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Associated top-quark pair production with isolated photons

Daniel Stremmer

In collaboration with: Malgorzata Worek

Based on [JHEP 08 \(2023\) 179](#)

and [arXiv: 2403.03796 \[hep-ph\]](#)



Collaborative Research Center TRR 257

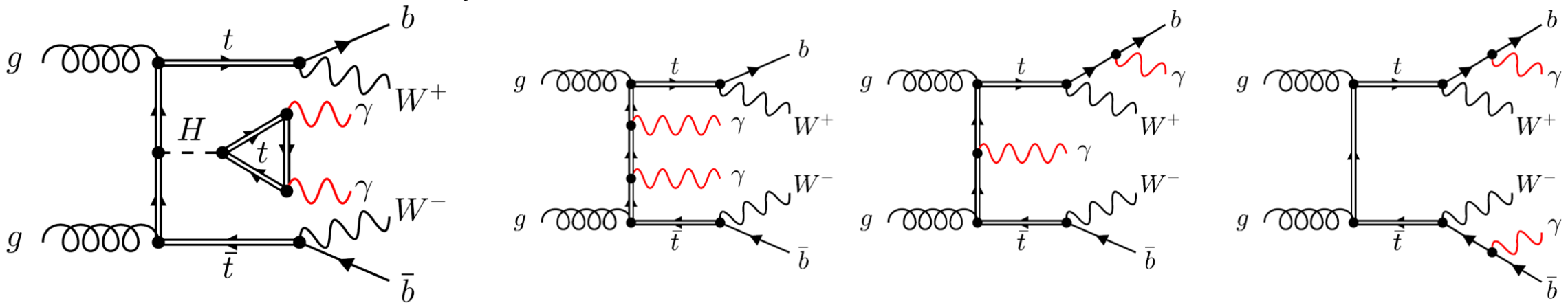


Particle Physics Phenomenology after the Higgs Discovery

LHCP 2024, Boston, USA, 07 June 2024

Motivation of $pp \rightarrow t\bar{t}\gamma(\gamma)$

- Unique features with respect to other associated $pp \rightarrow t\bar{t}$ processes:
 - Large fraction of photon radiation from top-quark decays ($t\bar{t}\gamma$: $\sim 50\%$)
 - Photon isolation criterion to reduce secondary photon production (fragmentation processes, hadron decays)
- Probe $t - \gamma$ coupling
- Irreducible background to $pp \rightarrow t\bar{t}H(H \rightarrow \gamma\gamma)$
- $H \rightarrow \gamma\gamma$ small branching ratio with $\sim 0.2\%$
- $pp \rightarrow t\bar{t}H(H \rightarrow \gamma\gamma)$ first single-channel observation of $pp \rightarrow t\bar{t}H$ *Phys.Rev.Lett. 125 (2020) 6, 061801*
Phys.Rev.Lett. 125 (2020) 6, 061802
- No observation of $pp \rightarrow t\bar{t}\gamma\gamma$ yet



Theory status ($pp \rightarrow t\bar{t}\gamma$)

- Stable top quarks

- NLO QCD
- NLO EW
- complete NLO
- aNNLO QCD

Duan, Ma, Zhang, Han, Guo, Wang '09 '11
Maltoni, Pagani, Tsiniikos '16

Duan, Zhang, Wang, Song, Li '17

Pagani, Shao, Tsiniikos, Zaro '21

Kidonakis, Tonerio, '21

- Matched to Parton showers at NLO QCD

- POWHEL/POWHEG

Kardos, Trócsányi '15

- Higher order corrections and photon radiation in decays

- NLO QCD in NWA
- NLO QCD with full off-shell effects
- Complete NLO in NWA

Melnikov, Schulze, Scharf '11

Bevilacqua, Hartanto, Kraus, Weber, Worek '20

Bevilacqua, Hartanto, Kraus, Weber, Worek '18

Stremmer, Worek '24

- All calculations based on smooth-cone isolation *Frixione '98*

Theory status ($pp \rightarrow t\bar{t}\gamma\gamma$)

- Stable top quarks at NLO QCD

- NLO QCD
- NLO QCD+EW

*Alwall, Frederix, Frixione, Hirschi, Maltoni,
Mattelaer, Shao, Stelzer, Torrielli, Zaro '14
Maltoni, Pagani, Tsiniikos '16*

Pagani, Shao, Tsiniikos, Zaro '21

- Matched to Parton Showers at NLO QCD

- POWHEL/POWHEG
- MC@NLO

Kardos, Trócsányi '15

van Deurzen, Frederix, Hirschi, Luisoni, Mastrolia '16

- Higher order corrections and photon radiation in decays

- NLO QCD in NWA
- Complete NLO in NWA

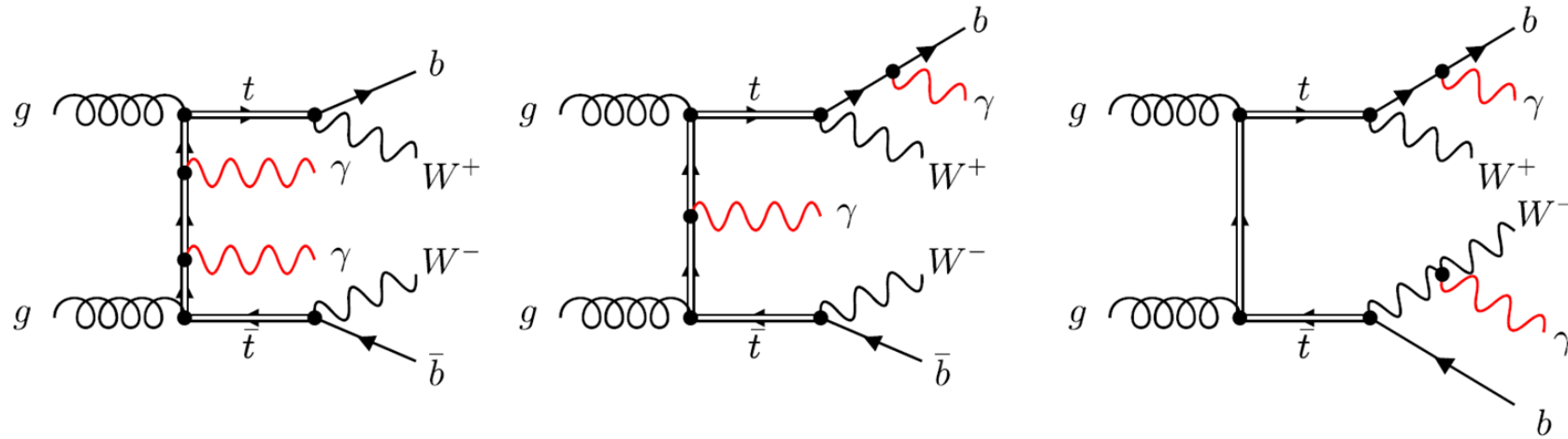
Stremmer, Worek '23

Stremmer, Worek '24

- All calculations based on smooth-cone isolation *Frixione '98*

Process definition

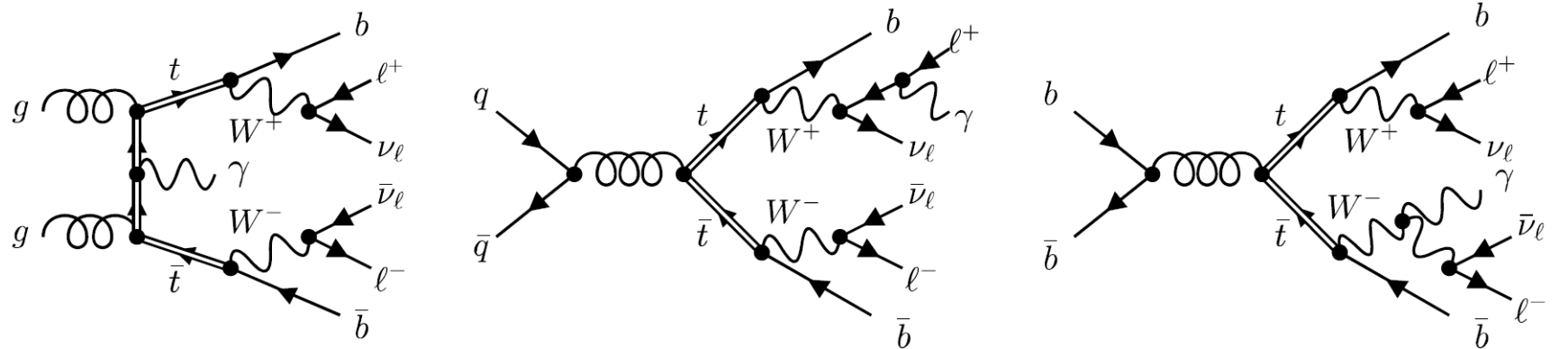
$$d\sigma_{t\bar{t}\gamma\gamma}^{\text{LO}} = \Gamma_t^{-2} \left(\underbrace{d\sigma_{t\bar{t}\gamma\gamma}^{\text{LO}} d\Gamma_{t\bar{t}}^{\text{LO}}}_{\text{Prod.}} + \underbrace{d\sigma_{t\bar{t}\gamma}^{\text{LO}} d\Gamma_{t\bar{t}\gamma}^{\text{LO}}}_{\text{Mixed}} + \underbrace{d\sigma_{t\bar{t}}^{\text{LO}} d\Gamma_{t\bar{t}\gamma\gamma}^{\text{LO}}}_{\text{Decay}} \right)$$



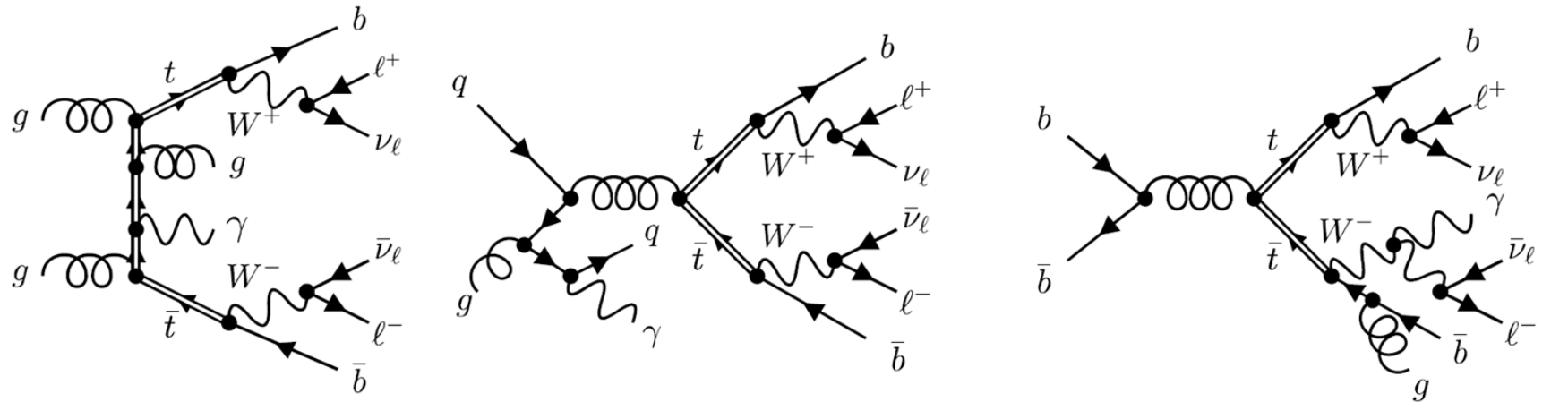
- Full calculation divided into three resonant contributions: **Prod.**, **Mixed** and **Decay**
- Calculation performed in **Narrow Width Approximation** preserving spin correlations
- **Photon bremsstrahlung** and **NLO** corrections included in $t\bar{t}$ production and decay
- NLO QCD corrections calculated for each resonant structure separately
- Mixing of resonant contributions in subleading NLO corrections

NLO QCD

LO₁ at $\mathcal{O}(\alpha_s^2 \alpha^{4+n_\gamma})$

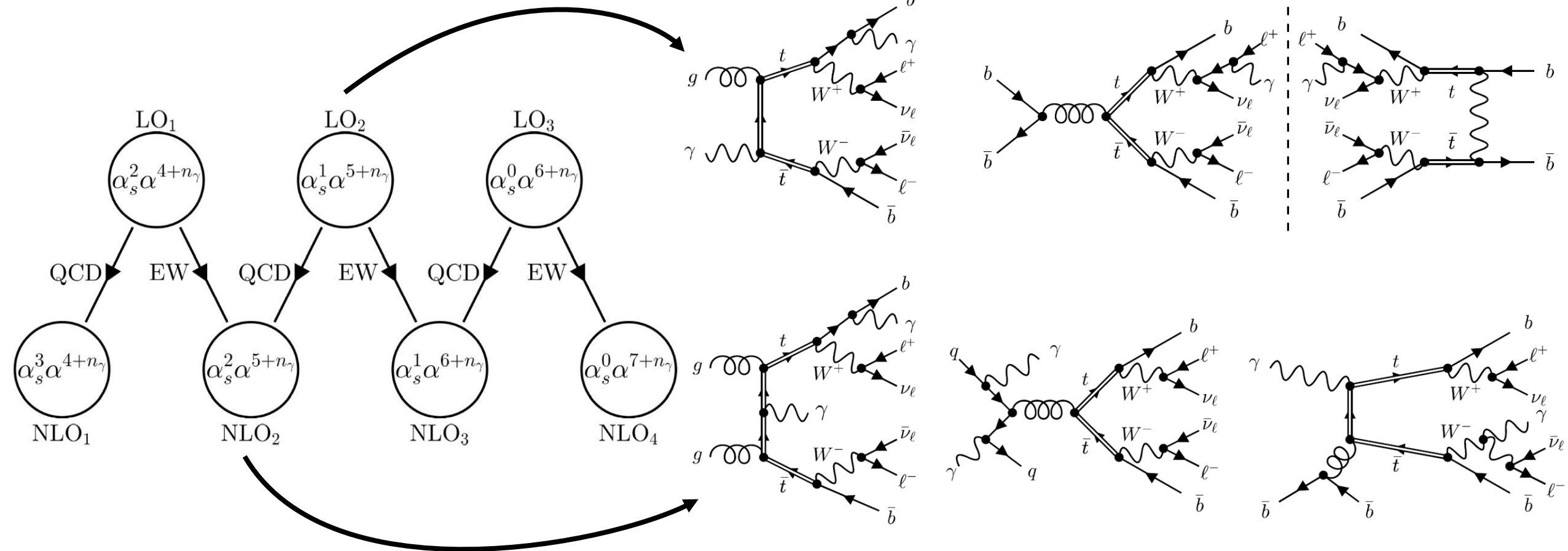


NLO₁ at $\mathcal{O}(\alpha_s^3 \alpha^{4+n_\gamma})$



$$\text{NLO}_{\text{QCD}} = \text{LO}_1 + \text{NLO}_1$$

Complete NLO



$$\text{LO} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3$$

$$\text{NLO} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_2 + \text{NLO}_3 + \text{NLO}_4$$

Computational framework

Virtual Corrections with **Recola** (*Actis, Denner, Hofer, Lang, Scharf, Uccirati '17*) + **Collier** (*Denner, Hofer, Dittmaier, Hofer '17*)

■ Further Modifications in Recola

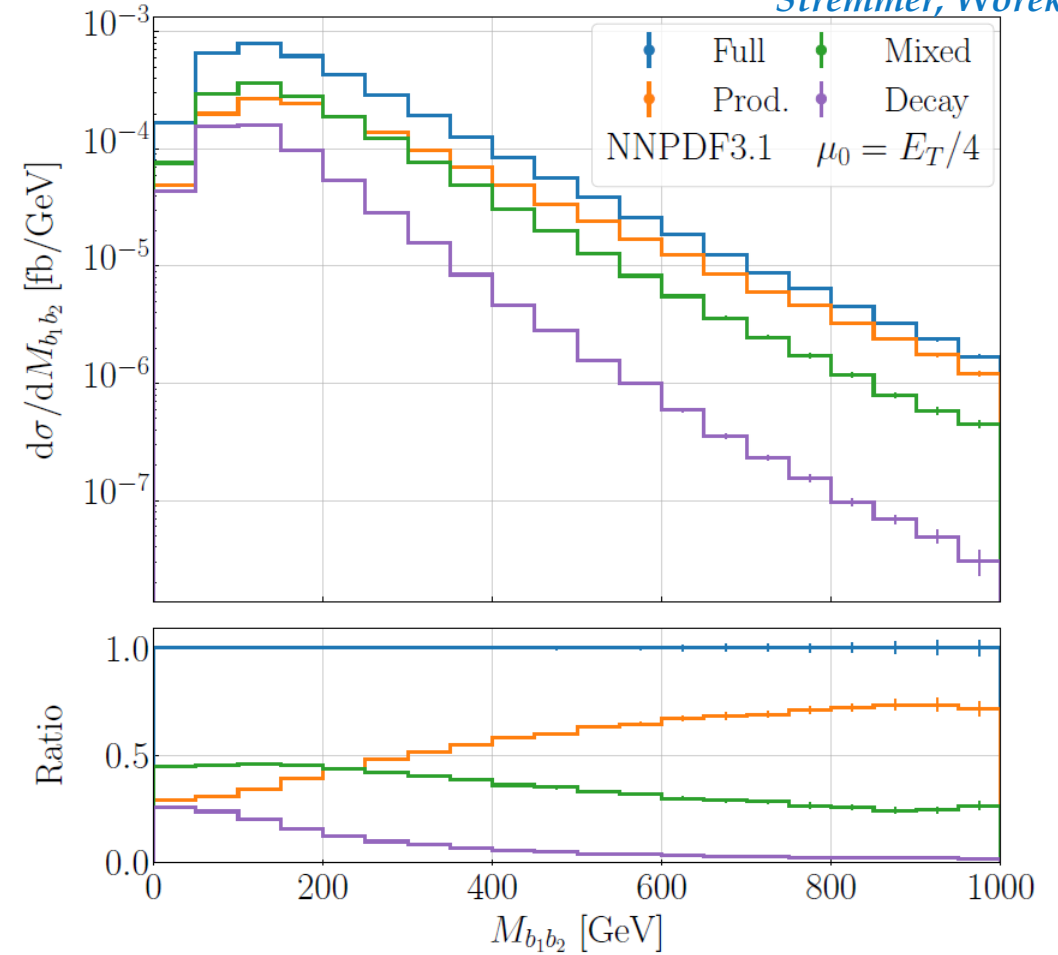
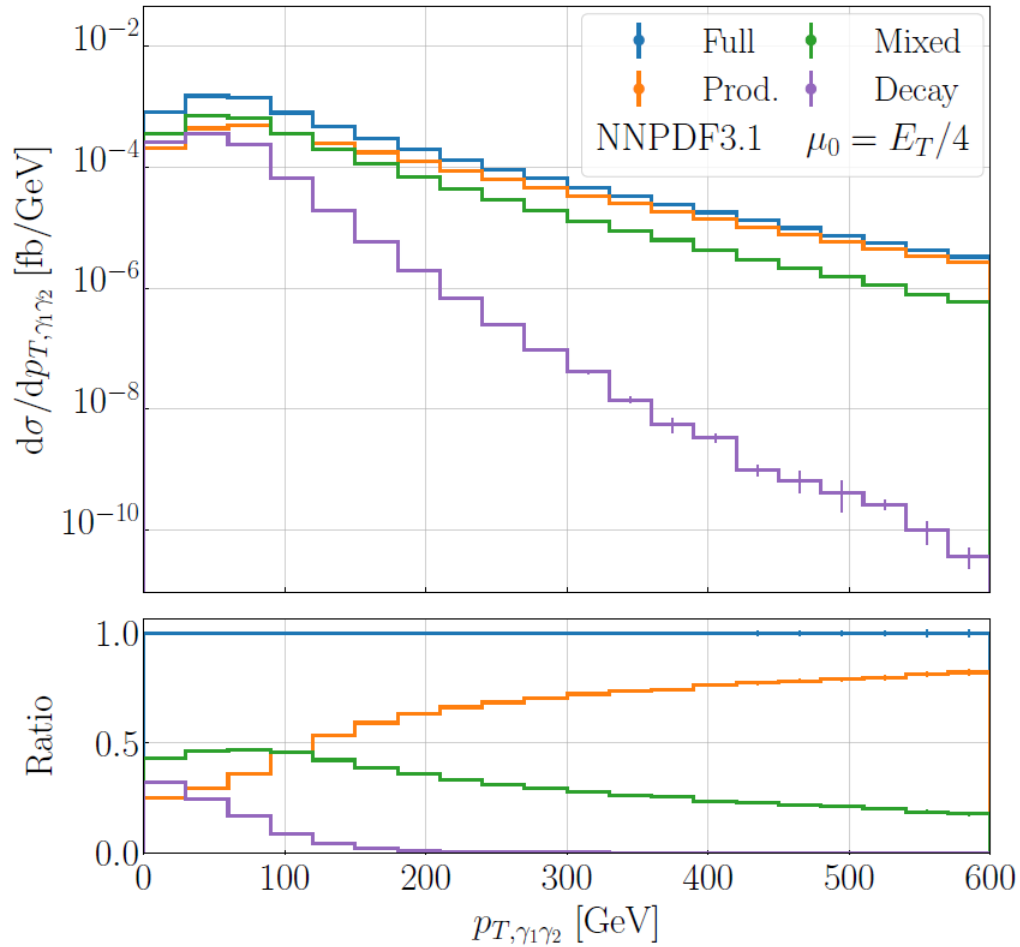
- Random polarisation method $\sum_{\lambda} |\mathcal{M}_{\lambda}|^2 = \frac{1}{2\pi} \int_0^{2\pi} d\phi |\mathcal{M}_{\phi}|^2$
- Alternative reduction to scalar integrals with **CutTools** (*Ossola, Papadopoulos, Pittau '09*) and **OneLoop** (*van Hameren '11*)
- Mixed renormalisation of α : $\alpha^n = \alpha_{G_{\mu}}^{n-n_{\gamma}} \alpha(0)^{n_{\gamma}}$

Real Corrections in Helac-Dipoles

- Nagy-Soper subtraction *Bevilacqua, Czakon, Kubocz, Worek '13*
 - QCD and QED-like subtraction in nested decay chains with massive/massless emitters
- Partially cross-checked with Catani-Seymour subtraction *Catani, Seymour '97* *Catani, Dittmaier, Seymour, Trocsanyi '02*
- Theoretical prediction are stored in modified **Les Houches Event Files (LHEFs)** *Bern, Dixon, Febres Cordero, Hoeche, Ita, Kosower, Maitre '14*
- Reweighting to different renormalisation/factorisation scales and PDF sets

Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel at NLO QCD

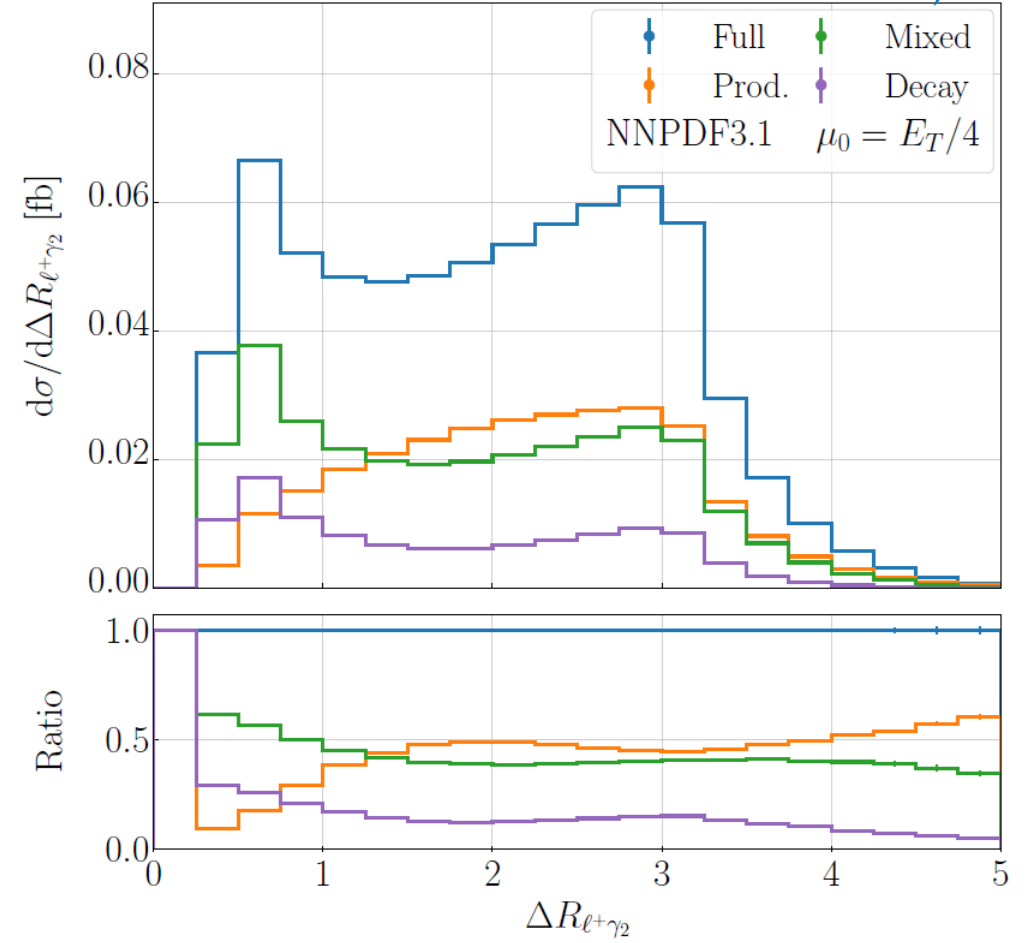
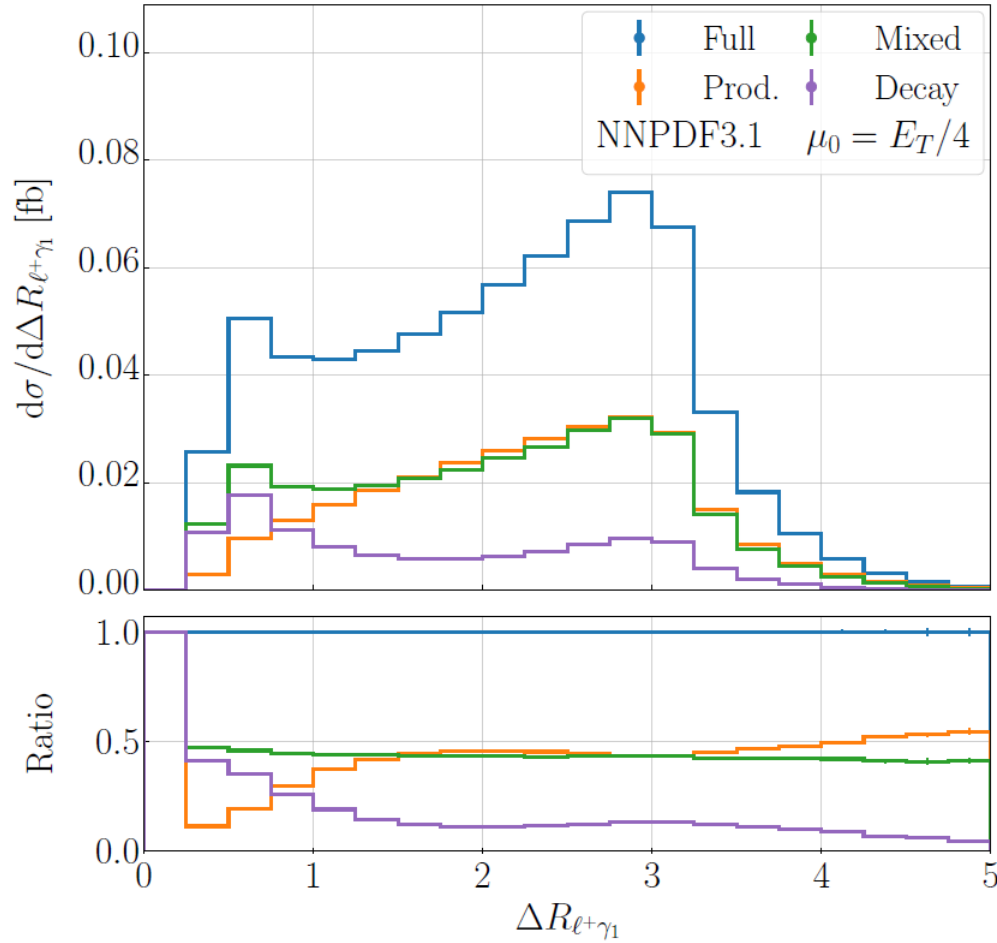
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- Integrated level: **Full = Prod. (40%) + Mixed (44%) + Decay (16%)**
- Large contributions from photon emission in decays in bulk of distribution
- Tails dominated by **Prod. (79 – 82% of Full)**

Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel at NLO QCD

Stremmer, Worek '23

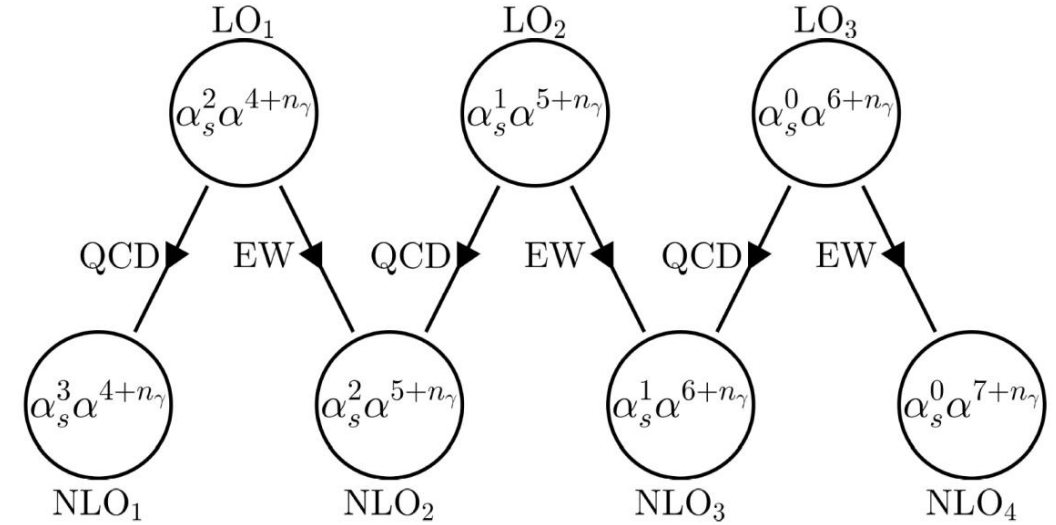


- Different peak structures for **Prod.**, **Mixed** and **Decay**
- Only sum leads to reliable predictions
- Similar conclusions in **lepton + jet** top-quark decay channel

Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma$ in di-lepton channel

		σ_i [fb]	Ratio to LO ₁
LO ₁	$\mathcal{O}(\alpha_s^2 \alpha^5)$	55.604(8) ^{+31.4%} _{-22.3%}	1.00
LO ₂	$\mathcal{O}(\alpha_s^1 \alpha^6)$	0.18775(5) ^{+20.1%} _{-15.4%}	+0.34%
LO ₃	$\mathcal{O}(\alpha_s^0 \alpha^7)$	0.26970(4) ^{+14.3%} _{-16.9%}	+0.49%
NLO ₁	$\mathcal{O}(\alpha_s^3 \alpha^5)$	+3.44(5)	+6.19%
NLO ₂	$\mathcal{O}(\alpha_s^2 \alpha^6)$	-0.1553(9)	-0.28%
NLO ₃	$\mathcal{O}(\alpha_s^1 \alpha^7)$	+0.2339(3)	+0.42%
NLO ₄	$\mathcal{O}(\alpha_s^0 \alpha^8)$	+0.001595(8)	+0.003%
LO		56.061(8) ^{+31.2%} _{-22.1%}	1.0082
NLO _{QCD}		59.05(5) ^{+1.6%} _{-5.9%}	1.0620
NLO _{prd}		59.08(5) ^{+1.5%} _{-5.9%}	1.0626
NLO		59.59(5) ^{+1.6%} _{-5.9%}	1.0717

Stremmer, Worek '24

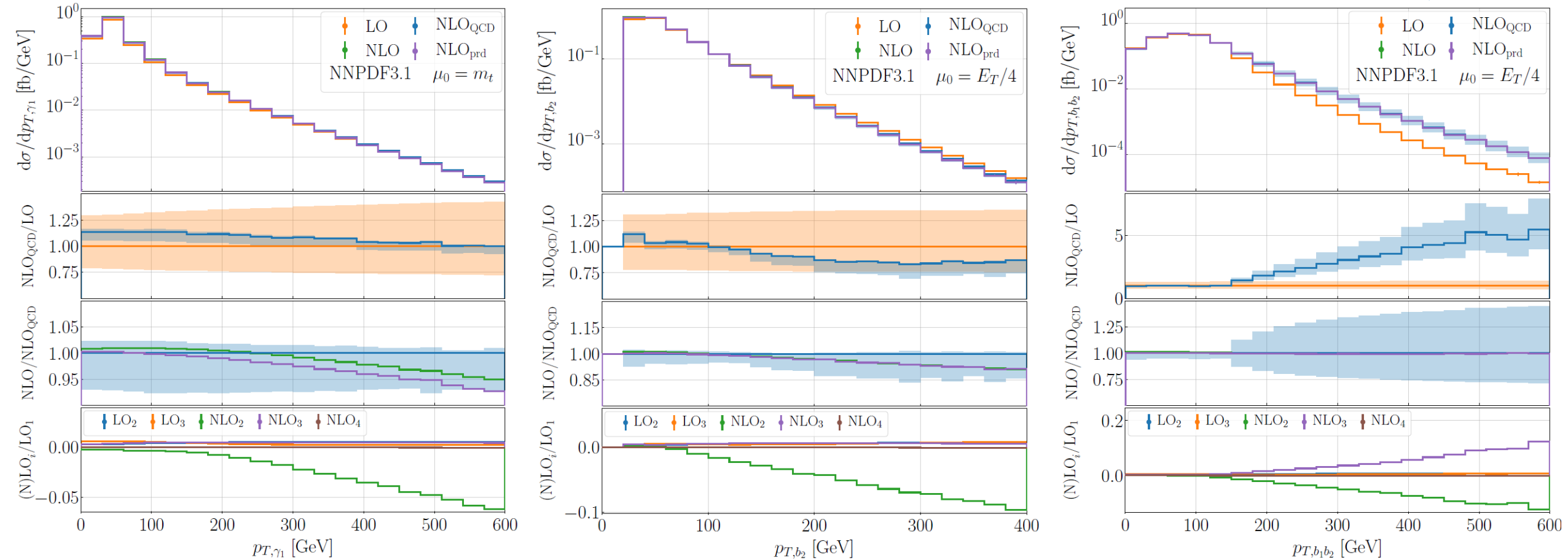


- Subleading LO contributions below **1%**
- NLO corrections dominated by **NLO₁**
- Subleading NLO corrections below **1%**
- Similar conclusions for $pp \rightarrow t\bar{t}\gamma\gamma$

- $\text{NLO}_{\text{prd}} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_{2,\text{prd}} + \text{NLO}_{3,\text{prd}} + \text{NLO}_{4,\text{prd}}$
- No photon radiation and higher-order corrections in top-quark decays in subleading NLO contributions

Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma$ in di-lepton channel

Stremmer, Worek '24

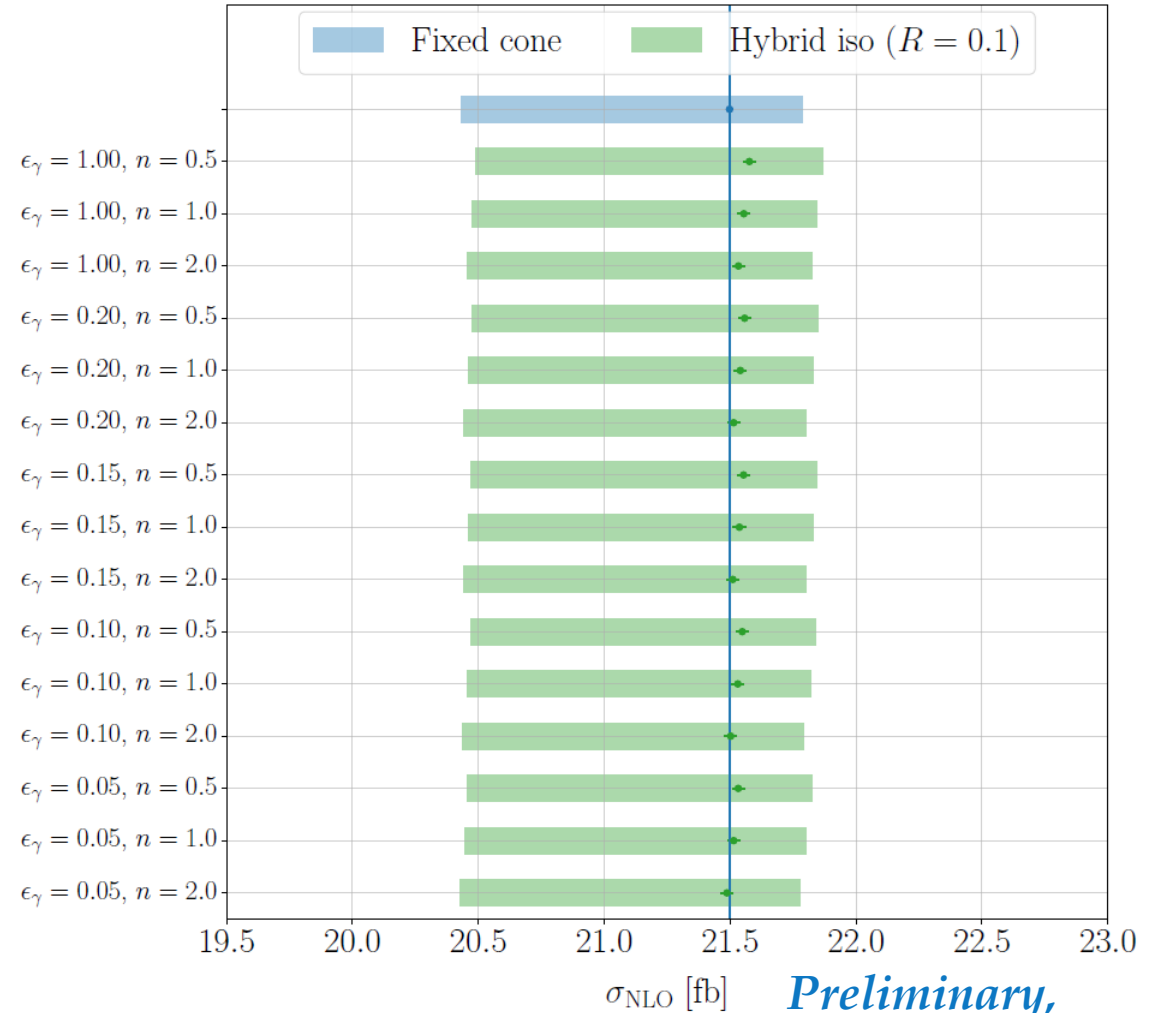
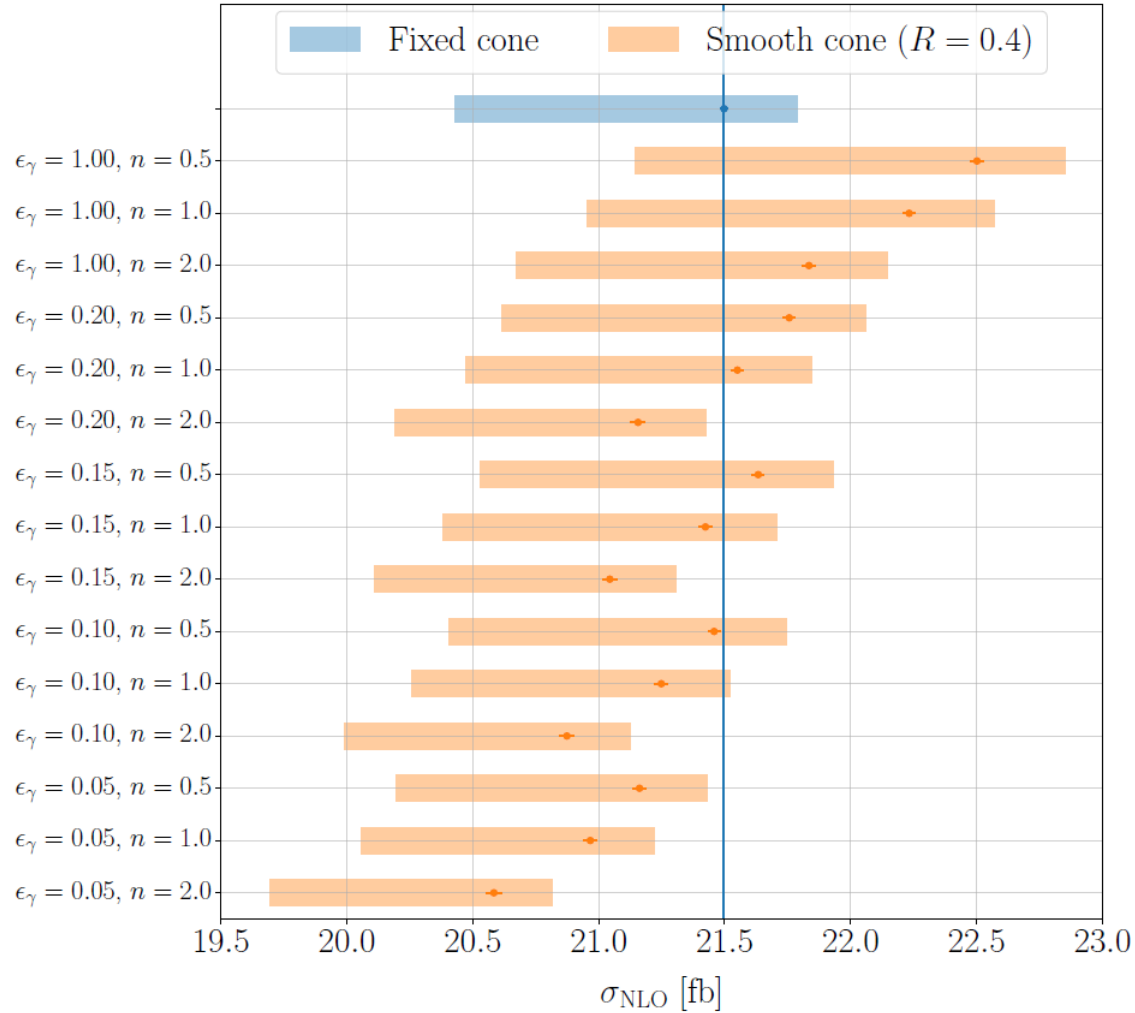


- Subleading NLO corrections as large as **10%** due to EW Sudakov logarithms in **NLO₂**
- Accidental cancellations between **NLO₂** and **NLO₃**
- Negligible differences between **NLO_{prd}** and **NLO** of less than **2%**

Photon isolation criteria

- Smooth-cone isolation *Frixione '98*
 - $E_{T,\text{had}}(R) \leq \epsilon_\gamma E_{T,\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n$ for all $R \leq R_{\gamma j}$
 - Removes collinear photon-quark configurations → Removes fragmentation contribution
 - Cannot directly be used in experiments
 - Input parameters ϵ_γ , n (and $R_{\gamma j}$) are arbitrary
- Fixed-cone isolation
 - $E_{T,\text{had}}(R_{\gamma j}) \leq E_{T,\text{max}}(E_{T,\gamma})$
 - Collinear photon-quark configurations allowed
 - $d\hat{\sigma}^{\gamma+X,\text{NLO}} = d\hat{\sigma}_\gamma^{\text{NLO}} + \sum_p d\hat{\sigma}_p^{\text{LO}} \otimes D_{p \rightarrow \gamma} - \frac{\alpha}{2\pi} \sum_p d\hat{\sigma}_p^{\text{LO}} \otimes \mathbf{\Gamma}_{p \rightarrow \gamma}^{(0)}$
- Hybrid photon isolation
 - First use smooth-cone isolation to remove fragmentation contribution and then the fixed-cone isolation
 - Reduces dependence on (arbitrary) input parameters in smooth-cone isolation
- Setup based on recent ATLAS analysis: [arXiv: 2403.09452 \[hep-ex\]](https://arxiv.org/abs/2403.09452)
 - $E_{T,\text{had}}(R = 0.4) < 0.022 \cdot E_{T,\gamma} + 2.45 \text{ GeV}$ and $E_{T,\text{had}}(R = 0.2) < 0.05 \cdot E_{T,\gamma}$
 - ALEPH LO quark-to-photon fragmentation function

Photon isolation in $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} \gamma$ at $\sqrt{s} = 13.6$ TeV



- Fragmentation contribution negligible small with $\sim 0.2\%$
- Hybrid photon isolation reduces dependence on input parameters in (inner) smooth-cone isolation

*Preliminary,
Stremmer, Worek*

Conclusion

- Prompt photon distribution in $pp \rightarrow t\bar{t}\gamma$ in the NWA
 - Only 40% of integrated fiducial cross section from Prod.
 - Only sum of all resonant contributions leads to accurate predictions
- Calculation of complete NLO corrections in $pp \rightarrow t\bar{t}\gamma$ and $pp \rightarrow t\bar{t}\gamma\gamma$ in the NWA
 - Negligible impact at the integrated level
 - Enhancement of EW Sudakov logarithms in NLO_2 → Reduction in tails up to 10%
 - Accidental cancellations between NLO_2 and NLO_3
 - NLO_{prd} is good approximation → Sufficient to include subleading NLO corrections in $t\bar{t}\gamma(\gamma)$ production
- First calculation of $pp \rightarrow t\bar{t}\gamma$ at NLO QCD with fixed-cone isolation
 - Small fragmentation contribution $\sim 0.2\%$
 - Large dependence on input parameters in smooth-cone isolation → Requires tuning of parameters
 - Basically no dependence on input parameters in hybrid photon isolation

Outlook

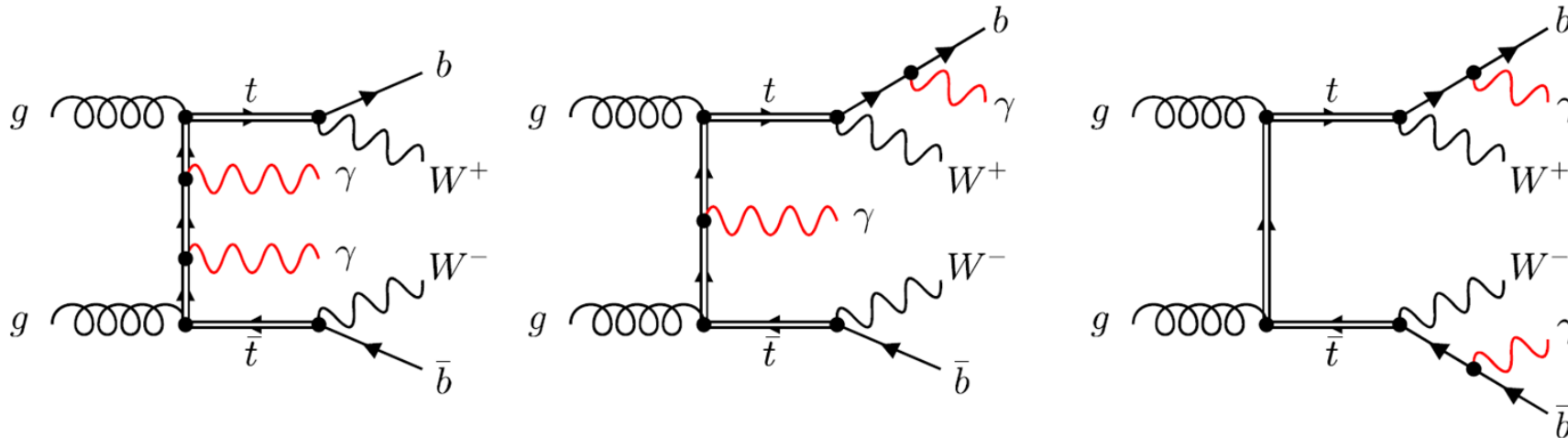
- Extend study of realistic photon isolation condition to $pp \rightarrow t\bar{t}\gamma$ and lepton + jet top-quark decay channel

Backup

Setup

$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \begin{cases} l^+l^- \nu_e\bar{\nu}_e b\bar{b} \gamma\gamma \\ l^-\bar{\nu}_e jj b\bar{b} \gamma\gamma \end{cases} \quad l^\pm = e^\pm, \mu^\pm$$

- LHC with $\sqrt{s} = 13$ TeV
- Calculation performed in [Narrow Width Approximation](#) preserving spin correlations
- [Photon bremsstrahlung](#) and [NLO QCD](#) corrections included in $t\bar{t}$ production and decay
- Diagonal CKM matrix
- 5 flavour scheme ($m_b = 0$)
- Top-quark width treated as fixed parameter ($\Gamma_t^{NLO}(\mu_R = m_t)$)



Setup of the calculation

- G_μ scheme: $\alpha = \frac{\sqrt{2}}{\pi} G_\mu M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right)$
- External photon radiation with $\alpha^{-1} = \alpha^{-1}(0) = 137.035999084$
- Renormalisation/Factorisation scale: $\mu_R = \mu_F = \mu_0 = \frac{E_T}{4}$ $E_T = \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} + p_{T,\gamma_1} + p_{T,\gamma_2}$
- NNPDF3.1(luxQED) NLO PDF set with $\alpha_s(M_Z) = 0.118$

- Smooth-cone isolation *Frixione '98*

$$\sum_i E_{T,i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T,\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n \quad \text{for all } R \leq R_{\gamma j}$$

- with $R_{\gamma j} = 0.4$ and $\epsilon_\gamma = n = 1$
- Anti- k_T jet algorithm ($R = 0.4$) *Cacciari, Salam, Soyez '08*

Setup of the calculation (2)

- Exclusive in $n_b = 2$

- Event selection:

$$p_{T,\ell} > 25 \text{ GeV}, \quad |y_\ell| < 2.5, \quad \Delta R_{\ell\ell} > 0.4,$$

$$p_{T,b} > 25 \text{ GeV}, \quad |y_b| < 2.5, \quad \Delta R_{bb} > 0.4,$$

$$p_{T,\gamma} > 25 \text{ GeV}, \quad |y_\gamma| < 2.5, \quad \Delta R_{\gamma\gamma} > 0.4,$$

$$\Delta R_{bl} > 0.4, \quad \Delta R_{\gamma l} > 0.4, \quad \Delta R_{\gamma b} > 0.4$$

- Additional cuts in lepton+jet channel:

$$p_{T,j} > 25 \text{ GeV}, \quad |y_j| < 2.5, \quad \Delta R_{jj} > 0.4,$$

$$\Delta R_{\ell j} > 0.4, \quad \Delta R_{bj} > 0.4, \quad \Delta R_{\gamma j} > 0.4$$

$$|m_W - M_{jj}| < 15 \text{ GeV}$$

- Modifications in fixed-cone isolation setup:

$$\text{▪ } n_b \geq 2, \quad p_{T,\gamma} > 20 \text{ GeV}, \quad |y_\gamma| < 2.37$$

Integrated Fiducial cross section in di-lepton channel

$$pp \rightarrow t\bar{t}(\gamma\gamma) \rightarrow W^+W^-b\bar{b}(\gamma\gamma) \rightarrow \ell^+\ell^-\nu_e\bar{\nu}_e b\bar{b}\gamma\gamma$$

μ_0		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
	σ_{Full} [fb]	$0.13868(3)^{+31.2\%}_{-22.1\%}$	$0.1773(1)^{+1.8\%}_{-6.2\%}$	1.28
$E_T/4$	$\sigma_{\text{Prod.}}$ [fb]	$0.05399(2)^{+30.6\%}_{-21.7\%}$	$0.07130(6)^{+2.5\%}_{-7.2\%}$	1.32
	σ_{Mixed} [fb]	$0.06022(2)^{+31.9\%}_{-22.5\%}$	$0.07733(8)^{+1.5\%}_{-6.2\%}$	1.28
	σ_{Decay} [fb]	$0.024473(7)^{+30.9\%}_{-22.1\%}$	$0.02863(4)^{+0.9\%}_{-4.9\%}$	1.17

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- NLO QCD corrections $\sim 30\%$
- Scale uncertainties reduced from 31% to 6%
- Relative size to Full: Prod. (40%), Mixed (44%) and Decay (16%)
- Internal PDF uncertainties: NNPDF3.1 1.0% , MSHT20 1.4% , CT18 2.0%

Resonant contributions

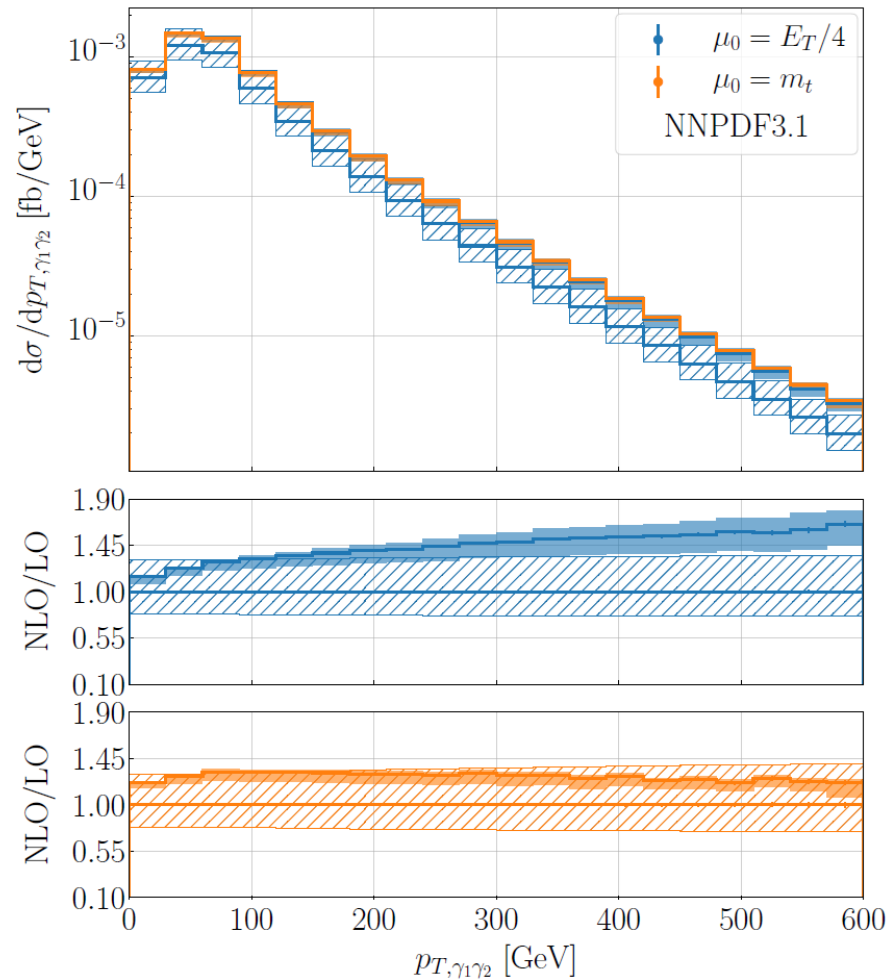
		gg	gg/pp	$q\bar{q}$	$q\bar{q}/pp$	$qg + \bar{q}g$	$(qg + \bar{q}g)/pp$
$\sigma_{\text{Full}}^{\text{NLO}}$	[fb]	0.0999(1)	56.4%	0.04307(4)	24.3%	0.03428(4)	19.3%
$\sigma_{\text{Prod.}}^{\text{NLO}}$	[fb]	0.02587(4)	36.3%	0.02672(4)	37.5%	0.01871(3)	26.2%
$\sigma_{\text{Mixed}}^{\text{NLO}}$	[fb]	0.04928(8)	63.7%	0.01408(2)	18.2%	0.01398(2)	18.1%
$\sigma_{\text{Decay}}^{\text{NLO}}$	[fb]	0.02476(4)	86.5%	0.002268(3)	7.9%	0.00160(2)	5.6%

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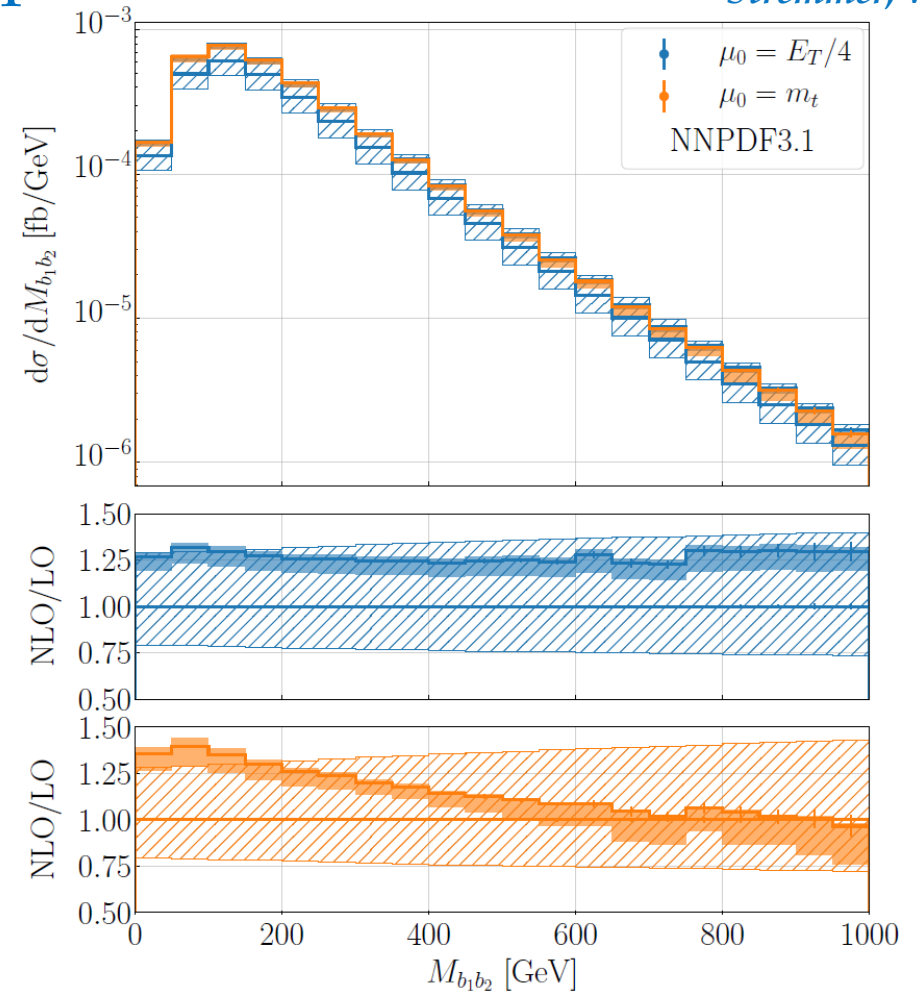
- Full dominated by gg with 56.4%
- $q\bar{q}$ channel decreases, gg channel increases in absolute size from Prod. to Mixed
- gg channel suppressed for increasing number of photons in $t\bar{t}$ production
- Conclusions also hold in lepton + jet top-quark decay channel

Differential Fiducial cross section in di-lepton channel

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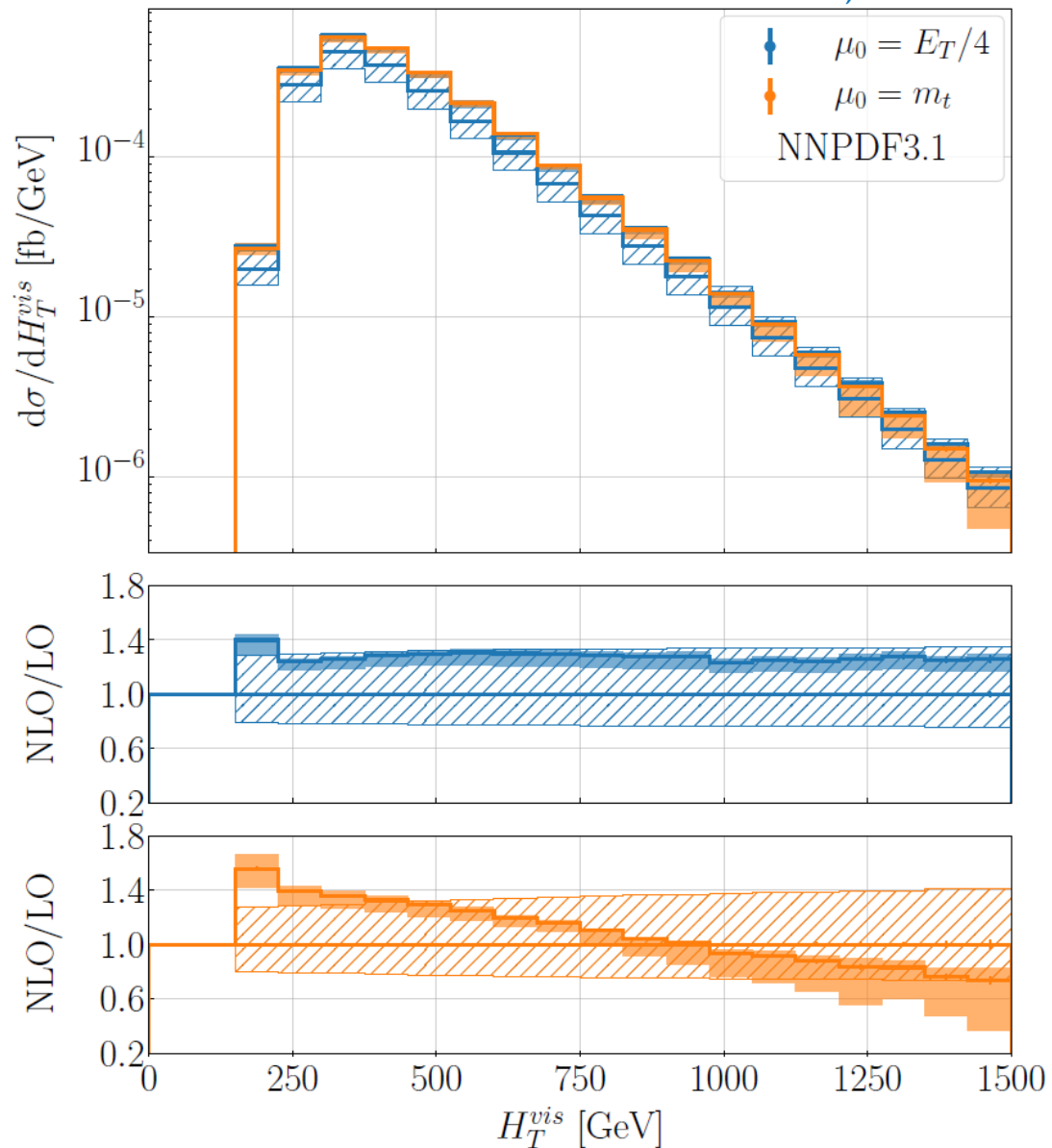
- NLO QCD corrections up to 65%
- Smaller corrections for $\mu_0 = m_t$
- Scale uncertainties 5% – 13%



- NLO QCD corrections $\sim 25\% - 30\%$
- Scale uncertainties reduced from $\sim 35\%$ to 5% – 8%
- Increasing scale uncertainties in tails for $\mu_0 = m_t$

Differential Fiducial cross section in di-lepton channel

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$$H_T^{vis} = p_{T,\ell^+} + p_{T,\ell^-} + p_{T,b_1} + p_{T,b_2} + p_{T,\gamma_1} + p_{T,\gamma_2}$$

- Fixed scale unstable for general dimensionful observables:
 - Large shape distortions
 - NLO scale uncertainties, up to 50%, exceeding LO ones

→ Dynamical scale in general required

Integrated Fiducial cross section in lepton + jet channel

$$|m_W - M_{jj}| < 15 \text{ GeV}$$

μ_0		LO	NLO	$\mathcal{K} = \sigma_{\text{NLO}}/\sigma_{\text{LO}}$
$E_T/4$	σ_{Full} [fb]	$0.24214(4)^{+31.1\%}_{-22.0\%}$	$0.2973(3)^{+1.9\%}_{-5.4\%}$	1.23
	$\sigma_{\text{Prod.}}$ [fb]	$0.11960(3)^{+30.5\%}_{-21.6\%}$	$0.1405(2)^{+2.1\%}_{-4.6\%}$	1.17
	σ_{Mixed} [fb]	$0.09632(3)^{+31.9\%}_{-22.5\%}$	$0.1205(2)^{+1.5\%}_{-5.7\%}$	1.25
	σ_{Decay} [fb]	$0.026230(9)^{+30.9\%}_{-22.1\%}$	$0.03629(7)^{+3.3\%}_{-7.7\%}$	1.38

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- NLO corrections $\sim 23\%$, scale uncertainties reduced from $\sim 31\%$ to $\sim 5\%$
- **Prod.** increased from 40% (di-lepton) to 48% (lepton + jet) because of by additional cut

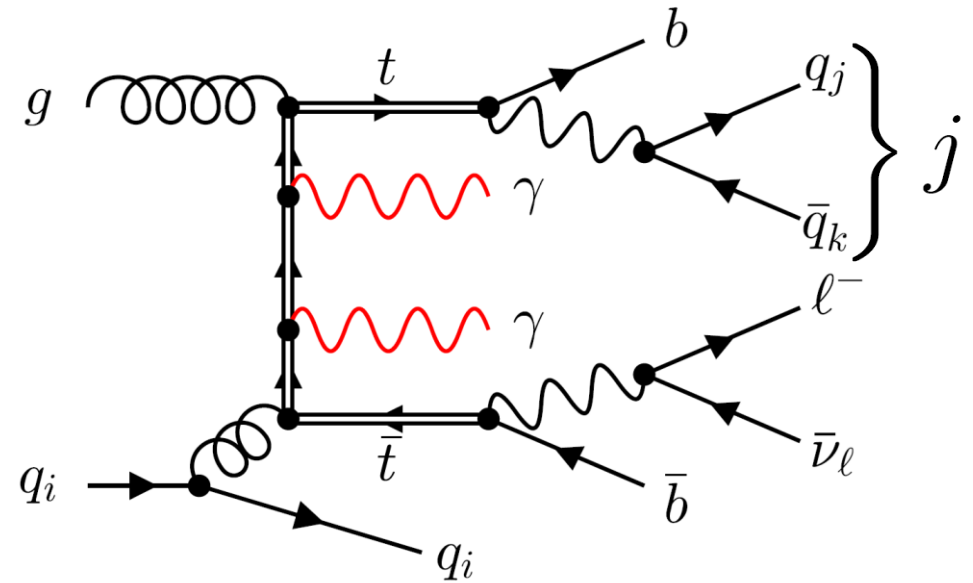
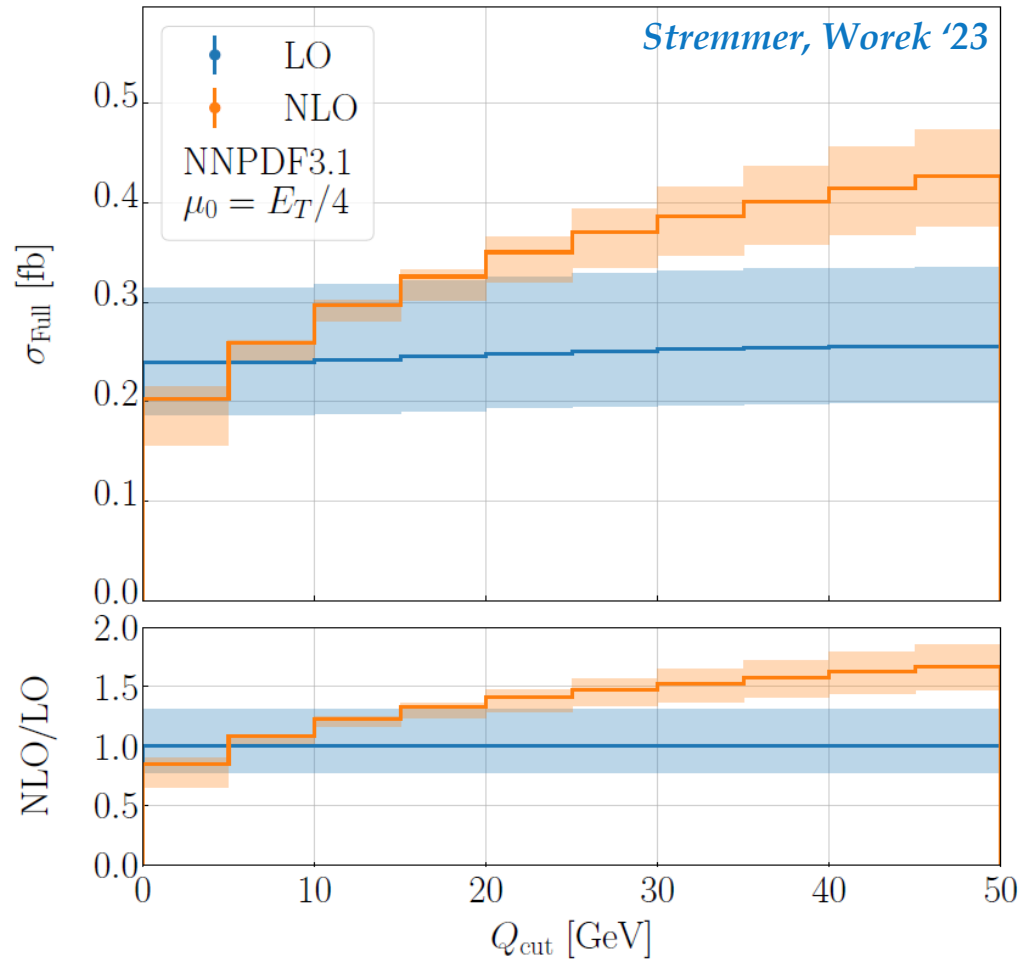
$$\sigma_{\text{Full}}^{\text{NLO}}(\epsilon_\gamma = 0.5) = 0.2832(7) \text{ fb}$$

$$\sigma_{\text{Full}}^{\text{NLO}}(E_{T\gamma} \epsilon_\gamma = 10 \text{ GeV}) = 0.2666(8) \text{ fb}$$

$$\sum_i E_{T_i} \Theta(R - R_{\gamma i}) \leq \epsilon_\gamma E_{T\gamma} \left(\frac{1 - \cos(R)}{1 - \cos(R_{\gamma j})} \right)^n$$

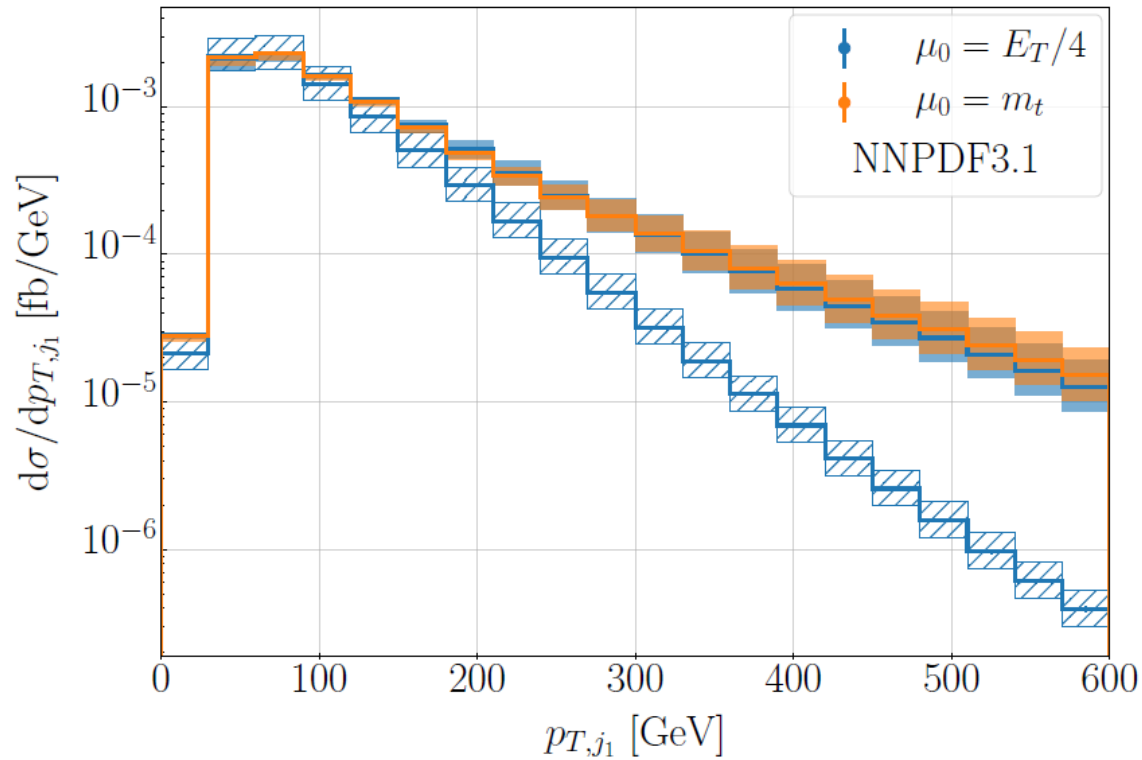
- Significant deviations ($5\% - 10\%$) between different input parameters in Smooth photon isolation prescription

Integrated Fiducial cross section in lepton + jet channel

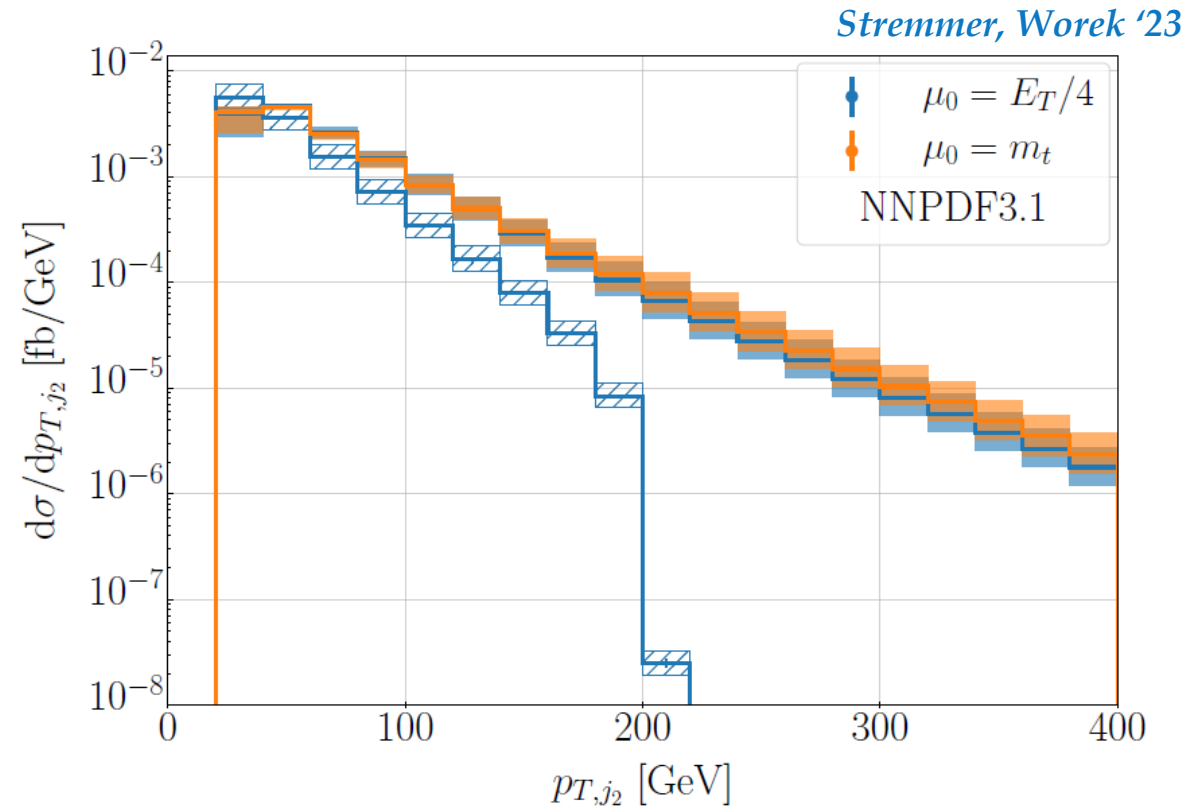


- Large NLO QCD corrections of $\sim 140\%$ for $Q_{\text{cut}} \rightarrow \infty$ caused by hard radiation in production stage
- NLO QCD corrections drastically reduced by additional $|m_W - M_{jj}| < Q_{\text{cut}}$

Differential Fiducial cross section in lepton + jet channel



- Huge NLO QCD corrections caused by hard jets in the production stage
- Scale uncertainties in tails $\sim 50\%$

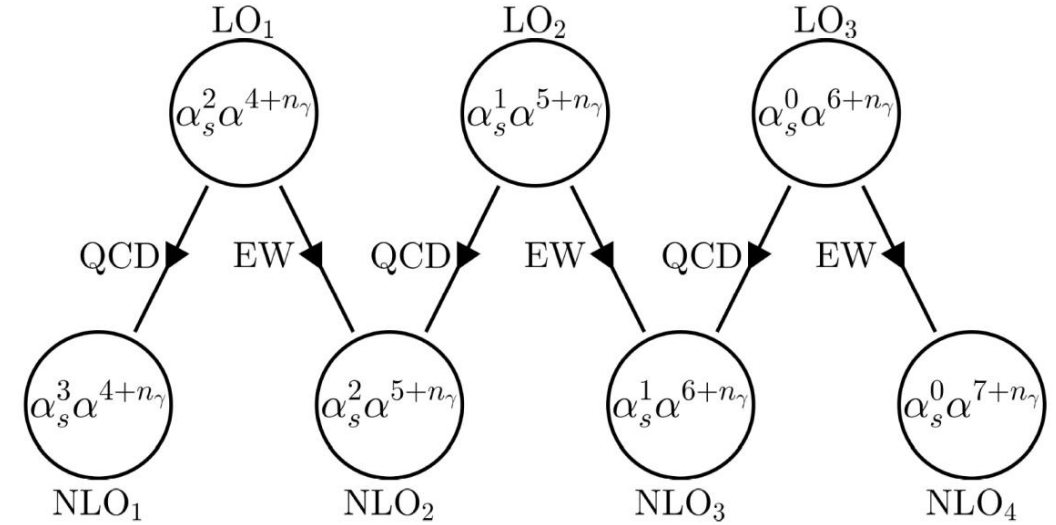


- LO spectrum limited by finite W boson mass
 $p_{T,j_2,max} \sim m_W/\Delta R_{jj} \sim 203$ GeV
- Scale uncertainties in tails $\sim 50\%$

Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel

		σ_i [fb]	Ratio to LO ₁
LO ₁	$\mathcal{O}(\alpha_s^2\alpha^6)$	0.15928(3) ^{+31.3%} _{-22.1%}	1.00
LO ₂	$\mathcal{O}(\alpha_s^1\alpha^7)$	0.0003798(2) ^{+25.8%} _{-19.2%}	+0.24%
LO ₃	$\mathcal{O}(\alpha_s^0\alpha^8)$	0.0010991(2) ^{+10.6%} _{-13.1%}	+0.69%
NLO ₁	$\mathcal{O}(\alpha_s^3\alpha^6)$	+0.0110(2)	+6.89%
NLO ₂	$\mathcal{O}(\alpha_s^2\alpha^7)$	-0.00233(2)	-1.46%
NLO ₃	$\mathcal{O}(\alpha_s^1\alpha^8)$	+0.000619(1)	+0.39%
NLO ₄	$\mathcal{O}(\alpha_s^0\alpha^9)$	-0.0000166(2)	-0.01%
LO		0.16076(3) ^{+30.9%} _{-21.9%}	1.0093
NLO _{QCD}		0.1703(2) ^{+1.9%} _{-6.2%}	1.0690
NLO _{prd}		0.1694(2) ^{+1.7%} _{-5.9%}	1.0637
NLO		0.1700(2) ^{+1.8%} _{-6.0%}	1.0674

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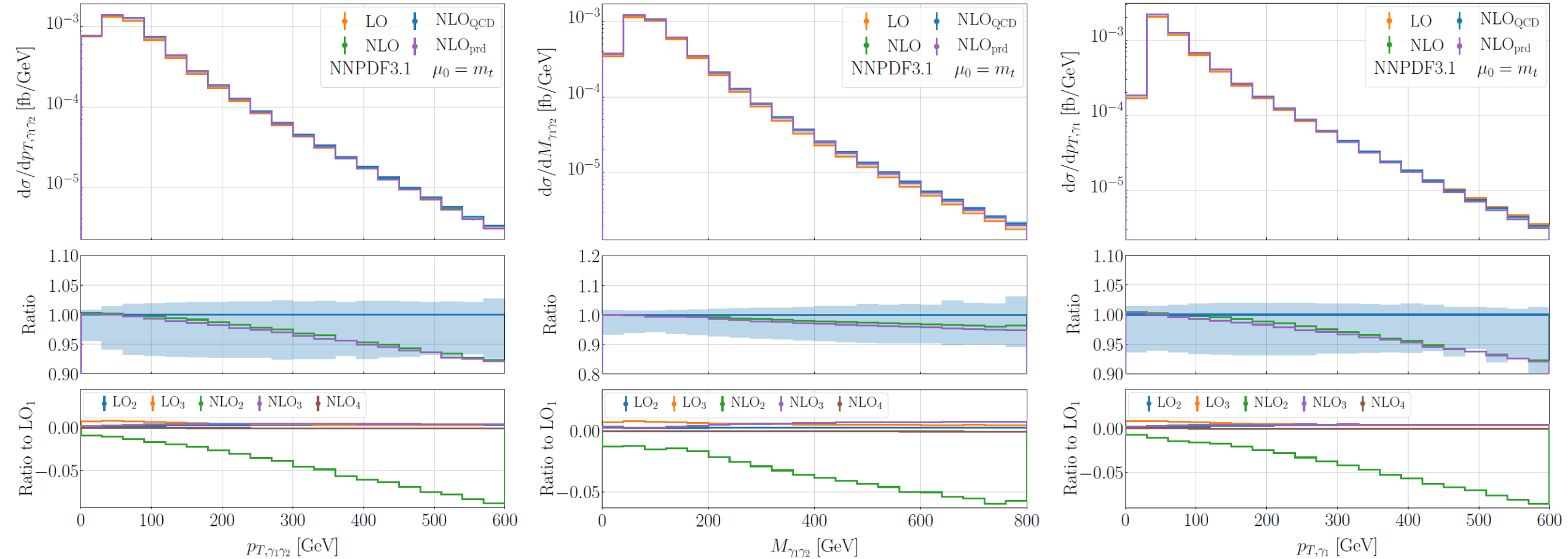


- Subleading LO contributions $\sim 1\%$
- NLO corrections dominated by **NLO₁**
- Subleading NLO corrections $\sim 1\%$

- $\text{NLO}_{\text{prd}} = \text{LO}_1 + \text{LO}_2 + \text{LO}_3 + \text{NLO}_1 + \text{NLO}_{2,\text{prd}} + \text{NLO}_{3,\text{prd}} + \text{NLO}_{4,\text{prd}}$
- No photon radiation and higher-order corrections in top-quark decays in subleading NLO contributions

Complete NLO predictions for $pp \rightarrow t\bar{t}\gamma\gamma$ in di-lepton channel

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- Subleading NLO corrections as large as **10%** due to EW Sudakov logarithms in **NLO₂**
- Accidental cancellations between **NLO₂** and **NLO₃**
- Negligible differences between **NLO_{prd}** and **NLO** of less than **2%**