# Generating Particle Cloud Jets with Denoising Diffusion

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#### **Problem and Goal**

Kansal et. al. 2022



- Deep learning methods for jet generation is a growing topic in HEP
  - Fast-Sim:
    - ML methods can improve generation times by orders of magnitude
  - Template building:
    - Use for anomaly detection
- Solution: use **Diffusion** 
  - Generation = iterative **denoising steps**

#### **Diffusion as differential equations**



#### **Diffusion as differential equations**



#### Sample Generation

- Numerically integrate reverse process
  - Which process (SDE or ODE) and which integration method is **flexible**
- Each step **requires a forward pass** of the network
  - Generation needs more computation than GANs and Flows
  - Main **detriment** to using **diffusion** models

Always a trade-off between time and fidelity

- Using the <u>JetNet</u> dataset and metrics
- Large radius **point clouds** jets
  - Gluon, Quark, Top, W, Z
  - Up to 150 constituents
  - $\circ \quad (\Delta \eta, \Delta \phi, p_{\mathsf{T}})$

#### PC-Jedi Setup

- First attempt at particle cloud diffusion
- Based on a transformer
- Trained **separate models** for gluon and top
- Denoising objective



#### **PC-Jedi Results**

Model was competitive to SOTA <u>MPGAN</u>



#### **PC-Jedi Results**

- Struggled recreating substructure variables for top jets
- And was slow



# JeDi — Droid

#### **PC-Droid**

One conditional model for all jet types

- Now **predicting denoised data** (not noise)
- **Smarter noise sampling** to focus on key areas of the trajectory during training.
- Skip connections for stability during training.

Compatible with SotA SDE/ODE Solvers.



#### Improvements with PC-Droid: ODE Trajectories



#### Speed and scaling improvements: CAE Architecture

Increase number of constituents from 30 to 150

- Introduced new network type: Cross Attention Encoder
- Bipartite graph between point cloud and collection of global tokens
  - Number of global tokens is a hyperparameter (M)
  - $\circ$  O(NM) computations compared to O(N<sup>2</sup>) of standard transformer



#### **PC-Droid Results**

- Great performance on 150 dataset
- New CAE network performs similarly with a big increase in generation speed



#### **PC-Droid Results**

- Massive improvements over our older diffusion model and MPGAN on 30 constituent dataset
- Significantly overtaking SOTA models



#### Further speed improvements: Consistency Distillation

- One of many diffusion **distillation methods**
- Use a **pretrained model** to train a **student model** to perform diffusion in less steps
- In some cases even allowing generation in **1 step**



#### Time vs Fidelity Trade-Off

- Comparison with other generative models on 150 dataset
  - <u>FPCD</u>
  - EPIC-GAN



#### Time vs Fidelity Trade-Off

- Comparison with other generative models on 150 dataset
  - <u>FPCD</u>
  - EPIC-GAN

- PC-Droid performance on higher end is now close to ideal and 5 times faster
- Can sacrifice fidelity to get up to 100 times faster with distillation



#### Outlook

- Introduced diffusion models into HEP for point cloud generation with PC-JeDI
- Significantly improved quality with PC-Droid
- Looked at all models in terms of time-vs-quality trade off
- We are now looking at new ways to use such models beyond fast-sim (Next talk!)

#### Current work

- PC-JeDi: Diffusion for Particle Cloud Generation in High Energy Physics
  - March 2023
  - Theory based on <u>Score-Based Generative Modeling through Stochastic Differential Equations</u>
- PC-Droid: Faster diffusion and improved quality for particle cloud generation
  - July 2023
  - Theory based on <u>Elucidating the Design Space of Diffusion-Based Generative Models</u> and <u>Consistency Models</u>
- EPiC-ly Fast Particle Cloud Generation with Flow-Matching and Diffusion
  - September 2023

### **Thank You**

# Backup

#### Proposal

- Use Diffusion
  - Generation = iterative **denoising steps**
- Point clouds
  - Replace the typical UNet with a message passing network
- Can use the **conditional generation** 
  - Generate jets with desired high-level features
    - Momentum, mass, signal type
  - Required for Fast-Sim and template building



#### Diffusion as an **SDE**



#### Diffusion as an **SDE**



Approximating the score function with a network is impossible  $\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_t \sim p(\boldsymbol{x}_t)} \| \boldsymbol{s}_{\theta}(\boldsymbol{x}_t, t) - \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t) \|^2$ time diffused neural network score of diffused data

Approximating the score function with a network is impossible  $\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_t \sim p(\boldsymbol{x}_t)} \| \boldsymbol{s}_{\theta}(\boldsymbol{x}_t, t) - \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t) \|^2$ 

> marginal diffused densities are intractable

Approximating the score function with a network is impossible  $\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_t \sim p(\boldsymbol{x}_t)} \| \boldsymbol{s}_{\theta}(\boldsymbol{x}_t, t) - \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t) \|^2$ 

Instead we look at the diffusion process of a single sample  $\mathbf{x}_{0}$  $\min_{\theta} \underbrace{\mathbb{E}_{t \sim U(0,1)}}_{\text{time}} \underbrace{\mathbb{E}_{\mathbf{x}_{0} \sim p(\mathbf{x}_{0})}}_{\text{data sample diffused sample}} \underbrace{\mathbb{E}_{\mathbf{x}_{t} \sim p(\mathbf{x}_{t} | \mathbf{x}_{0})}}_{\text{score of diffused sample}} \|\mathbf{s}_{\theta}(\mathbf{x}_{t}, t) - \underbrace{\nabla_{\mathbf{x}_{t}} \log p(\mathbf{x}_{t} | \mathbf{x}_{0})}_{\text{score of diffused sample}} \|\mathbf{x}_{0}\|^{2}$ 

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> This change is <u>allowed</u> because after expectations  $s_{\theta}(\boldsymbol{x}_t,t) \sim \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t)$

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> This change is <u>allowed</u> because after expectations  $\boldsymbol{s}_{\theta}(\boldsymbol{x}_t,t) \sim \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t)$

This change is <u>useful</u> because the conditional density is tractable  $p(\boldsymbol{x}_t | \boldsymbol{x}_0) = \mathcal{N}(\boldsymbol{x}_t; \gamma(t) \boldsymbol{x}_0, \sigma(t)^2 \boldsymbol{I})$ 

Old Learning Objective

\_ \_ \_

$$\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_0 \sim p(\boldsymbol{x}_0)} \mathbb{E}_{\boldsymbol{x}_t \sim p(\boldsymbol{x}_t | \boldsymbol{x}_0)} \| \boldsymbol{s}_{\theta}(\boldsymbol{x}_t, t) - \nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t | \boldsymbol{x}_0) \|^2$$

Conditional Density:

$$p(\boldsymbol{x}_t | \boldsymbol{x}_0) = \mathcal{N}(\boldsymbol{x}_t; \gamma(t) \boldsymbol{x}_0, \sigma(t)^2 \boldsymbol{I})$$

Diffused Sample Score:

$$\nabla_{\boldsymbol{x}_t} \log p(\boldsymbol{x}_t | \boldsymbol{x}_0) = \nabla_{\boldsymbol{x}_t} \frac{(\boldsymbol{x}_t - \gamma(t) \boldsymbol{x}_0)^2}{2\sigma(t)^2} = -\frac{\boldsymbol{x}_t - \gamma(t) \boldsymbol{x}_0}{\sigma(t)^2} = -\frac{\gamma(t) \boldsymbol{x}_0 + \sigma(t) \boldsymbol{\epsilon} - \gamma(t) \boldsymbol{x}_0}{\sigma(t)^2} = -\frac{\boldsymbol{\epsilon}}{\sigma(t)}$$

Neural Network Parameterisation:

$$\hat{\boldsymbol{\epsilon}}_{\theta}(\boldsymbol{x}_t, t) = -\sigma(t)s_{\theta}(\boldsymbol{x}_t, t)$$

New Learning objective:

$$\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_0 \sim p(\boldsymbol{x}_0)} \mathbb{E}_{\boldsymbol{\epsilon} \sim \mathcal{N}(\boldsymbol{0},\boldsymbol{I})} \frac{1}{\sigma(t)^2} \| \hat{\boldsymbol{\epsilon}}_{\theta}(\boldsymbol{x}_t,t) - \boldsymbol{\epsilon} \|^2$$
30

$$\min_{\theta} \mathbb{E}_{t \sim U(0,1)} \mathbb{E}_{\boldsymbol{x}_0 \sim p(\boldsymbol{x}_0)} \mathbb{E}_{\boldsymbol{\epsilon} \sim \mathcal{N}(\boldsymbol{0},\boldsymbol{I})} \frac{1}{\sigma(t)^2} \| \hat{\boldsymbol{\epsilon}}_{\theta}(\boldsymbol{x}_t,t) - \boldsymbol{\epsilon} \|^2$$

Sample time:	t~U[0,1]
Sample data:	x0~{Training set}
Sample noise:	$\epsilon \sim N(0,1)_d$
Corrupt data:	$xt = \gamma(t) * x0 + \sigma(t) * \epsilon$
Get loss:	$L = c(t) * [NN(xt,t) - eps]^2$

# PC-Jedi: Paper 1

#### **Improvements with PC-Droid**

1. Change to EDM setup with preprocessing and sigma sampling SDE:  $dx_t = \sqrt{2t} dw$ ODE:  $dx_t = -t\nabla_x \log p(x;t) dt$ 



#### PC-Jedi Setup

- For generation we tested:
  - Euler
  - Euler-Maruyama (SDE)
  - **RK4**
  - DDIM



Generated Constituents

#### **Conditional Adherence**

Is our conditional model actually obeying its conditions?

- Natural difference between conditional and point cloud variables in the data
- Slightly larger spread in **p**<sub>T</sub>
  - Majority within 0.3%



#### **PC-Jedi Results**

Model was competitive to SOTA <u>MPGAN</u>



#### **PC-Jedi Results**

• Struggled recreating substructure variables for top jets



## PC-Droid: Paper 2

#### **CD Models Results**

- Tested CD model with **1 and 5** step generation
- Significantly faster than base model (100x) but lower quality



#### **Sample Generation**

- Numerically integrate reverse process
  - Which process (SDE or ODE) and which integration method is flexible
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  - Main **detriment** to using **diffusion** models

#### Always a trade-off between time and fidelity

**SDE** with Euler-Maruyama



