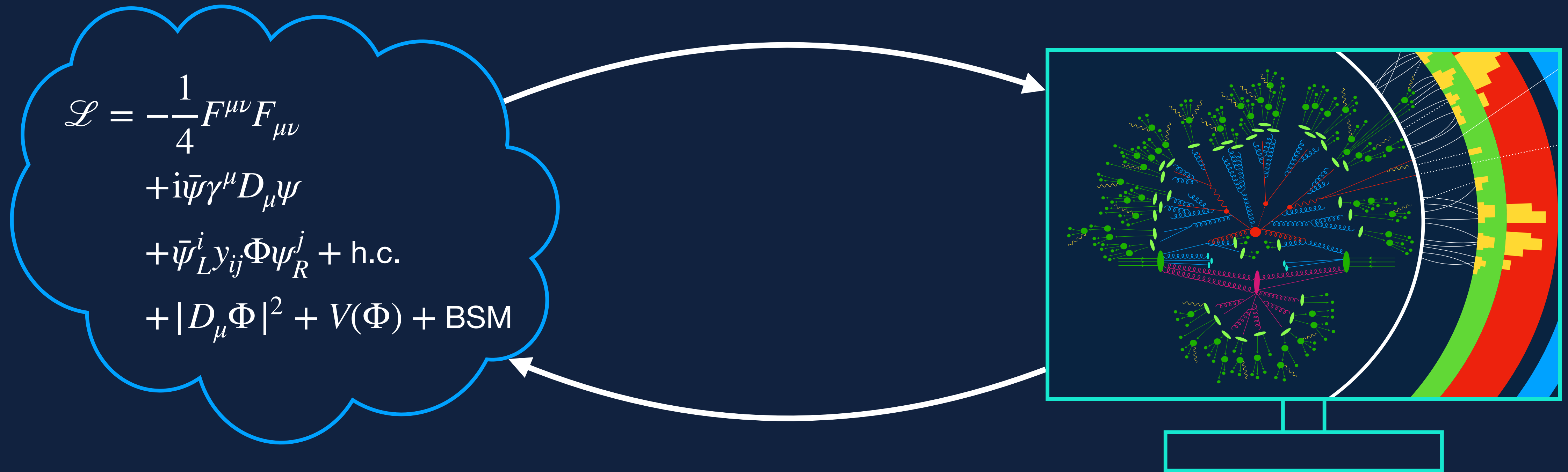


# Modern Machine Learning for the LHC Simulation Chain

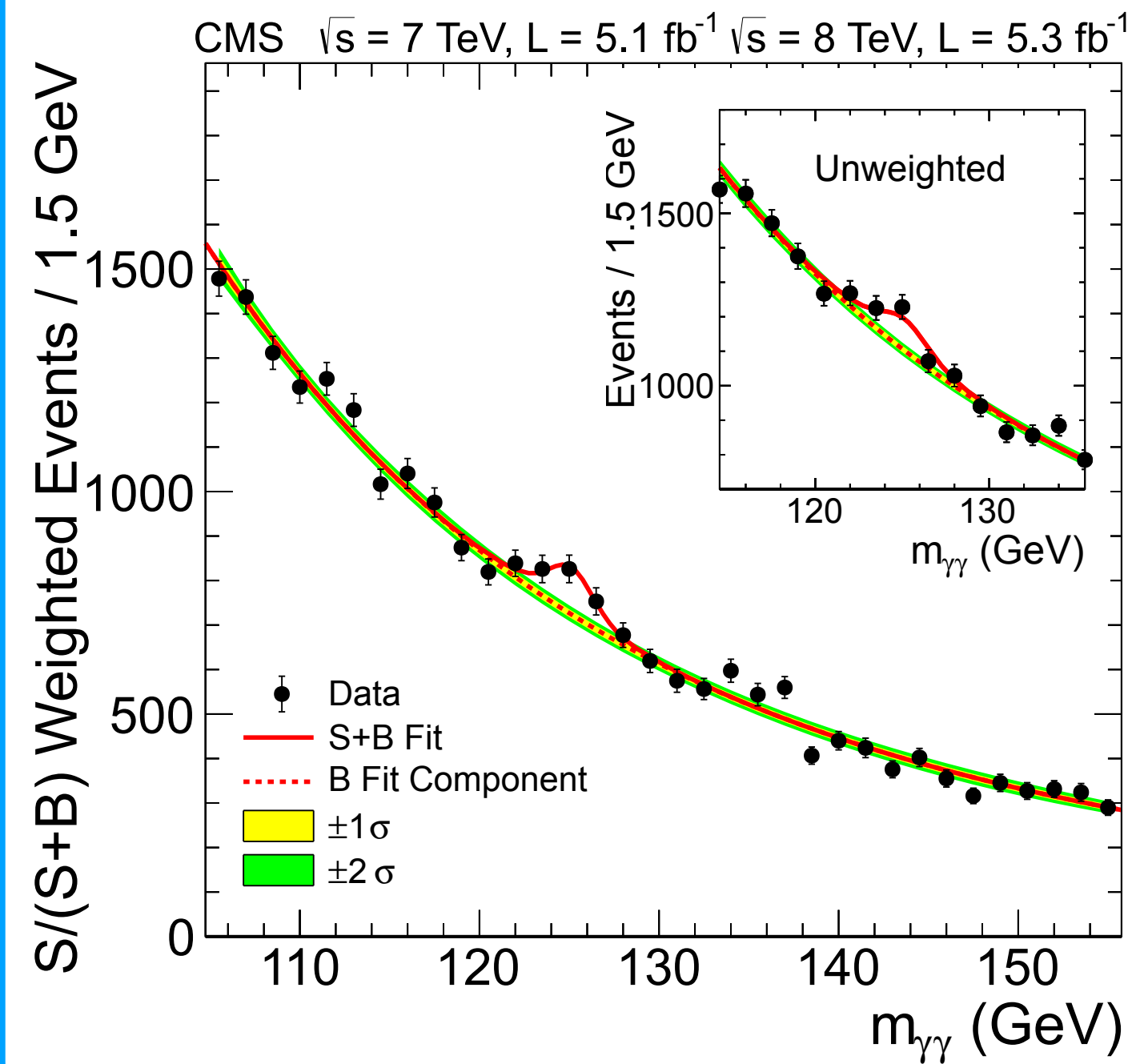


**Why do we talk about simulations?**

# We will have a lot more data soon

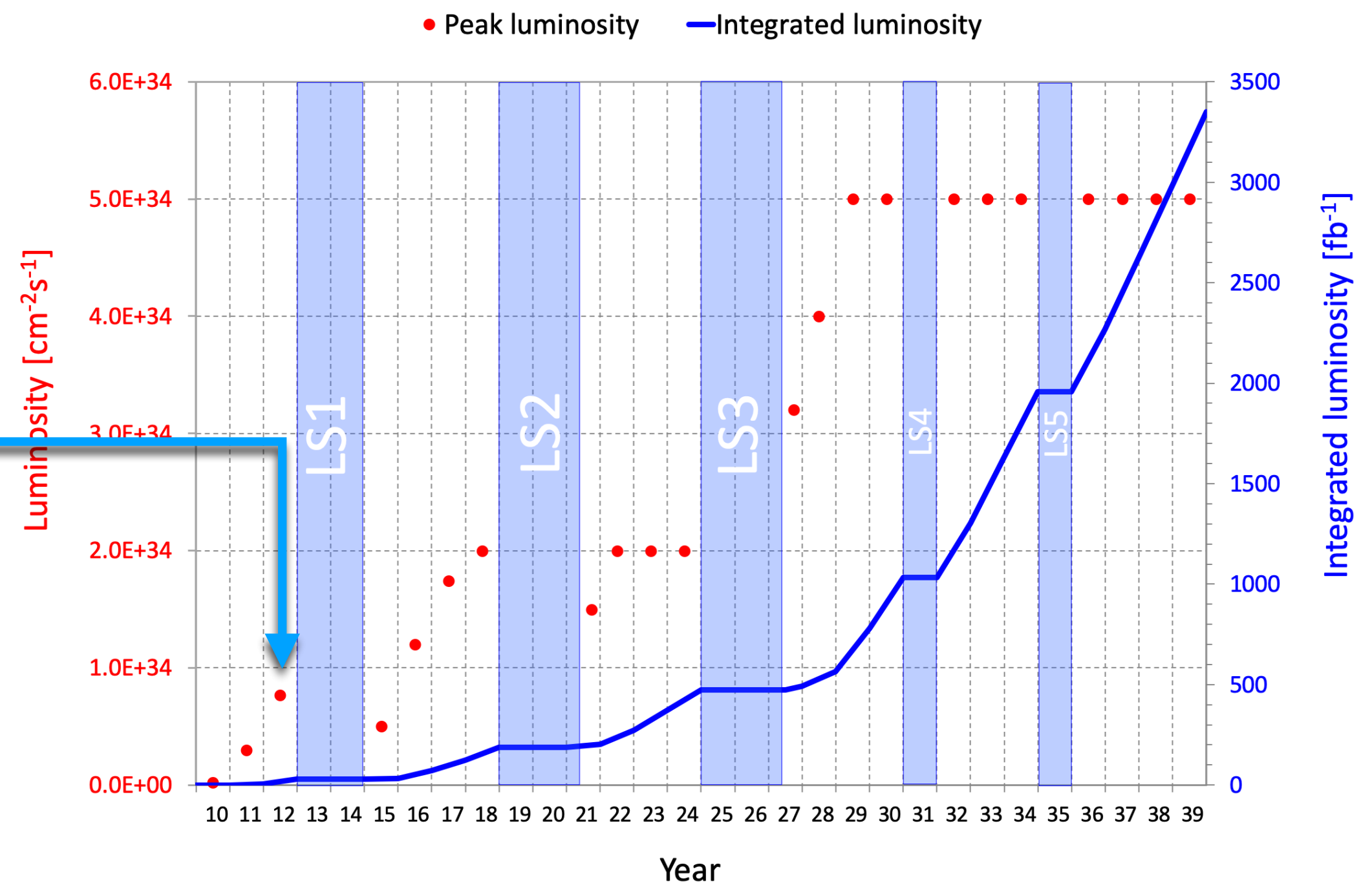


CMS Collaboration [arXiv:1207.7235, Phys.Lett.B]



2012

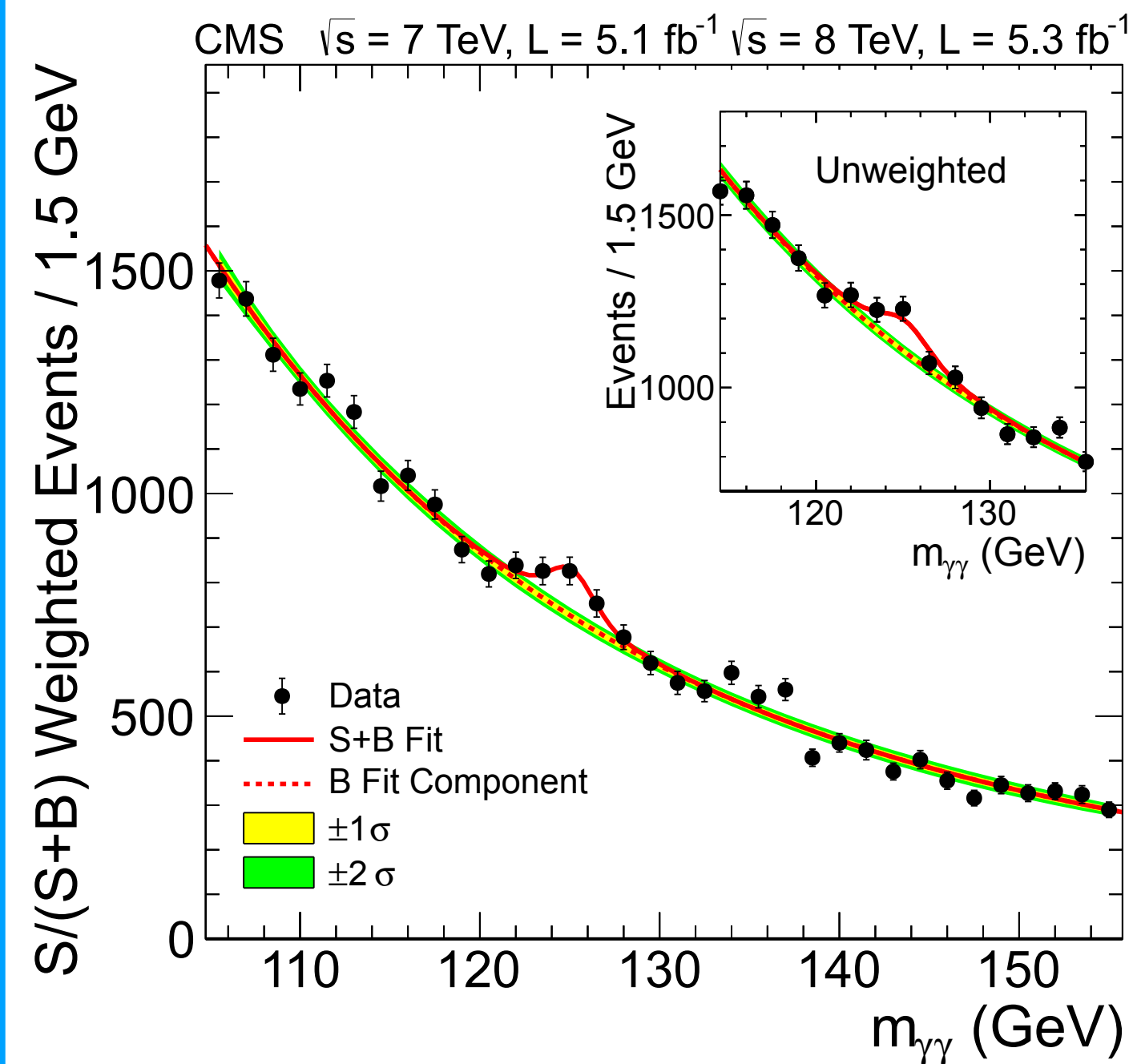
<https://lhc-commissioning.web.cern.ch/schedule/HL-LHC-plots.htm>



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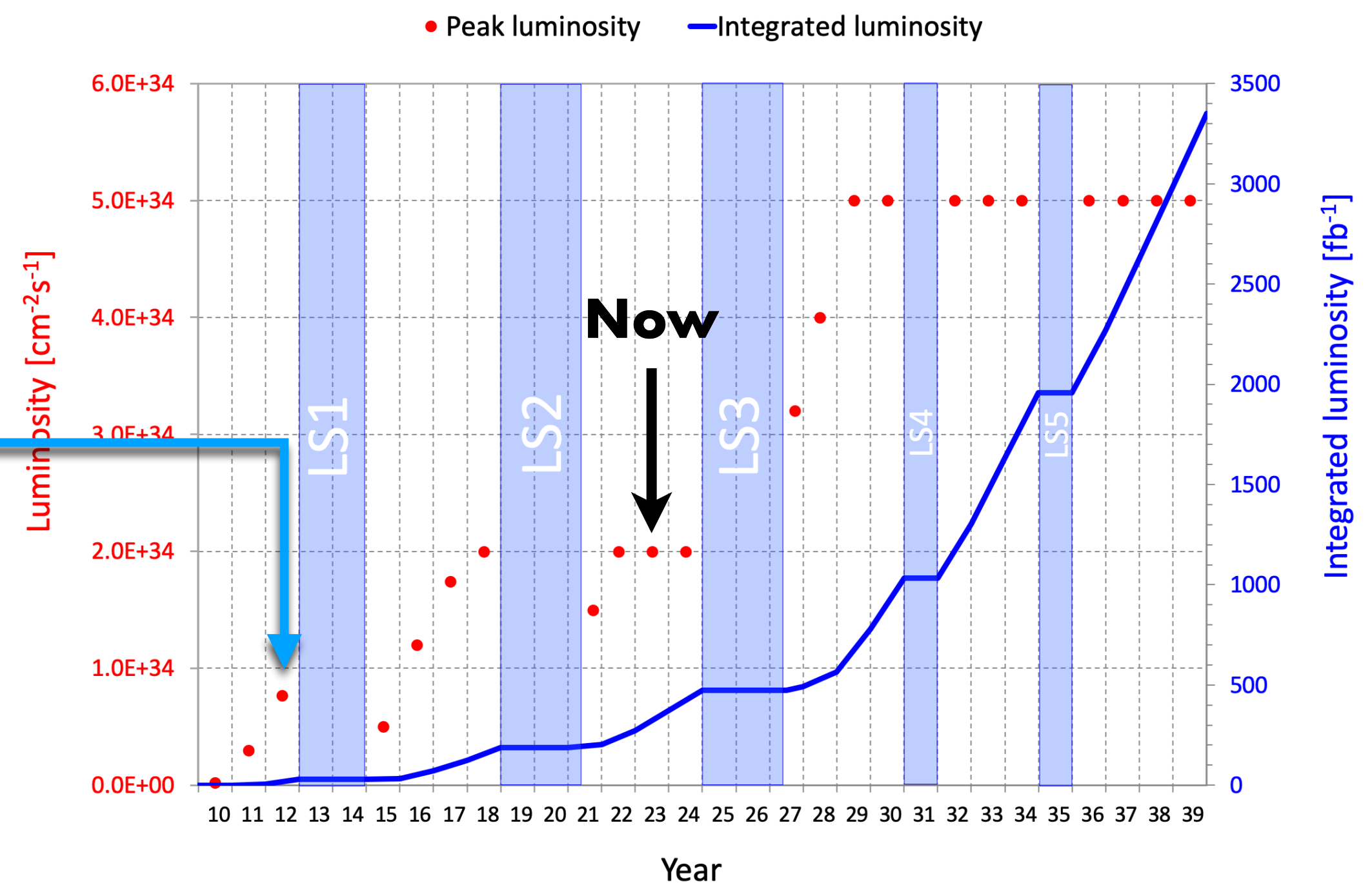


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2012

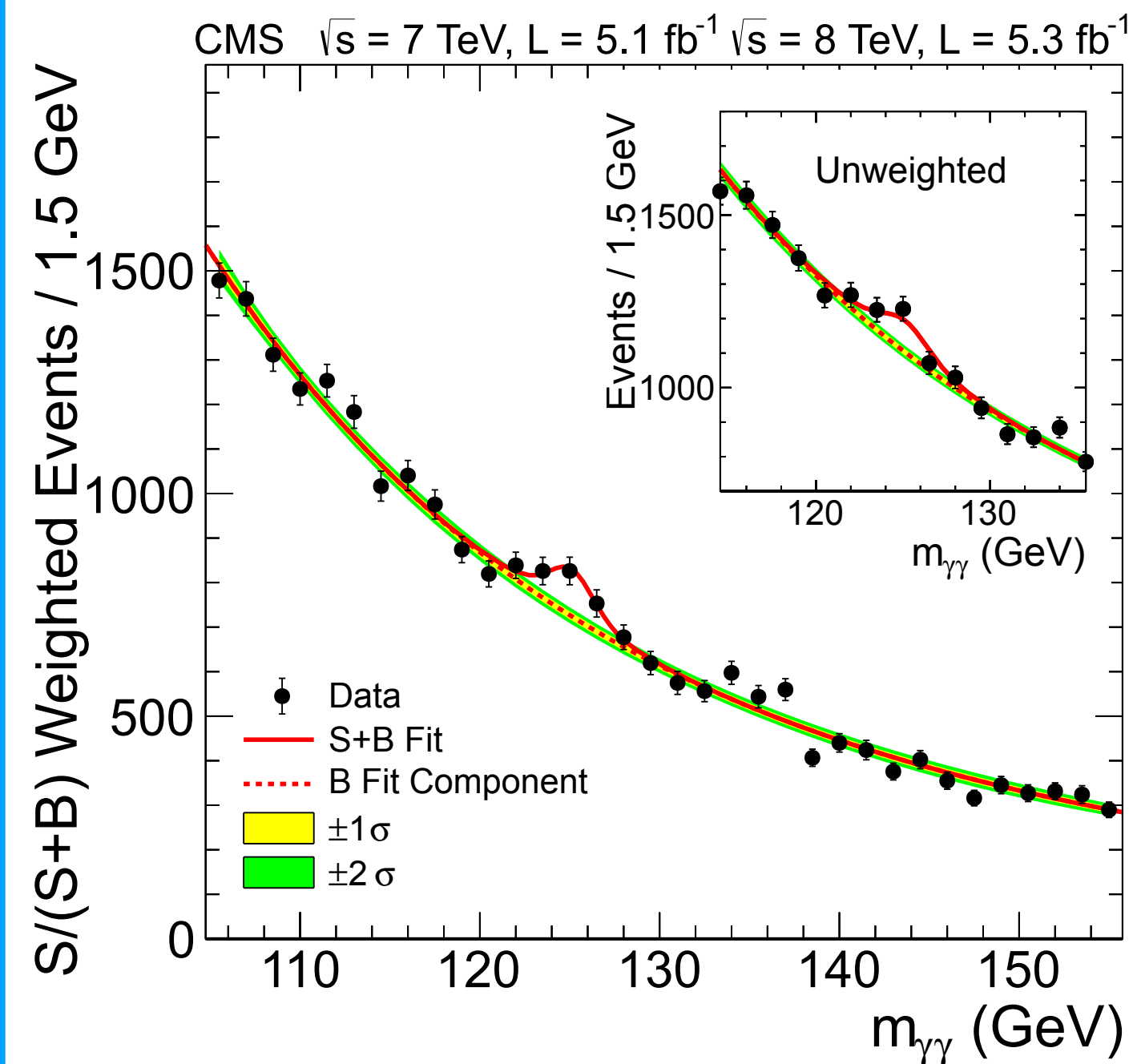
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# We will have a lot more data soon

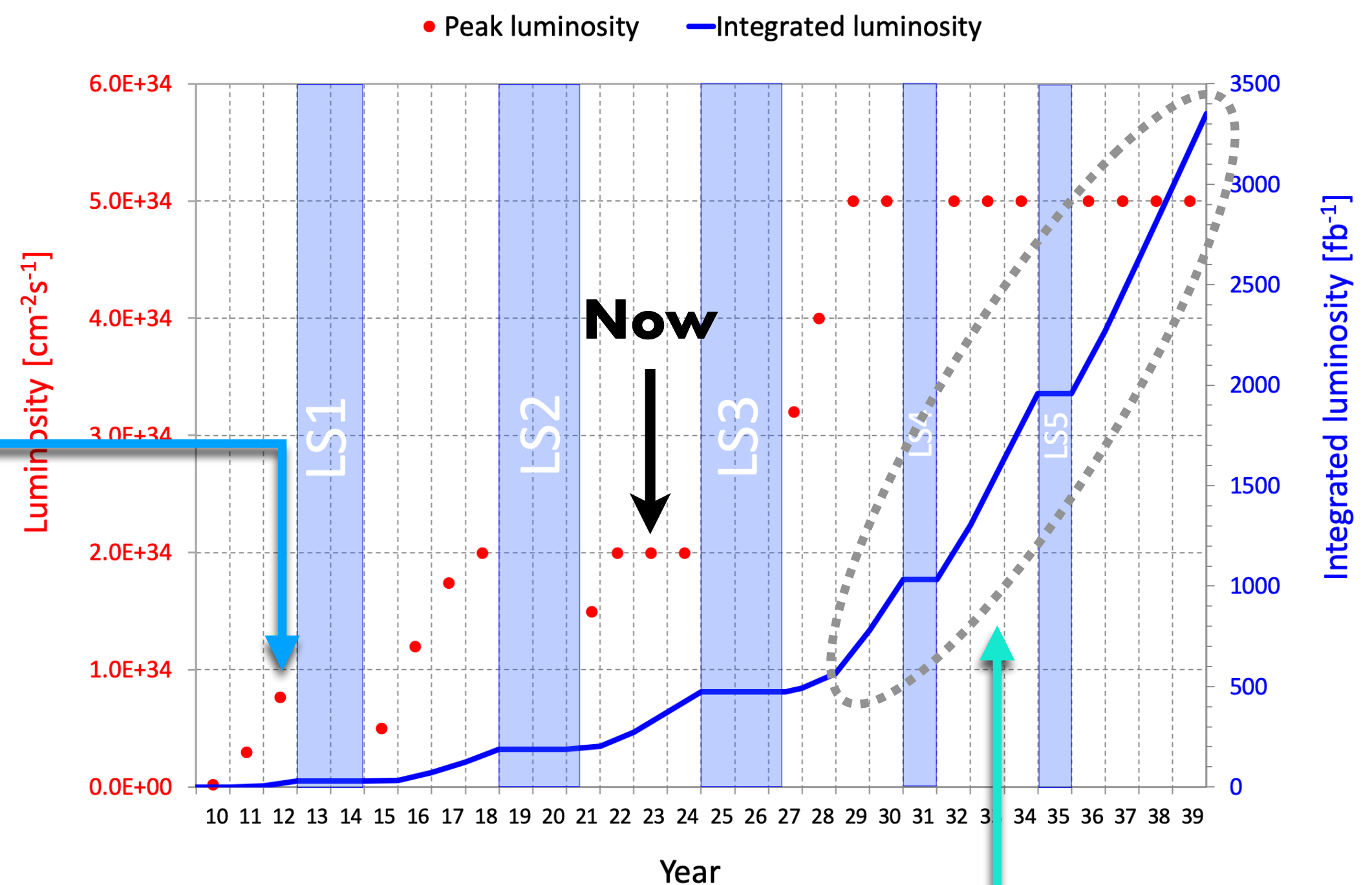


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2012

<https://lhc-commissioning.web.cern.ch/schedule/HL-LHC-plots.htm>



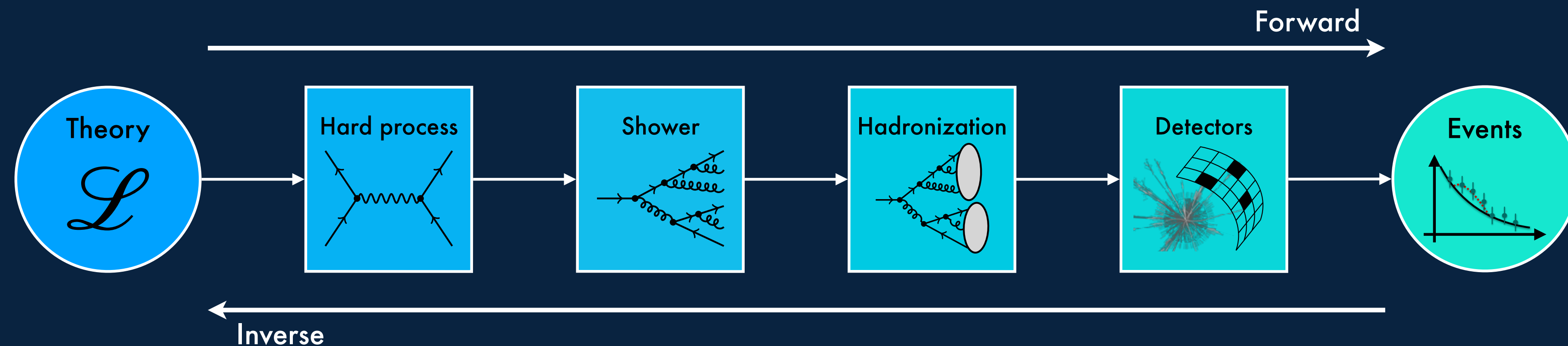
- We will have **20-25x** more data
- ➔ We want to understand **all aspects** of data based on **first principles!**

# Understanding LHC data based on 1<sup>st</sup> principles



What do we need to understand the data?

1. Precision simulations (a lot)
2. Optimized analyses for high-dimensional data

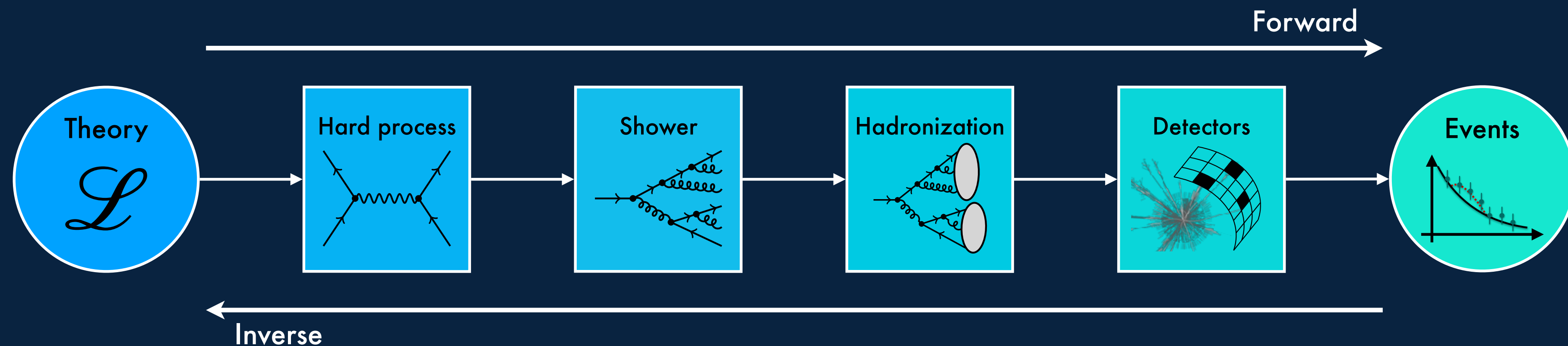


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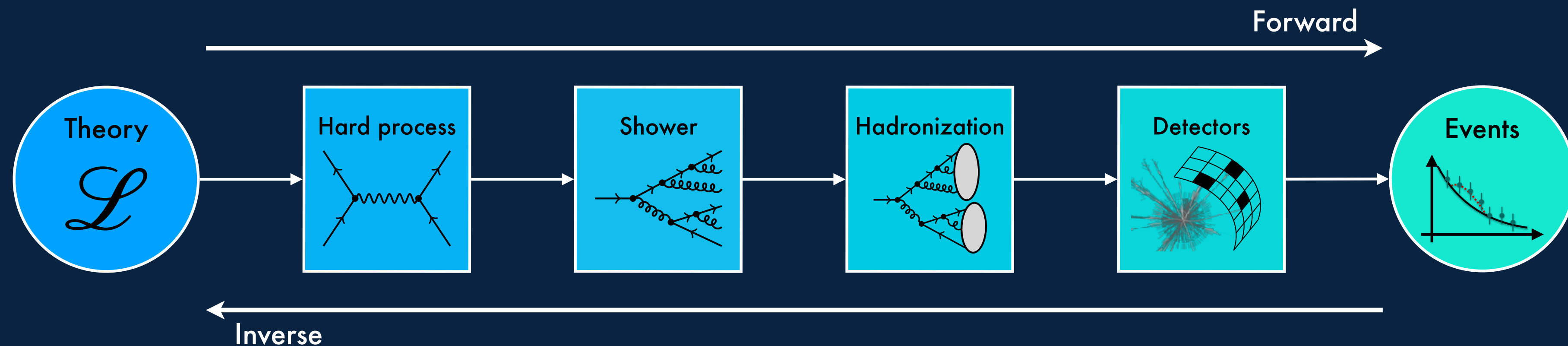
➡ Machine Learning has significant impact on all aspects

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What do we need to understand the data?

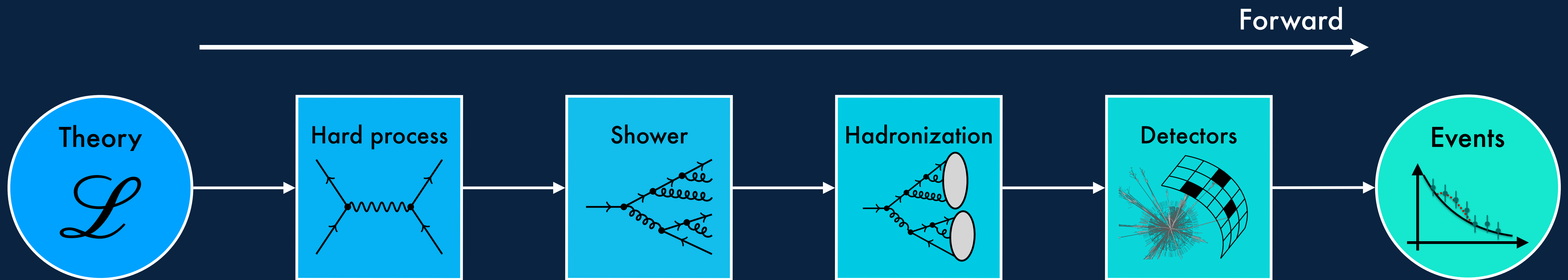
1. Precision simulations (a lot) ← this talk
2. Optimized analyses for high-dimensional data



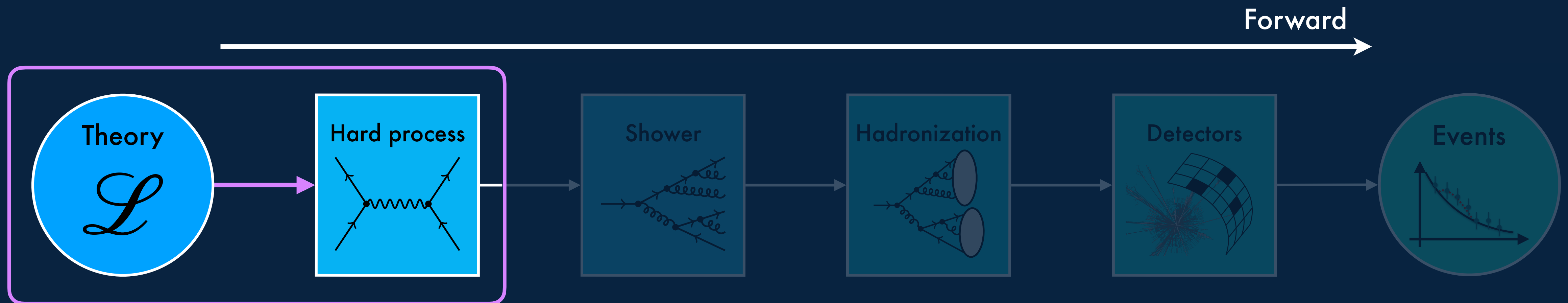
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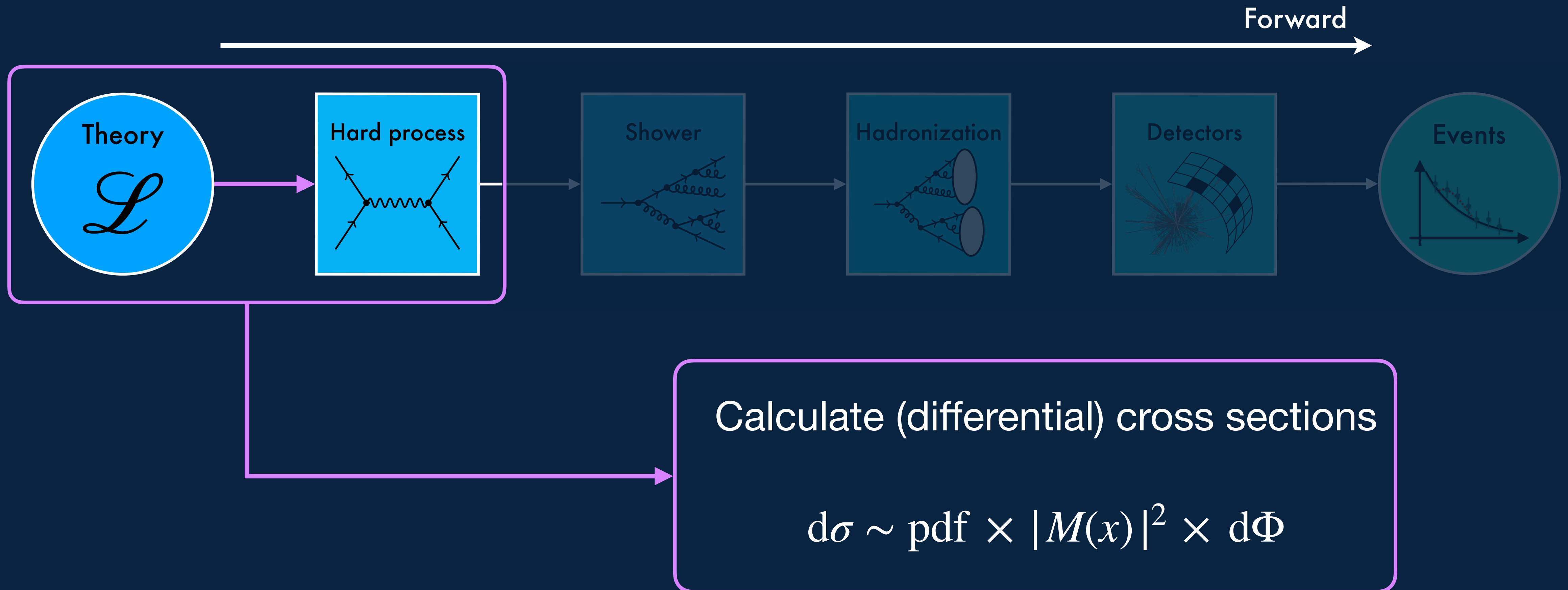
# ML for forward simulations



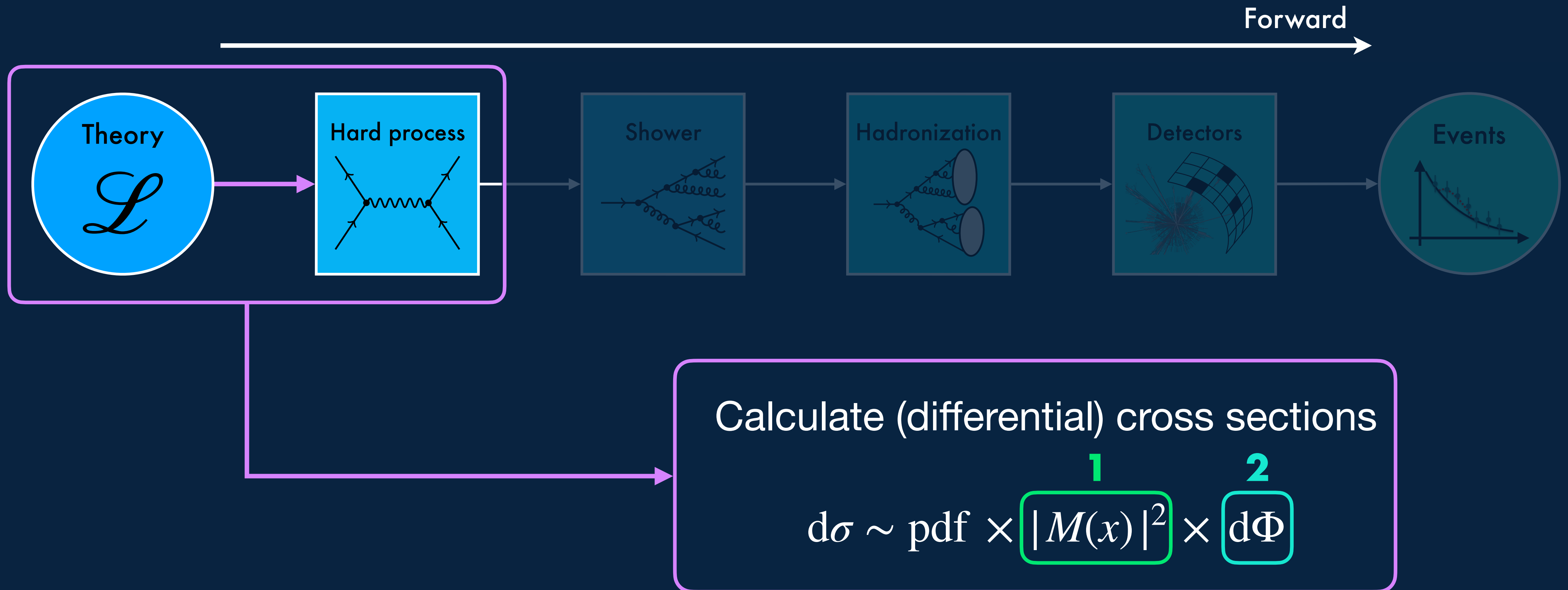
# ML for forward simulations



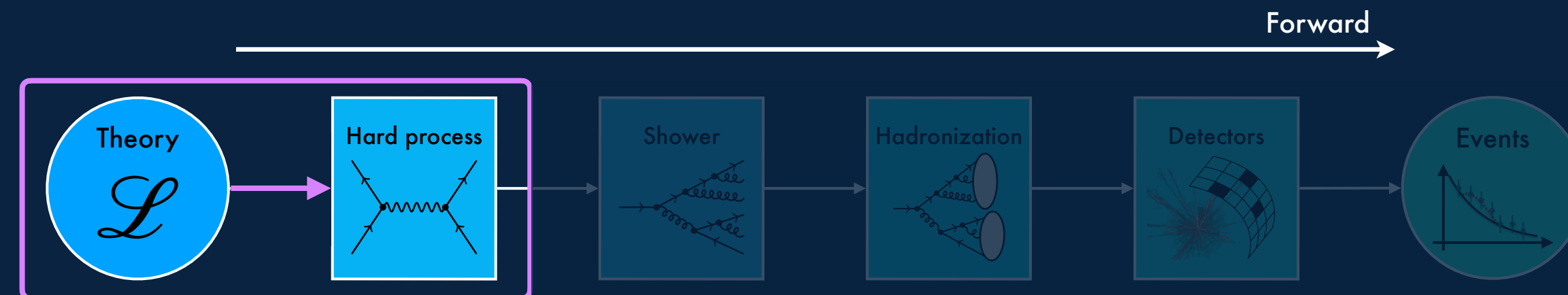
# ML for forward simulations



# ML for forward simulations



# ML for forward simulations



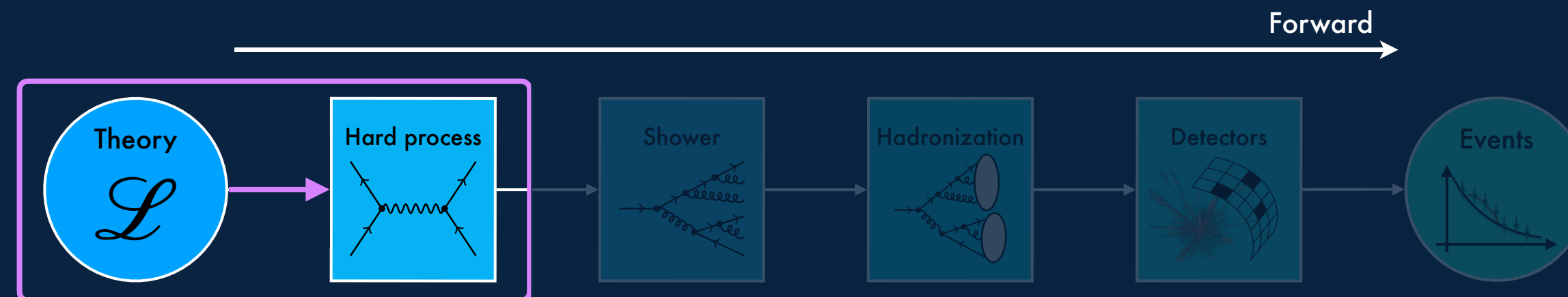
$$d\sigma \sim \text{pdf} \times |M(x)|^2 \times \text{phase space}$$

**Amplitudes:** avoid expensive matrix element

- As “simple” **regression** task

[1912.11055, 2002.07516, 2006.16273, 2008.10949, 2104.14182, 2105.04898, 2106.09474, 2107.06625, 2109.11964, 2112.09145, 2201.04523, 2206.08901, 2206.04115, 2206.14831, 2301.13562, 2302.04005, 2306.07726,.....]

# ML for forward simulations

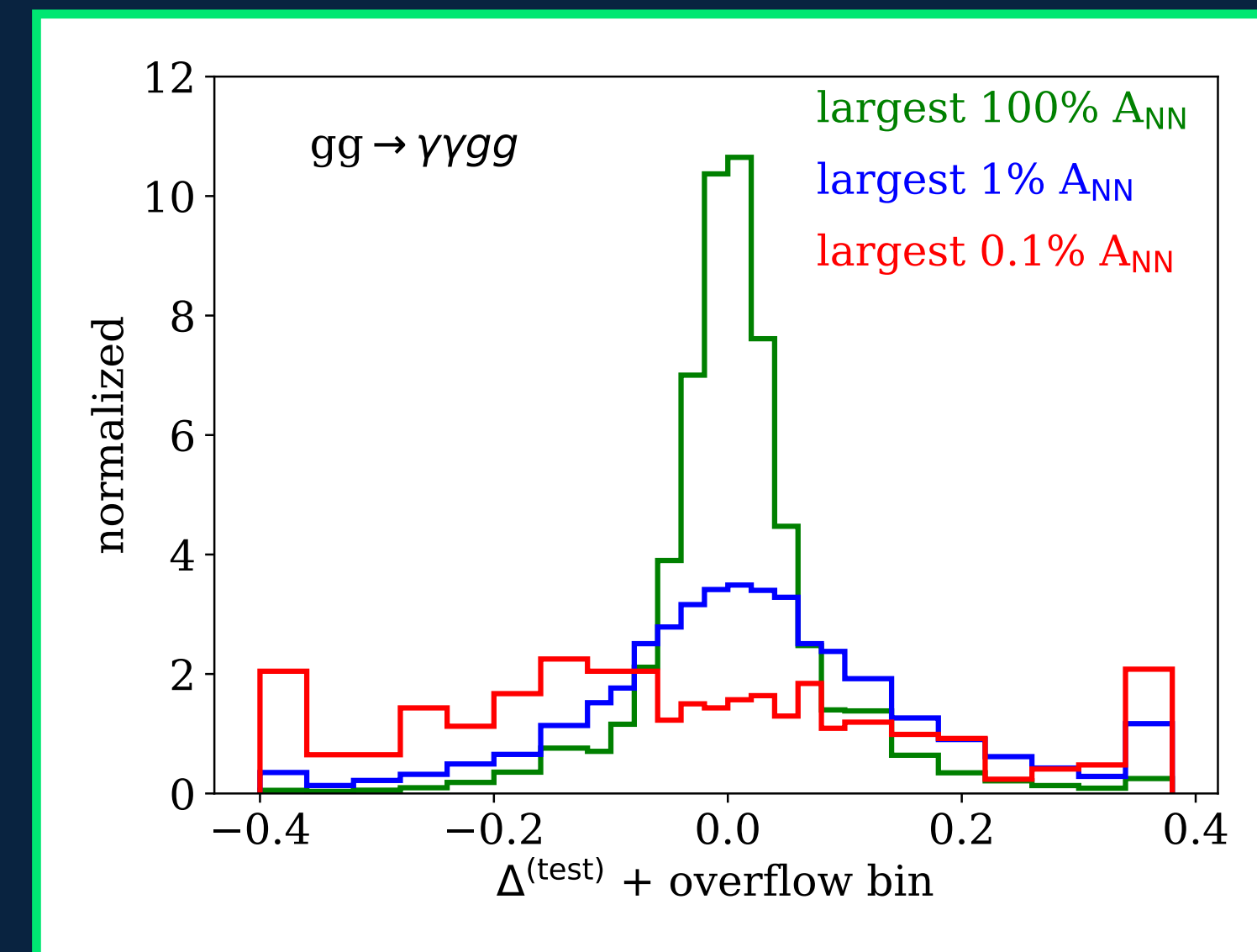


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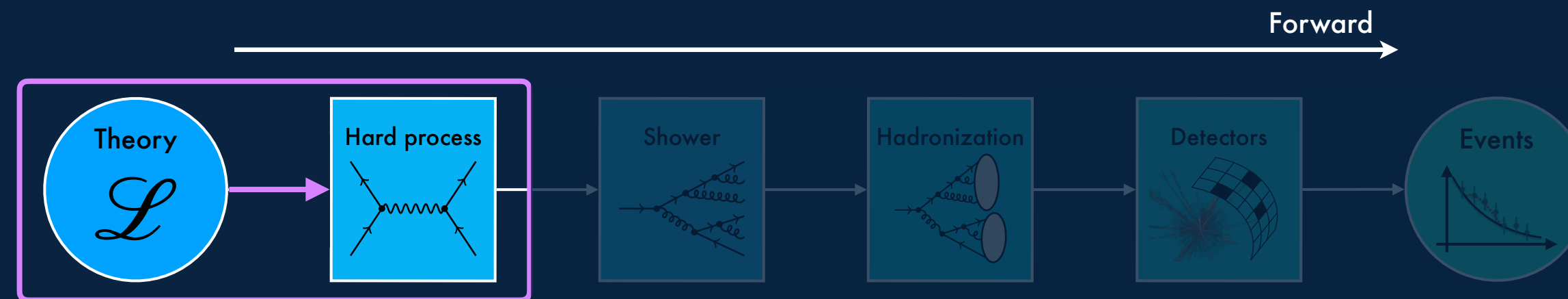
- As “simple” **regression** task
- With uncertainties/boosting using **Bayesian NN**

Badger, Butter, Luchman, Pitz, Plehn [2206.14831]



[1912.11055, 2002.07516, 2006.16273, 2008.10949, 2104.14182, 2105.04898, 2106.09474, 2107.06625, 2109.11964, 2112.09145, 2201.04523, 2206.08901, 2206.04115, 2206.14831, 2301.13562, 2302.04005, 2306.07726,.....]

# ML for forward simulations

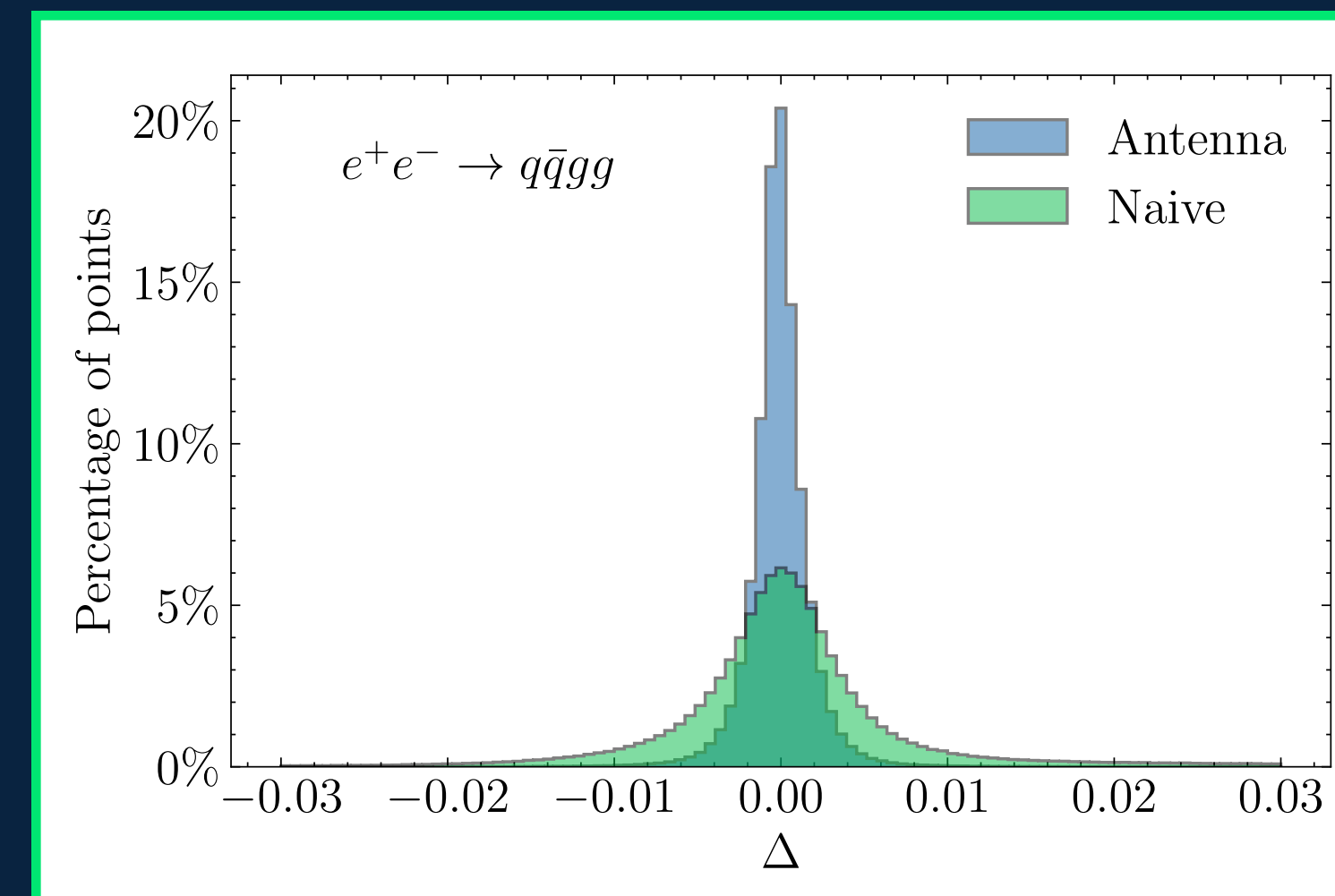


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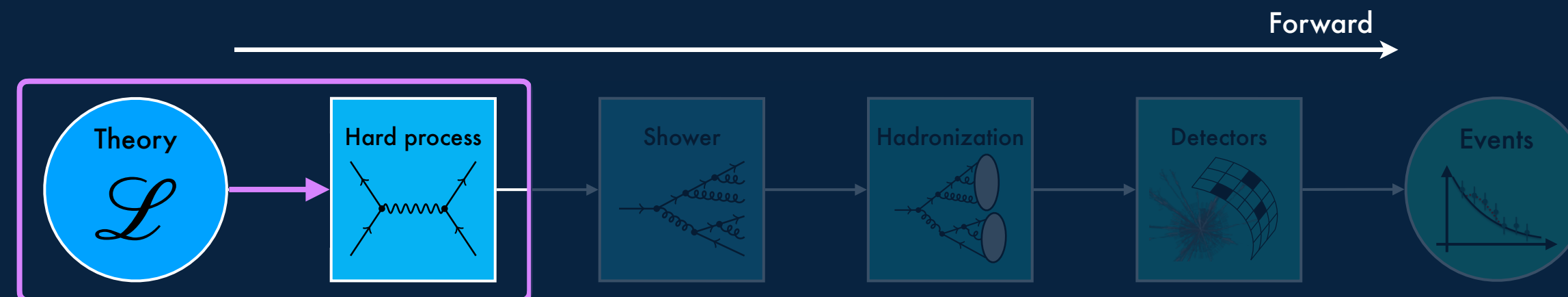
- As “simple” **regression** task
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- Using factorisation ansatz to reach **% level** accuracy

Maître, Truong [2302.04005]



[1912.11055, 2002.07516, 2006.16273, 2008.10949, 2104.14182, 2105.04898, 2106.09474, 2107.06625, 2109.11964, 2112.09145, 2201.04523, 2206.08901, 2206.04115, 2206.14831, 2301.13562, 2302.04005, 2306.07726,.....]

# ML for forward simulations

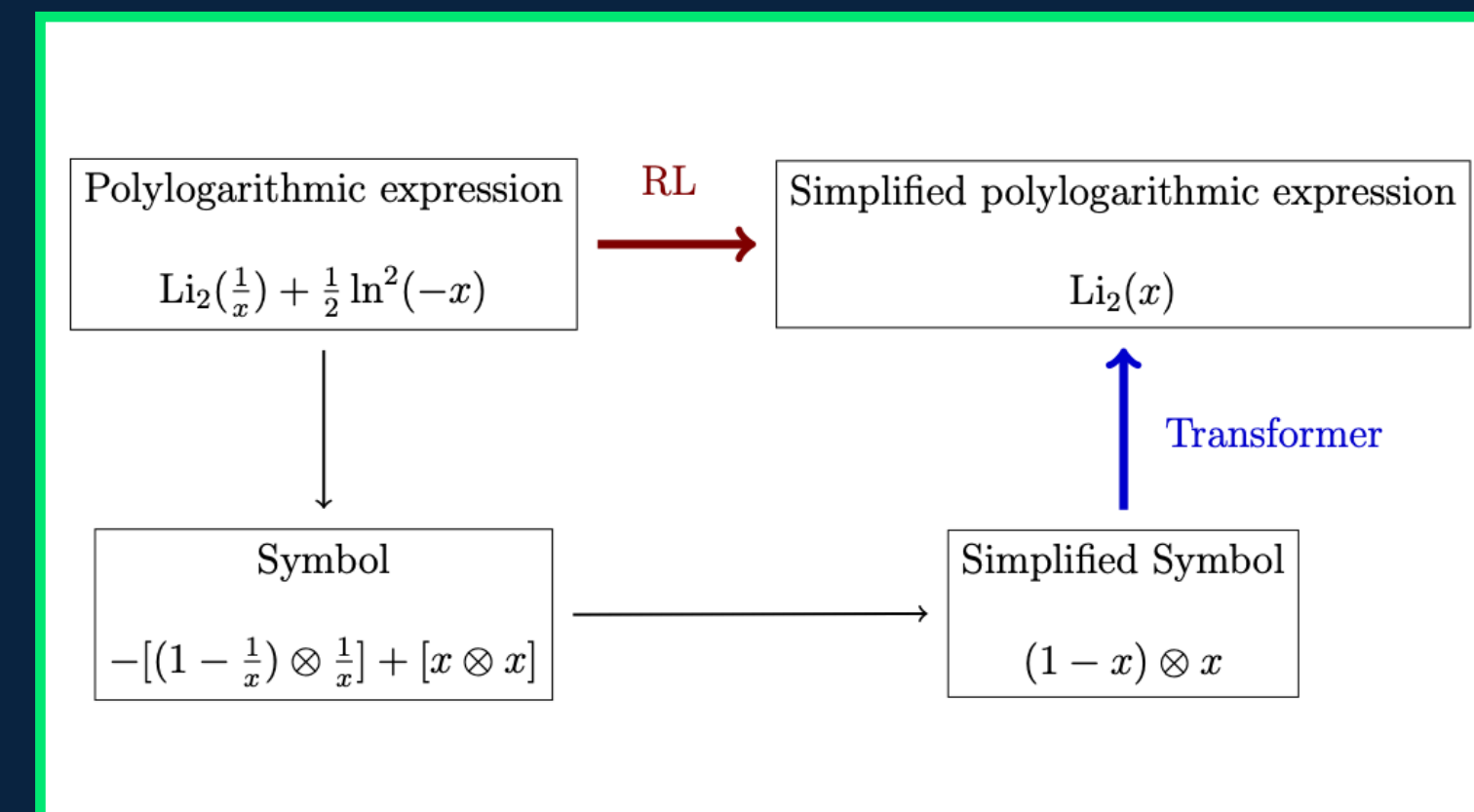


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- **RL and/or Transformer** for simplifications of Polylogarithms

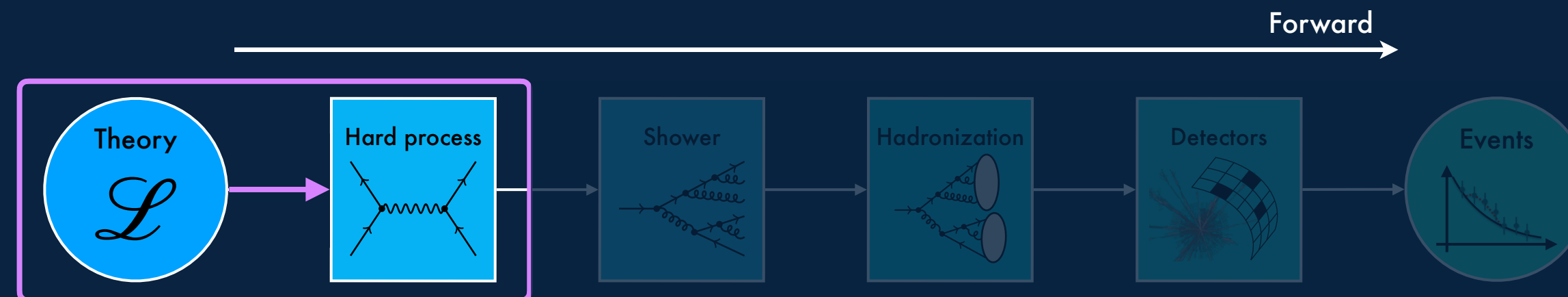
Dersey, Schwartz, Zhang [2206.04115]



[1912.11055, 2002.07516, 2006.16273, 2008.10949, 2104.14182, 2105.04898, 2106.09474, 2107.06625, 2109.11964, 2112.09145, 2201.04523, 2206.08901, 2206.04115, 2206.14831, 2301.13562, 2302.04005, 2306.07726,.....]



# ML for forward simulations

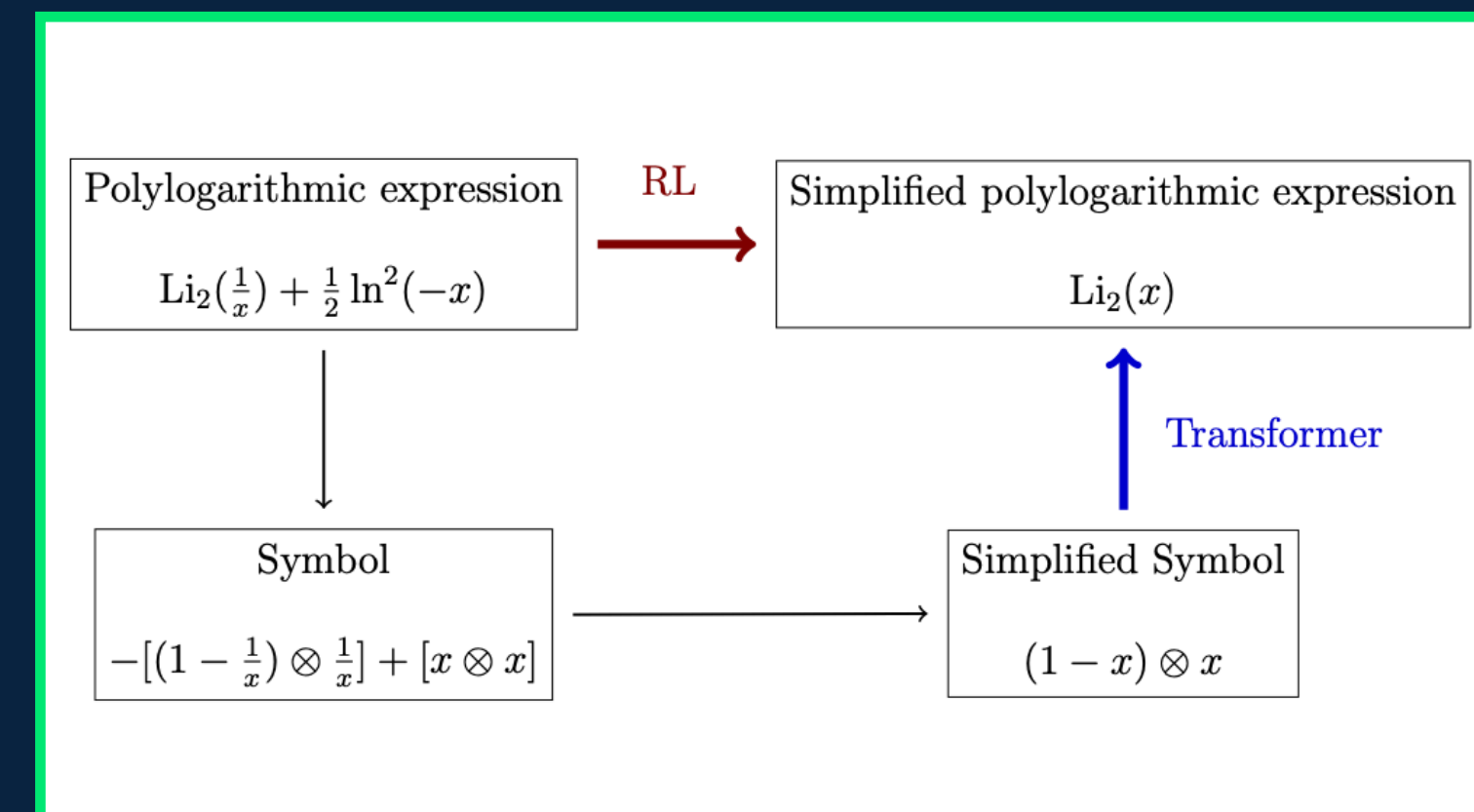


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- Using factorisation ansatz to reach **% level** accuracy
- **RL and/or Transformer** for simplifications of Polylogarithms
- NN-assisted **contour deformation** (Loop integrals)

Dersey, Schwartz, Zhang [2206.04115]



[1912.11055, 2002.07516, 2006.16273, 2008.10949, 2104.14182, 2105.04898, 2106.09474, 2107.06625, 2109.11964, 2112.09145, 2201.04523, 2206.08901, 2206.04115, 2206.14831, 2301.13562, 2302.04005, 2306.07726,.....]

# NNContour

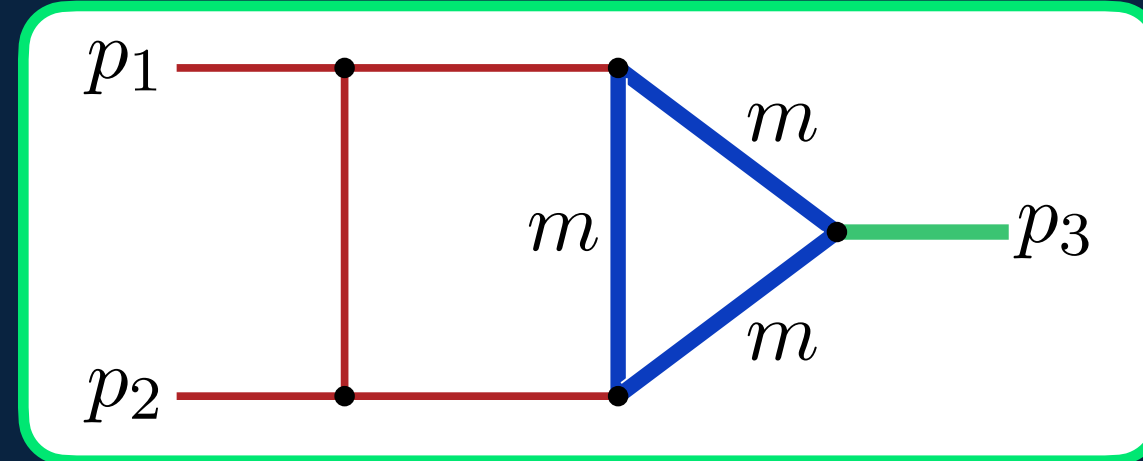
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**ML for loop integrals**

# NNContour — ML for loop integrals



$$G \propto \int_0^1 \prod_{j=1}^{N-1} dx_j x_j^{\nu_j-1} \frac{U^{\nu-(L+1)D/2}}{F^{\nu-LD/2}}$$

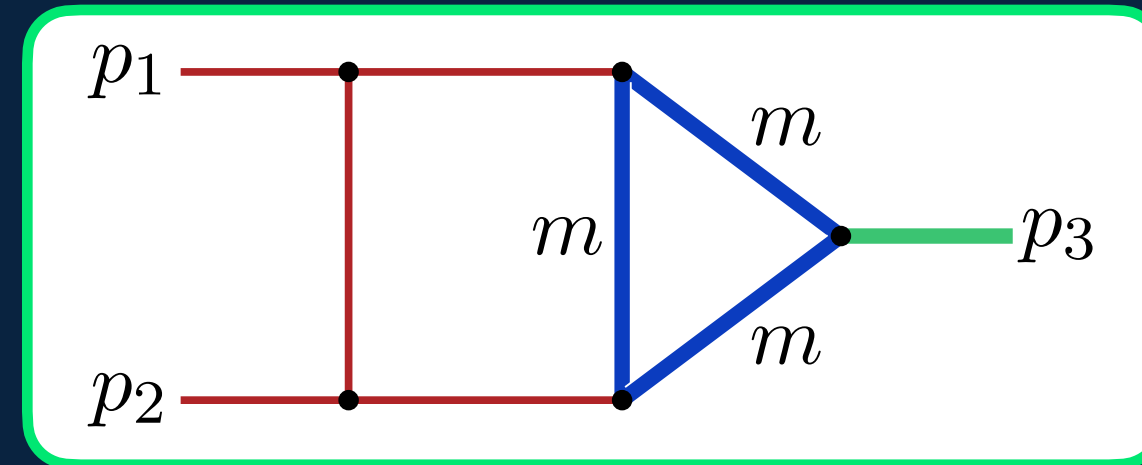


Contains singularities

# NNContour — ML for loop integrals



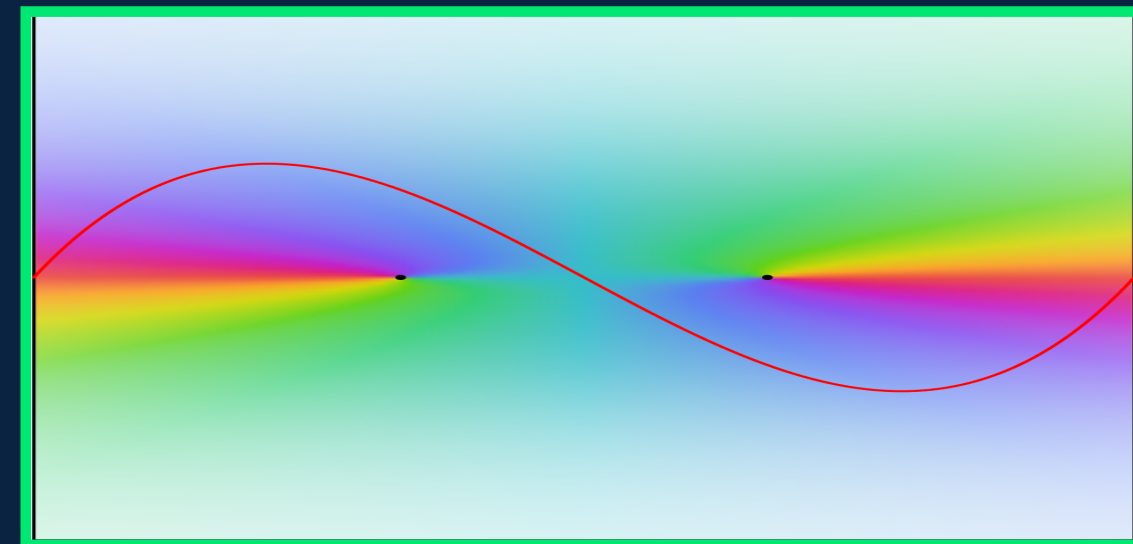
$$G \propto \int_0^1 \prod_{j=1}^{N-1} dx_j x_j^{\nu_j-1} \frac{U^{\nu-(L+1)D/2}}{F^{\nu-LD/2}}$$



Contains singularities

**Cauchy-Theorem** → Contour deformation

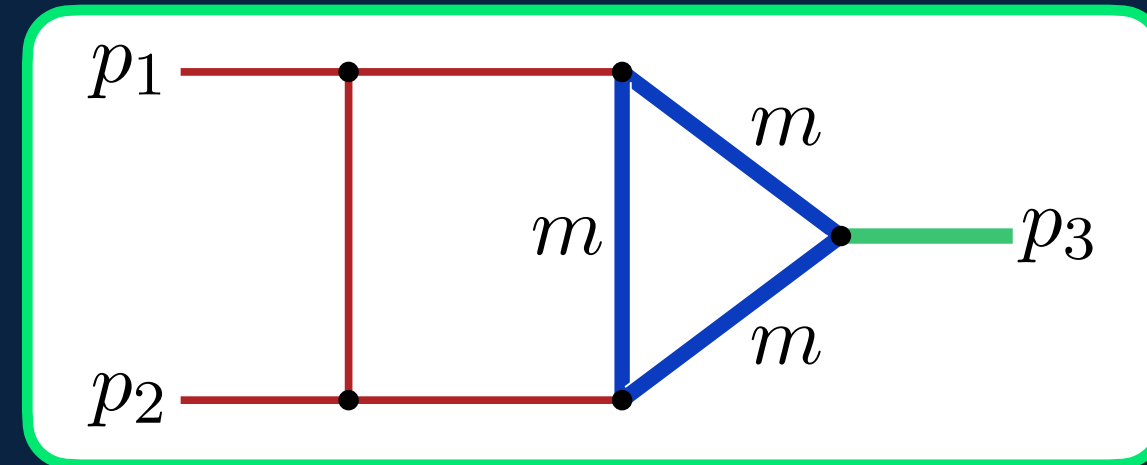
$$\int_0^1 \prod_{j=1}^N dx_j I(\vec{x}) = \int_{\gamma} \prod_{j=1}^N dz_j I(\vec{z})$$



# NNContour — ML for loop integrals



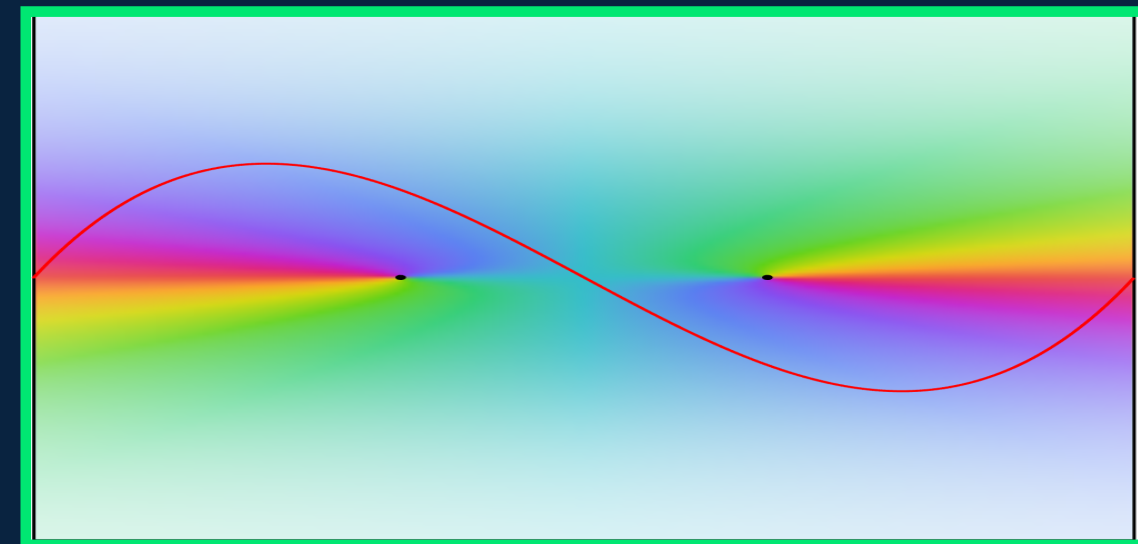
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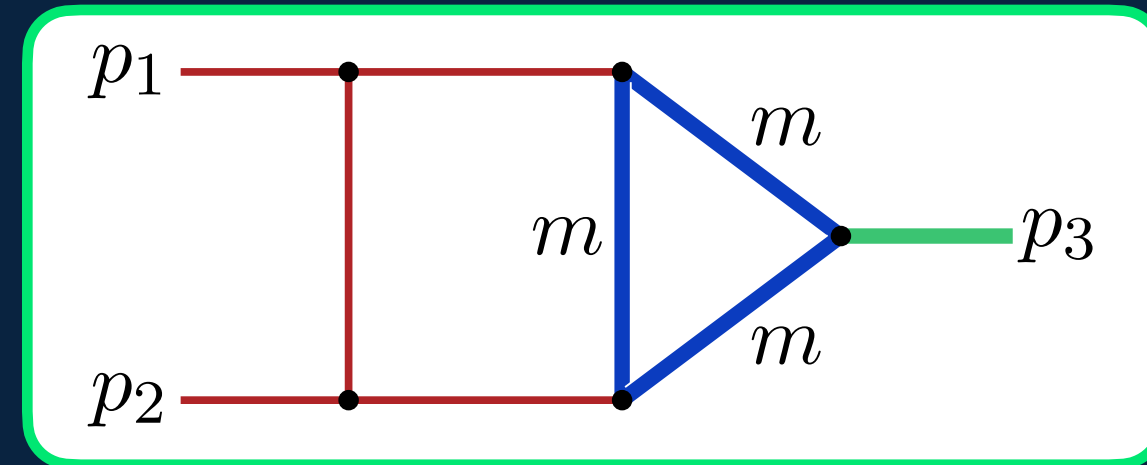


Parametrize with **NF + NN**

# NNContour — ML for loop integrals



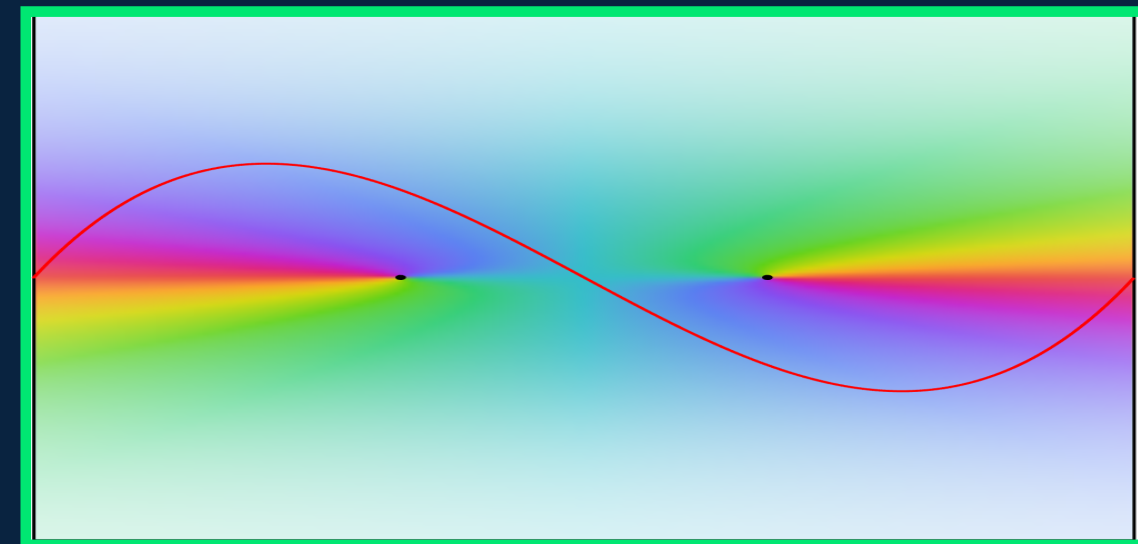
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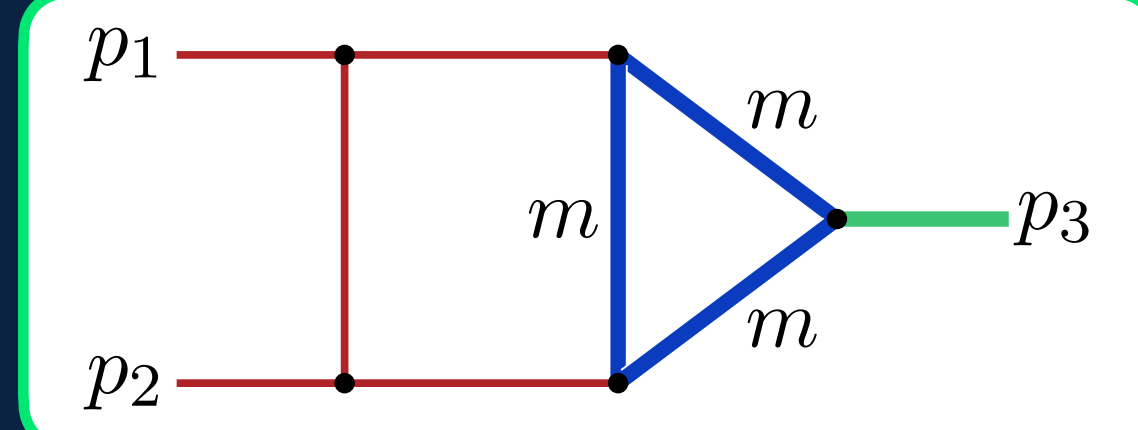
Parametrize with **NF + NN**

→ Optimal parametrization = small variance

# NNContour — ML for loop integrals

RW, Magerya, Villa, Jones,  
Kerner, Butter, Heinrich, Plehn [2112.09145]

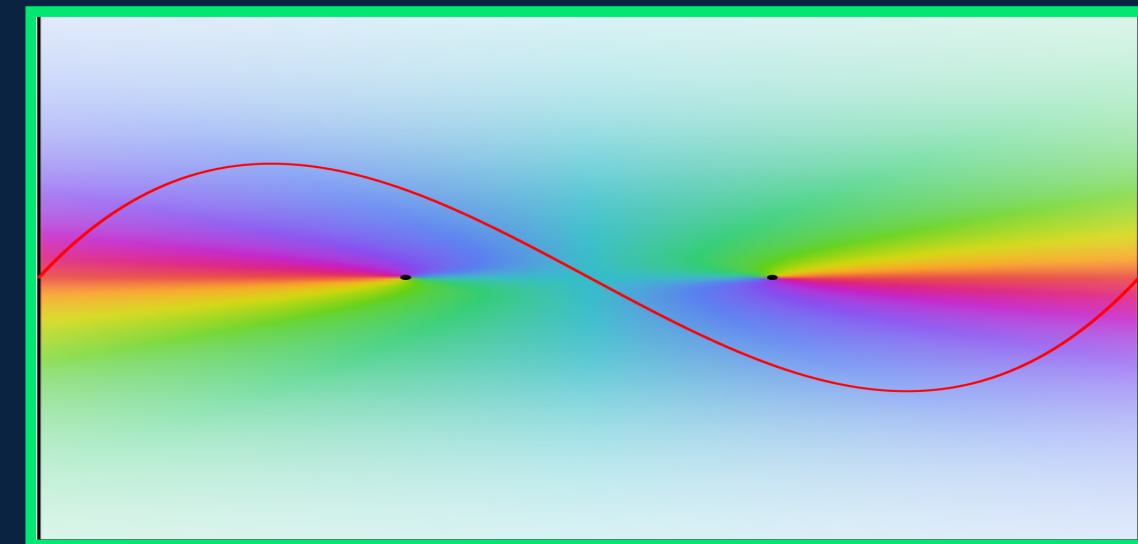
$$G \propto \int_0^1 \prod_{j=1}^{N-1} dx_j x_j^{\nu_j-1} \frac{U^{\nu-(L+1)D/2}}{F^{\nu-LD/2}}$$



Contains singularities

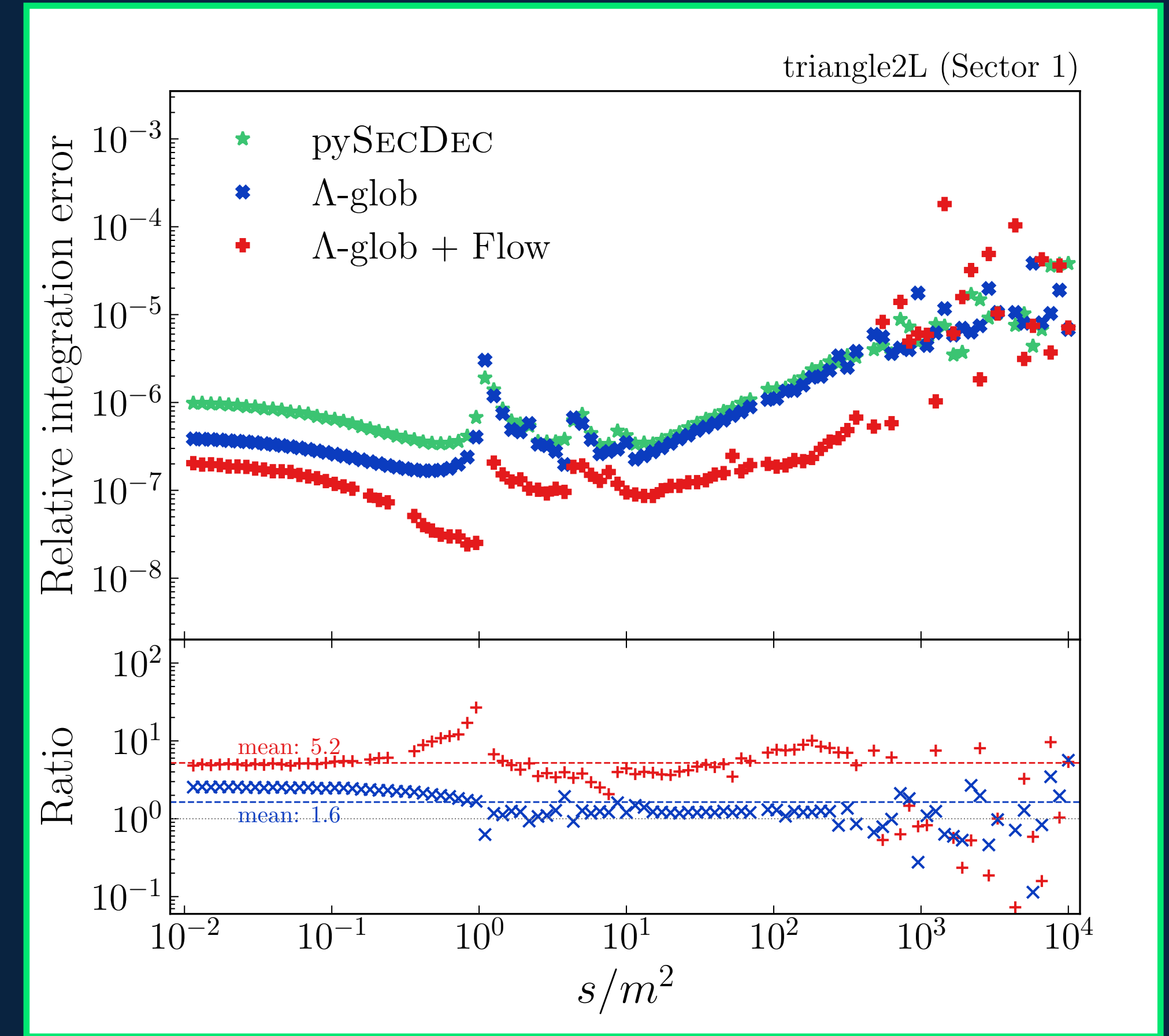
Cauchy-Theorem → Contour deformation

$$\int_0^1 \prod_{j=1}^N dx_j I(\vec{x}) = \int_{\gamma} \prod_{j=1}^N dz_j I(\vec{z})$$



Parametrize with **NF + NN**

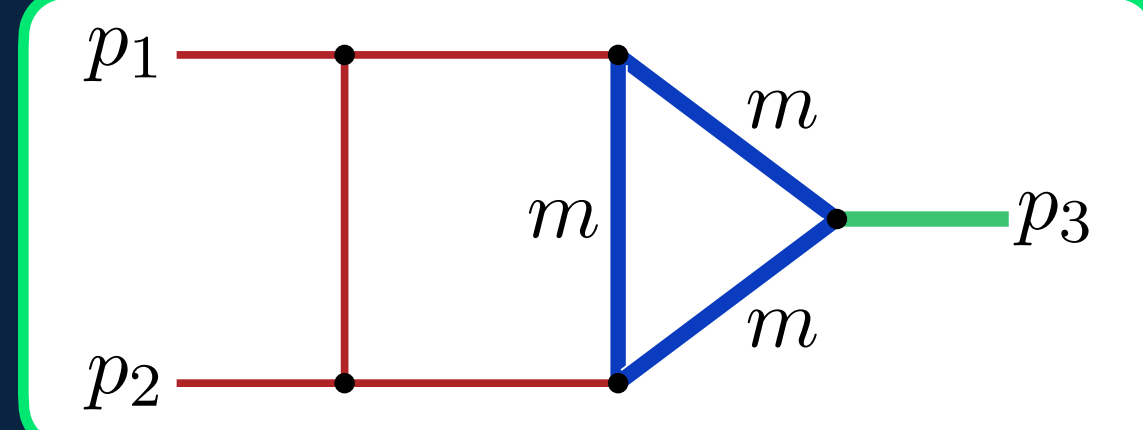
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RW, Magerya, Villa, Jones,  
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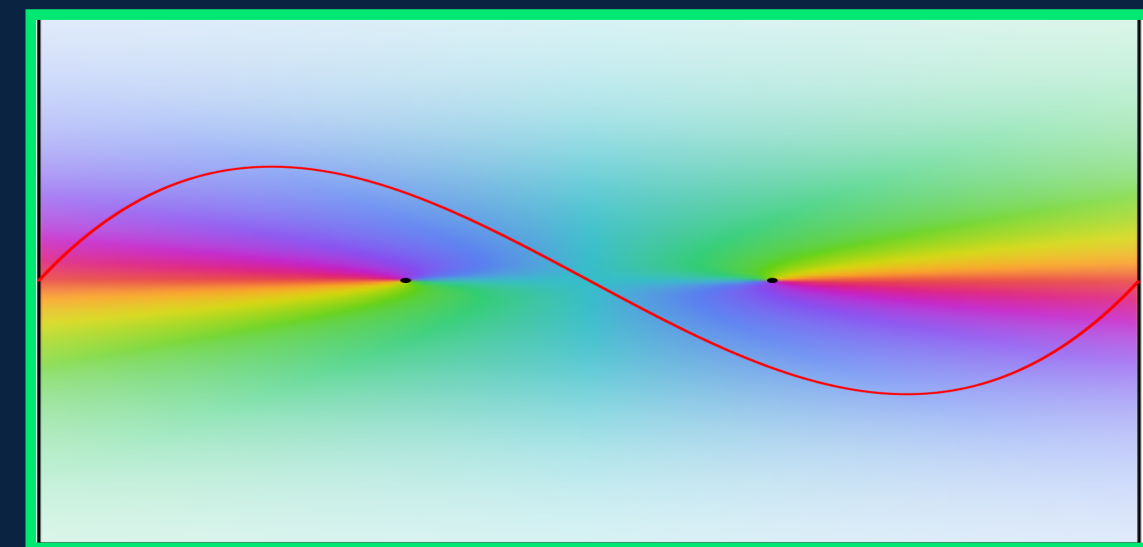
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Contains singularities

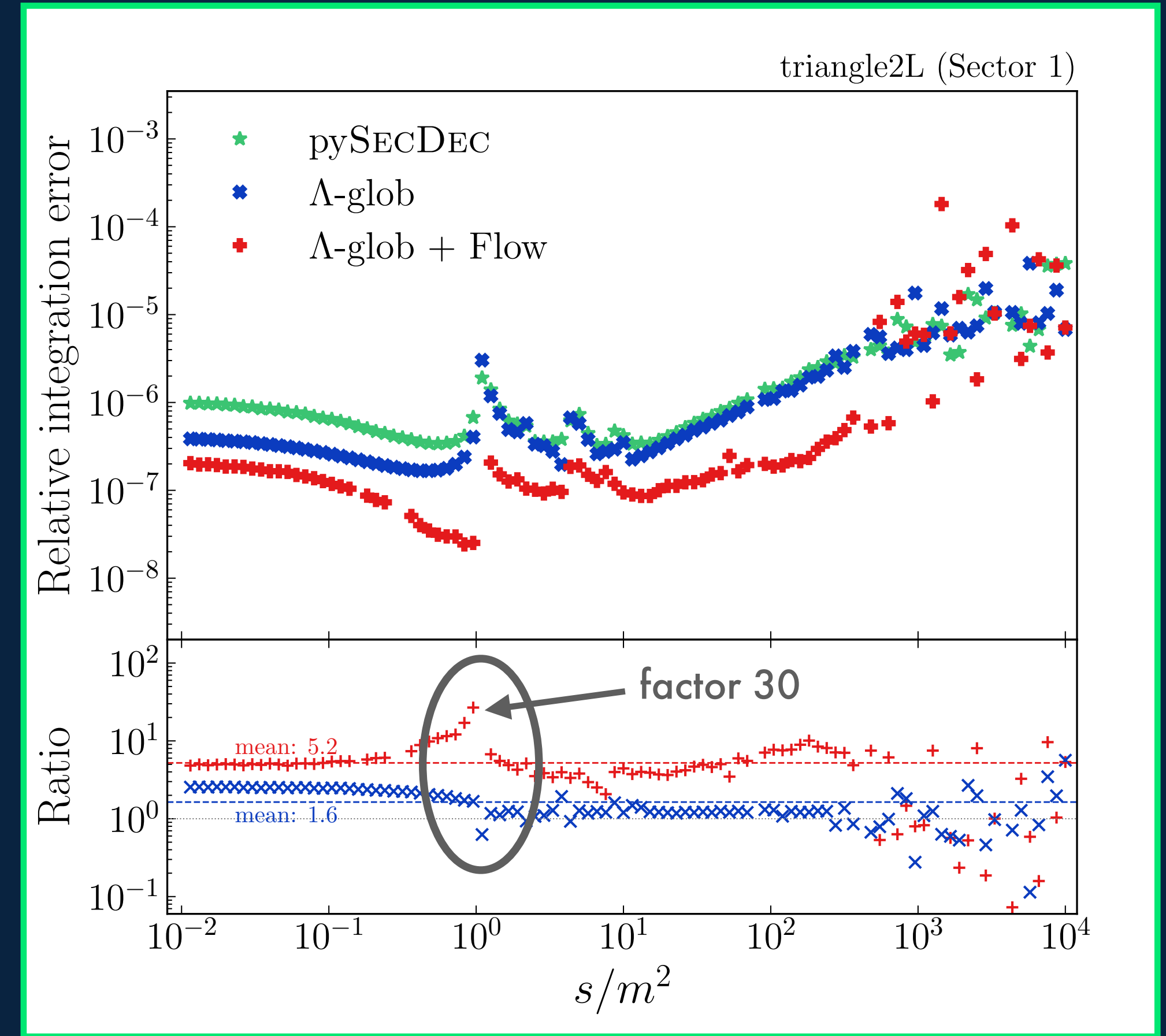
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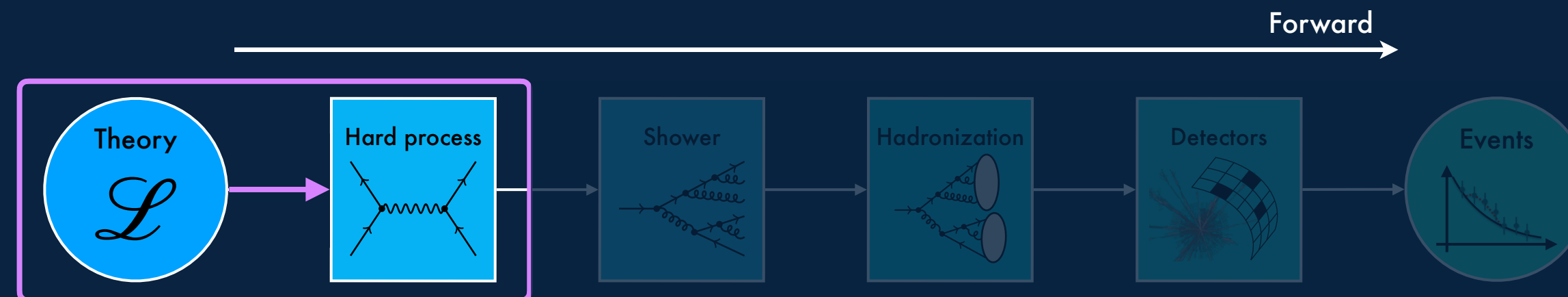
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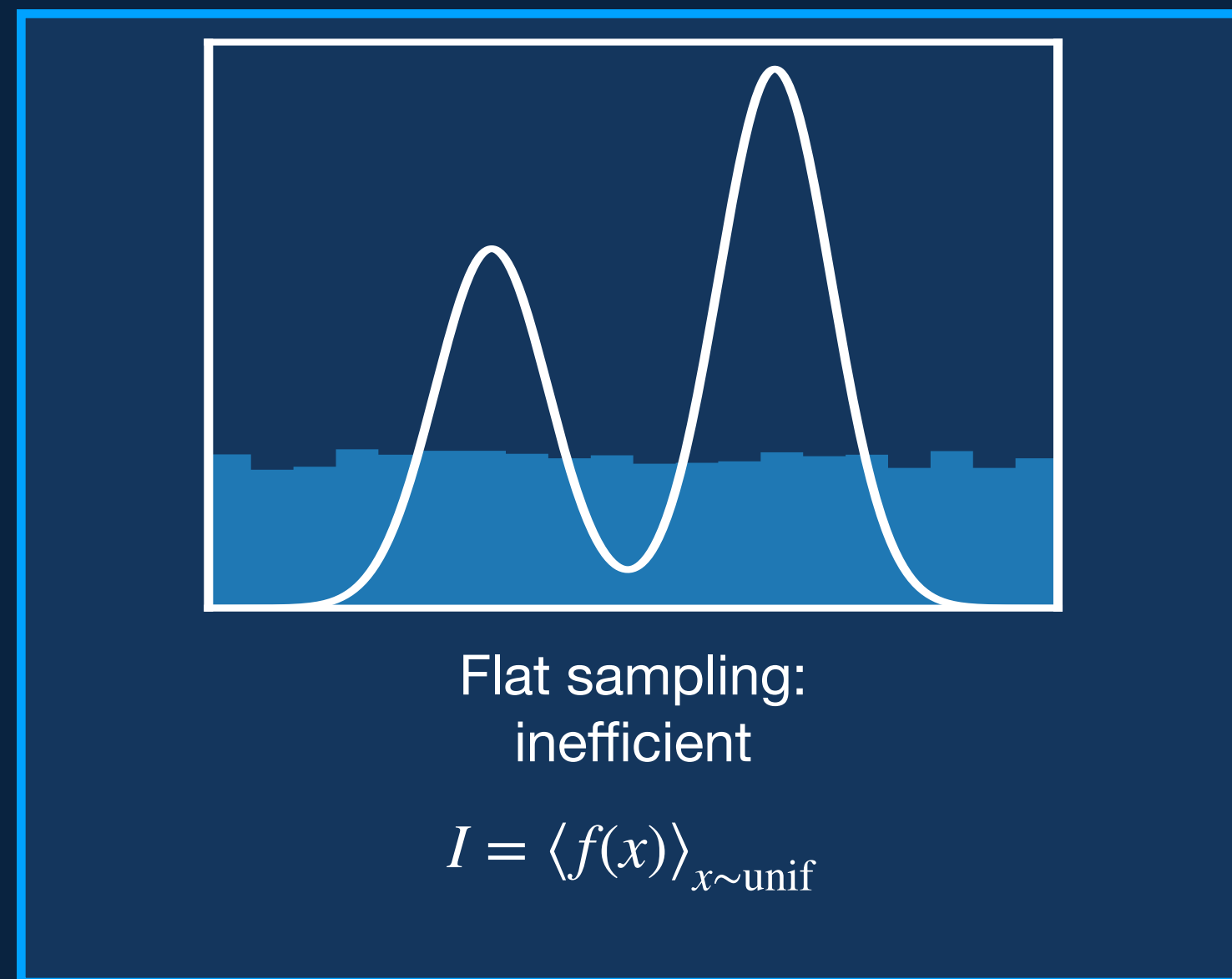


# ML for forward simulations

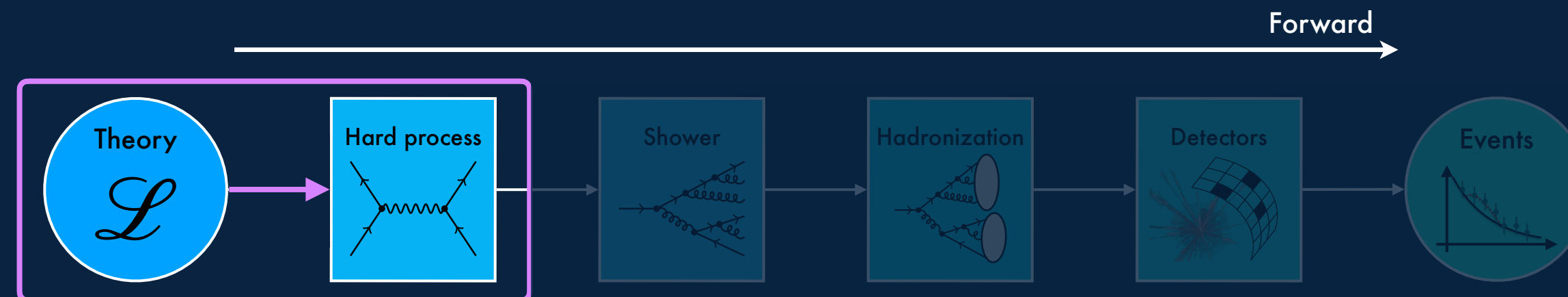


$$d\sigma \sim \text{pdf} \times |M(x)|^2 \times \text{phase space}$$

**Phase space:** increase unweighting efficiency

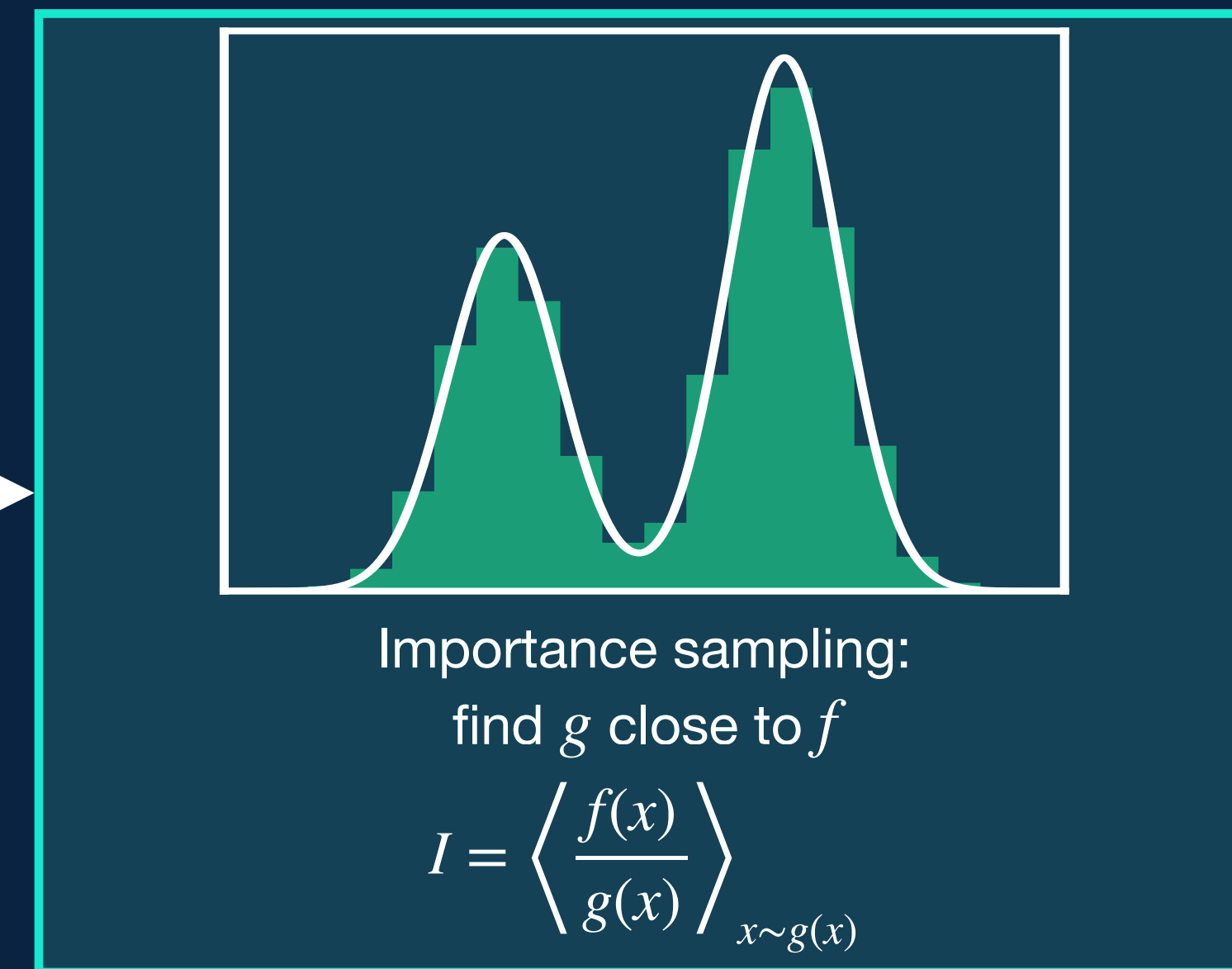
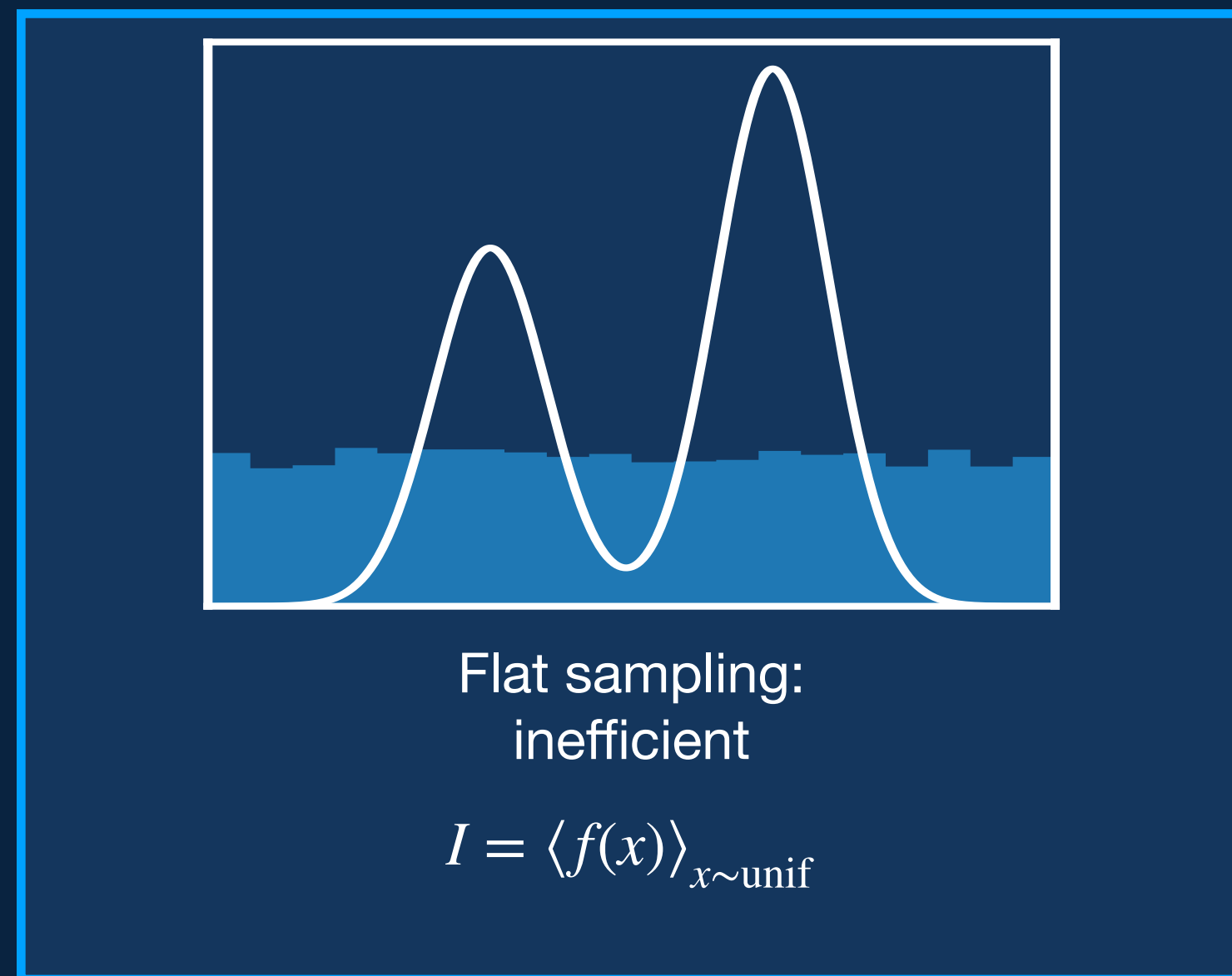


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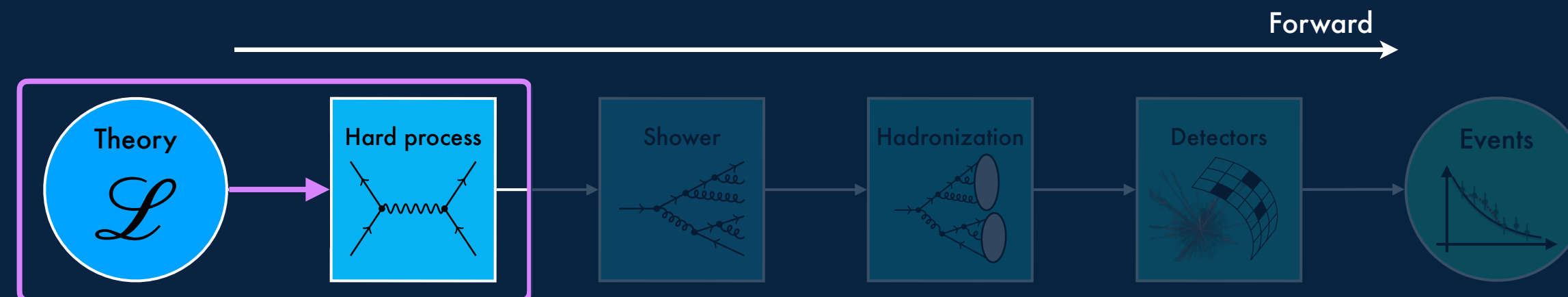


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# ML for forward simulations



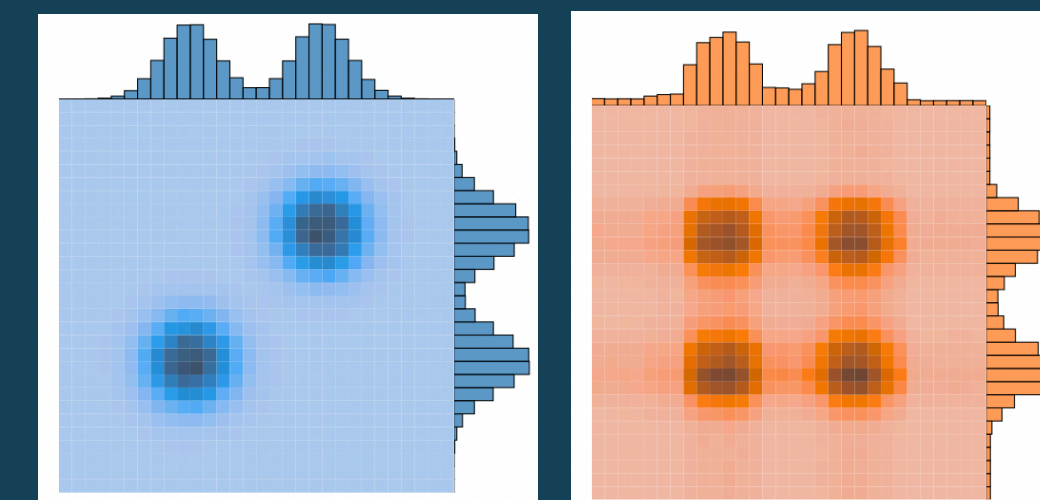
$$d\sigma \sim \text{pdf} \times |M(x)|^2 \times \text{phase space}$$

**Phase space:** increase unweighting efficiency

- Standard **VEGAS** approach → **fast** but **no correlations**

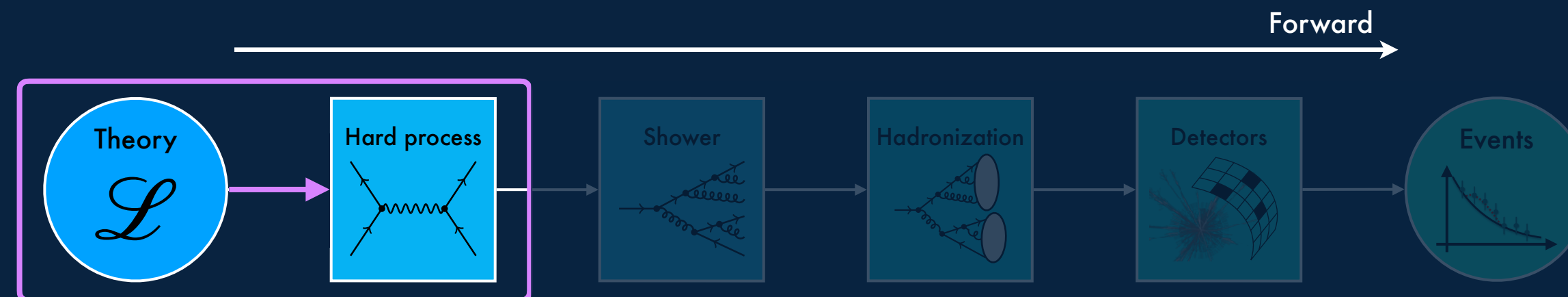
[G. P. Lepage, 1978]

- ⊕ Computationally cheap
- ⊖ High-dim and rich peaking functions → **slow convergence**
- ⊖ Peaks not aligned with grid axes → **phantom peaks**



[1707.00028, 1810.11509, 2001.05478, 2001.05486, 2001.10028, 2005.12719, 2009.07819, 2011.13445, 2109.11964, 2112.09145, 2212.06172, 2301.13562, 2309.12369, 2311.01548.....]

# ML for forward simulations



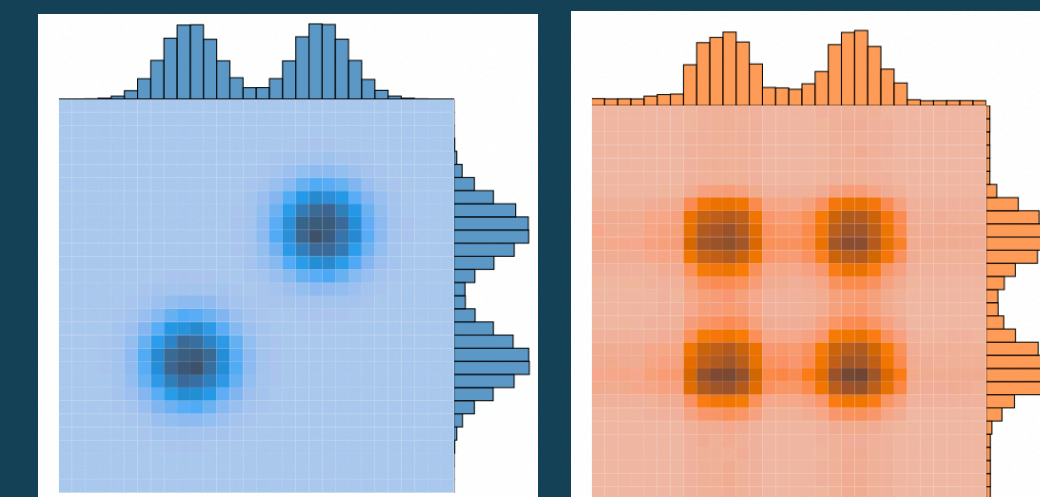
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- Standard **VEGAS** approach → **fast** but **no correlations**
- Improve with **NN** → **correlations** but **unstable**

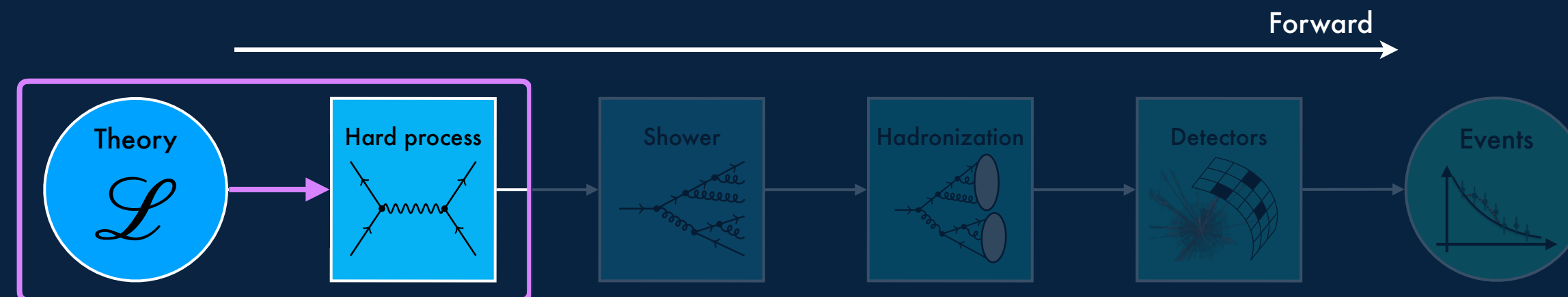
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# ML for forward simulations

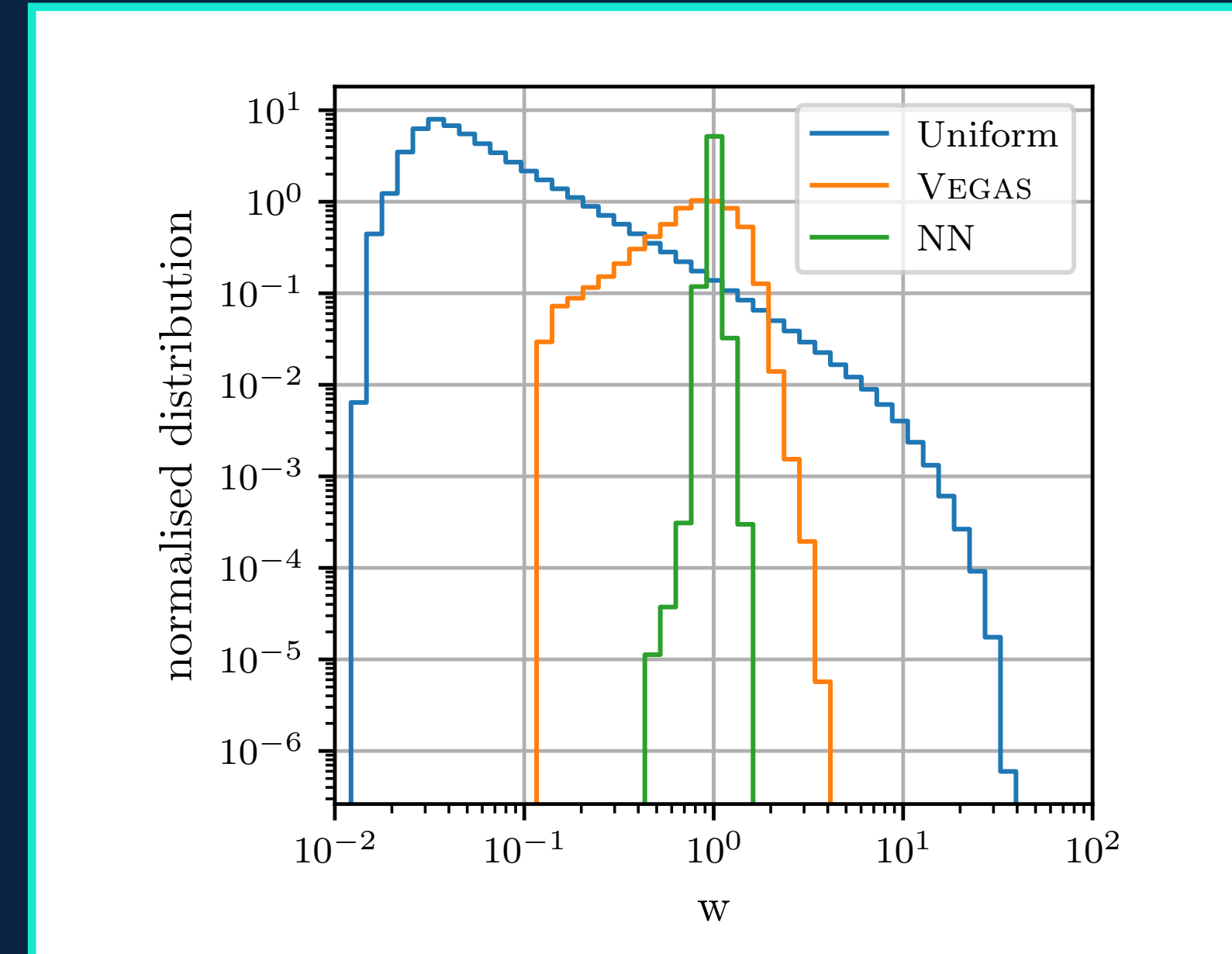


$$d\sigma \sim \text{pdf} \times |M(x)|^2 \times \text{phase space}$$

**Phase space:** increase unweighting efficiency

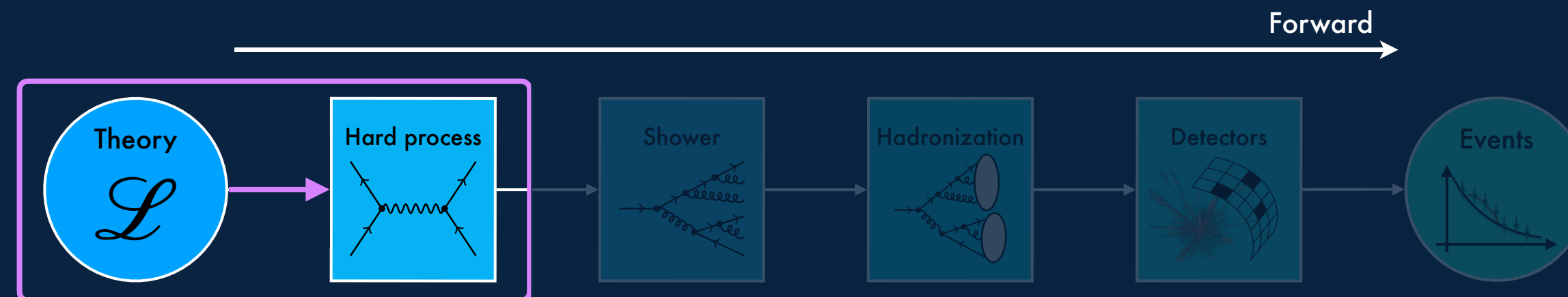
- Standard **VEGAS** approach → **fast** but **no correlations**
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- Use **normalizing flows** → **correlations** and **stable**

Bothmann, Janßen, Knobbe, Schmale, Schumann [2001.05478]



[1707.00028, 1810.11509, 2001.05478, 2001.05486, 2001.10028, 2005.12719, 2009.07819, 2011.13445, 2109.11964, 2112.09145, 2212.06172, 2301.13562, 2309.12369, 2311.01548.....]

# ML for forward simulations

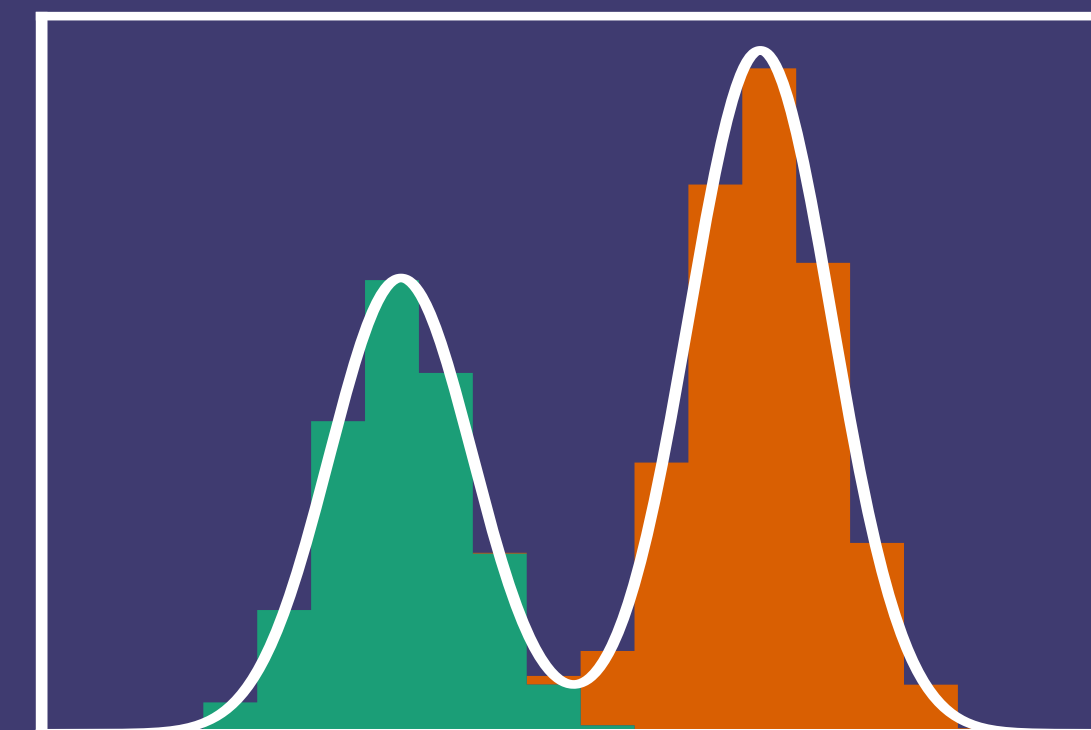


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- **Multi-channel** approach → split the integral

Kleiss, Pittau [hep-ph/9405257], Maltoni, Stelzer [hep-ph/0208156]

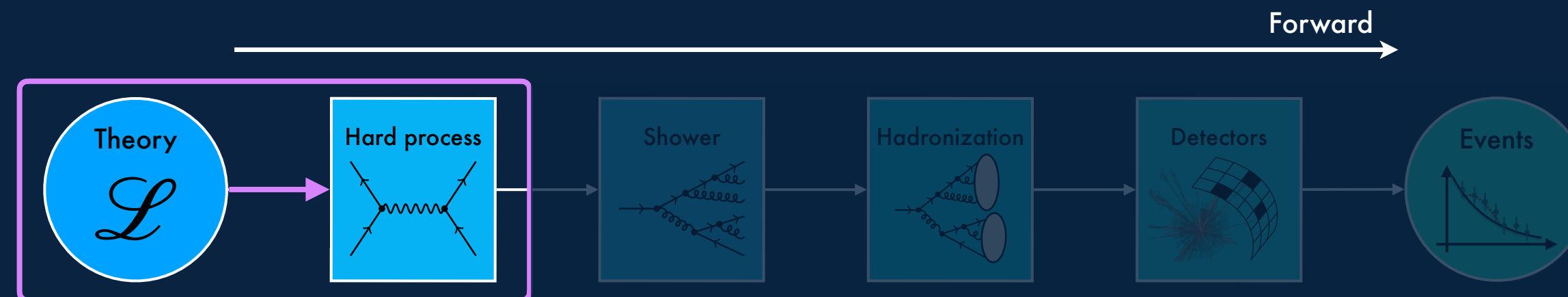


Multi-channel:  
one map for each channel

$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{g_i(x)} \right\rangle_{x \sim g_i(x)}$$

[1707.00028, 1810.11509, 2001.05478, 2001.05486, 2001.10028, 2005.12719, 2009.07819, 2011.13445, 2109.11964, 2112.09145, 2212.06172, 2301.13562, 2309.12369, 2311.01548.....]

# ML for forward simulations



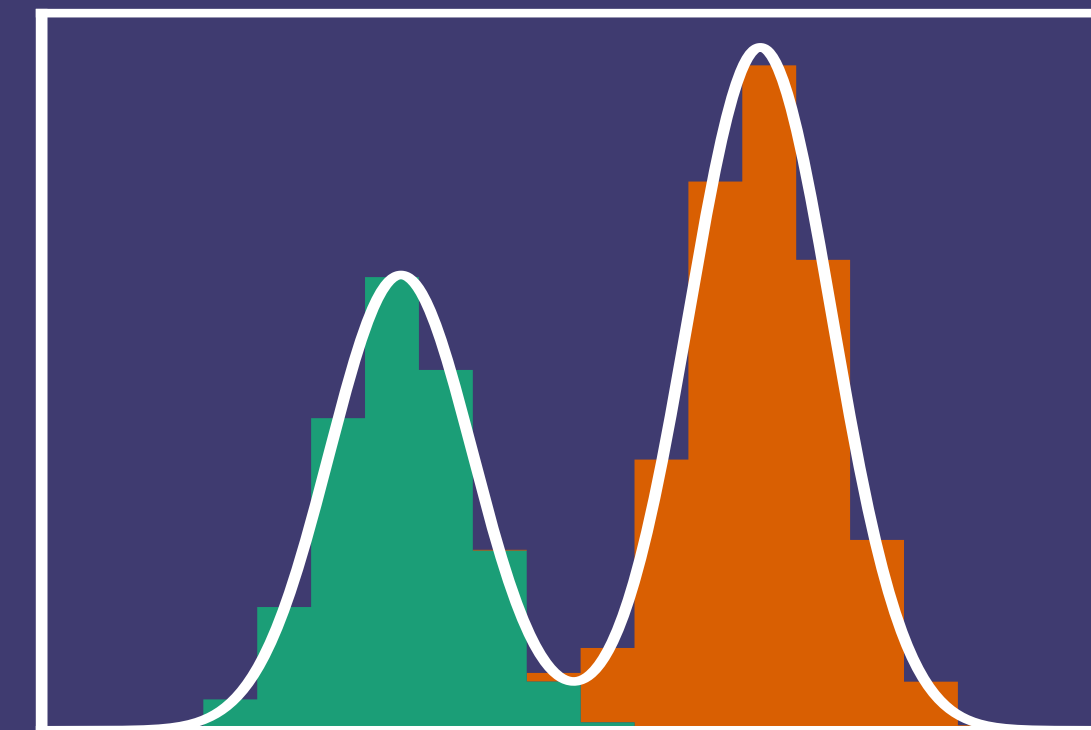
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- Improve with **NN** → **correlations** but **unstable**
- Use **normalizing flows** → **correlations** and **stable**
- **Multi-channel** approach → split the integral
- Combine all (VEGAS, learned  $\alpha_i$ , NF, symmetries,..) → **MadNIS** framework

[1707.00028, 1810.11509, 2001.05478, 2001.05486, 2001.10028, 2005.12719, 2009.07819, 2011.13445, 2109.11964, 2112.09145, 2212.06172, 2301.13562, 2309.12369, 2311.01548.....]

Kleiss, Pittau [hep-ph/9405257], Maltoni, Stelzer [hep-ph/0208156]



Multi-channel:  
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$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{g_i(x)} \right\rangle_{x \sim g_i(x)}$$

# MadNIS

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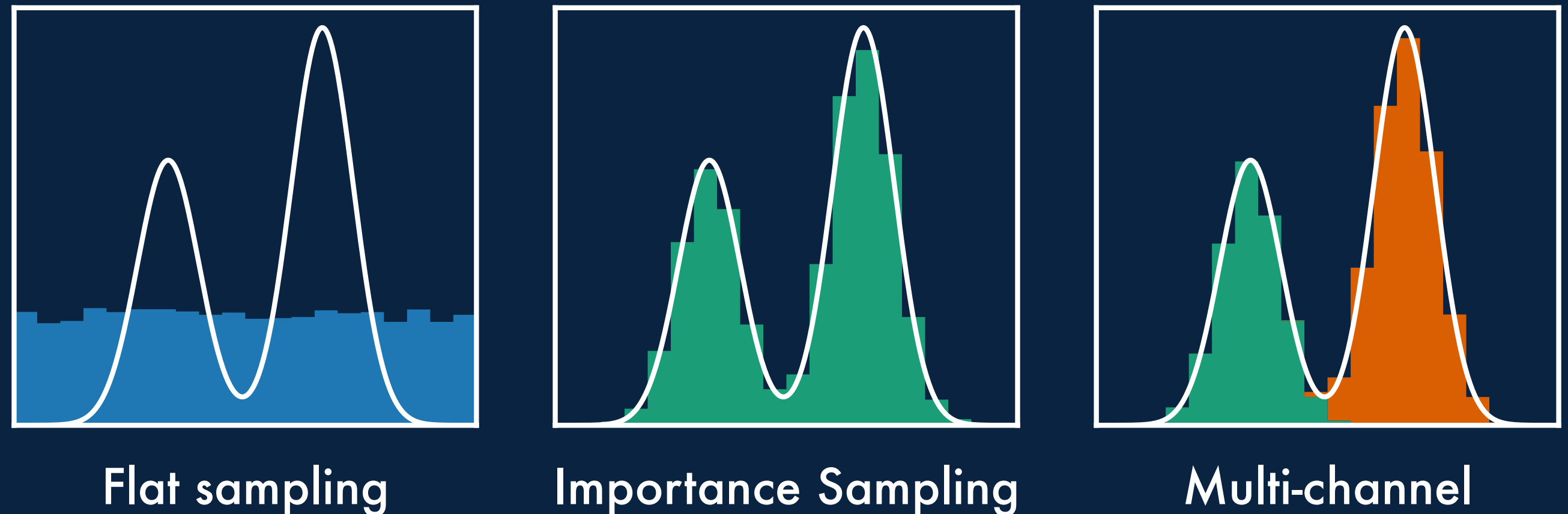
## Neural Importance Sampling

Heimel, Huetsch, Maltoni, Mattelaer, Plehn, RW [[2311.01548](#)]

Heimel, RW, Butter, Isaacson, Krause, Maltoni, Mattelaer, Plehn [[2212.06172](#)]



# MadNIS — Neural importance sampling

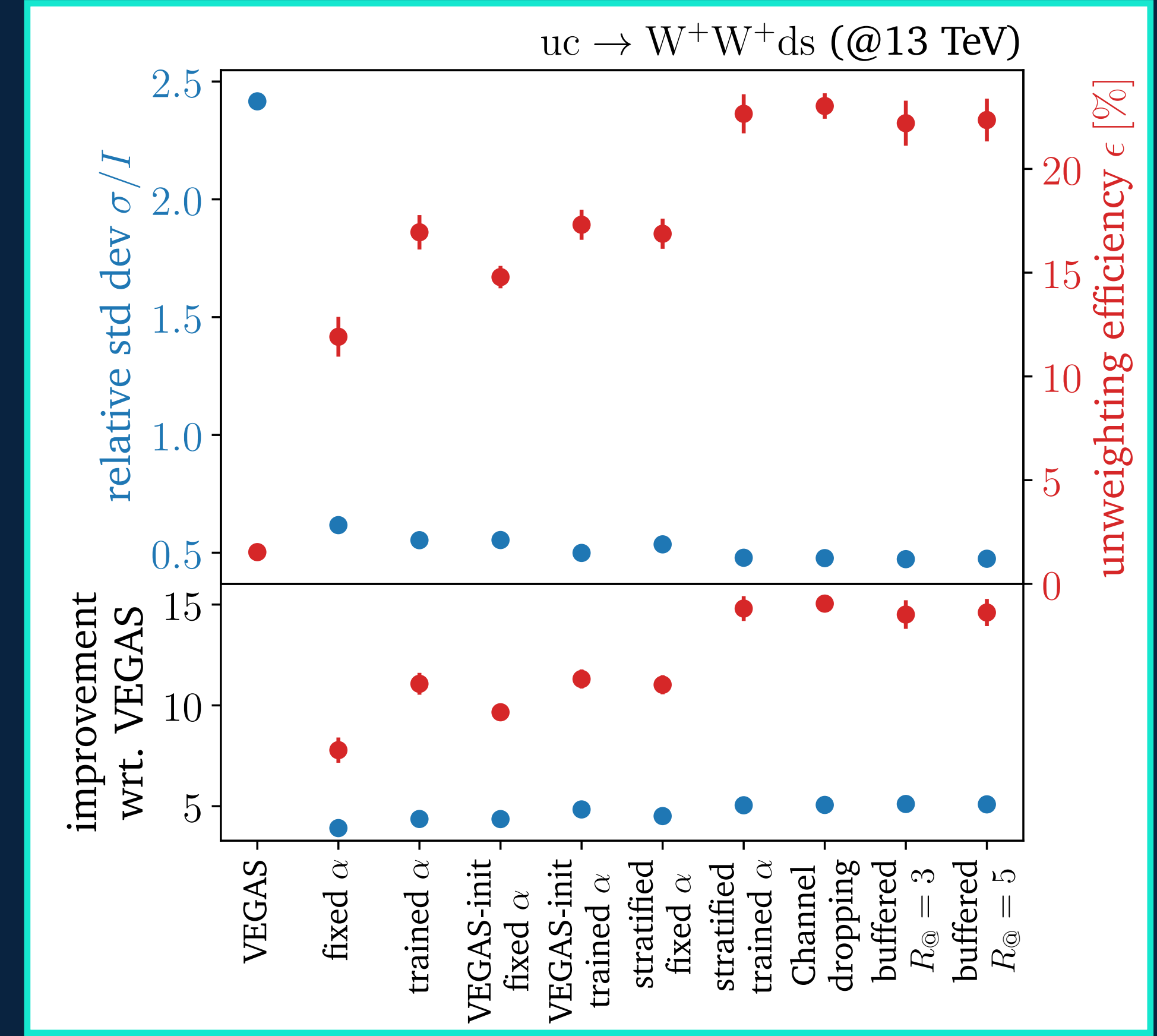


$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{g_i(x)} \right\rangle_{x \sim g_i(x)}$$

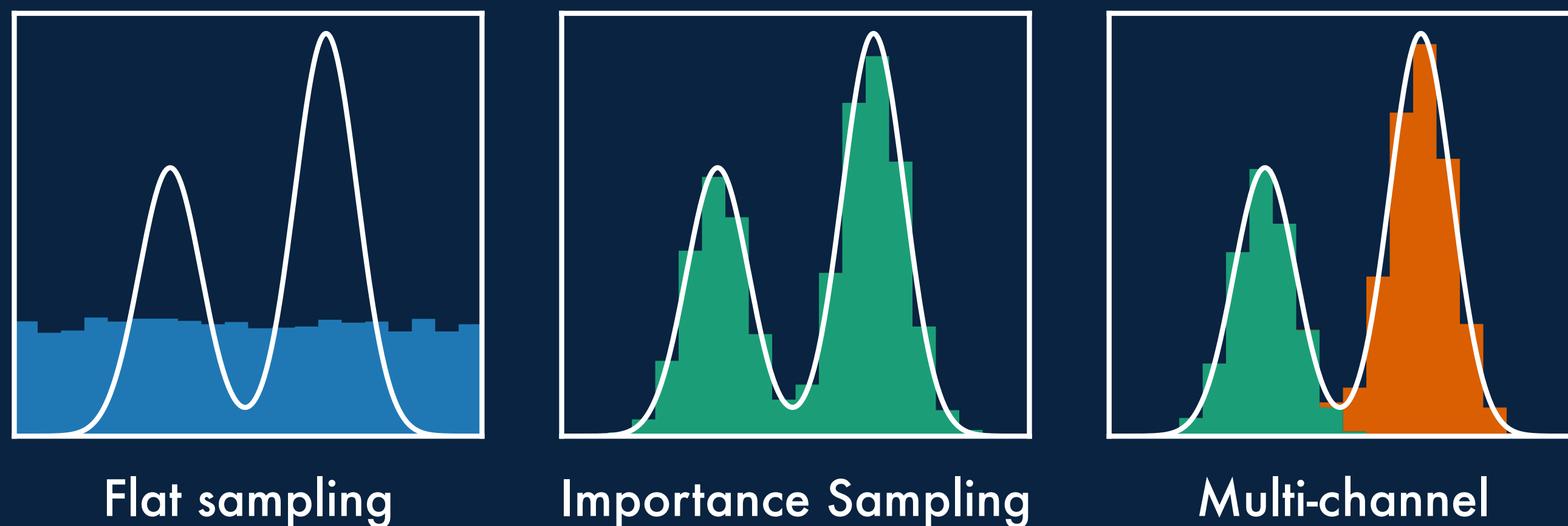
Parametrize with **NN**

Parametrize with **NF**

Heimel, Huetsch, Maltoni, Mattelear, Plehn, RW [2311.01548]



# MadNIS — Neural importance sampling



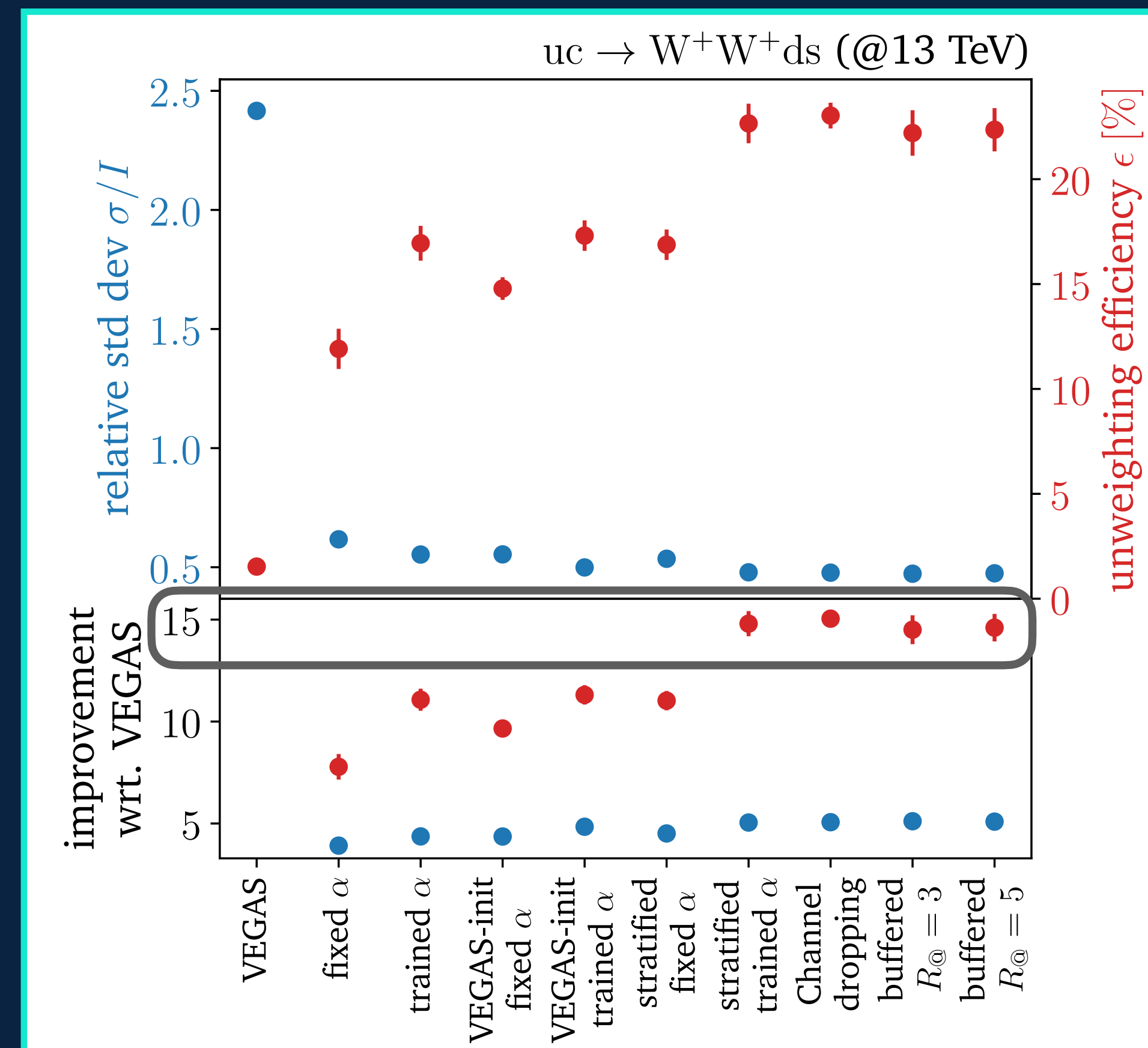
$$I = \sum_i \left\langle \alpha_i(x) \frac{f(x)}{g_i(x)} \right\rangle_{x \sim g_i(x)}$$

Parametrize with **NN**

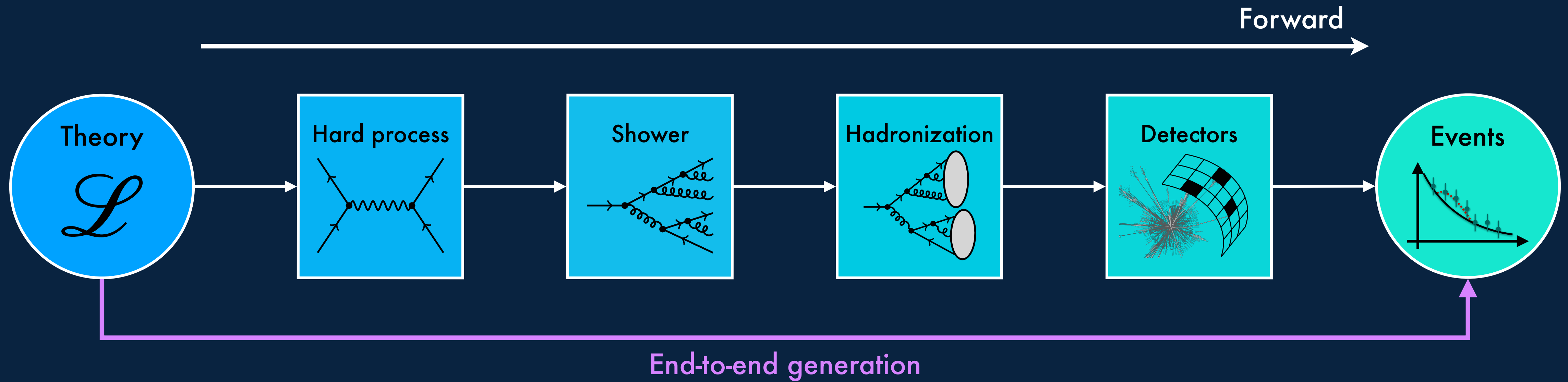
Parametrize with **NF**

→ Details in talk by **Theo Heimerl**

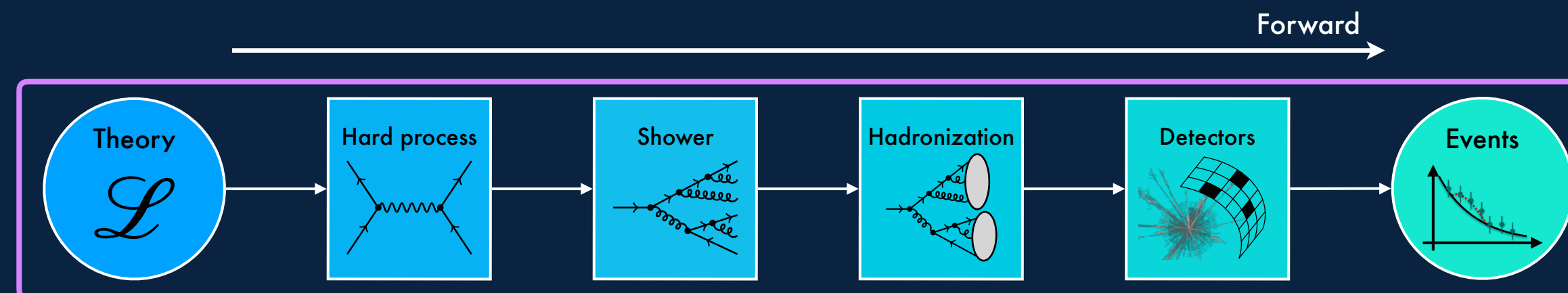
Heimerl, Huetsch, Maltoni, Mattelear, Plehn, RW [2311.01548]



# ML for forward simulations



# ML for forward simulations

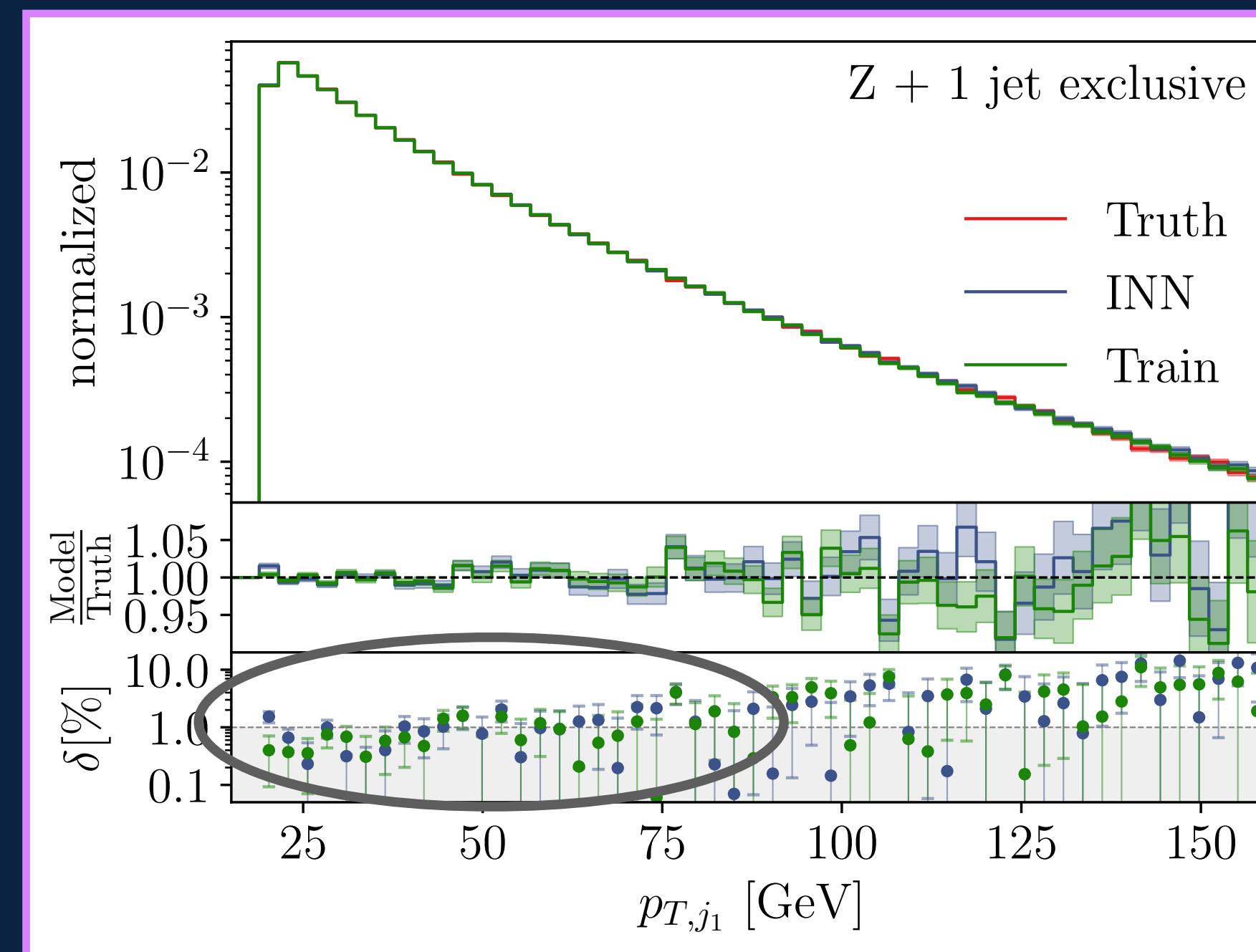


End-to-end generators learn multiple steps at once

Butter, Heimes, Hummerich, Krebs, Plehn, Rousselot, Vent [2110.13632]

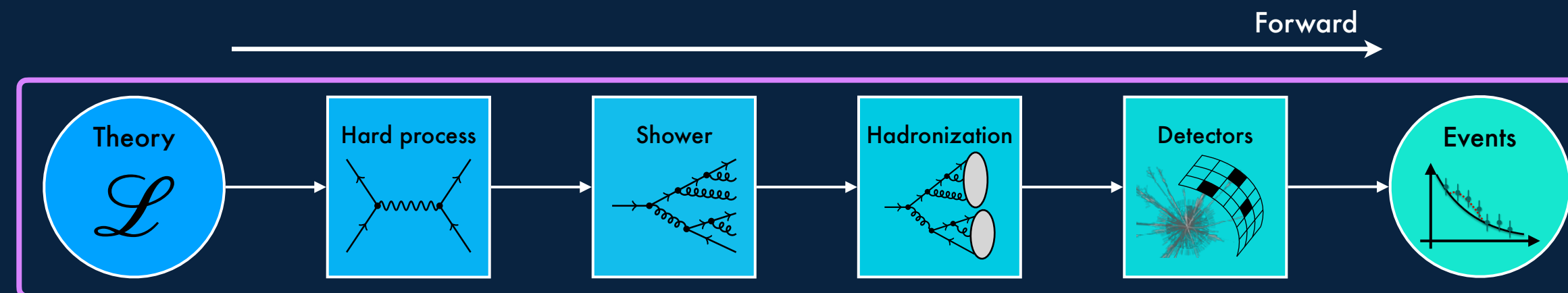
## Precision generation

- First attempts based on **GANs and VAEs**
- Improved speed and efficiency with **Flows**



[1901.00875, 1901.05282, 1903.02433, 1907.03764, 1912.02748, 2001.11103, 2011.13445, 2101.08944, 2110.13632, 2211.13630, 2303.05376, 2305.07696, 2305.10475, 2305.16774, 2307.06836 .....]

# ML for forward simulations



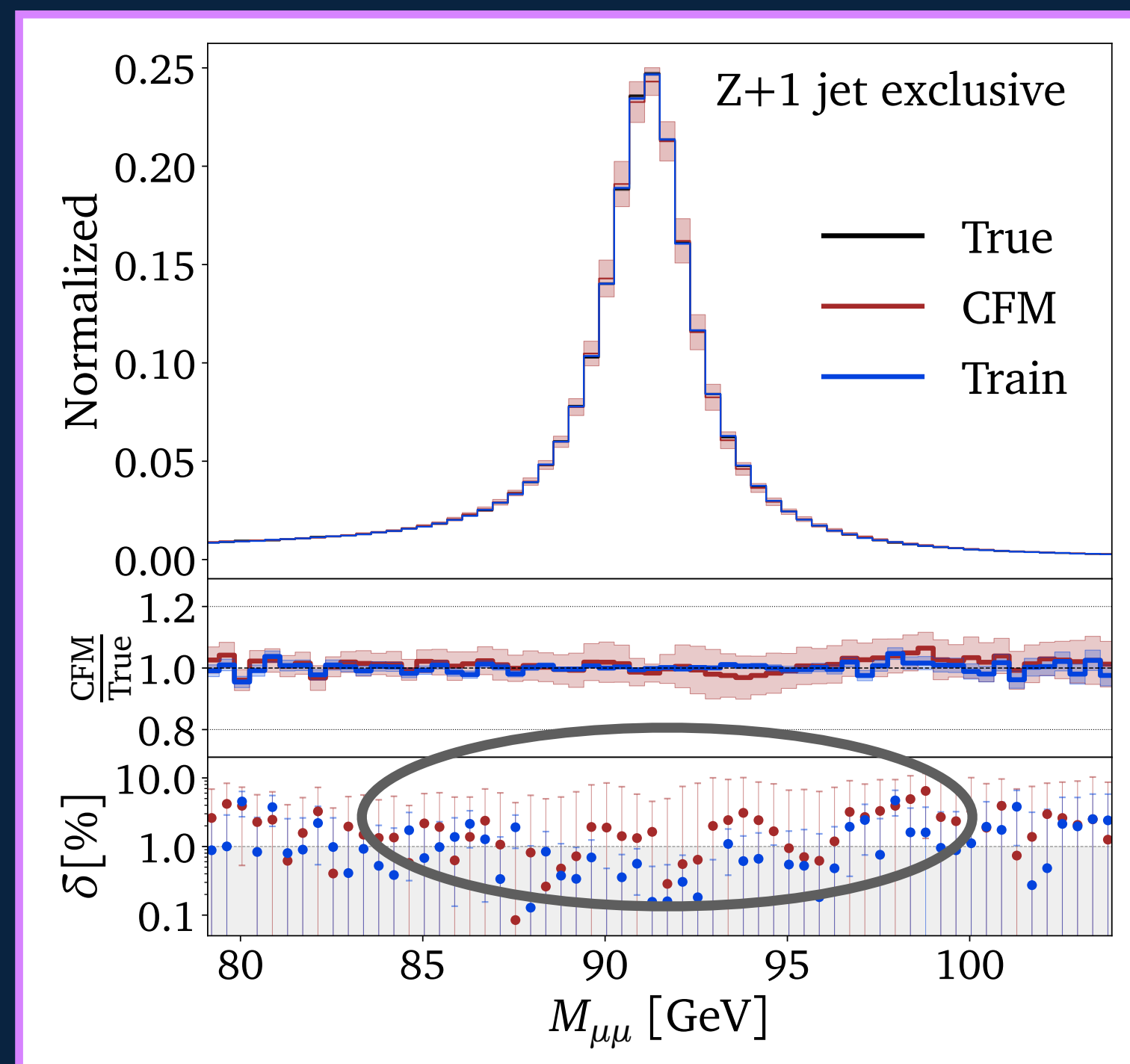
End-to-end generators learn multiple steps at once

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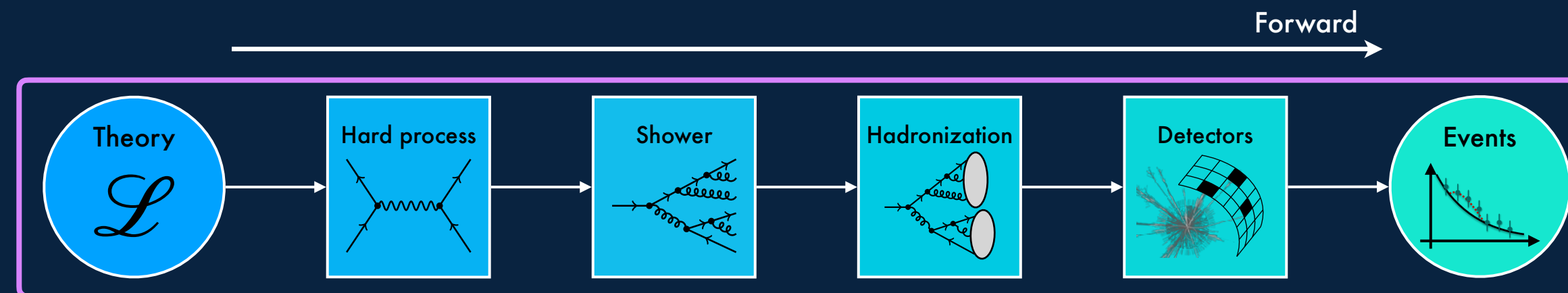
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[1901.00875, 1901.05282, 1903.02433, 1907.03764, 1912.02748, 2001.11103, 2011.13445, 2101.08944, 2110.13632, 2211.13630, 2303.05376, 2305.07696, 2305.10475, 2305.16774, 2307.06836 .....]

Butter, Huetsch, Schweitzer, Plehn, Sorrenson, Spinner [2110.11377]



# ML for forward simulations



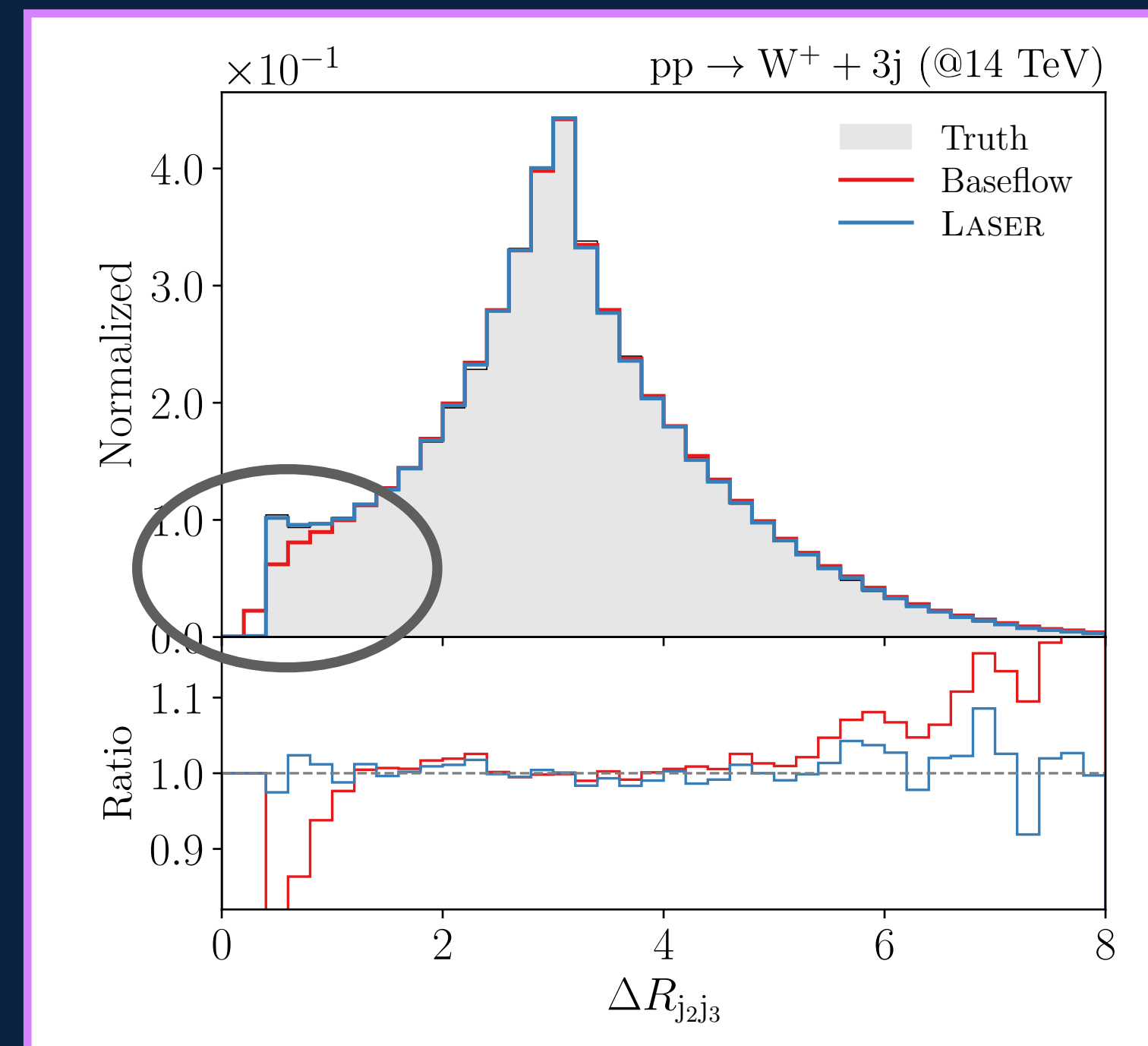
End-to-end generators learn multiple steps at once

## Precision generation

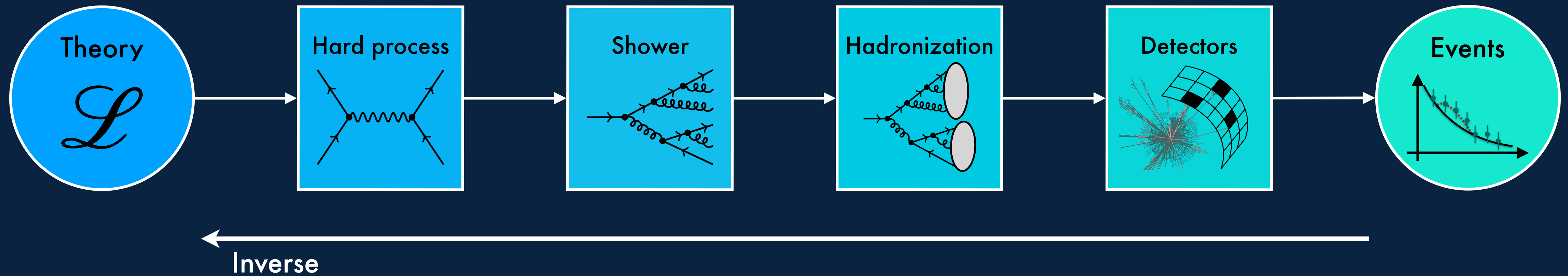
- First attempts based on **GANs and VAEs**
- Improved speed and efficiency with **Flows**
- High precision with **Diffusion** and **Transformer** models
- **Bayesian NN** and **classifiers** for full control

[1901.00875, 1901.05282, 1903.02433, 1907.03764, 1912.02748, 2001.11103, 2011.13445, 2101.08944, 2110.13632, 2211.13630, 2303.05376, 2305.07696, 2305.10475, 2305.16774, 2307.06836 .....]

Nachman, RW [2305.07696]

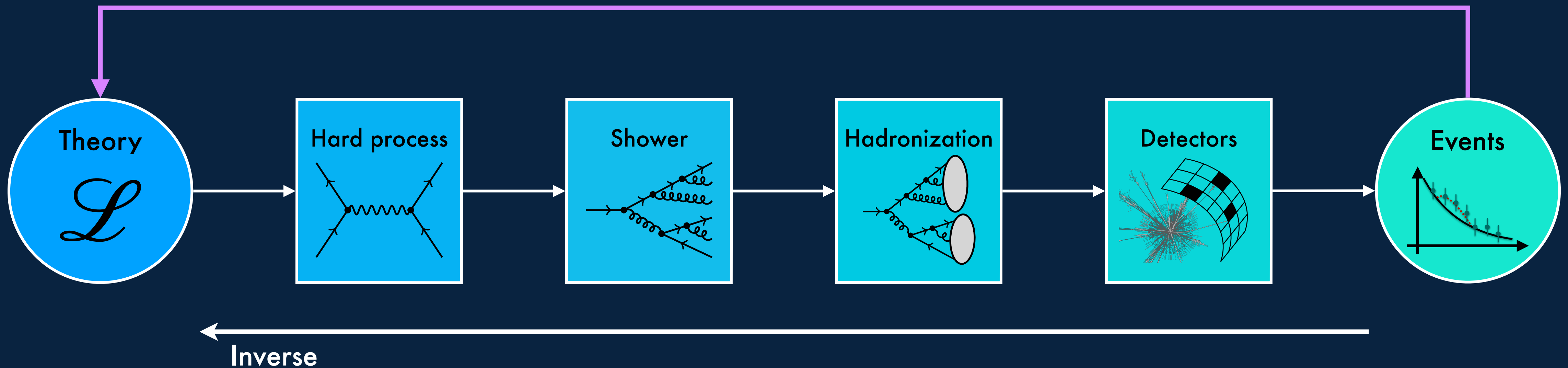


# ML for inverse simulations



# ML for inverse simulations

## Matrix Element Method



**Historically** → **Tevatron**

Top mass: D0 (98', 04'), CDF 06', Fiedler et al. [1003.1316]

Single-top: Review [1710.10699]



# MEM-ML

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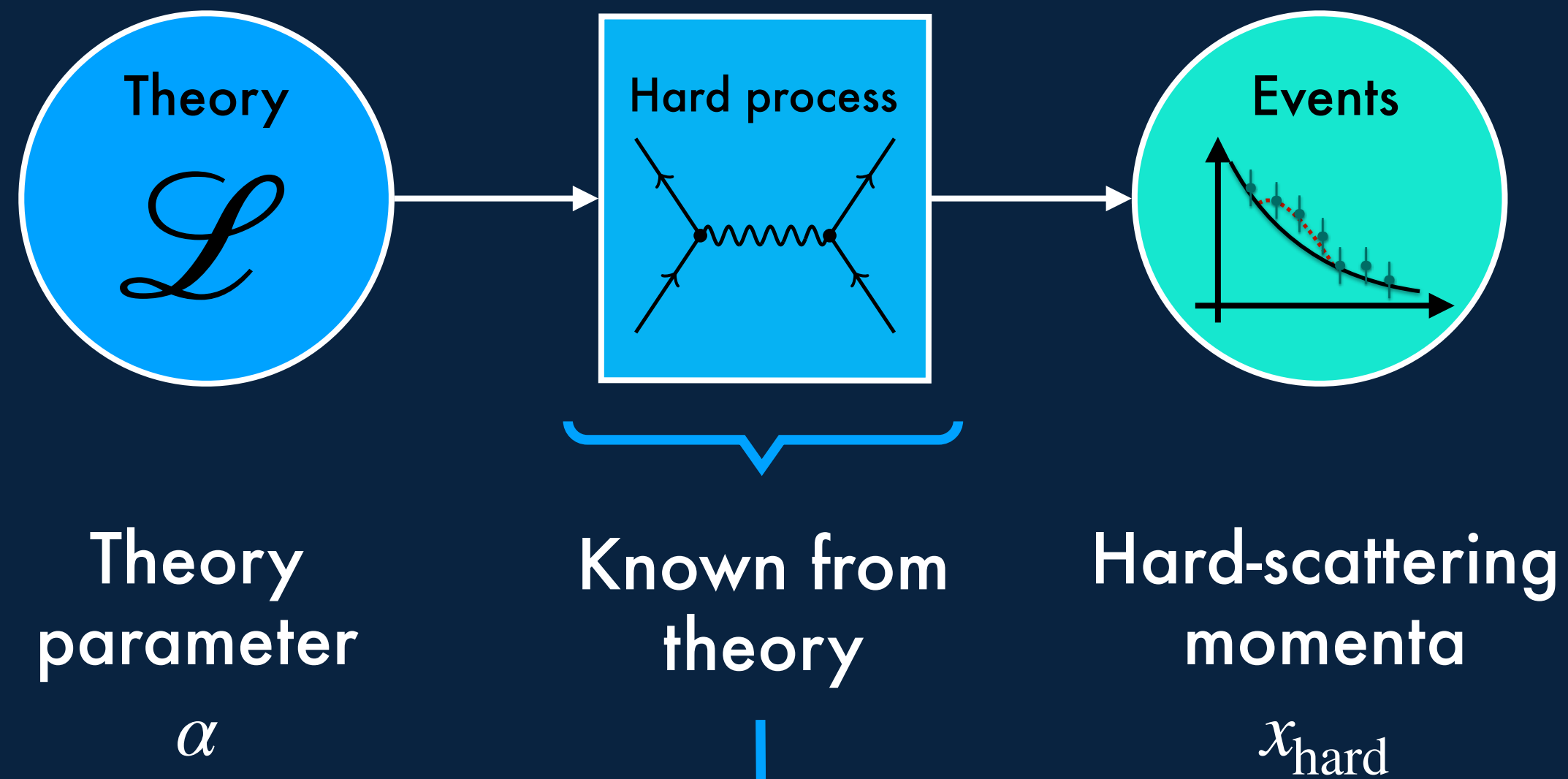
## Matrix Element Method

Heimel, Huetsch, RW, Plehn, Butter [[2310.07752](#)]

Butter, Heimel, Martini, Peitzsch, Plehn [[2210.00019](#)]

# Matrix Element Method – Theory

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Likelihood from differential cross section

$$p(x_{\text{hard}} | \alpha) = \frac{1}{\sigma(\alpha)} \frac{d\sigma(\alpha)}{dx_{\text{hard}}}$$

## Classical analysis

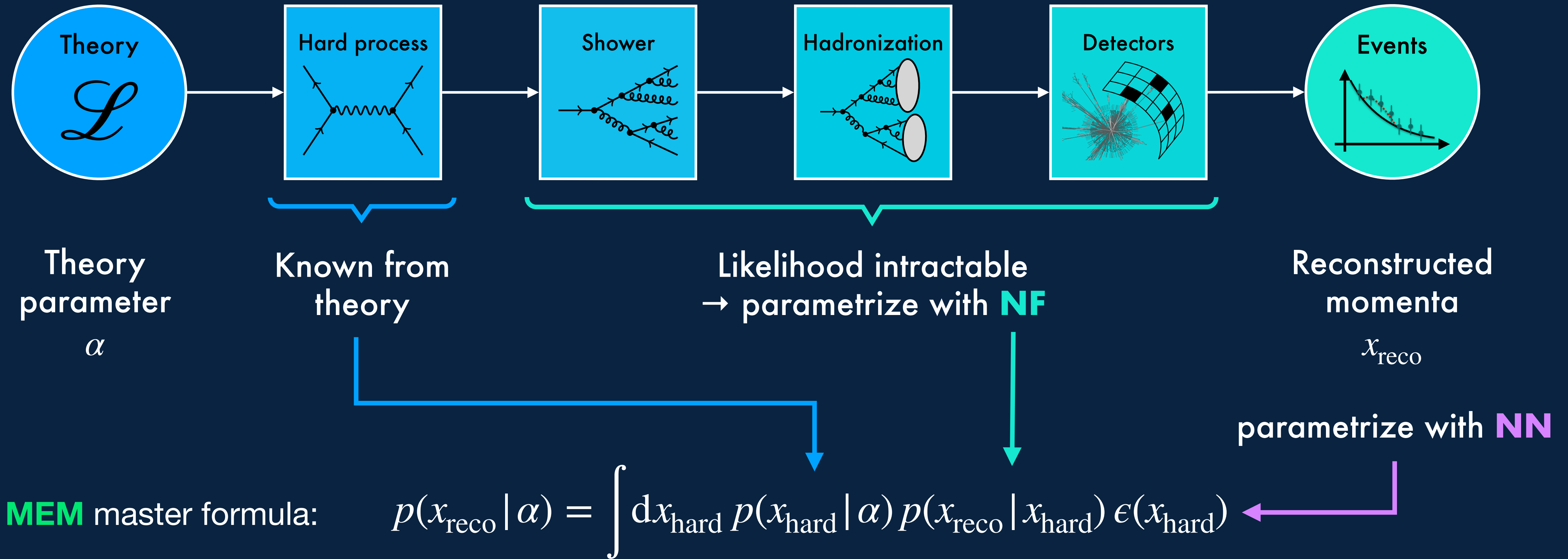
- ⊖ hand-crafted observables
- ⊖ binned data
- not all information is used 😞



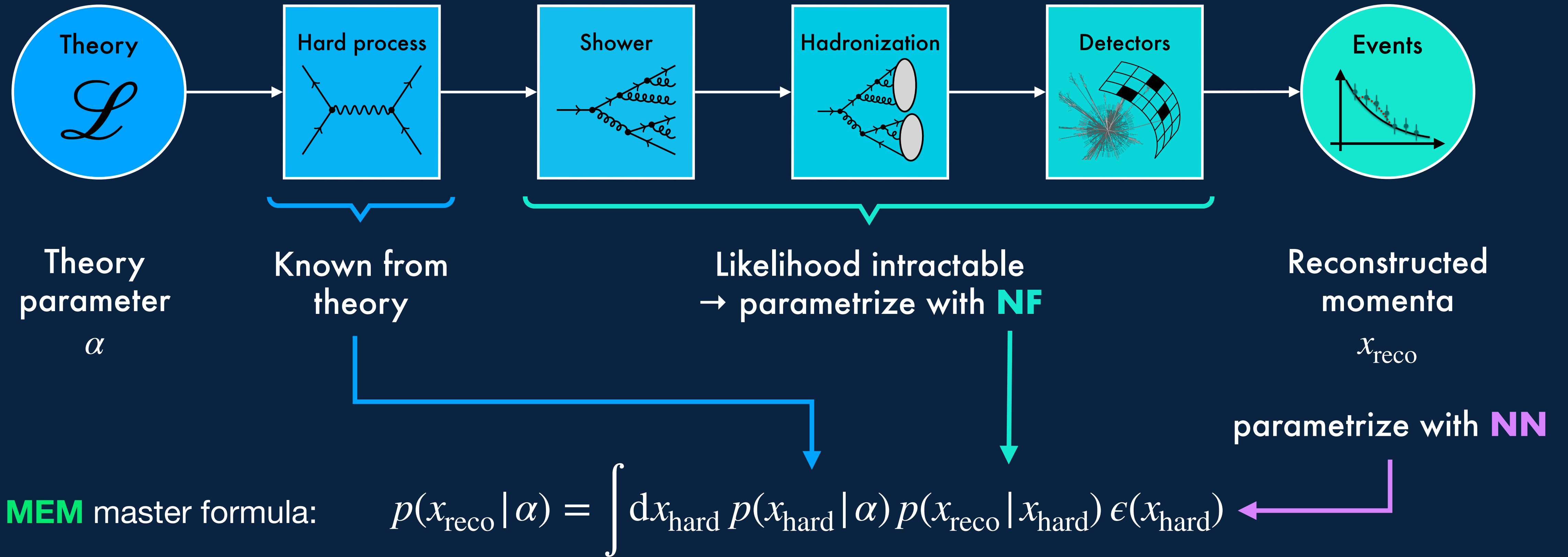
## Matrix Element Method (MEM)

- ⊕ based on first principles
- ⊕ estimates uncertainties reliably
- ⊕ optimal use of information
- perfect for processes with few events 😊

# Matrix Element Method – Reality



# Matrix Element Method – Reality

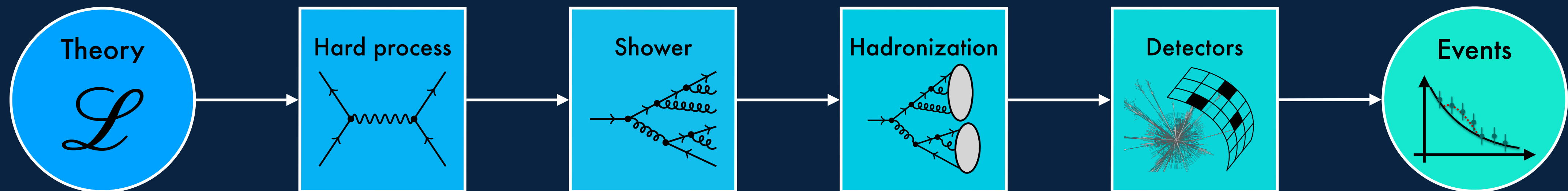


→ Details in talk by **Nathan Huetsch**

# Summary and Outlook

## Take-home message

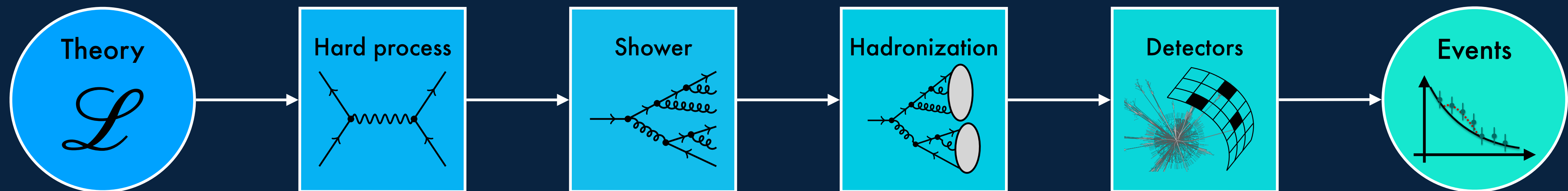
- ML beneficial in **every step** in the simulation chain
- We find both **proof-of-concepts** as well as established use cases ( $\rightarrow$  **MadNIS**)
- Interesting **interplay** between **HEP** and **ML**



# Summary and Outlook

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→ HEP simulations provide **~infinite data** for ML

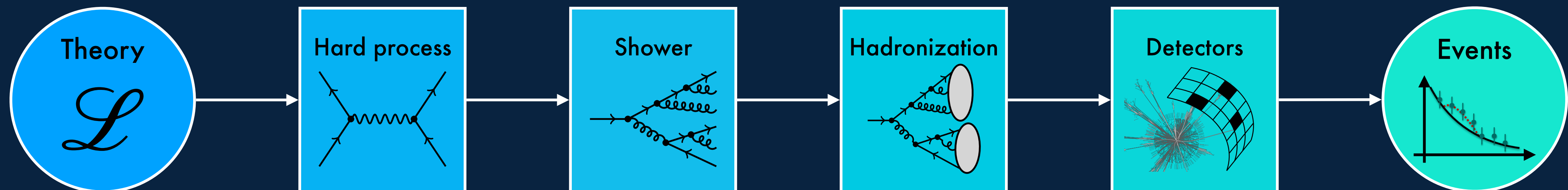


# Summary and Outlook

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## Take-home message

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  - HEP simulations provide **~infinite data** for ML
  - HEP requirements (**precision, symmetries,...**) **different** than industry applications



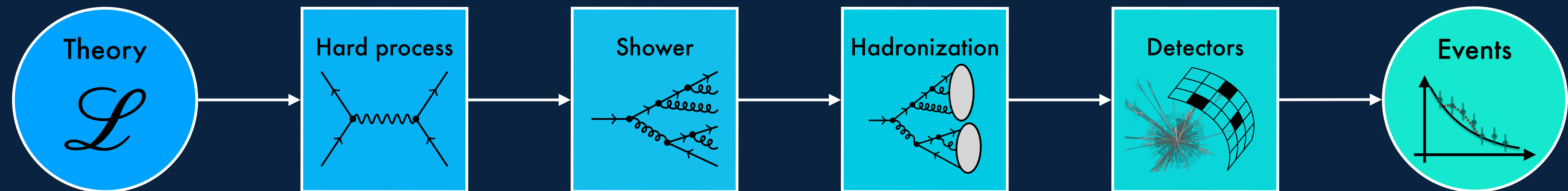
# Summary and Outlook

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## Future tasks

- **Full integration** of ML-based simulations into standard tools → **MadGraph,....**
- Make everything run on the **GPU and differentiable** (MadJax - Heinrich et al. [[2203.00057](#)])
- Further foster collaboration between **theory, experiment, and ML** community





# Summary and Outlook

## Machine learning and LHC event generation

Anja Butter<sup>1,2</sup>, Tilman Plehn<sup>1</sup>, Steffen Schumann<sup>3</sup>, Simon Badger<sup>4</sup>, Sascha Caron<sup>5,6</sup>, Kyle Cranmer<sup>7,8</sup>, Francesco Armando Di Bello<sup>9</sup>, Etienne Dreyer<sup>10</sup>, Stefano Forte<sup>11</sup>, Sanmay Ganguly<sup>12</sup>, Dorival Gonçalves<sup>13</sup>, Eilam Gross<sup>10</sup>, Theo Heimel<sup>1</sup>, Gudrun Heinrich<sup>14</sup>, Lukas Heinrich<sup>15</sup>, Alexander Held<sup>16</sup>, Stefan Höche<sup>17</sup>, Jessica N. Howard<sup>18</sup>, Philip Ilten<sup>19</sup>, Joshua Isaacson<sup>17</sup>, Timo Janßen<sup>3</sup>, Stephen Jones<sup>20</sup>, Marumi Kado<sup>9,21</sup>, Michael Kagan<sup>22</sup>, Gregor Kasieczka<sup>23</sup>, Felix Kling<sup>24</sup>, Sabine Kraml<sup>25</sup>, Claudius Krause<sup>26</sup>, Frank Krauss<sup>20</sup>, Kevin Kröniger<sup>27</sup>, Rahool Kumar Barman<sup>13</sup>, Michel Luchmann<sup>1</sup>, Vitaly Magerya<sup>14</sup>, Daniel Maitre<sup>20</sup>, Bogdan Malaescu<sup>2</sup>, Fabio Maltoni<sup>28,29</sup>, Till Martini<sup>30</sup>, Olivier Mattelaer<sup>28</sup>, Benjamin Nachman<sup>31,32</sup>, Sebastian Pitz<sup>1</sup>, Juan Rojo<sup>6,33</sup>, Matthew Schwartz<sup>34</sup>, David Shih<sup>25</sup>, Frank Siegert<sup>35</sup>, Roy Stegeman<sup>11</sup>, Bob Stienen<sup>5</sup>, Jesse Thaler<sup>36</sup>, Rob Verheyen<sup>37</sup>, Daniel Whiteson<sup>18</sup>, Ramon Winterhalder<sup>28</sup>, and Jure Zupan<sup>19</sup>

### Abstract

First-principle simulations are at the heart of the high-energy physics research program. They link the vast data output of multi-purpose detectors with fundamental theory predictions and interpretation. This review illustrates a wide range of applications of modern machine learning to event generation and simulation-based inference, including conceptual developments driven by the specific requirements of particle physics. New ideas and tools developed at the interface of particle physics and machine learning will improve the speed and precision of forward simulations, handle the complexity of collision data, and enhance inference as an inverse simulation problem.

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- Make everything run on the **GPU and differentiable** (MadJax - Heinrich et al. [2203.00057])
- Further foster collaboration between **theory, experiment, and ML** community
- More details in our **Snowmass report**

