

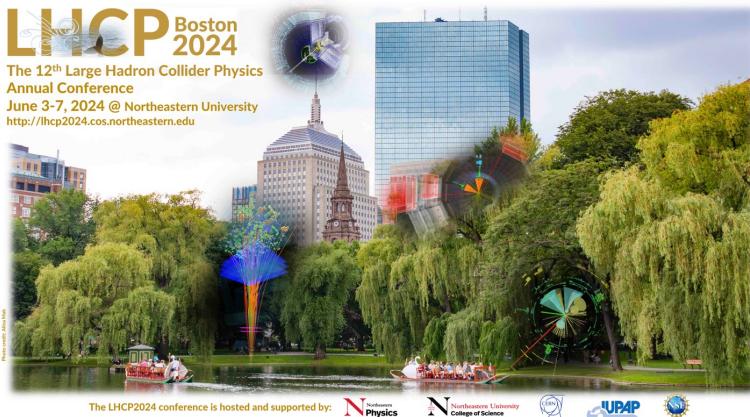
# Progress in top-quark pair production cross section calculations and impact on PDFs

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with

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and with N. Kidonakis, and A. Tonero



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# Main goals and motivations

$t\bar{t}$  production at the LHC: clean probe for PDFs at intermediate and large  $x$   
(where it complements jet prod.) PDFs currently poorly constrained at large  $x$ .

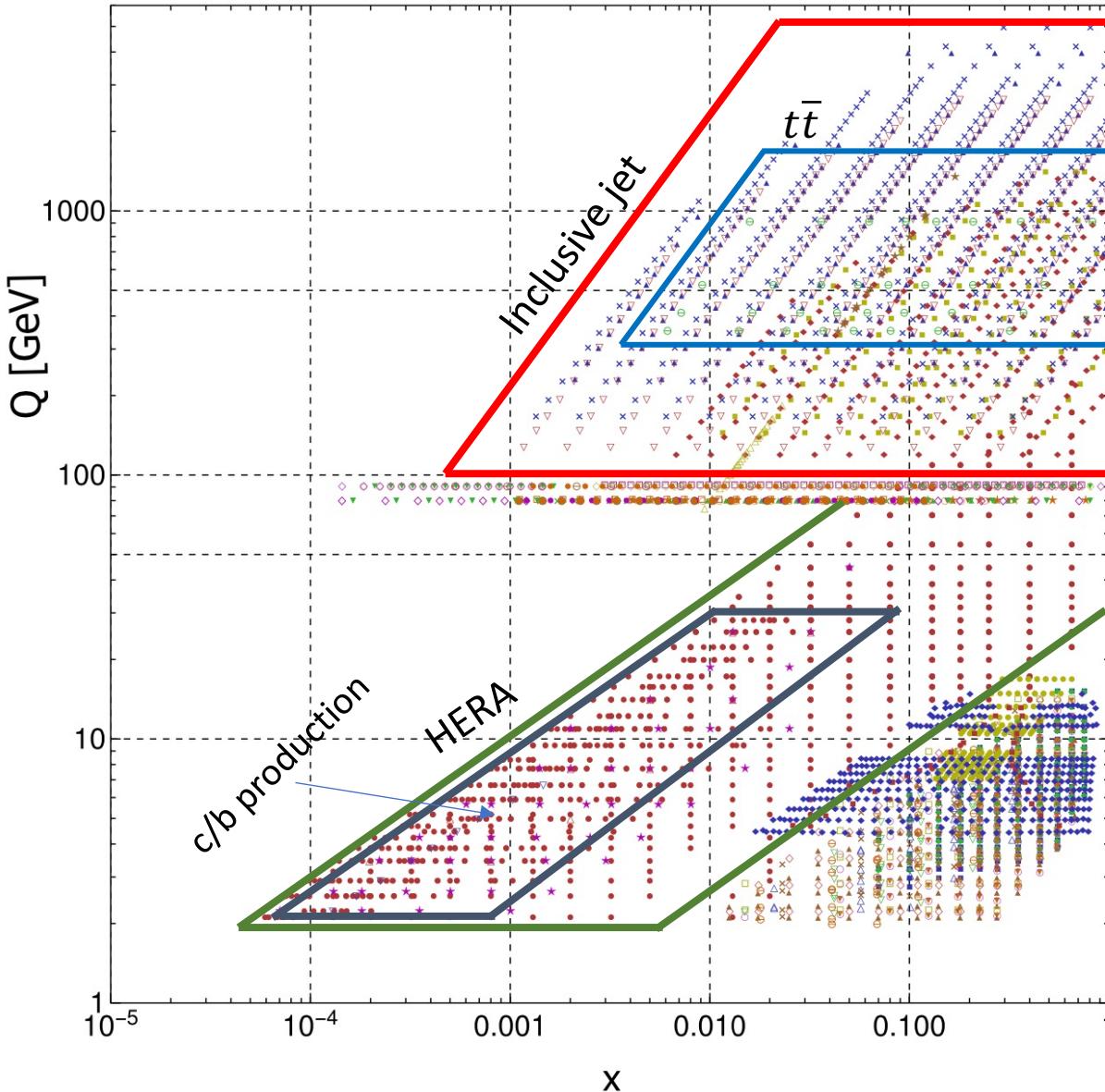
- Toward the next (CT2X) CTEQ-PDFs release. Efforts are being put into:
  1. Selecting sensitive data from recent high-precision measurements at the LHC
  2. Understand current PDF uncertainties (tolerance, methodology, functional forms,...)
  3. State-of-the-art calculations

This talk:

- eligible  $t\bar{t}$  production 1D abs. diff. Xsec measurements at the LHC 13 TeV and their impact on the gluon at large  $x$  from an optimal baseline selection in NNLO global fits  
(Ablat, MG, Xie, et al. 2307.11153, PRD 2024)
- Explore the impact of aN<sup>3</sup>LO QCD corrections + NLO EW on  $t\bar{t}$  observables  
(Kidonakis, MG, Tonero, 2306.06166, PRD 2023)

# PDF Kinematics in the $Q$ - $x$ plane

Experimental data in CT18 PDF analysis

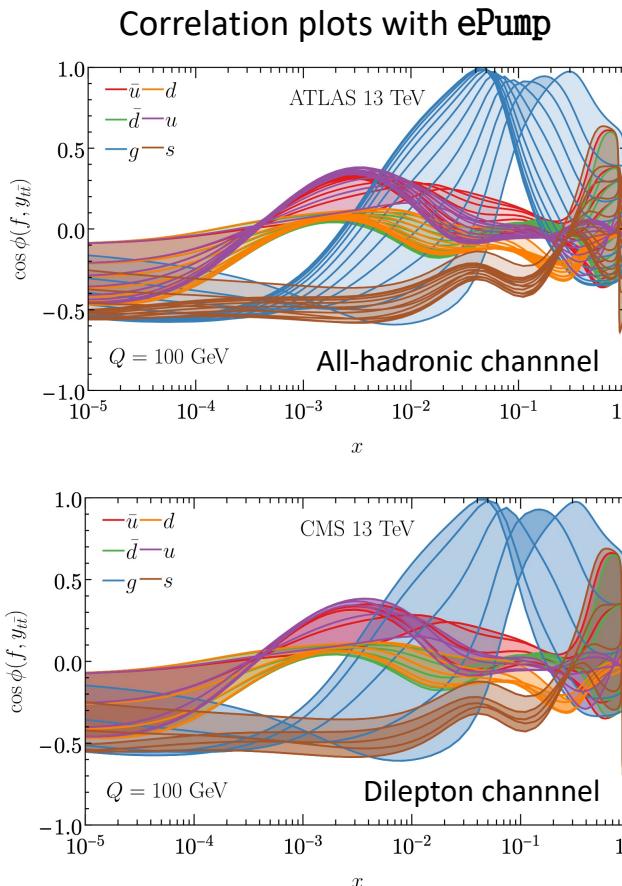


Top-quark pair production  
@LHC can already probe  
the gluon PDF at  $x \gtrsim 0.01$



$$x_{1,2} \approx \frac{\sqrt{p_T^2 + m_Q^2}}{\sqrt{S}} e^{\pm y}$$

Jet and  $t\bar{t}$  complement each other in the kinematic plane.  
They impact the gluon PDF at large  $x$ . Important to disentangle the effect due to jet production and top-quark data.

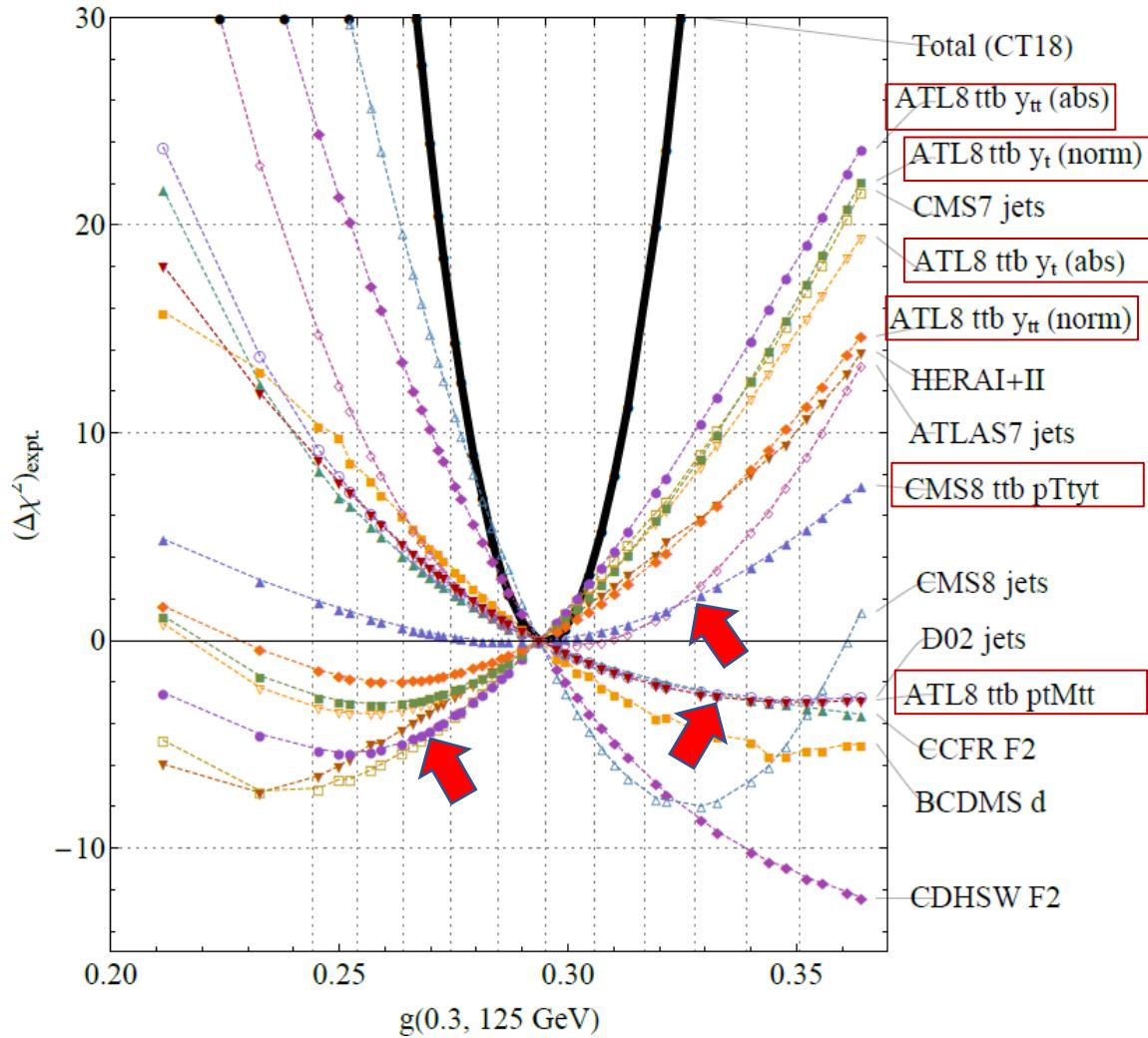


$t\bar{t}$  and jet data in CT18

Top-quark  
1511.04716 ATLAS 8 TeV tt<sub>b</sub> ptT diff. distributions  
1511.04716 ATLAS 8 TeV tt<sub>b</sub> mtt diff. distributions  
1703.01630 CMS 8 TeV tt<sub>b</sub> (pT, yt) 2d diff. distrib.

Jet production  
1406.0324 CMS incl. jet at 7 TeV with R=0.7  
1410.08857 ATLAS incl. jet at 7 TeV with R=0.6  
1609.05331 CMS incl. jet at 8 TeV with R=0.7

# Constraints from 8 TeV $t\bar{t}$ production data in CT18



Realistic PDF error estimates account for:

- multiple PDF functional forms
- disagreements between measurements

→ mild impact from  $t\bar{t}$  data

In the figure: Pulls on the gluon from ATLAS8  $y_{t\bar{t}}$  and  $y_t$  distributions (absolute or normalized) agree with HERA DIS, oppose ATLAS8  $d^2\sigma/(dp_{T,t} dm_{t\bar{t}})$  and CMS8  $d^2\sigma/(dp_{T,t} dy_{t,\text{ave}})$

# Impact of LHC 13 TeV $t\bar{t}$ production on CTEQ PDFs

**CT2X ⊇ CT18 + new optimal combination of top-quark pair production @LHC13 TeV from:**

- ATLAS all hadronic, JHEP 01 (2021) 033, arXiv:2006.09274
- ATLAS lepton + jets, EPJC 79 (2019) 1028, arXiv:1908.07305
- CMS dilepton, JHEP 1902 (2019) 149, arXiv:1811.06625
- CMS lepton + jets, PRD 104 092013 (2021), arXiv:2108.02803

(Ablat, MG, Xie, et al. 2307.11153, PRD 2024)

**Correlated Systematic Uncertainties:**   
**ATLAS -> nuisance parameters**  
**CMS -> Covariance matrix representation**  
 (we converted to nuisance param. )

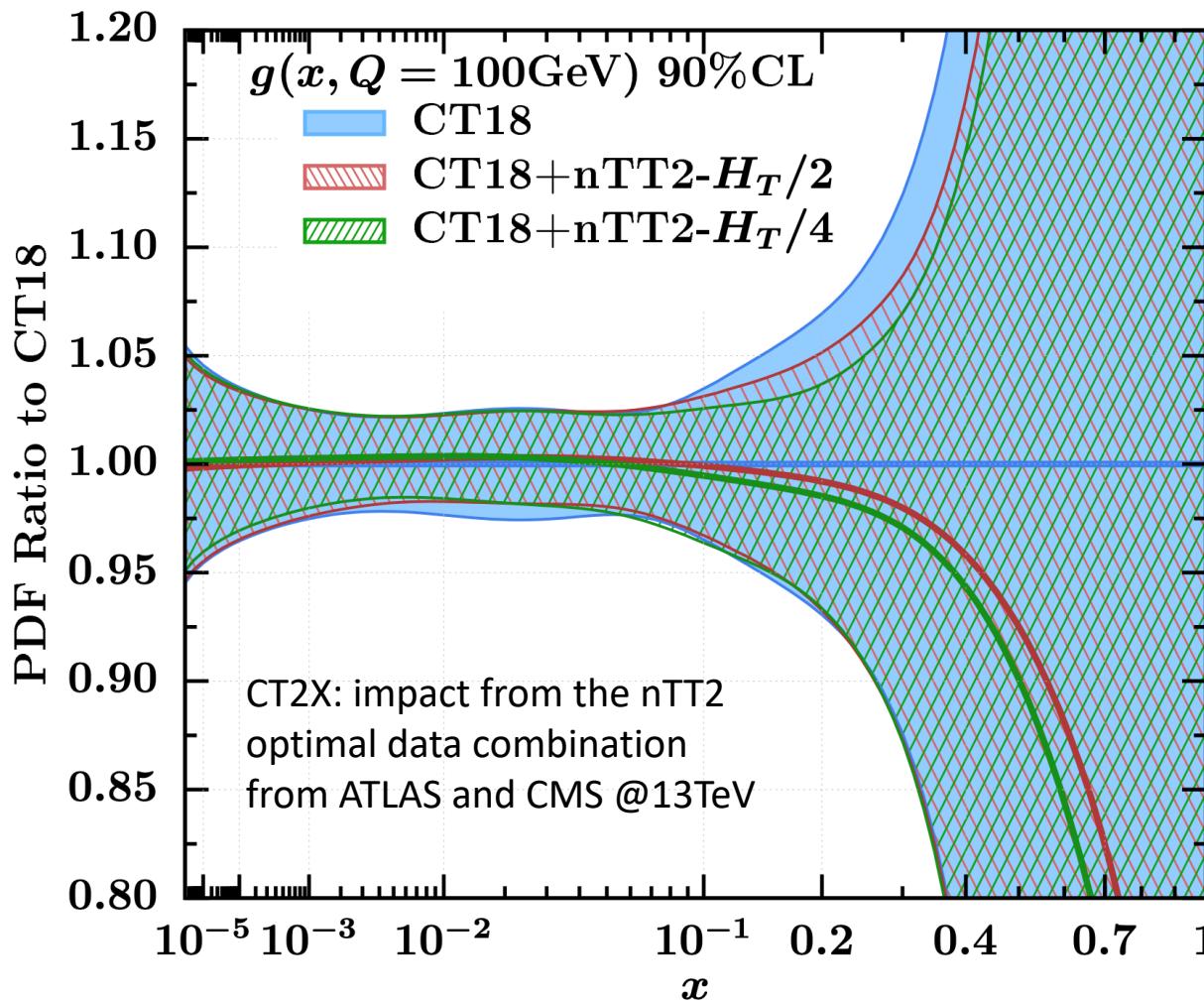
**When statistical correlations not provided**  data added one at a time on top of the CT18 baseline

We studied the impact on PDFs due to several factors such as:

- $\mu_F$  and  $\mu_R$  scale dependence
- different binning for the same distribution
- statistical correlations

Exp	Obs	$N_{pt}$	ePump			Global fit	
			$H_T$	$H_T/2$	$H_T/4$	$H_T/2$	$H_T/4$
ATL13had	$m_{t\bar{t}}$	9	1.75	1.57	1.60	1.53	1.47
	$H_T^{t\bar{t}}$	11	1.98	1.77	1.59	1.50	1.74
	$y_{t\bar{t}}$	12	1.28	1.15	0.94	1.05	1.07
	$p_{T,t_1}$	10	1.30	1.19	1.12	1.20	1.33
	$p_{T,t_2}$	8	1.13	0.84	1.05	0.84	1.59
CMS13ll	$m_{t\bar{t}}$	7	3.46	3.07	3.14	3.12	3.23
	$y_{t\bar{t}}$	10	1.66	0.97	0.68	0.94	0.67
	$p_{T,t}$	6	3.60	3.70	3.68	3.56	3.05
	$y_t$	10	1.33	0.94	0.87	1.00	0.69
CMS13lj	$m_{t\bar{t}}$	15	1.49	1.38	1.81	1.20	1.67
	$y_{t\bar{t}}$	10	6.47	6.24	6.42	6.01	5.88
ATL13lj	CMS bins						
	$m_{t\bar{t}}$	7	2.40	1.17	0.68	0.83	0.66
	$y_{t\bar{t}}$	10	0.91	0.69	0.62	0.74	0.75
	$p_{T,t}$	6	2.34	2.01	2.47	1.35	1.43
	$y_t$	10	1.30	1.07	1.10	1.16	0.68
	ATLAS bins without statistical correlation (NSC)						
	$m_{t\bar{t}}$	9	1.55	1.12	0.94	1.27	0.92
	$y_{t\bar{t}}$	7	0.91	0.74	0.80	0.76	0.90
	$y_{t\bar{t}}^B$	9	1.40	1.27	1.53	0.85	0.93
	$H_T^{t\bar{t}}$	9	1.35	0.91	0.93	0.81	0.80
	$m_{t\bar{t}} + y_{t\bar{t}} + y_{t\bar{t}}^B + H_T^{t\bar{t}}$	34	1.87	1.28	1.46	0.93	1.06
	ATLAS bins with statistical correlations (WSC)						
	$m_{t\bar{t}}$	9	1.68	1.35	0.98	1.29	0.96
	$y_{t\bar{t}}$	7	0.88	0.75	0.92	0.75	0.92
	$y_{t\bar{t}}^B$	9	1.06	0.87	1.01	0.86	0.99
	$H_T^{t\bar{t}}$	9	1.40	0.85	0.85	0.86	0.86
	$m_{t\bar{t}} + y_{t\bar{t}} + y_{t\bar{t}}^B + H_T^{t\bar{t}}$	34	3.10	1.61	1.32	1.59	1.32

# Impact of new high-precision LHC 13 TeV $t\bar{t}$ data on the gluon PDF



Theory predictions:

- MATRIX (Catani, Devoto, et al. PRD 2019, JHEP 2019)
- FastNNLO (Czakon, Mitov, 1704.08551; Czakon, Fiedler, et al., JHEP2016)

Blue band: CT18NNLO 90% C.L.

Hatched bands: CT18 + new top-quark data

Green:  $\mu_R = \mu_F = H_T/2$

Red:  $\mu_R = \mu_F = H_T/4$

Differences related to different scale choices are well within the CT18 PDF error band.

nTT2 baseline consists of 1D abs ttbar Xsec from:

- ATLAS all hadronic, ytt
- ATLAS lepton + jets, {ytt, Mtt, yBtt, HTtt} stat. comb.
- CMS dilepton, ytt
- CMS lepton + jets, Mtt

# NNLO theory predictions: setup

- CMS (dilepton ch): FastNLO grids for the NNLO theory– ([Czakon et al. 1704.08551](#))
- ATLAS: bin-by-bin NNLO/NLO K-factors generated by MATRIX ([Catani, Devoto, et al. PRD2019; JHEP2019](#))

The NLO QCD calculation is obtained using our in-house APPLGrid fast tables ([Carli et al. EPJC 2010](#)) for the public MCFM calculation ([Campbell, Ellis JPG 2015](#))

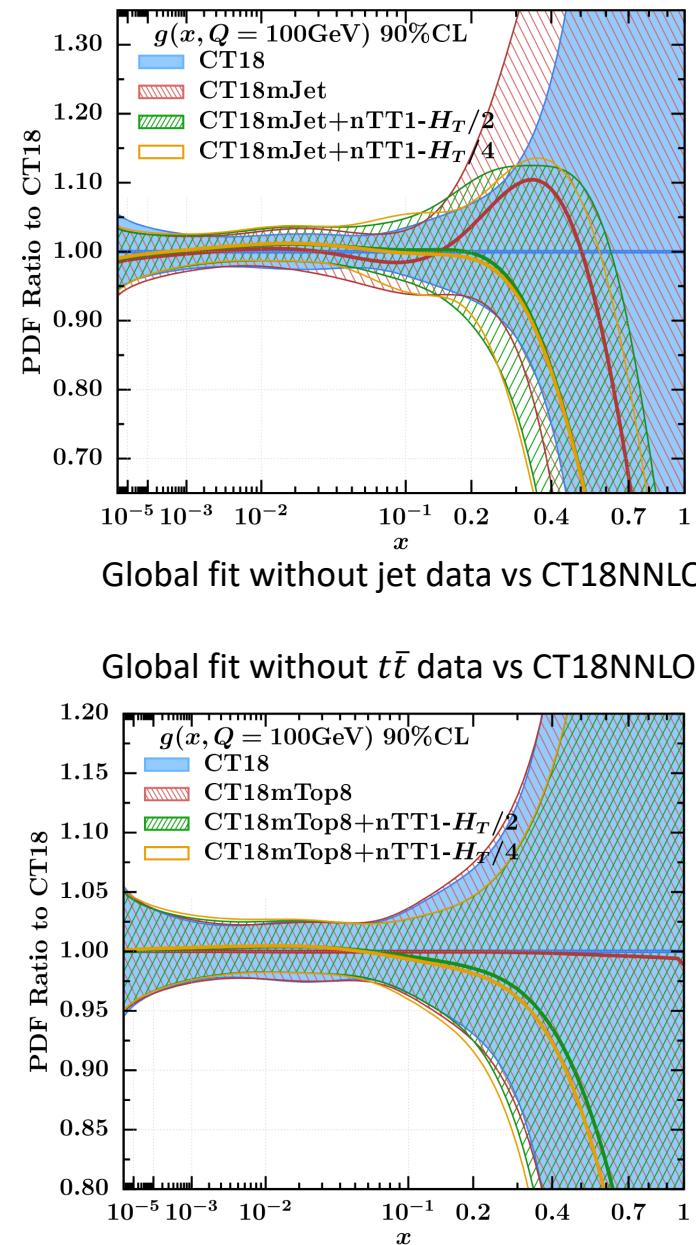
- $m_t(\text{pole}) = 172.5 \text{ GeV}$
- Fact/Ren scale choice:

$m_{tt}, p_{T,tt}, y_{tt}, y_t$  use:  $H_T/4$  and  $H_T/2$ ;  $p_{T,t}$ , use  $M_T$ ;  $p_{T,t} \text{ avg}$  use  $M_T/2$  ([Czakon et al. JHEP 2017](#))

$$\mu_F = \mu_R = H_T/4 = \left( \sqrt{m_t^2 + p_{T,t}^2} + \sqrt{m_t^2 + p_{T,\bar{t}}^2} \right) / 4 \quad \mu_{F,R} = M_T^t/2 = \sqrt{m_t^2 + p_T^2}/2$$

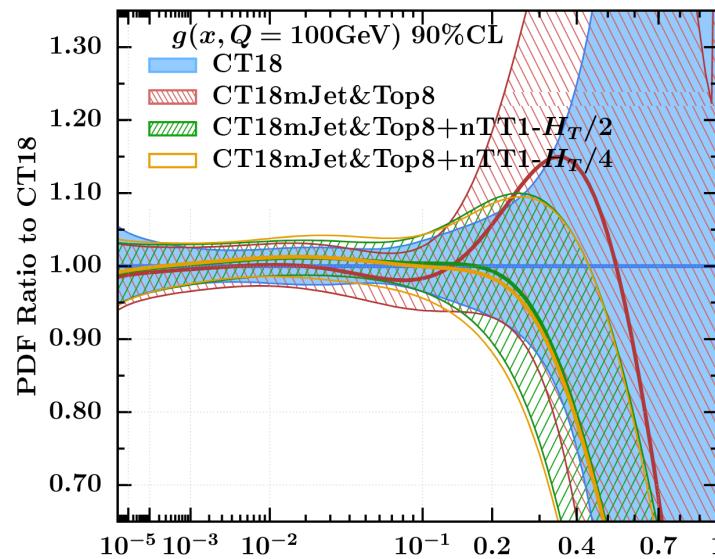
- **EW corrections considered:** negligible impact on our fits.

# Interplay between $t\bar{t}$ and QCD jets

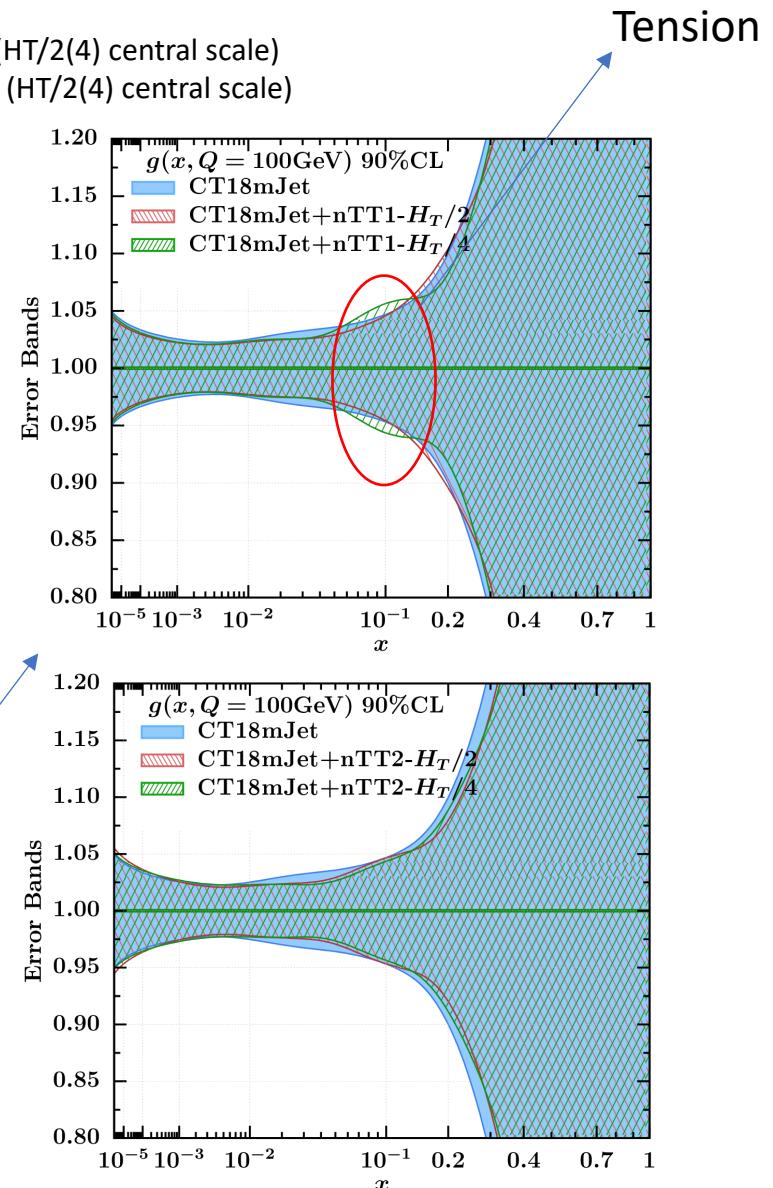


- CT18mTop = CT18 without all  $t\bar{t}$  8 TeV and 13 TeV
- CT18mJet = CT18 without all jet data
- CT18mJet+nTT1- $H_T/2(4)$  = CT18 without all jet data, but with  $t\bar{t}$  13 TeV ( $H_T/2(4)$  central scale)
- CT18mTop+nTT1- $H_T/2(4)$  = CT18 without all  $t\bar{t}$  8 TeV, but with  $t\bar{t}$  13 TeV ( $H_T/2(4)$  central scale)

Global fit without jet and  $t\bar{t}$  data vs CT18NNLO

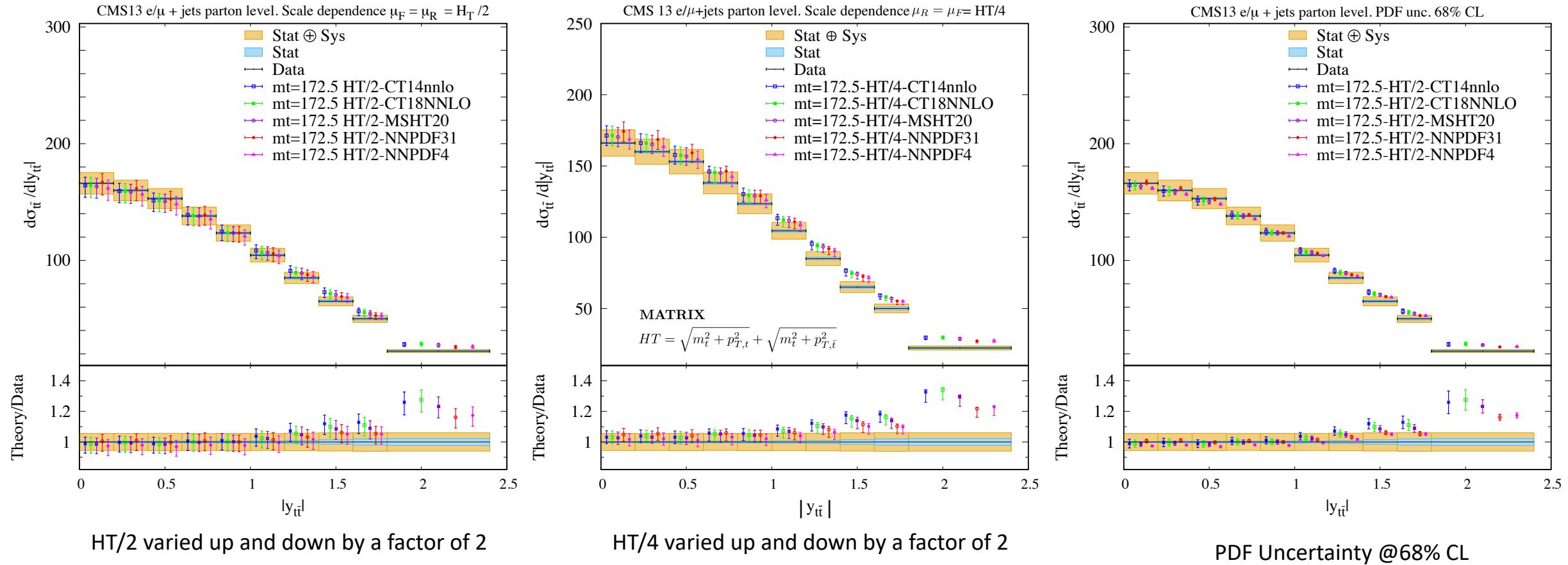


Differences between two optimal baseline selections of 13 TeV  $t\bar{t}$  data



# Theory errors: scale vs PDFs

Scale uncertainty: the recommended scale choice is not always the best. We select the scale choice that yields the smaller  $\chi^2/N_{pt}$



Scale uncertainty comparable or larger than PDF uncertainty

# Top-quark cross sections and distributions at aN^3LO

Theory calculation from Kidonakis 1405.7046, PRD (2014) and 1411.2633, PRD (2015) ([Kidonakis, MG, Tonero, 2306.06166, PRD 2023](#))

$$d\sigma_{pp \rightarrow t\bar{t}} = \sum_{a,b} \int dx_a dx_b \phi_{a/p}(x_a, \mu_F) \phi_{b/p}(x_b, \mu_F) d\hat{\sigma}_{ab \rightarrow t\bar{t}}(s_4, \mu_F) \quad \xrightarrow{\text{Laplace transf.}} \quad d\tilde{\sigma}_{ab \rightarrow t\bar{t}}(N) = \tilde{\phi}_{a/a}(N_a, \mu_F) \tilde{\phi}_{b/b}(N_b, \mu_F) d\hat{\sigma}_{ab \rightarrow t\bar{t}}(N, \mu_F)$$

$$\tilde{\phi}(N) = \int_0^1 e^{-N(1-x)} \phi(x) dx \quad \text{and} \quad d\tilde{\sigma}_{ab \rightarrow t\bar{t}}(N) = \int_0^s (ds_4/s) e^{-Ns_4/s} d\hat{\sigma}_{ab \rightarrow t\bar{t}}(s_4)$$

$$d\tilde{\sigma}_{ab \rightarrow t\bar{t}}(N) = \tilde{\psi}_{a/a}(N_a, \mu_F) \tilde{\psi}_{b/b}(N_b, \mu_F) \text{tr} \left\{ H_{ab \rightarrow t\bar{t}}(\alpha_s(\mu_R)) \tilde{S}_{ab \rightarrow t\bar{t}} \left( \frac{\sqrt{s}}{N\mu_F} \right) \right\} \quad \text{Refactorization in the N-space}$$

And from previous expressions

$$d\tilde{\sigma}_{ab \rightarrow t\bar{t}}(N, \mu_F) = \frac{\tilde{\psi}_{a/a}(N_a, \mu_F) \tilde{\psi}_{b/b}(N_b, \mu_F)}{\tilde{\phi}_{a/a}(N_a, \mu_F) \tilde{\phi}_{b/b}(N_b, \mu_F)} \text{tr} \left\{ H_{ab \rightarrow t\bar{t}}(\alpha_s(\mu_R)) \tilde{S}_{ab \rightarrow t\bar{t}} \left( \frac{\sqrt{s}}{N\mu_F} \right) \right\}$$

# Top-quark cross sections and distributions at aN<sup>^</sup>3LO

$$\begin{aligned}
d\tilde{\sigma}_{ab \rightarrow t\bar{t}}^{\text{resum}}(N, \mu_F) = & \exp \left[ \sum_{i=a,b} E_i(N_i) \right] \exp \left[ \sum_{i=a,b} 2 \int_{\mu_F}^{\sqrt{s}} \frac{d\mu}{\mu} \gamma_{i/i}(N_i) \right] \times \text{tr} \left\{ H_{ab \rightarrow t\bar{t}} \left( \alpha_s(\sqrt{s}) \right) \bar{P} \exp \left[ \int_{\sqrt{s}}^{\sqrt{s}/N} \frac{d\mu}{\mu} \Gamma_{S ab \rightarrow t\bar{t}}^\dagger(\alpha_s(\mu)) \right] \right. \\
& \left. \times \tilde{S}_{ab \rightarrow t\bar{t}} \left( \alpha_s \left( \frac{\sqrt{s}}{N} \right) \right) P \exp \left[ \int_{\sqrt{s}}^{\sqrt{s}/N} \frac{d\mu}{\mu} \Gamma_{S ab \rightarrow t\bar{t}}(\alpha_s(\mu)) \right] \right\}
\end{aligned}$$

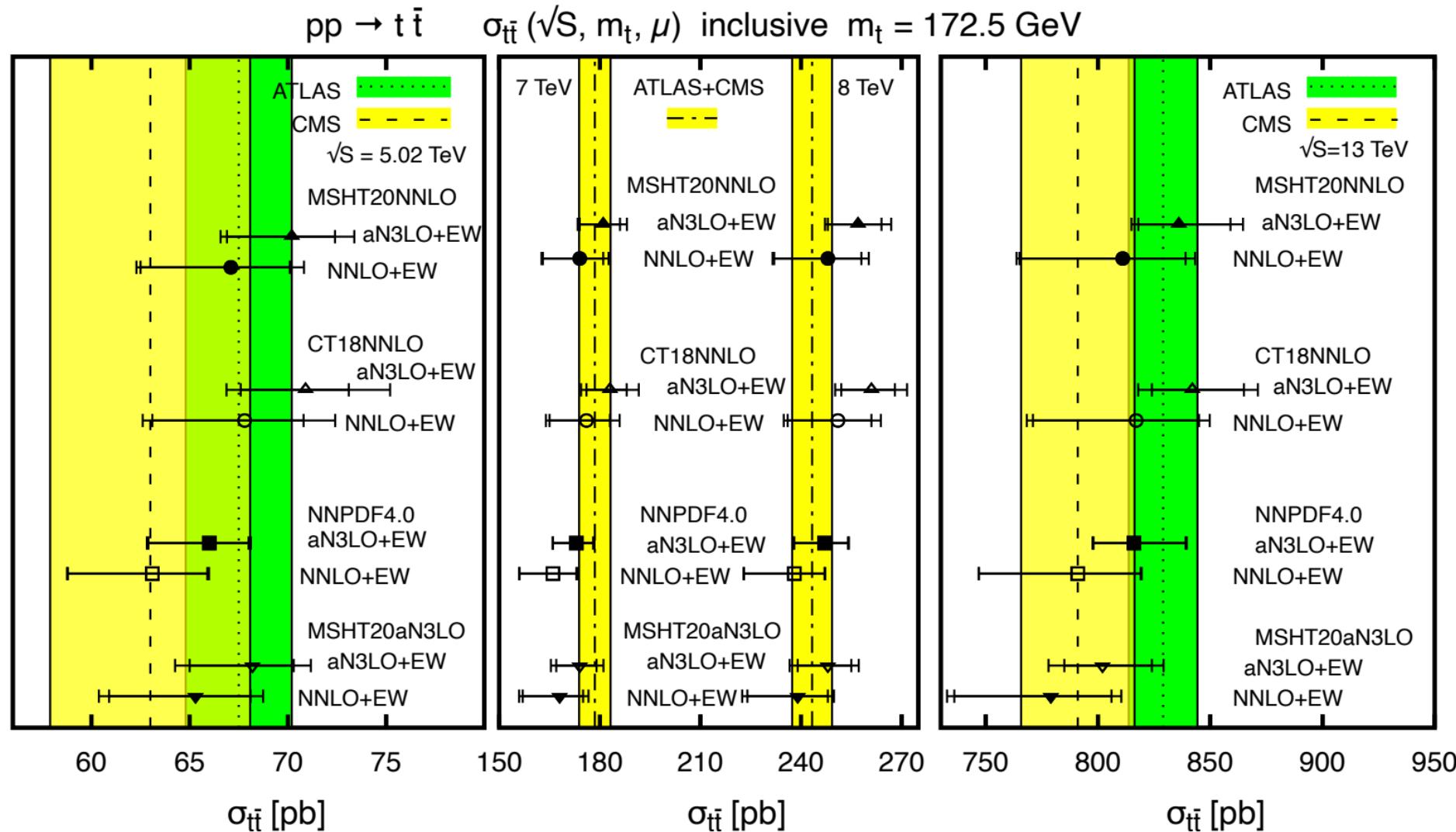
The inverse transform at fixed perturbative order, the soft-gluon corrections take the form of plus distributions of logs of s4

$$\begin{aligned}
\frac{d^2 \sigma_{ij \rightarrow t\bar{t}}^{(3)}}{dt_1 du_1} = & \left( \frac{\alpha_s}{\pi} \right)^5 \left\{ D_{ij}^{(5)} \left[ \frac{\ln^5(s_4/m_t^2)}{s_4} \right]_+ + D_{ij}^{(4)} \left[ \frac{\ln^4(s_4/m_t^2)}{s_4} \right]_+ + D_{ij}^{(3)} \left[ \frac{\ln^3(s_4/m_t^2)}{s_4} \right]_+ \right. \\
& + D_{ij}^{(2)} \left[ \frac{\ln^2(s_4/m_t^2)}{s_4} \right]_+ + D_{ij}^{(1)} \left[ \frac{\ln(s_4/m_t^2)}{s_4} \right]_+ + D_{ij}^{(0)} \left[ \frac{1}{s_4} \right]_+ + R_3 \delta(s_4) \Big\} + ...
\end{aligned}$$

which is matched to the fixed order NNLO calculation.

# $t\bar{t}$ total cross section at aN<sup>3</sup>LO

Kidonakis, MG, Tonero, 2306.06166, PRD 2023

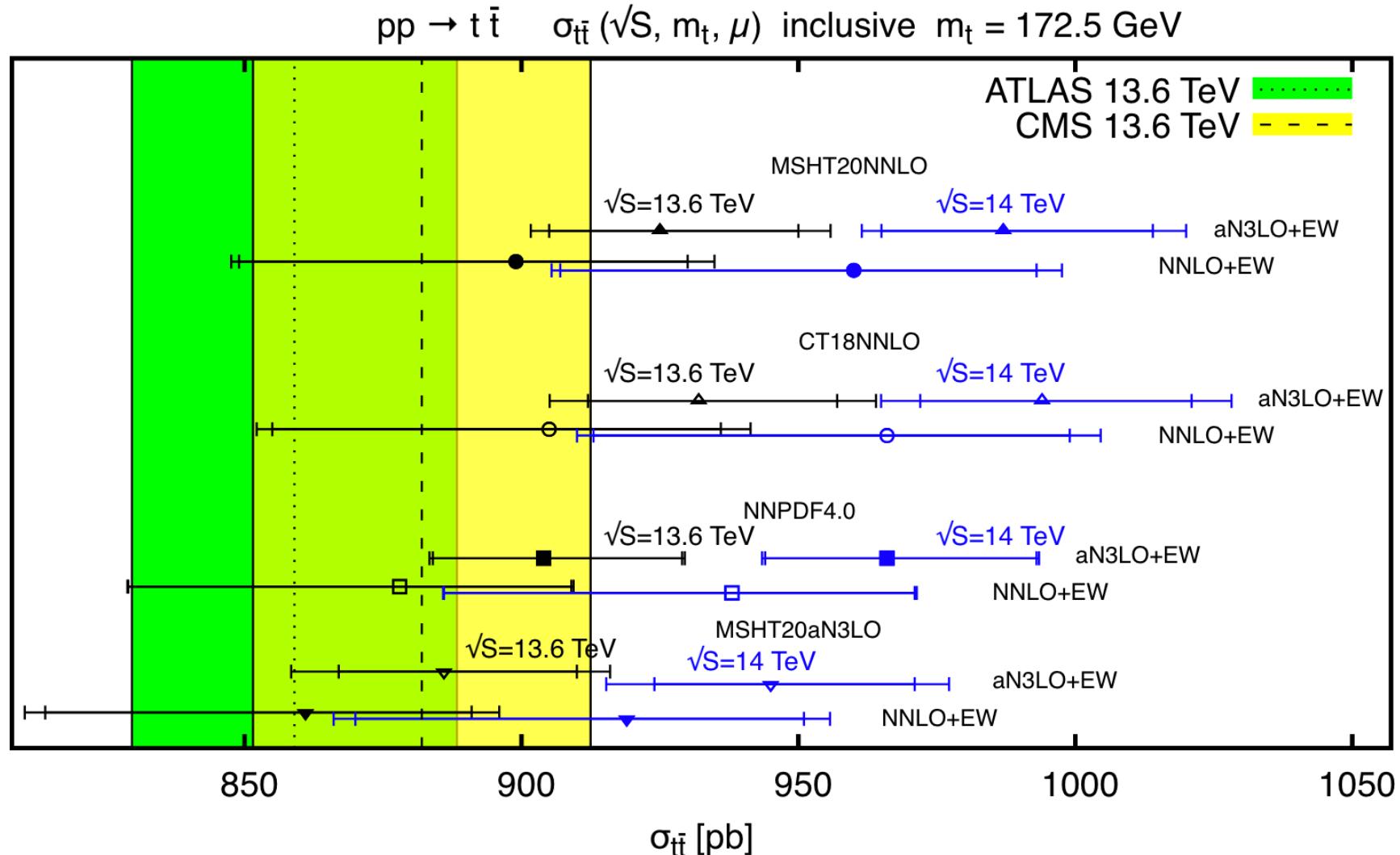


The results at NNLO QCD are calculated using Top++2.0 ([Czakon and Mitov CPC \(2014\)](#)).

NLO QCD+EW -> MadGraph5 aMC@NLO ([Alwall, et al. JHEP\(2014\); Frederix, Frixione, et al. JHEP \(2018\)](#))

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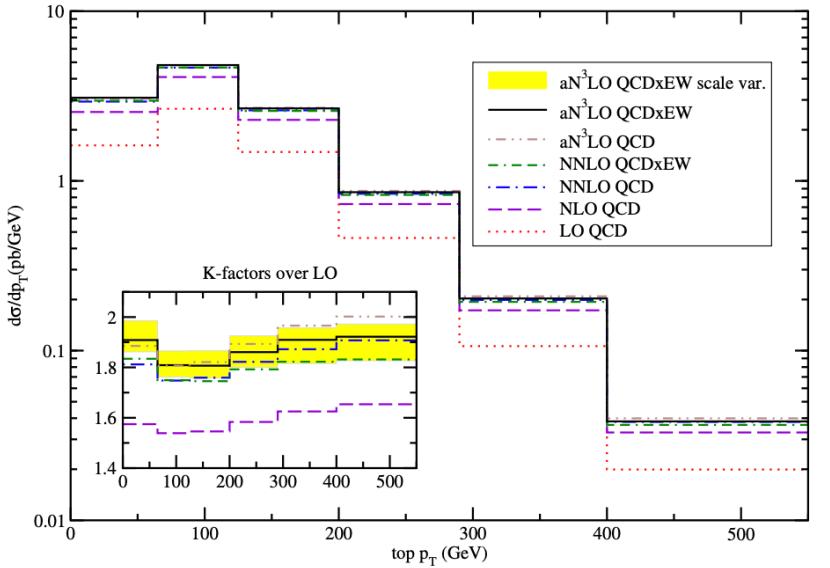


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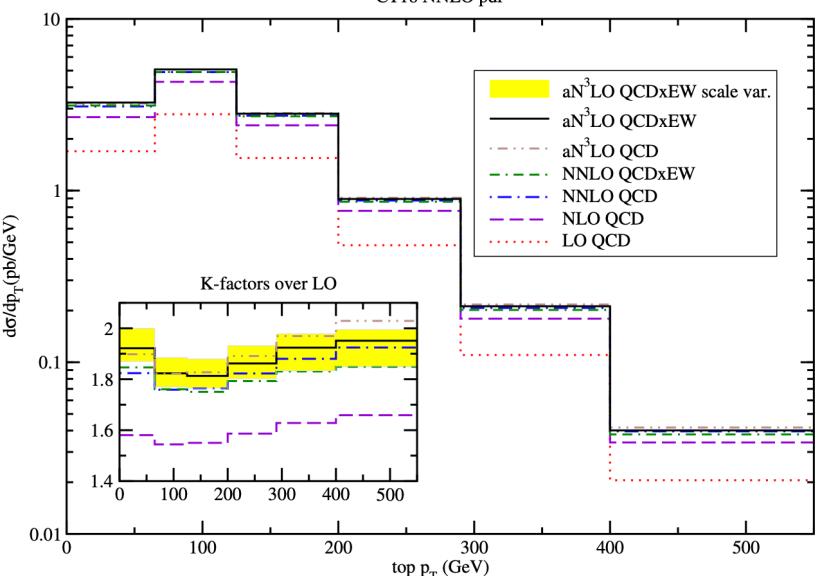
NLO QCD+EW -> MadGraph5 aMC@NLO ([Alwall, et al. JHEP\(2014\); Frederix, Frixione, et al. JHEP \(2018\)](#))

# $t\bar{t}$ production at aN<sup>3</sup>LO: top pT-distributions

p p ->  $t\bar{t}$  top p<sub>T</sub>  $\sqrt{S}=13$  TeV  $\mu=m_T$   $m_t=172.5$  GeV  
MSHT20 aN<sup>3</sup>LO pdf

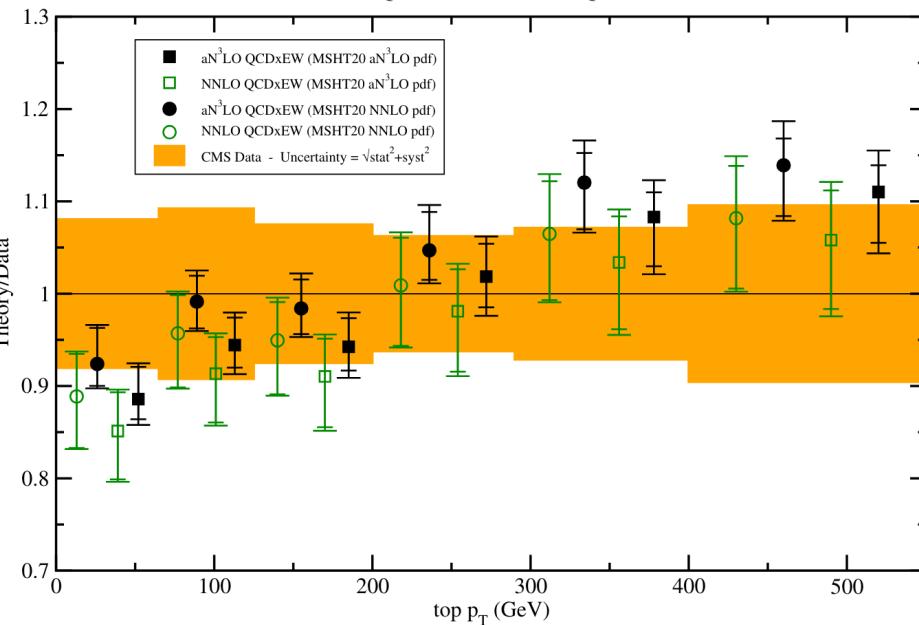


p p ->  $t\bar{t}$  top p<sub>T</sub>  $\sqrt{S}=13$  TeV  $\mu=m_T$   $m_t=172.5$  GeV  
CT18 NNLO pdf

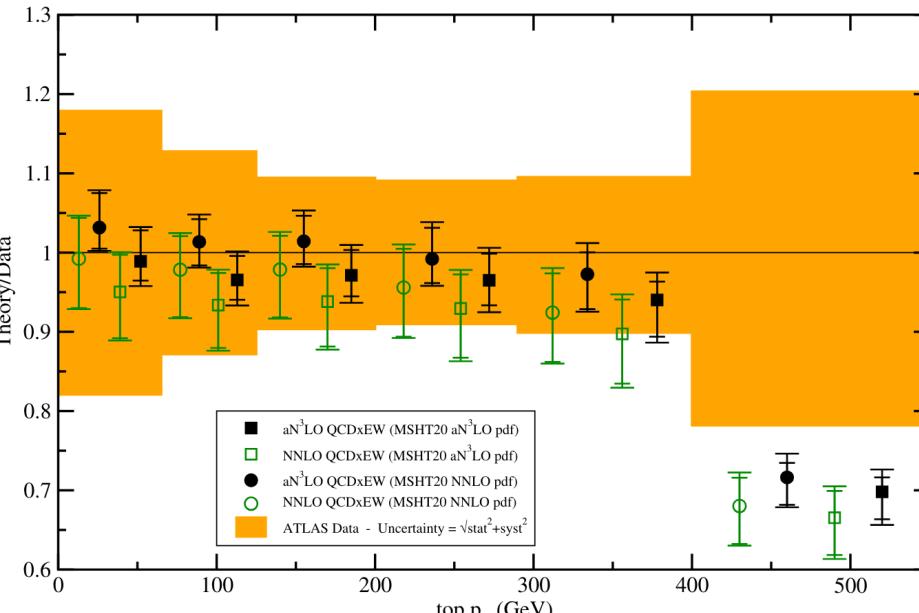


Kidonakis, MG, Tonero, 2306.06166, PRD 2023

p p ->  $t\bar{t}$  top p<sub>T</sub>  $\sqrt{S}=13$  TeV  $m_t=172.5$  GeV  
NNLO QCDxEW vs aN<sup>3</sup>LO QCDxEW



p p ->  $t\bar{t}$  top p<sub>T</sub>  $\sqrt{S}=13$  TeV  $m_t=172.5$  GeV  
NNLO QCDxEW vs aN<sup>3</sup>LO QCDxEW

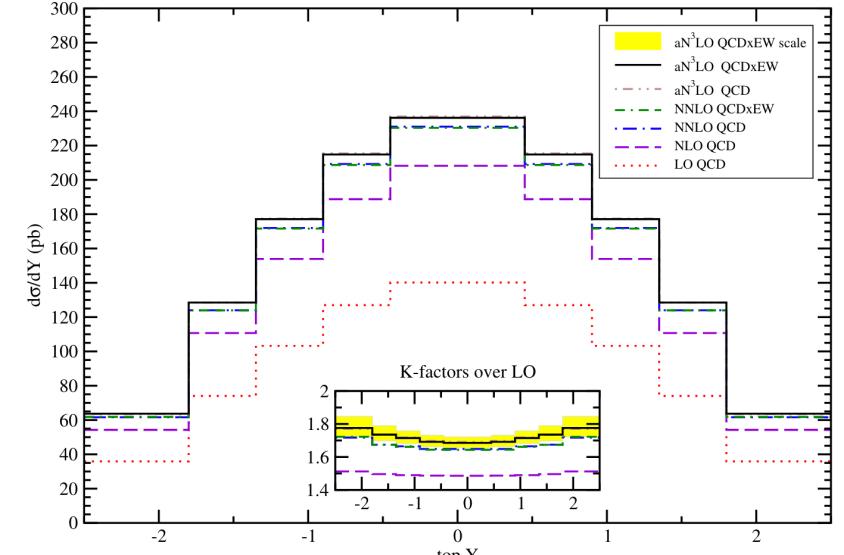


NLO EW corrections from Czakon,  
Heymes, et al. JHEP (2017)  
1705.04105.

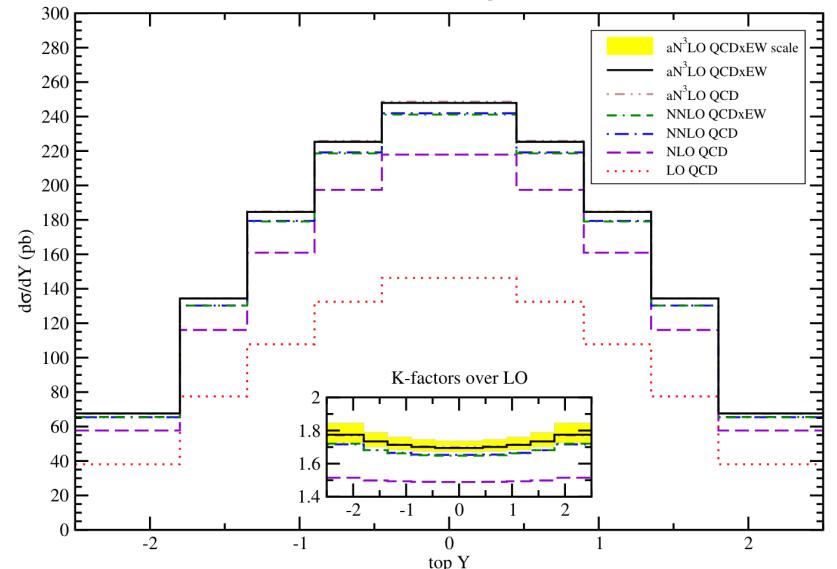
The combined QCDxEW corrections include  $\mathcal{O}(\alpha_s^2 \alpha)$  and the subleading  $\mathcal{O}(\alpha_s \alpha^2)$ ,  $\mathcal{O}(\alpha^3)$ ,  $\mathcal{O}(\alpha_s^3 \alpha)$  which are included using the multiplicative method discussed in 1705.04105

# $t\bar{t}$ production at aN<sup>3</sup>LO: top Y-distributions

p p ->  $t\bar{t}$  top rapidity  $\sqrt{S}=13$  TeV  $\mu=m_t$   $m_t=172.5$  GeV  
MSHT20 aN<sup>3</sup>LO pdf

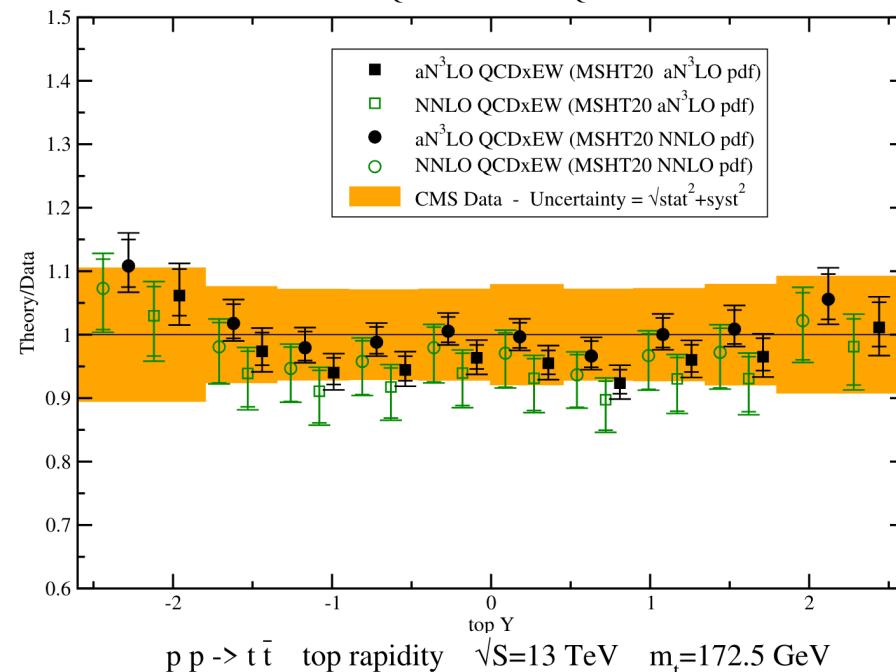


p p ->  $t\bar{t}$  top rapidity  $\sqrt{S}=13$  TeV  $\mu=m_t$   $m_t=172.5$  GeV  
CT18 NNLO pdf

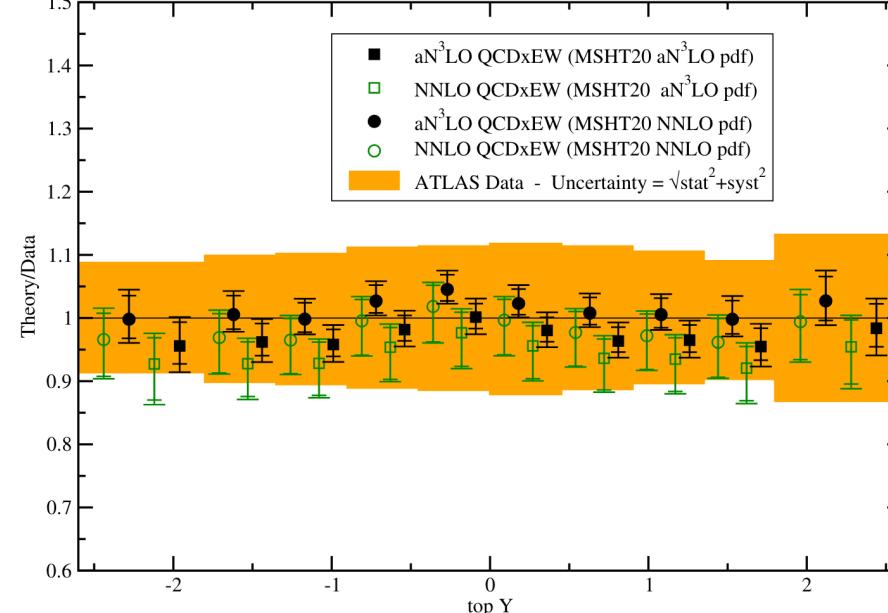


Kidonakis, MG, Tonero, 2306.06166, PRD 2023

p p ->  $t\bar{t}$  top rapidity  $\sqrt{S}=13$  TeV  $m_t=172.5$  GeV  
NNLO QCDxEW vs aN<sup>3</sup>LO QCDxEW



p p ->  $t\bar{t}$  top rapidity  $\sqrt{S}=13$  TeV  $m_t=172.5$  GeV  
NNLO QCDxEW vs aN<sup>3</sup>LO QCDxEW



NLO EW corrections from Czakon,  
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The combined QCDxEW corrections include  $\mathcal{O}(\alpha_s^2 \alpha)$  and the subleading  $\mathcal{O}(\alpha_s \alpha^2)$ ,  $\mathcal{O}(\alpha^3)$ ,  $\mathcal{O}(\alpha_s^3 \alpha)$  which are included using the multiplicative method discussed in 1705.04105

# Summary

- First comprehensive study on the impact of LHC 13TeV  $t\bar{t}$  data on CT PDFs
- Identified two optimal data selections: both have mild impact.
- Interplay between jets and  $t\bar{t}$ : jets still place stronger constraints on  $g(x)$
- $t\bar{t}$  13 TeV data prefer a softer gluon at large  $x$ , similar to the LHC jet data.
- Explored the impact of radiative corrections beyond NNLO using soft gluon resummation for the  $t\bar{t}$  Xsec and 1D distributions theory.
- Explored the impact of EW corrections as well.
- QCD Corrections substantially increase the rates for  $\sigma_{t\bar{t}}$ ,  $pT,t$  and  $Y_t$
- EW corrections important at large  $pT,t$

# BACK UP

# The CT18 analysis

## New CTEQ global analysis of quantum chromodynamics with high-precision data from the LHC

Tie-Jiun Hou,<sup>1,†</sup> Jun Gao,<sup>2</sup> T. J. Hobbs,<sup>3,4</sup> Keping Xie,<sup>3,5</sup> Sayipjamal Dulat,<sup>6,‡</sup> Marco Guzzi,<sup>7</sup> Joey Huston,<sup>8</sup> Pavel Nadolsky,<sup>9,§</sup> Jon Pumplin,<sup>8,\*</sup> Carl Schmidt,<sup>8</sup> Ibrahim Sitiwaldi,<sup>6</sup> Daniel Stump,<sup>8</sup> and C.-P. Yuan<sup>8,||</sup>

TABLE I. Datasets included in the CT18(Z) NNLO global analyses. Here we directly compare the quality of fit found for CT18 NNLO vs CT18Z NNLO on the basis of  $\chi_E^2$ ,  $\chi_E^2/N_{pt,E}$ , and  $S_E$ , in which  $N_{pt,E}$ ,  $\chi_E^2$  are the number of points and value of  $\chi^2$  for experiment  $E$  at the global minimum.  $S_E$  is the effective Gaussian parameter [38,42,56] quantifying agreement with each experiment. The ATLAS 7 TeV 35 pb<sup>-1</sup>  $W/Z$  dataset, marked by ‡, is replaced by the updated one (4.6 fb<sup>-1</sup>) in the CT18A and CT18Z fits. The CDHSW data, labeled by †, are not included in the CT18Z fit. The numbers in parentheses are for the CT18Z NNLO fit.

Exp. ID#	Experimental dataset	$N_{pt,E}$	$\chi_E^2$	$\chi_E^2/N_{pt,E}$	$S_E$
160	HERA I + II 1 fb <sup>-1</sup> , H1 and ZEUS NC and CC $e^\pm p$ reduced cross sec. comb.	[30]	1120	1408 (1378)	1.3 (1.2) 5.7 (5.1)
101	BCDMS $F_2^p$	[57]	337	374 (384)	1.1 (1.1) 1.4 (1.8)
102	BCDMS $F_2^d$	[58]	250	280 (287)	1.1 (1.1) 1.3 (1.6)
104	NMC $F_2^d/F_2^p$	[59]	123	126 (116)	1.0 (0.9) 0.2 (-0.4)
108†	CDHSW $F_2^p$	[60]	85	85.6 (86.8)	1.0 (1.0) 0.1 (0.2)
109†	CDHSW $x_B F_3^p$	[60]	96	86.5 (85.6)	0.9 (0.9) -0.7 (-0.7)
110	CCFR $F_2^p$	[61]	69	78.8 (76.0)	1.1 (1.1) 0.9 (0.6)
111	CCFR $x_B F_3^p$	[62]	86	33.8 (31.4)	0.4 (0.4) -5.2 (-5.6)
124	NuTeV $\nu\mu\mu$ SIDIS	[63]	38	18.5 (30.3)	0.5 (0.8) -2.7 (-0.9)
125	NuTeV $\bar{\nu}\mu\mu$ SIDIS	[63]	33	38.5 (56.7)	1.2 (1.7) 0.7 (2.5)
126	CCFR $\nu\mu\mu$ SIDIS	[64]	40	29.9 (35.0)	0.7 (0.9) -1.1 (-0.5)
127	CCFR $\bar{\nu}\mu\mu$ SIDIS	[64]	38	19.8 (18.7)	0.5 (0.5) -2.5 (-2.7)
145	H1 $\sigma_r^p$	[65]	10	6.8 (7.0)	0.7 (0.7) -0.6 (-0.6)
147	Combined HERA charm production	[66]	47	58.3 (56.4)	1.2 (1.2) 1.1 (1.0)
169	H1 $F_L$	[33]	9	17.0 (15.4)	1.9 (1.7) 1.7 (1.4)
201	E605 Drell-Yan process	[67]	119	103.4 (102.4)	0.9 (0.9) -1.0 (-1.1)
203	E866 Drell-Yan process $\sigma_{pd}/(2\sigma_{pp})$	[68]	15	16.1 (17.9)	1.1 (1.2) 0.3 (0.6)
204	E866 Drell-Yan process $Q^3 d^2\sigma_{pp}/(dQ dx_F)$	[69]	184	244 (240)	1.3 (1.3) 2.9 (2.7)
225	CDF run-1 lepton $A_{ch}$ , $p_{T\ell} > 25$ GeV	[70]	11	9.0 (9.3)	0.8 (0.8) -0.3 (-0.2)
227	CDF run-2 electron $A_{ch}$ , $p_{T\ell} > 25$ GeV	[71]	11	13.5 (13.4)	1.2 (1.2) 0.6 (0.6)
234	DØ run-2 muon $A_{ch}$ , $p_{T\ell} > 20$ GeV	[72]	9	9.1 (9.0)	1.0 (1.0) 0.2 (0.1)
260	DØ run-2 $Z$ rapidity	[73]	28	16.9 (18.7)	0.6 (0.7) -1.7 (-1.3)
261	CDF run-2 $Z$ rapidity	[74]	29	48.7 (61.1)	1.7 (2.1) 2.2 (3.3)
266	CMS 7 TeV 4.7 fb <sup>-1</sup> , muon $A_{ch}$ , $p_{T\ell} > 35$ GeV	[75]	11	7.9 (12.2)	0.7 (1.1) -0.6 (0.4)
267	CMS 7 TeV 840 pb <sup>-1</sup> , electron $A_{ch}$ , $p_{T\ell} > 35$ GeV	[76]	11	4.6 (5.5)	0.4 (0.5) -1.6 (-1.3)
268‡	ATLAS 7 TeV 35 pb <sup>-1</sup> $W/Z$ cross sec., $A_{ch}$	[77]	41	44.4 (50.6)	1.1 (1.2) 0.4 (1.1)
281	DØ run-2 9.7 fb <sup>-1</sup> electron $A_{ch}$ , $p_{T\ell} > 25$ GeV	[78]	13	22.8 (20.5)	1.8 (1.6) 1.7 (1.4)
504	CDF run-2 inclusive jet production	[79]	72	122 (117)	1.7 (1.6) 3.5 (3.2)
514	DØ run-2 inclusive jet production	[80]	110	113.8 (115.2)	1.0 (1.0) 0.3 (0.4)

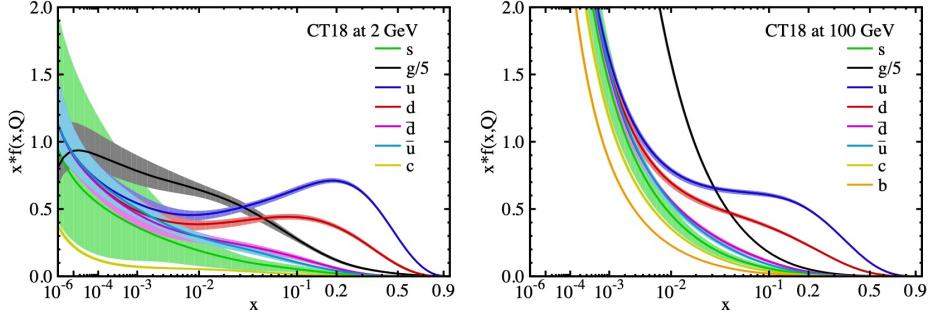


TABLE II. Like Table I, for newly included LHC measurements. The ATLAS 7 TeV  $W/Z$  data (4.6 fb<sup>-1</sup>), labeled by ‡, are included in the CT18A and CT18Z global fits, but not in CT18 and CT18Z.

Exp. ID#	Experimental dataset	$N_{pt,E}$	$\chi_E^2$	$\chi_E^2/N_{pt,E}$	$S_E$
245	LHCb 7 TeV 1.0 fb <sup>-1</sup> $W/Z$ forward rapidity cross sec.	[81]	33	53.8 (39.9)	1.6 (1.2) 2.2 (0.9)
246	LHCb 8 TeV 2.0 fb <sup>-1</sup> $Z \rightarrow e^-e^+$ forward rapidity cross sec.	[82]	17	17.7 (18.0)	1.0 (1.1) 0.2 (0.3)
248‡	ATLAS 7 TeV 4.6 fb <sup>-1</sup> , $W/Z$ combined cross sec.	[39]	34	287.3 (88.7)	8.4 (2.6) 13.7 (4.8)
249	CMS 8 TeV 18.8 fb <sup>-1</sup> muon charge asymmetry $A_{ch}$	[83]	11	11.4 (12.1)	1.0 (1.1) 0.2 (0.4)
250	LHCb 8 TeV 2.0 fb <sup>-1</sup> $W/Z$ cross sec.	[84]	34	73.7 (59.4)	2.1 (1.7) 3.7 (2.6)
253	ATLAS 8 TeV 20.3 fb <sup>-1</sup> , $Z$ $p_T$ cross sec.	[85]	27	30.2 (28.3)	1.1 (1.0) 0.5 (0.3)
542	CMS 7 TeV 5 fb <sup>-1</sup> , single incl. jet cross sec., $R = 0.7$ (extended in $y$ )	[86]	158	194.7 (188.6)	1.2 (1.2) 2.0 (1.7)
544	ATLAS 7 TeV 4.5 fb <sup>-1</sup> , single incl. jet cross sec., $R = 0.6$	[9]	140	202.7 (203.0)	1.4 (1.5) 3.3 (3.4)
545	CMS 8 TeV 19.7 fb <sup>-1</sup> , single incl. jet cross sec., $R = 0.7$ , (extended in $y$ )	[87]	185	210.3 (207.6)	1.1 (1.1) 1.3 (1.2)
573	CMS 8 TeV 19.7 fb <sup>-1</sup> , $t\bar{t}$ norm. double-diff. top $p_T$ and $y$ cross sec.	[88]	16	18.9 (19.1)	1.2 (1.2) 0.6 (0.6)
580	ATLAS 8 TeV 20.3 fb <sup>-1</sup> , $t\bar{t}$ $p_T^t$ and $m_{t\bar{t}}$ abs. spectrum	[89]	15	9.4 (10.7)	0.6 (0.7) -1.1 (-0.8)

Heavy-flavor production measurements at HERA and LHC included in the CT18 NNLO QCD global analysis.

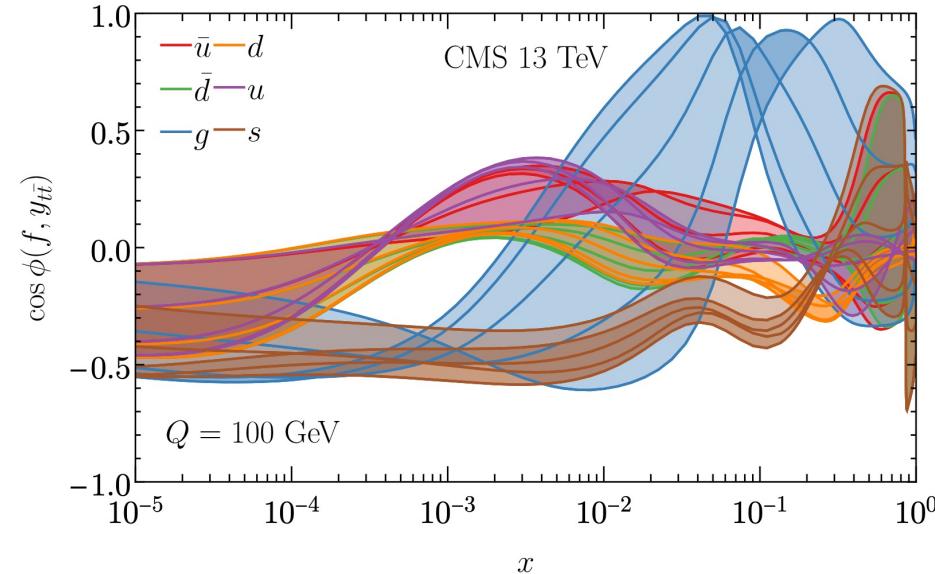
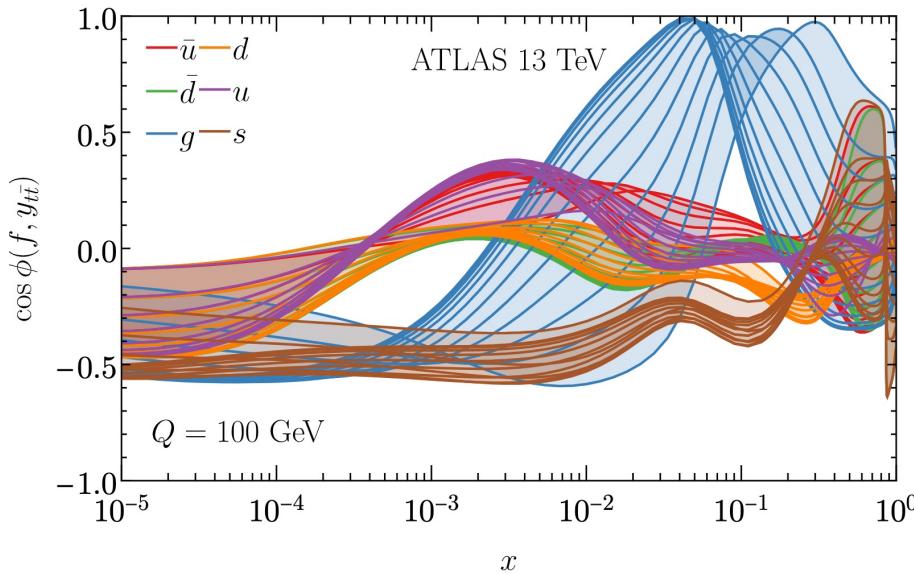
Top-quark pair production diff. Xsec. measurements at 8TeV

# What are data telling us?

- Heavy-quark production at the LHC at small  $p_T$  and large rapidity  $y$  of the heavy quark: sensitive to PDFs at both small and large  $x$  (especially true for c/b production)

$$x_{1,2} \approx \frac{\sqrt{p_T^2 + m_Q^2}}{\sqrt{S}} e^{\pm y}$$

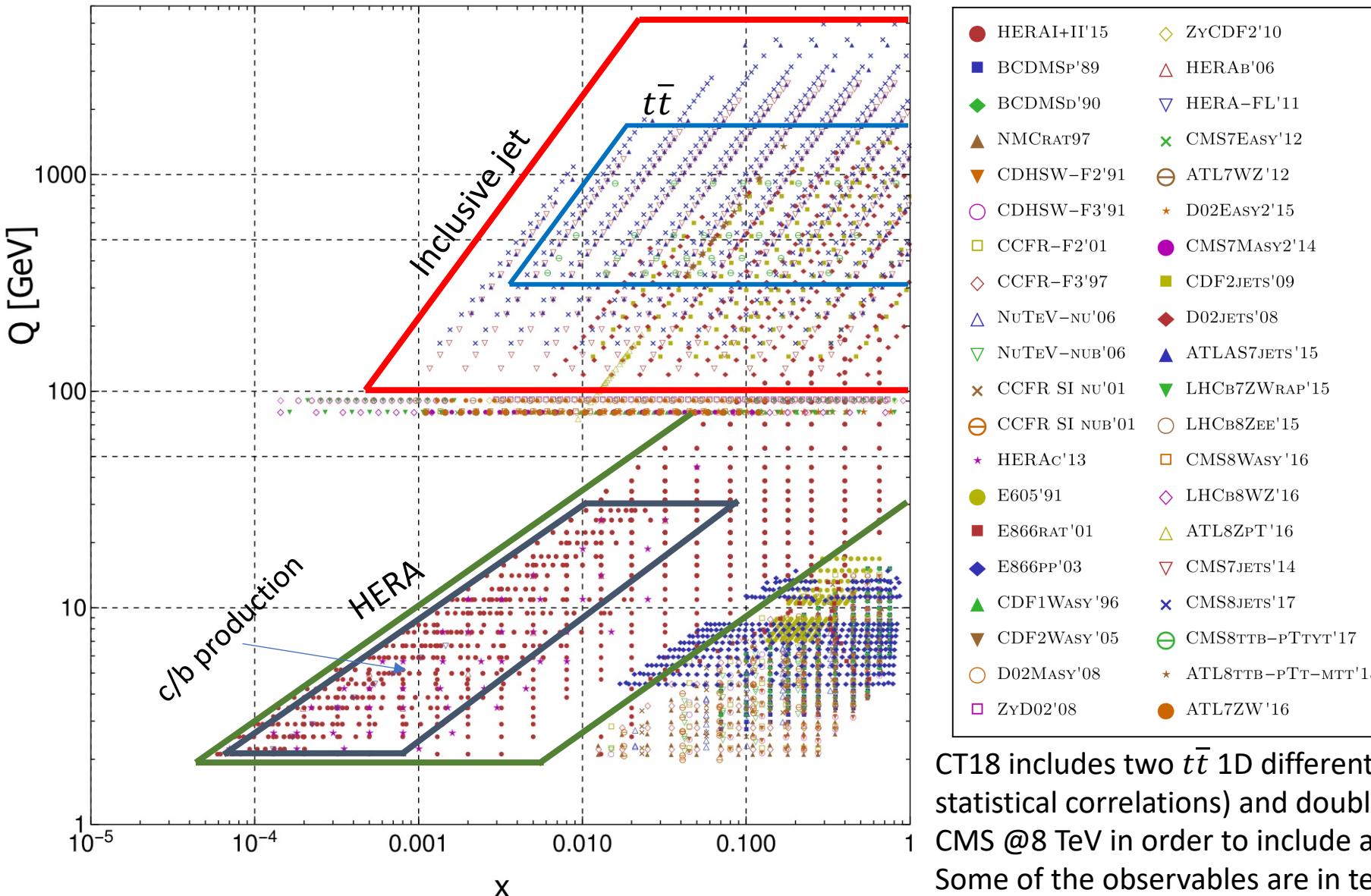
- In this kinematic region PDFs are poorly constrained by other experiments in global PDF fits.
- Top-quark pair production @LHC can already probe the gluon PDF at  $x \gtrsim 0.01$



Correlation plots with ePump for the ATLAS all-hadronic and CMS dilepton channel data

# PDF Kinematics in the $Q$ - $x$ plane

Experimental data in CT18 PDF analysis



Jet and  $t\bar{t}$  complement each other in the kinematic plane. They impact the gluon PDF at large  $x$ . Important to disentangle the effect due to jet production and top-quark data.

## Top and jet Data in CT18

Top-quark

- 1511.04716 ATLAS 8 TeV tt<sub>b</sub> ptT diff. distributions
- 1511.04716 ATLAS 8 TeV tt<sub>b</sub> mtt diff. distributions
- 1703.01630 CMS 8 TeV tt<sub>b</sub> (pT, yt) 2d diff. distrib.

Jet production

- 1406.0324 CMS incl. jet at 7 TeV with R=0.7
- 1410.8857 ATLAS incl. jet at 7 TeV with R=0.6
- 1609.05331 CMS incl. jet at 8 TeV with R=0.7

CT18 includes two  $t\bar{t}$  1D differential observables from ATLAS (using statistical correlations) and double differential measurements from CMS @8 TeV in order to include as much information as possible. Some of the observables are in tension with each other.

# Numerical values for the $t\bar{t}$ total Xsec

$t\bar{t}$ total cross sections at LHC energies with MSHT20 NNLO pdf						
$\sigma$ in pb	5.02 TeV	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
LO QCD	$40.9^{+15.5+1.2}_{-10.4-0.8}$	$105^{+37+3}_{-25-2}$	$150^{+50+4}_{-35-2}$	$487^{+142+10}_{-103-6}$	$540^{+155+10}_{-113-7}$	$576^{+163+11}_{-120-7}$
NLO QCD	$59.6^{+7.1+2.0}_{-8.1-1.2}$	$155^{+19+4}_{-20-3}$	$222^{+26+6}_{-28-4}$	$730^{+85+14}_{-86-10}$	$809^{+94+16}_{-94-11}$	$863^{+101+17}_{-99-11}$
NLO QCD+EW	$59.6^{+7.0+1.9}_{-8.1-1.2}$	$155^{+18+4}_{-20-3}$	$221^{+26+6}_{-28-3}$	$727^{+83+14}_{-85-10}$	$806^{+92+15}_{-93-11}$	$860^{+99+17}_{-99-11}$
NNLO QCD	$67.1^{+3.0+2.2}_{-4.6-1.4}$	$174^{+7+5}_{-11-3}$	$249^{+10+7}_{-16-4}$	$814^{+28+16}_{-46-11}$	$902^{+31+18}_{-50-12}$	$963^{+33+18}_{-53-13}$
NNLO QCD+EW	$67.1^{+3.0+2.2}_{-4.6-1.4}$	$174^{+7+5}_{-11-3}$	$248^{+10+7}_{-16-4}$	$811^{+28+16}_{-46-11}$	$899^{+31+18}_{-50-12}$	$960^{+33+18}_{-53-13}$
aN <sup>3</sup> LO QCD	$70.2^{+2.2+2.3}_{-3.3-1.5}$	$181^{+5+5}_{-7-3}$	$258^{+7+7}_{-9-4}$	$839^{+23+17}_{-18-11}$	$928^{+25+18}_{-20-12}$	$990^{+27+19}_{-22-13}$
aN <sup>3</sup> LO QCD+EW	$70.2^{+2.2+2.3}_{-3.3-1.5}$	$181^{+5+5}_{-7-3}$	$257^{+7+7}_{-9-4}$	$836^{+23+17}_{-18-11}$	$925^{+25+18}_{-20-12}$	$987^{+27+19}_{-22-13}$

$t\bar{t}$ total cross sections at LHC energies with MSHT20 aN <sup>3</sup> LO pdf						
$\sigma$ in pb	5.02 TeV	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
LO QCD	$40.0^{+14.9+1.1}_{-10.1-1.2}$	$103^{+35+3}_{-24-3}$	$146^{+48+3}_{-34-4}$	$469^{+133+9}_{-97-10}$	$518^{+145+10}_{-106-11}$	$553^{+153+11}_{-113-11}$
NLO QCD	$58.1^{+6.8+1.8}_{-7.8-2.0}$	$151^{+17+4}_{-20-5}$	$215^{+25+5}_{-27-6}$	$700^{+80+15}_{-80-15}$	$775^{+89+16}_{-88-16}$	$828^{+94+16}_{-94-18}$
NLO QCD+EW	$58.1^{+6.6+1.8}_{-7.8-2.0}$	$150^{+17+4}_{-19-4}$	$214^{+25+6}_{-26-6}$	$698^{+78+14}_{-80-16}$	$772^{+88+16}_{-87-16}$	$825^{+92+16}_{-93-18}$
NNLO QCD	$65.3^{+2.8+2.0}_{-4.4-2.2}$	$169^{+7+5}_{-11-5}$	$240^{+9+6}_{-15-7}$	$781^{+27+16}_{-43-17}$	$864^{+30+18}_{-47-19}$	$922^{+32+18}_{-49-20}$
NNLO QCD+EW	$65.3^{+2.8+2.0}_{-4.4-2.2}$	$168^{+7+5}_{-11-5}$	$239^{+9+6}_{-15-7}$	$779^{+27+16}_{-43-17}$	$861^{+30+18}_{-47-19}$	$919^{+32+18}_{-49-20}$
aN <sup>3</sup> LO QCD	$68.2^{+2.1+2.1}_{-3.2-2.3}$	$175^{+5+5}_{-7-5}$	$249^{+7+6}_{-9-7}$	$804^{+22+16}_{-17-17}$	$889^{+24+18}_{-19-20}$	$948^{+26+19}_{-21-21}$
aN <sup>3</sup> LO QCD+EW	$68.2^{+2.1+2.1}_{-3.2-2.3}$	$174^{+5+5}_{-7-5}$	$248^{+7+6}_{-9-7}$	$802^{+22+16}_{-17-17}$	$886^{+24+18}_{-19-20}$	$945^{+26+19}_{-21-21}$

# Numerical values for the top-pT distribution

Top-quark $p_T$ distribution at 13 TeV with MSHT20 aN <sup>3</sup> LO pdf			
$d\sigma/dp_T$ in pb/GeV	aN <sup>3</sup> LO QCD	aN <sup>3</sup> LO QCD×EW	aN <sup>3</sup> LO QCD / NNLO QCD
$0 < p_T < 65$ GeV	$3.05^{+0.12+0.06}_{-0.07-0.06}$	$3.09^{+0.12+0.06}_{-0.08-0.06}$	1.041
$65 < p_T < 125$ GeV	$4.81^{+0.15+0.09}_{-0.13-0.10}$	$4.81^{+0.15+0.10}_{-0.12-0.10}$	1.034
$125 < p_T < 200$ GeV	$2.70^{+0.09+0.05}_{-0.08-0.07}$	$2.68^{+0.08+0.05}_{-0.08-0.07}$	1.035
$200 < p_T < 290$ GeV	$0.873^{+0.031+0.021}_{-0.028-0.023}$	$0.858^{+0.030+0.021}_{-0.028-0.022}$	1.039
$290 < p_T < 400$ GeV	$0.209^{+0.005+0.006}_{-0.010-0.006}$	$0.203^{+0.005+0.006}_{-0.010-0.006}$	1.050
$400 < p_T < 550$ GeV	$0.0399^{+0.0010+0.0012}_{-0.0020-0.0013}$	$0.0383^{+0.0010+0.0012}_{-0.0019-0.0013}$	1.050

# Data description of top-pT distributions

pdf	NNLO QCD	NNLO QCD ×EW	aN <sup>3</sup> LO QCD	aN <sup>3</sup> LO QCD ×EW
MSHT20 NNLO	2.57	1.58	3.27	2.15
MSHT20 aN <sup>3</sup> LO	2.76	1.80	3.42	2.20
CT18 NNLO	2.86	1.79	3.68	2.44
NNPDF4.0 NNLO	1.56	0.91	1.92	1.09

Table 9: Summary of the  $\chi^2/N_{pt}$  for the top-quark  $p_T$  distributions at CMS.

pdf	NNLO QCD	NNLO QCD ×EW	aN <sup>3</sup> LO QCD	aN <sup>3</sup> LO QCD ×EW
MSHT20 NNLO	1.07	1.27	1.40	1.48
MSHT20 aN <sup>3</sup> LO	1.05	1.22	1.42	1.43
CT18 NNLO	1.17	1.30	1.53	1.57
NNPDF4.0 NNLO	1.18	1.58	1.32	1.62

Table 10: Summary of the  $\chi^2/N_{pt}$  for the top-quark  $p_T$  distributions at ATLAS.

# Data description of top-Y distributions

pdf	NNLO QCD	NNLO QCD ×EW	aN <sup>3</sup> LO QCD	aN <sup>3</sup> LO QCD ×EW
MSHT20 NNLO	0.71	0.76	0.66	0.70
MSHT20 aN <sup>3</sup> LO	0.85	0.91	0.79	0.83
CT18 NNLO	0.86	0.92	0.81	0.88
NNPDF4.0 NNLO	0.68	0.71	0.56	0.61

Table 15: Summary of the  $\chi^2/N_{pt}$  for the top-quark rapidity distributions at CMS.

pdf	NNLO QCD	NNLO QCD ×EW	aN <sup>3</sup> LO QCD	aN <sup>3</sup> LO QCD ×EW
MSHT20 NNLO	0.70	0.66	0.49	0.44
MSHT20 aN <sup>3</sup> LO	0.70	0.66	0.56	0.46
CT18 NNLO	0.71	0.69	0.71	0.70
NNPDF4.0 NNLO	1.26	1.18	0.90	0.84

Table 16: Summary of the  $\chi^2/N_{pt}$  for the top-quark rapidity distributions at ATLAS.