

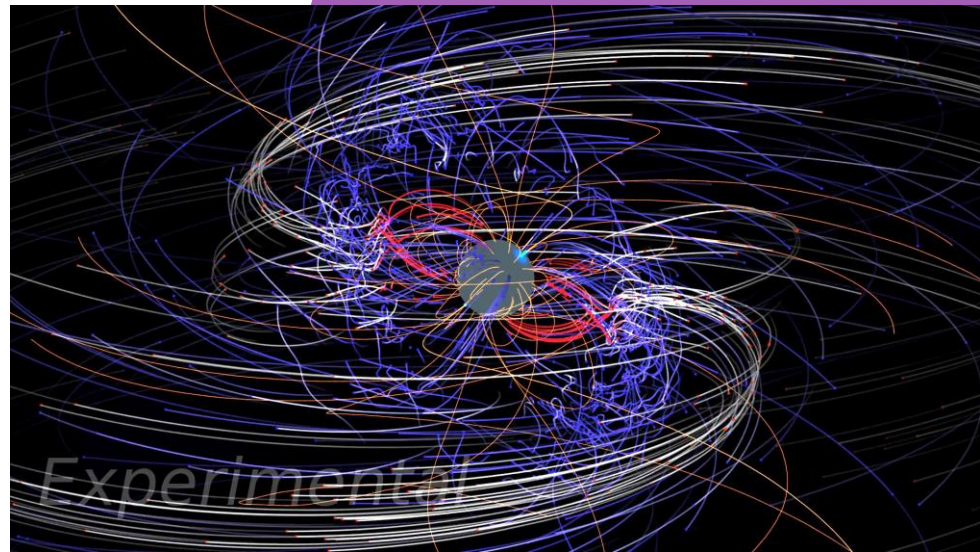


Addressing Challenges in Pulsar Science in the Era of Multi-messenger Astronomy

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**Applications of Quantum Information in
Astrophysics and Cosmology, 24–26 April
2023, Cape Town**



Setting the Scene

**Quantum
Information
Theory**

Astrophysics

Maths

Physics

**Computer
Science**

Neutrinos

Cosmology

**Multi-
wavelength
Astronomy**

Applications?

Setting the Scene

**Quantum
Information
Theory**

Astrophysics

Physics

**Multi-
wavelength
Astronomy**

Pulsars

Overlaps?



Astrono- mical Facilities



MeerKAT Radio Telescope

- Inaugurated in July 2018 in Carnarvon, Northern Cape
- 64 dishes; 13.5 m diameter
- Modes: Continuum, spectral lines, timing, polarisation, transient searches
- Receivers:
 - 0.58 – 1.015 GHz;
 - 0.9 – 1.67 GHz;
 - 8 – 14.5 GHz
- SKA Pathfinder
- MeerKAT Extended: 84 dishes (MPIFR)
- Massive computing and digital processing systems on site



Credit: SARAO

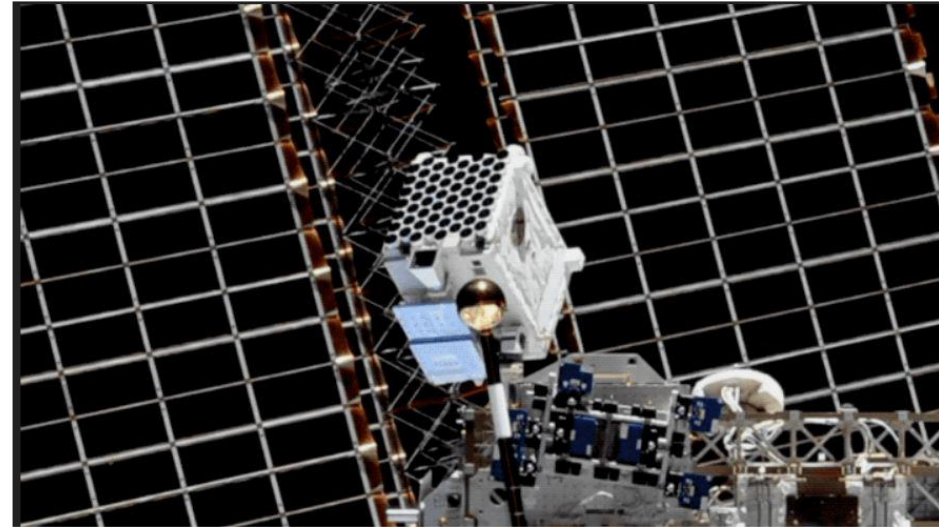
Southern African Large Telescope (SALT)

- Largest single optical telescope in Southern Hemisphere
- Located at SAAO outside Sutherland
- 11 m hexagonal primary mirror array
- 320 – 1700 nm
(near UV- near IR)
- Imaging, spectra, polarisation, transients
- Legacy Survey of Space and Time (LSST): South African involvement; 10-year survey of Southern Sky; 15 TB / night

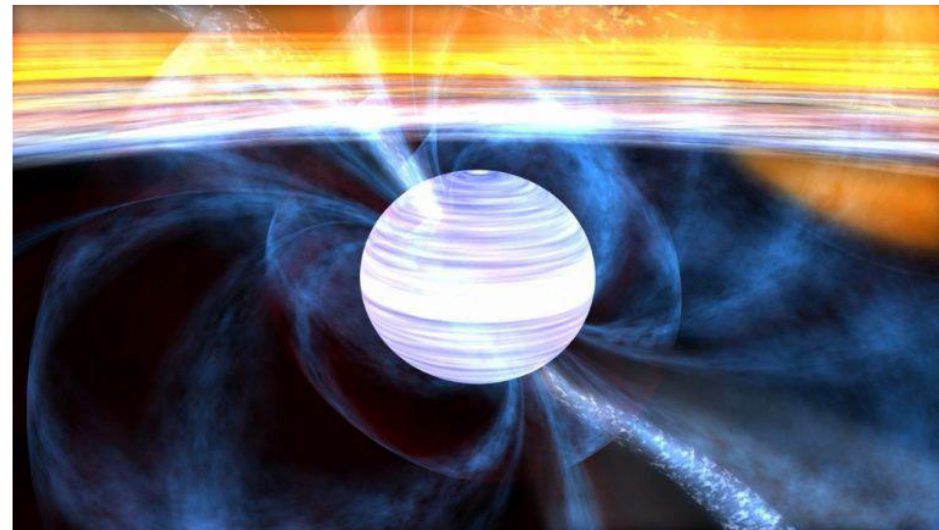


NICER

- Neutron star Interior Composition Explorer
- NASA's payload (372 kgs) on the ISS since 2017
- Planned: 18 months
- X-ray timing instrument: array of 56 X-ray photon detectors
- Soft (0.2–12 keV) X-ray band
- Unprecedented sensitivity
- Science goals:
 - ✓ Fundamental investigation of extremes in gravity, material density, and EM fields
 - ✓ Better understanding of the extreme nature and composition of neutron stars (NSs)
 - ✓ Constrain EOS to high precision



<https://heasarc.gsfc.nasa.gov/docs/nicer>



Fermi Large Area Telescope (LAT)

- Launched in June 2008
- Low-Earth orbit
- Pair-conversion instrument
- FoV > 2 sr (20% of sky)
- Scans whole sky every 3 h
- 20 MeV – 300 GeV (gamma rays)
- > 8000 cm² effective area
- Pulsars, nebulae, novae, supernova remnants, active galaxies, globular clusters, GRBs, Fermi Bubbles, Galactic Centre, cosmic rays, terrestrial flashes, sun, etc.



H.E.S.S. Telescopes

- High Energy Stereoscopic System
- Ground-based Imaging Atmospheric (Air) Cherenkov Telescopes (IACTs)
- Very-high-energy gamma-ray photons (50 GeV to 100 TeV)
- 4 x 12-m and 1 x 28-m telescopes
- PWNe, AGNe, SNRs, GRBs, binaries, galaxies, haloes, MM follow-up...
- And now also **pulsars!**
- Next: Cherenkov Telescope Array (CTA)

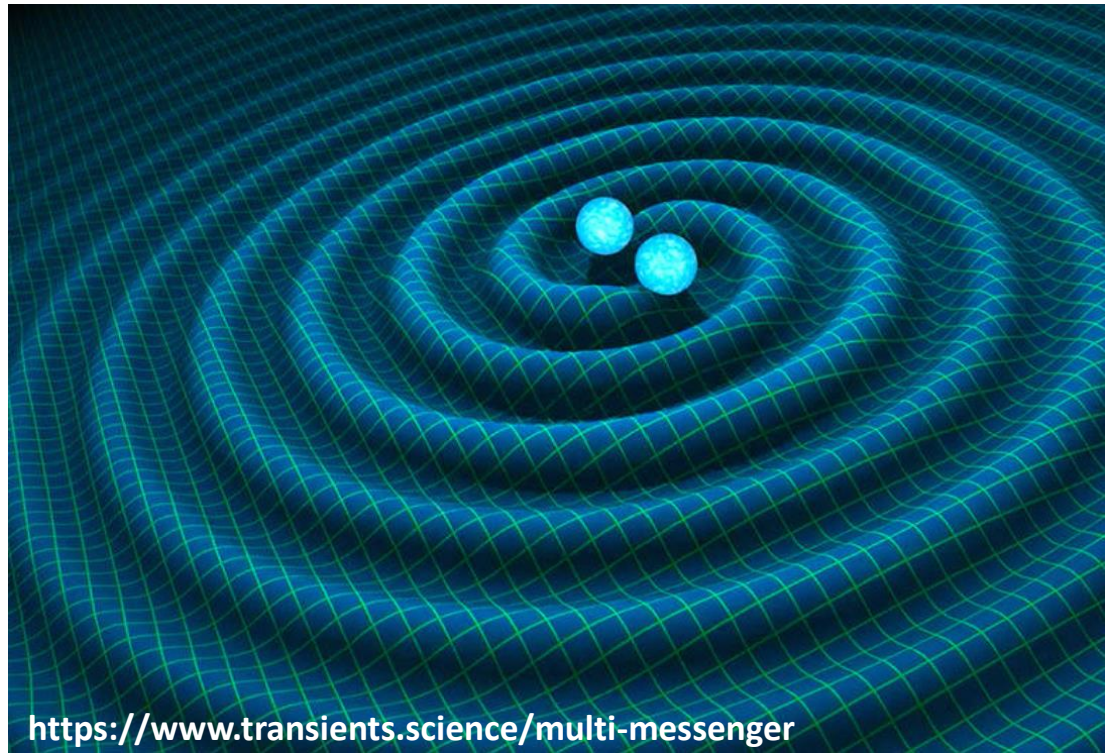


Multi-messenger Astronomy

GW170817:

- Binary neutron star merger
- Gravitational waves by LIGO
- *Fermi* GBM: short GRB
- Bright optical transient
- X-ray and radio emission
- No VHE gamma rays / neutrinos

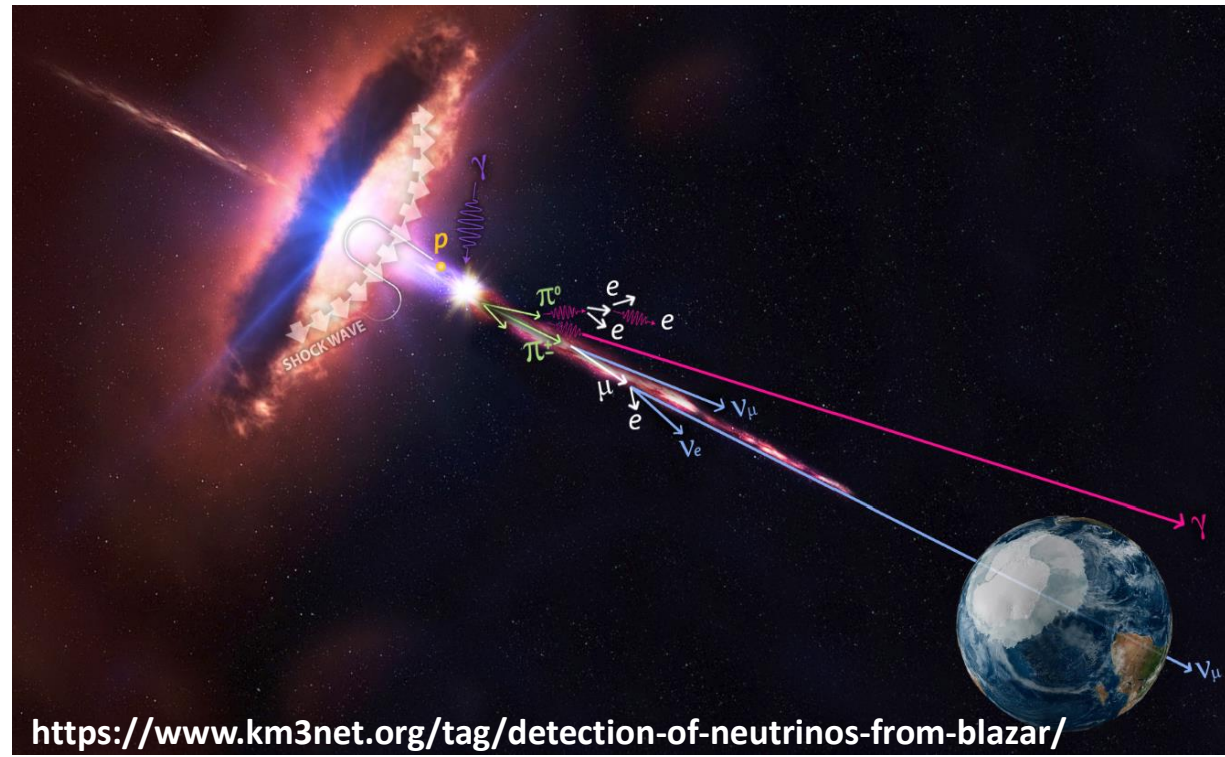
(Abbott et al. 2017)



Multi-messenger Astronomy

TXS 0506+056:

- IceCube Neutrino Telescope detected a 290 TeV neutrino passing through deep South Pole Ice on 22/09/2017
- Flaring Blazar (VHE)
- Archival data:
excess of neutrino events
- Solved century-old riddle as to the source of cosmic rays
(Aartsen et al. 2018)

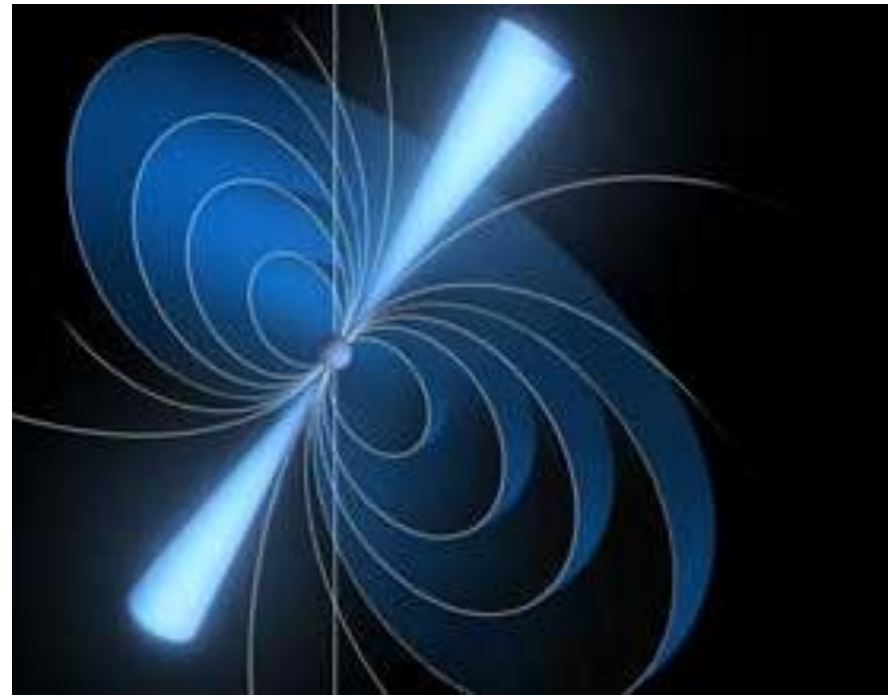
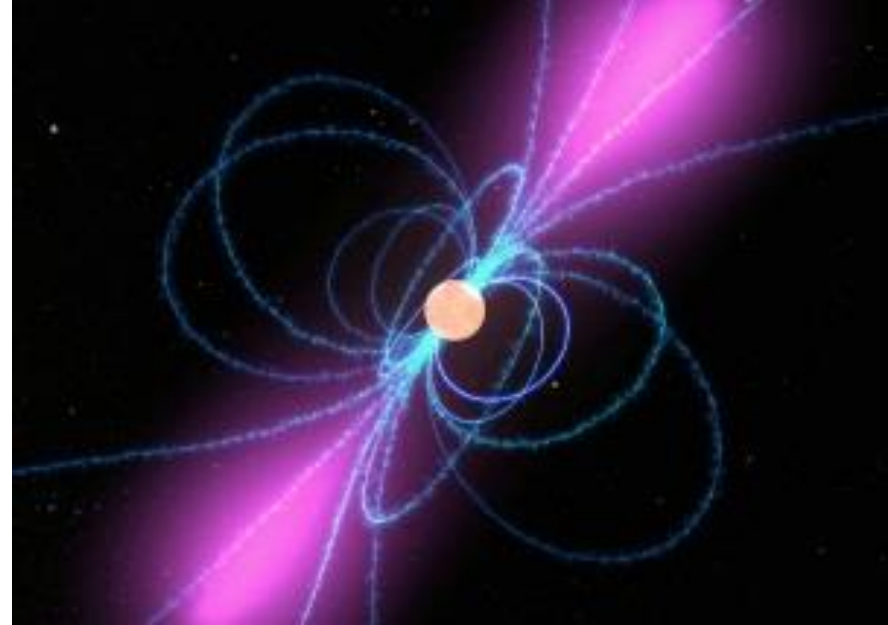


Pulsars



Pulsars

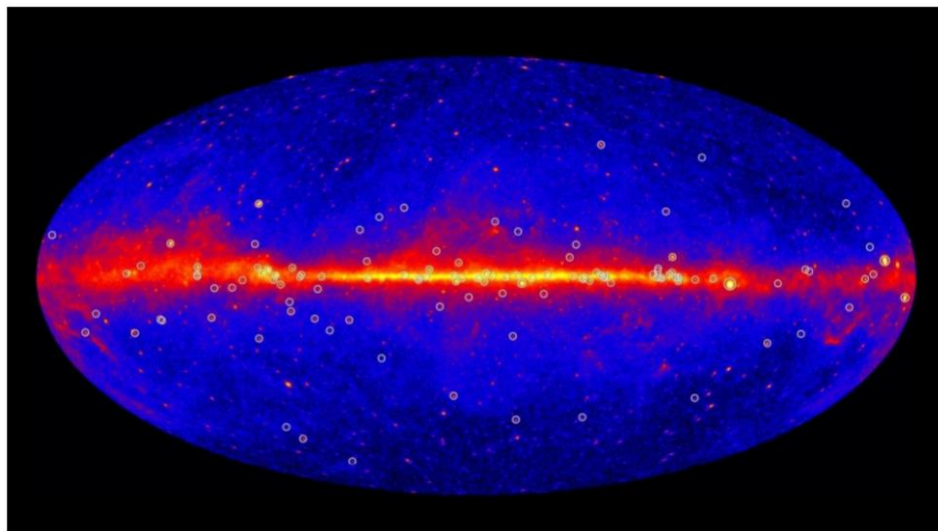
- Rapidly-rotating, highly-magnetised neutron stars
- Progeny of supernova explosions
- Spin-modulated, beamed pulsations across the EM band, wind of particles
- ~2 500 in radio, ~270 in GeV, also tens in X-rays, optical.
- “Pulsar zoo”: magnetars, RRATs, MSPs, binaries, MeV pulsars, transitional systems, etc.



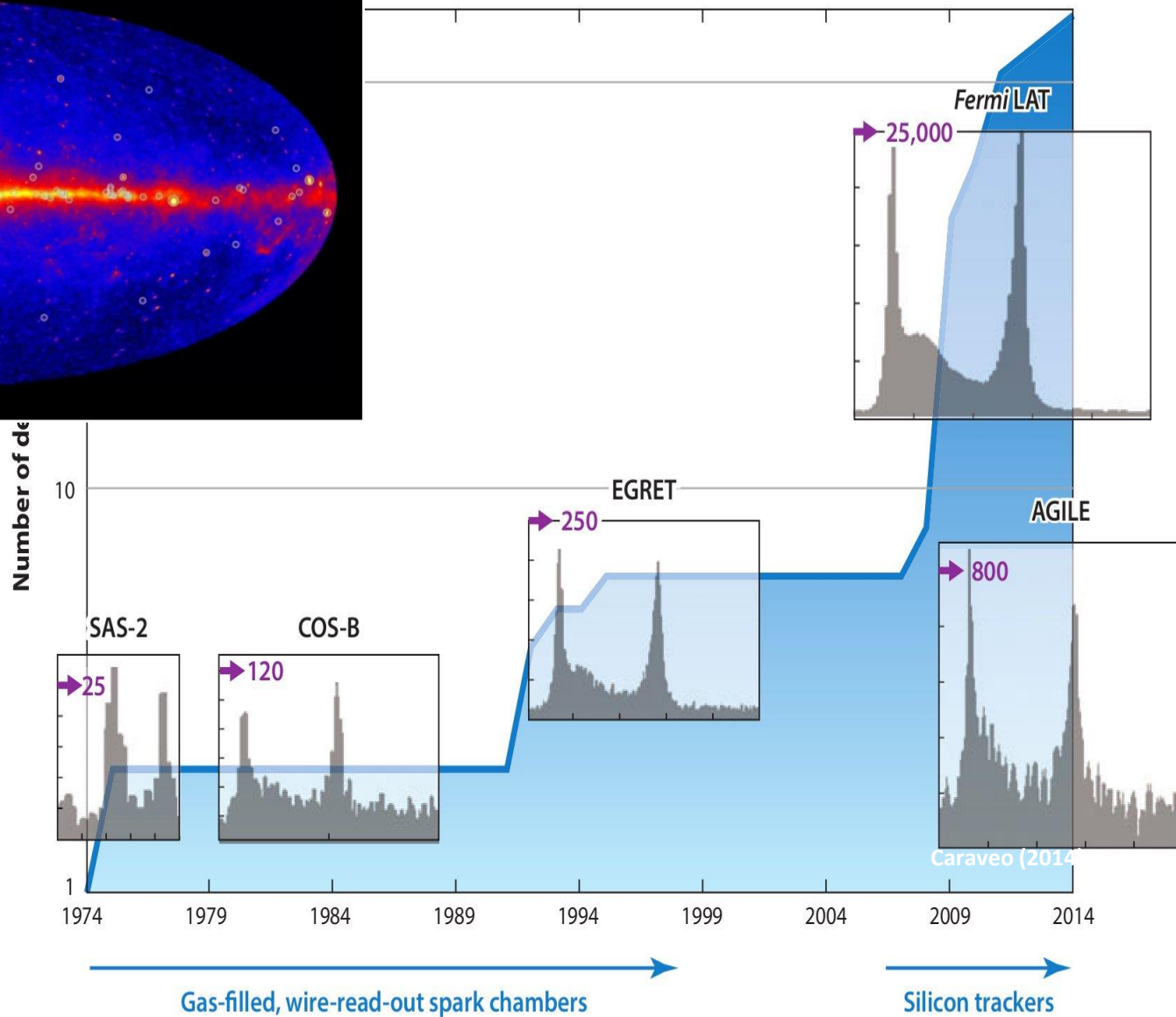
Observational Highlights



Fermi LAT Observations



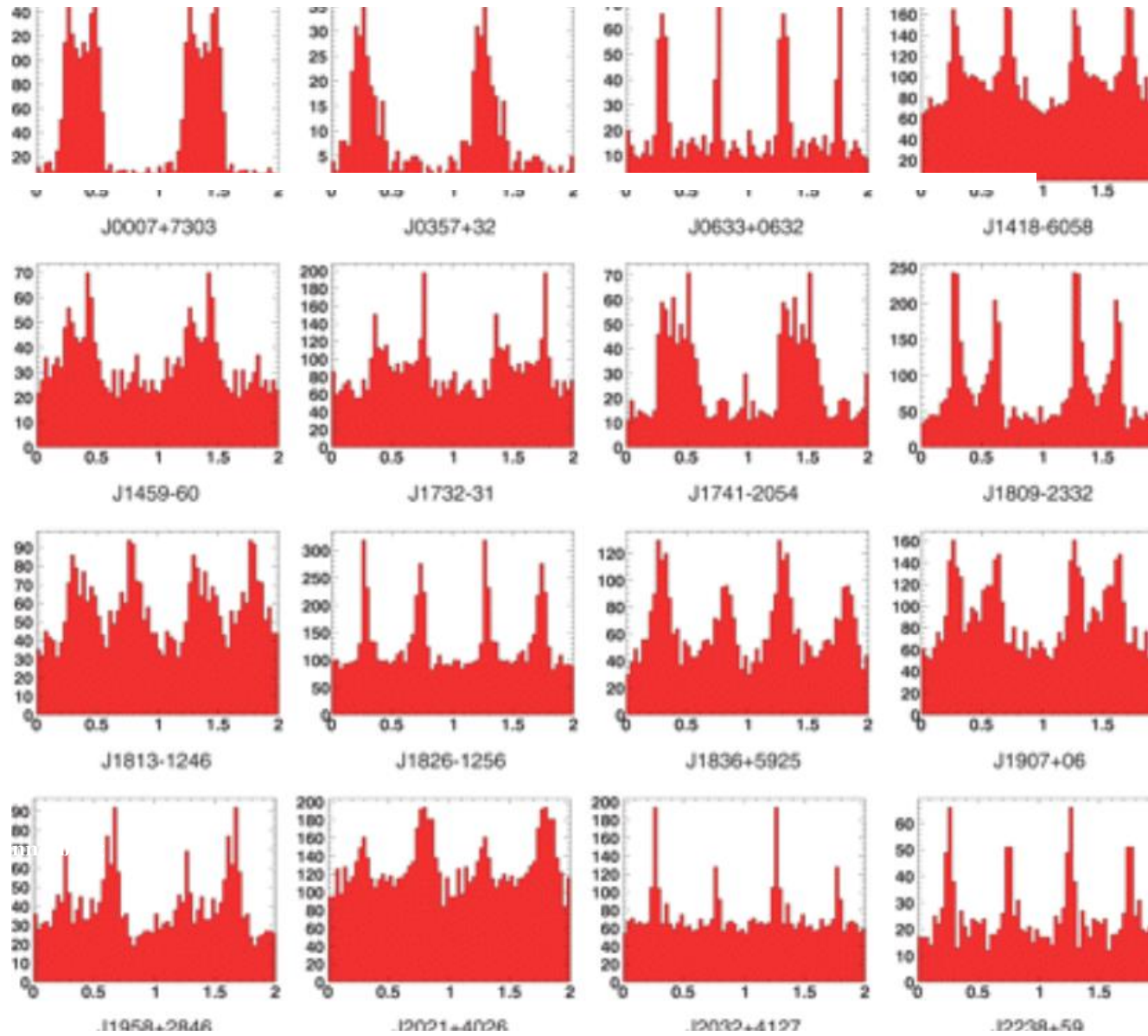
- Revolution in pulsars science
- >250 pulsars, 118 MSPs
- 3PC in production: Light curves, spectra, trends



Observations

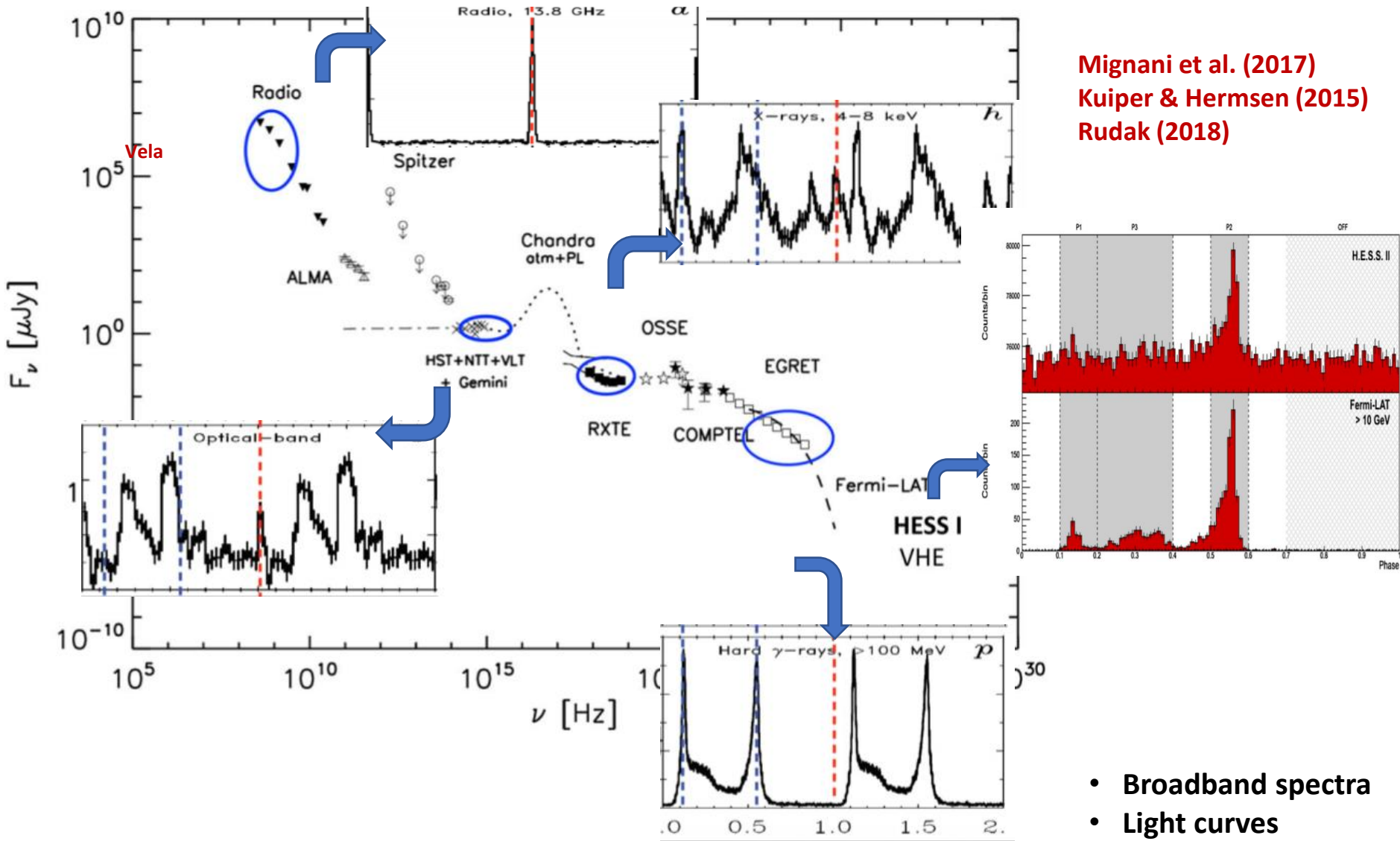
Abdo et al. (2009)

- Diversity of light curves (LC)
- 3PC



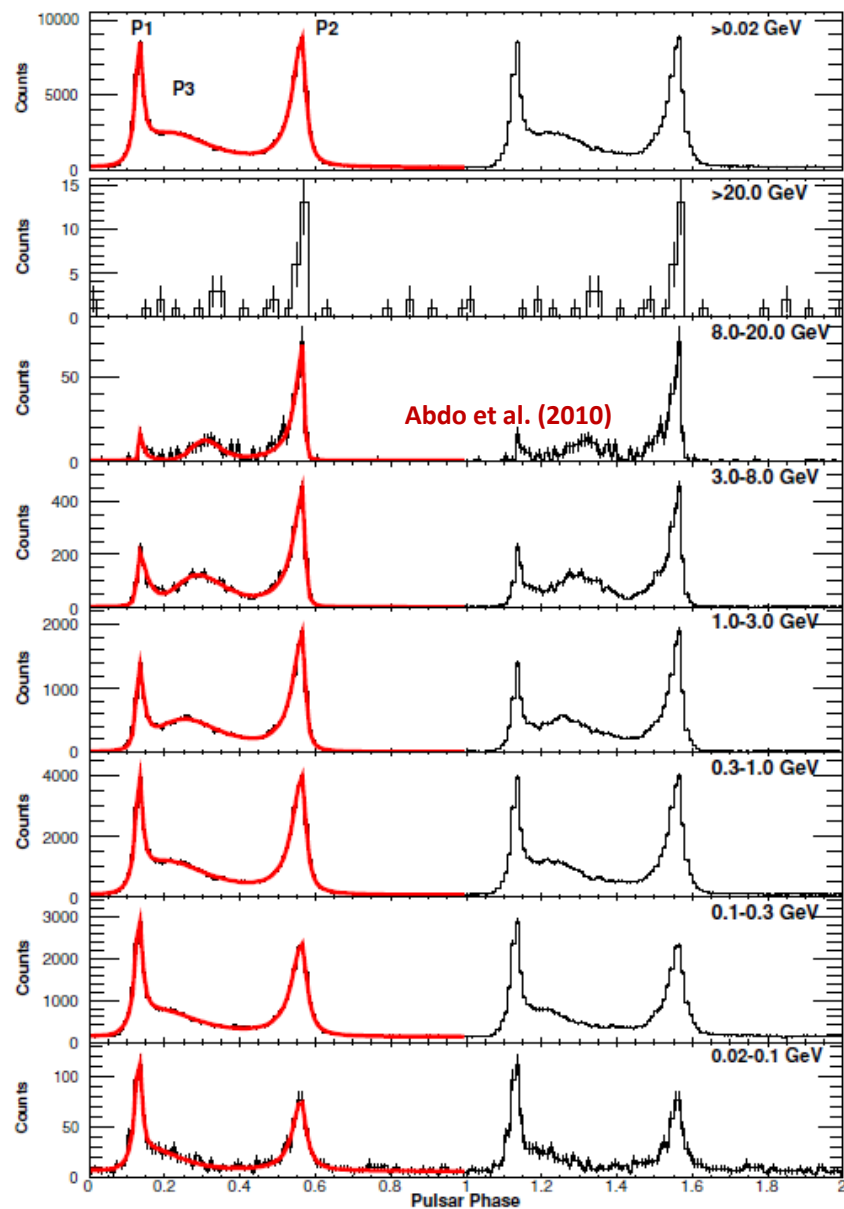
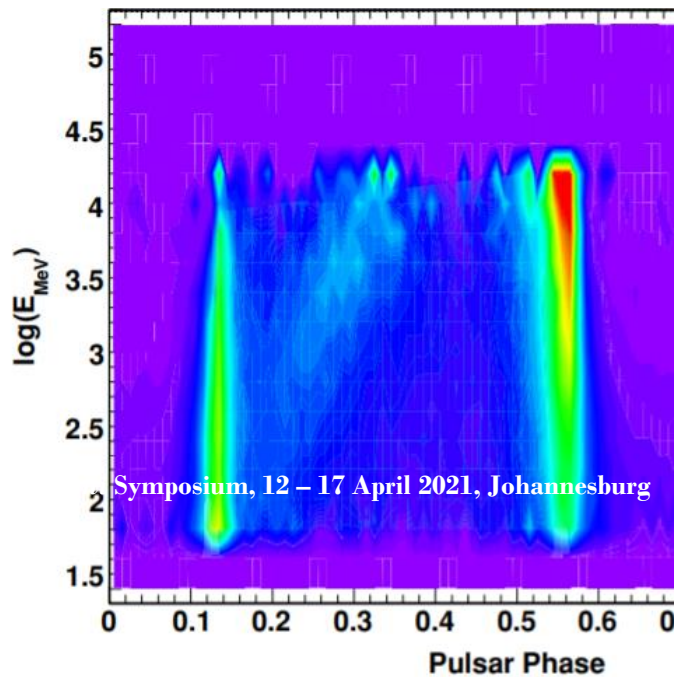
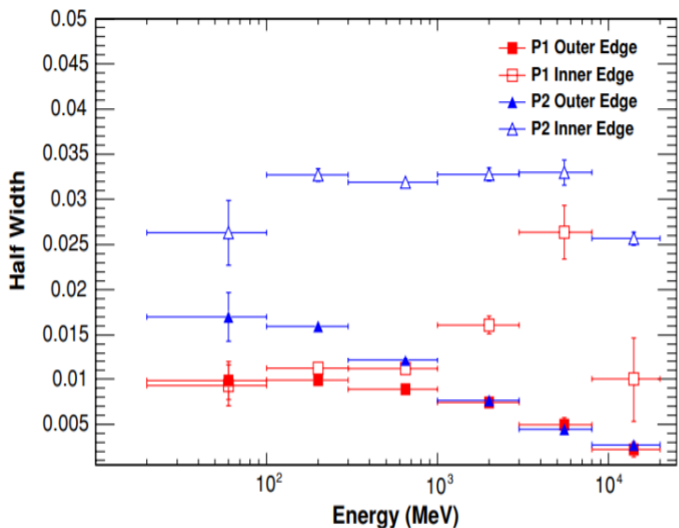
Observations

Mignani et al. (2017)
 Kuiper & Hermsen (2015)
 Rudak (2018)



- Broadband spectra
- Light curves

Observations

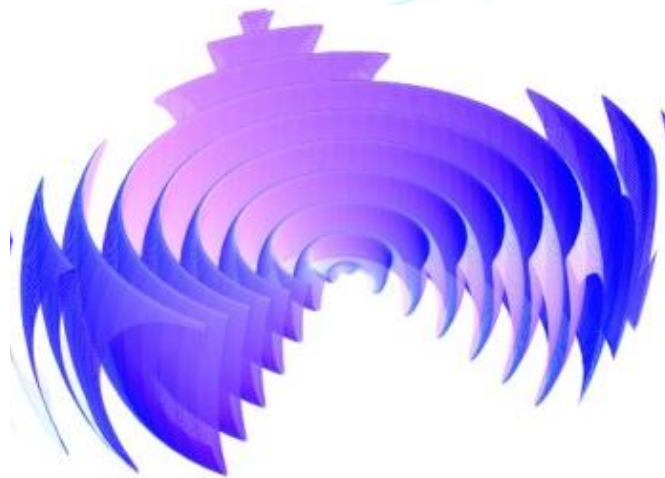
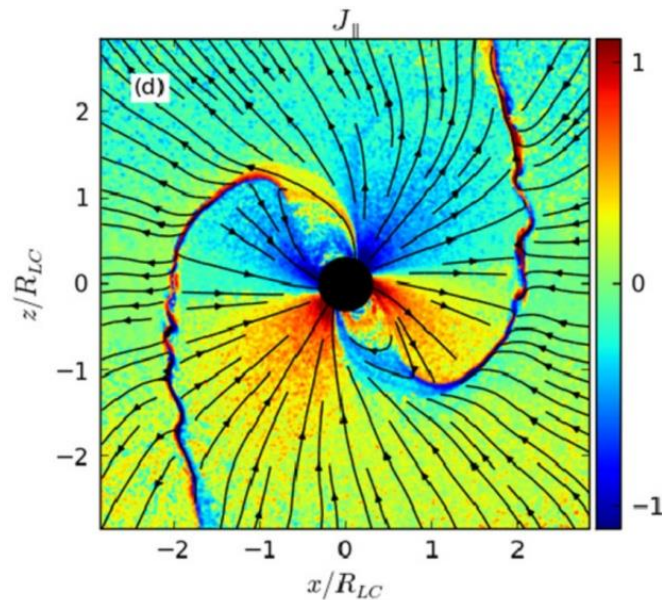
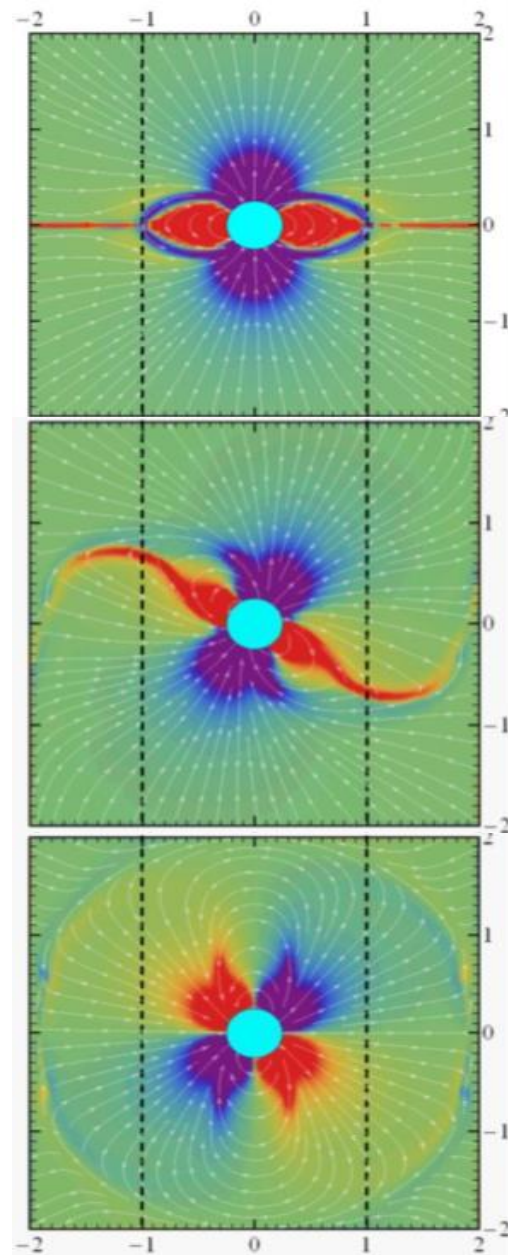
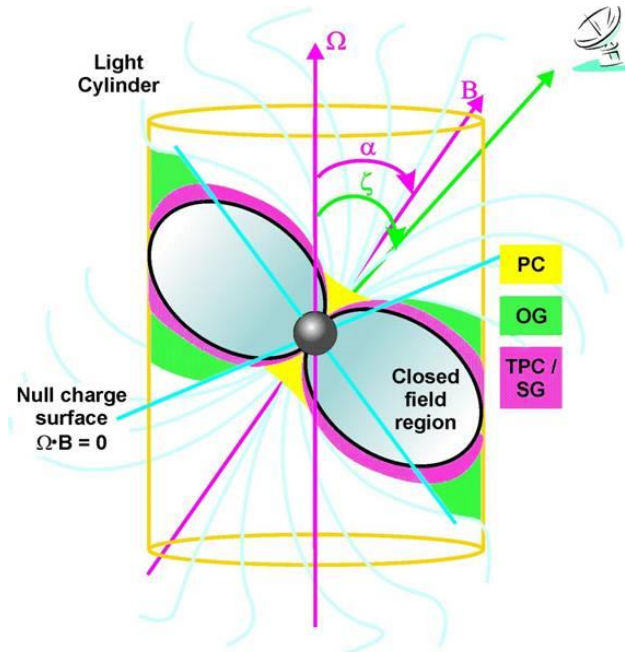


Models



Model Overview

- Traditional models
- Striped-wind models
- Separatrix / current sheet models
- PIC models

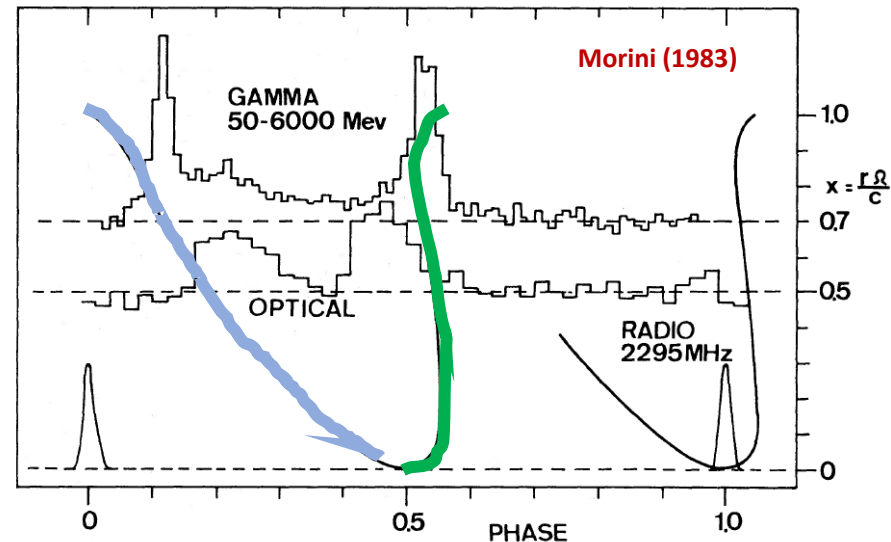
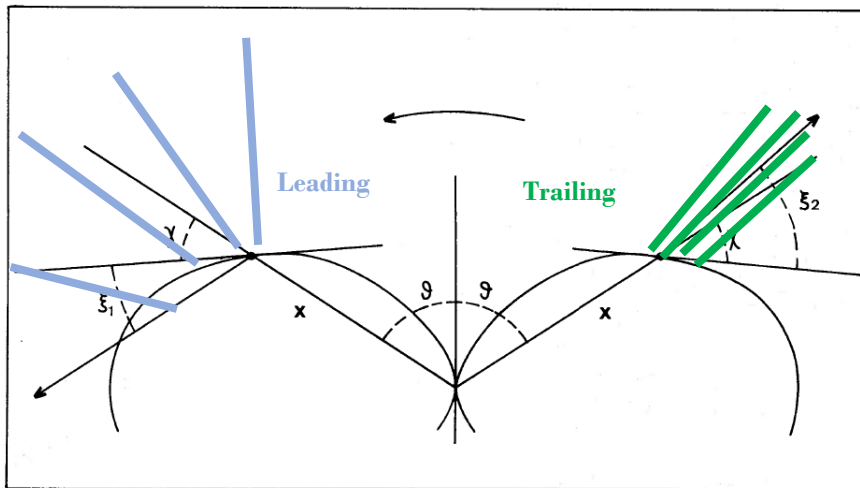


Light Curve Modelling of Pulsars



Caustics / Photon Bunching

- Traditional models

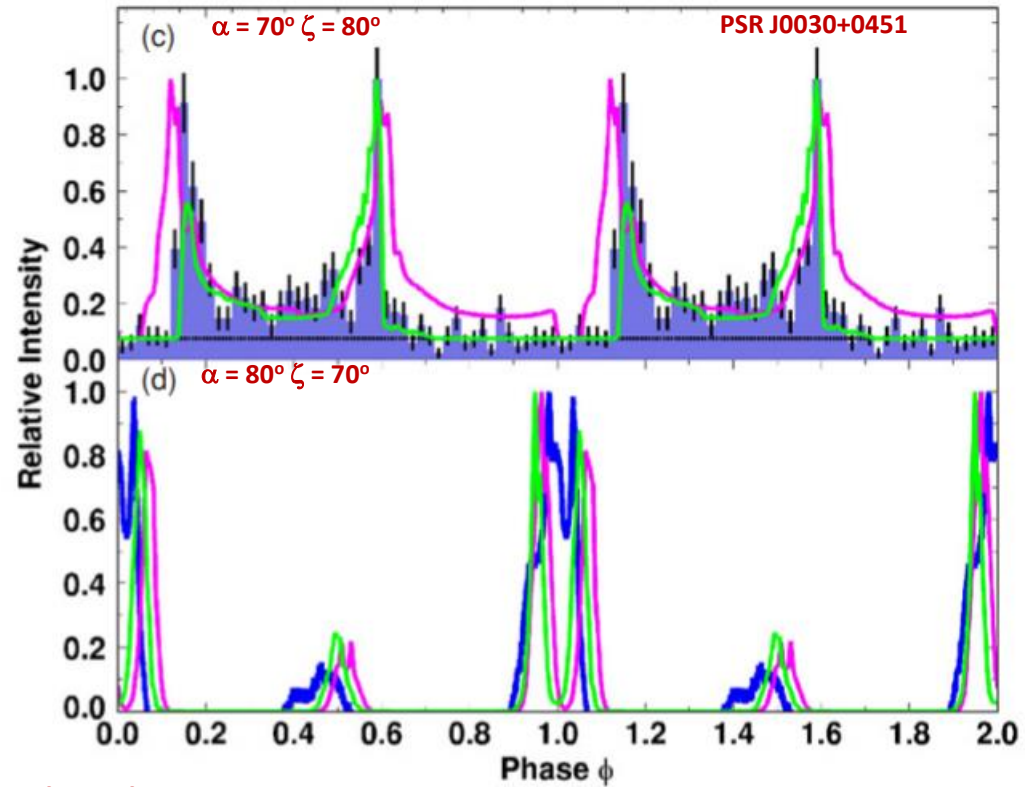
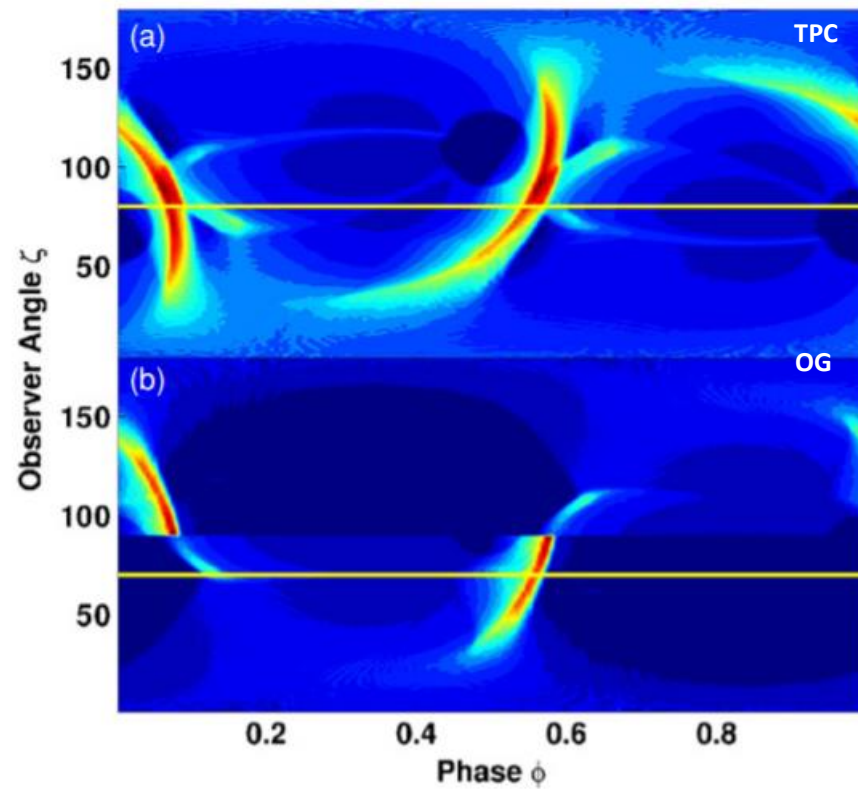


Morini (1983)
 Romani & Yadigaroglu (1995)
 Dyks et al. (2004)

Bunching of photons (from different field lines / heights) in phase due to:

1. B-field structure
2. Aberration when transforming from co-rotating to lab frame
3. Time-of-flight delays

Caustics / Photon Bunching



Venter et al. (2009)

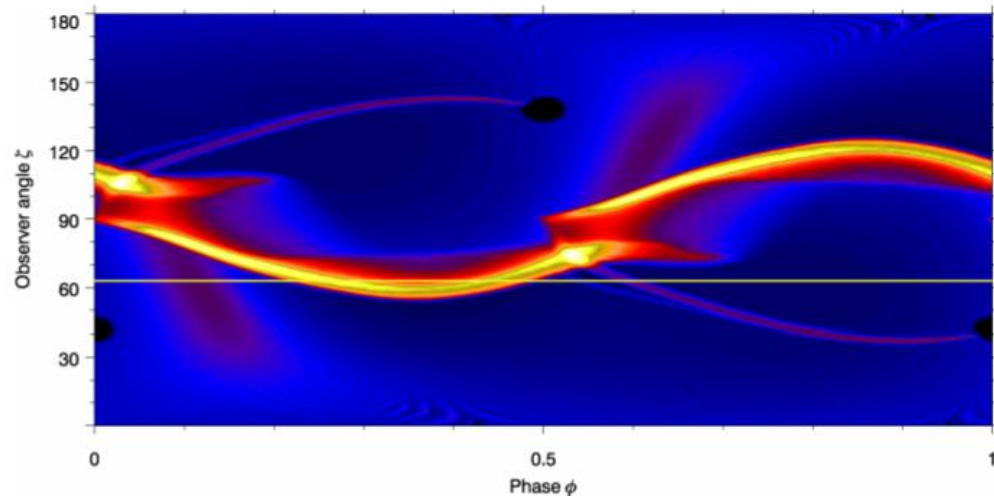
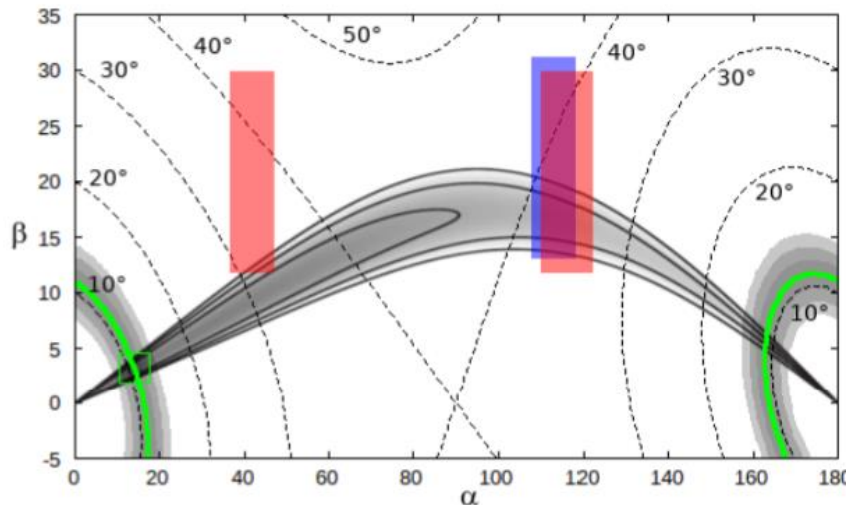
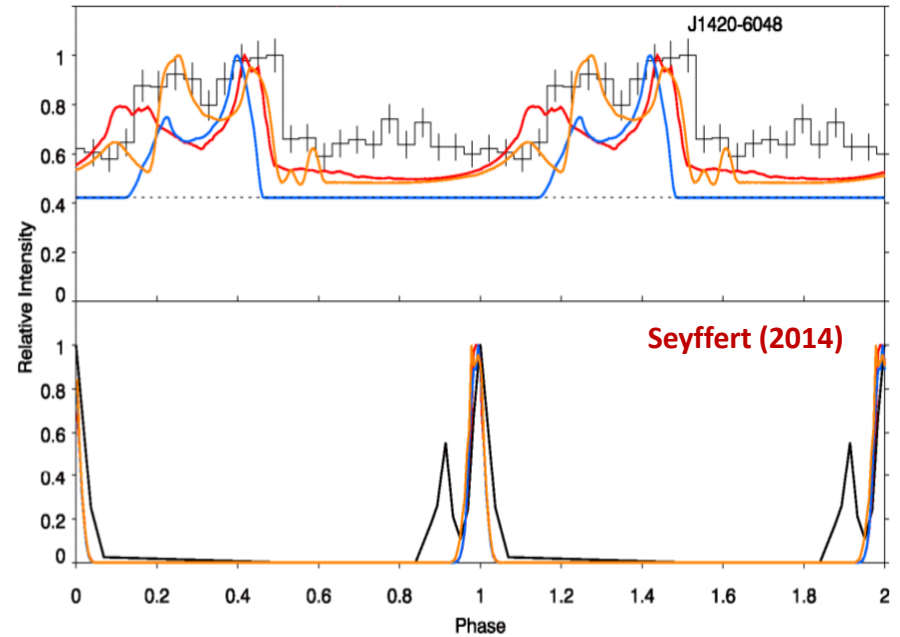
Probing Pulsar Geometry

- E.g., a **single-peaked γ -ray LC**
- Cut γ -ray caustic almost tangentially
- Use radio light curve information: rotating vector model (RVM), phase shift

$$\tan(\psi - \psi_0) = \frac{\sin \alpha \sin(\phi - \phi_0)}{\sin \zeta \cos \alpha - \cos \zeta \sin \alpha \cos(\phi - \phi_0)},$$

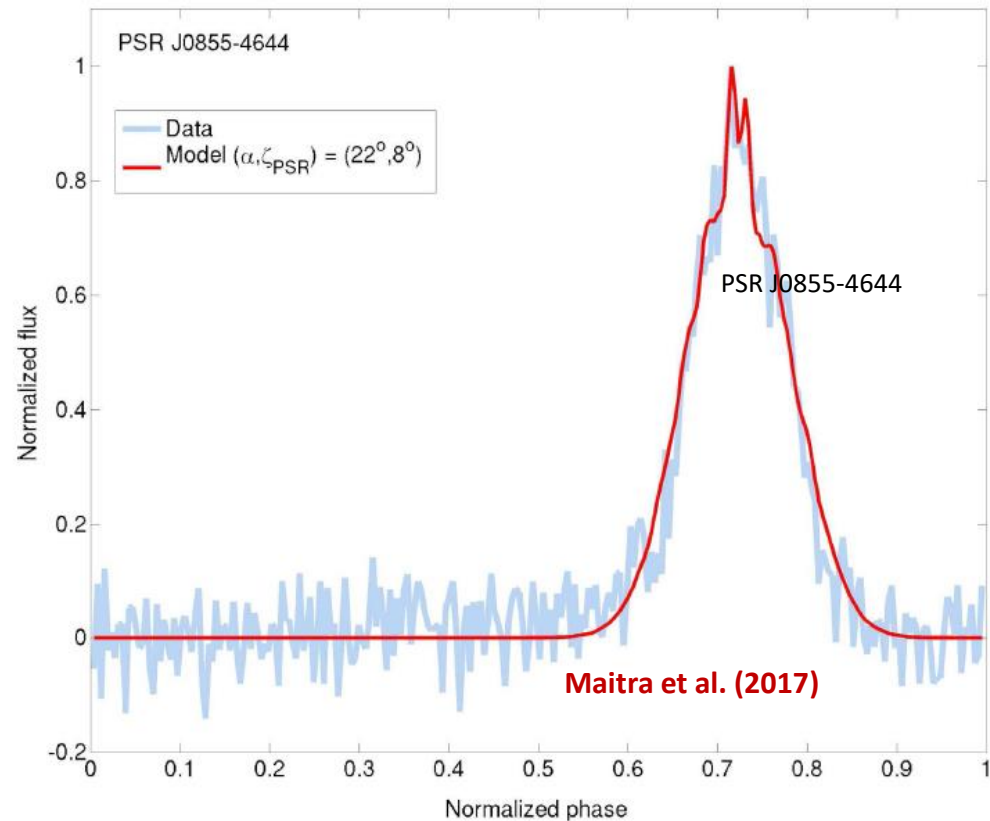
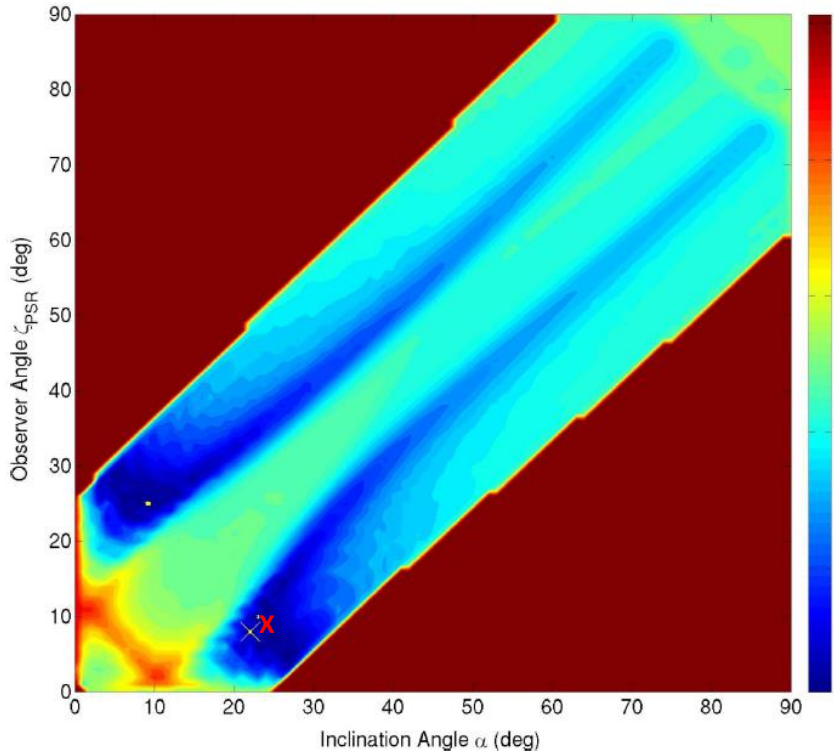
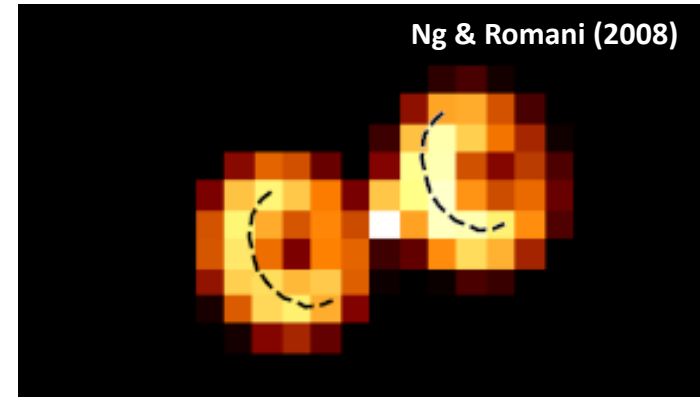
$$h_{\text{P.A.}} = \frac{Pc}{8\pi} \Delta\phi = \frac{1}{4} R_{\text{LC}} \Delta\phi$$

Weltevrede et al. (2010)
Cf. Rookyard et al. (2015)



Probing Pulsar Geometry

- E.g., a **γ -ray-quiet pulsar**
- Double-torus fitting: $\zeta = 32.5^\circ \pm 4.3^\circ$
- Thermal pulsed X-rays: low $\beta = \zeta - \alpha$
- Single radio peak: $\beta > 10^\circ$
- Radio visibility: $\beta < 30^\circ$
- γ -ray invisibility: $\alpha < 55^\circ, \zeta < 55^\circ$
- Best-fit radio LC: $(\alpha, \zeta) = (22^\circ, 8^\circ)$

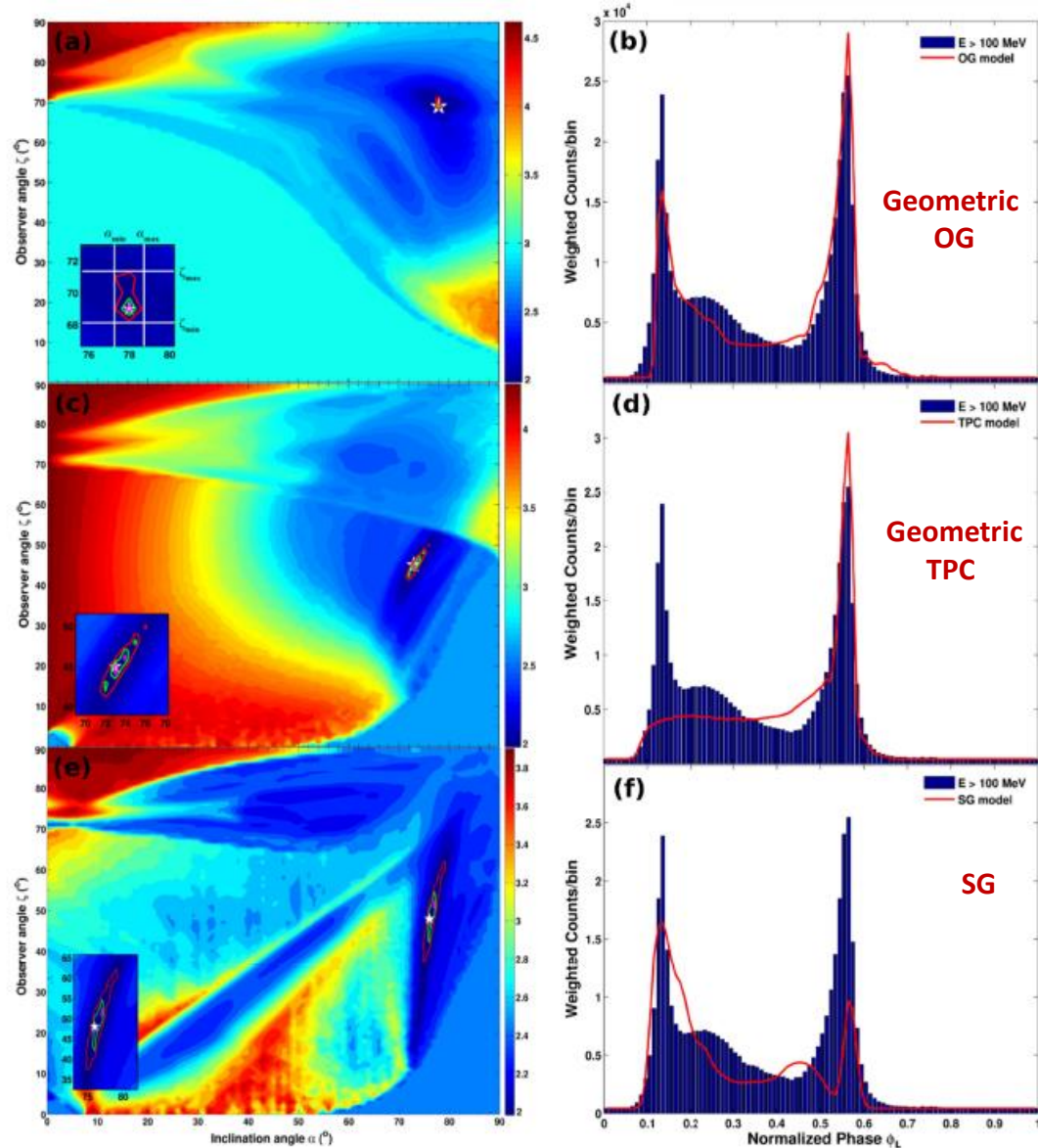
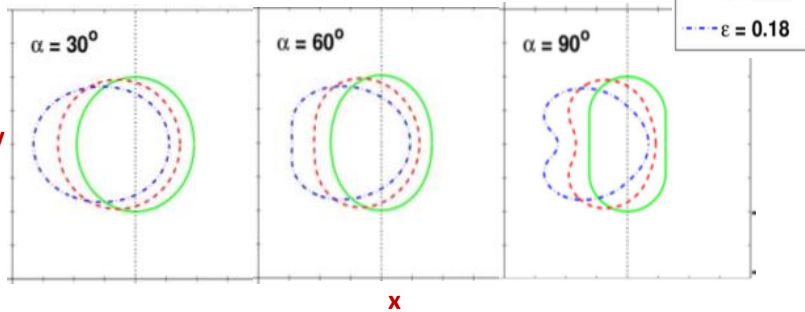


B / E-field Structure

- Offset-dipole fields: geometric / emission models

$$B'_{OPCs} \approx \frac{\mu'}{r'^3} \left[\cos \theta' \hat{r}' + \frac{1}{2}(1+a) \sin \theta' \hat{\theta}' - \epsilon \sin \theta' \cos \theta' \sin(\phi' - \phi'_0) \hat{\phi}' \right],$$

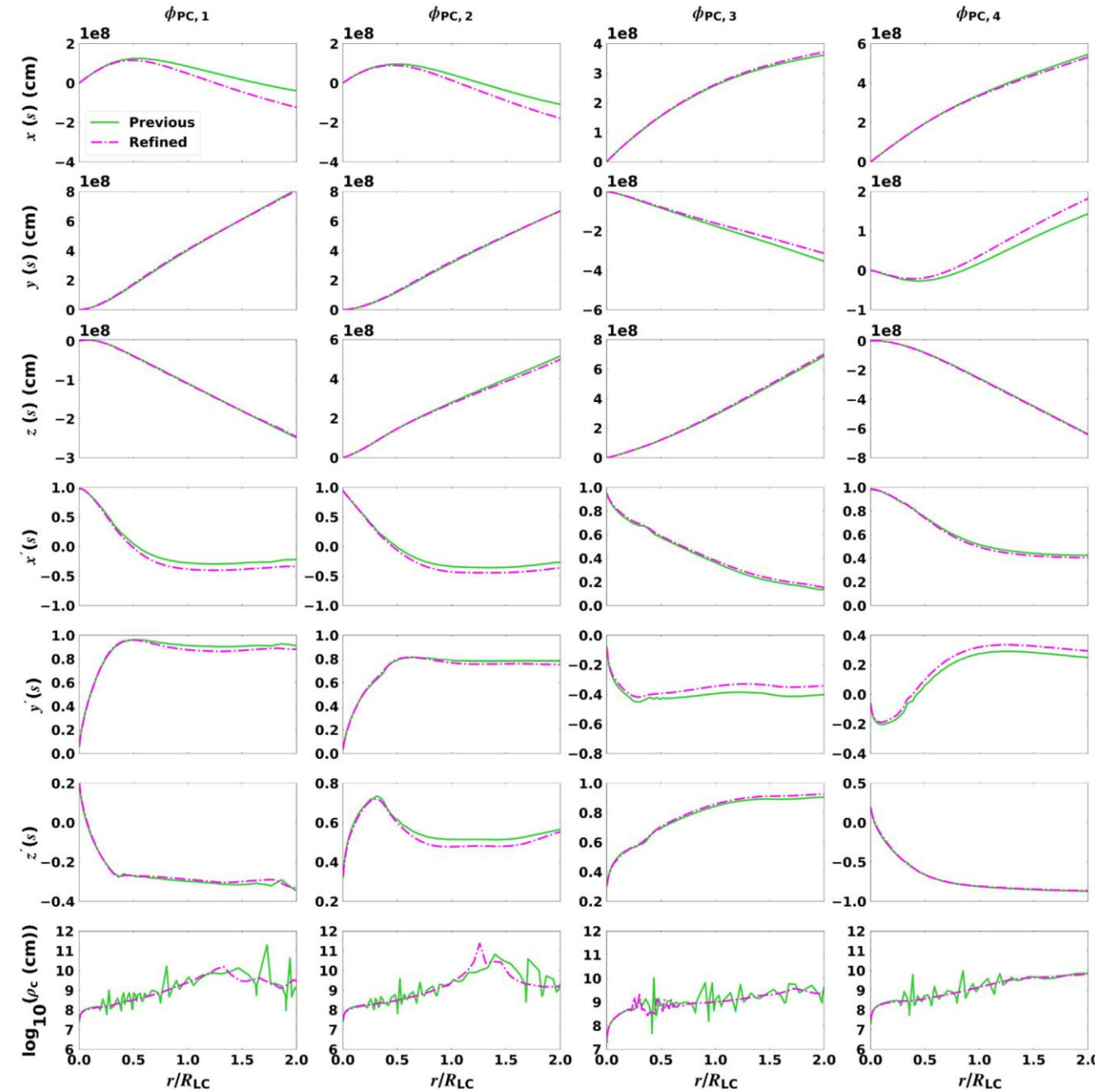
Barnard et al. (2016)



Energy- dependent Light Curve Modelling of Pulsars



Refinement of the Curvature Radius



- 4 sample trajectories
- Refine x, y, z components
- Refine derivatives of trajectories
- Refine r_c

Previous

Refined

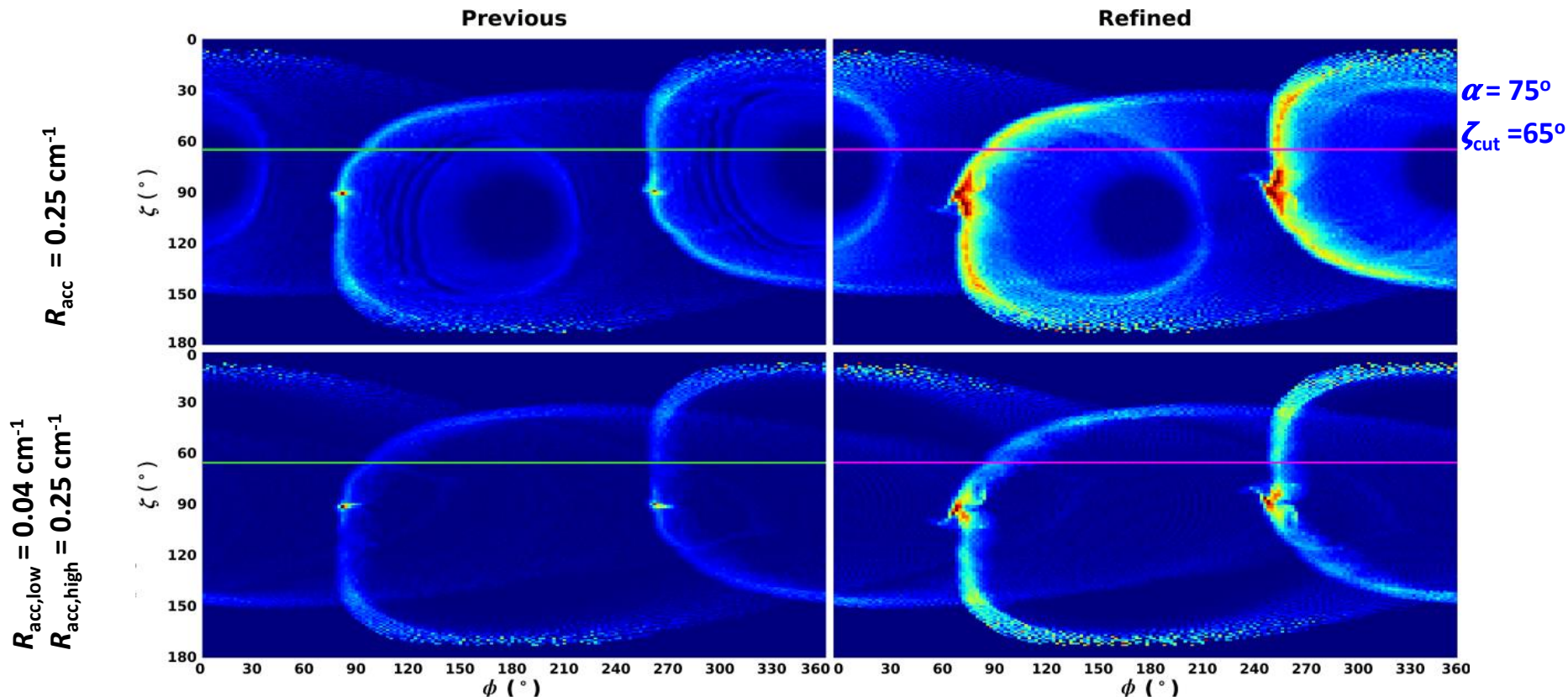
$$E_{\gamma, CR} = \frac{3\lambda_c \gamma^3}{2\rho_c} m_e c^2$$

Credit: M. Barnard

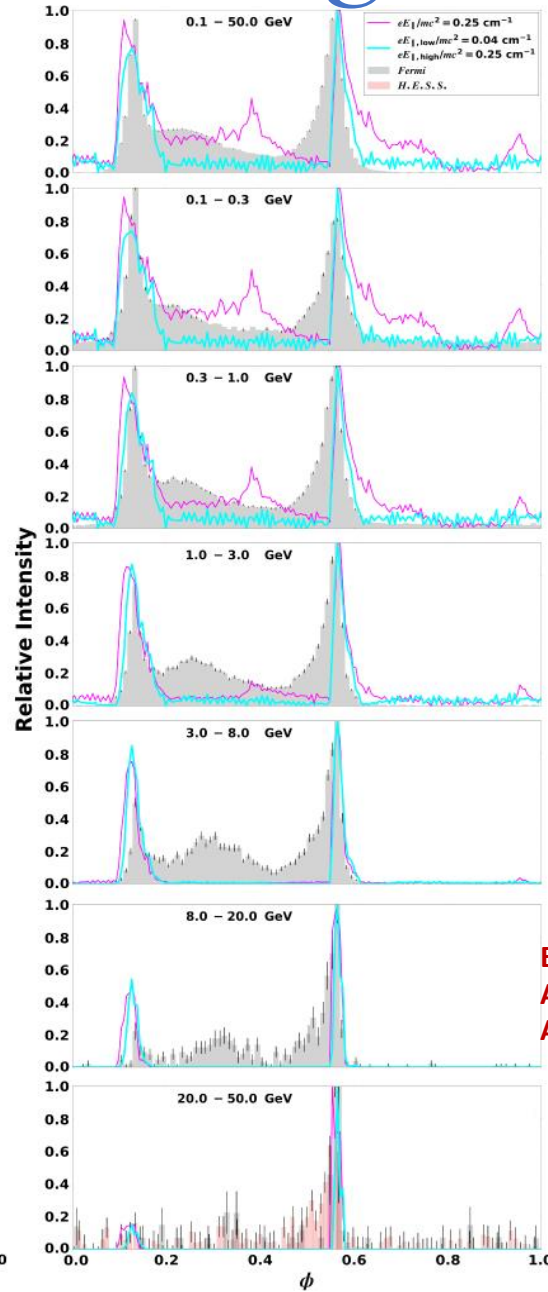
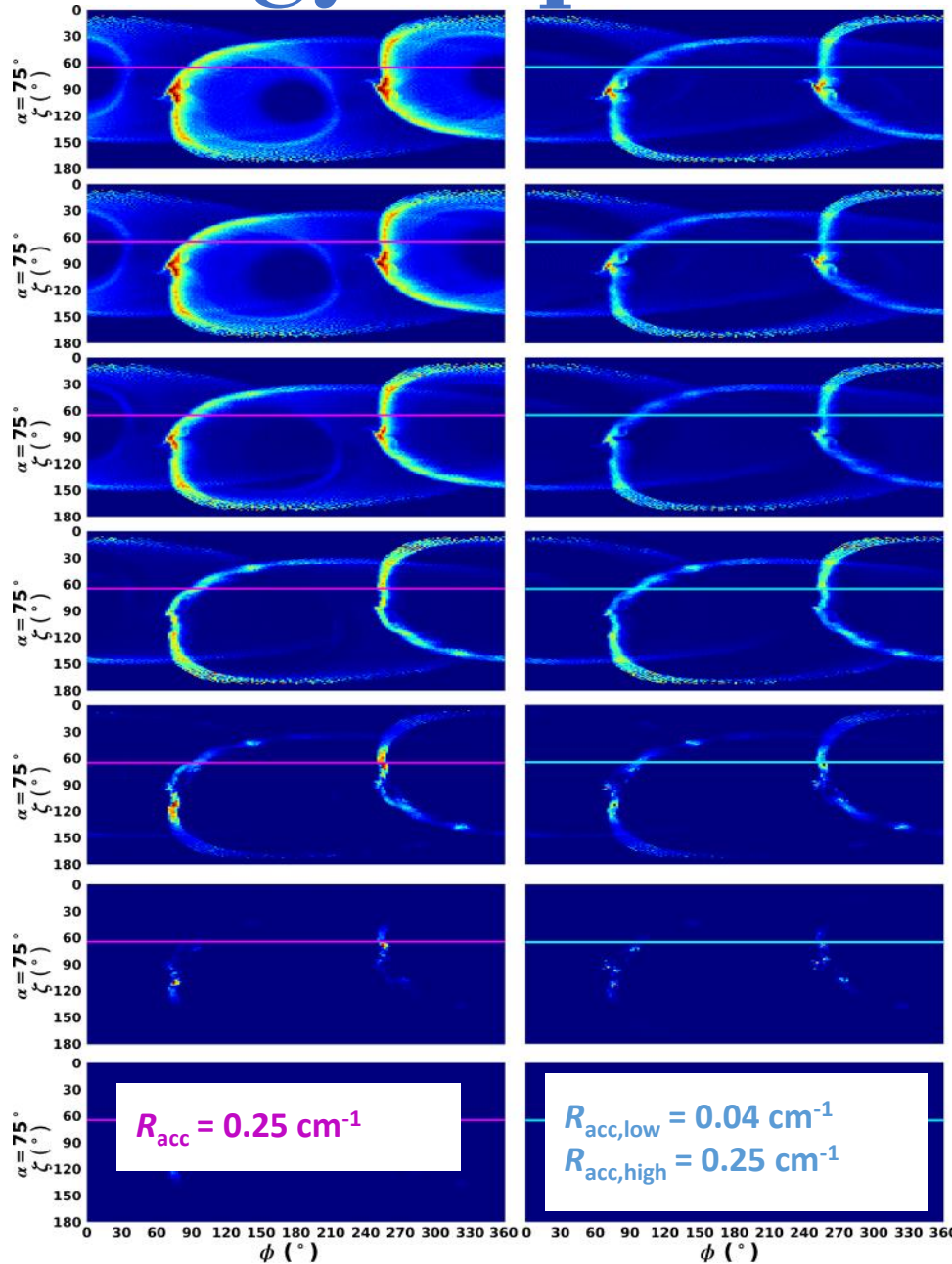
Refinement of the Curvature Radius

Barnard et al. (2022)

- One and two-step function for the accelerating E -field (motivated by kinetic simulations).
- Refined calculation of the curvature radius of particle trajectories - impacts the transport, light curves, and spectra.
- Did a small parameter study to find optimal parameters, i.e., α , ζ_{cut} , R_{acc} , and selected the best spatial resolution.



Energy-dependent CR Light Curves



$\alpha = 75^\circ$

$\zeta_{\text{cut}} = 65^\circ$

Trends:

- P1/P2
- Widths
- Phase

Barnard et al. (2022)
 Abdo et al. (2010,2013)
 Abdalla et al. (2018)

Phase-avg. / Phase-resolved Spectra

Barnard et al. (2022)

$\alpha = 75^\circ$

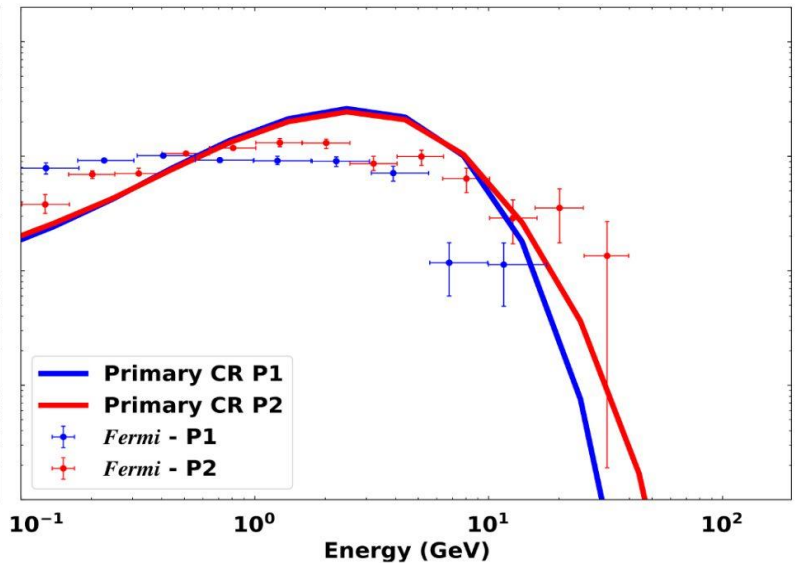
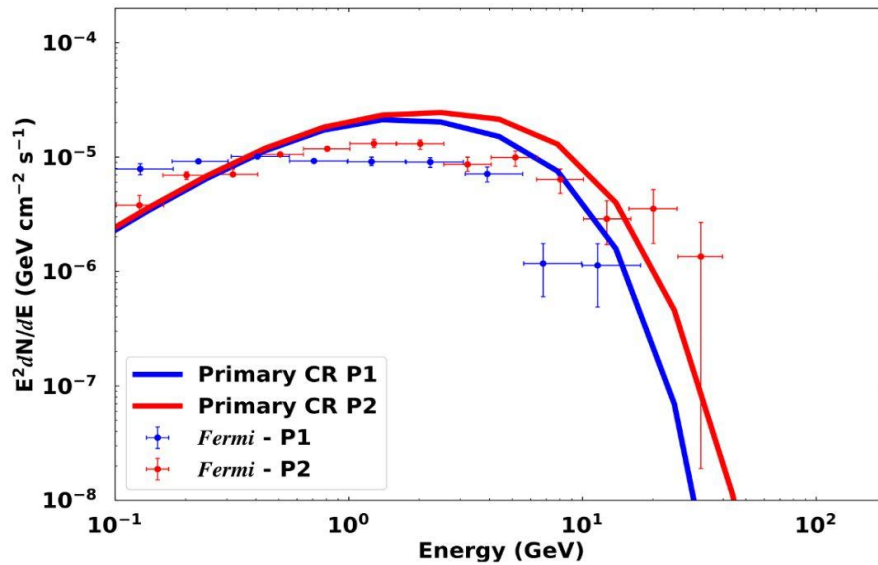
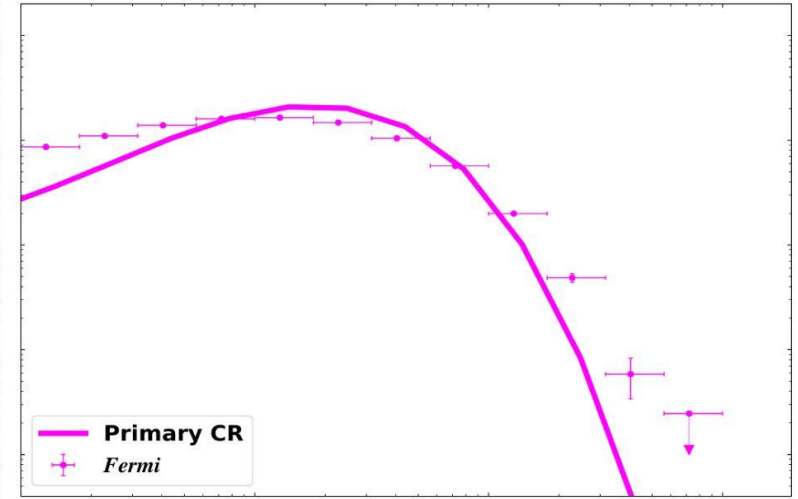
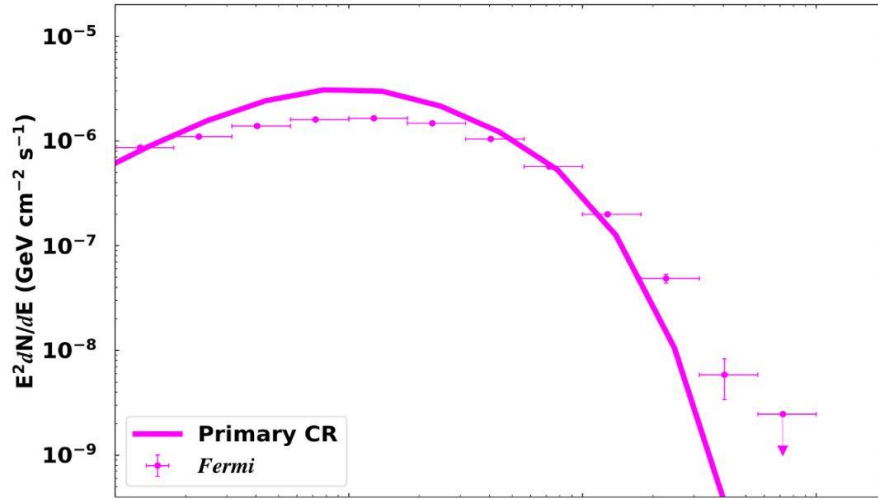
$\zeta_{\text{cut}} = 65^\circ$

$R_{\text{acc}} = 0.25 \text{ cm}^{-1}$

Norm = $5J_{\text{GJ}}$

$R_{\text{acc,low}} = 0.04 \text{ cm}^{-1}; R_{\text{acc,high}} = 0.25 \text{ cm}^{-1}$

Norm = $8.5J_{\text{GJ}}$



Abdo et al. (2010,2013)

Local Environment: P1/P2

$$E_{\gamma, \text{CR}} = \frac{3\lambda_c \gamma^3}{2\rho_c} m_e c^2$$

$\alpha = 75^\circ$

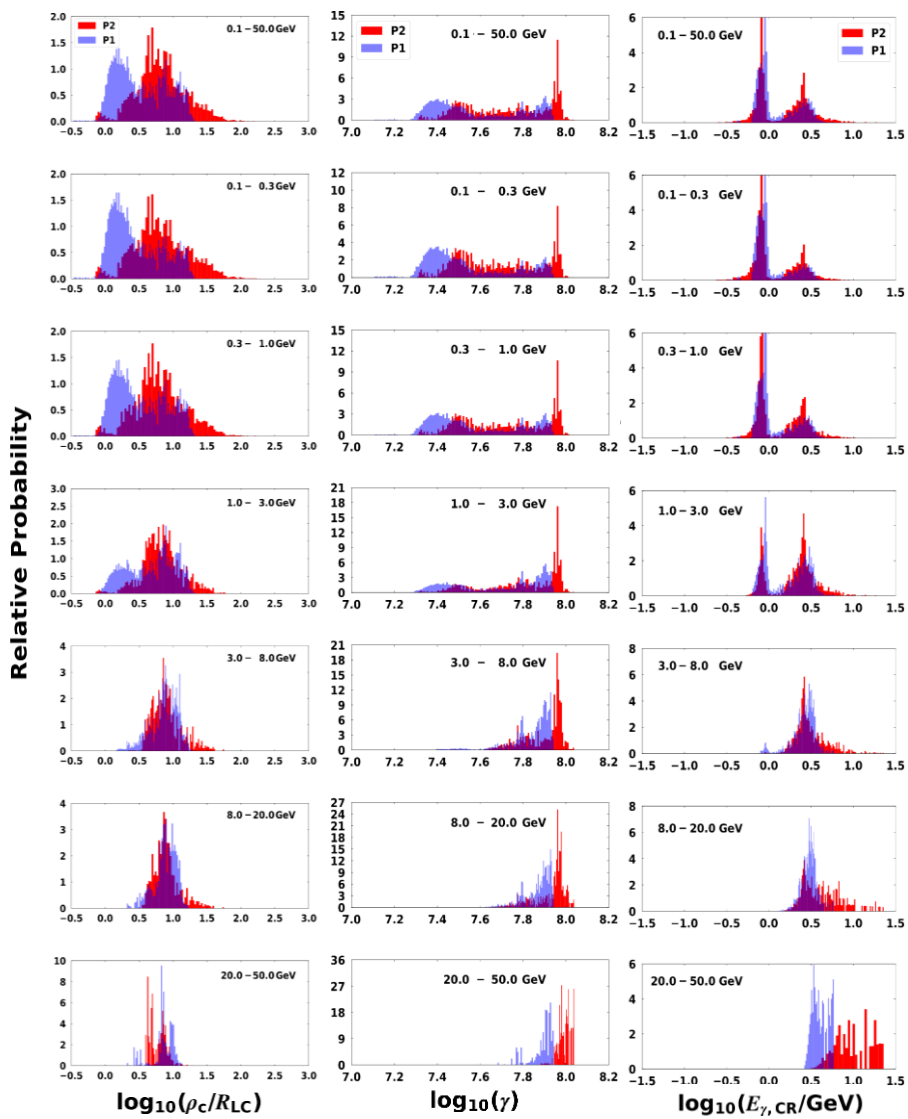
$\zeta_{\text{cut}} = 65^\circ$

$R_{\text{acc}} = 0.25 \text{ cm}^{-1}$

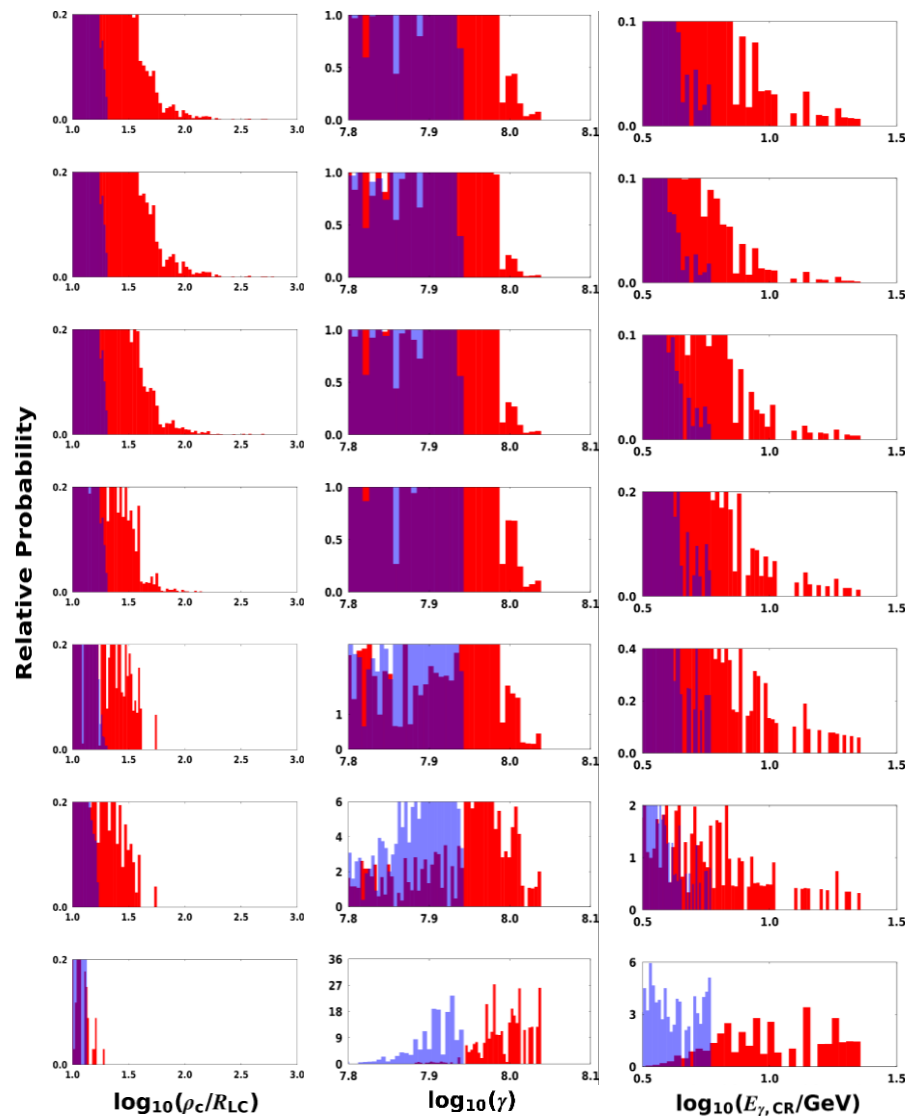
Barnard et al. (2022)

P1

P2



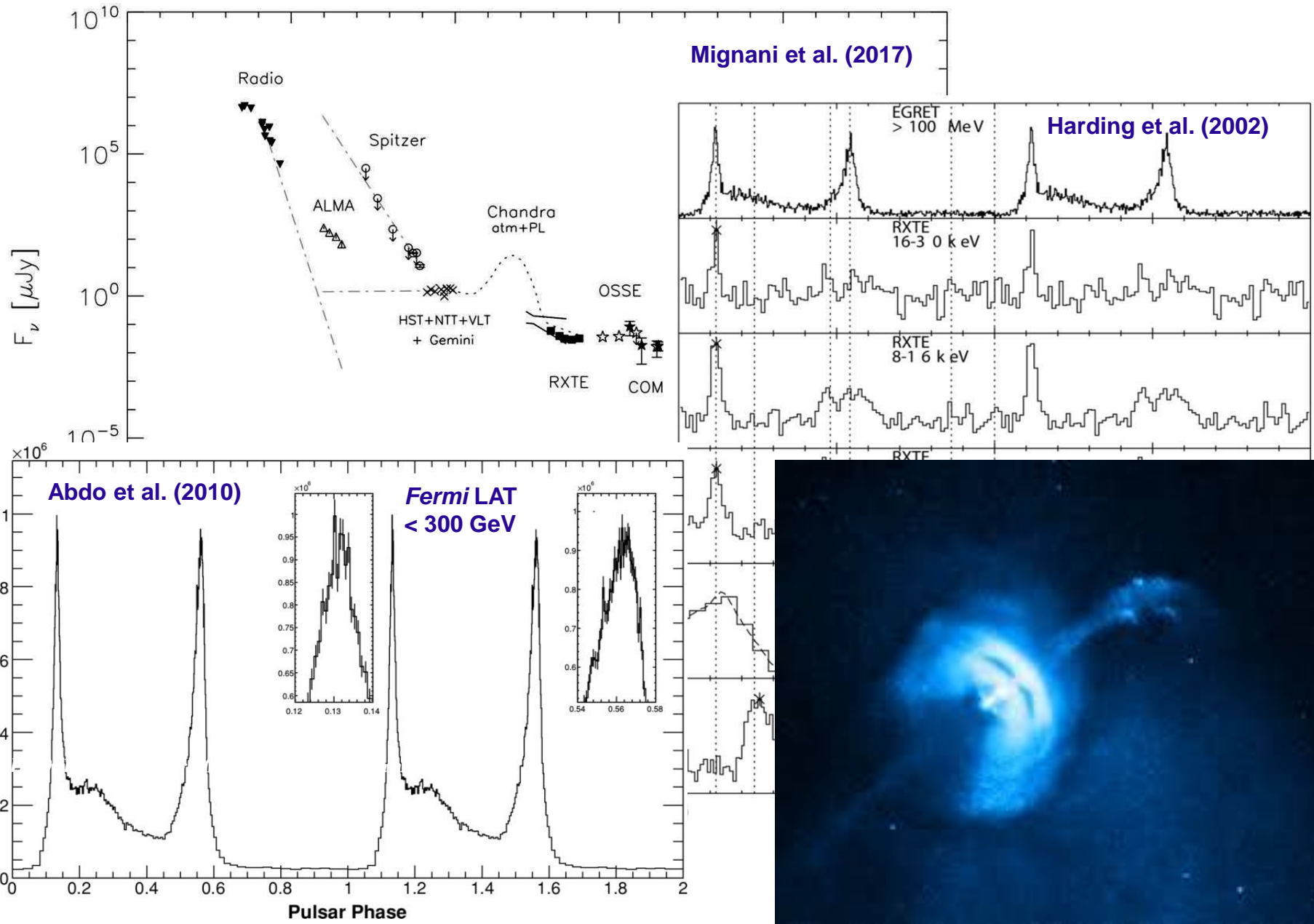
Tails of histograms on the left (same E's)



Spectral Modelling of the Broadband Emission from Pulsars

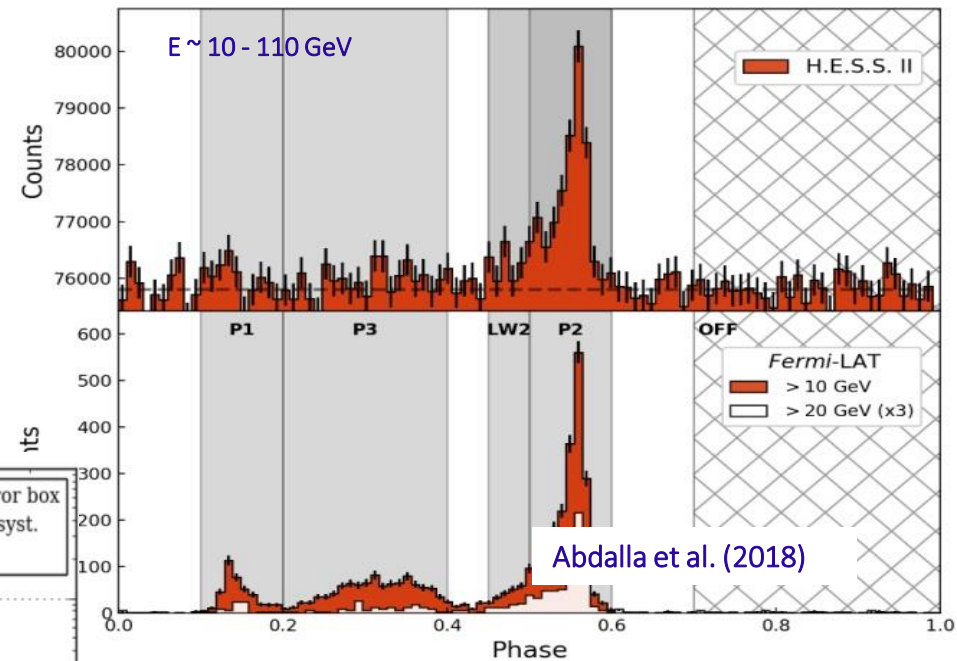
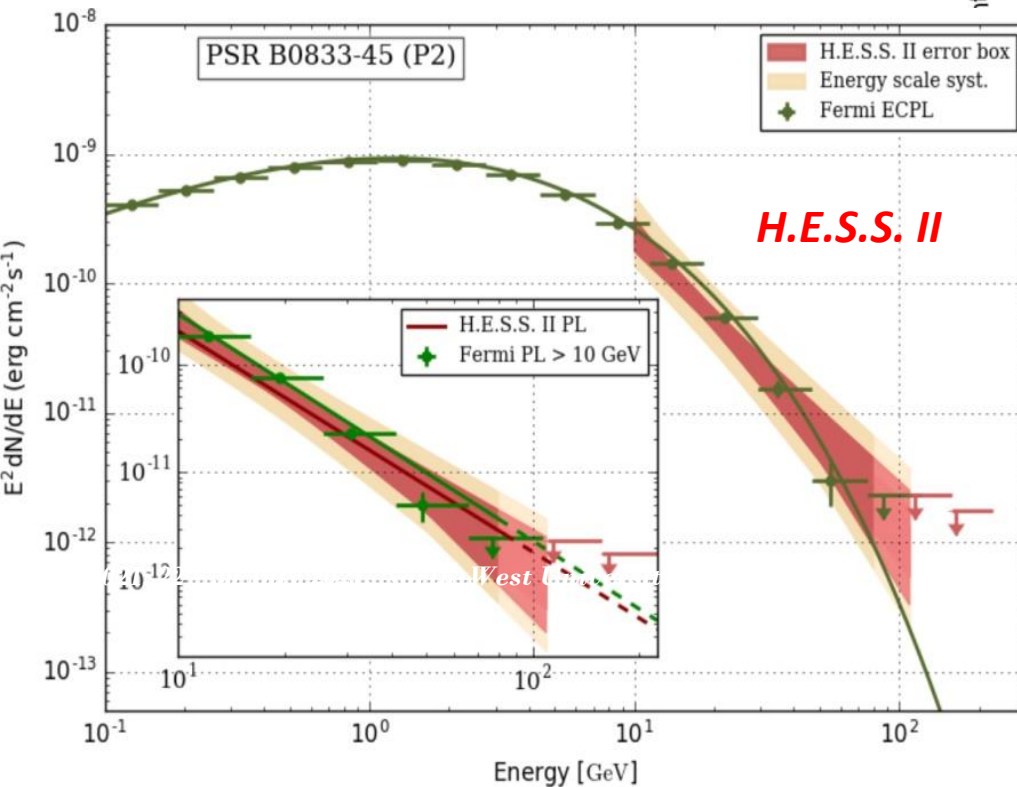


Energy-dependent LCs: Vela Pulsar



Pulsed TeV Emission from Vela PSR

- 3 – 7 TeV.
- Only P2 detected at 5.6σ level, P1 not visible.



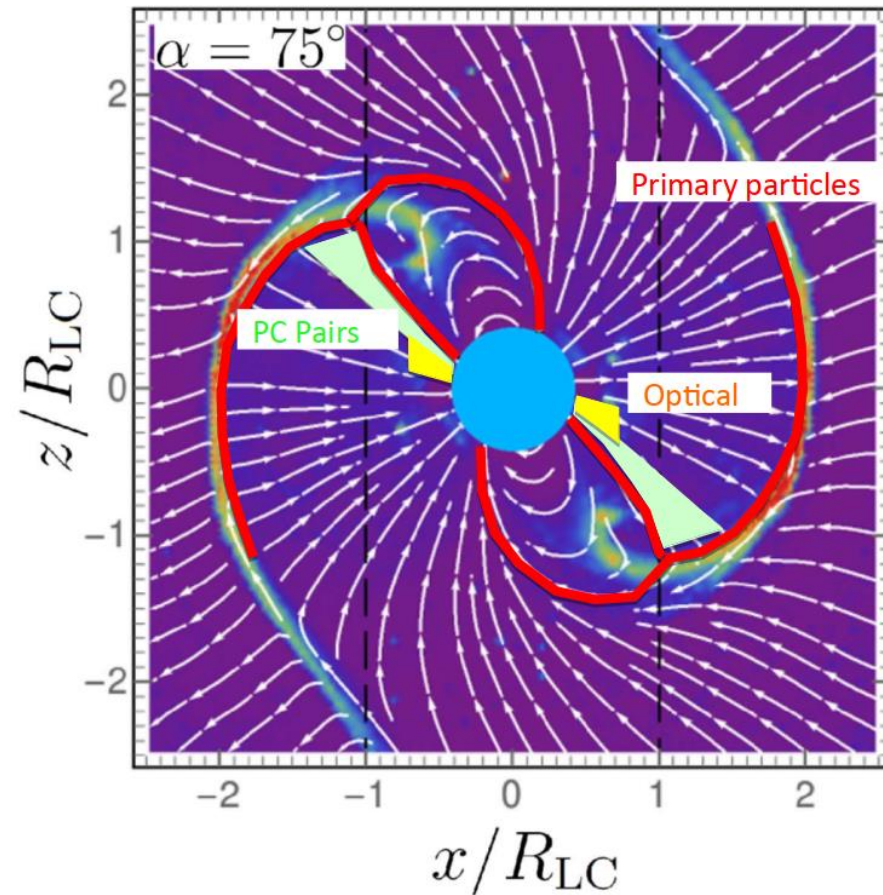
MOTIVATION:

Curved spectrum favoured by H.E.S.S. ($>3\sigma$).

CR tail or a different component?

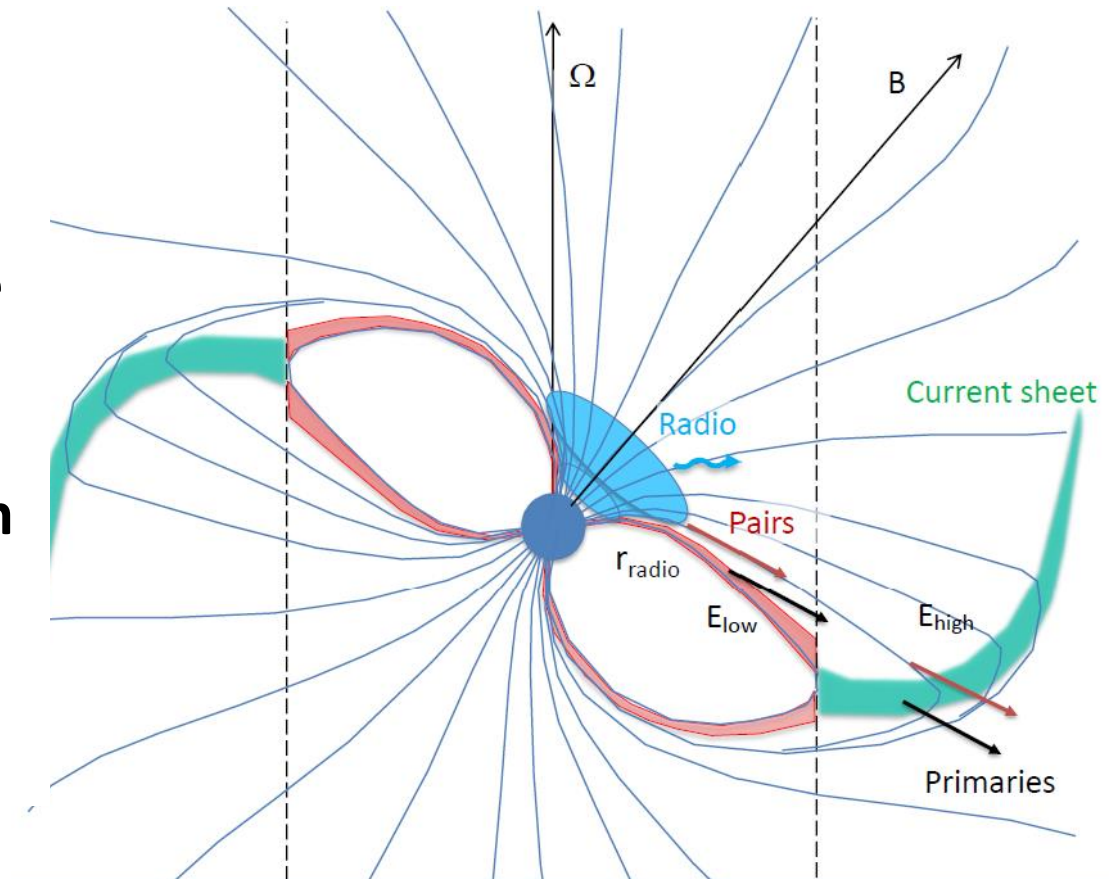
Separatrix / Current Sheet Emission Model

- Force-free magnetosphere
- Pairs and primaries from steady cascade in offset-PC field (Harding & Muslimov 2011a,b).
- Primaries accelerated only in extended SG and CS (out to $r = 2R_{LC}$) assuming a constant E -field.
- No pair acceleration. Chosen pair multiplicity.
- Empirical radio core / cone model.
- Resonant cyclotron absorption of radio photons (cf. Lyubarski & Petrova 1998).
- Solve particle dynamics.
- CR, SR, ICS, SSC radiation mechanisms.
- Inertial observer frame.



Separatrix / Current Sheet Emission Model

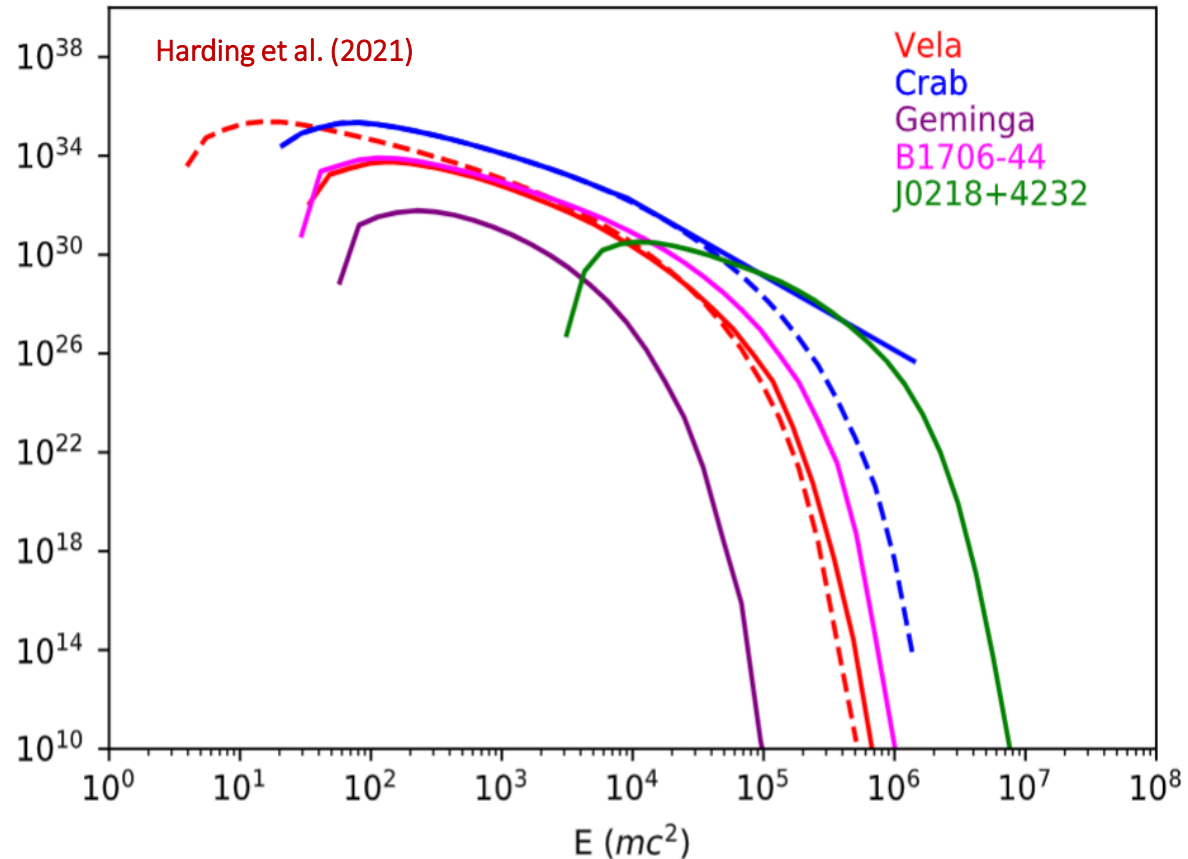
- Force-free $0.2 - 2 R_{LC}$
- Vacuum Retarded Dipole below $0.2 R_{LC}$
- Polar cap pairs produce SR in UV / optical at lower altitudes → eV
- Synchro-curvature from primaries → GeV
- Primaries scatter pair SR → TeV
- Pair SSC → MeV



Credit: A Harding

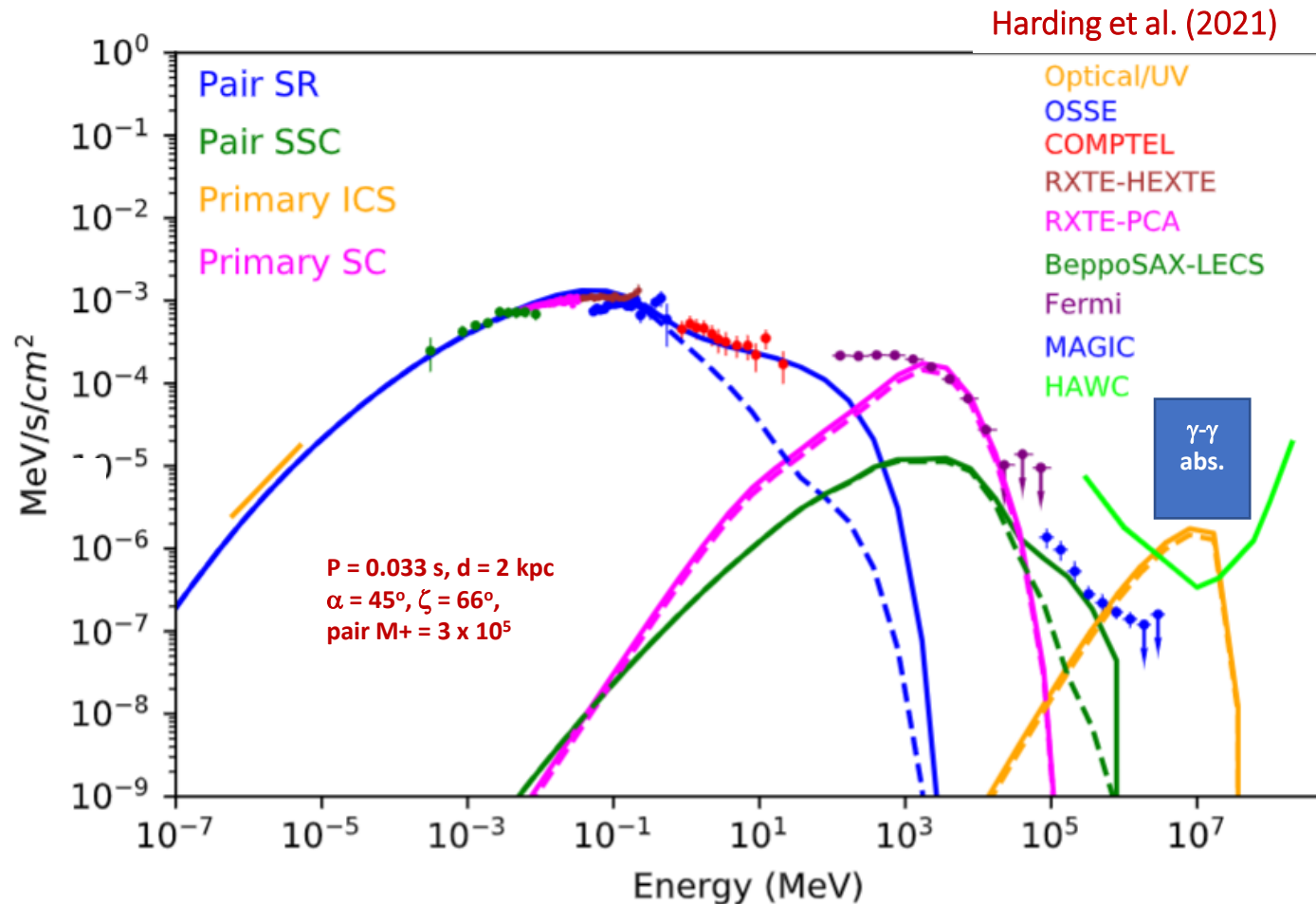
Polar Cap Pair Cascades

- First-principle calculation
- Primaries radiate gamma rays
- These are converted to electron-positron pairs in the strong B -field
- Sensitive to photon energy and B -field geometry
- Injected into magnetosphere: SR



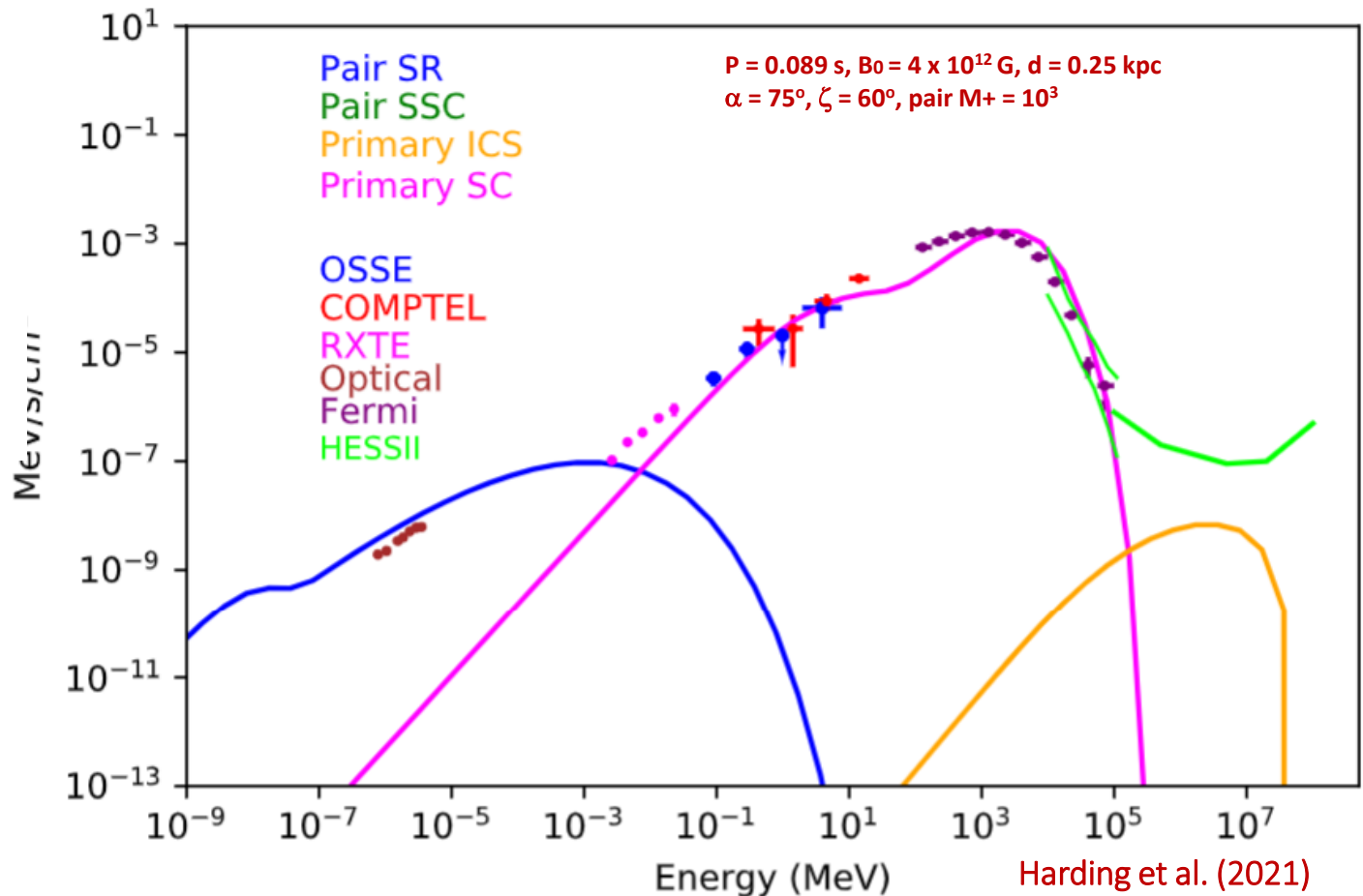
Results: Crab Spectrum

- Pair emission near current sheet
- >10 TeV component detectable by HAWC?
- Violation of MAGIC data?
- γ - γ absorption?
- MeV gap?



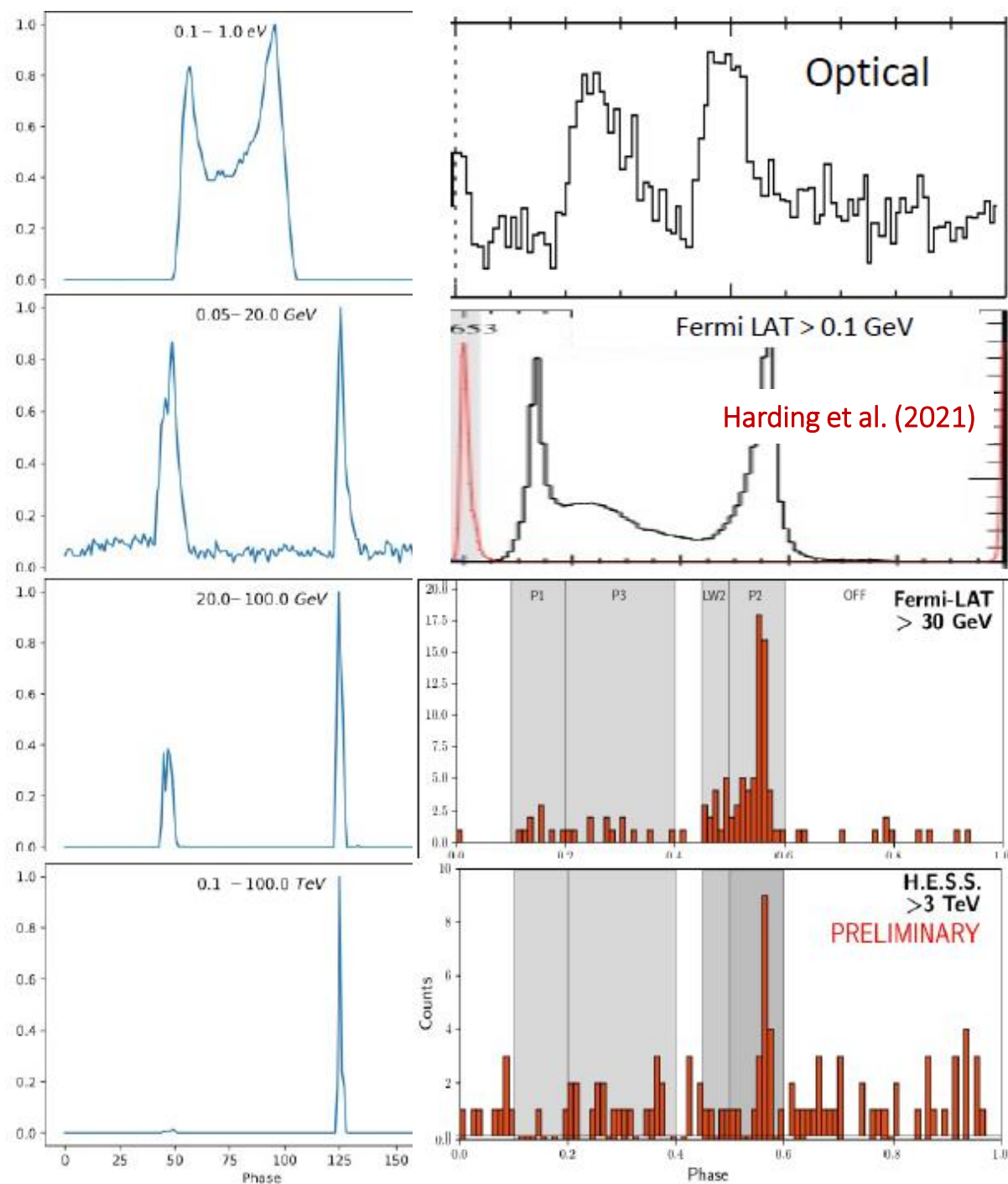
Results: Vela Spectrum

- Detectable primary IC component around 10 TeV!
- Pair SR matches optical data
- TeV emission requires high γ_{\max} , pointing to CR in GeV band



Results: Vela LCs

- Reasonable multi-wavelength LCs
- P1/P2 vs. E effect: higher-energy photons in P2 – larger ρ_c
- Only P2 in TeV: highest-energy particles responsible
- Azimuthally-dependent emissivity in current sheet may solve radio-to- γ lag

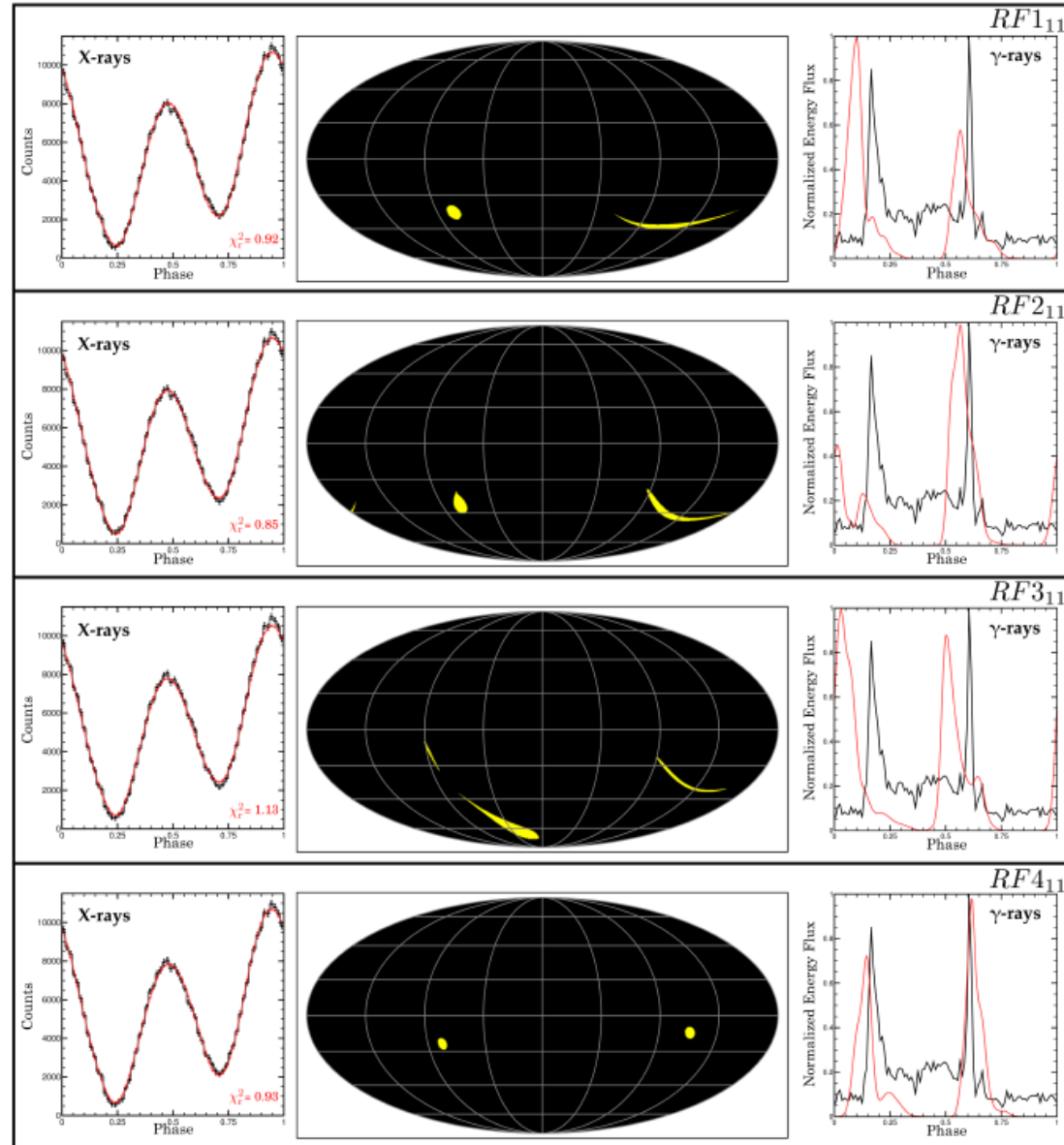


Multipolar *B*-Fields



Multipolar B -fields

- Miller et al. (2019) and Riley et al. (2019) reported strong evidence of multipolar B -fields via X-ray LC modelling
- Dual-band LC fitting (X-ray & g-ray) proved constraining for 11-parameter model that assumes offset-dipole and offset-quadrupole B -field components (Kalapotharakos et al. 2020)



Spider Binaries

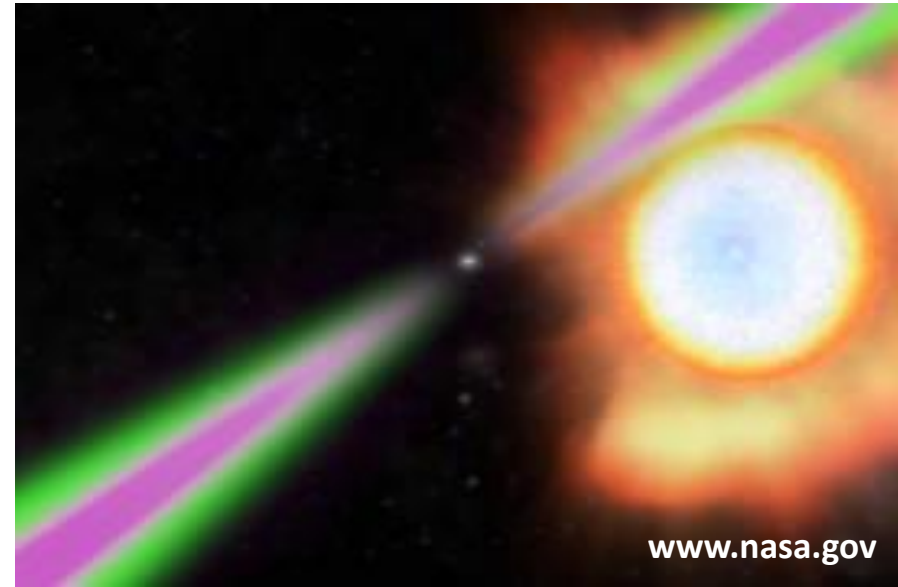


Spider Binaries

- Black widow (BW) & Redback (RB) spiders: devour male partners.
- Similar behaviour among **MSP** binary systems.
- **Tight binaries** $P_{\text{orb}} < 24$ h.
- Intense pulsar **wind heats** tidally-locked companion and excites companion wind / ablates it.
- **Flares** on companion star: variable heating. Hot 'day side'.
- Interaction of pulsar and companion winds forms an intra-binary **shock** – site for particle acceleration.
- BWs: smaller, lower-mass semi-degenerate companions ($< 0.05 M_{\text{sun}}$) than RBs ($\sim 0.1 - 0.5 M_{\text{sun}}$) cf. Roberts (2013).



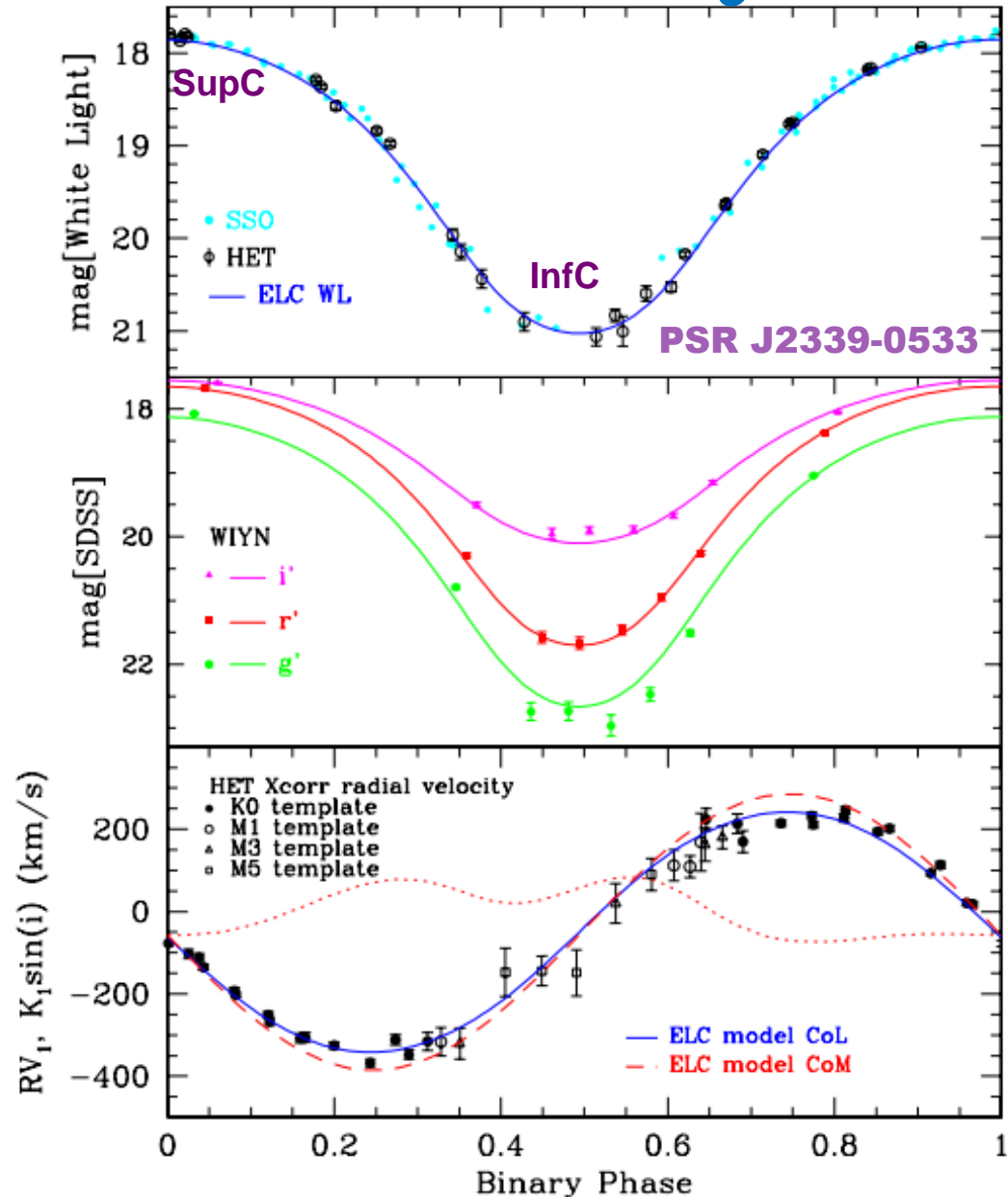
www.australiawidefirstaid.com.au



www.nasa.gov

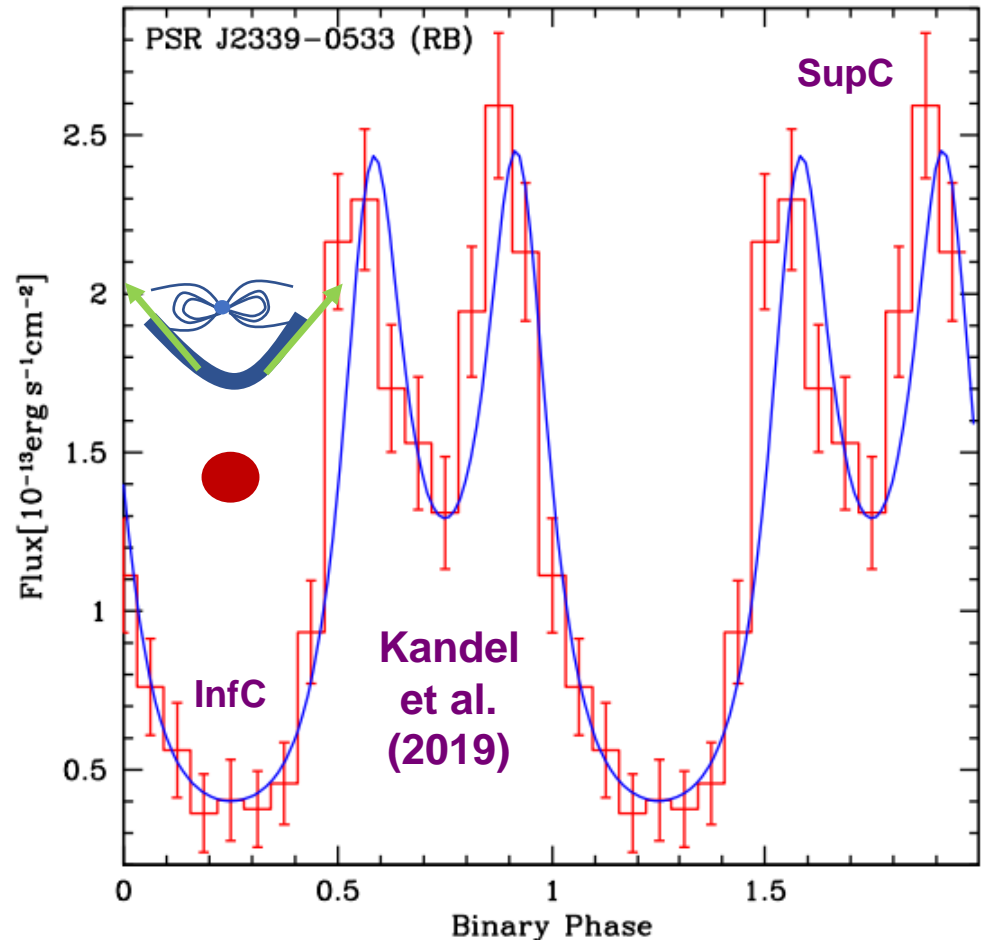
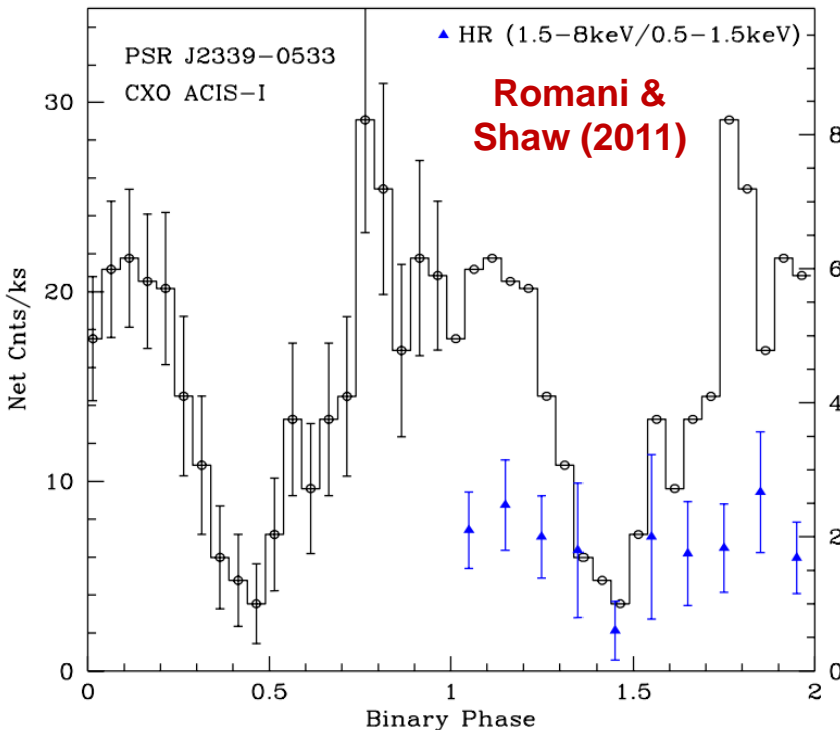
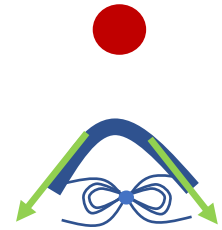
Optical Photometry

- Optical photometry on *Fermi* UnID source revealed orbital modulation
(Romani & Shaw 2011)
- Optical spectroscopy / radial velocity curve:
 $T_{\text{comp}} \sim 2\,800\text{ K} - 6\,900\text{ K}$
- Approximate binary parameters
- Need to constrain surface heating pattern



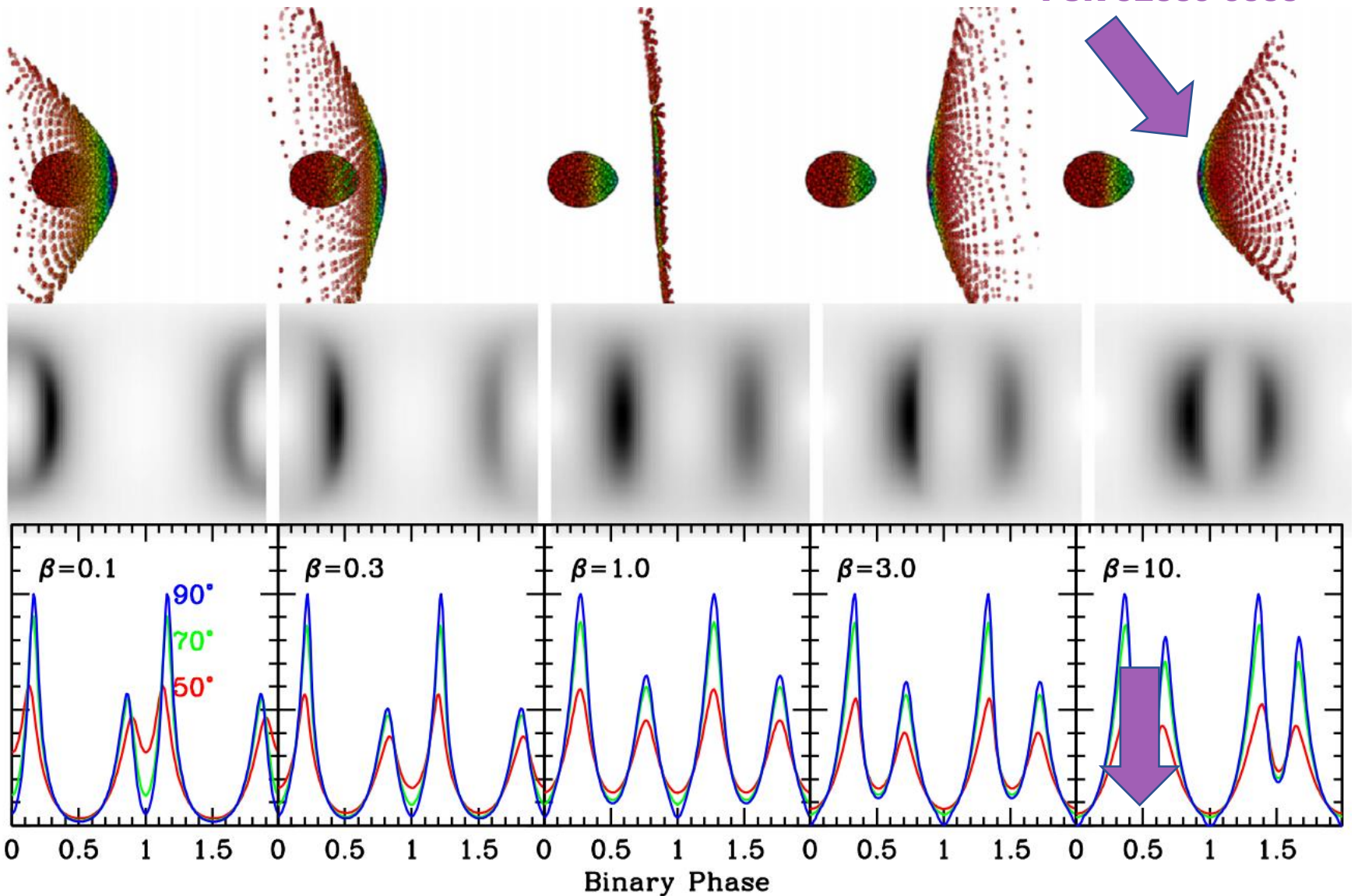
X-ray Modulation

- Archival *CXO* data
- $F(0.5-8 \text{ keV}) = (2.3^{+1.2}_{-0.3}) \times 10^{-13} \text{ erg/cm}^2/\text{s}$
- $G_{\text{PL}} = 1.09^{+0.40}_{-0.13}$
- Hardness ratio a minimum at companion inferior conjunction (eclipsing pulsar)



Intra-binary Shock

PSR J2339-0533



Particle Transport

$$\frac{\partial N_e}{\partial t} = -\vec{V} \cdot (\vec{\nabla} N_e) + \kappa(E_e) \nabla^2 N_e + \frac{\partial}{\partial E_e} (\dot{E}_{e,\text{tot}} N_e) - (\vec{\nabla} \cdot \vec{V}) N_e + Q$$

Solid Angle & Diffusion:

Van der Merwe et al. (2020)

$$Q_{\text{PSR}}(E_e) = Q_0 E_e^{-\Gamma} \exp\left(-\frac{E_e}{E_{\text{cut}}}\right)$$

$$Q_1 = \left(\frac{1}{4\pi} \int_0^{2\pi} \int_{\lambda_1}^{\lambda_2} \sin \lambda \, d\lambda \, d\phi \right) Q_{\text{PSR}} = \frac{1}{2} (\cos \lambda_1 - \cos \lambda_2) Q_{\text{PSR}}$$

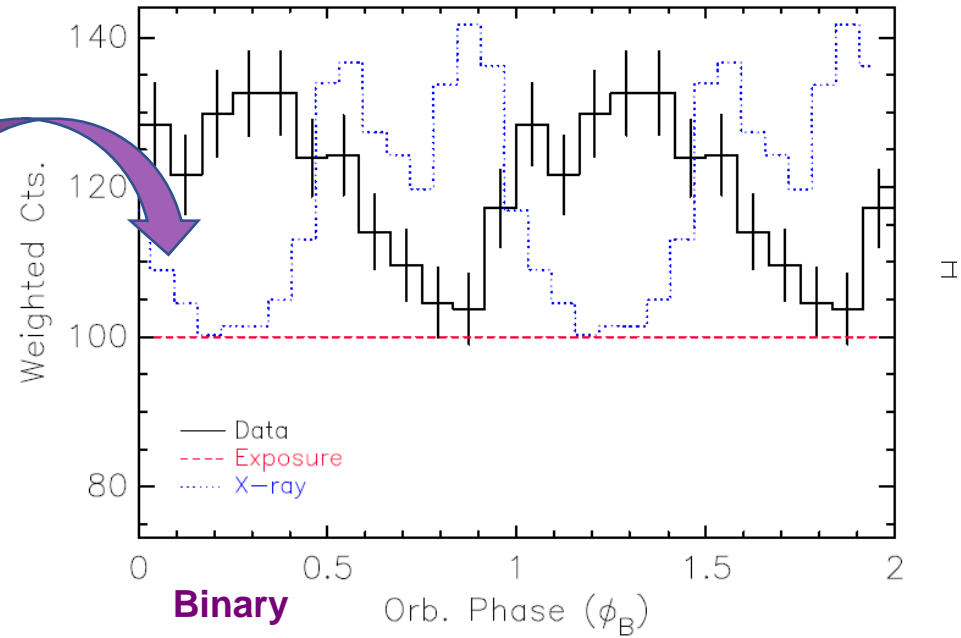
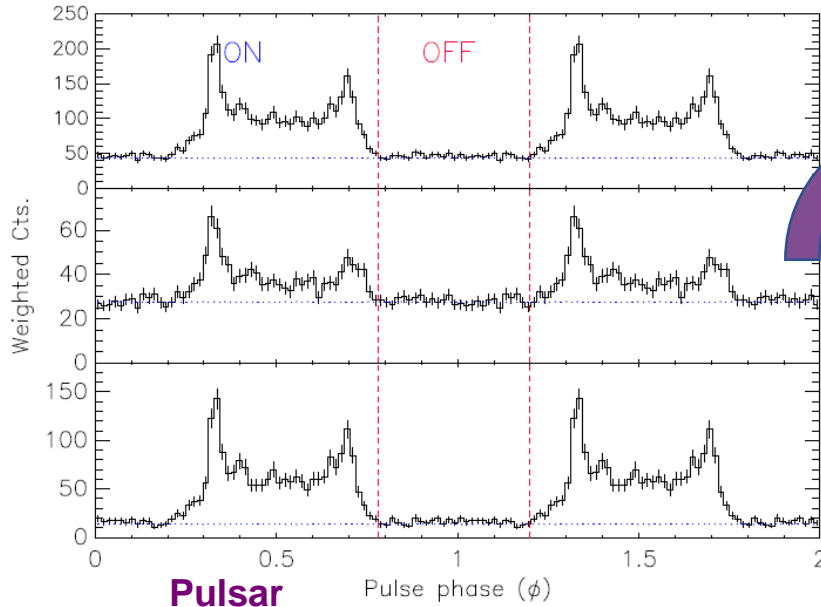
$$Q_i = \frac{1}{t_{\text{diff}}} \frac{dN_{e,i-1}}{dE_e} + \frac{1}{2} (\cos \lambda_i - \cos \lambda_{i+1}) Q_{\text{PSR}}, \quad i > 1$$

Normalisation - Current and Energetics:

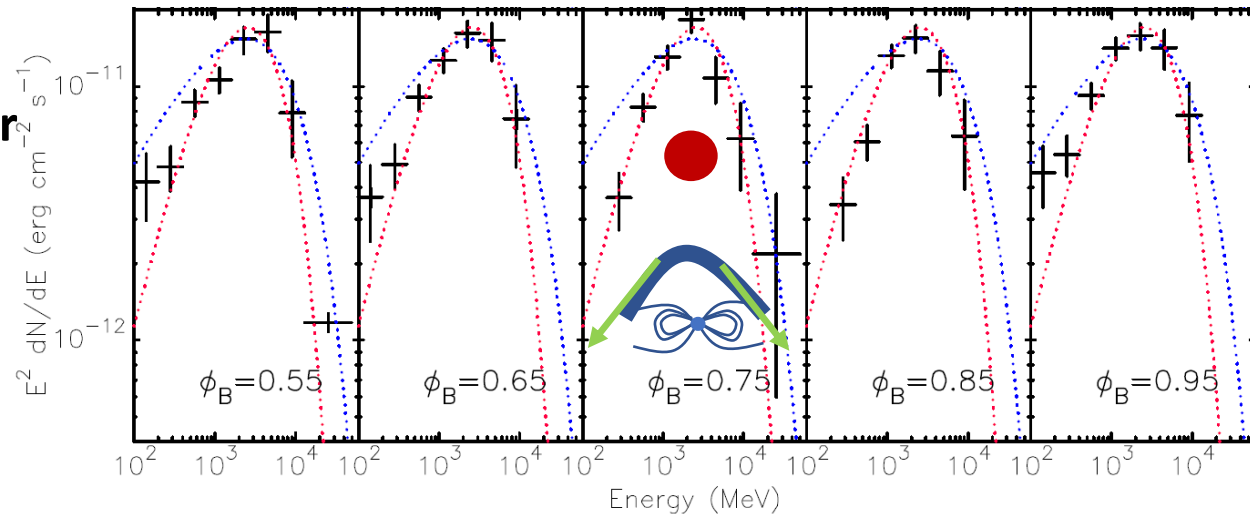
$$\dot{N}_{\text{GJ}} = \frac{B_{\text{PSR}} 4\pi^2 R_{\text{PSR}}^3}{2ceP^2} \quad \dot{N}_{\text{II}} = M_{\pm} \dot{N}_{\text{GJ}}$$

$$\int_{E_{\text{min}}}^{\infty} Q_{\text{PSR}} dE_e = (M_{\pm} + 1) \dot{N}_{\text{GJ}} \quad \int_{E_{\text{min}}}^{\infty} E_e Q_{\text{PSR}} dE_e = \eta_p \dot{E}_{\text{rot}}$$

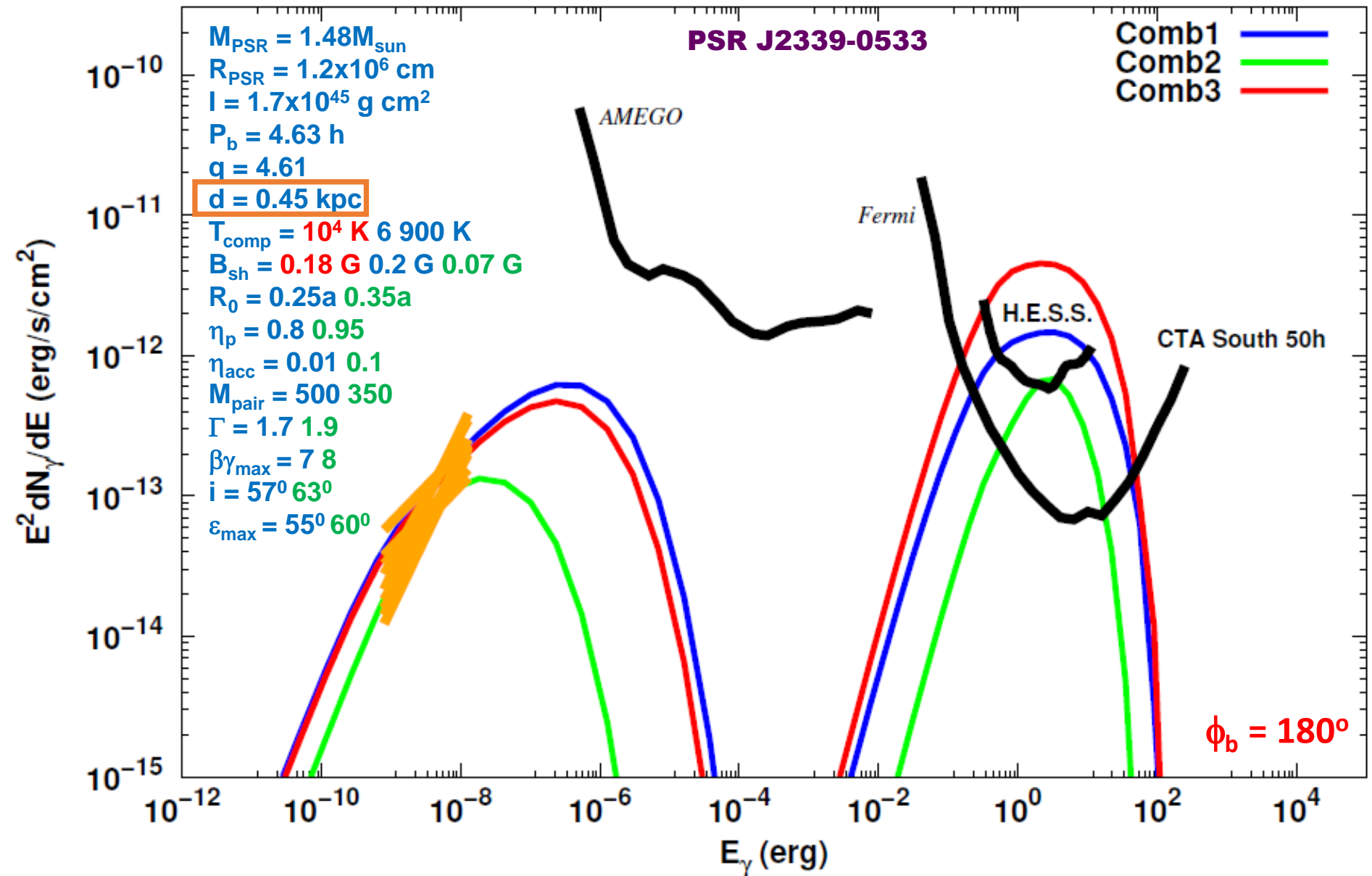
subGeV Modulation



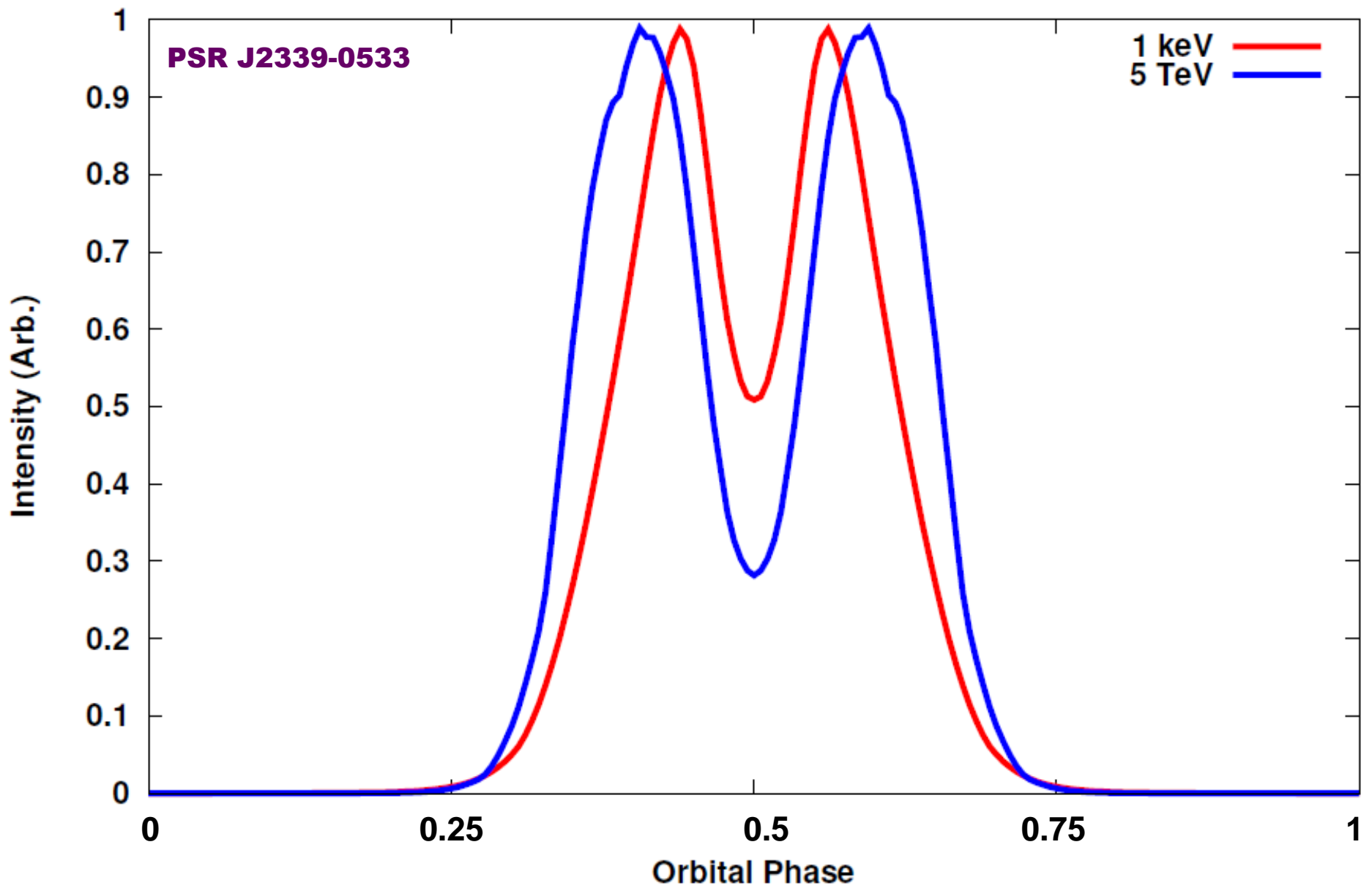
- 100 – 600 MeV orbital modulation
- Peaks near pulsar superior conjunction
- Detected in on-pulse interval: variation in pulsed 2.9 ms signal itself (An & Romani 2020)



Spectral Modelling



Orbital Light Curve Modelling



Pulsar Wind Nebulae



PWN Background

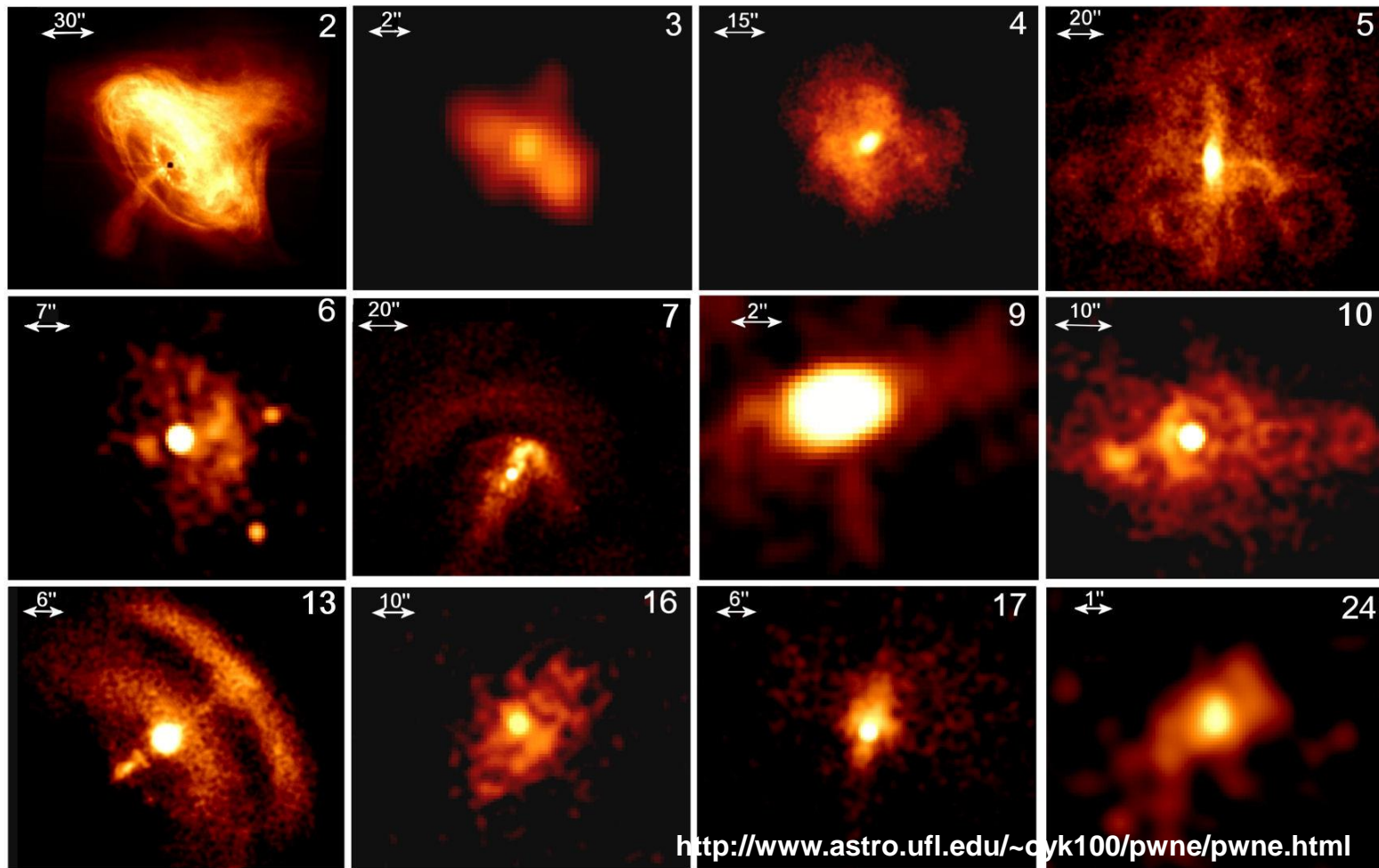
- **Supernova explosion: remnant neutron star**
- **Rotation-powered / magnetic-powered pulsar (PWN or MWN)**
- **Radio: SR shell for SNR and flat-spectrum central PWN**
- **Composite SNRs (plerions)**
- **Dissipate rotational energy via relativistic wind of positrons and electrons**
- **May encounter inward reverse shock of SNR**



Spatial Dependence of PWNe

- Torus + jets
- Change in properties with central distance

X-ray band (*Chandra* images)



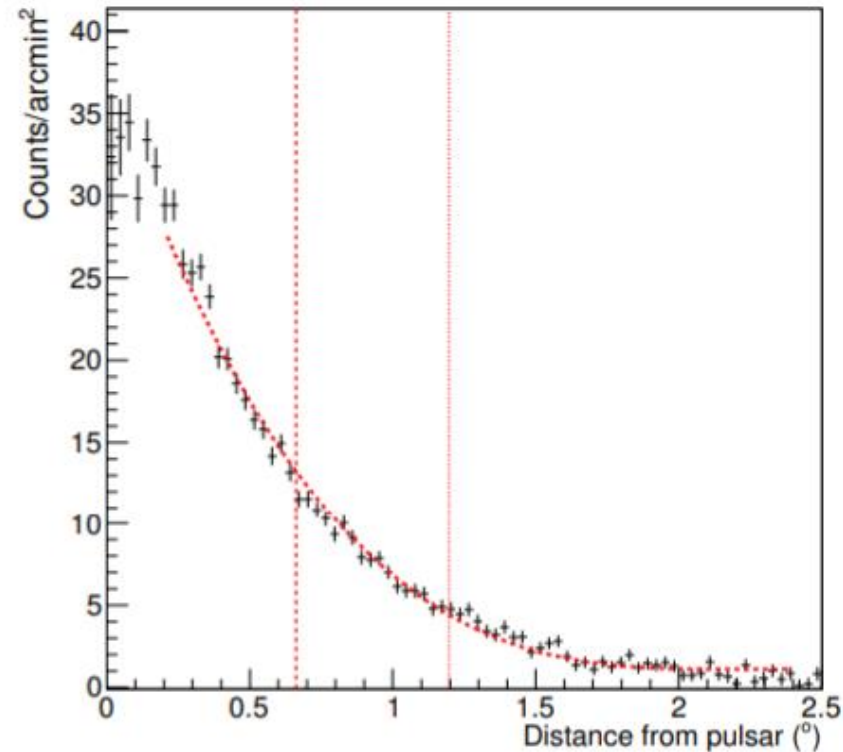
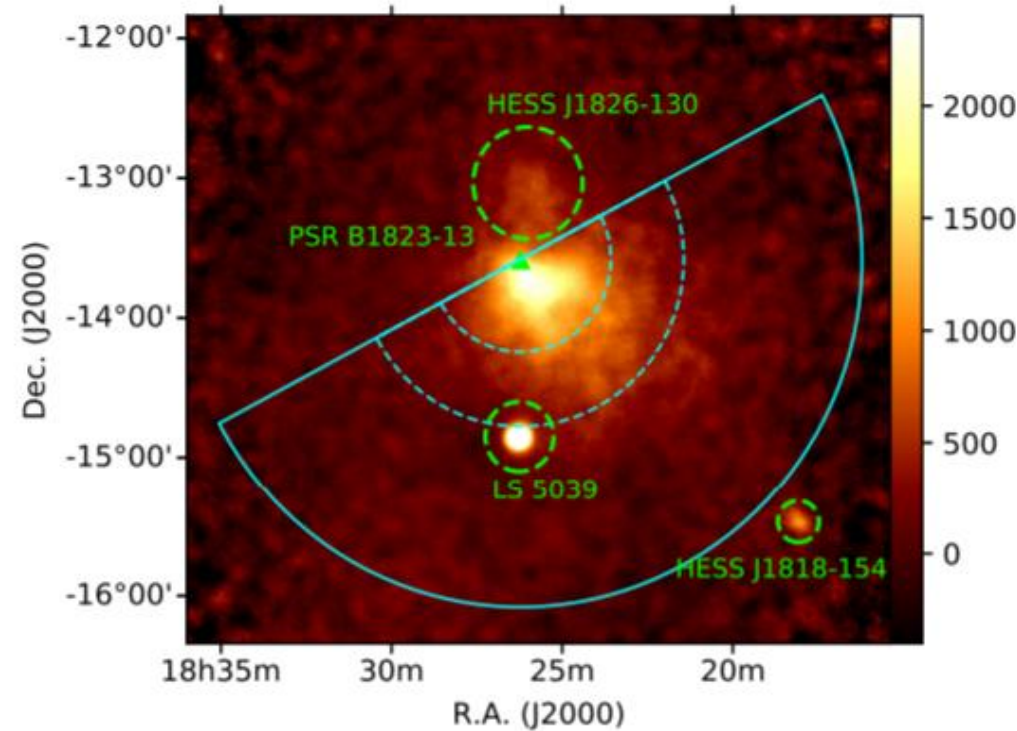
Spatial Dependence of PWNe

- TeV radial profile

$$y = \begin{cases} a(x - r_0)^n + c & (x < r_0) \\ c & (x \geq r_0) \end{cases}$$

Abdalla
et al. (2018)

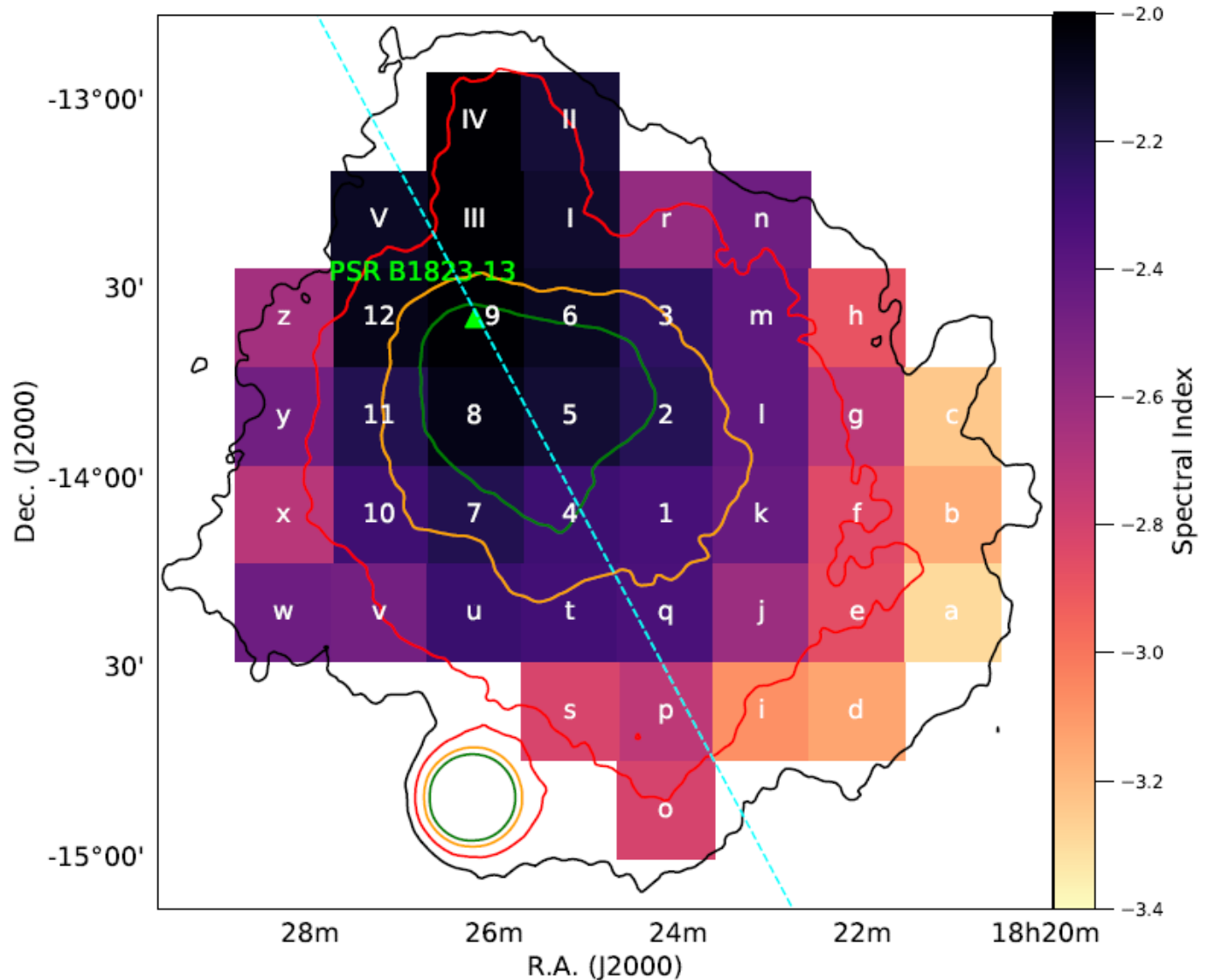
HESS J1825-137



Spatial Dependence of PWNe

- Spectral steepening with distance
- First direct evidence of electron cooling (at the time cir. 2006)

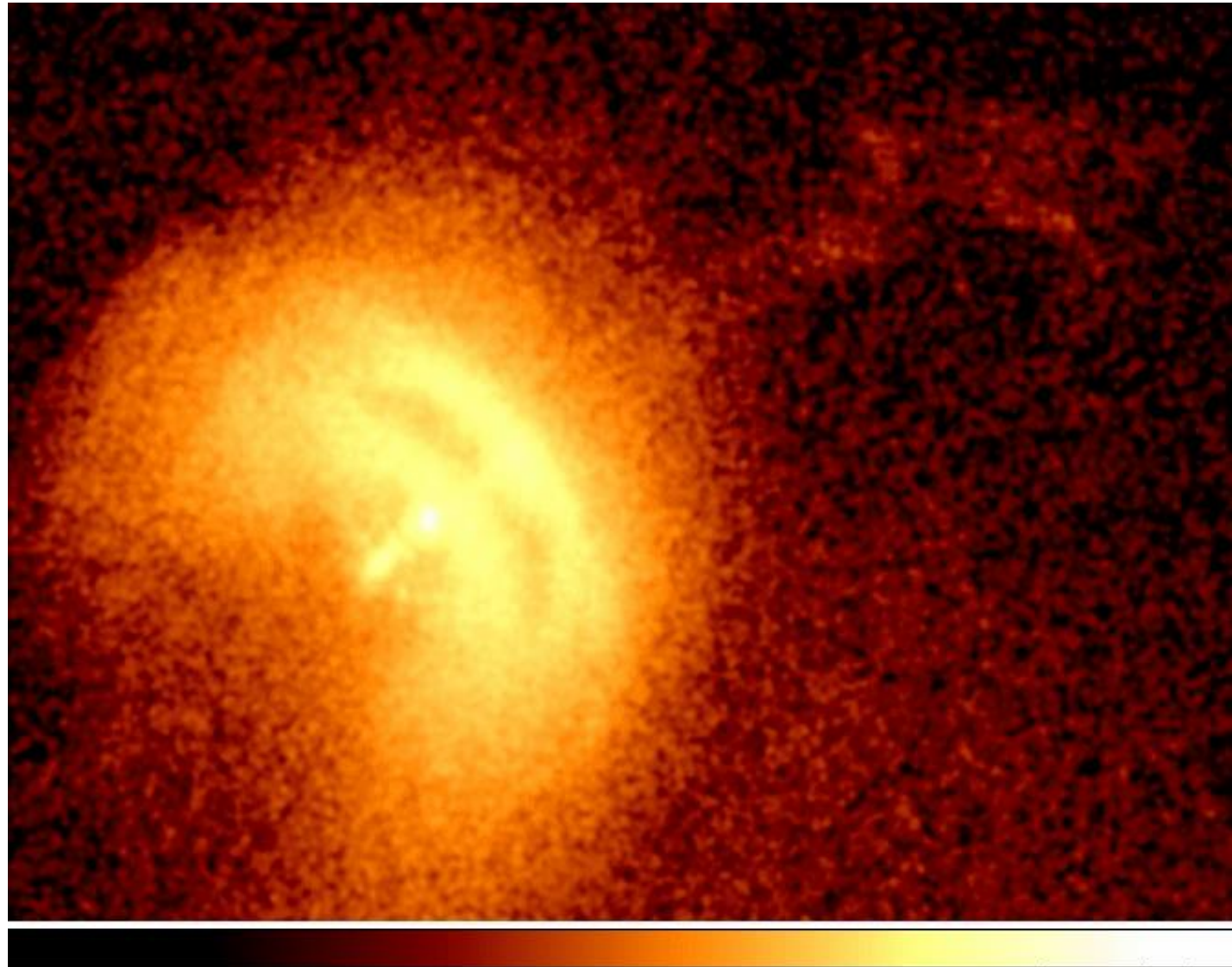
Abdalla
et al. (2018)



Temporal Dependence of PWNe

- Spin-down
- Also variability on shorter timescales
- E.g., Vela PWN

www.astro.ufl.edu/~oyk100/pwne/pwne.html



Kes 75 Background

- One of the youngest composite supernova remnants (~700 yr).
- Contains the pulsar wind nebula (PWN) of young glitching PSR J1846–0258.
- Youngest pulsar in Galaxy (360 – 530 yr)

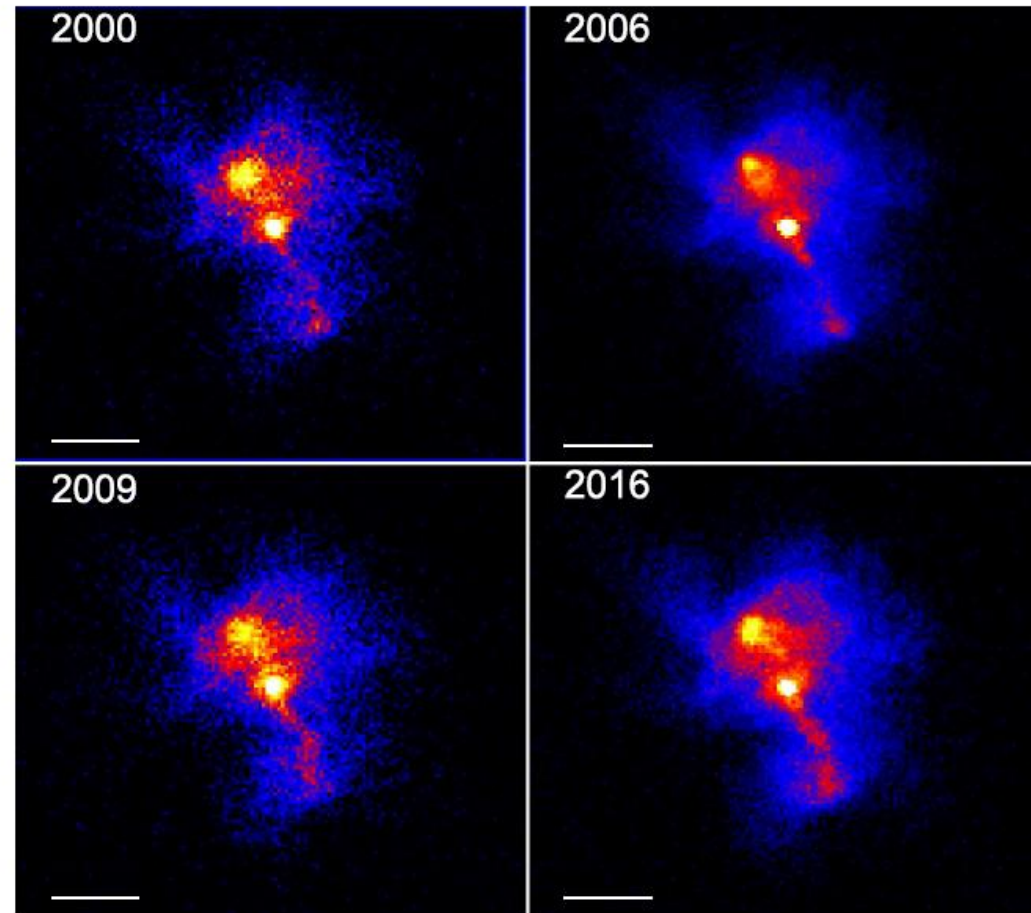


Credit: X-ray: NASA/CXC/NCSU/S. Reynolds; Optical: PanSTARRS

Recent Observations

- **Chandra:** rapid PWN expansion ($\sim 0.2\%$ in yr) = 1 million m/s!
- PWN expanding into a relatively low-density environment.
- $\sim 10\%$ flux decrease in 7 years
- Absence shell emission to the east: very strong density gradient of surrounding medium

Reynolds et al. (2018)



Transport Equation (I)

$$\frac{\partial N_e}{\partial t} = -\mathbf{V} \cdot (\nabla N_e) + \kappa \nabla^2 N_e + \frac{1}{3} (\nabla \cdot \mathbf{V}) \left(\left[\frac{\partial N_e}{\partial \ln E} \right] - 2N_e \right) + \frac{\partial}{\partial E} (\dot{E}_{\text{rad}} N_e) + Q(\mathbf{r}, E, t)$$

Van Rensburg et al. (2018)

Injection spectrum

$$Q(E_e, t) = \begin{cases} Q_0(t) \left(\frac{E_e}{E_b} \right)^{\alpha_1} & E_e < E_b \\ Q_0(t) \left(\frac{E_e}{E_b} \right)^{\alpha_2} & E_e \geq E_b. \end{cases}$$

Venter & de Jager (2007)

Time-dependent normalization:

$$\epsilon L(t) = \int_{E_{\min}}^{E_b} Q E_e dE_e + \int_{E_b}^{E_{\max}} Q E_e dE_e$$

$$L(t) = L_0 \left(1 + \frac{t}{\tau_c} \right)^{-(n+1)/(n-1)}$$

Pacini & Salvati (1973)

Transport Equation (II)

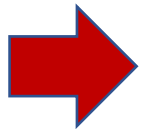
- ❑ SR & IC radiative losses
- ❑ Adiabatic losses
- ❑ Convection
- ❑ Diffusion
- ❑ Limiting energy

$$V(r) = V_0 \left(\frac{r}{r_0} \right)^{\alpha_V}$$

$$\kappa = \kappa_0 \left(\frac{E}{E'_0} \right)^q$$

$$B(r, t) = B_{\text{age}} \left(\frac{r}{r_0} \right)^{\alpha_B} \left(\frac{t}{t_{\text{age}}} \right)^{\beta_B}$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{V} \times \mathbf{B})$$

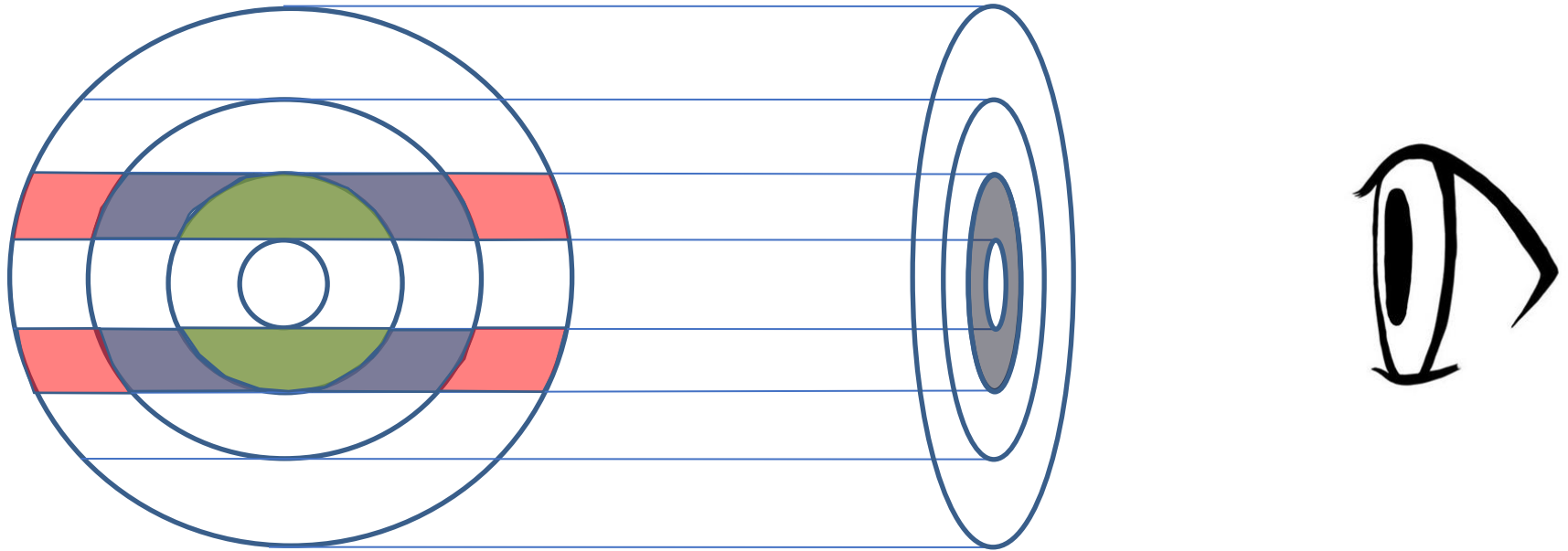


$$\alpha_V + \alpha_B = -1$$

$$E_{\text{max}} = \frac{e}{2} \sqrt{\frac{L(t)\sigma}{c(1+\sigma)}}$$

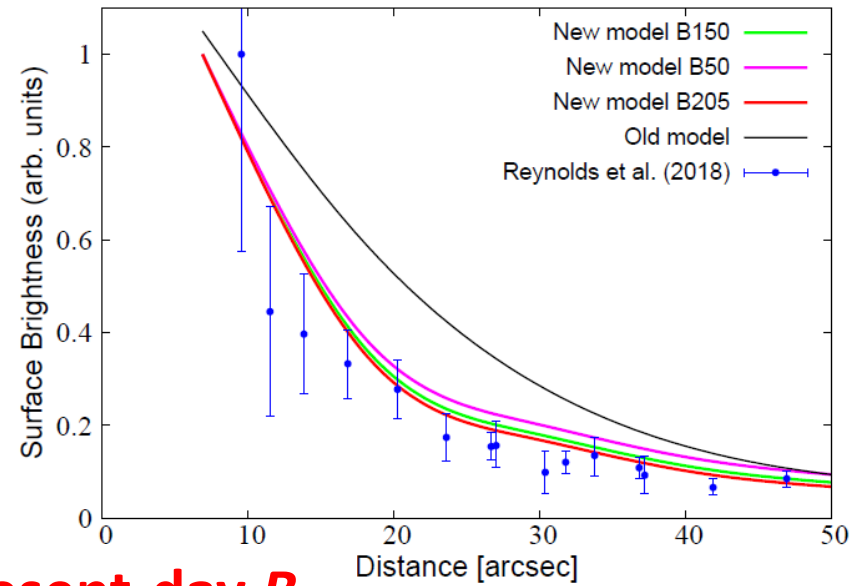
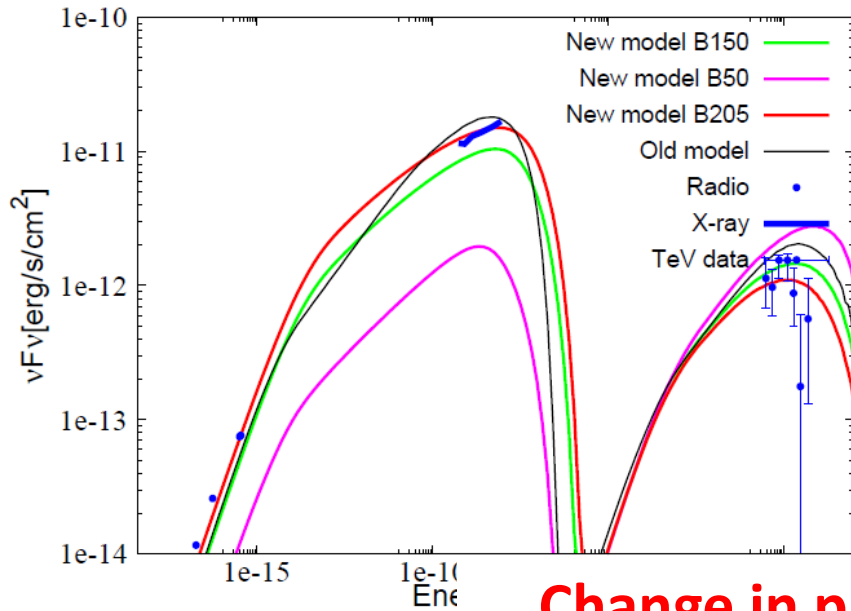
Kennel & Coroniti (1984a)

Line-of-Sight (LOS) Calculation

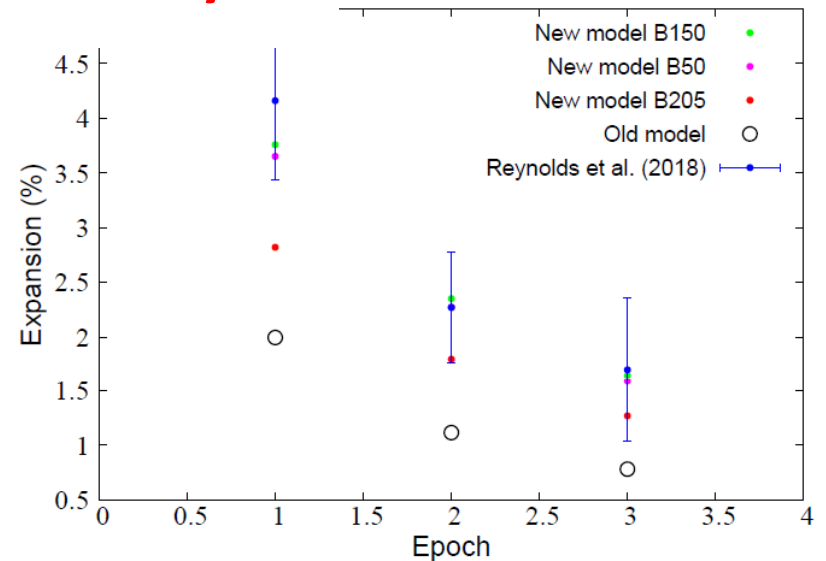
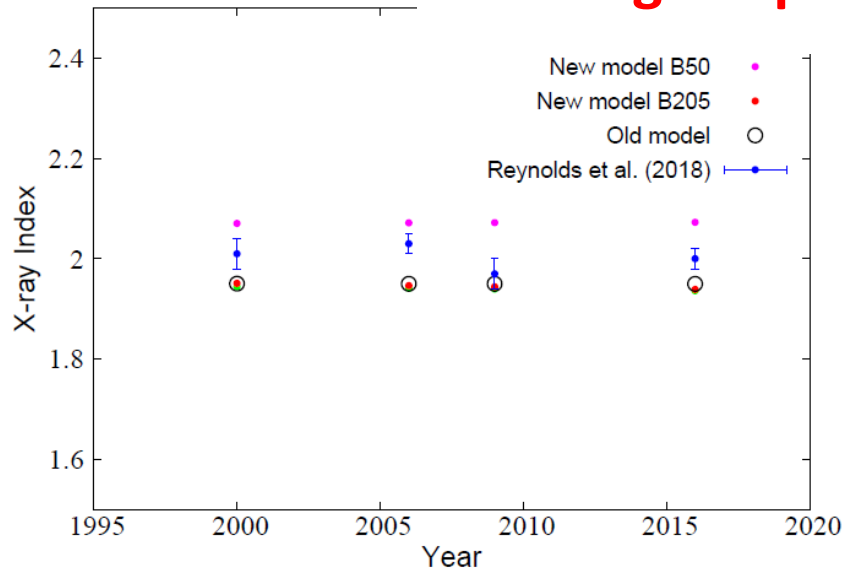


Credit: C van Rensburg

Fitting Results



Change in present-day *B*

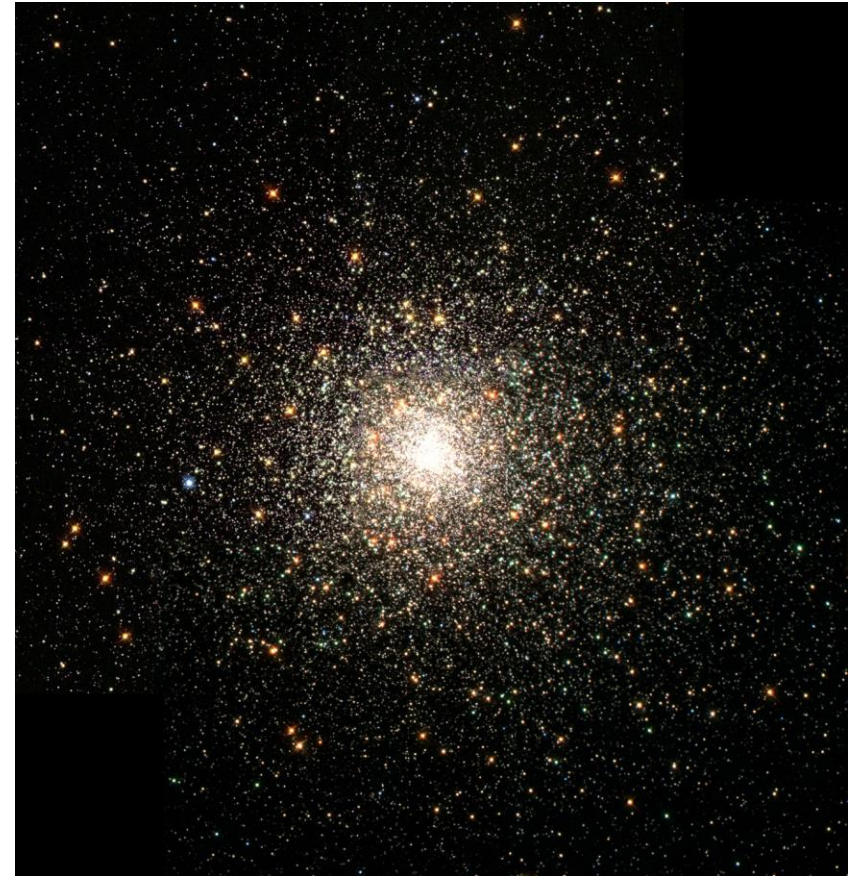
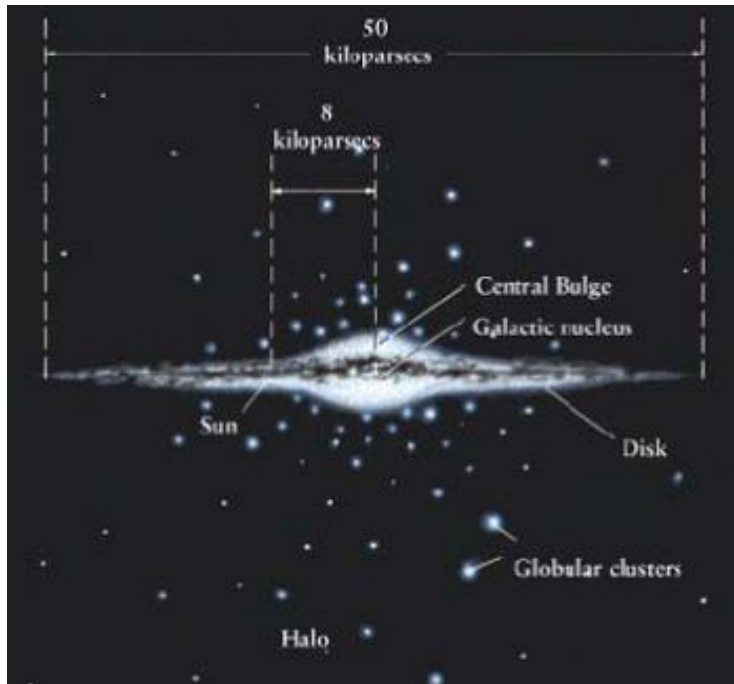


Pulsars in Globular Clusters



Globular Clusters (GCs)

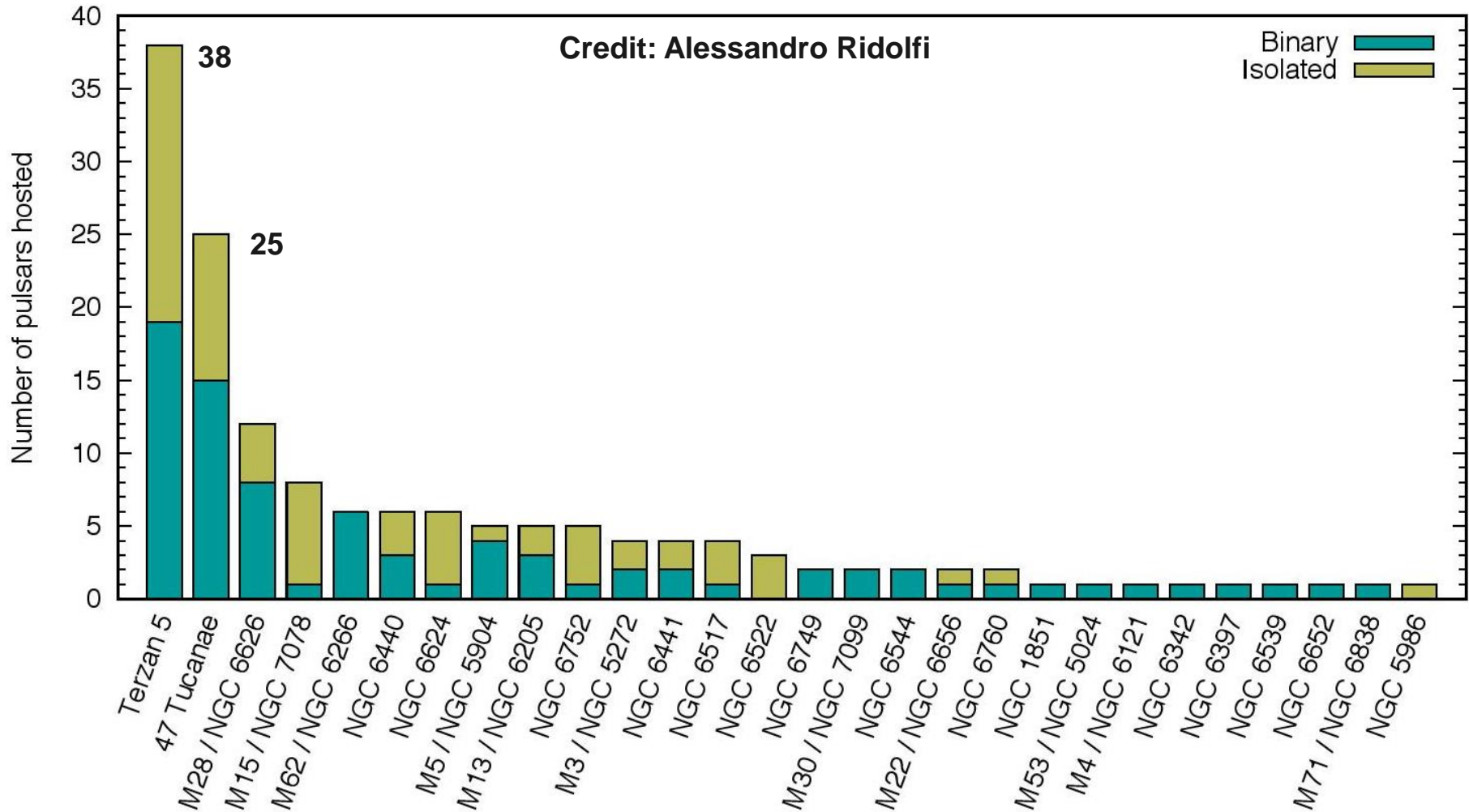
- ~160 Galactic clusters (Harris 1996, 2010)
- $10^4 - 10^6$ stars
- Spherical distribution about Galactic Centre with $\langle d \rangle \sim 12$ kpc



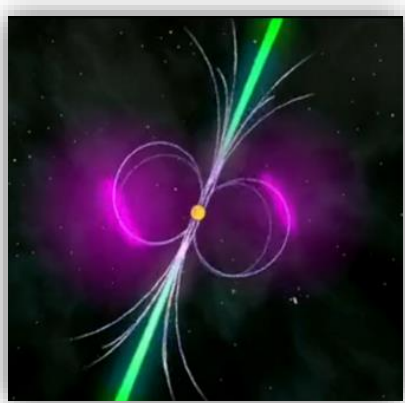
- Exotic stellar members (BHs, MSPs, WDs, CVs, etc.)
- Multi-wavelength objects

Millisecond Pulsars in GCs

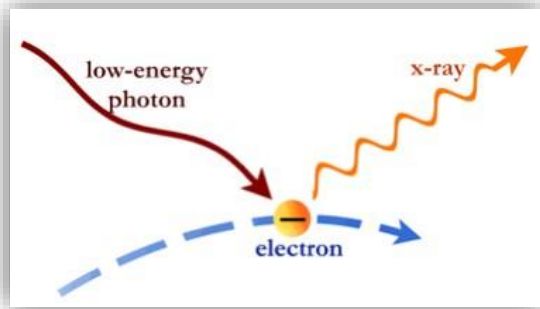
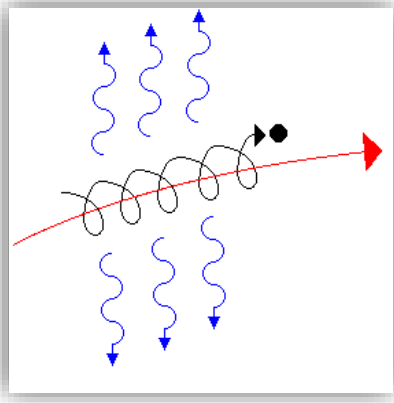
150 radio MSPs in 28 GCs*



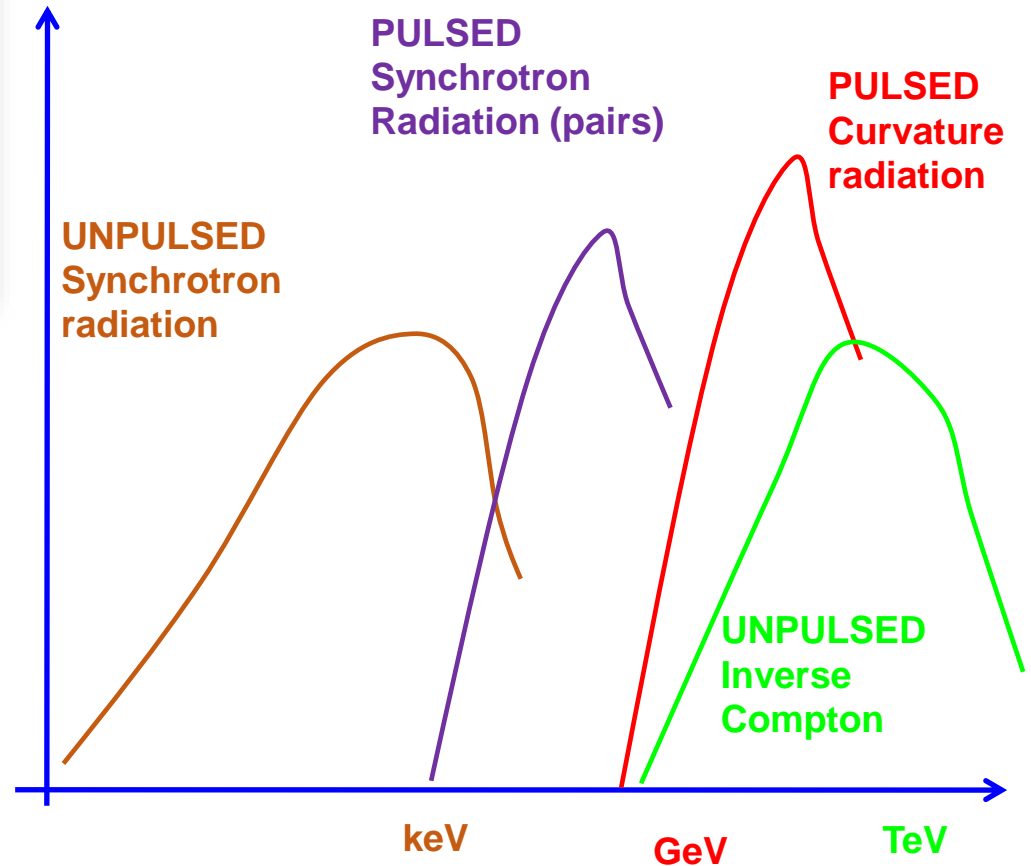
Spectral Components Expected from GC MSPs



<http://i.space.com/images/i/000/013/110/i02/nasa-fermi-pulsar-J1823-2021a.jpg?1320348068>



<http://www.astro.wisc.edu/~bank/img/inversecompton.jpg>



SED & Parameter Constraints

Cluster parameters:

$$R_c, R_h, R_t \propto d$$

$$F_g \propto d^2$$

$$u(r) \propto N_* R^2 T^4 \int_0^{R_t} \rho(R_c, R_h, R_t)$$

Kopp et al. (2013)

Ndiyavala-Davids et al. (2021)

CR/SR parameters:

$$E_{||}, N_{MSP}, \text{gap width}, M_+$$

Injection spectrum:

$$E_{min}, E_{max}, \Gamma, N_{MSP}$$

$$\propto N_{MSP} \eta_p \langle \dot{E} \rangle$$

Diffusion parameters:

$$\kappa = \kappa_0 E^\delta$$

SR parameters:

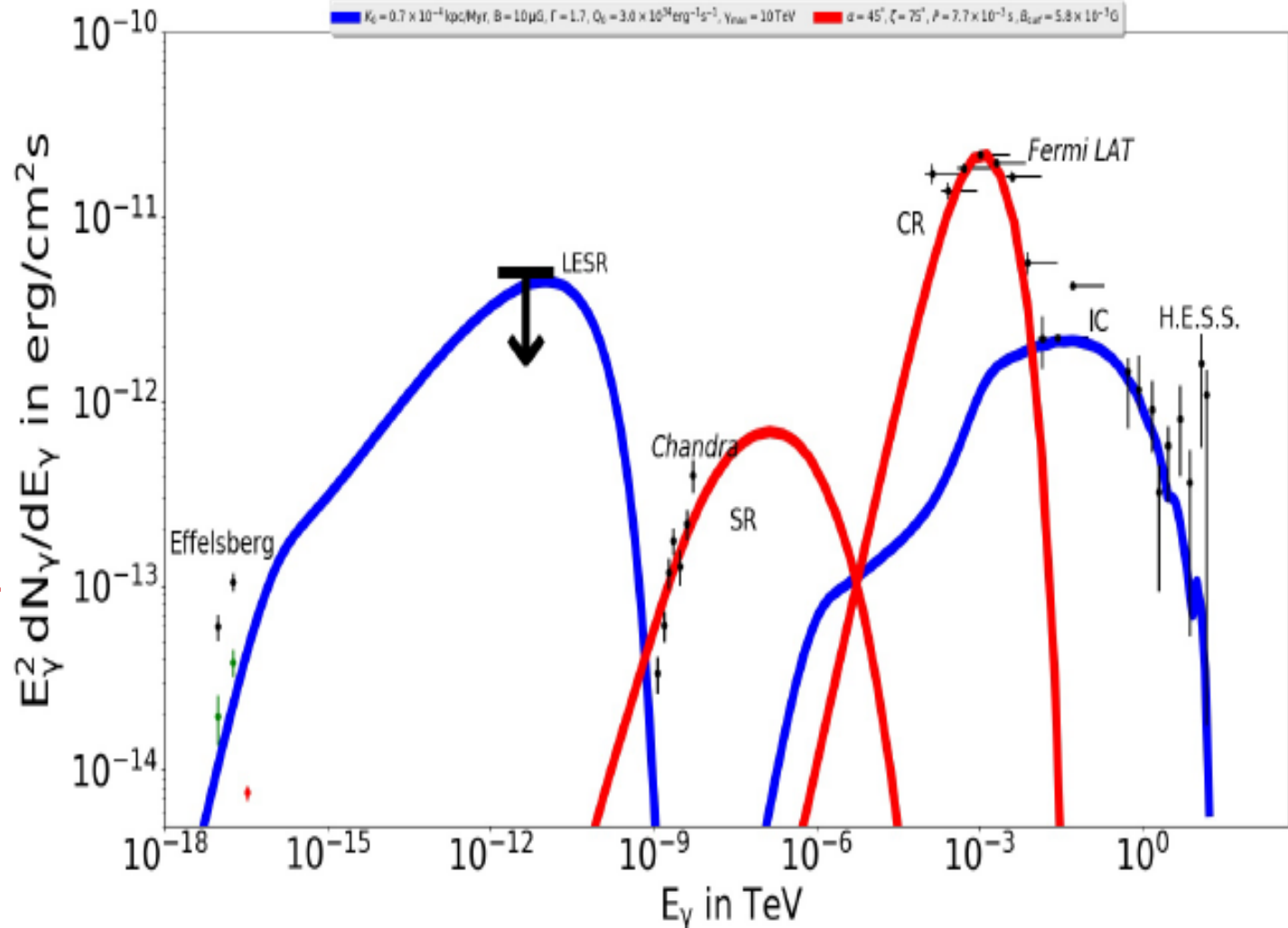
$$E \propto B^2$$

$$N_e(u_i, B, \kappa) \propto N_{MSP} \eta_p \langle \dot{E} \rangle$$

IC parameters:

$$u(r), u_{CMB}, u_{BG}$$

$$N_e(u_i, B) \propto N_{MSP} \eta_p \langle \dot{E} \rangle$$

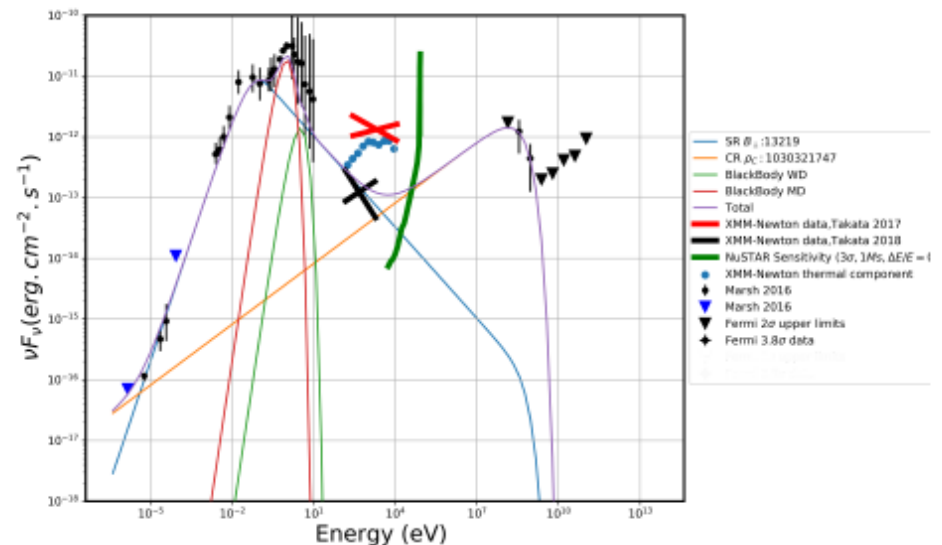
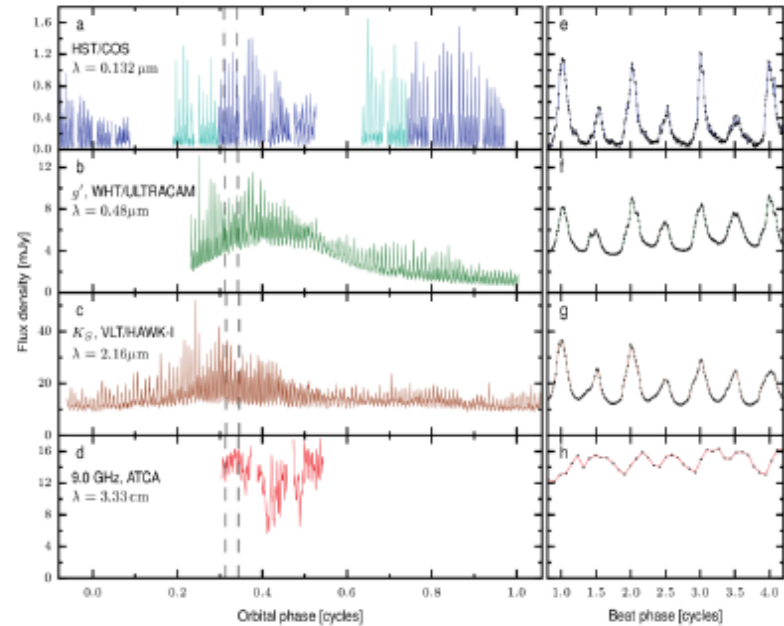


White Dwarf Pulsar



AR Sco Observations

- ▶ Marsh et al. (2016) detected optical and radio pulsations from the binary white dwarf (WD) system AR Scorpii
- ▶ Orbital period of 3.55 hours and a “pulsar” spin period of 1.95 min
- ▶ Constrained the mass of the WD to $\sim 0.8M_{\odot}$ and the M-dwarf companion to $\sim 0.3M_{\odot}$
- ▶ Stiller et al. (2018) obtained a $\dot{P} = 7.18 \times 10^{-13} \text{ ss}^{-1}$



AR Sco Observations

- ▶ Optical and UV emission lines show no indication of an accretion disc
- ▶ The optical and UV are non-thermal emission and pulsed at the WD spin period
- ▶ This gives a light cylinder radius of $R_{LC} = 5.6 \times 10^{11} \text{ cm}$ and an orbital semi-major axis of $a = 8.5 \times 10^{10} \text{ cm}$
- ▶ Buckley et al. (2017) found that the system exhibits strong linear optical polarisation (up to $\sim 40\%$) and estimated the WD B-field to be $\sim 500\text{MG}$

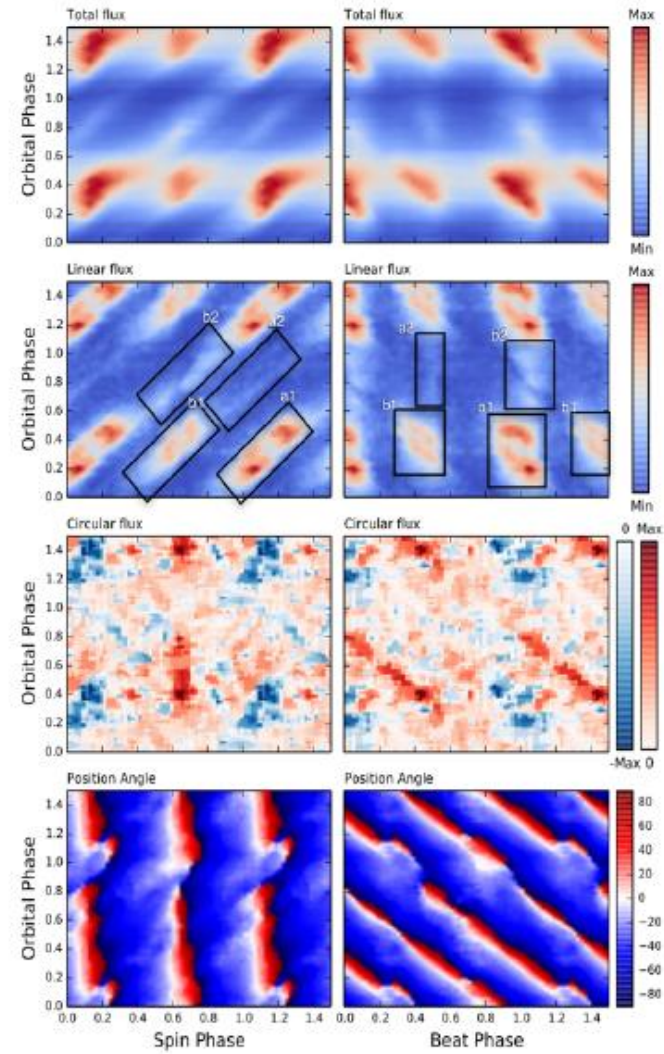


Figure: Optical data from Potter and Buckley (2018)

Radiation-reaction Force

- Use equation from Landau and Lifshitz for general radiation-reaction force:

$$\frac{d\mathbf{p}}{dt} = q \left(\mathbf{E} + \frac{c\mathbf{p} \times \mathbf{B}}{\sqrt{m^2c^4 + \mathbf{p}^2c^2}} \right) + \frac{2e^4}{3m^2c^4} \left\{ \mathbf{E} \times \mathbf{H} + \frac{1}{c} \mathbf{H} \times (\mathbf{H} \times \mathbf{v}) + \frac{1}{c} \mathbf{E} (\mathbf{v} \cdot \mathbf{E}) \right\} - \frac{2e^4\gamma^2}{3m^2c^5} \mathbf{v} \left\{ \left(\mathbf{E} + \frac{1}{c} \mathbf{v} \times \mathbf{H} \right)^2 - \frac{1}{c^2} (\mathbf{E} \cdot \mathbf{v})^2 \right\}. \quad (3)$$

- The first term of Equation 3 requires 9, 18 or 36 evaluations of the B-field per stage to find the derivatives.
- This first term is $\sim 10^8 - 10^{10}$ times smaller than the largest component.
- The super-relativistic form of Equation 3 is given by:

$$f_x = -\frac{2e^4\gamma^2}{3m^2c^4} \left\{ (E_y - H_z)^2 + (E_z + H_y)^2 \right\} \quad (4)$$

- Equation 3 and 4 converge at a Lorentz factor around $10^4 - 10^5$.

$$P_{rad} = \mathbf{F}_{rad} \cdot \mathbf{v},$$

$$E_{rad} = \int \mathbf{F}_{rad} \cdot \mathbf{v} \cdot dt \quad (5)$$

Adaptive Time-step Evaluation

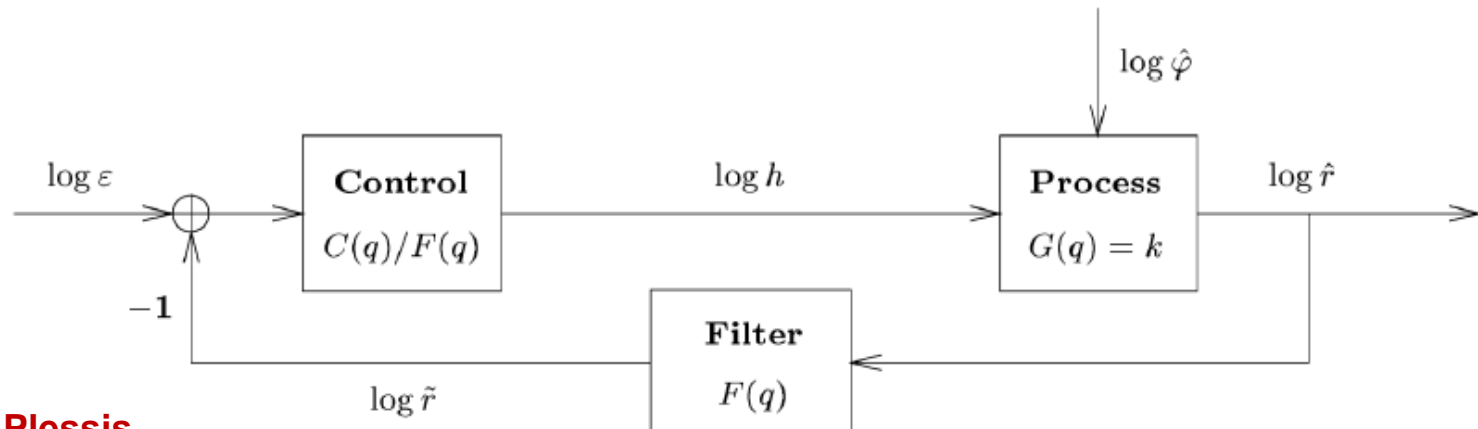
- ▶ Discovered numerical instability from adaptive time step.
- ▶ We investigated new higher precision adaptive time step methods.

$$\Delta t_{n+1} = \Delta t_n \left(\frac{TOL}{T_{err}} \right)^{-\frac{1}{kp}} \left(\frac{TOL}{T_{err;n-1}} \right)^{-\frac{1}{kp}} \left(\frac{\Delta t_n}{\Delta t_{n-1}} \right)^{-\frac{1}{kp}}. \quad (7)$$

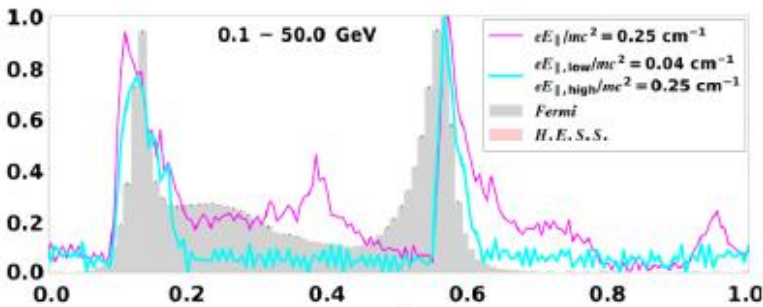
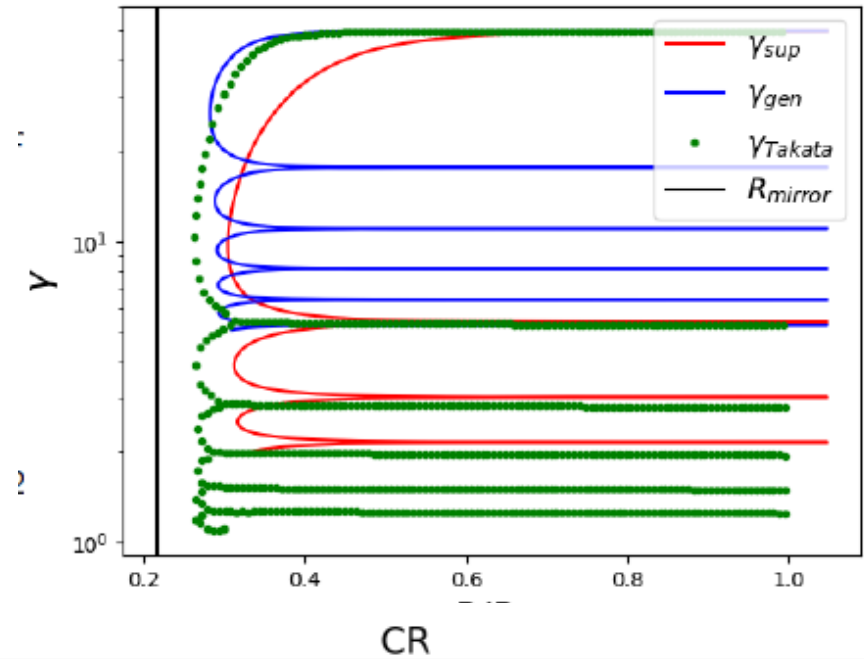
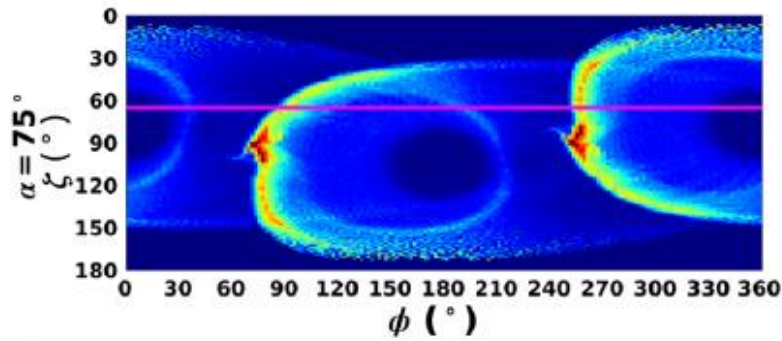
- ▶ Δt is the time step, TOL is the chosen tolerance for the truncation error T_{err} , p is the order of the chosen numerical method and $k = 8$.
- ▶ We used a limiting function to constrict the new time step.

$$\Delta t_l = \Delta t_n \left[1 + \kappa \arctan \left(\frac{\Delta t_{n+1} - \Delta t_n}{\kappa \Delta t_n} \right) \right]. \quad (8)$$

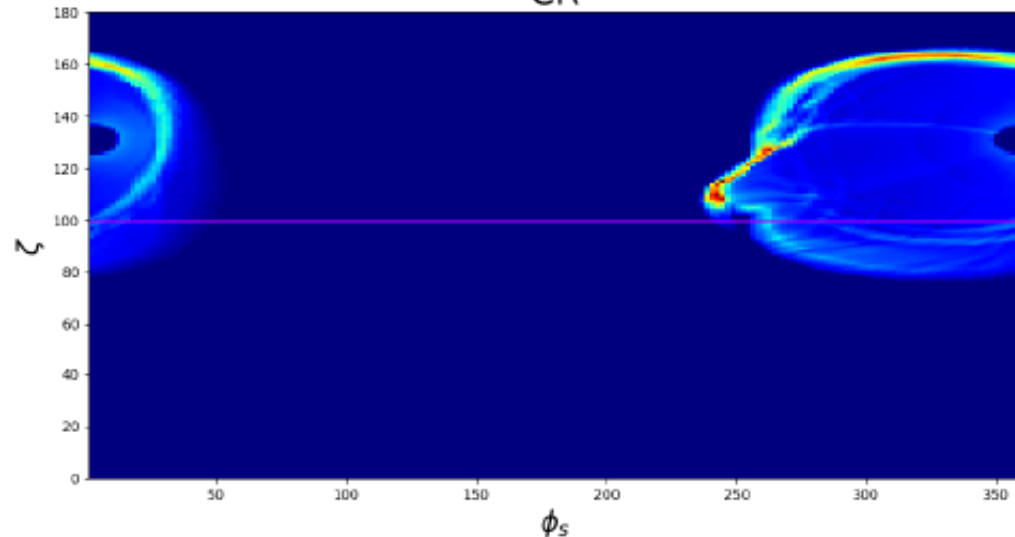
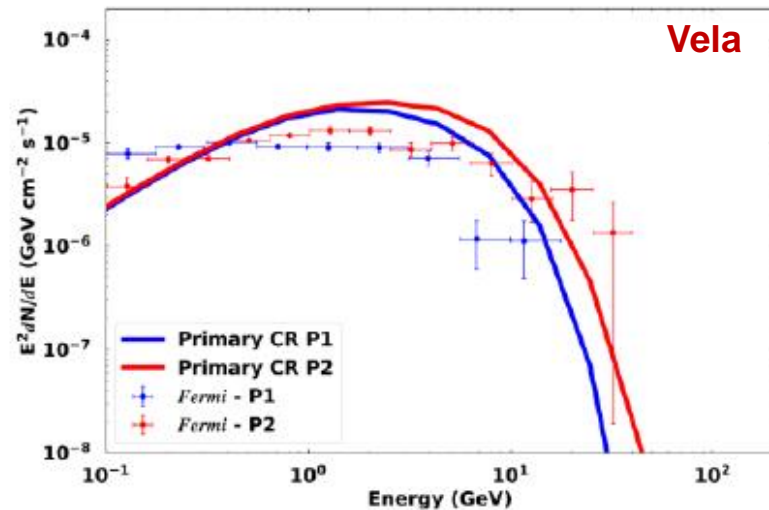
- ▶ $\kappa \in [0.7, 2.0]$.



Calibration of Code



Barnard et al. (2022) ϕ



RUNTIME!! Strong B-field

AR Sco

MeerKAT Observations



Open Time Round 1, 2, 3, 4

A search for persistent radio emission associated with
localised FRBs

MeerKAT Open Time Proposal

Overview

Fast Radio

Monthly Notices

of the

ROYAL ASTRONOMICAL SOCIETY



MNRAS 00, 1 (2022)

Advance Access publication 2022 June 16

<https://doi.org/10.1093/mnras/stac1601>

11 0000

**A MeerKAT
transient e**

MNRAS 000, 1–13 (2022)

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Discovery of an apparently non-repeating fast radio burst with the hallmarks of a repeater

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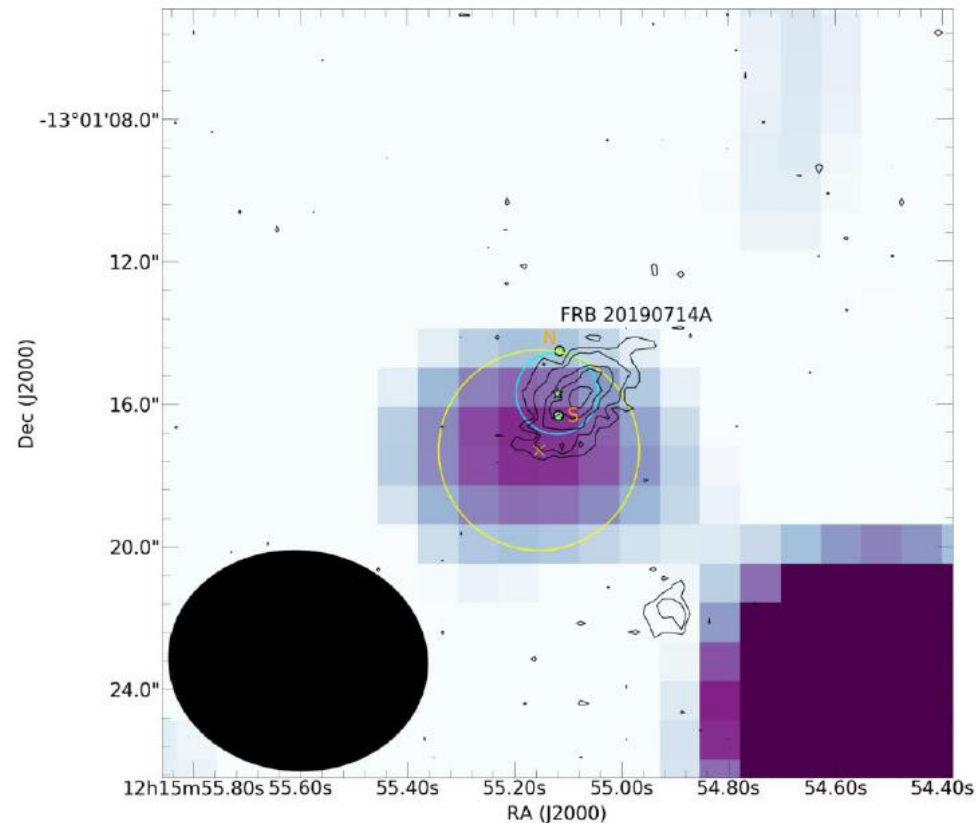
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⁶ Instituto de Física, Pontificia Universidad Católica de Valparaíso. Casilla 4059. Valparaíso. Chile

Open Time Round 1, 2, 3, 4

- Search for persistent radio emission from the one-off fast radio burst (FRB) 20190714A, as well as from two repeating FRBs, 20190711A and 20171019A, using MeerKAT.
- For FRB 20171019A, simultaneous observations with H.E.S.S. and searched for signals in the uv, optical, and X-ray bands.
- UV flux upper limit of $1.39 \times 10^{-16} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ \AA}^{-1}$.
- X-ray limit of $\sim 6.6 \times 10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$
- $F(E > 120 \text{ GeV}) < 1.7 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}$.
- Radio UL $\sim 15 \mu\text{Jy beam}^{-1}$ for persistent emission at the locations of both FRBs 20190711A and 20171019A.



Some Open Questions

- Debates:
 - SR vs. CR responsible for GeV spectrum?
 - OG vs. SG – break degeneracy using TeV emission
- Spectral shape of emitting particles (primaries / pairs)?
- Which emission mechanisms contribute to the broadband SED?
- Local and global electrodynamical properties?
- Pulsar (magnetosphere) geometry? Novel systems?

Spectral and energy-dependent light curve modelling
(*Polarimetry*)

Overlaps?

Quantum processes

- **One-photon pair production**
- **Two-photon pair production**
- **Photon splitting**
- **Critical B -fields $B > 4e13$ G:
effect on radiation physics**

Overlaps?

Computational power needed!

- **Diverse data sets**
- **Diverse models addressing different scales / quantities**
- **E.g., statistics, searching, classifying**
- **E.g., triple integrals, coupled differential equations, Maxwell's equations, trajectories (SR, beaming), Monte Carlo, pair production, polarisation, binning...**

Overlaps?

Storage of information

- **MeerKAT: 2 TB/h**
- **On-the-fly analysis, discarding a lot of data due to space limitations**
- **IDIA / CHPC: storage constraints**
- **Data mining (Machine Learning)**

Conclusions

- **Lots of outstanding theoretical issues in pulsar science**
- **Lots of new (multi-messenger) and high-quality data**
- **Quantum effects in physical processes**
- **Computational requirements sometimes prohibitive**
- **New ideas? Overlaps?**

Thanks!

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<https://www.slieverussell.ie>

“The heavens declare the glory of God; the skies proclaim the work of his hands.” (Ps. 19:1)