

Leptogenesis Triggered by a First-Order Phase Transition

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Leptogenesis, Two Birds with One Stone

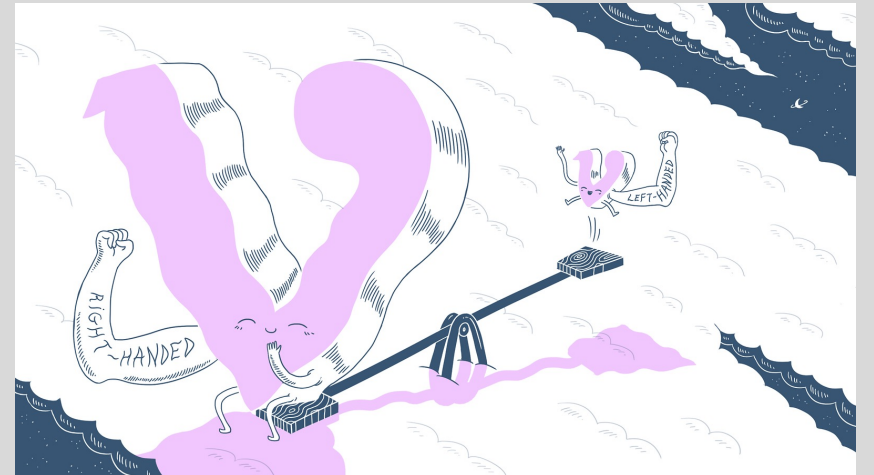
- Type-I seesaw introduce right-handed neutrinos (mass M)

$$\mathcal{L} \supset \sum_i \bar{\nu}_R^i i \gamma^\mu \partial_\mu \nu_R^i - \frac{1}{2} \sum_{i,j} \left(M^{ij} \bar{\nu}_R^{i,c} \nu_R^j + \text{h.c.} \right) \\ - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L^i \tilde{H} \nu_R^j + \text{h.c.} \right)$$

$$\mathcal{M} = \begin{pmatrix} 0 & \frac{\lambda_D v}{\sqrt{2}} \\ \frac{\lambda_D v}{\sqrt{2}} & M \end{pmatrix}$$

$$m_\nu \simeq \frac{|\lambda_D|^2 v_{EW}^2}{2M} \\ \simeq 0.08 \text{ eV} \left(\frac{\lambda_D}{0.5} \right)^2 \left(\frac{10^{14} \text{ GeV}}{M} \right)$$

Minkowski, 1977



Leptogenesis

$$\mathcal{L} \supset \sum_i \bar{\nu}_R^i i \gamma^\mu \partial_\mu \nu_R^i - \frac{1}{2} \sum_{i,j} \left(M^{ij} \bar{\nu}_R^{i,c} \nu_R^j + \text{h.c.} \right) \quad \cancel{\text{L}} \\ - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L^i \tilde{H} \nu_R^j + \text{h.c.} \right) \quad \cancel{\text{CP}}$$

~~Thermal Equilibrium~~

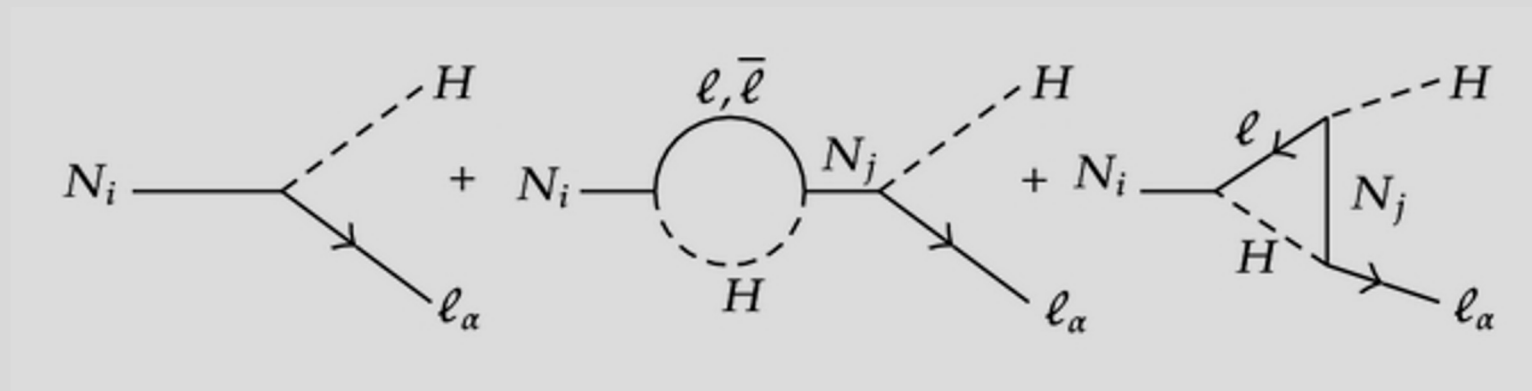
RHN decays

All three Sakharov conditions are satisfied

M. Fukugita, T. Yanagida, 1986
Luty 1992

Leptogenesis

Generate the Baryon asymmetry through the lepton asymmetry



$$\mathcal{L} \supset - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L^i \tilde{H} \nu_R^j + \text{h.c.} \right)$$

1. The Right Handed Neutrinos, decay (CP violating) asymmetrically

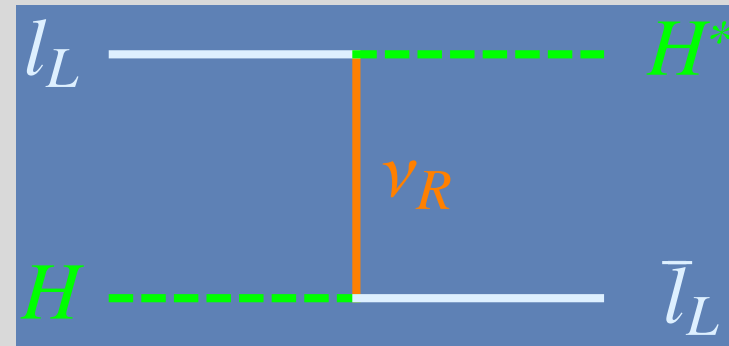
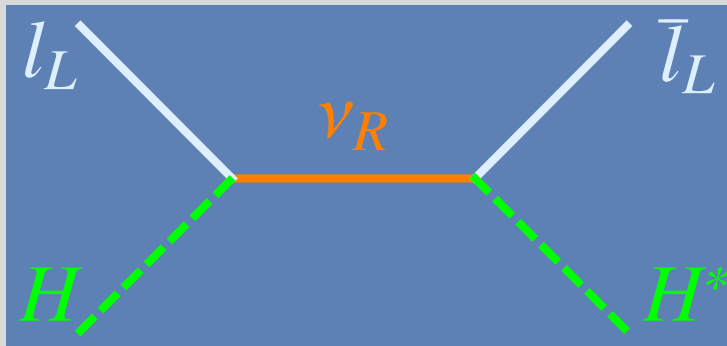
$$\epsilon_i = \frac{\sum_j \Gamma(\nu_R^i \rightarrow \ell_L^j H) - \Gamma(\nu_R^i \rightarrow \bar{\ell}_L^j H^*)}{\sum_j \Gamma(\nu_R^i \rightarrow \ell_L^j H) + \Gamma(\nu_R^i \rightarrow \bar{\ell}_L^j H^*)} \propto \text{Im} \left[\left(\lambda_D \lambda_D^\dagger \right)^2 \right]$$

M. Fukugita, T. Yanagida, 1986
Luty 1992

2. Part of the generated asymmetry will be converted to a baryon asymmetry (about order one, detailed calculation gives 28/79)

Difficulties in Leptogenesis

3. Inverse decays and scattering wash out the generated asymmetry



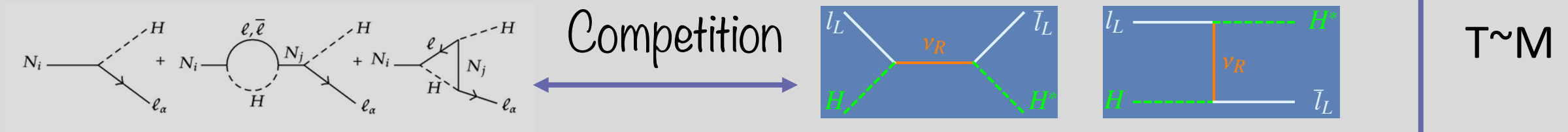
Only 1% of the generated asymmetry will survive

How to fix this? – This talk

Difficulties in Leptogenesis

- Naively, the strong washout effect is unavoidable

See for example, Flanz et al, 1996, Pilaftsis, 1997, Dev et al, 2017 ...

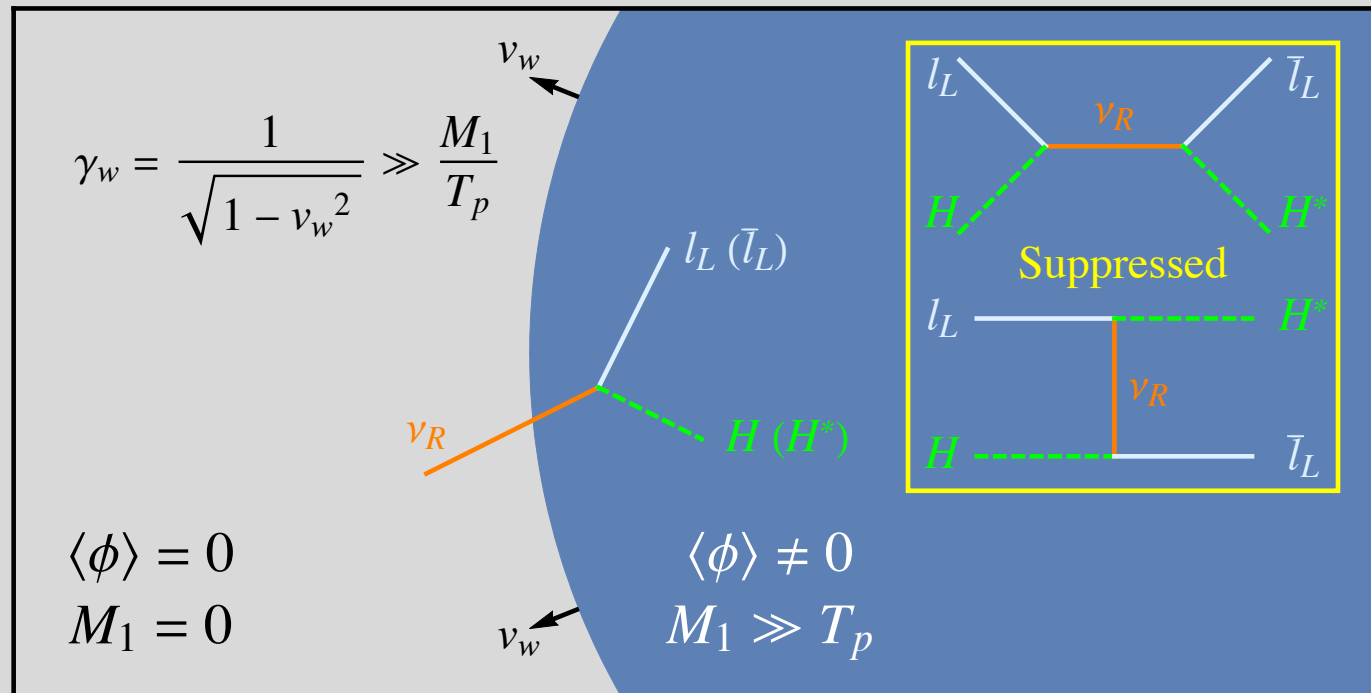


- The RHN decouples from the thermal bath at $T \sim M$
- Only if the cosmic temperature changes discontinuously, the RHN decays, generates the lepton asymmetry. Then the temperature falls $T \ll M$, the washout effects are Boltzmann suppressed

Avoiding the Washout Effects With a Mass Jump

- The cosmic temperature can not change discontinuously, but the mass of the RHNs can -- first-order PT!

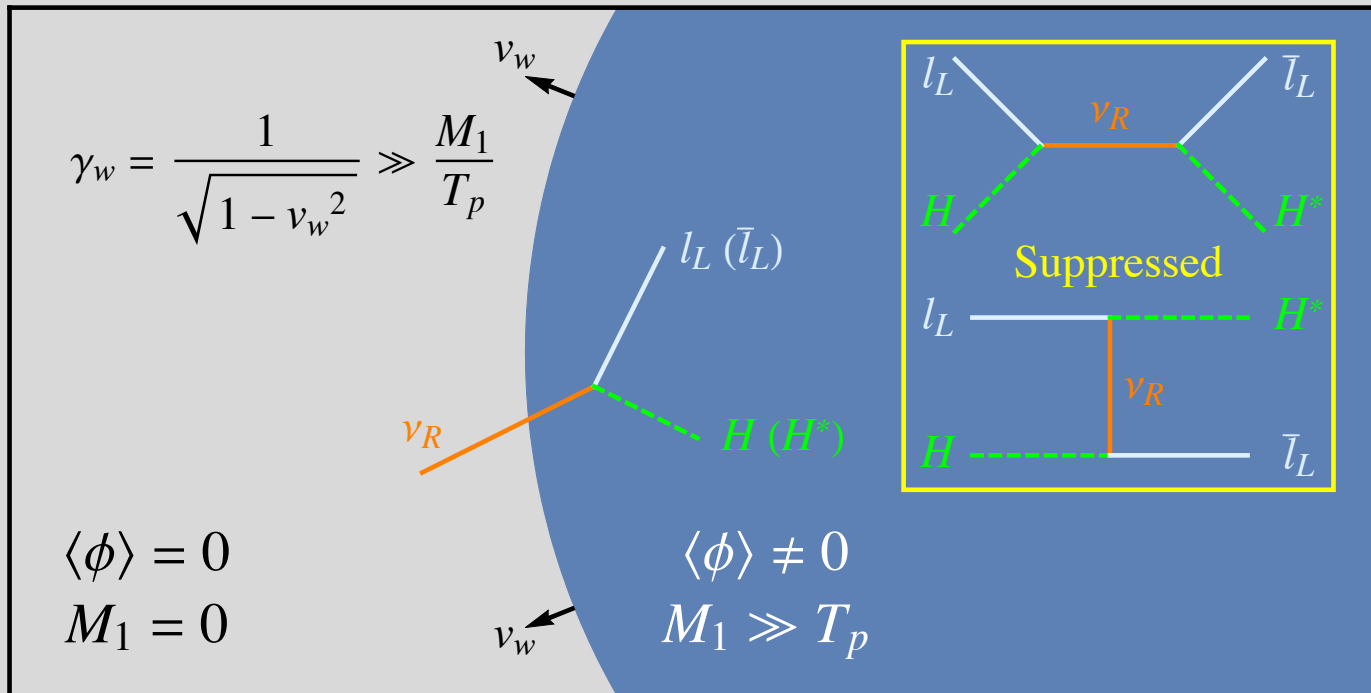
$$\mathcal{L} \supset - \sum_{i,j} \frac{1}{2} \left(\lambda_R^{ij} \bar{\nu}_R^{i,c} \nu_R^j \frac{\phi}{\sqrt{2}} + \text{h.c.} \right),$$



- The RHNs are massless in the old vacuum
- During the PT, the RHN gains mass M_1
- If $M_1 \gg T_p$, the washout effects are Boltzmann suppressed

Wait – $M_1 \gg T_p$, How Can That Happen?

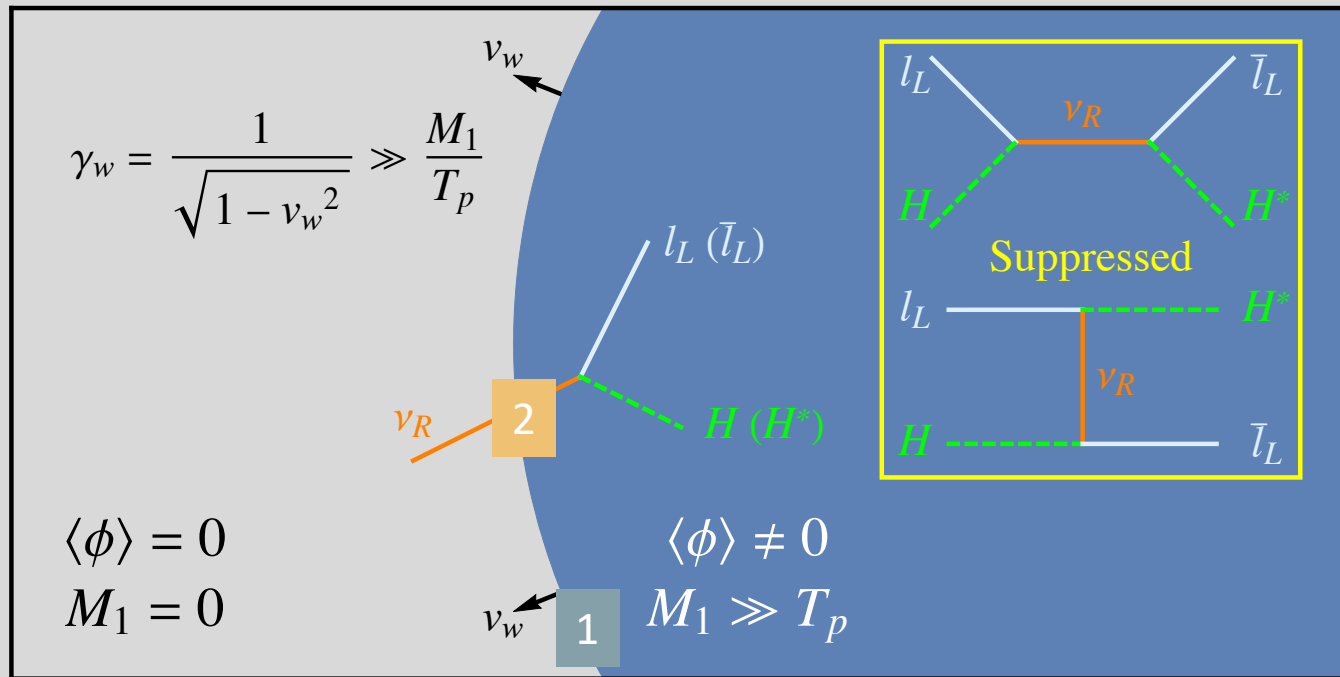
$M_1 \gg T_p$, how?



- If the phase transition is very strong, the bubble wall can be relativistic
- Although in the plasma frame, RHs are in thermal equilibrium, they have very high energy in the wall frame
- They can penetrate into the true vacuum, and decay immediately

Leptogenesis with a first-order PT

PH, K. P. Xie 2022



To suppress the wash-out

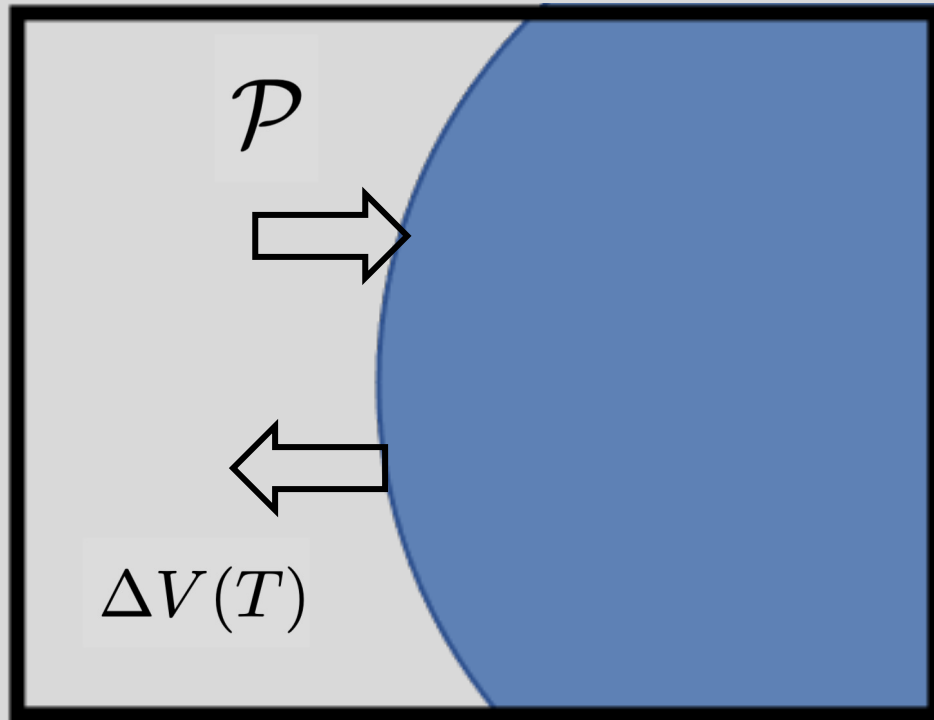
1. $M_1 \gg T_p$, easy

$$\mathcal{L} \supset - \sum_{i,j} \frac{1}{2} \left(\lambda_R^{ij} \bar{\nu}_R^{i,c} \nu_R^j \frac{\phi}{\sqrt{2}} + \text{h.c.} \right),$$

2. RHN can penetrate into the new vacuum -> relativistic walls

Model building task: write down the scalar potential for ϕ , that undergoes a strong first-order PT, and the bubble walls are relativistic.

Relativistic Walls



The wall velocity is determined by

At LO, $\Delta V(T) - \mathcal{P}$

$$\mathcal{P}_{1 \rightarrow 1} = \sum c_i \frac{\Delta m_i^2 T^2}{24}$$

Bodeker and Moore, 2009

All order resummation,

$$\mathcal{P}_{1 \rightarrow N} \sim \gamma_w$$

$$\mathcal{P}_{1 \rightarrow N} \sim \gamma_w^2$$

Gouttenoire, Jinno and Sala, 2021 Hoeche et al, 2021

Terminal wall velocity,

$$\gamma_{\text{eq}} = \sqrt{\frac{\Delta V_p - \mathcal{P}_{1 \rightarrow 1}}{\mathcal{P}_{1 \rightarrow N} / \gamma_w^2}}; \quad \gamma_{\text{eq}} = \frac{\Delta V_p - \mathcal{P}_{1 \rightarrow 1}}{\mathcal{P}_{1 \rightarrow N} / \gamma_w}$$

Relativistic Walls

- Relativistic walls can be achieved if

$$\Delta V(T) \gg \mathcal{P}_{1 \rightarrow 1} = \sum c_i \frac{\Delta m_i^2 T^2}{24}$$

- This can be easily done in a classical conformal theory,

$$\begin{aligned} \mathcal{L}_{B-L} = & \sum_i \bar{\nu}_R^i i \gamma^\mu D_\mu \nu_R^i - \frac{1}{2} \sum_{i,j} \left(\lambda_R^{ij} \bar{\nu}_R^{i,c} \Phi \nu_R^j + \text{h.c.} \right) - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L \tilde{H} \nu_R^j + \text{h.c.} \right) \\ & + D_\mu \Phi^\dagger D^\mu \Phi - V(\Phi) - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} \end{aligned}$$

Iso, Okada, and Orikasa, 2009

$$V_{tree}(\Phi) = \lambda_\phi |\Phi|^4 \quad \text{C-W potential,} \quad V(\phi) = V_0 + \frac{B}{4} \phi^4 \left(\ln \frac{\phi}{v_\phi} - \frac{1}{4} \right)$$

$$M_{Z'} = 2g_{B-L} v_\phi, \quad M_i = \lambda_{R,i} \frac{v_\phi}{\sqrt{2}}, \quad M_\phi = \sqrt{B} v_\phi$$

Relativistic Walls, CC B-L

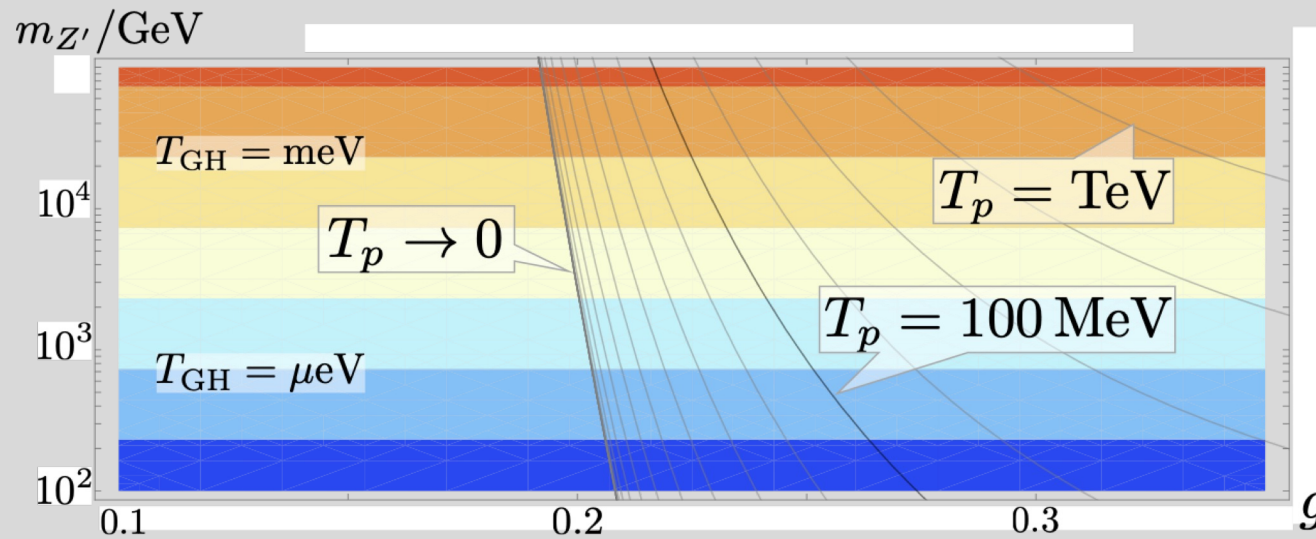


Figure 1: Contour plot of the percolation temperature T_p (black lines) as a function of g and $m_{Z'}$. The horizontal color bands show the temperature $T_{\text{GH}} \equiv \mathcal{H}/2\pi$.

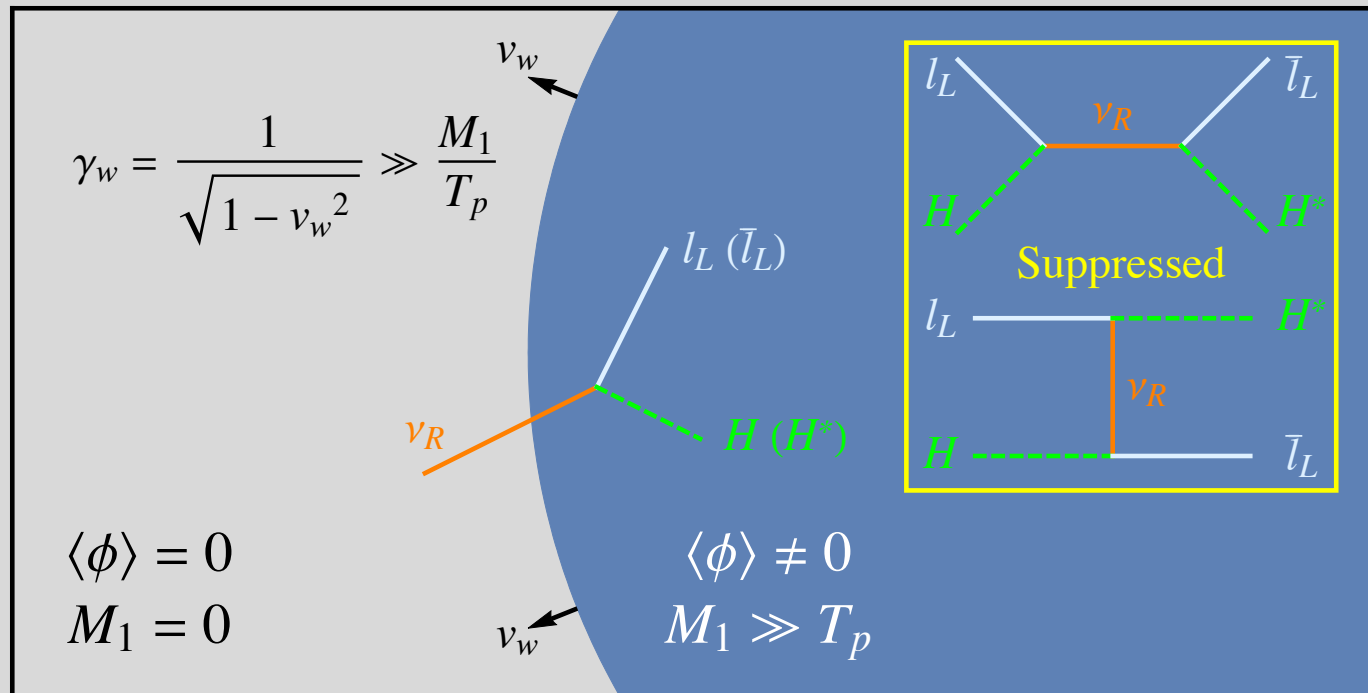
$$V(\phi) \sim \frac{g_{B-L}^2 T^2}{2} + \frac{3g_{B-L}^4 \phi^4}{4\pi^2} \left[\ln\left(\frac{\phi^2}{v_\phi}\right) - \frac{1}{2} \right]$$

Iso, Serpico, and Shimada, 2017

$$\Delta V(T) \gg \mathcal{P}_{1 \rightarrow 1} = \sum c_i \frac{\Delta m_i^2 T^2}{24}$$

Relativistic walls can be achieved

Towards an Actual Model



- RHN in thermal equilibrium
- ✓ ϕ undergoes a 1st order PT, with relativistic bubble walls.

After penetration...

- ? Completing processes?
- ? Additional washouts from the decay products?
- ? Strong reheating?

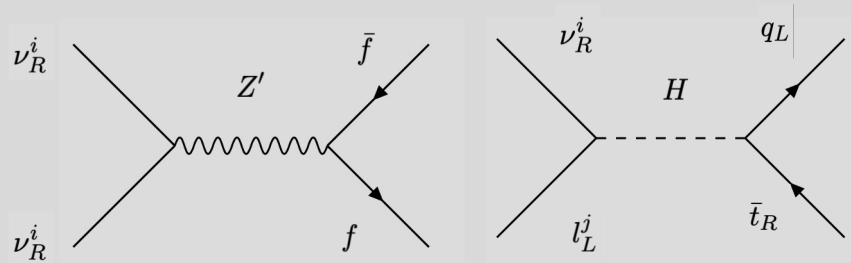
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Similar ideas in Baldes et al, 2021

Dasgupta, Dev, Ghoshal, Mazumdar 2022

After penetration

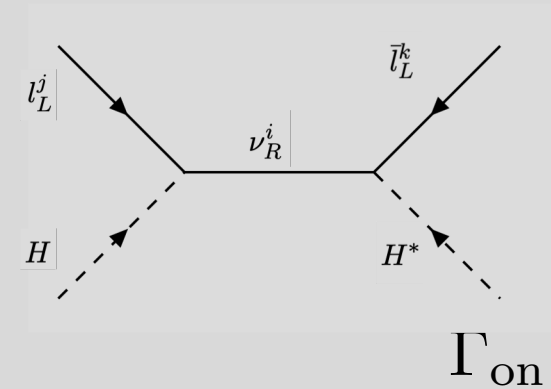
Competing processes



$$\Gamma_D > \Gamma_{\text{ann}}, \quad \Gamma_D > \Gamma_{\text{sca}}.$$

No additional washouts

$$E_1 = \gamma_1 M_1 = M_1^2 / T_p.$$



$$\Gamma_{\text{th}} > \Gamma_{\text{on}}, \quad \Gamma_{\text{th}} > H_p$$

Ensures thermalization is fast enough

Considerations

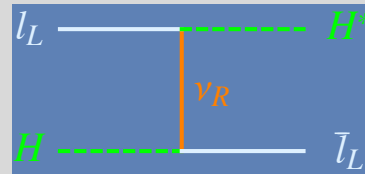
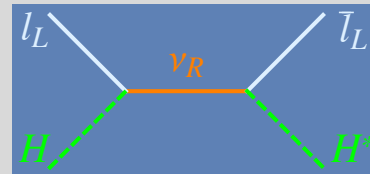
Strong reheating?

The latent heat released from the PT will reheat the universe to

$$T_{\text{rh}} = (1 + \alpha)^{1/4} T_p,$$

For the PT to provide ultra-relativistic bubble walls, typically $\alpha \gg 1$

With a high reheating temperature,



will become active

The generated asymmetry will be diluted by $\sim (T_p/T_{\text{rh}})^3$

Difficulties in the Minimal Model

- The minimal gauged $U(1)_{B-L}$ model

$$\mathcal{L}_{B-L} = \sum_i \bar{\nu}_R^i i \gamma^\mu D_\mu \nu_R^i - \frac{1}{2} \sum_{i,j} \left(\lambda_R^{ij} \bar{\nu}_R^{i,c} \Phi \nu_R^j + \text{h.c.} \right) - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L \tilde{H} \nu_R^j + \text{h.c.} \right) \\ + D_\mu \Phi^\dagger D^\mu \Phi - V(\Phi) - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu}$$

- The scalar potential $V(\phi) = V_0 + \frac{B}{4} \phi^4 \left(\ln \frac{\phi}{v_\phi} - \frac{1}{4} \right)$

- In the minimal gauged $U(1)_{B-L}$ $B = \frac{6}{\pi^2} \left(g_{B-L}^4 - \sum_i \frac{\lambda_{R,i}^4}{96} \right) = \frac{3}{8\pi^2 v_\phi^4} \left(M_{Z'}^4 - \sum_i \frac{2M_i^4}{3} \right)$

$$T_{\text{rh}} = \left(1 + \frac{B v_\phi^4 / 16}{\pi^2 g_* T_p^4 / 30} \right)^{1/4} \sim g_{B-L} v_\phi \sim M_{Z'} \gtrsim M_1$$

>0, for stability

Wash-out unavoidable!!

Extend the Minimal Model

- Wash-out unavoidable

$$T_{\text{rh}} = \left(1 + \frac{Bv_\phi^4/16}{\pi^2 g_* T_p^4/30} \right)^{1/4} \propto M_{Z'}$$

- Add a new scalar

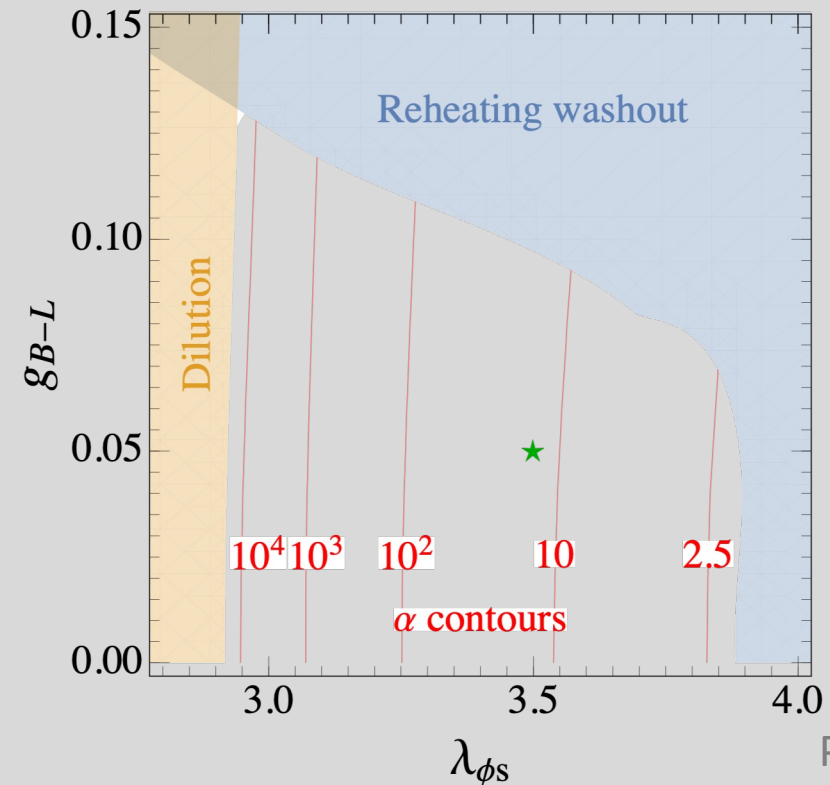
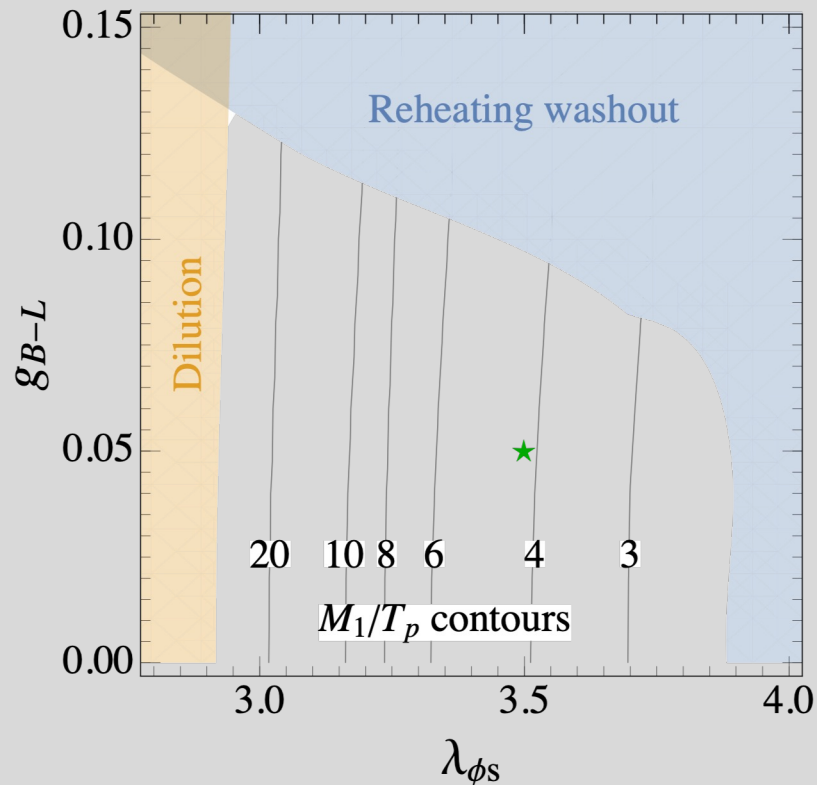
$$\begin{aligned} \mathcal{L}_{B-L} = & \sum_i \bar{\nu}_R^i i \not{D} \nu_R^i - \frac{1}{2} \sum_{i,j} \left(\lambda_R^{ij} \bar{\nu}_R^{i,c} \Phi \nu_R^j + \text{h.c.} \right) - \sum_{i,j} \left(\lambda_D^{ij} \bar{\ell}_L^i \tilde{H} \nu_R^j + \text{h.c.} \right) \\ & + D_\mu \Phi^\dagger D^\mu \Phi + D_\mu S^\dagger D^\mu S - V(\Phi, S) - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu}, \end{aligned}$$

$$V_{\text{tree}}(\Phi, S) = \lambda_\phi |\Phi|^4 + \lambda_s |S|^4 + \lambda_{\phi s} |\Phi|^2 |S|^2, \quad B = \frac{6}{\pi^2} \left(\frac{\lambda_{\phi s}^2}{96} + g_{B-L}^4 - \sum_i \frac{\lambda_{R,i}^4}{96} \right),$$

T_{rh} no longer correlated with $M_{Z'}$, wash-out avoidable

Parameter Space

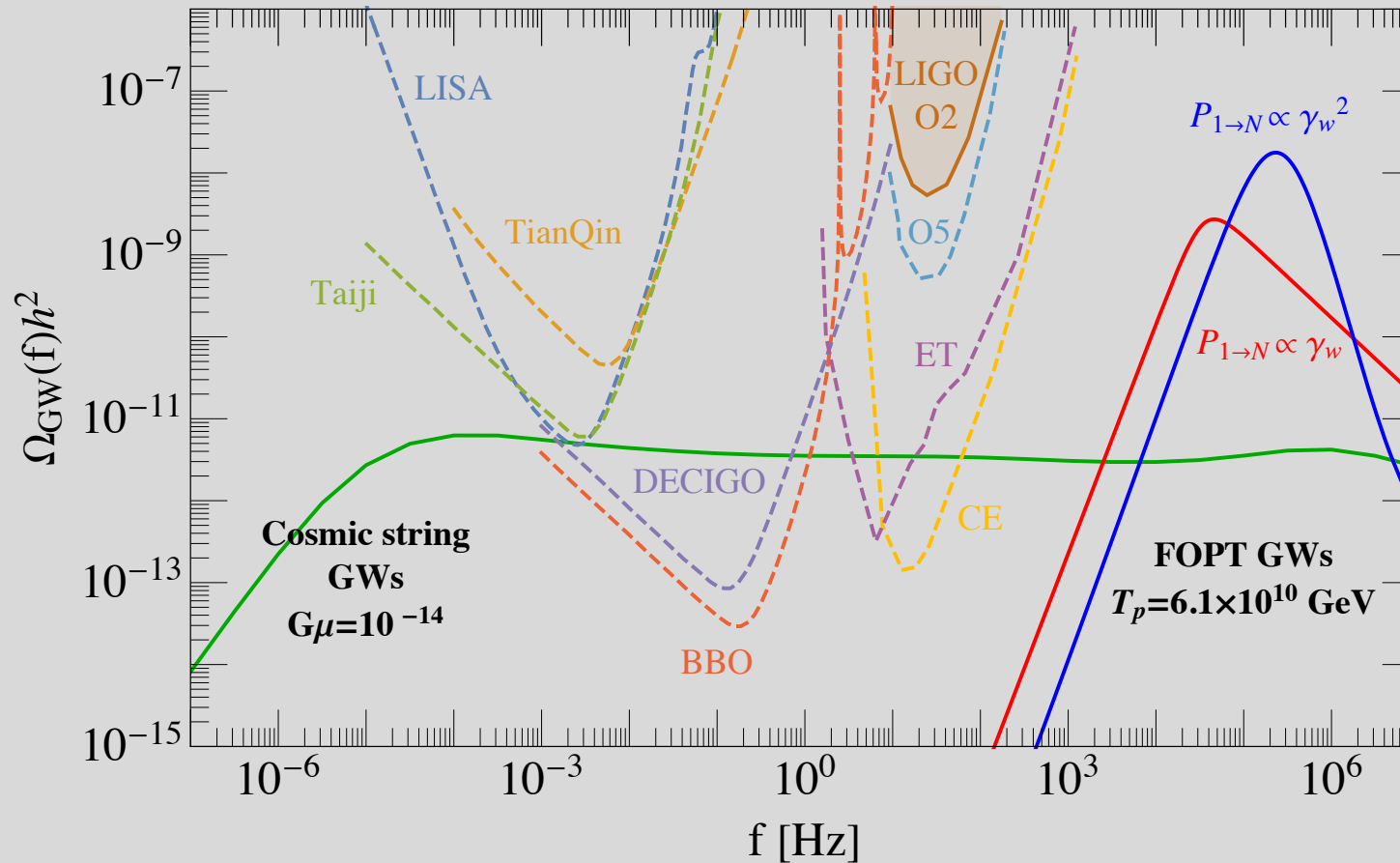
$$M_1 = 2.5 \times 10^{11} \text{ GeV}, \quad \lambda_{R,1} = 0.3, \quad \lambda_{R,2} = \lambda_{R,3} = 4\lambda_{R,1},$$



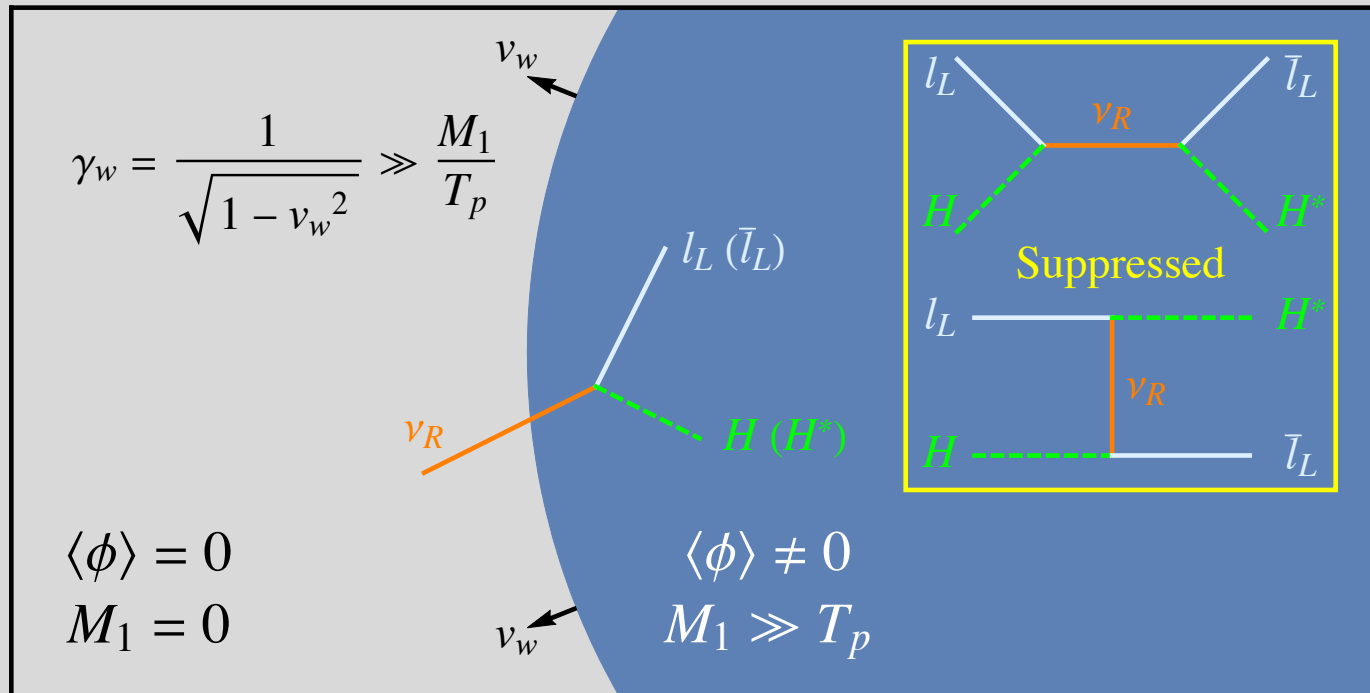
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Conventional Leptogenesis needs CPV 30 times stronger

Gravitational Wave signal



Conclusion



- Suppress the washout effects via a strong first-order PT
- Expand the parameter space for Leptogenesis
- Can be probed by GWs