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# Oblique S and T parameters at one-loop and heavy resonances

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#### Work in progress

PRD 102 (2020) 035012 [arXiv: 2004.02827] JHEP 05 (2019) 092 [arXiv: 1810.10544] JHEP 04 (2017) 012 [arXiv: 1609.06659] PRD 93 (2016) 055041 [arXiv: 1510.03114] JHEP 01 (2014) 157 [arXiv: 1310.3121] PRL 110 (2013) 181801 [arXiv: 1212.6769] JHEP 08 (2012) 106 [arXiv: 1206.3454]

## OUTLINE

- 1) Motivation
- 2) The effective resonance Lagrangian
- 3) Oblique Electroweak Observables: S and T at NLO
- 4) Phenomenology
- 5) Conclusions

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- 1) **Motivation**
- 2) The effective resonance Lagrangian
- 3)
- 4)
- 5)



#### 1. Motivation

- The Standard Model (SM) provides an extremely successful description of the electroweak and strong interactions.
- A key feature is the particular mechanism adopted to break the electroweak gauge symmetry to the electroweak subgroup, SU(2)<sub>L</sub> x U(1)<sub>Y</sub> → U(1)<sub>QED</sub>, so that the W and Z bosons become massive. The LHC discovered a new particle around 125 GeV\*.



 Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore, we can use EFTs because it seems there is a large mass gap.



Effective Field Theories

<sup>\*</sup> CMS and ATLAS Collaborations.

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Effective Field Theories

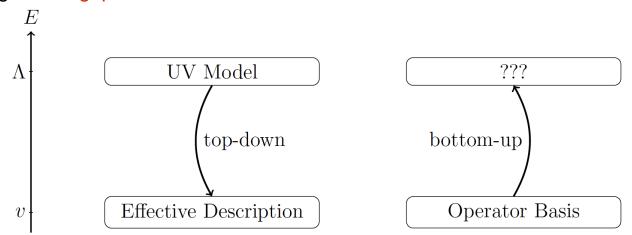


Diagram by C. Krause [PhD thesis, 2016]

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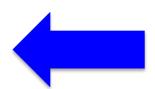
- Depending on the nature of the EWSB we have two possibilities for these EFTs (or something in between):
  - The decoupling (linear) EFT: SMEFT
    - SM-Higgs (forming a doublet with the EW Goldstones, as in the SM)
    - Weakly coupled
    - LO: SM
    - Expansion in canonical dimensions
  - The more general non-decoupling (non-linear) EFT: EWET, HEFT, EWChL
    - Non-SM Higgs (being a scalar singlet)
    - Strongly coupled
    - LO: Higgsless SM + scalar h + 3 GB (chiral Lagrangian)
    - Expansion in loops or chiral dimensions
    - Some composite Higgs models can be described within the EWET.

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See also

Domènec's talk

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#### What do we want to do?

S and T at NLO



Inclusion of BSM resonances in the effective Lagrangian in order to calculate S and T at NLO in terms of resonance parameters.

Short-distance constraints



Short-distance contraints are fundamental because we understand the resonance Lagrangian as an interpolation between low- and high energies and in order to reduce the number of resonance parameters.

Phenomenology



Following a typical bottom-up approach, what values for resonance masses are compatible with phenomenology?

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## Similarities to Chiral Symmetry Breaking in QCD

- i) Custodial symmetry: The Lagrangian is approximately invariant under global  $SU(2)_L \times SU(2)_R$  transformations. Electroweak Symmetry Breaking (EWSB) turns to be  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{L+R}$ .
- ii) Similar to the Chiral Symmetry Breaking (ChSB) occurring in QCD, *i.e.*, similar to the "pion" Lagrangian of Chiral Perturbation Theory (ChPT)\* $^{\wedge}$ , by replacing  $f_{\pi}$  by v=1/ $\sqrt{(2G_F)}$ =246 GeV. Rescaling naïvely we expect resonances at the TeV scale.

<sup>\*</sup> Weinberg '79

<sup>\*</sup> Gasser and Leutwyler '84 '85

<sup>\*</sup> Bijnens et al. <u>'99</u> <u>'00</u>

<sup>\*\*</sup> Ecker et al. '89

<sup>\*\*</sup> Cirigliano et al. '06

<sup>^</sup>Dobado, Espriu and Herrero '91

<sup>^</sup>Espriu and Herrero '92

<sup>^</sup>Herrero and Ruiz-Morales '94

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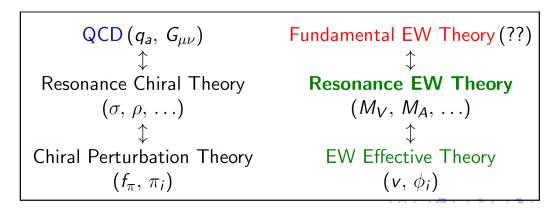


Diagram by J. Santos [VIII CPAN days, 2016]

#### 2. The effective resonance Lagrangian

- Custodial symmetry
- Degrees of freedom: bosons x (EW goldstones, gauge bosons, h) + BSM resonances (V,A). The inclusion of fermions  $\psi$  is the next step in the project.
- Chiral power counting\*

$$\frac{\chi}{v} \sim \mathcal{O}\left(p^0\right) \qquad \partial_{\mu}, \, m \sim \mathcal{O}(p) \qquad \mathcal{T} \sim \mathcal{O}(p) \qquad g, \, g' \sim \mathcal{O}(p)$$

Inclusion of odd-parity operators, not considered in Pich, IR, Santos and Sanz-Cillero '13'14.

\* Appelguist and Bernand '80

\* Hirn and Stern '05 \* Longhitano '80 '81

\* Alonso et al. '12 \* Delgado et al. '14

\* Manohar, and Georgi '84

\* Buchalla, Catá and Krause '13 \* Pich, IR, Santos and Sanz-Cillero '16 '17 Brivio et al. '13

\* Gasser and Leutwyler '84 '85

\* Krause, Pich, IR, Santos and Sanz-Cillero '19

Diagram by J.J. Sanz-Cillero [HEP 2017]

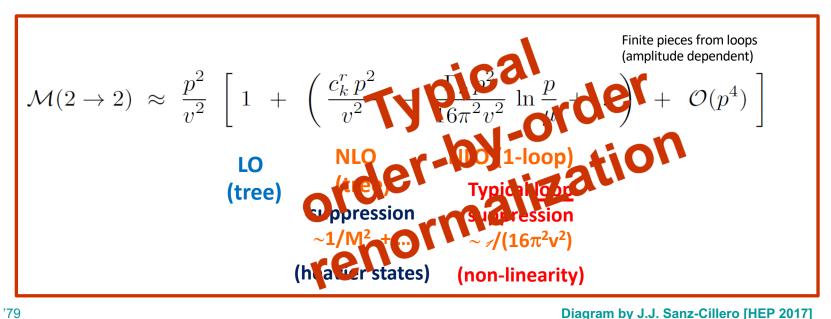
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✓ The Lagrangian reads:

$$\begin{split} \Delta\mathcal{L}_{\mathrm{RT}} &= \quad \frac{v^2}{4} \left( 1 + \frac{2\kappa_{W}}{v} h \right) \langle u_{\mu} u^{\mu} \rangle_{2} \\ &+ \langle V_{3\,\mu\nu}^{1} \left( \frac{F_{V}}{2\sqrt{2}} f_{+}^{\mu\nu} + \frac{iG_{V}}{2\sqrt{2}} [u^{\mu}, u^{\nu}] + \frac{\widetilde{F}_{V}}{2\sqrt{2}} f_{-}^{\mu\nu} + \frac{\widetilde{\lambda}_{1}^{hV}}{\sqrt{2}} \left[ (\partial^{\mu}h) u^{\nu} - (\partial^{\nu}h) u^{\mu} \right] \right) \rangle_{2} \\ &+ \langle A_{3\,\mu\nu}^{1} \left( \frac{F_{A}}{2\sqrt{2}} f_{-}^{\mu\nu} + \frac{\lambda_{1}^{hA}}{\sqrt{2}} \left[ (\partial^{\mu}h) u^{\nu} - (\partial^{\nu}h) u^{\mu} \right] + \frac{\widetilde{F}_{A}}{2\sqrt{2}} f_{+}^{\mu\nu} + \frac{i\widetilde{G}_{A}}{2\sqrt{2}} [u^{\mu}, u^{\nu}] \right) \rangle_{2} \,. \end{split}$$

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- Including resonance masses, we have 10 resonance parameters. This number can be reduced by using short-distance information, but in contrast to the QCD case, we ignore the underlying dynamical theory (BSM).
  - ✓ Vanishing form factors at high energies allow us to determine  $\left(G_V, \widetilde{G}_A, \lambda_1^{hA}, \widetilde{\lambda}_1^{hV}\right)$  in terms of the remaining parameters:

$$\frac{G_V}{F_A} = -\frac{\widetilde{G}_A}{\widetilde{F}_V} = \frac{\lambda_1^{hA}v}{\kappa_W F_V} = -\frac{\widetilde{\lambda}_1^{hV}v}{\kappa_W \widetilde{F}_A} = \frac{v^2}{F_V F_A - \widetilde{F}_V \widetilde{F}_A}$$

- ✓ Weinberg sum rules (WSRs) at LO and at NLO.
  - ✓ 1st WSR. Vanishing of the 1/s term of  $\Pi_{VV}(s) \Pi_{AA}(s)$ :  $\left(F_V^2 \widetilde{F}_V^2\right) \left(F_A^2 \widetilde{F}_A^2\right) = v^2$
  - $\checkmark$  2nd WSR. Vanishing of the 1/s² term of  $\Pi_{\text{VV}}(\mathbf{s}) \Pi_{\text{AA}}(\mathbf{s})$ :  $\left(F_V^2 \widetilde{F}_V^2\right) M_V^2 \left(F_A^2 \widetilde{F}_A^2\right) M_A^2 = 0$

#### 3. Oblique Electroweak Observables: S and T at NLO

✓ Universal oblique corrections via the EW boson self-energies (transverse in the Landau gauge)

$$\mathcal{L}_{\text{v.p.}} \doteq -\frac{1}{2} W_{\mu}^{3} \Pi_{33}^{\mu\nu}(q^{2}) W_{\nu}^{3} - \frac{1}{2} B_{\mu} \Pi_{00}^{\mu\nu}(q^{2}) B_{\nu} - W_{\mu}^{3} \Pi_{30}^{\mu\nu}(q^{2}) B_{\nu} - W_{\mu}^{+} \Pi_{WW}^{\mu\nu}(q^{2}) W_{\nu}^{-}$$

✓ S parameter\*: new physics in the difference between the Z self-energies at  $Q^2=M_Z^2$  and  $Q^2=0$ .

$$e_3 = \frac{g}{g'} \widetilde{\Pi}_{30}(0), \qquad \Pi_{30}(q^2) = q^2 \widetilde{\Pi}_{30}(q^2) + \frac{g^2 \tan \theta_W}{4} v^2, \qquad S = \frac{16\pi}{g^2} (e_3 - e_3^{SM}).$$

✓ T parameter\*: custodial symmetry breaking

$$e_1 = \frac{\Pi_{33}(0) - \Pi_{WW}(0)}{M_W^2} \stackrel{**}{=} \frac{Z^{(+)}}{Z^{(-)}} - 1$$
  $T = \frac{4\pi}{g'^2 \cos^2 \theta_W} \left( e_1 - e_1^{\text{SM}} \right)$ 

✓ We follow the useful dispersive representation introduced by Peskin and Takeuchi\* for S and a dispersion relation for T (checked for the lowest cuts):

$$S = \frac{16\pi}{g^2 \tan \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t} \left( \rho_S(t) - \rho_S(t)^{\mathrm{SM}} \right)$$
$$T = \frac{16\pi}{g'^2 \cos^2 \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t^2} \left( \rho_T(t) - \rho_T(t)^{\mathrm{SM}} \right)$$

- ρ<sub>S</sub>(t) and ρ<sub>T</sub>(t) are the spectral functions of the W³B and of the difference of the neutral and charged Goldstone boson self-energies, respectively.
- ✓ They need to be well-behaved at short-distances to get the convergence of the integral.
- ✓ S and T parameters are defined for a reference value for the SM Higgs mass.

- Ve consider only the lightest two-particle absorptive cuts  $(\phi\phi,\,h\phi)$  and in general we take as working assumptions  $M_A > M_V$  and  $\widetilde{F}_{V,A}^2 < F_{V,A}^2$ .
- ✓ LO result (T<sub>LO</sub>=0):
  - $\checkmark$  With 1st and 2nd WSR:  $S_{\text{LO}} = \frac{4\pi v^2}{M_V^2} \left(1 + \frac{M_V^2}{M_A^2}\right) \rightarrow \frac{4\pi v^2}{M_V^2} < S_{\text{LO}} < \frac{8\pi v^2}{M_V^2}$
  - $\checkmark$  Assuming only the 1st WSR:  $S_{
    m LO} > {4\pi v^2\over M_V^2}$
- ✓ NLO result including 1st and 2nd WSR:

$$\begin{split} S_{\text{NLO}} &= 4\pi v^2 \bigg( \frac{1}{M_V^{r^2}} + \frac{1}{M_A^{r^2}} \bigg) + \Delta S_{\text{NLO}}^{\text{P-even}} + \Delta S_{\text{NLO}}^{\text{P-odd}} \\ \Delta S_{\text{NLO}}^{\text{P-even}} &= \frac{1}{12\pi} \left[ (1 - \kappa_W^2) \left( \log \frac{M_V^2}{m_h^2} - \frac{11}{6} \right) + \kappa_W^2 \left( \frac{M_A^2}{M_V^2} - 1 \right) \log \frac{M_A^2}{M_V^2} \right] \\ \Delta S_{\text{NLO}}^{\text{P-odd}} &= \frac{1}{12\pi} \left( \frac{\tilde{F}_V^2}{F_V^2} + 2\kappa_W^2 \frac{\tilde{F}_V \tilde{F}_A}{F_V F_A} - \kappa_W^2 \frac{\tilde{F}_A^2}{F_A^2} \right) \left( \frac{M_A^2}{M_V^2} - 1 \right) \log \frac{M_A^2}{M_V^2} + \Omega \left( \frac{\tilde{N}_V^2}{V_{V,A}} \right) \\ T_{\text{NLO}} &= \Delta T_{\text{NLO}}^{\text{P-even}} + \Delta T_{\text{NLO}}^{\text{P-odd}} \\ \Delta T_{\text{NLO}}^{\text{P-even}} &= \frac{3}{16\pi \cos^2 \theta_W} \left[ (1 - \kappa_W^2) \left( 1 - \log \frac{M_V}{m_h^2} \right) + \kappa_W^2 \log \frac{M_A^2}{M_V^2} \right] \\ \Delta T_{\text{NLO}}^{\text{P-odd}} &= \frac{3}{16\pi \cos^2 \theta_W} \left[ 2\kappa_W^2 \frac{\tilde{F}_A}{I_A} - \frac{2\tilde{F}_V}{F_V} + \frac{M_V^2}{M_A^2 - M_V^2} \log \frac{M_A^2}{M_V^2} \left( 2\frac{\tilde{F}_V}{F_V} - 2\kappa_W^2 \frac{M_A^2}{M_V^2} \frac{\tilde{F}_A}{F_A} \right) \\ &+ \frac{M_V^2}{M_A^2 - M_V^2} \log \frac{M_A^2}{M_V^2} \left[ \left( \kappa_W^2 \frac{\tilde{F}_A^2}{F_A^2} - \frac{\tilde{F}_V^2}{F_V^2} \right) \left( 1 + \frac{M_A^2}{M_V^2} \right) + 2\frac{\tilde{F}_V \tilde{F}_A}{F_V F_A} \left( \kappa_W^2 \frac{M_A^2}{M_V^2} - 1 \right) \right] \\ &+ 2 \left( \frac{\tilde{F}_V^2}{F_V^2} - \kappa_W^2 \frac{\tilde{F}_A^2}{F_A^2} + \left( 1 - \kappa_W^2 \right) \frac{\tilde{F}_V \tilde{F}_A}{F_V F_A} \right) + \mathcal{O} \left( \frac{\tilde{F}_V^3}{F_V^3} \right) \end{split}$$

 $\Delta S_{
m NLO}^{
m P-even}$  and  $\Delta T_{
m NLO}^{
m P-even}$  correspond to Pich, IR and Sanz-Cillero '13 '14

Expansion in  $rac{\widetilde{F}_{V,A}}{F_{V,A}}$  .

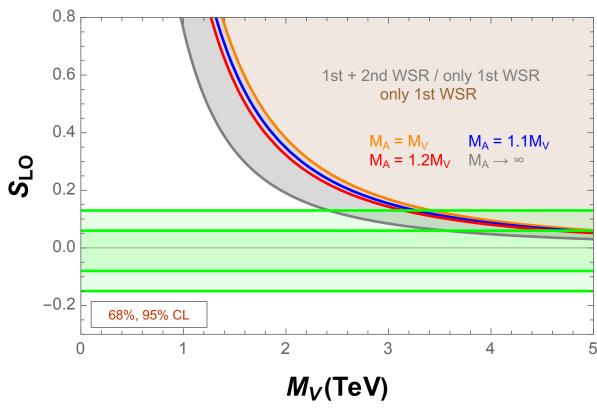
## 4. Phenomenology

✓ Oblique electroweak observables\*\* (S and T).

$$S = -0.01 \pm 0.07 *$$
  
 $T = 0.04 \pm 0.06 *$ 

- Short-distance constraints.
- Assumptions: lightest two-particle absorptive cuts,  $M_A > M_V$  and  $\widetilde{F}_{V,A}^2 < F_{V,A}^2$ .

#### i) LO results



<sup>\*</sup> PDG '22

<sup>\*\*</sup> Peskin and Takeuchi '92

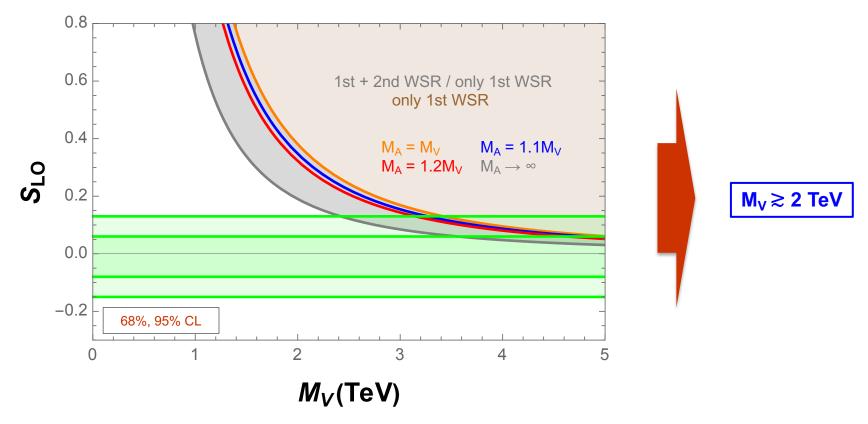
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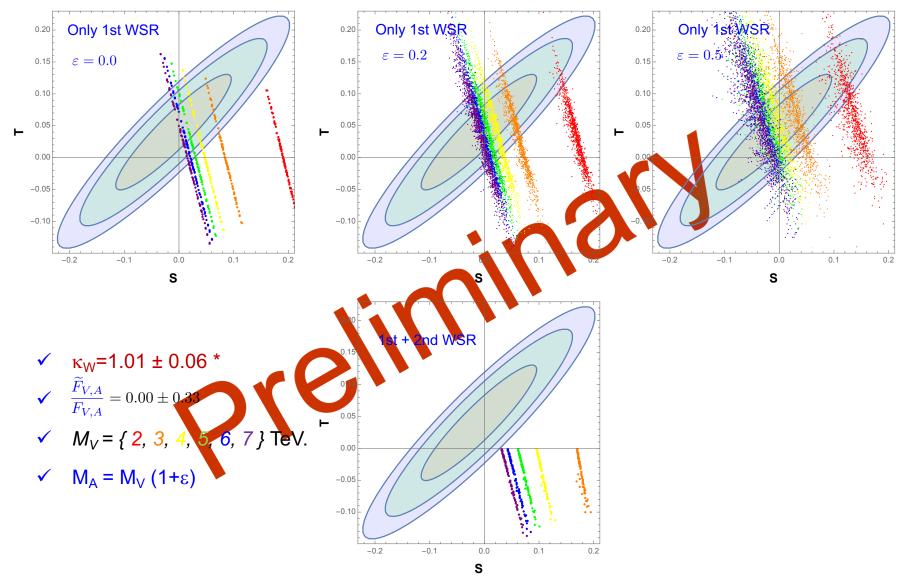
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## ii) NLO results

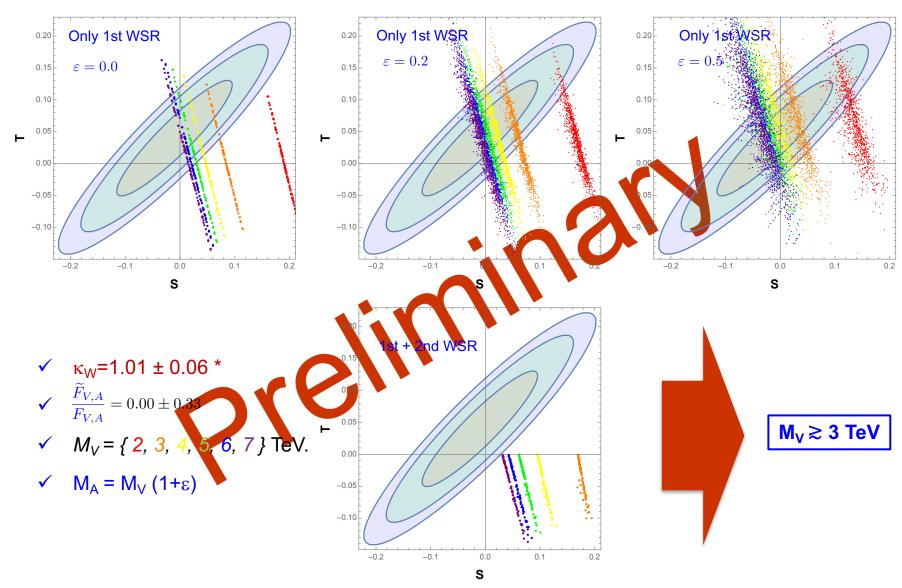
Results in terms of only  ${
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#### ii) NLO results

Results in terms of only  ${\sf M_V}$ ,  ${\sf M_A}$  (only 1st WSR),  ${\sf \kappa_W}$  and  $\frac{\tilde{F}_{V,A}}{F_{V,A}}$ 



<sup>\*</sup> de Blas, Eberhardt and Krause '18

#### 4. Conclusions

- ✓ Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore we can use EFTs because we have a mass gap.
- ✓ As a consequence of the mass gap, bottom-up EFTs are appropriate to search for BSM. Depending on the nature of the EWSB we have two possibilities:
  - ✓ Decoupling (linear) EFT: SMEFT
    - ✓ SM-Higgs and weakly coupled
    - ✓ Expansion in canonical dimensions
  - ✓ Non-decoupling (non-linear) EFT: EWET (HEFT or EWChL)
    - ✓ Non-SM Higgs and strongly coupled
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- ✓ Phenomenology: S and T at NLO
  - ✓ Short-distance constraints: WSRs and well-behaved form factors at high energies.
  - ✓ Assumptions: lightest two-particle absorptive cuts,  $M_A \gtrsim M_V$  and  $\widetilde{F}_{V,A}^2 < F_{V,A}^2$ .
  - $\checkmark$  Results in terms of only  $M_V$ ,  $M_A$ ,  $\kappa_W$  and  $\frac{\widetilde{F}_{V,A}}{F_{V,A}}$ .

Room for these BSM scenarios and  $M_V \gtrsim 3$  TeV.