

# NLO QCD predictions for polarised $W^+Z$ production with semileptonic decay

Christoph Haitz

in collaboration with Ansgar Denner and Giovanni Pelliccioli

Institut für Theoretische Physik 2  
Julius-Maximilians-Universität Würzburg

08.03.2023

based on arXiv:2211.09040 (accepted by PRD)

# Table of contents

- 1 Motivation
- 2 Definition of polarised cross-sections
- 3 Setup
- 4 Integrated results
- 5 Differential results
- 6 Summary

# Motivation

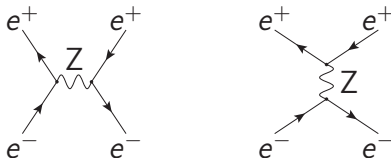
- Polarised processes allow for deep insights into spontaneous symmetry breaking
- Polarised cross-sections are very sensitive to beyond-Standard Model effects
- Polarisation is well suited for tests of the Standard Model
- Polarised WZ production processes are a subject of ongoing research

# Existing Work on polarised ZW production

- Focus is on purely leptonic decay modes
- Narrow-width approximation
  - ▶ MadGraph5\_aMC@NLO LO-study, Buarque Franzosi et al. 2020, arXiv:1912.01725 [1]
- Double-pole approximation
  - ▶ NLO QCD, Denner and Pelliccioli 2021, arXiv:2010.07149 [2]
  - ▶ NLO QCD und NLO EW, Le and Baglio 2022, arXiv:2203.01470 [3], Le et al. 2022, arXiv:2208.09232 [4], Le et al. 2022, arXiv:2302.03324 [5]
- Experimental studies
  - ▶ ATLAS 2019, arXiv:1902.05759 [6]
  - ▶ CMS 2022, arXiv:2110.11231 [7]
  - ▶ ATLAS 2022, arXiv:2211.09435 [8] (next talk)

# Definition of polarised cross-sections

- Diagrams with and without the wanted (s-channel) resonance contribute to a given process



- Remove non-resonant diagrams in a gauge-independent way
  - ▶ This can be achieved by using a pole approximation
    - ★ Set resonant particles on-shell  $\{p_i\} \Rightarrow \{\tilde{p}_i\}$
    - ★ Conserve some off-shell effects by using the off-shell denominators of the propagators and applying the phase-space cuts to the off-shell momenta

$$M(\{\tilde{p}\}, p_{res}^2) = M_{\mu, \text{production}}(\{\tilde{p}\}) \frac{N^{\mu\nu}(\{\tilde{p}\})}{p_{res}^2 - m^2 - im\Gamma} M_{\nu, \text{decay}}(\{\tilde{p}\})$$

# Definition of polarised cross-sections

- Numerator of the resonant propagator contains a sum over all polarisation states

$$\sum_{\text{polarisations}} \epsilon_{\mu}^* \epsilon_{\nu} = -g_{\mu\nu} \quad (\text{Feynman-'t Hooft gauge})$$

$$M(\{\tilde{p}\}, p_{res}^2) = \sum_{\lambda} M_{\mu, \text{production}}(\{\tilde{p}\}) \frac{\epsilon_{\lambda}^{\mu*}(\{\tilde{p}\}) \epsilon_{\lambda}^{\nu}(\{\tilde{p}\})}{p_{res}^2 - m^2 - im\Gamma} M_{\nu, \text{decay}}(\{\tilde{p}\})$$

$$M(\{\tilde{p}\}, p_{res}^2) = \sum_{\lambda} M_{\lambda}(\{\tilde{p}\}, p_{res}^2)$$

# Definition of polarised cross-sections

- Take the square of the matrix element to calculate the cross-section

$$\underbrace{|M(\{\tilde{\mathbf{p}}\}, p_{res}^2)|^2}_{\text{unpolarised}} = \sum_{\lambda} \underbrace{|M_{\lambda}(\{\tilde{\mathbf{p}}\}, p_{res}^2)|^2}_{\text{polarisation } \lambda} + \underbrace{\sum_{\lambda \neq \lambda'} M_{\lambda}^*(\{\tilde{\mathbf{p}}\}, p_{res}^2) M_{\lambda'}(\{\tilde{\mathbf{p}}\}, p_{res}^2)}_{\text{interferences}}$$

# Setup

$$p p \rightarrow Z(\rightarrow e^- e^+) W^+(\rightarrow \text{jets})$$

- Z boson decays leptonically into an electron-positron pair
- $W^+$  boson decays hadronically (jet system)
- Polarisation is defined in the center-of-mass frame of the two bosons
- Resolved setup
  - ▶ Two light jets (AK4)
  - ▶ Jet system = the two jets with an invariant mass closest to the W-mass
- Unresolved setup
  - ▶ One massive fat jet (AK8)
  - ▶ Jet system = fat jet with the largest transverse momentum



# Phase-space cuts

- Phase-space cuts mimic the CMS analysis arXiv:2111.13669 [9]
- Different phase-space cuts are applied in the two setups
- Suppress non-resonant background
- Z and  $W^+$  are very boosted
- Anti-kT jet algorithm
  - ▶ Resolved:  $R_0 = 0.4$
  - ▶ Unresolved:  $R_0 = 0.8$

		resolved	unresolved
Jet selection	min $p_T$	30 GeV	200 GeV
	max $ y $	2.4	2.4
	min $\Delta R_{Jl^\pm}$	0.4	0.8
	min $M$	-	65 GeV
	max $M$	-	105 GeV
Cuts on the jet system ( $W^+$ -Boson)	min $p_T$	200 GeV	-
	min $M$	65 GeV	-
	max $M$	105 GeV	-
Cuts on single leptons	min $p_T$	40 GeV	40 GeV
	max $ y $	2.4	2.4
Cuts on the lepton pair (Z-Boson)	min $p_T$	200 GeV	200 GeV
	min $M$	76 GeV	76 GeV
	max $M$	106 GeV	106 GeV

# Integrated results

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}[\%]$	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}[\%]$	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved, $Z(e^+e^-)W^+(\text{jj})$						
unpol.	1.8567(2) <sup>+1.2%</sup> <sub>-1.4%</sub>	100	3.036(2) <sup>+6.8%</sup> <sub>-5.3%</sub>	100	1.635	1.033
$Z_{\text{L}}W_{\text{L}}^+$	0.64603(5) <sup>+0.2%</sup> <sub>-0.6%</sub>	34.8	0.6127(4) <sup>+0.9%</sup> <sub>-0.7%</sub>	20.2	0.948	1.031
$Z_{\text{L}}W_{\text{T}}^+$	0.08687(1) <sup>+0.2%</sup> <sub>-0.6%</sub>	4.7	0.17012(6) <sup>+8.6%</sup> <sub>-6.8%</sub>	5.6	1.958	0.967
$Z_{\text{T}}W_{\text{L}}^+$	0.08710(1) <sup>+0.1%</sup> <sub>-0.6%</sub>	4.7	0.24307(7) <sup>+10.2%</sup> <sub>-8.2%</sub>	8.0	2.791	1.017
$Z_{\text{T}}W_{\text{T}}^+$	0.97678(7) <sup>+2.0%</sup> <sub>-2.2%</sub>	52.6	2.0008(7) <sup>+8.9%</sup> <sub>-7.1%</sub>	65.8	2.048	1.059
interf.	0.0595(1)	3.2	0.009(2)	0.4	—	—
unresolved, $Z(e^+e^-)W^+(\text{J})$						
unpol.	1.6879(2) <sup>+1.9%</sup> <sub>-2.1%</sub>	100	3.112(2) <sup>+7.6%</sup> <sub>-6.1%</sub>	100	1.843	1.193
$Z_{\text{L}}W_{\text{L}}^+$	0.61653(5) <sup>+1.0%</sup> <sub>-1.3%</sub>	36.5	0.6799(5) <sup>+0.9%</sup> <sub>-0.7%</sub>	21.9	1.103	1.170
$Z_{\text{L}}W_{\text{T}}^+$	0.06444(1) <sup>+0.7%</sup> <sub>-1.0%</sub>	3.8	0.17584(6) <sup>+10.8%</sup> <sub>-8.6%</sub>	5.7	2.729	1.158
$Z_{\text{T}}W_{\text{L}}^+$	0.07437(1) <sup>+0.6%</sup> <sub>-0.9%</sub>	4.4	0.24742(8) <sup>+11.0%</sup> <sub>-8.9%</sub>	8.0	3.327	1.193
$Z_{\text{T}}W_{\text{T}}^+$	0.88233(9) <sup>+2.9%</sup> <sub>-2.9%</sub>	52.3	2.0041(8) <sup>+9.6%</sup> <sub>-7.7%</sub>	64.3	2.271	1.227
interf.	0.0503(3)	3.0	0.004(2)	0.1	—	—

# Integrated results

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}[\%]$	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}[\%]$	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved, $Z(e^+e^-)W^+(\text{jj})$						
unpol.	1.8567(2) <sup>+1.2%</sup> <sub>-1.4%</sub>	100	3.036(2) <sup>+6.8%</sup> <sub>-5.3%</sub>	100	<b>1.635</b>	1.033
$Z_{\text{L}}W_{\text{L}}^+$	0.64603(5) <sup>+0.2%</sup> <sub>-0.6%</sub>	34.8	0.6127(4) <sup>+0.9%</sup> <sub>-0.7%</sub>	20.2	0.948	1.031
$Z_{\text{L}}W_{\text{T}}^+$	0.08687(1) <sup>+0.2%</sup> <sub>-0.6%</sub>	4.7	0.17012(6) <sup>+8.6%</sup> <sub>-6.8%</sub>	5.6	<b>1.958</b>	0.967
$Z_{\text{T}}W_{\text{L}}^+$	0.08710(1) <sup>+0.1%</sup> <sub>-0.6%</sub>	4.7	0.24307(7) <sup>+10.2%</sup> <sub>-8.2%</sub>	8.0	<b>2.791</b>	1.017
$Z_{\text{T}}W_{\text{T}}^+$	0.97678(7) <sup>+2.0%</sup> <sub>-2.2%</sub>	52.6	2.0008(7) <sup>+8.9%</sup> <sub>-7.1%</sub>	65.8	<b>2.048</b>	1.059
interf.	0.0595(1)	3.2	0.009(2)	0.4	—	—
unresolved, $Z(e^+e^-)W^+(\text{J})$						
unpol.	1.6879(2) <sup>+1.9%</sup> <sub>-2.1%</sub>	100	3.112(2) <sup>+7.6%</sup> <sub>-6.1%</sub>	100	<b>1.843</b>	1.193
$Z_{\text{L}}W_{\text{L}}^+$	0.61653(5) <sup>+1.0%</sup> <sub>-1.3%</sub>	36.5	0.6799(5) <sup>+0.9%</sup> <sub>-0.7%</sub>	21.9	1.103	1.170
$Z_{\text{L}}W_{\text{T}}^+$	0.06444(1) <sup>+0.7%</sup> <sub>-1.0%</sub>	3.8	0.17584(6) <sup>+10.8%</sup> <sub>-8.6%</sub>	5.7	<b>2.729</b>	1.158
$Z_{\text{T}}W_{\text{L}}^+$	0.07437(1) <sup>+0.6%</sup> <sub>-0.9%</sub>	4.4	0.24742(8) <sup>+11.0%</sup> <sub>-8.9%</sub>	8.0	<b>3.327</b>	1.193
$Z_{\text{T}}W_{\text{T}}^+$	0.88233(9) <sup>+2.9%</sup> <sub>-2.9%</sub>	52.3	2.0041(8) <sup>+9.6%</sup> <sub>-7.7%</sub>	64.3	<b>2.271</b>	1.227
interf.	0.0503(3)	3.0	0.004(2)	0.1	—	—

- Large NLO corrections mostly from gluon initiated real emission processes

# Integrated results

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}[\%]$	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}[\%]$	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved, $Z(e^+e^-)W^+(\text{jj})$						
unpol.	1.8567(2) $^{+1.2\%}_{-1.4\%}$	100	3.036(2) $^{+6.8\%}_{-5.3\%}$	100	1.635	1.033
$Z_L W_L^+$	0.64603(5) $^{+0.2\%}_{-0.6\%}$	34.8	0.6127(4) $^{+0.9\%}_{-0.7\%}$	20.2	0.948	1.031
$Z_L W_T^+$	0.08687(1) $^{+0.2\%}_{-0.6\%}$	4.7	0.17012(6) $^{+8.6\%}_{-6.8\%}$	5.6	1.958	0.967
$Z_T W_L^+$	0.08710(1) $^{+0.1\%}_{-0.6\%}$	4.7	0.24307(7) $^{+10.2\%}_{-8.2\%}$	8.0	2.791	1.017
$Z_T W_T^+$	0.97678(7) $^{+2.0\%}_{-2.2\%}$	52.6	2.0008(7) $^{+8.9\%}_{-7.1\%}$	65.8	2.048	1.059
interf.	0.0595(1)	3.2	0.009(2)	0.4	—	—
unresolved, $Z(e^+e^-)W^+(\text{J})$						
unpol.	1.6879(2) $^{+1.9\%}_{-2.1\%}$	100	3.112(2) $^{+7.6\%}_{-6.1\%}$	100	1.843	1.193
$Z_L W_L^+$	0.61653(5) $^{+1.0\%}_{-1.3\%}$	36.5	0.6799(5) $^{+0.9\%}_{-0.7\%}$	21.9	1.103	1.170
$Z_L W_T^+$	0.06444(1) $^{+0.7\%}_{-1.0\%}$	3.8	0.17584(6) $^{+10.8\%}_{-8.6\%}$	5.7	2.729	1.158
$Z_T W_L^+$	0.07437(1) $^{+0.6\%}_{-0.9\%}$	4.4	0.24742(8) $^{+11.0\%}_{-8.9\%}$	8.0	3.327	1.193
$Z_T W_T^+$	0.88233(9) $^{+2.9\%}_{-2.9\%}$	52.3	2.0041(8) $^{+9.6\%}_{-7.7\%}$	64.3	2.271	1.227
interf.	0.0503(3)	3.0	0.004(2)	0.1	—	—

- Large contribution of the purely longitudinal polarisation state compared to more inclusive set-ups (no strong  $p_T$  cut) [2]
- Goldstone boson contributions are unsuppressed because diagrams with three gauge-boson vertices contribute at LO

# Integrated results

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}$ [%]	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}$ [%]	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved, $Z(e^+e^-)W^+(\text{jj})$						
unpol.	1.8567(2) <sup>+1.2%</sup> <sub>-1.4%</sub>	100	3.036(2) <sup>+6.8%</sup> <sub>-5.3%</sub>	100	1.635	1.033
$Z_{\text{L}}W_{\text{L}}^+$	0.64603(5) <sup>+0.2%</sup> <sub>-0.6%</sub>	34.8	0.6127(4) <sup>+0.9%</sup> <sub>-0.7%</sub>	20.2	0.948	1.031
$Z_{\text{L}}W_{\text{T}}^+$	0.08687(1) <sup>+0.2%</sup> <sub>-0.6%</sub>	4.7	0.17012(6) <sup>+8.6%</sup> <sub>-6.8%</sub>	5.6	1.958	0.967
$Z_{\text{T}}W_{\text{L}}^+$	0.08710(1) <sup>+0.1%</sup> <sub>-0.6%</sub>	4.7	0.24307(7) <sup>+10.2%</sup> <sub>-8.2%</sub>	8.0	2.791	1.017
$Z_{\text{T}}W_{\text{T}}^+$	0.97678(7) <sup>+2.0%</sup> <sub>-2.2%</sub>	52.6	2.0008(7) <sup>+8.9%</sup> <sub>-7.1%</sub>	65.8	2.048	1.059
interf.	0.0595(1)	3.2	0.009(2)	0.4	–	–
unresolved, $Z(e^+e^-)W^+(\text{J})$						
unpol.	1.6879(2) <sup>+1.9%</sup> <sub>-2.1%</sub>	100	3.112(2) <sup>+7.6%</sup> <sub>-6.1%</sub>	100	1.843	1.193
$Z_{\text{L}}W_{\text{L}}^+$	0.61653(5) <sup>+1.0%</sup> <sub>-1.3%</sub>	36.5	0.6799(5) <sup>+0.9%</sup> <sub>-0.7%</sub>	21.9	1.103	1.170
$Z_{\text{L}}W_{\text{T}}^+$	0.06444(1) <sup>+0.7%</sup> <sub>-1.0%</sub>	3.8	0.17584(6) <sup>+10.8%</sup> <sub>-8.6%</sub>	5.7	2.729	1.158
$Z_{\text{T}}W_{\text{L}}^+$	0.07437(1) <sup>+0.6%</sup> <sub>-0.9%</sub>	4.4	0.24742(8) <sup>+11.0%</sup> <sub>-8.9%</sub>	8.0	3.327	1.193
$Z_{\text{T}}W_{\text{T}}^+$	0.88233(9) <sup>+2.9%</sup> <sub>-2.9%</sub>	52.3	2.0041(8) <sup>+9.6%</sup> <sub>-7.7%</sub>	64.3	2.271	1.227
interf.	0.0503(3)	3.0	0.004(2)	0.1	–	–

- Significant differences between the resolved and unresolved setup at LO caused by the recombination of the jets
- Differences become smaller at NLO

# Integrated results

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}$ [%]	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}$ [%]	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved, $Z(e^+e^-)W^+(\text{jj})$						
unpol.	1.8567(2) <sup>+1.2%</sup> <sub>-1.4%</sub>	100	3.036(2) <sup>+6.8%</sup> <sub>-5.3%</sub>	100	1.635	1.033
$Z_{\text{L}}W_{\text{L}}^+$	0.64603(5) <sup>+0.2%</sup> <sub>-0.6%</sub>	34.8	0.6127(4) <sup>+0.9%</sup> <sub>-0.7%</sub>	20.2	0.948	1.031
$Z_{\text{L}}W_{\text{T}}^+$	0.08687(1) <sup>+0.2%</sup> <sub>-0.6%</sub>	4.7	0.17012(6) <sup>+8.6%</sup> <sub>-6.8%</sub>	5.6	1.958	0.967
$Z_{\text{T}}W_{\text{L}}^+$	0.08710(1) <sup>+0.1%</sup> <sub>-0.6%</sub>	4.7	0.24307(7) <sup>+10.2%</sup> <sub>-8.2%</sub>	8.0	2.791	1.017
$Z_{\text{T}}W_{\text{T}}^+$	0.97678(7) <sup>+2.0%</sup> <sub>-2.2%</sub>	52.6	2.0008(7) <sup>+8.9%</sup> <sub>-7.1%</sub>	65.8	2.048	1.059
<b>interf.</b>	<b>0.0595(1)</b>	<b>3.2</b>	<b>0.009(2)</b>	<b>0.4</b>	—	—
unresolved, $Z(e^+e^-)W^+(\text{J})$						
unpol.	1.6879(2) <sup>+1.9%</sup> <sub>-2.1%</sub>	100	3.112(2) <sup>+7.6%</sup> <sub>-6.1%</sub>	100	1.843	1.193
$Z_{\text{L}}W_{\text{L}}^+$	0.61653(5) <sup>+1.0%</sup> <sub>-1.3%</sub>	36.5	0.6799(5) <sup>+0.9%</sup> <sub>-0.7%</sub>	21.9	1.103	1.170
$Z_{\text{L}}W_{\text{T}}^+$	0.06444(1) <sup>+0.7%</sup> <sub>-1.0%</sub>	3.8	0.17584(6) <sup>+10.8%</sup> <sub>-8.6%</sub>	5.7	2.729	1.158
$Z_{\text{T}}W_{\text{L}}^+$	0.07437(1) <sup>+0.6%</sup> <sub>-0.9%</sub>	4.4	0.24742(8) <sup>+11.0%</sup> <sub>-8.9%</sub>	8.0	3.327	1.193
$Z_{\text{T}}W_{\text{T}}^+$	0.88233(9) <sup>+2.9%</sup> <sub>-2.9%</sub>	52.3	2.0041(8) <sup>+9.6%</sup> <sub>-7.7%</sub>	64.3	2.271	1.227
<b>interf.</b>	<b>0.0503(3)</b>	<b>3.0</b>	<b>0.004(2)</b>	<b>0.1</b>	—	—

- The interference contribution is small
- Interference becomes smaller at NLO

# Comparison background

process	resolved		unresolved	
	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$
DPA $ZW^+$	1.8567(2) $^{+1.2\%}_{-1.4\%}$	0.353	1.6879(2) $^{+1.9\%}_{-2.1\%}$	0.425
DPA $ZW^-$	1.0527(1) $^{+1.3\%}_{-1.6\%}$	0.200	0.9003(1) $^{+2.0\%}_{-2.1\%}$	0.227
DPA ZZ	2.1430(3) $^{+1.3\%}_{-1.6\%}$	0.408	1.2804(2) $^{+2.6\%}_{-2.7\%}$	0.323
DPA ZV	5.0523(4) $^{+1.3\%}_{-1.5\%}$	0.961	3.8685(3) $^{+2.2\%}_{-2.3\%}$	0.975
full $O(\alpha^4)$	5.253(1) $^{+1.2\%}_{-1.5\%}$	1.000	3.967(2) $^{+2.1\%}_{-2.3\%}$	1.000
full $O(\alpha_s\alpha^3)$	-0.3124(6) $^{+9.2\%}_{-10.7\%}$	-0.059	-0.2145(6) $^{+9.7\%}_{-11.4\%}$	-0.054
full $O(\alpha_s^2\alpha^2)$	97.91(7) $^{+24.3\%}_{-18.4\%}$	18.638	62.55(7) $^{+25.0\%}_{-18.8\%}$	15.768

- Non-resonant background
- Resonant ZZ and  $ZW^-$  pair production background
  - ▶ Have to be treated as additional contributions

# Comparison background

process	resolved		unresolved	
	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$
DPA $ZW^+$	$1.8567(2)^{+1.2\%}_{-1.4\%}$	0.353	$1.6879(2)^{+1.9\%}_{-2.1\%}$	0.425
DPA $ZW^-$	$1.0527(1)^{+1.3\%}_{-1.6\%}$	0.200	$0.9003(1)^{+2.0\%}_{-2.1\%}$	0.227
DPA ZZ	$2.1430(3)^{+1.3\%}_{-1.6\%}$	0.408	$1.2804(2)^{+2.6\%}_{-2.7\%}$	0.323
DPA ZV	$5.0523(4)^{+1.3\%}_{-1.5\%}$	<b>0.961</b>	$3.8685(3)^{+2.2\%}_{-2.3\%}$	<b>0.975</b>
full $O(\alpha^4)$	$5.253(1)^{+1.2\%}_{-1.5\%}$	1.000	$3.967(2)^{+2.1\%}_{-2.3\%}$	1.000
full $O(\alpha_s\alpha^3)$	$-0.3124(6)^{+9.2\%}_{-10.7\%}$	-0.059	$-0.2145(6)^{+9.7\%}_{-11.4\%}$	-0.054
full $O(\alpha_s^2\alpha^2)$	$97.91(7)^{+24.3\%}_{-18.4\%}$	18.638	$62.55(7)^{+25.0\%}_{-18.8\%}$	15.768

- DPA approximates the full electroweak process well (2% – 4%)



# Comparison background

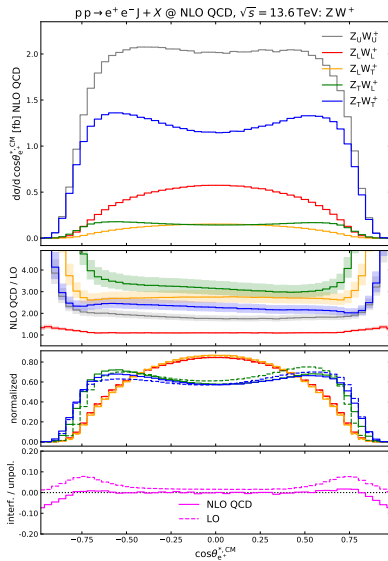
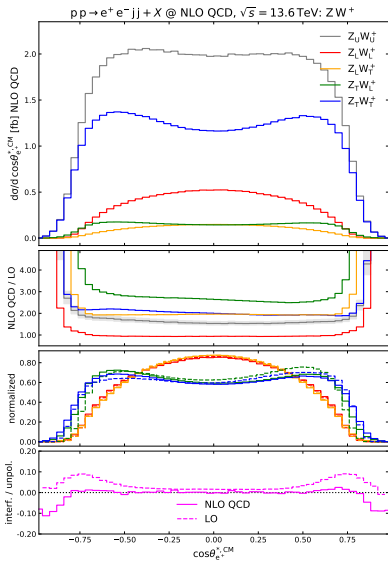
process	resolved		unresolved	
	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$	$\sigma_{\text{LO}}$ [fb]	ratio over full $O(\alpha^4)$
DPA $ZW^+$	1.8567(2) <sup>+1.2%</sup> <sub>-1.4%</sub>	0.353	1.6879(2) <sup>+1.9%</sup> <sub>-2.1%</sub>	0.425
DPA $ZW^-$	1.0527(1) <sup>+1.3%</sup> <sub>-1.6%</sub>	0.200	0.9003(1) <sup>+2.0%</sup> <sub>-2.1%</sub>	0.227
DPA ZZ	2.1430(3) <sup>+1.3%</sup> <sub>-1.6%</sub>	0.408	1.2804(2) <sup>+2.6%</sup> <sub>-2.7%</sub>	0.323
DPA ZV	5.0523(4) <sup>+1.3%</sup> <sub>-1.5%</sub>	0.961	3.8685(3) <sup>+2.2%</sup> <sub>-2.3%</sub>	0.975
full $O(\alpha^4)$	5.253(1) <sup>+1.2%</sup> <sub>-1.5%</sub>	1.000	3.967(2) <sup>+2.1%</sup> <sub>-2.3%</sub>	1.000
full $O(\alpha_s\alpha^3)$	-0.3124(6) <sup>+9.2%</sup> <sub>-10.7%</sub>	-0.059	-0.2145(6) <sup>+9.7%</sup> <sub>-11.4%</sub>	-0.054
full $O(\alpha_s^2\alpha^2)$	97.91(7) <sup>+24.3%</sup> <sub>-18.4%</sub>	18.638	62.55(7) <sup>+25.0%</sup> <sub>-18.8%</sub>	15.768

- Very large QCD background that needs to be subtracted before carrying out a polarisation analysis

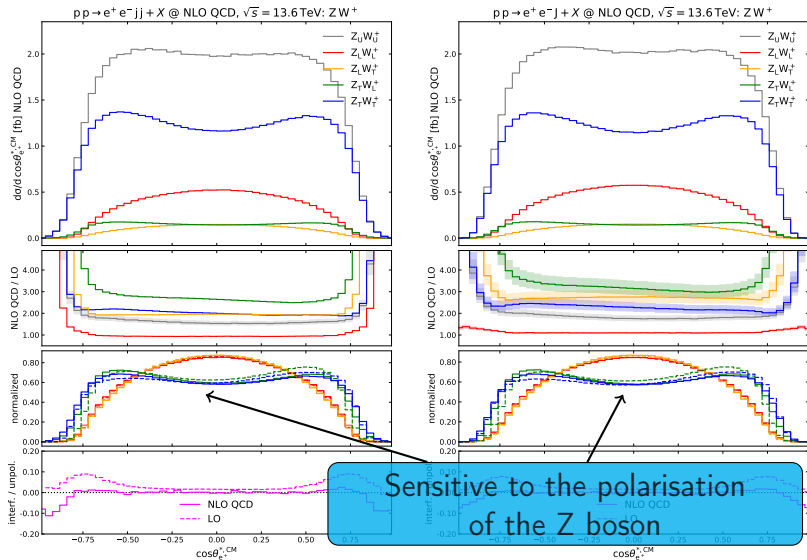
# Differential results

- Differential cross-sections show the dependence on physical observables
- Differences of the two setups and the polarisation states
- Polarisation dependent variables are of particular interest
- Shapes of the distributions are needed for the measurement of polarisation fractions

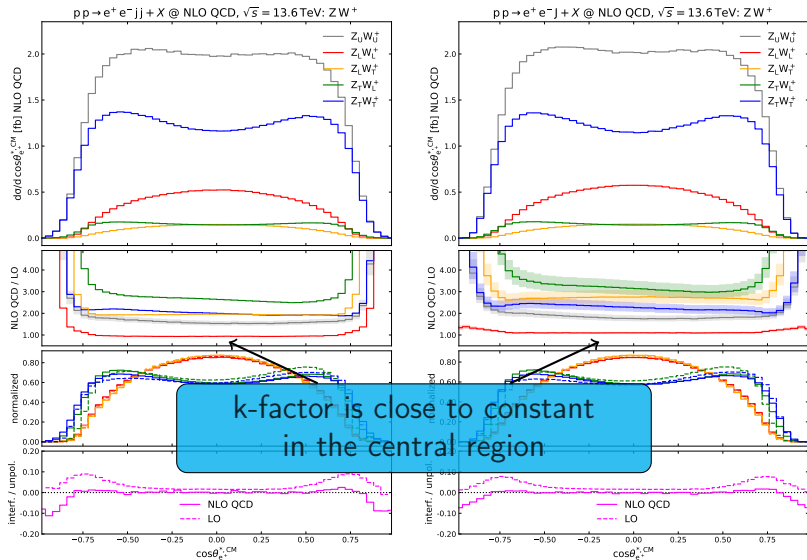
# Electron decay angle $\cos(\vartheta_{e^-}^{*,\text{CM}}) = \frac{\vec{p}_{e^-}^* \cdot \vec{p}_{e^+e^-}^{\text{CM}}}{|\vec{p}_{e^-}^*| |\vec{p}_{e^+e^-}^{\text{CM}}|}$



# Electron decay angle $\cos(\vartheta_{e^-}^{*,CM}) = \frac{\vec{p}_{e^-}^* \cdot \vec{p}_{e^+e^-}^{CM}}{|\vec{p}_{e^-}^*| |\vec{p}_{e^+e^-}^{CM}|}$

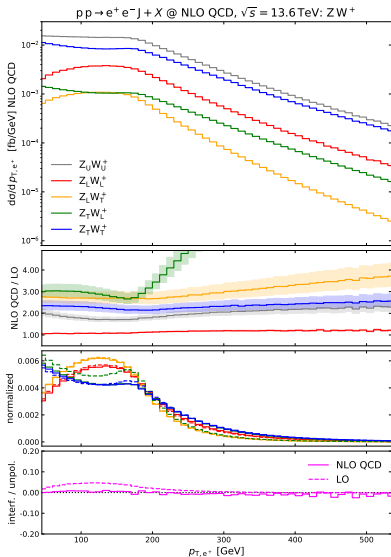
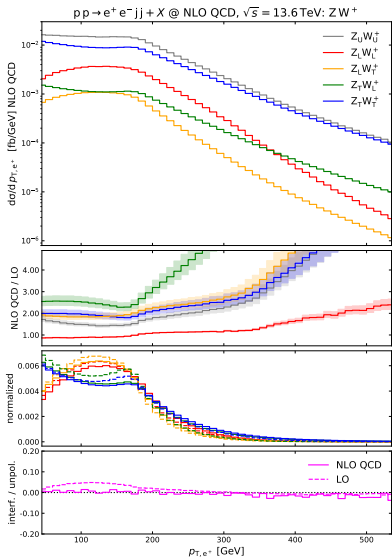


# Electron decay angle $\cos(\vartheta_{e^-}^{*,CM}) = \frac{\vec{p}_{e^-}^* \cdot \vec{p}_{e^+e^-}^{CM}}{|\vec{p}_{e^-}^*| |\vec{p}_{e^+e^-}^{CM}|}$

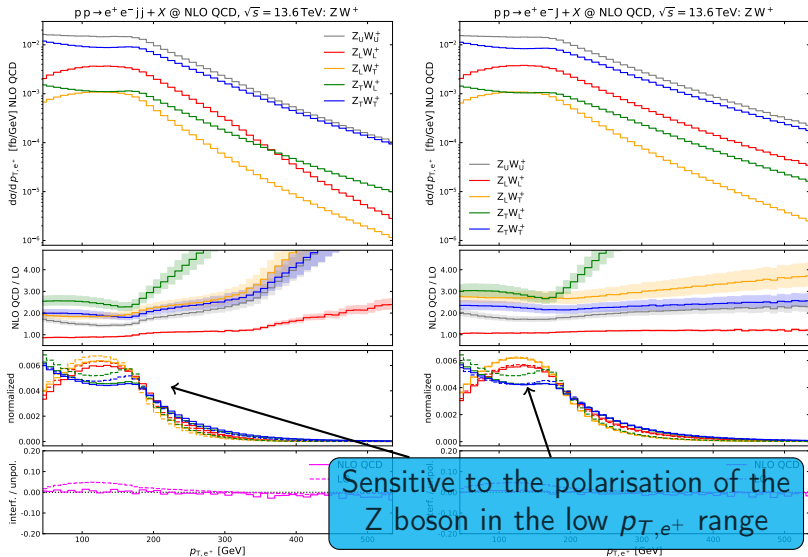


k-factor is close to constant in the central region

# Positron transverse momentum $p_{T,e^+} = \sqrt{p_{1,e^+}^2 + p_{2,e^+}^2}$



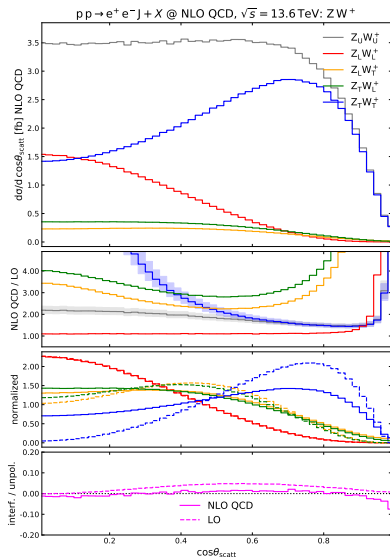
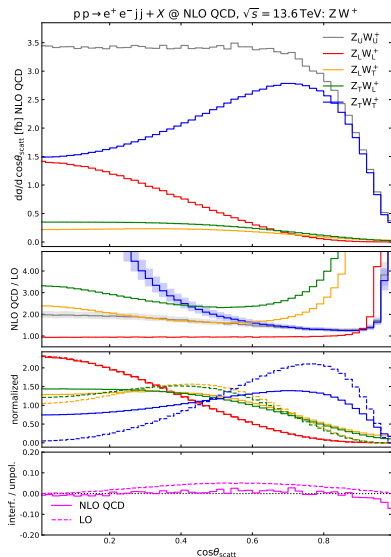
# Positron transverse momentum $p_{T,e^+} = \sqrt{p_{1,e^+}^2 + p_{2,e^+}^2}$



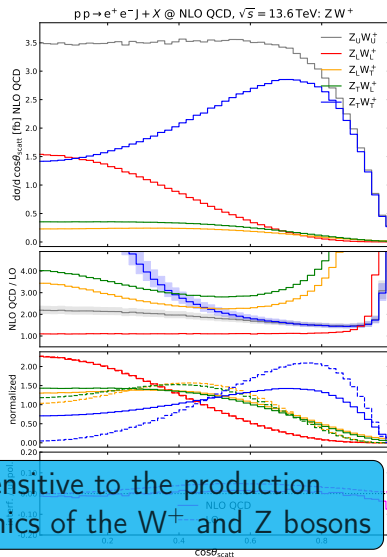
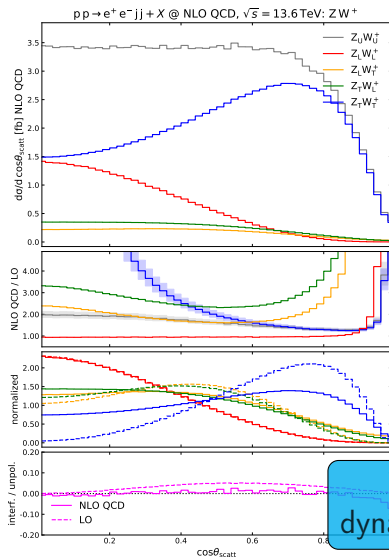




# Scattering angle $\cos(\vartheta_{scatt}) = \frac{|\vec{p}_{e^+e^-}^{CM}, z|}{|\vec{p}_{e^+e^-}^{CM}|}$

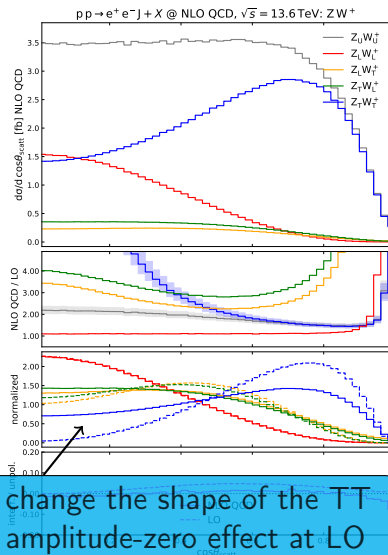
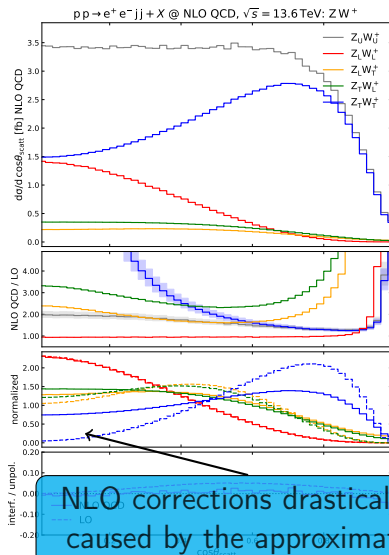


Scattering angle  $\cos(\vartheta_{scatt}) = \frac{|\vec{p}_{e^+e^-}^{CM}, z|}{|\vec{p}_{e^+e^-}^{CM}|}$



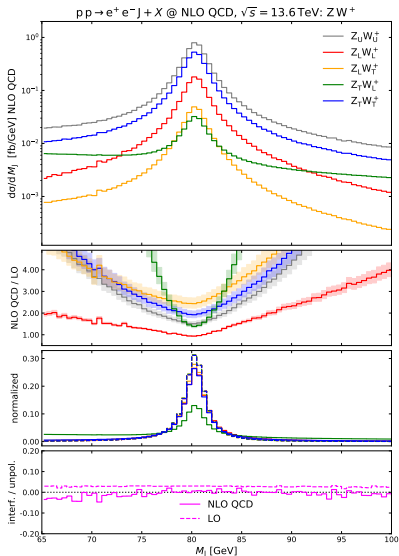
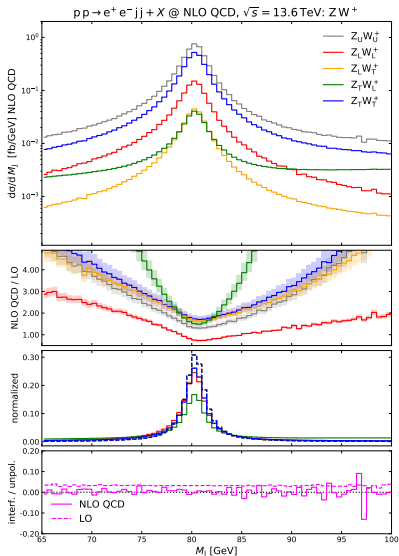
Sensitive to the production dynamics of the W<sup>+</sup> and Z bosons

# Scattering angle $\cos(\vartheta_{scatt}) = \frac{|\vec{p}_{e^+e^-}^{CM}, z|}{|\vec{p}_{e^+e^-}^{CM}|}$

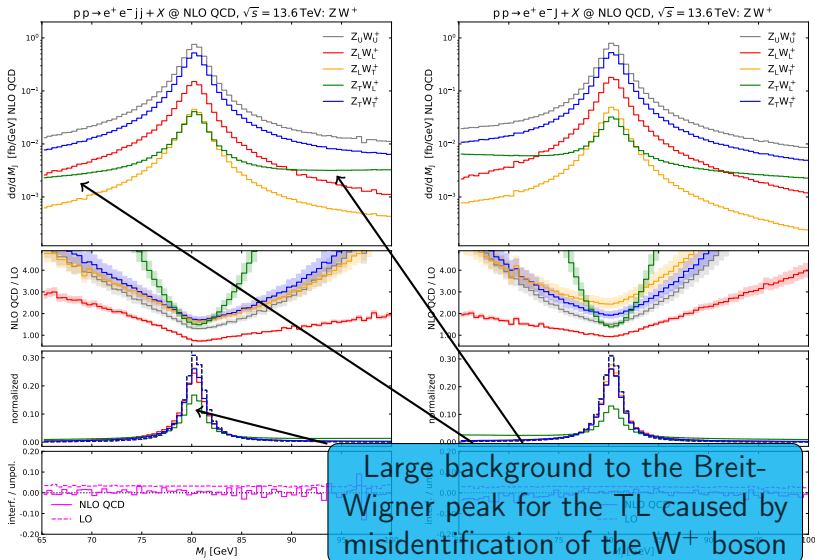


NLO corrections drastically change the shape of the TT caused by the approximate amplitude-zero effect at LO

# Invariant mass jet-system $M_J = \sqrt{p_J^2}$

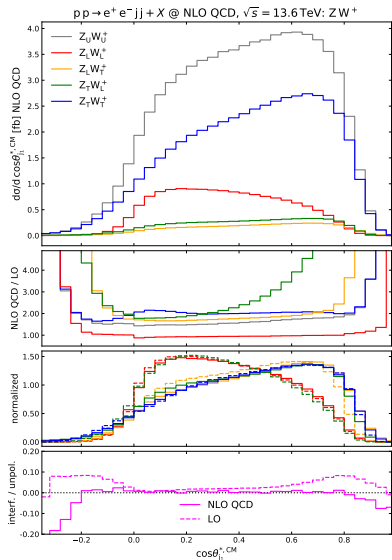


# Invariant mass jet-system $M_J = \sqrt{p_J^2}$

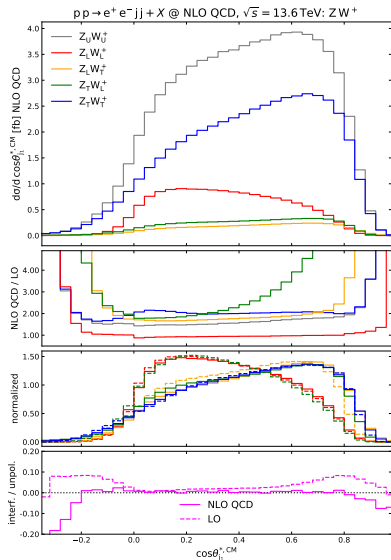


Large background to the Breit-Wigner peak for the TLQCD caused by misidentification of the W<sup>+</sup> boson

# Decay angle hardest decay-jet $\cos(\vartheta_{j_1}^{*,\text{CM}}) = \frac{\vec{p}_{j_1}^* \cdot \vec{p}_J^{\text{CM}}}{|\vec{p}_{j_1}^*| |\vec{p}_J^{\text{CM}}|}$



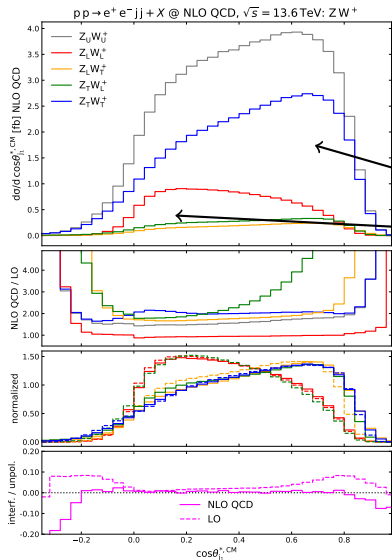
# Decay angle hardest decay-jet $\cos(\vartheta_{j_1}^{*,\text{CM}}) = \frac{\vec{p}_{j_1}^* \cdot \vec{p}_J^{\text{CM}}}{|\vec{p}_{j_1}^*| |\vec{p}_J^{\text{CM}}|}$



This variable is very sensitive to the polarisation of the W<sup>+</sup> boson similar to the decay angles of the leptons

The jets can only be distinguished by their transverse momentum or other measurable quantities not by their flavour

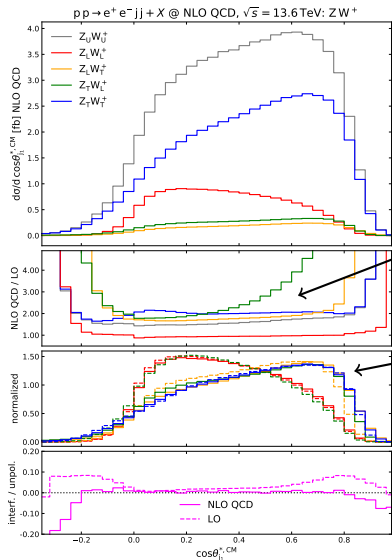
# Decay angle hardest decay-jet $\cos(\vartheta_{j_1}^{*,CM}) = \frac{\vec{p}_{j_1}^* \cdot \vec{p}_J^{CM}}{|\vec{p}_{j_1}^*| |\vec{p}_J^{CM}|}$



Hardest jet is predominantly emitted in the direction of the jet system



# Decay angle hardest decay-jet $\cos(\vartheta_{j_1}^{*,\text{CM}}) = \frac{\vec{p}_{j_1}^* \cdot \vec{p}_J^{\text{CM}}}{|\vec{p}_{j_1}^*| |\vec{p}_J^{\text{CM}}|}$








k-factor is flat in the central region for LL, TT, LT

TL has a large shape change from LO to NLO




# Summary

- Calculated the polarised cross-sections for  $ZW^+$  production with semileptonic decay
  - ▶ Used the double-pole approximation to define polarised  $ZW^+$  production
  - ▶ Used methods can be directly extended to the calculation of the NLO QCD corrections to semileptonic decays of other processes
    - ★ Resonant background  $ZZ$  and  $ZW^-$  production
    - ★ Vector-boson pair production processes
    - ★ Vector-boson scattering processes
- Hadronic decays are different from purely leptonic decays
  - ▶ Higher event rate
  - ▶ Very large QCD background and resonant  $ZZ$ ,  $ZW^-$  background
- Many observables are well suited to distinguish the polarisation states
  - ▶ This sensitivity remains even when the jets are recombined to one jet and become indistinguishable (unresolved setup)

# Bibliography I

-  D. Buarque Franzosi, O. Mattelaer, R. Ruiz, and S. Shil, *Automated predictions from polarized matrix elements*, *JHEP* **04** (2020) 082, [arXiv:1912.01725].
-  A. Denner and G. Pelliccioli, *NLO QCD predictions for doubly-polarized WZ production at the LHC*, *Phys. Lett. B* **814** (2021) 136107, [arXiv:2010.07149].
-  D. N. Le and J. Baglio, *Doubly-polarized WZ hadronic cross sections at NLO QCD+EW accuracy*, arXiv:2203.01470.
-  D. N. Le, J. Baglio, and T. N. Dao, *Doubly-polarized WZ hadronic production at NLO QCD+EW: Calculation method and further results*, arXiv:2208.09232.
-  T. N. Dao and D. N. Le, *Enhancing the doubly-longitudinal polarization in WZ production at the LHC*, arXiv:2302.03324.

# Bibliography II

-  ATLAS Collaboration, *Measurement of  $W^\pm Z$  production cross sections and gauge boson polarisation in  $pp$  collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector*, *Eur. Phys. J. C* **79** (2019) 535, [arXiv:1902.05759].
-  CMS Collaboration, *Measurement of the inclusive and differential  $WZ$  production cross sections, polarization angles, and triple gauge couplings in  $pp$  collisions at  $\sqrt{s} = 13$  TeV*, *Journal of High Energy Physics* **2022** (jul, 2022) [arXiv:2110.11231].
-  ATLAS Collaboration, *Observation of gauge boson joint-polarisation states in  $W^\pm Z$  production from  $pp$  collisions at  $\sqrt{s} = 13$  TeV with the ATLAS detector*, arXiv:2211.09435.

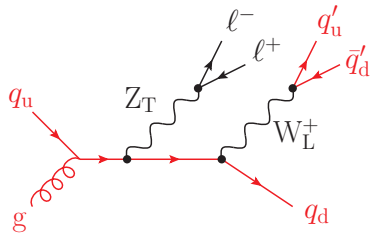
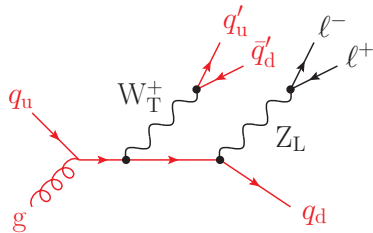
# Bibliography III



CMS Collaboration, *Search for heavy resonances decaying to ZZ or ZW and axion-like particles mediating nonresonant ZZ or ZH production at  $\sqrt{s} = 13$  TeV*, *JHEP* **04** (2022) 087, [arXiv:2111.13669].

# Backup Slides

# Dominant Diagrams LT TL



- For these diagrams the longitudinally polarised boson and the additional quark are predominantly emitted in a similar spatial direction
- This allows for a lower transverse momentum of the longitudinally polarised boson
- The lower transverse momentum leads to less unitarity cancellations

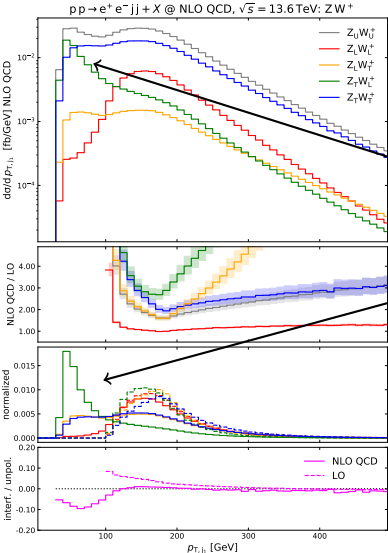
# Results without $p_T$ cut on the jet system

state	$\sigma_{\text{LO}}$ [fb]	$f_{\text{LO}}[\%]$	$\sigma_{\text{NLO}}$ [fb]	$f_{\text{NLO}}[\%]$	$K_{\text{NLO}}$	$K_{\text{NLO}}^{(\text{no g})}$
resolved (no minimum $p_{Tjj}$ cut), $Z(e^+e^-)W^+(jj)$						
unpol.	1.8564(1) <sup>+1.2%</sup> <sub>-1.4%</sub>	100	5.5388(8) <sup>+10.6%</sup> <sub>-8.6%</sub>	100	2.984	1.371
$Z_L W_L^+$	0.64605(3) <sup>+0.2%</sup> <sub>-0.6%</sub>	34.8	0.7525(4) <sup>+1.5%</sup> <sub>-1.2%</sub>	13.6	1.165	1.194
$Z_L W_T^+$	0.08687(1) <sup>+0.2%</sup> <sub>-0.6%</sub>	4.7	0.3057(1) <sup>+11.4%</sup> <sub>-9.2%</sub>	5.5	3.519	1.462
$Z_T W_L^+$	0.08710(1) <sup>+0.1%</sup> <sub>-0.6%</sub>	4.7	1.0486(1) <sup>+14.6%</sup> <sub>-11.9%</sub>	18.9	12.04	2.408
$Z_T W_T^+$	0.97677(7) <sup>+2.0%</sup> <sub>-2.2%</sub>	52.6	3.5506(9) <sup>+11.8%</sup> <sub>-9.6%</sub>	64.1	3.635	1.424
interf.	0.0595(1)	3.2	-0.119(2)	-2.1	-	-

- LO results are unchanged
- NLO corrections become larger in particular for TL

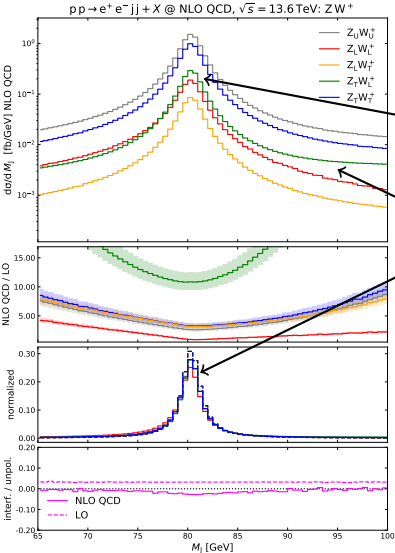


# Results without $p_T$ cut on the jet system



Large peak in the low  $p_{T,j_1}$  region of TL is cut away by transverse momentum cut on the  $W^+$  boson

# Results without $p_T$ cut on the jet system



Breit-Wigner peak is now unsuppressed

Background still exists but is smaller compared to the peak