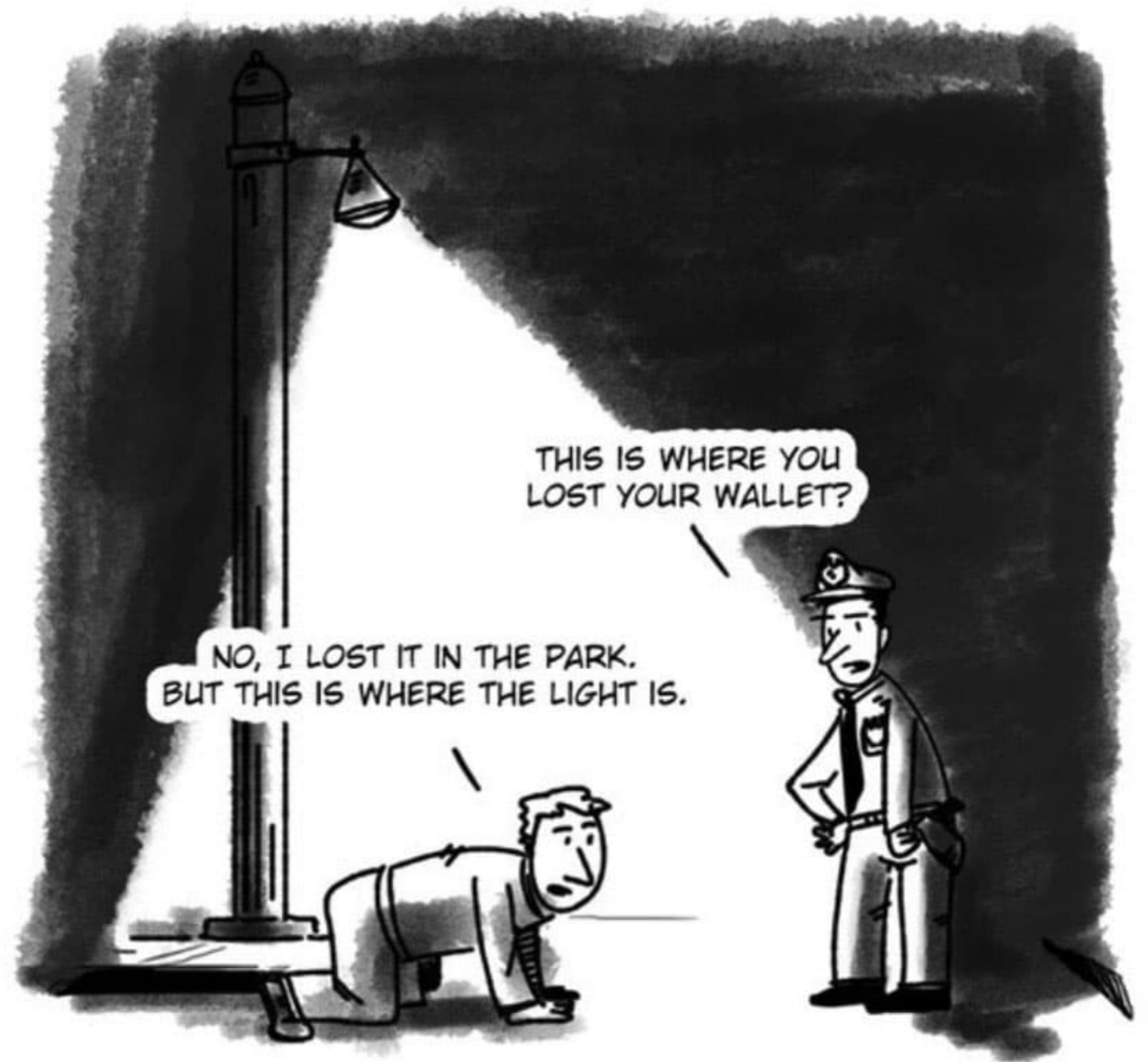
$$\mathcal{L} = \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 - \lambda S^2(H^\dagger H)$$

\Rightarrow experiment decides!

Higgs portal

Philosophy of this talk

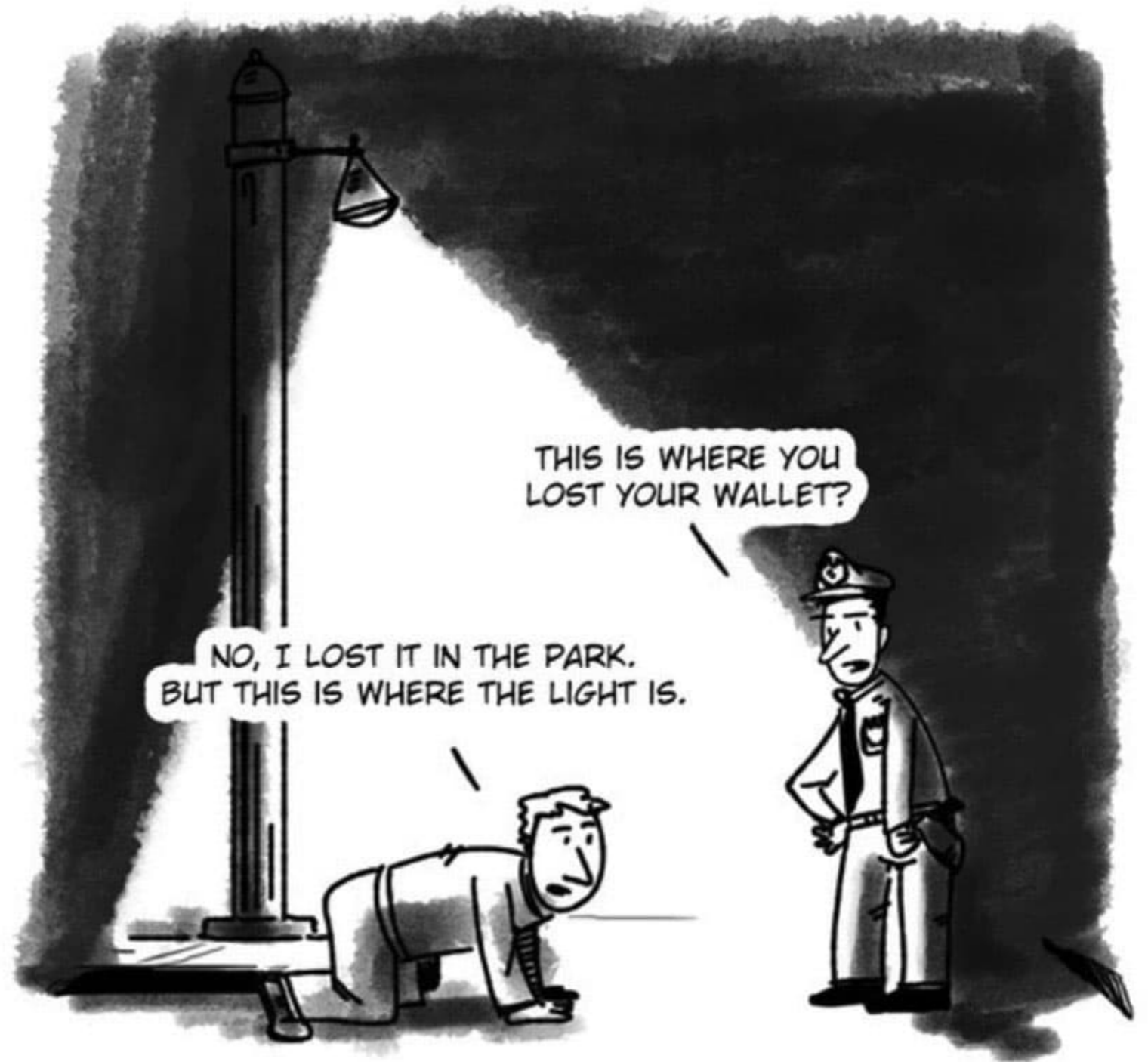
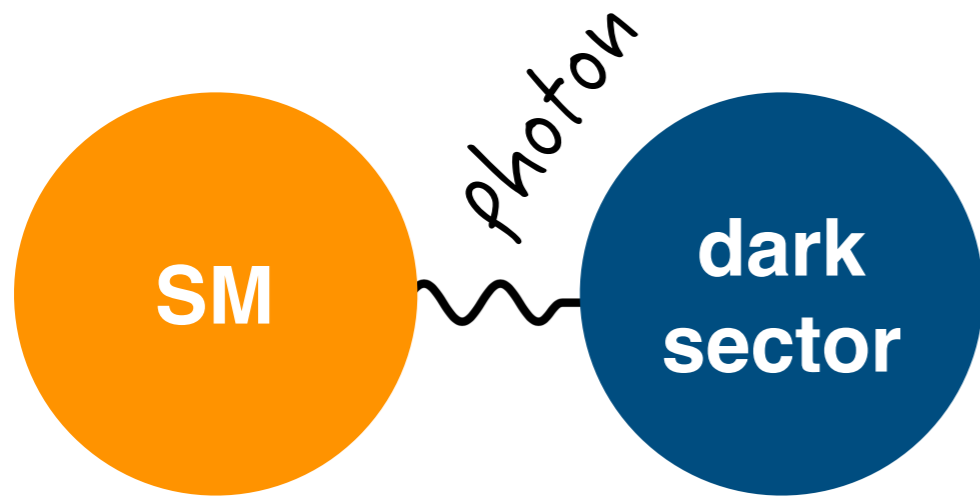
Streetlight effect or Drunkard search principle



Philosophy of this talk

Streetlight effect or Drunkard search principle

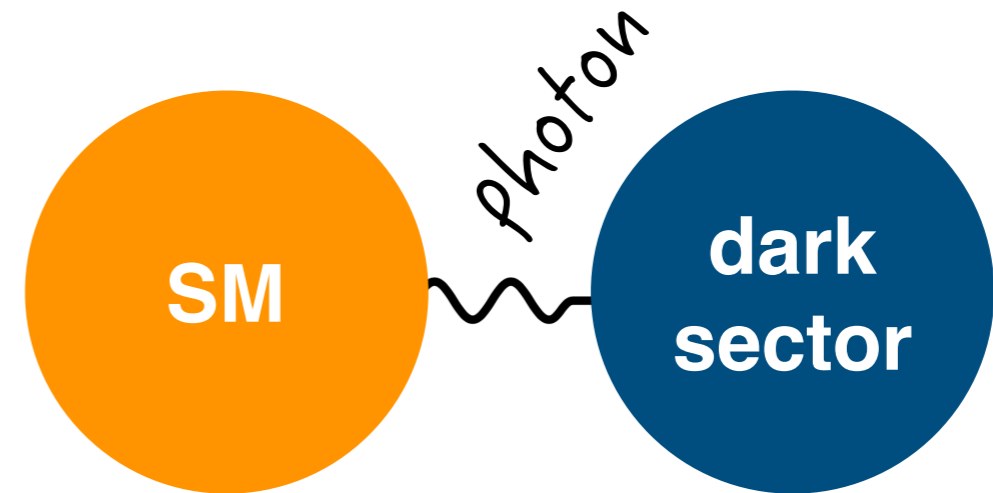
=> let's search under the lamppost



1. Dark states with EM form factors

Photon-portal

Dark Matter obviously needs to be (largely) neutral, but how dark is dark?



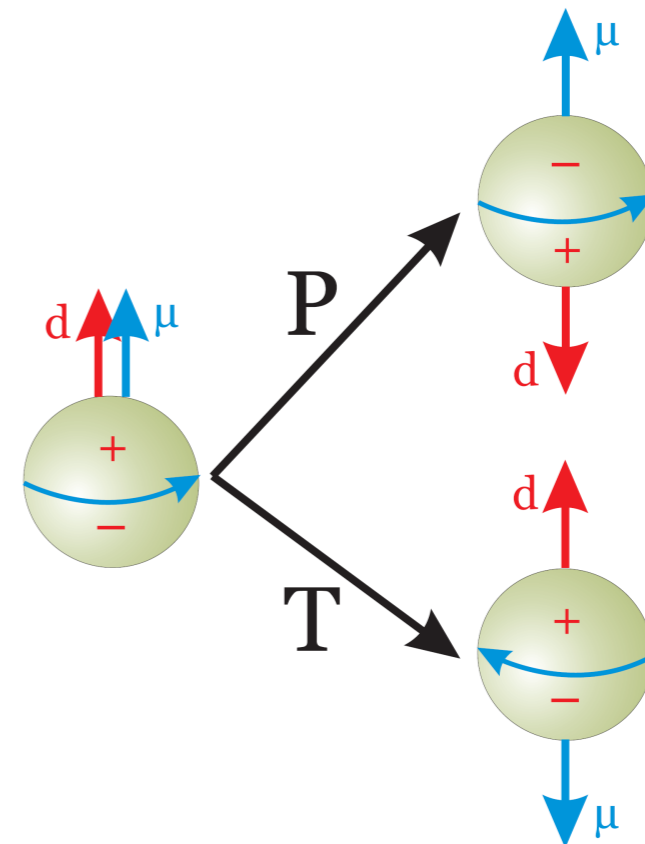
Even perfectly neutral particles can couple to photons

$$H_{\text{MDM}} = -\mu_\chi(\vec{B} \cdot \vec{\sigma}_\chi)$$

magnetic dipole moment (P and T even)

$$H_{\text{EDM}} = -d_\chi(\vec{E} \cdot \vec{\sigma}_\chi)$$

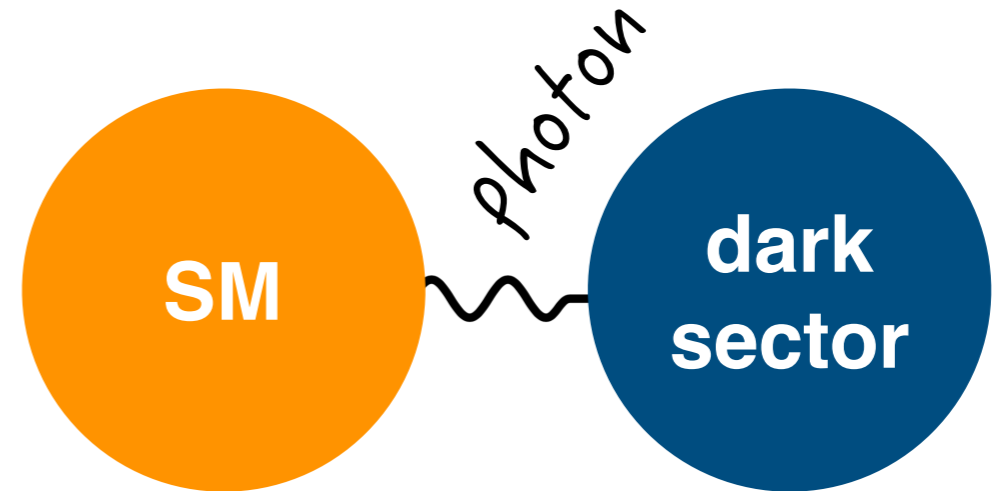
electric dipole (P and T odd => CP violating)



1. Dark states with EM form factors

Photon-portal

Dark Matter obviously needs to be (largely) neutral, but how dark is dark?



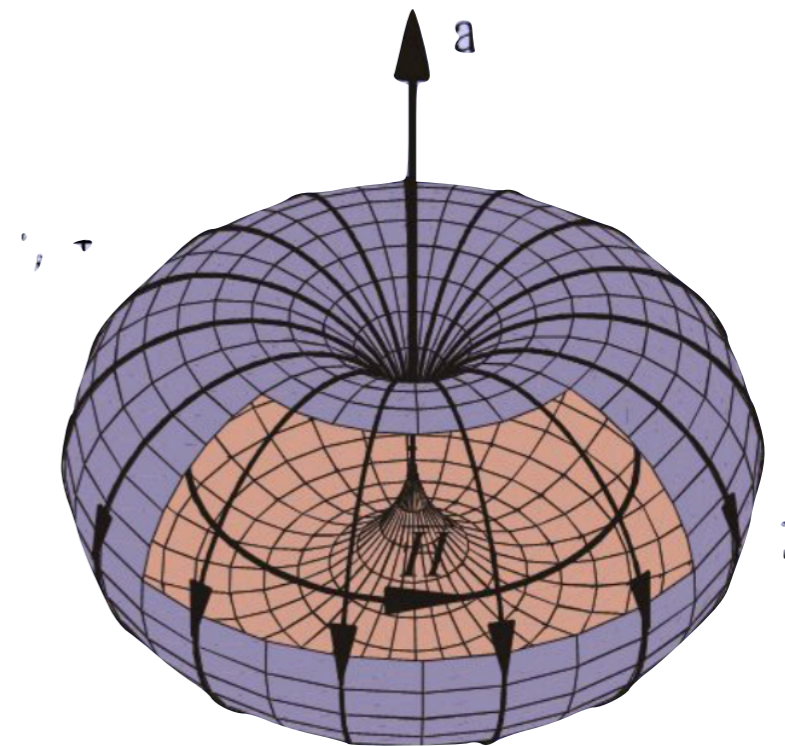
Even perfectly neutral particles can couple to photons

$$H_{AM} = -a_\chi(\vec{J} \cdot \vec{\sigma}_\chi)$$

anapole moment (P odd but CP even)

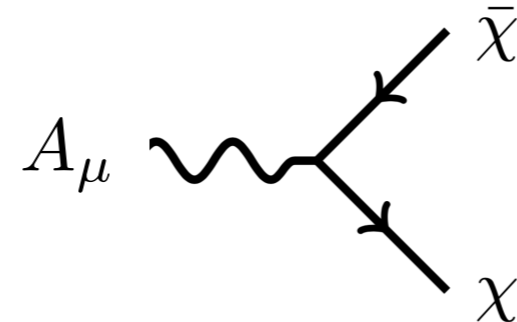
$$H_{CR} = -b_\chi(\vec{\nabla} \cdot \vec{E})$$

charge radius (P and T even)



1. Dark states with EM form factors

Photon-portal



Effective operators

millicharge (ϵQ):

$$\epsilon e \bar{\chi} \gamma^\mu \chi A_\mu, \quad \text{dim 4}$$

magnetic dipole (MDM):

$$\frac{1}{2} \mu_\chi \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu}, \quad \dots\dots\dots$$

electric dipole (EDM):

$$\frac{i}{2} d_\chi \bar{\chi} \sigma^{\mu\nu} \gamma^5 \chi F_{\mu\nu}, \quad \text{dim 5}$$

anapole moment (AM):

$$a_\chi \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu}, \quad \dots\dots\dots$$

charge radius (CR):

$$b_\chi \bar{\chi} \gamma^\mu \chi \partial^\nu F_{\mu\nu}. \quad \text{dim 6}$$

Vertex

$$\Gamma^\mu(q) = i\sigma^{\mu\nu} q_\nu [M(q^2) + iD(q^2)\gamma^5] + (q^2\gamma^\mu - q^\mu \not{q}) [V(q^2) - A(q^2)\gamma^5]$$

$$\mu_\chi = M(0), \quad d_\chi = D(0), \quad a_\chi = A(0), \quad b_\chi = V(0)$$

1. Dark states with EM form factors

Photon-portal

Rayleigh/Susceptibility ops

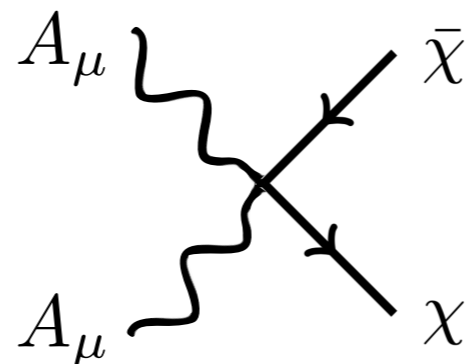
$$\bar{\chi}\chi$$

\otimes

$$F_{\mu\nu}F^{\mu\nu}$$

$$\bar{\chi}\gamma^5\chi$$

$$F_{\mu\nu}\tilde{F}^{\mu\nu}$$



.....

dim 7

.....

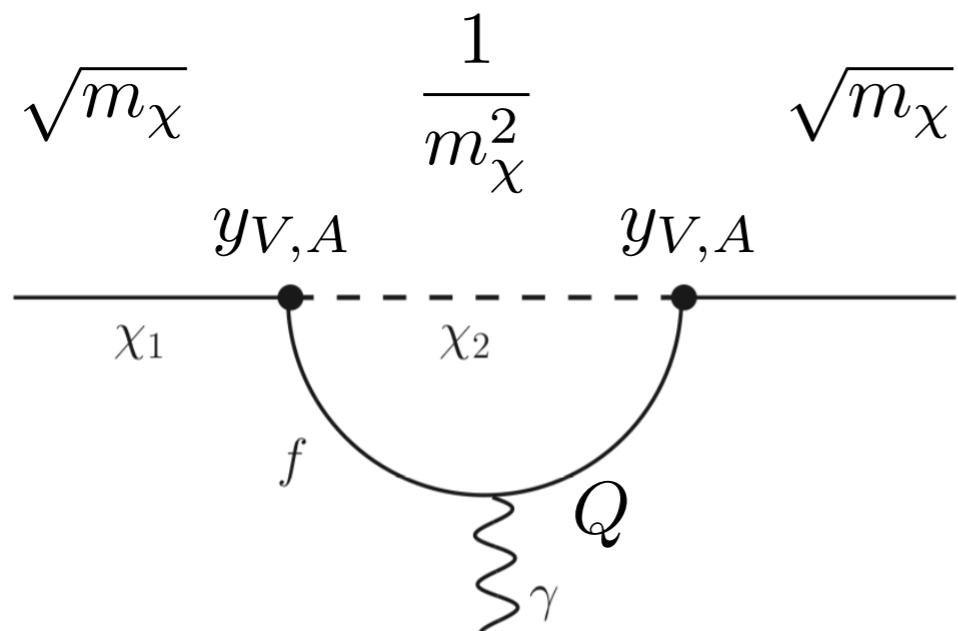
=> different (or loop-suppressed) phenomenology

Complex scalars: dim-6 Rayleigh and charge radius interaction

Vectors: also quadrupole moments exist

1. Dark states with EM form factors

Photon-portal



$$\mu_\chi \sim \frac{Q|y_{A,V}|^2}{m_\chi} \quad d_\chi \sim \frac{Q \operatorname{Im}[y_{V,A} y_A^*]}{m_\chi}$$

$$a_\chi, b_\chi \sim \frac{Q|y_{A,V}|^2}{M^2}$$

or

$$a_\chi, b_\chi \sim \frac{Q|y_{A,V}|^2}{m_\chi} \times \frac{1}{\Delta m}$$

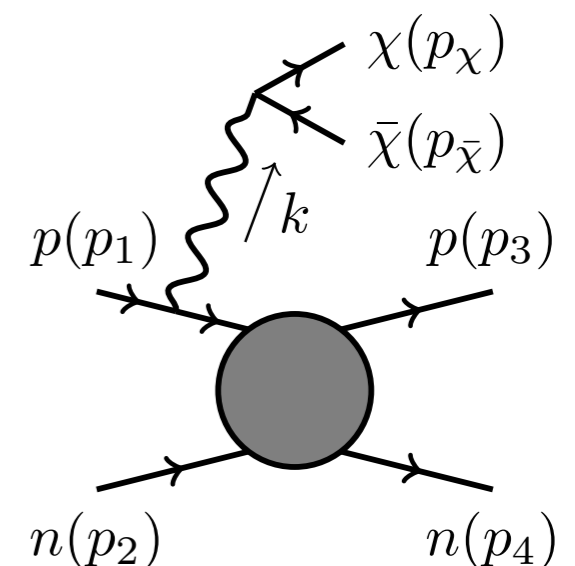
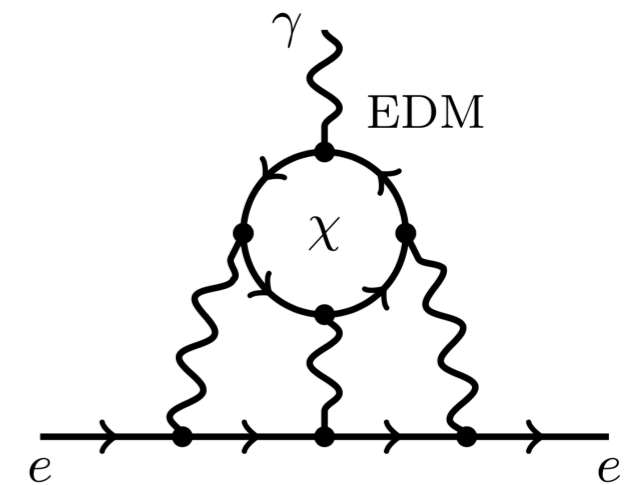
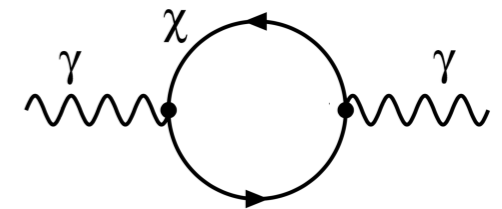
e.g. Bagnasco, Dine, Thomas 1994; Foadi, Frandsen, Sannino 2009;
Antipin, Redi, Strumia, and Vigiani 2015; Kavanagh, Panci, Ziegler 2018

1. Dark states with EM form factors

Photon-portal

Tinkering with the photon may affect many known phenomena

- changes the strength of the EM interaction at various energy scales
- affects SM precision observables, e.g. $g-2$
- provides new photon-mediated decay channels of particles
- can we produce those “dark states” in the laboratory?
- can we have a “theory of dark matter” through the photon coupling?
- implications for astrophysics? is it cosmologically viable?



Muon g-2

- Muon g-2 puzzle: (3-4) σ tension between SM prediction and measurement

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (290 \pm 90) \times 10^{-11}$$

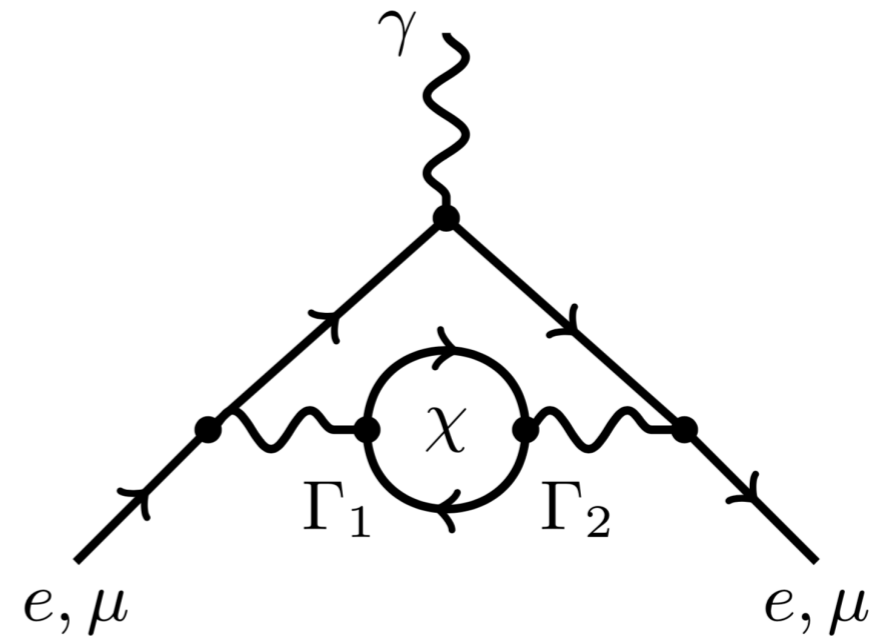
- For form-factor interactions, contributions enter through the vacuum polarization

e.g. use dispersion relation + unitarity

$$\Delta a_\mu = \frac{1}{4\pi^3} \int_{4m_\chi^2} ds \sigma_{e^+e^- \rightarrow \chi\bar{\chi}}(s) K(s)$$

solution to g-2 for

$$|\mu_\chi|, |d_\chi| \sim \text{few} \times 10^{-3} \mu_B$$

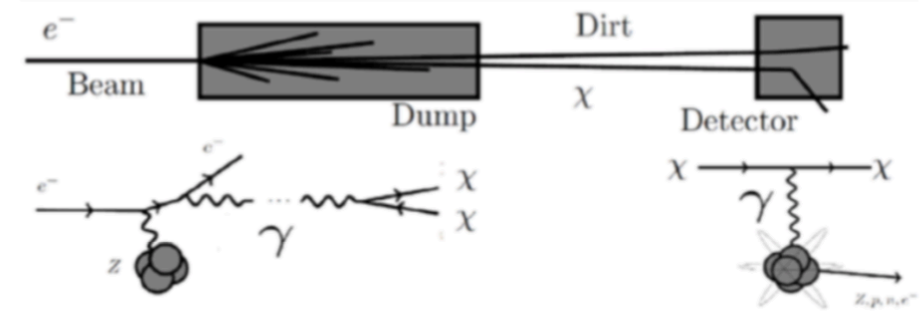
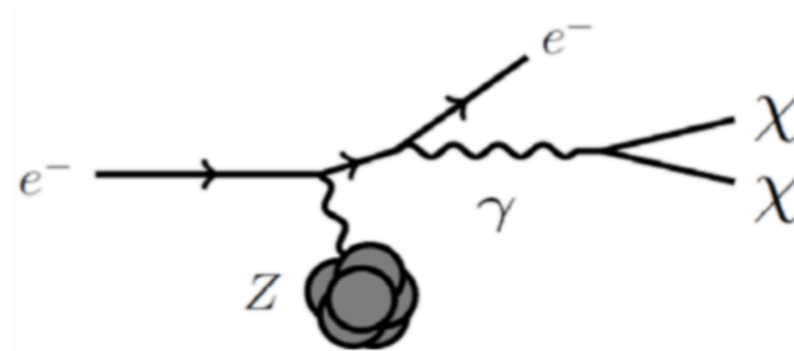
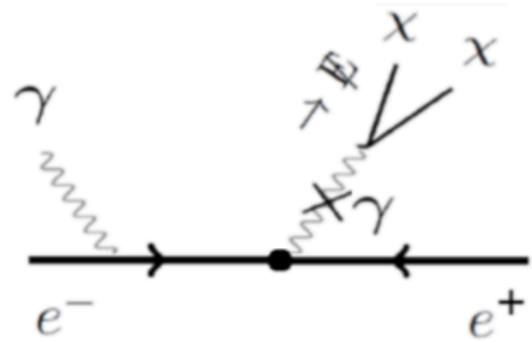


sub-GeV states: a target for intensity frontier

missing momentum

missing energy

direct search



BaBar:

- CM energy: 10 GeV
- Luminosity: 28/19 fb⁻¹

Belle II (projected):

- Luminosity: 50 ab⁻¹

Main Backgrounds:

- $e^+e^- \rightarrow \gamma\gamma$
- $e^+e^- \rightarrow \gamma\gamma\gamma$
- $e^+e^- \rightarrow \gamma e^+e^-$

NA64:

- Beam energy: 100 GeV
- Lead Target
- EOT: 10¹⁰

LDMX (projected):

- Beam energy: 4/8 GeV
- Tungsten/Aluminum Target
- EOT: 10¹⁴ / 10¹⁵

Almost no Backgrounds:

- Active veto system
- Cuts on search region

mQ:

- Beam energy: 30 GeV
- Tungsten Target
- EOT: 10¹⁹

BDX (projected):

- Beam energy: 11 GeV
- Aluminum Target
- EOT: 10²²

Main Backgrounds:

- High energy neutrinos

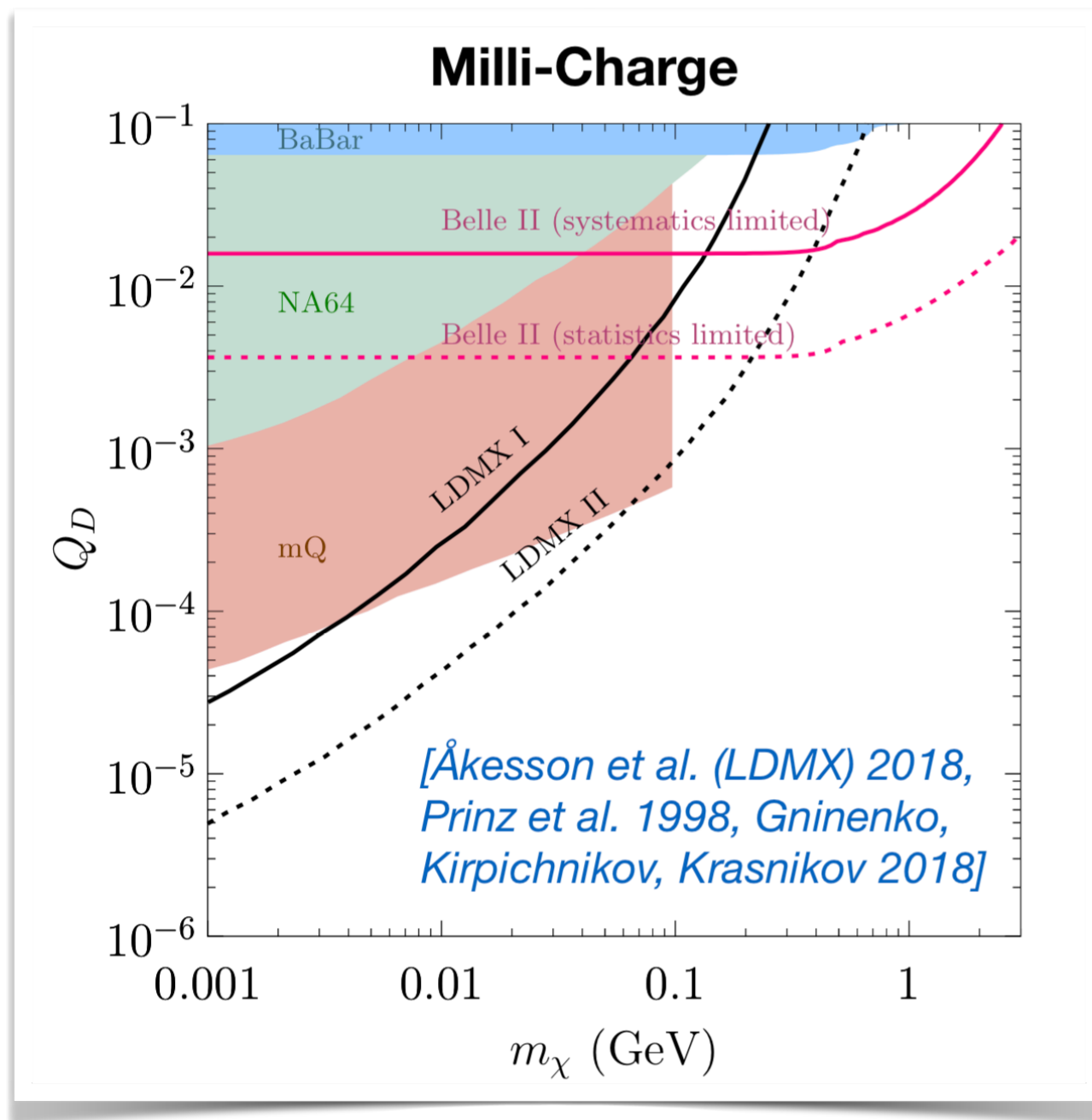
Dark states with EM form factors

Photon-portal

MeV-GeV mass bracket

Chu, JP, Semmelrock 2019

Chu, Kuo, JP 2020



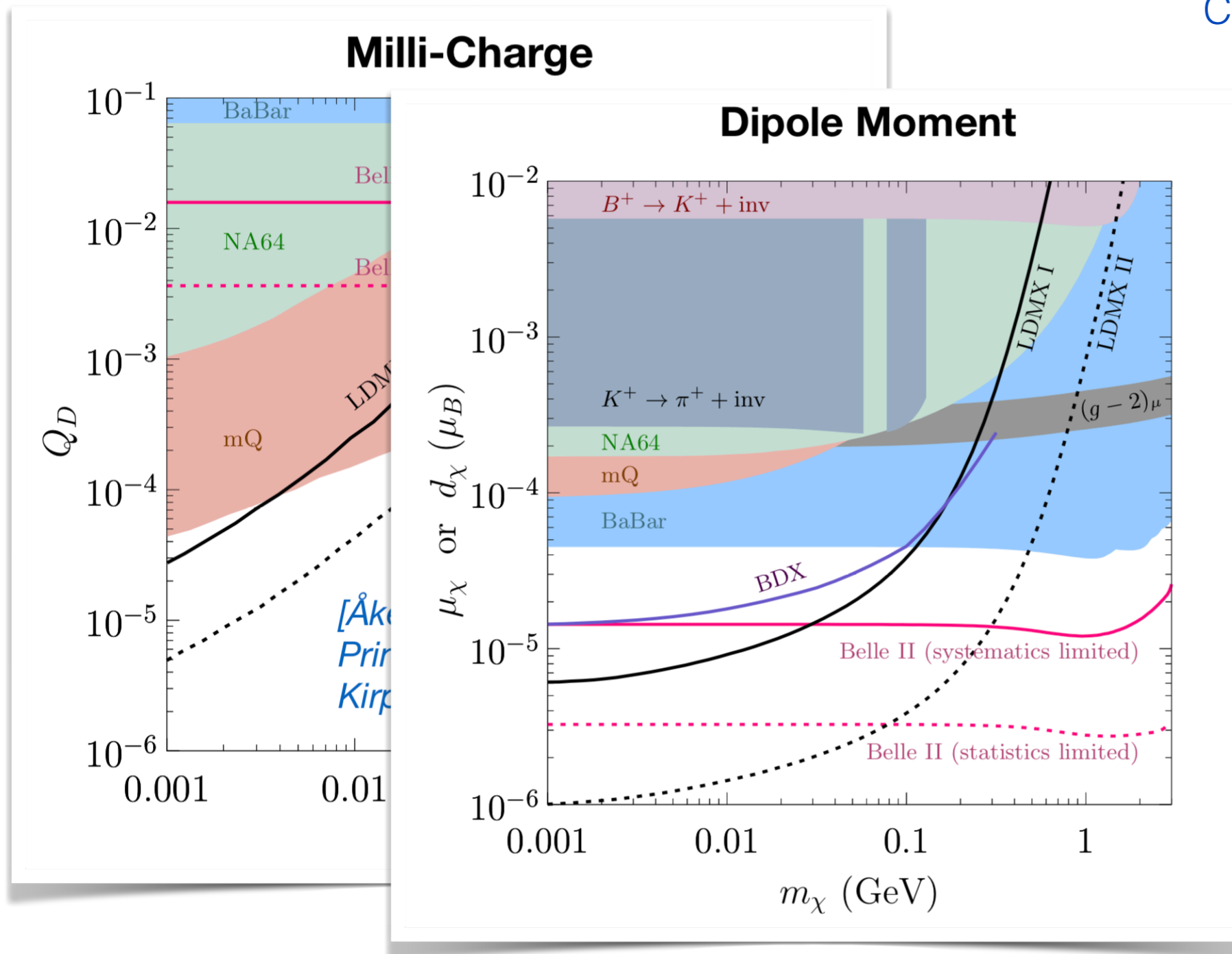
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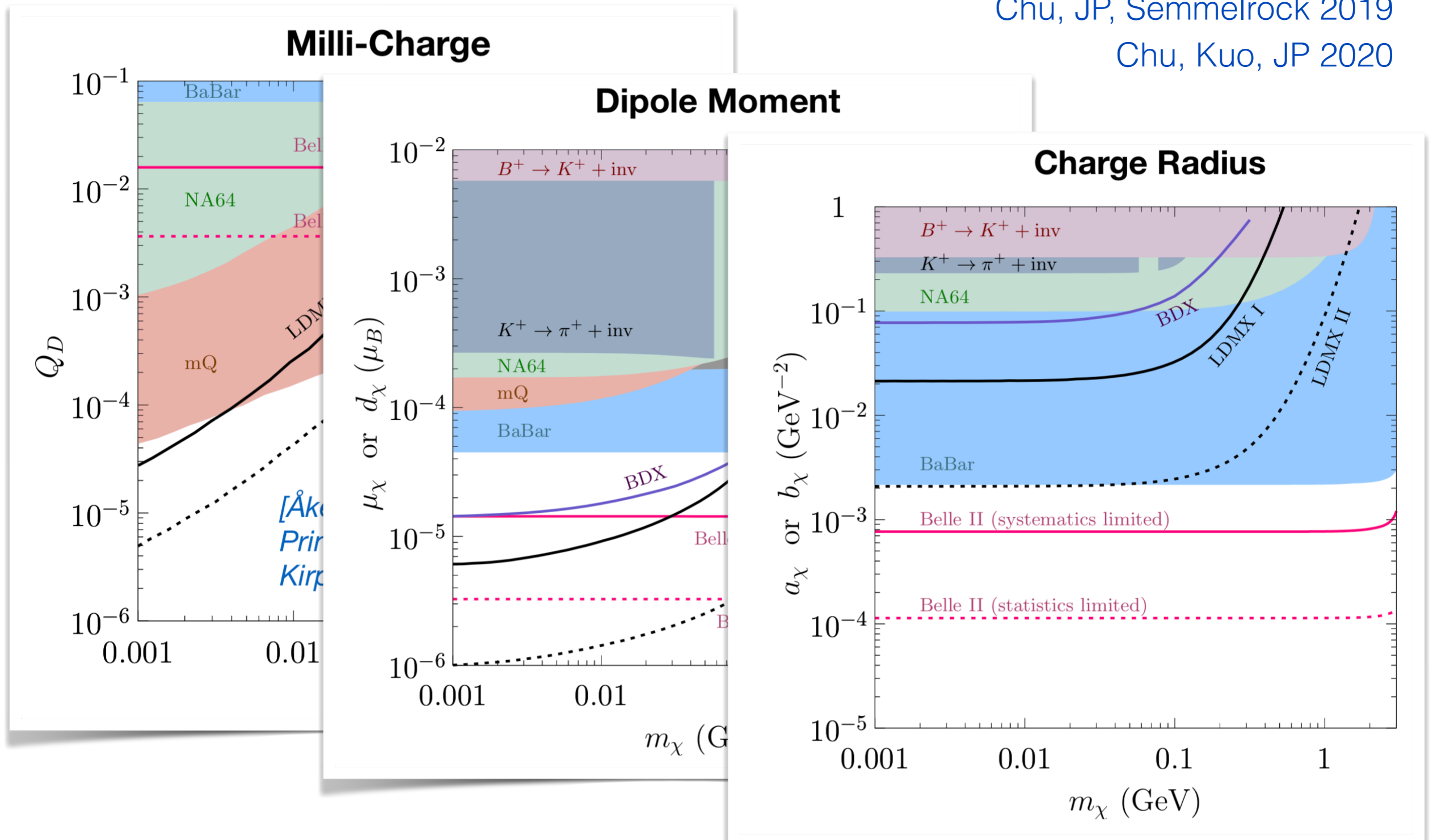
Dark states with EM form factors

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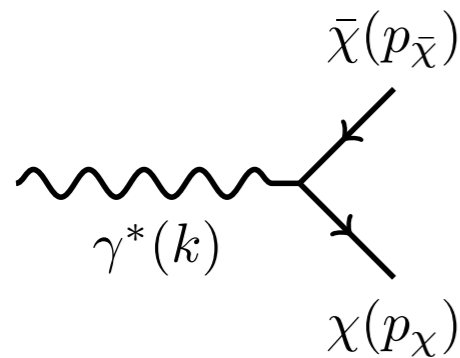
Chu, JP, Semmelrock 2019

Chu, Kuo, JP 2020



Stars as laboratories

Anomalous energy loss



$$\omega_p \sim \begin{cases} 0.3 \text{ keV} & \text{Sun's core} \\ 2.6 \text{ keV} & \text{HB's core} \\ 8.6 \text{ keV} & \text{RG's core} \\ 17.6 \text{ MeV} & \text{SN's core} \end{cases}$$

$\langle E_{\text{kin}} + E_{\text{grav}} \rangle$ becomes smaller from stellar energy loss

1. Stars supported by radiation pressure (active stars):

Virial theorem: $\langle E_{\text{kin}} \rangle = -\frac{1}{2} \langle E_{\text{grav}} \rangle$

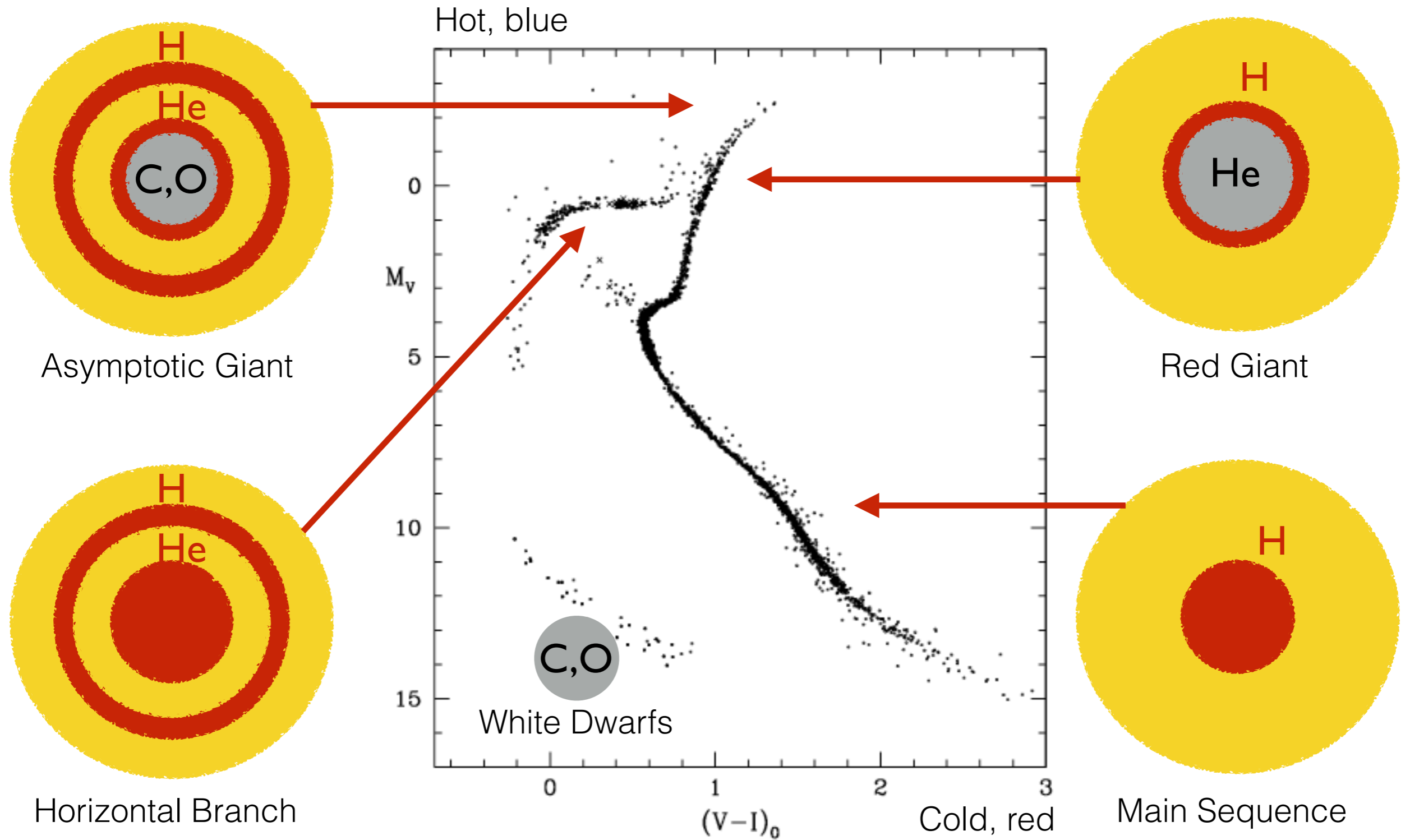
=> Gravitational potential energy becomes more negative (tighter bound)

=> average kinetic energy increases, **star becomes hotter**

2. Stars supported by degeneracy pressure (white dwarfs, neutron stars):

=> star cools by the energy loss

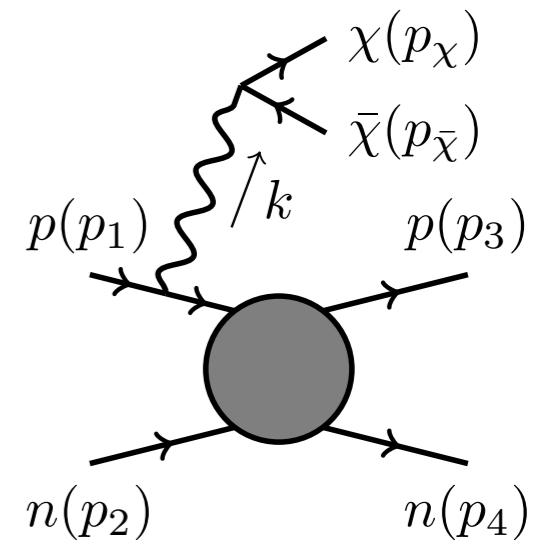
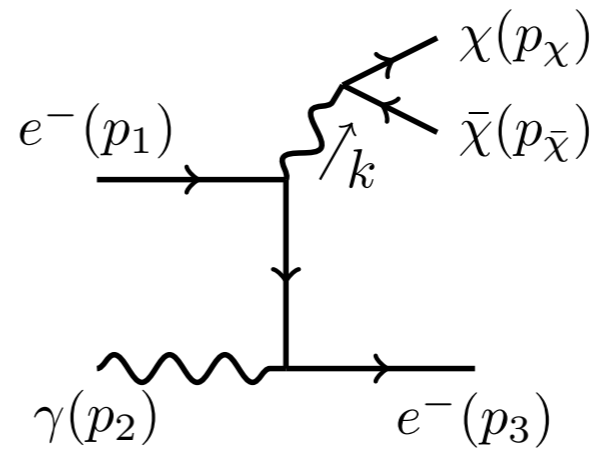
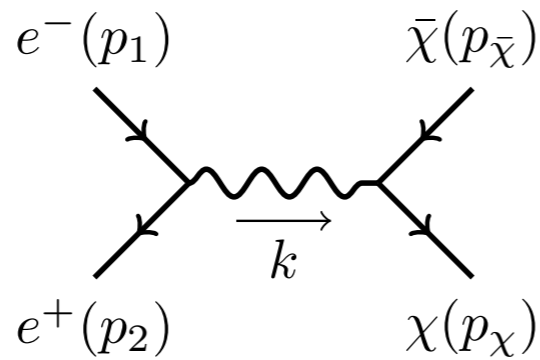
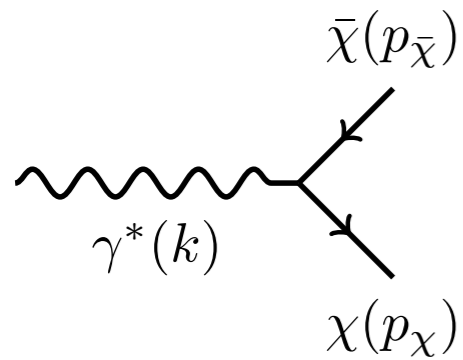
Stars as laboratories



Globular Cluster color-magnitude diagram

Energy loss in dark states

Stellar probes of dark sector - photon interactions



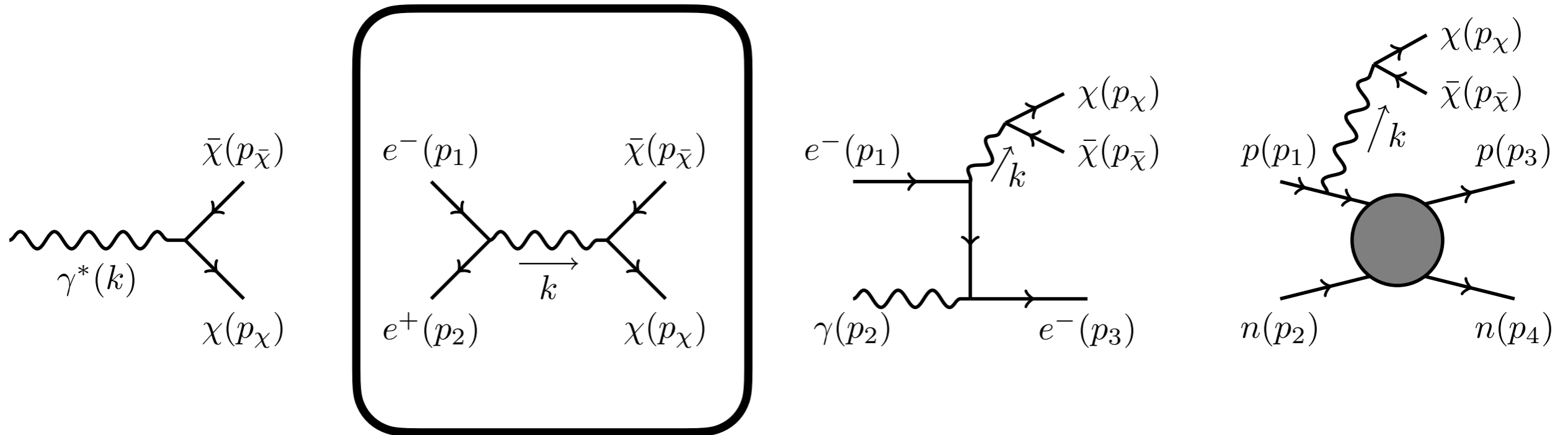
T/L “Plasmon” decay

(all)

$$\omega_p \sim \begin{cases} 0.3 \text{ keV} & \text{Sun's core} \\ 2.6 \text{ keV} & \text{HB's core} \\ 8.6 \text{ keV} & \text{RG's core} \\ 17.6 \text{ MeV} & \text{SN's core} \end{cases}$$

Energy loss in dark states

Stellar probes of dark sector - photon interactions



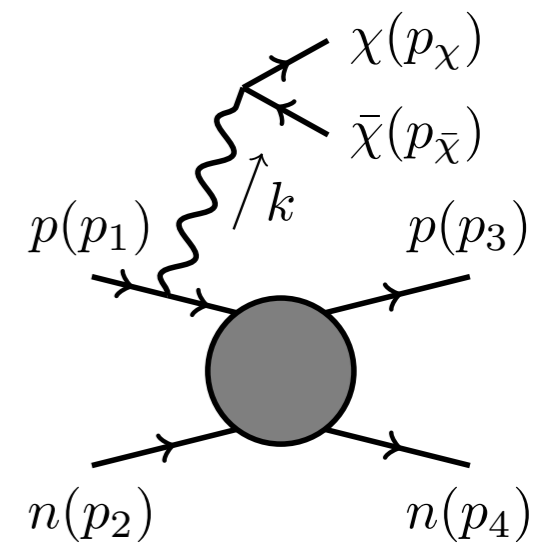
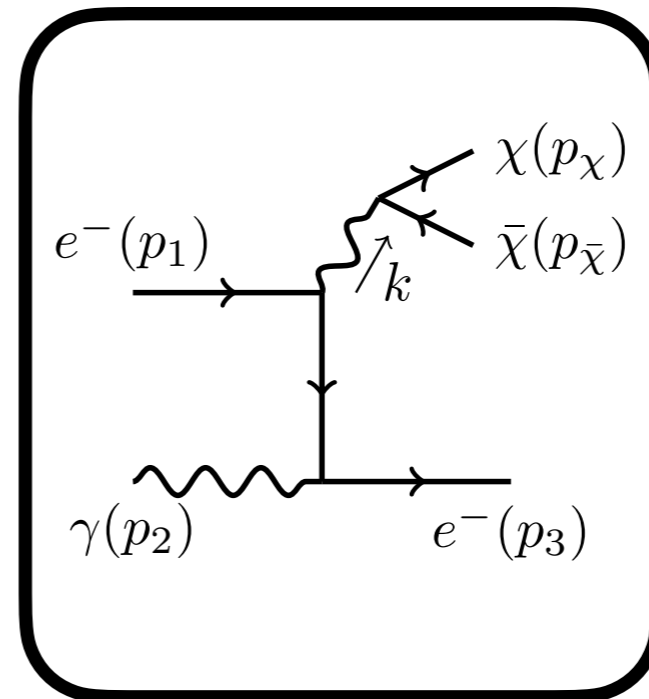
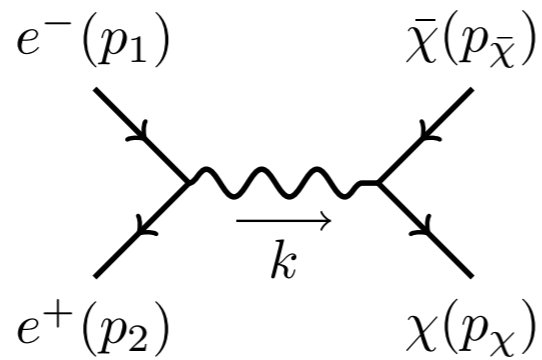
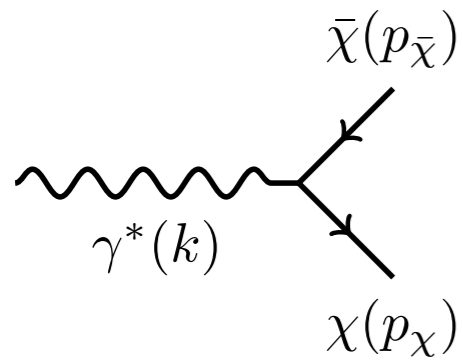
e^+e^- annihilation

(SN)

NB: no overlap with plasmon decay

Energy loss in dark states

Stellar probes of dark sector - photon interactions

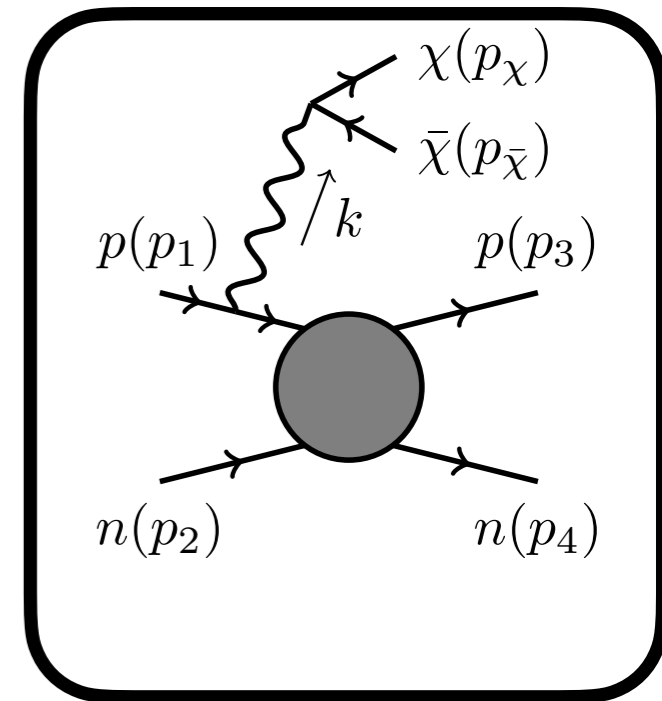
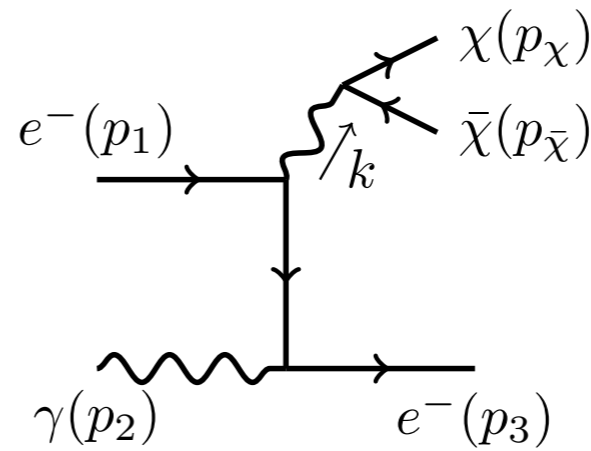
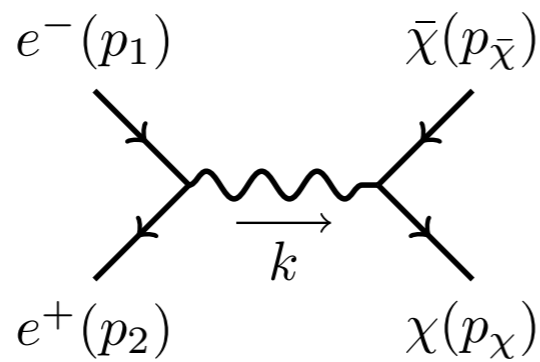
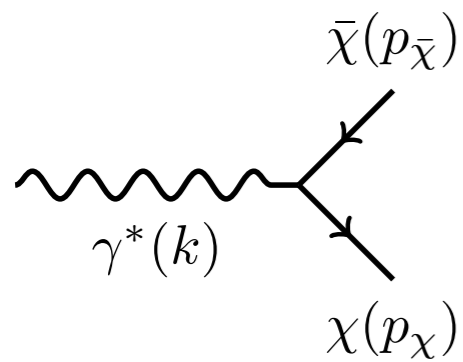


Compton 2- \rightarrow 3 production

(all)

Energy loss in dark states

Stellar probes of dark sector - photon interactions



Electron-nucleus Bremsstrahlung

(RG, HB, Sun)

Neutron-proton Bremsstrahlung

(SN)

NB: soft-photon approximation
not applicable

NB: we use exp. data for np-brems

Rrapaj, Reddy 2016

Energy loss in dark states

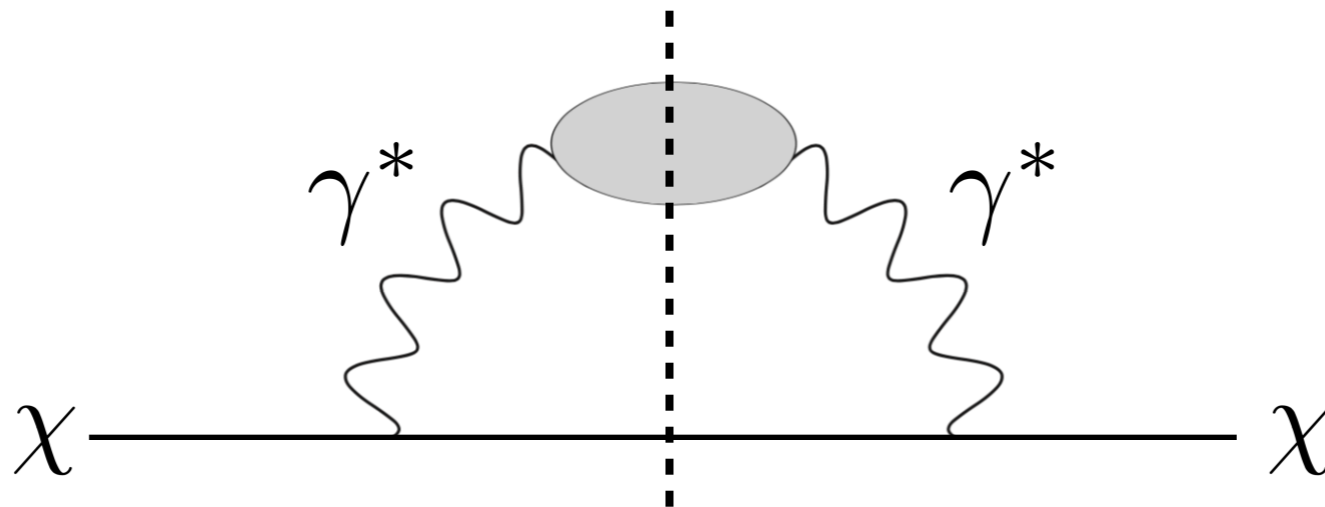
Unifying formula for pair emission

$$\dot{N}_\chi = - \int \frac{d^3 \vec{p}_\chi}{(2\pi)^3} \frac{1}{(e^{E_\chi/T} + 1)} \frac{\text{Im} \Pi_\chi(E_\chi, \vec{p}_\chi)}{E_\chi}$$

Finite-T optical theorem: rate with which a particle comes into thermal equilibrium is given by the discontinuity of the self energy

$$\text{Im} \Pi_\chi(E_\chi, \vec{p}_\chi) = \bar{u}(p_\chi) \Sigma(E_\chi, \vec{p}_\chi) u(p_\chi)$$

Weldon 1983



Energy loss in dark states

Unifying formula for pair emission

$$\frac{d\dot{N}_\chi}{ds_{\chi\bar{\chi}}} = - \sum_{i=T,L} g_i \int \frac{d^3\vec{k}}{(2\pi)^3} \frac{1}{(e^{\omega/T} - 1)} \frac{\text{Im } \Pi_i(\omega, \vec{k})}{\omega} \times \frac{f(s_{\chi\bar{\chi}})}{16\pi^2 |s_{\chi\bar{\chi}} - \Pi_i|^2} \sqrt{1 - \frac{4m_\chi^2}{s_{\chi\bar{\chi}}}}$$

In this version (derived from works on dilepton-production in hot matter) the imaginary part of the *photon self-energy* enters

$$\Pi^{\mu\rho} = (\epsilon_{T,1}^\mu \epsilon_{T,1}^\rho + \epsilon_{T,2}^\mu \epsilon_{T,2}^\rho) \Pi_T + \epsilon_L^\mu \epsilon_L^\rho \Pi_L$$

=> leading contribution from the pole $s_{\chi\bar{\chi}} = \text{Re } \Pi_{L,T}$
recover plasmon-decay rate

=> further contributions to chi-pair production found from identifying the contributions to the photon self-energy

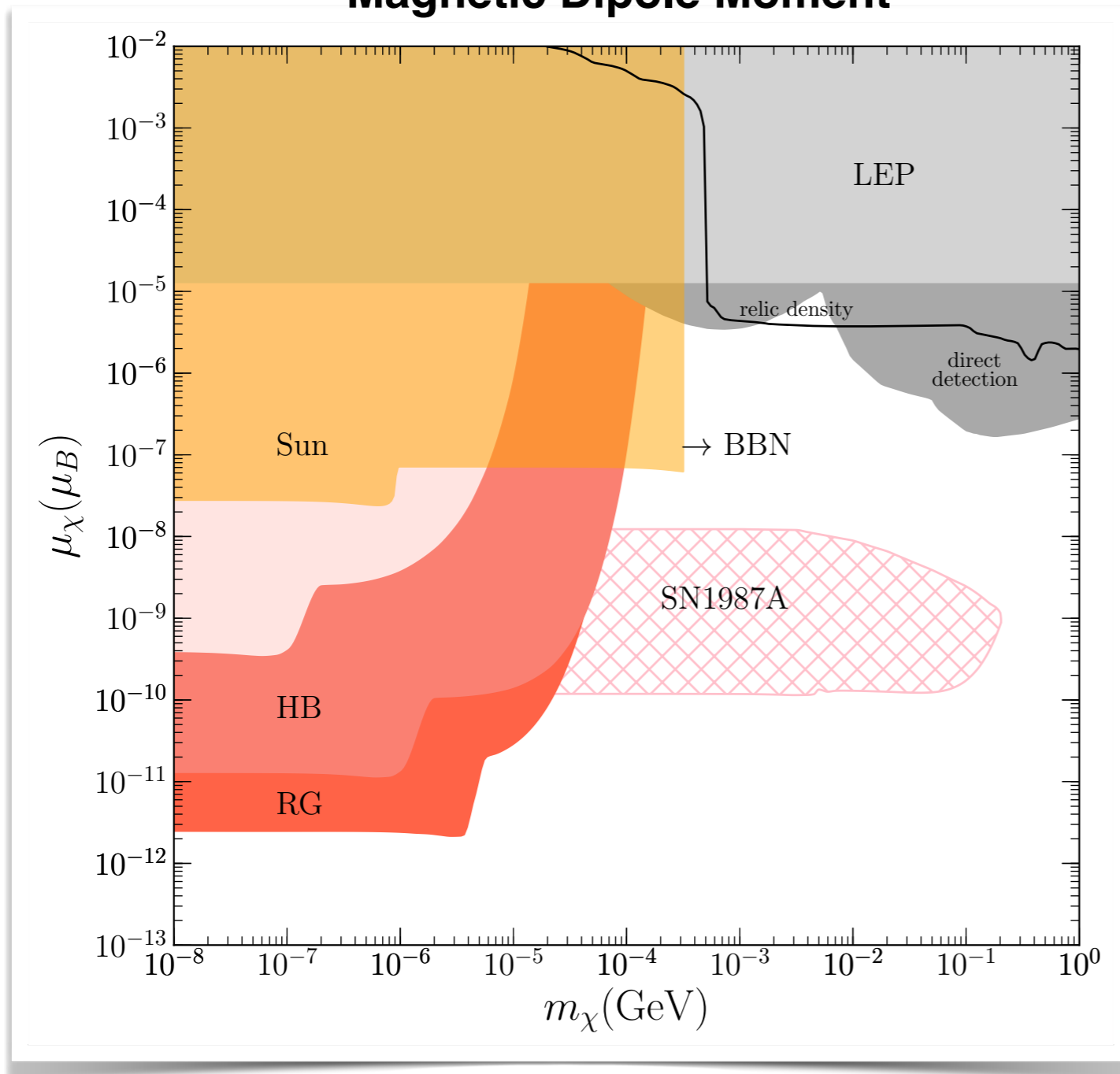
Application 1

Photon-portal

keV-MeV mass bracket

Chu, Kuo, JP, Semmelrock 2019

Magnetic Dipole Moment



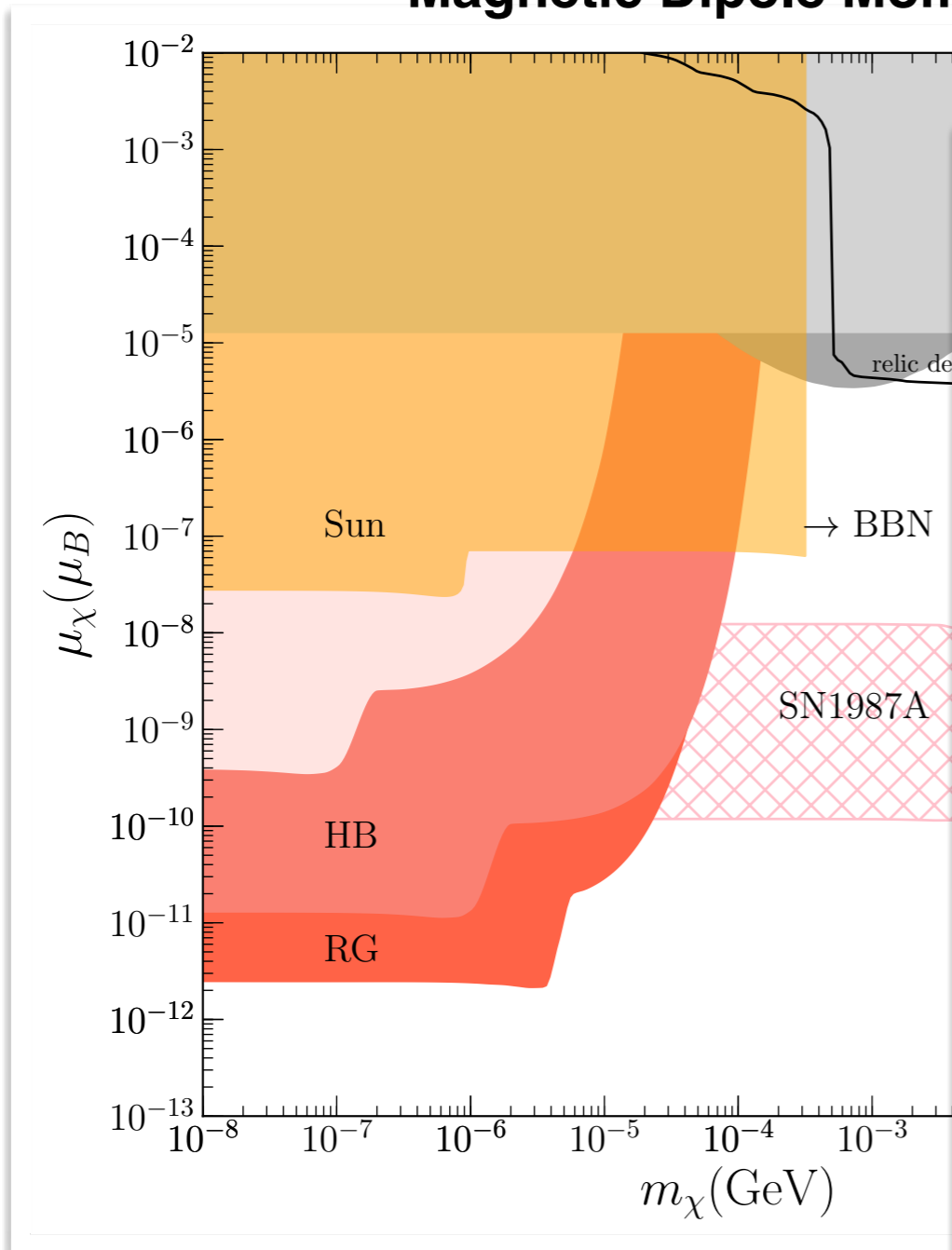
Application 1

keV-MeV mass bracket

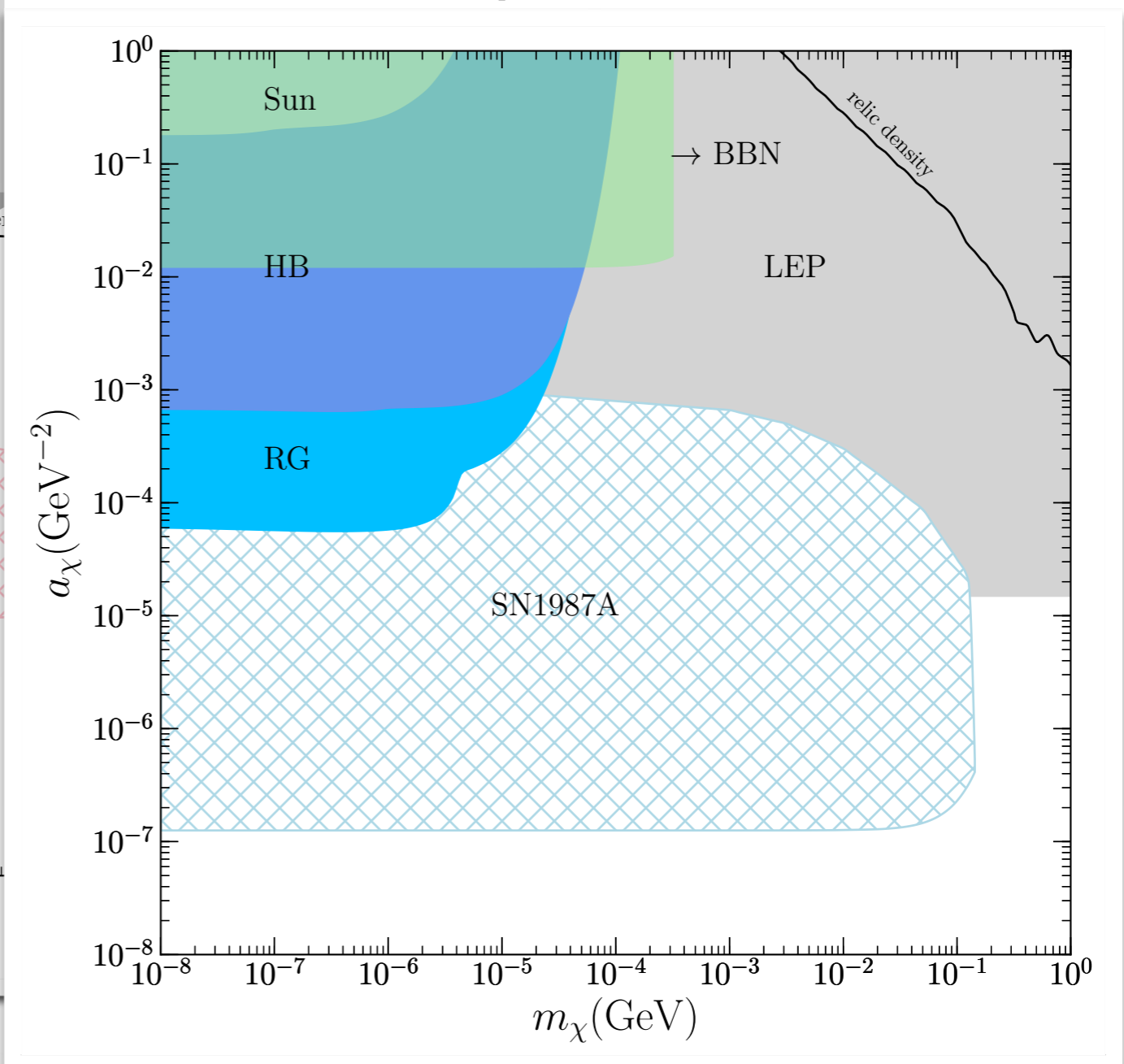
Photon-portal

Chu, Kuo, JP, Semmelrock 2019

Magnetic Dipole Moment

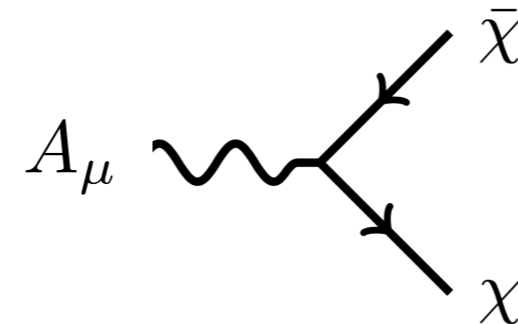


Anapole Moment



Dark states with EM form factors

SPIN 1/2 case is now familiar



Effective operators

millicharge (ϵQ):

$$\epsilon e \bar{\chi} \gamma^\mu \chi A_\mu,$$

dim 4

magnetic dipole (MDM):

$$\frac{1}{2} \mu_\chi \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu},$$

.....

electric dipole (EDM):

$$\frac{i}{2} d_\chi \bar{\chi} \sigma^{\mu\nu} \gamma^5 \chi F_{\mu\nu},$$

dim5

anapole moment (AM):

$$a_\chi \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu},$$

.....

charge radius (CR):

$$b_\chi \bar{\chi} \gamma^\mu \chi \partial^\nu F_{\mu\nu}.$$

dim6

=> SPIN 1 case has comparatively received much less attention

Vector Dark States

Chu, Ibarra, Hisano, Kuo, JP
2303.13643

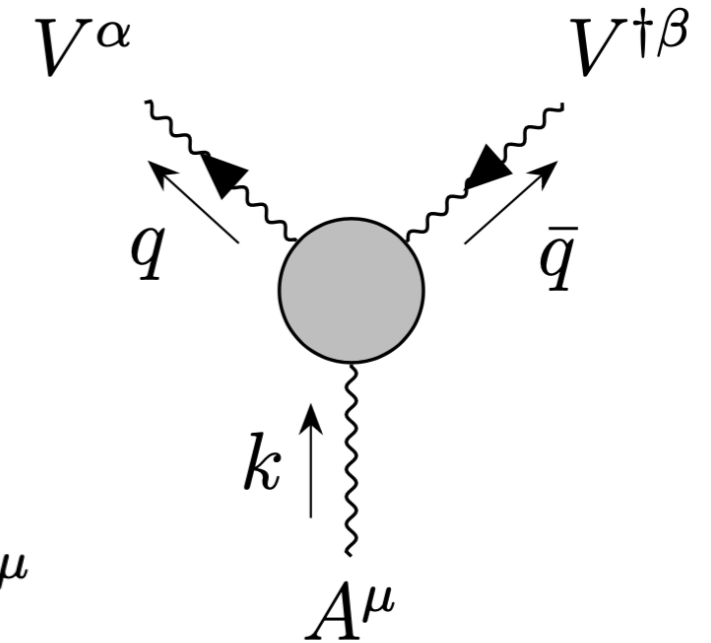
SPIN1 case: construction

Consider all possible Lorentz structures

=> yields 9 structures

$$i\Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu}(q, \bar{q}, k) =$$

$$\begin{aligned} \Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu} = & c_1(k^2) p^\mu g^{\alpha\beta} + c_2(k^2) k^\alpha g^{\beta\mu} + c_3(k^2) k^\beta g^{\alpha\mu} \\ & + c_4(k^2) k_\lambda \epsilon^{\mu\alpha\beta\lambda} + c_5(k^2) p_\lambda \epsilon^{\mu\alpha\beta\lambda} \\ & + c_6(k^2) k^\alpha k^\beta p^\mu \\ & + c_7(k^2) p^\mu [kp]^{\alpha\beta} + c_8(k^2) k^\alpha [kp]^{\beta\mu} + c_9(k^2) k^\beta [kp]^{\mu\alpha} \end{aligned}$$



$$p = q - \bar{q} \quad \partial_\mu V^\mu = 0$$

$$[kp]^{\mu\nu} = \epsilon^{\mu\nu\rho\sigma} k_\rho p_\sigma$$

Hagiwara, Peccei, Zeppenfeld 1987
Ibarra, Hisano, Ryo 2022

Vector Dark States

Chu, Ibarra, Hisano, Kuo, JP
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SPIN1 case: construction

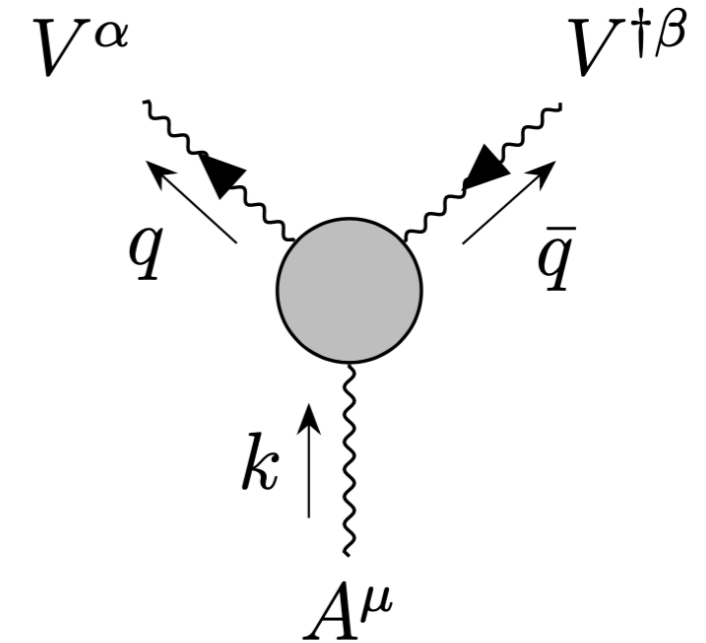
Consider all possible Lorentz structures

=> yields 9 structures

only seven out of the nine helicity states of the V pair can be reached by s-channel vector boson exchange (J = 1 channel)

=> 7 independent structures

$$i\Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu}(q, \bar{q}, k) =$$



$$\begin{aligned} \Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu}/e &= f_1^A(k^2)p^\mu g^{\alpha\beta} - \frac{f_2^A(k^2)}{m_V^2}p^\mu k^\alpha k^\beta + f_3^A(k^2)(k^\alpha g^{\mu\beta} - k^\beta g^{\mu\alpha}) \\ &+ if_4^A(k^2)(k^\alpha g^{\mu\beta} + k^\beta g^{\mu\alpha}) + if_5^A(k^2)\epsilon^{\mu\alpha\beta\rho}p_\rho \\ &- f_6^A(k^2)\epsilon^{\mu\alpha\beta\rho}k_\rho - \frac{f_7^A(k^2)}{m_V^2}p^\mu [kp]^{\alpha\beta}. \end{aligned}$$

Hagiwara, Peccei, Zeppenfeld 1987
Ibarra, Hisano, Ryo 2022

Vector Dark States

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SPIN1 case: construction

Consider all possible Lorentz structures

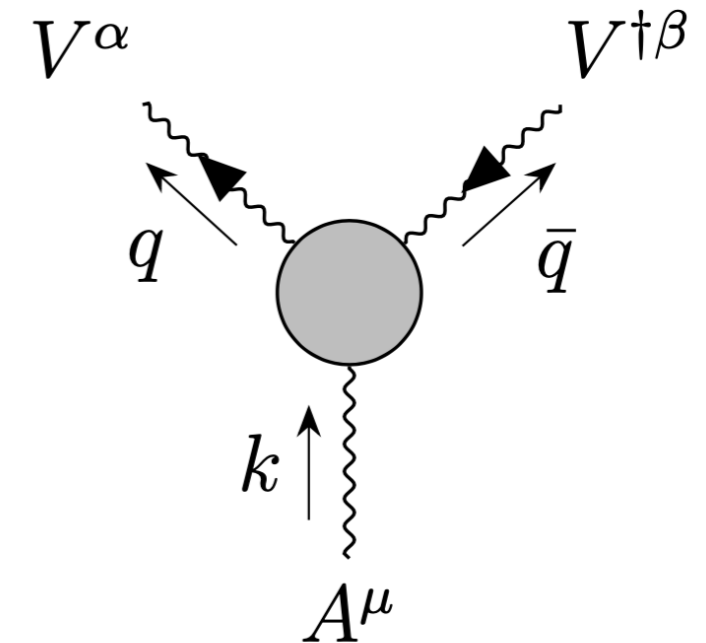
=> yields 9 structures

=> 7 independent structures

neutrality of V and gauge invariance of A require

=> $f_{1,4,5}^A(0) = 0$

$$i\Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu}(q, \bar{q}, k) =$$



$$f_1^A(k^2) = \cancel{f_1^A(0)} + \frac{k^2}{2\Lambda^2} [g_1^A(k^2) + \lambda_A(k^2)]$$

$$f_4^A(k^2) = \cancel{f_4^A(0)} + \frac{k^2}{\Lambda^2} g_4^A(k^2)$$

$$f_5^A(k^2) = \cancel{f_5^A(0)} + \frac{k^2}{\Lambda^2} g_5^A(k^2)$$

$$f_2^A(k^2) = \lambda_A(k^2)$$

$$f_3^A(k^2) = \kappa_A(k^2) + \lambda_A(k^2)$$

$$f_6^A(k^2) = \tilde{\kappa}_A(k^2) - \tilde{\lambda}_A(k^2)$$

$$f_7^A(k^2) = -\frac{1}{2} \tilde{\lambda}_A(k^2)$$

Hagiwara, Peccei, Zeppenfeld 1987
Ibarra, Hisano, Ryo 2022

Vector Dark States

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SPIN1 case: construction

Matched onto the following effective Lagrangian

$$\begin{aligned}\frac{\mathcal{L}}{e} = & \frac{ig_1^\Lambda}{2\Lambda^2} \left[(V_{\mu\nu}^\dagger V^\mu - V^{\dagger\mu} V_{\mu\nu}) \partial_\lambda F^{\lambda\nu} - V^{\dagger\mu} V^\nu \square F_{\mu\nu} \right] \\ & + \frac{g_4^\Lambda}{\Lambda^2} V_\mu^\dagger V_\nu (\partial^\mu \partial_\rho F^{\rho\nu} + \partial^\nu \partial_\rho F^{\rho\mu}) \\ & + \frac{g_5^\Lambda}{\Lambda^2} \epsilon^{\mu\nu\rho\sigma} \left(V_\mu^\dagger \overleftrightarrow{\partial}_\rho V_\nu \right) \partial^\lambda F_{\lambda\sigma} \\ & + i\kappa_\Lambda V_\mu^\dagger V_\nu F^{\mu\nu} + \frac{i\lambda_\Lambda}{\Lambda^2} V_{\lambda\mu}^\dagger V^\mu{}_\nu F^{\nu\lambda} \\ & + i\tilde{\kappa}_\Lambda V_\mu^\dagger V_\nu \tilde{F}^{\mu\nu} + \frac{i\tilde{\lambda}_\Lambda}{\Lambda^2} V_{\lambda\mu}^\dagger V^\mu{}_\nu \tilde{F}^{\nu\lambda},\end{aligned}$$

Vector Dark States

Chu, Ibarra, Hisano, Kuo, JP
2303.13643

SPIN1 case: construction

Matched onto the following effective Lagrangian

$$\begin{aligned} \frac{\mathcal{L}}{e} = & \frac{ig_1^\Lambda}{2\Lambda^2} [(V_\mu^\dagger V^\mu - \\ & + \frac{g_4^\Lambda}{\Lambda^2} V_\mu^\dagger V_\nu (\partial^\mu \partial_\rho F^{\rho\nu} \\ & + \frac{g_5^\Lambda}{\Lambda^2} \epsilon^{\mu\nu\rho\sigma} (V_\mu^\dagger \overleftrightarrow{\partial}_\rho V_\nu \\ & + i\kappa_\Lambda V_\mu^\dagger V_\nu F^{\mu\nu} + \\ & + i\tilde{\kappa}_\Lambda V_\mu^\dagger V_\nu \tilde{F}^{\mu\nu} + \end{aligned}$$

interaction type	coupling	C	P	CP
magn. dipole	$\mu_V = \frac{e}{2m_V} (\kappa_\Lambda + \frac{m_V^2}{\Lambda^2} \lambda_\Lambda)$	+1	+1	+1
elec. dipole	$d_V = \frac{e}{2m_V} (\tilde{\kappa}_\Lambda + \frac{m_V^2}{\Lambda^2} \tilde{\lambda}_\Lambda)$	+1	-1	-1
magn. quadrupole	$Q_V = -\frac{e}{m_V^2} (\kappa_\Lambda - \frac{m_V^2}{\Lambda^2} \lambda_\Lambda)$	+1	+1	+1
elec. quadrupole	$\tilde{Q}_V = -\frac{e}{m_V^2} (\tilde{\kappa}_\Lambda - \frac{m_V^2}{\Lambda^2} \tilde{\lambda}_\Lambda)$	+1	-1	-1
charge radius	$g_1^A / m_V^2 = g_1^\Lambda / \Lambda^2$	+1	+1	+1
toroidal moment	$g_4^A / m_V^2 = g_4^\Lambda / \Lambda^2$	-1	+1	-1
anapole moment	$g_5^A / m_V^2 = g_5^\Lambda / \Lambda^2$	-1	-1	+1

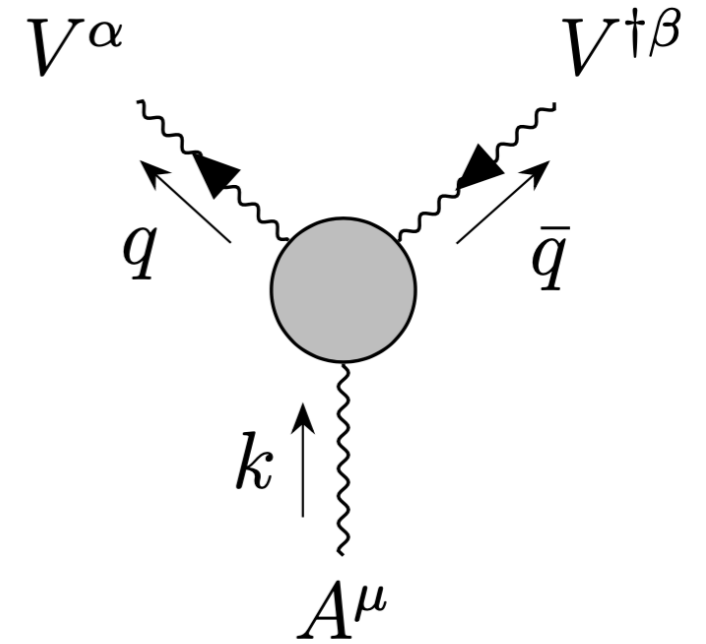
Vector Dark States

Vertex factor

Consider all possible Lorentz structures

$$i\Gamma_{VV^\dagger\gamma}^{\alpha\beta\mu}(q, \bar{q}, k) =$$

$$\begin{aligned} i\Gamma^{\mu\alpha\beta}(k, p) = & -\frac{ieg_1^A}{2m_V^2} k^2 p^\mu g^{\alpha\beta} \\ & -\frac{eg_4^A}{m_V^2} k^2 (k^\alpha g^{\mu\beta} + k^\beta g^{\mu\alpha}) - \frac{eg_5^A}{m_V^2} k^2 \epsilon^{\mu\alpha\beta\rho} p_\rho \\ & - 2im_V \mu_V \left[k^\alpha g^{\mu\beta} - k^\beta g^{\mu\alpha} + \frac{1}{4m_V^2} (k^2 g^{\alpha\beta} p^\mu - 2k^\alpha k^\beta p^\mu) \right] \\ & - \frac{iQ_V}{4} (k^2 g^{\alpha\beta} p^\mu - 2k^\alpha k^\beta p^\mu) \\ & - \frac{id_V}{2m_V} p^\mu [kp]^{\alpha\beta} - \frac{i\tilde{Q}_V}{4} \left(p^\mu [kp]^{\alpha\beta} + 4m_V^2 \epsilon^{\mu\alpha\beta\rho} k_\rho \right), \end{aligned}$$



=> interactions grouped by their CP properties and familiar nomenclature; defined such that m_V is the only explicit scale

Vector Dark States

Chu, Ibarra, Hisano, Kuo, JP
2303.13643

Universal description of V-pair production

Spin-summed matrix element of VV production

$$\sum_{\lambda, \lambda'} |\mathcal{M}^{\lambda\lambda'}|^2 = D_{\mu\nu}(k) D_{\rho\sigma}^*(k) \mathcal{T}_{\text{SM}}^{\mu\rho} \mathcal{T}_{\text{DM}}^{\nu\sigma}$$

any SM-current producing $\gamma^*(k)$
(can receive medium corrections)

interaction type	$f(s)$
magnetic dipole	$\frac{\mu_V^2 s(s - 4m_V^2)(16m_V^2 + 3s)}{12m_V^2}$
electric dipole	$\frac{d_V^2 s(s - 4m_V^2)^2}{6m_V^2}$
magnetic quadrupole	$\frac{Q_V^2 s^2(s - 4m_V^2)}{16}$
electric quadrupole	$\frac{\tilde{Q}_V^2 s^2(s + 8m_V^2)}{24}$
charge radius	$\frac{e^2 (g_1^A)^2 s^2 (s - 4m_V^2)(12m_V^4 - 4m_V^2 s + s^2)}{48m_V^8}$
toroidal moment	$\frac{e^2 (g_4^A)^2 s^3 (s - 4m_V^2)}{3m_V^6}$
anapole moment	$\frac{e^2 (g_5^A)^2 s^2 (s - 4m_V^2)^2}{3m_V^6}$

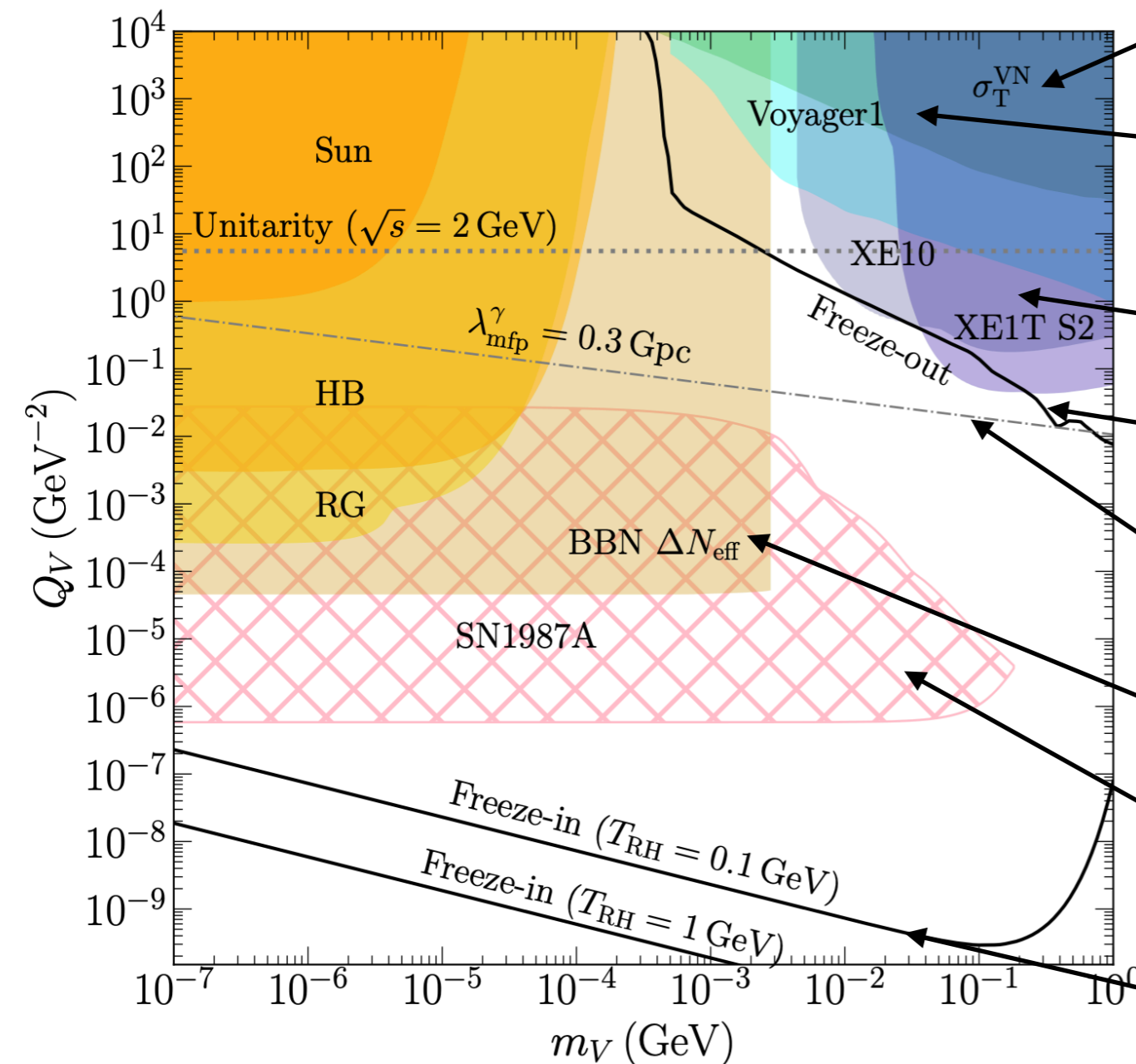
$$\int d\Phi_2 \mathcal{T}_{\text{DM}}^{\nu\sigma} = \frac{1}{8\pi} \sqrt{1 - \frac{4m_V^2}{s}} f(s) \left(-g^{\nu\sigma} + \frac{k^\nu k^\sigma}{s} \right)$$

$f(s)$ with mass-dimension 2 summarizes
all effective interactions when VV phase
space can be integrated

Vector DM

Mass vs. coupling plane

electric quadrupole



modification of matter power spectrum

indirect detection limit by annihilation
(weak because of velocity suppression)

direct detection DM-e scattering

annihilation into e^+e^- and $\gamma\gamma$
(typically p- or d-wave)

transparency to TeV photons

BBN limit on N_{eff} from minimal T_R

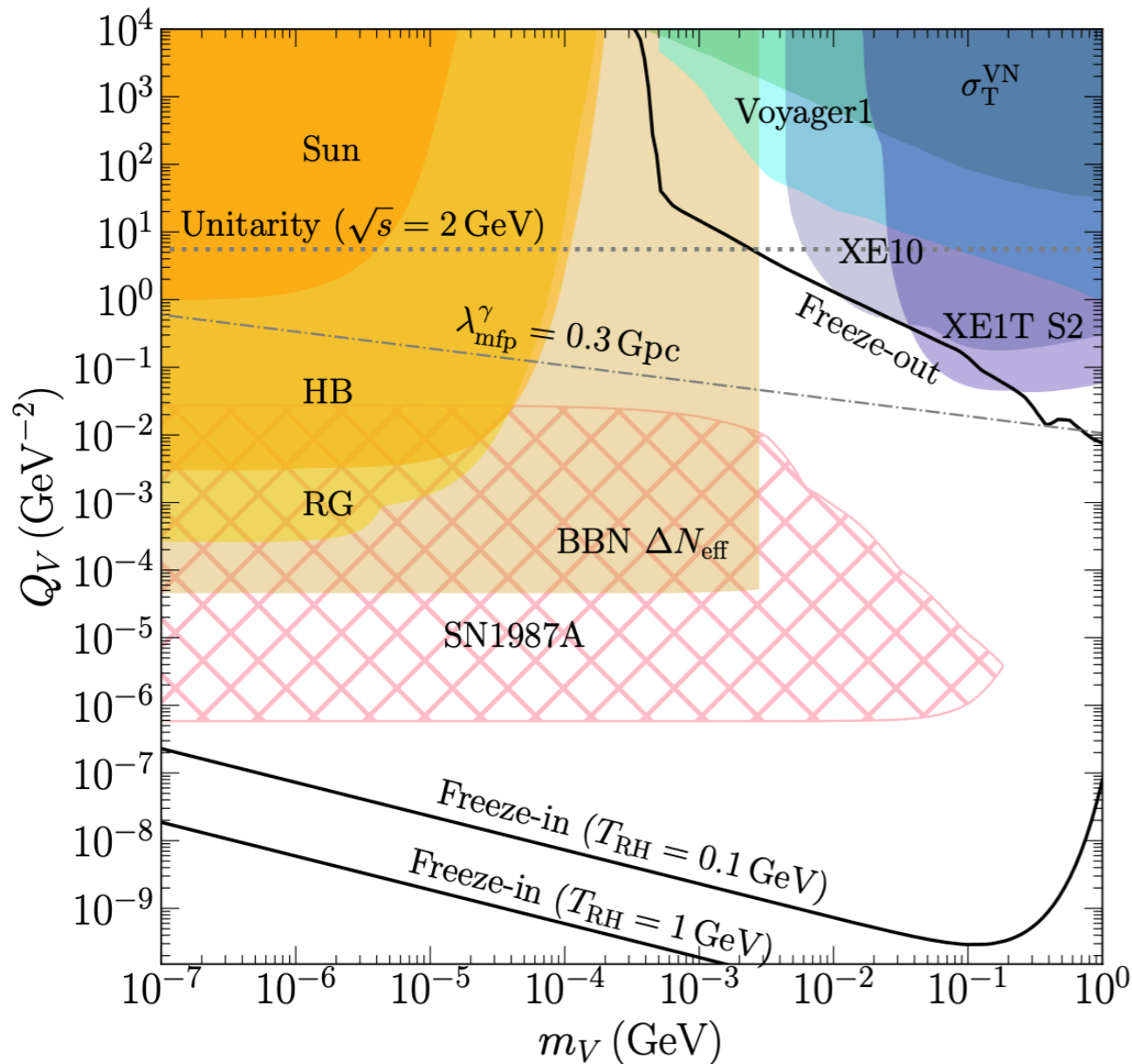
SN-limit bounded from above by trapping

UV-dominated freeze-in

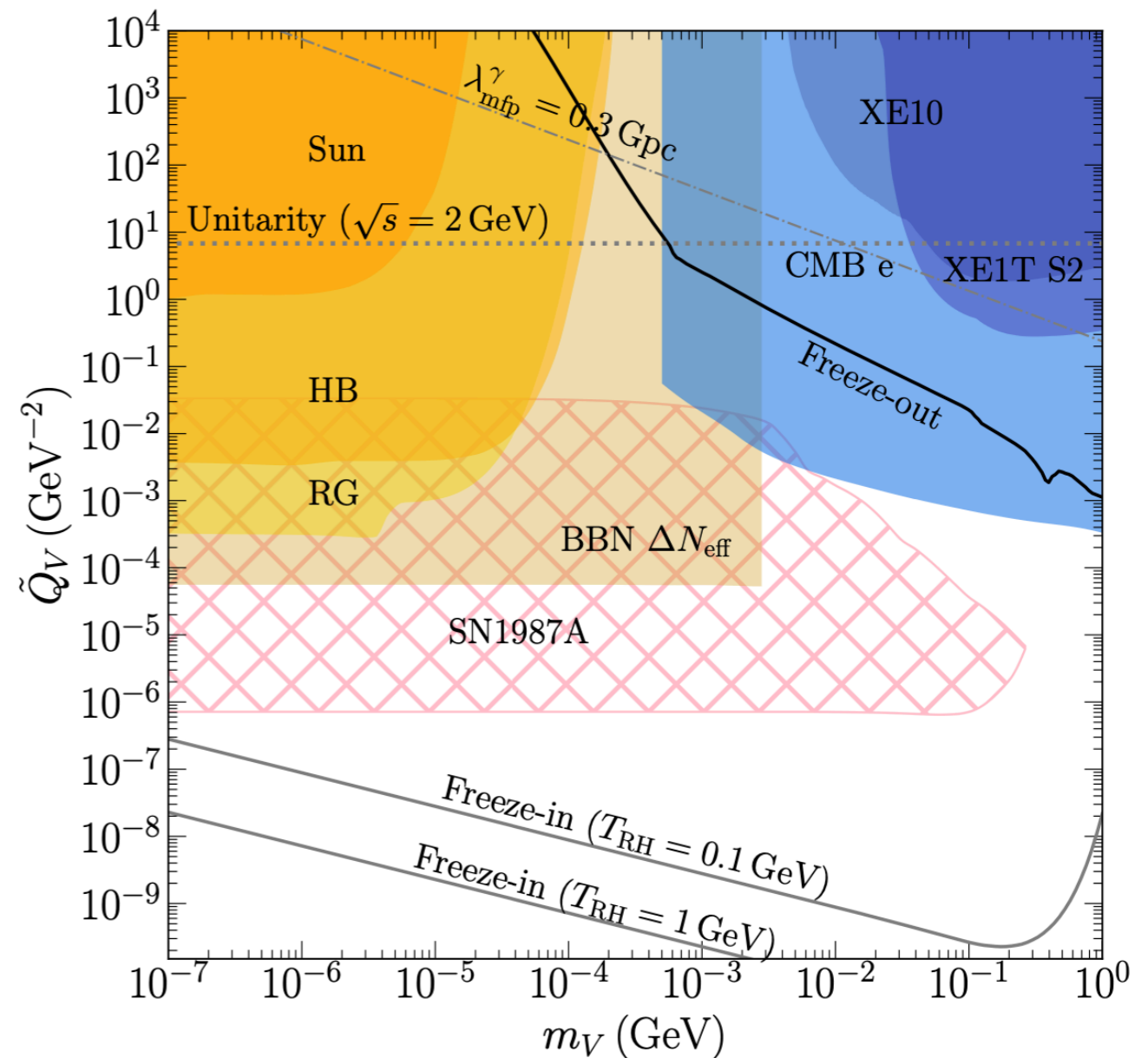
Vector DM

Mass vs. coupling plane

electric quadrupole



magnetic quadrupole



Vector DM

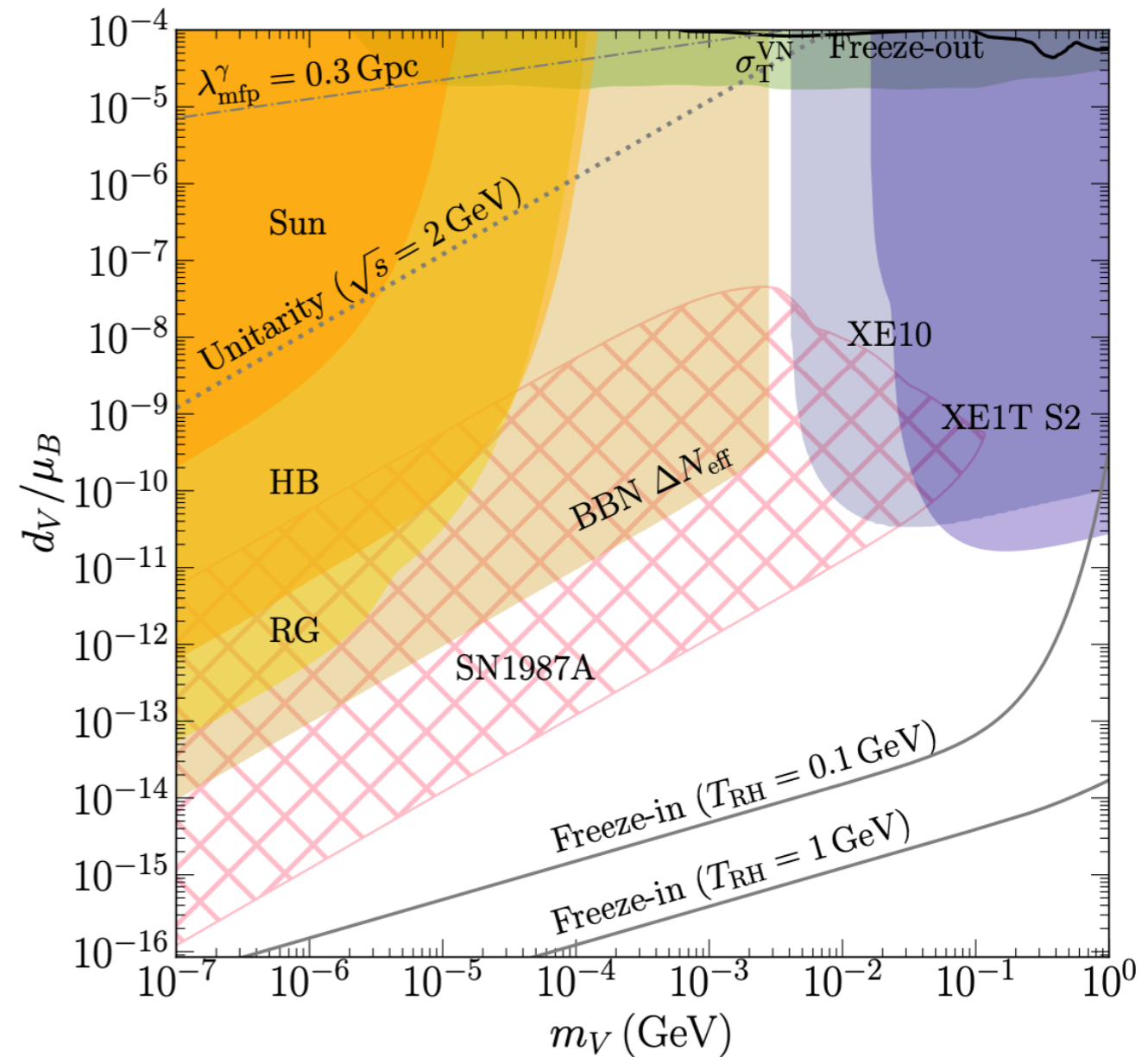
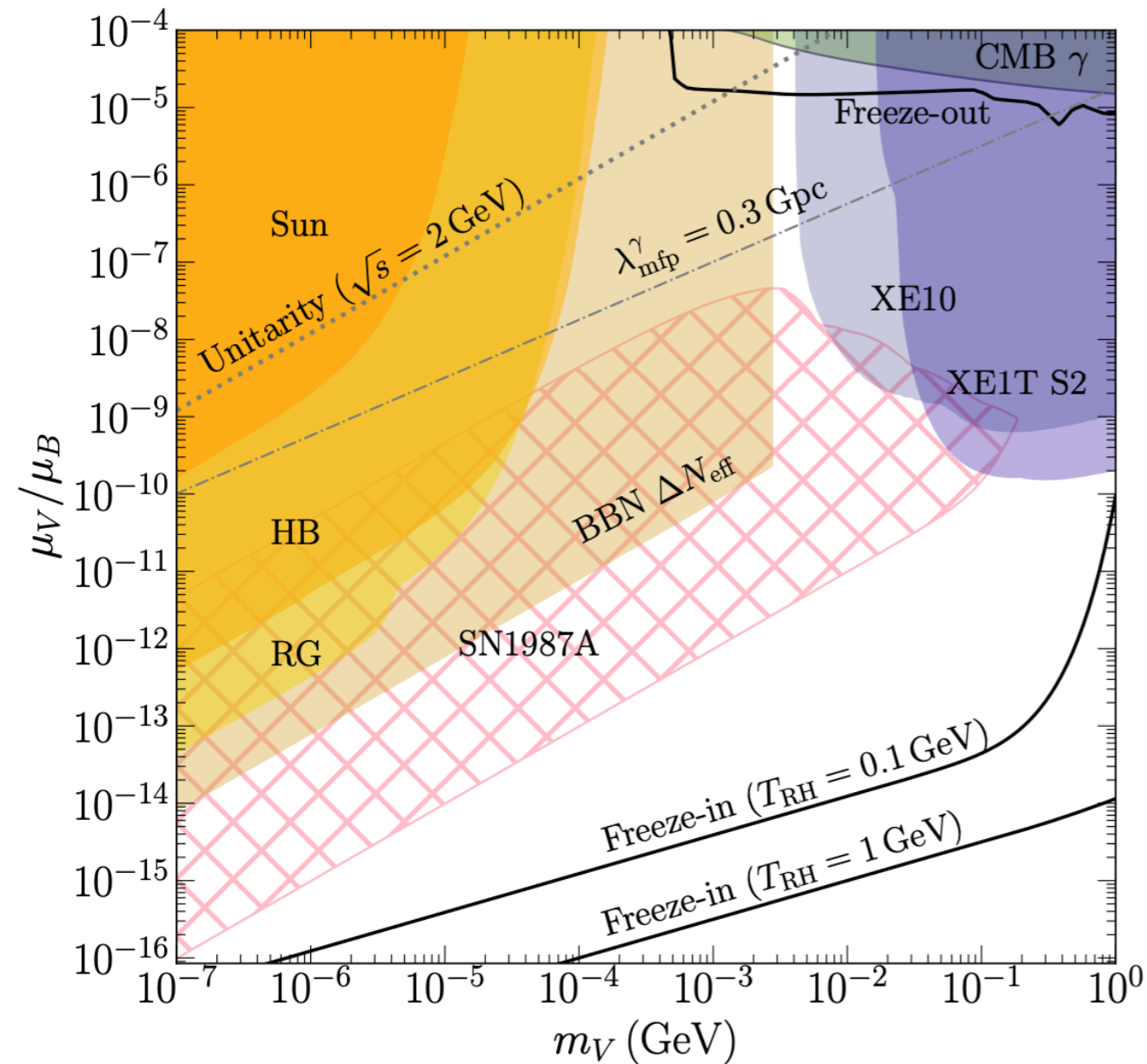
Chu, Ibarra, Hisano, Kuo, JP

[2303.13643](#)

Mass vs. coupling plane

magnetic dipole

electric dipole

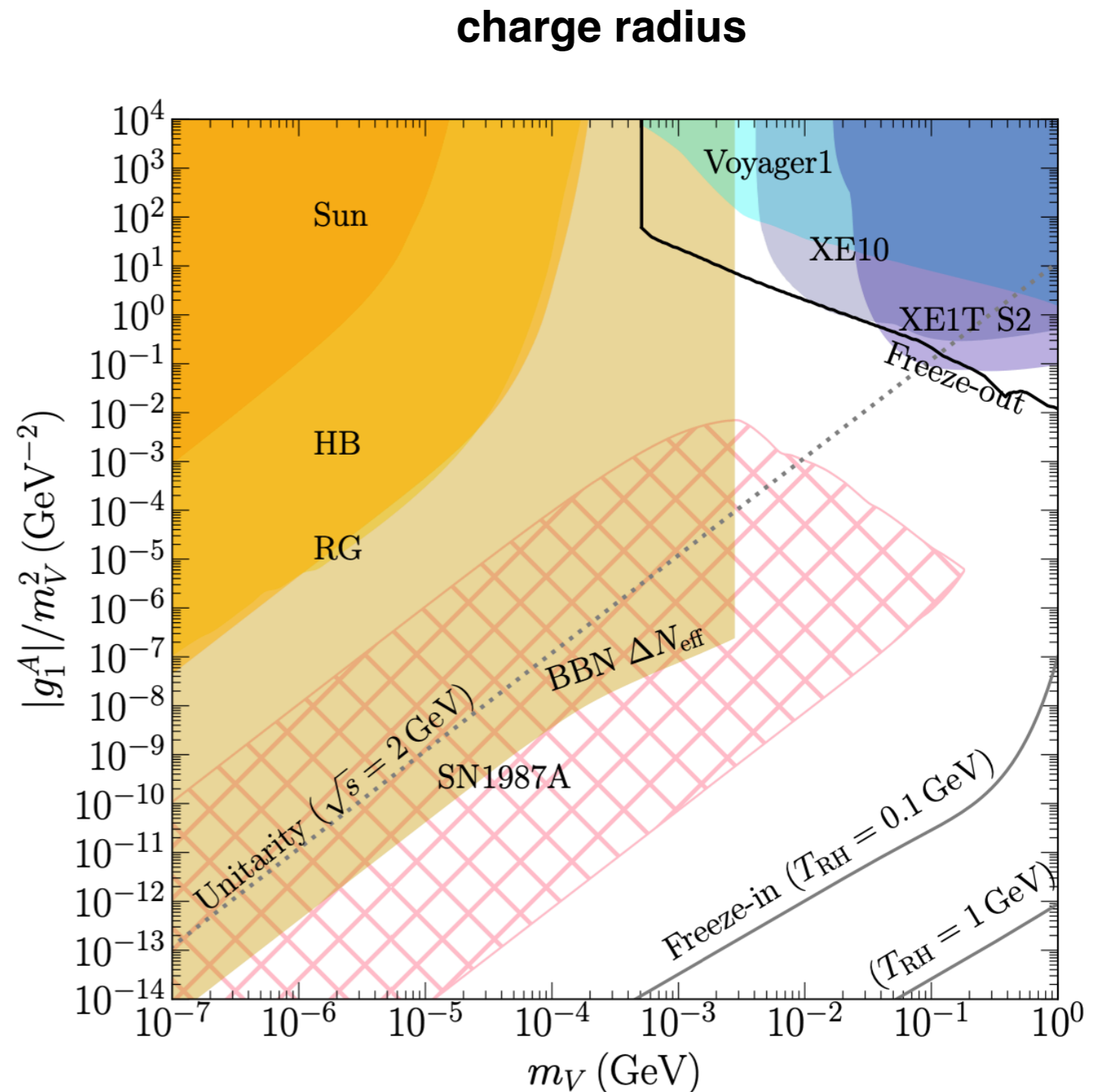


Vector DM

Validity of the effective approach?

$m_V \rightarrow 0$ limit appears worrisome for most of the effective interactions. Appears as if rates diverge in the zero mass limit.

$\sqrt{s} \lesssim v_D$ must hold as otherwise contributions from the dark Higgs will enter.



Vector DM

Chu, Ibarra, Hisano, Kuo, JP

2303.13643

Expected scaling of rates from naive dimensional analysis

Production rates should scale according to their transverse (T) and longitudinal (V) polarity as

$$\dot{Q}_{\lambda\lambda'} \propto \begin{cases} g_D^4/m_V^4 & \lambda\lambda' = \text{LL}, \\ g_D^4/m_V^2 & \lambda\lambda' = \text{LT}, \\ g_D^4 & \lambda\lambda' = \text{TT}. \end{cases} \quad \text{for } \sqrt{s}/m_V \gg 1 \quad (\text{high-energy limit})$$
$$\epsilon_L = \left(\frac{p}{m_V}, 0, 0, \frac{E}{m_V} \right), \quad \epsilon_T^\pm = \left(0, \frac{1}{\sqrt{2}}, \pm \frac{i}{\sqrt{2}}, 0 \right)$$

For example, in the UV-picture $m_V \sim g_D v_D$

$$\dot{Q}_{\text{LL}} \propto |(g_D \epsilon_{L,1})(g_D \epsilon_{L,2})|^2 \propto \frac{g_D^4}{m_V^4} \propto \frac{1}{v_D^4} \quad \text{FINITE, independent of gauge coupling (Goldstone boson equivalence thm.)}$$

BUT: even effective operators that do NOT permit LL mode (e.g. electric dipole) show same scaling

=> resolution in the UV-picture

Vector DM

UV-completion

Dark $SU(2)_D \times$ global $U(1)_X$ with a vector triplet W_D^a , dark fermions Ψ , Higgsed by Φ_D

Charge assignment such that two of the W 's are protected from decay

$$V = W^-, V^\dagger = W^+, m_V = m_{W_D}$$

↑ ↑
global quantum number

Ibarra, Hisano, Ryo (2020)

$$\langle \Phi_D \rangle = v_D / \sqrt{2}$$

$$m_{W_D} = g_D v_D / 2$$

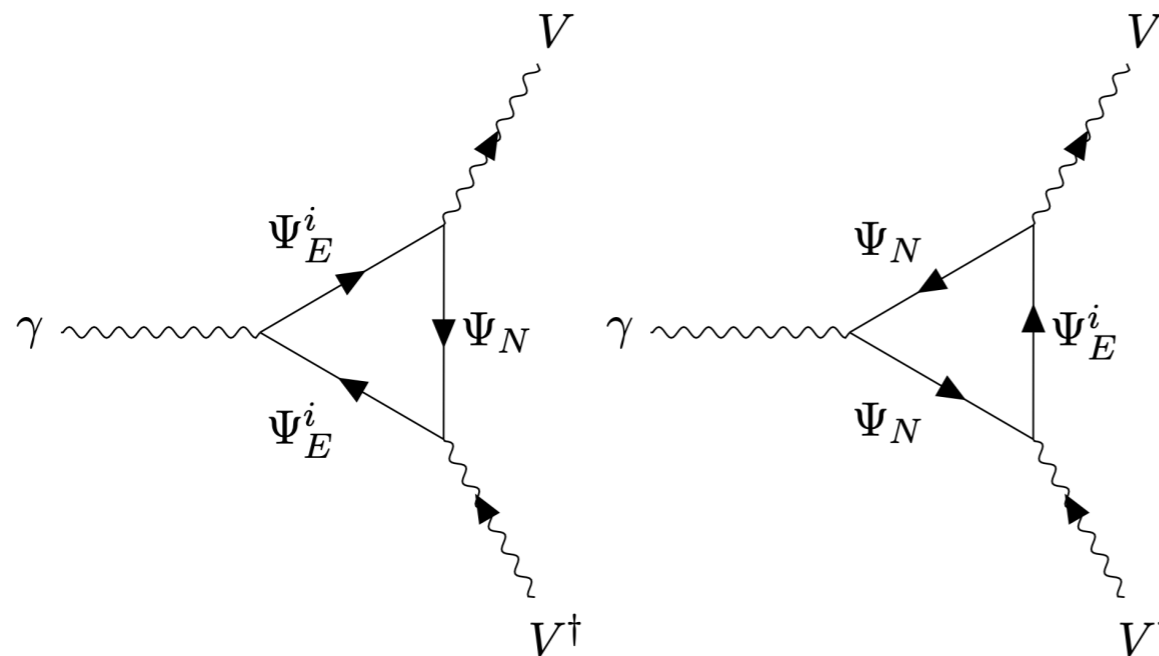
W_D^0, Ψ 's unprotected and decay to SM (W^0 via radiatively induced kinetic mixing)

Vector DM

UV-completion

Dark $SU(2)_D \times \text{global } U(1)_X$ with a vector triplet W_D^a , dark fermions Ψ , Higgsed by Φ_D
 \Rightarrow six of the seven operators radiatively induced

Ibarra, Hisano, Ryo (2020)



$$\langle \Phi_D \rangle = v_D / \sqrt{2}$$

$$m_{W_D} = g_D v_D / 2$$

$$\mathcal{L}_{\text{int}} = -\frac{g_D}{\sqrt{2}} \left(\bar{\Psi}_E^i [(V_L)_{1i} P_L + (V_R)_{1i} P_R] \gamma^\mu \Psi_N W_{D\mu}^- + \text{h.c.} \right) - e \Psi_N \gamma^\mu \Psi_N A_\mu - e \bar{\Psi}_E^i \gamma^\mu \Psi_E^i A_\mu.$$

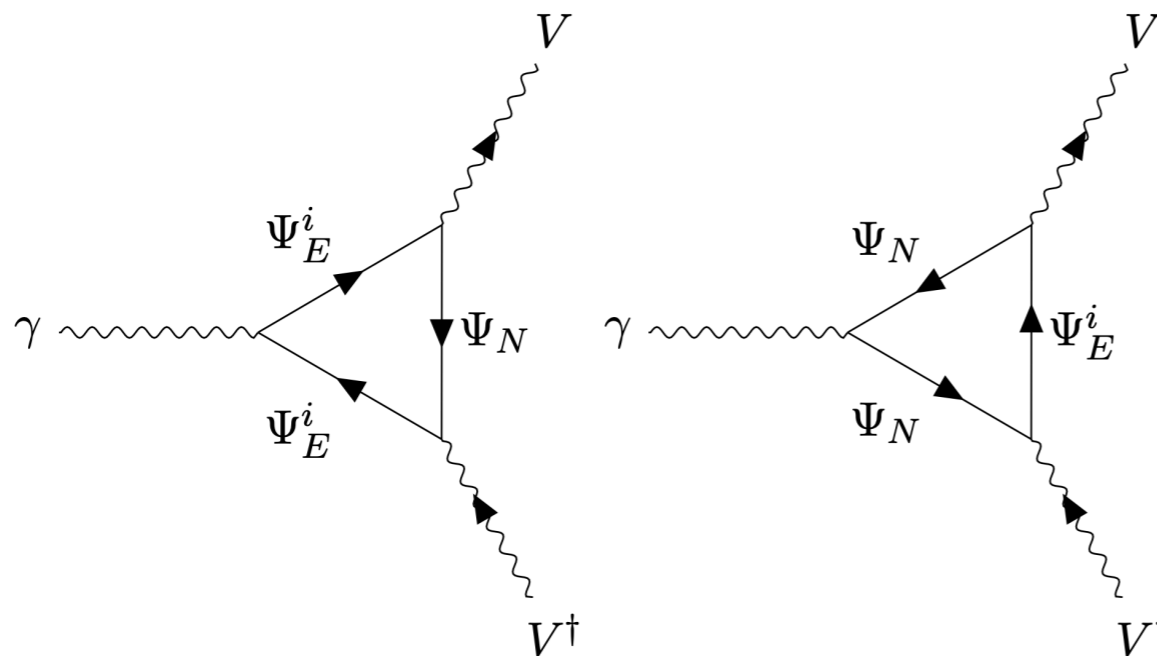
V 's diagonalize Ψ 's after SSB

Vector DM

UV-completion

Dark $SU(2)_D \times$ global $U(1)_X$ with a vector triplet W_D^a , dark fermions Ψ , Higgsed by Φ_D
 \Rightarrow six of the seven operators radiatively induced

Ibarra, Hisano, Ryo (2020)



$$\langle \Phi_D \rangle = v_D / \sqrt{2}$$

$$m_{W_D} = g_D v_D / 2$$

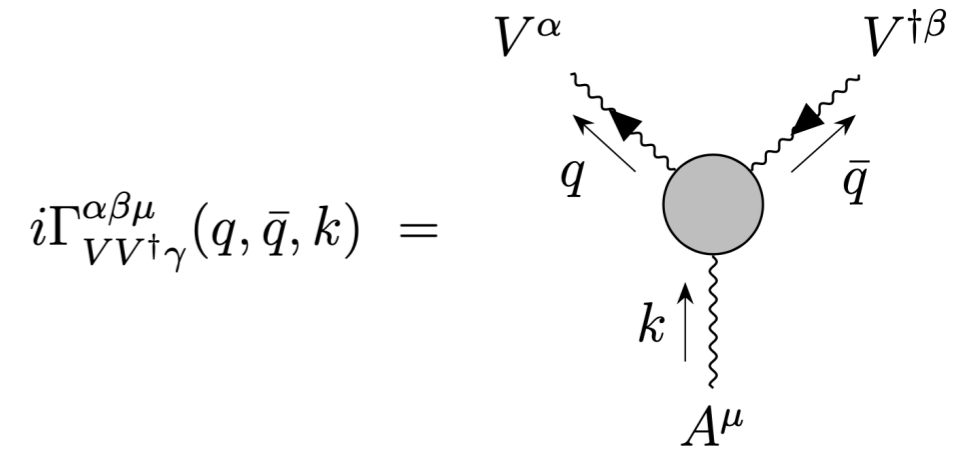
For example:

$$\mu_V = -e \frac{g_D^2}{64\pi^2} \frac{1}{m_V} \sum_{i=1}^2 (1 - x_i^2) \left[\left(|(V_L)_{1i}^2|^2 + |(V_R)_{1i}^2|^2 \right) \times \text{loop function} \right]$$

$$d_V = e \frac{g_D^2}{64\pi^2} \frac{1}{m_V} \sum_{i=1}^2 \text{Im} \left((V_L)_{1i}^* (V_R)_{1i}^* \right) \times \text{loop function}$$

Vector DM

proper high energy limit



Coupl.	UV model	$\dot{Q} \propto f(s)$	$\dot{Q} _{m_V \rightarrow 0}$	pol.
μ_V	$\frac{g_D^2}{m_V} \propto \frac{g_D}{v_D}$	$\frac{\mu_V^2}{m_V^2} \propto \frac{1}{v_D^4}$	finite	all
d_V	$\frac{g_D^2}{m_V} \propto \frac{g_D}{v_D}$	$\frac{d_V^2}{m_V^2} \propto \frac{1}{v_D^4}$	finite	TT

From the UV perspective, multipole moments are not independent, emission rate probes $i\Gamma^{\alpha\beta\mu}$

magn. dipole	$\mu_V = \frac{e}{2m_V} \left(\kappa_\Lambda + \frac{m_V^2}{\Lambda^2} \lambda_\Lambda \right)$
elec. dipole	$d_V = \frac{e}{2m_V} \left(\tilde{\kappa}_\Lambda + \frac{m_V^2}{\Lambda^2} \tilde{\lambda}_\Lambda \right)$

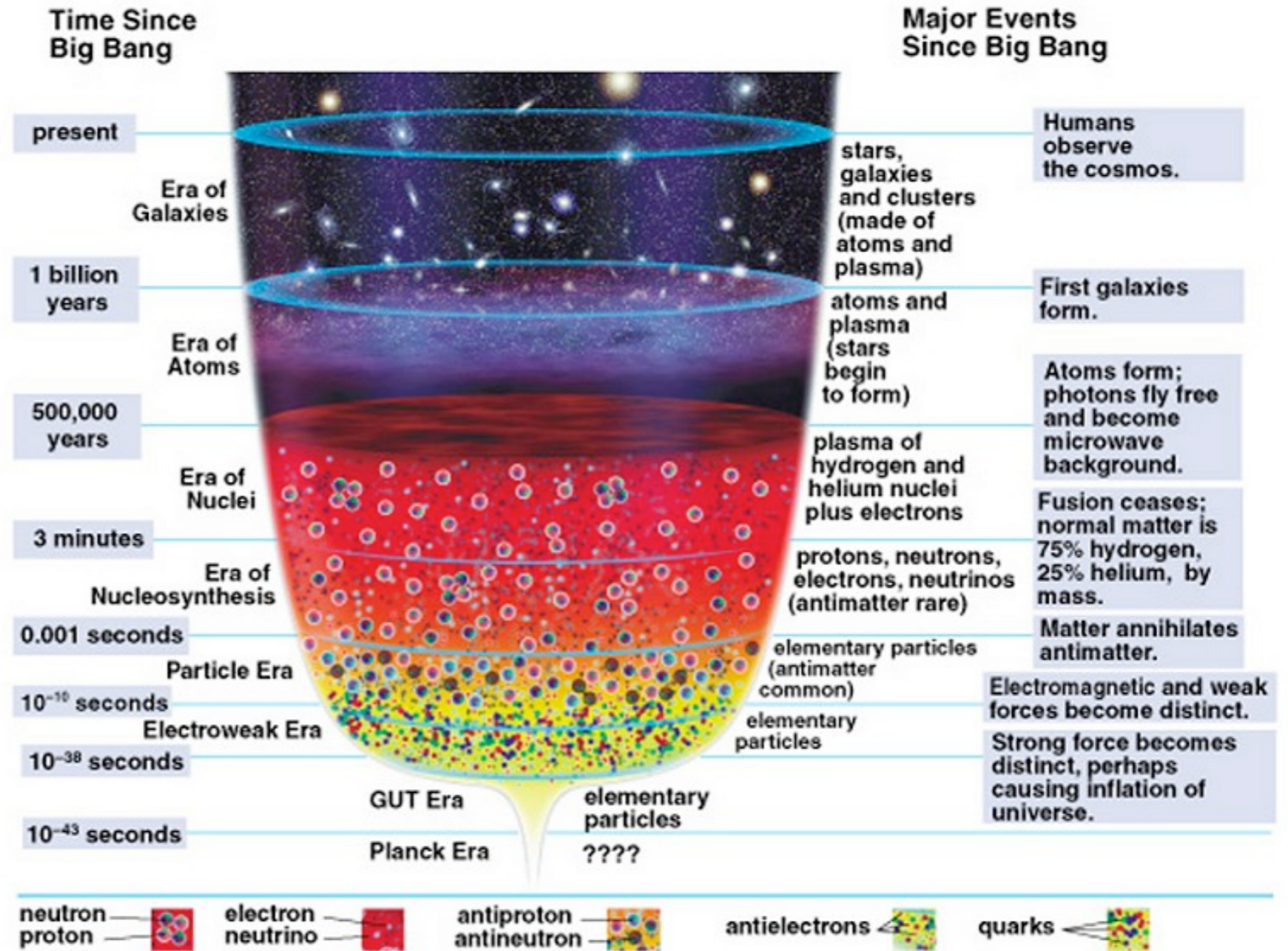
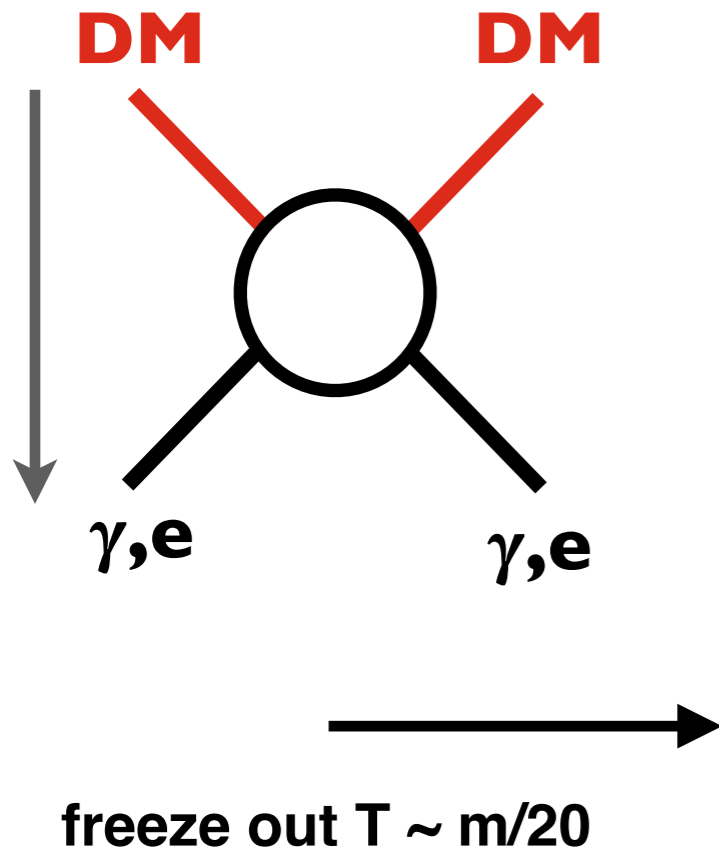
=> switch basis

	κ_Λ	λ_Λ	g_1^A
UV	g_D^2	$\frac{g_D^2 \Lambda^2}{m_N^2}$	$\frac{g_D^2 m_V^2}{m_N^2}$
C,P	(+, +)		
\dot{Q}_{LL}	$\frac{\kappa_\Lambda^2}{m_V^4}$	$\propto \frac{g_D^4}{m_V^4}$	
\dot{Q}_{LT}	$\frac{\kappa_\Lambda^2}{m_V^2}$	$\propto \frac{g_D^4}{m_V^2}$	
\dot{Q}_{TT}	$\left(\frac{\lambda_\Lambda}{\Lambda^2} + \frac{g_1^A}{m_V^2} \right)^2 \propto g_D^4$		

=> when all operators that share C,P properties are considered jointly, rates scale precisely as NDA suggests!

2. Thermal MeV DM

OR: what is the lightest thermal DM mass?



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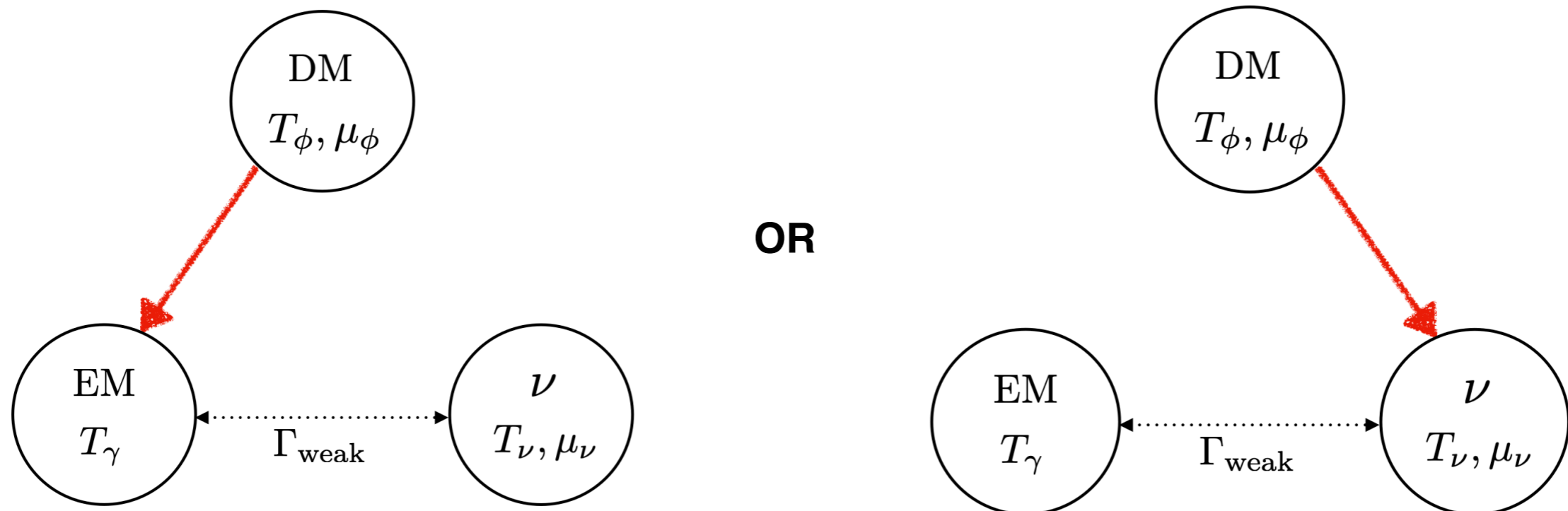
2. Thermal MeV DM

Chu, Kuo, JP, PRD 2022
Chu, JP arXiv:2310.06611

OR: what is the lightest thermal DM mass?

Well known that MeV-DM subject to Neff bound from heating by annihilation

Previous treatments had to assume a branching either into EM-sector OR neutrinos:



2. Thermal MeV DM

Chu, Kuo, JP, PRD 2022
Chu, JP arXiv:2310.06611

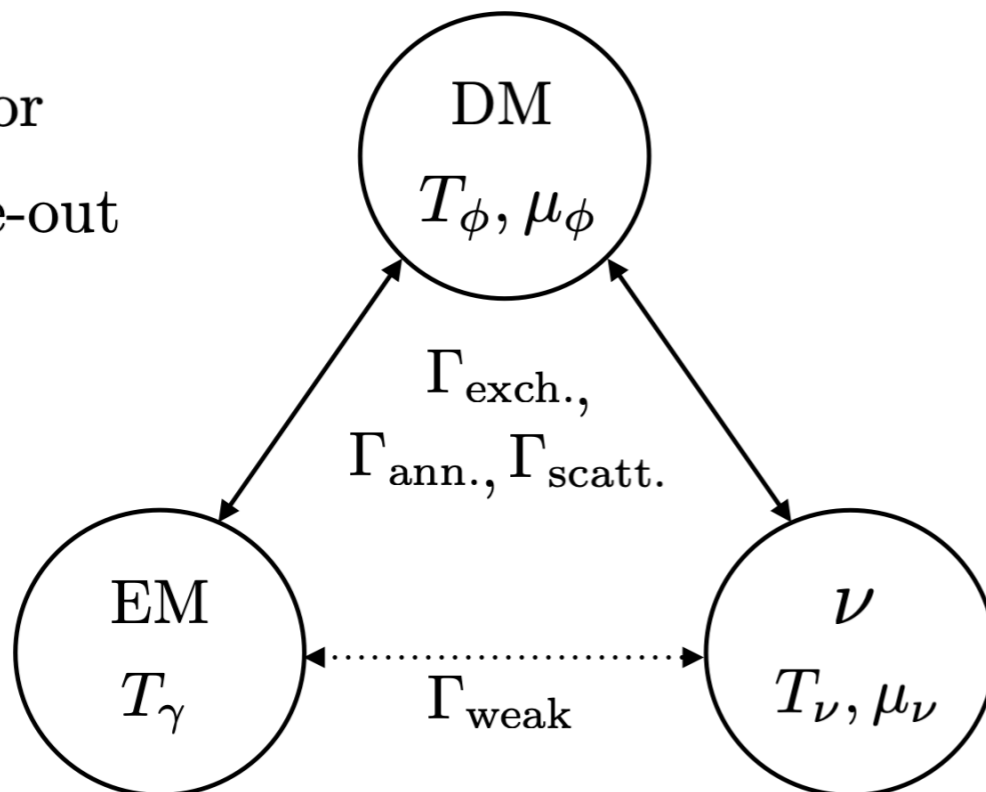
OR: what is the lightest thermal DM mass?

Well known that MeV-DM subject to Neff bound from heating by annihilation

In the full picture, joint treatment of the three coupled sectors is necessary

three-sector

DM freeze-out



$$\Gamma_{\text{weak}} \equiv n_e G_F^2 T_\gamma^2 ,$$

$$\Gamma_{\text{ann.}} \equiv n_\phi \langle \sigma_{\text{ann.}} v \rangle ,$$

$$\Gamma_{\text{exch.},i} \equiv n_\phi^2 \langle \sigma_{\text{ann.},i} v \delta E \rangle / \rho_i ,$$

$$\Gamma_{\text{scatt.},i} \equiv n_i \langle \sigma_{\text{scatt.}}^{\phi i} v \rangle .$$

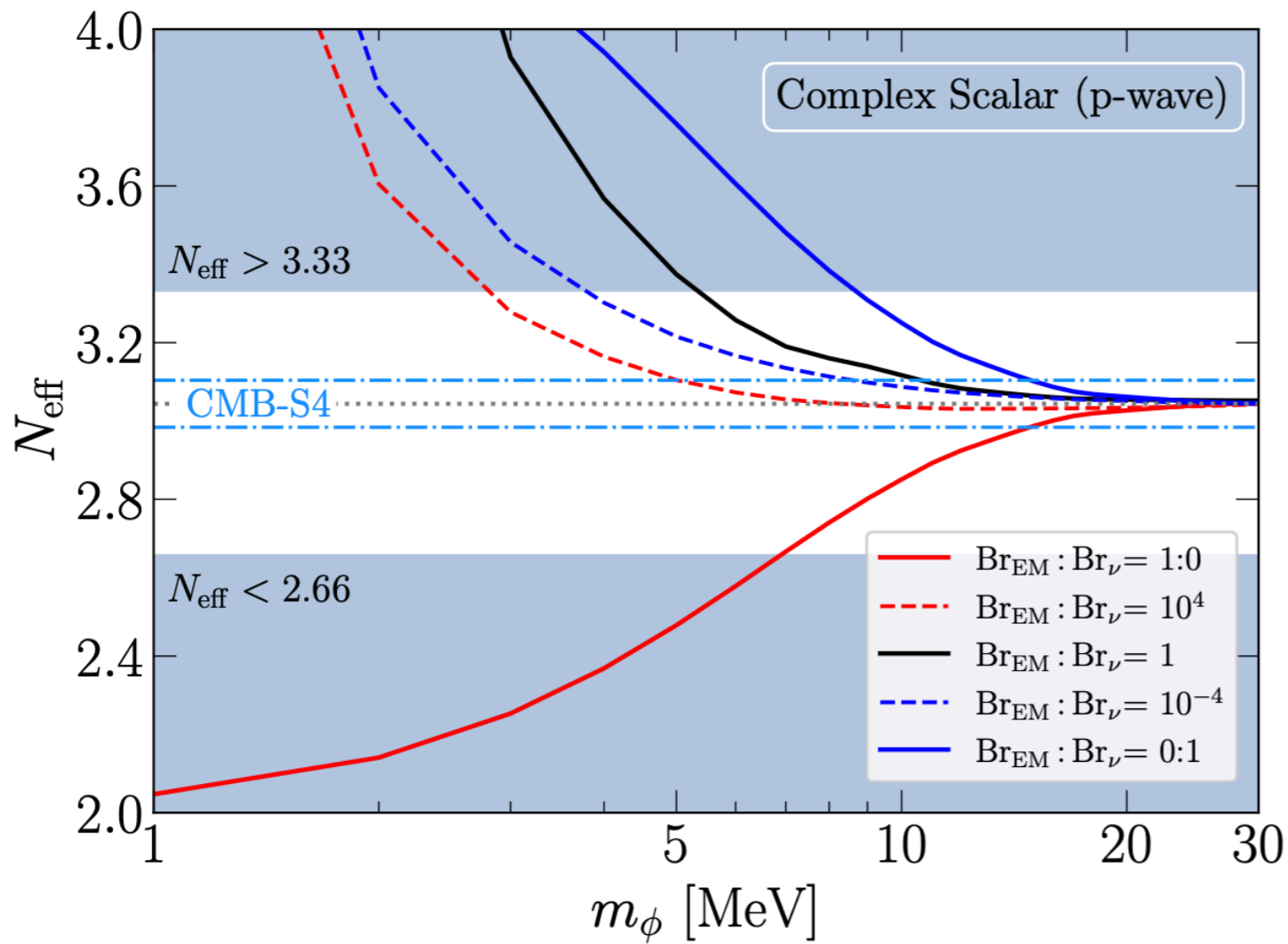
=> we are the first to be able to treat a relative branching AND to include energy transfer from elastic scattering

=> allows to track DM temperature (feeds into efficiency of annihilation for p-, d- ... wave)

=> allows for a precision prediction of Neff and to derive a lower bound on the DM mass

Light DM freeze out

What is the lightest thermal DM mass?

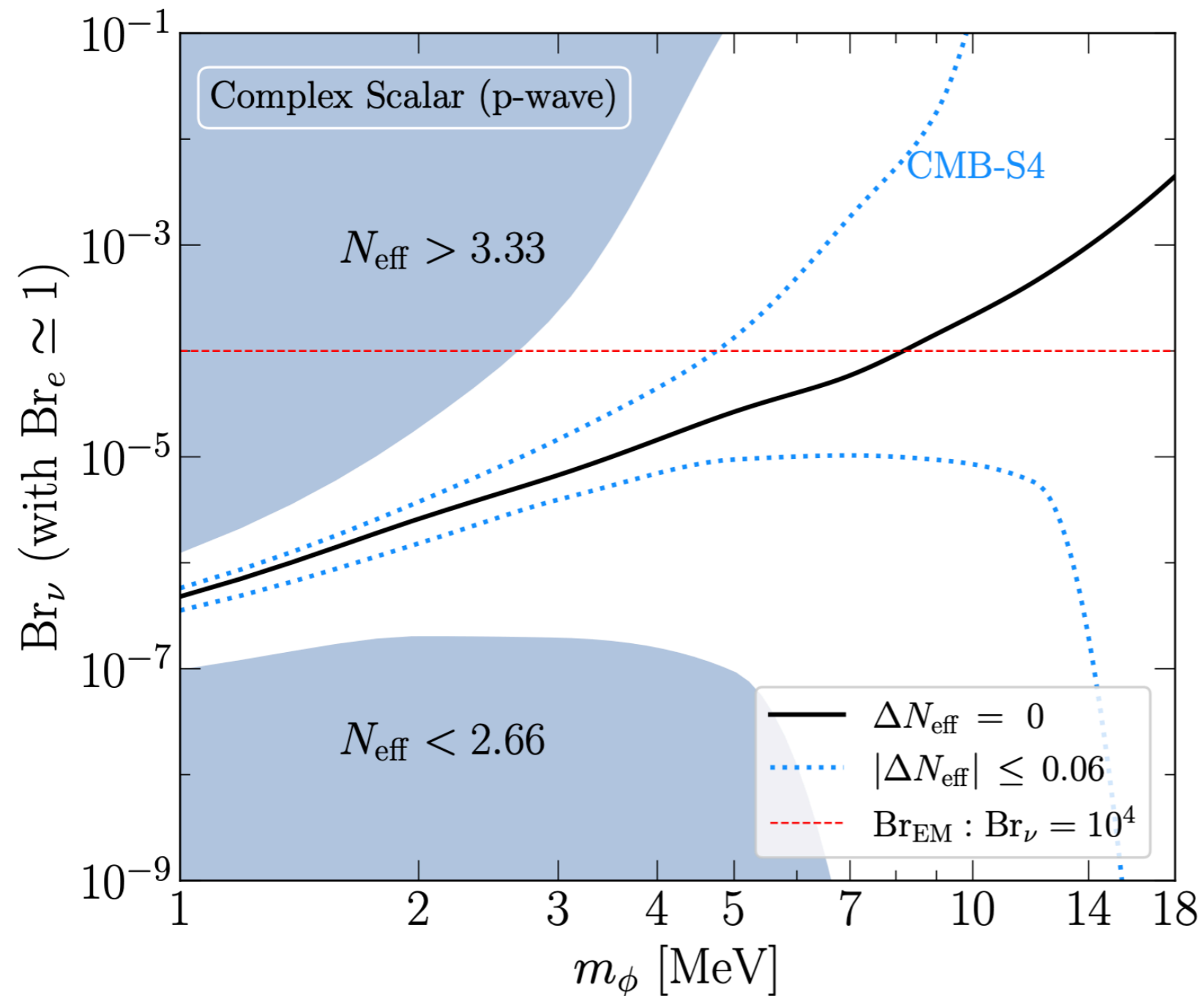


Example: p-wave annihilation

Evading Neff bound

Chu, JP arXiv:2310.06611

OR: How low can you go?

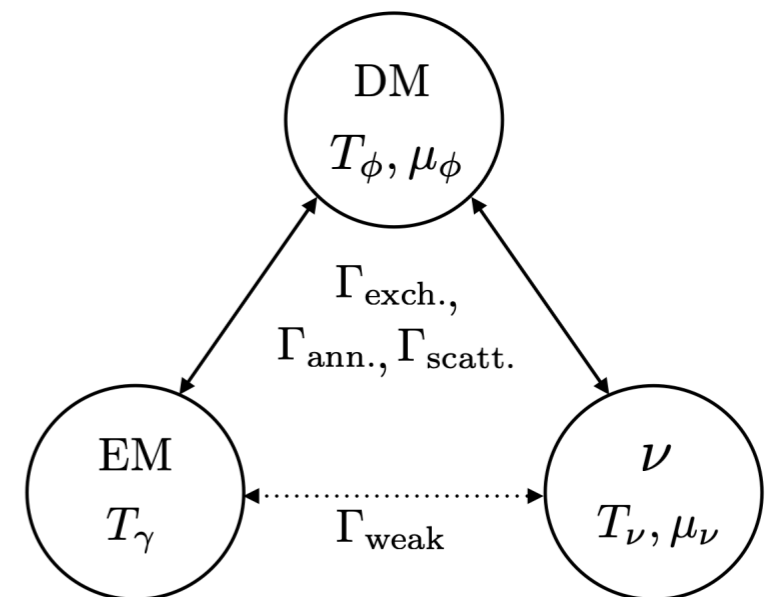
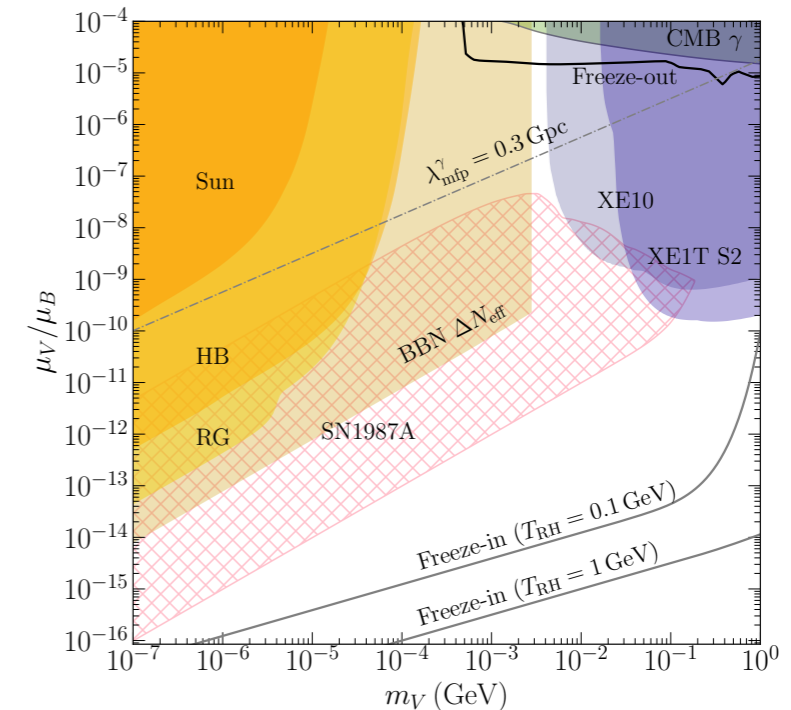


Fine-tuned branching
into neutrinos evades
Neff constraint.

Summary

sub-GeV dark state phenomenology

- neutral dark particles can couple to the photon through higher dimensional electromagnetic moment interactions. Spin-1/2 and 1 particles have many
 - thermal freeze-out excluded by direct detection and indirect detection constraints (exceptions are anapole and toroidal moment interactions)
 - thermal freeze-in line is never touched by any considered probes, but dark state parameter space otherwise severely constrained by astrophysical limits
-
- A comprehensive assessment of thermal MeV-scale DM necessitates a three-sector treatment of vastly changing rates => found a systematic formulation



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Austrian Academy of Sciences, Institute of High Energy Physics (HEPHY)

Position ID: [Austrian Academy of Sciences-Institute of High Energy Physics \(HEPHY\)-POSTDOC \[#26842, HEPHY157PD223\]](#)

Position Title: POSTDOC on Dark Matter Theory

Position Type: Postdoctoral

Position Location: Vienna, Wien 1010, Austria [[map](#)] 🌐

Subject Areas: [Physics / Astroparticle Physics](#), [HEP-Phenomenology \(hep-ph\)](#), [Particle Theory](#), [theoretical astroparticle physics](#), [Theoretical Particle Physics](#), [Theoretical Physics](#), [HEP-Phenomenology \(hep-ph\)](#), [Astrophysics \(astro-ph\)](#), [GR-Cosmology \(gr-qc\)](#), [Cosmology](#), [Gravity](#), [Astrophysics Theory](#), [Particle Astrophysics](#), [Theoretical Particle Physics](#), [Particle/Cosmology Theory](#), [Fundamental Theory/Cosmology](#), [particl](#)

Appl Deadline: 2023/12/31 11:59PM (posted 2023/12/11, listed until 2024/06/11)

Position Description: [Edit \[revs\]](#) [\[viewed\]](#) [Preview](#) [Status](#) [mv](#) 🤖



Postdoc position open

The Theory Group at the Institute of High Energy Physics (HEPHY) of the Austrian Academy of Sciences (OeAW) solicits applications for a POSTDOCTORAL POSITION (F/M/X) on Dark Matter Theory and Physics beyond the Standard Model (full-time, 40 hours per week) for an initial duration of two years, beginning in Fall 2024 or earlier.

We invite applications in all areas of theoretical particle physics, in particular from candidates with a strong background in theoretical astroparticle physics and particle phenomenology. The position is in the group of Prof. Josef Pradler which is supported by the ERC Consolidator Grant NLO-DM. The successful candidate will have experience in one or more of the following areas

- Beyond the Standard Model particle physics
- Particle physics applied in astrophysical and/or cosmological contexts, including but not limited to Dark Matter.
- Dark Matter direct detection and its intersect with condensed matter physics.

The successful candidate is expected to work independently as well collaboratively on theoretical particle and astroparticle physics, with a particular focus on dark matter phenomenology (laboratory detection, early Universe cosmology, astrophysical aspects, among other topics) and support the ERC funded efforts.

The Institute of High Energy Physics is Austria's leading non-university institution for science and research and performs a rich experimental particle physics program participating in accelerator and non-accelerator-based experiments. The institute has significant involvements in CMS at CERN, the Belle II experiment at KEK, and several Dark Matter discovery experiments. Theory and machine learning groups complete the research profile of the institute.