

# Experimental status of

$b \rightarrow s\ell^+\ell^-$  and  $b \rightarrow c\ell\nu$   
transitions

LHCP, June 2024



Massachusetts  
Institute of  
Technology

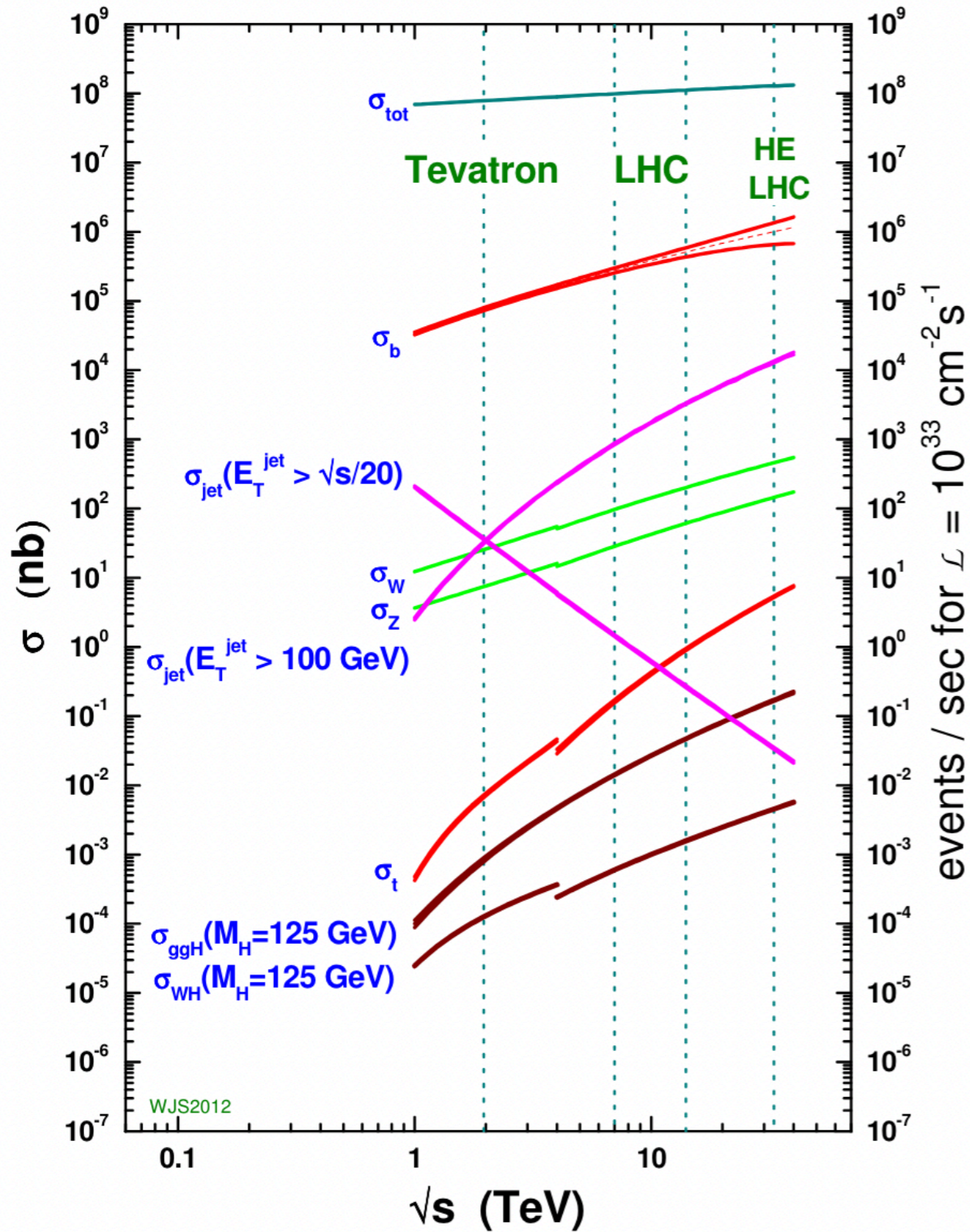
Eluned Smith

[eluned@mit.edu](mailto:eluned@mit.edu)

On behalf of the ATLAS, CMS  
and LHCb collaborations

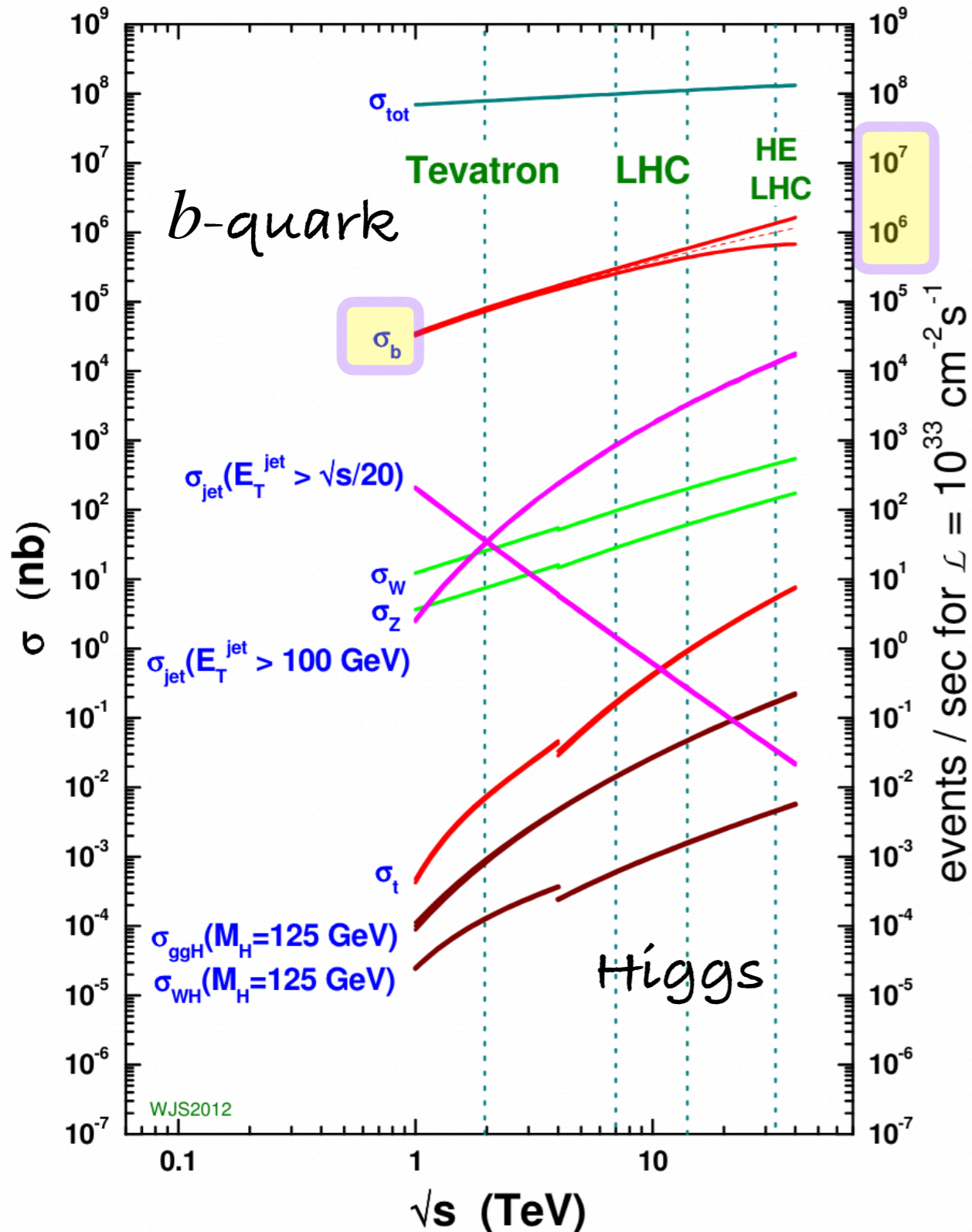
# $b$ -quarks at the LHC

proton - (anti)proton cross sections



# $b$ -quarks at the LHC

proton - (anti)proton cross sections

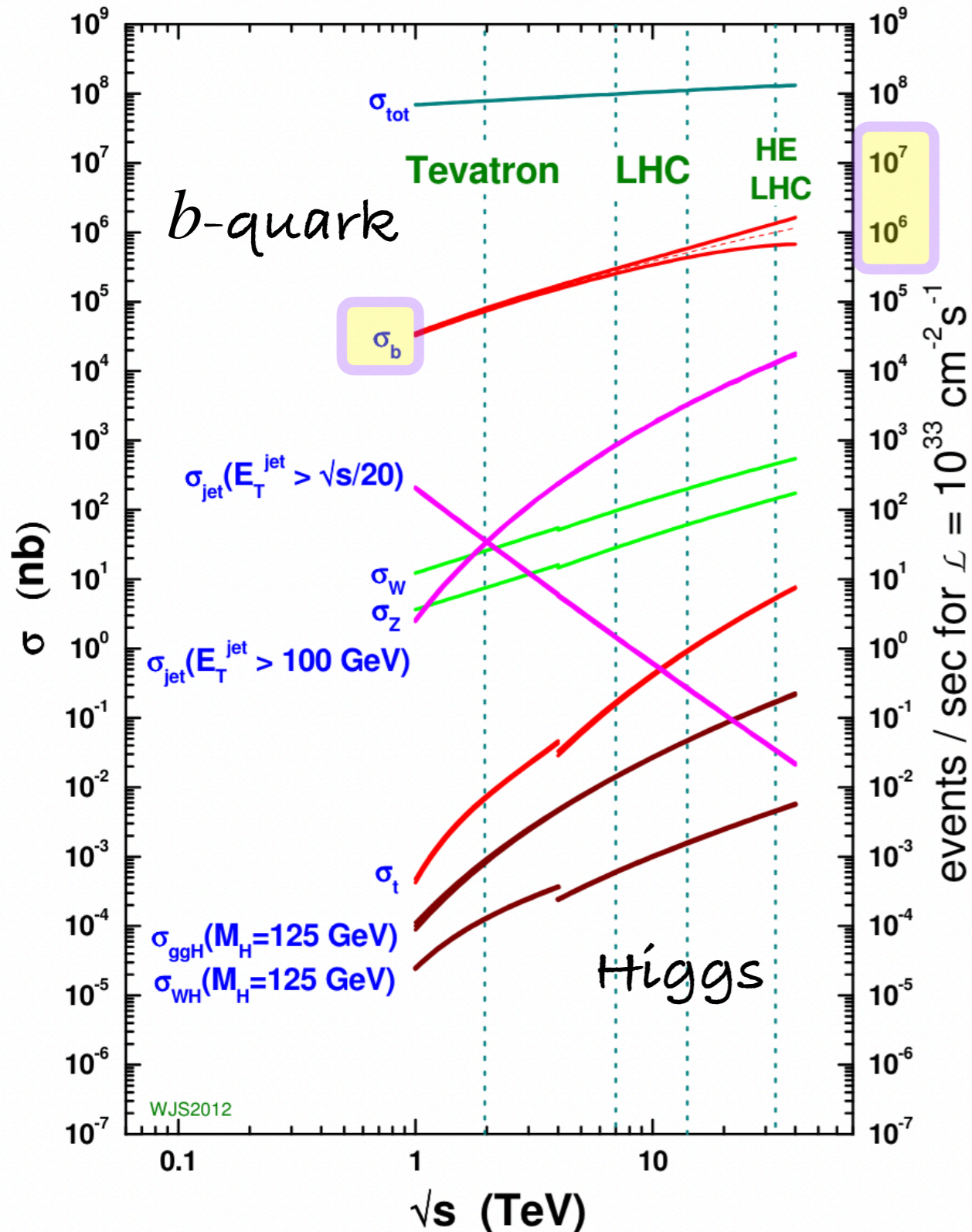


*We have a lot...*

- Cross-section  $\mathcal{O}(100) \mu b$
- Millions of  $b\bar{b}$  pairs produced per second

# $b$ -quarks at the LHC

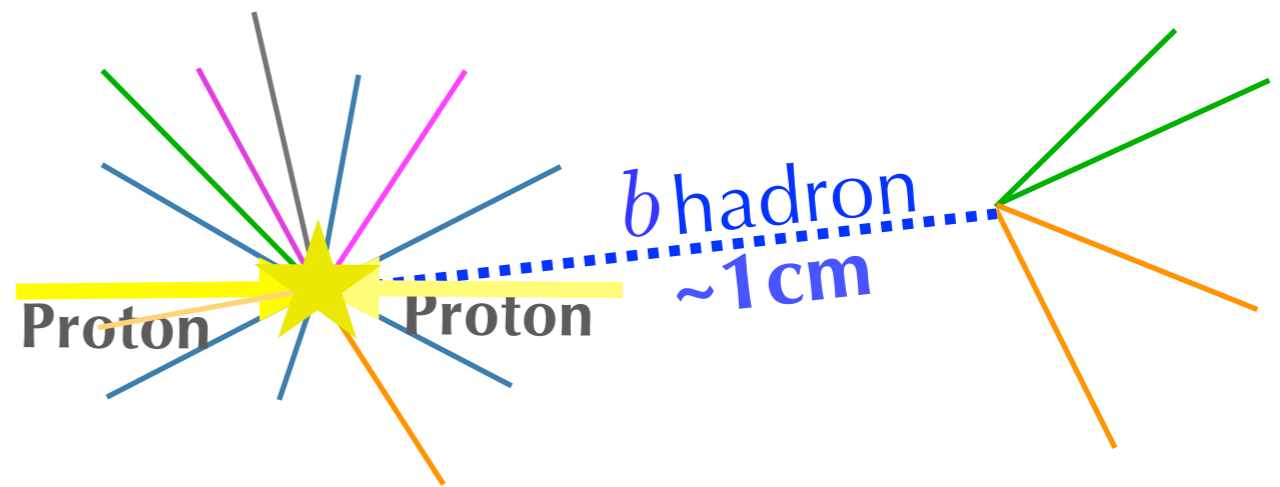
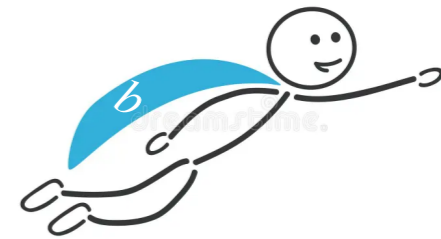
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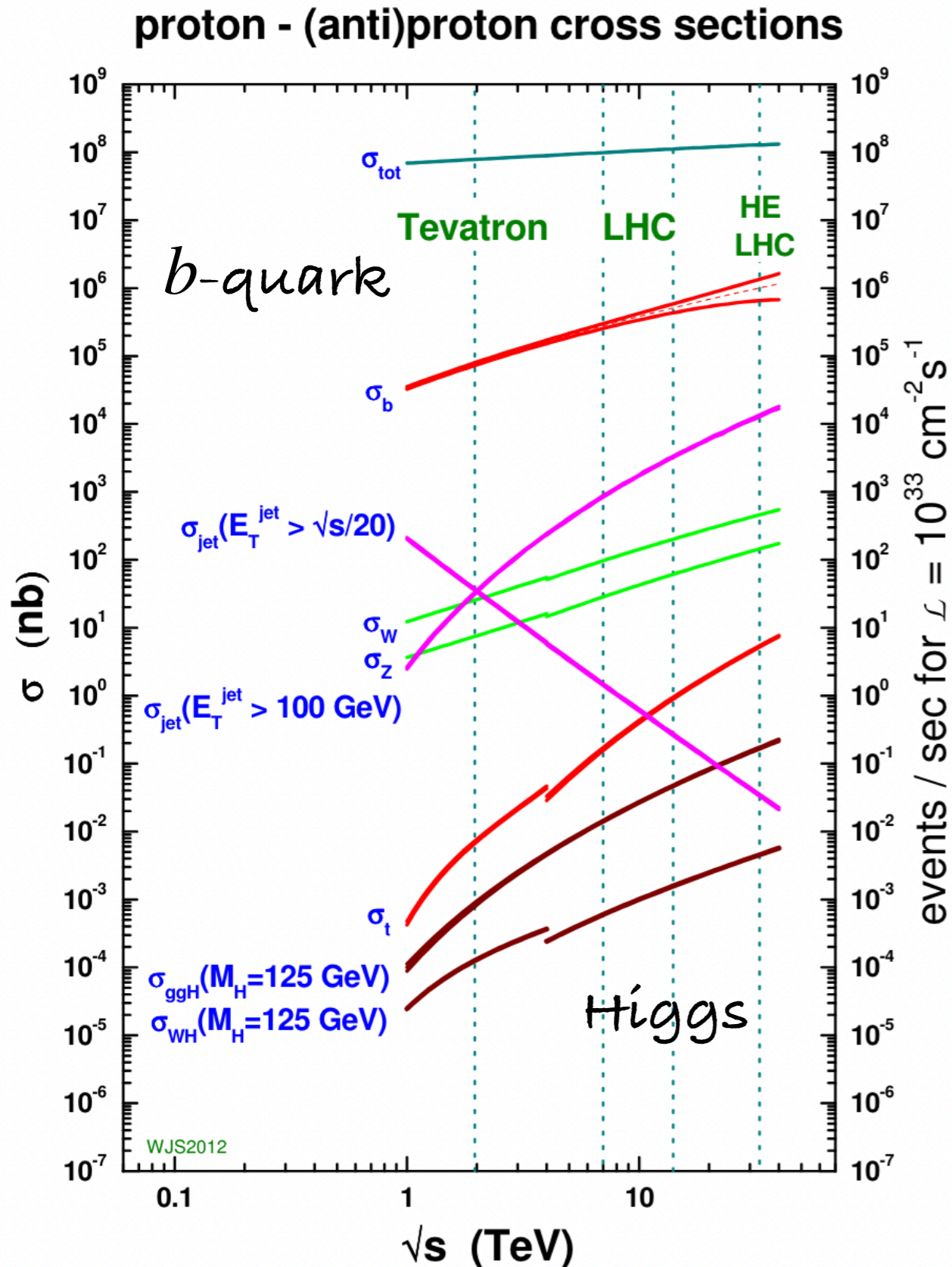
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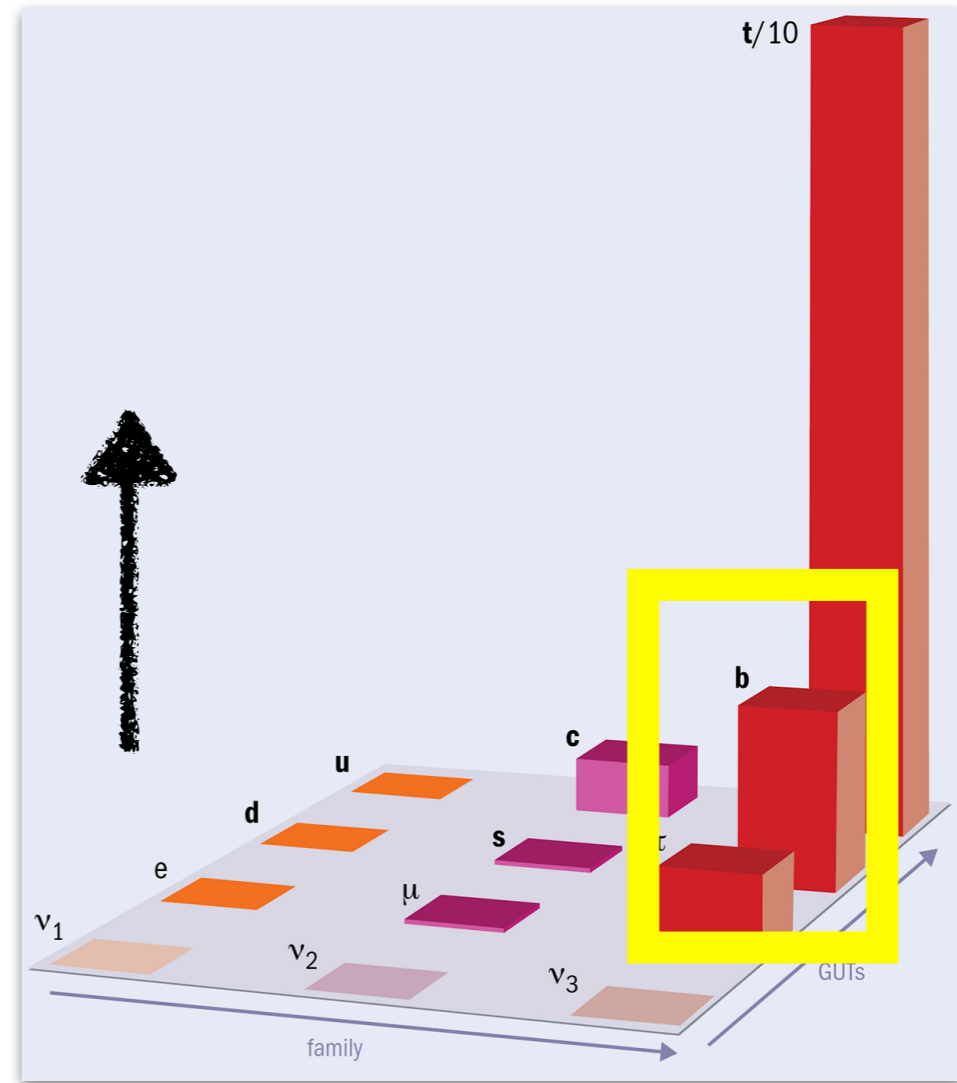
*And they fly...*



# $b$ -quarks at the LHC



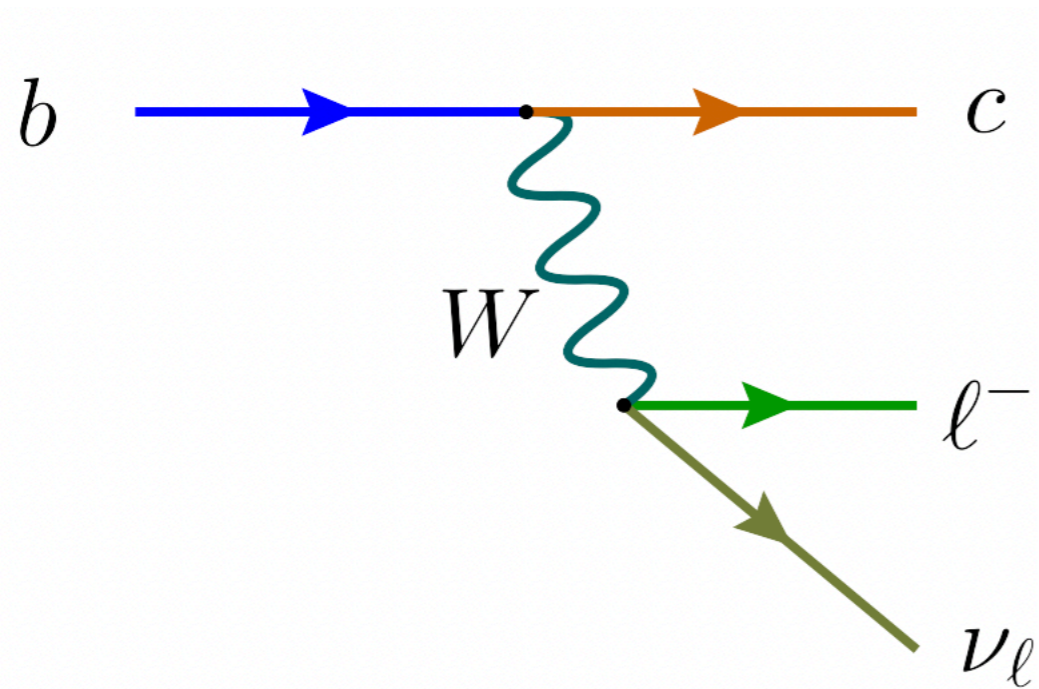
heaviest stable quark



3rd generation - sensitivity to BSM

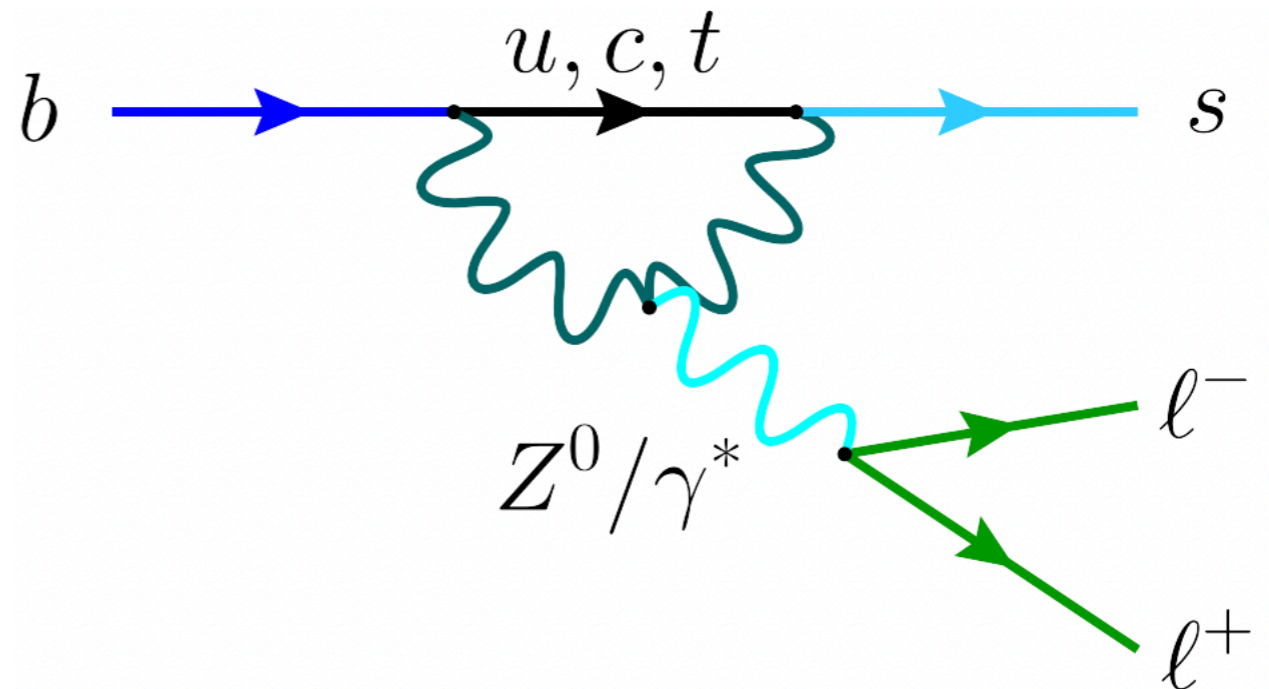
# Semi-leptonic $b$ quark decays

$$b \rightarrow c \ell \nu$$



**Charged current:**

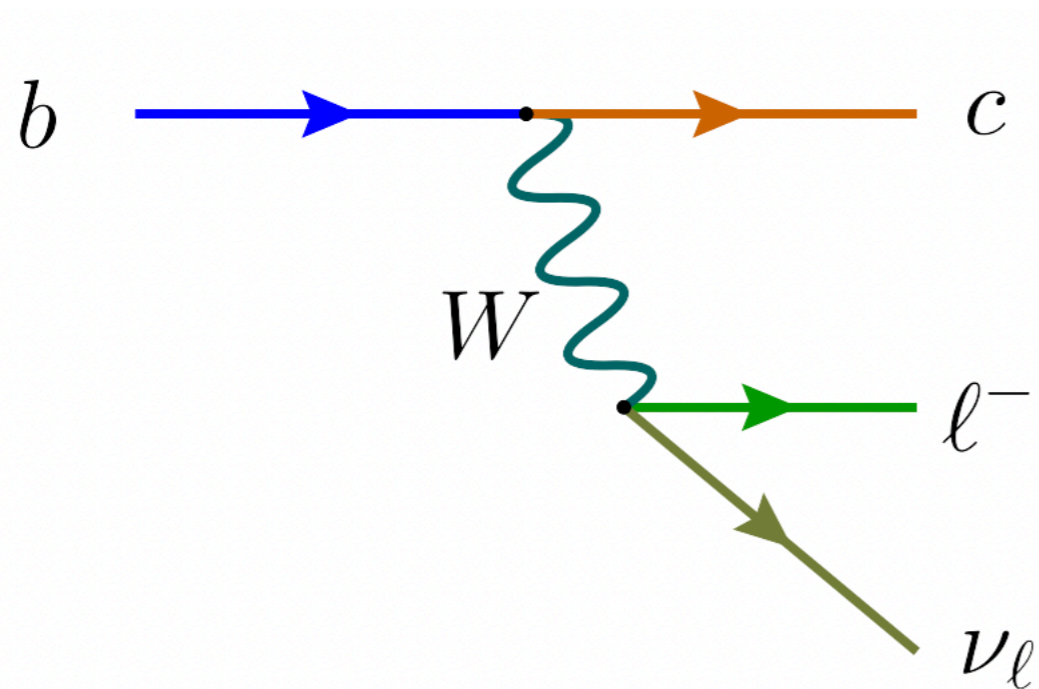
$$b \rightarrow s \ell \ell$$



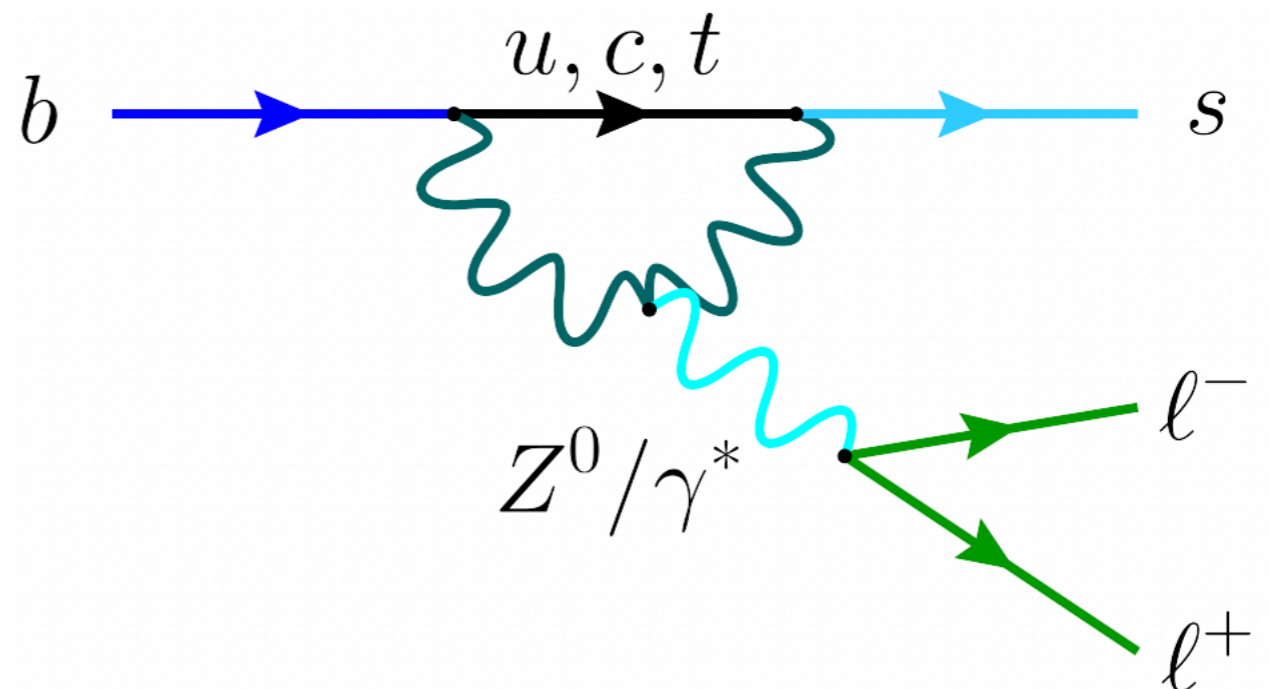
**Neutral current:**

# Semi-leptonic $b$ quark decays

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$$b \rightarrow s \ell \ell$$



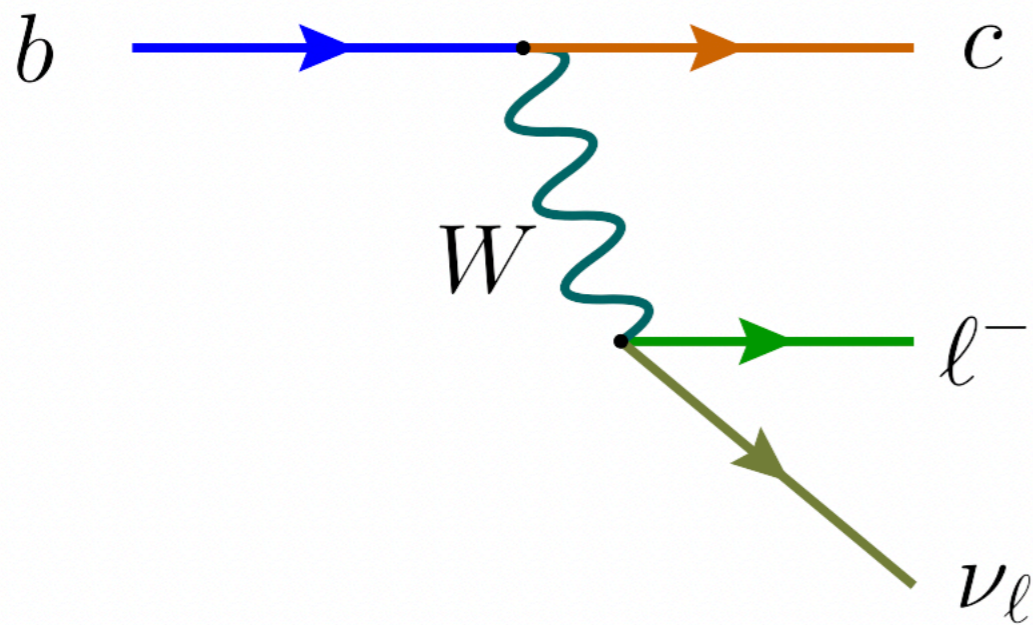
## Charged current:

- Tree-level
- $\mathcal{B}$  order %

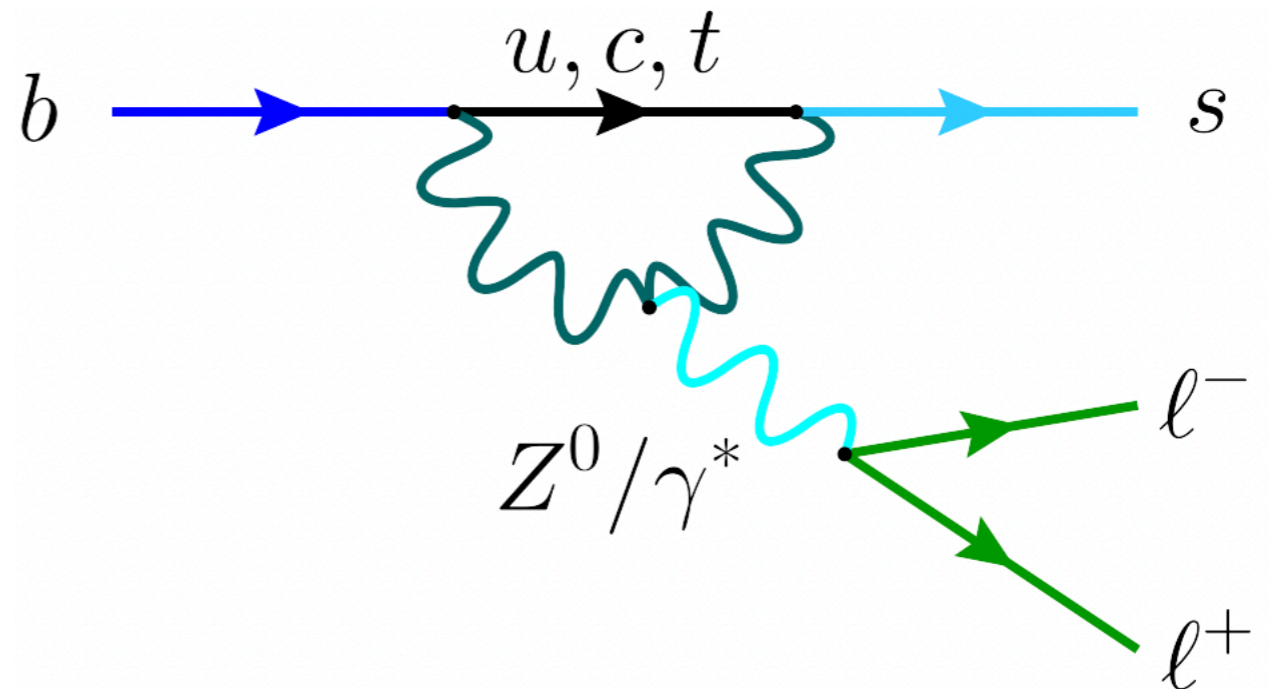
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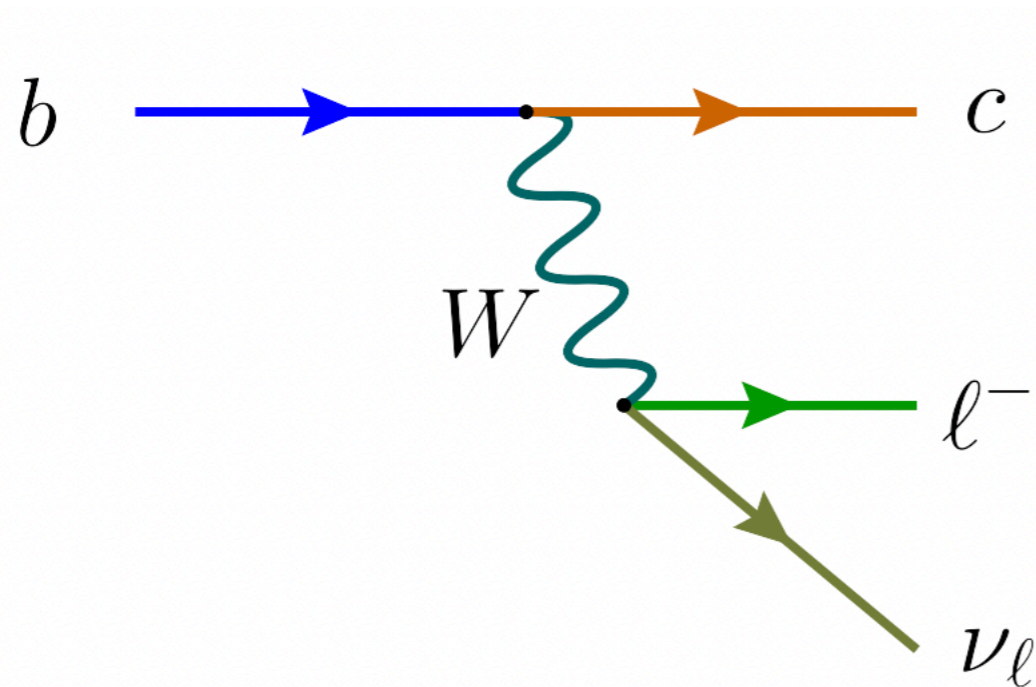
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- Neutrino in final state (invisible)

## Neutral current:

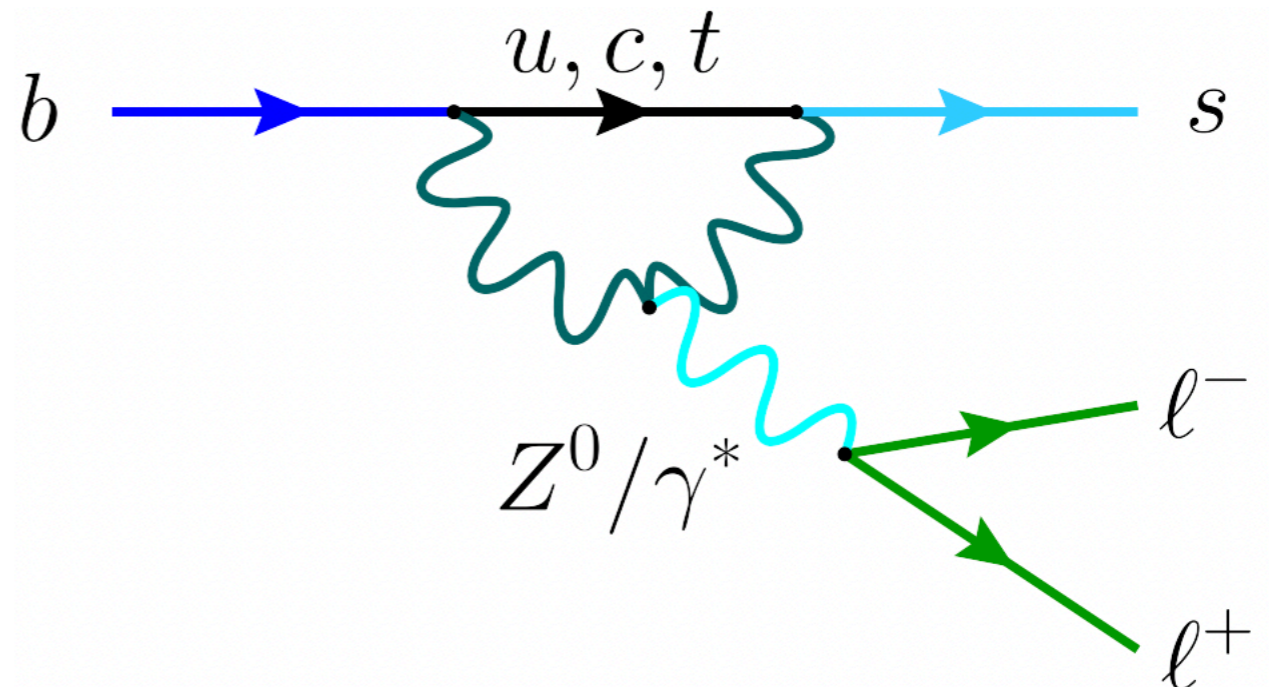


# Semi-leptonic $b$ quark decays

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$$b \rightarrow s \ell \ell$$



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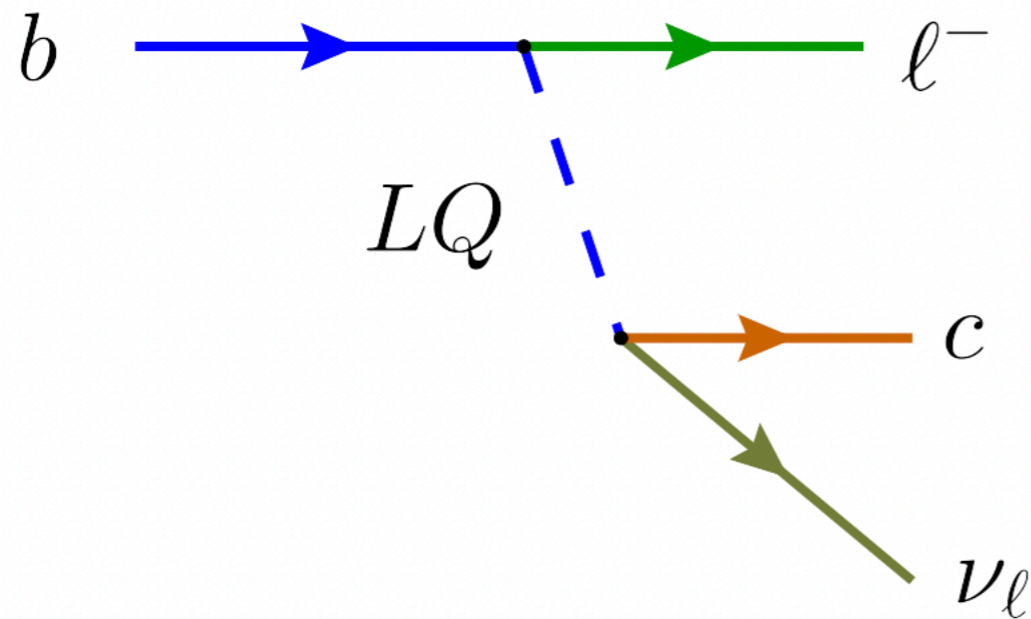
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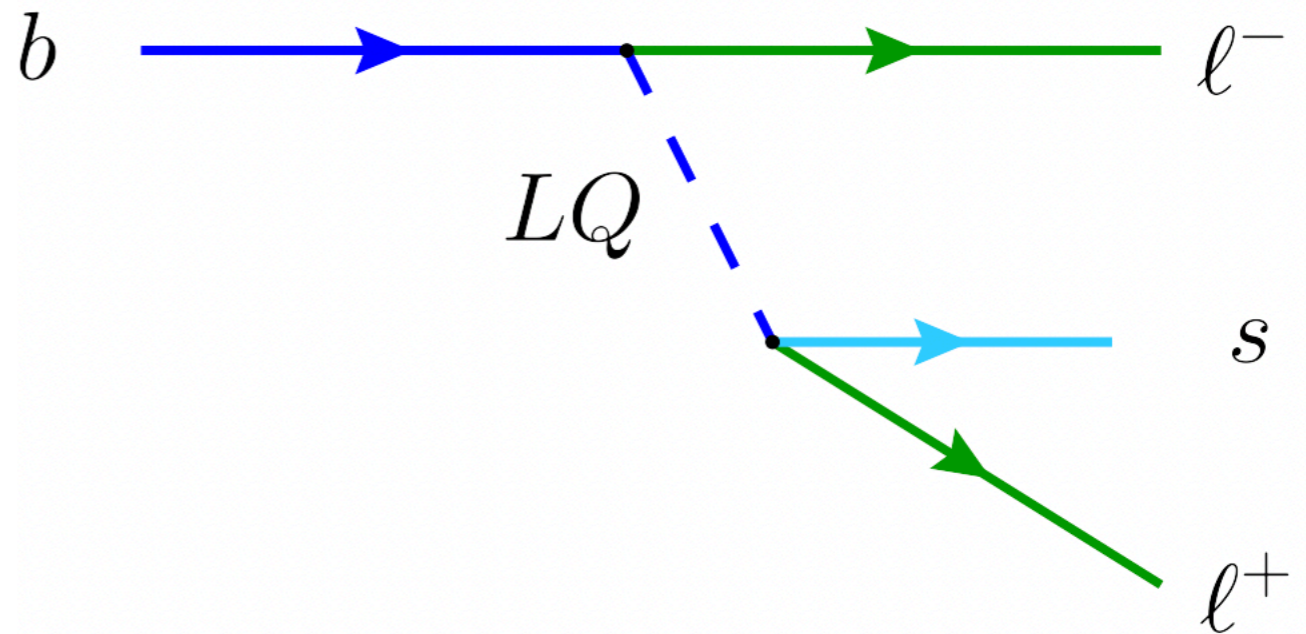
- Loop-suppressed:
  - $\mathcal{B}$  order  $10^{-7} - 10^{-9}$
- Full reconstructed final state

# Semi-leptonic $b$ quark decays

$$b \rightarrow c \ell \nu$$



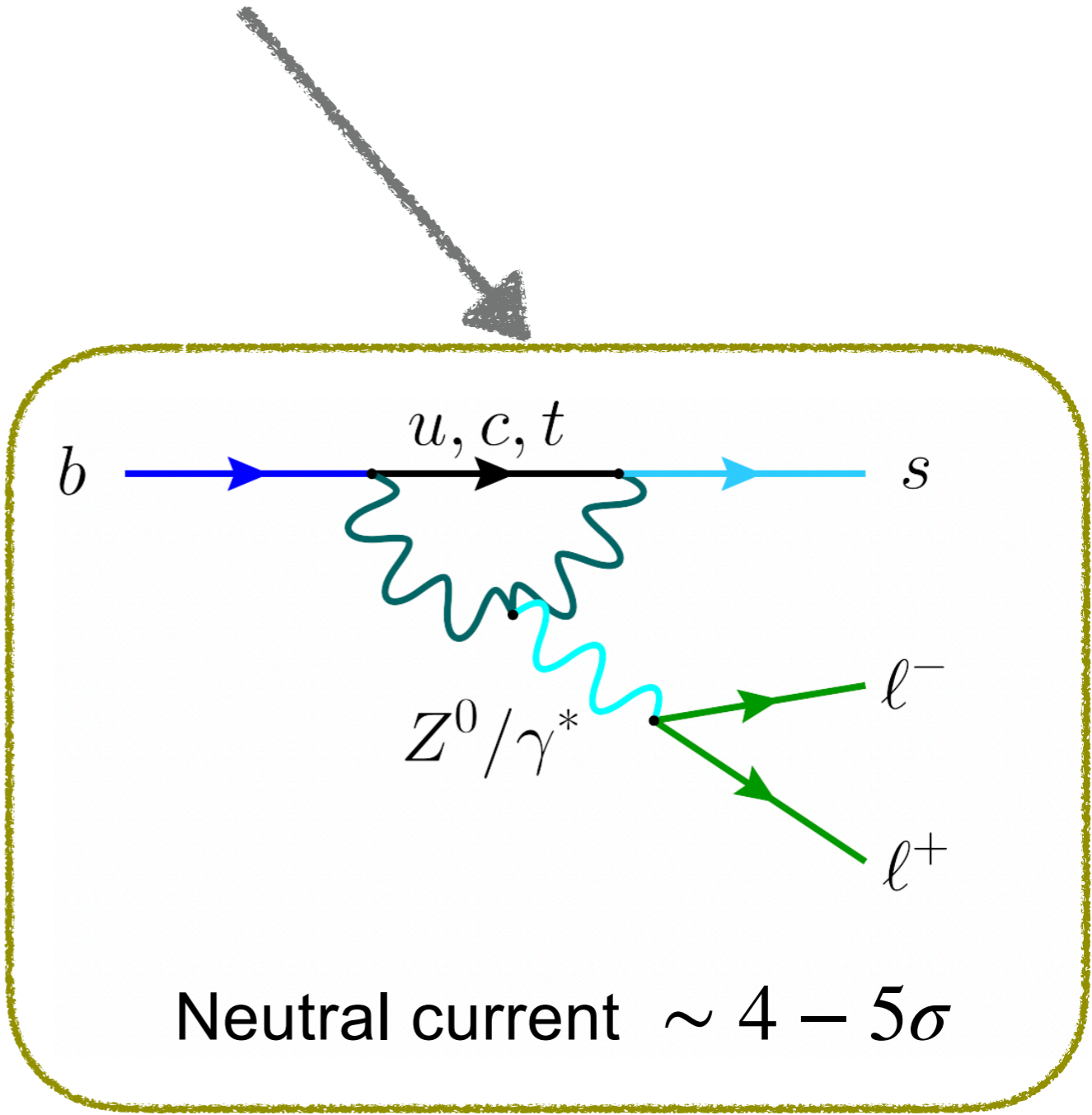
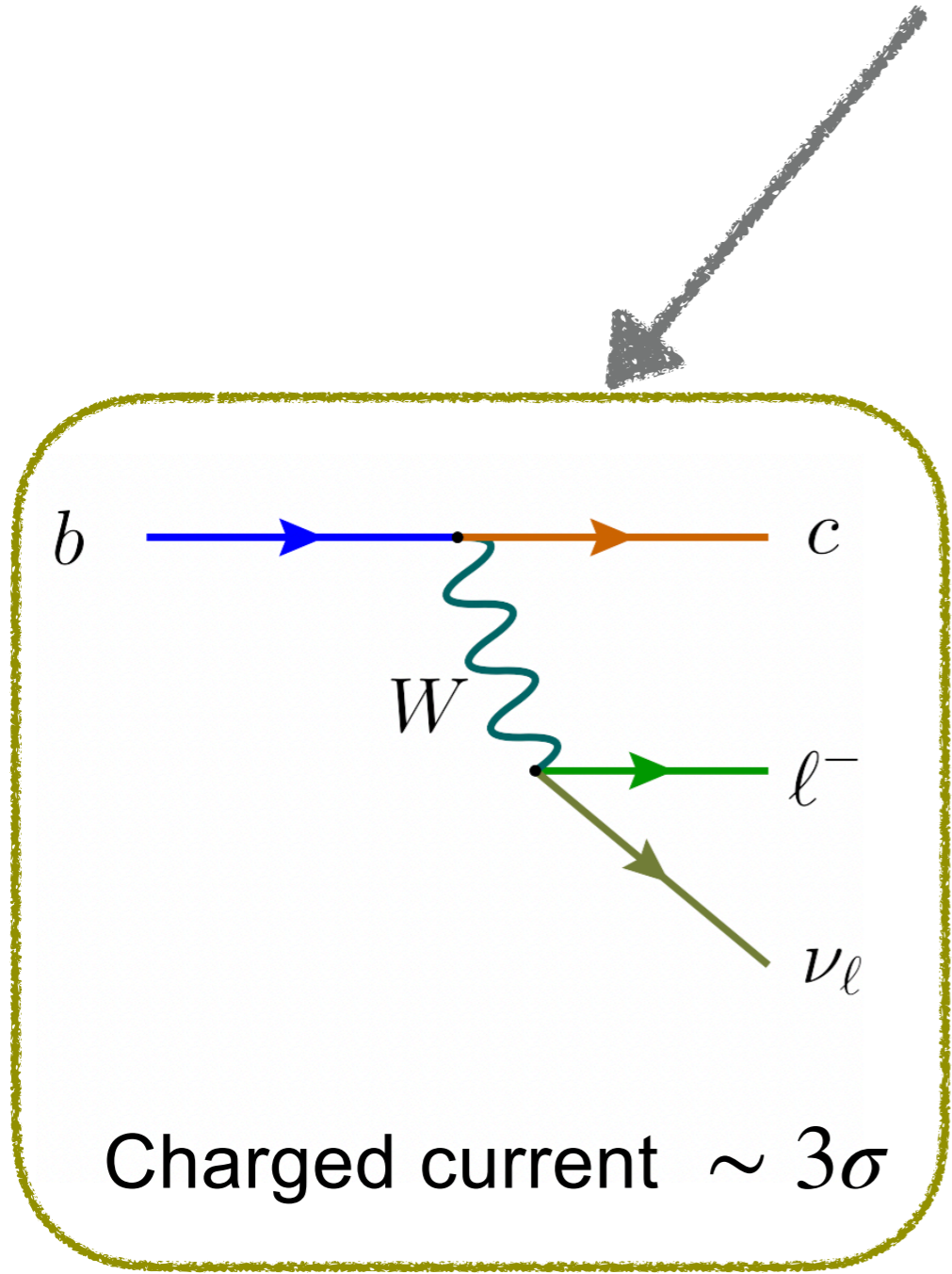
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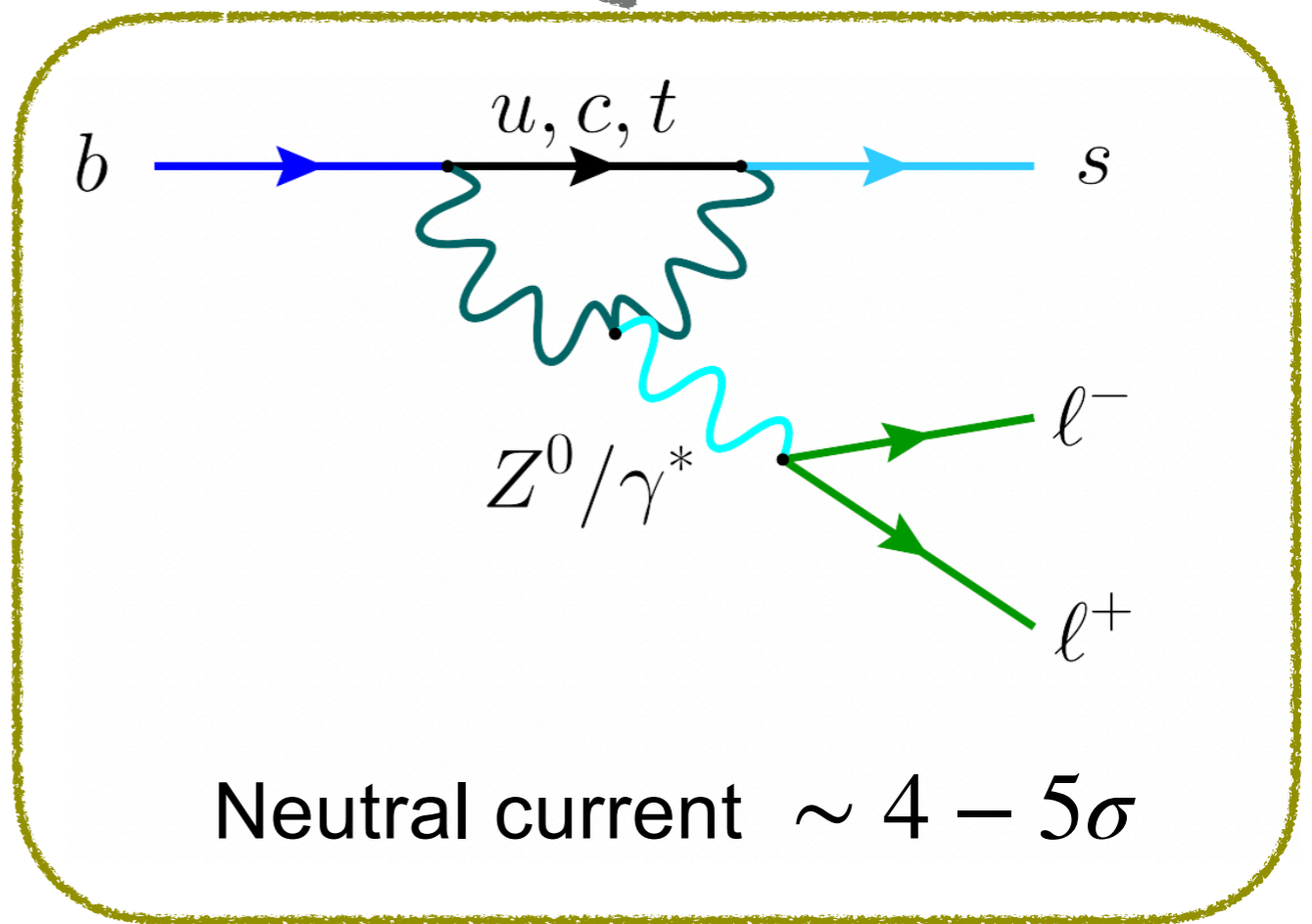
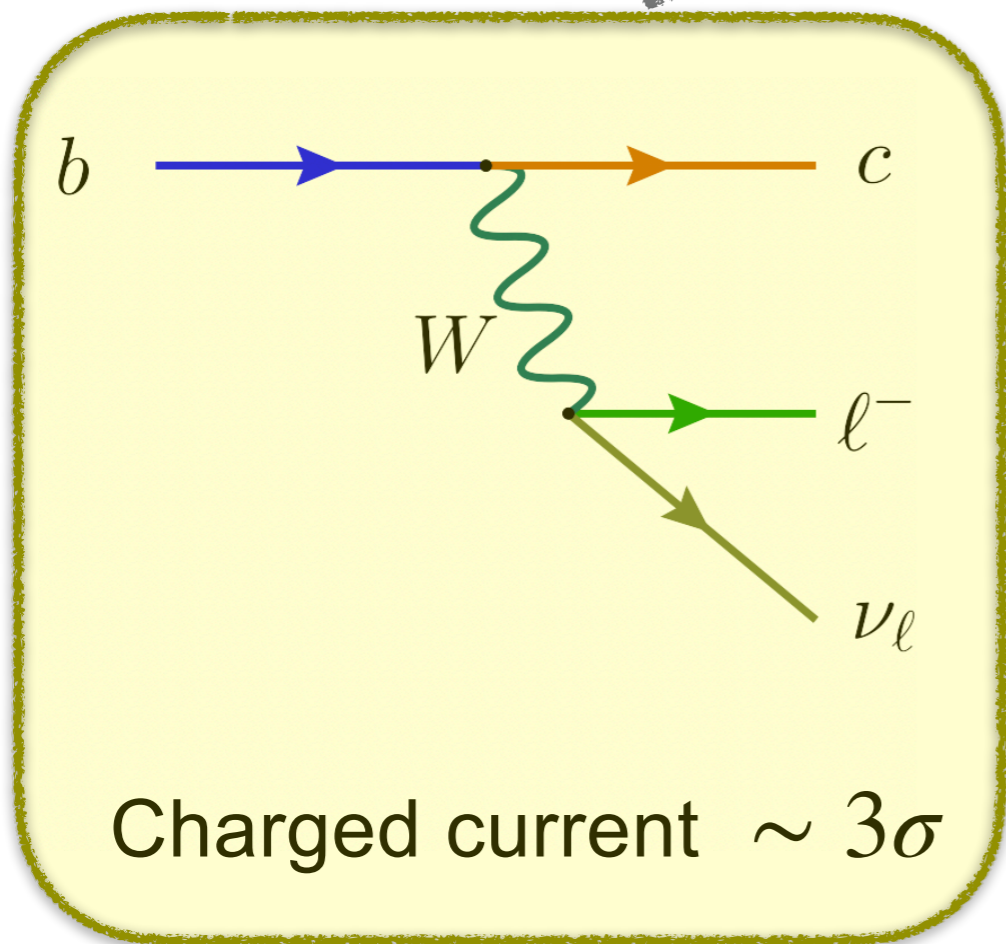
Heisenberg's uncertainty principle:

- New physics (NP) particles with mass  $> \text{TeV}$  can distort measured decay rates
- For example the Leptoquark (LQ)

# The B-anomalies



# The B-anomalies



# Charged current anomalies

$$R(D^{(*,+)} ) = \frac{\mathcal{B}(B^{(+)} \rightarrow D^{(*,+)} \tau \nu_\tau)}{\mathcal{B}(B^{(+)} \rightarrow D^{(*,+)} \ell \nu_\ell)}$$

$\ell \in \mu, e$ , (LHCb only  $\mu$ )

## Isospin

$$R(D^0) = R(D^+)$$

$$R(D^{*0}) = R(D^{*+})$$

## Hadronic

$$\tau \rightarrow \nu_\tau \pi X$$

## Semi-leptonic (SL)

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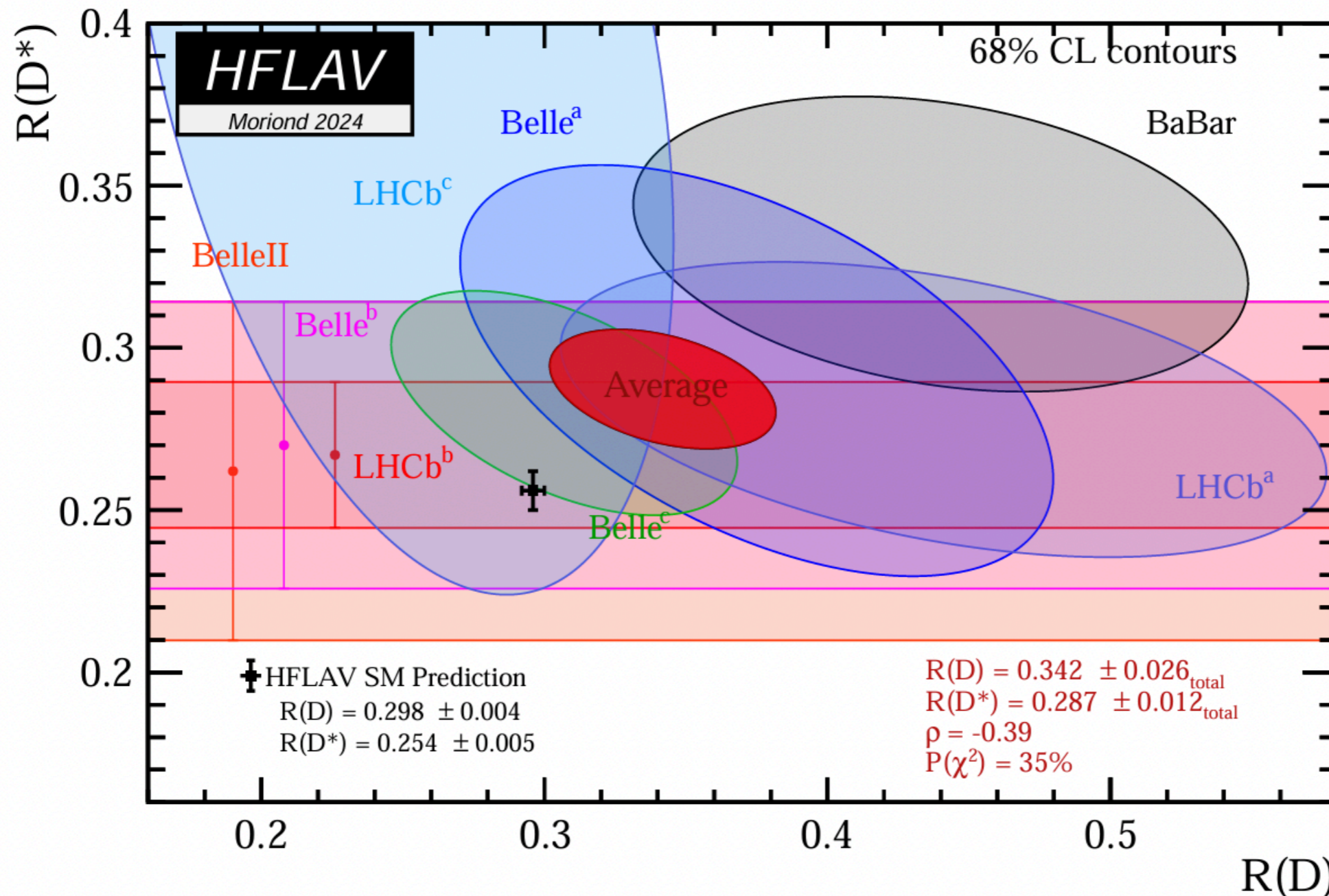
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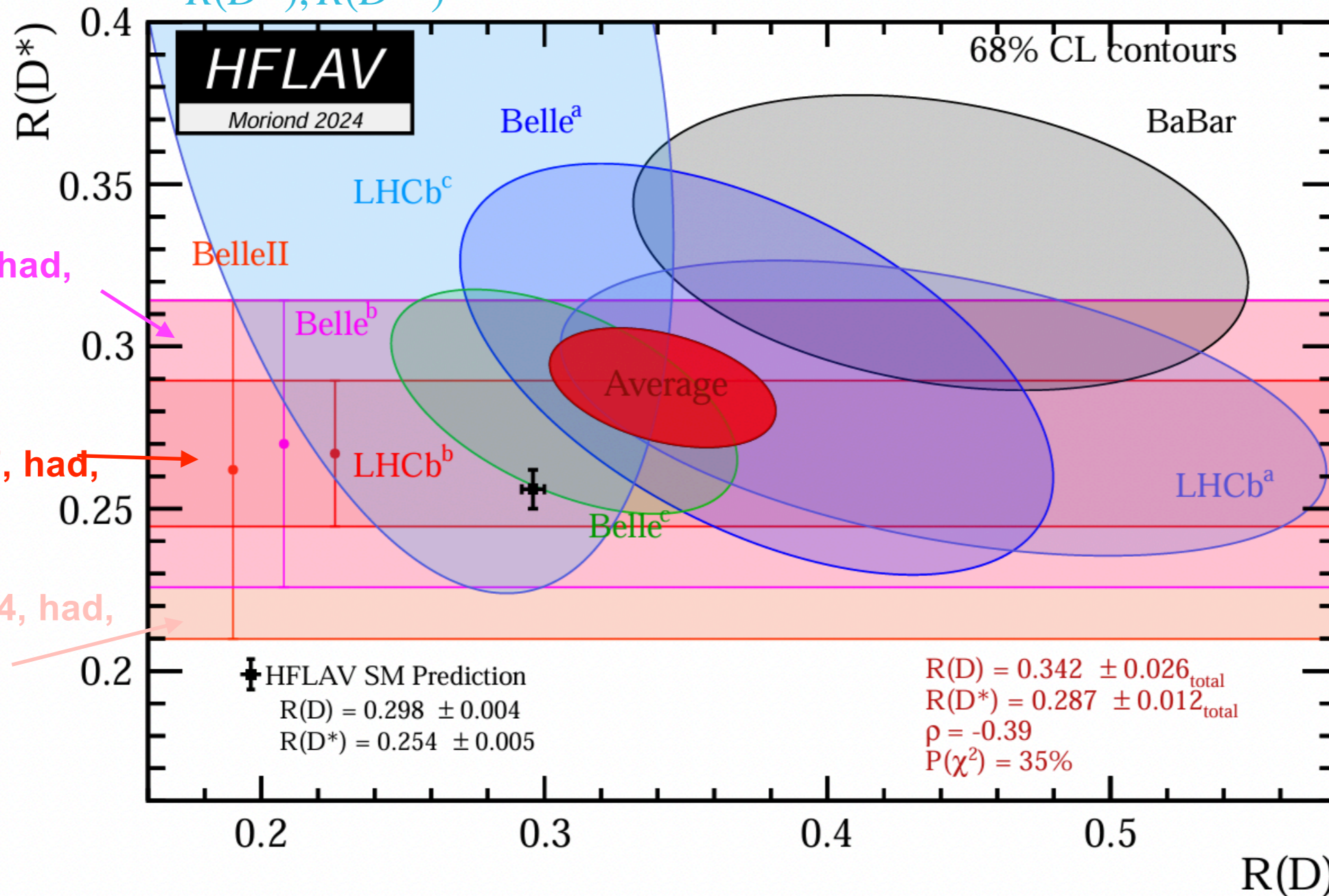
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LHCb 2024, SL,  
 $R(D^+), R(D^{*+})$   $D^{*(+)} \rightarrow D^+(\rightarrow K^- \pi^+ \pi^+) \pi^0$



Belle 2017 had,  
 $R(D^{*+})$

LHCb 2017, had,  
 $R(D^{*+})$

Belle II 2024, had,  
 $R(D^*)$

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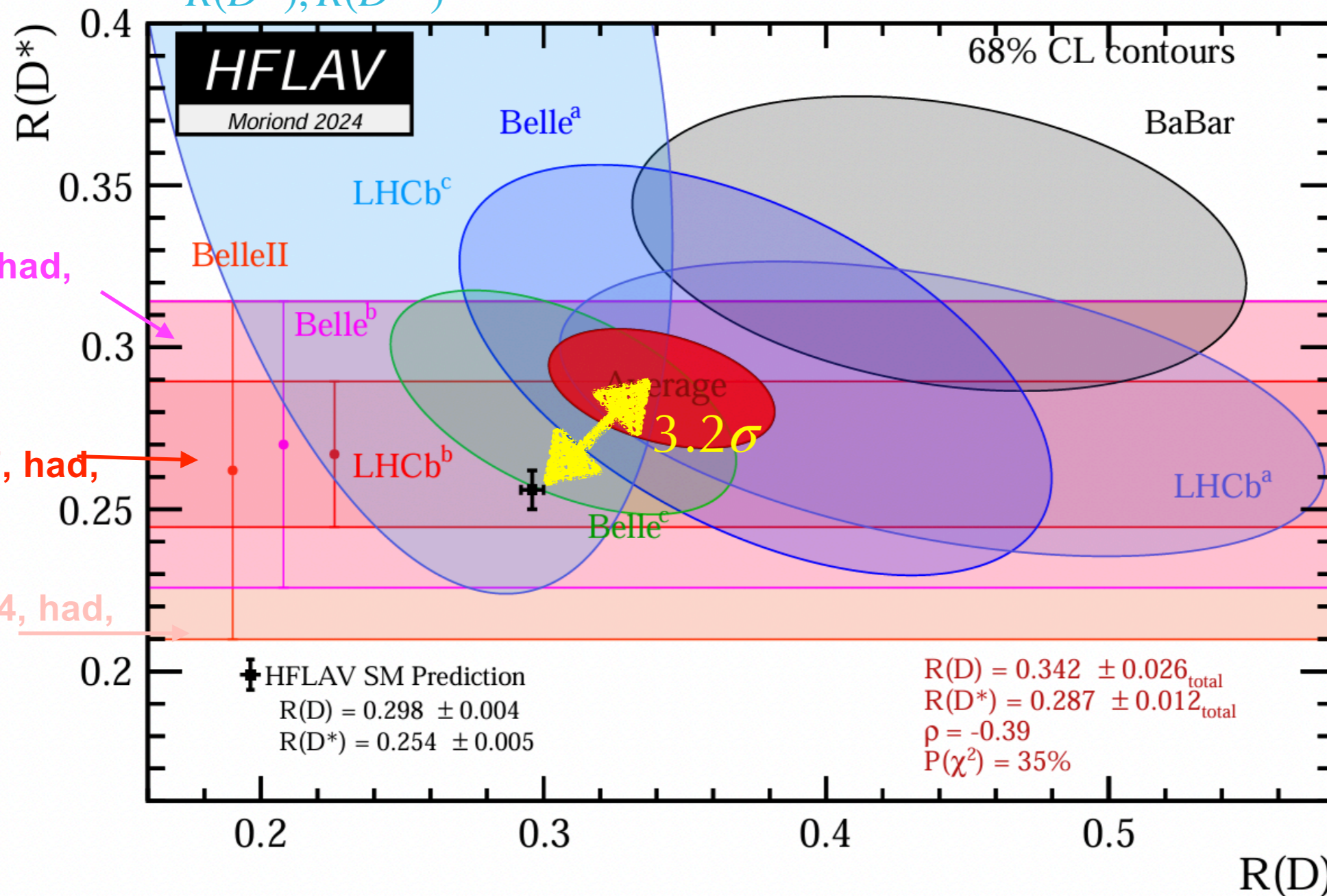
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LHCb  
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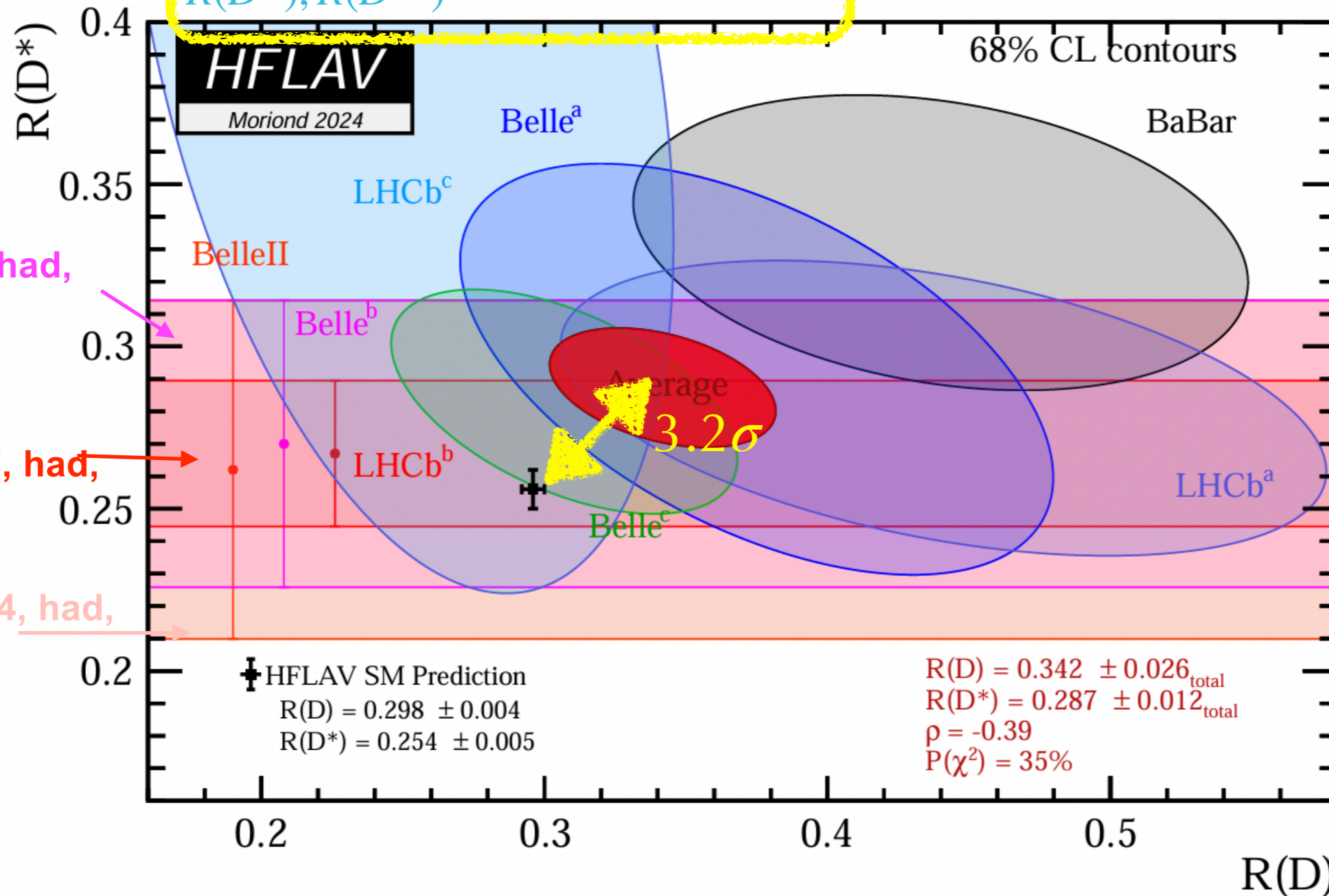
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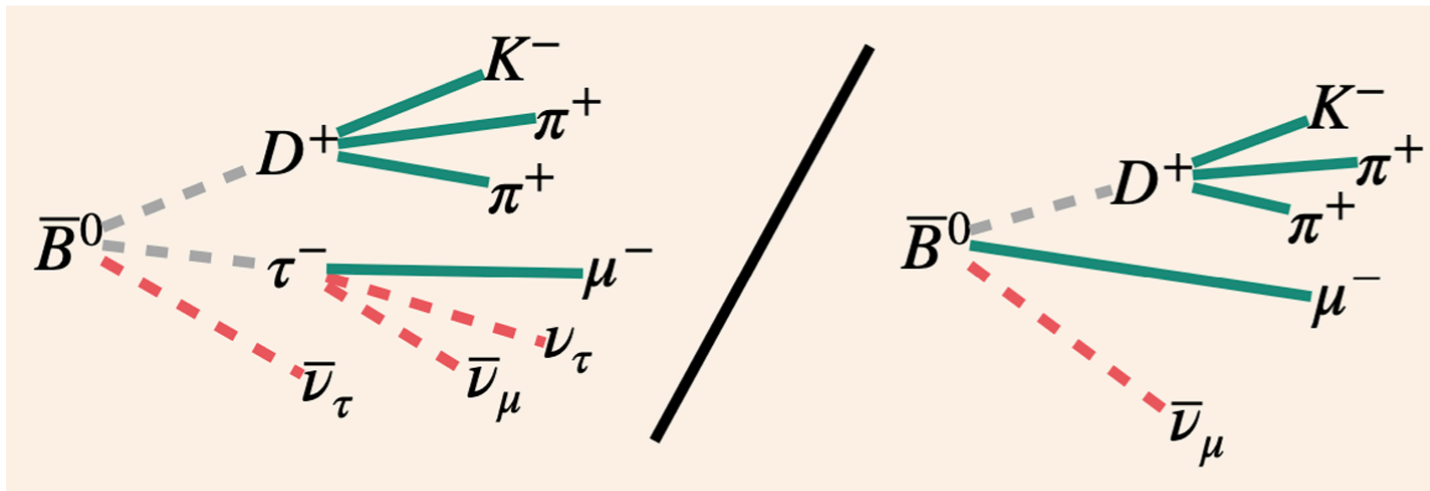
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 $R(D^+), R(D^{*+})$   $D^{*(+)} \rightarrow D^+(\rightarrow K^- \pi^+ \pi^+) \pi^0$



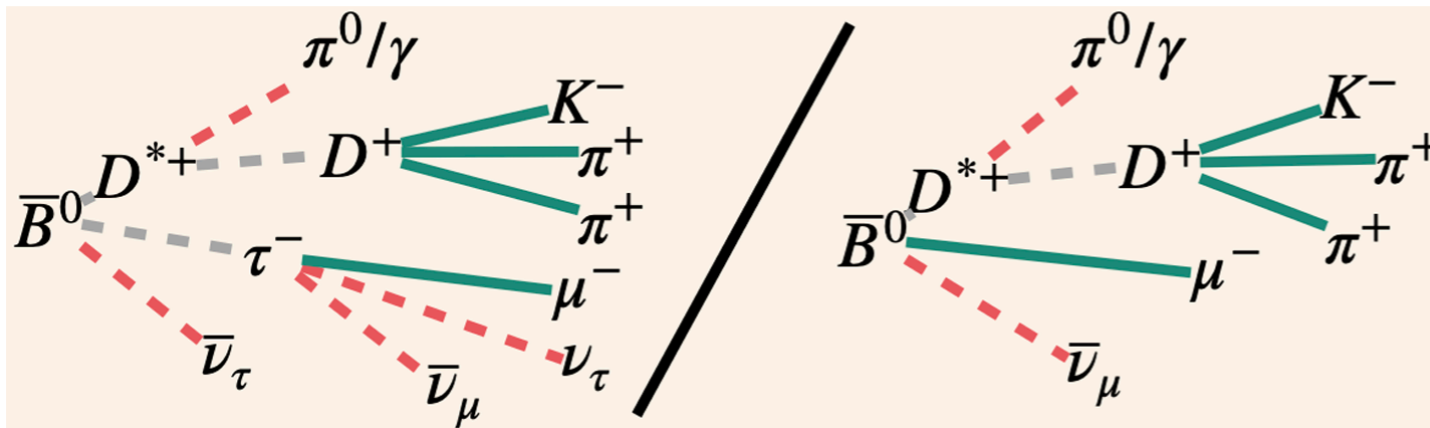
LHCb  
 2023, SL  
 $R(D^0), R(D^{*(+)})$   
 $D^{*(+)} \rightarrow D^0 X$

# Measurement of $R(D^{*+})$ and $R(D^+)$ at LHCb

$$R(D^+) =$$



$$R(D^{*+}) =$$



Reconstruct only  $D^+(\rightarrow K^- \pi^+ \pi^+)$  and  $\mu^-$

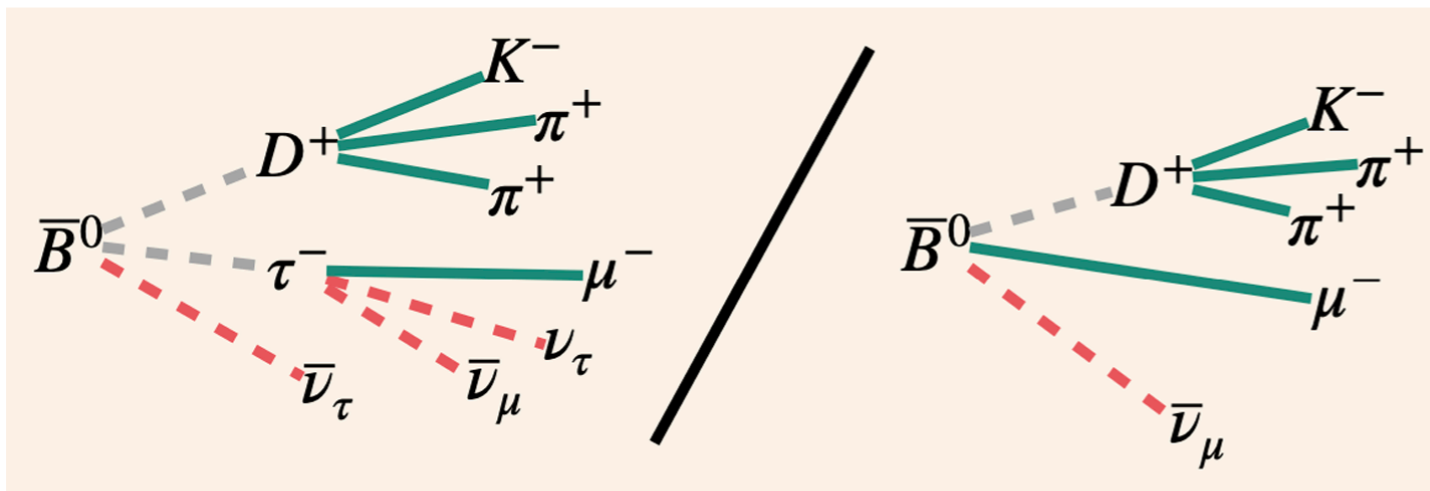
Simulation

Fits to data

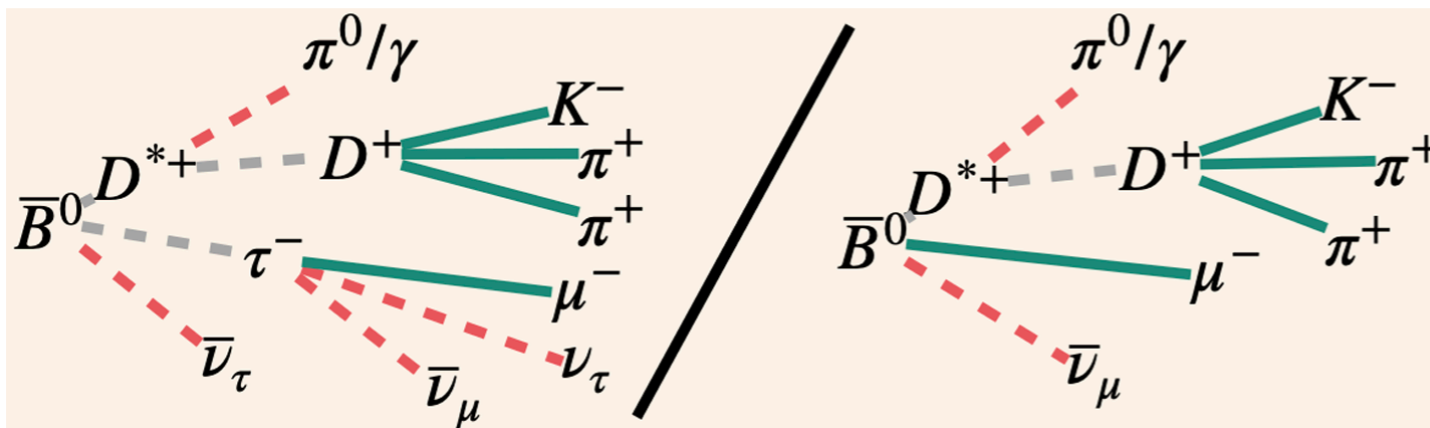
$$R(D^{(*)+}) = \frac{\epsilon_\mu^{D^{(*)+}} N_\tau^{D^{(*)+}}}{\epsilon_\tau^{D^{(*)+}} N_\mu^{D^{(*)+}}} \frac{1}{\mathcal{B}(\tau^- \rightarrow \mu^- \nu_\tau)}$$

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*Simulation*

*Fits to data*

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Perform simultaneous fit to **3 kinematic variables** across **4 samples** to constrain background

*Samples defined by candidate isolation*

- only  $D^+\mu^-$ ? Signal
- $D^+\mu^-\pi^-$ ?  $B \rightarrow D^{**}\ell^-\nu_\ell$
- $D^+\mu^-\pi^-\pi^+$ ?  $B \rightarrow D^{**}\ell^-\nu_\ell$
- $D^+\pi^-K^+$ ?  $B \rightarrow D^+H_cX$

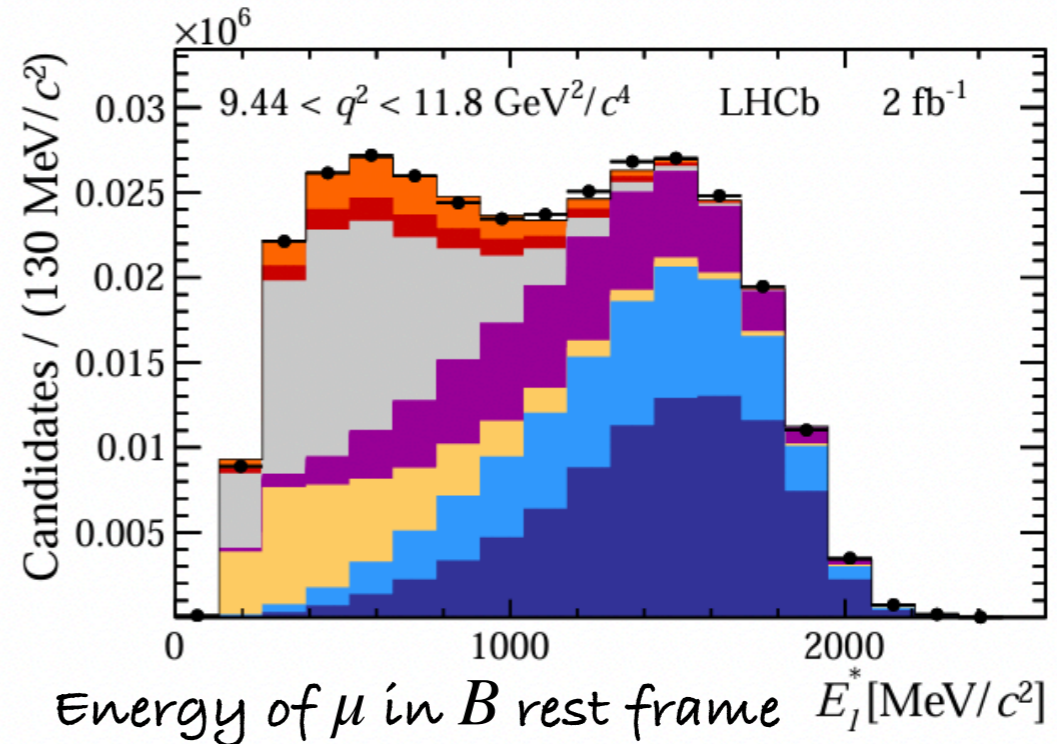
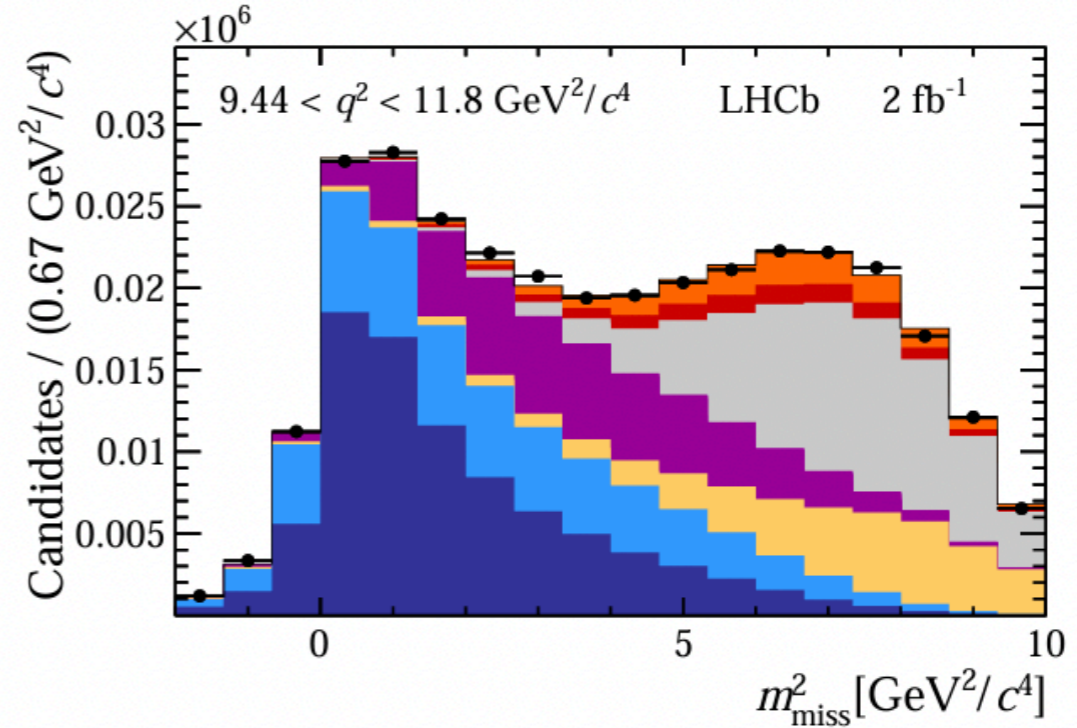
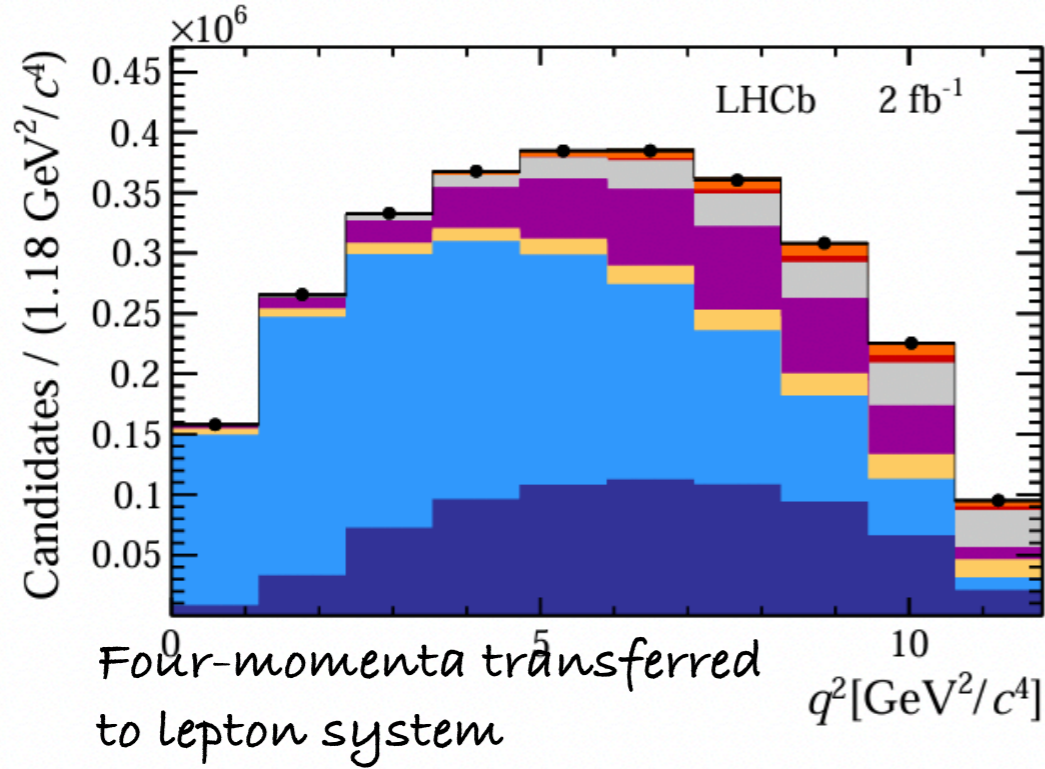
**Form-factors** dictate **shape** of signal and yields

- Use BGL parameterisation  
Phys.Rev.D 56 (1997) 6895-6911
- Float in fit, with constrains from lattice predictions

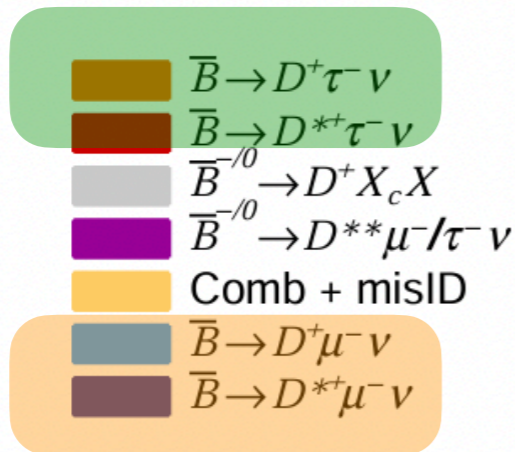
# Measurement of $R(D^{*\,+})$ and $R(D^+)$ at LHCb

LHCb-PAPER-2024-007

## Fits for signal-sample



Signal



Norm.

# Measurement of $R(D^{*+})$ and $R(D^+)$ at LHCb

LHCb-PAPER-2024-007

$$\begin{aligned} R(D^+) &= 0.249 \pm 0.043(\text{stat}) \pm 0.047(\text{syst}) \\ R(D^*) &= 0.402 \pm 0.081(\text{stat}) \pm 0.085(\text{syst}) \end{aligned} \quad \rho = -0.39$$

## Systematics-led analysis

Source	$\mathcal{R}(D^+)$	$\mathcal{R}(D^{*+})$
Form factors	0.023	0.035
$B \rightarrow D^{**}[D^+ X]\mu/\tau\nu$ fractions	0.024	0.025
$B \rightarrow D^+ X_c X$ fractions	0.020	0.034
Misidentification	0.019	0.012
Simulation size	0.009	0.030
Combinatorial background	0.005	0.020
Data/simulation agreement	0.016	0.011
Muon identification	0.008	0.027
Multiple candidates	0.007	0.017
Total systematic uncertainty	0.047	0.086

## Main systematics:

- Background modelling/branching fractions
- Form factor parameterisation

# Measurement of $R(D^{*+})$ and $R(D^+)$ at LHCb

LHCb-PAPER-2024-007

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## Systematics-dominated analysis

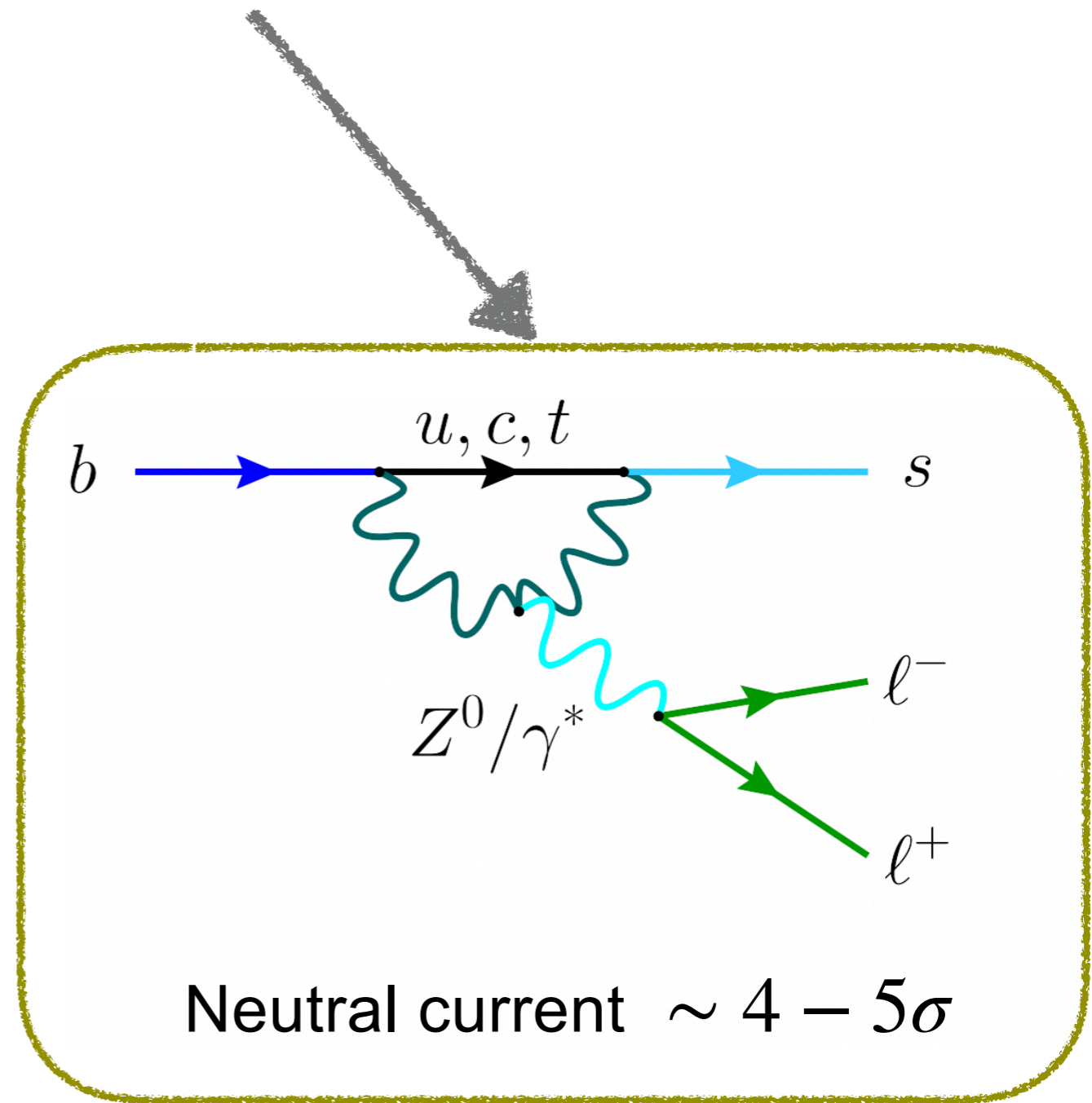
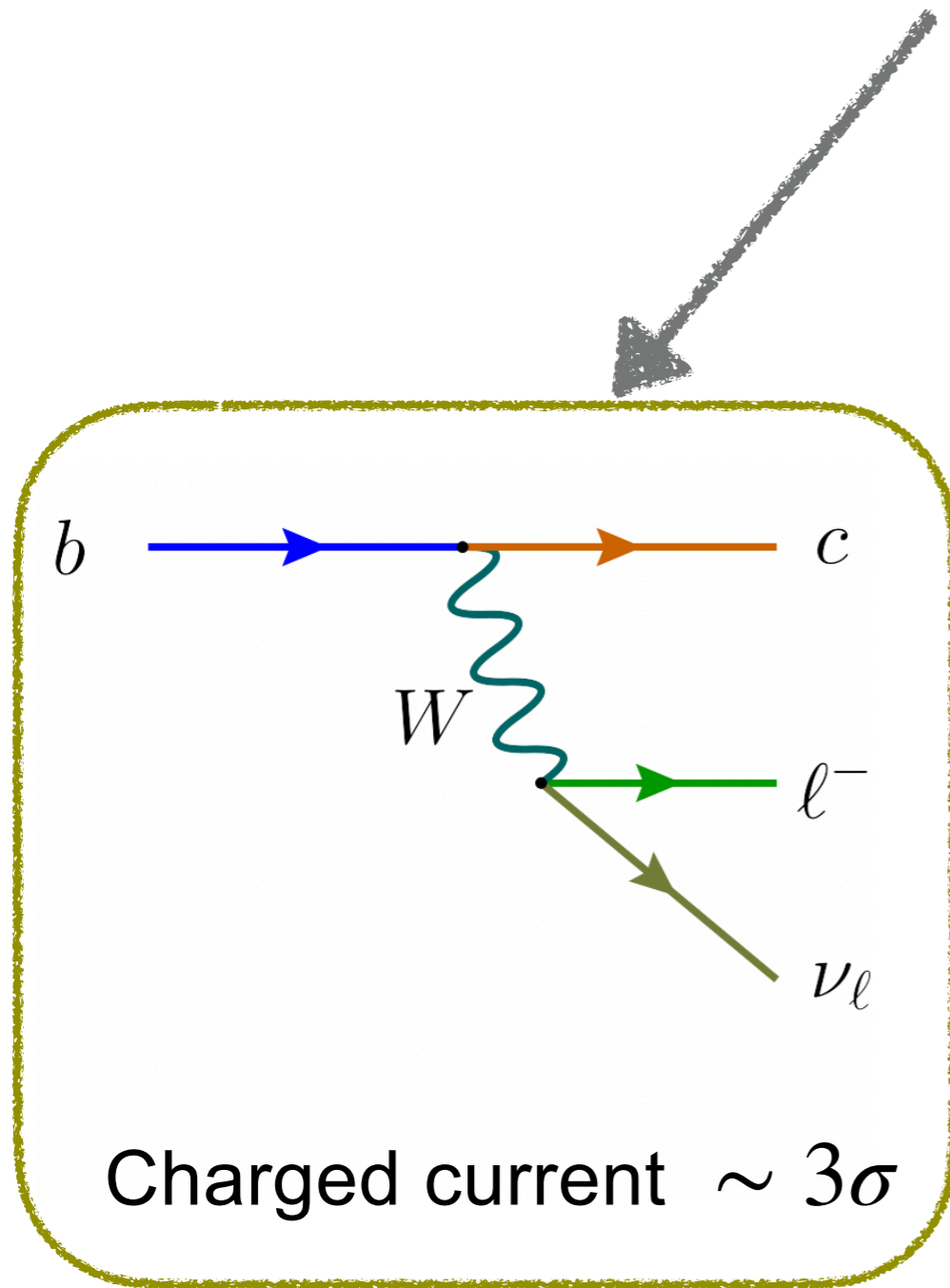
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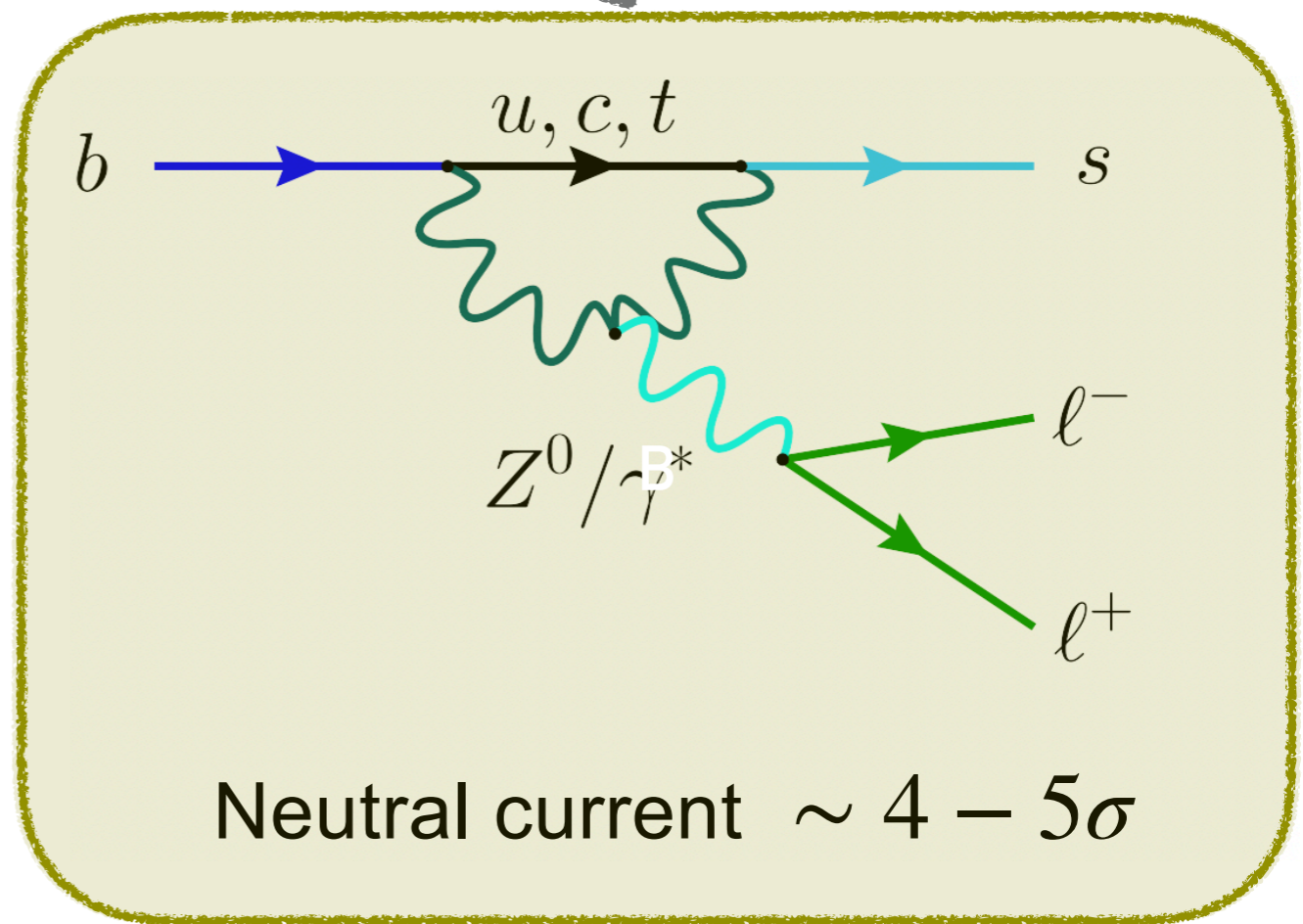
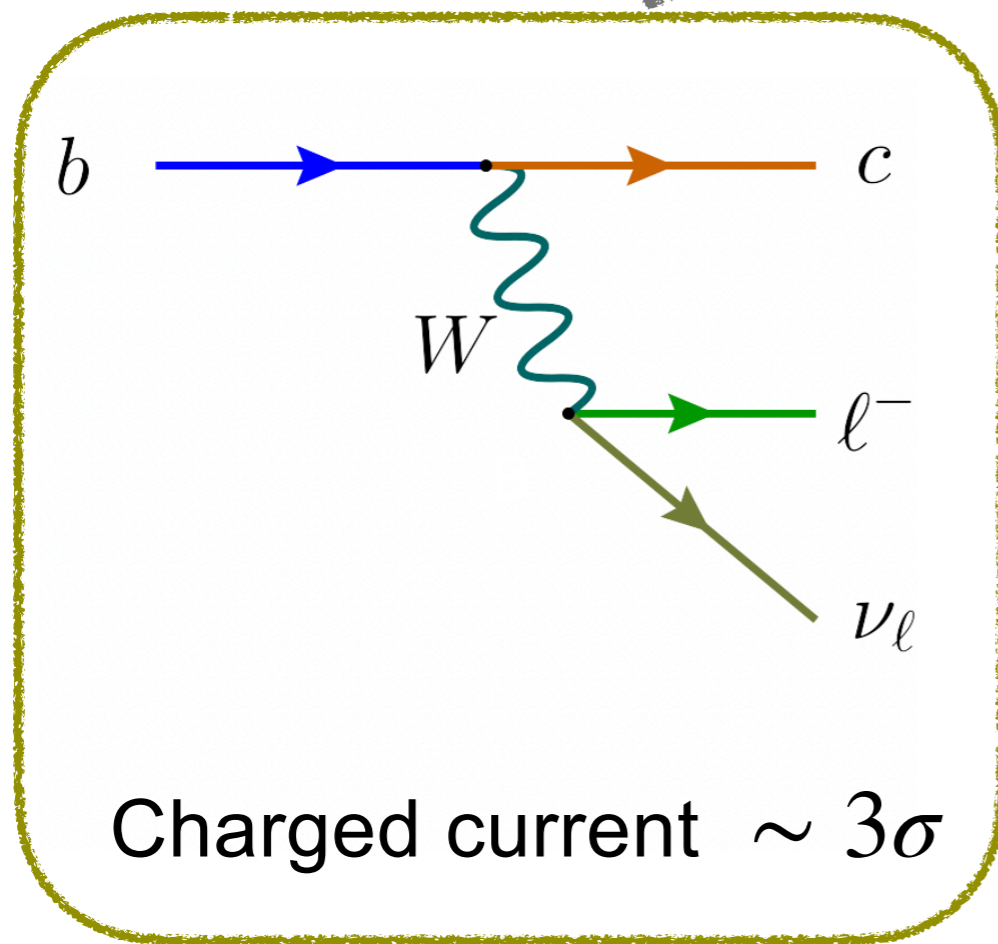
- Background modelling/ branching fractions
- Form factor parameterisation

***New:*** systematic due to simulation size no longer leading systematic, due to new approaches to speed up MC, see details in G. Pietrzyk's talk

# The B-anomalies

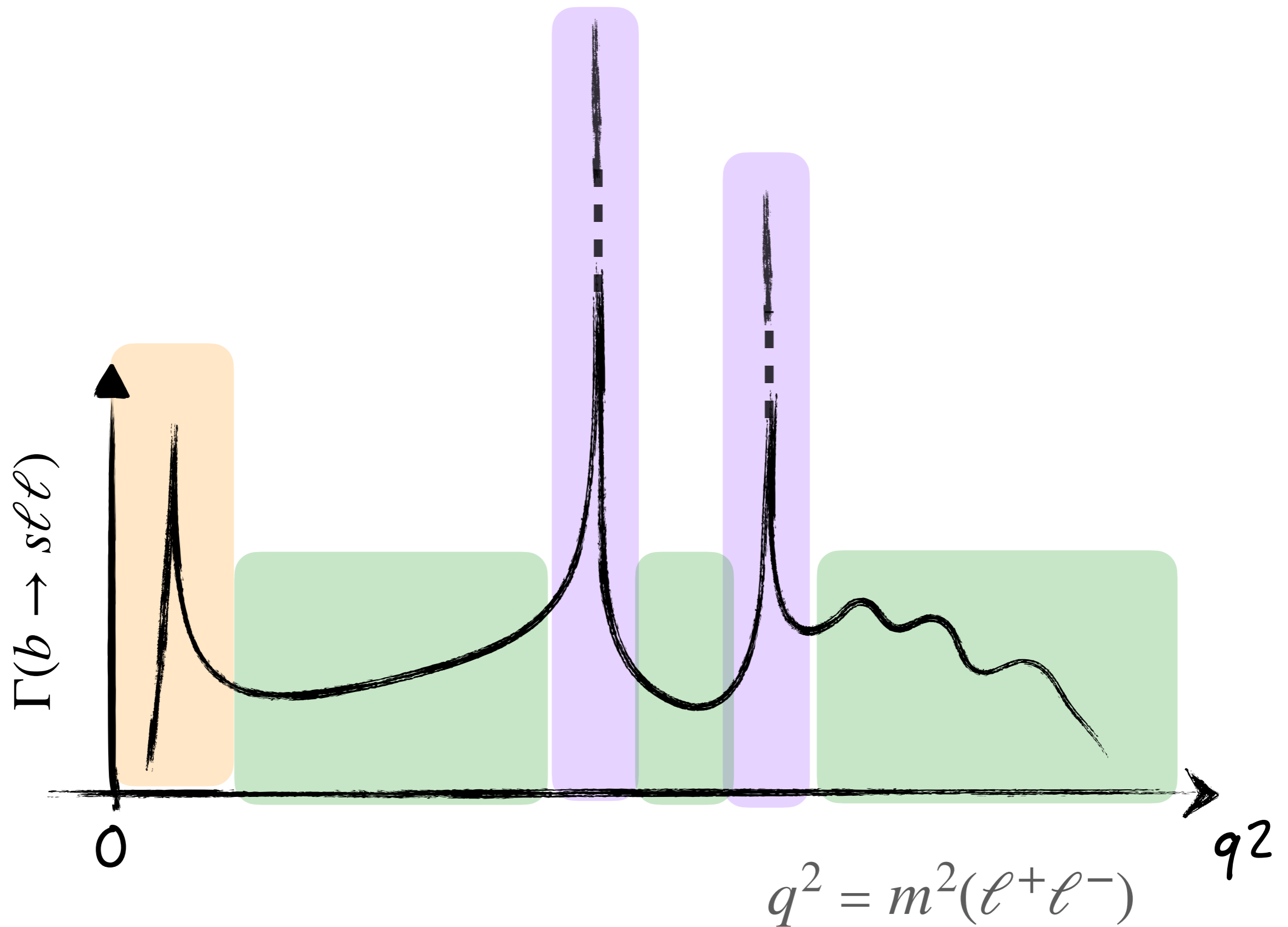


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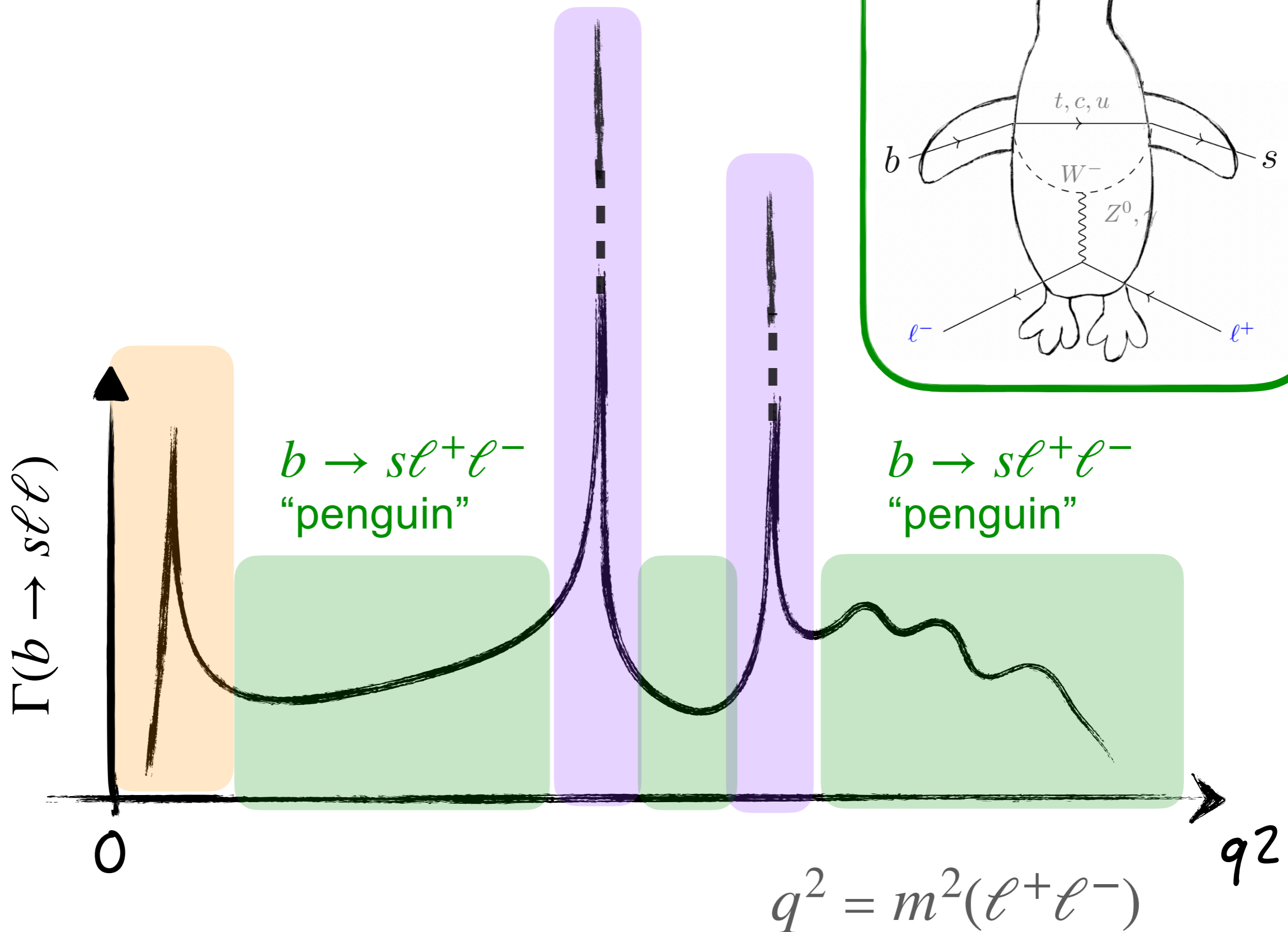




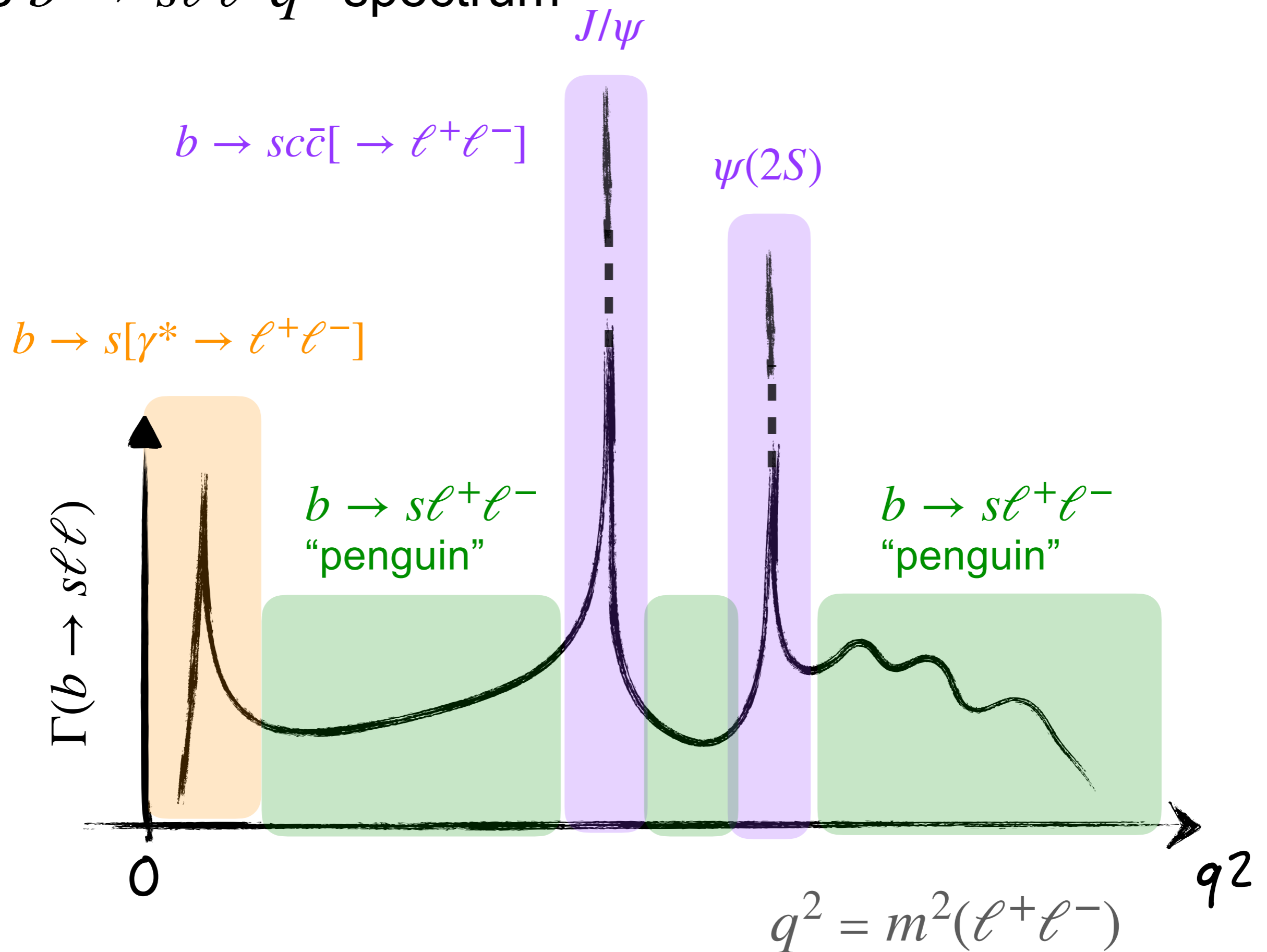
# The $b \rightarrow s\ell\ell$ $q^2$ spectrum



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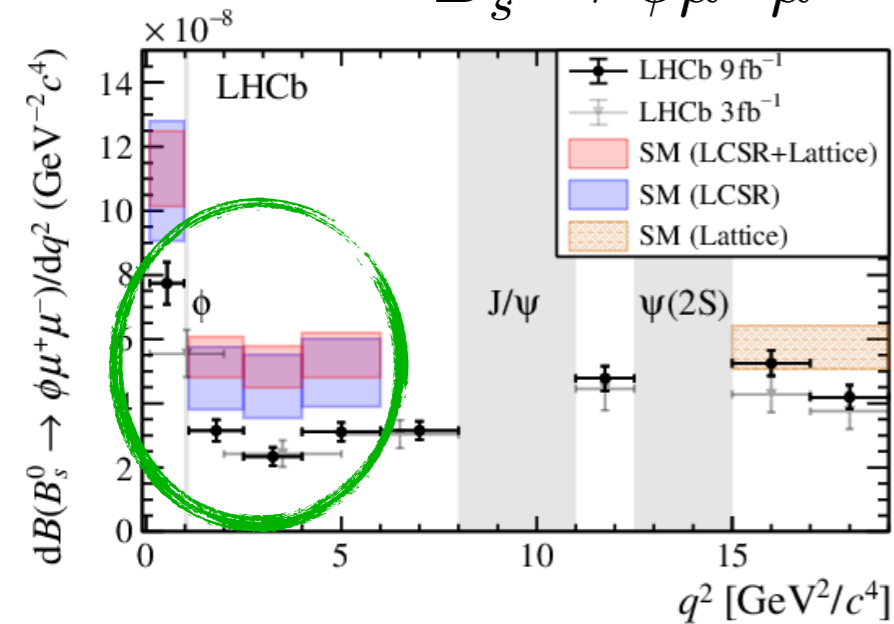


# The $b \rightarrow s\ell\ell$ $q^2$ spectrum

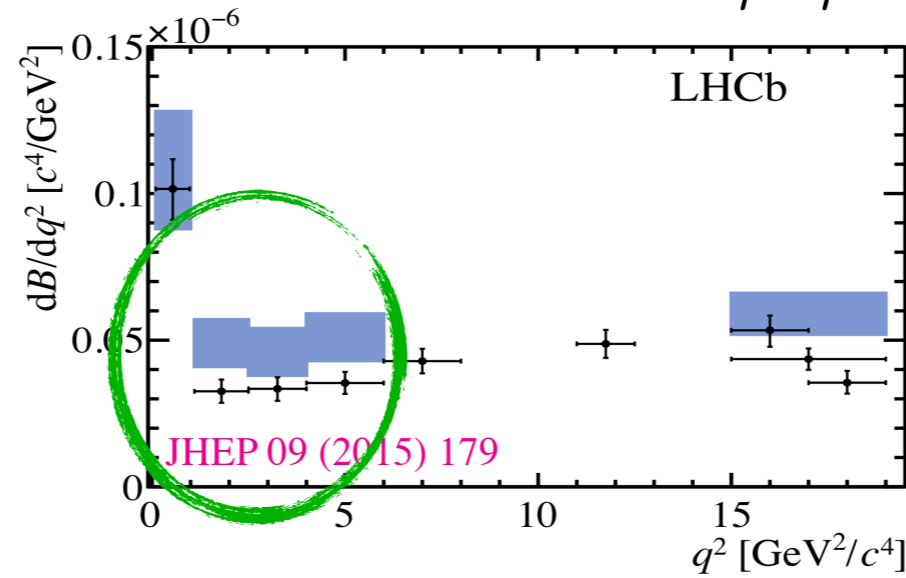


# Branching fractions

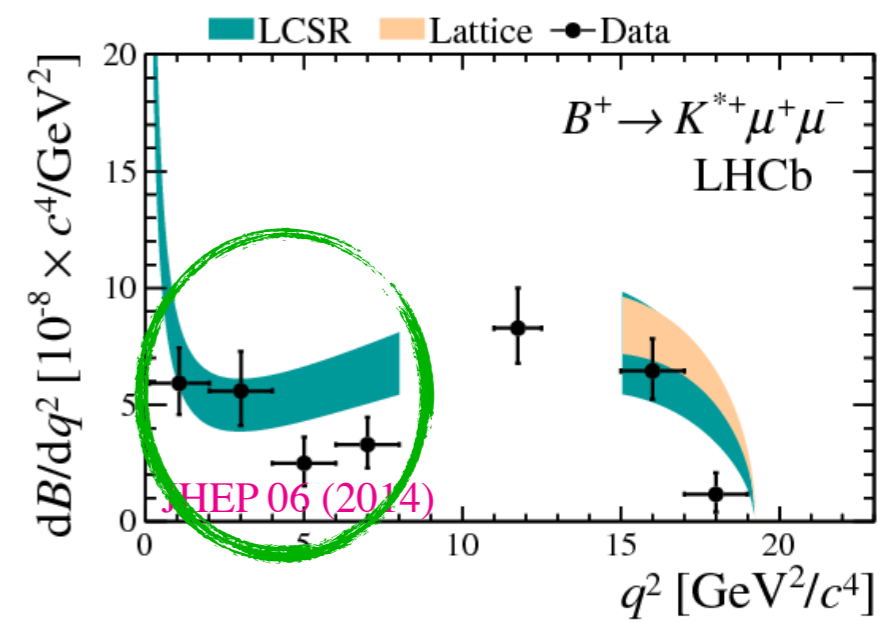
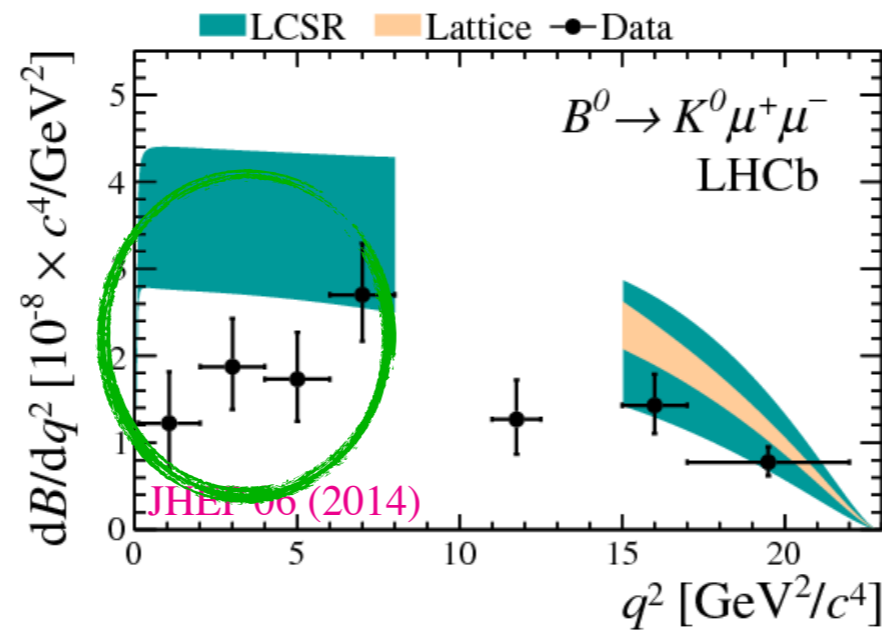
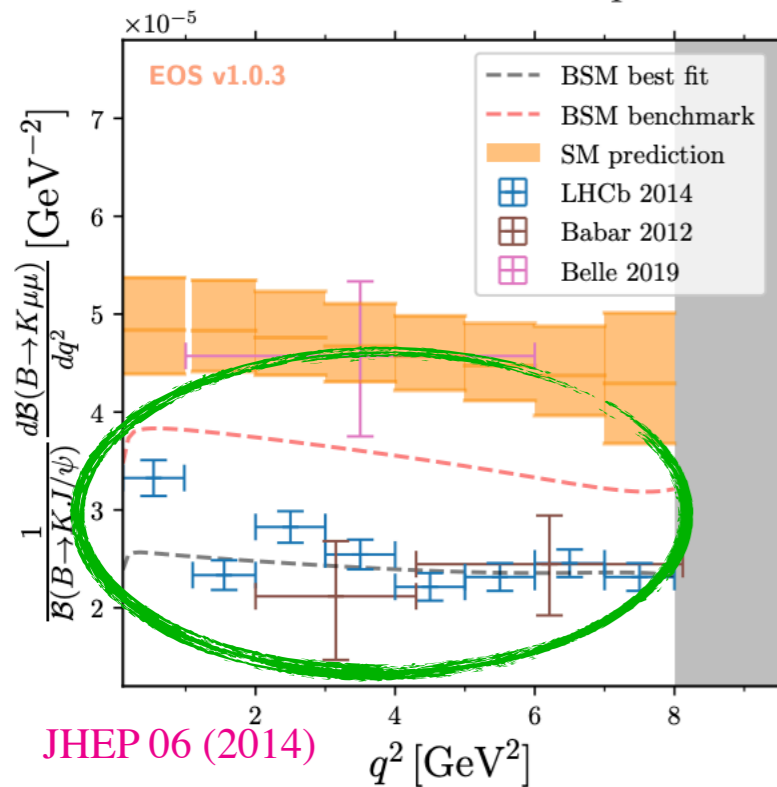
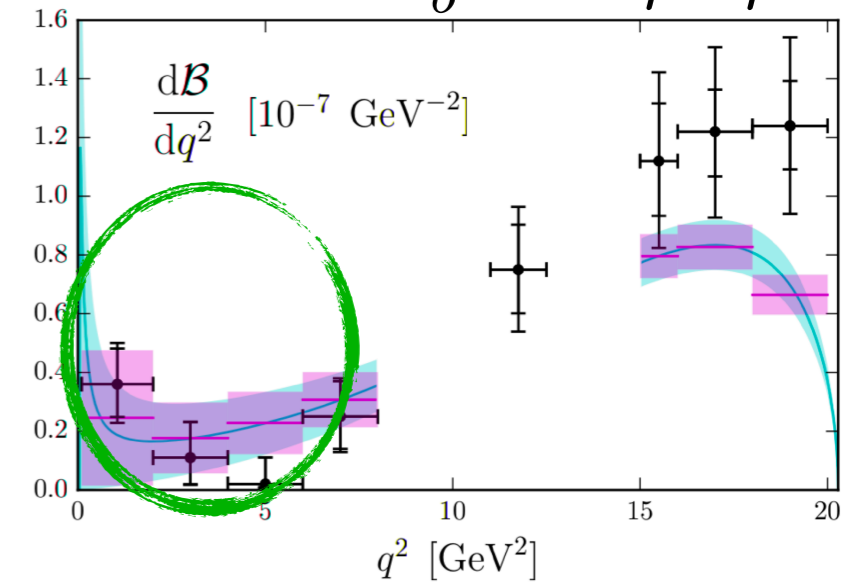
$$B_s^0 \rightarrow \phi \mu^+ \mu^-$$



$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$



$$\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$$



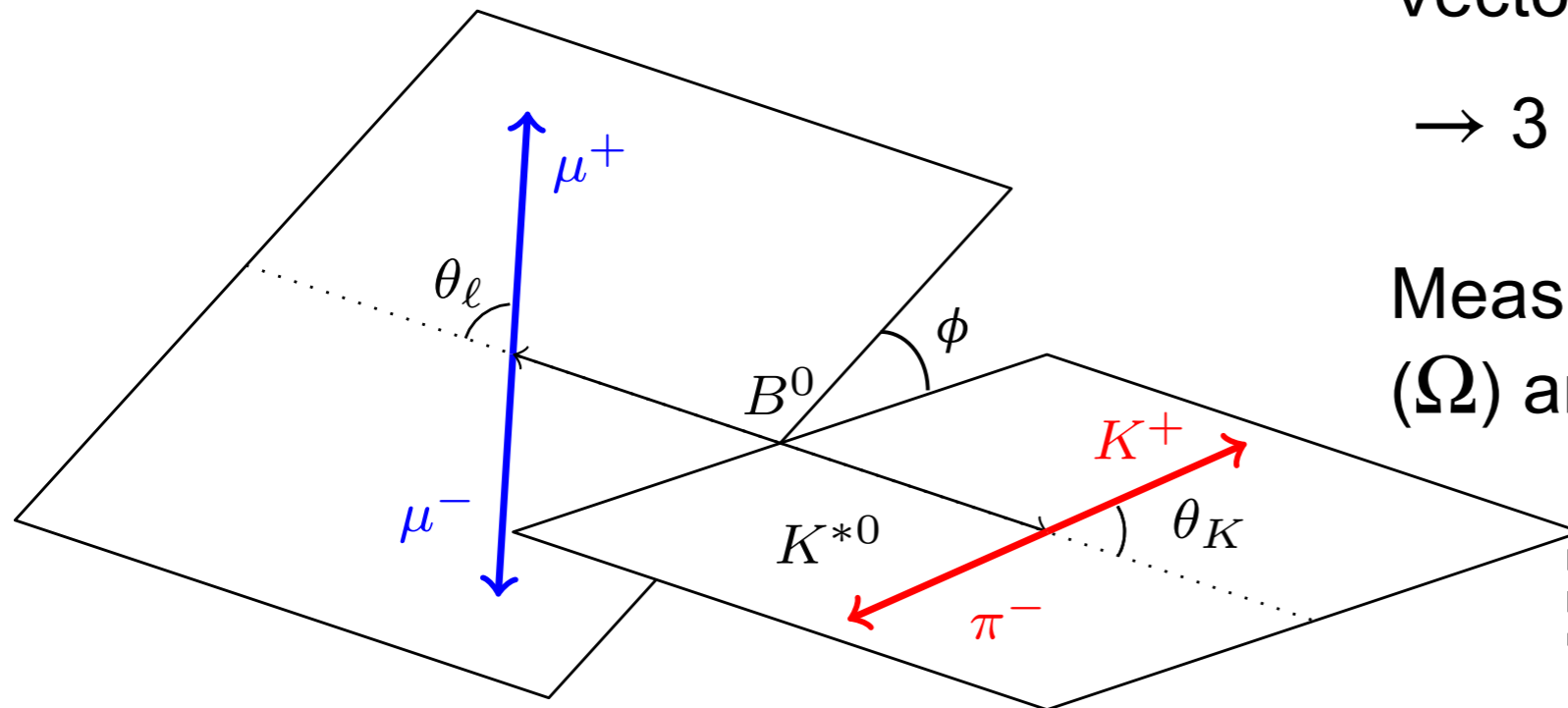
Same pattern, decay rate too low!!

# Angular analysis of $B \rightarrow V(\rightarrow h^+h^-)\mu^+\mu^-$

Vector = spin 1 = P-wave

→ 3 polarisation amplitudes

Measure decay rate across 3 angles ( $\Omega$ ) and  $q^2$



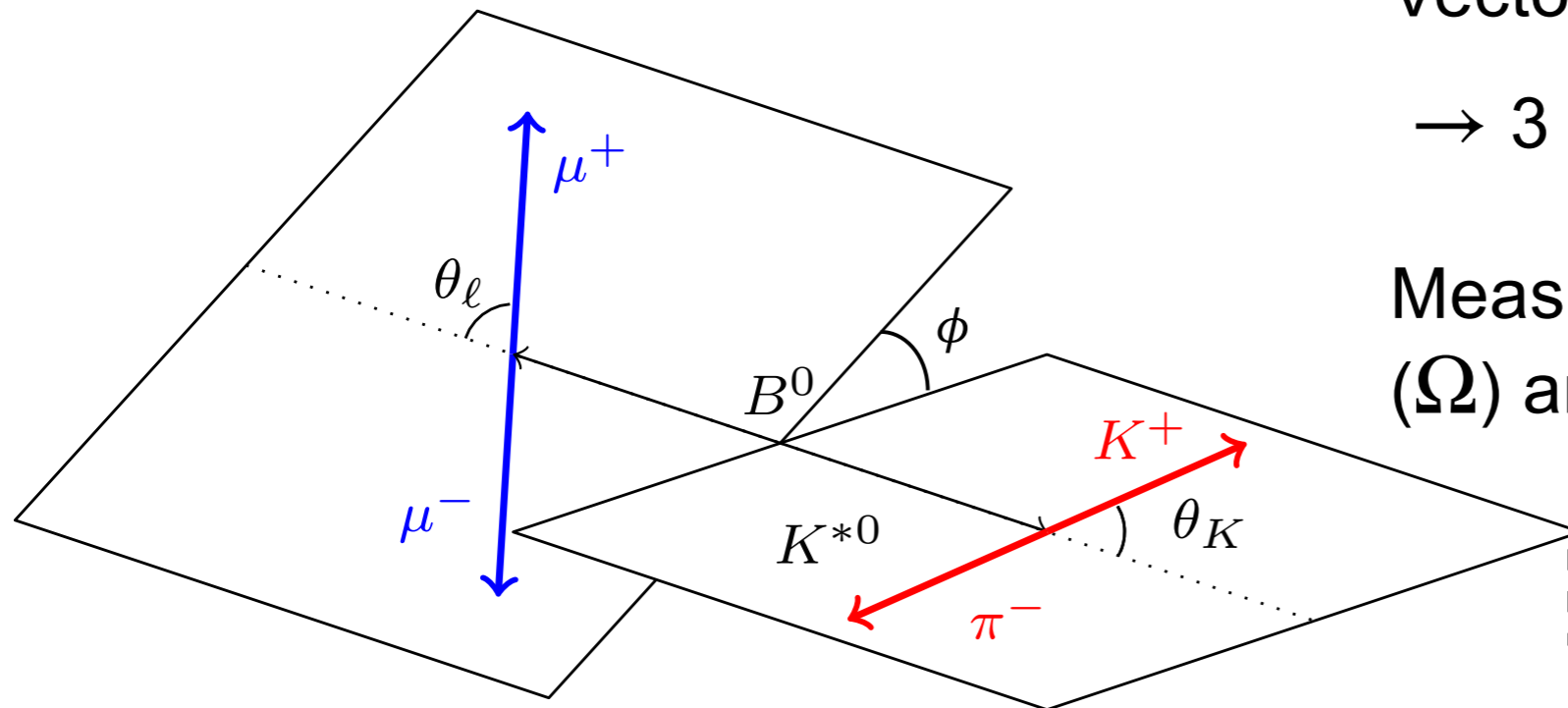
“Traditionally” perform in bins of  $q^2$

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angular coefficients - function of amplitudes

$$\frac{d^4\Gamma(B^0 \rightarrow K^{*0}\mu^+\mu^-)}{d\hat{\Omega}dq^2} = \sum_i I_i(q^2) f_i(\Omega)$$

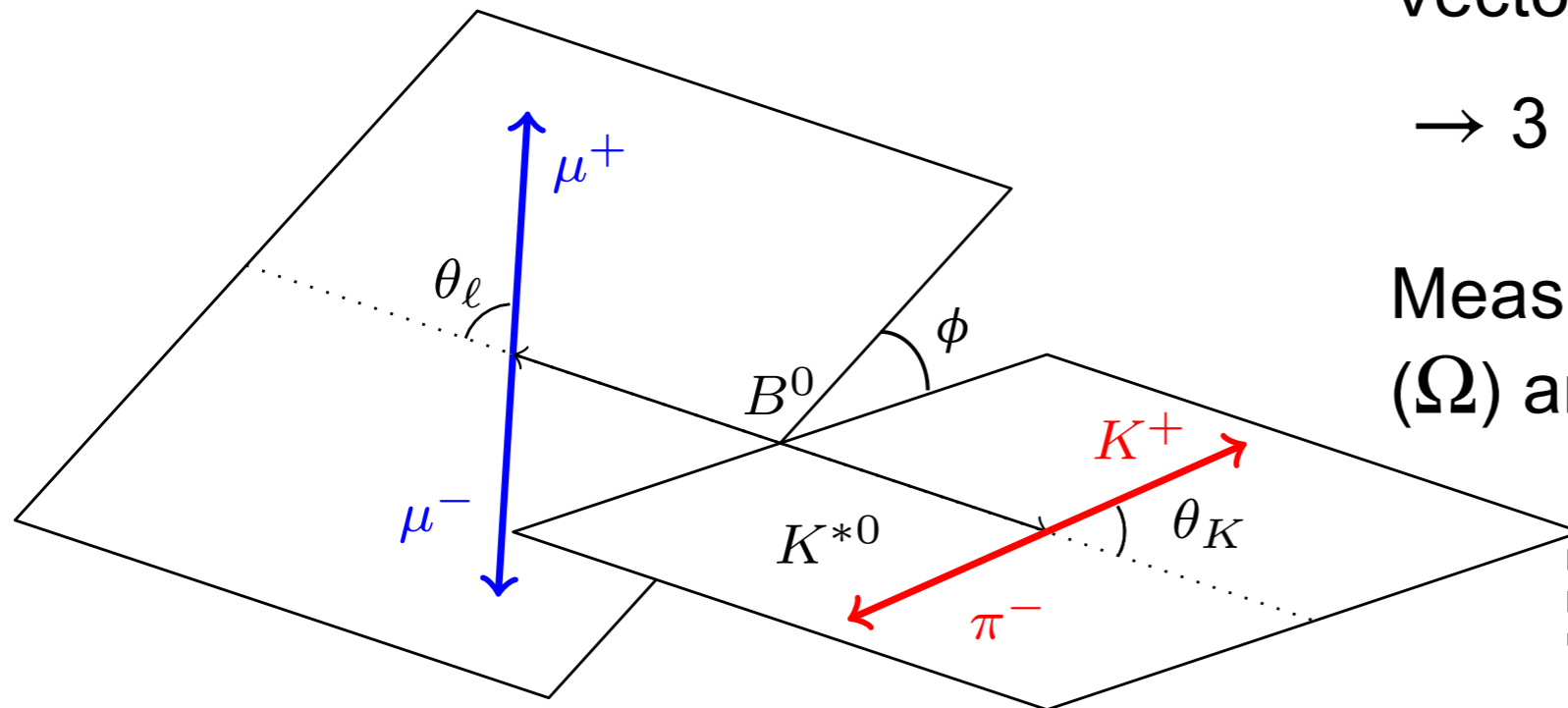
Spherical harmonics

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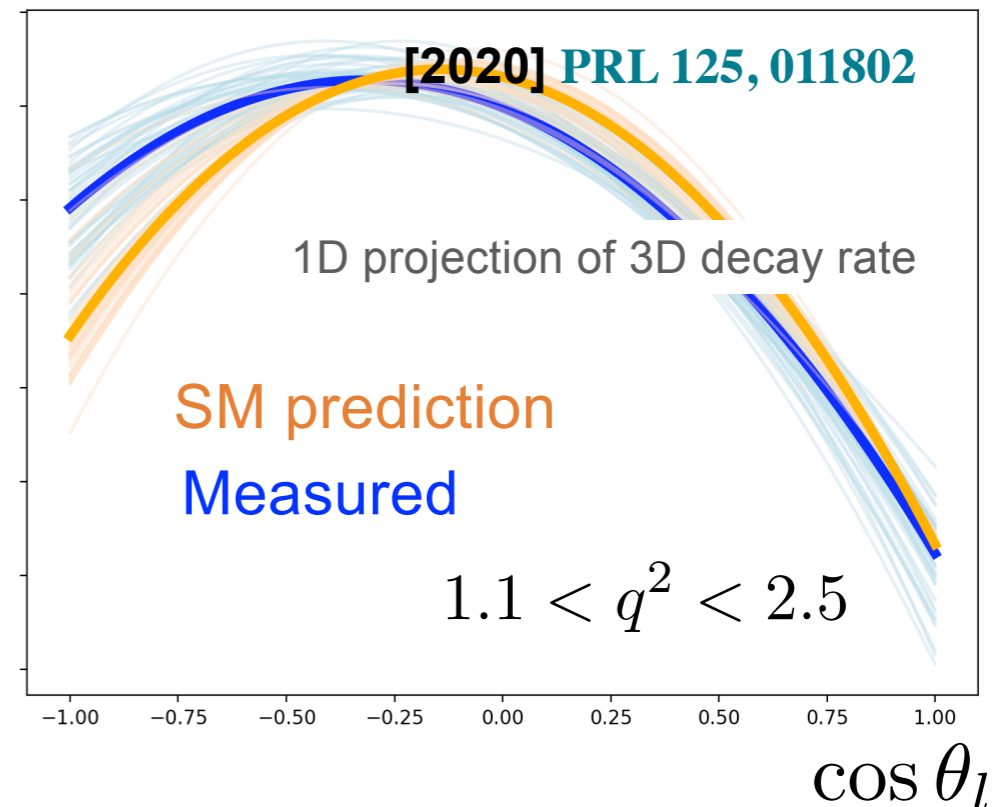


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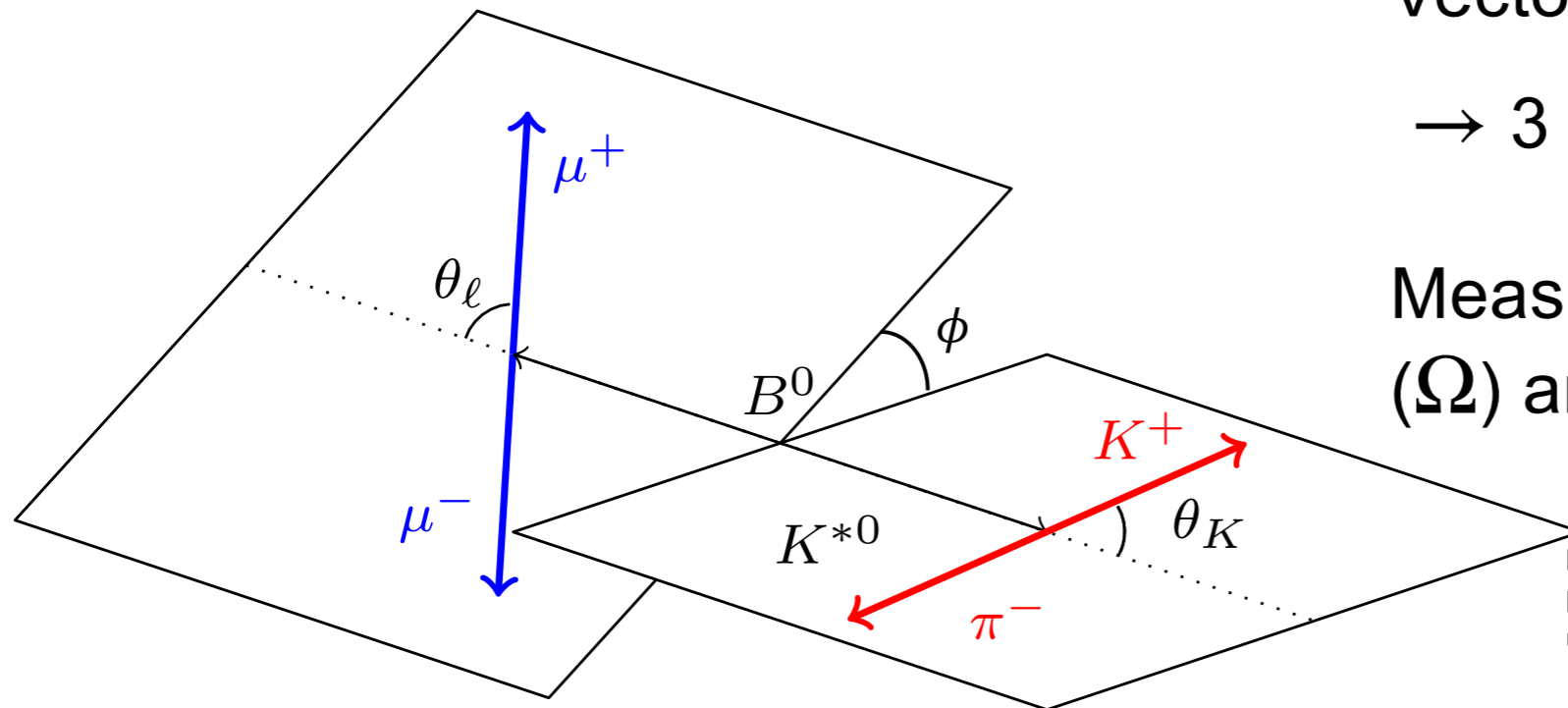


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CP-averaged + averaged over  $q^2 = P^{(')}$

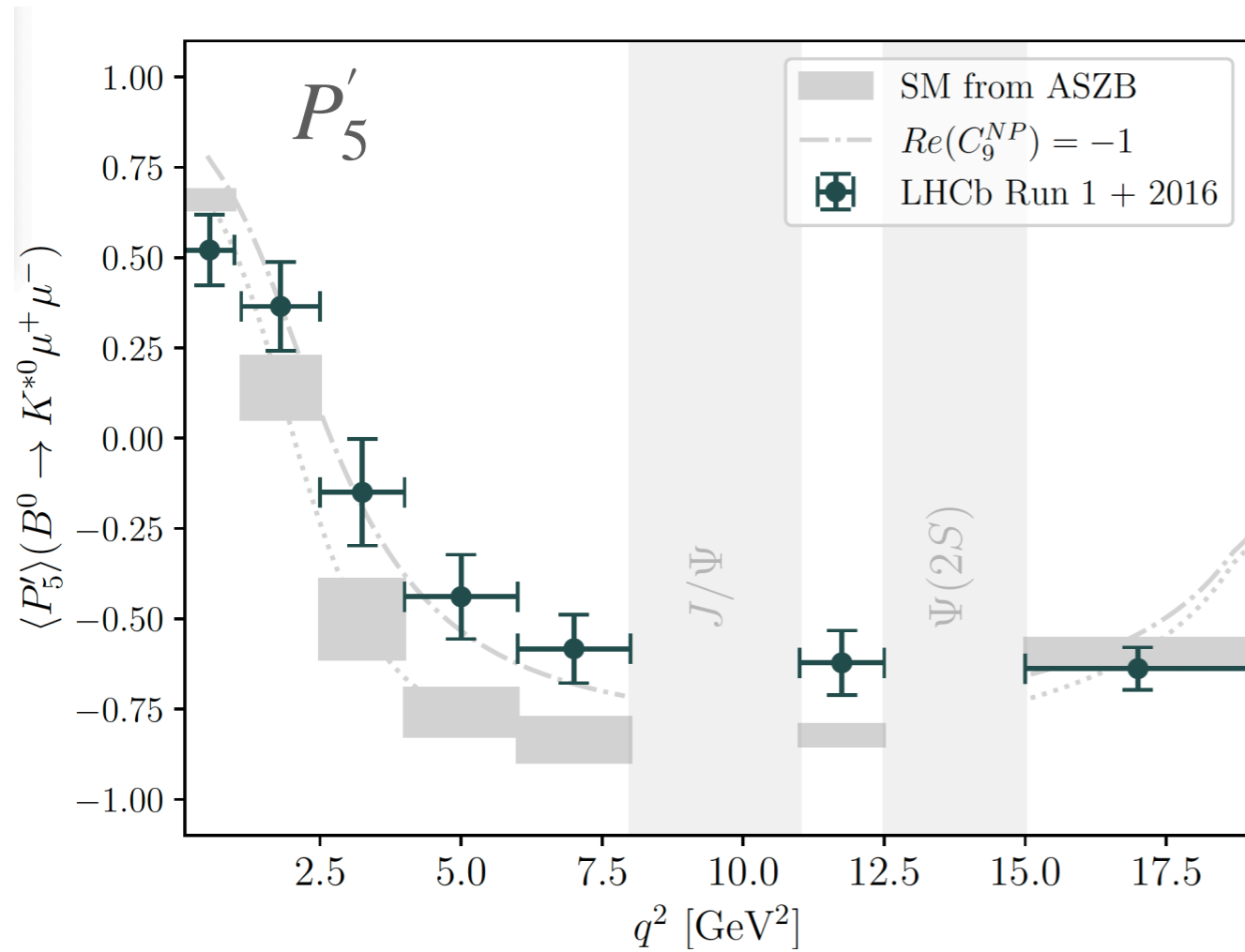
Spherical harmonics



# Example: analysis of $B^0 \rightarrow K^{*0}[\rightarrow K^+\pi^-]\mu^+\mu^-$

LHCb B0 PRL 125, 011802 (2020) . LHCb B+ PRL 161802 (2021) ATLAS: JHEP 10 (2018) 047

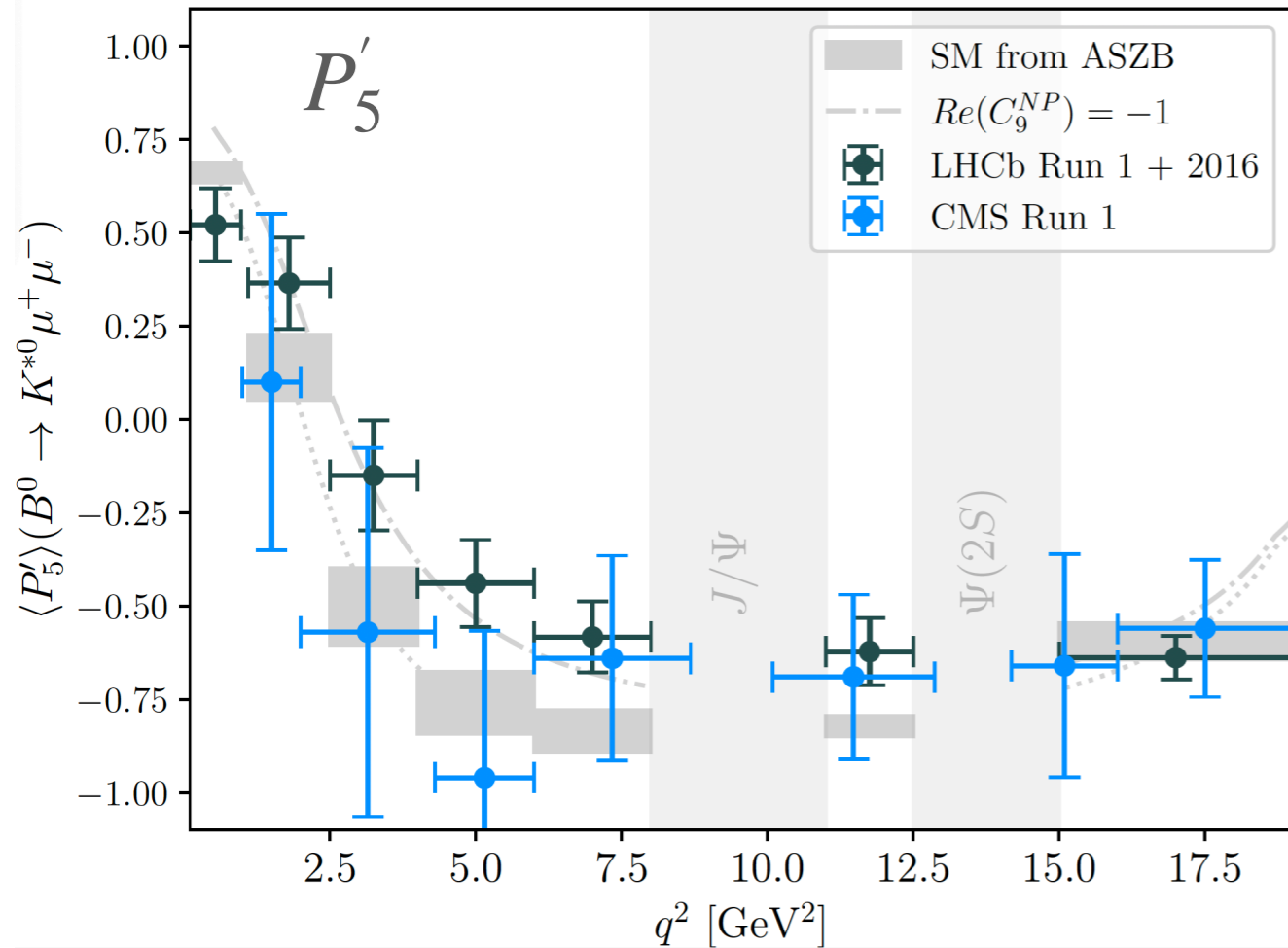
Belle: PRL 118 (2017), CMS:PLB 781 (2018) 517541



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LHCb B0 PRL 125, 011802 (2020) . LHCb B+ PRL 161802 (2021) ATLAS: JHEP 10 (2018) 047

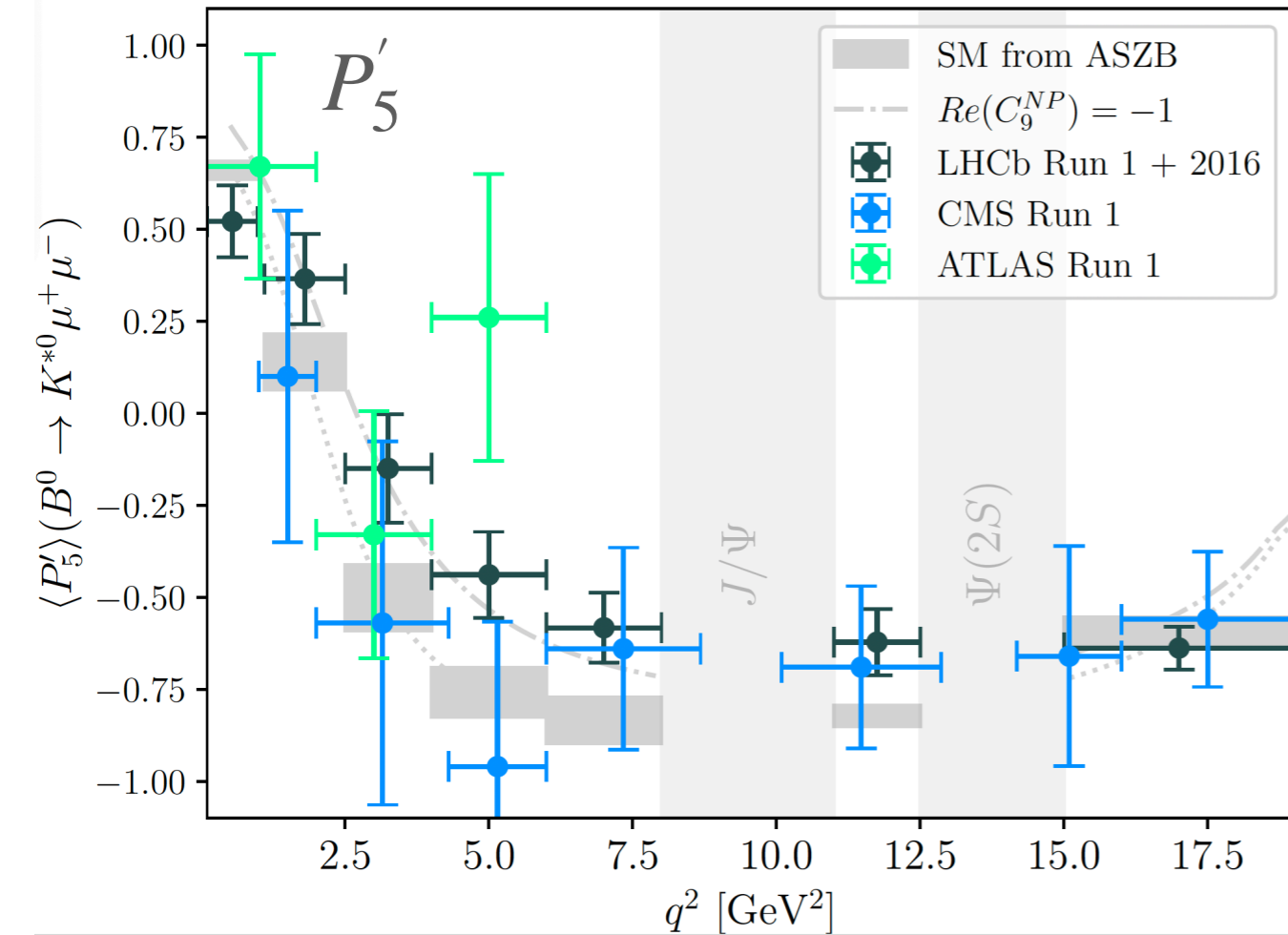
Belle: PRL 118 (2017), CMS:PLB 781 (2018) 517541



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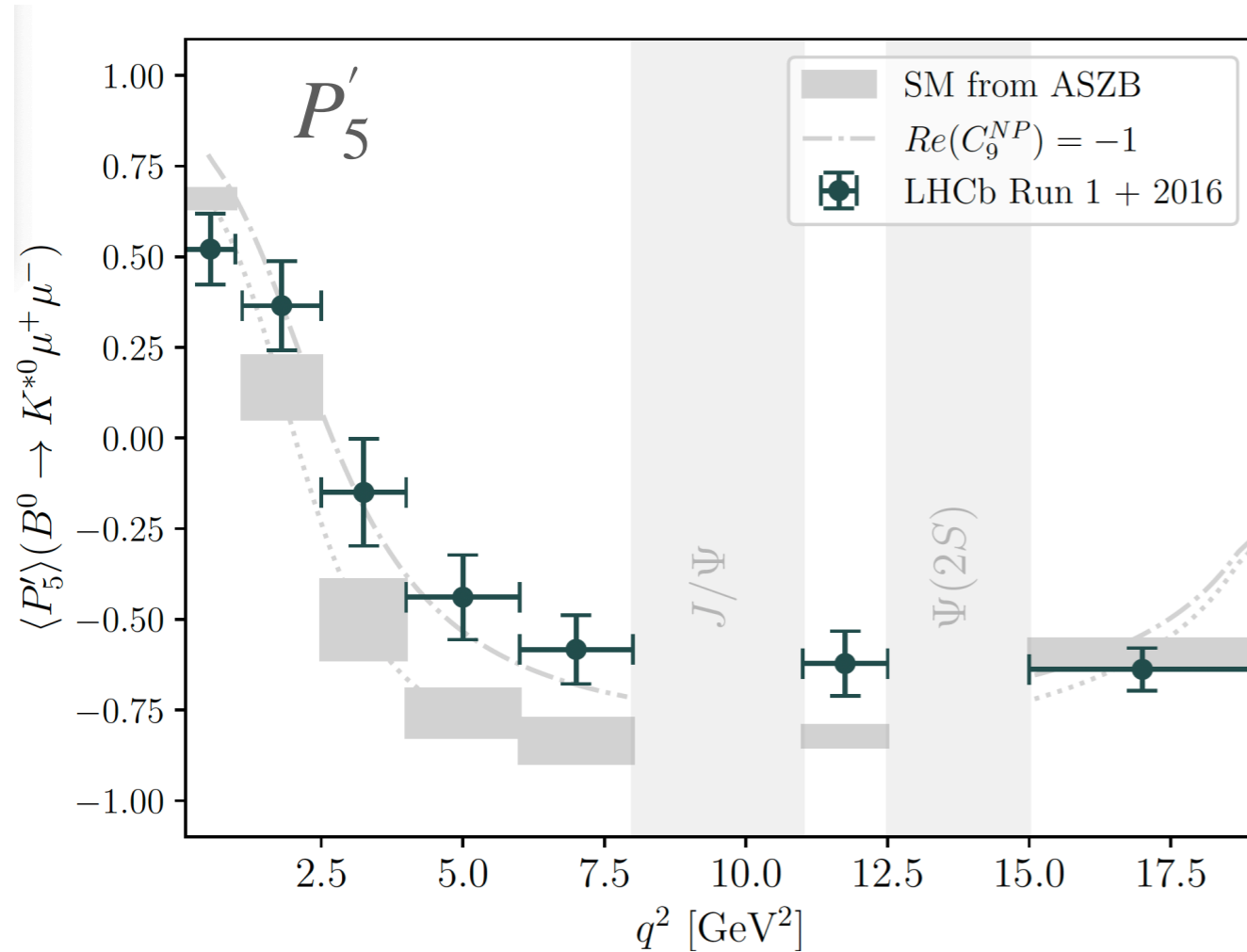
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One angular observable of 8 (or 12) P-wave observables in total

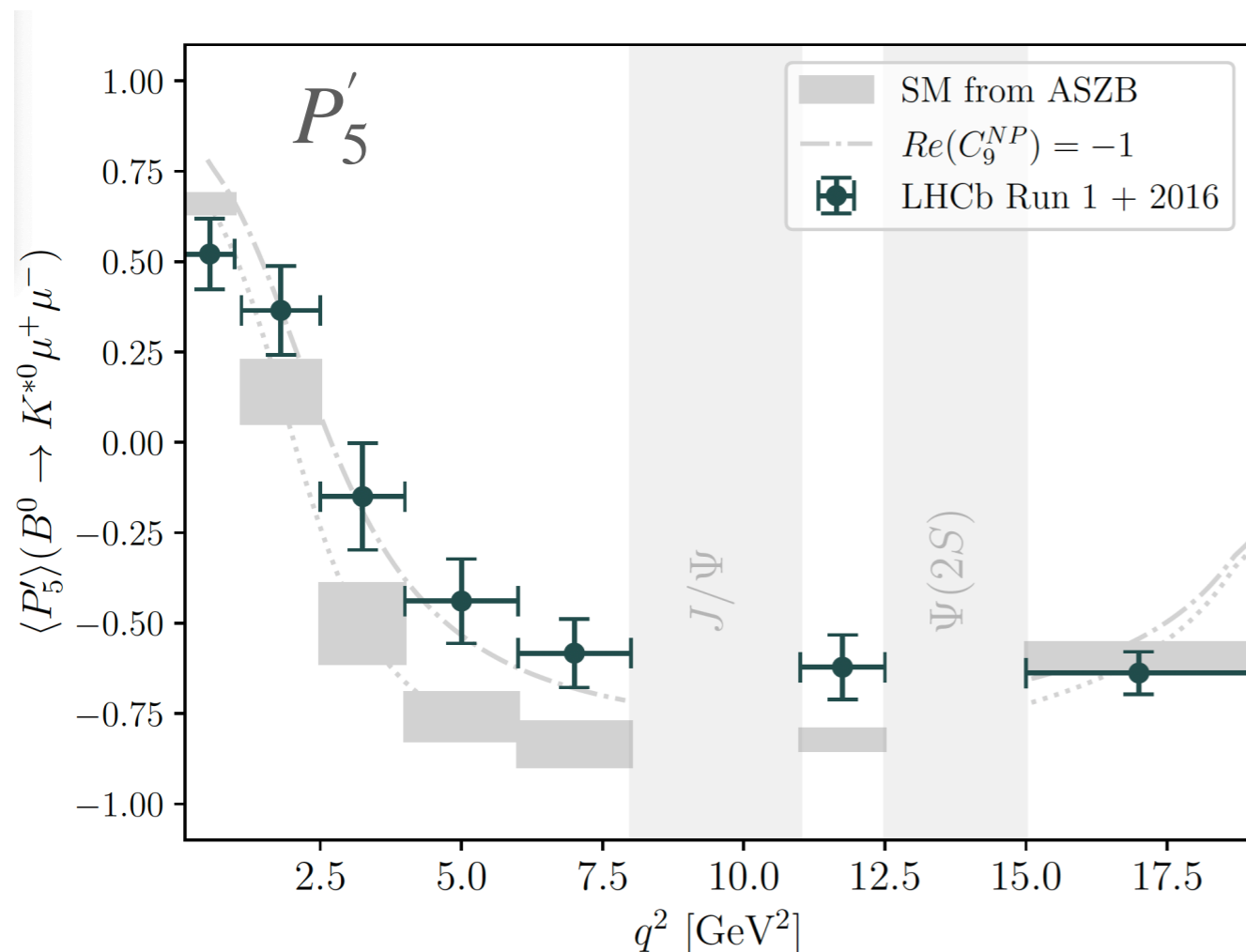
$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_K d\phi} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\
+ \frac{1}{4}(1 - F_L) \sin^2 \theta_K - F_L \cos^2 \theta_K) \cos 2\theta_l \\
+ \frac{1}{2}P_1(1 - F_L) \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\
+ \sqrt{(1 - F_L)F_L} \left( \frac{1}{2}P'_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + P'_5 \sin 2\theta_K \sin \theta_l \cos \phi \right) \\
- \sqrt{(1 - F_L)F_L} \left( P'_6 \sin 2\theta_K \sin \theta_l \sin \phi - \frac{1}{2}P'_8 \sin 2\theta_K \sin 2\theta_l \sin \phi \right) \\
\left. + 2P_2(1 - F_L) \sin^2 \theta_K \cos \theta_l - P_3(1 - F_L) \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]$$

# Example: analysis of $B^0 \rightarrow K^{*0}[\rightarrow K^+\pi^-]\mu^+\mu^-$

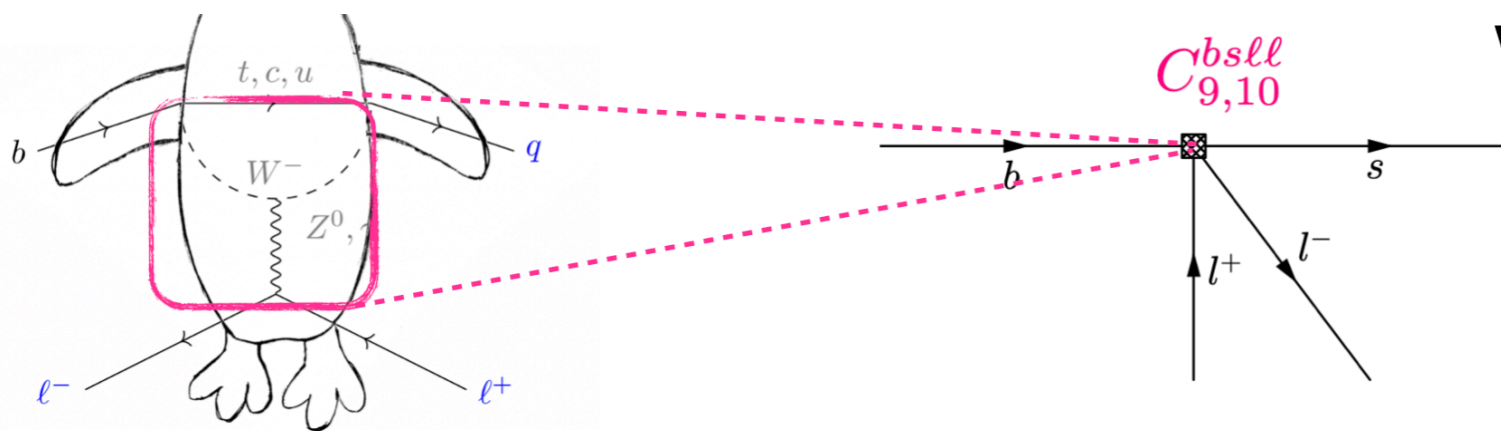
LHCb B0 PRL 125, 011802 (2020) . LHCb B+ PRL 161802 (2021) ATLAS: JHEP 10 (2018) 047

Belle: PRL 118 (2017), CMS:PLB 781 (2018) 517541

Global agreement with SM?



EW scale  $\gg m_b$ , replace loop with effective couplings

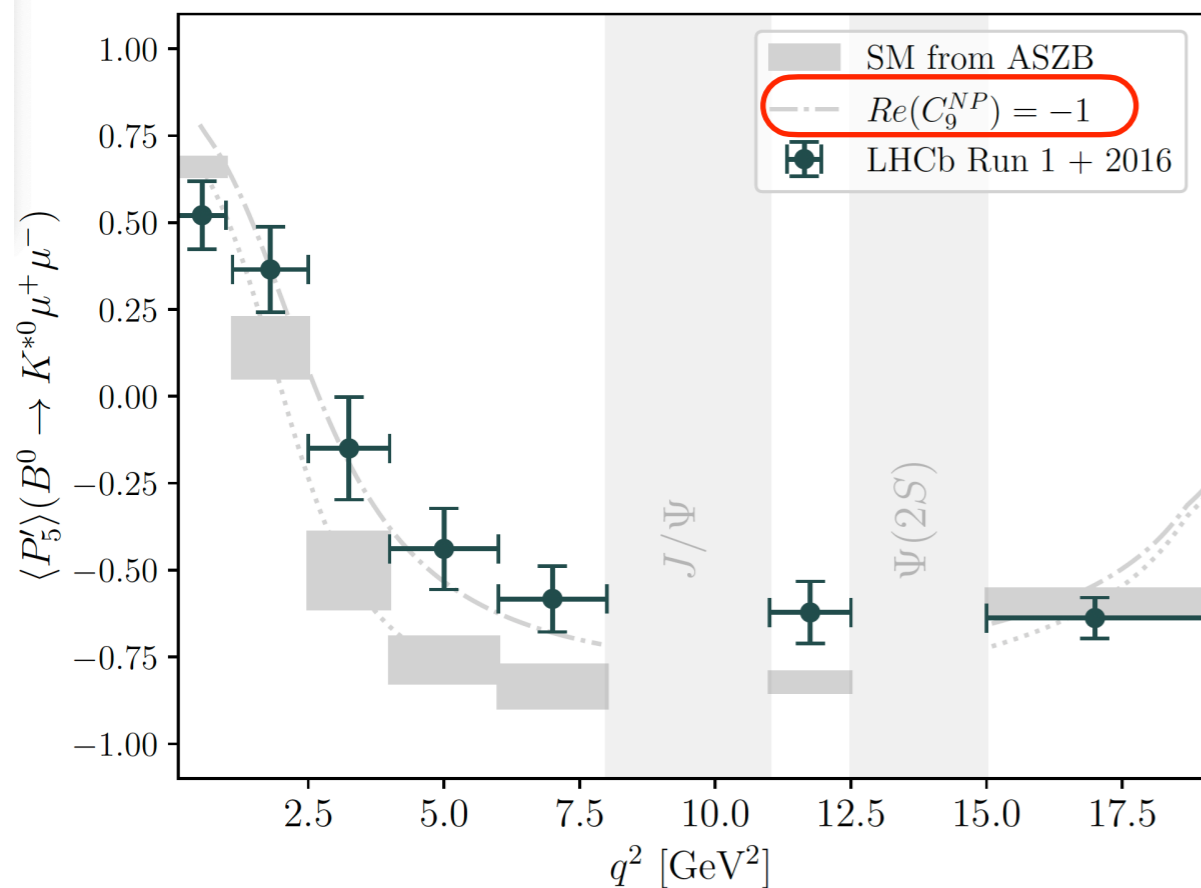


$C_9 = bsl\ell$  vector current

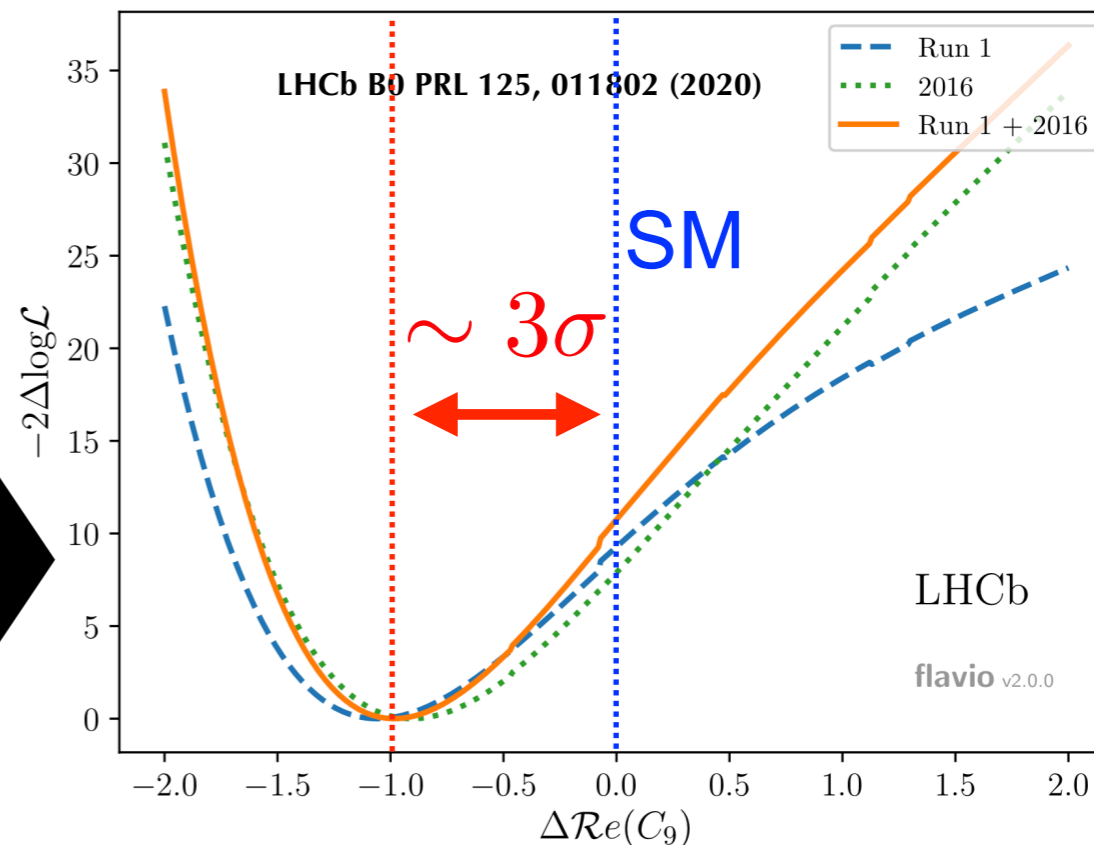
$C_{10} = bsl\ell$  axial-vector current

# Example: analysis of $B^0 \rightarrow K^{*0} [ \rightarrow K^+ \pi^- ] \mu^+ \mu^-$

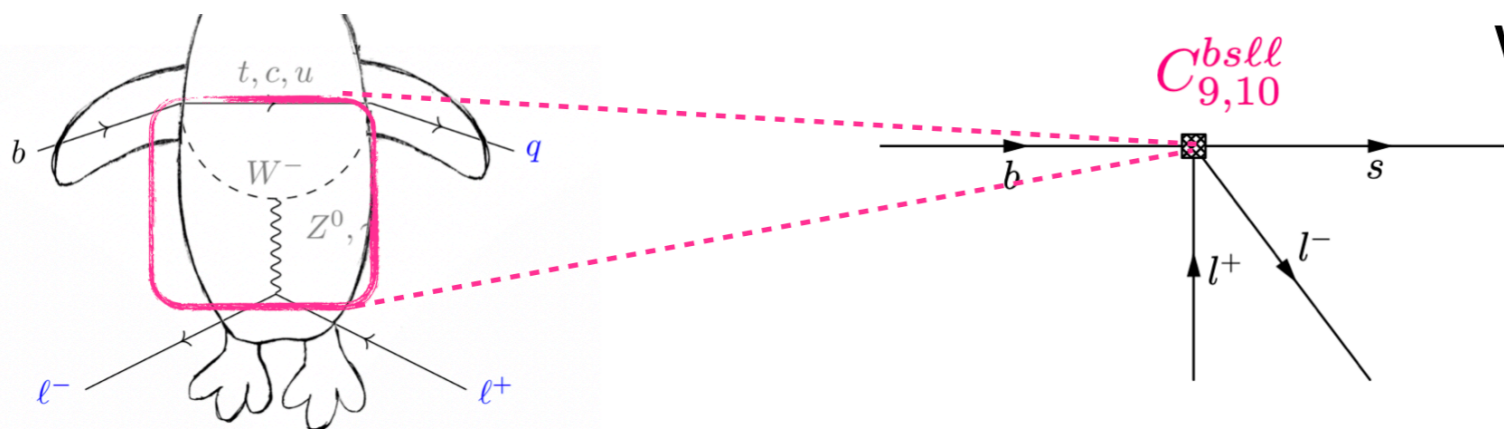
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+ 7 other observables



EW scale  $\gg m_b$ , replace loop with effective couplings



$C_9 = bs\ell\ell$  vector current

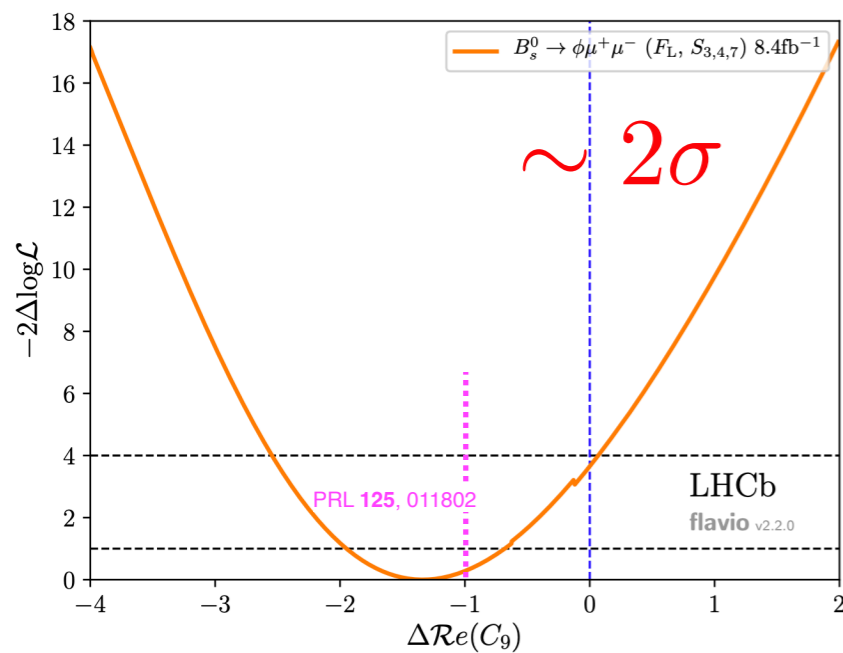
$C_{10} = bs\ell\ell$  axial-vector current

# Summary of angular analysis

$$B_s^0 \rightarrow \phi \mu^+ \mu^-$$

$$\Delta \mathcal{R}e(\mathcal{C}_9) = -1.3^{+0.7}_{-0.6}$$

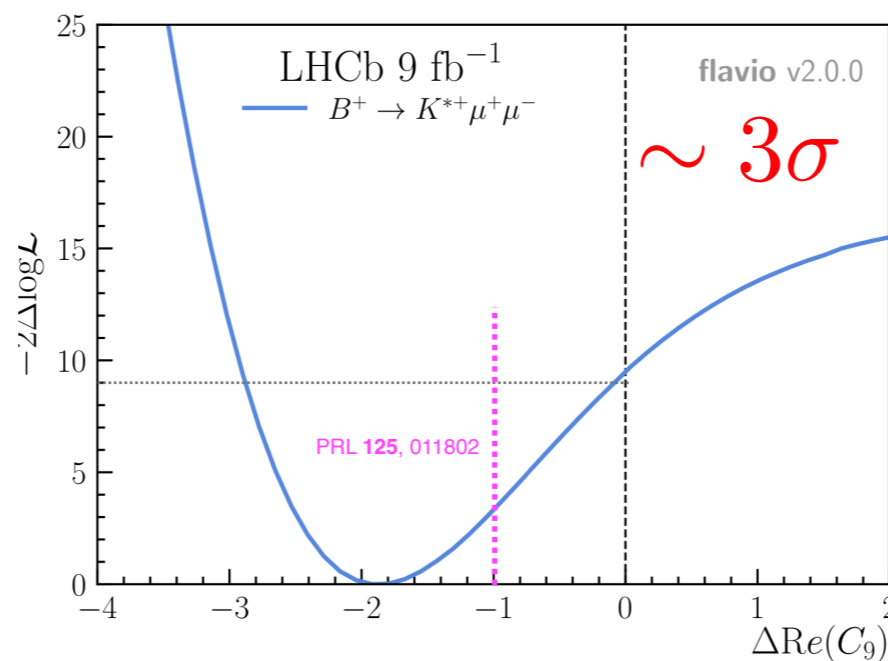
JHEP 11 (2021) 043



$$B^+ \rightarrow K^{*+} \mu^+ \mu^-$$

$$\Delta \mathcal{R}e(\mathcal{C}_9) = -1.9$$

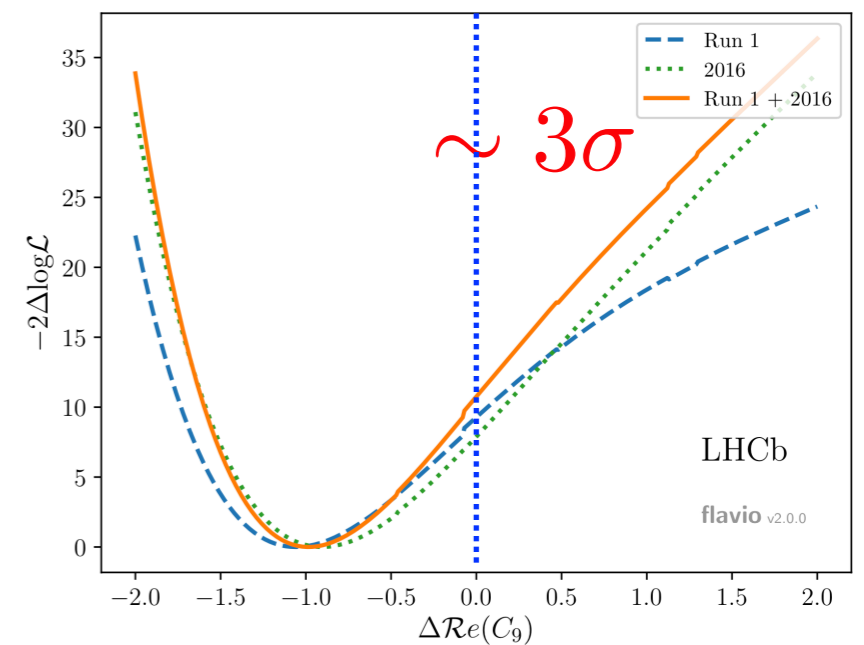
Phys. Rev. Lett. **126**, 161802



$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$

$$\Delta \mathcal{R}e(\mathcal{C}_9) = -0.99^{+0.25}_{-0.21}$$

Phys. Rev. Lett. **125**, 011802



Same pattern, negative definitions in effective coupling

New!!  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  with  $140 \text{ fb}^{-1}$  from CMS

Increase in data:

- fit full angular distribution (no angular folding, in contrast to Run 1)
- Full parameterisation of  $[K\pi]$  spin-0 partial wave (S-wave)



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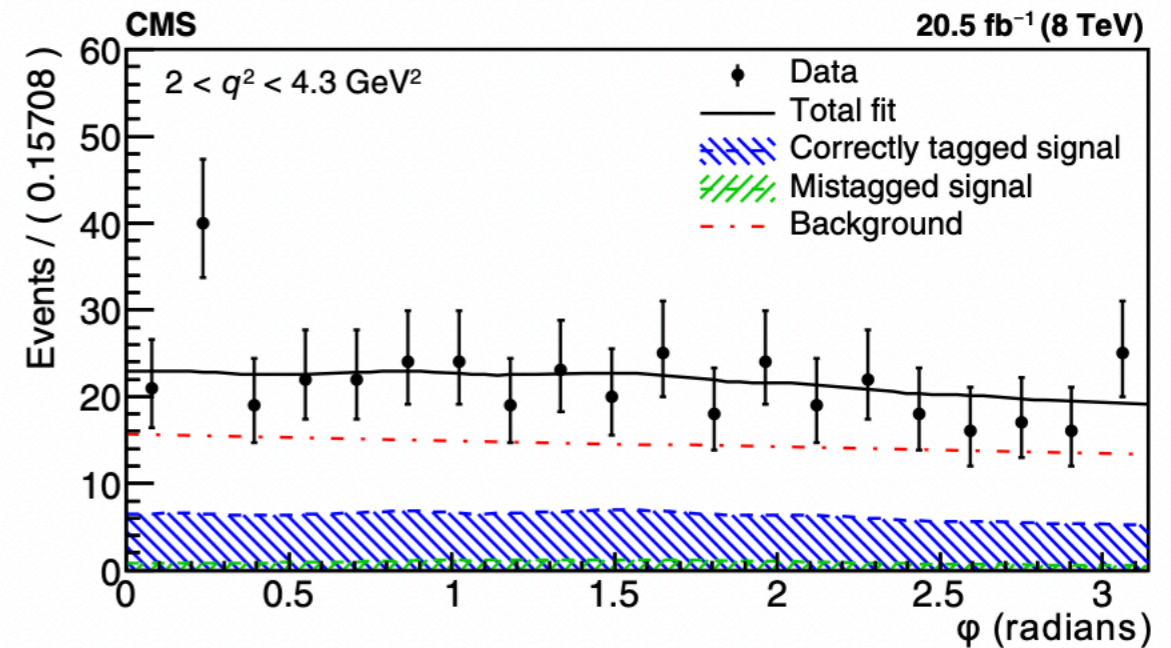
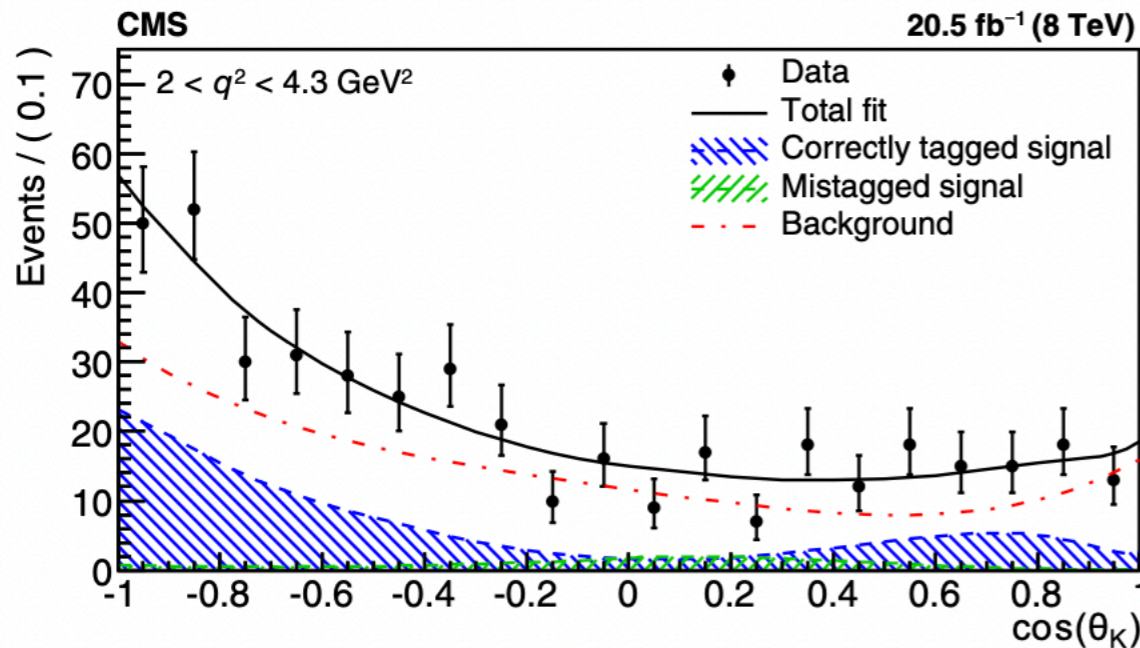
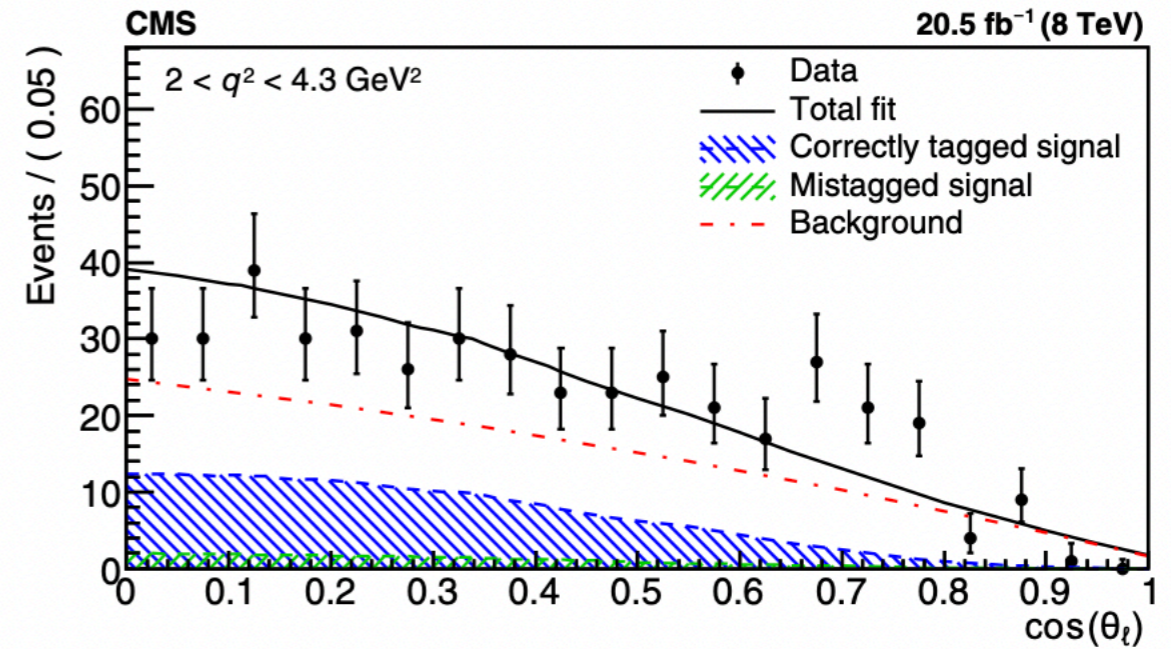
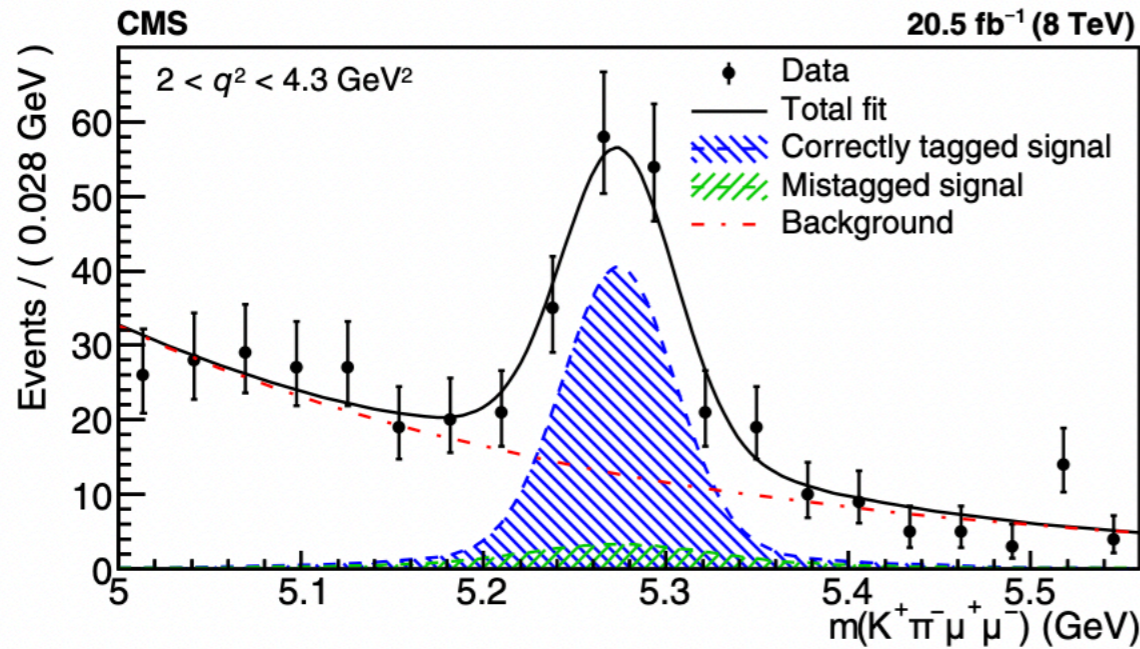
- Take the hypothesis which gives  $m(K\pi)$  closest to pole mass

Assumptions

- Massless leptons and no scalar or tensor amplitudes

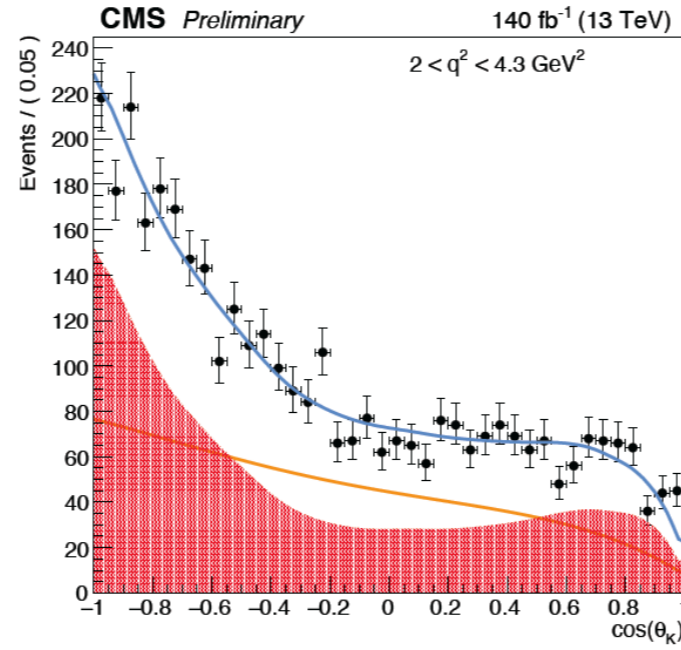
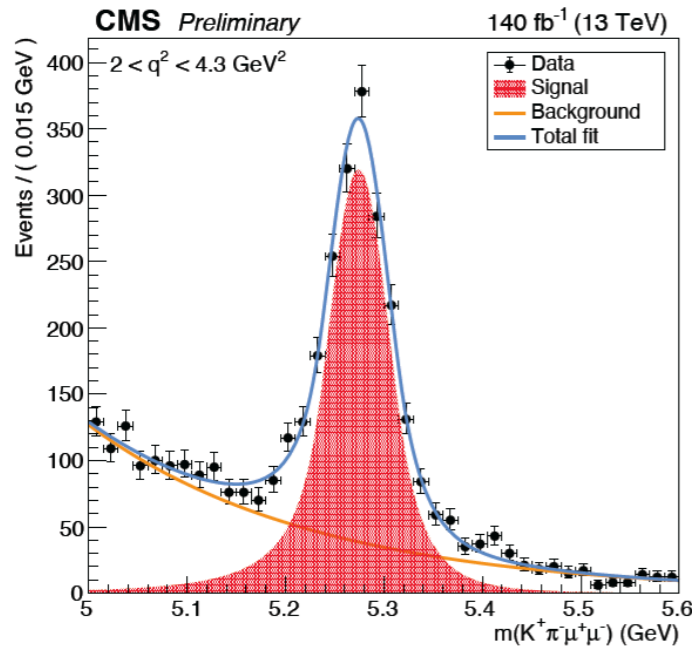
# New!! $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ with $140 \text{ fb}^{-1}$ from CMS

Previous Run 1 only result



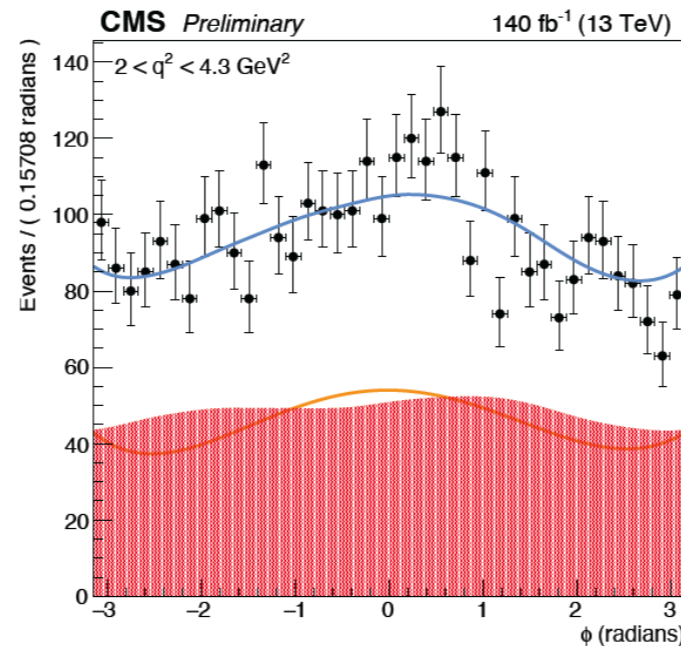
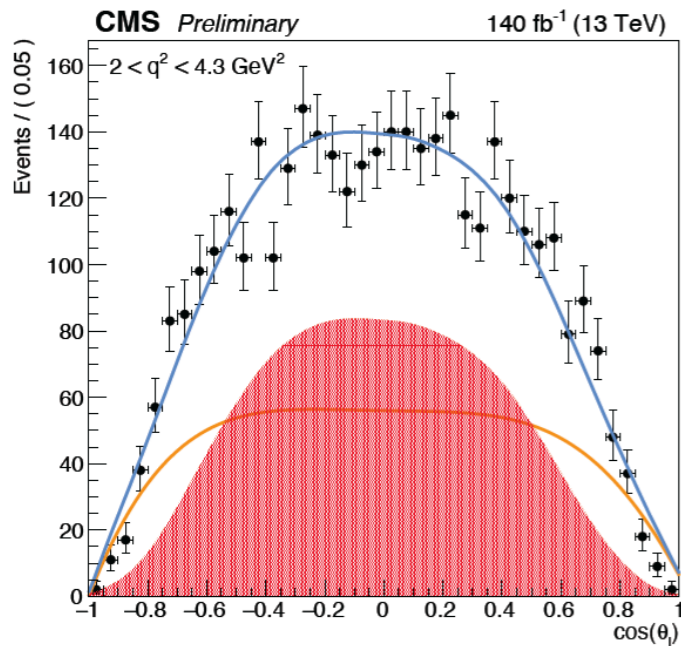
# New!! $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ with $140 \text{ fb}^{-1}$ from CMS

## New Run 2 results



Result is still statistically dominated

Effect on  $P'_5$  ?



# New!! $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ with $140 \text{ fb}^{-1}$ from CMS

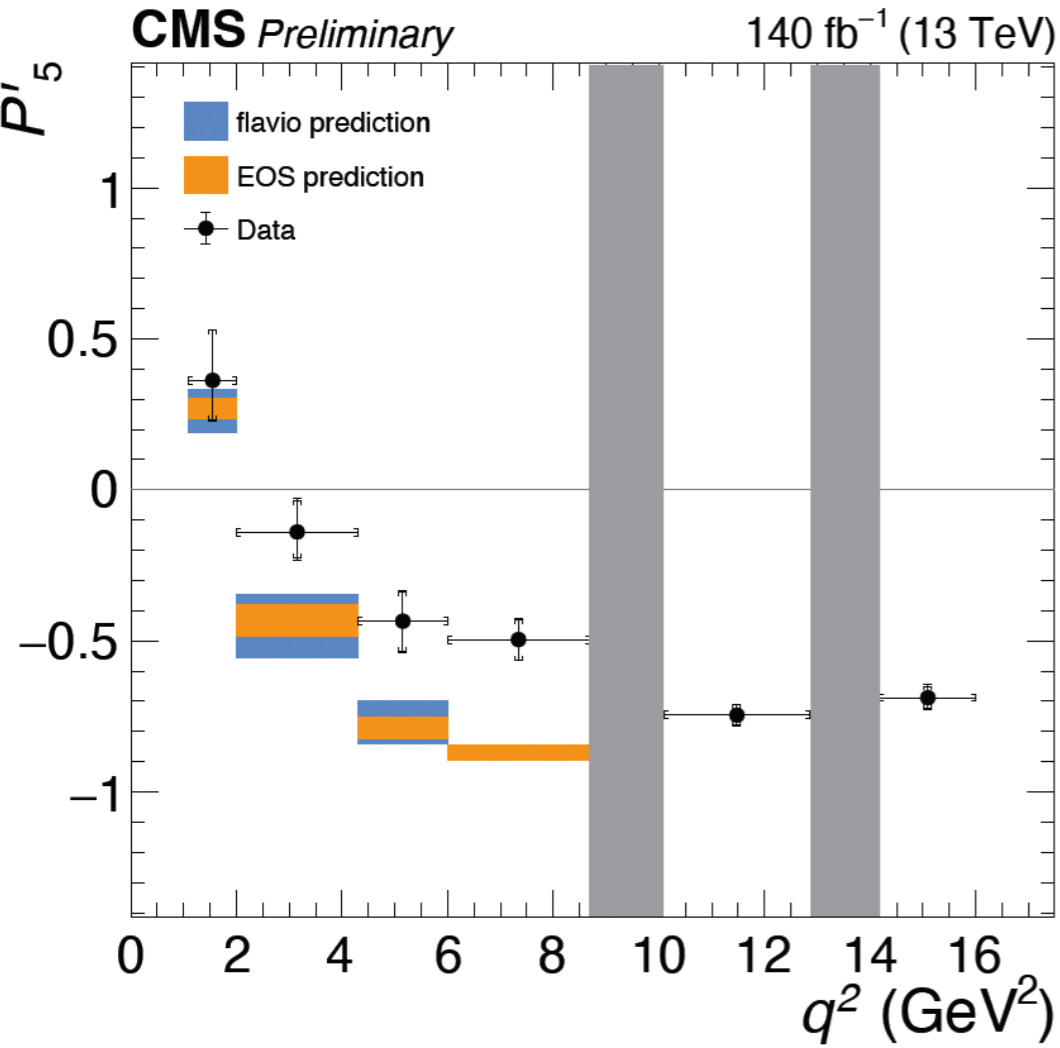


Table 1: Preliminary results, CMS Run 2

	$1.1 < q^2 < 2 \text{ GeV}^2$	$2 < q^2 < 4.3 \text{ GeV}^2$	$4.3 < q^2 < 6 \text{ GeV}^2$
$F_L$	$0.709^{+0.073}_{-0.054} \pm 0.021$	$0.810^{+0.036}_{-0.030} \pm 0.016$	$0.714^{+0.032}_{-0.030} \pm 0.012$
$P_1$	$0.089^{+0.234}_{-0.204} \pm 0.040$	$-0.285^{+0.187}_{-0.208} \pm 0.051$	$-0.297^{+0.153}_{-0.168} \pm 0.038$
$P_2$	$-0.374^{+0.173}_{-0.125} \pm 0.095$	$-0.244^{+0.094}_{-0.077} \pm 0.039$	$0.121^{+0.080}_{-0.076} \pm 0.030$
$P_3$	$-0.045^{+0.209}_{-0.216} \pm 0.044$	$-0.187^{+0.196}_{-0.218} \pm 0.089$	$-0.027^{+0.143}_{-0.143} \pm 0.081$
$P'_4$	$-0.436^{+0.289}_{-0.323} \pm 0.111$	$-0.431^{+0.160}_{-0.185} \pm 0.075$	$-0.717^{+0.154}_{-0.158} \pm 0.074$
$P'_5$	$0.363^{+0.165}_{-0.132} \pm 0.028$	$-0.139^{+0.103}_{-0.087} \pm 0.039$	$-0.435^{+0.096}_{-0.101} \pm 0.027$
$P'_6$	$0.000^{+0.094}_{-0.097} \pm 0.021$	$0.108^{+0.075}_{-0.071} \pm 0.018$	$0.129^{+0.074}_{-0.071} \pm 0.011$
$P'_8$	$-0.157^{+0.368}_{-0.369} \pm 0.113$	$-0.727^{+0.193}_{-0.184} \pm 0.056$	$0.007^{+0.215}_{-0.216} \pm 0.036$
	$6 < q^2 < 8.68 \text{ GeV}^2$	$10.09 < q^2 < 12.86 \text{ GeV}^2$	$14.18 < q^2 < 16 \text{ GeV}^2$
$F_L$	$0.627^{+0.016}_{-0.016} \pm 0.011$	$0.474^{+0.011}_{-0.013} \pm 0.009$	$0.394^{+0.012}_{-0.012} \pm 0.009$
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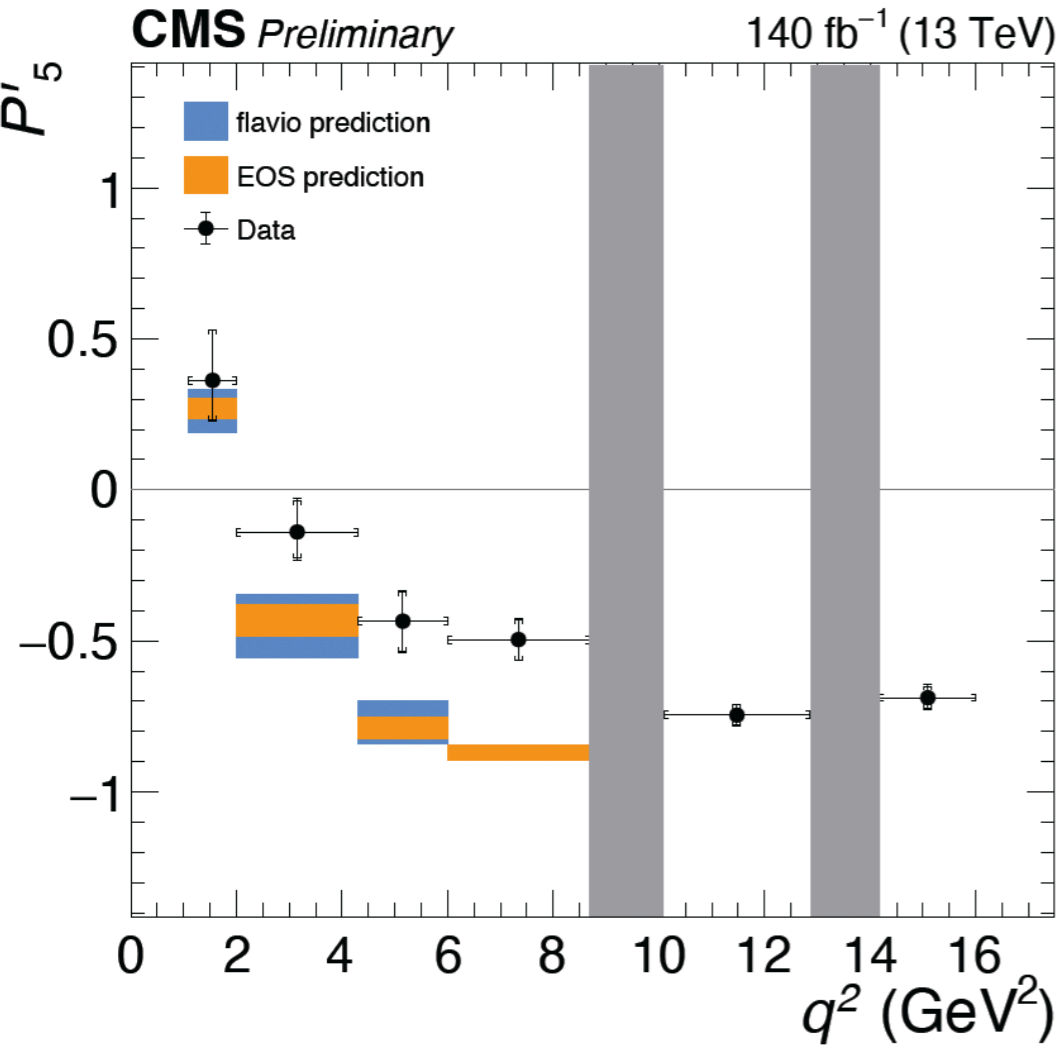
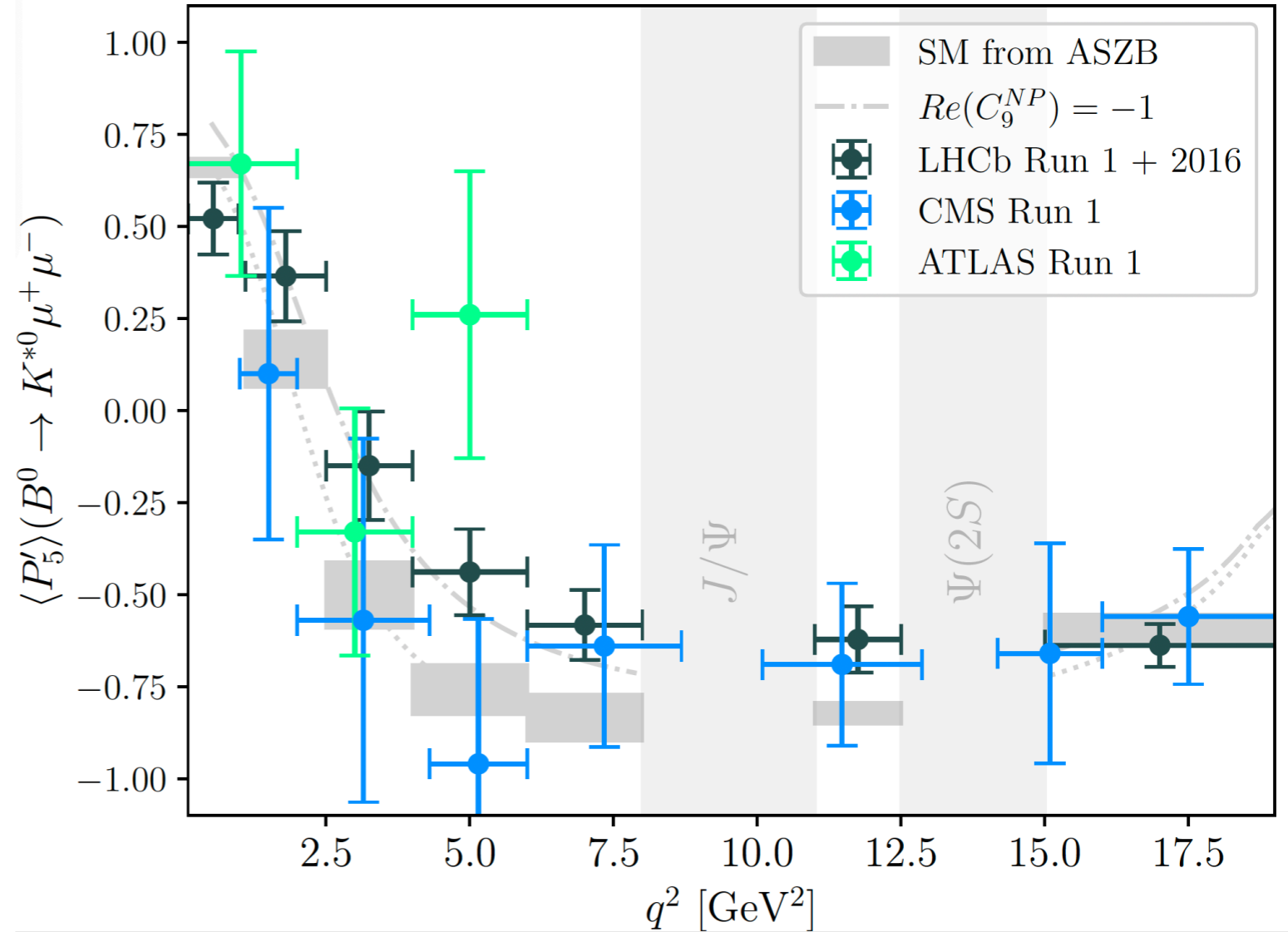


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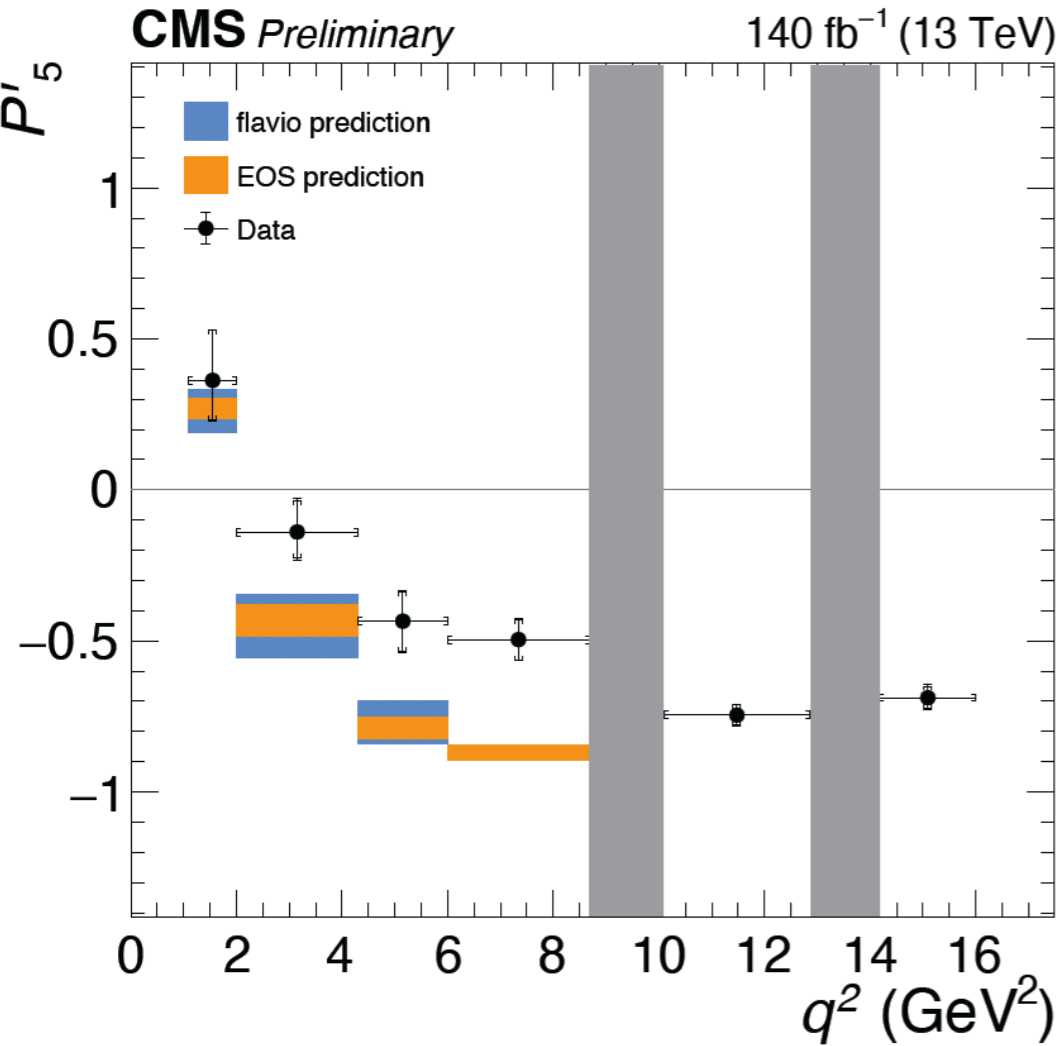
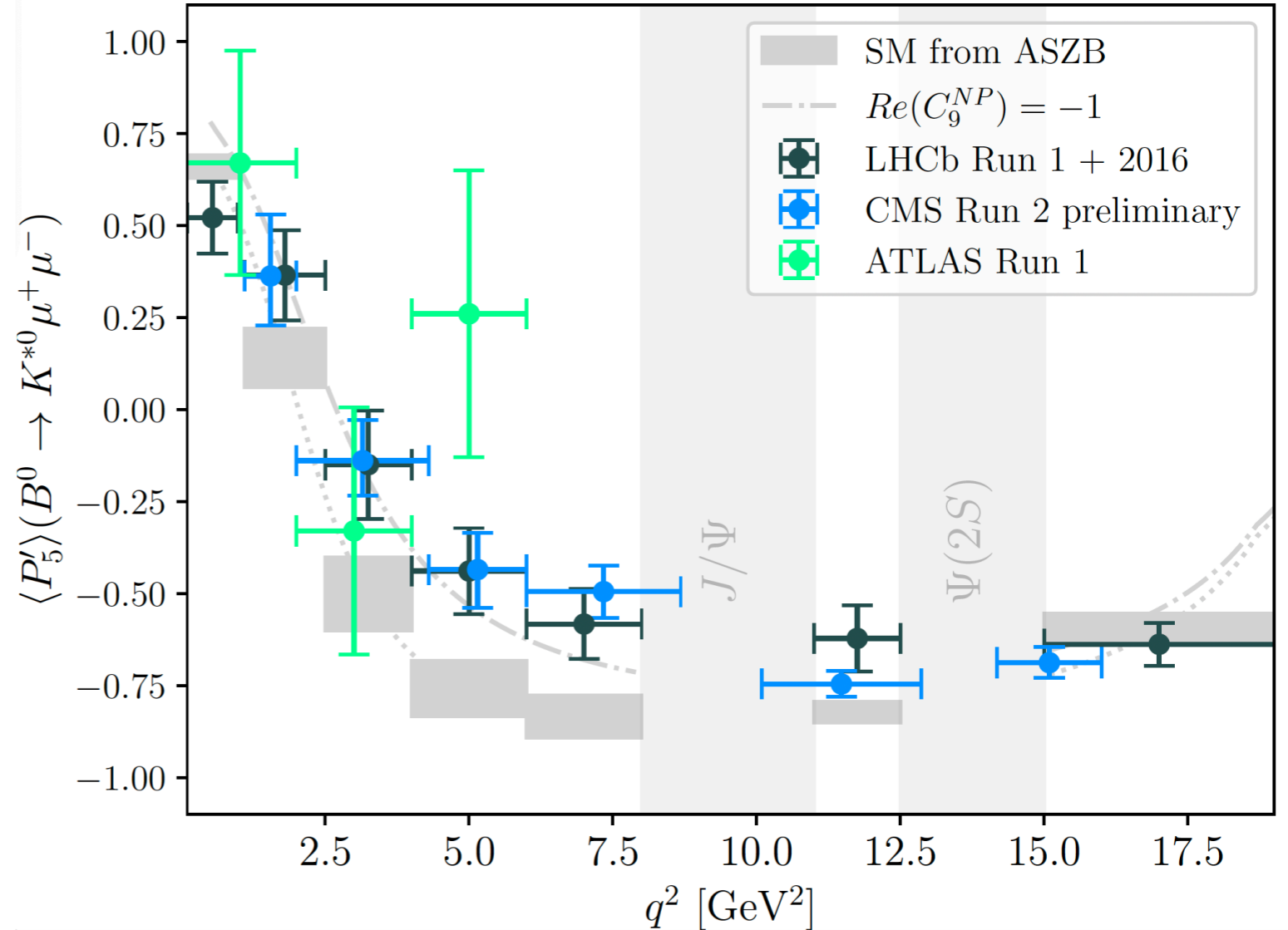
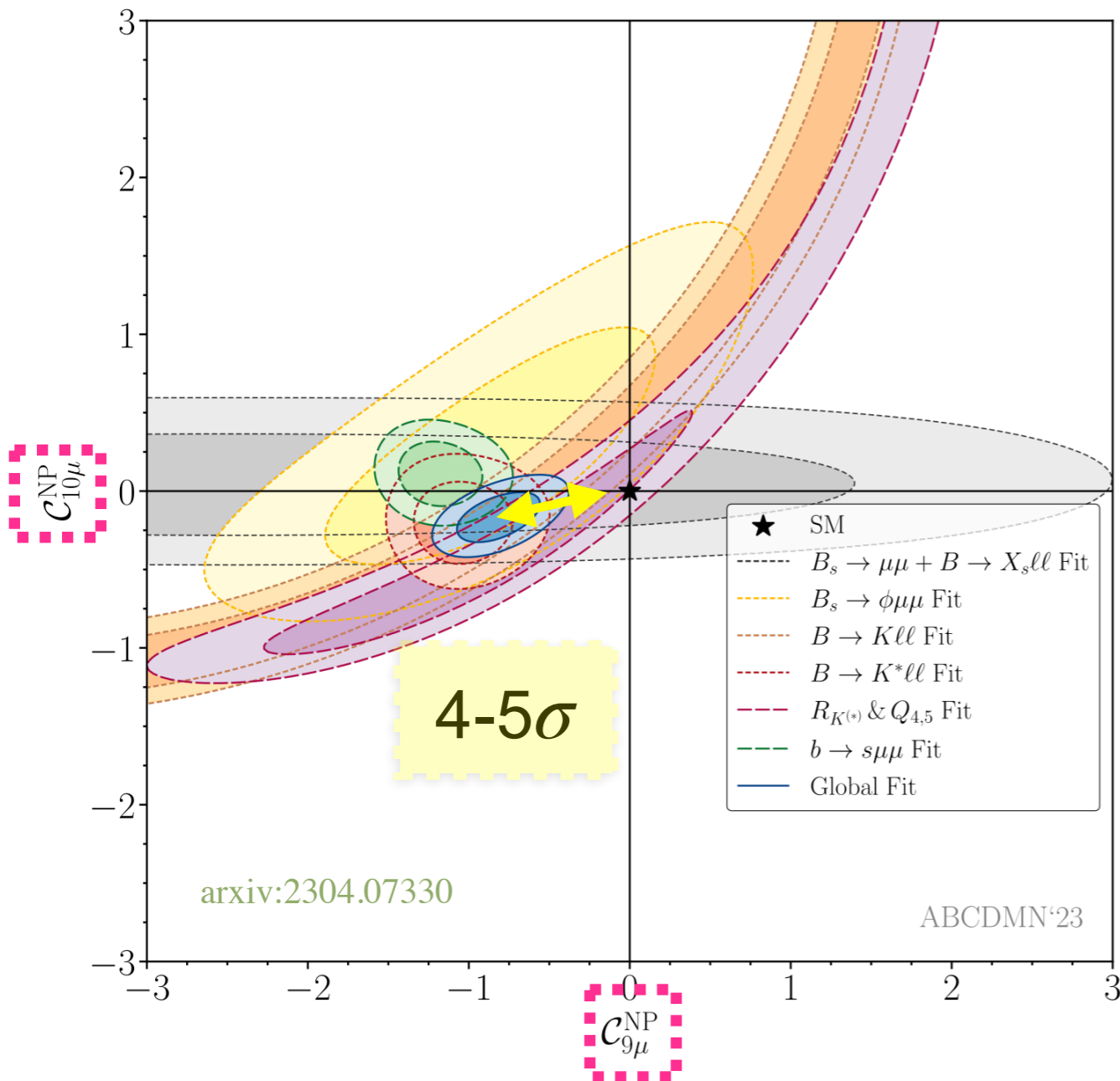


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# Global deviation from SM over all $b \rightarrow s\ell\ell$ ?



Highest experimental precision in  $b \rightarrow s\mu^+\mu^-$  decays

Combine branching fraction and angular information for all experiments and measured  $b \rightarrow s\mu^+\mu^-$  modes

Disagreement with SM at level of  $4-5\sigma$

Long-standing discrepancy- why aren't we claiming new physics?



# Hadronic cleanliness

Lepton Flavour Universality  
and  $B_s \rightarrow \mu^+ \mu^-$



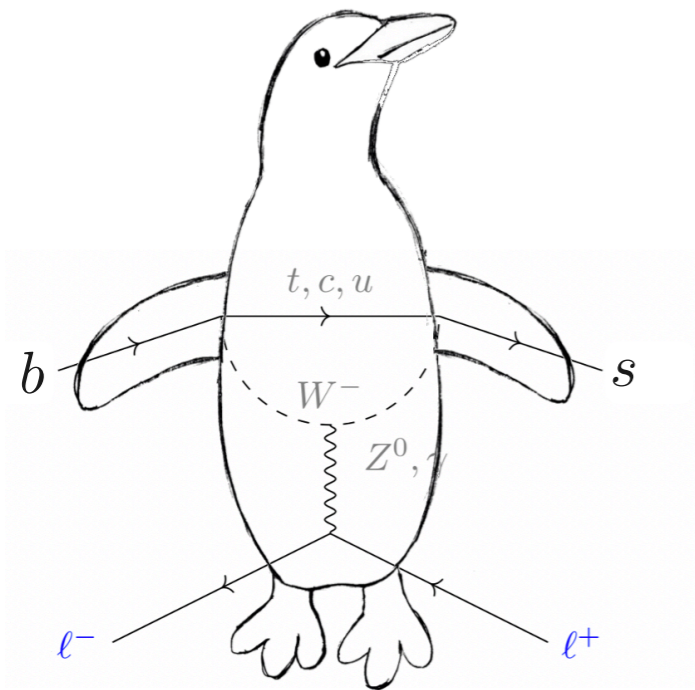
Angular analyses



Branching fractions



# Cause of anomalies?



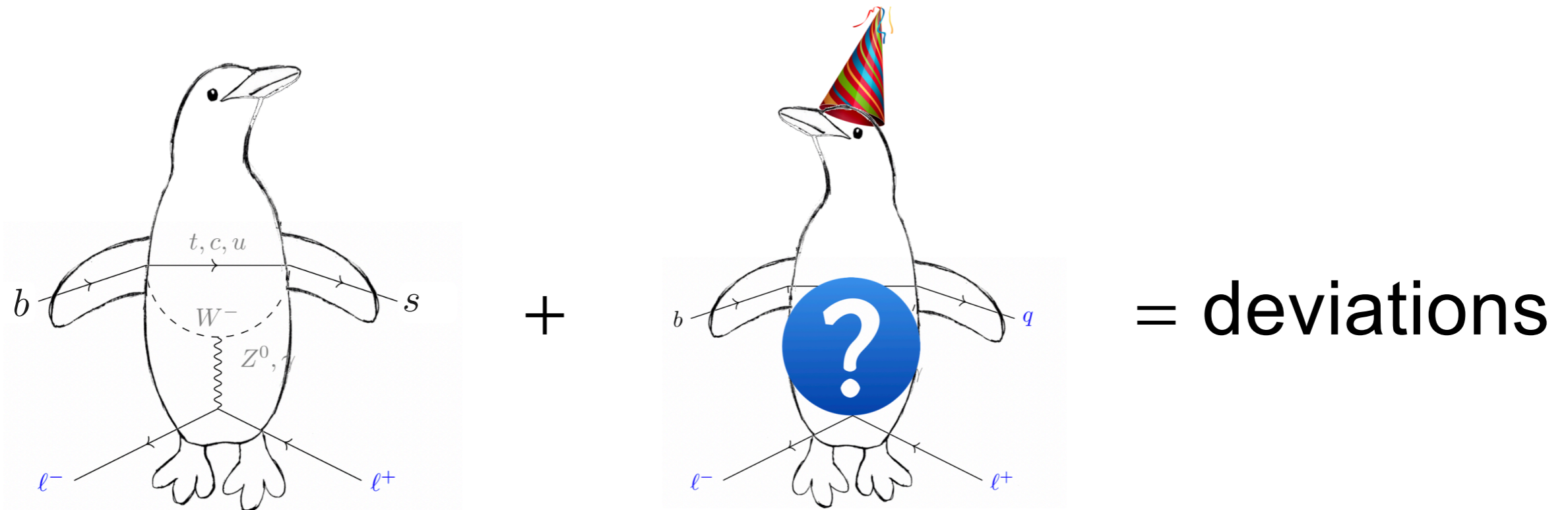
+



= deviations

# Cause of anomalies?

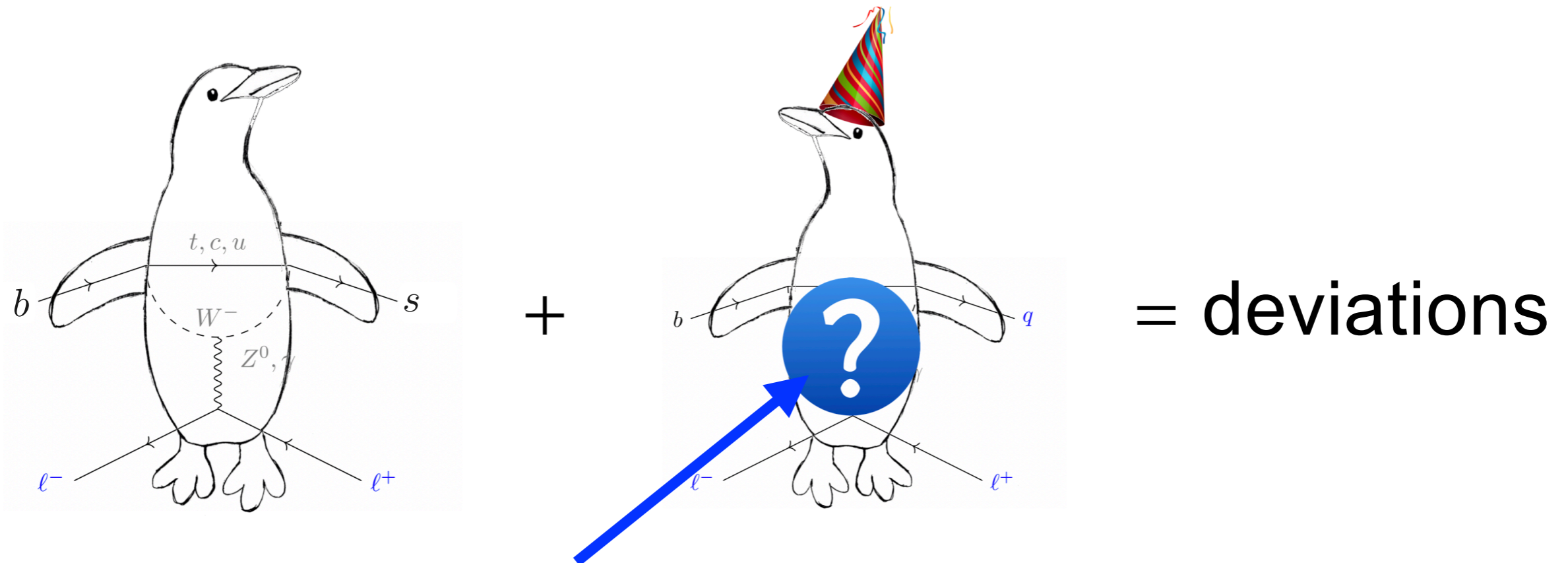
## Option 1 - New Physics



# Cause of anomalies?

## Option 1 - New Physics

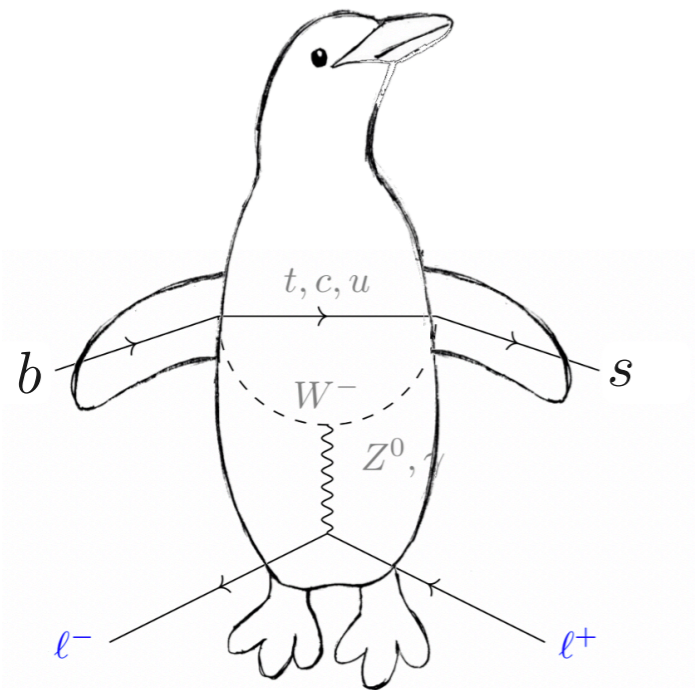
- e.g. enhancements in  $b \rightarrow s\tau^+\tau^-$  gives combined explanation for  $B$ -anomalies



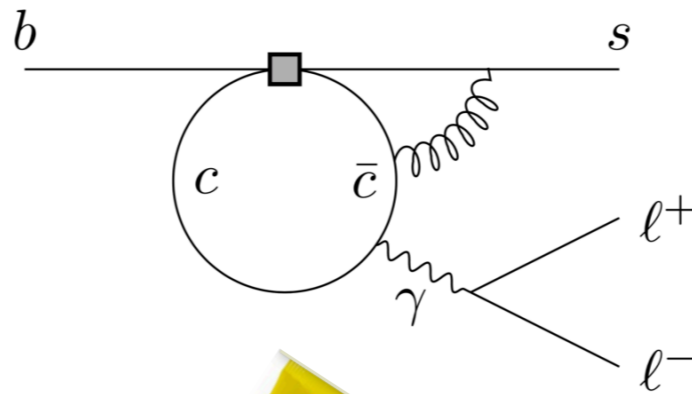
CP violating? Leptoquark?  $b \rightarrow s\tau^+\tau^-$  ?

# Cause of anomalies?

## Option 2 - misunderstood QCD processes



+



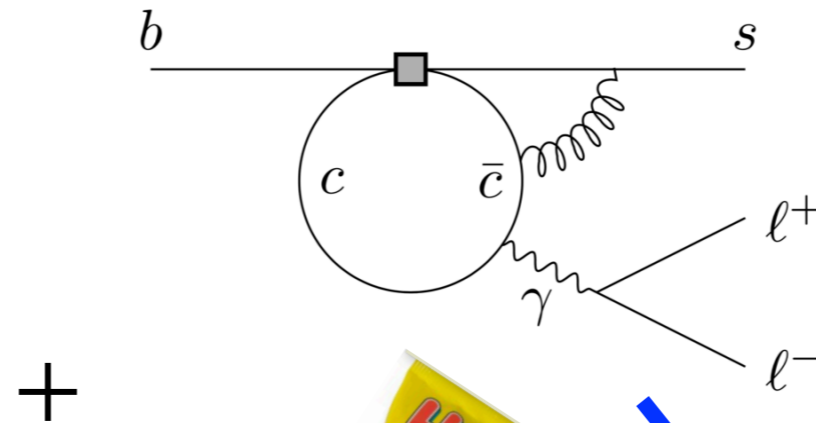
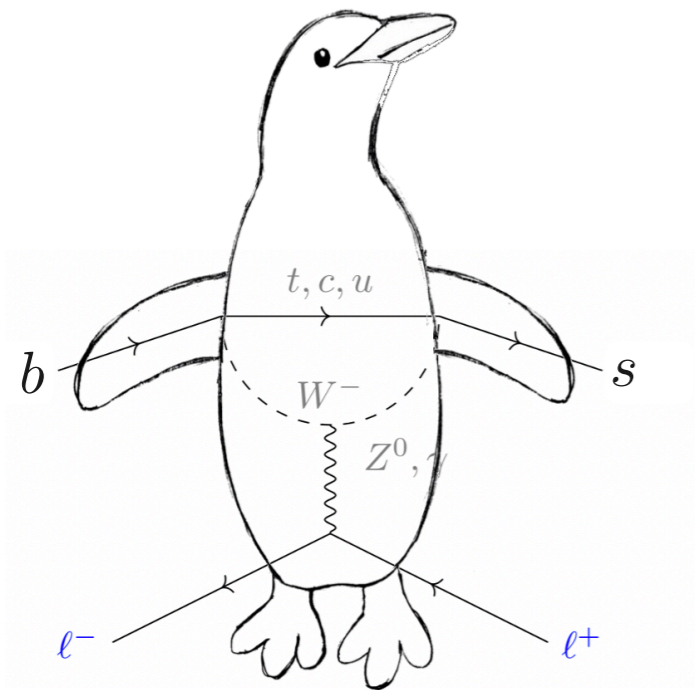
= deviations



# Cause of anomalies?

## Option 2 - misunderstood QCD processes

- $b \rightarrow sc\bar{c}[c\bar{c} \rightarrow \gamma^* \rightarrow \mu^+\mu^-]$  (charm-loops) difficult to calculate and can mimic deviations in  $C_9$

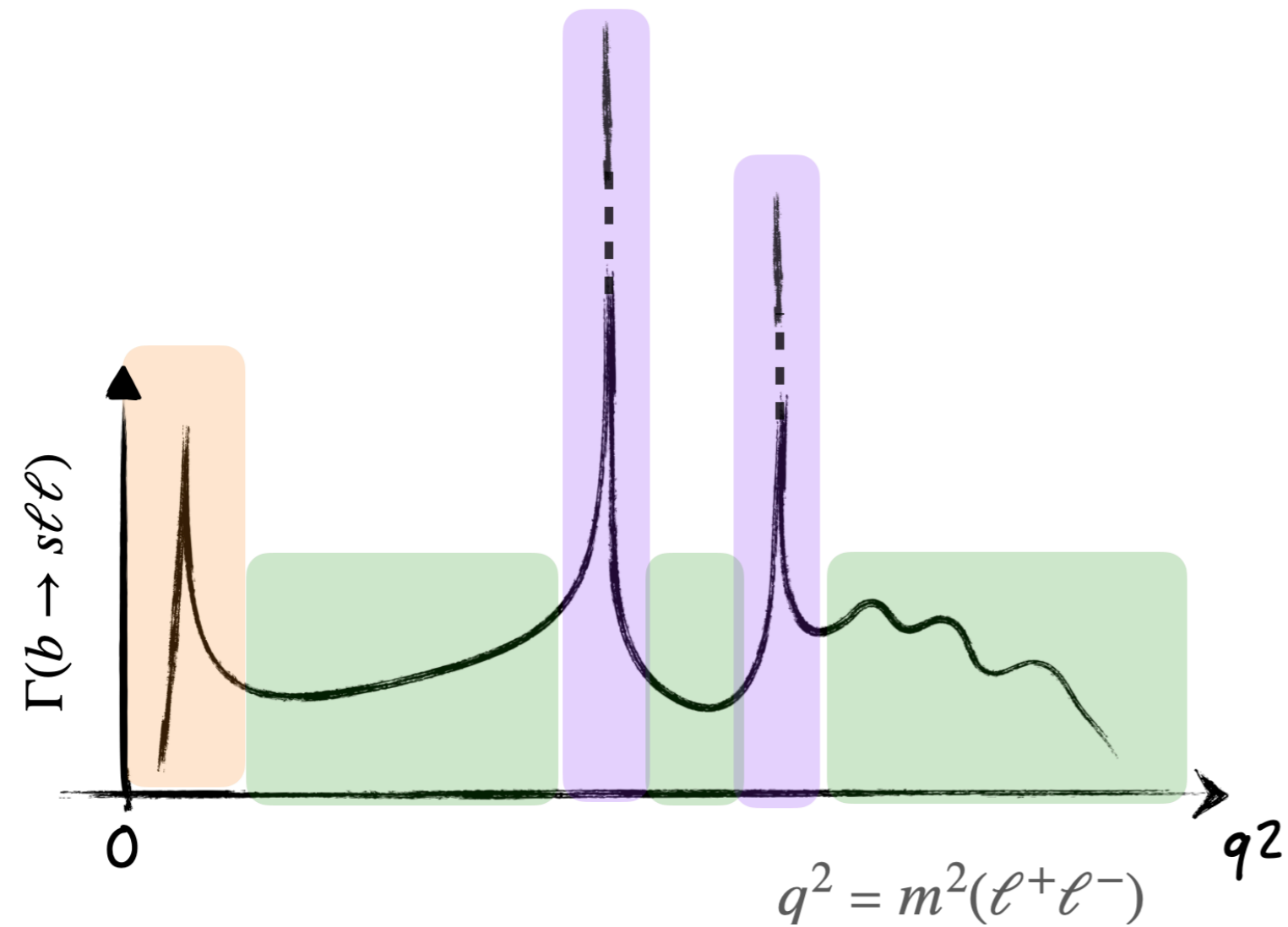


= deviations



Fit theory models to data to constrain amplitudes

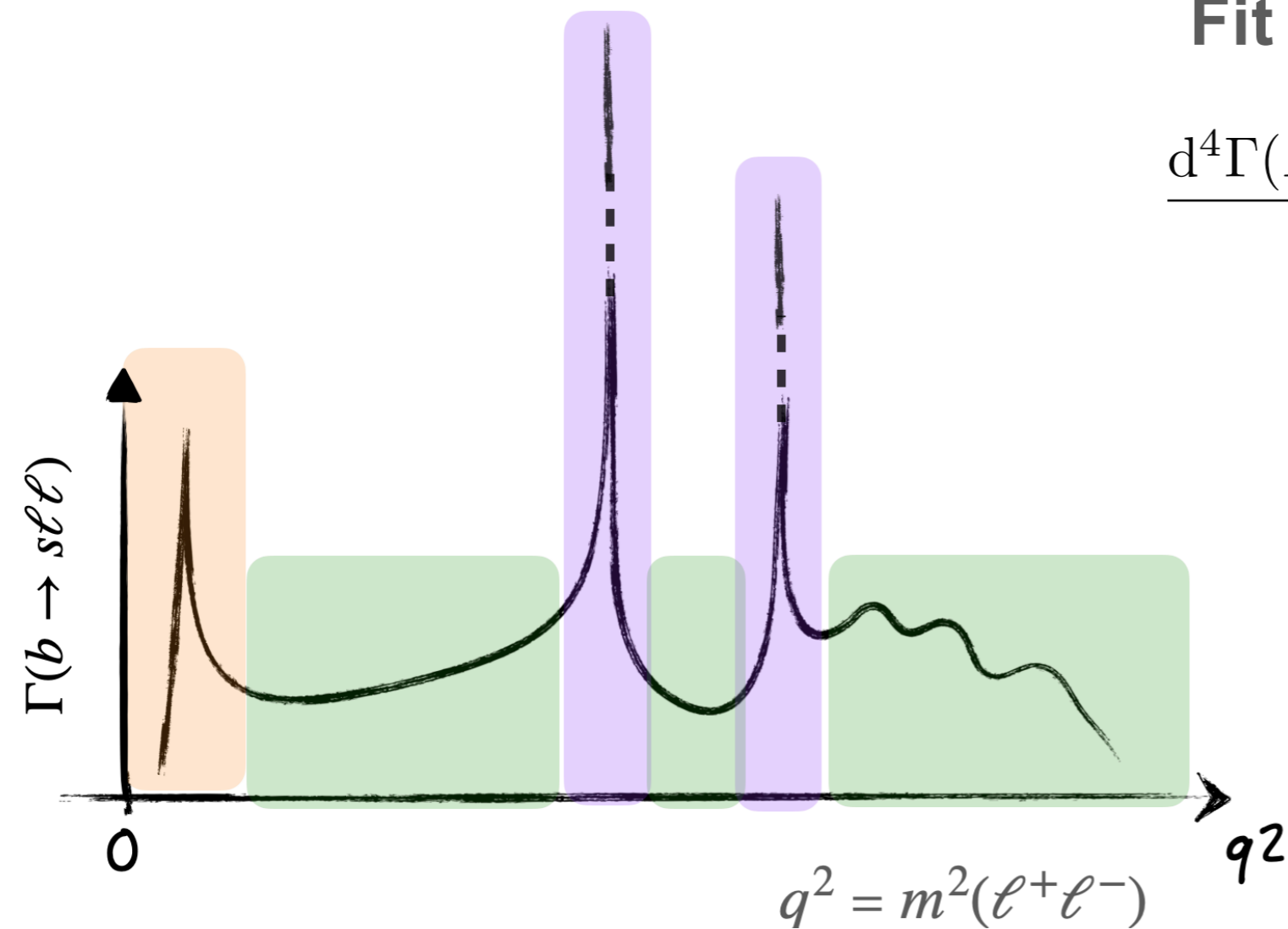
Fit  $q^2$  spectrum continuously to disentangle **long (non-local)** and **short** distance contributions to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



Fit  $q^2$  spectrum continuously to disentangle **long (non-local)** and **short** distance contributions to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

Fit the angular *and*  $q^2$  spectrum

$$\frac{d^4\Gamma(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{d\hat{\Omega}dq^2} = \sum_i \underbrace{I_i(q^2)}_{\text{long distance}} \underbrace{f_i(\Omega)}_{\text{short distance}}$$





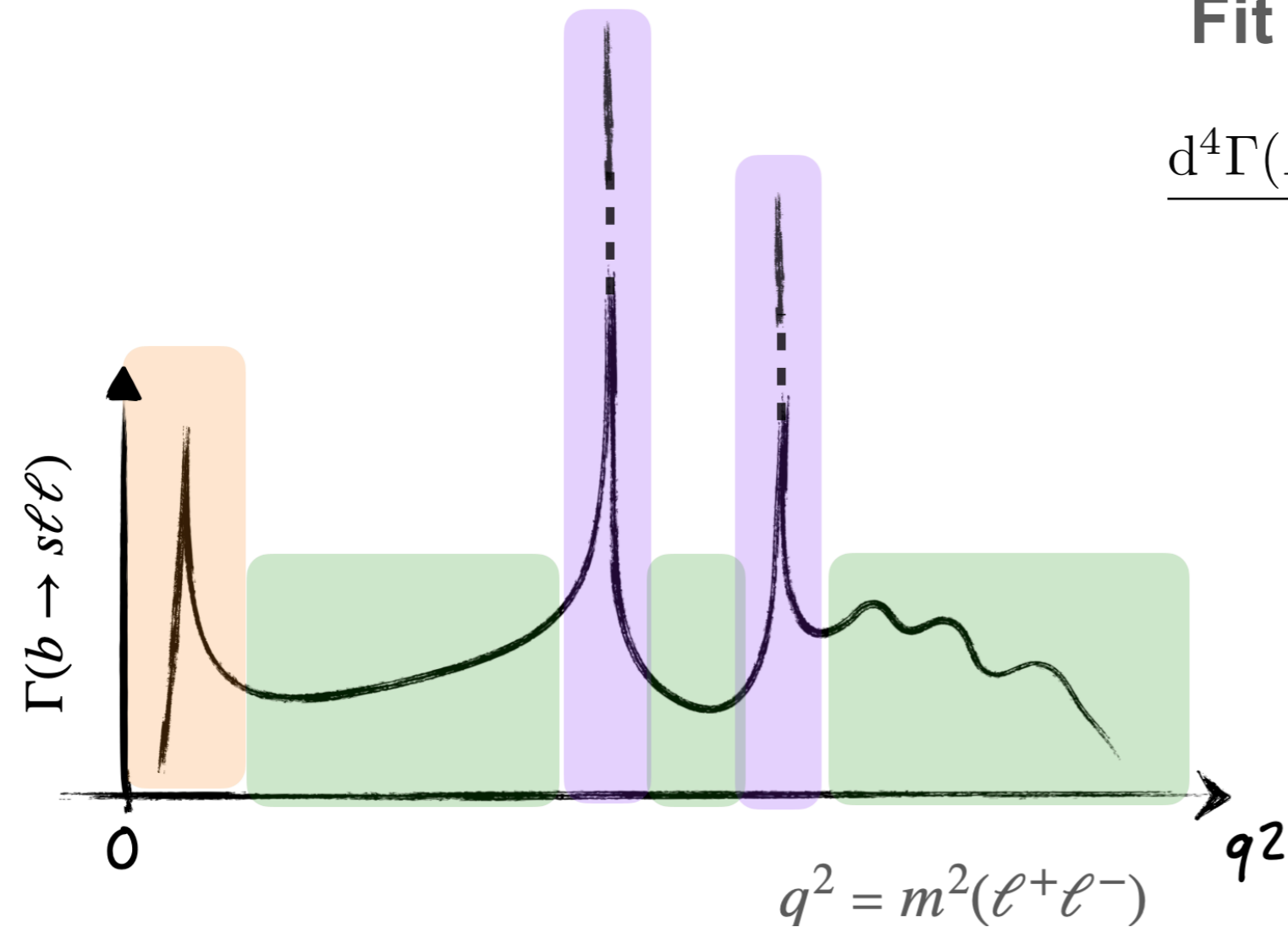
Fit  $q^2$  spectrum continuously to disentangle **long (non-local)** and **short** distance contributions to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

Fit the angular *and*  $q^2$  spectrum

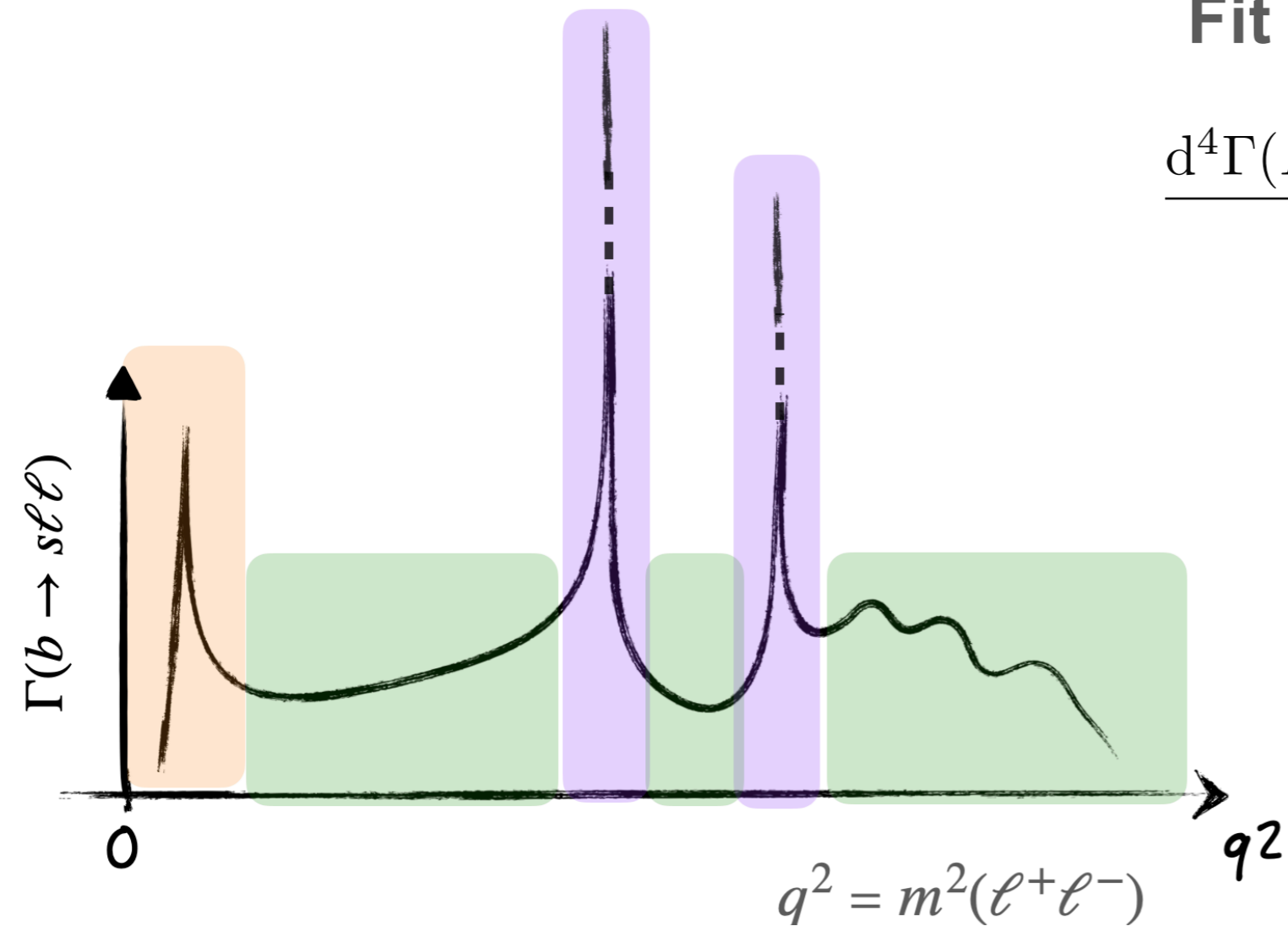
$$\frac{d^4\Gamma(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{d\hat{\Omega}dq^2} = \sum_i I_i(q^2) f_i(\Omega)$$



Combinations of  $\mathcal{A}^\lambda(q^2)$   
 $\lambda \in 0, ||, \perp$



Fit  $q^2$  spectrum continuously to disentangle **long (non-local)** and **short** distance contributions to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



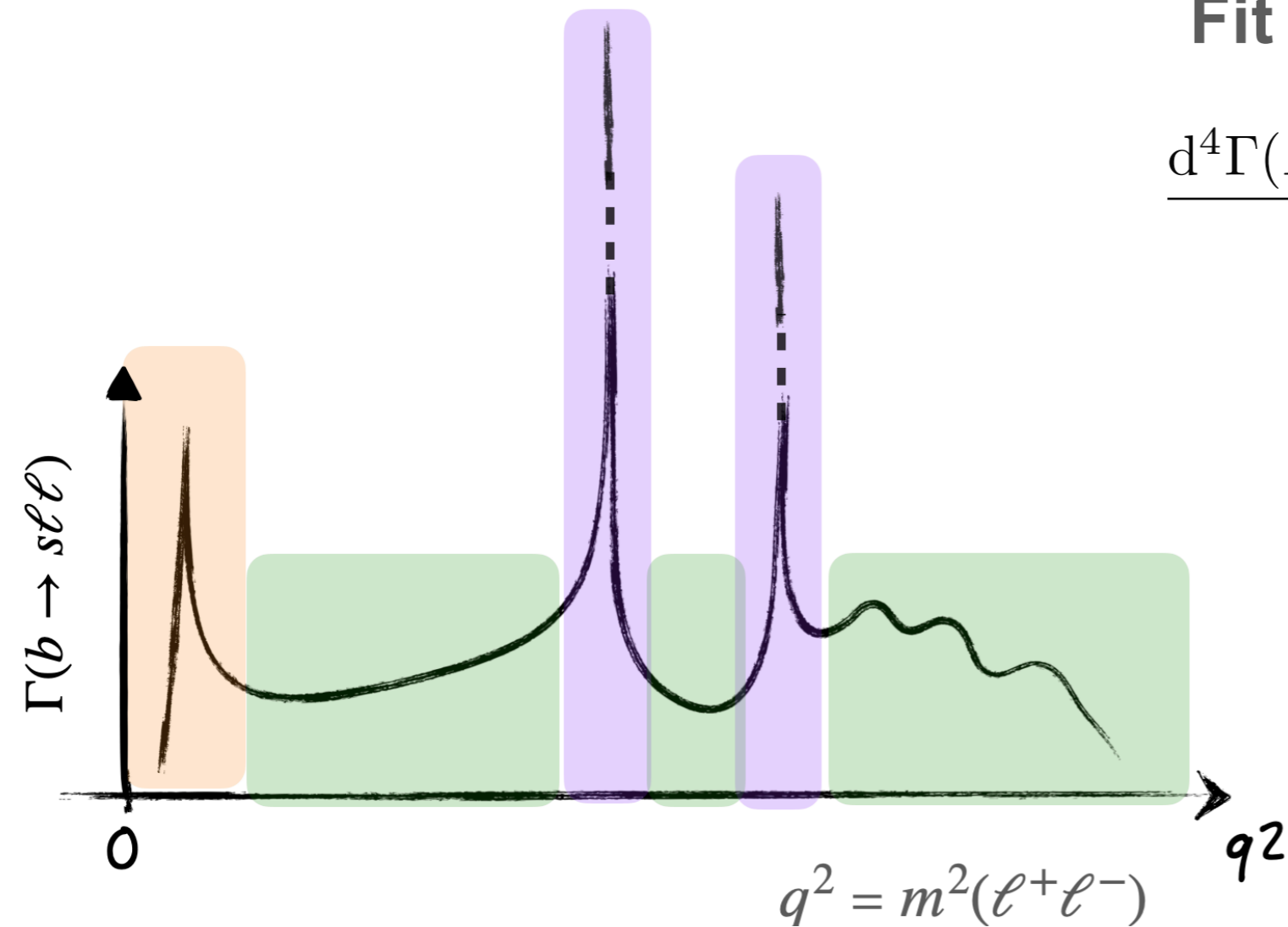
Fit the angular *and*  $q^2$  spectrum

$$\frac{d^4\Gamma(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{d\hat{\Omega}dq^2} = \sum_i I_i(q^2) f_i(\Omega)$$

Combinations of  $\mathcal{A}^\lambda(q^2)$   
 $\lambda \in 0, ||, \perp$

$\mathcal{A}^\lambda(q^2)$  depends on  
 $C_{7,9,10}$  and form factors

Fit  $q^2$  spectrum continuously to disentangle **long (non-local)** and **short** distance contributions to  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



$C_9$  (vector) is altered by non-local charm-loop

Fit the angular *and*  $q^2$  spectrum

$$\frac{d^4\Gamma(B^0 \rightarrow K^{*0} \mu^+ \mu^-)}{d\hat{\Omega}dq^2} = \sum_i I_i(q^2) f_i(\Omega)$$

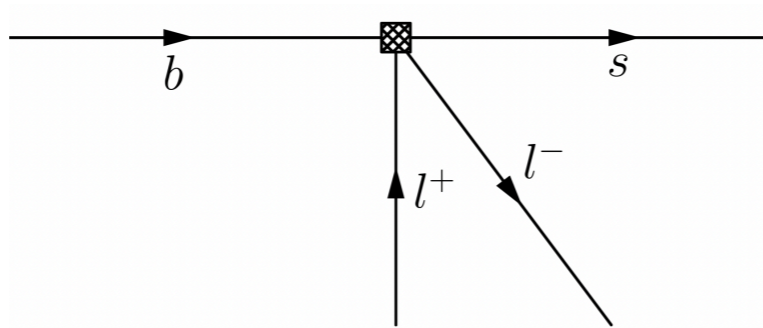
Combinations of  $\mathcal{A}^\lambda(q^2)$   
 $\lambda \in 0, ||, \perp$

$\mathcal{A}^\lambda(q^2)$  depends on  $C_{7,9,10}$  and form factors

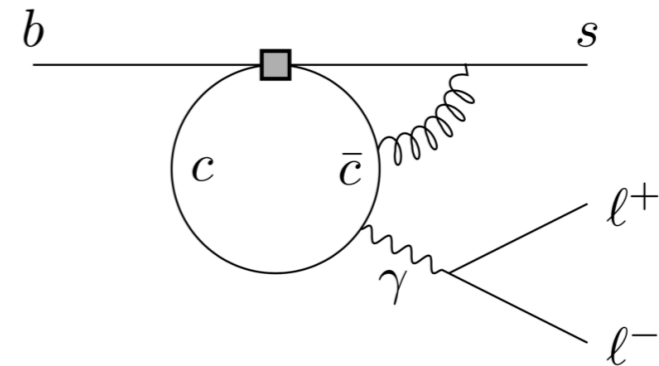
# Parameterising non-local form-factors

$\lambda \in 0, ||, \perp$

$$C_{9,\lambda}^{eff}(q^2) =$$



+



$$C_{9,\lambda}^{eff}(q^2) =$$

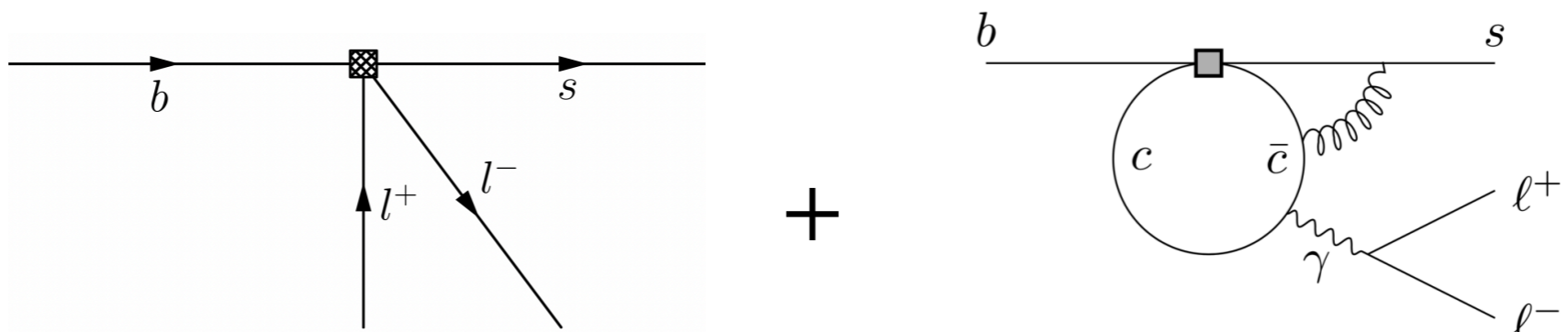
$C_9$

+

$H_\lambda(q^2)$

# Parameterising non-local form-factors

$\lambda \in 0, ||, \perp$

$$C_{9,\lambda}^{eff}(q^2) =$$


$$C_{9,\lambda}^{eff}(q^2) = C_9 + \boxed{H_\lambda(q^2)}$$

Two different analyses done, with different models for  $H_\lambda(q^2)$ :

- Z-expansion (LHCb-PAPER-2023-033,032), partial  $q^2$
- Amplitude analysis over full  $q^2$  (LHCb-PAPER-2024-011)

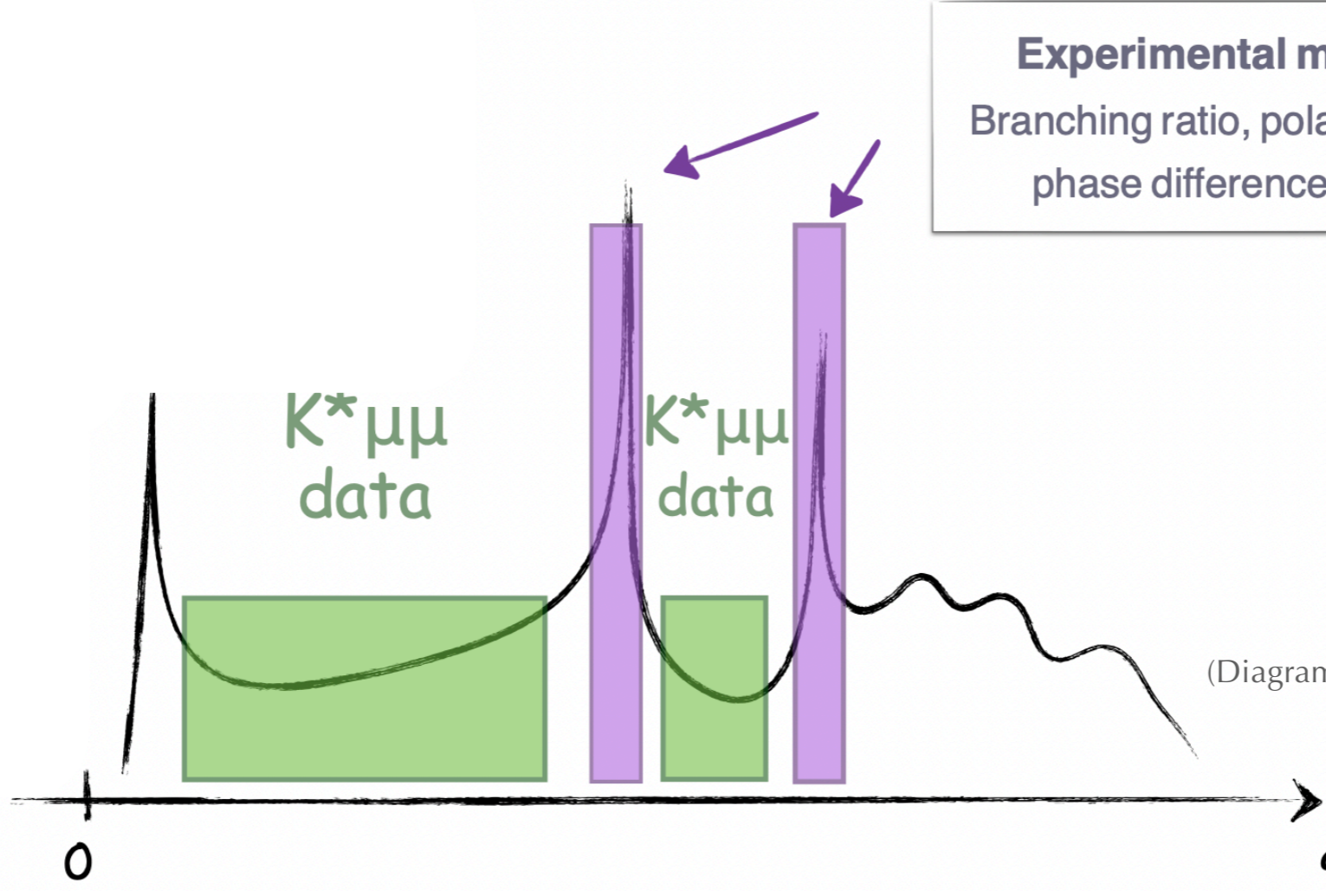
Polynomial-expansion

# Z-expansion

$$\mathcal{H}_\lambda(z) = \frac{1 - z z_{J/\psi}^*}{z - z_{J/\psi}} \frac{1 - z z_{\psi(2S)}^*}{z - z_{\psi(2S)}} \times \dots \times \sum_n \alpha_{\lambda,n} z^n$$

$z = \text{remapping of } q^2$

**Experimental measurements**  
 Branching ratio, polarization fraction and phase difference from  $B^0 \rightarrow \psi_n K^{*0}$



- PRD 76 031102(R) (2007)
- PRD 88 052002 (2013)
- PRD 88 074026 (2013)
- PRD 90 112009 (2014)

Polynomial-expansion

# Z-expansion

$$\mathcal{H}_\lambda(z) = \frac{1 - z z_{J/\psi}^*}{z - z_{J/\psi}} \frac{1 - z z_{\psi(2S)}^*}{z - z_{\psi(2S)}} \times \dots \times \sum_n \alpha_{\lambda,n} z^n$$

- 2 models used:**
- With theory info from  $\langle q^2 \rangle$  (n = 4)
  - With no theory info (n = 2)

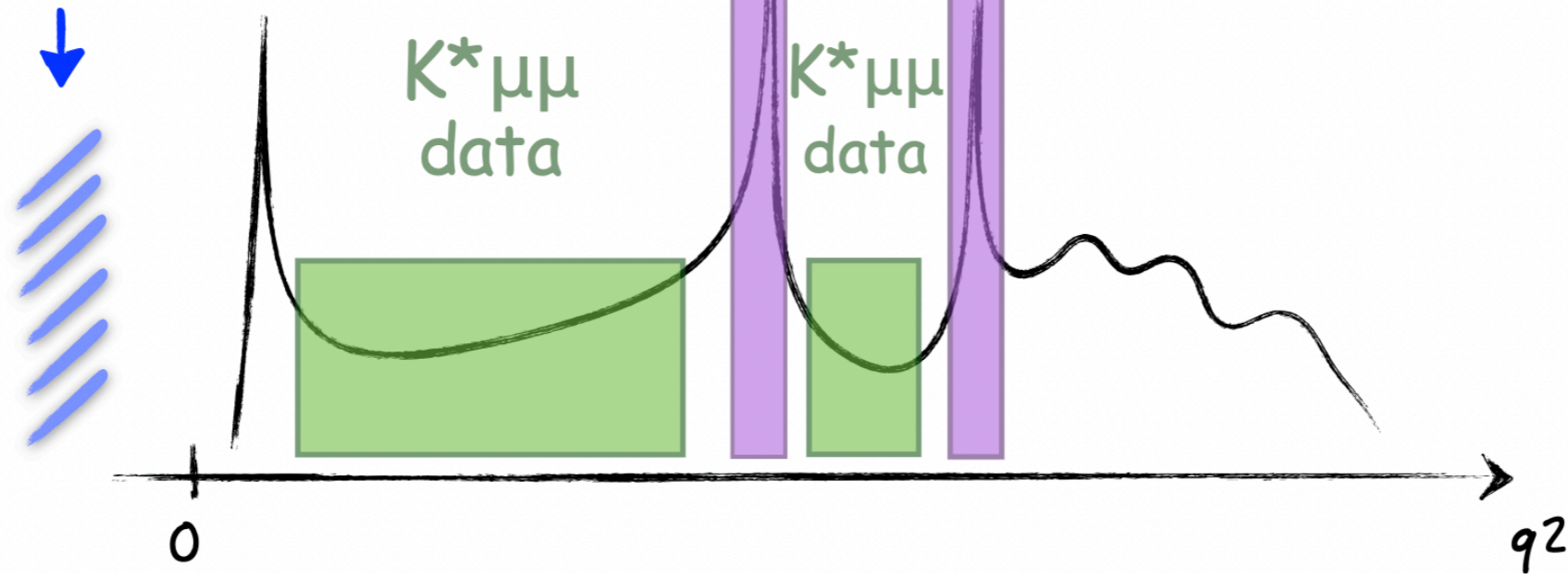
$z = \text{remapping of } q^2$

**Theory information**  
 Value of charm-loop at  $q^2 < 0$   
 ► reliable for  $q^2 \ll 4m_c^2$

**Experimental measurements**  
 Branching ratio, polarization fraction and phase difference from  $B^0 \rightarrow \psi_n K^{*0}$

PRD 76 031102(R) (2007)  
 PRD 88 052002 (2013)  
 PRD 88 074026 (2013)  
 PRD 90 112009 (2014)

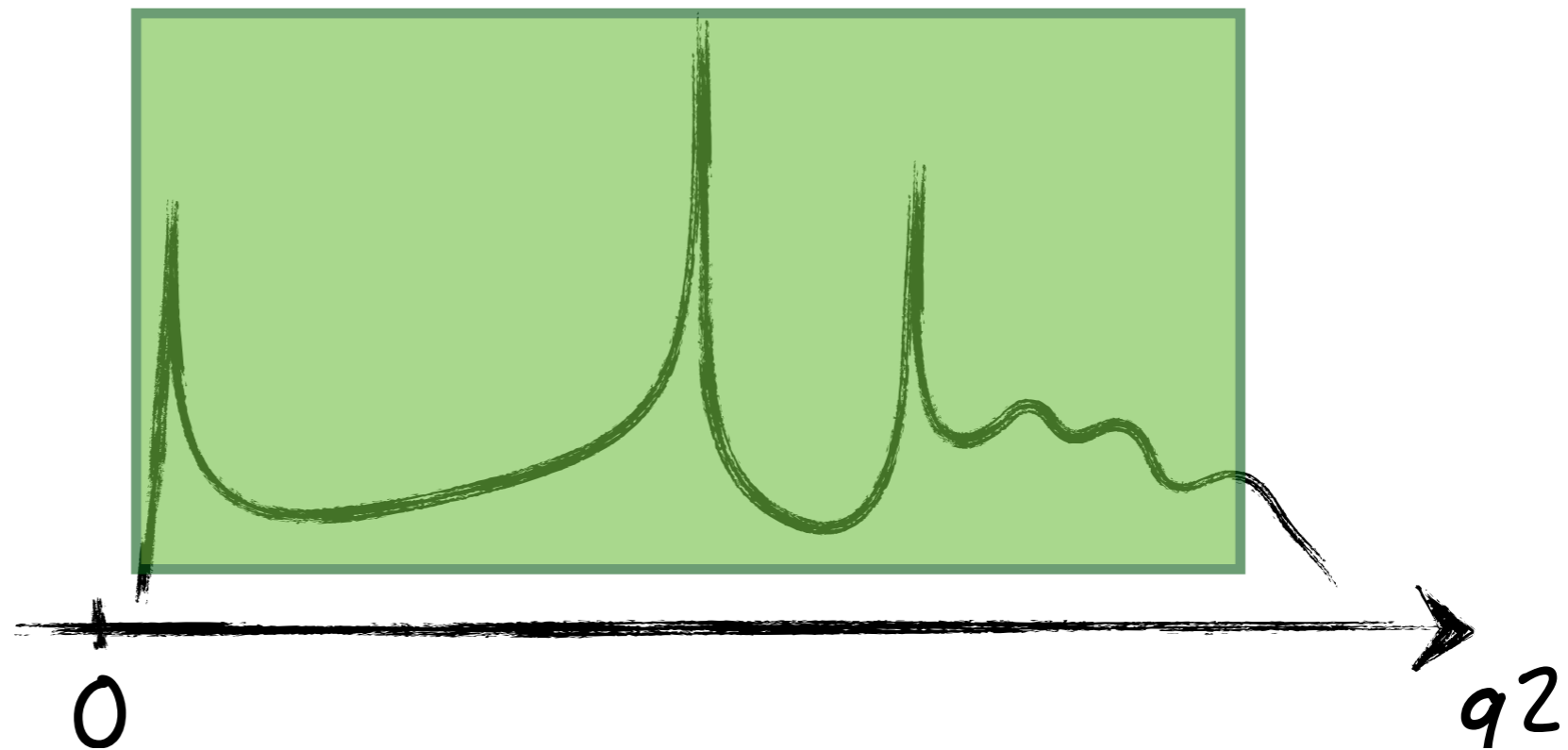
JHEP 09 (2022) 133



# Amplitude parameterisation

$$H_\lambda(q^2) = \sum_{j=\text{all possible resonances}} A_{\lambda,j} \mathcal{L}(q^2) = |A_{\lambda,j}| e^{i\delta_{j,\lambda}} \mathcal{L}(q^2)$$

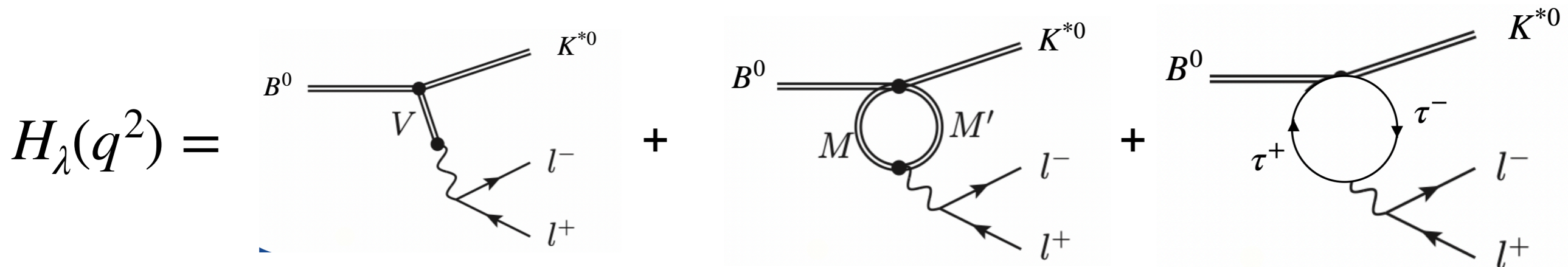
Fit full  
 $K^* \mu\mu$   
Spectrum





# Amplitude analysis over all $q^2$ - new!

$$H_\lambda(q^2) = \sum_{j=\text{all possible resonances}} A_{\lambda,j} \mathcal{L}(q^2) = |A_{\lambda,j}| e^{i\delta_{j,\lambda}} \mathcal{L}(q^2)$$



## 1-particle contributions

Includes:

$\omega(782)$ ,  $\psi(2S)$ ,  
 $\rho(770)$ ,  $\psi(3770)$ ,  
 $\phi(1020)$ ,  $\psi(4040)$ ,  
 $J/\psi$ ,  $\psi(4160)$

## 2-particle contributions

Includes:

$D\bar{D}$ ,  
 $D^*\bar{D}$ ,  
 $D^*\bar{D}^*$

## Tau loop contribution

Sensitive to  $C_9^\tau$

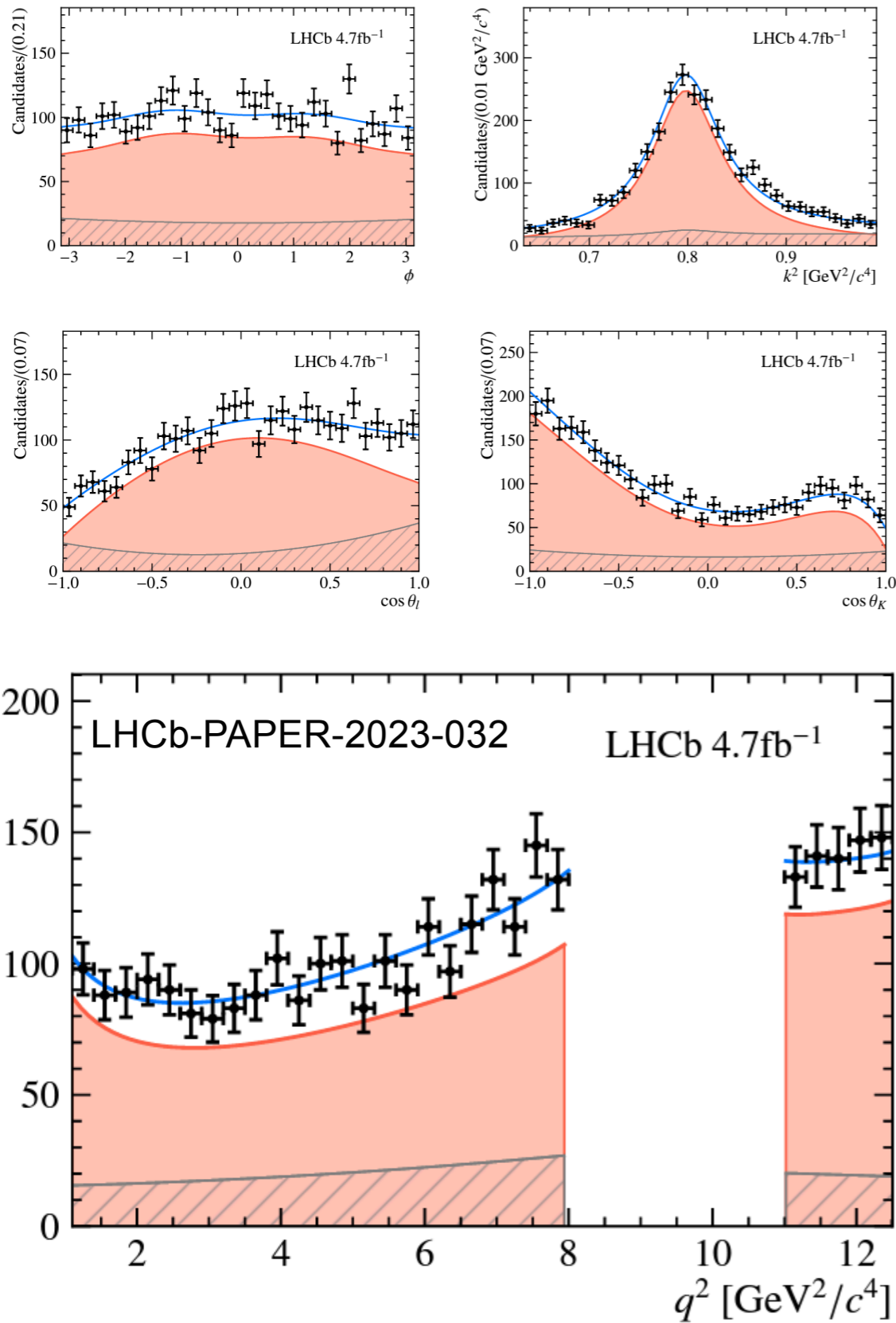
$\mathcal{L} = \text{Breit} - \text{Wigner}$

$\mathcal{L} = \text{Dispersion} - \text{relation}$

# Fit projections

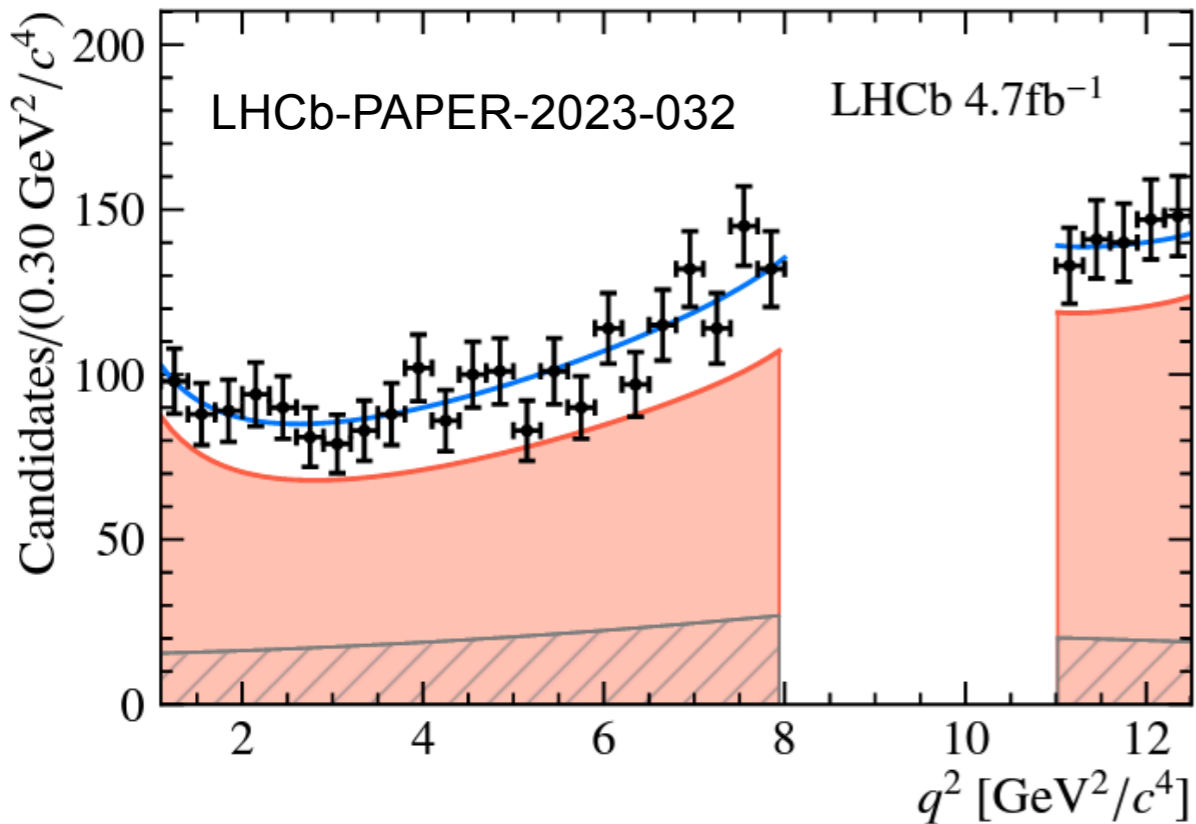
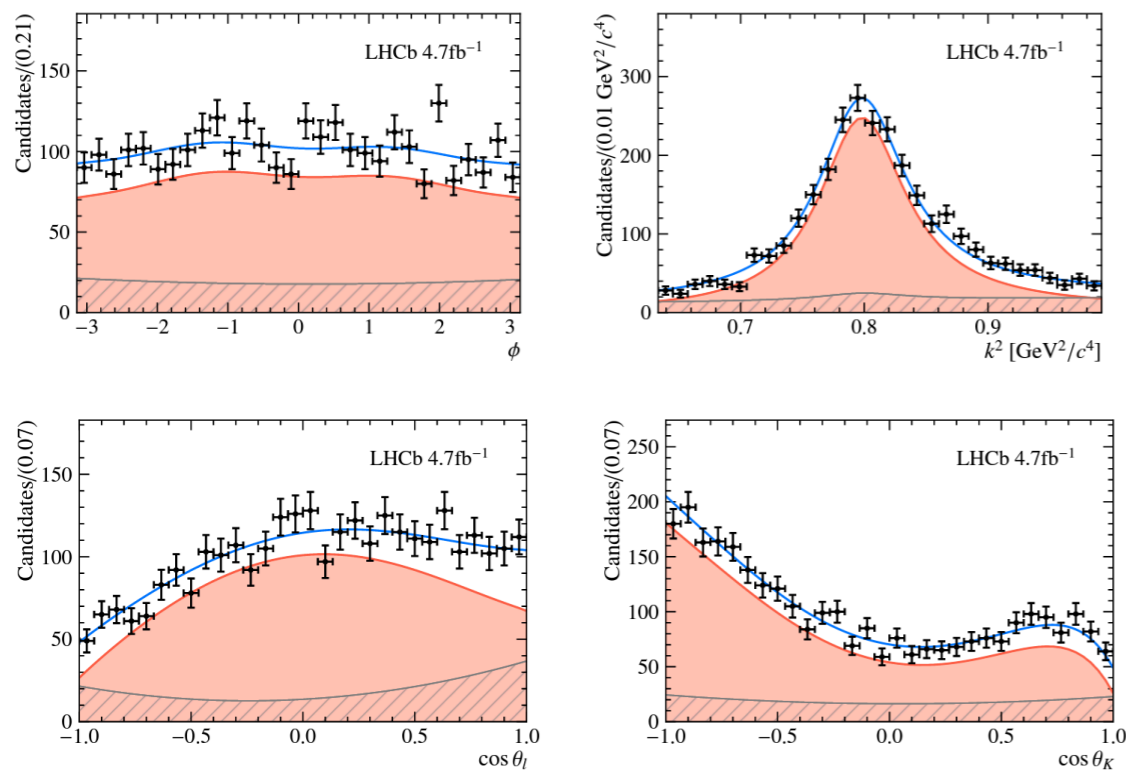
Z-expansion

Amplitude model

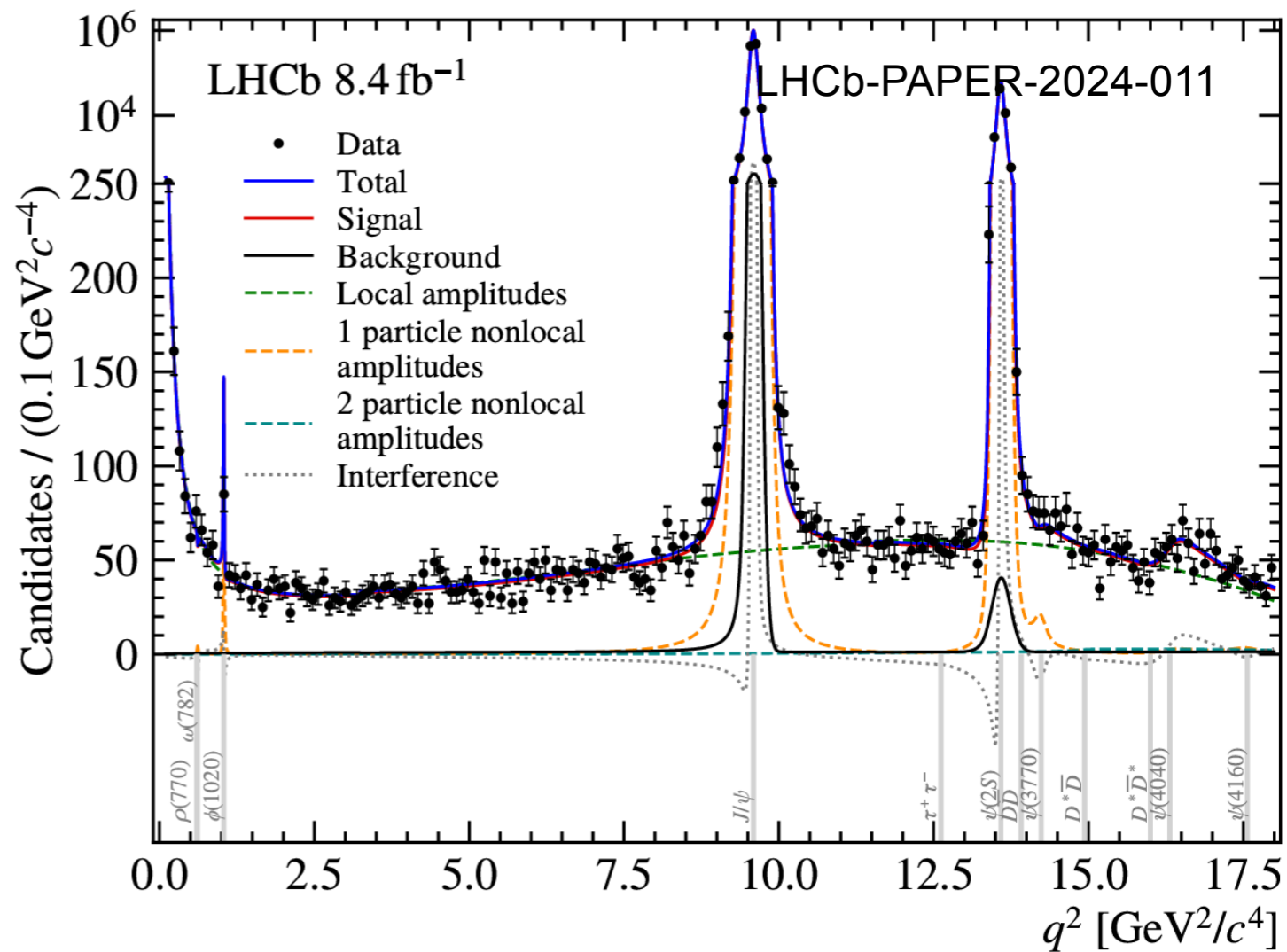
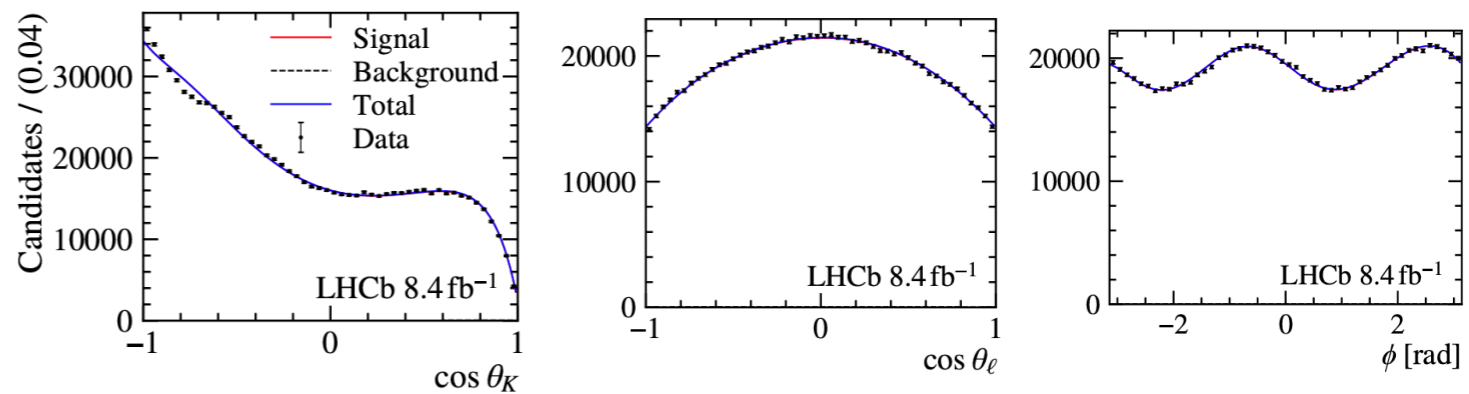


# Fit projections

Z-expansion

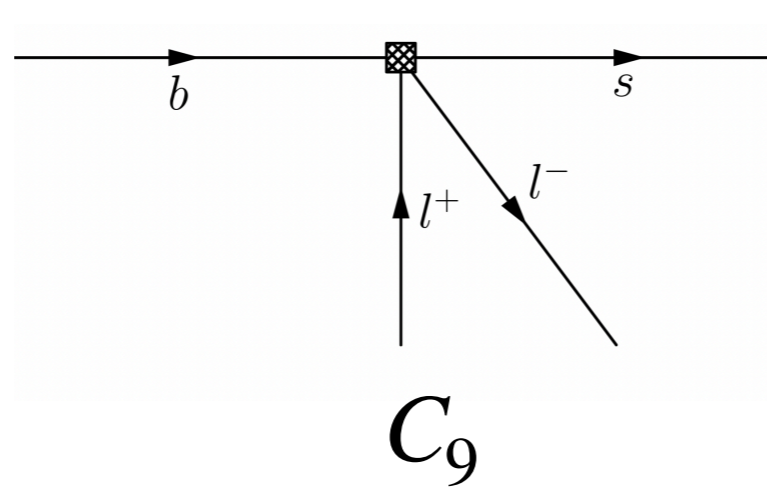


Amplitude model

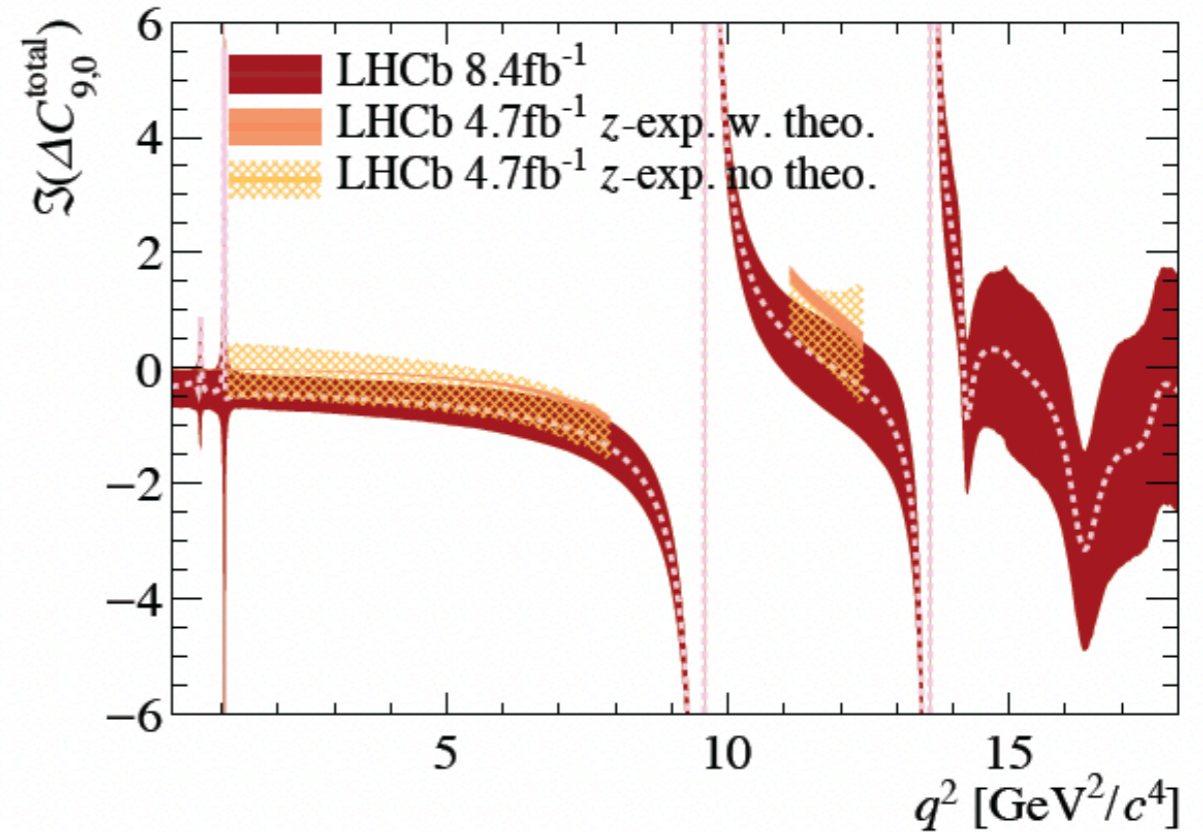
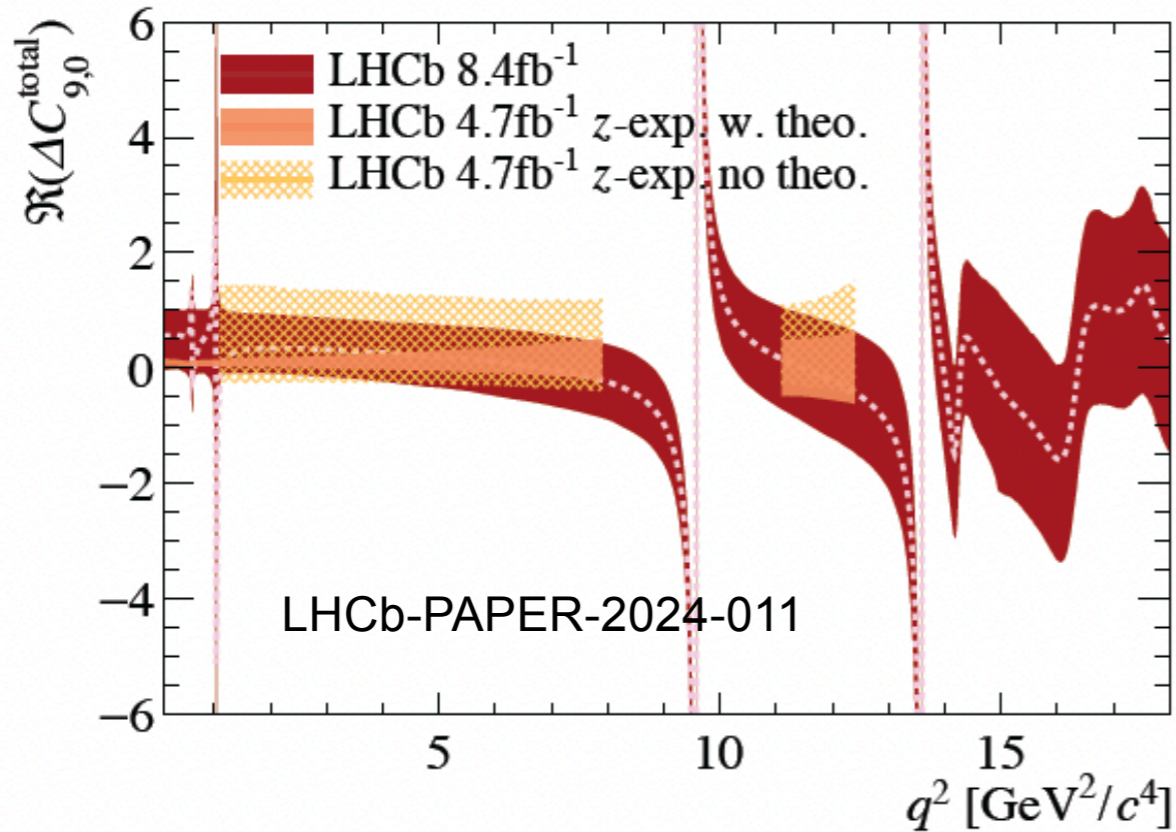
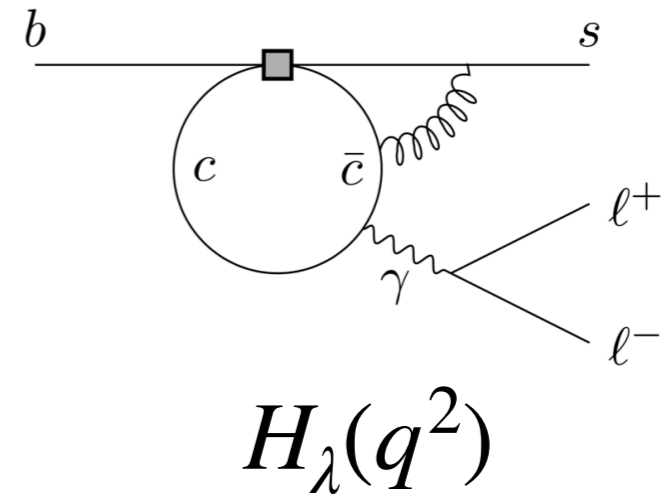


# Size of $H_\lambda(q^2)$ ?

$$C_{9,\lambda}^{eff}(q^2) =$$

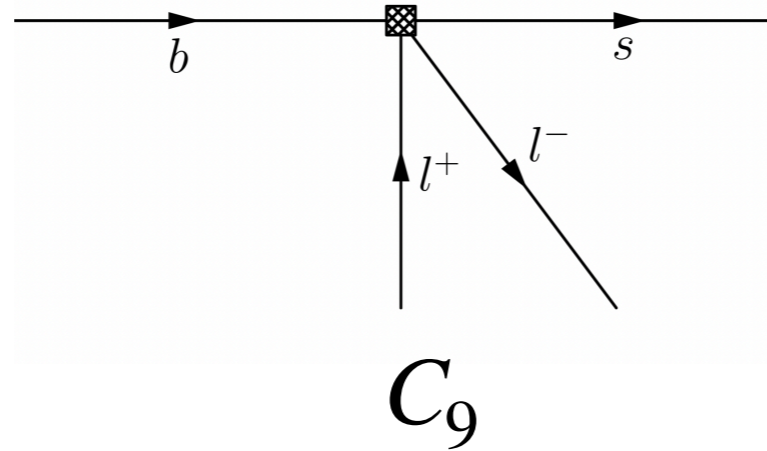


+

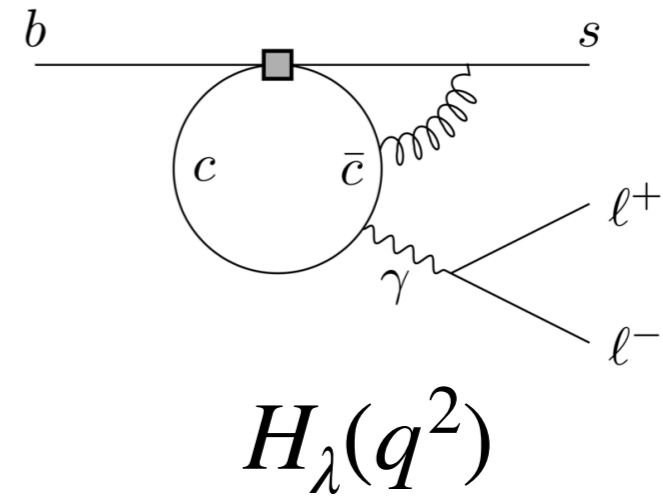


# Size of $H_\lambda(q^2)$ ?

$$C_{9,\lambda}^{eff}(q^2) =$$

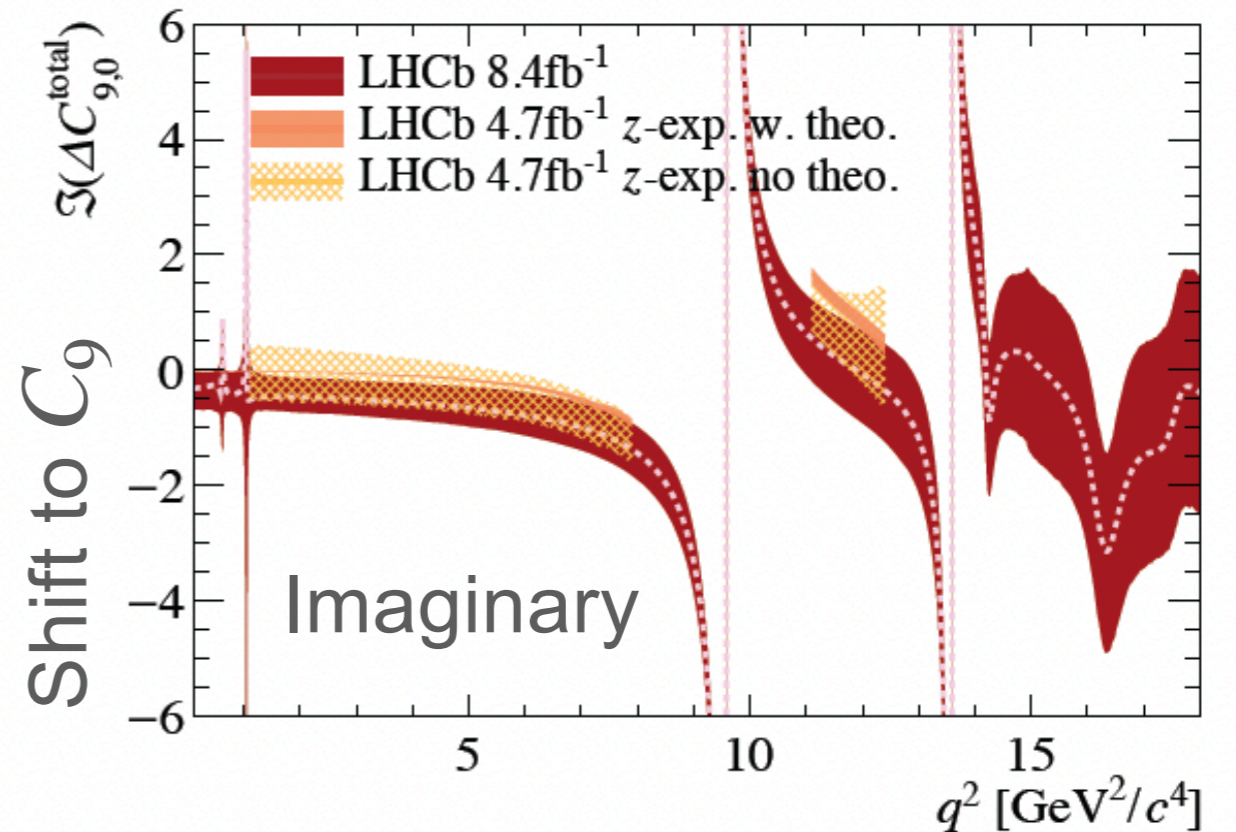
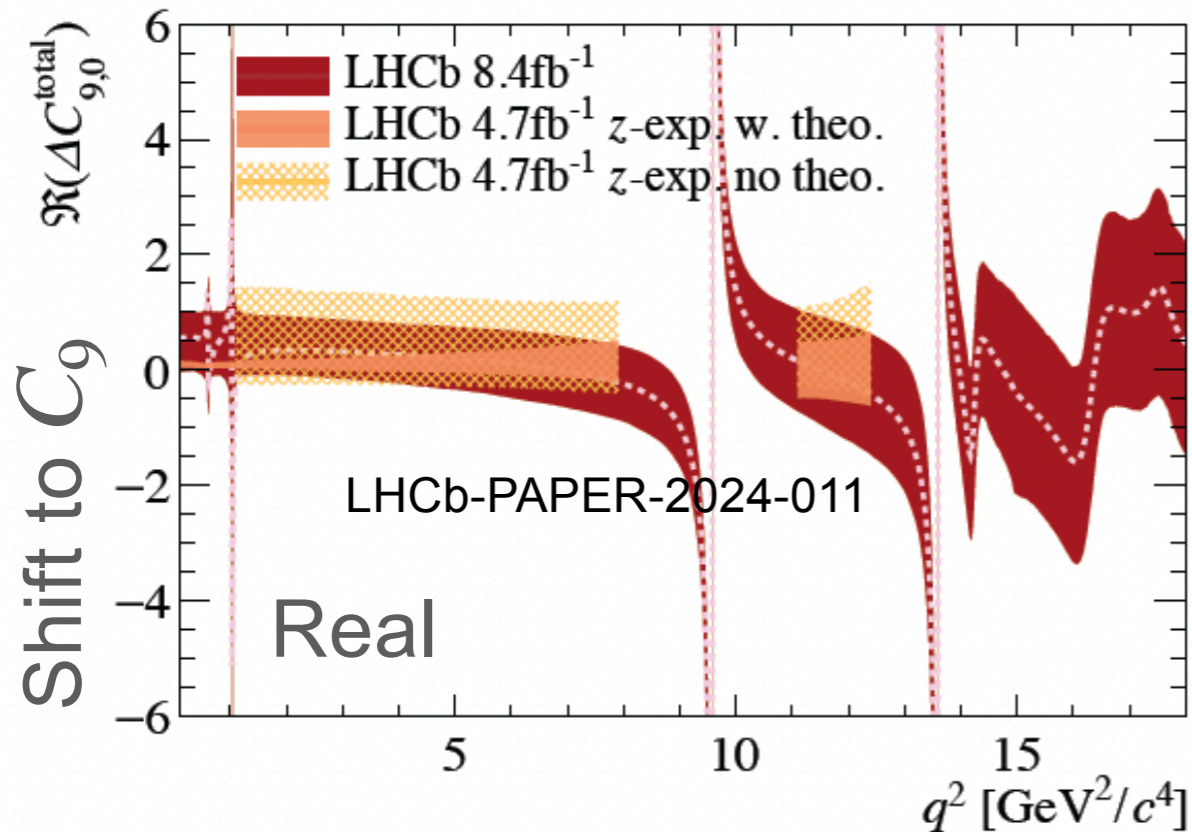


+



*Z-expansion Amplitude*

Example  $\lambda = 0$



Measured values of  $C_9$  ?

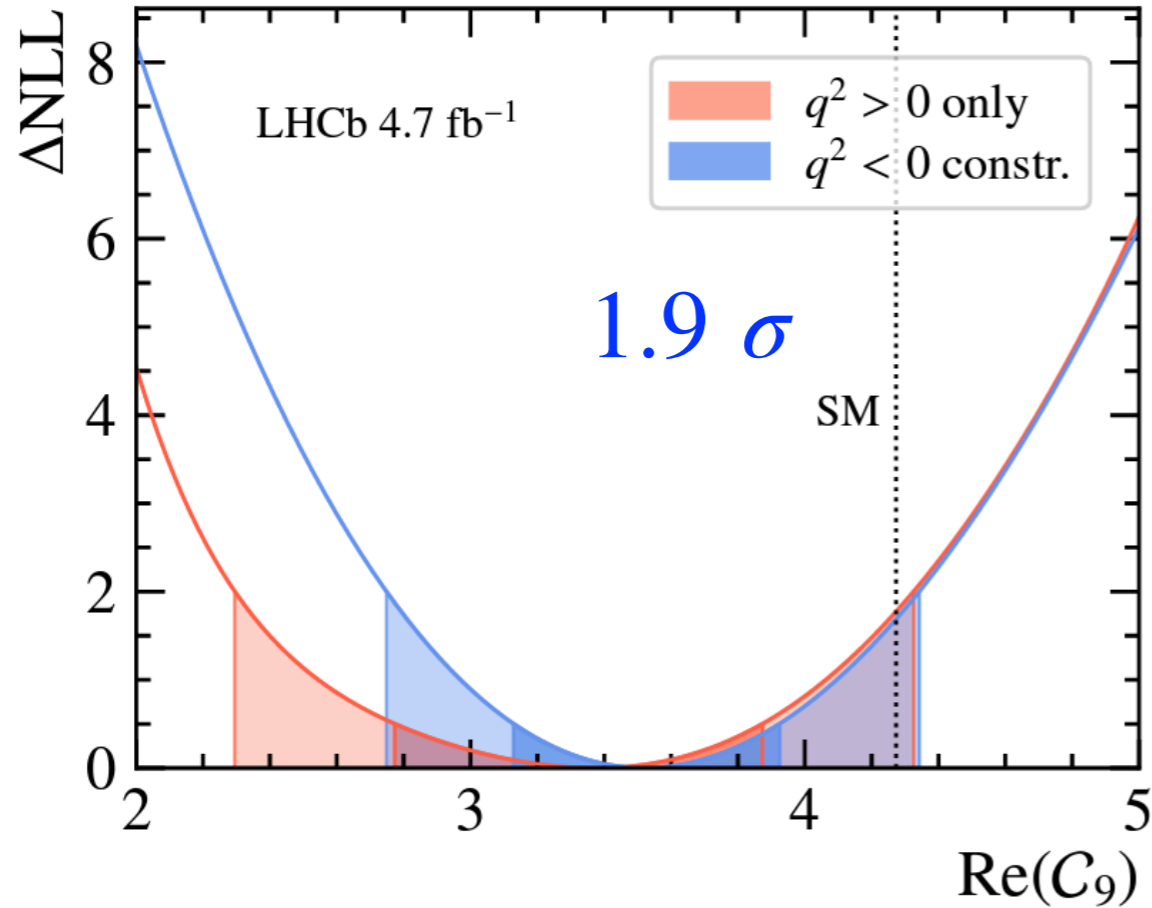
# Measured values of $C_9$ ?

LHCb-PAPER-2023-032

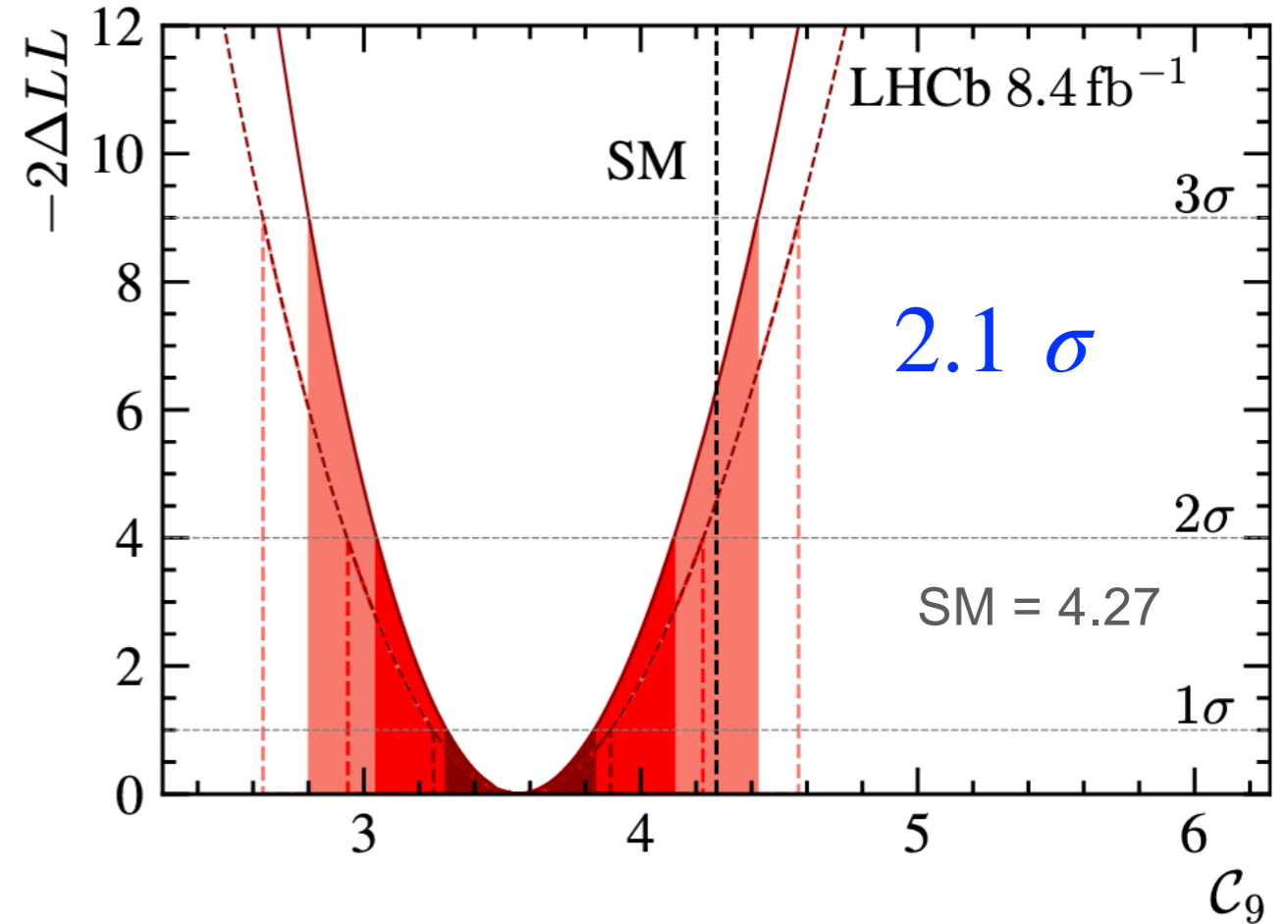
LHCb-PAPER-2024-011

*Z-expansion*

*Amplitude model*



$$\Delta C_9^{NP} = -0.93^{+0.53}_{-0.57}$$



$$\Delta C_9^{NP} = -0.71 \pm 0.33$$

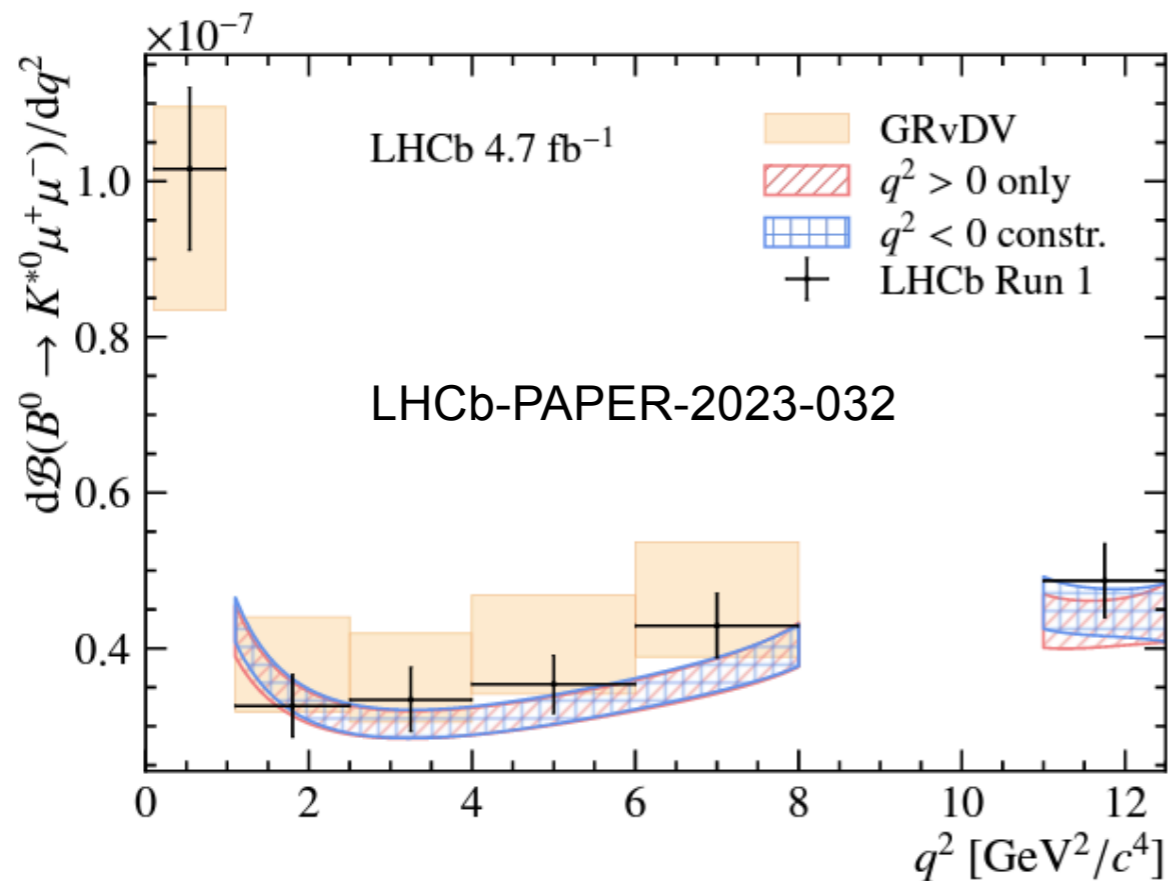
	best fit value	$q^2 > 0$ only		SM value	deviation from SM
		68% C.I.	95% C.I.		
$C_9$	3.34	[ 2.77, 3.87]	[ 2.30, 4.33]	4.27	1.9 $\sigma$
$C_{10}$	-3.69	[-4.00, -3.40]	[-4.33, -3.12]	-4.17	1.5 $\sigma$
$C'_9$	0.48	[-0.07, 0.97]	[-0.62, 1.45]	0	0.9 $\sigma$
$C'_{10}$	0.38	[ 0.13, 0.66]	[-0.14, 0.92]	0	1.5 $\sigma$

Wilson Coefficient results	
$C_9$	$3.56 \pm 0.28 \pm 0.18$
$C_{10}$	$-4.02 \pm 0.18 \pm 0.16$
$C'_9$	$0.28 \pm 0.41 \pm 0.12$
$C'_{10}$	$-0.09 \pm 0.21 \pm 0.06$
$C_{9\tau}$	$(-1.0 \pm 2.6 \pm 1.0) \times 10^2$

# Affect of non-local contributions on branching fractions?

## Z-expansion

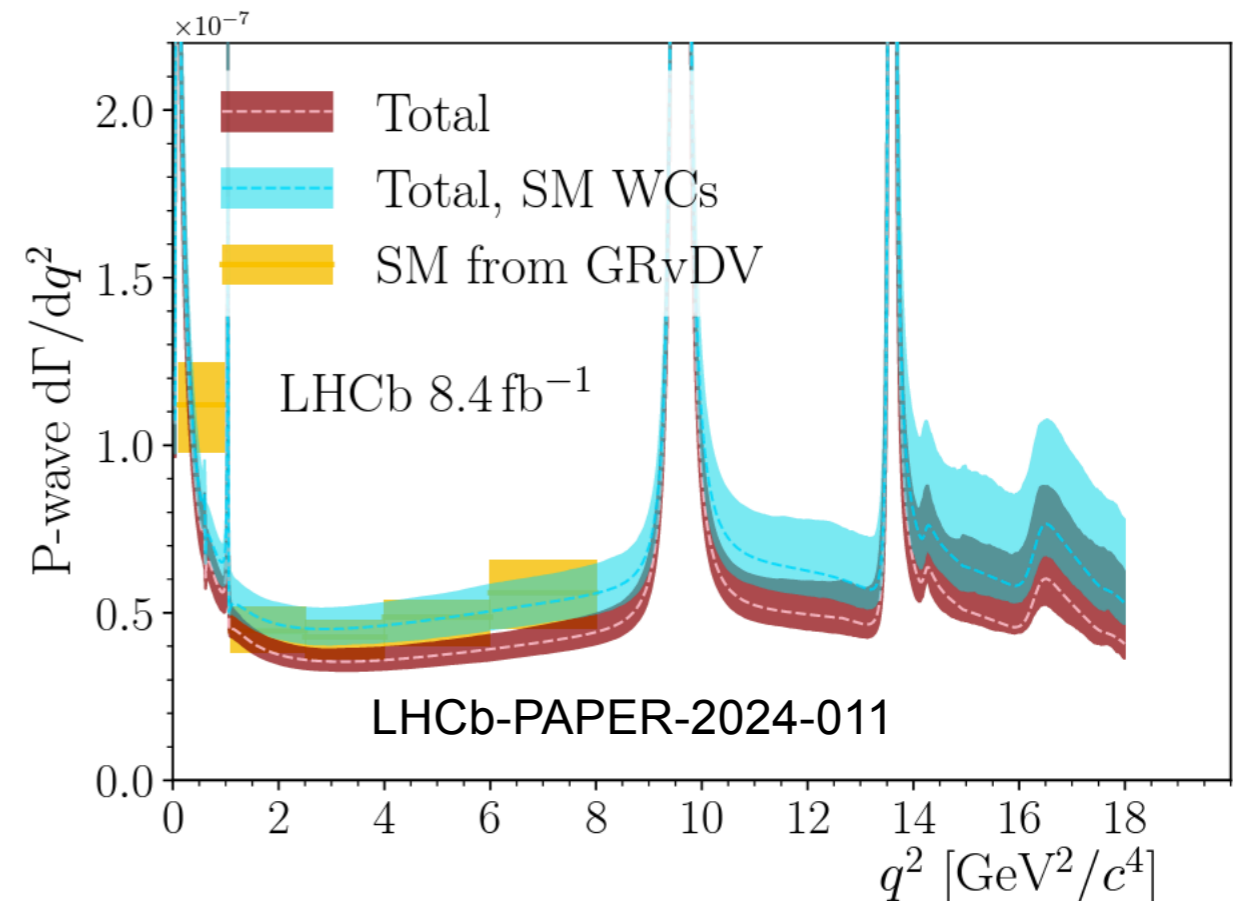
-comparison with previous measurements



Increased tension with respect to previous measurements

## Amplitude model

- affect on SM predictions



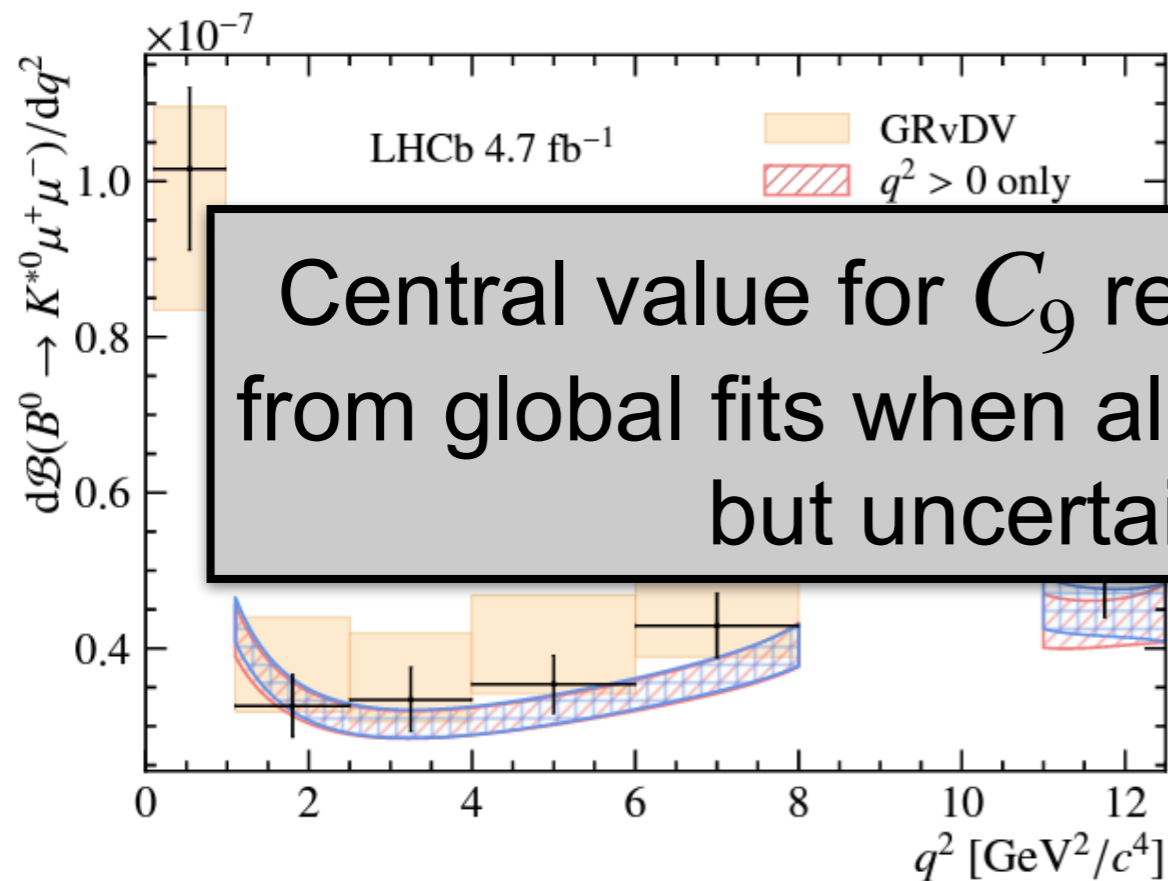
Minimal modification to SM predictions, tension remains



# Affect of non-local contributions on branching fractions?

## Z-expansion

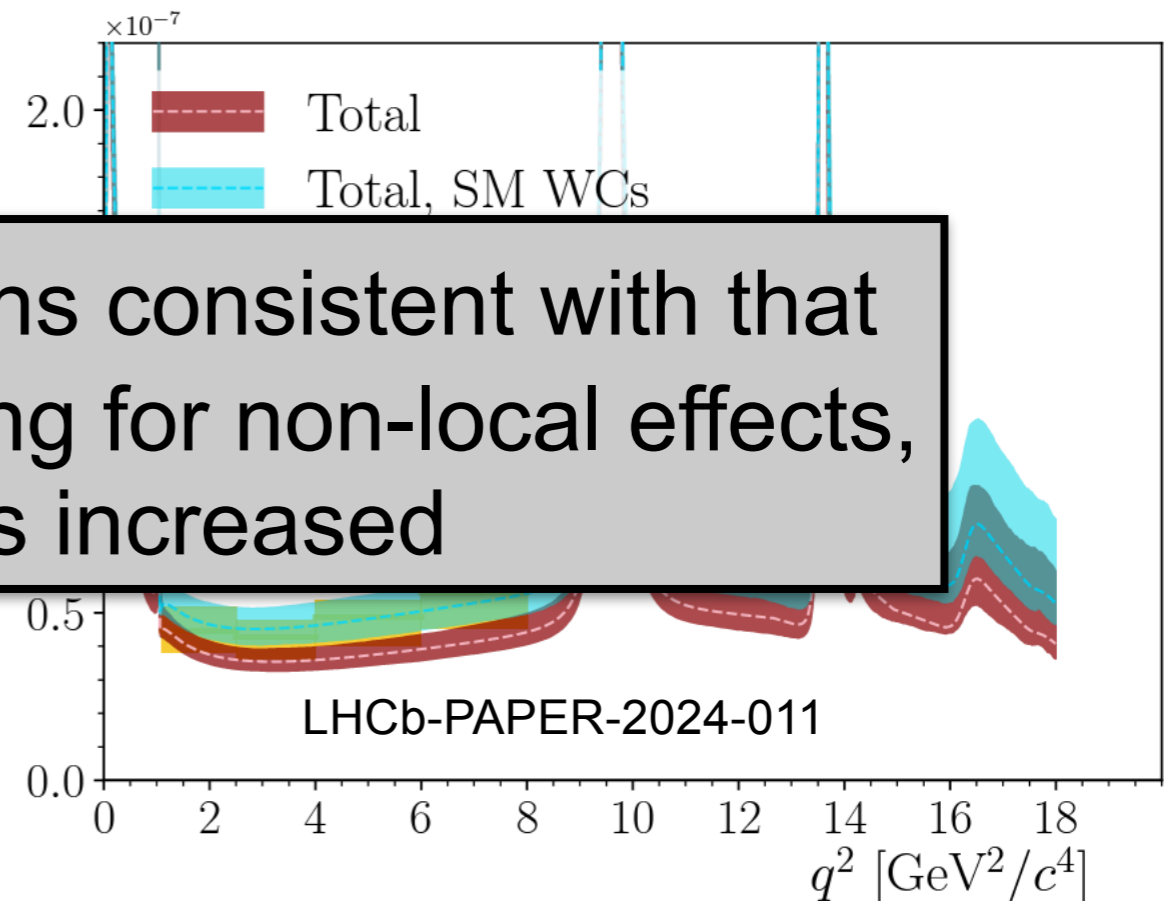
-comparison with previous measurements



Increased tension with respect to previous measurements

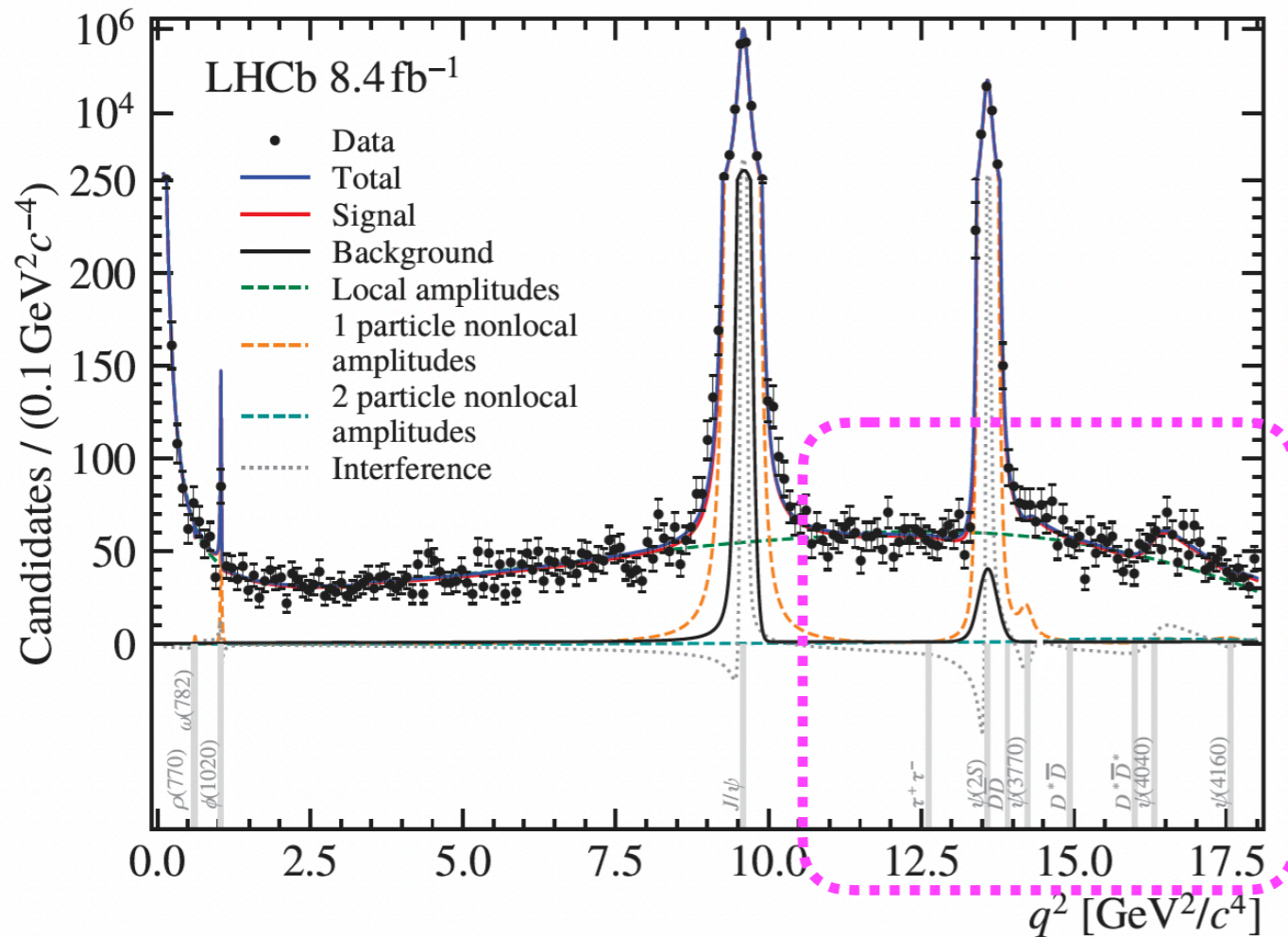
## Amplitude model

- affect on SM predictions

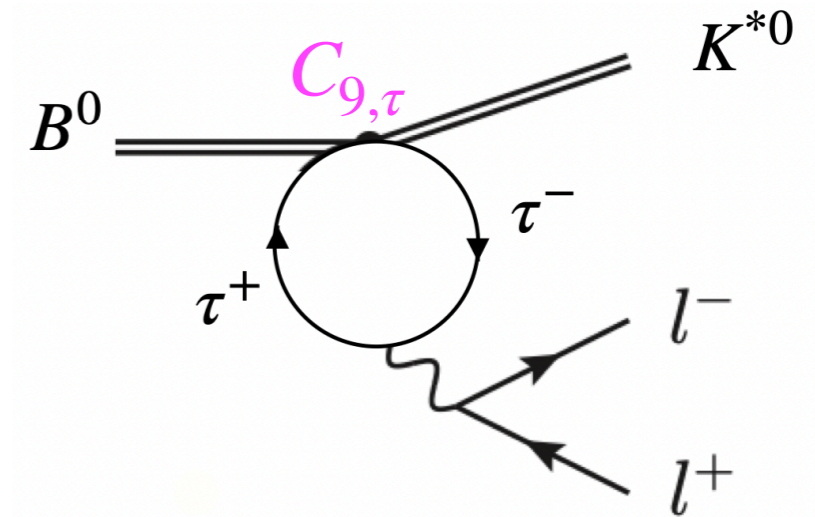


Minimal modification to SM predictions, tension remains

# Bonus: worlds first direct measurement of $C_{9,\tau}$



LHCb-PAPER-2024-011



Muon analysis is sensitive to  $C_{9,\tau}$  via

$$B^0 \rightarrow K^{*0} [\tau^+ \tau^- \rightarrow \gamma^* \rightarrow \mu^+ \mu^-]$$

$$\propto C_{9,\tau}$$

Convert to 90% CL on

$$\mathcal{B}(B^0 \rightarrow K^{*0} \tau^+ \tau^-) \sim [1.7 - 2.2] \times 10^{-3}$$

Best direct measurement of  $\mathcal{B}(B^0 \rightarrow K^{*0} \tau^+ \tau^-) = 3.1 \times 10^{-3}$  90% CL Belle, Phys. Rev. D108 (2023) L011102

SM prediction  $\mathcal{O}(10^{-7})$ , NP models  $\mathcal{O}(10^{-4})$

Worlds first direct measurement of  $C_{9,\tau}$

$$C_{9,\tau} = (-1.0 \pm 2.6 \pm 1.0) \times 10^2$$

# Hadronic cleanliness

Lepton Flavour Universality  
and  $B_s \rightarrow \mu^+ \mu^-$



Angular analyses



Branching fractions



# Hadronic cleanliness

Lepton Flavour Universality  
and  $B_s \rightarrow \mu^+ \mu^-$



Angular analyses

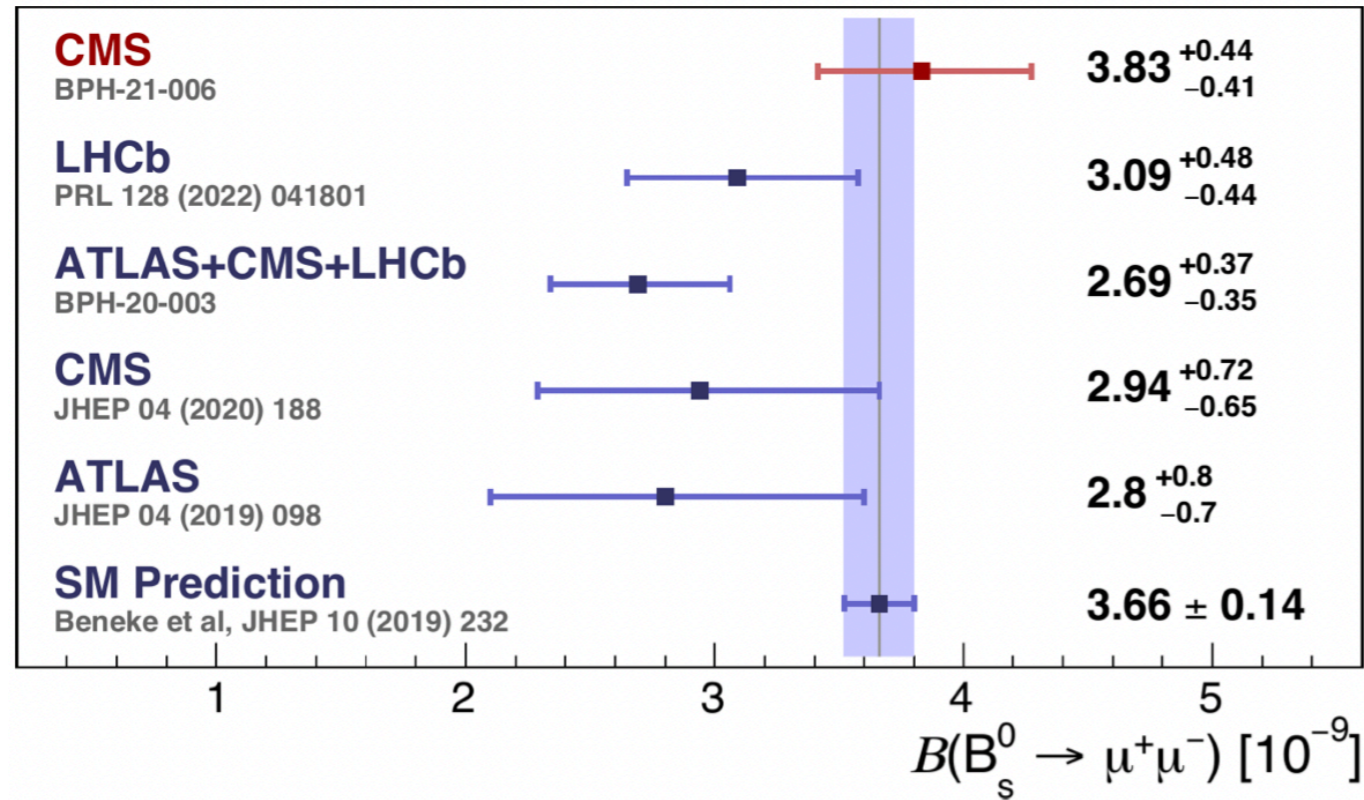


Branching fractions

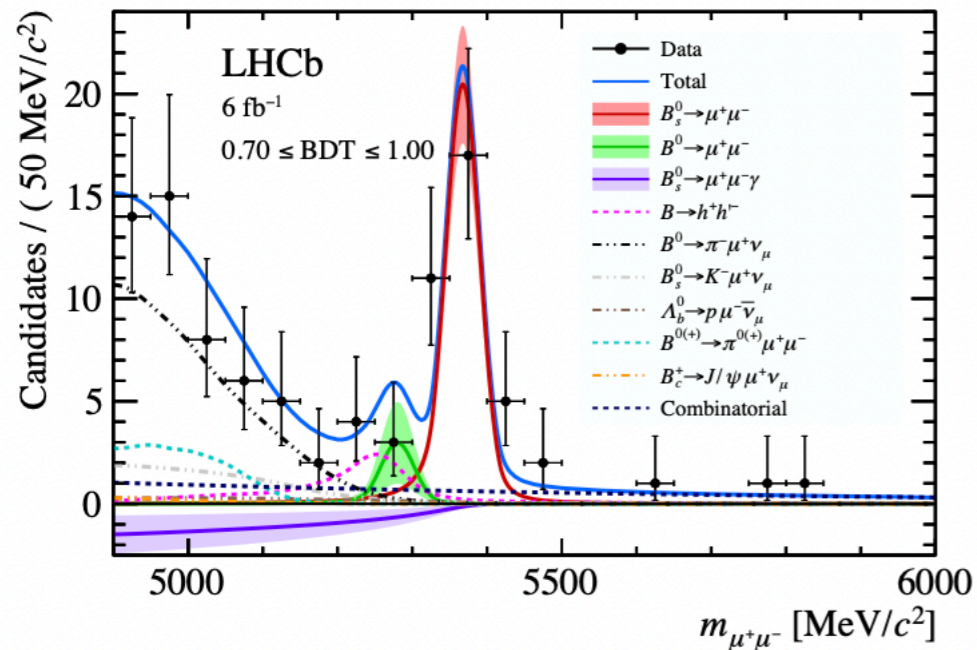


# $B_s \rightarrow \mu^+ \mu^-$ : branching fraction

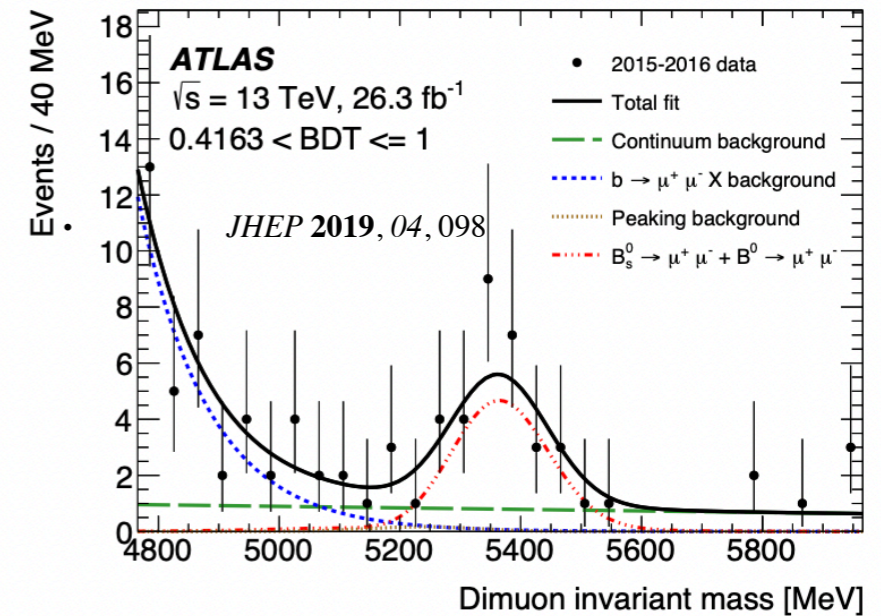
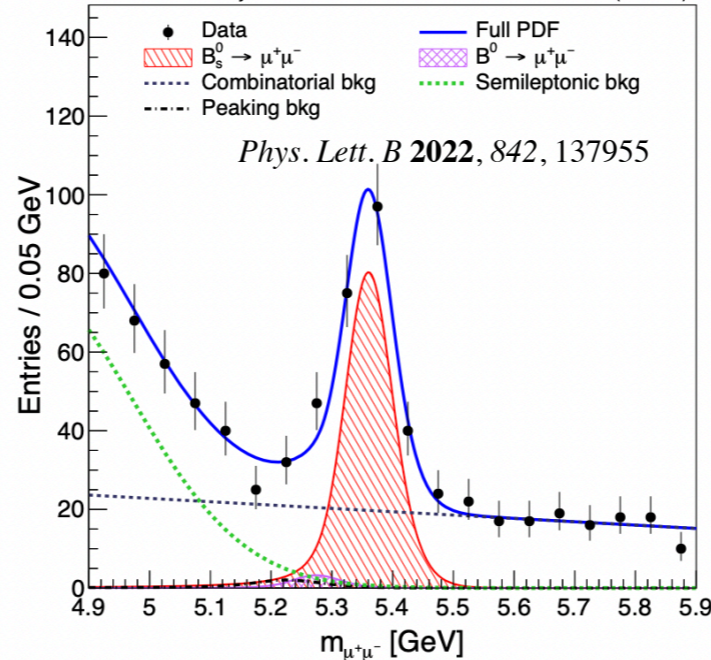
Clean observable, sensitive to  $C_{10}$



*Phys. Rev. Lett.* **2022**, 128, 041801



CMS Preliminary 140 fb<sup>-1</sup> (13 TeV)



# $B_s \rightarrow \mu^+ \mu^-$ : effective lifetime

In the SM, just the heavy mass eigenstate  $B_H$  decays to  $\mu^+ \mu^-$

CP-averaged lifetime more sensitive to (NP) contributions from **light mass eigenstate** than branching fraction

$$\begin{aligned}\tau_{\mu\mu} &\equiv \frac{\int_0^\infty t \langle \Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \rangle dt}{\int_0^\infty \langle \Gamma(B_s^0 \rightarrow \mu^+ \mu^-) \rangle dt} \\ &= \frac{\tau_{B_s^0}}{1 - y_s^2} \left[ \frac{1 + 2\mathcal{A}_{\Delta\Gamma} y_s + y_s^2}{1 + \mathcal{A}_{\Delta\Gamma} y_s} \right]\end{aligned}$$

$$y_s \sim 0.1$$

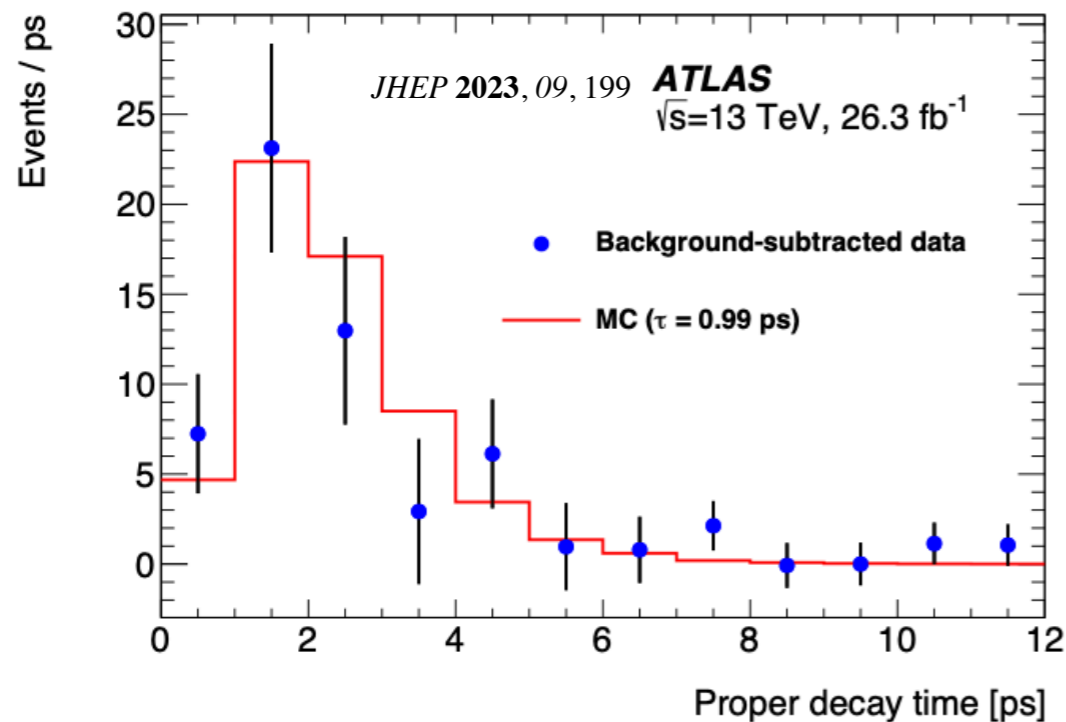
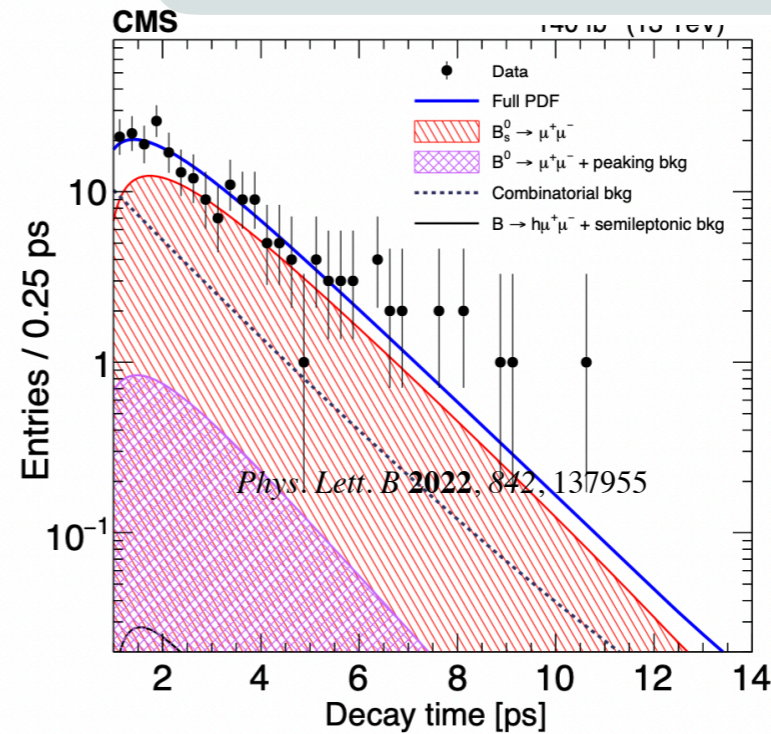
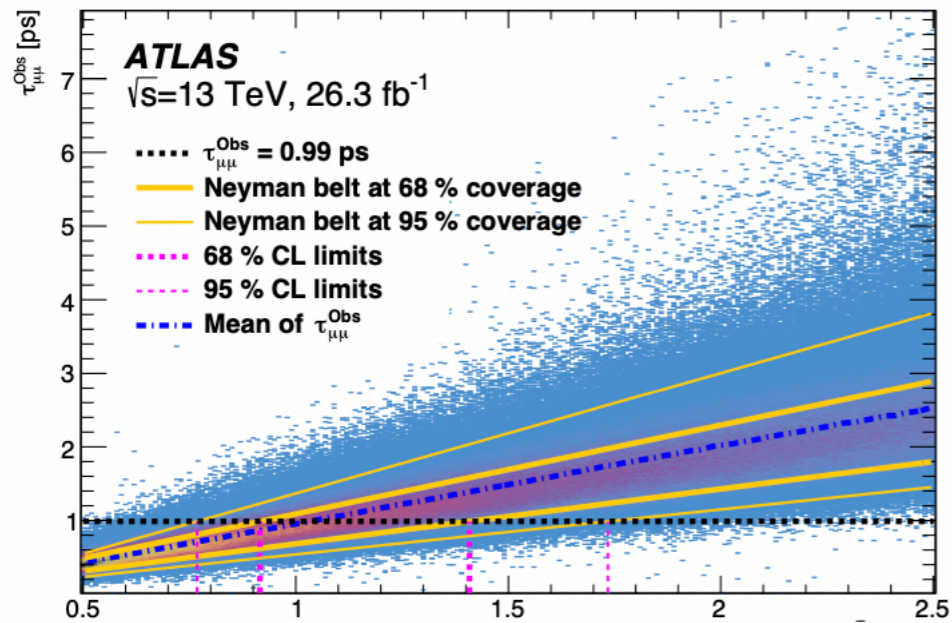
$$\mathcal{A}_{\Delta\Gamma} \equiv \frac{R_H^{\mu^+ \mu^-} - R_L^{\mu^+ \mu^-}}{R_H^{\mu^+ \mu^-} + R_L^{\mu^+ \mu^-}}$$

# $B_s \rightarrow \mu^+ \mu^-$ : effective lifetime

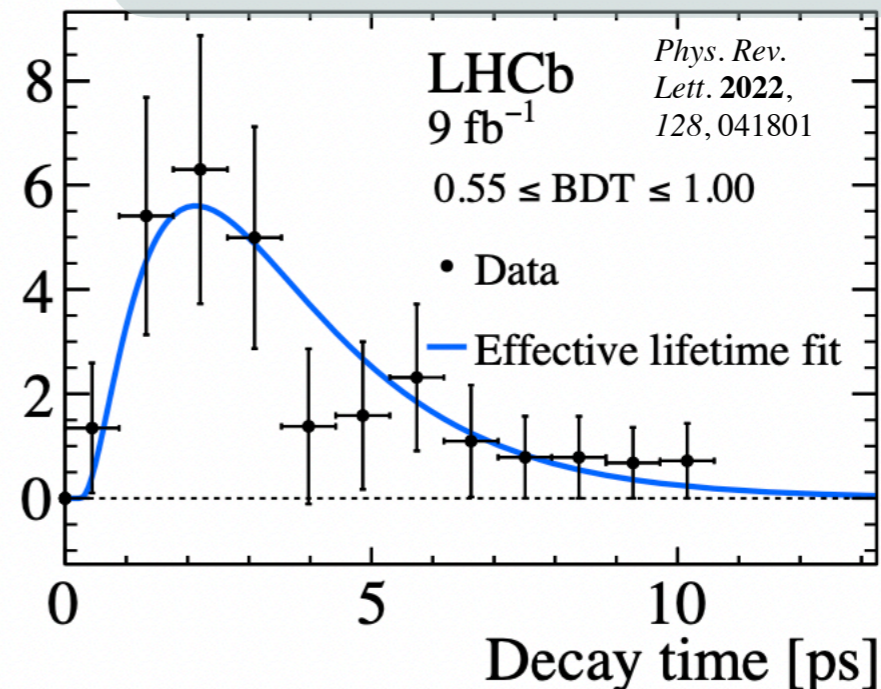
$$\tau_{\mu\mu}^{SM} = 1.624 \pm 0.009 \text{ ps}$$

$$\tau_{\mu\mu} = 0.99^{+0.42}_{-0.07} (\text{stat.}) \pm 0.17 (\text{syst.})$$

$$\tau_{\mu\mu} = 1.83^{+0.23}_{-0.20} (\text{stat})^{+0.04}_{-0.04} (\text{syst}) \text{ ps,}$$



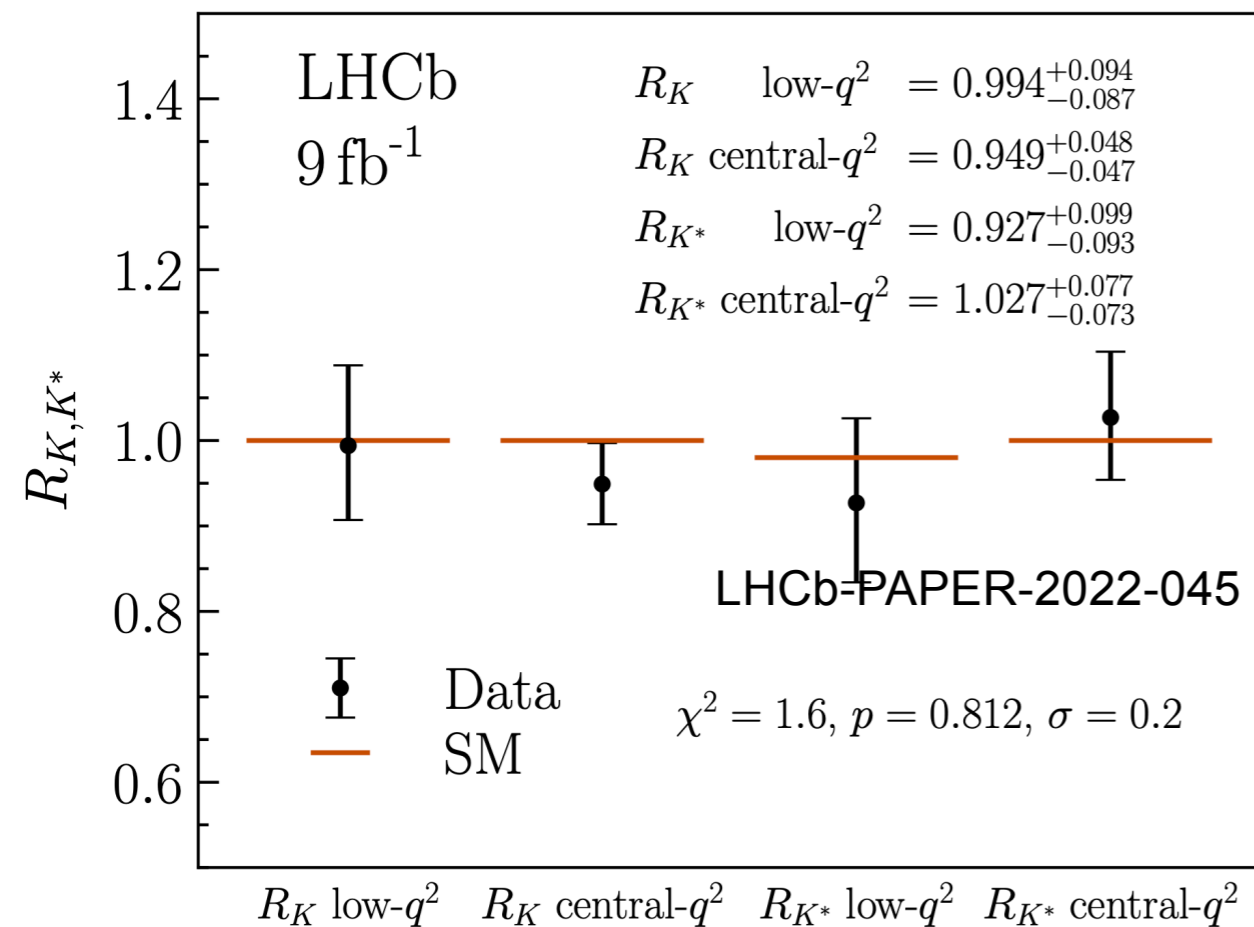
$$\tau_{\mu^+ \mu^-} = 2.07 \pm 0.29 \pm 0.03 \text{ ps,}$$



# Lepton flavour universality tests

$$R(X) = \frac{\mathcal{B}(B \rightarrow X \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow X e^+ e^-)}$$

Precisely predicted to be  $\sim 1$  in SM



Precisely predicted to be  $\sim 1$  in SM



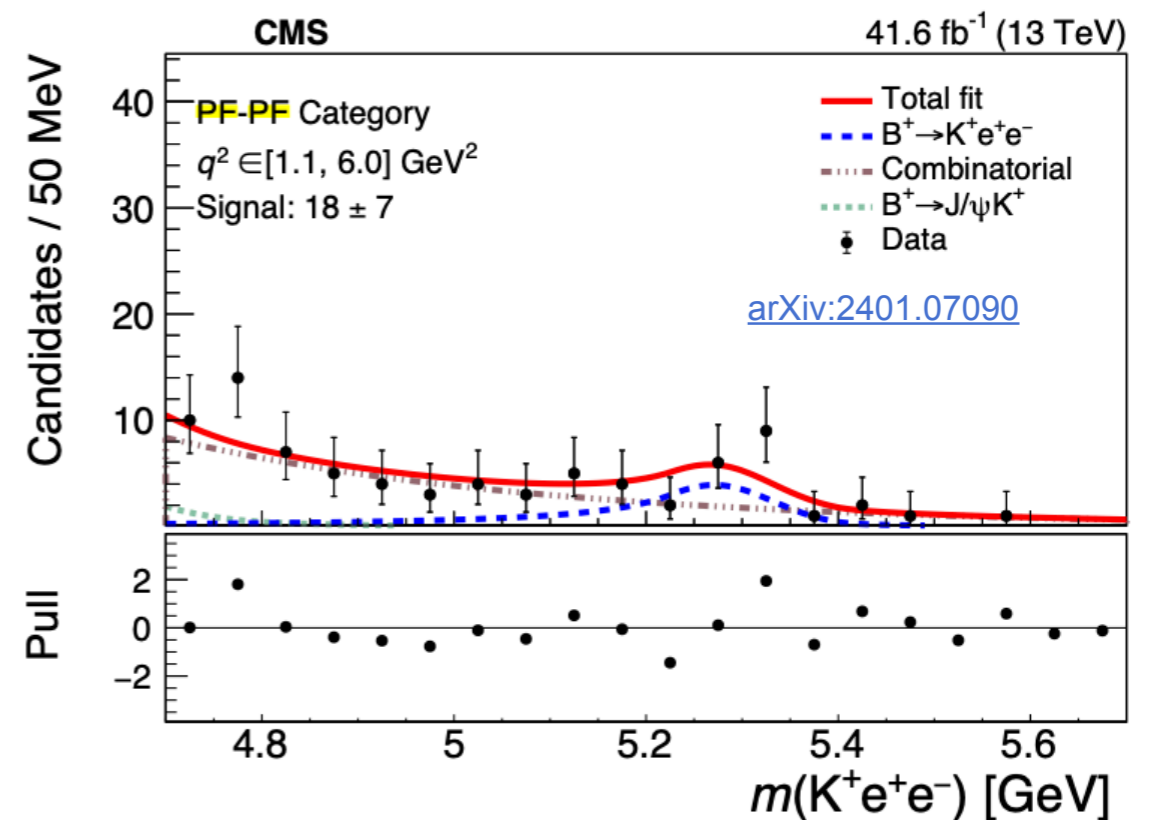
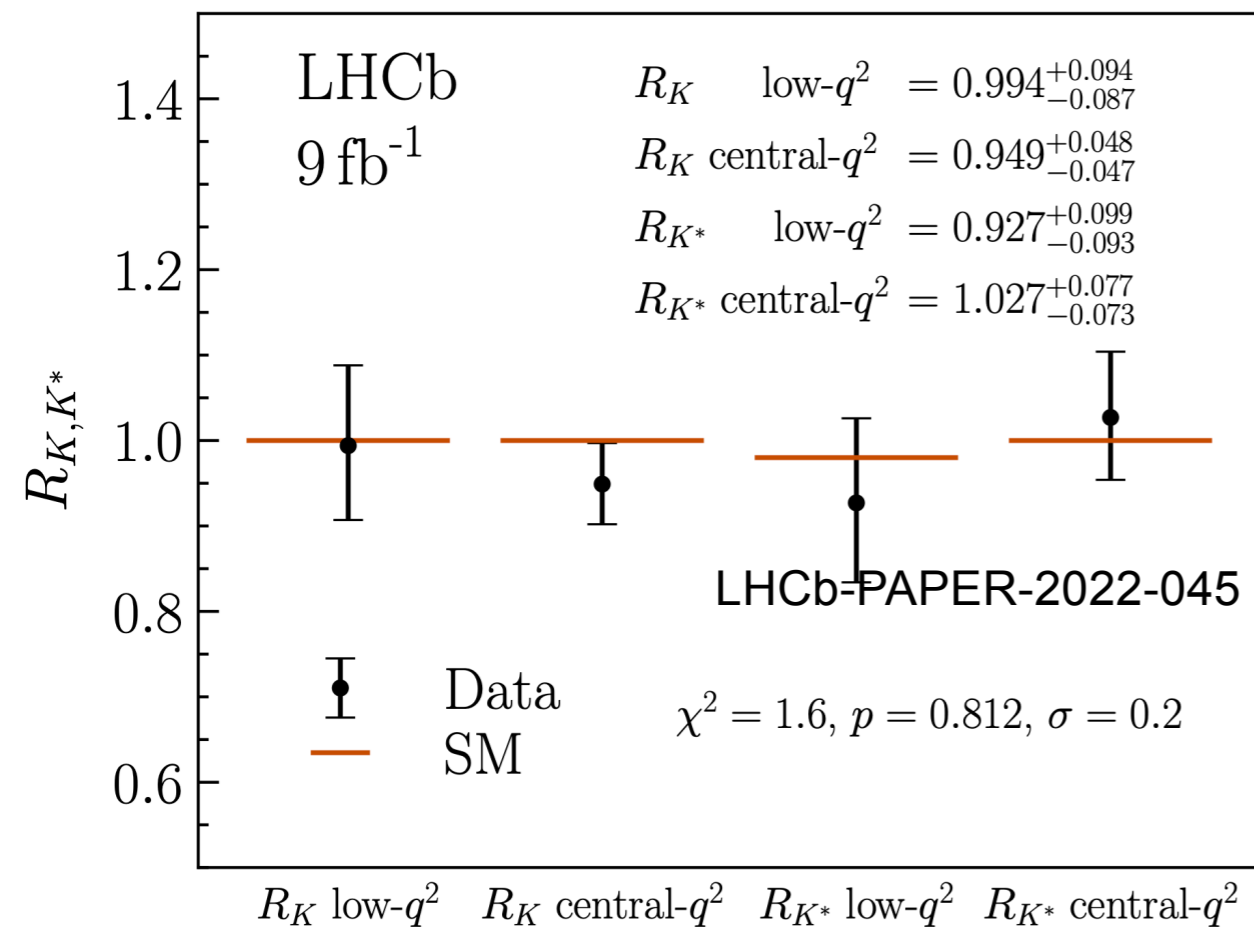
# Lepton flavour universality tests

$$R(X) = \frac{\mathcal{B}(B \rightarrow X \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow X e^+ e^-)}$$

Precisely predicted to be  $\sim 1$  in SM

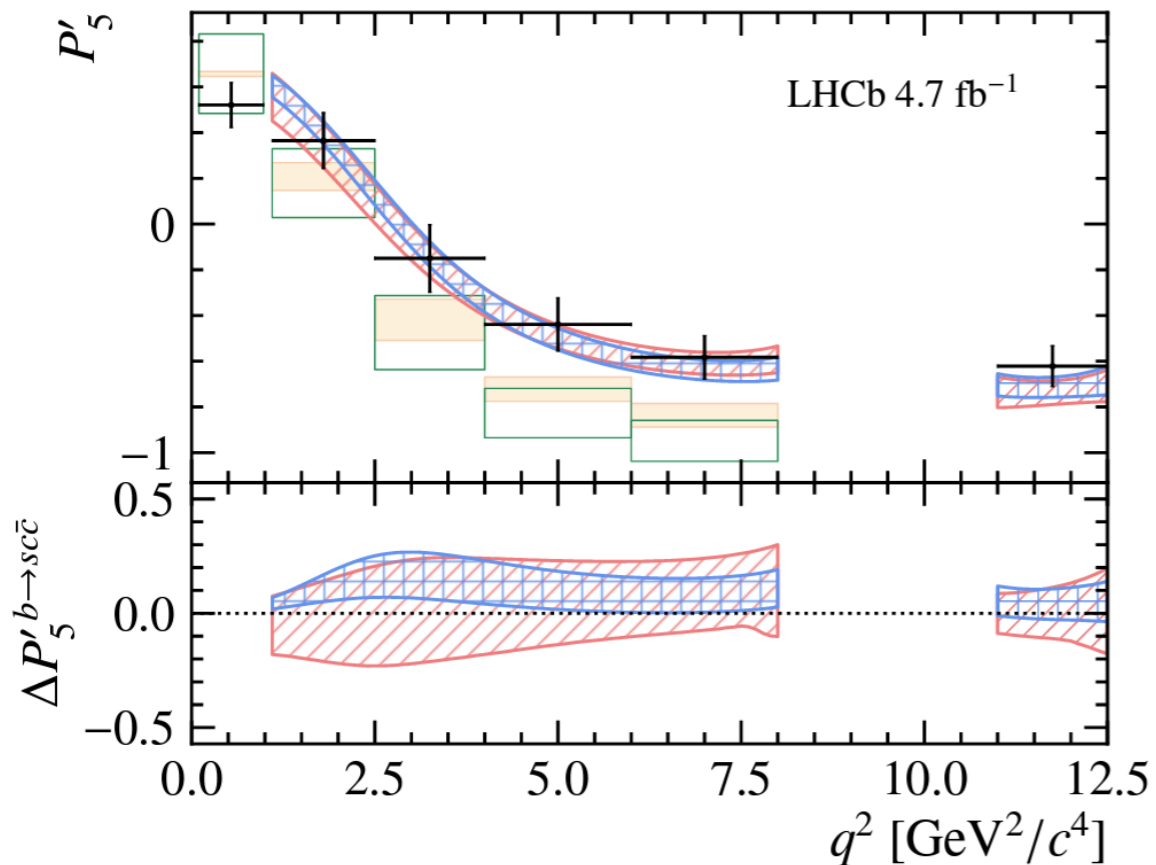
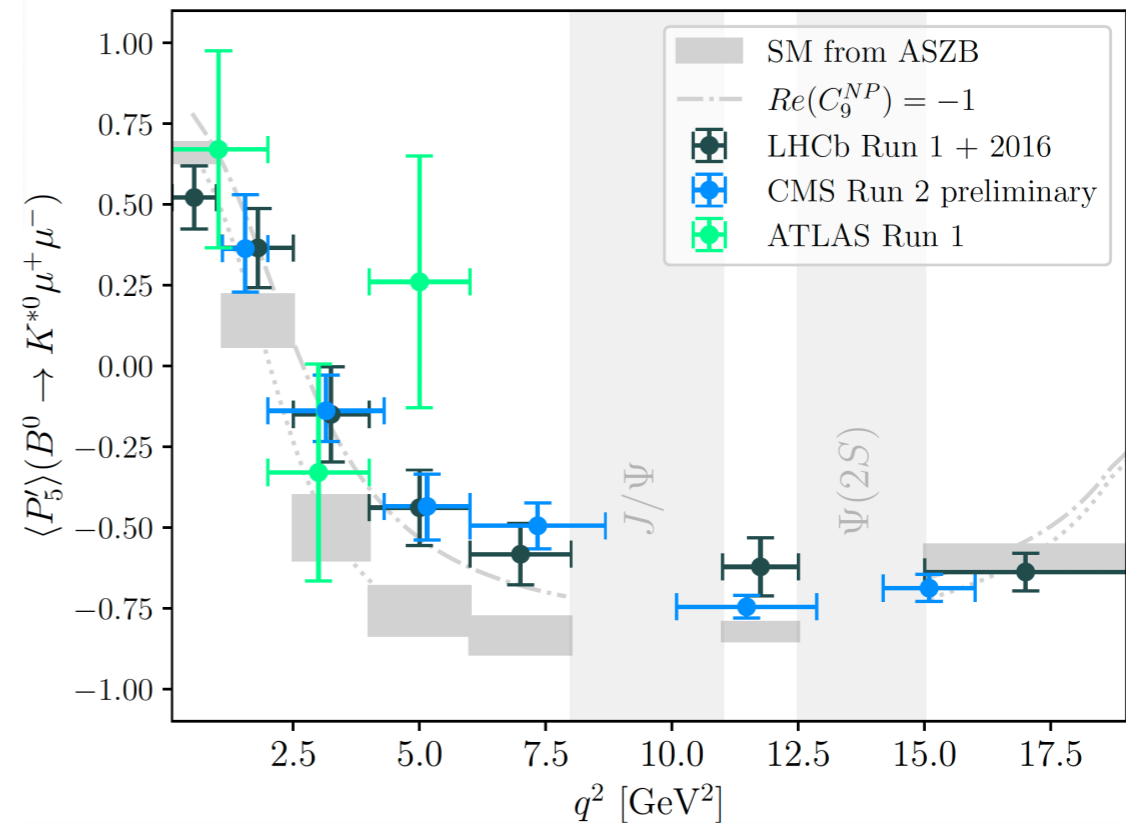
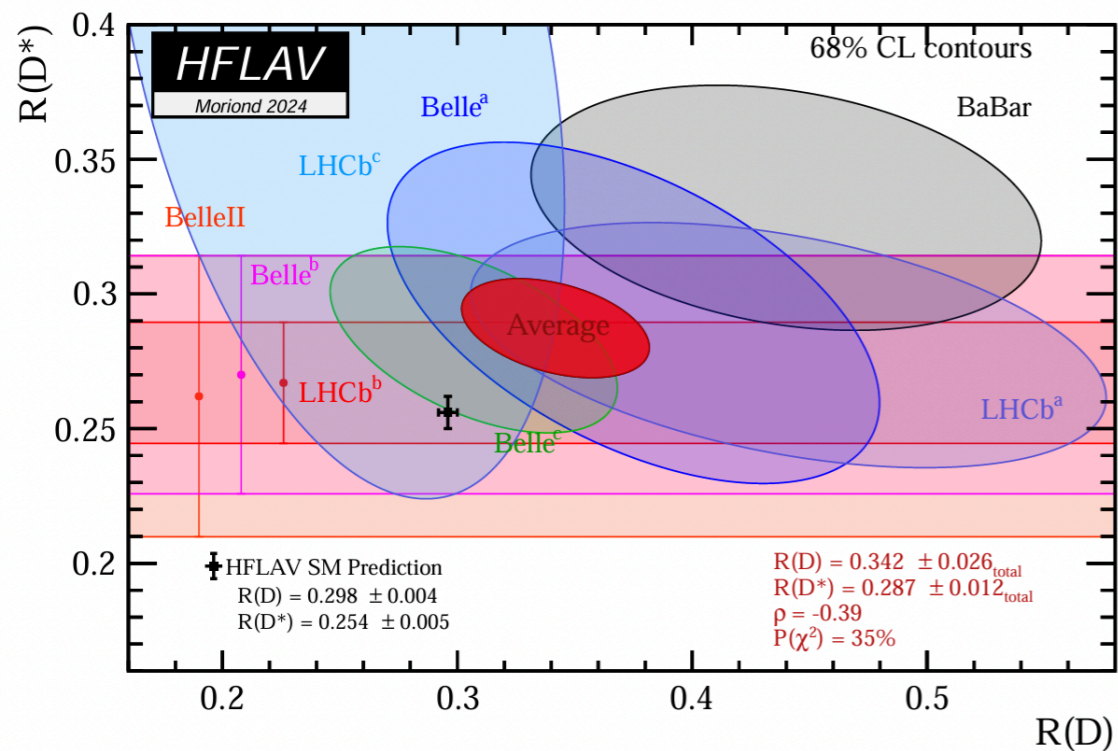
## New CMS result

$$R(K) = 0.78^{+0.47}_{-0.23}$$



Precisely predicted to be  $\sim 1$  in SM

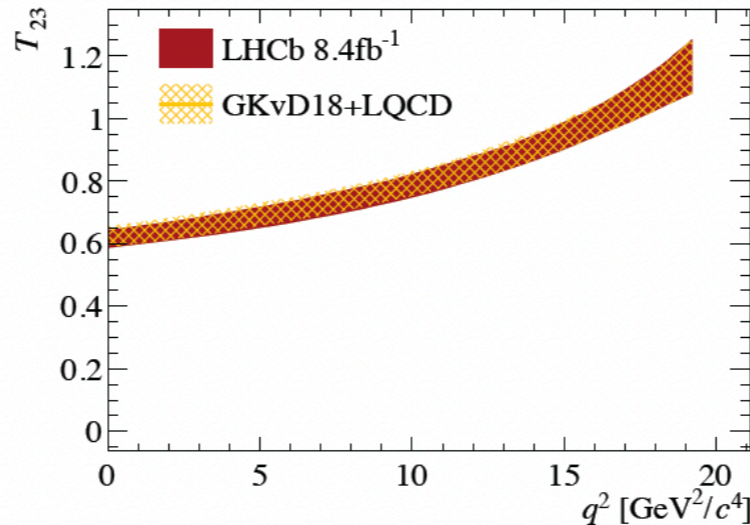
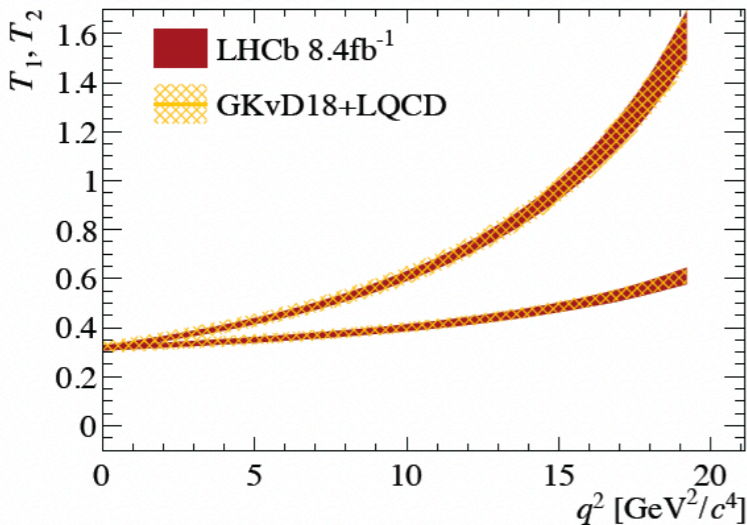
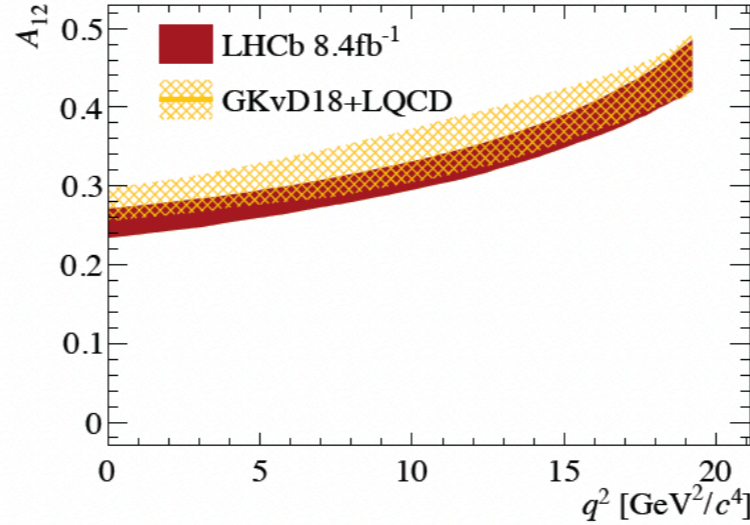
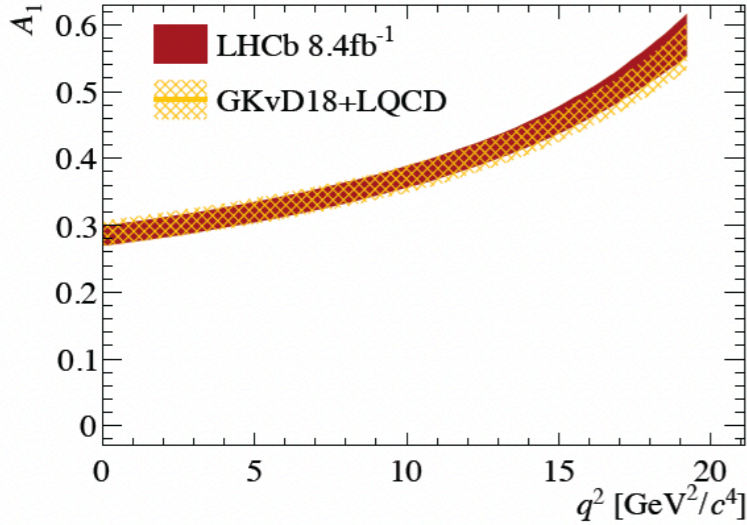
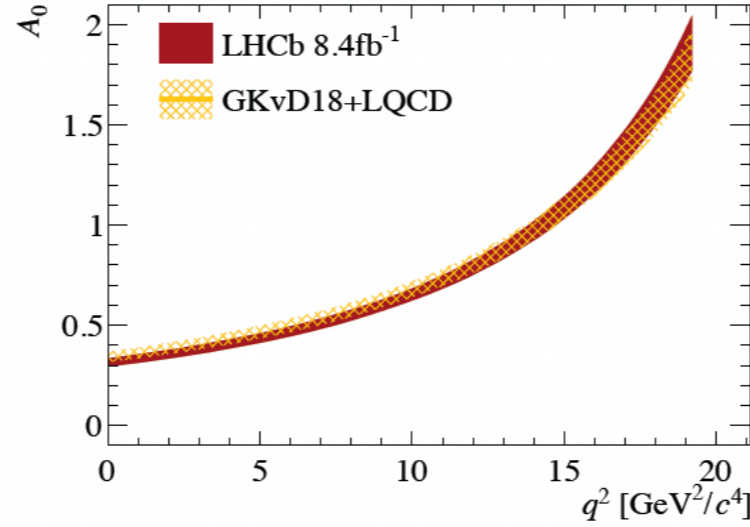
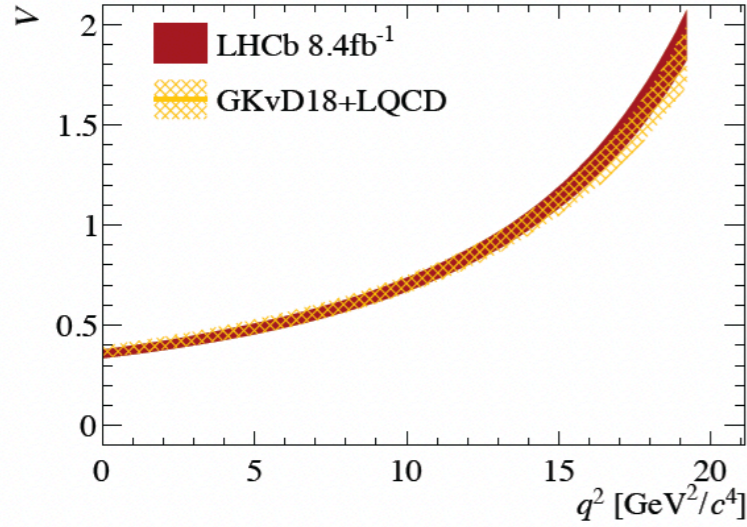
# Summary



- New results in both  $b \rightarrow c \ell \nu$  and  $b \rightarrow s \ell \ell$
- Tensions in  $b \rightarrow s \ell \ell$  remain with new data + allowing for non-local effects
- Further Run 2 results + Run 3 will help resolve anomalies

# Back-ups

# Amplitude analysis over all $q^2$ : results



## Local form factors

Local form-factor results		
Parameter	Prior [34]	Posterior
$\alpha_1^{A_0}$	$-1.12 \pm 0.20$	$-1.21 \pm 0.19 \pm 0.02$
$\alpha_2^{A_0}$	$2.18 \pm 1.76$	$3.23 \pm 1.69 \pm 0.18$
$\alpha_0^{A_1}$	$0.29 \pm 0.02$	$0.29 \pm 0.01 \pm 0.00$
$\alpha_1^{A_1}$	$0.46 \pm 0.13$	$0.40 \pm 0.10 \pm 0.01$
$\alpha_2^{A_1}$	$1.22 \pm 0.73$	$1.21 \pm 0.69 \pm 0.10$
$\alpha_0^{A_{12}}$	$0.28 \pm 0.02$	$0.26 \pm 0.02 \pm 0.00$
$\alpha_1^{A_{12}}$	$0.55 \pm 0.34$	$0.47 \pm 0.22 \pm 0.04$
$\alpha_2^{A_{12}}$	$0.58 \pm 2.08$	$0.53 \pm 1.26 \pm 0.17$
$\alpha_0^V$	$0.36 \pm 0.03$	$0.36 \pm 0.02 \pm 0.00$
$\alpha_1^V$	$-1.09 \pm 0.17$	$-1.09 \pm 0.17 \pm 0.01$
$\alpha_2^V$	$2.73 \pm 1.99$	$3.93 \pm 1.74 \pm 0.25$
$\alpha_1^{T_1}$	$-0.95 \pm 0.14$	$-0.94 \pm 0.14 \pm 0.01$
$\alpha_2^{T_1}$	$2.11 \pm 1.28$	$2.07 \pm 1.16 \pm 0.05$
$\alpha_0^{T_2}$	$0.32 \pm 0.02$	—
$\alpha_1^{T_2}$	$0.60 \pm 0.18$	$0.61 \pm 0.16 \pm 0.01$
$\alpha_2^{T_2}$	$1.70 \pm 0.99$	$1.78 \pm 0.98 \pm 0.03$
$\alpha_0^{T_{23}}$	$0.62 \pm 0.03$	—
$\alpha_1^{T_{23}}$	$0.97 \pm 0.32$	$0.95 \pm 0.30 \pm 0.01$
$\alpha_2^{T_{23}}$	$1.81 \pm 2.45$	$1.68 \pm 2.15 \pm 0.04$

# Amplitude analysis over all $q^2$ : results

Nonlocal parameter results			
$ A_{J/\psi}^{\parallel} $	$(3.98 \pm 0.01 \pm 0.15) \times 10^{-3}$	$\delta_{J/\psi}^{\parallel}$	$0.23 \pm 0.01 \pm 0.01$
$ A_{J/\psi}^{\perp} $	$(3.85 \pm 0.01 \pm 0.14) \times 10^{-3}$	$\delta_{J/\psi}^{\perp}$	$-0.21 \pm 0.00 \pm 0.01$
$ A_{J/\psi}^0 $	–	$\delta_{J/\psi}^0$	$-1.92 \pm 0.05 \pm 0.02$
$ A_{\psi(2S)}^{\parallel} $	$(9.59 \pm 0.28 \pm 0.82) \times 10^{-4}$	$\delta_{\psi(2S)}^{\parallel}$	$0.84 \pm 0.02 \pm 0.19$
$ A_{\psi(2S)}^{\perp} $	$(8.38 \pm 0.27 \pm 0.62) \times 10^{-4}$	$\delta_{\psi(2S)}^{\perp}$	$-0.44 \pm 0.02 \pm 0.11$
$ A_{\psi(2S)}^0 $	$(13.4 \pm 0.4 \pm 1.1) \times 10^{-4}$	$\delta_{\psi(2S)}^0$	$-2.54 \pm 0.13 \pm 0.12$
$ A_{\rho(770)}^0 $	–	$\delta_{\rho(770)}^0$	$1.38 \pm 0.53 \pm 0.65$
$ A_{\omega(782)}^0 $	–	$\delta_{\omega(782)}^0$	$-0.49 \pm 0.92 \pm 0.53$
$ A_{\phi(1020)}^0 $	–	$\delta_{\phi(1020)}^0$	$0.10 \pm 0.82 \pm 0.78$

Nonlocal parameter results ( $\times 10^{-5}$ )			
$\Re(A_{\psi(3770)}^{\parallel})$	$3.68 \pm 1.34 \pm 0.73$	$\Im(A_{\psi(3770)}^{\parallel})$	$2.87 \pm 1.88 \pm 0.49$
$\Re(A_{\psi(3770)}^{\perp})$	$-3.53 \pm 1.45 \pm 0.47$	$\Im(A_{\psi(3770)}^{\perp})$	$-0.86 \pm 1.56 \pm 0.53$
$\Re(A_{\psi(3770)}^0)$	$-3.14 \pm 1.39 \pm 0.60$	$\Im(A_{\psi(3770)}^0)$	$1.67 \pm 1.54 \pm 0.62$
$\Re(A_{\psi(4040)}^{\parallel})$	$-2.39 \pm 1.53 \pm 0.96$	$\Im(A_{\psi(4040)}^{\parallel})$	$-0.71 \pm 1.80 \pm 1.11$
$\Re(A_{\psi(4040)}^{\perp})$	$-2.01 \pm 1.47 \pm 0.59$	$\Im(A_{\psi(4040)}^{\perp})$	$0.35 \pm 1.49 \pm 0.82$
$\Re(A_{\psi(4040)}^0)$	$-5.62 \pm 1.71 \pm 1.07$	$\Im(A_{\psi(4040)}^0)$	$1.32 \pm 1.87 \pm 0.99$
$\Re(A_{\psi(4160)}^{\parallel})$	$0.04 \pm 1.72 \pm 0.56$	$\Im(A_{\psi(4160)}^{\parallel})$	$1.91 \pm 1.98 \pm 1.45$
$\Re(A_{\psi(4160)}^{\perp})$	$-2.81 \pm 1.75 \pm 0.61$	$\Im(A_{\psi(4160)}^{\perp})$	$0.32 \pm 0.15 \pm 0.09$
$\Re(A_{\psi(4160)}^0)$	$1.03 \pm 1.77 \pm 0.39$	$\Im(A_{\psi(4160)}^0)$	$-1.66 \pm 1.67 \pm 1.04$

Nonlocal parameter results			
$\Re(A_{D^0\bar{D}^0}^{\parallel})$	$-0.07 \pm 0.93 \pm 0.69$	$\Im(A_{D^0\bar{D}^0}^{\parallel})$	$-0.44 \pm 0.71 \pm 0.73$
$\Re(A_{D^0\bar{D}^0}^{\perp})$	$-0.12 \pm 0.83 \pm 0.71$	$\Im(A_{D^0\bar{D}^0}^{\perp})$	$0.02 \pm 0.80 \pm 0.74$
$\Re(A_{D^0\bar{D}^0}^0)$	$-0.33 \pm 0.91 \pm 0.70$	$\Im(A_{D^0\bar{D}^0}^0)$	$-0.27 \pm 0.77 \pm 0.81$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.06 \pm 0.96 \pm 0.63$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.25 \pm 0.79 \pm 0.67$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.16 \pm 0.91 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.03 \pm 0.85 \pm 0.70$
$\Re(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.17 \pm 0.95 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.28 \pm 0.85 \pm 0.78$
$\Re(A_{D^{*0}\bar{D}^0}^{\parallel})$	$0.02 \pm 0.42 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^0}^{\parallel})$	$-0.46 \pm 0.32 \pm 0.58$
$\Re(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.24 \pm 0.42 \pm 0.70$	$\Im(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.11 \pm 0.39 \pm 0.61$
$\Re(A_{D^{*0}\bar{D}^0}^0)$	$-0.51 \pm 0.41 \pm 0.68$	$\Im(A_{D^{*0}\bar{D}^0}^0)$	$0.12 \pm 0.35 \pm 0.58$
$\Re(\Delta\mathcal{C}_7^{\parallel})$	$0.00 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\parallel})$	$-0.10 \pm 0.03 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^{\perp})$	$-0.05 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\perp})$	$-0.04 \pm 0.04 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^0)$	$0.33 \pm 0.33 \pm 0.09$	$\Im(\Delta\mathcal{C}_7^0)$	$-0.19 \pm 0.20 \pm 0.09$

# Amplitude analysis over all $q^2$ : results

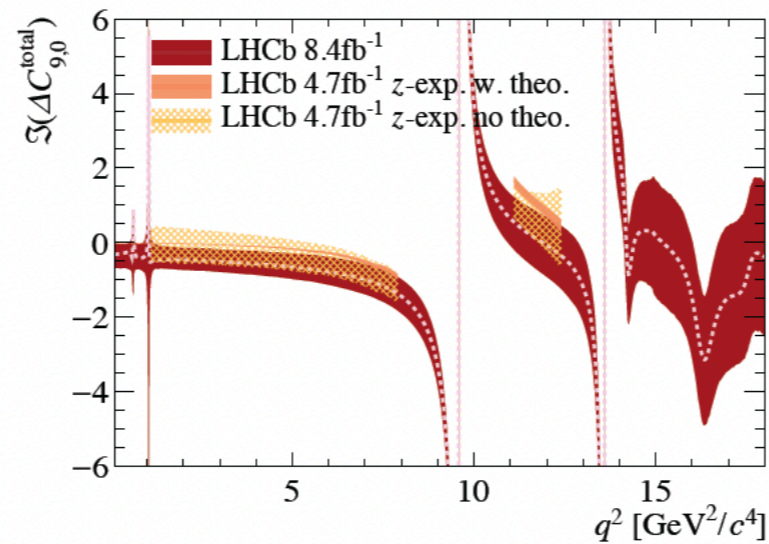
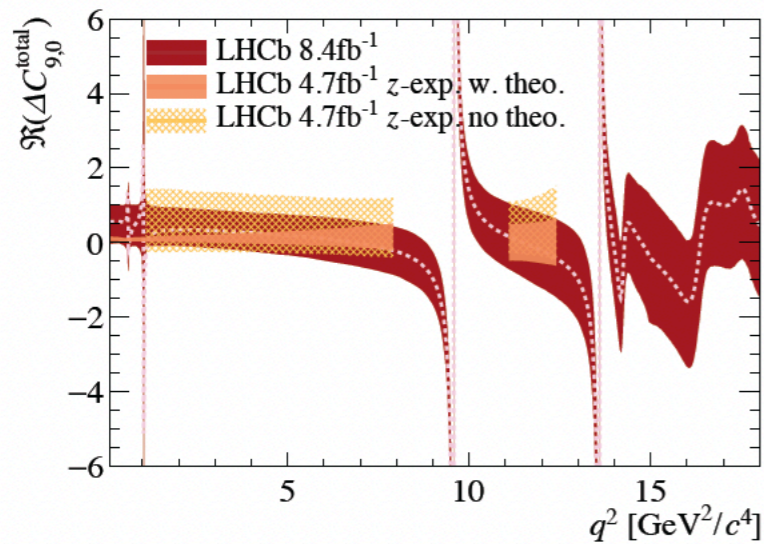
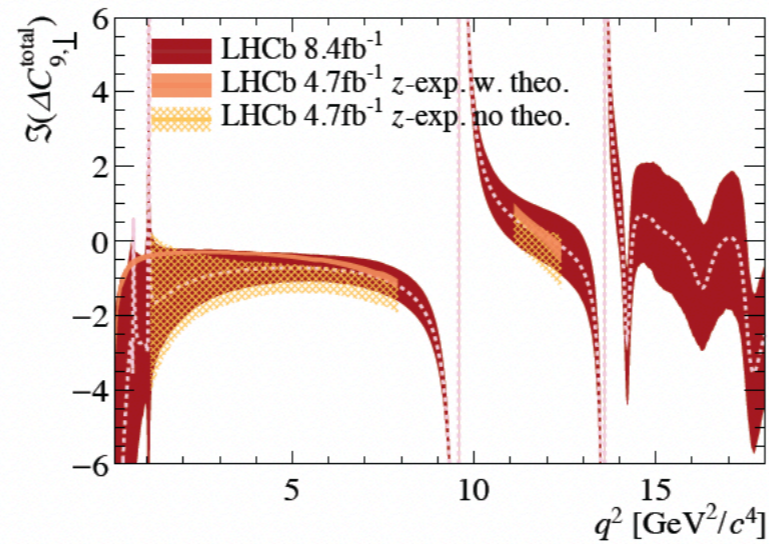
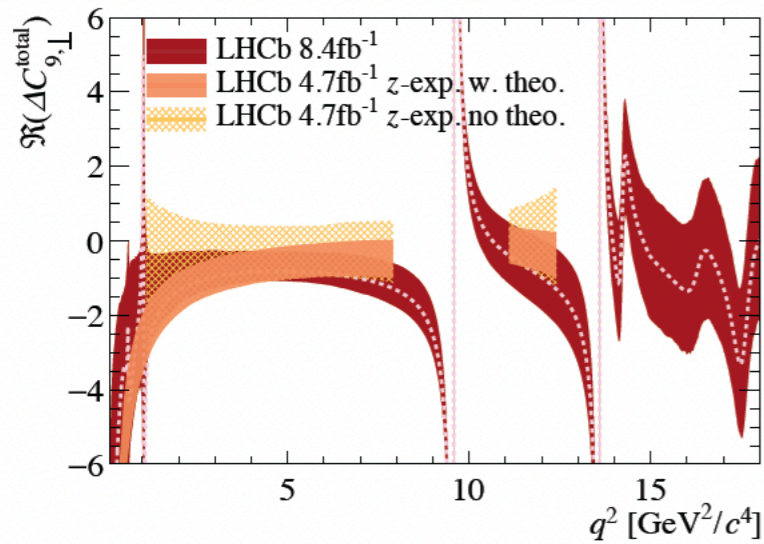
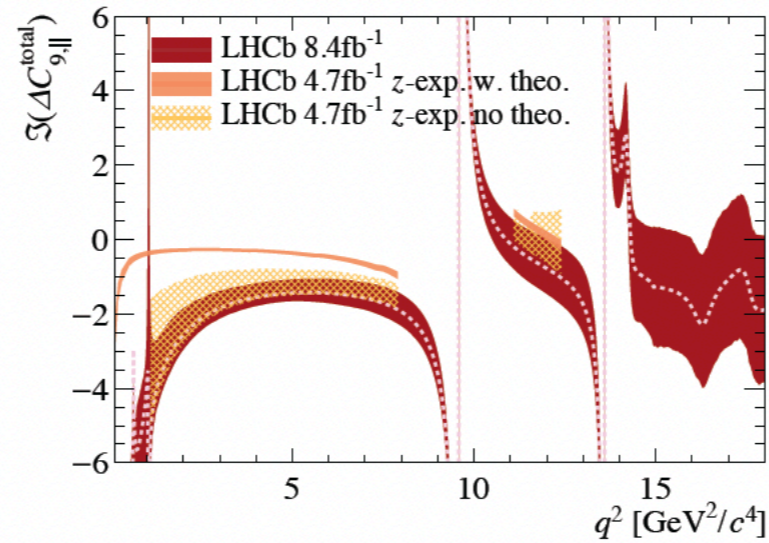
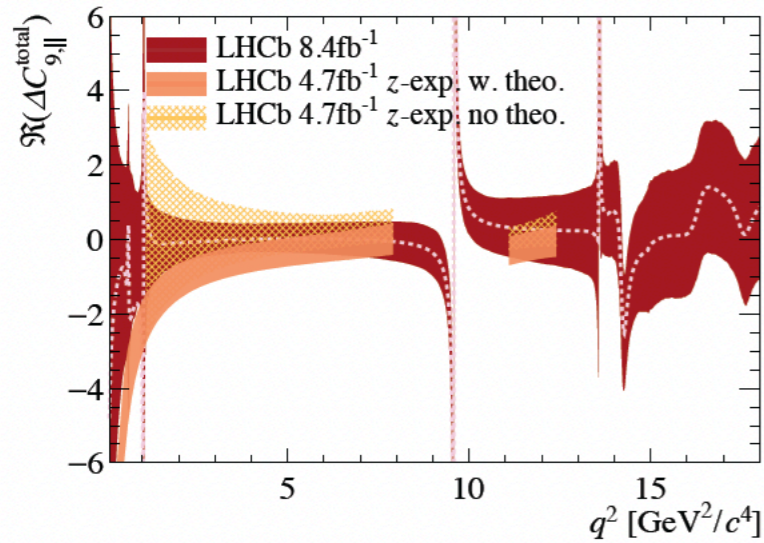
Nonlocal parameter results			
$ A_{J/\psi}^{\parallel} $	$(3.98 \pm 0.01 \pm 0.15) \times 10^{-3}$	$\delta_{J/\psi}^{\parallel}$	$0.23 \pm 0.01 \pm 0.01$
$ A_{J/\psi}^{\perp} $	$(3.85 \pm 0.01 \pm 0.14) \times 10^{-3}$	$\delta_{J/\psi}^{\perp}$	$-0.21 \pm 0.00 \pm 0.01$
$ A_{J/\psi}^0 $	–	$\delta_{J/\psi}^0$	$-1.92 \pm 0.05 \pm 0.02$
$ A_{\psi(2S)}^{\parallel} $	$(9.59 \pm 0.28 \pm 0.82) \times 10^{-4}$	$\delta_{\psi(2S)}^{\parallel}$	$0.84 \pm 0.02 \pm 0.19$
$ A_{\psi(2S)}^{\perp} $	$(8.38 \pm 0.27 \pm 0.62) \times 10^{-4}$	$\delta_{\psi(2S)}^{\perp}$	$-0.44 \pm 0.02 \pm 0.11$
$ A_{\psi(2S)}^0 $	$(13.4 \pm 0.4 \pm 1.1) \times 10^{-4}$	$\delta_{\psi(2S)}^0$	$-2.54 \pm 0.13 \pm 0.12$
$ A_{\rho(770)}^0 $	–	$\delta_{\rho(770)}^0$	$1.38 \pm 0.53 \pm 0.65$
$ A_{\omega(782)}^0 $	–	$\delta_{\omega(782)}^0$	$-0.49 \pm 0.92 \pm 0.53$
$ A_{\phi(1020)}^0 $	–	$\delta_{\phi(1020)}^0$	$0.10 \pm 0.82 \pm 0.78$

Nonlocal parameter results ( $\times 10^{-5}$ )			
$\Re(A_{\psi(3770)}^{\parallel})$	$3.68 \pm 1.34 \pm 0.73$	$\Im(A_{\psi(3770)}^{\parallel})$	$2.87 \pm 1.88 \pm 0.49$
$\Re(A_{\psi(3770)}^{\perp})$	$-3.53 \pm 1.45 \pm 0.47$	$\Im(A_{\psi(3770)}^{\perp})$	$-0.86 \pm 1.56 \pm 0.53$
$\Re(A_{\psi(3770)}^0)$	$-3.14 \pm 1.39 \pm 0.60$	$\Im(A_{\psi(3770)}^0)$	$1.67 \pm 1.54 \pm 0.62$
$\Re(A_{\psi(4040)}^{\parallel})$	$-2.39 \pm 1.53 \pm 0.96$	$\Im(A_{\psi(4040)}^{\parallel})$	$-0.71 \pm 1.80 \pm 1.11$
$\Re(A_{\psi(4040)}^{\perp})$	$-2.01 \pm 1.47 \pm 0.59$	$\Im(A_{\psi(4040)}^{\perp})$	$0.35 \pm 1.49 \pm 0.82$
$\Re(A_{\psi(4040)}^0)$	$-5.62 \pm 1.71 \pm 1.07$	$\Im(A_{\psi(4040)}^0)$	$1.32 \pm 1.87 \pm 0.99$
$\Re(A_{\psi(4160)}^{\parallel})$	$0.04 \pm 1.72 \pm 0.56$	$\Im(A_{\psi(4160)}^{\parallel})$	$1.91 \pm 1.98 \pm 1.45$
$\Re(A_{\psi(4160)}^{\perp})$	$-2.81 \pm 1.75 \pm 0.61$	$\Im(A_{\psi(4160)}^{\perp})$	$0.32 \pm 0.15 \pm 0.09$
$\Re(A_{\psi(4160)}^0)$	$1.03 \pm 1.77 \pm 0.39$	$\Im(A_{\psi(4160)}^0)$	$-1.66 \pm 1.67 \pm 1.04$

Nonlocal parameter results			
$\Re(A_{D^0\bar{D}^0}^{\parallel})$	$-0.07 \pm 0.93 \pm 0.69$	$\Im(A_{D^0\bar{D}^0}^{\parallel})$	$-0.44 \pm 0.71 \pm 0.73$
$\Re(A_{D^0\bar{D}^0}^{\perp})$	$-0.12 \pm 0.83 \pm 0.71$	$\Im(A_{D^0\bar{D}^0}^{\perp})$	$0.02 \pm 0.80 \pm 0.74$
$\Re(A_{D^0\bar{D}^0}^0)$	$-0.33 \pm 0.91 \pm 0.70$	$\Im(A_{D^0\bar{D}^0}^0)$	$-0.27 \pm 0.77 \pm 0.81$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.06 \pm 0.96 \pm 0.63$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.25 \pm 0.79 \pm 0.67$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.16 \pm 0.91 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.03 \pm 0.85 \pm 0.70$
$\Re(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.17 \pm 0.95 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.28 \pm 0.85 \pm 0.78$
$\Re(A_{D^{*0}\bar{D}^0}^{\parallel})$	$0.02 \pm 0.42 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^0}^{\parallel})$	$-0.46 \pm 0.32 \pm 0.58$
$\Re(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.24 \pm 0.42 \pm 0.70$	$\Im(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.11 \pm 0.39 \pm 0.61$
$\Re(A_{D^{*0}\bar{D}^0}^0)$	$-0.51 \pm 0.41 \pm 0.68$	$\Im(A_{D^{*0}\bar{D}^0}^0)$	$0.12 \pm 0.35 \pm 0.58$
$\Re(\Delta\mathcal{C}_7^{\parallel})$	$0.00 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\parallel})$	$-0.10 \pm 0.03 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^{\perp})$	$-0.05 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\perp})$	$-0.04 \pm 0.04 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^0)$	$0.33 \pm 0.33 \pm 0.09$	$\Im(\Delta\mathcal{C}_7^0)$	$-0.19 \pm 0.20 \pm 0.09$

A lot of numbers describing non-local effects...easier to see graphically

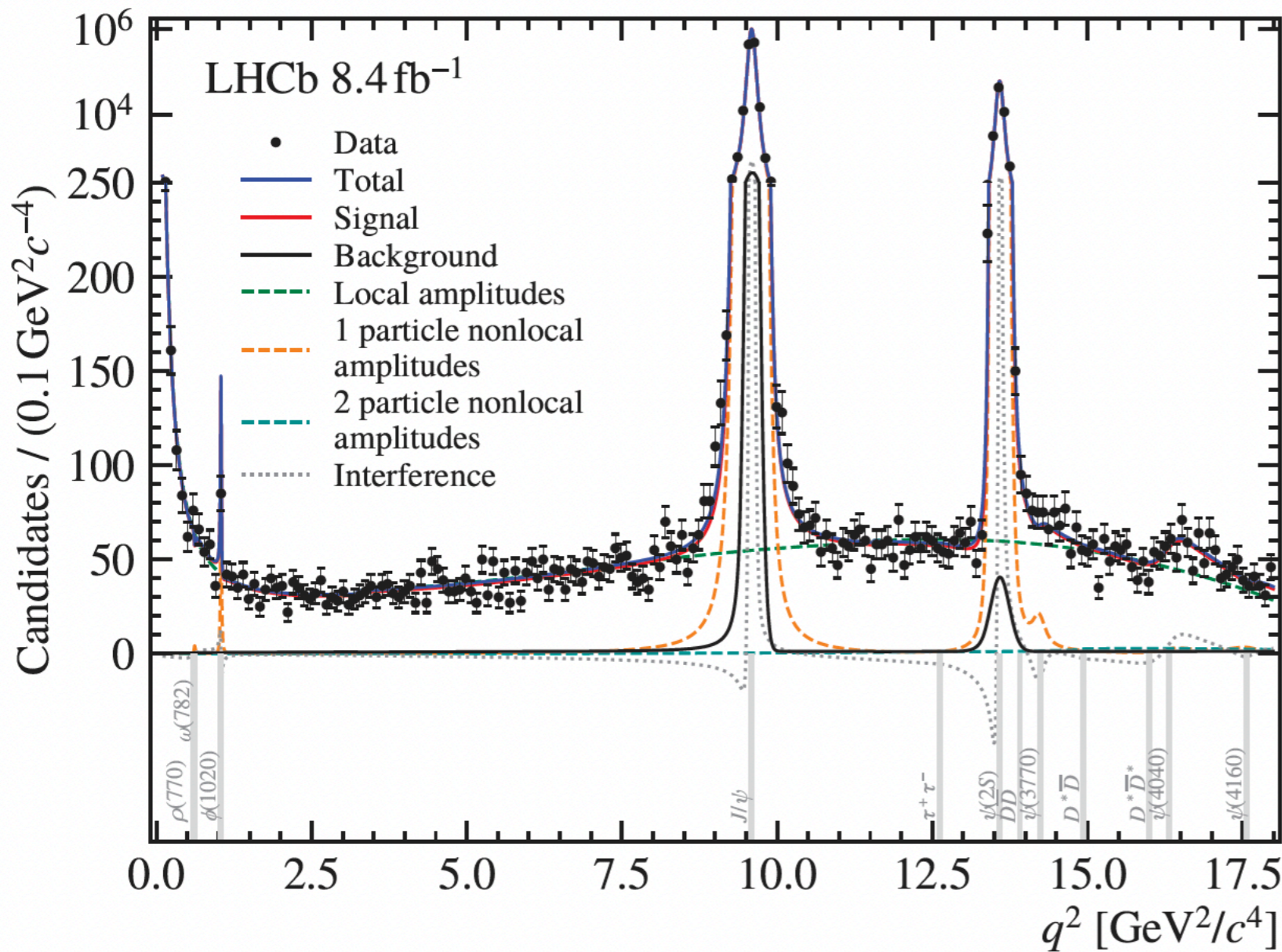
# Amplitude analysis over all $q^2$ : results



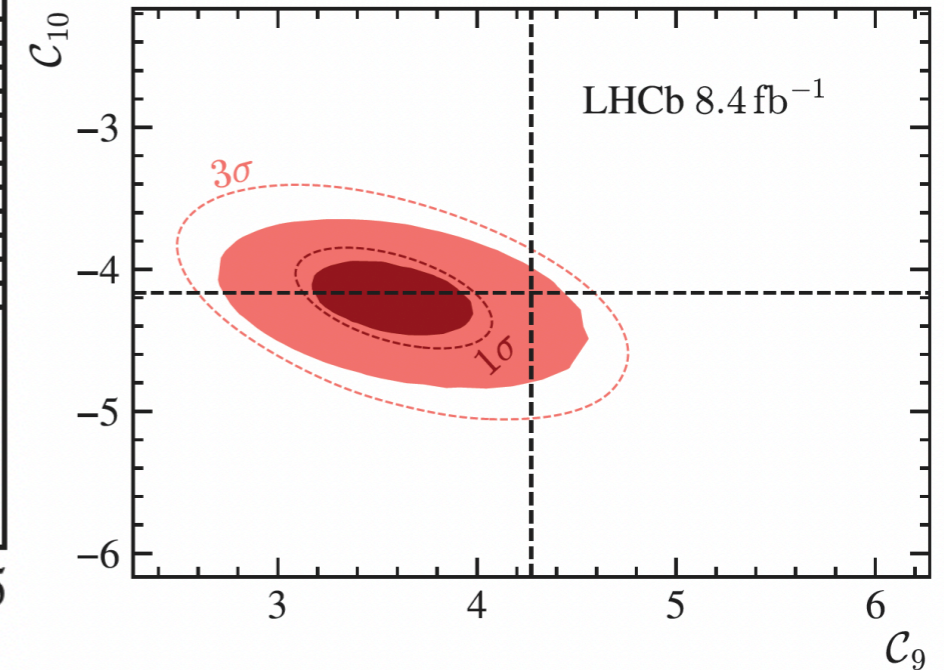
Non-local form factors  
(amplitude analysis +  
z-expansion)

# Amplitude analysis over all $q^2$ : results

$$\Delta\mathcal{C}_9^{\text{NP}} = -0.71 \pm 0.33$$



Wilson Coefficient results	
$\mathcal{C}_9$	$3.56 \pm 0.28 \pm 0.18$
$\mathcal{C}_{10}$	$-4.02 \pm 0.18 \pm 0.16$
$\mathcal{C}'_9$	$0.28 \pm 0.41 \pm 0.12$
$\mathcal{C}'_{10}$	$-0.09 \pm 0.21 \pm 0.06$
$\mathcal{C}_{9\tau}$	$(-1.0 \pm 2.6 \pm 1.0) \times 10^2$



Central value for  $\mathcal{C}_9$  remains consistent with anomalies, but larger uncertainty reduces tension to  $2.1\sigma$



# Semi-leptonic $b$ quark decays

$$\mathcal{H}_{obs} = \mathcal{H}_{SM} + \mathcal{H}_{NP}$$

$$\mathcal{H}_{NP} = \alpha \frac{\kappa}{\Lambda_{NP}^2}$$

$\kappa$  coupling  
NP mass scale

$$\Lambda_{NP}^2 \propto \frac{\kappa}{\mathcal{H}_{obs} - \mathcal{H}_{SM}}$$

Larger observed deviation from SM, lower  $\Lambda_{NP}$  bounds

# Semi-leptonic $b$ quark decays

$$\mathcal{H}_{obs} = \mathcal{H}_{SM} + \mathcal{H}_{NP}$$

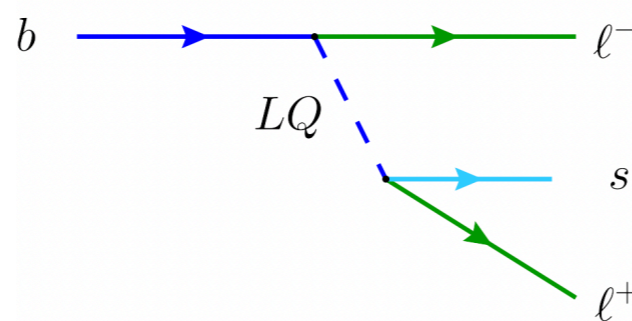
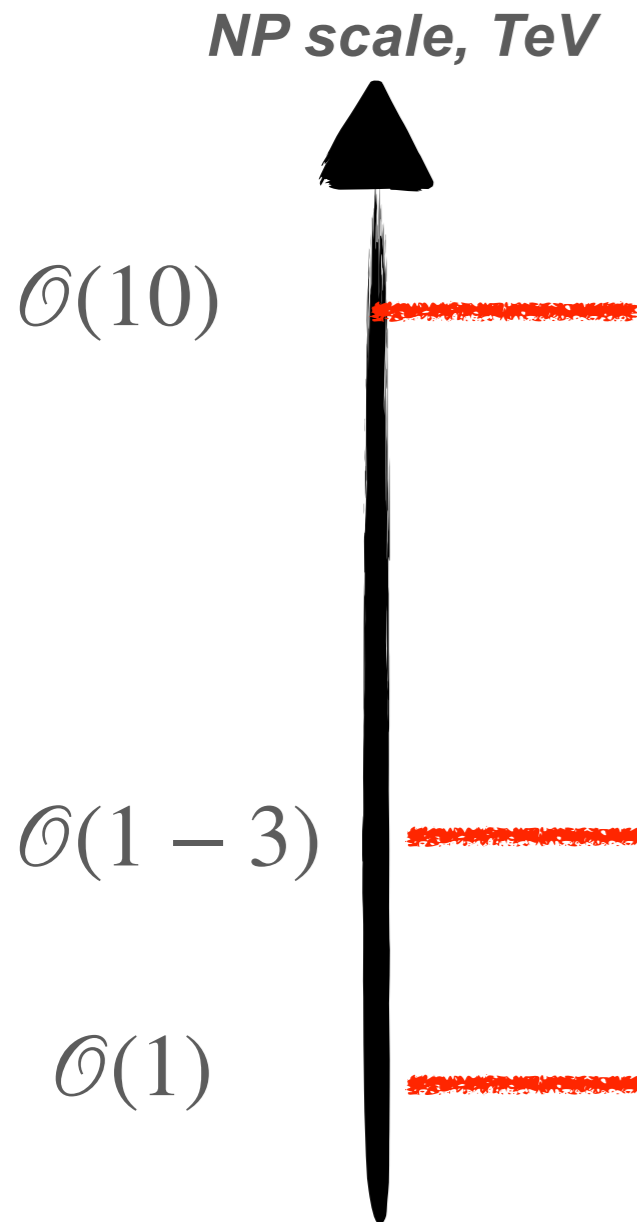
$$\mathcal{H}_{NP} = \alpha \frac{\kappa}{\Lambda_{NP}^2}$$

$\kappa$  coupling

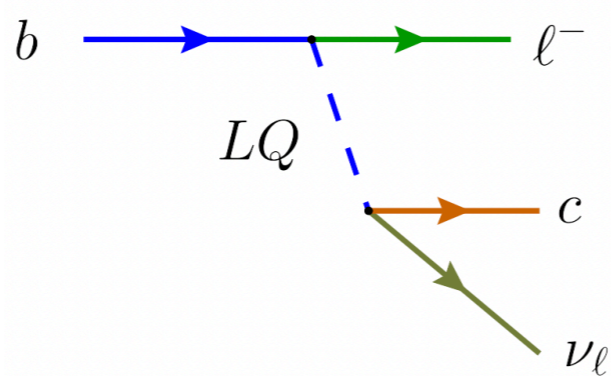
$\Lambda_{NP}^2$  NP mass scale

$$\Lambda_{NP}^2 \propto \frac{\kappa}{\mathcal{H}_{obs} - \mathcal{H}_{SM}}$$

Larger observed deviation from SM, lower  $\Lambda_{NP}$  bounds



$$b \rightarrow s \ell^+ \ell^-$$



$$b \rightarrow c \ell \nu$$

Direct searches

# Semi-leptonic $b$ quark decays

$$\mathcal{H}_{obs} = \mathcal{H}_{SM} + \mathcal{H}_{NP}$$

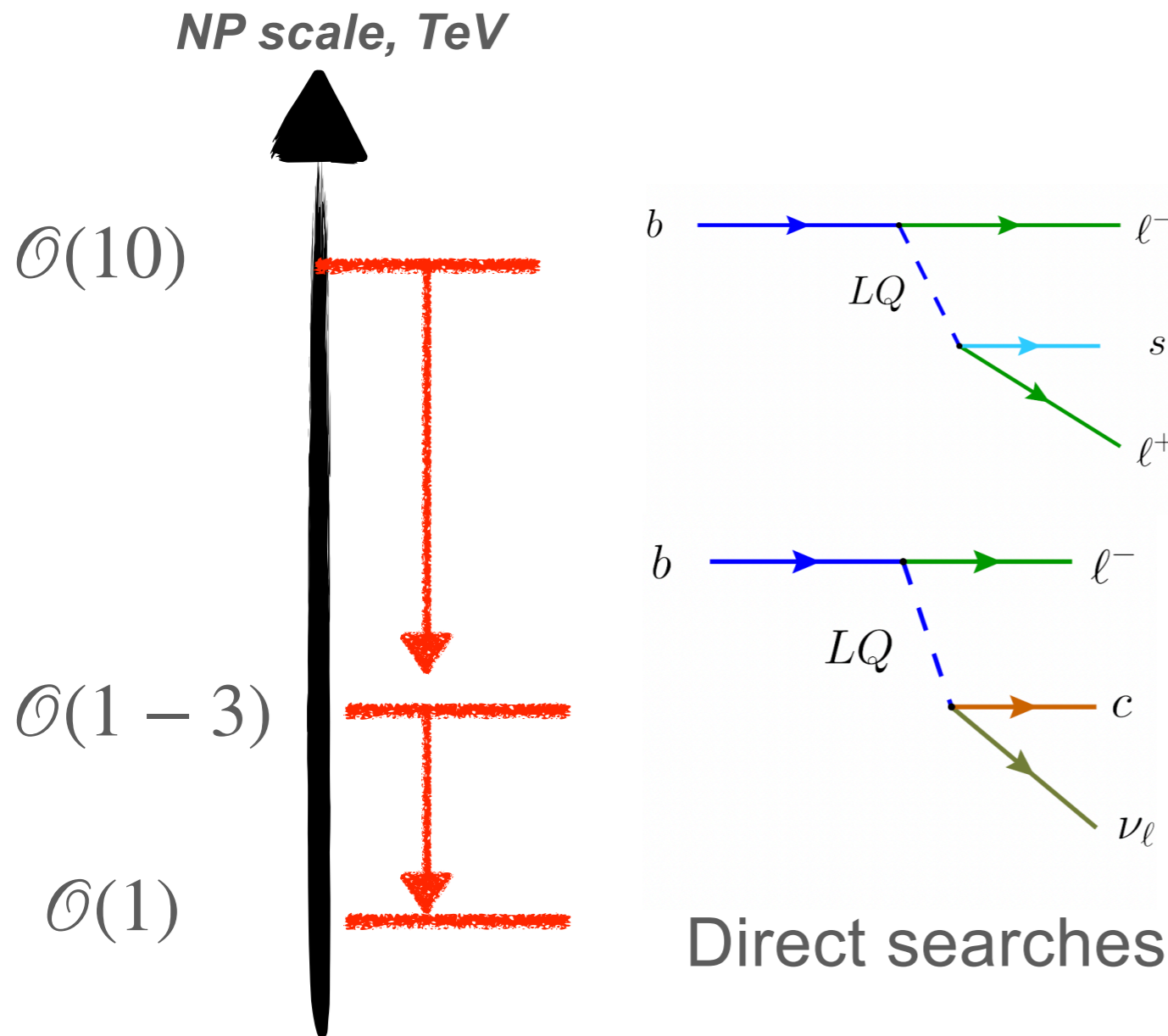
$$\mathcal{H}_{NP} = \propto \frac{\kappa}{\Lambda_{NP}^2}$$

*coupling*

*NP mass scale*

$$\Lambda_{NP}^2 \propto \frac{\kappa}{\mathcal{H}_{obs} - \mathcal{H}_{SM}}$$

Larger observed deviation from SM, lower  $\Lambda_{NP}$  bounds



$$b \rightarrow s \ell^+ \ell^-$$

Suppressed in SM - as high as  $\mathcal{O}(10)$  TeV (can be lower)

$$b \rightarrow c \ell \nu$$

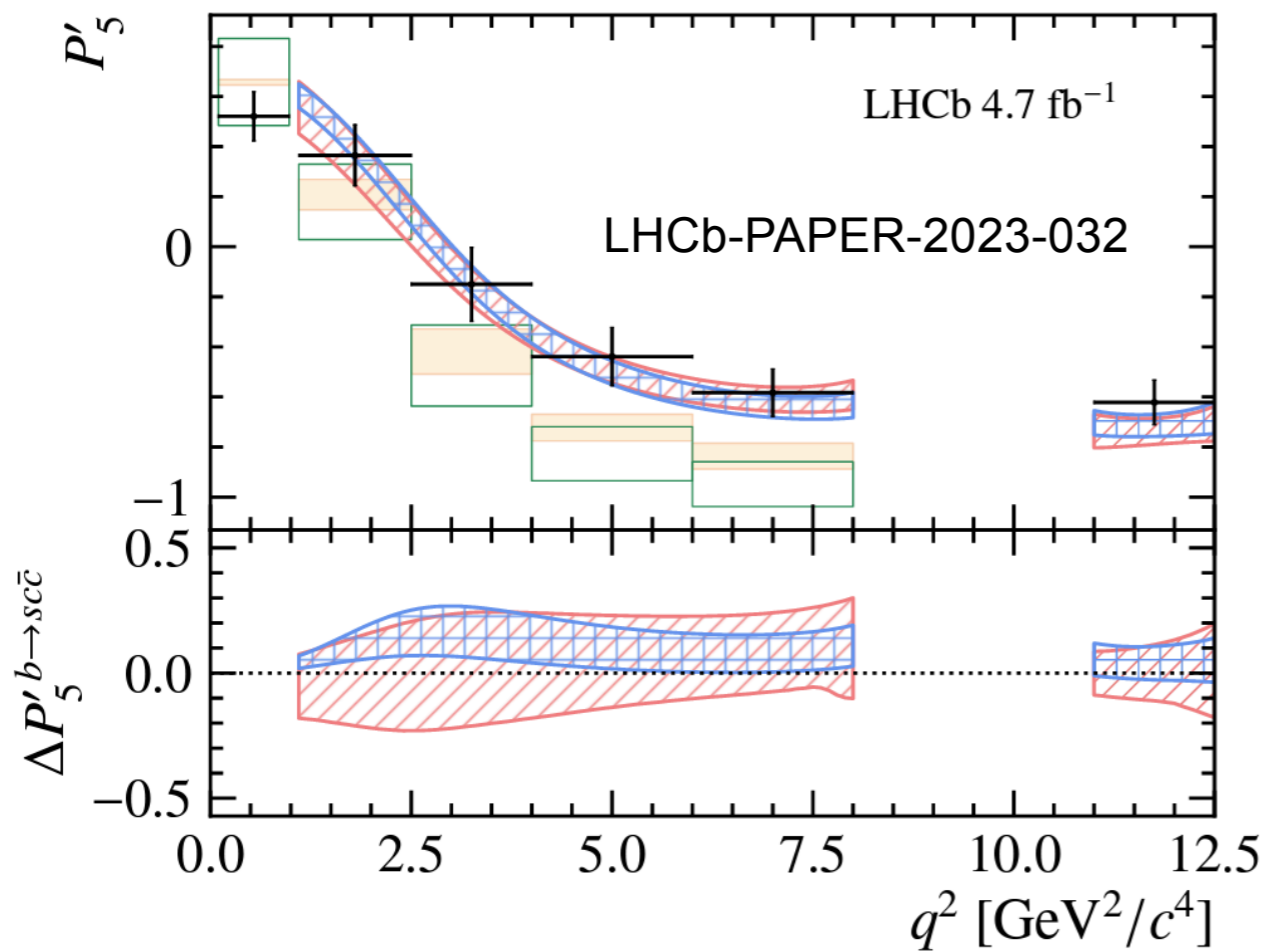
e.g. Stefaneke: [BeyondFlavour2023](#)

Large rate in SM  $\implies$  NP scale lower, tails in direct searches?

# Affect of non-local contributions on angular observables?

Z-expansion

-comparison with previous measurements



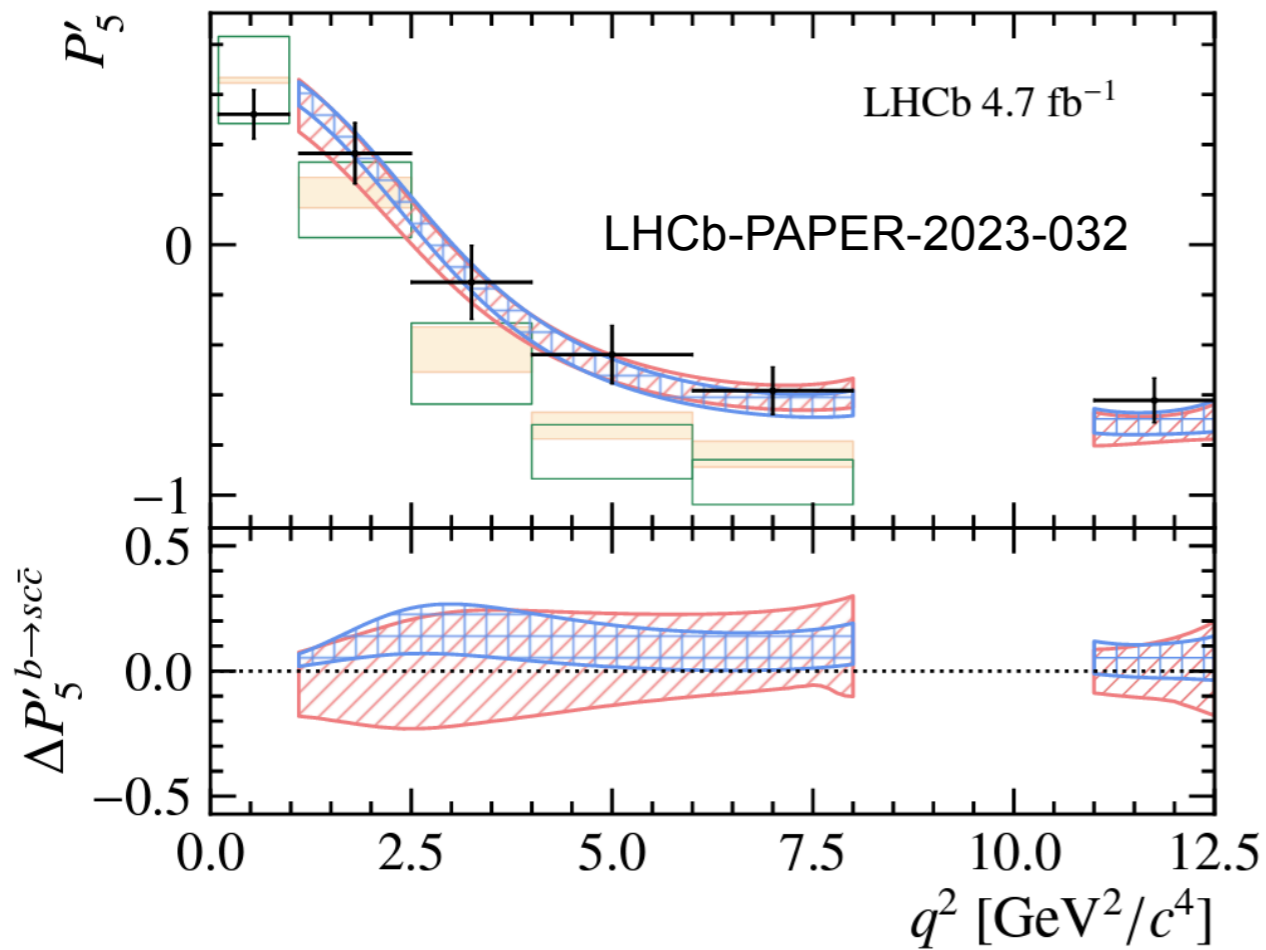
- GRvDV
- DHMV
- $q^2 > 0$  only
- $q^2 < 0$  constr.
- + LHCb PRL 125 (2020) 011802

Agreement with previous measurements

# Affect of non-local contributions on angular observables?

## Z-expansion

-comparison with previous measurements

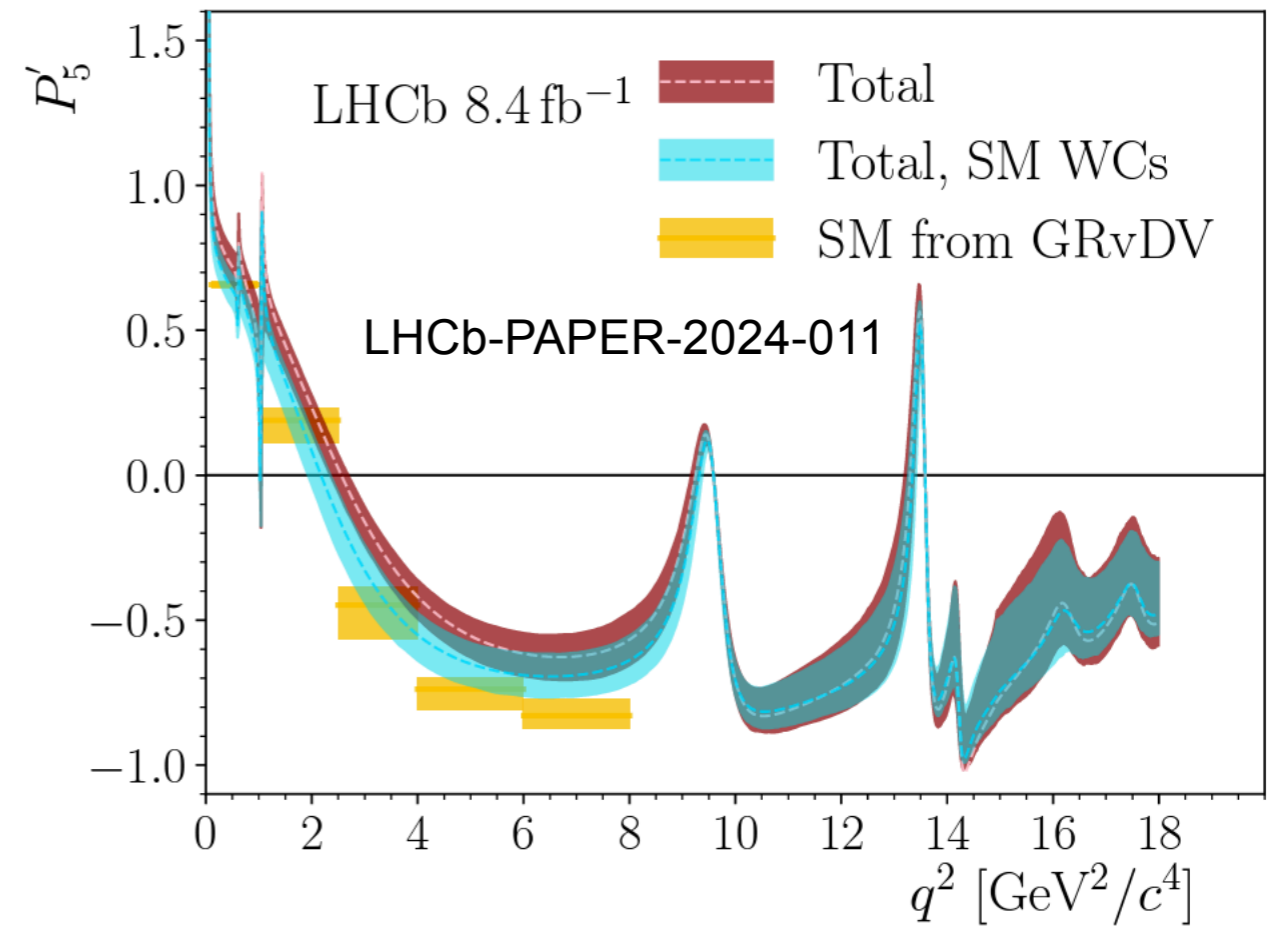


- GRvDV
- DHMV
- $q^2 > 0$  only
- $q^2 < 0$  constr.
- + LHCb PRL 125 (2020) 011802

Agreement with previous measurements

## Amplitude model

- affect on SM predictions



Small modification to SM predictions, but still a shift wrt data

# Size of $H_\lambda(q^2)$ ?

$$H_\lambda(q^2) = \sum_{j=\text{all possible resonances}} A_{\lambda,j} \mathcal{L}(q^2) = |A_{\lambda,j}| e^{i\delta_{j,\lambda}} \mathcal{L}(q^2)$$

Nonlocal parameter results			
$ A_{J/\psi}^{\parallel} $	$(3.98 \pm 0.01 \pm 0.15) \times 10^{-3}$	$\delta_{J/\psi}^{\parallel}$	$0.23 \pm 0.01 \pm 0.01$
$ A_{J/\psi}^{\perp} $	$(3.85 \pm 0.01 \pm 0.14) \times 10^{-3}$	$\delta_{J/\psi}^{\perp}$	$-0.21 \pm 0.00 \pm 0.01$
$ A_{J/\psi}^0 $	–	$\delta_{J/\psi}^0$	$-1.92 \pm 0.05 \pm 0.02$
$ A_{\psi(2S)}^{\parallel} $	$(9.59 \pm 0.28 \pm 0.82) \times 10^{-4}$	$\delta_{\psi(2S)}^{\parallel}$	$0.84 \pm 0.02 \pm 0.19$
$ A_{\psi(2S)}^{\perp} $	$(8.38 \pm 0.27 \pm 0.62) \times 10^{-4}$	$\delta_{\psi(2S)}^{\perp}$	$-0.44 \pm 0.02 \pm 0.11$
$ A_{\psi(2S)}^0 $	$(13.4 \pm 0.4 \pm 1.1) \times 10^{-4}$	$\delta_{\psi(2S)}^0$	$-2.54 \pm 0.13 \pm 0.12$
$ A_{\rho(770)}^0 $	–	$\delta_{\rho(770)}^0$	$1.38 \pm 0.53 \pm 0.65$
$ A_{\omega(782)}^0 $	–	$\delta_{\omega(782)}^0$	$-0.49 \pm 0.92 \pm 0.53$
$ A_{\phi(1020)}^0 $	–	$\delta_{\phi(1020)}^0$	$0.10 \pm 0.82 \pm 0.78$

Nonlocal parameter results ( $\times 10^{-5}$ )			
$\Re(A_{\psi(3770)}^{\parallel})$	$3.68 \pm 1.34 \pm 0.73$	$\Im(A_{\psi(3770)}^{\parallel})$	$2.87 \pm 1.88 \pm 0.49$
$\Re(A_{\psi(3770)}^{\perp})$	$-3.53 \pm 1.45 \pm 0.47$	$\Im(A_{\psi(3770)}^{\perp})$	$-0.86 \pm 1.56 \pm 0.53$
$\Re(A_{\psi(3770)}^0)$	$-3.14 \pm 1.39 \pm 0.60$	$\Im(A_{\psi(3770)}^0)$	$1.67 \pm 1.54 \pm 0.62$
$\Re(A_{\psi(4040)}^{\parallel})$	$-2.39 \pm 1.53 \pm 0.96$	$\Im(A_{\psi(4040)}^{\parallel})$	$-0.71 \pm 1.80 \pm 1.11$
$\Re(A_{\psi(4040)}^{\perp})$	$-2.01 \pm 1.47 \pm 0.59$	$\Im(A_{\psi(4040)}^{\perp})$	$0.35 \pm 1.49 \pm 0.82$
$\Re(A_{\psi(4040)}^0)$	$-5.62 \pm 1.71 \pm 1.07$	$\Im(A_{\psi(4040)}^0)$	$1.32 \pm 1.87 \pm 0.99$
$\Re(A_{\psi(4160)}^{\parallel})$	$0.04 \pm 1.72 \pm 0.56$	$\Im(A_{\psi(4160)}^{\parallel})$	$1.91 \pm 1.98 \pm 1.45$
$\Re(A_{\psi(4160)}^{\perp})$	$-2.81 \pm 1.75 \pm 0.61$	$\Im(A_{\psi(4160)}^{\perp})$	$0.32 \pm 0.15 \pm 0.09$
$\Re(A_{\psi(4160)}^0)$	$1.03 \pm 1.77 \pm 0.39$	$\Im(A_{\psi(4160)}^0)$	$-1.66 \pm 1.67 \pm 1.04$

Nonlocal parameter results			
$\Re(A_{D^0\bar{D}^0}^{\parallel})$	$-0.07 \pm 0.93 \pm 0.69$	$\Im(A_{D^0\bar{D}^0}^{\parallel})$	$-0.44 \pm 0.71 \pm 0.73$
$\Re(A_{D^0\bar{D}^0}^{\perp})$	$-0.12 \pm 0.83 \pm 0.71$	$\Im(A_{D^0\bar{D}^0}^{\perp})$	$0.02 \pm 0.80 \pm 0.74$
$\Re(A_{D^0\bar{D}^0}^0)$	$-0.33 \pm 0.91 \pm 0.70$	$\Im(A_{D^0\bar{D}^0}^0)$	$-0.27 \pm 0.77 \pm 0.81$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.06 \pm 0.96 \pm 0.63$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\parallel})$	$-0.25 \pm 0.79 \pm 0.67$
$\Re(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.16 \pm 0.91 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^{\perp})$	$-0.03 \pm 0.85 \pm 0.70$
$\Re(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.17 \pm 0.95 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^{*0}}^0)$	$-0.28 \pm 0.85 \pm 0.78$
$\Re(A_{D^{*0}\bar{D}^0}^{\parallel})$	$0.02 \pm 0.42 \pm 0.66$	$\Im(A_{D^{*0}\bar{D}^0}^{\parallel})$	$-0.46 \pm 0.32 \pm 0.58$
$\Re(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.24 \pm 0.42 \pm 0.70$	$\Im(A_{D^{*0}\bar{D}^0}^{\perp})$	$-0.11 \pm 0.39 \pm 0.61$
$\Re(A_{D^{*0}\bar{D}^0}^0)$	$-0.51 \pm 0.41 \pm 0.68$	$\Im(A_{D^{*0}\bar{D}^0}^0)$	$0.12 \pm 0.35 \pm 0.58$
$\Re(\Delta\mathcal{C}_7^{\parallel})$	$0.00 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\parallel})$	$-0.10 \pm 0.03 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^{\perp})$	$-0.05 \pm 0.03 \pm 0.02$	$\Im(\Delta\mathcal{C}_7^{\perp})$	$-0.04 \pm 0.04 \pm 0.01$
$\Re(\Delta\mathcal{C}_7^0)$	$0.33 \pm 0.33 \pm 0.09$	$\Im(\Delta\mathcal{C}_7^0)$	$-0.19 \pm 0.20 \pm 0.09$