



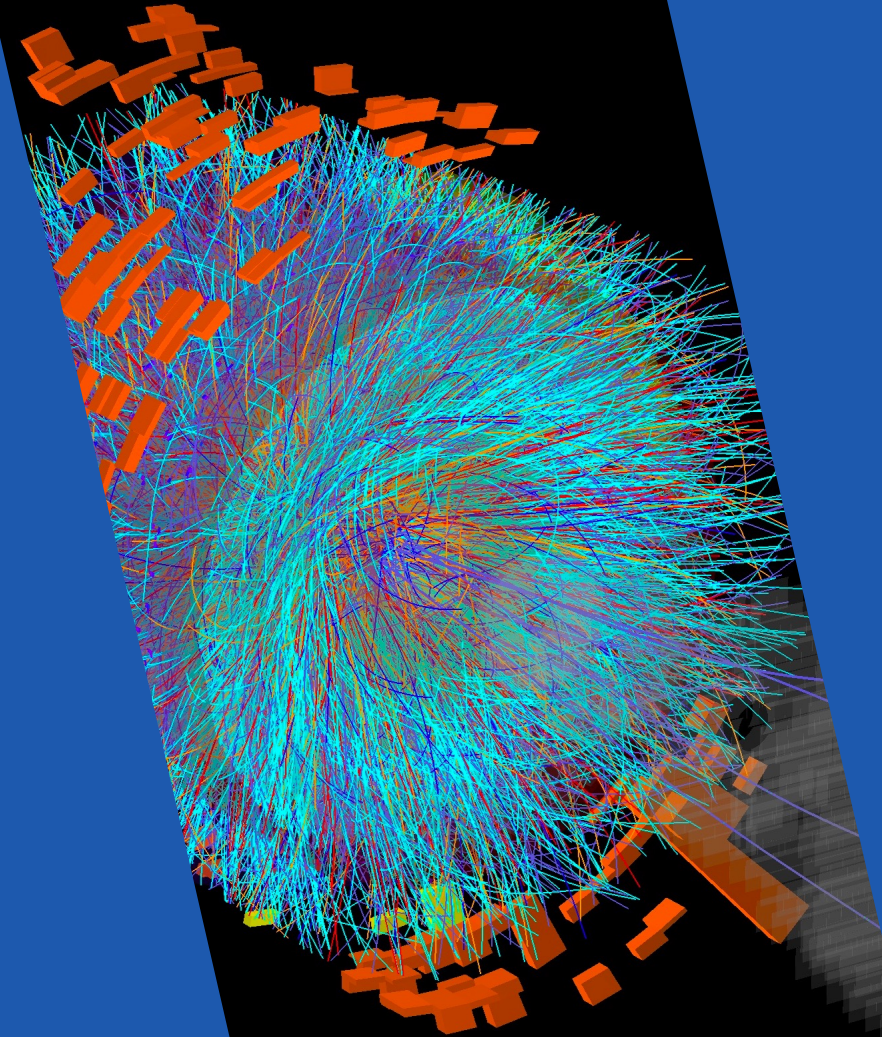
CERN Summer Student Lectures 2023

# Heavy Ions 2/3

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# Production and characterization of the QGP at the LHC

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# Kinematic variables

**Momentum and transverse momentum:**  $p = \sqrt{p_L^2 + p_T^2}$

**Transverse mass:**  $m_T := \sqrt{m^2 + p_T^2}$

**Rapidity** (generalizes longitudinal velocity  $\beta_L = p_L/E$ ):  $y := \operatorname{arctanh} \beta_L = \frac{1}{2} \ln \frac{1 + \beta_L}{1 - \beta_L} = \frac{1}{2} \ln \frac{E + p_L}{E - p_L}$

- In a collider where 2 beams of different ions:  $y_{CM} = \frac{1}{2} \ln \frac{Z_1 A_2}{A_1 Z_2}$
- In fixed-target mode:  $y_{CM} = (y_{\text{target}} + y_{\text{beam}})/2 = y_{\text{beam}}/2$

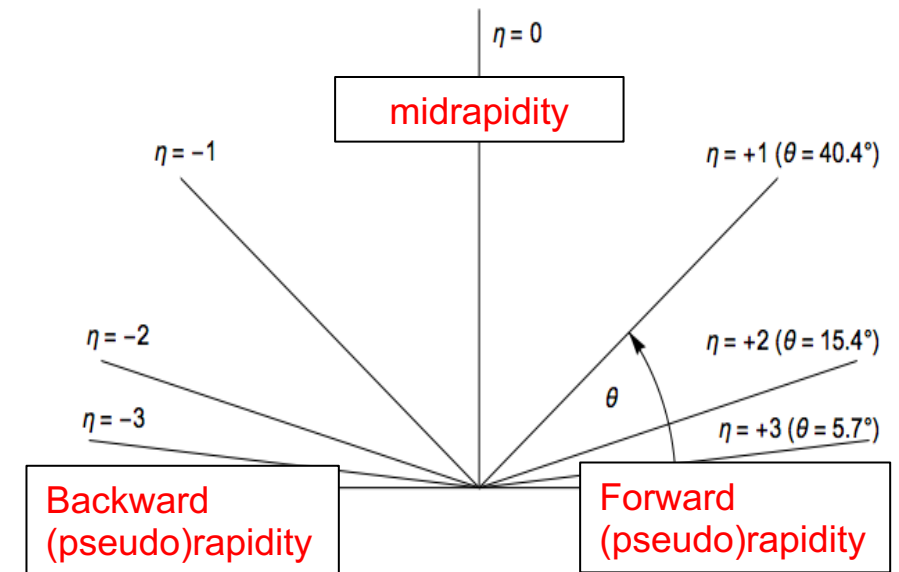
The rapidity can be approximated by **pseudorapidity** in the **ultra-relativistic limit** ( $p \gg m$ ):

$$y = \frac{1}{2} \ln \frac{E + p \cos \vartheta}{E - p \cos \vartheta} \stackrel{p \gg m}{\approx} \frac{1}{2} \ln \frac{1 + \cos \vartheta}{1 - \cos \vartheta} = \frac{1}{2} \ln \frac{2 \cos^2 \frac{\vartheta}{2}}{2 \sin^2 \frac{\vartheta}{2}} = -\ln \left[ \tan \frac{\vartheta}{2} \right] =: \eta$$

$$\cos(2\alpha) = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha$$

where  $\vartheta$  is the angle between the direction of the beam and the particle.

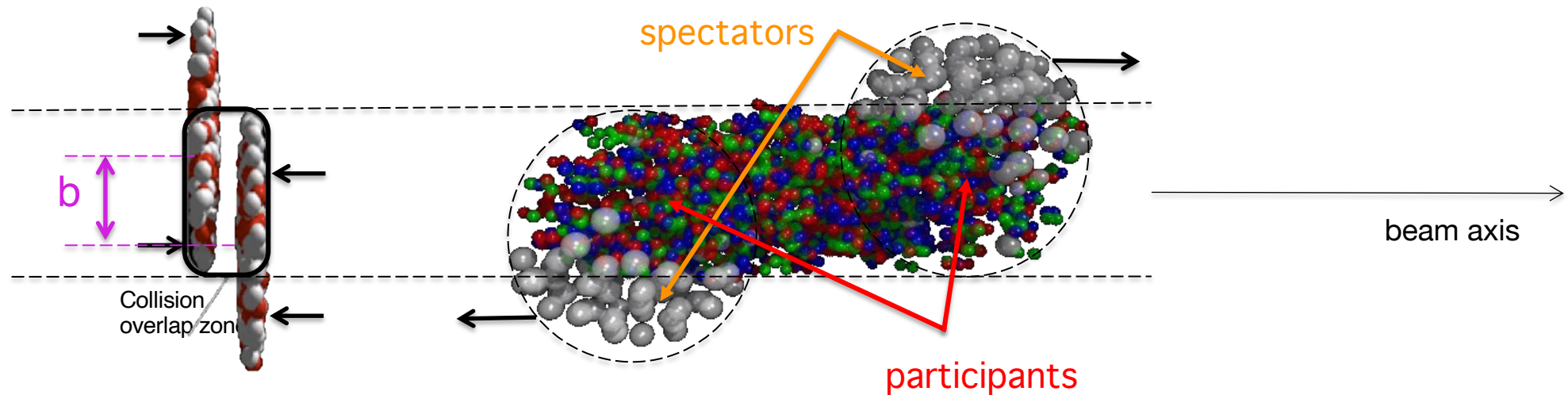
In general  $y \neq \eta$ , especially at low momenta.



# Geometry of heavy-ion collisions 1/2

We can control **a posteriori** the geometry of the collision by selecting in **centrality**.

**Centrality** = fraction of the total hadronic cross section of a nucleus-nucleus collision, typically expressed in percentile, and related to the impact parameter (**b**)



Other variables related to centrality:

- $N_{\text{coll}}$ , number of binary nucleon-nucleon collisions
- $N_{\text{part}}$  number of participating nucleons

# Geometry of heavy-ion collisions 2/2



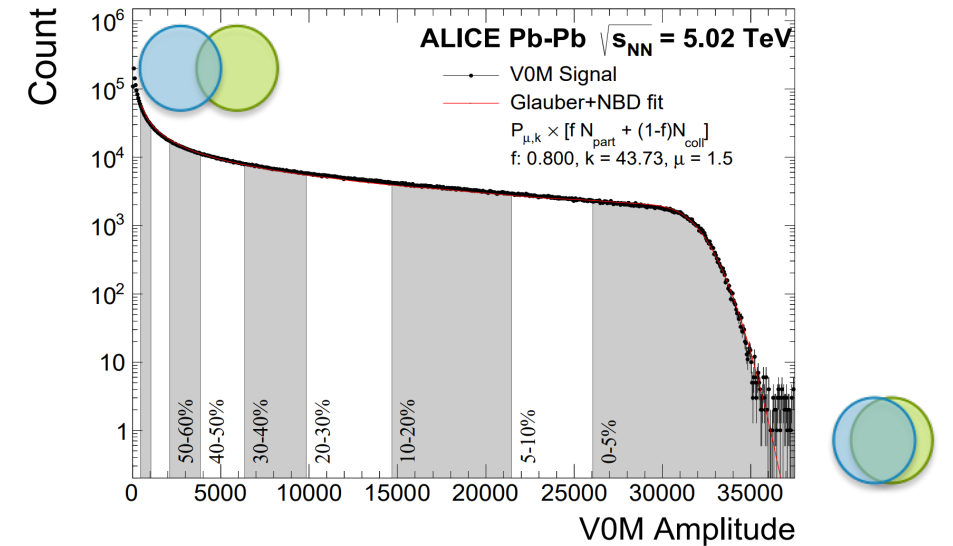
- More **central**, ie. “head-on” collisions
- smaller impact parameter
  - larger overlap region
  - more participants
  - more particles produced

More **peripheral** collision

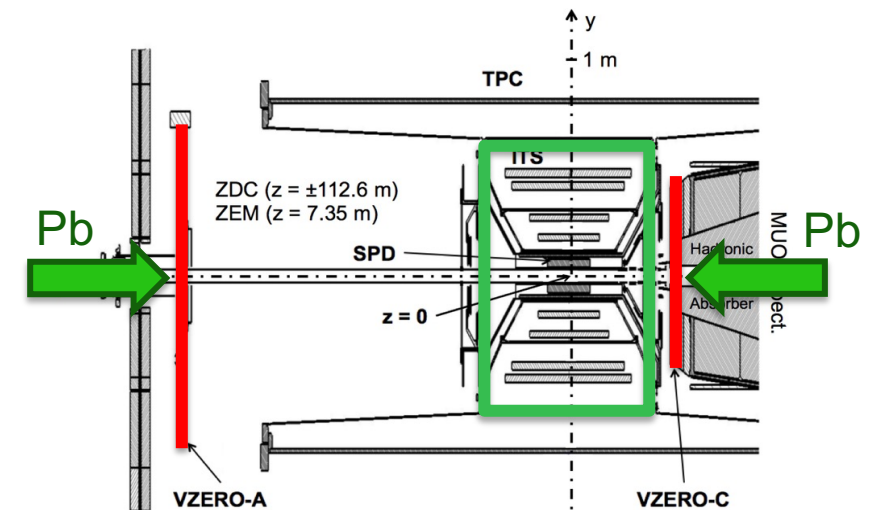
- larger impact parameter
- smaller overlap region
- less participants
- fewer particles produced



Centrality is determined by counting the number of particles (multiplicity) or measuring the energy deposition in a region of phase space *independent* from the measurement, to avoid biases/autocorrelations in the results.



ALICE, PRL 106 (2011) 032301, PRC 91 (2015) 064905



# Rapidity distributions in HI collisions

**Before the collision:** beams with given rapidity

E.g. at RHIC:

- $p_{\text{BEAM}} = 100 \text{ GeV}/c$  per nucleon
- $E_{\text{BEAM}} = \sqrt{(m_p^2 + p_{\text{BEAM}}^2)} = 100.0044$  per nucleon
- $\beta = 0.999956$ ,  $\gamma_{\text{BEAM}} \approx 100$
- $y_{\text{BEAM}1} = -y_{\text{BEAM}2} = 5.36 \rightarrow \Delta y = 10.8$

**After the collision,** 2 possible scenarios

## 1. Nuclei stopping

- For  $\sqrt{s_{\text{NN}}} \sim 5 - 10 \text{ GeV}$  (AGS,...)

## 2. Transparency

- For  $\sqrt{s_{\text{NN}}} > 100 \text{ GeV}$  (RHIC, **LHC**)
- nuclei slow down to lower  $\gamma$  and  $y$
- particles are produced with a “plateau” at midrapidity

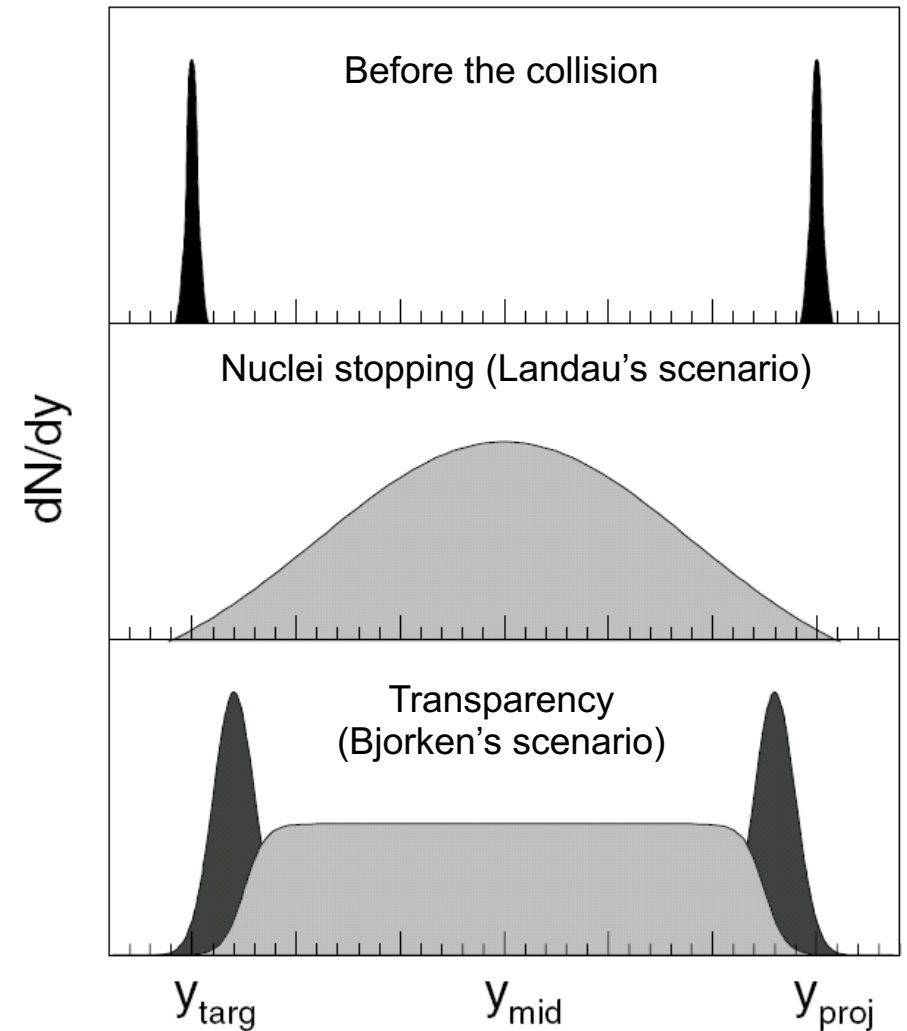
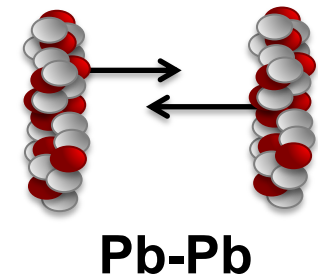
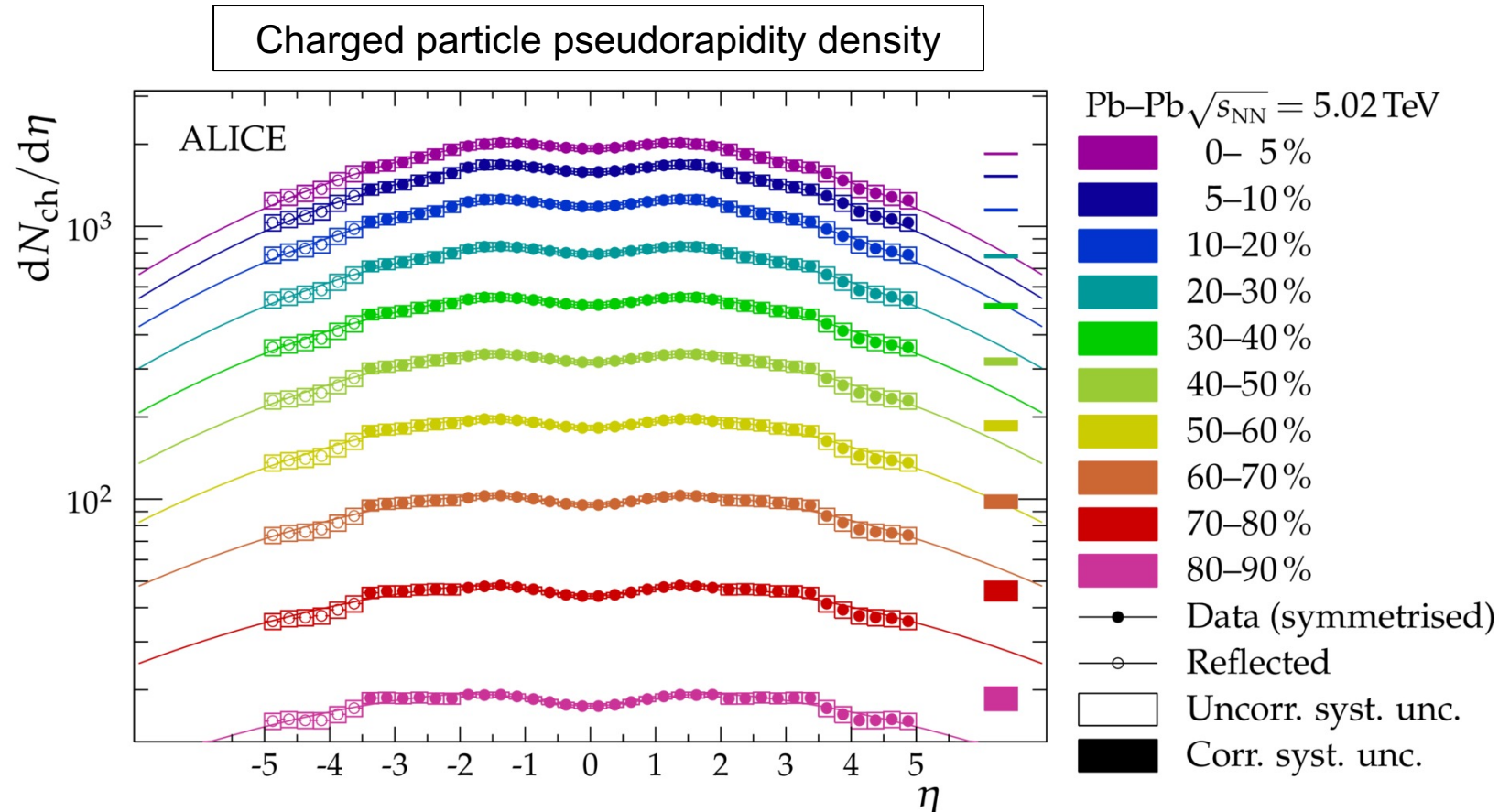


Figure from K. Reygers

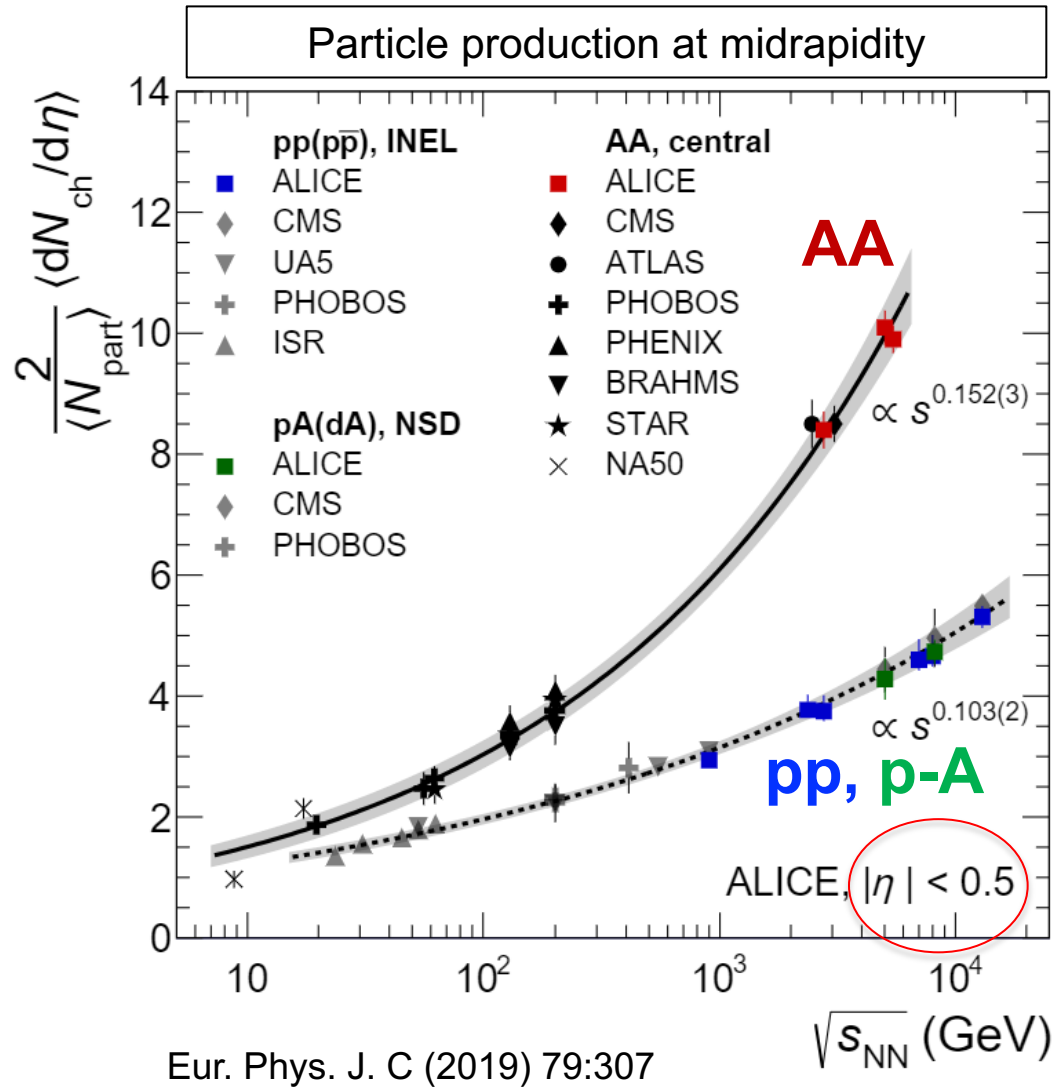
# Charged particle multiplicity vs centrality



ALI-PUB-115086

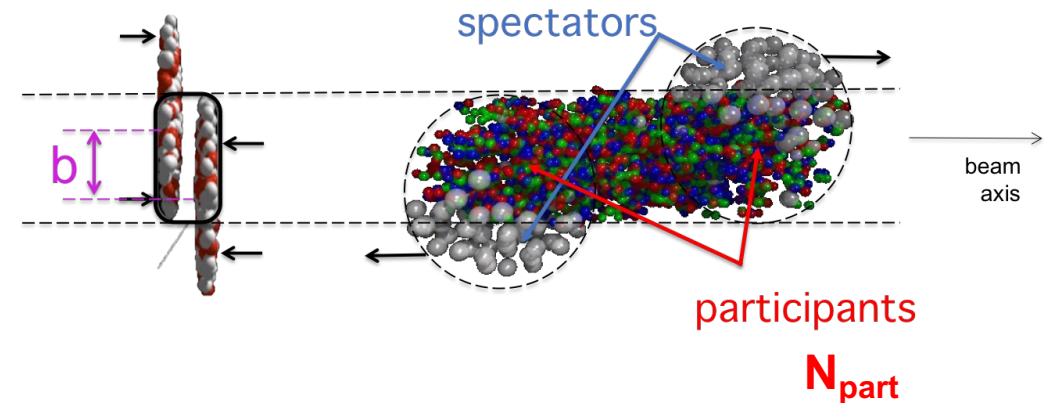
ALICE, Phys.Lett. B 772 (2017) 567-577

# Charged particle production in central HI collisions



**Particle production per participant in HI collisions** follows a steeper power law than in pp, pA and increases by 2-3x from RHIC to the LHC

Heavy-ion collisions are more efficient in transferring energy from beam- to mid-rapidity than pp

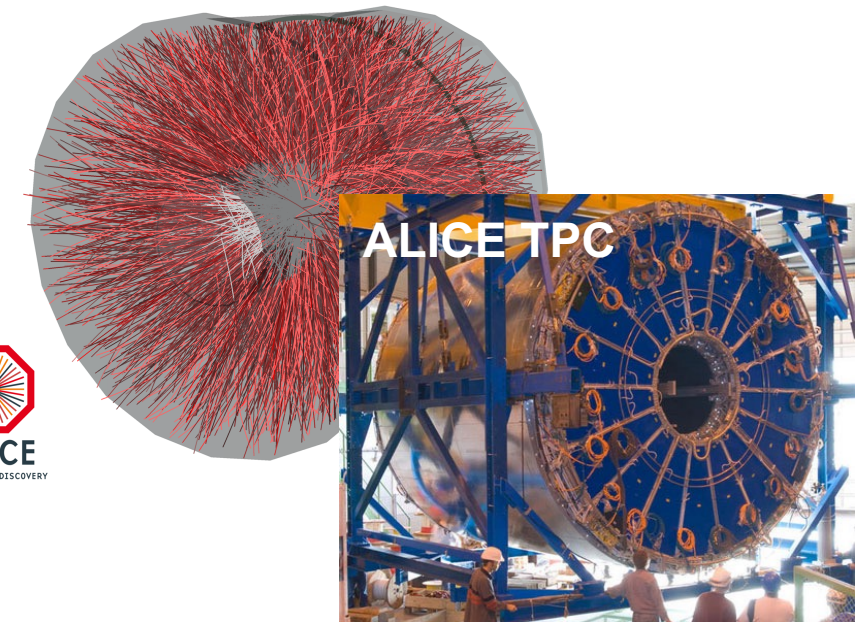
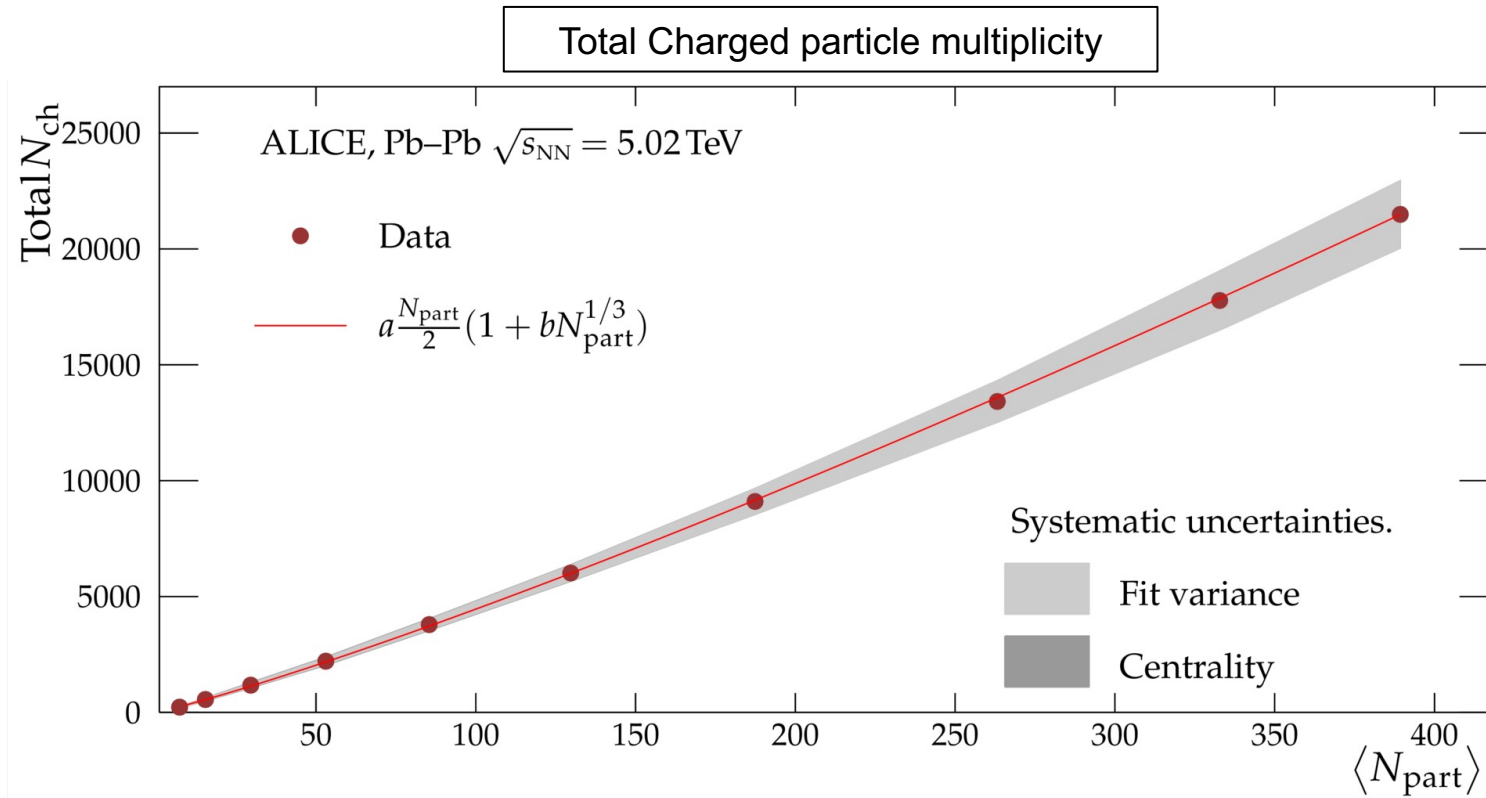




# How many particles are created in a collision?

In a central Pb-Pb collision at the LHC, more than 20000 charged tracks must be reconstructed.

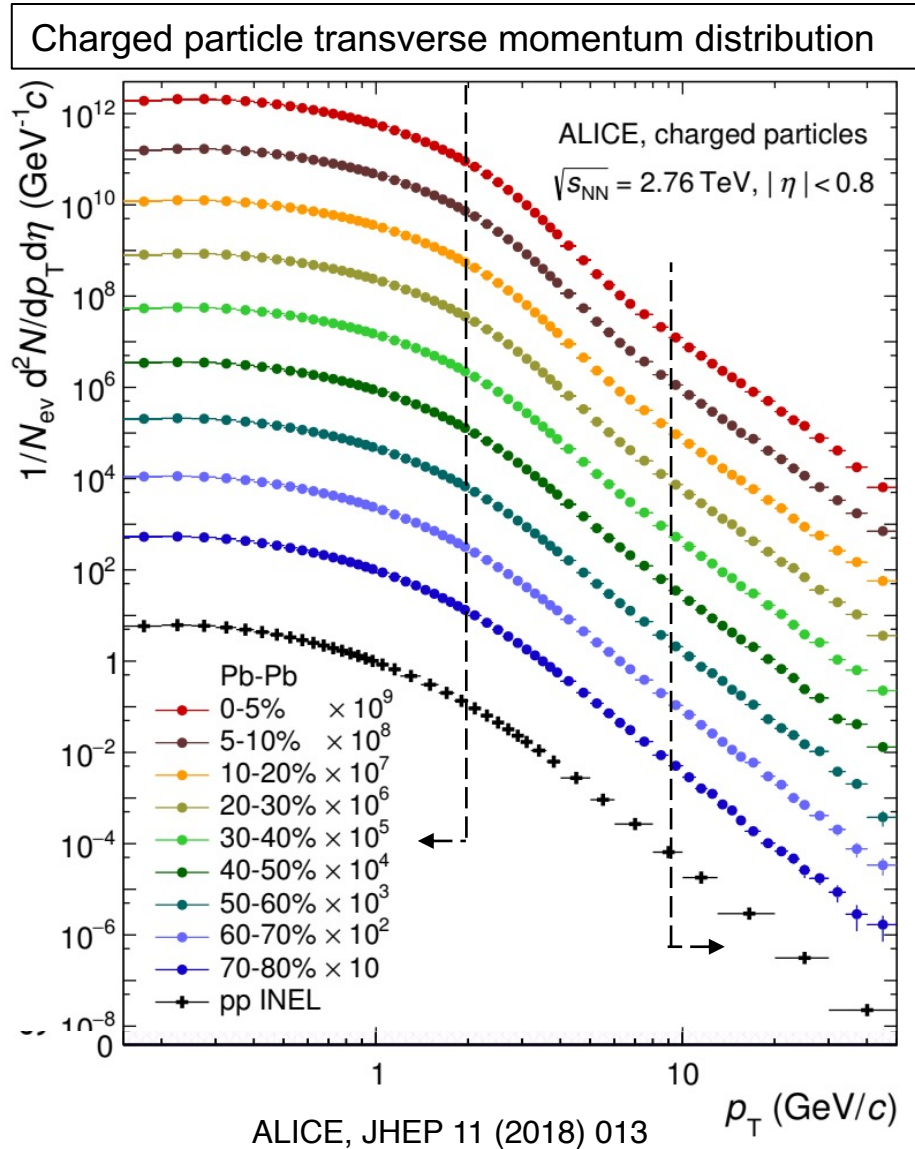
→ High granularity tracking systems, primary importance of tracking, vertexing calibration



ALI-PUB-115091

ALICE, Phys.Lett. B 772 (2017) 567-577

# Particle “spectra”



## Low $p_T (< 2 \text{ GeV}/c)$

- Particle spectra are described by a Boltzmann distribution  $\rightarrow$  “thermal”,  $\sim \exp(-1/k_B T)$
- “Bulk” dominated by light flavor particles
- Non-perturbative QCD regime

## High $p_T (> 8-10 \text{ GeV}/c)$

- Particle spectra described by a power law
- Dominated by parton fragmentation (jets)
- Perturbative QCD regime

## Mid $p_T (2 \text{ to } 8 \text{ GeV}/c)$

- Interplay of parton fragmentation and recombination of partons from QGP

Heavy-ion and high-energy physics have different goals and thus different detector requirements.

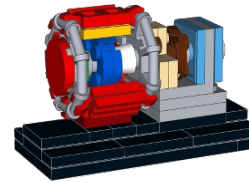
### Observables:

- soft (low  $p_T$ ) and hard (high  $p_T$ ) probes
- hadron production rates (needs PID)
- flow (needs acceptance coverage)
- photon/W/Z (calorimetry)
- jets (coverage, high  $p_T$ )

In HI physics also emphasis on:

- **midrapidity** measurements
- **identification** of hadron species
- soft (non-perturbative) regime, i.e. **low  $p_T$**
- **minimum bias** events

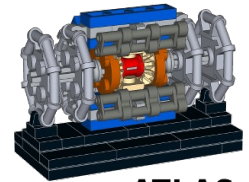
### Complementarity of the LHC experiments



ALICE

#### ALICE

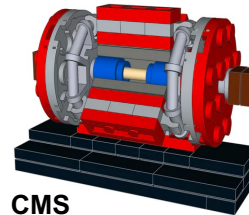
- Low  $p_T$
- PID
- Low material budget next to IP



ATLAS

#### ATLAS/CMS

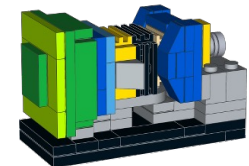
- Wide pseudorapidity coverage
- High  $p_T$  jets



CMS

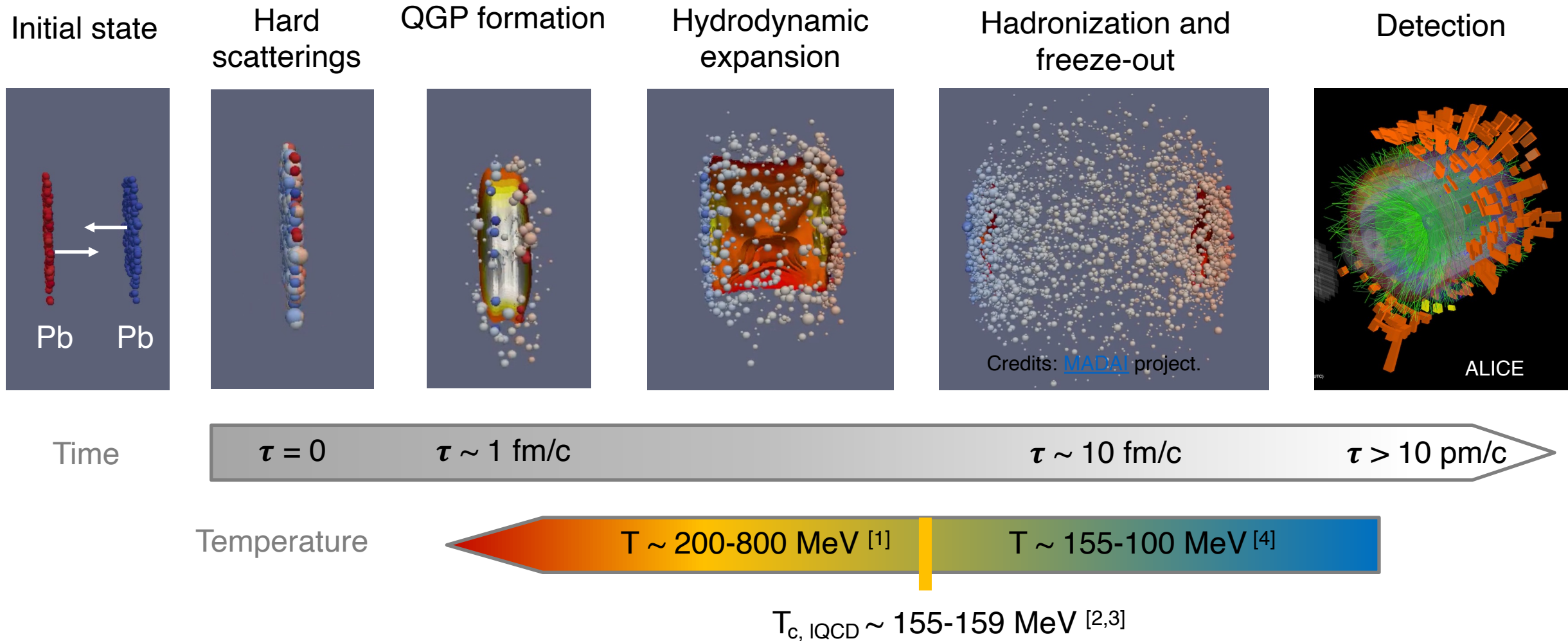
#### LHCb

- Forward pseudorapidity
- PID
- Fixed target



LHCb

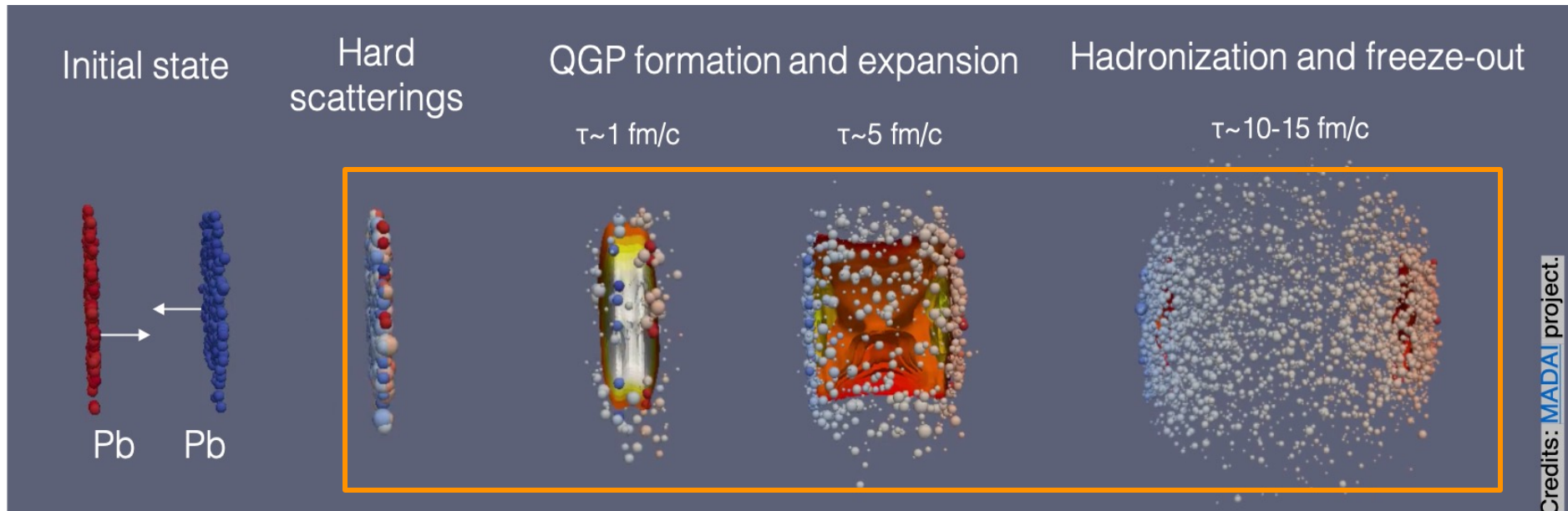
# The standard model of heavy-ion collisions



No direct observation of the QGP is possible  
 → rely on emerging particles as “probes”

- [1] F. Gardim et al. Nature Phys. 16 (2020) 6, 615-619
- [2] A. Bazavov et al., Phys. Lett. B 795 (2019)
- [3] Borsaniy et al. PRL 125 (2020) 5, 052001
- [4] A. Andronic et al., Nature 561 (2018) 7723, 321-330

# Probes 1/2



1 fm/c =  $3 \times 10^{-24}$  s, 1 MeV  $\sim 10^{10}$  K

**High- $p_T$  partons ( $\rightarrow$  jets), charm and beauty quarks ( $\rightarrow$  open HF, quarkonia)**

produced in the early stages in hard processes,

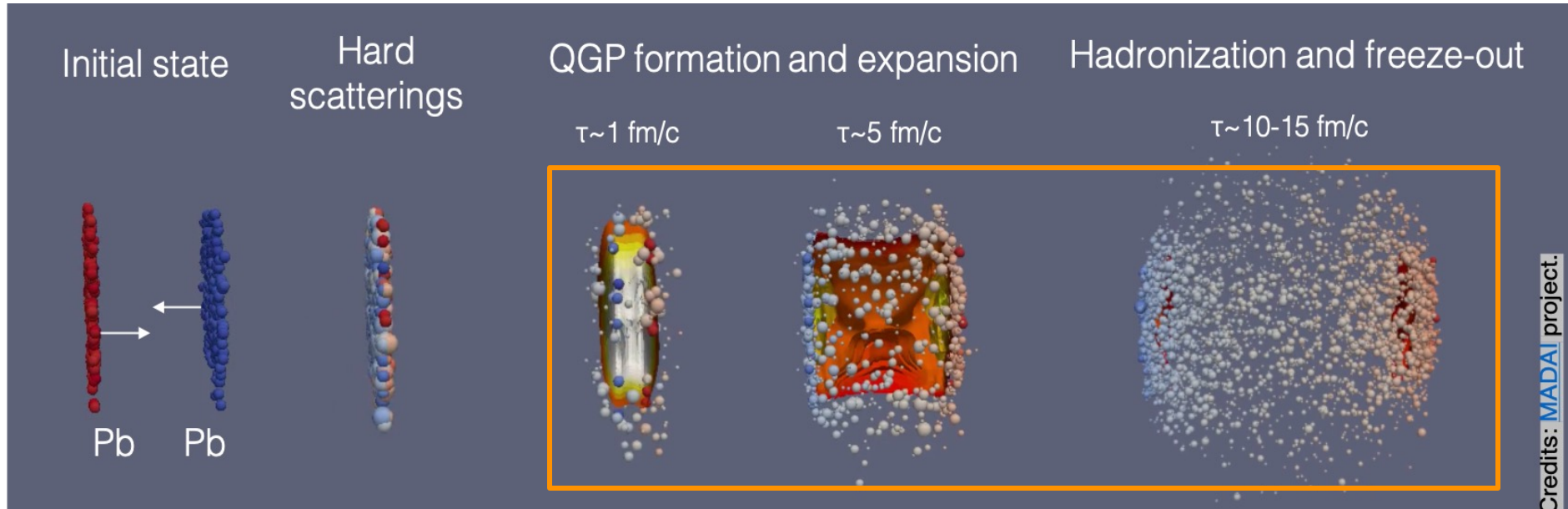
traverse the QGP interacting with its constituents = colored probes in a colored medium

$\rightarrow$  **rare, calibrated probes, perturbative QCD**

$\rightarrow$  **in-medium interaction (energy loss) and transport properties**

$\rightarrow$  **in-medium modification of the strong force and of fragmentation**

# Probes 2/2



1 fm/c =  $3 \times 10^{-24}$  s, 1 MeV  $\sim 10^{10}$  K

## Low- $p_T$ particles, light flavour hadrons (u,d,s, +nuclei)

produced from hadronization of the strongly-interacting, thermalized QGP constitute the bulk of the system

→ **non-perturbative QCD regime**

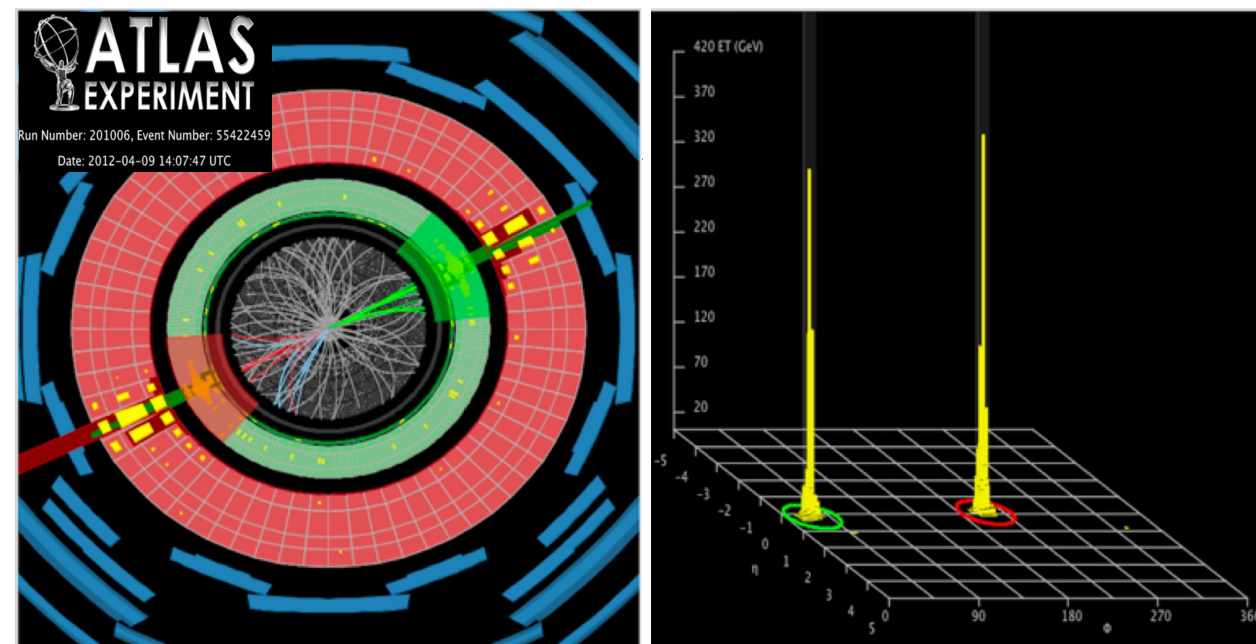
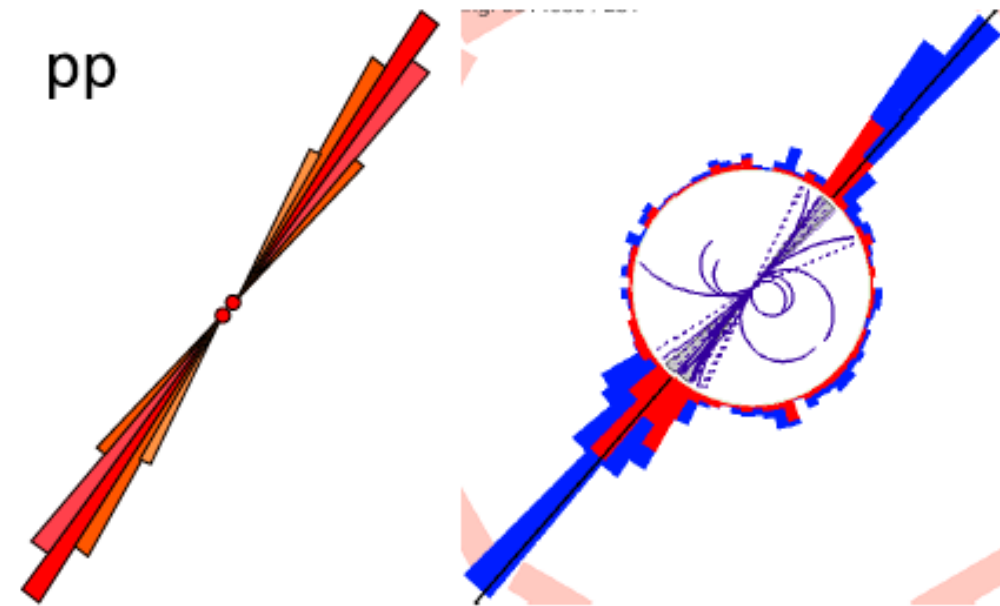
→ **thermodynamical, hydrodynamical and transport properties**

How does the presence of a colored QGP affect particle production?

# Jets

In the early stages of the collision, hard scatterings produce back-to-back recoiling partons, which fragment into collimated “sprays” of hadrons.

→ **in-vacuum fragmentation**



ATLAS, pp collision event display



# Jets

In the early stages of the collision, hard scatterings produce back-to-back recoiling partons, which fragment into collimated “sprays” of hadrons.

→ **in-vacuum fragmentation**

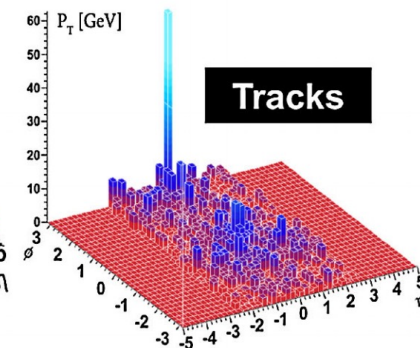
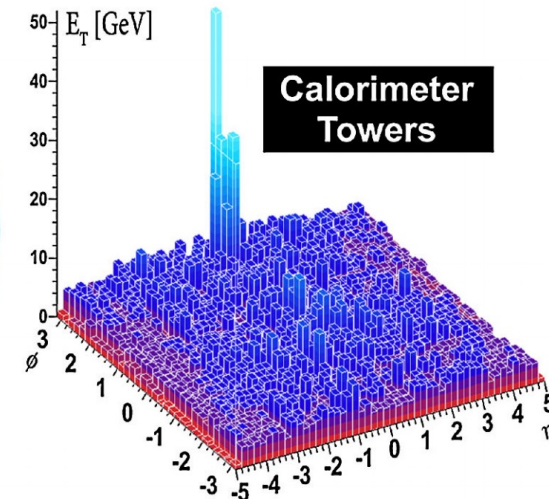
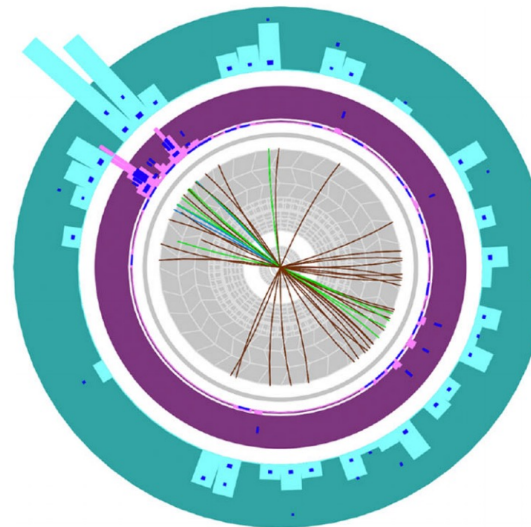
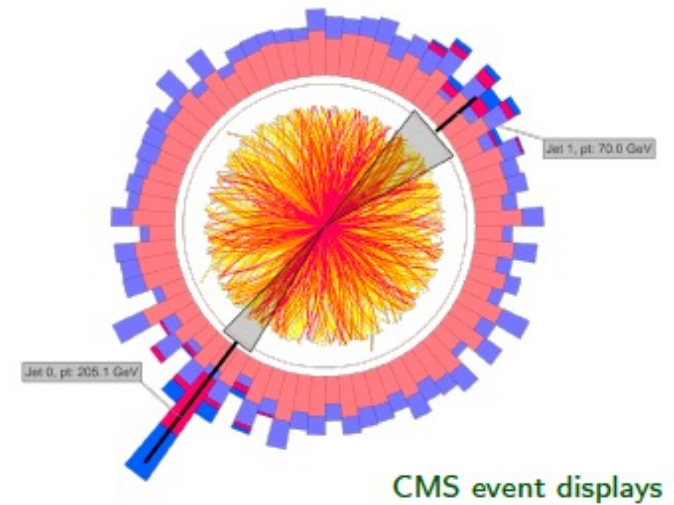
When a QGP is formed, the colored partons traverse and interact with a colored medium.

→ **in-medium fragmentation**

→ **jet “quenching” (energy loss)**

Goal: understand the nature of this energy loss to characterize the strongly-interacting QGP

PbPb



ATLAS

Run: 169045  
Event: 1914004  
Date: 2010-11-12  
Time: 04:11:44 CET

# The nuclear modification factor, $R_{AA}$

$$R_{AA}(p_T) = \frac{1}{\langle N_{coll} \rangle} \frac{dN_{AA} / dp_T}{dN_{pp} / dp_T}$$

If a AA collision is a incoherent superposition of independent pp collisions, the  $p_T$  spectra in AA collisions can be obtained by scaling the  $p_T$  spectra in pp collisions by the number of nucleon-nucleon collisions,  $N_{coll}$  :

$$dN_{AA} / dp_T = N_{coll} \times dN_{pp} / dp_T$$

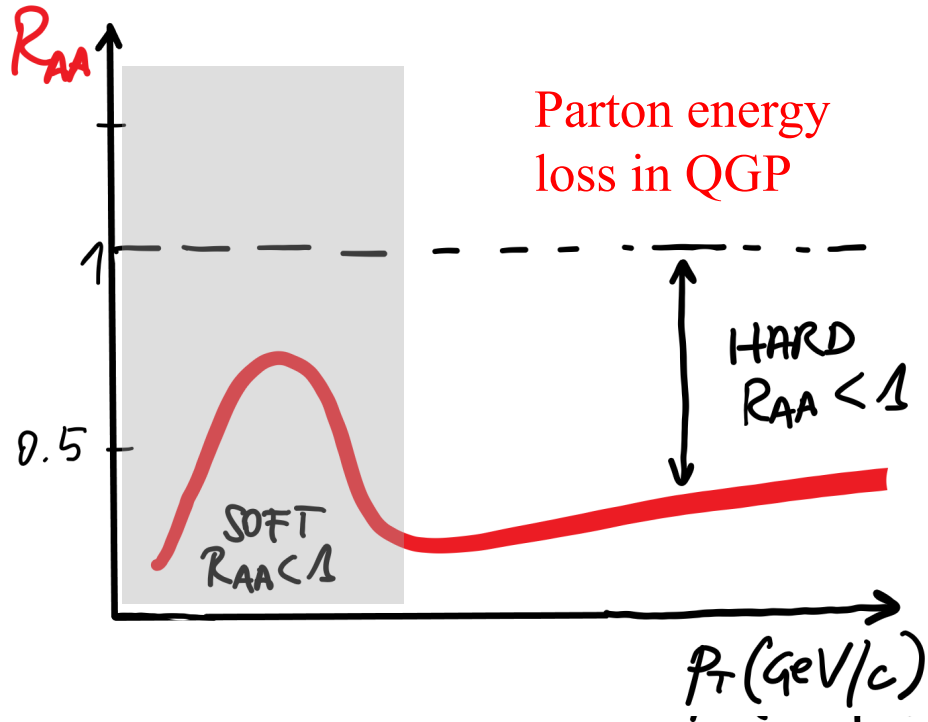
and  $R_{AA} = 1$  at high  $p_T$

→ the medium is transparent to the passage of partons

If  $R_{AA} < 1$  at high  $p_T$

→ the medium is opaque to the passage of partons

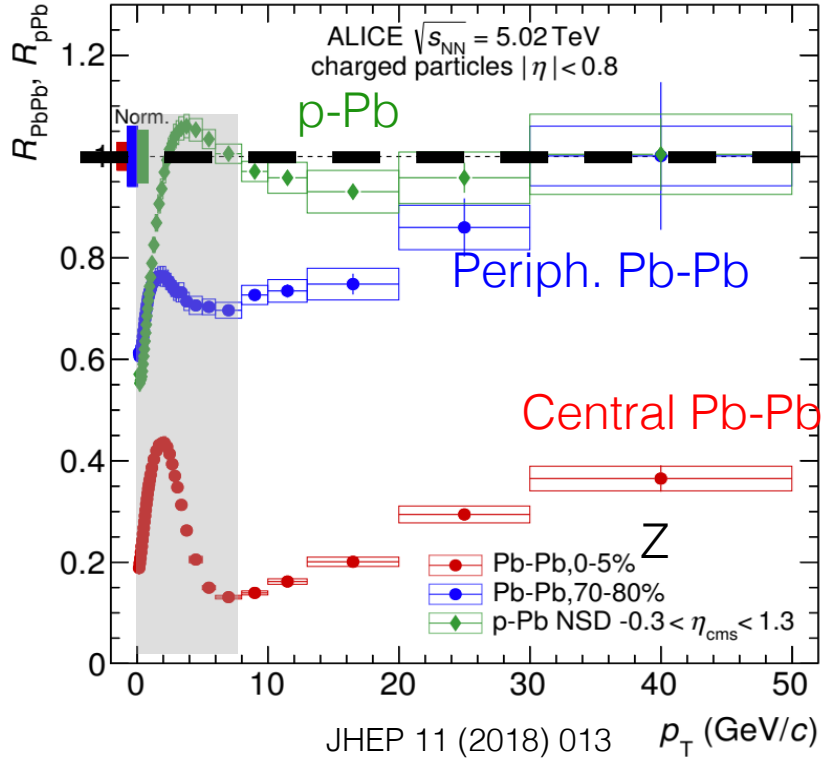
→ **parton-medium final state interactions, energy loss, modification of fragmentation in the medium**



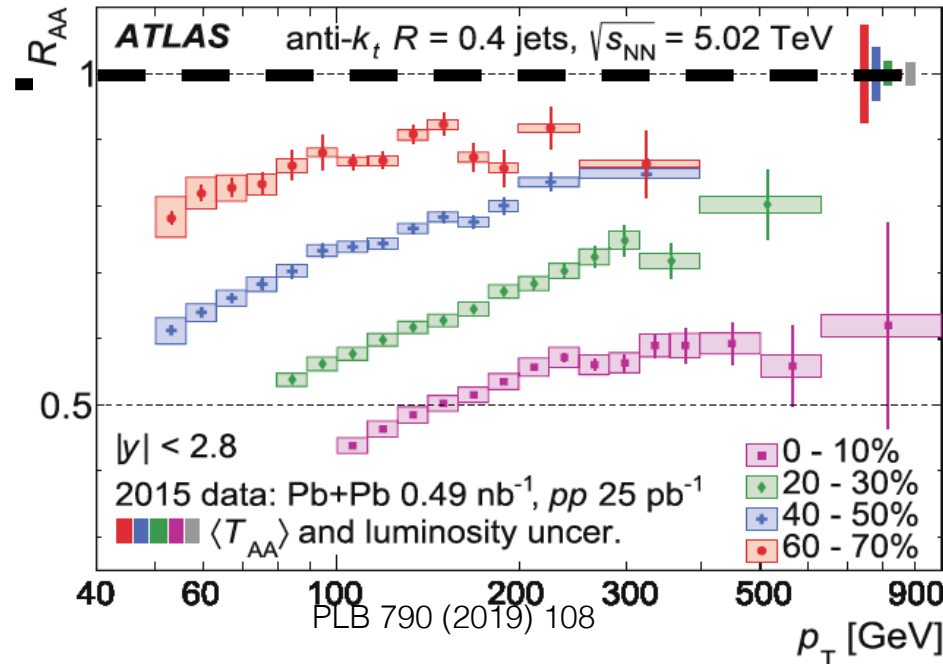
# Evidence of parton energy loss in QGP

$$R_{AA}(p_T) = \frac{1}{\langle N_{coll} \rangle} \frac{dN_{AA} / dp_T}{dN_{pp} / dp_T}$$

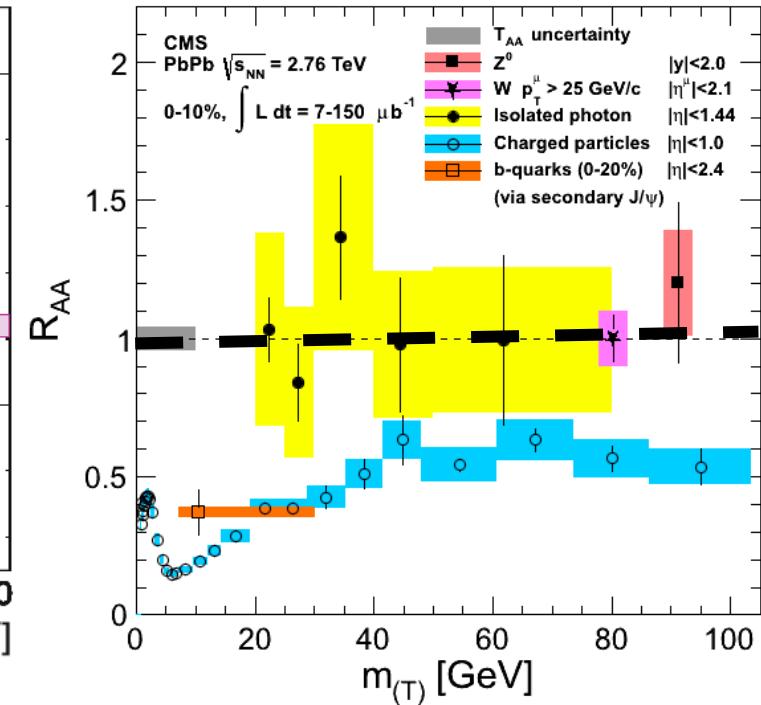
Charged particles



Inclusive jets



EW bosons



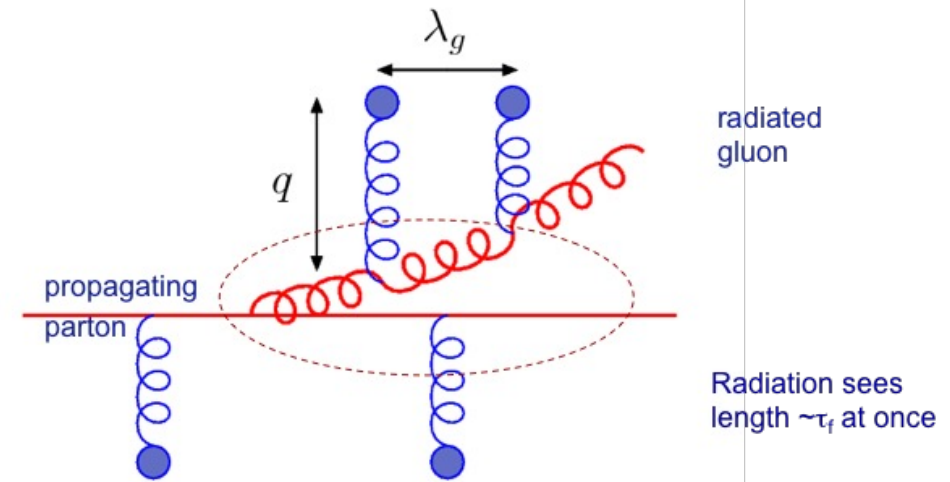
A strong suppression of high- $p_T$  hadrons and jets is observed in central Pb-Pb collisions. No suppression observed in p-Pb collisions, nor for the color-less Z bosons and photons.

→ Jet quenching is explained as **parton energy loss in a strongly interacting plasma**

# Radiative energy loss

In the BDMPS (*Baier-Dokshitzer-Mueller-Peigné-Schiff*) approach, the energy loss depends on

- the **color-charge** via the Casimir factors  $C_r$ 
  - $C_r = C_A = 3$  for g interactions
  - $C_r = C_F = 4/3$  for q,qbar interactions
- the **strong coupling**
- the **path length**  $L$
- the **transport coefficient**  $\hat{q}$  (“q-hat”)
  - gives an estimate of the “strength” of the jet quenching
  - is not directly measurable → from data through model(s)



$$\frac{dE}{dx} = -C_r \alpha_s \hat{q} L$$

$$\hat{q} = \frac{\mu^2}{\lambda}$$

Average transverse momentum transfer

Mean free path

$$\lambda \propto \frac{1}{\rho}$$

Density

# How much energy is lost?

From the BDMPS formula :

$$\langle \Delta E \rangle = \frac{1}{4} \alpha_s C_R \hat{q} L^2 \xrightarrow{\text{Dimensional analysis}} \langle \Delta E \rangle = \frac{\alpha_s C_R \hat{q} L^2}{4\hbar c}$$

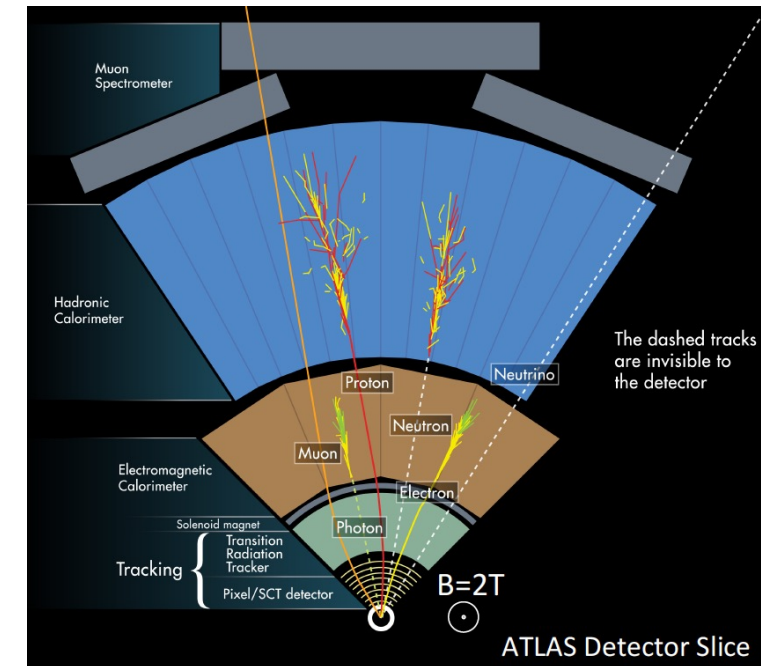
If we take

- $\hat{q} \sim 5 \text{ GeV}^2/\text{fm}$
- $\alpha_s = 0.2$ , strong coupling for  $Q^2 = 10 \text{ GeV}$
- $C_R = 4/3$
- $L = 7.5 \text{ fm}$

we obtain  $\langle \Delta E \rangle \sim 95 \text{ GeV}$

Only partons with  $E \gtrsim 105 \text{ GeV}$  can traverse a 7.5 fm radius fireball and exit with  $p_T \gtrsim 10 \text{ GeV}/c$

In other words, it takes a  $\sim 7.5 \text{ fm}$  radius QGP droplet to stop a jet of  $\sim 100 \text{ GeV}$  (or  $\sim 1.5 \text{ m}$  of hadronic calorimeter)



# Jet transport coefficient $\hat{q}$

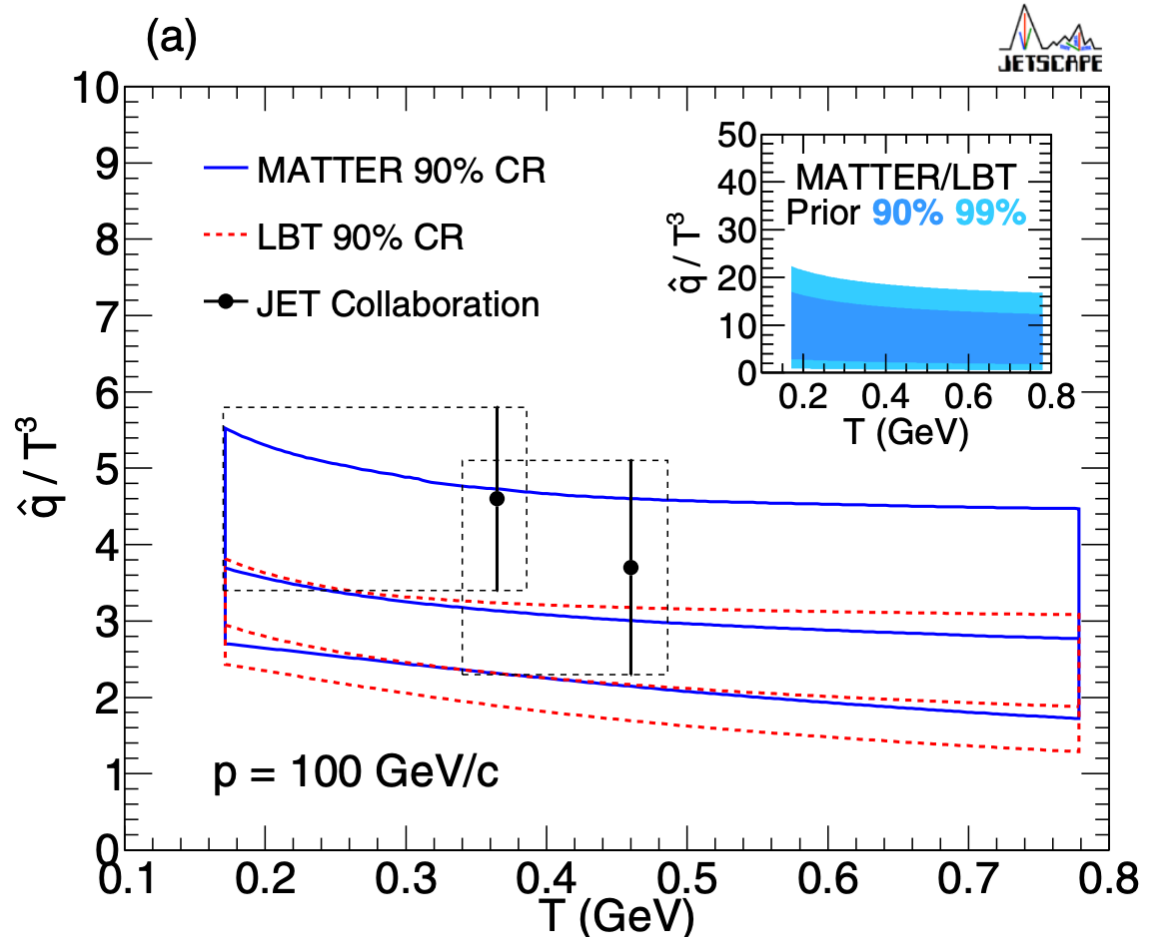
A recent combined analysis of the RHIC and the LHC data on jet quenching (inclusive hadron  $R_{AA}$ ) allowed to extract a value for the  $\hat{q}$  parameter

$$\frac{\hat{q}}{T^3} \approx \begin{cases} 4.6 \pm 1.2 & \text{at RHIC,} \\ 3.7 \pm 1.4 & \text{at LHC,} \end{cases}$$

For a quark jet with  $E = 10$  GeV

$$\hat{q} \approx \begin{cases} 1.2 \pm 0.3 \\ 1.9 \pm 0.7 \end{cases} \text{ GeV}^2/\text{fm} \text{ at } \begin{cases} T=370 \text{ MeV} \\ T=470 \text{ MeV} \end{cases}$$

→ Still large uncertainties, but important step **towards a quantitative characterisation** of the QGP.



S. Cao et al., PRC 104, 024905 (2021)

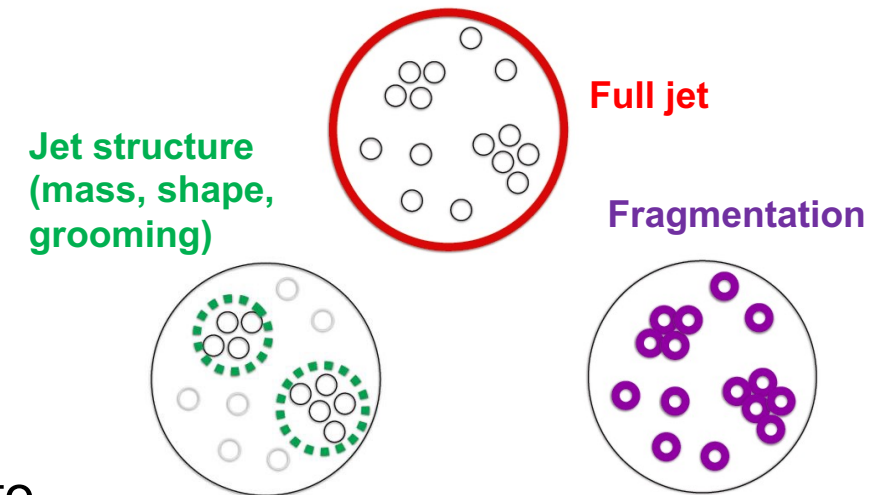
# In-medium jets: main questions

Related to the nature and **properties of the medium**

- Density of the medium and transport properties
- Nature of the scattering centers
- Distribution of the radiated energy
- ...

Related to the nature of the **energy loss mechanism**

- Path length dependence
- Broadening effects
- Microscopic mechanism for energy loss  
→ Study the **shape and structure of jets** for insight into the details of jet modification mechanisms due to interactions with the plasma
  
- Flavour dependence  
→ **measure charm and beauty  $R_{AA}$**



# Charm and beauty

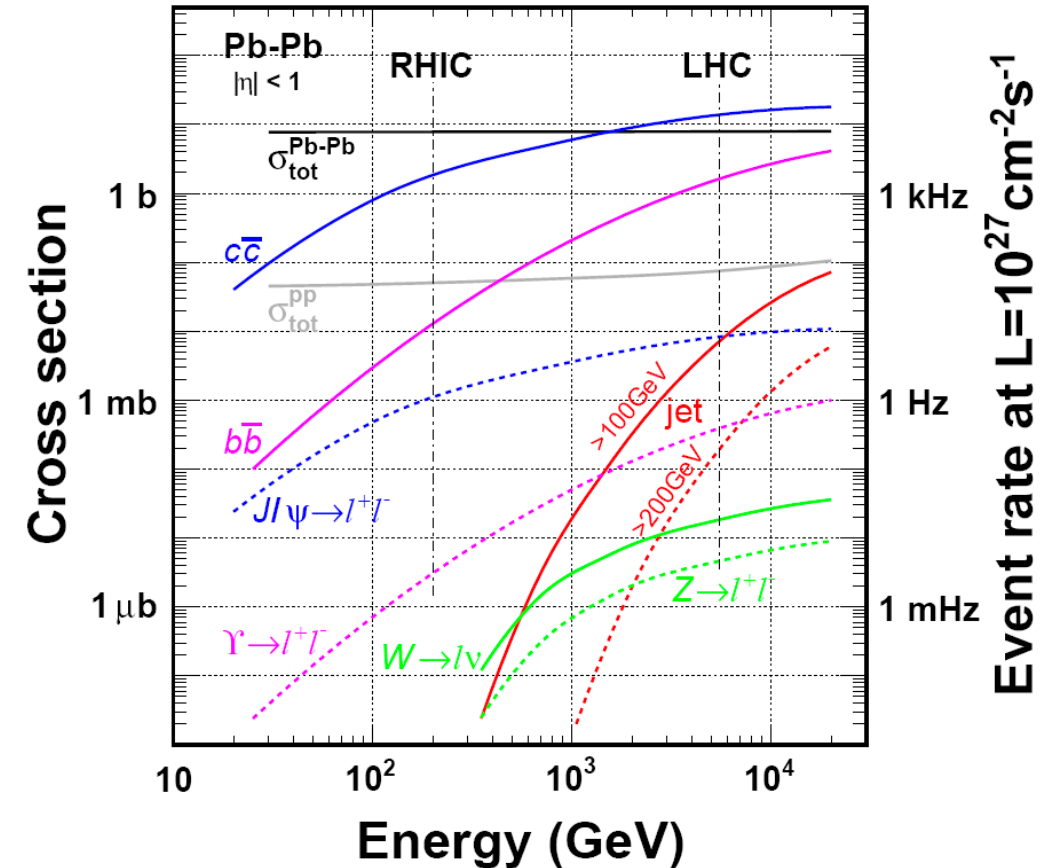
Heavy flavours:

$m(\text{charm}) \sim 1.3 \text{ GeV}/c^2$

$m(\text{beauty}) \sim 4.7 \text{ GeV}/c^2$

are ideal probes of the QGP at the LHC:

- **large production cross sections**
- Produced in **initial hard** parton scatterings
- **controlled** values of mass and colour charge of the propagating parton
- “brownian” motion through the medium, **diffusion**
- sensitive to QGP **hadronisation** (baryon/meson)





# Energy loss of charm and beauty

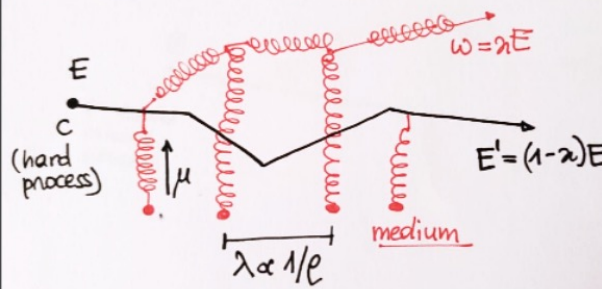
Charm and beauty lose energy via **gluon radiation + elastic collisions**

Due to the large masses, radiative energy loss is subject to the **dead cone effect** = suppression of the gluon radiation emitted by a (slow) heavy quark at small angles,  $\vartheta < \vartheta_{DC} \sim m_q/E_q$

→ **hierarchy** in energy loss:  $\Delta E_g > \Delta E_c > \Delta E_b$

→ radiative energy loss reduced by 25% (c) and 75% (b) [ $\mu = 1 \text{ GeV}/c^2$ ]

In-medium  $E_{\text{loss}}$



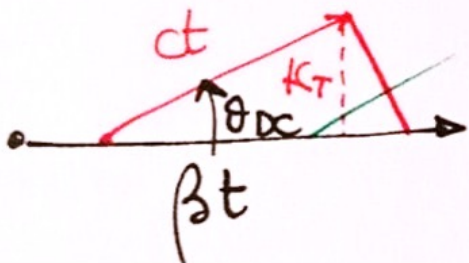
Baier-Dokshitzer-Mueller-Peigné-Schiff,  
Nucl. Phys. B. 483 (1997) 291

$$\langle \Delta E \rangle \propto \alpha_s C_r \hat{q} L^2$$

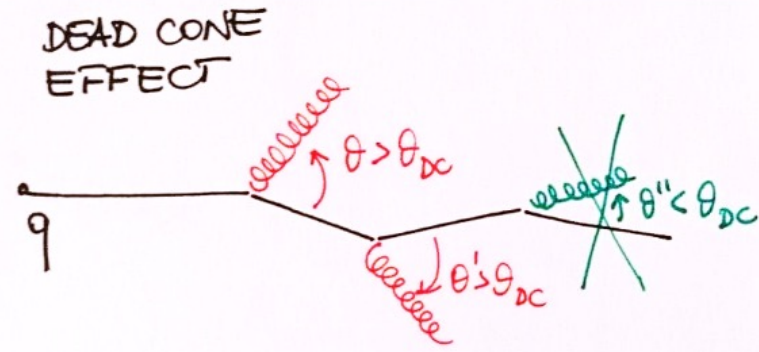
$\hat{q} = \frac{\mu^2}{\lambda}$

Average transverse momentum transfer  
Mean free path  $\sim 1/\text{density}$

## Dead cone effect

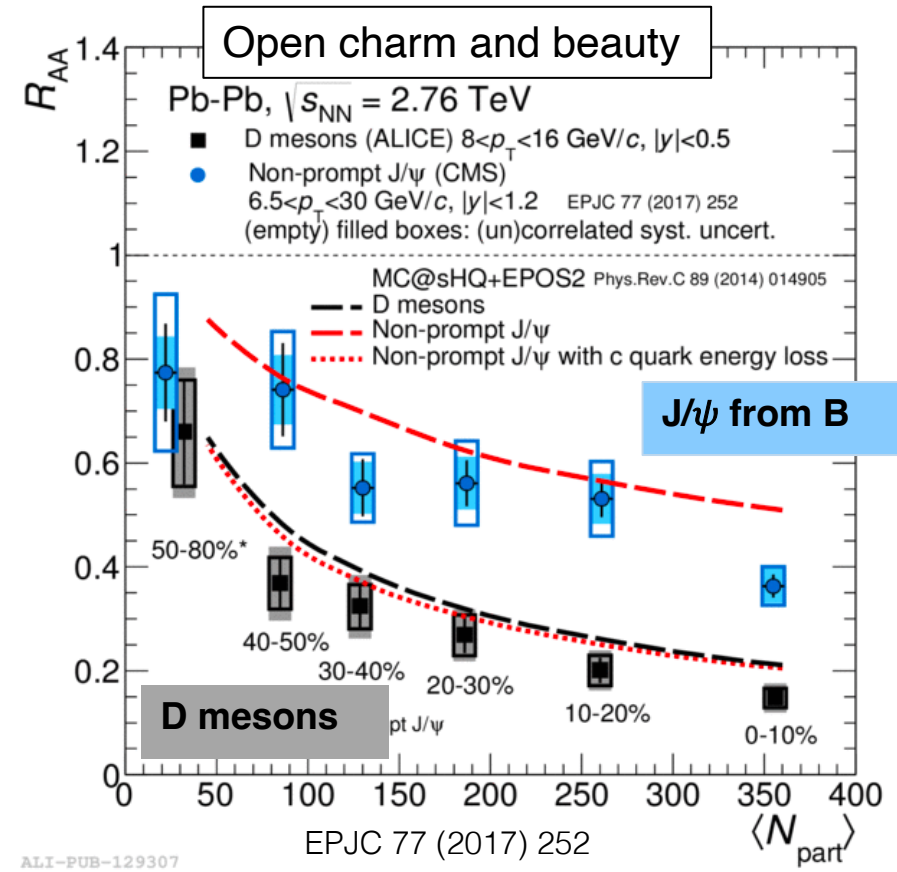
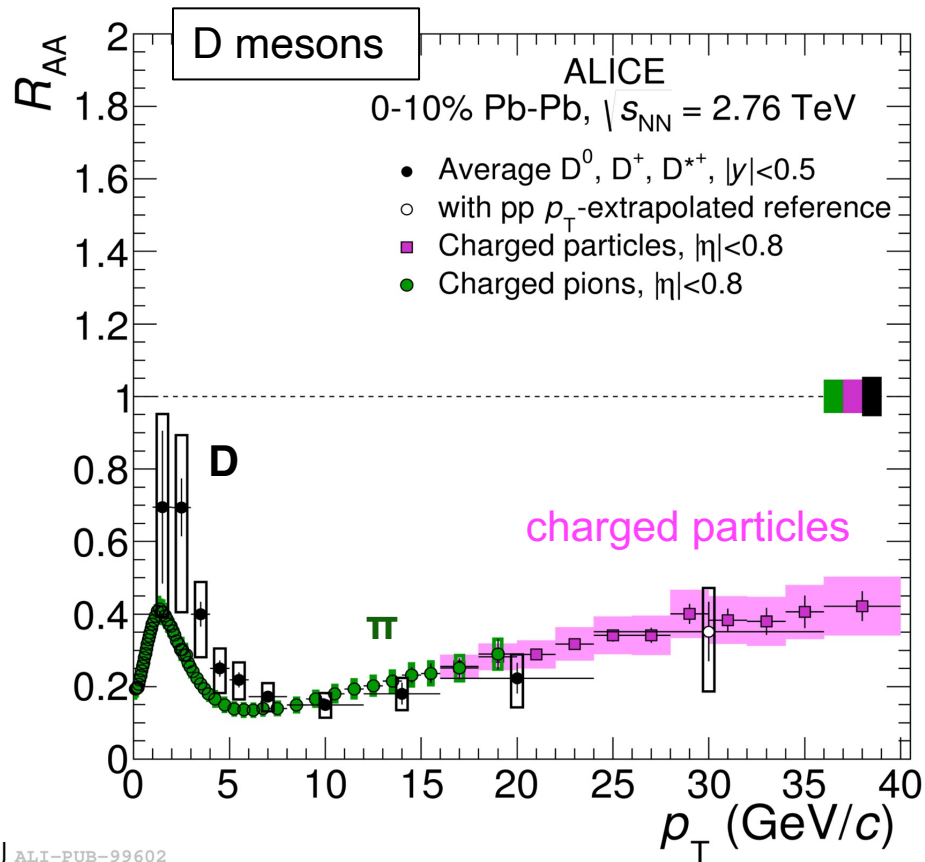


$$\sin \theta_{DC} = 1 - \beta^2 = \left( \frac{M}{E} \right)^2$$

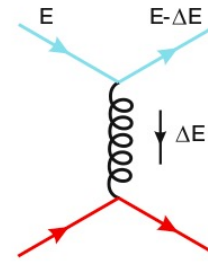


# Nuclear modification of charm and beauty

A strong suppression is observed in the  $R_{AA}$  of D mesons  $J/\psi$  from b decay.  
 $J/\psi$  from beauty is less suppressed than D mesons from charm  $\rightarrow \Delta E_c > \Delta E_b$



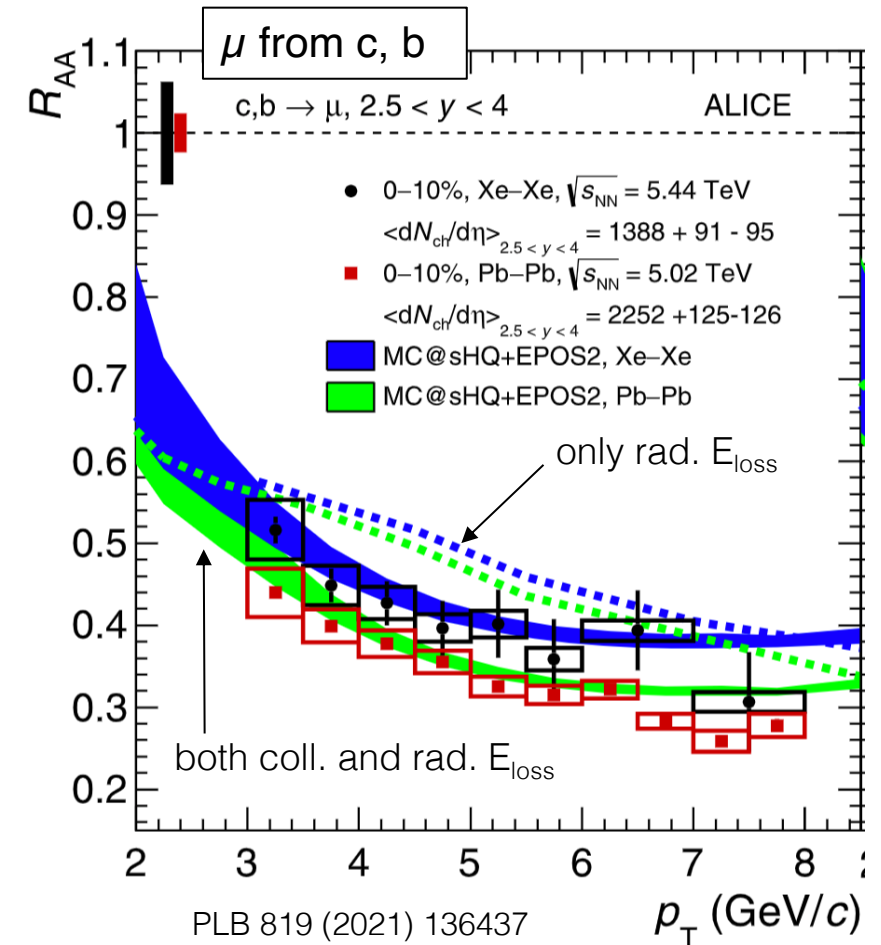
# Collisional energy loss



It depends on

- **path length** through the medium,  $L$  (linearly)
- **parton type**
  - For light quarks  $\Delta E_{q,g} \sim \alpha_S C_R \mu^2 L \ln \frac{ET}{\mu^2}$
  - For heavy quarks  $+ \alpha_S^2 T^2 C_R \mu^2 L \ln \frac{ET}{M^2}$
- **temperature** of the medium,  $T$
- **mass** of the heavy quark  $M$
- average transverse momentum transfer  $\mu$  in the medium

→ Data are well described by models that **include both collisional and radiative  $E_{\text{loss}}$**

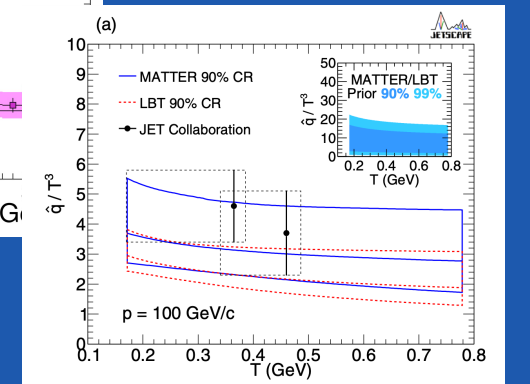
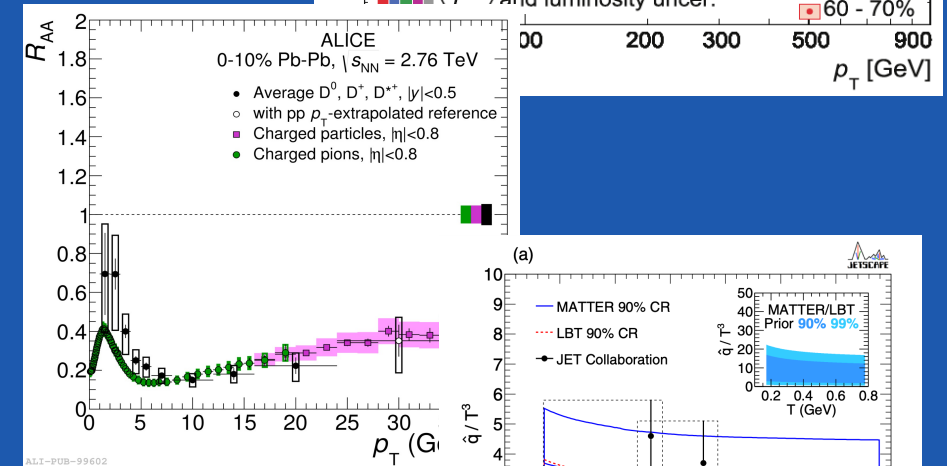
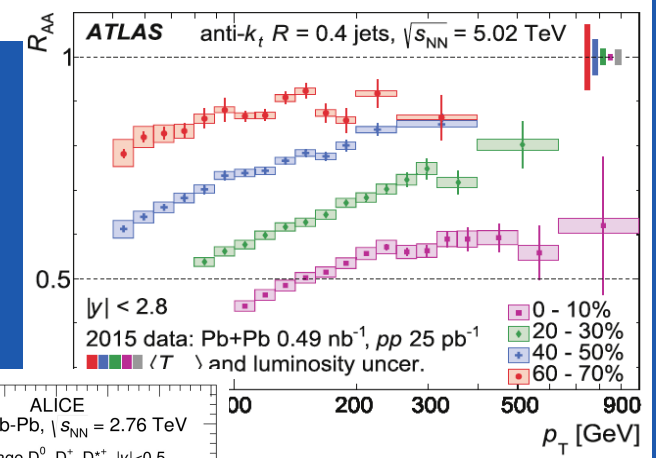
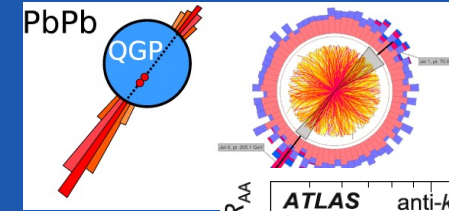


# Summary 1/2

**Evidence of the creation of a strongly-interacting medium** in central heavy ion collisions comes from the observed strong suppression of particle production, explained by the energy loss of colored partons in the colored QGP.

- Radiative energy loss dominates at high  $p_T$  for light flavours, gluons and charm
- Collisional and radiative energy loss play similar role for beauty

A quantitative characterization of the properties of the medium (e.g. transport coefficient, ...) requires **models**.



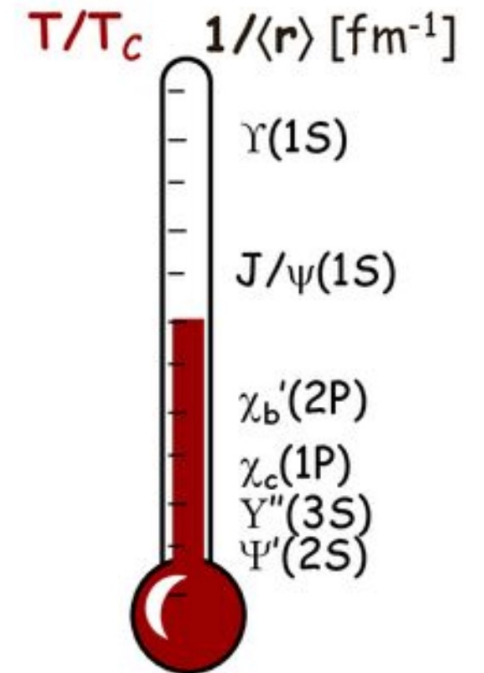
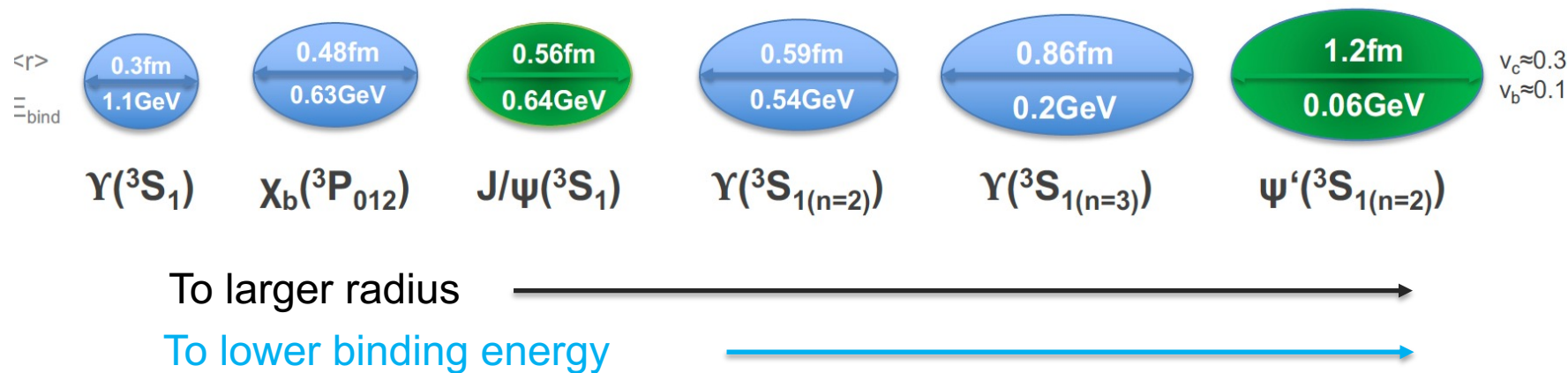
How does the presence of a colored QGP affect hadron formation?

# Quarkonia

c-cbar ( $J/\psi$ ,  $\psi'$ , ...) and b-bar ( $\Upsilon'$ ,  $\Upsilon''$ ,  $\Upsilon'''$ ) pairs are a **laboratory for QCD**:

- Small decay width ( $\sim$ keV), significant BR into dileptons
- Intrinsic separation of energy scales:  $m_Q \gg \Lambda_{\text{QCD}}$  and  $m_Q \gg B_E$
- A variety of states characterized by different binding energies

→ Goal: understand mechanisms of **dissociation and regeneration** in QGP



# Quarkonium as a thermometer for QGP

Charmonium suppression ( $J/\psi$ ,  $\psi'$ , ...) suggested as "smoking gun" signatures for the QGP back in the 1980's.

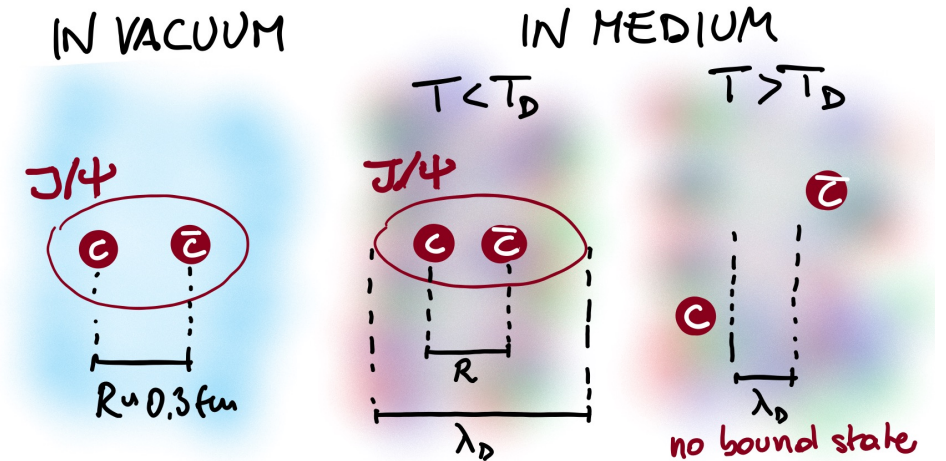
In vacuum ( $T=0$ ), qqbar is bound by the Cornell potential.

$$V(r) = -\frac{\alpha}{r} + kr$$

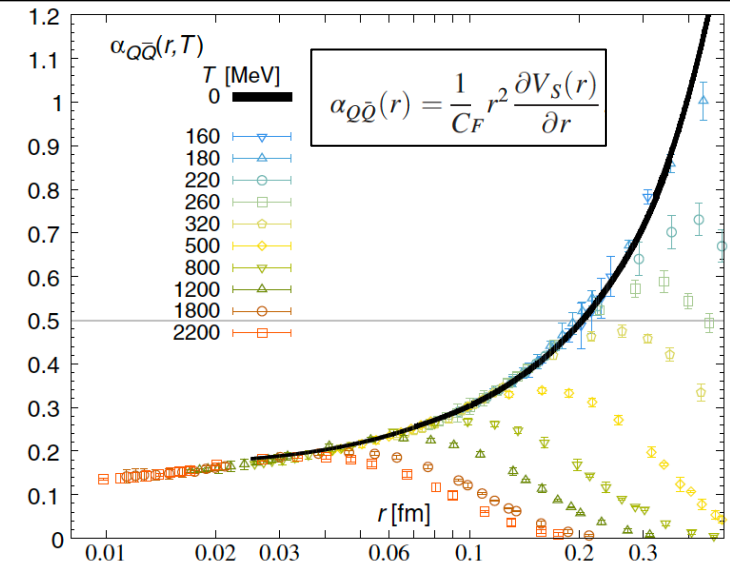
When the qqbar is immersed **in the dense and hot QGP ( $T > 0$ )**, the surrounding color charges screen the binding potentials (color Debye screening), resulting in

$$V(r) = -\frac{\alpha}{r} e^{-r/\lambda_D}$$

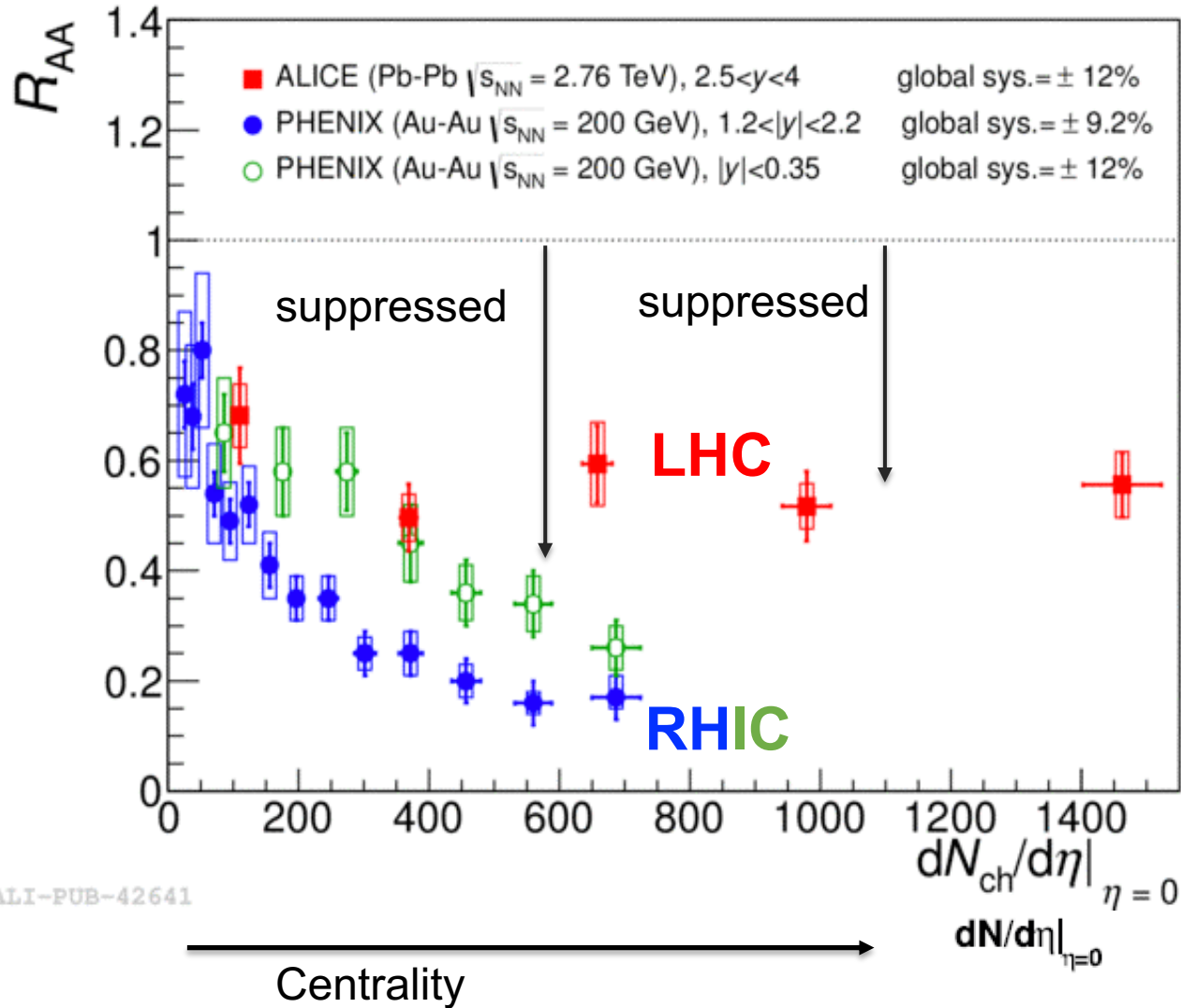
The effective coupling between q and qbar at large distances gets reduced  $\rightarrow$  **q-qbar melting**



Effective coupling from (2+1) QCD at various T



# J/ψ suppression



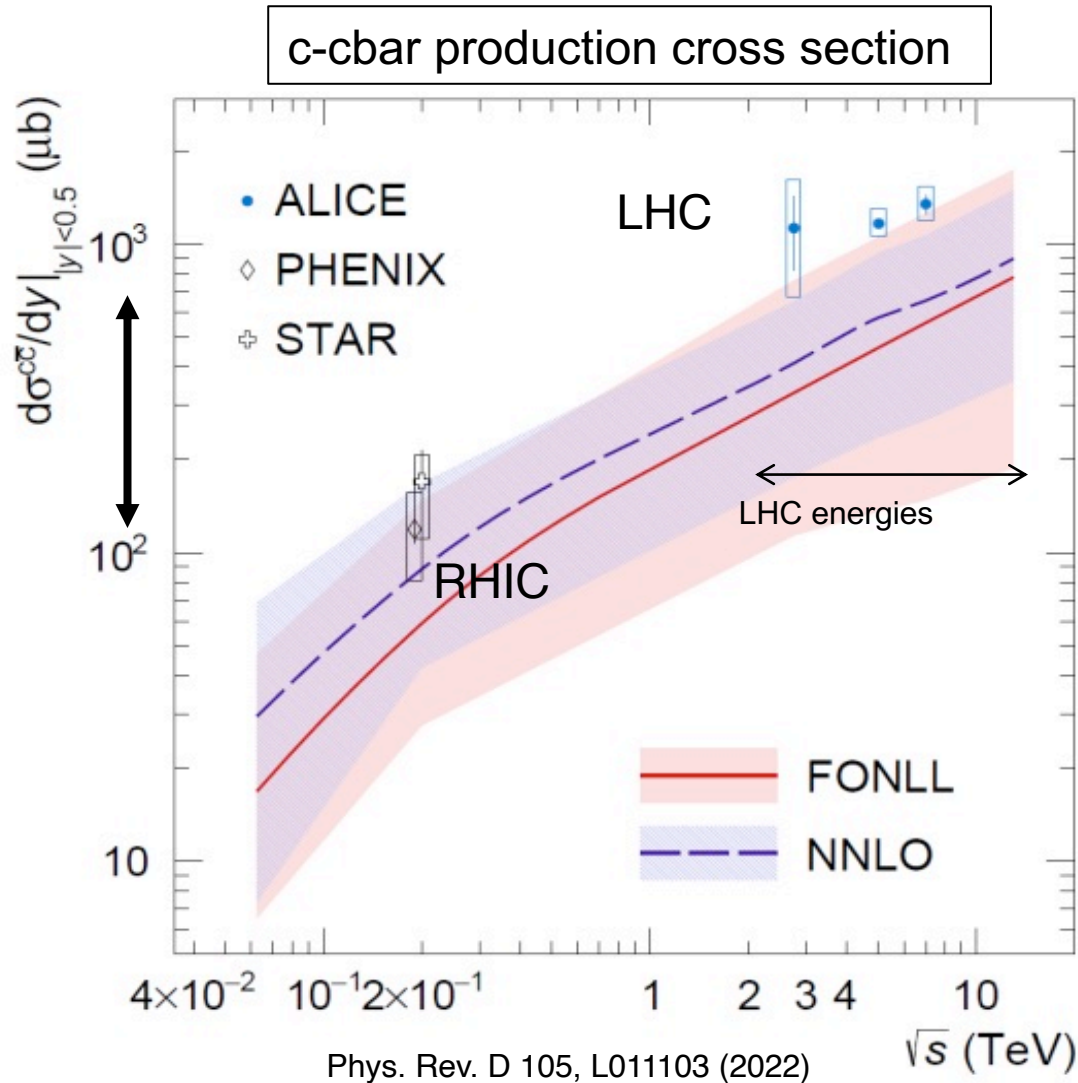
- observed at the SPS ( $\sqrt{s_{NN}} = 17$  GeV)
- later measured at RHIC ( $\sqrt{s_{NN}} = 200$  GeV) up to very high multiplicities

For similar multiplicities the suppression at SPS is similar to that at RHIC despite the energy difference

At the LHC ( $\sqrt{s_{NN}} = 2.76$  TeV), J/ψ is less suppressed, due to the larger charm cross section.



# J/ $\psi$ production vs $\sqrt{s}$



The cross section for producing a c-cbar pair increases with  $\sqrt{s}$

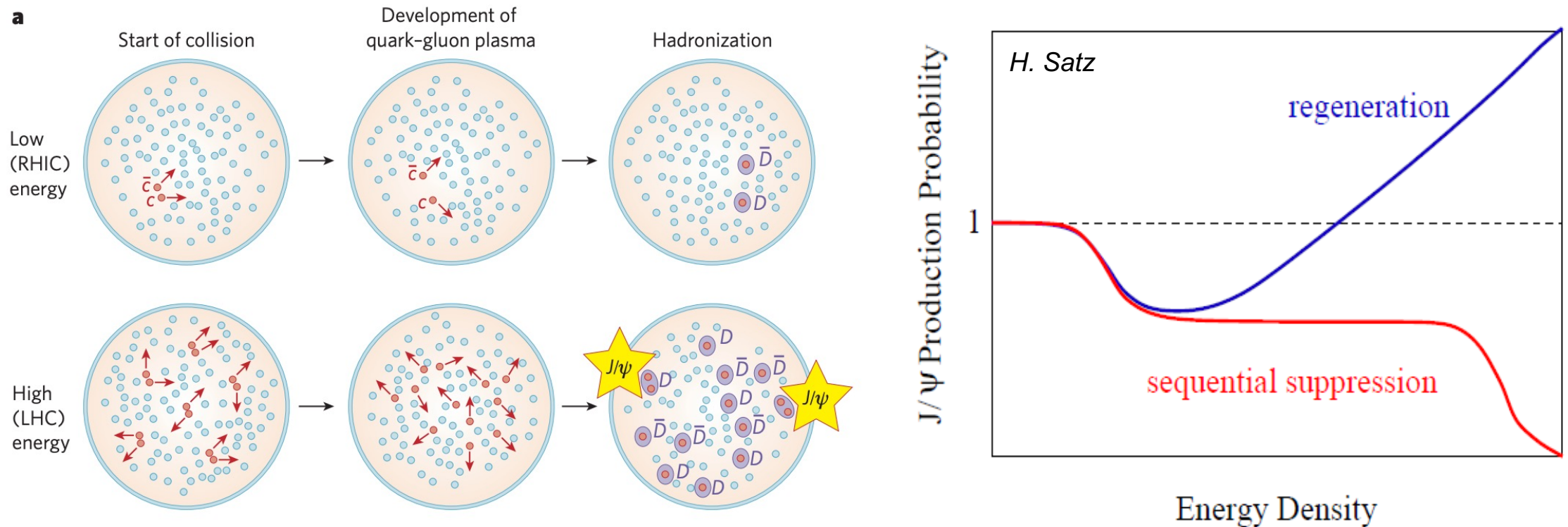
In a central event  
At SPS  $\sim 0.1$  c-cbar  
At RHIC  $\sim 10$  c-cbar  
At LHC  $\sim 100$  c-cbar

c from one c-cbar pair may combine with cbar from another c-cbar pair at hadronization to form a J/ $\psi$   
→ **regeneration!**

# J/ψ suppression vs regeneration 1/2

**(Re)generation of charmonium** and charmed hadron production take place at the phase boundary or in QGP.

Dissociation and regeneration work in opposite directions vs energy density.

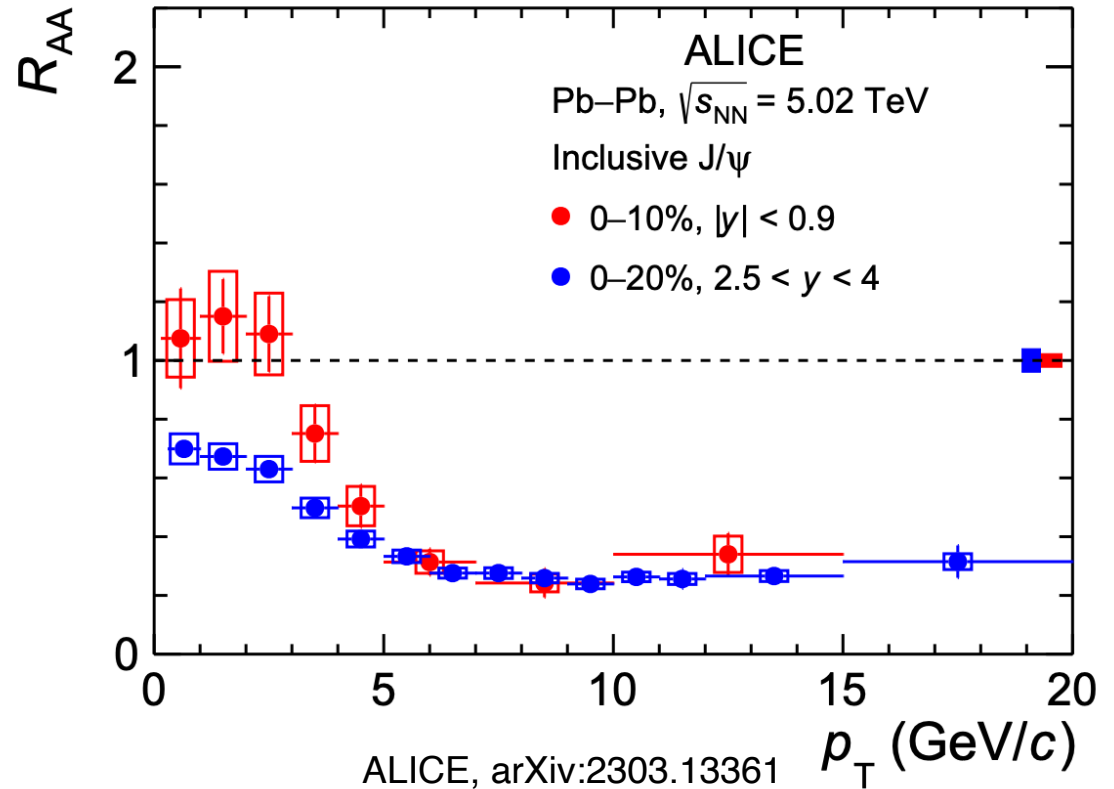
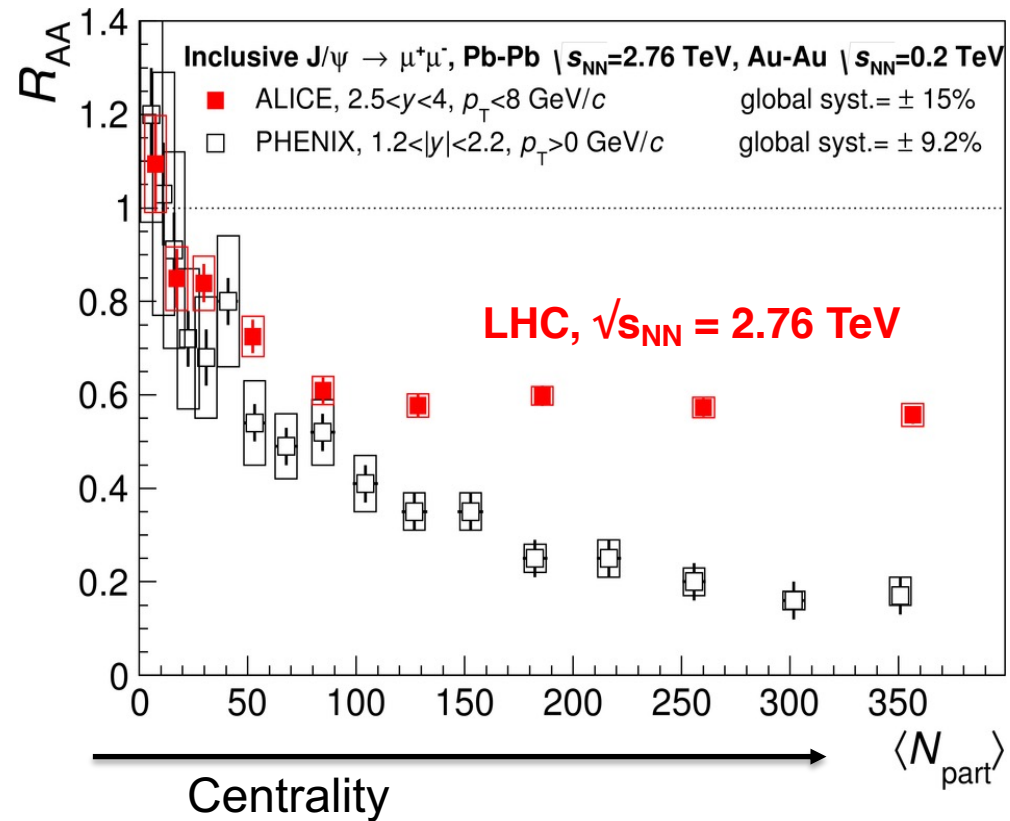


P. Braun-Munzinger, J. Stachel., Nature 448, 302–309 (2007)

# J/ $\psi$ suppression vs regeneration 2/2

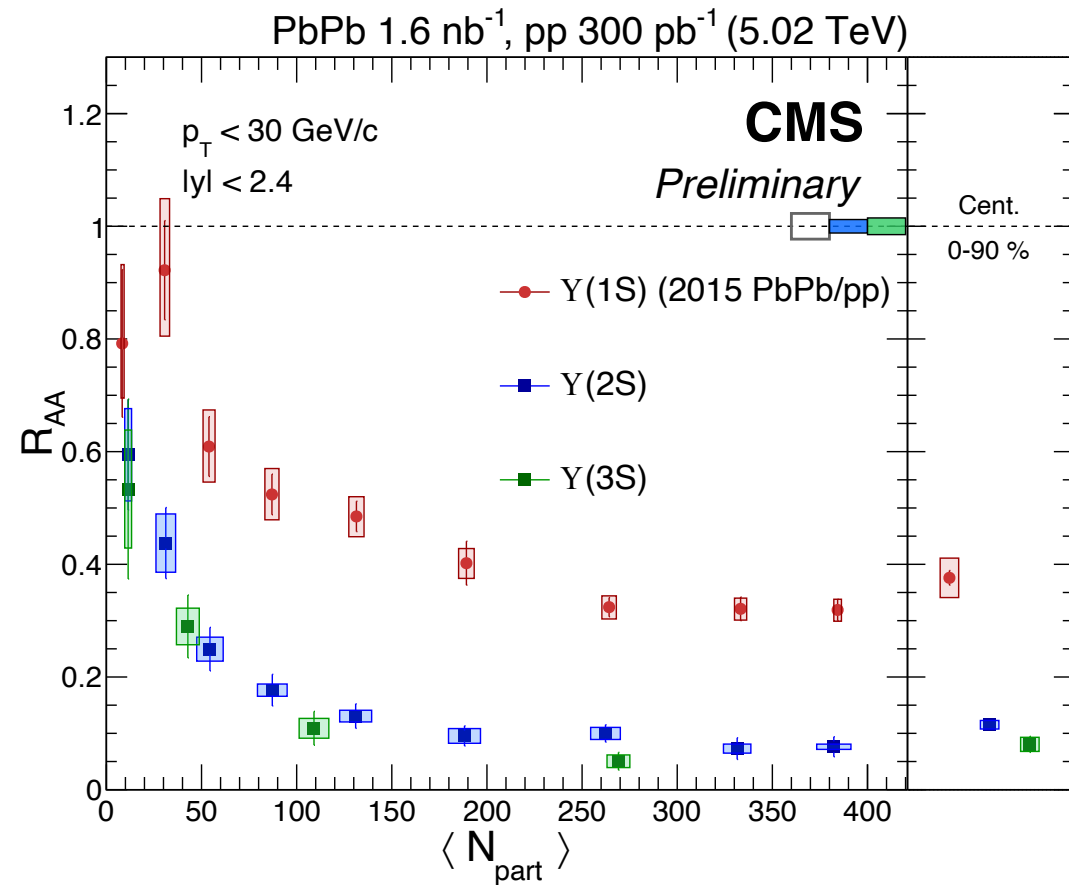
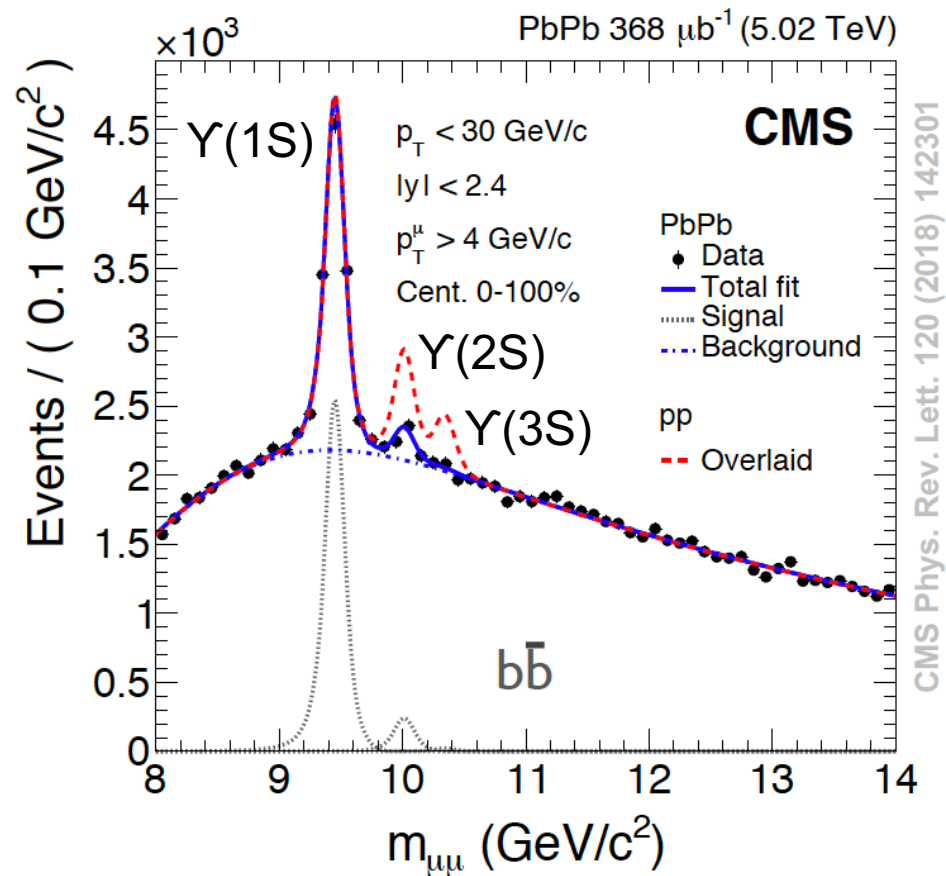
ALICE data from 5.02 TeV Pb-Pb collisions confirm the J/ $\psi$  recombination picture:

- $R_{AA}(\text{LHC}) > R_{AA}(\text{RHIC})$
  - $R_{AA}$  midrapidity  $>$   $R_{AA}$  forward rapidity
- **Signature of de-confinement.**

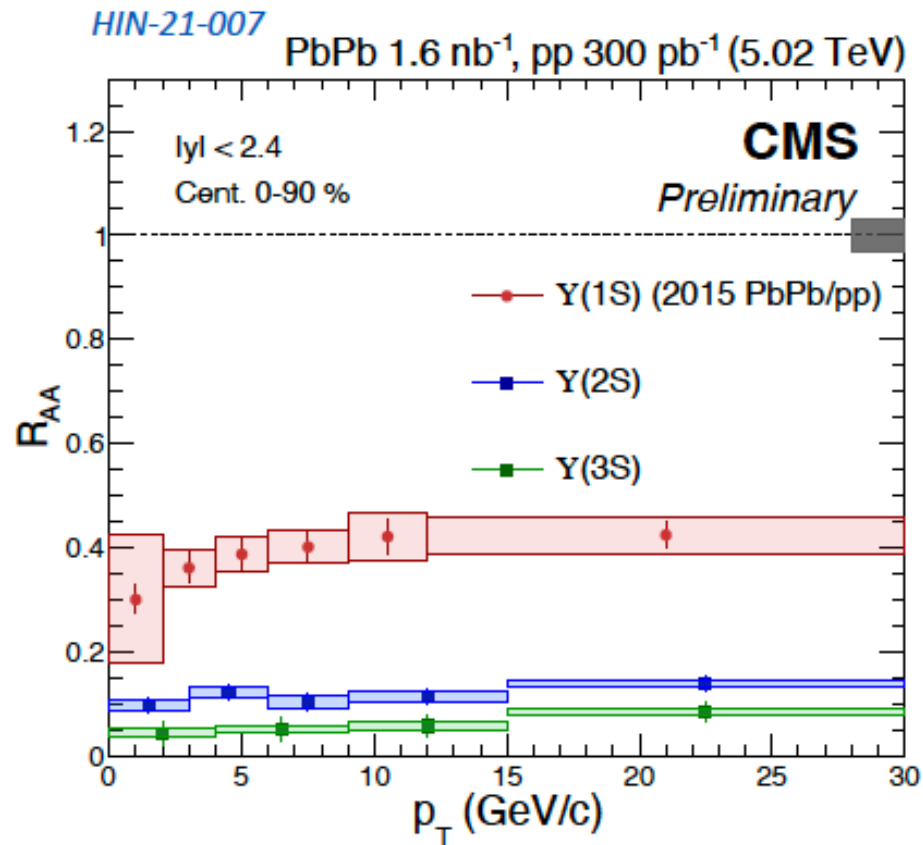


# Sequential melting of quarkonia 1/2

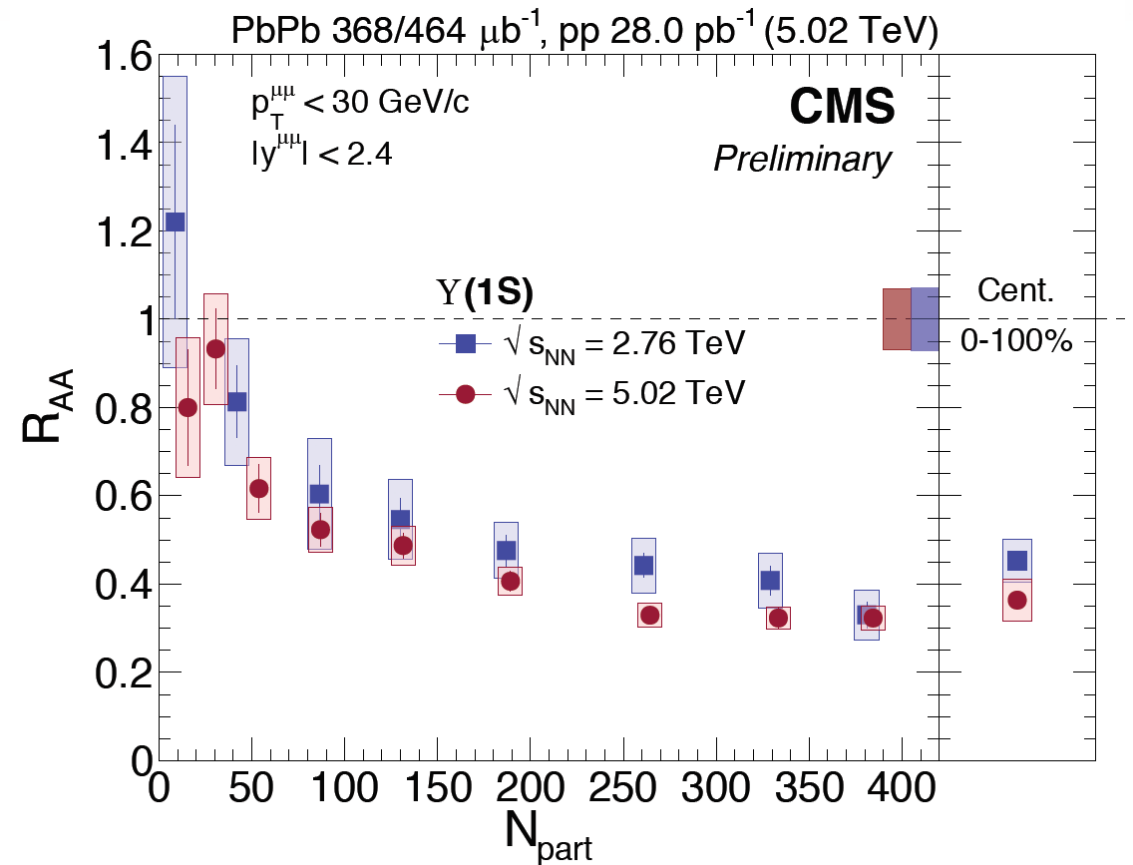
Measurements reveal a **sequential suppression of high mass bottomonium** states. The centrality dependence of the suppression is consistent with progressive suppression in a hotter medium.



# Sequential melting of quarkonia 2/2



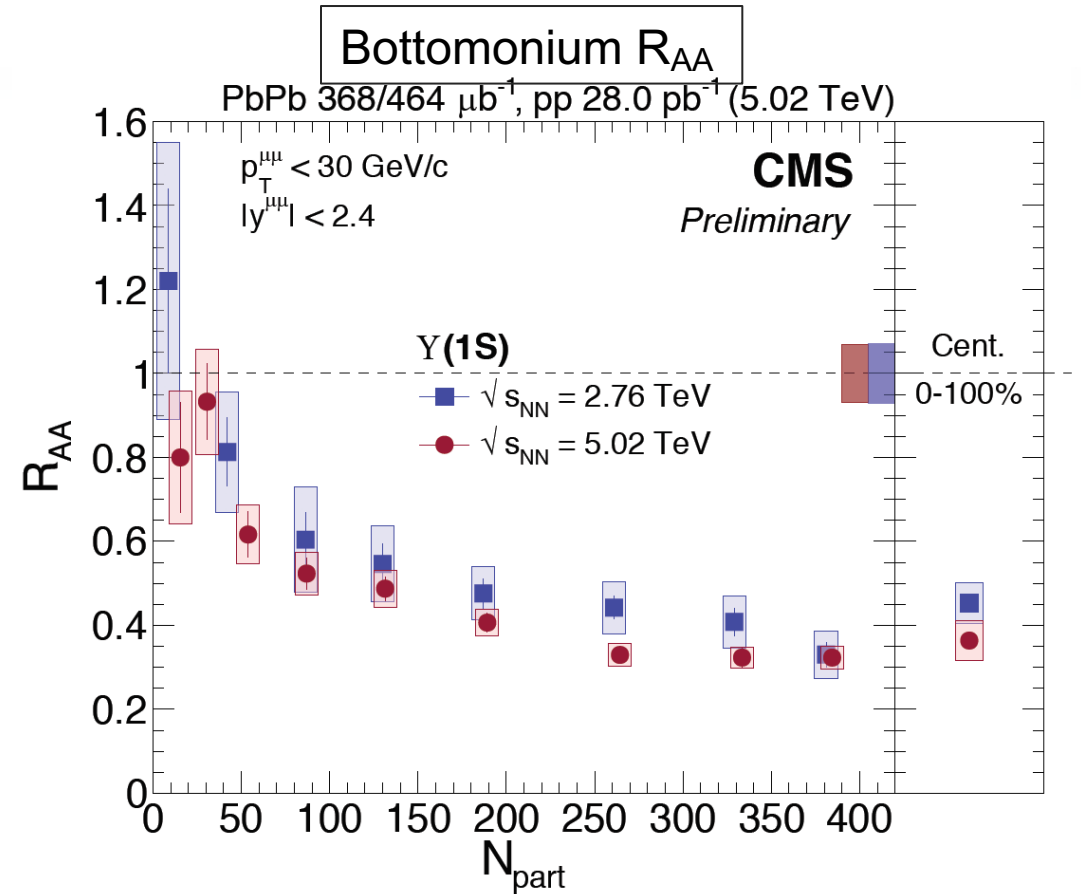
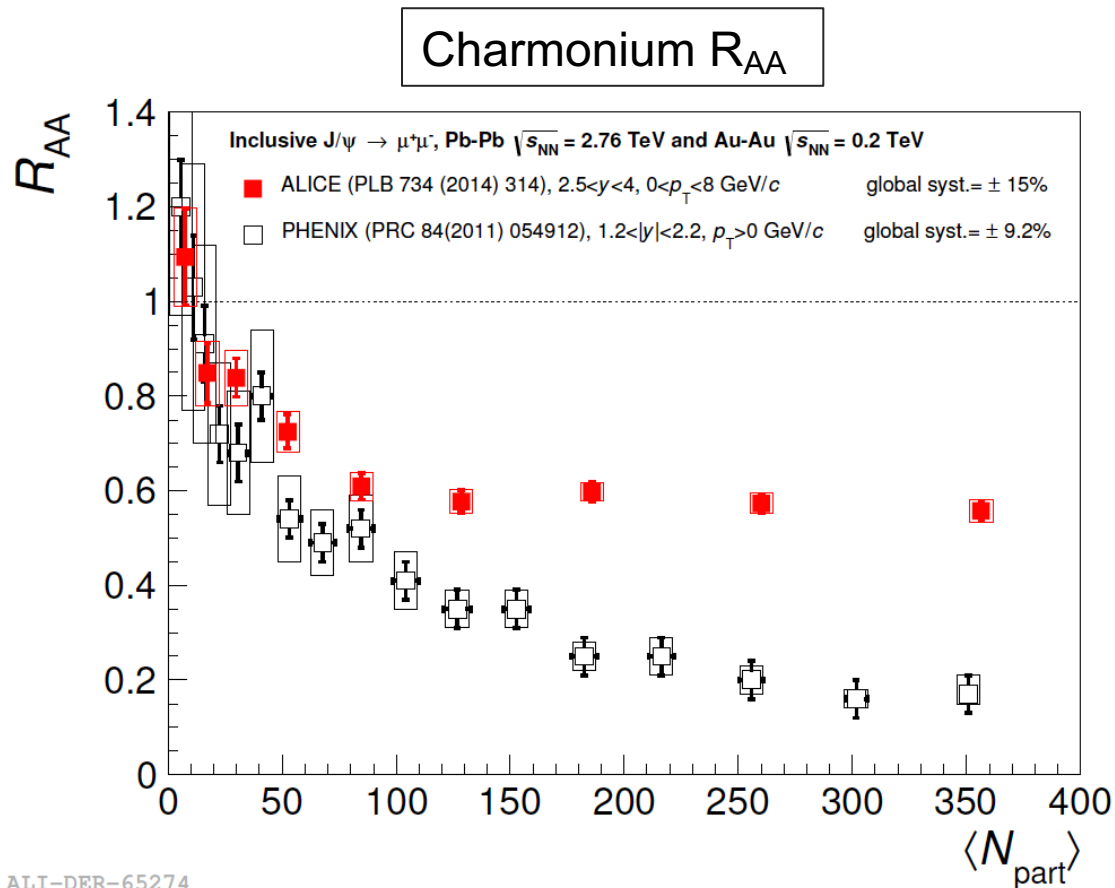
$R_{AA}(Y(3S)) \sim 0.5 R_{AA}(Y(2S))$   
 → Can be used to constrain models!



Increased suppression with increased collision energy

→ no recombination at hadronisation

# Heavy quarks in equilibrium?



ALI-DER-65274

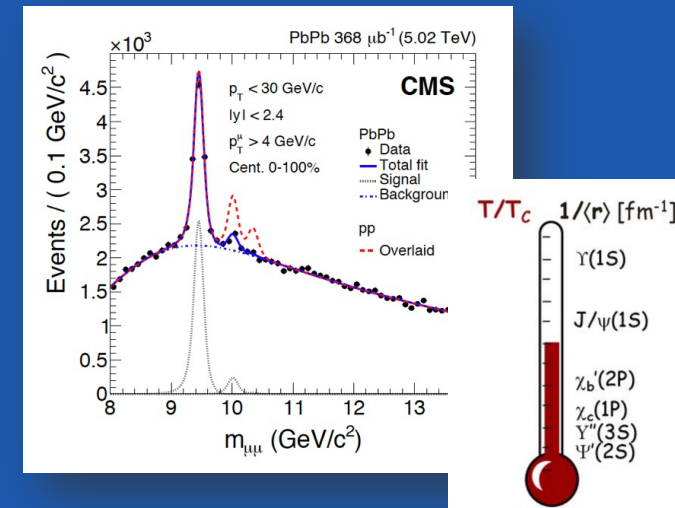
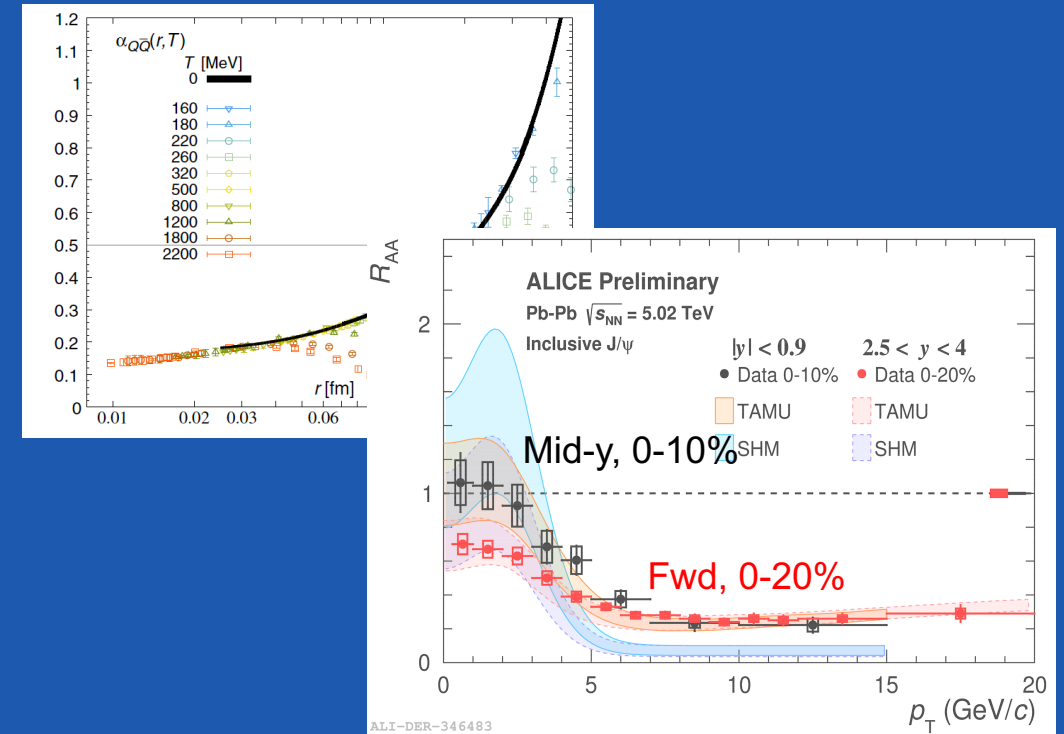
Charm is partially equilibrated (thermalised) with the medium  
**→ a partially-equilibrated probe of the late hadronization stages**

Beauty/bottomonia: no evidence that beauty is even partially equilibrated with the medium  
**→ non-equilibrium probe**

# Summary 2/2

The study of quarkonium ( $c\bar{c}$ ,  $b\bar{b}$ ) states provides information on the mechanisms of **dissociation and regeneration** of strongly-bound state in a medium ( $T > 0$ ).

- The high density of color charges in the QGP leads to melting of quarkonia
- The large abundance of charm quarks at LHC results in regeneration of the amount of  $J/\psi$
- States with smaller binding energies are more suppressed



Bonus material



# Characteristics of a heavy-ion detector: ALICE

ALICE is the dedicated heavy-ion detector at the LHC, designed and built specifically for this purpose.

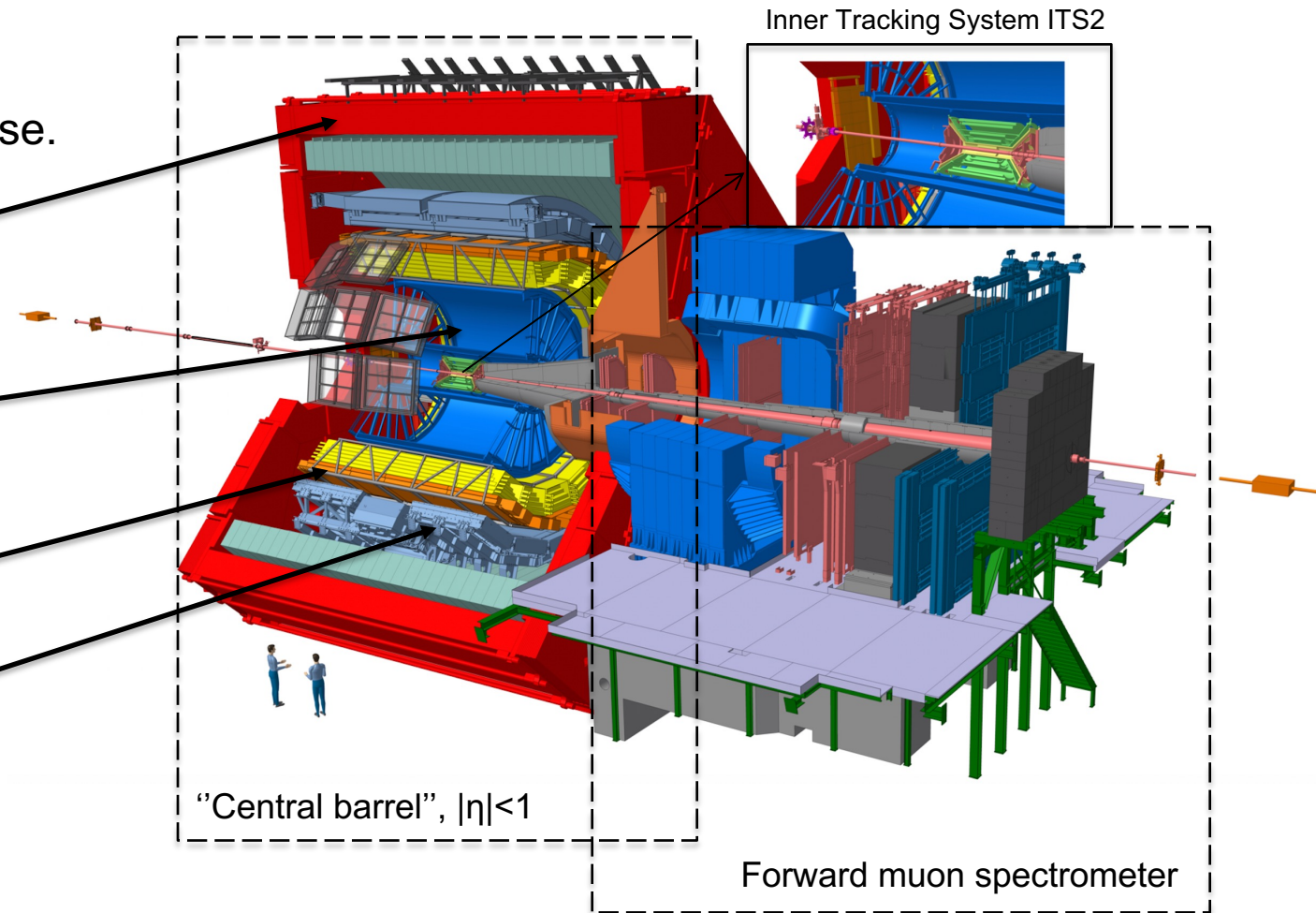
**Solenoid:** magnetic field  $B = 0.5 \text{ T}$

**Inner Tracking System + Time Projection Chamber:** vertexing and tracking + identification (TPC) down to very low  $p_T \sim 0.1 \text{ GeV}/c$

**Time-Of-Flight, TRD, HMPID, etc.:** Particle identification detectors

**Electromagnetic calorimeters**

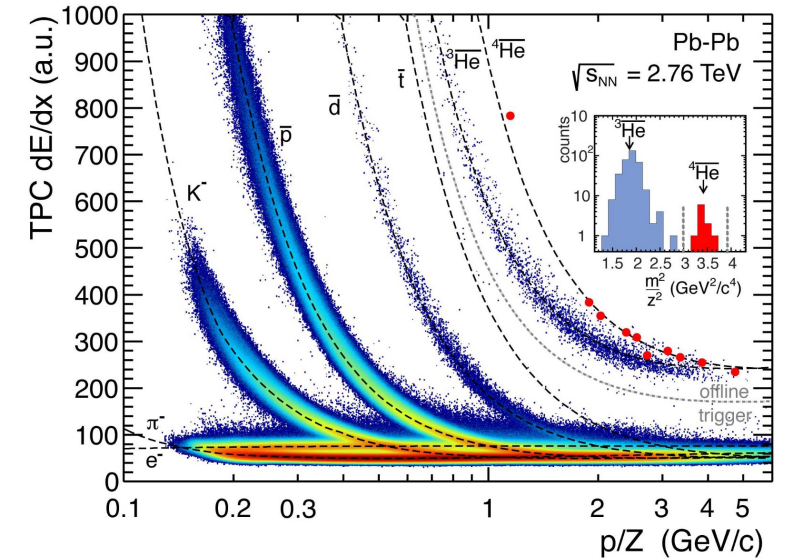
**+ Forward rapidity detectors and ZDC:** trigger, centrality, event time determination, ...



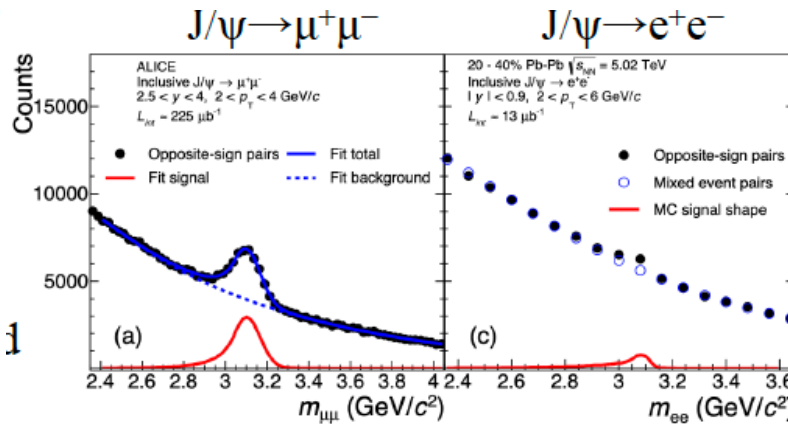
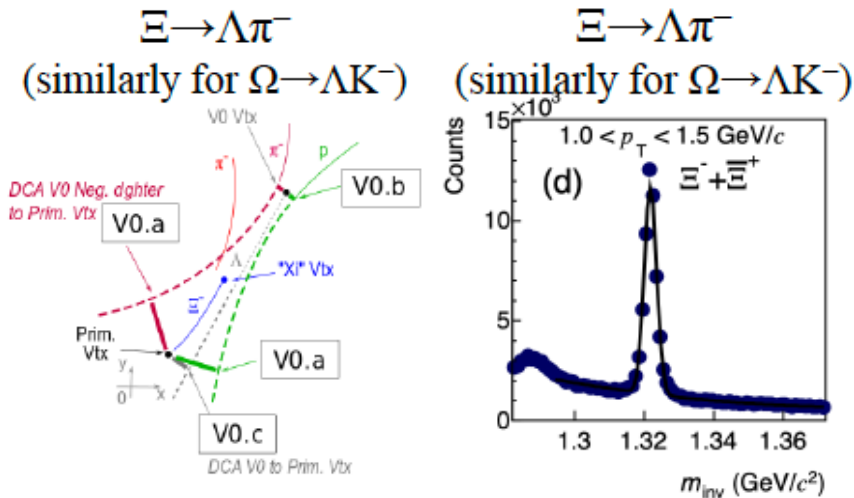
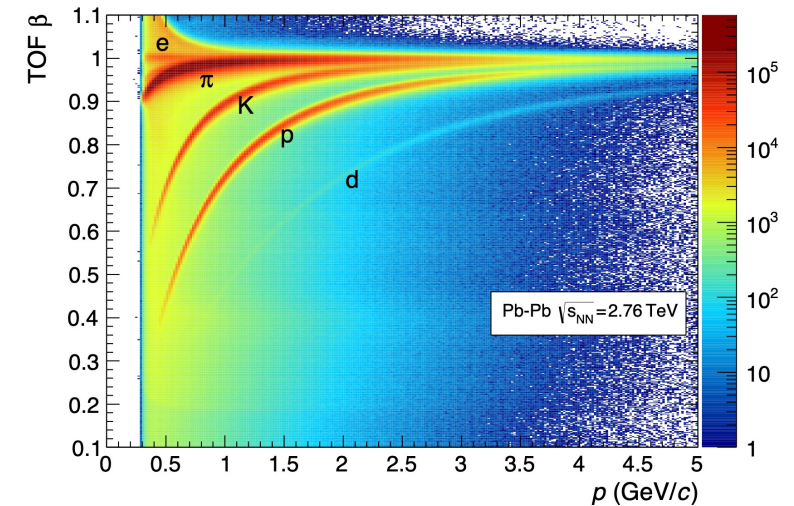
# Particle identification

- Direct identification:  $\pi$ , K, p, light (anti)nuclei
- Electron identification using calorimeters and transition radiation detectors
- Strange and heavy-flavour hadrons:
  - reconstruction of secondary vertex and weak decay topology + PID + invariant mass reconstruction
- Photons detected in calorimeters and through pair production
- Quarkonia through leptonic decays

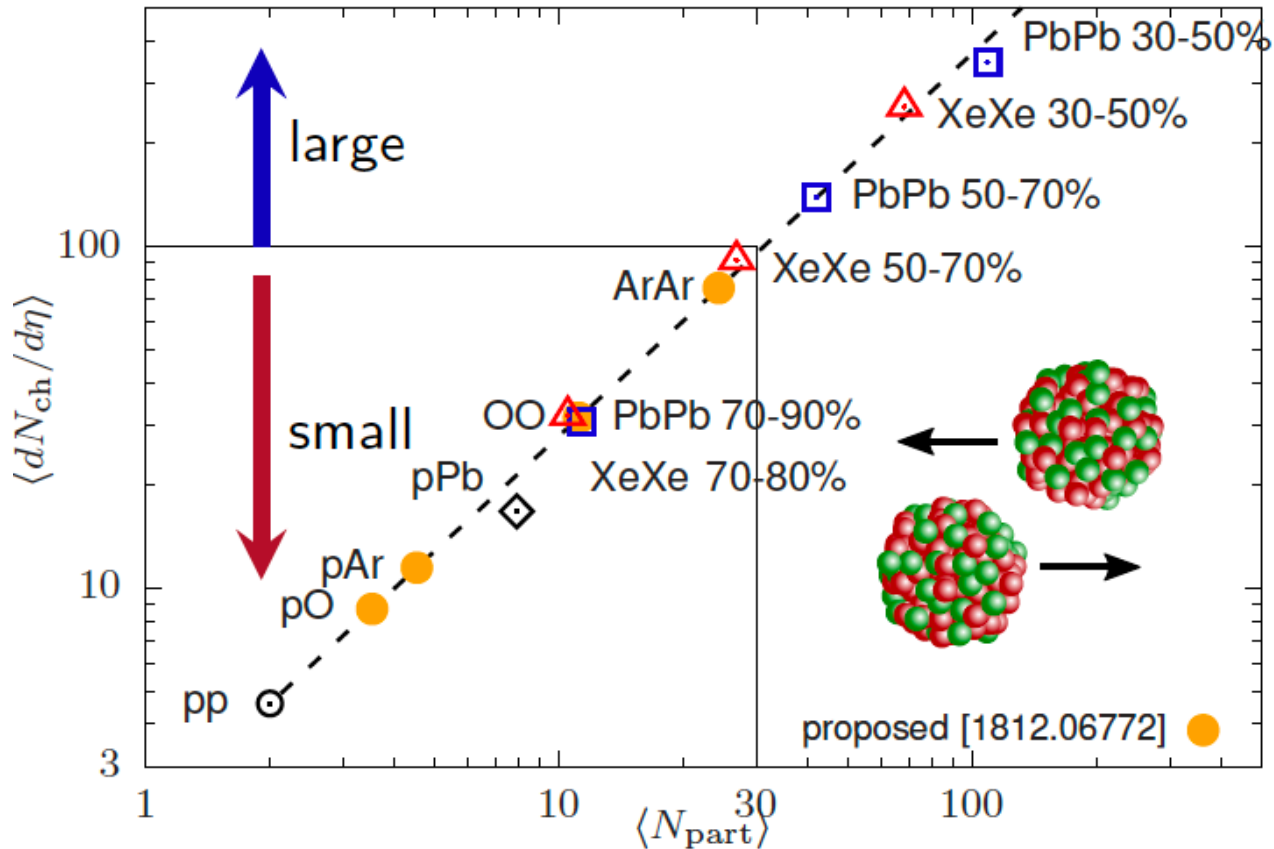
Energy loss of long lived particles in TPC



Particle velocity from TOF measurement and momentum



# Light ions at the LHC



From A. Mazeliauskas, EPS-HEP 2021:

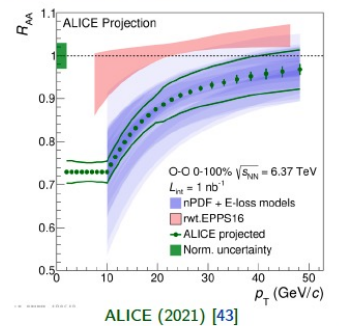
Light-ions (e.g. O, Ar, Kr) [Yellow report \(2018\) \[17\]](#):

- High achievable luminosity.
- Short oxygen run planned in LHC Run 3.
- $pO$ : strong interest from cosmic ray physics.
- $OO$  comparable to  $pPb$ , but better geometry control.
- Many physics opportunities [see OppOatLHC \[indico\]](#)

Experimental projections and theory calculations show measurable energy loss signal in  $10 \text{ GeV} < p_T < 50 \text{ GeV}$ .

[Huss, Kurkela, AM, Paatalainen, van der Schee, Wiedemann \(2020\) \[41\]](#)

*Opportunity to discover jet quenching in small systems.*

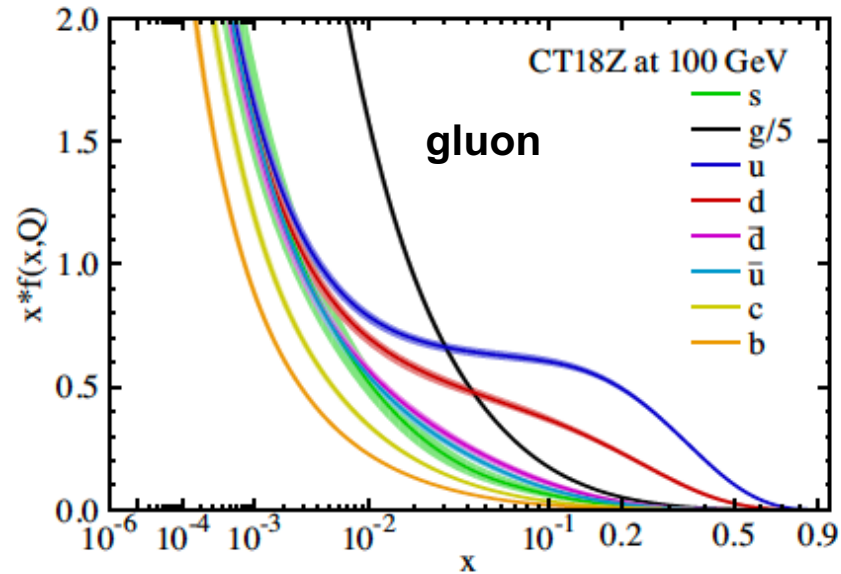


Aleksas Mazeliauskas

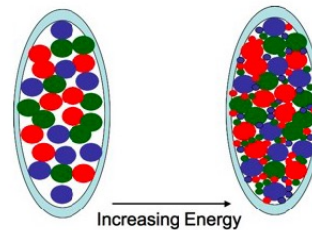
aleksas.eu

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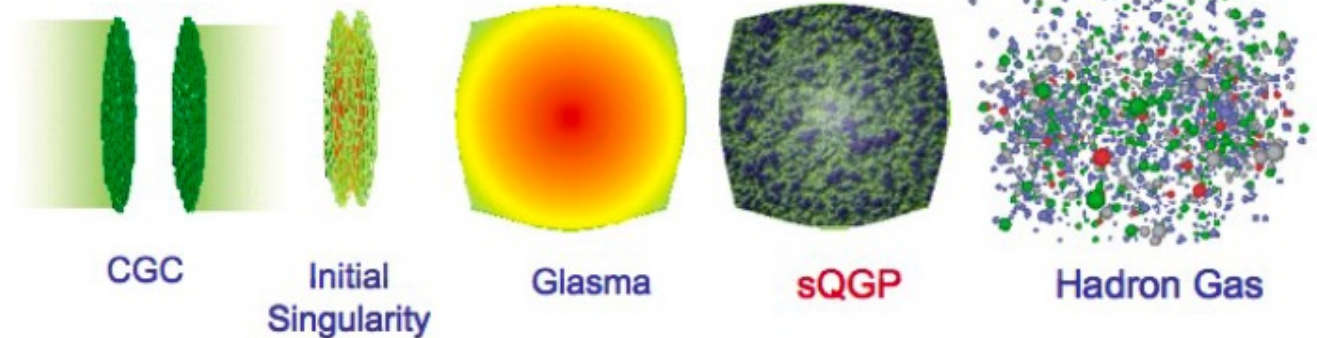
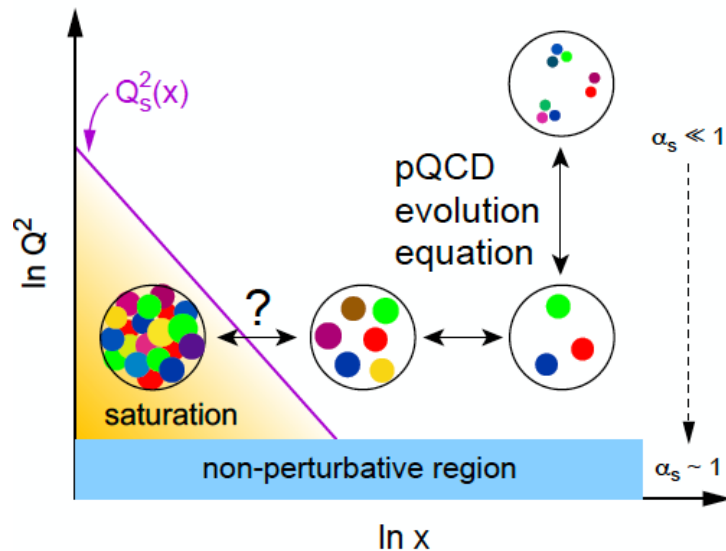
# Initial stage of heavy ion collisions



**Color Glass Condensate:** at high energy and small x, the hadron content is dominated by gluonic matter “packed” into high density



Saturation (momentum) scale  
 $Q_{\text{sat}}$  = inverse size scale of  
 smallest gluons which are  
 closely packed  
 → gluons of size larger than  
 $1/Q_{\text{sat}}$  no longer fit



L. McLerran, [https://bib-pubdb1.desy.de/record/296833/files/ismd08\\_mcl\\_intro-corr.pdf](https://bib-pubdb1.desy.de/record/296833/files/ismd08_mcl_intro-corr.pdf)  
 + more reviews in literature,

# Glauber model

Nucleus-nucleus interaction as **incoherent superposition of nucleon-nucleon collisions** calculated in a probabilistic approach

[M. L. Miller et al., An. Rev. Nucl. Part. Sci. 57 (2007) 205-243]

- nucleons in nuclei are considered as point-like and non-interacting
- nuclei (and nucleons) have straight-line trajectories (no deflection)

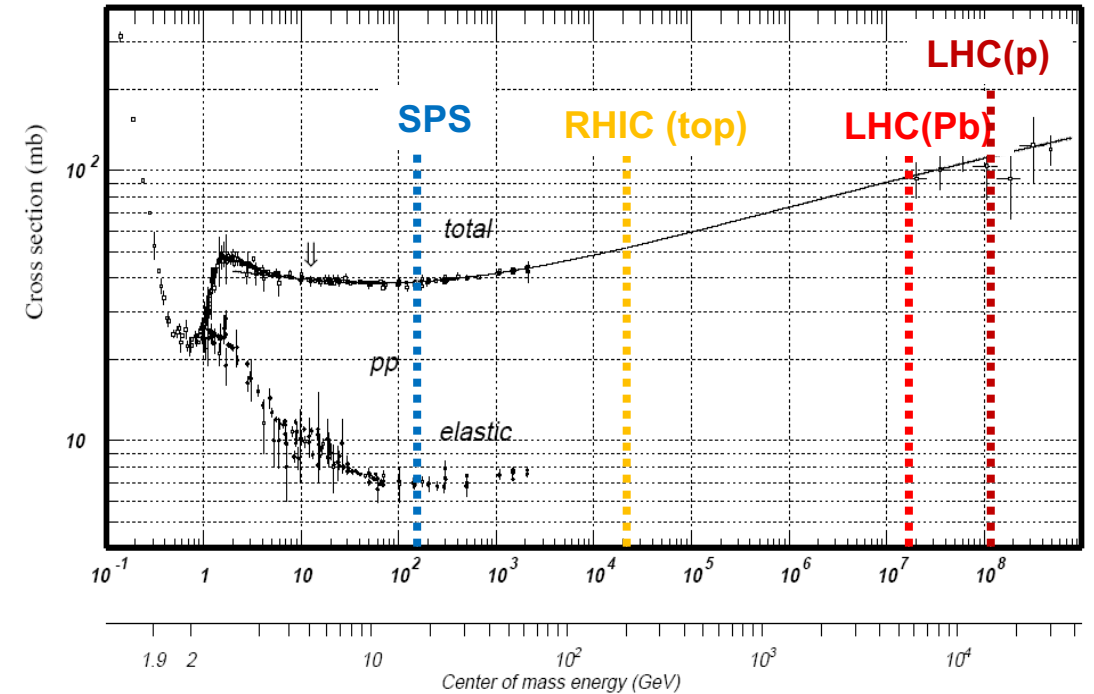
## Input:

- Nucleon-nucleon inelastic cross section
- Nuclear density distribution, e.g. Fermi

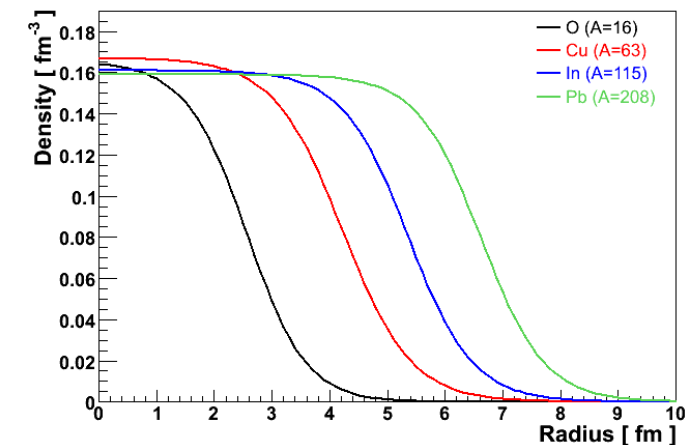
$$\rho(r) = \rho_0 \frac{1 + w(r/R)^2}{1 + \exp\left(\frac{r-R}{a}\right)}$$

$\rho^0$  = density in the nucleus center  
 $R$  = nucleus radius  
 $a$  = skin depth  
 $w$  = deviations from spherical shape

Proton-proton cross section (from PDG)



Examples of density distributions of nuclei



# Glauber model (2)

## Output:

- Interaction probability
- **Number of elementary nucleon-nucleon collisions ( $N_{\text{coll}}$ )**
- **Number of participant nucleons ( $N_{\text{part}}$ )**
- **Number of spectator nucleons**
- Size of the nuclei overlap region

These variables are fundamental to study the scaling properties of observables in HIC – **Rule of thumb:**

- $N_{\text{part}}$  scaling of **soft particle production**  
→ **bulk** of the system
- $N_{\text{coll}}$  scaling of **high  $p_T$  particle production**  
→ **hard** partons produced **early** in the collision

