

Probing Medium Properties in Ultra-Central Collisions

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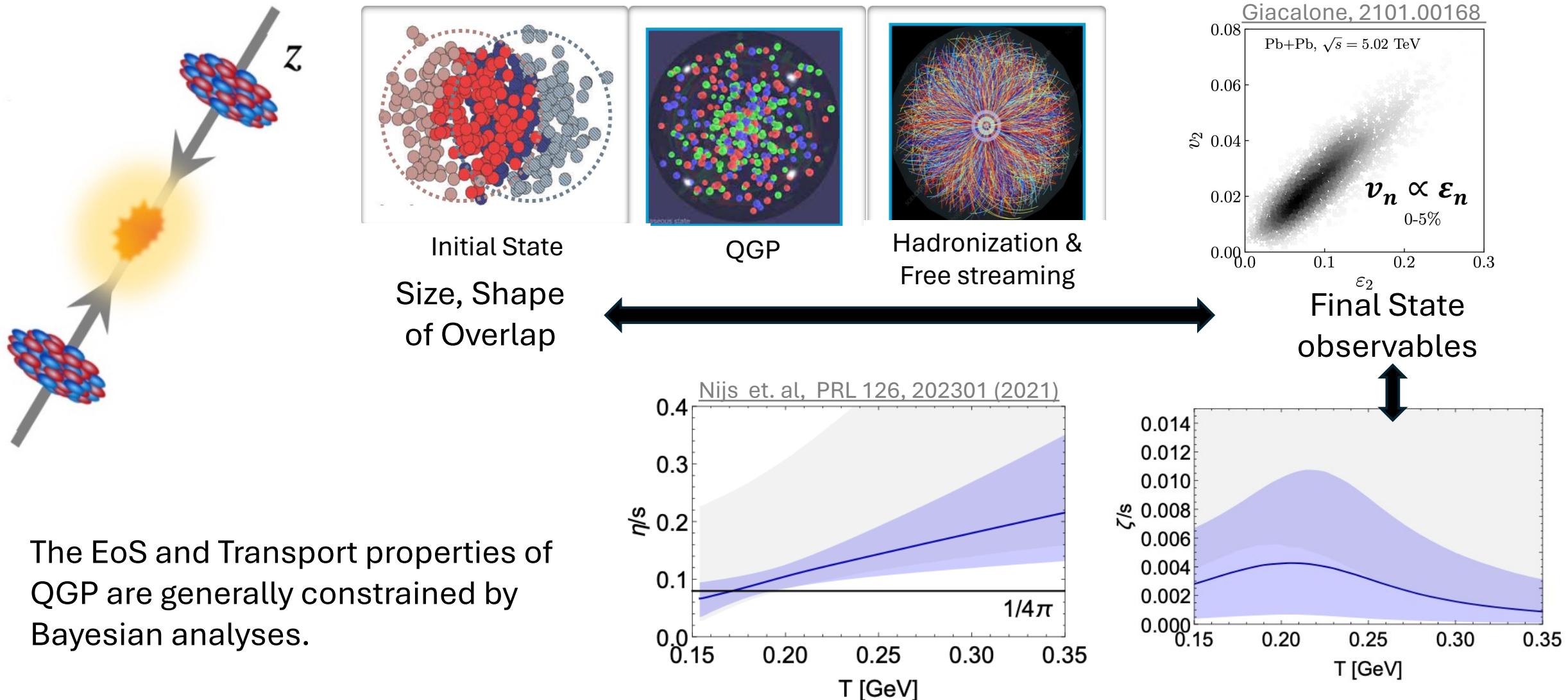
On behalf of: ALICE, ATLAS & CMS



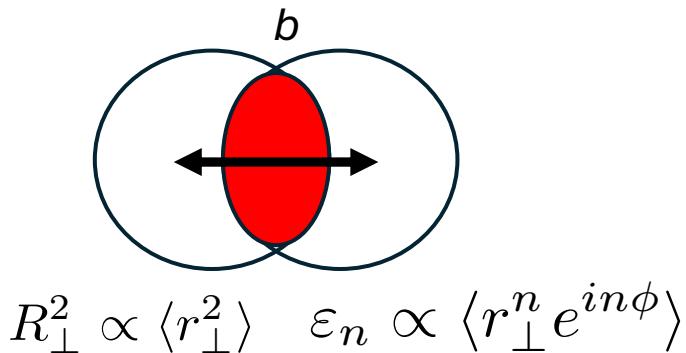
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University



Relativistic Heavy-Ion Collisions



“Geometry” of Initial State Overlap Region

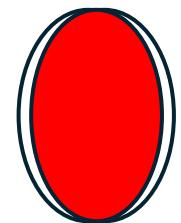
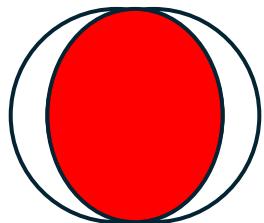


Experimentally Characterized by “Centrality” of collisions:

“Geometry” of initial state → **Size** **Shape**

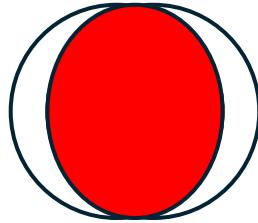
Controlled by: **1. Nuclear Deformation.**
2. Impact Parameter (b).
3. Quantum Fluctuations in position of nucleons.

1.



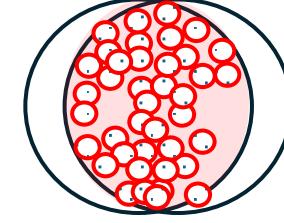
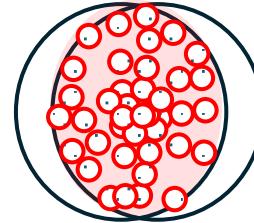
$R_{\perp} \uparrow, \varepsilon_2 \uparrow$
Spherical vs. Deformed Nucleus

2.



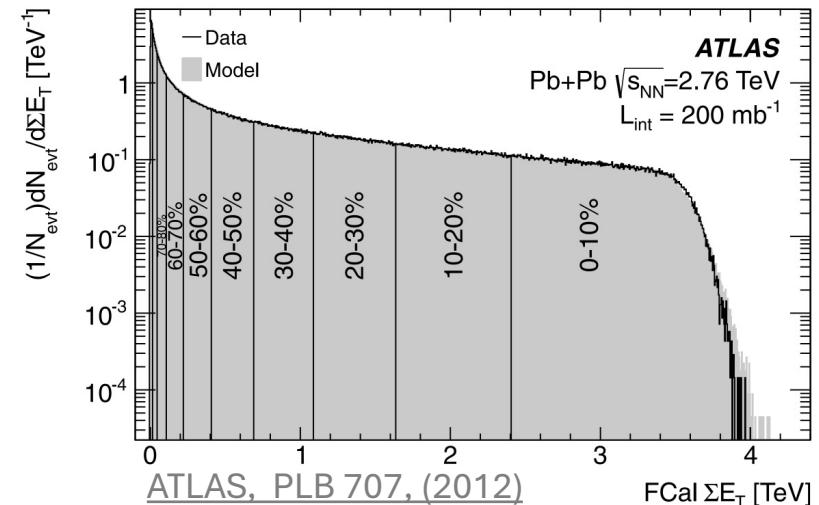
$b \downarrow \Rightarrow R_{\perp} \uparrow, \varepsilon_2 \downarrow$

3.



Same b , but different R_{\perp}, ε_2

- Most-Central collisions have $b \approx 0$, max. overlap Area \Rightarrow Ideal to probe factors controlling initial state
- Note: Currently no clear definition of UCC, 1% centrality is commonly used.

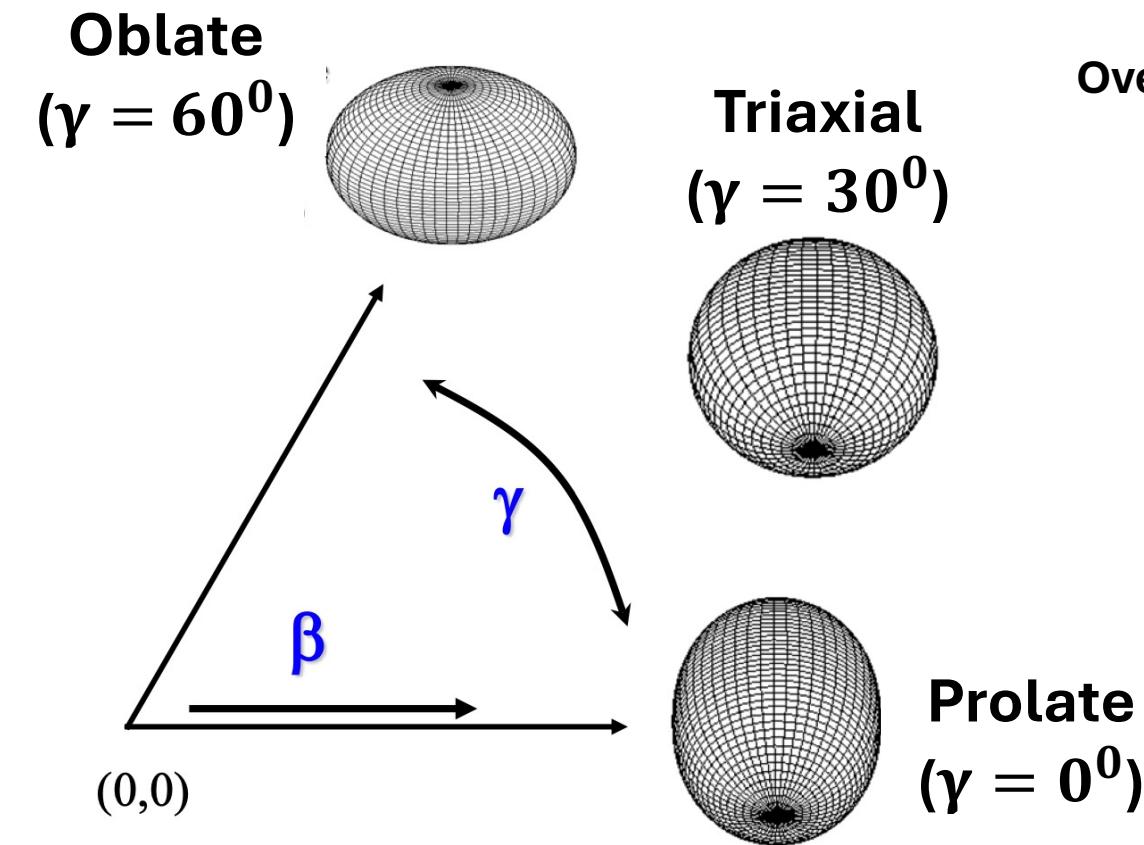


Effect of Nuclear Deformation on Overlap Geometry

- Usually, the geometry of colliding nuclei approximated using a Woods-Saxon form:

$$\rho(r) = \frac{\rho_0}{[1 + \exp(r - R(\theta, \phi))/a]}$$

$$R(\theta, \phi) = R_0(1 + \beta(\cos\gamma Y_{20}(\theta, \phi) + \sin\gamma Y_{22}(\theta, \phi)))$$



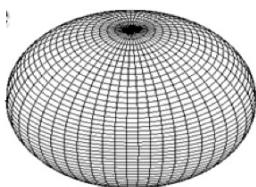
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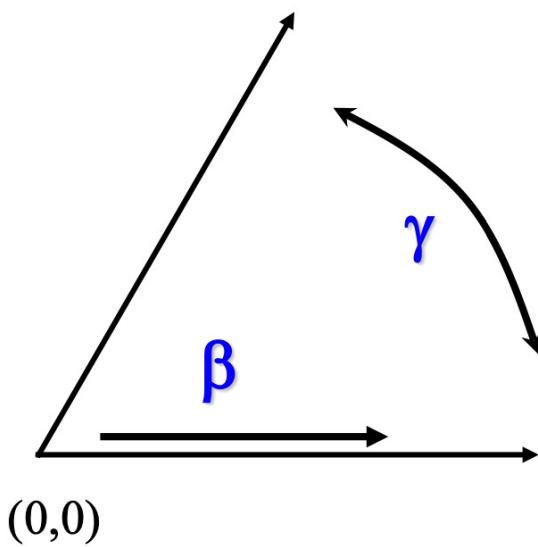
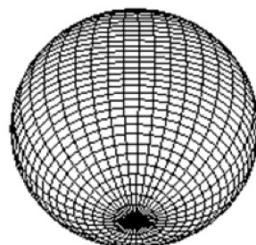
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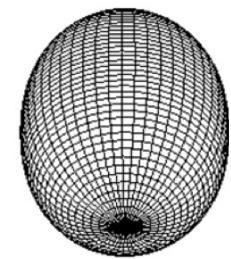
Oblate
 $(\gamma = 60^\circ)$



Triaxial
 $(\gamma = 30^\circ)$



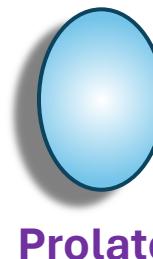
Prolate
 $(\gamma = 0^\circ)$



Overall Quadrupole Deformation

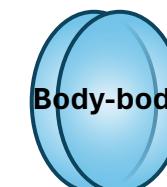
Triaxiality

Nucleus Geometry



Prolate

Central Collision configurations



Body-body



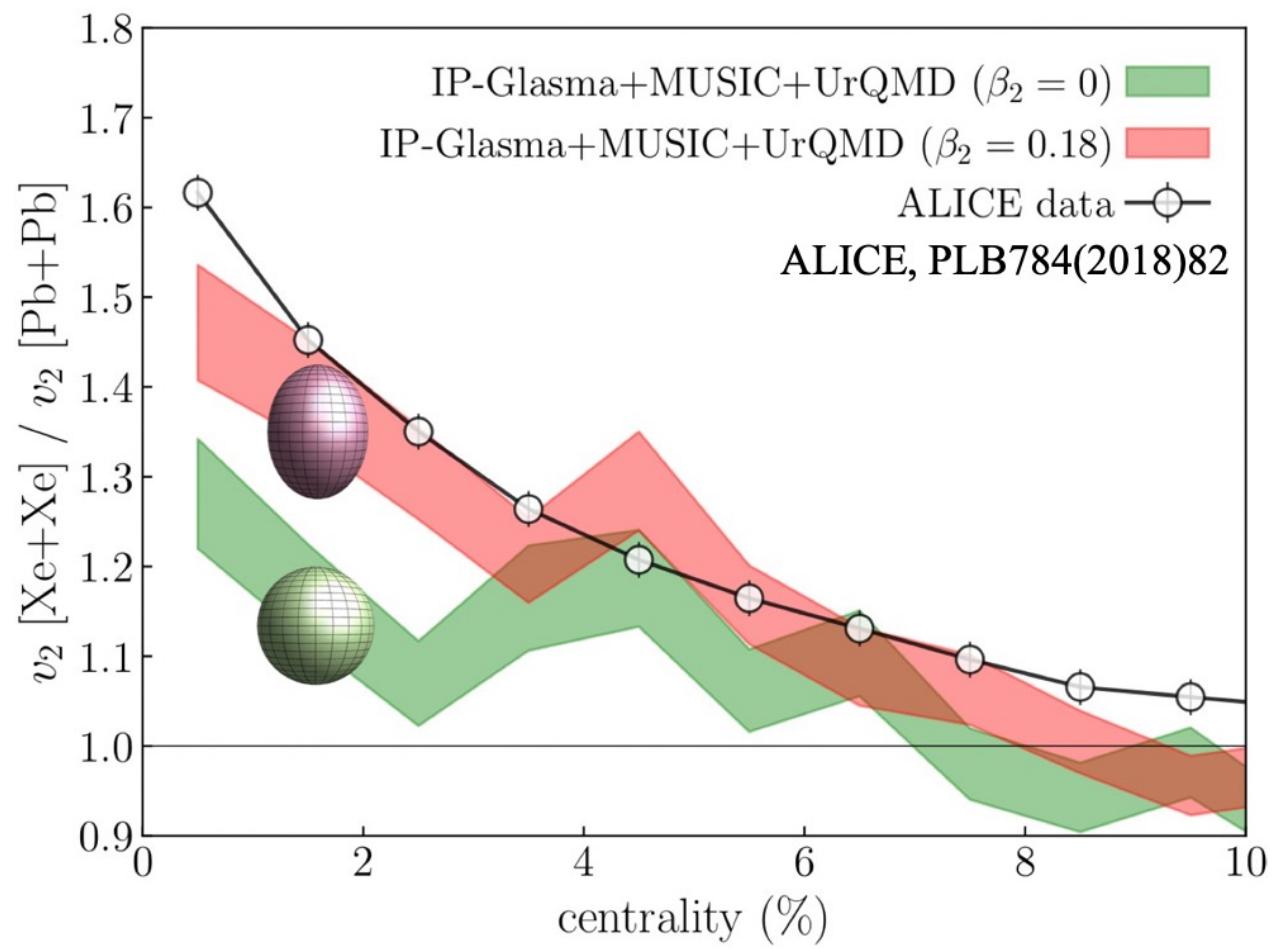
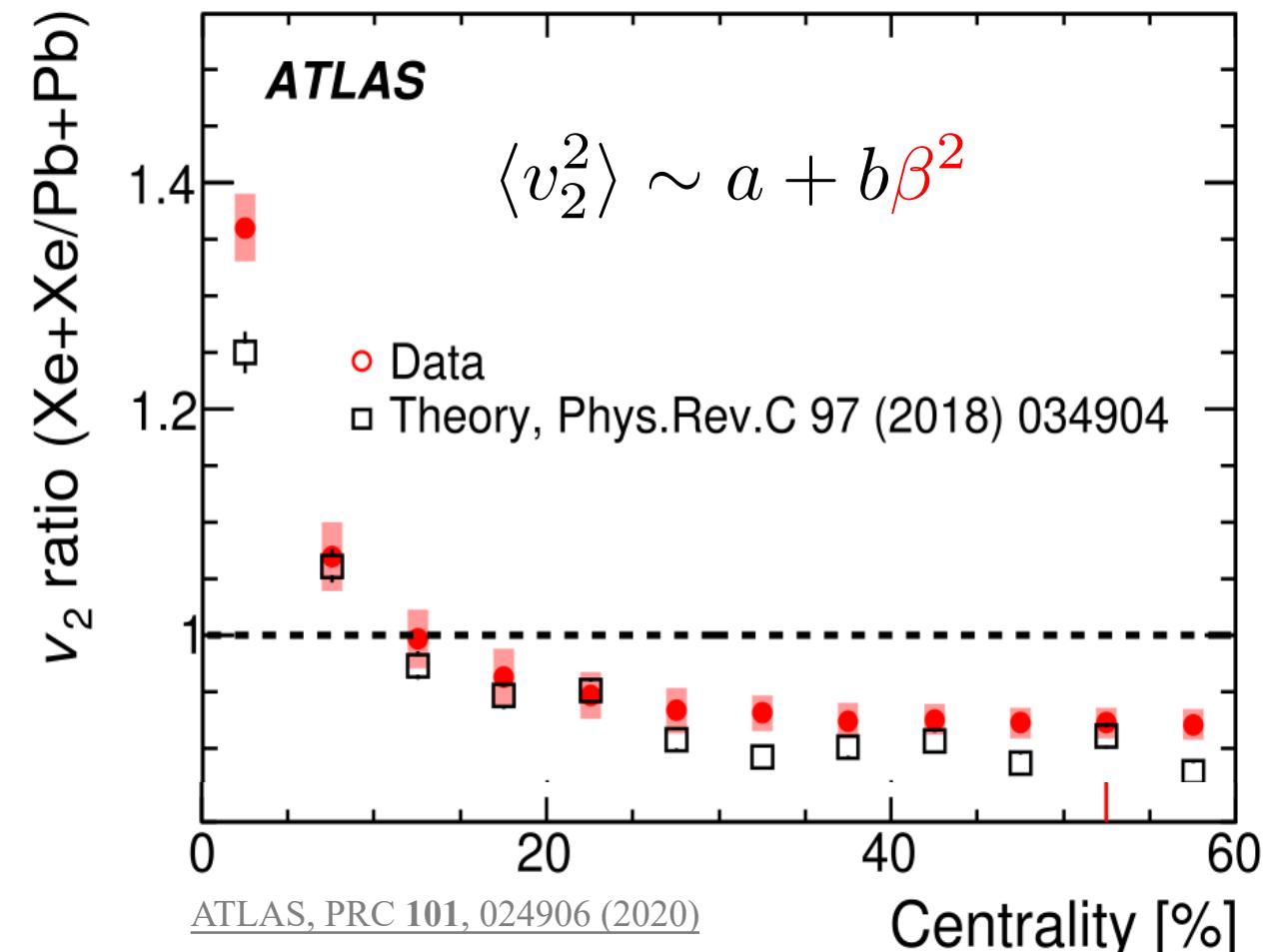
Tip-tip

$\epsilon_2 \uparrow, d_\perp \uparrow$

$\epsilon_2 \downarrow, d_\perp \downarrow$

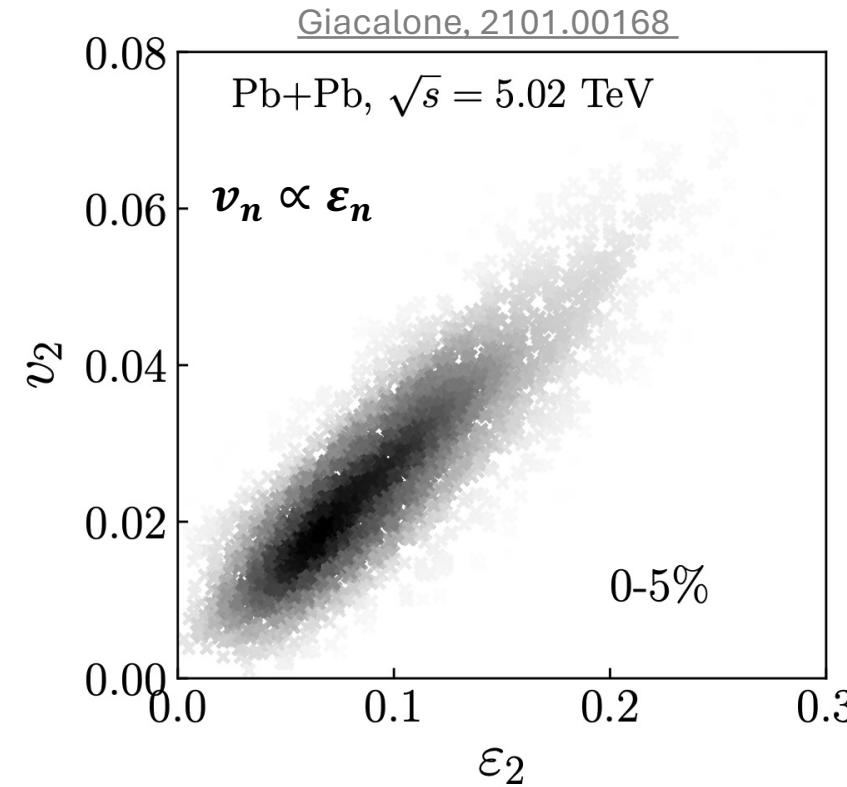
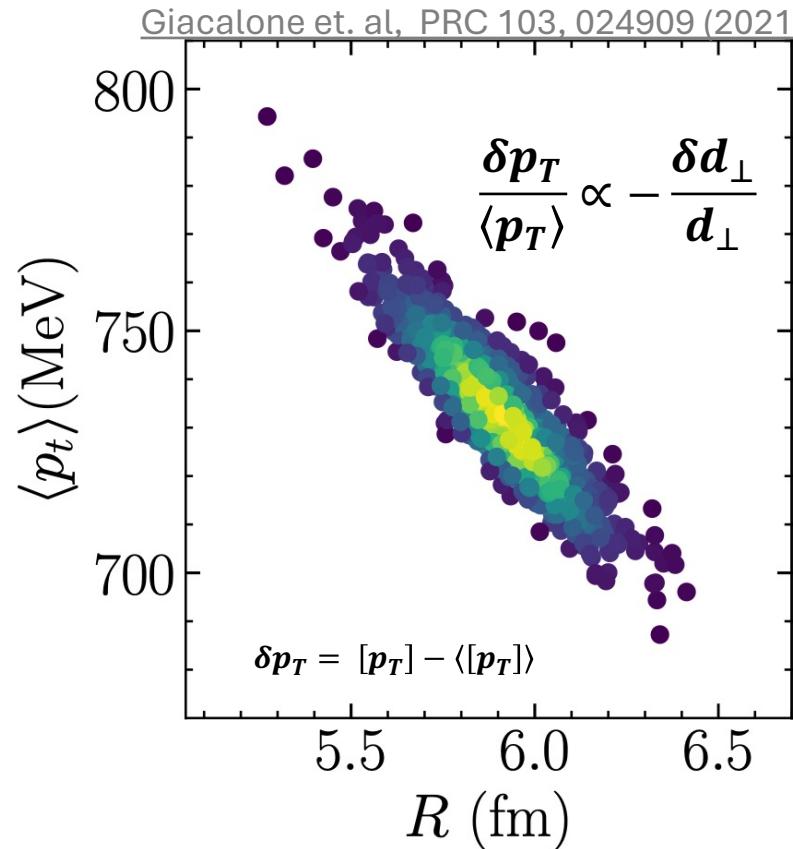
- Nuclear deformation expected to enhance eccentricity and size fluctuations of overlap region

Constraining β using 2-particle correlation measurements



- Nuclear deformation inputs (eg: $\beta_{2,Xe} \geq 0.18$) are essential to describe experimentally measured $v_{2,Xe}$.
- In turn, nuclear deformation should be input in Bayesian analyses to constrain initial state.

Constraining Triaxiality (γ) using Heavy-Ion Collisions



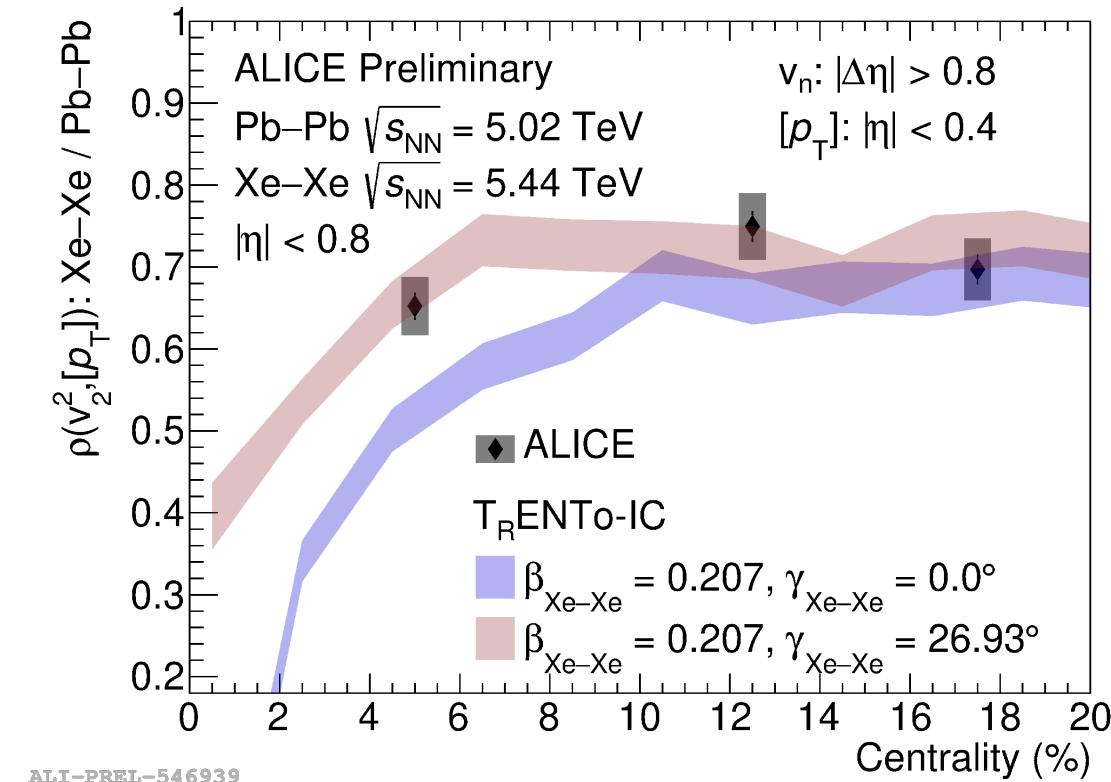
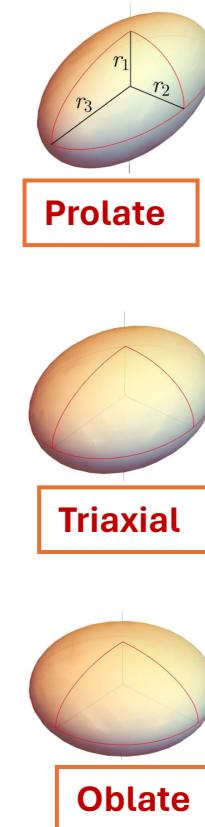
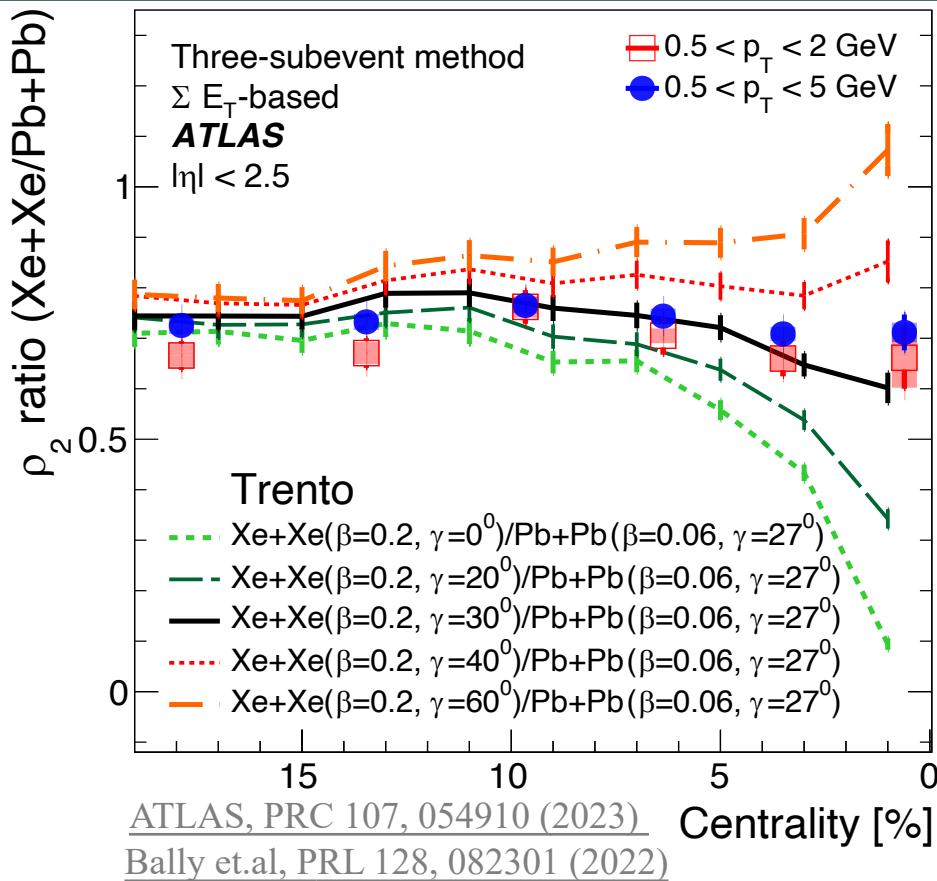
$\varepsilon_n - d_\perp$ Correlation $\Leftrightarrow v_n - [p_T]$ Correlation (ρ_n):
“Shape-Size Correlation”

$$\rho(v_n^2, [p_T]) = \frac{cov(v_n^2, [p_T])}{\sqrt{var(v_n^2\{2\})_{dyn} c_k}}$$

3-particle
Correlation

- ρ_n provides important constraint on origin of final state as a response to initial state fluctuations.

Constraining γ Using ρ_n Measurements

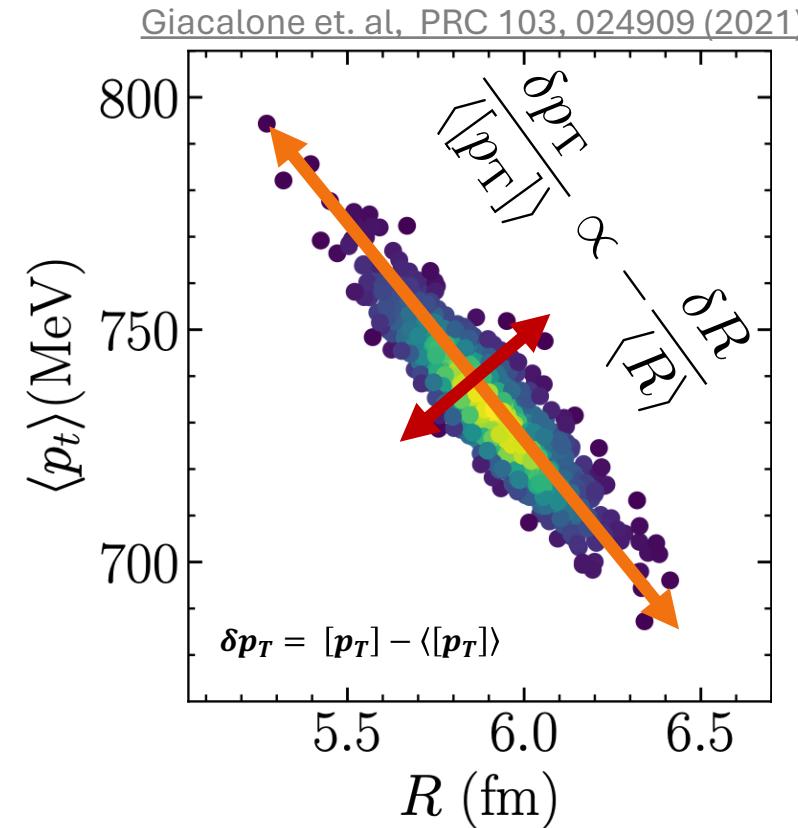


$\langle v_2^2 \delta p_T \rangle \sim a - b \langle \beta^3 \cos(3\gamma) \rangle$ ➤ Pb corresponds to $\beta \sim 0.06$ and $\gamma \sim 27^\circ$ (near spherical);
Xe corresponds to $\beta \sim 0.21$ and $\gamma \sim 27^\circ$ (highly deformed triaxial nucleus).

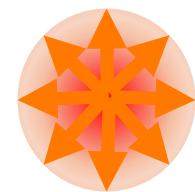
➤ Ultra-Central heavy ion collisions provide ideal conditions to constrain Nuclear structure, which controls geometry of initial state

Geometric and Non-Geometric Fluctuations

- On an event-by event basis, there are two sources of fluctuations influencing final state measured $\langle [p_T] \rangle$

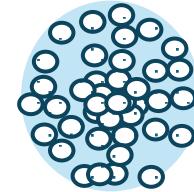


Geometric: hydrodynamic response to the size fluctuations



“Geometric Component”

Intrinsic: Fluctuations arising from Initial state, medium evolution.

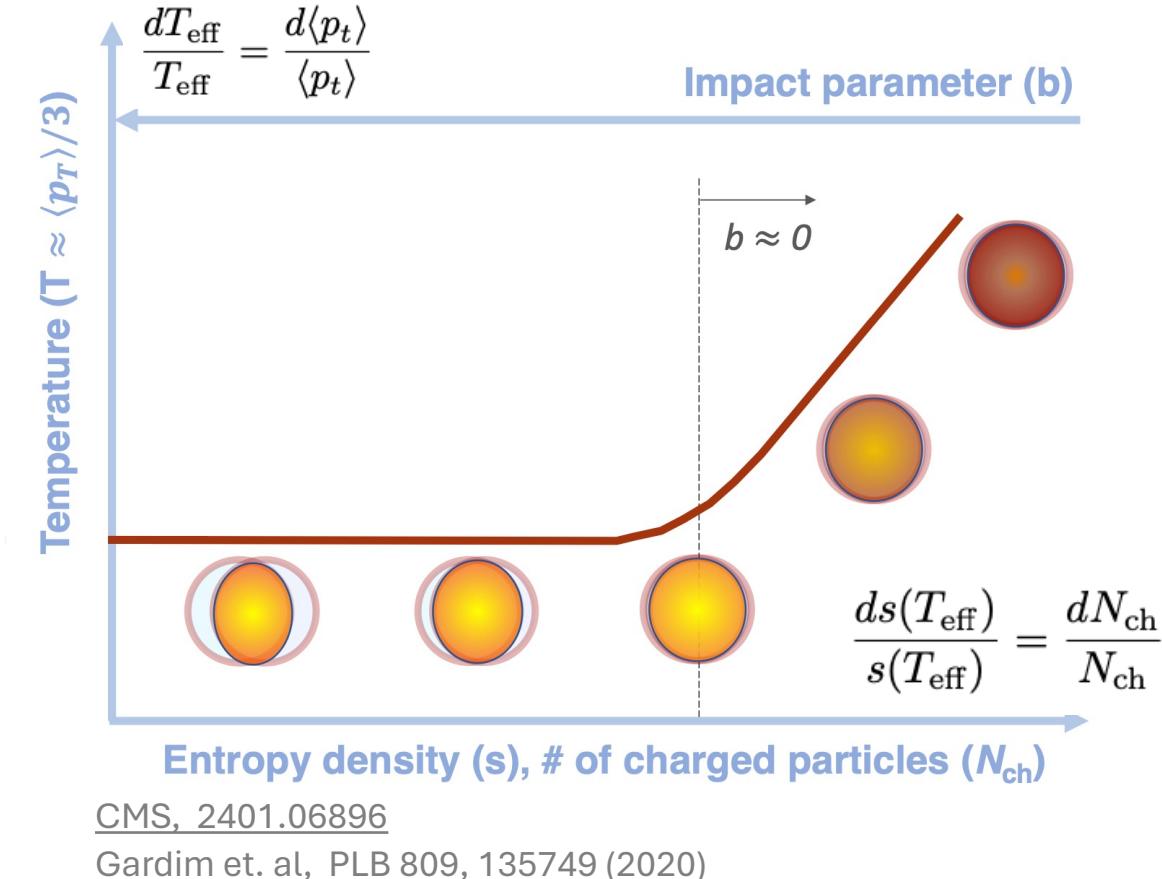
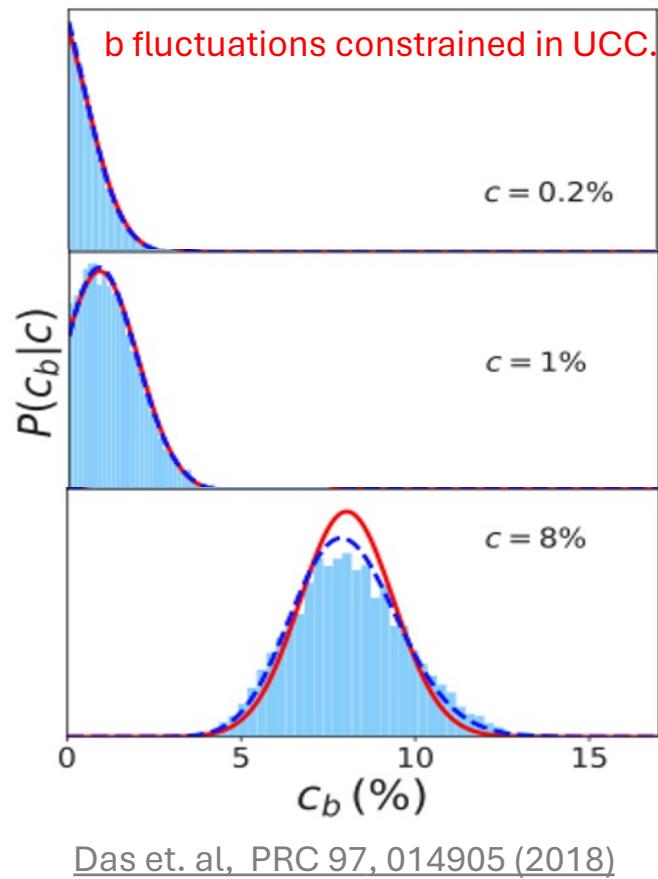


“Intrinsic Component”

$$\text{Event-by-Event } [p_T] \text{ Fluctuations} = \text{ Geometric} + \text{ Intrinsic}$$

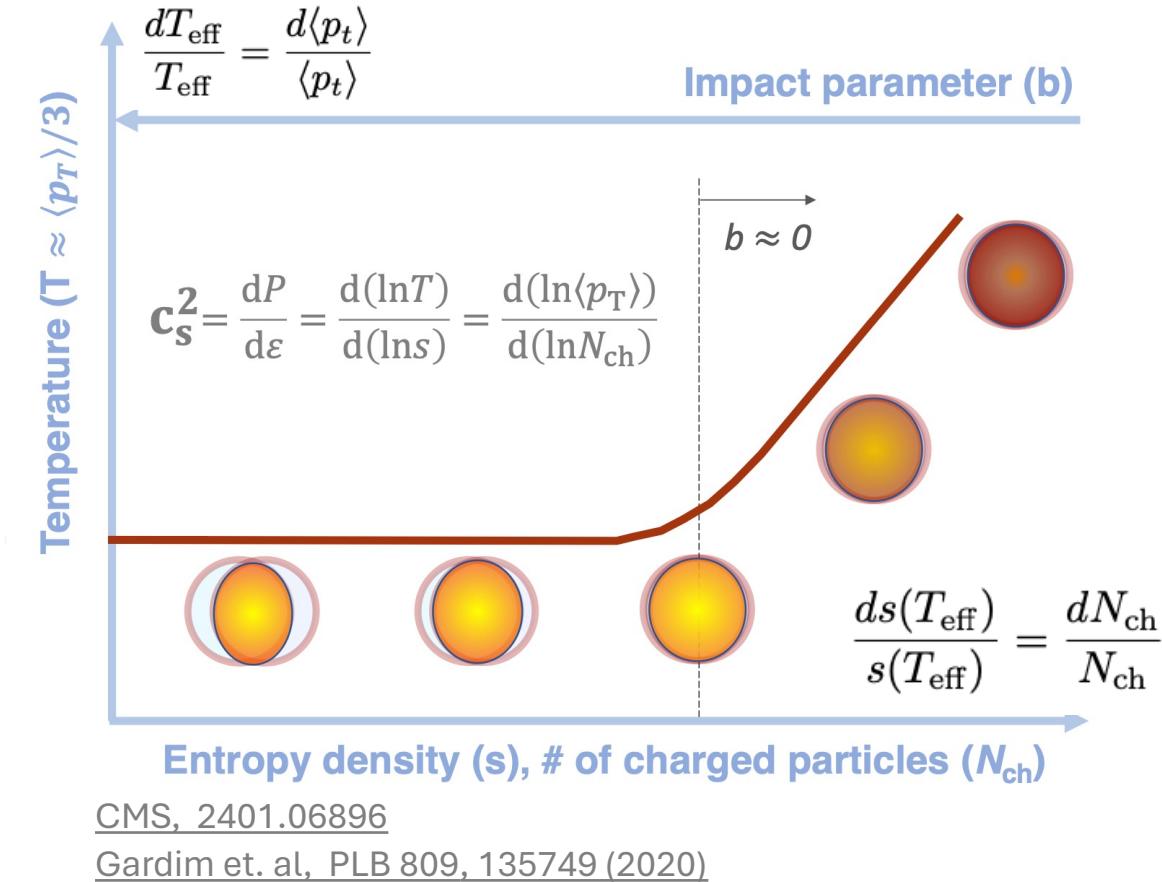
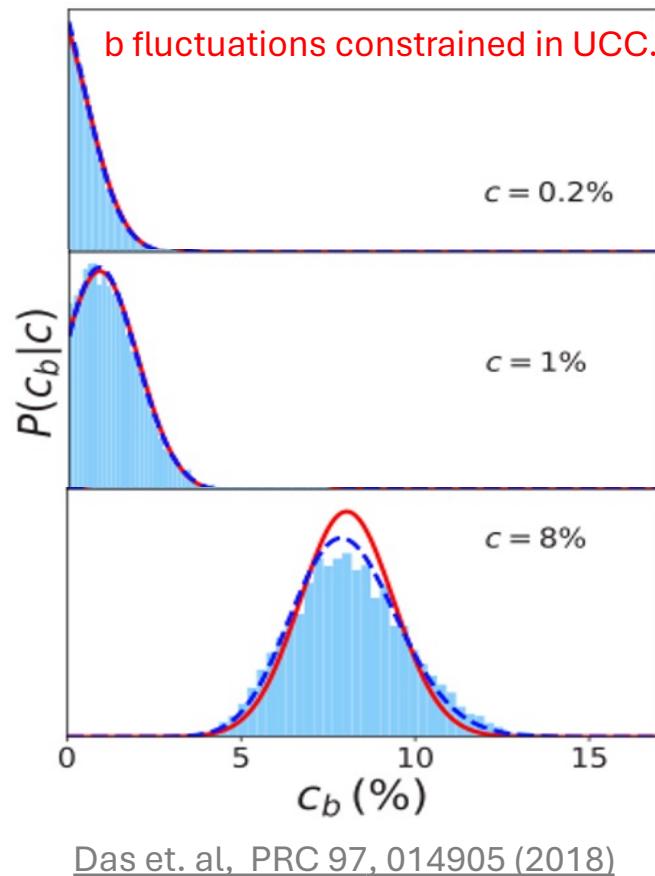
- Distinguishing Geometric and Intrinsic fluctuations is important to constrain both initial state and medium evolution.

Using Mean of $P([p_T])$ to Constrain c_S



- In UCC, within approximately fixed geometry (b), choosing larger N_{ch} chooses events with larger entropy density arising from intrinsic component.
- Larger entropy density within a fixed geometry leads to larger radial push or $\langle [p_T] \rangle$.

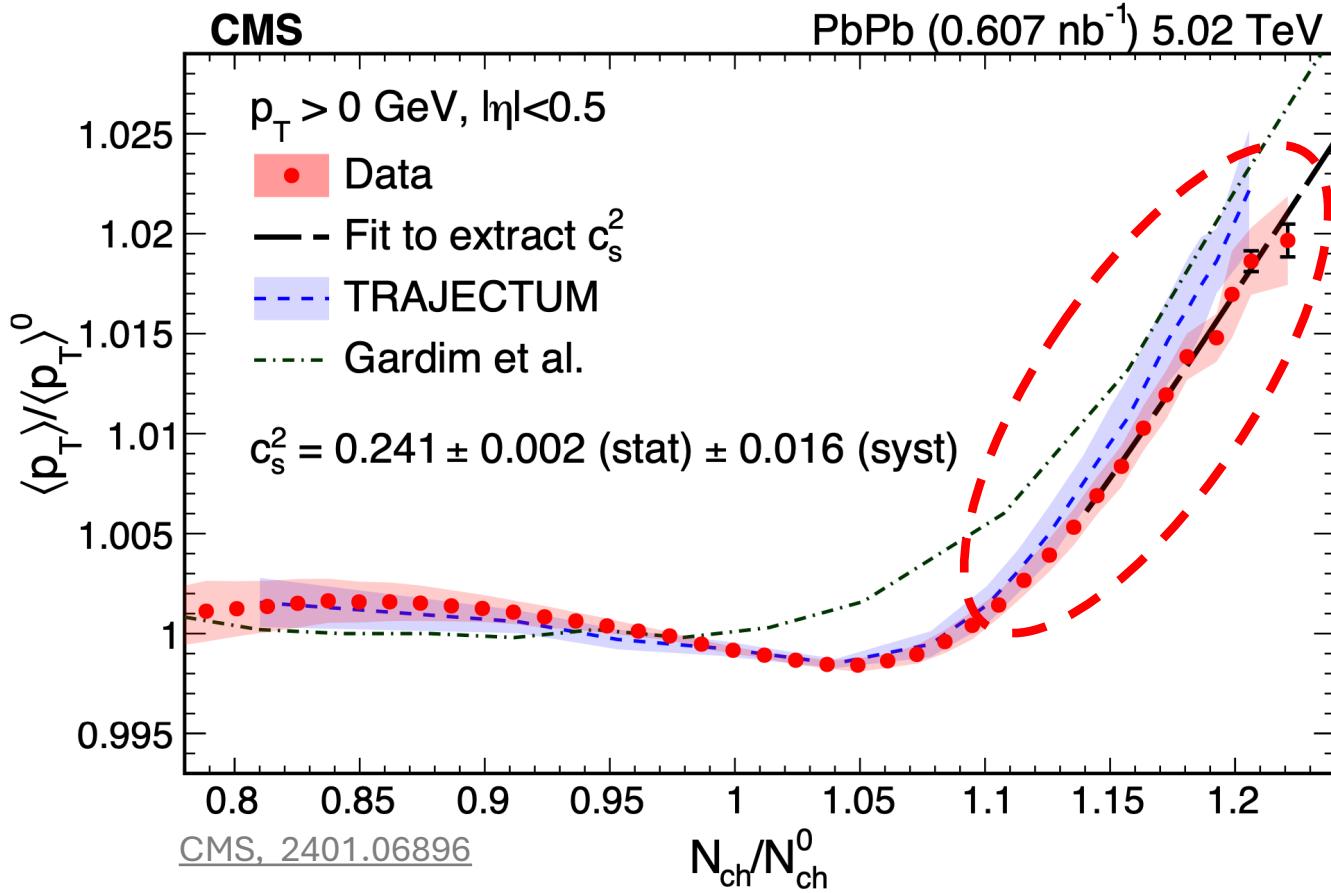
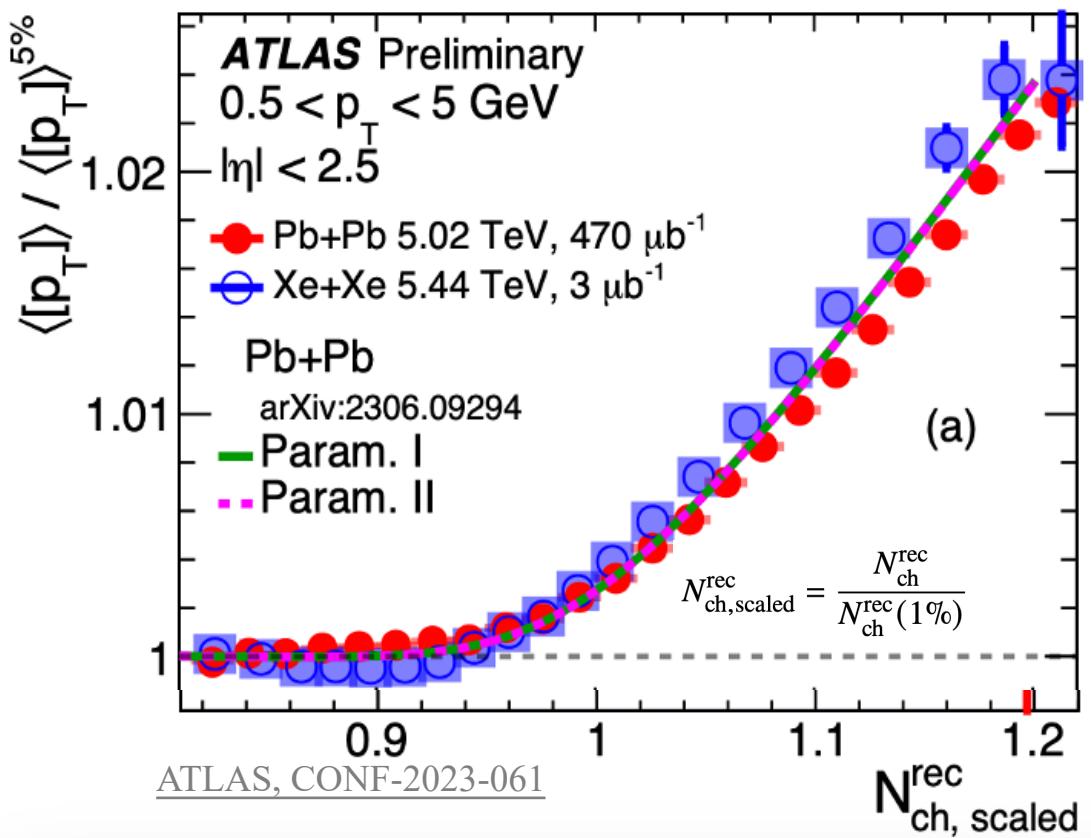
Using Mean of $P([p_T])$ to Constrain c_s



- The slope of this rise of $\langle\langle p_T \rangle\rangle$ in UCC can be related to speed of sound of QGP:

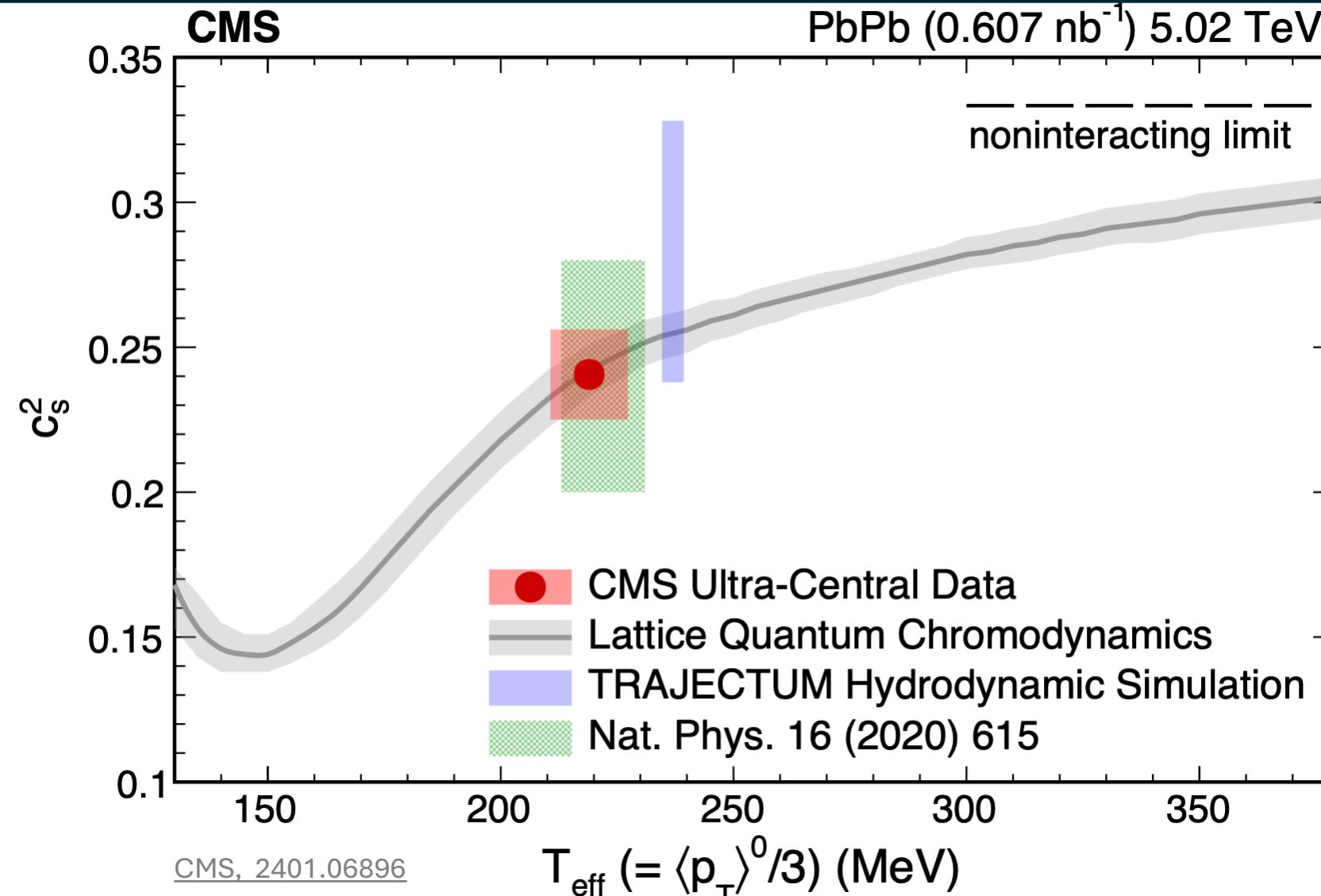
$$c_s^2 = \frac{dP}{d\epsilon} = \frac{d(\ln T)}{d(\ln s)} = \frac{d(\ln \langle p_T \rangle)}{d(\ln N_{\text{ch}})}$$

Using Mean of $\langle [p_T] \rangle$ to Constrain c_s



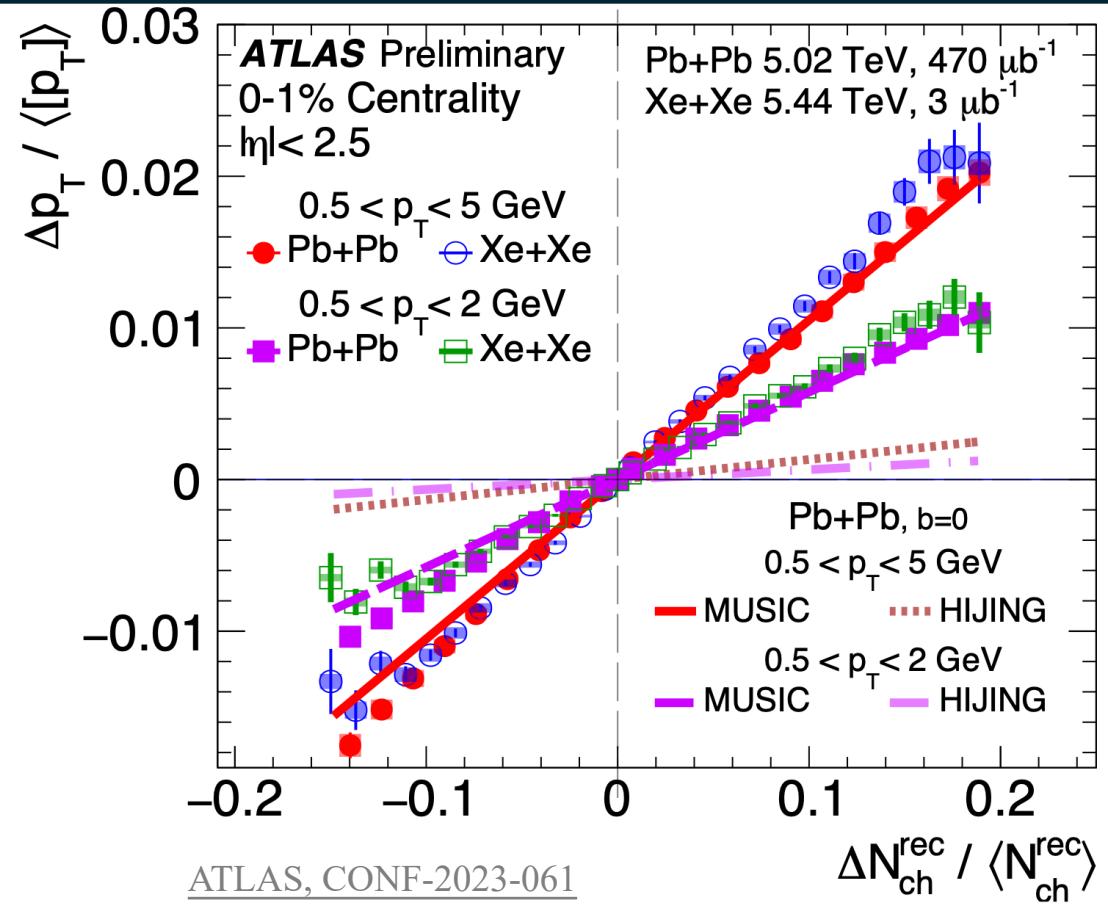
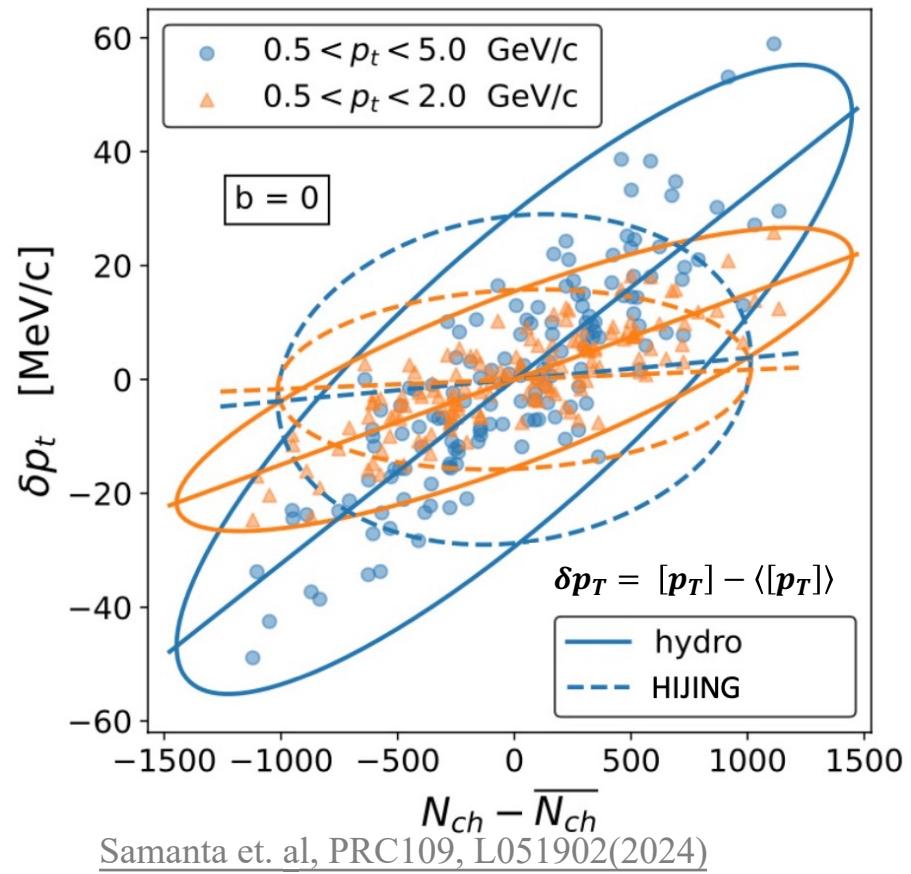
- Both ATLAS and CMS have observed the steep increase in slope of $\langle [p_T] \rangle$ in UCC.
 \Rightarrow Evidence of overlap area reaching its maximum and Hydro evolution of system.
- CMS extracted the slope of this rise: claimed the speed of sound of QGP, $c_s^2 \approx 0.241$.

Using Mean of $\langle [p_T] \rangle$ to Constrain c_s^2



- The value of c_s^2 extracted by CMS is consistent with Lattice QCD calculations at an effective temperature of about 220 MeV with small systematic error.
- UCC measurement of $\langle [p_T] \rangle$ provides direct information on c_s^2 of QGP.

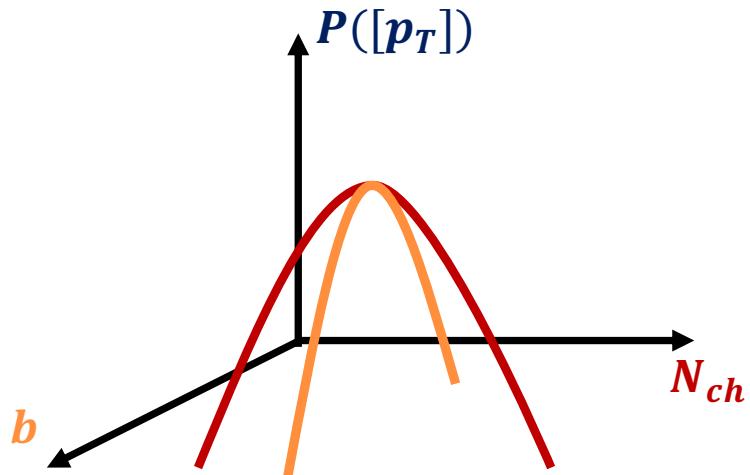
Dependence of UCC Slope of $\langle [p_T] \rangle$ on Evolution Dynamics



- ATLAS: slope of this rise depends on the p_T -range of the particles, consistent with Hydro models.
- Models without hydro evolution or mechanisms to relate initial entropy densities to number of particles fail to describe slope.

$$c_s^2(T_{\text{eff}}) \propto \frac{d \ln(\langle [p_T] \rangle)}{d \ln(N_{ch}^{\text{rec}})} \approx \frac{\Delta p_T / \langle [p_T] \rangle}{\Delta N_{ch}^{\text{rec}} / \langle N_{ch}^{\text{rec}} \rangle}$$

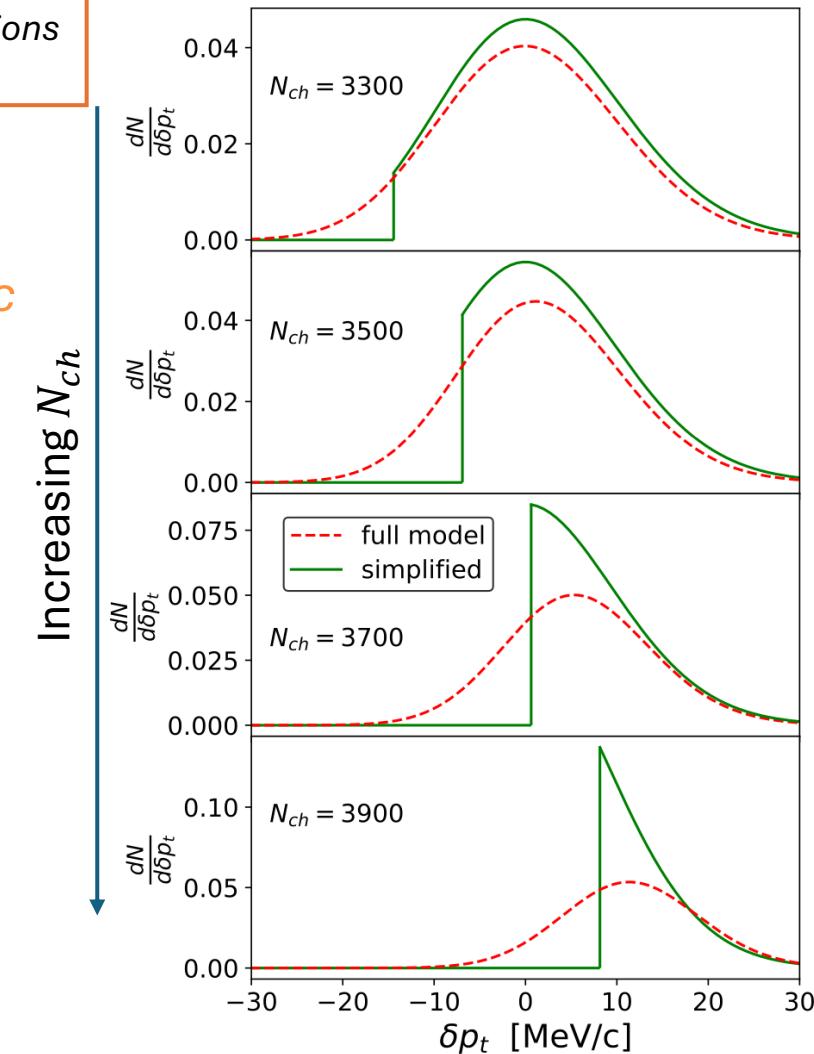
Using $[p_T]$ Cumulants to Constrain Fluctuations in IS



*Effect of diminishing b fluctuations
with increasing N_{ch}*

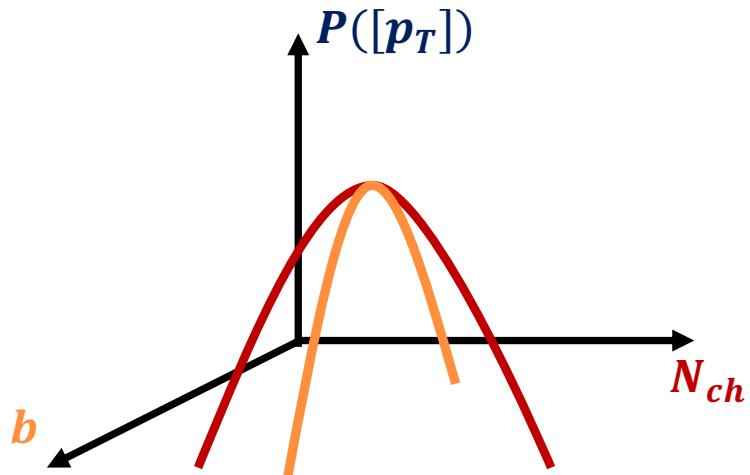
At fixed N_{ch} , b fluctuates : *Geometric*
At fixed b , N_{ch} fluctuates: *Intrinsic*

- In ultra-central collisions, $b \rightarrow 0$.
 \Rightarrow upper bound on $R \Rightarrow$ Imposes lower bound on δp_T . $\frac{\delta p_T}{\langle [p_T] \rangle} \propto -\frac{\delta R}{\langle R \rangle}$



[Samanta et. al, PRC108, 024908 \(2023\)](#)
[Samanta et. al, PRC109, L051902\(2024\)](#)

Using $[p_T]$ Cumulants to Constrain Fluctuations in IS

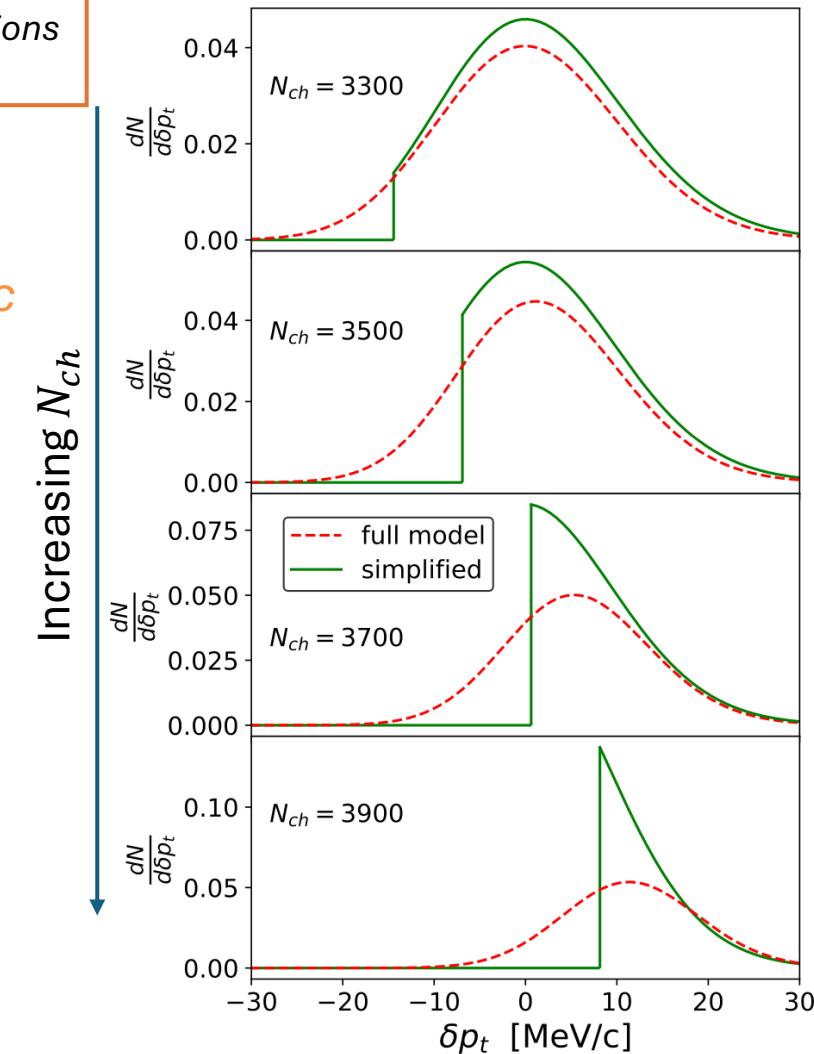


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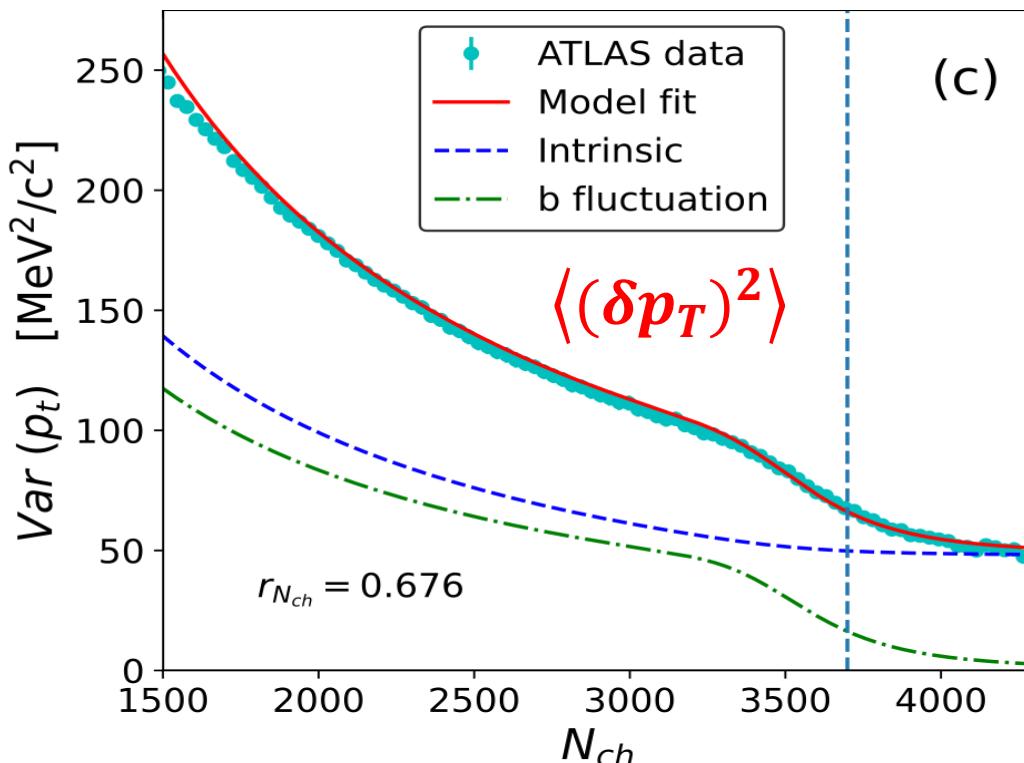
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- With increasing N_{ch} in UCC, expect:
1. Decrease variance of $P([p_T])$,
 2. Increase skewness of $P([p_T])$,
due to constraints on geometrical fluctuations



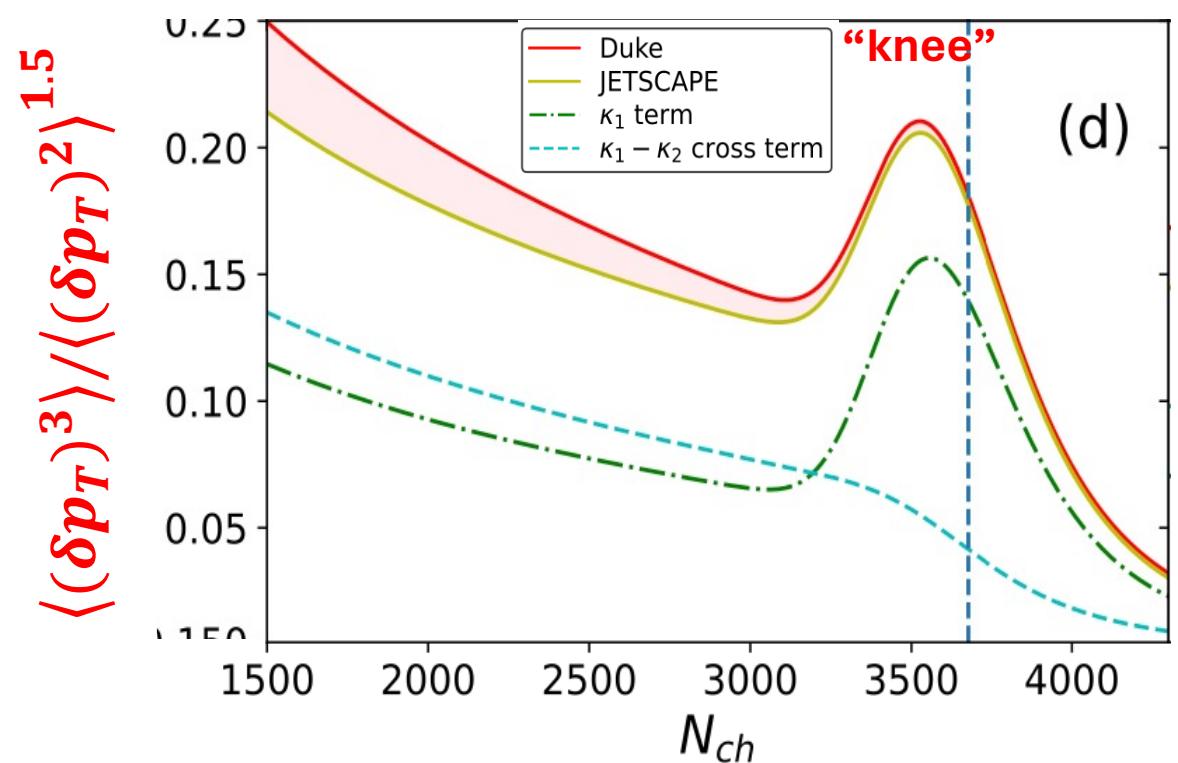
Samanta et. al, PRC108, 024908 (2023)
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Constraining Geometric and Non-Geometric fluctuations



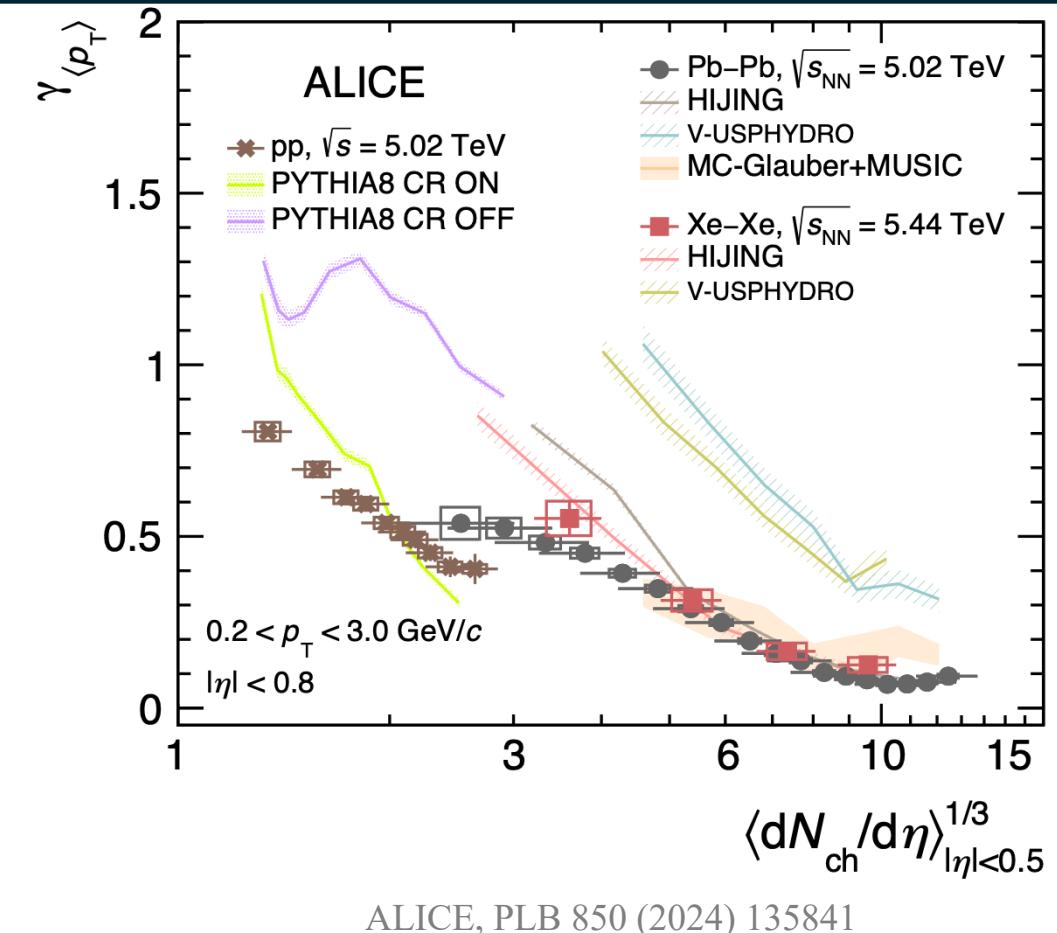
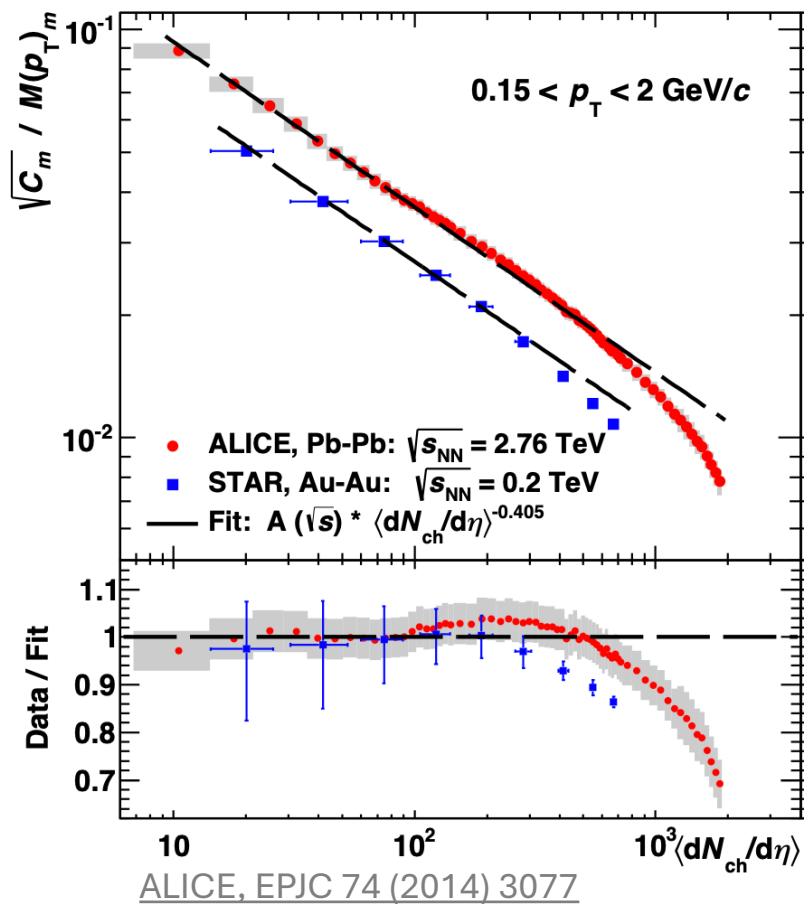
Samanta et. al, PRC108, 024908 (2023)

ATLAS, PRC 107 (2023) 054910



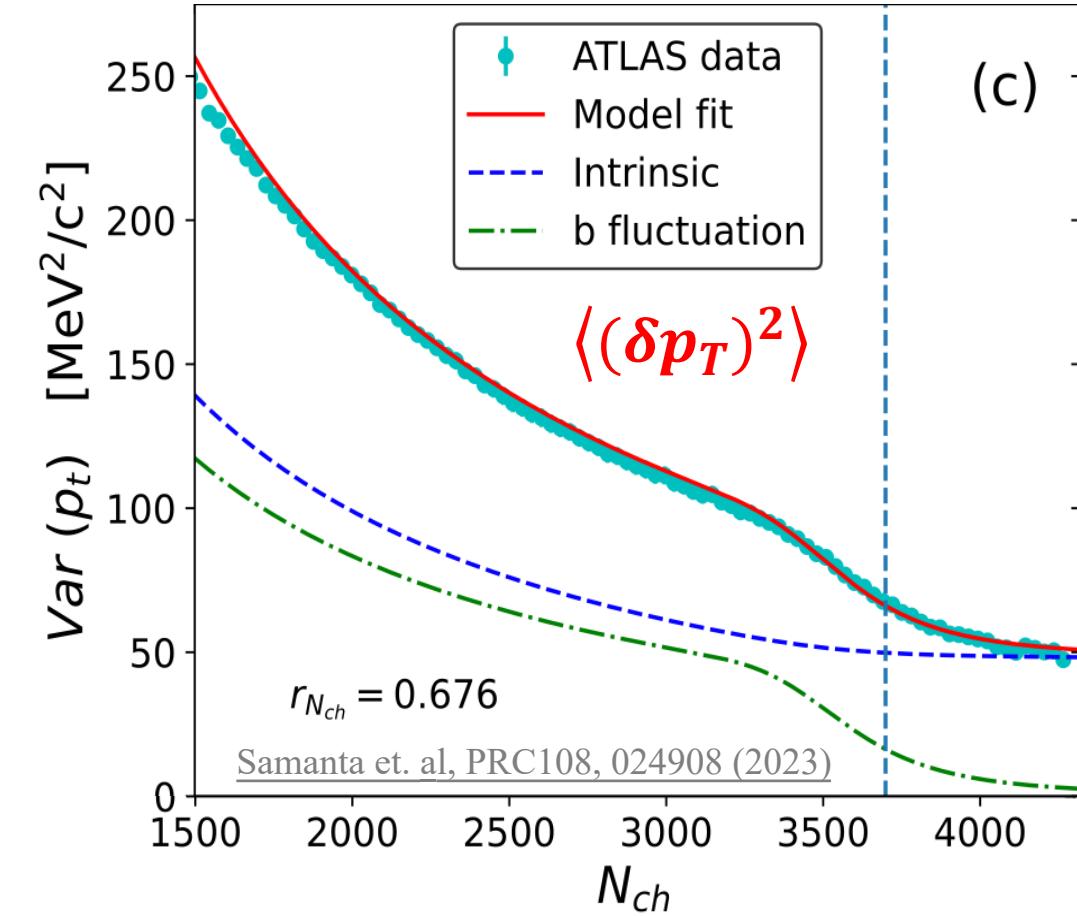
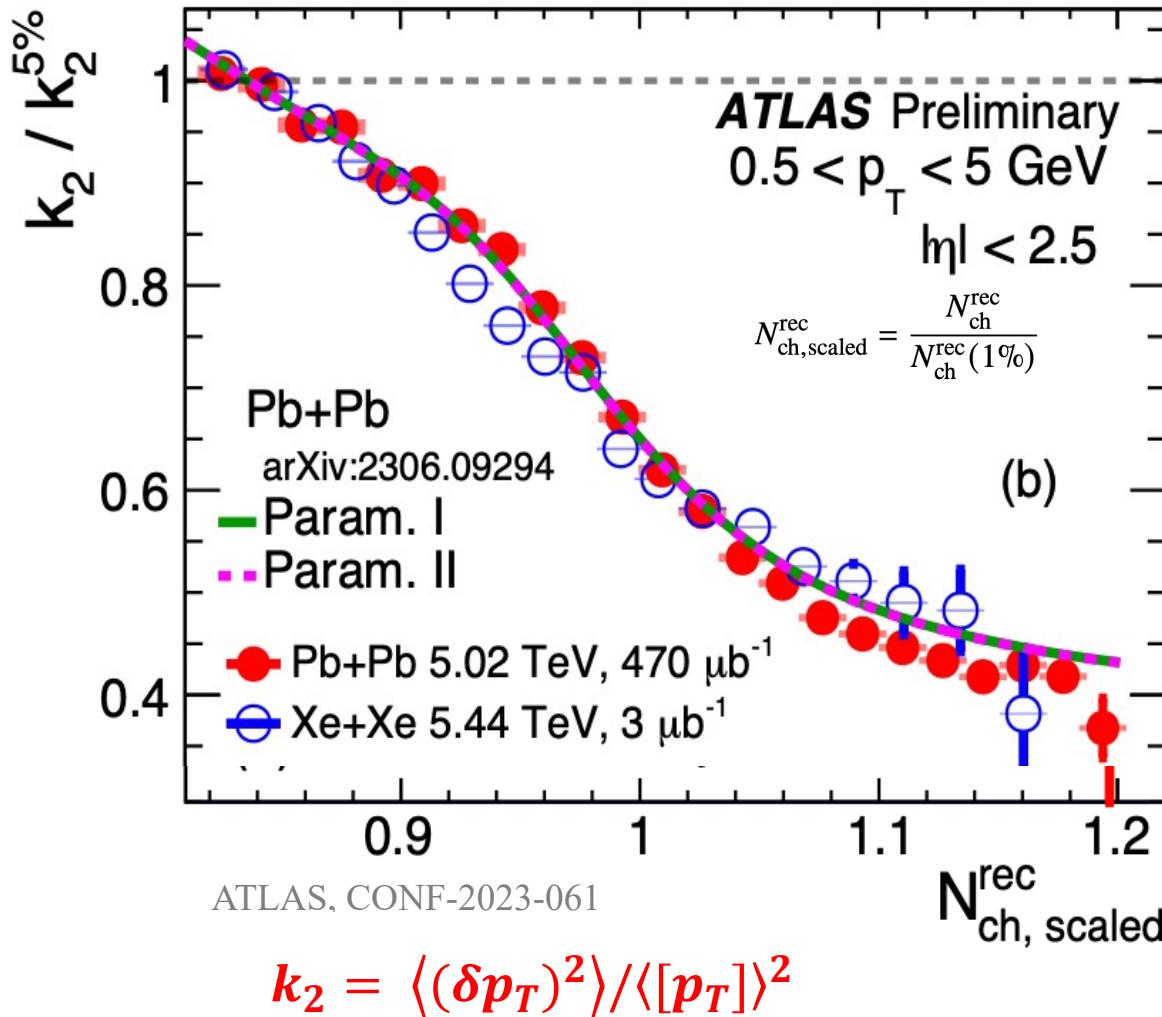
- In Ultra-Central Collisions: 1. The variance of Geometric fluctuations diminishes $\Rightarrow b$ almost gets fixed.
2. The skewness goes up due to truncation of distribution of event-wise $\langle p_T \rangle$.
- Experimental measurement of the cumulants of $P([p_T])$ can help in:
Isolating magnitude of “Geometric-fluctuations” from “Intrinsic fluctuations” in HIC.

Using $[p_T]$ Cumulants to Constrain Medium Evolution



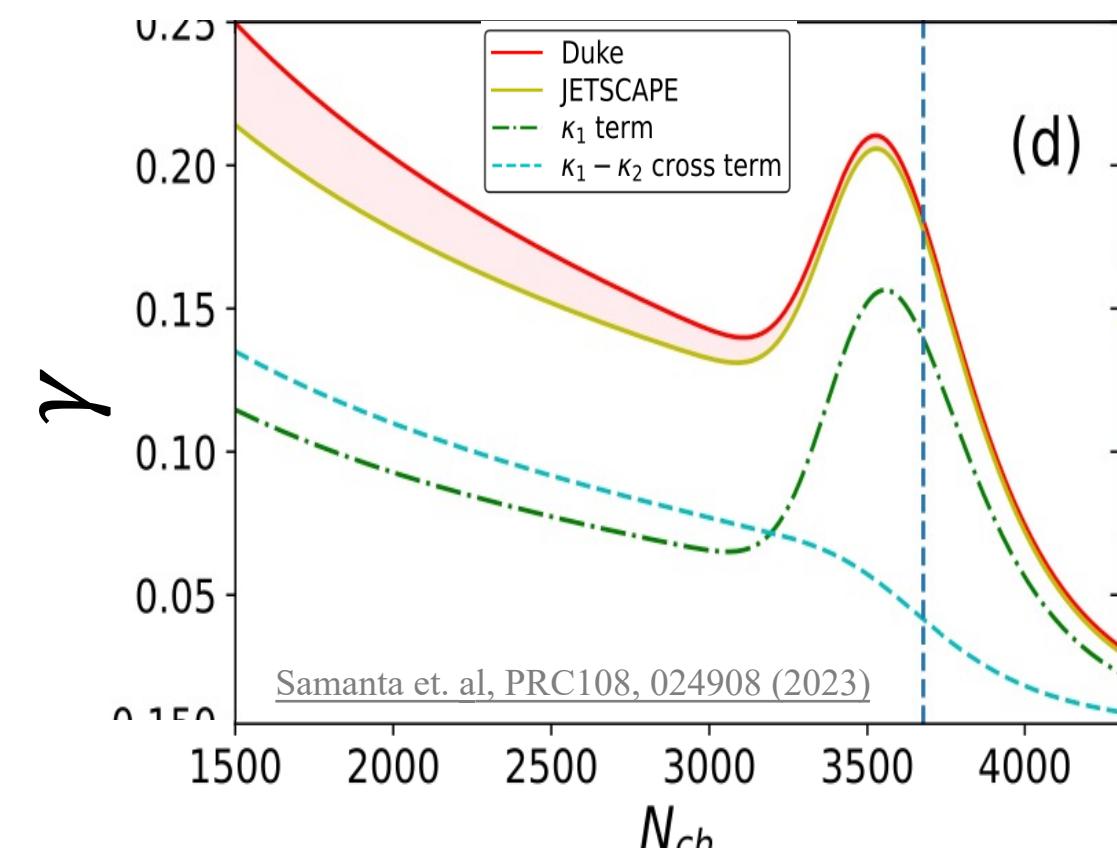
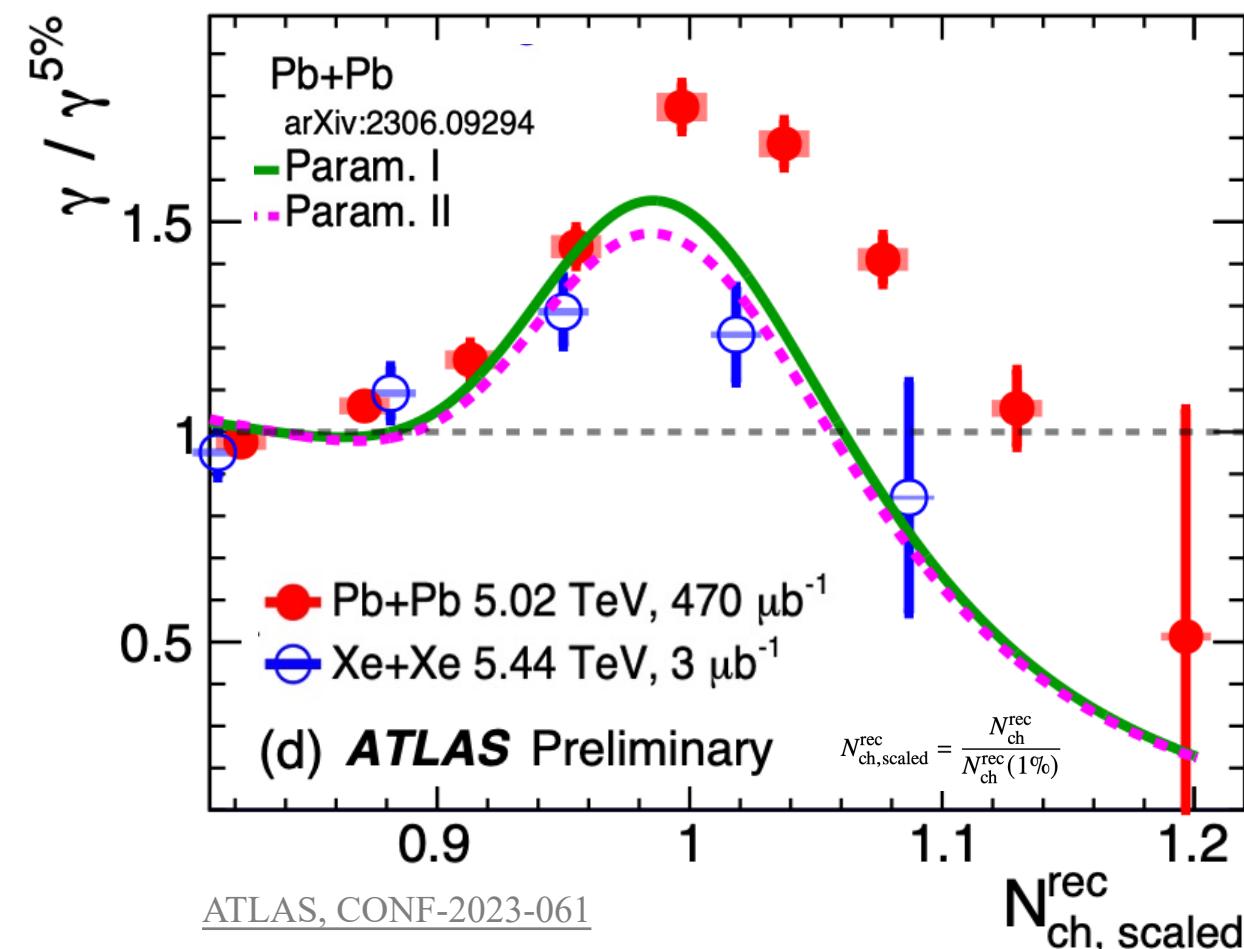
- ALICE: variance and skewness of $P([p_T])$ show deviations from power-law in UCC.
 ➤ Positive skewness excess from its baseline : indicates hydrodynamic evolution of QGP

Using $[p_T]$ Cumulants to Constrain Fluctuations



- Observed UCC features arise from diminishing component from b fluctuations (Geometric component).

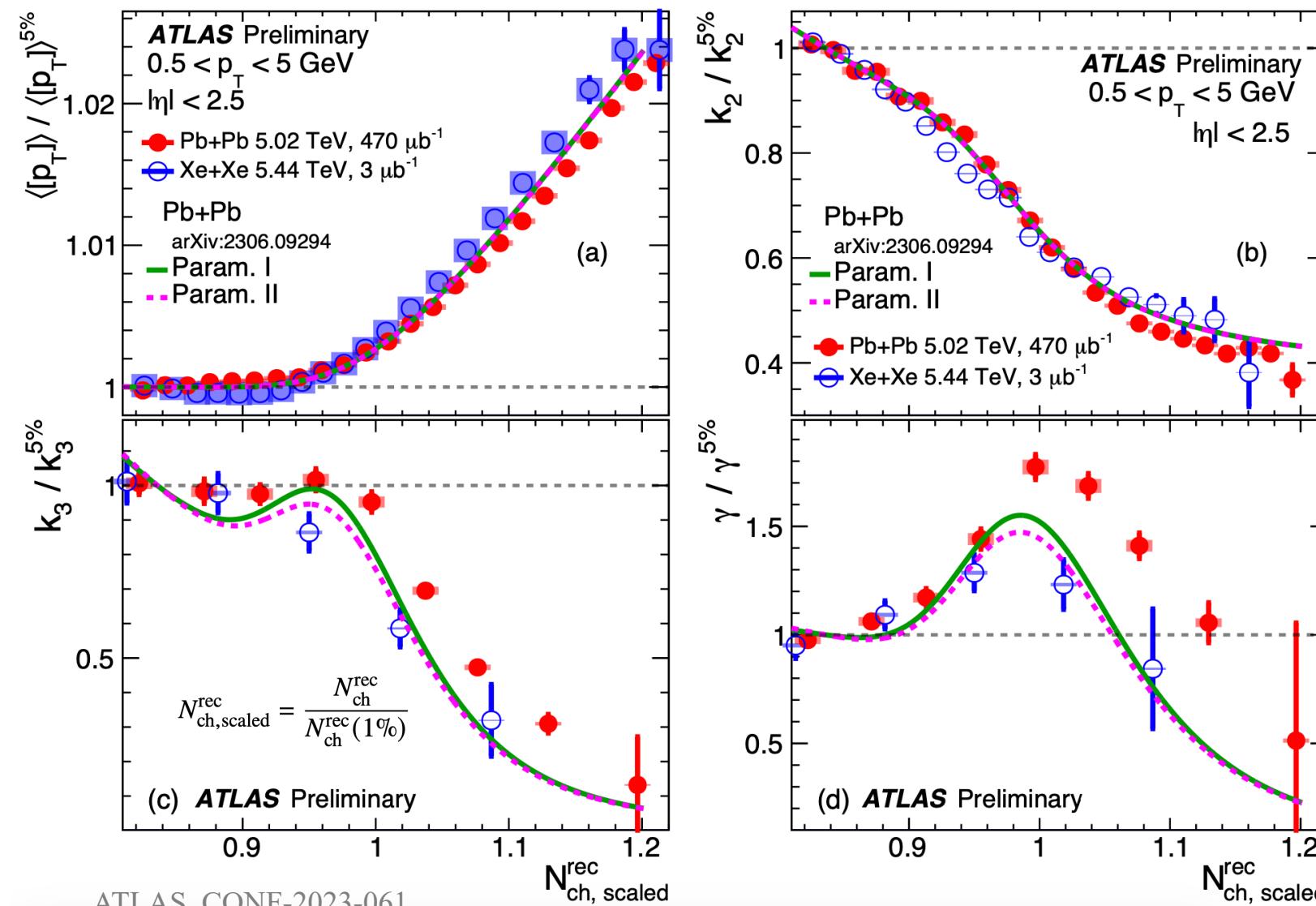
Using $[p_T]$ Cumulants to Constrain Fluctuations



$$\gamma = \langle (\delta p_T)^3 \rangle / \langle (\delta p_T)^2 \rangle^{1.5}$$

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Using $[p_T]$ Cumulants to Constrain Fluctuations



ATLAS, CONF-2023-061

Samanta et. al, PRC108, 024908 (2023)

ATLAS measurement shows:

- Observed UCC features arise from diminishing component from b fluctuations (Geometric component).
- First experimental constraint on magnitude of Intrinsic fluctuations in heavy-ion collisions.

Conclusion

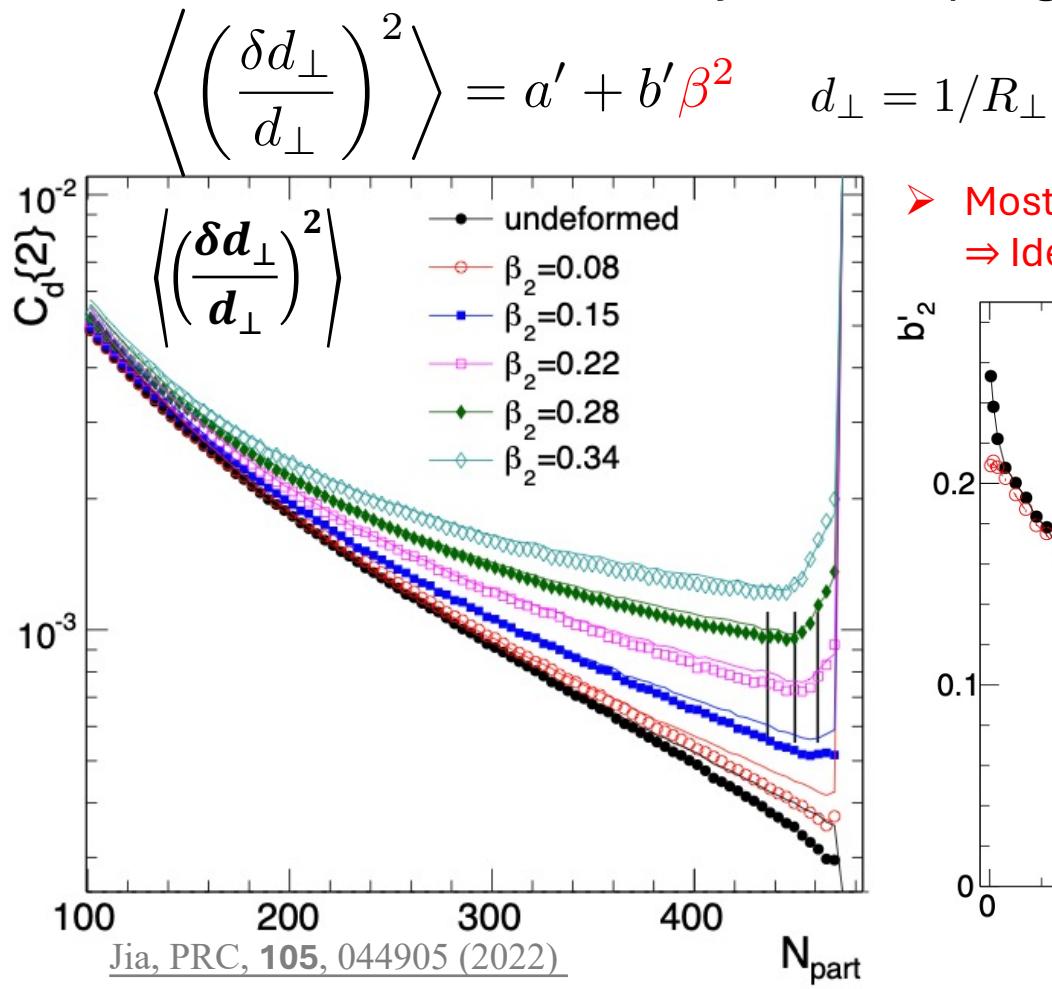
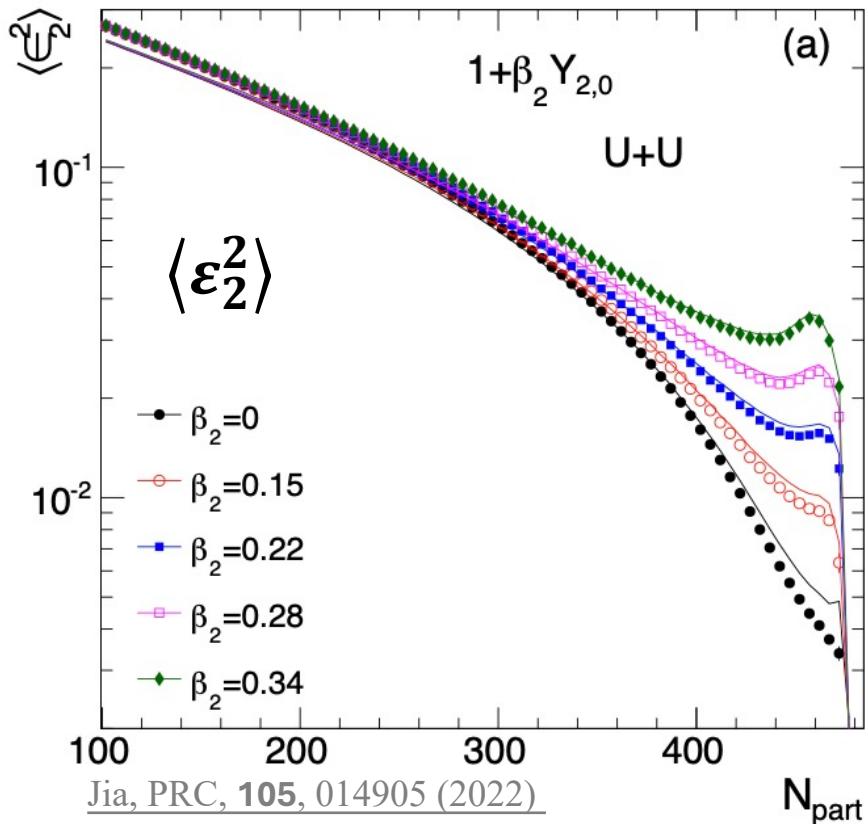
- Ultra-Central heavy-ion collisions provide ideal conditions to constrain geometry and sources of fluctuations in the Initial state & from medium evolution.
- Recent measurements from LHC on flow and $[p_T]$ correlations in UCC has shown:
 1. Nuclear deformation parameters β, γ can be reliably extracted from Ultra-Central HIC. The extracted deformation are valuable inputs for Bayesian analysis to constrain Initial state.
 2. Measured slope of rise of $\langle [p_T] \rangle$ provides evidence of hydrodynamic evolution of system. Provided precise and direct constraint on speed of sound of QGP.
 3. In UCC, the $[p_T]$ cumulants show clear signs of diminishing geometric fluctuations. Provide experimental constraint on Geometric and Intrinsic fluctuations from Initial state and medium evolution of HIC.

Backup

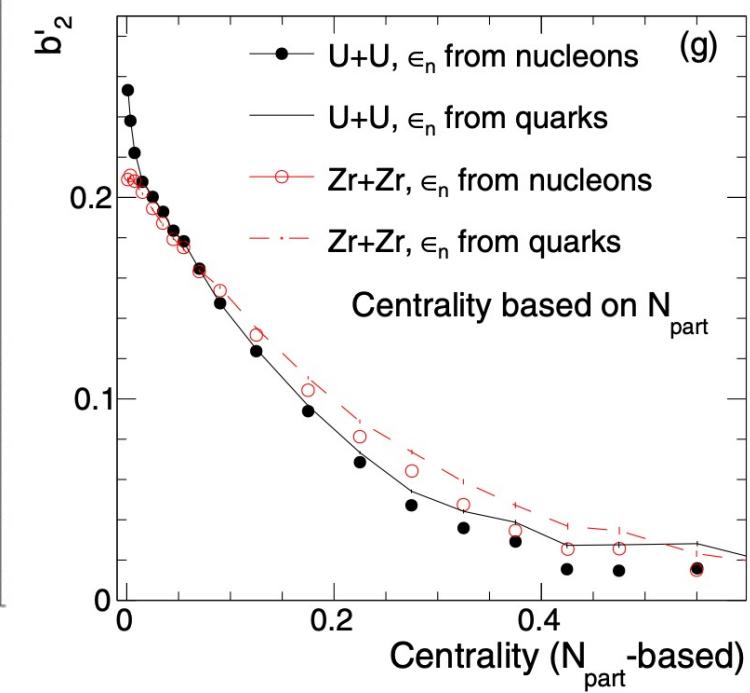
Effect of β on Overlap Geometry

- Nuclear deformation enhances fluctuations in size and eccentricity of overlap region

$$\langle \varepsilon_2^2 \rangle = a + b\beta^2$$



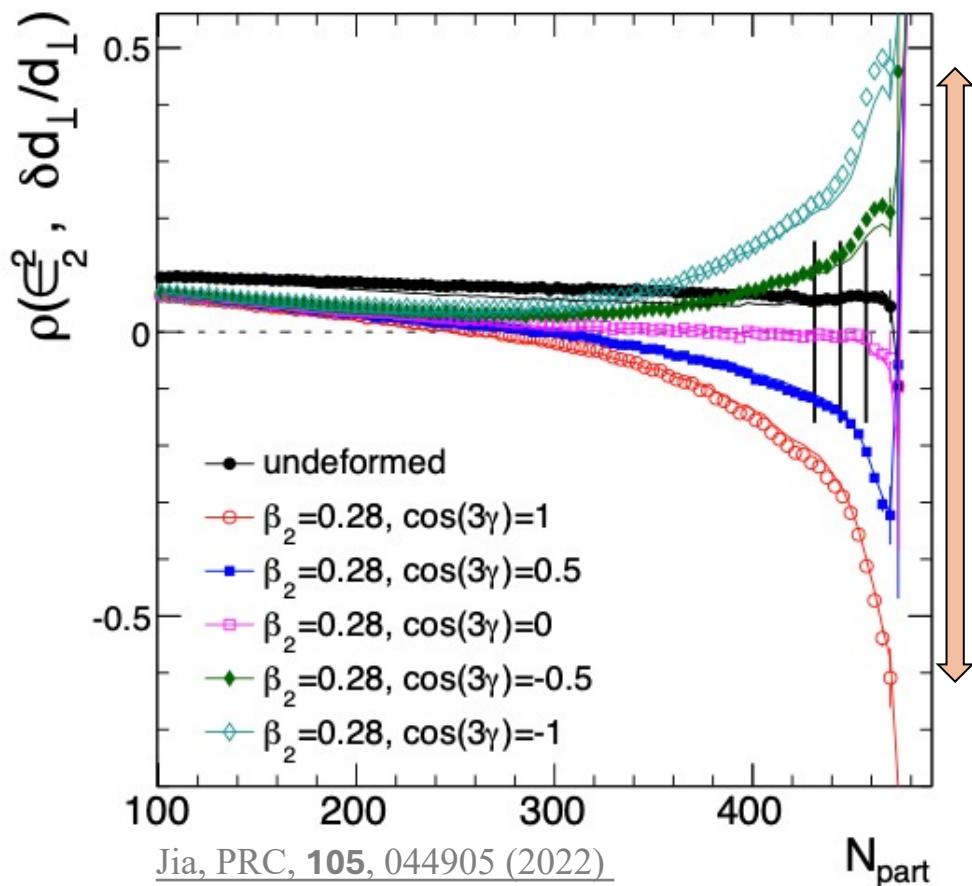
➤ Most-Central collisions: max overlap
⇒ Ideal to probe Nuclear deformation



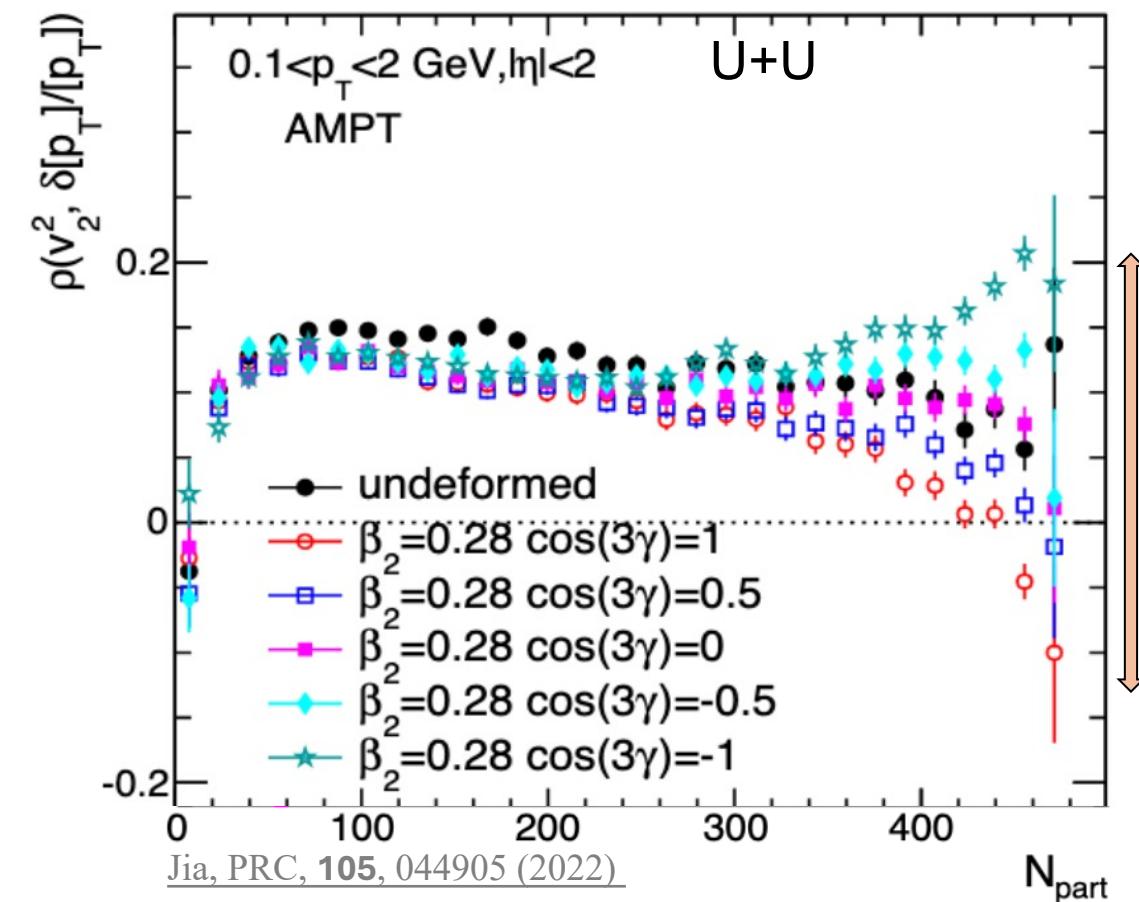
➤ The effect of deformation on eccentricity and size fluctuations is maximum in ultra central collisions.

Effect of γ on Shape-Size Correlations of Overlap Geometry

Initial state correlation



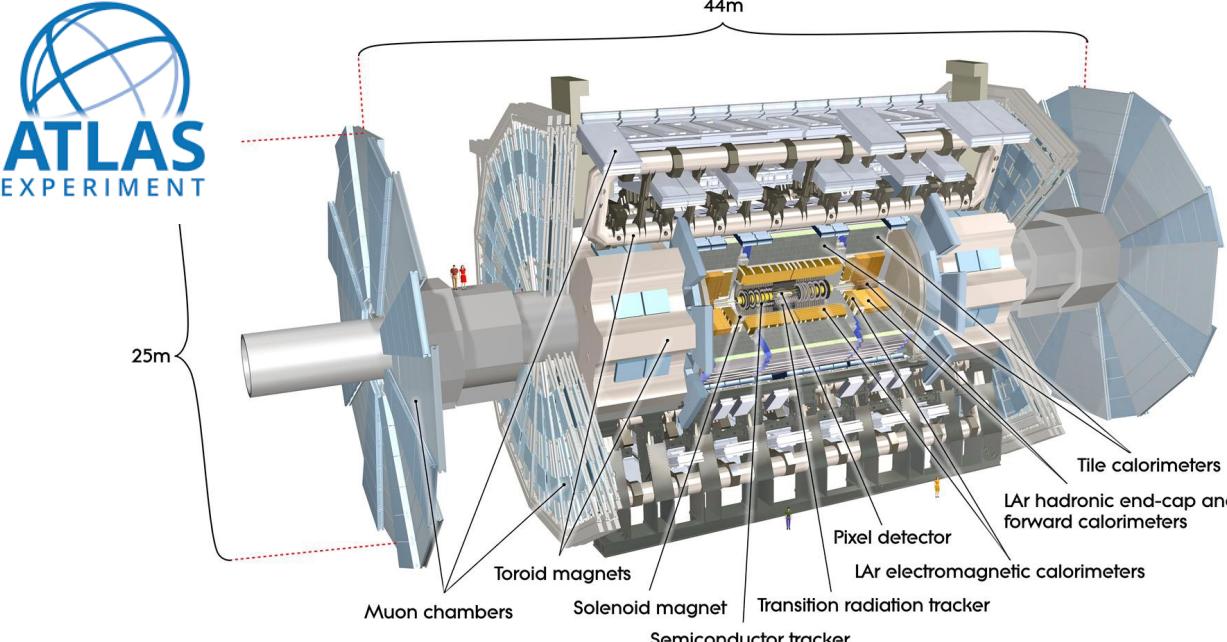
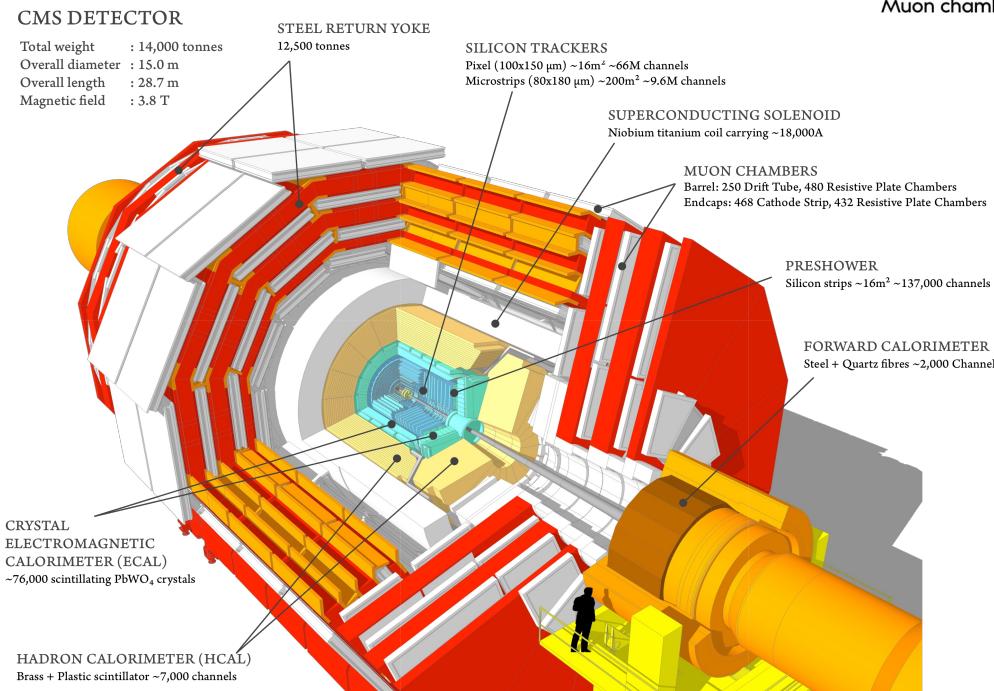
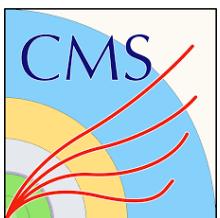
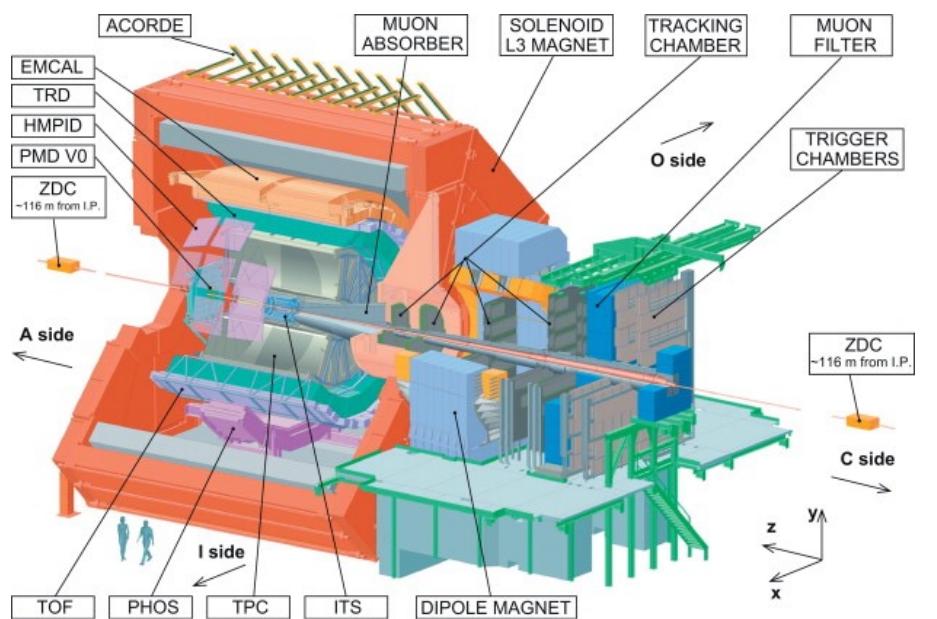
Final state correlation



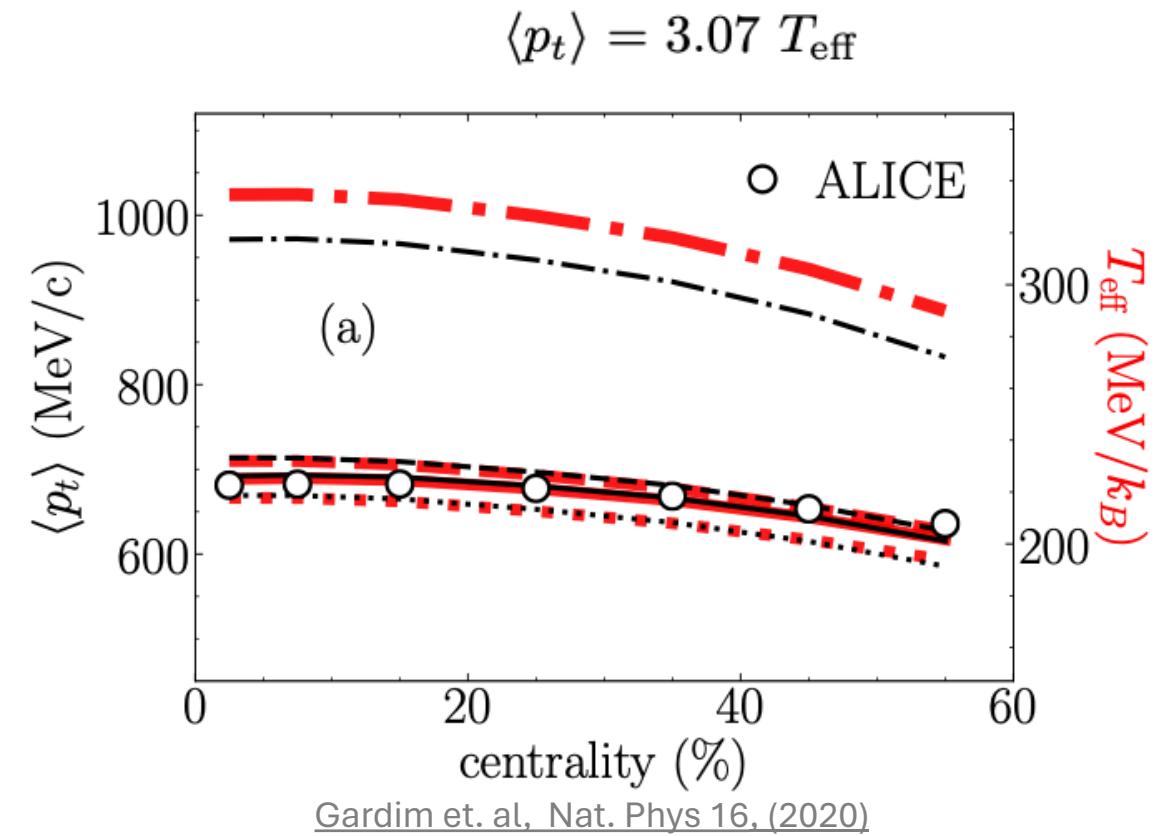
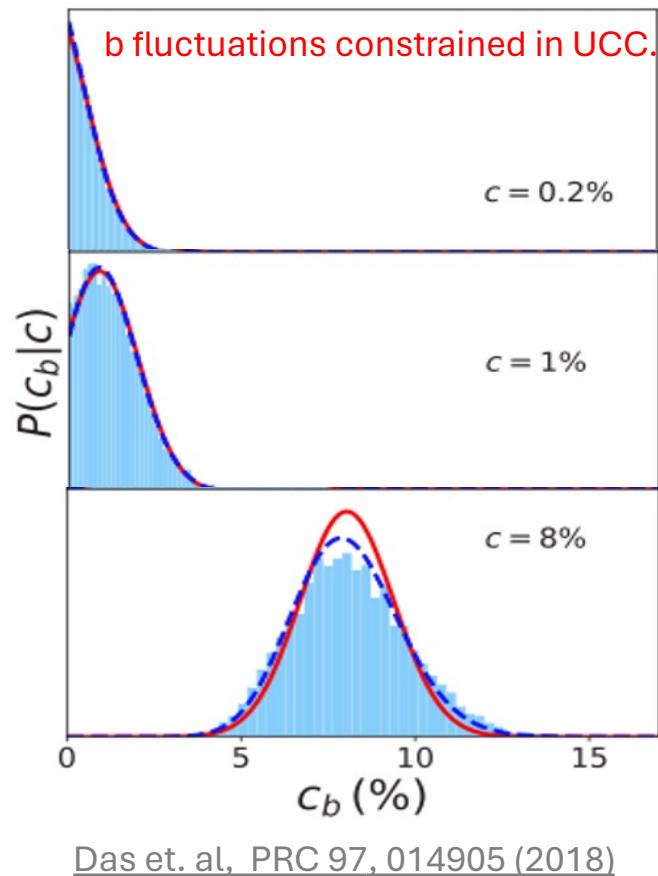
- Clear sensitivity to triaxiality for BOTH Initial state $\rho(\varepsilon_2^2, \delta d_\perp / d_\perp)$ & final state $\rho(v_2^2, \delta [p_T] / [p_T])$ in models.



ALICE

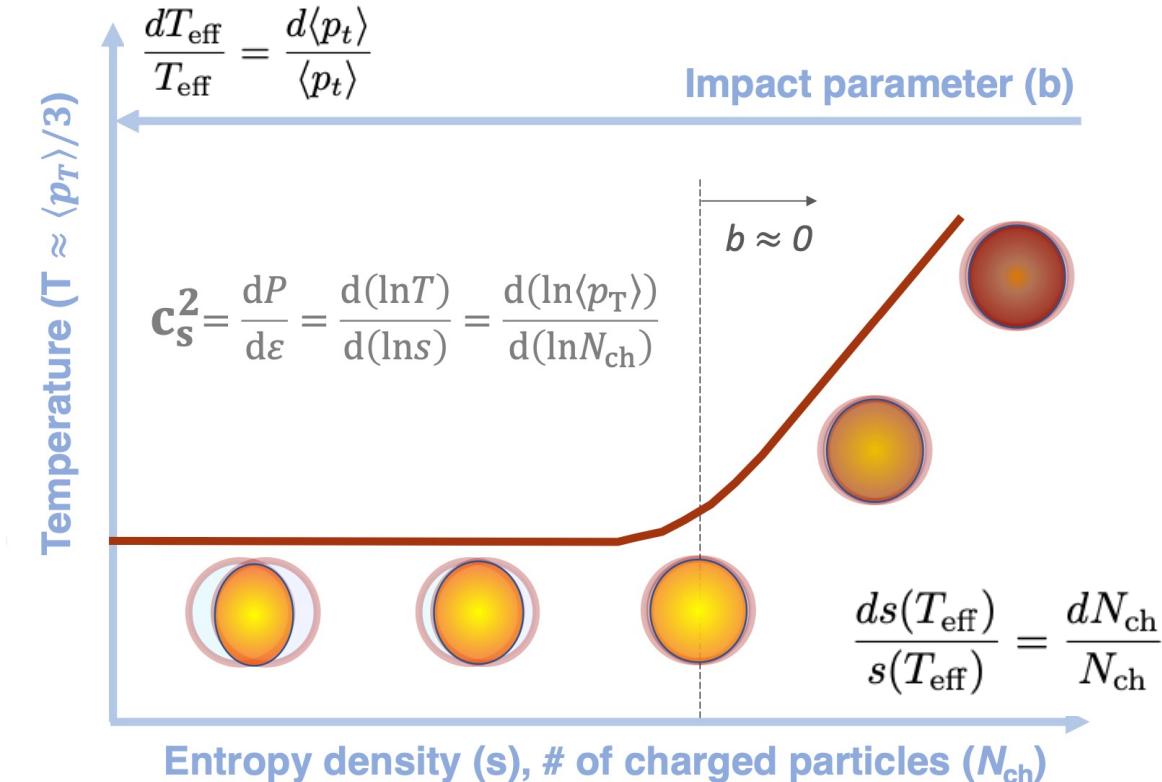


Using Mean of $P([p_T])$ to Constrain c_S

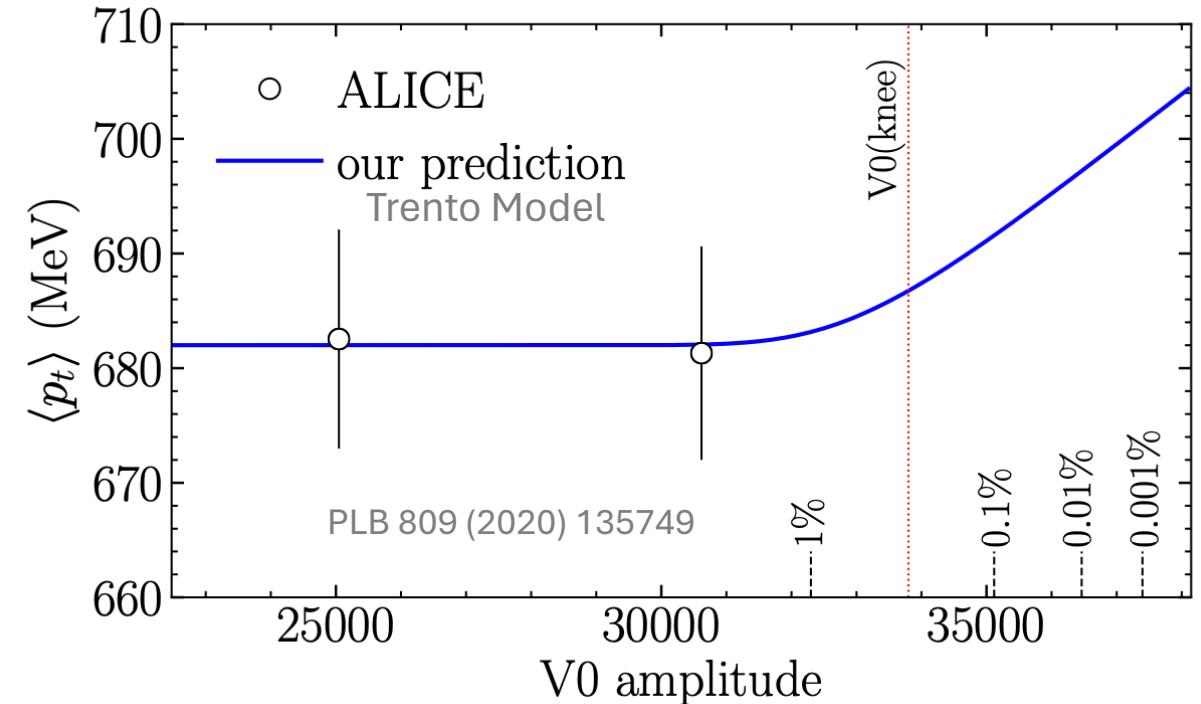


- In UCC, within approximately fixed b , choosing larger N_{ch} chooses events with larger entropy density.
- Larger entropy density within a fixed geometry leads to larger radial push or $\langle [p_T] \rangle$.

Using Mean of $P([p_T])$ to Constrain c_s



[CMS, 2401.06896](#)



[Gardim et. al, PLB 809, 135749 \(2020\)](#)

- The slope of this rise of $\langle\langle p_T \rangle\rangle$ in UCC can be related to speed of sound following:

$$c_s^2 = \frac{dP}{d\epsilon} = \frac{d(\ln T)}{d(\ln s)} = \frac{d(\ln \langle p_T \rangle)}{d(\ln N_{\text{ch}})}$$