

# INVESTIGATION OF THE TWO- PARTICLE SOURCE FUNCTION AT $\sqrt{s_{NN}} = 2.76$ TEV WITH EPOS

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[arXiv:2212.02980](https://arxiv.org/abs/2212.02980)

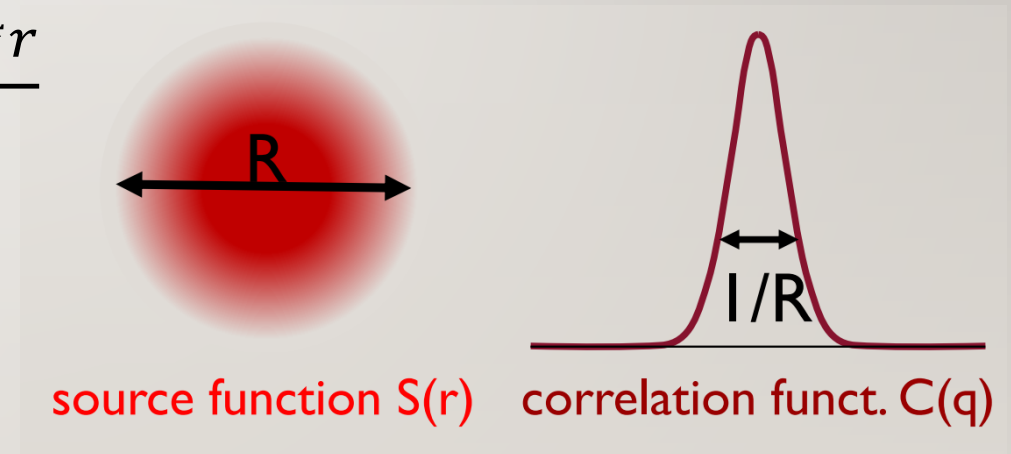


## 2 / III FEMTOSCOPY – THE TWO-PARTICLE SOURCE

- Two-particle (pair) source:  $D(r, K) = \int S\left(\rho + \frac{r}{2}, K\right) S\left(\rho - \frac{r}{2}, K\right) d^4\rho$ 

relative coordinate  $\leftarrow$  average momentum  $\uparrow$  single-particle  $\uparrow$  phase-space density  $\uparrow$
- Correlation function:  $C(q, K) = \frac{\int D(r, K) |\Psi_q(r)|^2 d^4r}{\int D(r, K) d^4r}$ 

relative momentum  $\uparrow$  pair wave function  $\uparrow$
- Experiments – no direct access to pair-source
  - Assume given source shape and wave function
  - Calculate the correlation function
  - Test the assumptions on the measured correlation
- Event generator models (like EPOS) – direct access to pair-source!

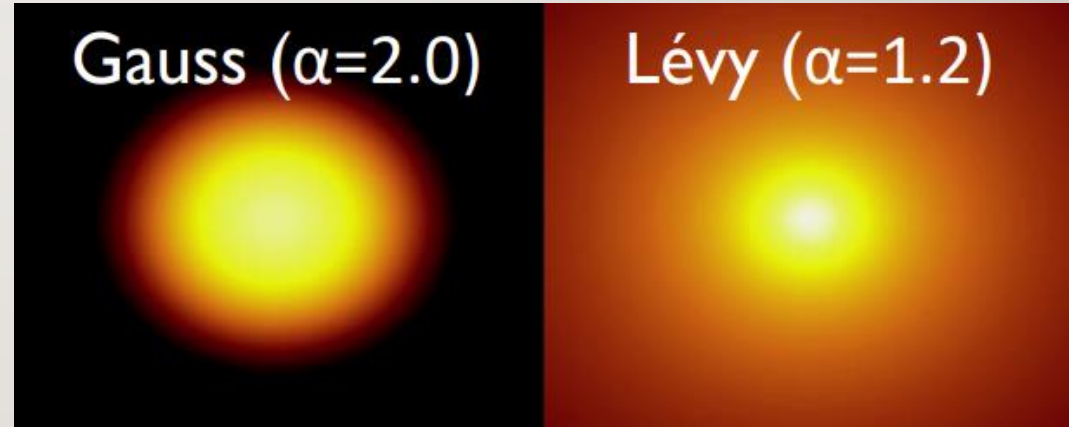


# 3 / 11 LÉVY DISTRIBUTIONS IN HEAVY ION PHYSICS

- Measurements suggest phenomena beyond Gaussian distribution

- Lévy-stable distribution:  $L(\mathbf{r}; \alpha, R) = (2\pi)^{-3} \int d^3\mathbf{q} e^{i\mathbf{q}\mathbf{r}} e^{-\frac{1}{2}|\mathbf{q}R|^\alpha}$

- $\alpha$ : Lévy stability index
  - Gaussian distribution:  $\alpha = 2$
  - Cauchy distribution  $\alpha = 1$
- $R$ : Lévy scale parameter



- Some possible causes:

- **Event averaging** (Cimerman et al., *Phys.Part.Nucl.* 51 (2020) 282)
- **Resonance decays** (Csanád, Csörgő, Nagy, *Braz.J.Phys.* 37 (2007) 1002; Kincses, Stefaniak, Csanád, *Entropy* 24 (2022) 308)
- **Hadronic rescattering, anomalous diffusion** (*Braz.J.Phys.* 37 (2007) 1002; *Entropy* 24 (2022) 308)

# 4 / III THE EPOS MODEL

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- EPOS = **E**nergy conserving quantum mechanical multiple scattering approach, based on **P**artons (parton ladders), **O**ff-shell remnants, and **S**aturation of parton ladders *K. Werner et al., PRC82 (2010) 044904, PRC89 (2014) 064903*
- Monte-Carlo based phenomenological model
- Stages of the evolution:
  - Initial stage – parton based Gribov-Regge theory
  - Core-corona separation
  - 3+1D viscous hydrodynamic evolution
  - Hadronic rescattering – UrQMD
- Dataset: EPOS3 2.76 TeV PbPb, 800k events



# RECONSTRUCTING THE TWO-PARTICLE SOURCE

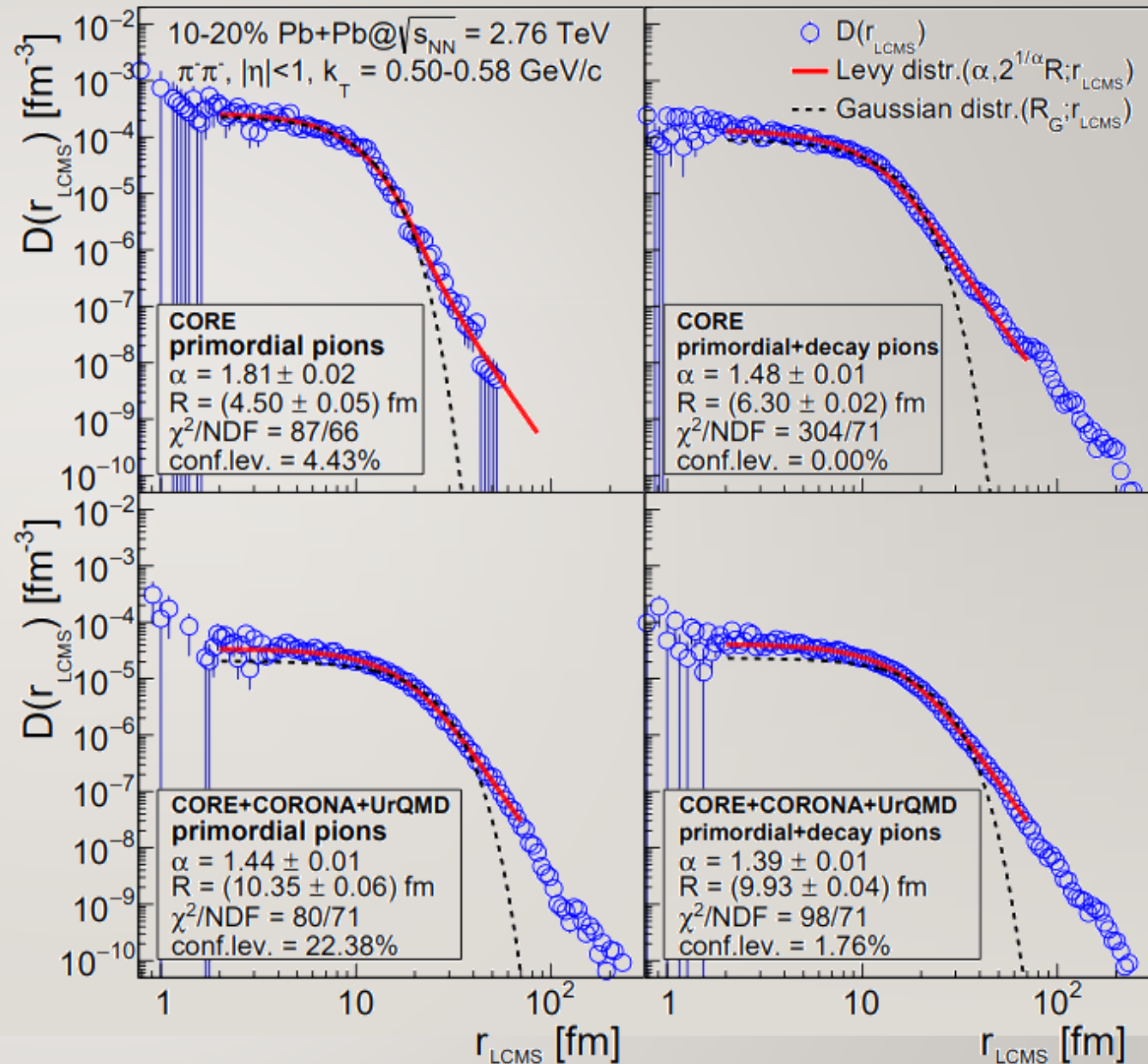
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- Source spherically symmetric in the LCMS (*PHENIX coll., Phys. Rev. Lett. 93 (2004), 152302*)
- $\mathbf{r}_{LCMS} = \left( x_1 - x_2, y_1 - y_2, \frac{z_1 - z_2 - \beta(t_1 - t_2)}{\sqrt{1 - \beta^2}} \right), \beta = \frac{p_{z,1} + p_{z,2}}{E_1 + E_2}$
- Calculate  $D(r_{LCMS})$  event-by-event!
- Average transverse momentum ( $k_T$ ) classes
- Investigated cases:
  - Pions:
    - CORE, primordial
    - CORE, primordial+decay
    - CORE+CORONA+UrQMD, primordial
    - CORE+CORONA+UrQMD, primordial+decay
  - Kaons: CORE+CORONA+UrQMD, primordial+decay
  - Protons: CORE+CORONA+UrQMD, primordial+decay

# LÉVY FITS TO THE TWO-PARTICLE SOURCE

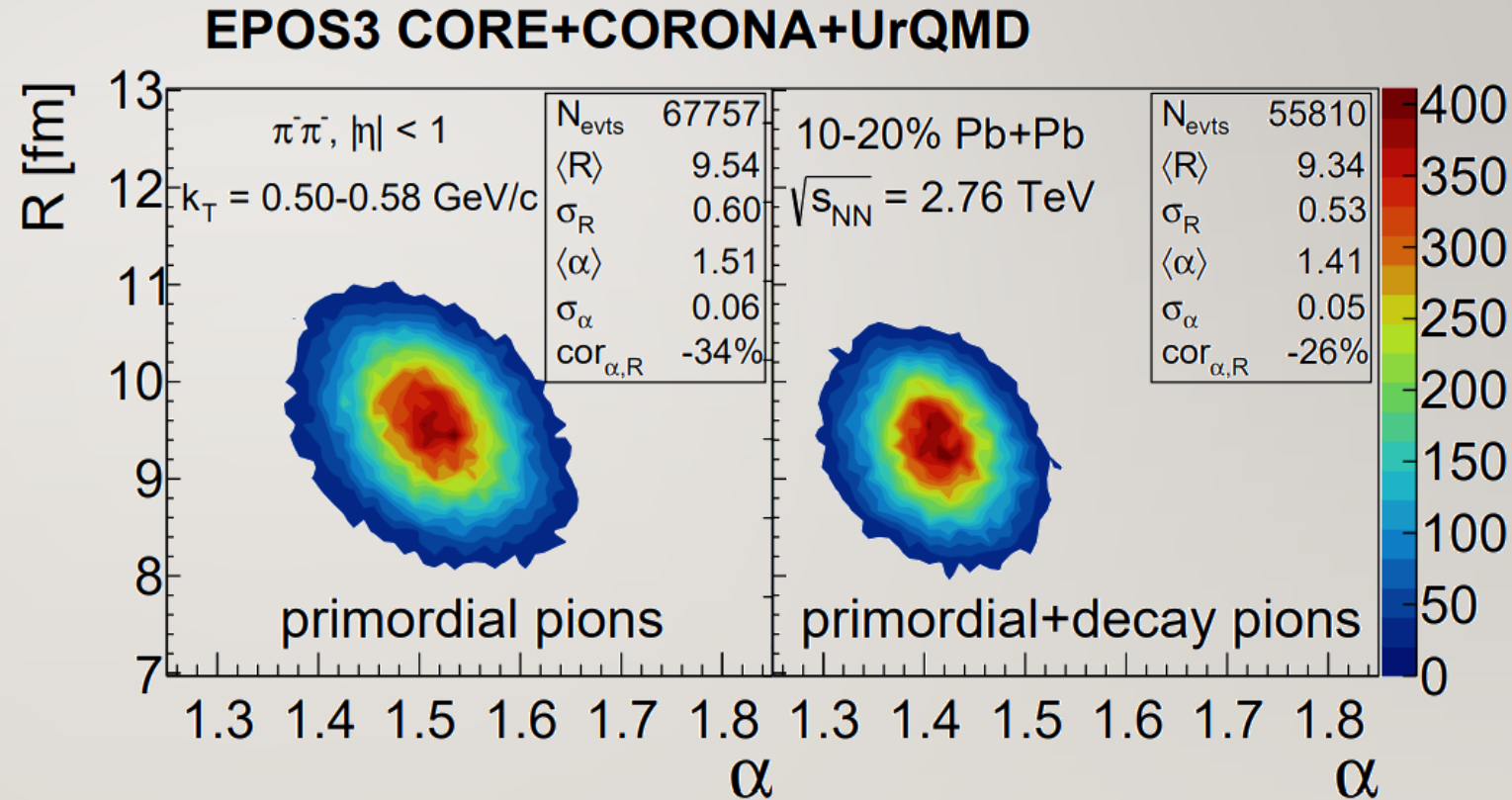
- Event-by-event Lévy fits
- Without decays and UrQMD  $\rightarrow$  close to Gaussian
- After decays or UrQMD  $\rightarrow$  far from Gaussian
- Lévy shape appears in single events!
- Similar fits for kaons and protons
- Only keep fits with  $CL > 0.1\%$

## EPOS3 single event



# 7/11 DISTRIBUTION OF THE SOURCE PARAMETERS

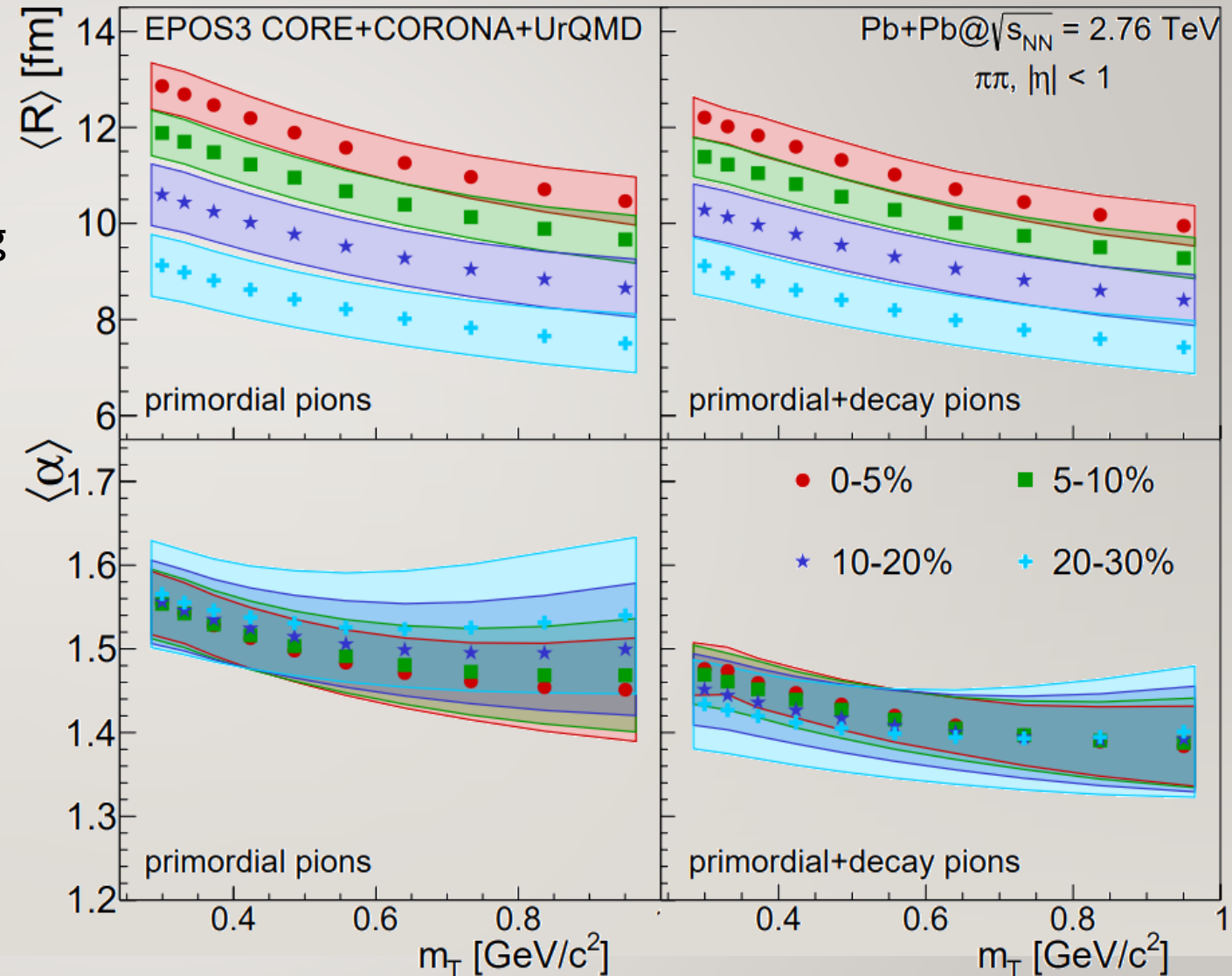
- Collect all fit results in  $R$  vs  $\alpha$  histograms
- Similar figures for each centrality,  $k_T$  and for kaons or protons
- Extract average values  $\langle R \rangle$  and  $\langle \alpha \rangle$
- Extract standard deviations
- Investigate centrality and  $k_T$  dependence





# 8/11 PION SOURCE PARAMETERS

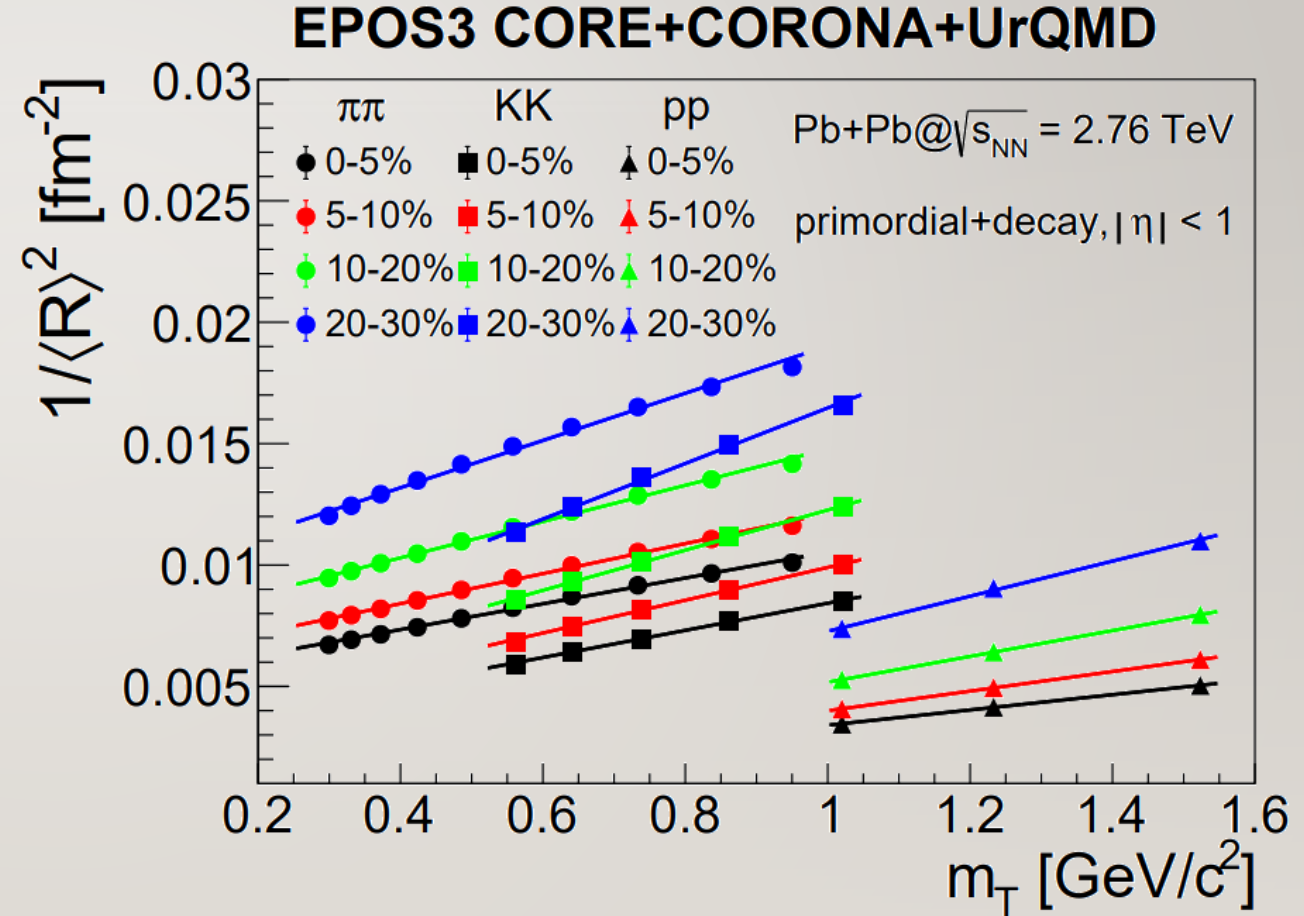
- Lévy scale parameter ( $R$ ):
  - Larger in central collisions  $\rightarrow$  spatial scale
  - Decreases with  $m_T \rightarrow$  hydrodynamic scaling
  - Small effect of decay products
- Lévy stability index ( $\alpha$ ):
  - Weak centrality dependence
  - Small decrease with  $m_T$
  - Smaller after decays  $\rightarrow$  source shape influenced
- Similar trends to experimental results
- Magnitudes of the parameters different





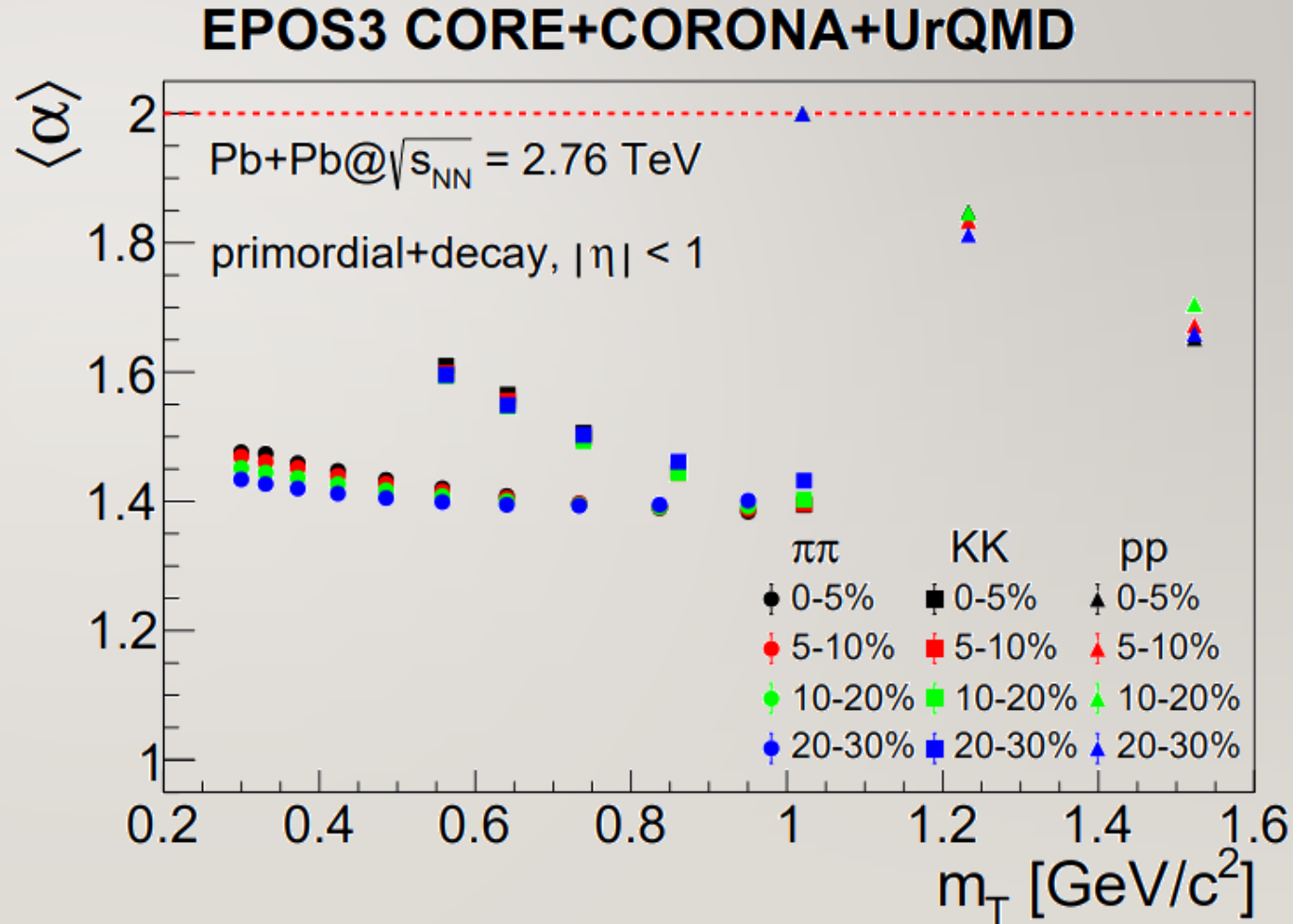
# 9/11 PION, KAON, PROTON LÉVY SCALE PARAMETER

- Similar trends
- Hydrodynamics + Gaussian source  $\rightarrow$   
 $\frac{1}{R^2} \sim m_T$  particle independent scaling
- EPOS  $\rightarrow R$  depends on the particle type
- No universal  $m_T$  scaling in EPOS
- For given species scaling is fulfilled
- Stat. uncertainties smaller than markers



# 10/11 PION, KAON, PROTON LÉVY STABILITY INDEX

- Source deviation from Gaussian ( $\alpha = 2$ )
- In case of anomalous diffusion:
  - Smaller cross-section  $\rightarrow$  larger mean free path  $\rightarrow$  longer power-law tail  $\rightarrow$  smaller  $\alpha$
- Prediction:  $\alpha_K < \alpha_\pi < \alpha_p$
- Only partially fulfilled!
- Anomalous diffusion cannot be the only reason for the Lévy shape



# SUMMARY

## • Analysis steps:

- Event-by-event reconstruction of the two-particle source in EPOS 2.76 TeV PbPb
- Single event Lévy fits – event-by-event Lévy shape
- Extract mean Lévy parameters  $\langle R \rangle$  and  $\langle \alpha \rangle$

## • Results:

- Hydrodynamic and geometric scaling of  $\langle R \rangle$
- $\langle \alpha \rangle$  affected by decays
- Similar trends to experiment, but different magnitudes
- Particle species dependent  $\langle R \rangle$
- Partially fulfilled predictions of anomalous diffusion
- Preprint: [arXiv:2212.02980](https://arxiv.org/abs/2212.02980) (submitted to PLB)

} pions

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**THANK YOU FOR  
YOUR ATTENTION!**

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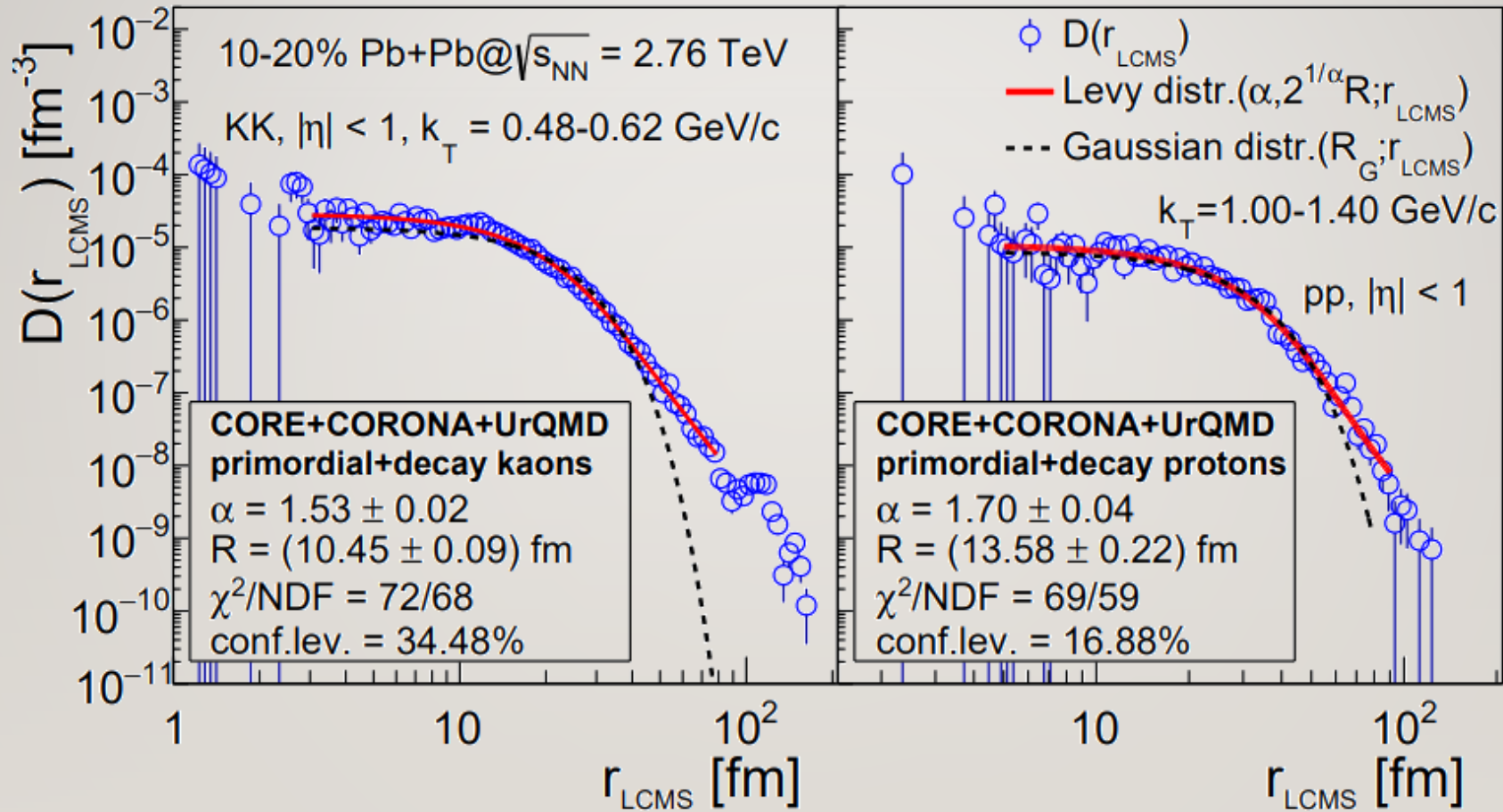
# BACKUP SLIDES

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# 14 KAON AND PROTON EXAMPLE FIT

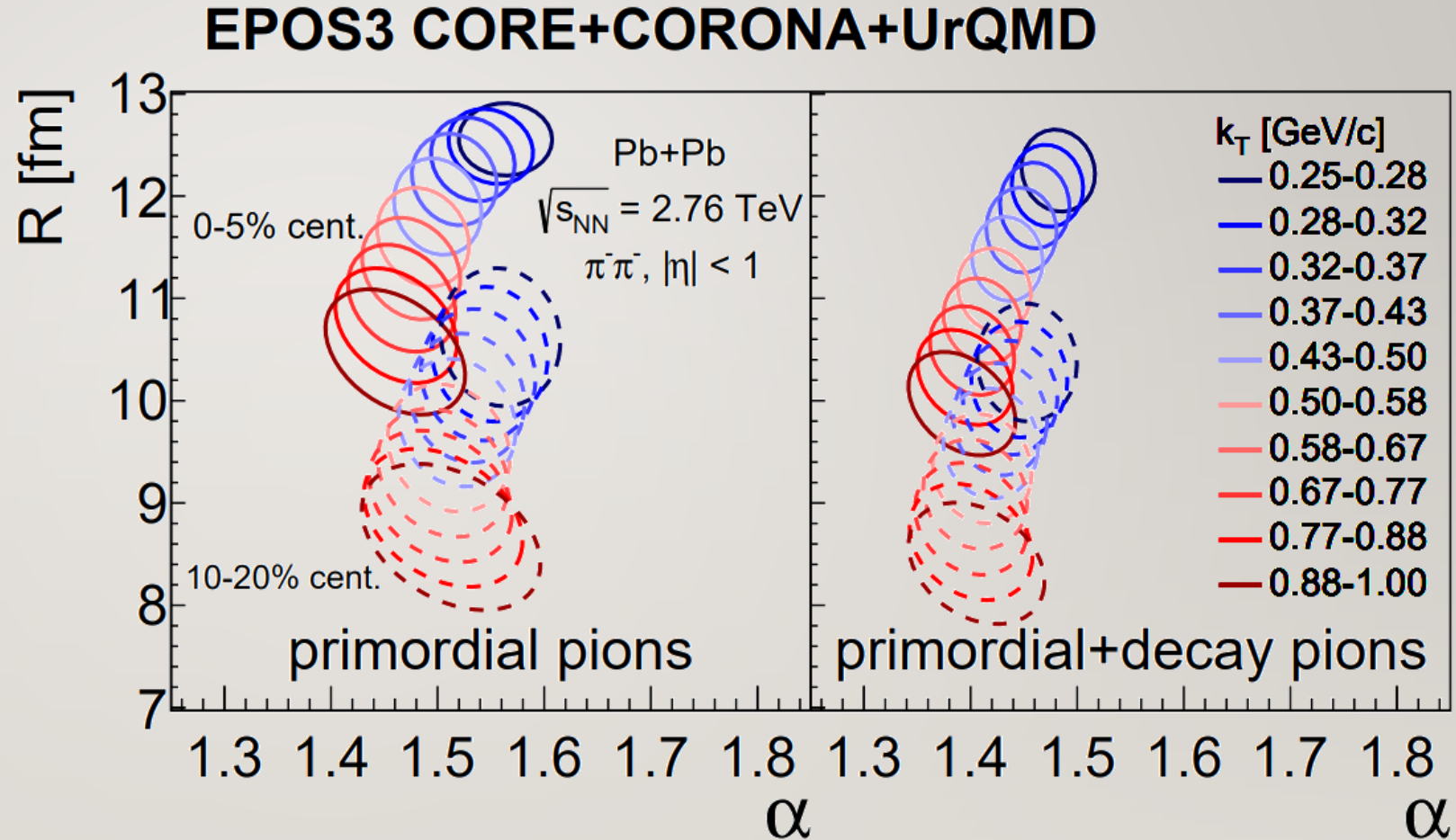
## EPOS3 single event





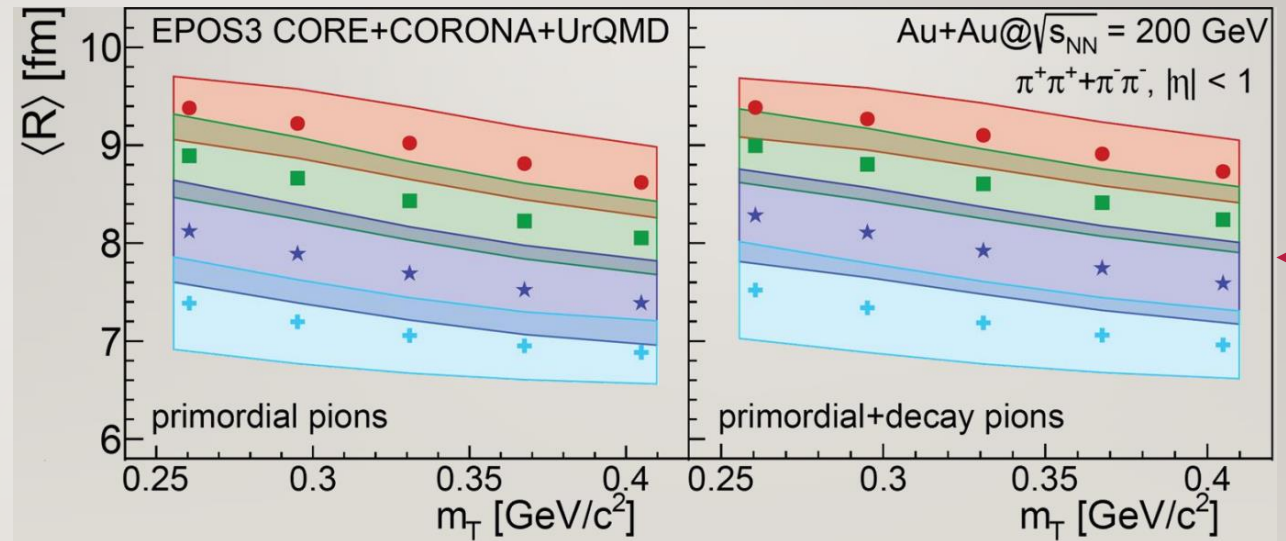
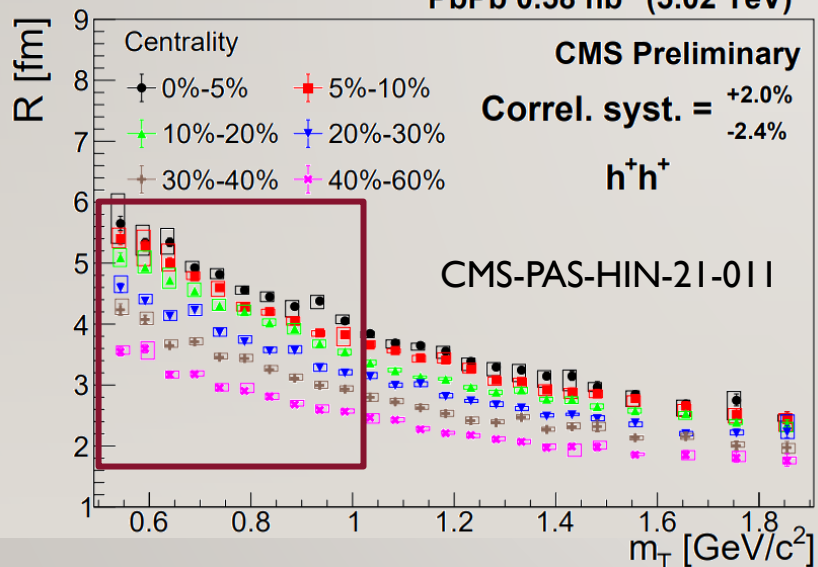
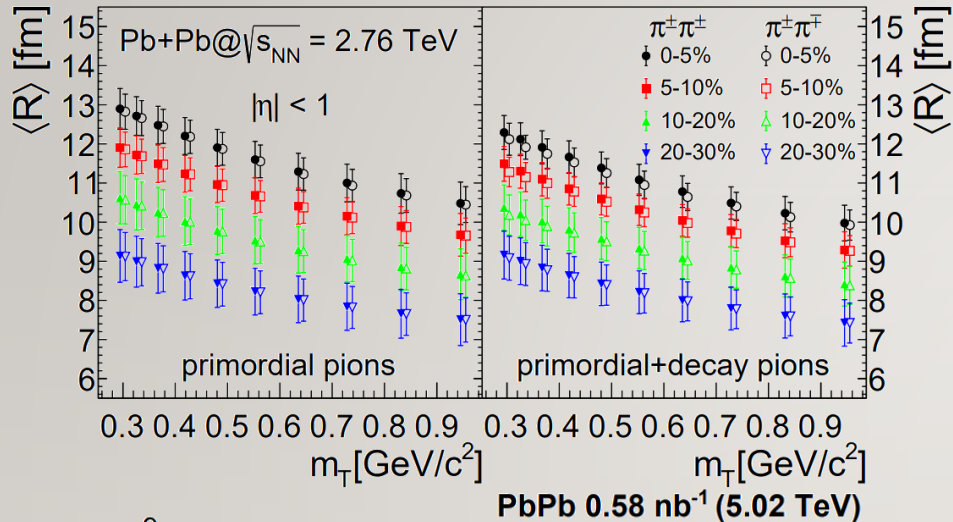
# 15 CONTOURS OF THE $R$ VS $\alpha$ DISTRIBUTIONS

- $1\sigma$  contours for all  $k_T$  classes
  - Ellipses from  $\sigma_\alpha$ ,  $\sigma_R$  and  $cor_{\alpha,R}$
  - Only 2 centralities in one figure for clarity
- $\alpha - R$  anti-correlation
- Illustrates centrality and  $k_T$  dependence



# 16 COMPARISON TO DATA AND LOWER ENERGY EPOS

## EPOS3 CORE+CORONA+UrQMD

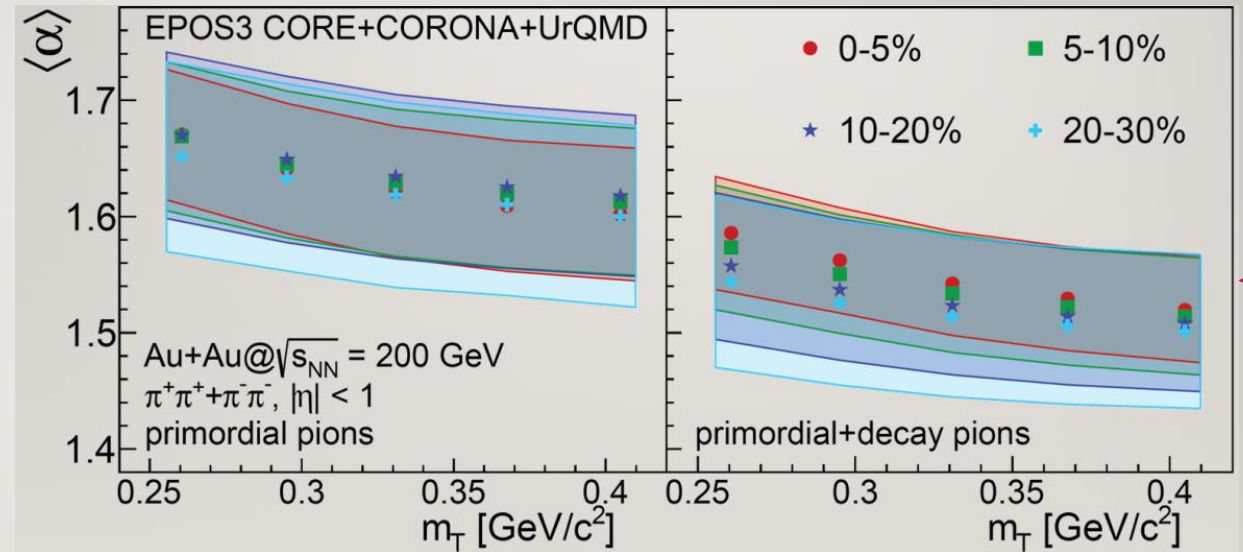
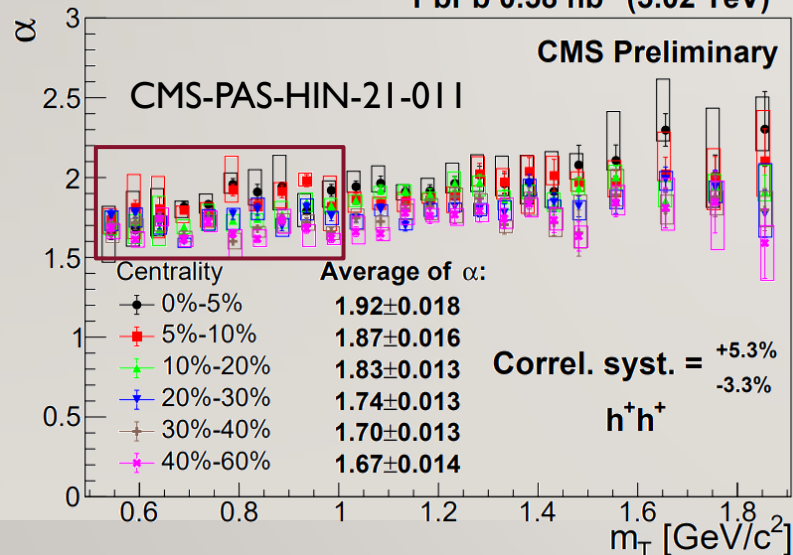
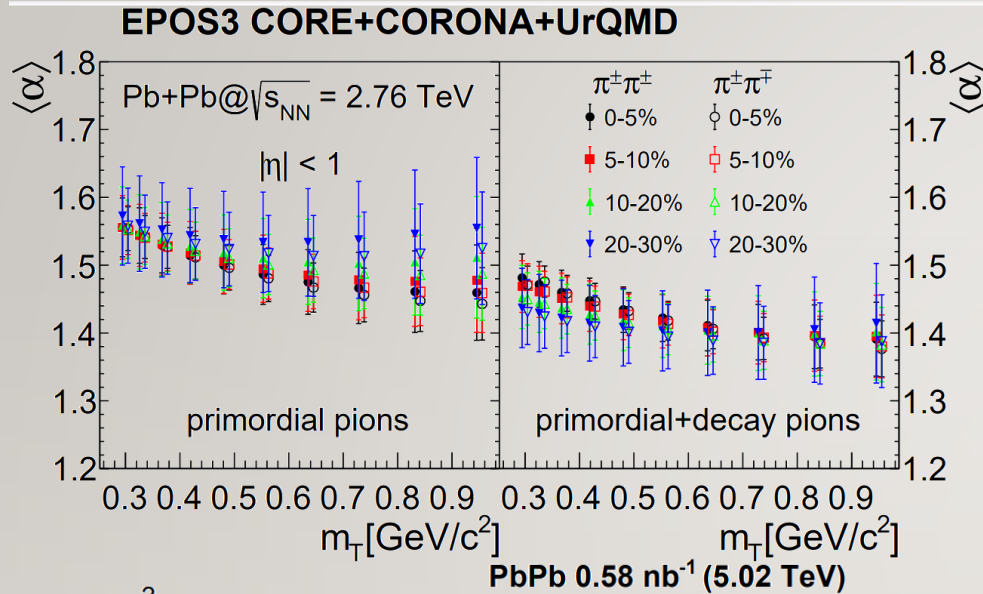


Kincses, Stefaniak, Csanád, *Entropy* 24 (2022) 308

- Similar centrality and  $m_T$  dependence
- $\langle R \rangle(2.76 \text{ TeV EPOS}) > \langle R \rangle(200 \text{ GeV EPOS})$
- $\langle R \rangle(2.76 \text{ TeV EPOS}) > R(5.02 \text{ TeV data})$  ?



# 17 COMPARISON TO DATA AND LOWER ENERGY EPOS



Kincses, Stefaniak, Csanád, *Entropy* 24 (2022) 308

- Similar centrality and  $m_T$  dependence
- $\langle \alpha \rangle(2.76 \text{ TeV EPOS}) < \langle \alpha \rangle(200 \text{ GeV EPOS})$
- $\langle \alpha \rangle(2.76 \text{ TeV EPOS}) < \alpha(5.02 \text{ TeV data})$

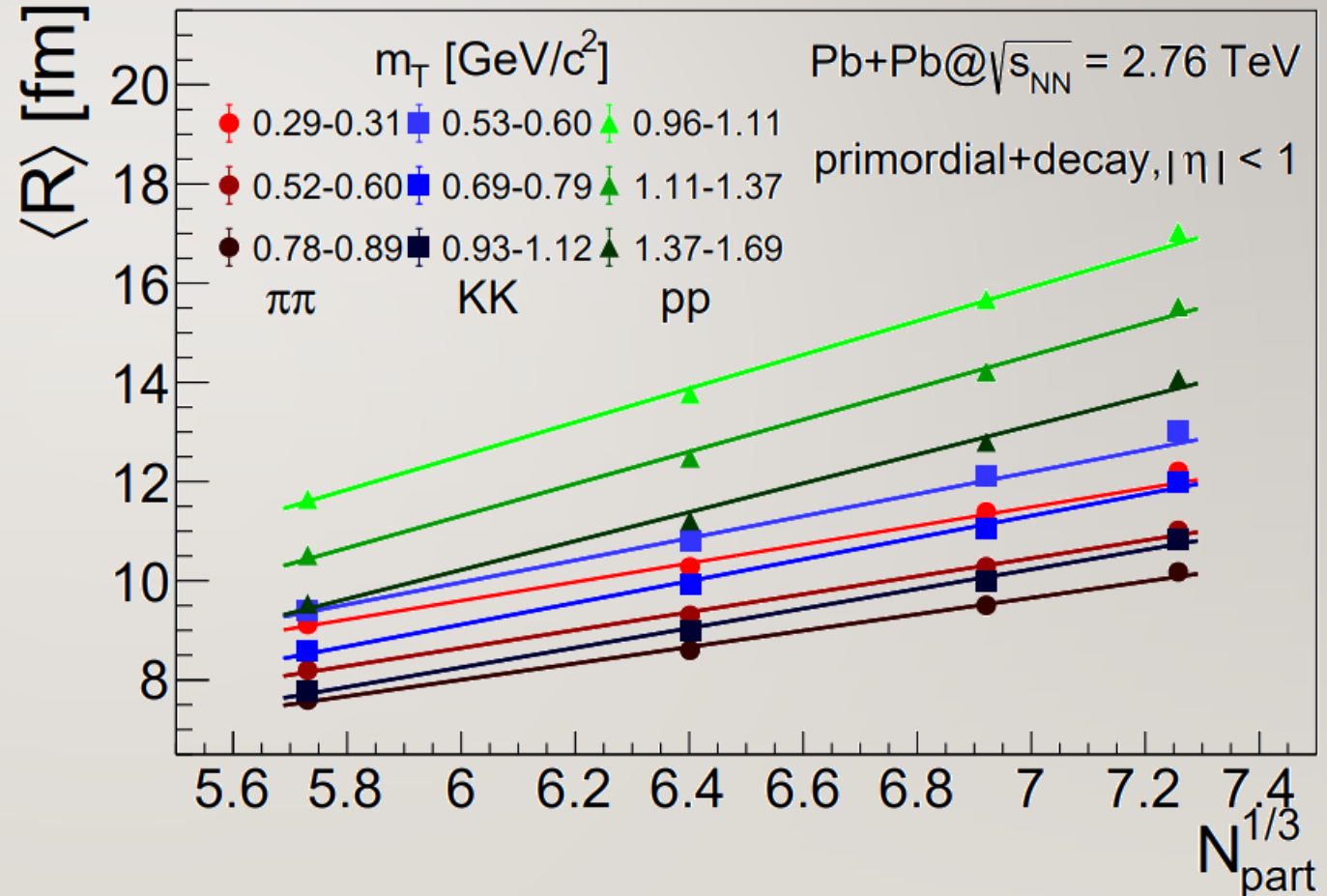


# 18 LÉVY SCALE PARAMETER VS $N_{part}$

- $N_{part}$  : average number of participating nucleons
- $N_{part}^{1/3} \sim$  one-dimensional initial size
- Approximately linear scaling  $\rightarrow$  geometric interpretation
- Super small statistical uncertainties:

$$\frac{\sigma_R}{\sqrt{N_{evts}}} \approx 0.01\%$$

## EPOS3 CORE+CORONA+UrQMD



# 19 INTERESTING SPECIES INDEPENDENT SCALING OF $R$

- $R$  vs.  $m_T - m \rightarrow$  same curve for pions and kaons
- Divide  $R$  with one plus the number of valence quarks  $\rightarrow$  same curve for protons
- Unknown reasons and interpretation

## EPOS3 CORE+CORONA+UrQMD

