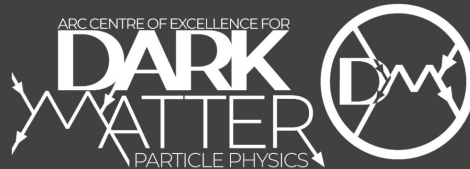


The Migdal effect for dark matter detection

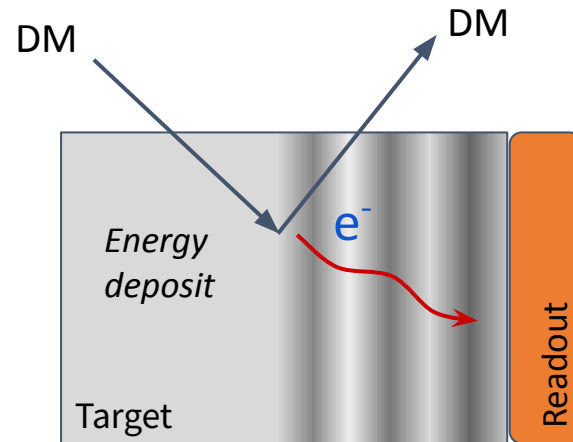
CYGNUS Workshop,
The University of Sydney
Dec. 2023

Jayden Newstead



Direct detection fundamentals

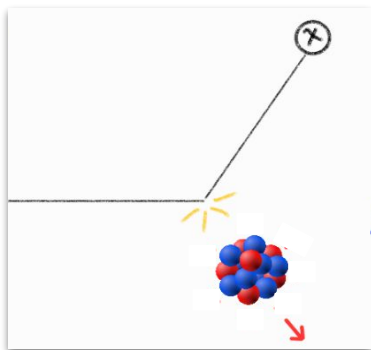
- Look for signals of dark matter from the galactic halo scattering off nuclei or electrons in a detector
- Kinetic energy of recoil deposited as:
 - Scintillation
 - Ionization
 - Phonons
- This is read out via PMT's, current, TES, imaging



The Migdal effect allows us to probe lighter dark matter, which would otherwise fall below threshold



Direct detection's kinematic problem



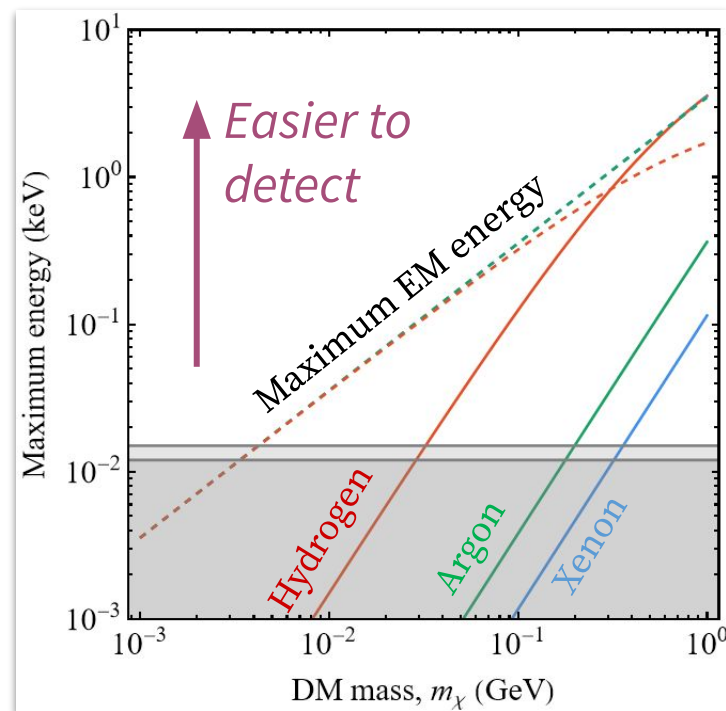
$$E_{R_{\max}} = \frac{2\mu_T^2}{m_T} v_{\max}^2$$

$$E_{EM_{\max}} = \frac{\mu_T}{2} v_{\max}^2$$

$$E_{R_{\max}} \approx \frac{m_\chi^2}{m_T} \times 10^{-5}$$

$$E_{EM_{\max}} \approx m_\chi \times 10^{-5}$$

→ Light dark matter does not pack much of a punch



* assuming $v_{\max} = 800$ km/s

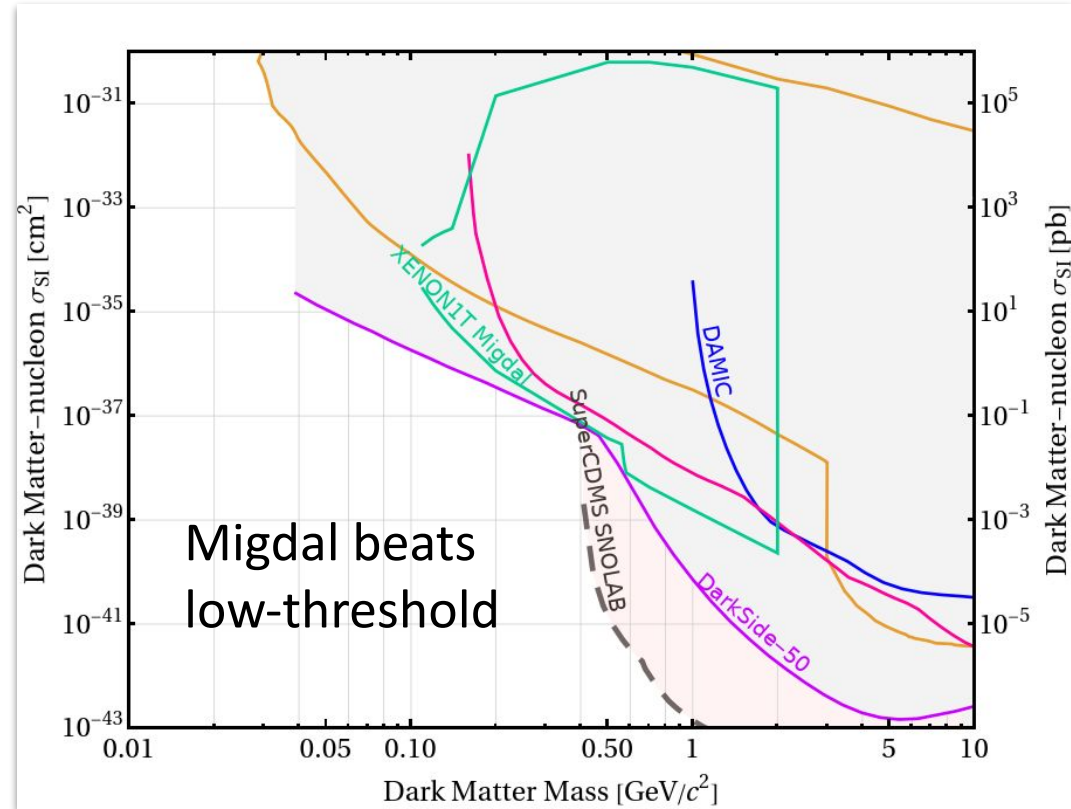
Future of direct detection

Present/near term:

- XENONnT: 5 tonne x 4 years (Xe)
- LZ: 5.5 tonnes x 1000 days (Xe)
- PandaX-4T: 3.7 tonnes x 2 years
- SuperCDMS: 81 (25) kg.years Ge (Si)

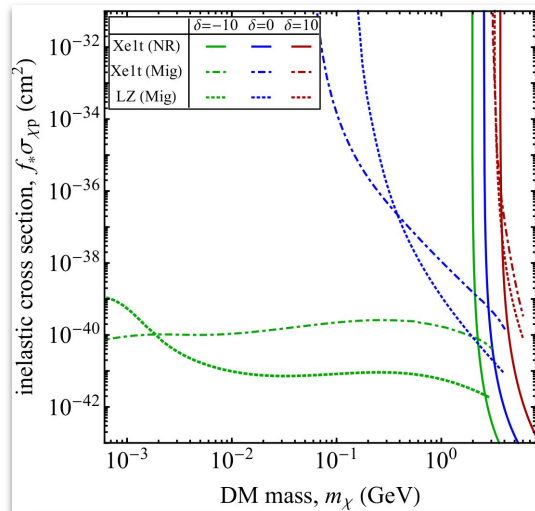
Future:

- DarkSide-20k: 20t x 5 years (Ar), 2026+
- XLZD: 40t x 10 years (Xe), 2027+
- Argo: 300t x 10 years



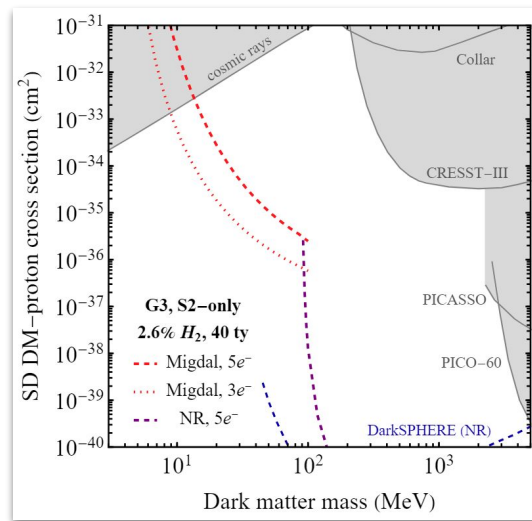
What can we do with the Migdal Effect?

Migdal from inelastic DM:



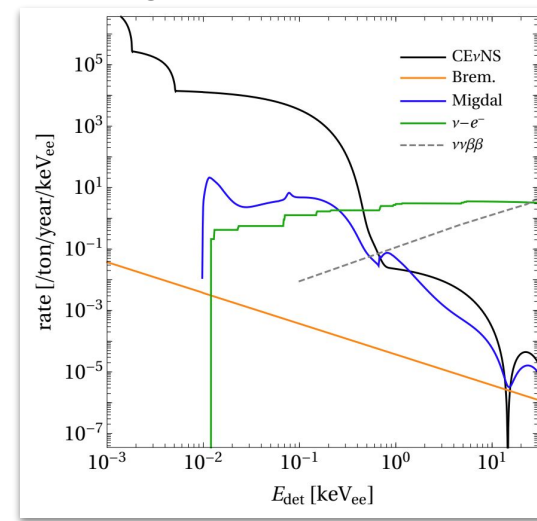
Bell, Dent, Dutta, Kumar, **JLN**
[arXiv:2103.05890](https://arxiv.org/abs/2103.05890)

Migdal + Hydrogen-doping:



N. Bell, P.Cox, M.Dolan, **JLN**, A.Ritter
[arXiv:2305.04690](https://arxiv.org/abs/2305.04690)

Migdal from neutrinos

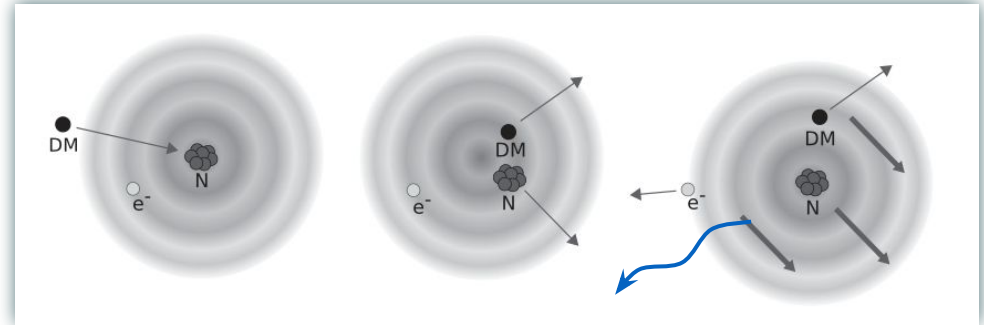


N. Bell, Dent, **JLN**, Sabharwal, Weiler
[arXiv:1905.00046](https://arxiv.org/abs/1905.00046)



The Migdal Effect

- The Migdal effect is atomic ionization or excitation due to a nuclear recoil
- ‘Electron shakeoff’ has been observed during nuclear decay, but not due to scattering (see for example: *Couratin et al. Phys. Rev. Lett.* **108** (2012))
 - **Agreement with theory is mixed**



Credit: Dolan et al. PRL 2017



A brief history of the Migdal effect

1939: A.B. Migdal, J. Phys. USSR 4 449

1958: Landau and Lifshitz Vol. 3: Quantum Mechanics, sec. 41:

PROBLEM 2. The nucleus of an atom in the normal state receives an impulse which gives it a velocity v ; the duration τ of the impulse is assumed short in comparison both with the electron periods and with a/v , where a is the dimension of the atom. Determine the probability of excitation of the atom under the influence of such a “jolt” (A. B. MIGDAL 1939).

(A. B. *Мигдал*, 1939).

2005: First application to DM detection:

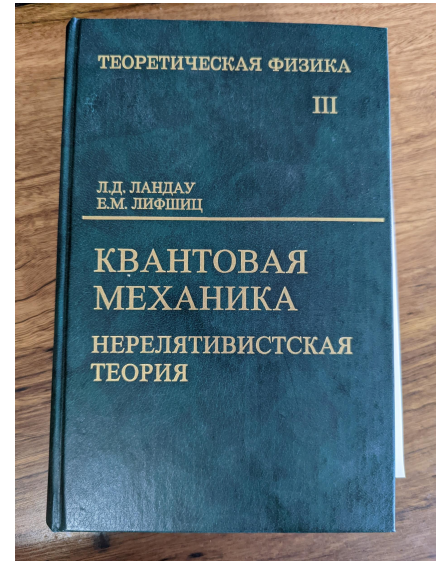
J.D. Vergados and H. Ejiri, *Phys. Lett. B* 606, 313, [arXiv:hep-ph/0401151](https://arxiv.org/abs/hep-ph/0401151)

2018: First detailed atomic calculations for DM:

M. Ibe, W. Nakano, Y. Shoji and K. Suzuki, *JHEP* 1803 (2018) 194 [arXiv:1707.07258](https://arxiv.org/abs/1707.07258)

2018: First experimental constraints:

M. Dolan, F. Kahlhoefer and C. McCabe *Phys. Rev. Lett.* 121 (2018) [arXiv:1711.09906](https://arxiv.org/abs/1711.09906)



Ionization probabilities

What goes into the rate calculation?

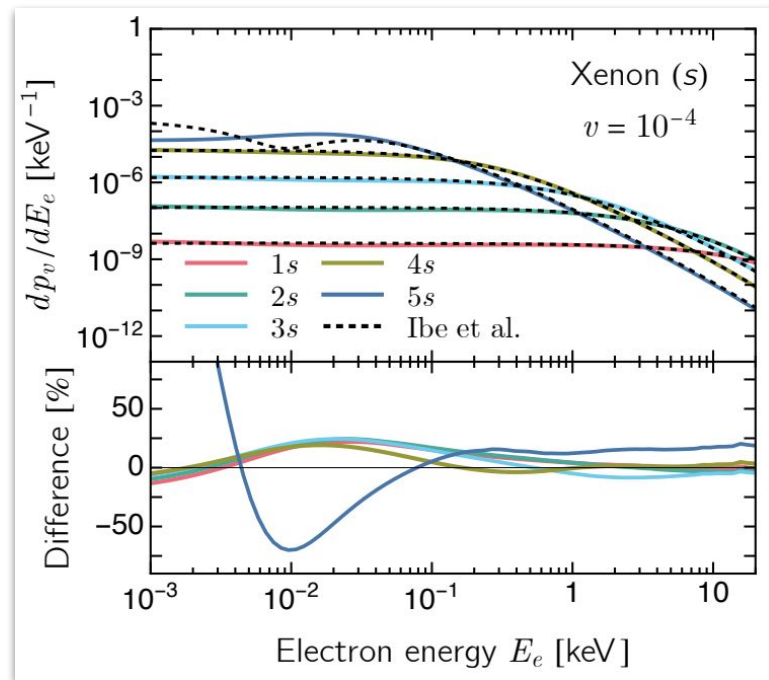
$$\frac{d^2 R}{dE_{\text{NR}} dE_i} = \frac{d^2 R_{iT}}{dE_{\text{NR}} dE_i} \times |Z_{\text{ion}}|^2$$

$$|Z_{\text{ion}}|^2 = \frac{1}{2\pi} \sum_{n,\ell} \int dE_e \frac{d}{dE_e} p_{q_e}^c(nl \rightarrow (E_e))$$

Ionization prob.

Relevant matrix elements obtained by boosting the electronic wavefunction:

$$\left\langle \Psi_f \left| \exp \left(i m_e \mathbf{v} \cdot \sum_{k=1}^N \mathbf{r}_k \right) \right| \Psi_i \right\rangle$$



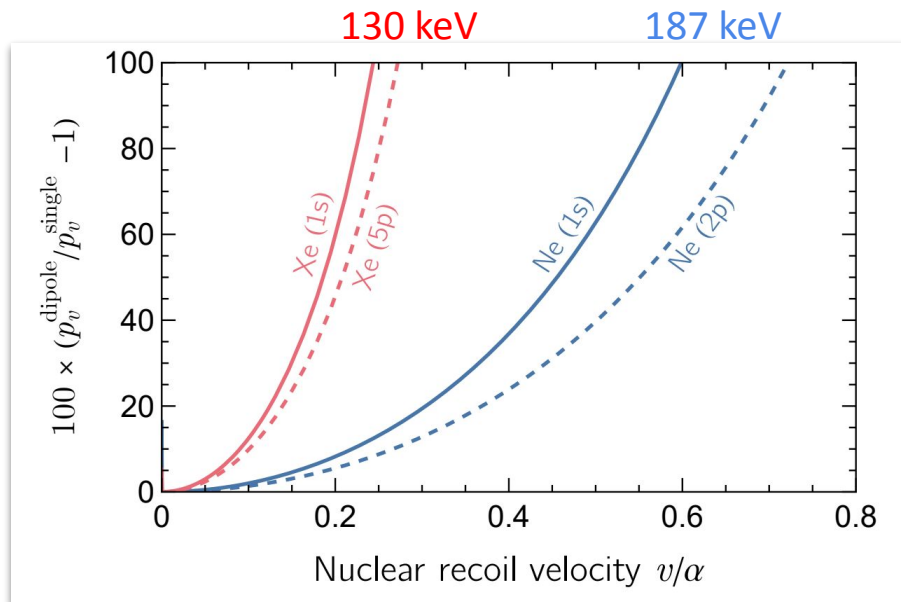
Cox et al. Phys.Rev.D 107 (2023)

[arXiv:2208.12222](https://arxiv.org/abs/2208.12222)

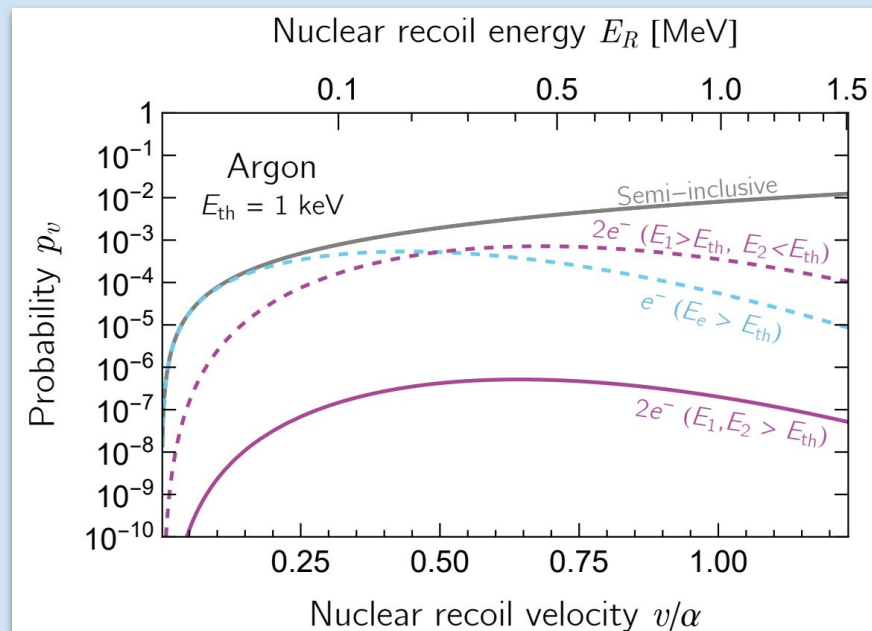


Ionization probabilities cont.

i) Dipole approx is fine for DM, but breaks down rapidly

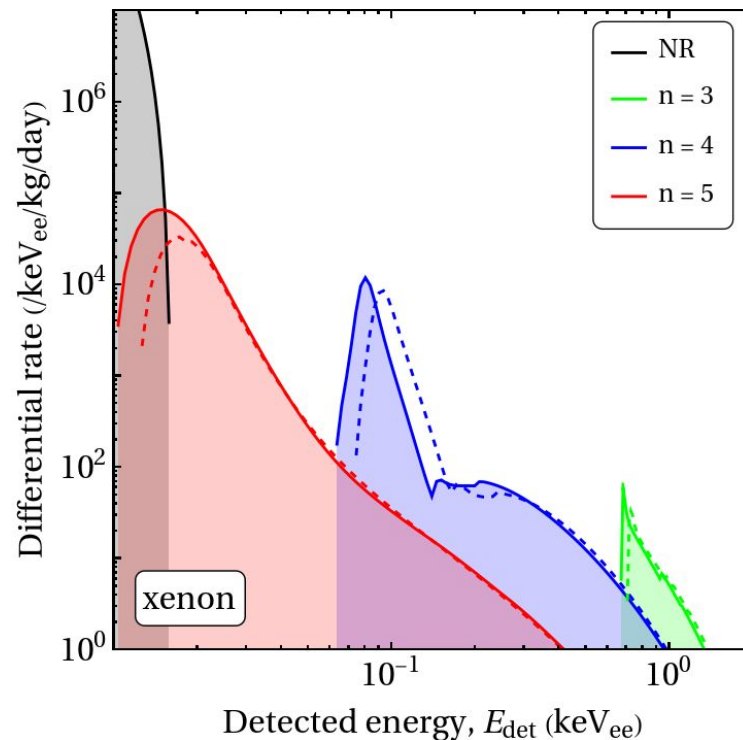
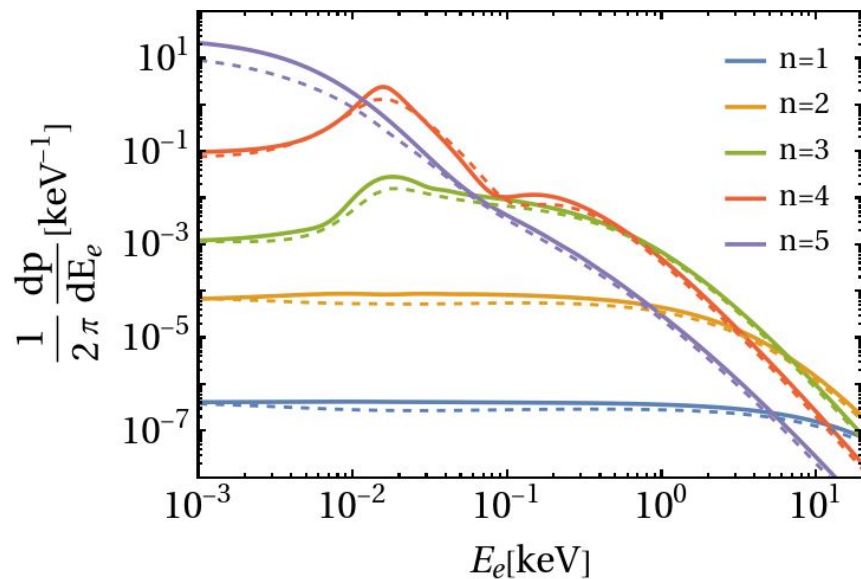


ii) Single electron is fine for DM



Ionization probabilities: Cox (dashed) vs. Ibe (solid)

Difference mostly from shifted ionization energies

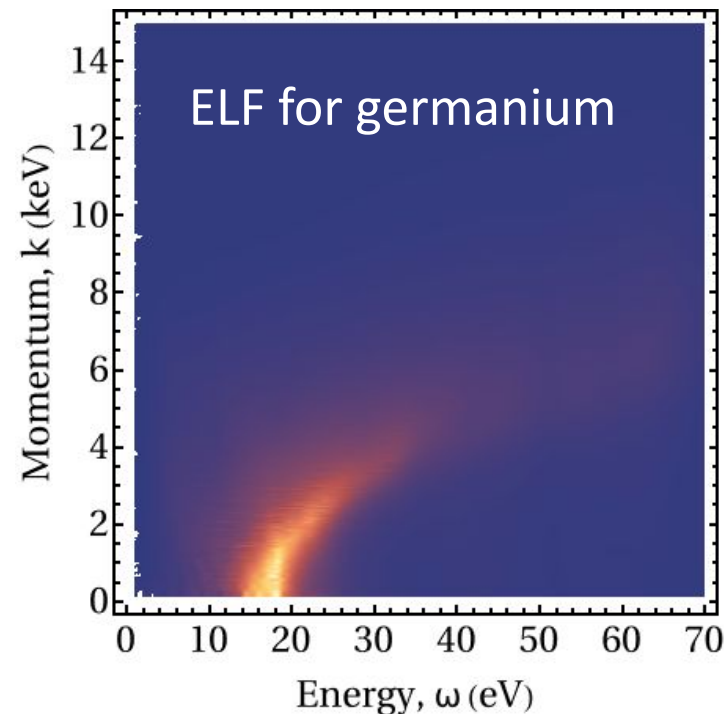
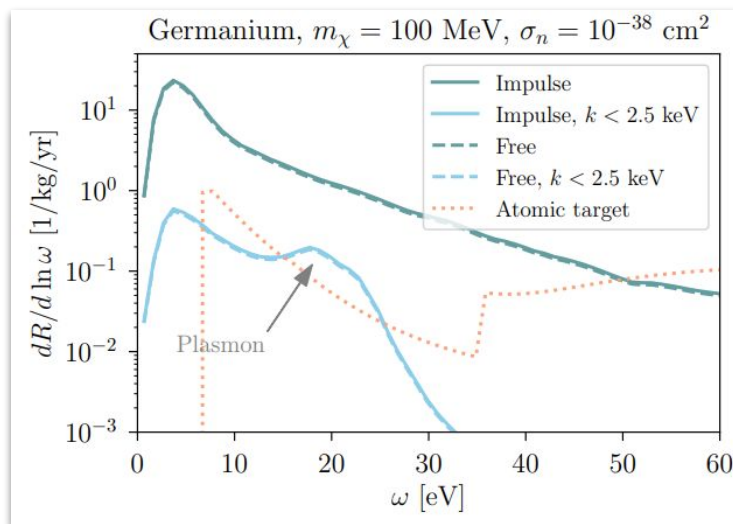


Ionization probabilities in semiconductors

When the atom is not isolated things are more complicated

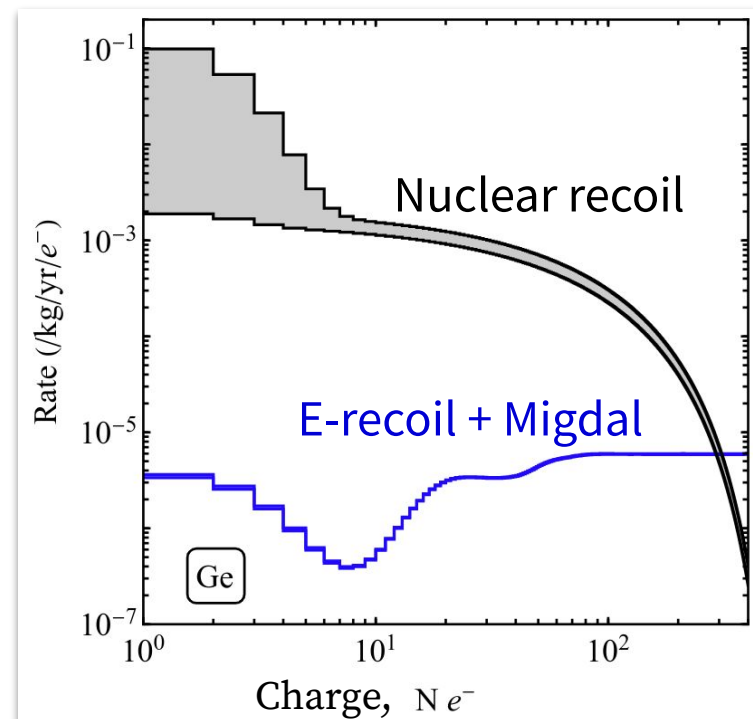
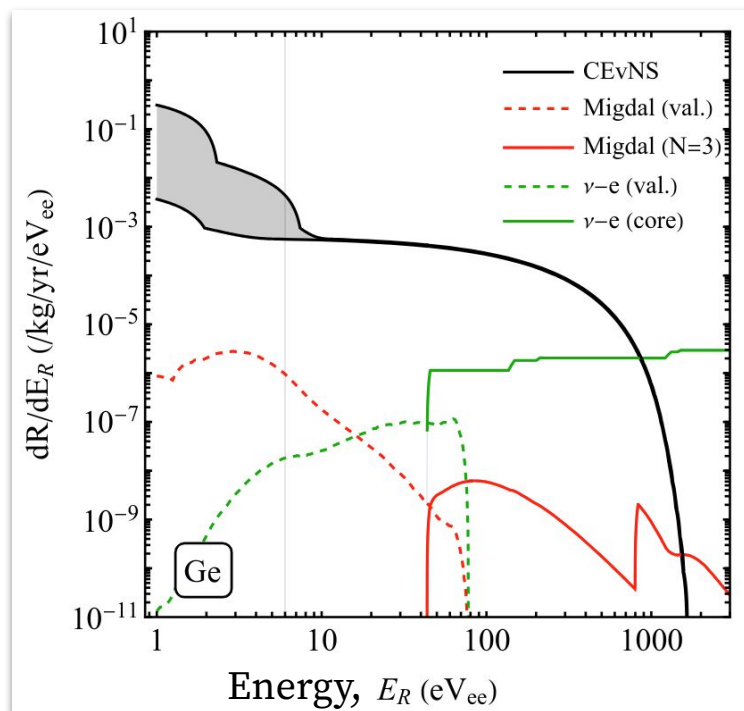
Energy loss function

$$\frac{dP}{d\omega} = 4\alpha \int \frac{d^3\mathbf{k}}{(2\pi)^3} \frac{Z_{\text{ion}}^2(k)}{k^2} \text{Im} [-\epsilon_{00}^{-1}(\mathbf{k}, \omega)] \frac{|\mathbf{v}_N \cdot \mathbf{k}|^2}{\omega^4}.$$



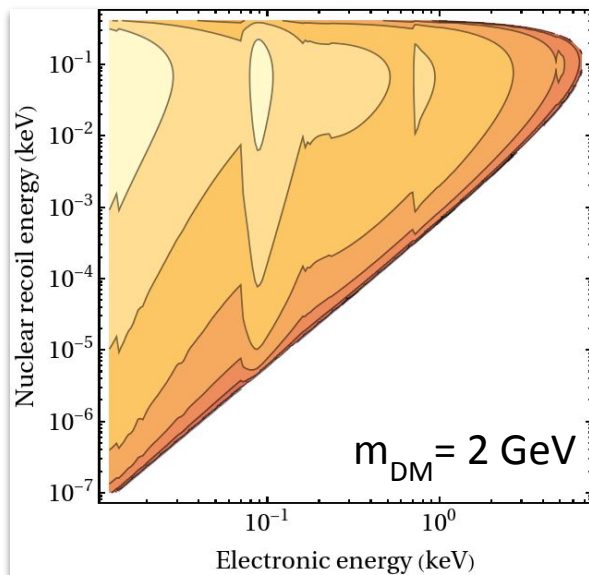
From the [DarkELF package](#), calculated with DFT (GPAW)

Neutrino rates in semiconductors

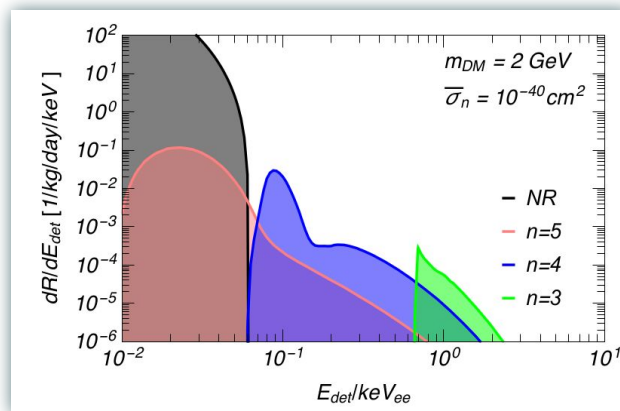


What does a Migdal event look like?

Energy deposited:

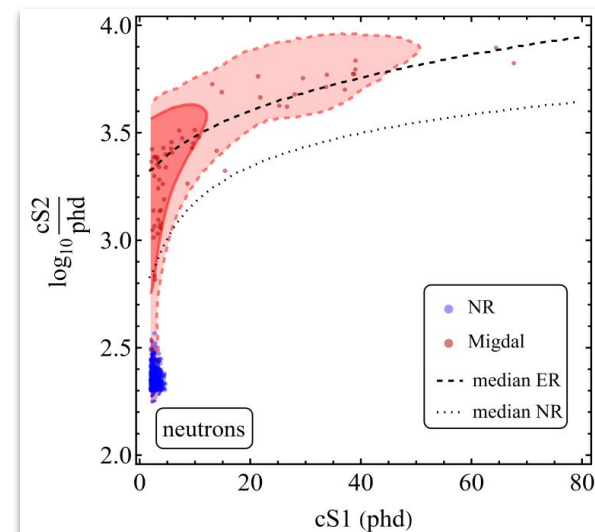


Energy deposited w quenching:



$$E_{det} = \mathcal{L}E_R + E_e + E_{nl}$$

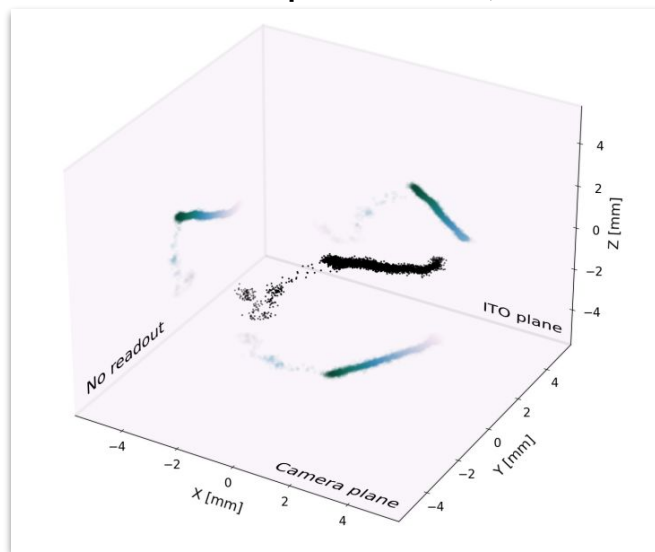
Detector modelling, e.g.:



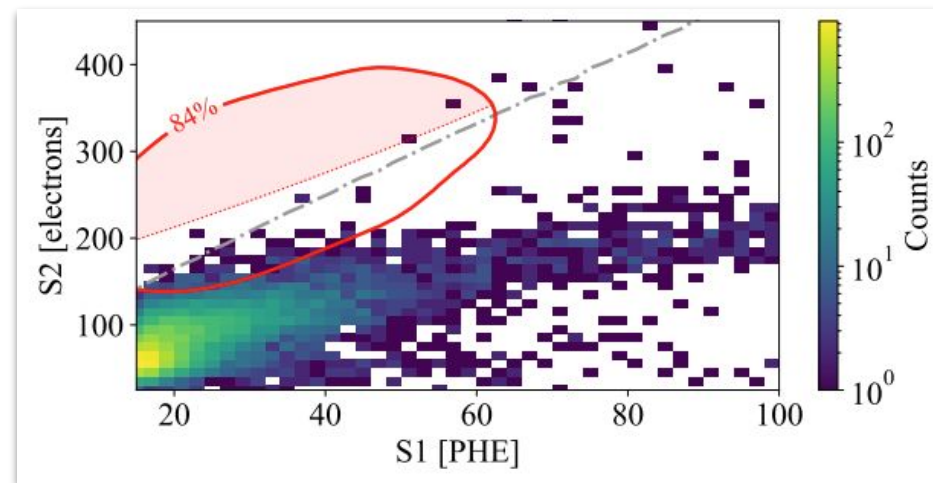
Calibrating the Migdal effect (in LXe TPCs)

Two experimental goals:

1. Verify theoretical predictions:
The MIGDAL experiment (see next talk)

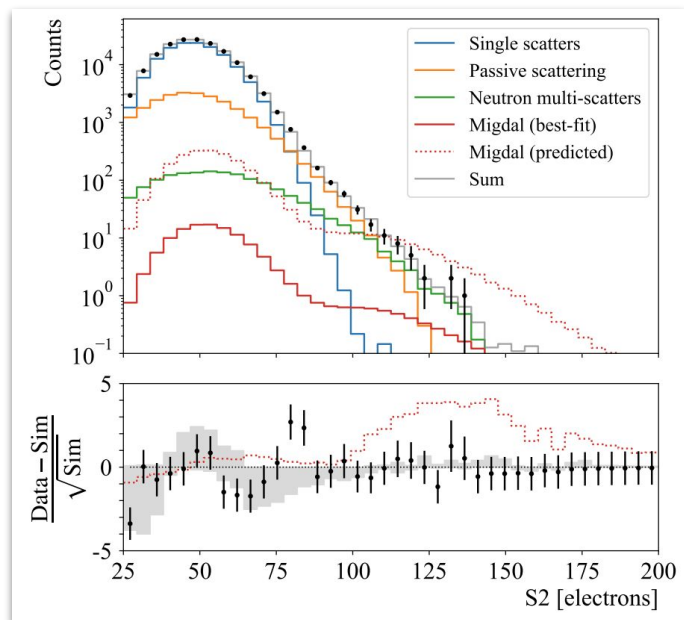


2. Calibrate detector response

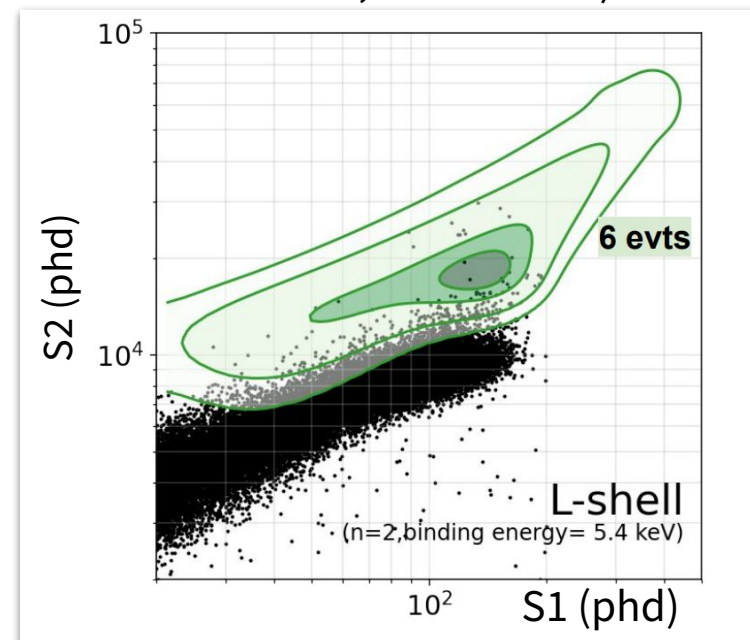


Calibrating the detector response to the Migdal effect

Livermore group dedicated measurement
(DT generator 14 MeV neutrons, 7 keV NR):



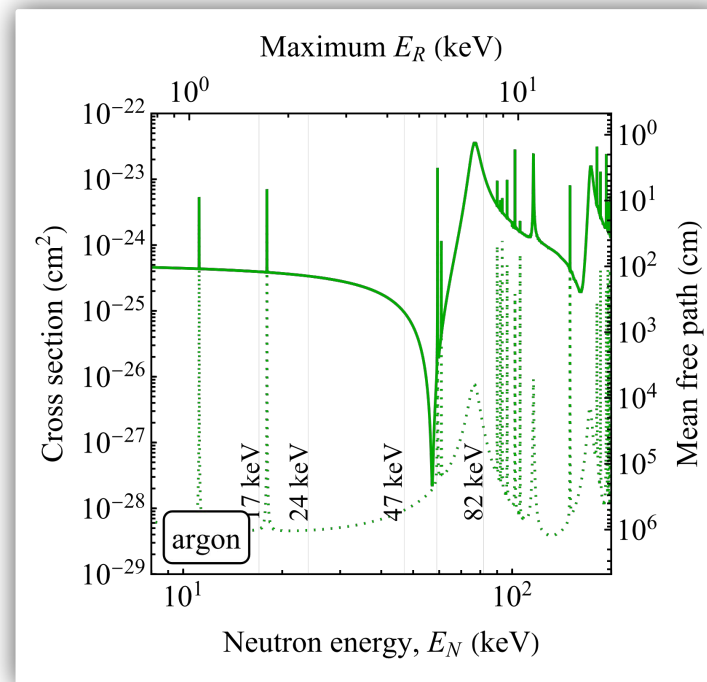
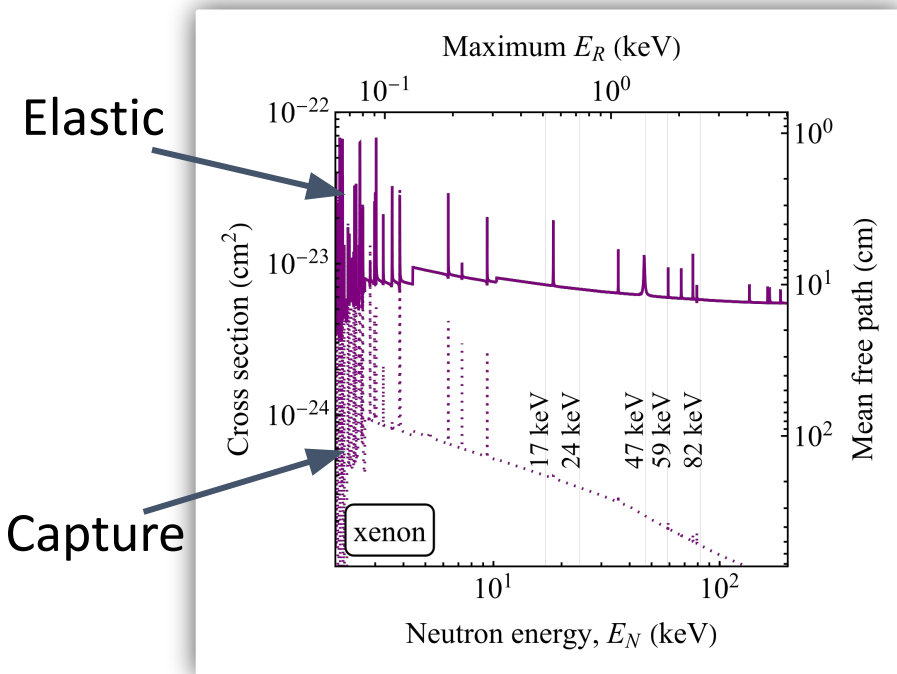
LZ *in situ* measurement (DD generator
2.45 MeV neutrons, >20 keV NR):



Xu et al. [arXiv:2307.12952](https://arxiv.org/abs/2307.12952)

Bang (LZ Collaboration) [UCLADM2023 talk](#)

Low-energy neutron cross sections

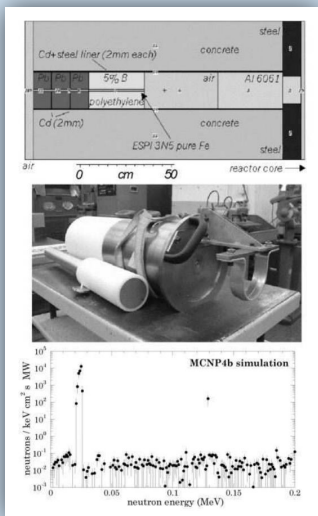


- Radiative capture of neutrons will be a significant background
- Inelastic scattering is >100 keV threshold for all but xenon-129



Potential low-energy neutron sources

Nuclear reactor + filter



Pros:

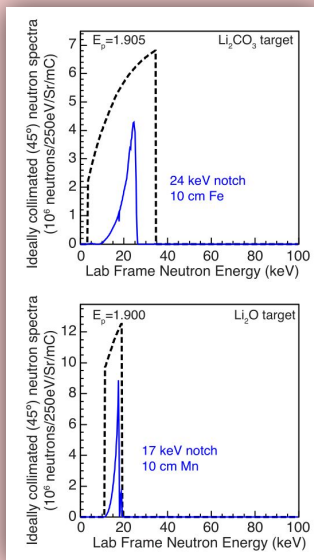
- Large flux
- Continuous operation

Cons:

- Gamma backgrounds
- Location

Barbeau et al. [arXiv:nucl-ex/0701011](https://arxiv.org/abs/0701011)

Li + p near threshold + filter



Pros:

- Pulsed beam

Cons:

- May require large/cooled targets
- Location

Joshi et al. [arXiv:1403.1285](https://arxiv.org/abs/1403.1285)

DT/DD-generator + measure recoil angle

14 MeV

The diagram shows a vertical arrow pointing down labeled '14 MeV'. A dashed vertical line extends from the tip of the arrow. A solid arrow points downwards and to the right from the tip of the dashed line, representing the recoil angle measurement.

Pros:

- Potential for in situ

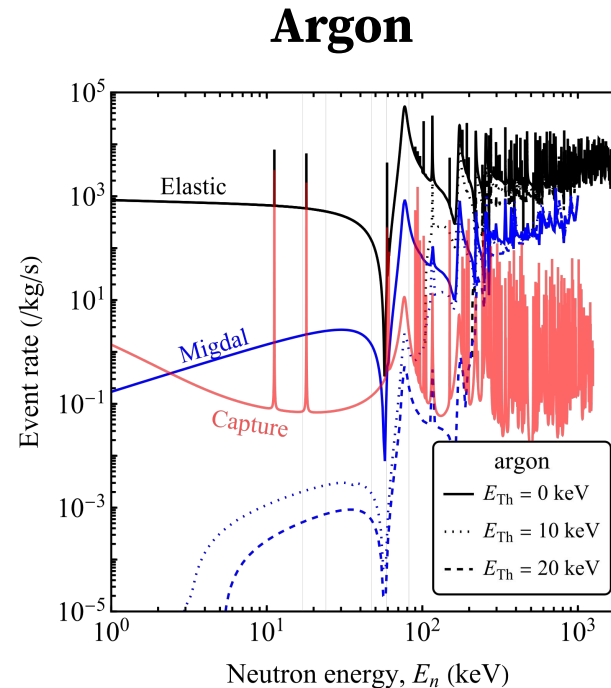
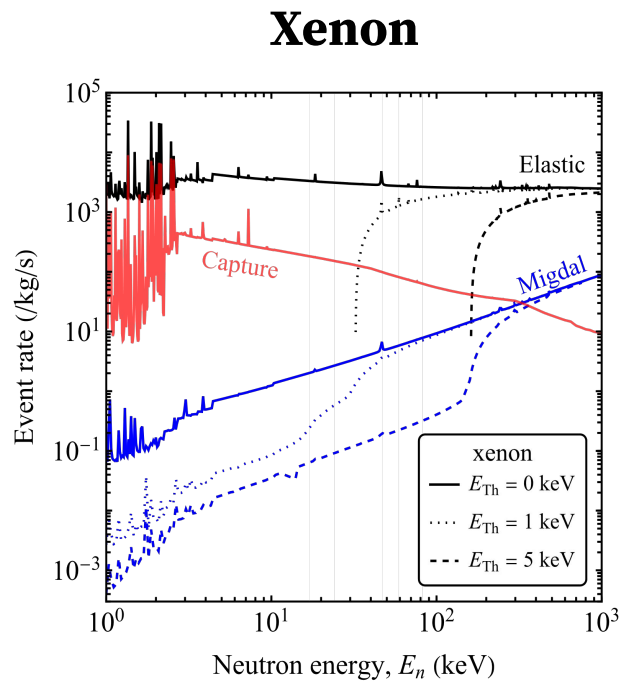
Cons:

- Small flux

Xu et al. [arXiv:2307.12952](https://arxiv.org/abs/2307.12952)

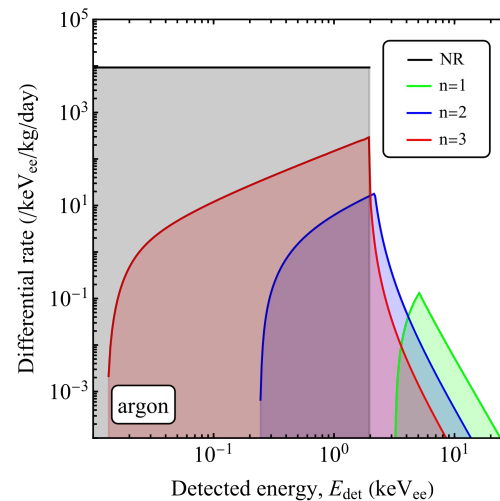
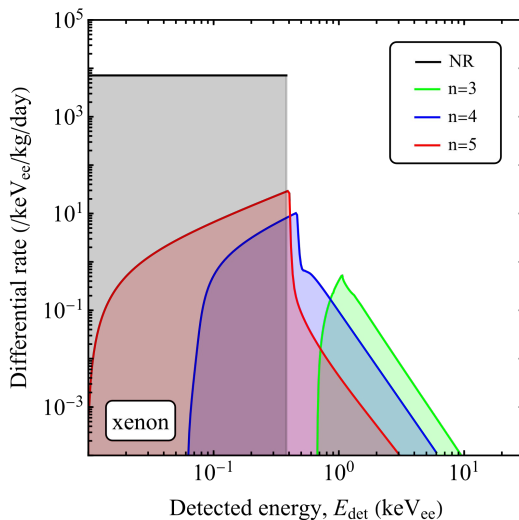


Low-energy neutron scattering rates



Low-energy neutron Migdal rates

$E = 82 \text{ keV}$ neutrons, flux = $100 \text{ n/cm}^2/\text{s}$



Total rates:

Nuclear: 2,700 events/kg/s

Migdal: 8 events/kg/s

12,300 events/kg/s

320 events/kg/s

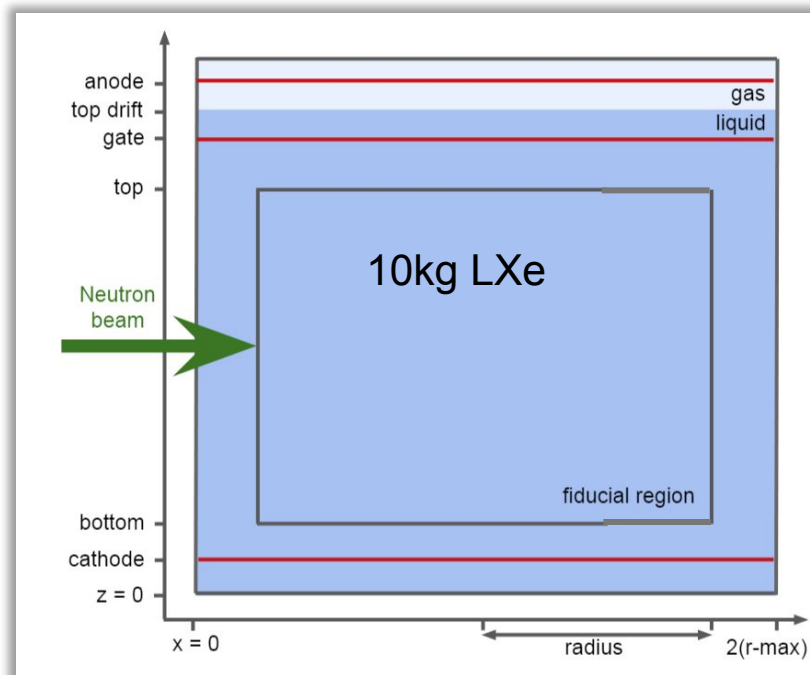


Simulation of LXe detector and neutron beam

Gaussian
neutron beam:

FWHM = 6cm
Peak flux = 10^8 n/hr
(avg 100 n/cm²/s)

Modelled on Barbeau
et al.



dimension	position (mm)
r_{\max}	120.
radius	100.
cathode	20.0
bottom	40.0
top	160.
gate	190.
top drift	195.
anode	200.

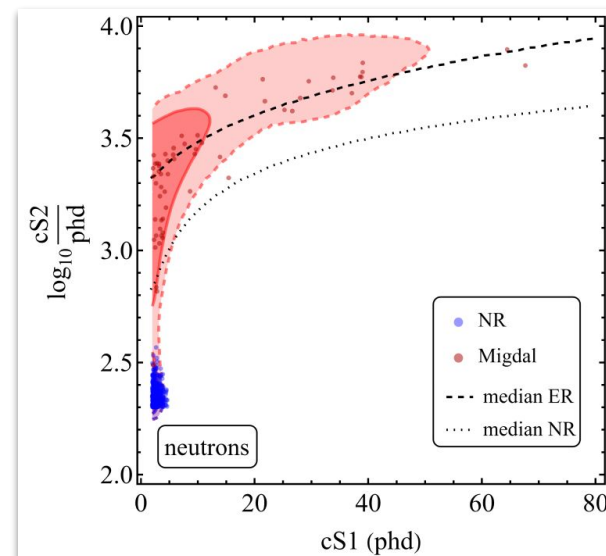
parameter	value
g_1	0.15 PE/ γ
g_2	24 PE/ e^-
field	300 V/cm
e^- lifetime	350. μ s
min S1	2 phd
min S2	250 phd
no. PMTs	60



Simulation with NEST (xenon)

Monte Carlo procedure:

1. Random NR energy from E_R distribution, calculate max. allowed E_{EM}
2. Loop over atomic shells, E_{nl} , and randomly ionize an electron with E_e
3. Calculate the yields of ions and excitons produced by E_R , E_e and E_{nl} using models for NR, β and β respectively
4. Calculate the quanta from the summed yields and the subsequent S1 & S2

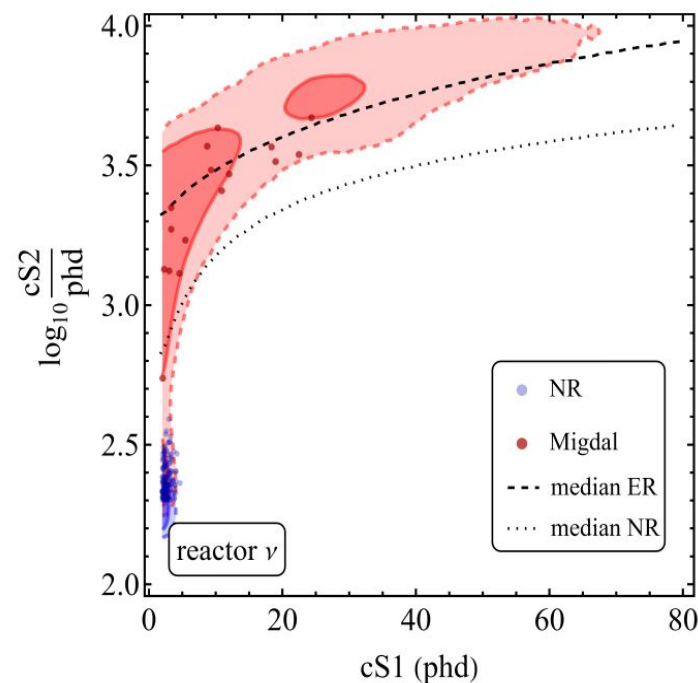
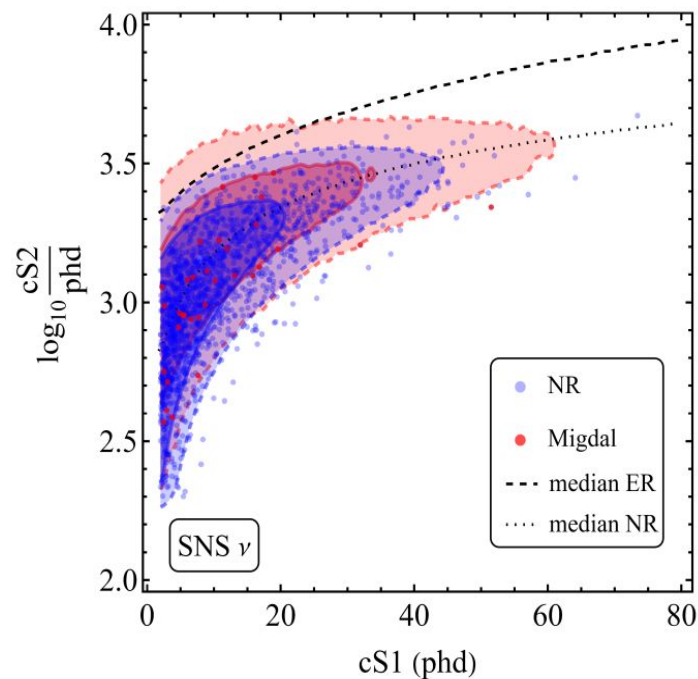


Source	Calc. ratio	Sim. ratio	Sim. rate/kg/day
neutron (17 keV)	6.0×10^{-4}	0.1	600
reactor neutrinos	1.7×10^{-4}	0.1	4.3×10^{-4}
SNS neutrinos	1.5×10^{-2}	0.02	8.8×10^{-3}
^{51}Cr neutrinos	5.4×10^{-6}	∞	8.2×10^{-6}

→ Neutrons are the only viable candidate



Migdal from low-energy neutrino sources



Directional Migdal Effect?

- **Isolated atoms:**

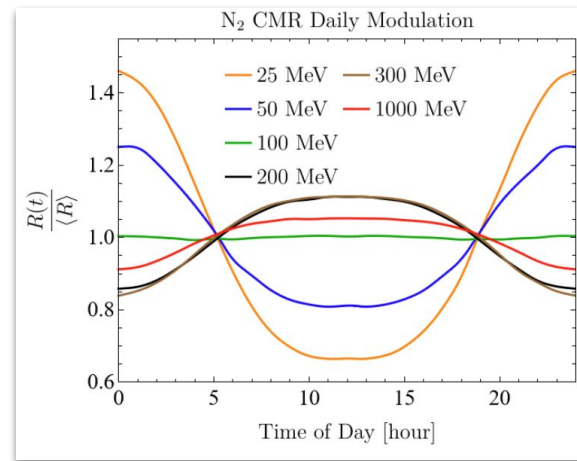
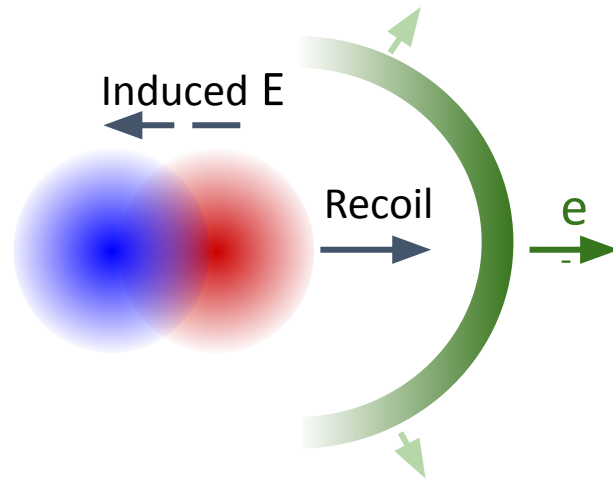
The nuclear recoil creates a dipole - the electron is preferentially emitted in direction of recoil (see e.g. from [alpha decay](#))

- **Molecular:**

Ionization prob. depends on molecular axis \rightarrow indirect/statistical directional information (see [Blanco et al.](#))

- **Condensed matter:**

The dielectric function has angular dependence \rightarrow indirect/statistical directional information



Summary

- The Migdal effect allows access the lighter DM
- It's important to both verify experimental predictions *and* calibrate detector responses
- Directional nature of the Migdal effect is likely weak, but it should be investigated further

Collaborators:

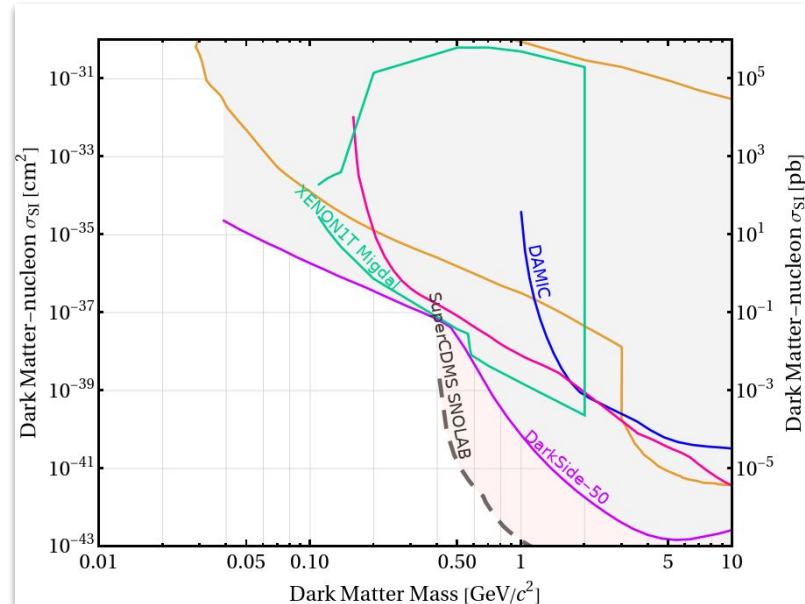
Nicole Bell, Alex Ritter, Peter Cox, Matt Dolan (UniMelb)

James Dent (Sam Houston)

Bhaskar Dutta (TAMU)

Rafael Lang (Purdue)

Jason Kumar (Hawaii)



`~/code$`

<https://zenodo.org/record/5587760>

<https://github.com/jaydenn/nuMigdalCalc>

<https://github.com/jaydenn/thinNEST>

<https://github.com/jaydenn/MigdalMC>



Directional Migdal Effect?

- Predictions for neutron scattering on He**

Single ionization has forward-only e

Double ionization has slight backward e

From: [Pindzola et al J. Phys. B 53 \(2020\)](#)

