

# HNL at Muon Colliders

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## HNL at Muon Colliders

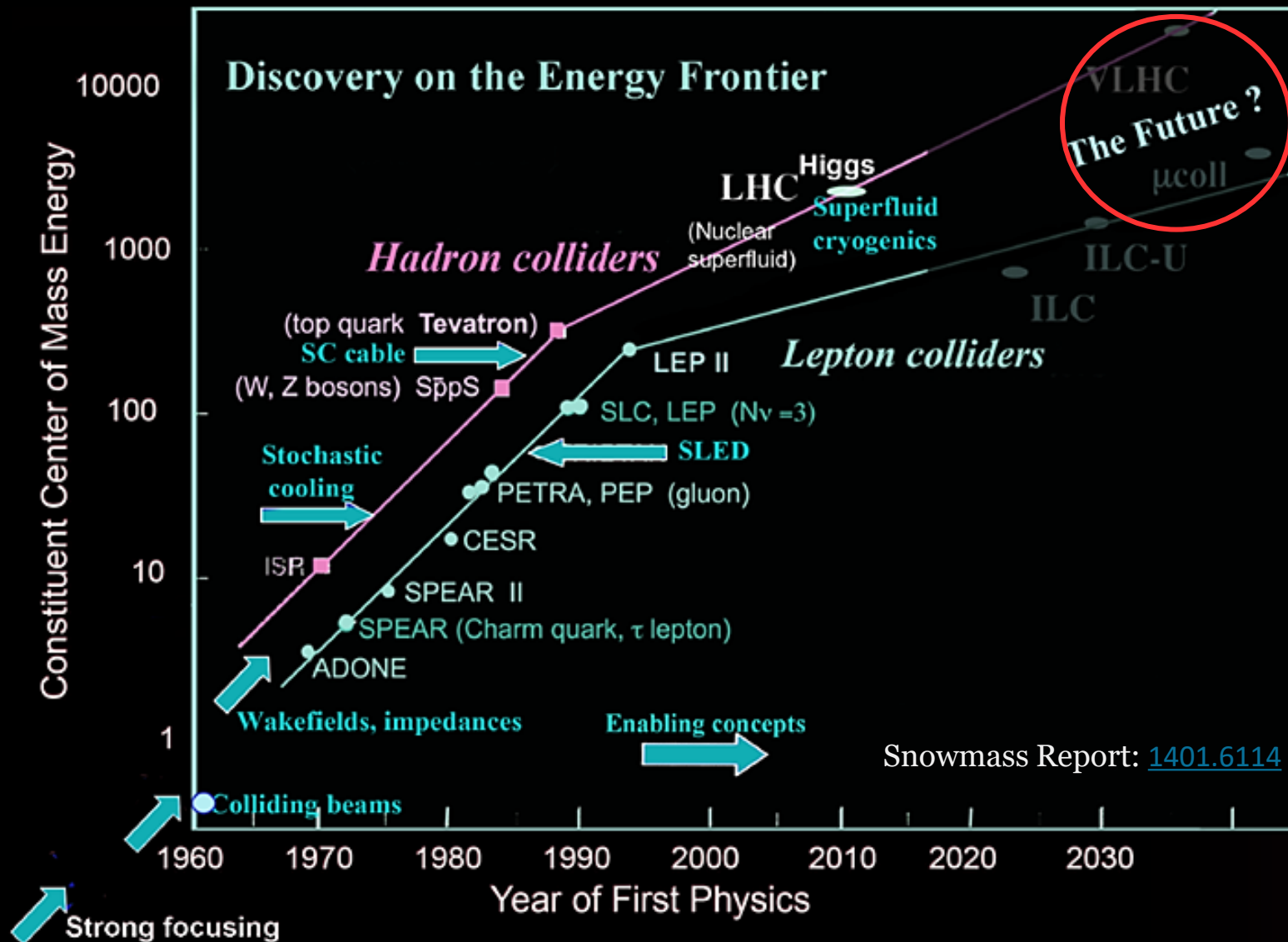
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Mainly based  
upon **Peiran Li**,  
ZL, **Kun-Feng**  
**Lyu**, [2301.07117](#),



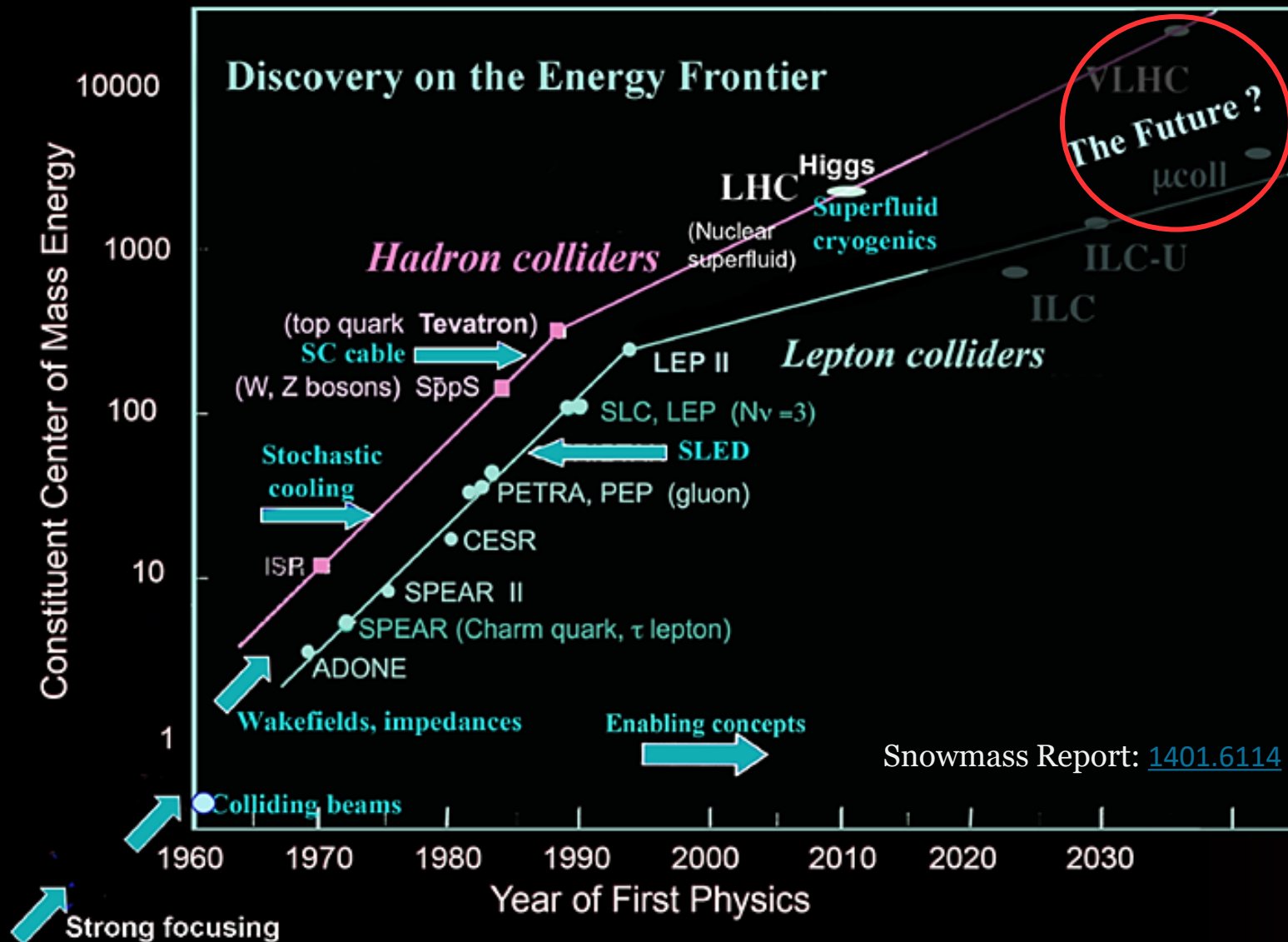
# High Energy Rules



The forefront of tech & ambitions leads to discoveries.

The dream for high energy machines persists in our field

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People's perspectives change over time, now:

- there are excitement/call for future high energy muon collider from theory, accelerator and experimental community.
- Interesting aspects of physics to be examined.

# Neutrino is a puzzling sector

- In SM, neutrino is massless. While the experiments have confirmed its tiny mass  $< 0.1$  eV.
- Seesaw mechanism
  - Simple Type I
  - Inverse seesaw model
  - Linear seesaw model
- We choose to work in a simple scenario. Suppose there is a heavy neutral lepton. We can parametrize its mass  $m_N$  and mixing angle with SM neutrino  $U_\ell = \sin\theta_\ell$ .

$$\mathcal{L} = \mathcal{L}_W + \mathcal{L}_Z + \mathcal{L}_H$$

$$\mathcal{L}_W = \frac{gU_l}{\sqrt{2}} (W_\mu \bar{l}_L \gamma^\mu N + h.c.)$$

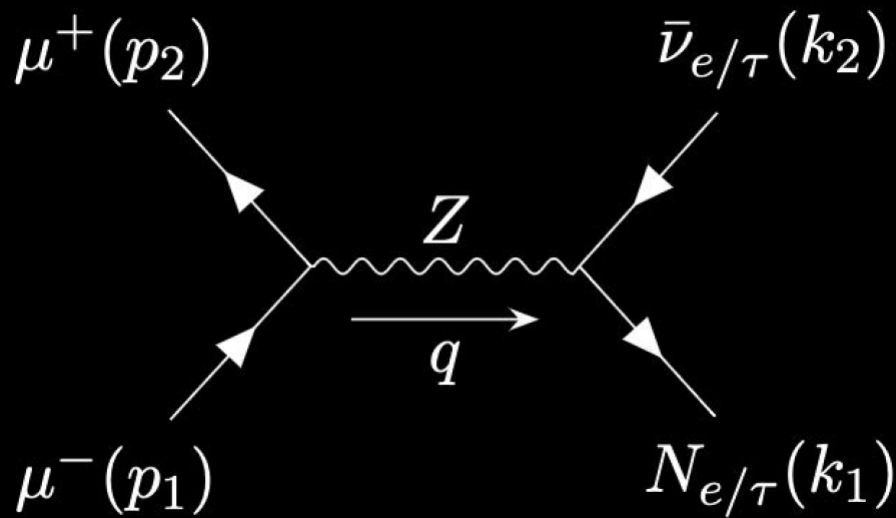
$$\mathcal{L}_Z = -\frac{gU_l}{2 \cos \theta_m} Z_\mu (\bar{\nu}_L \gamma^\mu N + \bar{N} \gamma^\mu \nu_L)$$

$$\mathcal{L}_H = -\frac{U_l m_N}{v} h (\bar{\nu}_L N + \bar{N} \nu_L)$$

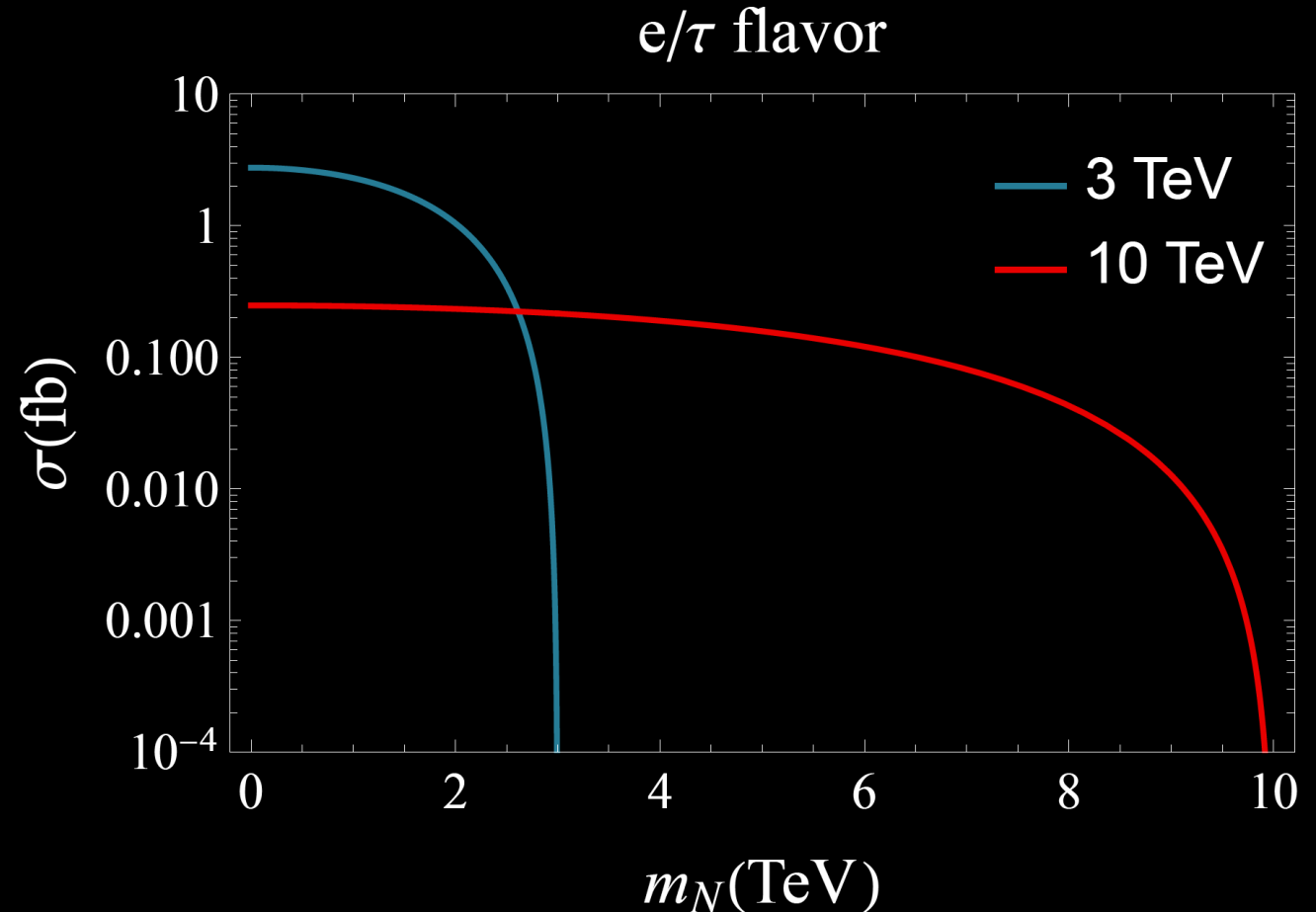
# The physics is rich

- Direct Particle Probes:
  - Production
    - Meson decay, heavy lepton decay
    - (On-shell/Off-shell) Gauge/Higgs boson decay
  - Decay
    - Short-lived
    - Long-lived
- Cosmo and astrophysical probe: BBN, CMB, etc (see in B. Dev's talk.)
- Indirect constraints: branching ratio of SM particles decays, oscillations, etc.

# S-channel production ( $e/\mu/\tau$ flavored)



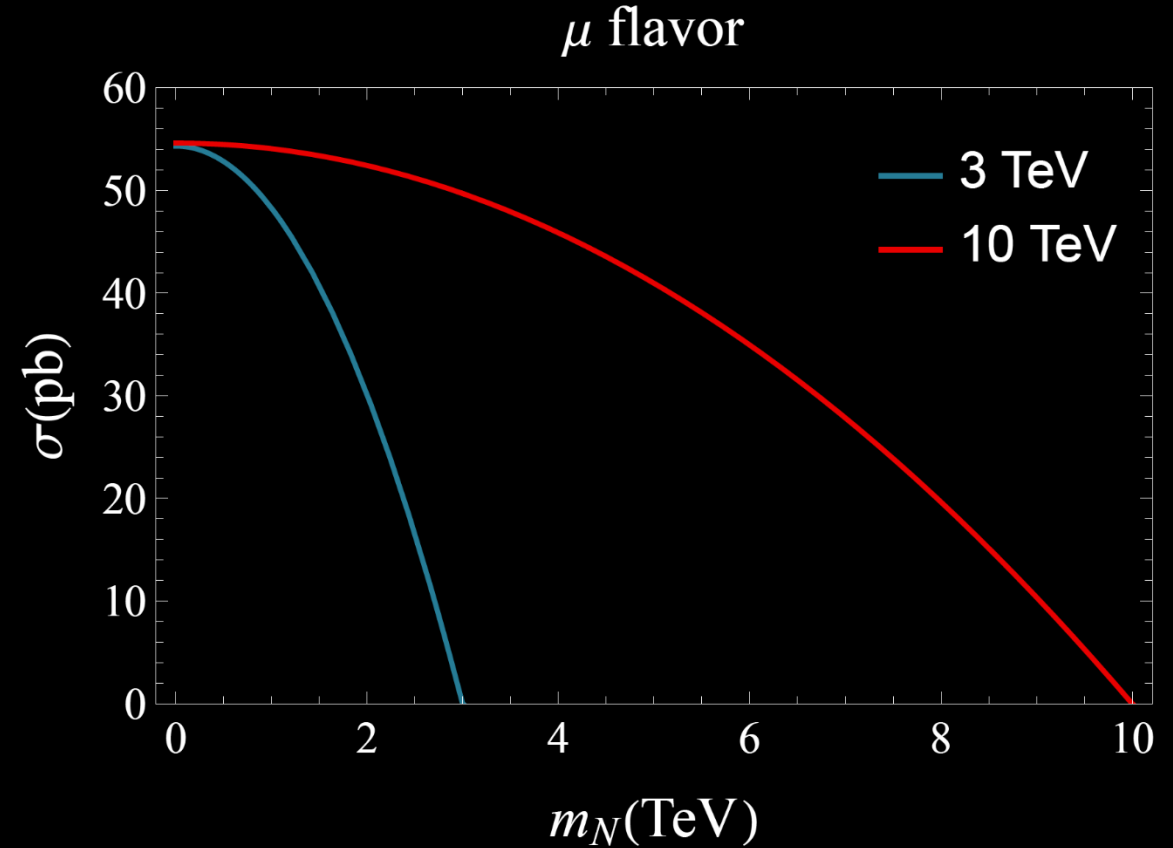
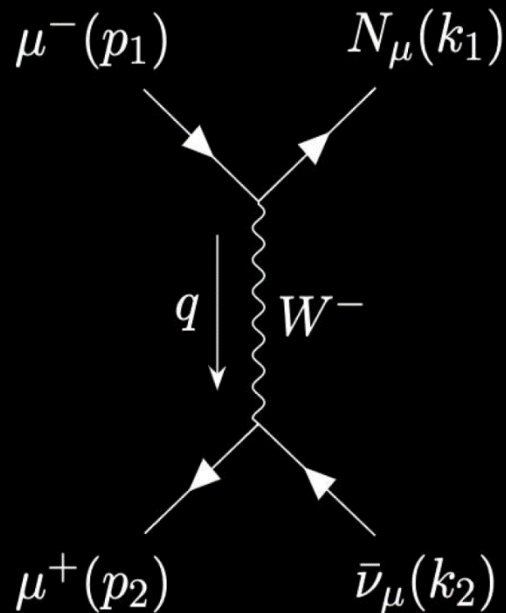
- $1/s$  suppressed;
- Flat rate until near the threshold  $s/2$
- $O(fb)$  cross section;



# Muon Flavor

Production dominated by t-channel

$$\mu^+ + \mu^- \rightarrow N_\mu + \bar{\nu}_\mu$$



Type	Signal process	$\sigma/ U_\mu ^2$ (w. conj. channel) $m_N = 1$ TeV
t-channel	$\mu^+ \mu^- \rightarrow N_\mu \bar{\nu}_\mu$	20.28 pb
VBF	$\mu^+ \mu^- \rightarrow \mu^+ \mu^- N_\mu \bar{\nu}_\mu$	$\sim 1$ pb
VBF	$\mu^+ \mu^- \rightarrow \bar{\nu}_\mu \nu_\mu N_\mu \bar{\nu}_\mu$	$\sim 0.1$ pb



# Decay selection $m_N > O(100) \text{ GeV}$

- $N_\mu \rightarrow W^+ + \mu^-$
- $N_\mu \rightarrow Z + \nu_\mu$
- $N_\mu \rightarrow H + \nu_\mu$

$$N_\mu \rightarrow W^+ + \mu^-, \quad W \rightarrow jj$$

$$\mu^+ + \mu^- \rightarrow N_\mu + \bar{\nu}_\mu \rightarrow jj + \mu^- + \bar{\nu}_\mu$$

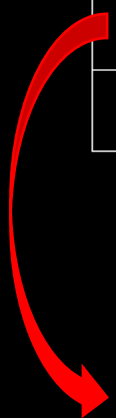
The dijets almost come from onshell W/Z boson.

We focus on the final states of  $W$  and  $\mu$  and reconstruct its invariant mass distribution.

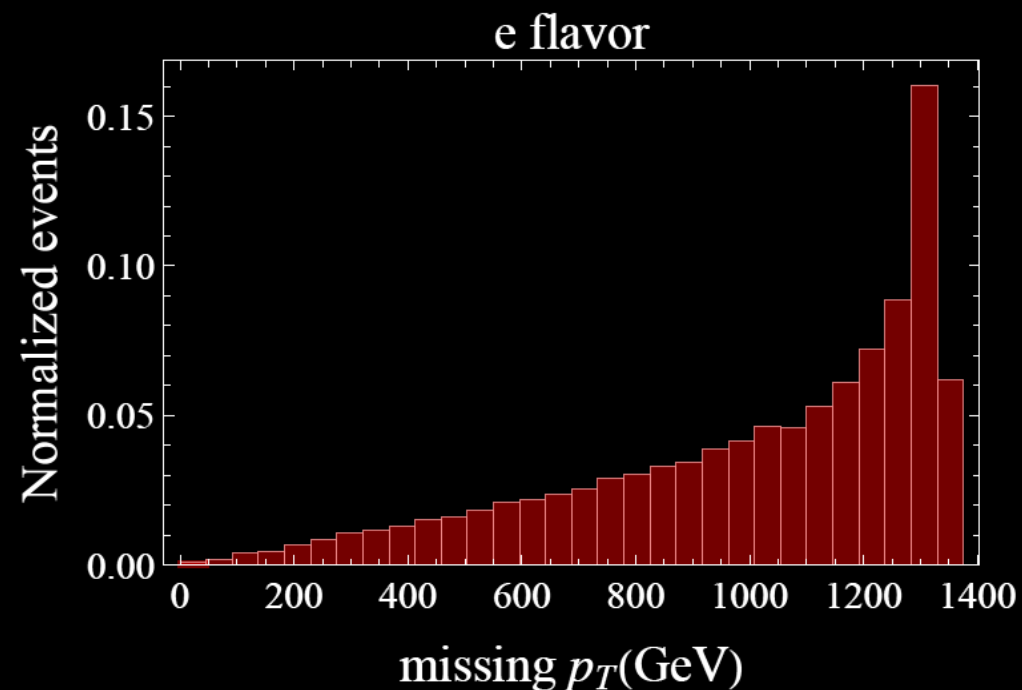
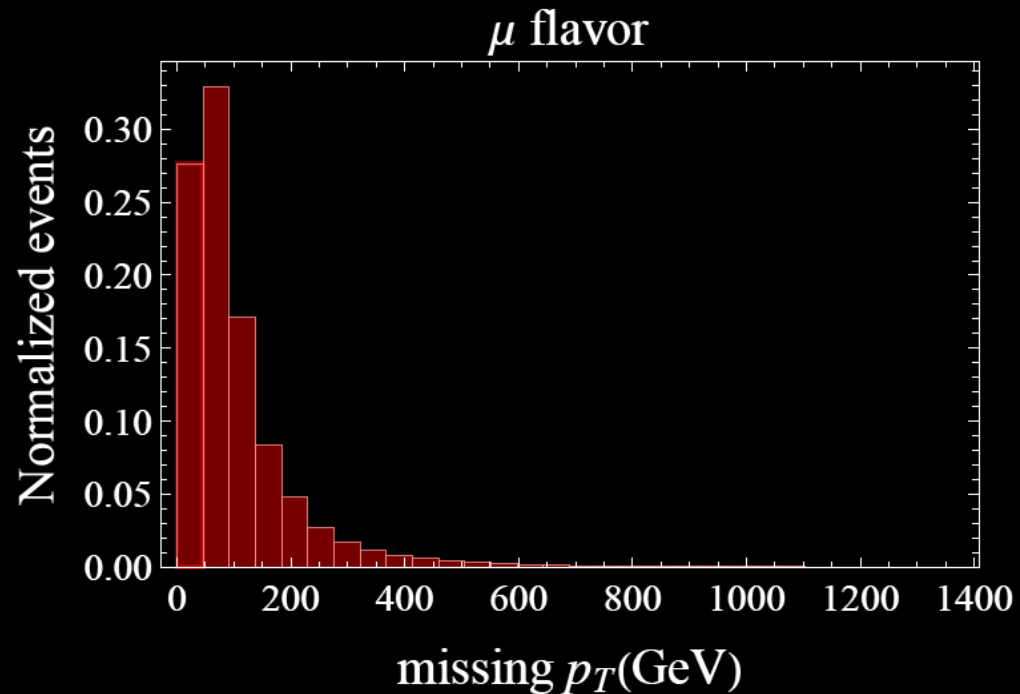
Including the charge conjugation process

# 10TeV Background

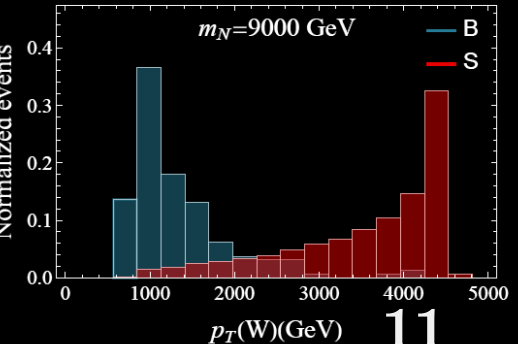
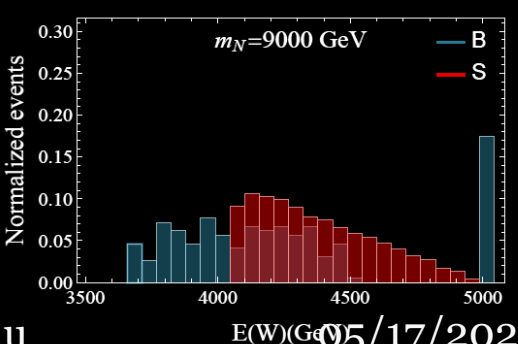
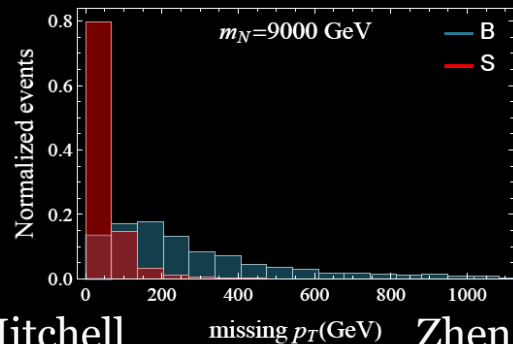
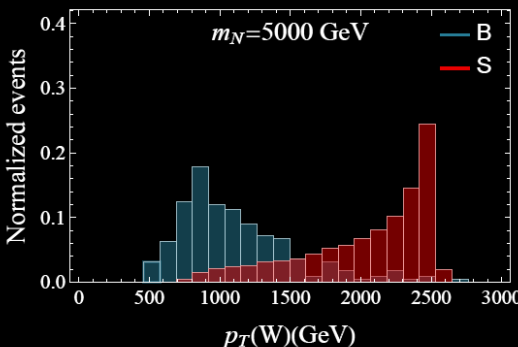
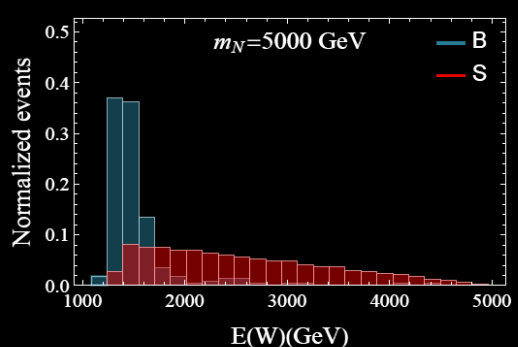
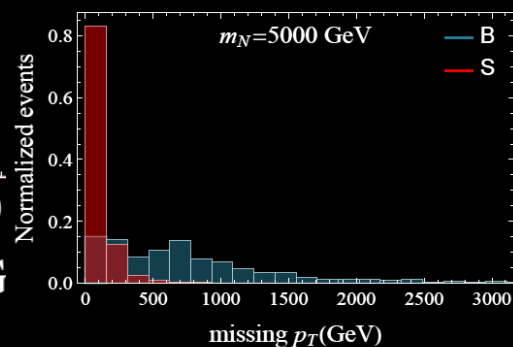
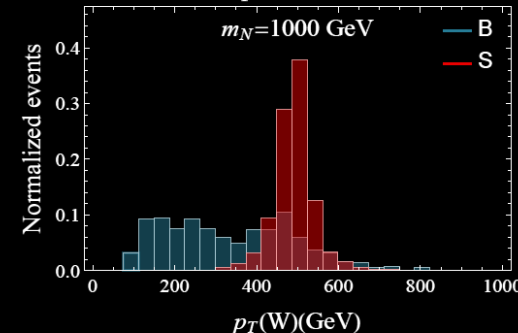
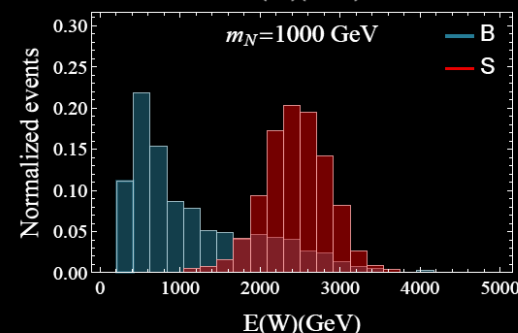
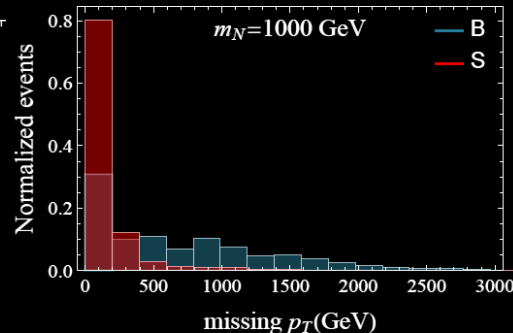
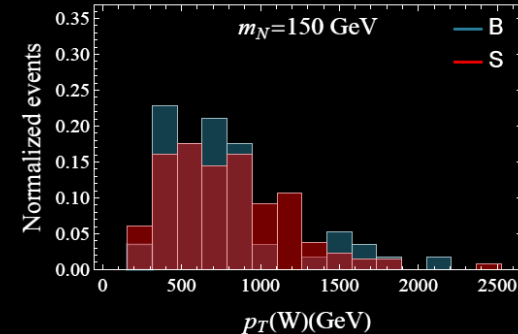
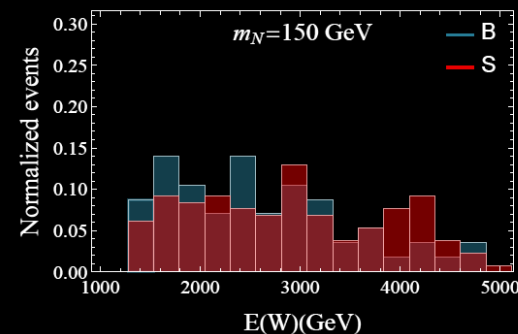
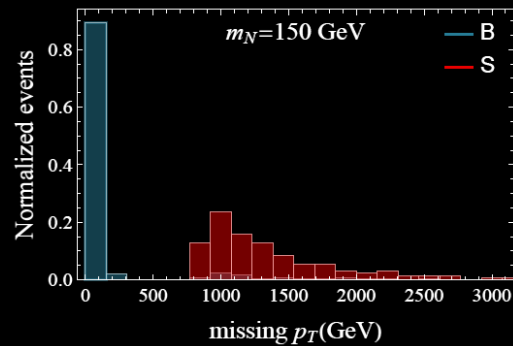
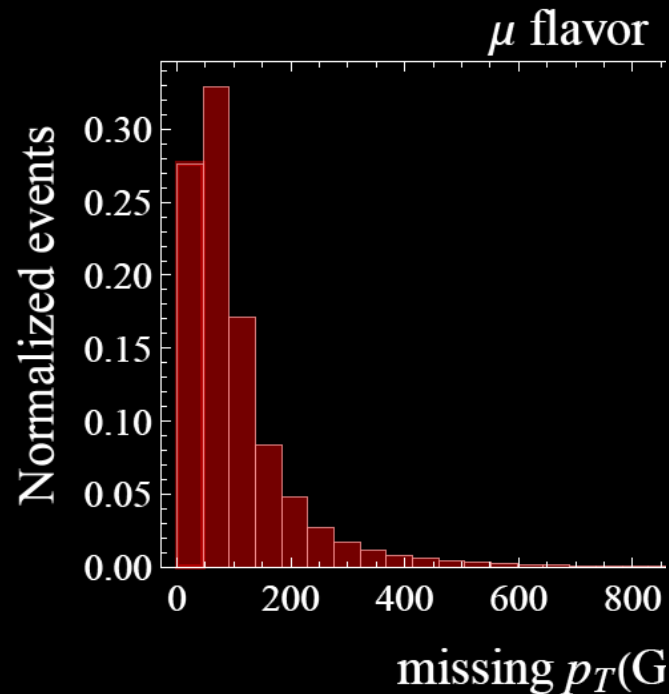
Type	Background process	$\sigma$ (w. conj. channel)	Pre-selection cut (PSC)
$t$ -channel	$\mu^+\mu^- \longrightarrow W^+\mu^-\bar{\nu}_\mu$	0.214 pb	PSC
$t$ -channel	$\mu^+\mu^- \longrightarrow Z\mu^+\mu^-$	0.464 pb	PSC & missing $\mu^+$
VBF	$\mu^+\mu^- \longrightarrow \mu^+\mu^-W^+\mu^-\bar{\nu}_\mu$	0.401 pb	PSC & missing $\mu^+\mu^-$
VBF	$\mu^+\mu^- \longrightarrow \bar{\nu}_\mu\nu_\mu W^+\mu^-\bar{\nu}_\mu$	0.0686 pb	PSC

- 
- Using EVA in MadGraph, especially photon PDF (EVA: Effective Vector-Boson Approximation)
  - Including Z boson: Dijets can come from either W or Z boson.

# Kinematics



# Kinematics



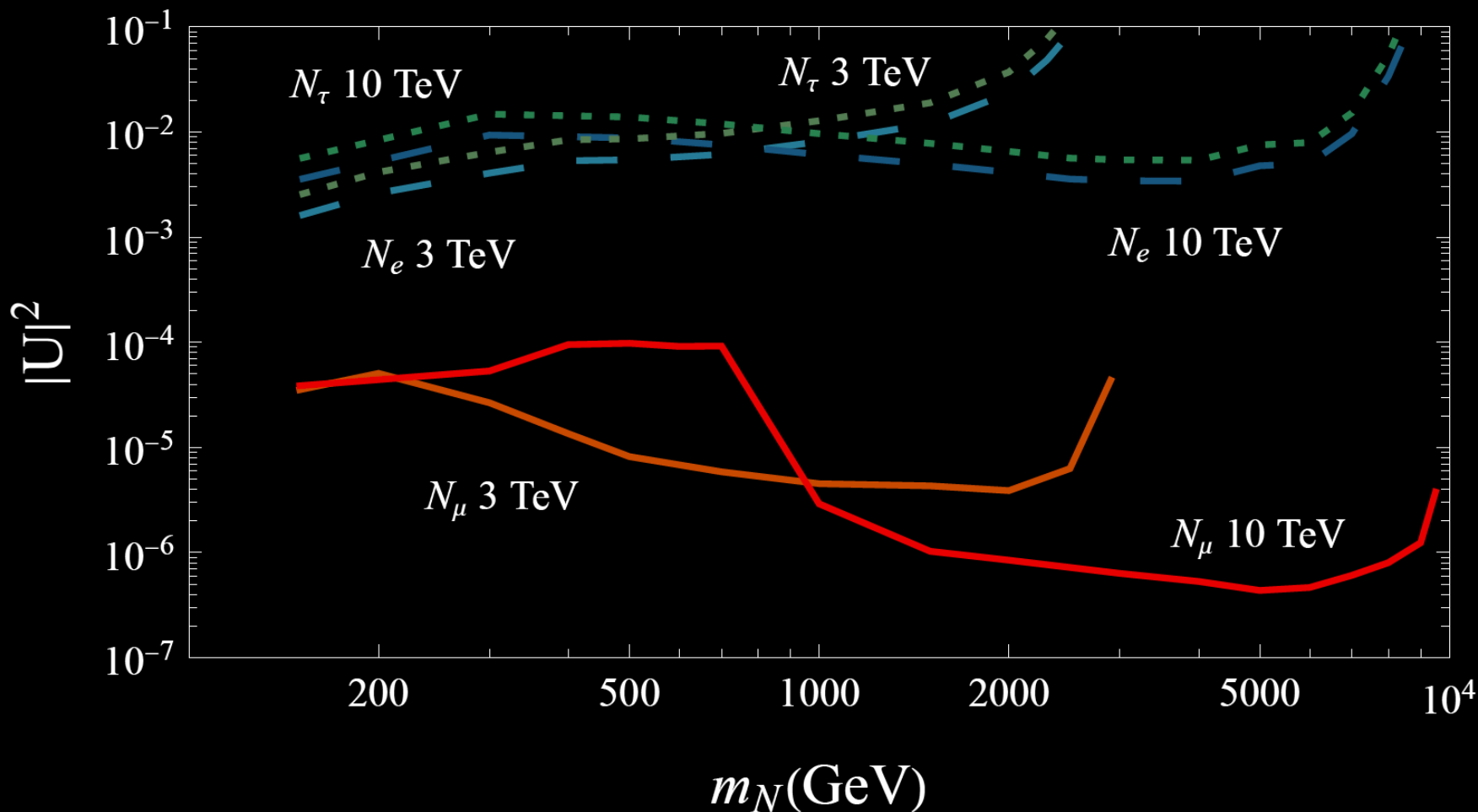
# Cutflow Analysis

$$\mu^+ + \mu^- \rightarrow N_\mu + \bar{\nu}_\mu \rightarrow jj + \mu^- + \bar{\nu}_\mu$$

- Pre-selection: require single visible charged lepton
  - $|\eta(\mu)| < 2.5$  and  $p_T(\mu) > 20$  GeV
- Central hadronic W selection: require visible on-shell W boson
  - $|\eta(W)| < 2.5$  and  $p_T(W) > 20$  GeV
- Mass window: reconstructed mass  $m_{W\mu}$  within  $m_N \pm 5\%m_N$
- Optimization cuts:
  - Customized cut on missing  $p_T$ ,  $E(W)$ ,  $p_T(W)$  for each  $m_N$  benchmark

Background process	Central W	Mass window 150/1000/5000/9000 GeV	Optimization
$\mu^+\mu^- \rightarrow W^+\mu^-\bar{\nu}_\mu$	89.14%	0.28/2.4/3.2/1.6%	0.28/0.42/1.1/0.80%
$\mu^+\mu^- \rightarrow Z\mu^+\mu^-$	1.60%	0/0.085/0.039/0.016%	0/0.051/0/0%
$\mu^+\mu^- \rightarrow \mu^+\mu^-W^+\mu^-\bar{\nu}_\mu$	43.39%	1.6/0.75/0.011/0%	0/0.73/0.0083/0%
$\mu^+\mu^- \rightarrow N_\mu\bar{\nu}_\mu$	Central W	Mass window	Optimization
$m_N = 150$ GeV	55.04%	55.04%	55.04%
$m_N = 1000$ GeV	54.75%	54.75%	51.63%
$m_N = 5000$ GeV	99.93%	99.93%	97.46%
$m_N = 9000$ GeV	99.99%	99.99%	98.27%

# Projected sensitivity



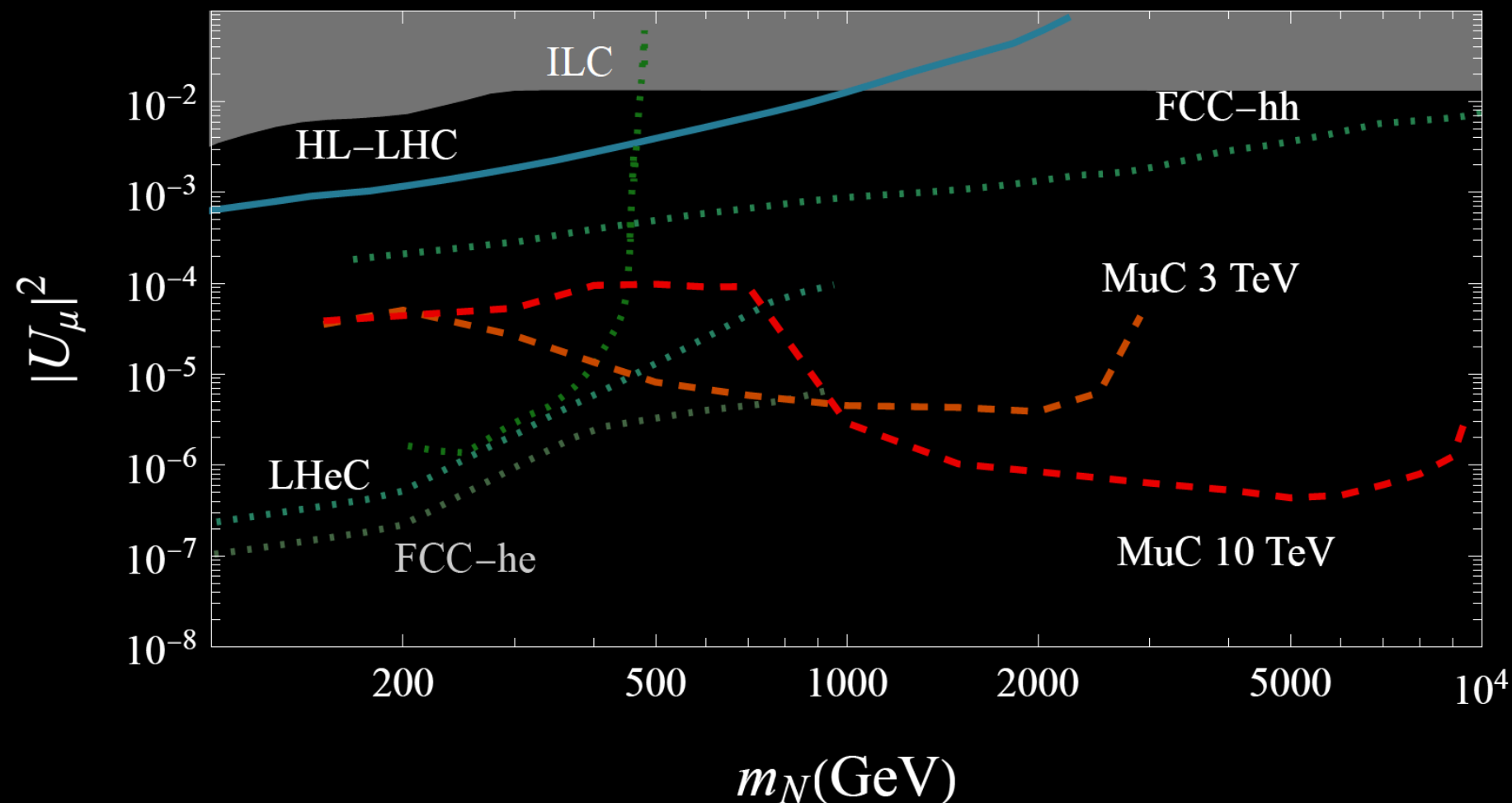
Sensitivity to  $e$  and  $\tau$  flavor is moderate

Muon Collider features the strong direct probe of the  $\mu$  flavored HNL

10 TeV muon collider can probe the  $|U_\mu|^2$  to a few  $10^{-7}$  for TeV scale HNLs.

The VBF background increases for high energy muon colliders and renders the 3 TeV muon collider competitive in sub TeV scale.

# Projections w. others

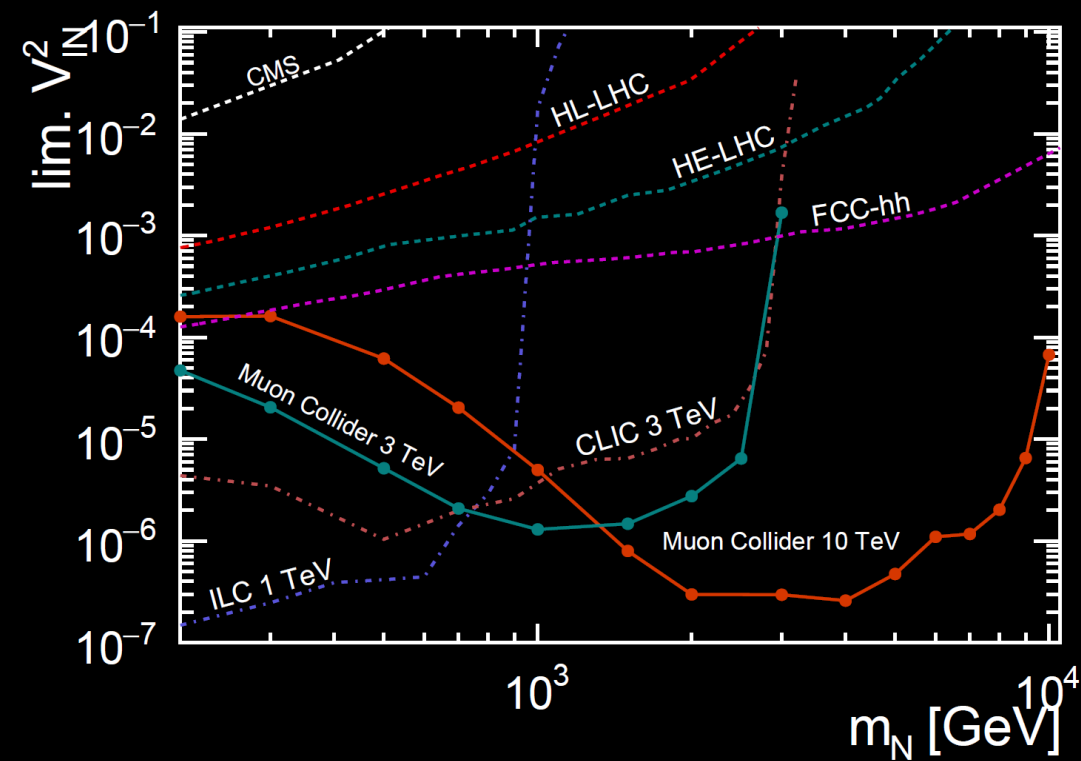
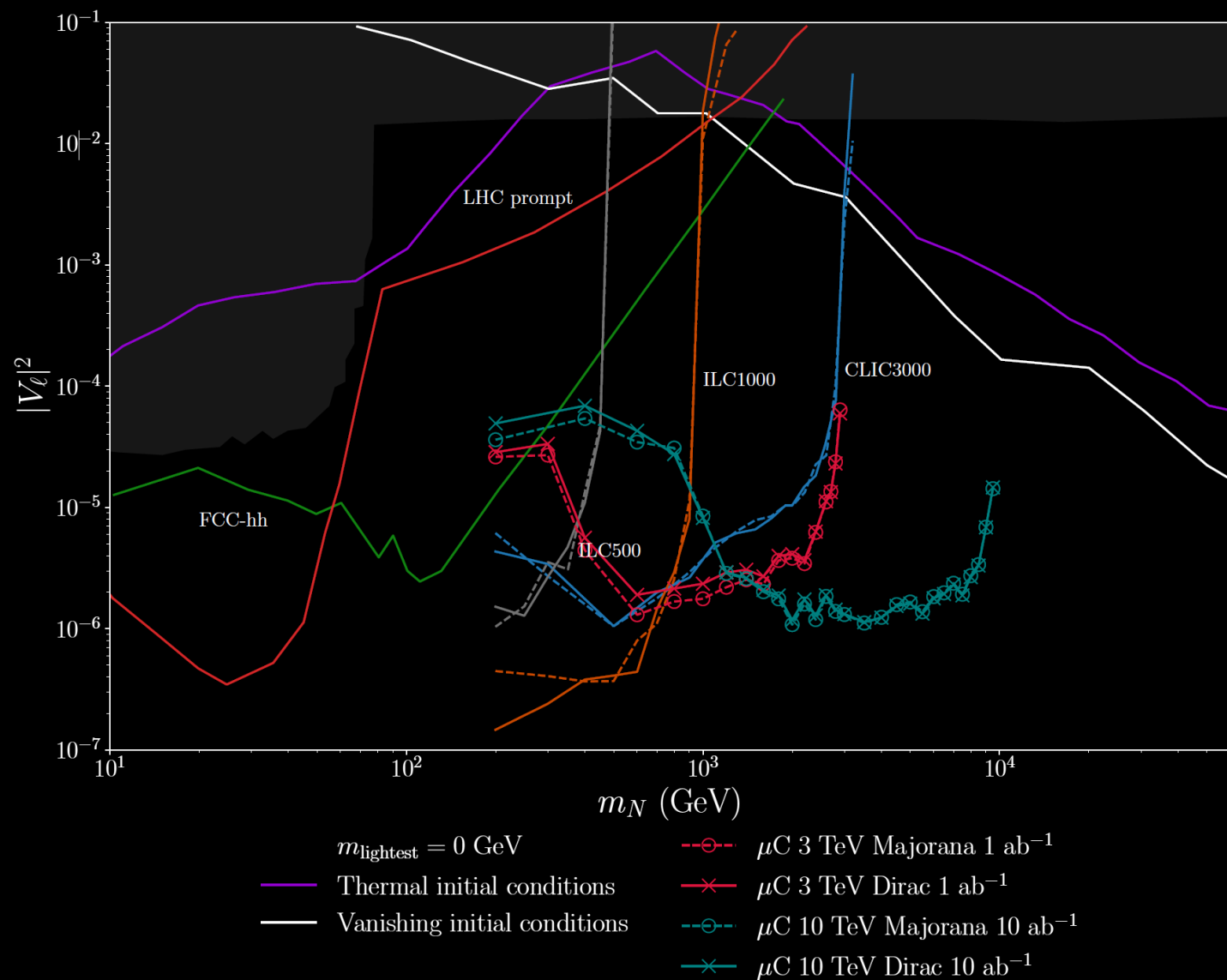


Focusing on the muon-flavored case:

LHC and EWPd probe  $O(10^{-3})$

Muon Collider has unique roles in probing the parameter space (thanks to the t-channel enhancement).

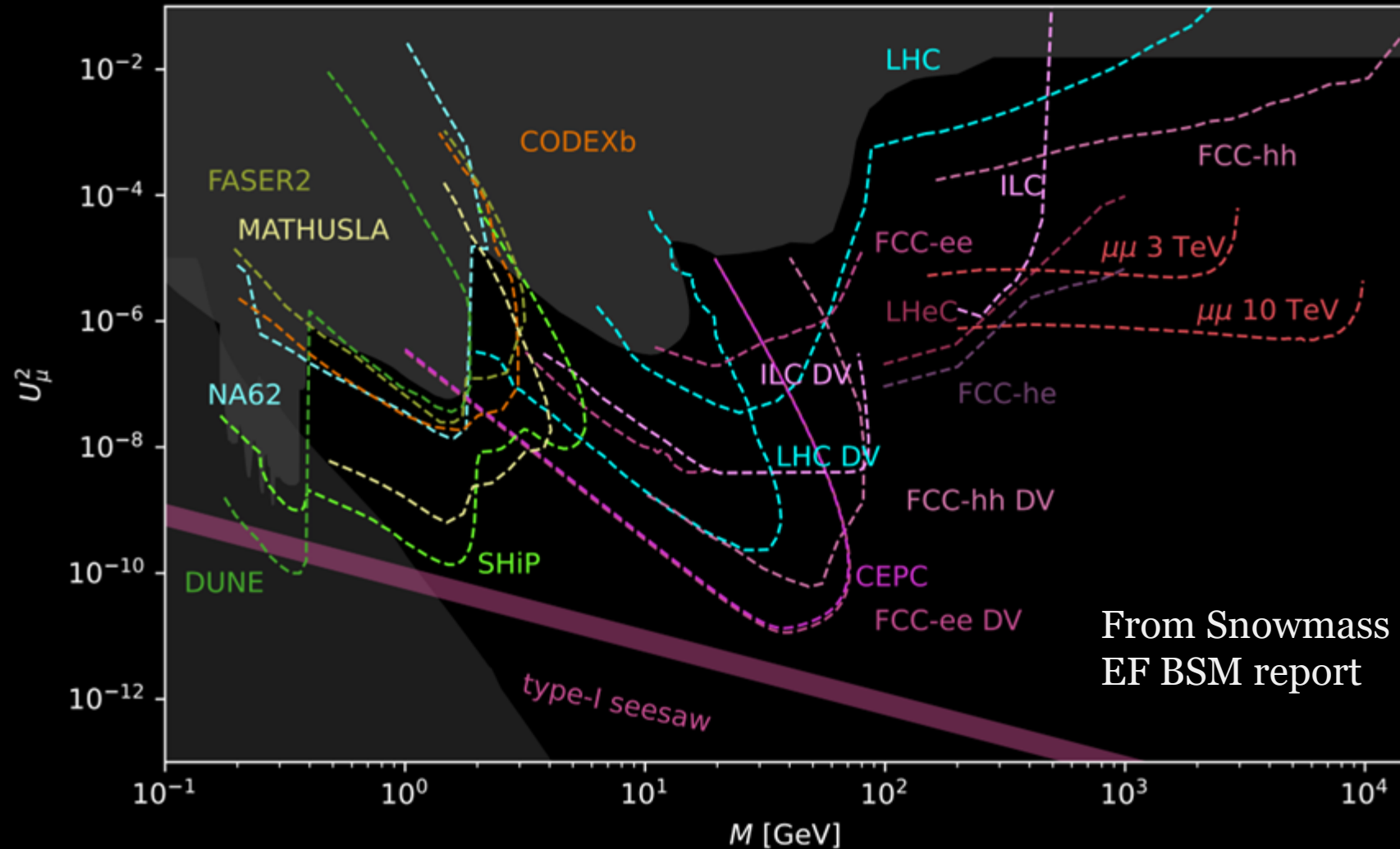
# BDT-based projections



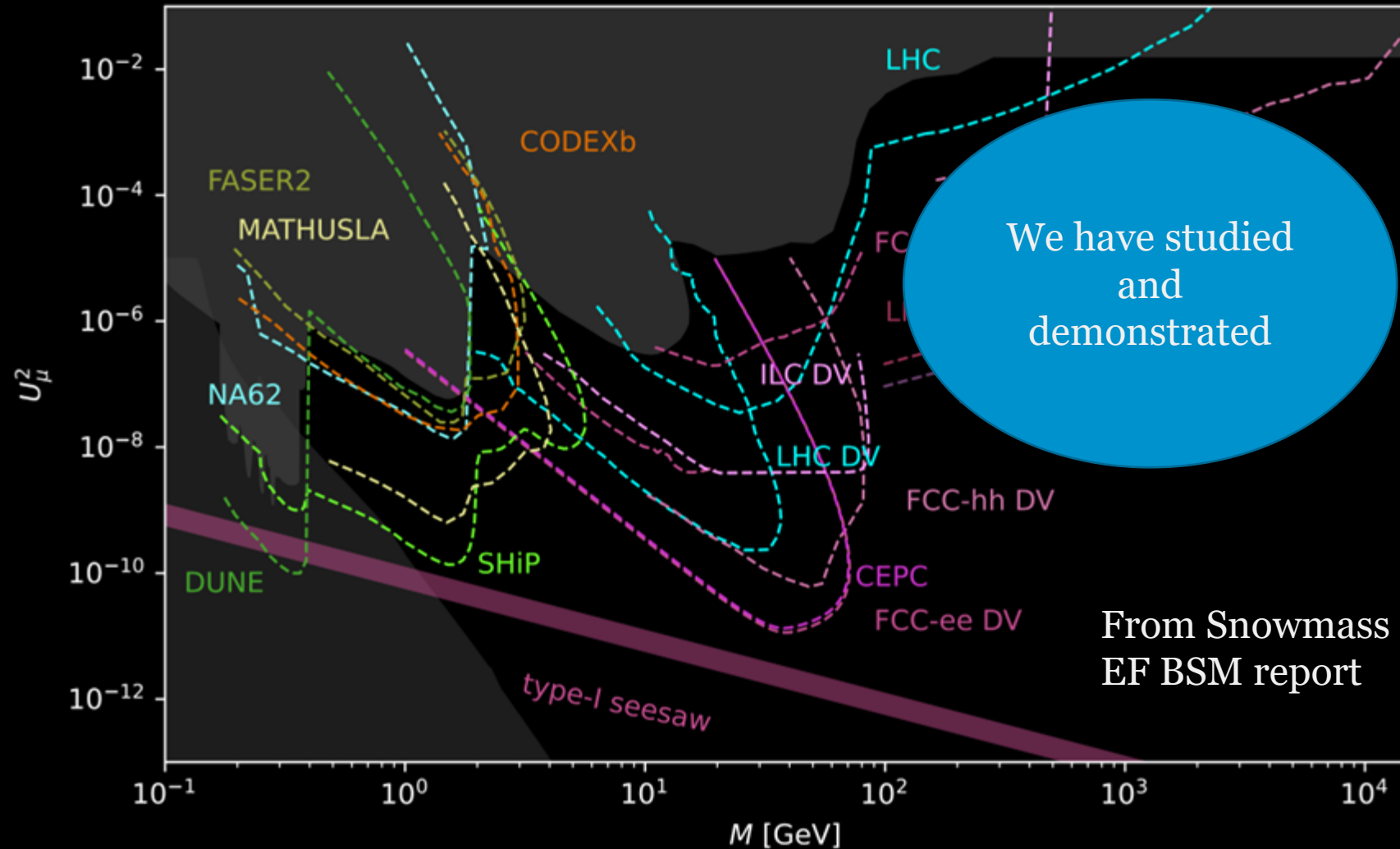
T.H. Kwok, L. Li, T. Liu and A. Rock,  
[arXiv:2301.05177](https://arxiv.org/abs/2301.05177)  
 K. Mekała, J. Reuter and A.F. Zarnecki,  
[arXiv:2301.02602](https://arxiv.org/abs/2301.02602)



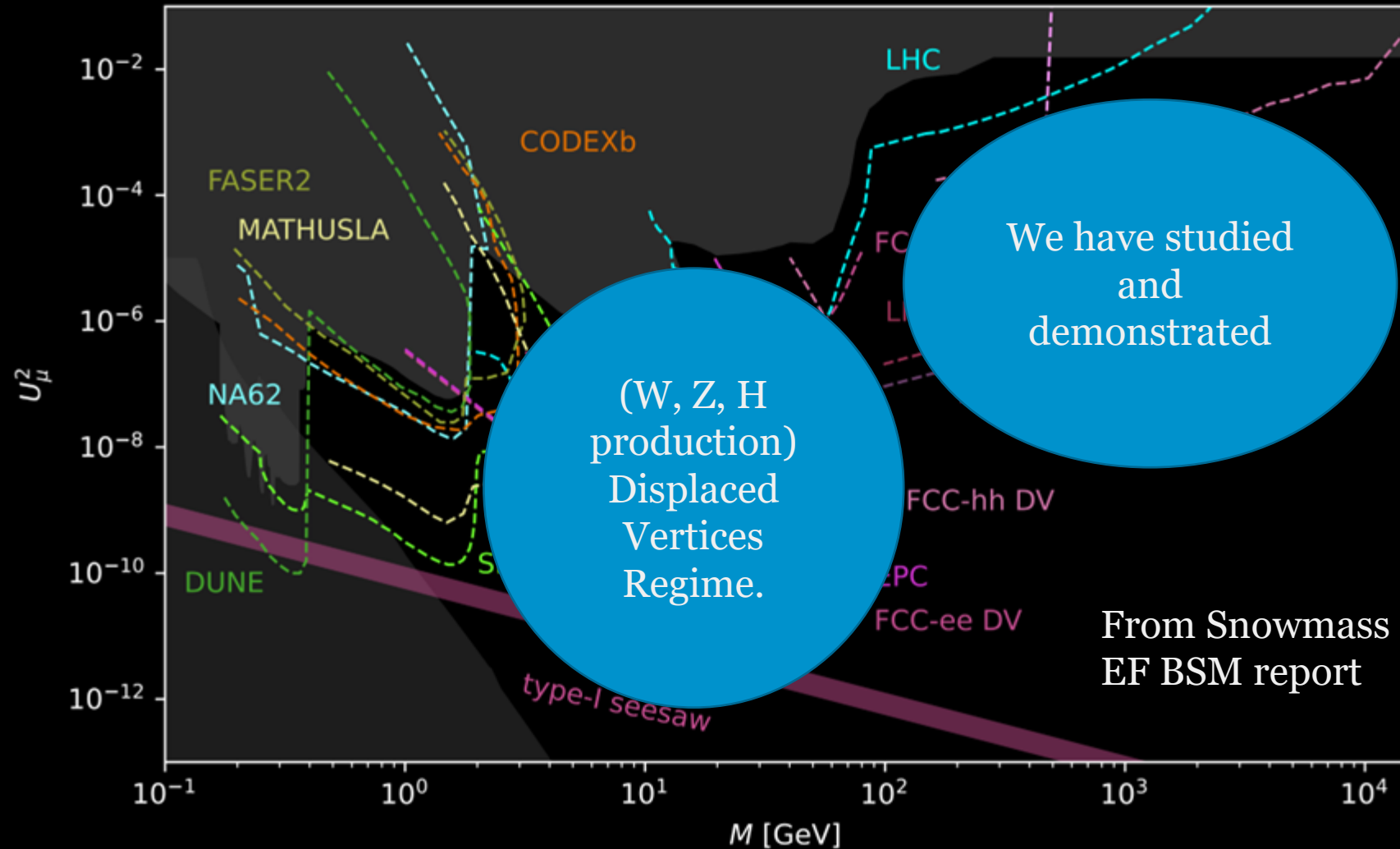
# New studies for other regions



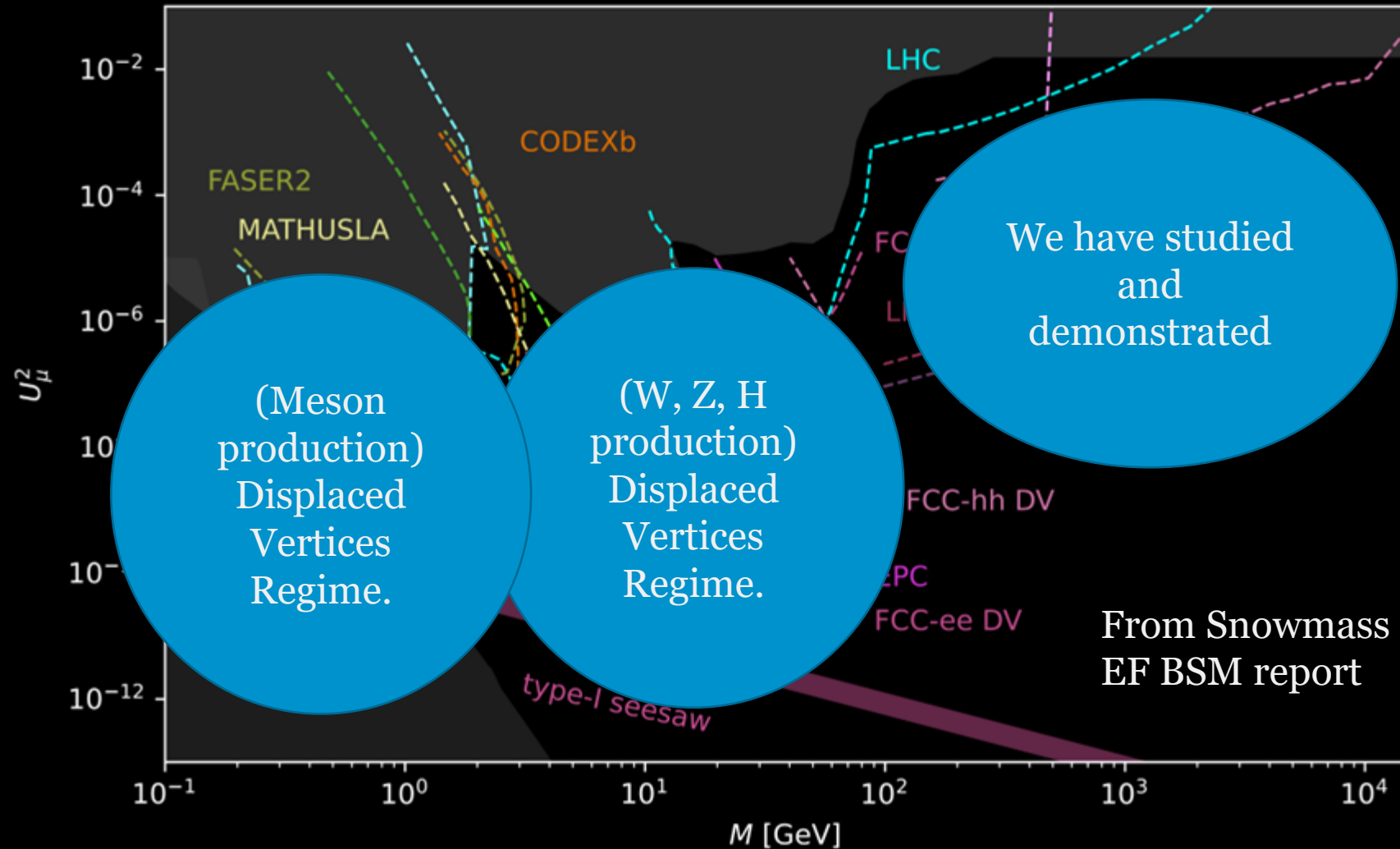
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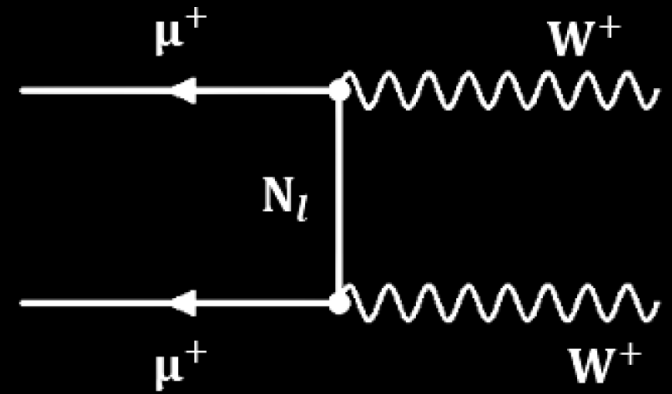
***A few other aspects***

# Same-sign muon collider

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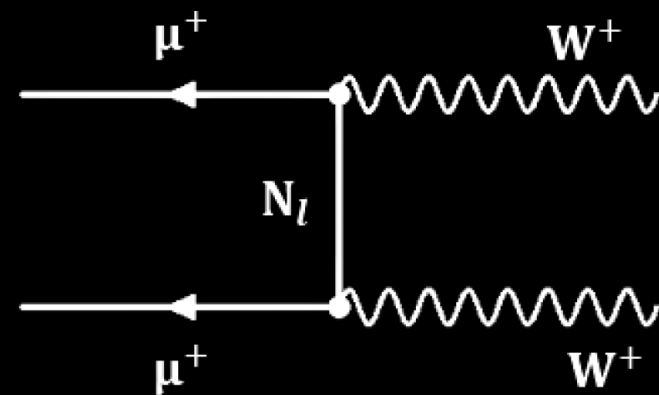
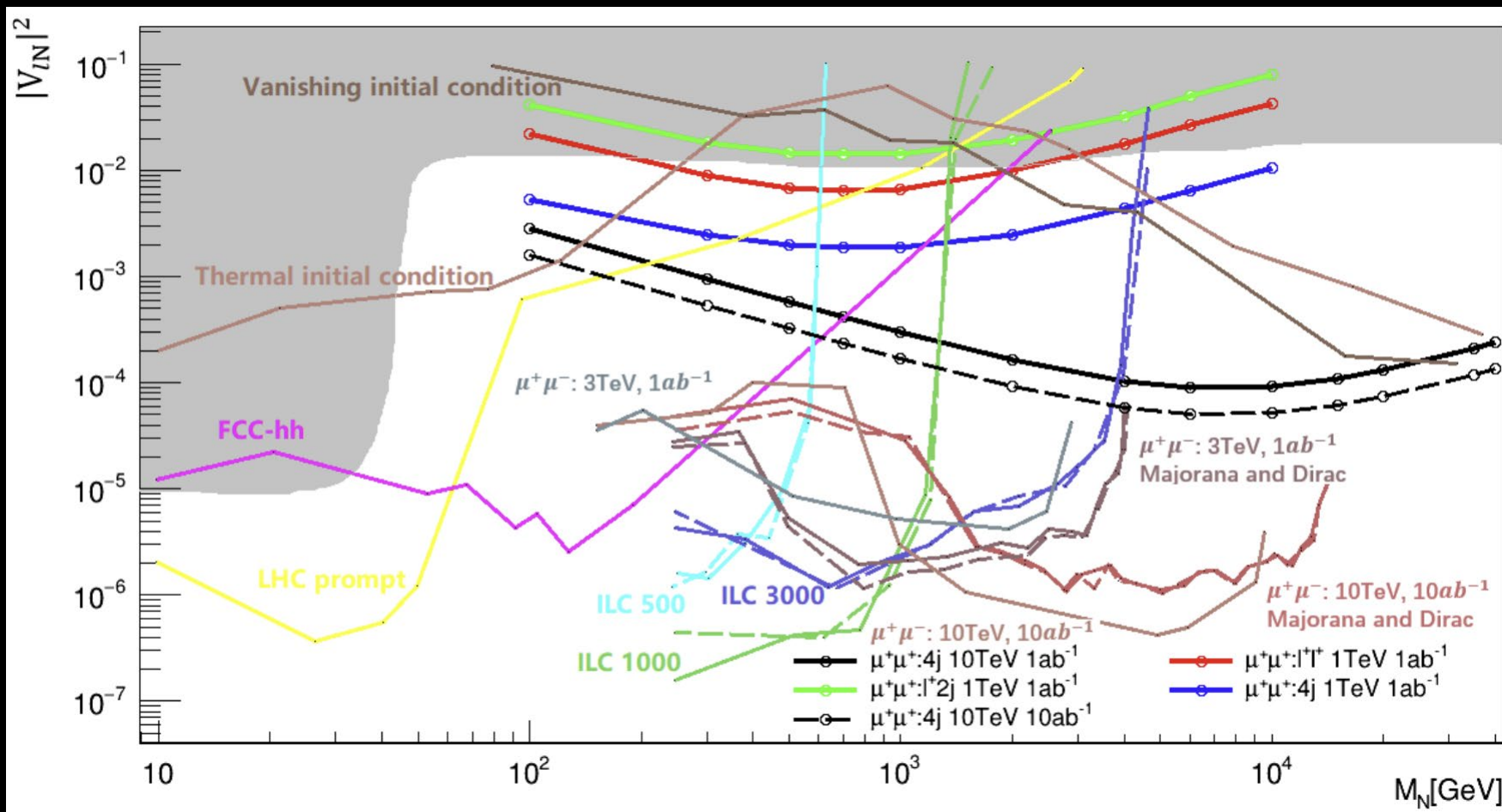
$\mu^+\mu^+$  collider, KEK  
muon program  
motivated, see,  
Kitano et al,  
[2304.14020](#),  
[2210.11083](#),  
[2201.06664](#)

# Same-sign muon collider



$\mu^+\mu^+$  collider, KEK  
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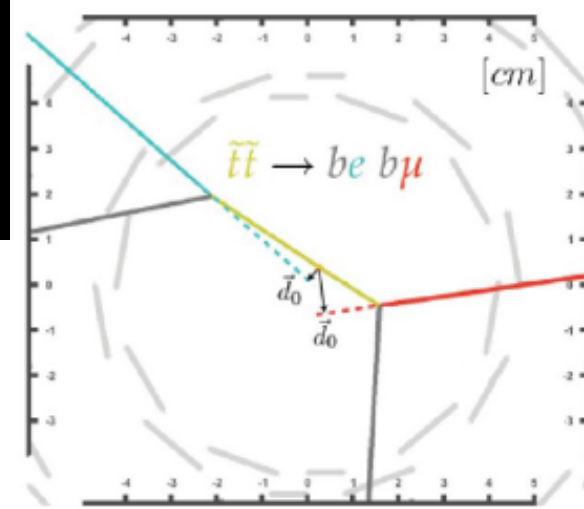
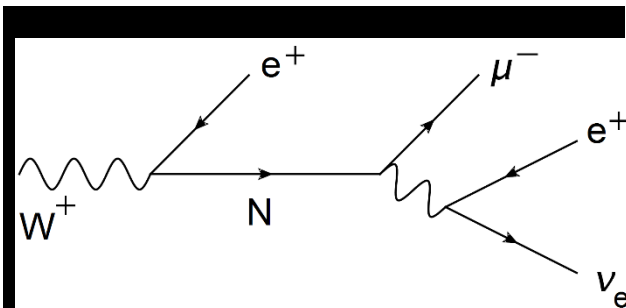
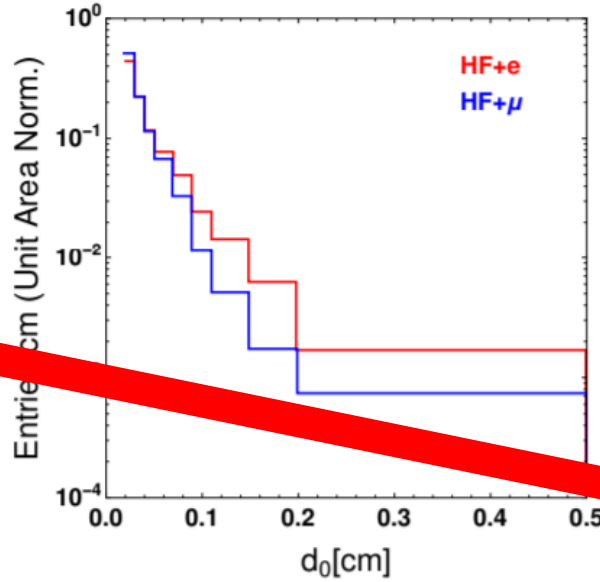
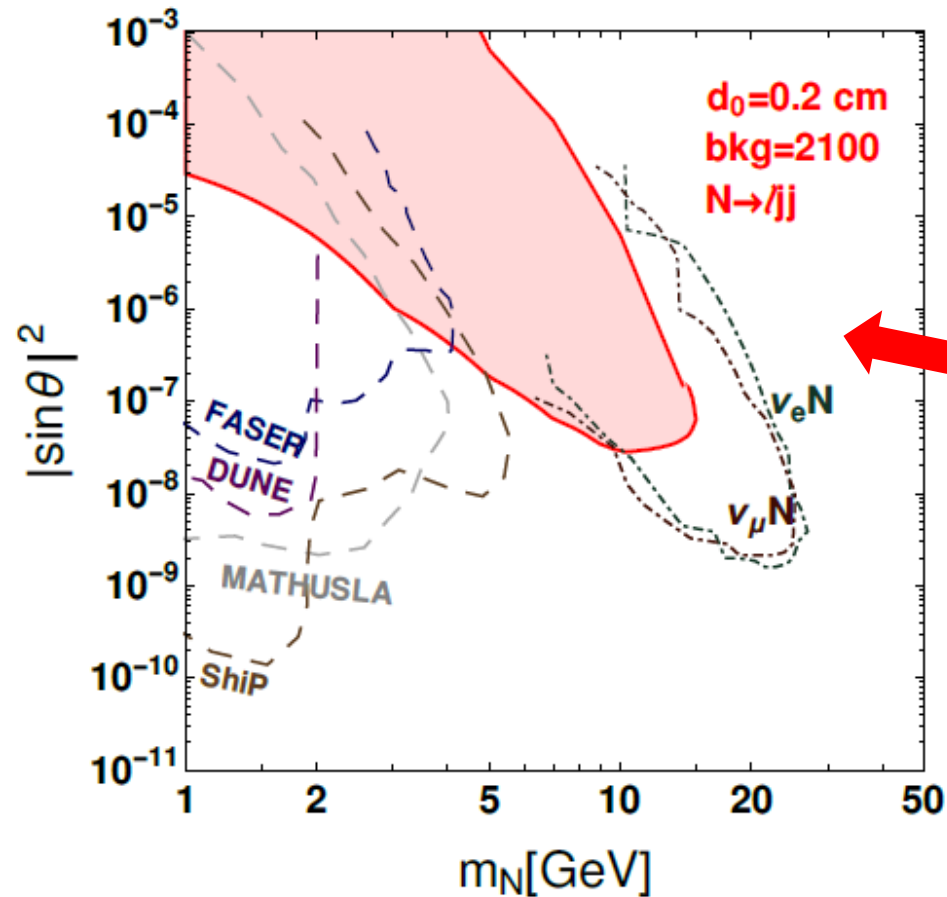


$\mu^+\mu^+$  collider, KEK  
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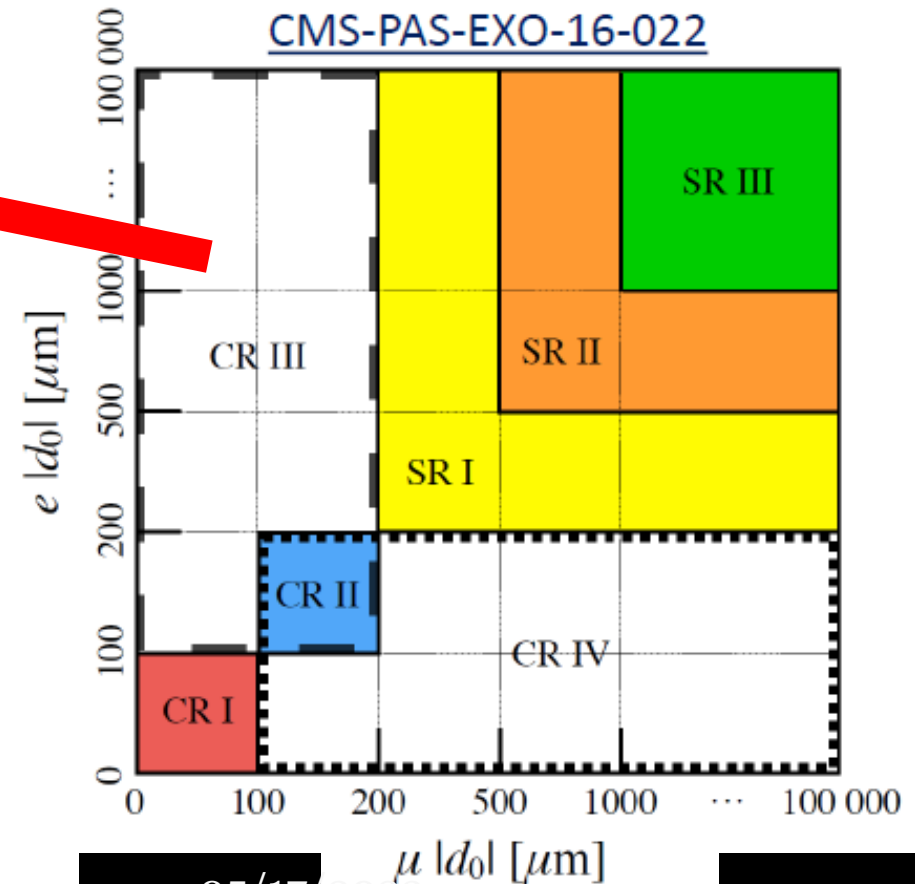
Jiang, Yang, Qian, Ban, Li, You, Li,  
[2304.04483](#)



# displaced lepton for HNL



← Single displaced leptons not from the same vertex; focused on e-mu state



Digging hard and use the control region studies to propose new searches on sterile neutrinos.

ZL, J. Liu, L.-T. Wang, X. Wang, [1904.01020](#)

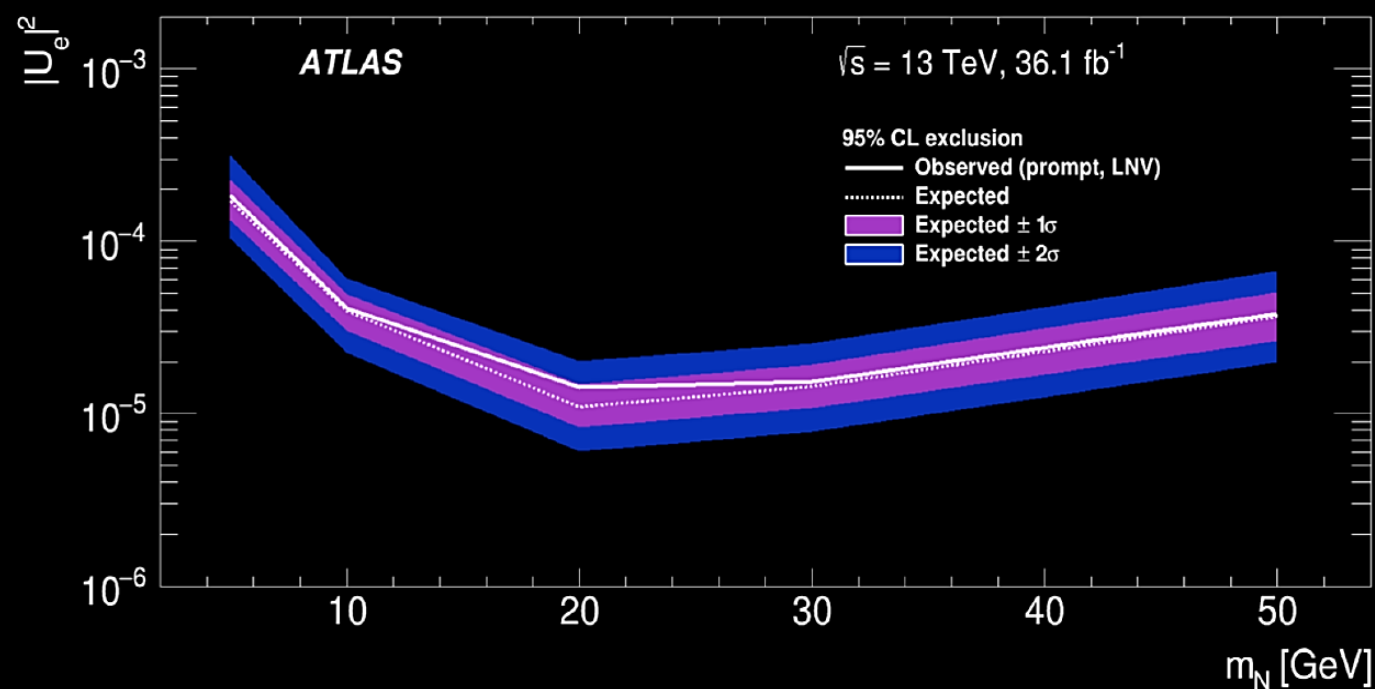
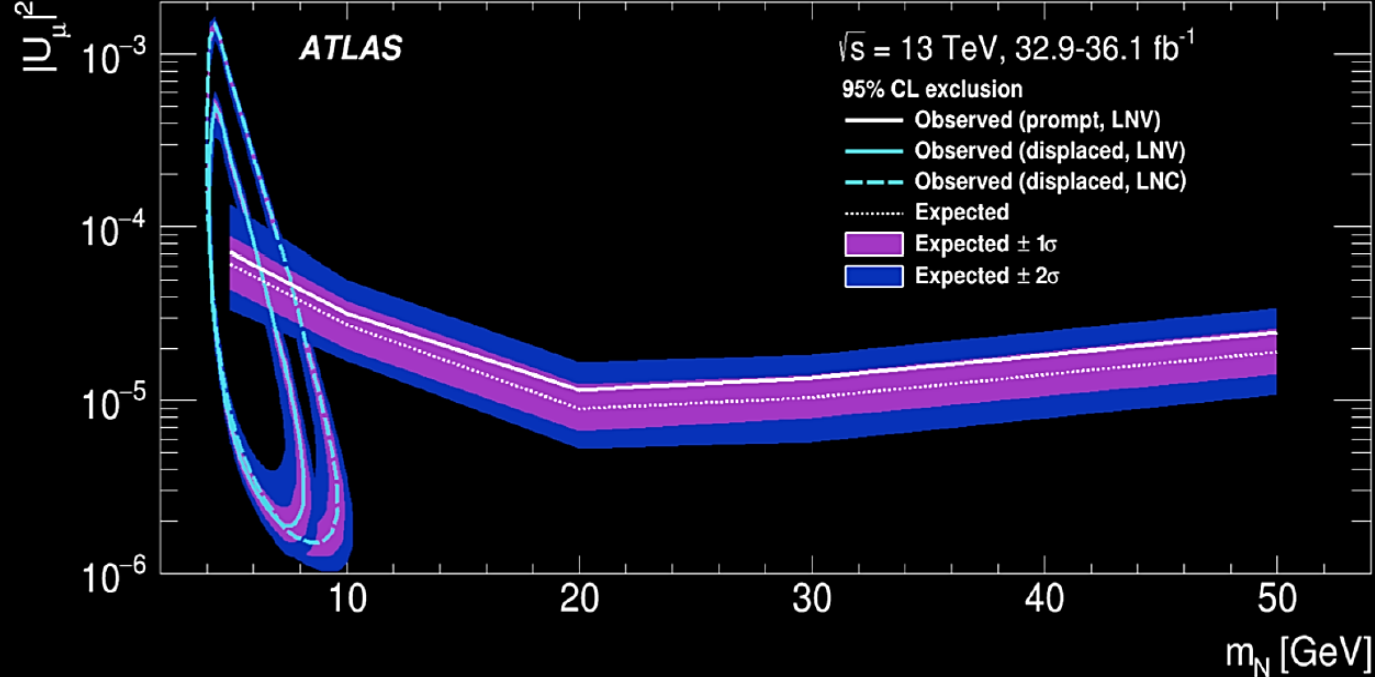
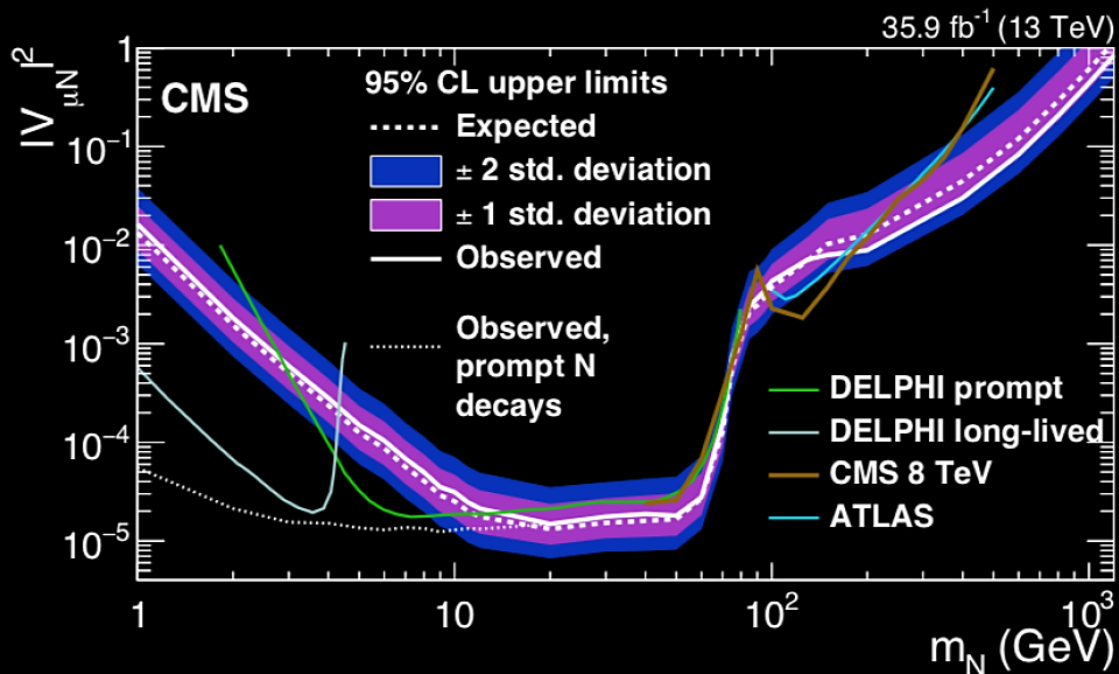
HNL @ MuC

TAMU Mitchell

Zhen Liu

05/17/2023

# Current LHC



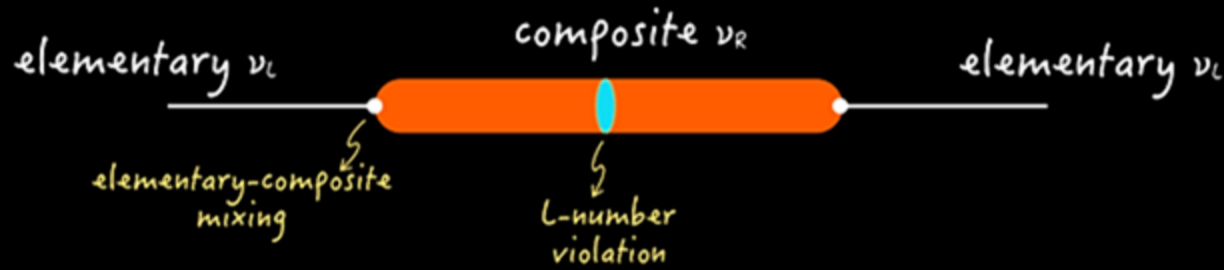
# Further motivating Inverse Seesaw

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$$L_{IR} \ni -m_N \bar{N} N - (\lambda \bar{L} \tilde{H} N_R + \mu N_L^2 + h.c.)$$

$$m_\nu \approx \mu \left( \frac{\lambda v_{EW}}{M_N} \right)^2$$

# Further motivating Inverse Seesaw



Chacko, Fox, ZL, Harnik, [2012.01443](#);

General CFT:

$$L_{UV} \supset L_{CFT} + \frac{\hat{\lambda}}{M^{\Delta-3/2}} \bar{L} \tilde{H} O_N + \frac{\hat{\mu}}{M^{\Delta_{2N}-4}} O_{2N}$$

CFT  
generates

CFT deformation  
generates

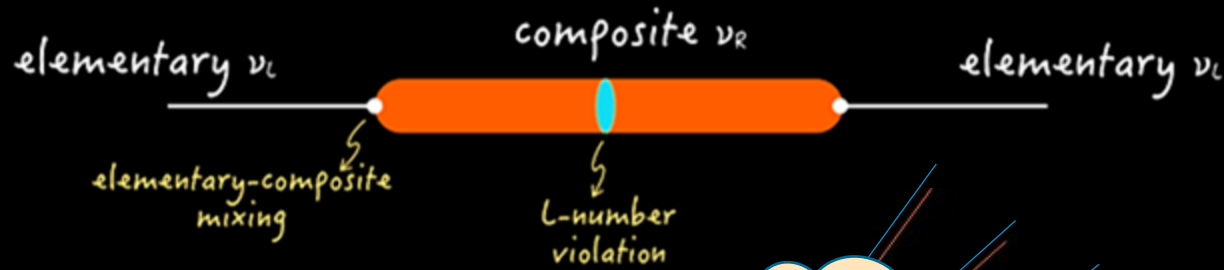
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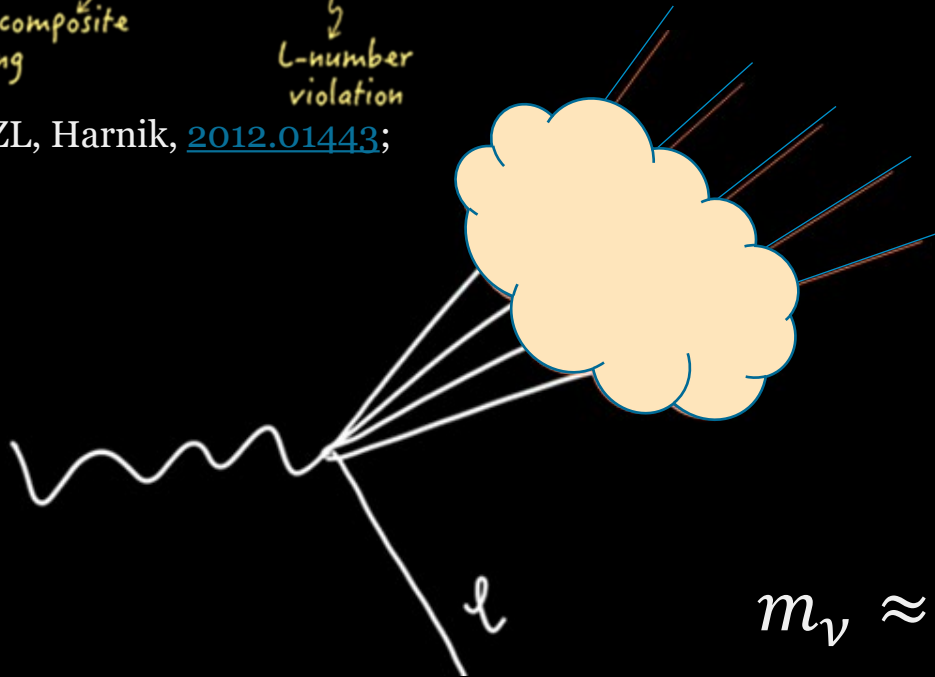
$$\Lambda \quad C_\lambda \hat{\lambda} \left( \frac{\Lambda}{M} \right)^{\Delta-\frac{3}{2}} \quad C_\mu \hat{\mu} \left( \frac{\Lambda}{M} \right)^{\Delta_{2N}-4}$$

Arkani-Hamed, Grossman, [hep-ph/9806223](#), Okui, [hep-ph/0405083](#), Grossman, Tsai, [0811.0871](#), Grossman, Robinson, [1009.2781](#), McDonald, [1010.2659](#), Robinson, Tsai, [1205.0569](#), [1404.7118](#)...

# Further motivating Inverse Seesaw



Chacko, Fox, ZL, Harnik, [2012.01443](#);



A shower of Sterile Neutrinos...  
Chacko, Dev, ZL, Sanket, in progress;

$$m_\nu \approx \mu \left( \frac{\lambda v_{EW}}{M_N} \right)^2$$

General CFT:

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CFT  
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Arkani-Hamed, Grossman, [hep-ph/9806223](#), Okui, [hep-ph/0405083](#), Grossman, Tsai, [0811.0871](#), Grossman, Robinson, [1009.2781](#), McDonald, [1010.2659](#), Robinson, Tsai, [1205.0569](#), [1404.7118](#)...

# Conclusion

- Muon Collider is a good platform to probe the TeV scale HNL.

We can open a new region in the parameter space.

- For the muon flavor case, we can probe the  $|U_\mu|^2$  down to  $10^{-7}$ .
- There are t-channel singularity cases one should be careful to deal with.
- Many more interesting pheno in the HNL sector.

