

# Hyperon polarization and its correlation with directed flow in heavy ion collisions

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# Outline

## 1. Introduction

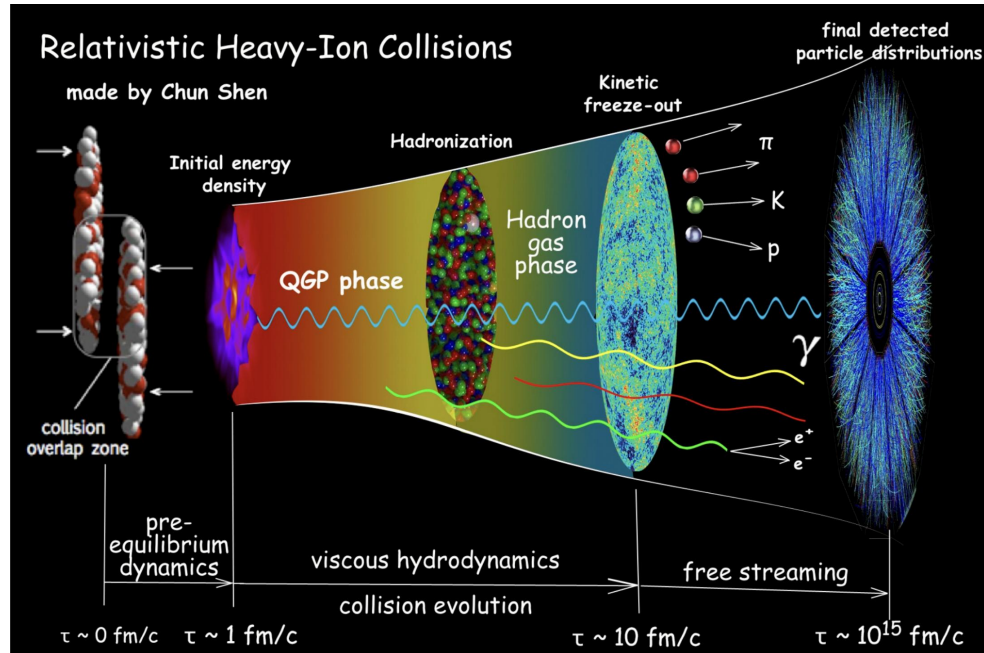
## 2. Theory framework

- tilted initial condition
- (3+1)-D hydrodynamic CLVisc
- spin polarization

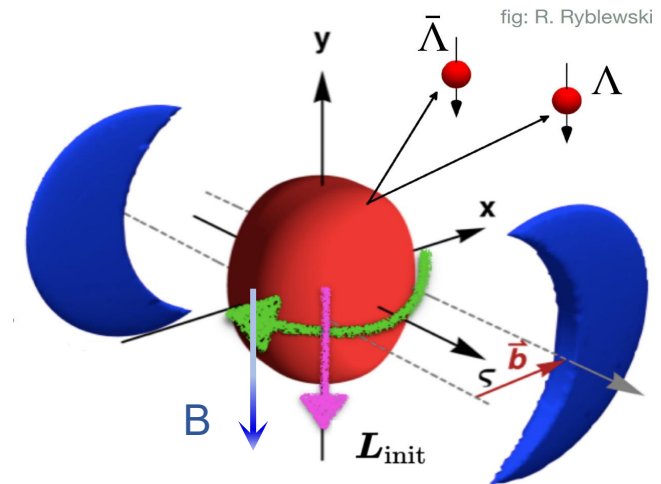
## 3. Numerical results

## 4. Summary

# Introduction



“ Standard Model ” of heavy ion collision



Spin physics in a strongly coupled system.  
CKT: CME, CVE, CVW and spin-hydrodynamic.

# Introduction: global polarization

Using screened potential model to calculate the global quark polarization

Z. T. Liang, X. N. Wang, Phys. Rev. Lett. 94 (2005) 102301

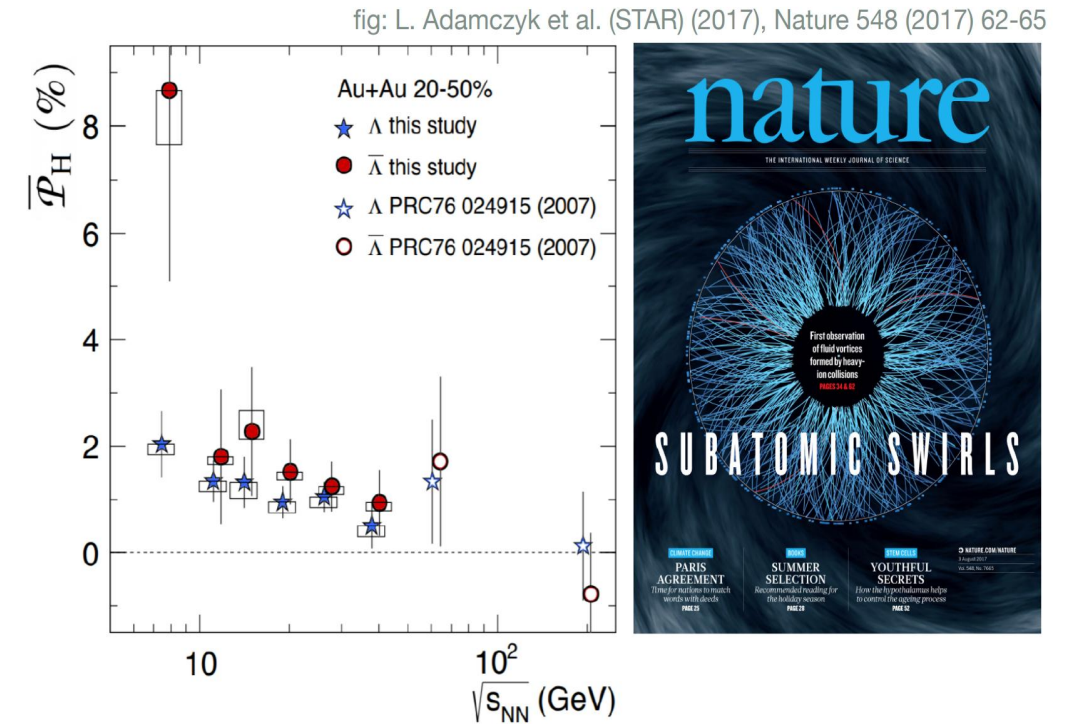
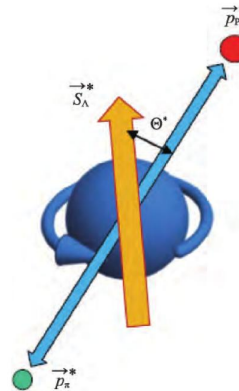
$\Lambda$  and  $\bar{\Lambda}$  hyperons are “self-analysing”,  $\Lambda \rightarrow p + \pi$ , the proton tends to be emitted along the spin direction of the parent hyperons

$$\frac{dN}{d \cos \theta^*} = \frac{1}{2} \left( 1 + \alpha_H |\mathcal{P}_H| \cos \theta^* \right)$$

$\theta^*$ : the angle between proton momentum

And  $\Lambda$  polarization vector  $\mathcal{P}_H$

$\alpha_H$ : the decay parameter



$$\omega = (P_\Lambda + P_{\bar{\Lambda}}) k_B T / \hbar \sim 0.6 - 2.7 \times 10^{22} \text{ s}^{-1}$$

...the hottest, least viscous – and most vortical – fluid produced in the laboratory...

# Introduction: global polarization

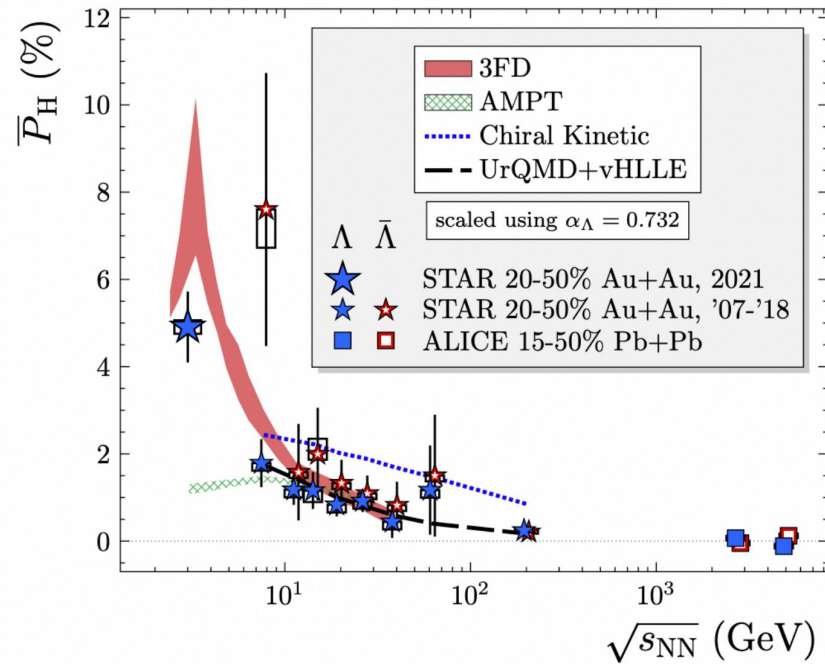
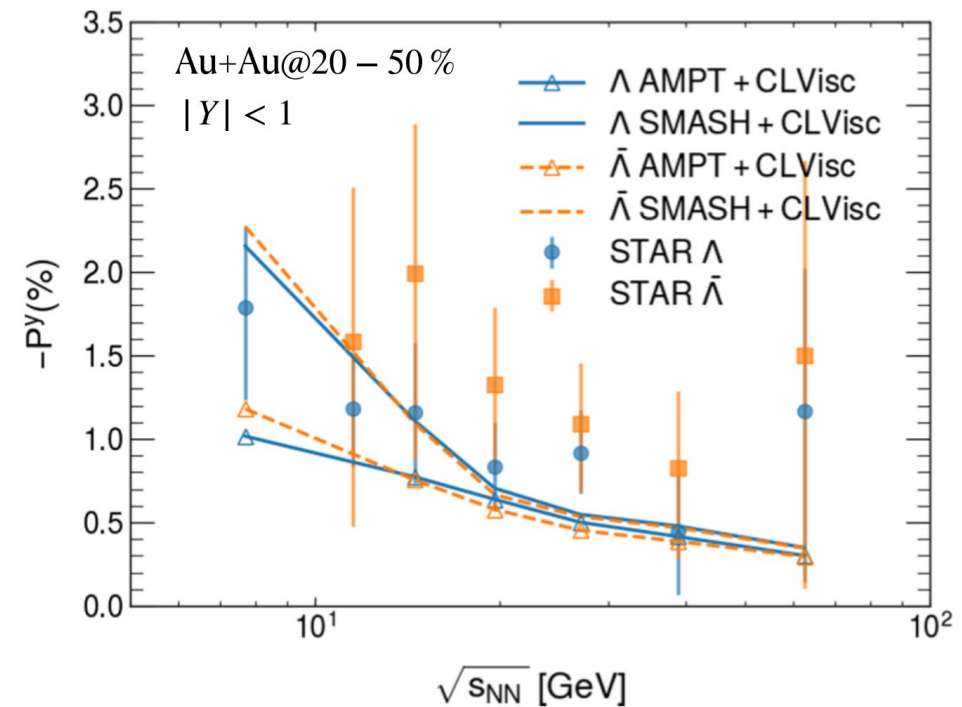


Fig: CLVisc 2.0, Xiangyu Wu



- Hydrodynamic model and transport model reproduce the global polarization of  $\Lambda$  hyperons above 7.7 GeV
- The global polarization is sensitive to the initial state of the system

# Initial condition: longitudinal tilted geometry of QGP

Jiang, Wu, Cao, Zhang, Phys. Rev. C 107, 034904 (2023)

Based on the results of directed flow  $v_1$ , a counter-clockwise tilted of the medium profile is expected in the reaction plane

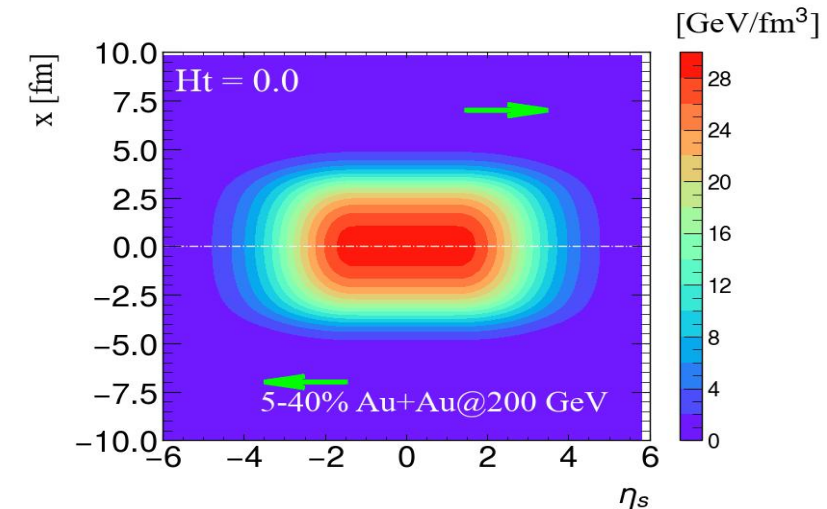
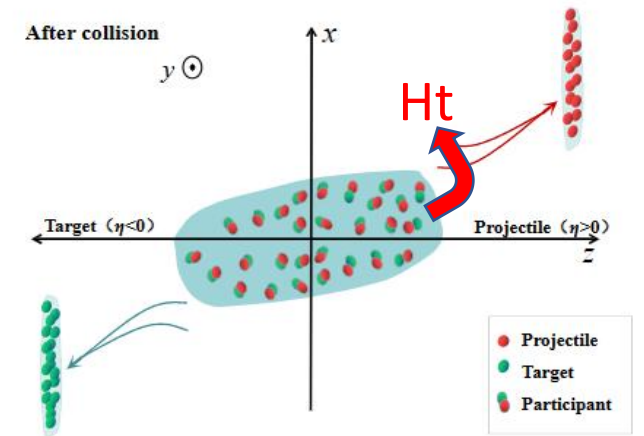
$$W_N(x, y, \eta_s) = T_1(x, y) + T_2(x, y) + \boxed{H_t} [T_1(x, y) - T_2(x, y)] \tan\left(\frac{\eta_s}{\eta_t}\right)$$

A larger value of  $H_t$  gives a more tilted fireball in the reaction plane.

The total weight function:  $W(x, y, \eta_s) = \frac{(1 - \alpha)W_N(x, y, \eta_s) + \alpha n_{BC}(x, y)}{[(1 - \alpha)W_N(0, 0, 0) + \alpha n_{BC}(0, 0)]|_{\mathbf{b}=0}}$

The initial energy density  $\varepsilon_0(x, y, \eta_s) = K \cdot W(x, y, \eta_s) \cdot H(\eta_s)$

The initial local baryon density:  $n(x, y, \eta_s) = \frac{1}{N} W(x, y, \eta_s) H(\eta_s) H_B(\eta_s)$



# Initial condition: initial fluid velocity field

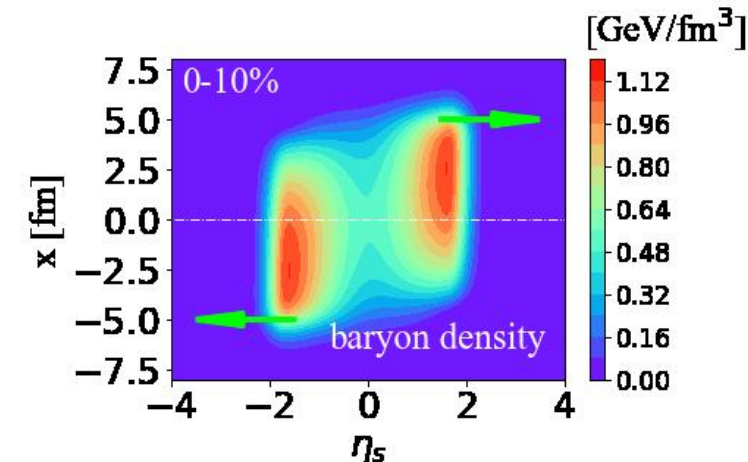
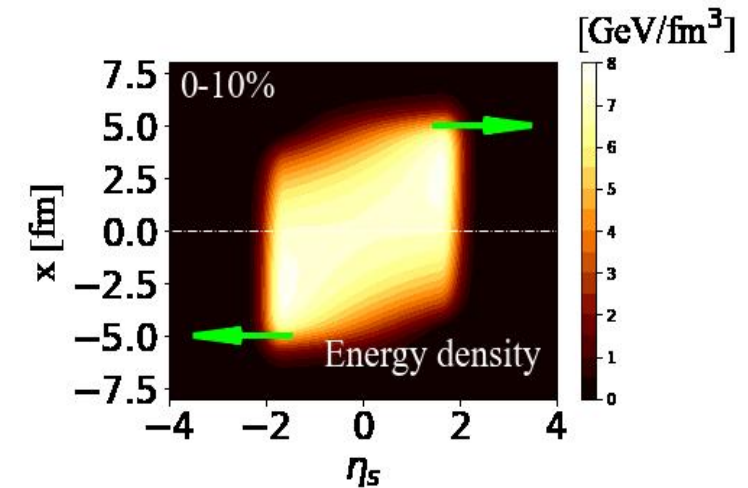
Ryu, Jopic, Shen, Phys. Rev. C 104 (2021) 5, 054908

At the initial proper time  $\tau_0$ , the initial energy-momentum tensor components are:

$$\left\{ \begin{array}{l} T^{\tau\eta_s} = \frac{1}{\tau_0} \varepsilon_0(x, y, \eta_s) \sinh(y_L) \\ T^{\tau\tau} = \varepsilon_0(x, y, \eta_s) \cosh(y_L) \\ y_L \equiv \boxed{f_v} y_{\text{CM}} \\ y_{\text{CM}} = \text{arctanh} \left[ \frac{T_1 - T_2}{T_1 + T_2} \tanh(y_{\text{beam}}) \right] \end{array} \right.$$

This  $f_v \in [0,1]$  parameter allows one to vary the magnitude of the longitudinal flow velocity gradient.

The transverse expansion is ignored:  $T^{\tau x} = T^{\tau y} = 0$  at  $\tau = \tau_0$ .



Au+Au @ 27 GeV

# Hydrodynamic evolution: (3+1)-D CLVisc

Wu, Qin, Pang, Wang, Phys. Rev. C 105 (2022) 3, 034909

Energy-momentum conservation and net baryon current conservation:

$$\begin{aligned}\nabla_{\mu} T^{\mu\nu} &= 0 & T^{\mu\nu} &= eU^{\mu}U^{\nu} - P\Delta^{\mu\nu} + \pi^{\mu\nu} \\ \nabla_{\mu} J^{\mu} &= 0 & J^{\mu} &= nU^{\mu} + V^{\mu}\end{aligned}$$

Equation of motion of dissipative current:

$$\begin{aligned}\Delta_{\alpha\beta}^{\mu\nu} D\pi^{\alpha\beta} &= -\frac{1}{\tau_{\pi}} (\pi^{\mu\nu} - \eta\sigma^{\mu\nu}) - \frac{4}{3}\pi^{\mu\nu}\theta - \frac{5}{7}\pi^{\alpha\langle}\sigma_{\alpha}^{\mu\nu}\rangle + \frac{9}{70}\frac{4}{e+P}\pi_{\alpha}^{\langle\mu}\pi^{\nu\rangle\alpha} \\ \Delta^{\mu\nu} DV_{\mu} &= -\frac{1}{\tau_V} \left( V^{\mu} - \kappa_B \nabla^{\mu} \frac{\mu}{T} \right) - V^{\mu}\theta - \frac{3}{10}V_{\nu}\sigma^{\mu\nu}\end{aligned}$$

The shear viscosity:  $\eta = C_{\eta} \frac{e+p}{T}$

The baryon diffusion:  $\kappa_B = \frac{C_B}{T} n \left( \frac{1}{3} \cot \left( \frac{\mu_B}{T} \right) - \frac{nT}{e+P} \right)$

Equation of state: NEOS-BQS



The polarization pseudo vector for spin  $\frac{1}{2}$  particles

$$\mathcal{S}^\mu(\mathbf{p}) = \frac{\int d\Sigma \cdot p \mathcal{J}_5^\mu(p, X)}{2m \int d\Sigma \cdot \mathcal{N}(p, X)}$$

axial charge current density

fermions number density

For massless fermions,  $S(p)$  can be decomposed into different sources

$$\mathcal{S}^\mu(\mathbf{p}) = \mathcal{S}_{\text{thermal}}^\mu(\mathbf{p}) + \mathcal{S}_{\text{shear}}^\mu(\mathbf{p}) + \mathcal{S}_{\text{accT}}^\mu(\mathbf{p}) + \mathcal{S}_{\text{chemical}}^\mu(\mathbf{p}) + \mathcal{S}_{\text{EB}}^\mu(\mathbf{p})$$

$$\mathcal{S}_{\text{thermal}}^\mu(\mathbf{p}) = \int d\Sigma^\sigma F_\sigma \epsilon^{\mu\nu\alpha\beta} p_\nu \partial_\alpha \frac{u_\beta}{T}$$

$$\mathcal{S}_{\text{shear}}^\mu(\mathbf{p}) = \int d\Sigma^\sigma F_\sigma \frac{\epsilon^{\mu\nu\alpha\beta} p_\nu u_\beta}{(u \cdot p) T} p^\rho (\partial_\rho u_\alpha + \partial_\alpha u_\rho - u_\rho D u_\alpha)$$

$$\mathcal{S}_{\text{accT}}^\mu(\mathbf{p}) = - \int d\Sigma^\sigma F_\sigma \frac{\epsilon^{\mu\nu\alpha\beta} p_\nu u_\alpha}{T} \left( D u_\beta - \frac{\partial_\beta T}{T} \right)$$

$$\mathcal{S}_{\text{chemical}}^\mu(\mathbf{p}) = 2 \int d\Sigma^\sigma F_\sigma \frac{1}{(u \cdot p)} \epsilon^{\mu\nu\alpha\beta} p_\alpha u_\beta \partial_\nu \frac{\mu}{T}$$

$$\mathcal{S}_{\text{EB}}^\mu(\mathbf{p}) = 2 \int d\Sigma^\sigma F_\sigma \left[ \frac{\epsilon^{\mu\nu\alpha\beta} p_\alpha u_\beta E_\nu}{(u \cdot p) T} + \frac{B^\mu}{T} \right]$$

Thermal vorticity

Shear viscous tensor

Fluid acceleration

Gradient of chemical potential

Electromagnetic Fields

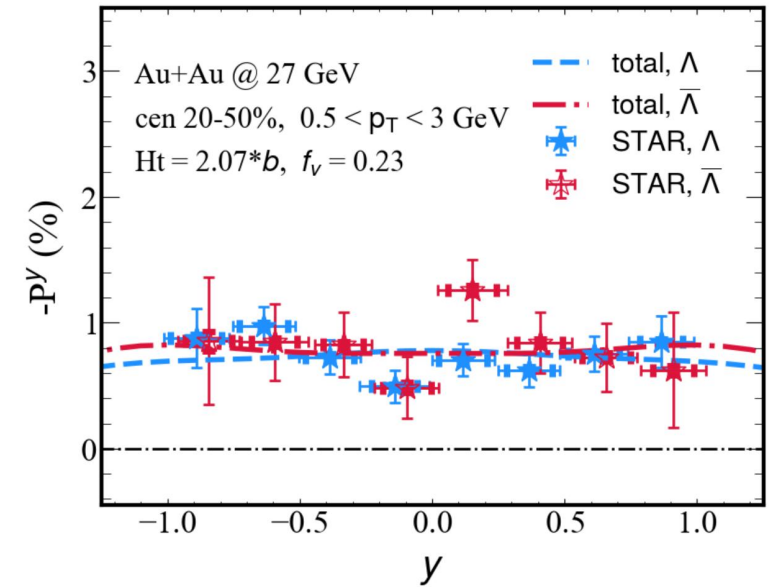
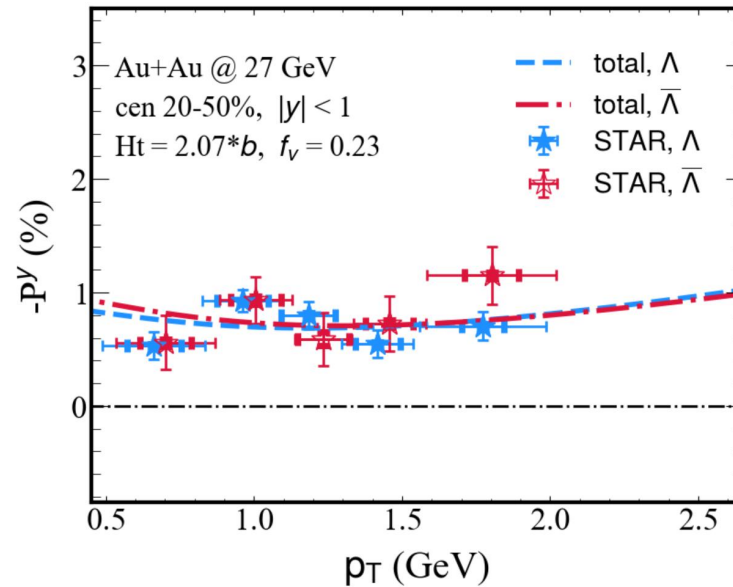
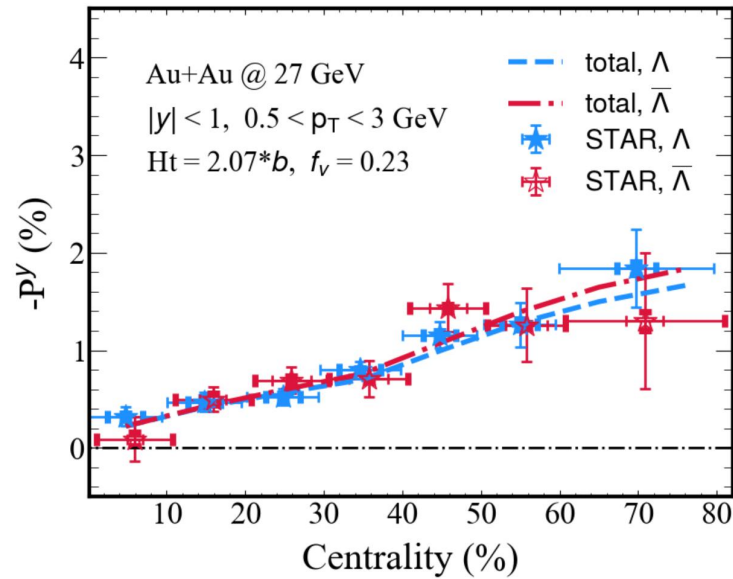
Here,

$$F^\mu = \frac{\hbar}{8m_\Lambda \Phi(\mathbf{p})} p^\mu f_{\text{eq}}(1 - f_{\text{eq}})$$

$$\Phi(\mathbf{p}) = \int d\Sigma^\mu p_\mu f_{\text{eq}}.$$

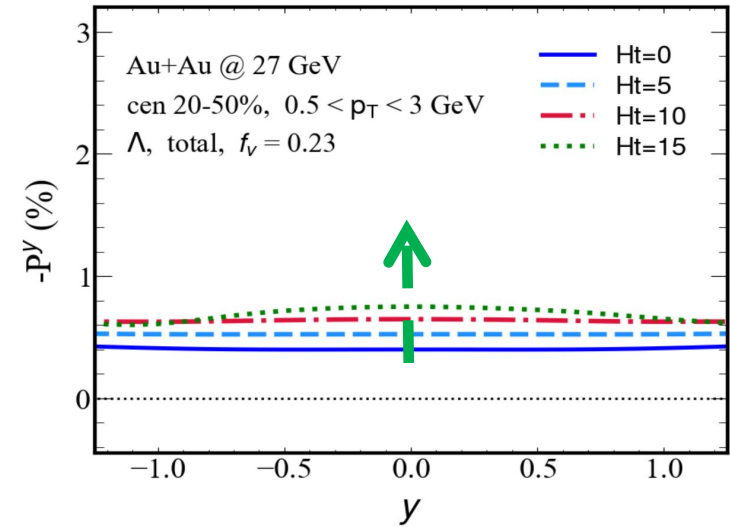
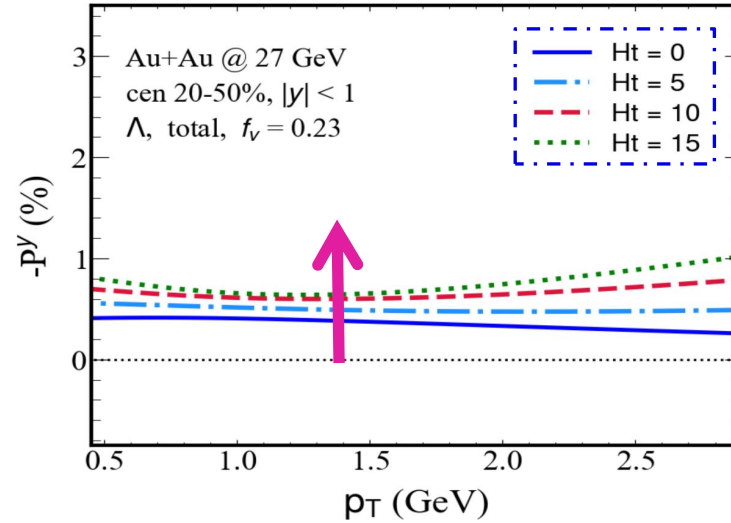
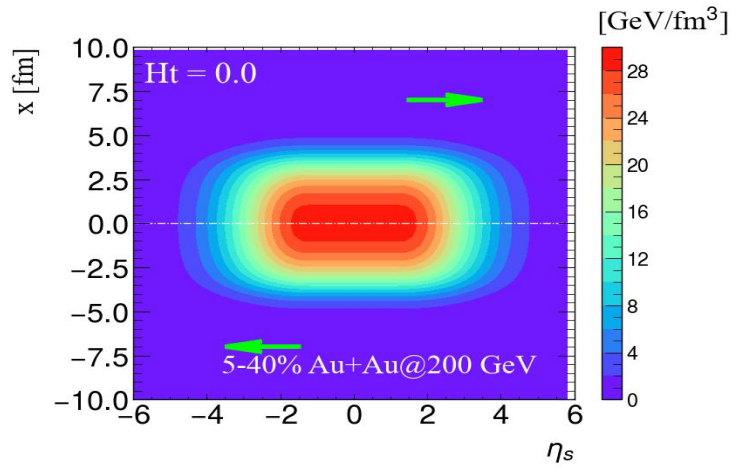
# Global polarization @ 27 GeV

STAR, arXiv: 2305.08705



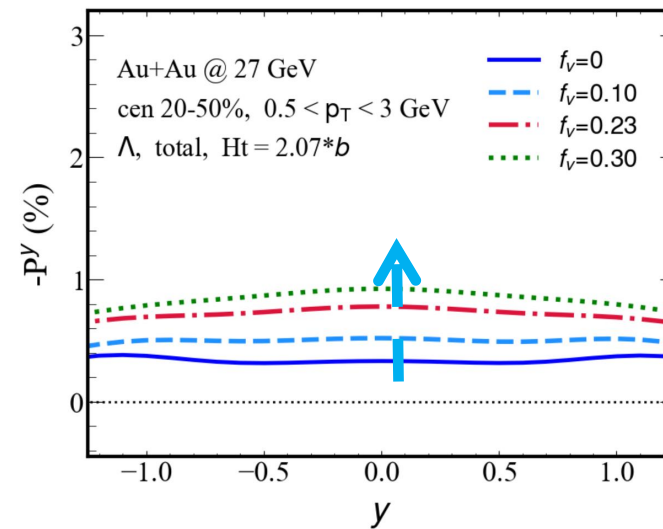
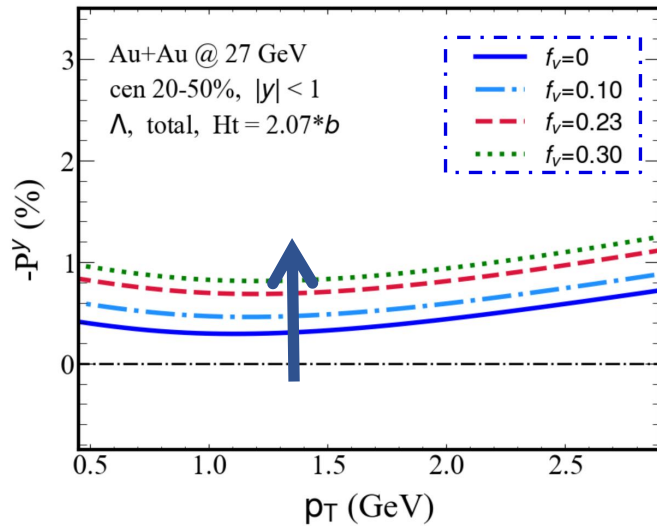
- Modified optical Glauber model coupled with CLVisc reproduce the STAR data.
- Total = thermal + shear + accT + Chemical

# Global polarization (effects of the tilted geometry)



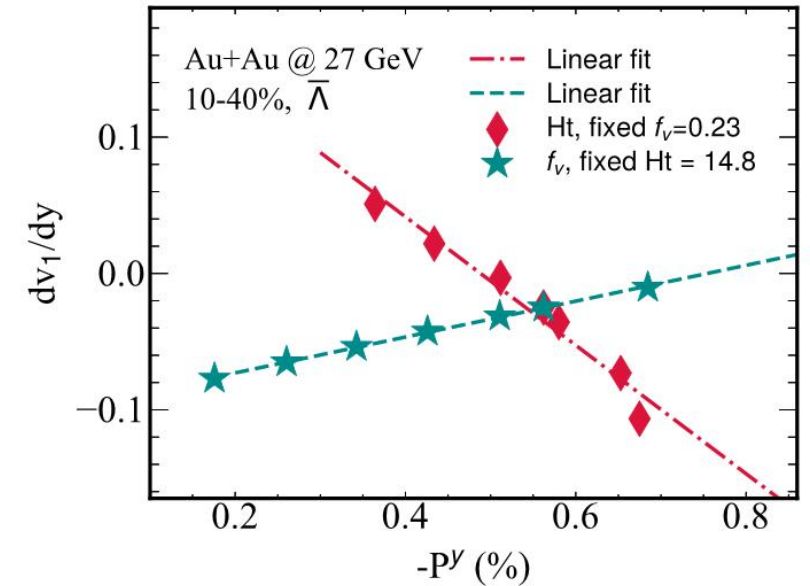
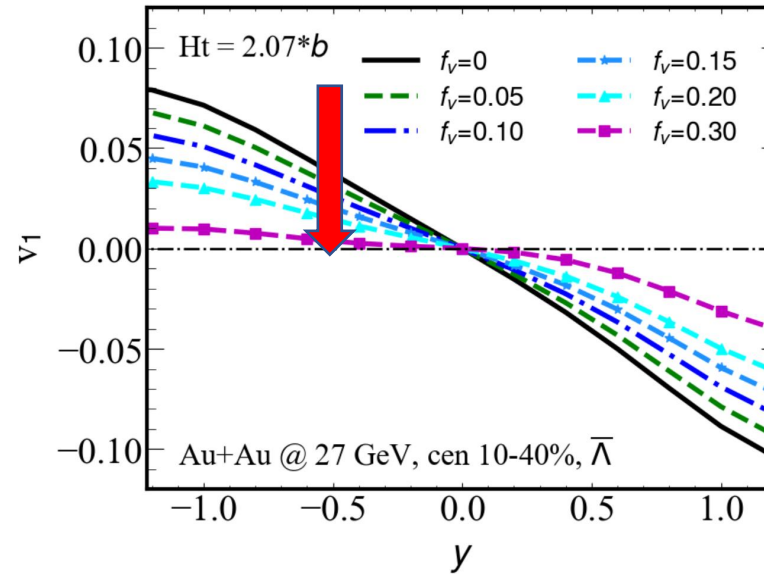
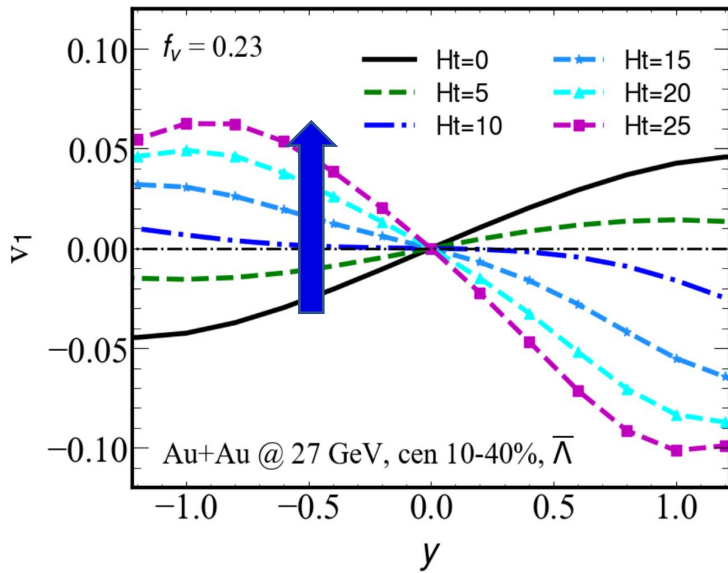
- The magnitude of  $-P^y$  is amplified with increasing  $Ht$  from 0 to 15.
- A non-monotonic behavior of polarization with respect to  $p_T$  appears when  $Ht$  is large.

# Global polarization (effects of longitudinal flow gradient)



- The stronger longitudinal velocity gradient (or larger  $f_v$ ) leads to a larger magnitude of the global vorticity and therefore the global polarization of hyperons.

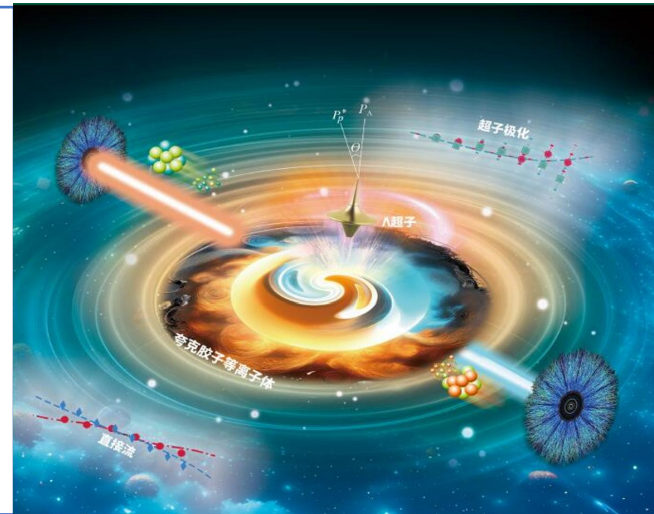
# Correlation between global polarization and directed flow



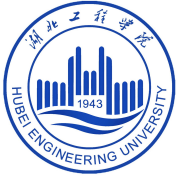
- When  $Ht$  is fixed, increasing  $f_v$  increases  $dv_1/dy$  and  $-P^y$ , resulting in a positive correlation.
- When  $f_v$  is fixed, increasing  $Ht$  increases  $-P^y$  but decreases  $dv_1/dy$ , resulting in an anti-correlation.

- We discuss the effects of tilted geometry and initial longitudinal flow of the QGP on the hyperon polarization.
- We propose a possible correlation between hyperon polarization and directed flow.

Köszönöm!  
Thank you!  
谢谢!



Many thanks to my supervisor in Hungary: prof. T. Csörgő and Prof. M. Csanád



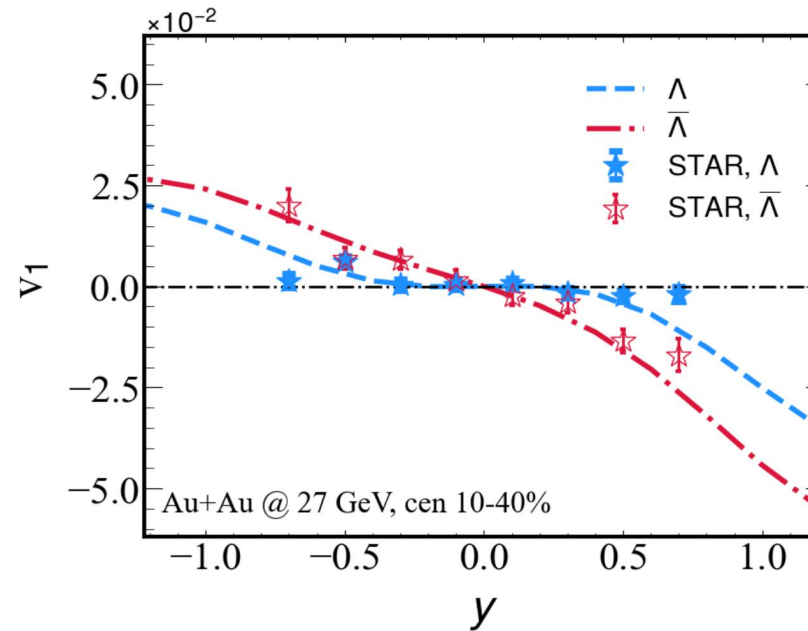
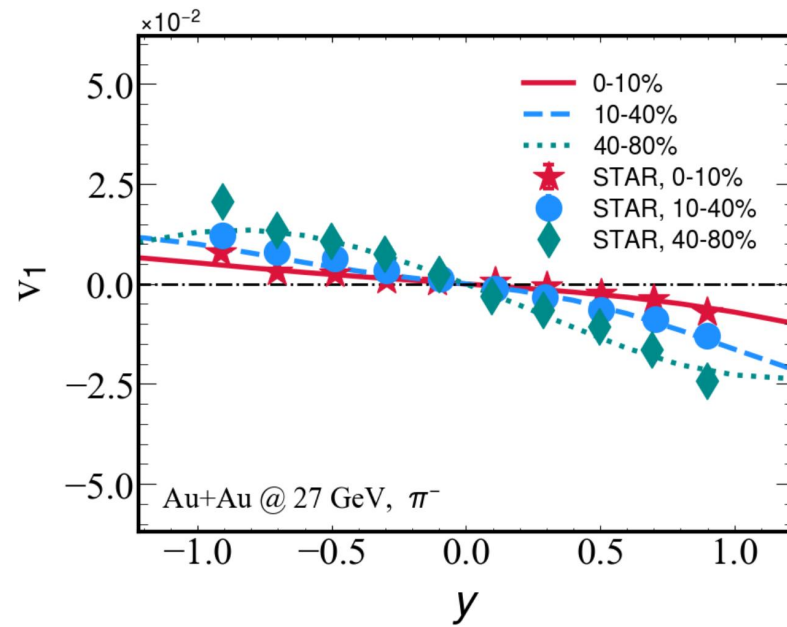
**Backup**



# directed flow $v_1$

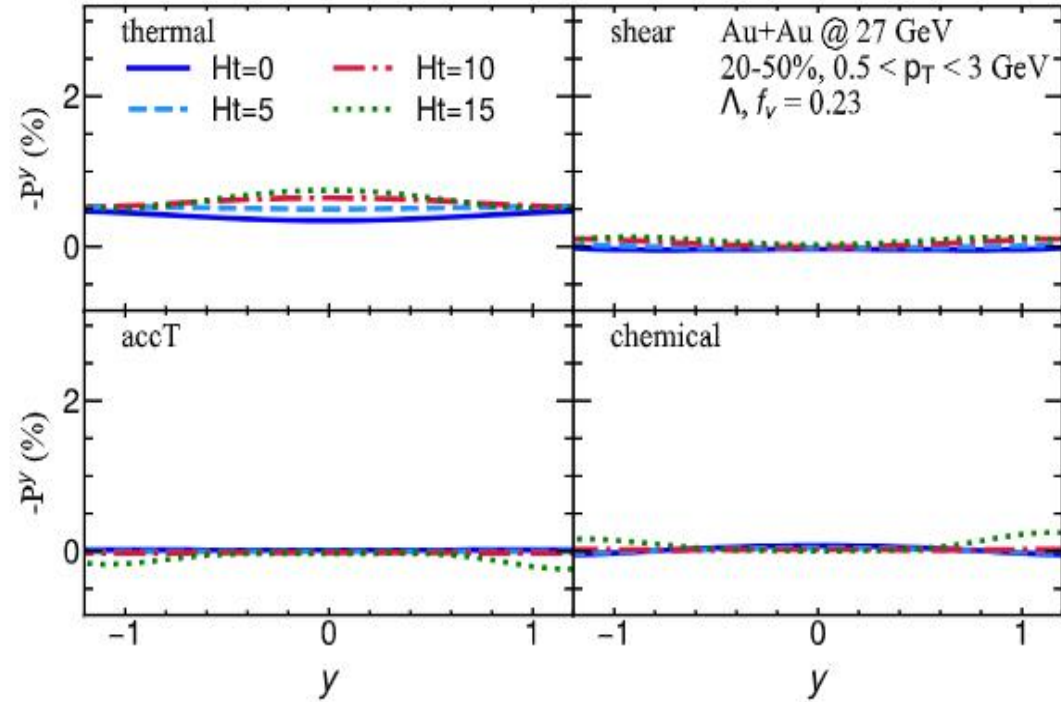
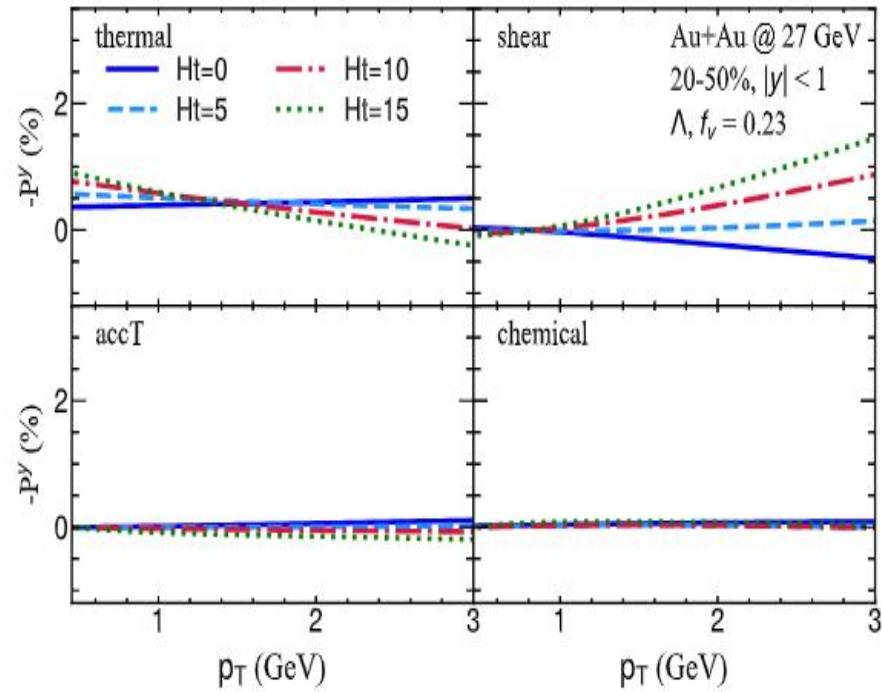
$$v_1 = \langle p_x/p_T \rangle$$

Jiang, Wu, Cao, Zhang, Phys. Rev. C 107, 034904 (2023)

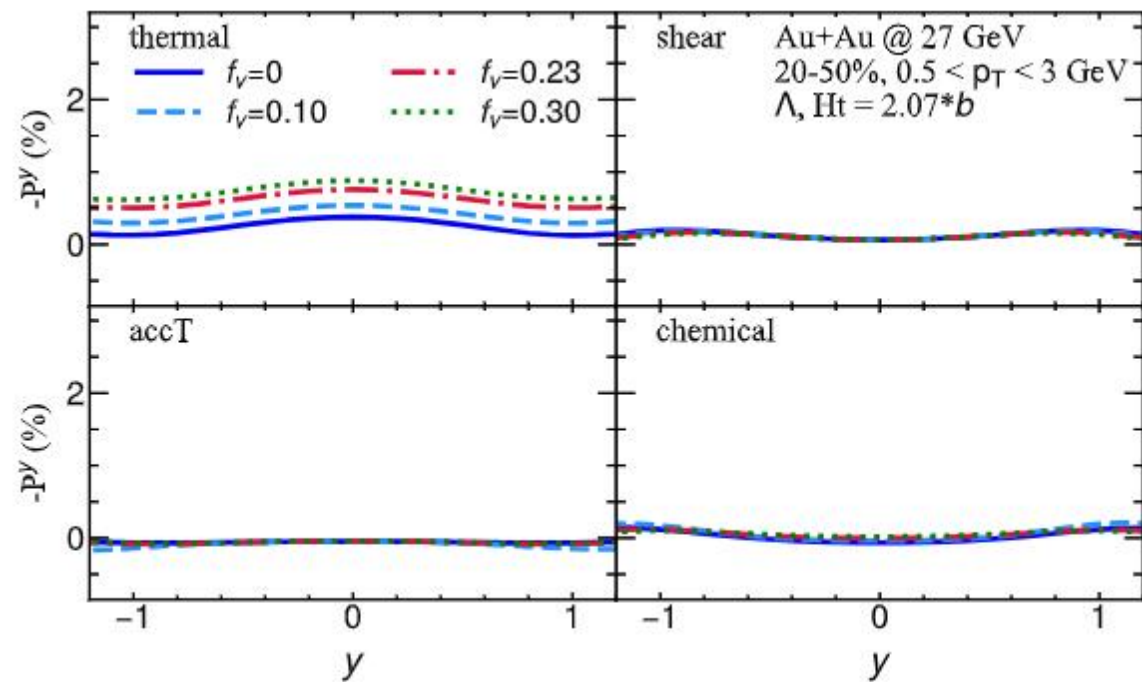
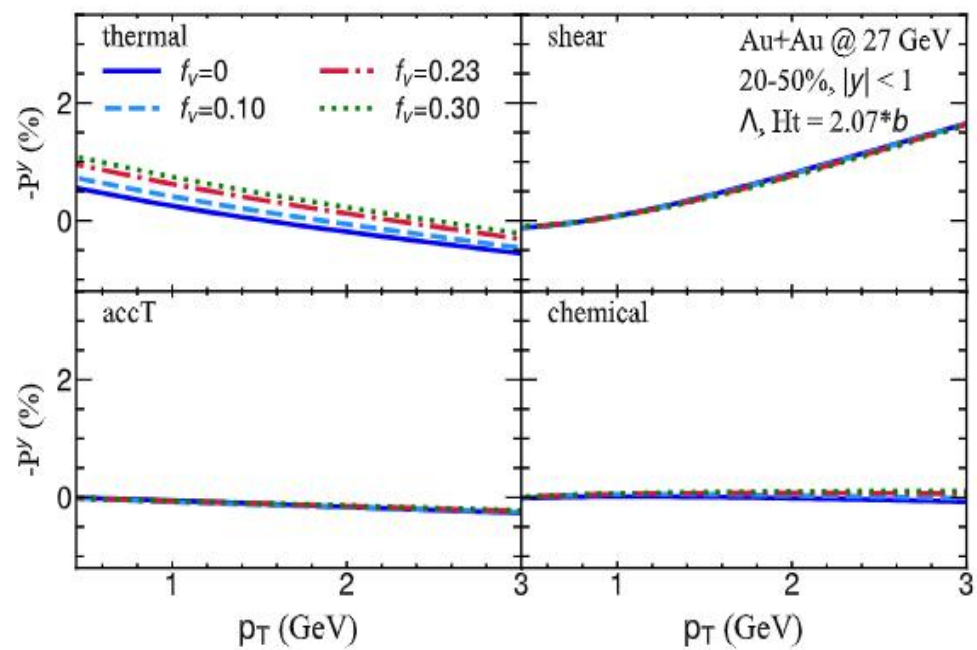


- $v_1$  is sensitive to the QGP volume, size, asymmetry shape and velocity field in transverse plane.
- Longitudinal shape and size of the QGP can be reconstructed from  $v_1$  data!

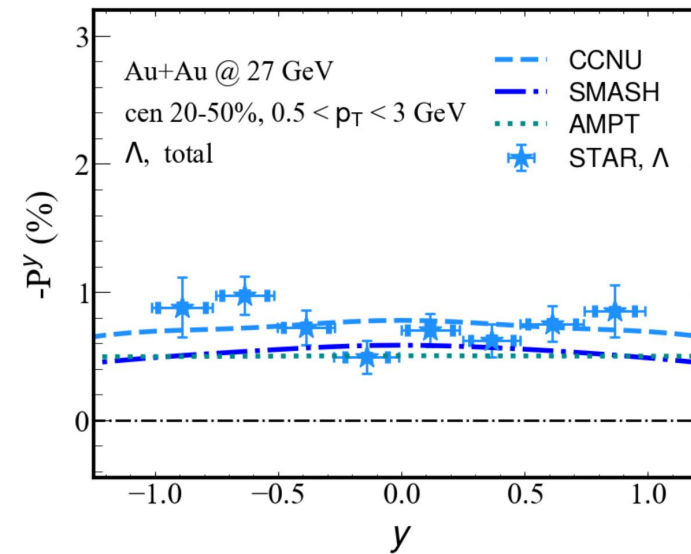
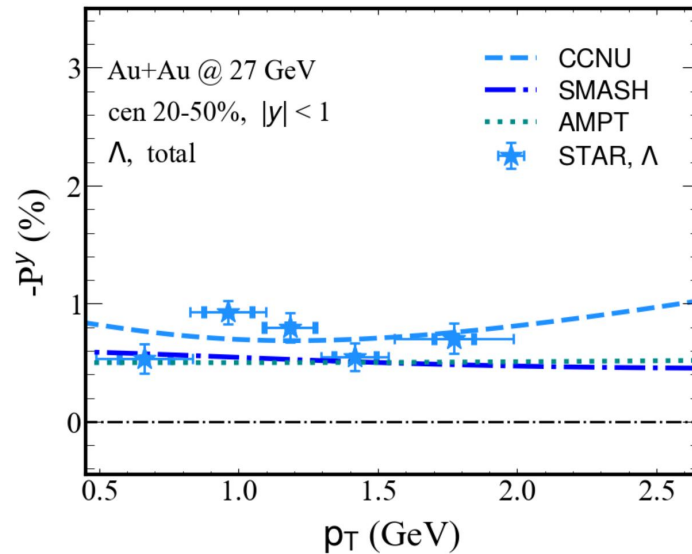
# Global polarization (different tilted fireball)



# Global polarization (different velocity field)



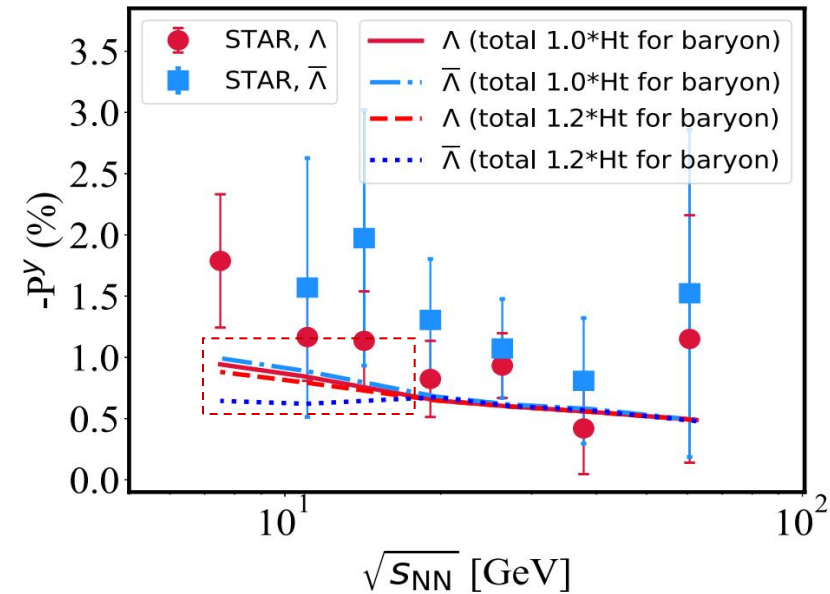
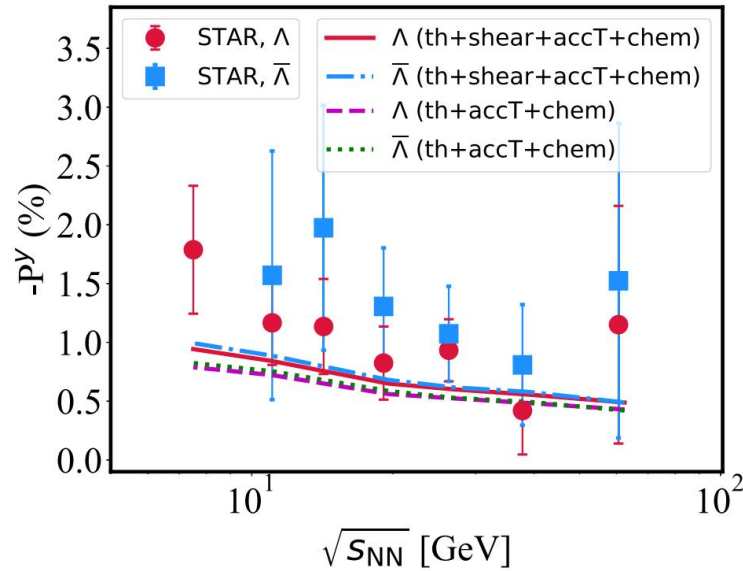
# Global polarization (different initial conditions)



- The tilted initial condition (CCNU) generates a **larger**  $-P^y$  than the SMASH and AMPT models in both transverse momentum and rapidity distribution
- All three initial conditions are capable of describing the STAR measurement data



# Global polarization



The modified optical Glauber model initial condition is able to reproduce the global polarization

- tilted fireball  $H_t$
- initial velocity field  $f_v$
- local baryon density distribution