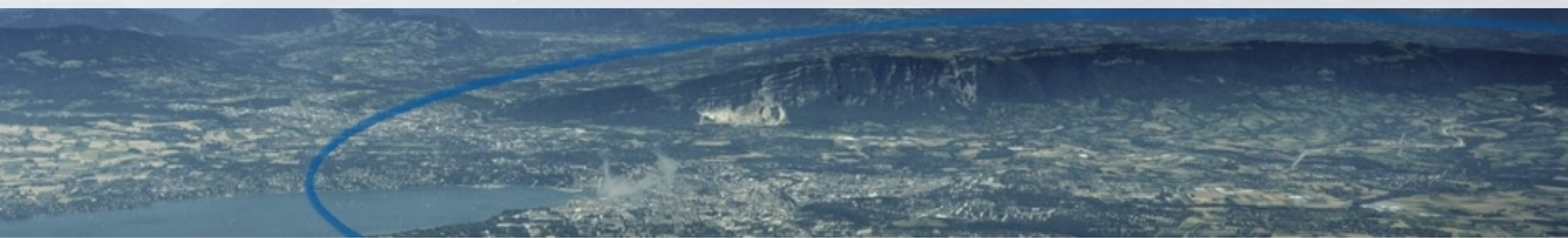


Experimental Physics at Lepton Colliders



Part II

Overview

A two-part story

- Part 1:
 - Scientific motivation
 - Future e^+e^- colliders in broad strokes
 - Detectors at future e^+e^- and $\mu^+\mu^-$ colliders
- **Part 2:**
 - Higgs physics
 - Electroweak precision
 - Top quark physics
 - Into the unknown

Disclaimer

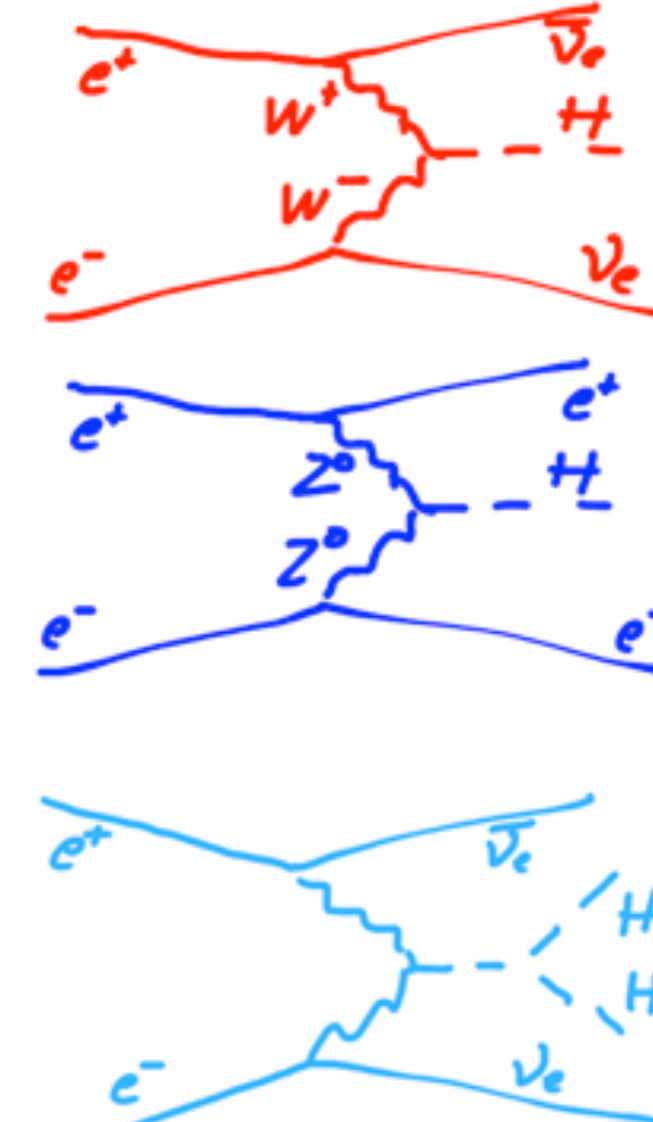
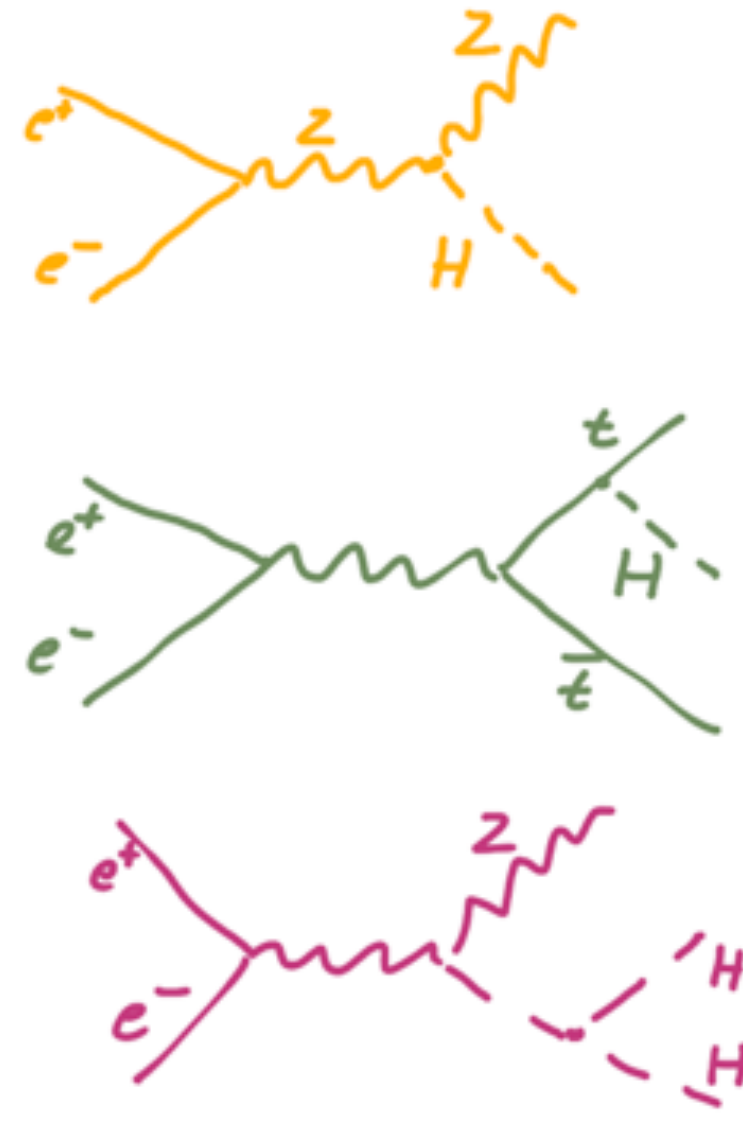
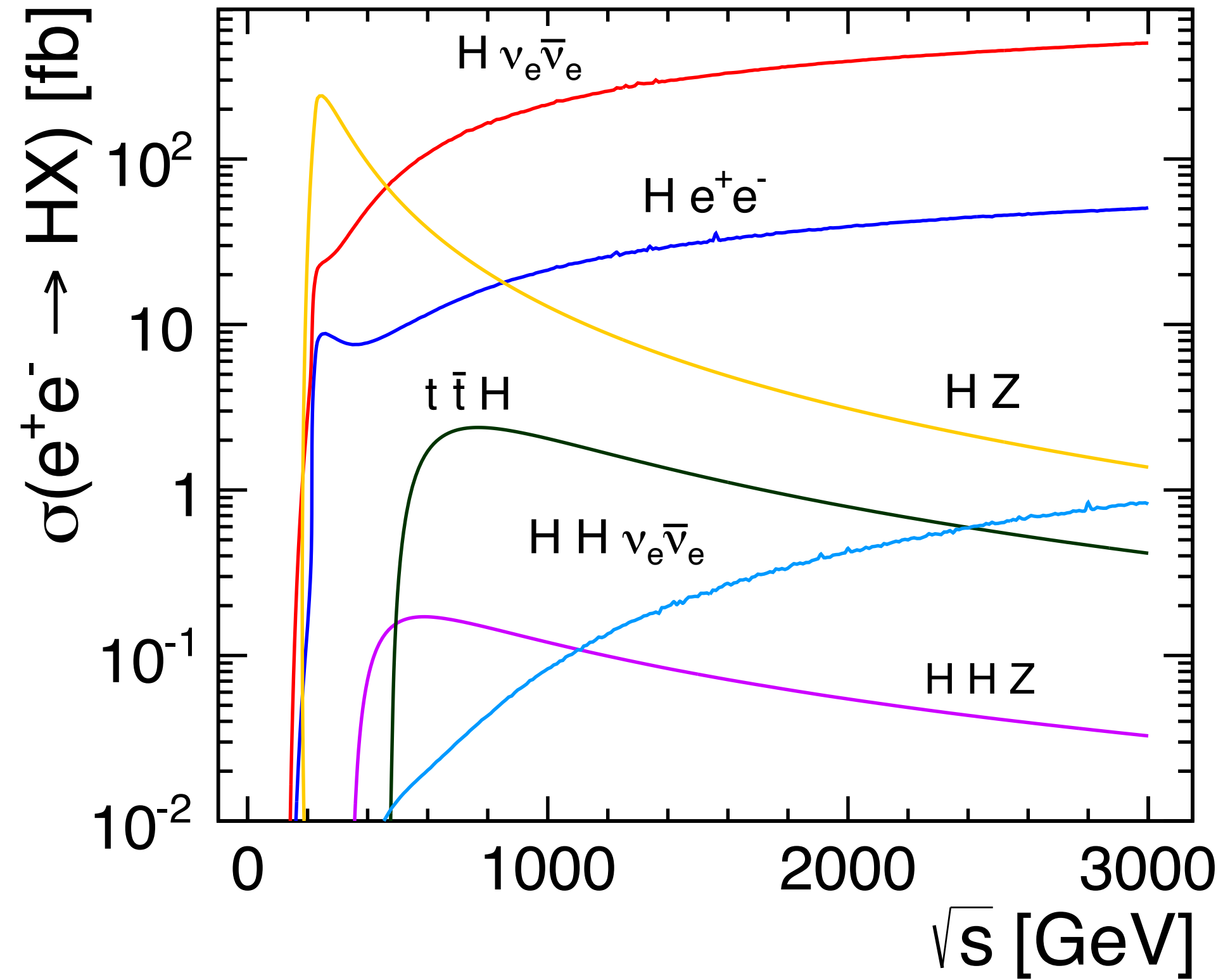
- The point of the following discussions is not to compare projects in the sense of drawing conclusions which one should be built - that is a multi-faceted question which extends beyond performance projections shown here.
- The numerical results may not always be perfectly up-to-date - again, the goal is not to compare, but to illustrate certain features of measurements and facilities
- I am focussing on e^+e^- colliders, only few remarks about $\mu^+\mu^-$

Precision Higgs Measurements

Higgs Factories and beyond

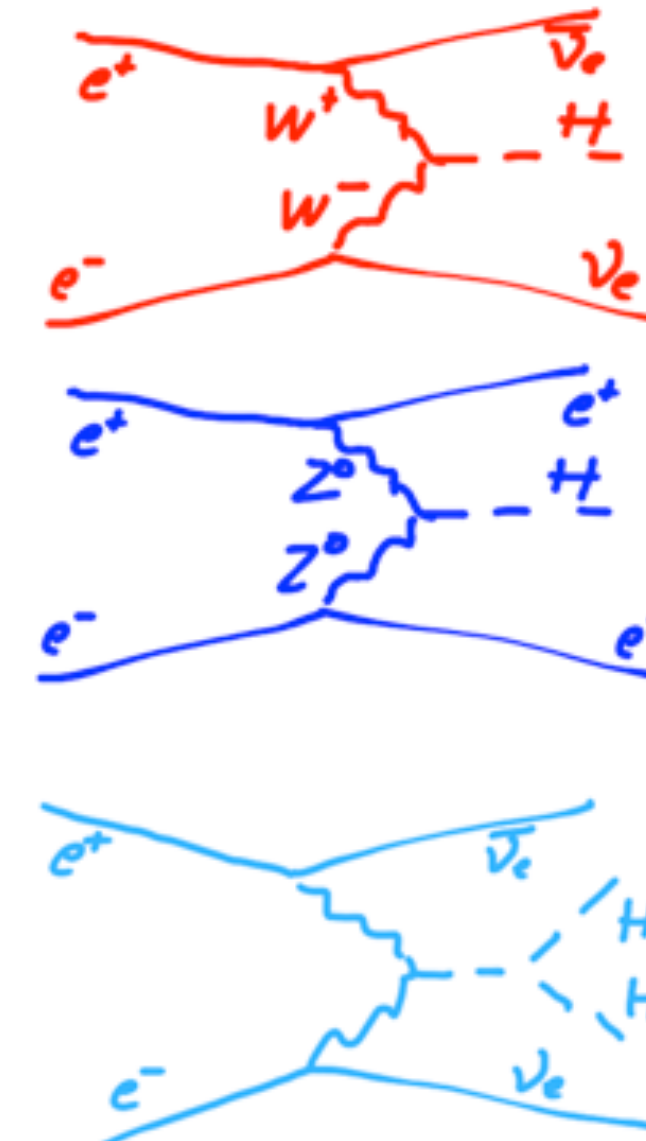
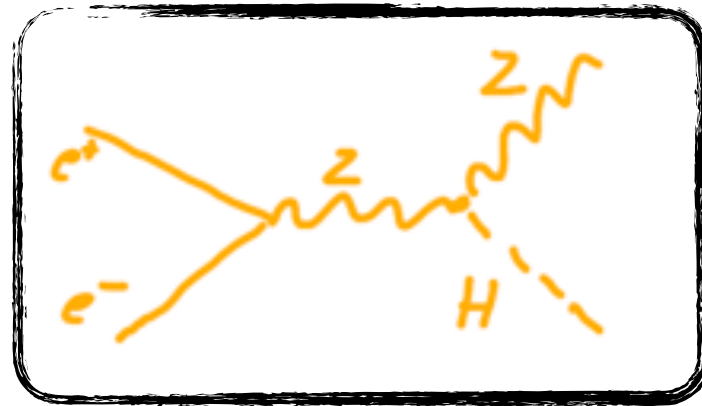
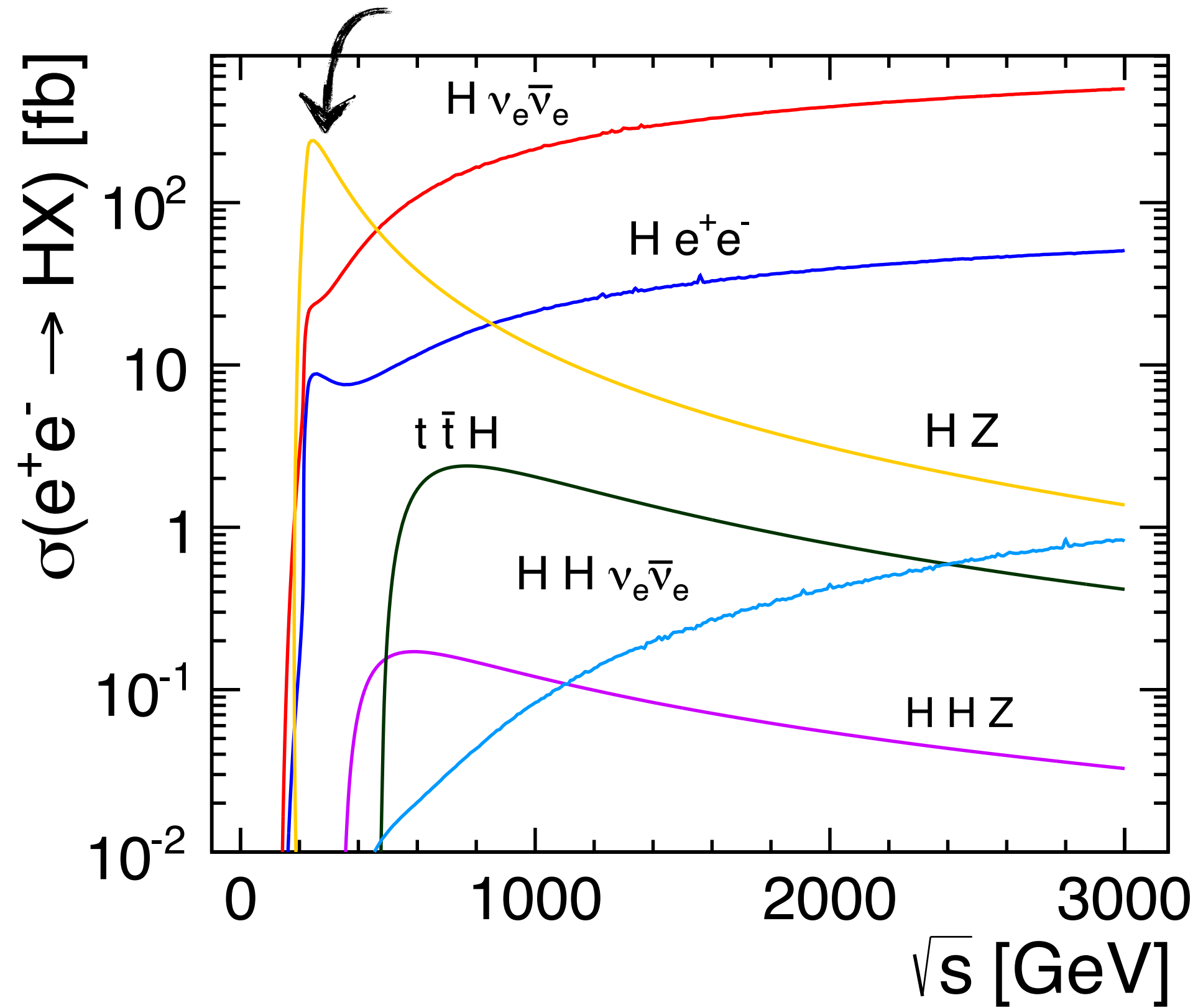
Higgs Boson Production in e^+e^-

A rich field to explore



Higgs Boson Production in e^+e^-

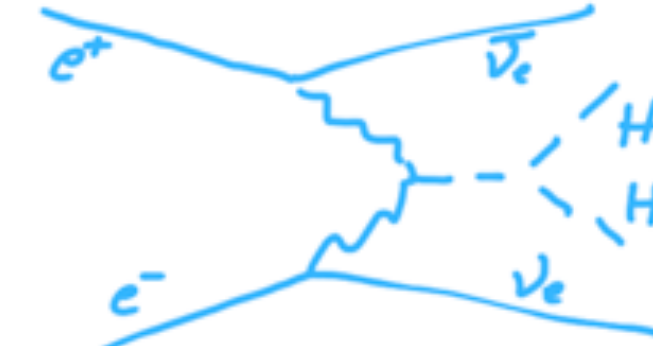
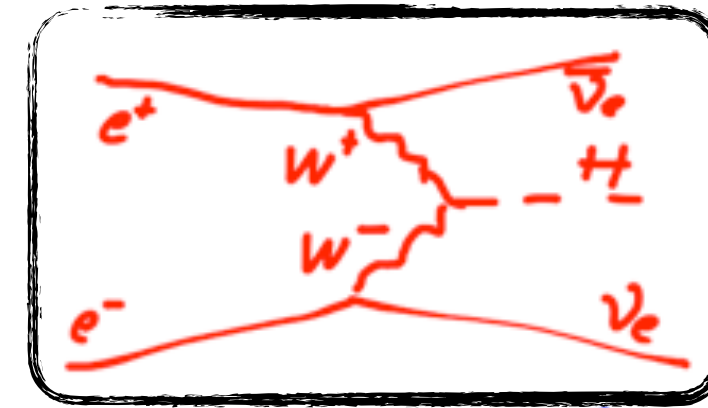
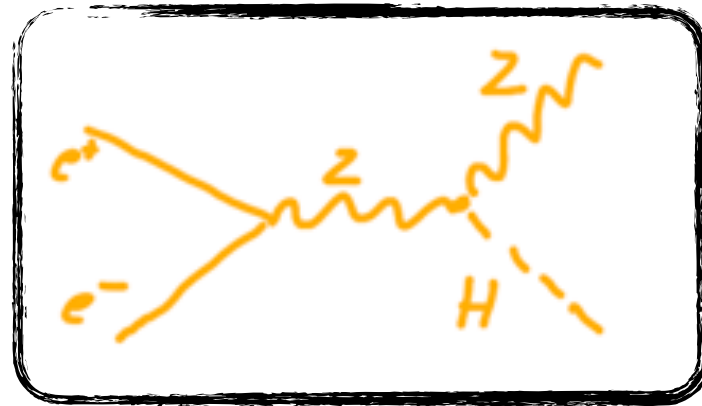
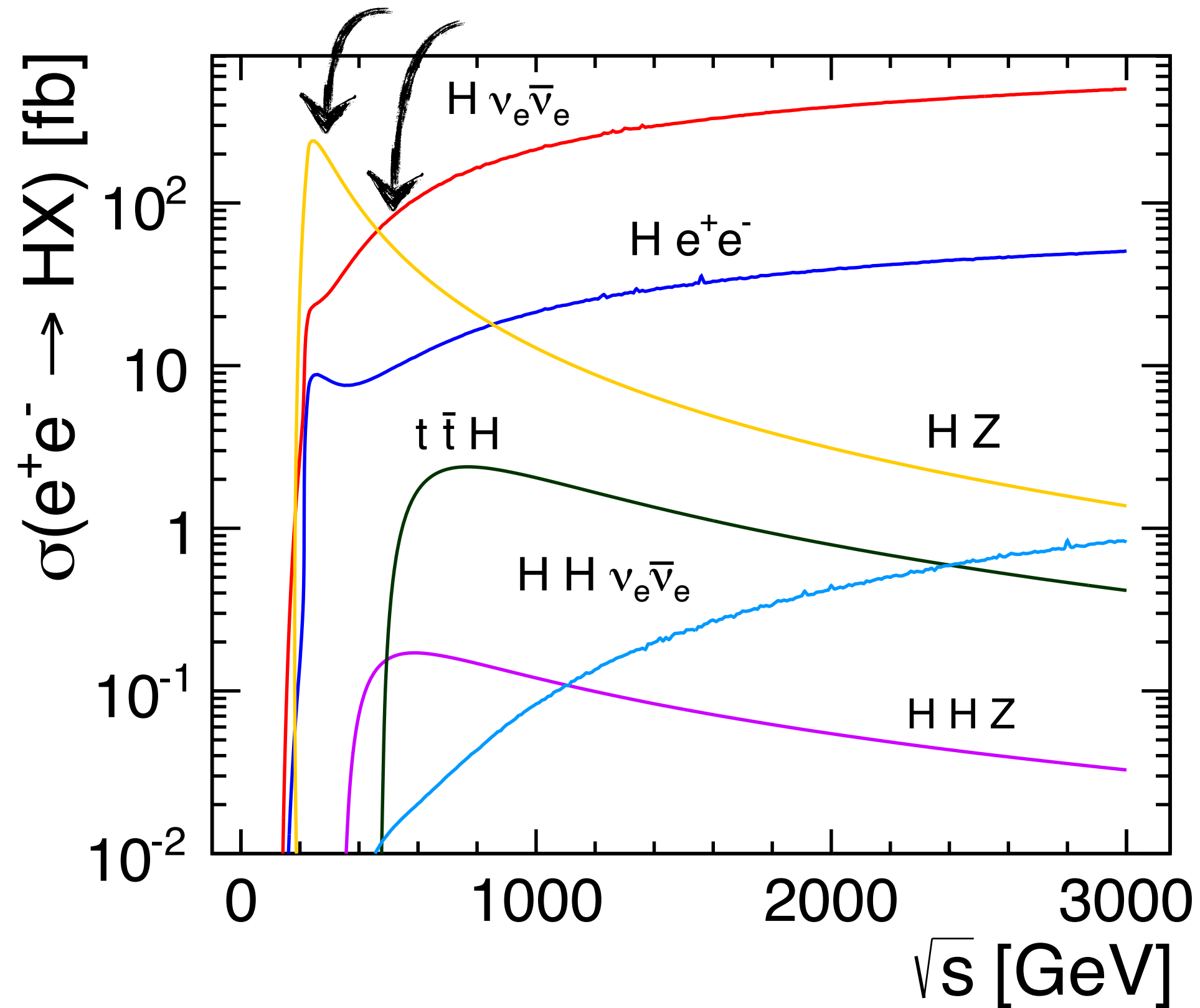
A rich field to explore



250 GeV:
Maximum of ZH production

Higgs Boson Production in e^+e^-

A rich field to explore

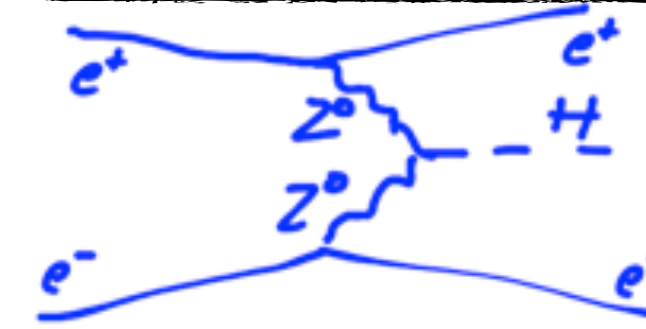
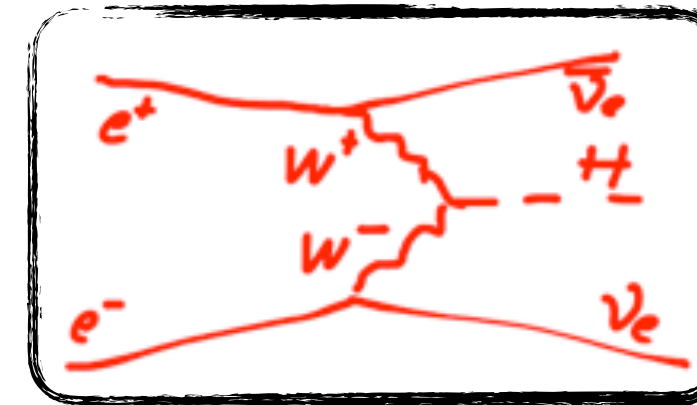
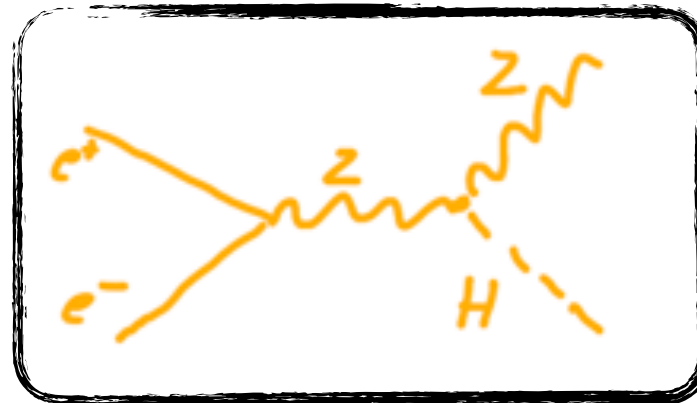
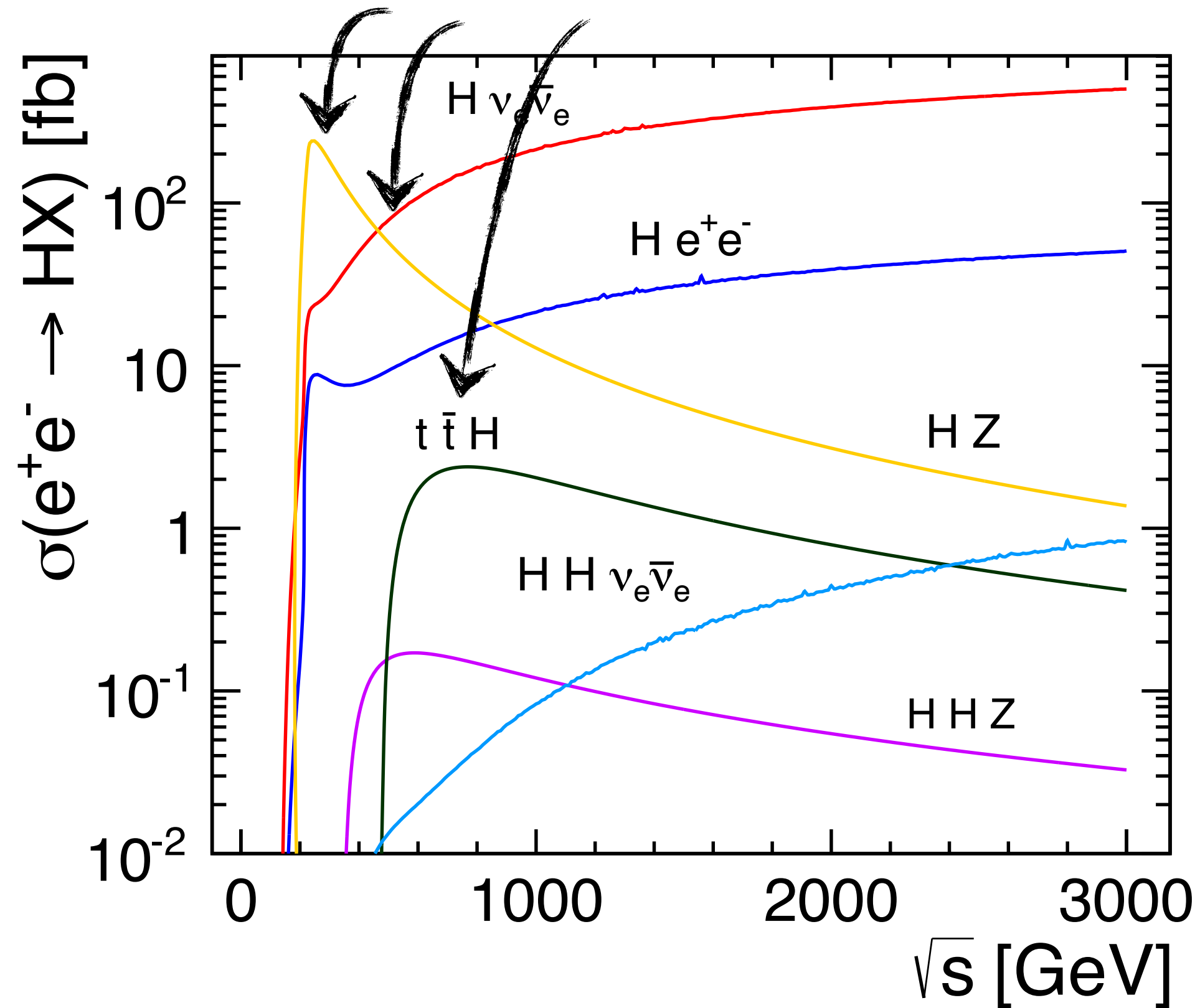


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350 GeV:
 WW fusion kicks in
(and top pair production)

Higgs Boson Production in e^+e^-

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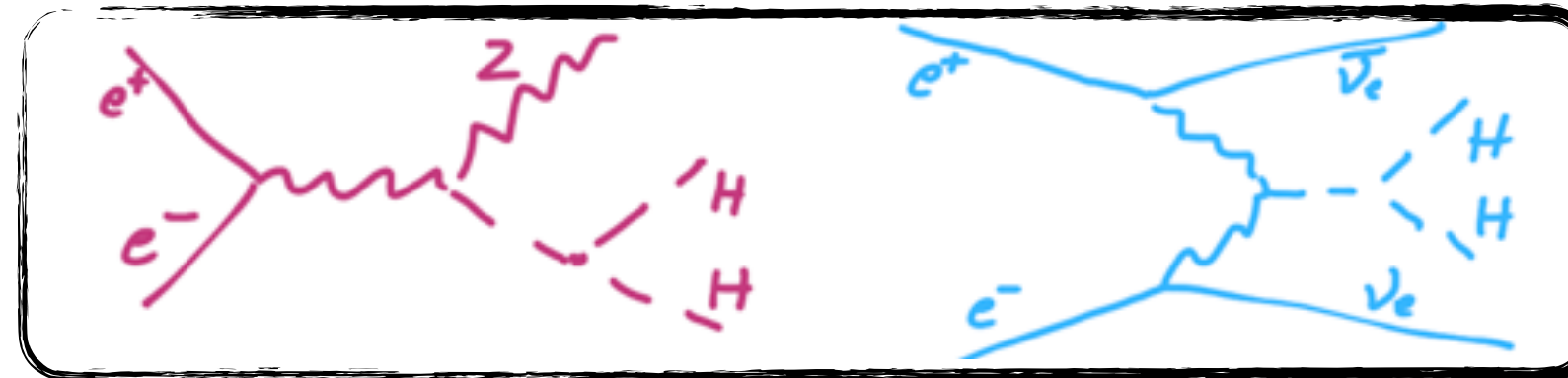
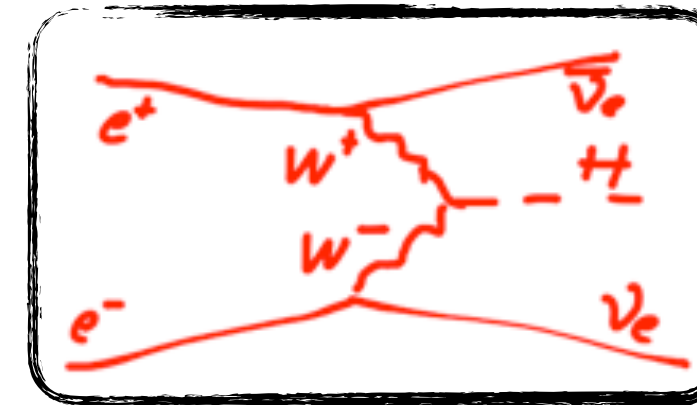
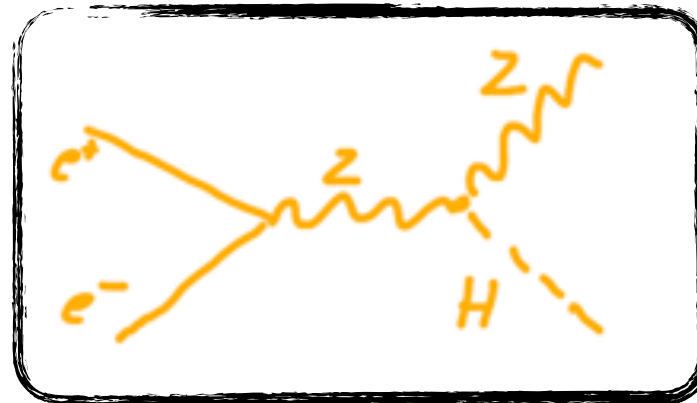
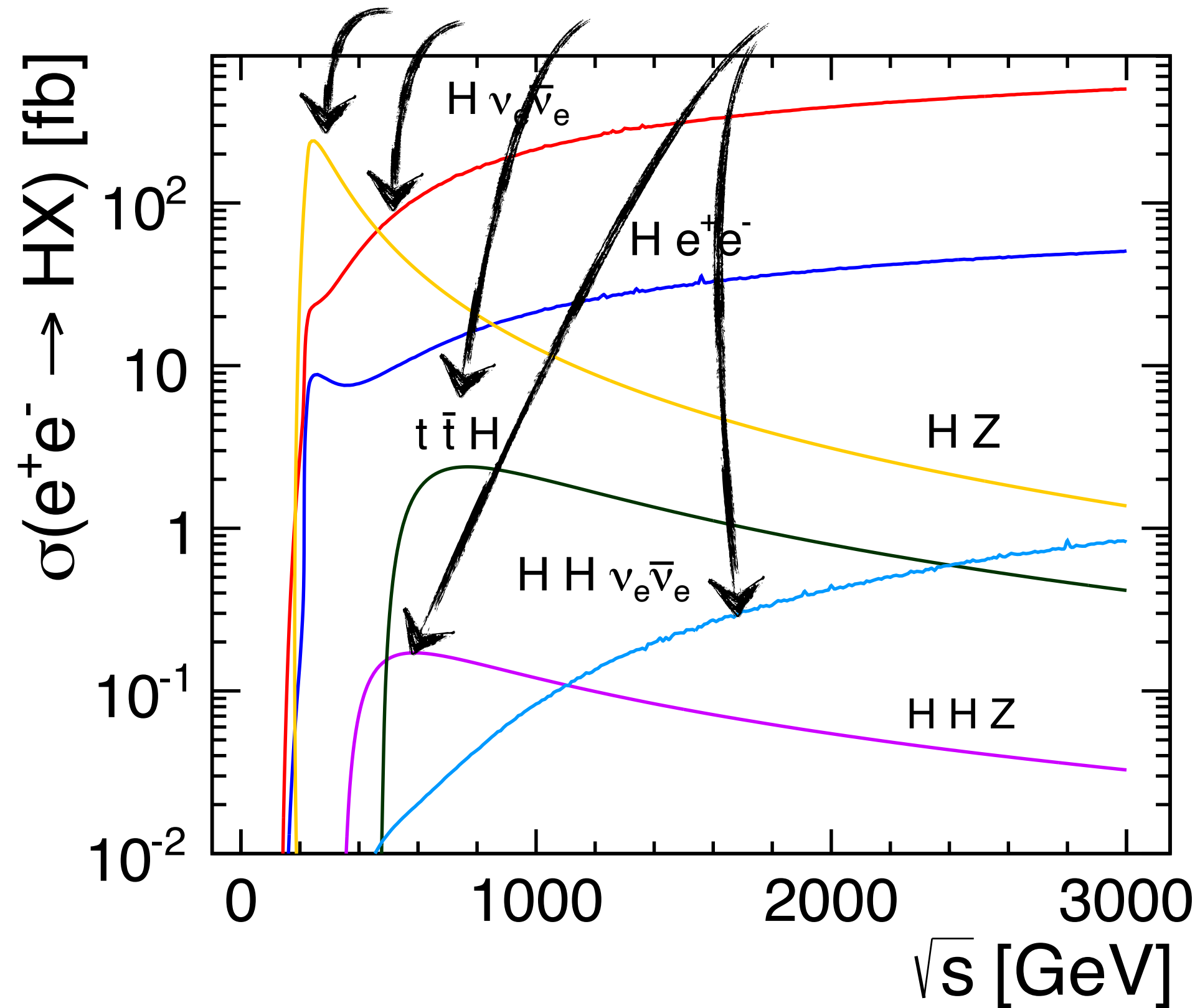
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500 - 1000+ GeV:

$t\bar{t}H$: direct access to top
Yukawa coupling

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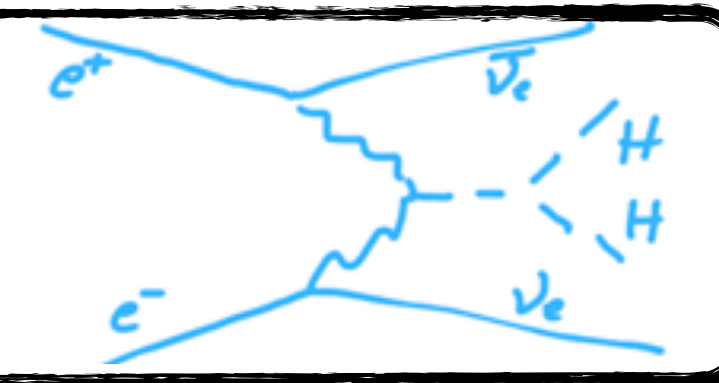
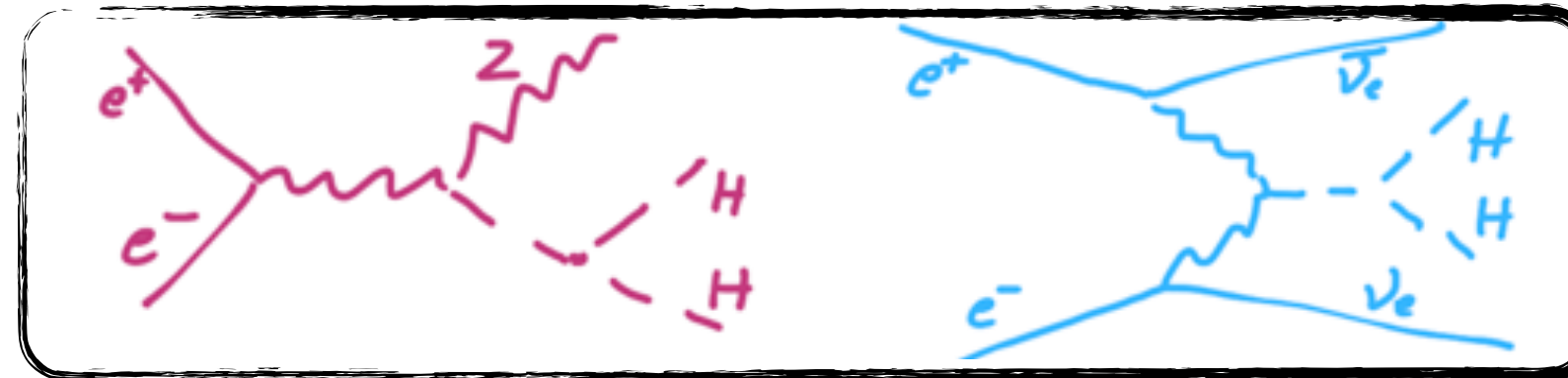
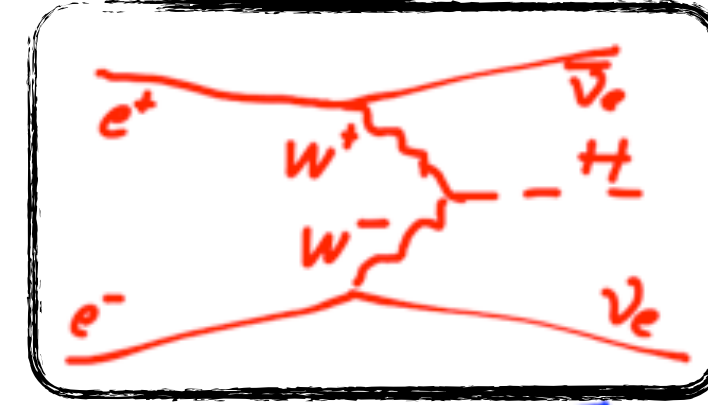
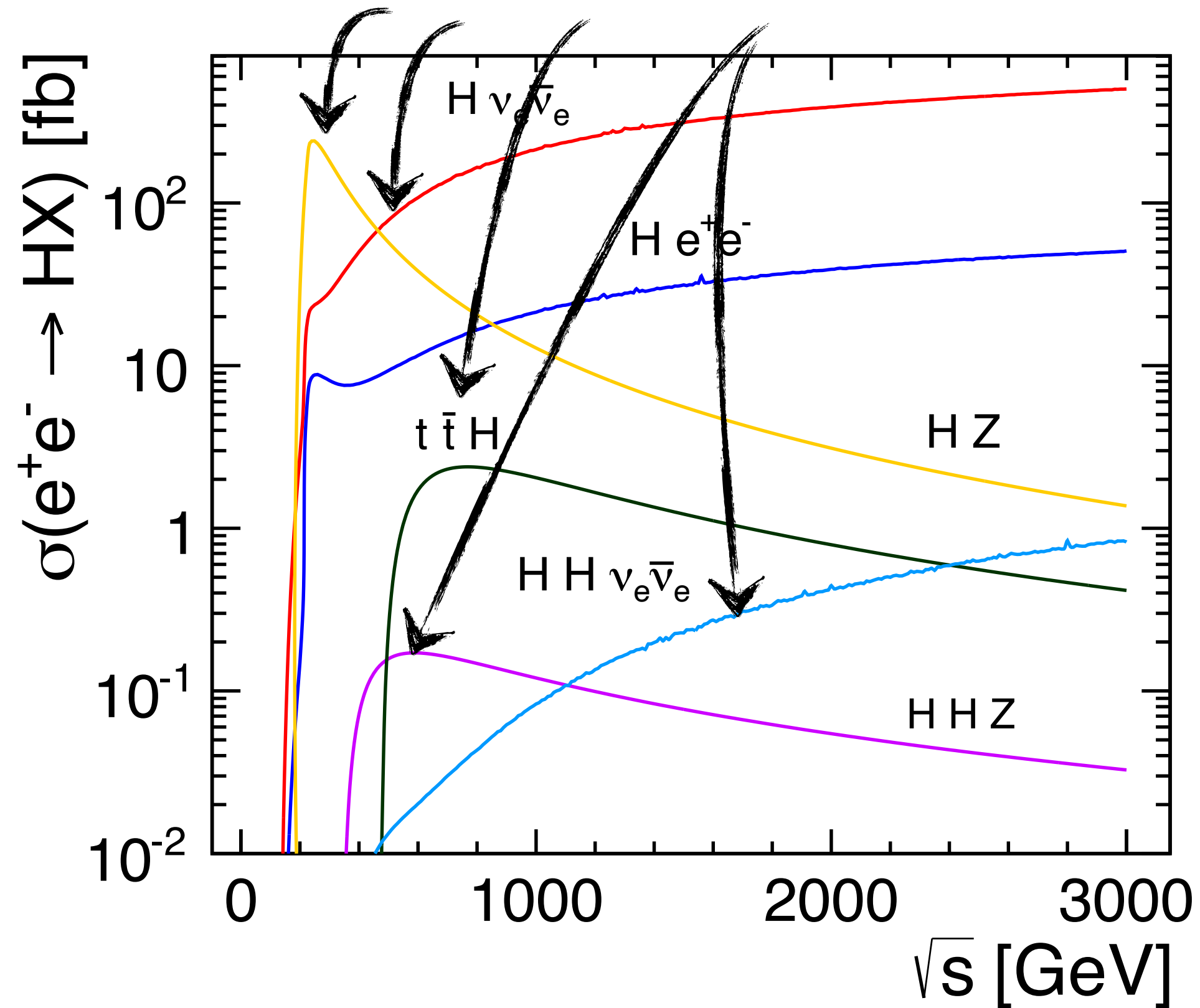
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Higgs self-coupling

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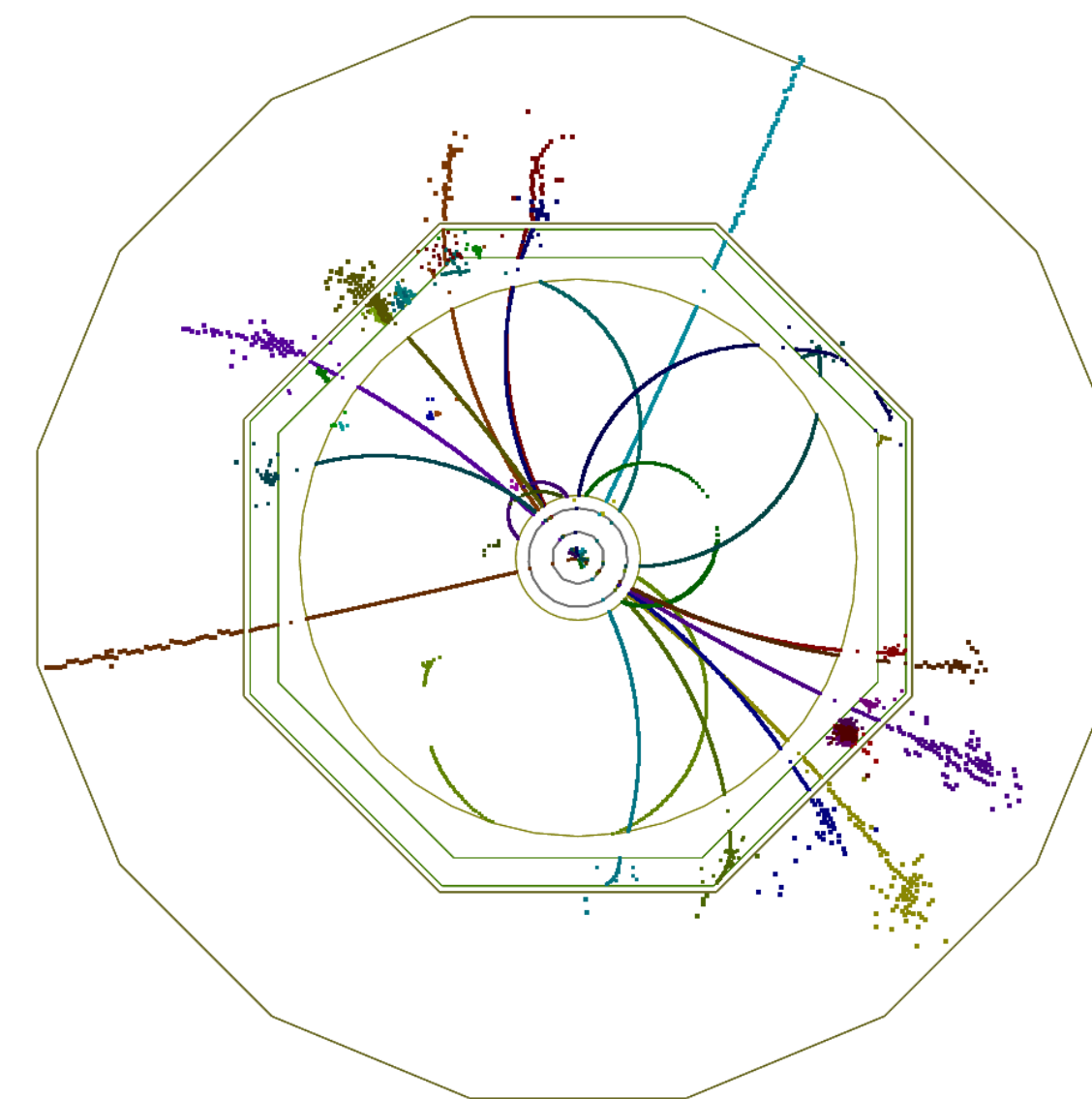
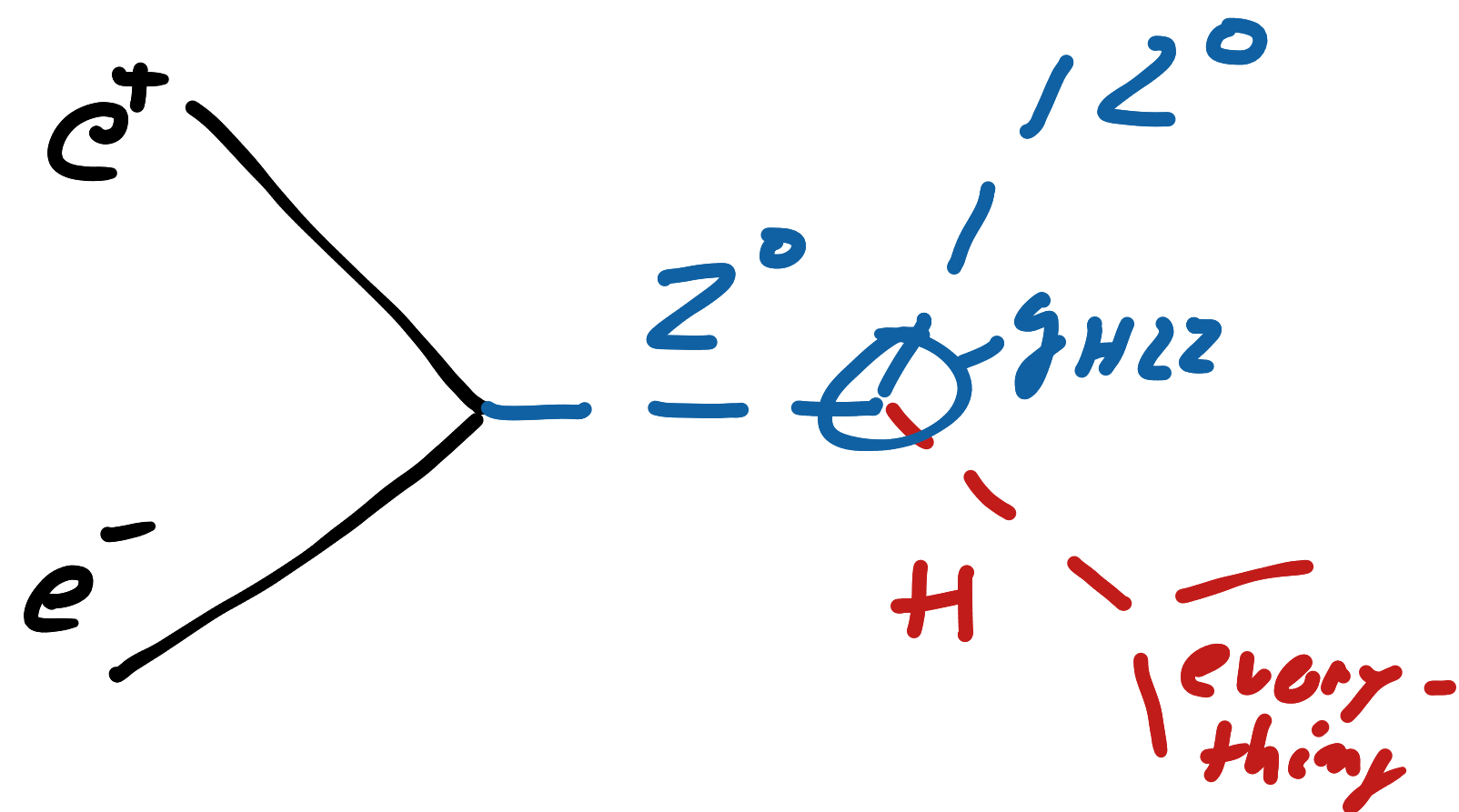
500 GeV; 1+ TeV:
Higgs self-coupling

- 240 - 250 GeV: the minimum energy for a Higgs factory
- ~ 350 GeV: Additional production mode, also still access to ZH
- Higher energies: More processes
- 125 GeV, and extreme luminosity: A possibility to measure electron Yukawa coupling

Model Independence: The Pillar of Higgs Physics in e^+e^-

The ZH Higgsstrahlung process

- What model independence means: Measure the coupling of the Higgs Bosons to elementary particles free from model assumptions (e.g. how it decays)
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 - Not possible at hadron colliders



ILD, 250 GeV

$$e^+e^- \rightarrow ZH \rightarrow \mu^+\mu^-b\bar{b}$$

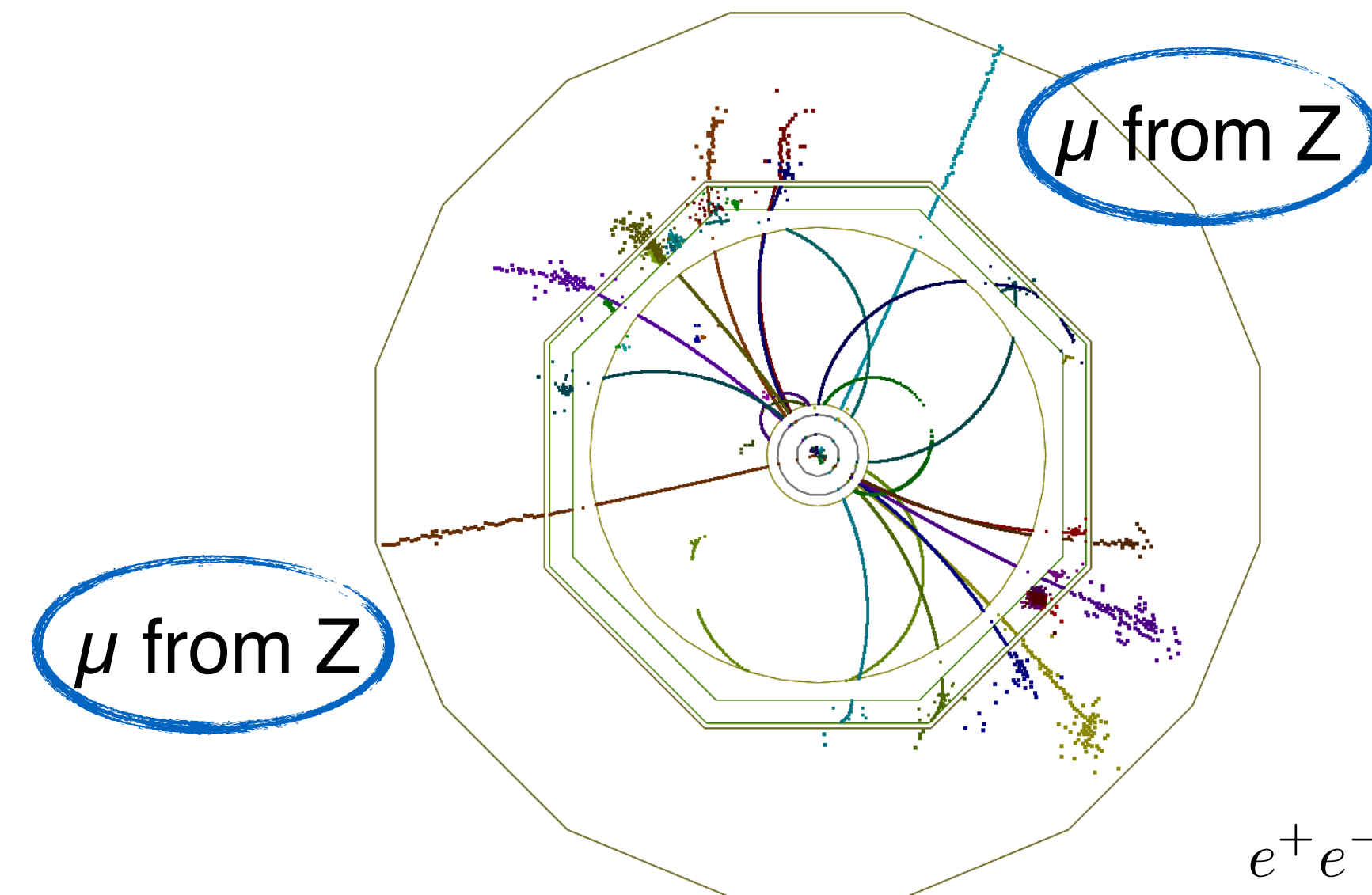
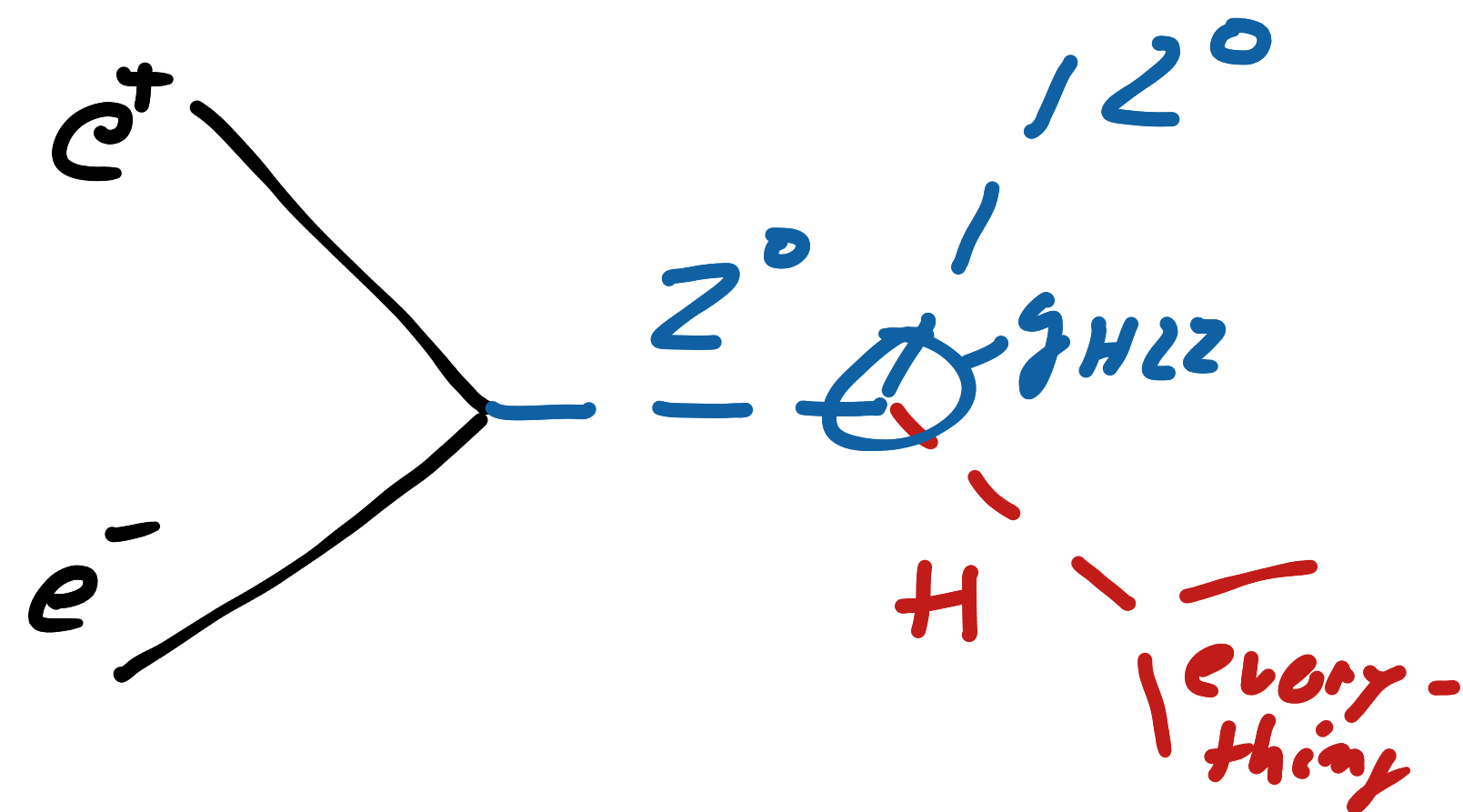
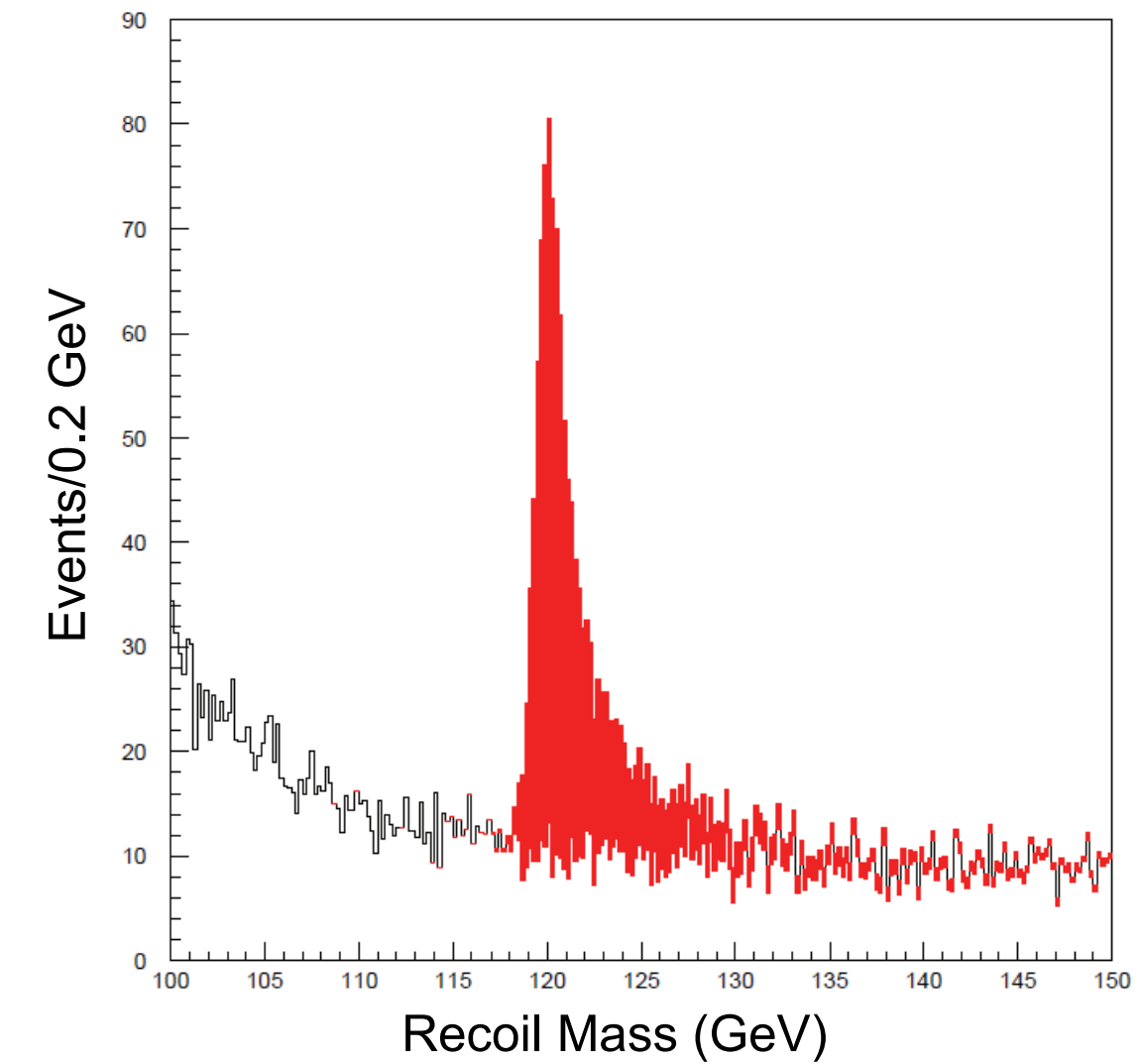
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recoil mass:
measure only the Z!

$$m_{rec}^2 = s + m_Z^2 - 2E_Z\sqrt{s}$$



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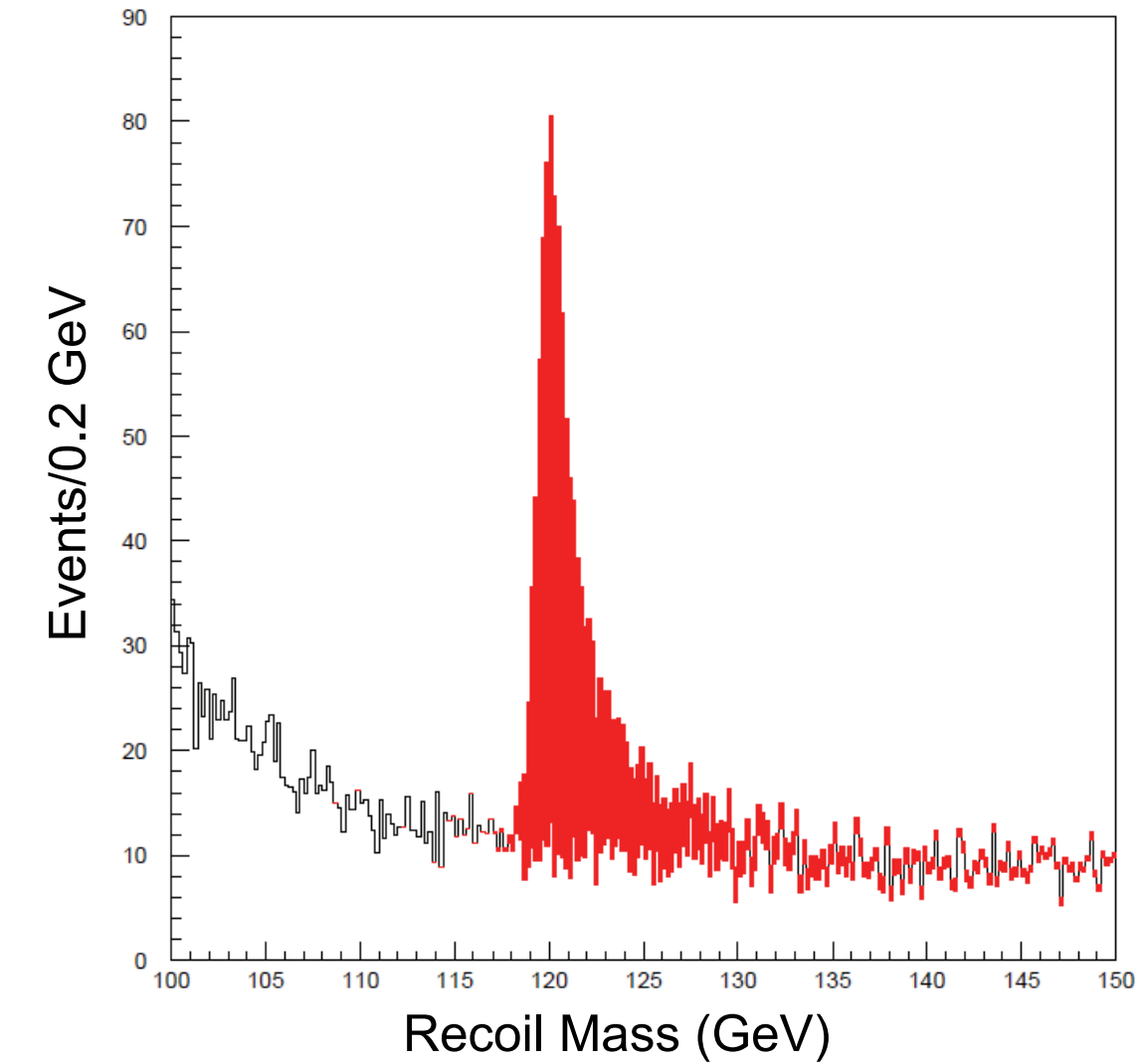
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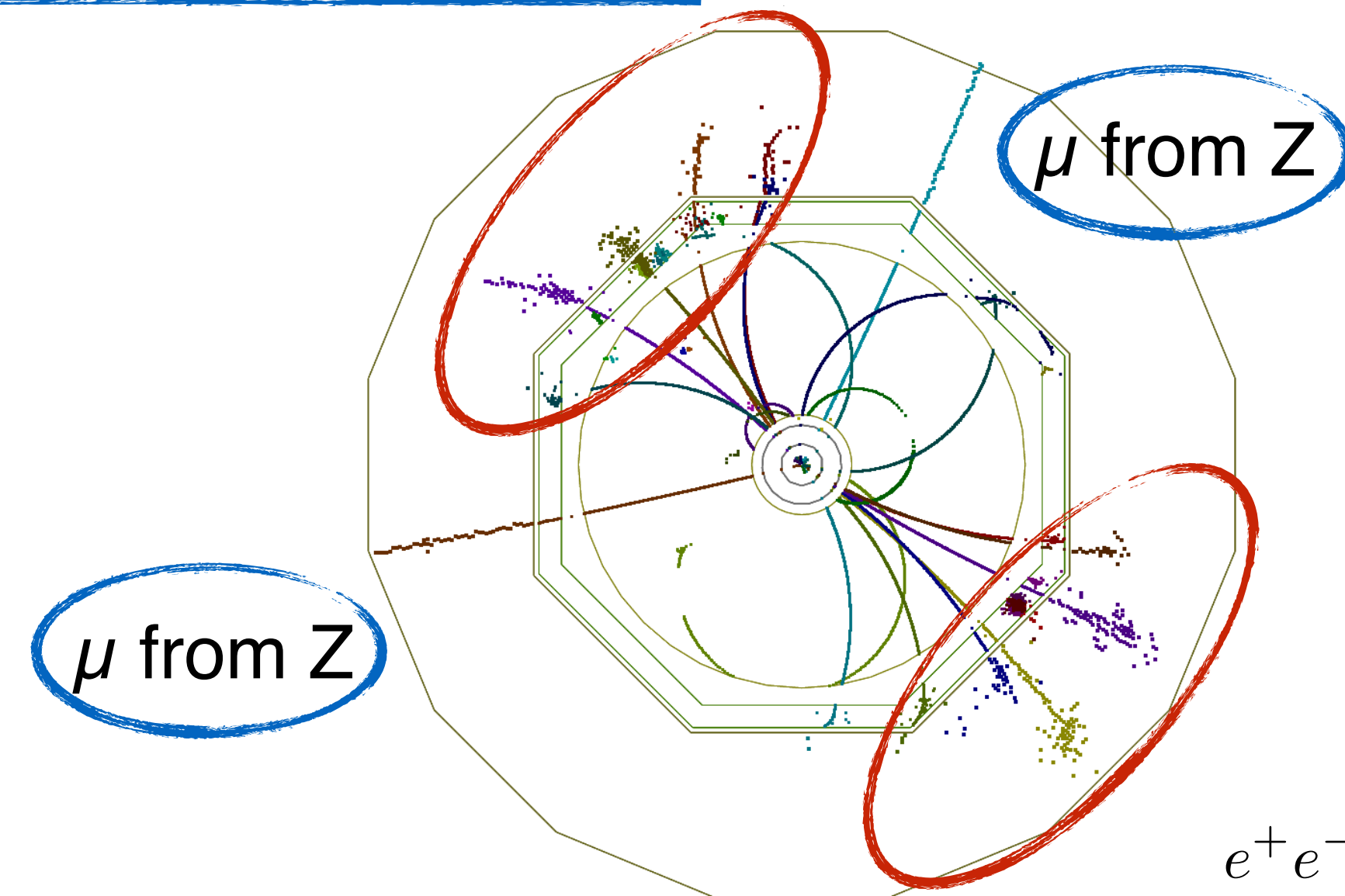
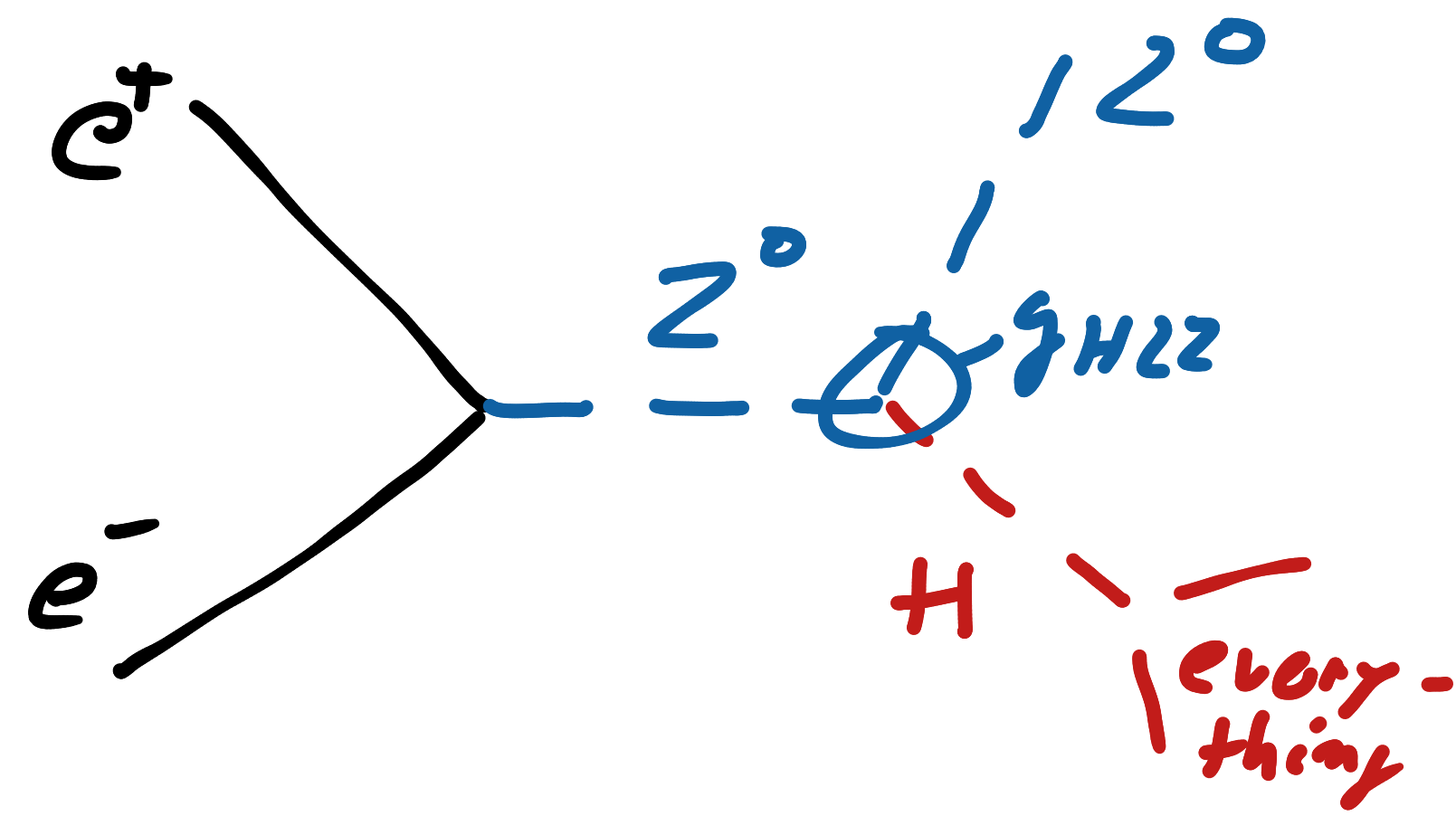
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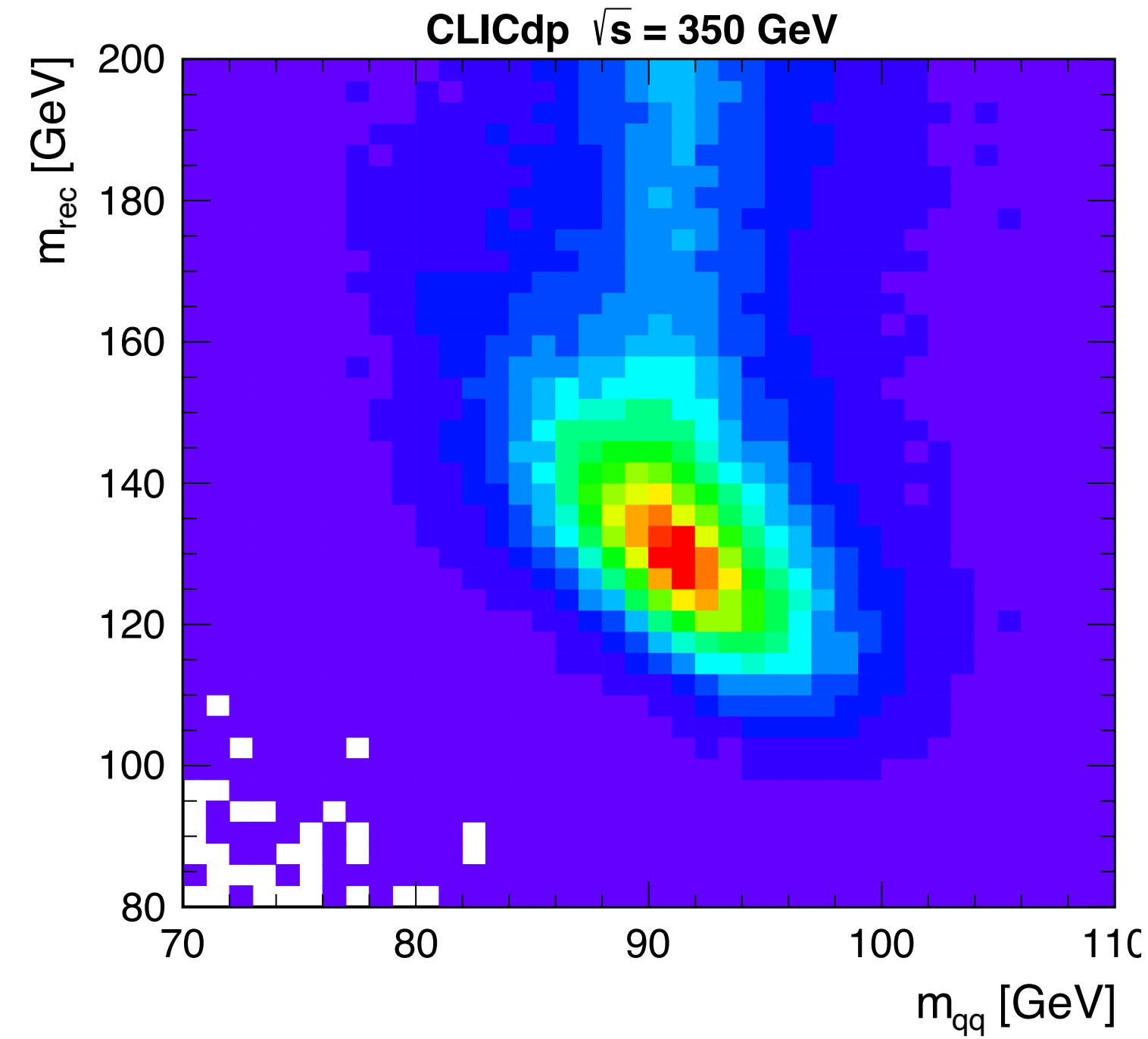


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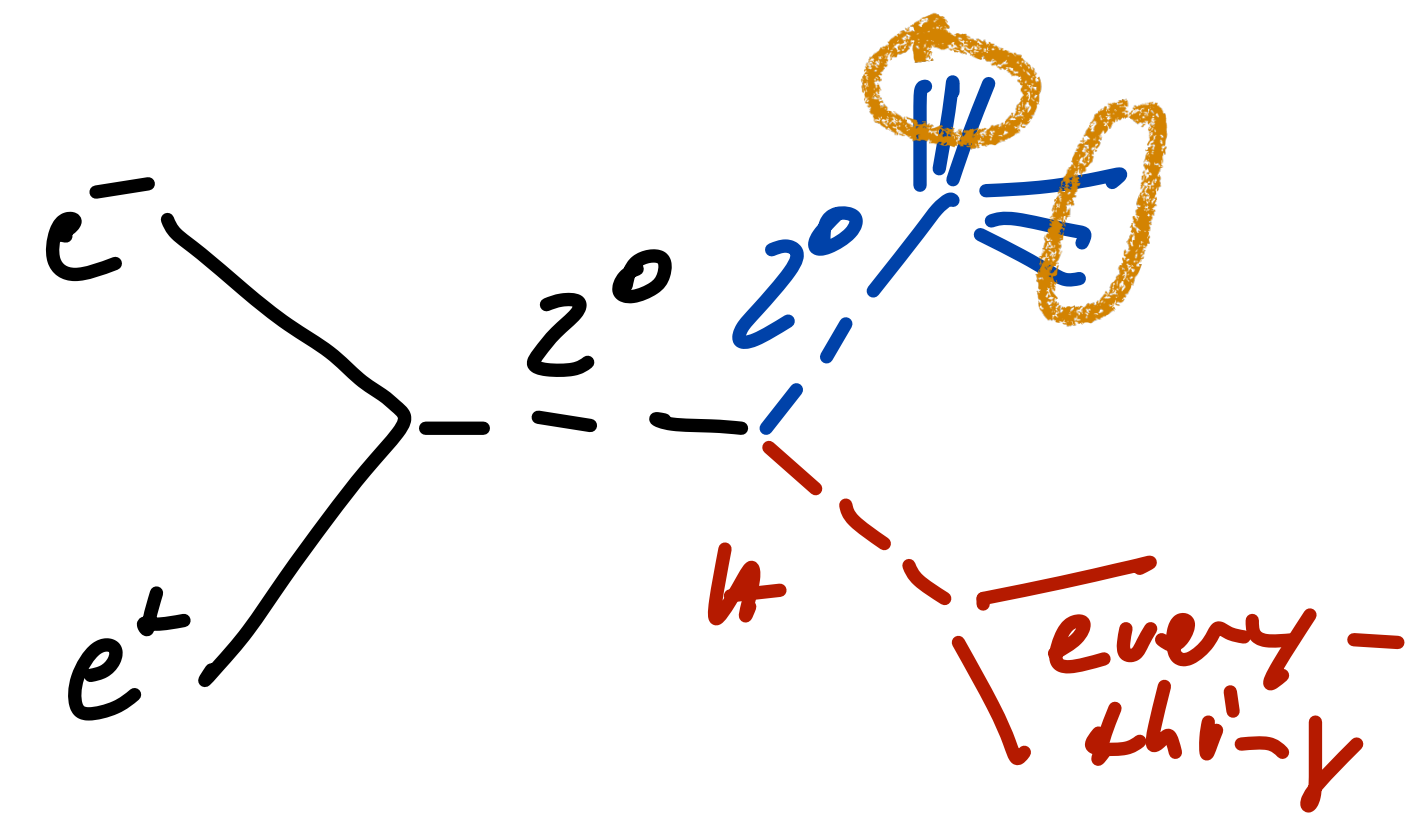
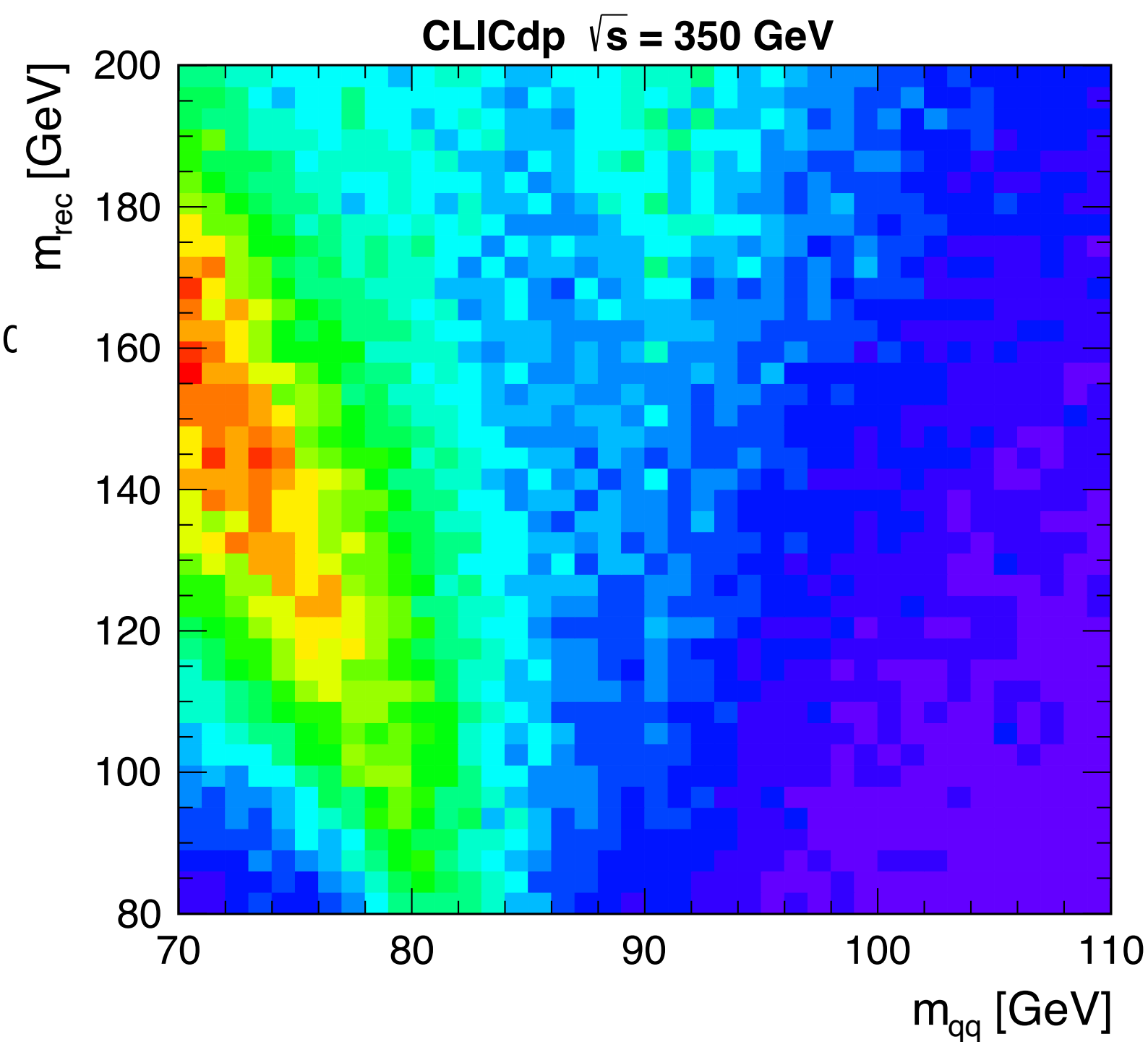
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Hadronic Recoils & Invisible Decays

Fully exploiting Higgsstrahlung



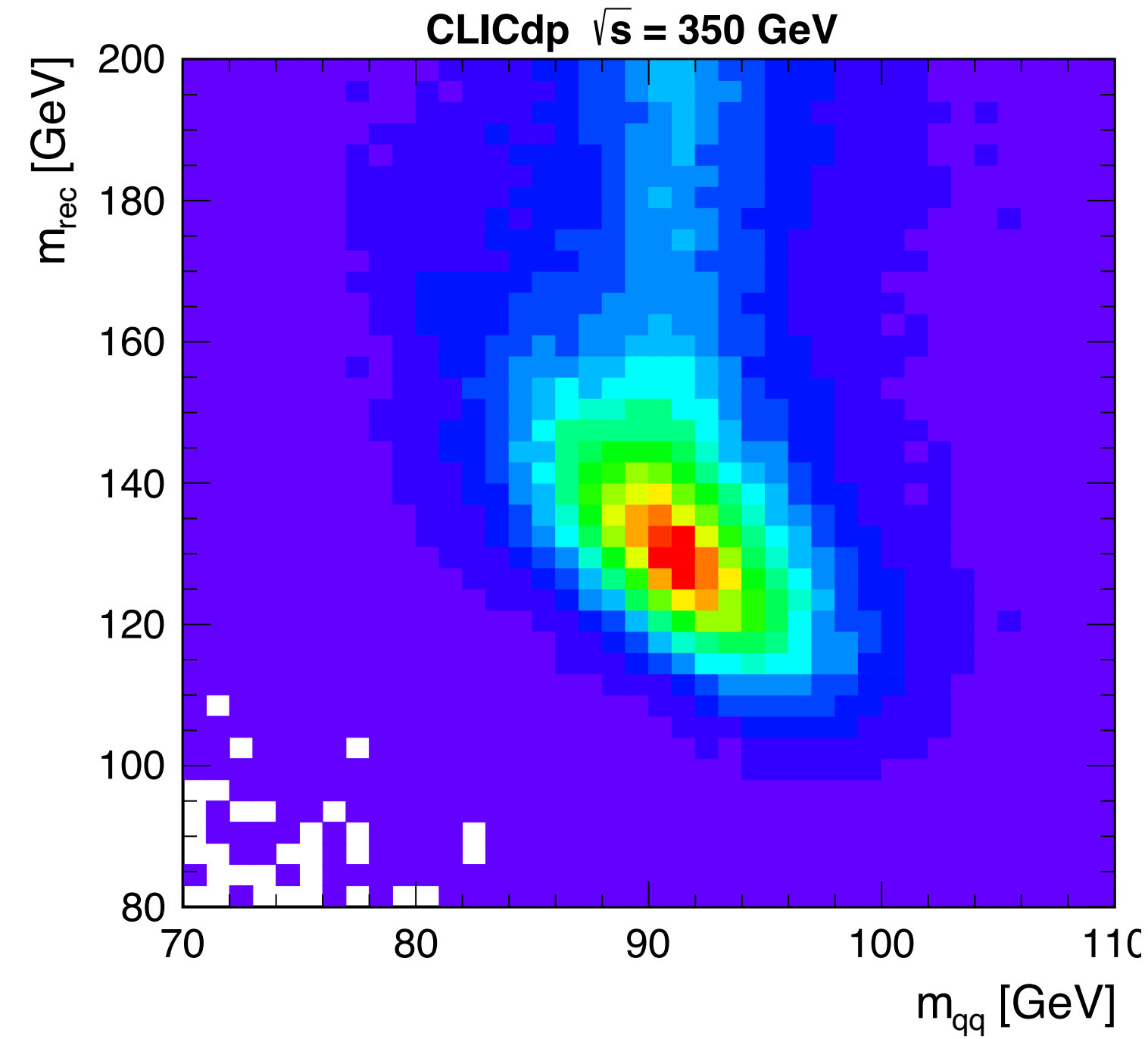
- Significantly extending the HZ sample:
Using hadronic Higgs decays - adds x4 in statistical sensitivity
- requires careful analysis setup to ensure model independence



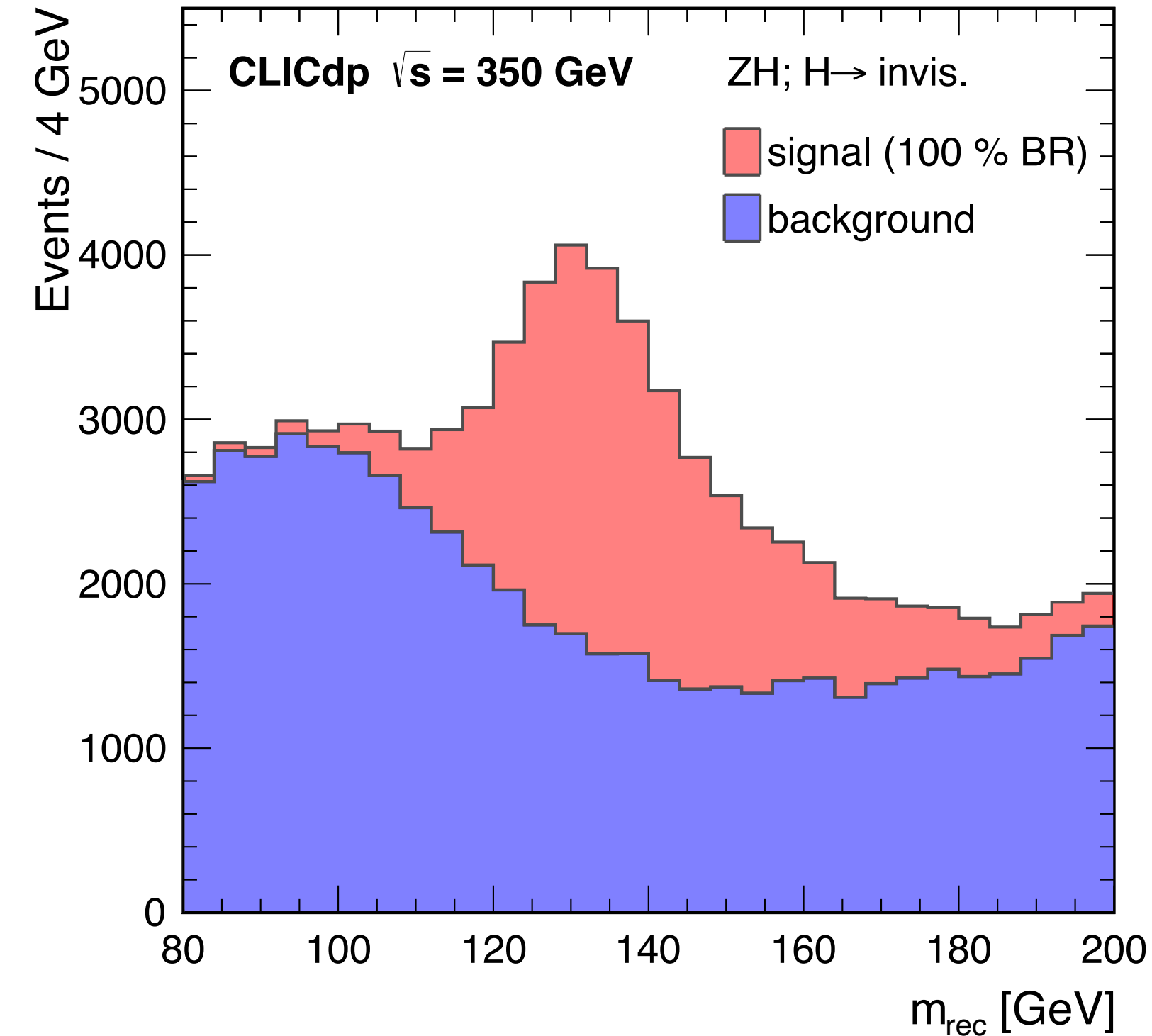
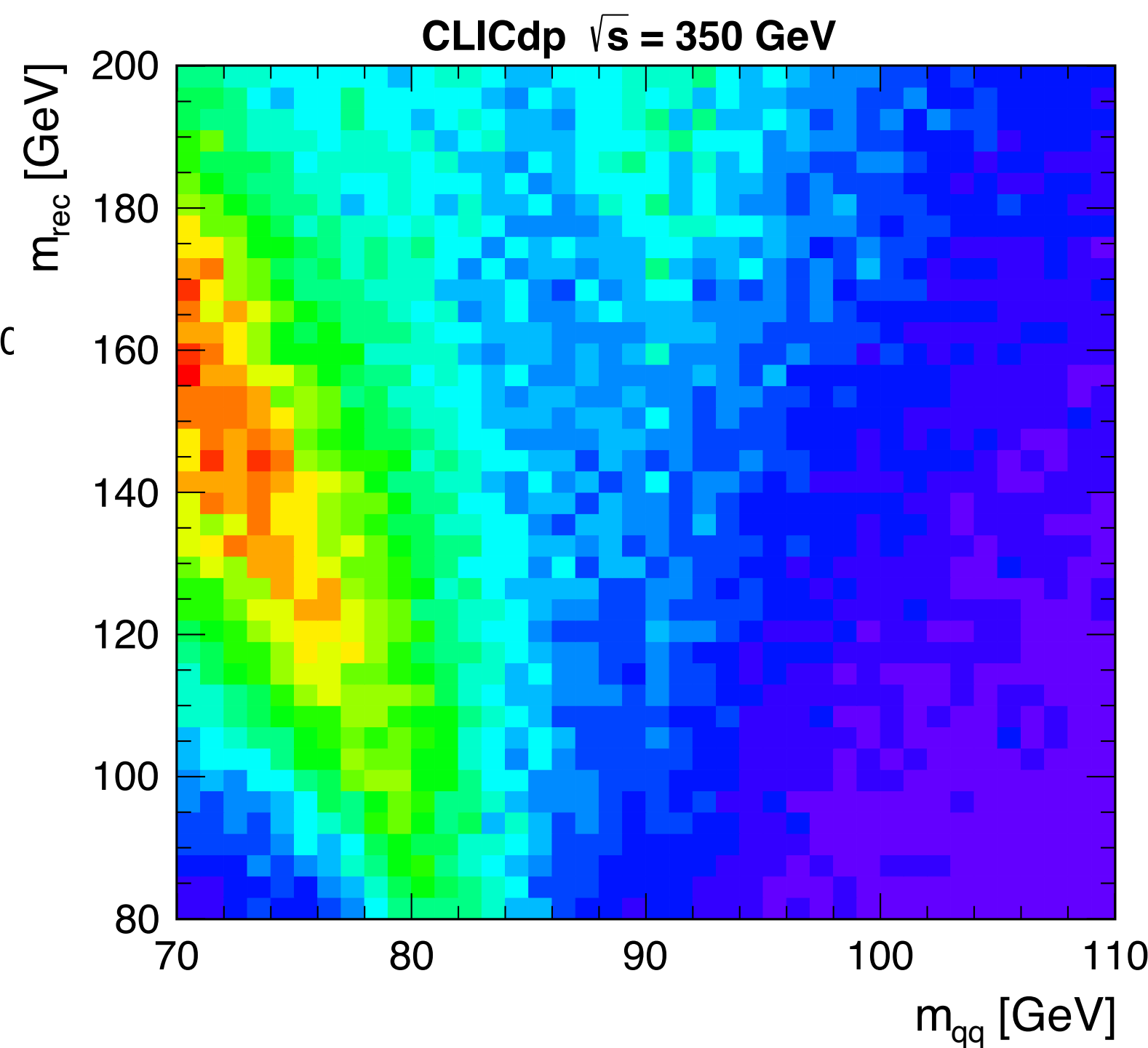
example from CLIC

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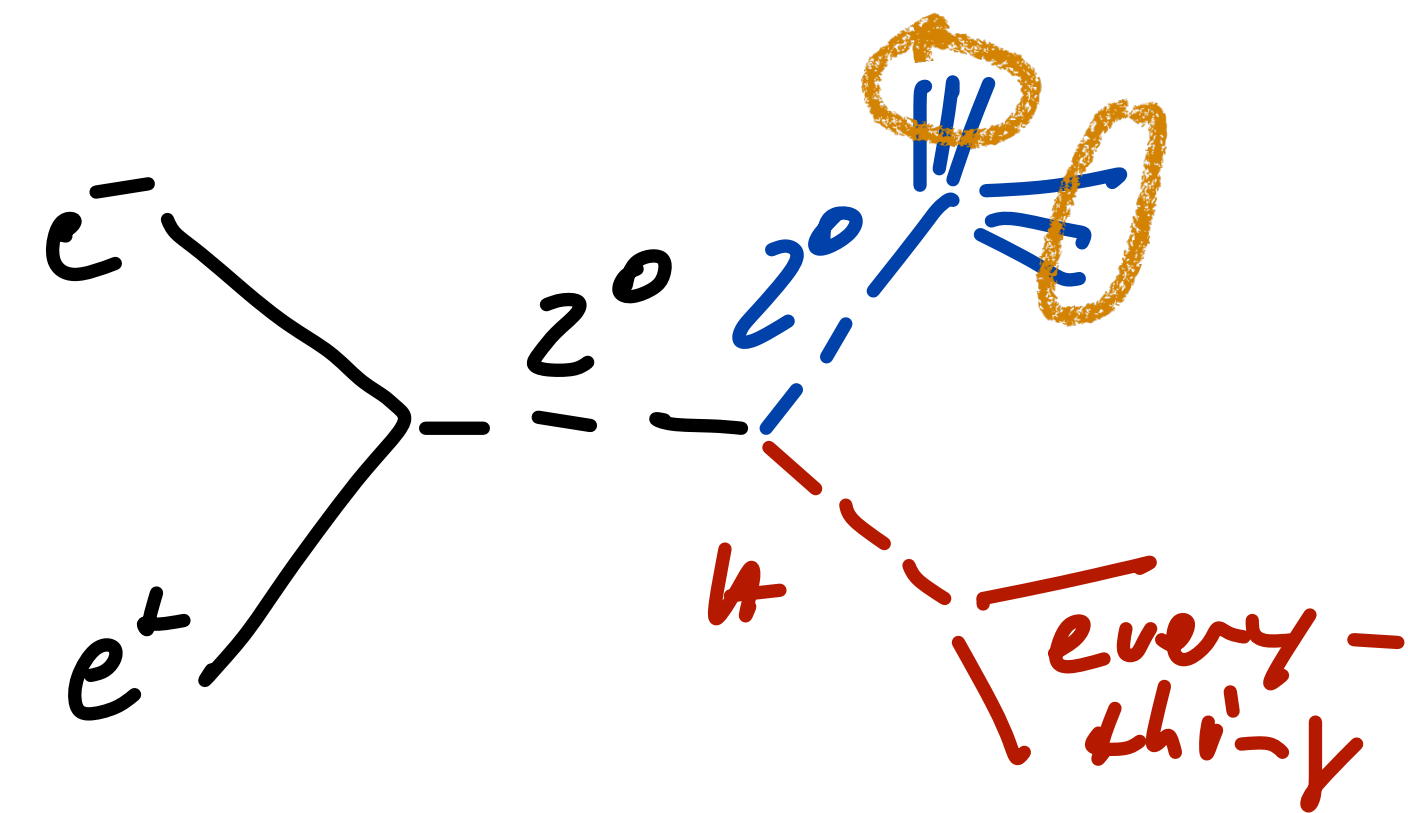
Fully exploiting Higgsstrahlung



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- HZ events can be used to constrain invisible Higgs decays: Limits on the few per mille level

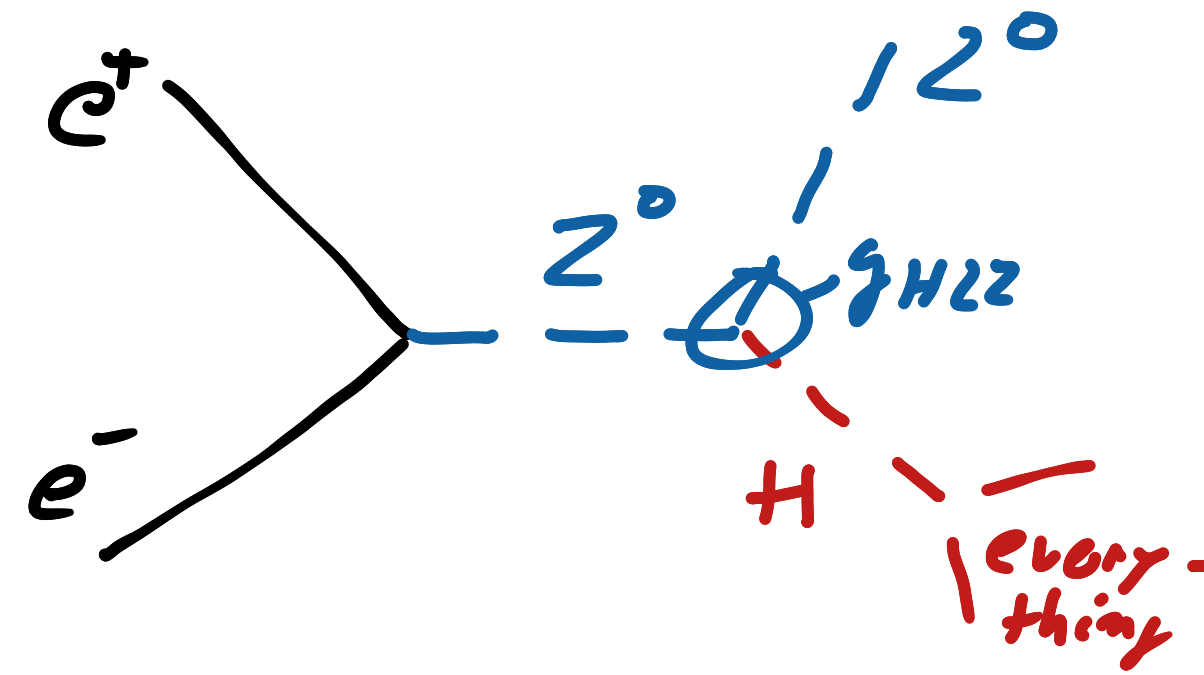


example from CLIC

- The main measurements to make:

σ for Z recoil measurements

$$\sigma_{\text{recoil}} \propto g_{HZZ}^2$$



directly constrain the coupling of Higgs to Z in a model-independent way

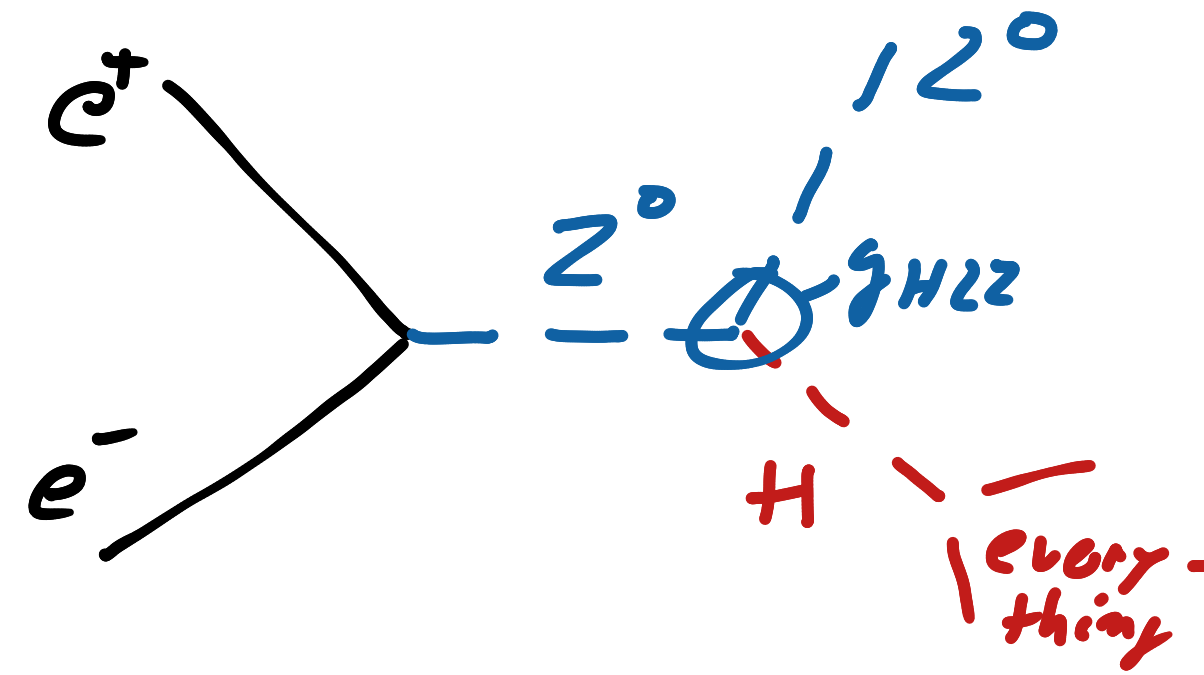
Precision Measurements of Couplings

Exploring the Higgs Sector

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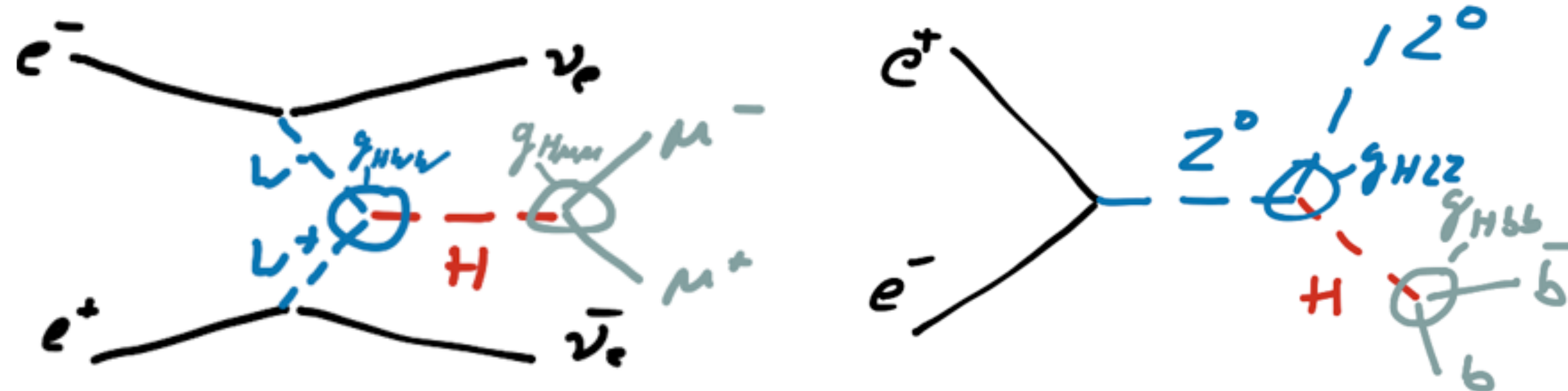
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$\sigma \times \text{BR}$ for specific Higgs decays - here the mass of 125 GeV is giving us many possibilities

$$\sigma \times \text{BR}(H \rightarrow ff) \propto \frac{g_{Hii}^2 g_{Hff}^2}{\Gamma_{\text{tot}}}$$



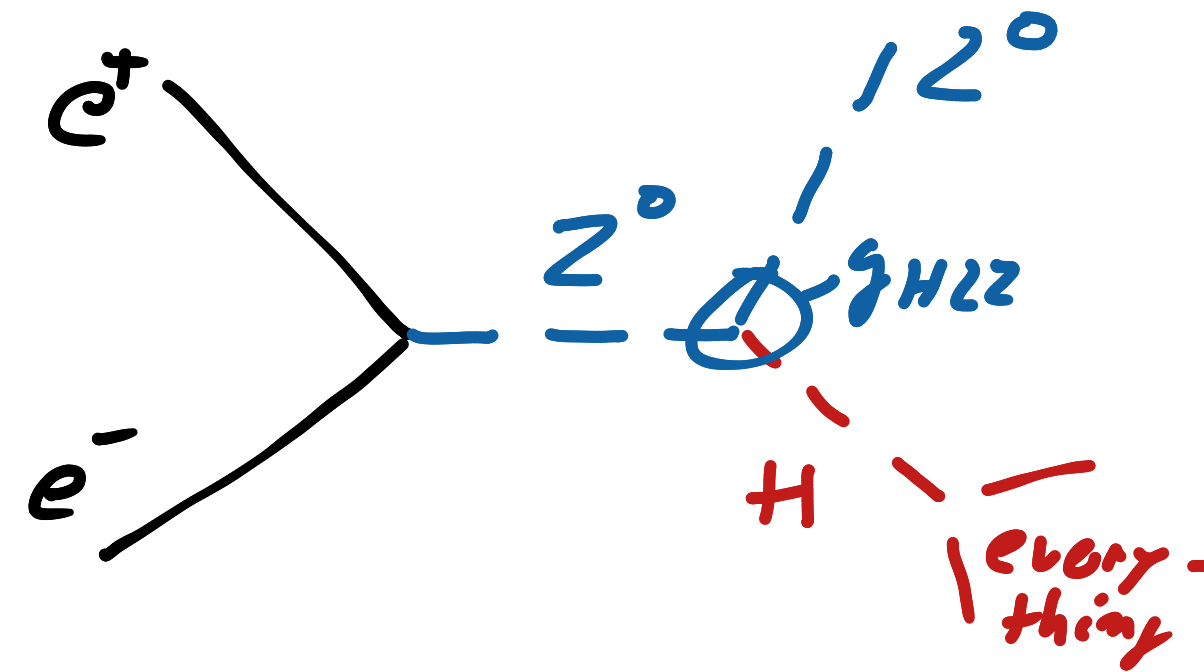
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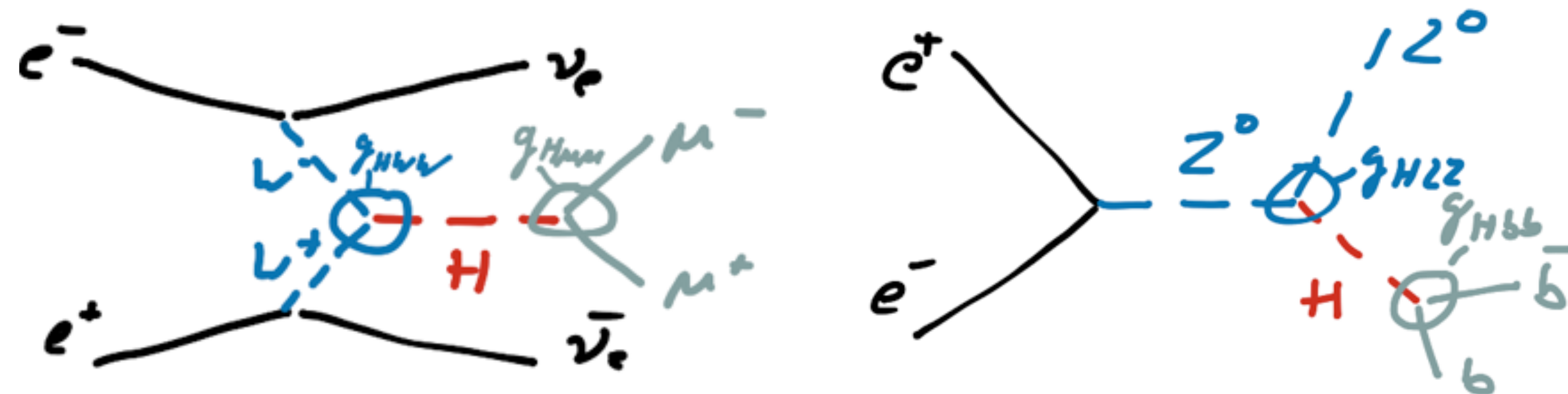
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measure couplings to fermions and bosons using production and decay

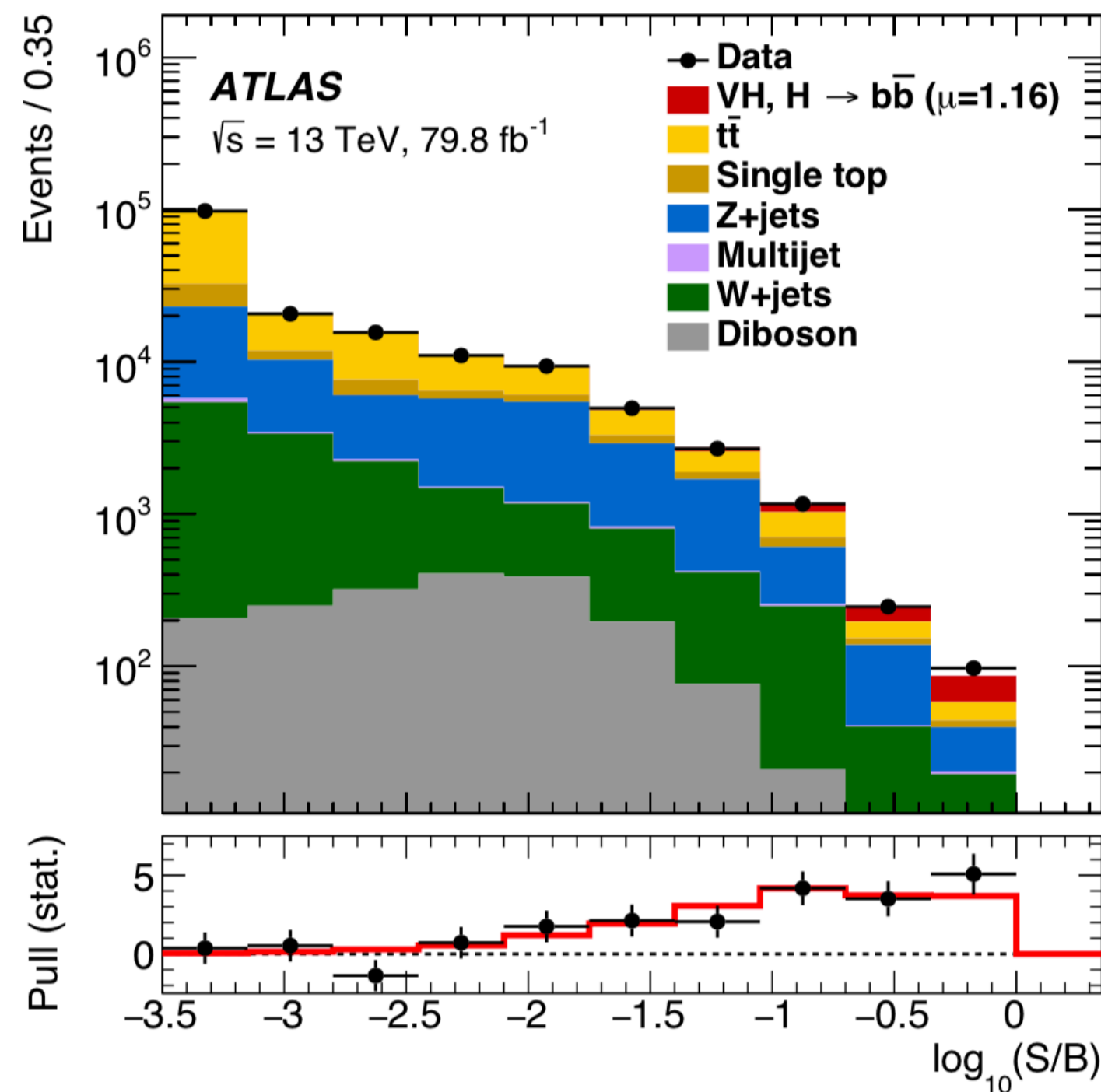
⇒ can be made model-independent in combination with the measurement of the HZ coupling in recoil

Unique Measurements at Lepton Colliders

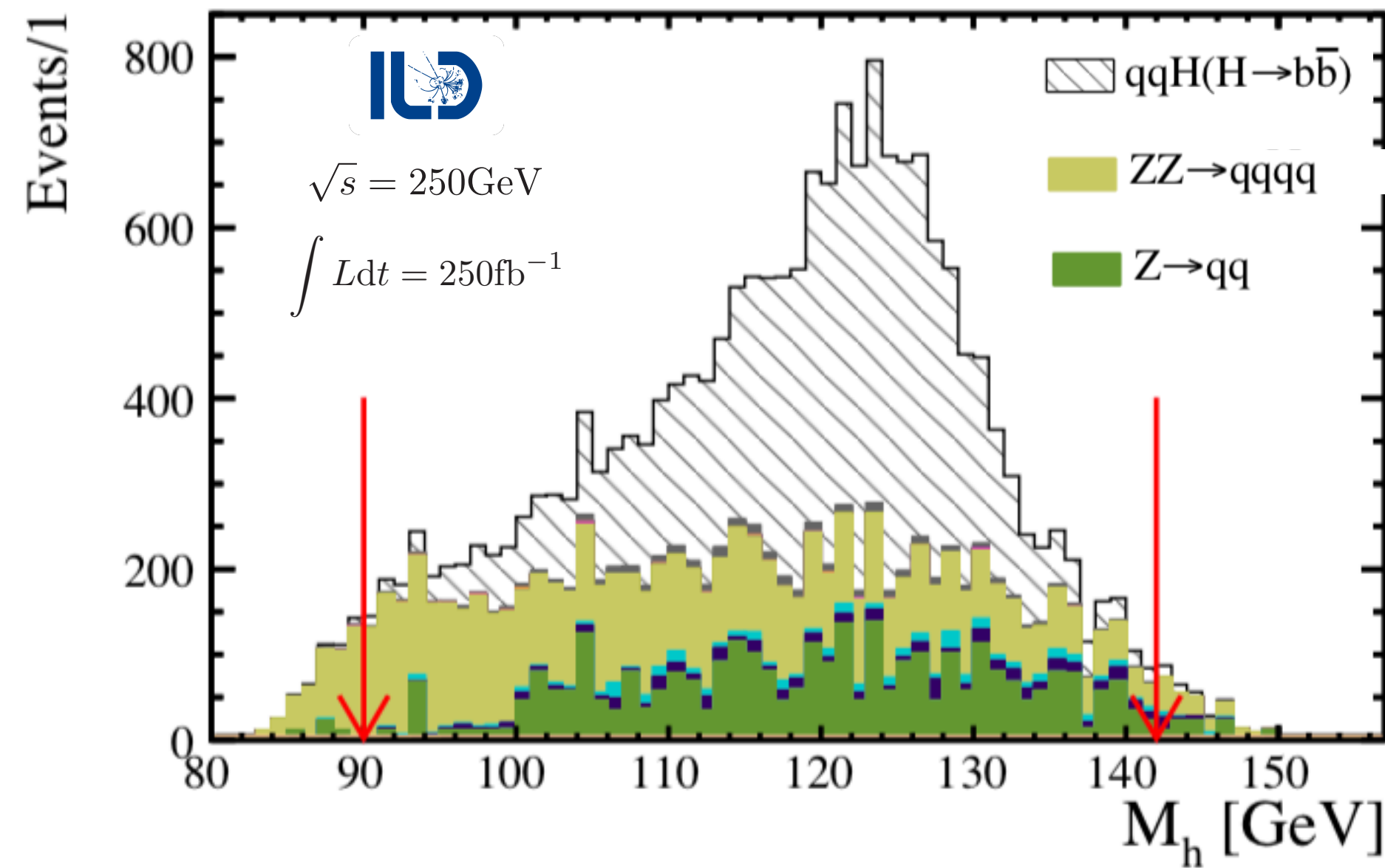
Enabled by the clean environment

- H->bb: A difficult channel at LHC, a “simple” measurement in e+e-

at LHC



at e+e-



with 1.3 fb⁻¹ data ~ 2 days running

- Low backgrounds, and highly capable detectors enable observations of final states that are hard or impossible at LHC

of Higgs produced: ~4,000,000

~400

significance: 5.4σ

5.2σ

J. Tiang, LCWS 2018

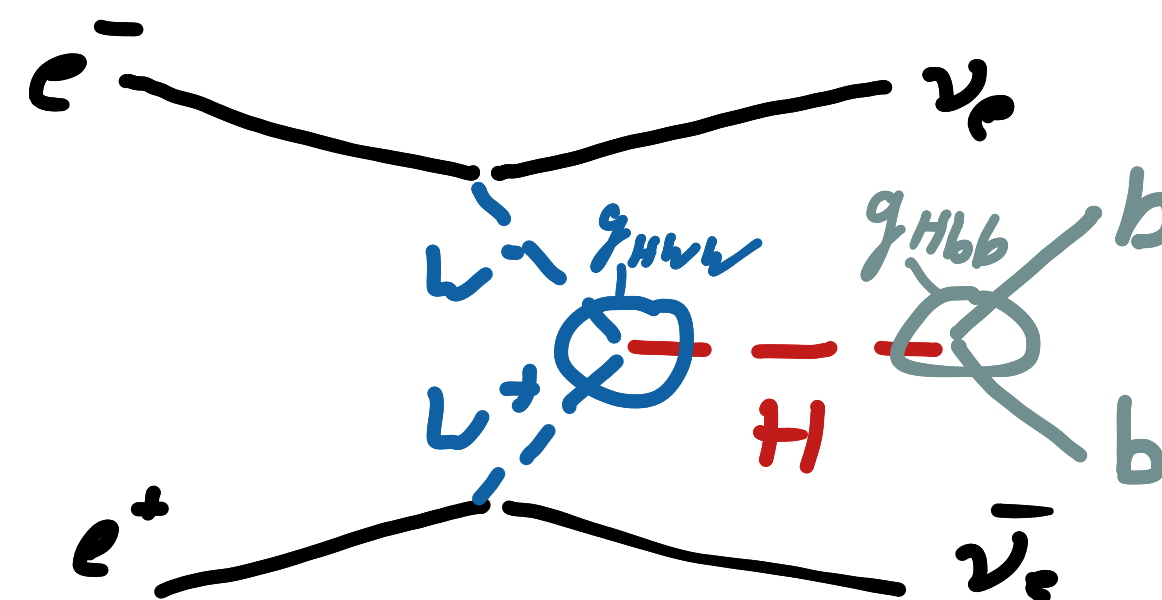
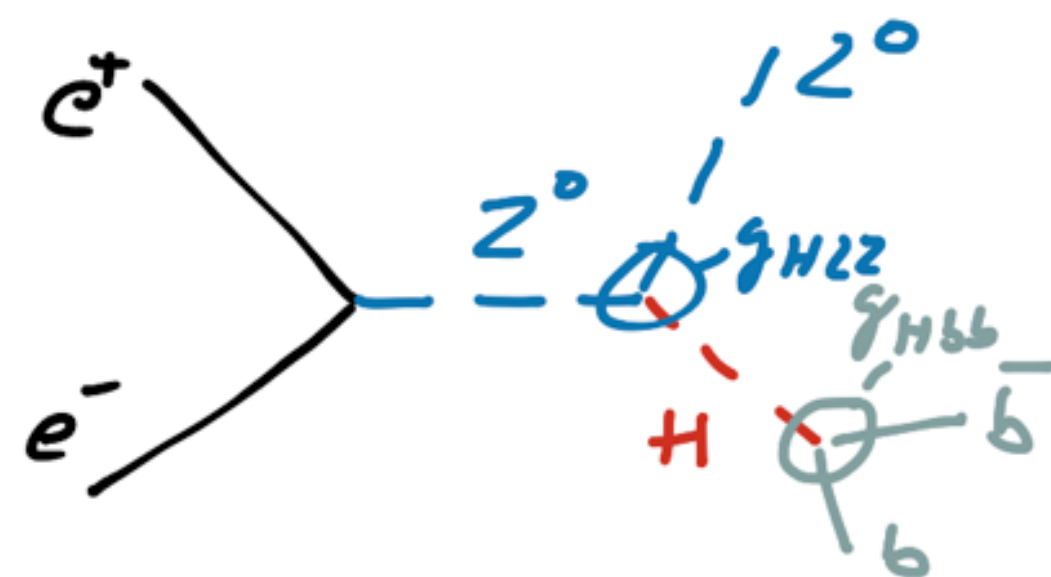
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- Higgs decays to jets: difficult (or impossible) at hadron colliders

Measurement of $H \rightarrow bb, cc, gg$

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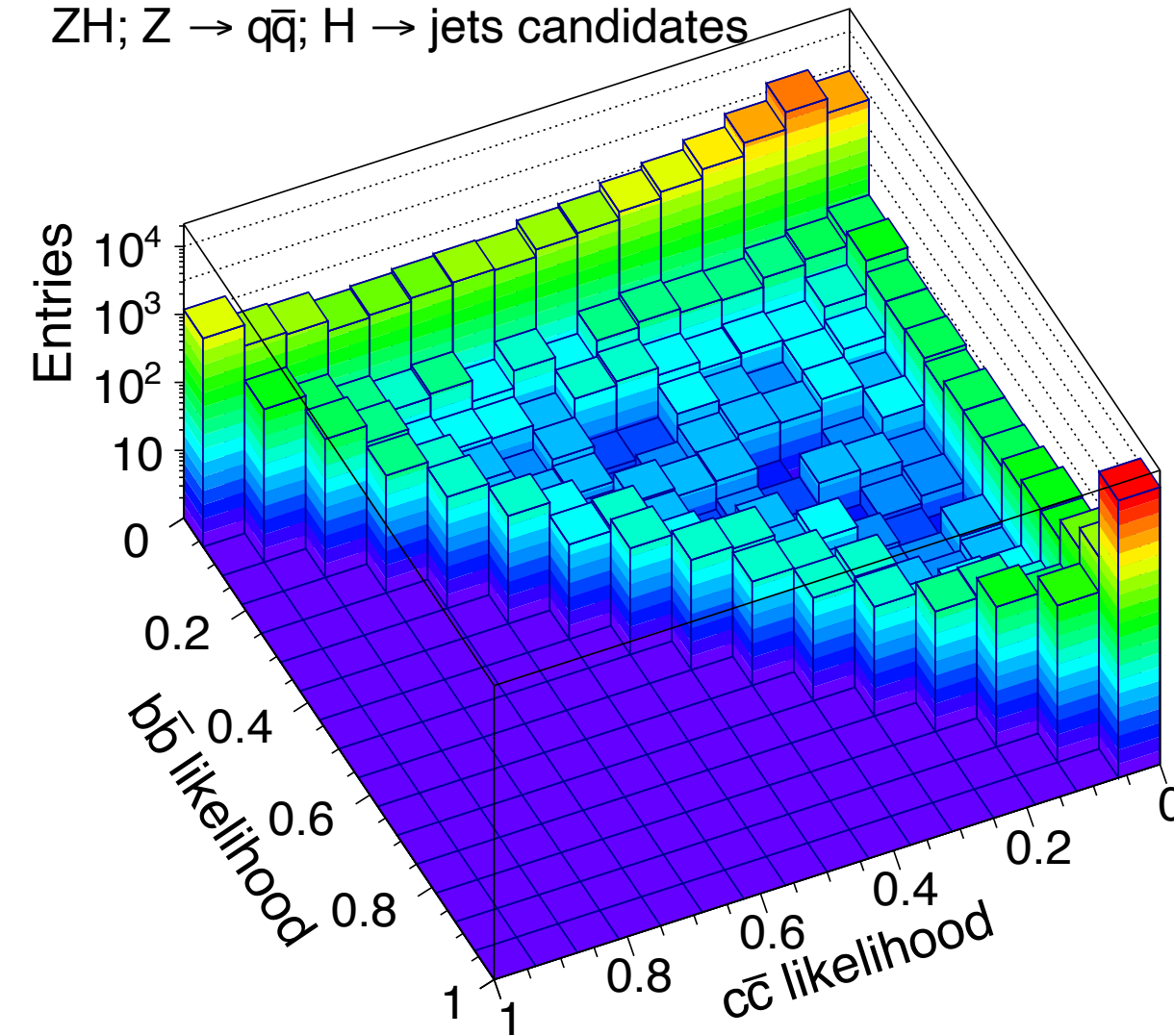
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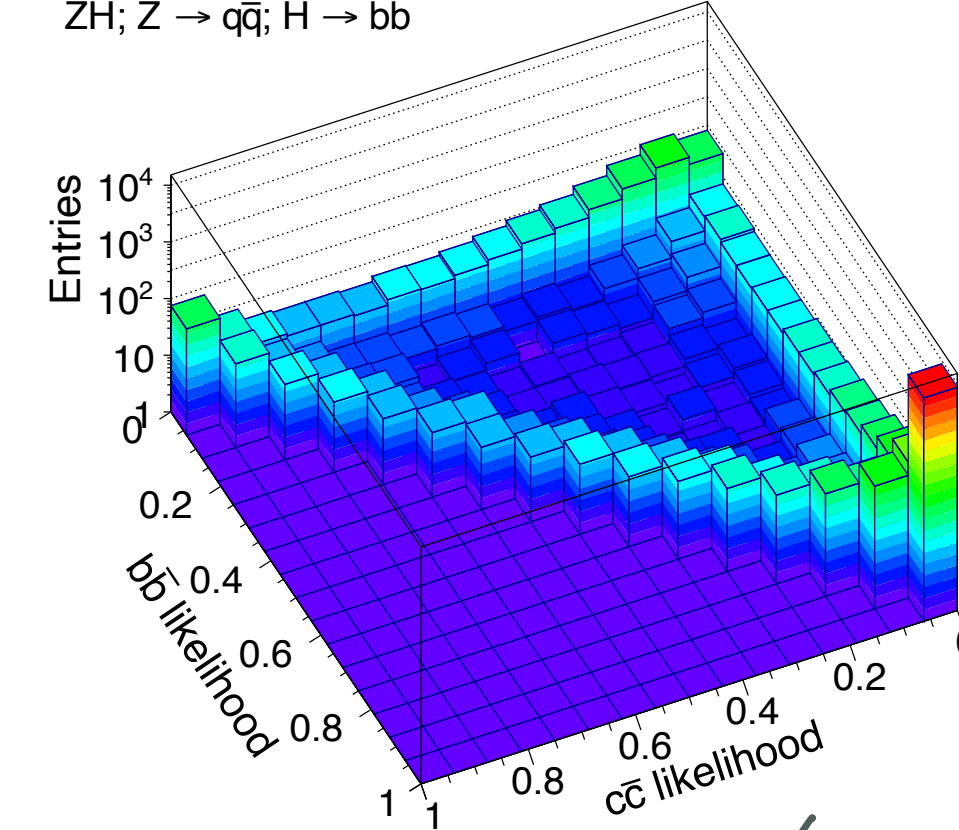
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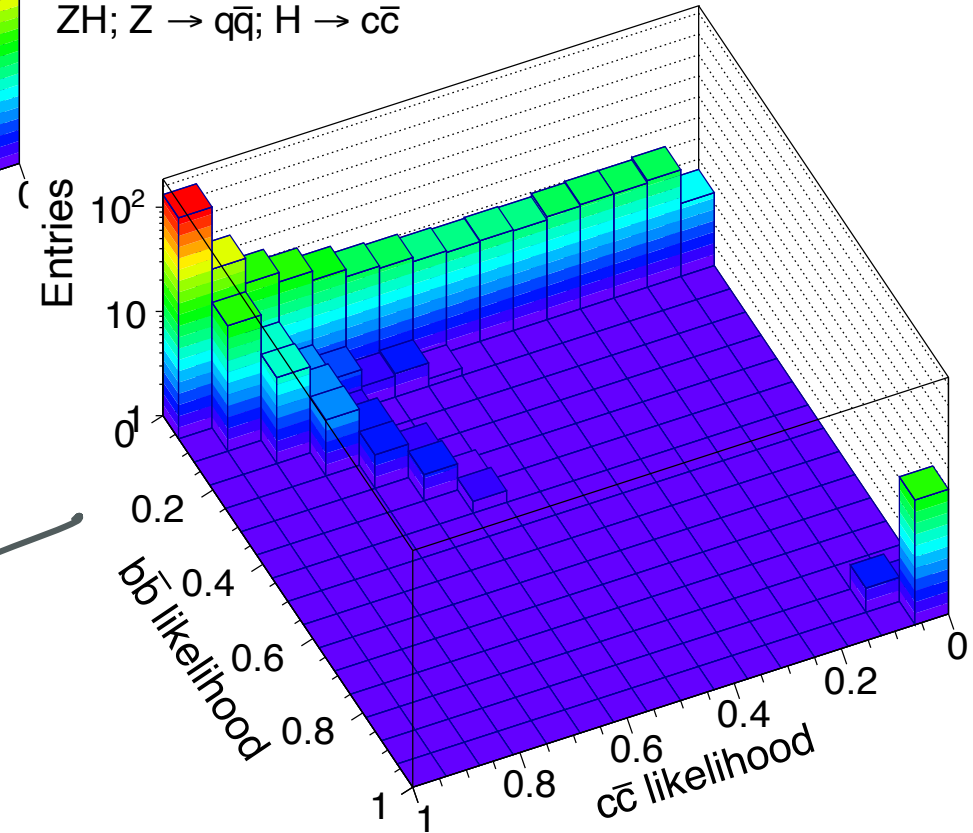
a) simulated data
ZH; Z \rightarrow q \bar{q} ; H \rightarrow jets candidates



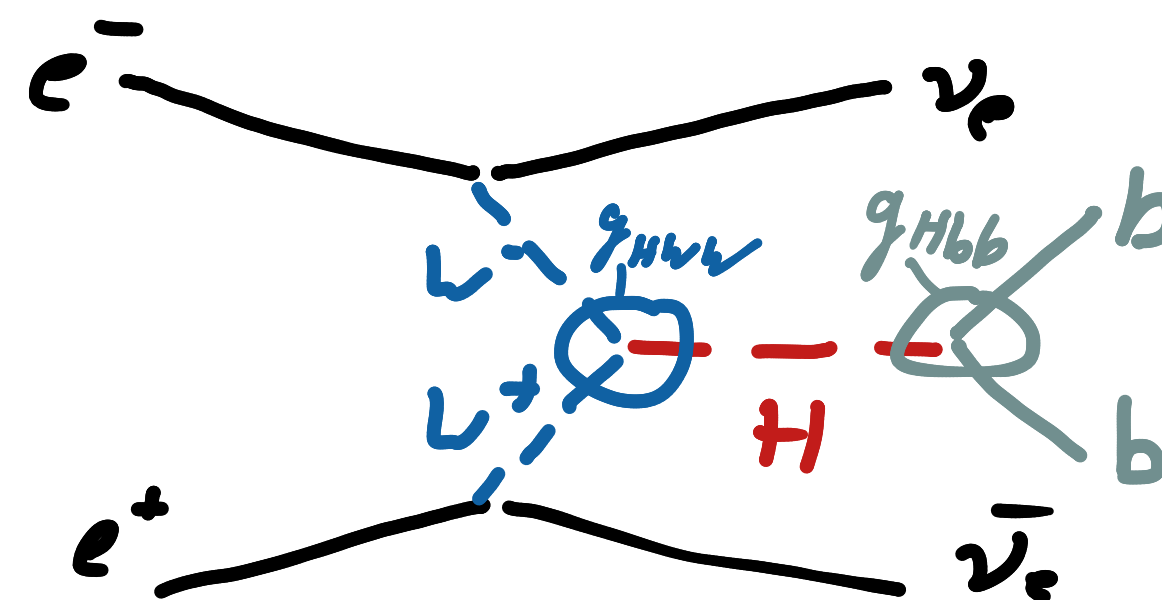
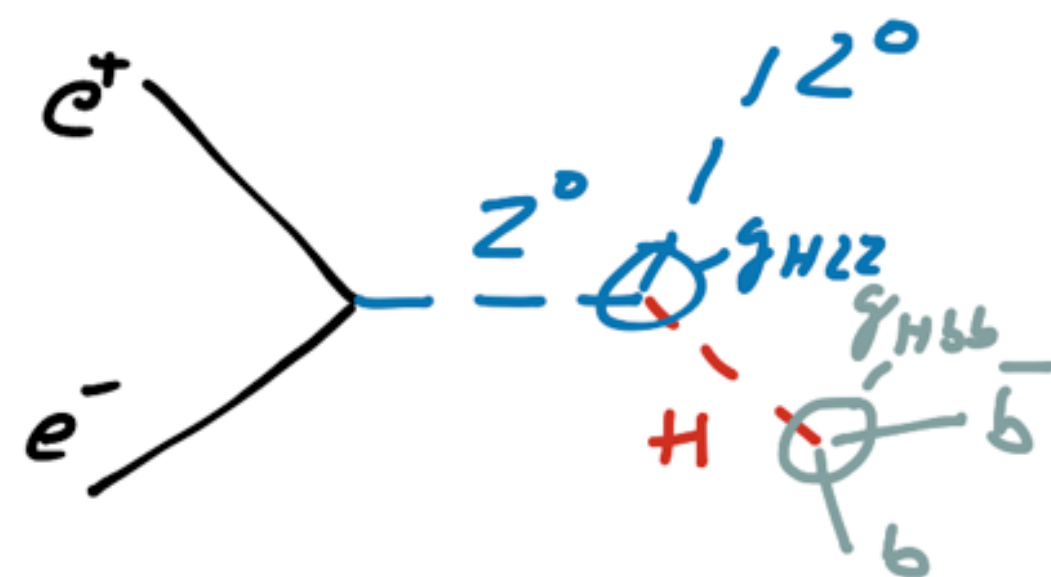
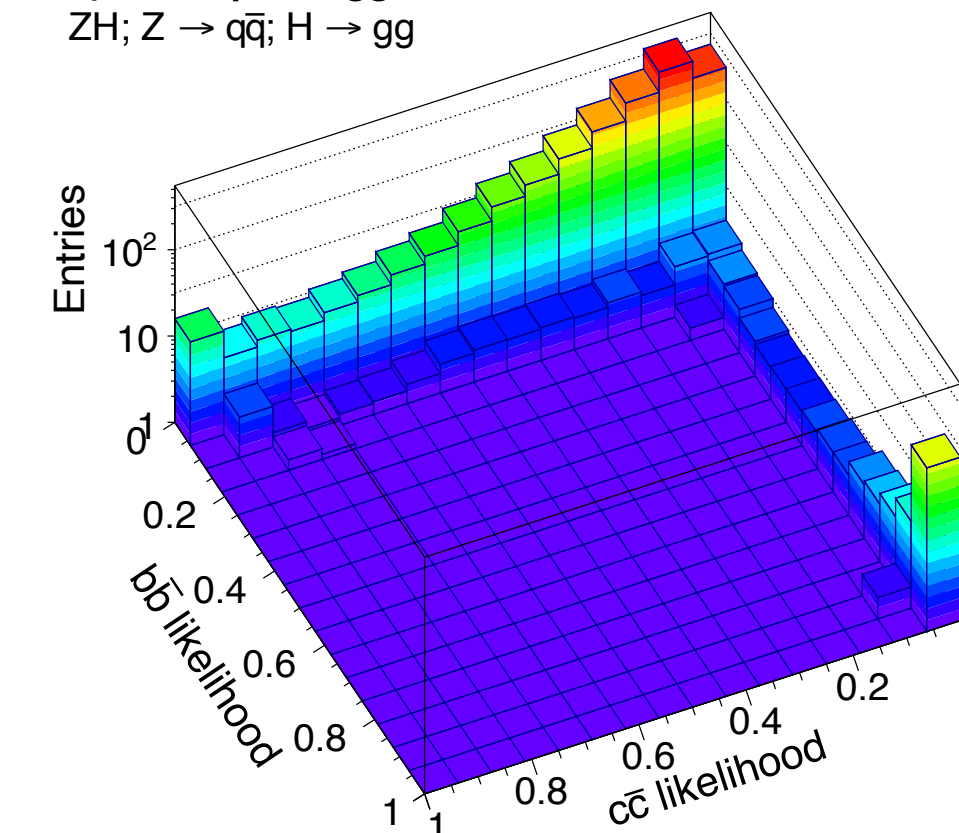
b) fit template: $b\bar{b}$ CLICdp $\sqrt{s} = 350$ GeV
ZH; Z \rightarrow q \bar{q} ; H \rightarrow $b\bar{b}$



c) fit template: $c\bar{c}$
ZH; Z \rightarrow q \bar{q} ; H \rightarrow $c\bar{c}$



d) fit template: gg
ZH; Z \rightarrow q \bar{q} ; H \rightarrow gg



- The Higgs coupling measurements at any present and future collider unfold their full potential in global fits of all observables - possibly beyond Higgs measurements alone
- The evaluation of the potential of future colliders is based on such fits using projected precisions on various Higgs (and other) measurements as input

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- **“Model-independent” fit**

minimize a χ^2 with all measurements:

$$\chi^2 = \sum_i \frac{(C_i - 1)^2}{\Delta F_i^2}$$

$$C_{ZH} = g_{HZZ}^2$$

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ΔF_i : uncertainty of measurement (σ or $\sigma \times \text{BR}$)

total width as a free parameter: no constraints imposed on BSM decays

N.B.: Not fully model independent, does not account for certain possible BSM features of HV couplings

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- **“Model-independent EFT” fit**

A global fit of Higgs and other EW observables parametrizing deviations from the SM by various operators - allows for couplings not included in κ fit, includes connections between W and Z couplings

Extracting the Total Width

Model independent measurement at high precision

- e^+e^- colliders provide the possibility for a model-independent measurement of the total width at the level of a few %:

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⇒ Profits substantially from higher energy, where WW fusion becomes relevant:

$$\sigma(\text{H}\nu_e\nu_e) \times \text{BR}(\text{H} \rightarrow \text{WW}^*) \propto \frac{g_{\text{HWW}}^4}{\Gamma_{\text{tot}}}$$

$$\frac{\sigma(e^+e^- \rightarrow \text{ZH}) \times \text{BR}(\text{H} \rightarrow b\bar{b})}{\sigma(e^+e^- \rightarrow \text{H}\nu_e\nu_e) \times \text{BR}(\text{H} \rightarrow b\bar{b})} \propto \frac{g_{\text{HZZ}}^2}{g_{\text{HWW}}^2}$$

need the “model-independent anchor”
of the ZH measurement

Extracting the Total Width

Model independent measurement at high precision

- e^+e^- colliders provide the possibility for a model-independent measurement of the total width at the level of a few %:
- In the “model-independent fit” framework the total width is obtained from production and decay of the Higgs:

$$\sigma(\text{ZH}) \times \text{BR}(\text{H} \rightarrow \text{ZZ}) \propto \frac{g_{\text{HZZ}}^4}{\Gamma_{\text{tot}}} \quad \text{and} \quad \sigma(\text{ZH}) \propto g_{\text{HZZ}}^2$$

⇒ The low BR of $\text{H} \rightarrow \text{ZZ}$ and correspondingly large uncertainties make this determination relatively imprecise

⇒ Profits substantially from higher energy, where WW fusion becomes relevant:

$$\sigma(\text{H}\nu_e\nu_e) \times \text{BR}(\text{H} \rightarrow \text{WW}^*) \propto \frac{g_{\text{HWW}}^4}{\Gamma_{\text{tot}}}$$

$$\frac{\sigma(e^+e^- \rightarrow \text{ZH}) \times \text{BR}(\text{H} \rightarrow b\bar{b})}{\sigma(e^+e^- \rightarrow \text{H}\nu_e\nu_e) \times \text{BR}(\text{H} \rightarrow b\bar{b})} \propto \frac{g_{\text{HZZ}}^2}{g_{\text{HWW}}^2}$$

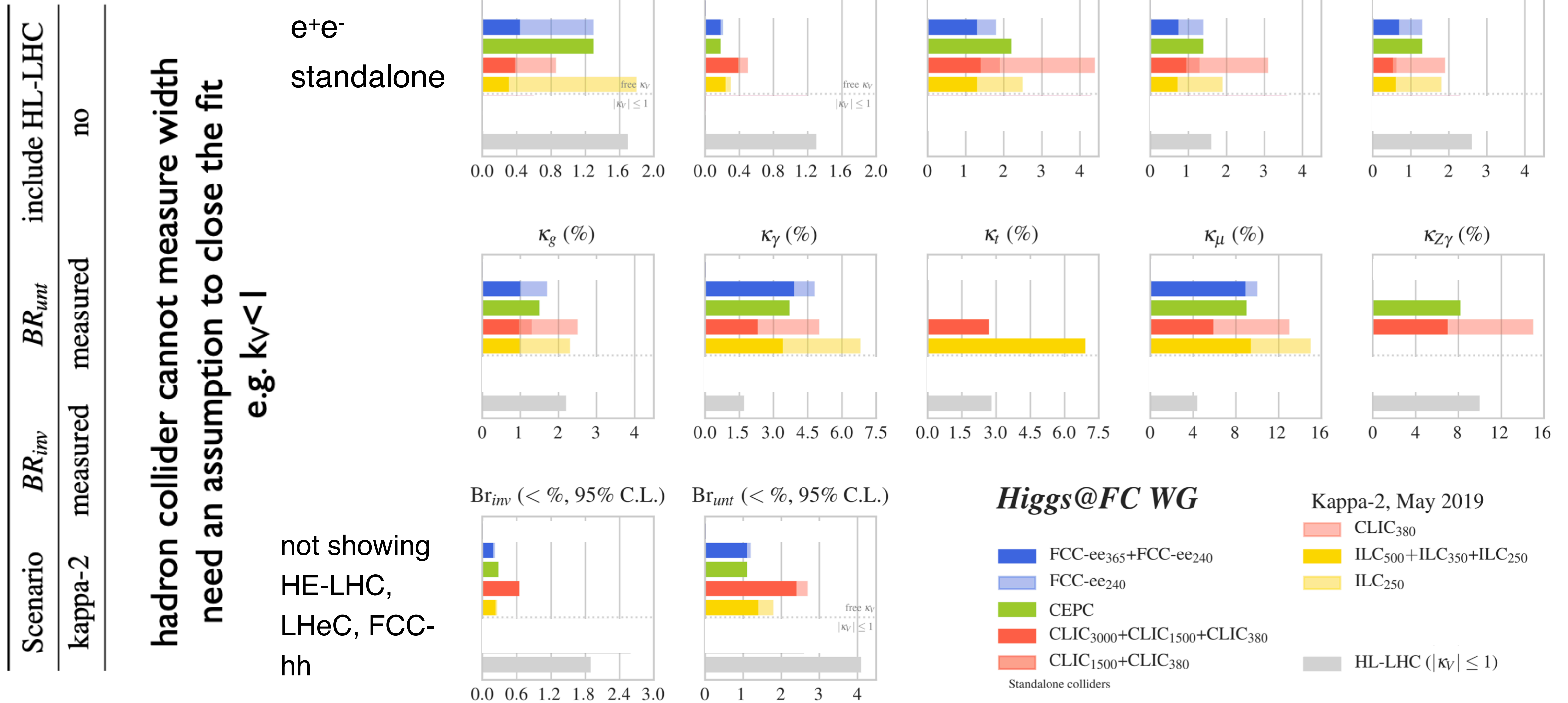
need the “model-independent anchor”
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⇒ Higher energies important for width measurements

⇒ In EFT fits W and Z are connected, there the width can be well constrained also without WW fusion

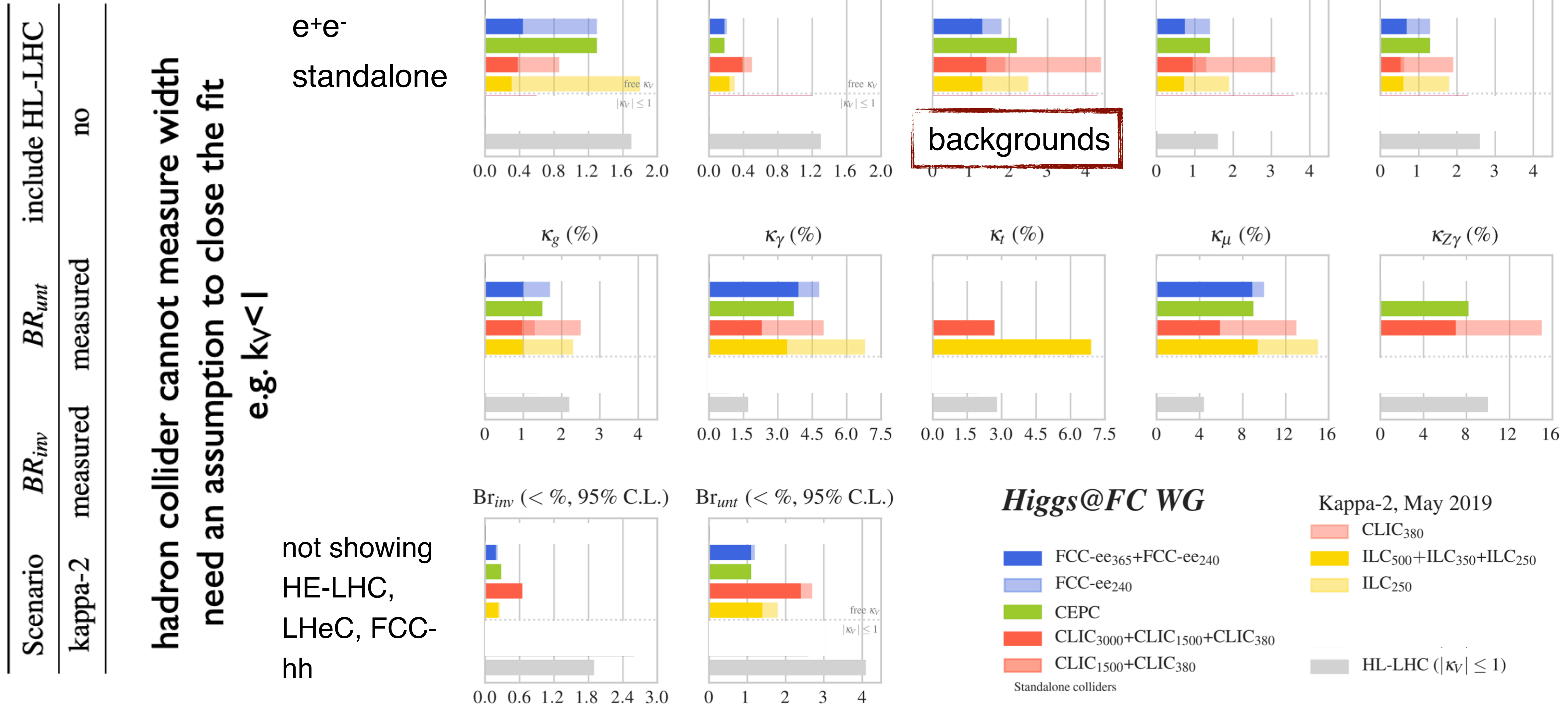
Perspectives on Precision

Illustrating Interplay and Reach



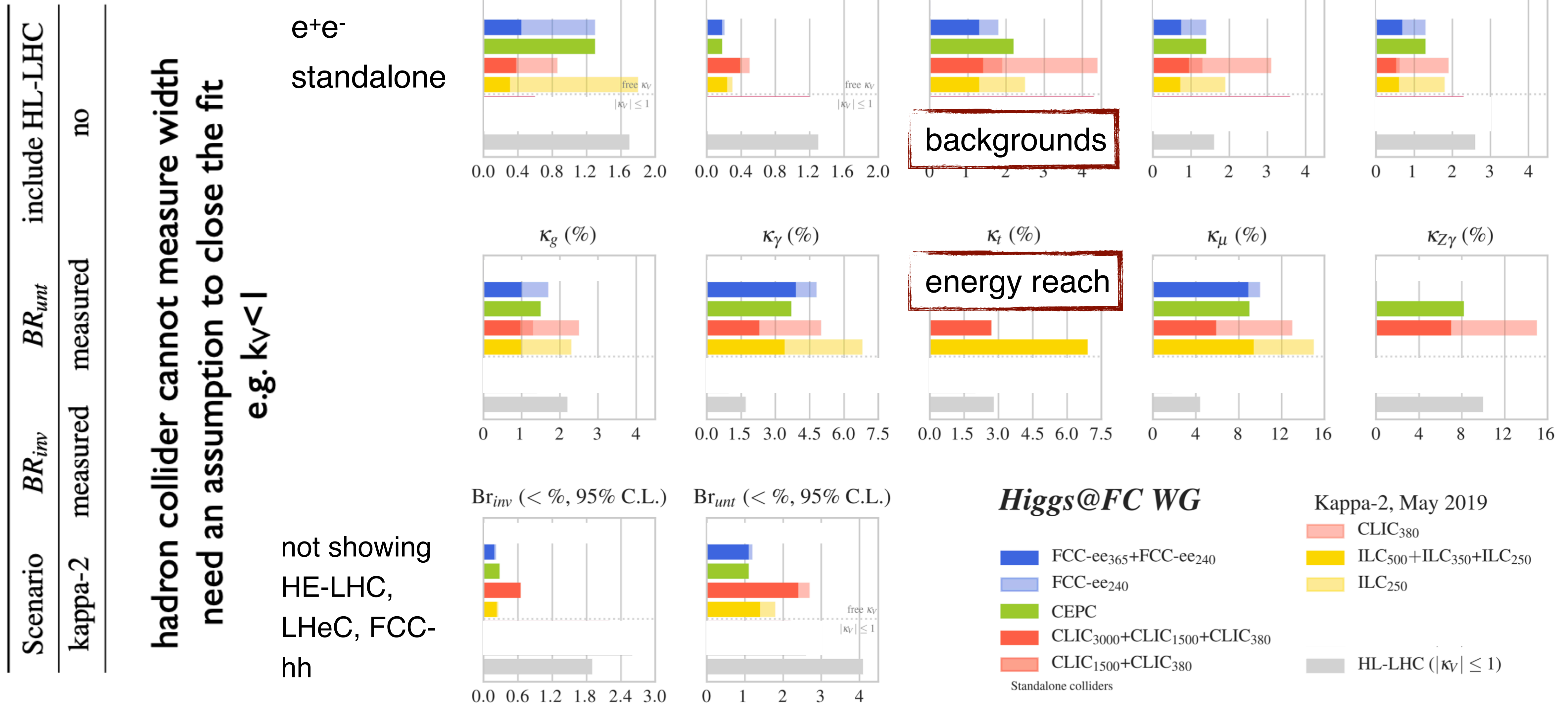
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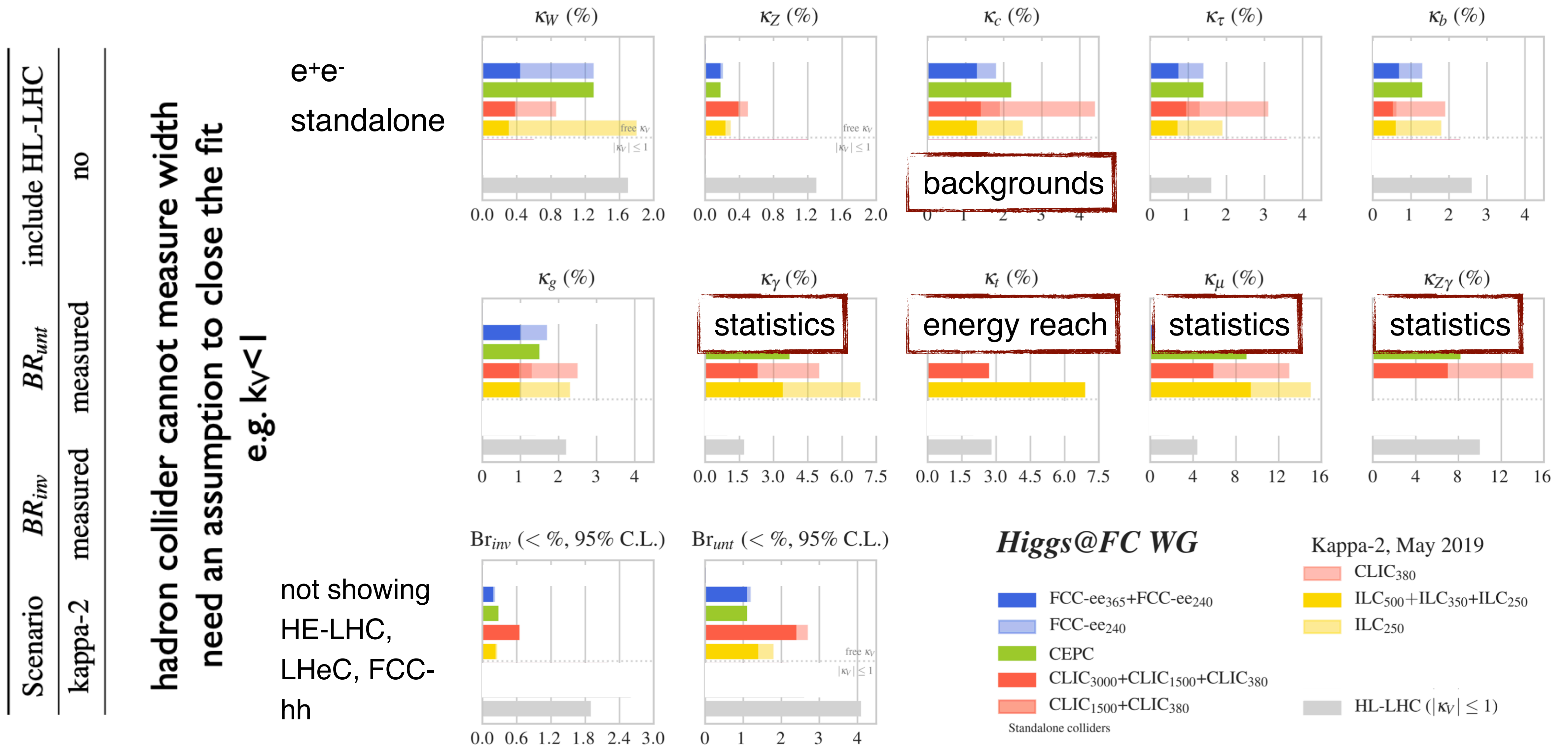
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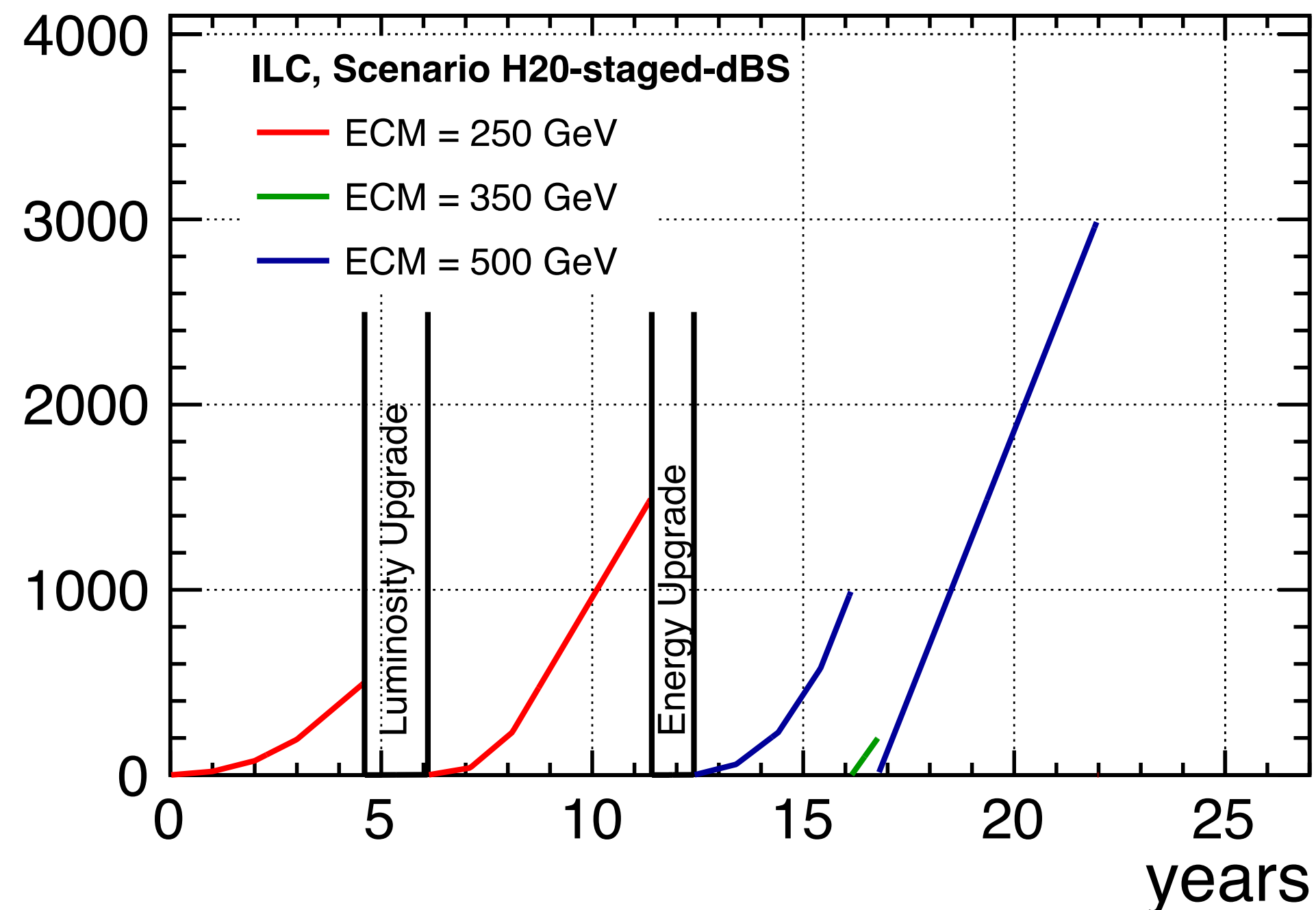
Illustrating Interplay and Reach



The Relevance of Higgs Coupling Measurements

One EFT Example for ILC

Integrated Luminosities [fb^{-1}]

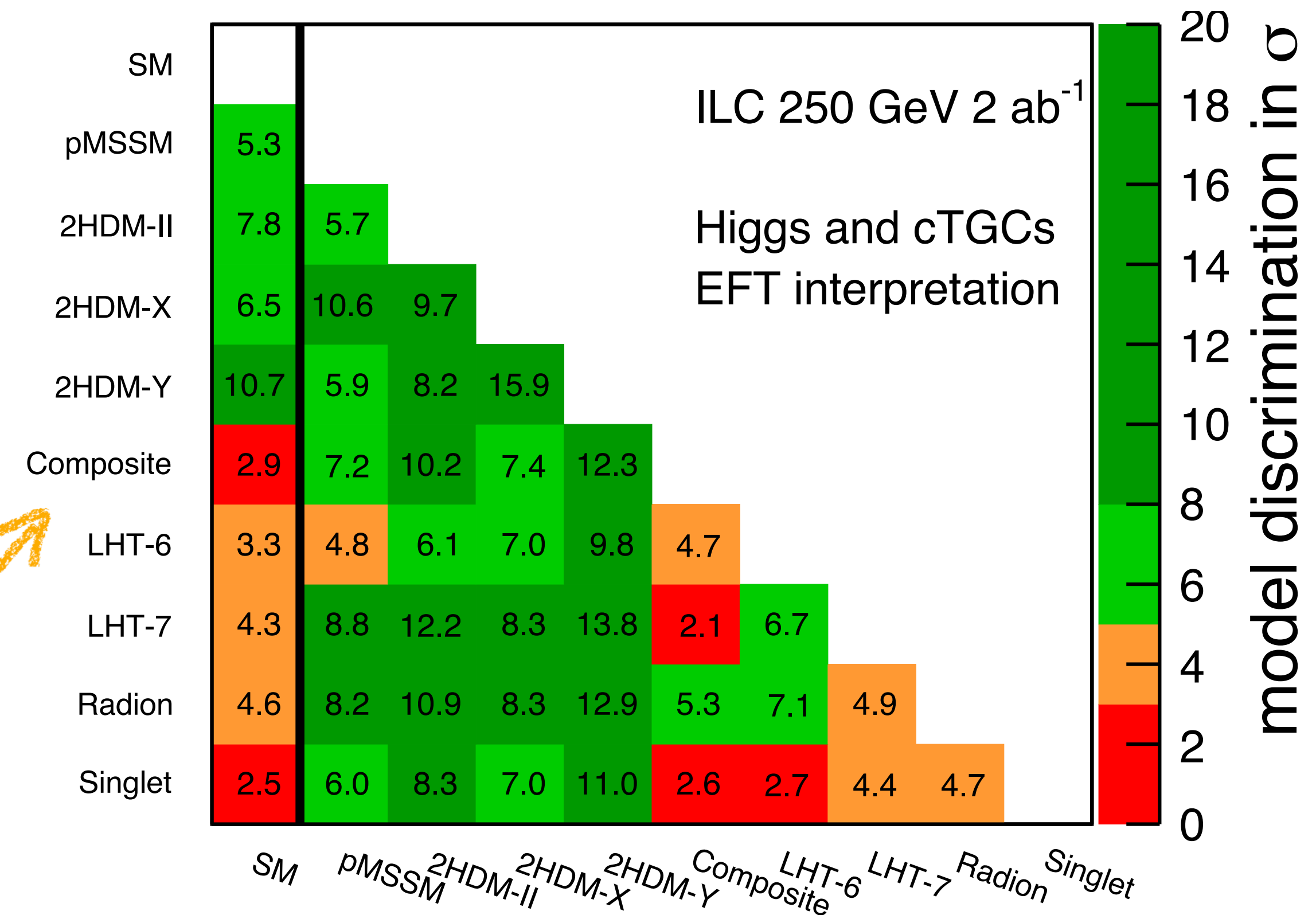
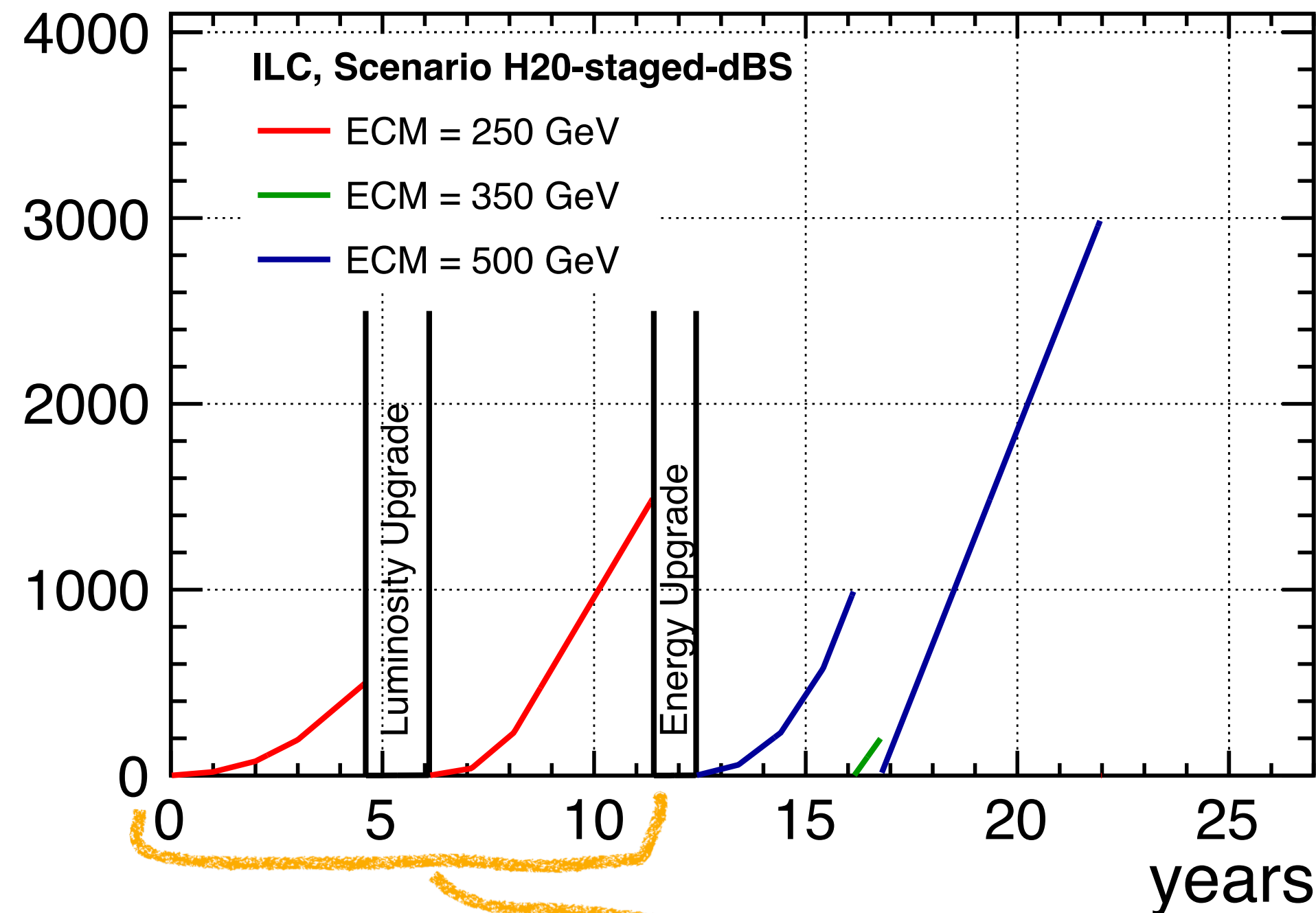


- Precision measurements of couplings may show deviations from the Standard Model
- “Fingerprinting” of deviation pattern reveals underlying mechanisms

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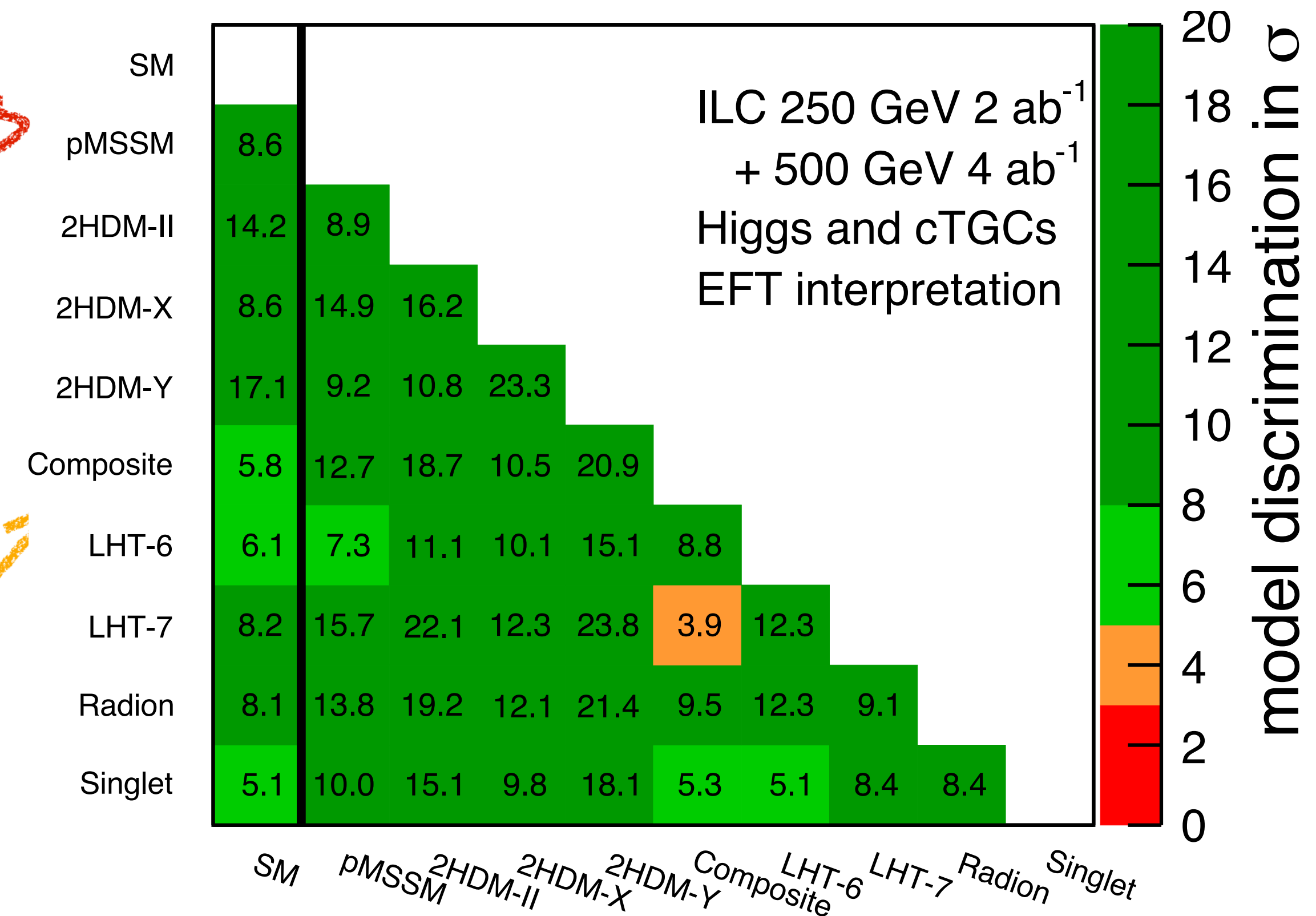
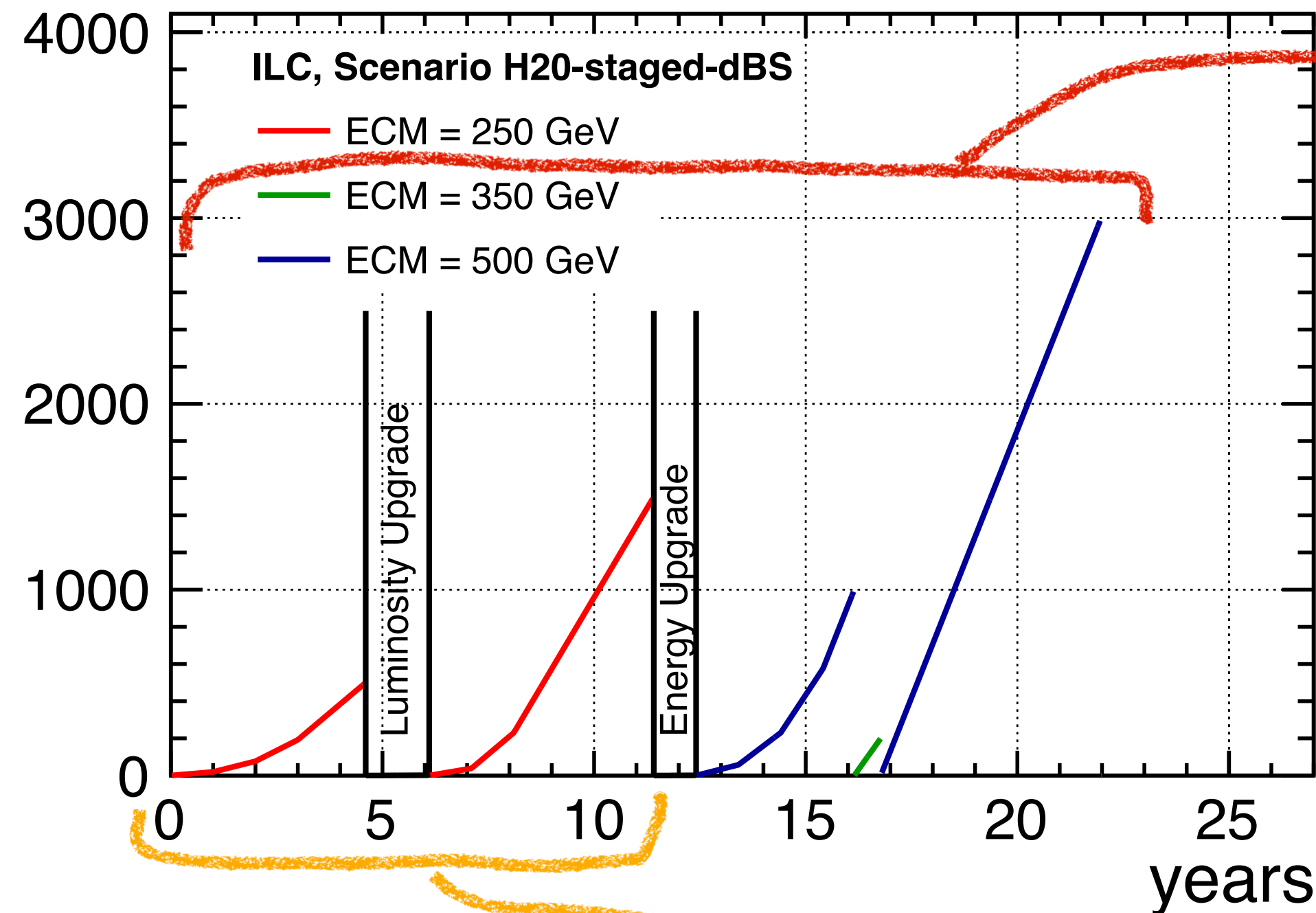
- Discrimination power between models illustrated with EFT fit of ILC projections

arXiv:1708.08912
arXiv:1710.07621

The Relevance of Higgs Coupling Measurements

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Integrated Luminosities [fb^{-1}]



- Precision measurements of couplings may show deviations from the Standard Model
 - “Fingerprinting” of deviation pattern reveals underlying mechanisms

- Discrimination power between models illustrated with EFT fit of ILC projections
 - higher energy may be decisive

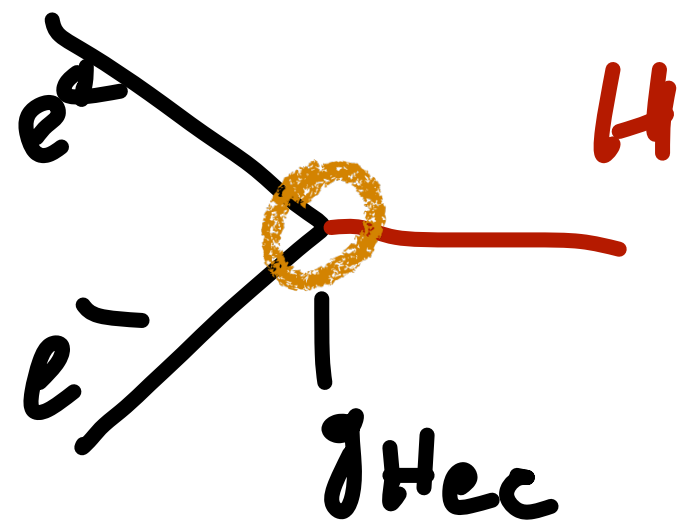
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Accessing the Couplings to First Generation Leptons

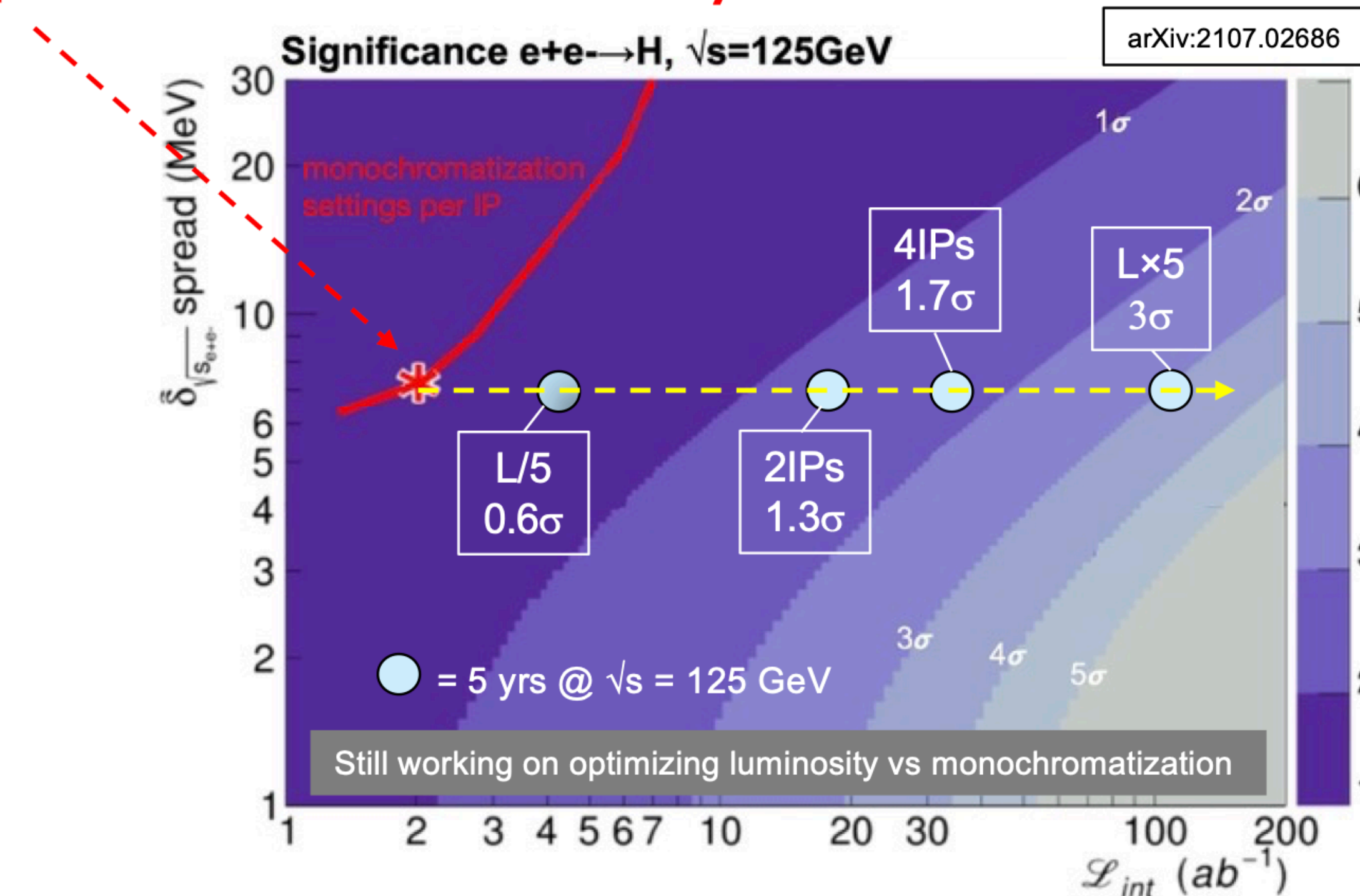
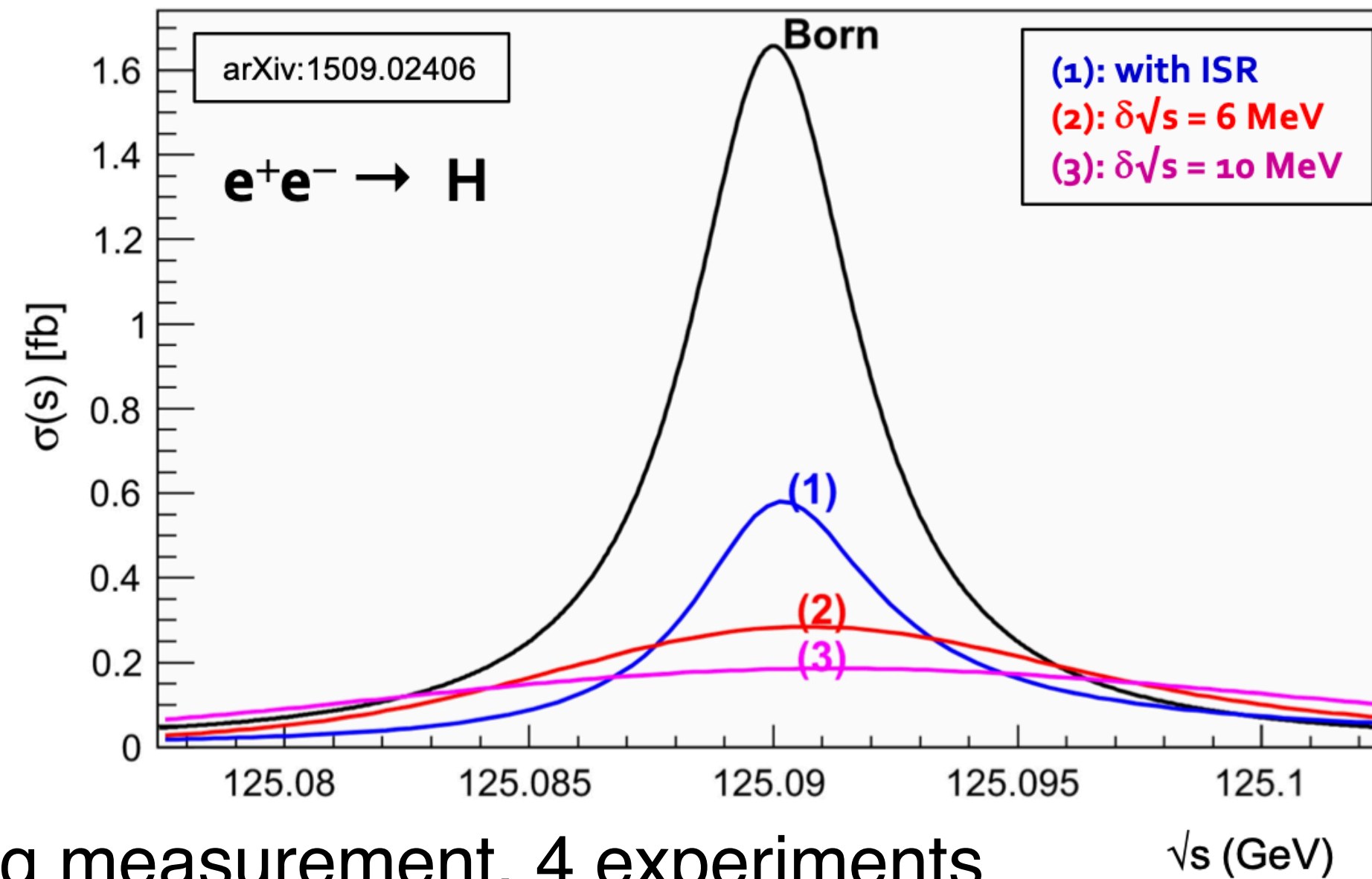
Requiring extreme luminosities of circular colliders

- The only chance to access couplings to first generation: Study of s-channel Higgs production in e^+e^- collisions
- Requires high luminosities and very small energy spread at 125.1 GeV

Requires special monochromatization to



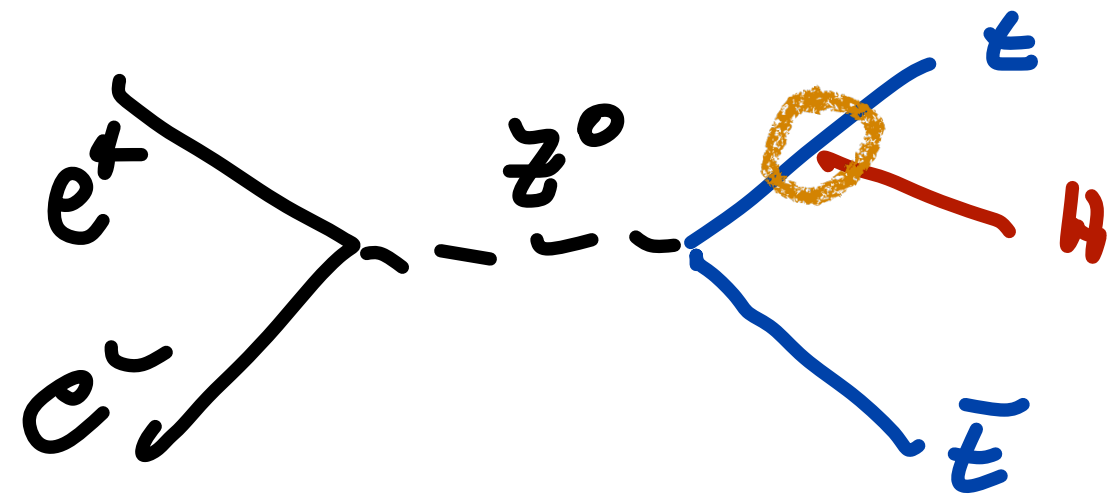
□ **First studies indicate a significance of 0.4σ with one detector in one year**



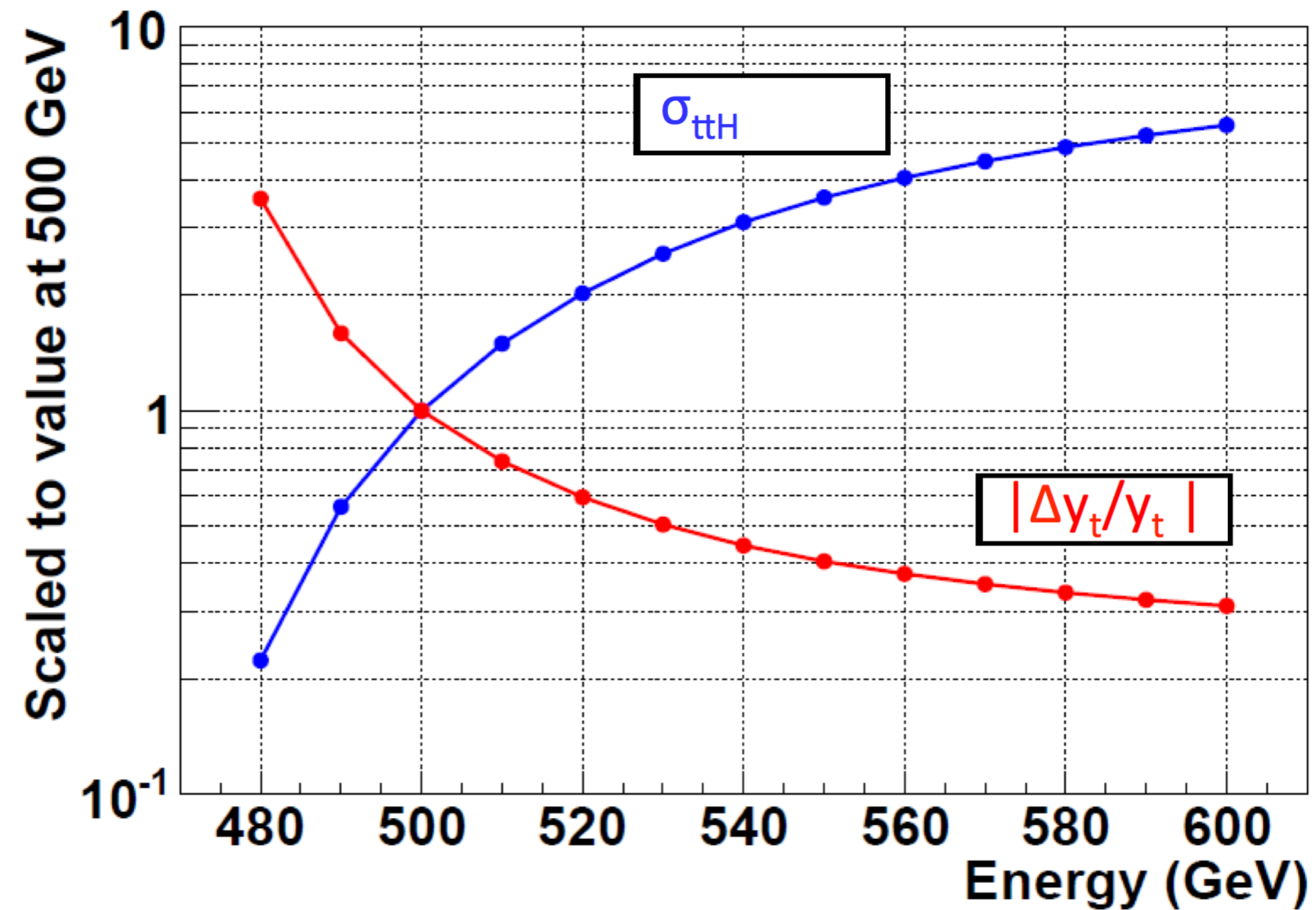
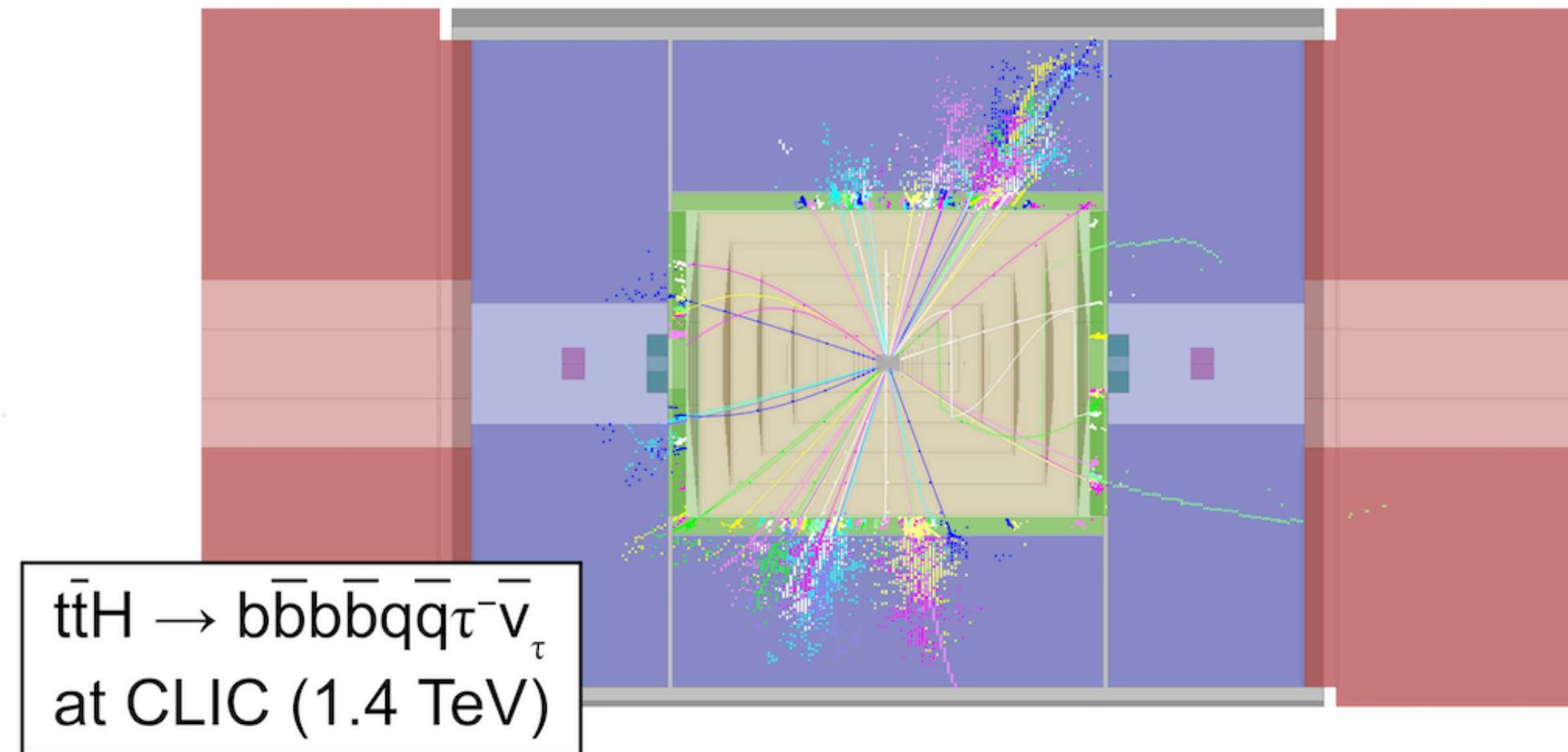
⇒ A very challenging measurement, 4 experiments and 3 years may reach a result

Directly measuring the Coupling to the Top Quark

A higher-energy exclusive



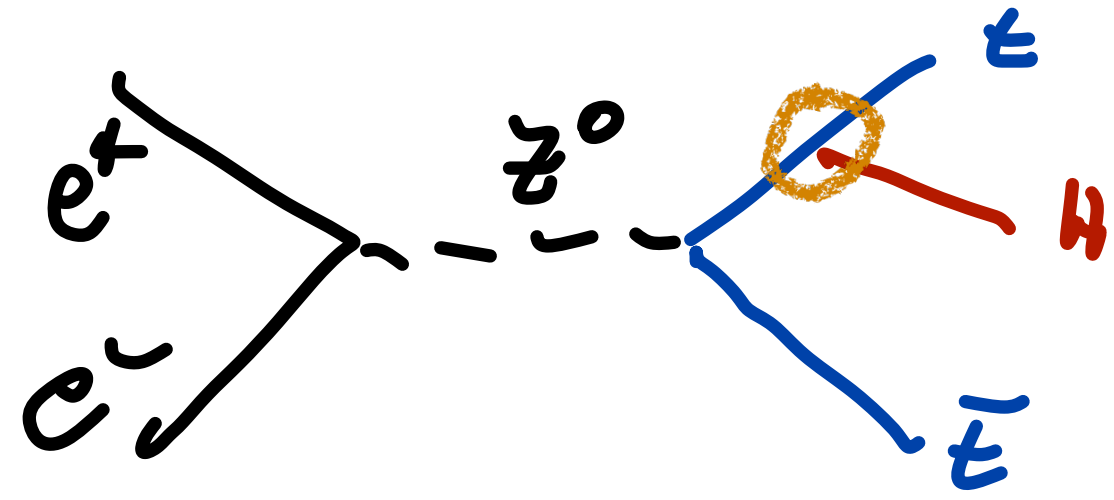
- Direct access to the top Yukawa coupling provided by ttH final state: requires energy ≥ 500 GeV (ideal ~ 550 GeV - 1.5 TeV)



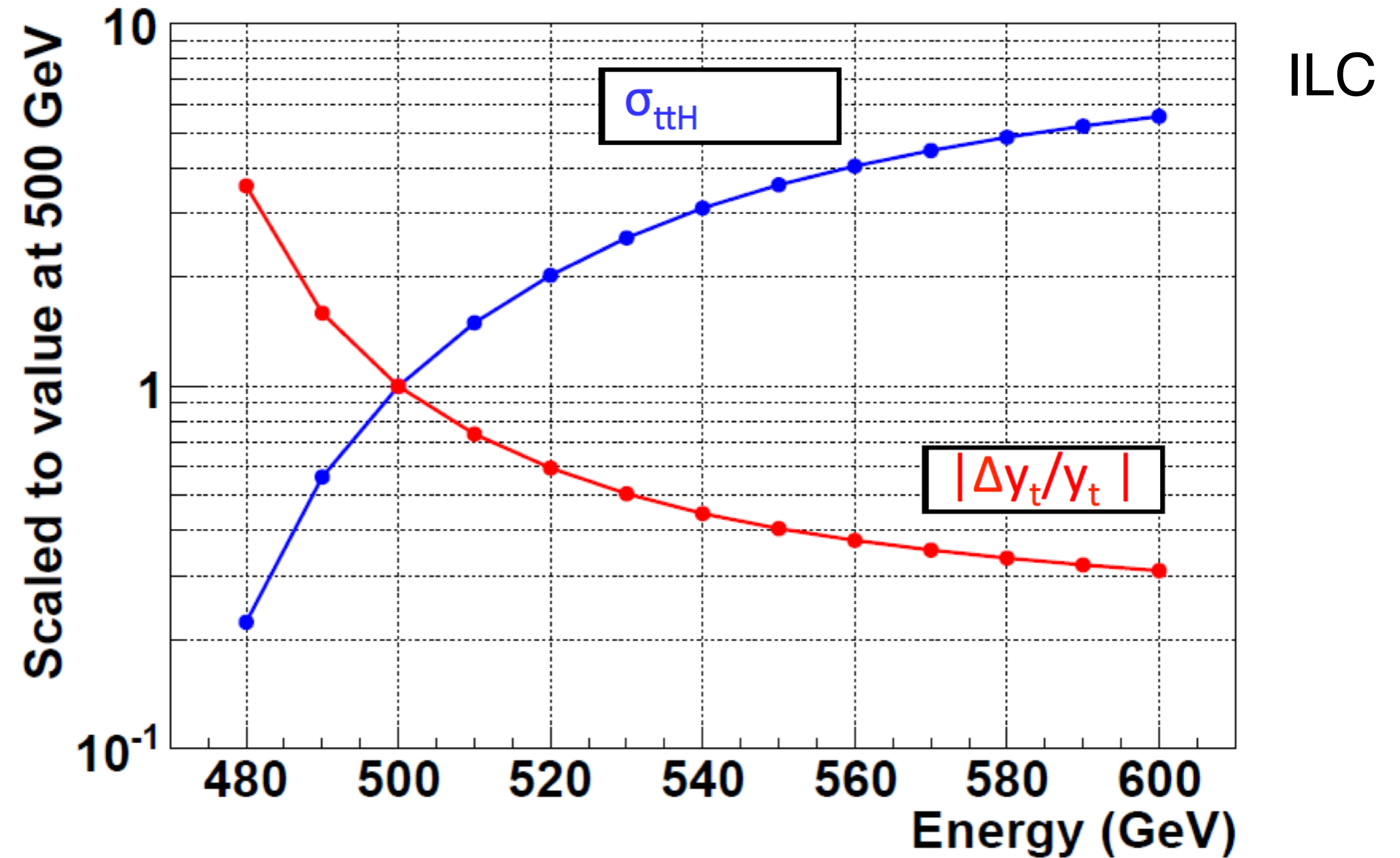
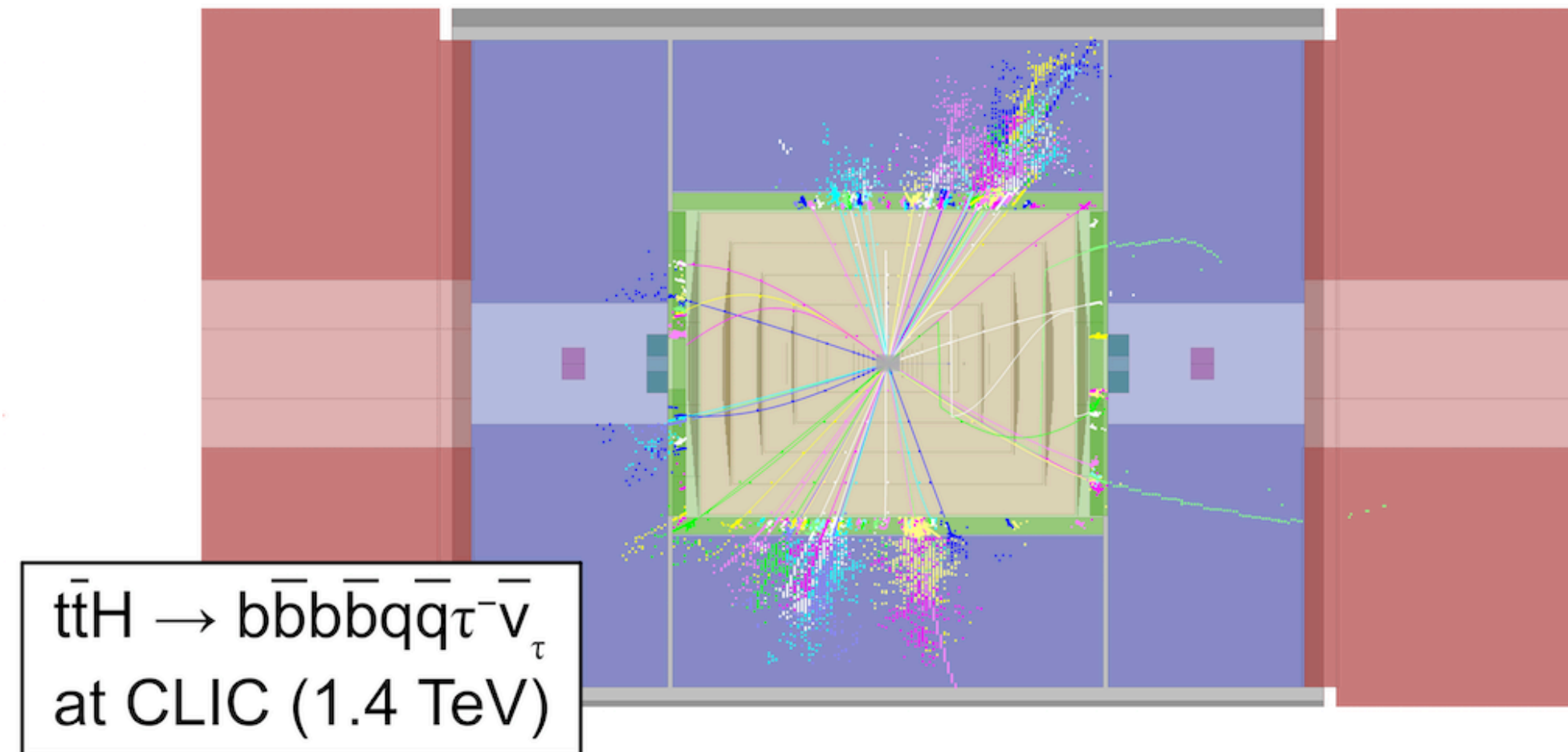
ILC

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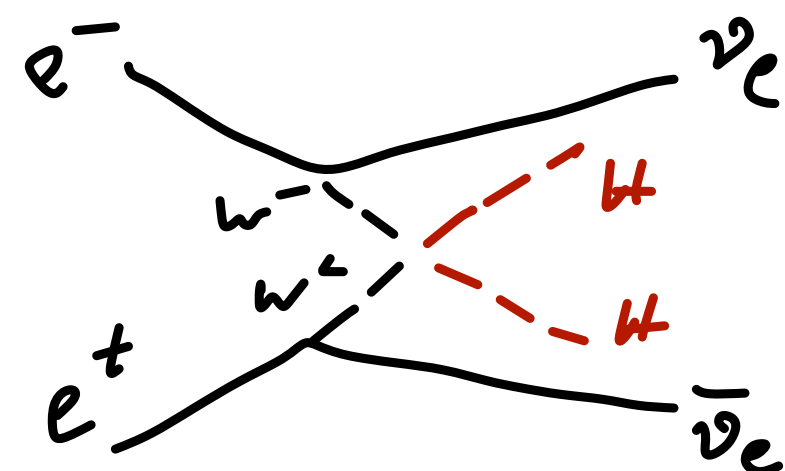
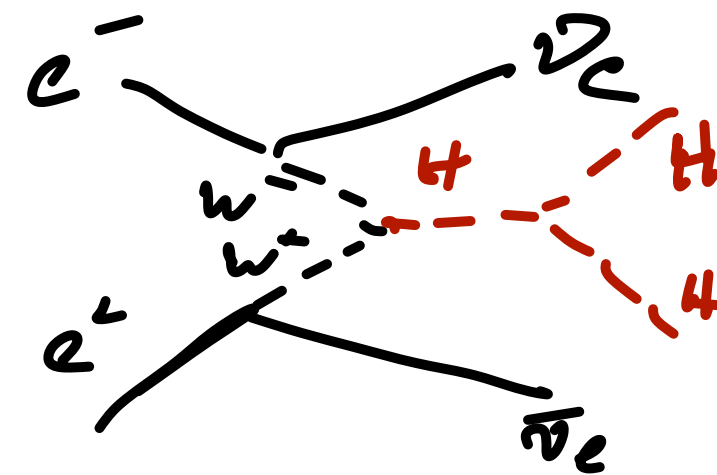
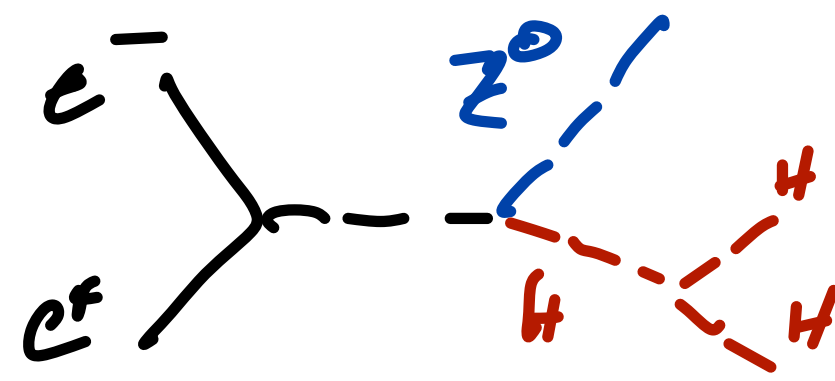
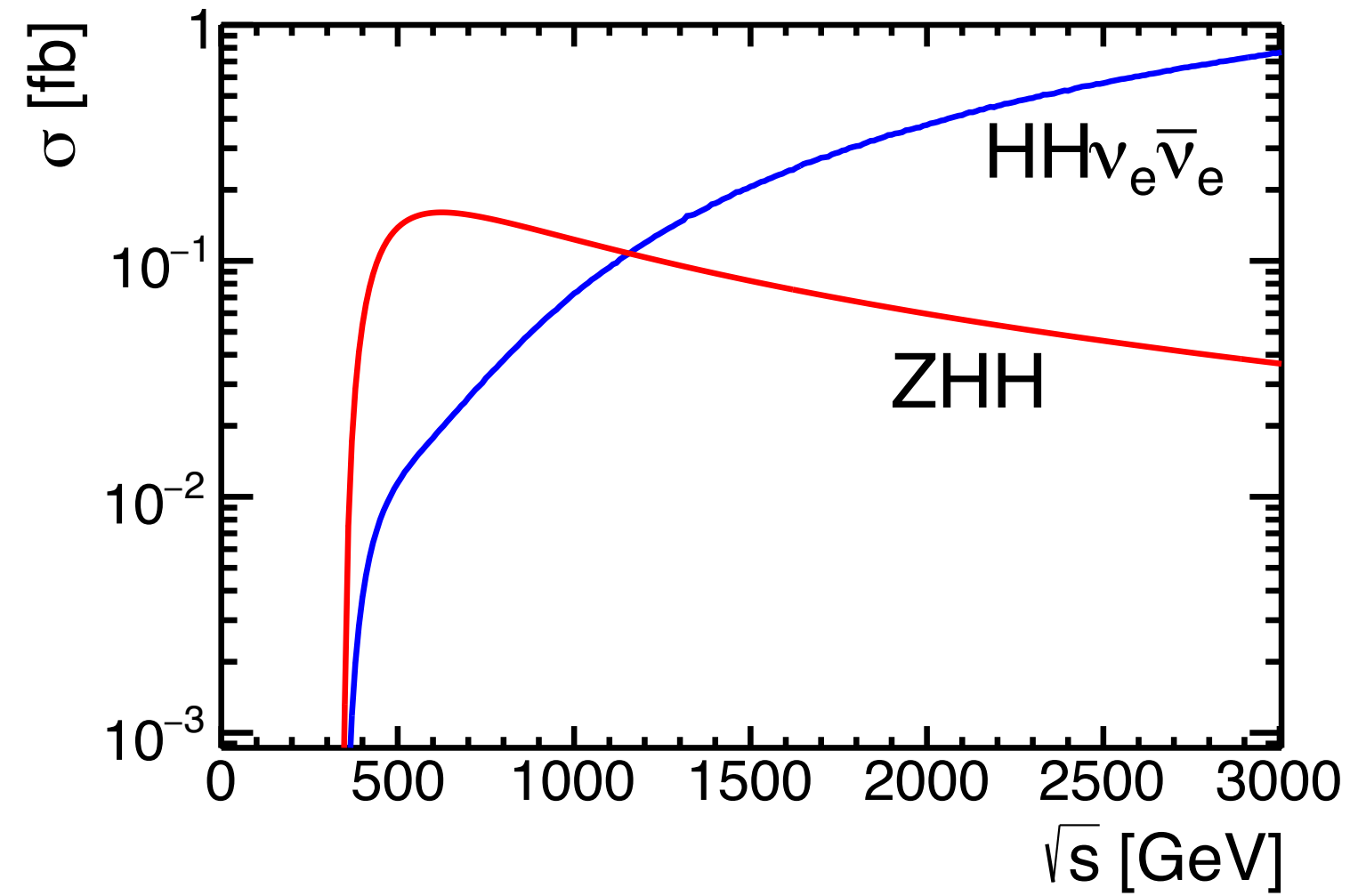
ILC: $\Delta g_{ttH}/g_{ttH} \sim 6.3\%$ with 4 ab^{-1} @ 500 GeV
 would be $\sim 3\%$ @ 550 GeV
 (and $\sim 13\%$ @ 485 GeV: achieving design energy critical!)

CLIC: $\Delta g_{ttH}/g_{ttH} \sim 2.9\%$ with 2.5 ab^{-1} @ 1.4 TeV

The Higgs Self-Coupling

Requires higher energy - one of the key challenges of HEP

- Two processes with sensitivity at e^+e^- colliders:

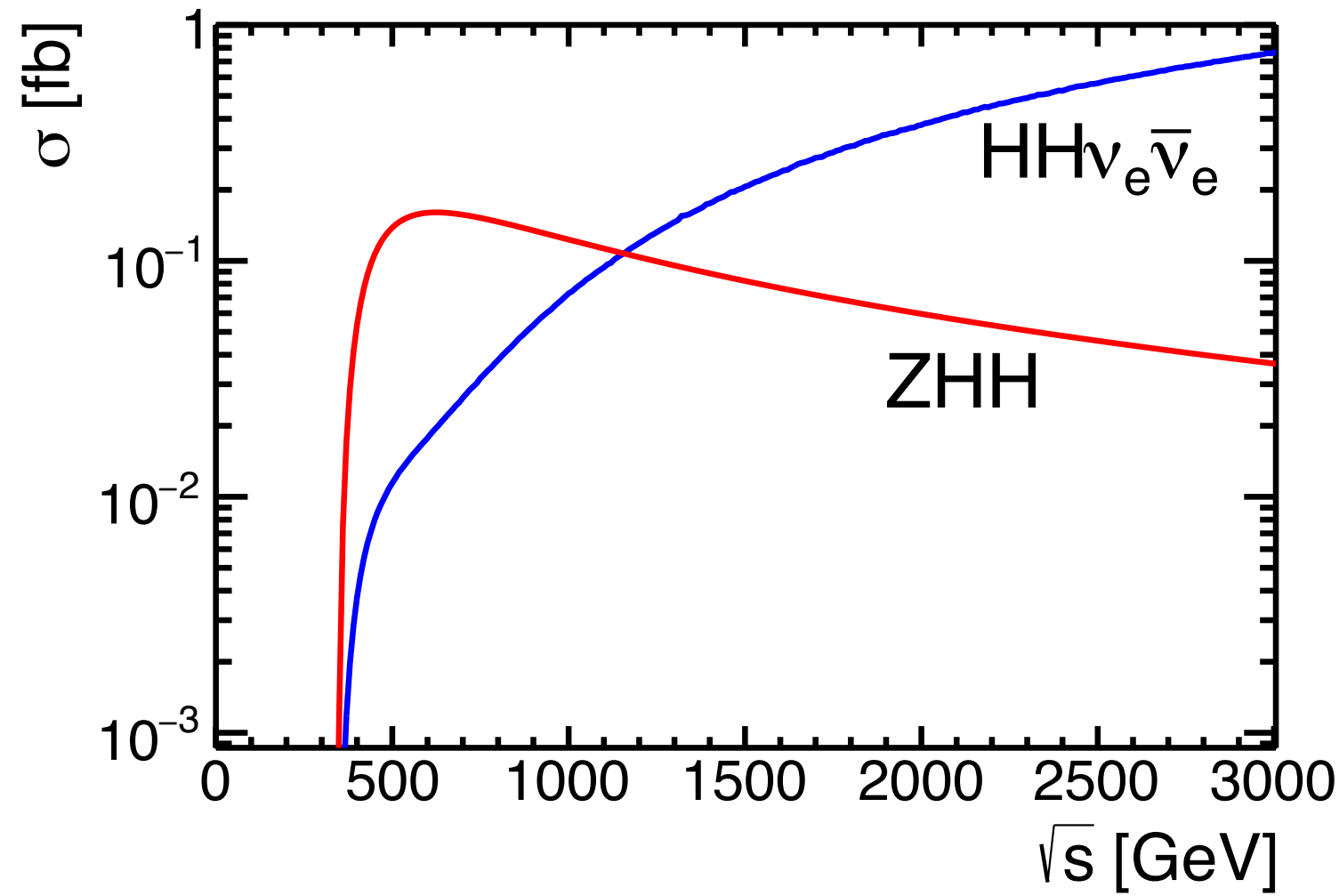


the final state also receives contributions from the quartic coupling

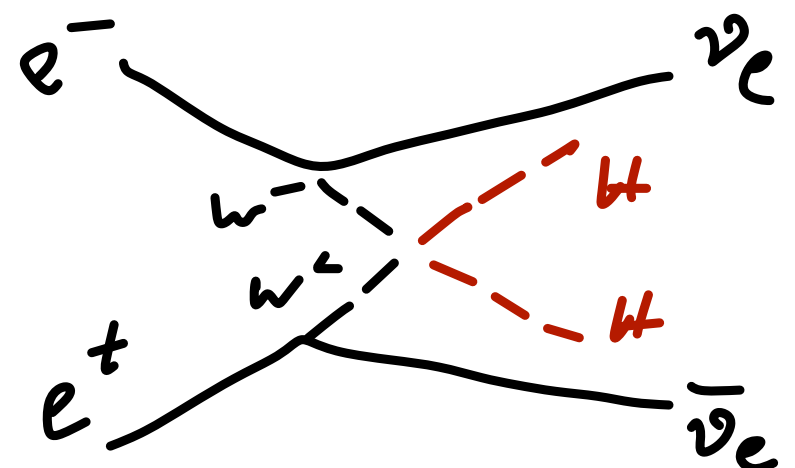
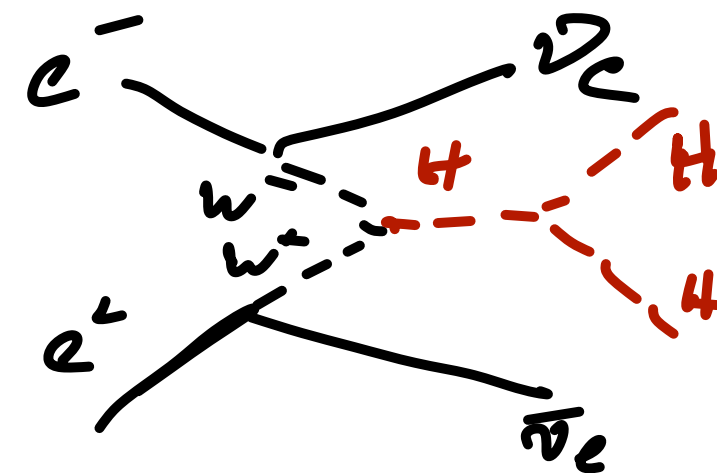
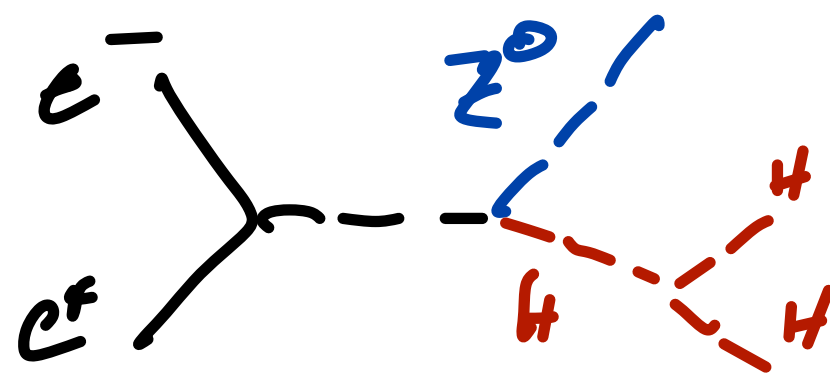
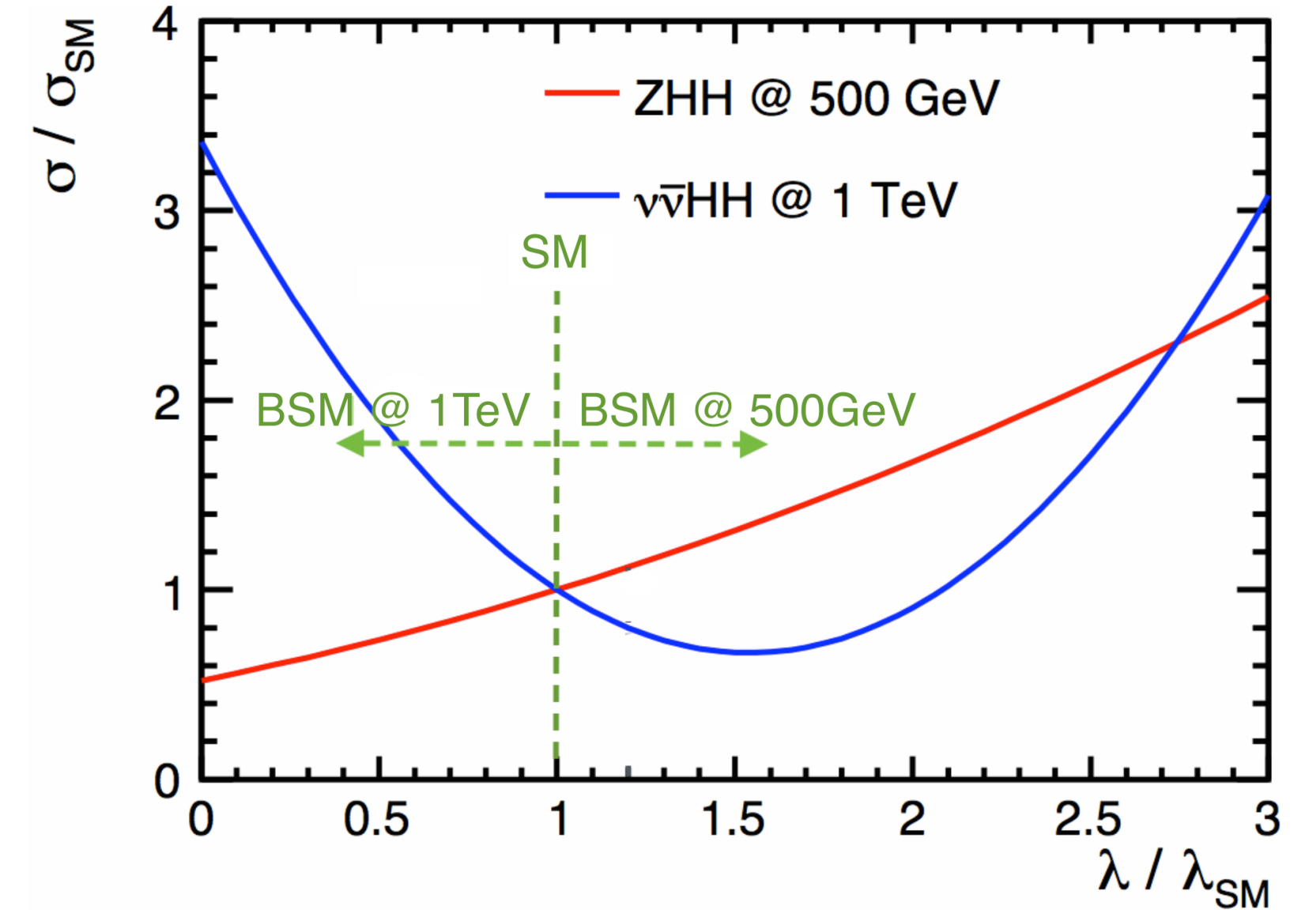
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cross section depends non-linearly on λ , measurements at different energies / of different processes lift degeneracies

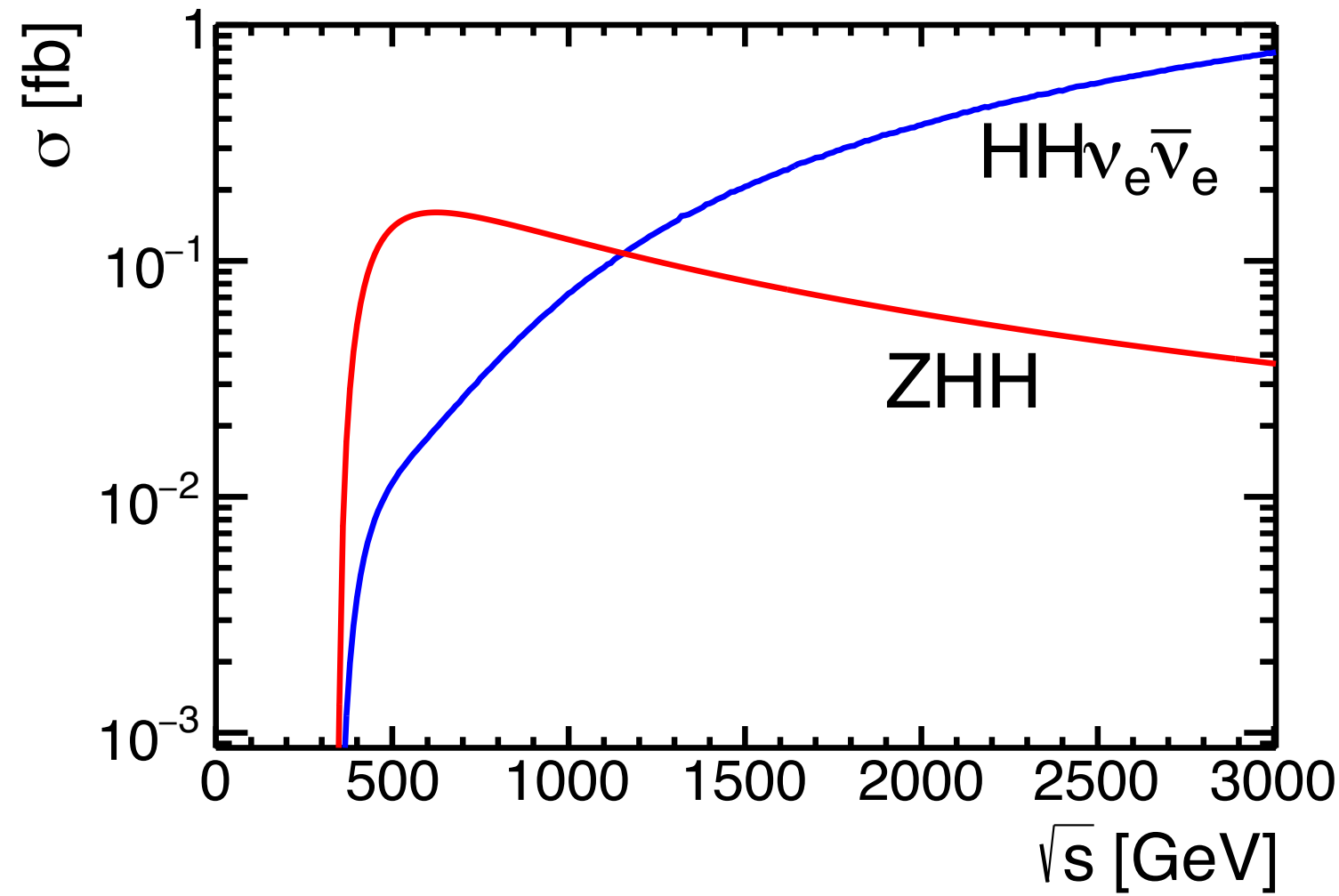


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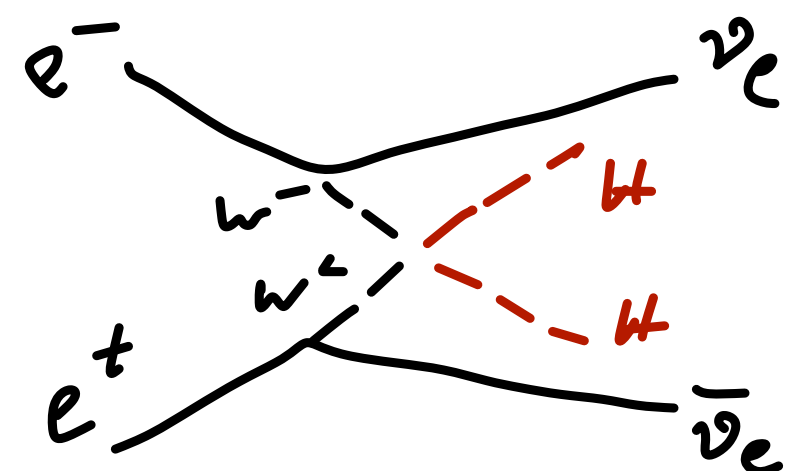
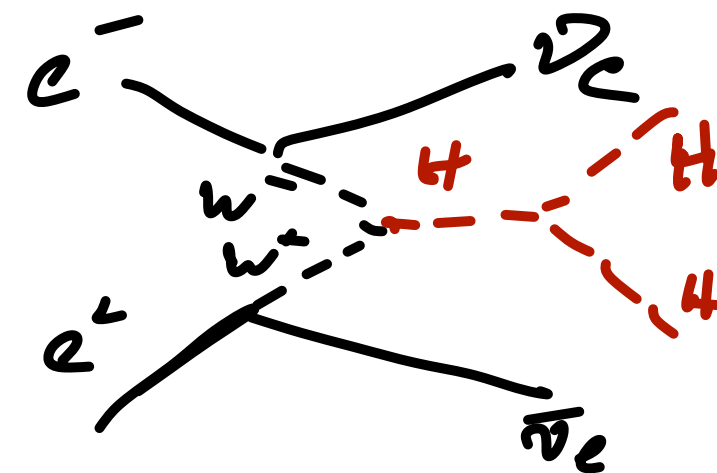
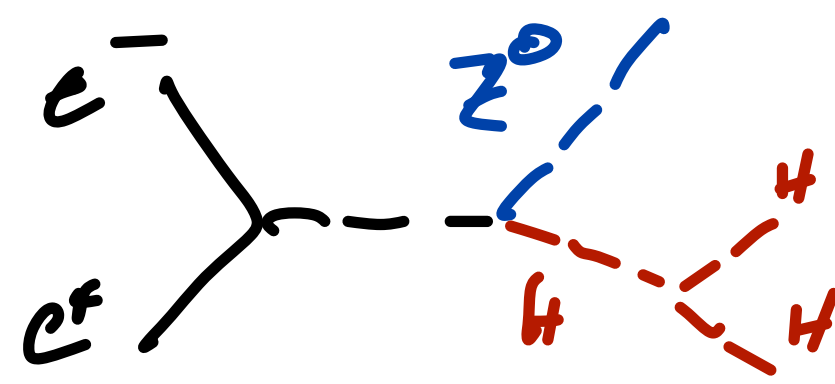
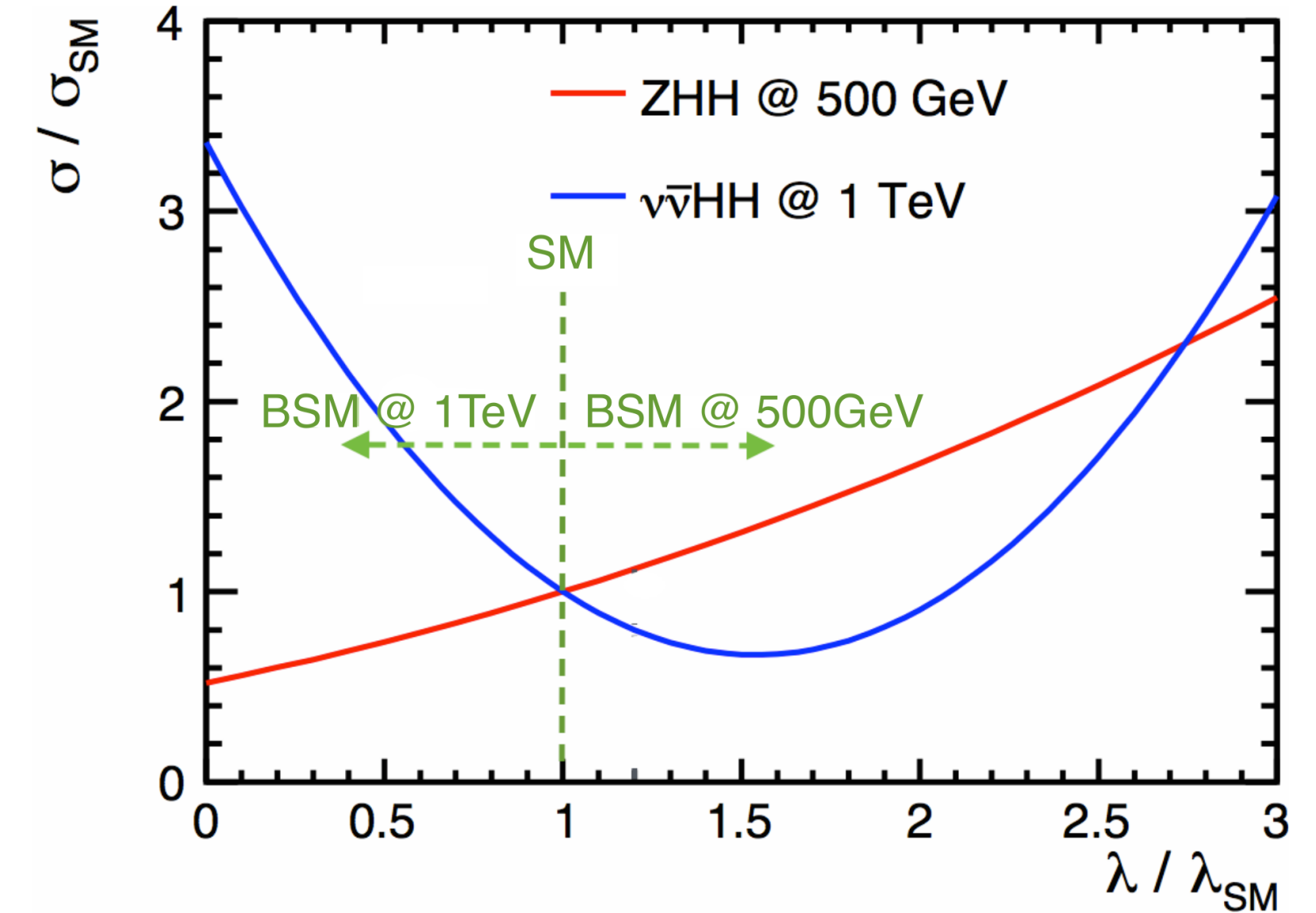
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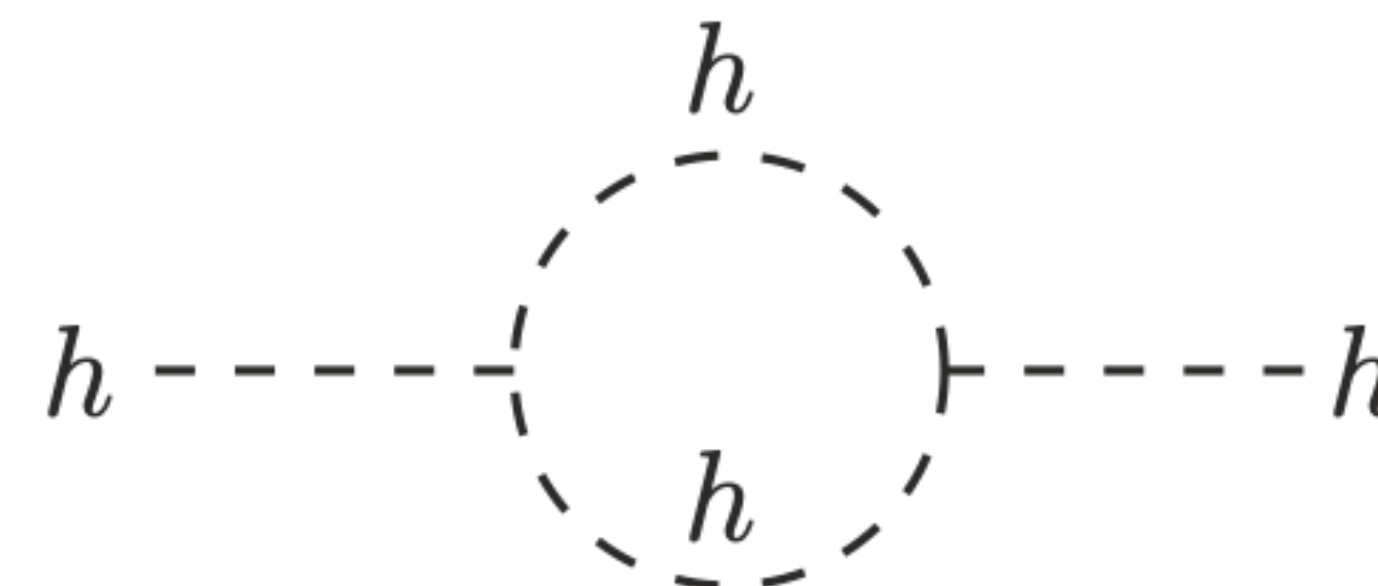
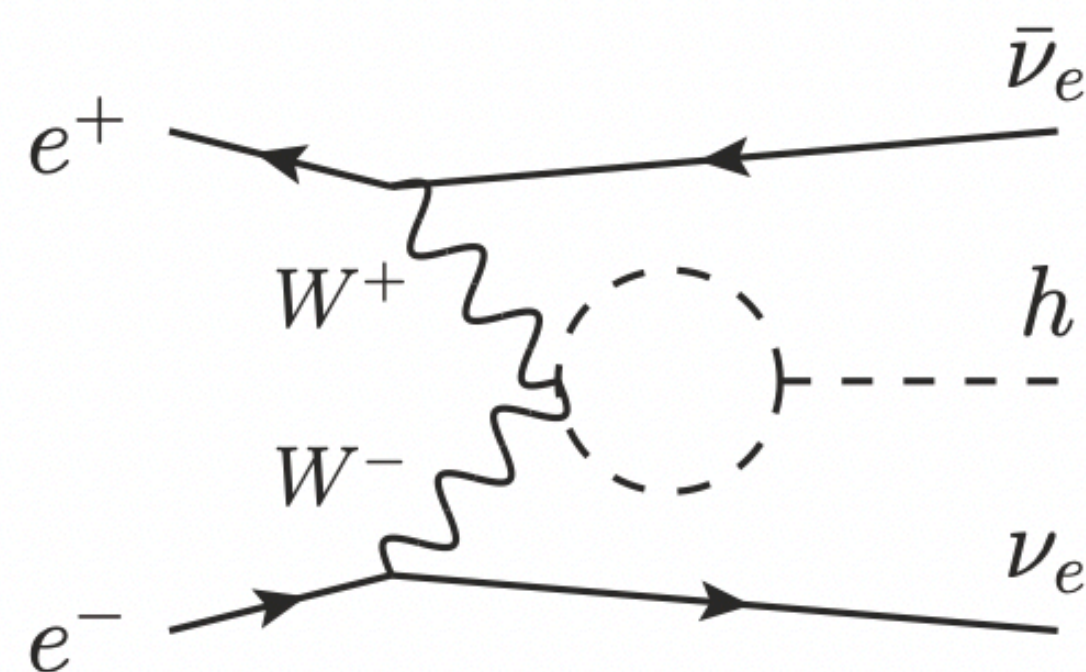
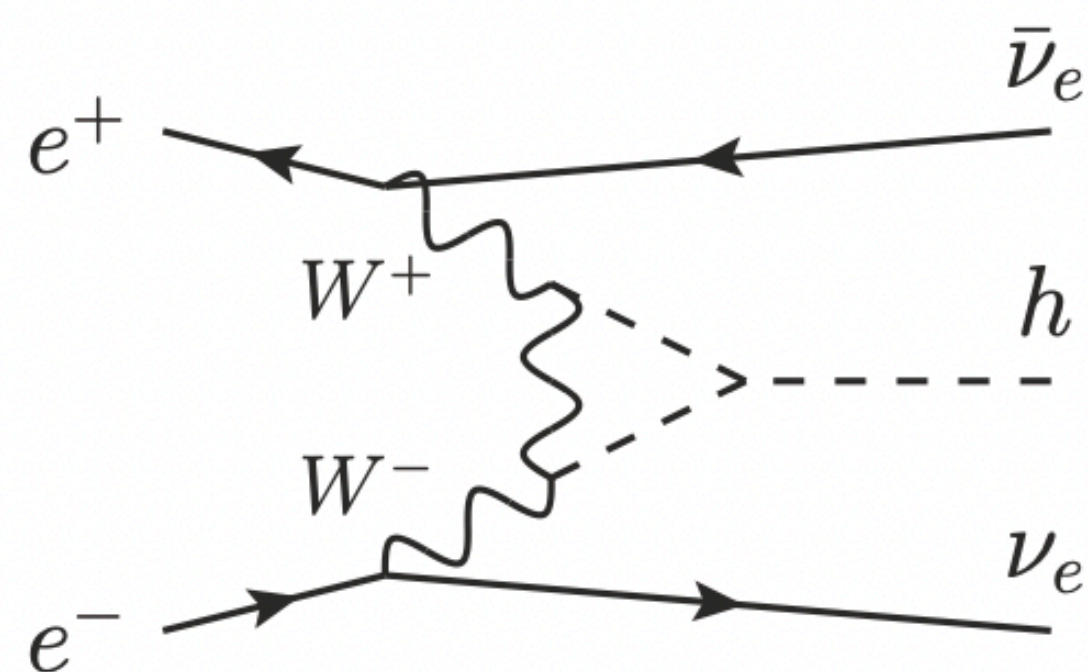
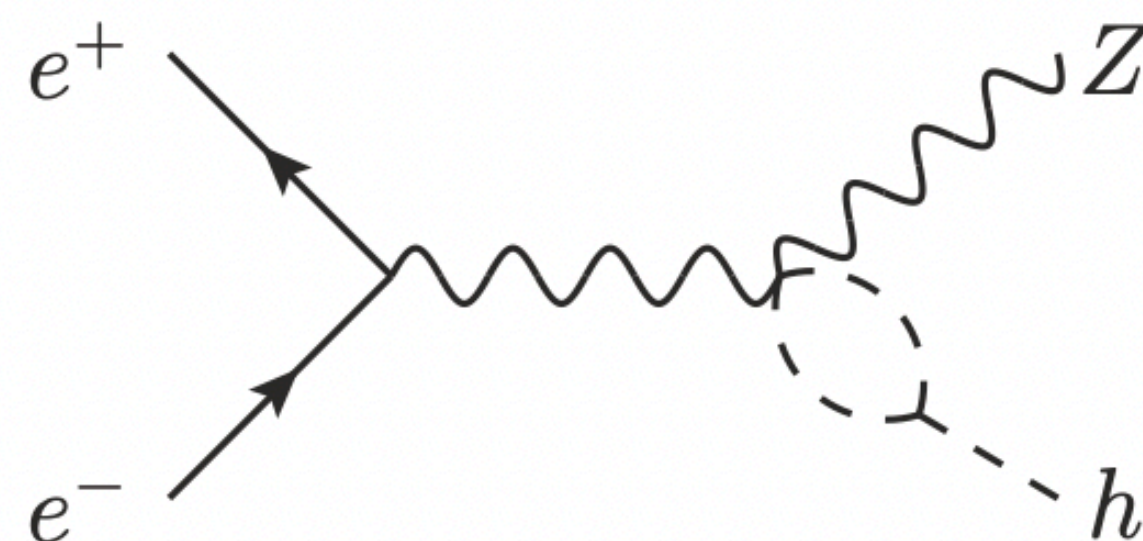
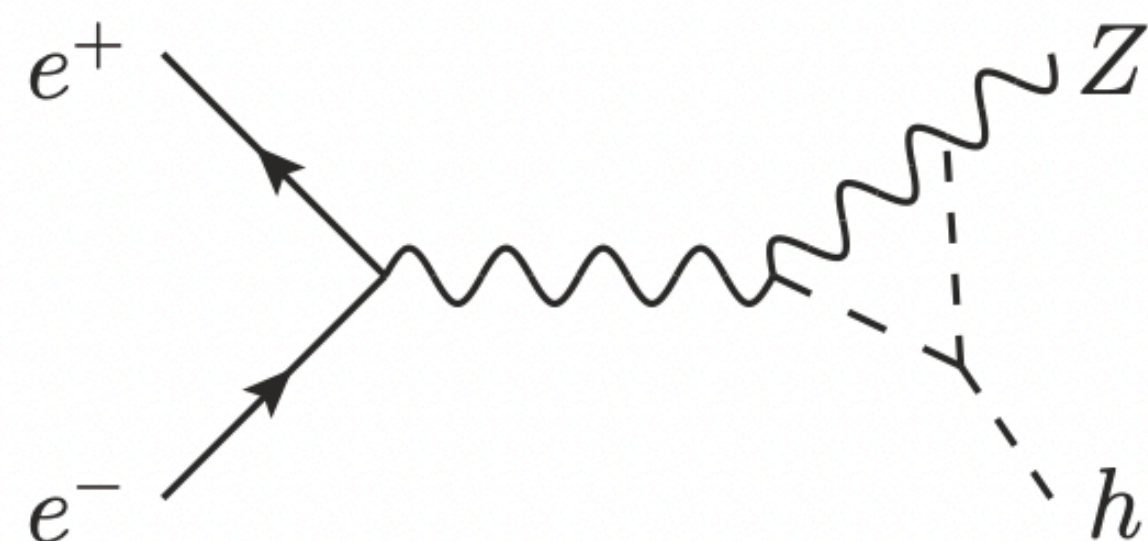
Full potential unfolds in the multi-TeV region through growing σ of VBF process:

- ⇒ 10% measurement feasible
- ⇒ Significant observation also of ZHH channel in lower-energy running (up to ~ 1.5 TeV)

Indirect Measurement of the Self Coupling

Accessible via particle loops

- The self-coupling also influences single Higgs production:



Model-dependent: assumptions required for interpretation!

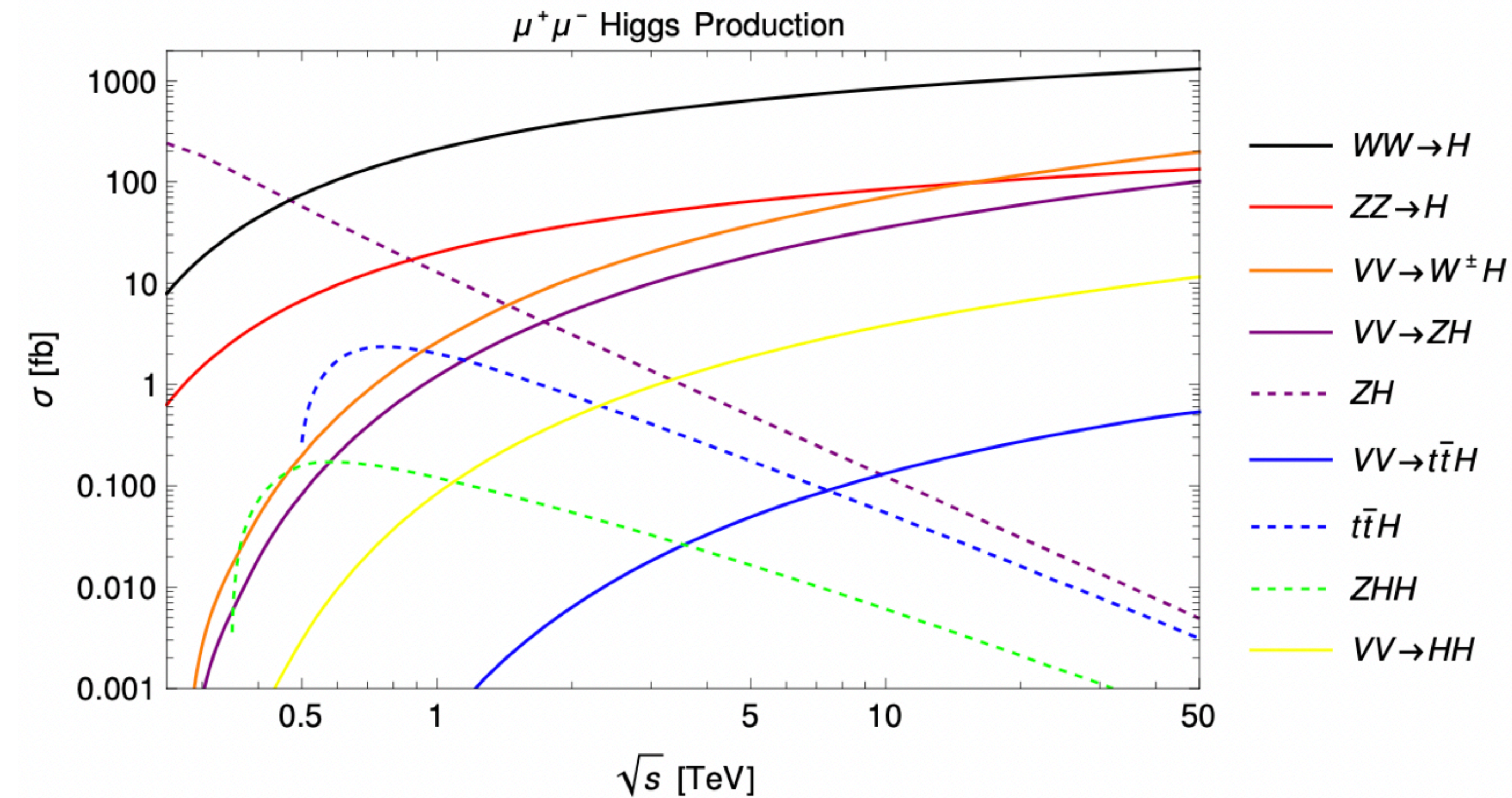
Overall precision limited, $\sim 33\%$ at FCC-ee combined with HL-LHC (which provides $\sim 50\%$)

Interplay of different energies key. With optimised running, and increased L_{int} at 240 GeV and 365 GeV 20% may be doable.

Higgs Physics at Muon Colliders

Brief overview

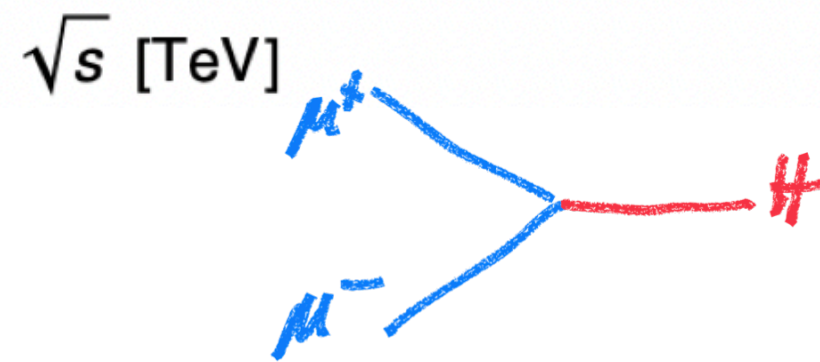
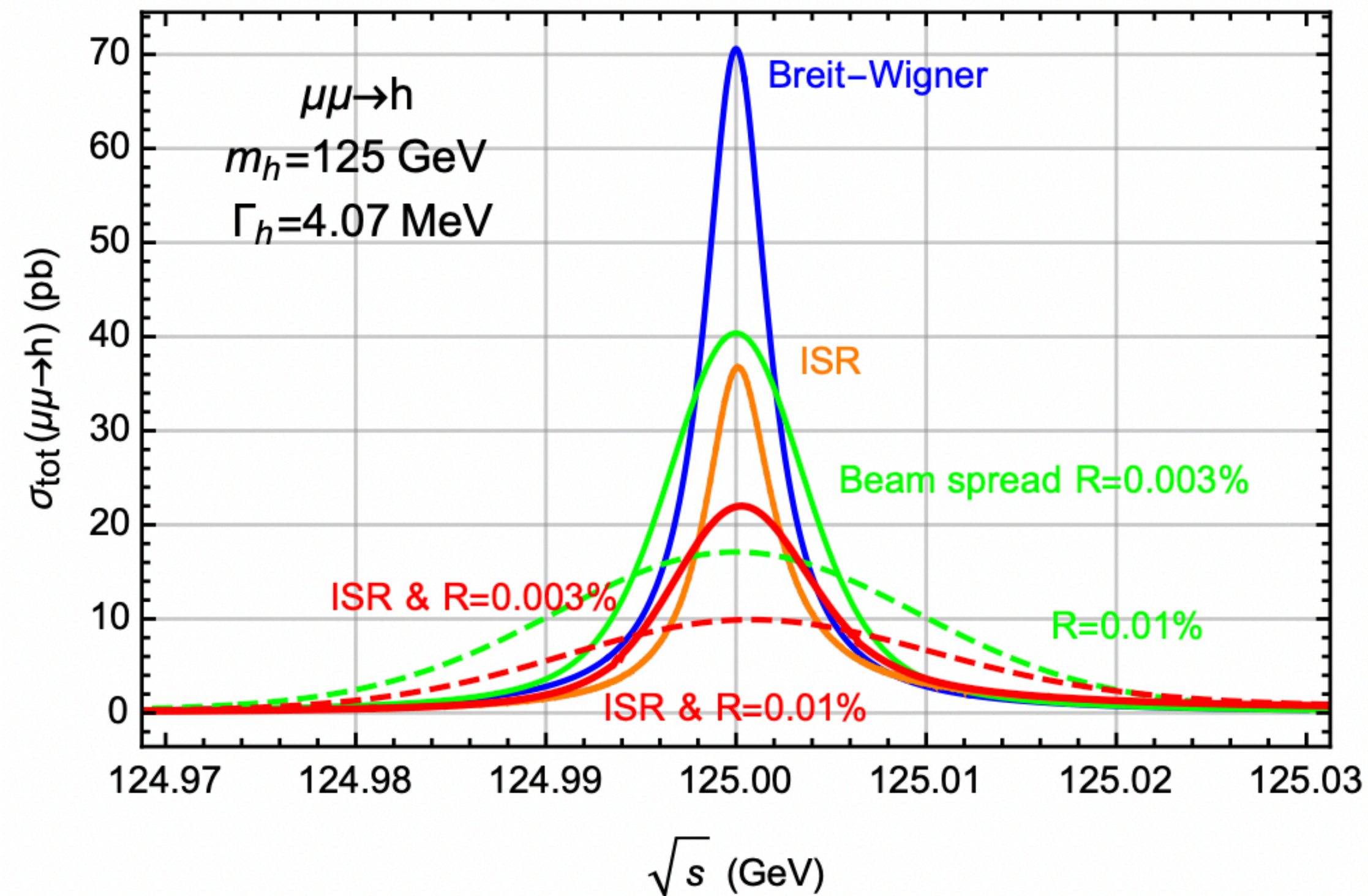
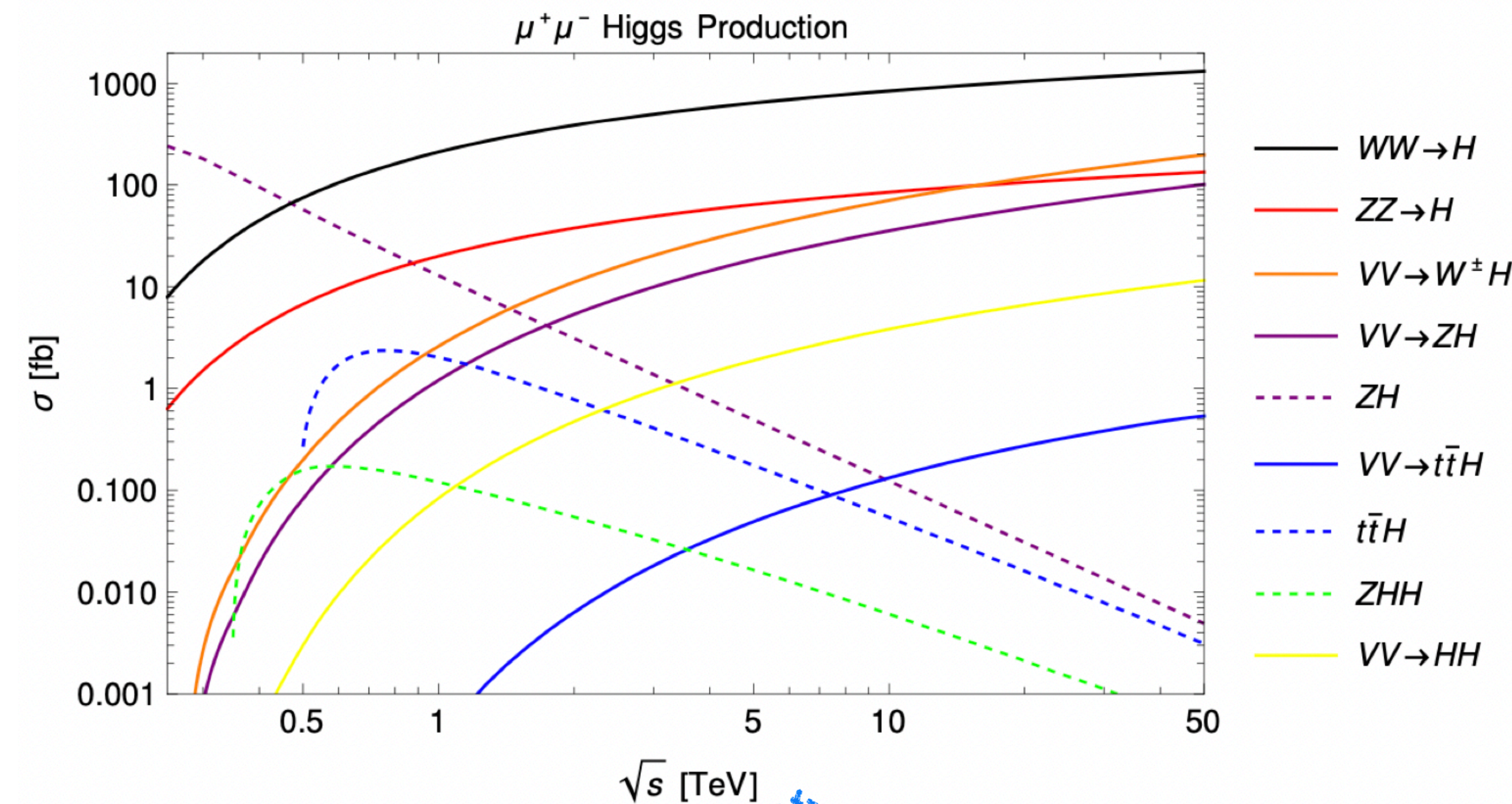
- In general the same processes as for e^+e^- , but with the backdrop of a much larger background, and reduced acceptance at small angles (which has an impact on WW fusion processes in particular). Here (much) higher energy can compensate!



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s-channel production at 125 GeV:

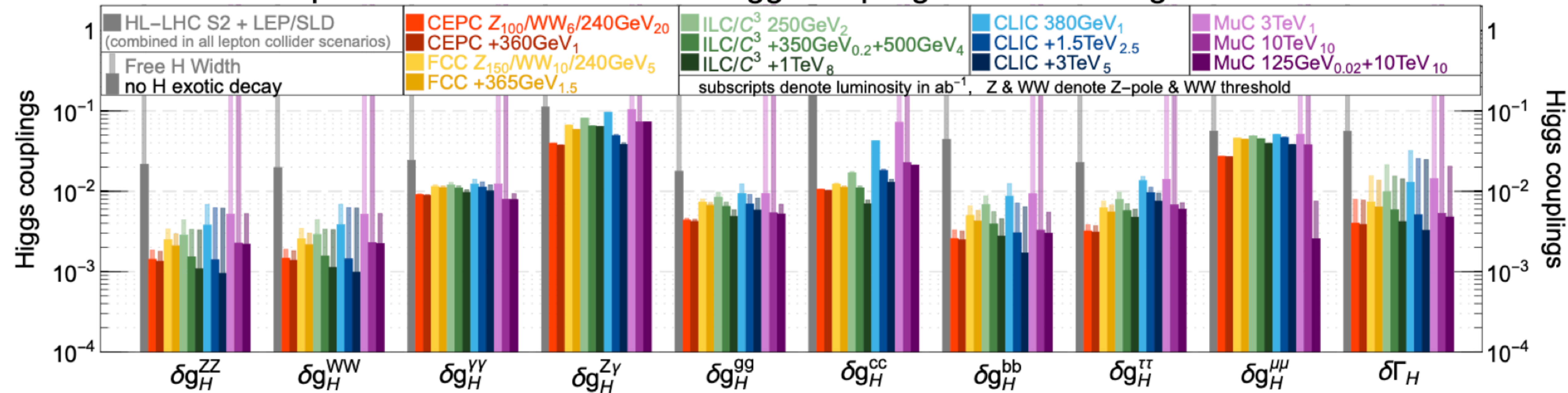
Cross section $\sim 10^5 \times e^+e^-$: Coupling, + reduced ISR smearing for μ

Overall Precision Perspective

Including muon colliders

- An EFT fit, performed for Snowmass

precision reach on effective Higgs couplings from SMEFT global fit

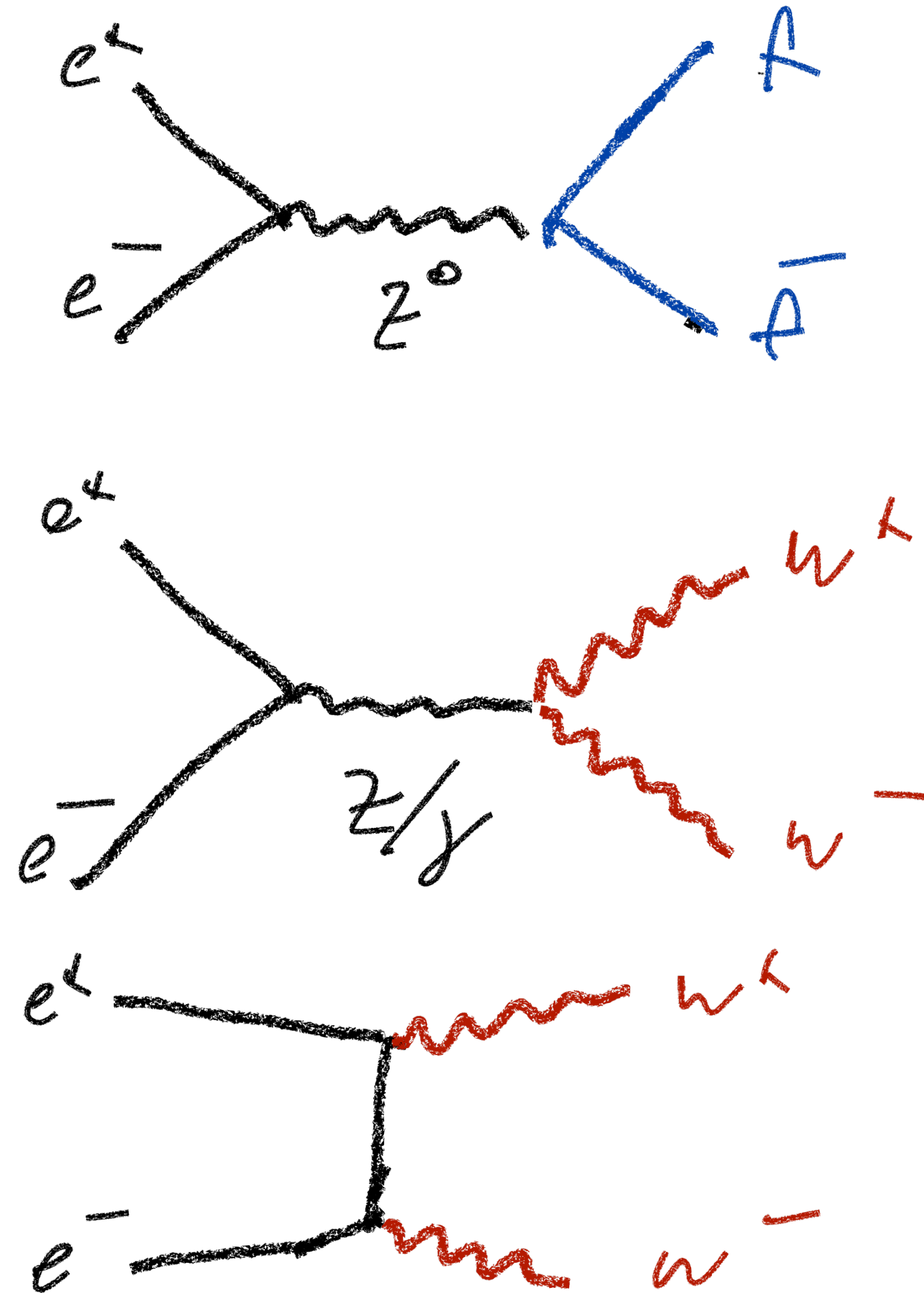


Electroweak Precision

A Playground for Circular Colliders

The FCC-ee Program at Z and WW

The ultimate electroweak program



- Building on the success of LEP & LEP II
- High-statistics program at the Z - pole
- W pair production - mass measurement and beyond

with 2 IPs:

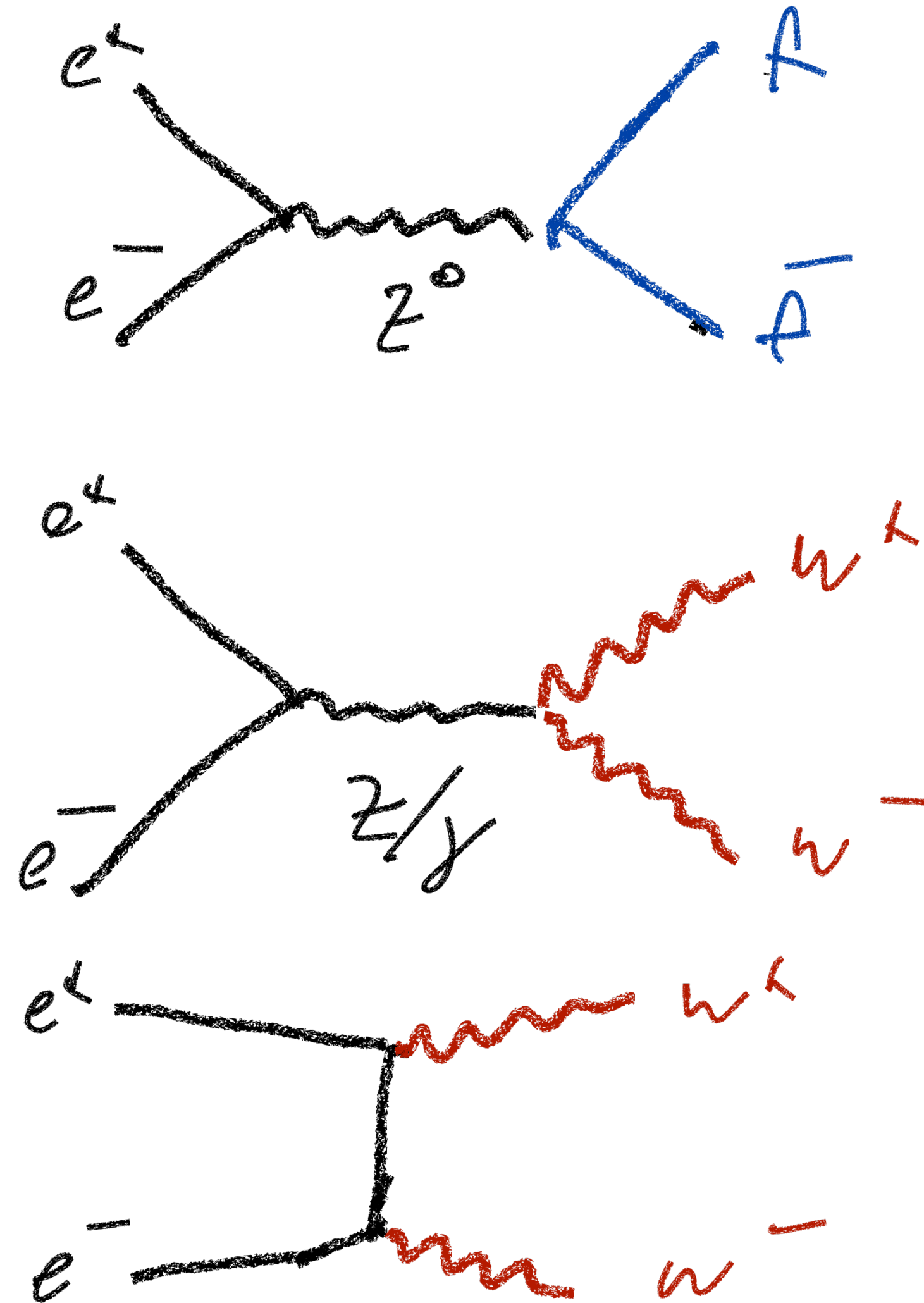
5×10^{12} Zs ($10^5 \times$ LEP)

10^8 W pairs ($2 \times 10^3 \times$ LEP)

N.B.: Measurements also possible at linear colliders, but the statistics will be orders of magnitude smaller due to their lower luminosity at low energy.

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⇒ Improving electroweak precision observables, enter into global fits

⇒ Indirect searches for New Physics

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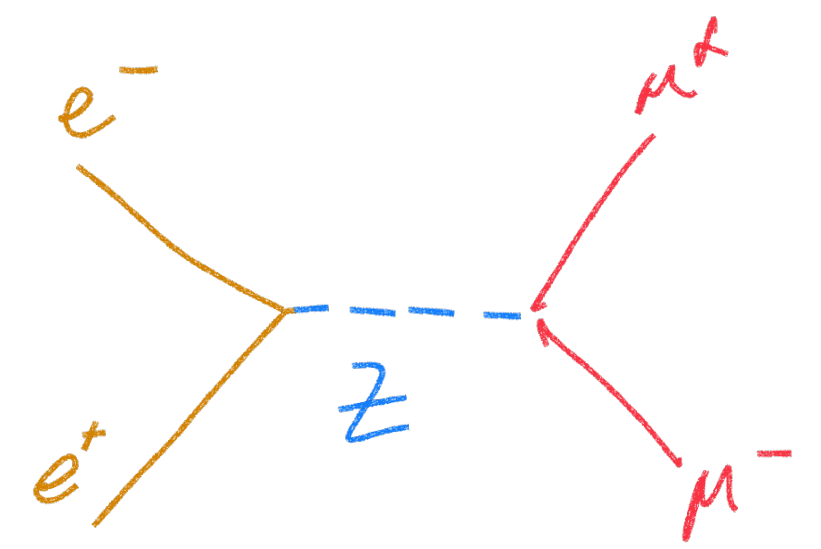
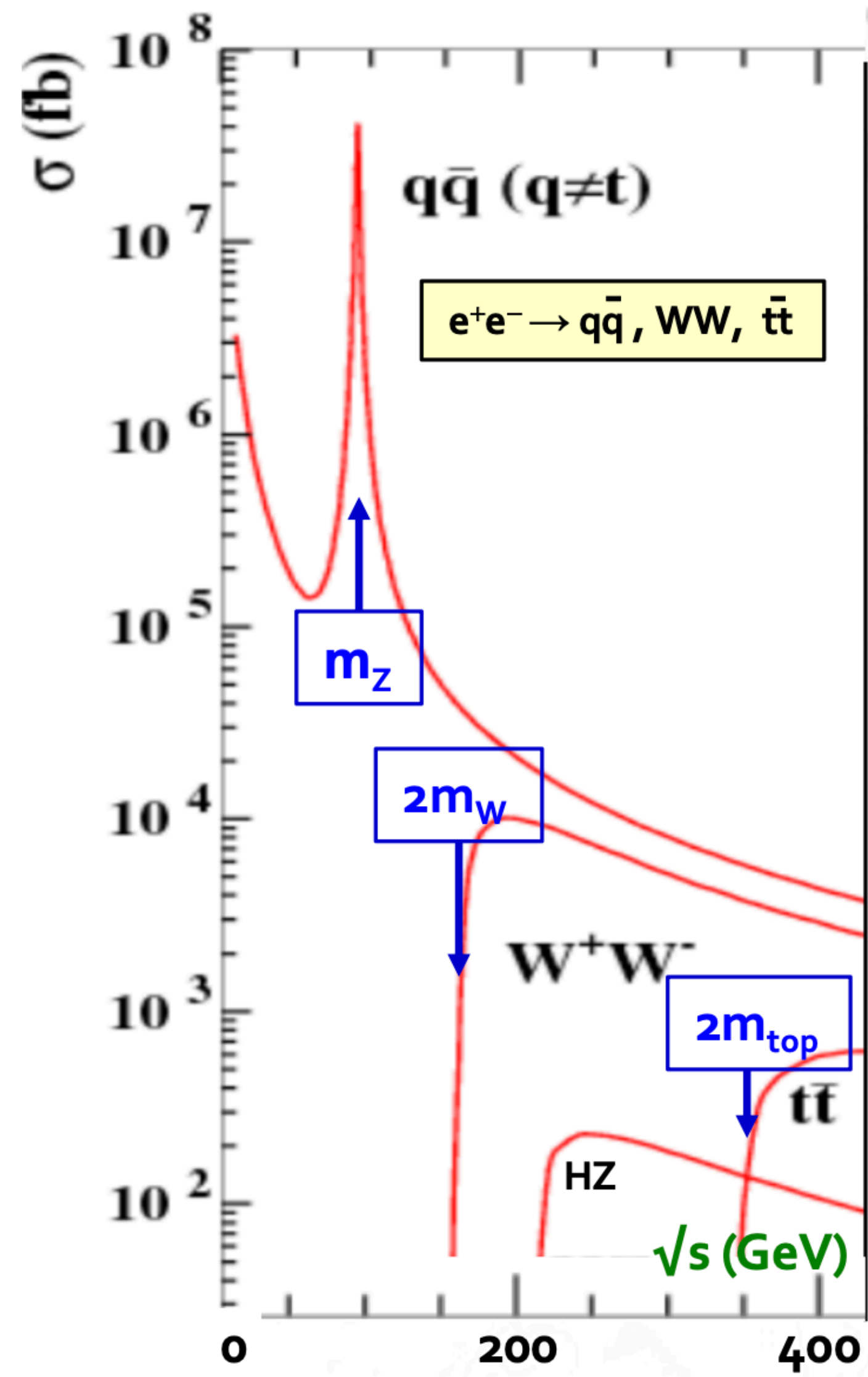
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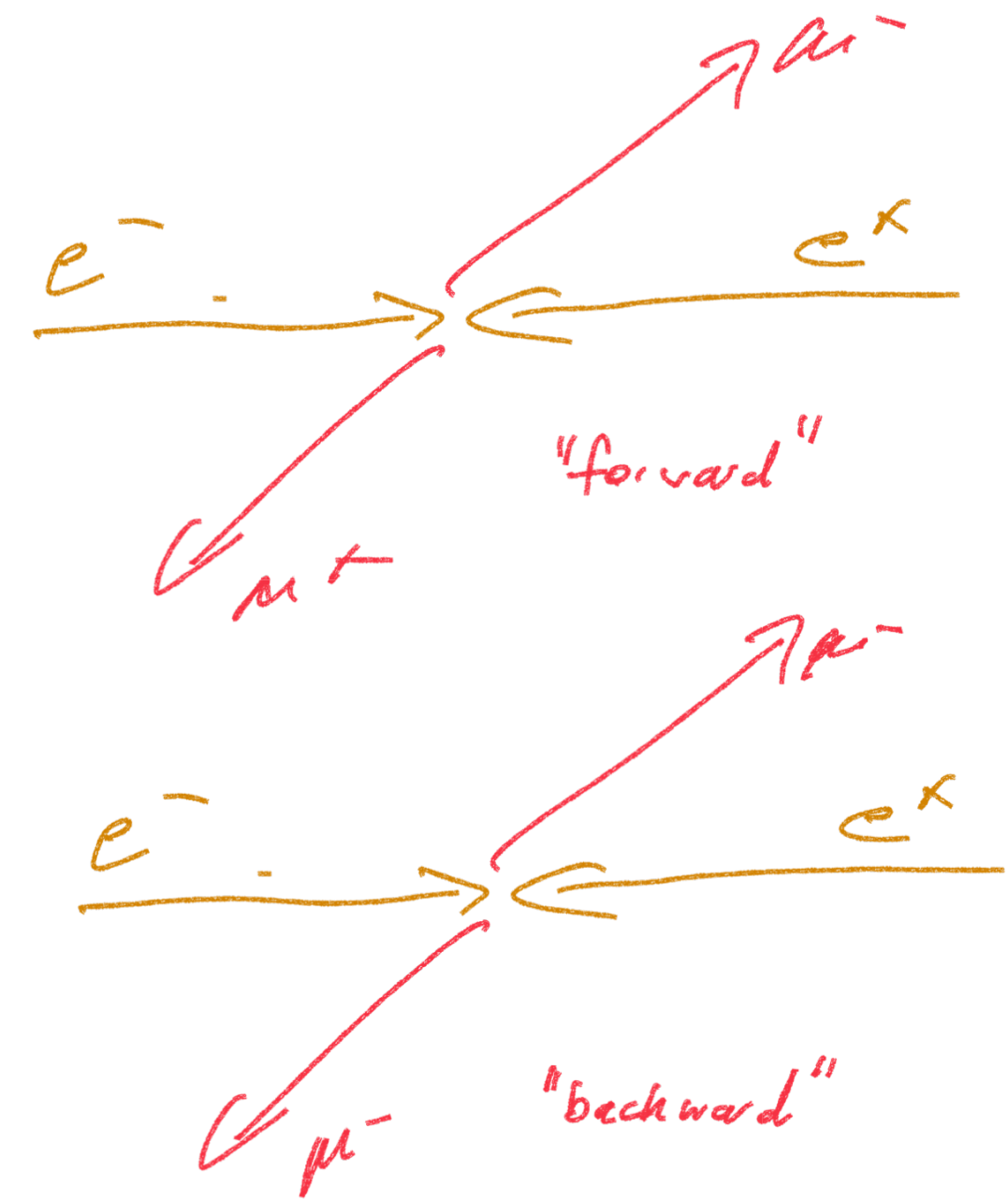
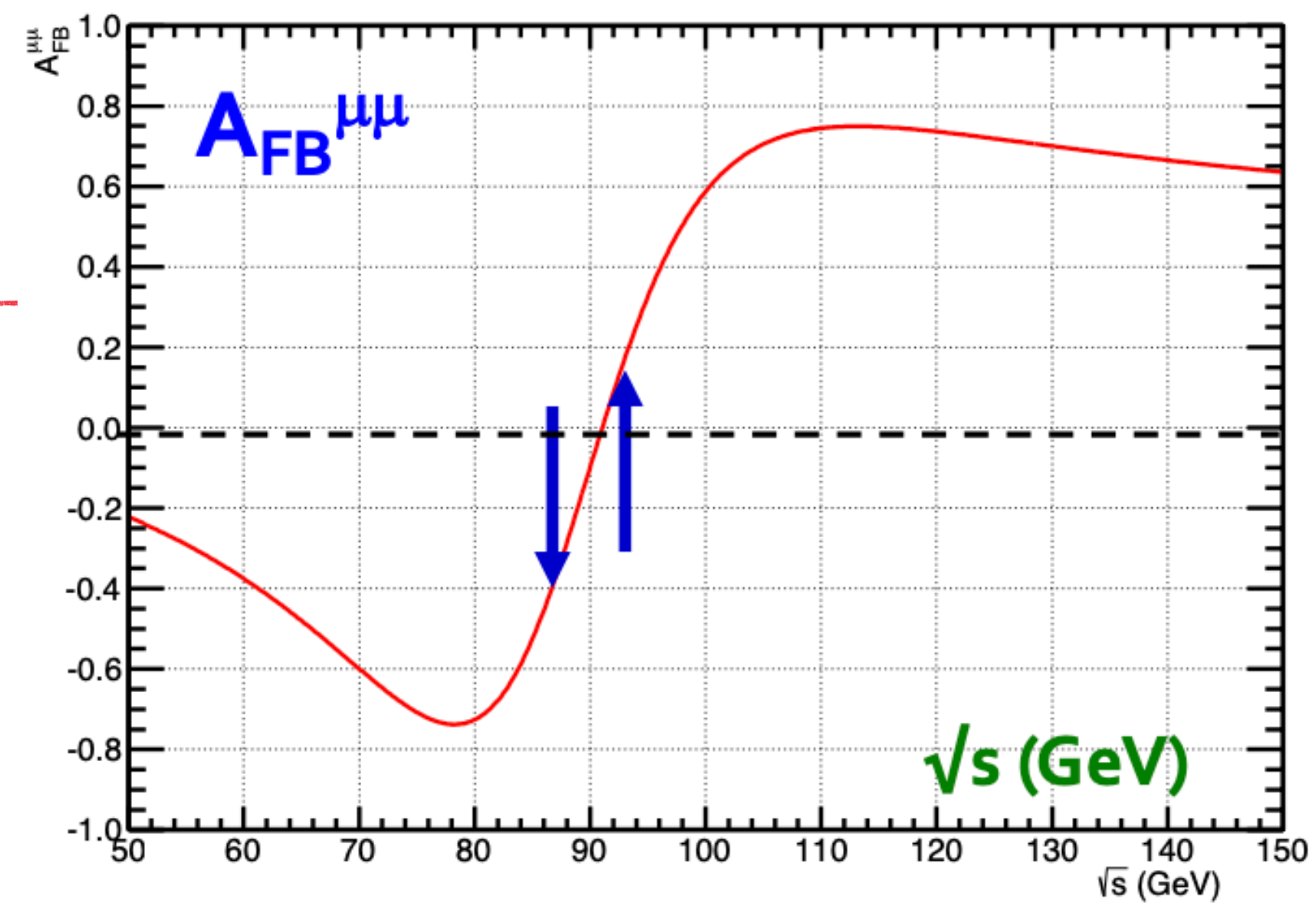
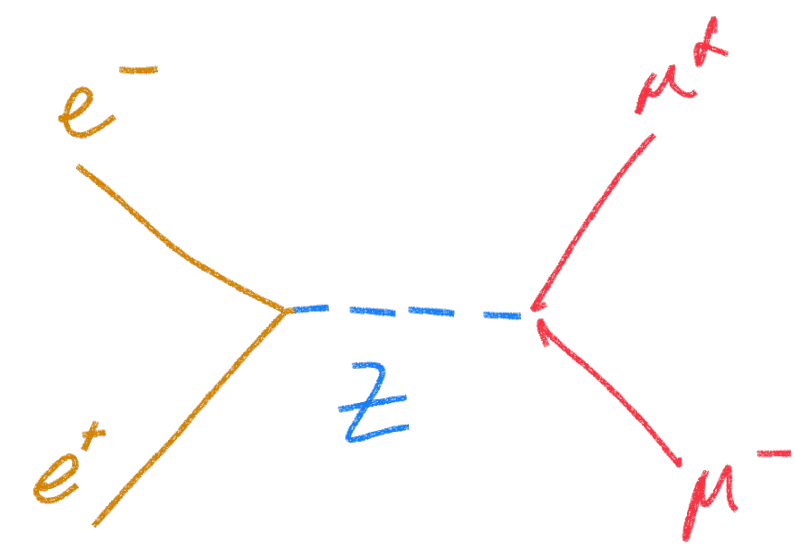
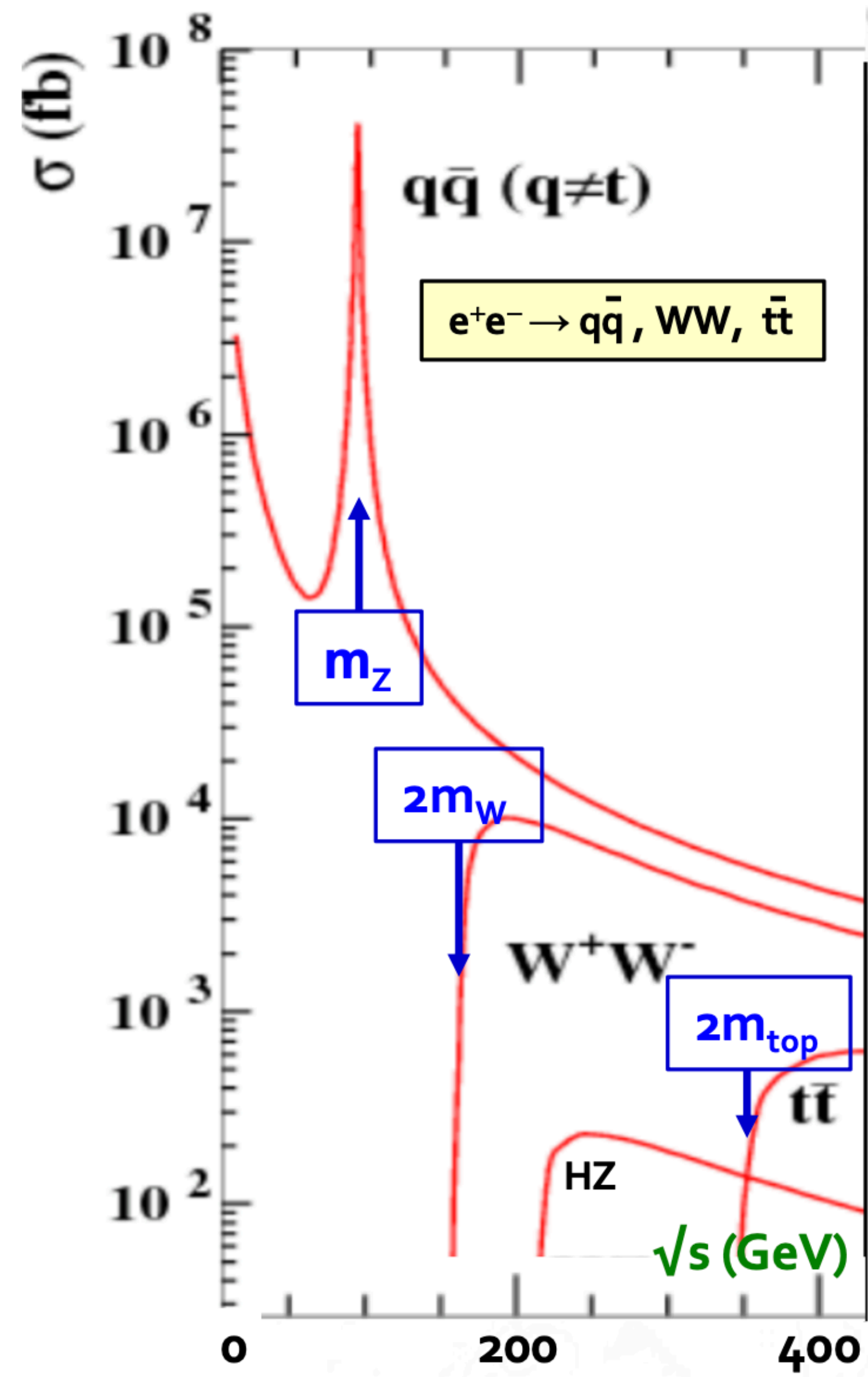
Electroweak Measurements

Cross sections and asymmetries



Electroweak Measurements

Cross sections and asymmetries

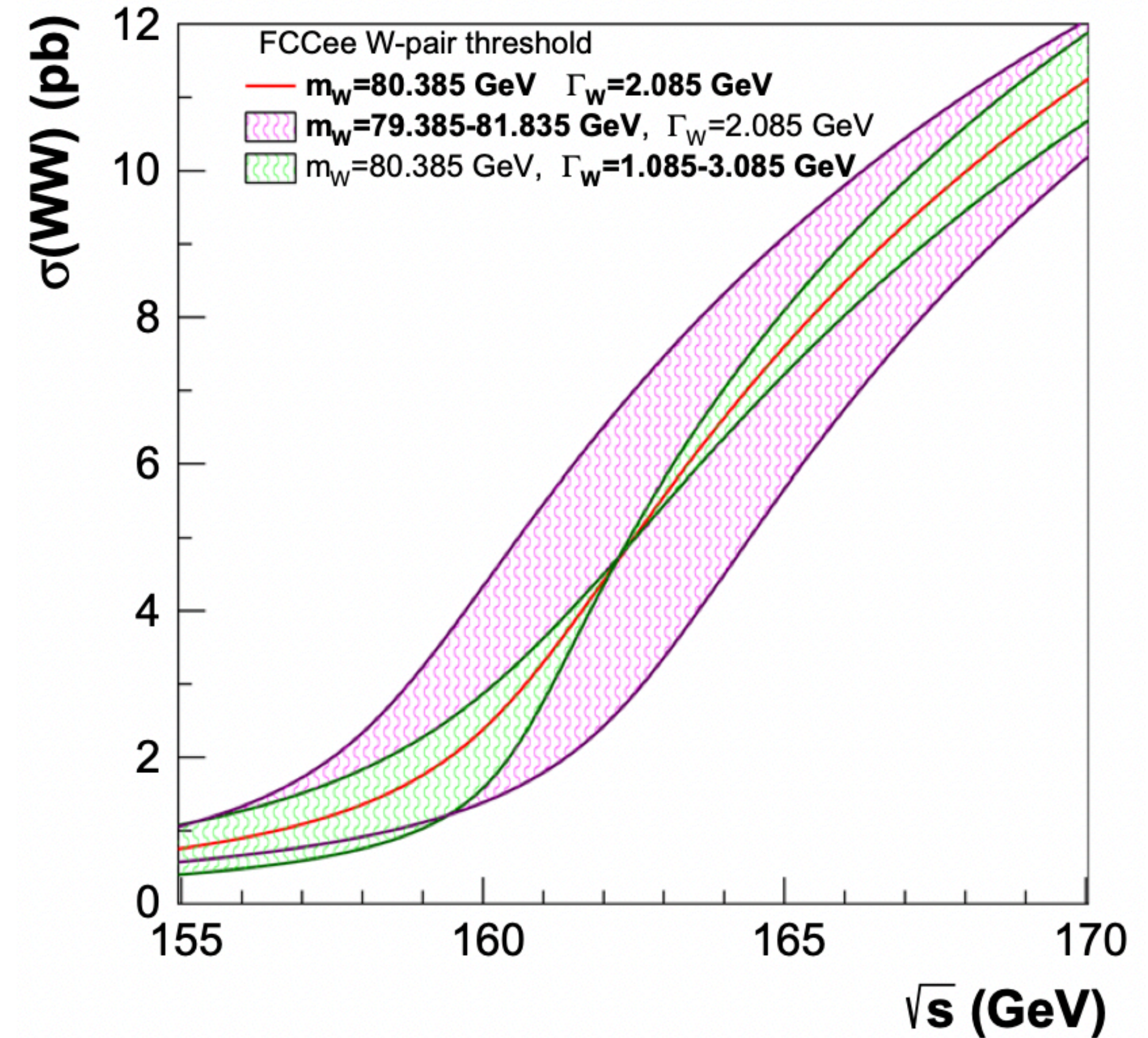
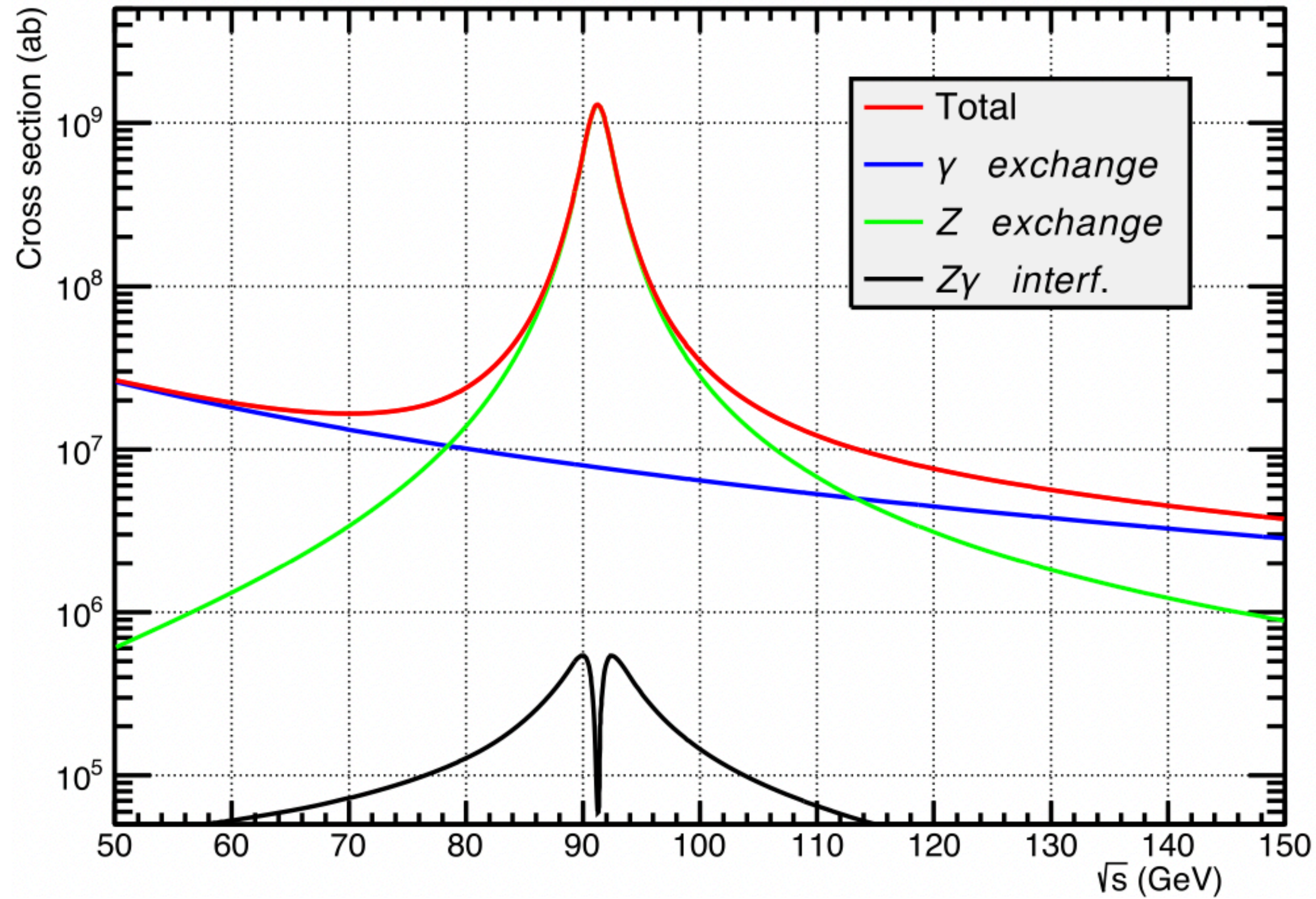


$$A_{FB}^{\mu\mu} = \frac{N_F^{\mu+} - N_B^{\mu+}}{N_F^{\mu+} + N_B^{\mu+}} \approx f(\sin^2 \vartheta_W^{eff}) + \alpha_{QED}(s) \frac{s - m_Z^2}{2s} g(\sin^2 \vartheta_W^{eff})$$

- Measure $\sin^2 \Theta_W$ via A_{FB} at $\sqrt{s} = m_Z$
- Measure $\alpha_{QED}(m_Z)$ via A_{FB} slightly below and above resonance

Lineshapes and Thresholds

The things to explore



- Lineshapes, cross sections, asymmetries provide access to a wide range of electroweak precision measurements, putting the Standard Model to extremely stringent tests

FCC-ee Electroweak Projections

Summary

Observable	Present value \pm error	FCC-ee Stat.	FCC-ee Syst.	Comment and dominant exp. error
m_Z (keV)	91,186,700 \pm 2200	4	100	From Z lineshape scan; beam energy calibration
Γ_Z (keV)	2,495,200 \pm 2300	4	25	From Z lineshape scan; beam energy calibration
R_ℓ^Z ($\times 10^3$)	20,767 \pm 25	0.06	0.2 – 1.0	Ratio of hadrons to leptons; acceptance for leptons
$\alpha_S(m_Z^2)$ ($\times 10^4$)	1,196 \pm 30	0.1	0.4 – 1.6	From R_ℓ^Z above
R_b ($\times 10^6$)	216,290 \pm 660	0.3	< 60	Ratio of $b\bar{b}$ to hadrons; stat. extrapol. from SLD
σ_{had}^0 ($\times 10^3$) (nb)	41,541 \pm 37	0.1	4	Peak hadronic cross section; luminosity measurement
N_ν ($\times 10^3$)	2,996 \pm 7	0.005	1	Z peak cross sections; luminosity measurement
$\sin^2 \theta_W^{\text{eff}}$ ($\times 10^6$)	231,480 \pm 160	1.4	1.4	From $A_{\text{FB}}^{\mu\mu}$ at Z peak; beam energy calibration
$1/\alpha_{\text{QED}}(m_Z^2)$ ($\times 10^3$)	128,952 \pm 14	3.8	1.2	From $A_{\text{FB}}^{\mu\mu}$ off peak
$A_{\text{FB}}^{b,0}$ ($\times 10^4$)	992 \pm 16	0.02	1.3	b -quark asymmetry at Z pole; from jet charge
A_e ($\times 10^4$)	1,498 \pm 49	0.07	0.2	from $A_{\text{FB}}^{\text{pol},\tau}$; systematics from non- τ backgrounds
m_W (MeV)	80,350 \pm 15	0.25	0.3	From WW threshold scan; beam energy calibration
Γ_W (MeV)	2,085 \pm 42	1.2	0.3	From WW threshold scan; beam energy calibration
N_ν ($\times 10^3$)	2,920 \pm 50	0.8	Small	Ratio of invis. to leptonic in radiative Z returns
$\alpha_S(m_W^2)$ ($\times 10^4$)	1,170 \pm 420	3	Small	From R_ℓ^W

- An e^+e^- collider running at the Z pole is also an excellent flavour factory!

The 5×10^{12} Zs at FCC-ee will provide: 10^{12} bb events, 1.7×10^{11} $\tau^+\tau^-$ events

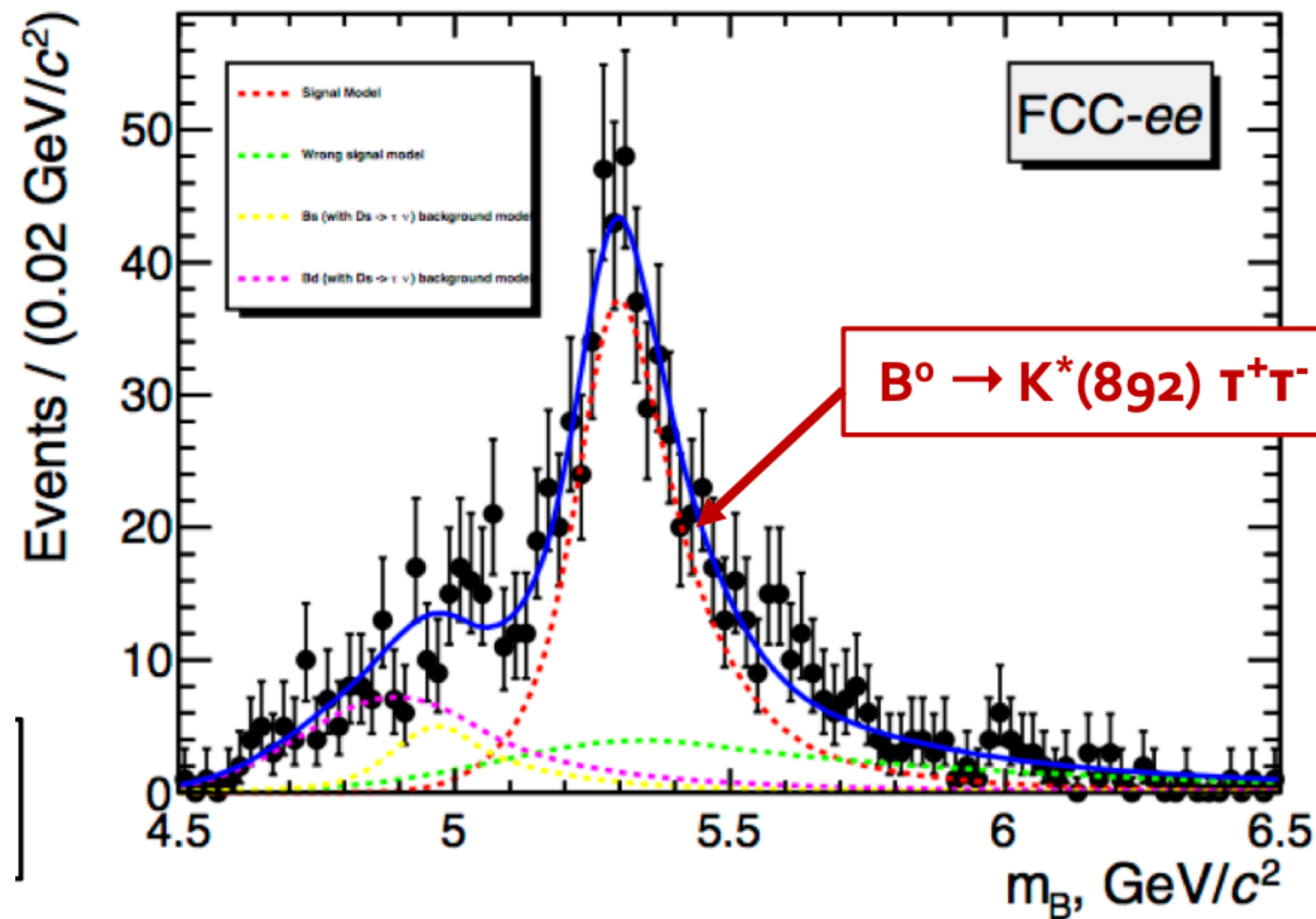
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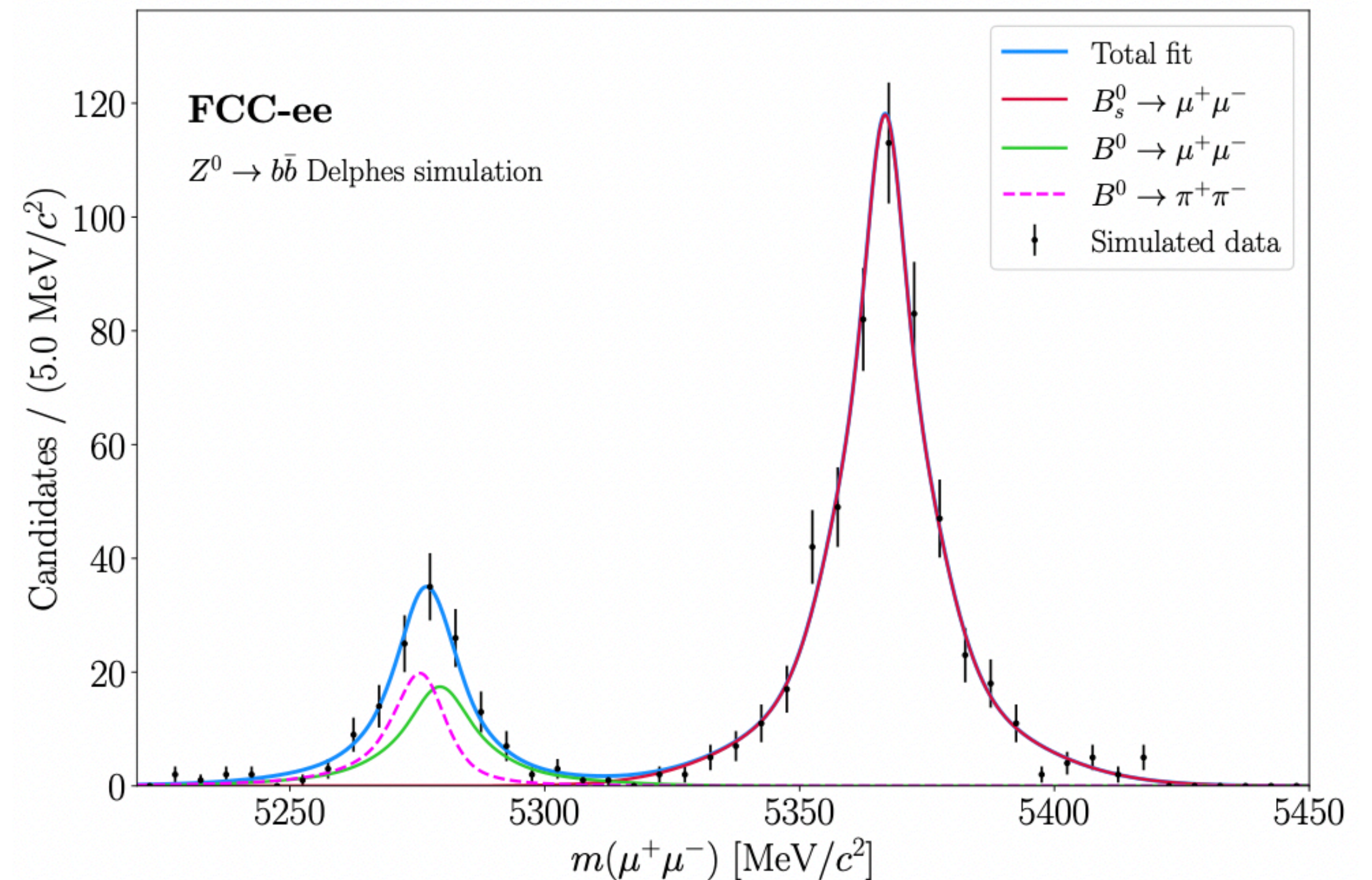
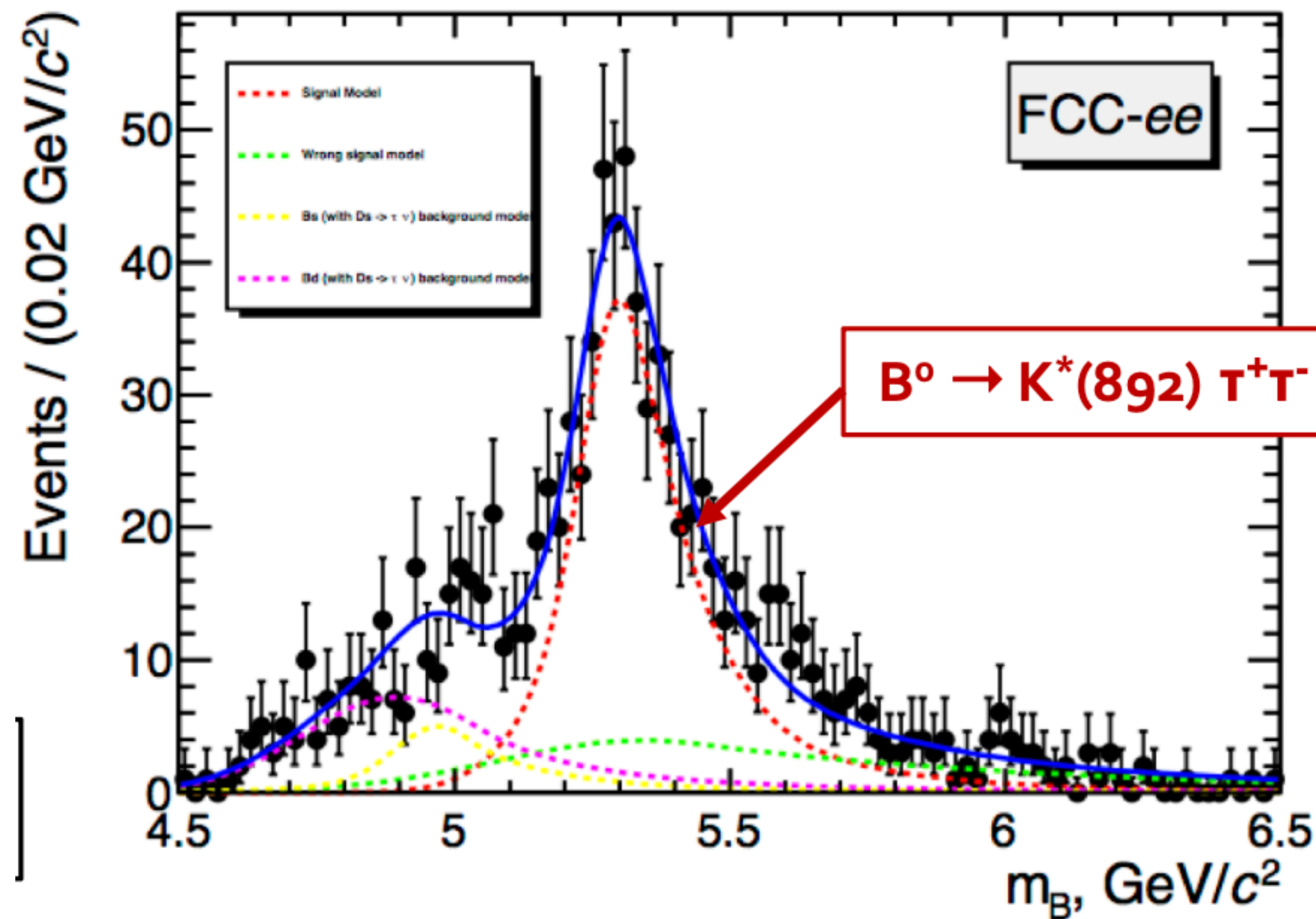
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Explore rare be decays with unprecedented precision.
Study of CP violation, the CKM matrix, ...



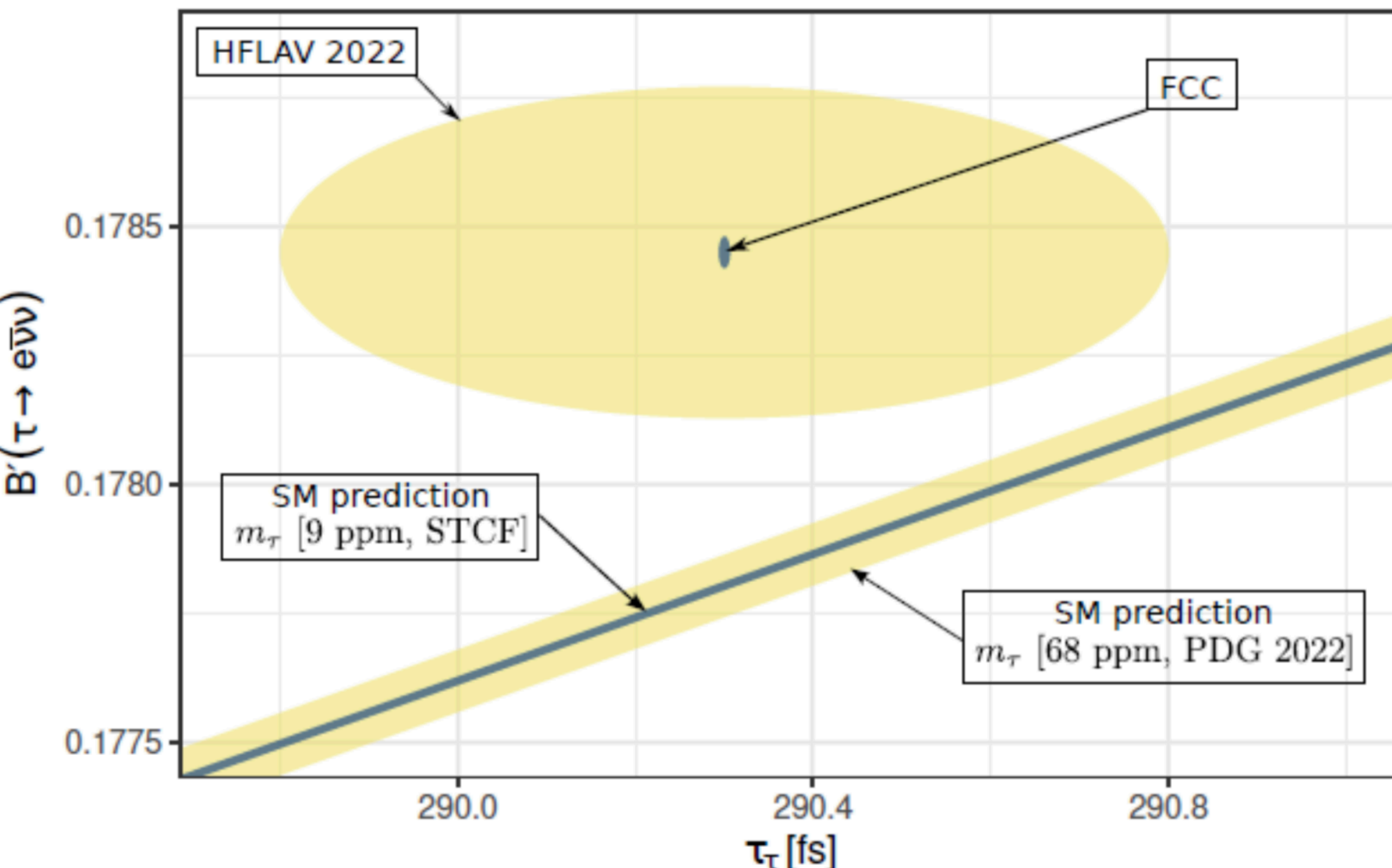
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A precise study of the τ - extending beyond Belle II now beginning

Canonical Tau Lepton Universality test
HFLAV 2022 in yellow, FCC estimates in blue



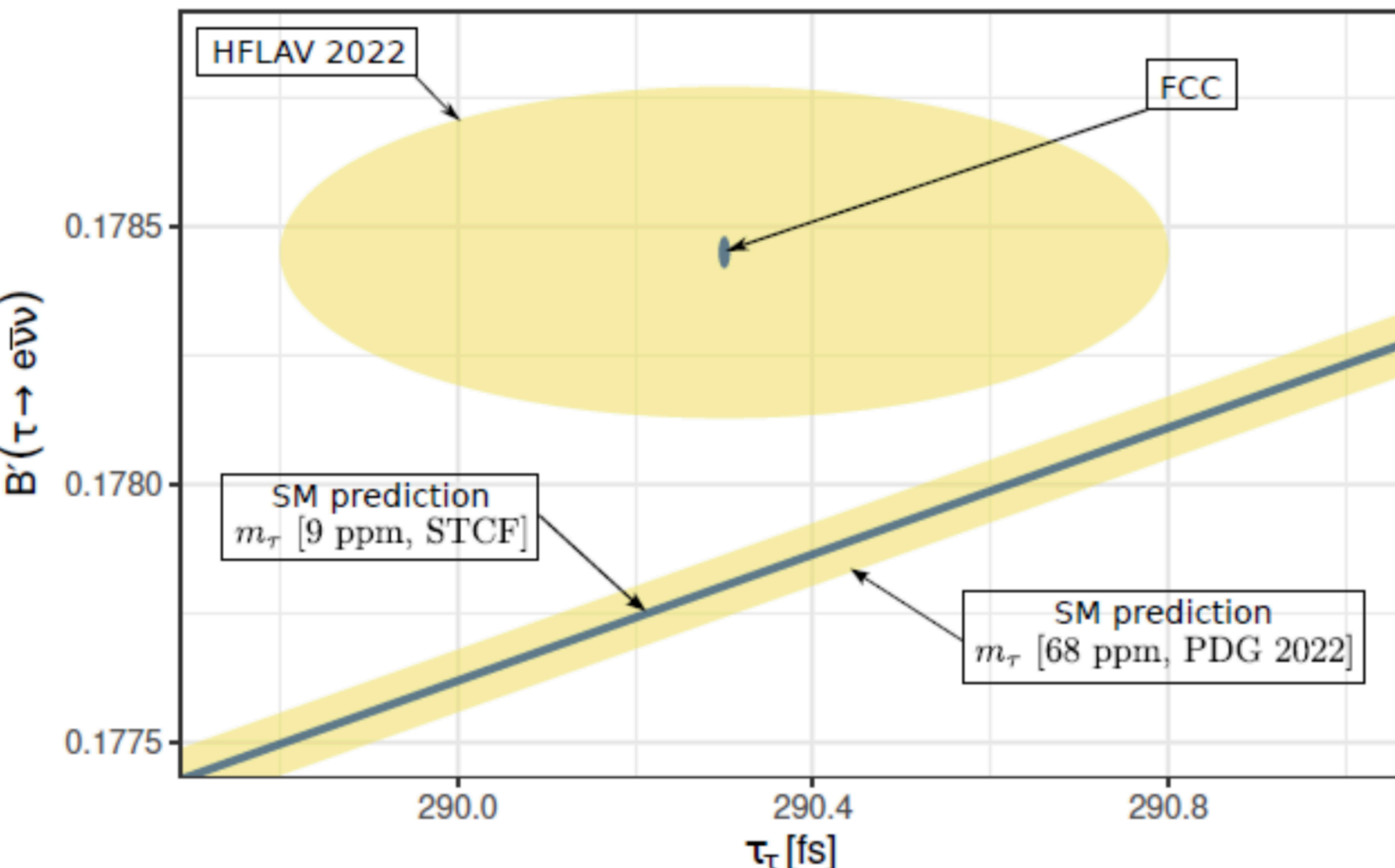
Observable	Current precision	FCC-ee stat.	Possible syst.
m_τ [MeV]	1776.86 ± 0.12	0.004	0.1
τ_τ [fs]	290.3 ± 0.5 fs	0.001	0.04
$B(\tau \rightarrow e\nu\nu)$ [%]	17.82 ± 0.05	0.0001	0.003
$B(\tau \rightarrow \mu\nu\nu)$ [%]	17.39 ± 0.05		

- An e^+e^- collider running at the Z pole is also an excellent flavour factory!

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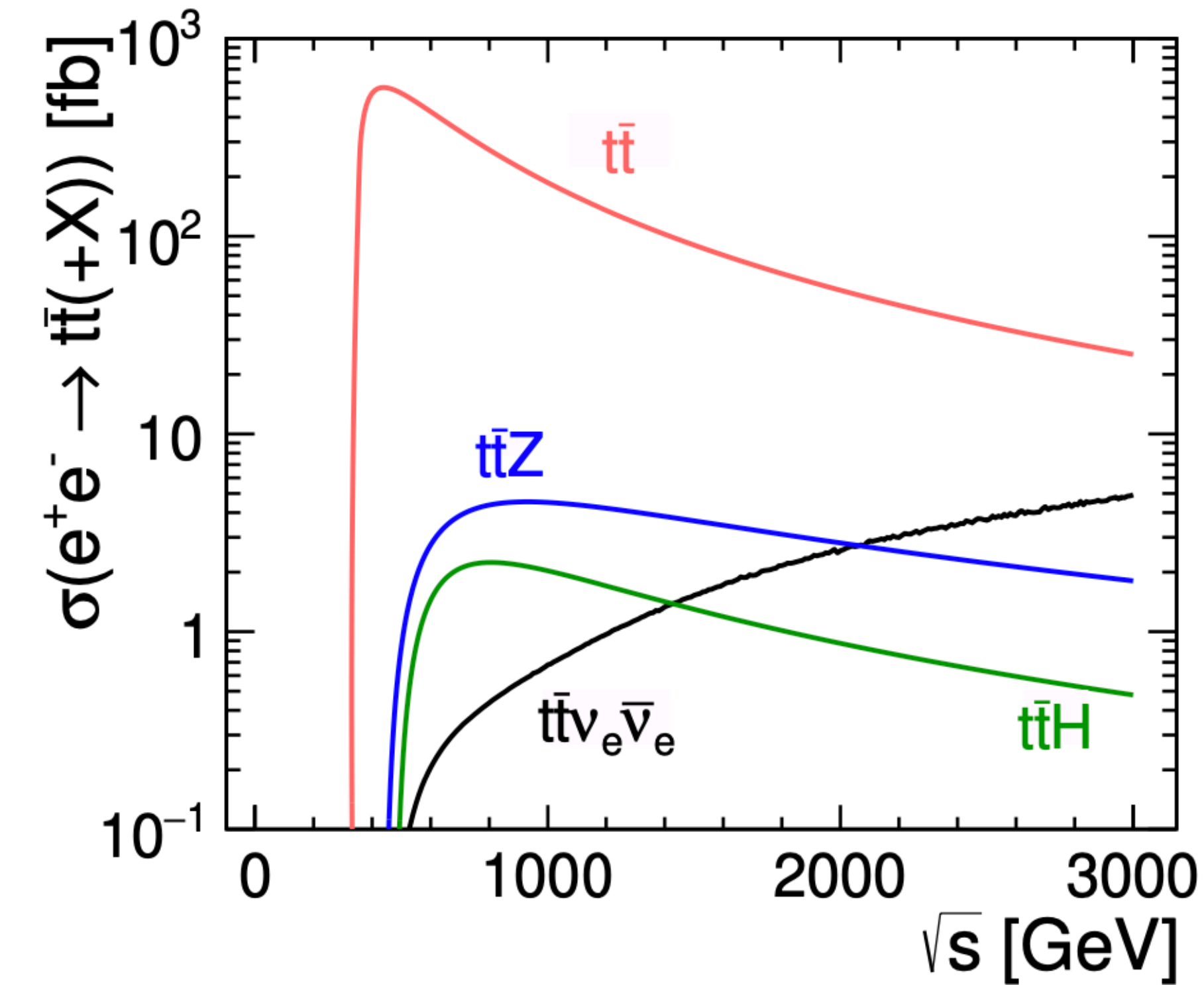
N.B.: Flavour physics introduces specific detector requirements such as PID, typically not front-and-center in Higgs Factory detector designs

The Top Quark

A new arena at 350 GeV and above

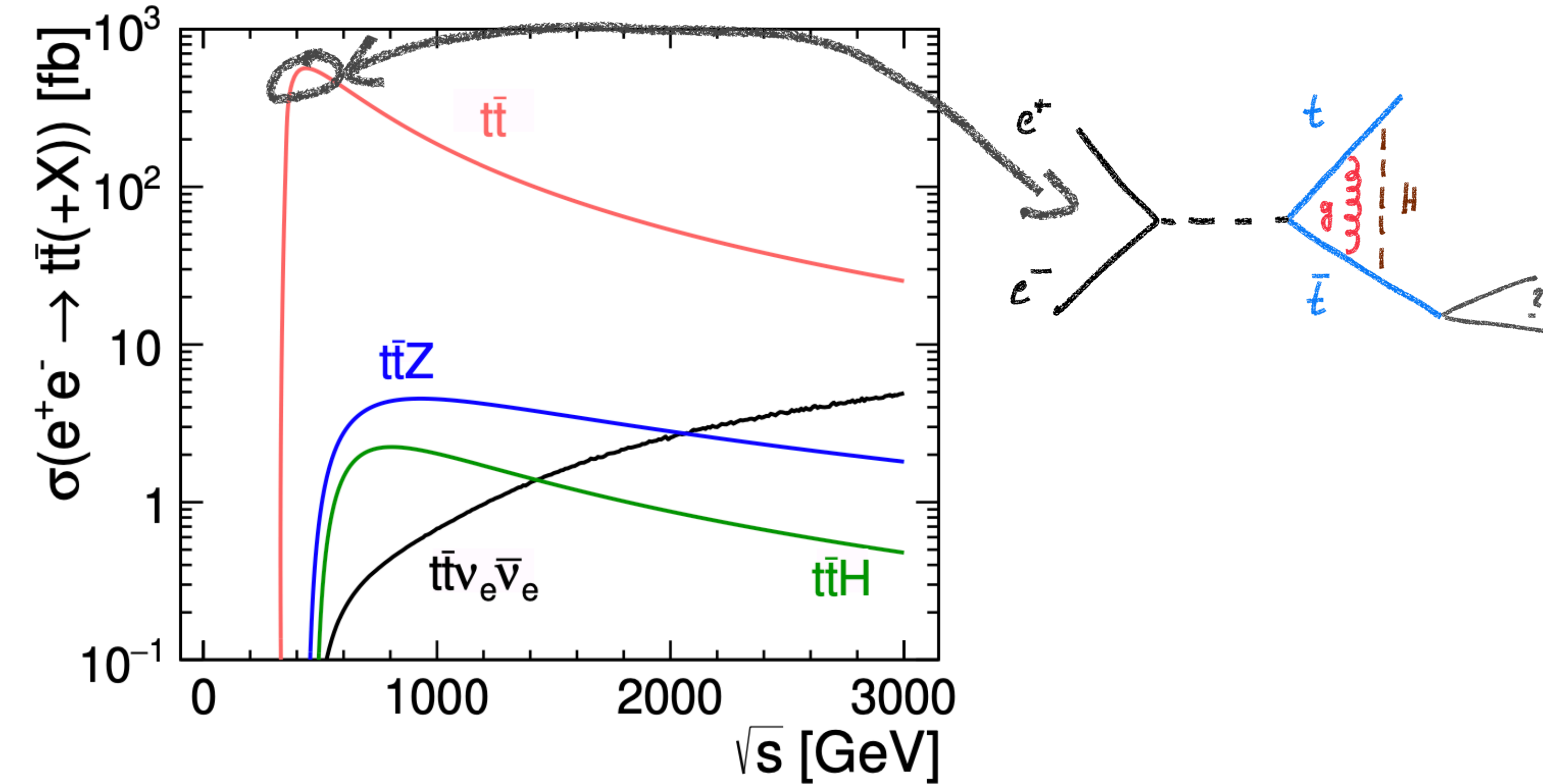
Overview: Top Physics at e^+e^- Colliders

Understanding the Top, using the Top



Overview: Top Physics at e^+e^- Colliders

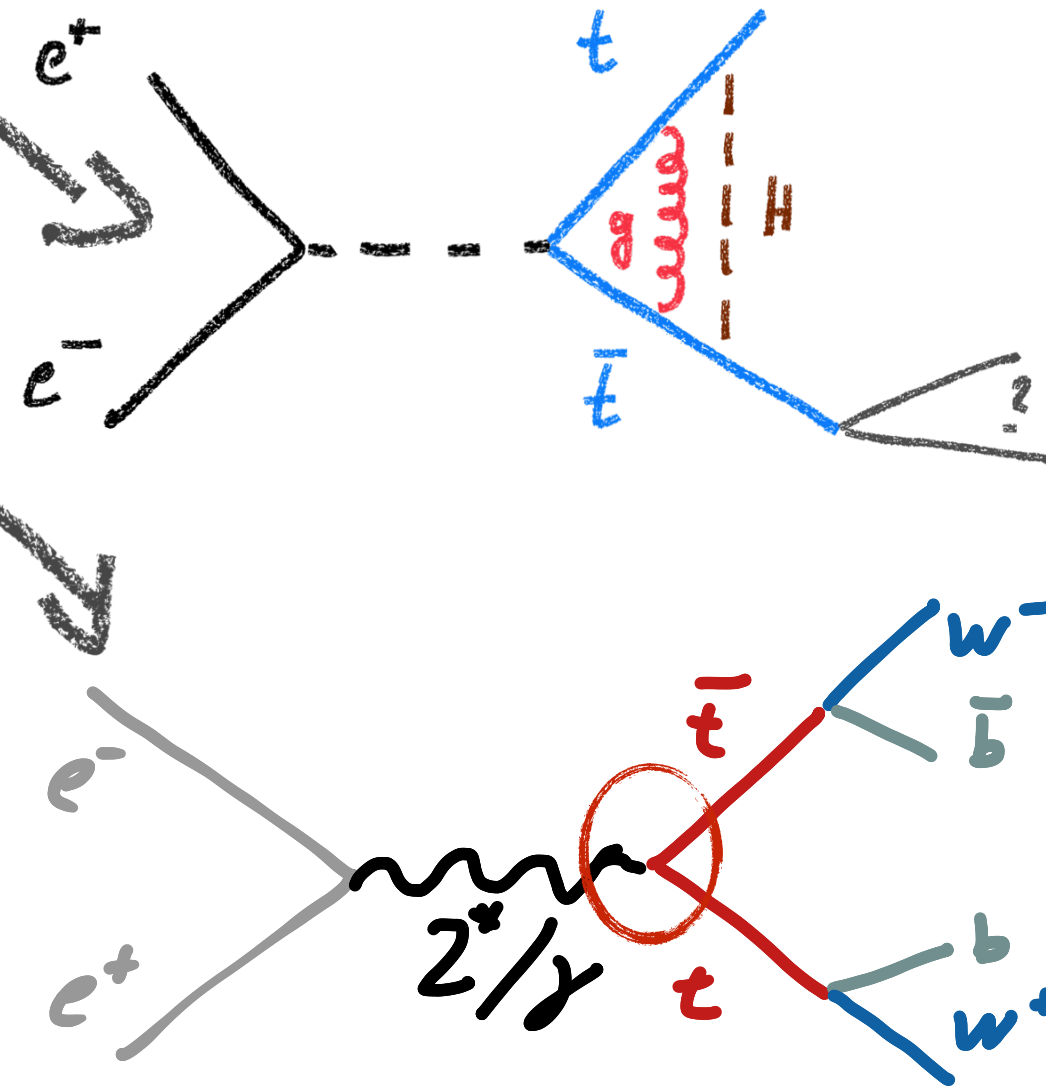
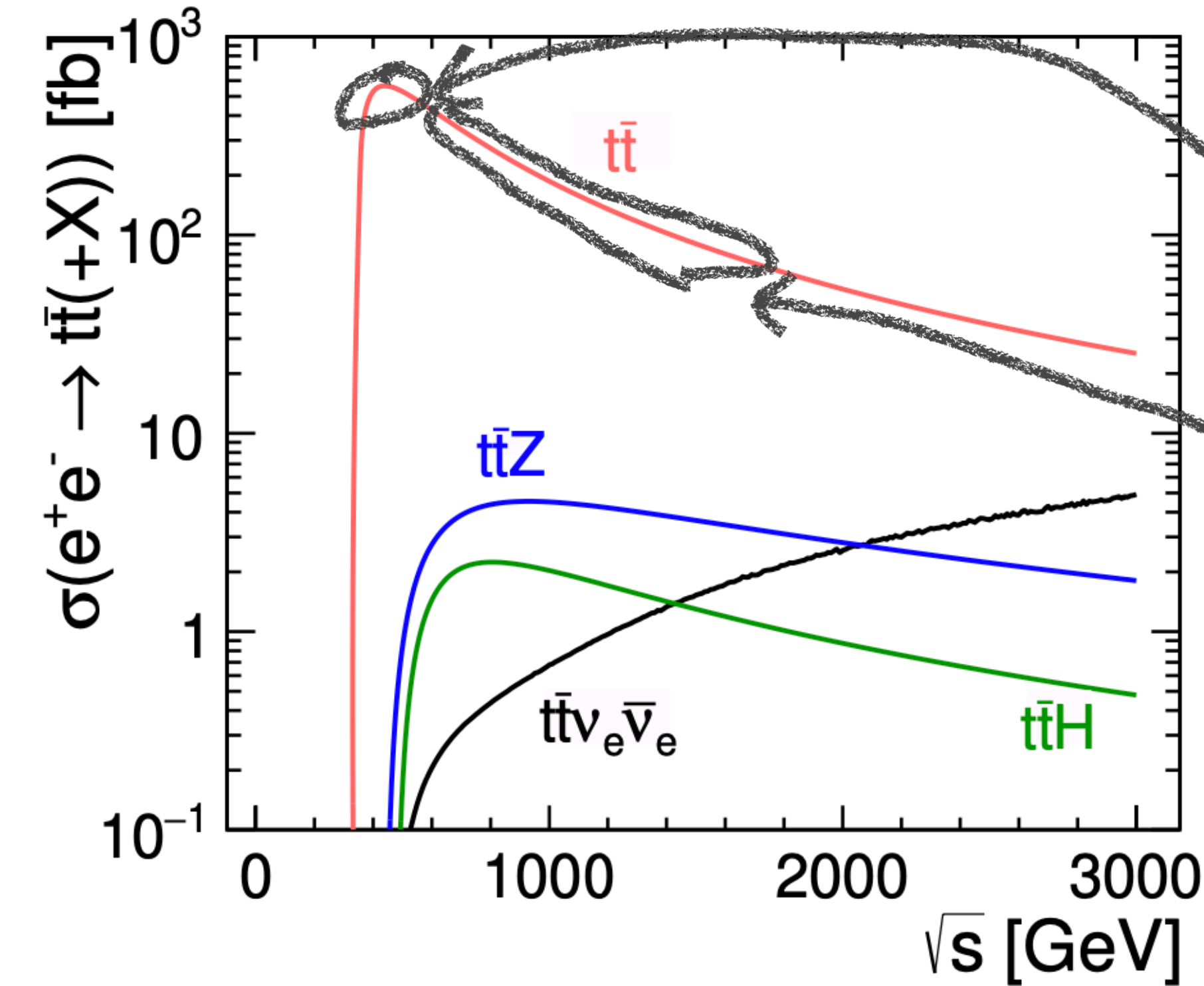
Understanding the Top, using the Top



- Measuring the top quark mass (and other parameters) in theoretically well-defined frameworks
- Search for BSM decays in clean environment

Overview: Top Physics at e^+e^- Colliders

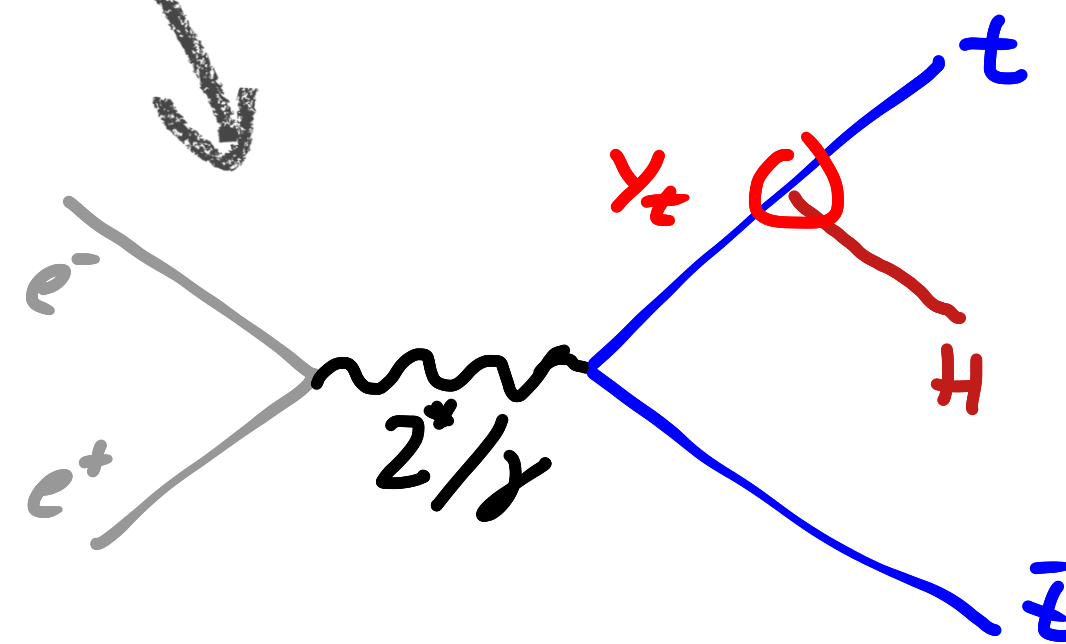
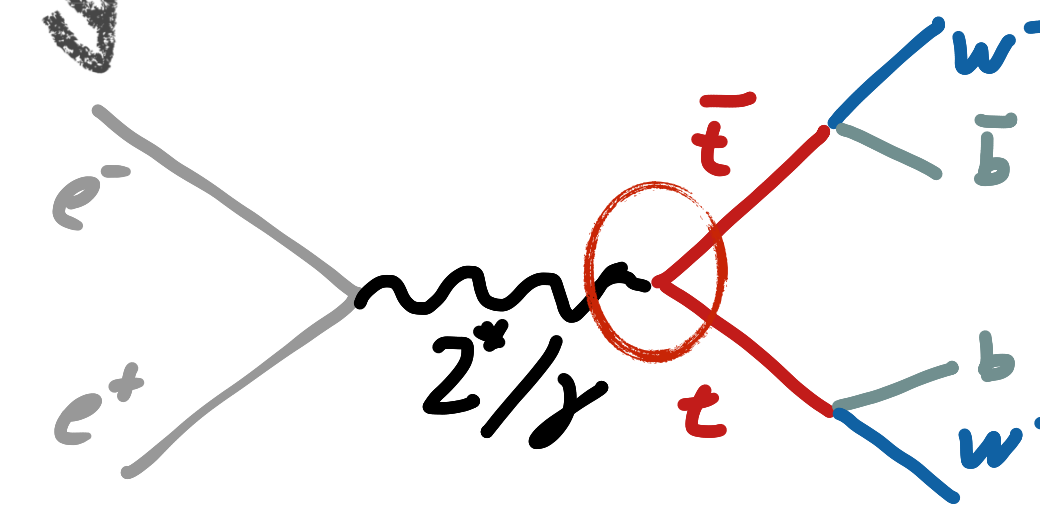
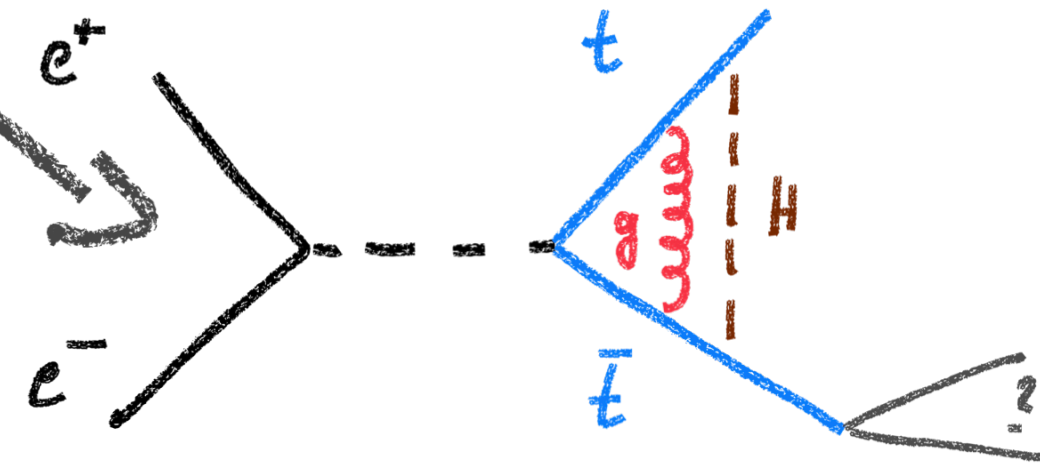
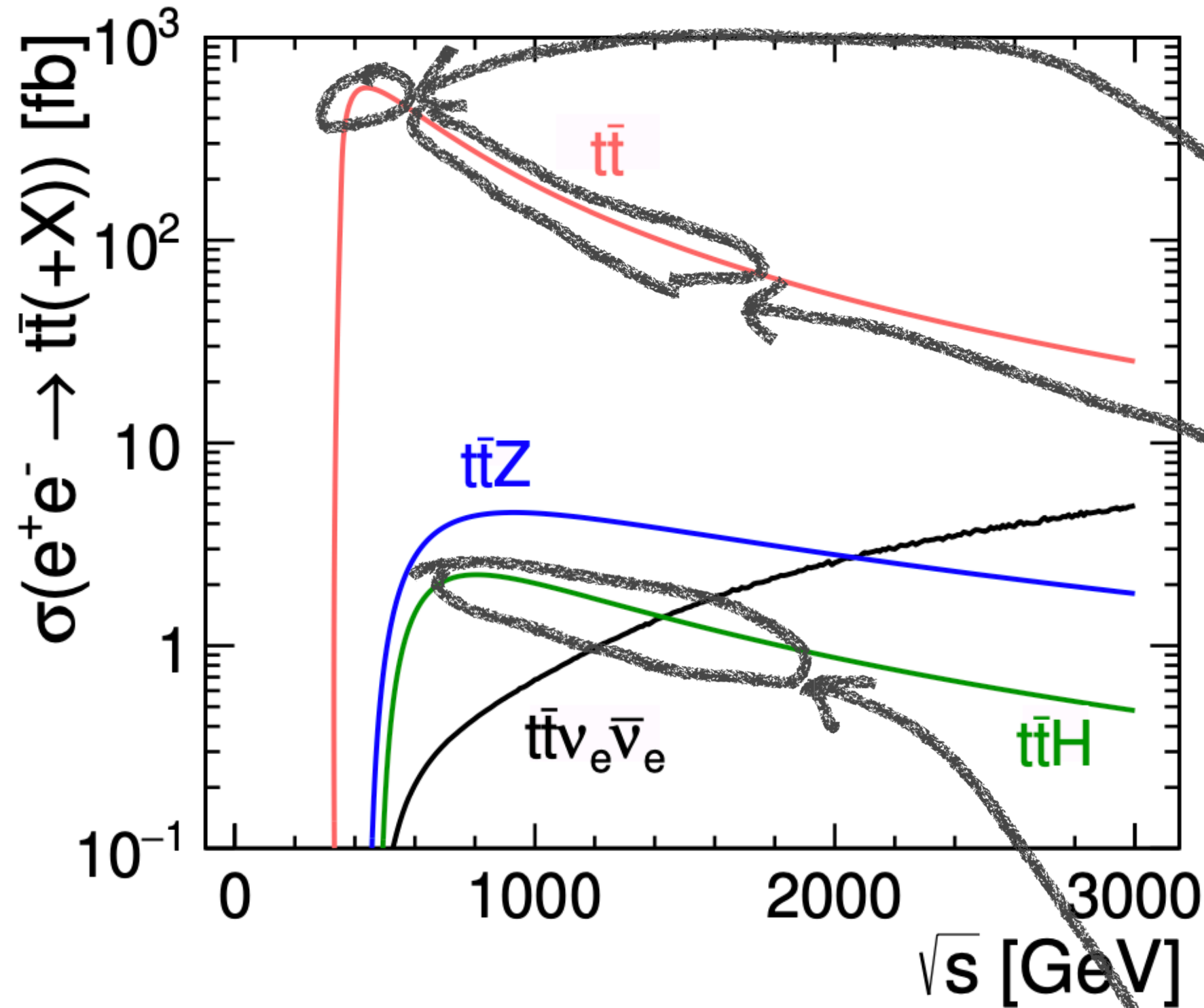
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Overview: Top Physics at e^+e^- Colliders

Understanding the Top, using the Top



- Measuring the top quark mass (and other parameters) in theoretically well-defined frameworks
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- Electroweak couplings of the top quark as a probe for New Physics

- Direct measurement of the top Yukawa coupling, ultimate potential of 2% [requires > 500 GeV, full scope assumes ~ 1 TeV]

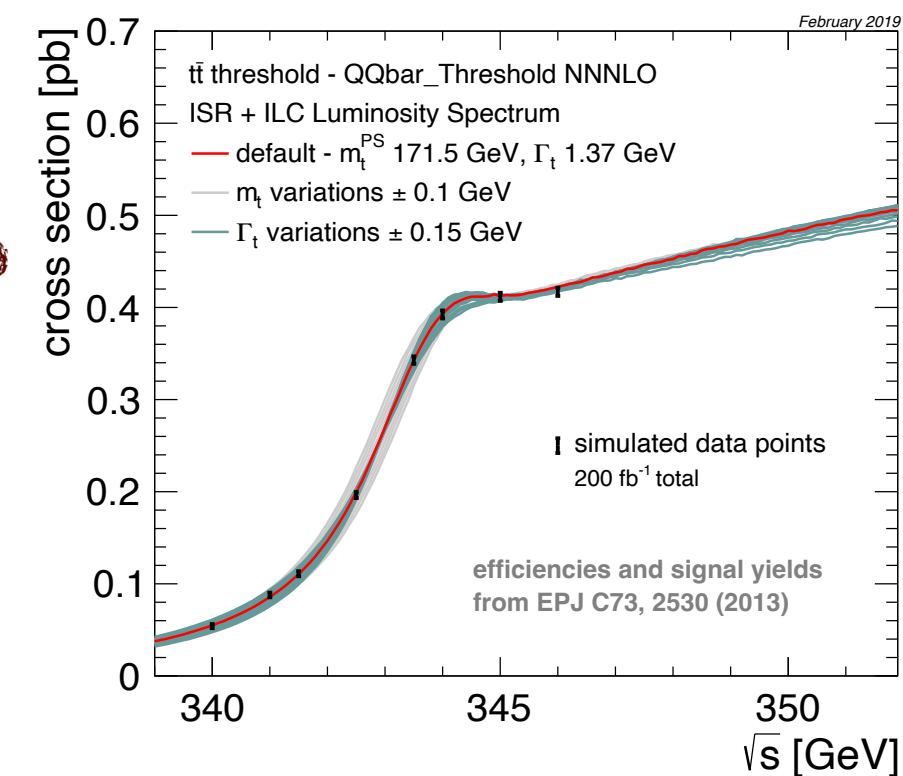
The Top Quark Mass (and other parameters)

Possibilities & Precision

- The accelerator side: Requires sufficient collision energy for top pair production
 - So far thoroughly studied for ILC, CLIC, threshold studies common for CLIC, FCC-ee, ILC

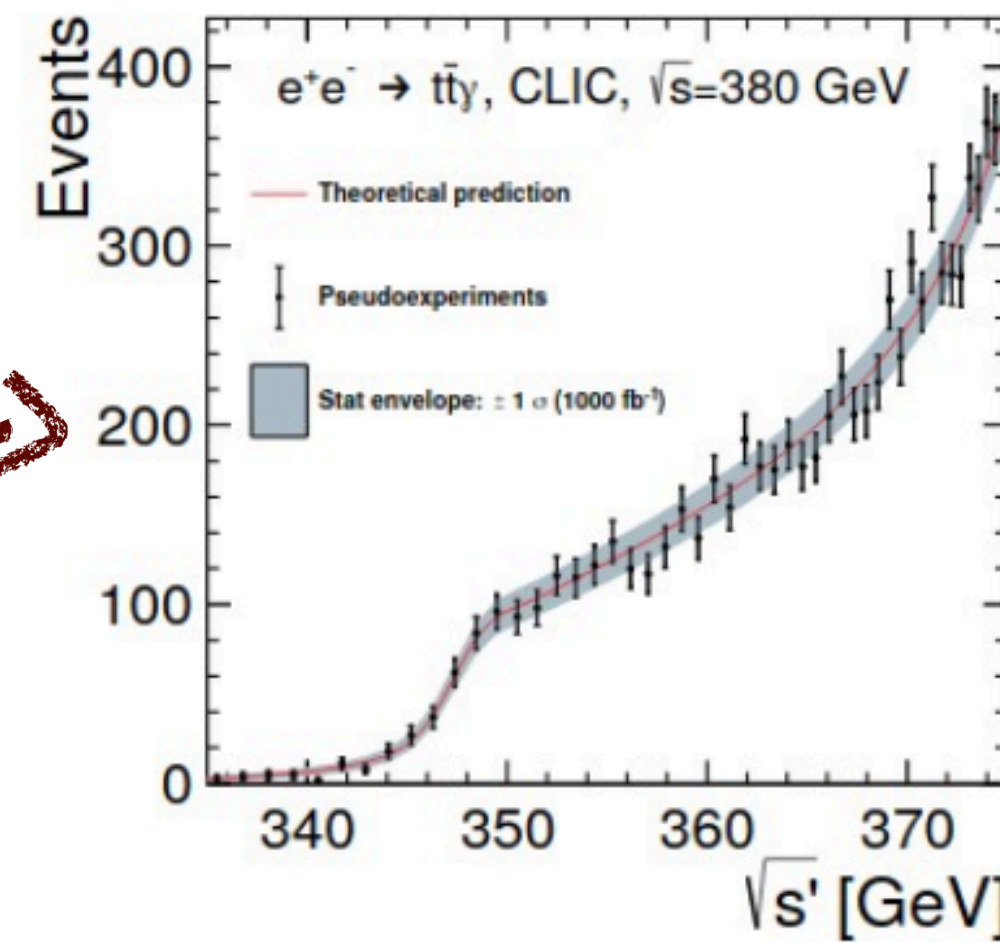
Three approaches to the top mass

The threshold scan around 350 GeV



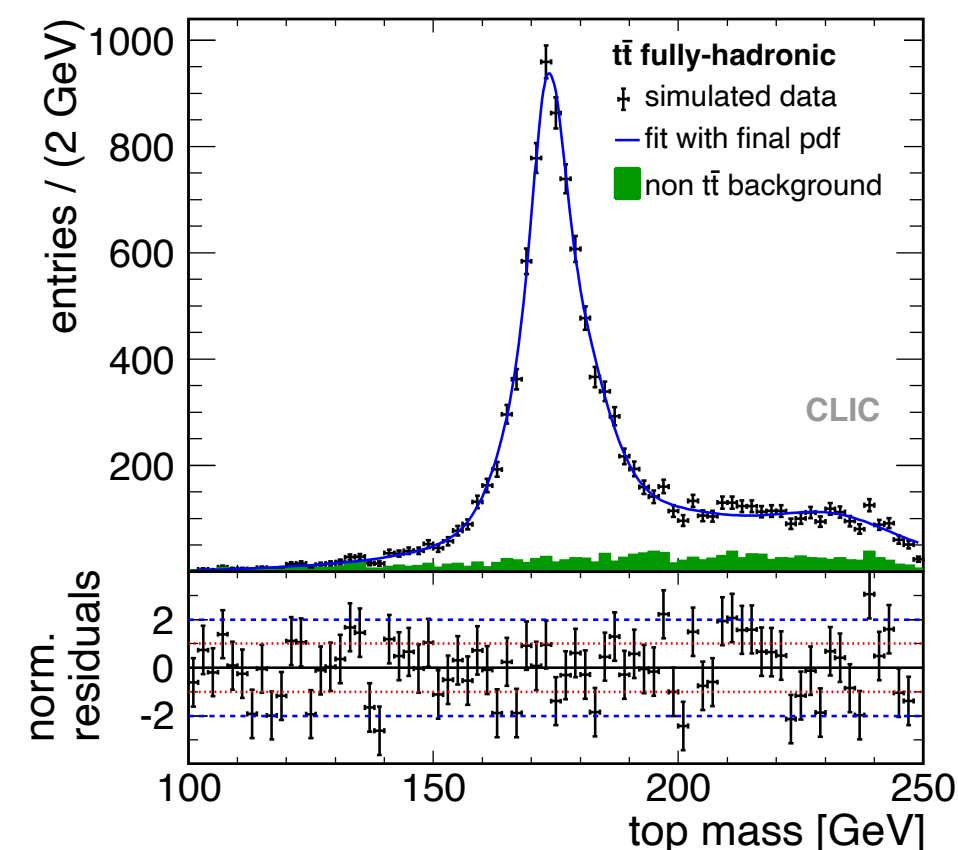
Extraction of the mass in theoretically well-defined mass definition (1S, PS): can directly be used in precision calculations, minimal conversion uncertainties to M_{Sbar} mass etc.

The top mass from radiative events



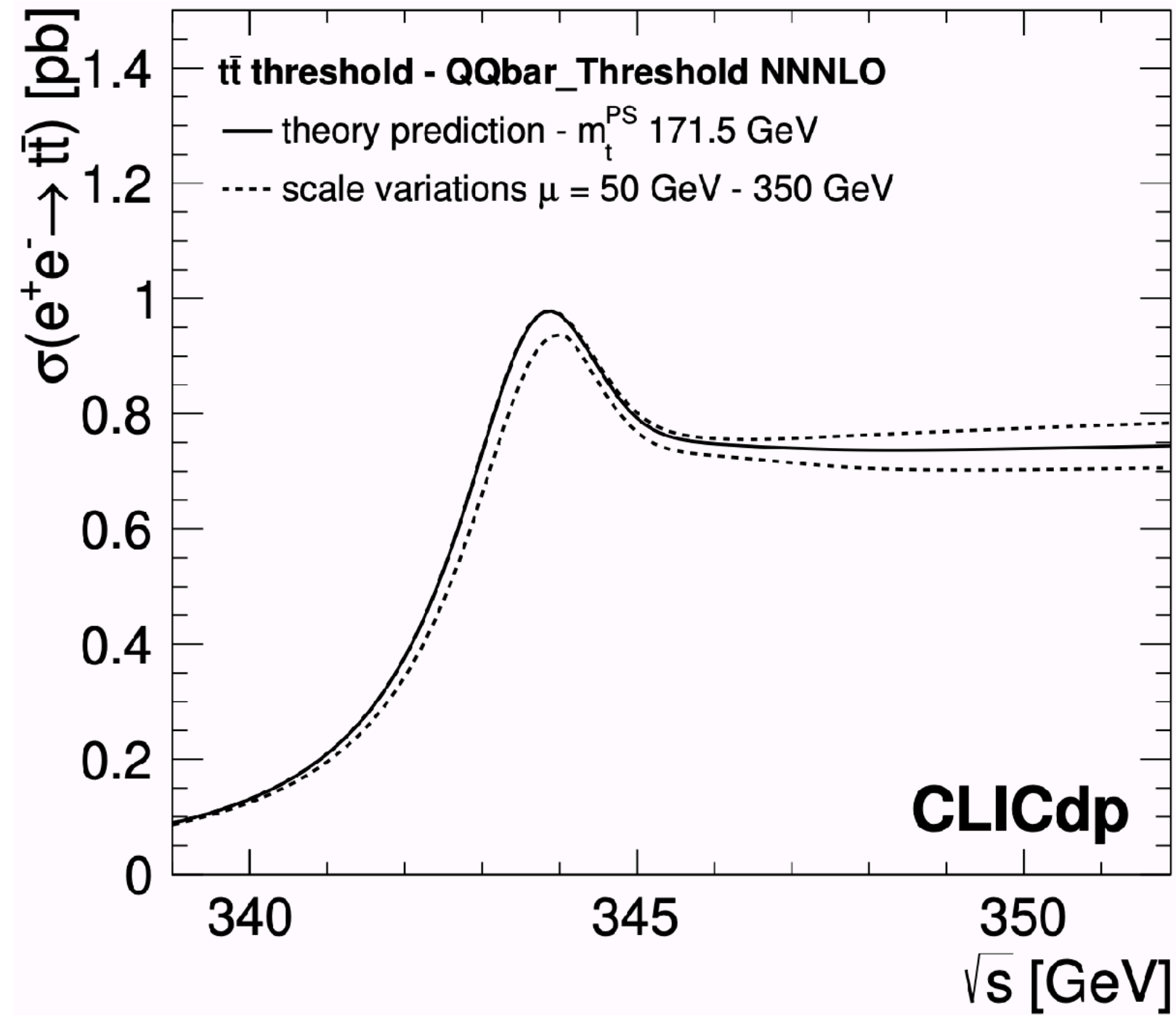
measurement of a “MC mass”: Interpretation uncertainties of several 100 MeV

Direct kinematic reconstruction



The Top Quark Mass

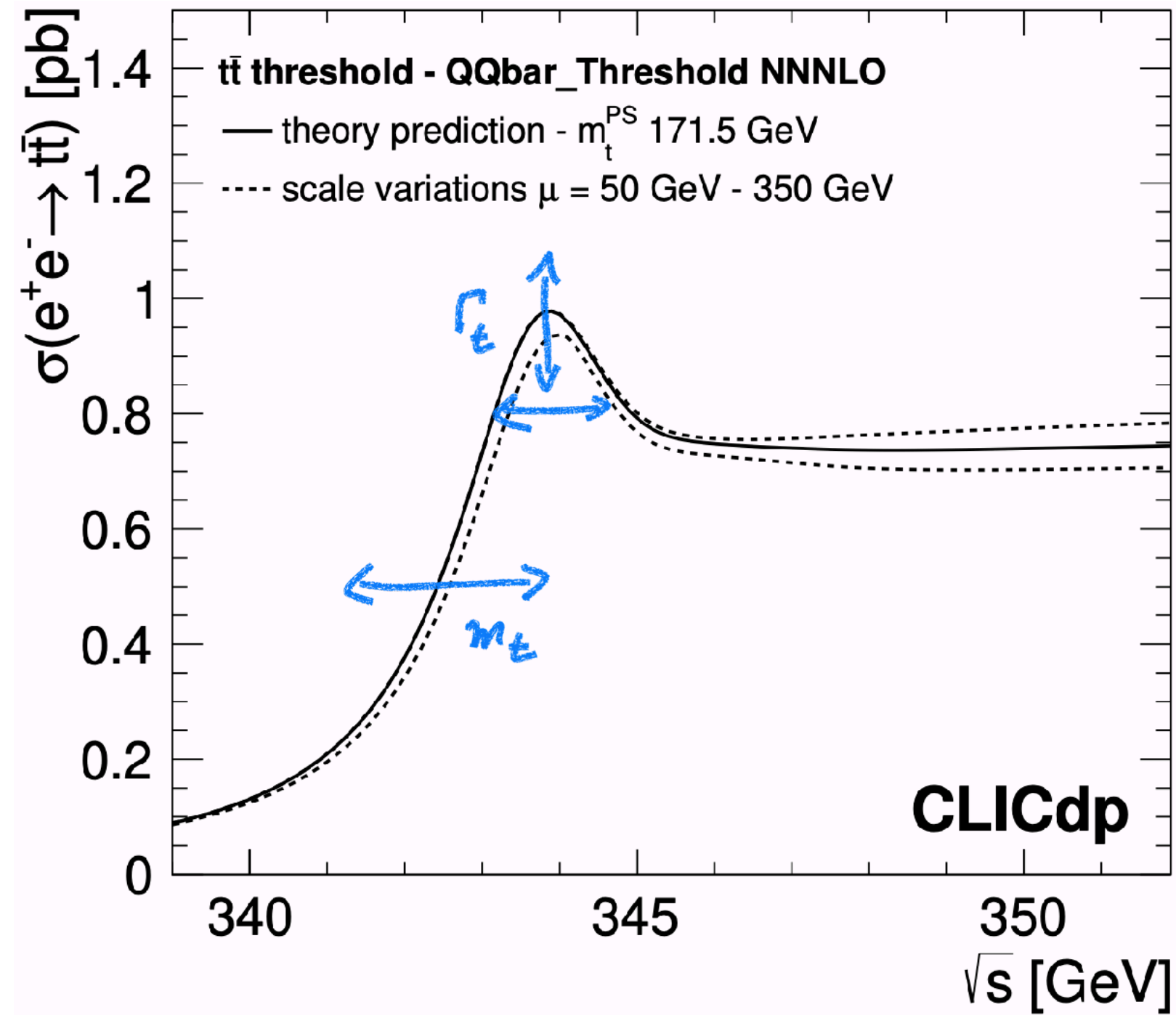
Ultimate precision at the threshold



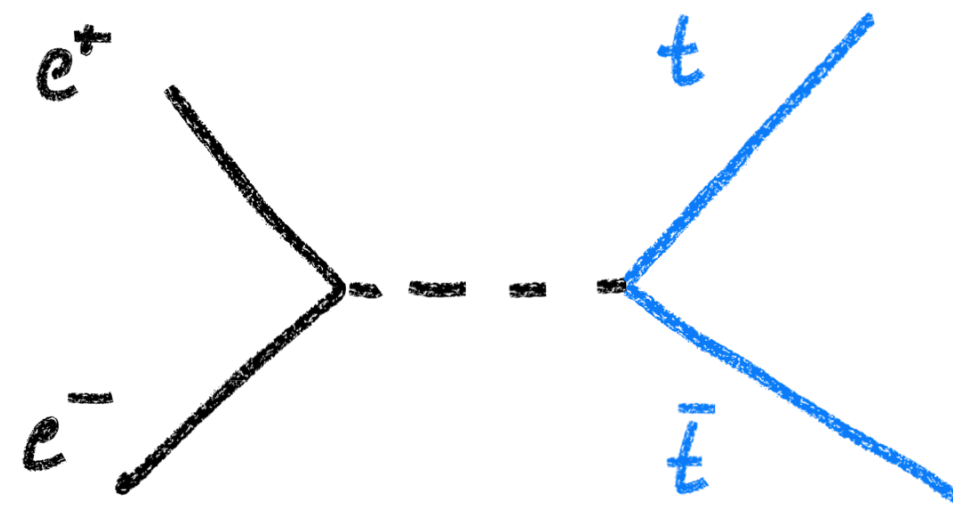
- Exploit precise theoretical calculations of cross section in the threshold region, in well-defined mass schemes (m_t^{PS} , m_t^{1S} ...) -> Can be converted directly into MSbar mass.

The Top Quark Mass

Ultimate precision at the threshold



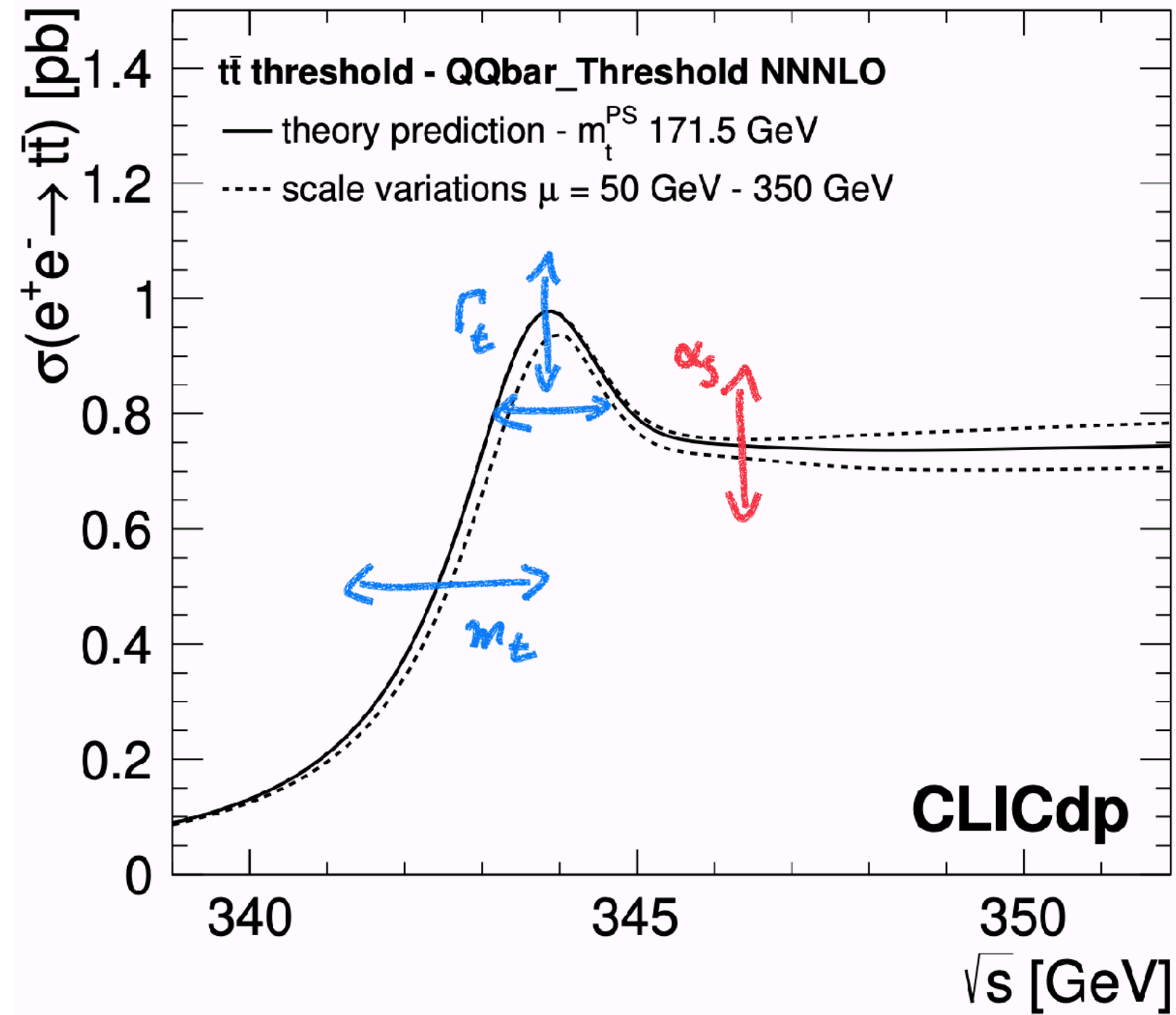
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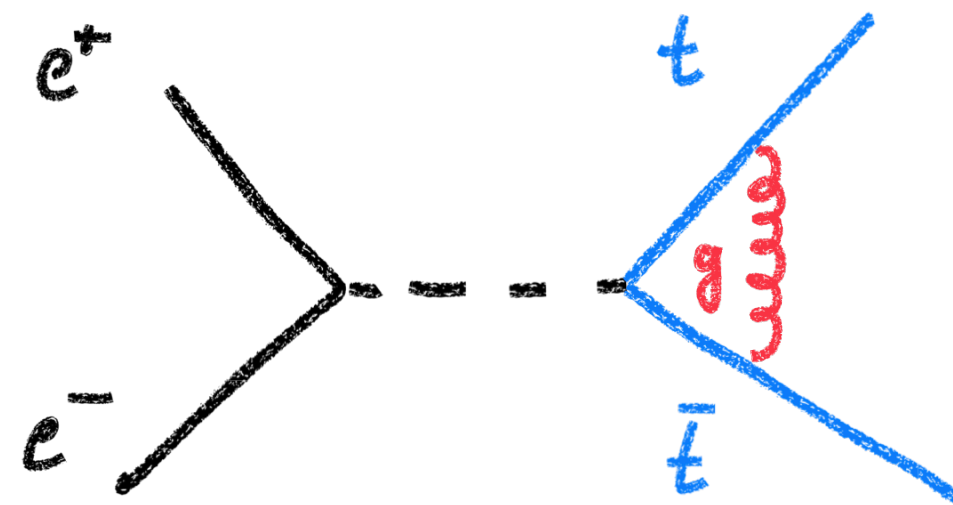
The threshold is sensitive to top quark properties

The Top Quark Mass

Ultimate precision at the threshold



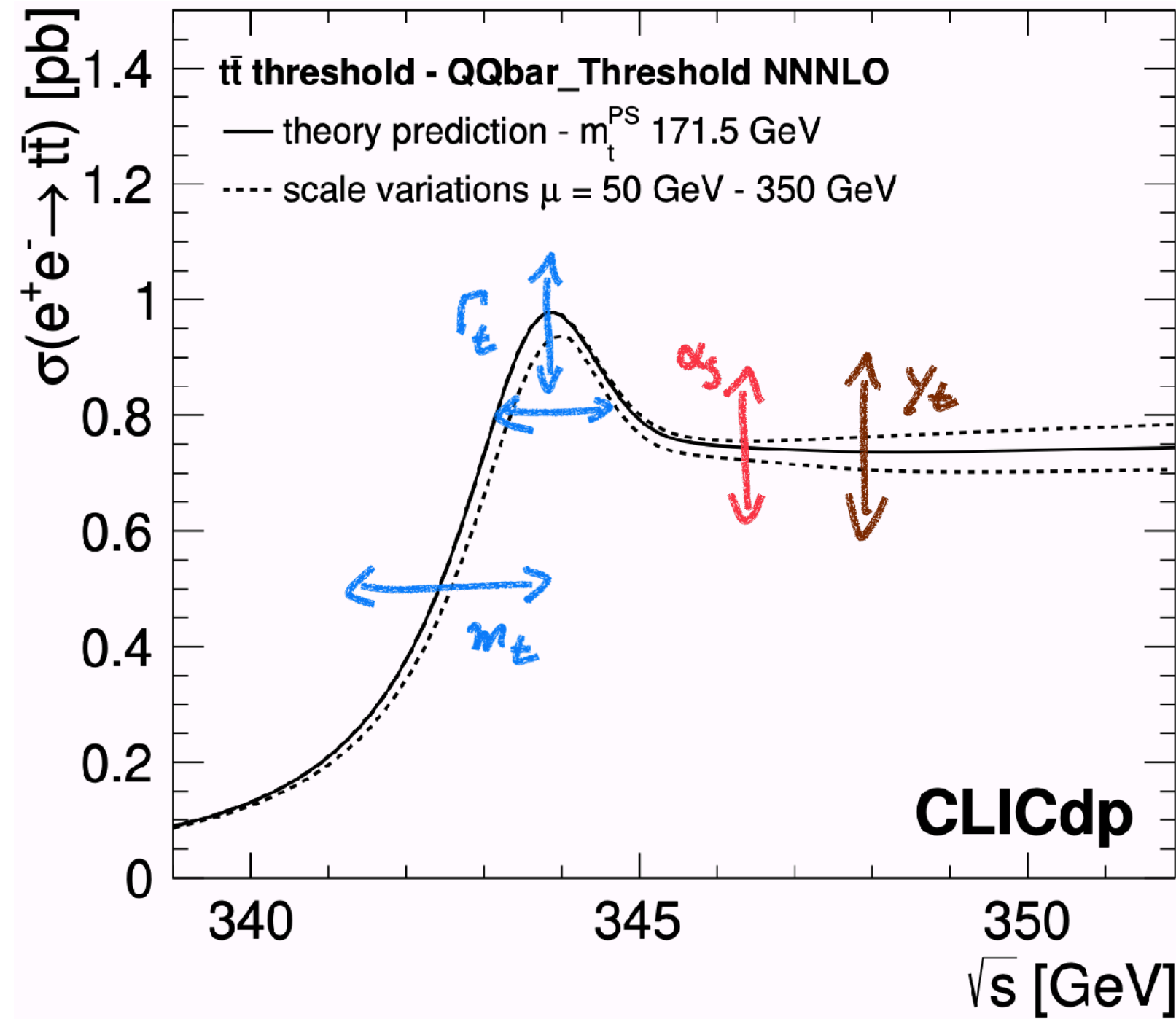
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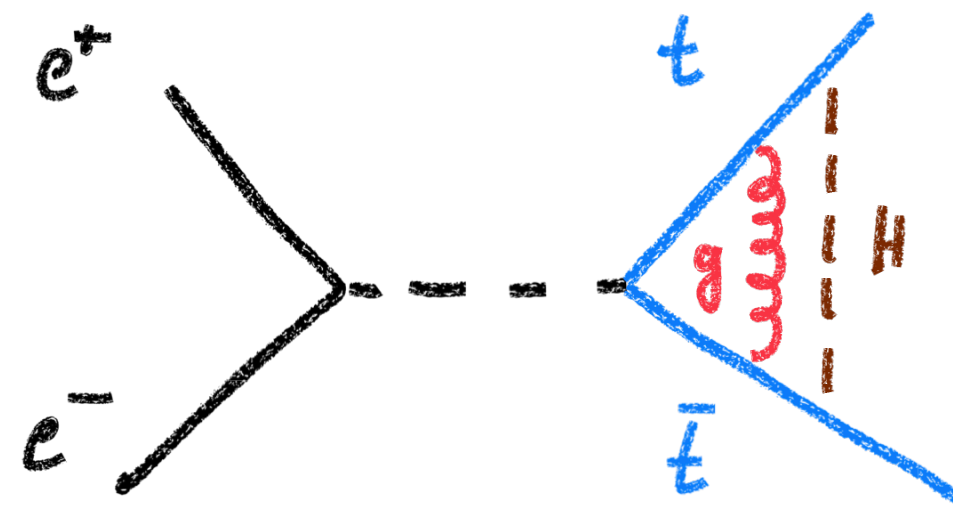
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The Top Quark Mass

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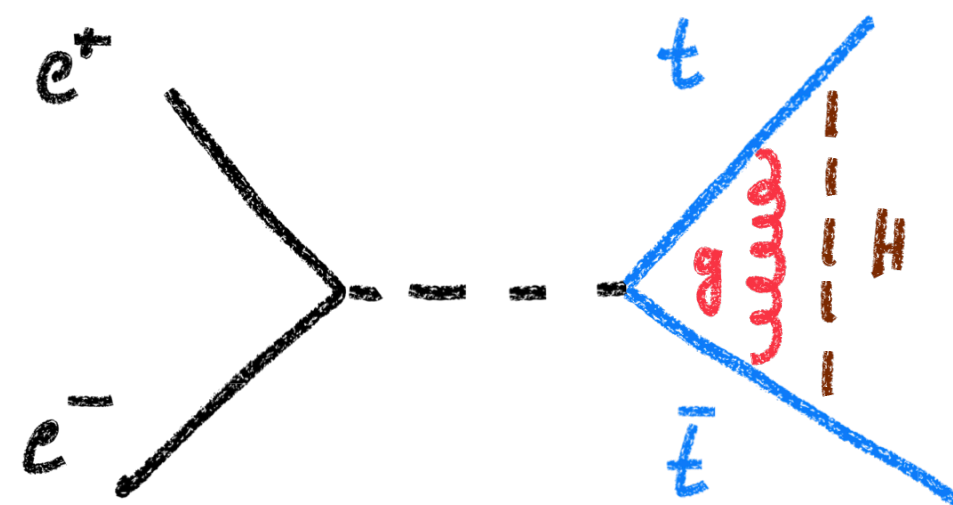
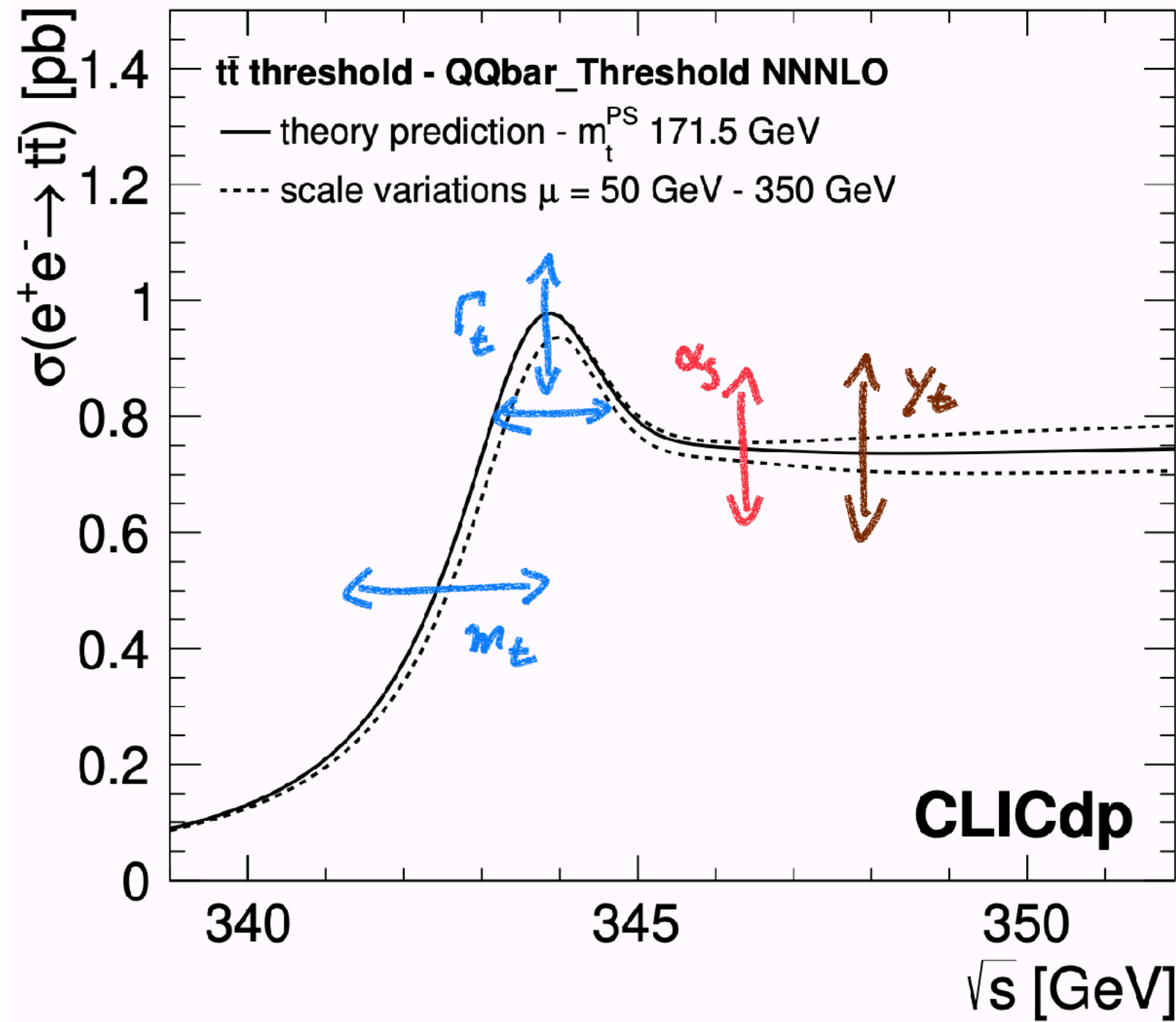
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The Top Quark Mass

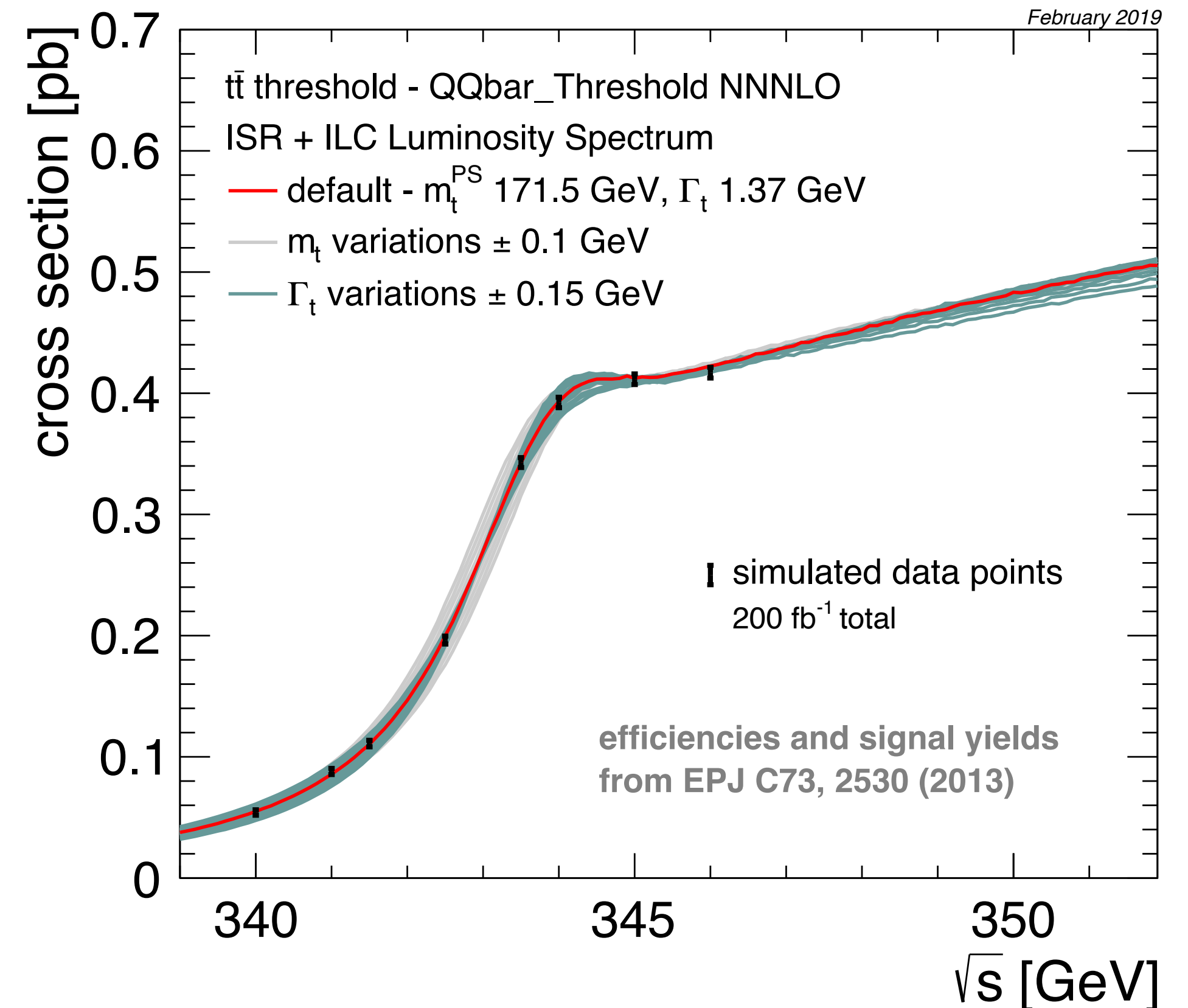
Ultimate precision at the threshold



- Exploit precise theoretical calculations of cross section in the threshold region, in well-defined mass schemes (m_t^{PS} , $m_t^{1\text{S}} \dots$) -> Can be converted directly into MSbar mass.

ISR, luminosity spectrum, reconstruction

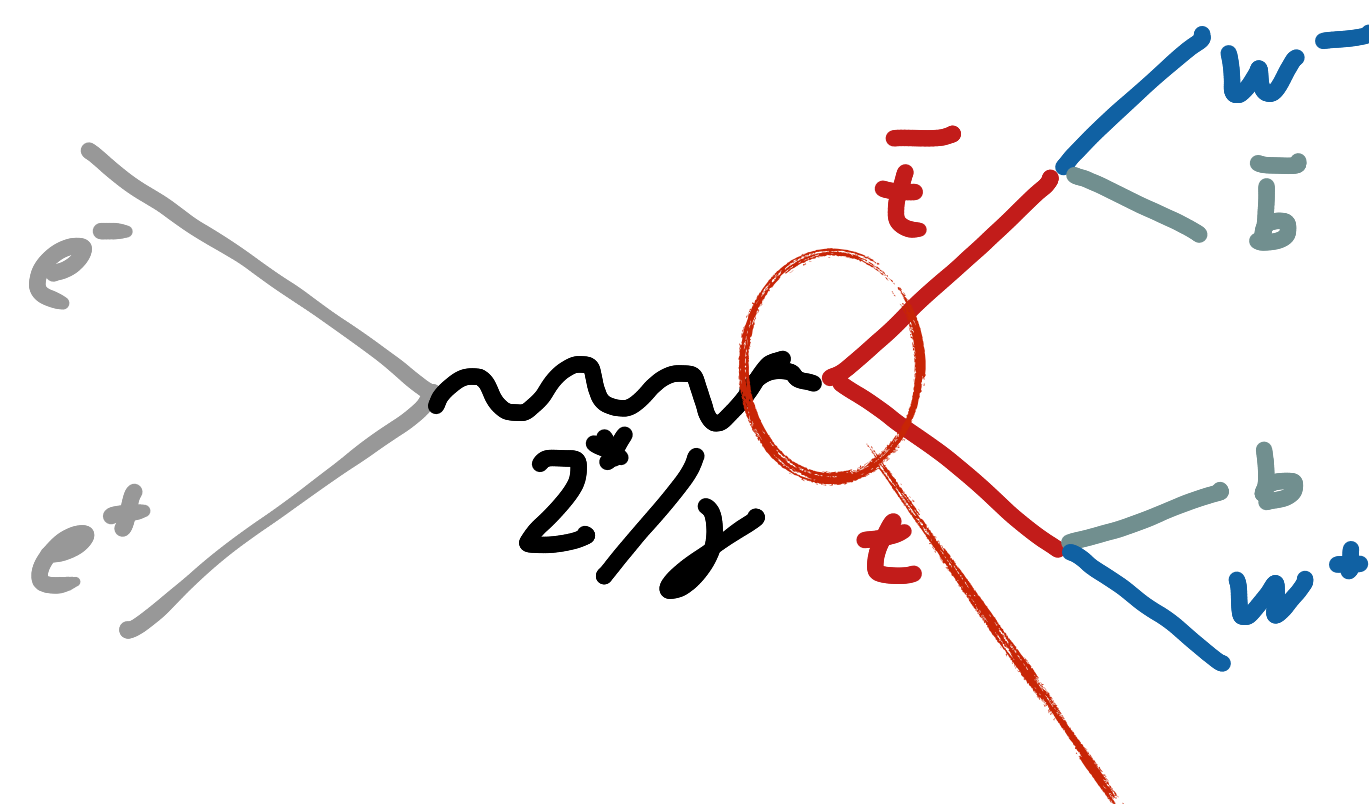
The potential for a measurement of the mass with < 50 MeV total uncertainty (dominated by theory) - stat. precision ~ 10 MeV



The threshold is sensitive to top quark properties

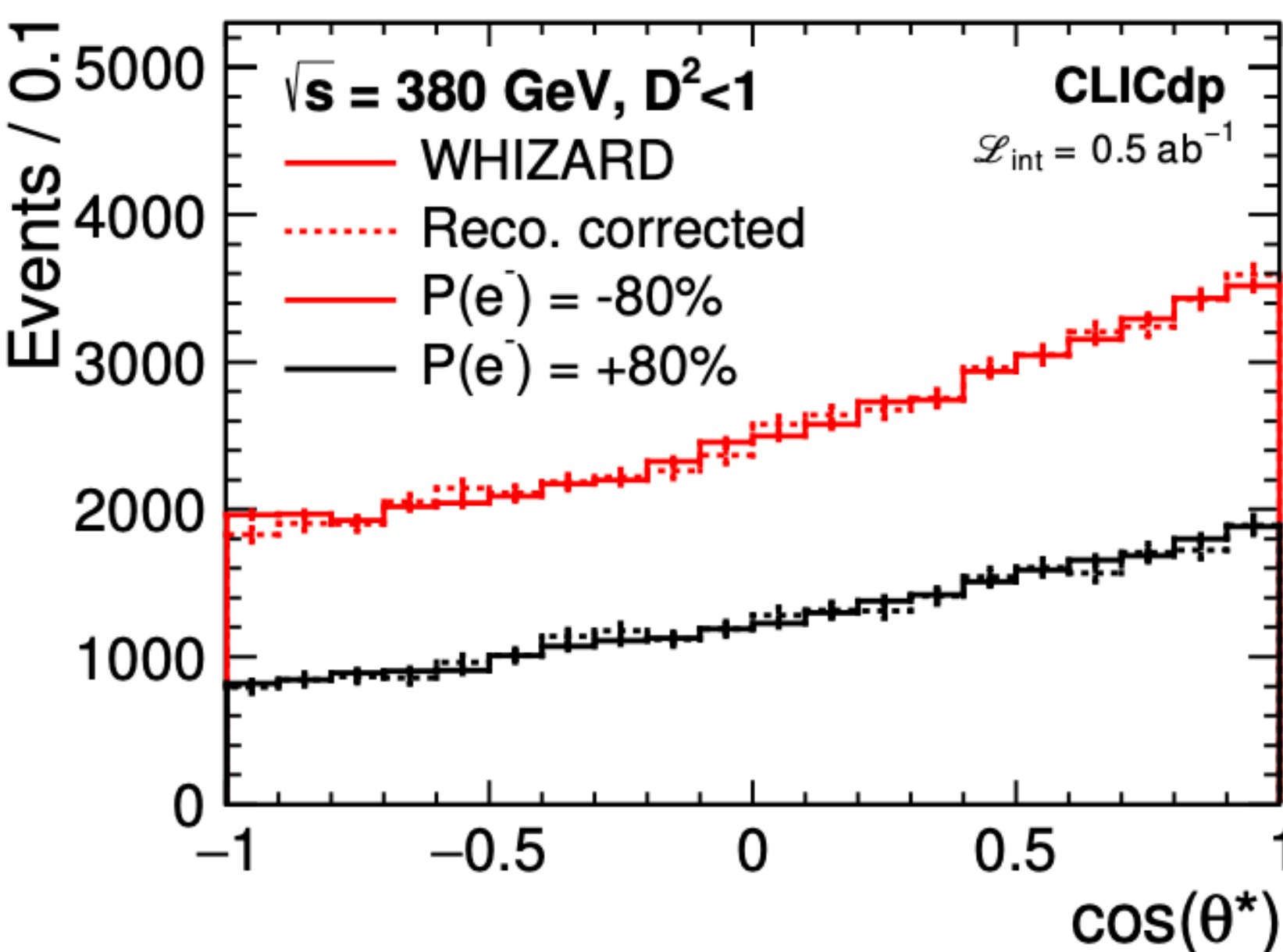
Electroweak Couplings of the Top Quark

Access via cross section and asymmetries



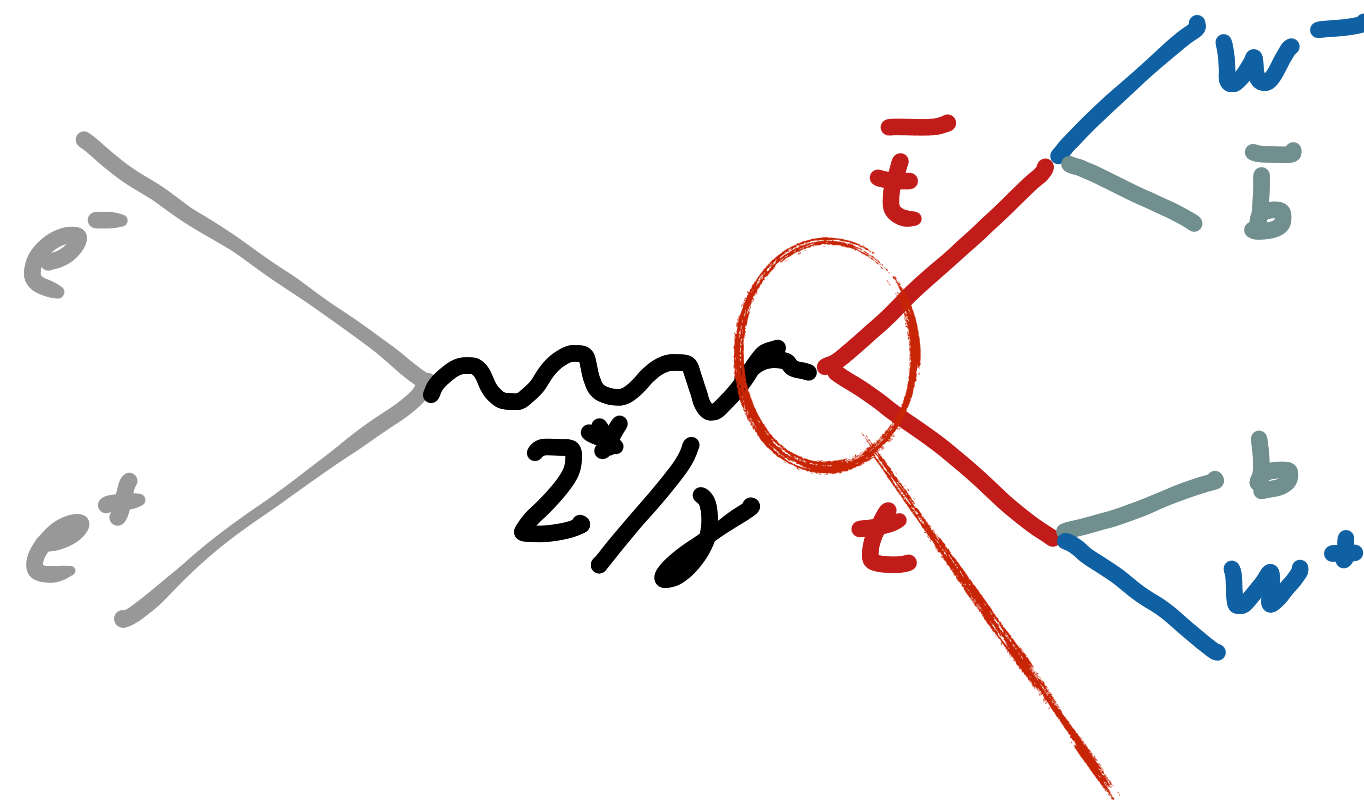
- At Linear Colliders:
 - Using different beam polarisations
 - Measuring cross section, A_{FB} , and helicity angle (some studies)
 - Particularly powerful with two (or more) energy points

Accessing electroweak couplings in $t\bar{t}b\bar{b}$



Electroweak Couplings of the Top Quark

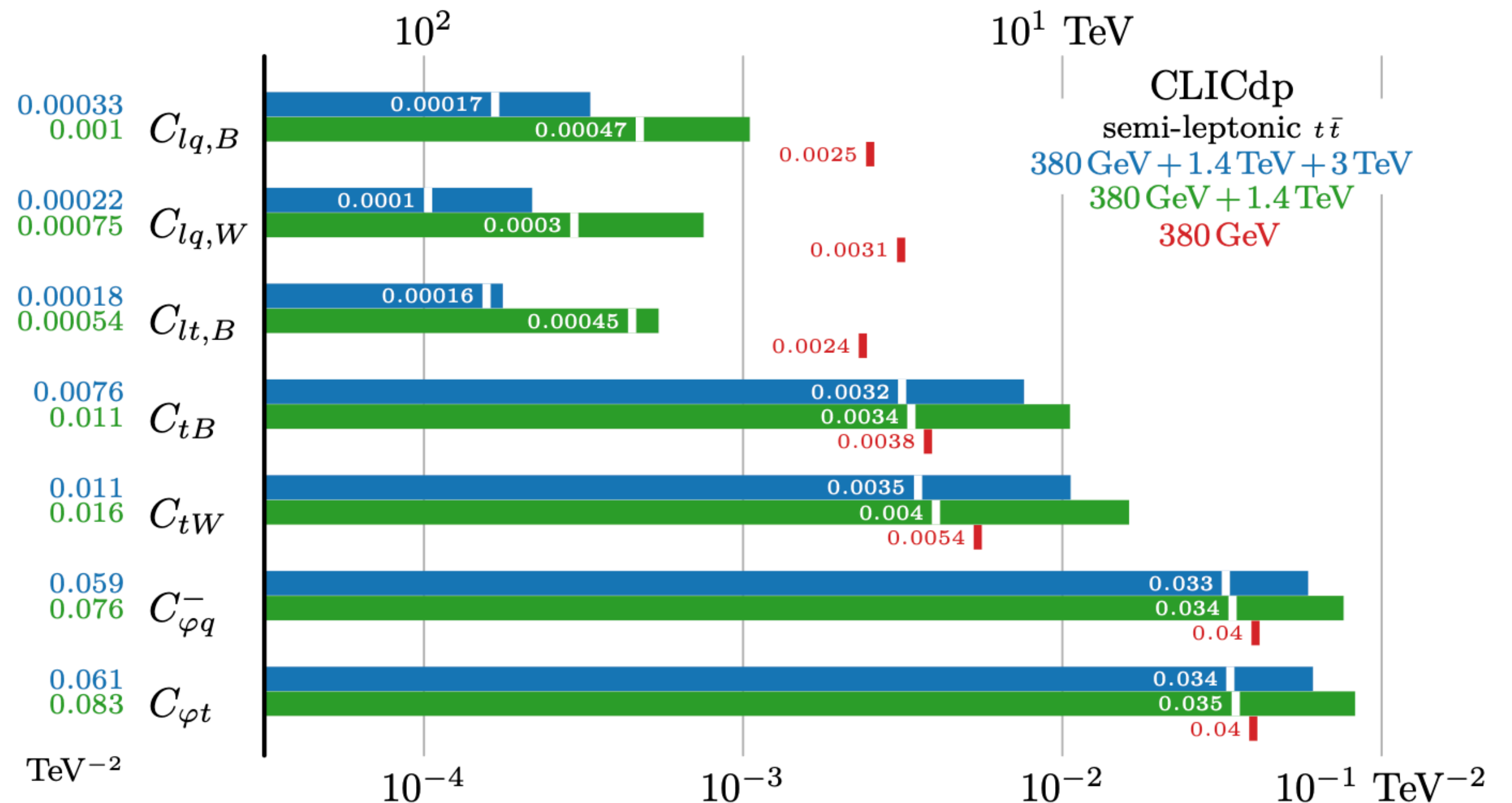
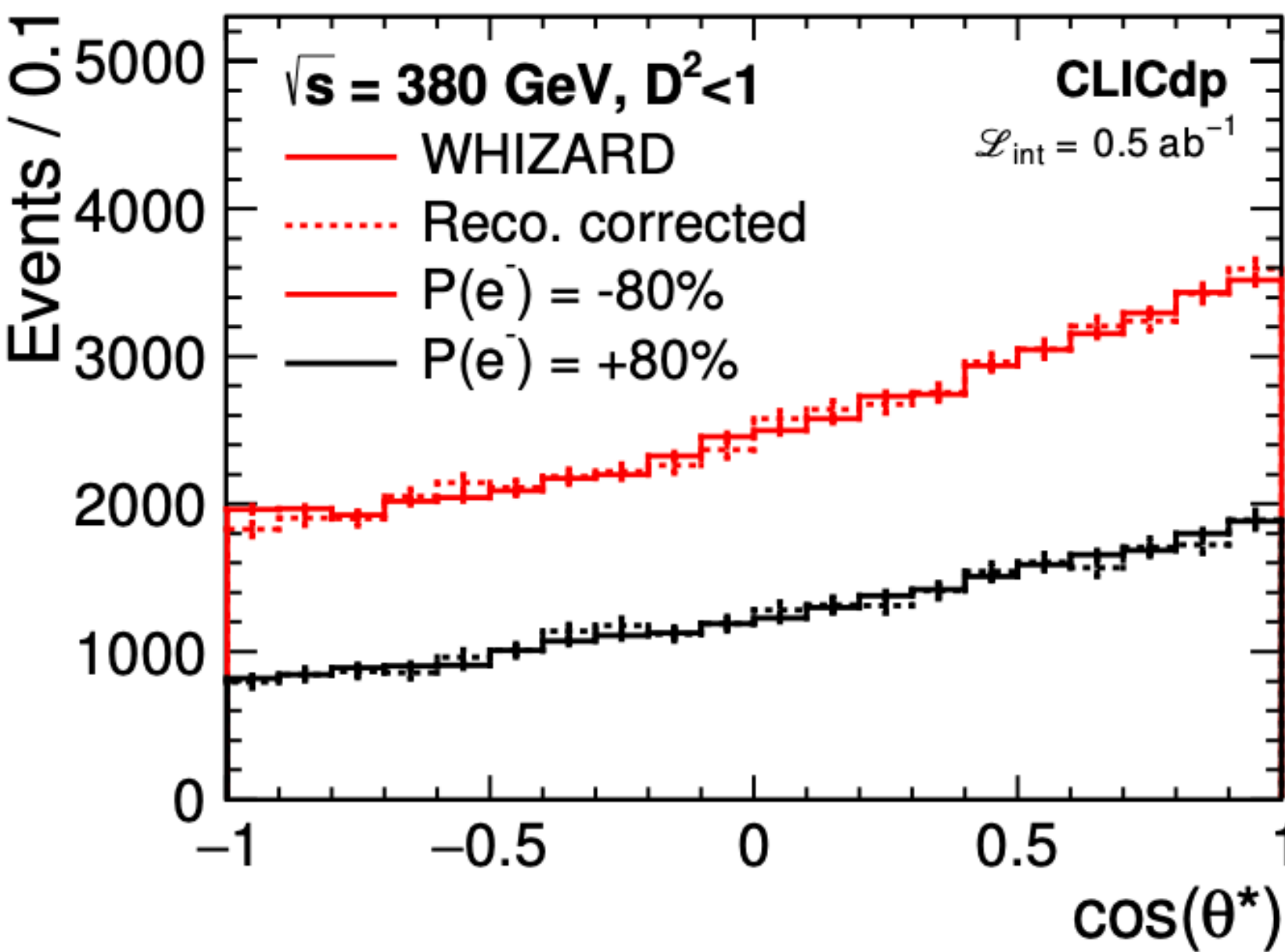
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Accessing electroweak couplings in $t\bar{t}b\bar{b}$

- At Linear Colliders:
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As an example: CLIC EFT-interpretation -> Reach up to 100 TeV



Into the Unknown

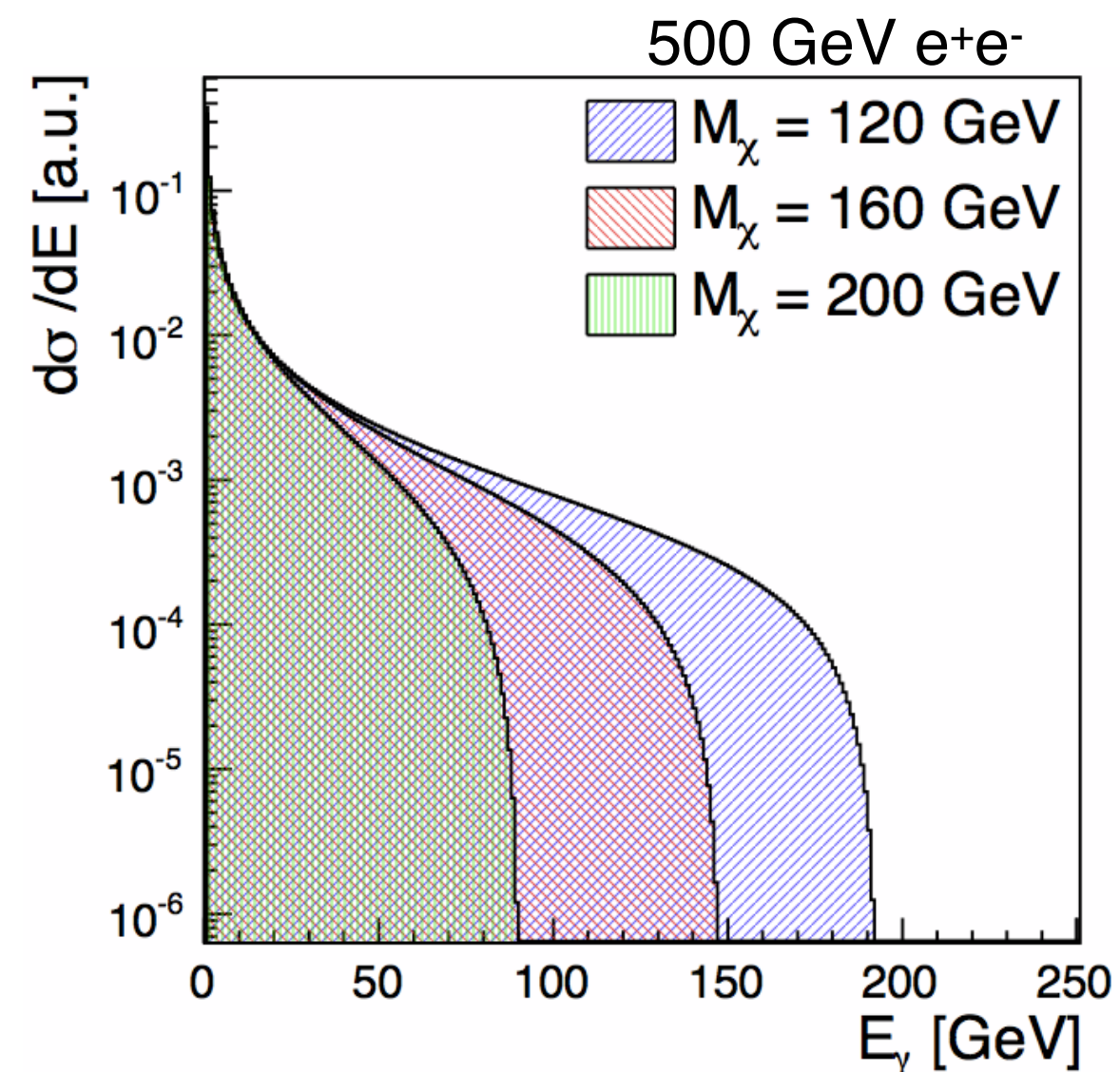
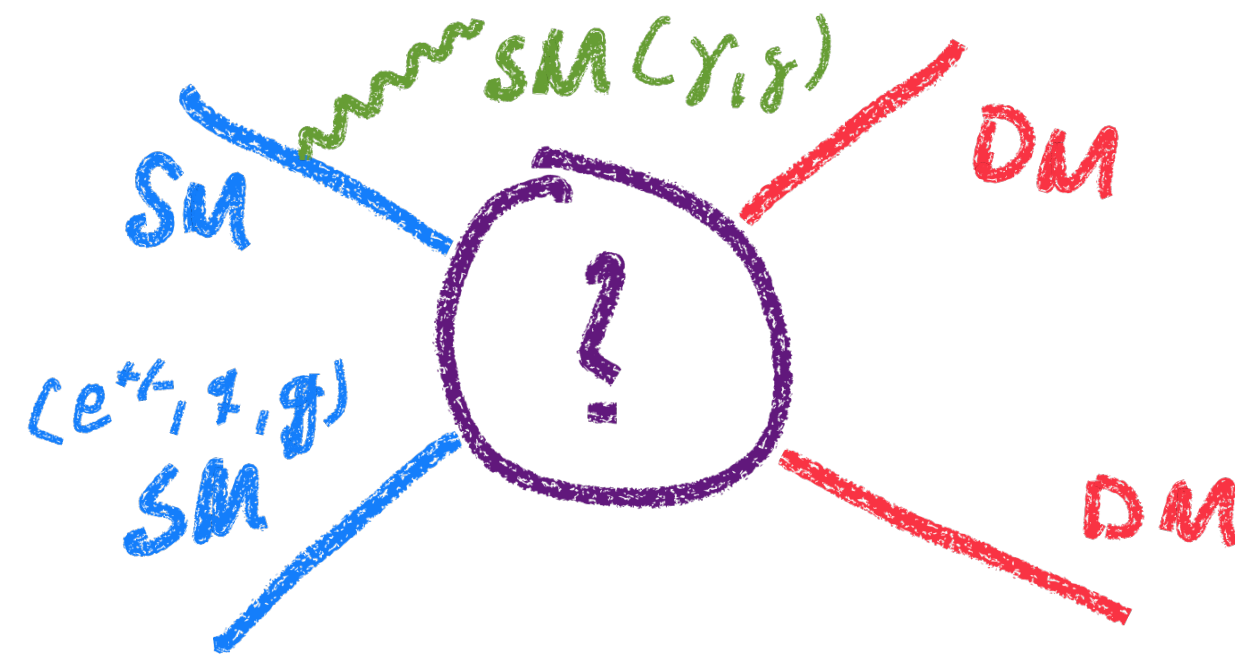
Searching for New Physics

Into the Unknown

Searching for Dark Matter

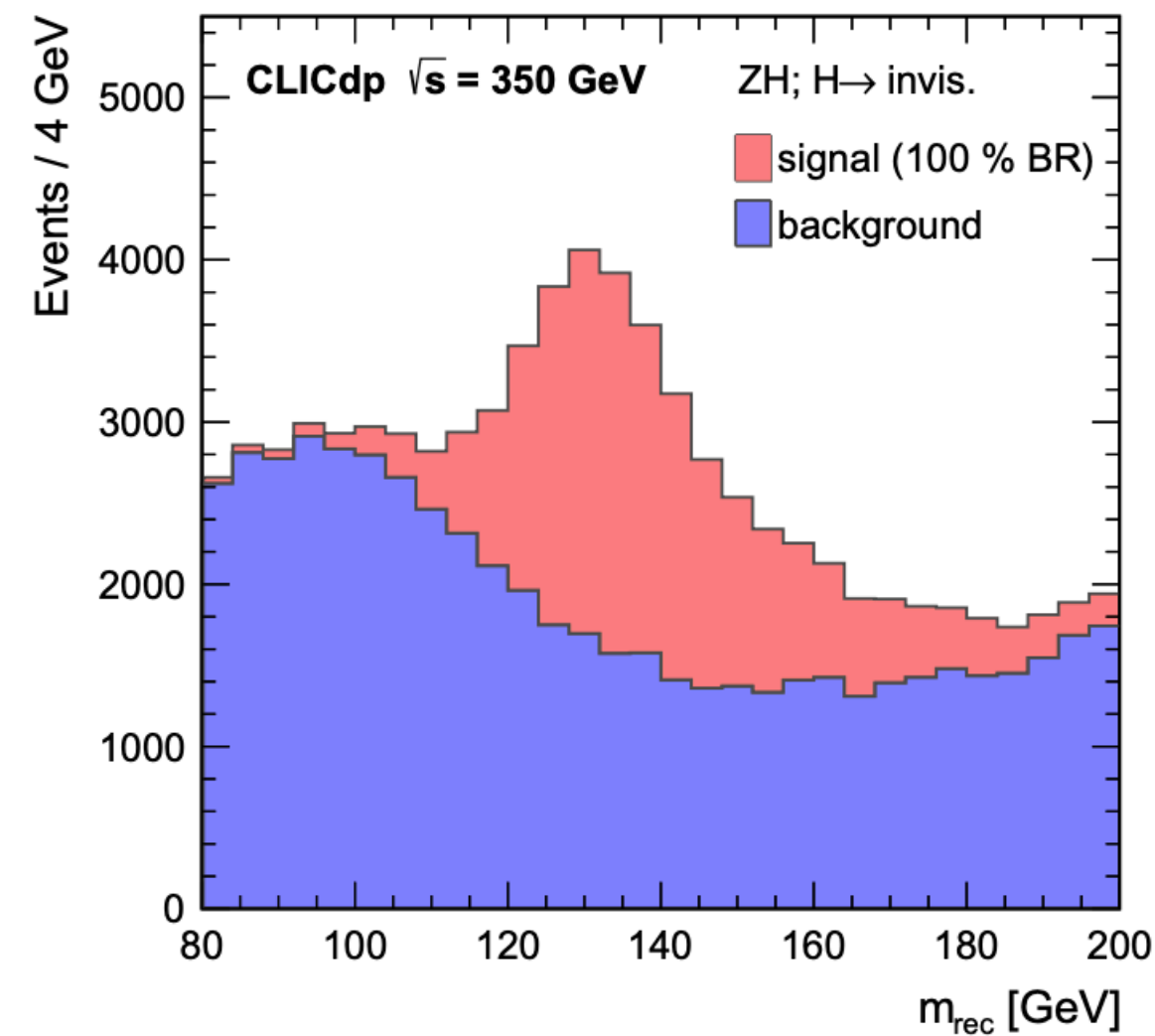
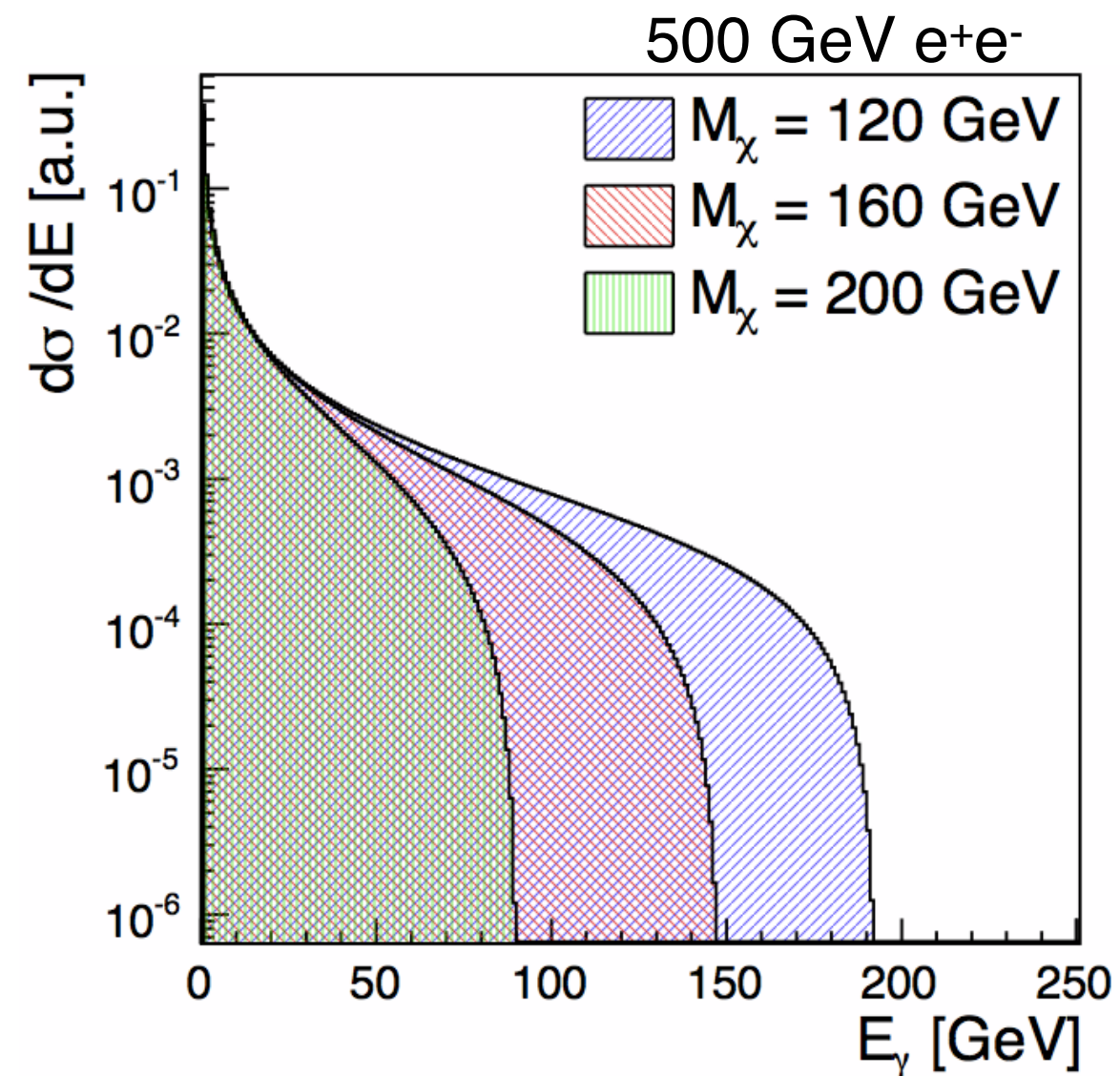
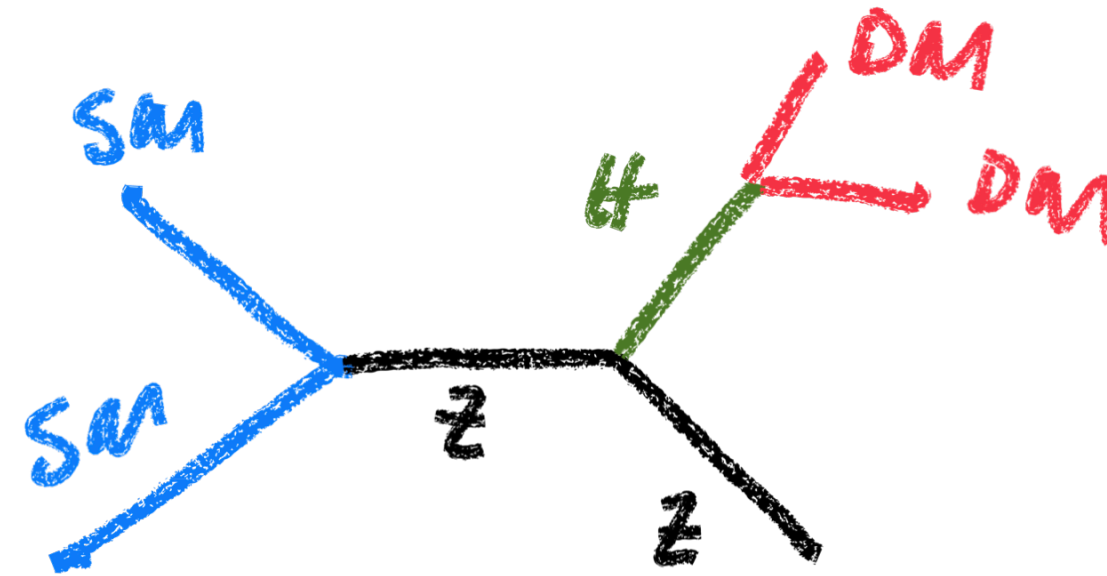
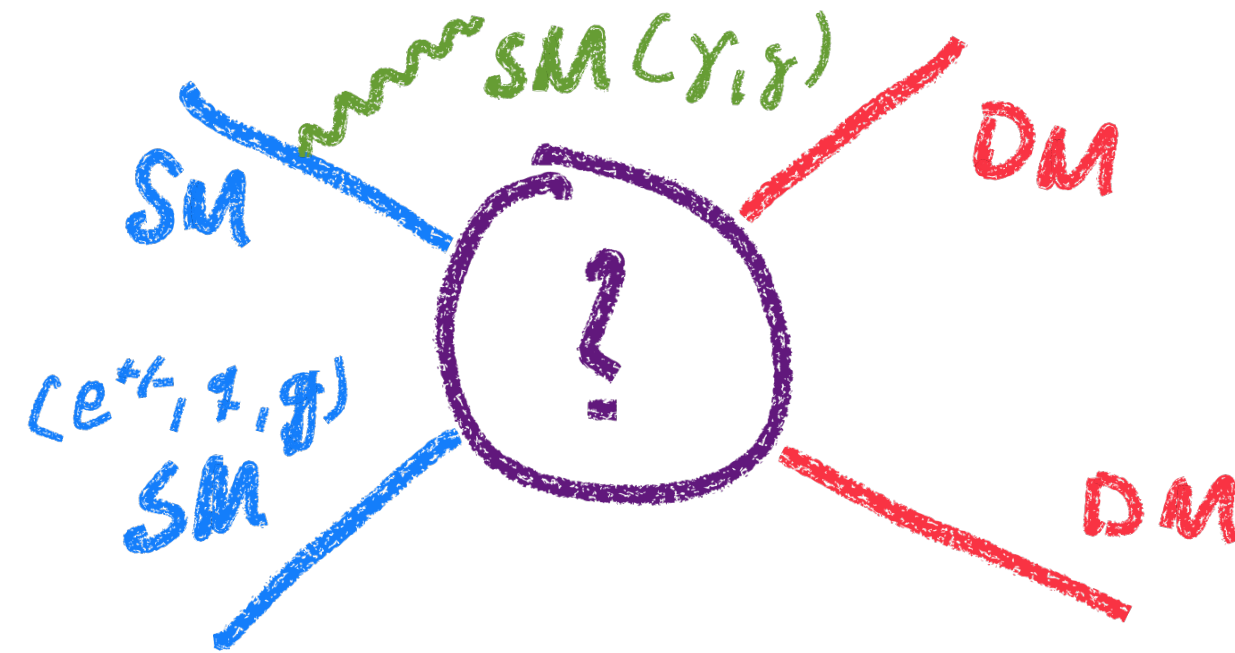
- A (very) wide range of possibilities - a few obvious examples:

Search for Dark Matter



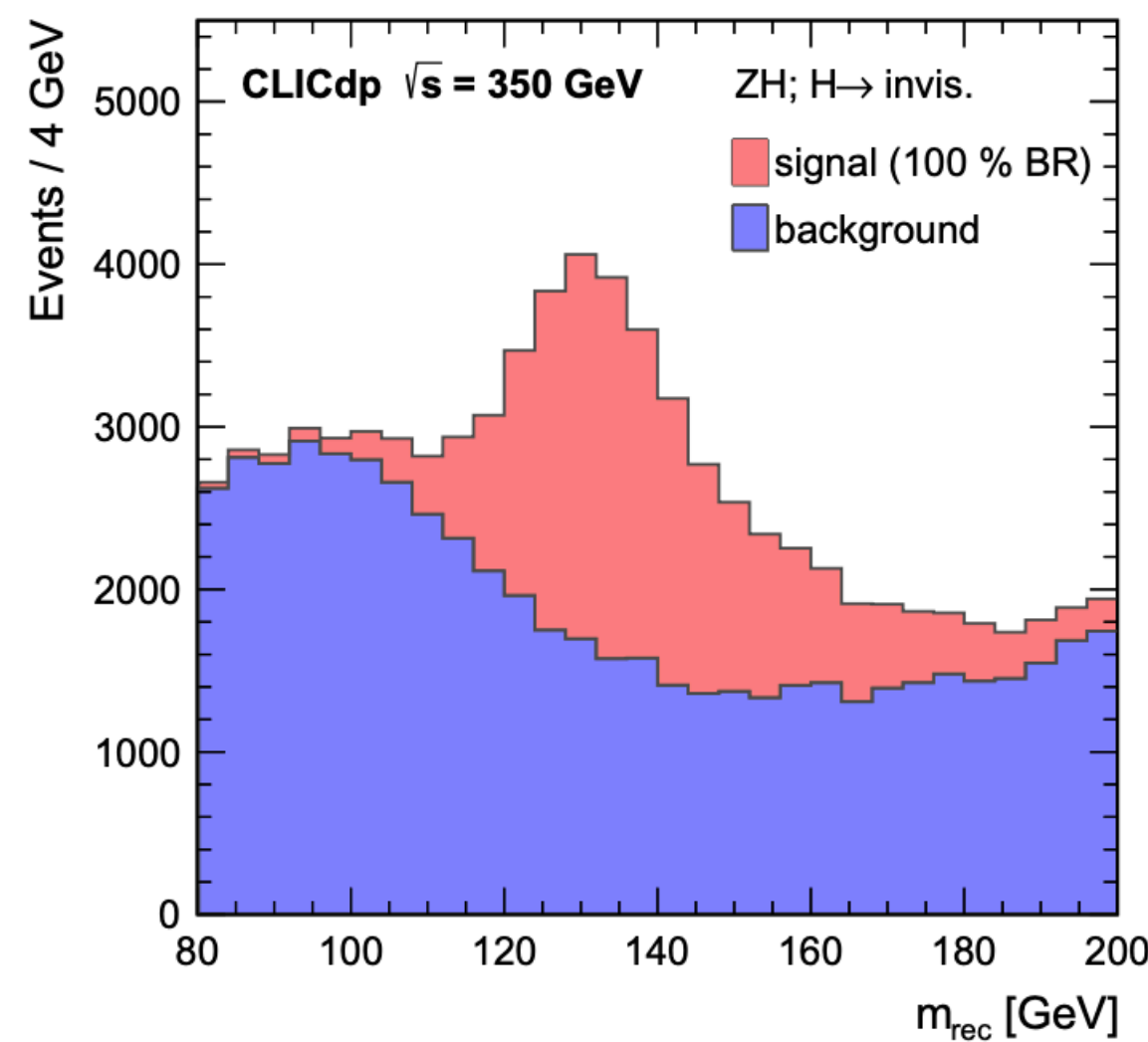
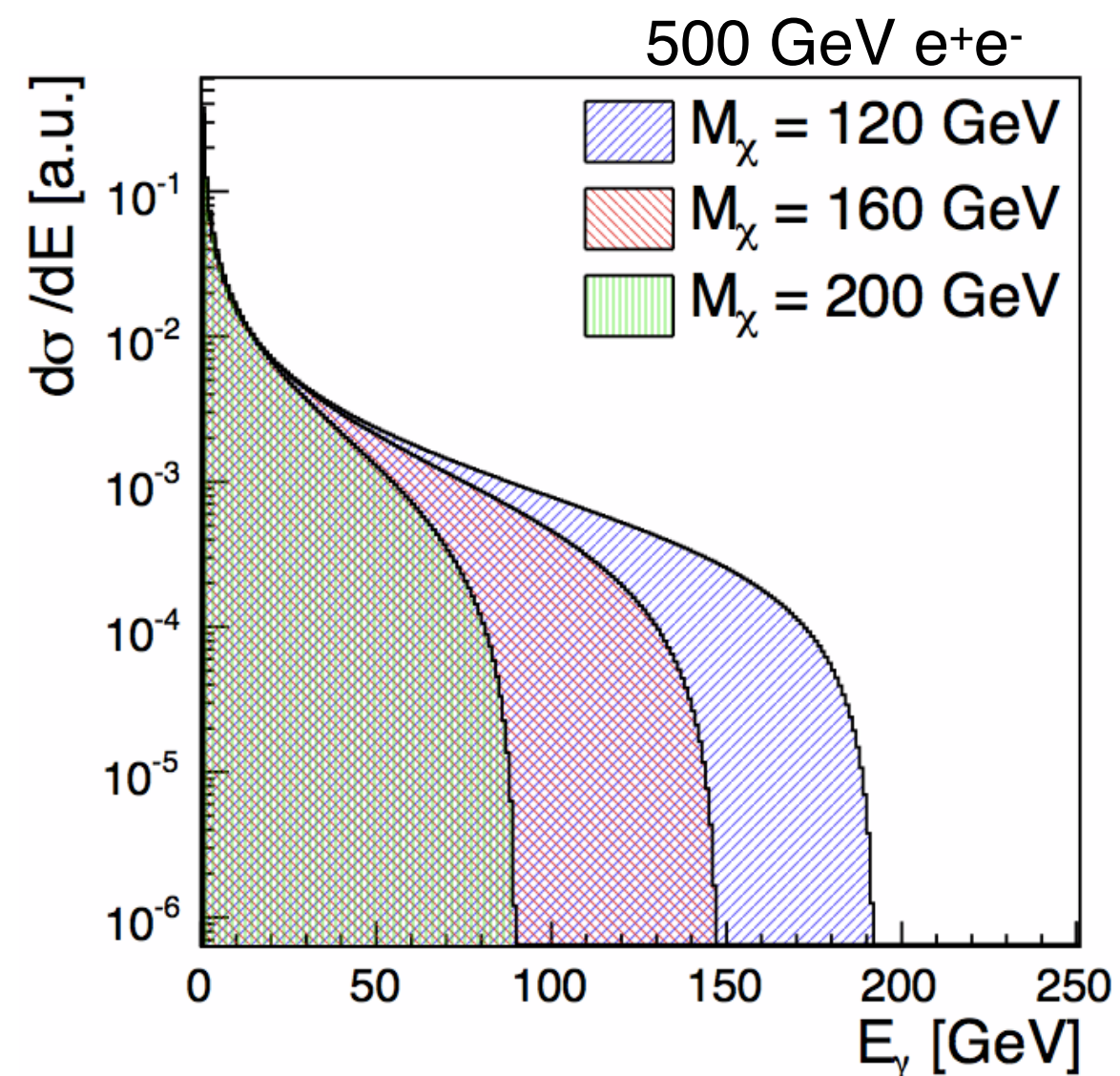
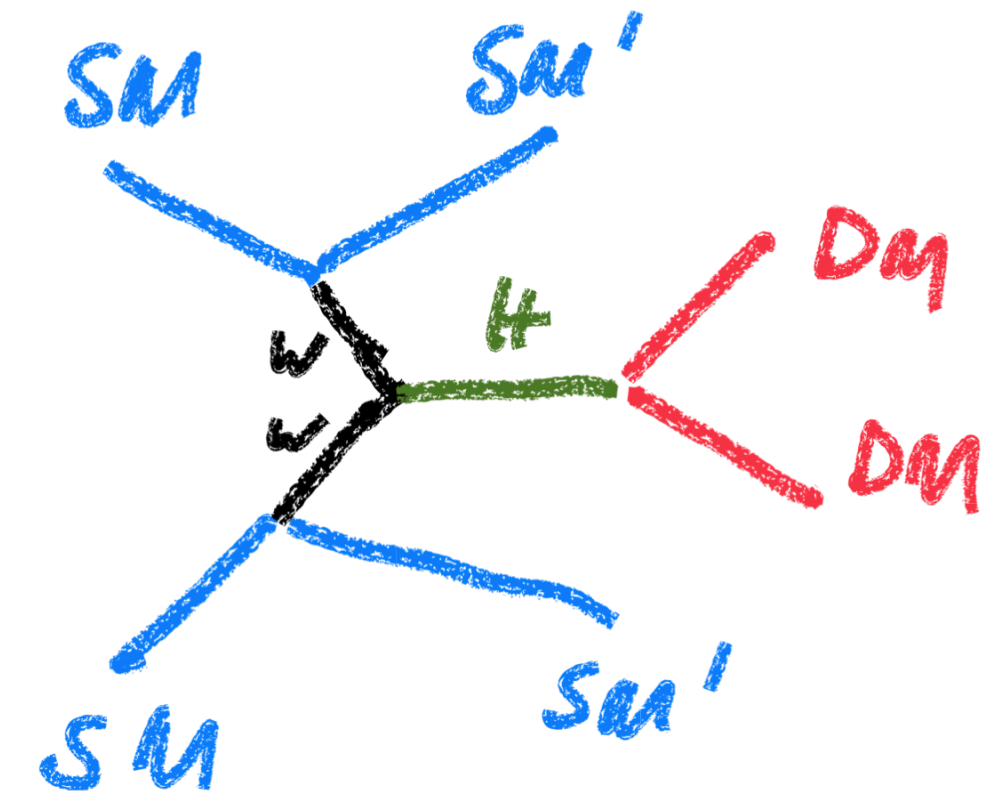
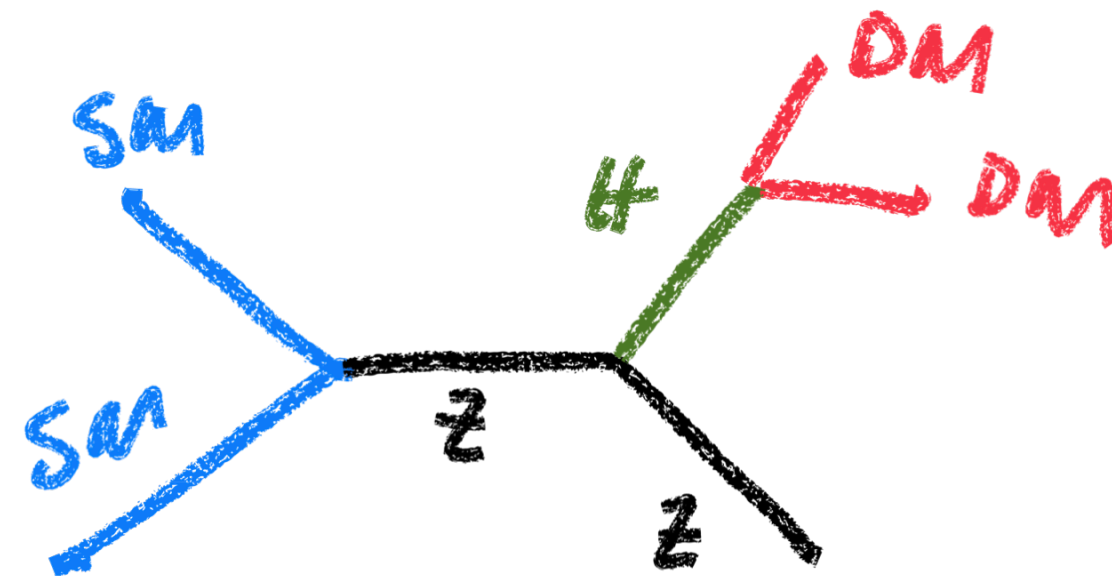
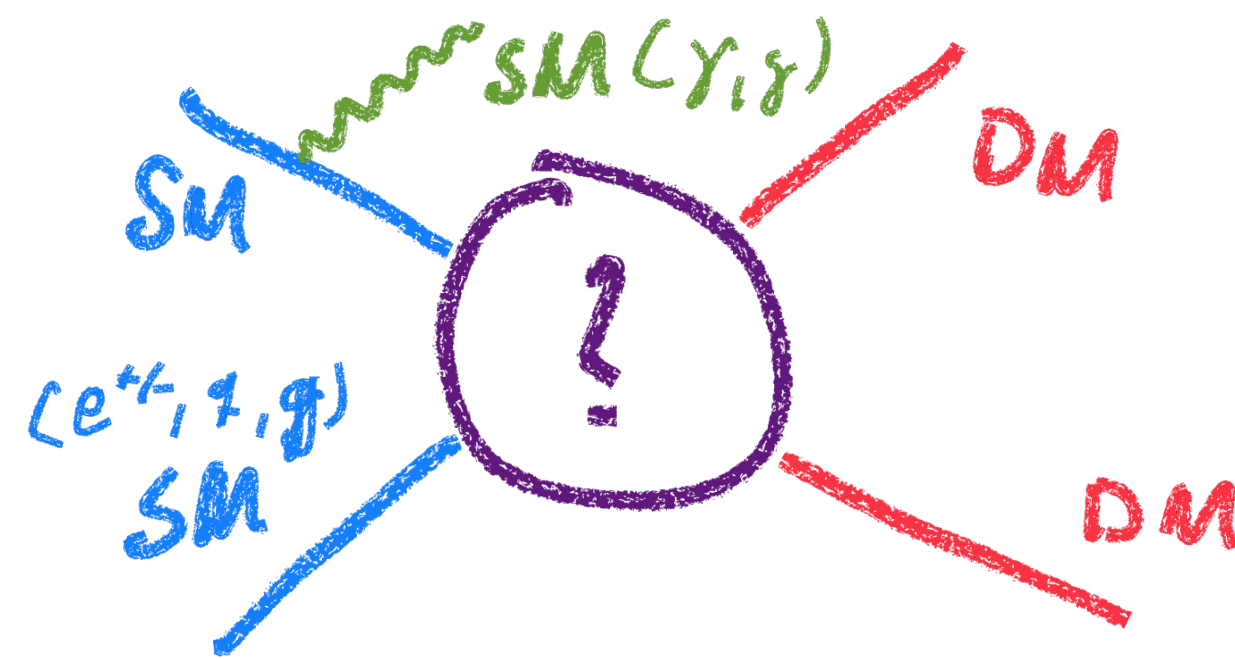
- A (very) wide range of possibilities - a few obvious examples:

Search for Dark Matter



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Search for Dark Matter

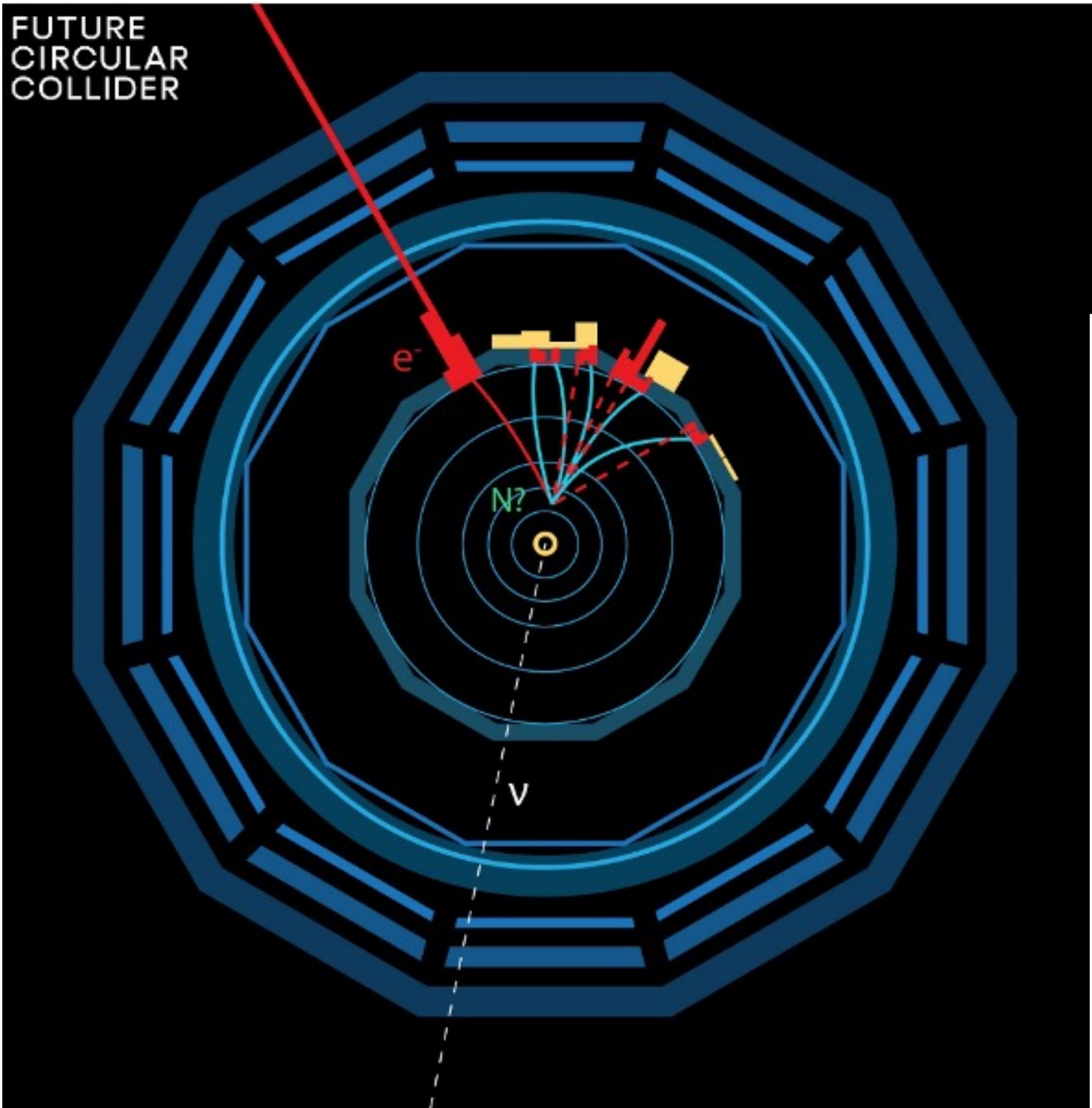


Sensitivity depends on

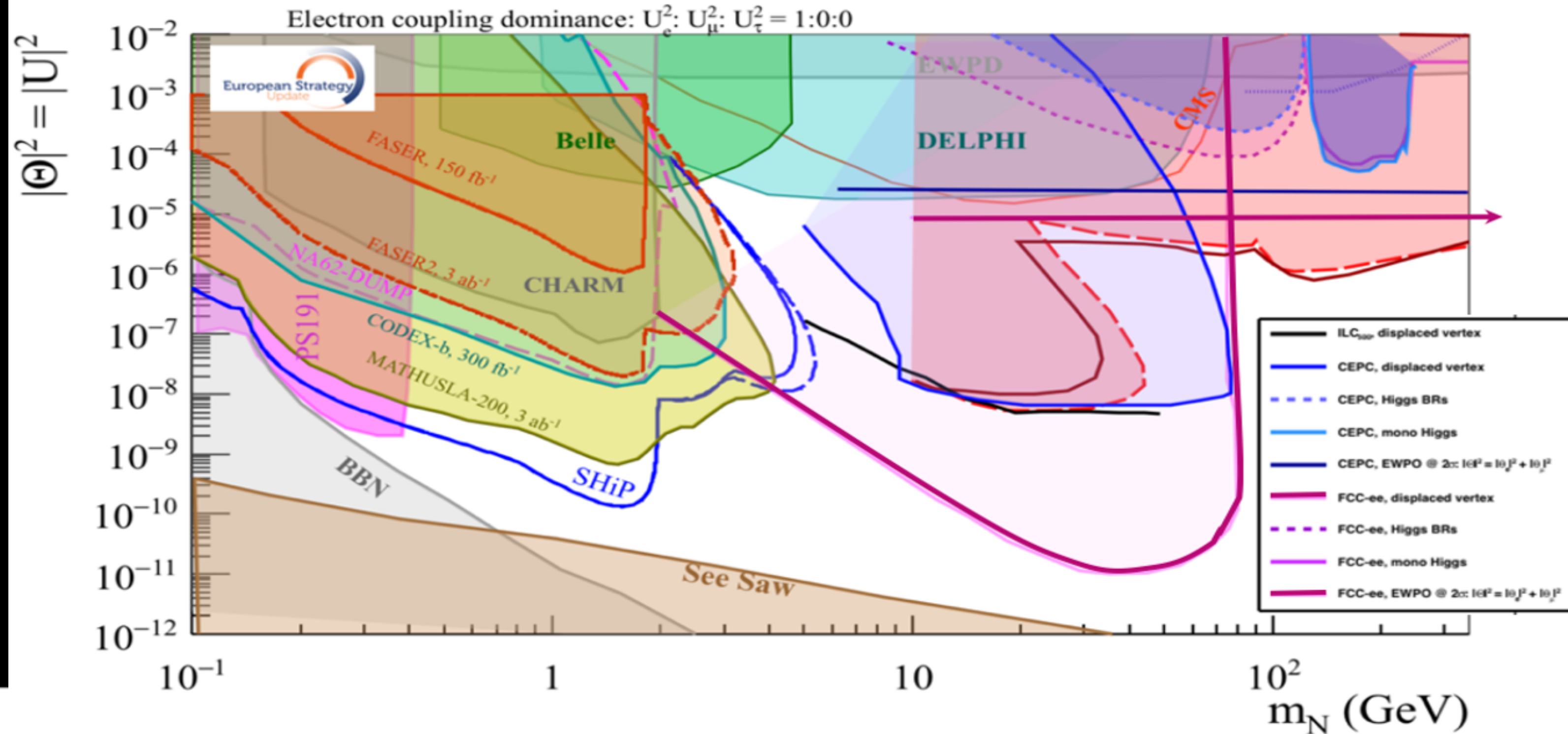
- Energy reach -> Mass coverage
- Background levels: Sensitivity to small couplings

Into the Unknown

Dark Sector Searches - an FCC-ee example

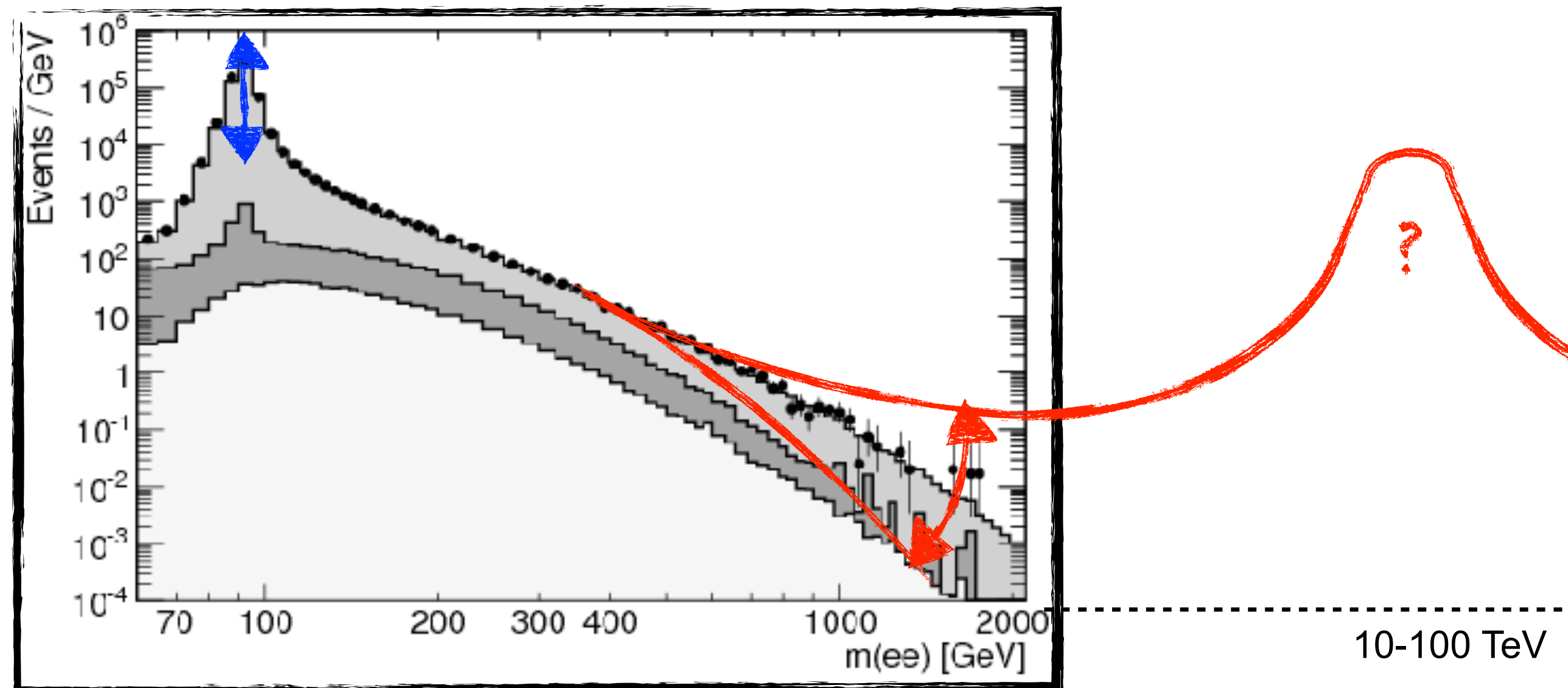


- Exploiting extreme statistics to search for heavy neutral leptons (right-handed sterile neutrinos, ...): $Z \rightarrow \nu + \text{HNL}$



mass vs mixing² - unique phase space covered by FCC-ee

- Indirect probes with lepton colliders



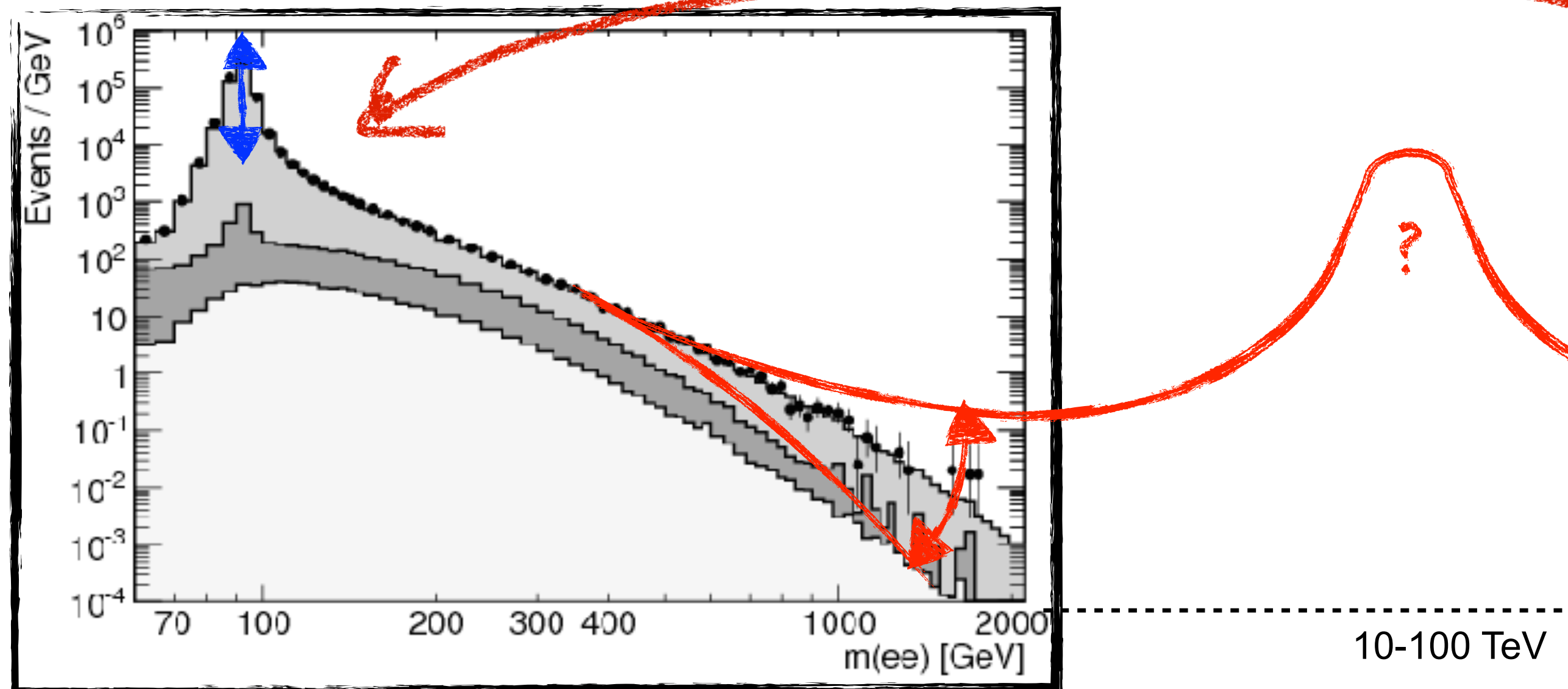
For many generic models & new interactions:
Corrections to SM suppressed by $1/(\text{mass scale})^2$

⇒ Sensitivity grows with s

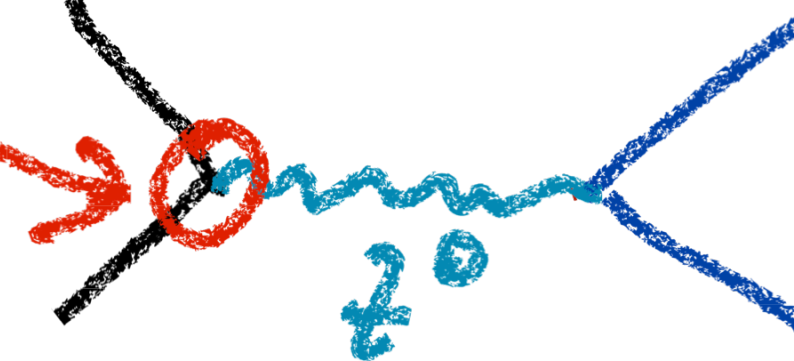
Into the Unknown

Indirect and direct exploration of the highest energy scales

- Indirect probes with lepton colliders



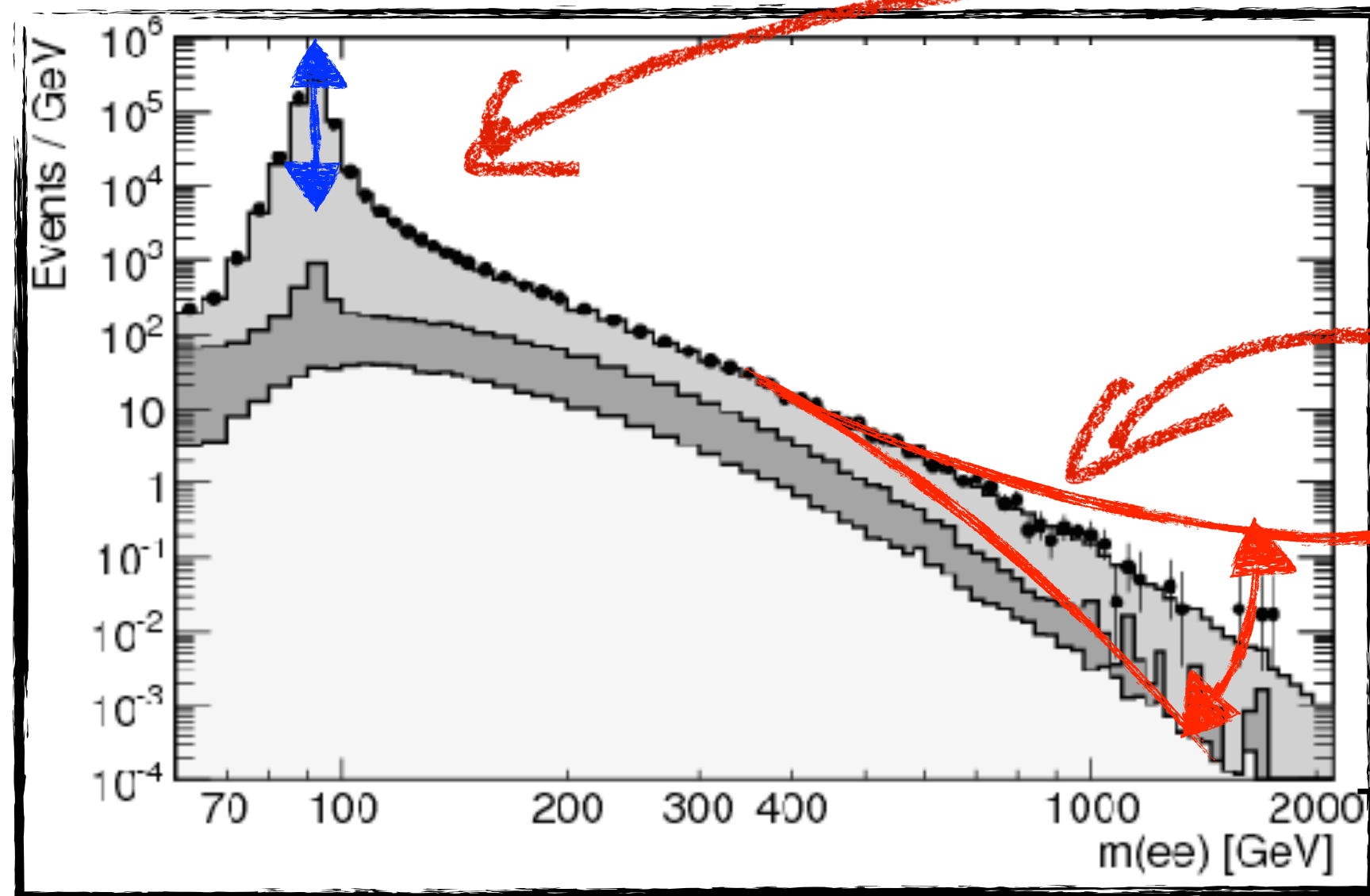
extreme precision with Z-pole programs
(and other measurements we talked about)



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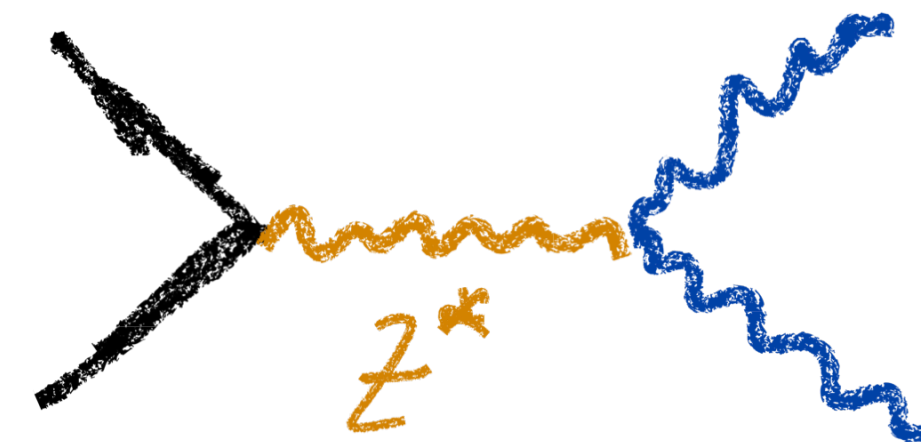


10-100 TeV

extreme precision with Z-pole programs
(and other measurements we talked about)



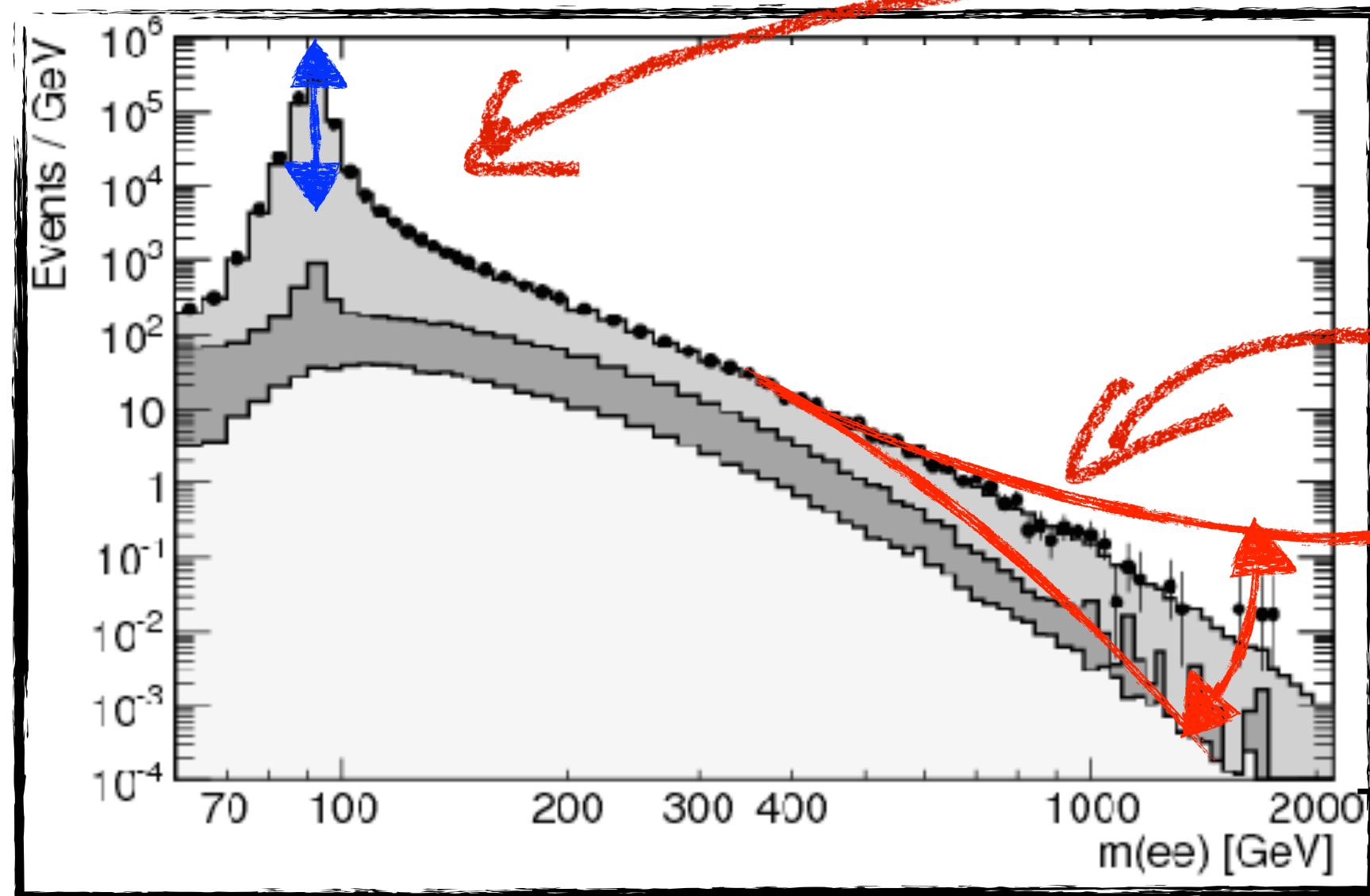
larger effects at higher energies



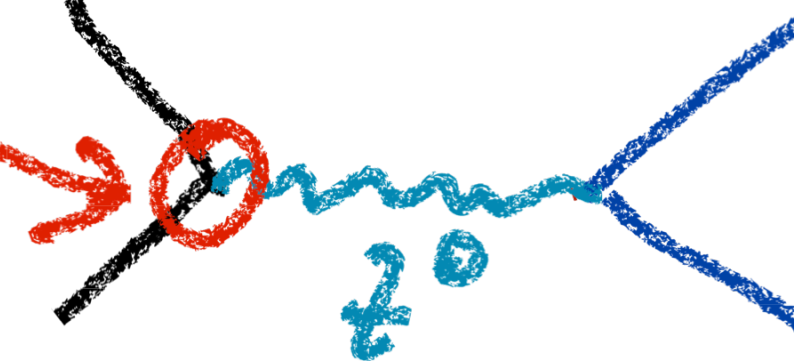
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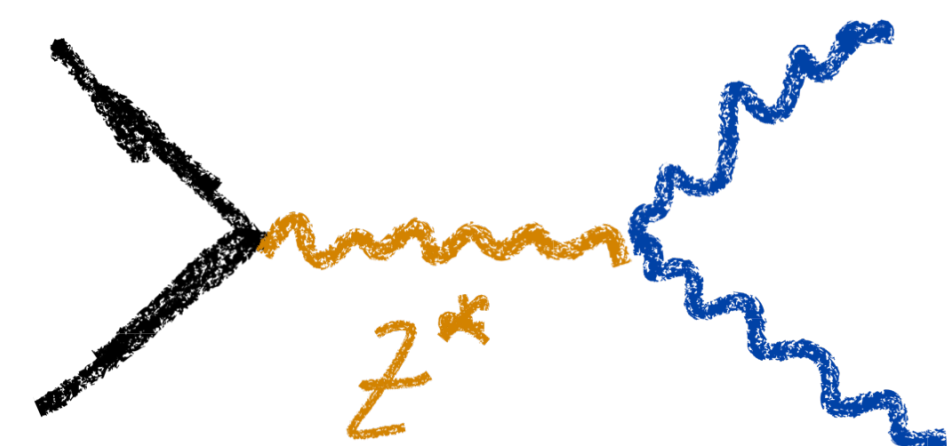
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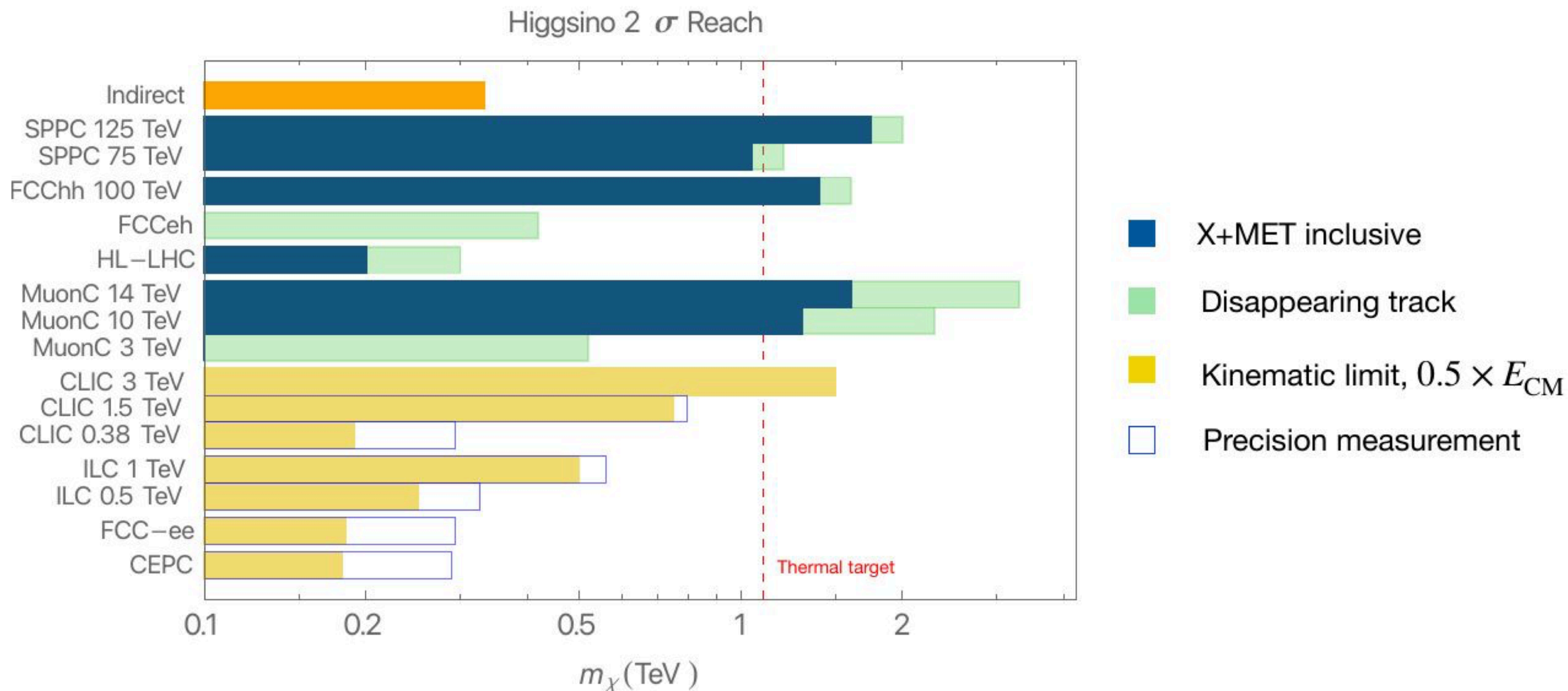
For many generic models & new interactions:
 Corrections to SM suppressed by $1/(\text{mass scale})^2$
 ⇒ Sensitivity grows with s

Potential for direct production at highest energies - primarily hadron colliders, or 10+ TeV muon colliders

Sensitivity to High Scales

The Strength of CLIC and Muon Colliders

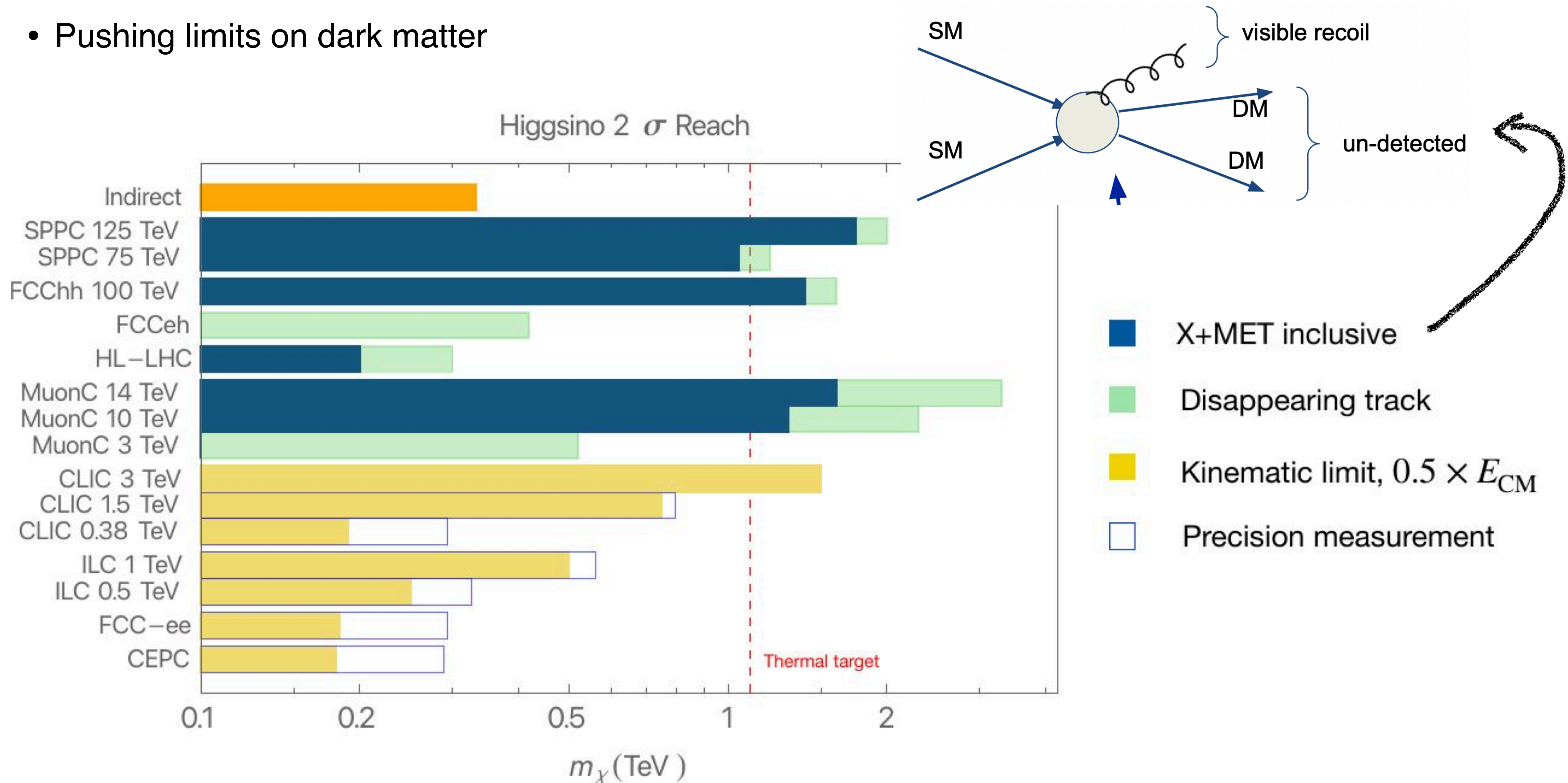
- Pushing limits on dark matter



Sensitivity to High Scales

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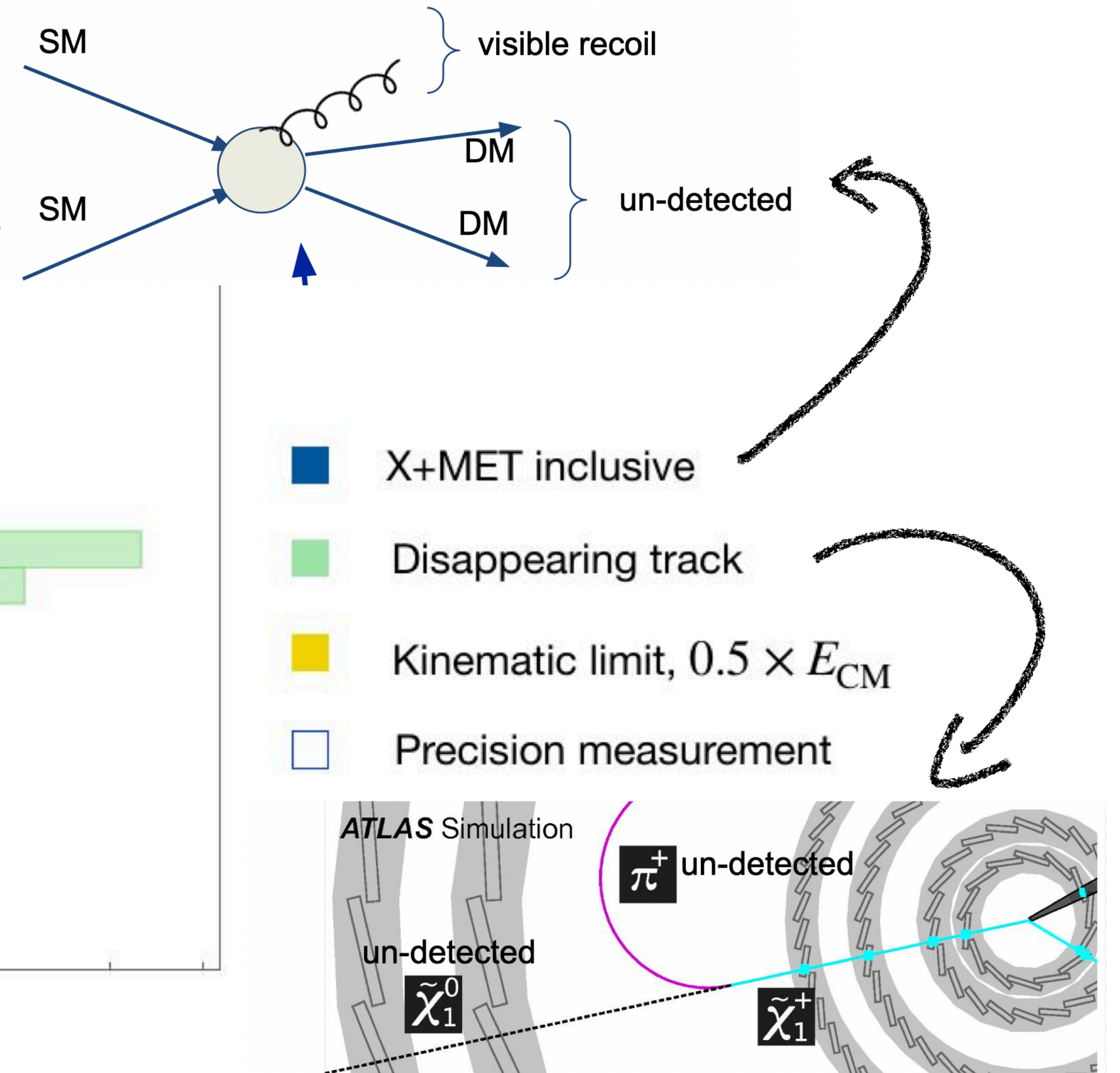
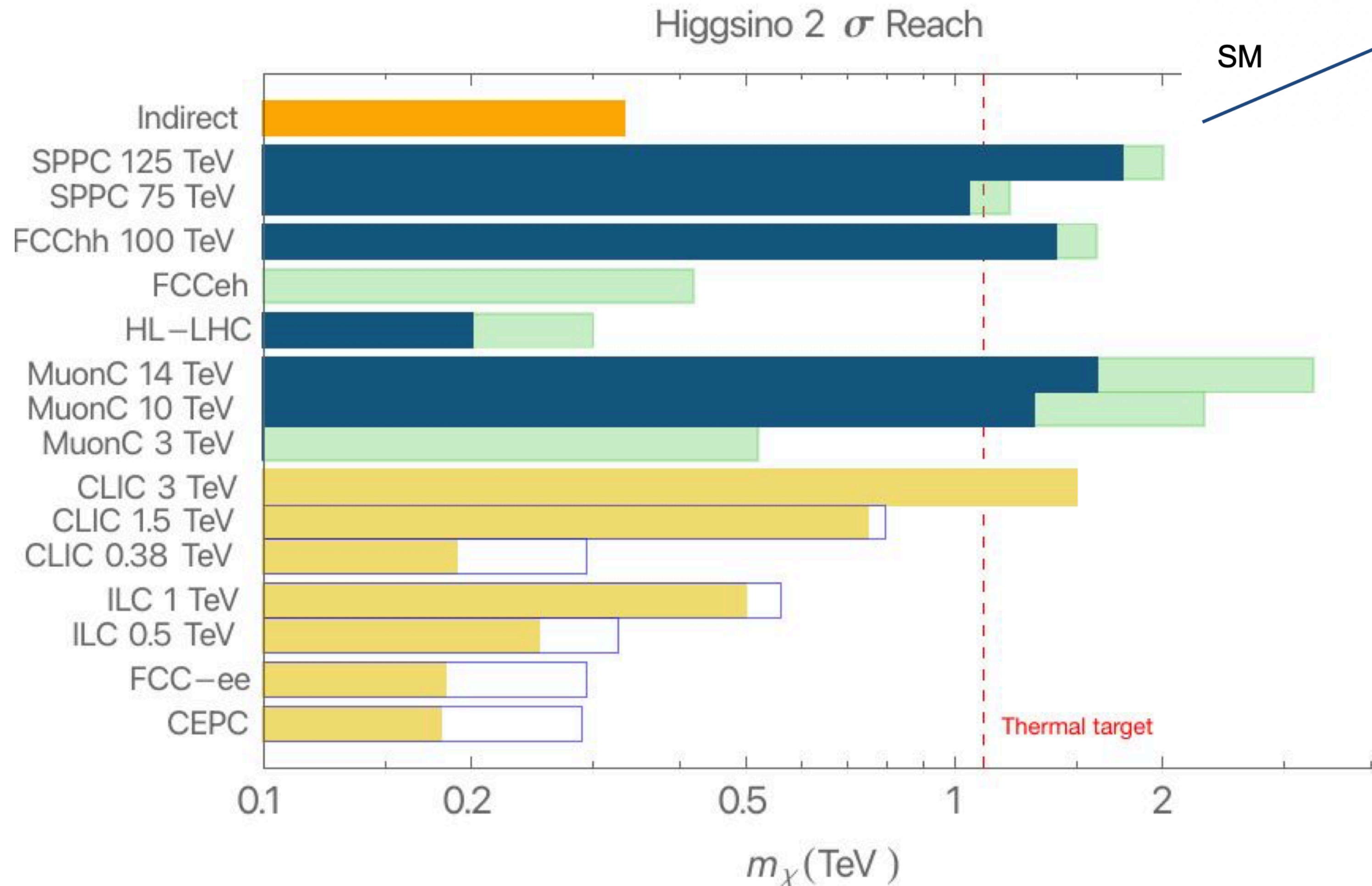
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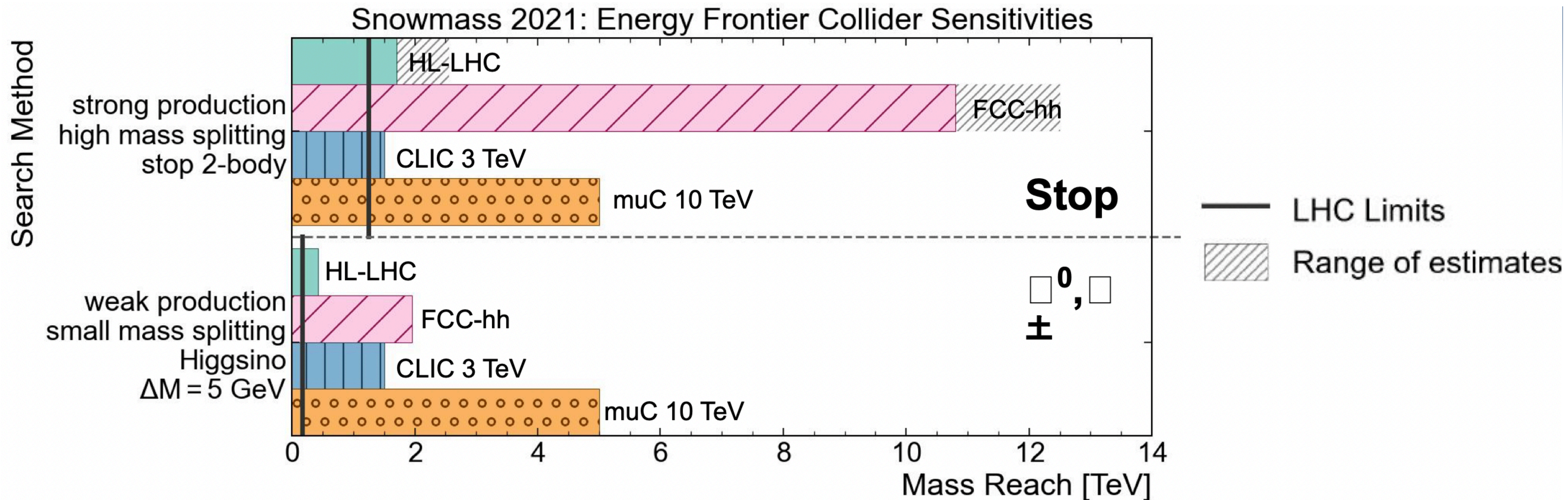
- Pushing limits on dark matter



Sensitivity to High Scales

The Strength of CLIC and Muon Colliders

- Discovery potential for new particles - SUSY as an example



Lepton colliders: Full collision energy available for new particles -> Sensitivity up to kinematic limit.

Conclusions

Wrapping up

- An e^+e^- collider operating around 250 - 380 GeV will provide a model-independent, precise investigation of the Higgs sector, and studies of unprecedented precision of the top quark
- A revisit to the Z pole with much higher luminosity than LEP will enable to electroweak precision tests of the Standard Model at completely new levels. At the same time, this will also be a high-statistics flavour physics program.
- Scales in the TeV region and above can directly be probed by high-energy lepton colliders - CLIC, a (multi-)TeV ILC, and a muon collider. This also includes the measurement of the self-coupling of the Higgs.

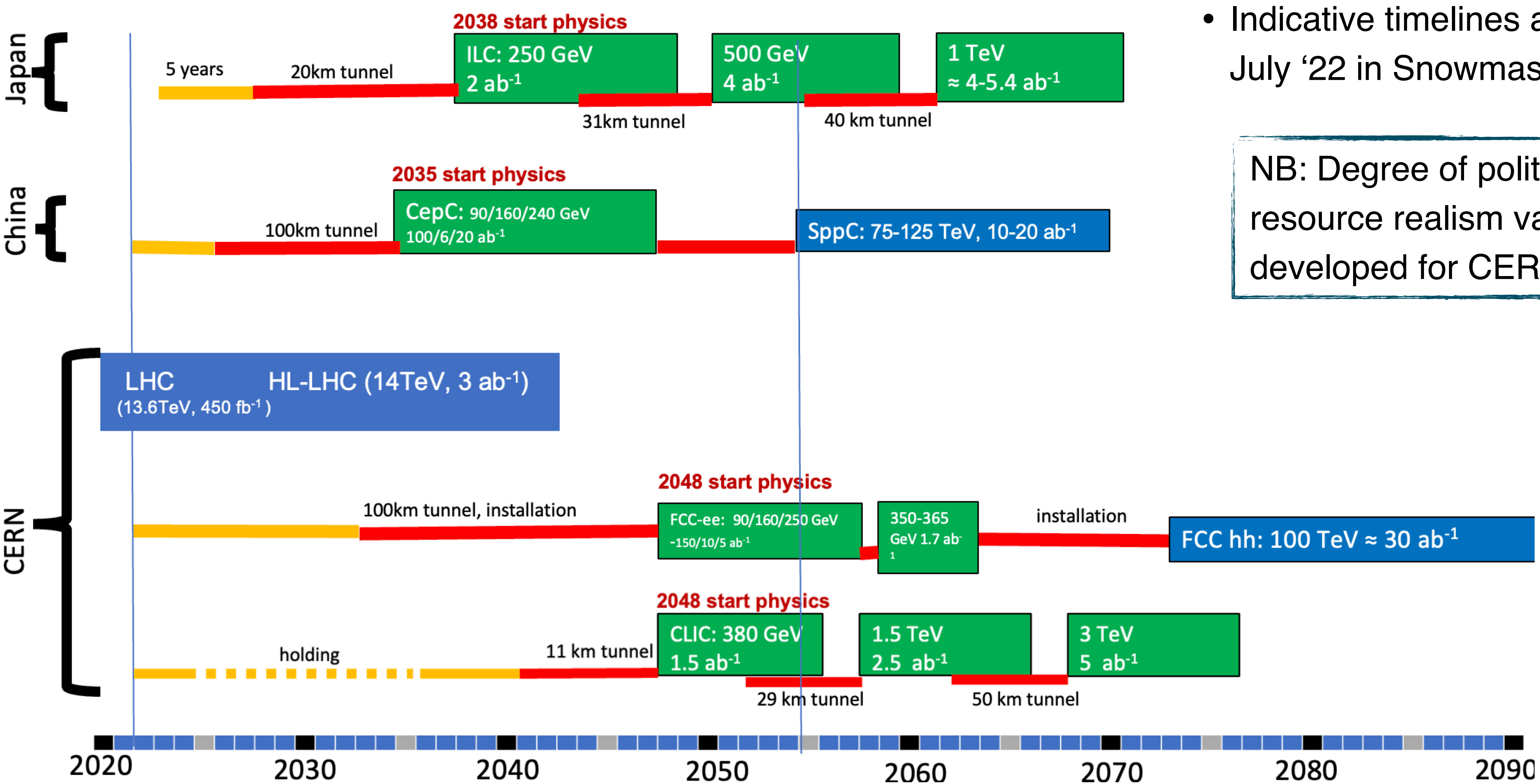
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CERN is currently studying the feasibility of the **Future Circular Collider**:

- An e^+e^- machine running from the Z-pole up to 365 GeV - precision Higgs, Top, Electroweak.
- Followed by a ~ 100 TeV hadron collider - exploration of the highest energy scales, measurement of the self-coupling of the Higgs.
- **CLIC** is studied as “Option B” in case FCC cannot go forward.

The Way Forward

Strategies and Timescales - taken from last year's Snowmass Meeting

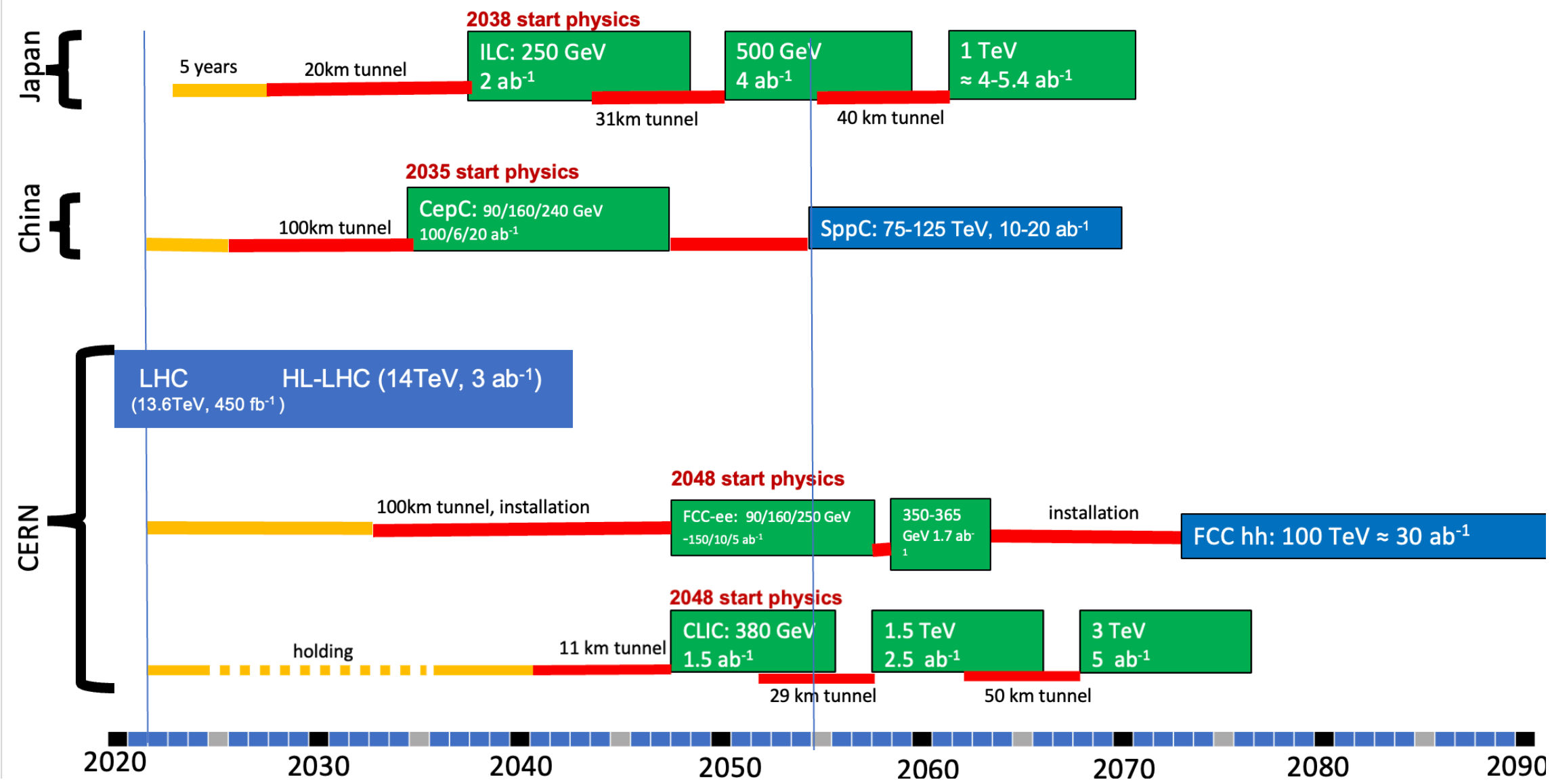


- Indicative timelines as discussed July '22 in Snowmass @ Seattle

NB: Degree of political and resource realism varies - most developed for CERN projects

The Way Forward

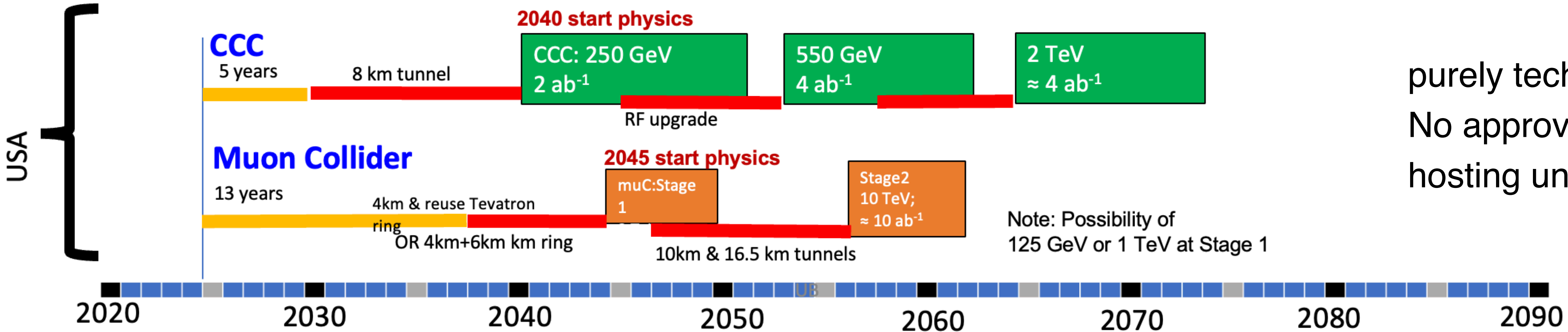
Strategies and Timescales - taken from last year's Snowmass Meeting



- Indicative timelines as discussed in Snowmass @ Seattle

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Proposals emerging from this Snowmass for a US based collider



purely technical!
No approval process yet,
hosting unclear

There are very exciting questions in high energy physics - a new e^+e^- collider may answer some of them!

Global large projects = long time scales - but contributions are needed now to make them happen.

This will be *your* HEP facility!

Extras Lecture 2

FCC-ee Time Line to Physics

Making a new facility happen

