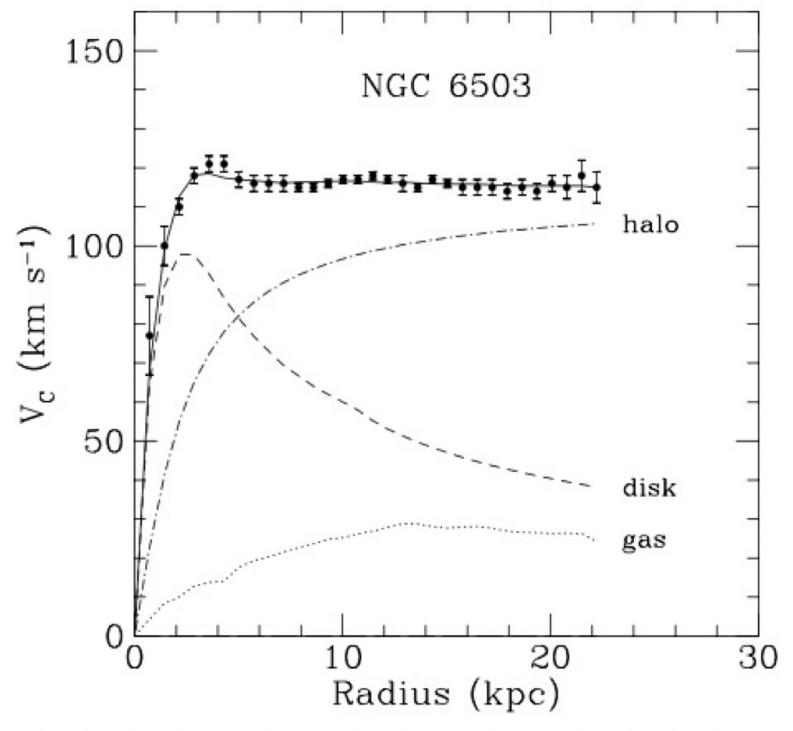


Dark Matter

Data and Candidates

Mads Toudal Frandsen

Recap



- Particle physics candidates for DM particle
 - Sterile neutrino
 - axion
 - WIMP

M. Shaposhnikov's lecture

$$\rho(r) \sim \frac{1}{r^2} \text{ at large } r$$

Recap

$$\rho(r) \sim \frac{1}{r^2} \text{ at large } r$$

Is this inferred DM density
consistent with particle DM?

Isothermal sphere

Self-gravitating isothermal sphere of ideal gas:

$$\frac{dp}{dr} = \frac{k_B T}{m} \frac{d\rho}{dr} = -\rho \frac{d\Phi}{dr} = -\rho \frac{GM(r)}{r^2},$$

Simple(st) particle model of DM halo yields

Solution for density

$$\rho(r) = \frac{\sigma^2}{2\pi G r^2}.$$

$$\rho(r) \sim \frac{1}{r^2} \text{ at large } r$$

This solution describes the **singular isothermal sphere**. The mass interior to radius r , the circular speed and the gravitational potential are (eqs. 2.60, 2.61, and 2.62)

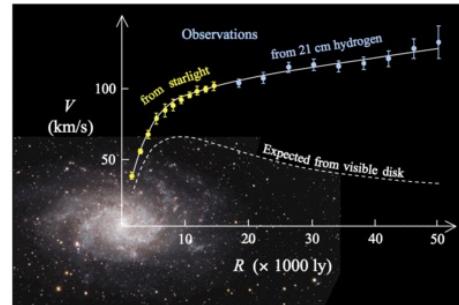
$$M(r) = \frac{2\sigma^2 r}{G} ; \quad v_c(r) = \sqrt{2}\sigma ; \quad \Phi(r) = 2\sigma^2 \ln(r) + \text{constant}, \quad (4.104)$$

(Binney & Tremaine; Galactic Dynamics)

Missing mass problem

Galactic scales

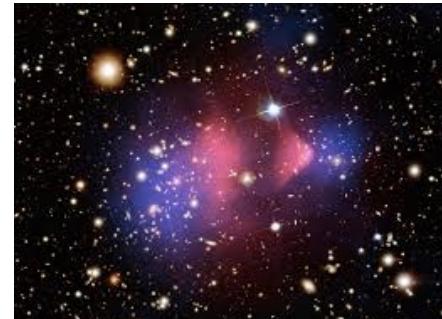
Rotation curves of stars and gas
(Freeman '70, Bosma '78, Rubin et al '78)



Gravitational evidence from kpc to Gpc scales

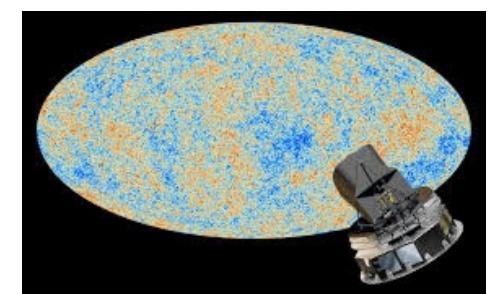
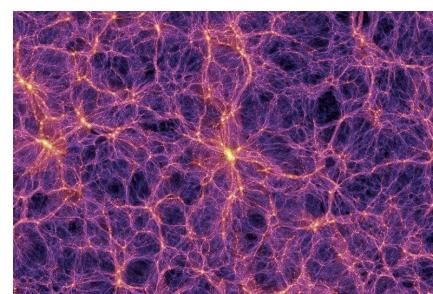
Cluster Scales

Galaxy velocity dispersions,
Cluster mergers
(Zwicky '33, Clowe et al '06)



Cosmological scales

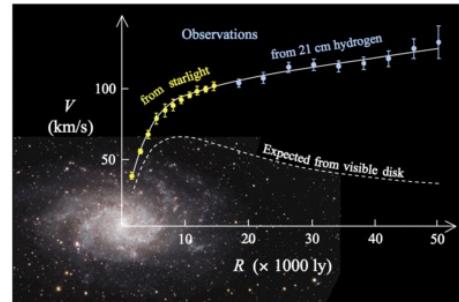
CMB and LSS
(Davis et al '82, Peebles '82)



Missing *gravity* problem

Galactic scales

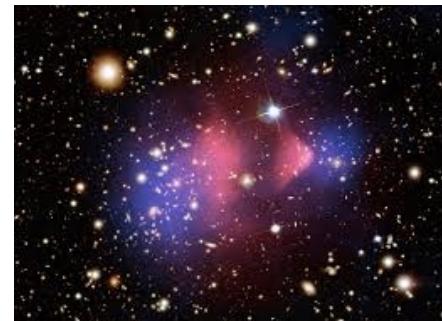
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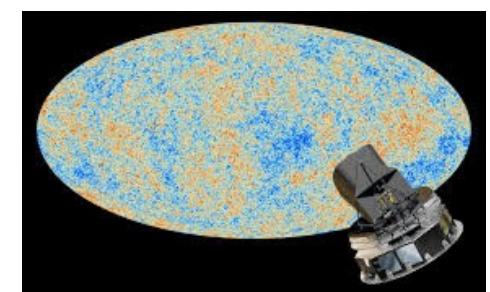
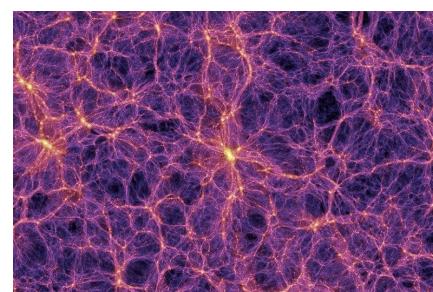
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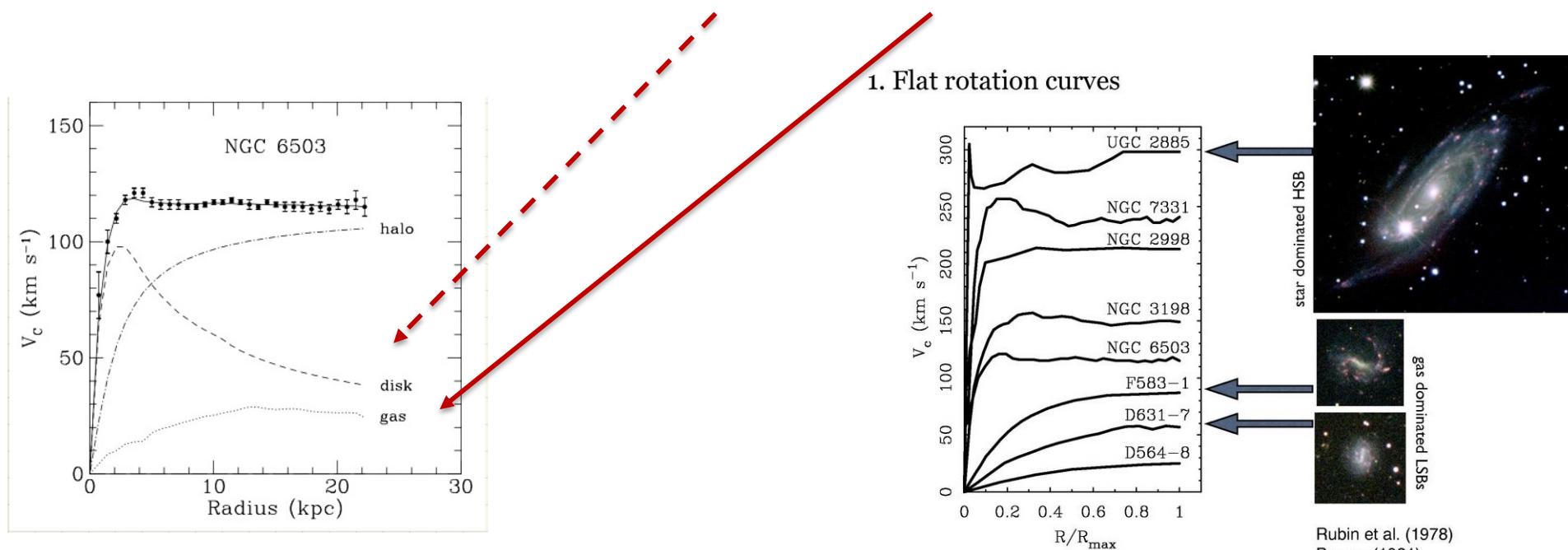


Many types of observational techniques
and systems at each scale
E.g. for rotation curves



175 late-type spirals and irregulars.

Stellar mass range 5 dex, surface brightnesses 4 dex, range of gas fractions

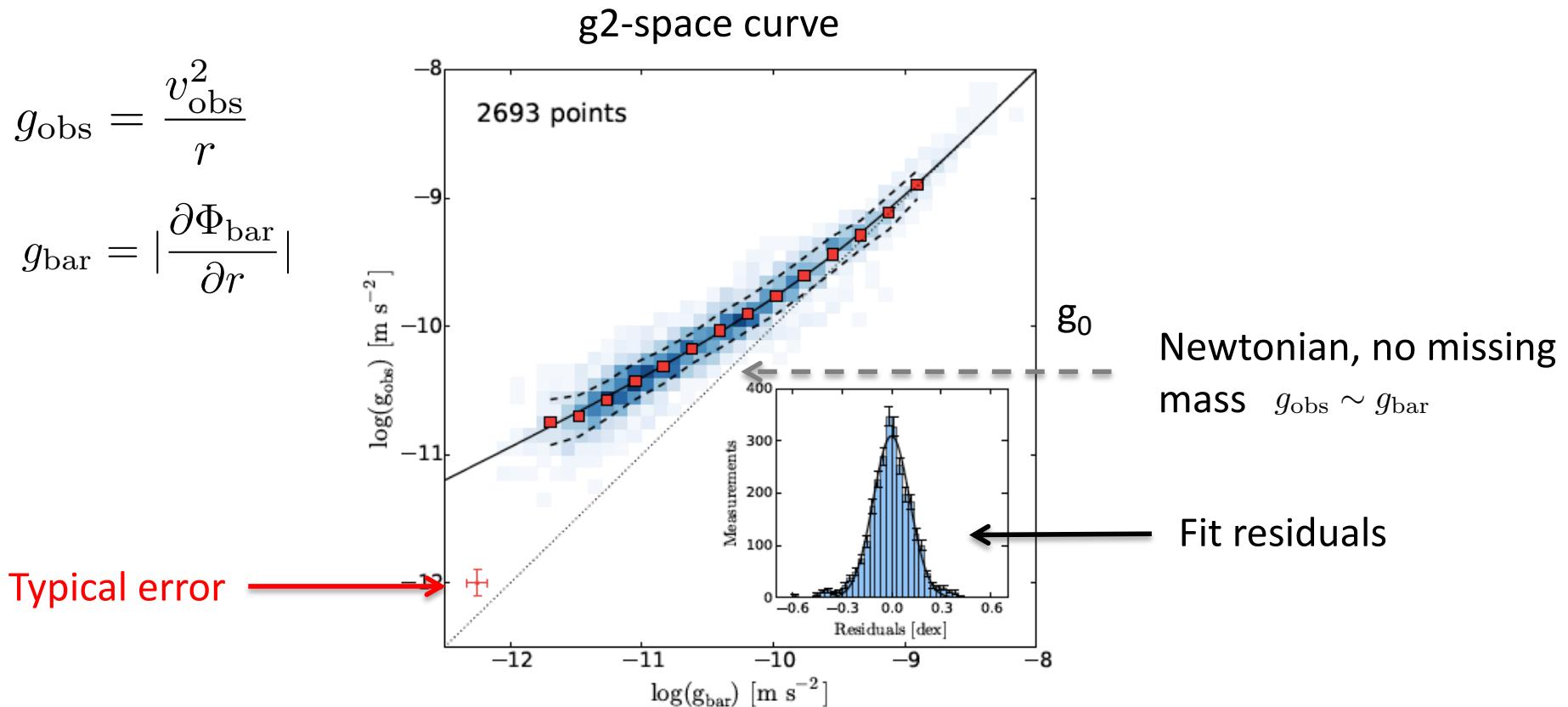


(From McGaugh, KITP DM workshop '18)

Radial Acceleration Relation

Correlation found between baryonic acceleration and total acceleration in ~ 2700 data points from 175 galaxies from the SPARC database

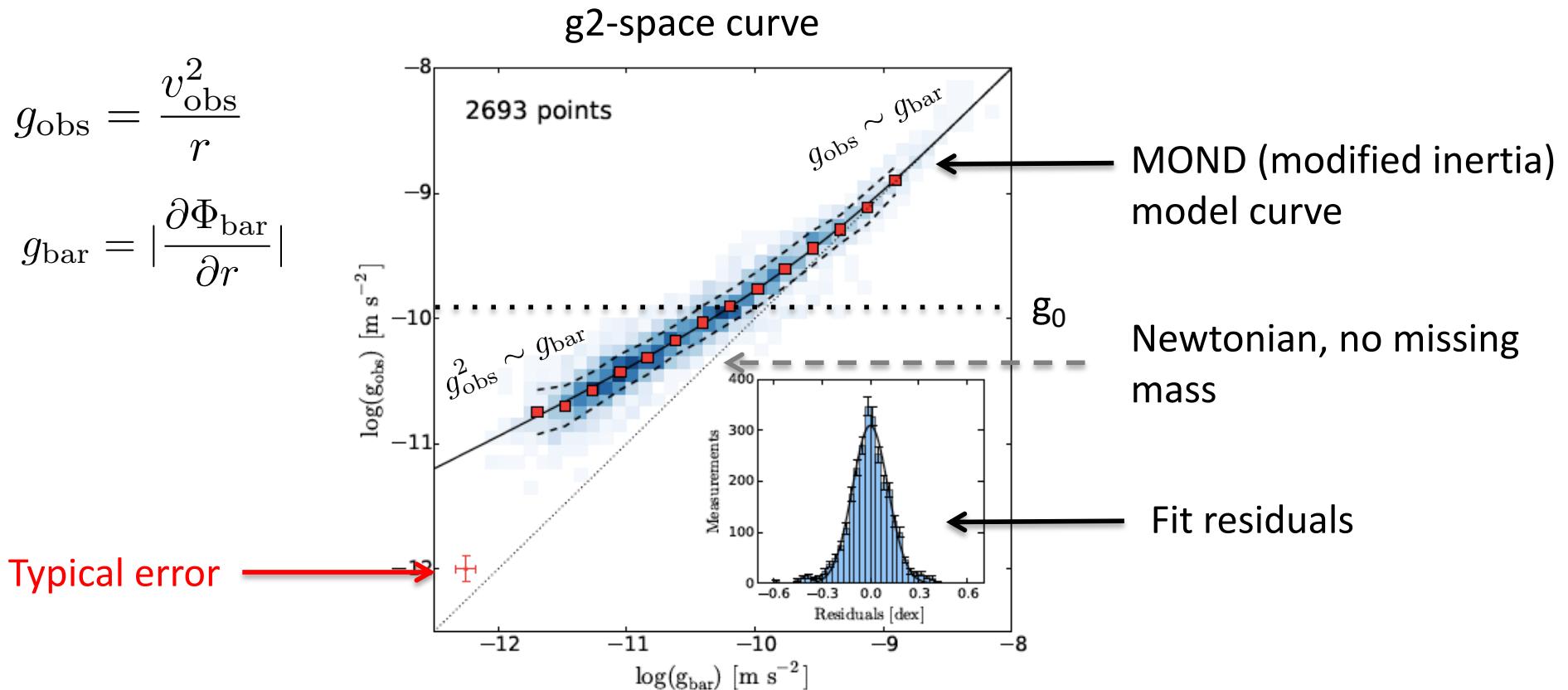
(McGaugh, Lelli & Schombert '16)



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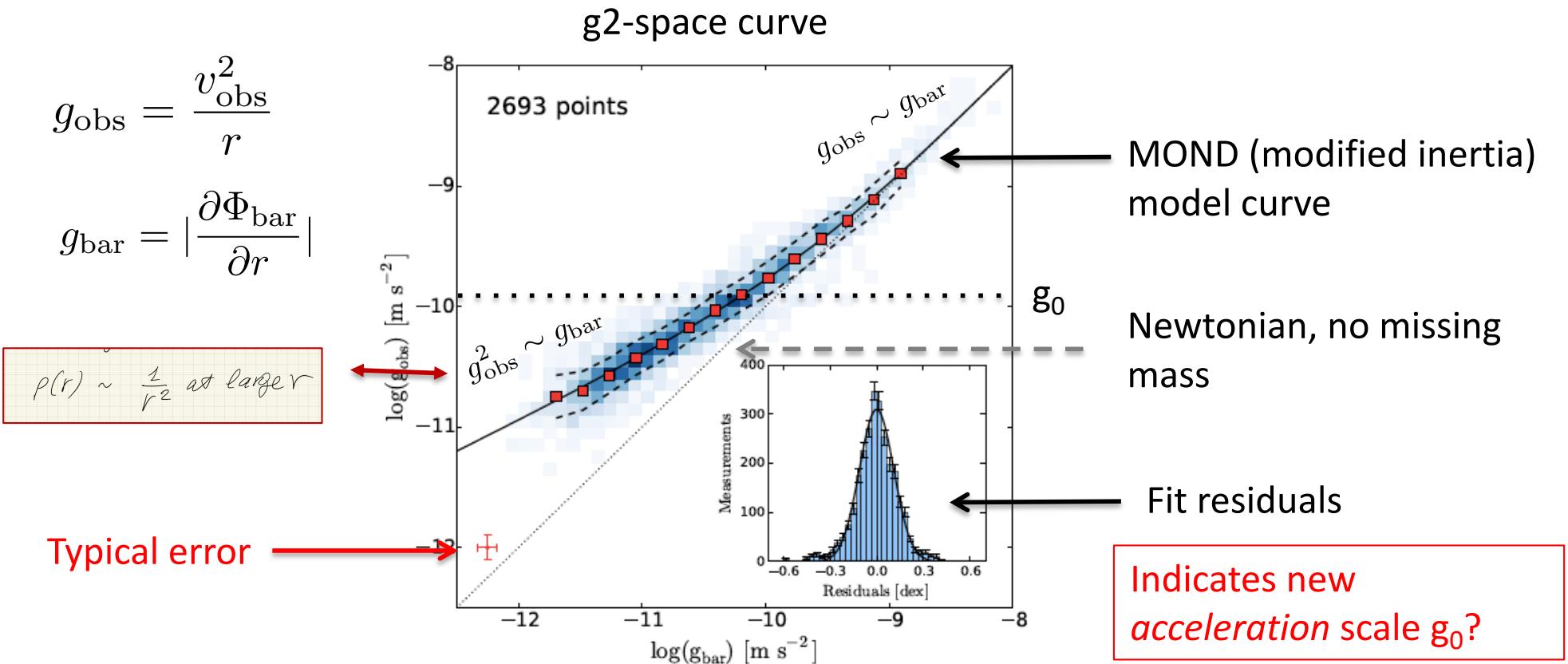
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Radial Acceleration Relation

Correlation found between baryonic acceleration and total acceleration in ~ 2700 data points from 175 galaxies from the SPARC database

(McGaugh, Lelli & Schombert '16)



Modified Newtonian Dynamics

Newtonian acceleration modified below $g_0 \sim 1.2 \times 10^{-10} \text{ m/s}^2$
to account for flat rotation curves

(Milgrom '83
Bekenstein & Milgrom '85)

Bekenstein-Milgrom MOND

$$\vec{\nabla} \cdot \left(\mu \left(\frac{g_M}{g_0} \right) \vec{g}_M \right) = 4\pi G \rho_{\text{bar}} = \vec{\nabla} \cdot \vec{g}_{\text{bar}}$$

MOND acceleration

Baryonic matter distribution ρ_{bar}

Newtonian Poisson Equation

Newtonian acceleration

MOND interpolation function

$$\mu(x) = \begin{cases} \mu(x) \simeq 1 & x \gg 1 \text{ Newtonian regime} \\ \mu(x) \simeq x & x \ll 1 \text{ Mondian regime} \end{cases}$$

Radial Acceleration Relation

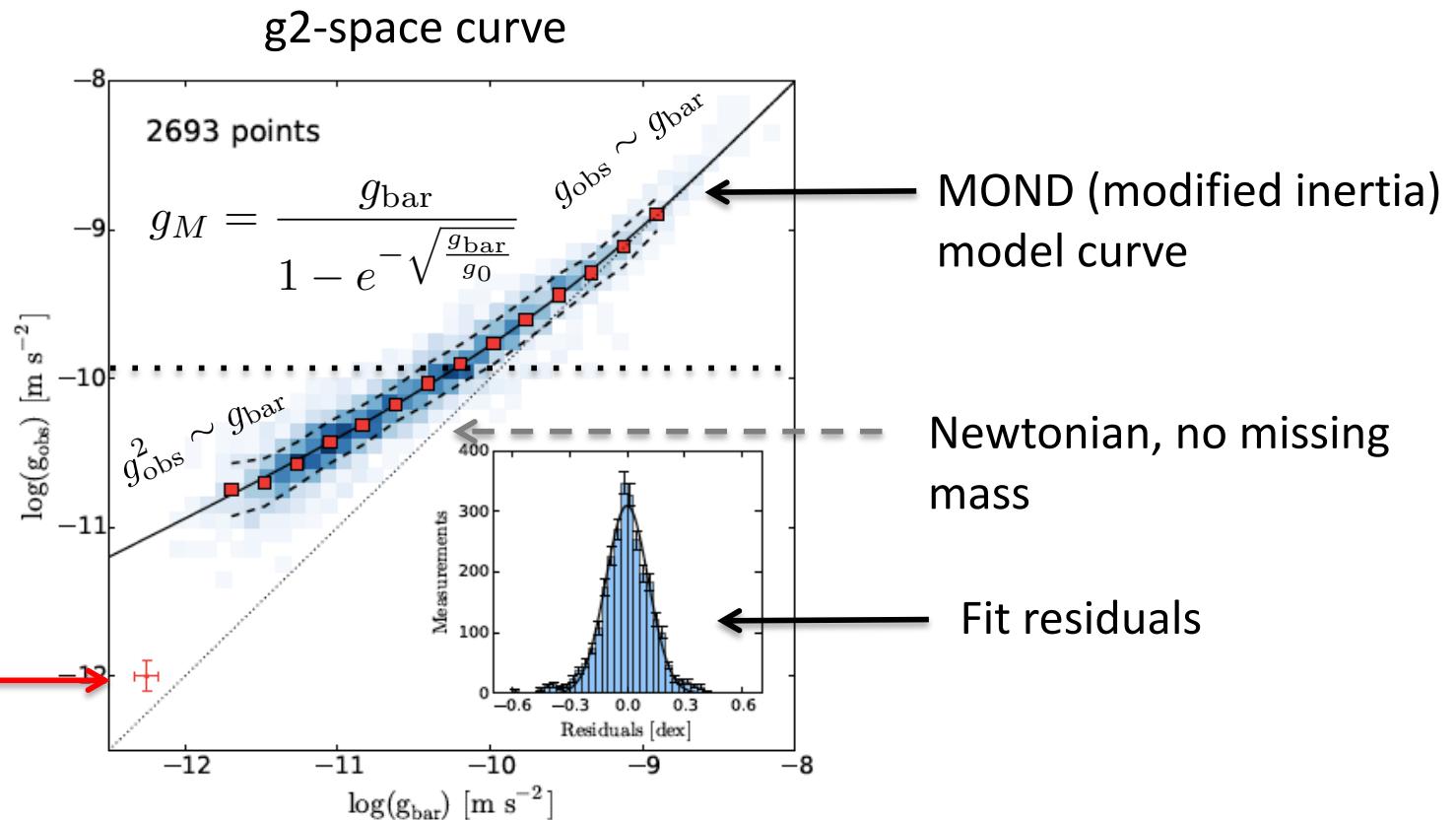
g2-space cuve
shows

- 1) Correlation between baryonic acceleration and total acceleration
- 2) MOND modified inertia fit.
- 3) (Simplest) approximation to MOND modified gravity fit.

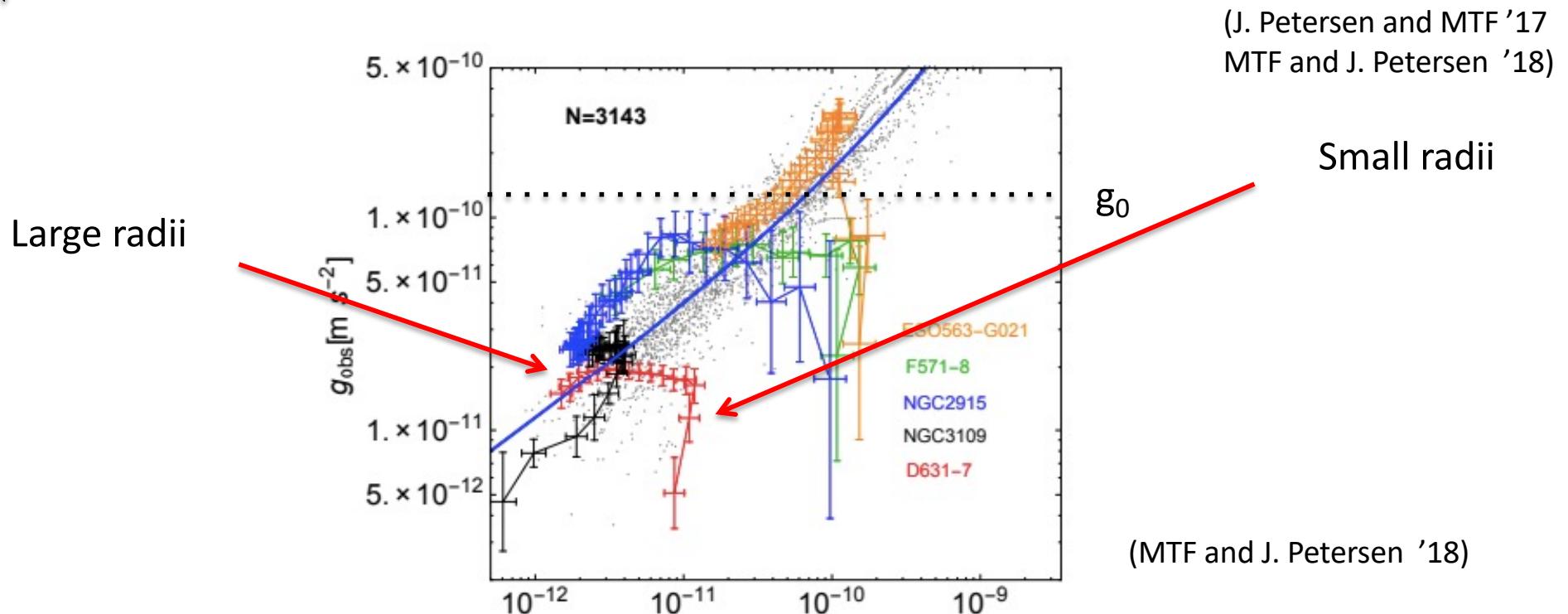
$$g_{\text{obs}} = \frac{v_{\text{obs}}^2}{r}$$

$$g_{\text{bar}} = \left| \frac{\partial \Phi_{\text{bar}}}{\partial r} \right|$$

Typical error



SPARC Individual galaxies



Highlighted galaxies don't follow Radial Acceleration Relation at smallest radii

Result of baryonic complexities at small radii?

Universality vs Diversity

NFW scaling of radial DM density profiles from dwarf galaxies to galaxy clusters

DM only cosmological N-body simulations. No baryons

$$\rho_{\text{NFW}}(r) = \frac{\rho_{0,\text{NFW}}}{r_s(1 + \frac{r}{r_s})^2}$$

(Navarro, Frenk & White '95)

MOND/RAR: Total acceleration in circular motion correlates with that from baryons
At galactic scales

(Tully & Fisher '77; McGaugh '11)

Cusp/Core

Flat or cored DM profiles in dwarf and Low Surface Brightness galaxies

$$\rho_{\text{ISO}}(r) = \frac{\rho_{0,\text{ISO}}}{1 + (\frac{r}{r_c})^2}$$

(Moore '94; Flores & Primack '94)

Missing Satellites & Too-big-to-fail

Too many satellites that are too dense and massive are predicted

(Moore, Quinn, Governato, Stadel & Lake '99; Klypin, Kravtsov, Valenzuela & Prada '99; Boylan-Kolchin, Bullock, Kaplinghat '11)

Universality vs Diversity

Baryonic physics

Discrepancies arise from comparing to DM-only simulations

(J. Read talk ZPW19)

Adiabatic contraction

Supernova feedback

AGN

DM (self-) interactions

Small scales are high DM density and DM interaction rates

Velocity dependence

Long range, short range

Gravity

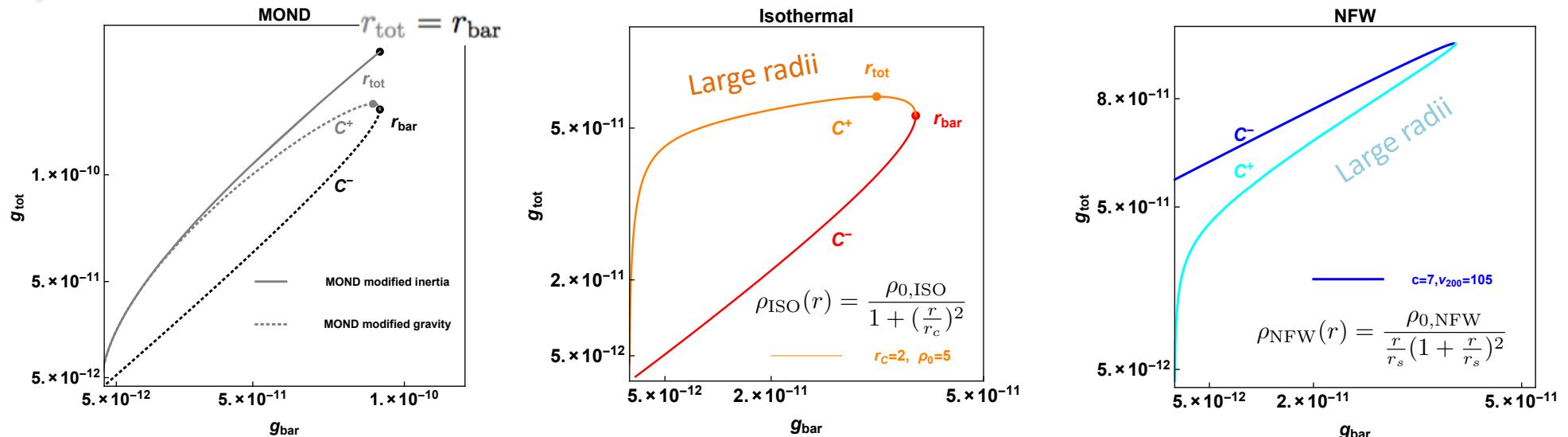
Discrepancies arise assuming Newtonian gravity

With or without DM

Modified Newtonian Dynamics

Modified Gravity

MOND and DM geometry in g2-space



Geometric Classification

- Mond Modified Inertia
- MOND Modified Gravity
- DM Pseudo-Isothermal
- DM Navarro-Frenk-White

Models	Reference radii	Curve segments	Curve Area ^a
MOND-MI	$r_{\text{tot}} = r_{\text{bar}}$	$\mathcal{C}^+ = \mathcal{C}^-$	$\mathcal{A}(\mathcal{C}) = 0$
MOND-MG	$r_{\text{tot}} > r_{\text{bar}}$	$\mathcal{C}^+ > \mathcal{C}^-$	$\mathcal{A}(\mathcal{C}) > 0$
DM-ISO	$r_{\text{tot}} > r_{\text{bar}}$	$\mathcal{C}^+ > \mathcal{C}^-$	$\mathcal{A}(\mathcal{C}) > 0$
DM-NFW	$r_{\text{tot}} < r_{\text{bar}}$	$\mathcal{C}^+ < \mathcal{C}^-$	Curves open

THE ASTROPHYSICAL JOURNAL

OPEN ACCESS

Breakdown of the Newton–Einstein Standard Gravity at Low Acceleration in Internal Dynamics of Wide Binary Stars

Kyu-Hyun Chae¹ 

Published 2023 July 24 • © 2023. The Author(s). Published by the American Astronomical Society.

[The Astrophysical Journal, Volume 952, Number 2](#)

Citation Kyu-Hyun Chae 2023 *ApJ* 952 128

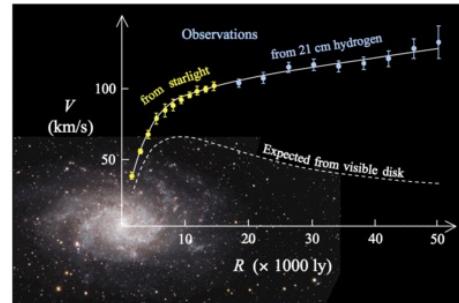
DOI 10.3847/1538-4357/ace101

MOND keeps sparking some interest
but hard to reconcile MOND with
observations on all scales

Missing mass problem

Galactic scales

Rotation curves of stars and gas
(Freeman '70, Bosma '78, Rubin et al '78)



Gravitational evidence from kpc to Gpc scales

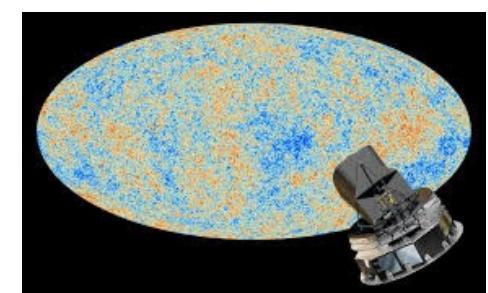
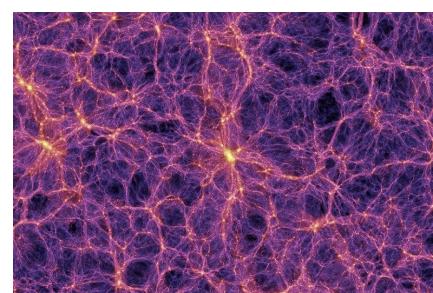
Cluster Scales

Galaxy velocity dispersions,
Cluster mergers
(Zwicky '33, Clowe et al '06)



Cosmological scales

CMB and LSS
(Davis et al '82, Peebles '82)



Back to particle DM

To summarise, what we know about
DM particles

- lifetime $\tau > \tau_{\text{univers}}$
- Relatively light particles must be neutral and very weakly interacting
- DM should be sufficiently cold
- fermions should be heavier than $\sim 500 \text{ eV}$
- bosons should be heavier than $\sim 10^{-22} \text{ eV}$

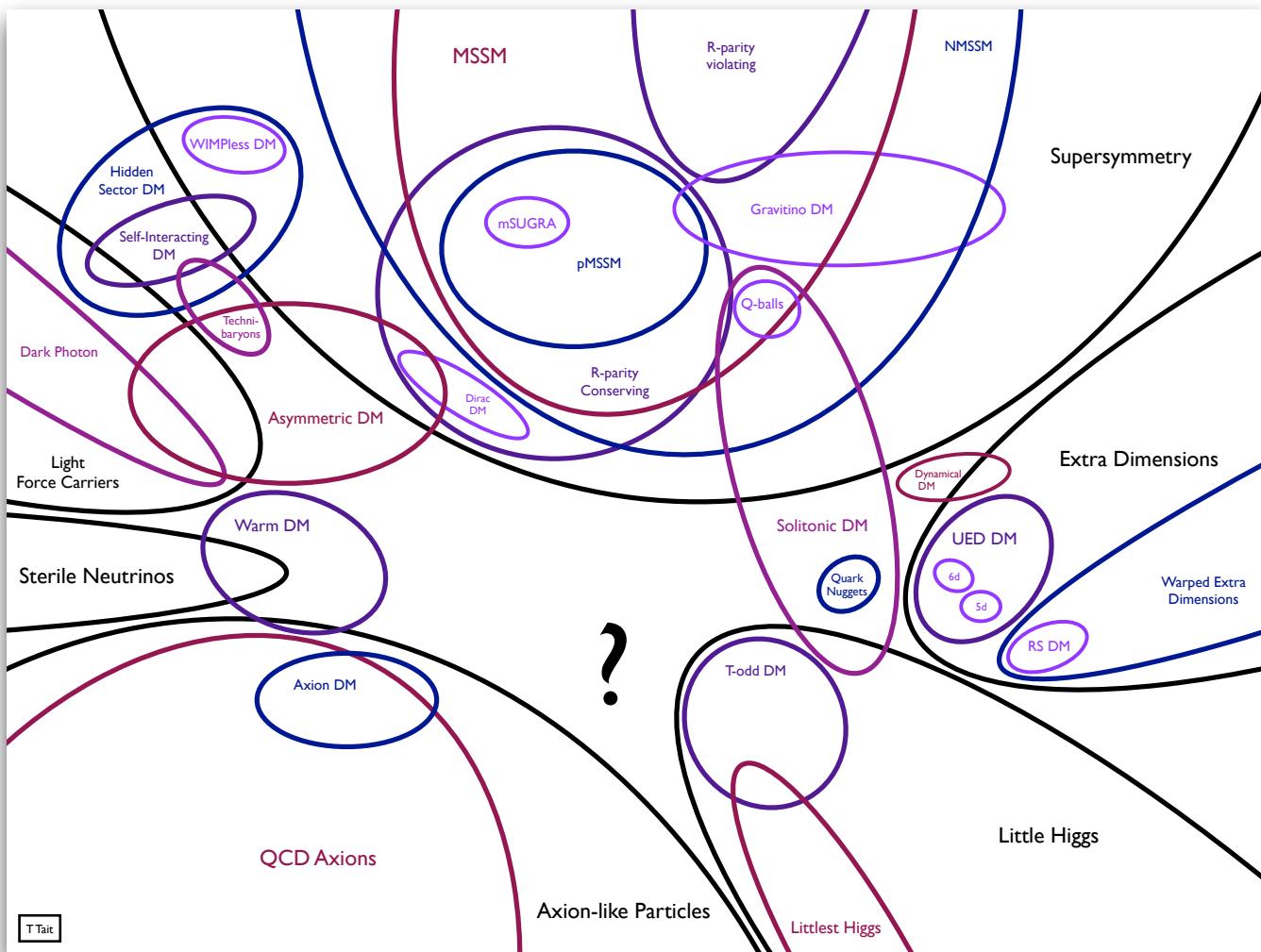
Need theory input!

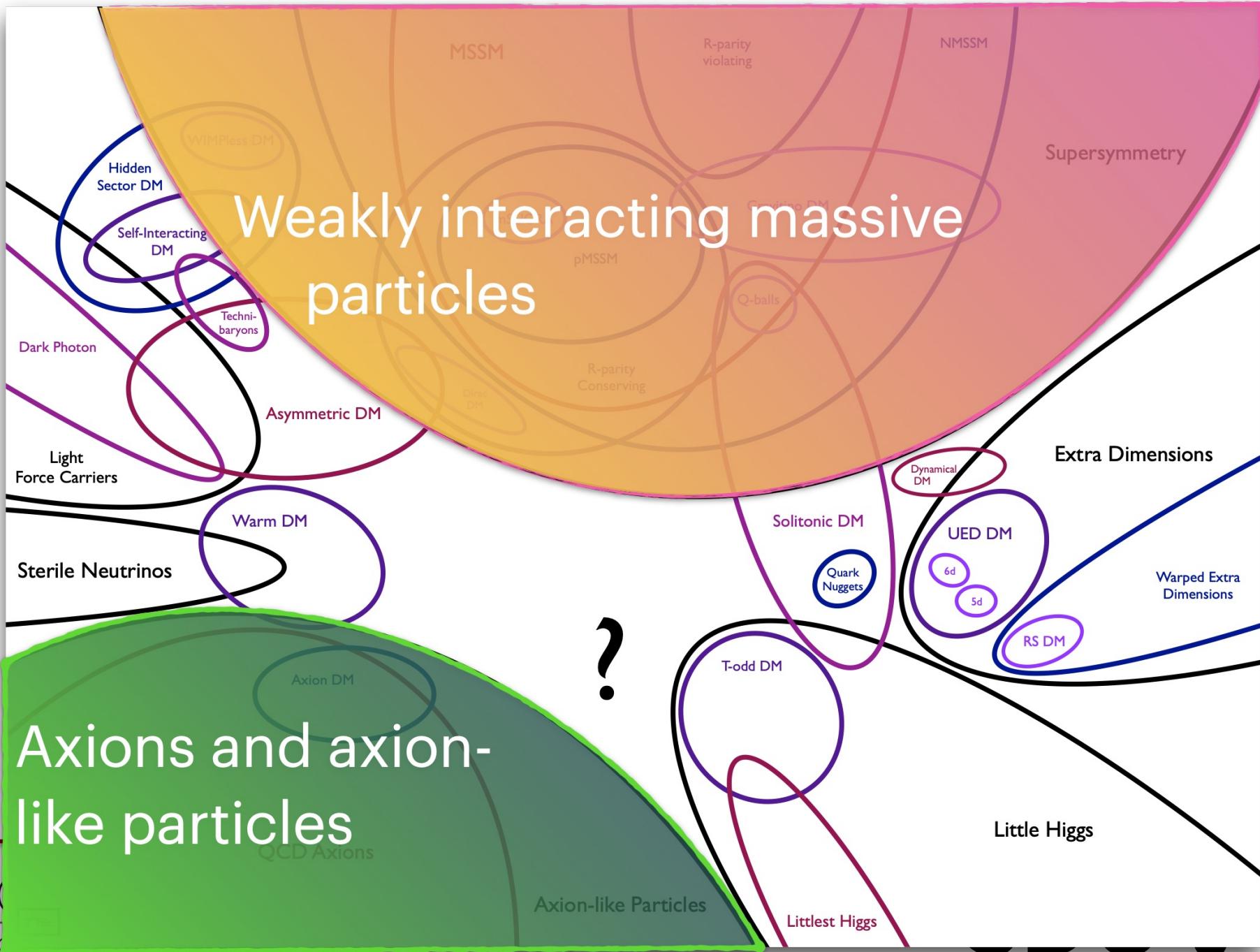
M. Shaposhnikov's lecture

Particle DM

- Particle physics candidates for DM particle
 - sterile neutrino
 - axion
 - WIMP M. Shaposhnikov's lecture

Particle DM





Particle DM strategies/classifications

- Generalize SM ‘DM candidates’:
 - Generalize the SM neutrino relic – see Shaposhnikovs lecture
 - Generalize the SM baryonic relic (neutron) – Composite DM

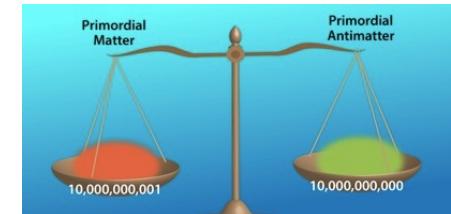
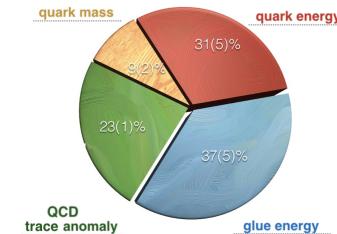
- Classify by the origin of the DM relic density:
 - SM neutrino relic – thermal freeze-out (WIMP)
 - SM baryonic relic (neutron) – asymmetry (Composite DM)

Baryonic relic density

- Proton stability (longevity) due to a **U(1) symmetry**
- Proton mass from **strong dynamics** (and Higgs)
- Proton relic density from some **asymmetry**
- **Neutron** lightest table baryon for zero current quark masses.
Self-interactions from strong dynamics

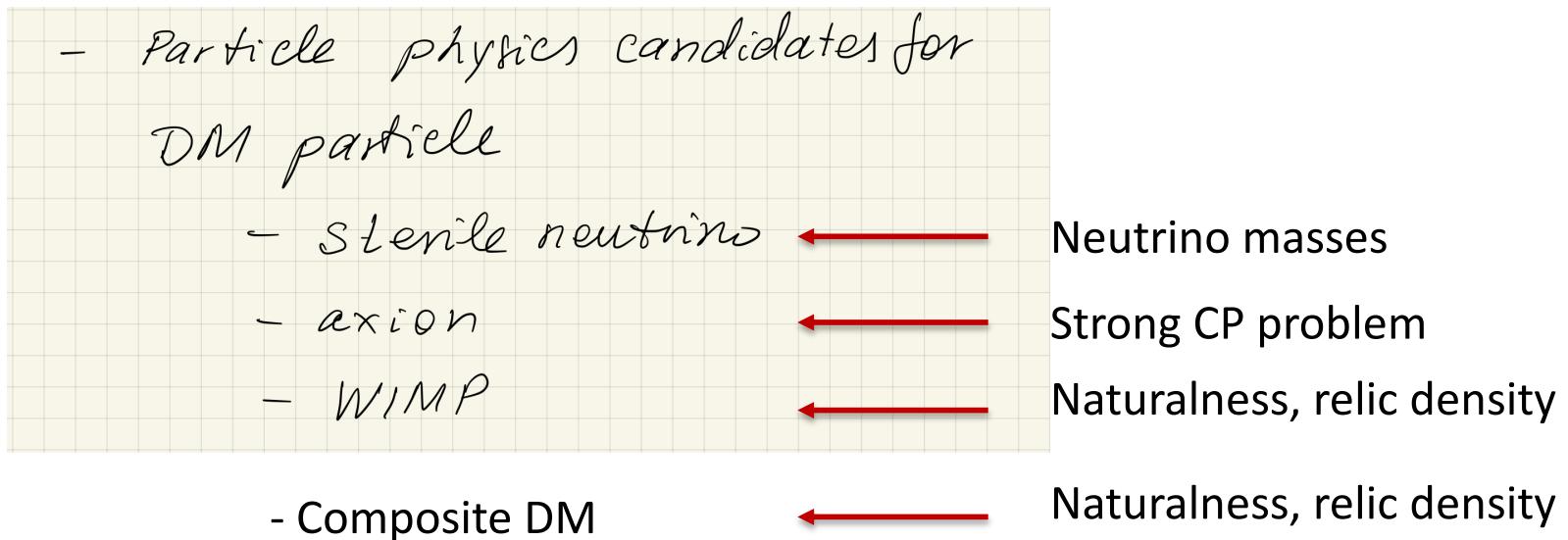
2 flavor massless QCD

$$SU(2)_L \times SU(2)_R \times U(1)_B \\ \rightarrow SU(2)_V \times U(1)_B$$



Particle DM strategies/classifications

➤ DM as byproduct(?) from solving other SM problems...



Axions

- Particle physics candidates for DM particle
 - Sterile neutrino
 - axion

Shaposhnikov lecture
Strong CP problem

The image shows a screenshot of a news article from the SDU website. The article is titled "Physicists to search for traces of dark matter in new experiment". It features a large photograph of a complex scientific apparatus, specifically the ALPSII detector, which consists of two long cylindrical vacuum tanks. The tanks are yellow and blue, and the entire setup is mounted on a blue platform with various pipes and equipment attached. The text below the photo reads: "Physicists to search for traces of dark matter in new experiment". The SDU logo is visible at the top left of the page.



Axions

QCD:

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F_{\mu\nu}^a + \sum_{\text{quarks}} \bar{q}_i \not{D} q_i$$

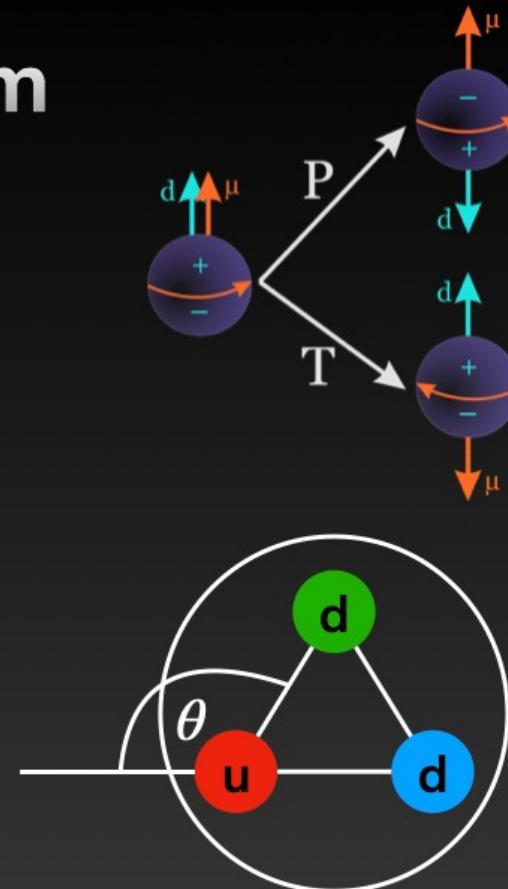
$$\sum_j m_{ij} \bar{q}_{iL} q_{jR} + h.c. + \frac{\alpha_s}{8\pi} \theta F_{\mu\nu}^a \tilde{F}_{\mu\nu}^a$$

$$\tilde{F}_{\mu\nu}^a = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} F_{\rho\sigma}^a$$

From M. Shaposhnikov's lecture
See this for further details

The strong CP problem

- Theory of strong force (QCD) predicts electric dipole moment of the neutron with strength $\theta \in [-\pi, \pi]$
- Violates **P** and **T** symmetry
- Calculation: $|d_n| \approx 2.4 \times 10^{-16} \theta e \text{ cm}$
- Measurement [Abel et al. 2020]: $|d_n| < 1.8 \times 10^{-26} e \text{ cm}$
- $\Rightarrow |\theta| < 0.8 \times 10^{-10}$



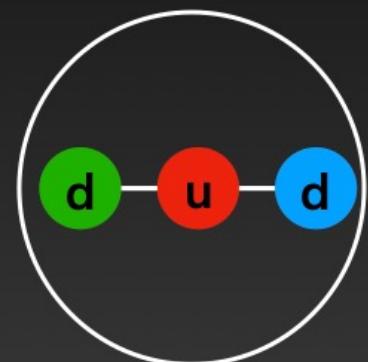
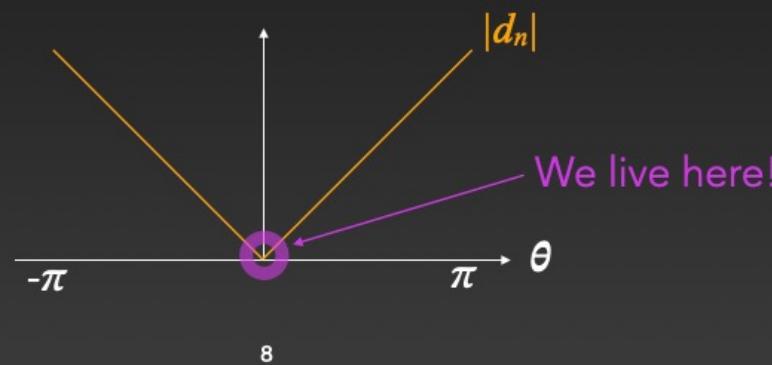
[Peccei & Quinn 1977;
Weinberg 1978; Wilczek 1978]
Slide credit: Ben Safdi & Axel Lindner

7

[Hook 2018]

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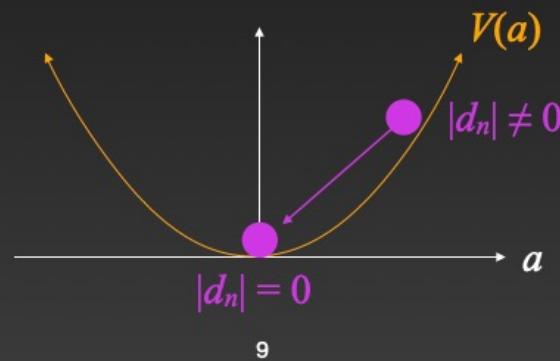
[Peccei & Quinn 1977;
Weinberg 1978; Wilczek 1978]
Slide credit: Ben Safdi & Axel Lindner

[Hook 2018]

Axion solves the strong CP problem

- $\theta \rightarrow a / f_a$ with scalar field a and scale f_a
- Potential $V(a)$ generated by QCD, axion acquires mass

$$m_a \approx 10^{-9} \text{ eV} \left(\frac{10^{16} \text{ GeV}}{f_a} \right)$$



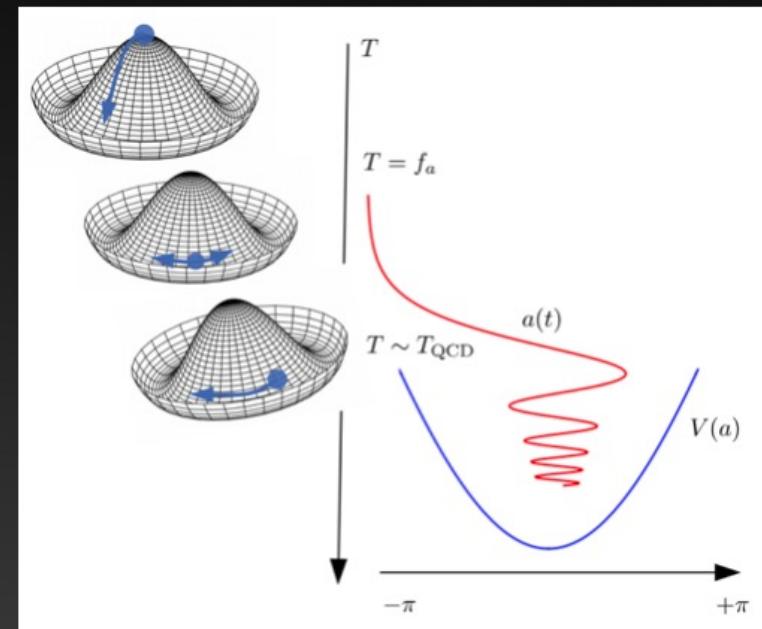
[Peccei & Quinn 1977;
Weinberg 1978; Wilczek 1978]

Axions as cold dark matter

Through misalignment mechanism

$$\ddot{a} + 3H(t)\dot{a} + m_a^2(t)a = 0$$

- Overdamped in early Universe as long as $3H \gg m_a$, field frozen at its initial value a_I
- Once $3H \sim m_a$ field will start to oscillate; happens at $t = t_{\text{osc}}$ or equivalently $T = T_{\text{osc}}$
- Oscillations have properties of cold dark matter

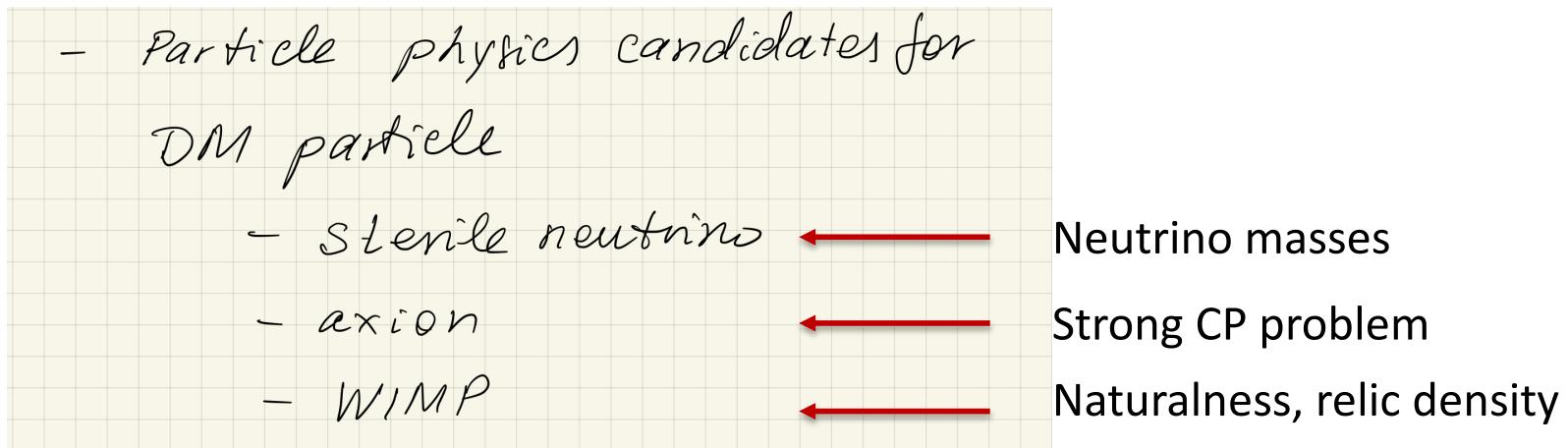


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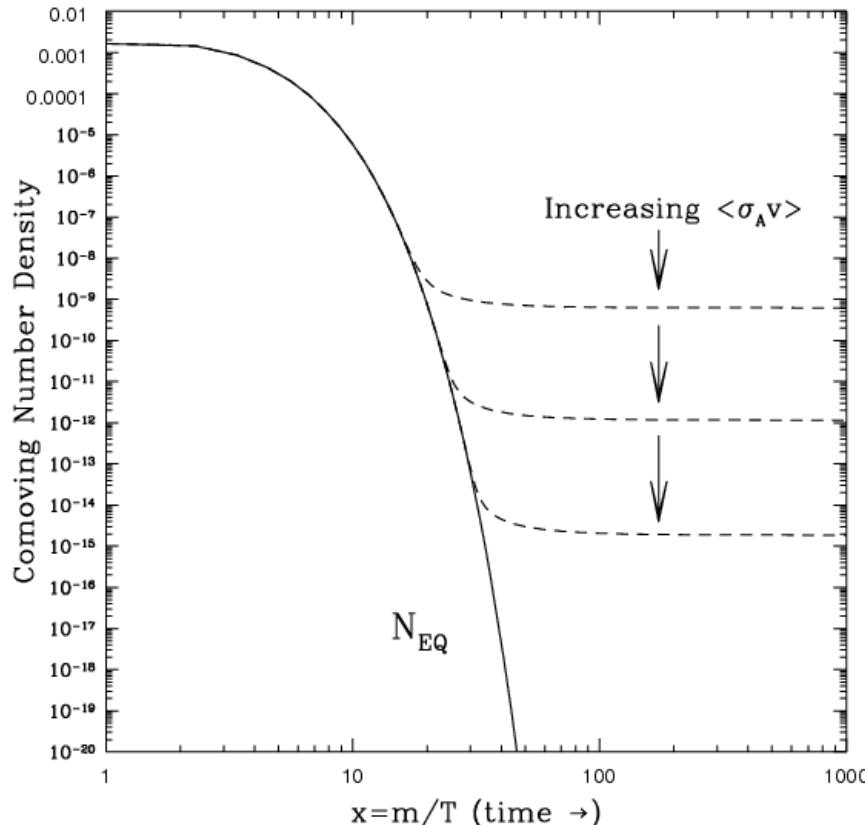
[See e.g. this PhD thesis, Marsh 1510.07633, Arias et al. 1201.5902]

Particle DM strategies/classifications

➤ DM as byproduct(?) from solving other SM problems...



WIMP DM



Computation of abundance

$\chi \bar{\chi} \leftrightarrow$ particles of the SM,

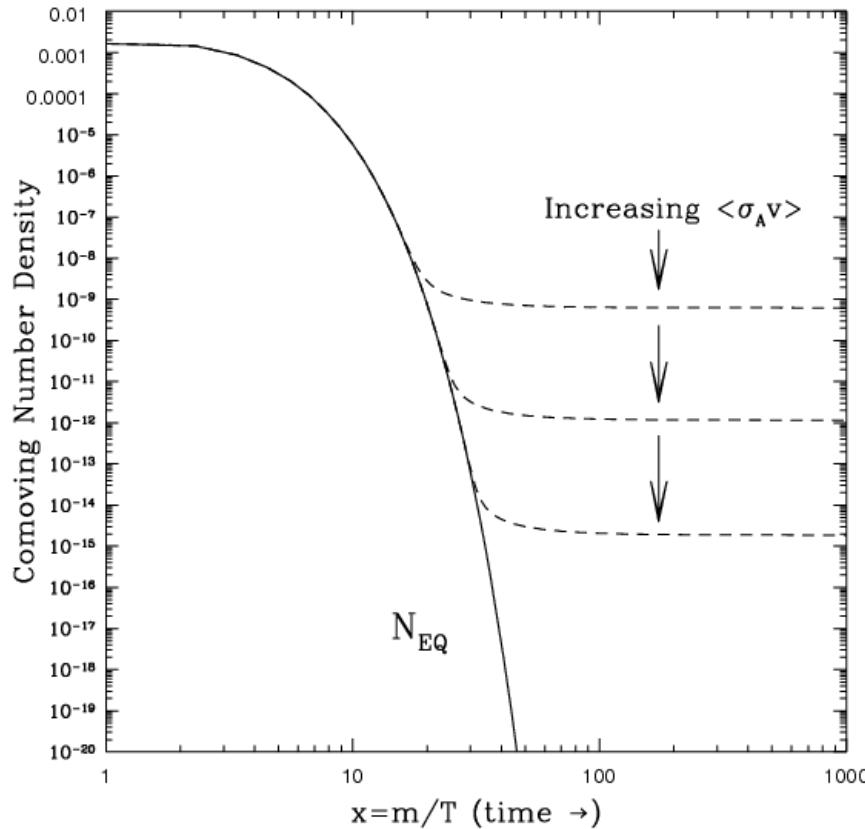
$$\Omega_{\text{ann}} = \frac{\sigma_0}{v} \leftarrow \text{velocity.}$$

Concentration of X :

$$n_X = g_X \left(\frac{M T}{2 \pi} \right)^{3/2} e^{-M/T}$$

spin factor

WIMP DM



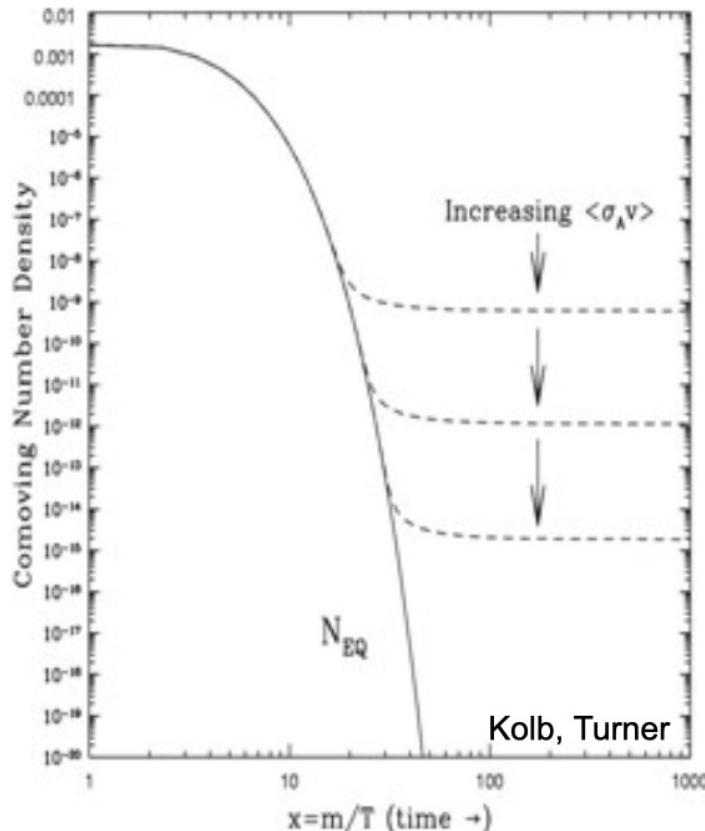
Freeze-out temperature

$$\langle \sigma v \rangle = H = \frac{T^2}{M_0}$$

↑
rate of reactions

↑
rate of expansion

THE WIMP MIRACLE



- Assume a new (heavy) particle X is initially in thermal equilibrium
- Its relic density is

$$\Omega_X \propto \frac{1}{\langle \sigma v \rangle} \sim \frac{m_X^2}{g_X^4}$$

$$\left. \begin{array}{l} m_X \sim m_{\text{weak}} \sim 100 \text{ GeV} \\ g_X \sim g_{\text{weak}} \sim 0.6 \end{array} \right\} \Omega_X \sim 0.1$$

Jonathan Feng
University of California, Irvine

Particle DM strategies/classifications

➤ DM as byproduct(?) from solving other SM problems...

- Particle physics candidates for DM particle
 - Sterile neutrino ← Neutrino masses
 - axion ← Strong CP problem
 - WIMP ← Naturalness, relic density

Particle DM strategies/classifications

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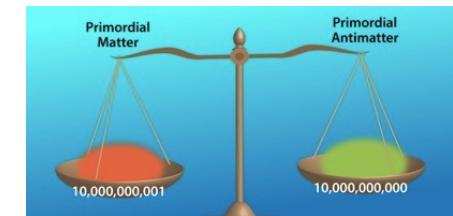
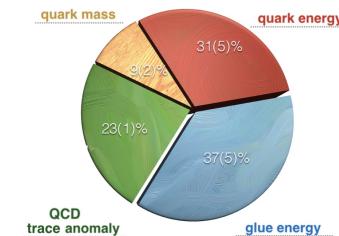
- Particle physics candidates for DM particle
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 - WIMP ← Naturalness, relic density
- Composite DM ← Naturalness, relic density

Baryonic relic density

- Proton stability (longevity) due to a **U(1) symmetry**
- Proton mass from **strong dynamics** (and Higgs)
- Proton relic density from some **asymmetry**
- **Neutron** lightest table baryon for zero current quark masses.
Self-interactions from strong dynamics

2 flavor massless QCD

$$SU(2)_L \times SU(2)_R \times U(1)_B \\ \rightarrow SU(2)_V \times U(1)_B$$



$$\Omega_{\text{DM}}/\Omega_{\text{B}} \sim 5$$

New Composite Dynamics

- 4d Gauge-Yukawa model with fermions and strong interactions
- May also (partially) break EW symmetry $\langle Q^I Q^J \rangle \sim f^3 E_Q^{IJ}$

$$\mathcal{L} = \mathcal{L}_{\text{SD}} + \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{SD+SM}}$$

CD breaks EW:
e.g TC, CH

$$\mathcal{O}_{\text{CD}} \sim QQ$$

$$\mathcal{L} = \mathcal{L}_{\text{SD}} + \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{SD+SM}}$$

CD induces EW breaking:
e.g. PCH,

$$\mathcal{O}_{\text{CD+SM}} \sim QHQ$$

$$\mathcal{O}_{\text{CD+SM}} \sim QQH^\dagger H$$

$$\mathcal{L} = \mathcal{L}_{\text{SD}} + \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{SD+SM}}$$

SM breaks EW:
e.g. SIDM

$$\mathcal{O}_{\text{SM}} \sim H^\dagger H$$

(Spergel & Steinhardt)

New Composite Dynamics

- 4d Gauge-Yukawa model with fermions and strong interactions
- May also (partially) break EW symmetry $\langle Q^I Q^J \rangle \sim f^3 E_Q^{IJ}$

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CD induces EW breaking:
e.g. PCH,

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SM breaks EW:
e.g. SIDM

$$\mathcal{O}_{SM} \sim H^\dagger H$$

(Spergel & Steinhardt)

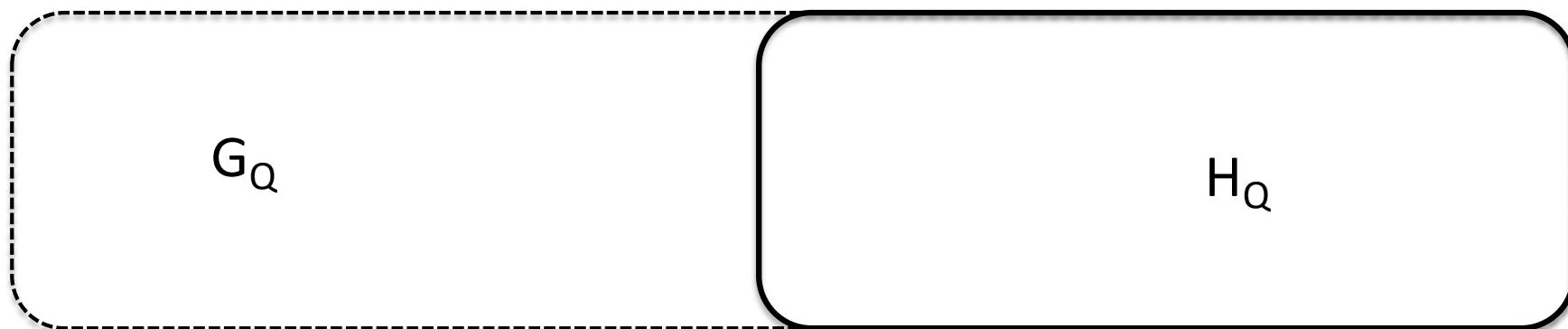
New Composite Dynamics

UV: $\mathcal{L}_{UV} = \bar{Q}\gamma^\mu D_\mu Q + \mathcal{L}_{SM-Higgs} + \delta\mathcal{L}$

IR: $\langle Q^I Q^J \rangle \sim f^3 E_Q^{IJ}$

$$G_Q \supset SU(2) \times SU(2) \times U(1) \quad \rightarrow \quad H_Q \supset SU(2) \times U(1)$$

SM custodial symmetry DM symmetry



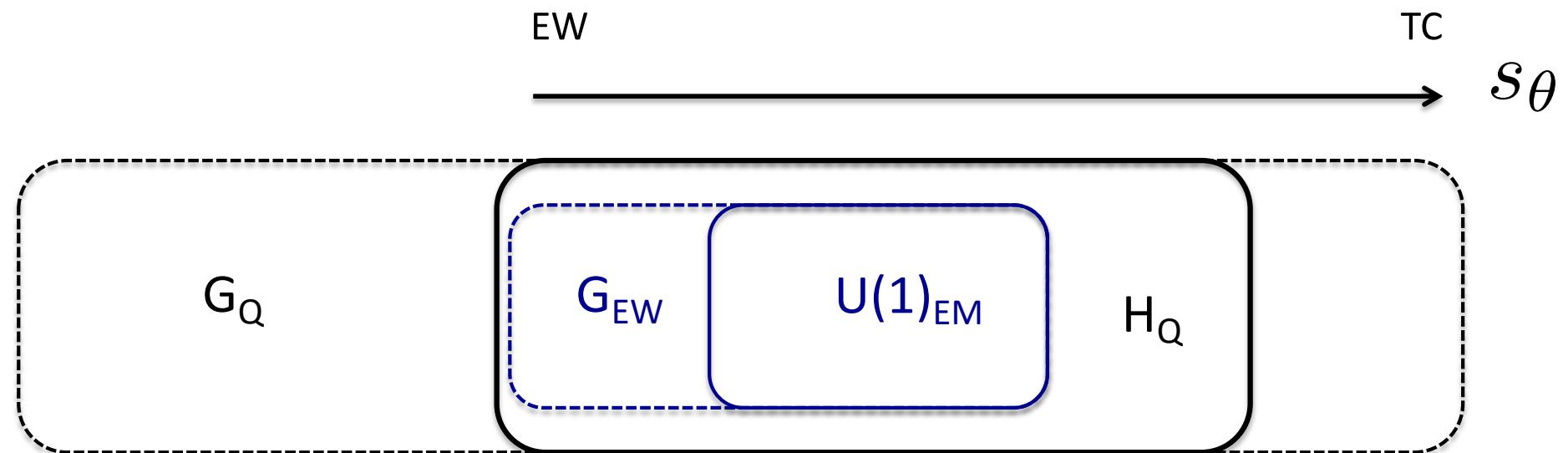
Framework: Composite Dynamics

UV: $\mathcal{L}_{UV} = \bar{Q}\gamma^\mu D_\mu Q + \mathcal{L}_{SM-Higgs} + \delta\mathcal{L}$

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$$G_Q \supset SU(2) \times SU(2) \times U(1) \quad \rightarrow \quad H_Q \supset SU(2) \times U(1)$$

SM custodial symmetry DM symmetry



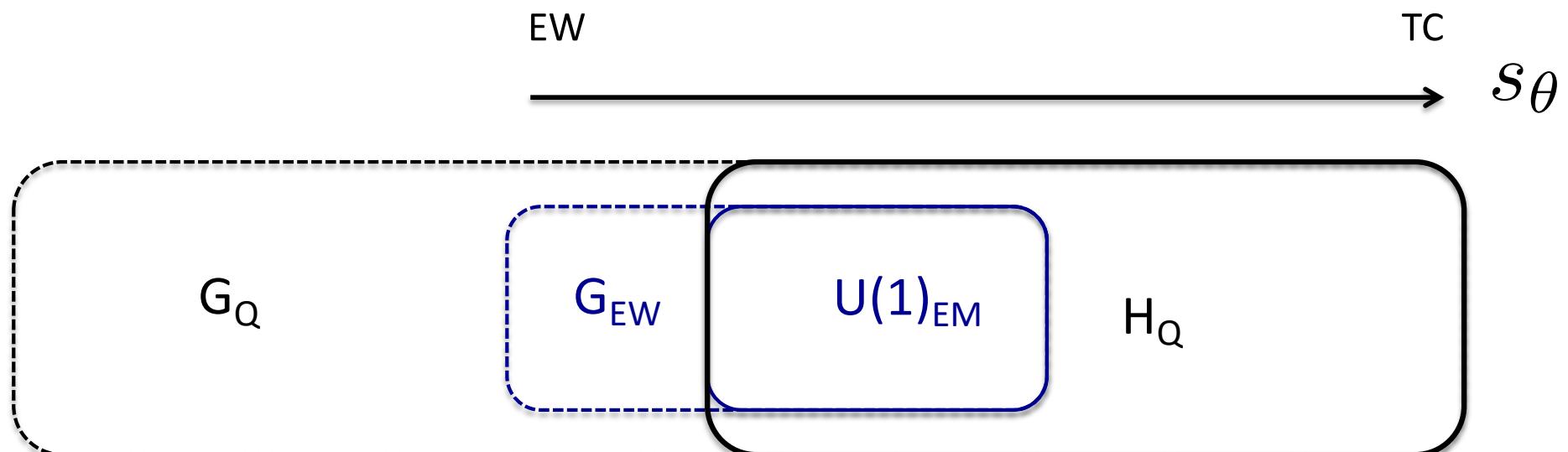
New Composite Dynamics

UV: $\mathcal{L}_{UV} = \bar{Q}\gamma^\mu D_\mu Q + \mathcal{L}_{SM-Higgs} + \delta\mathcal{L}$

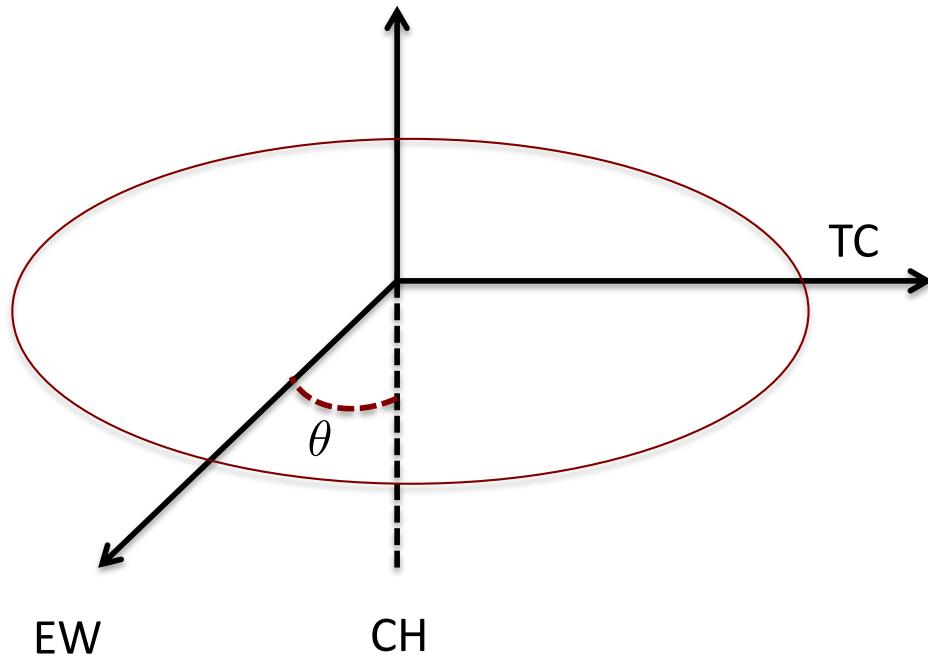
IR: $\langle Q^I Q^J \rangle \sim f^3 E_Q^{IJ}$

$$G_Q \supset SU(2) \times SU(2) \times U(1) \quad \rightarrow \quad H_Q \supset SU(2) \times U(1)$$

SM custodial symmetry DM symmetry



SU(2) Composite Dynamics with 2 flavors



Framework: Composite Dynamics

$$\text{UV: } \mathcal{L}_{UV} = \bar{Q}\gamma^\mu D_\mu Q + \mathcal{L}_{SM-Higgs} + \delta\mathcal{L} \quad \text{IR: } \langle Q^I Q^J \rangle \sim f^3 E_Q^{IJ}$$

$$G_Q \supset SU(2) \times SU(2) \times U(1) \quad \rightarrow \quad H_Q \supset SU(2) \times U(1)$$

SM custodial symmetry DM symmetry

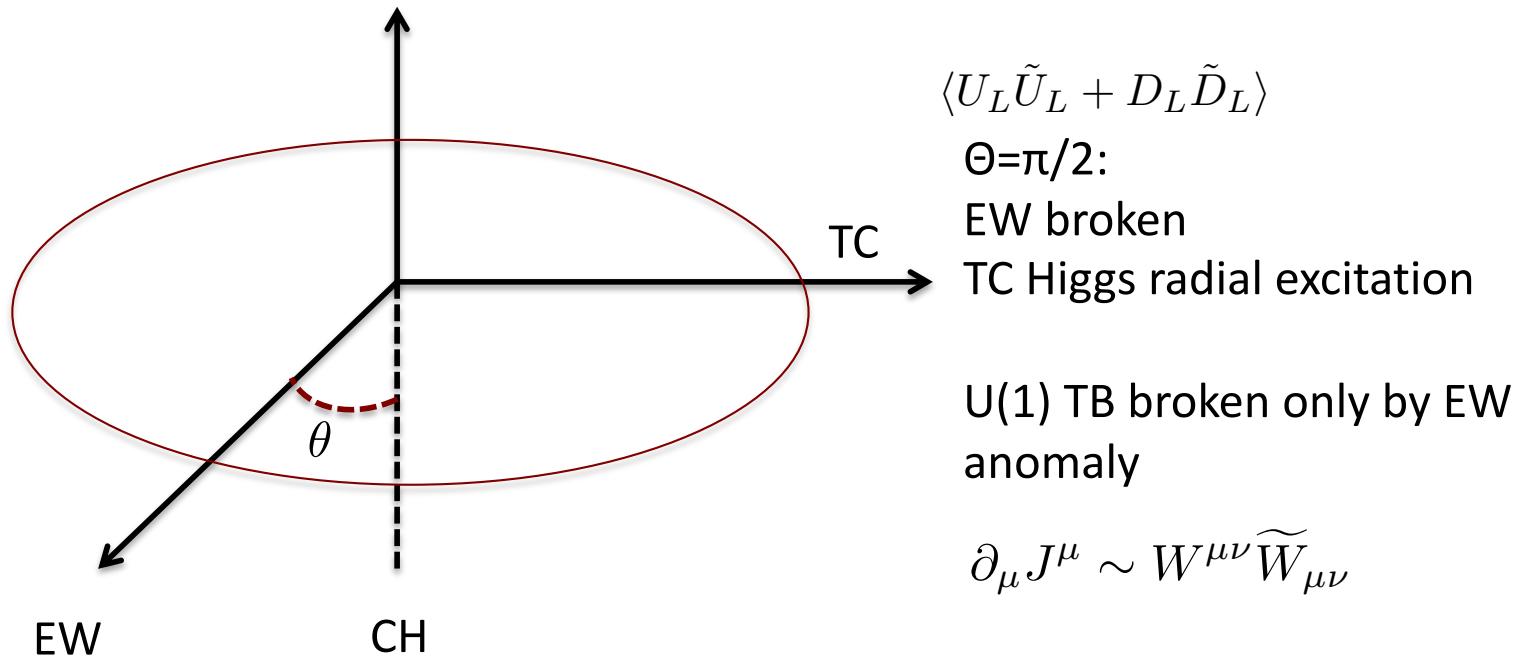
$$\text{Example: } G_Q = SU(4) \quad \rightarrow \quad H_Q = Sp(4)$$

	SU(2) _{TC}	SU(2) _W	U(1) _Y
(U_L, D_L)	□	□	0
\tilde{U}_L	□	1	-1/2
\tilde{D}_L	□	1	+1/2

$$Q = \begin{pmatrix} U_L \\ D_L \\ \tilde{U}_L \\ \tilde{D}_L \end{pmatrix}$$

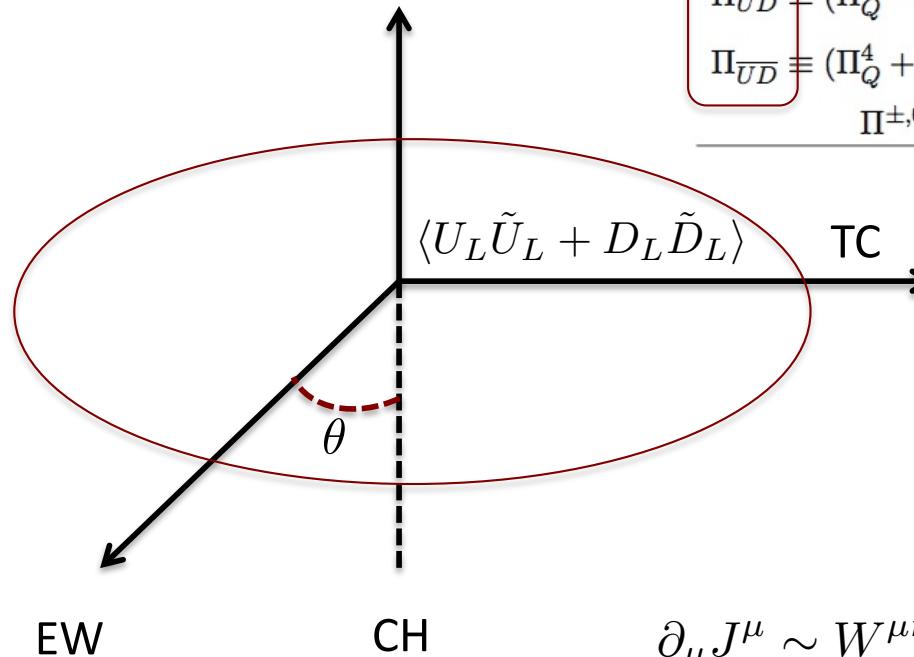
Which condensate Preserves/breaks EW

SU(2) Composite Dynamics with 2 flavors



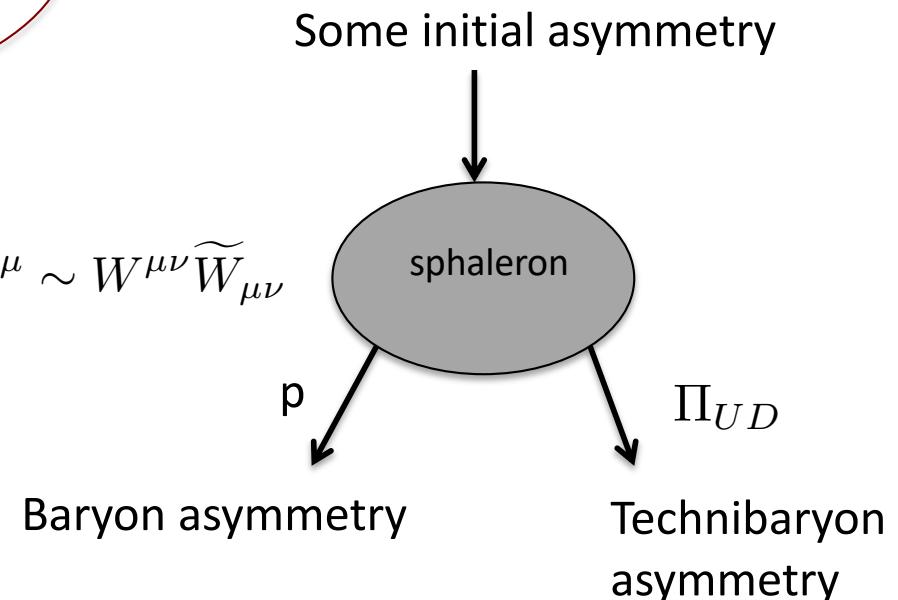
Technicolor limit

Compelling, apparently wrong limit



Composites	$U(1)_{\text{TB}}$	$U(1)_{\text{EM}}$	Θ
$\Pi_{UD} \equiv (\Pi_Q^4 - i\Pi_Q^5)/\sqrt{2} \sim U^T C D$	$\frac{1}{\sqrt{2}}$	0	$\pi/2$
$\Pi_{\bar{U}\bar{D}} \equiv (\Pi_Q^4 + i\Pi_Q^5)/\sqrt{2} \sim \bar{U} C \bar{D}^T$	$-\frac{1}{\sqrt{2}}$	0	$\pi/2$
$\Pi^{\pm,0} \equiv \Pi^{1,2,3}$	0	$\pm 1, 0$	$\pi/2$

$$\mathcal{L}_{\text{kin}} \supset -\frac{g^2}{2} s_\theta^2 W_\mu^+ W^{-\nu} \Pi_{UD} \bar{\Pi}_{UD}$$



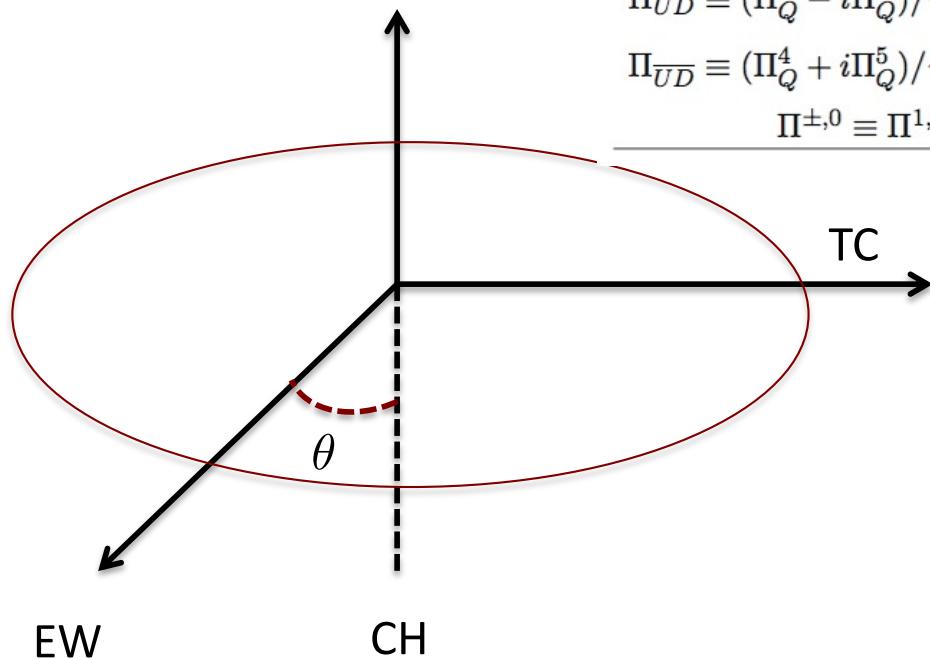
Technicolor

- Technibaryon stability (longevity) due to a U(1) symmetry
- Technibaryon mass from new strong dynamics (and Higgs)
- Technibaryon relic density from baryon asymmetry
- Self-interactions from new strong dynamics
(though not necessarily big enough to address cusp-core)

Observed Higgs physics not obviously consistent with TC!

Framework: Composite Higgs

Composites	$U(1)_{\text{TB}}$	$U(1)_{\text{EM}}$	Θ
$\Pi_{UD} \equiv (\Pi_Q^4 - i\Pi_Q^5)/\sqrt{2} \sim U^T CD$	$\frac{1}{\sqrt{2}}$	0	$\pi/2$
$\Pi_{\bar{U}\bar{D}} \equiv (\Pi_Q^4 + i\Pi_Q^5)/\sqrt{2} \sim \bar{U} C \bar{D}^T$	$-\frac{1}{\sqrt{2}}$	0	$\pi/2$
$\Pi^{\pm,0} \equiv \Pi^{1,2,3}$	0	$\pm 1, 0$	$\pi/2$



Composites	$U(1)_{\text{TB}}$	$U(1)_{\text{EM}}$	Θ
$h \equiv \Pi_Q^4 \sim \bar{U}U + \bar{D}D$	–	0	0
$\eta \equiv \Pi_Q^5 \sim \text{Im } U^T CD$	–	0	0
$\Pi^{\pm,0} \equiv \Pi^{1,2,3}$	0	$\pm 1, 0$	0

No underlying stabilizing symmetry
for the CH range of parameters

(Galloway, Evans, Luty & Tacchi '10; Ferretti & Karateev '13;
Cacciapaglia & Sannino'14; Alanne, Buarque Franzosi & MTF '17)

Summary

- Composite Dynamics compelling framework for DM and EW
U(1) stabilizing symmetries, dynamical symmetry breaking, naturalness, non-triviality, predictability (lattice)
- Vast space of models from 4d gauge-fermion-Yukawa theories
CH limit yields pNGB Higgs with properties tunably close to the SM Higgs.
Correlated with DM turning WIMPy (in studied model)
- Lattice and diverse experiments test underlying models

