Jets in hot nuclear matter (A unified picture of medium-induced radiation)

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VERSITÃT DELBERG

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Introduction to medium-induced emissions

arXiv:2206.02811





QCD in a background medium

[Zakharov, BDMPS]

QCD with color bkg: $\mathcal{A}(t, \mathbf{x}) + \mathcal{A}_0(t, \mathbf{x})$ 800 8000 8000 Multiple scatterings Medium Feynman rules: medium propagator: medium vertex:

> Medium average:

> > $\langle \mathcal{A}_0^-(t, \mathbf{x}) \mathcal{A}_0^-(t', \mathbf{x}') \rangle_{med}$

- weakly coupled, thermal plasma
- random fields
- "idk, evaluate later"

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QCD in a background medium

[Zakharov, BDMPS] [Blaizot, Dominiguez, Iancu, Mehtar-Tani]

QCD with color bkg: $\mathcal{A}(t, \pmb{x}) + \mathcal{A}_0(t, \pmb{x})$

• Multiple scatterings

Medium Feynman rules:

- medium propagator:
- medium vertex:



• Medium average:

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QCD in a background medium

[Zakharov, BDMPS]

200

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Multiple scatterings

Medium Feynman rules:

- medium propagator:
- medium vertex:



Medium average:

 $\langle \mathcal{A}_0^-(t, \mathbf{x}) \mathcal{A}_0^-(t', \mathbf{x}') \rangle_{med}$

- weakly coupled, thermal plasma Ο
- 0 random fields
- "idk, evaluate later" Ο

Medium-induced emission

LO radiation in vacuum:



Medium-induced emission

LO radiation:



$$\frac{dI}{d\omega d\vartheta} = \frac{dI^{vac}}{d\omega d\vartheta} + \frac{dI^{med}}{d\omega d\vartheta} = \text{complicated integral}$$
[Isaksen,Tywoniuk(2023)]

- $I^{med} > 0$: induced emissions
- I^{med} : no collinear divergence: ϑ is integrated

Approximate solutions:

- 1. analytic:
 - harmonic oscillator [BDMPSZ(1997)]
 - opacity expansion [GLV-Wiedemann(2000)]
 - improved opacity expansion [Mehtar-Tani(2020)]
- 2. numeric: [Feal,Vazquez(2018)] [Andres,Aploinario,Dominigues(2020)] [Schlichting,Soudi(2021)]

Medium-induced emission

LO radiation:



$$\frac{dI}{d\omega d\vartheta} = \frac{dI^{vac}}{d\omega d\vartheta} + \frac{dI^{med}}{d\omega d\vartheta} = \text{complicated integral}_{[\text{Isaksen,Tywoniuk(2023)}]}$$

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Leading physical picture of
$$\frac{dI^{med}}{d\omega} = \int d\vartheta \frac{dI^{med}}{d\omega d\vartheta}$$
:



Physical picture of
$$\frac{dI^{med}}{d\omega} = \int d\vartheta \frac{dI^{med}}{d\omega d\vartheta}$$
:





 ω_{BH}

ln L

 λ_{mfp}

34



Physical picture of $\frac{dI^{med}}{d\omega} = \int d\vartheta \frac{dI^{med}}{d\omega d\vartheta}$: multiple soft scatterings 2000 WBH. wçln L rare hard scatterings λ_{mfp} 34 000 lnω

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Testing the unified picture

Comparing to numerical solution:



Application of the unified picture $\underline{arXiv:2206.02811}$



Application: MIE cascade

Medium-induced fragmentation function:



 $D(x,t) = x \frac{dN}{dx}$

Application: MIE cascade





Application: MIE cascade





Summary

- Understanding jet modification in medium
- In this work:

• single induced emission $\frac{dI}{d\omega}$,

- \circ energy loss of a parton
- Outlook:
 - \circ event generator implementation
 - \circ energy loss of a whole jet
 - $\circ~$ understanding pQCD in the plasma to all orders

Thank you for the attention!



Expansion in scatterings:

Multiple soft scatterings:

$$\omega_c = \frac{L}{\lambda} \,\overline{\omega}_c$$

Expansion in real scatterings:

$$\omega_{BH} = \frac{\overline{\omega}_c}{L/\lambda}$$

$$\omega \frac{dI}{d\omega} = \begin{cases} \text{Opacity expansion , } L \ll \lambda \\ \bar{\alpha} \frac{L}{\lambda} \sum_{n=1}^{\infty} g_n \left(\frac{\omega}{\omega_{BH}}\right), \omega \ll \omega_{BH} \end{cases}$$





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 $\ln \omega$

non-physical

ln L

20

Expansion in scatterings:

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Multiple soft scatterings:

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Expansion in real scatterings:

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Single emission in vacuum

$$\int dz \int d\vartheta P^{LO}(z,\vartheta) = \mathcal{O}(\alpha_s L^2) + \mathcal{O}(\alpha_s L) + \mathcal{O}(\alpha_s)$$

logarithmic enhancement: soft & collinear emission

Power counting in vacuum



Single emission in medium

$$\int dz \int d\vartheta \ I^{LO_m}(z,\vartheta) = \mathcal{O}(\alpha_s P_m) + \mathcal{O}(\alpha_s L_m) + \mathcal{O}(\alpha_s)$$

power & logarithmic enhancement: soft emission & large medium

Power counting in medium

$$\Sigma_{m}(v) = \int dv' \frac{1}{\sigma_{0}} \frac{d\sigma_{m}}{dv'}$$

$$= 1 + \alpha_{s}(\Sigma_{12}P_{m} + \Sigma_{11}L_{m} + \Sigma_{10})$$

$$+ \alpha_{s}^{2}(\Sigma_{24}P_{m}^{2} + \Sigma_{23}P_{m}L_{m} + \Sigma_{22}L_{m}^{2} + \cdots)$$

$$+ \cdots$$

$$+ \alpha_{s}^{n}(\Sigma_{n,n}P_{m}^{n} + \Sigma_{n,n-1}P_{m}^{n-1}L_{m} + \cdots)$$

$$P_{m} \qquad NP_{m}$$

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 $\mathbf{\Sigma}$

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