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Istituto Nazionale di Fisica Nucleare PRIN "The consequences of flavor"

# Dipoles and flavor at high energy

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IMCC Annual Meeting - Orsay, 20.06.2023

+ Flavor processes: rare decays & tiny effects

 $BR(B_s \to \mu\mu) \sim 10^{-9}, \quad BR(\tau \to 3\mu) \lesssim 10^{-8}, \quad \Delta a_\mu \approx 10^{-9}$ 

- need billions of events, usually probed by means of high-intensity experiments
- Muon-collider: very large number of (clean) EW particles, but overall event rate not comparable to flavor factories



- New Physics effects are more important at high energies
  - ► NP is heavy compared to the flavor scale: EFT description



- taken to the extreme at a µ-collider with 10's of TeV
- even more powerful for flavor processes: gain can be as large as  $(E/m_{\mu})^2$

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Collisions between 2nd generation particles

 muon collider can have access to flavor processes than cannot be efficiently probed elsewhere



- EW interactions are flavor-universal: an accidental property of the gauge lagrangian, *not* a fundamental symmetry of nature!
  - Example: Yukawa couplings, the only non-gauge interactions in the SM, violate flavor universality maximally!

$$m_u \sim (\cdot \cdot \bullet)$$
  $m_d \sim (\cdot \cdot \bullet)$   $m_\ell \sim (\cdot \cdot \bullet)$ 

 New Physics (especially if related to the Higgs sector) could distinguish the different families of fermions.

#### Lepton flavor violation



Four-fermion interactions: muon current coupled to flavor-violating bilinear

 $\frac{c_{\tau 3\mu}}{\Lambda 2} (\bar{\tau}_{L,R} \gamma^{\rho} \mu_{L,R}) (\bar{\mu}_{L,R} \gamma_{\rho} \mu_{L,R})$ 

+ Charged lepton flavor violating processes:  $\tau \rightarrow \ell \gamma$ ,  $\mu \rightarrow e \gamma$ ,  $\mu \rightarrow 3e$ some of the strongest bounds on (generic) BSM interactions



• 3rd generation less severely constrained:  $\tau \rightarrow 3\mu$  constrains NP scale  $\Lambda > 15$  TeV [Belle]

$$\mathrm{BR}(\tau \to 3\mu) \sim \frac{m_W^4}{\Lambda^4} \qquad \sigma(\mu\bar{\mu} \to \tau\bar{\mu}) \sim \frac{E^2}{\Lambda^4}$$

already at 3 TeV the same sensitivity as Belle II,  $\Lambda > 40$  TeV "Muon smasher quide" 21

"Muon smasher guide" 2103.14043 Homiller, Lu, Reece 2203.08825

#### Lepton flavor violation



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#### Quark flavor violation



Four-fermion interactions: muon current coupled to flavor-violating bilinear

$$\frac{c_{bs}}{\Lambda^2}(\bar{b}_{L,R}\gamma^{\rho}s_{L,R})(\bar{\mu}_{L,R}\gamma_{\rho}\mu_{L,R})$$

• Contributes to (semi-)leptonic rare B decays  $b \rightarrow s \mu \mu$ : branching ratios & angular observables of various hadronic processes

$$B_s \to \mu\mu, \qquad B \to K^{(*)}\mu\mu, \qquad B_s \to \phi\mu\mu, \qquad \Lambda_b \to \Lambda\mu\mu$$

 Theory uncertainties: cannot improve indefinitely with rare decays

$$BR(B \to K\mu\mu) \sim \frac{m_W^4}{\Lambda^4}, \quad \sigma(\mu\bar{\mu} \to jj) \sim \frac{E^2}{\Lambda^4}$$

Azatov, Garosi, Greljo, Marzocca, Salko, Trifinopoulos 2205.13552



# The muon g-2

- Longstanding discrepancy between experimental results and SM prediction
- Also tension between lattice and dispersive computation of SM
  - If you trust lattice: 4σ tension in e<sup>+</sup>e<sup>-</sup> → hadrons cross-section
  - If you trust e+e-: 4σ tension in muon g-2

$$\Delta a_{\mu} = a_{\mu}^{(\exp)} - a_{\mu}^{(th)} = 251(59) \times 10^{-11}$$

- + Theoretical/systematic errors need to be controlled at the level of  $\Delta a_{\mu} \sim 10^{-9}$ 
  - → Independent test of  $\Delta a_{\mu}$  is desirable (ideally with different sys. & th. errors)

A muon collider can give a model-independent, high-energy test of  $\Delta a_{\mu}$ 



#### Muon g-2 @ muon collider

- If new physics is light enough (i.e. weakly coupled), a Muon Collider can directly produce the new particles
   direct searches: model-dependent
- + If new physics is heavy: EFT! One dim. 6 operator contributes at tree-level:  $\mathscr{L}_{g-2} = \frac{C_{e\gamma}}{\Lambda^2} H(\bar{\ell}_L \sigma_{\mu\nu} e_R) eF^{\mu\nu} + h.c.$



Dipole operator generates both  $\Delta a_{\mu}$  and  $\mu \mu \rightarrow h \gamma$ 

#### B, Paradisi 2012.02769

Capdevilla et al. 2006.16277

- At high energy  

$$\sigma_{\mu^+\mu^- \to h\gamma} = \frac{s}{48\pi} \frac{|C_{e\gamma}|^2}{\Lambda^4} \approx 0.7 \operatorname{ab} \left(\frac{\sqrt{s}}{30 \operatorname{TeV}}\right)^2 \left(\frac{\Delta a_{\mu}}{3 \times 10^{-9}}\right)^2$$

$$N_{h\gamma} = \sigma \cdot \mathscr{L} \approx \left(\frac{\sqrt{s}}{10 \operatorname{TeV}}\right)^4 \left(\frac{\Delta a_{\mu}}{3 \times 10^{-9}}\right)^2 \quad \text{need } E > 10 \operatorname{TeV}$$

# Muon g-2 @ muon collider



• Other operators enter g-2 at 1 loop:

$$\Delta a_{\mu} \approx \left(\frac{250 \,\mathrm{TeV}}{\Lambda^2}\right)^2 \left(C_{e\gamma} - \frac{C_{Tt}}{5} - \frac{C_{Tc}}{1000} - \frac{C_{eZ}}{20}\right)$$

Full set of operators with Λ ≥ 100 TeV
 can be probed at a high-energy
 muon collider





Muon EDM @ muon collider



• Dipole operator contributes also to  $h \rightarrow \ell \ell \gamma$  decays



$$\mathrm{BR}_{h \to \mu^+ \mu^- \gamma}^{(\mathrm{NP})} \approx 5 \times 10^{-10} \left(\frac{\Delta a_{\mu}}{3 \times 10^{-9}}\right)$$

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Tau magnetic dipole moment: enhanced due to the larger mass

$$\Delta a_{\tau} = \frac{4v \, m_{\tau}}{\Lambda^2} C_{e\gamma}^{\tau} \approx \Delta a_{\mu} \frac{m_{\tau}^2}{m_{\mu}^2} \approx 10^{-6}$$
  
if  $C_{e\gamma}^{\ell}$  scales as  $y_{\ell}$ 

Present bound:  $\Delta a_{\tau} \lesssim 10^{-2}$ from LEP  $e^+e^- \rightarrow e^+e^-\tau^+\tau^$ hep-ex/0406010 Can be improved to few 10-3 at HL-LHC 1908.05180

• Contribution to  $h \rightarrow \tau \tau \gamma$  decays:

 $\mathrm{BR}^{(\mathrm{SM})}_{h \to \tau^+ \tau^- \gamma} \approx 5 \times 10^{-4}$  (with cut on soft collinear photon)



could be measured at few % level by Higgs factory

$$\mathsf{BR}_{h \to \tau^+ \tau^- \gamma}^{(\mathsf{NP})} \approx 0.2 \times \Delta a_{\tau}$$



$$\mathrm{BR}_{h\to\tau^+\tau^-\gamma}^{(\mathrm{SM})} \approx 5 \times 10^{-4} \qquad \qquad \mathrm{BR}_{h\to\tau^+\tau^-\gamma}^{(\mathrm{NP})} \approx 0.2 \times \Delta a_{\tau}$$

★ MuC: 10<sup>7</sup> Higgs bosons @ 10 TeV ⇒ 5k H → ττγ events, 2% precision on SM,
 Δa<sub>τ</sub> ≤ 3 × 10<sup>-5</sup> (signal only)
 3 o.o.m. improvement of current limit!



$$BR_{h\to\tau^+\tau^-\gamma}^{(SM)} \approx 5 \times 10^{-4} \qquad BR_{h\to\tau^+\tau^-\gamma}^{(NP)} \approx 0.2 \times \Delta a_{\tau}$$

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- e+e- factory: ~ 400  $H \rightarrow \tau \tau \gamma$  events  $\Rightarrow$  5% precision on SM,  $\Delta a_{\tau} \lesssim \text{few} \times 10^{-4}$
- **LHC:** large number of Higgs bosons, but large backgrounds
   Rescaling *H* → *ττ* searches ~ 350 reconstructed *H* → *ττγ* events at HL-LHC,
   but 10x more background ⇒ 20% precision on SM, *Δa<sub>τ</sub>* ≤ 5 × 10<sup>-4</sup>

#### Tau g-2 from high-energy probes

Further possibilities to measure  $\Delta a_r$  precisely from high-energy probes

Pair production



$$\sigma_{\rm SM} \sim \frac{4\pi\alpha^2}{3s}$$
$$\sigma_{\rm NP} = \frac{4\pi\alpha^2}{3} \frac{|C_{e\gamma}^{\ell}|^2 v^2}{\Lambda^4} \sim \frac{\pi\alpha^2 \Delta a_{\ell}^2}{6m_{\ell}^2}$$

Limit on g-2: 
$$\Delta a_{\ell} \lesssim \frac{\text{const.}}{\sqrt{\mathscr{L}}} \sim E^{-1}$$

• equivalently, 
$$\Lambda \sim \sqrt{E}$$

EFT description breaks down above few TeV!





w/ Levati, Maltoni, Paradisi, Wang

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+  $H\tau\tau$  associated production



work in progress with Levati, Paradisi, Maltoni, Wang

• Main background from  $\mu\mu \rightarrow Z\gamma$ (where Z is mistaken for H)

#### Could probe $\Delta a_{\tau} \sim 10^{-5}$ @ 10 TeV



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#### Could probe $\Delta a_{\tau} \sim 10^{-5}$ @ 10 TeV



#### Tau g-2 from high-intensity probes

A high-energy lepton collider has a huge VBF rate!

•  $\Delta a_{\tau}$  from vector boson scatterings  $\ell^+\ell^- \rightarrow \ell^+\ell^-\tau^+\tau^-, \nu\bar{\nu}\tau^+\tau^-$ 



Caveat: VBF is a "soft" process,
 EFT mainly affects high-mass region

Still, could probe  $\Delta a_{\tau} \sim \text{few } 10^{-5}$ 

charged and neutral channel can separately constrain  $C_{eB}$  and  $C_{eW}$ 

(same as LEP bound)

work in progress with Levati, Paradisi, Maltoni, Wang

$$\Delta a_{\tau} \times 10^4$$
 from  $\ell^+ \ell^- \to \tau^+ \tau^- \nu \bar{\nu}$ 



# Radiation & high-energy neutrinos

- Radiation effects are important.
- Hard neutrinos from μ<sup>±</sup> → W<sup>±</sup>ν have a large PDF ⇒ can access neutrino initial state at high energy!
  - talks by David, Alfredo, David
     see also Chen, Glioti, Rattazzi,
     Ricci, Wulzer 2202.10509





- Directly probe neutrino interactions at high energy: usual E<sup>2</sup> gain
  - can put strong constraints on BSM neutrino physics

talk by Zahra this afternoon

 ★ complementary to µ<sup>+</sup>µ<sup>-</sup> scattering, can remove flat directions and probe operators with different flavor structure

- + High energy muon collider offers new ways to test flavor:
  - gain from high energy probes
  - access to second generation processes
- Bounds on lepton- and quark-flavor violating interactions can surpass low-energy precision measurements!
- + Can improve lepton g-2 and EDM bound by orders of magnitude
- Rare Higgs decays + Higgs production
- Radiative corrections: access to neutrino interactions



### Muon g-2 @ muon collider: direct searches

- If new physics is light enough (i.e. weakly coupled, m<sub>\*</sub> ~ Λ·g<sub>\*</sub>/4π),
   a Muon Collider can directly produce the new particles
  - direct searches: model-dependent

Classify New Physics that can enter the loop, under reasonable assumptions:  $\ell_L$ 

- electroweak charges
- flavor structure
- naturalness
- number of particles
- A 20–30 TeV muon collider can test the most motivated, weakly coupled models

Capdevilla et al. 2006.16277, 2101.10334



### Muon g-2 @ muon collider

- SM irreducible background is small:  $\sigma_{\mu^+\mu^- \to h\gamma}^{(SM)} \approx 10^{-2} \operatorname{ab} \left(\frac{30 \operatorname{TeV}}{\sqrt{s}}\right)^2$ tree-level is suppressed by muon mass; loop contribution dominant -
- Main background from  $\mu\mu \rightarrow Z\gamma$  (where Z is mistaken for H) (large due to transverse Z polarizations)

Search in h  $\rightarrow$  bb channel:  $\epsilon_b \approx 80 \%$  |  $\cos \theta_{cut}$  | < 0.6 BR<sub> $h \rightarrow b\bar{b}$ </sub> = 58 % At 30 TeV, 90 ab<sup>-1</sup>, for  $\Delta a_\mu = 3 \times 10^{-9}$ :  $N_S = 22$ ,  $N_B = 886 \times p_{Z \rightarrow h}$  $\Delta a_\mu$  can be tested at 95% CL at a 30 TeV

collider if  $Z \rightarrow h$  mistag probability < 10-15%

50 100 150 200 m<sub>jet</sub> [GeV]

s140 up 120

80

60

40

20

0

0

√s>2500 GeV

-H jet, corr --- H jet, orig

--- Z jet, orig

 $100 \vdash -Z$  jet, corr

L=4 ab<sup>-1</sup>,e<sup>-</sup> pol -80%

1911.02523

Other operators contribute to g-2 at one loop:

$$\mathcal{L} = \frac{C_{eB}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) H B_{\mu\nu} + \frac{C_{eW}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) \tau^I H W^I_{\mu\nu} + \frac{C_{qT}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) \epsilon (\bar{q}_L \sigma_{\mu\nu} u_R)$$

(+ other effects suppressed by  $y_{\mu}$ )  $|H|^2 W^a_{\mu\nu} W^{\mu\nu,a} |H|^2 B_{\mu\nu} B^{\mu\nu}$  $(H^{\dagger} \sigma^a H) W^a_{\mu\nu} B^{\mu\nu}$ 



Including 1-loop running:

$$\begin{split} \Delta a_{\mu} &\simeq \frac{4m_{\mu}v}{e\Lambda^{2}} \Big( C_{e\gamma}(m_{\mu}) - \frac{3\alpha}{2\pi} \frac{c_{W}^{2} - s_{W}^{2}}{s_{W}c_{W}} C_{eZ} \log \frac{\Lambda}{m_{Z}} \Big) - \sum_{q=c,t} \frac{4m_{\mu}m_{q}}{\pi^{2}} \frac{C_{Tq}}{\Lambda^{2}} \log \frac{\Lambda}{m_{q}} \\ &\approx \Big( \frac{250 \text{ TeV}}{\Lambda^{2}} \Big)^{2} (C_{e\gamma} - 0.2C_{Tt} - 0.001C_{Tc} - 0.05C_{eZ}) \end{split}$$
 B, Paradisi 2012.02769



$$\mathscr{L} = \frac{C_{eB}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) H B_{\mu\nu} + \frac{C_{eW}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) \tau^I H W^I_{\mu\nu} + \frac{C_{qT}}{\Lambda^2} (\bar{\ell}_L \sigma^{\mu\nu} e_R) \epsilon (\bar{q}_L \sigma_{\mu\nu} u_R)$$

 Full set of operators with Λ ≥ 100 TeV can be probed at a high energy muon collider



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24

tree-level is suppressed by muon mass; loop contribution dominant

• Main background from  $\mu\mu \rightarrow Z\gamma$  (where Z is mistaken for H) (large due to transverse Z polarizations)

$$\frac{d\sigma_{\mu\mu\to h\gamma}}{d\cos\theta} = \frac{|C^{\mu}_{e\gamma}(\Lambda)|^2}{\Lambda^4} \frac{s}{64\pi} (1 - \cos^2\theta)$$

$$\frac{d\sigma_{\mu\mu\to Z\gamma}}{d\cos\theta} = \frac{\pi\alpha^2}{4s} \frac{1+\cos^2\theta}{\sin^2\theta} \frac{1-4s_W^2+8s_W^4}{s_W^2c_W^2}$$

-Search in h 
$$\rightarrow$$
 bb channel:  
 $\epsilon_b \approx 80 \%$   $|\cos \theta_{\rm cut}| < 0.6$   ${\rm BR}_{h \rightarrow b\bar{b}} = 58 \%$   
At 30 TeV, 90 ab<sup>-1</sup>, for  $\Delta a_\mu = 3 \times 10^{-9}$ :  
 $N_S = 22$ ,  $N_B = 886 \times p_{Z \rightarrow h}$ 

 $\Delta a_{\mu}$  can be tested at 95% CL at a 30 TeV collider if Z→h mistag probability < 10-15%



New physics: 
$$\frac{d\sigma_{NP}}{dx_1 dx_2} = \frac{1}{192\pi^3} \frac{Q^2}{\Lambda^4} \left[ (Q_\mu e \, \mathcal{C}_\gamma)^2 + \left(\frac{g \, \mathcal{C}_Z}{4c_w}\right)^2 \right] (2x_1 x_2 - x_1 - x_2 + 1)$$

Interference:

$$\frac{d\sigma_{N\gamma}}{dx_1dx_2} = -\frac{\sqrt{2}}{96\pi^3}\frac{m_\tau}{v}\frac{e^3}{\Lambda^2}Q_\mu\,\mathcal{C}_\gamma;$$

Standard Model:

$$\begin{split} \frac{d\sigma_{\gamma}}{dx_{1}dx_{2}} &= \frac{1}{192\pi^{3}} \frac{m_{\tau}^{2}e^{4}}{v^{2}} \frac{1}{Q^{2}} \bigg[ \frac{1-x_{1}}{1-x_{2}} + 2 + \frac{1-x_{2}}{1-x_{1}} \bigg];\\ \frac{d\sigma_{2}}{dx_{1}dx_{2}} &= \frac{1}{3 \cdot 2^{14}\pi^{3}} \frac{m_{\tau}^{2}g^{4}}{v^{2}c_{w}^{4}} \frac{1}{Q^{2}} \bigg[ \frac{1-x_{1}}{1-x_{2}} - 2 + \frac{1-x_{2}}{1-x_{1}} \bigg];\\ \frac{d\sigma_{3}}{dx_{1}dx_{2}} &= \frac{1}{6 \cdot 2^{16}\pi^{3}} \frac{g^{8}}{c_{w}^{8}} \frac{v^{2}}{Q^{4}} \bigg[ \frac{x_{1}x_{2} + x_{1} + x_{2} - 1}{(x_{1} + x_{2} - 1)^{2}} \bigg]; \end{split}$$



# Hττ signal

