

# Nuclear physics: the ISOLDE facility

Lecture 2: Science of ISOLDE

Meet ISOLDE trailer:

https://videos.cern.ch/record/2285037

Magdalena Kowalska CERN, PH-Dept.

kowalska@cern.ch

on behalf of the CERN ISOLDE team www.cern.ch/isolde



### **Outline**

#### Aimed at both physics and non-physics students

Lecture 1: Nuclear and ISOLDE facility

This lecture: Science of ISOLDE

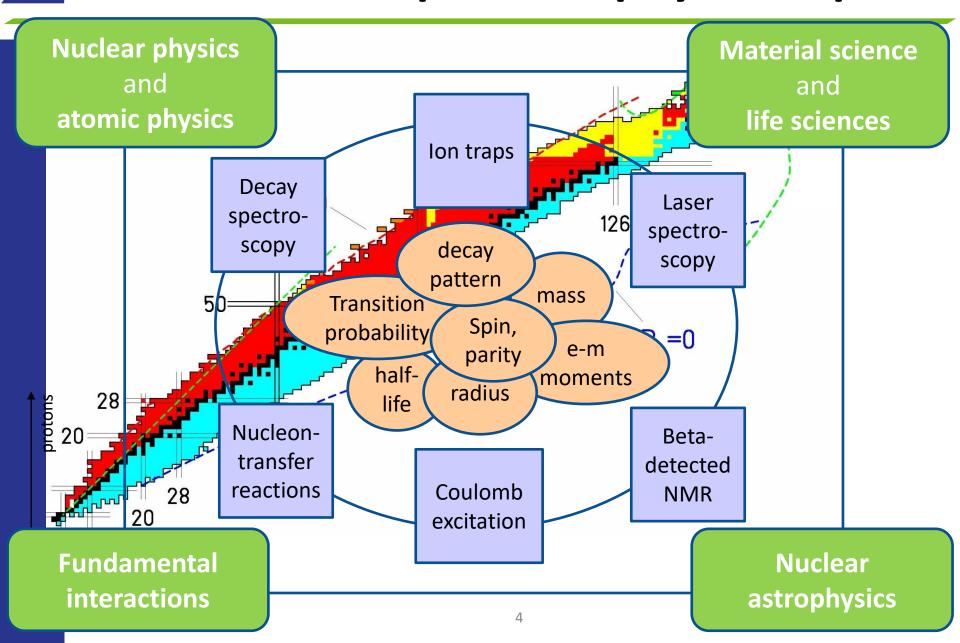
- Measured properties and used techniques
- Recent studies in:
  - nuclear physics
  - nuclear astrophysics
  - fundamental studies
  - material science
  - biology
  - > medicine

# **Baking-powder quiz**

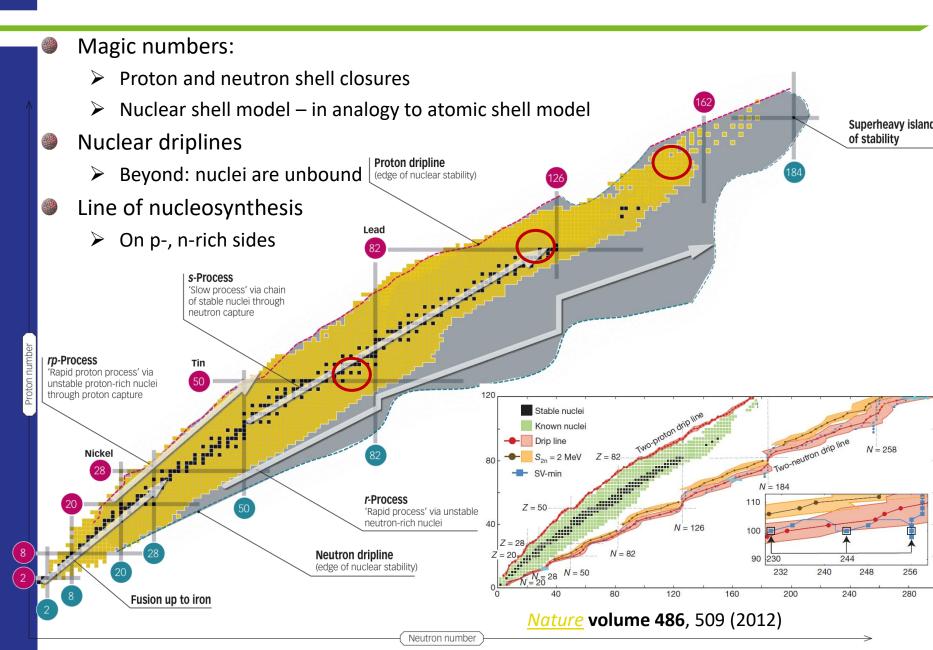
#### Prize winners:

- > Amal
- Lea-Maria
- Peter
- Lucas, Elisa, Elli, Andres
- > Alice

# **ISOLDE** techniques and physics topics



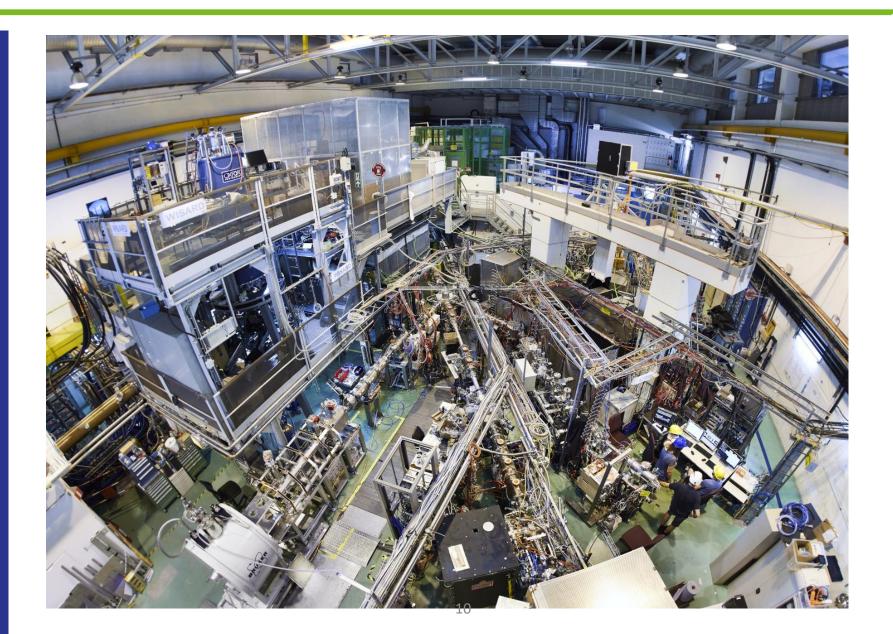
#### Chart of nuclei



# **ISOLDE** experimental setups



# **ISOLDE** experiments

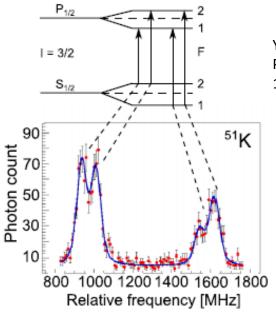


#### Laser spectroscopy and nuclear properties

Lasers allow studying ground-state (and isomeric) properties of nuclei, based on:

Atomic **hyperfine structure (HFS)** (interaction of nuclear and atomic spins)

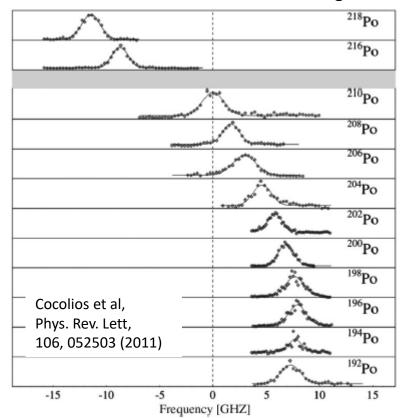
- HFS details depend on:
  - > Spin -> orbit of last proton&neutron
  - Magnetic dipole moment -> orbits occupied by protons&neutrons
  - Electric quadrupole moment -> deformations



Yordanov et al, Phys. Rev. Lett., 110, 172503 (2013) **Isotope shifts (IS)** in atomic transitions

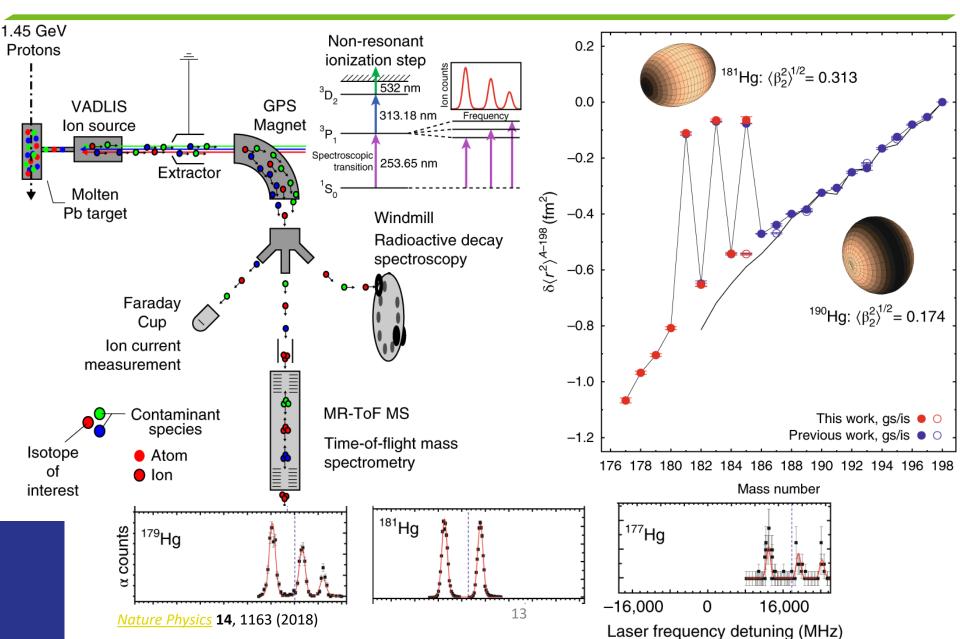
(change in mass and size of different isotopes of the same chemical element)

- IS between 2 isotopes depends on:
  - difference in their masses & charge radii



12

#### Shape staggering of mercury isotopes with RILIS

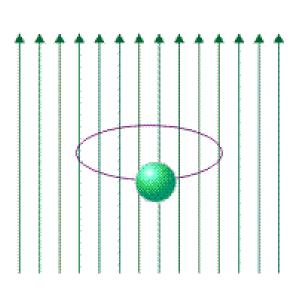


# Penning-trap mass spectrometry

- Penning trap
  - superposition of static magnetic and electric field
  - Ion manipulation with radiofrequencies

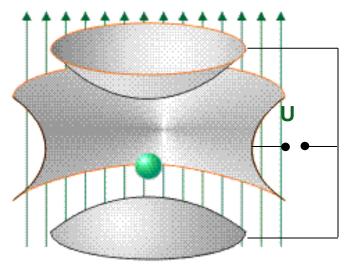


B



B

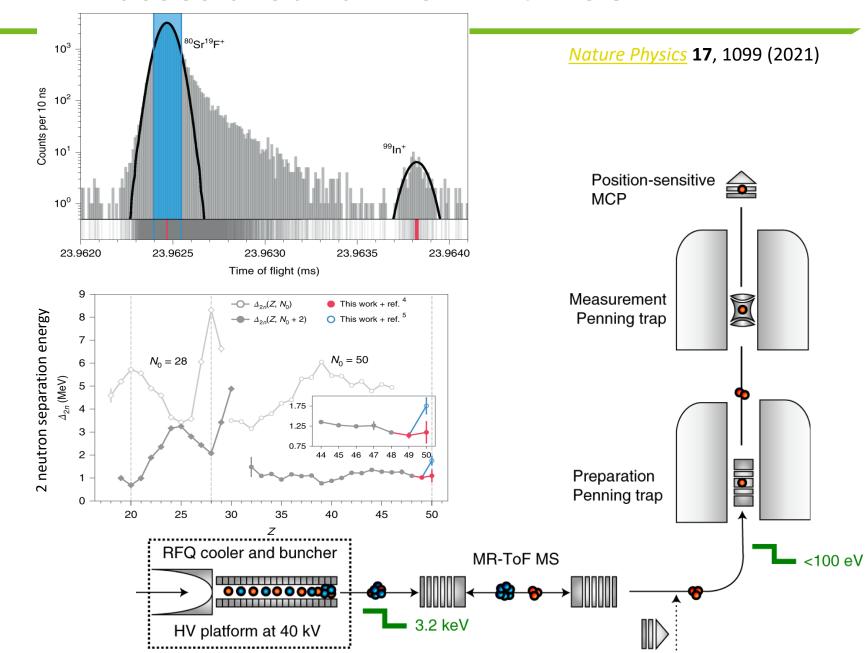
Ion q/m
Charge q
Mass m



Free cyclotron frequency is inversely proportional to the mass of the ions!

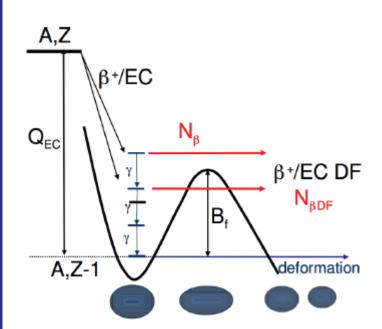
$$\omega_c = qB/m$$

#### Masses around <sup>100</sup>Sn with ISOLTRAP



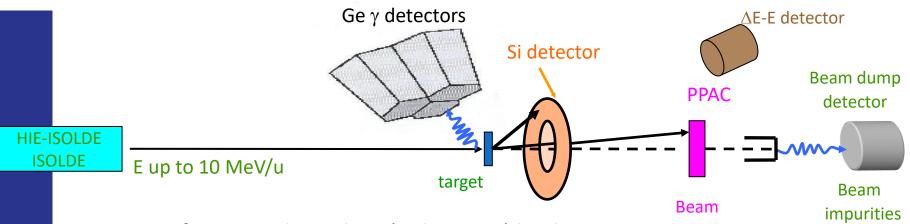
# **Decay spectroscopy**

- Different detectors to sensitive to emitted:
  - Alpha particles
  - Beta particles
  - Gamma rays
  - Protons or neutrons
- Isolde Decay Station
- soon: polarised beams at VITO

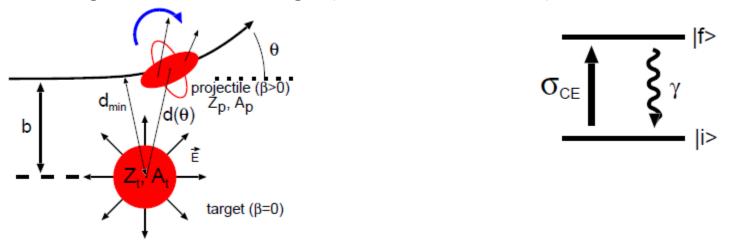




### **Coulomb excitation**



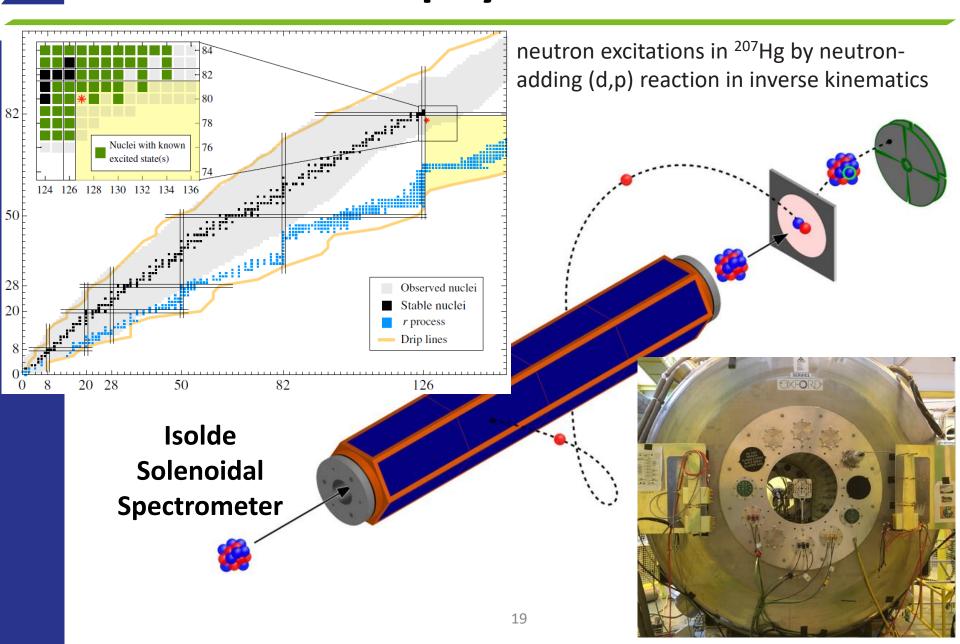
Excitation of a projectile nucleus (radioactive) by the electromagnetic field of the target (made of stable nuclei)



**Observables:** Transition energies and intensities

=> Determine new excited levels and study deformations

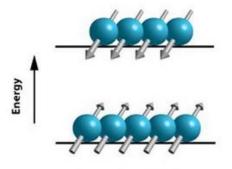
## **Nuclear astrophysics at HIE-ISOLDE**

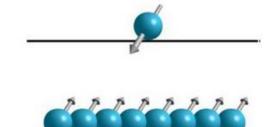


# Beta-NMR in organic samples

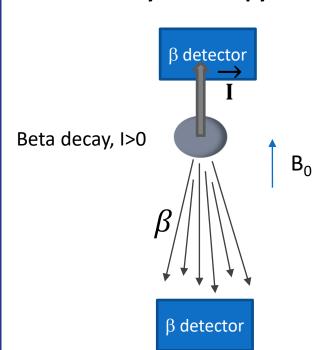
Unstable probe nuclei with spin > 0 in magnetic field

**Spin hyperpolarisation** 

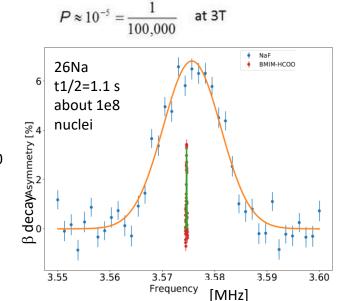




+ beta decay anisotropy



Thermal equilibrium



Hyperpolarized

$$P \approx 50\% = \frac{50,000}{100,000}$$

Up to 10 orders of magnitude more sensitive than conventional NMR,

100 x more precise than solid state NMR

Applications in biology (metal ion interactions)

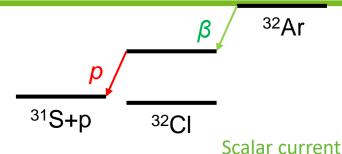
And nuclear physics: distribution of magnetisation

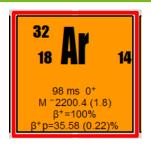
Phys. Rev. X 10, 041061 (2020)

#### Scalar currents with <sup>32</sup>Ar



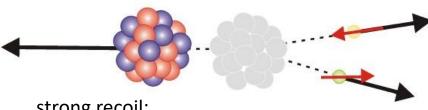
Aim: search for scalar current contribution in predominantly vector current of  $\beta$  decay via  $\beta$ – $\nu$  correlation





Vector current



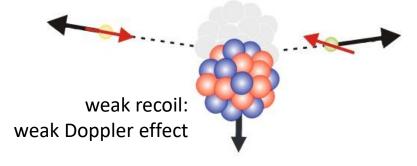


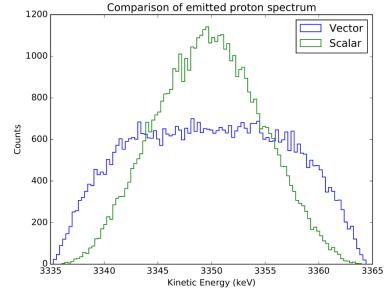
strong recoil: strong Doppler effect

#### WISARD experiment

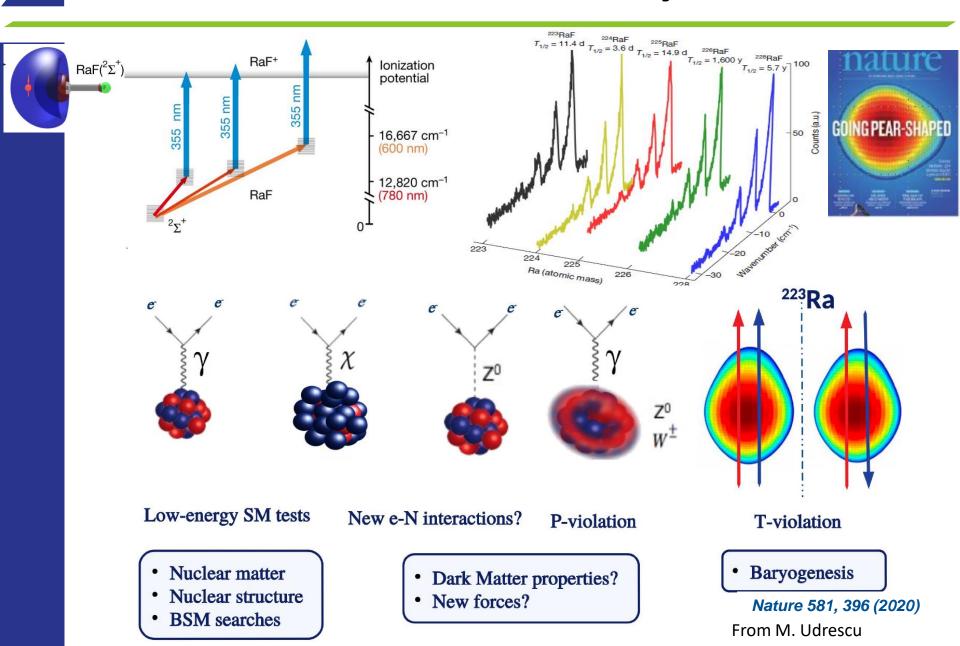
- Tool: β-delayed p decay of <sup>32</sup>Ar, Doppler effect on proton energy
- Present limits on scalar current from  $\beta v$ correlation  $a_{\rm F} = 0.65\%$

L. Hayen CRADLE++ (https://github.com/leenderthayen/CRADLE)



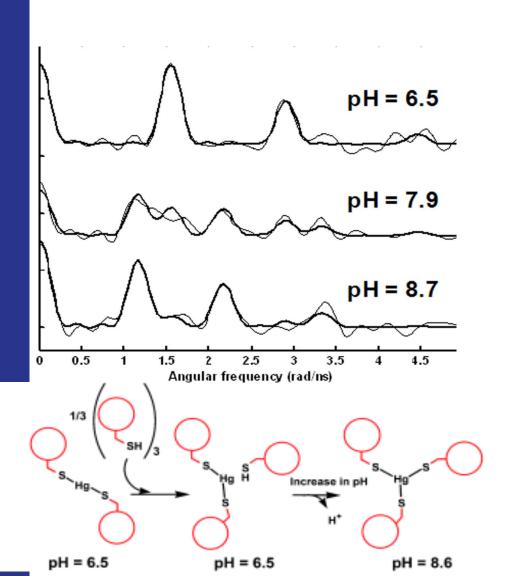


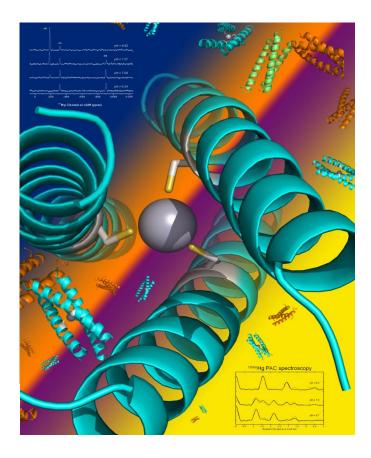
### Radioactive molecules & Beyond SM



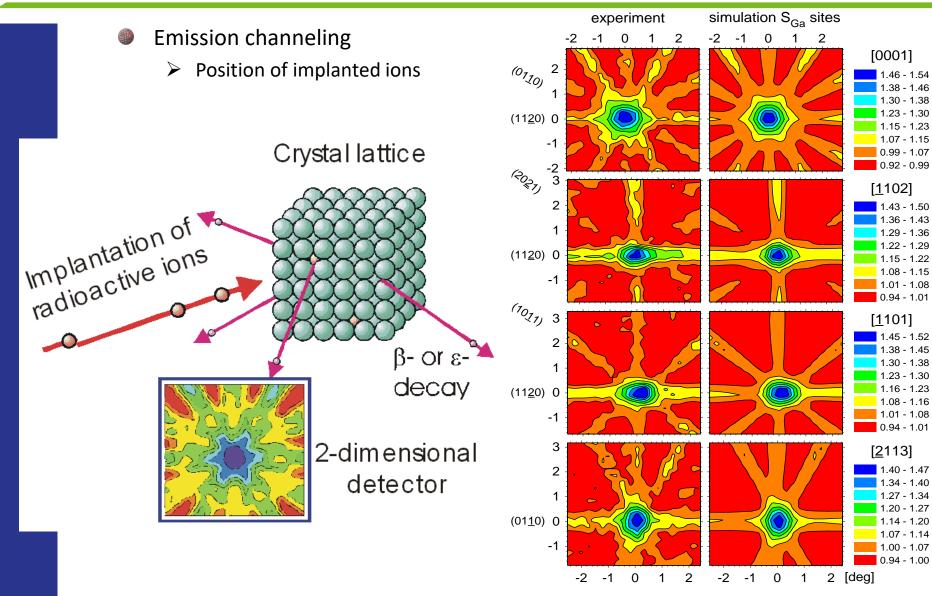
# **Heavy-ion toxicity**

Studied with Perturbed Angular Correlation method





### Material science

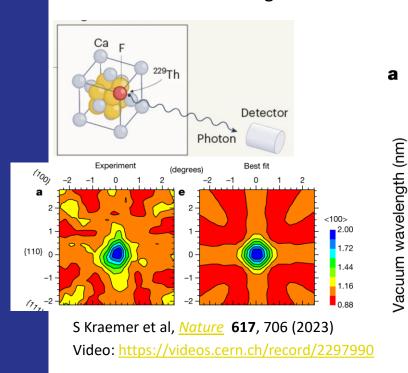


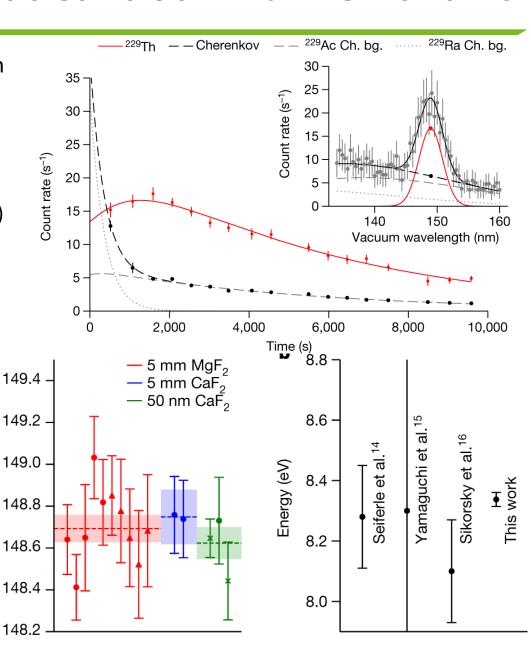
Emission channelling pattern

#### <sup>229m</sup>Th: towards a nuclear clock with VUV and EC

# Determination of isomer energy with vacuum UV spectroscopy:

- 229Ac decay to 229mTh
- Internal conversion decay branch removed via study in a crystal
- CaF as host (wide band gap material)
- Implantation site verified with emission channeling





# New medical isotopes

Collection at ISOLDE

Radiochemical purification and labeling

Injection into mouse

PET/SPECT imaging and tumor treatment



- Theranostics = therapy and diagnostics together
  - Production of isotopes at ISOLDE
  - Chemical selection and mice treatment in PSI
- Soon at ISOLDE-Medicis

	Dy 150 7.2 m	Dy 151 17 m	Dy 152 2.4 h	Dy 153 6.29 h	Dy 154 3.0 · 10 <sup>6</sup> a	Dy 155 10.0 h	Dy 156 0.056	Dy 157 8.1 h	Dy 158 0.095	Dy 159 144.4 d	Dy 160 2.329	Dy 161 18.889	Dy 162 25.475
	α 4.23 γ 387	4; a 4.07 7 386; 49; 546; 176 g; m	6 3.63 1/257 0	4; β1* α 3.46 γ 81; 214; 100; 254	u 2.87	5 <sup>+</sup> 0.9; 1.1 7227	#33 Hn #<0.009	4 γ 326	#33 # <sub>0.4</sub> < 0.006	e 758; e <sup>-</sup> 9 8000	ir60 ire, ii <0.0003	எ600 ஈ.எ <1E-6	# 170
	Tb 149 42 m 4.1 h  # -3.57 # -3.67 # 190 7 700, 100 100	Tb 150 \$.8 m   3.67 h * 4(8*31; 1600; 8.7, 1600; 8.3.49 1600; 1600, 801; 1600, 801; 1600, 801; 1600, 801; 1600,	Tb 151 25 a 17.6 h 1,48; a 241 23 a 241 200, 207, 108	Tb 152 4.2 m 17.5 h	Tb 153 2.34 d	Tb 154 22 h   8.0 h   211 4 h   1 h	Tb 155 5.32 d	Tb 156	Tb 157 99 a	Tb 158 10.5 s 180 a	Tb 159 100	Tb 160 72.3 d β=0.6:1.7 y879:299; 966 # 670	Tb 161 6.90 d β=0.5; 0.6 γ26; 49; 75
	Gd 148 74.6 a α 3.183 α 14000	Gd 149 9.28 d e; a 3.016 y 150; 299; 347	Gd 150 1.8 · 10 <sup>8</sup> a	Gd 151 120 d 4; a 2.60 7154; 243; 175	Gd 152 0.20 1.1 · 10 <sup>14</sup> a a 2.14; cr 700 c <sub>n, a</sub> <0.007	Gd 153 239.47 d *97; 103; 70 #20000 #h. a 0.03	Gd 154 2.18	Gd 155 14.80 "61000 "61, 10.00008	Gd 156 20.47	Gd 157 15.65 17254000 171, 14 < 0.05	Gd 158 24,84	Gd 159 18.48 h	Gd 160 21.86

# **Upcoming projects**

- MIRACLS: laser spectroscopy in electrostatic trap (MR-TOF)
- PUMA: trapped antiprotons from AD to measure neutron skins
- BELAPEX: spin and parities of neutron emitting states with polarised nuclei
- Distribution of magnetisation and neutron halos

# Quiz 2

What is Hulk's connection to the topic of these lectures?



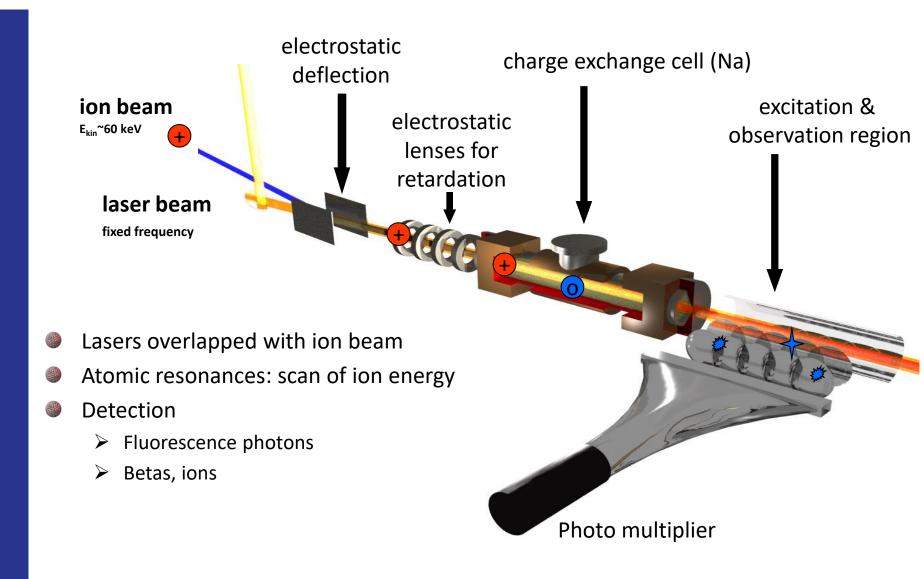


Replies can be sent to <a href="mailto:Kowalska@cern.ch">Kowalska@cern.ch</a>

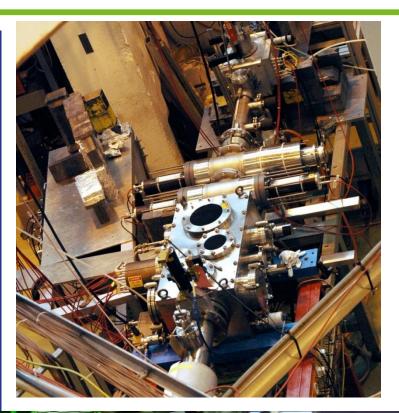
# Summary

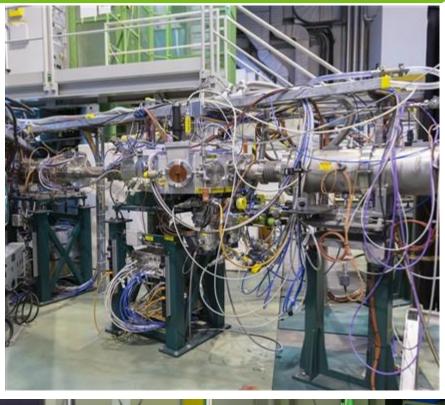
- Research topics with radionuclides:
  - Nuclear and atomic physics
  - > Astrophysics
  - Fundamental studies
  - > Applications
- Studied properties:
  - mass, radius, spin, moments, half-life, decay pattern, transition probabilities
- Examples of ISOLDE experimental techniques
  - Laser spectroscopy
  - Ion traps
  - Decay spectroscopy
  - Coulomb excitation
  - Nucleon-transfer reactions
- Applications
  - Material science
  - Life sciences: bio- and medical

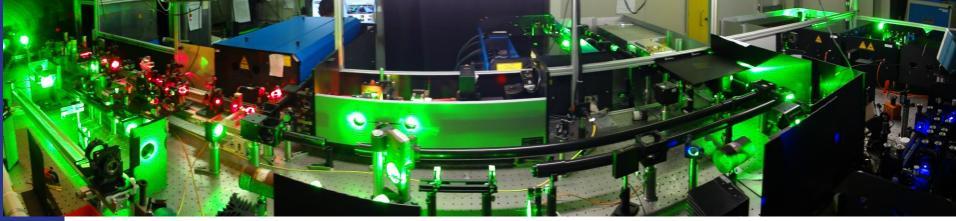
# **Collinear laser spectroscopy**



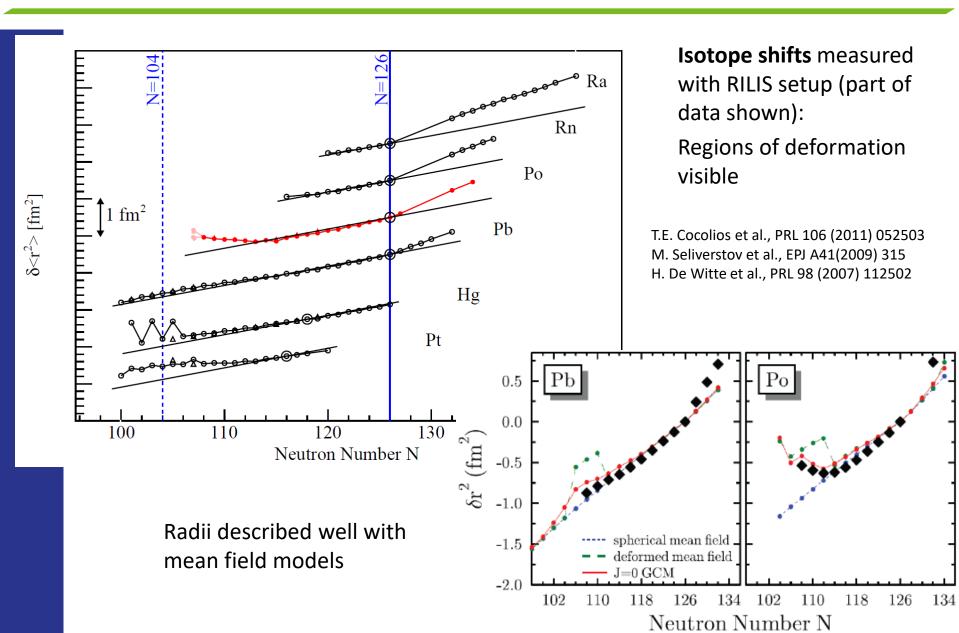
# COLLAPS, CRIS, RILIS

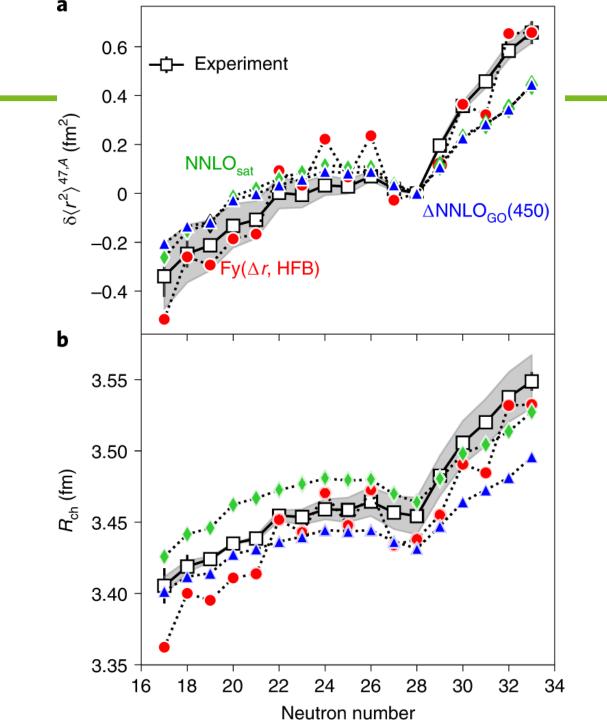




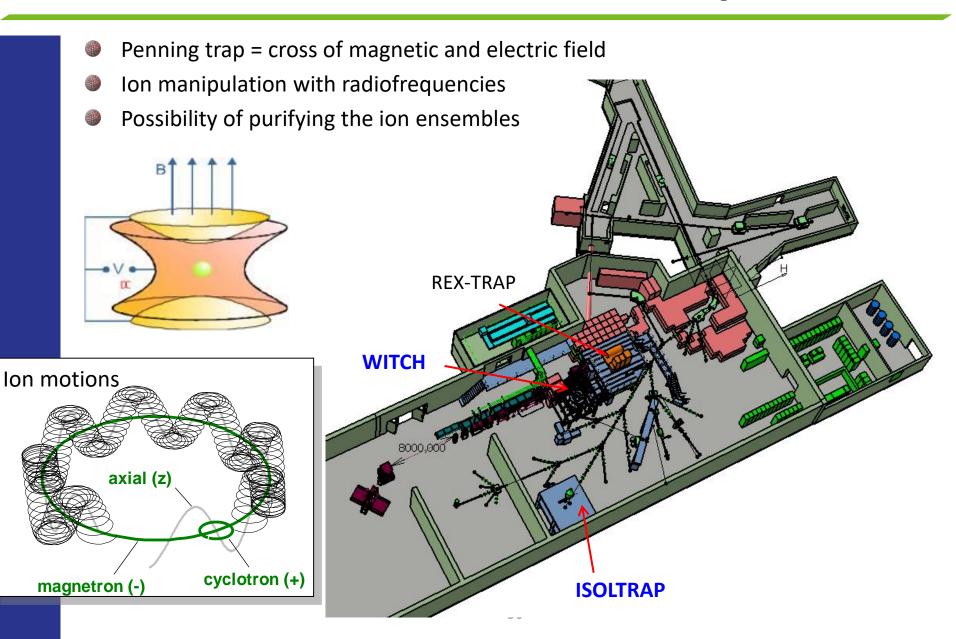


# Charge radii around lead





# Studies with ion traps

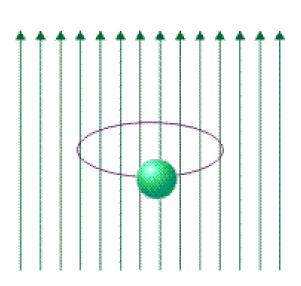


# Penning-trap mass spectrometry

- Penning trap
  - superposition of static magnetic and electric field
  - Ion manipulation with radiofrequencies

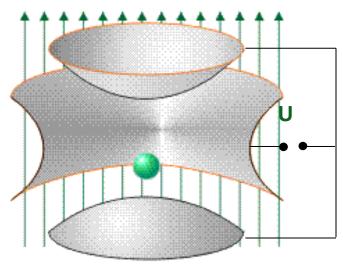


B



B

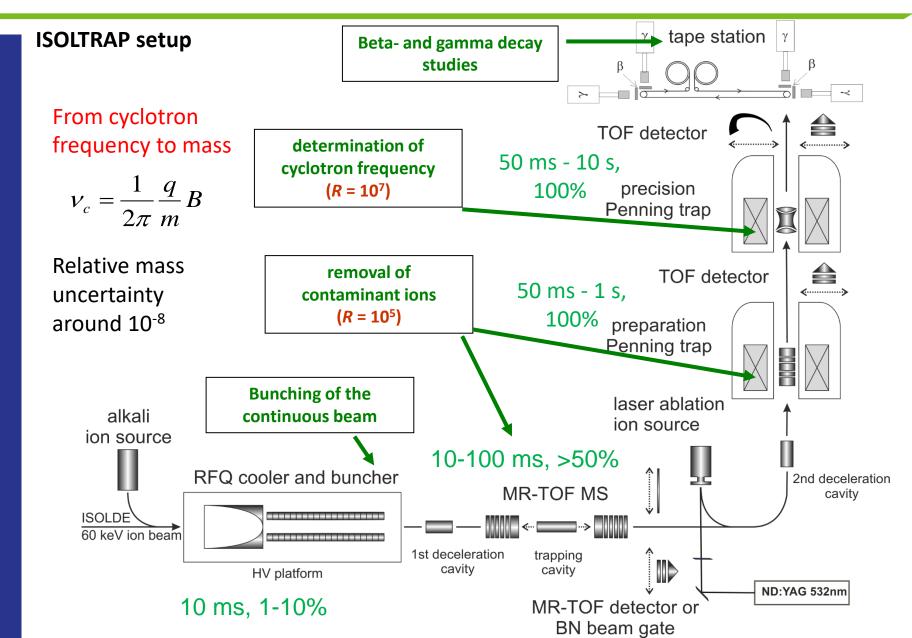
Ion q/m
Charge q
Mass m



Free cyclotron frequency is inversely proportional to the mass of the ions!

$$\omega_c = qB/m$$

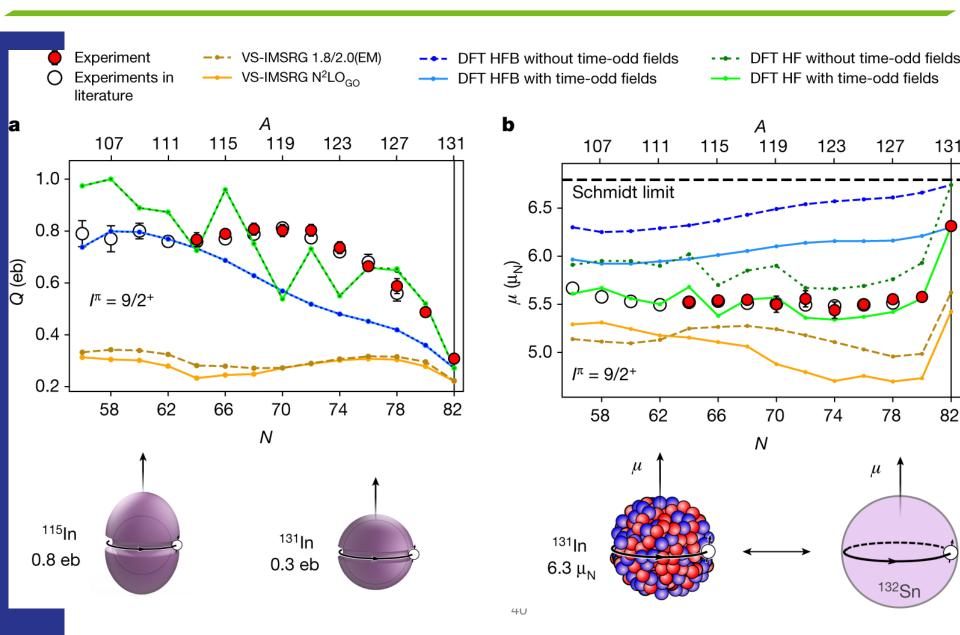
# Penning-trap mass spectrometry



# **ISOLTRAP**







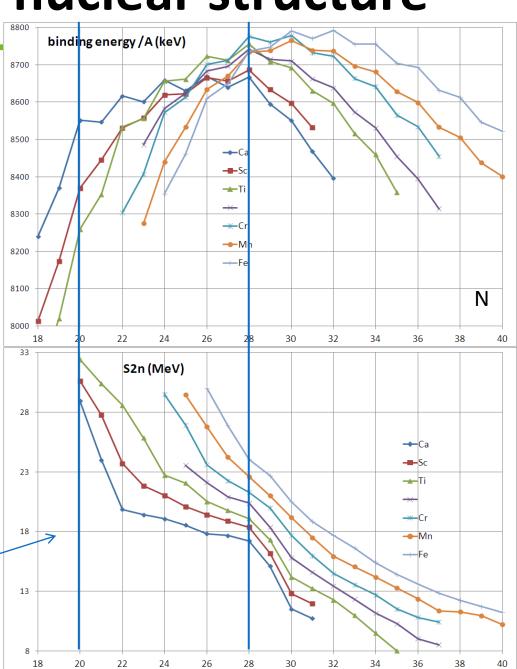
### Masses and nuclear structure

- Mass filters (mass differences) to "filter out" specific effects, e.g.
  - Differences in binding energies (one- or two-neutron/proton separation energies)

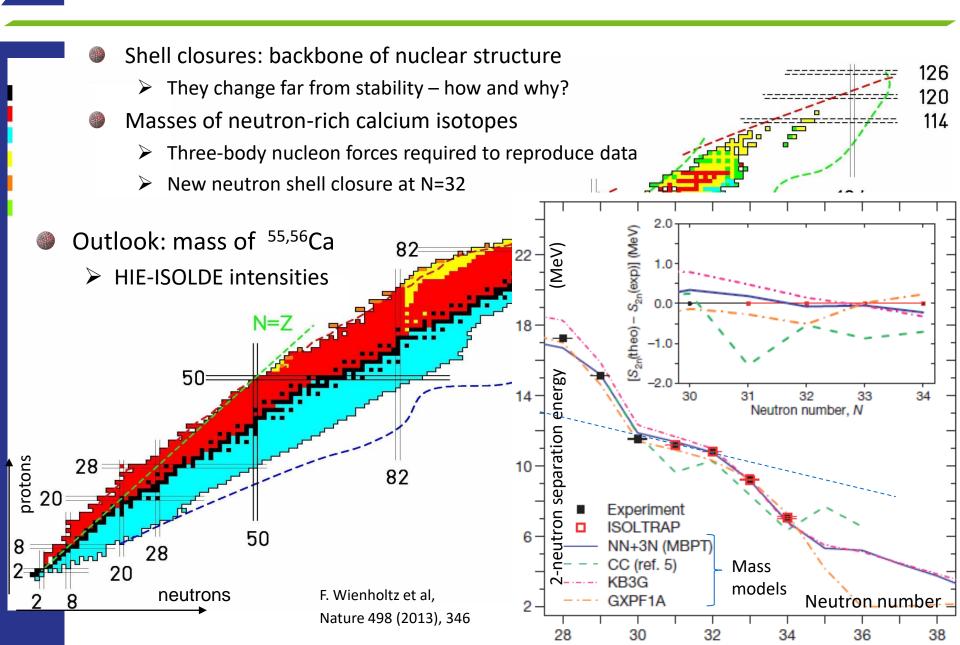
Two-neutron separation energy

$$S_{2n} = B(N-2, Z) - B(N, Z),$$

Closed shells visible as a sudden drop after the magic number (N=20 and 28)



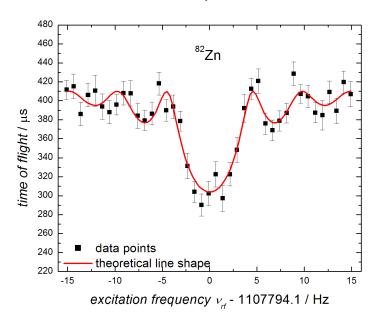
# Calcium-54 and nuclear forces



### Mass of zinc-82

# After several attempts at ISOLTRAP and elsewhere

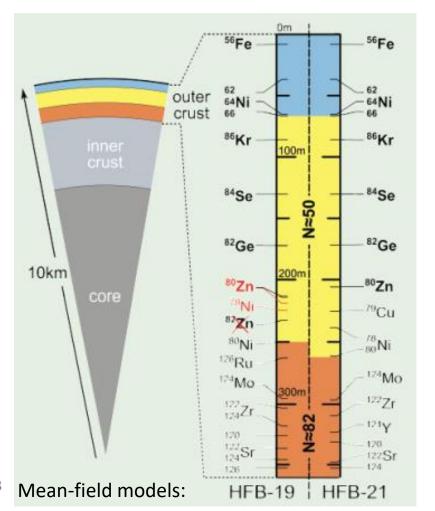
- Combined ISOLDE technical know-how:
  - neutron-converter and quartz transfer line (contaminant suppression)
  - laser ionisation (beam enhancement)



R.N. Wolf et al, Phys. Rev. Lett. 110, 041101 (2013)

#### Neutron-star composition:

- Test of models
- 82Zn is not in the crust

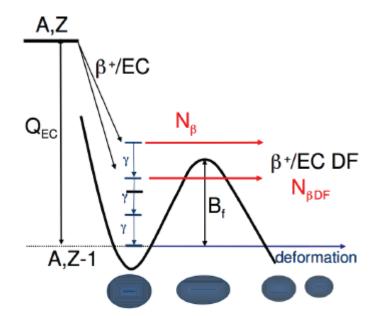


# **Decay spectroscopy**

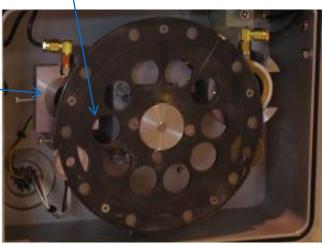
Si detector

for alphas

- Different detectors to sensitive to emitted:
  - > Alpha particles
  - Beta particles
  - Gamma rays
  - Protons or neutrons
  - For example WINDMILL setup:
    - Alpha and gamma detectors
    - Used for studies of beta-delayed fission (i.e. fission following a beta decay)



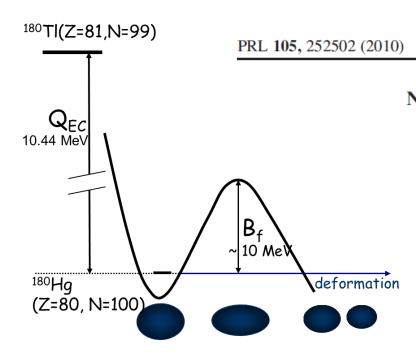
C foil for implantation





# Beta-delayed fission of mercury-180

#### **WINDMILL** setup

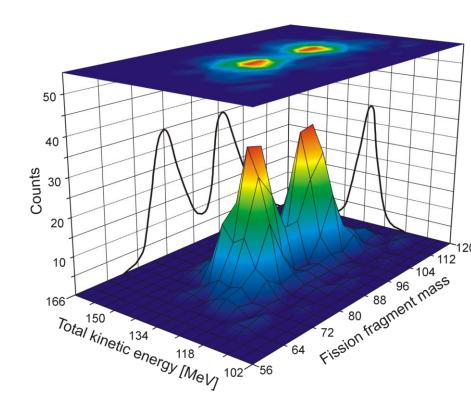


- Nuclear shell effects are important in fission, but:
  - Unexpectedly 180Hg does not fission in two semi-magic 90Zr (Z=40,N=50)
  - Fission theories do not predict the results correctly

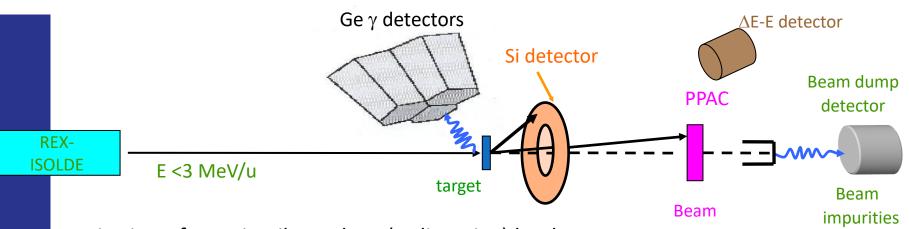




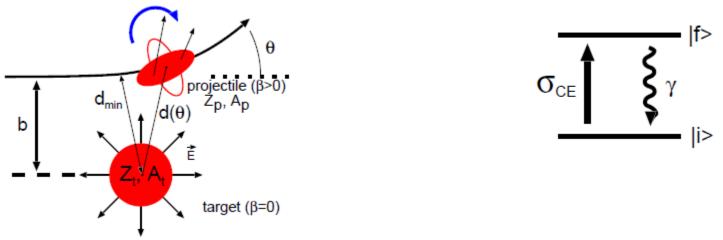
PHYSICAL REVIEW LETTERS



### **Coulomb excitation**



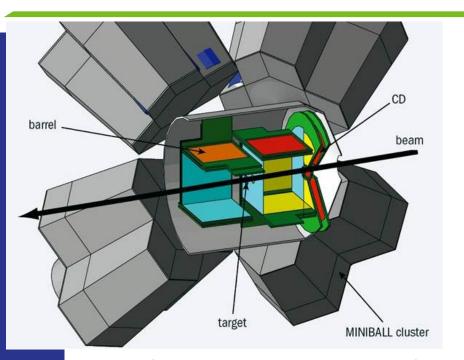
Excitation of a projectile nucleus (radioactive) by the electromagnetic field of the target (made of stable nuclei)



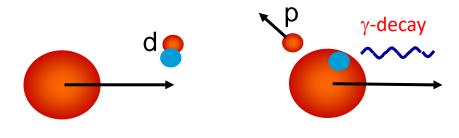
**Observables:** Transition energies and intensities

=> Determine new excited levels and study deformations

# **Nucleon-transfer reactions**



**Miniball + T-REX setup** (Si detector barrel): gamma detectors and particle identification



<u>Typical reactions</u>: one or two-nucleon transfer (d,p), (t,p)

#### Information:

#### <u>Observables</u>

- energies of protons (+ E<sub>g</sub>)
- angular distributions of protons (+ γ-rays)
- (relative) spectroscopic factors

(single-particle) level energies spin/parity assignments

particle configurations

study single-particle properties of nuclei

= > Similar configurations = large overlap of wave functions = Large probability of transfer reaction 47

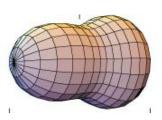
# Octupole deformation and MINIBALL

Octupole shape – very rare nuclear shape

> Test ground for nuclear models

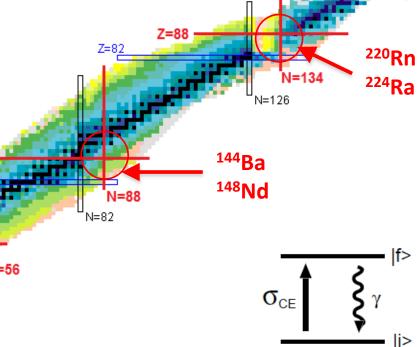
Important in searches for permanent electricdipole moments (EDM) – beyond Standard

Model





- Beam accelerated to 2.8 MeV/u
- Excitation of a projectile nucleus by e-m field of the target nuclei
- Detection with MINIBALL gamma-array
  - Germanium detectors high efficiency gamma detection
  - Silicon detectors for particle identification

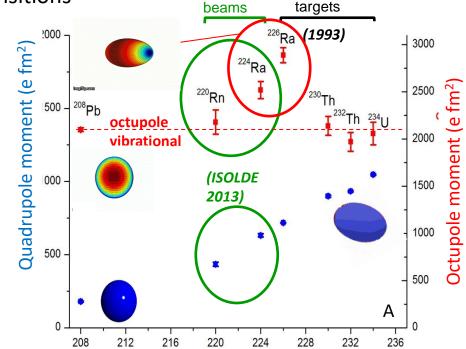




L.P. Gaffney et al, Nature 497 (2013) 199

# Pear-shape: beyond Standard Model

- Results: Enhanced electric-octupole transitions
  - direct measure of octupole correlations
- Pear shape shown experimentally in radium-224
- Best candidates for EDM searches identified: radium-223, 225
- Enhanced atomic EDM moment
  - Schiff moment enhanced by ~ 3 orders of magnitude in pear-shaped nuclei
  - In radium atoms, additional enhancement due to near-degeneracy of atomic states



radioactive

radioactive

- Outlook HIE-ISOLDE:
  - > Coulomb excitation on odd-mass radium and radon isotopes
  - > Searches for permanent EDM in trapped radium isotopes
  - => Looking for physics beyond the Standard Model



# **Applications**

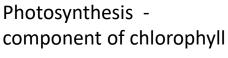
- Use known radiation from not totally exotic radioisotopes
- Profit from radionuclides:
  - Pure samples of radioisotopes (offline studies)
  - High detection efficiency for radiation (online studies)
- Techniques:
  - > Emission Channeling
  - PAC (Perturbed Angular Correlations)
  - Diffusion
  - Photoluminescence

# **Biophysics and Parkinson disease**

Over 1/3 of all proteins require metal ions to function:

# Magnesium

Catalysis in cellular energy transformations





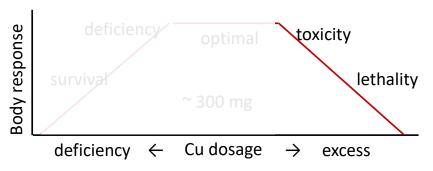
But they are difficult to study:

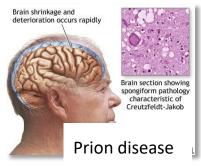
"Magnesium in biological chemistry is a Cinderella element: We know its hidden power and personality only indirectly since we are unable to label and follow it in a sensitive manner."

Copper









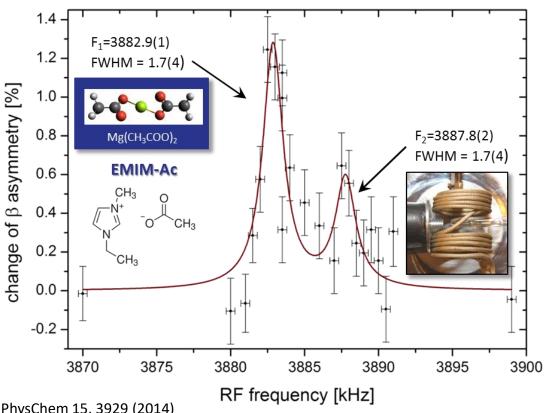


# Metals in biology and beta-NMR

New approach – beta-Nuclear Magnetic Resonance

COLLAPS setup

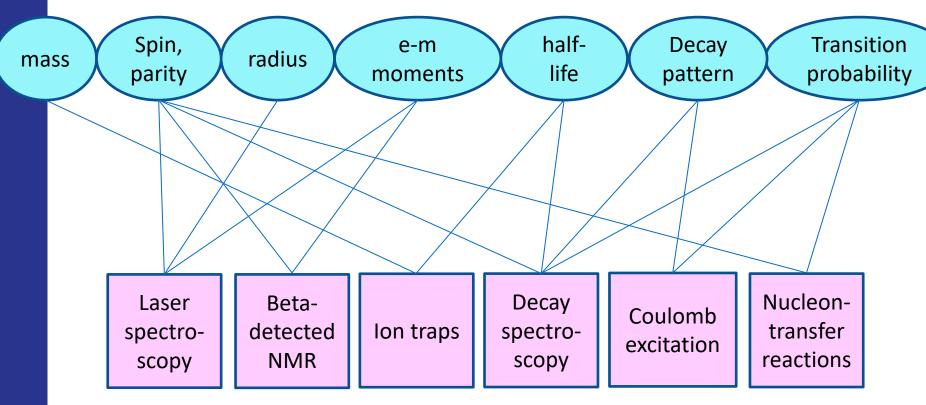
- > Beta-decay of polarized nuclei is anisotropic
- Resonances observed as change in decay asymmetry
- $\Rightarrow$  Up to 10<sup>10</sup> more sensitive than conventional NMR
- Proof-of-principle experiment
  - Magnesium-31 beam
  - Polarization with lasers
  - > 1st beta-NMR in a liquid
- Outlook:
  - Funding from CERN Knowledge Transfer Fund
  - First biological studies on Mg and Cu



A. Gottberg, M. Stachura, M. Kowalska, et al, ChemPhysChem 15, 3929 (2014) Soon be continued within MK'EU ERC Starting Grant

### Studies of radioactive nuclides

**Properties/observables** (for ground states and isomers – long-lived excited states)

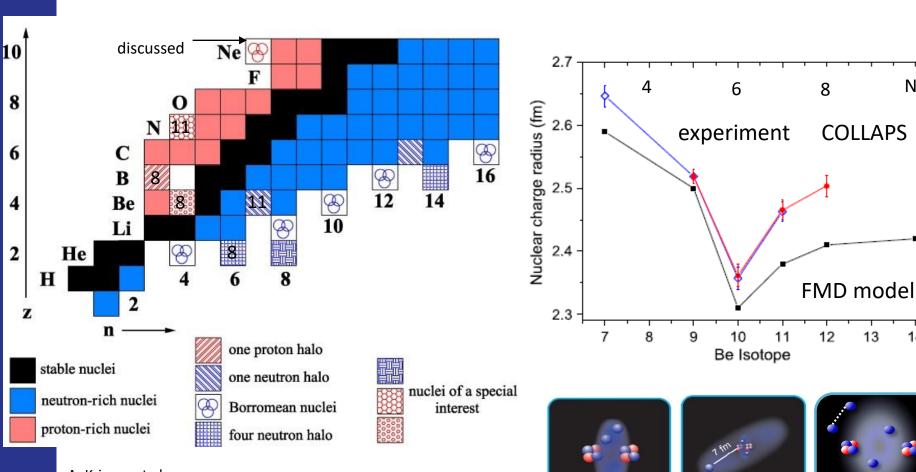


Techniques/ devices

# Charge radii of Be isotopes

Ν

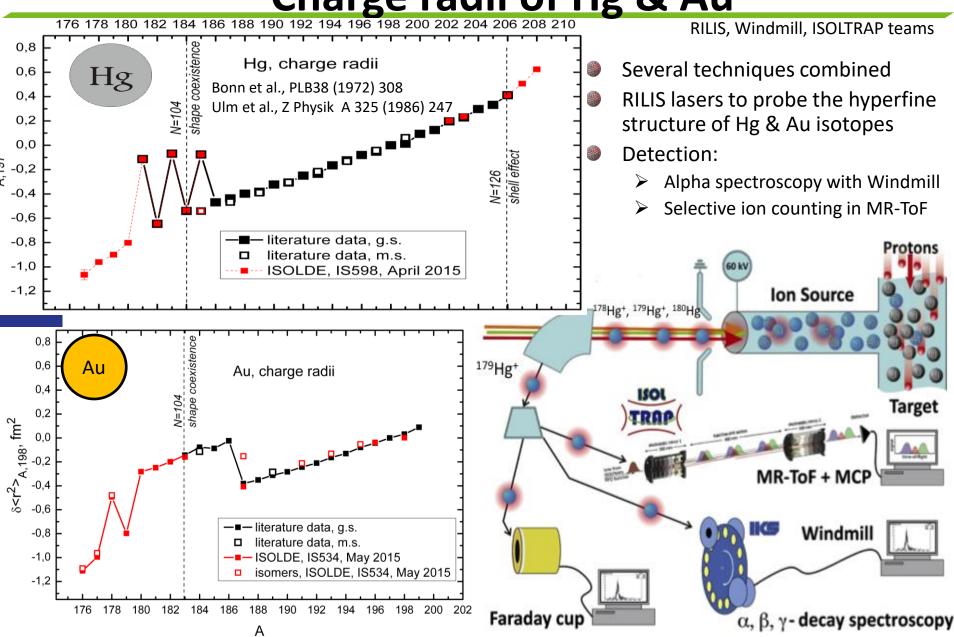
- **Halo:** nucleus built from a core and at least one neutron/proton with spatial distribution much larger than that of the core
  - Interaction of the core and halo nucleons not well understood



A. Krieger et al, Phys. Ref. Lett. 108 (2012) 142501

10R

# Combination of techniques: Charge radii of Hg & Au



### **EDM** searches in radionuclides

odd-A Rn [TRIUMF]

odd-A Ra [Argonne]

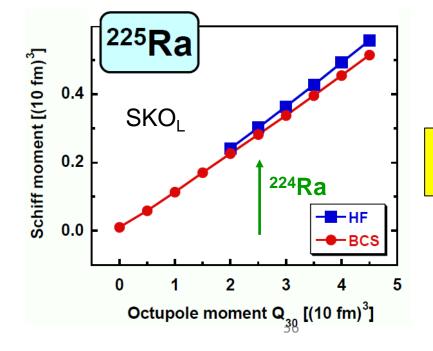
odd-A Ra [Groningen]

odd-A Rn:

<sup>219,221</sup>Rn inferior to <sup>223,225</sup>Ra

Next step: <sup>223,225</sup>Rn HIE-ISOLDE (CERN)

odd-A Ra:



Next step: <sup>225</sup>Ra directly TSR@HIE-ISOLDE

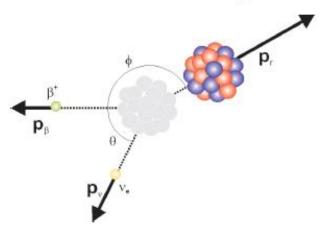
# Fundamental studies with traps

determine beta-neutrino ( $\beta v$ ) correlation in  $\beta$  decay of <sup>35</sup>Ar with ( $\Delta a/a$ )<sub>stat</sub>  $\leq$  0.5 % =>test the Standard Model

$$H_{\beta} = H_S + H_V + H_T + H_A + H_P$$

Angular distribution of  $\boldsymbol{\beta}$  radiation

$$W(\theta) \approx 1 + a \frac{v}{c} cos\theta$$

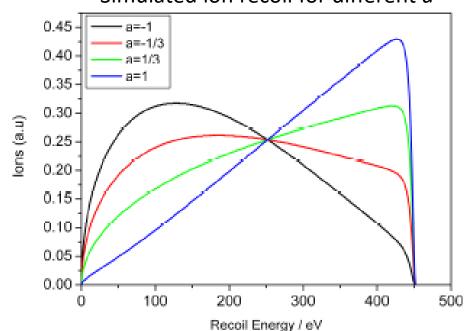


Current experimental limits: (from nuclear & neutron  $\beta$  decay)  $\frac{C_s}{C_V} < 7\%$ ,  $\frac{C_T}{C_A} < 9\%^1$ 

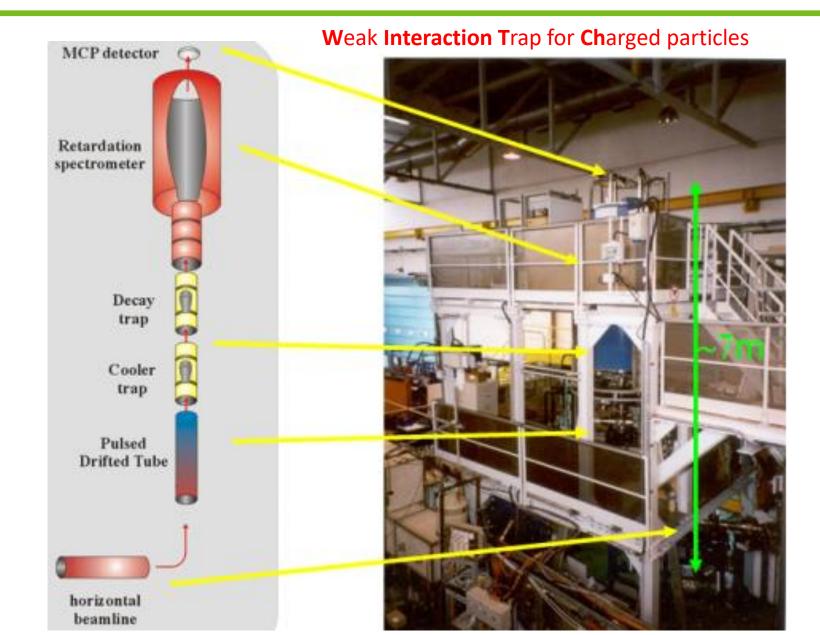
e.g: Fermi  $\beta$  decay  $(0^+ \rightarrow 0^+)$ 

$$a \approx 1 - \frac{|C_S|^2 + |C_S'|^2}{|C_V|^2}$$

Simulated ion recoil for different a



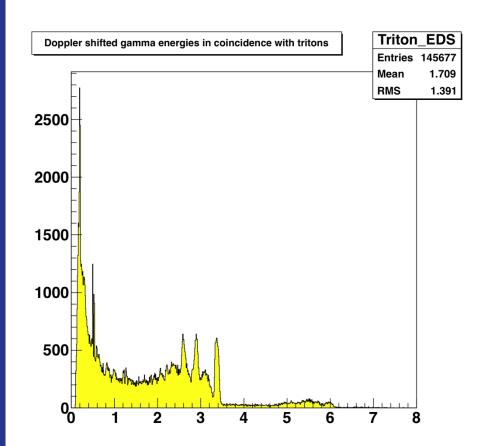
# **WITCH**



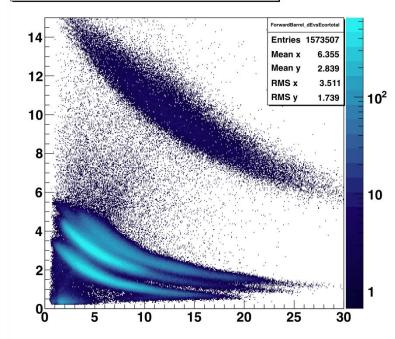
# Transfer reactions on beryllium-11

#### 11Be:

- Halo nucleus
- Cluster structures in neighbours
- ➤ N=8 broken in 12Be



#### dE vs Eback corrected for all fordet



### **CRIS**

- Collinear Resonant Ionisation Spectroscopy
- High sensitivity, lower resolution -> perfect for heavy ions

5. lons deflected on to decay spectroscopy station

**6.** Alpha-gamma coincidences used to identify the decay of <sup>204g,m</sup>Fr to <sup>200</sup>At

2. Doppler tuning voltage applied to ion bunch

1. Bunched ion beam of ~1µs temporal width

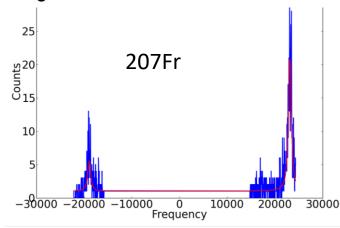
4. Bunch is ionized when on resonance with laser

Ion bunch neutralized by alkali vapour charge exchange cell

#### **Open projects:**

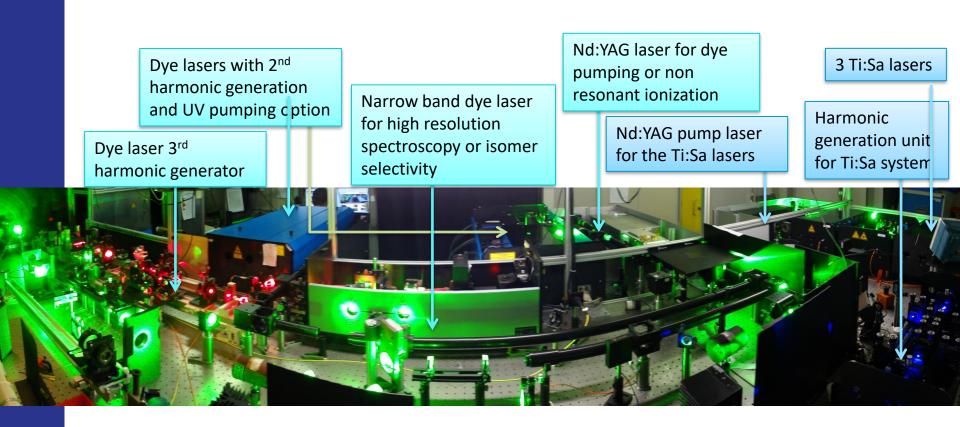
IS471: Collinear resonant ionization laser spectroscopy of rare francium isotopes

IS531: Collinear resonant ionization spectroscopy for neutron rich copper isotopes



### **RILIS**

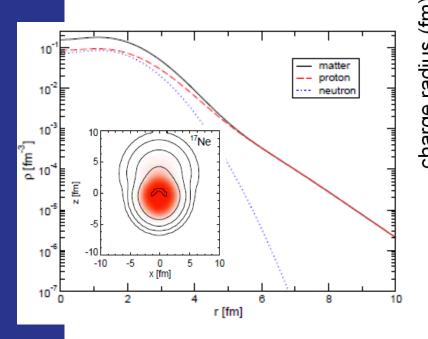
Resonant Ionization Laser Ion Source

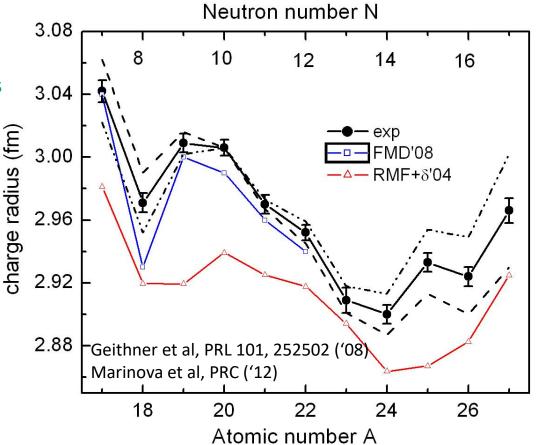


# **COLLAPS** – Ne charge radii

#### **Laser spectroscopy**



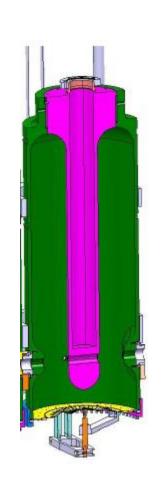




### **HIE-ISOLDE**

Quarter-wave resonators (Nb sputtered)

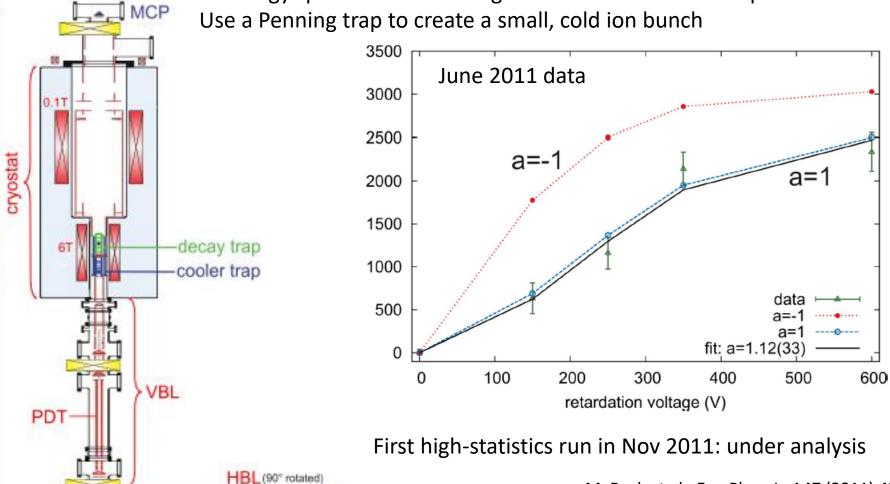
- SC-linac between 1.2 and 10 MeV/u
- 32 SC QWR (20 @  $\beta_0$ =10.3% and 12@  $\beta_0$ =6.3%)
- Energy fully variable; energy spread and bunch length are tunable. Average synchronous phase fs= -20 deg
- 2.5<A/q<4.5 limited by the room temperature cavity
- 16.02 m length (without matching section)
- No ad-hoc longitudinal matching section (incorporated in the lattice)
- New beam transfer line to the experimental stations





### WITCH

-> energy spectrum of recoiling ions with a retardation spectrometer



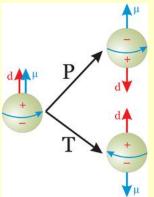
M. Beck et al., Eur. Phys. J. A47 (2011) 45 M. Tandecki et al., NIM A629 (2011) 396 S. Van Gorp et al., NIM A638 (2011) 192

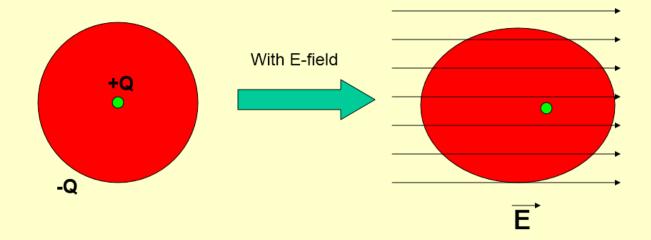


### **EDM**









Schiff Theorem: neutral atomic system of point particles in electric field readjusts itself to give zero E field at all charges.

BUT: finite size and shape of nucleus breaks the symmetry



### **EDM**



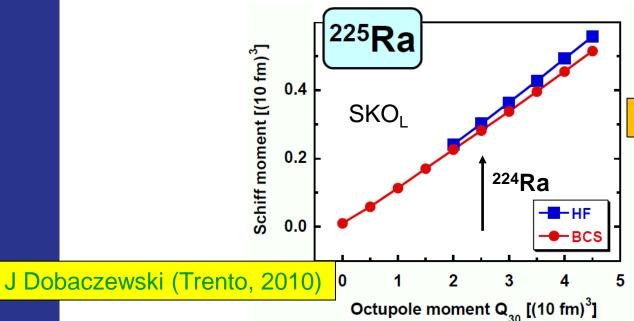
V Spevak, N Auerbach, and VV Flambaum PR C 56 (1997) 1357

chiff moment:

related to  $Q_3$  P,T-violating n-n interaction S=-2  $\frac{1}{J}$   $<\hat{S}_z><\hat{V}_{PT}>$ 

energy splitting of parity doublet

Schiff moment enhanced by ~ 3 orders of magnitude in pear-shaped nuclei



<sup>219,221</sup>Rn inferior to <sup>223,225</sup>Ra



### **EDM** searches



odd-A Rn [TRIUMF]

odd-A Ra [Argonne]

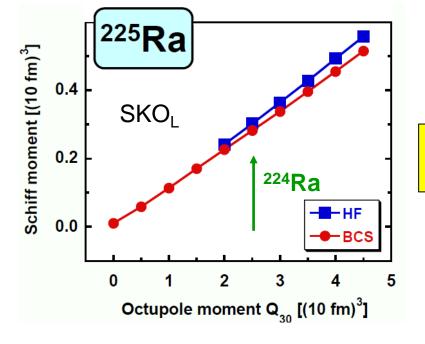
odd-A Ra [Groningen]

odd-A Rn:

<sup>219,221</sup>Rn inferior to <sup>223,225</sup>Ra

Next step: <sup>223,225</sup>Rn HIE-ISOLDE (CERN)

odd-A Ra:



Next step: 225Ra directly TSR@HIE-ISOLDE



### **EDM**



### In units of *e–cm*, selected EDM limits are:

Particle	EDM limit	System	SM Prediction	New Physics
е	$1.9 \times 10^{-27}$	<sup>205</sup> Tl atom	$10^{-38}$	$10^{-27}$
μ	$1.1 \times 10^{-19}$	rest frame <b>Ē</b>	10 <sup>-35</sup>	10 <sup>-22</sup>
τ	$3.1 \times 10^{-16}$	$e^+e^-  ightarrow  au^+ au^-\gamma$	$10^{-34}$	10 <sup>-20</sup>
p	$6.5 \times 10^{-23}$	TIF molecule	10 <sup>-31</sup>	10 <sup>-26</sup>
n	$2.9 \times 10^{-26}$	UCN	$10^{-31}$	$10^{-26}$
<sup>199</sup> Hg	$2.1 \times 10^{-28}$	atom cell	$10^{-33}$	$10^{-28}$

#### A non-exhaustive list:

Leptonic	EDMs	Hadronic EDMs		
System	Group	System	Group	
Cs (trapped)	Penn St.	n (UCN)	SNS	
Cs (trapped)	Texas	n (UCN)	ILL	
Cs (fountain)	LBNL	n (UCN)	PSI	
YbF (beam)	Imperial	n (UCN)	Munich	
PbO (cell)	Yale	<sup>199</sup> Hg (cell)	Seattle	
HBr <sup>+</sup> (trapped)	JILA	<sup>129</sup> Xe (liquid)	Princeton	
PbF (trapped)	Oklahoma	<sup>225</sup> Ra (trapped)	Argonne	
GdIG (solid)	Amherst	<sup>213,225</sup> Ra (trapped)	KVI	
GGG (solid)	Yale/Indiana	<sup>223</sup> Rn (trapped)	TRIUMF	
muon (ring)	J-PARC	deuteron (ring)	BNL?	



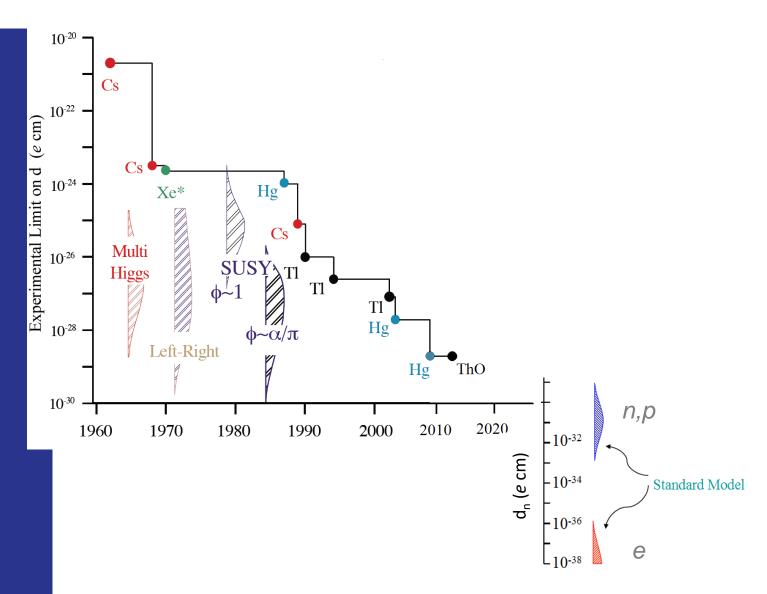
### **Matter-antimatter**



- Sakharov conditions require CP symmetry violation
- This violation is observed in electro-weak interaction, but probably cannot account for matter-antimatter imbalance
- No evidence for CP violation in strong interaction
- $\|d(n)\| < 3.1 \times 10^{-26} \text{ e cm } (Baker et al PRL 97 (2006) 131801)$
- $\| |d(^{199}Hg)| < 3.1 \times 10^{-29} \text{ e cm } (Griffith et al PRL 102 (2009) 101601)$
- $\| |d(ThO)| < 8.7 \times 10^{-29} \text{ e cm } (Baron et al arXiv:1310.7534v2 (2013))$
- In many cases provides best test of extensions of the Standard Model
- that violate CP symmetry.
  - Accounted for by cancellations?
  - study of minimal supersymmetric SM (J Ellis)
- © CP violation in the lepton sector is not known, could also account for matterantimatter difference

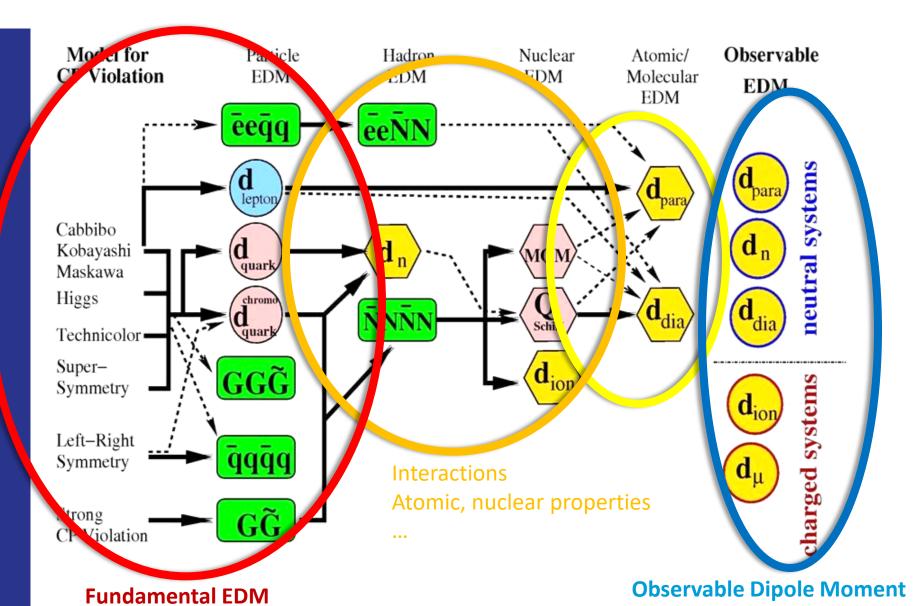






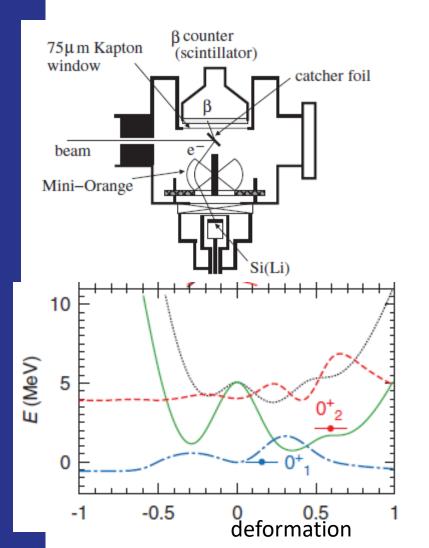




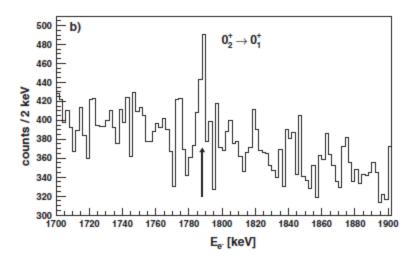


# 30Mg: E0 transition

E0 decay of 30Mg electron spectrometer



Identification of 0+ state at 1789 keV; small mixing amplitude with spherical ground state => deformed state



**30Mg:** spherical 0+ground-state, deformed 1<sup>st</sup> 0+ state (2 neutrons across N=20) => **shape coexistence** 

W. Schwerdtfeger et al., Phys. Rev. Lett. 103, 012501 (2009)

# Laser spectroscopy and nuclear physics

- **Spin** (orbital+intrinsic angular momentum), **parity** ( $I^{\pi}$ )
- Nuclear *g***-factor** and **magnetic** dipole **moment** ( $g_i$  and  $\mu_i$ )
  - Electric quadrupole moment (Q)
    - -Charge radius  $(\langle r^2 \rangle)$

#### Give information on:

- Configuration of neutrons and protons in the nucleus
  - Size and form of the nucleus

 $I^{\pi}$ 

$$oldsymbol{g}_{l}$$
 and  $oldsymbol{\mu}_{l}$ 

1/2+
$$0d_{3/2} - \mu = +0.54$$

$$1s_{1/2} - 0d_{5/2} - 00000$$

$$1^{p}=2^{+}$$

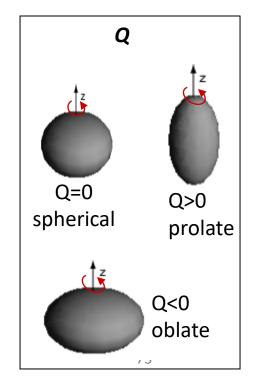
$$0d_{3/2} - 00000$$

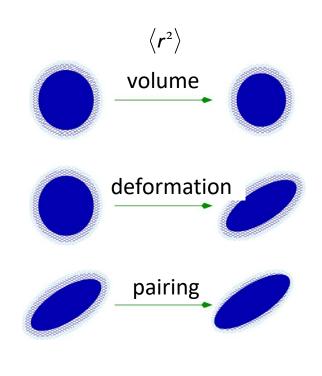
$$1s_{1/2} - 00000$$

$$0d_{5/2} - 00000$$



$$I^{p}=2^{+}$$
 $\mu = +1.83$ 
 $0d_{3/2} - - - 1s_{1/2} - - 0d_{5/2} - - -$ 





# Laser spectroscopy

#### Atomic hyperfine structure

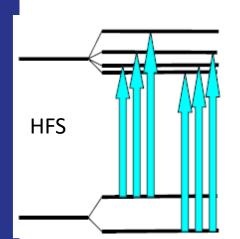
(interaction of nuclear and atomic spins)

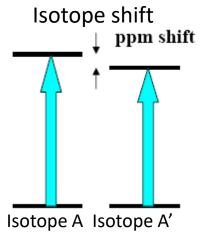
$$\Delta E_{HFS} = \frac{A}{2}K + \frac{B}{2} \frac{\frac{3}{4}K(K+1) - I(I+1)J(J+1)}{2(2I-1)(2J-1)I \cdot J}$$

where 
$$K = F(F+1) - I(I+1) - J(J+1)$$

$$\mathbf{A} = \frac{\mu_I H_e(0)}{I \cdot J}$$

$$\mathbf{B} = eQV_{zz}(0)$$





#### **Isotope shifts** in atomic transitions

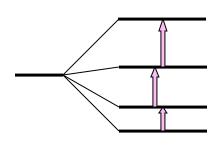
(change in mass and size of different isotopes of the same chemical element)

$$\delta v^{A,A'} = (K_{NMS} + K_{SMS}) \times \frac{A' - A}{A'A} + F \times \delta \langle r^2 \rangle^{A,A'}$$

#### **Nuclear Magnetic Resonance** – NMR

(Zeeman splitting of nuclear levels)

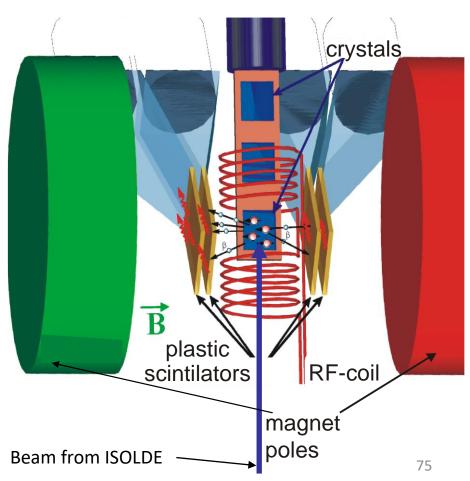
$$\Delta E_{mag} = \left| \mathbf{g}_{I} \right| \cdot \mu_{N} \cdot B + \frac{1}{2} \mathbf{Q} \cdot V_{zz}$$



$$B = 0$$
  $B \neq 0$ 

### **Beta-detected NMR**

Beta particles (e-,e+) can be used as a detection tool, instead of rf absorption (beams down to 1000 ions/s can be studied)



#### Measured asymmetry:

$$A = \frac{N(0^{\circ}) - N(180^{\circ})}{N(0^{\circ}) + N(180^{\circ})}$$

### Nuclear Magnetic Resonance – NMR (Zeeman splitting of nuclear levels)

$$\Delta E_{mag} = |g_I| \cdot \mu_N \cdot B + \frac{1}{2} Q \cdot V_{zz}$$

$$B = 0 \qquad B \neq 0$$

#### **Results:**

Magnetic and electric moments of nuclei (position of last nucleons, shapes)