



Double alpha decay

PHENIICS Fest 2023

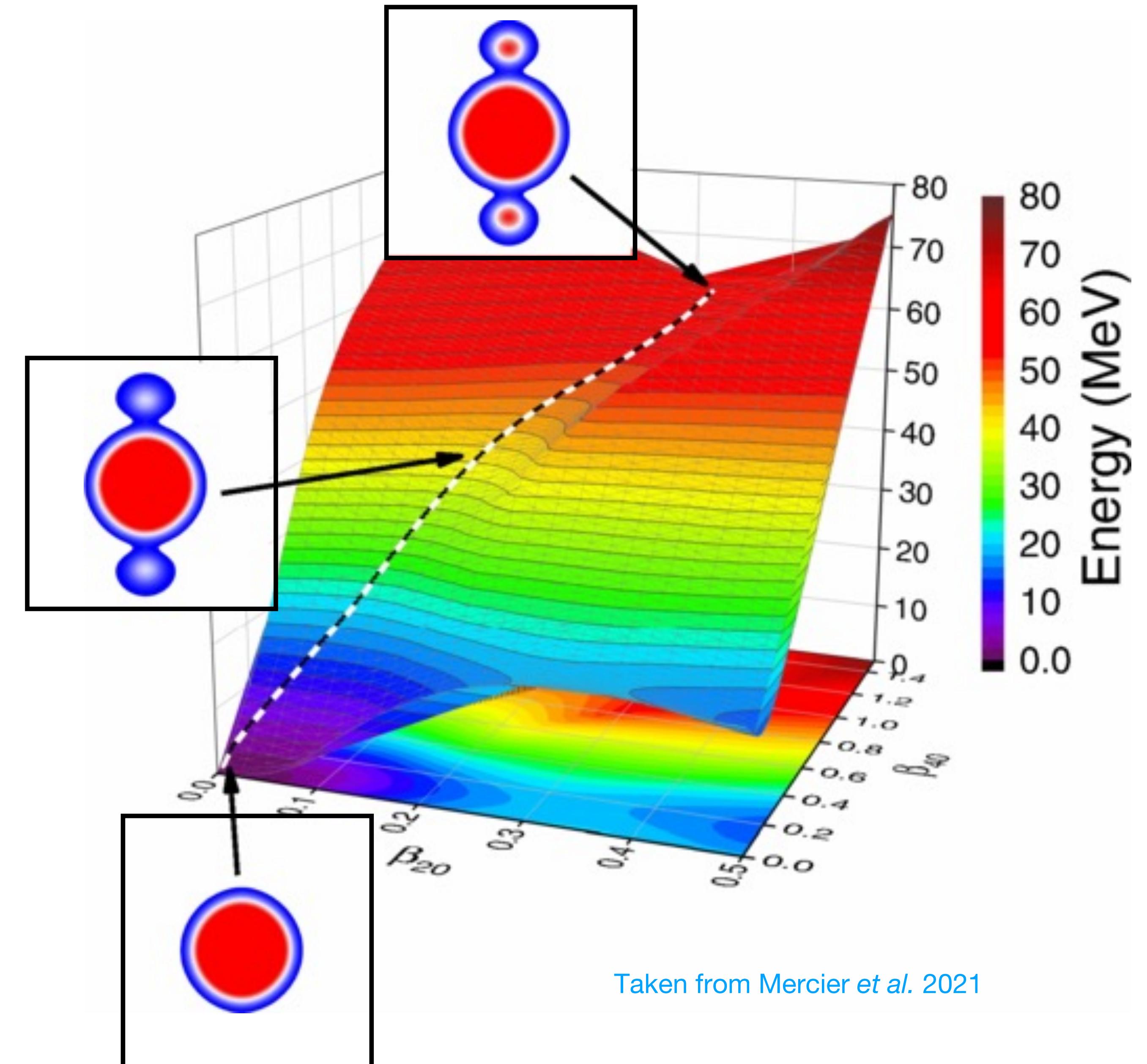
L. Heitz



Henri Cartier-Bresson
Naples, 1960

Outline

- Theoretical framework
- Experimental search for 2α
 - FRS Ion Catcher / GSI
 - Isolde, CERN / Saclay

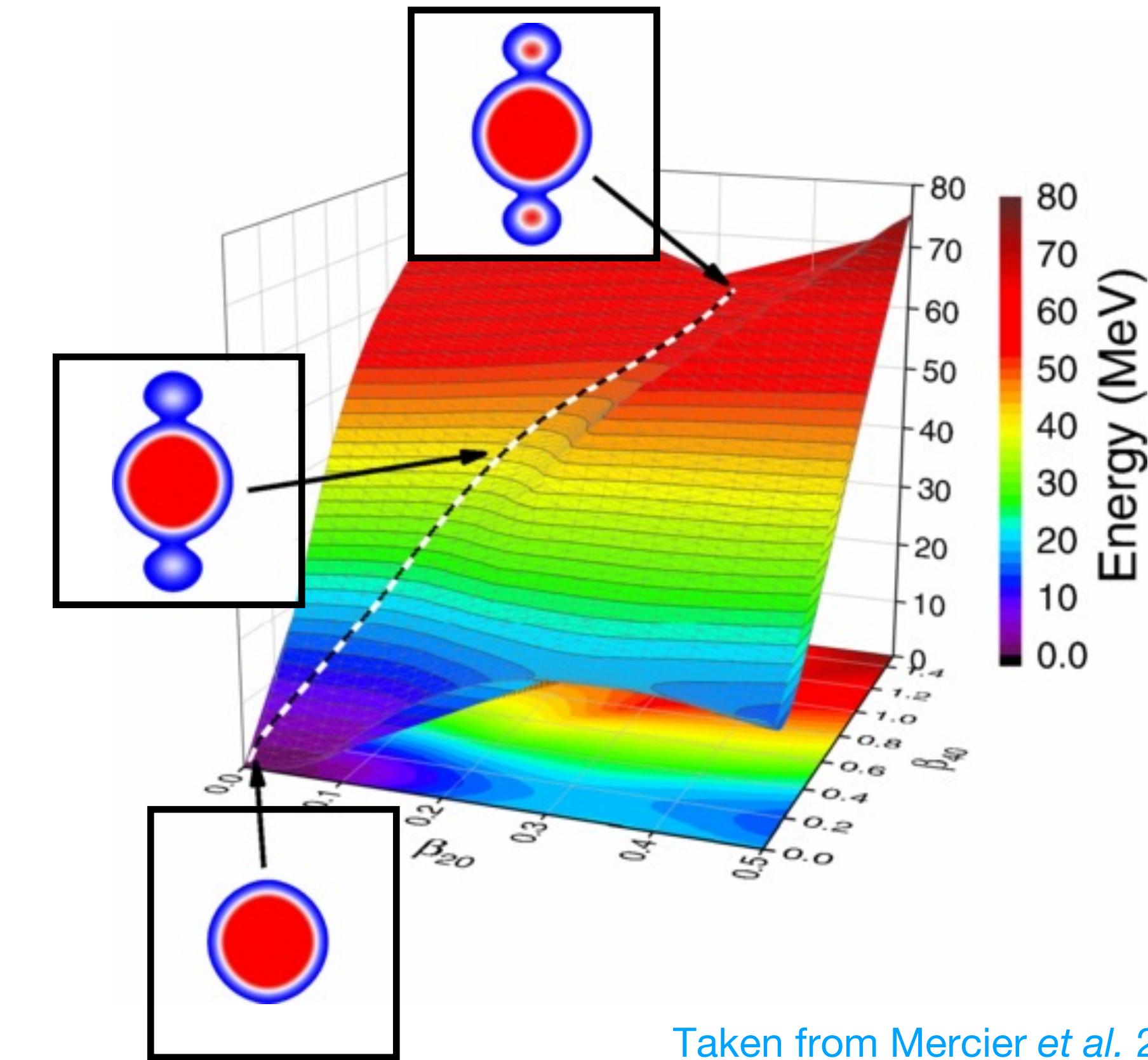


Theoretical framework

Microscopic description of radioactivity



2021



Taken from Mercier et al. 2021

Theoretical framework

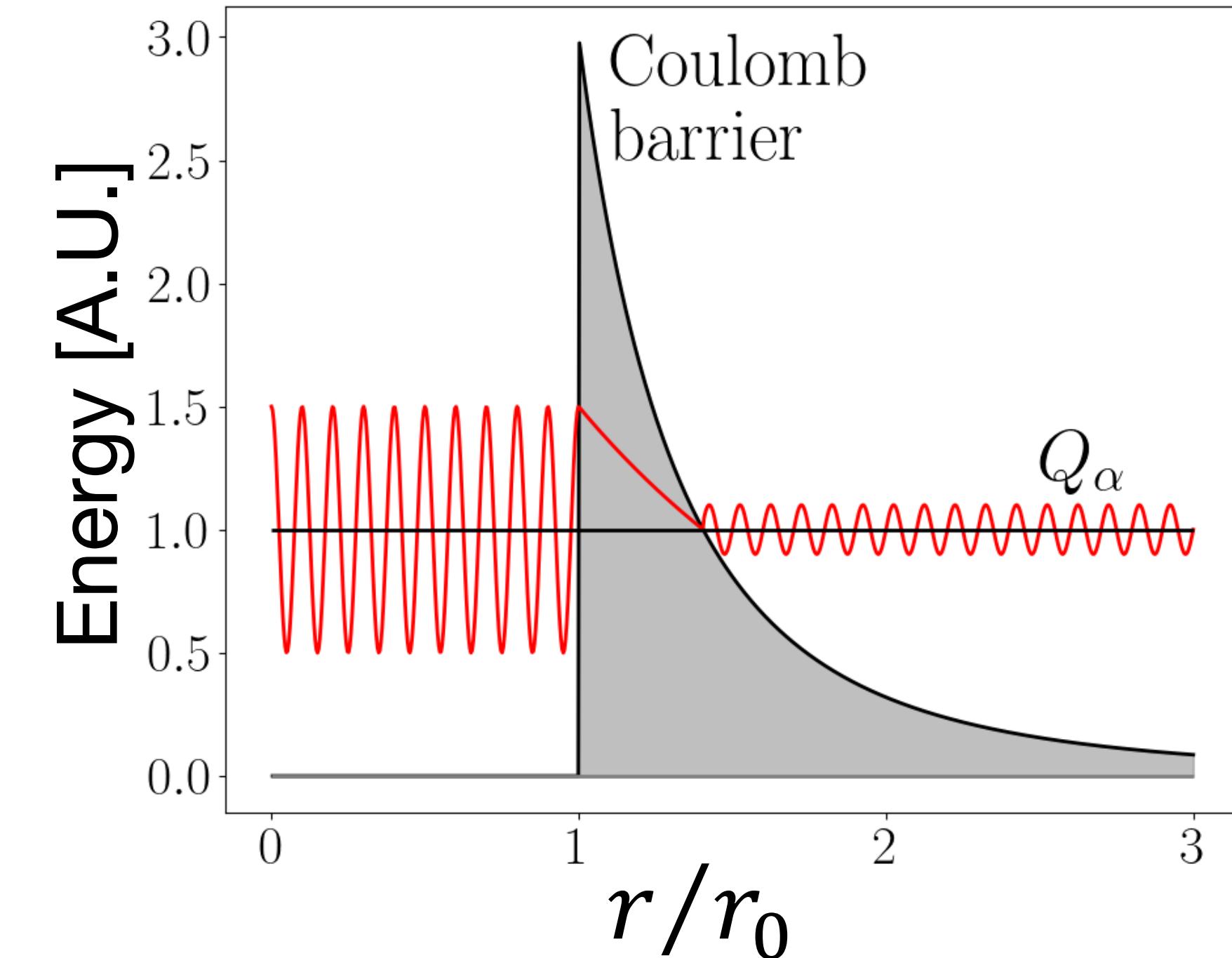
Alpha & double alpha radioactivities



Theoretical framework

Alpha & double alpha radioactivities

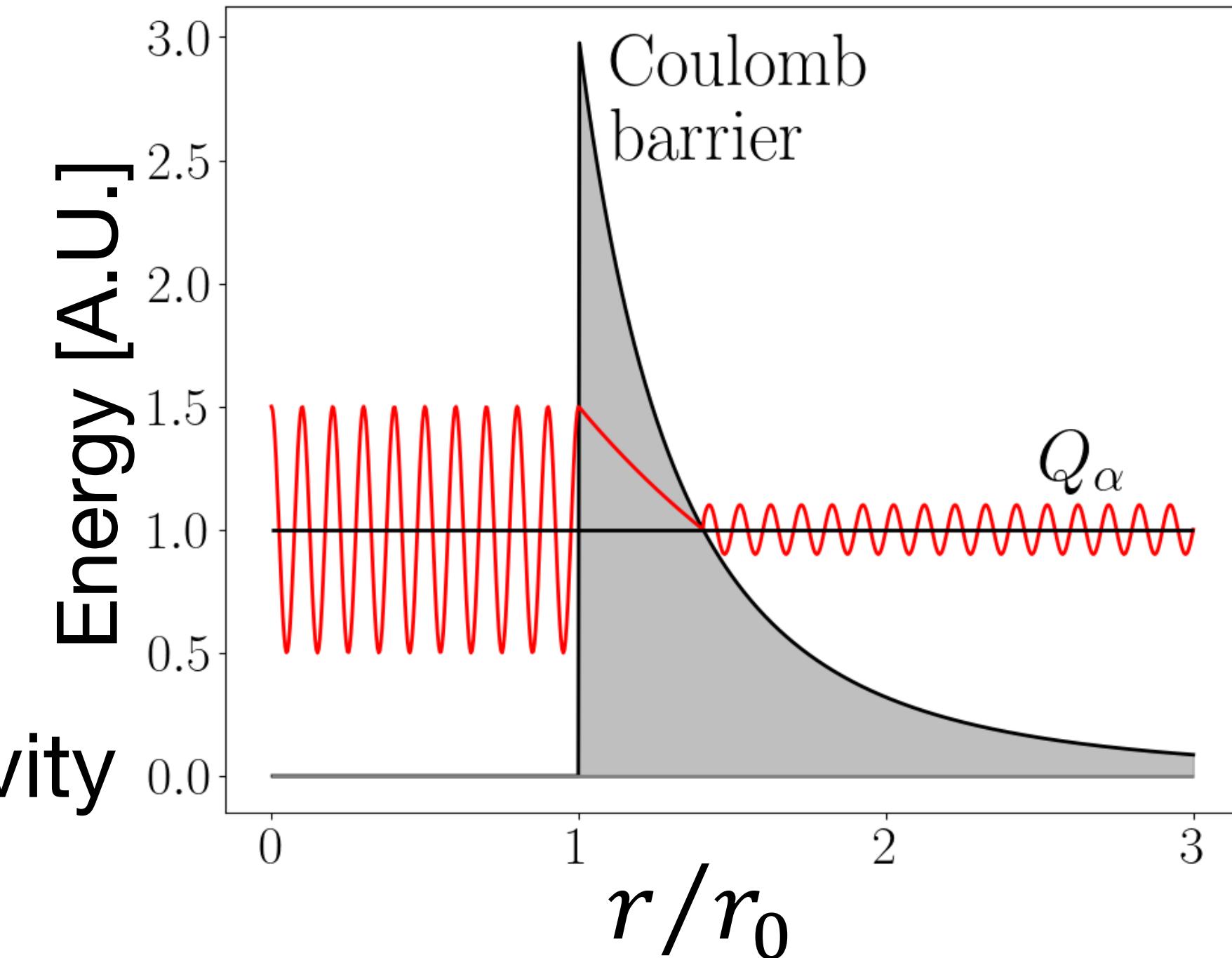
- First model for α decay : Gamow 1928 (tunneling)



Theoretical framework

Alpha & double alpha radioactivities

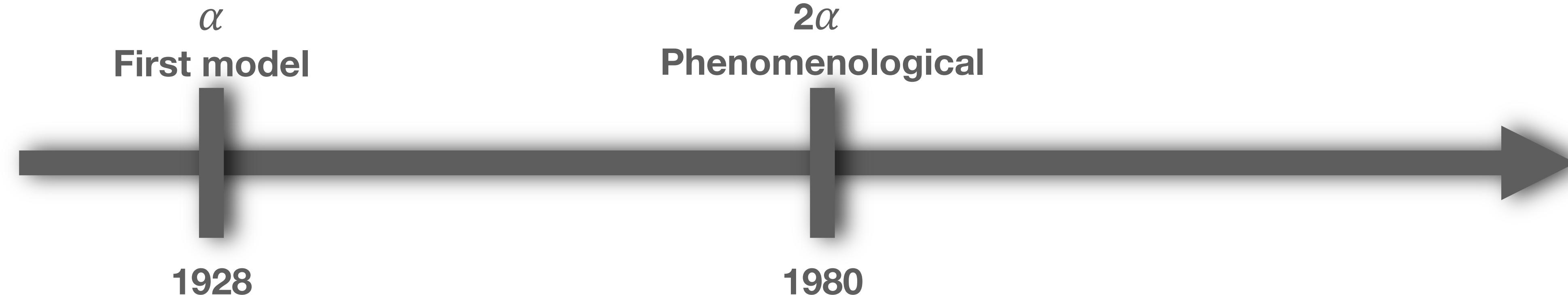
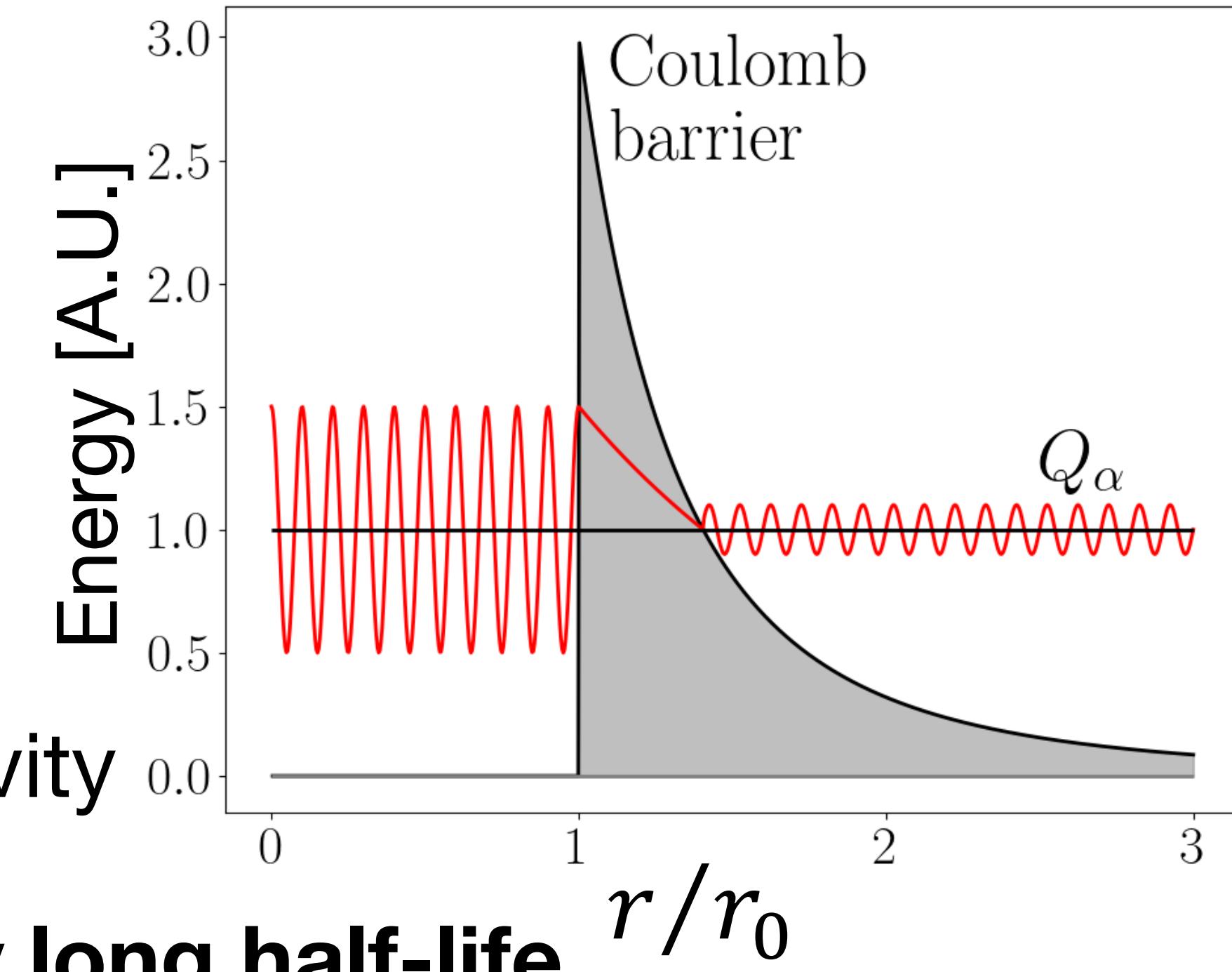
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- Phenomenological models for alpha/cluster radioactivity



Theoretical framework

Alpha & double alpha radioactivities

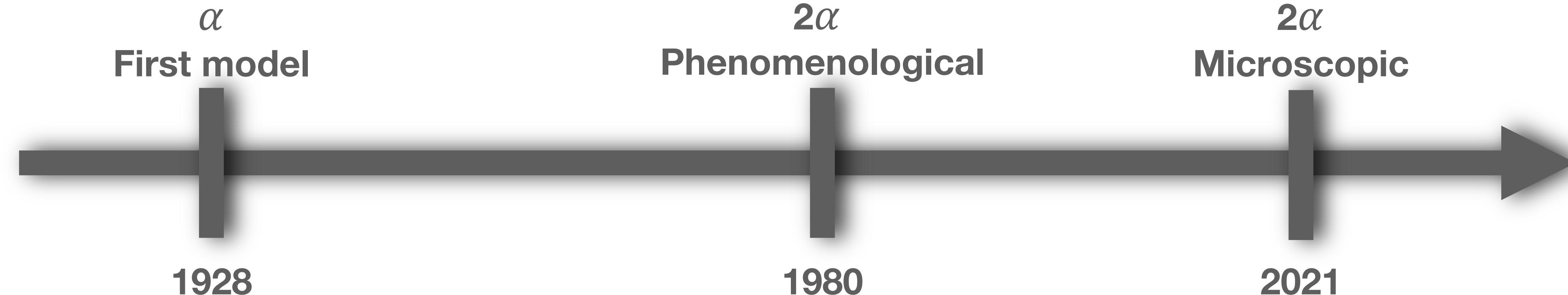
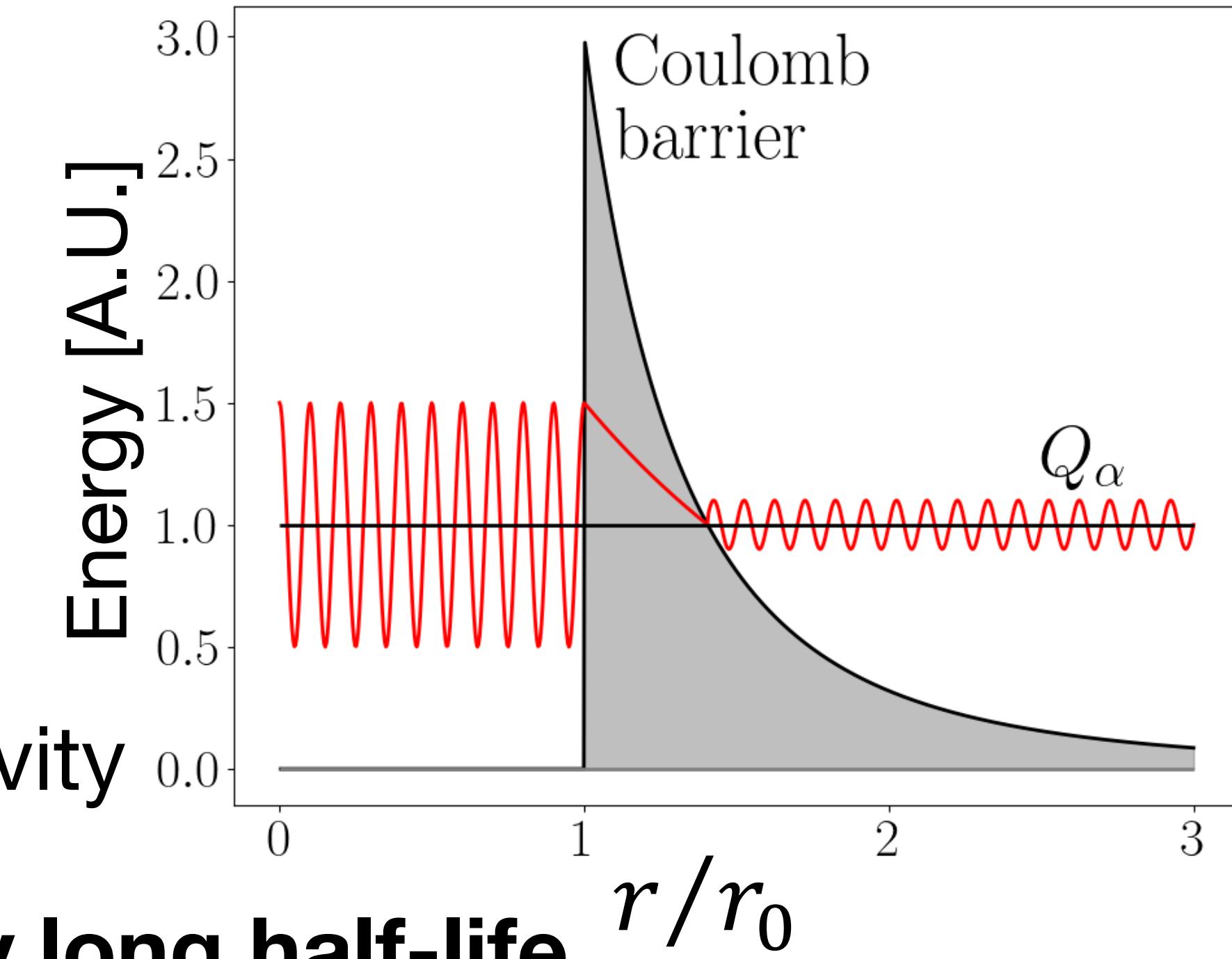
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- First prediction for 2α : Poenaru 1980 , ${}^8\text{Be}$ -like, very long half-life



Theoretical framework

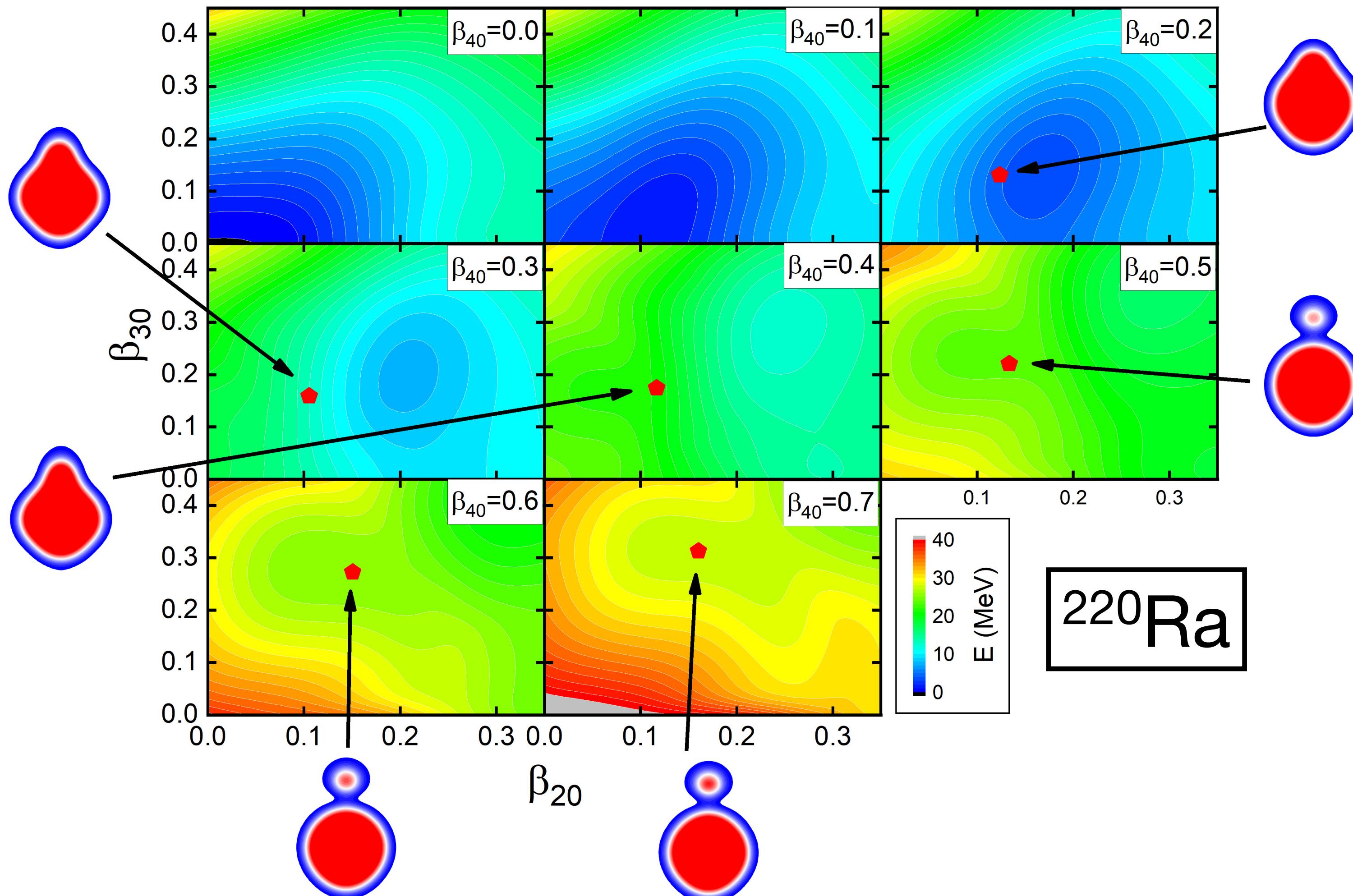
Alpha & double alpha radioactivities

- First model for α decay : Gamow 1928 (tunneling)
- Phenomenological models for alpha/cluster radioactivity
- First prediction for 2α : Poenaru 1980 , ${}^8\text{Be}$ -like, very long half-life
- Microscopic description : Mercier 2021, Zhao 2023, of α , 2α decays (& cluster)



Theoretical framework

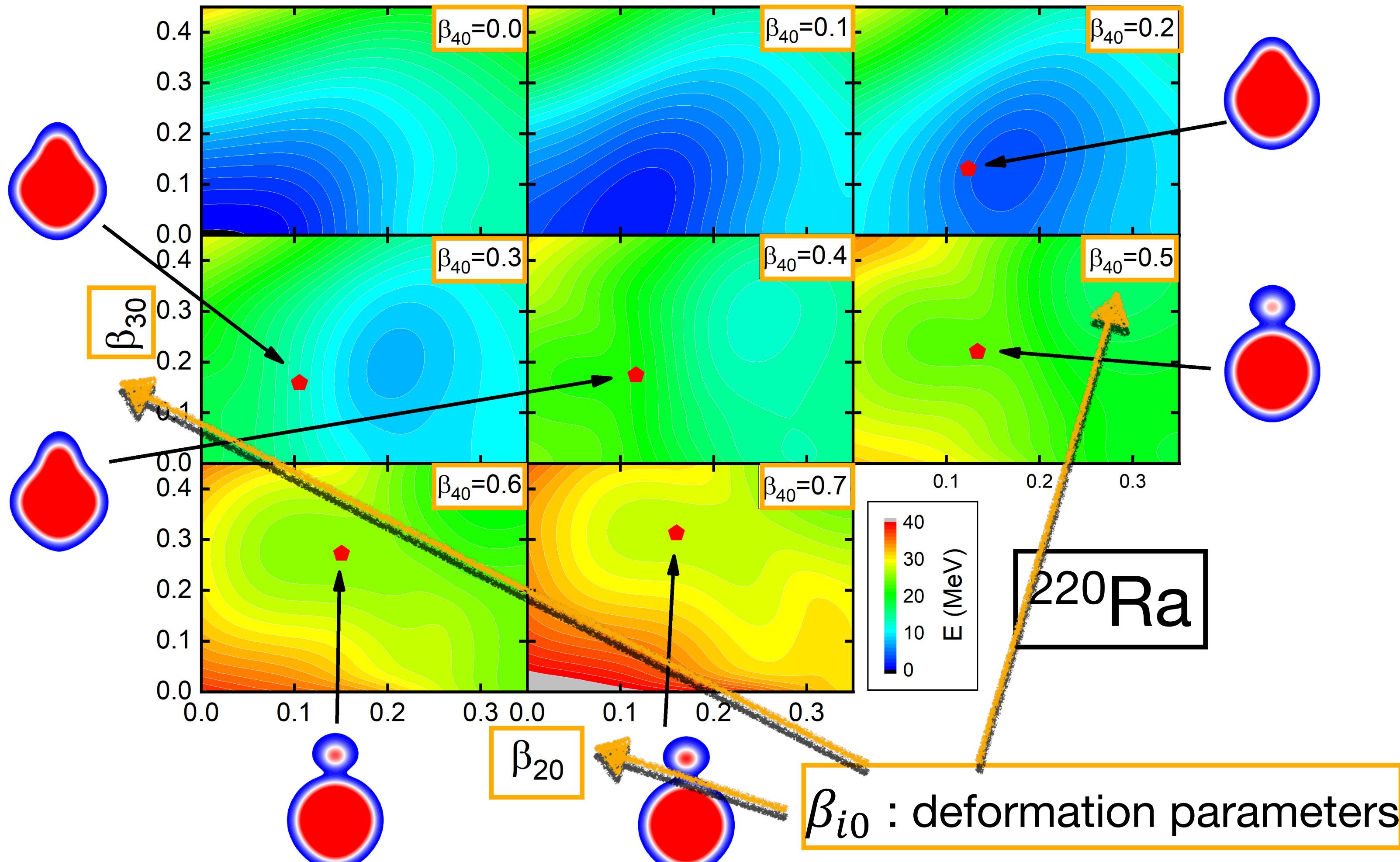
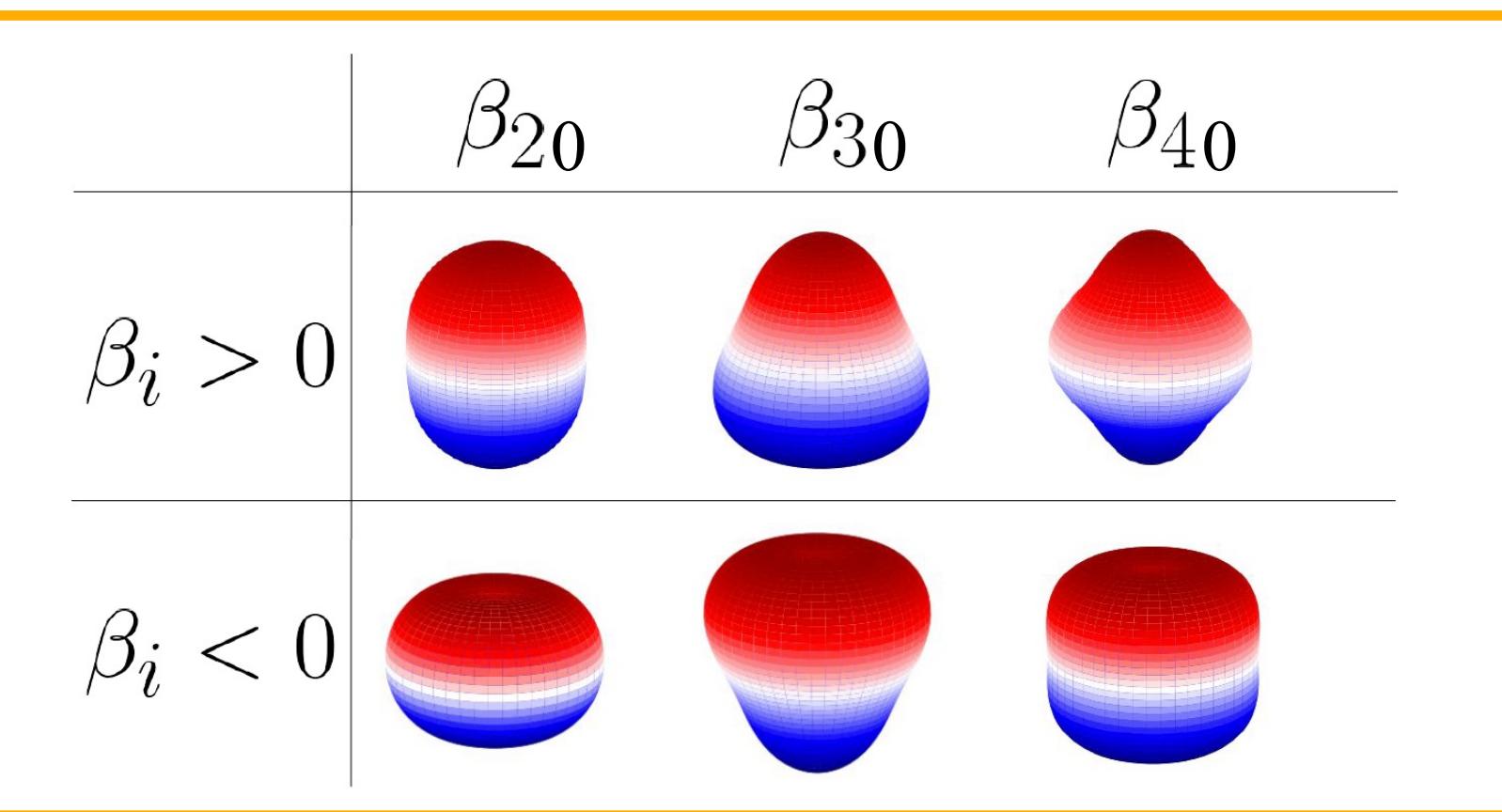
Single alpha decay



Theoretical framework

Single alpha decay

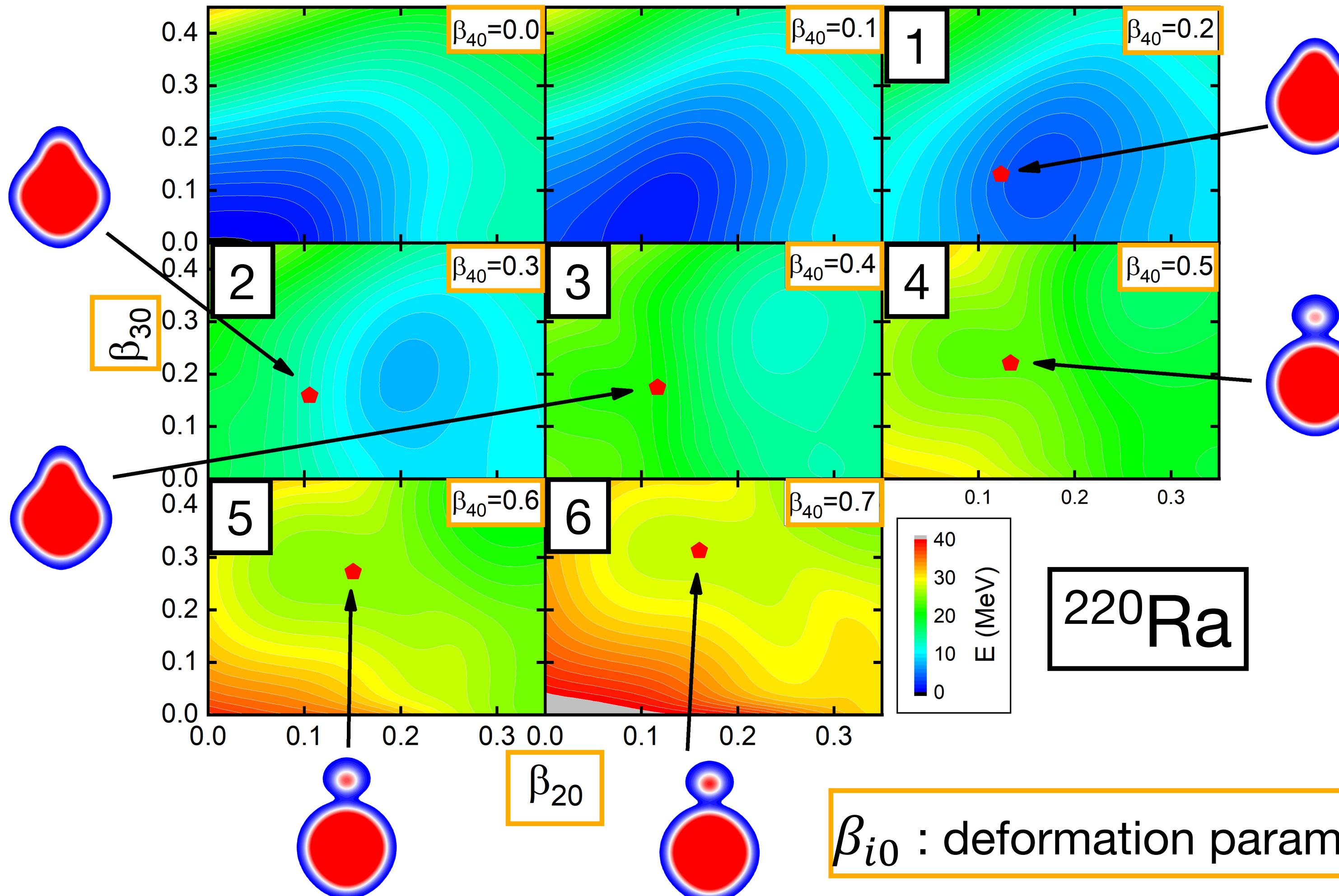
Taken from
Mercier PhD thesis



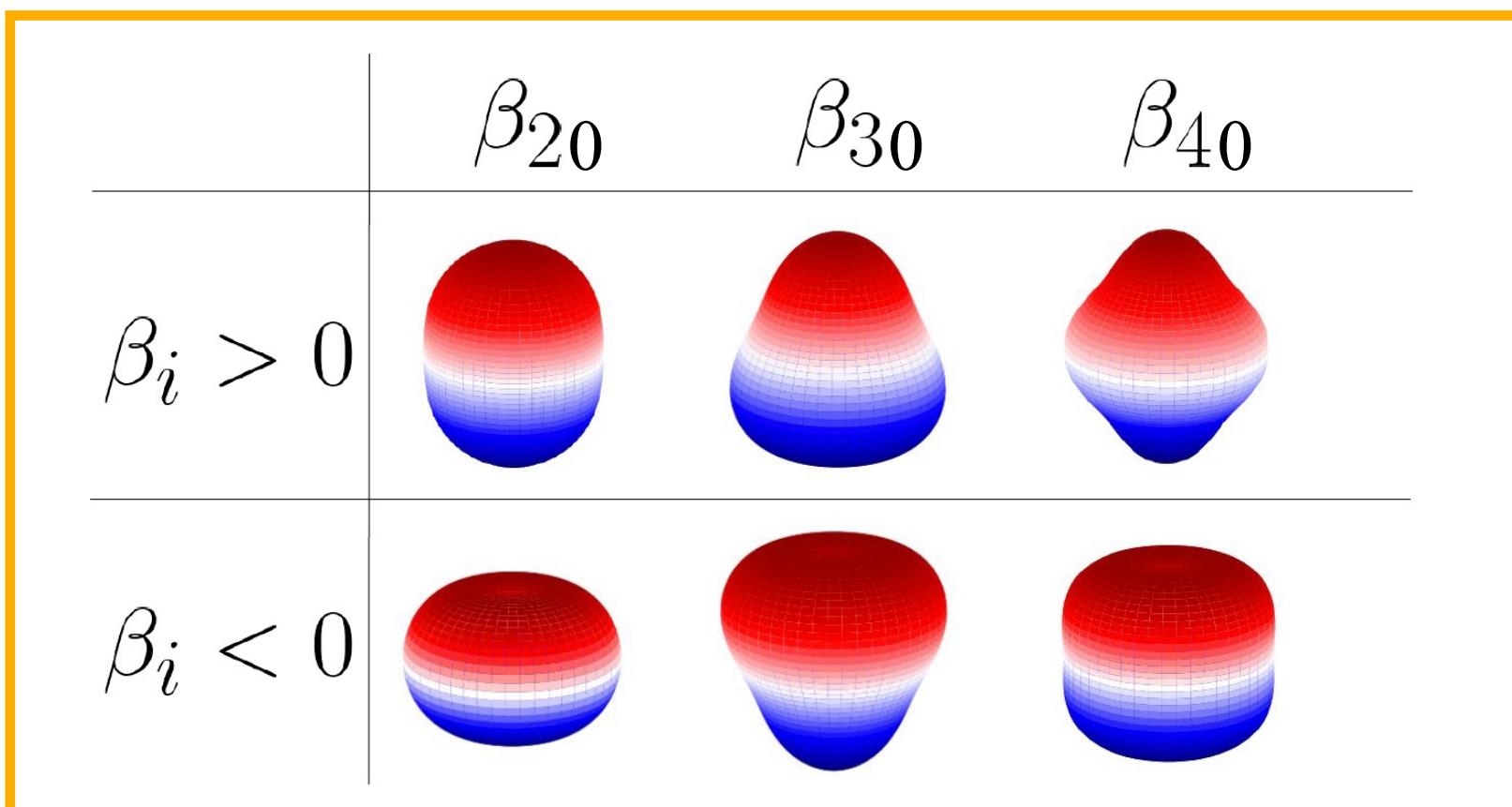
Theoretical framework

Single alpha decay

Points along
dynamical path

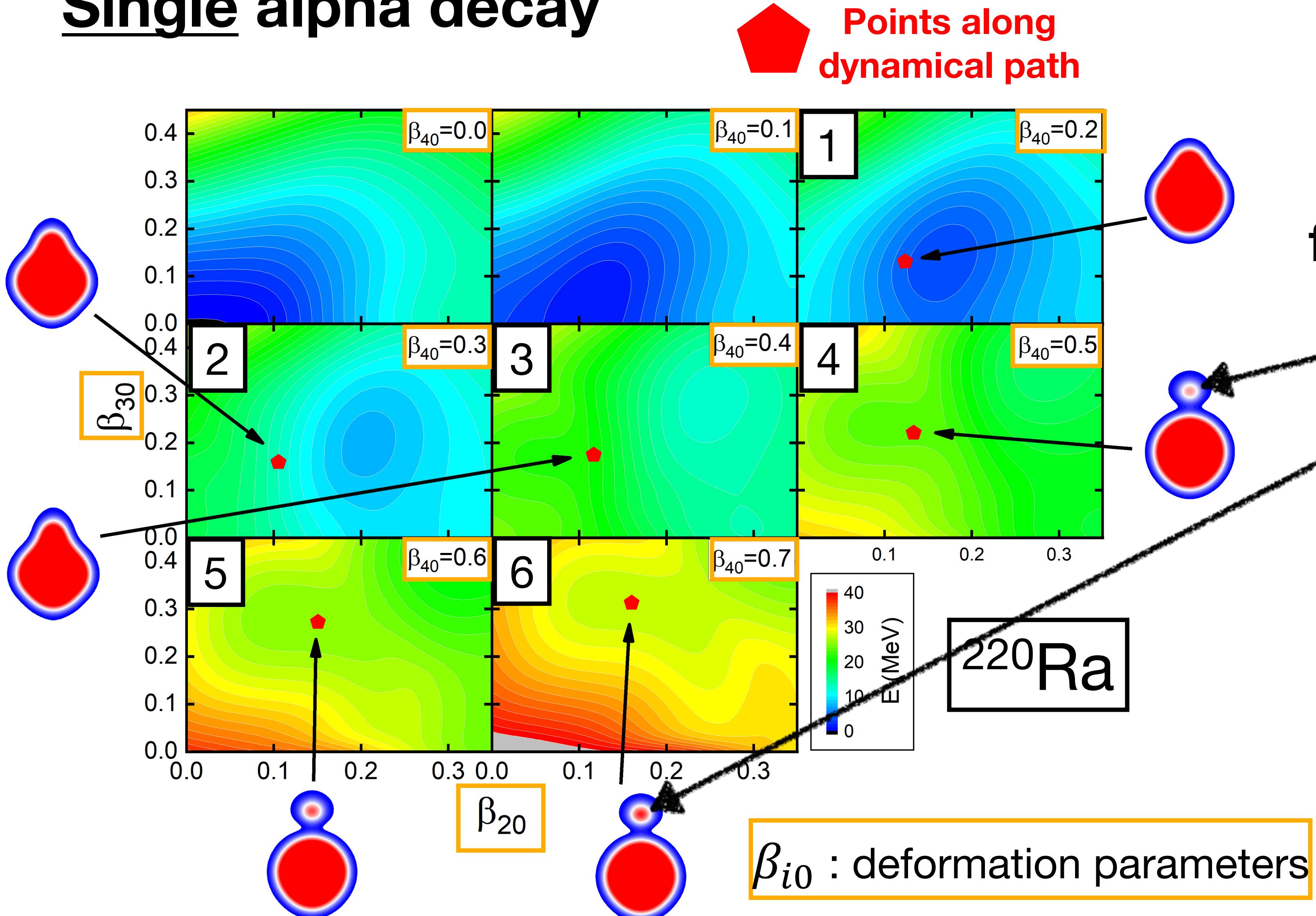


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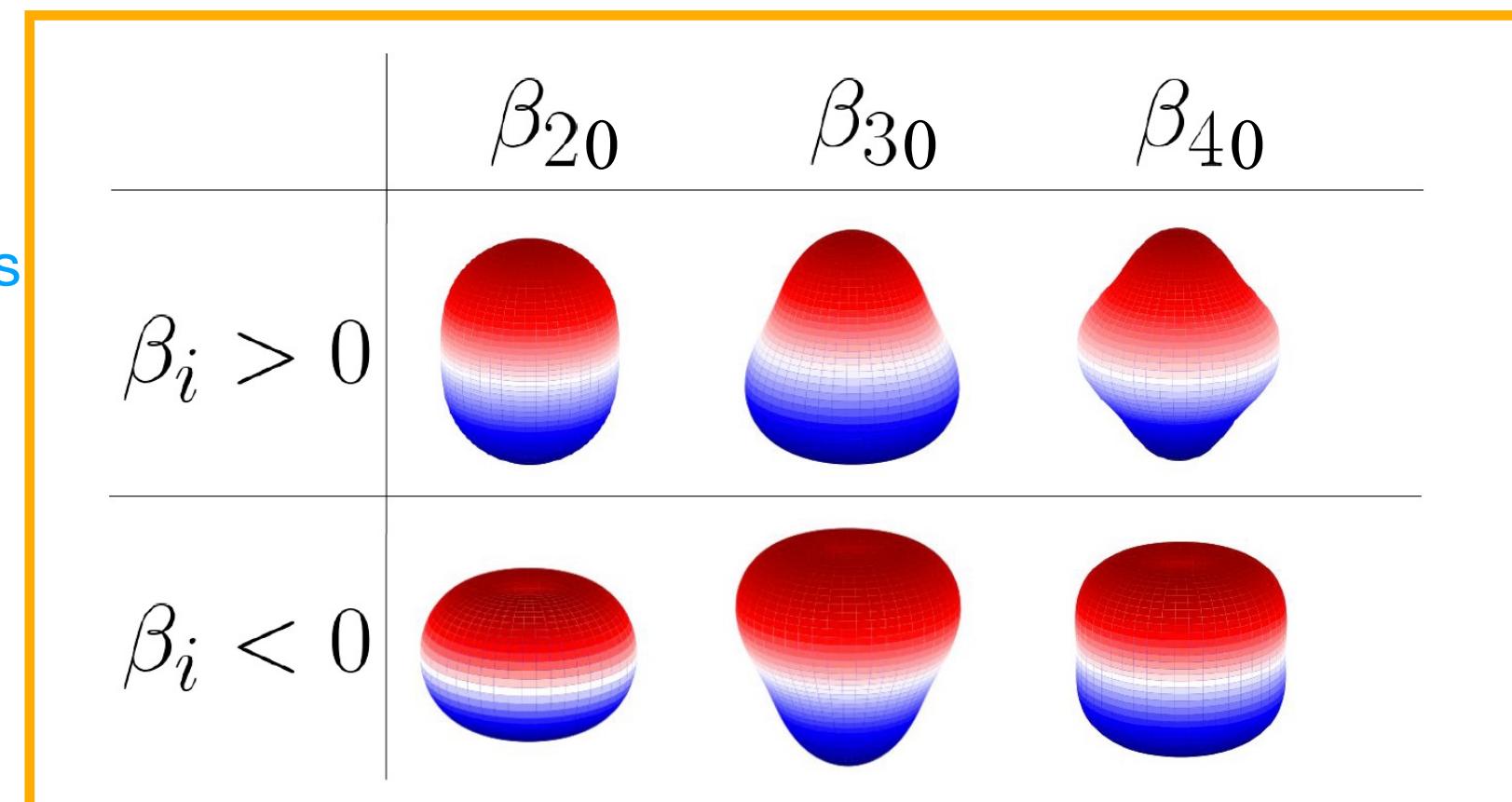


Theoretical framework

Single alpha decay



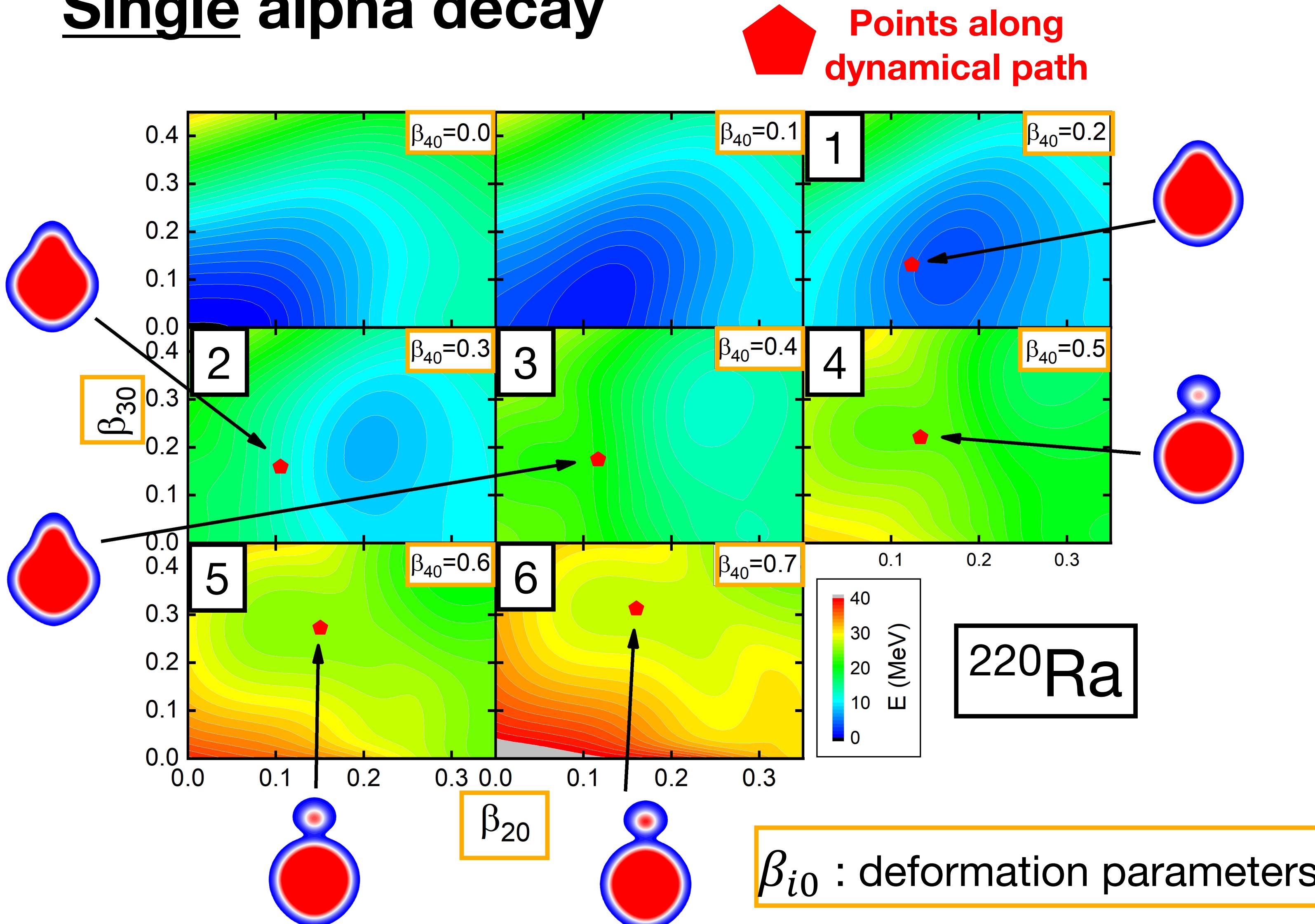
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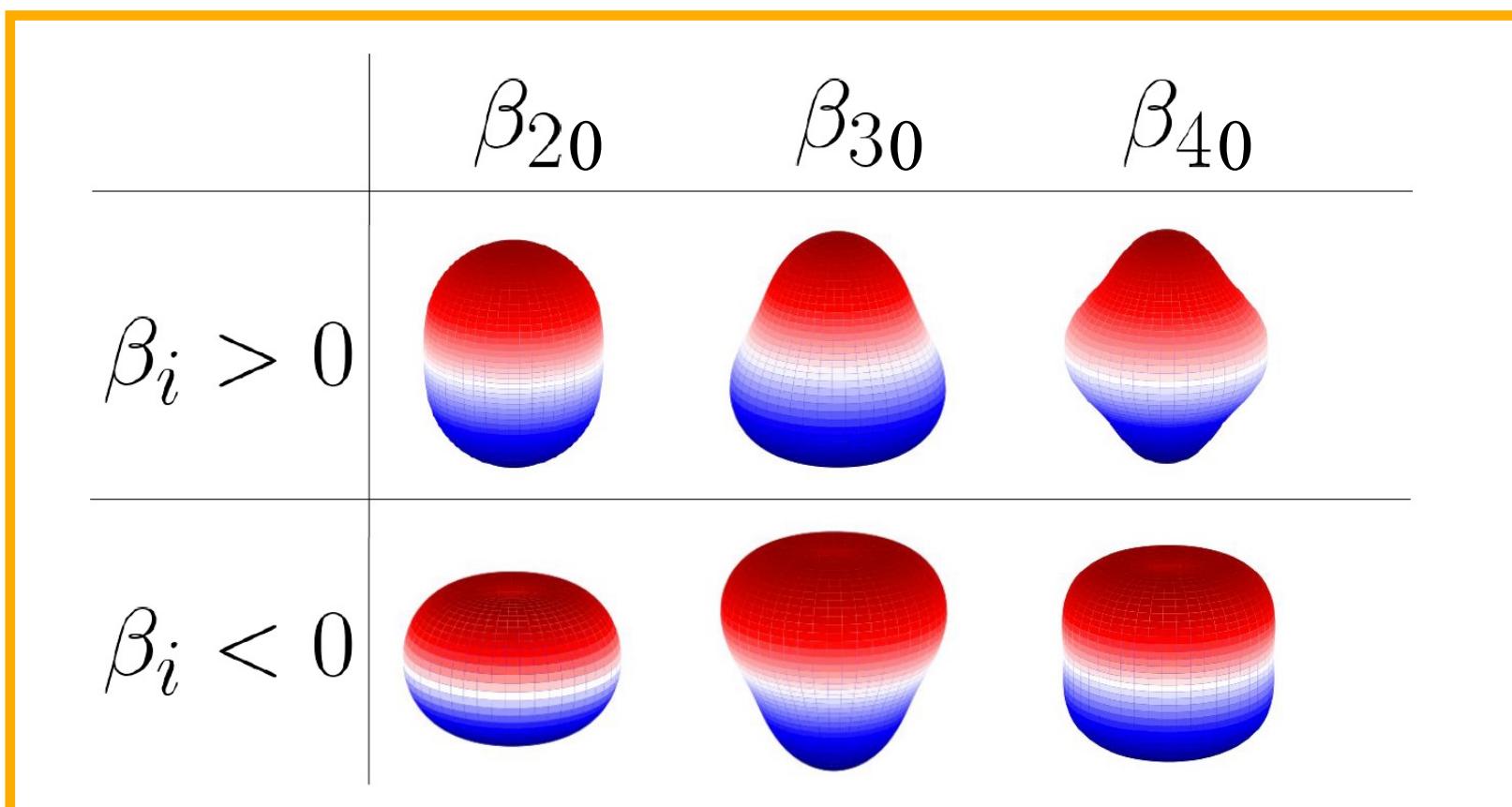
Dynamical evolution:
formation of an α particle

Theoretical framework

Single alpha decay



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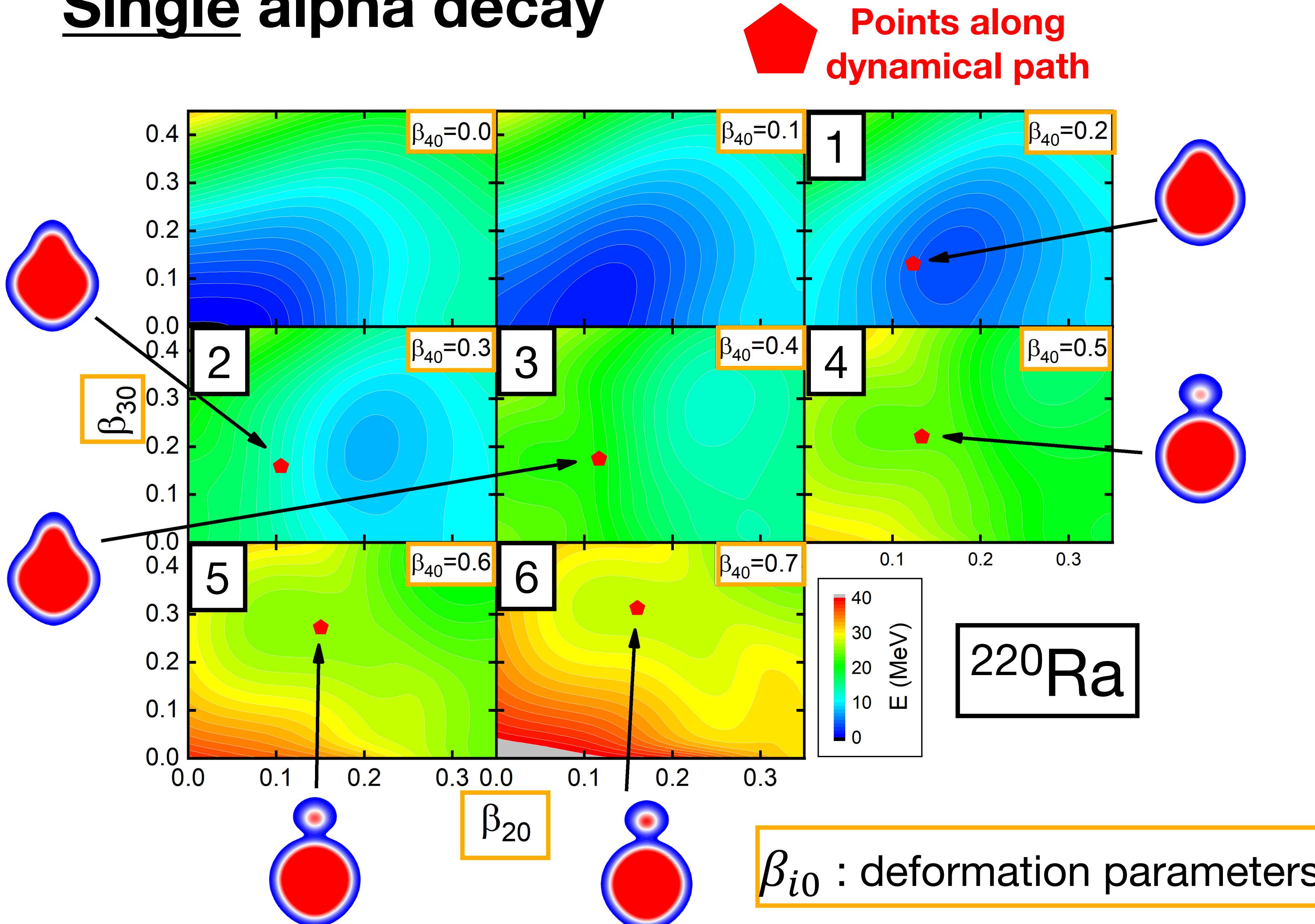
Dynamical evolution:
formation of an α particle

$$\tau_{\text{exp}} = 18 \text{ ms}$$

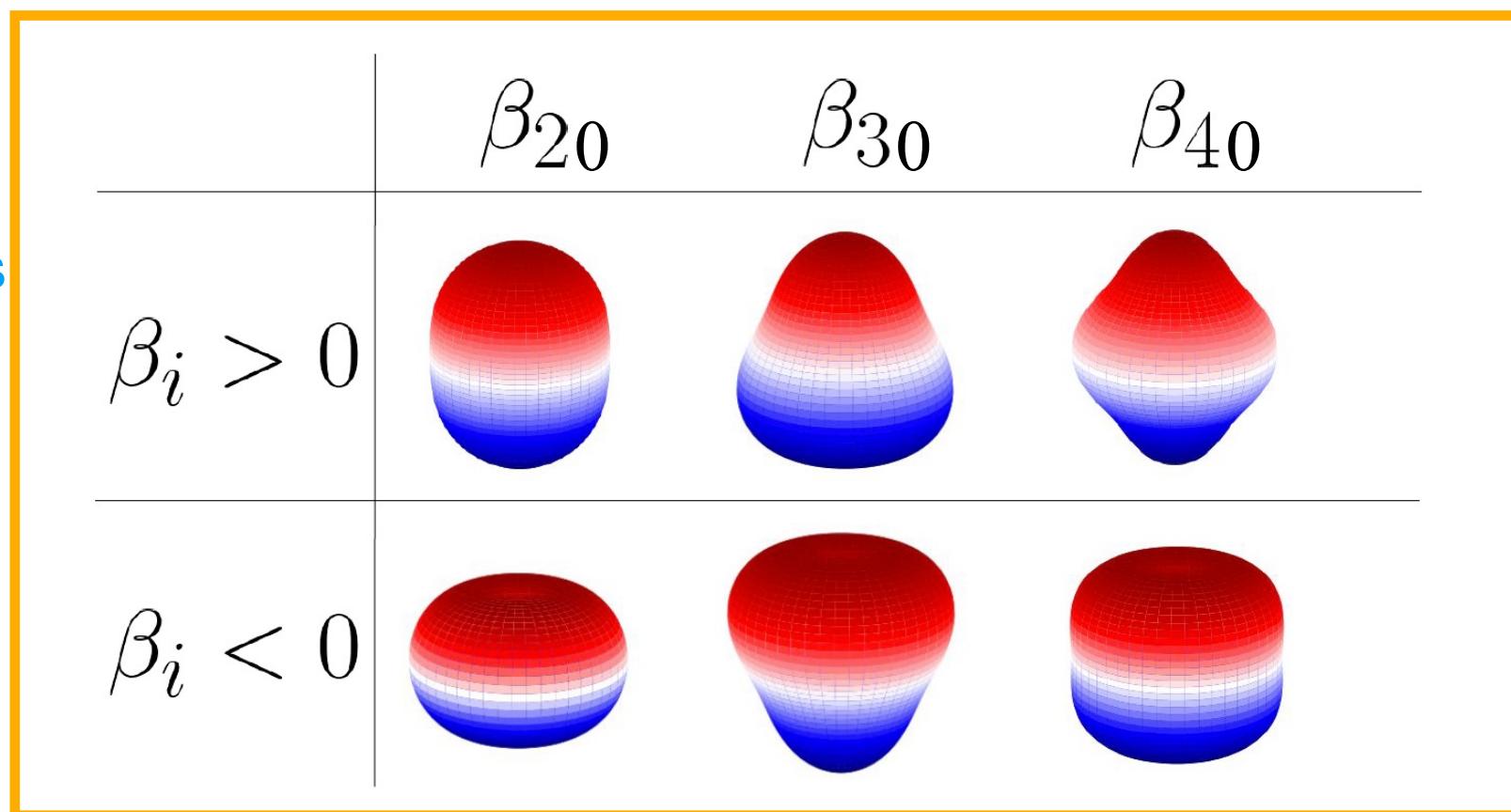
$$\tau_{\text{th}} = 60 \text{ ms}$$

Theoretical framework

Single alpha decay



Taken from
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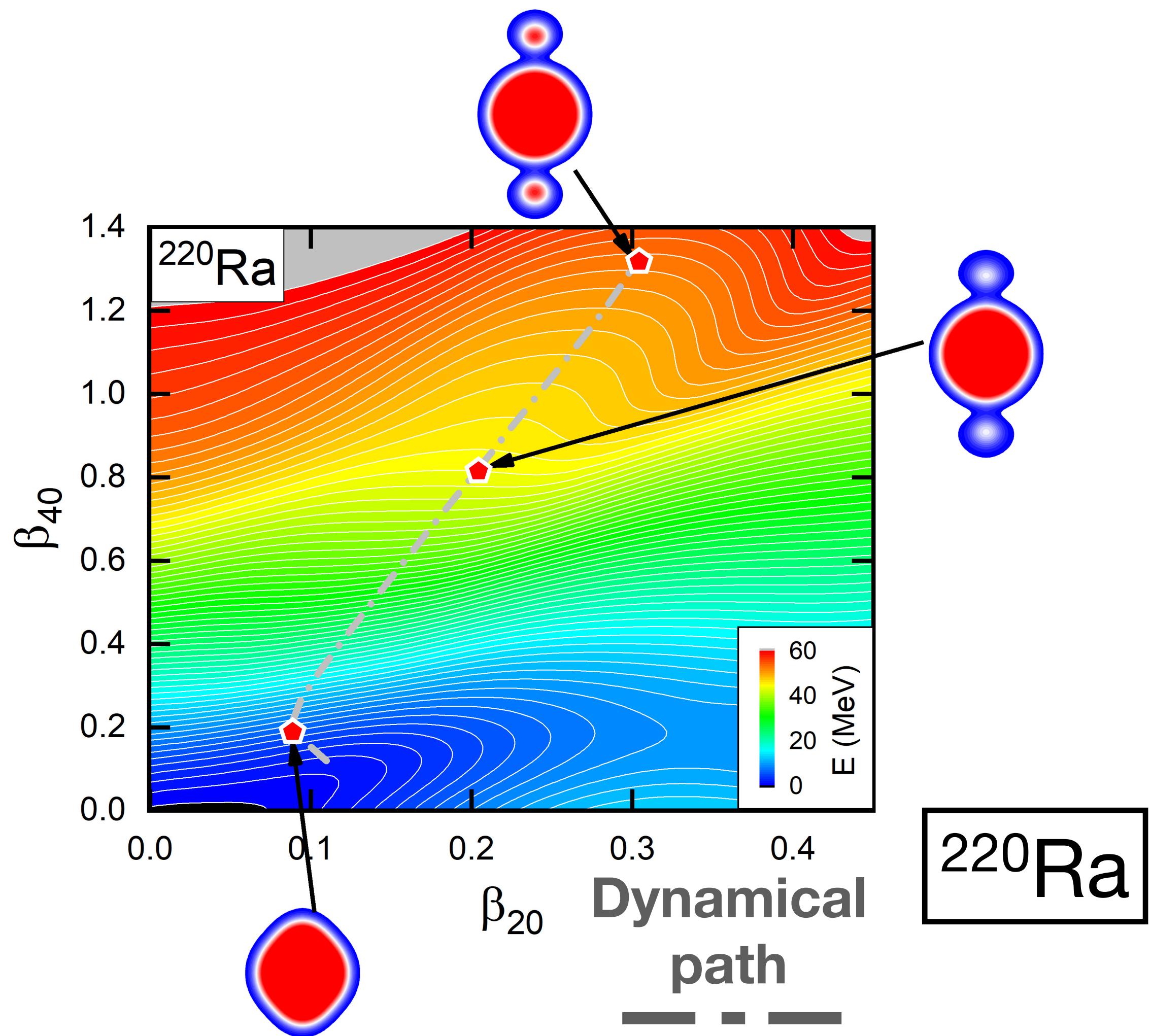
$$\tau_{\text{exp}} = 18 \text{ ms}$$

$$\tau_{\text{th}} = 60 \text{ ms}$$

Quantity computed : $\log \tau$
 → Very good agreement !

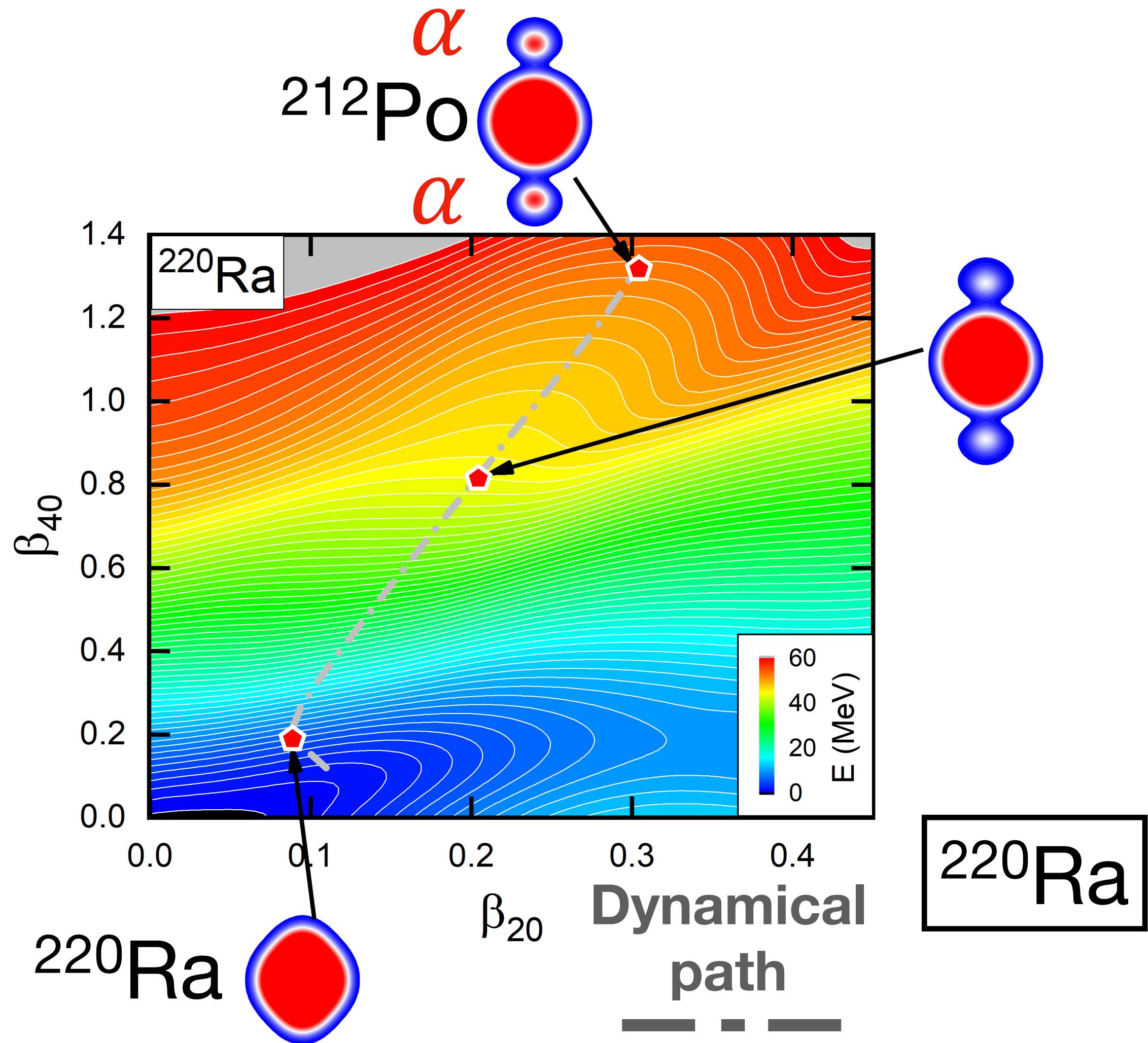
Theoretical framework

Double alpha decay



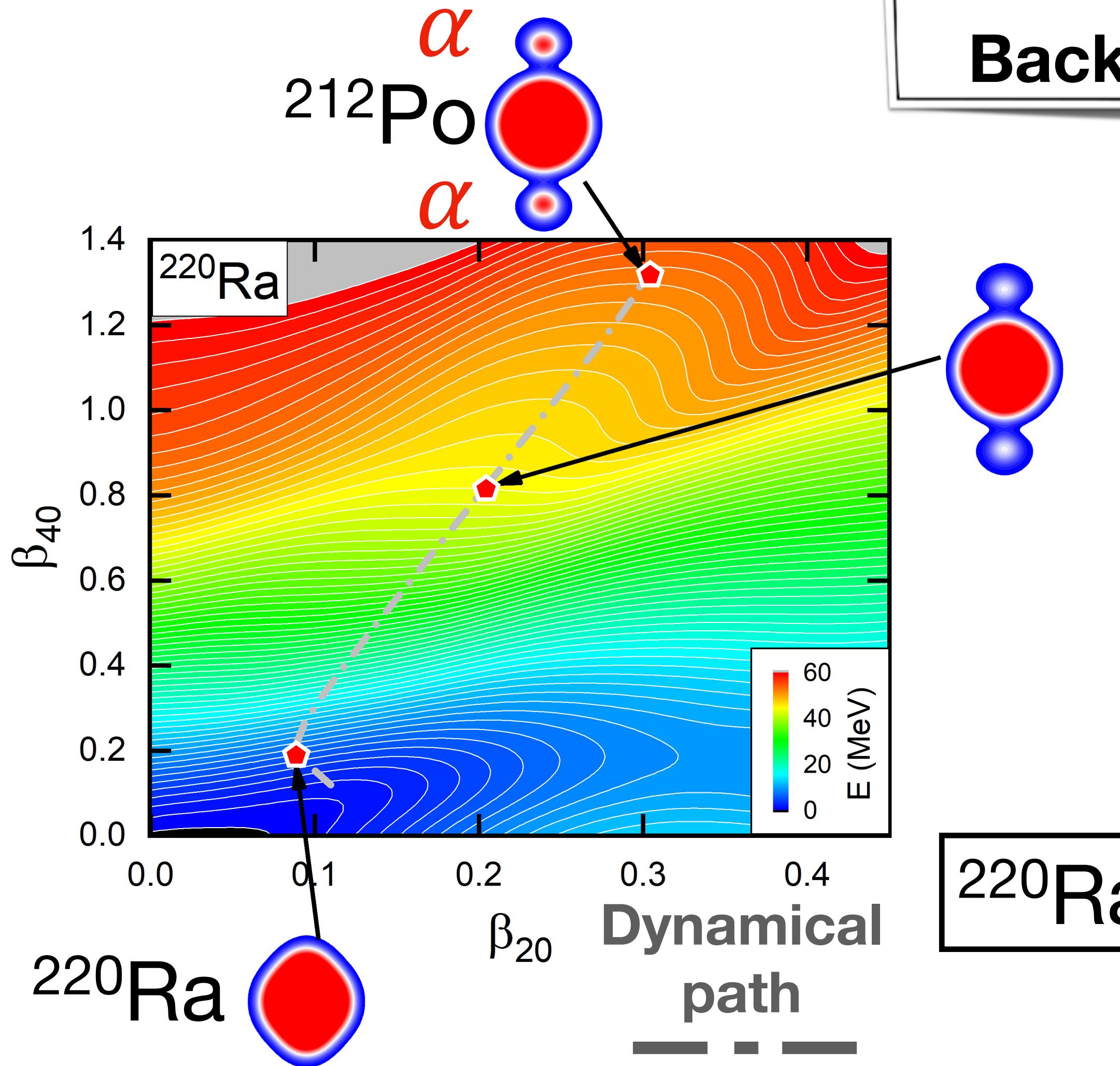
Theoretical framework

Double alpha decay



Theoretical framework

Double alpha decay

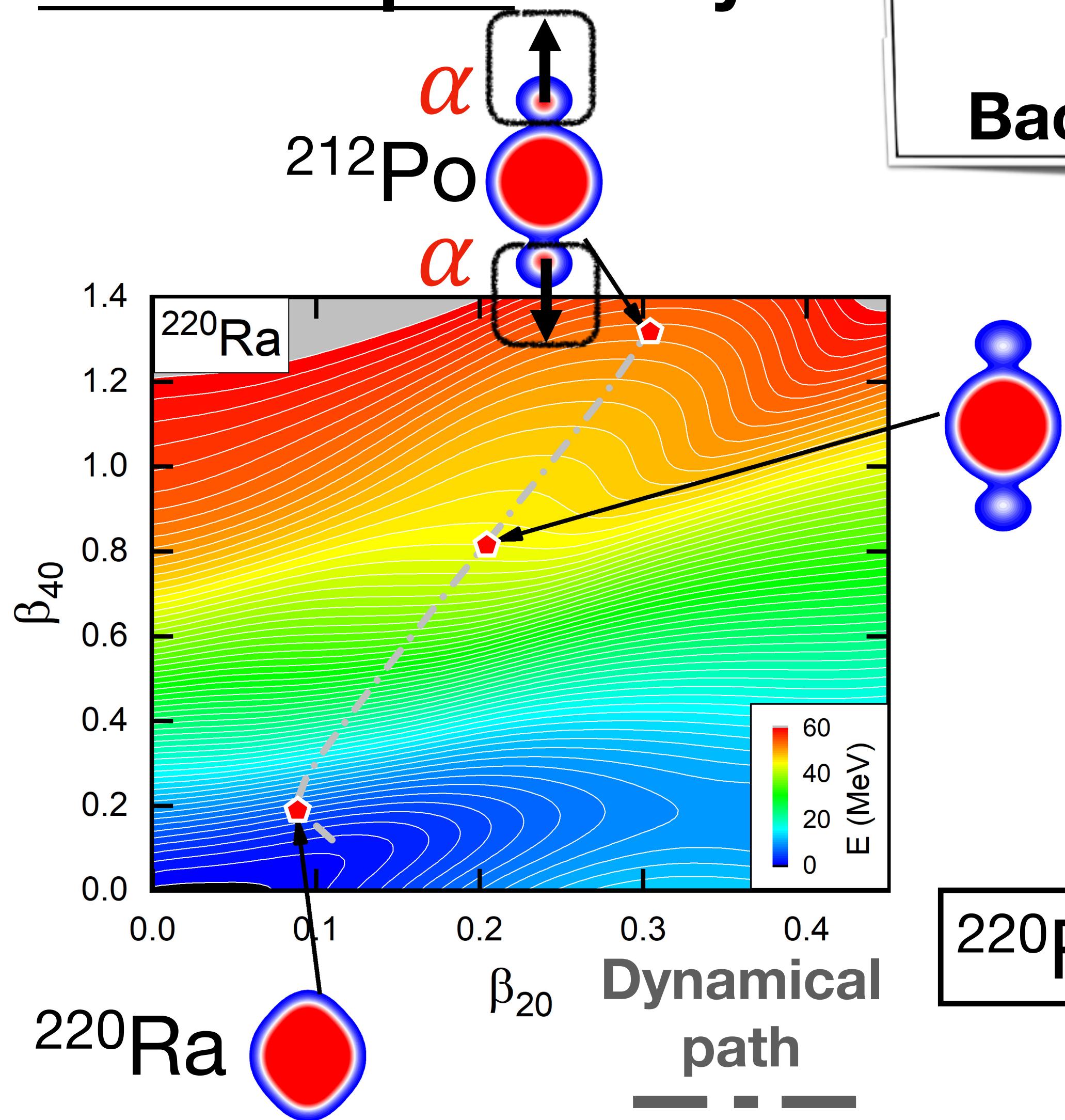


New type of radioactivity :
Back-to-back double alpha decay !

^{220}Ra

Theoretical framework

Double alpha decay

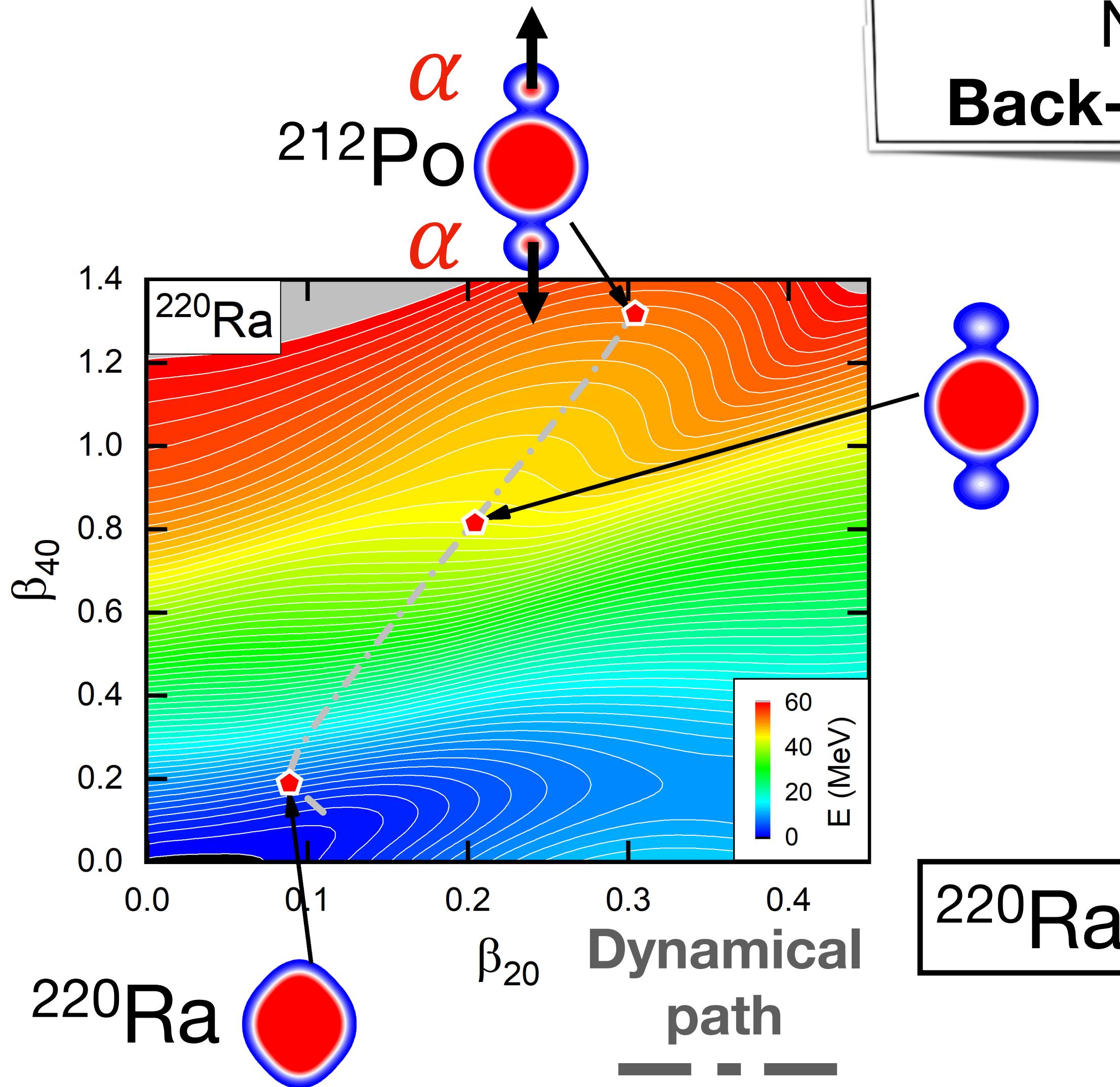


New type of radioactivity :
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Back-to-back emission of 2 α particles

Theoretical framework

Double alpha decay



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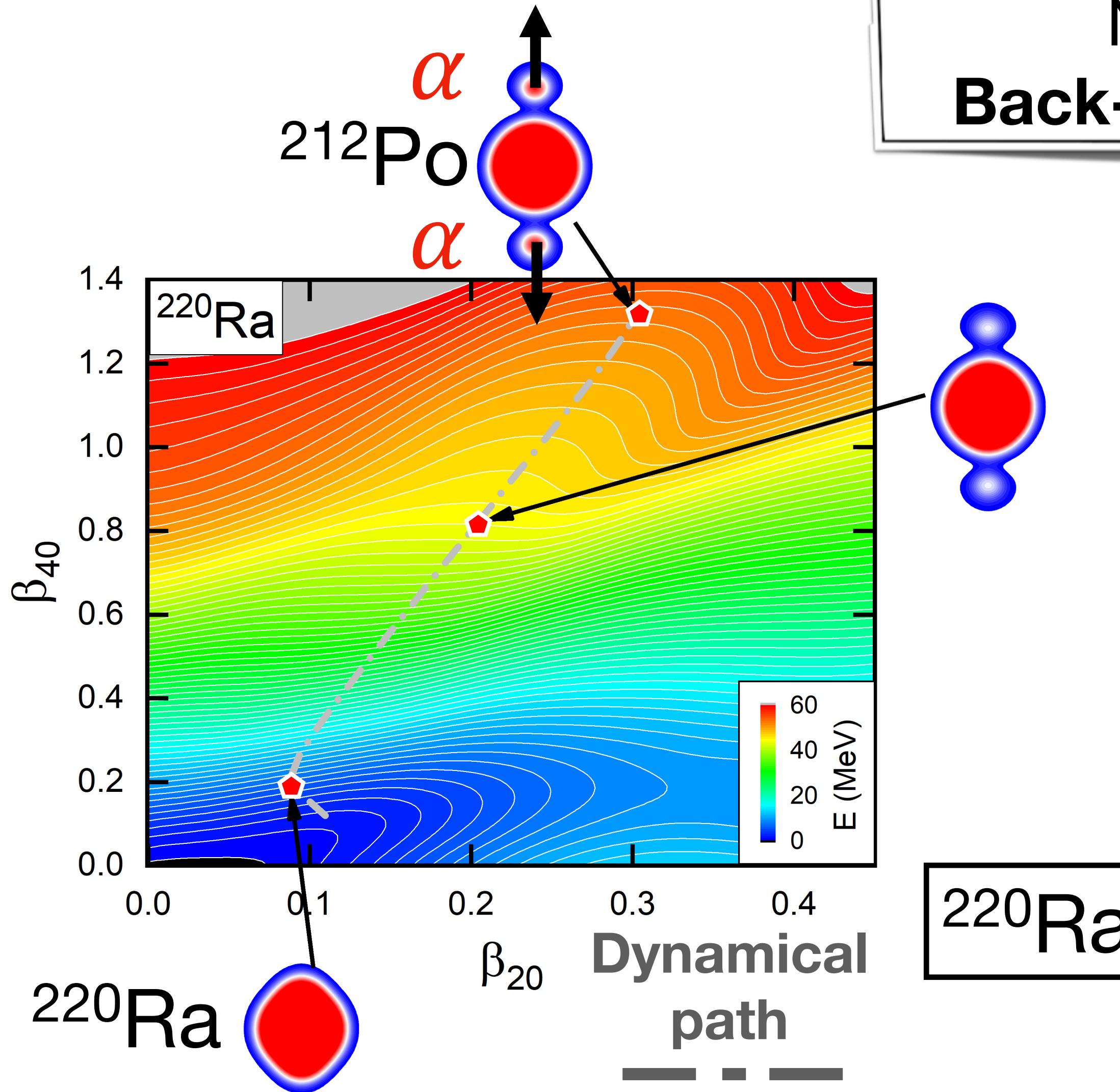
$$\log_{10} \tau_{\text{th}} [\text{s}] = 6.1$$

$$\log_{10} \tau_{\text{exp}} [\text{s}] = ??$$

^{220}Ra

Theoretical framework

Double alpha decay



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Back-to-back emission of 2 α particles

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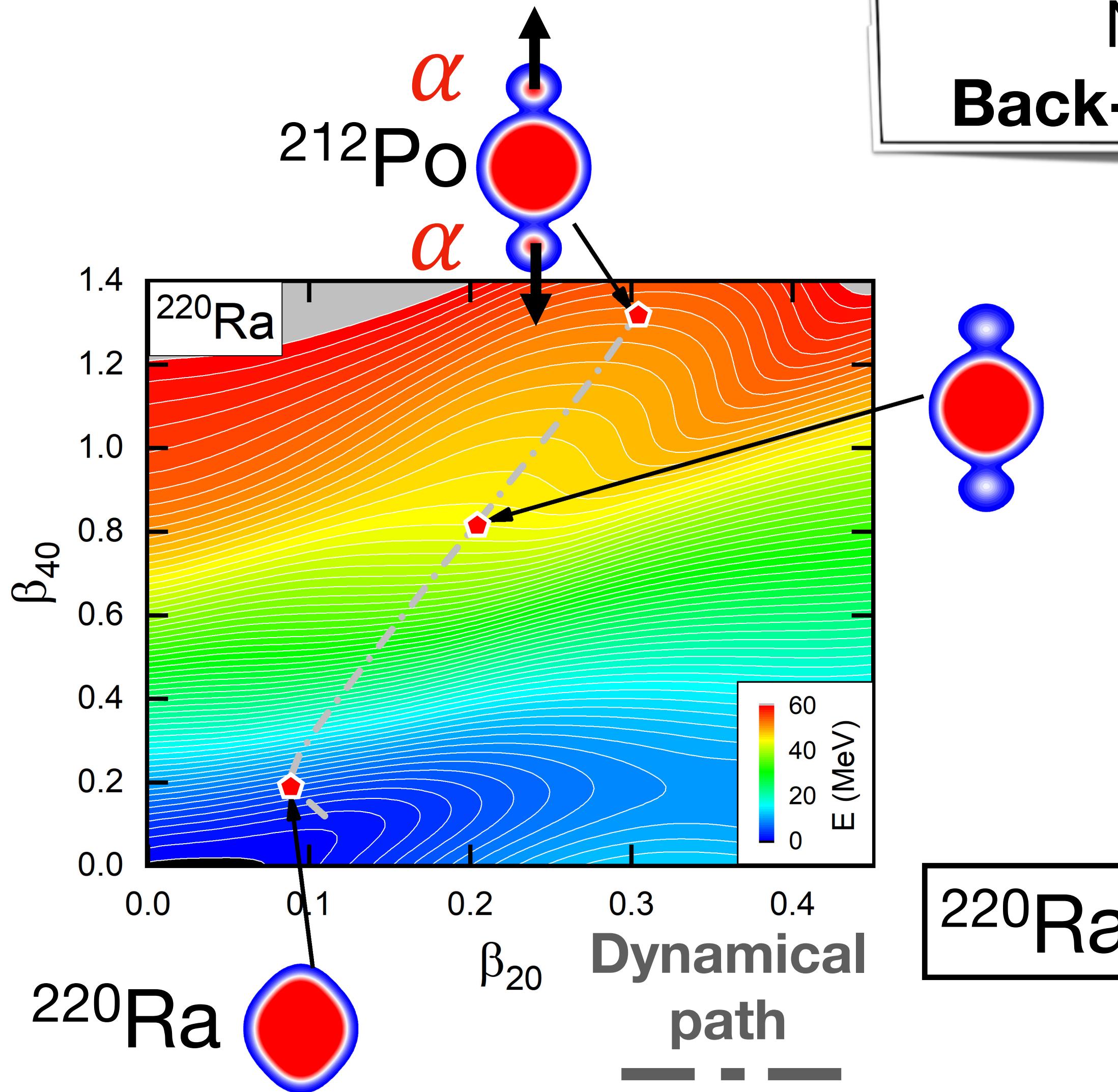
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Branching Ratio (BR) :

$$\text{BR} = \frac{\tau_{2\alpha}}{\tau_\alpha} \sim 10^{-7.3}$$

Theoretical framework

Double alpha decay



$\text{BR}_{\text{cluster}} \sim 10^{-10}$
Already observed

New type of radioactivity :
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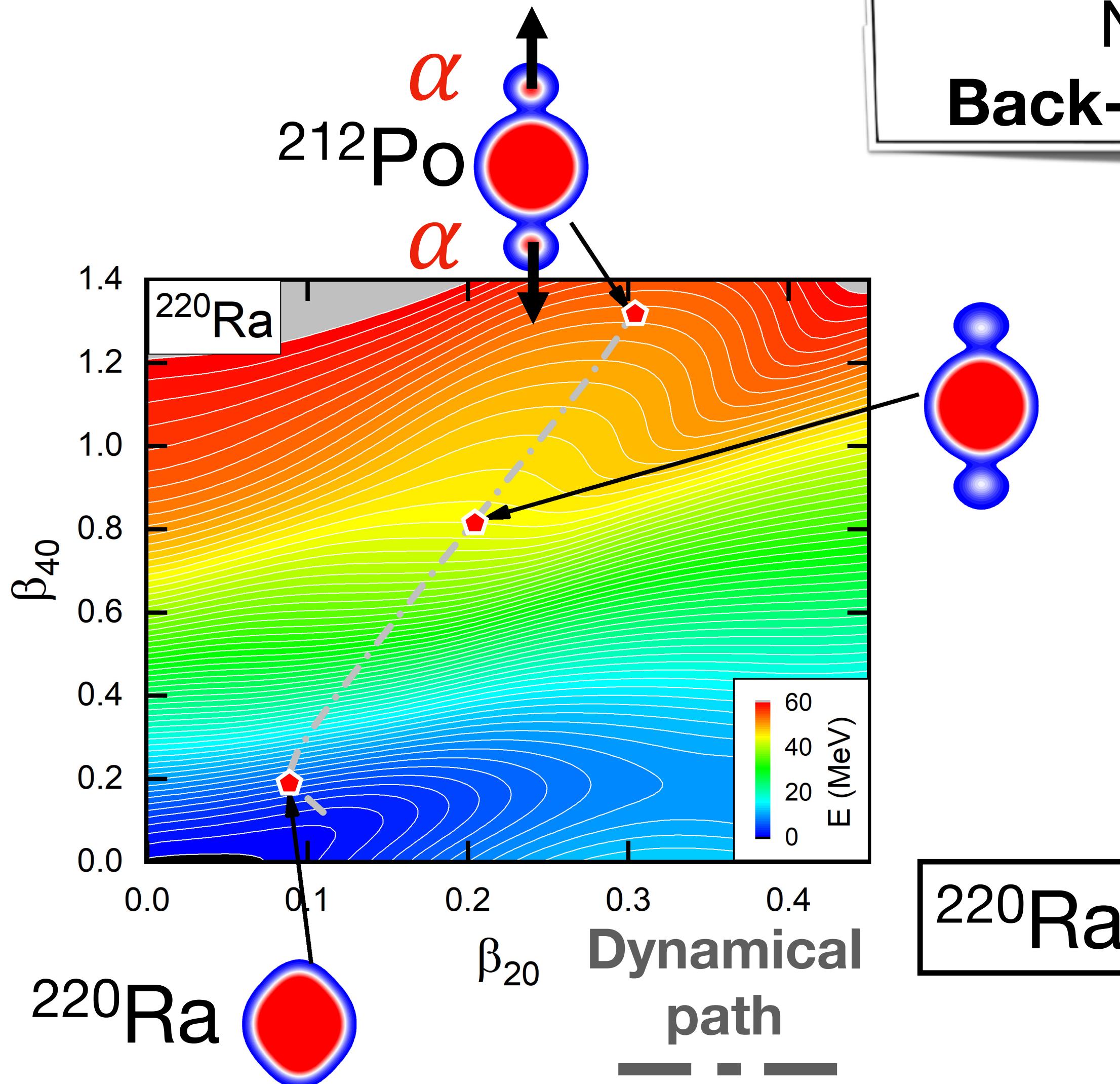
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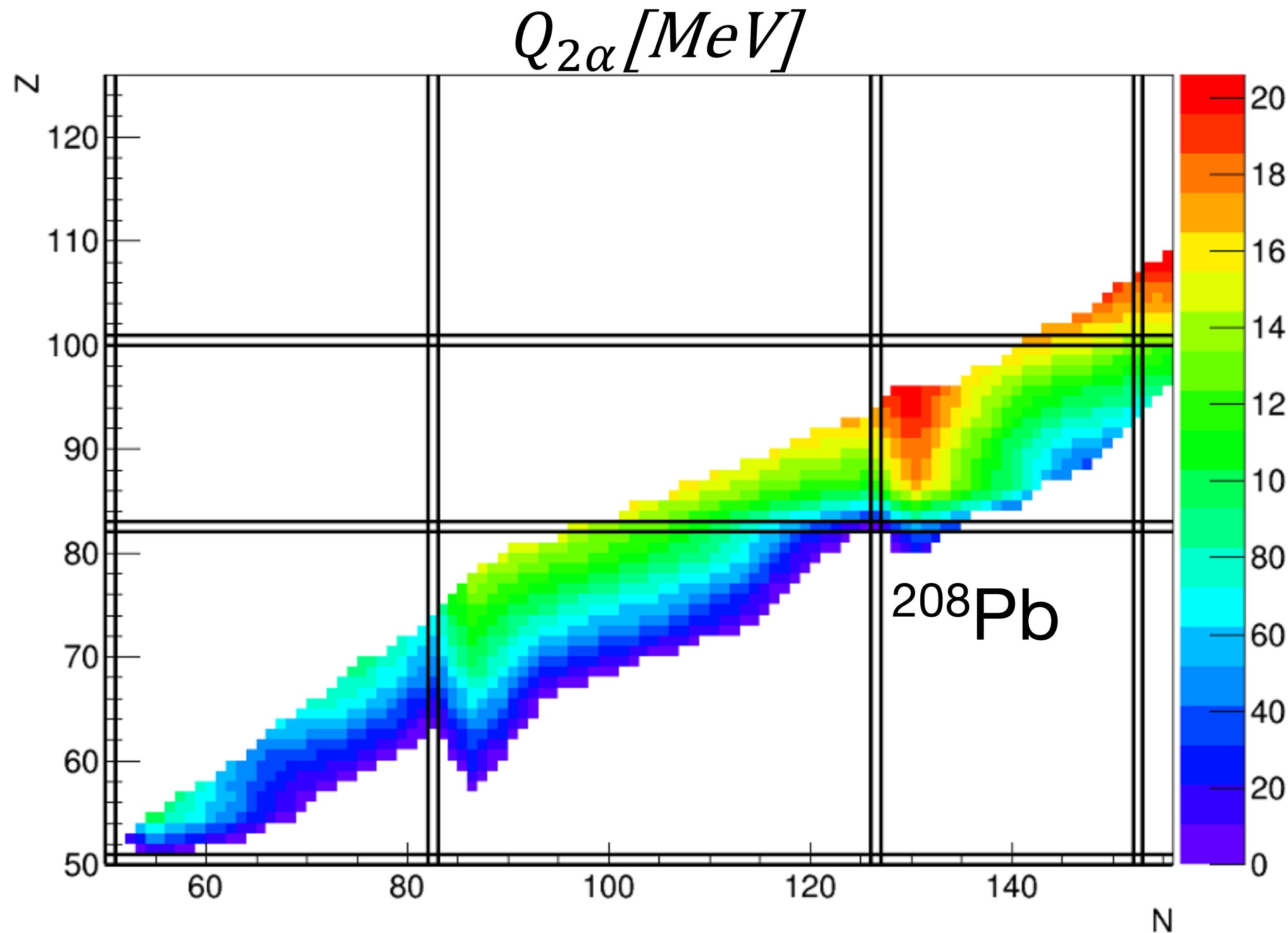
$$\text{BR} = \frac{\tau_{2\alpha}}{\tau_\alpha} \sim 10^{-7.3}$$

Experimentally
Interesting !

$\text{BR}_{\text{cluster}} \sim 10^{-10}$
Already observed

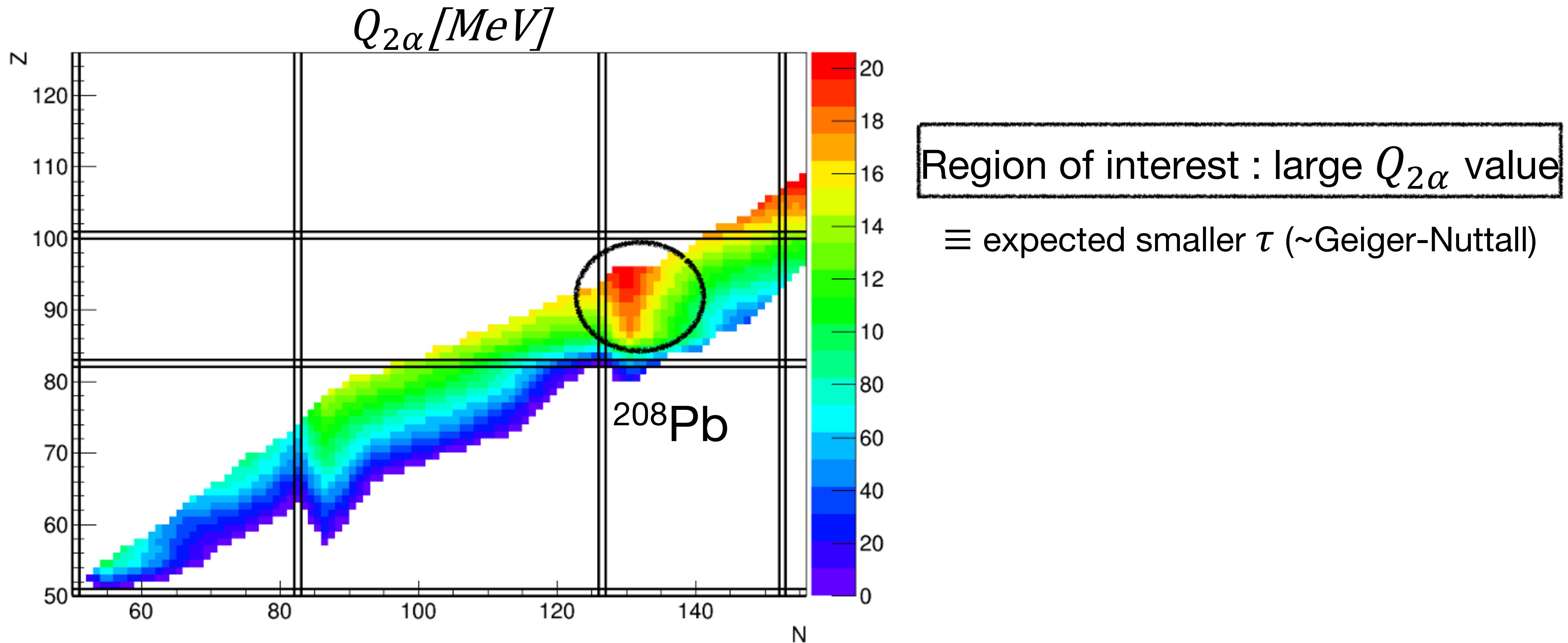
Theoretical framework

Double alpha candidates



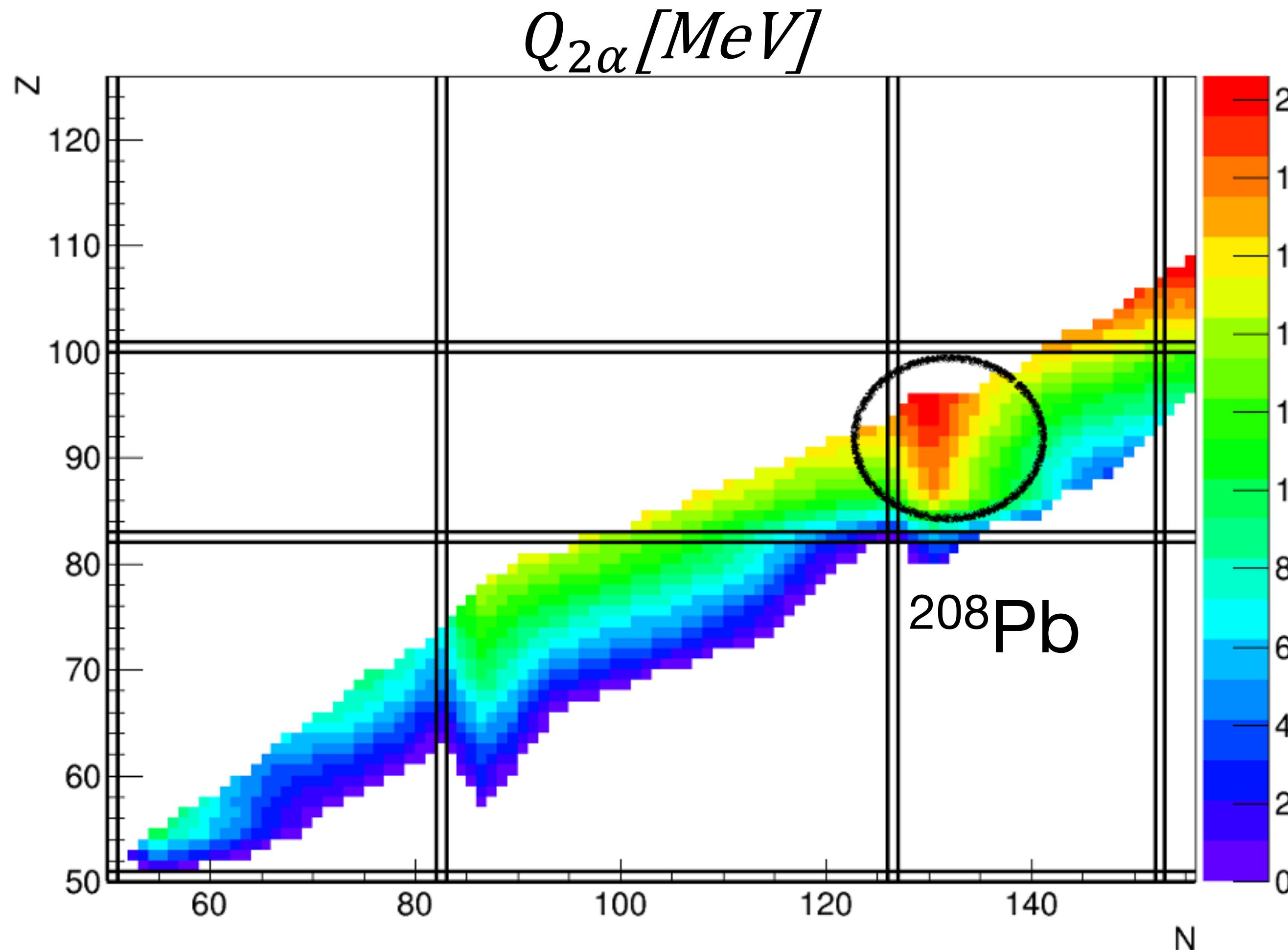
Theoretical framework

Double alpha candidates



Theoretical framework

Double alpha candidates



Region of interest : large $Q_{2\alpha}$ value

≡ expected smaller τ (~Geiger-Nuttall)

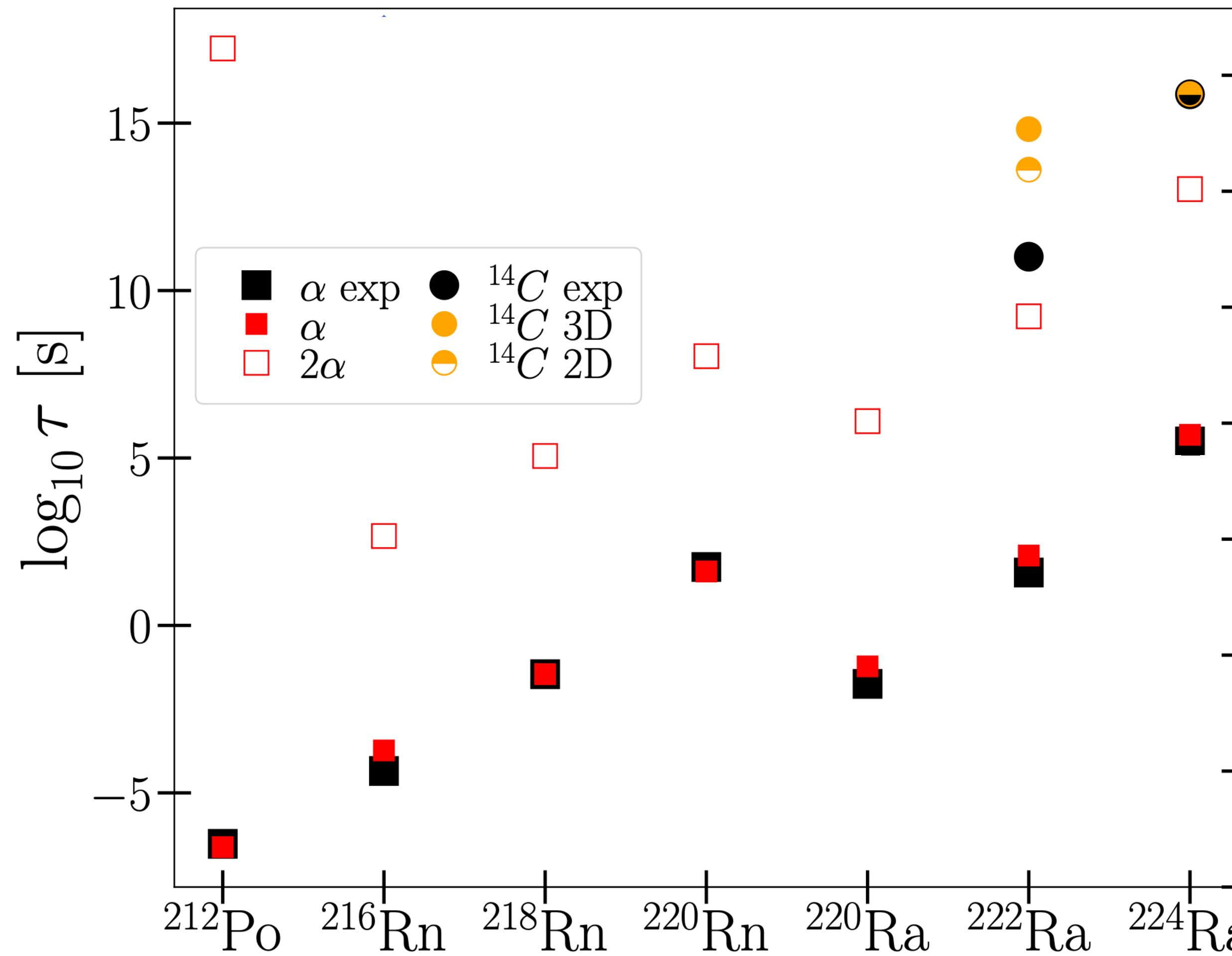


Other candidates :
 $^{218,220}\text{Rn}$ $^{220-224}\text{Ra}$

Theoretical framework

Summary

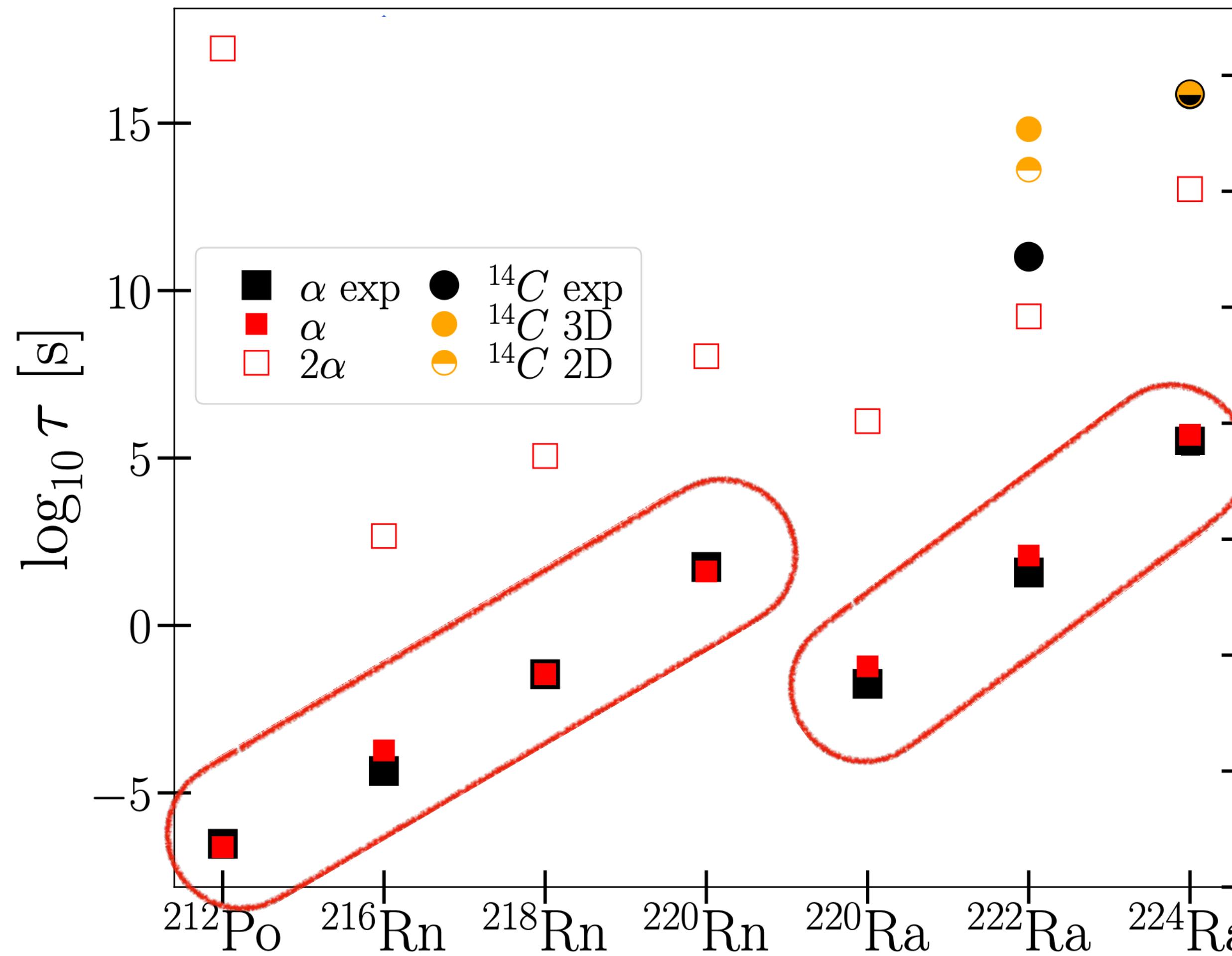
Black = exp Color = theory



Theoretical framework

Summary

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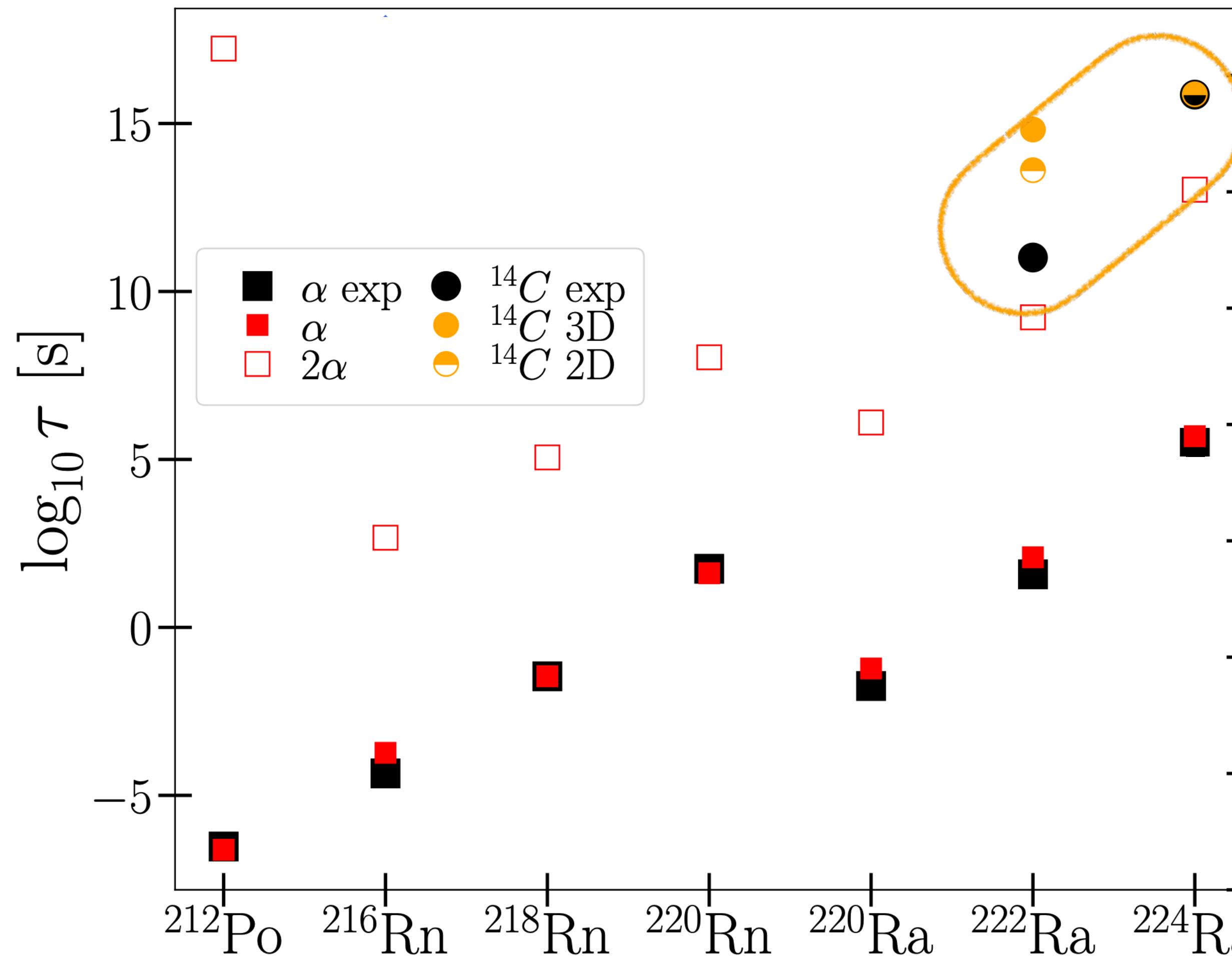


Single alpha : Excellent agreement

Theoretical framework

Summary

Black = exp **Color = theory**



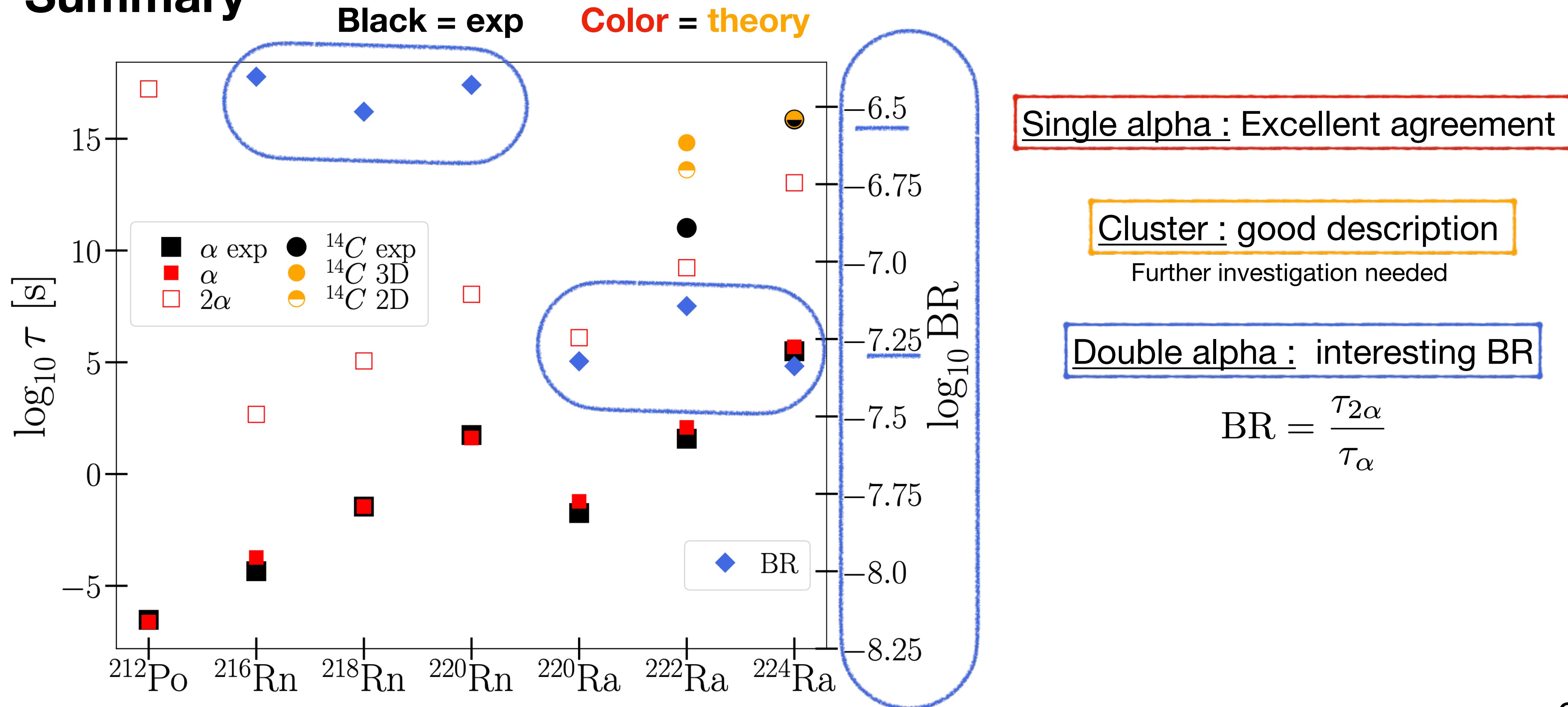
Single alpha : Excellent agreement

Cluster : good description

Further investigation needed

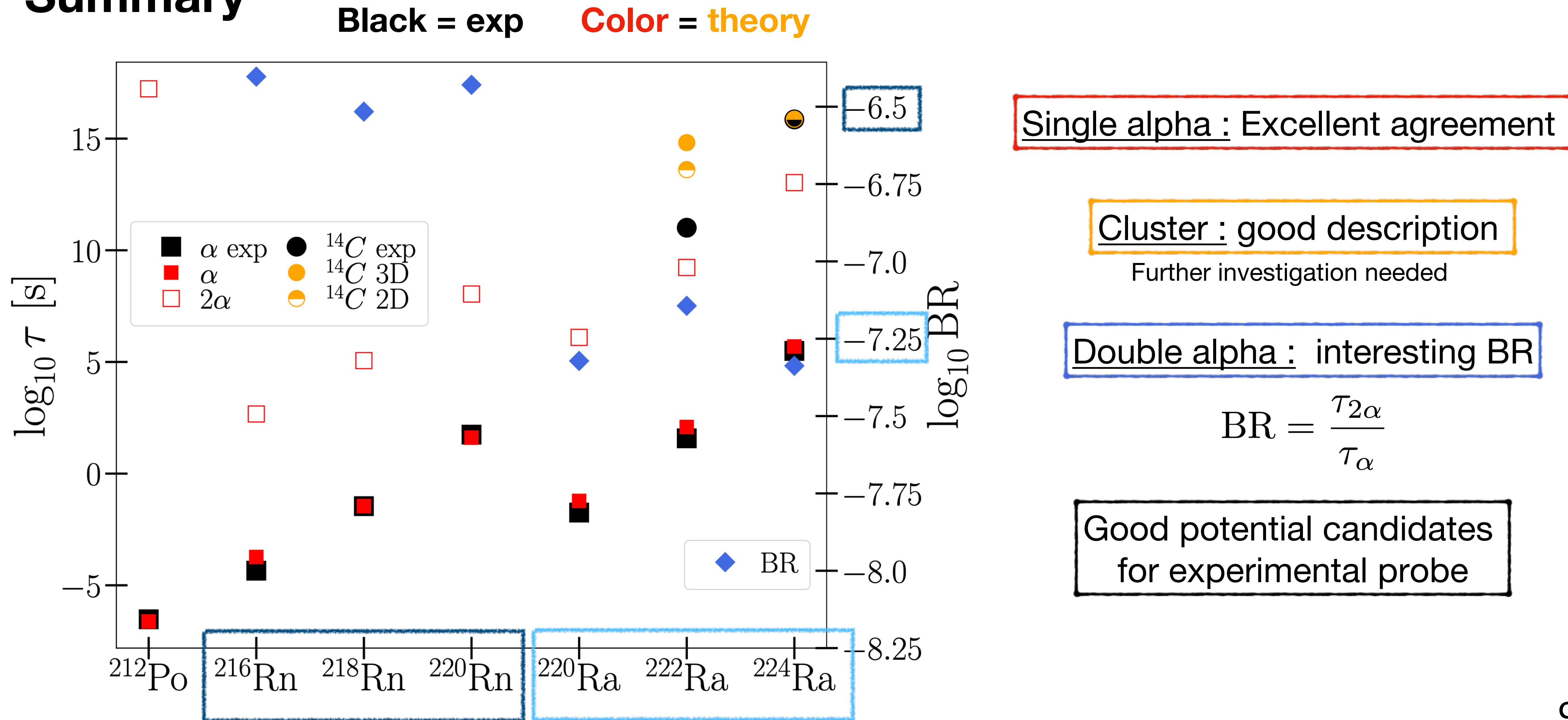
Theoretical framework

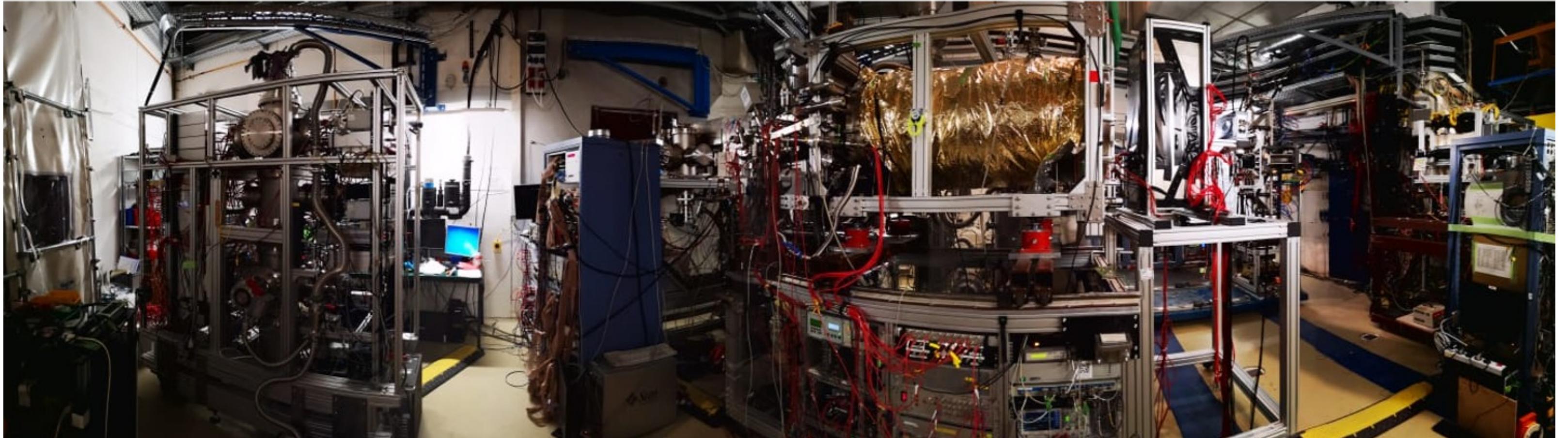
Summary



Theoretical framework

Summary





Experimental search for 2α FRS-Ion catcher GSI

H. Wilsenach courtesy

Theoretical
prediction



2021

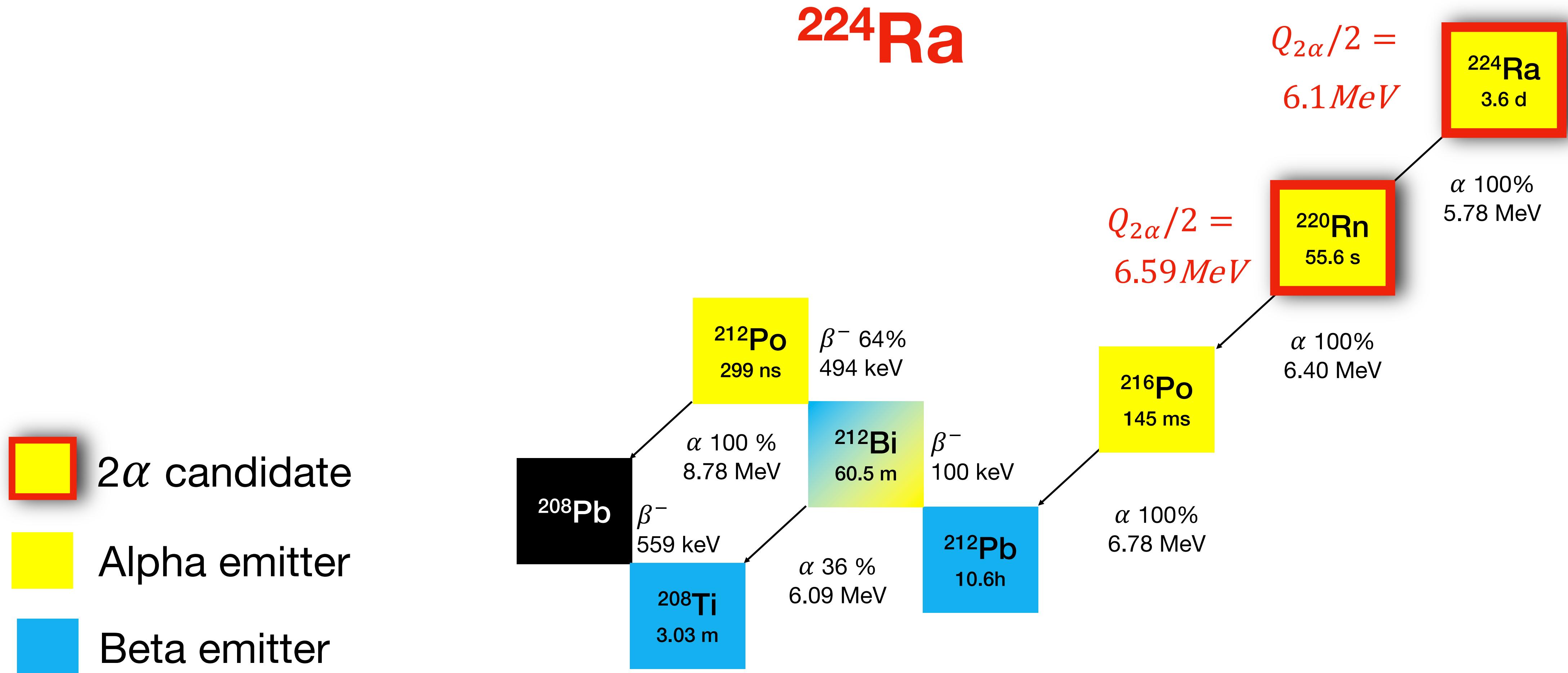
Run
@GSI



2022

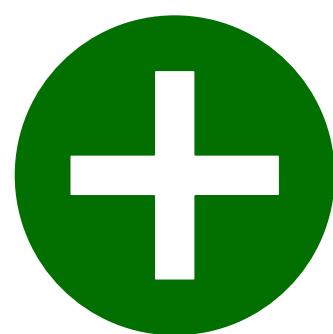
FRS Ion Catcher - GSI

Isotope choice - decay chain

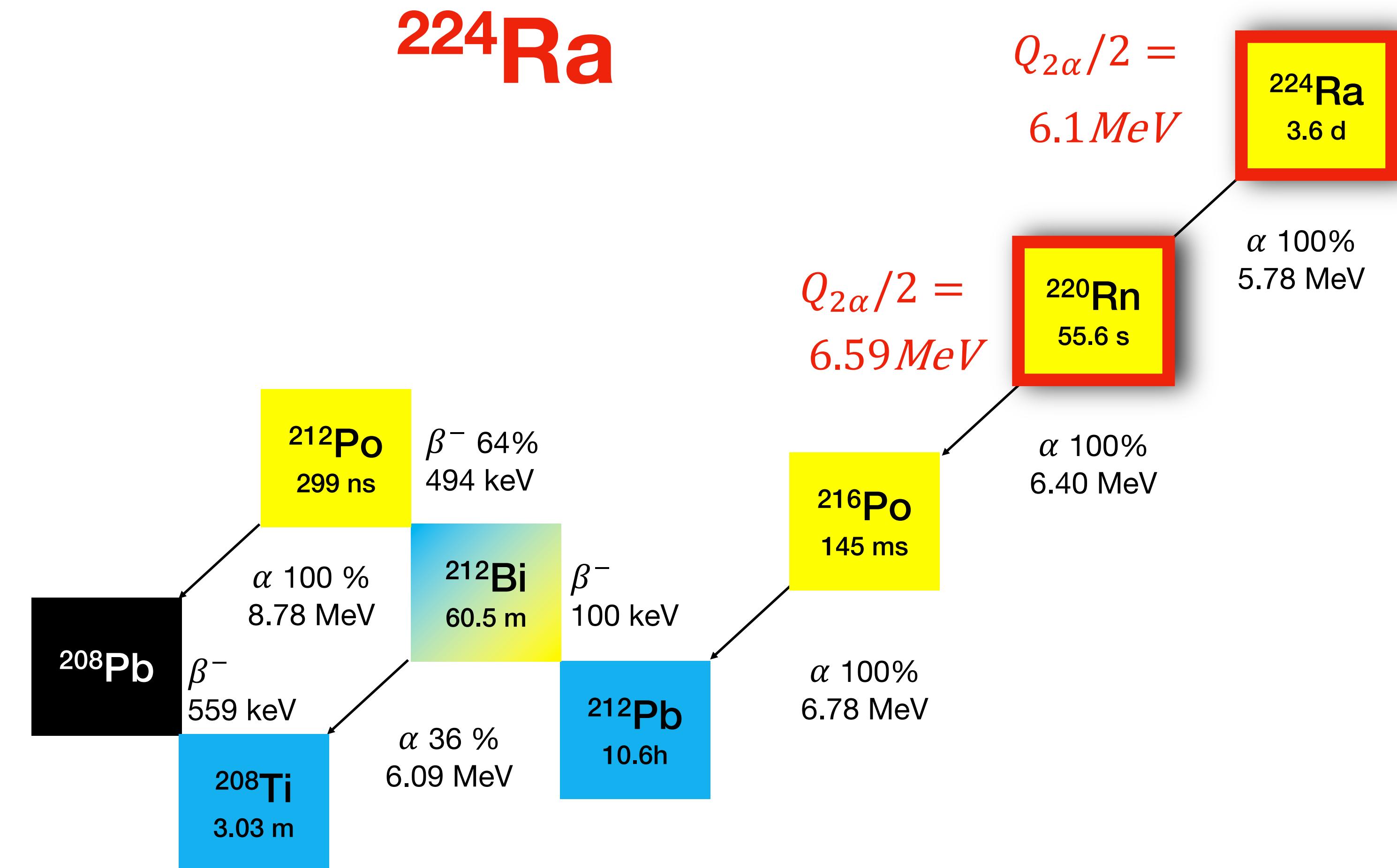


FRS Ion Catcher - GSI

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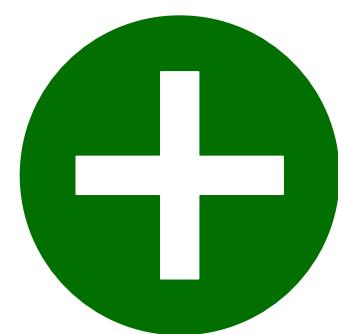


- 2α candidate
- Alpha emitter
- Beta emitter



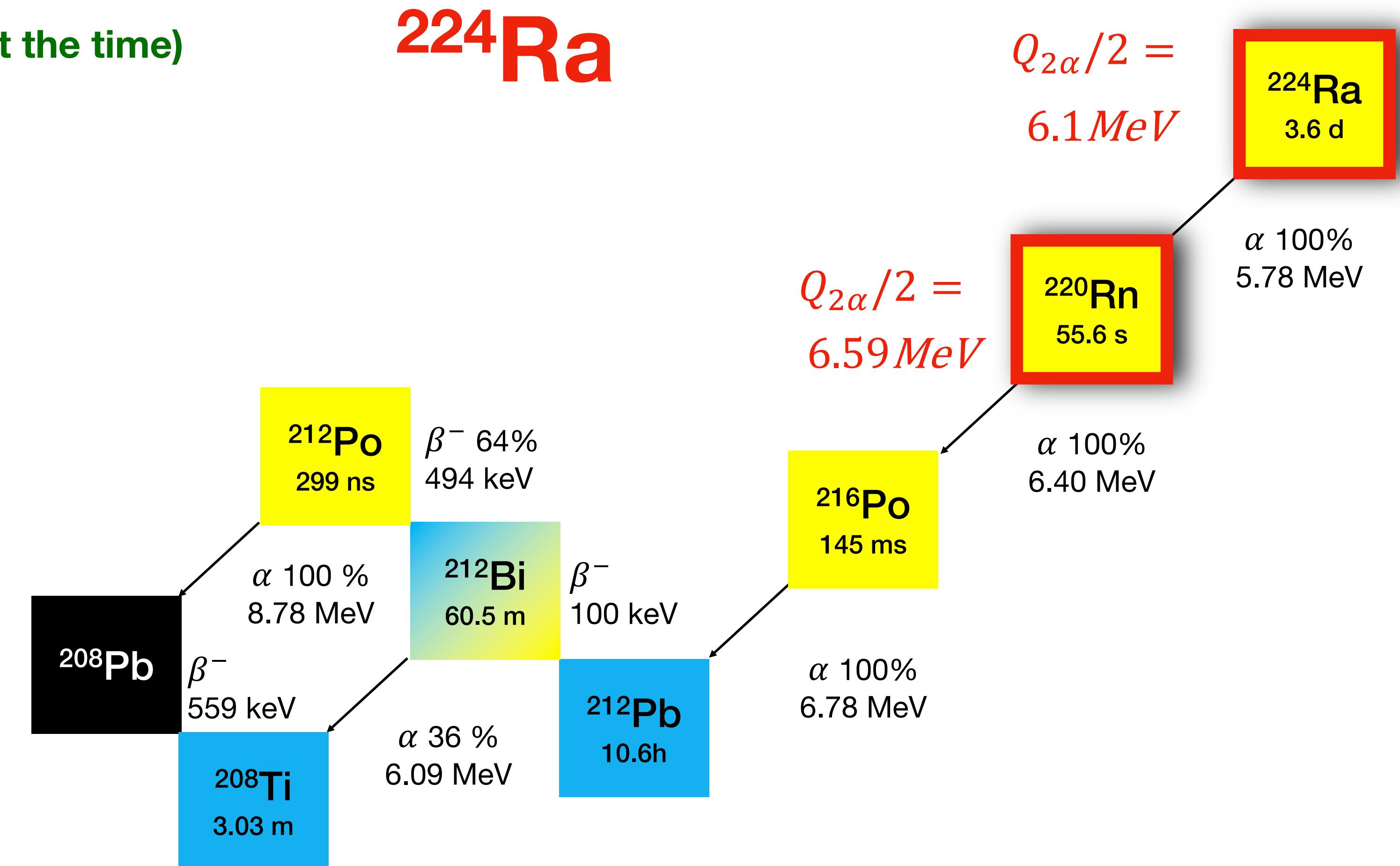
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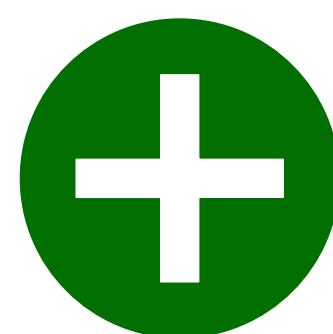
(Only theoretical candidate at the time)

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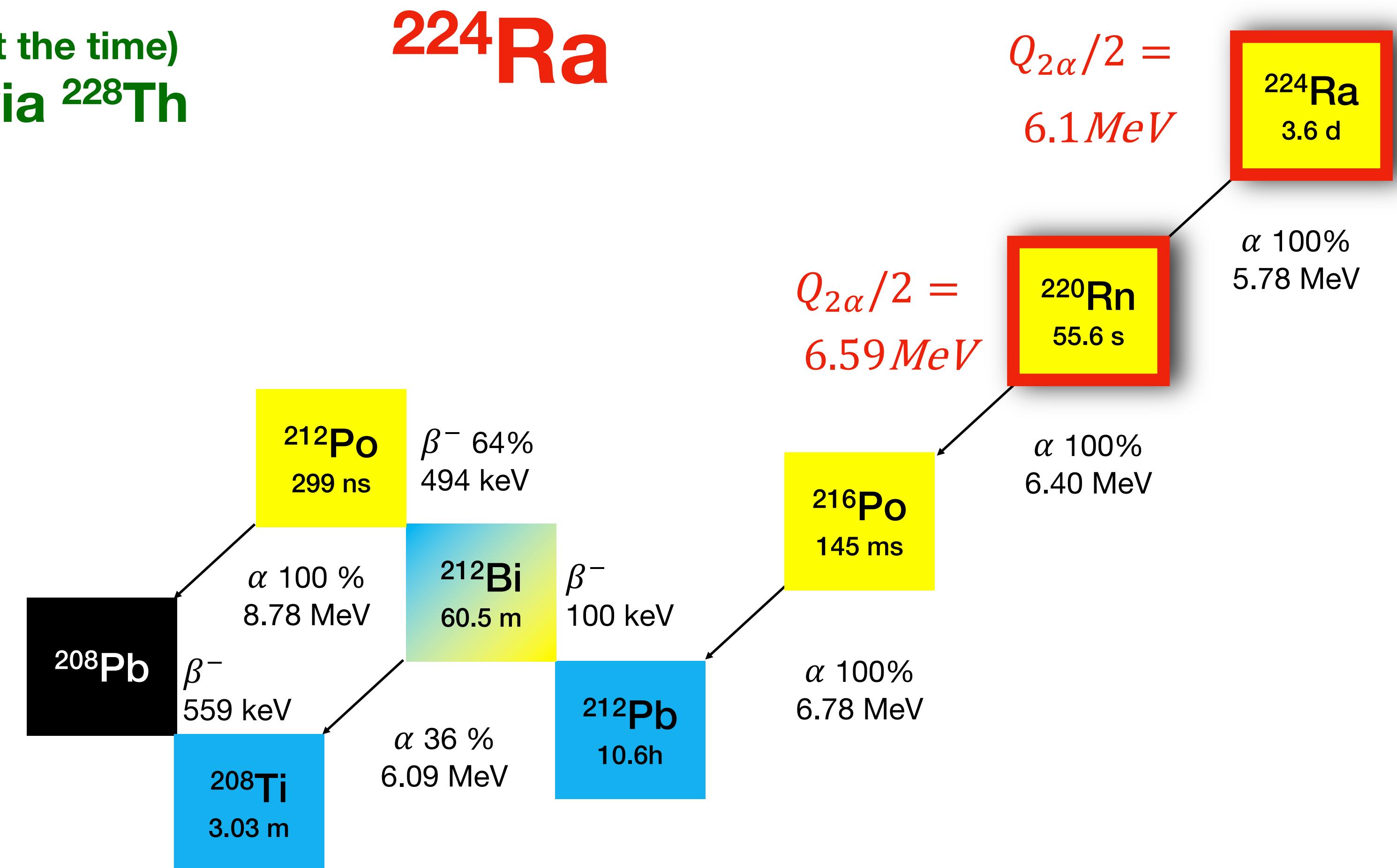
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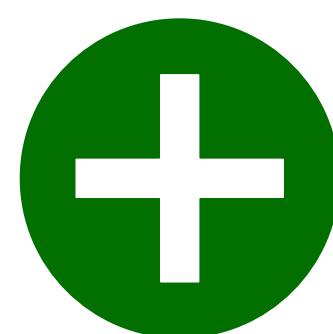
(Only theoretical candidate at the time)
Source production via ^{228}Th

- 2α candidate
- Alpha emitter
- Beta emitter

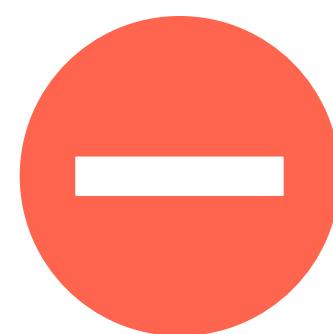


FRS Ion Catcher - GSI

Isotope choice - decay chain



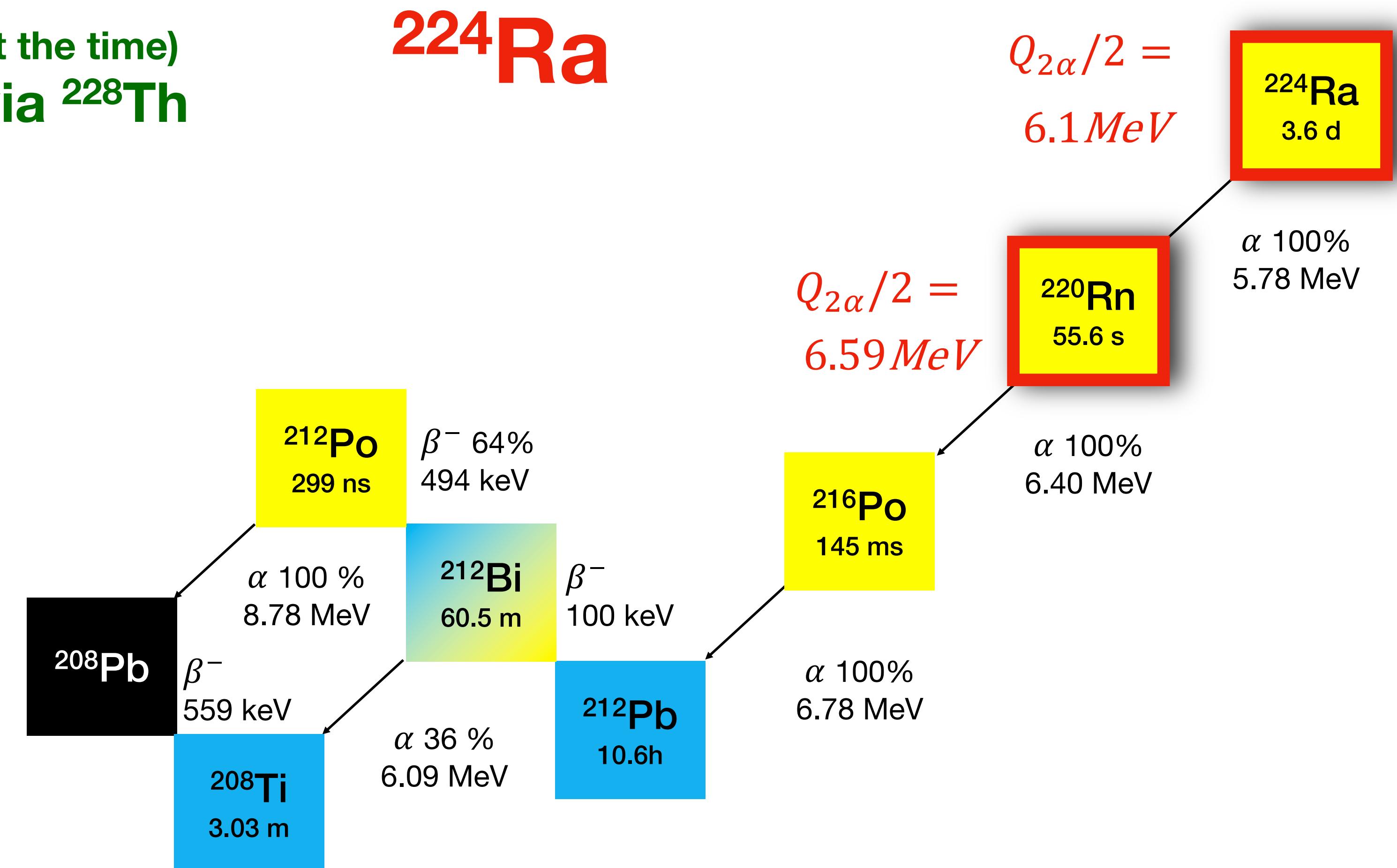
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Source production via ^{228}Th



■ 2α candidate

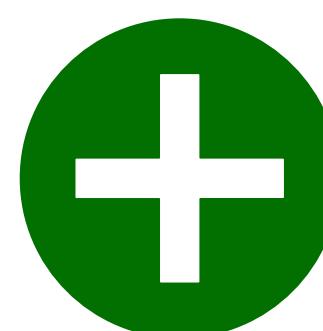
■ Alpha emitter

■ Beta emitter

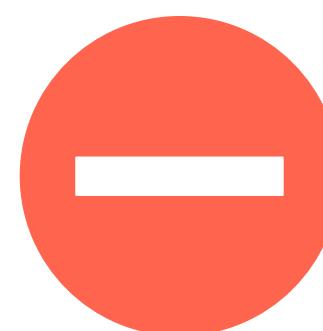


FRS Ion Catcher - GSI

Isotope choice - decay chain



(Only theoretical candidate at the time)
Source production via ^{228}Th



Beta background

2α candidate

Alpha emitter

Beta emitter

^{224}Ra

$$Q_{2\alpha}/2 = 6.1 \text{ MeV}$$

^{224}Ra
3.6 d

$$Q_{2\alpha}/2 = 6.59 \text{ MeV}$$

^{220}Rn
55.6 s

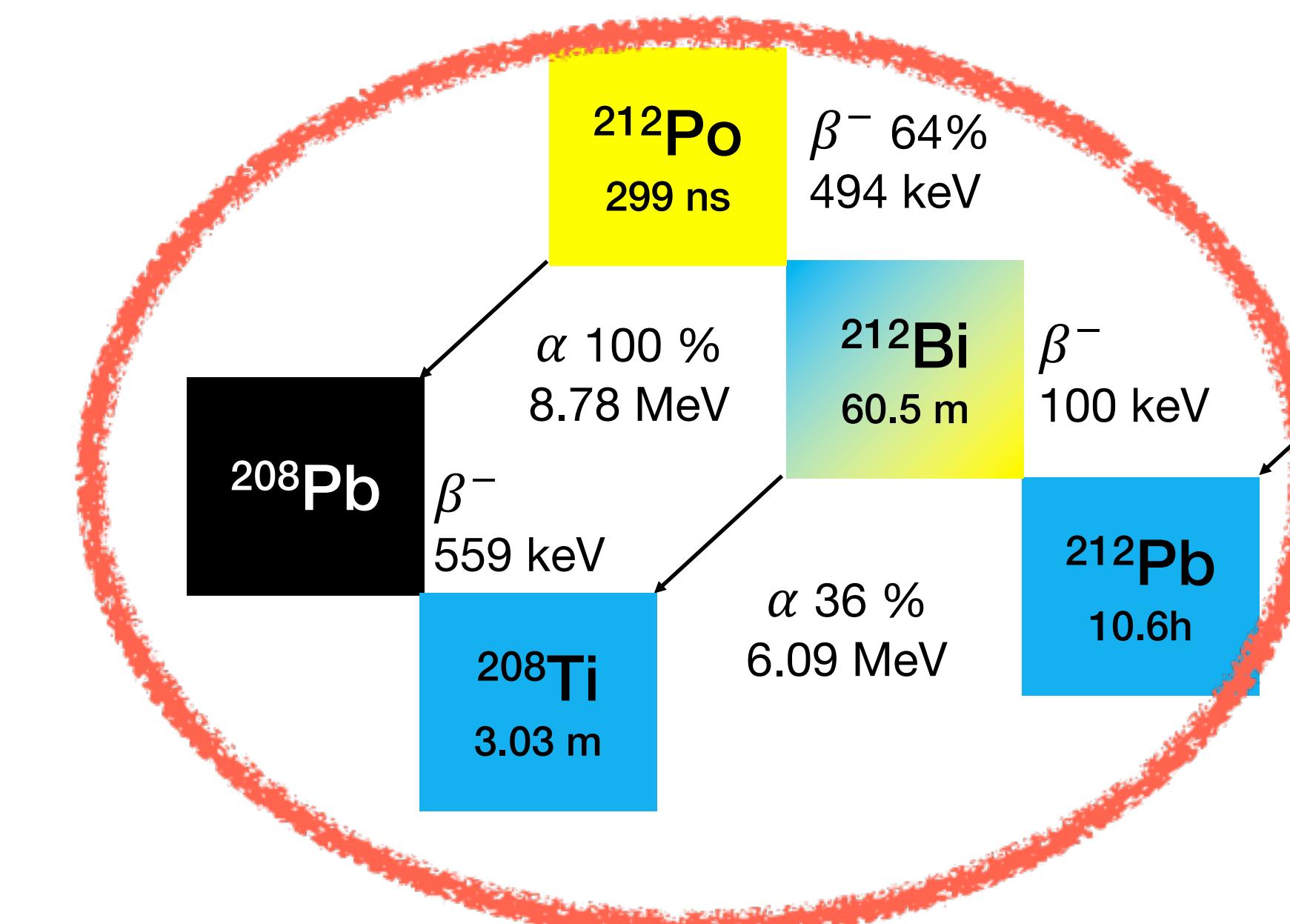
α 100%
5.78 MeV

^{216}Po
145 ms

α 100%
6.40 MeV

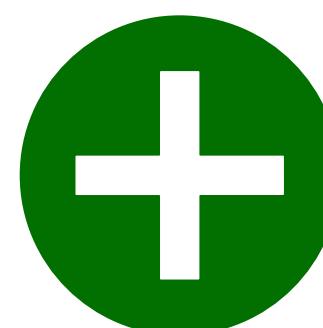
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Background

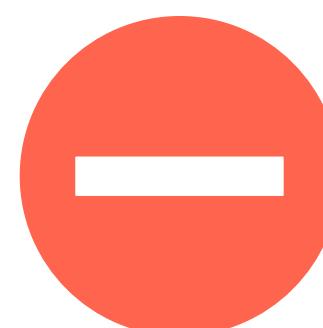


FRS Ion Catcher - GSI

Isotope choice - decay chain



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Source production via ^{228}Th

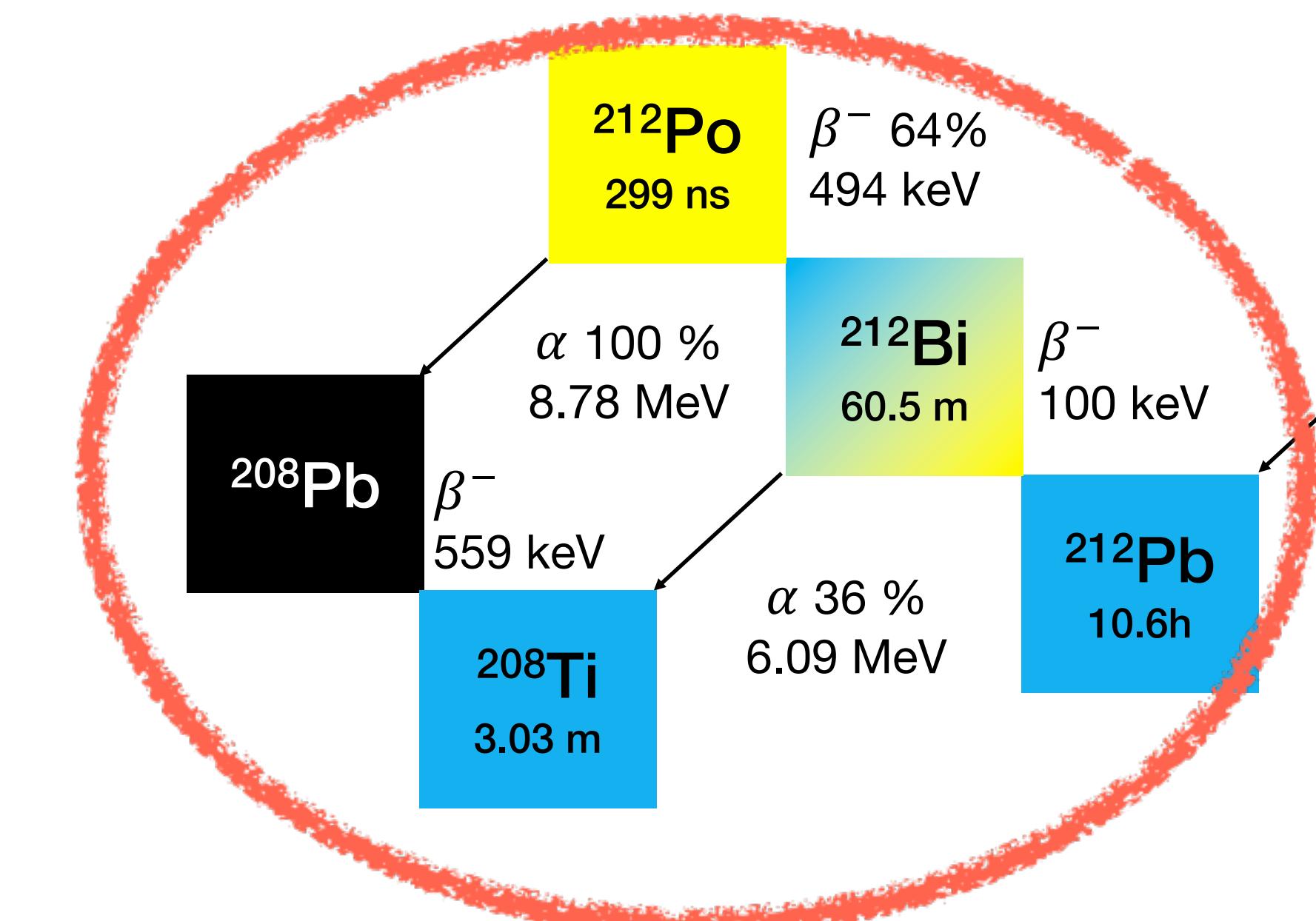


Beta background

2α candidate

Alpha emitter

Beta emitter



^{224}Ra

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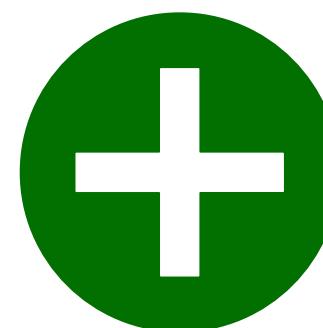
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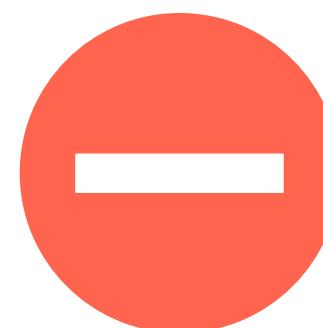
Background

FRS Ion Catcher - GSI

Isotope choice - decay chain



(Only theoretical candidate at the time)
Source production via ^{228}Th

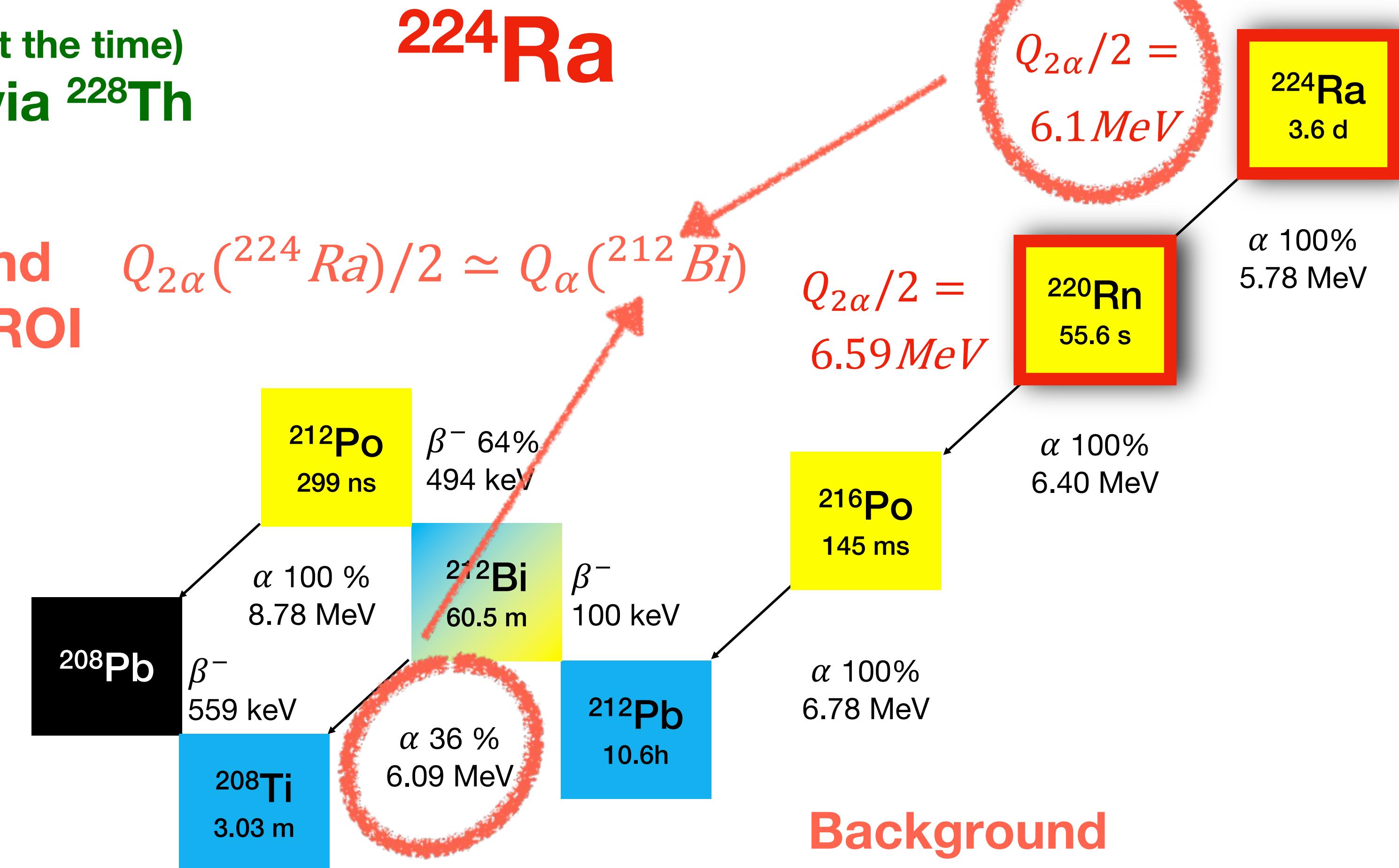


Beta background
Contaminant in ROI

■ 2α candidate

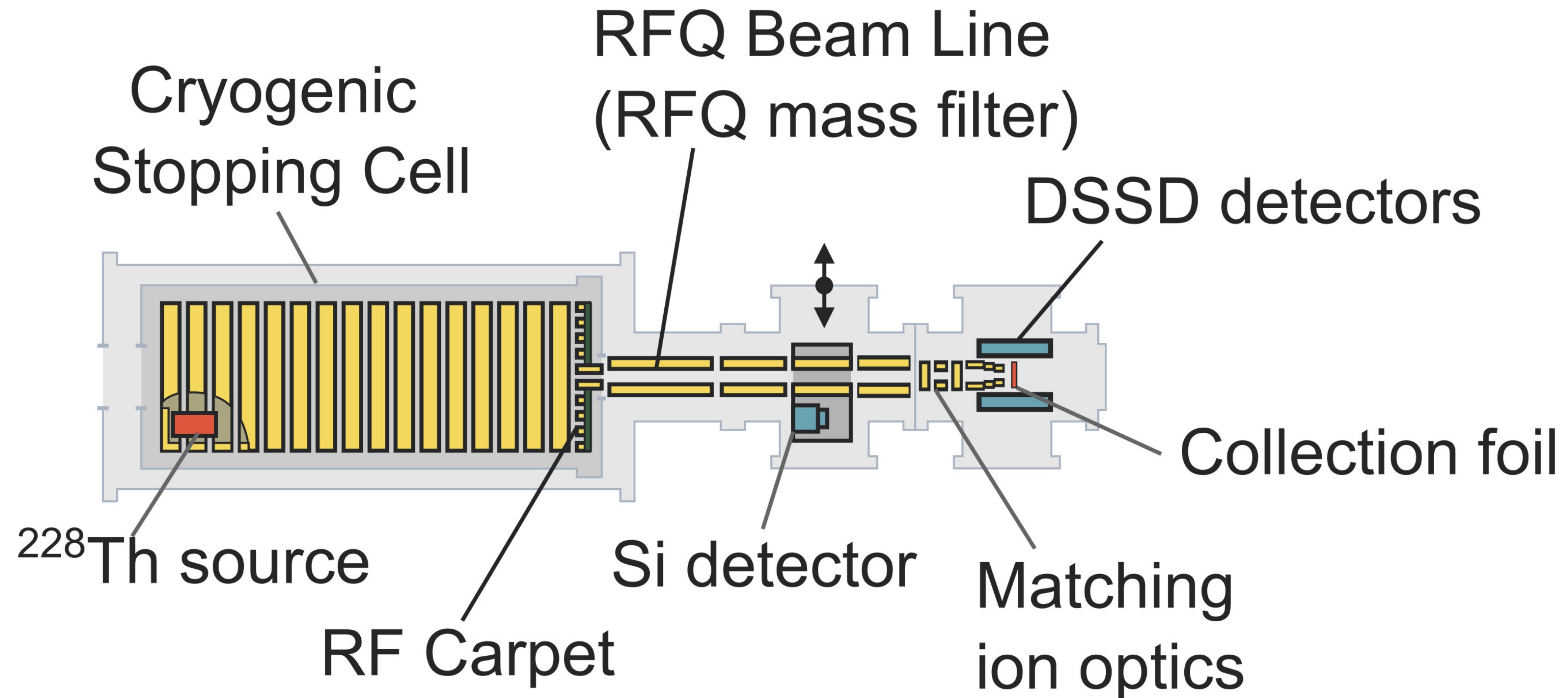
■ Alpha emitter

■ Beta emitter



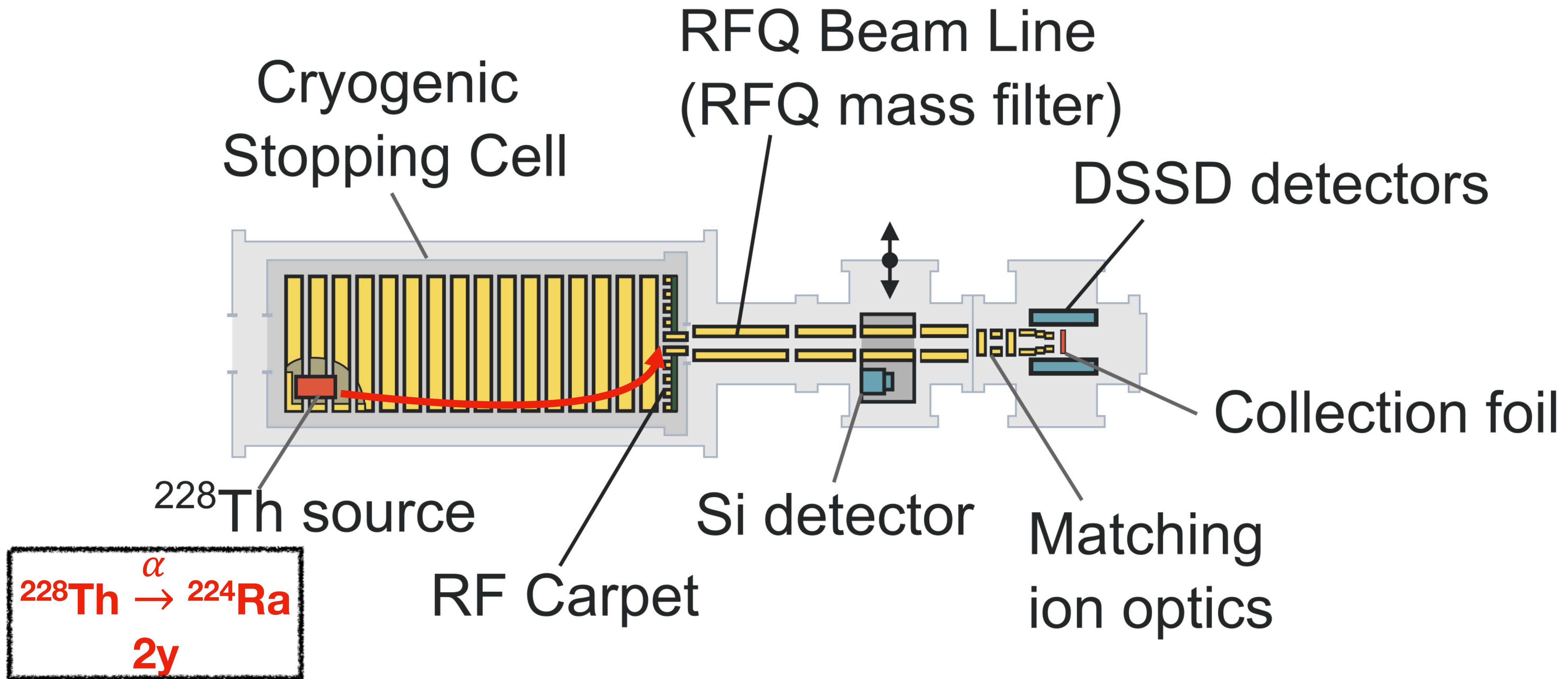
FRS Ion Catcher - GSI

Sketch of the setup



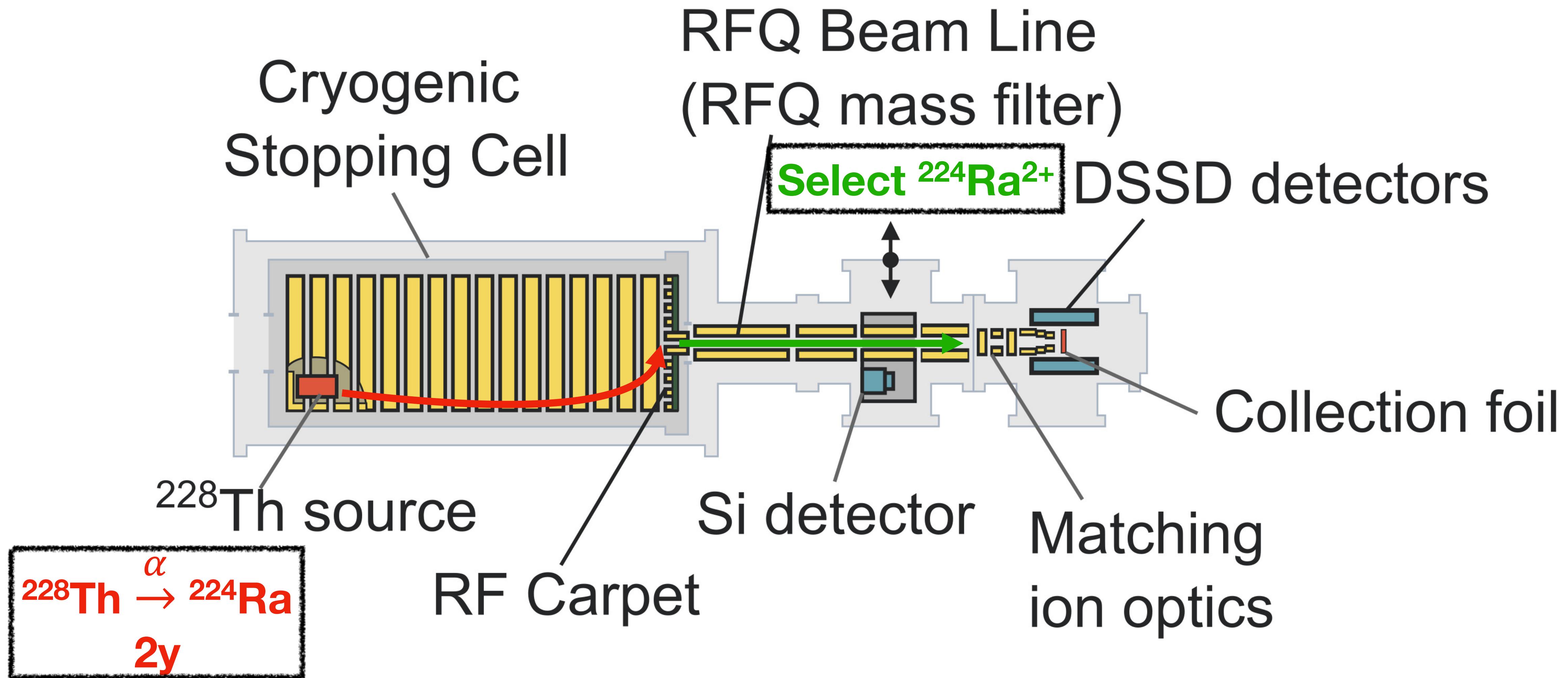
FRS Ion Catcher - GSI

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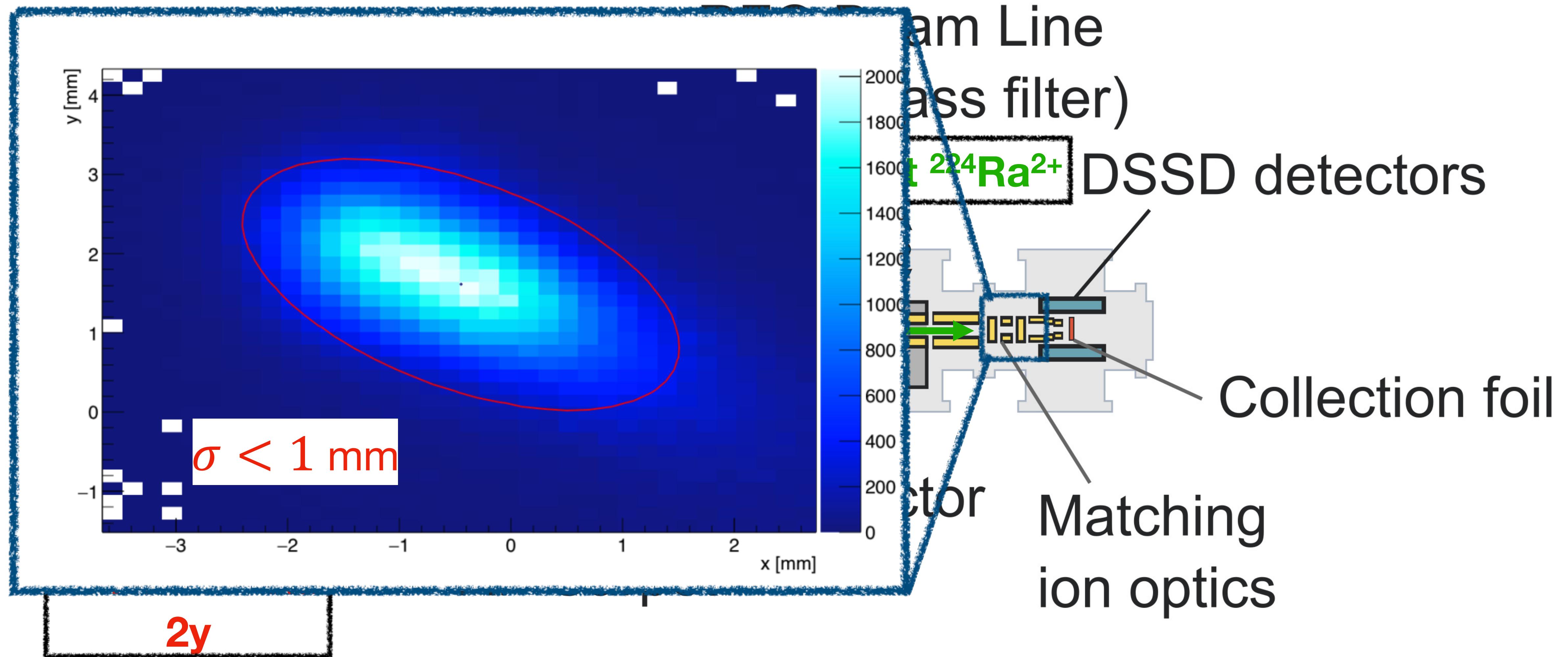
FRS Ion Catcher - GSI

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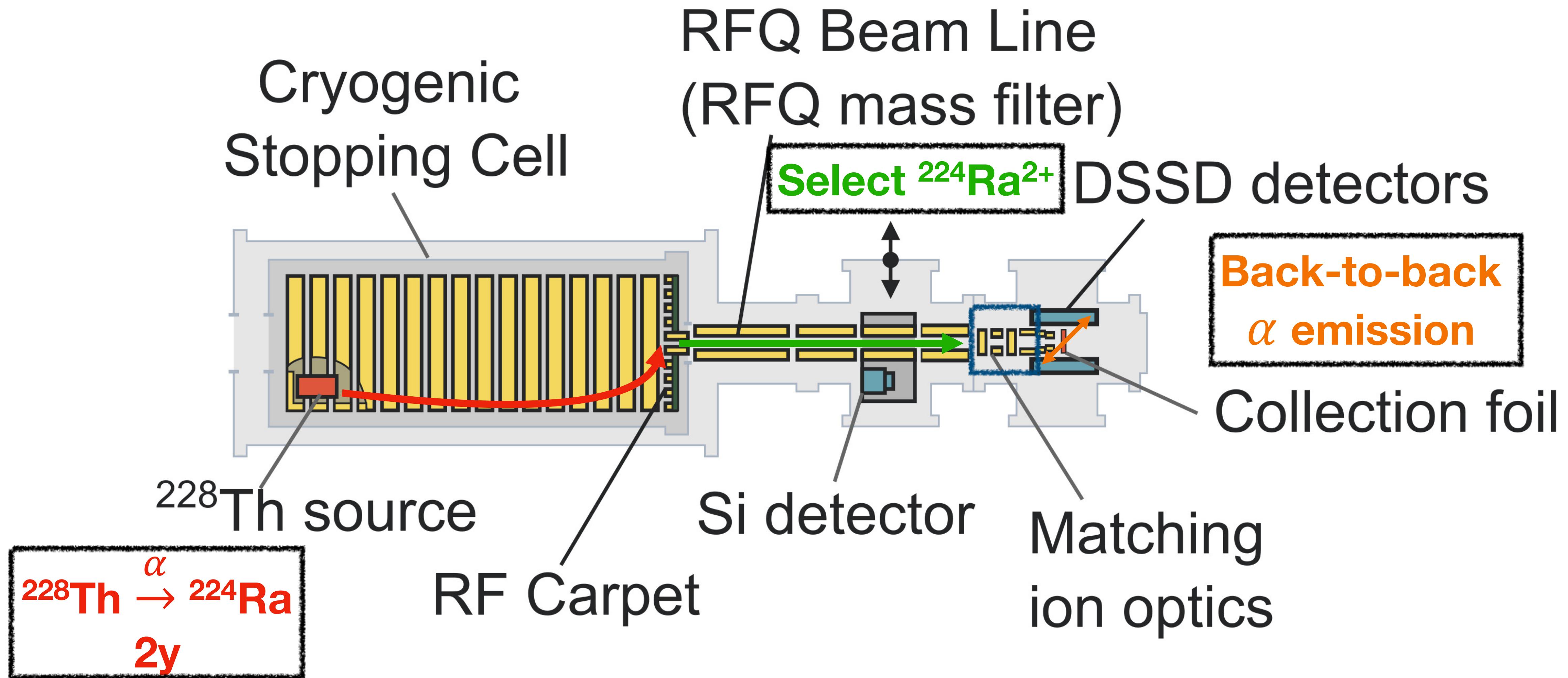
FRS Ion Catcher - GSI

Sketch of the setup



FRS Ion Catcher - GSI

Sketch of the setup



FRS Ion Catcher - GSI

Sketch of the setup

Cryogenic
Stopping Cell

^{228}Th source

RF Carpet

$^{228}\text{Th} \xrightarrow{\alpha} ^{224}\text{Ra}$
2y

RFQ Beam Line
(RFQ mass filter)

Select $^{224}\text{Ra}^{2+}$

Si detector

DSSD detectors

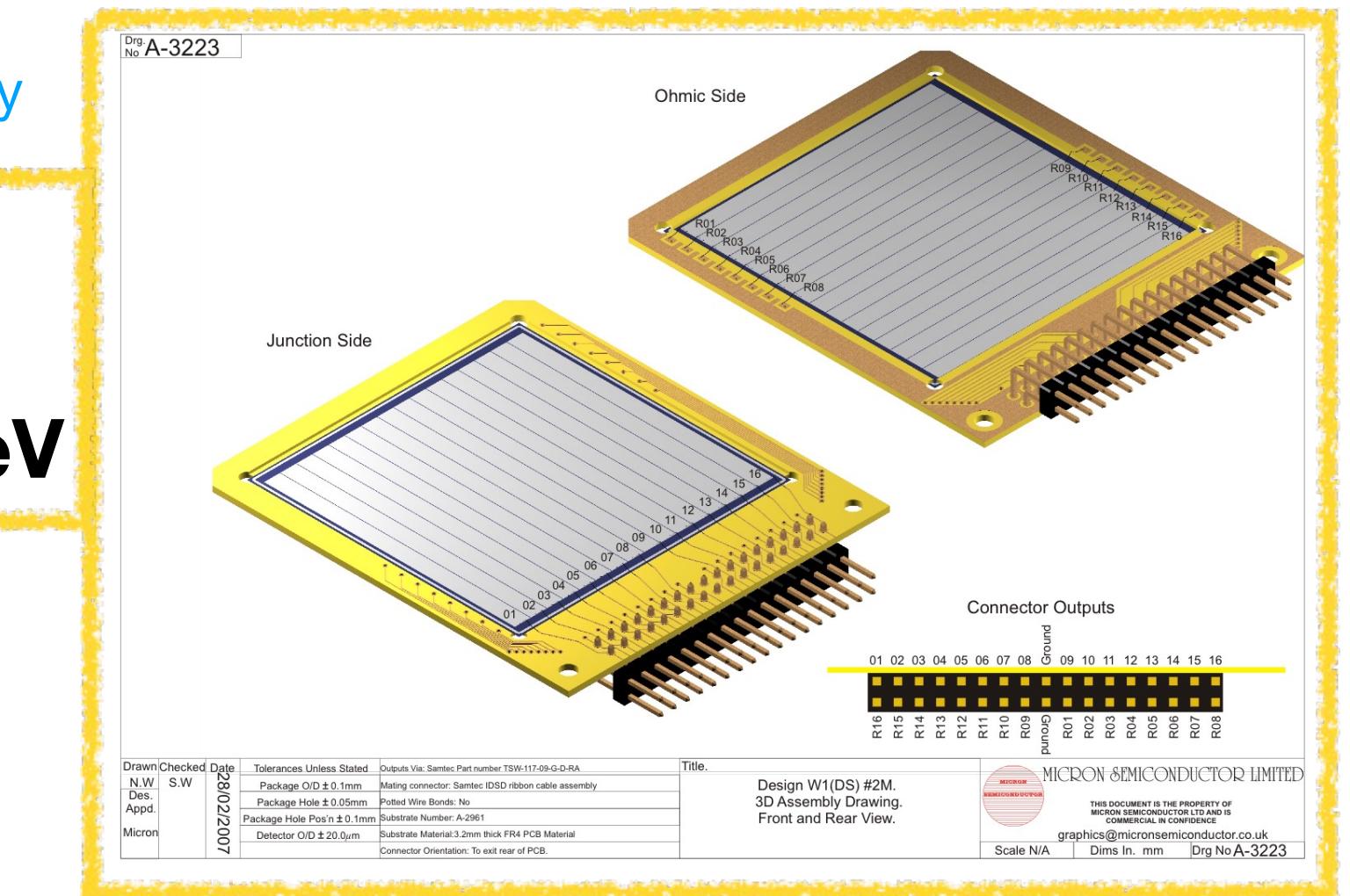
Back-to-back
 α emission

Collection foil

Matching
ion optics

H. Wilsenach courtesy

50 x 50 mm²
16 x 16 strips
Resolution ~ 25 keV



H. Wilsenach courtesy

FRS Ion Catcher - GSI

Data Acquisition (2022)

M	T	W	T	F	S	S
31	1	2	3	4	5	6
				Run 121	Run 121	Run 121
7	8	9	10	11	12	13
Run 121						
14	15	16	17	18	19	20
Run 121	Run 124	Run 121	Run 121	Run 131	Run 131	Run 131
21	22	23	24	25	26	27
Run 131	Run 133					
28	1	2	3	4	5	6
Run 135	Run 138	Run 138	Run 139	Run 142	Run 142	Run 142
7	8	9	10	11	12	13
Run 142	Run 142	Run 142	Run 142			
14	15	16	17	18	19	20
			Run 150	Run 150	Run 150	Run 150
21	22	23	24	25	26	27
Run 150	Run 151	Run 154	Tests	Run 212	Run 212	Run 212
28	29	30	31	1	2	3
Run 212	Run 212	Run 212	Run 246	Run 246	Run 246	Run 248
4	5	6	7	8	9	10
Run 248						
11	12	13	14	15	16	17
Run 248	Run 248	Run 248	Run 249	Run 249	Run 249	Run 249
18	19	20	21	22	23	24
Run 249	Run 249	Run 249	Run 280	Run 280	Run 280	Run 280

FEB

MAR

APR

M	T	W	T	F	S	S
25	26	27	28	29	30	1
						Run 315
2	3	4	5	6	7	8
Run 315	Run 315	Run 315	Run 315	Run 316	Run 316	Run 318
9	10	11	12	13	14	15
Run 320	Run 321	Run 321	Run 321	Run 322	Run 322	Run 322
16	17	18	19	20	21	22
Run 322						
23	24	25	26	27	28	29
Run 322	Run 323	Run 323	Run 323	Run 323	Run 324	Run 324
30	31	1	2	3	4	5
Run 326						
Run 331						
13	14	15	16	17	18	19
Run 331	Run 331	Run 331	Run 331	Run 333	Run 333	Run 333
20	21	22	23	24	25	26
Run 334	Run 334	Run 334	Run 334	Run 336	Run 336	Run 336
27	28	1	2	3	4	5
Run 336						
4	5	6	7	8	9	10
Run 336	Run 336	Run 336	Run 336	Run 337	Run 337	Run 337
11	12	13	14	15	16	17
Run 337	Run 337	Run 337	Run 337			

MAY

JUN

JUL

All

224Ra

BG

FRS Ion Catcher - GSI

Data Acquisition (2022)

M	T	W	T	F	S	S
31	1	2	3	4	5	6
				Run 121	Run 121	Run 121
7	8	9	10	11	12	13
Run 121						
14	15	16	17	18	19	20
Run 121	Run 124	Run 121	Run 121	Run 131	Run 131	Run 131
21	22	23	24	25	26	27
Run 131	Run 133					
28	1	2	3	4	5	6
Run 135	Run 138	Run 138	Run 139	Run 142	Run 142	Run 142
7	8	9	10	11	12	13
Run 142	Run 142	Run 142	Run 142			
14	15	16	17	18	19	20
			Run 150	Run 150	Run 150	Run 150
21	22	23	24	25	26	27
Run 150	Run 151	Run 154	Tests	Run 212	Run 212	Run 212
28	29	30	31	1	2	3
Run 212	Run 212	Run 212	Run 246	Run 246	Run 246	Run 248
4	5	6	7	8	9	10
Run 248						
11	12	13	14	15	16	17
Run 248	Run 248	Run 248	Run 249	Run 249	Run 249	Run 249
18	19	20	21	22	23	24
Run 249	Run 249	Run 249	Run 280	Run 280	Run 280	Run 280

FEB

MAR

APR

M	T	W	T	F	S	S
25	26	27	28	29	30	1
						Run 315
2	3	4	5	6	7	8
Run 315	Run 315	Run 315	Run 315	Run 316	Run 316	Run 318
9	10	11	12	13	14	15
Run 320	Run 321	Run 321	Run 321	Run 322	Run 322	Run 322
16	17	18	19	20	21	22
Run 322						
23	24	25	26	27	28	29
Run 322	Run 323	Run 323	Run 323	Run 323	Run 324	Run 324
30	31	1	2	3	4	5
Run 326						
Run 331						
13	14	15	16	17	18	19
Run 331	Run 331	Run 331	Run 331	Run 333	Run 333	Run 333
20	21	22	23	24	25	26
Run 334	Run 334	Run 334	Run 334	Run 336	Run 336	Run 336
27	28	1	2	3	4	5
Run 336						
4	5	6	7	8	9	10
Run 336	Run 336	Run 336	Run 336	Run 337	Run 337	Run 337
11	12	13	14	15	16	17
Run 337	Run 337	Run 337	Run 337			

MAY

JUN

JUL

All

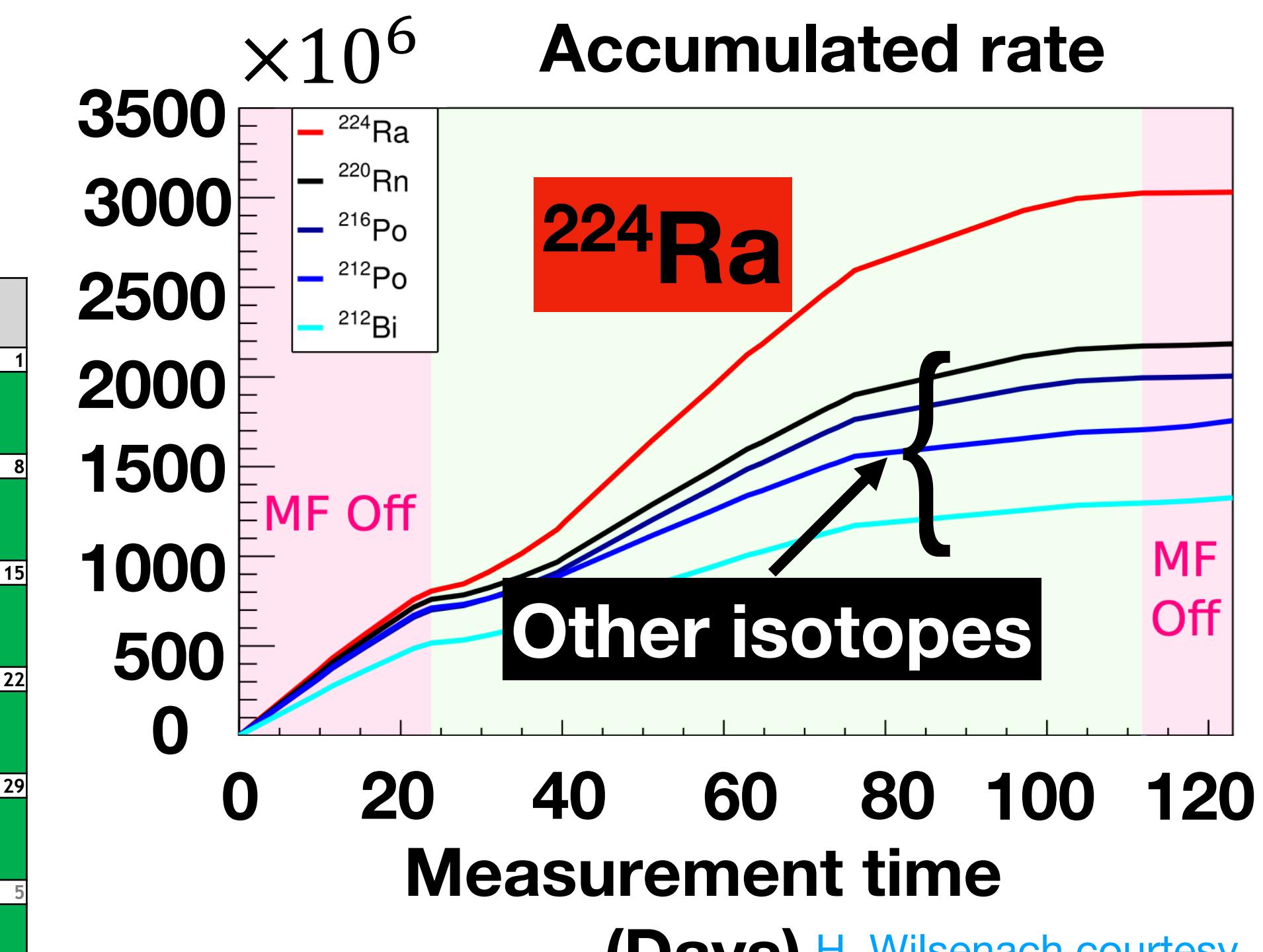
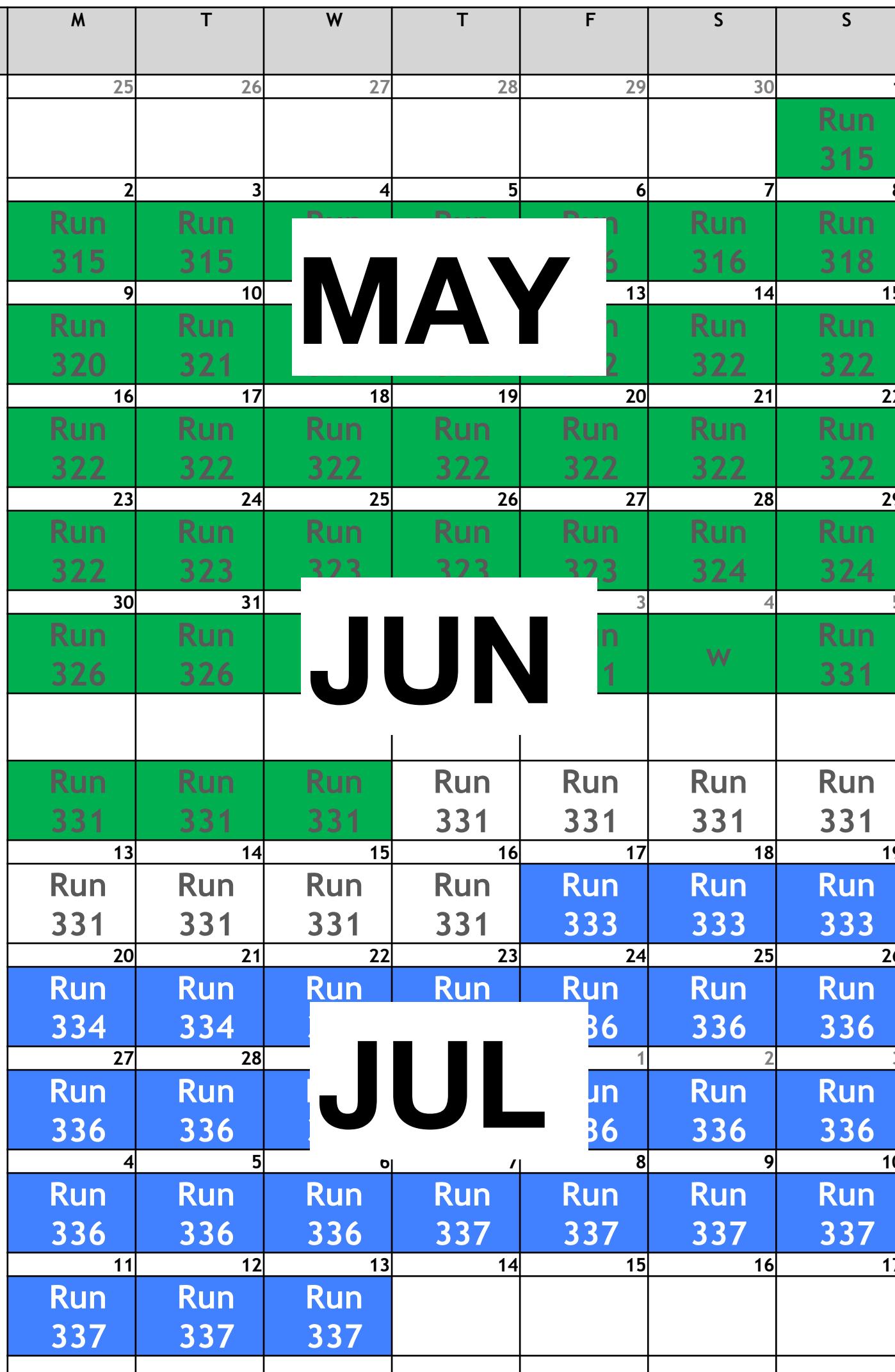
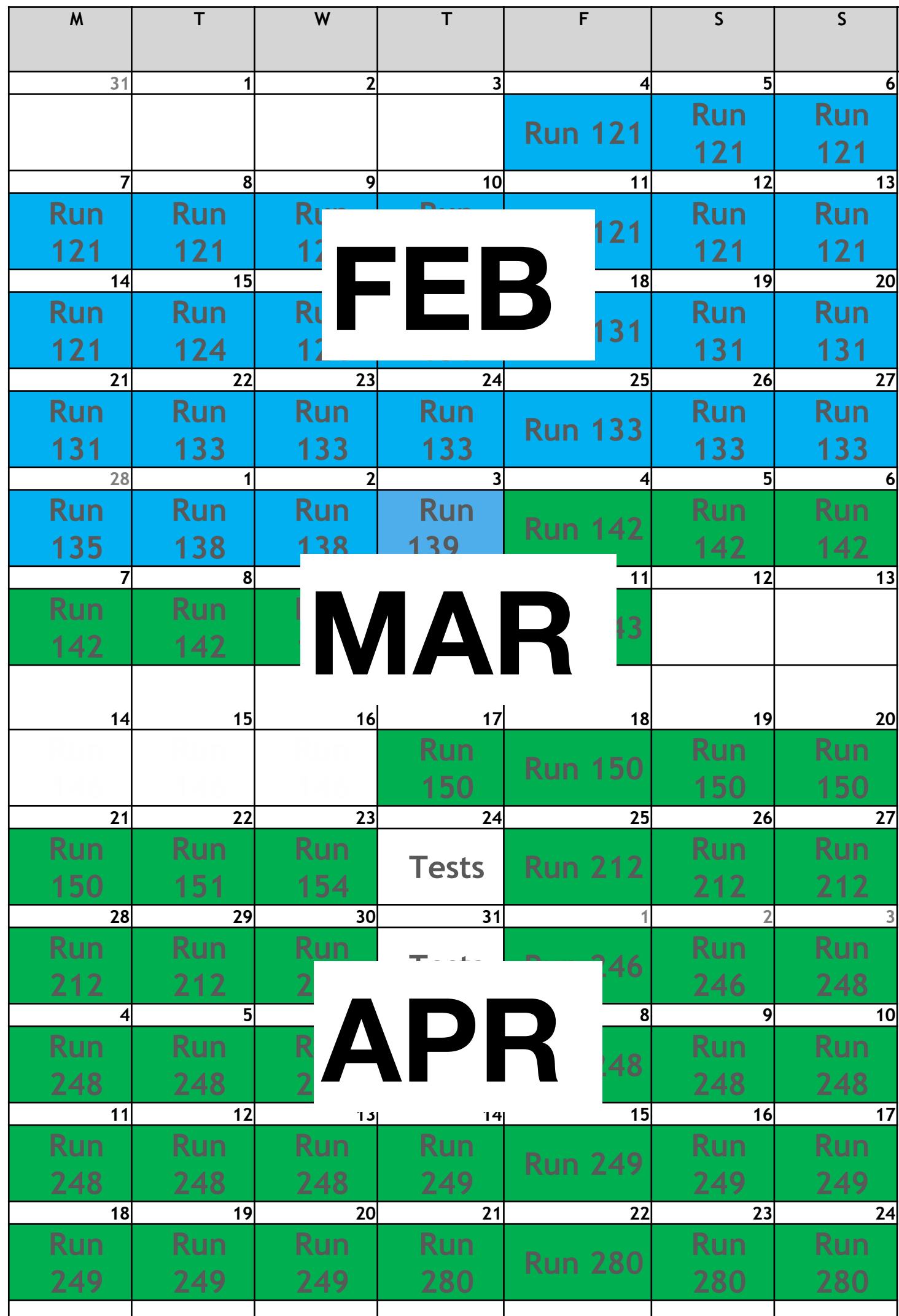
^{224}Ra

BG

~120 days of data

FRS Ion Catcher - GSI

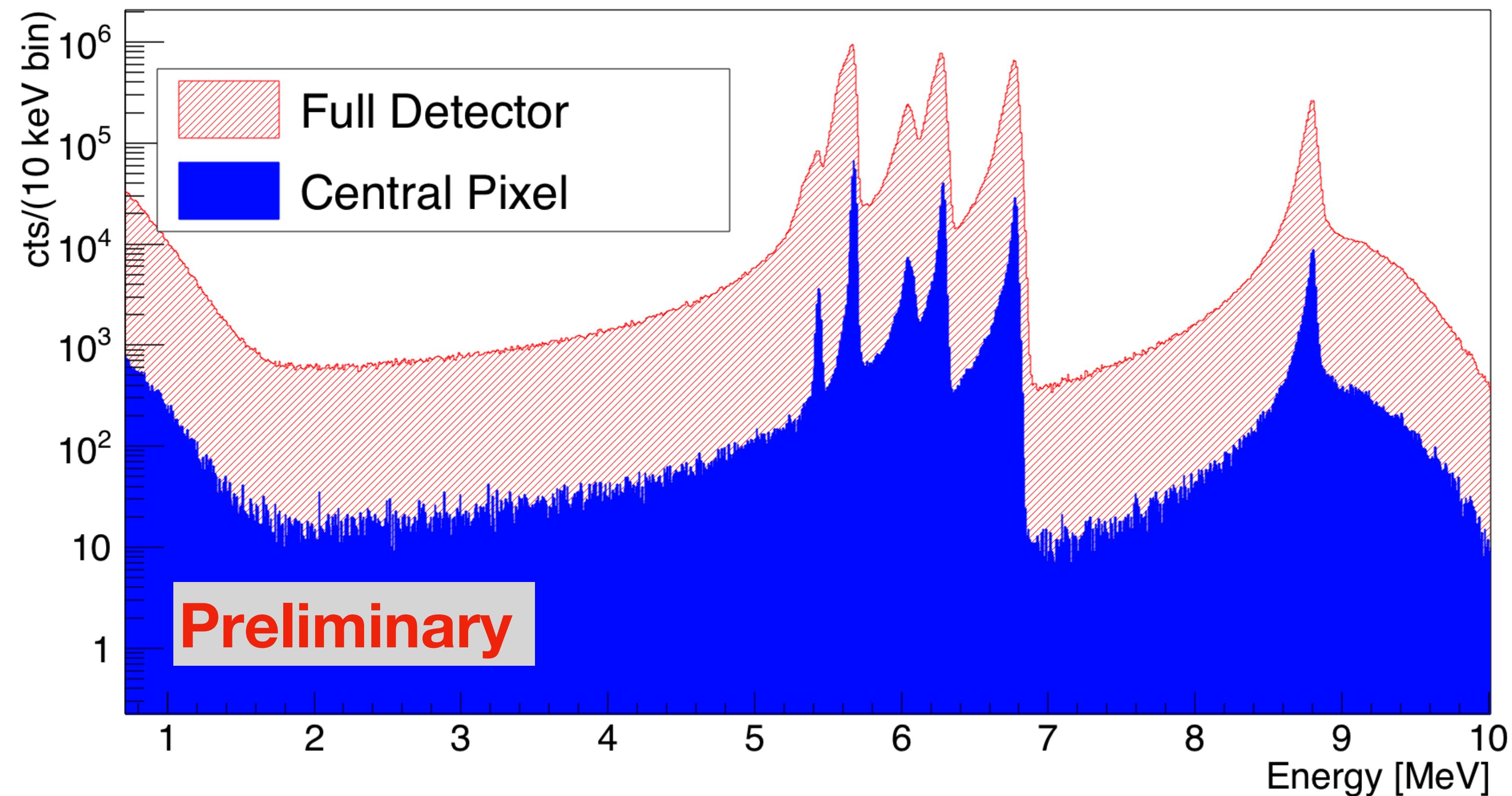
Data Acquisition (2022)



~120 days of data
 $\sim 3 \times 10^9$ ^{224}Ra implanted

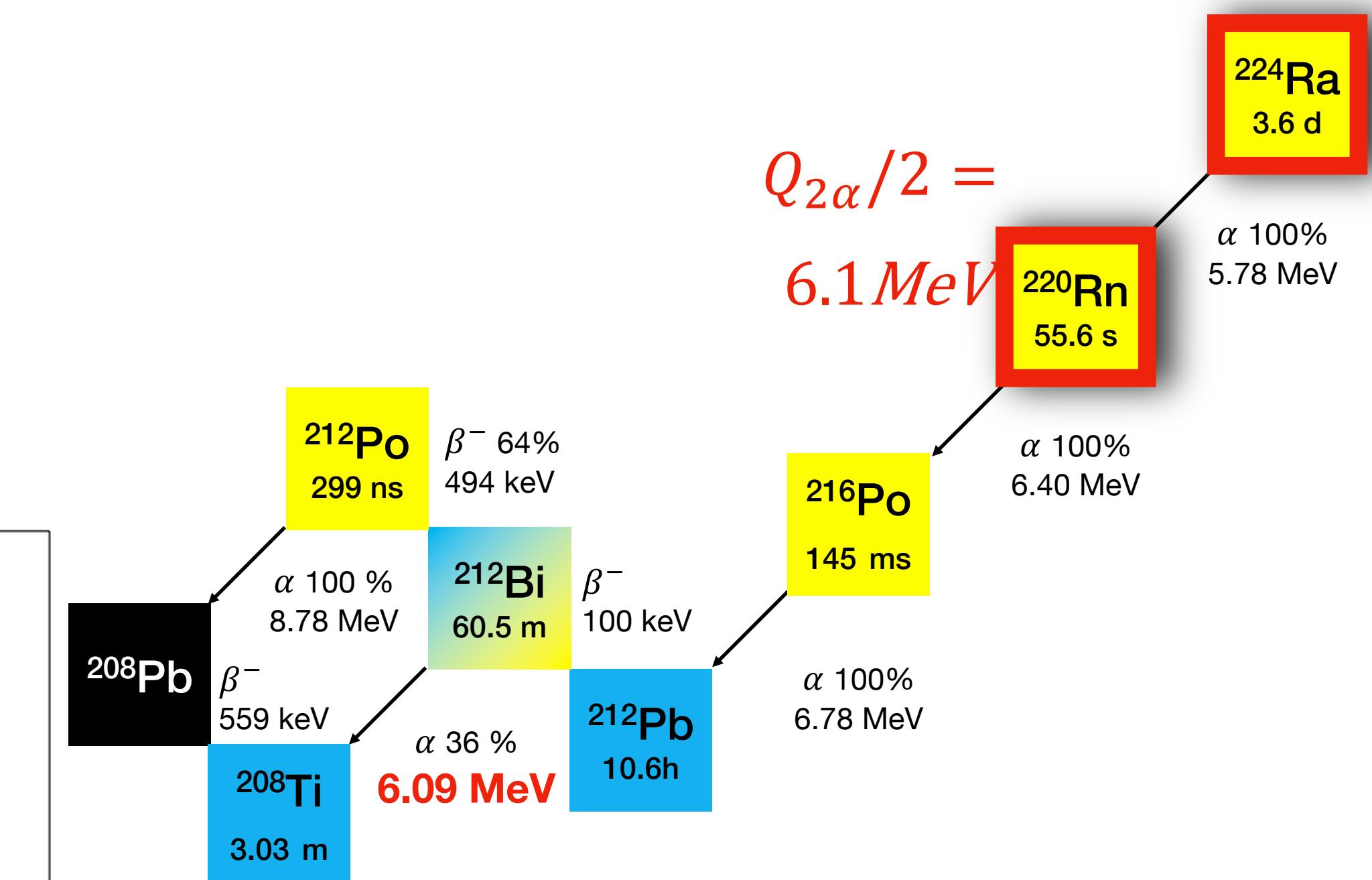
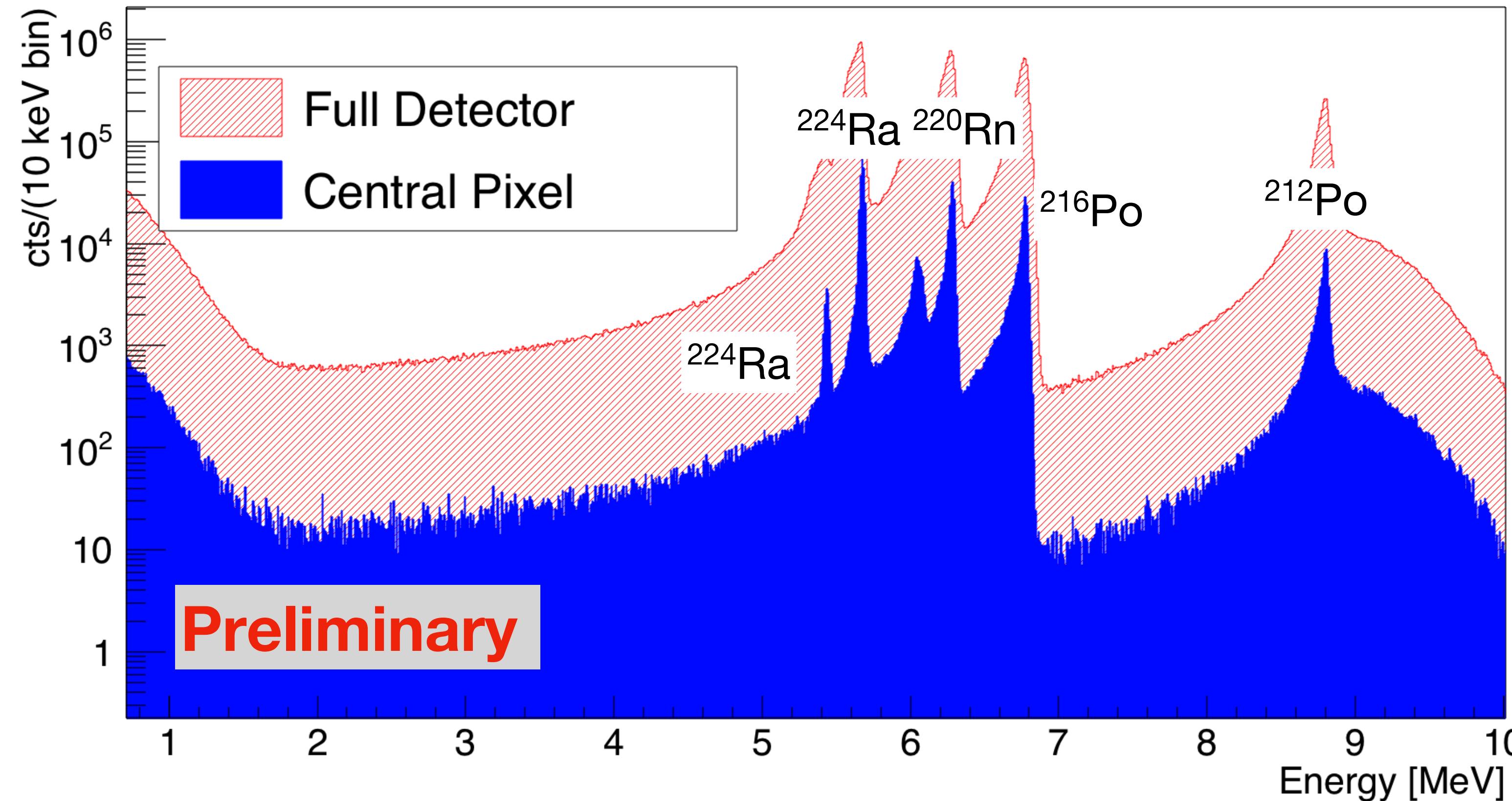
FRS Ion Catcher - GSI

Data analysis



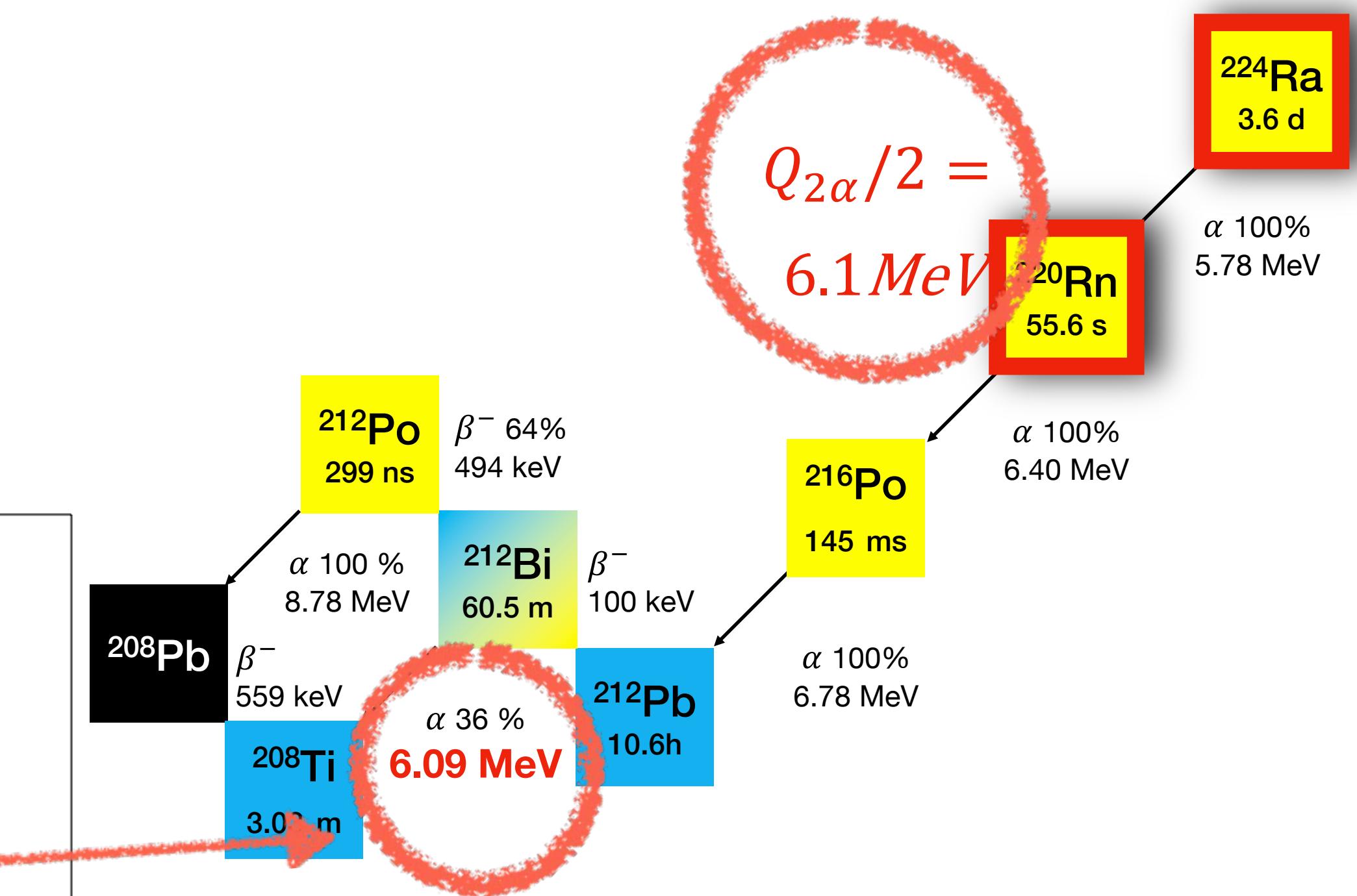
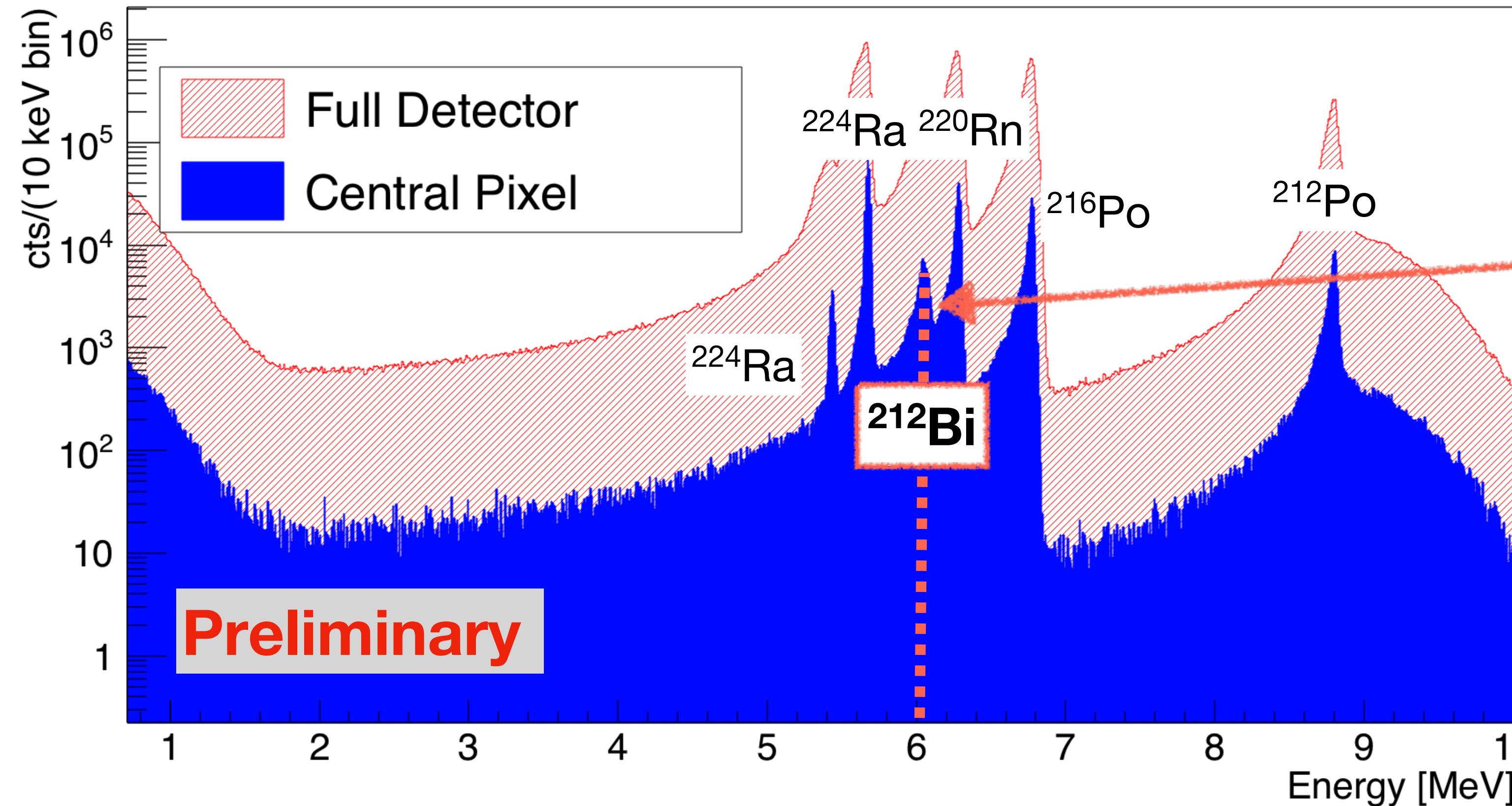
FRS Ion Catcher - GSI

Data analysis



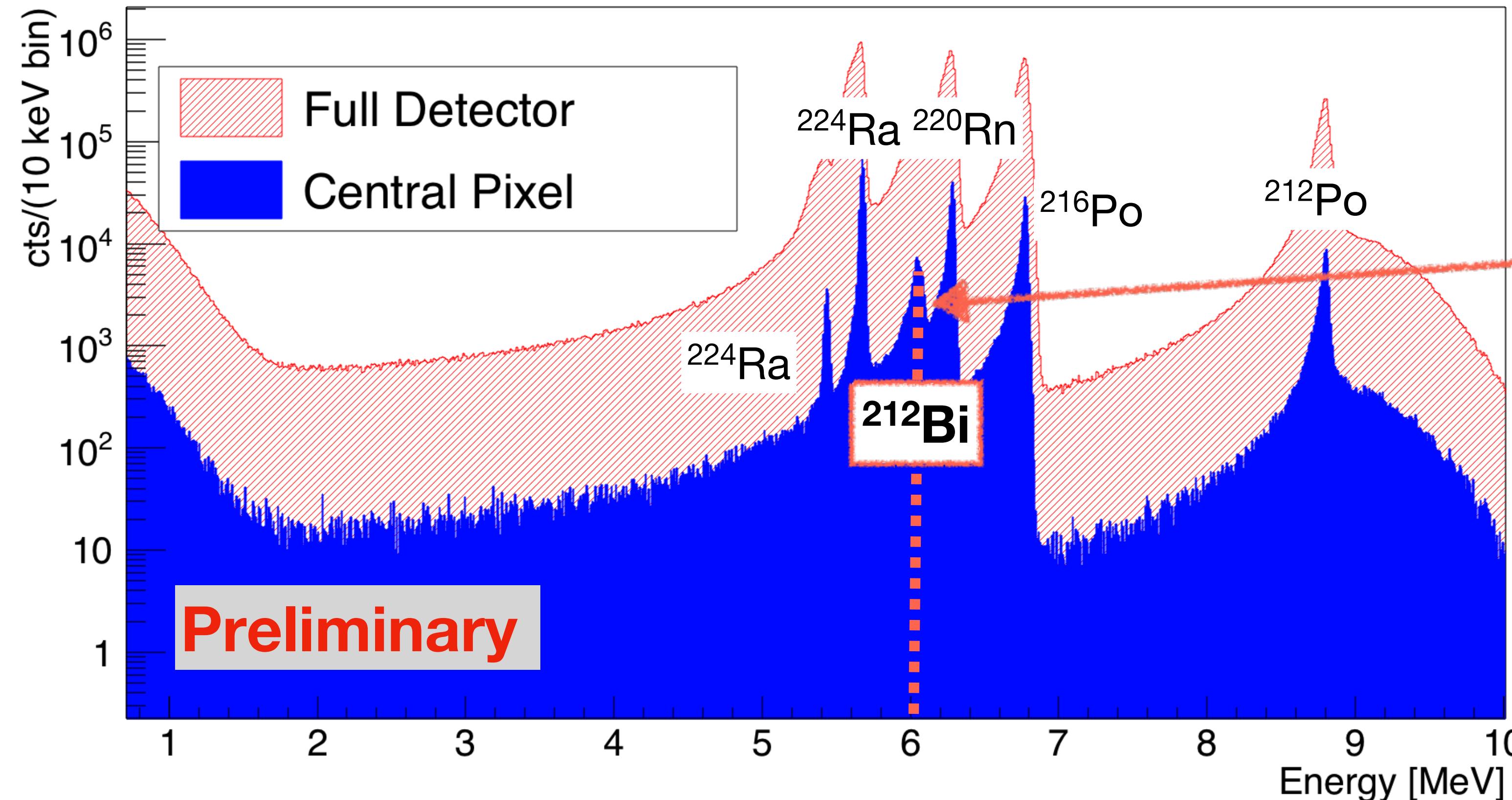
FRS Ion Catcher - GSI

Data analysis

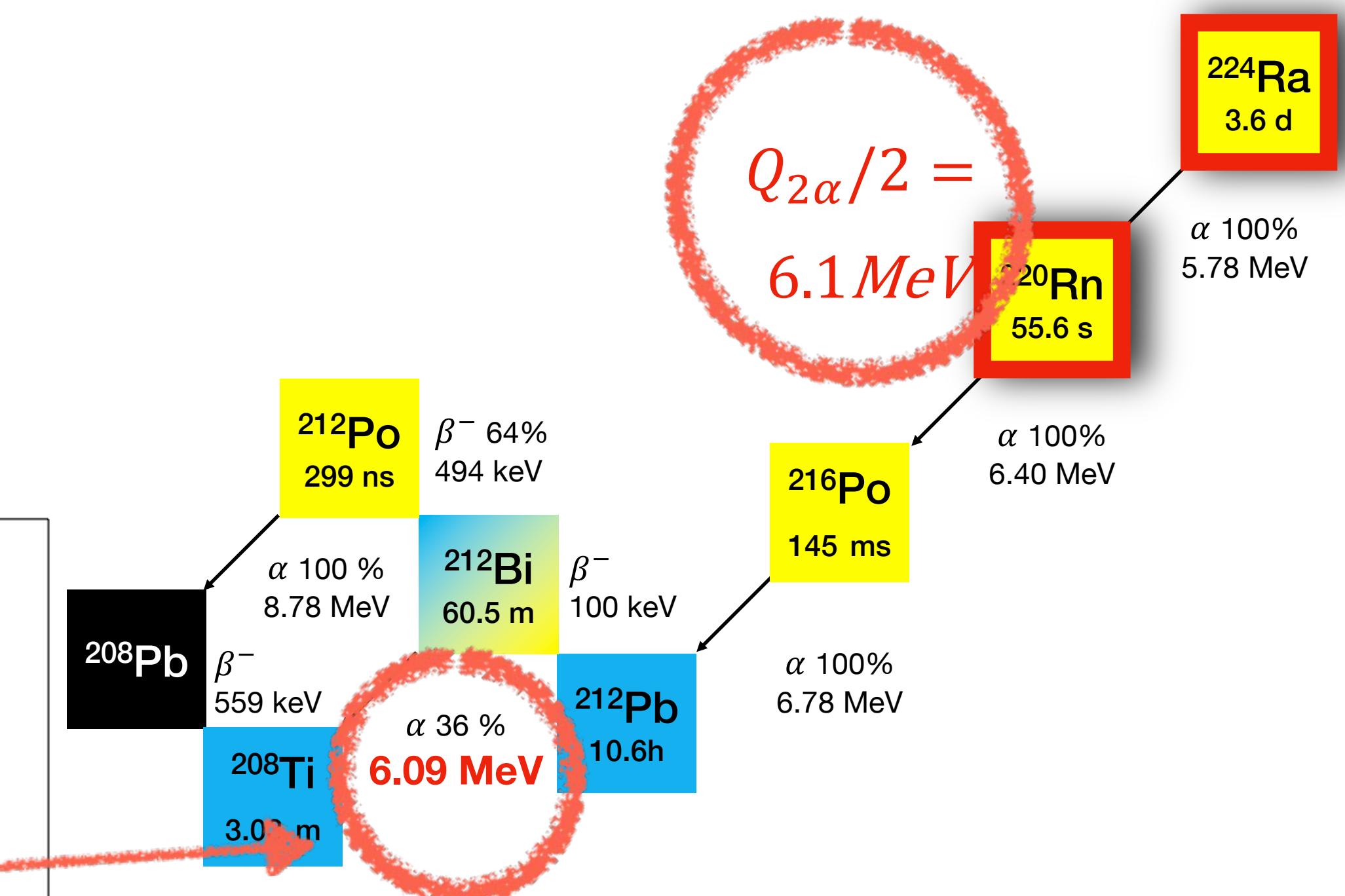


FRS Ion Catcher - GSI

Data analysis



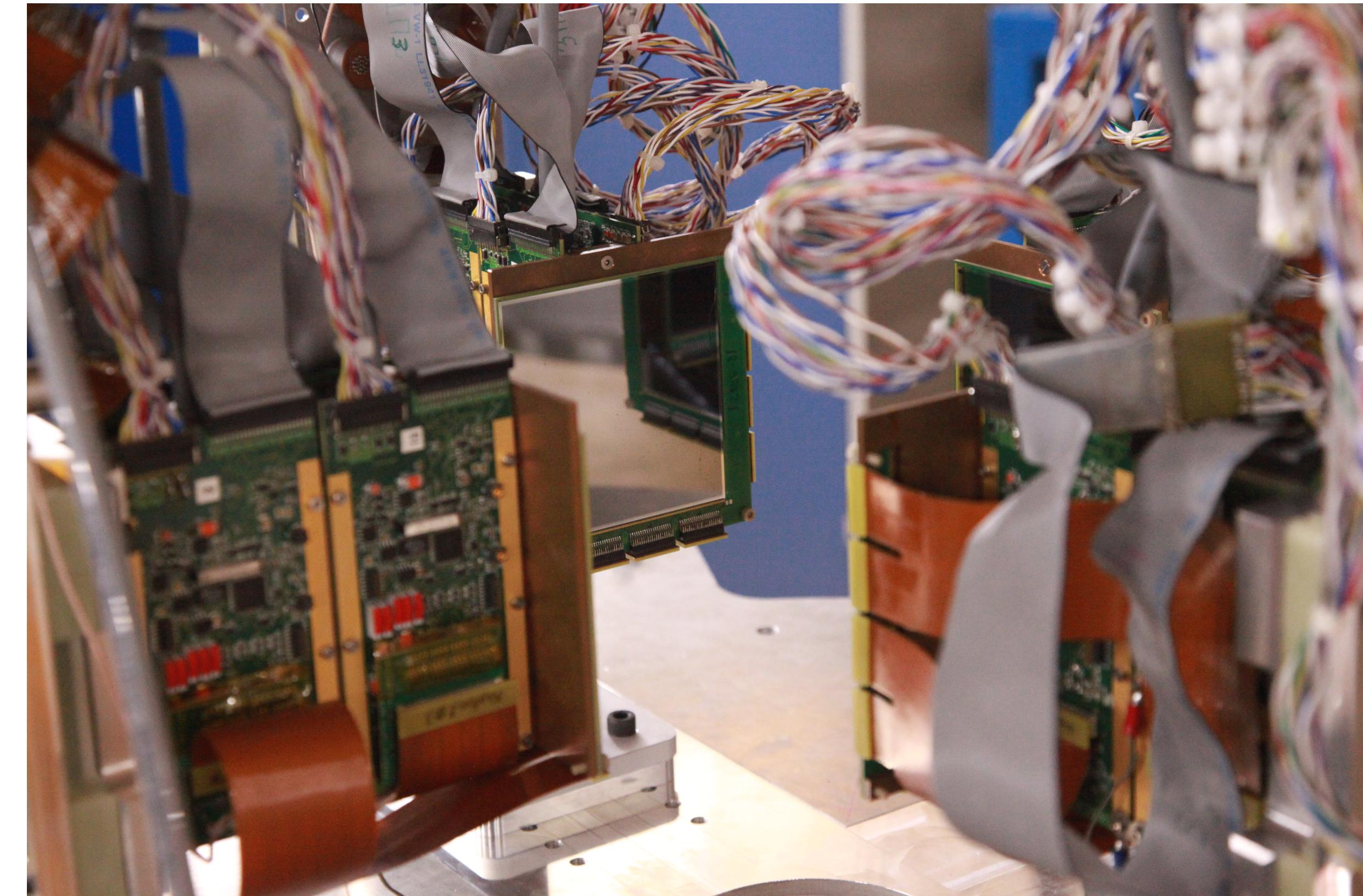
H. Wilsenach courtesy



Contamination in ROI for ^{224}Ra
 ^{220}Rn better candidate ?

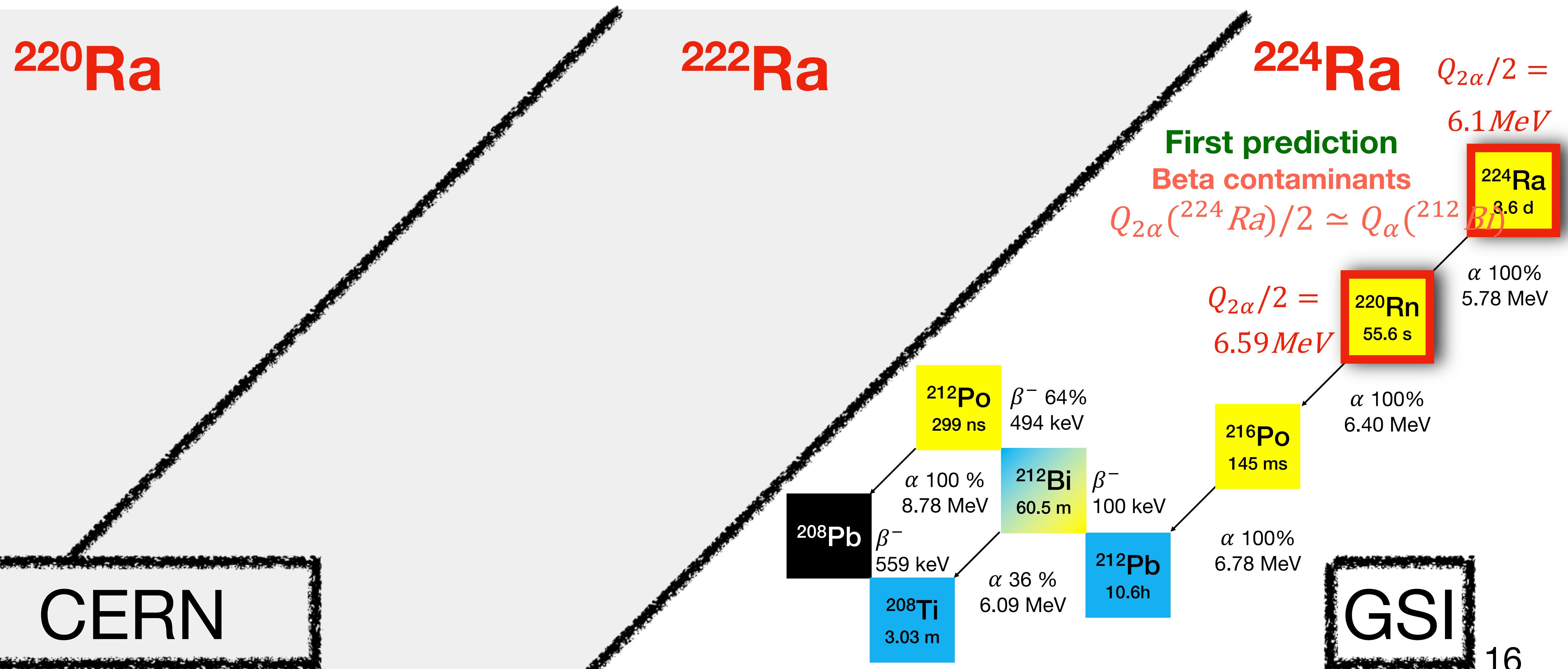
Experimental search for 2α

CERN/Isolde - Saclay



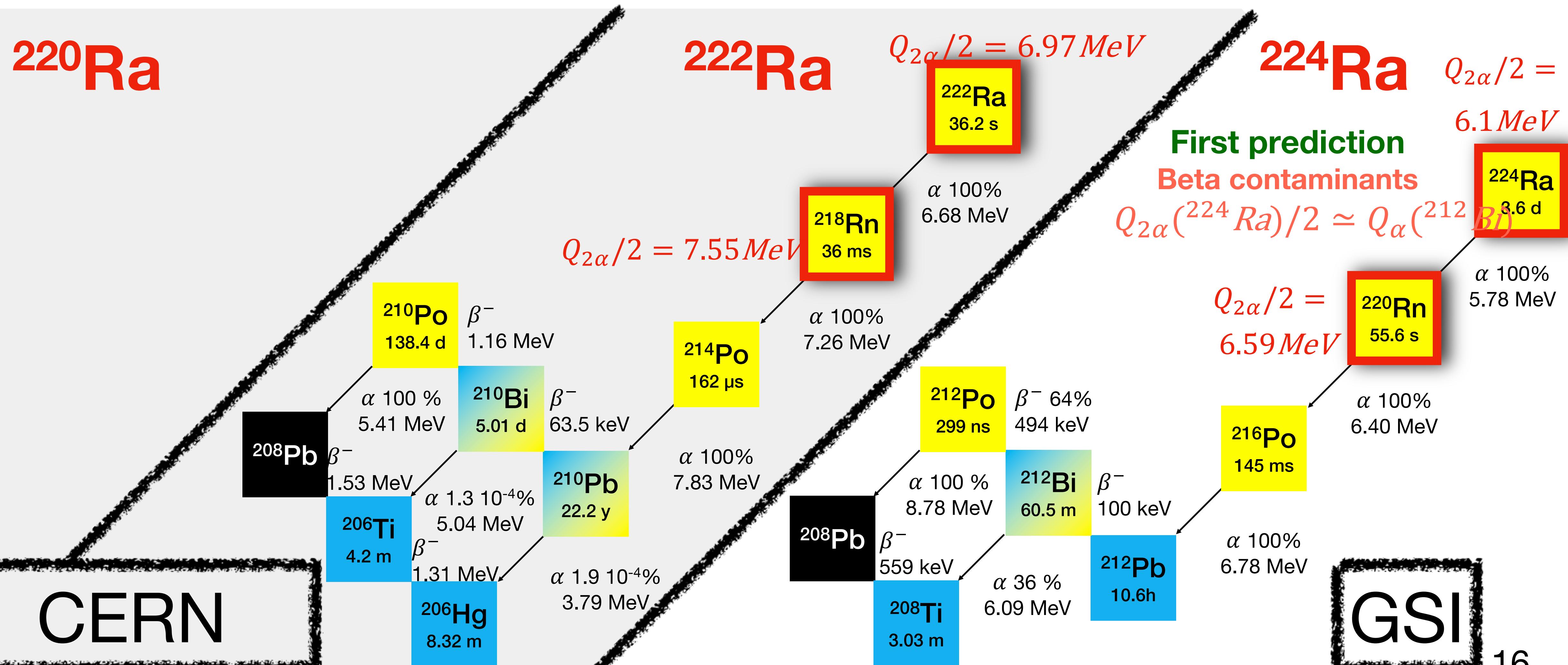
Experimental search for 2α Decay chains

■ 2α candidate
 ■ Alpha emitter
■ Beta emitter



Experimental search for 2α Decay chains

■ 2α candidate
 ■ Alpha emitter
■ Beta emitter



CERN

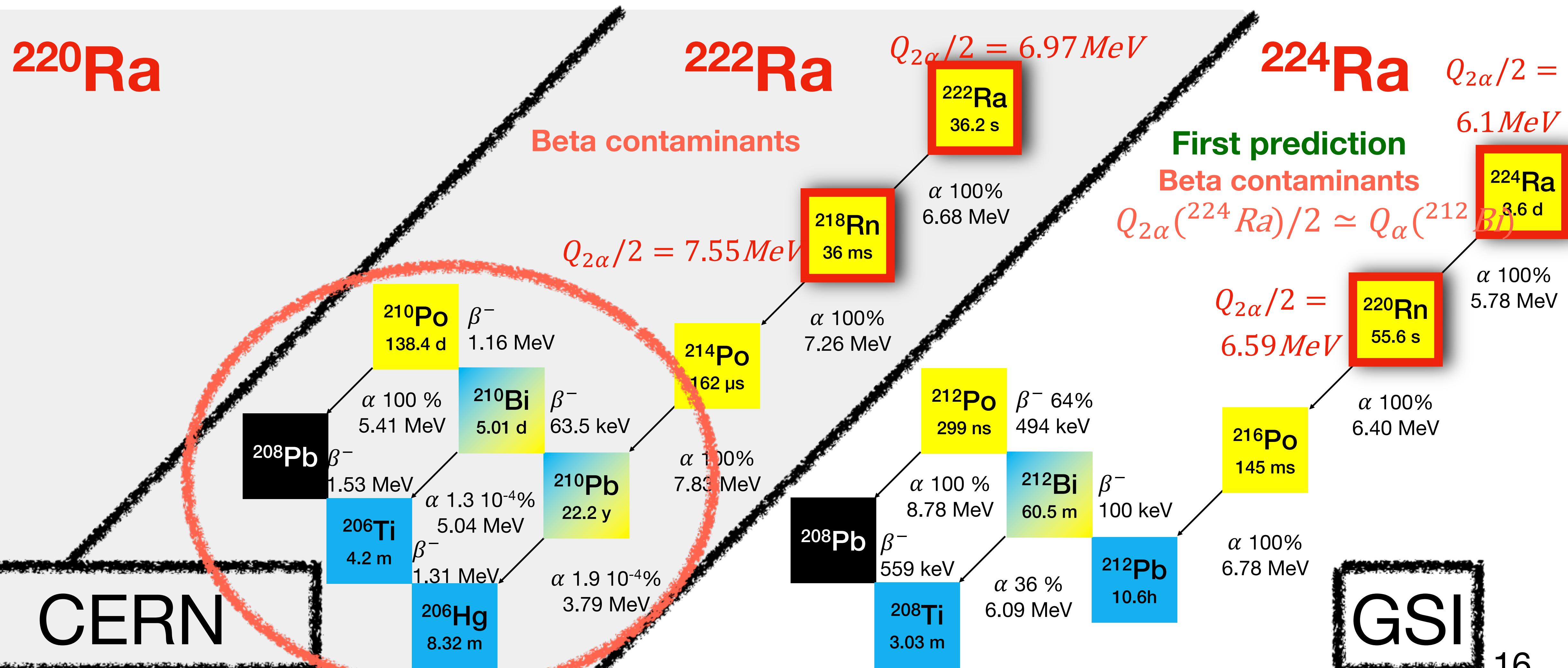
GSI

Experimental search for 2α Decay chains

2α candidate

Alpha emitter

Beta emitter



CERN

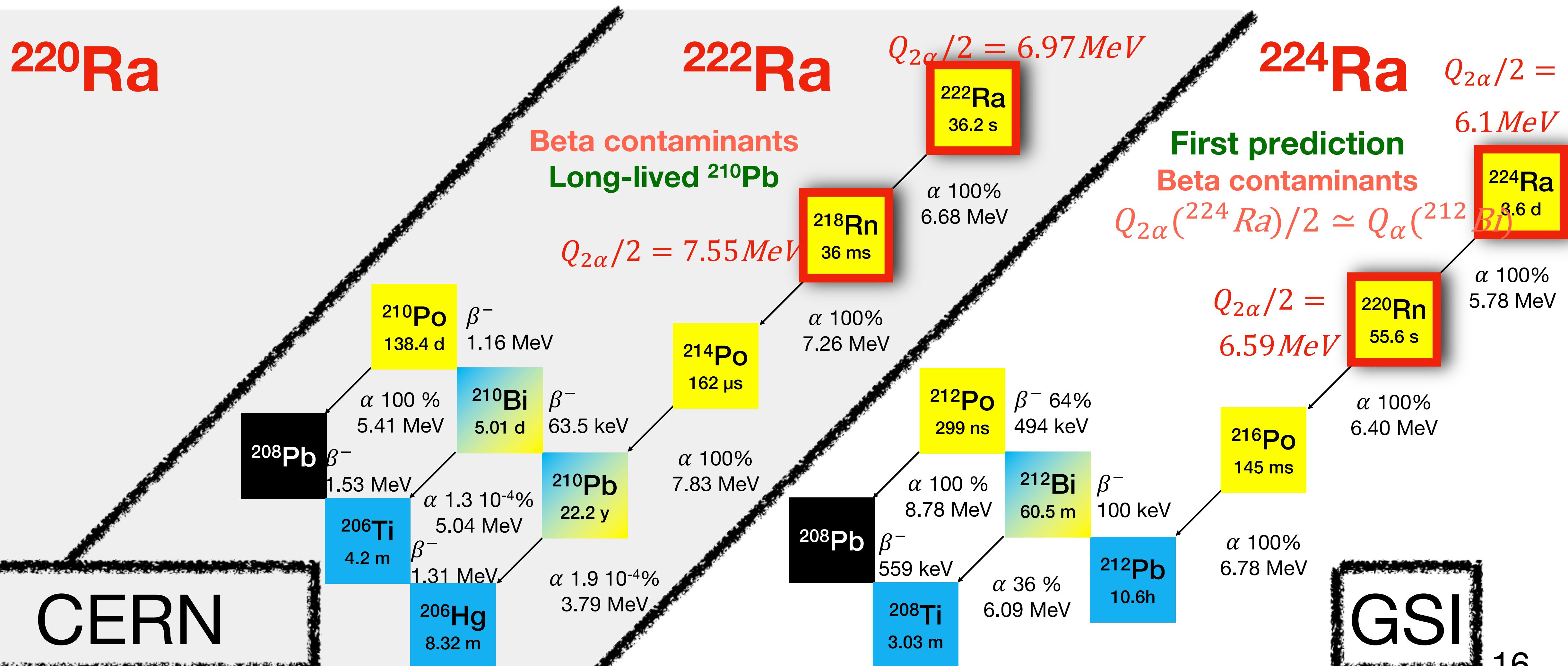
GSI

Experimental search for 2α Decay chains

2α candidate

Alpha emitter

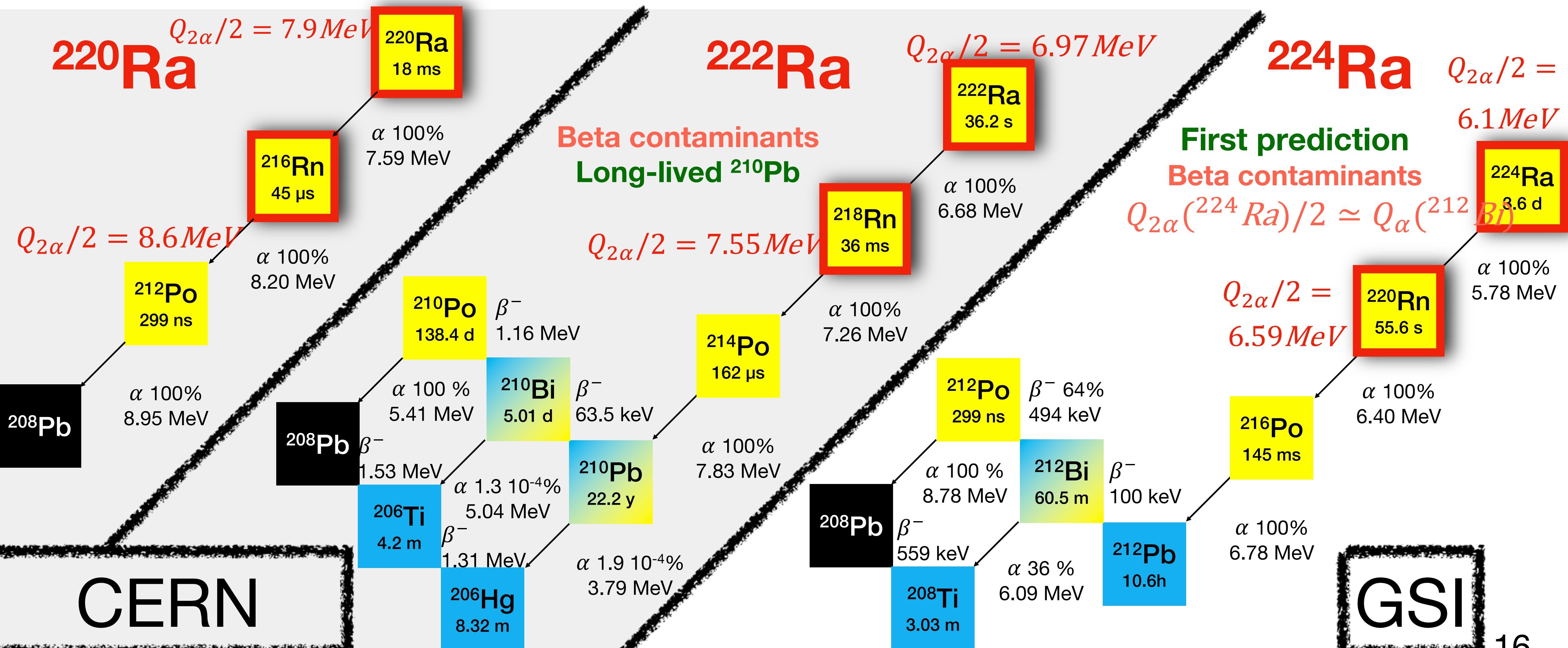
Beta emitter



Experimental search for 2α

Decay chains

■ 2α candidate
 ■ Alpha emitter
■ Beta emitter

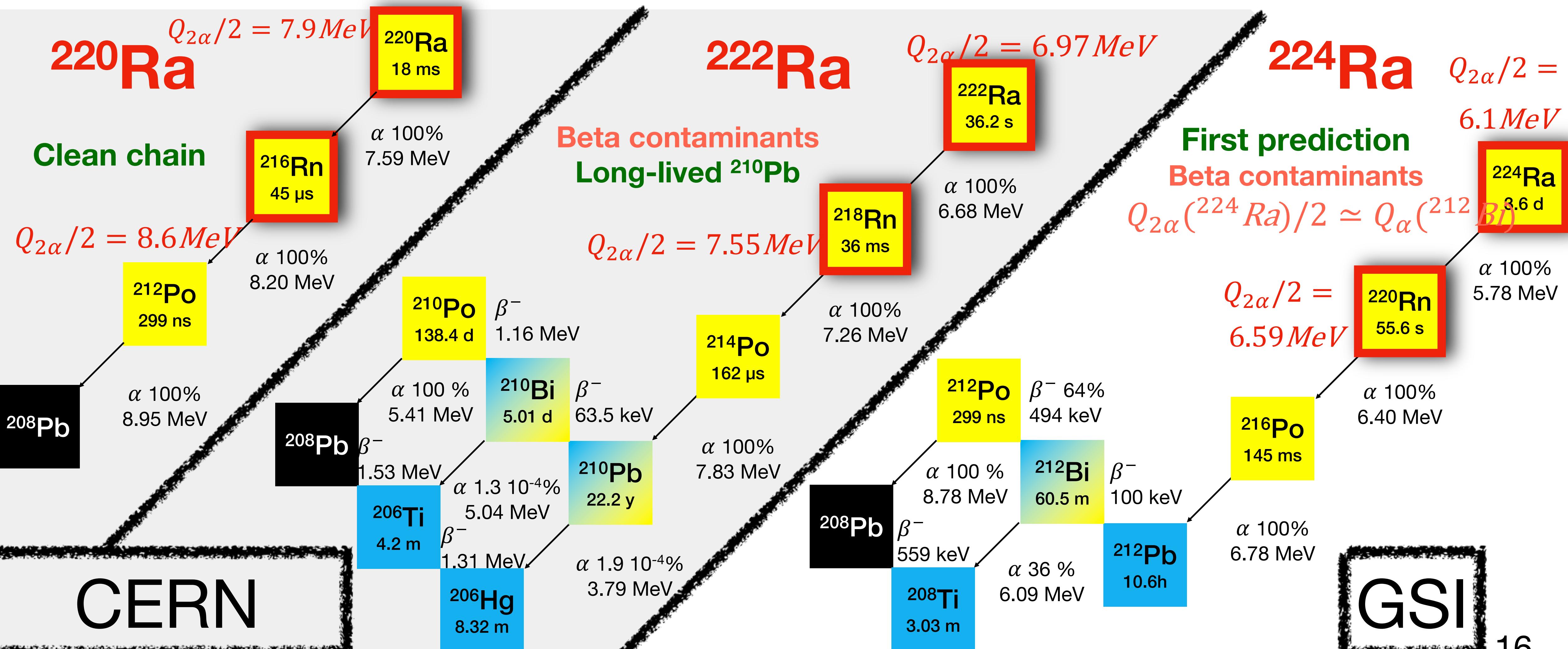


CERN

GSI

Experimental search for 2α

Decay chains

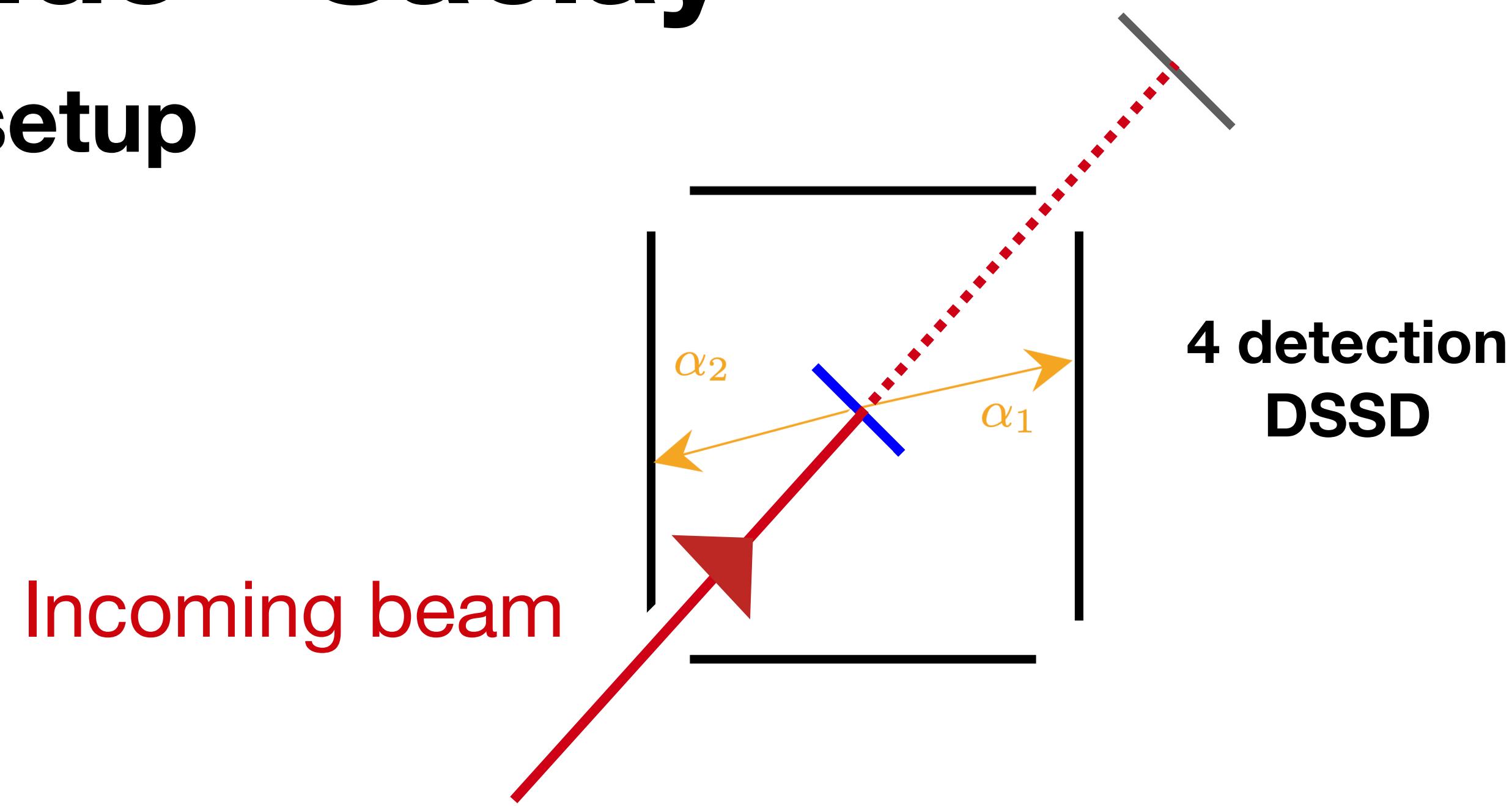


CERN

GSI

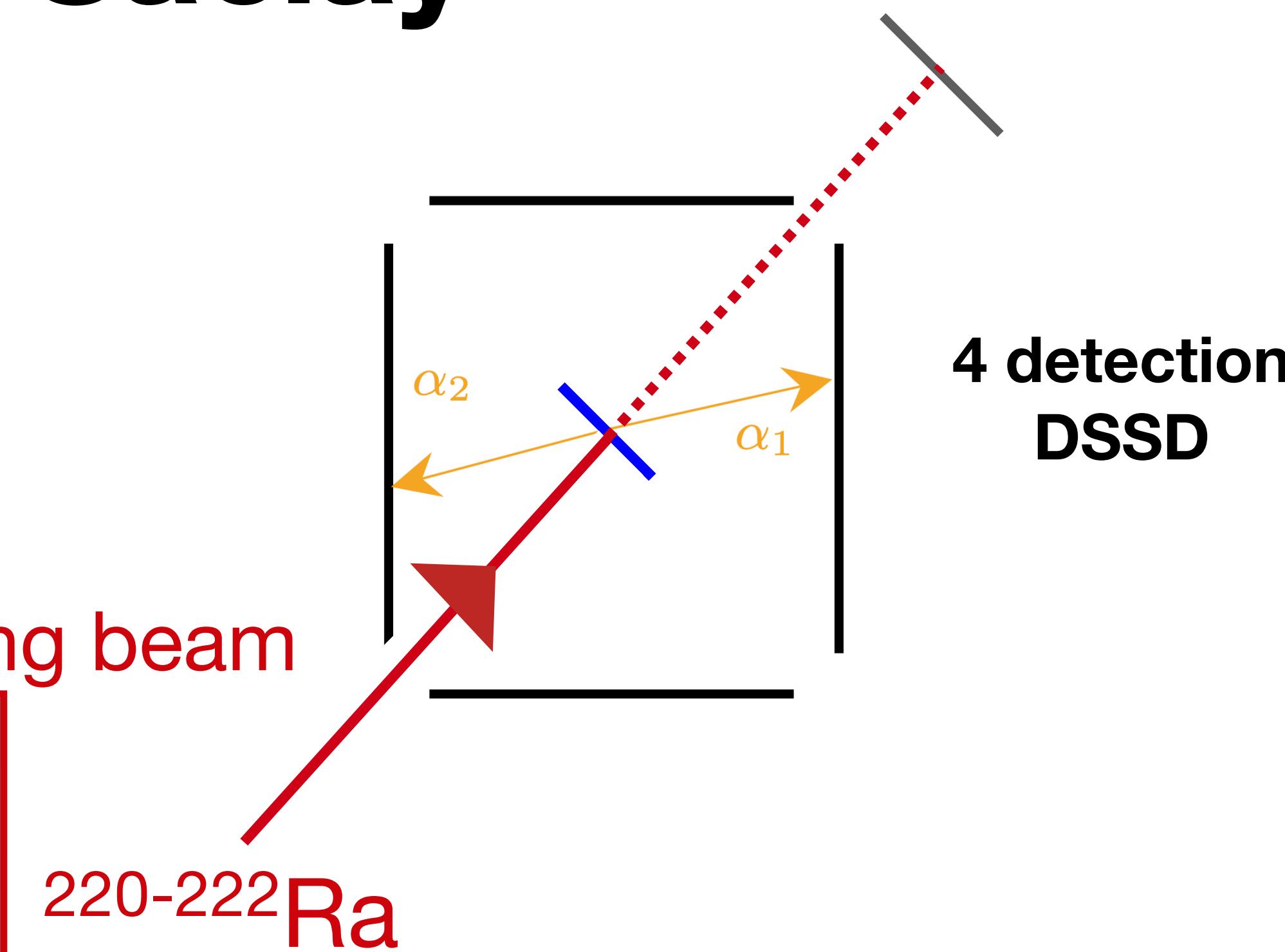
CERN/Isolde - Saclay

Sketch of the setup



CERN/Isolde - Saclay

Sketch of the setup

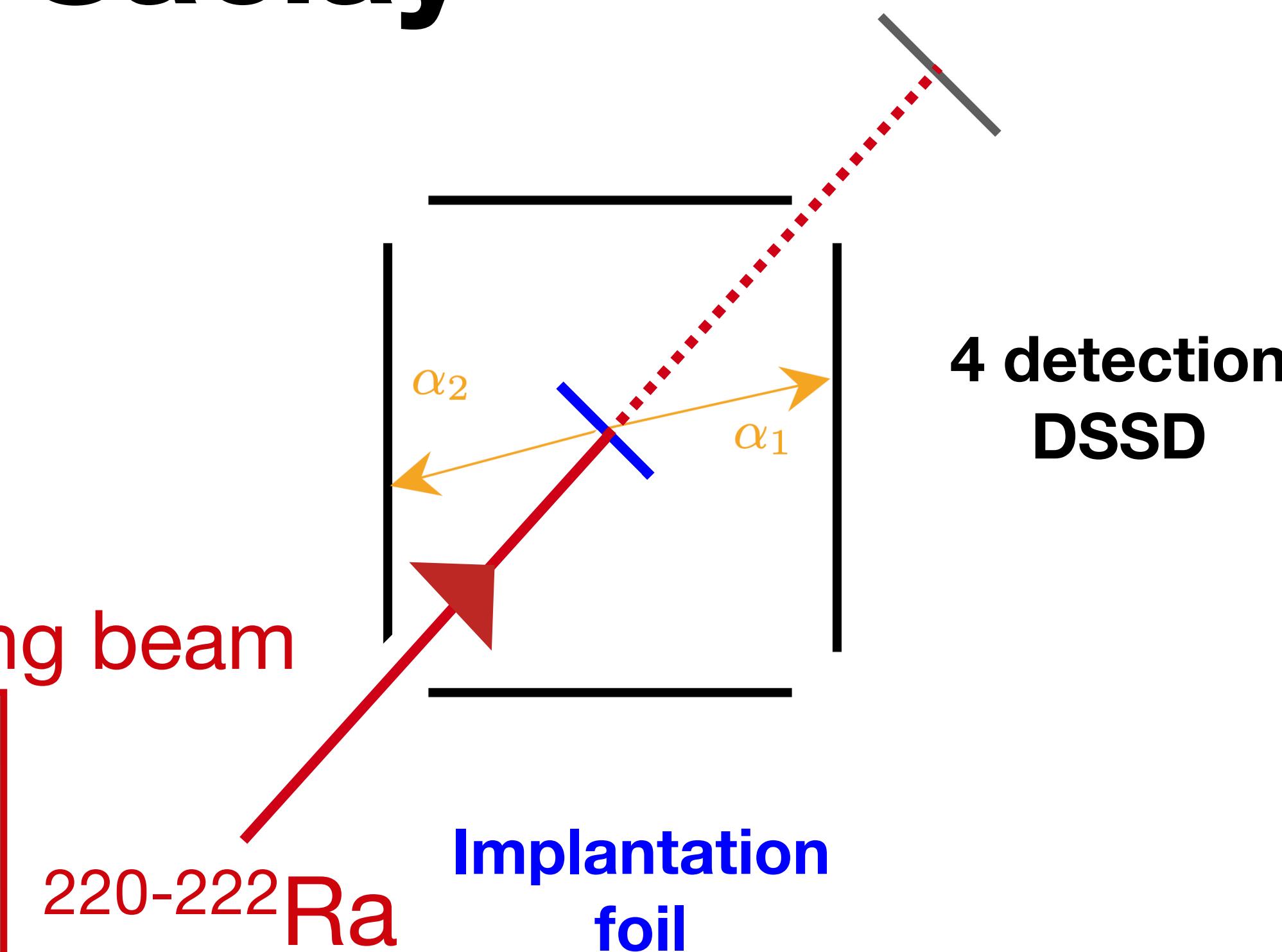


$\sim 2 \cdot 10^4$ pps
30 keV/A
1 week

\sim tens of events
expected

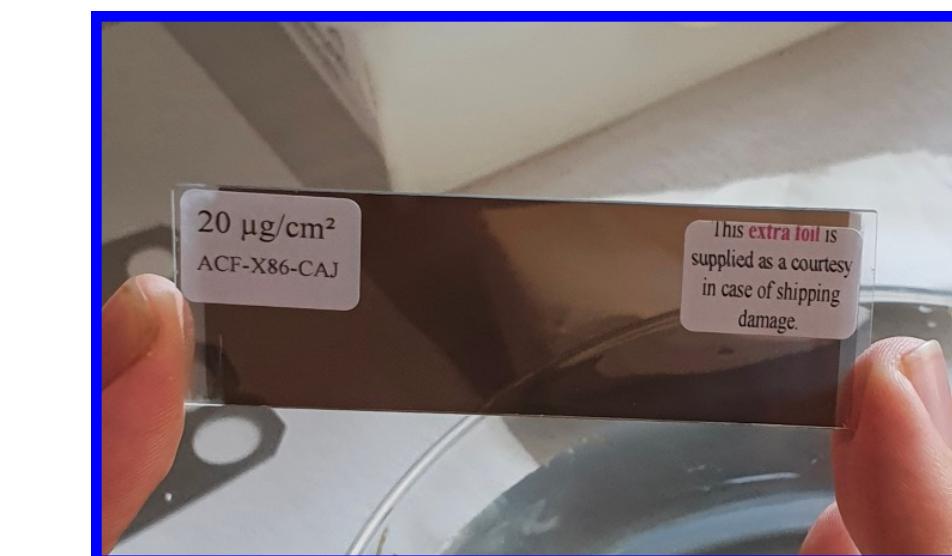
CERN/Isolde - Saclay

Sketch of the setup



$\sim 2 \cdot 10^4$ pps
30 keV/A
1 week

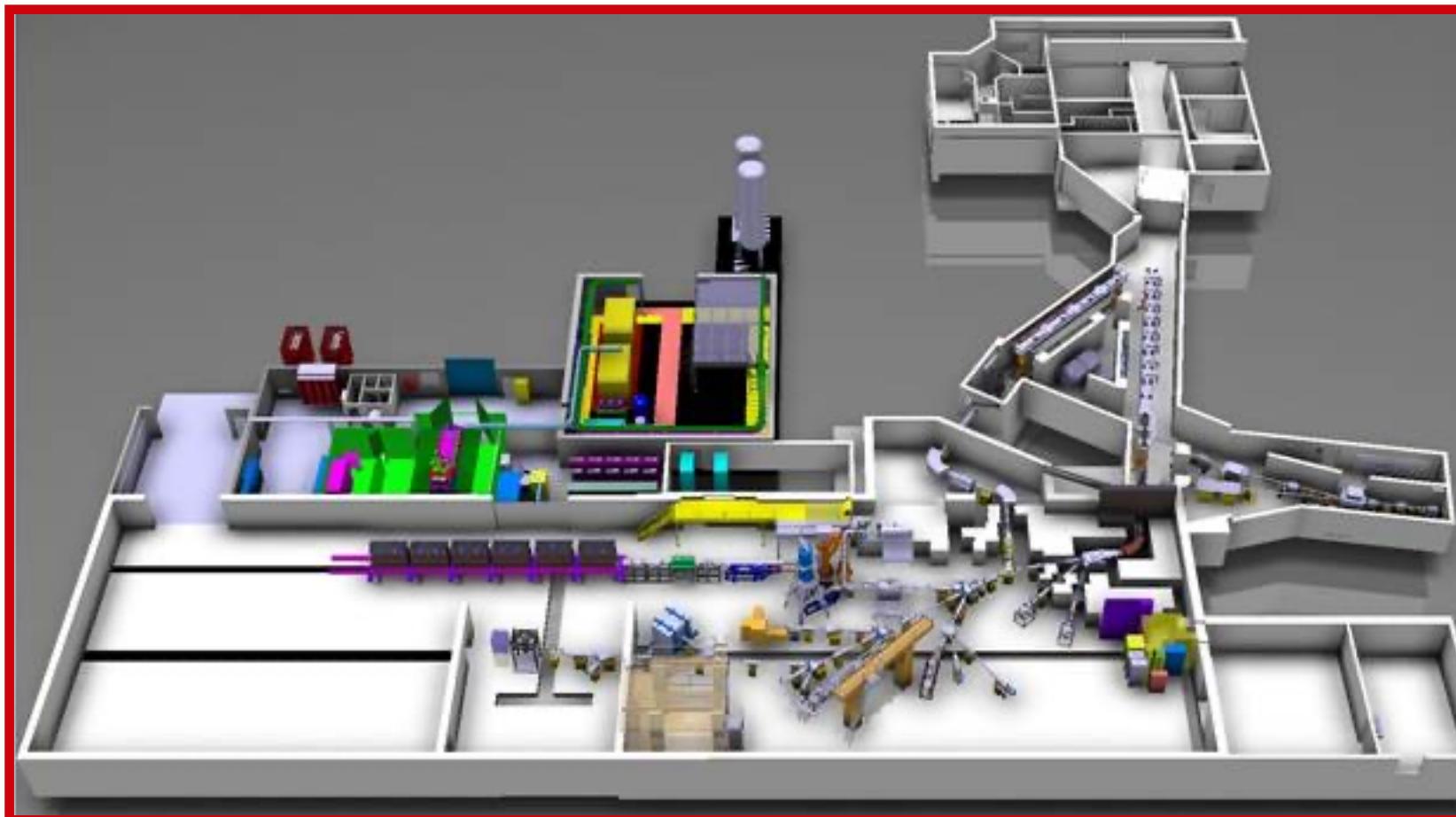
\sim tens of events
expected



$20 \mu\text{g}/\text{cm}^2$ Carbon foil

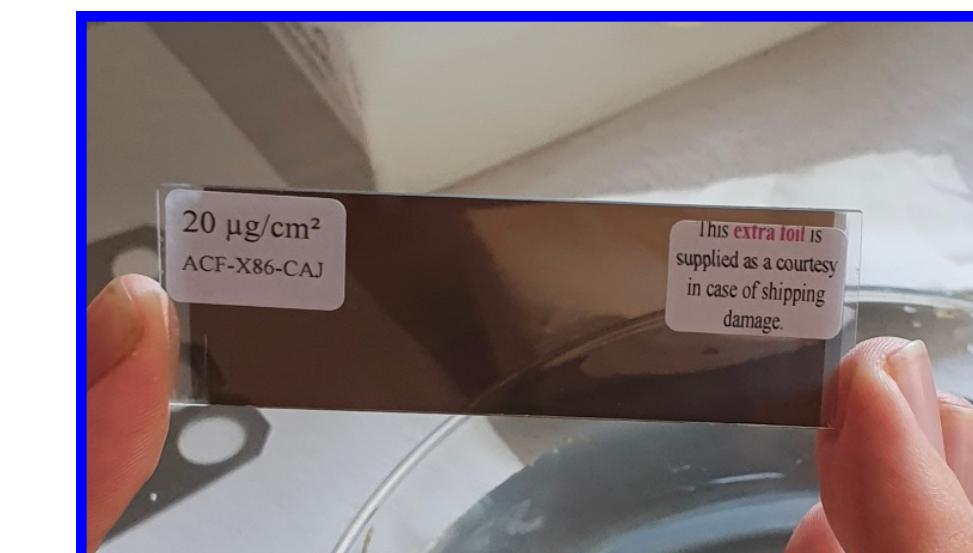
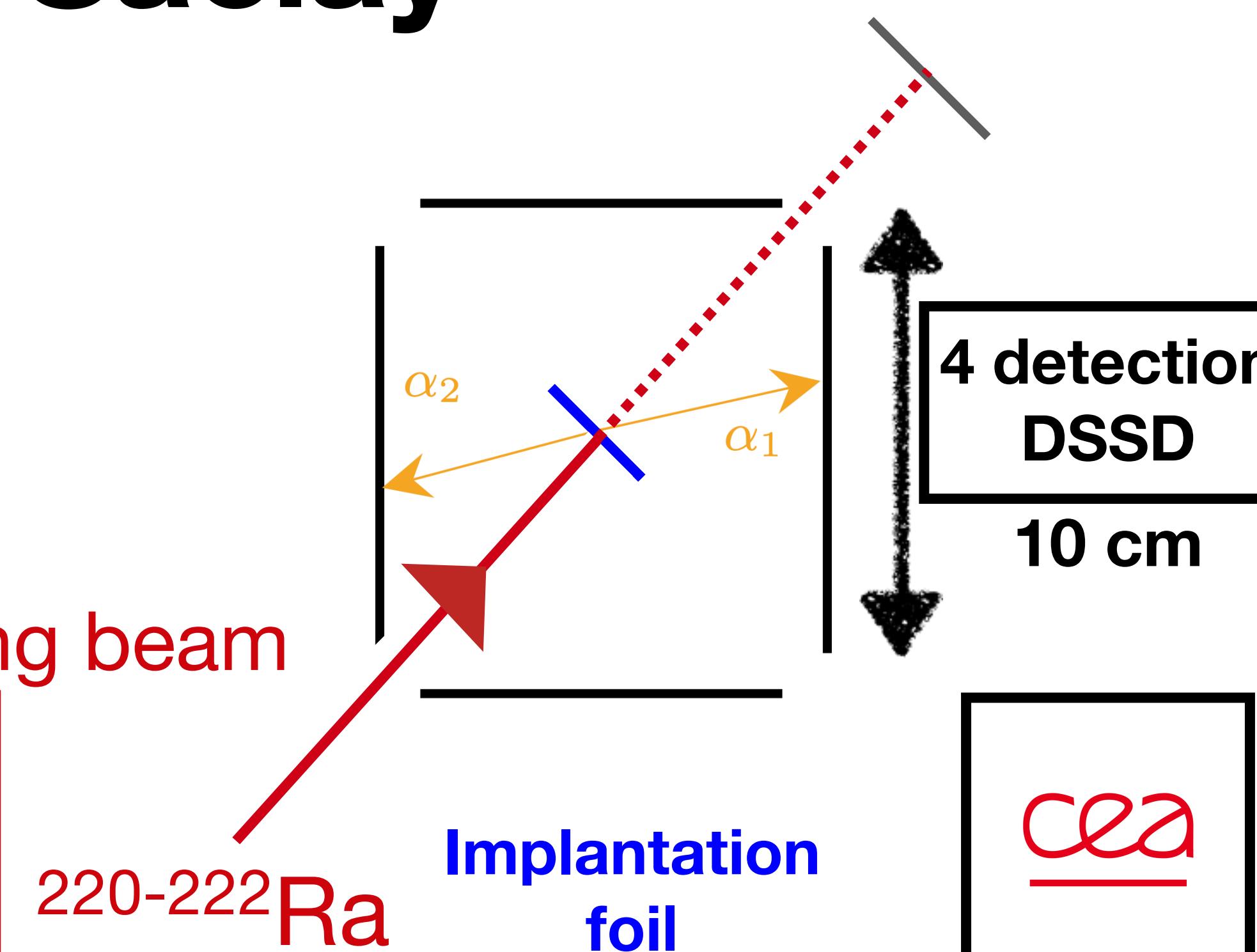
CERN/Isolde - Saclay

Sketch of the setup

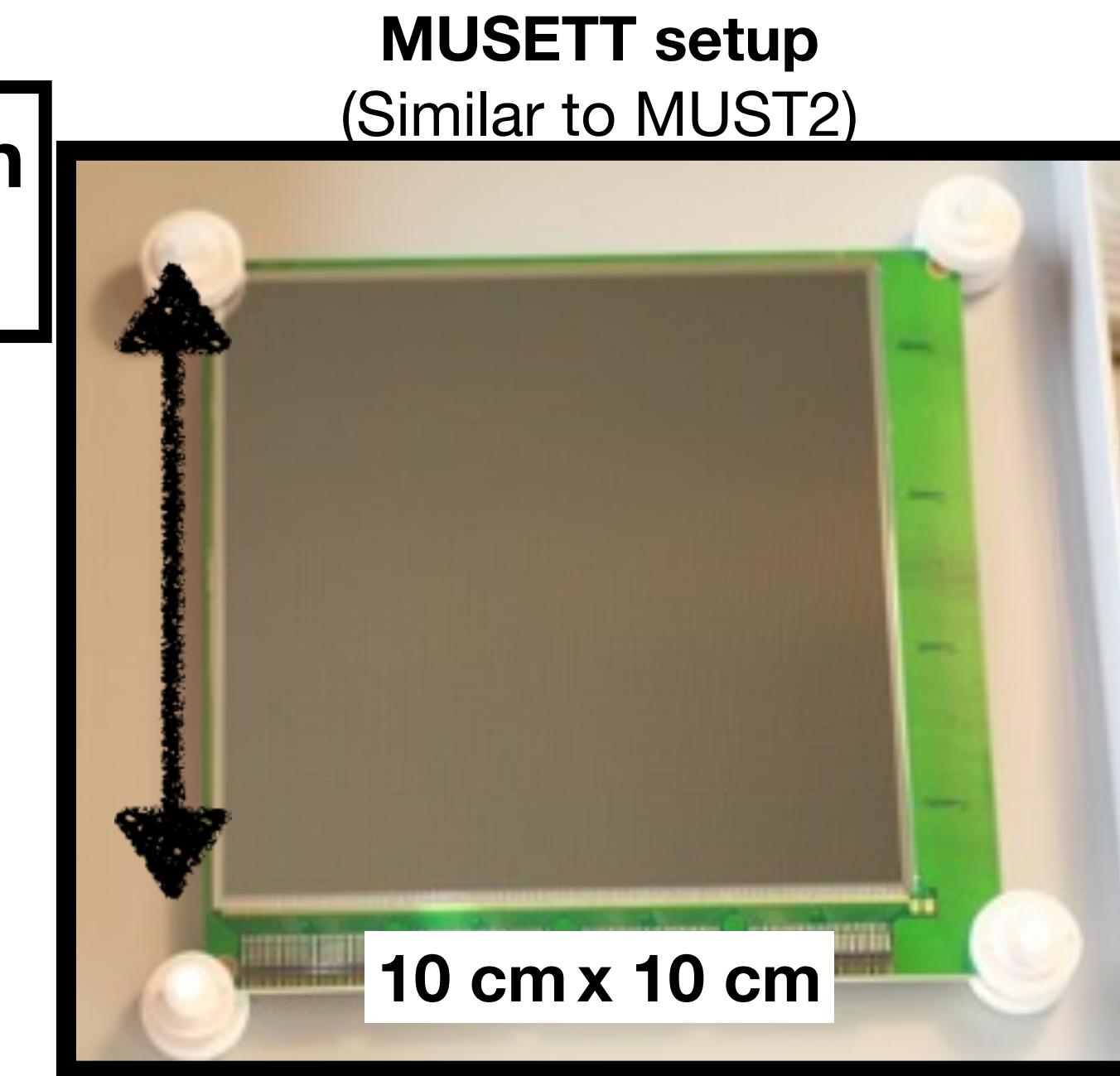


$\sim 2 \cdot 10^4$ pps
30 keV/A
1 week

\sim tens of events
expected



20 $\mu\text{g}/\text{cm}^2$ Carbon foil



MUSSETT setup
(Similar to MUST2)
 $10 \text{ cm} \times 10 \text{ cm}$
128 + 128 strips
Electronics & DAQ by GANIL & IJCLab

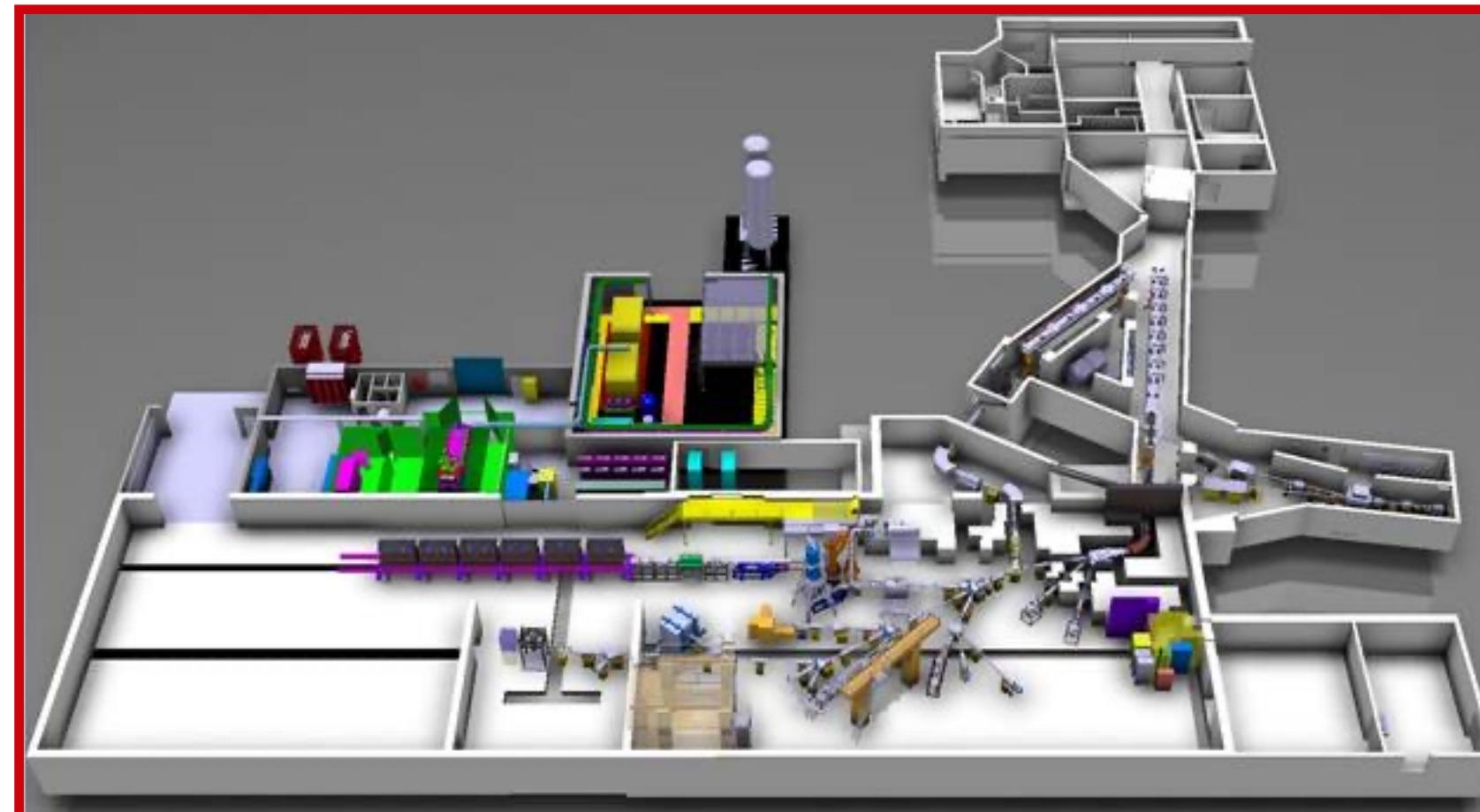
Back-to-back spatial coincidence

CERN/Isolde - Saclay

Sketch of the setup

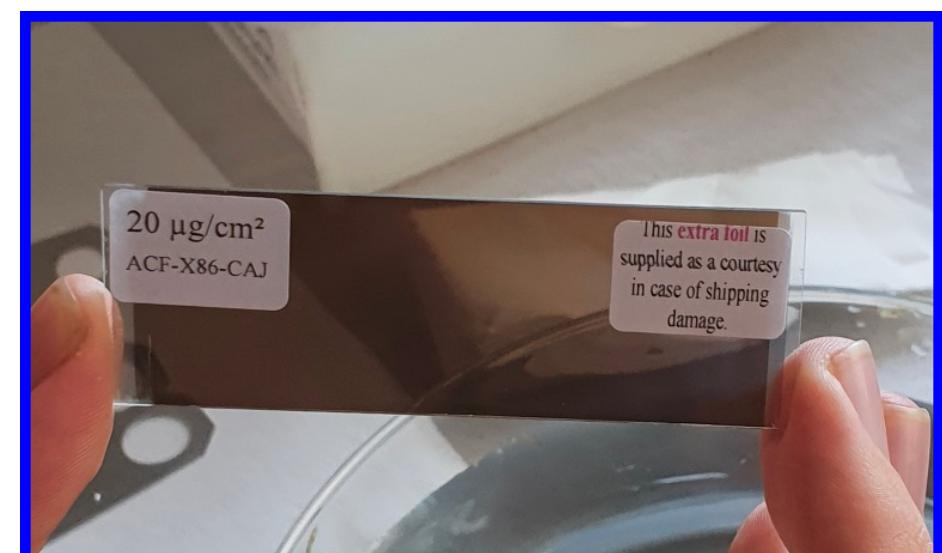
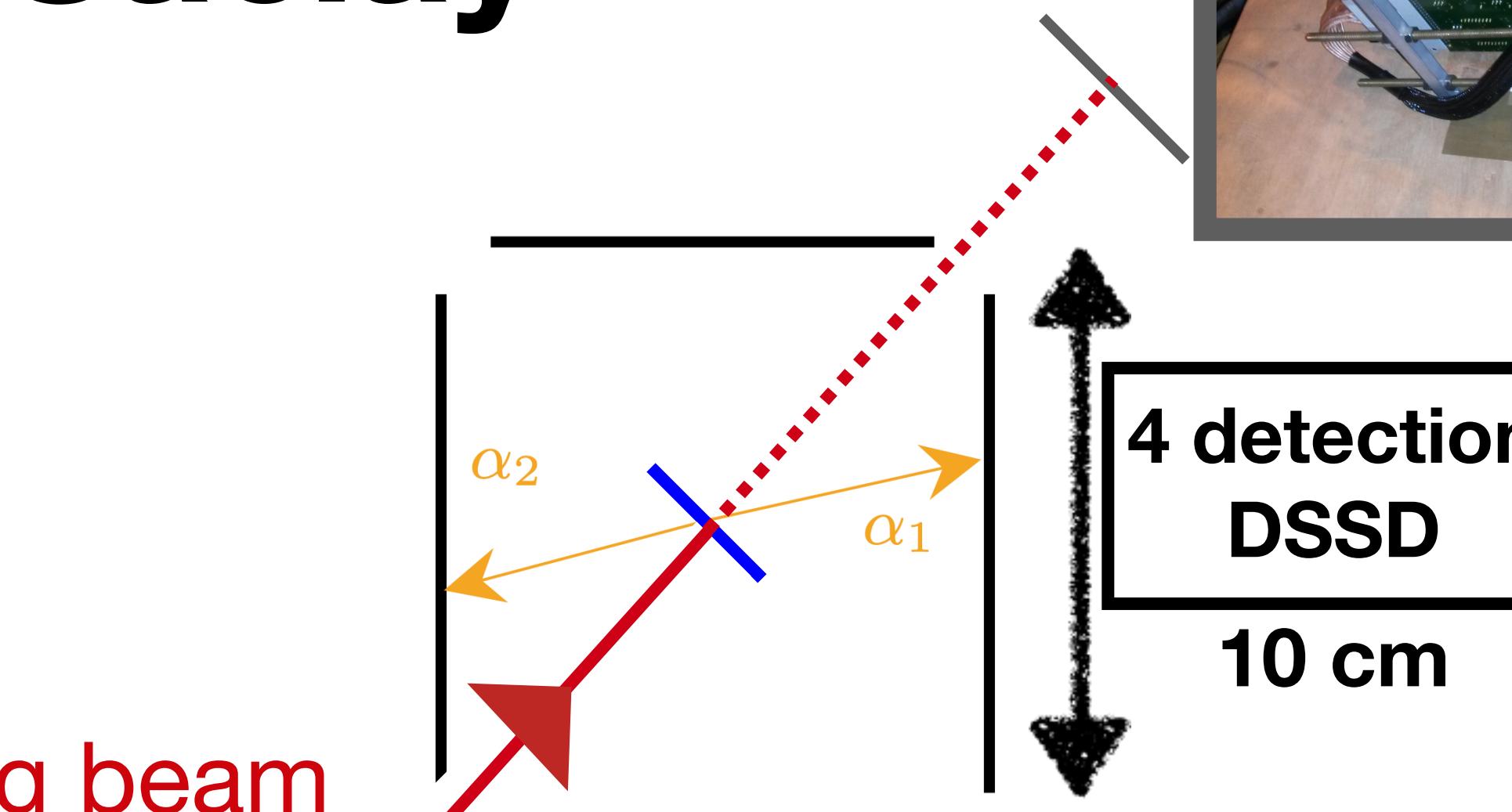


Beam
inspection
DSSD

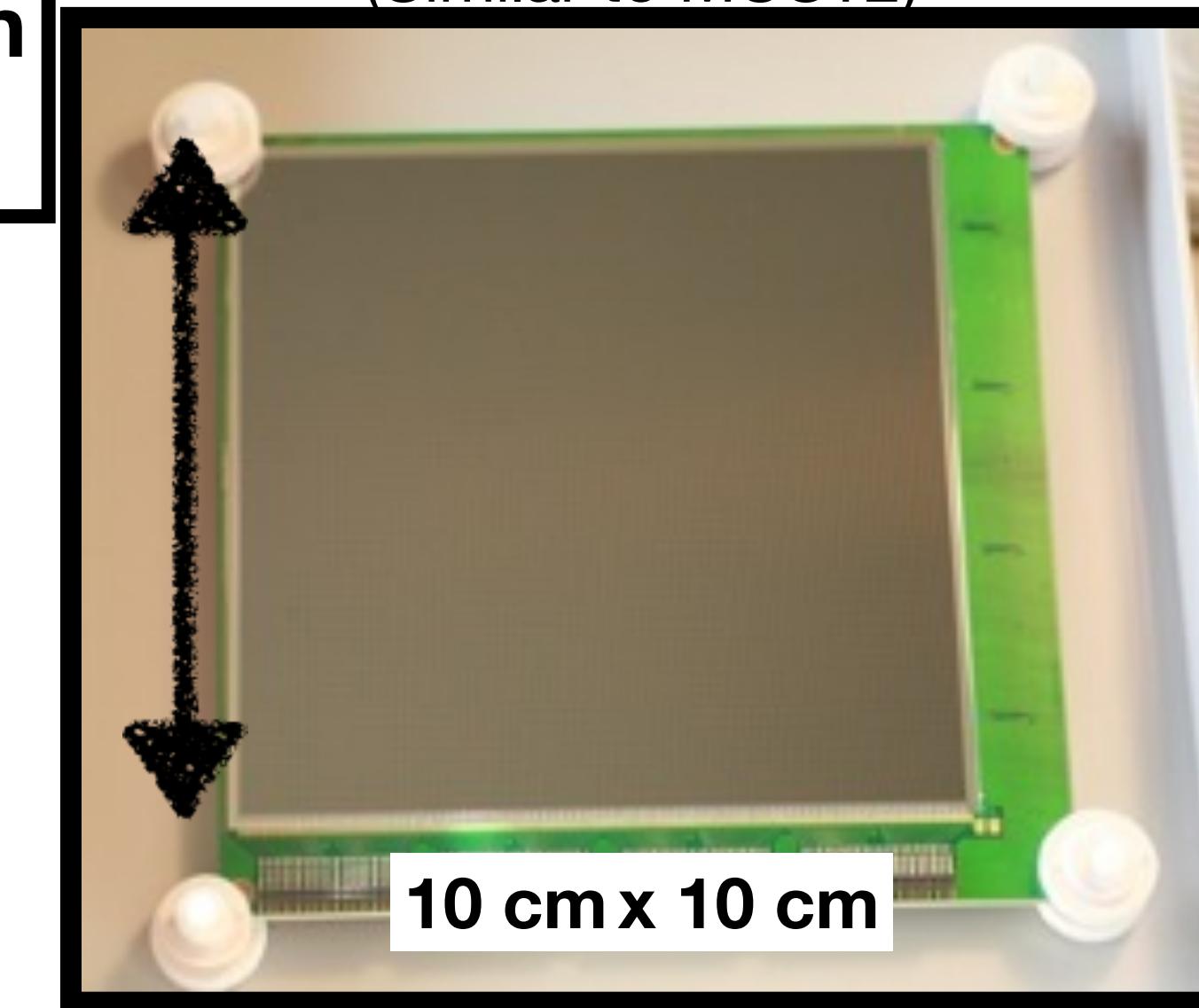


$\sim 2 \cdot 10^4$ pps
30 keV/A
1 week

\sim tens of events
expected



$20 \mu\text{g}/\text{cm}^2$ Carbon foil

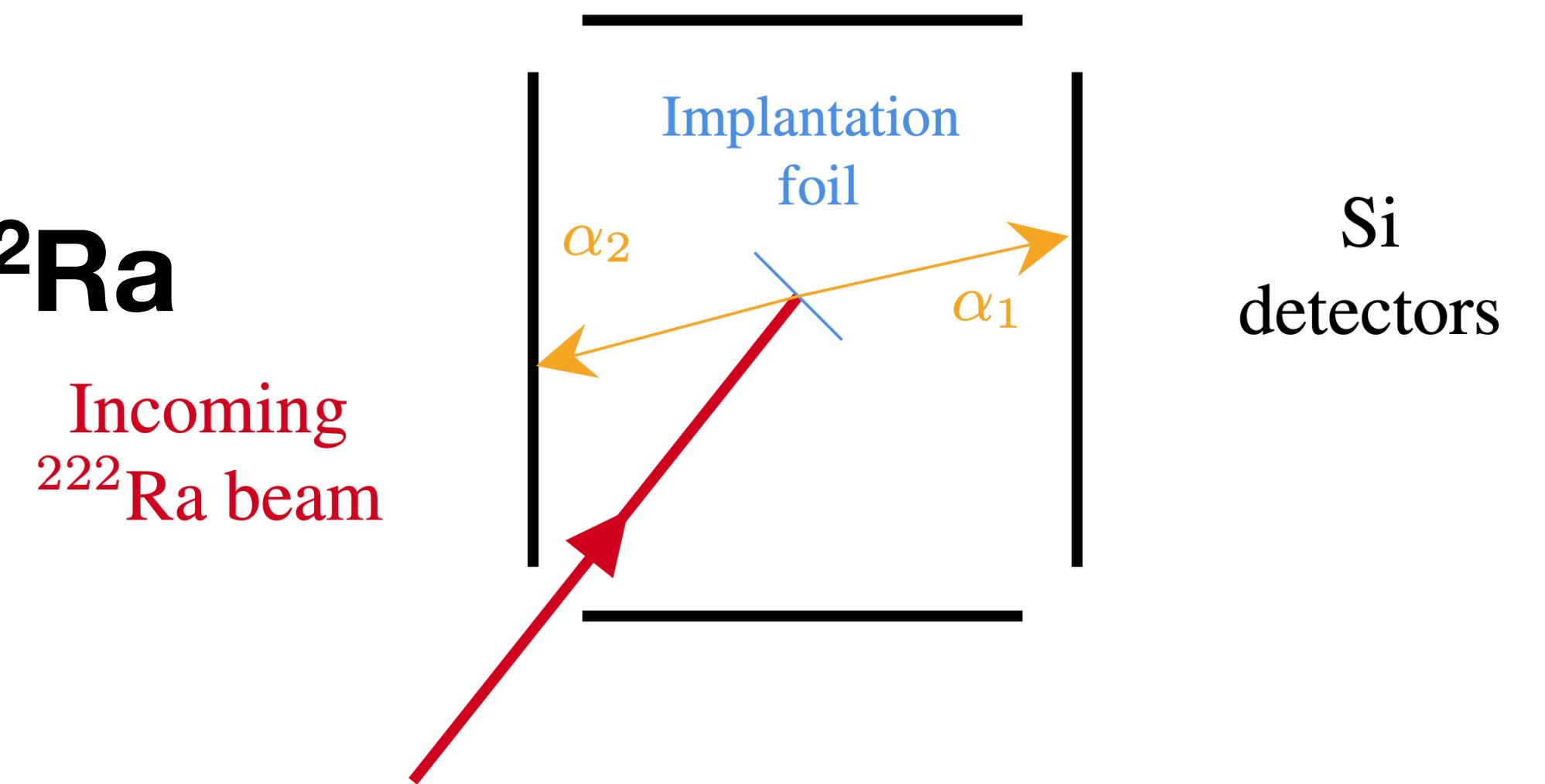


10 cm x 10 cm
128 + 128 strips
Electronics & DAQ by GANIL & IJCLab

Back-to-back spatial coincidence

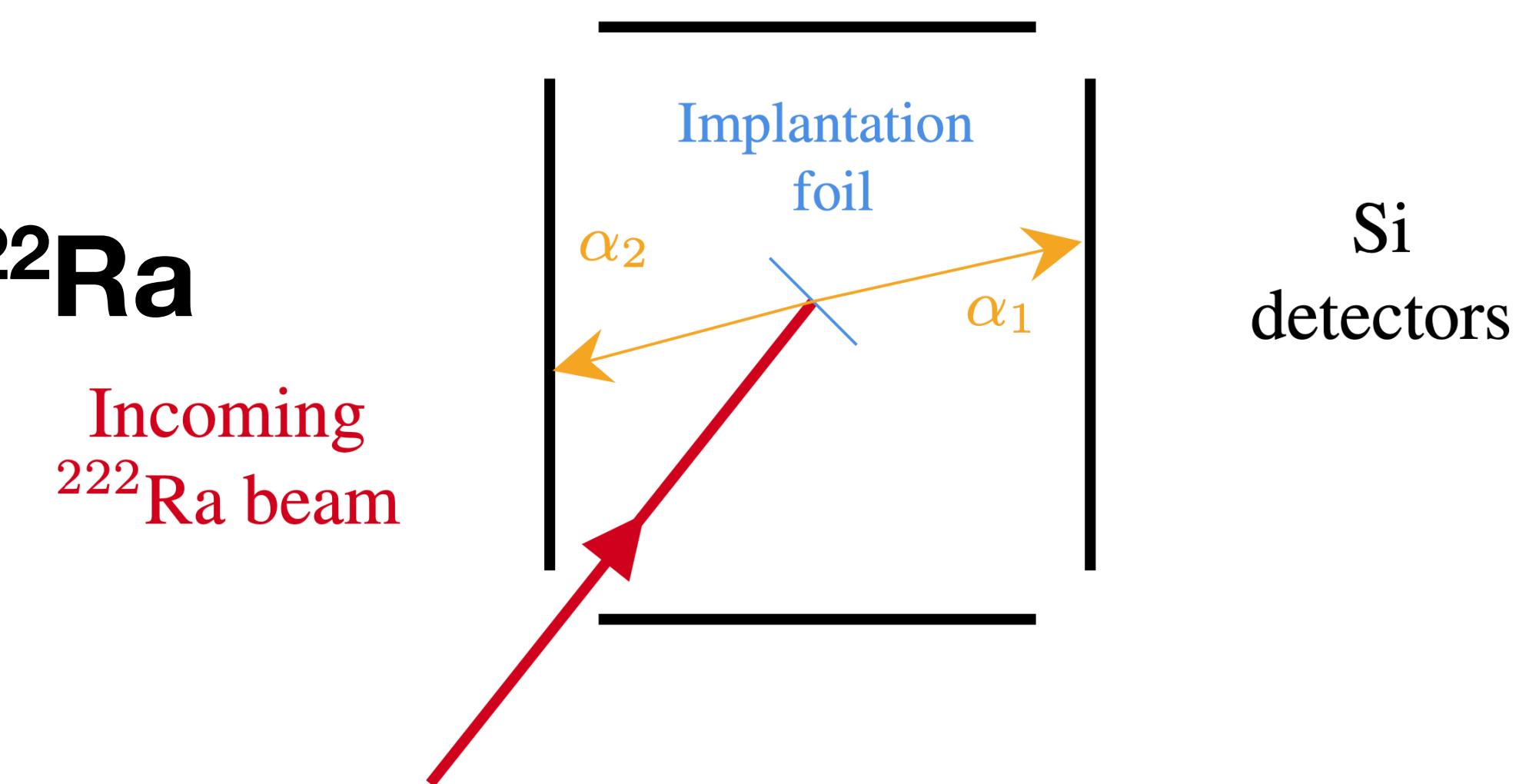
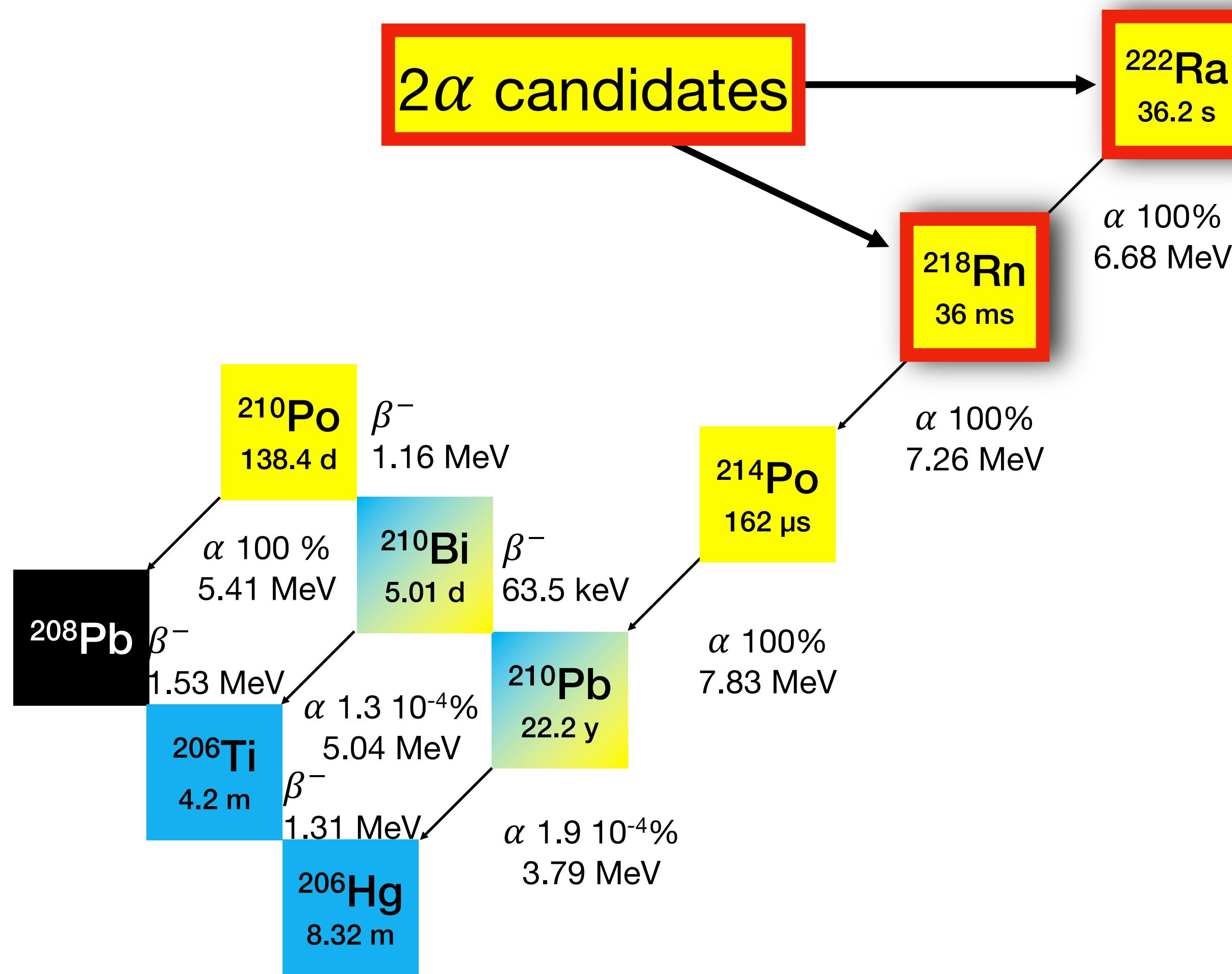
CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra



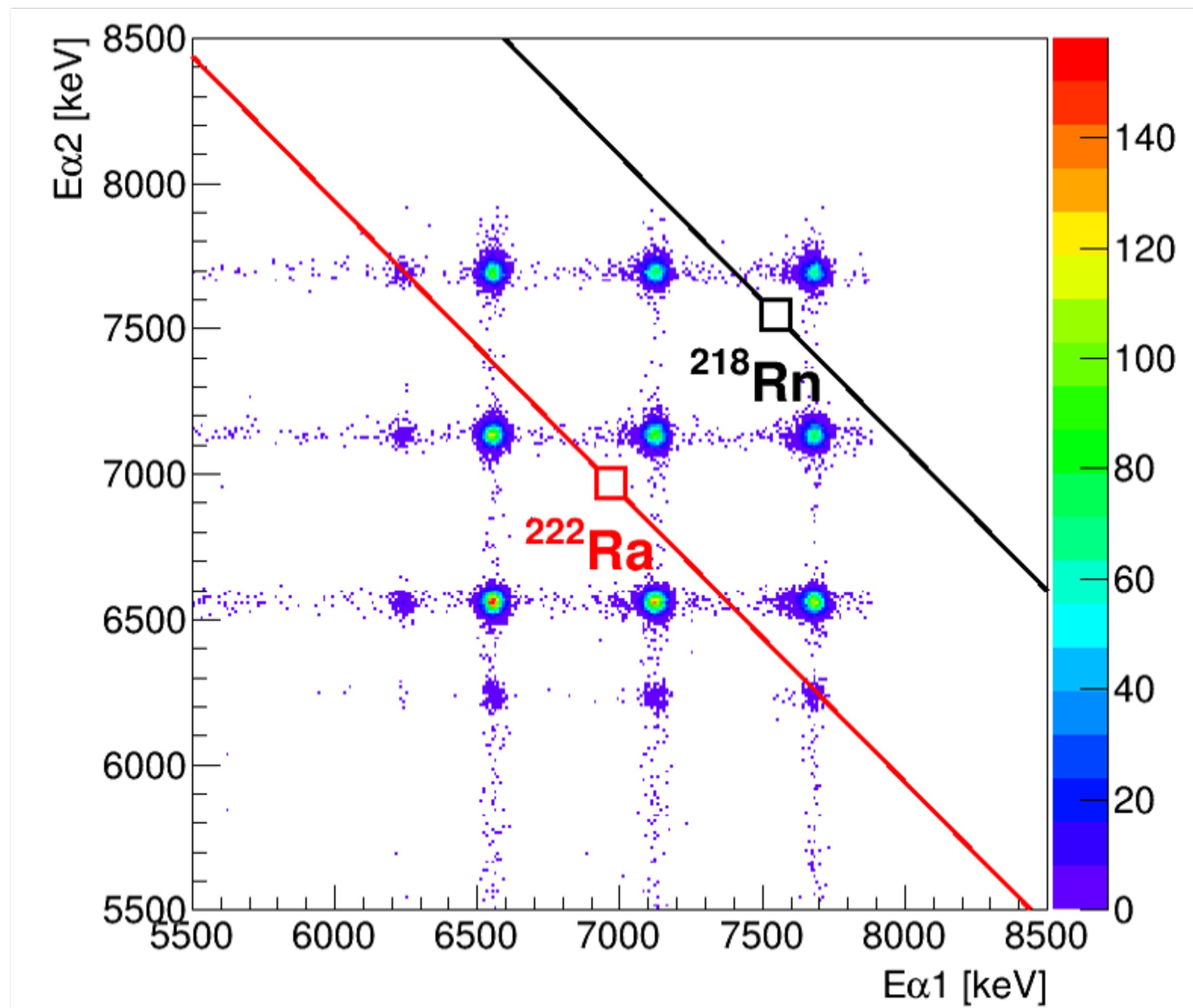
CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra

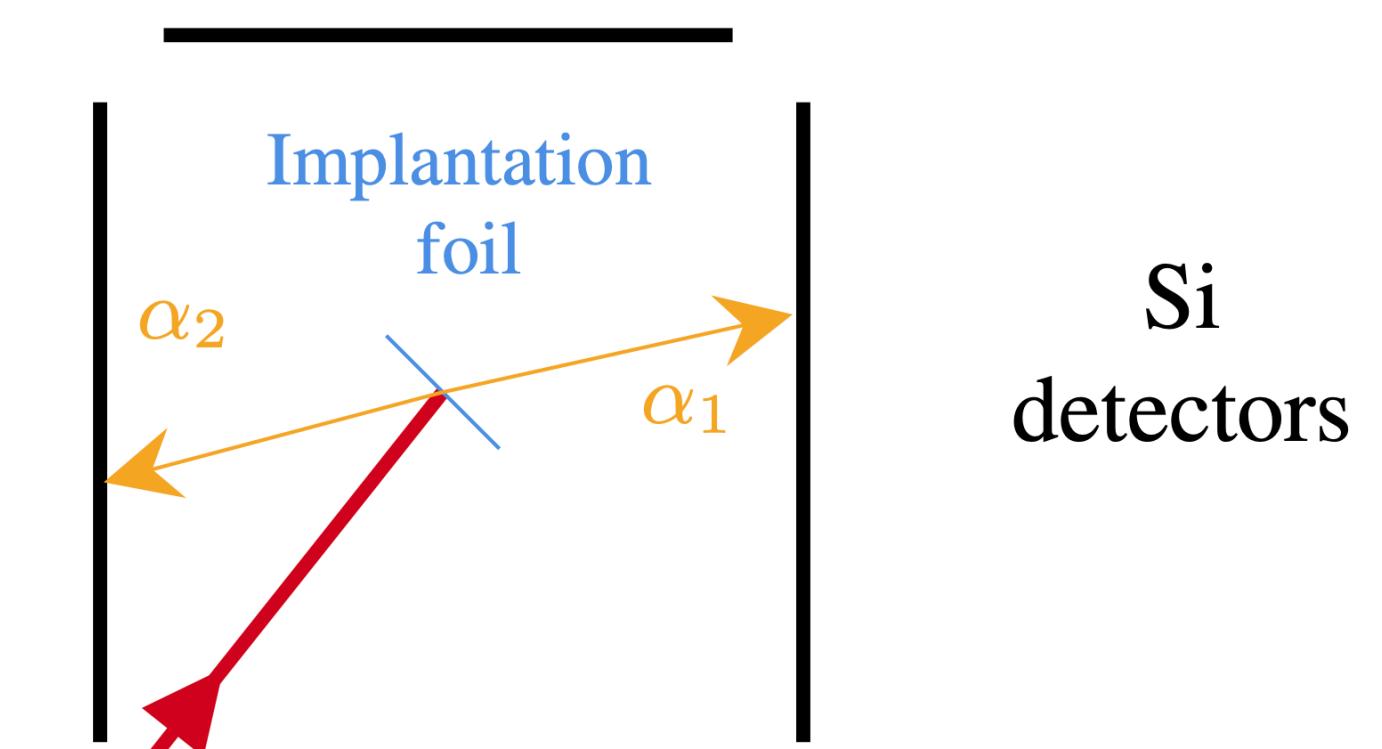


CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra

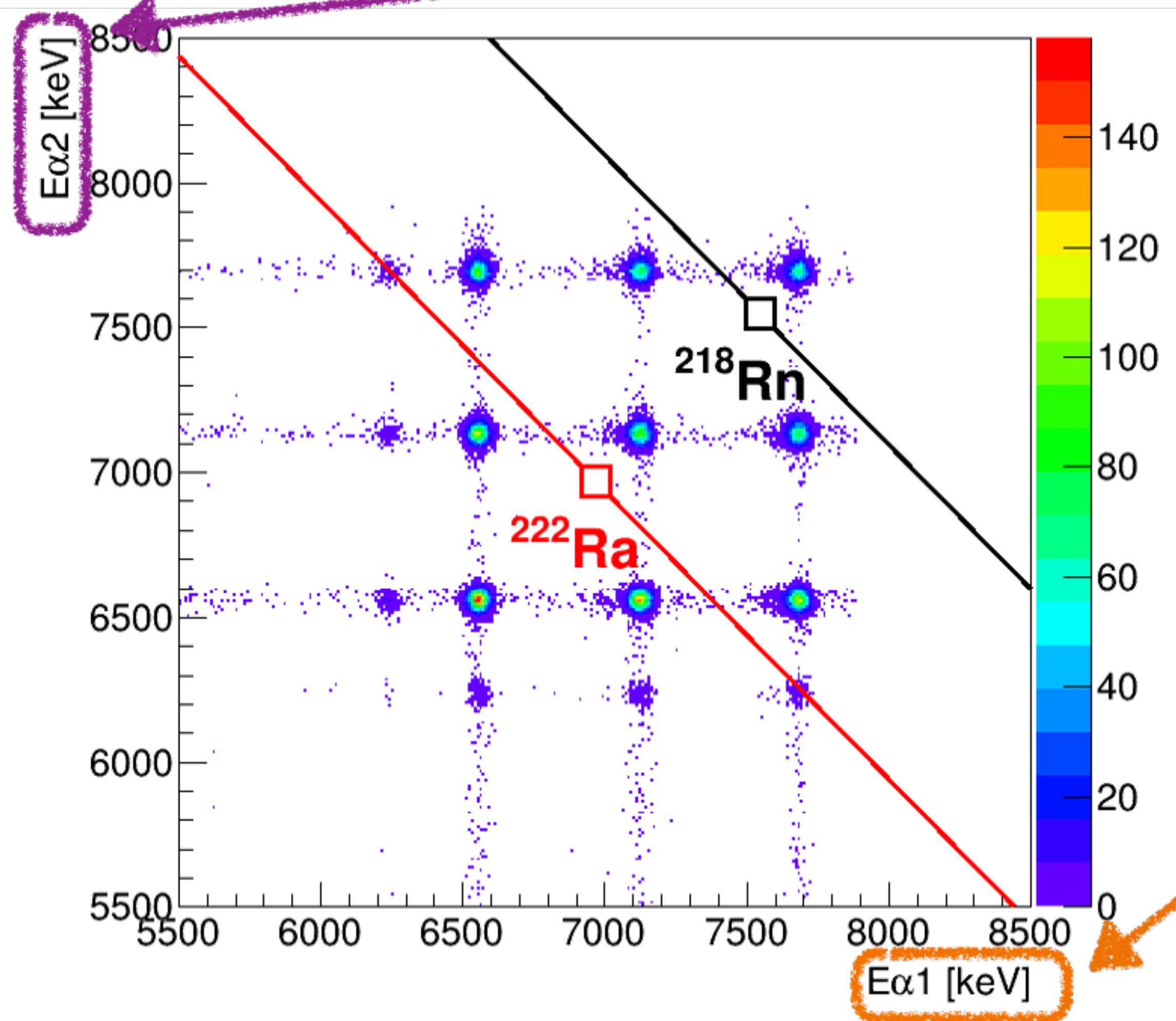


Spatial cut :
Back-to-Back emission
(+ time cuts)



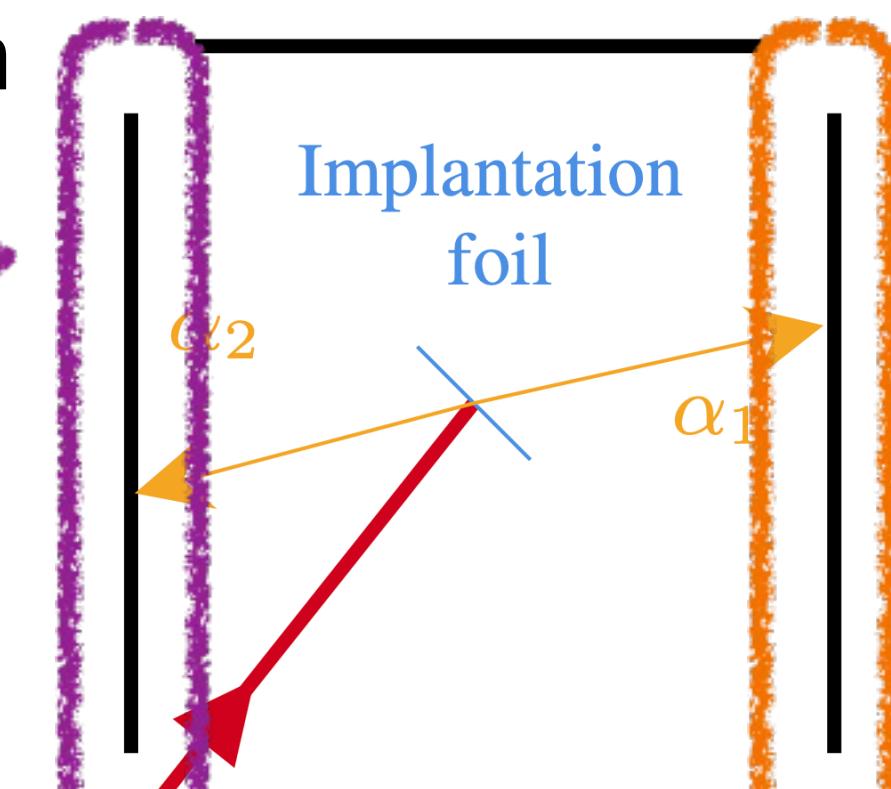
CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra



Spatial cut :

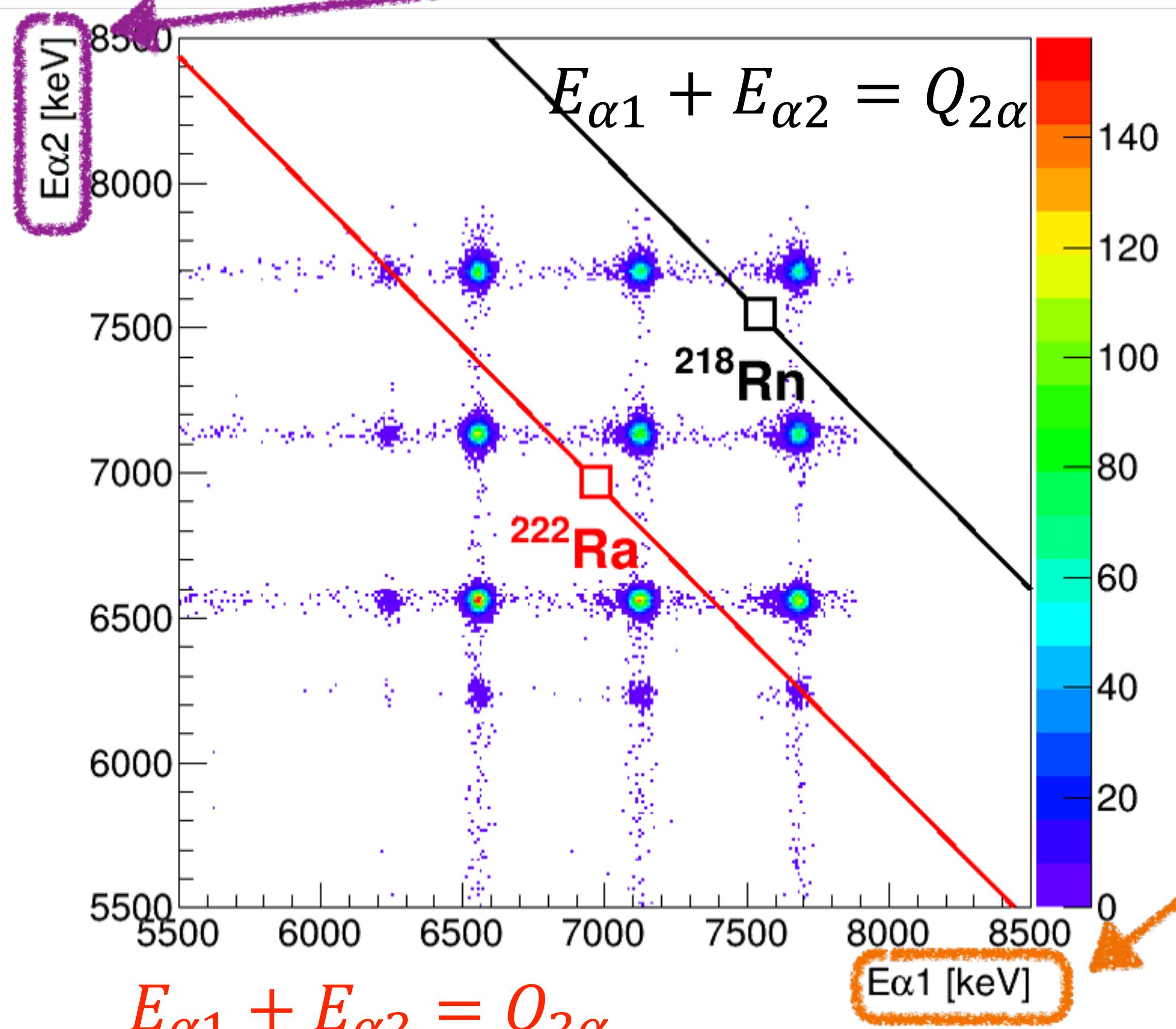
Back-to-Back emission
(+ time cuts)



Si
detectors

CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra



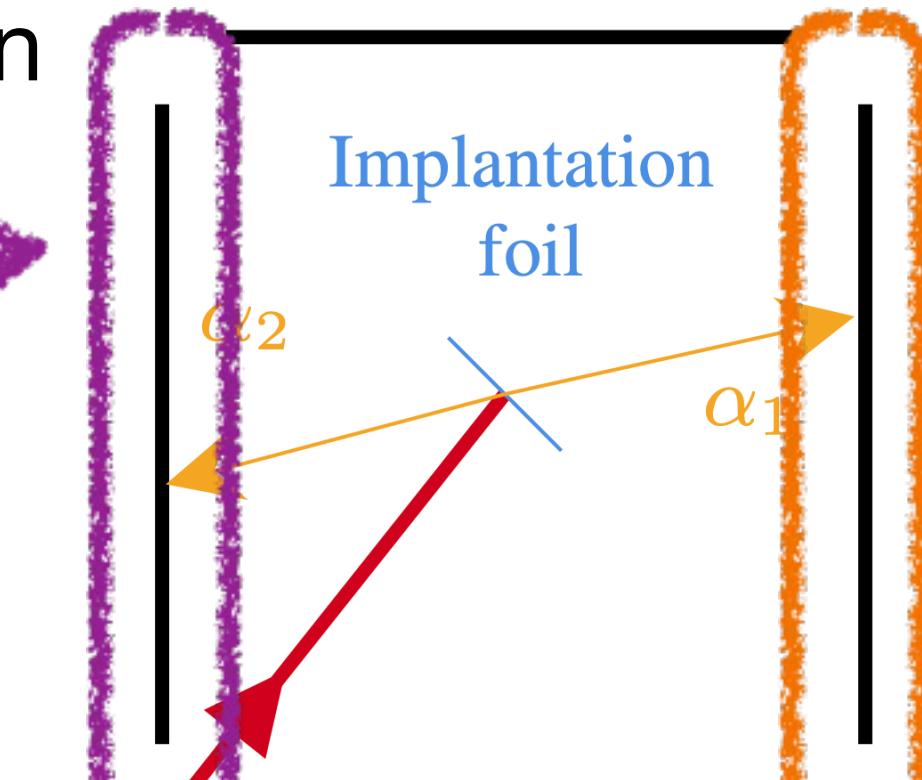
Spatial cut :

Back-to-Back emission
(+ time cuts)

Incoming
 ^{222}Ra beam

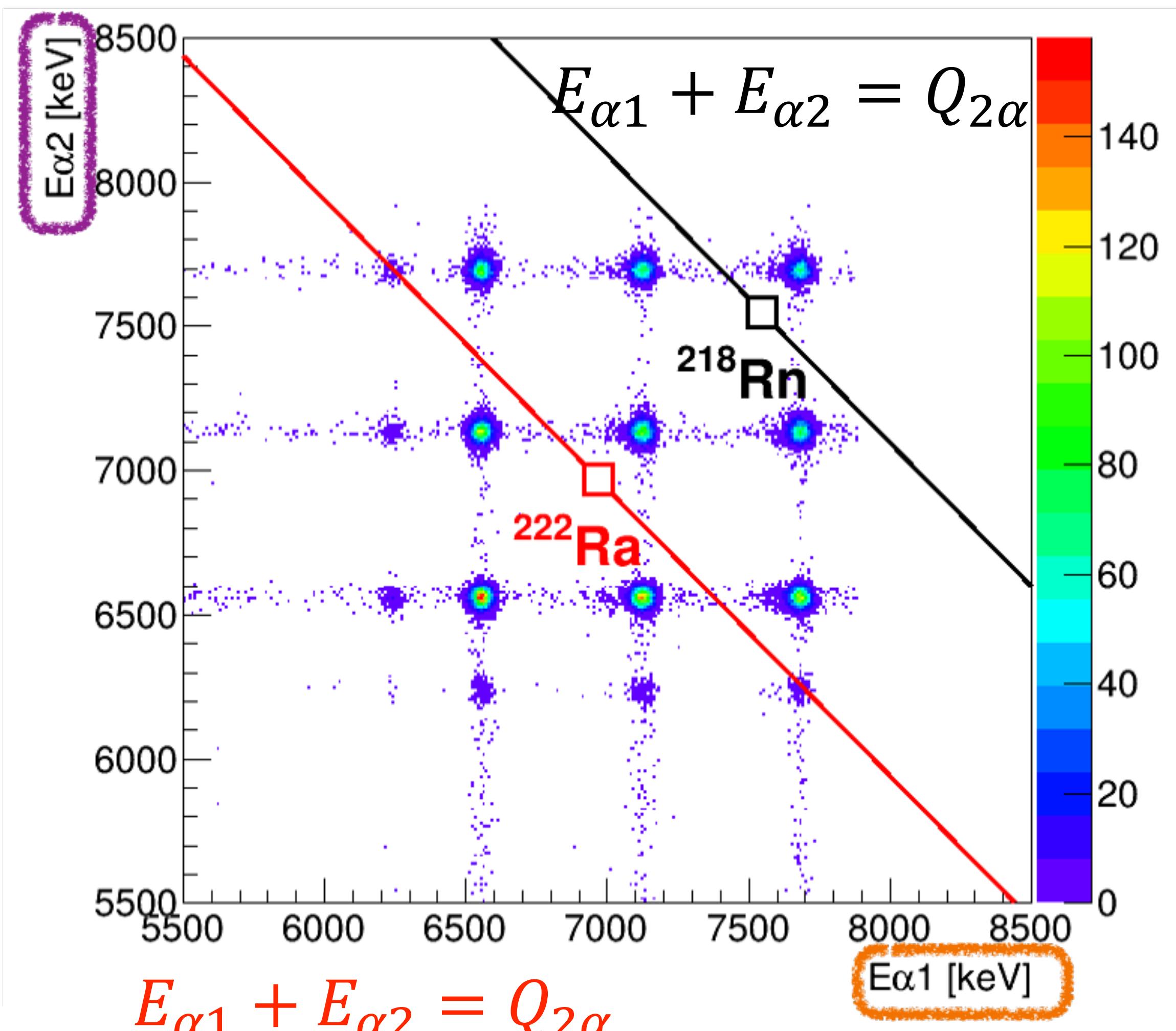
Implantation
foil

Si
detectors



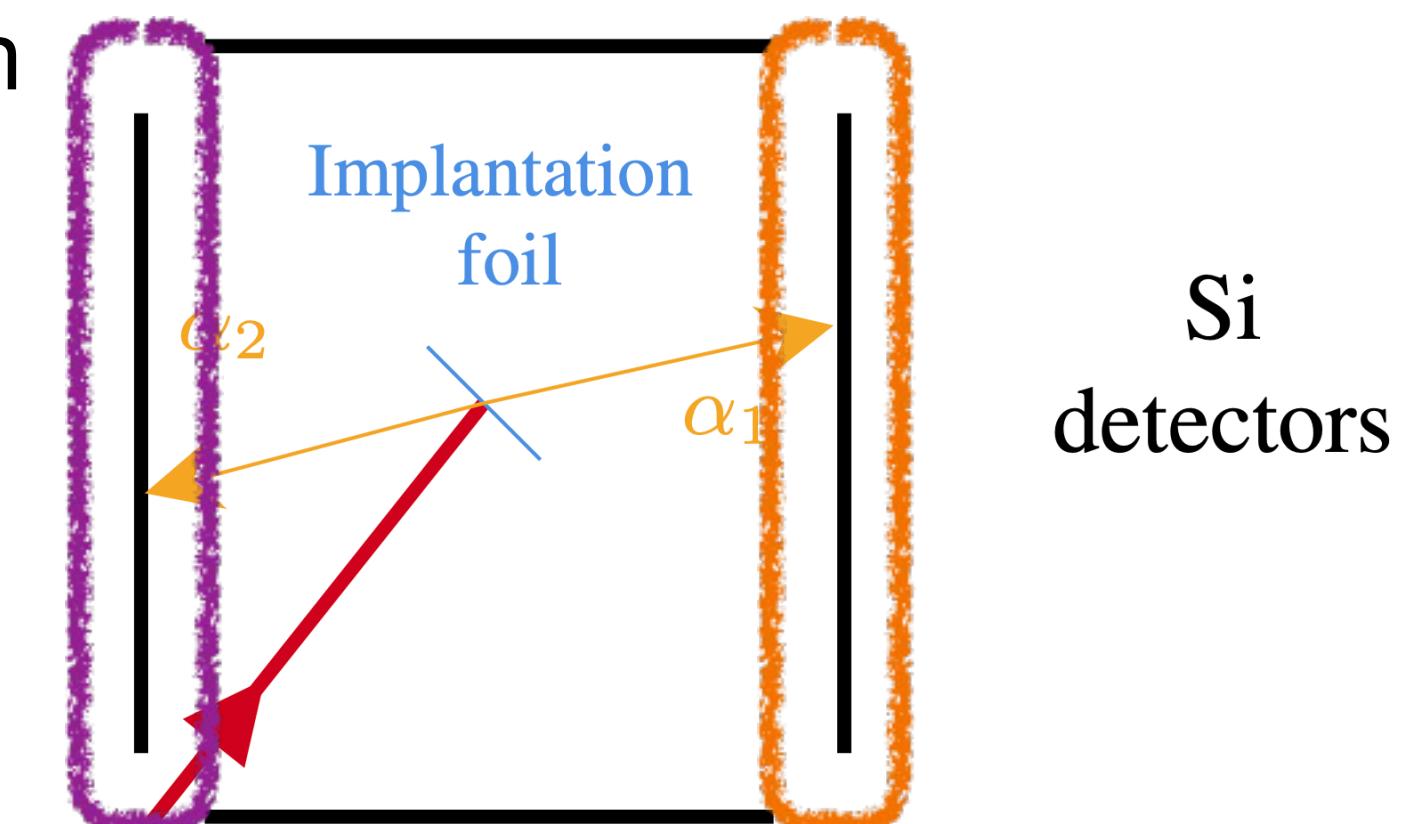
CERN/Isolde - Saclay

Simulation for background estimate- ^{222}Ra



Spatial cut :

Back-to-Back emission
(+ time cuts)

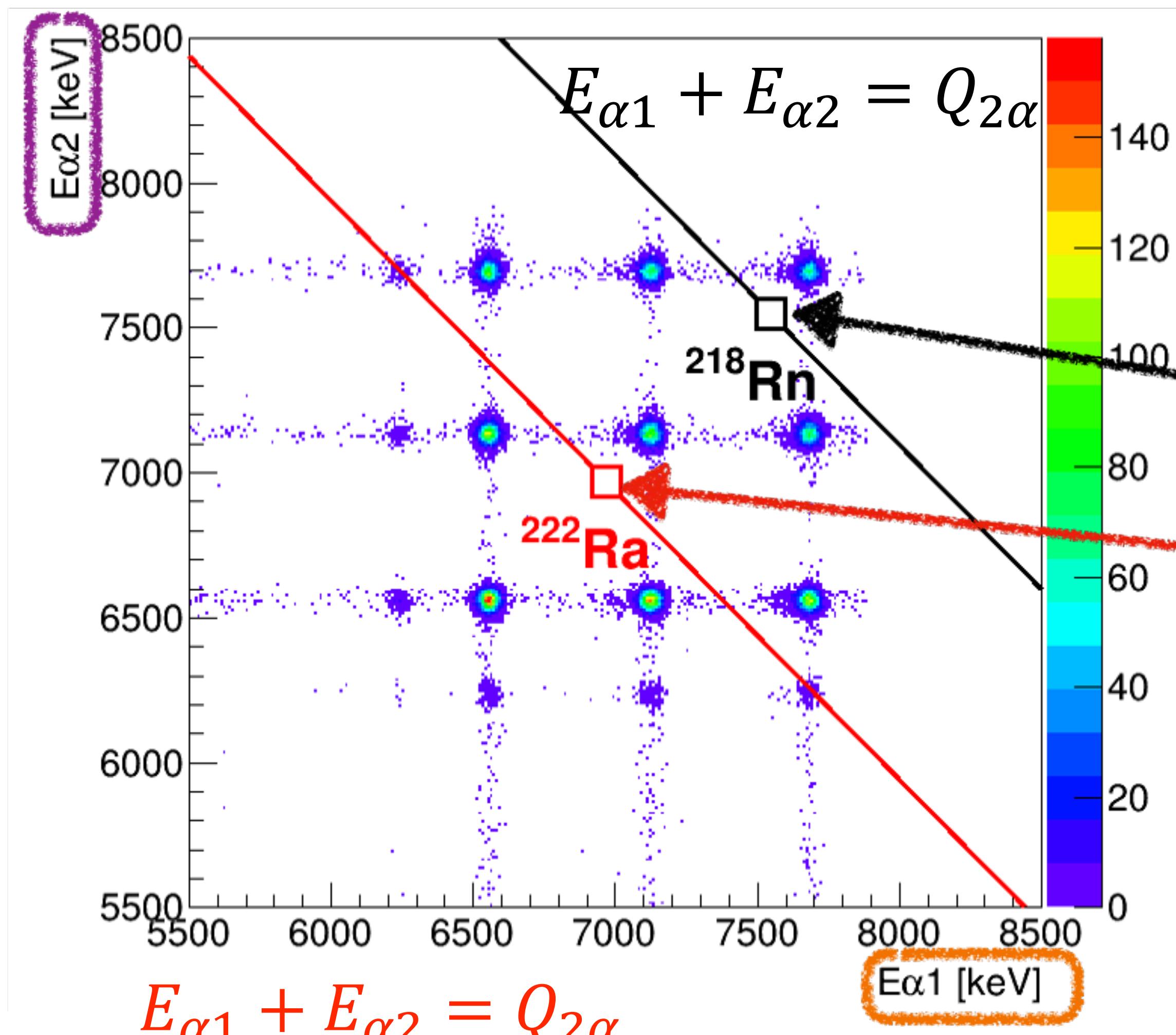


CERN/Isolde - Saclay

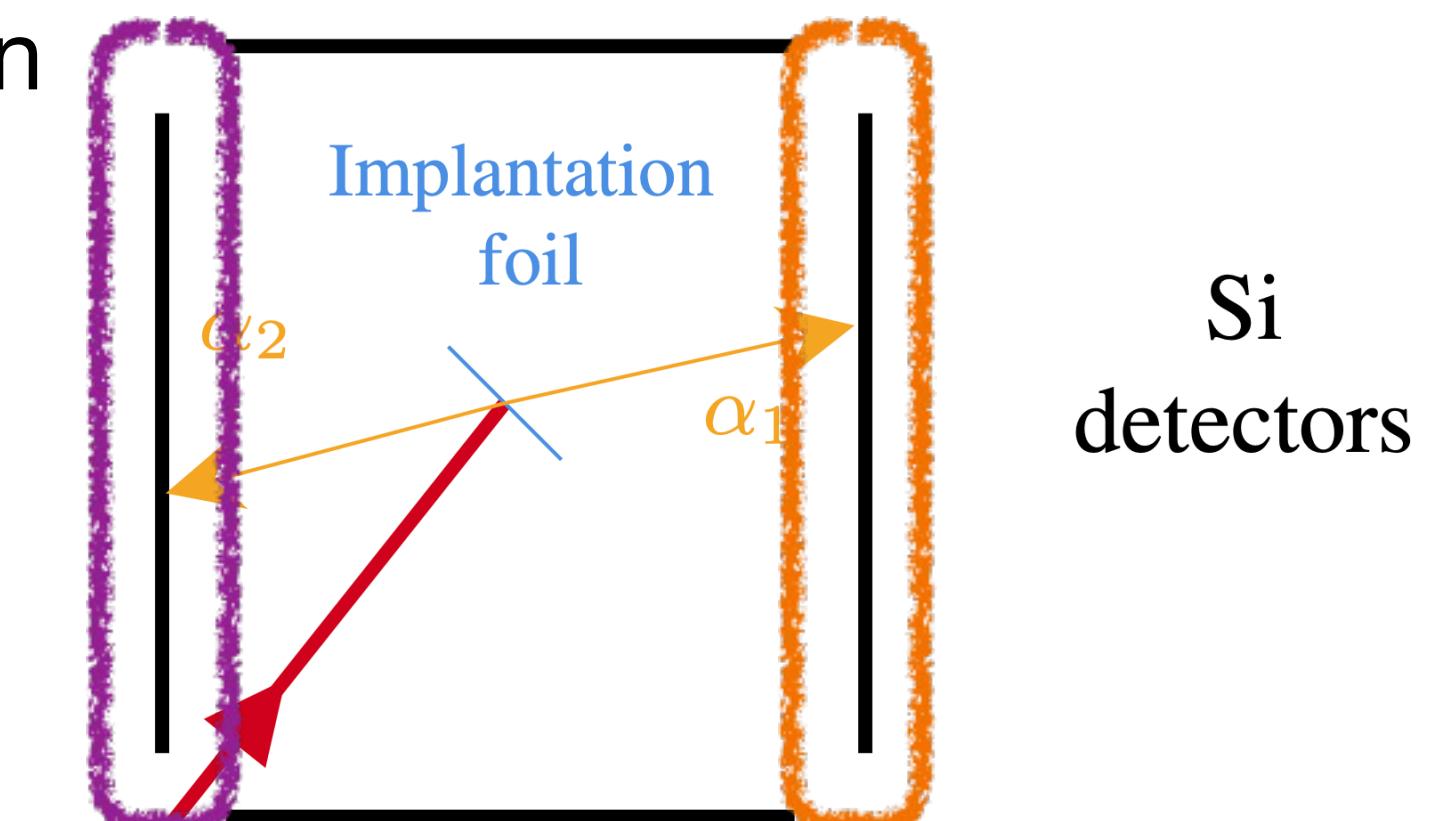
Spatial cut :

Back-to-Back emission
(+ time cuts)

Simulation for background estimate- ^{222}Ra



Incoming
 ^{222}Ra beam

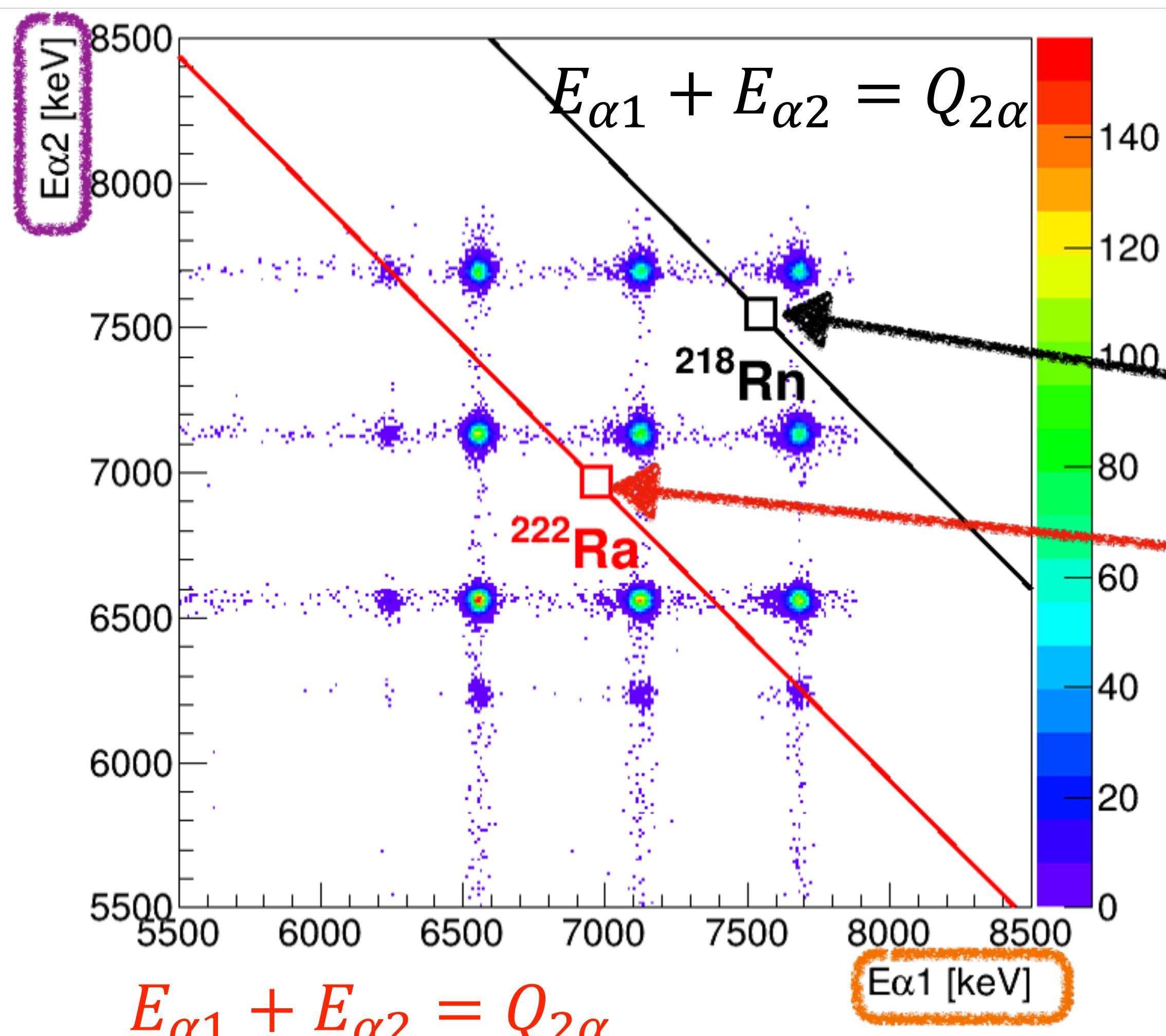


$$E_{\alpha 1} = E_{\alpha 2} = \frac{Q_{2\alpha}}{2}$$

$$E_{\alpha 1} = E_{\alpha 2} = \frac{Q_{2\alpha}}{2}$$

CERN/Isolde - Saclay

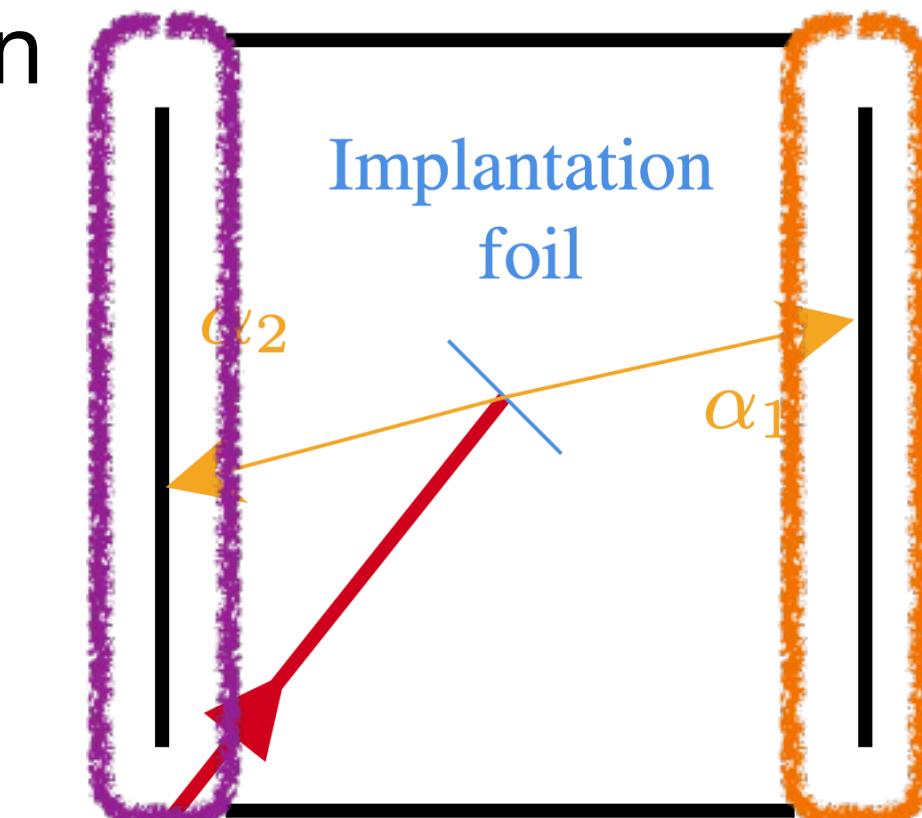
Simulation for background estimate- ^{222}Ra



Spatial cut :

Back-to-Back emission
(+ time cuts)

Incoming
 ^{222}Ra beam



Si
detectors

$$E_{\alpha 1} = E_{\alpha 2} = \frac{Q_{2\alpha}}{2}$$

$$E_{\alpha 1} = E_{\alpha 2} = \frac{Q_{2\alpha}}{2}$$

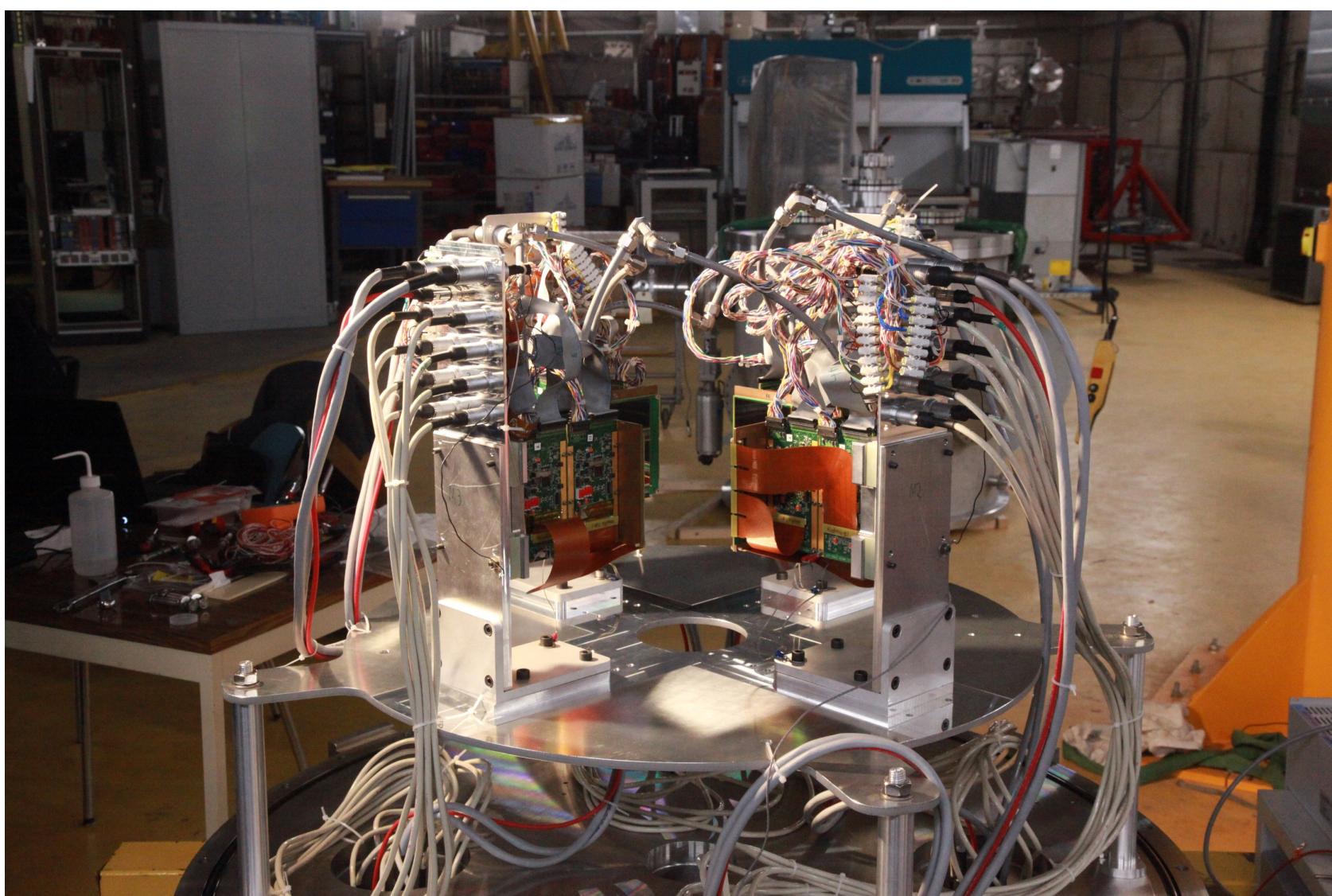
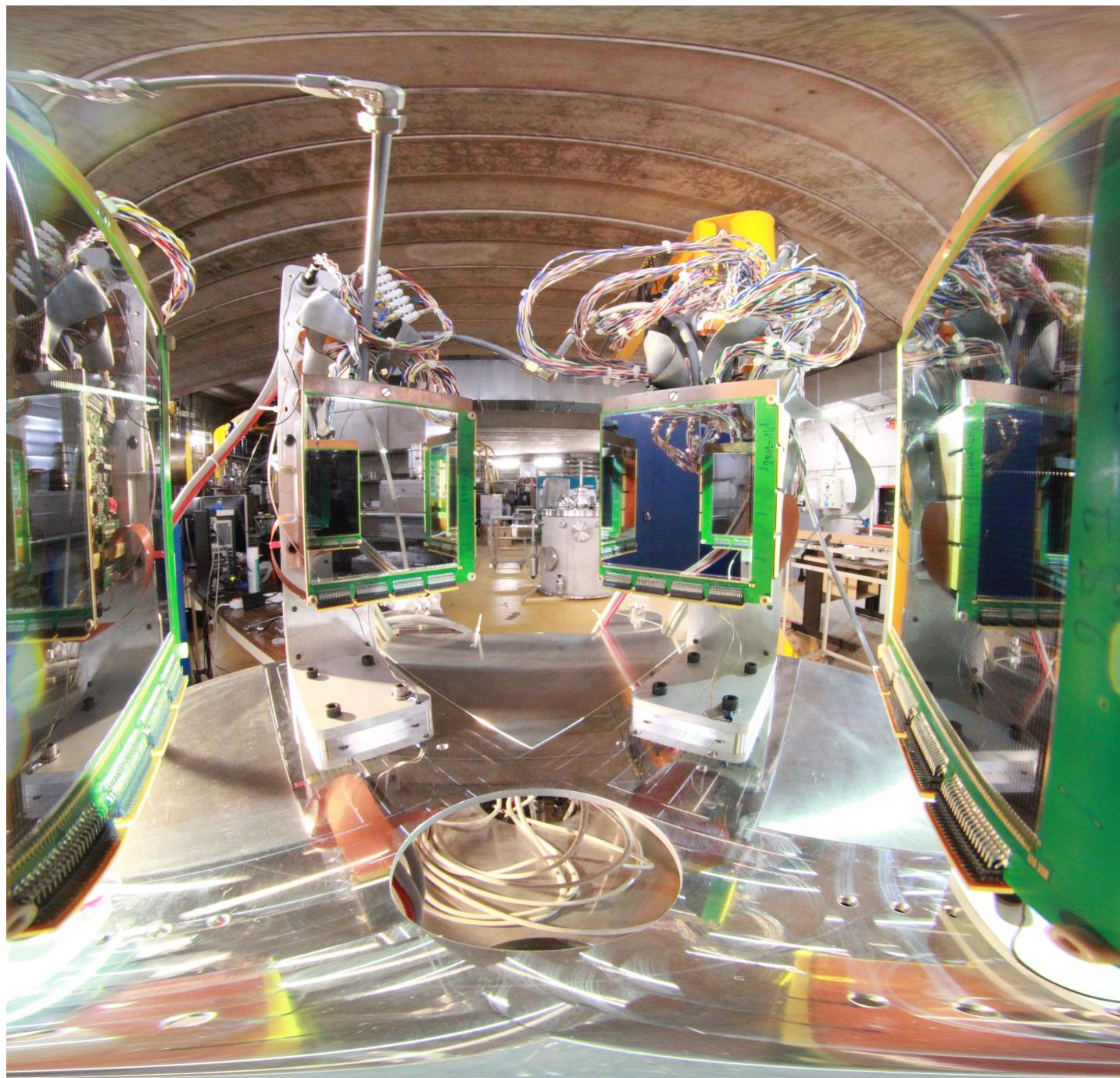
D. Thisse - C. Theisen
**Free of
contaminants !**
(Same conclusion for ^{220}Ra)



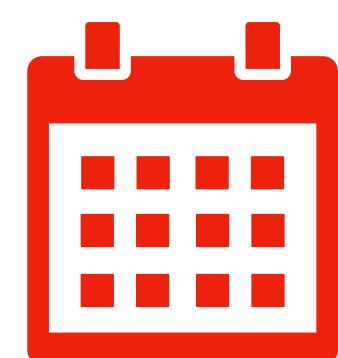
CERN/Isolde - Saclay

Current status

Detectors & electronics tested
Saclay/GANIL



Full setup ready
GANIL



Scheduled on June 20th

Experimental search for 2α

Experiment	GSI (FRS-Ion Catcher)	Saclay (CERN/Isolde)
Isotope production	Source	Beam
Experiment duration	~ 3 months	1 week
Double alpha candidates	^{224}Ra - ^{220}Rn	^{222}Ra - ^{218}Rn ^{220}Ra - ^{216}Rn
Current status	Data analysis	Final setup ready

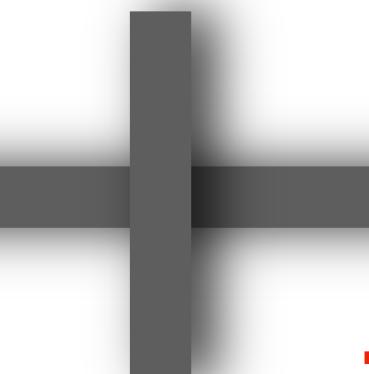


Theoretical prediction



2021

Run
@GSI



2022

Run
@CERN



2023

?

Henri Cartier-Bresson
Le Mur de Berlin

Thank you for your attention !

H. Wilsenach, O. Hall, T. Dickel, PM. Reiter, D. Amanbayev, T. Davinson, L. Heitz, I.Pohjalainen, M. Simonov ,N. Tortorelli, L. Varga, J. Yu, J. Zhao, S. Ayet, S. Beck, Z. Ge, H. Geissel, C. Hornung, N. Kalantar-Nayestanaki, E. Khan, G. Kripko-Koncz, I. Mardor, D. Morrissey, M. Narang, W. Plaß, C. Scheidenberger, A. State, C. Theisen, M. Vandebrouck, P. Woods
and the FRS Ion Catcher Collaboration

C. Theisen, E. Khan, L. Heitz, T. Roger, T. Chaminade, B. Blank, J. Giovinazzo, M. Vandebrouck, B.Sulignano, D.Thisse, J.-P. Ebran, M. Zielinska, A. Drouart, L. Thuilliez, E. Clement, H. Wilsenach, T. Dickel, M. Simonov, M. Assié, D. Beaumel, Y. Blumenfeld, I. Moore, I. Pohjalainen, PM Reiter, P. Woods, T.Davinson, M. Kowalska
and the Double Alpha @CERN Collaboration

Robert Doisneau
L'horloge



Back-up

2 alpha predictions

	Approach	Comments	Best B.R.
Poenaru - 1985	Super Asymetric Fission	Large BR. Close to ${}^8\text{Be}$	$\sim 10^{-13}$
Tretyak - 2021	${}^8\text{Be}$ cluster	Very Large BR ($T_{2\alpha} > 10^{33}$ yr)	...
Santhosh - 2021	Modified Liquid Drop Model	Large BR. Close to ${}^8\text{Be}$, weird ${}^{209}\text{Bi}$	Close to Poenaru
Mercier Zhao - 2021,2023	Time Dependant evolution, EDF	uncertainties hard to estimate	$\sim 10^{-6.5}$
Denisov - 2022	Modification of Unified Model for Alpha Decay	Very small B.R.	$\sim 10^{-2}$

Half-life computation

- > Generic (phenomenological) formula for radioactive decays

$$\tau^{-1} = \nu \times S \times P_S$$

Half-life → τ^{-1}

Assault frequency ($\sim 10^{20} s^{-1}$) → ν

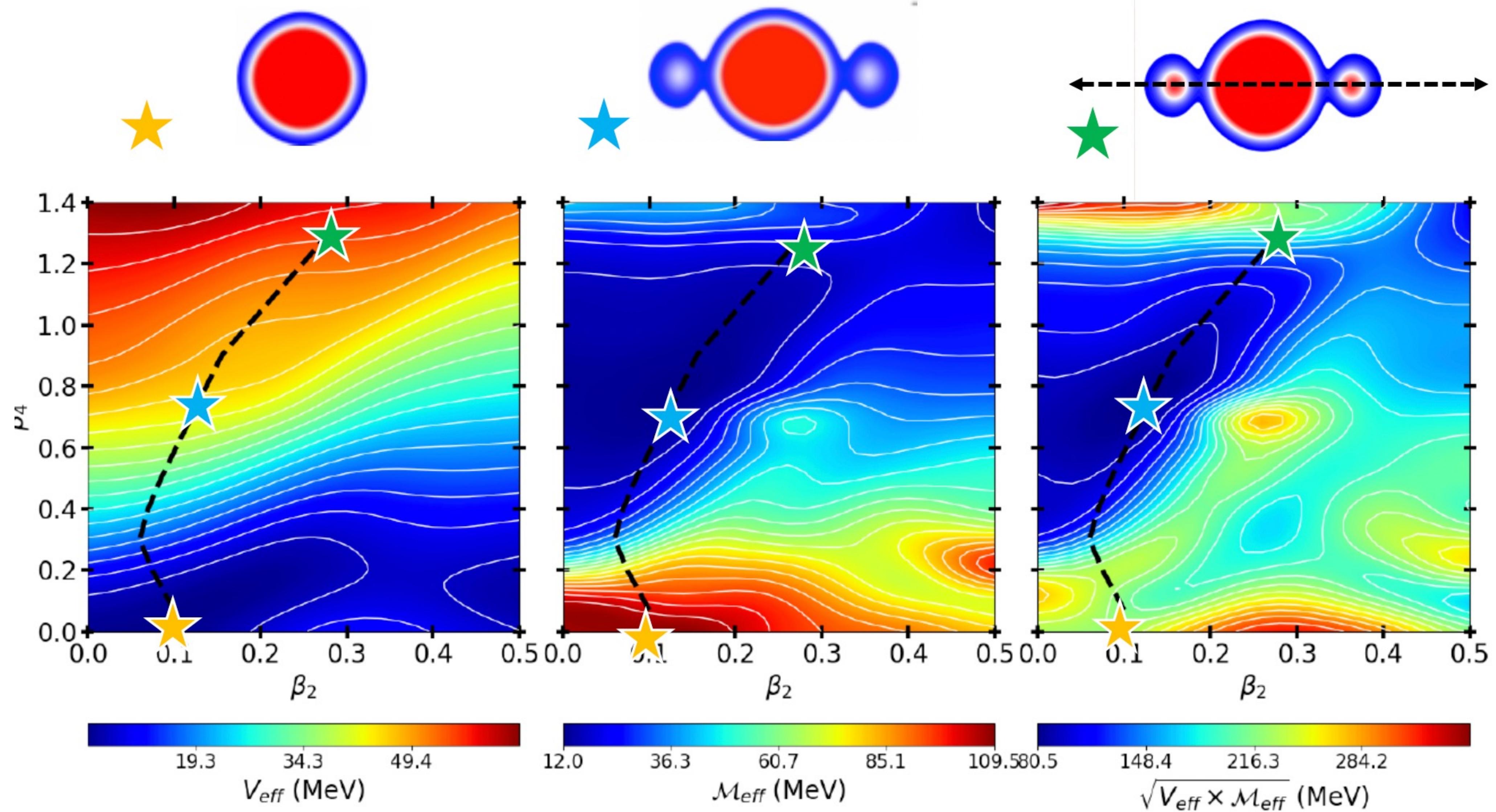
Preformation factor
Hard to estimate → S

Barrier Penetration Probability
WKB-like expressions → P_S

$\log P_S \propto -2 \int dr \sqrt{2B(r)(E(r) - E_0)}$

- > Different models : different S, P_S (E and B)

$B \sim$ reduced mass
 $E \sim$ energy of the system



$$S(L) = \int_{s_{\text{in}}}^{s_{\text{out}}} \frac{1}{\hbar} \sqrt{2\mathcal{M}_{\text{eff}}(s)[V_{\text{eff}}(s) - E_0]} ds$$

$$P = \frac{1}{1 + \exp[2S(L)]}$$

$$T_{1/2} = \frac{\ln(2)}{nP}$$

Half-life computation

$$\tau^{-1} = \nu \frac{1}{1 + \exp 2S}$$

Half-life computation

$$\tau^{-1} = \frac{1}{\nu - \frac{1}{1 + \exp 2S}}$$

Assault
frequency

Half-life computation

$$\tau^{-1} = \frac{1}{\nu \frac{1 + \exp 2S}{1}}$$

Assault frequency Minimised integral action

$$\delta S = 0$$

$$S = \int_{s_{in}}^{s_{out}} ds \sqrt{\mathcal{M}_{eff}(s)(V_{eff}(s) - E_0)}$$

Half-life computation

$$\tau^{-1} = \frac{1}{\nu \frac{1 + \exp(2S)}{1}}$$

Assault frequency **Minimised integral action**

$$\delta S = 0$$

$$S = \int_{s_{in}}^{s_{out}} ds \sqrt{\mathcal{M}_{eff}(s)(V_{eff}(s) - E_0)}$$

PES
Information about
energy cost of a path
(Computed w/ RHB)

Half-life computation

$$\tau^{-1} = \nu \frac{1}{1 + \exp 2S}$$

Assault frequency

Minimised integral action

$$\delta S = 0$$

$$S = \int_{s_{in}}^{s_{out}} ds \sqrt{\mathcal{M}_{eff}(s)(V_{eff}(s) - E_0)}$$

Inertial effective mass

Information about energy needed
to deform nucleus

(Computed w/ ATDHB & perturbed cranked approx)

$$\mathcal{M}_{eff}(s) = \sum_{ij} \mathcal{M}_{ij} \frac{dq_i}{ds} \frac{dq_j}{ds}$$

$$\mathcal{M} = M_{(1)}^{-1} M_{(3)} M_{(1)}^{-1}$$

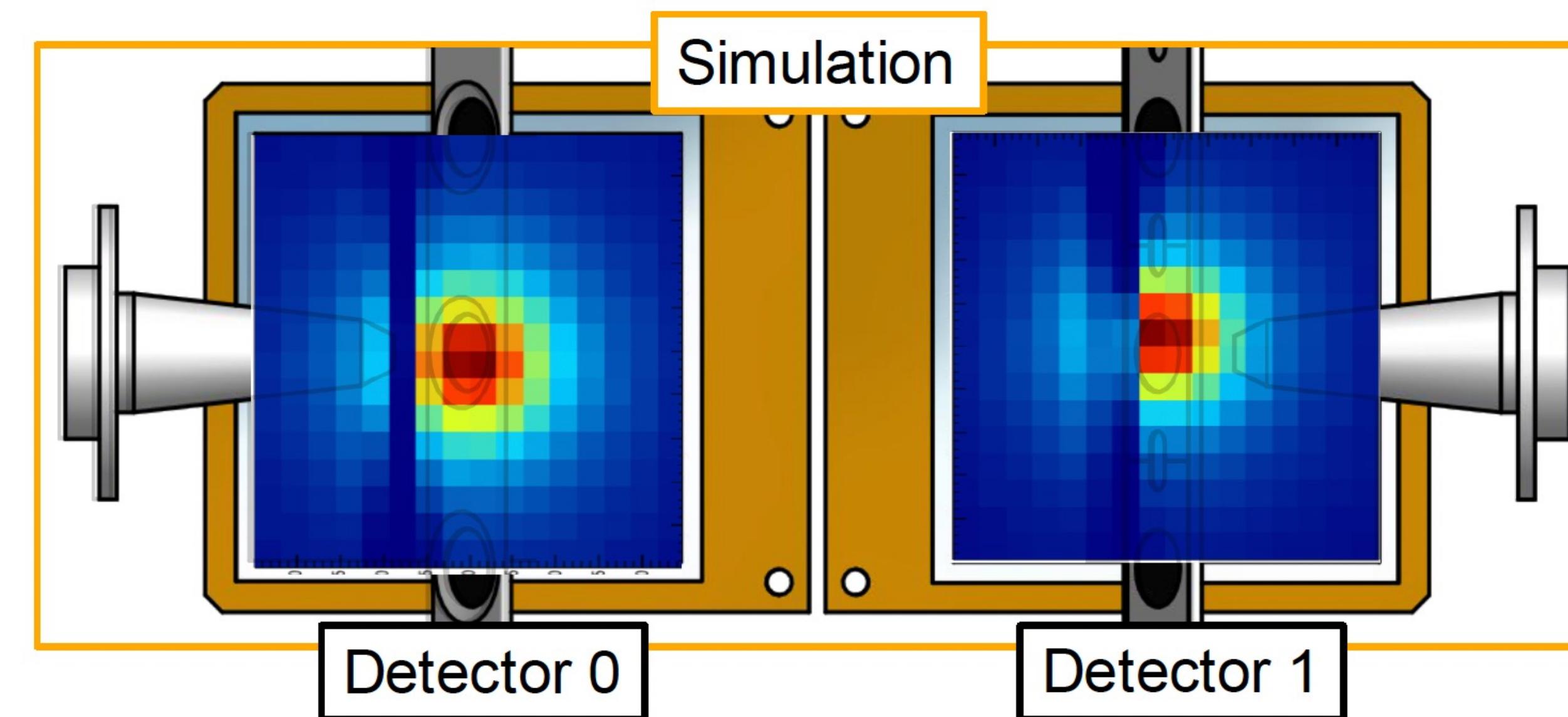
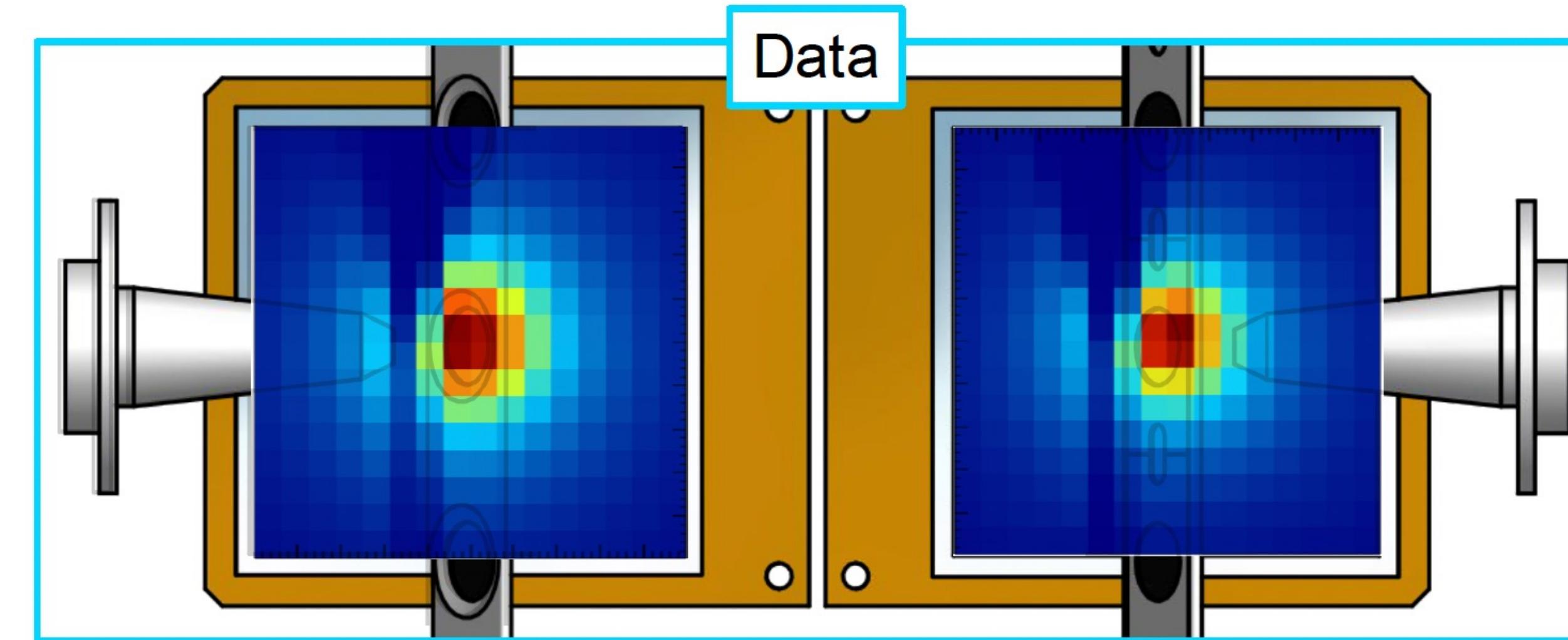
$$[M_{(k)}]_{ij} = \sum_{\mu\nu} \frac{\langle 0|\hat{q}_i|\mu\nu\rangle \langle \mu\nu|\hat{q}_j|0\rangle}{(E_\mu + E_\nu)^k}$$

PES

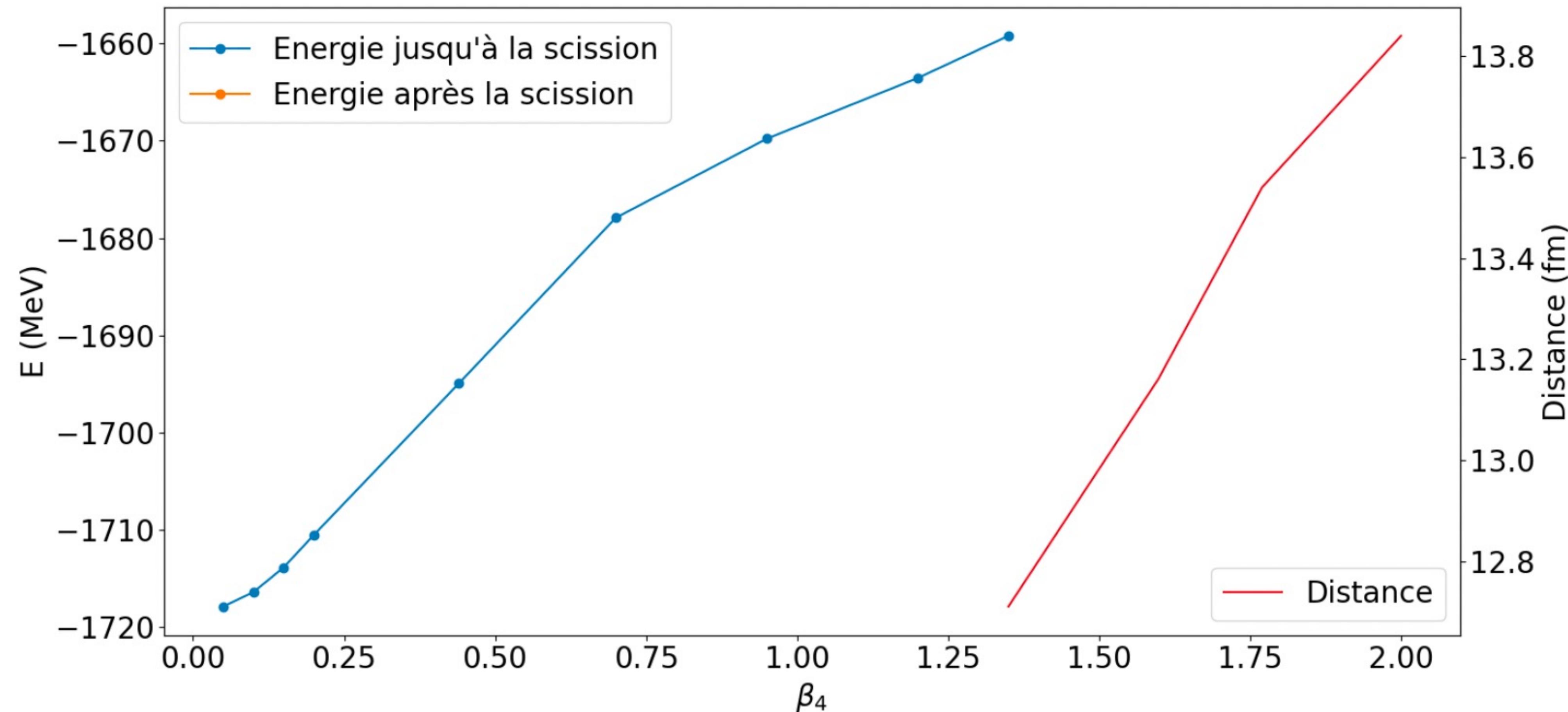
Information about
energy cost of a path
(Computed w/ RHB)

FRS Ion Catcher - GSI

Simulations



Barrier



History of radioactivity

- 1895 Wilhelm Röntgen : **X-ray**
- 1896 Henri Becquerel : **radioactivity**
- 1898 Ernest Rutherford : **α and β rays**
- 1900 Paul Villard : **gamma rays**
- 1929 Maria Goeppert-Mayer : **double gamma prediction**
- 1934 Irène and Frédéric Joliot-Curie : **artificial radioactivity**
- 1935 Maria Goeppert-Mayer : **double beta prediction**
- 1937 Luis Alvarez : **electron capture**
- 1938 Otto Hahn, Fritz Strassmann, Lise Meitner : **fission**
- 1946 L.L. Green and D.L. Livesey, San-Tsiang Tsien et al. : **ternary fission**
- 1960 Vitalii I Goldansky : **proton and double proton prediction**
- 1970 K.P. Jackson et al. : **proton emission** (from an isomeric state)
- 1980 A. Sandulescu, D.N. Poenaru and W. Greiner : **cluster radioactivity prediction**
- 1984 H.J. Rose and G.A. Jones : **cluster radioactivity**
- 1987 S. R. Elliott, A. A. Hahn, and M. K. Moe : **double beta decay**
- 1985 Dorin Poenaru : **double, triple alpha prediction**
- 2002 Jérôme Giovinazzo et al., Marek Pfützner et al : **double proton**