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**Forward-backward correlations with the Σ
quantity in the wounded-constituent
framework at energies available at the
CERN Large Hadron Collider**

IWONA SPUTOWSKA



Institute of Nuclear Physics
Polish Academy of Sciences

Introduction: Why and how do we study correlations and fluctuations?



PRE-COLLISION

PRE-EQUILIBRIUM

QGP AND EQUILIBRIUM

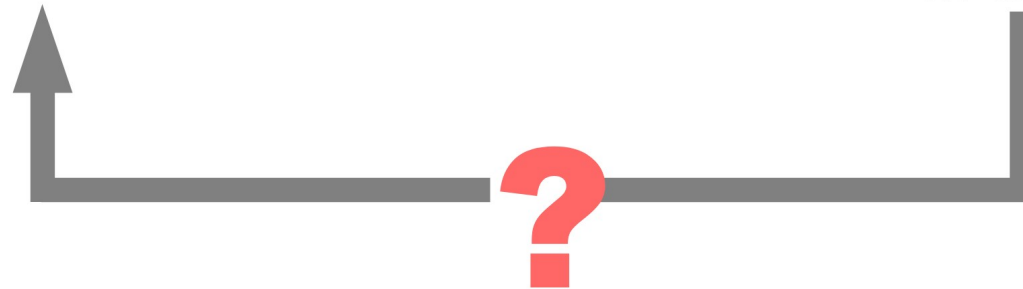
HADRONIZATION

HADRONIZATION FREEZE-OUT



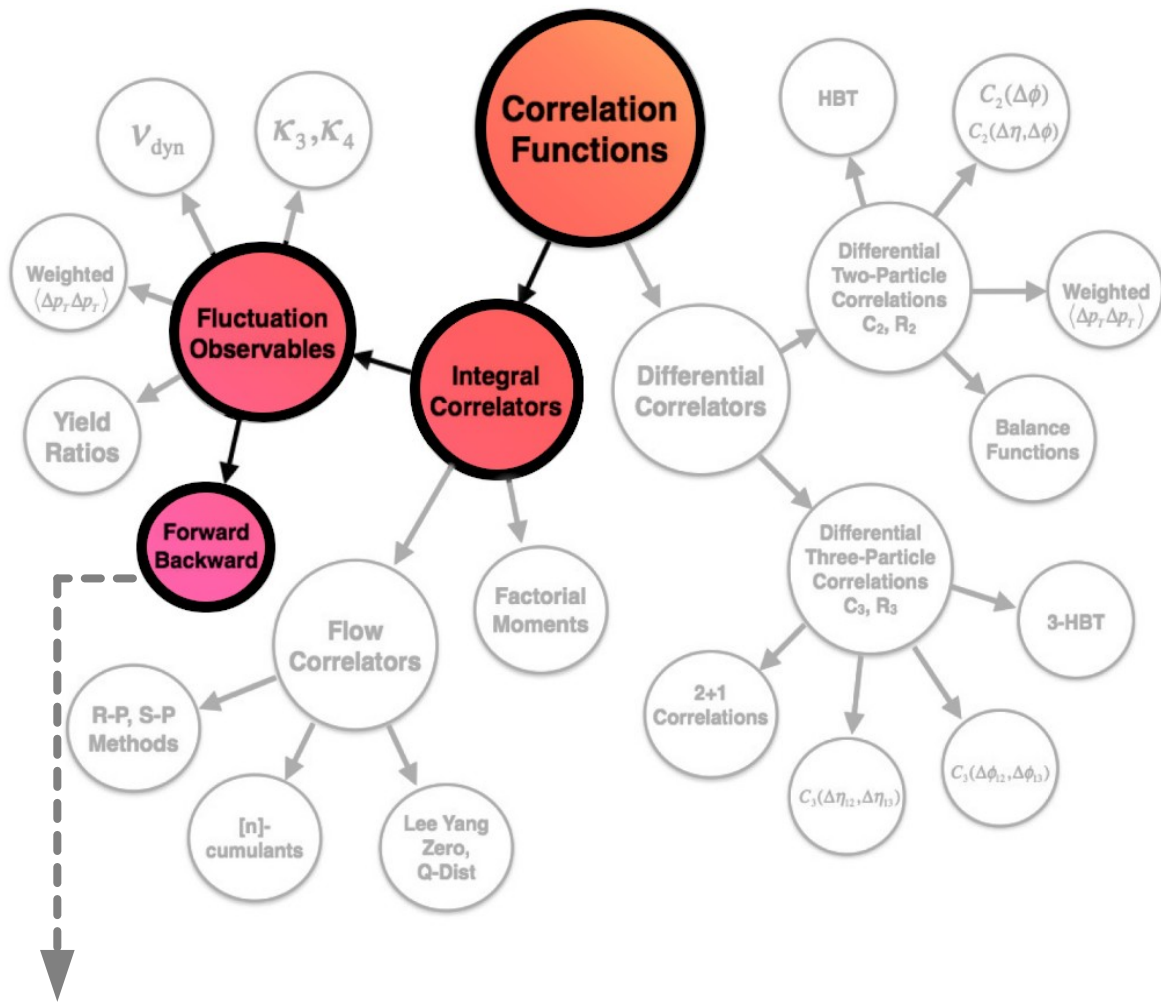
What we want to know...

What we measure
in the detector...



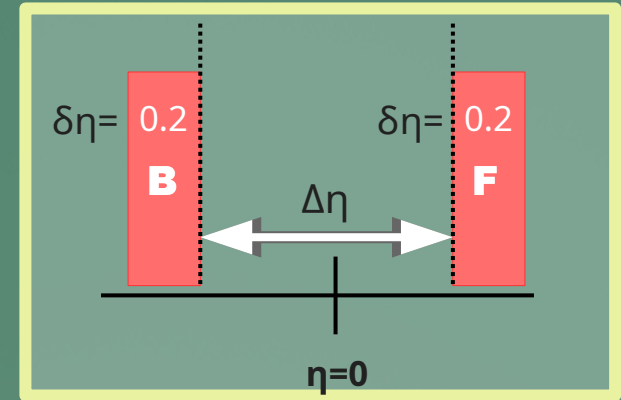
Analysis of correlations and fluctuations can provide information about **the early stages of heavy-ion collisions.**

Introduction: Why and how do we study correlations and fluctuations?



We are here!

The forward-backward (FB) correlation:



A popular technique:

The FB correlation coefficient

b_{corr} is:

$$b_{\text{corr}} = \frac{\text{Cov}(n_F, n_B)}{\sqrt{\text{Var}(n_F)\text{Var}(n_B)}}$$

- largely influenced by **geometrical (volume) fluctuations.**
- dependent on **centrality estimator.**



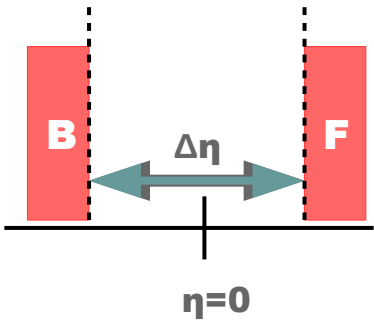
Introduction: FB correlations with strongly intensive quantity Σ



- **Strongly intensive quantities** do not depend on system volume nor system volume fluctuations.

Gaździcki, Gorenstein, Phys.Rev. C84 (2011) 014904

STRONGLY INTENSIVE QUANTITY Σ :



$$\Sigma = \frac{\langle n_F \rangle \omega_B + \langle n_B \rangle \omega_F - 2\text{Cov}(n_F, n_B)}{\langle n_F \rangle + \langle n_B \rangle},$$

where ω is scaled variance: $\omega = \text{Var}(n) / \langle n \rangle$

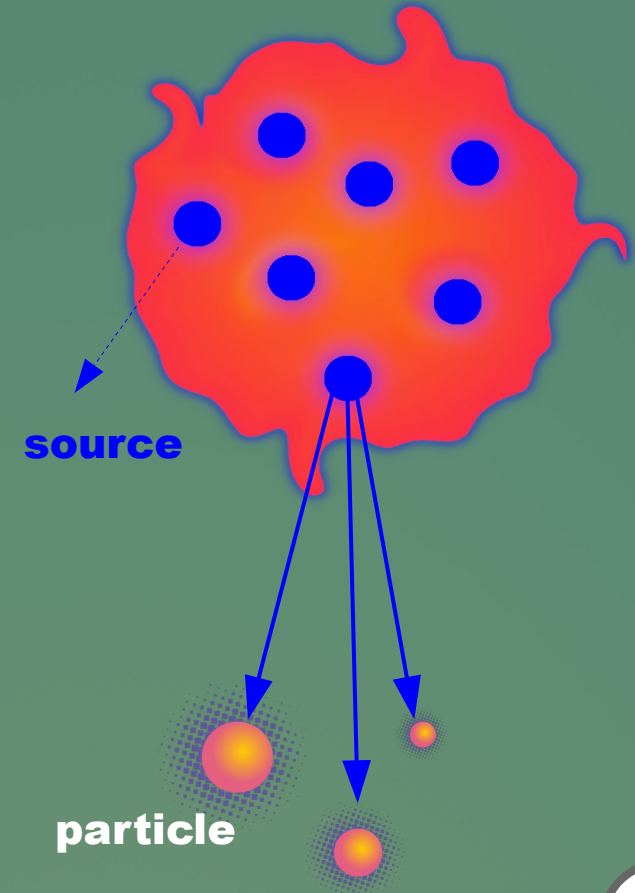
- For a symmetric collision $\omega_B = \omega_F$ and $\langle n_F \rangle = \langle n_B \rangle$,

$$\Sigma \approx \omega(1 - b_{\text{corr}}).$$

For Poisson distribution: $\omega=1$ & $b_{\text{corr}}=0 \rightarrow \Sigma=1$

Independent source model:

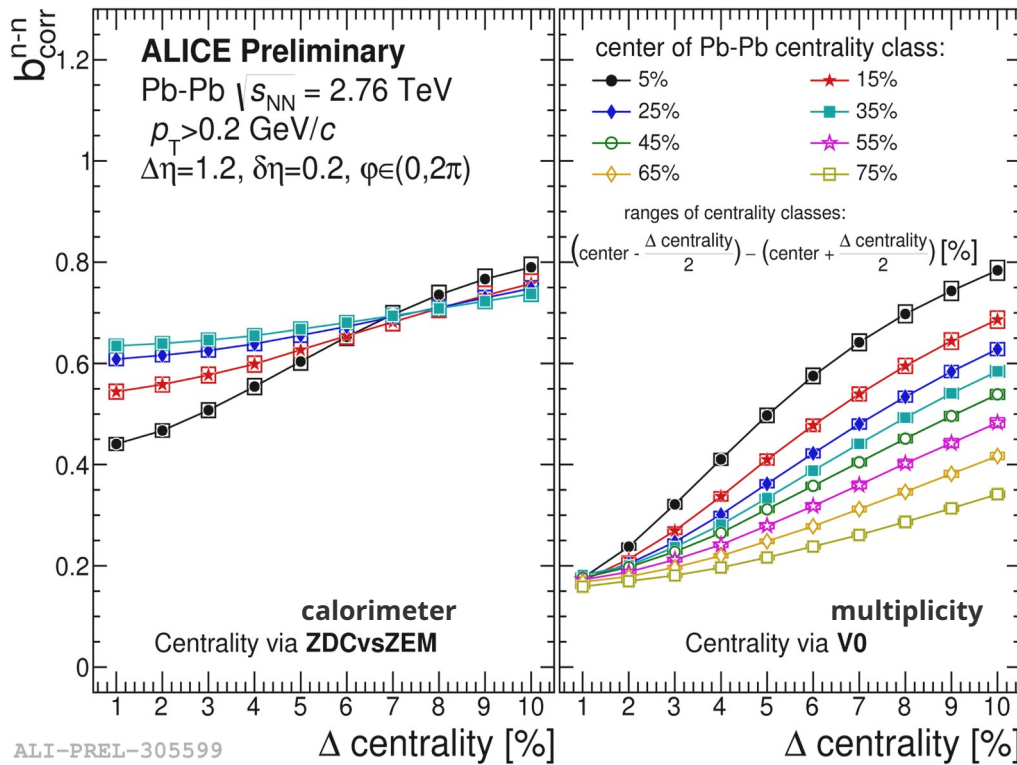
$\Sigma \rightarrow$ gives direct information about characteristics of **single source distribution!**



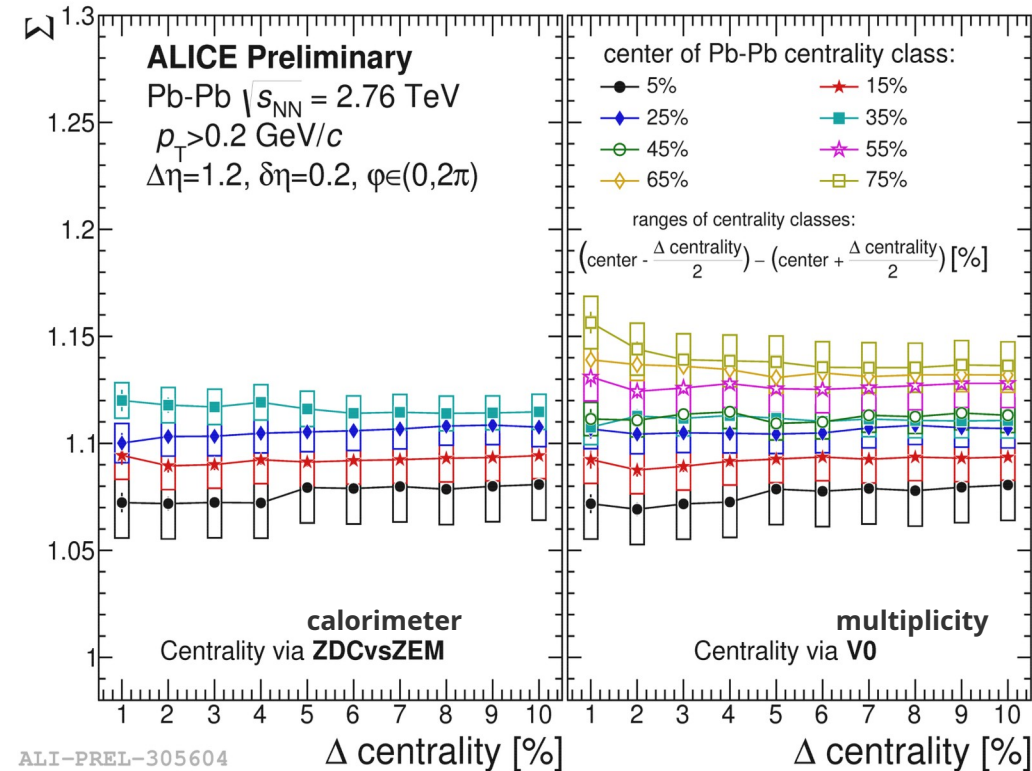
ALICE: Σ as a function of centrality bin width



The FB correlation coefficient b_{corr}^{n-n}



The Σ quantity

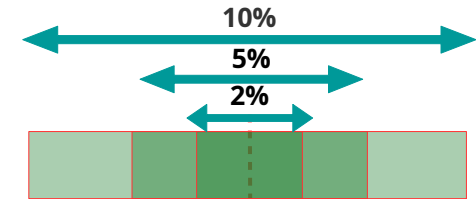


increase of volume fluctuations

- Σ does not depend on centrality bin width (volume fluctuations).
- Σ does not depend on centrality estimator!

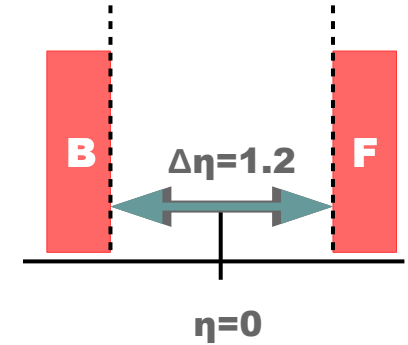
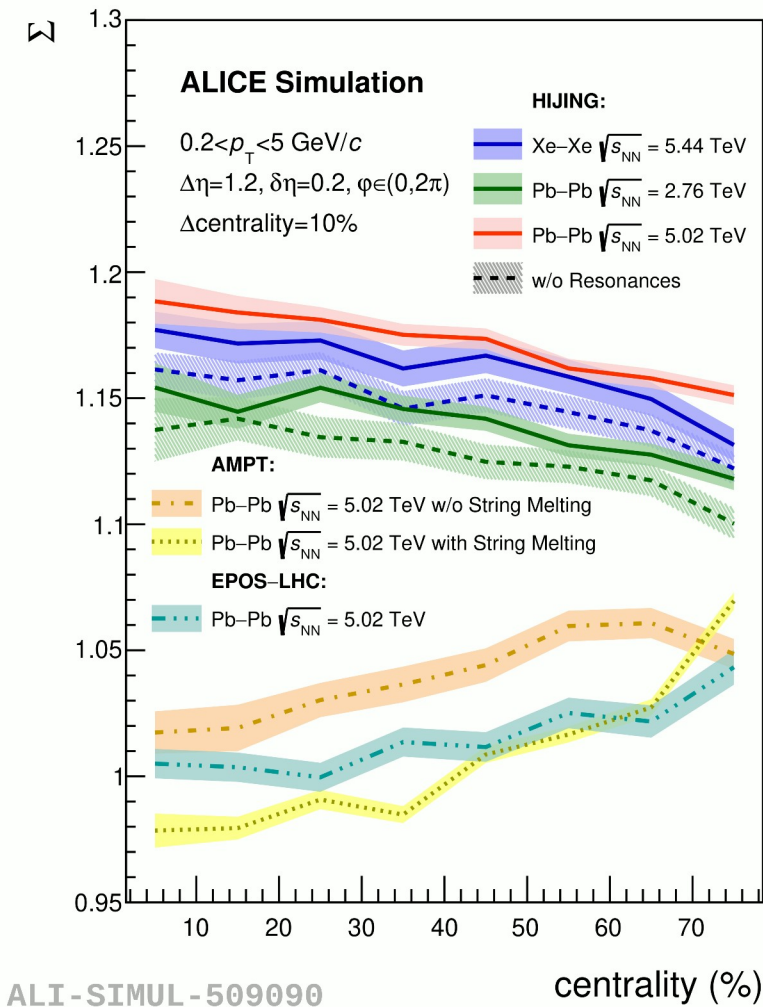
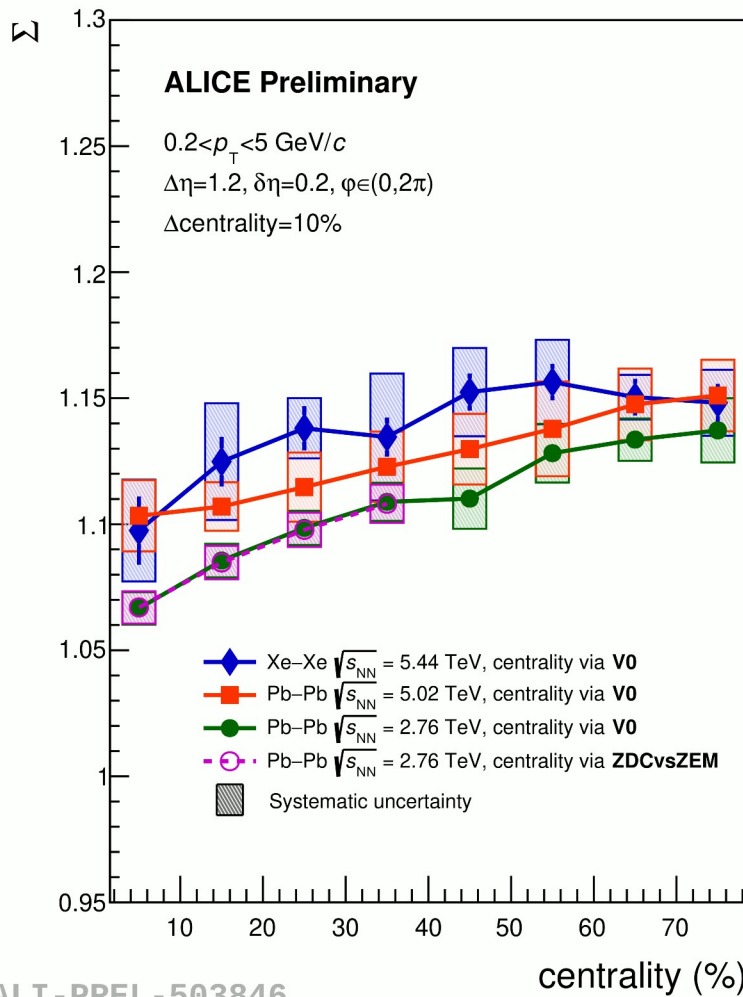
exhibits the properties of a strongly intensive quantity!

width of centrality class (Δ centrality):



center of centrality class

ALICE: Σ as a function of centrality



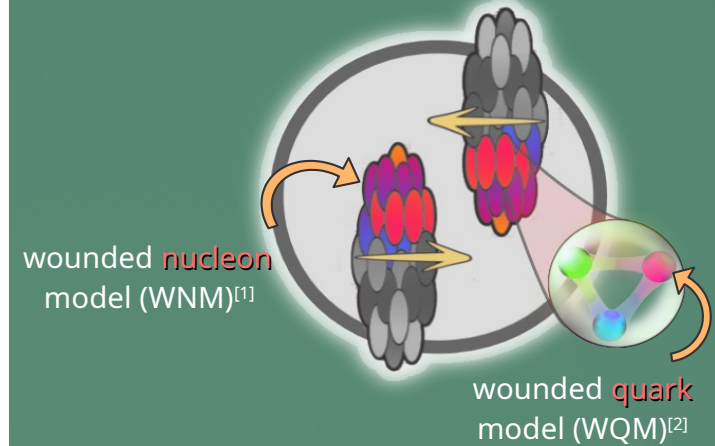
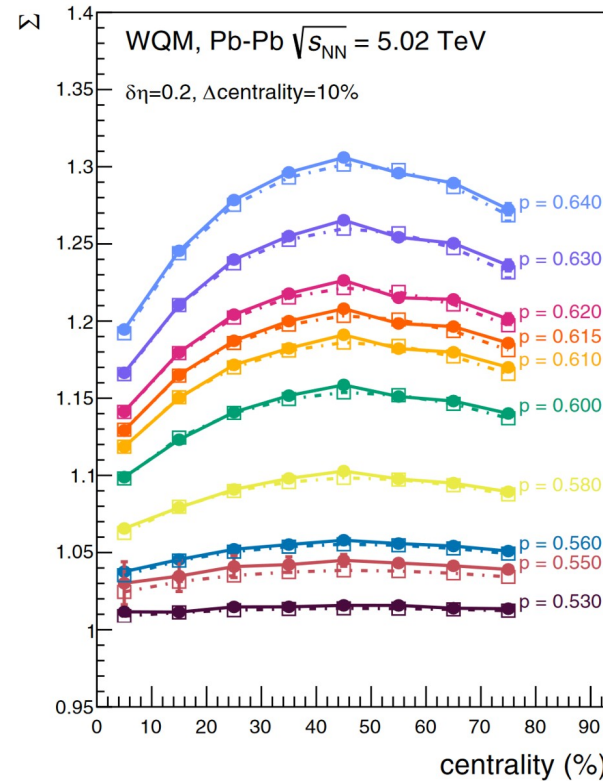
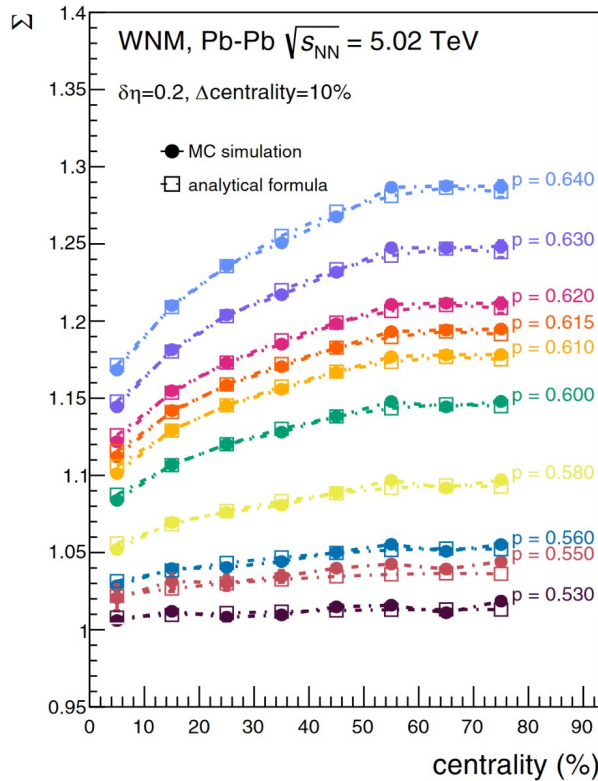
note!
 $V0 \approx ZDCvsZEM$
 → no dependence on centrality estimator!

- Values of Σ **increase with energy** and **increase with decreasing centrality** in experimental data, contrary behavior noted for MC HIJING results.
- MC AMPT and MC EPOS reproduce dependence on centrality **qualitatively** but **not quantitatively**.
- From results for MC AMPT it is evident that Σ is sensitive to the **mechanism** of particle production.

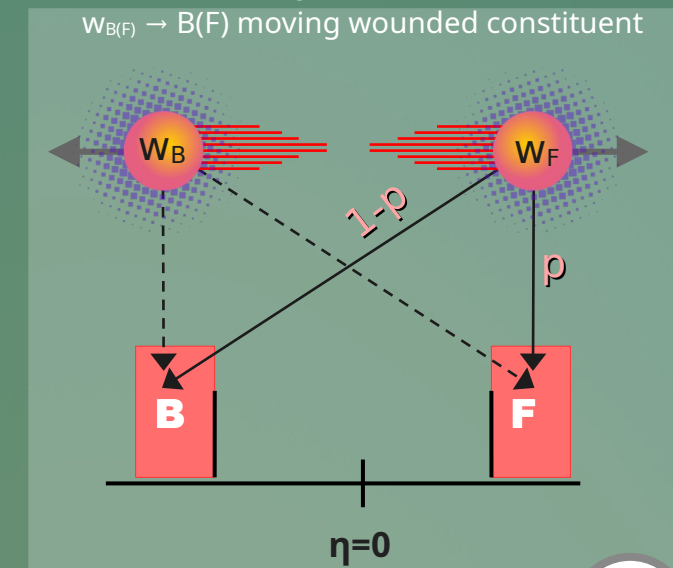
FB correlations with the Σ quantity in the wounded-constituent framework:



AA collision \rightarrow a superposition of constituent-constituent interactions



Two-component scenario^[3]:



Σ in WNM and WQM for a symmetric AA collision:

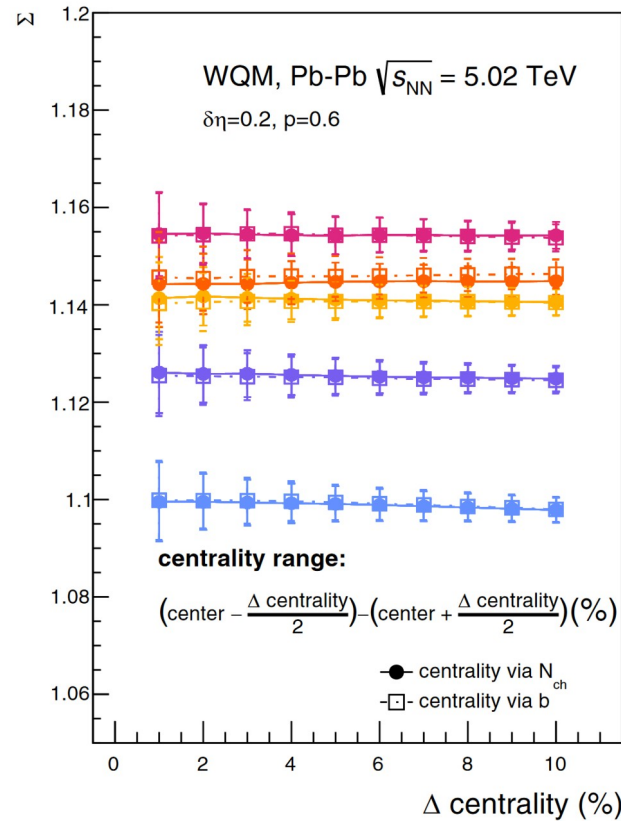
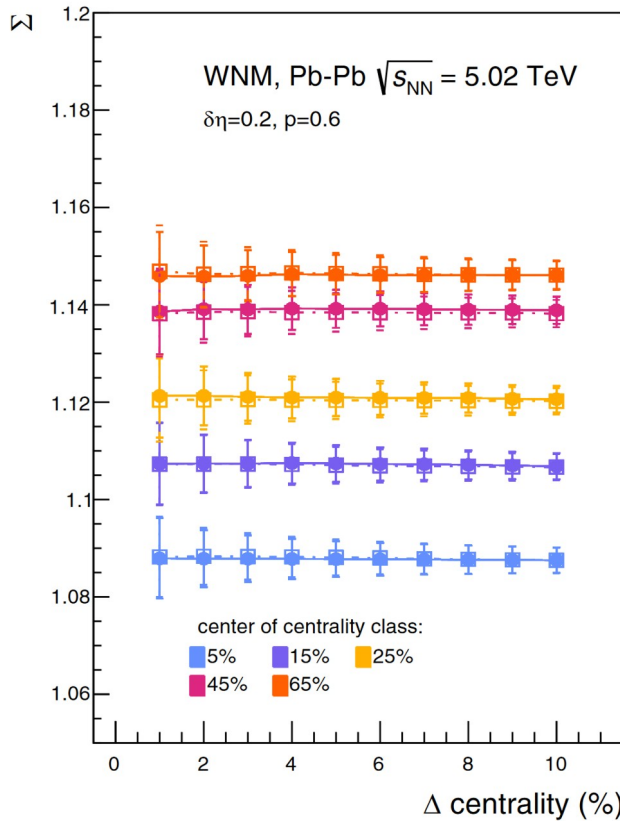
$$C = 2p - 1$$

$$\Sigma = 1 + \frac{\bar{n}}{2} C^2 \left[\frac{\langle (w_B - w_F)^2 \rangle}{2\langle w_F \rangle} + \frac{2}{k} \right]$$

- $p = 0.5 \iff C=0: \Sigma=1$ and Σ is SIQ;
- $p \neq 0.5 \iff C \neq 0: \Sigma > 1$ and shows intrinsic dependence on the number of w_F and $w_B \rightarrow$ **no longer** a strongly intensive quantity!

[1] A. Białas, M. Bleszyński and W. Czyż, Nucl. Phys. B 111, 461 (1976)
 [2] A. Białas, W. Czyż and W. Furmański, Acta Phys. Polon. B 8, 585 (1977)
 [3] Adam Bzdak, Phys. Rev. C 80, 024906

WN(Q)M: Σ quantity as a function of centrality bin width and centrality selection method



Σ in WNM and WQM:

$$\Sigma = 1 + \frac{\bar{n}}{2} C^2 \left[\frac{\langle (w_B - w_F)^2 \rangle}{2 \langle w_F \rangle} + \frac{2}{k} \right]$$

- $p \neq 0 \rightarrow C \neq 0$: intrinsic dependence on the number of w_F and $w_B \rightarrow$ no longer a strongly intensive quantity!

, but ...

- resemblance to the behavior reported by ALICE (slide 5)
- Σ **does not** depend on centrality bin width (volume fluctuations).
- Σ **does not** depend on centrality estimator!



This can be explained theoretically if one notes that Σ in WN(Q)M can be rewritten in terms of

partial covariance.

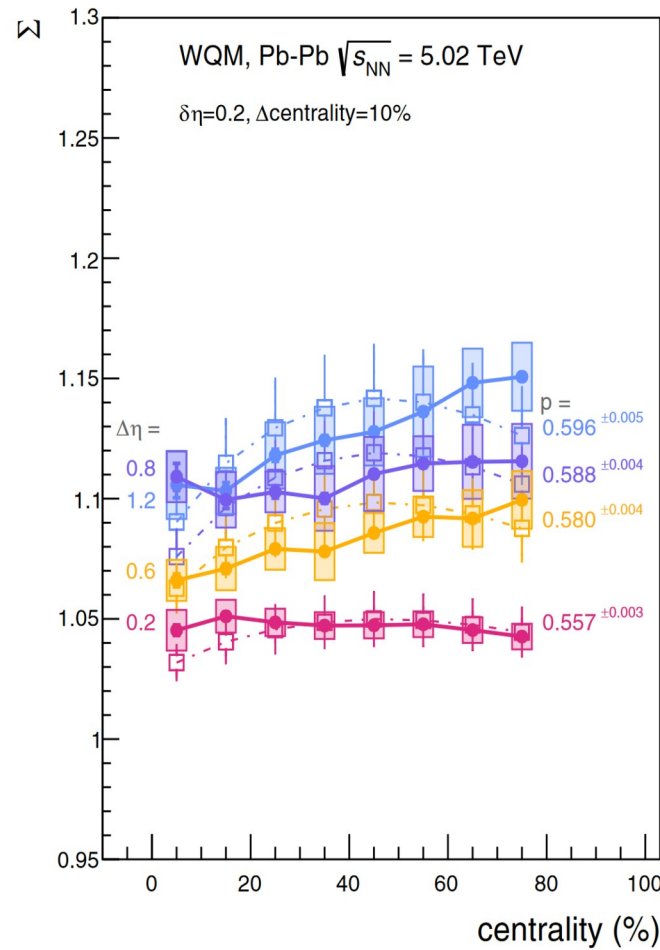
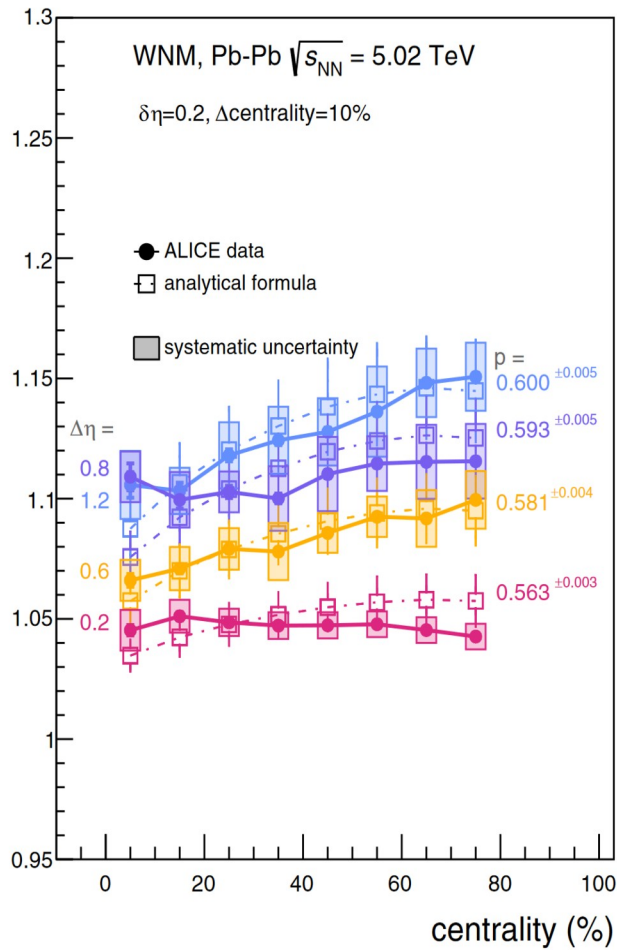
$$\Sigma = 1 + \frac{\bar{n}}{2} C^2 \left[\frac{-2 \text{Cov}(w_F, w_B \bullet w)}{\langle w_F \rangle} + \frac{2}{k} \right]$$

$$w = w_F + w_B$$

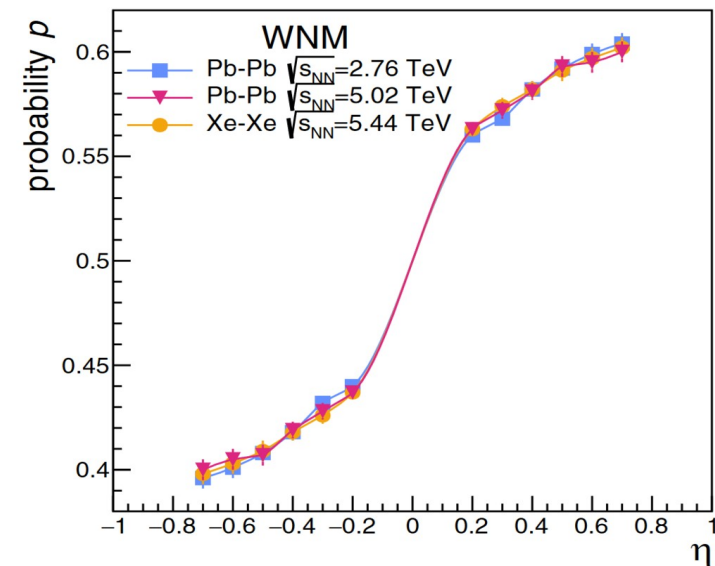
“strongly-intensive-quantity-like” properties!



WN(Q)M: Σ quantity as a function of centrality



- WNM and WQM → accurately depict the trend of Σ with centrality observed in the experimental data^[4](also for Pb-Pb at $\sqrt{s_{NN}}=2.76$ and Xe-Xe at $\sqrt{s_{NN}}=5.44$ TeV^[5]).
- Values of Σ in the WNM and WQM are sensitive to the probability value p .



- From comparison the data with WN(Q)M: **probability p changes as a function of pseudorapidity.**
- These probability values provide a new way to estimate the wounded nucleon (quark) **fragmentation function** in **symmetric** AA collisions!

Wounded constituent fragmentation functions in symmetric Pb—Pb collisions

The particle production for each wounded nucleon/quark → described by **universal fragmentation function $F(\eta)$** :

$$N(\eta) = \langle w_F \rangle F(\eta) + \langle w_B \rangle F(-\eta) \quad (\odot)$$

$F(\eta)$ DETERMINATION :

“STANDARD”
METHOD

→ based on measurement of $N(\eta) = dN_{ch}/d\eta$ distribution:

$$F(\eta) = \frac{1}{2} \left(\frac{N(\eta) + N(-\eta)}{\langle w_F \rangle + \langle w_B \rangle} + \frac{N(\eta) - N(-\eta)}{\langle w_F \rangle - \langle w_B \rangle} \right)$$

only for asymmetric collisions $\langle w_F \rangle \neq \langle w_B \rangle$.

NEW
APPROACH:

- It is based on the **relation between p and Σ** in WN(Q)M.
- It provides a unique opportunity to determine the $F(\eta)$ **in a symmetric nucleus-nucleus collision.**

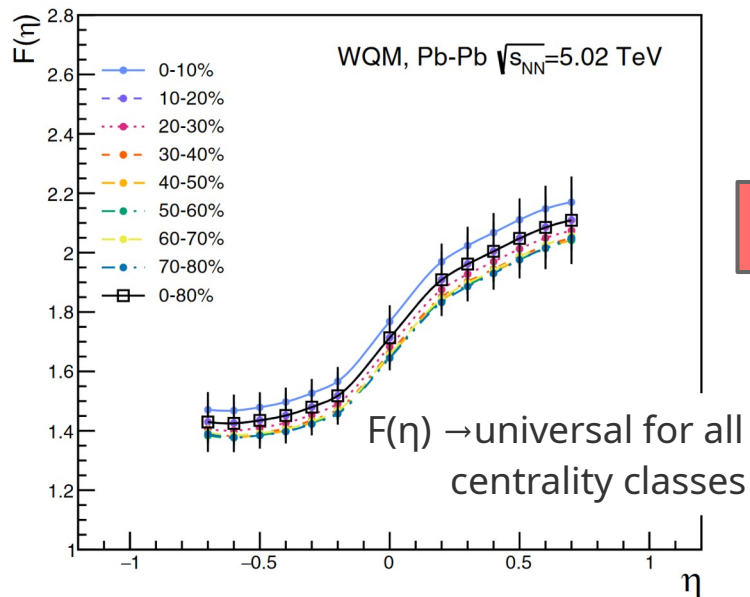
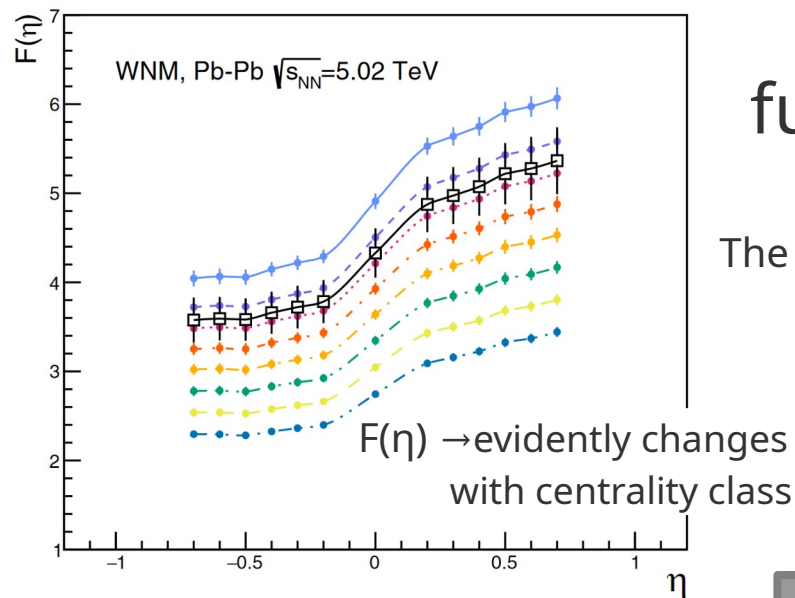
$$\text{Eq.}(\odot) \quad + \quad p = \frac{\int_{F(B)} F(\eta) d\eta}{\int_B F(\eta) d\eta + \int_F F(\eta) d\eta}$$

$$F(\eta) \approx \frac{p}{\langle w_F \rangle + \langle w_B \rangle} [N(-\eta) + N(\eta)]$$

based of measurement of Σ

from MC sim.

Pb-Pb
ALICE data^[6]



Summary

In this study I investigated the properties of Σ quantity at LHC energies using the wounded nucleon and wounded quark models:

- (1) Two-component scenario of forward- and backward-moving constituents → **collapses the strongly intensive properties** of Σ !
- (2) Even though in the WNM and WQM Σ is no longer a strongly intensive quantity, it **retains some of its properties** in symmetric AA collisions → due to its relation to partial covariance.
- (3) Σ results determined in WNM and WQM are in **good agreement with the ALICE data**. The models outperform more complex ones such as HIJING, AMPT, or EPOS, which struggle to describe Σ properly.
- (4) Σ is sensitive to probability p of particle emission in η interval by a wounded source. This relation allows the **direct determination of the fragmentation function** of a wounded nucleon or quark in a symmetric nucleus-nucleus collision, which has not been possible so far!

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Σ dependence on centrality selection and volume fluctuations

I. Sputowska (ALICE), MDPI Proc. 10, 14 (2019)

Σ in AA and pp collisions

I. Sputowska (ALICE), EPJ Web Conf. 274, 05003 (2022).

Strongly Intensive Quantities

M. I. Gorenstein and M. Gazdzicki, Phys. Rev. C 84, 014904 (2011), arXiv:1101.4865 [nucl-th.

Σ in WNM and WQM

I. Sputowska, Phys.Rev.C 108 (2023) 1, 014903

