



# Superconducting magnets for particle accelerators - 4

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# CONTENTS

- Accelerator magnets
  - Limits to highest field in Nb-Ti
  - Hints on Nb<sub>3</sub>Sn
- Hints on detector magnets
- Luminosity and operation
  - Luminosity definition and equation
  - Emittance, intensity and beam beam limit
  - Beta\*
  - Integrated luminosity
  - The present situation in the LHC





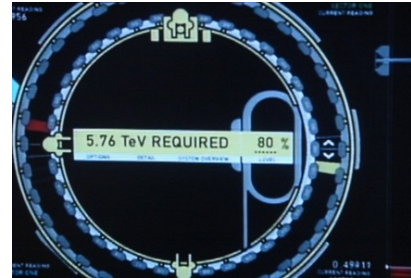
# INTERLUDE: THE TERMINATOR-3 ACCELERATOR

We apply some concepts to the accelerator shown in Terminator-3 [Columbia Pictures, 2003]

- Estimation of the magnetic field

$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$

- Energy = 5760 GeV
- Radius ~30 m
- Field =  $5760 / 0.3 / 30 \sim 700$  T (a lot !)



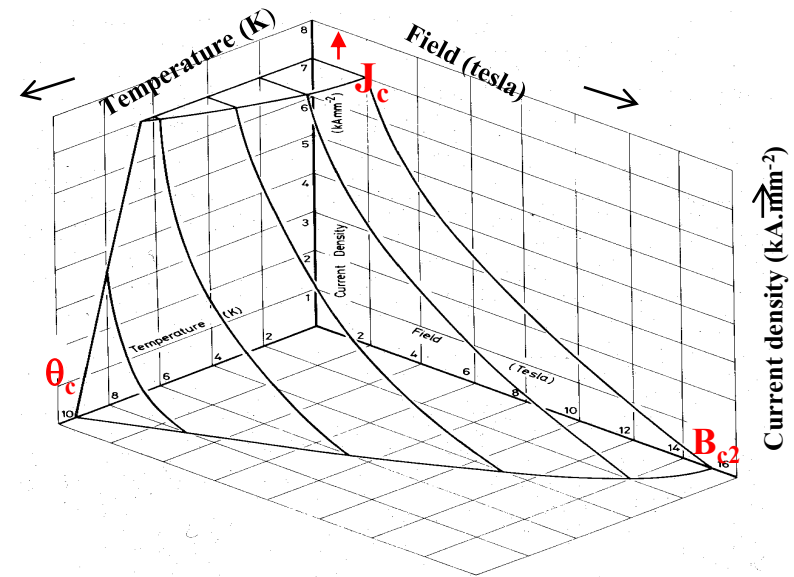
Energy of the machine (left) and size of the accelerator (right)

- Is it possible to have 700 T magnets ??

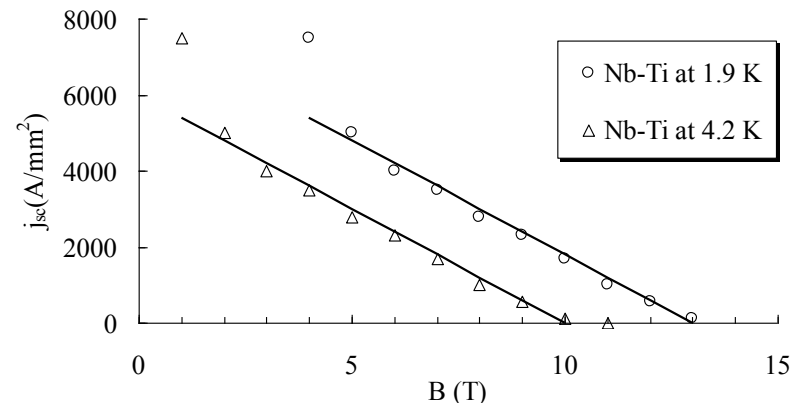


# LIMITS TO HIGH FIELDS

- The material is superconductor as long as  $B, j$ , and temperature stay below the critical surface
  - The **maximum current density**  $\sim 10\,000$   $\text{A}/\text{mm}^2$ , but this at zero field and zero temperature
  - In a magnet, the winding has a current density to create a magnetic field  $\rightarrow$  **the magnetic field is also in the winding**  $\rightarrow$  this reduces the current density
  - The obvious ultimate limit to Nb-Ti dipoles is 14 T at zero temperature and zero current density, and **13 T at 1.9 K**
  - In reality, **we cannot get 13 T but much less** – around 8 T in the LHC – why ?



Critical surface for Nb-Ti



Section of the Nb-Ti critical surface at 1.9 and 4.2 K, and linear fit

# LIMITS TO HIGH FIELDS

- We compute **what field can be reached for a sector coil of width  $w$** 
  - We characterize the **critical surface** by two parameters

$$j_c = \kappa c (B_{c2}^* - B)$$

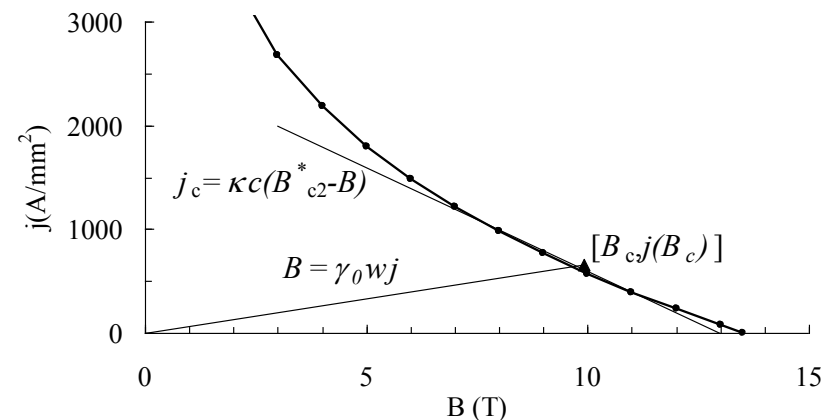
and we added  $\kappa$  which takes into account that only a fraction ( $\sim 1/4$ ) of the coil is made up to superconductor

- The relation between **current density  $j$  and field  $B$**  is  $B = \gamma_0 w j$   
( $w$  thickness of the coil,  $\gamma_0$  is a constant)

and the field that can be reached is given by  $B_c = \gamma_0 w j_c = \gamma_0 w \kappa c (B_{c2}^* - B_c)$

$$B_c = B_{c2}^* \frac{\kappa c \gamma_0 w}{1 + \kappa c \gamma_0 w}$$

- The larger coil, the smaller  $j_c$ ,  
the larger  $B$

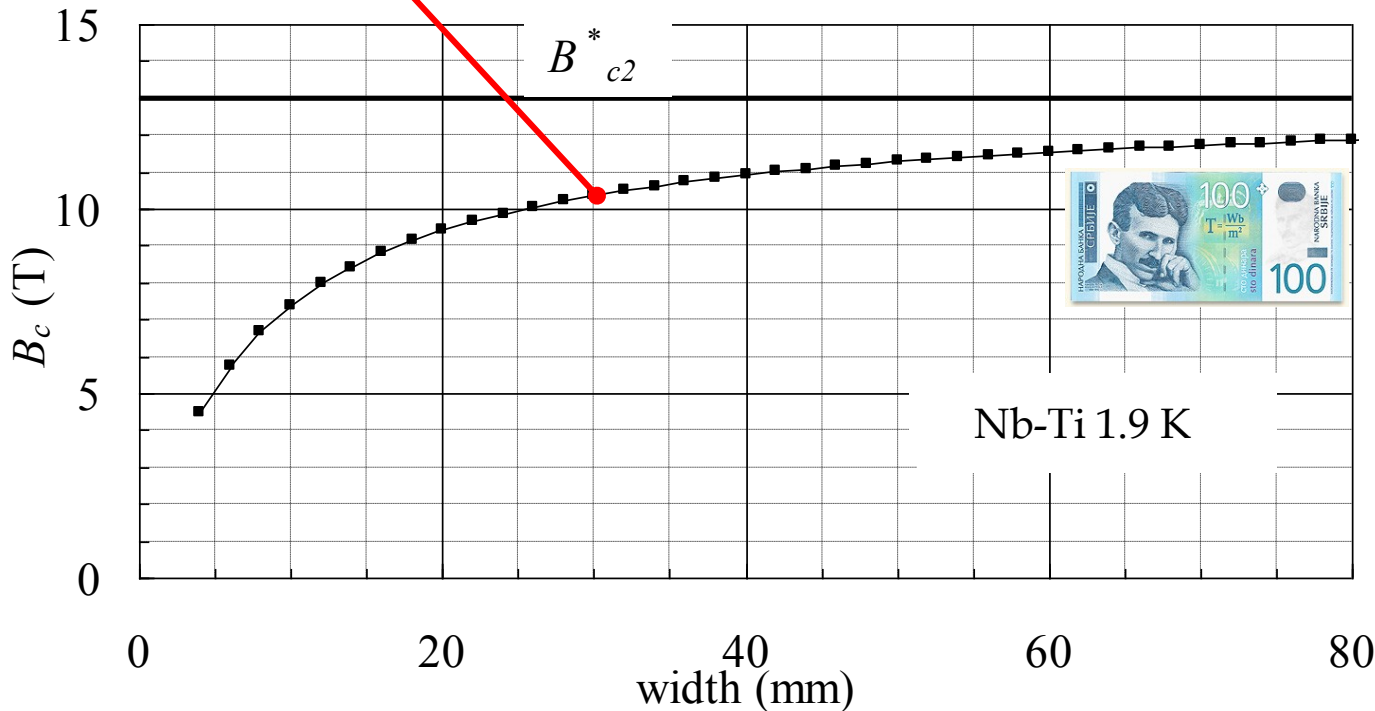


Critical surface for Nb-Ti:  $j$  versus  $B$  and magnet loadline

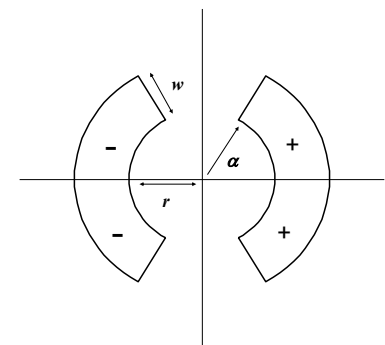
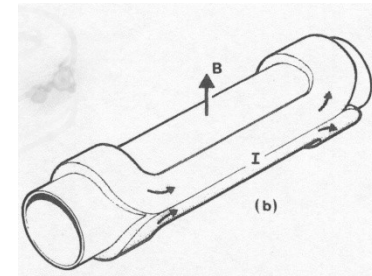
# LIMITS TO HIGH FIELDS

- We have computed what field can be reached for a sector coil of width  $w$  for Nb-Ti
  - There is a **slow saturation** towards 13 T
  - The **last Tesla are very expensive** in terms of coil
  - LHC dipole has been set on 30 mm coil width, giving ~10 T

$$B_c = B_{c2}^* \frac{\kappa \gamma_0 w}{1 + \kappa \gamma_0 w}$$

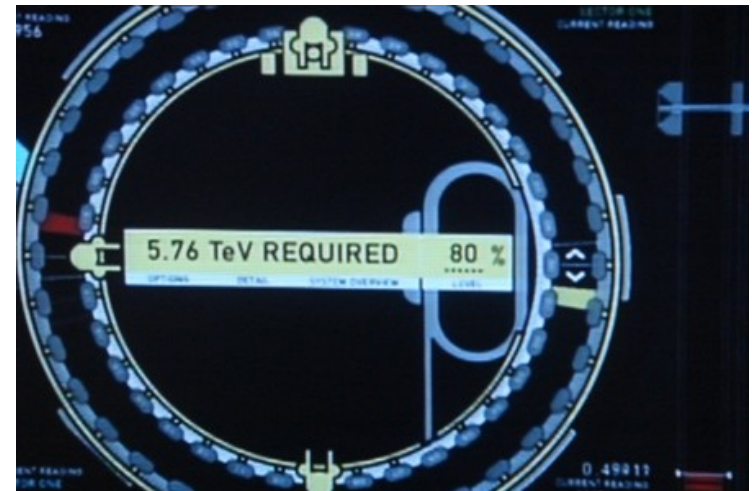


Field versus coil thickness for Nb-Ti at 1.9 K



# LIMITS TO HIGH FIELDS

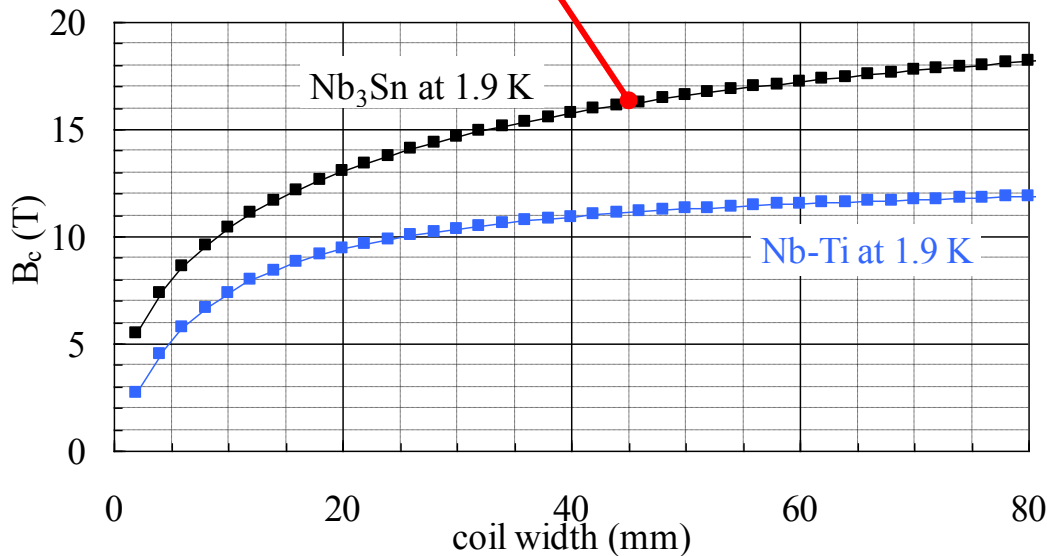
- One cannot work on the critical surface
  - Any **disturbance** producing energy (beam loss, coil movements under Lorentz forces) **increases the temperature** and the superconductivity is lost
    - In this case one has a transition called **quench** – the energy must be dumped without burning the magnet
    - The energy in the LHC dipoles is 8 MJ !
  - A **margin of ~10-20%** is usually taken, i.e. you work at **80-90%**
    - LHC dipoles are giving the maximum field 10 T given by a reasonable amount of coil (30 mm) for Nb-Ti at 1.9 K
    - With a 20% operational margin **one gets ~ 8 T** which is the baseline value



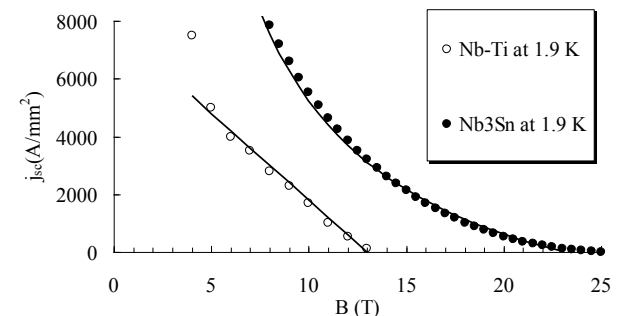
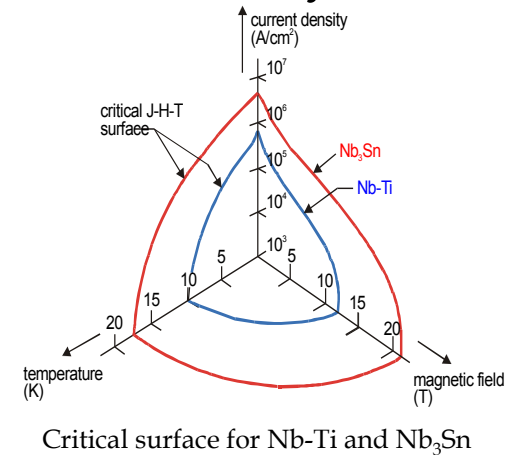
Operational limit of 20%  
 [Terminator-3, Columbia Pictures, 2003]

# LIMITS TO HIGH FIELDS: HINTS ON Nb<sub>3</sub>Sn

- Nb<sub>3</sub>Sn has a **wider critical surface**
  - But the material is **more difficult** to manufacture
  - It has never been used in accelerators, but tested successfully in short models and used in solenoids
  - With Nb<sub>3</sub>Sn one could go up to 15-18 T
  - **World record is 16 T** (HD1, Berkeley)



Field versus coil thickness for Nb-Ti and Nb<sub>3</sub>Sn at 1.9 K



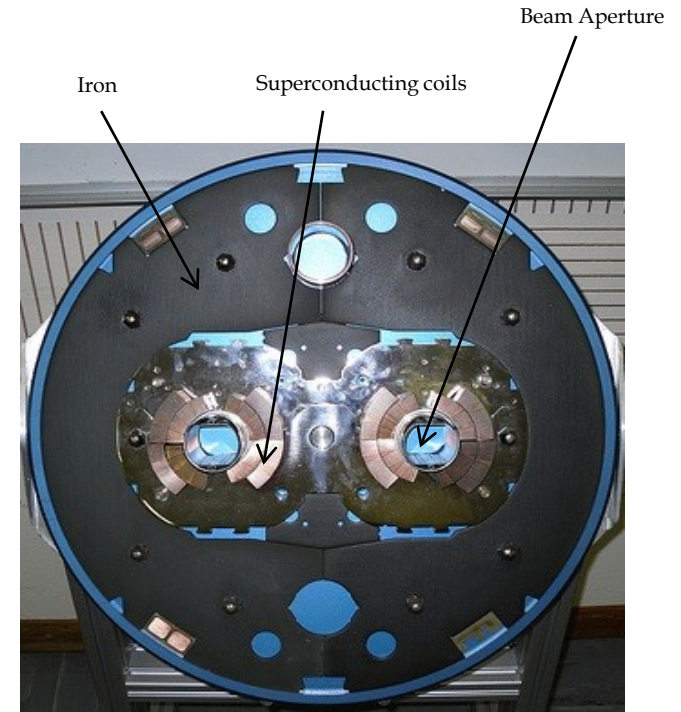


# SHIELDING

- The coils are surrounded by iron to avoid to have magnetic field outside the magnets
  - The iron can take at least 2 T, then it saturates



The iron lady got stuck on a magnet whose field is not shielded  
 [Terminator-3, Columbia Pictures, 2003]



LHC dipole cross-section

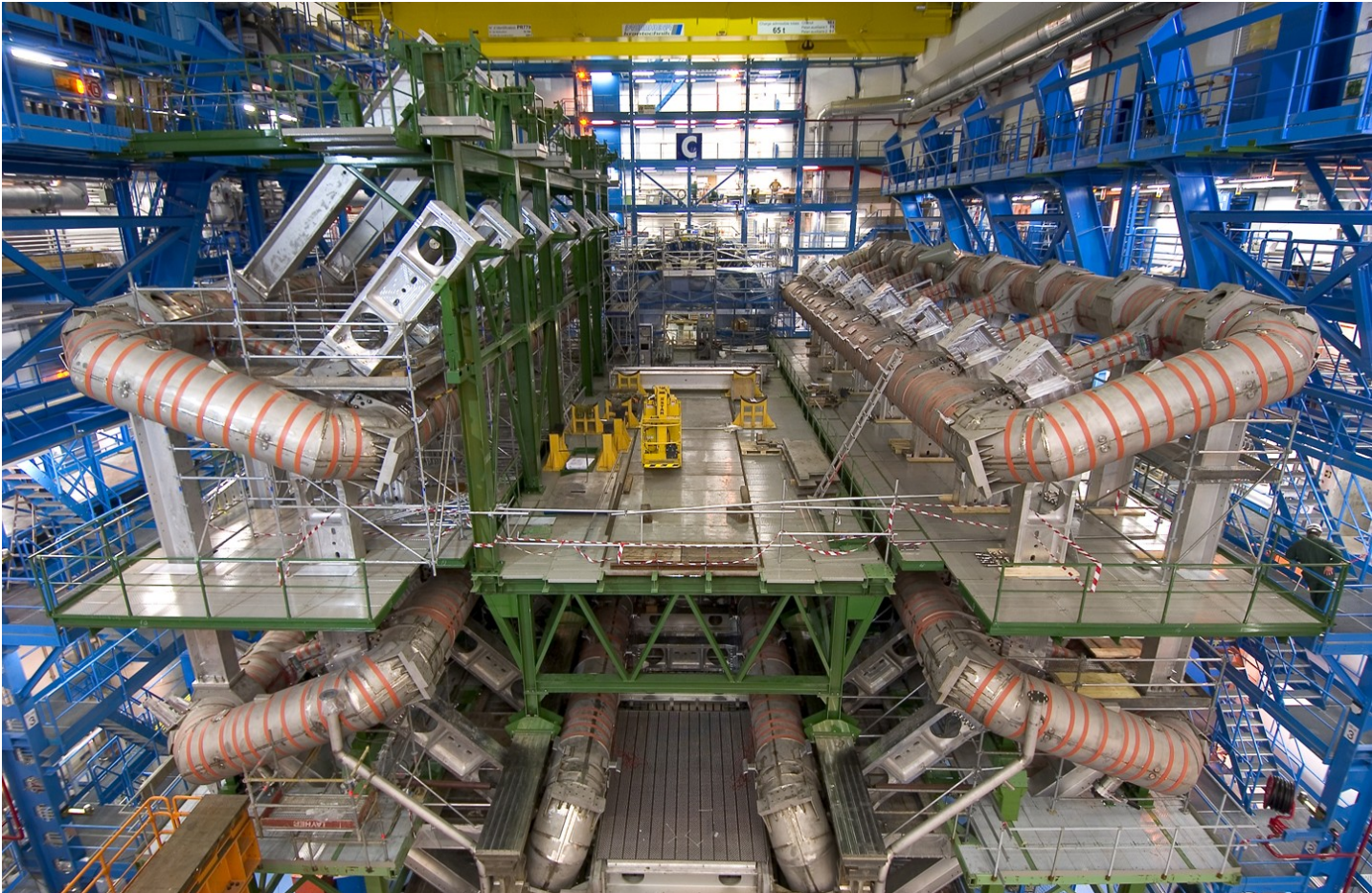
- For the LHC case: 28 mm aperture radius \* 8 T ~ 120 mm iron at 2 T
  - For the Terminator-3 field is 700 T, aperture could be ~ 50 mm, one would need  $700/2*50 \sim 17$  m of iron ! - that's why their magnets are not shielded

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# DETECTOR MAGNETS

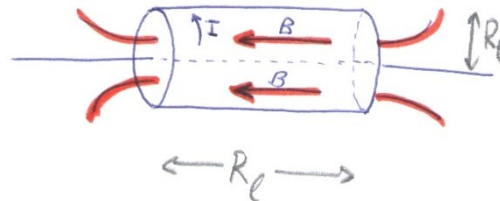
- The beam is small ... why are detectors so large ?



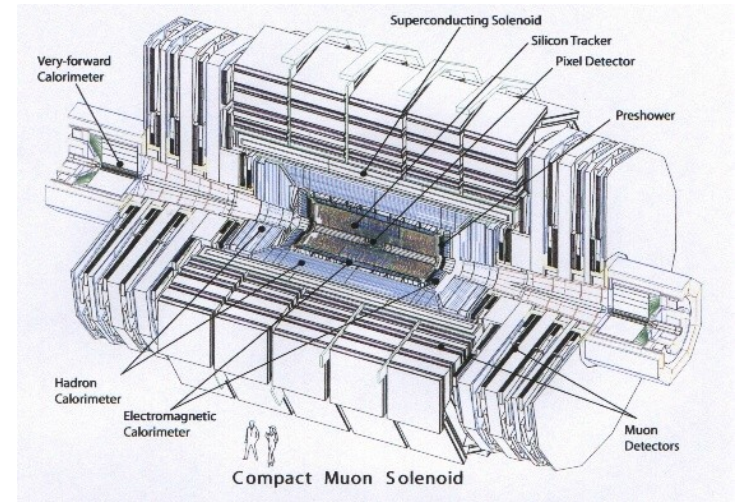
The toroidal coils of ATLAS experiment

# DETECTOR MAGNETS

- Detector magnets provide a field to bend the particles generated by collisions (not the particles of the beam !)
  - The measurement of the bending radius gives an estimate of the **charge and energy of the particle**
- Different lay-outs
  - A **solenoid** providing a field parallel to the beam direction (example: LHC CMS, LEP ALEPH, Tevatron CDF)
    - Field lines perpendicular to  $(x,y)$



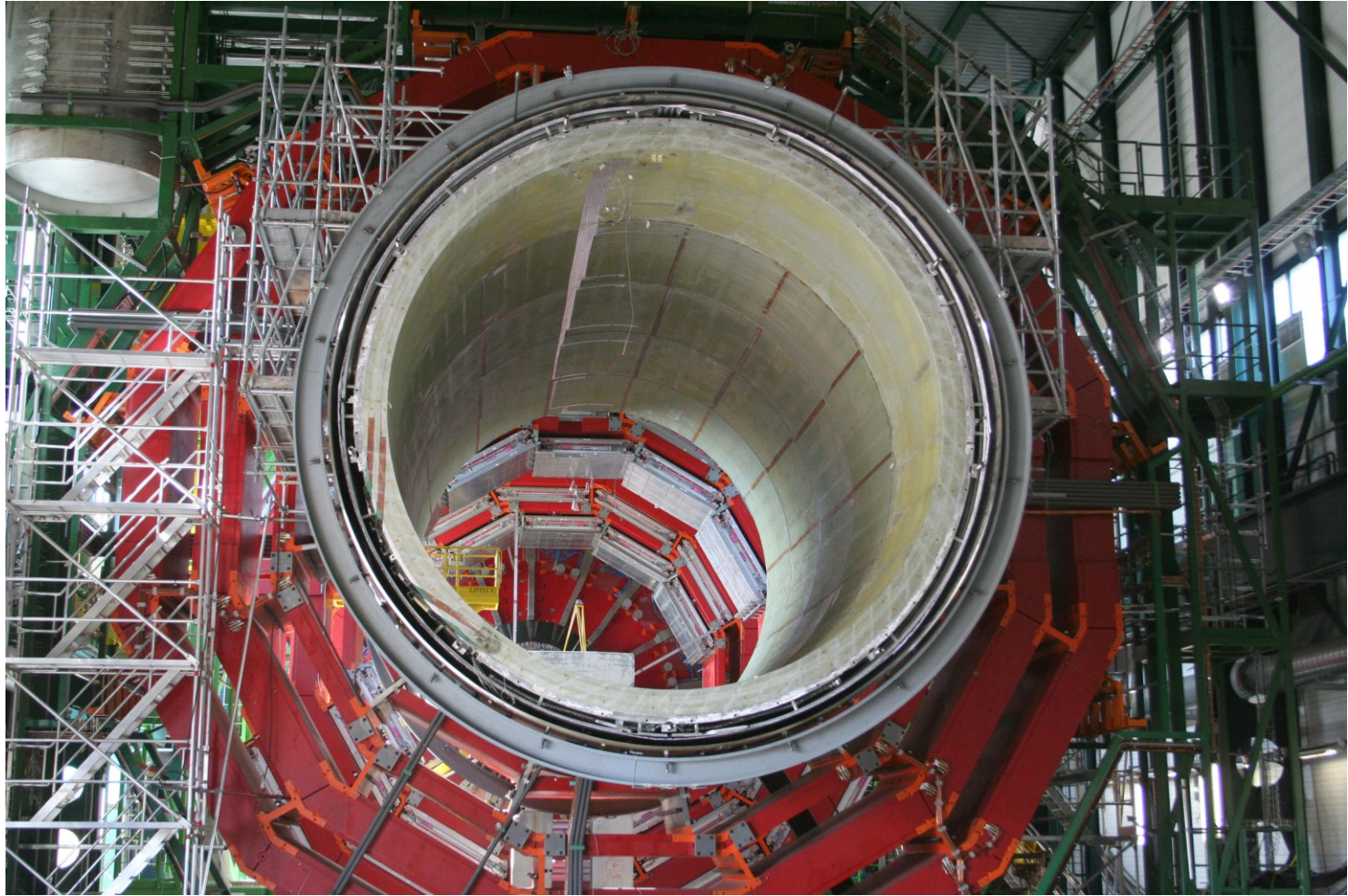
Sketch of a detector based on a solenoid



Sketch of the CMS detector in the LHC

- A series of **toroidal** coils to provide a circular field around the beam (example: LHC ATLAS)
  - Field lines of circular shape in the  $(x,y)$  plane

# DETECTOR MAGNETS



The solenoid of CMS experiment

- Detector **transverse size**

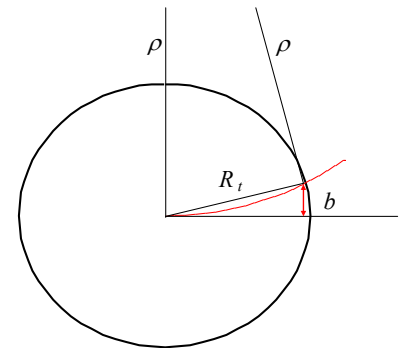
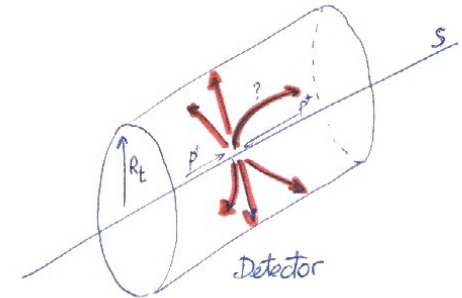
- The particle is bent with a **curvature radius**

$$E = eB\rho$$

- $B$  is the field in the detector magnet
- $R_t$  is the **transverse radius** of the detector magnet
- The **precision** in the measurements is related to the **parameter  $b$**
- A bit of trigonometry gives

$$b = \frac{R_t^2}{2\rho} = \frac{e R_t^2 B}{2 E}$$

- The magnetic field is limited by the technology
- If we **double the energy** of the machine, keeping the same magnetic field, we must make a **1.4 times larger** detector ...





# DETECTOR MAGNETS

- Detector **transverse size**

- $B$  is the field in the detector magnet
- $R_t$  is the transverse radius of the detector magnet
- The **precision in the measurements is  $\propto 1/b$**

$$b = \frac{R_t^2}{2\rho} = \frac{e}{2} \frac{R_t^2 B}{E}$$

$$b \sim 0.15 \frac{R_t^2 B}{E[\text{GeV}]}$$

- Examples

- LEP ALEPH:  $E=100$  GeV,  $B=1.5$  T,  $R_l=6.5$  m,  $R_t=2.65$  m,  $b=16$  mm
  - that's why we need sizes of **meters and not centimeters** !

- The magnetic field is limited by technology

- But fields are not so high as for accelerator dipoles (4T instead of 8 T)
- Note that the precision with  $BR_t^2$  – **better large than high field** ...

- Detector longitudinal size

- several issues are involved – not easy to give simple scaling laws

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# LUMINOSITY AND OPERATION

- The energy is not the only relevant parameter: the other is the frequency of collisions (how many data?)
  - The number of collisions (events) per second is given by the luminosity times the cross-section of the event

$$N_{event} [s^{-1}] = L [cm^{-2} s^{-1}] \sigma_{event} [cm^{-2}]$$

- The cross-section depends on the type of event (“surface of the particle”)
  - The luminosity depends on the accelerator and on the beam – it is a parameter of the whole machine
- One needs large luminosities to have more statistics!
  - But the detectors must be able to swallow all these events!

- Equation for the luminosity

$$L = \frac{N_b^2 n_b f_{rev} \gamma}{4\pi \epsilon_n \beta^*} F = \frac{c}{4\pi} \underbrace{\gamma \frac{1}{L}}_{\text{Machine features}} \underbrace{N_b^2 n_b}_{\text{Beam intensity features}} \underbrace{\frac{1}{\epsilon_n \beta^*}}_{\text{Beam geometry features}} F$$

## Machine features

Energy of the machine 7 TeV  
 Length of the machine 27 km

## Beam intensity features

$N_b$  Number of particles per bunch  $\sim 10^{11}$   
 $n_b$  Number of bunches  $\sim 3000$

## Beam geometry features

Size of the beam at collision



# LUMINOSITY AND OPERATION

- The beam-beam limit

$$L = \frac{N_b^2 n_b f_{rev} \gamma}{4\pi \epsilon_n \beta^*} F = \frac{c}{4\pi} \gamma \frac{1}{L} N_b^2 n_b \frac{1}{\epsilon_n \beta^*} F$$

$$\xi = \frac{r_p}{4\pi} \frac{N_b}{\epsilon_n} < 0.02$$

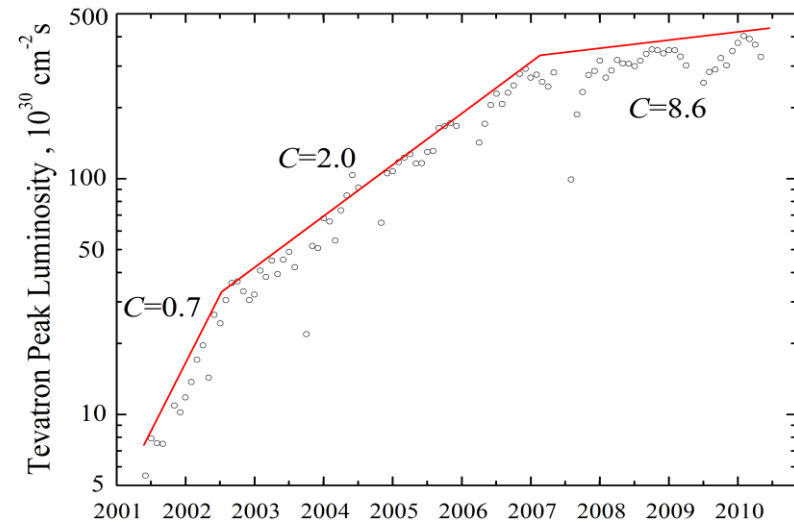
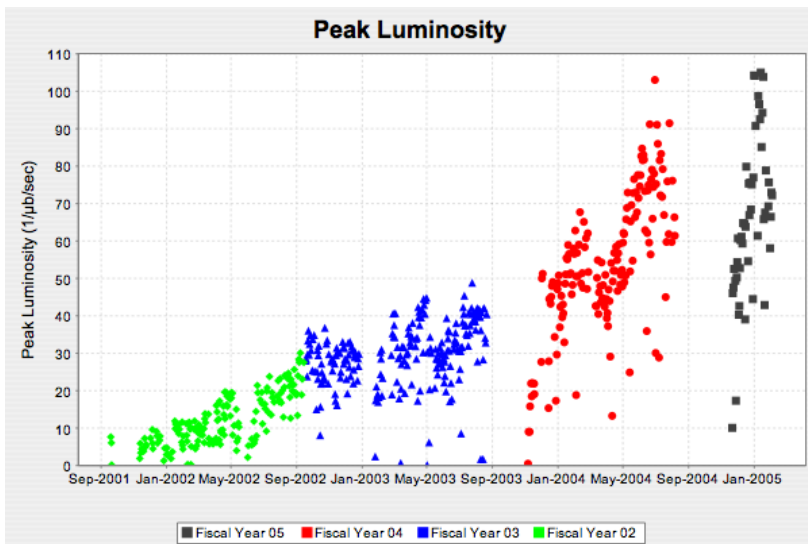
- $N_b$  Number of particles per bunch       $\epsilon_n$  transverse size of beam
- One cannot put too many particles in a “small space”
- Otherwise the Coulomb interaction when the beam collide make the beam unstable

- The stored energy

$$E \propto N_b n_b \gamma$$

- The higher the energy, the most challenging is the protection of the machine
  - A beam lost makes holes! Collimators protect the machine
- For the LHC the beam has a total energy of 350 MJ

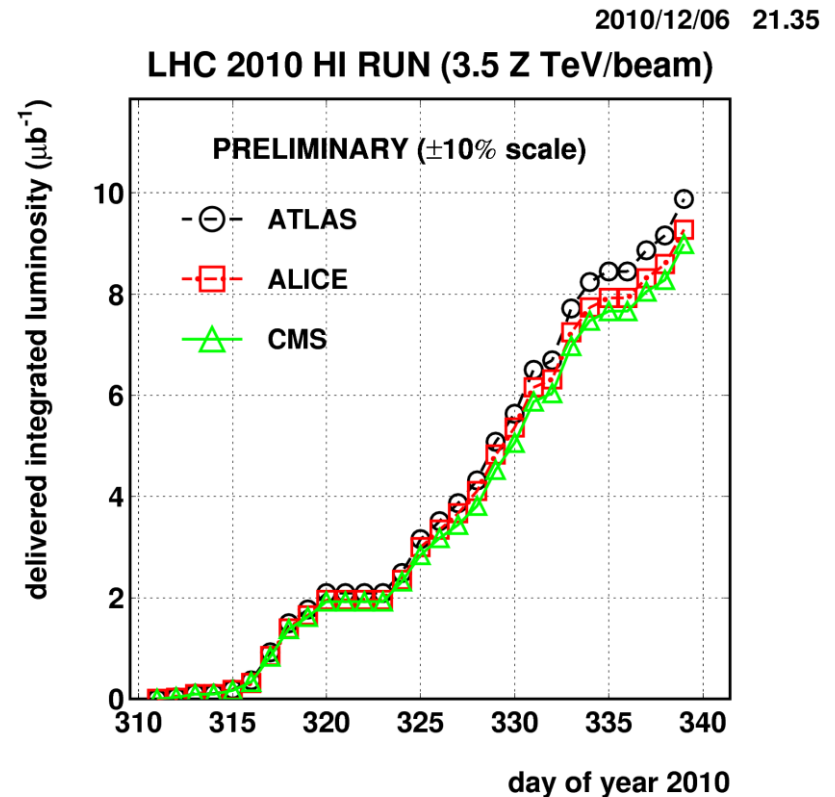
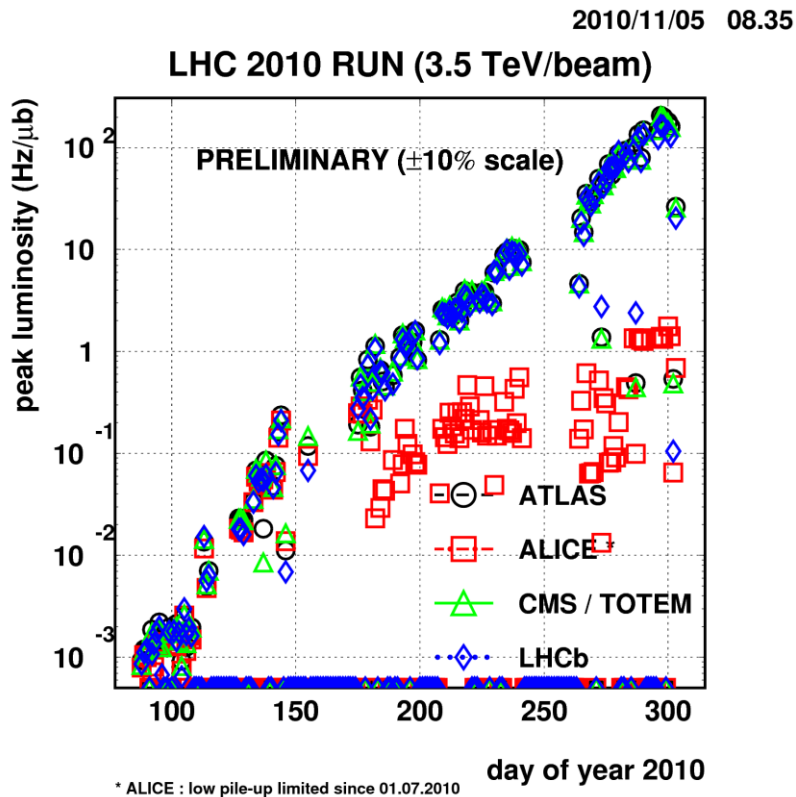
- Achieving the nominal performances is a long process!!
  - It usually takes years ...



Increase in luminosity in Tevatron Run II [V. Shiltsev]



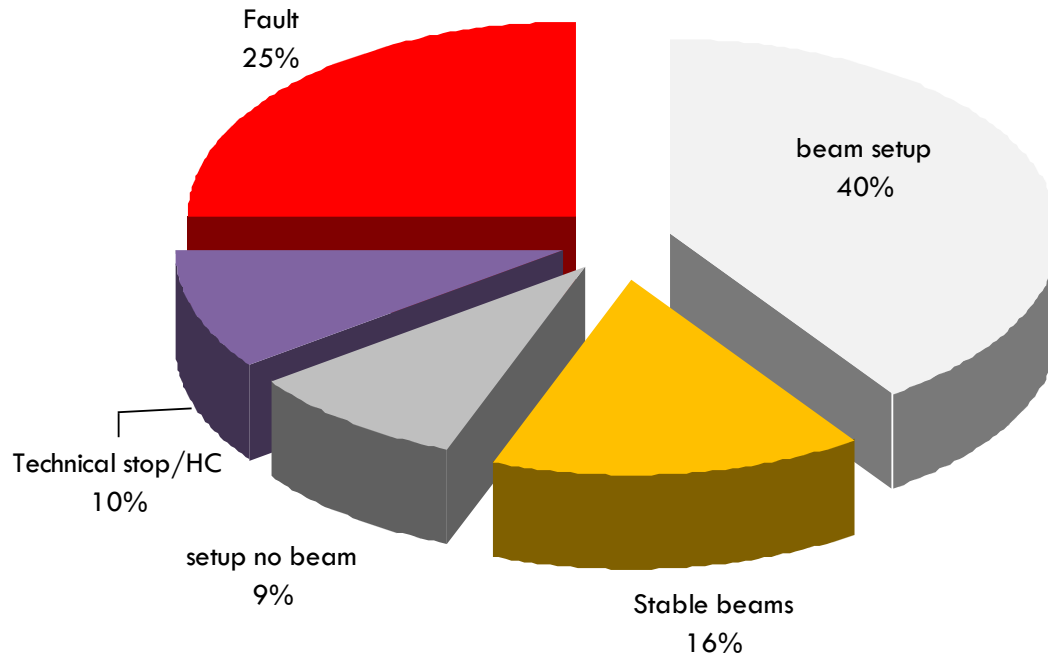
- Achieving the nominal performances is a long process!!
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Increase in luminosity in LHC 2010 [M. Lamont, M. Ferro Luzzi]

# LUMINOSITY AND OPERATION

- Achieving peak luminosity is not everything: one has to do it continuously
  - In 2010 we had 1/6 of the time used for making collisions – not bad



Time dedicated to beam in 2010 [W. Venturini Delsolaro]



# LUMINOSITY AND OPERATION

- Where are we today?

$$L = \frac{N_b^2 n_b f_{rev} \gamma}{4\pi \epsilon_n \beta^*} F = \frac{c}{4\pi} \gamma \frac{1}{L} N_b^2 n_b \frac{1}{\epsilon_n \beta^*} F$$

	Nominal	2010	Loss w.r.t. nominal	Reason
$N_b$	$1.15 \times 10^{11}$	$1.2 \times 10^{11}$	0.9	Better than expected - injectors can put many protons!
$n_b$	2808	400	7.0	Above 400 one start to see electron cloud - to be cured with scrubbing
$\gamma$	7000	3500	2.0	Limited to 3.5 TeV for interconnection problems (2010 incident)
$\epsilon$	3.75	2.5	0.7	Much better than expected - injectors can give smaller beams!
$\beta$	0.55	3.5	6.4	Limited to 3.5 m, but 2 m reached
L			54	

- Total reached in 2010: around a factor 50 less than nominal
- Very good for first year! But the hard part has to come ...