

Overview of composite Higgs models

Mikael Chala
(University of Granada)

based mostly on *1806.02836, 1812.01901, 2203.14984*
and ongoing work with **Renato Fonseca**

Disclaimer

One of the most important implications of CHMs is the presence of heavy quarks, which I will not discuss

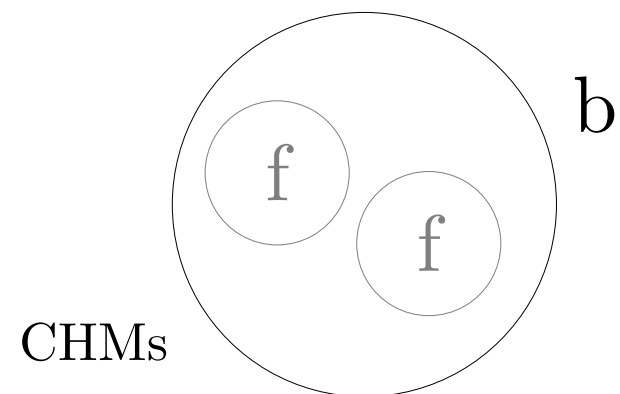
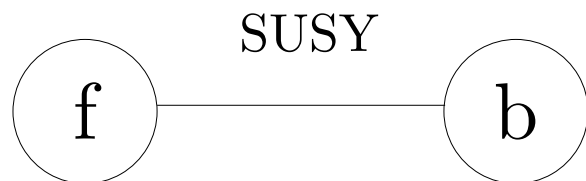
Very few studies about CHMs at e^+e^- colliders

Though not only, I will discuss mostly my own work

Motivation for CHMs

If we accept that fine-tuning is a problem (not generally accepted [Manohar '18]), then it requires a solution

CHMs relate unprotected fields (scalars) to protected ones (fermions) through compositeness



Two-flavour QCD

$$L_{\text{QCD}} = \bar{q}iDq + \dots \quad SU(2)_L \times SU(2)_R$$

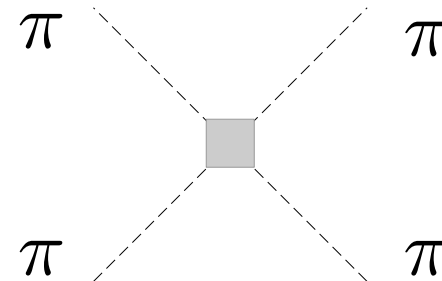


$$\langle \bar{q}_L q_R + \text{h.c.} \rangle \neq 0$$

$$SU(2)_{L+R}$$

Three NGBs (pions), much lighter than the characteristic scale f of about GeV

$$L_{\text{pions}} = \frac{1}{f^2} \partial\pi^2 \partial\pi^2 + \dots$$



CHMs

unknown Lagrangian

$\langle \text{vacuum} \rangle \neq 0$

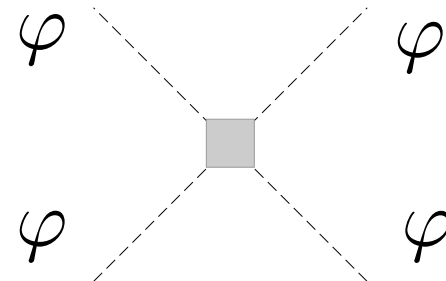
G



H

At least four NGBs (Higgs), much lighter than the characteristic scale f of TeV

$$L_{\text{NGBs}} = \frac{1}{f^2} \partial\varphi^2 \partial\varphi^2 + \dots$$



Conditions over $G \rightarrow H$

1. Custodial symmetry $SU(2) \times SU(2)$ in H
2. Higgs is a $(2, 2)$ of $SU(2) \times SU(2)$
3. There are no fractional electric charges

minimal case:

$$SO(5) \rightarrow SO(4)$$

$$\mathbf{4} = (\mathbf{2}, \mathbf{2}) = \mathbf{2}_{\frac{1}{2}} + \mathbf{2}_{-\frac{1}{2}} = (\varphi^+, \varphi^0)$$

Important results

1. **Any scalar sector** can ensue from a CHM (actually of the form $SO(n+1) \rightarrow SO(n)$)
2. The symmetry of the scalar sector can not be arbitrary
3. For a given number of NGBs, there is a **finite number of CHMs** (the “landscape”)

Landscape of CHMs with at most eight NGBs

(2, 2)

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$(2, 2) + (1, 1)$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$(2, 2) + (1, 3)$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$2 \times (2, 2)$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$(2, 2) + 2 \times (1, 1)$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$$(2, 2) + (1, 1) + (3, 1)$$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$$(2, 2) + 3 \times (1, 1)$$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

Landscape of CHMs with at most eight NGBs

$$(2, 2) + 4 \times (1, 1)$$

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

The 8 of $Sp(8)$ not a symmetry 2HDM

{S05}	{SU2, SU2}	{{2⊗2, 1}}
{SU4}	{S05}	{{1⊗1, 1}, {2⊗2, 1}}
{SU4}	{SU2, SU2, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S07}	{G2}	{{2⊗2, 1}, {3⊗1, 1}}
{S07}	{SU4}	{{1⊗1, 2}, {2⊗2, 1}}
{SP6}	{SU2, S05}	{{2⊗2, 2}}
{SP6}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, S05}	{SU2, SU2, U1}	{{1⊗1, 2}, {2⊗2, 1}}
{SU2, S05}	{SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU5}	{SU4, U1}	{{1⊗1, 0}, {2⊗2, 2}}
{S08}	{S07}	{{2⊗2, 1}, {3⊗1, 1}}
{S08}	{S07}	{{1⊗1, 3}, {2⊗2, 1}}
{S09}	{S08}	{{2⊗2, 2}}
{S09}	{S08}	{{1⊗1, 4}, {2⊗2, 1}}
{S09}	{S08}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU4}	{S05, U1}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, S07}	{SU4, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 4}, {2⊗2, 1}}
{S05, S05}	{SU2, SU2, SU2, SU2}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, S05}	{SU2, SU2, U1, U1}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{1⊗1, 3}, {2⊗2, 1}}
{SU2, SU2, S05}	{SU2, SU2, SU2}	{{2⊗2, 1}, {3⊗1, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 4}, {2⊗2, 1}}
{SU2, SU2, SU4}	{SU2, S05}	{{1⊗1, 1}, {2⊗2, 1}, {3⊗1, 1}}

(More or less) robust predictions of CHMs
(about the scalar sector)

Liu, Low, Yin '18

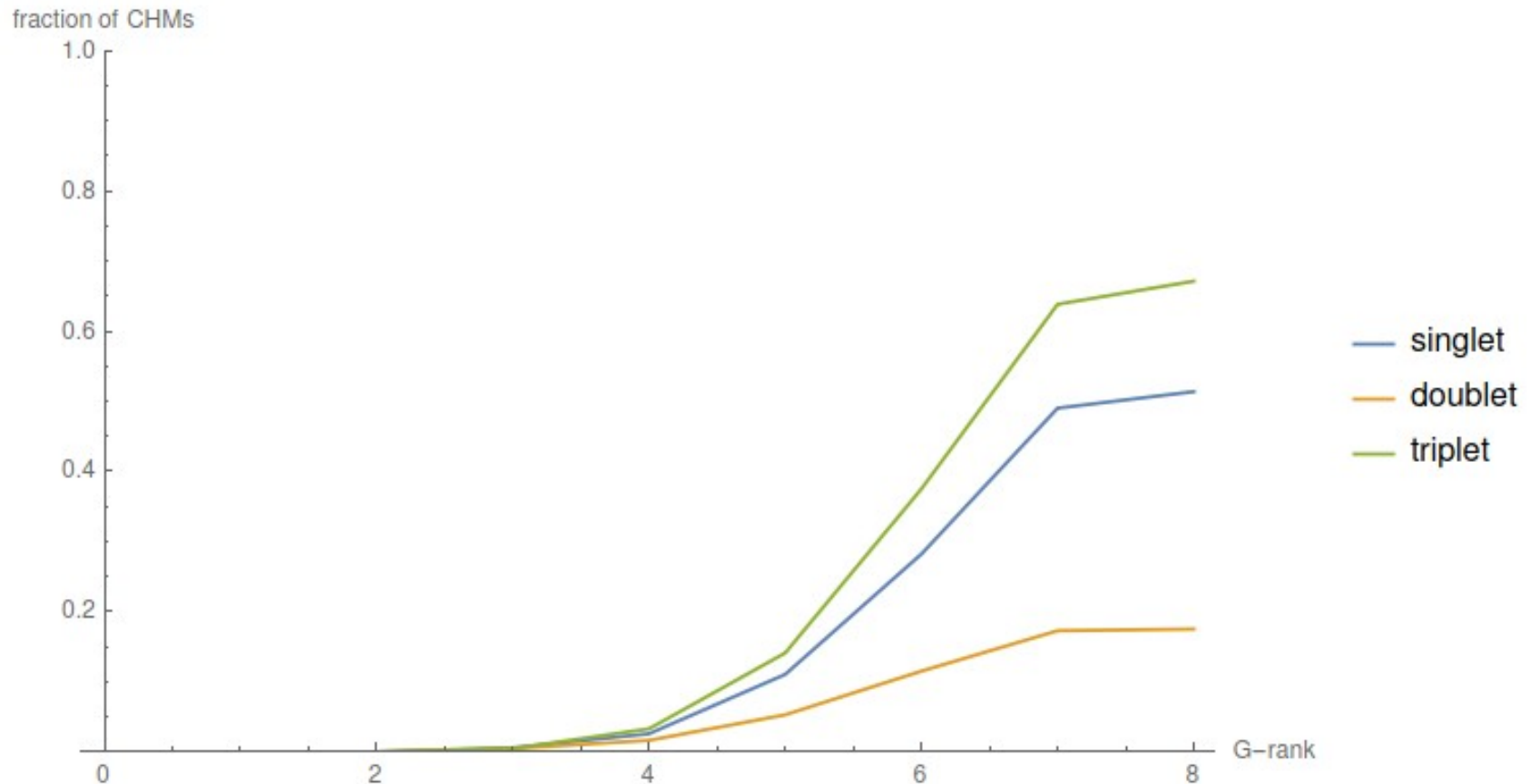
1. Effective field theory with many restrictions, e.g. $h \rightarrow h+c$. Reduced Higgs couplings

$$1 + 2\sqrt{1-\epsilon}\frac{h}{v} + (1-2\epsilon)\frac{h^2}{v^2} + \dots, \quad \epsilon < 1$$

2. **Extra scalars.** Only one minimal model, $SO(5) \rightarrow SO(4)$, “not UV completable”

Not all extra scalars equally likely

851 CHMs with at most 13 NGBs

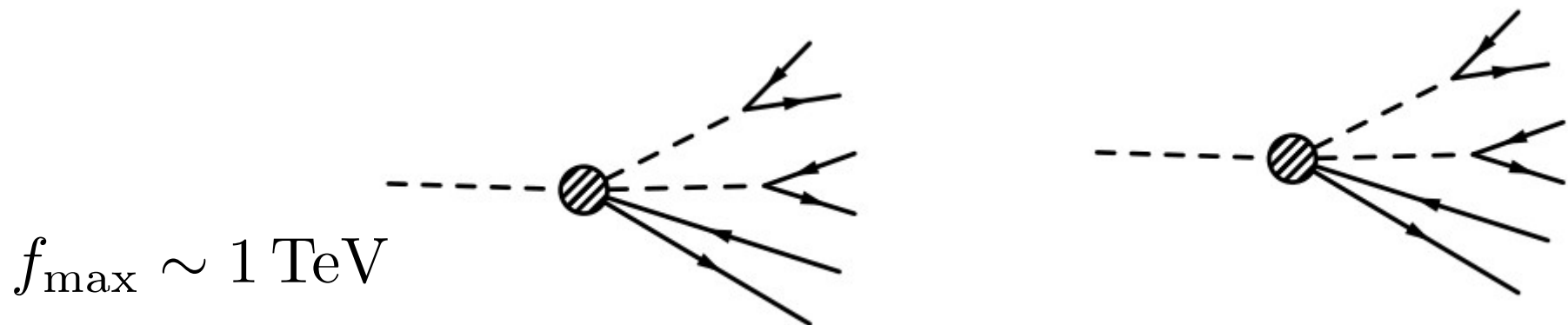
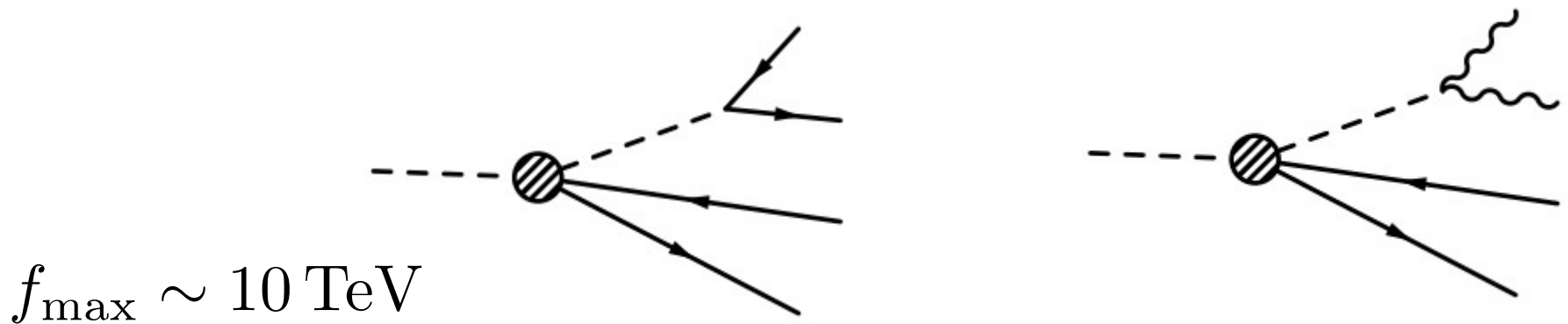


One extra singlet: $SO(6) \rightarrow SO(5)$

1. Rare Higgs decays (beyond $h \rightarrow SS$). About $O(10^6)$ Zh events at 240 GeV FCC-ee, ILC, ...

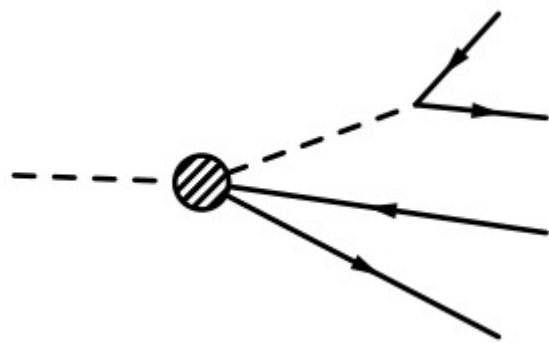
One extra singlet: $SO(6) \rightarrow SO(5)$

1. Rare Higgs decays (beyond $h \rightarrow SS$). About $O(10^6)$ Zh events at 240 GeV FCC-ee, ILC, ...

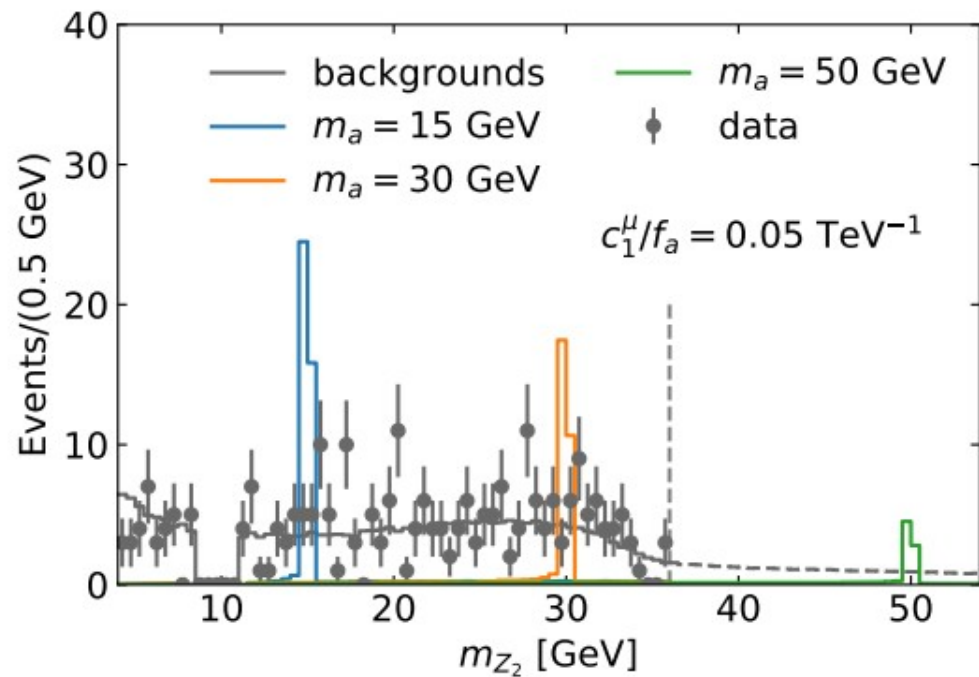


One extra singlet: $SO(6) \rightarrow SO(5)$

1. Rare Higgs decays (beyond $h \rightarrow SS$). About $O(10^6)$ Zh events at 240 GeV FCC-ee, ILC, ...



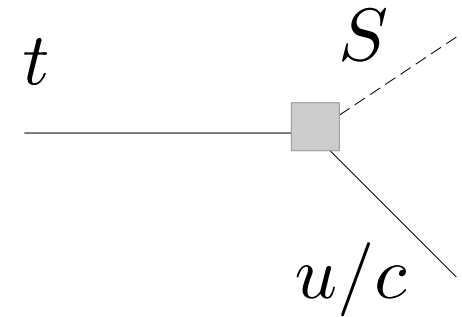
$$f_{\max} \sim 10 \text{ TeV}$$



One extra singlet: $SO(6) \rightarrow SO(5)$

2. Rare top decays. About $O(10^6)$ $t\bar{t}$ events at 350 GeV FCC-ee, ILC, ...

Supressed only by $1/f$



Higgs-mediated FCNC forbidden

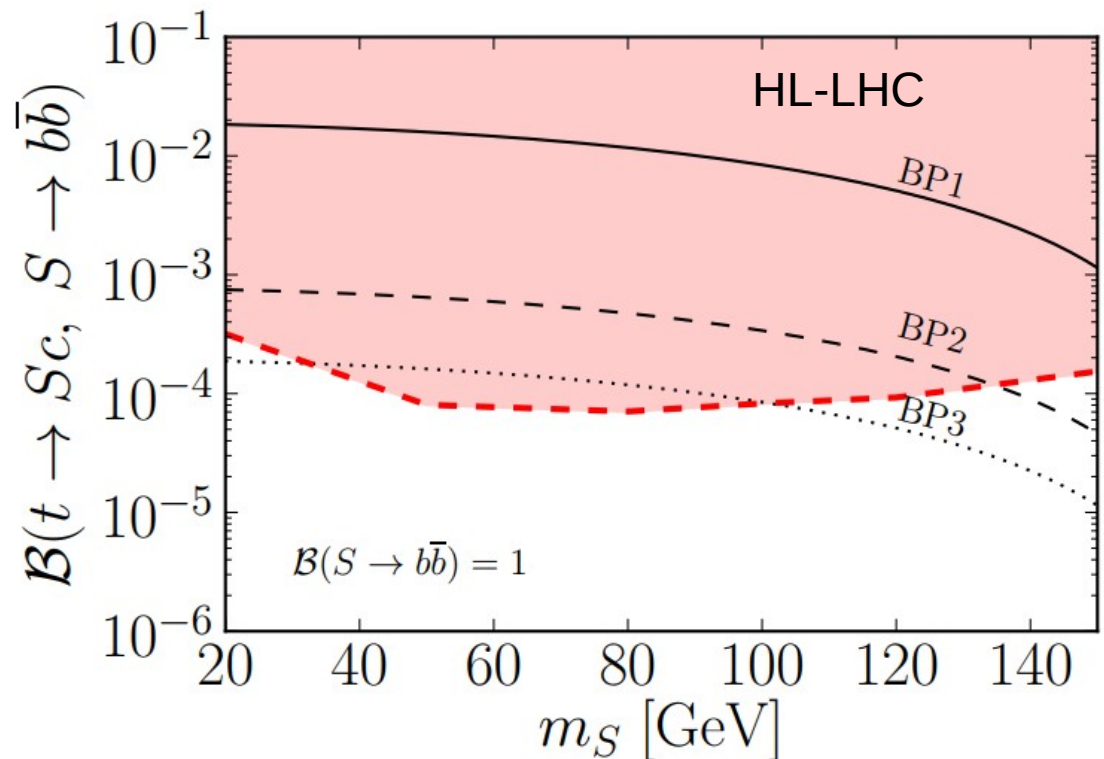
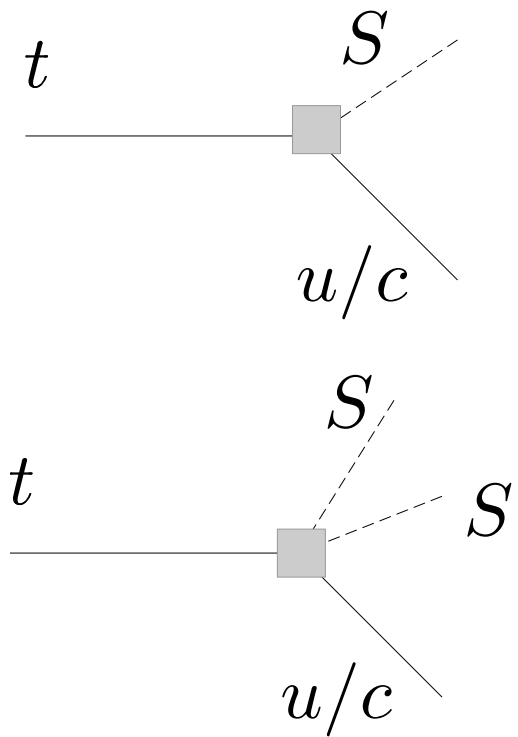
Agashe, Contino '09

In principle, S can have large decays into clean final states (leptons, photons, ...)

D^0 - \bar{D}^0 oscillations not fully constraining

One extra singlet: $SO(6) \rightarrow SO(5)$

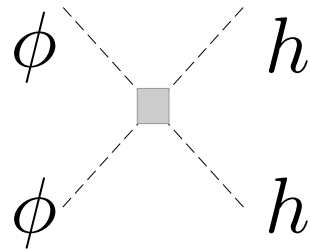
2. Rare top decays. About $O(10^6)$ $tt\bar{b}b$ events at 350 GeV FCC-ee, ILC, ...



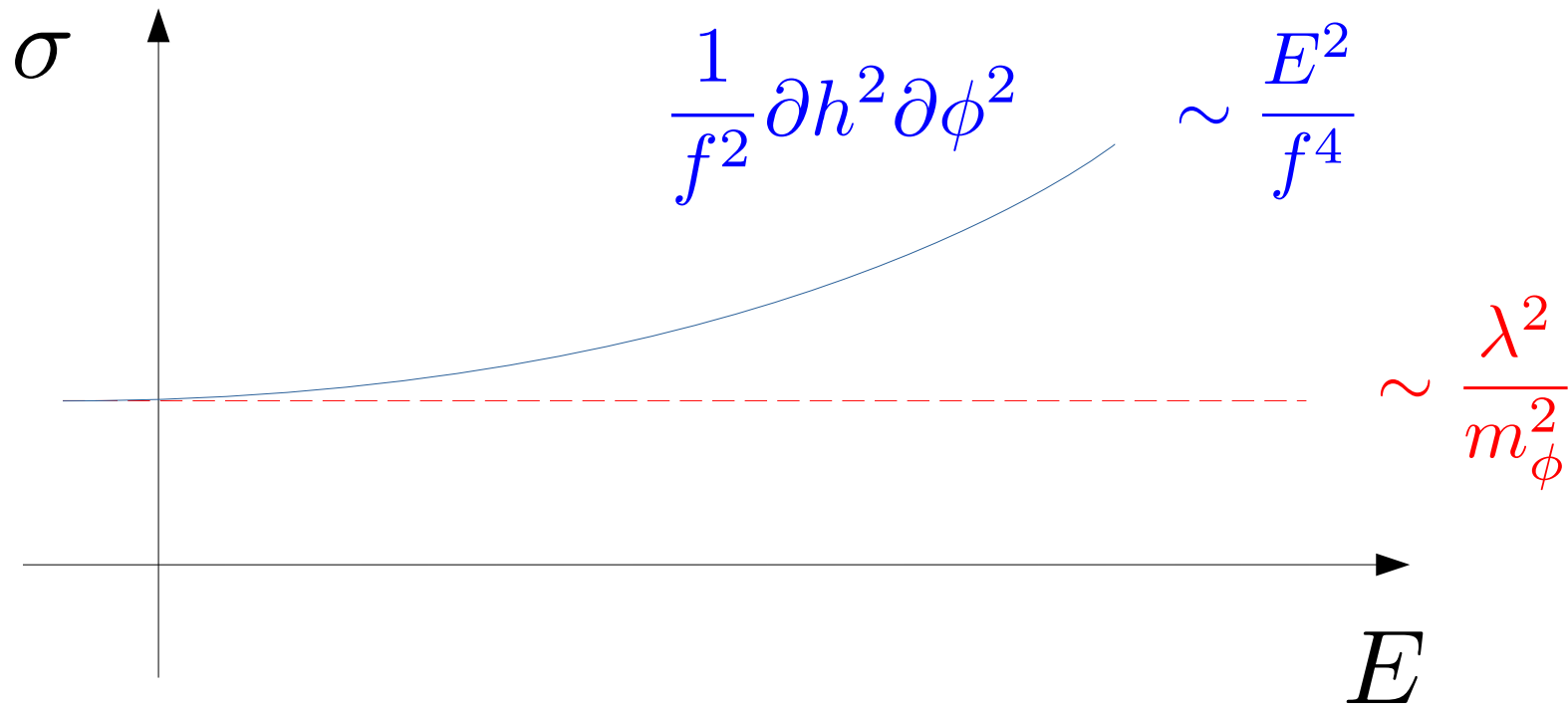
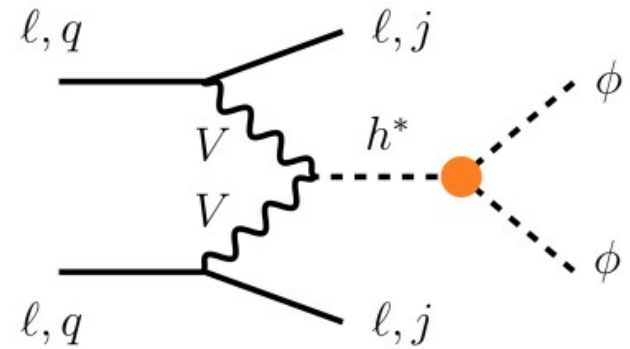
$f_{\max} \sim 100$ TeV

One extra singlet: $SO(6) \rightarrow SO(5)$

dark matter

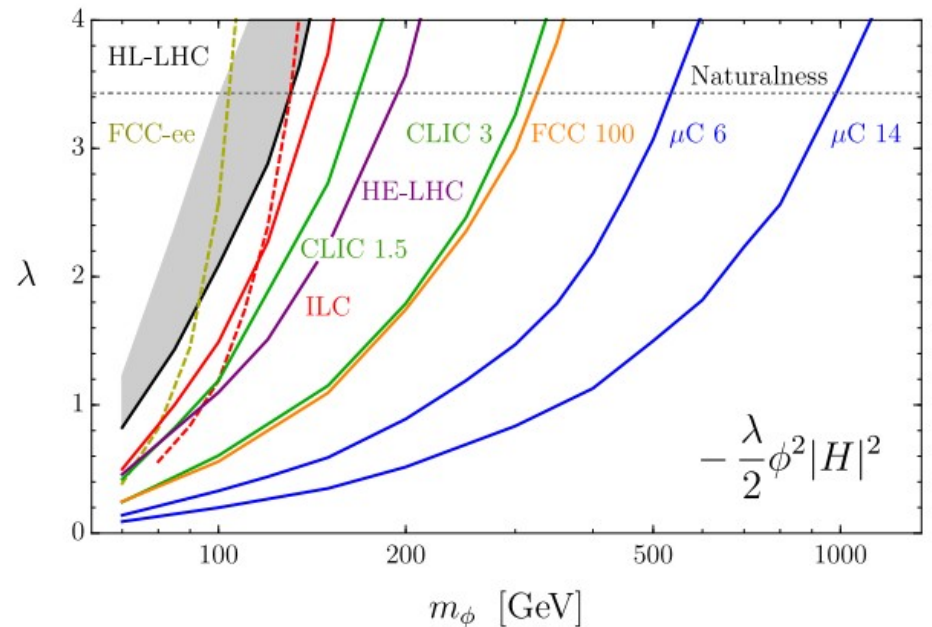
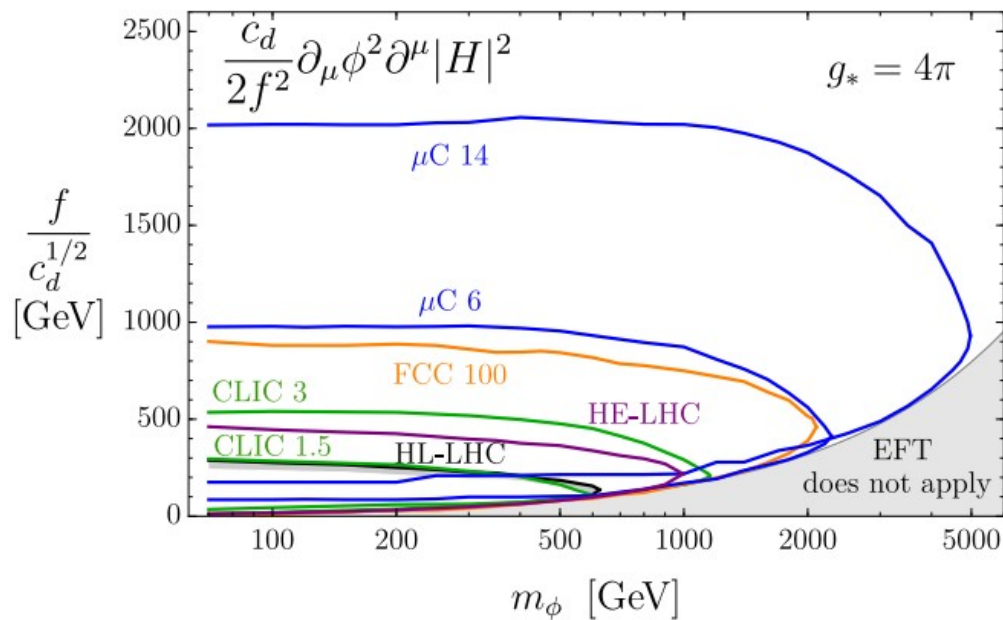
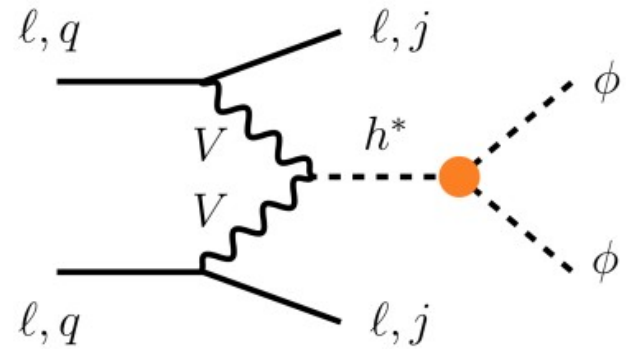


3. Off-shell Higgs portal



One extra singlet: $SO(6) \rightarrow SO(5)$

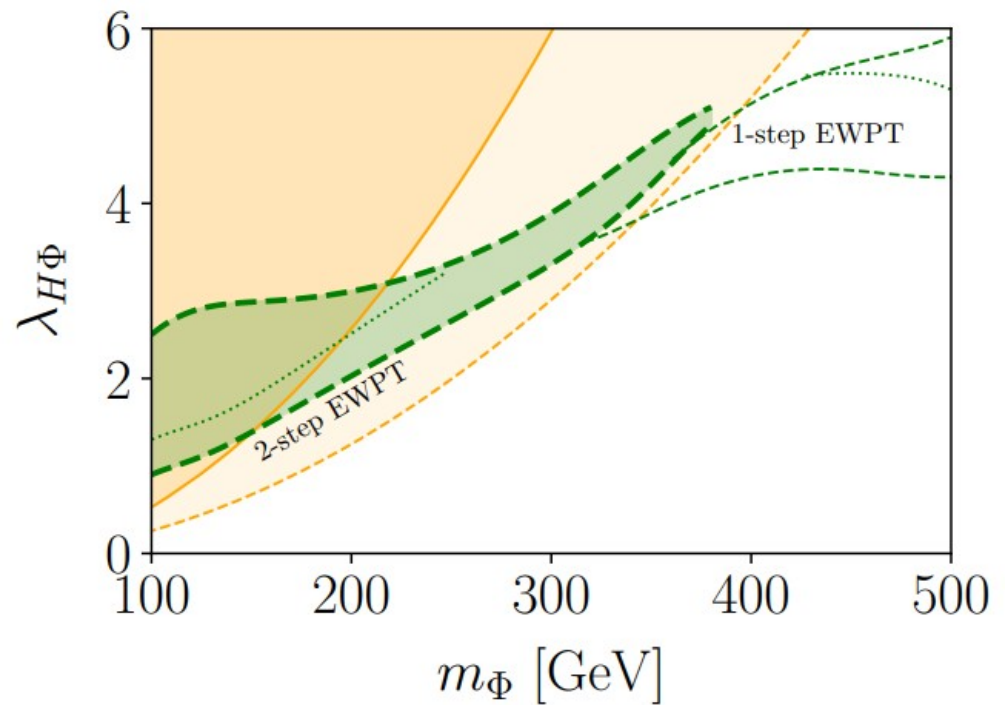
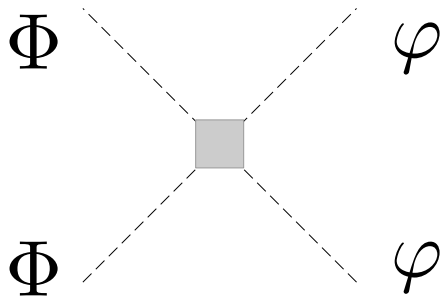
3. Off-shell Higgs portal



One extra triplet: $SO(8) \rightarrow SO(7)$

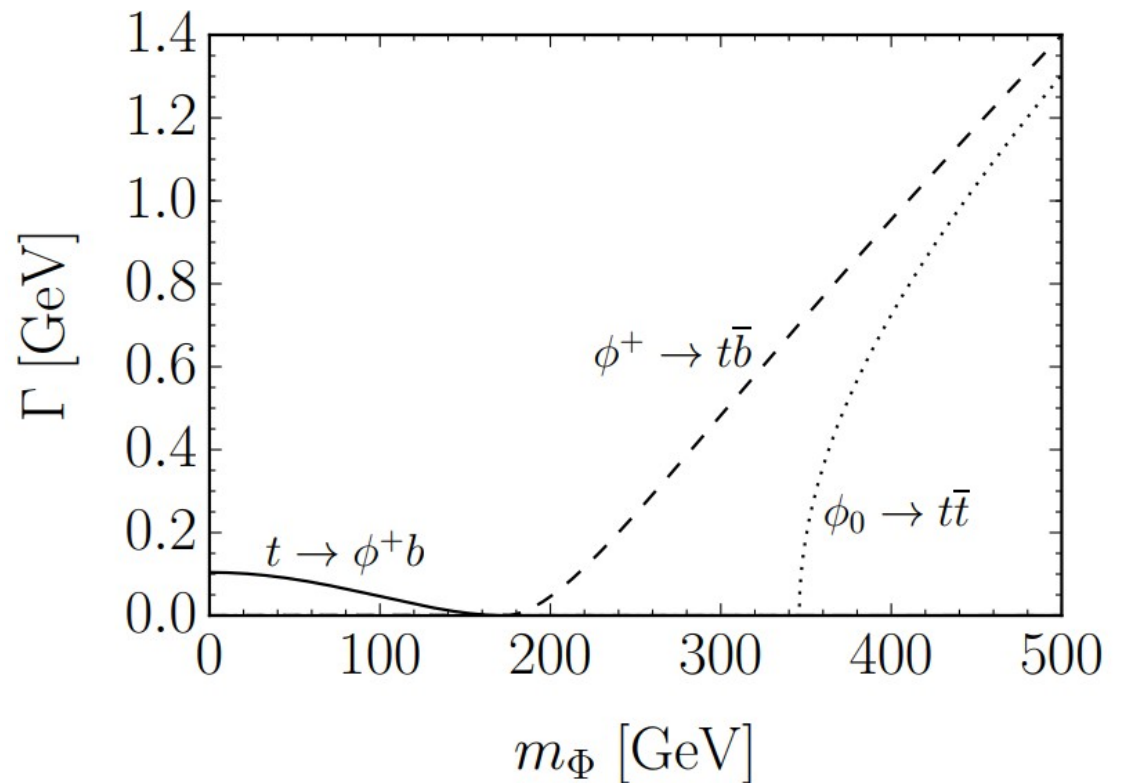
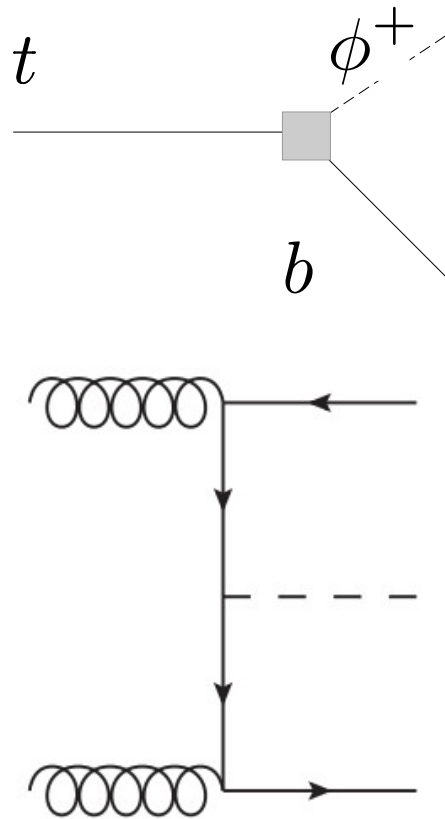
Baryogenesis occurs in the mass region 100-350 GeV

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \\ \phi^- \end{pmatrix}$$



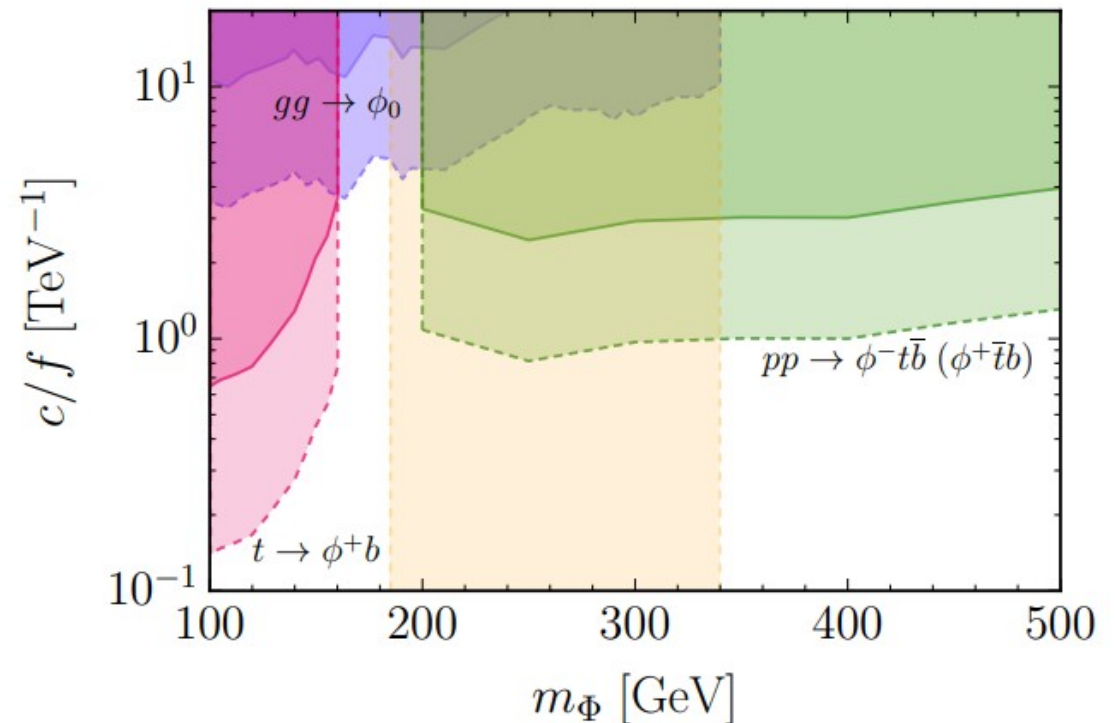
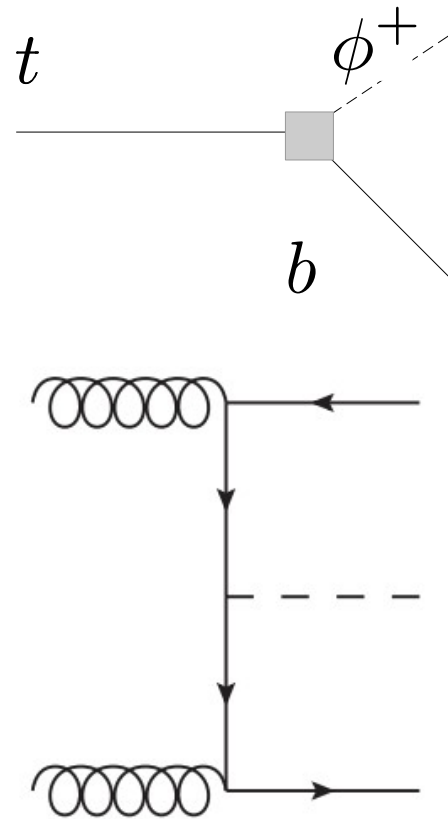
One extra triplet: $SO(8) \rightarrow SO(7)$

Rare top decays. Still mediated by effective interactions. Conserve flavor



One extra triplet: $SO(8) \rightarrow SO(7)$

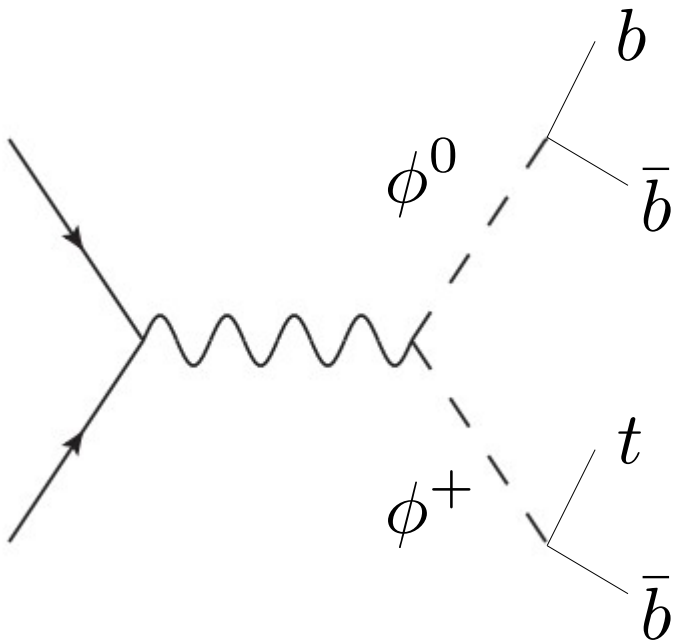
Rare top decays. Still mediated by effective interactions. Conserve flavor



One extra triplet: $SO(8) \rightarrow SO(7)$

Within this region, pair production of triplets in $3t+b$ final state (no Z exchange)

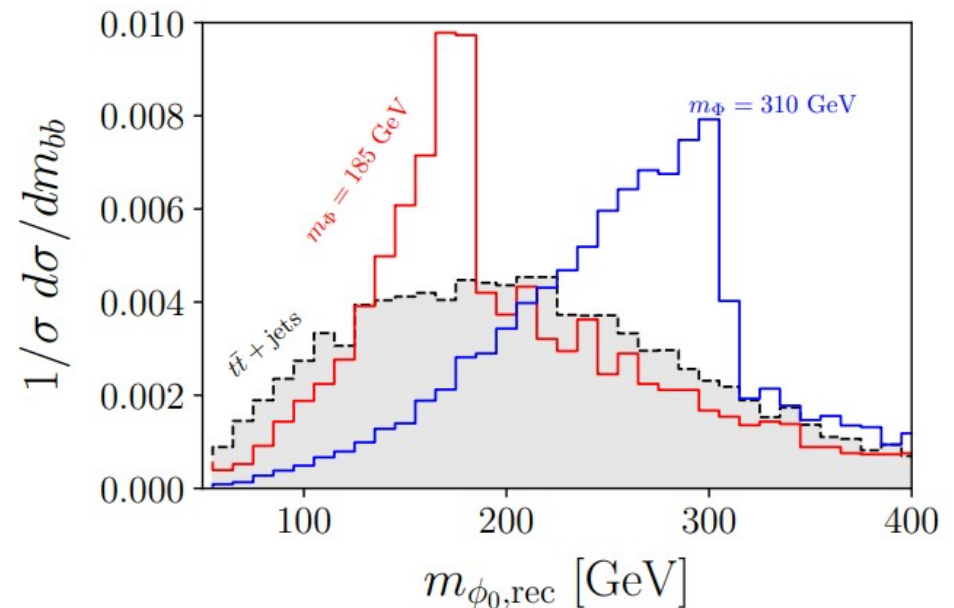
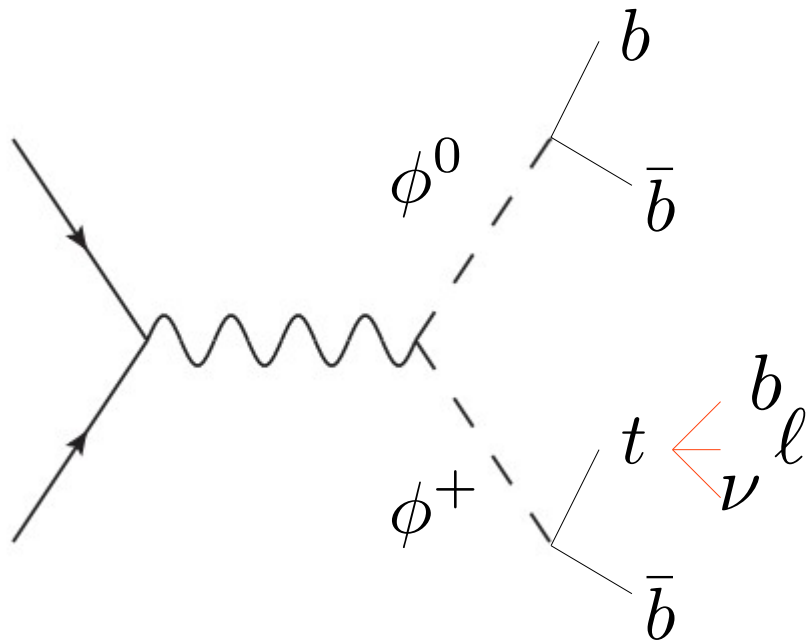
Not particularly clean at hadron colliders



One extra triplet: $SO(8) \rightarrow SO(7)$

Within this region, pair production of triplets in $3t+b$ final state (no Z exchange)

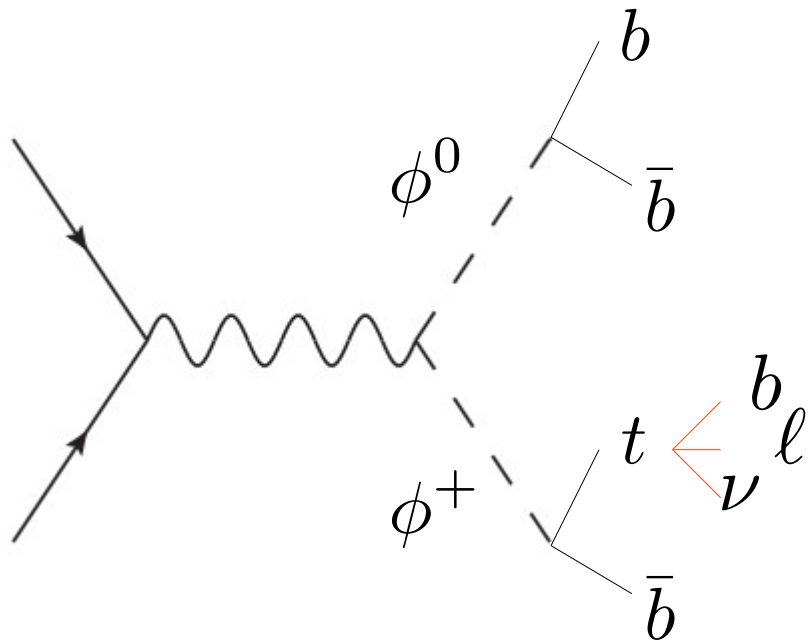
Not particularly clean at hadron colliders



One extra triplet: $SO(8) \rightarrow SO(7)$

Within this region, pair production of triplets in $3t+b$ final state (no Z exchange)

Not particularly clean at hadron colliders



final rec	signal	background	$s/\sqrt{s+b}$
$\Phi(185)$	0.39	25.6	4.2
$\Phi(235)$	0.78	33.5	7.3
$\Phi(285)$	0.41	26.5	4.3
$\Phi(335)$	0.22	19.0	2.7

Other possibilities

Precise measurements of custodial symmetry violation

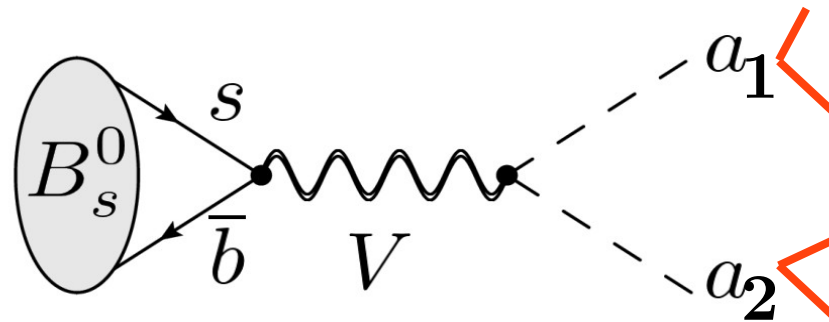
$$\rho = \frac{m_Z^2}{c_W^2 m_W^2} = 1$$

$SU(2) \times SU(2)$ symmetry guarantees this relation at tree level in renormalisable theories.

Generally, non-minimal CHMs (even 2HDMs) violate this

Other possibilities

New B-meson decays, in CHMs with several extra singlets, e.g. $SO(7)/SO(6)$



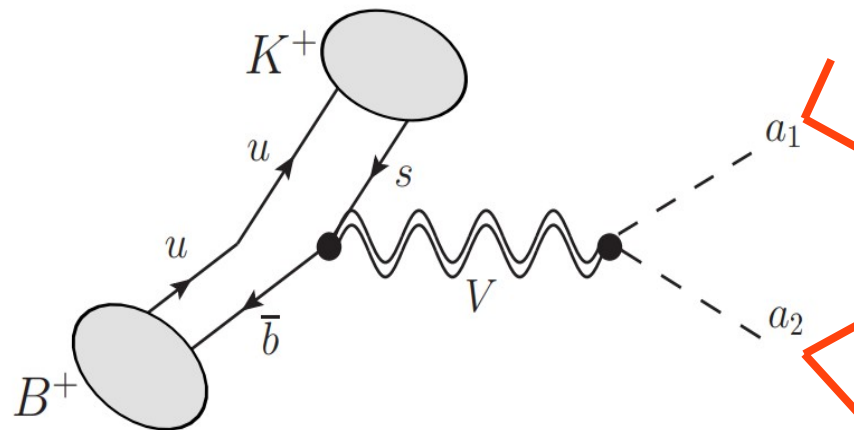
$$\Gamma = \frac{f_B^2}{16\pi m_V^4} (g_{sb}g_{12})^2 \frac{(m_1^2 - m_2^2)^2}{m_B} \mathcal{K}\left(\frac{m_1}{m_B}, \frac{m_2}{m_B}\right)$$

Other possibilities

New B-meson decays, in CHMs with several extra singlets, e.g. $SO(7)/SO(6)$

Not yet searched for. Smaller efficiency, compensated by larger cross section

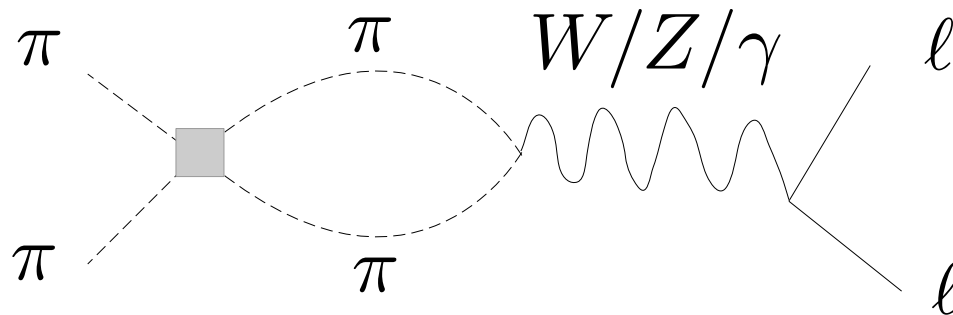
$$\mathcal{B}_{\min} \sim 10^{-11} \text{ @ ILC-250}$$



Other possibilities

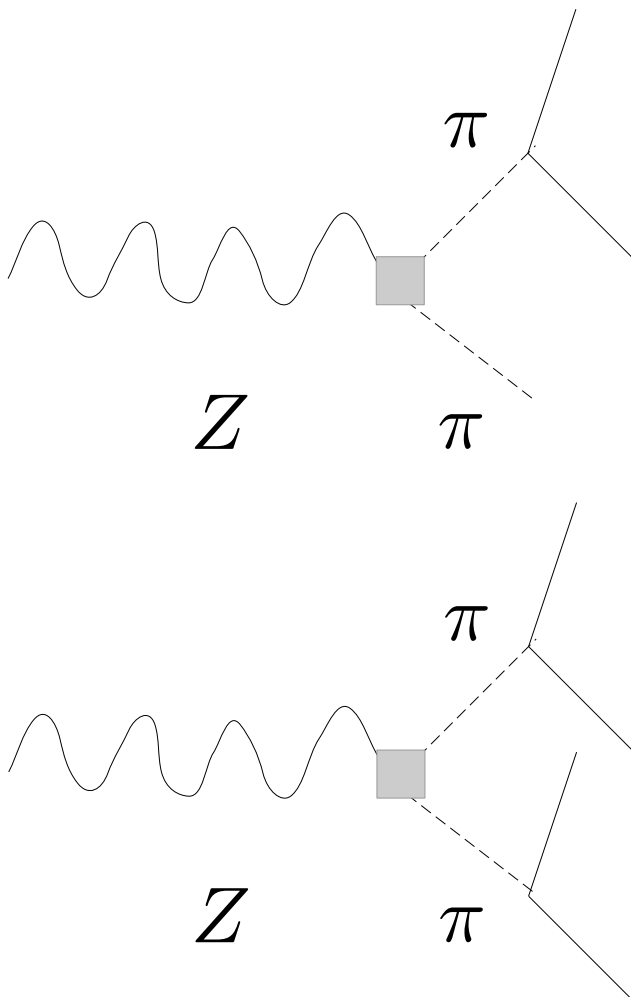
Radiative corrections to pair-production of new scalars

Fixed by coset structure. Sheds light on spontaneous-symmetry breaking



Other possibilities

Variety of (probably off-shell) Z decays



$Z \rightarrow \nu\nu\gamma$

$\Gamma \sim \frac{m_Z^3 v^2}{\pi \Lambda^4} \alpha_{NZ}^2$
 $\mathcal{B}^{\text{the}} \sim 10^{-3}$
 $\mathcal{B}^{\text{exp}} < 3.2 \times 10^{-6}$
[PLB 412 (1997) 201-209]

Theoretical estimates hold for $\Lambda = 1$ TeV and $O(1)$ couplings; I assume Z width is dominated by Standard Model

Naive estimate, based on 5×10^{12} Z bosons, requiring about 10 observed events and efficiency or order 0.2:
(0.85 exp. ref.)

$\mathcal{B}^{\text{exp}} \sim 10^{-11}$ ($\Lambda \sim 100$ TeV)

16

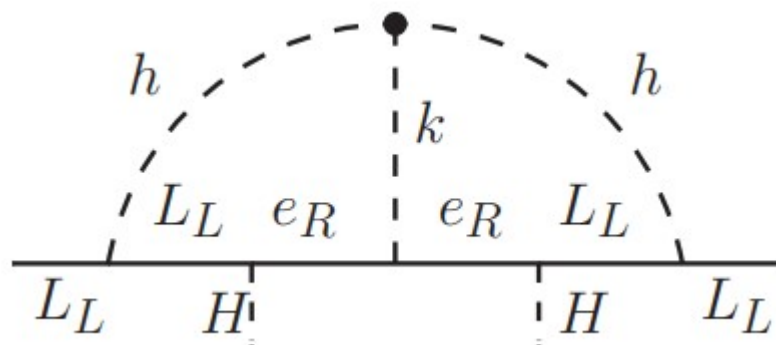
ECFA HTE meeting on Z pole physics;
September 2022

Other possibilities

Scalars related to neutrino masses

SO(10)/SO(9), 9 NGBs: $H, k^{\pm\pm}, h^{\pm}, \sigma$

Smallness of neutrino masses explained from their radiative origin



$$k^{++} \rightarrow h^+ h^+ \rightarrow \ell^+ \nu \ell^+ \nu$$

Conclusions

The sharpest prediction of CHMs in the scalar sector is modified (reduced) Higgs-gauge-boson couplings

It seems **very plausible that the scalar sector is extended** (singlets and triplets specially)

Plenty of different signals: rare top and Higgs (and Z and B meson) decays, untested production of new scalars, ...

Competitive with LHC? Definitely in some channels (involving hadronic activity)

Thank you!