

# Radial Strip Detectors for Cosmic Ray Studies

4th Allpix Squared User Workshop

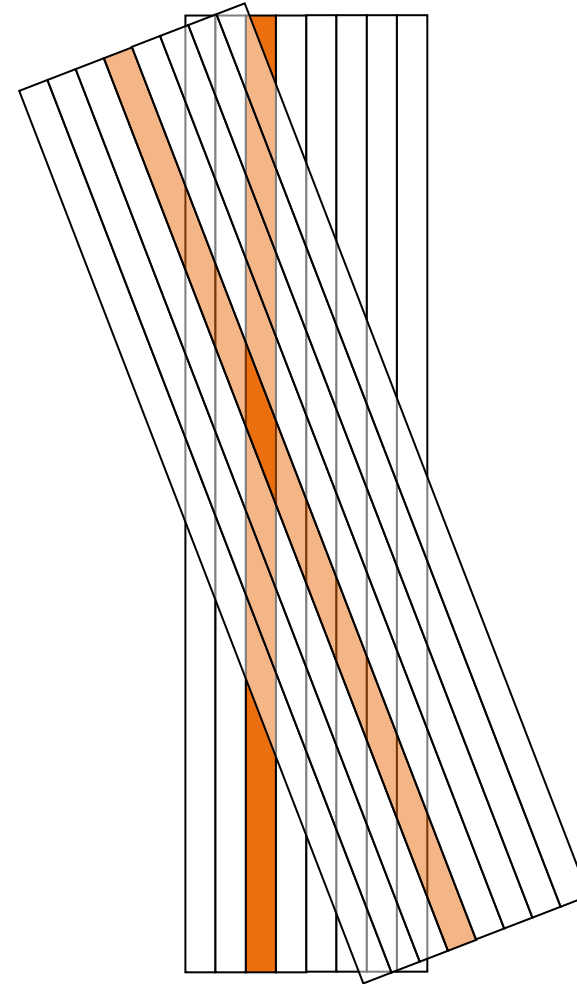
Maximilian Caspar, Radek Privara  
Hamburg, 22.05.2023

# ATLAS ITk Strips Modules

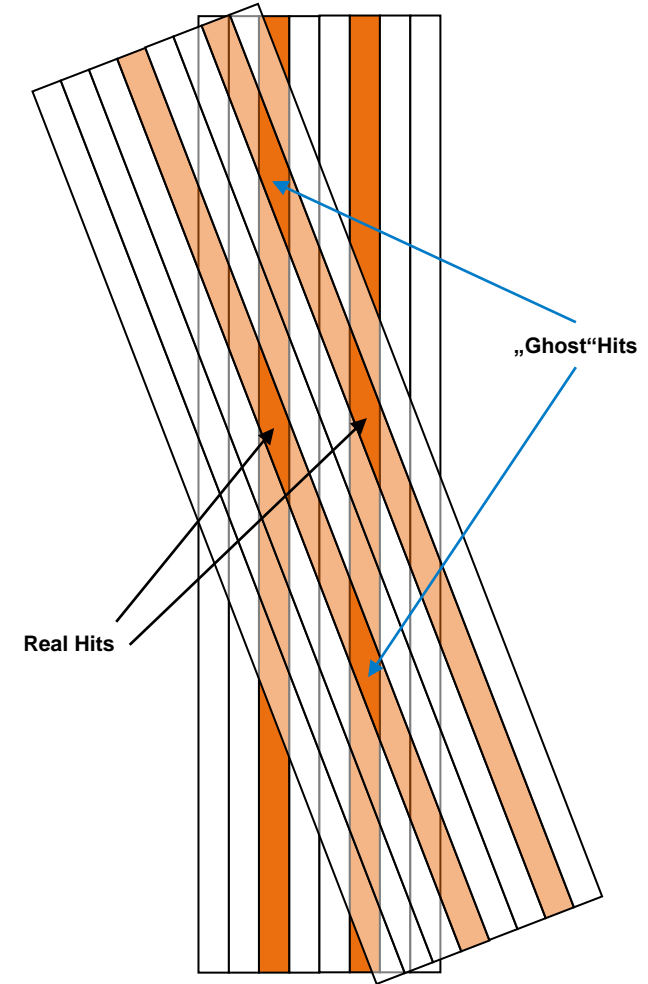
## What are Strip Detectors?

### Strips

- Strips are basically “very long pixels” (usually several cm)
- $n \times n$  Pixel Detector:  $n^2$  readout channels
- Covering the same area with 2 strip detectors:  $2n$  channels
- Stereo angle allows for reconstruction of 2D position, but leaves ambiguity in multi-hit events



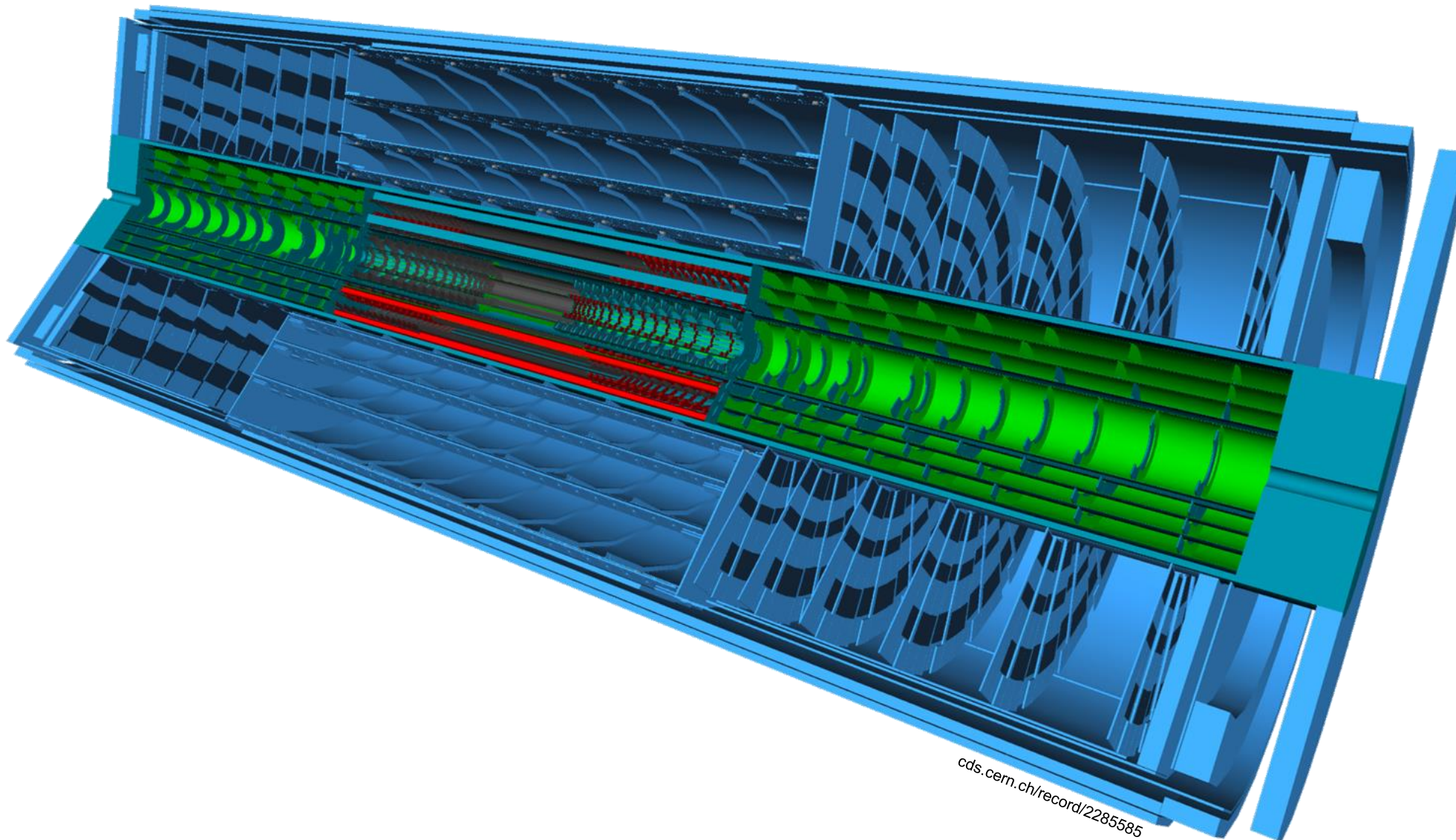
Single Hit with Stereo Angle



Multiple Hits with Stereo Angle

# ATLAS ITk Strips Modules

## The Detector Layout

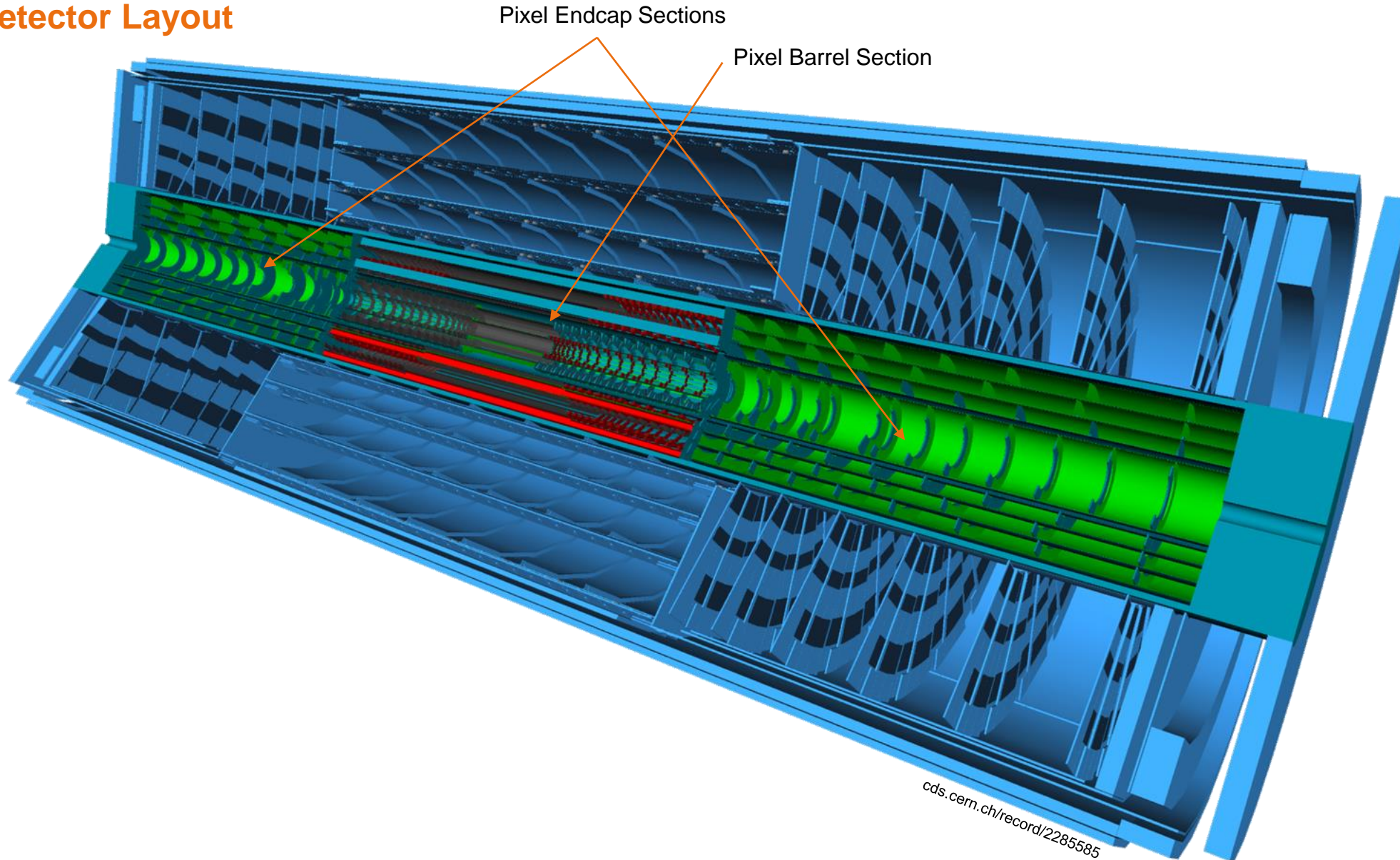


[cds.cern.ch/record/2285585](https://cds.cern.ch/record/2285585)



# ATLAS ITk Strips Modules

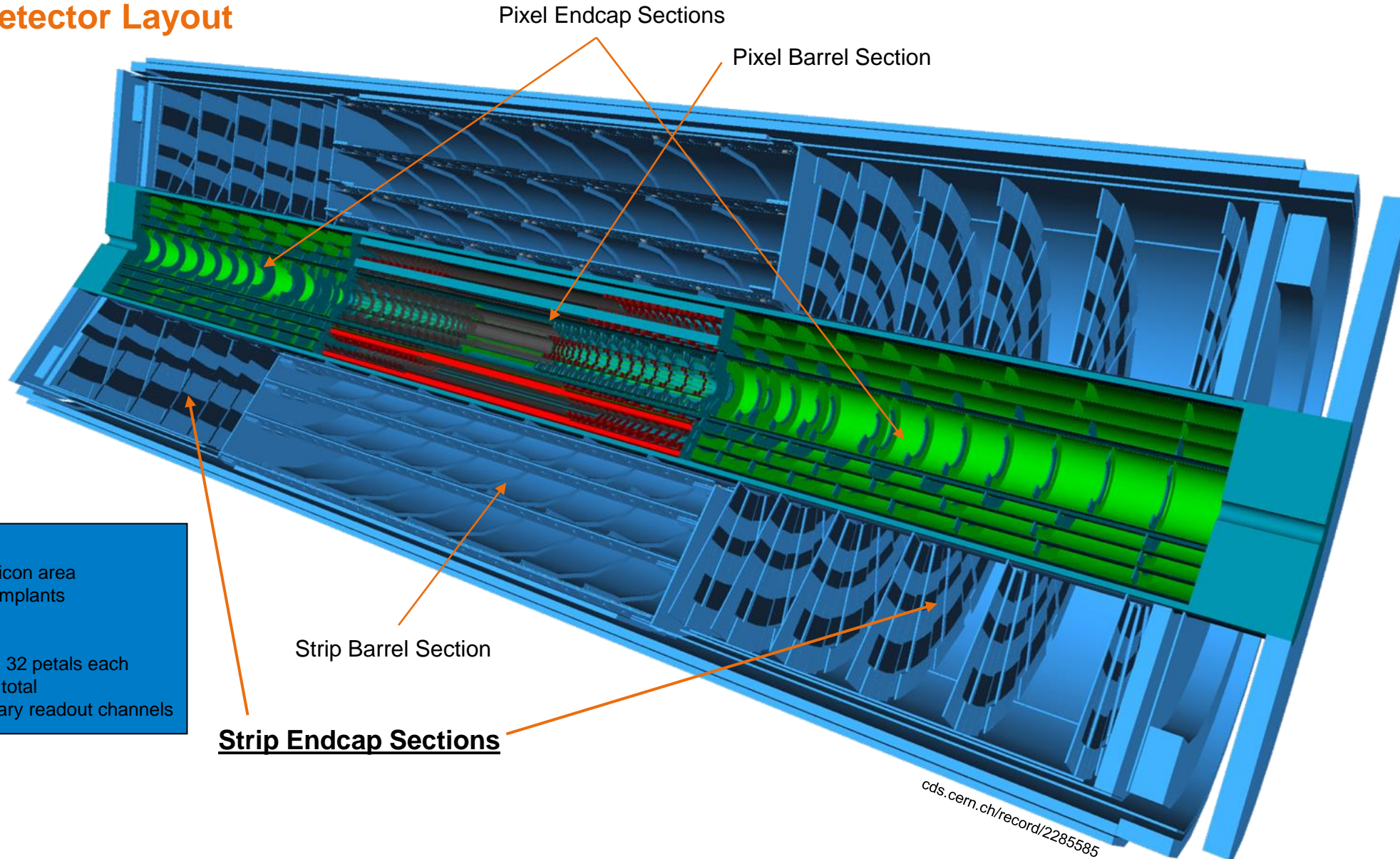
## The Detector Layout





# ATLAS ITk Strips Modules

## The Detector Layout



**Itk Strips**  
~ 165 m<sup>2</sup> of silicon area  
p-bulk with n implants

**Endcaps**  
2x6 discs with 32 petals each  
6912 sensors total  
22060032 binary readout channels

**Strip Endcap Sections**

Strip Barrel Section

Pixel Endcap Sections

Pixel Barrel Section

[cds.cern.ch/record/2285585](https://cds.cern.ch/record/2285585)

# ATLAS ITk Strips Modules

## Building the Petal

### The Rings

- Petal made up of six rings R0 – R5
- Module in rings R3 – R5 are split

### The Sides

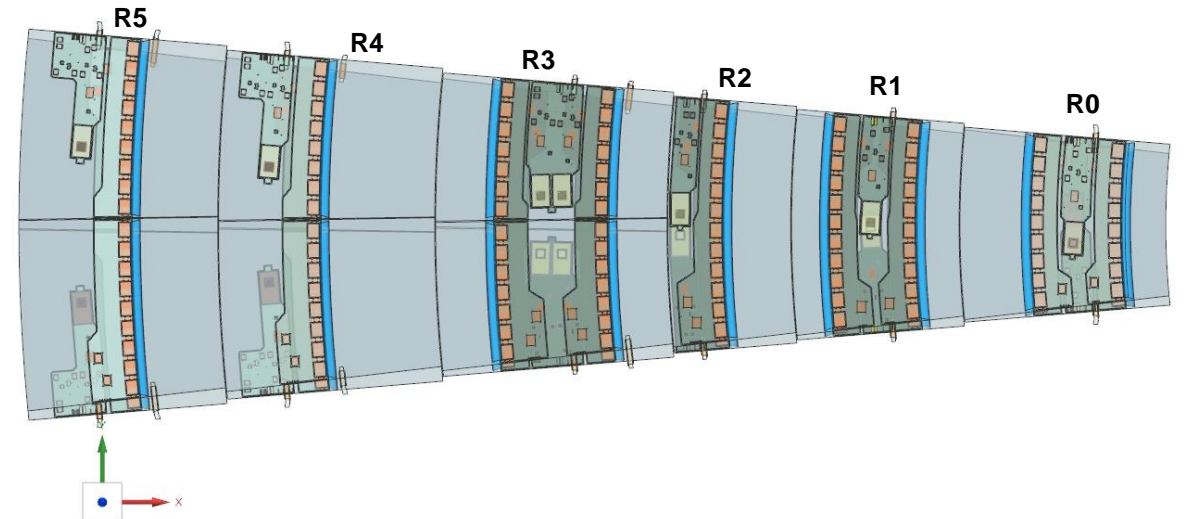
- Each petal has a front and a back side
- Back side sensors are rotated 180°

### For Simulations

- Complete module positions for a single petal available in an Allpix<sup>2</sup> example
  - In petal coordinates (relative to origin fiducial)

Available at

[https://gitlab.cern.ch/allpix-squared/allpix-squared/-/tree/radial\\_det\\_fix\\_center/examples/atlas\\_itk\\_petal](https://gitlab.cern.ch/allpix-squared/allpix-squared/-/tree/radial_det_fix_center/examples/atlas_itk_petal)



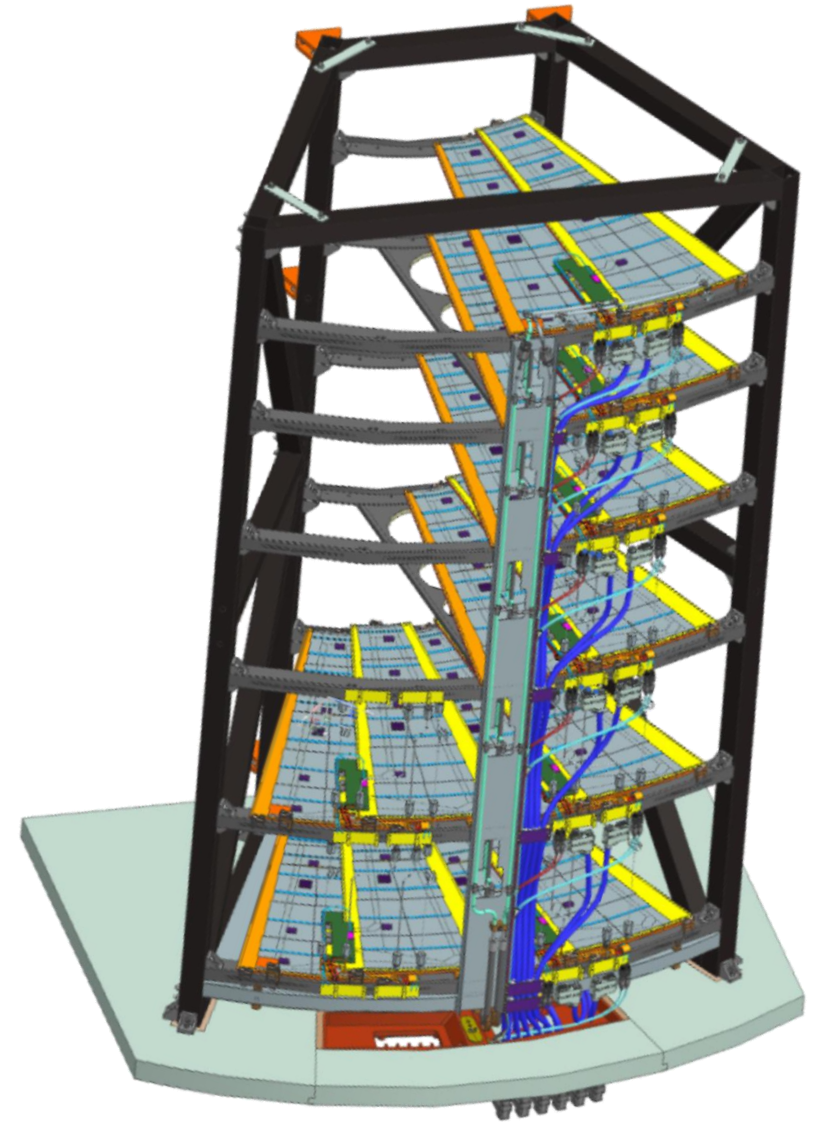
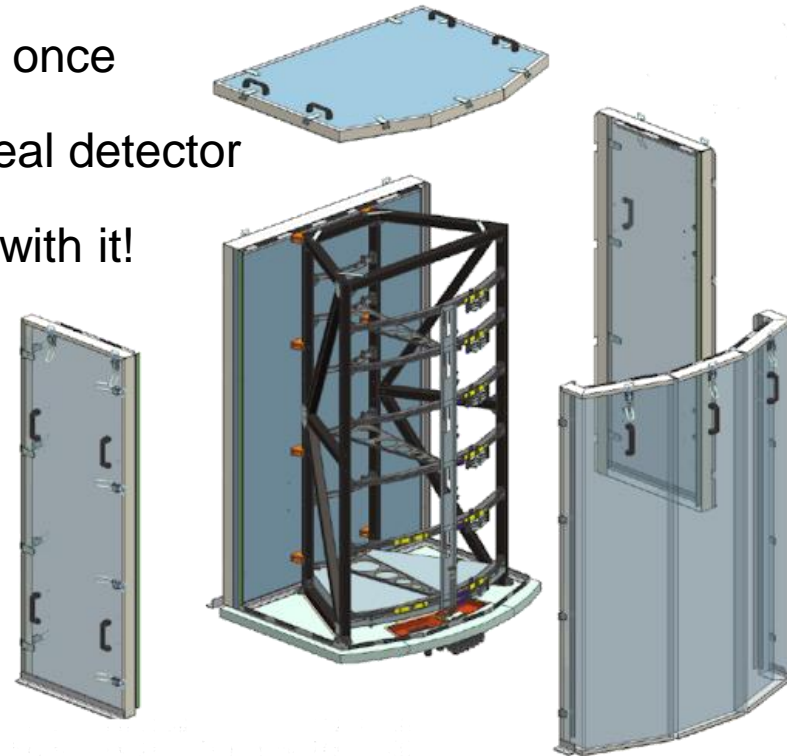


# ATLAS ITk Strips Modules

## Endcap System Test

### System Tests at DESY

- 1/8 slice of the Endcap as a testing environment
- Can support up to 12 petals at once
- Services & DAQ close to the real detector
- Plan: Measure cosmic muons with it!

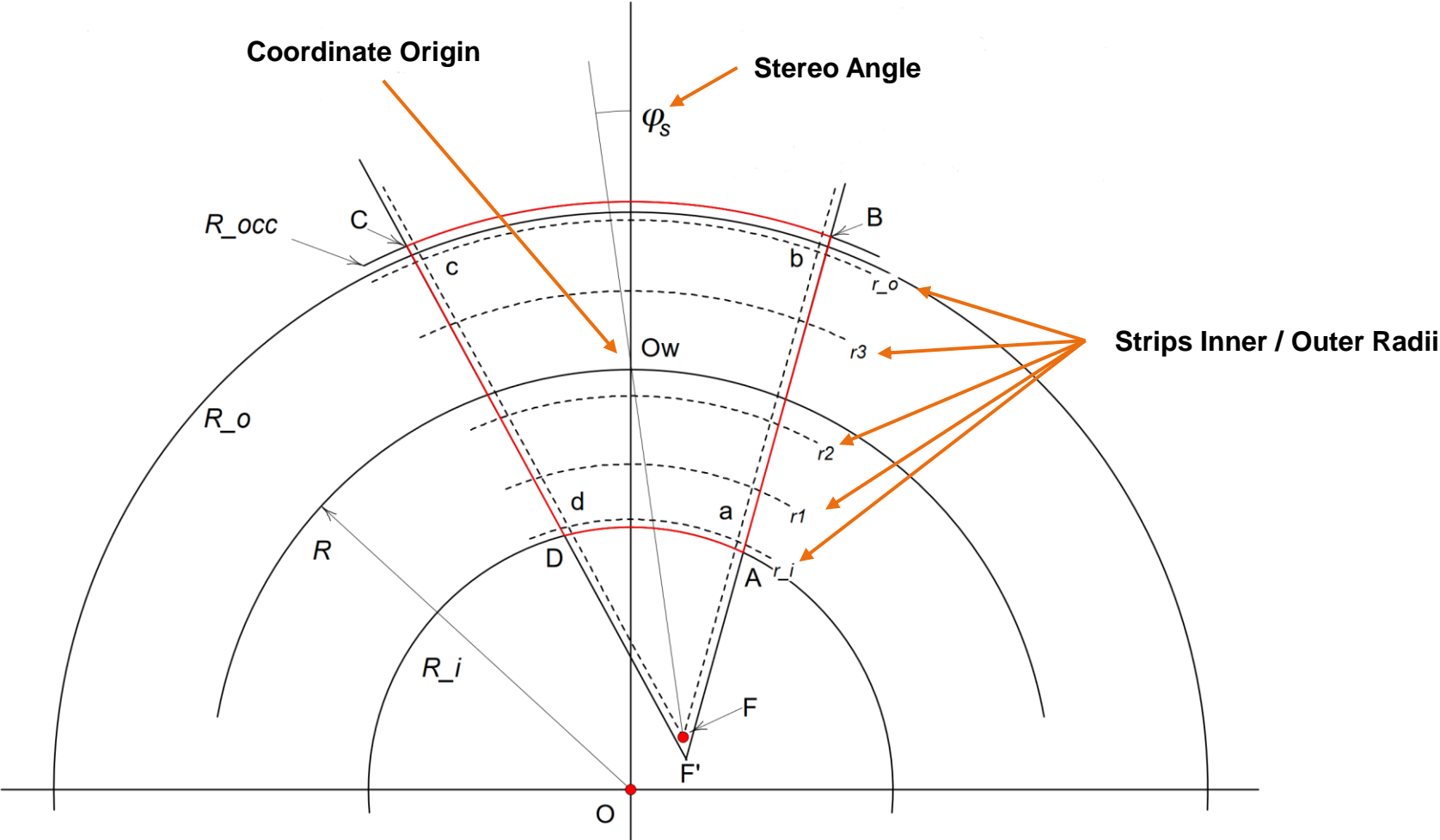






# ATLAS ITk Strips Modules

## The Stereo Annulus Geometry



# ATLAS ITk Strips Modules

## The Stereo Annulus Geometry

### Coordinate System

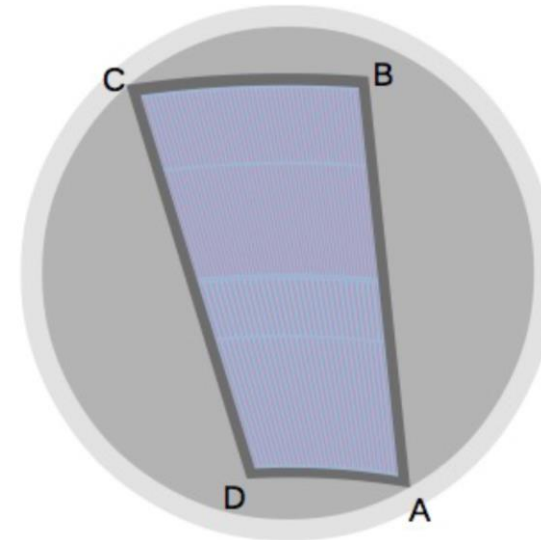
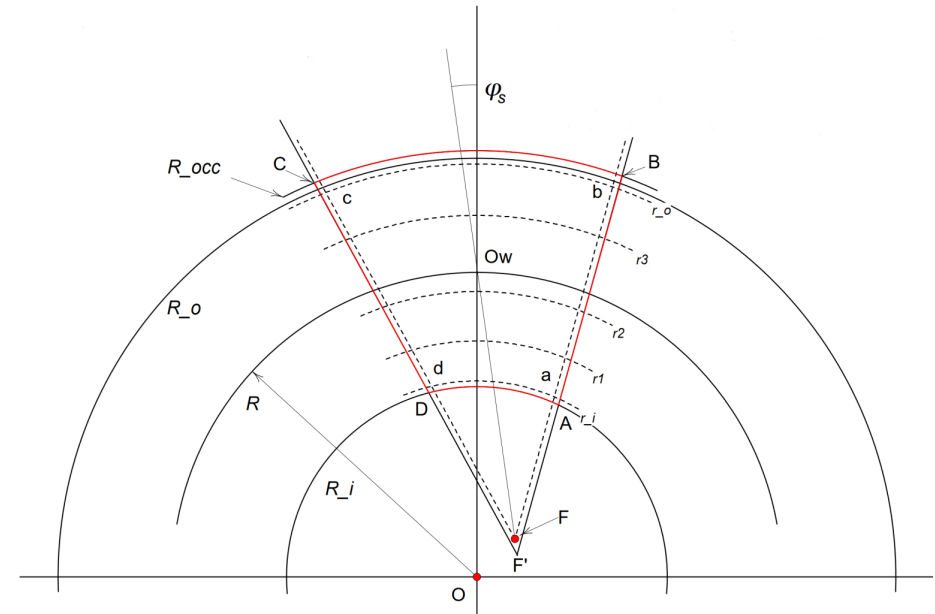
- R defined by distance to the beam axis
- $\Phi$  defined in relation to a shifted point F

### Outer Shape

- Intersection between two annulus sections
- The second annulus section is rotated by the stereo angle around the origin point
- Added additional distance around the active area

### Strips

- All strips in a row start & end at the same radii
- Each row has the same angular pitch



# Simulation

## Tacking Telescope with Radial Sensors

### R0 Telescope Simulation Benchmark

- Geometry of the Radial Strip sensors newly implemented in Allpix<sup>2</sup> & Corry
- Telescope made up of R0 modules served as a first benchmark of our implementation

### Results

- Good tracking performance with a Straight Line Track model

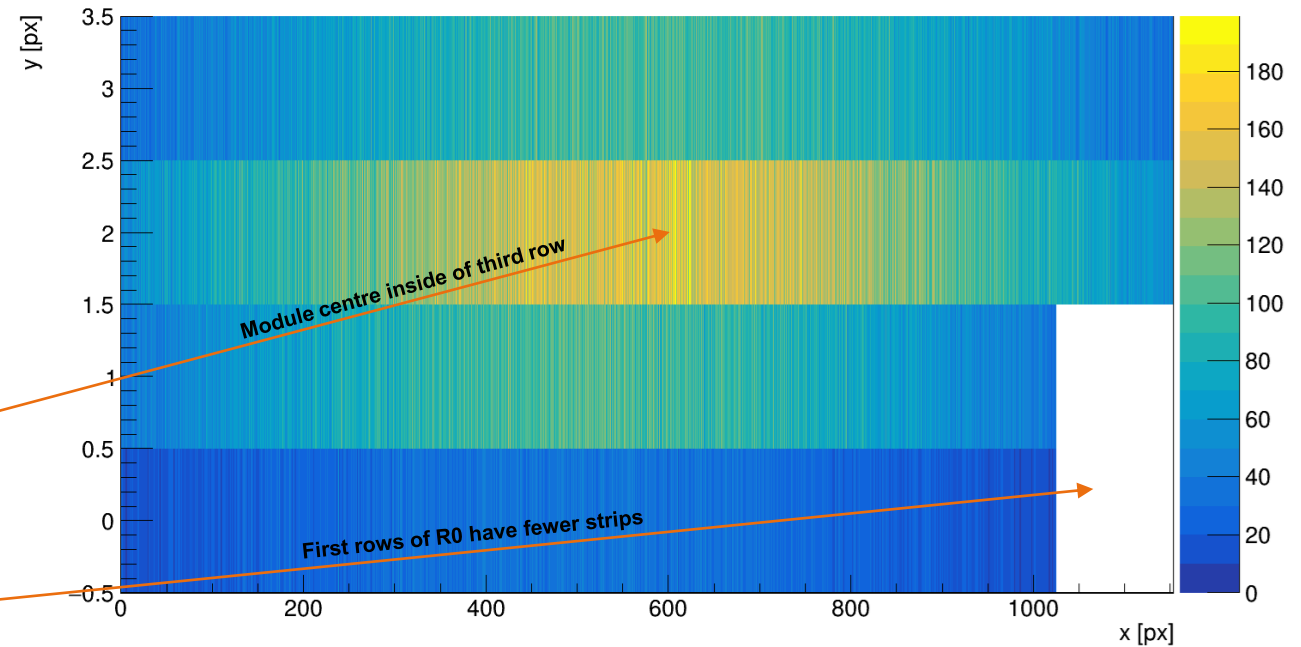
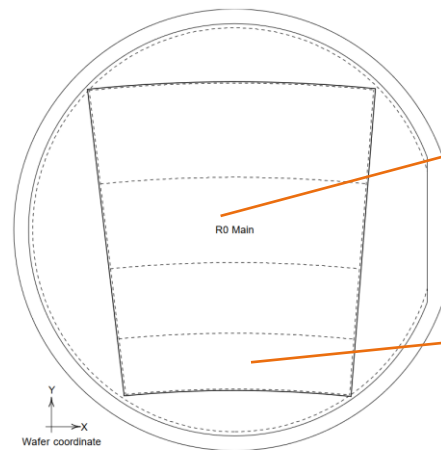
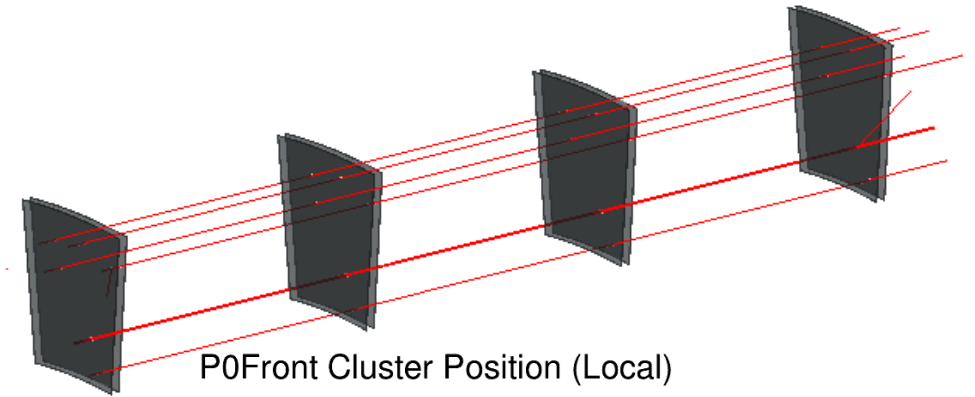


Fig.4 Endcap wafer layout: R0

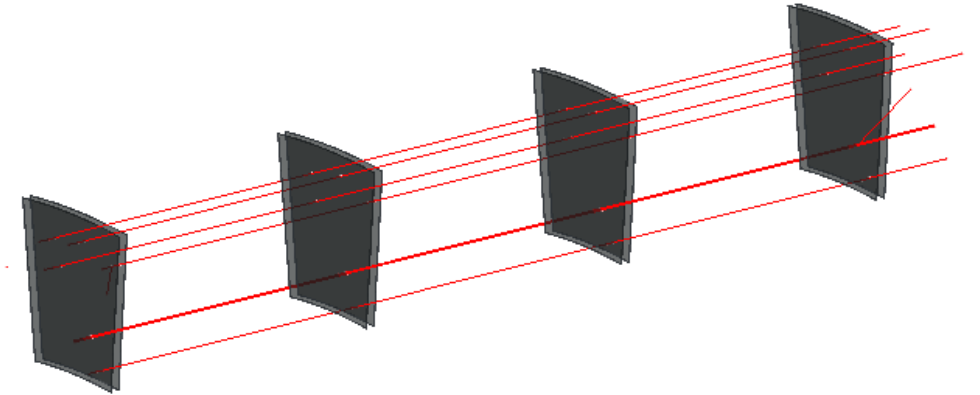


# Simulation

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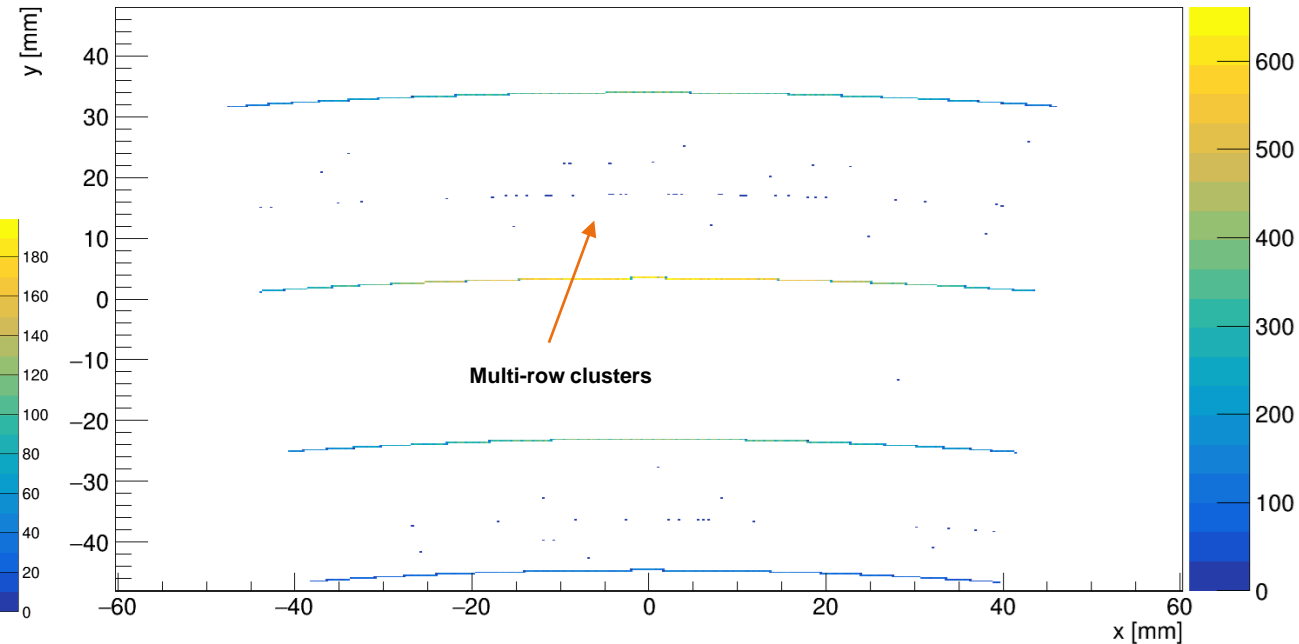
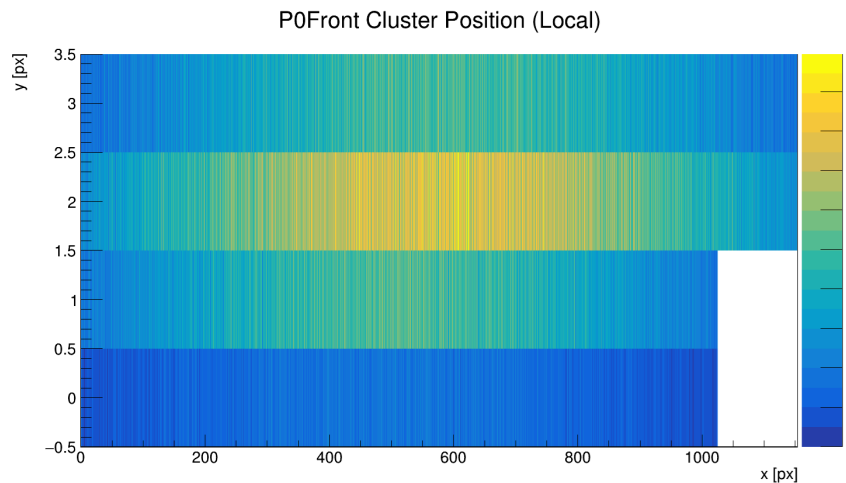
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P0Front Cluster Position (Global)

### Results

- Good tracking performance with a Straight-Line Track model

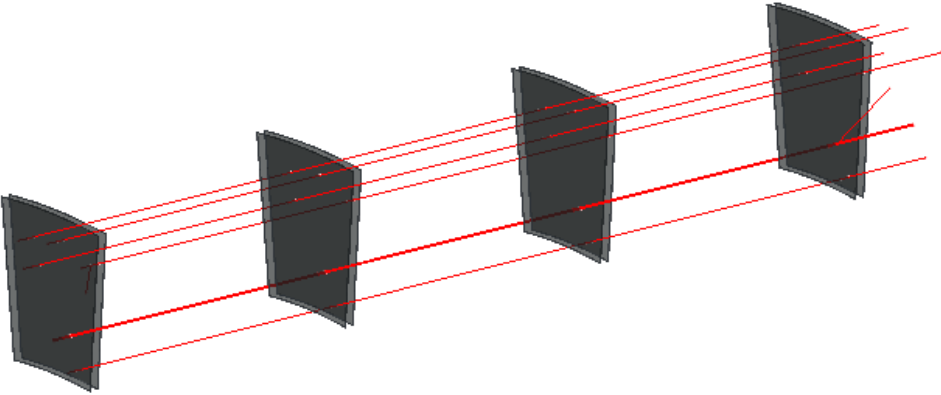


# Simulation

## Tacking Telescope with Radial Sensors

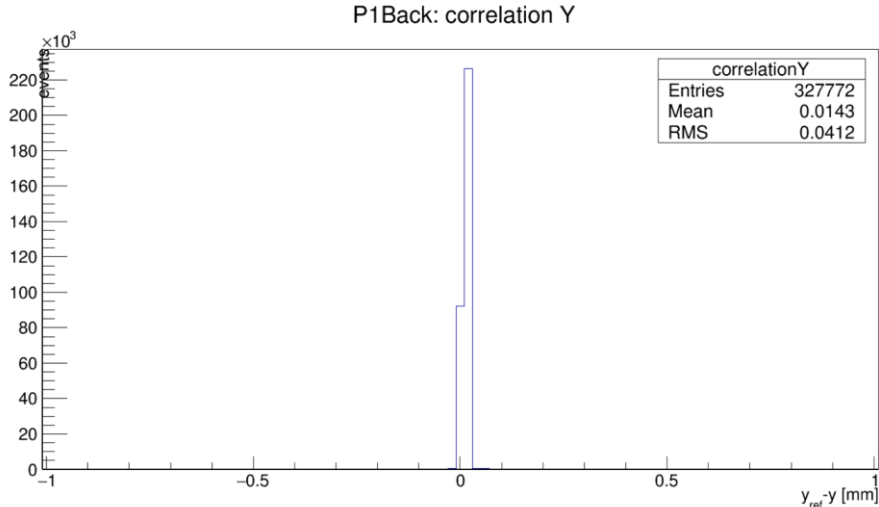
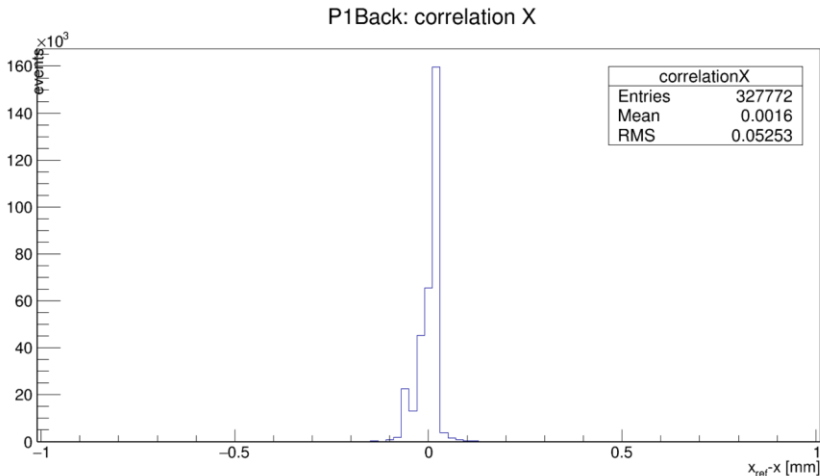
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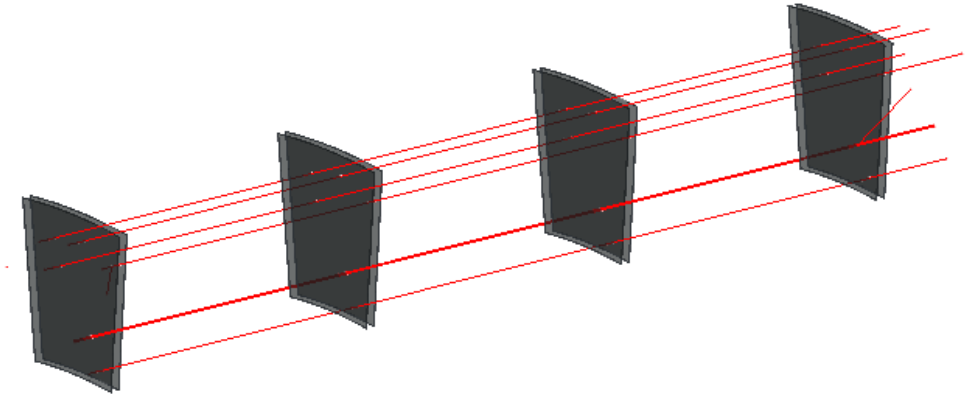


# Simulation

## Tacking Telescope with Radial Sensors

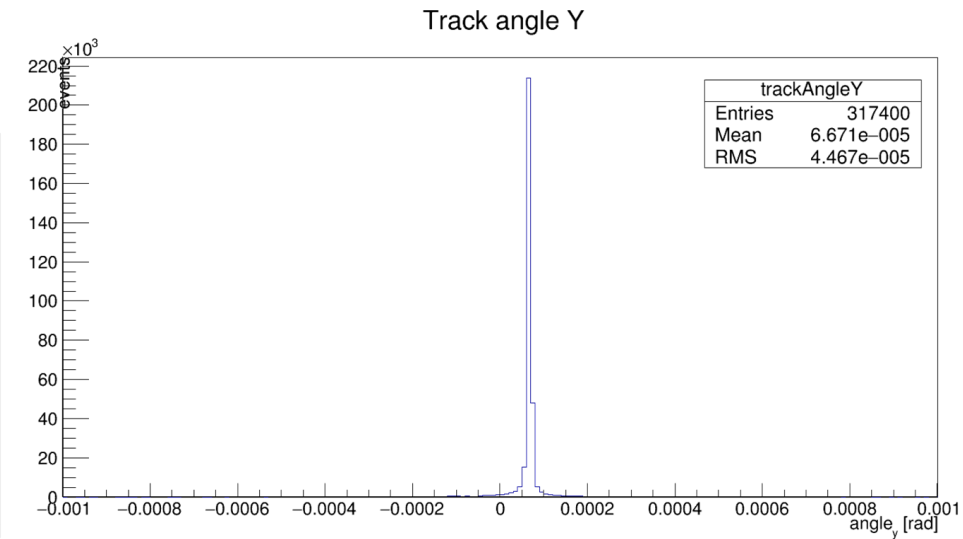
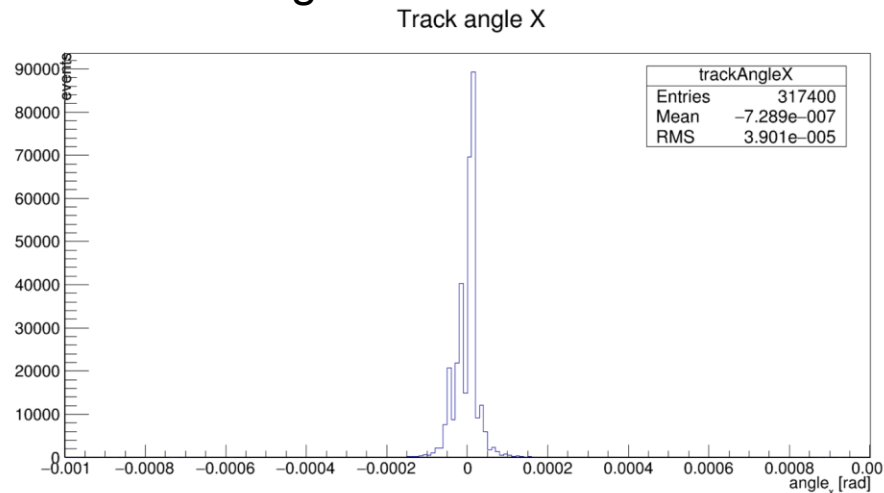
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### Results

- Good tracking performance with a Straight Line Track model





# Simulation

## Cosmic Rays in Allpix<sup>2</sup>

### Cosmic-ray Shower Library (CRY)

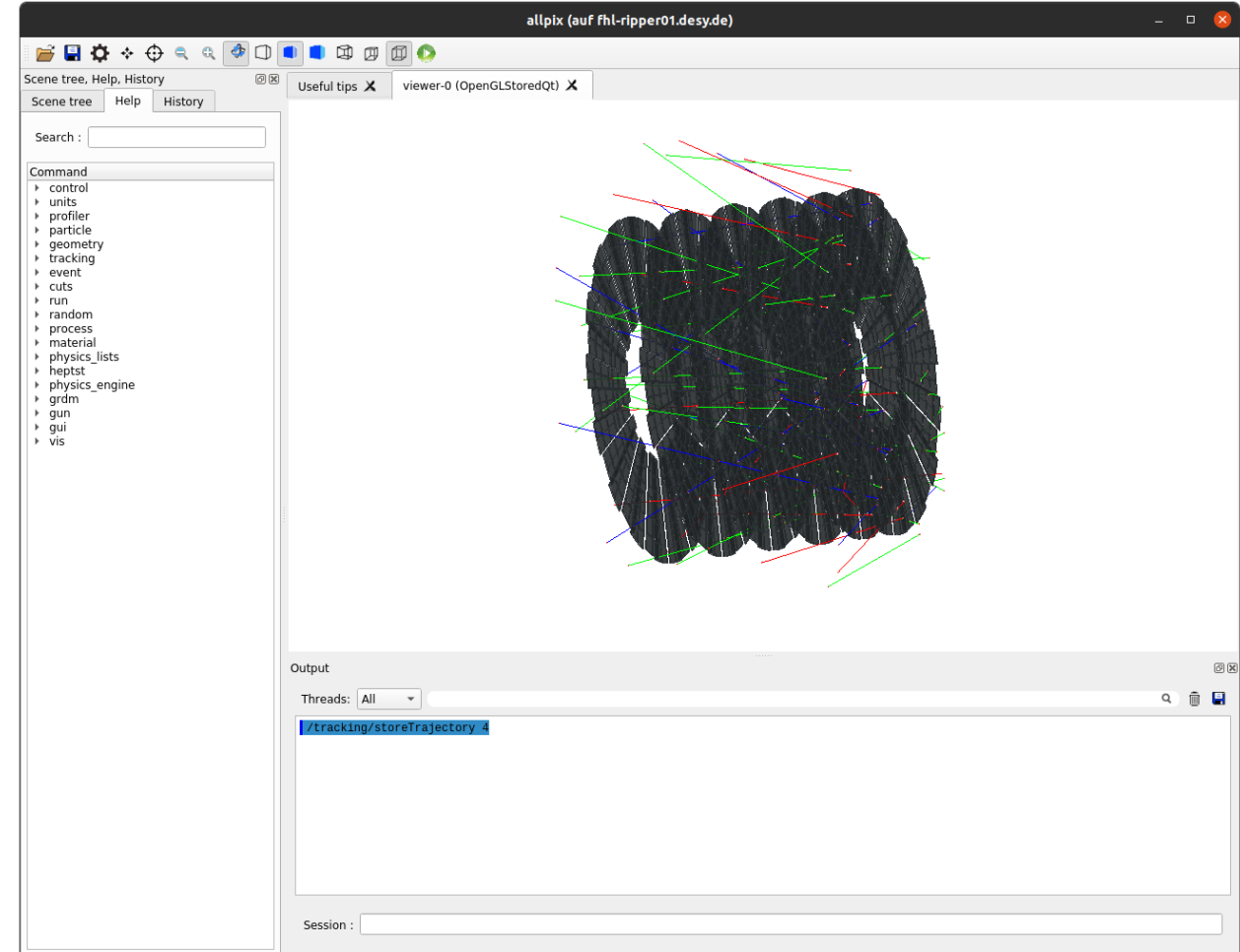
- Generates realistic cosmic ray distributions
- Particles are returned in a square plane surface

<https://doi.org/10.1109/NSSMIC.2007.4437209>

### The DepositionCosmics Module

- Can be called within Allpix<sup>2</sup> to generate showers
- Allows for selection of CRY framework parameters
  - Altitude & Latitude
  - Solar Cycle
  - Particles Types
- Returns total simulated time for all events

<https://gitlab.cern.ch/allpix-squared/allpix-squared/-/tree/master/src/modules/DepositionCosmics>



# Simulation

## Procedural Geometry Generation

### Endcap Geometry

- Endcap has 6 discs
  - Each disc has 16 front and 16 back petals
  - Petals are evenly spaced on the disc

### Procedural Generation

- For each petal position the sensor coordinates are transformed
  - Rotation of  $22.5^\circ$  per segment around the beam axis ( $+ 11.25^\circ$  for back petals)
  - Displacement in z depending on disc number ( $+ 17$  mm for front petals)
- Detector center of mass (in XY) is calculated and subtracted

```
def makePetal(disc=0, front=True, segment=0):
    discDisplacement = DISPLACEMENTS[disc]
    angleDisplacement = segment * 22.5
    if not front:
        angleDisplacement += 11.25
    else:
        discDisplacement += 17

    # Make front sensors
    sensors = getSensors()
    for s in sensors:
        module = {}
        module["Type"] = sensors[s]["type"]
        module["Z"] = sensors[s]["Z"]
        module["Z"] += discDisplacement
        module["X"] = cos(radians(angleDisplacement)) * sensors[s]["X"] - \
            sin(radians(angleDisplacement)) * sensors[s]["Y"]
        module["Y"] = sin(radians(angleDisplacement)) * sensors[s]["X"] + \
            cos(radians(angleDisplacement)) * sensors[s]["Y"]
        module["Alpha"] = sensors[s]["Alpha"] + angleDisplacement
    if front:
        module["Name"] = f"D{disc}S{segment}F{s}F"
    else:
        module["Name"] = f"D{disc}S{segment}B{s}F"
    module["Front"] = True
    modules.append(module)

# Make back sensors
sensors = getSensors()
for s in sensors:
    module = {}
    module["Type"] = sensors[s]["type"]
    module["Z"] = - sensors[s]["Z"]
    module["Z"] += discDisplacement
    module["X"] = -cos(radians(angleDisplacement)) * sensors[s]["X"] - \
        sin(radians(angleDisplacement)) * sensors[s]["Y"]
    module["Y"] = -sin(radians(angleDisplacement)) * sensors[s]["X"] + \
        cos(radians(angleDisplacement)) * sensors[s]["Y"]
    module["Alpha"] = - sensors[s]["Alpha"] + angleDisplacement
    if front:
        module["Name"] = f"D{disc}S{segment}F{s}B"
    else:
        module["Name"] = f"D{disc}S{segment}B{s}B"
    module["Front"] = False
    modules.append(module)
```

# Simulation

## System Test Cosmics Setup (4 Petals)

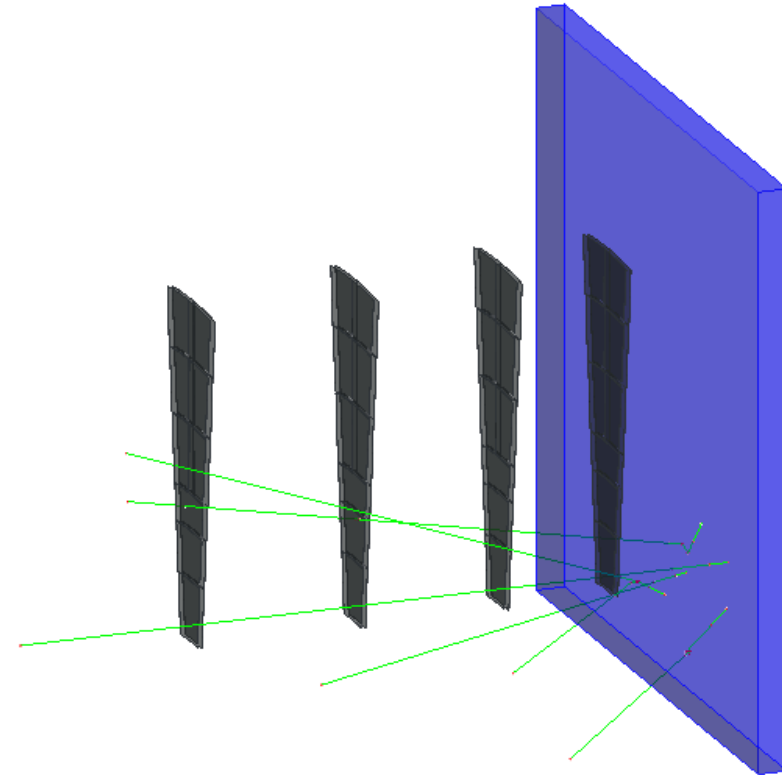
### The Setup in Allpix<sup>2</sup>

- Cosmic muon run with 4 petals planned this year
- Usage of 10 cm concrete ceiling to mimic the laboratory building
- Cosmics generated on 1m x 1m square

### The Analysis in Corryvreckan

- Clustering is done in radial coordinates before conversion into the cartesian system
- At least 7 hits per track
- Rejecting tracks where multiple clusters are in the same z plane

Allpix<sup>2</sup> Setup





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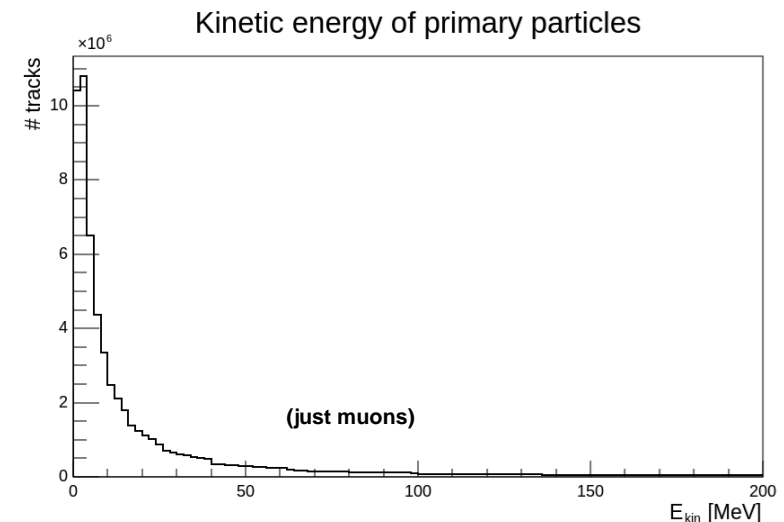
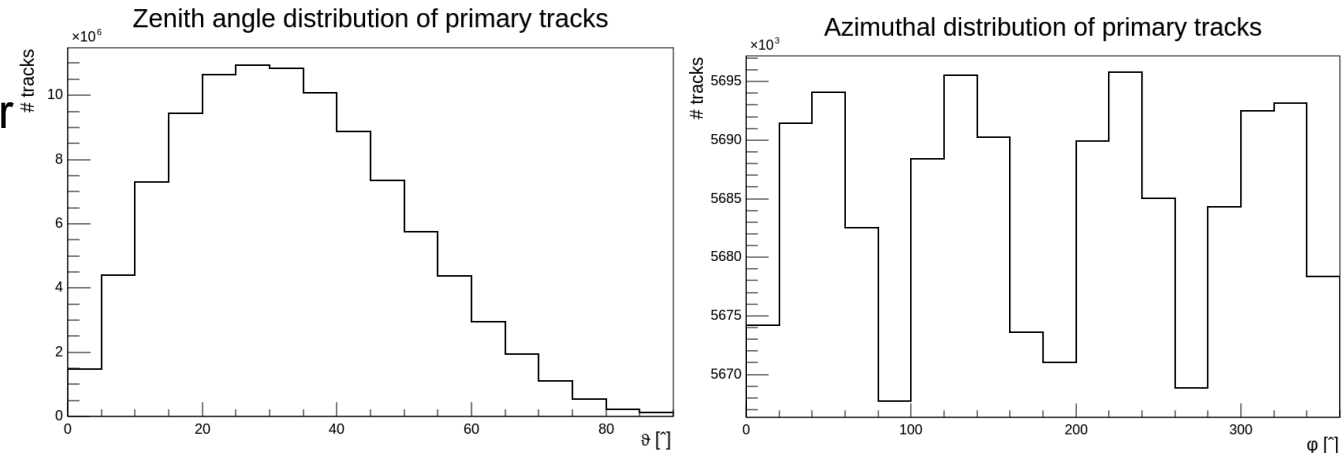
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## CRY Primary Particles



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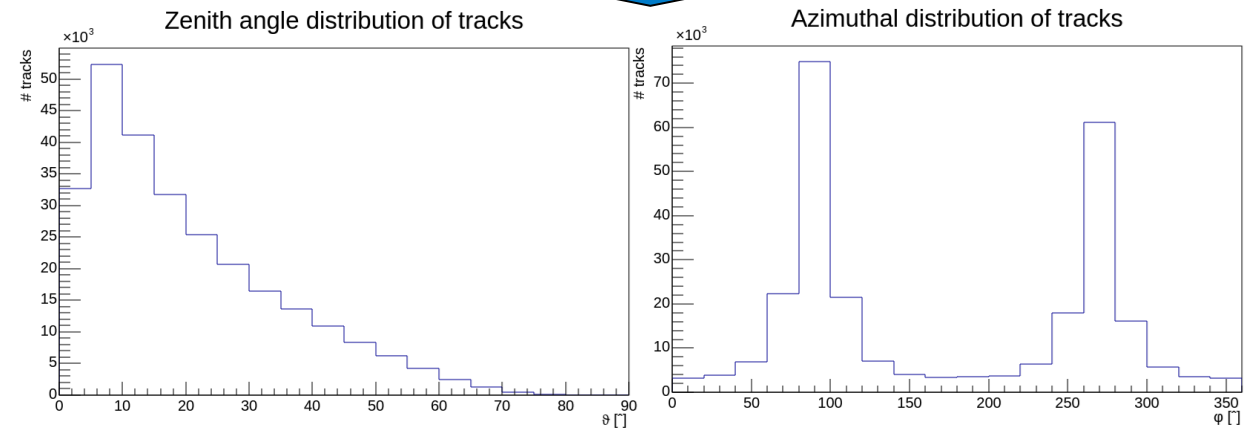
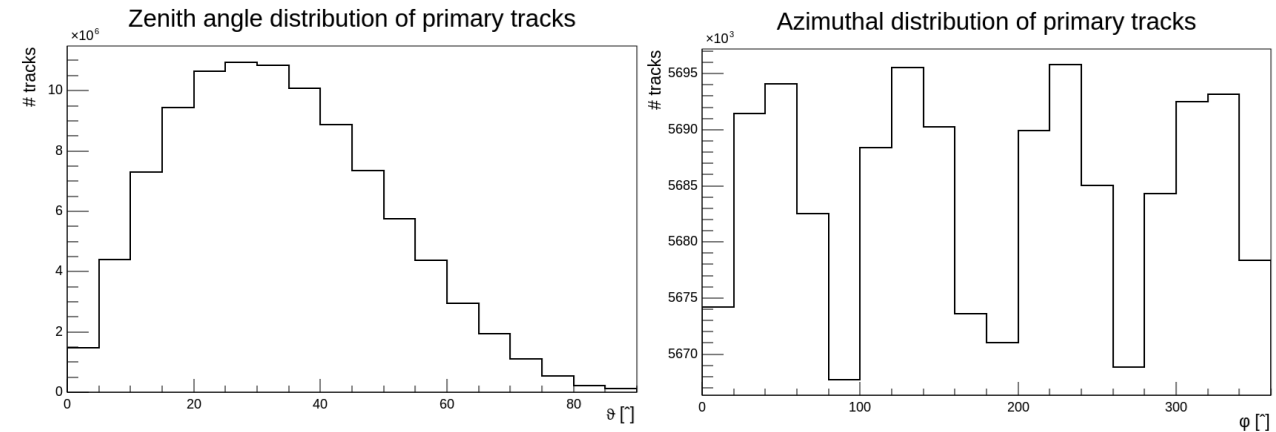
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- Clustering is done in radial coordinates before conversion into the cartesian system
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## Reconstructed Tracks



# Simulation

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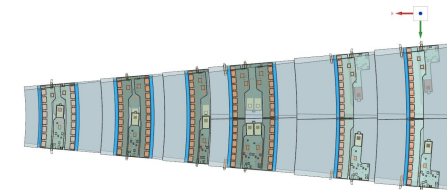
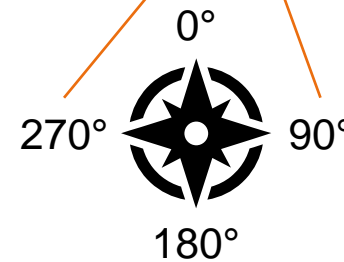
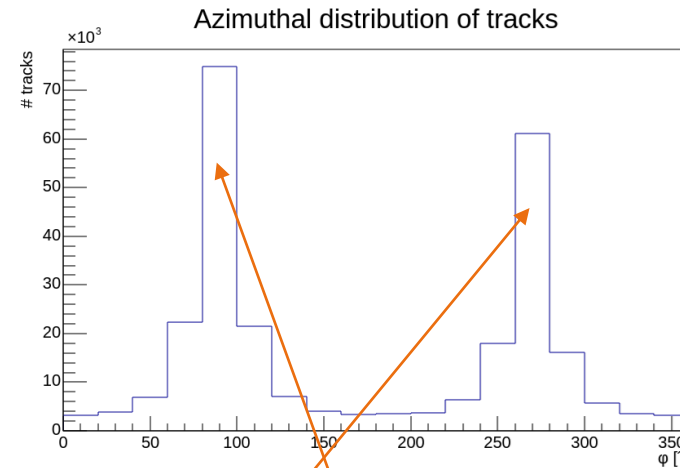
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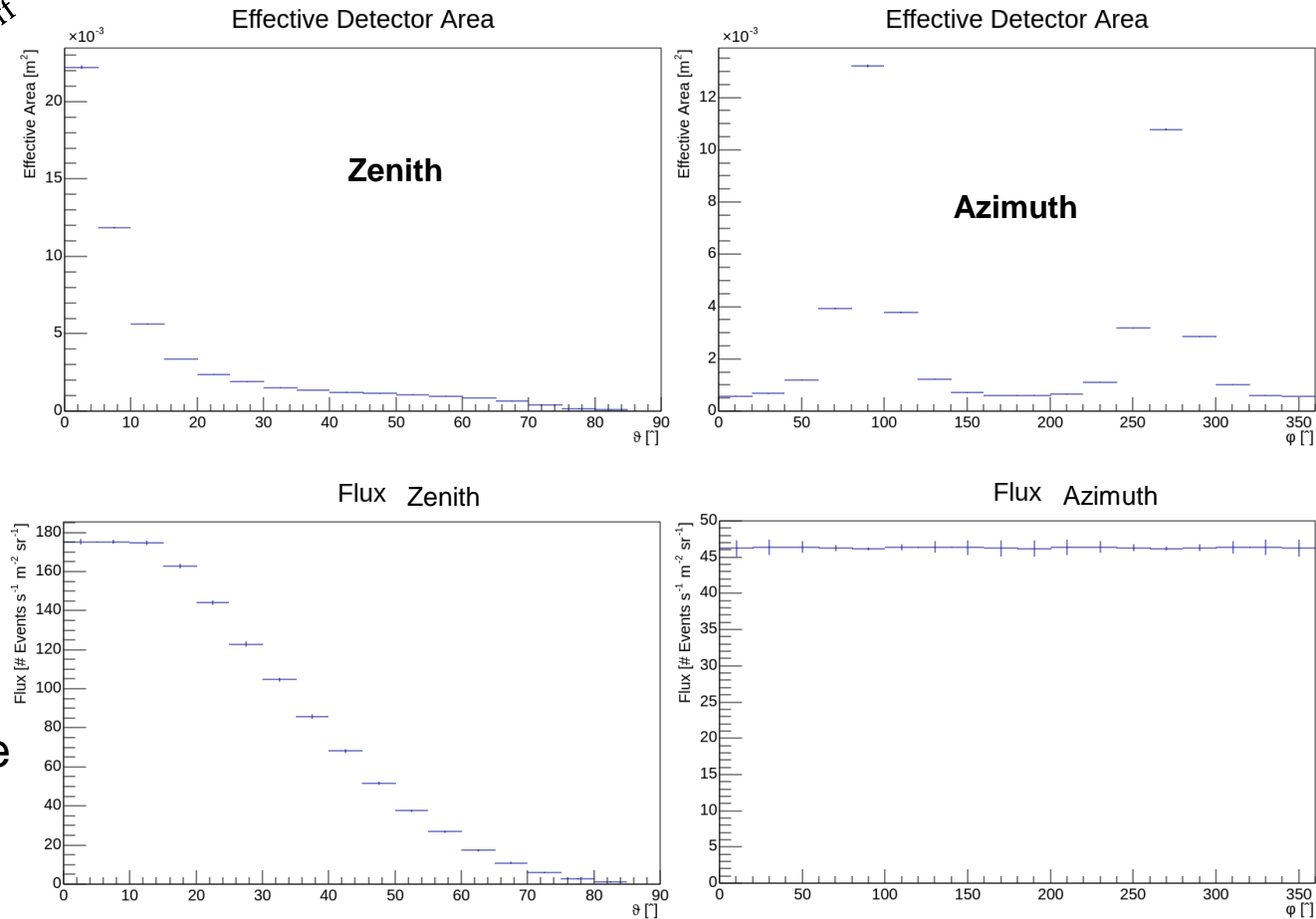
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$$A_{\text{Eff}} = A_0 \cdot \frac{N_{\text{Reconstructed}}}{N_{\text{MC}}}$$

<https://inspirehep.net/literature/1755341> (6.1)

### Flux Measurement



$$\Phi = \frac{N_{\text{Tracks}}}{\delta t \cdot \delta \Omega \cdot A_{\text{Eff}}}$$

# Simulation

## Affective Area Measurement in Allpix<sup>2</sup>

### Effective Area

- Gives detector area estimate for complex 3D particle detectors
- Area is defined by the fraction of particles accepted by the detector

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### Effective Area Simulation with Allpix<sup>2</sup>

1. Simulate cosmic rays hitting the detector using the DepositionCosmics module
  - DepositionGeant4 / DepositionCosmics have the option *record\_all\_tracks*. Enabling it make sure you get all primary particles
2. Record all parent *MCTrack* objects in the simulation or store histograms of their direction
3. Perform track reconstruction on the simulated events
4. Calculate the effective area

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### Effective Area Simulation with Allpix<sup>2</sup>

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2. Record all parent `MCTrack` objects in the simulation or store histograms of their direction
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```
[DepositionCosmics]
physics_list = FTFP_BERT_LIV
return_muons = true
return_neutrons = false
return_protons = false
return_electrons = false
return_pions = false
return_kaons = false
altitude = 0m
number_of_particles = 50
record_all_tracks = true
```

# Simulation

## Affective Area Measurement in Allpix<sup>2</sup>

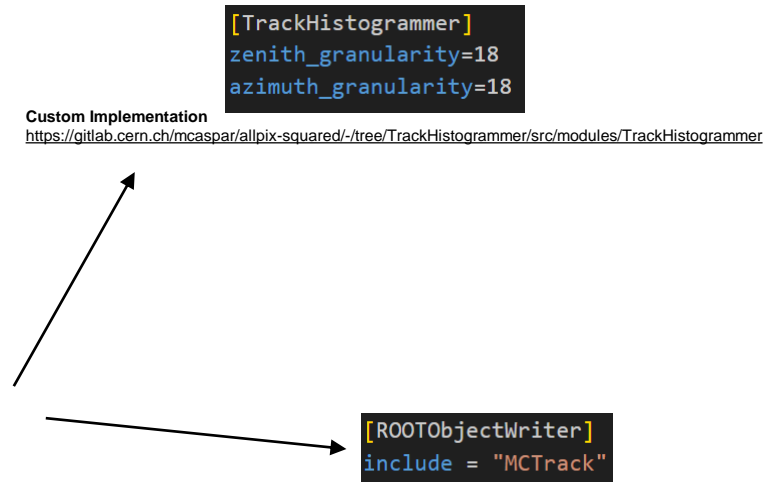
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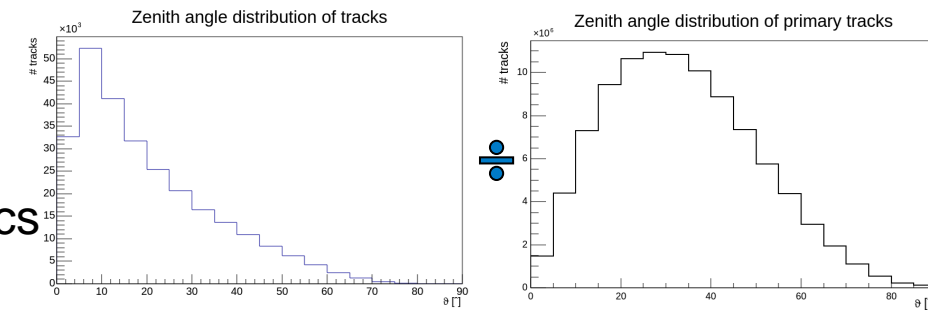
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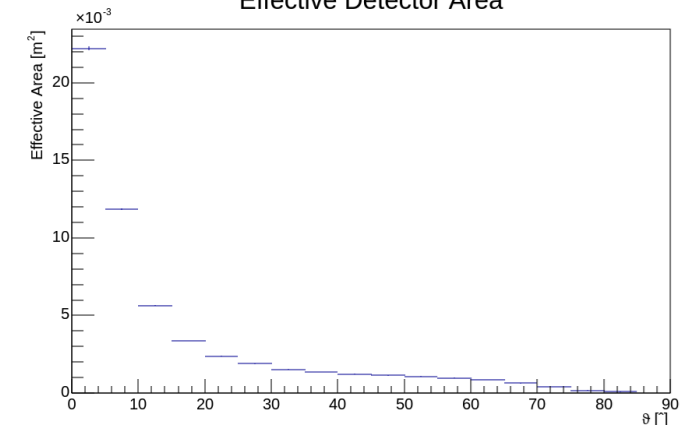
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Effective Detector Area



# Conclusion and Outlook

## What now?

### What we did

- Successfully tested & implemented:
  - Radial Strips geometry in Allpix<sup>2</sup>
  - Tracking for Radial Strips in Corryvreckan
  - Procedural generation of the endcap geometry
- Performed muon flux simulation for System Test studies

### What's left to do

- Test sensor alignment in Corryvreckan
- Study the tracking resolution of the System Test muon setup
- Test it all on real cosmics data 😊



# Thank you

## Contact

Deutsches Elektronen-  
Synchrotron DESY

[www.desy.de](http://www.desy.de)

Maximilian Felix Caspar  
ATLAS  
[maximilian.caspar@desy.de](mailto:maximilian.caspar@desy.de)

# Backup Slides

# ATLAS ITk Strips Modules

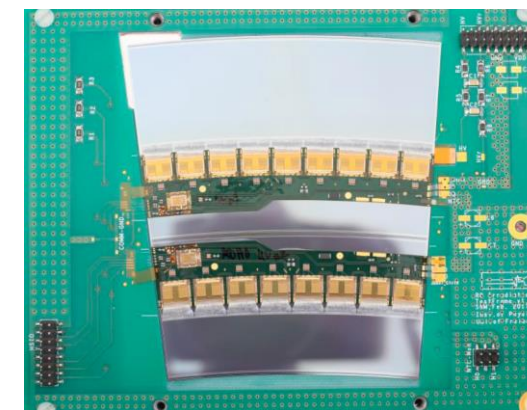
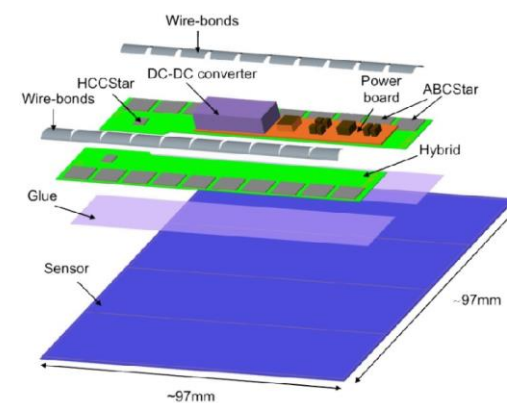
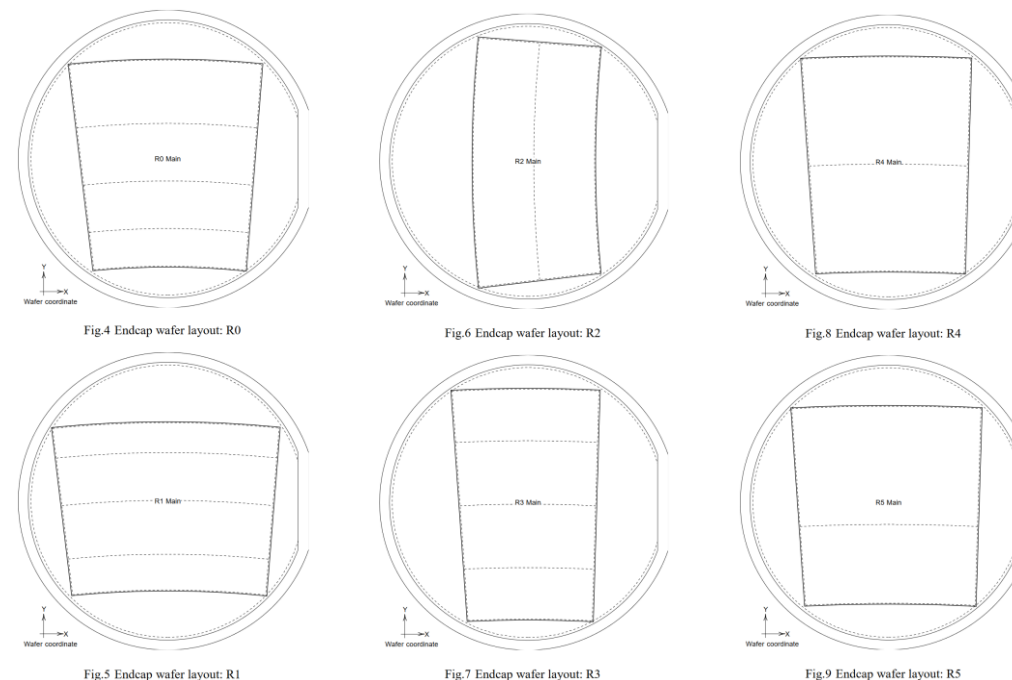
## The ITK Strips Endcap Modules

### Sensor

- 320  $\mu\text{m}$  p-bulk silicon, n-implant strips
- For Endcap: “Stereo Annulus”-shape

### Readout Electronics

- Front-end electronics located on a PCB (“Hybrid”) glued to the sensor
- Strips are wire bonded to the front-end chips
- Sensor is glued to a capton PCB (“Bustape”) that also carries an End-of-Substructure card with optical links



# Reconstruction in Corry

## Clustering in Radial Coordinates

### Radial Coordinates (on Sensor)

- Each row of strips is associated with an angular and radial pitch
- Resolutions in R /  $\varphi$  are calculated by assuming uniform distribution
- Radius and angle of the cluster centre are calculated using inverse-variance weighted averaging

### Cluster Centre

#### Radial Coordinate

#### Angular Coordinate

$$\omega_{R,i} = \frac{12}{\text{Pitch}_{R,i}^2}$$

Weight

$$\omega_{\varphi,i} = \frac{12}{\text{Pitch}_{\varphi,i}^2}$$

$$R = \frac{\sum_{i=1}^N \omega_{R,i} \cdot R_i}{\sum_{i=1}^N \omega_{R,i}}$$

Centre

$$\varphi = \frac{\sum_{i=1}^N \omega_{\varphi,i} \cdot \varphi_i}{\sum_{i=1}^N \omega_{\varphi,i}}$$

$$\sigma_R^2 = 1 / \sum_{i=1}^N \omega_{R,i}$$

Resolution

$$\sigma_{\varphi}^2 = 1 / \sum_{i=1}^N \omega_{\varphi,i}$$

Implemented in

[https://gitlab.cern.ch/mcaspar/corryvreckan/-/blob/polar\\_detectors/src/modules/ClusteringSpatial/ClusteringSpatial.cpp](https://gitlab.cern.ch/mcaspar/corryvreckan/-/blob/polar_detectors/src/modules/ClusteringSpatial/ClusteringSpatial.cpp)

# Reconstruction in Corry

## Cluster Centre in Cartesian Coordinates

### Cartesian Coordinates

- Cluster centres are translated into cartesian coordinates for tracking in Corryvreckan
- Resolutions in local cartesian coordinates are found using gaussian error propagation
- Global resolution matrix is calculated by rotating the error ellipsis

$$\alpha = \cos^{-1} \frac{L_F}{2 \cdot R_C}$$

Distance of focal point to the centre

Radius of the centre

$$\gamma = \sin^{-1} \left( \frac{L_F}{R} \cdot \sin(\alpha + \varphi + \varphi_{\text{Stereo}}) \right)$$

Angular component of cluster centre

Radial component of cluster centre

Detector's intrinsic stereo angle

$$\varphi^* = 2 \cdot \alpha + \gamma + \varphi + \varphi_{\text{Stereo}} - \pi$$

$$\begin{pmatrix} X \\ Y \end{pmatrix} = R \cdot \begin{pmatrix} \sin \varphi^* \\ \cos \varphi^* \end{pmatrix} \quad \text{Cartesian Position in local coordinates}$$

Implemented in

[https://gitlab.cern.ch/rprivara/corryvreckan/-/blob/polar\\_detectors/src/core/detector/PolarDetector.cpp](https://gitlab.cern.ch/rprivara/corryvreckan/-/blob/polar_detectors/src/core/detector/PolarDetector.cpp)



# Reconstruction in Corry

## Cluster Centre in Cartesian Coordinates

$$\begin{pmatrix} X \\ Y \end{pmatrix} = R \cdot \begin{pmatrix} \sin \varphi^* \\ \cos \varphi^* \end{pmatrix} \quad \text{Cartesian Position in local coordinates}$$

### Cartesian Coordinates

- Cluster centres are translated into cartesian coordinates for tracking in Corryvreckan
- Resolutions in local cartesian coordinates are found using gaussian error propagation
- Global resolution matrix is calculated by rotating the error ellipsis

#### Gaussian Error Propagation

$$\sigma_X^2 = \sigma_R^2 \cdot \left. \frac{\partial X}{\partial R} \right|_{(R,\varphi)}^2 + \sigma_\varphi^2 \cdot \left. \frac{\partial X}{\partial \varphi} \right|_{(R,\varphi)}^2$$

$$\sigma_Y^2 = \sigma_R^2 \cdot \left. \frac{\partial Y}{\partial R} \right|_{(R,\varphi)}^2 + \sigma_\varphi^2 \cdot \left. \frac{\partial Y}{\partial \varphi} \right|_{(R,\varphi)}^2$$

Implemented in

[https://gitlab.cern.ch/rprivara/corryvreckan/-/blob/polar\\_detectors/src/core/detector/PolarDetector.cpp](https://gitlab.cern.ch/rprivara/corryvreckan/-/blob/polar_detectors/src/core/detector/PolarDetector.cpp)