

[2310.10471]

Pair production of Higgs boson in composite two Higgs doublet model

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In collaboration with

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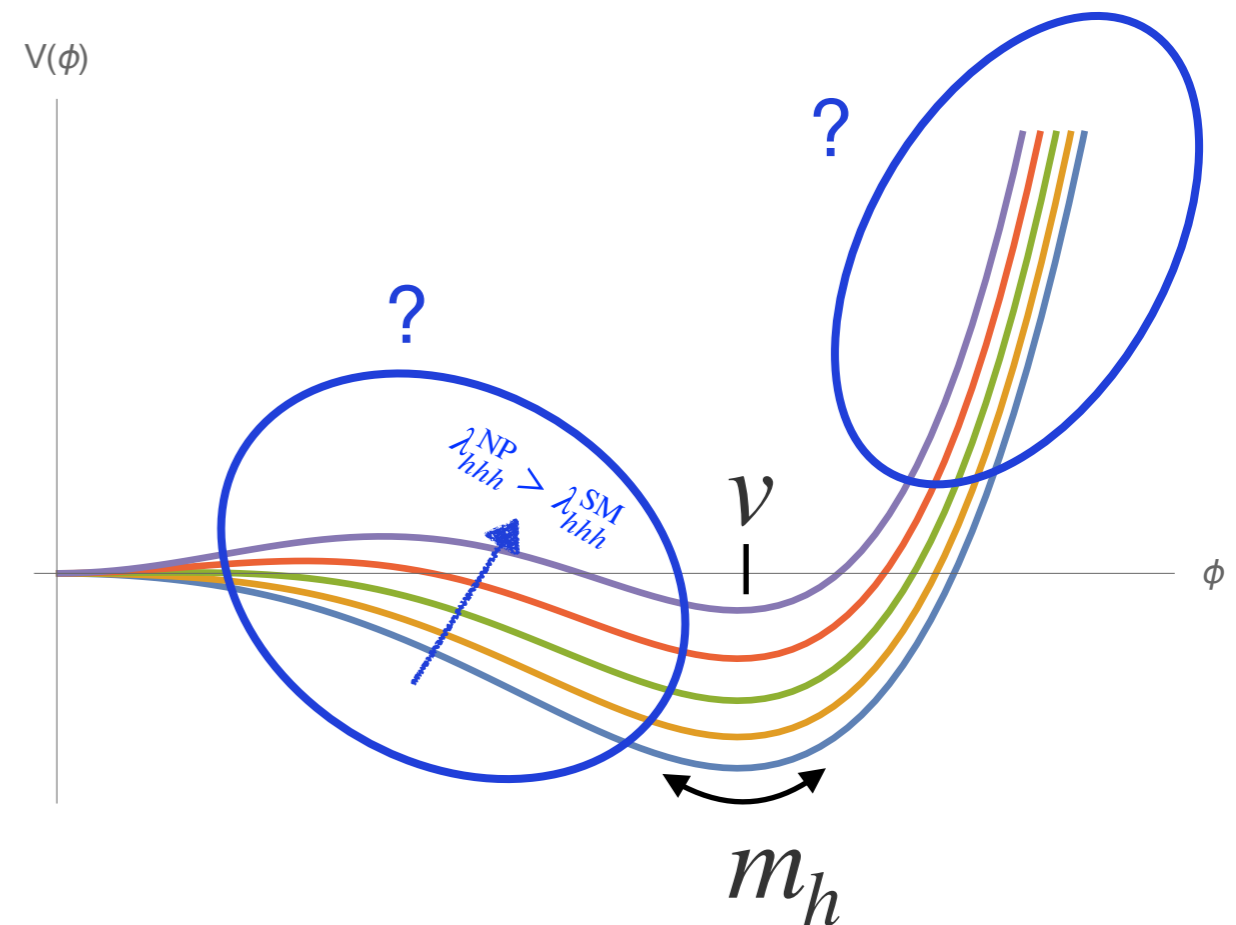
The shape of the Higgs potential is unknown

- After the discovery of the Higgs boson, the properties are measured in LHC experiments.
- What we know currently about the Higgs potential are two things:

- Position of the EW minimum
- The curvature of the potential around the minima.

- The hhh coupling is not measured accurately.

$$V(h) = \frac{1}{2}m_h^2 h^2 + \lambda_{hhh} h^3 + \lambda_{hhhh} h^4$$



→ The shape of the potential away from the minima is not determined.

Determination of the shape of Higgs potential

Determination of the shape of Higgs potential is a key to find New physics.

- We may restrict the shape of the Higgs sector.
- We may find a clue of a new paradigm beyond SM.

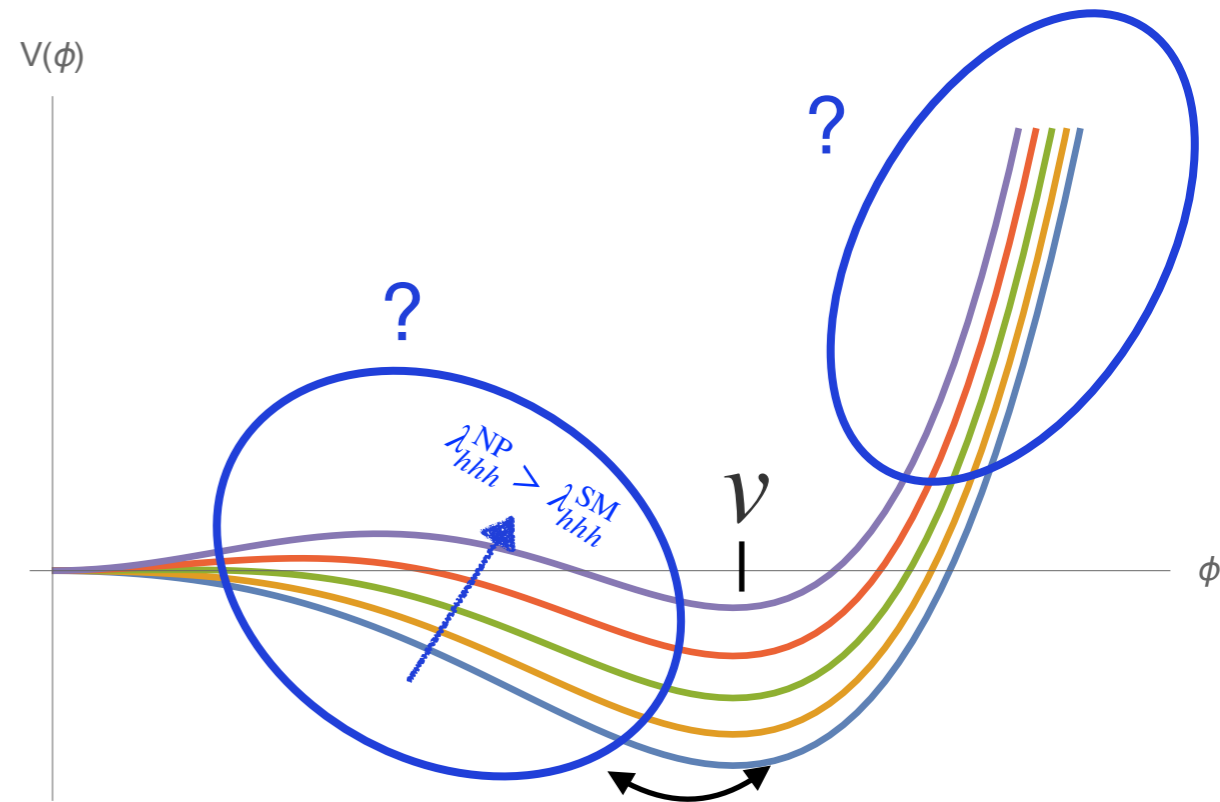
EX.) Models with two Higgs fields

$$\lambda_{hhh}^{\text{E2HDM}} \sim -\frac{m_h^2}{2v} + \frac{m_{12}^2}{v c_\beta s_\beta} c_{\beta-\alpha}^2 \quad (c_{\beta-\alpha} \ll 1)$$

$$\lambda_{hhh}^{\text{MSSM}} = 3 \frac{m_Z^2}{v} c_{2\alpha} s_{\alpha+\beta}$$

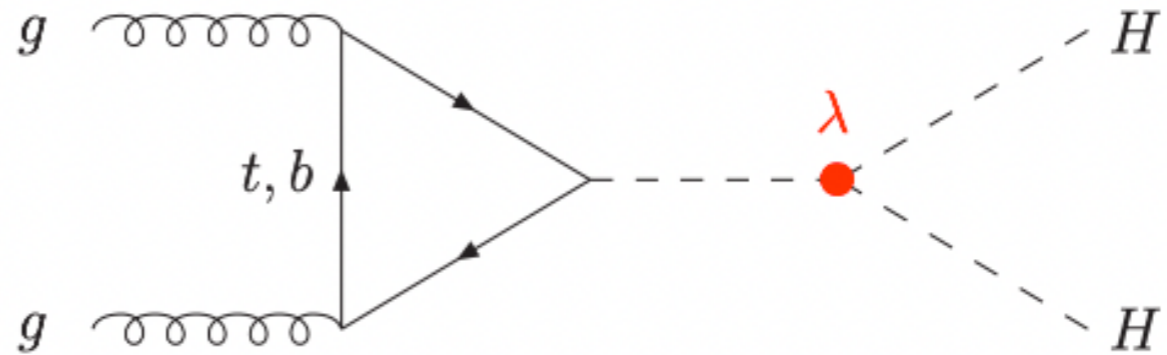
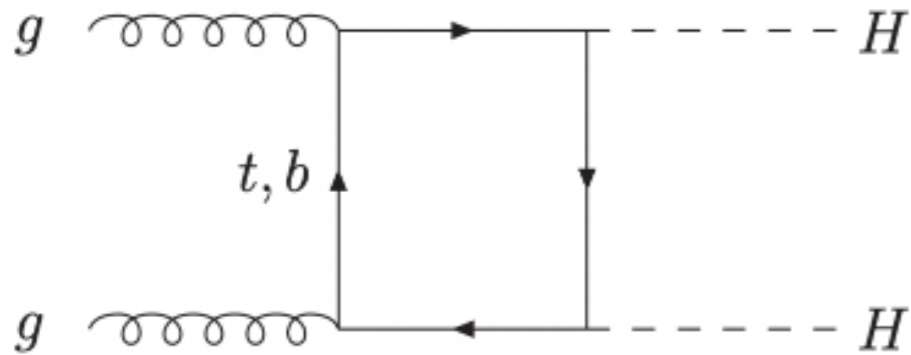
$$\lambda_{hhh}^{\text{C2HDM}} : \text{ depends on strong sector}$$

- How EWSB occurs (1st OPT GWs).



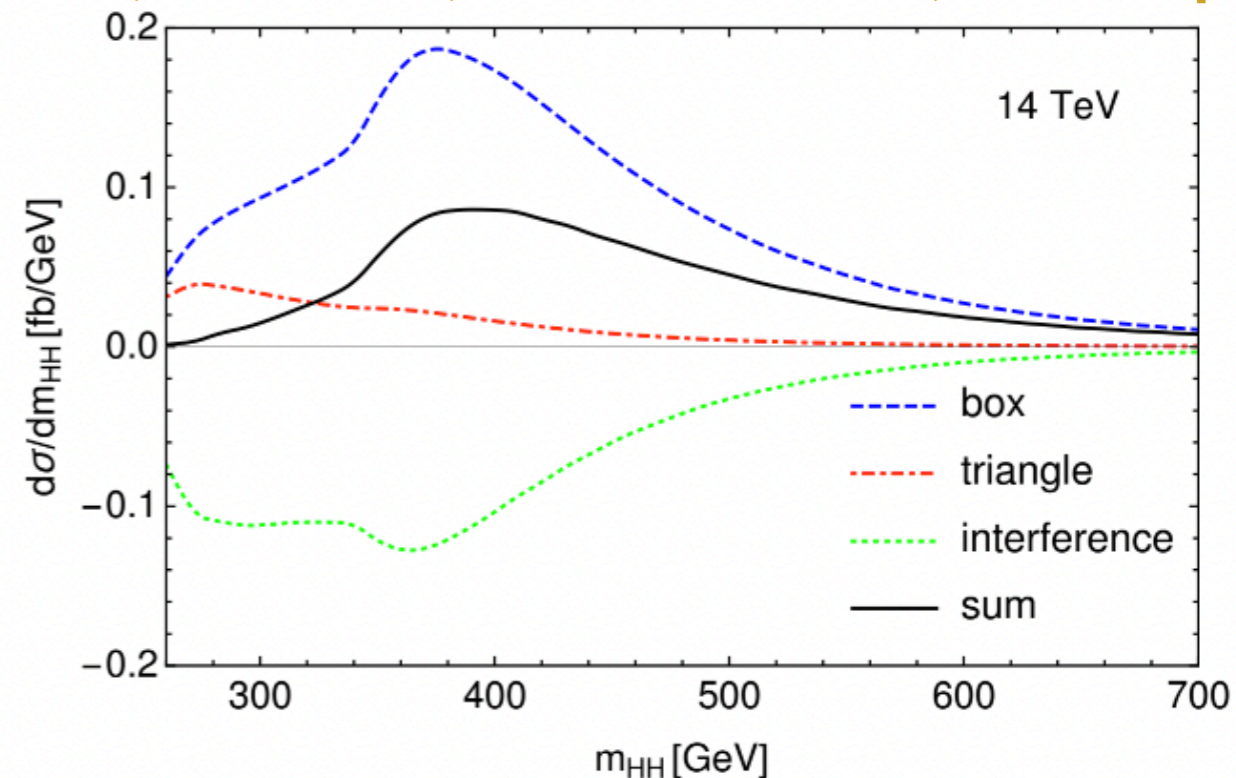
Di-Higgs production process

- λ_{hhh} appears in di-Higgs production process. Dominant one is $gg \rightarrow hh$

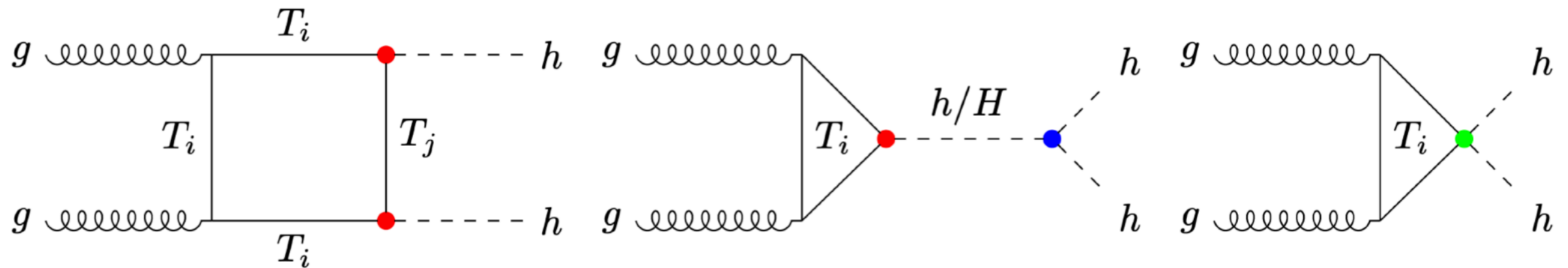


- Through λ_{hhh} , interference can change much.
- Predictions of di-Higgs boson should be prepared in various extended Higgs models to compare experiments such as LHC Run 3 HL-LHC.

[B. Micco, M. Gouzevitch, J. Mazzitelli C. Vernieri, 1910.00012]



Motivation of this study



- We discuss the theoretical behavior of di-Higgs production cross section in the composite two-Higgs doublet model.
- One has additional vector-like fermion loops (T_i) and heavy CP-even Higgs boson (H) as new physics effects.
- Open questions:
 - How much these new physics effects can enhance $\sigma_{pp \rightarrow hh}$?
 - How the prediction for $\sigma_{pp \rightarrow hh}$ can be changed from E2HDM?

Setup: Composite two Higgs doublet model

[S. De Curtis, et al, JHEP 12 (2018) 051]

- Group structure: $\frac{\mathcal{G}}{\mathcal{H}} = \frac{SO(6)}{SO(4) \times SO(2)}$,

[See the details in the slide by S. Moretti]

8 (=15-7) broken SO(6) generators exist. We have 8 NGBs, which corresponds to Higgs fields in 2HDM.

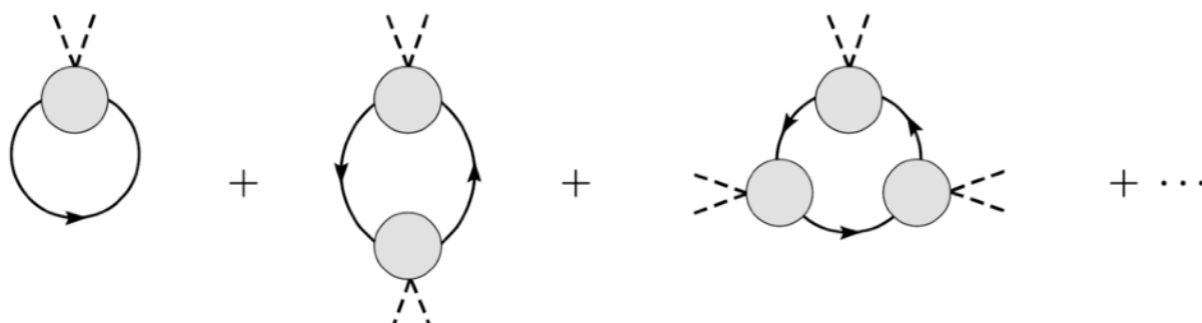
- How is the mass of the Higgs boson generated?

- The explicit breaking of SO(6) is required.

For gauge sector, gauging EW subgroup breaks SO(4)×SO(2).

For fermion sector, explicit breaking terms are introduced

- The Coleman-Weinberg potential is generated:



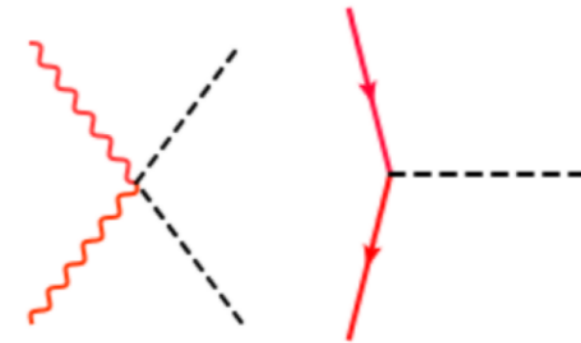
➔ masses and self int.

The potential is governed by composite parameters.

Setup: Composite two Higgs doublet model

$$\mathcal{L}_{\text{C2HDM}} = \mathcal{L}_{\text{elementary}} + \mathcal{L}_{\text{mixing}} + \mathcal{L}_{\text{resonances}}$$

$\mathcal{L}_{\text{resonances}}$: contains NGBs and heavy resonances.
It involves the interactions between them
with suppression $1/f$.



$\mathcal{L}_{\text{elementary}}$: constructed by W_{μ}^a , q_L and q_R .
It involves kinetic terms.

$\mathcal{L}_{\text{mixing}}$: gives int. between $\mathcal{L}_{\text{elementary}}$ and $\mathcal{L}_{\text{resonance}}$.

Setup: Composite two Higgs doublet model

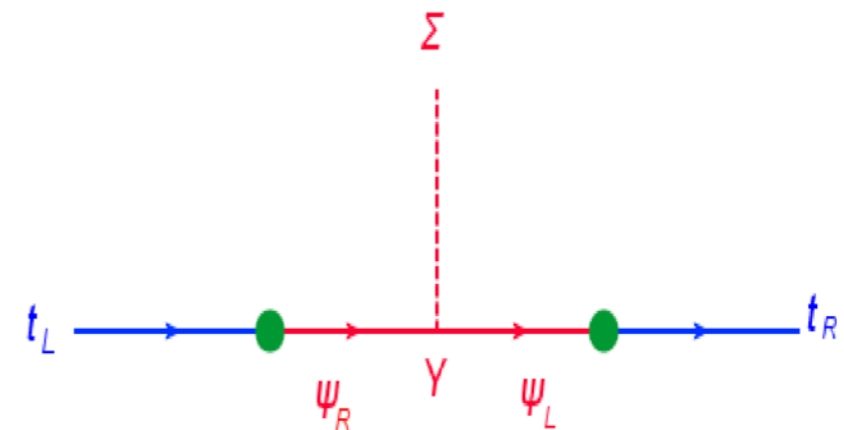
$\mathcal{L}_{\text{mixing}}$: gives int. between $\mathcal{L}_{\text{elementary}}$ and $\mathcal{L}_{\text{resonance}}$.

EX.) fermion sector (U : Higgs field ψ : VL fermion)

$$\mathcal{L}_{\text{mixing}} = y_L^{ij} f \bar{q}_L^i U \cdot (\psi^I)^j + \tilde{y}_L^{ij} f \bar{q}_L^i U \cdot (\psi^\alpha)^j + (q_L \rightarrow u_R, d_R, l_L, e_R)$$

- It explicitly breaks SO(6).
- It generates Yukawa int. masses of fermions
- We introduces two spices of ψ .

➔ 8 heavy top partners (T_i) are introduced.



Higgs pair production

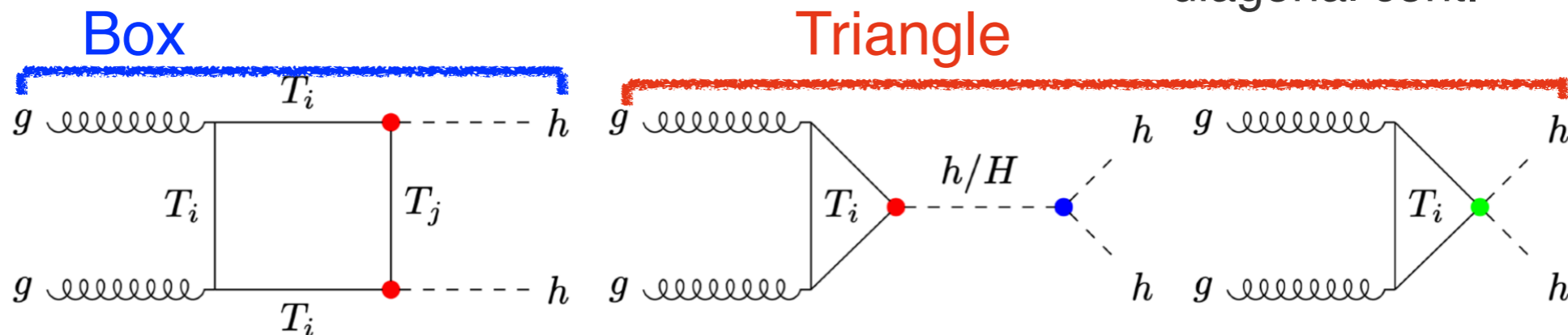
$$\frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} = \frac{\alpha_s^2}{512(2\pi)^3} \times \left[\sum_{i=1}^{n_q} C_{i,\Delta}^{hh} F_{\Delta}(m_i) + \sum_{i=1}^{n_q} \sum_{j=1}^{n_q} (C_{ij,\square}^{hh} F_{\square}^{hh}(m_i, m_j) + C_{ij,\square,5}^{hh} F_{\square,5}^{hh}(m_i, m_j)) \right]^2$$

$$+ \left[\sum_{i=1}^{n_q} \sum_{j=1}^{n_q} (C_{ij,\square}^{hh} G_{\square}^{hh}(m_i, m_j) + C_{ij,\square,5}^{hh} G_{\square,5}^{hh}(m_i, m_j)) \right]^2,$$

} Spin-0 contributions
} Spin-2 contributions

- Corresponding diagrams

The box contains off-diagonal cont.



- Heavy mass limit [T. Plehn, M. Spira, P. M. Zerwas, Nucl.Phys.B 479 (1996) 46]

$$F_{\Delta} \rightarrow \frac{s}{m_T} \frac{2}{3}, \quad F_{\square} \rightarrow -\frac{s}{m_T^2} \frac{2}{3}, \quad G_{\square} \rightarrow \mathcal{O}\left(\frac{s^2}{m_T^4}\right), \quad \Rightarrow \text{Spin-0 cont. is dominant.}$$

Scan analysis

- We scan the composite parameters by applying the following constraints:

[calculated by by Felix]

Parameter	Range	
	Lower	Upper
m_H	180 GeV	3 TeV
$m_{T,8}$	1300 GeV	23 TeV
$m_{T,1}$	2700 TeV	80 TeV
$\lambda_{hhh}/\lambda_{SM}$	0.7	1.07
$g_{htt}/g_{htt,SM}$	0.73	1.33

- Correct global EW minimum, m_t
- Perturbativity for λ_i
- LHC bounds for H, A, H^\pm and h
- $\sigma_{pp \rightarrow hh}$ through resonant search

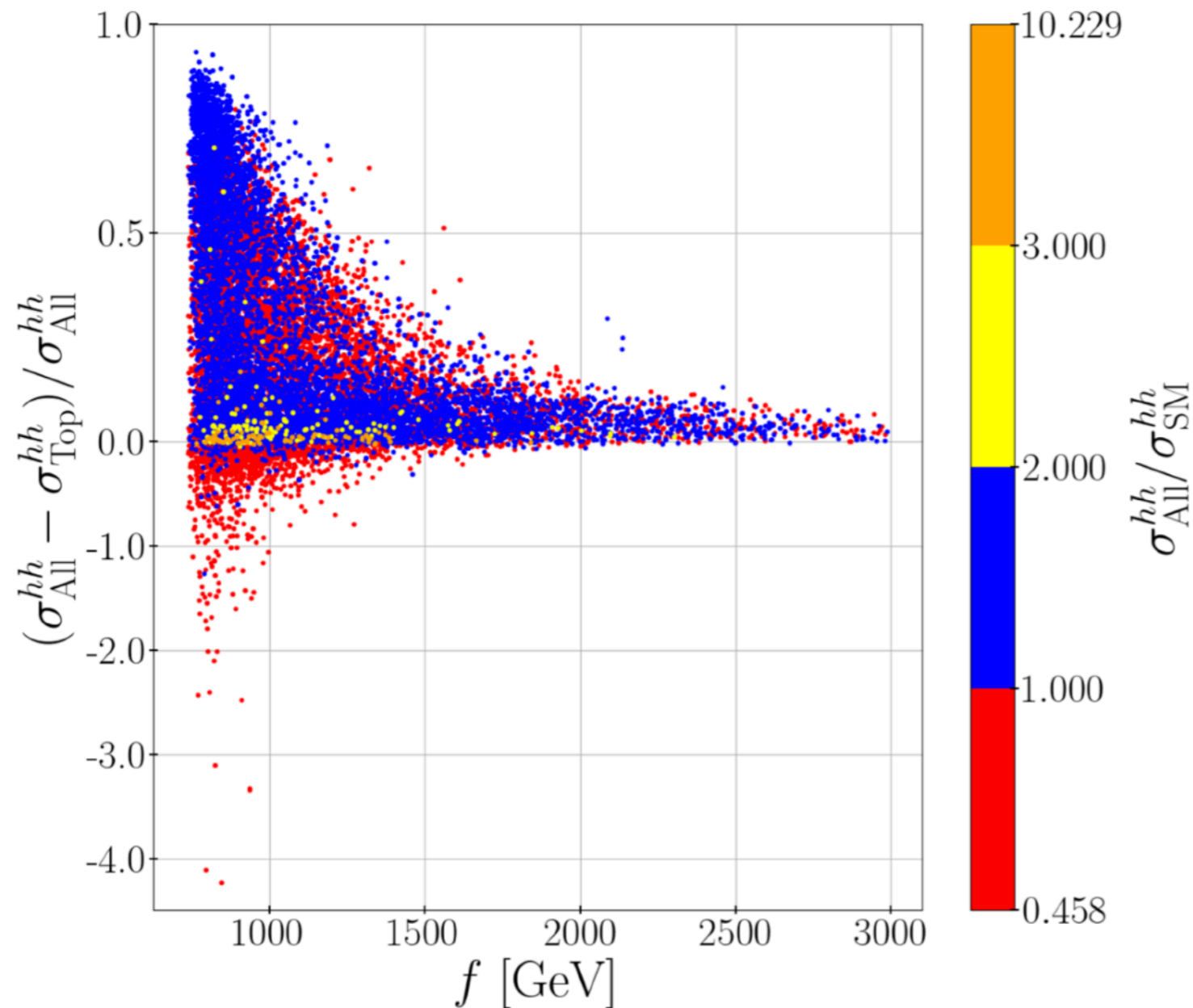
- We consider the two regime:

$$\text{Resonant case : } \frac{\sigma(gg \rightarrow H) \times \text{BR}(H \rightarrow hh)}{\sigma(gg \rightarrow hh)} > 0.1, \quad \text{and} \quad \Gamma_H/m_H < 5\%$$

$$\text{Nonresonant case : } \frac{\sigma(gg \rightarrow H) \times \text{BR}(H \rightarrow hh)}{\sigma(gg \rightarrow hh)} < 0.1 \quad \text{or} \quad m_H < 2m_h$$

Influence of Heavy top partner loop contributions

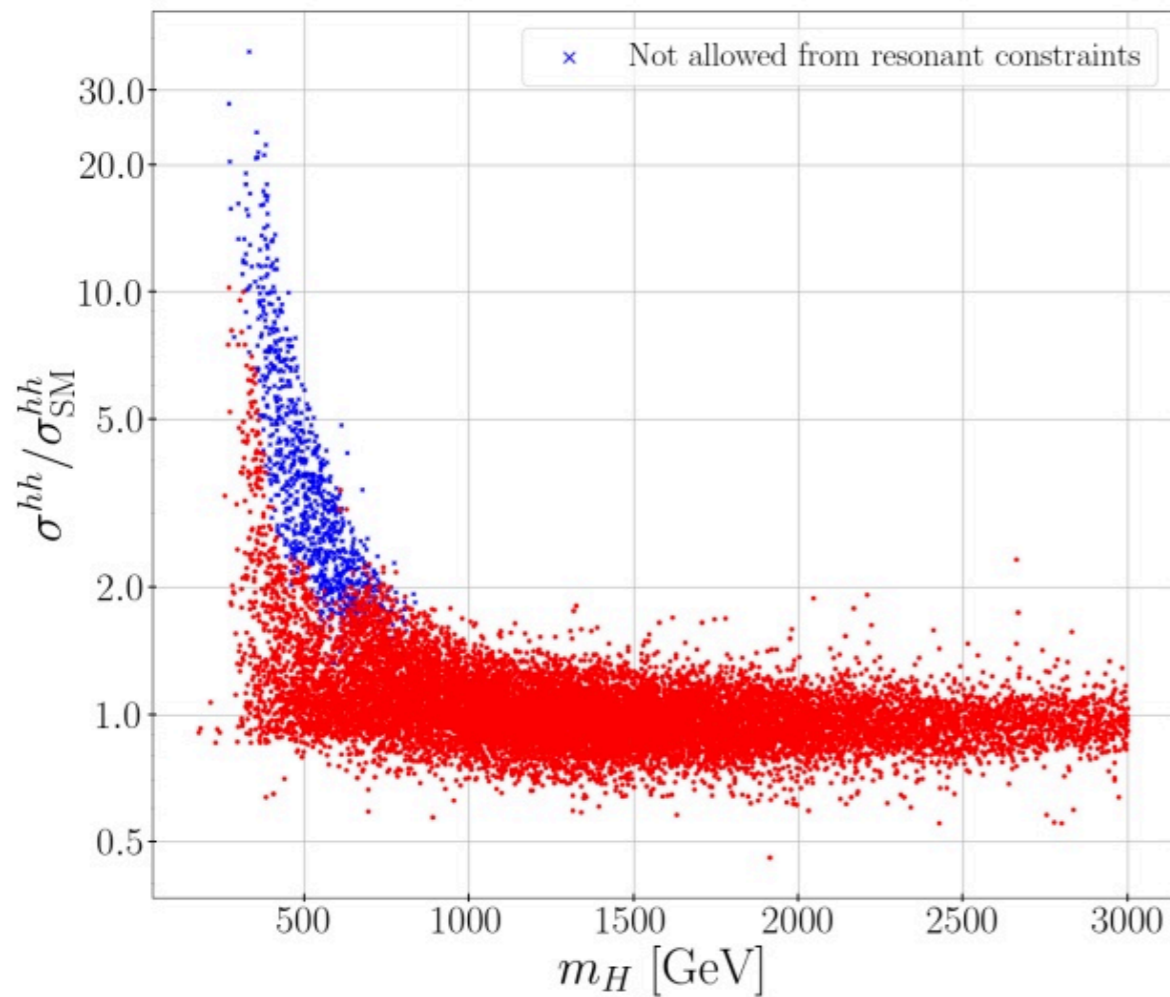
[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



- Heavy top partner gives destructive and constructive contributions.
- T_i contributions have influence when $\sigma^{hh} / \sigma_{SM}^{hh} \sim 0.5-2$.

Size of σ in resonant and non-resonant cases.

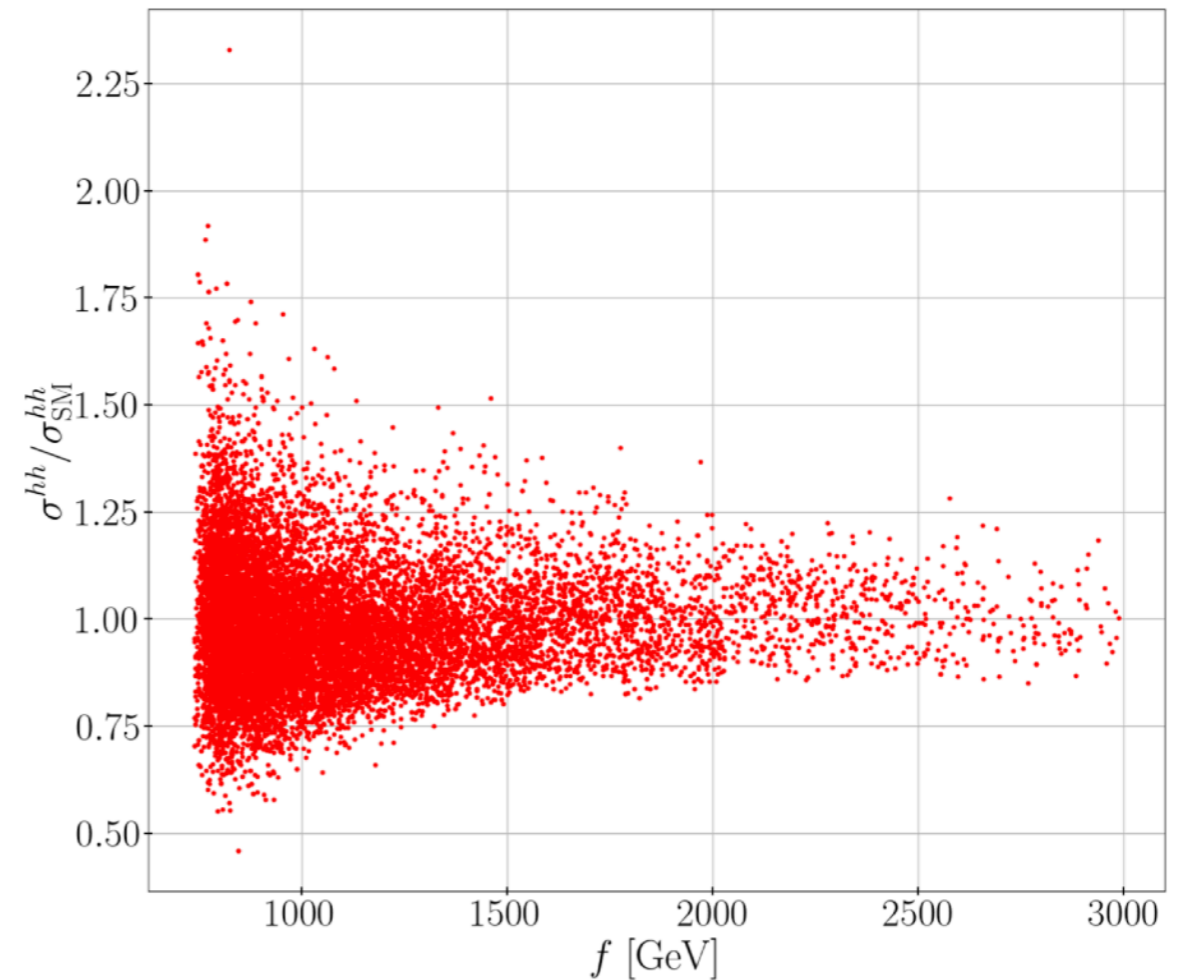
Resonant case



- If $m_H \sim 2m_h$, $\sigma^{hh}/\sigma_{SM}^{hh}$ can be ~ 10 .

Non-resonant case

[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



- $\sigma^{hh}/\sigma_{SM}^{hh}$ can reach ~ 2.3 .

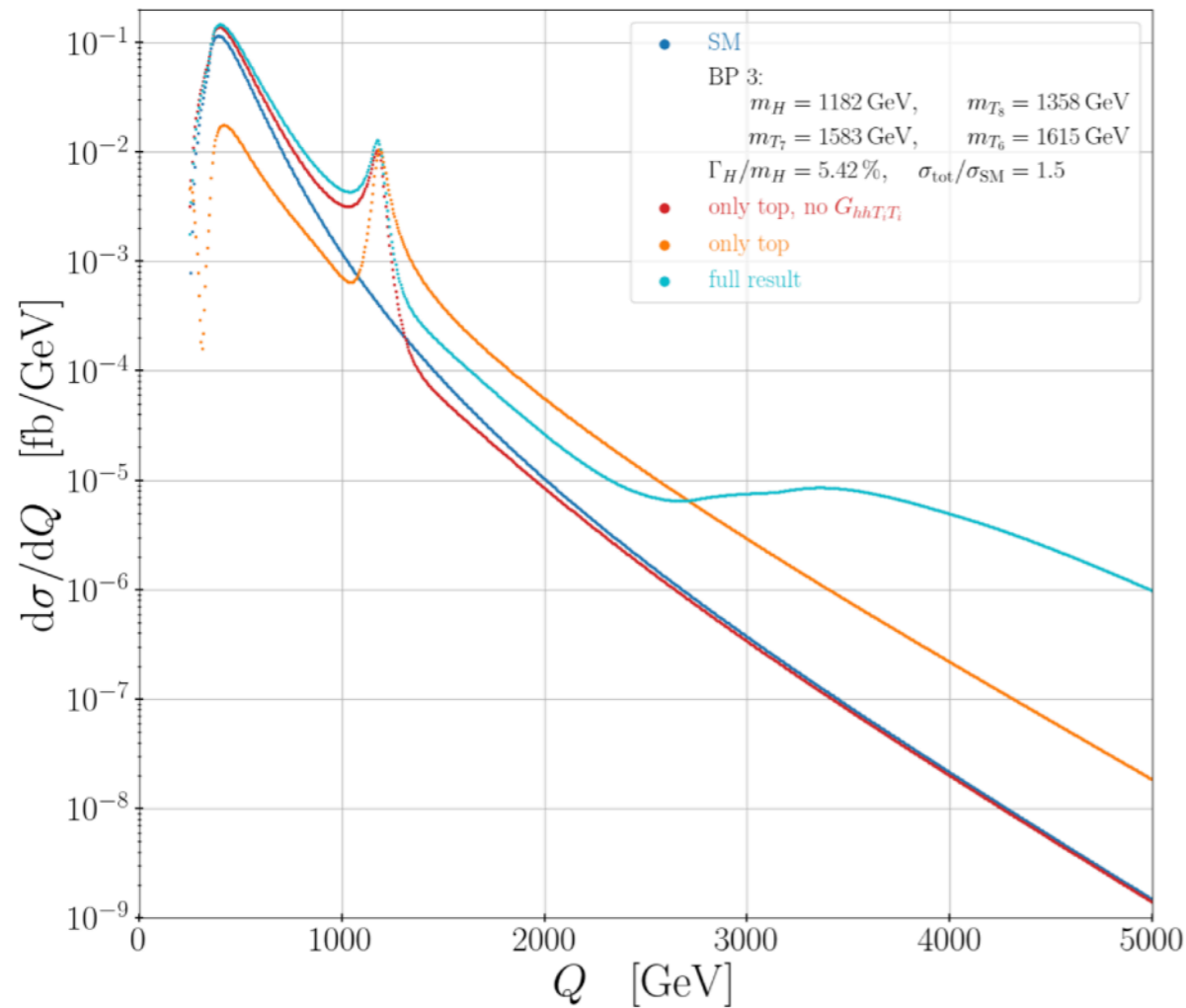
$\longleftrightarrow \mu_{HH} \lesssim 2.4$ @ATLAS, 139fb^{-1}

[ATLAS, 2211.0121]

Invariant mass distributions

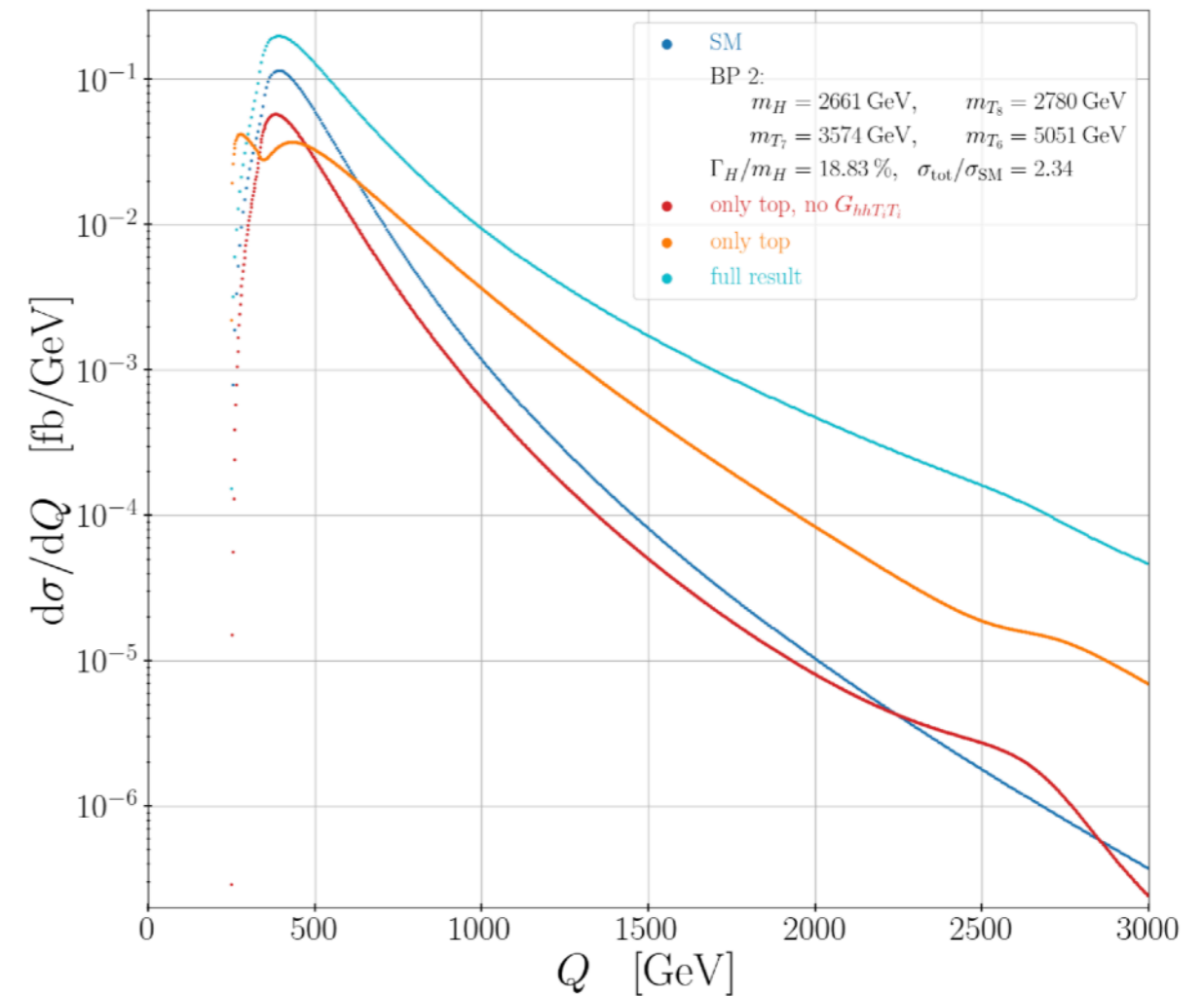
█ SM result
█ Full result

Resonant case



Nonresonant case

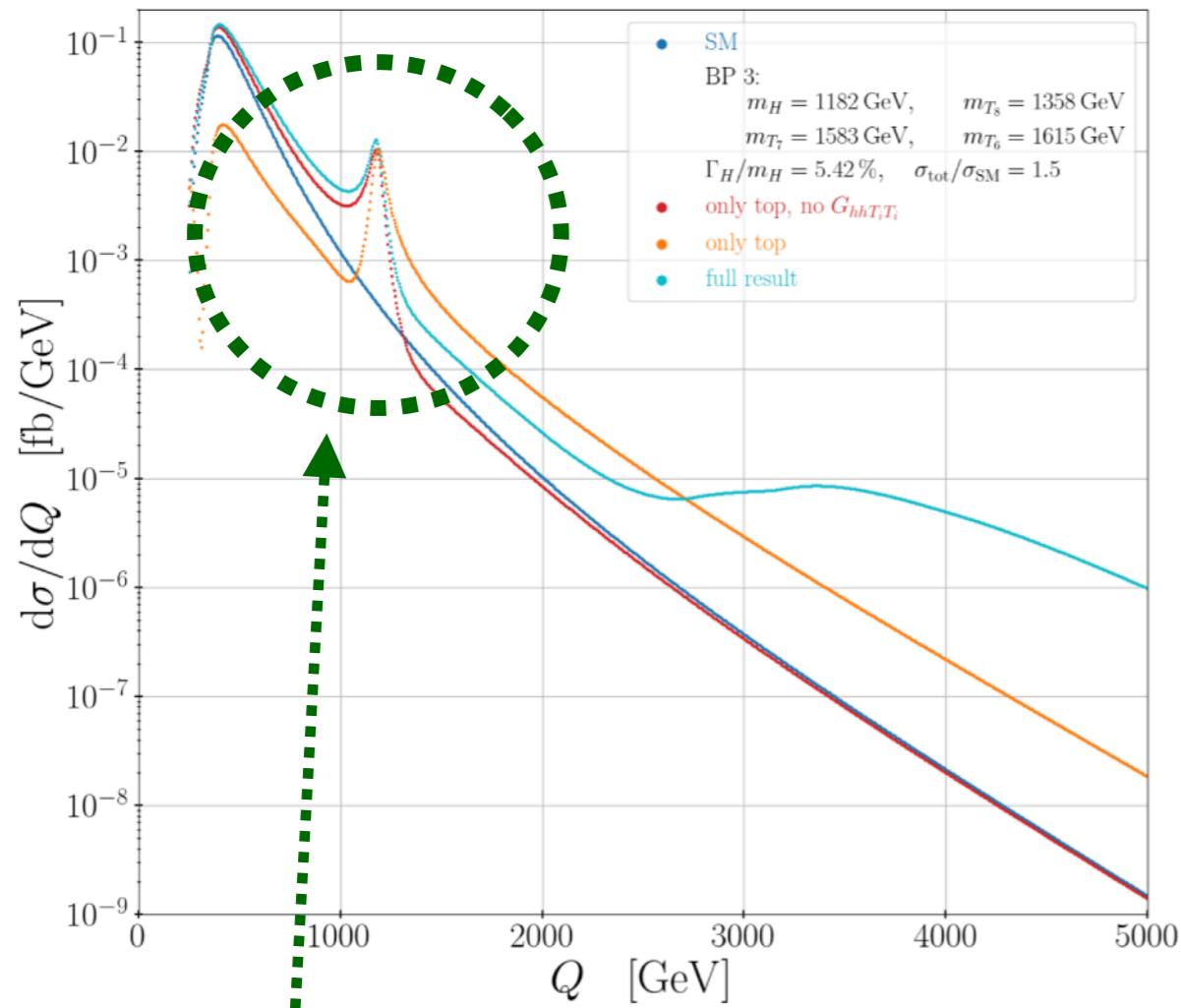
[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



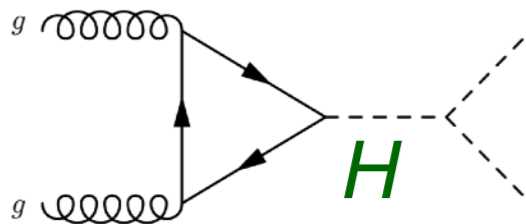
Invariant mass distributions

█ SM result
█ Full result

Resonant case

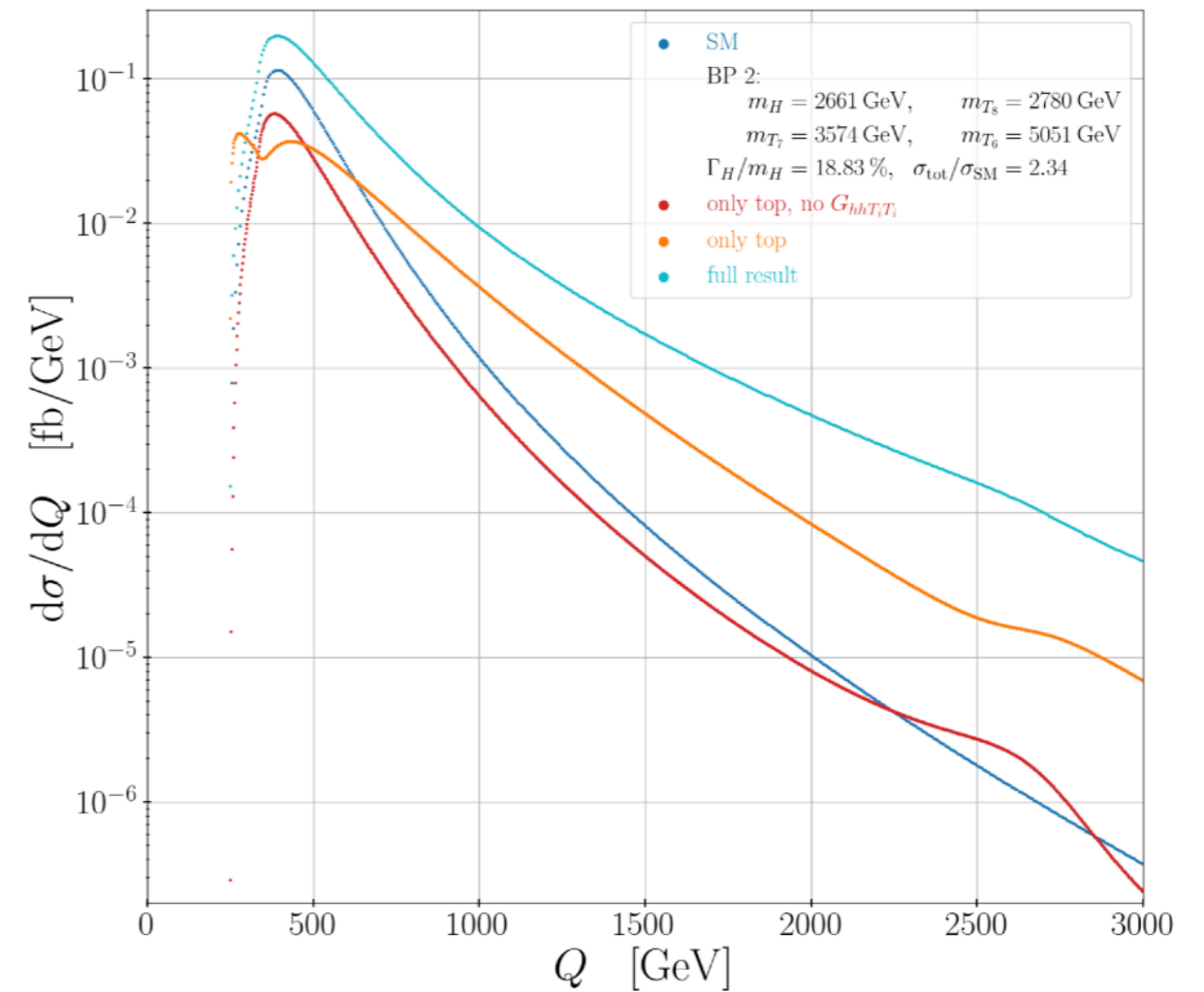


BW distortion



Nonresonant case

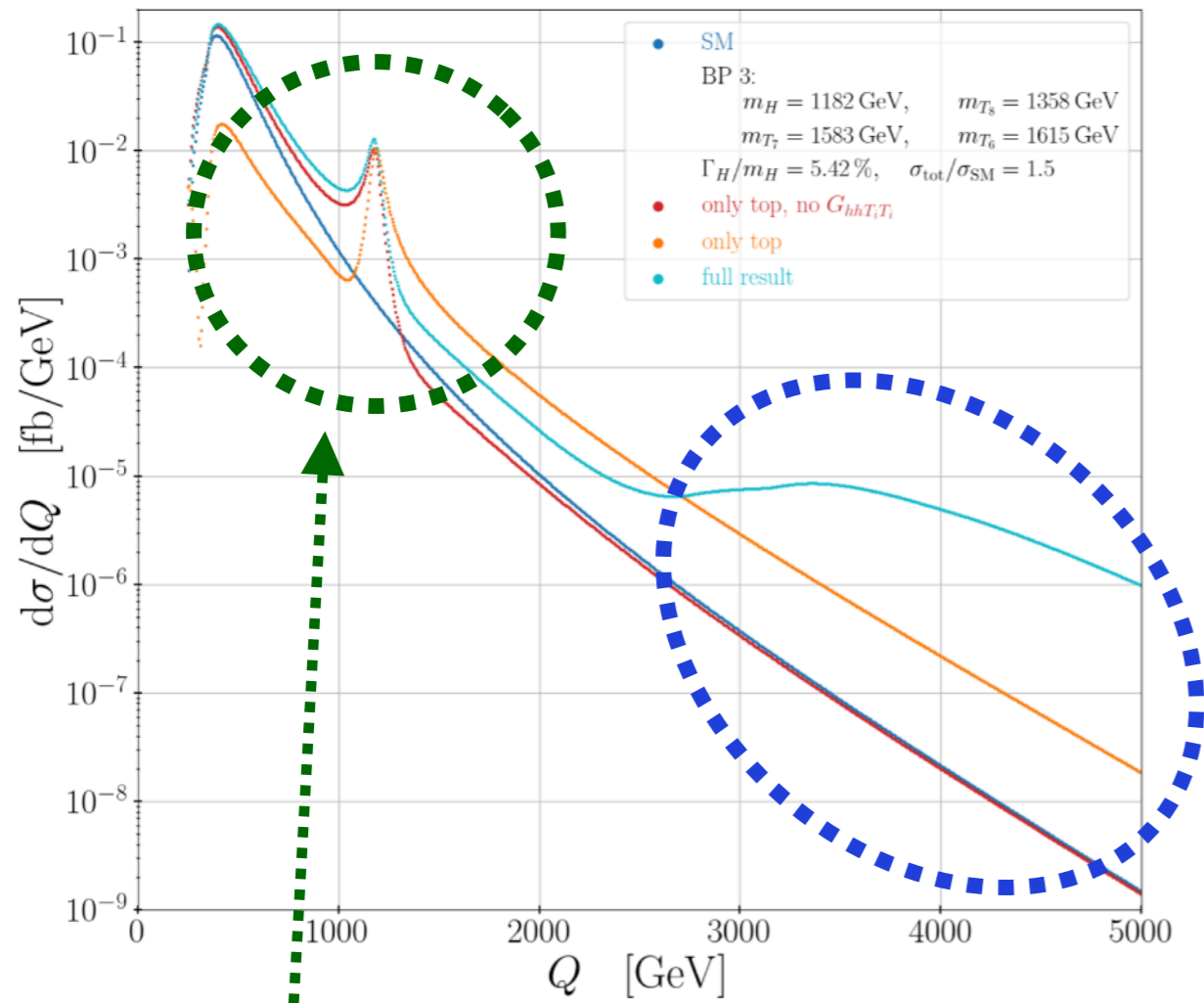
[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



Invariant mass distributions

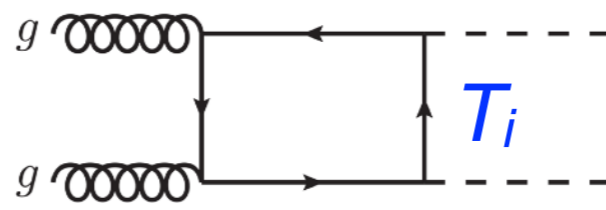
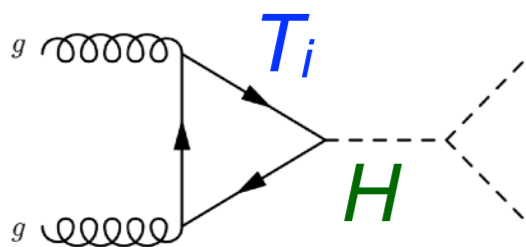
█ SM result
█ Full result

Resonant case



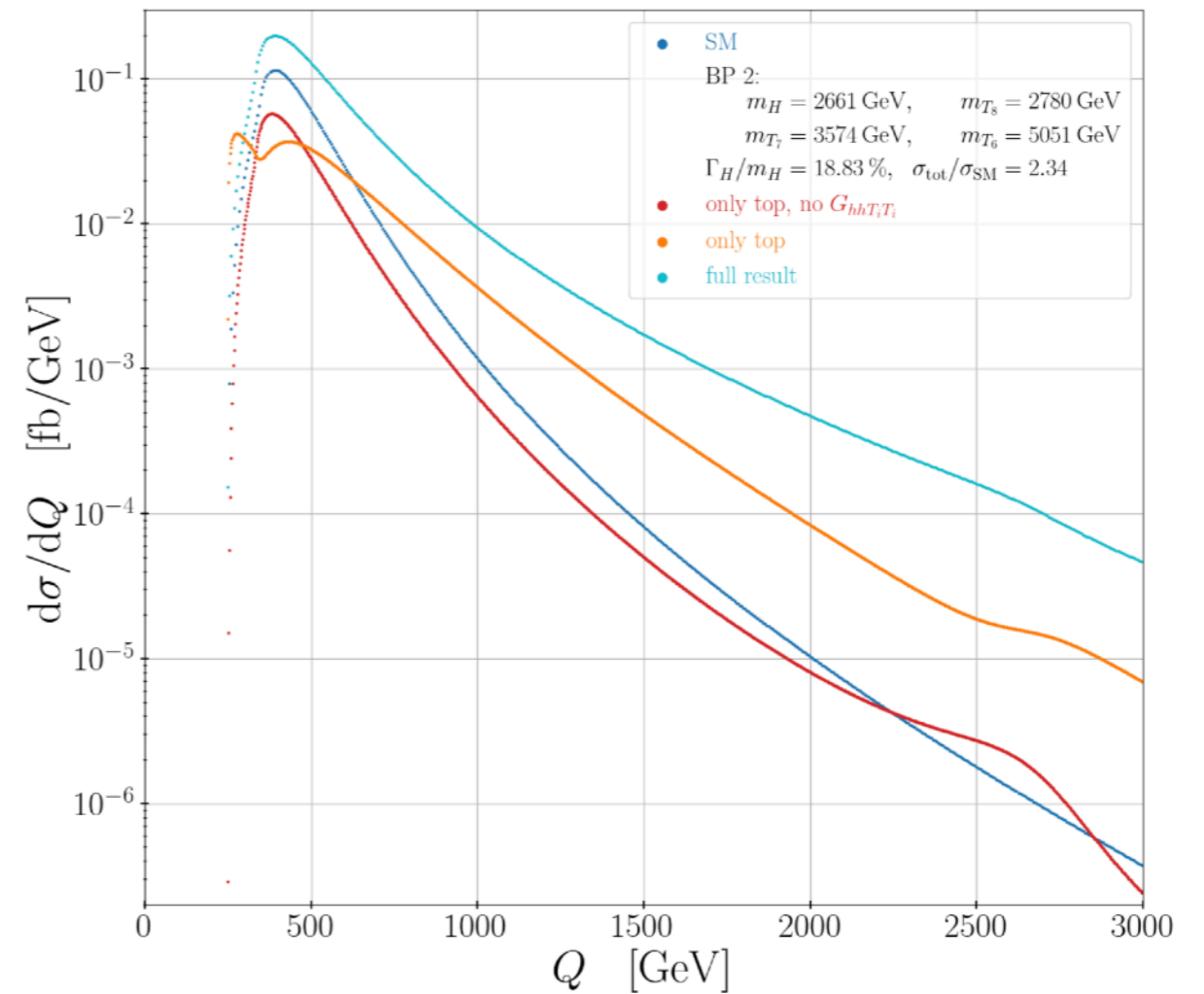
BW distortion

Tail effect



Nonresonant case

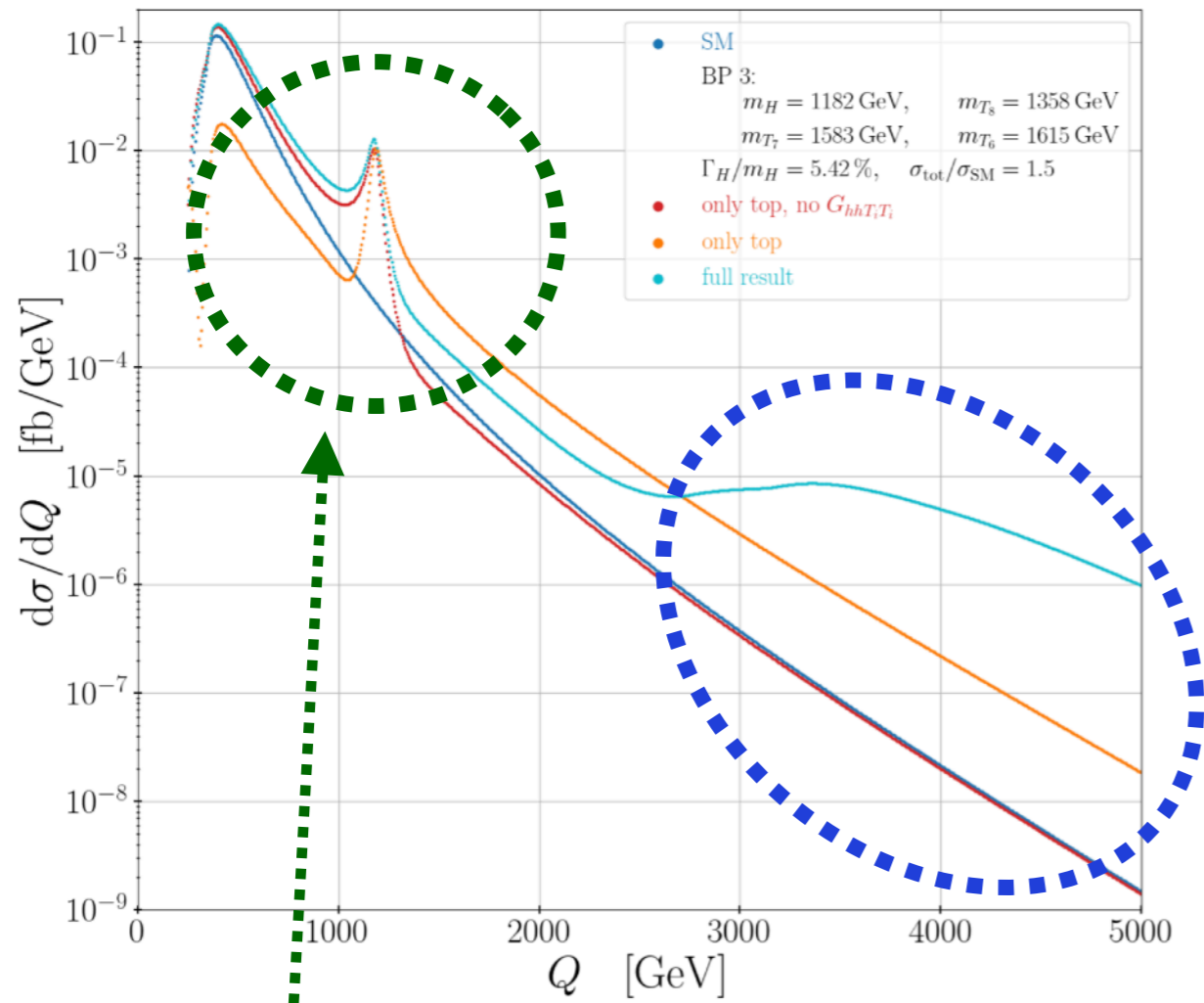
[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



Invariant mass distributions

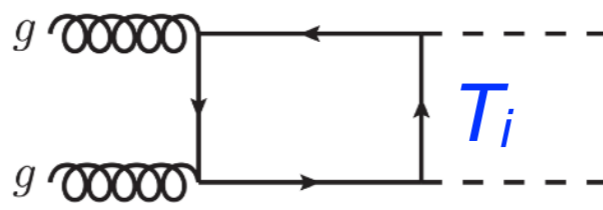
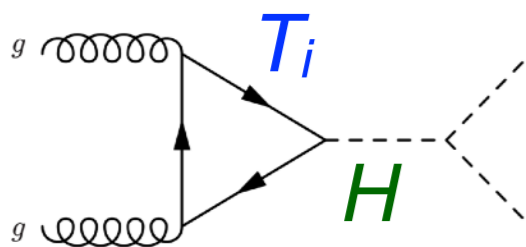
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Resonant case



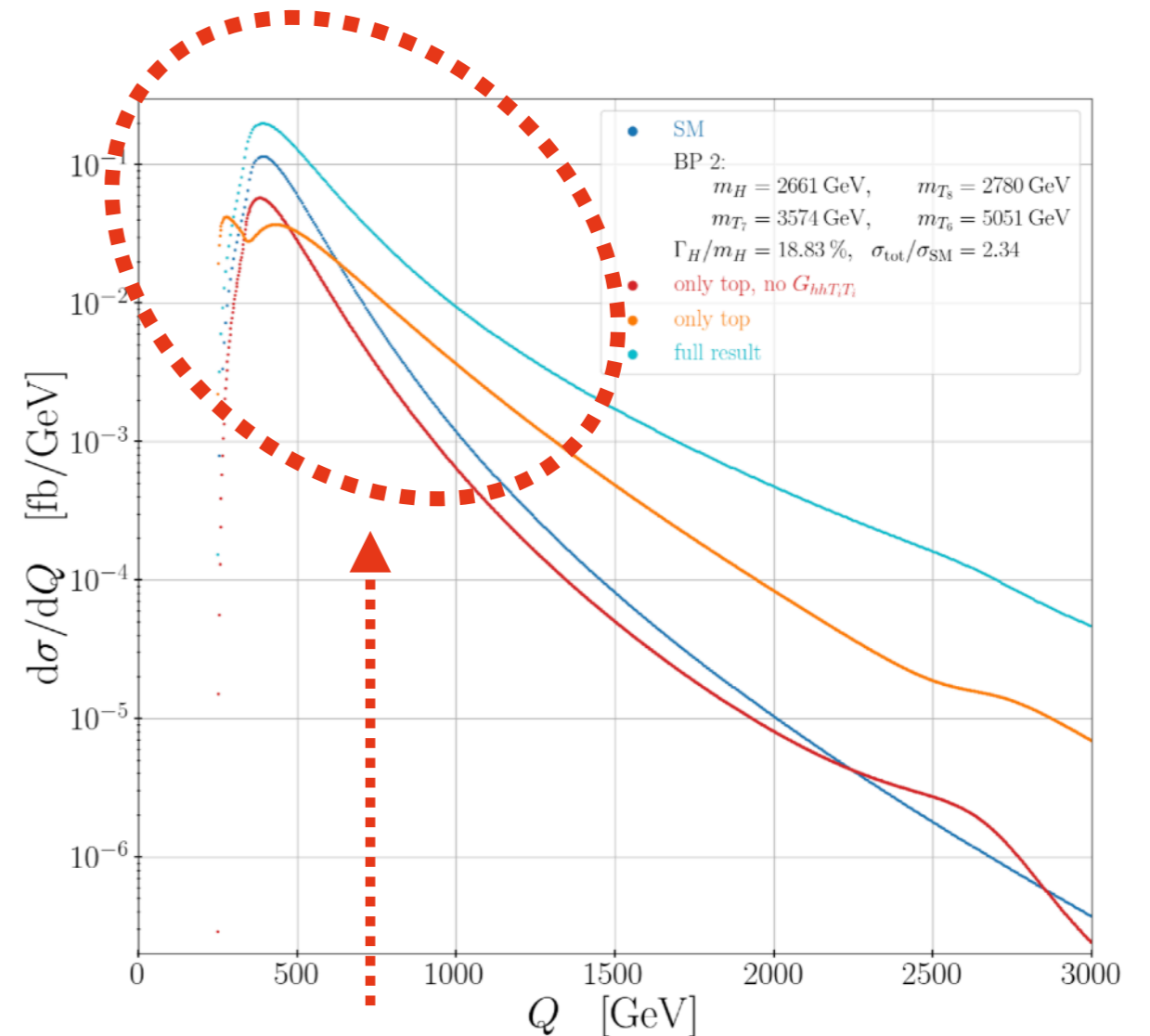
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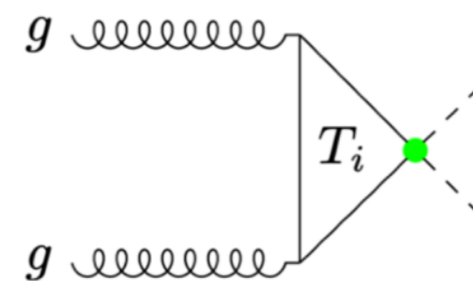


Nonresonant case

[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



Enhancement in low mass



Large $G_{hhT_iT_i}$
 (doesn't vanish
 in $Q \gg v.$)

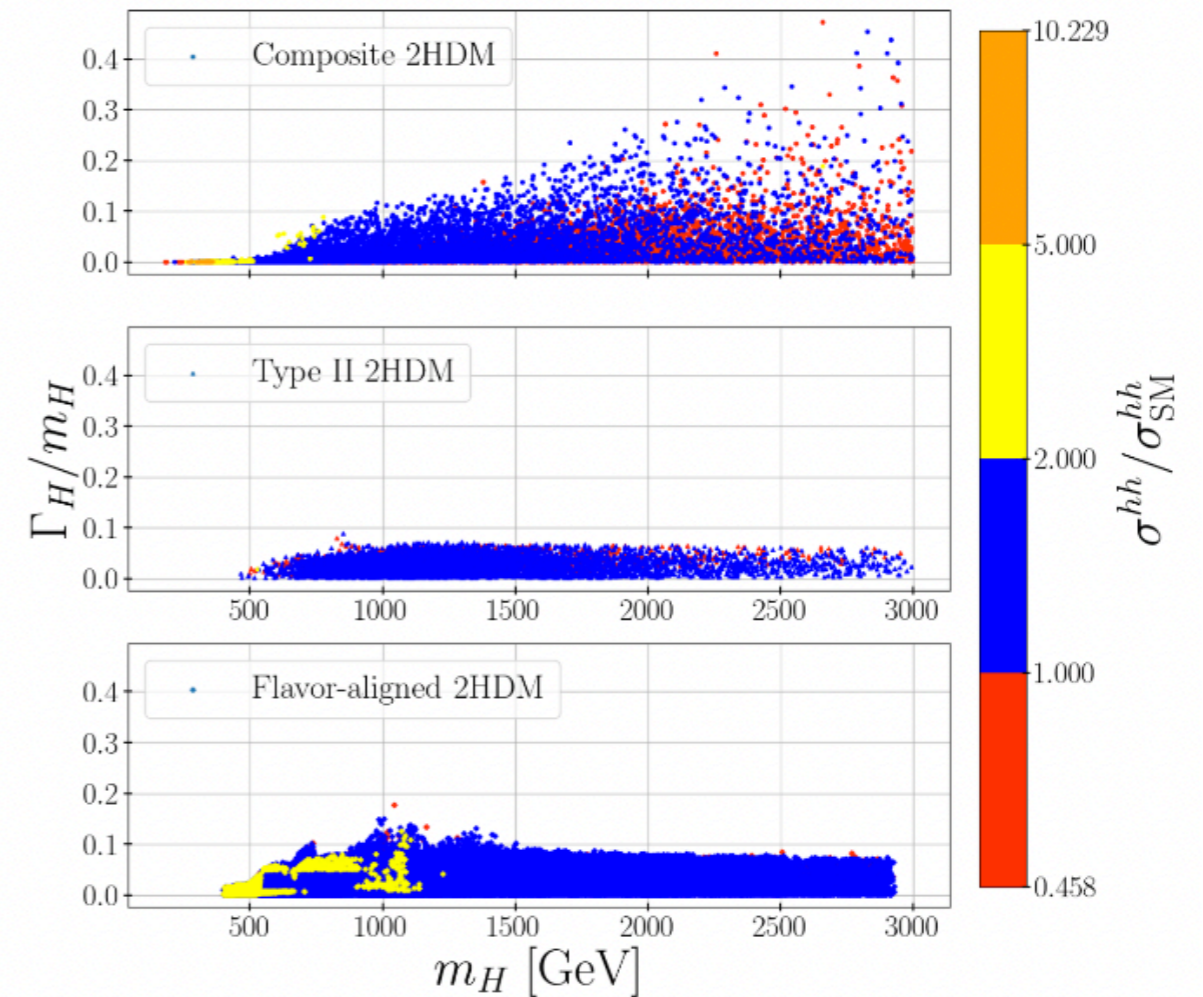
Comparison with elementary 2HDM

Maximum of $\sigma^{H_1 H_1}$ [JHEP09(2022)011]

	H_1	$\frac{\sigma^{H_1 H_1}}{\sigma_{SM}}$
R2HDM-I	444	~ 12
R2HDM-II	81	~ 2

Decay width of H

[De Curtis, Delle Rose, Egle, Mühlleitner, Moretti, KS]



- The maximum of the σ_{C2HDM}^{hh} is close to type-I.
- Γ_H^{C2HDM} glows in $m_H \gg v$ because of $H \rightarrow tT_i$.

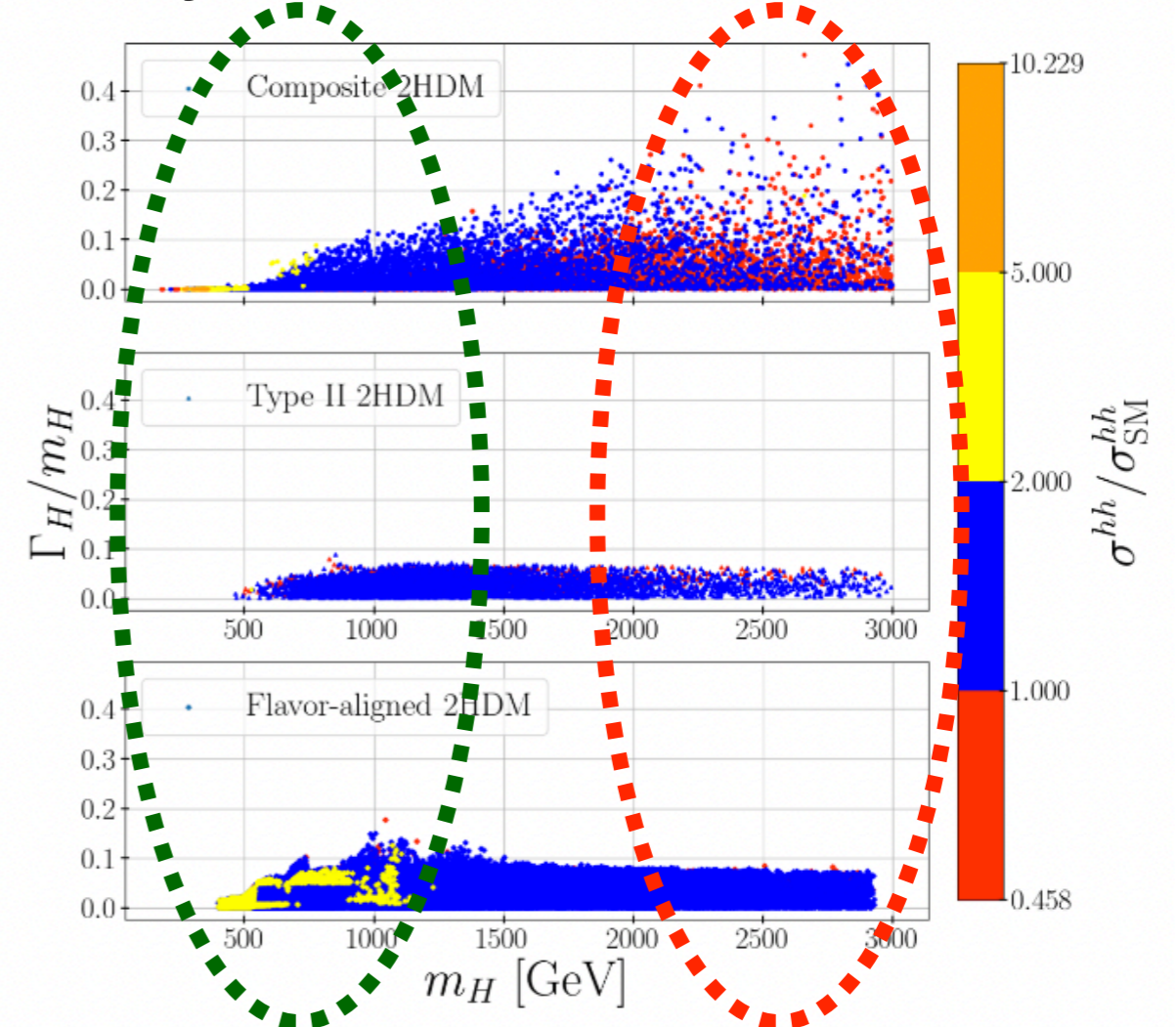
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Decay width of H

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- The maximum of the σ_{C2HDM}^{hh} is close to type-I.
- Γ_H^{C2HDM} glows in $m_H \gg v$ because of $H \rightarrow tT_i$.

➔ Difference in σ^{hh} or in Γ_H may distinguish C2HDM from E2HDM

Summary

- We studied di-Higgs production process in C2HDM.
- Heavy CP-even Higgs (H) and heavy top partner (T_i) give additional contributions to the process.
- These two effects are basically complementary. They become important in different parameter spaces.
- By precision measurements of di-Higgs production, one can get a clue to find compositeness.

Back up

Effective lagrangian

For $pp \rightarrow hh$, interactions for top and Higgs are only needed.

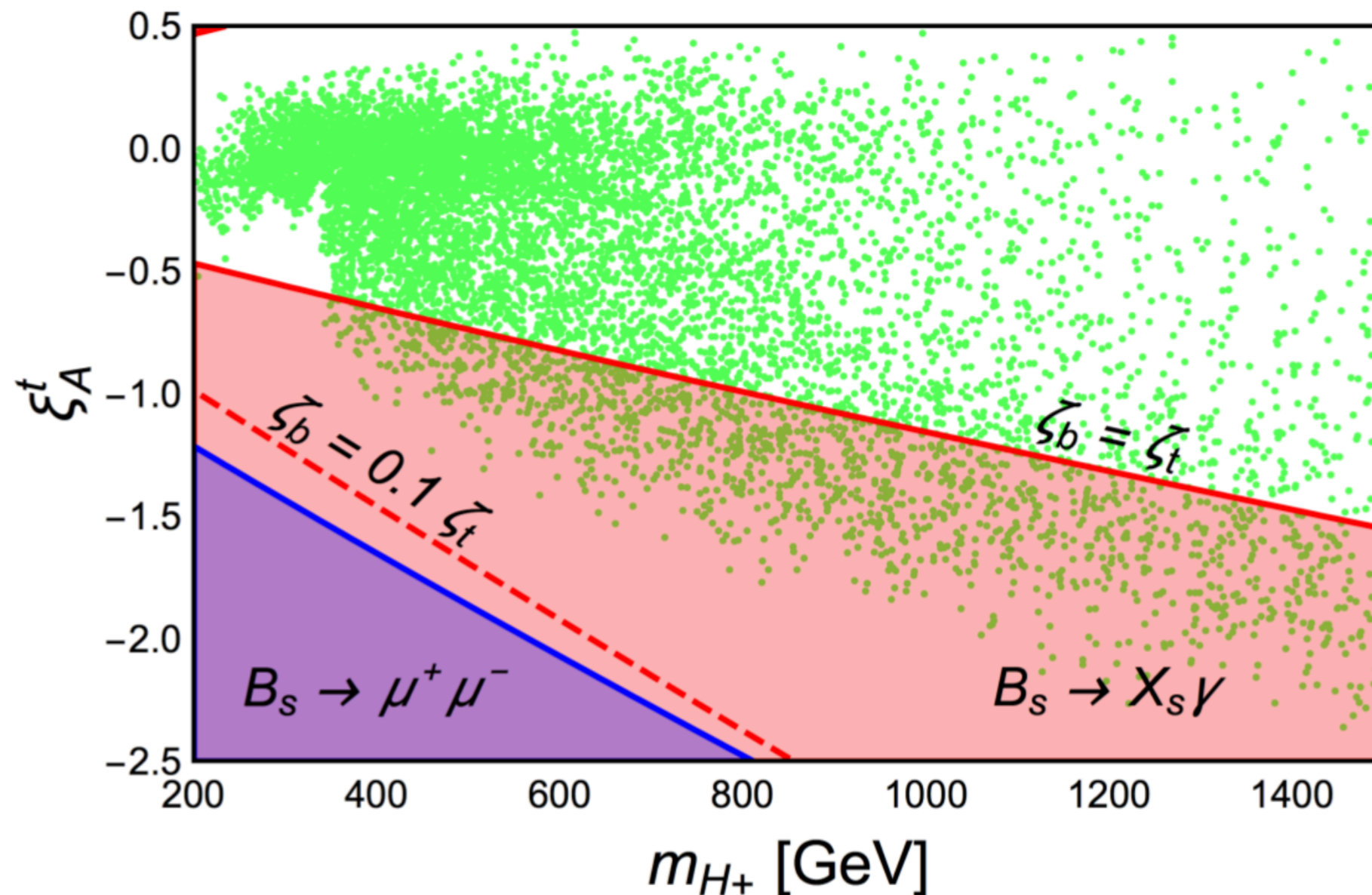
$$\begin{aligned}\mathcal{L}_{\text{Yuk}} = & -G_{h\bar{T}_i T_j} \bar{T}_{Li} T_{Rj} h - G_{H\bar{T}_i T_j} \bar{T}_{Li} T_{Rj} H + \text{h.c.} \\ & - \underline{G_{hhT_i T_i} \bar{T}_i T_i h^2} - \underline{G_{HHT_i T_i} \bar{T}_i T_i H^2} + \dots ,\end{aligned}$$

$$\begin{aligned}\mathcal{L}_{\text{scalar}}^{\text{int}} = & -\frac{1}{3!} \lambda_{hhh} h^3 - \frac{1}{2} \lambda_{hhH}^{(1)} h^2 H \\ & + \frac{v}{3f^2} (s_\theta \partial_\mu h + c_\theta \partial_\mu H) (H \partial^\mu h - h \partial^\mu H) + \dots , \\ & \underline{\equiv \lambda_{hhH}^{(2)} hhH + \lambda_{hHH}^{(2)} hHH}\end{aligned}$$

The couplings G_{hhTT} , G_{HHTT} , $\lambda_{hhH}^{(2)}$, $\lambda_{hHH}^{(2)}$ appears due to nonlinearities.

$b \rightarrow s \gamma$ constraint

[S. De Curtis, et al, JHEP 12 (2018) 051]



- Green points are allowed by current direct and indirect searches at the LHC.
- By taking $\xi_b = 0.1 \xi_t$, the constraint becomes weaker.

Lagrangian of the strong sector for spin-1/2 resonances Ψ_I

$$\mathcal{L}_{\text{strong}}^{\text{ferm}} + \mathcal{L}_{\text{mix}}^{\text{ferm}} = \bar{\Psi}^I i \not{D} \Psi^I + [-\bar{\Psi}_L^I M_{\Psi}^{IJ} \Psi_R^J - \bar{\Psi}_L^I (Y_1^{IJ} \Sigma + Y_2^{IJ} \Sigma^2) \Psi_R^J + (\Delta_L^I \bar{q}_L^{\mathbf{6}} \Psi_R^I + \Delta_R^I \bar{t}_R^{\mathbf{6}} \Psi_L^I)] + \text{h.c.},$$

$$\Sigma = U \Sigma_0 U^T$$

$$U = e^{i \frac{\Pi}{f}}, \quad \Pi \equiv \sqrt{2} \phi_i^{\hat{a}} T_i^{\hat{a}} = -i \begin{pmatrix} 0_{4 \times 4} & \mathbf{\Phi} \\ -\mathbf{\Phi}^T & 0_{2 \times 2} \end{pmatrix}, \quad \Phi_i = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi_i^{\hat{2}} + i \phi_i^{\hat{1}} \\ \phi_i^{\hat{4}} - i \phi_i^{\hat{3}} \end{pmatrix}.$$

$$q_L^{\mathbf{6}} = \frac{1}{\sqrt{2}} \begin{pmatrix} i b_L \\ b_L \\ i t_L \\ -t_L \\ 0 \\ 0 \end{pmatrix}, \quad t_R^{\mathbf{6}} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ c_{\theta_t} \\ i s_{\theta_t} \end{pmatrix} t_R, \quad \Psi = \begin{pmatrix} \psi_4 \\ \psi_2 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} i B_{-1/3} - i X_{5/3} \\ B_{-1/3} + X_{5/3} \\ i T_{2/3} + i X_{2/3} \\ -T_{2/3} + X_{2/3} \\ \sqrt{2} \tilde{T}_1 \\ \sqrt{2} \tilde{T}_2 \end{pmatrix},$$

- To ensure the finiteness of the effective potential, two species of Ψ_i are needed.
- The mixing angle θ_t is chosen as $\theta_t = 0$ to insure the CP conservation.

Lagrangian of the gauge sector

$$\mathcal{L}_{\text{C2HDM}}^{\text{gauge}} = \frac{f_1^2}{4} \text{Tr} |D_\mu U_1|^2 + \frac{f_2^2}{4} \text{Tr} |D_\mu \Sigma_2|^2 - \frac{1}{4g_\rho^2} (\rho^A)_{\mu\nu} (\rho^A)^{\mu\nu} - \frac{1}{4g_{\rho_X}^2} (\rho^X)_{\mu\nu} (\rho^X)^{\mu\nu} \\ - \frac{1}{4g_A^2} (A^A)_{\mu\nu} (A^A)^{\mu\nu} - \frac{1}{4g_X^2} X_{\mu\nu} X^{\mu\nu},$$

$$D_\mu U_1 = \partial_\mu U_1 - iA_\mu U_1 + iU_1 \rho_\mu, \quad \rho_\mu \equiv \rho_\mu^A T^A + \rho_\mu^X T^X \\ D_\mu \Sigma_2 = \partial_\mu \Sigma_2 - i[\rho_\mu, \Sigma_2], \quad A_\mu \equiv A_\mu^A T^A + X_\mu T^X$$

ρ_A and ρ_X are spin-1 resonances

T_A and T_X are generator of SO(6) and U(1)_X

Scan range of the composite parameters

$$f = [700, 3000] \text{ GeV}, \quad g_\rho = [2, 10]$$
$$\Delta_{L,R}^I = [-10, 10] \times f, \quad Y_{1,2}^{IJ} = [-10, 10] \times f$$

Branching ratios of the heavy Higgs boson H

