

Thermal Effects on Nonthermal Species



Michael Ratz



August 21 2023



Based on:

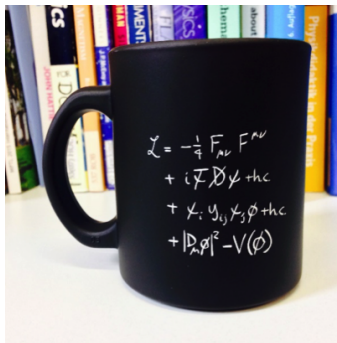
- W. Buchmüller, K. Hamaguchi, O. Lebedev & M.R. Nucl. Phys. B699, 292-308 (2004)
- B. Lillard, M.R., T. Tait & S. Trojanowski JCAP 1807 no. 07, 056 (2018)
- V. Knapp-Pérez, G. Mohlabeng, M.R. & T. Tait, in preparation

Disclaimers and apologies

DISCLAIMERS AND APOLOGIES

- very little citations
- many cartoons

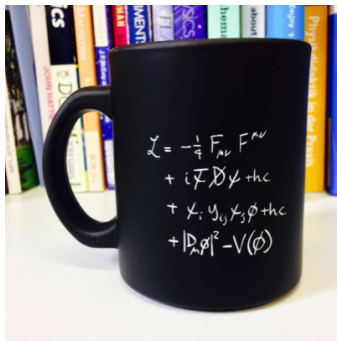
Main message



<https://home.cern/news/news/cern/sit-down-coffee-standard-model>

- ☞ standard model (SM) particles interact via gauge and Yukawa couplings

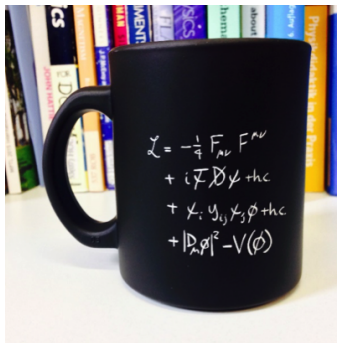
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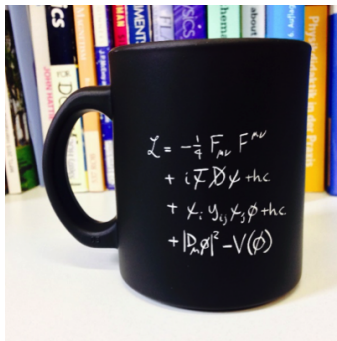
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- ☞ naive picture: equilibrium thermodynamics only concerns equilibrated species

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Main message of this talk

“equilibrium–style” thermodynamics can be particularly important for nonequilibrated species

Overview

- ☞ couplings may not be God-given but consequence of some dynamics

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- ☞ consider field-dependent couplings/masses

$$g = g(S/\Lambda) , \quad y = y(S/\Lambda) \quad \text{and/or} \quad m = m(S) \sim \lambda S$$

weakly coupled scalar (modulus, flavon, dark scalar ...)

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$$\frac{T^3}{\Lambda^2} \ll \frac{T^2}{M_{\text{P}}} \quad \text{for all relevant } T$$

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- in SUSY models often $m_S \sim m_{3/2} \stackrel{?}{\sim} \text{TeV}$

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e.g. [Bauer, Schell & Plehn \(2016\)](#)

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purpose of this talk:

discuss weakly coupled scalars in the hot early universe

Thermal potential

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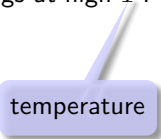
of

weakly coupled scalars

weakly coupled scalars

Main focus of this talk

- ☞ what can we say about field-dependent couplings at high T ?



temperature

Main focus of this talk

☞ what can we say about field-dependent couplings at high T ?

see lectures by Joe Davighi for many more applications of anomalies

☞ one can figure this out using anomalies. . .

☞ [Buchmüller, Hamaguchi & MR \(2003\)](#)

Main focus of this talk

☞ what can we say about field-dependent couplings at high T ?

☞ ... but it is more convenient to consider free energy

☞ Fardon, Nelson & Weiner (2004); ☞ Buchmüller, Hamaguchi, Lebedev & MR (2004); ☞ Lillard, MR, Tait & Trojanowski (2018)

$$\mathcal{F} = \mathcal{F}(T, S)$$

$$\simeq -\frac{\pi^2}{90} g_* T^4 + T^2 \left(\sum_i c_i^{(g)} g_i^2(S) + \sum_f c_f^{(y)} y_f^2(S) + \sum_j c_j^{(m)} m_j^2(S) \right)$$

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gauge factors

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fermions

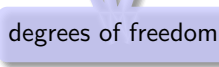
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degrees of freedom

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where

$$c^{(g)} = \frac{T^2}{64\pi^2} (N_c^2 - 1)(N_c + 3N_f) \quad \text{for SU}(N_c)$$

of colors

of flavors

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$$c_j^{(m)} = \frac{1}{24} \quad \text{e.g. if } m_j = h_j S$$

$$\curvearrowright \Delta\mathcal{F} = \frac{|h_j|^2}{24} T^2 S^2 \quad \text{for a boson}$$

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➡ free energy “wants” couplings and masses small

S -dependence of free energy

- dependence of free energy on mass of a boson/fermion

[Dolan & Jackiw \(1974\)](#); [Fardon, Nelson & Weiner \(2004\)](#);... [Batell & Ghalsasi \(2023\)](#)

$$\delta\mathcal{F} = -\frac{\nu}{2\pi^2} T^4 J_{B/F} \left(\frac{m^2(S)}{T^2} \right)$$

#(d.o.f.)

$$J_{B/F}(y^2) = \int_0^{\infty} dx x^2 \ln \left[1 \mp e^{-\sqrt{x^2+y^2}} \right]$$

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- leading contributions to \mathcal{F} from gauge and Yukawa interactions

$$\mathcal{F} = \mathcal{F}_{\text{non-interacting}} + \Delta\mathcal{F}_{\text{gauge}}^{(1)} + \Delta\mathcal{F}_{\text{Yukawa}}^{(1)} + \dots$$

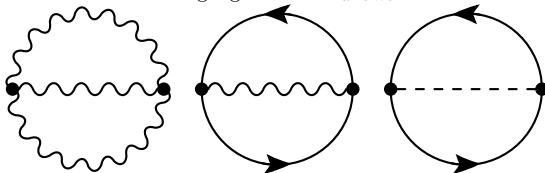
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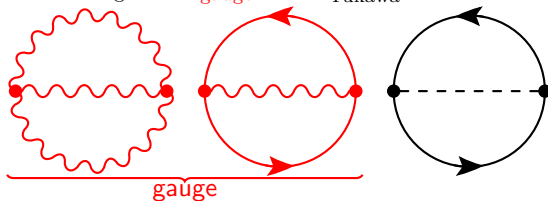
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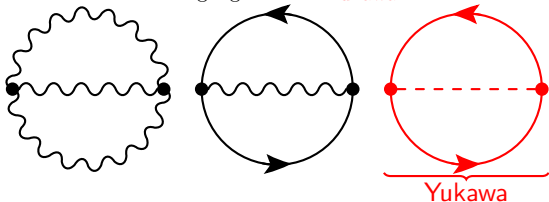
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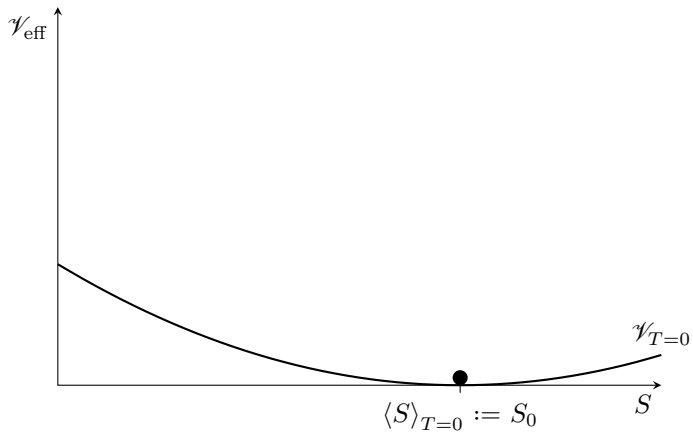
- $\alpha_2 = \frac{3}{196} (N_C^2 - 1) (N_C + 3N_F)$ for $SU(N_C)$ w/ N_F fundamentals

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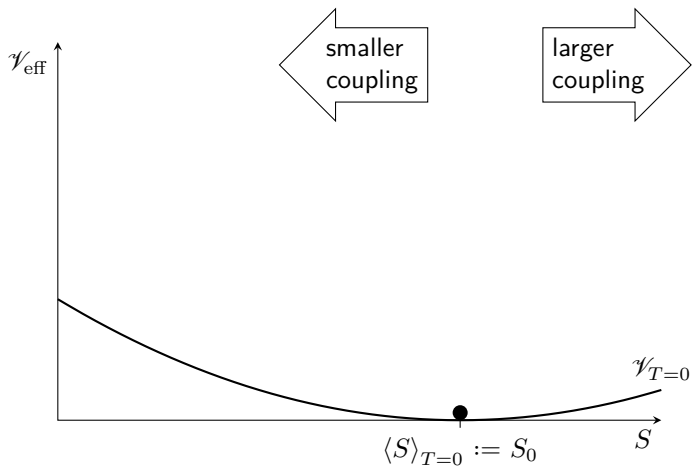
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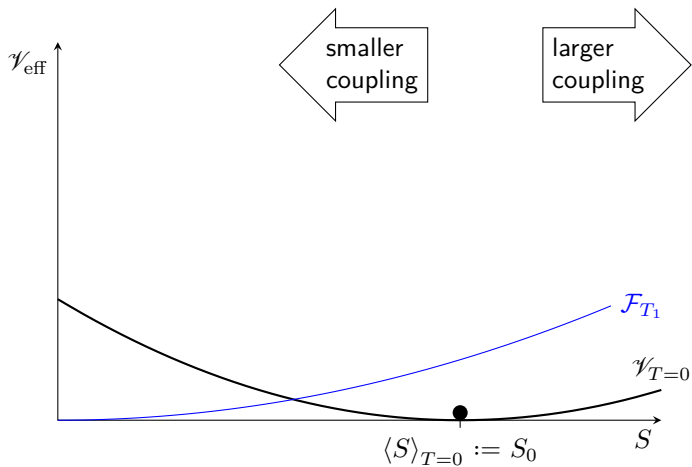
Qualitative discussion



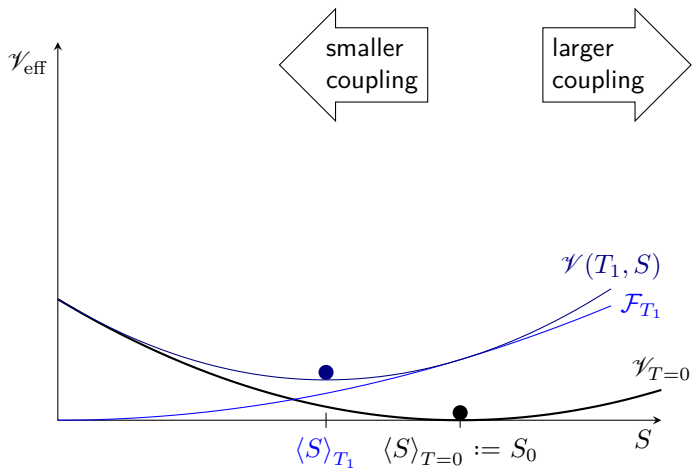
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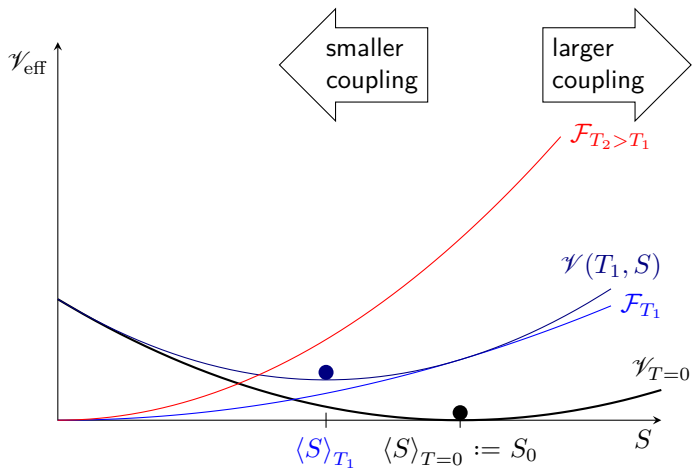
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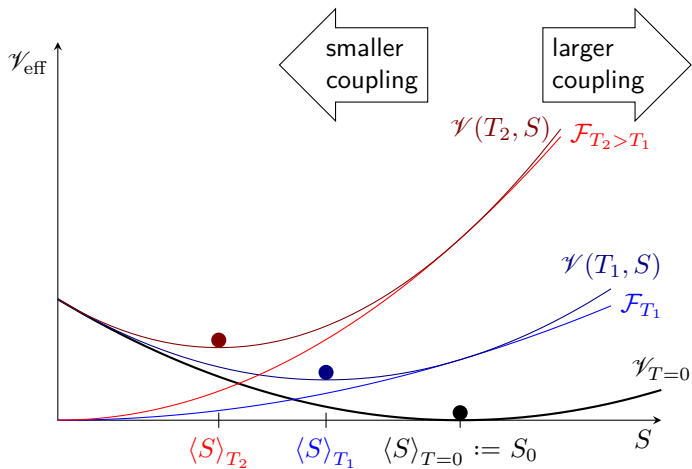
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Implications

☞ couplings at high temperature

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Gauge couplings at high temperature

- common relation between gauge coupling and dilaton

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in strings: $\Lambda = M_{\text{P}}$

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- gauge couplings turn essentially off at T_*

Dilaton destabilization

at

high temperature

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[Buchmüller, Hamaguchi, Lebedev & MR \(2004\)](#)

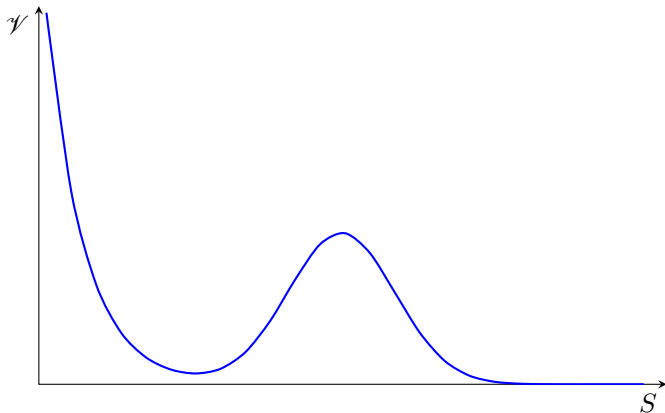
👁 typical dilaton potential: $g^2 = 1/S$

S is real part of stringy dilaton

Dilaton destabilization at high temperature

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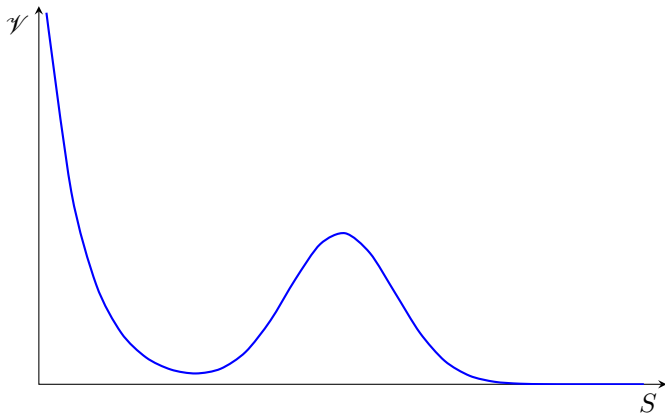
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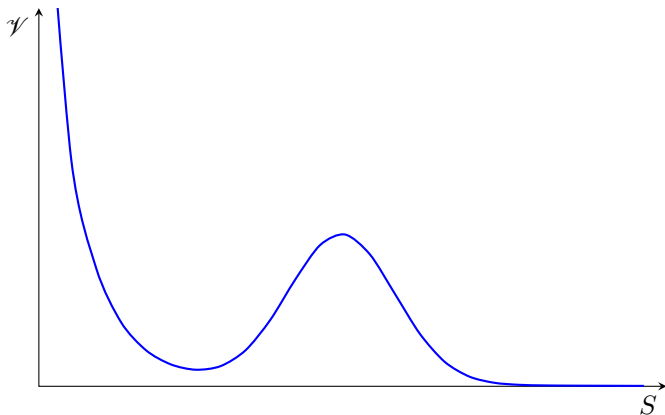


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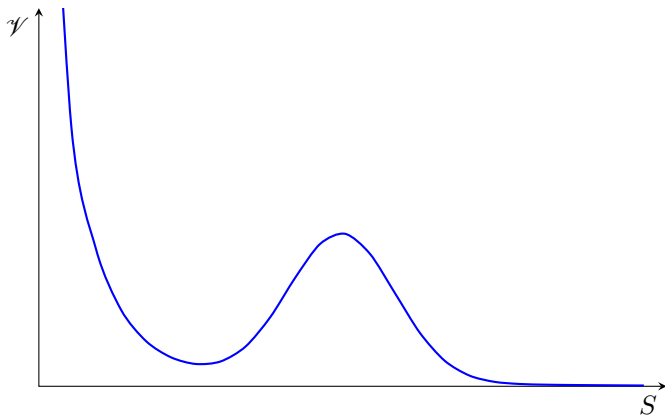


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☞ typical dilaton potential: $g^2 = 1/S$

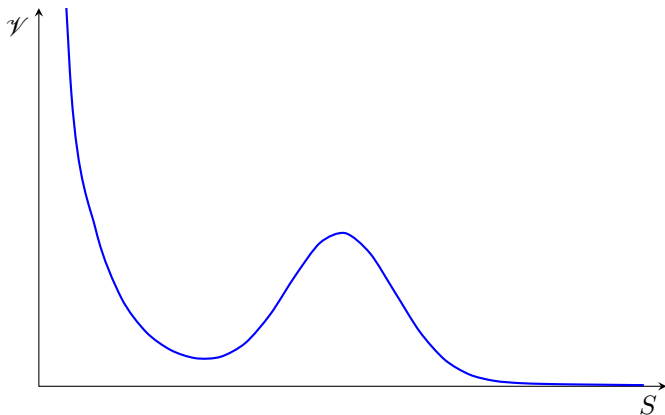


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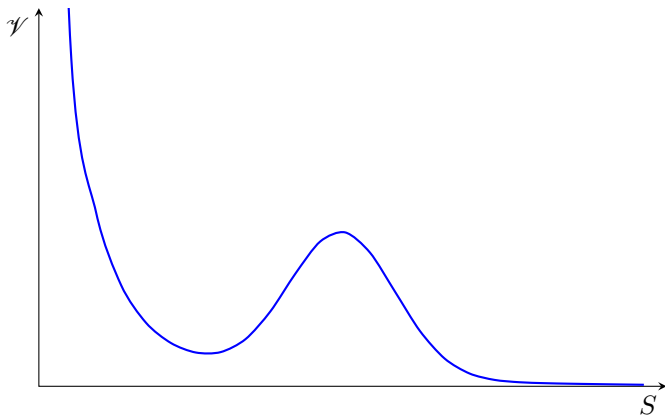


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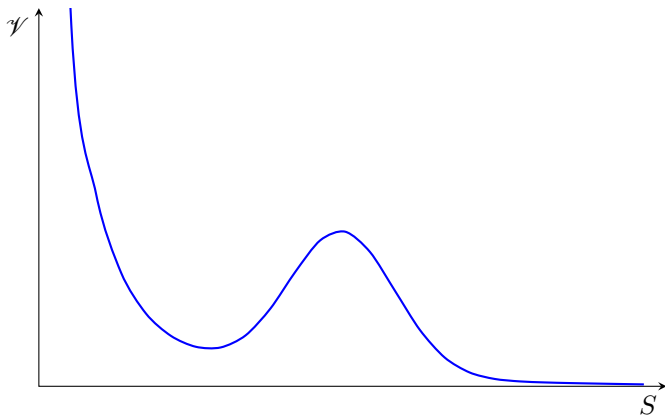


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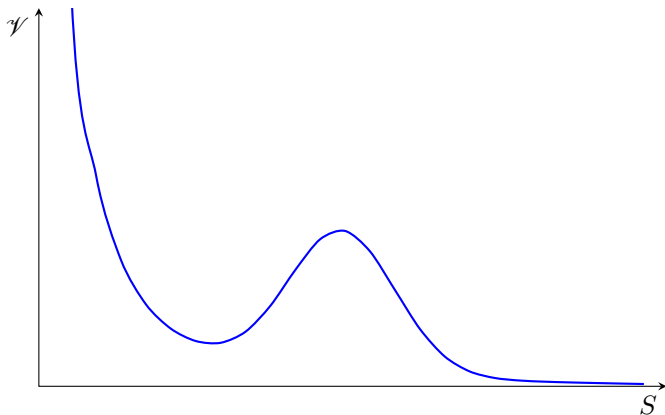


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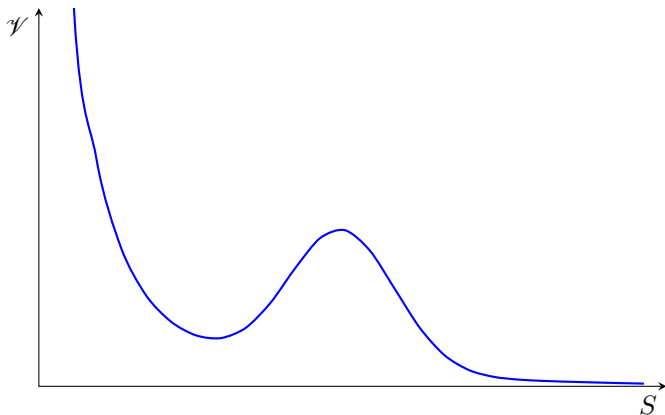


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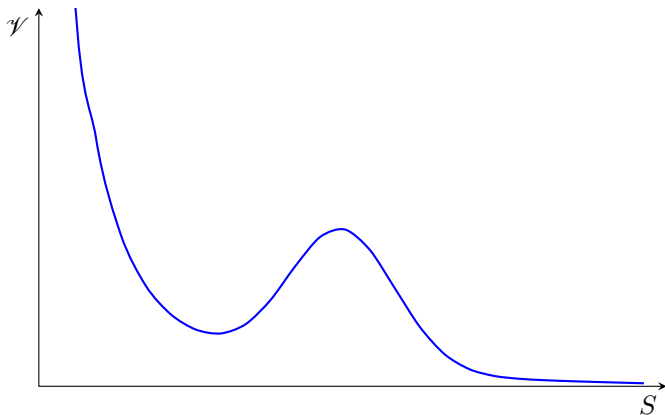


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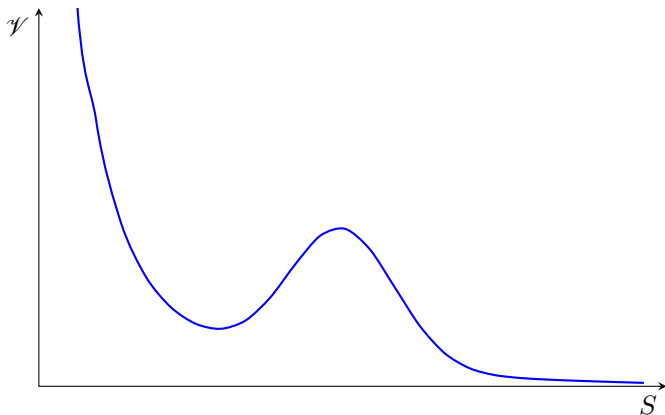


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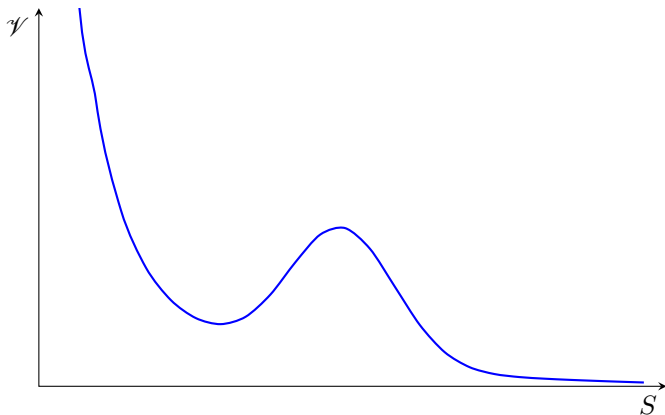


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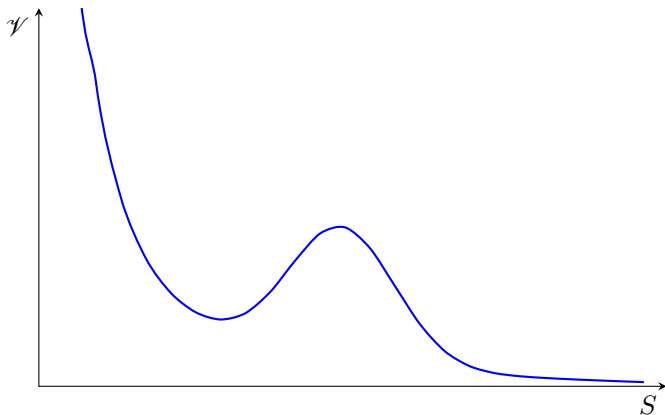


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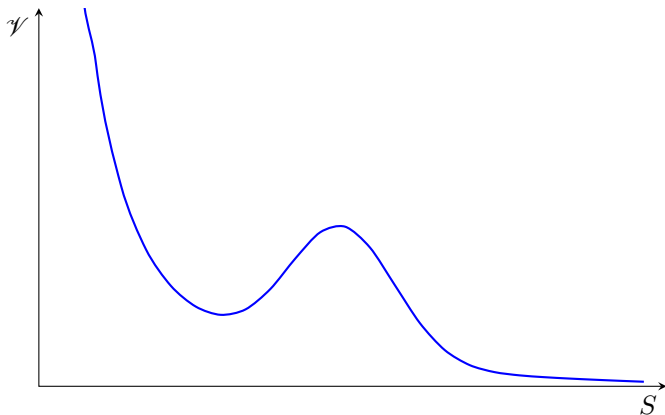


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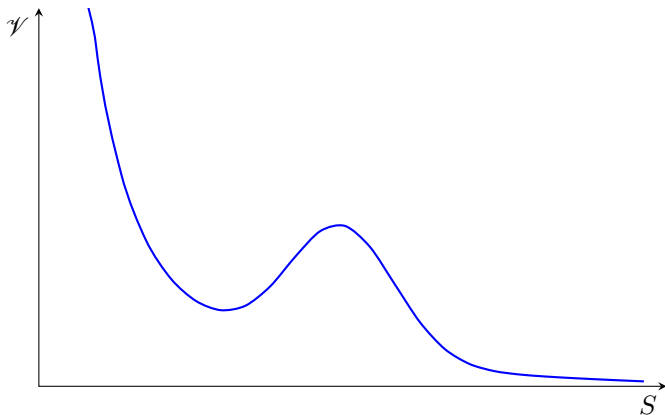


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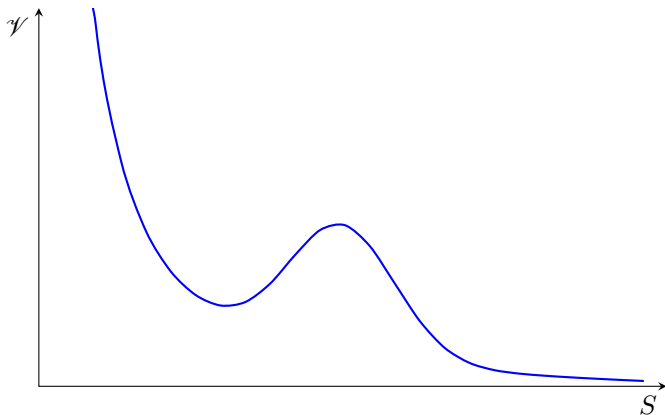


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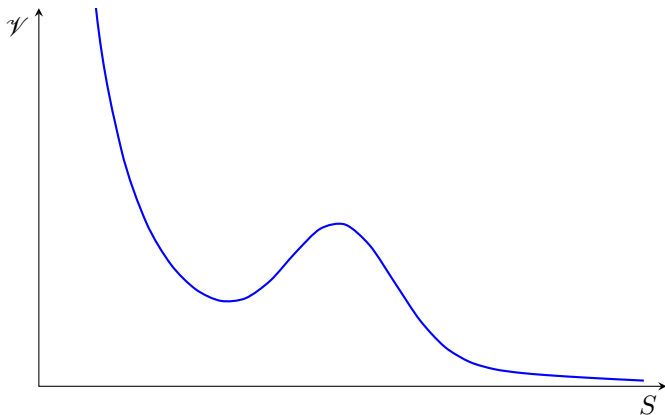


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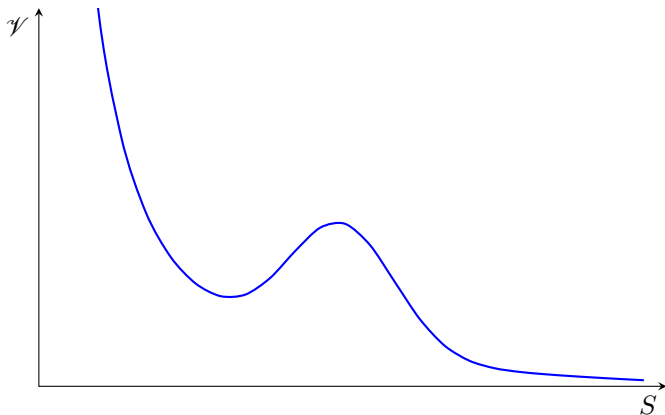


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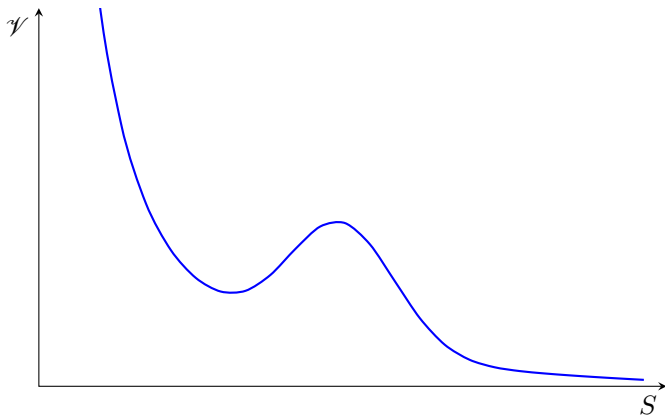


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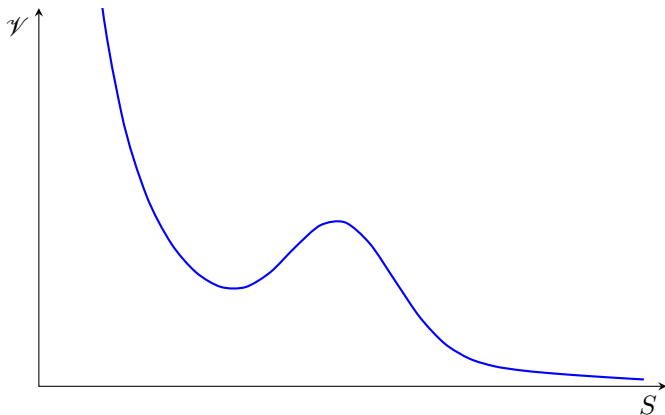


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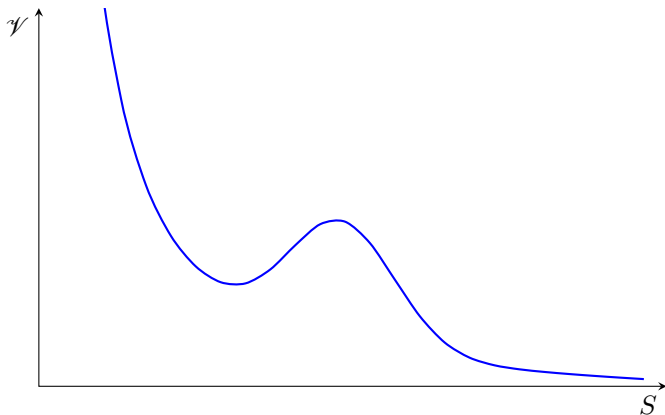


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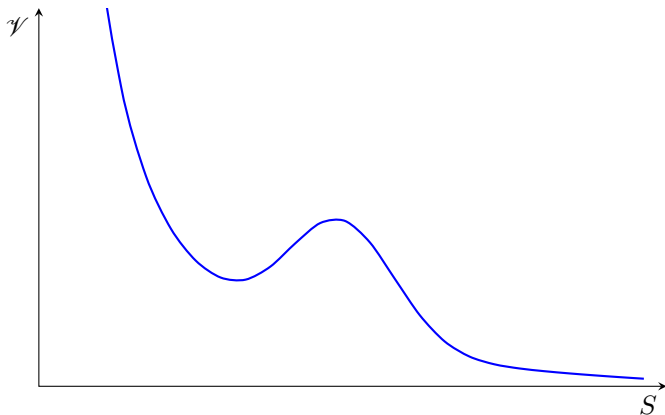


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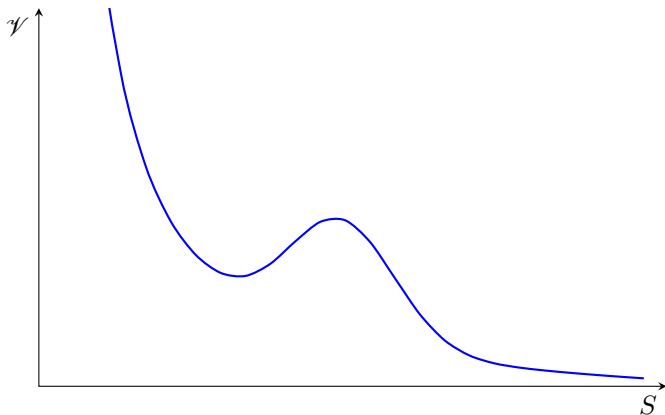


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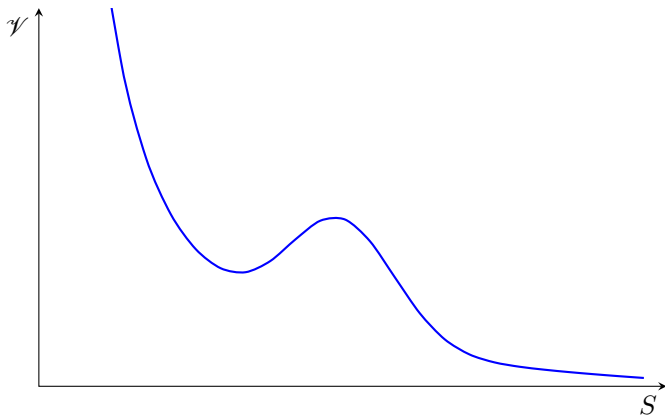


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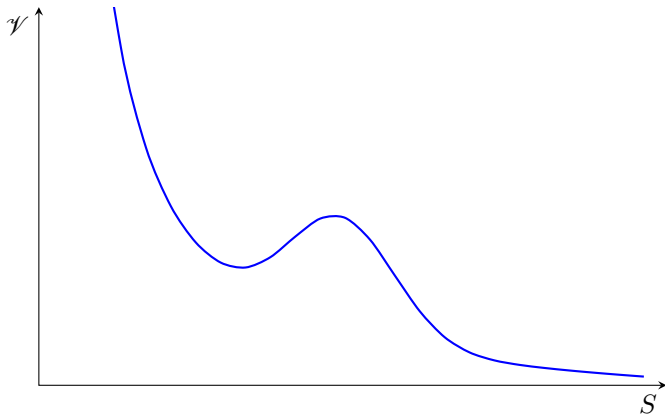


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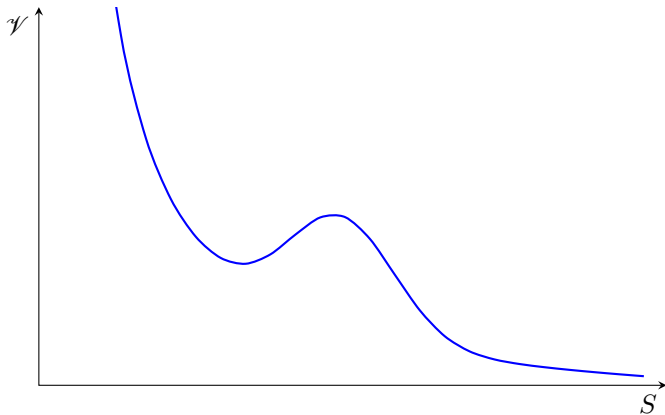


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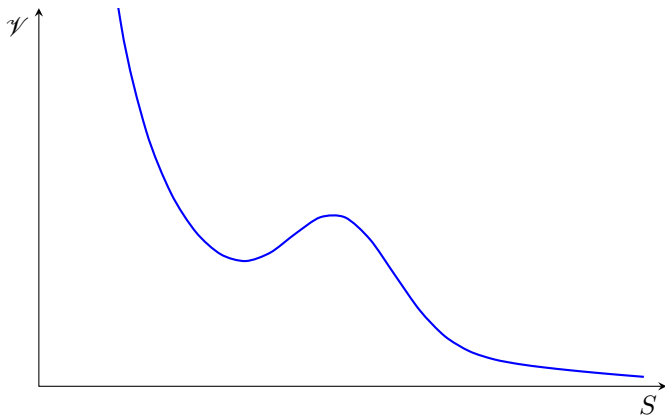


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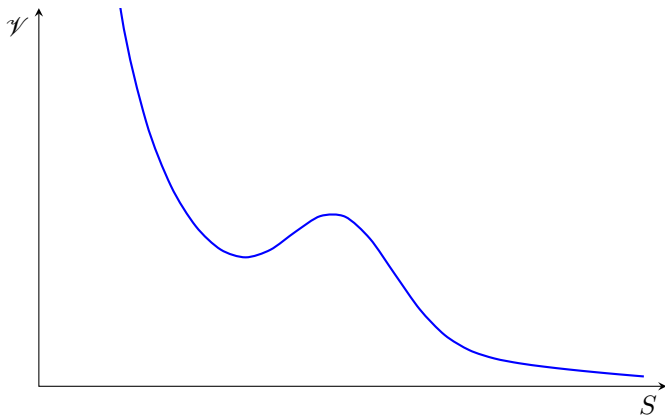


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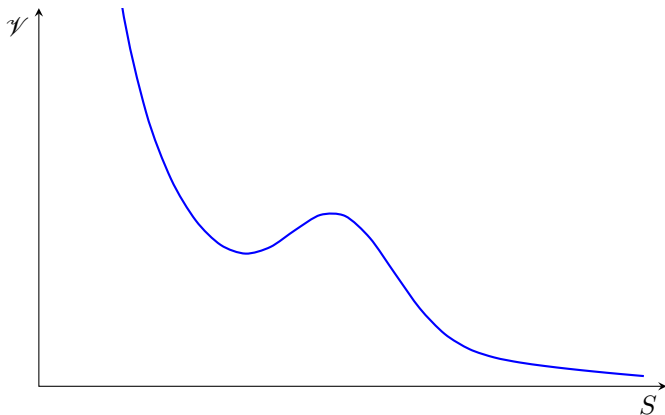


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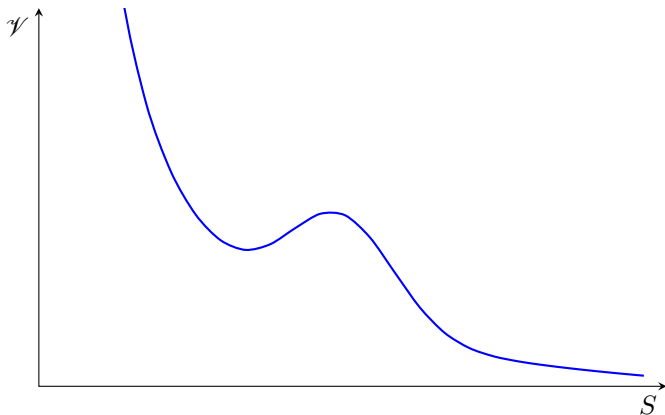


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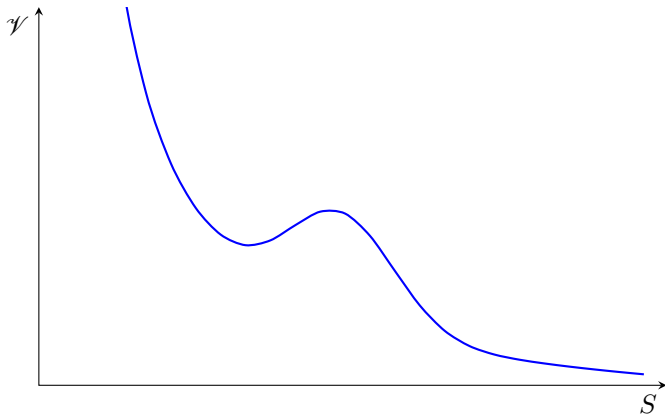


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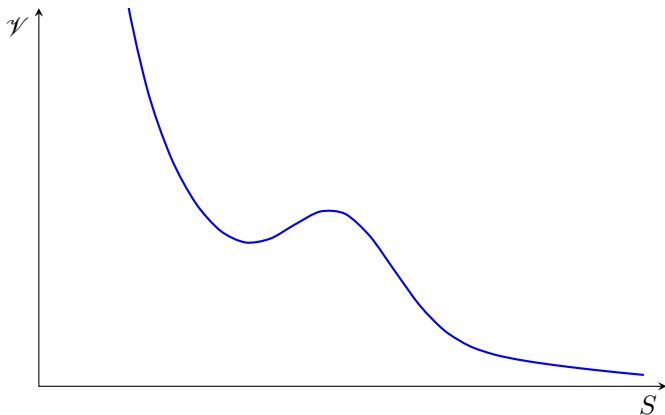


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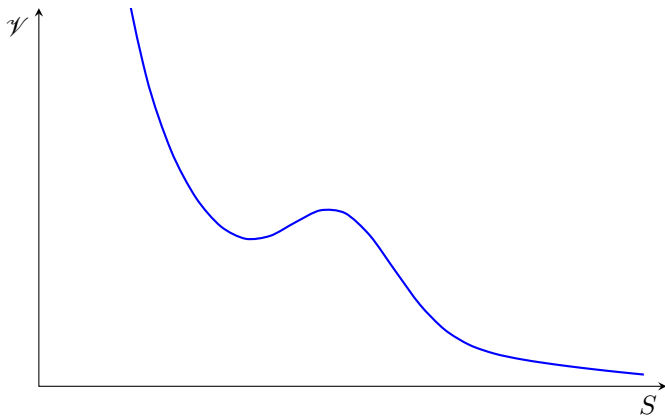


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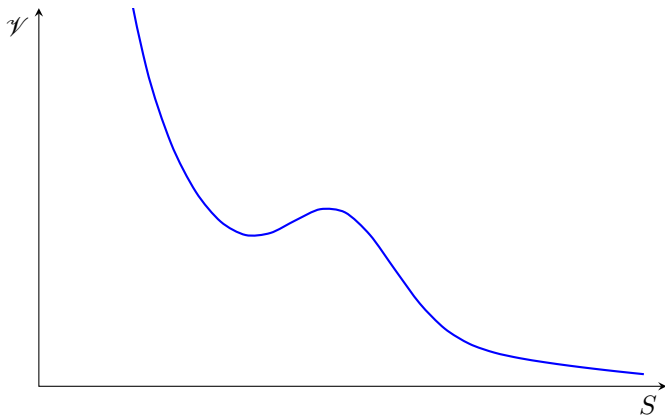


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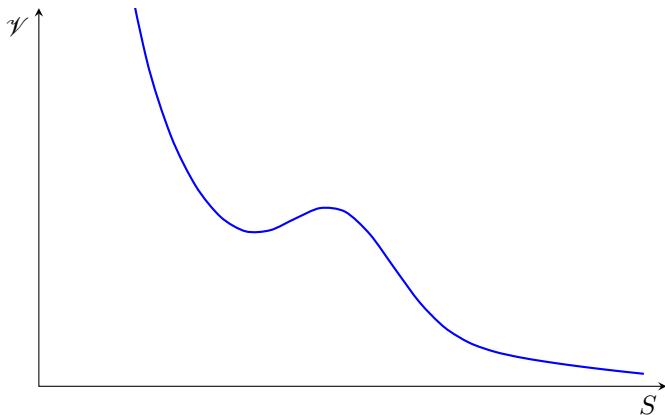


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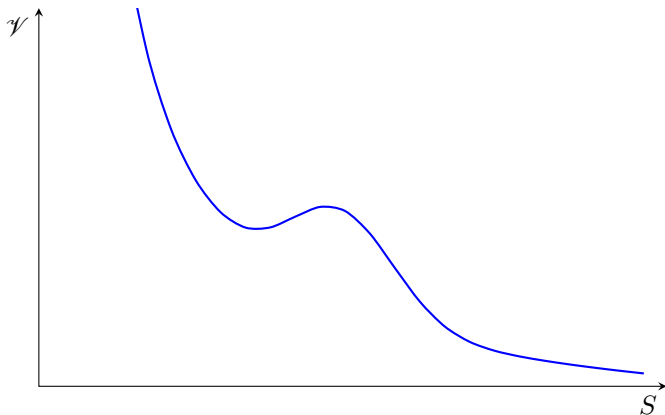


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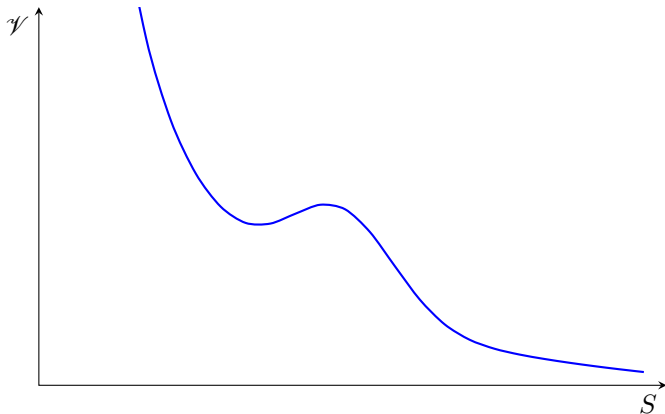


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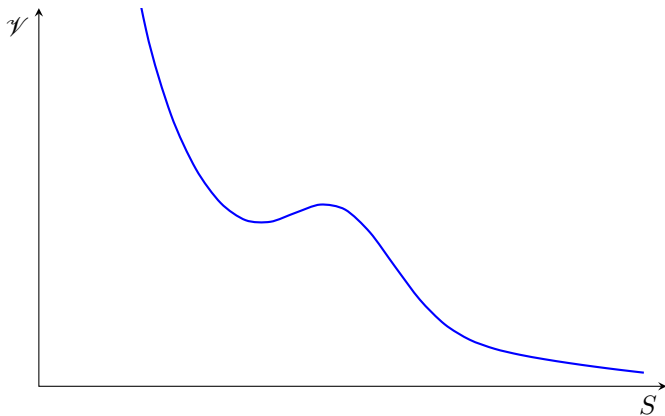


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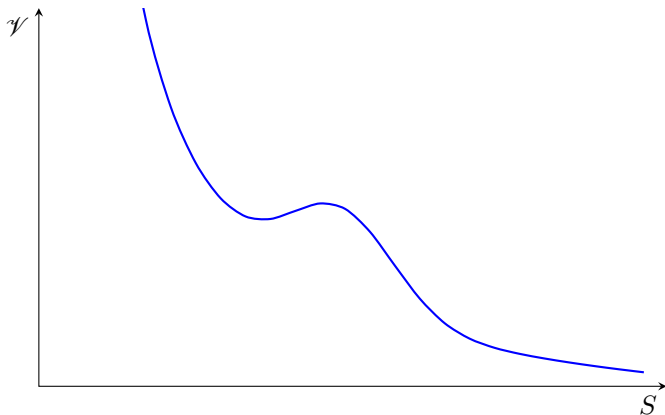


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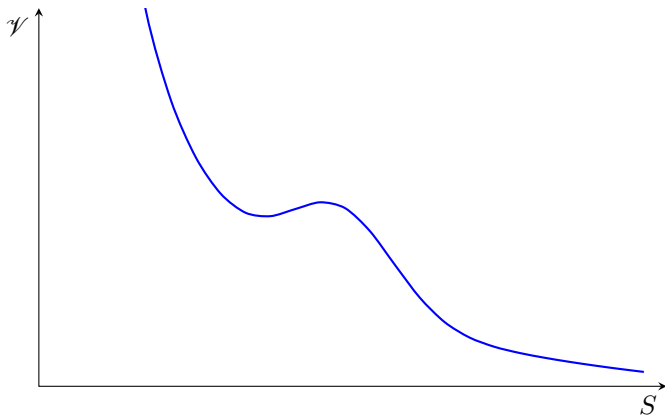


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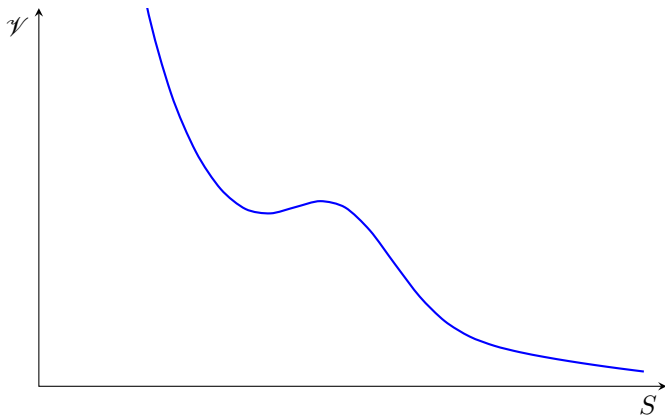


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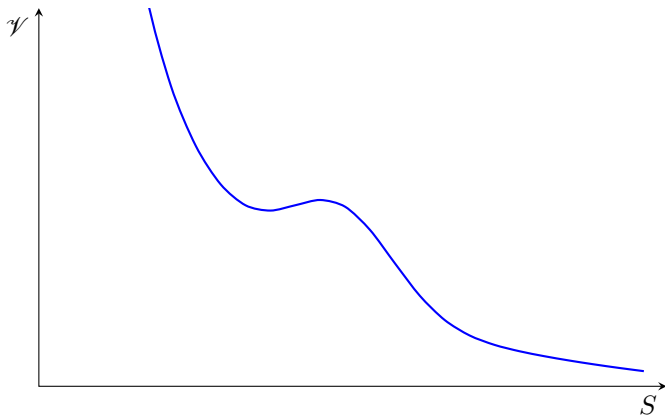


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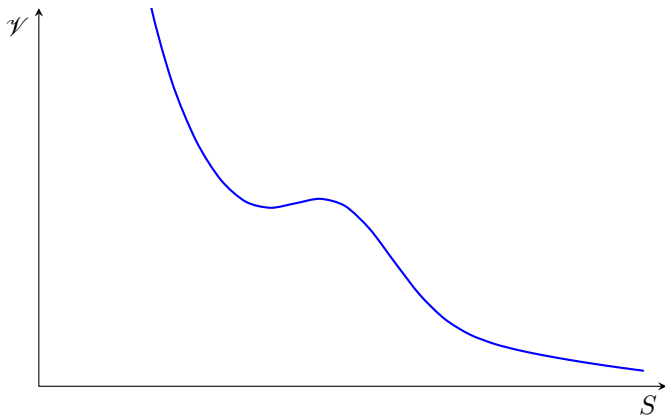


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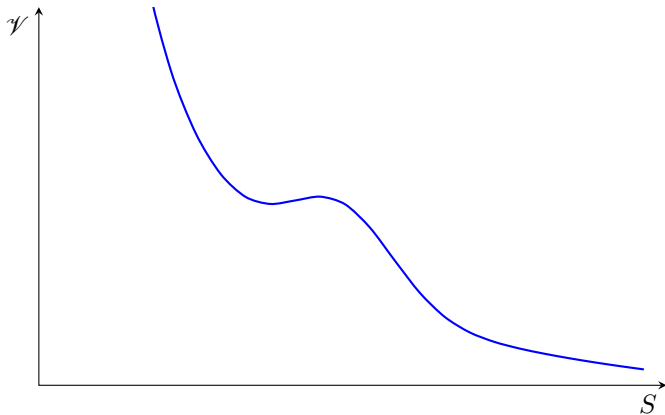


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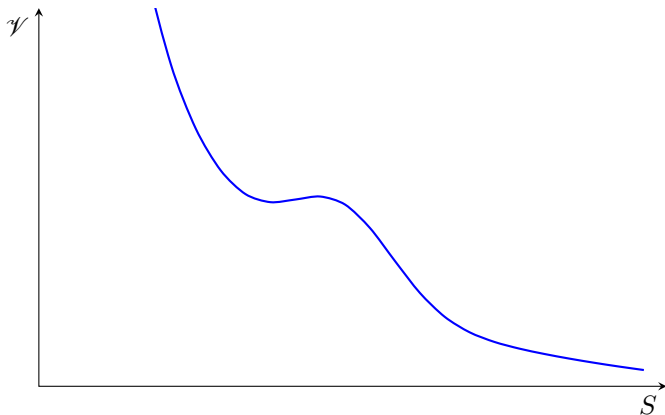


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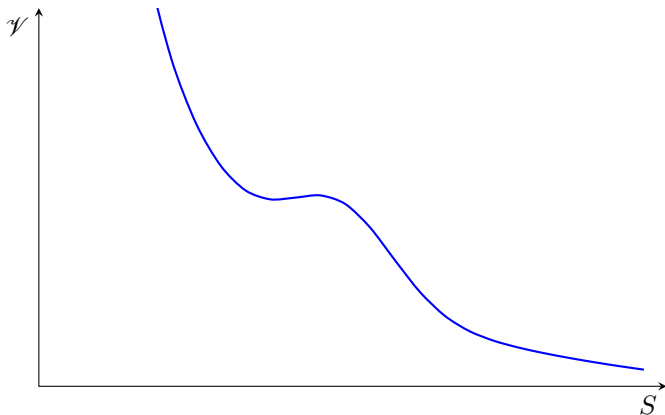


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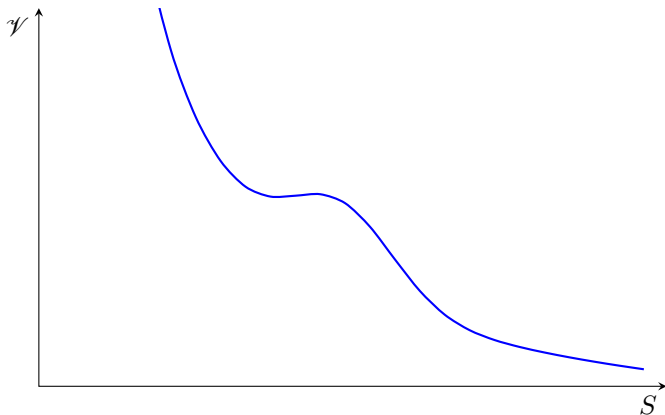


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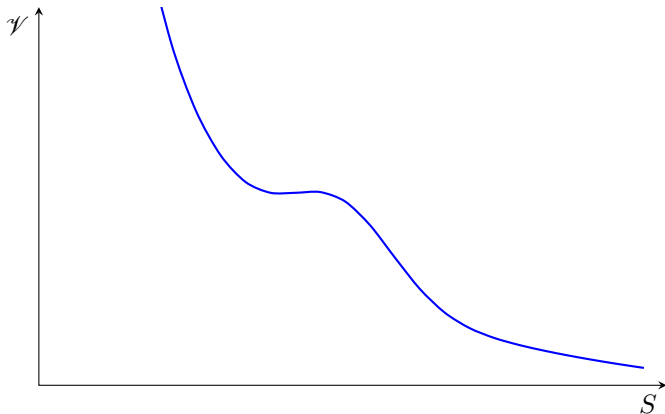


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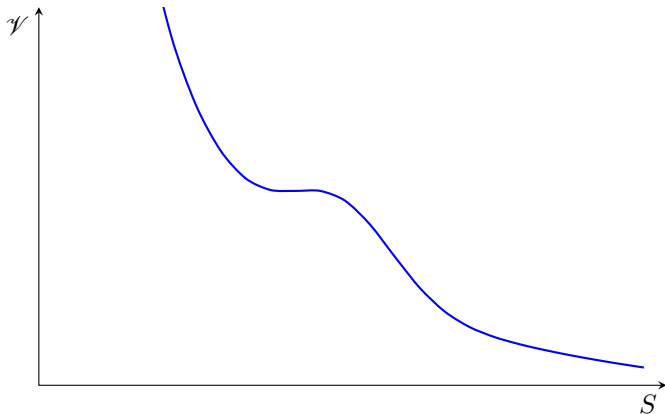


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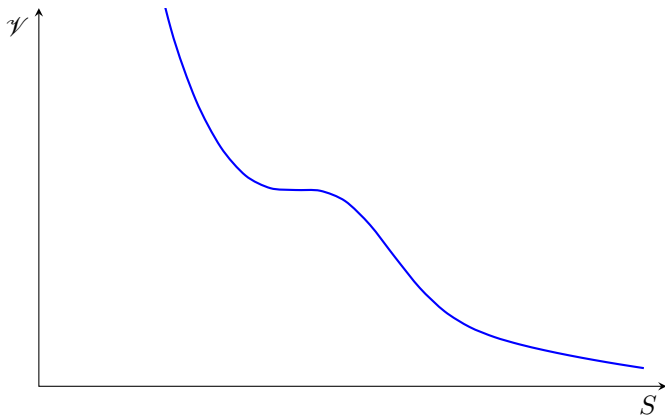


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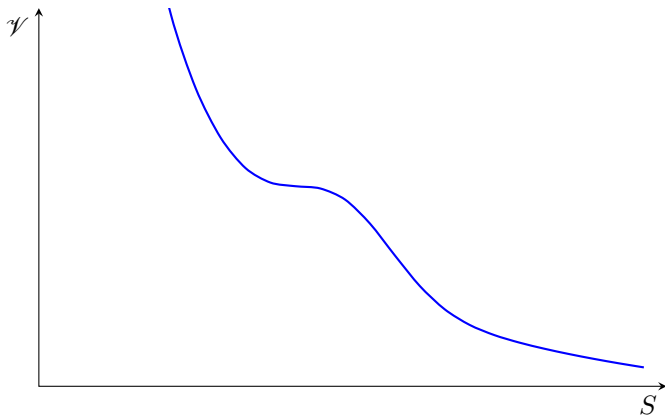


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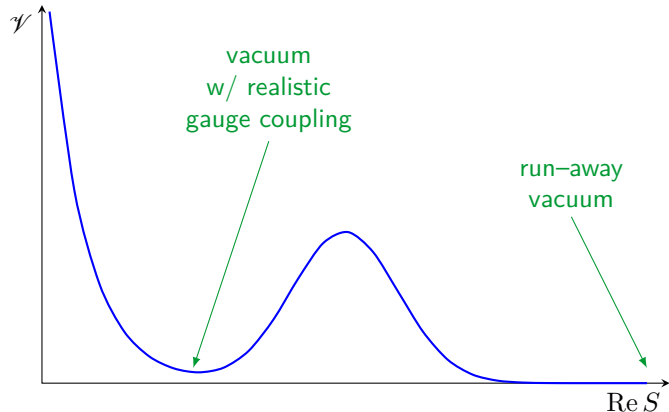
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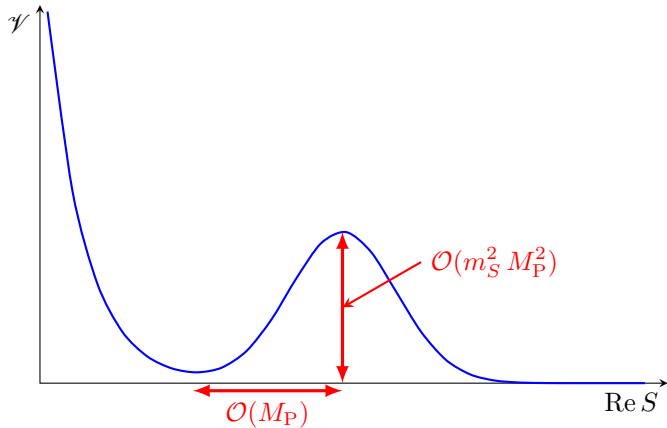


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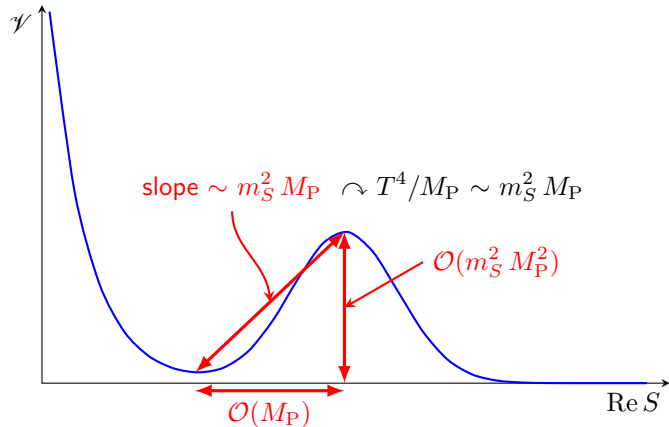
Critical temperature



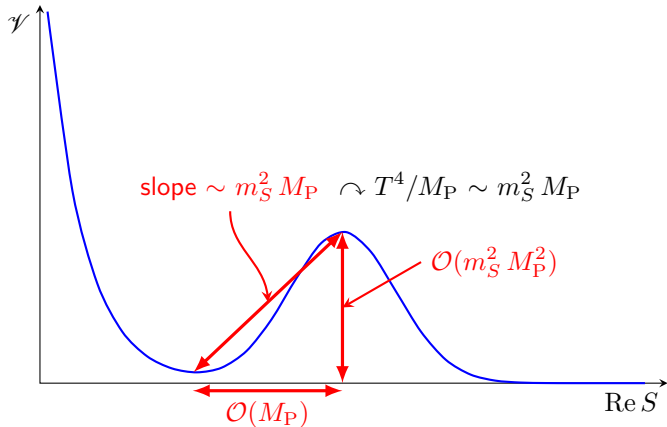
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bottom-line:

critical temperature $T_* \sim \sqrt{m_S M_P}$

Discussion

- if the dilaton has been destabilized, it will run away and cannot come back

model-independent constraint:

$$T_R \lesssim T_* \sim \sqrt{m_S M_P}$$

reheating temperature
(maximal temperature
of the radiation
dominated universe)

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[Kallosh & Linde \(2004\)](#)

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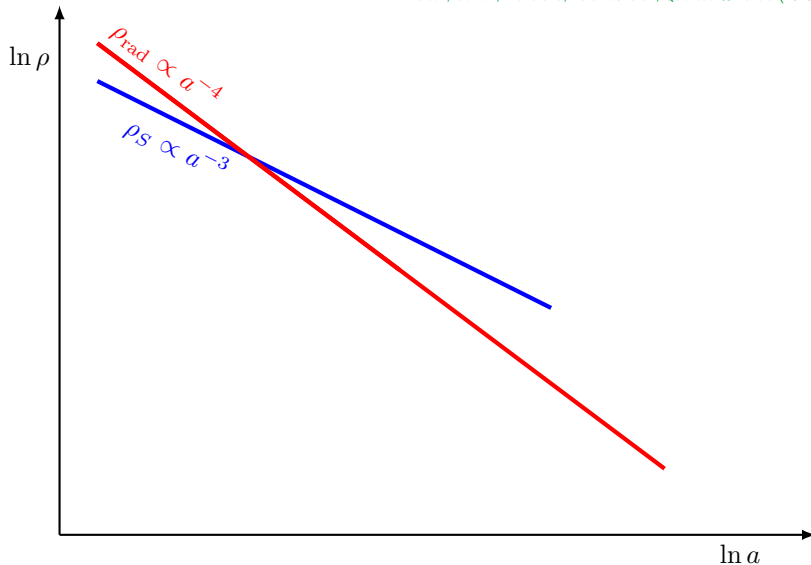
☞ Kallosh & Linde (2004)

- ☞ the bounds can be circumvented by stabilizing the field combination that fixes the gauge coupling in a different way (i.e. w/ an infinite barrier)

☞ Kane & Winkler (2019)

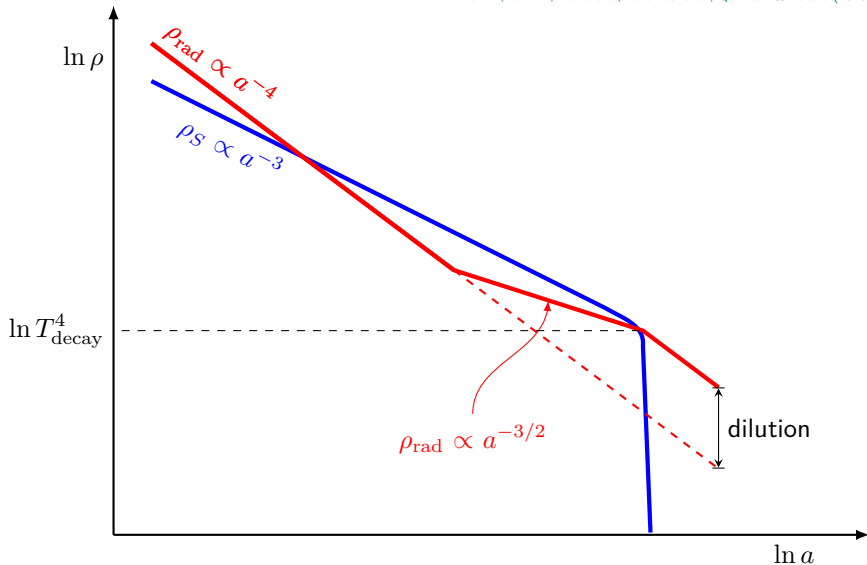
Moduli problems

[Coughlan, Fischler, Kolb, Raby & Ross \(1983\)](#); [de Carlos, Casas, Quevedo & Roulet \(1993\)](#), . . . ,
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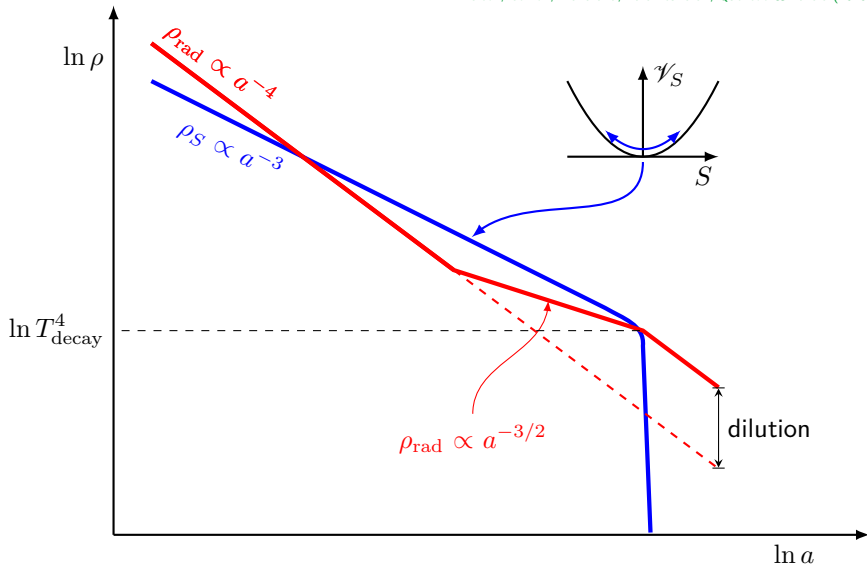
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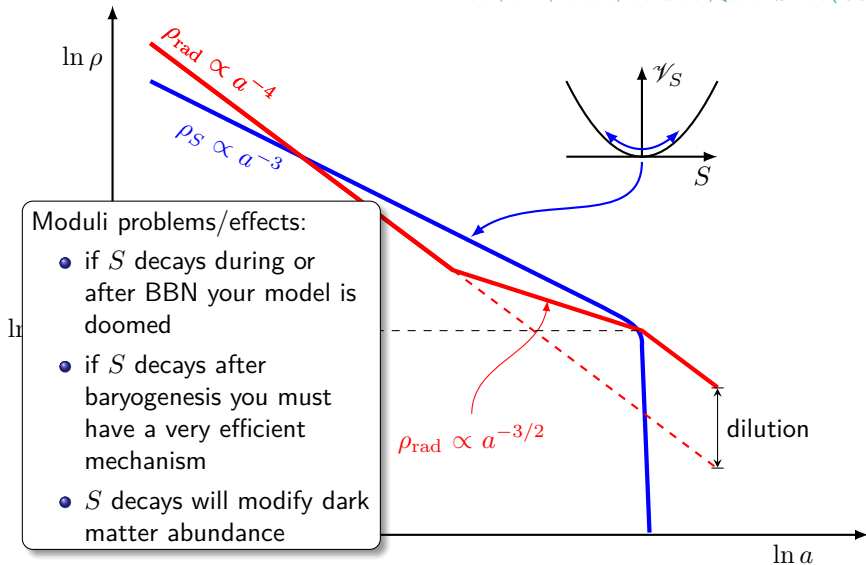
Moduli problems

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Moduli problems/effects:

- if S decays during or after BBN your model is doomed
- if S decays after baryogenesis you must have a very efficient mechanism
- S decays will modify dark matter abundance

Weight loss

Weight loss

solutions

solutions

Weight loss solutions



<https://unsplash.com/>

Weight loss solutions... in cosmology

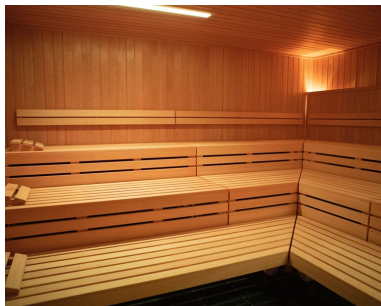


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main message

if masses and couplings of equilibrated particles depend on S , the dynamics of S will be such that the masses and couplings *decrease*

Weight loss solutions... in cosmology



<https://unsplash.com/>

main message

if masses and couplings of equilibrated particles depend on S , the dynamics of S will be such that the masses and couplings *decrease* i.e. the solution of the equations of motion entails weight loss

Constraints

on

flavons

Field-dependent fermion masses

e.g. Froggatt–Nielsen mechanism

[Froggatt & Nielsen \(1979\)](#); see lectures by Mu–Chun Chen

$$\mathcal{L}_{\text{FN}} = \sum_{i,j=1}^3 y_{ij}^u \left(\frac{S}{\Lambda}\right)^{n_{ij}^u} \bar{Q}_i \tilde{\Phi} u_j + \sum_{i,j=1}^3 y_{ij}^d \left(\frac{S}{\Lambda}\right)^{n_{ij}^d} \bar{Q}_i \Phi d_j + \text{h.c.}$$

flavon

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☞ potential

$$\mathcal{V}_S = -\mu_S^2 |S|^2 + \lambda_S |S|^4 + \lambda_{S\Phi} |S|^2 |\Phi|^2 + \text{U}(1)_{\text{FN}} \text{ breaking terms}$$

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➔ VEV at $T = 0$

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➔ VEV at $T = 0$

$$S = \frac{1}{\sqrt{2}}(v_S + \sigma + i\rho) \quad \alpha = \gamma \frac{\partial T_Y}{\partial \varepsilon} \sim 10^{-2}$$

☞ effective potential

$$\mathcal{V}_{\text{eff}}(\sigma, T) = \gamma T_Y T^4 + \alpha T^4 \frac{\sigma}{\Lambda} + \frac{m_\sigma^2(T)}{2} \sigma^2 + \frac{\kappa}{3!} \sigma^3 + \frac{\lambda_S}{4} \sigma^4 + \dots$$

Modular flavor symmetries

[Feruglio \(2019\)](#); see lectures by Mu-Chun Chen

more recent example: modular flavor symmetries

$$m \propto Y(\tau)$$

fermion
mass
matrix

vector-
valued
modular
form

modulus

Modular flavor symmetries

[Feruglio \(2019\)](#); see lectures by Mu-Chun Chen

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[Baur, Nilles, Trautner & Vaudrevange \(2019\)](#);...; [Feruglio, Gherardi, Romanino & Titov \(2021\)](#);...; [Feruglio \(2023\)](#);...

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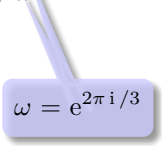
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- more generally, the size of the couplings depends on τ

- many couplings vanish for $\text{Im } \tau \rightarrow \infty$

- we could take e.g.

$$S = \text{Im} \frac{\tau - \omega}{\tau + \omega}$$



$$\omega = e^{2\pi i/3}$$

Flavon dynamics

[Lillard, MR, Tait & Trojanowski \(2018\)](#)

- the flavon gets driven away from its $T = 0$ minimum until it gets stopped by the mass term or Hubble friction

$$\Delta\sigma \simeq -\alpha \frac{T^4}{\Lambda m_{\text{eff}}^2} \quad \text{where } m_{\text{eff}}^2 = 6H^2 + m_\sigma^2$$

Flavon dynamics

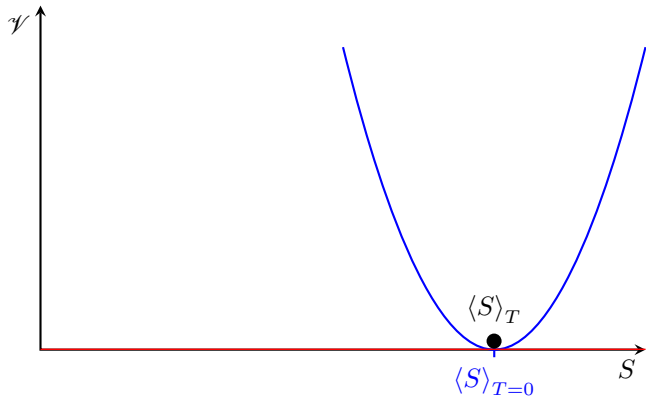
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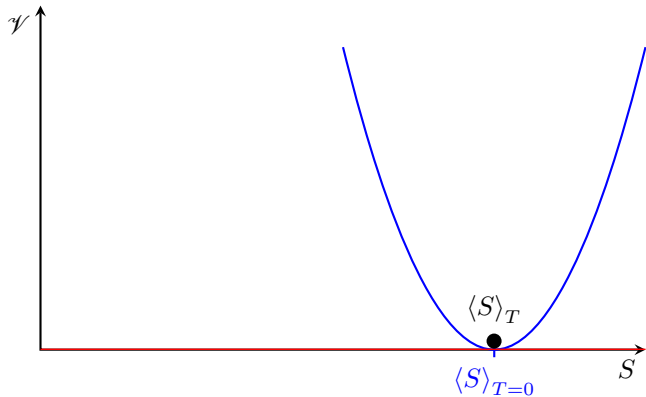
$$\Delta\sigma \simeq -\alpha \frac{T^4}{\Lambda m_{\text{eff}}^2} \quad \text{where } m_{\text{eff}}^2 = 6H^2 + m_\sigma^2$$

- as the temperature decreases, the flavon undergoes oscillations around the $T = 0$ minimum, which behave like nonrelativistic matter

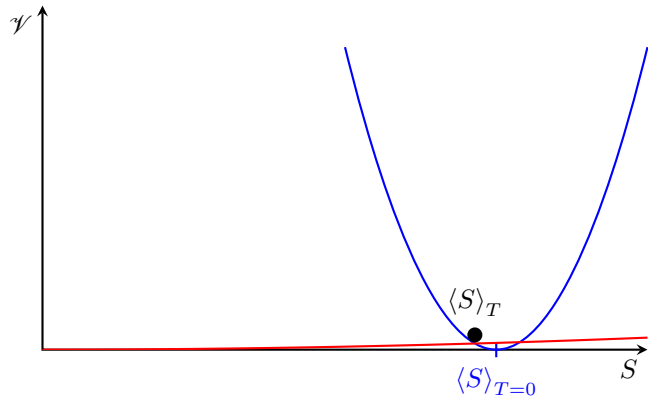
Thermal flavon potential (cartoon)



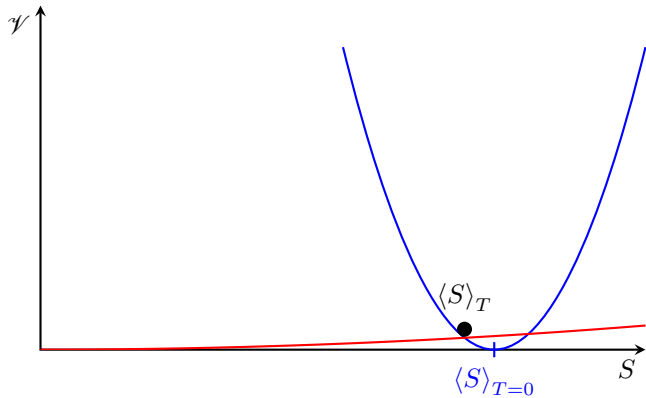
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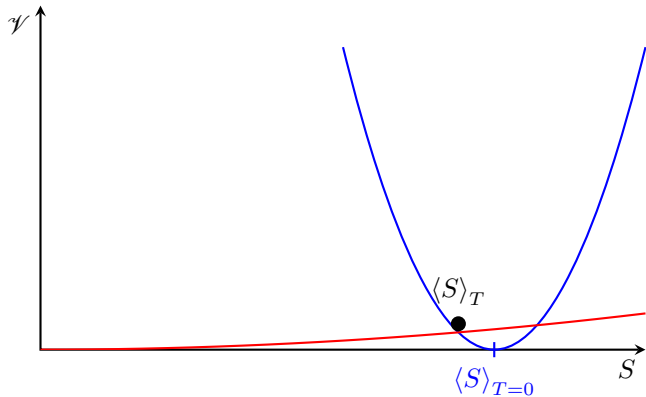
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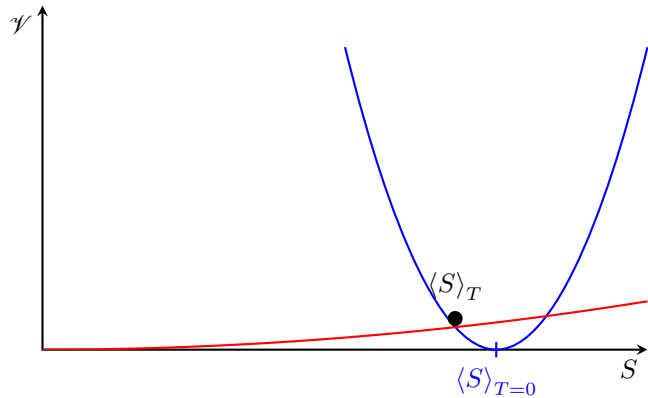
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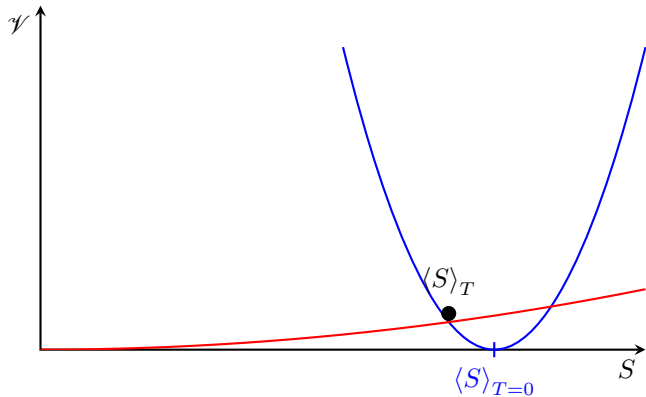
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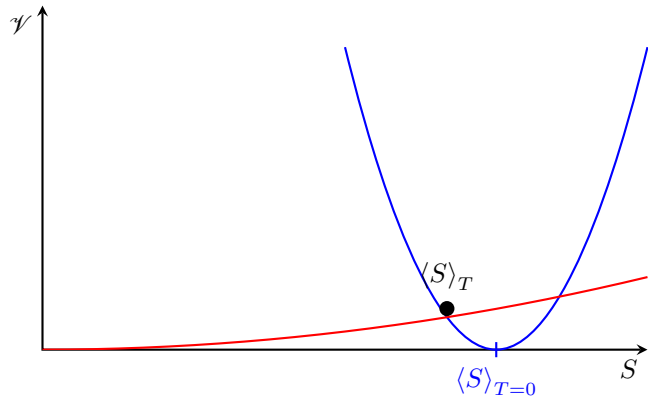
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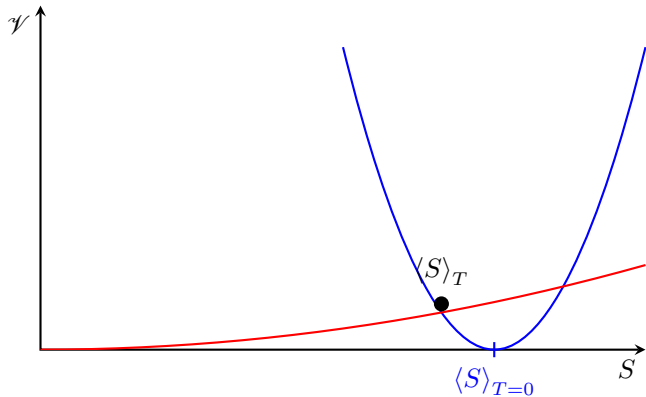
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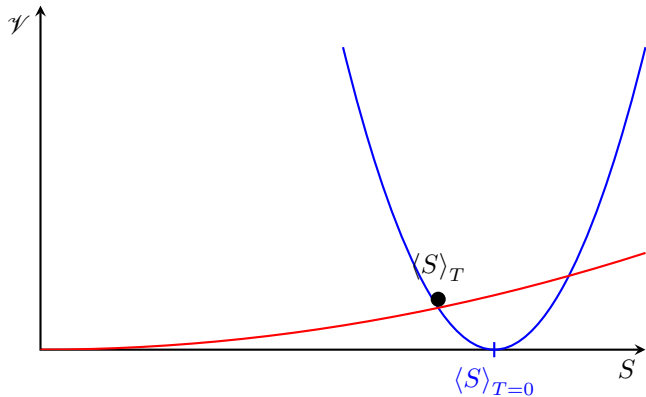
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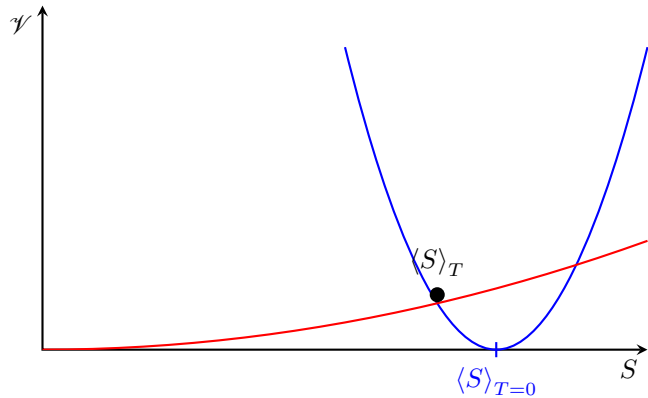
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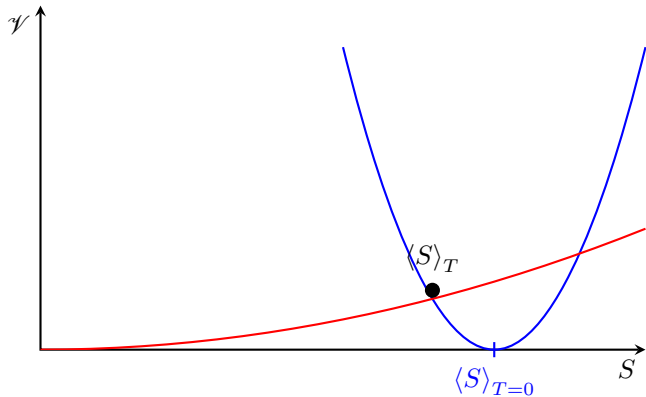
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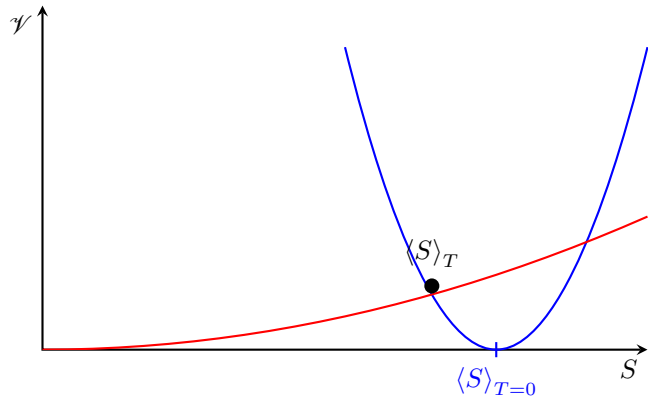
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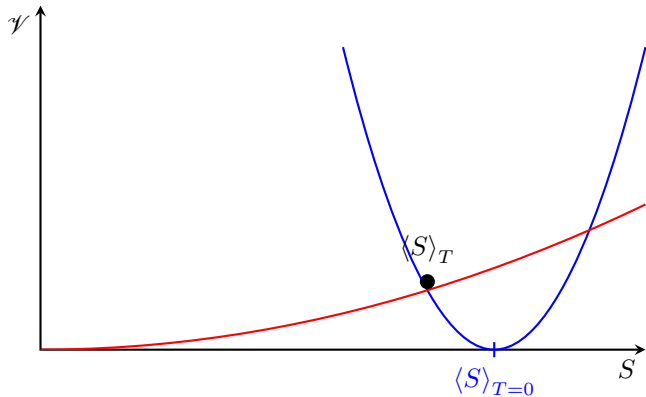
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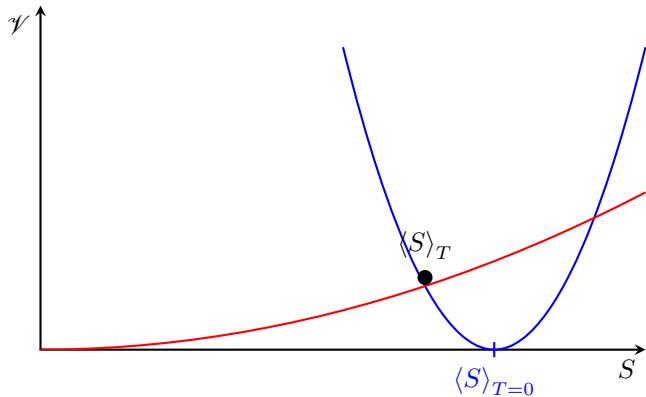
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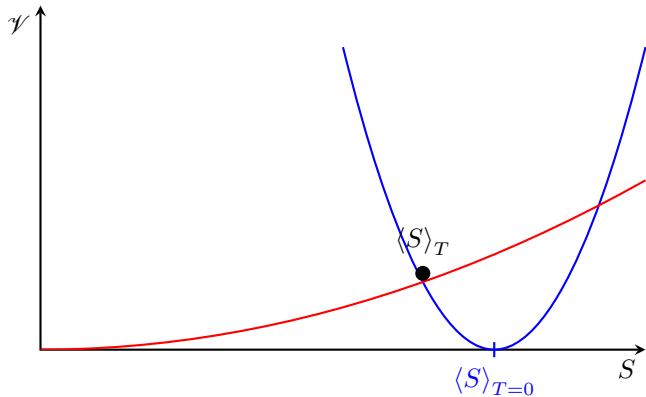
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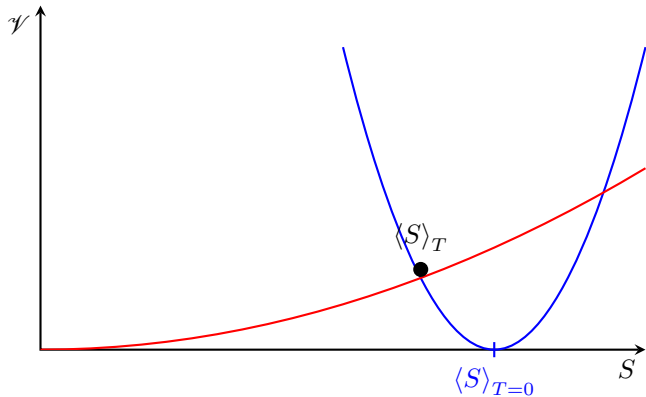
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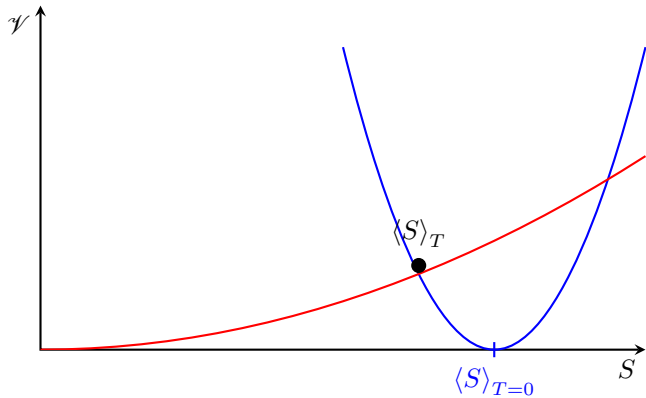
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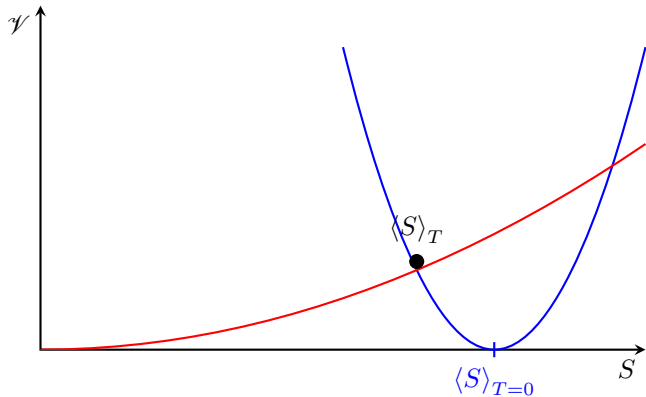
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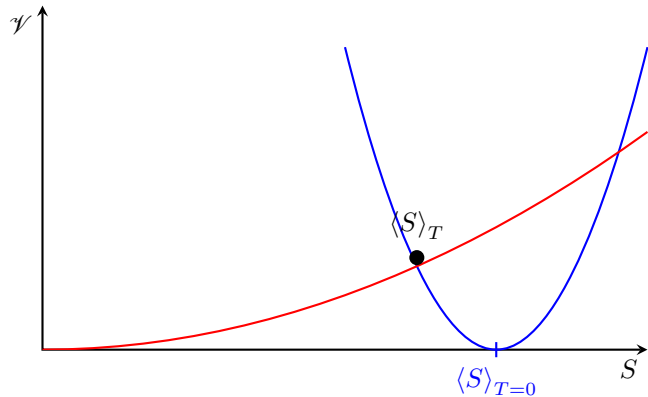
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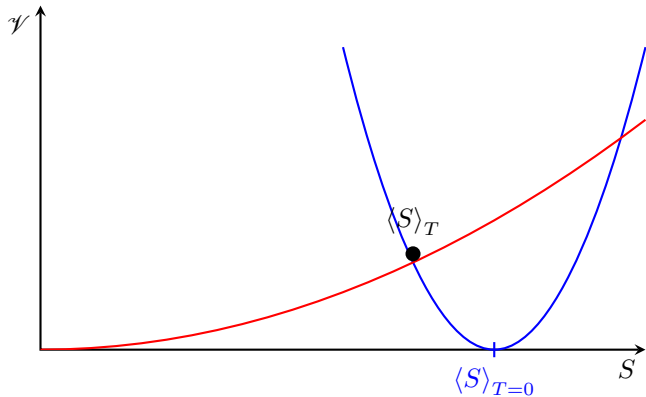
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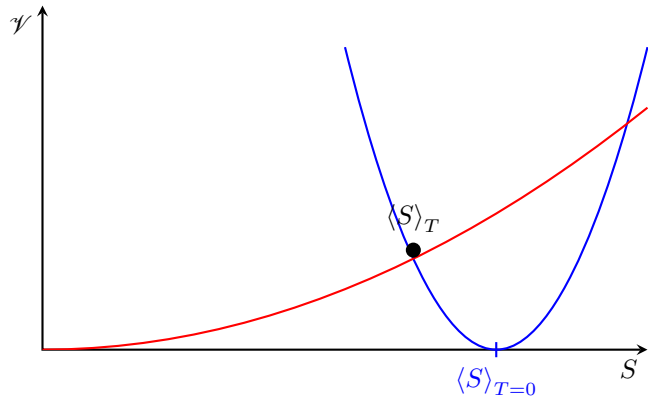
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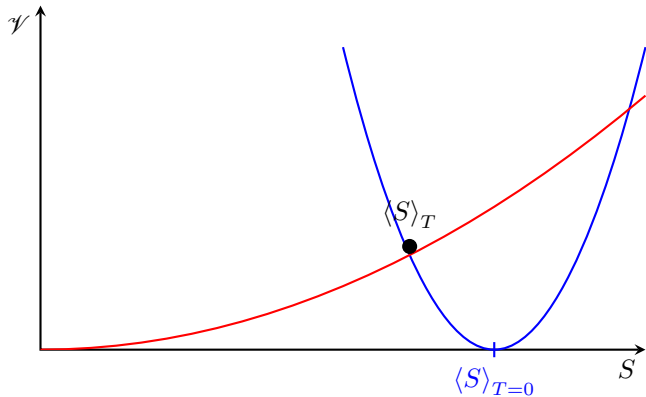
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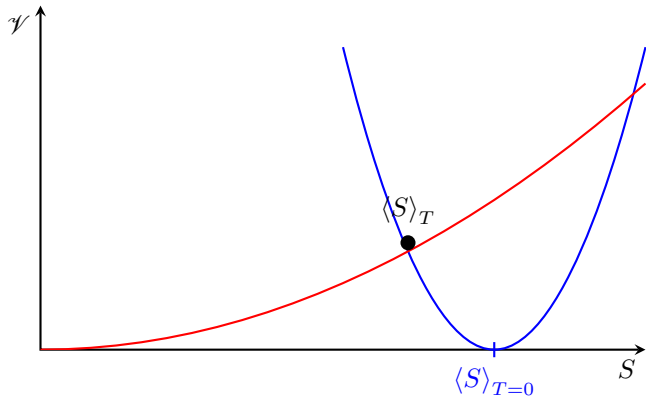
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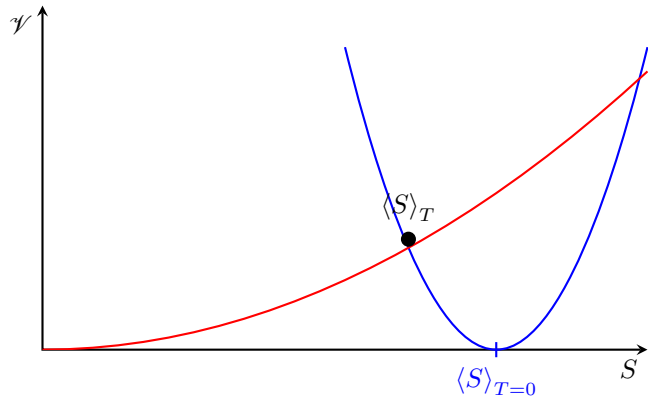
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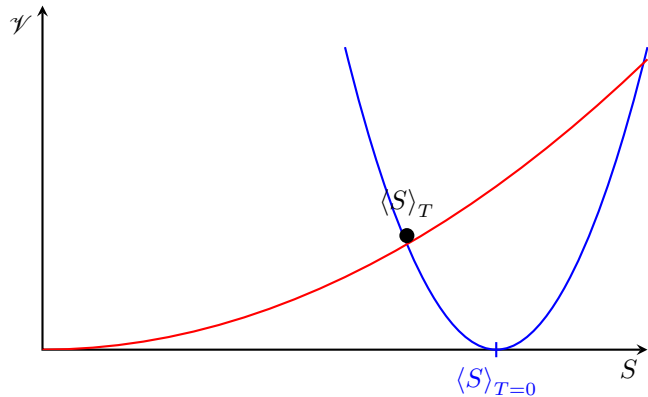
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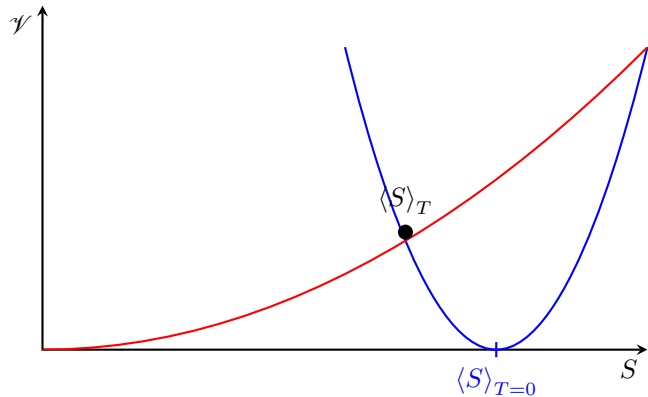
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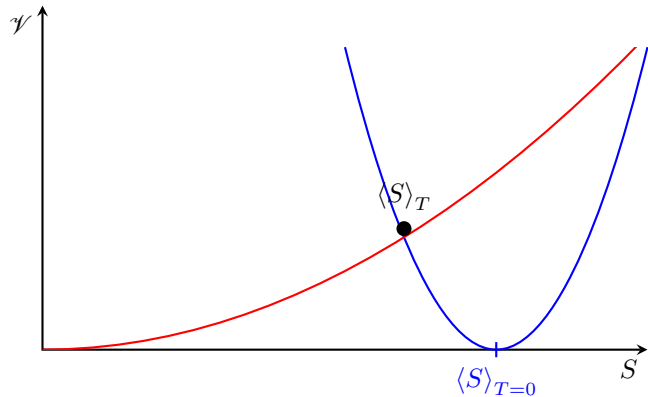
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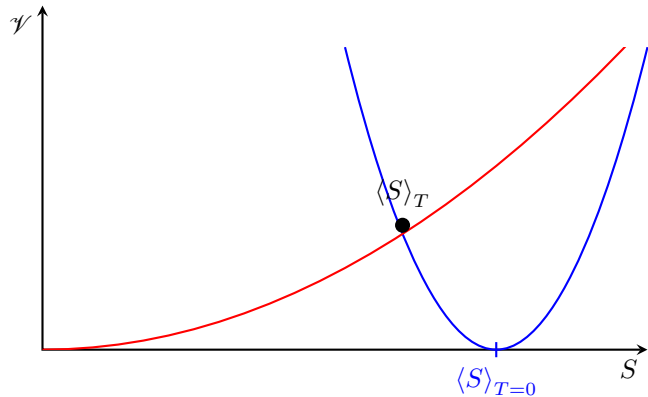
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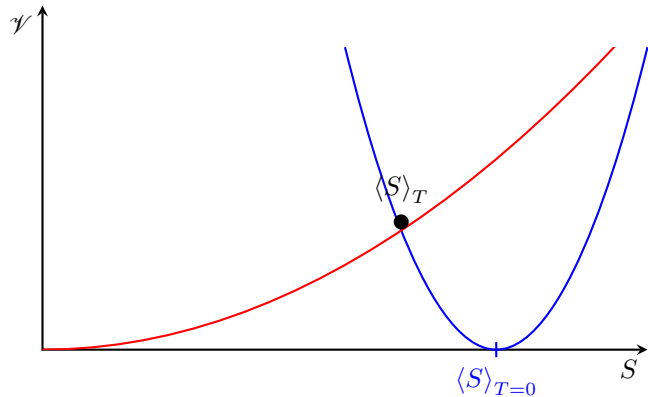
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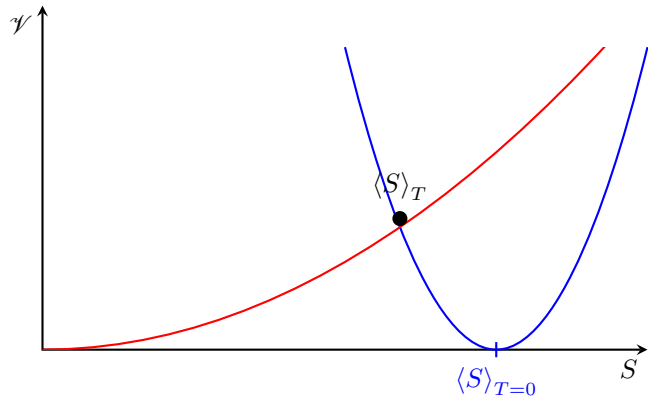
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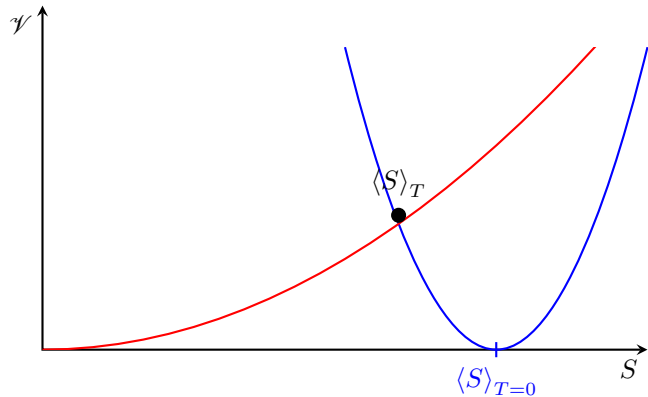
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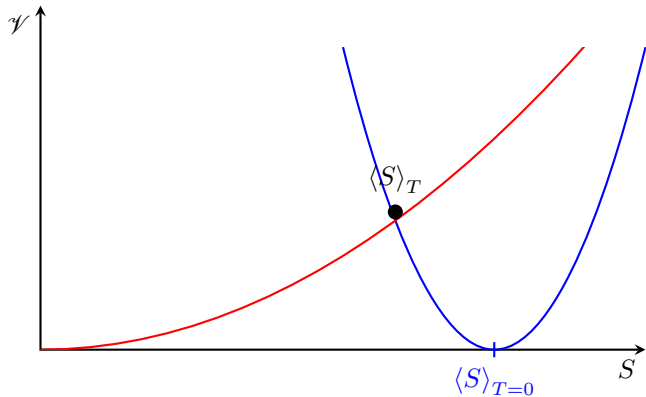
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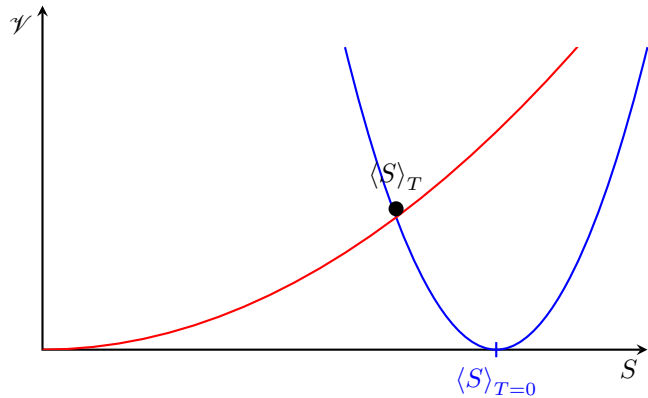
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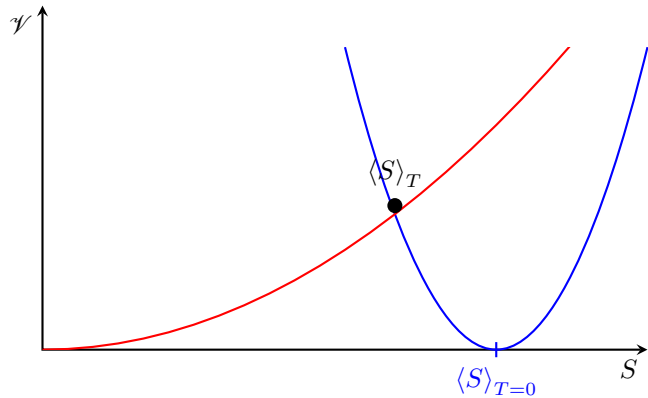
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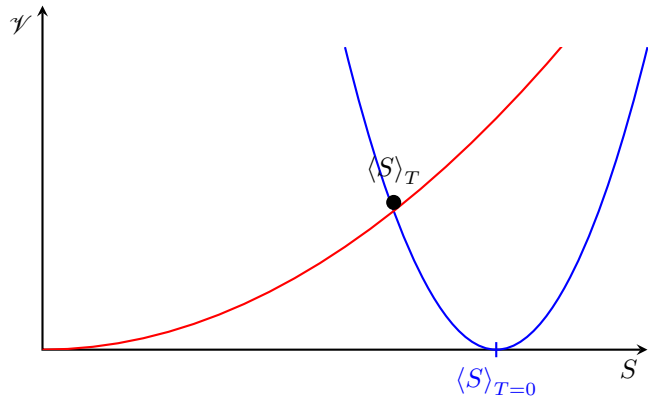
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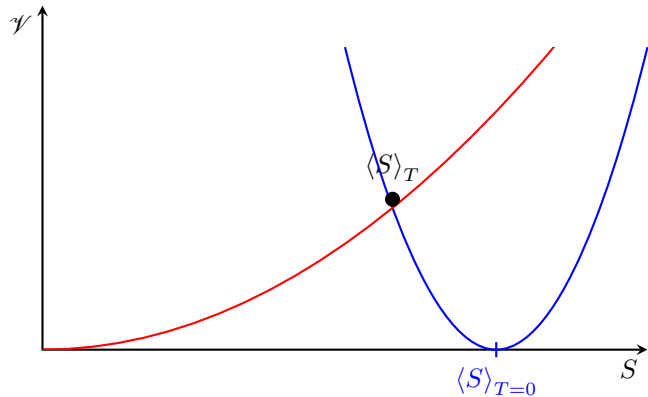
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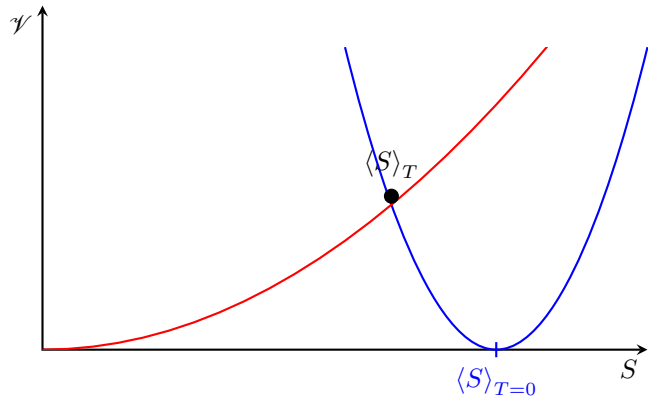
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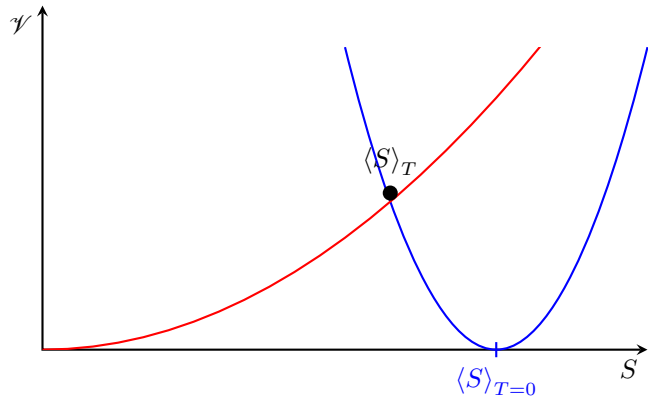
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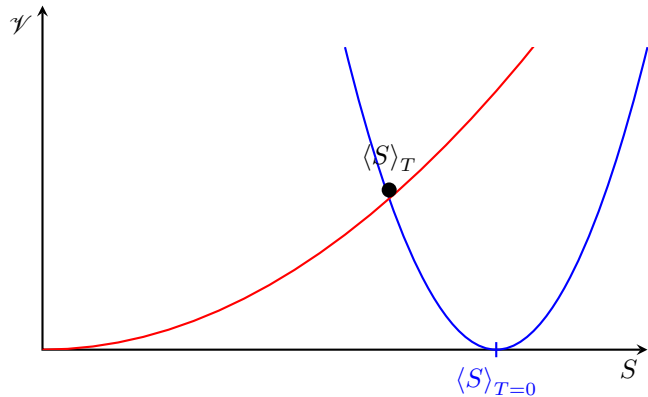
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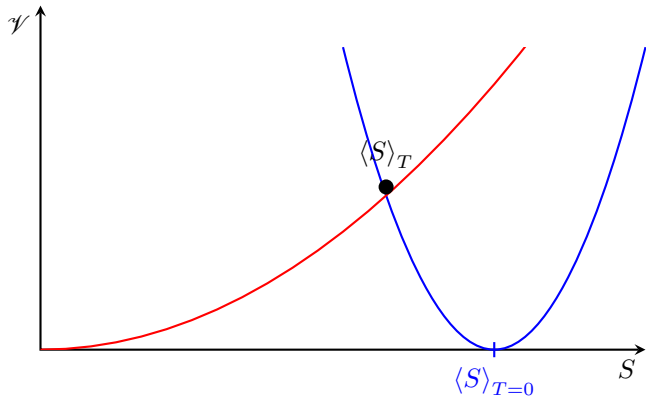
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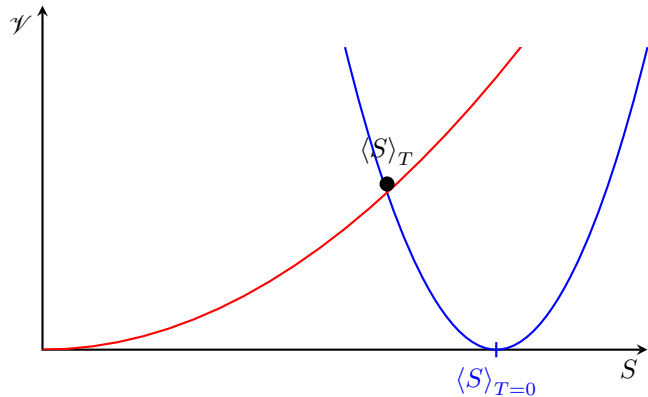
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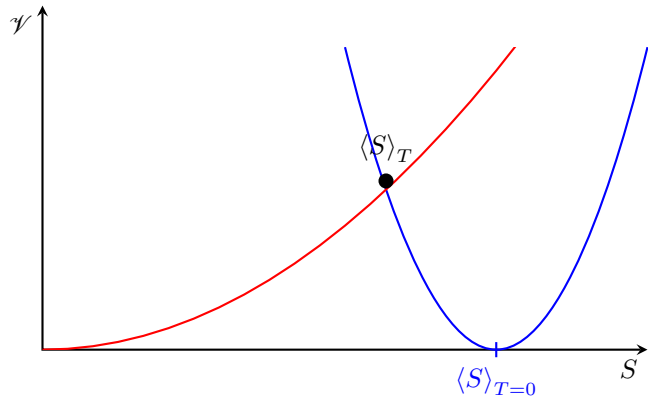
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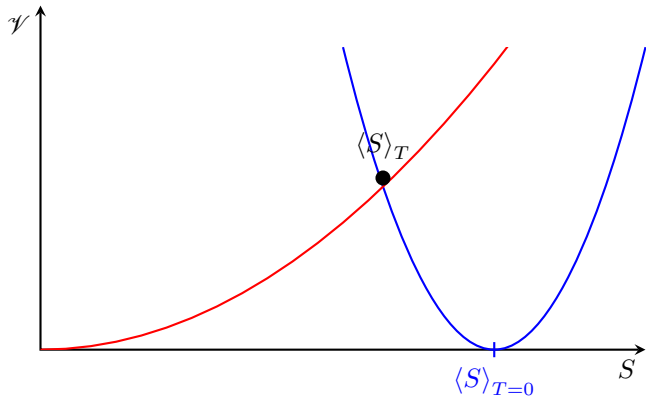
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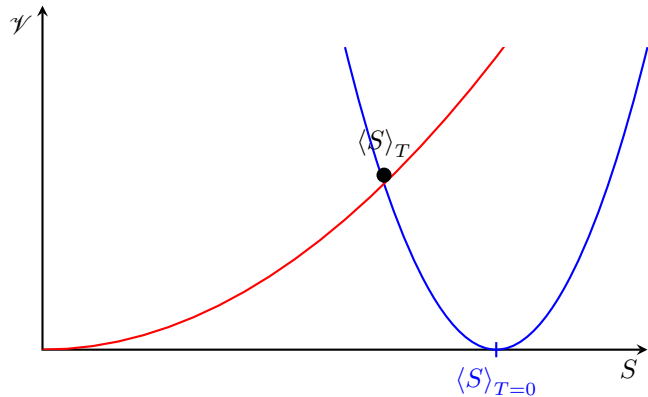
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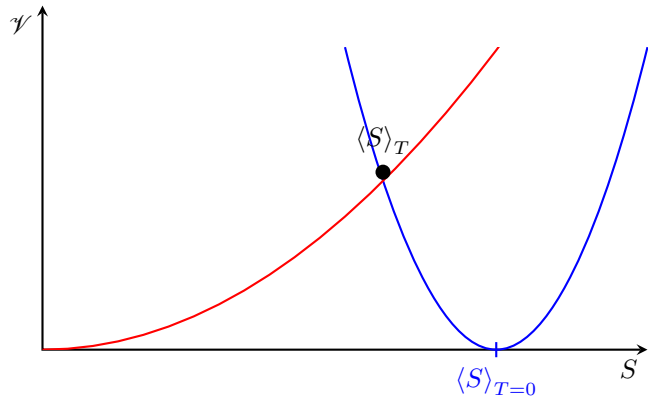
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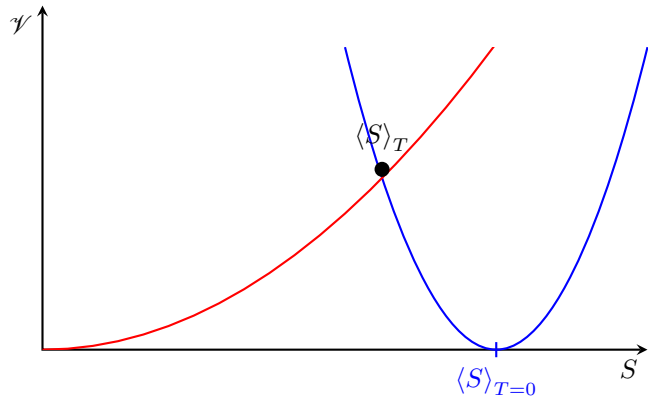
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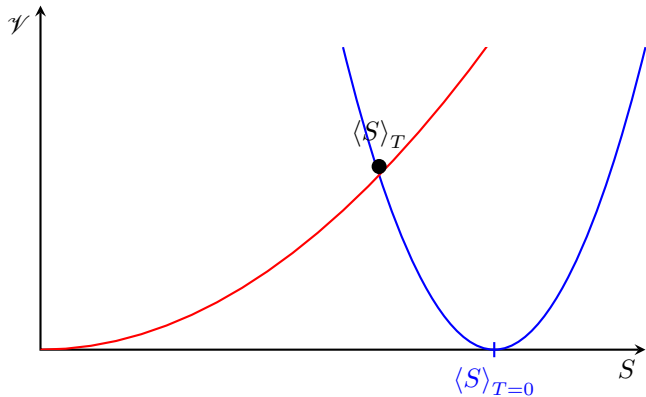
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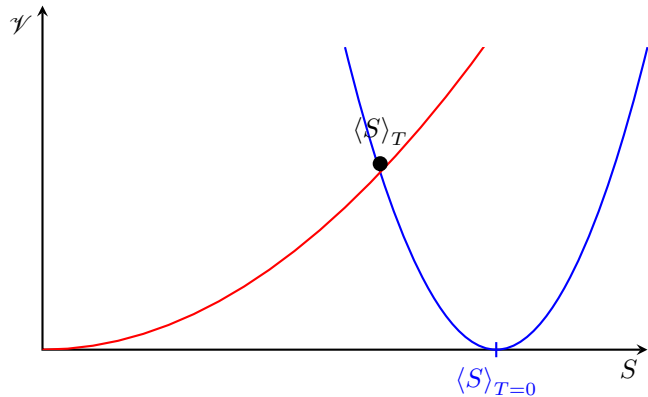
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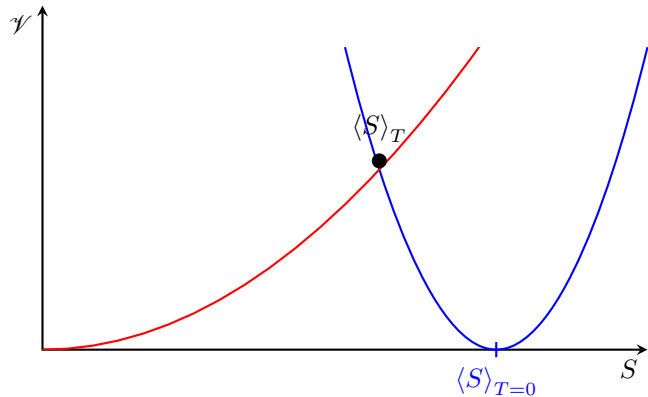
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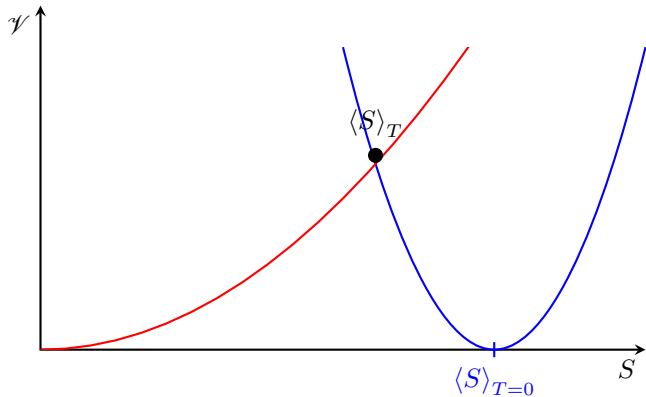
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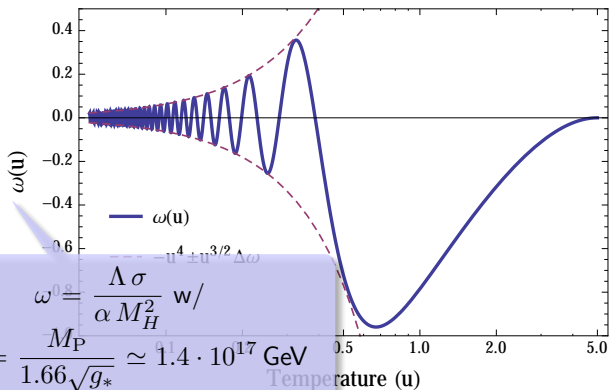
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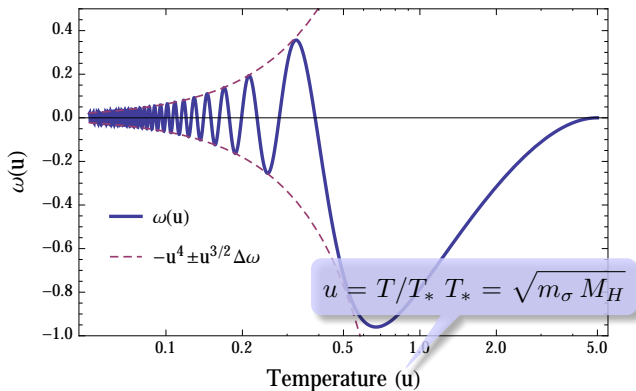
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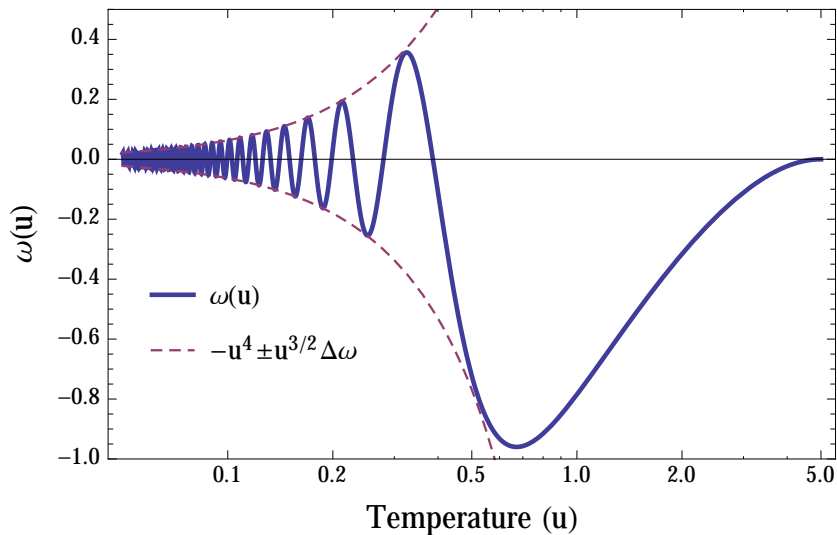
Flavon oscillations



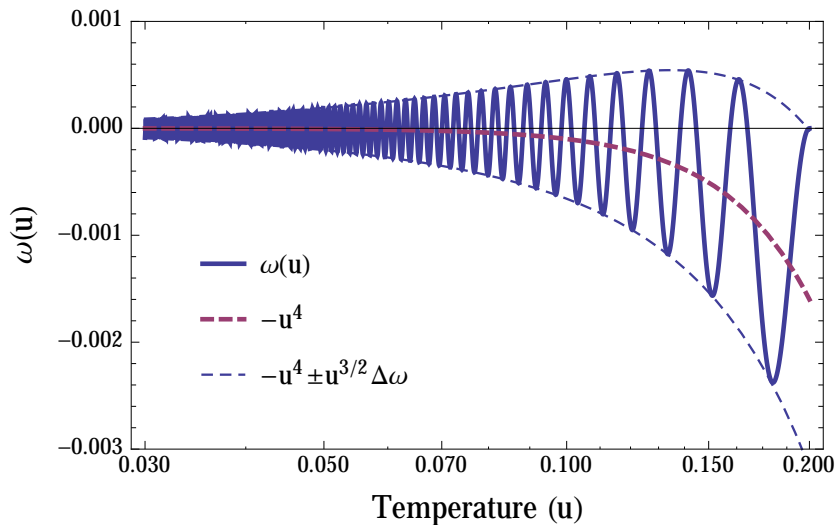
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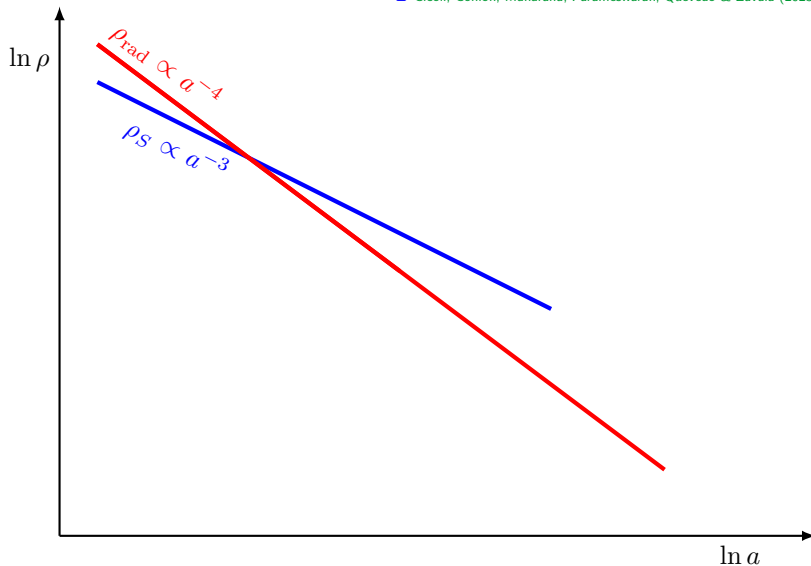


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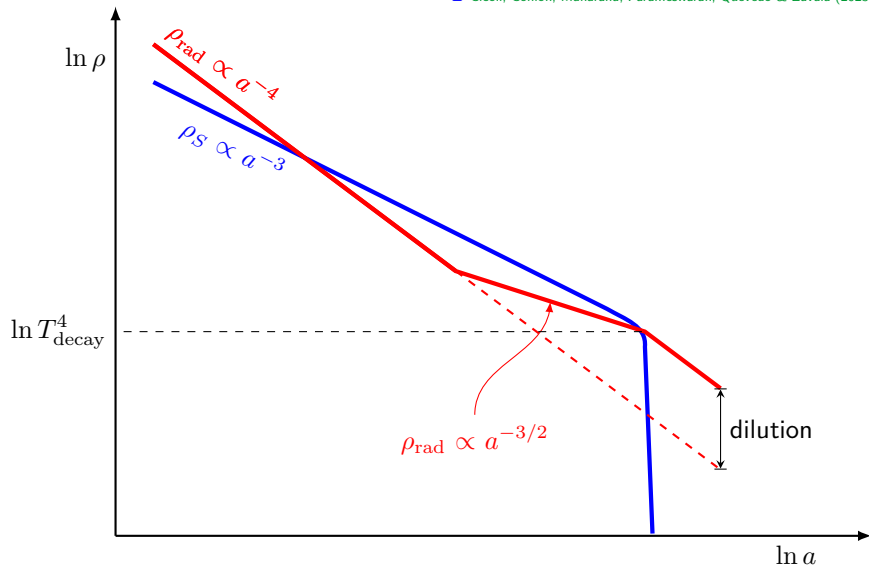
Moduli problems

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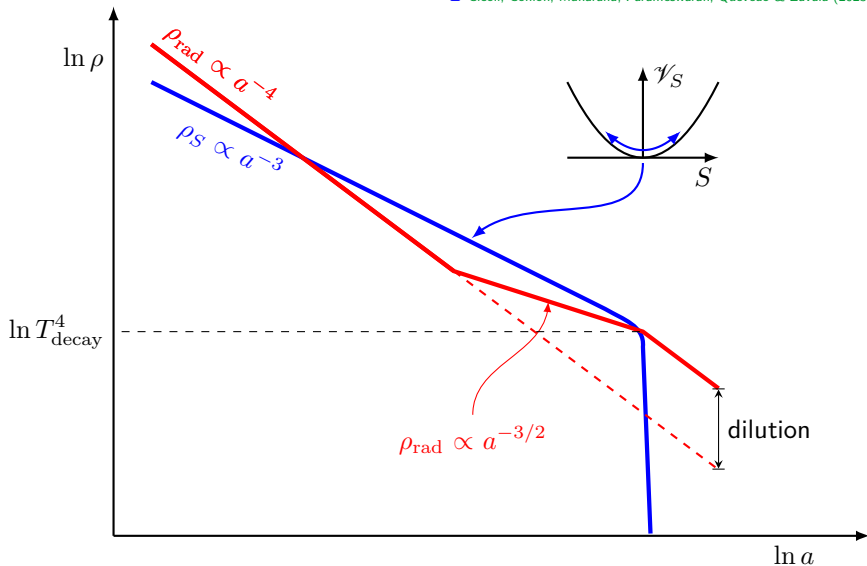
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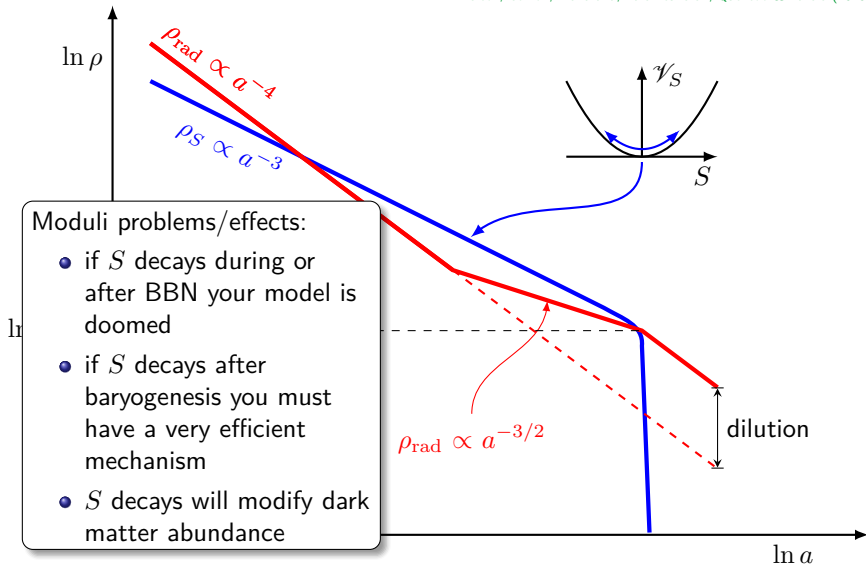
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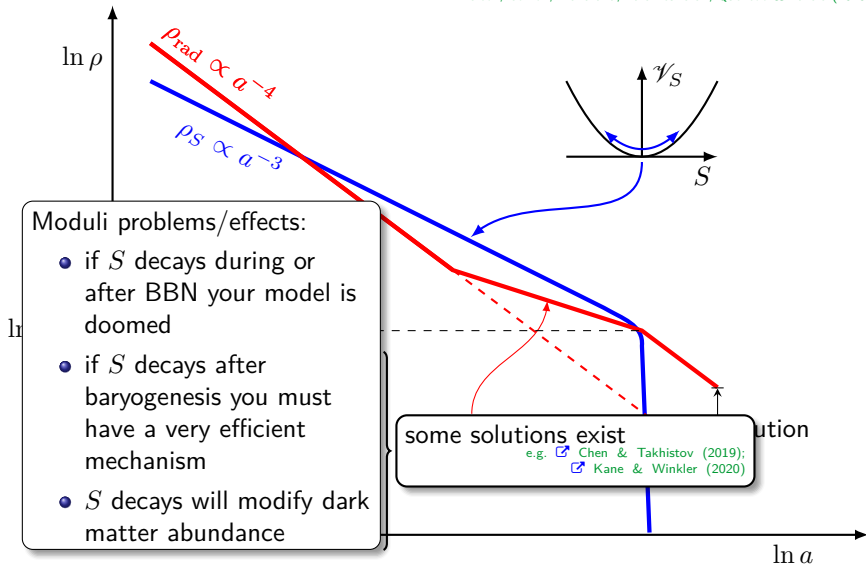
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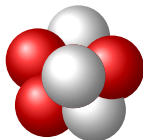


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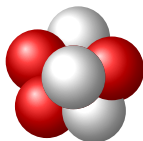
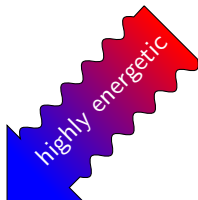
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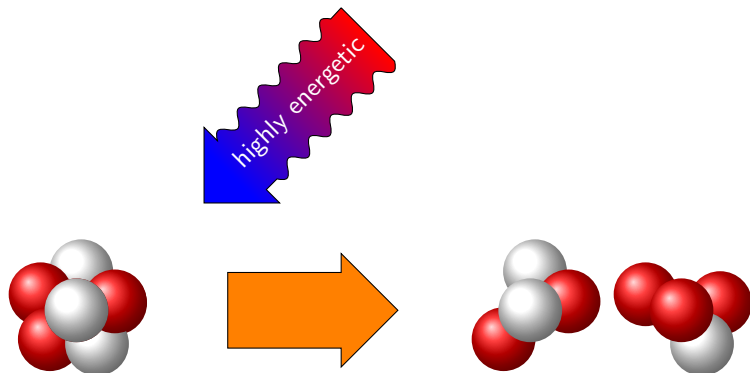
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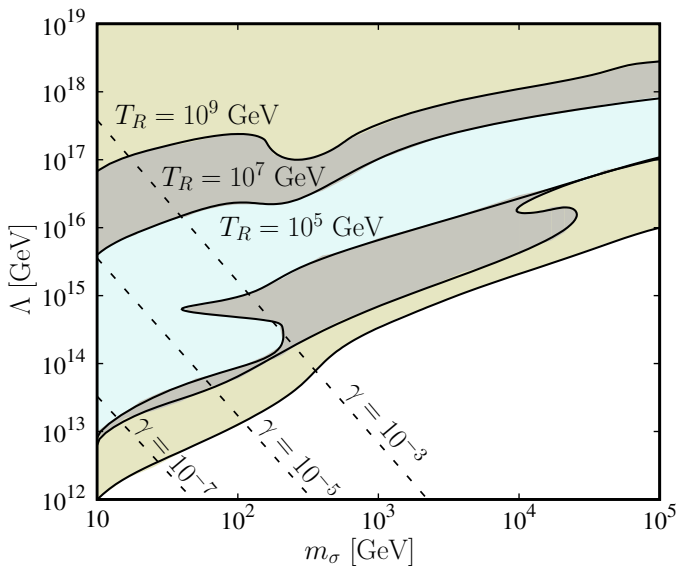


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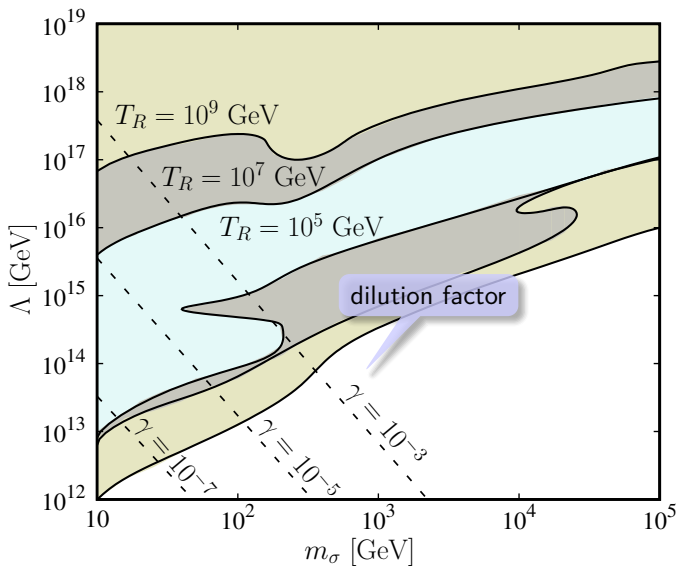
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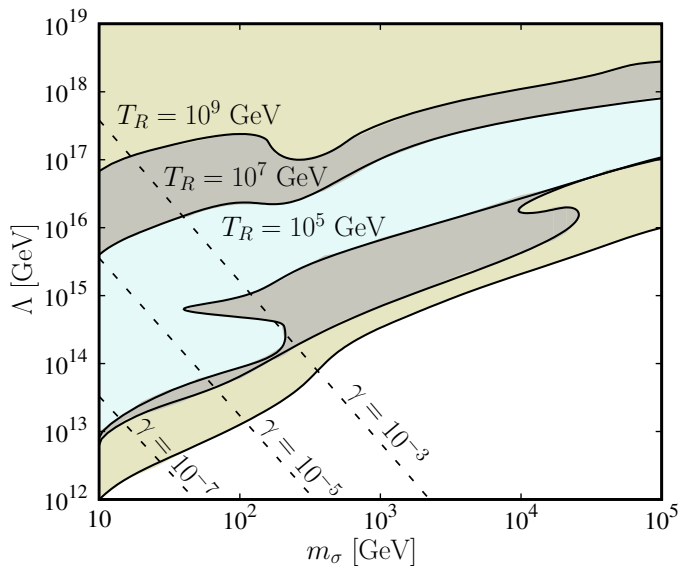
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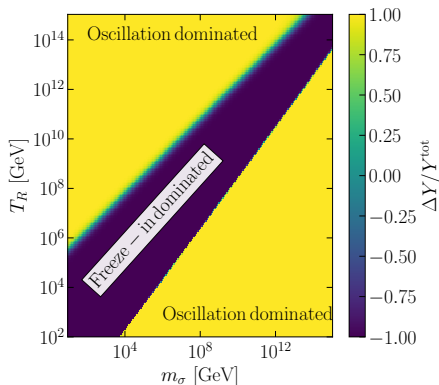
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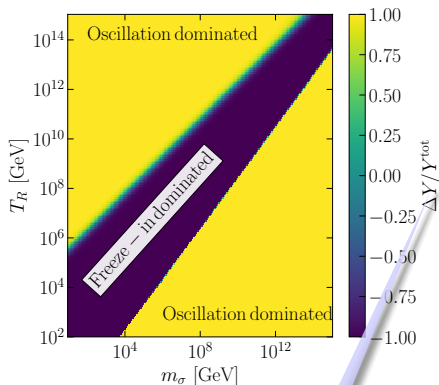
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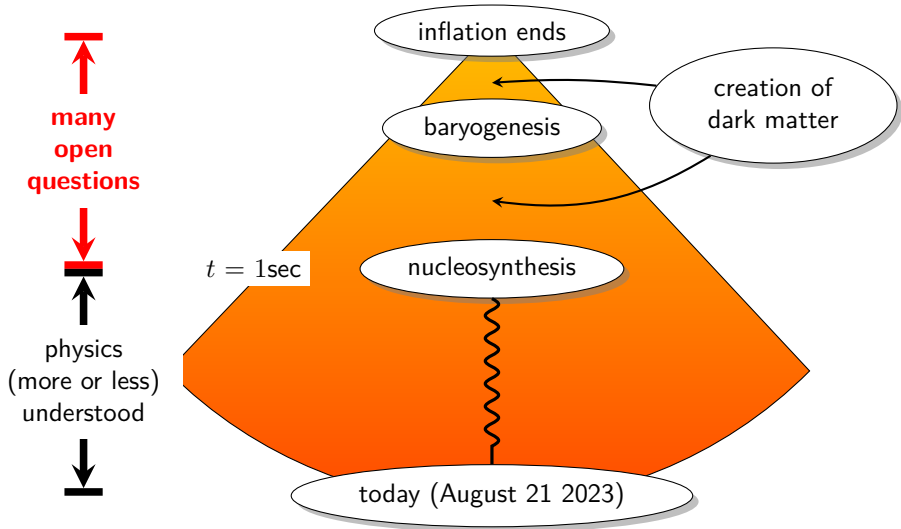
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 - flatness of inflaton potential may be easier to accomplish if couplings switch off (interplay between moduli and inflaton)

Thanks a lot!

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