

UPC 2023: International workshop on the physics of Ultra Peripheral Collisions
December 10-15, Playa del Carmen, Mexico

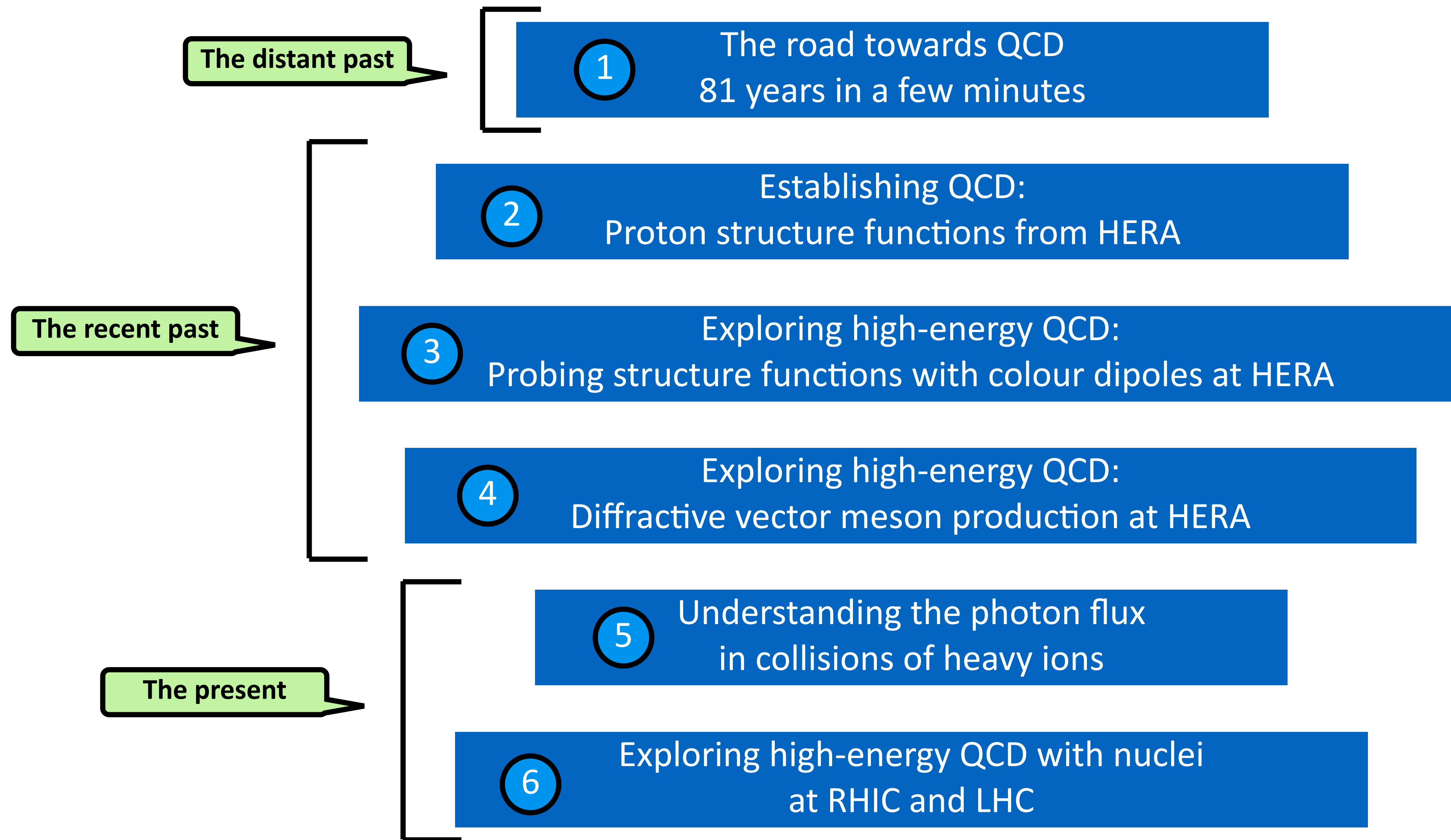
Photon-induced process to understand QCD (Mainly from the point of view of experiments)

Guillermo Contreras

Czech Technical University in Prague



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The road towards QCD
81 years in a few minutes

Science is a conversation amongst people
that takes place through articles

We have arrived late to this conversation, so let's have a look at what people have been talking about in the past

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In order to understand a bit better what we will discuss during this week

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Homework:

try to read at least one of the original papers in the next few pages

Photon-induced processes to understand the QCD structure of hadrons

Hadrons?

Photon-induced processes to understand the QCD structure of hadrons

Photon-induced processes to understand the QCD structure of hadrons

Hadrons?

structure?

Photon-induced processes to understand the QCD structure of hadrons

QCD?

Hadrons?

structure?

The first hadrons

Before we knew they were hadrons!

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1911: The discovery of nuclei (Rutherford)

Atoms have nuclei

<https://www.tandfonline.com/doi/abs/10.1080/14786440508637080>

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There are protons inside nuclei

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A new force is needed!

Some of the first models for the new force

1932: Nuclei of protons and neutrons (Heisenberg)

<https://link.springer.com/article/10.1007/BF01342433>

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New force and new particle carrying the force

1932: Nuclei of protons and neutrons (Heisenberg)

<https://link.springer.com/article/10.1007/BF01342433>

1935: A model for the nuclear force (Yukawa)

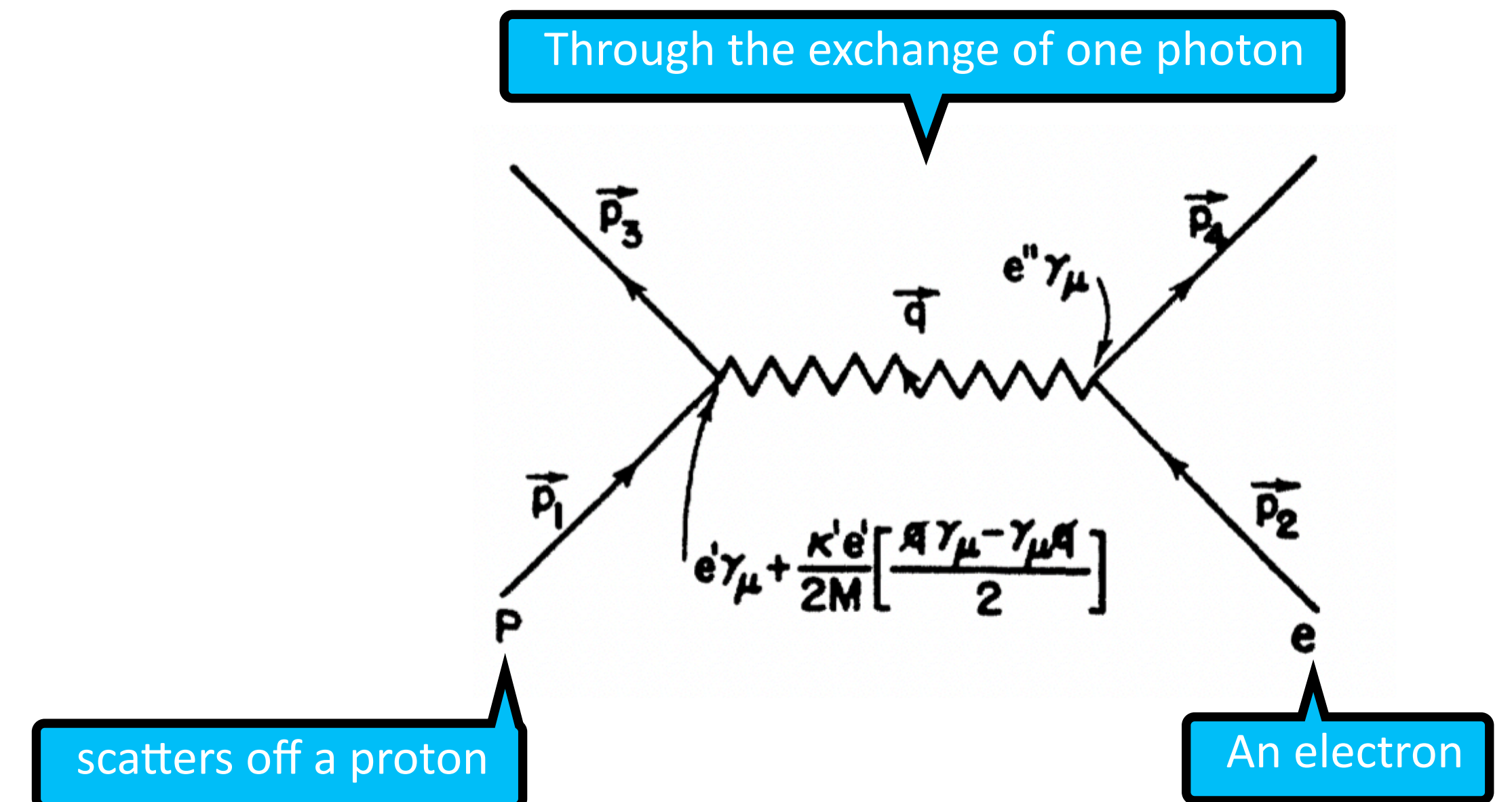
<https://academic.oup.com/ptps/article/doi/10.1143/PTPS.1.1/1878532>

At this point in time, we have hadrons and a new force

Studying hadrons with light

1950: High energy ep elastic scattering (Rosenbluth)

<https://journals.aps.org/pr/abstract/10.1103/PhysRev.79.615>



Studying hadrons with light

.... many other papers ...

1926: Collisions in QM (Born)

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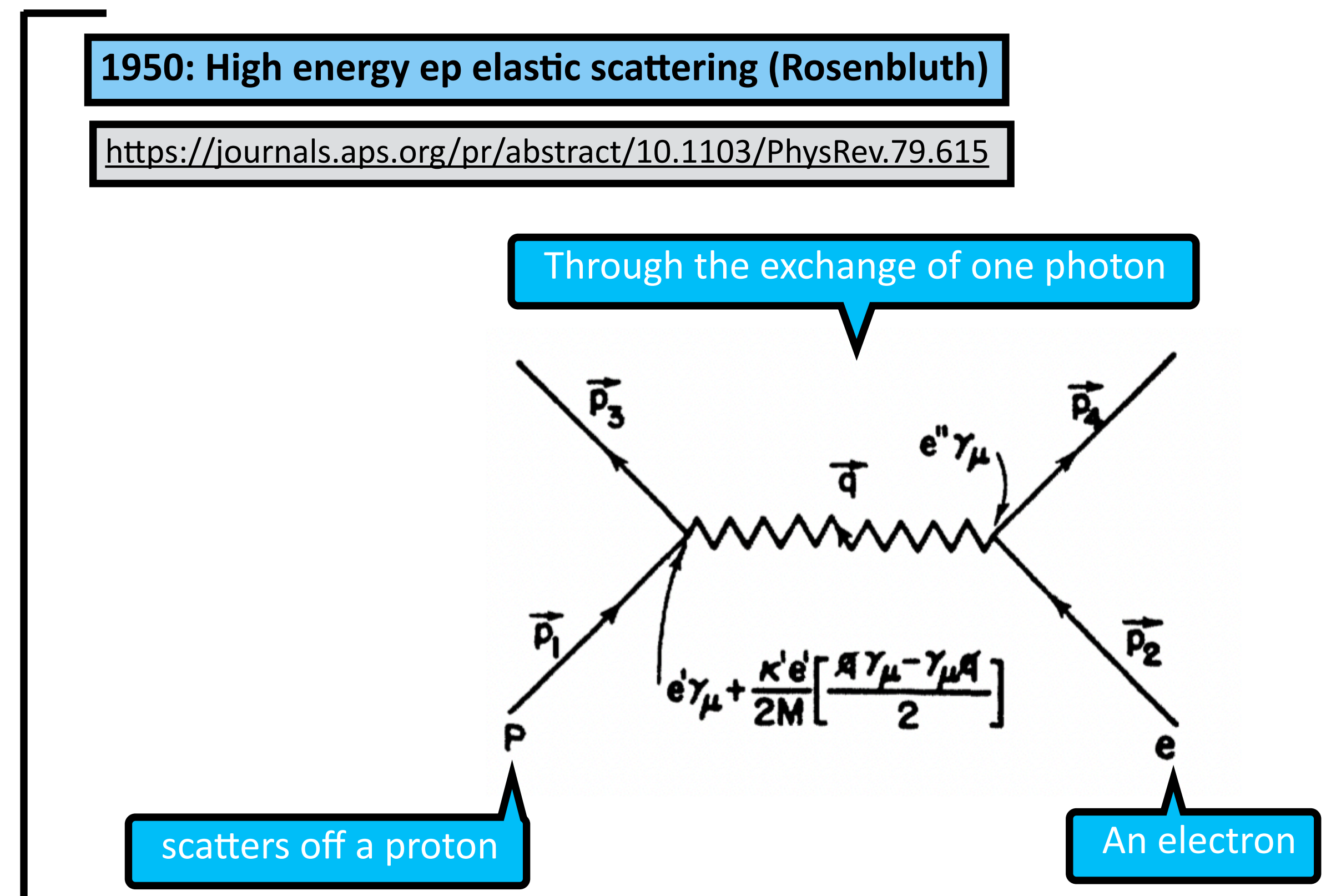
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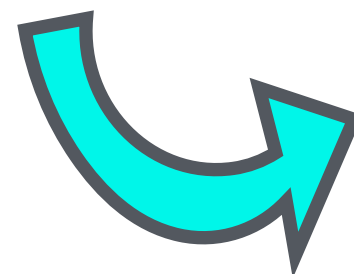
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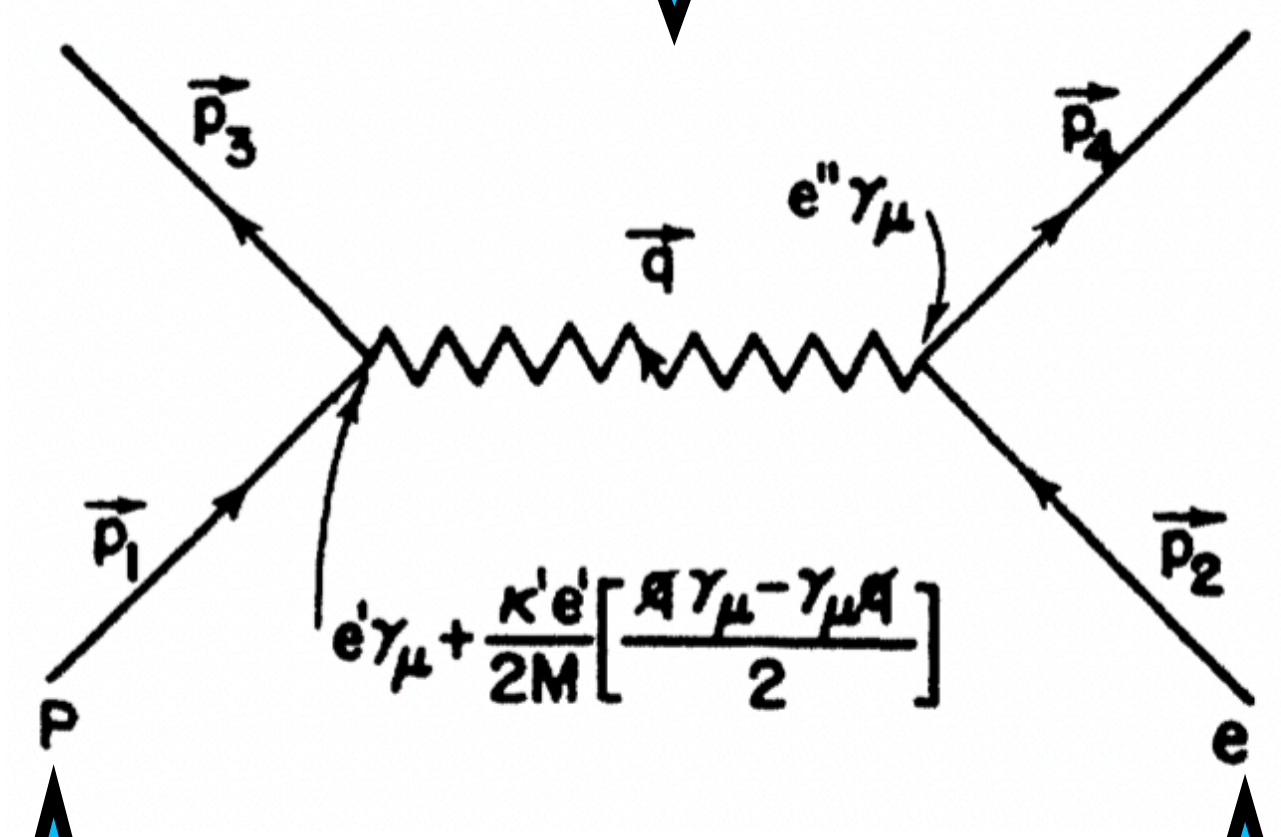
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Through the exchange of one photon

scatters off a proton

An electron



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Experiments to be performed with accelerators

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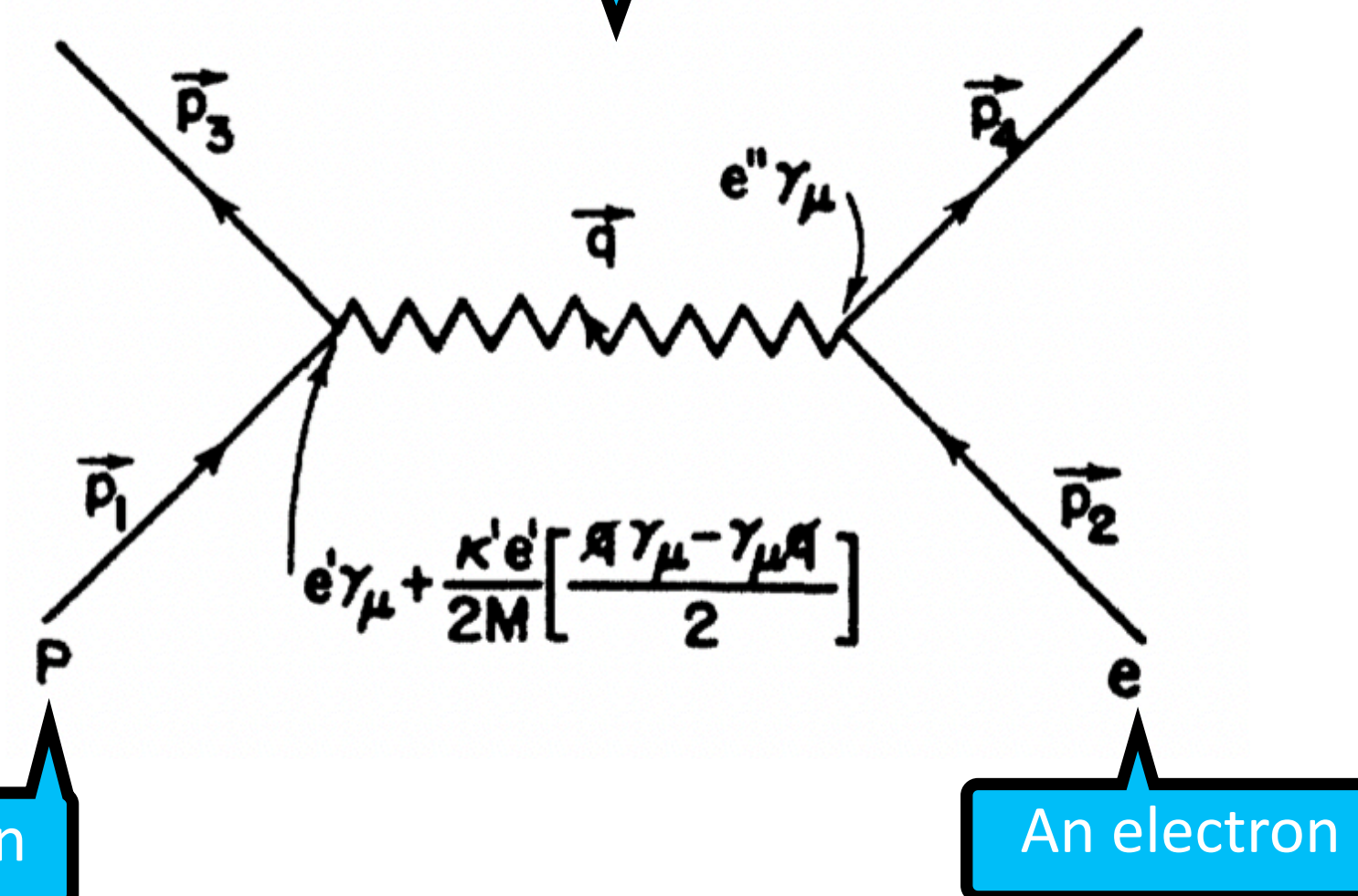
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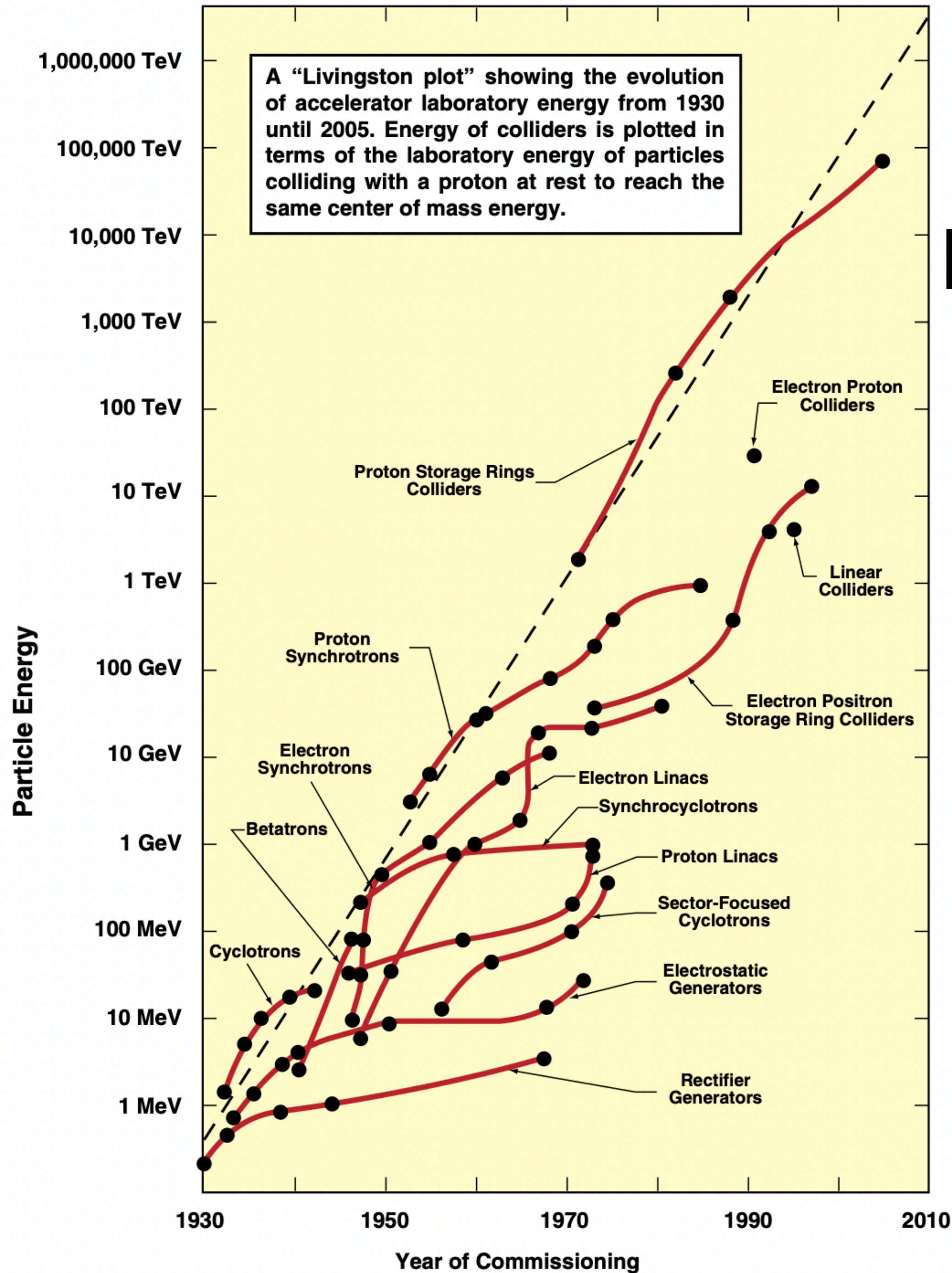
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... and we also have accelerators ...

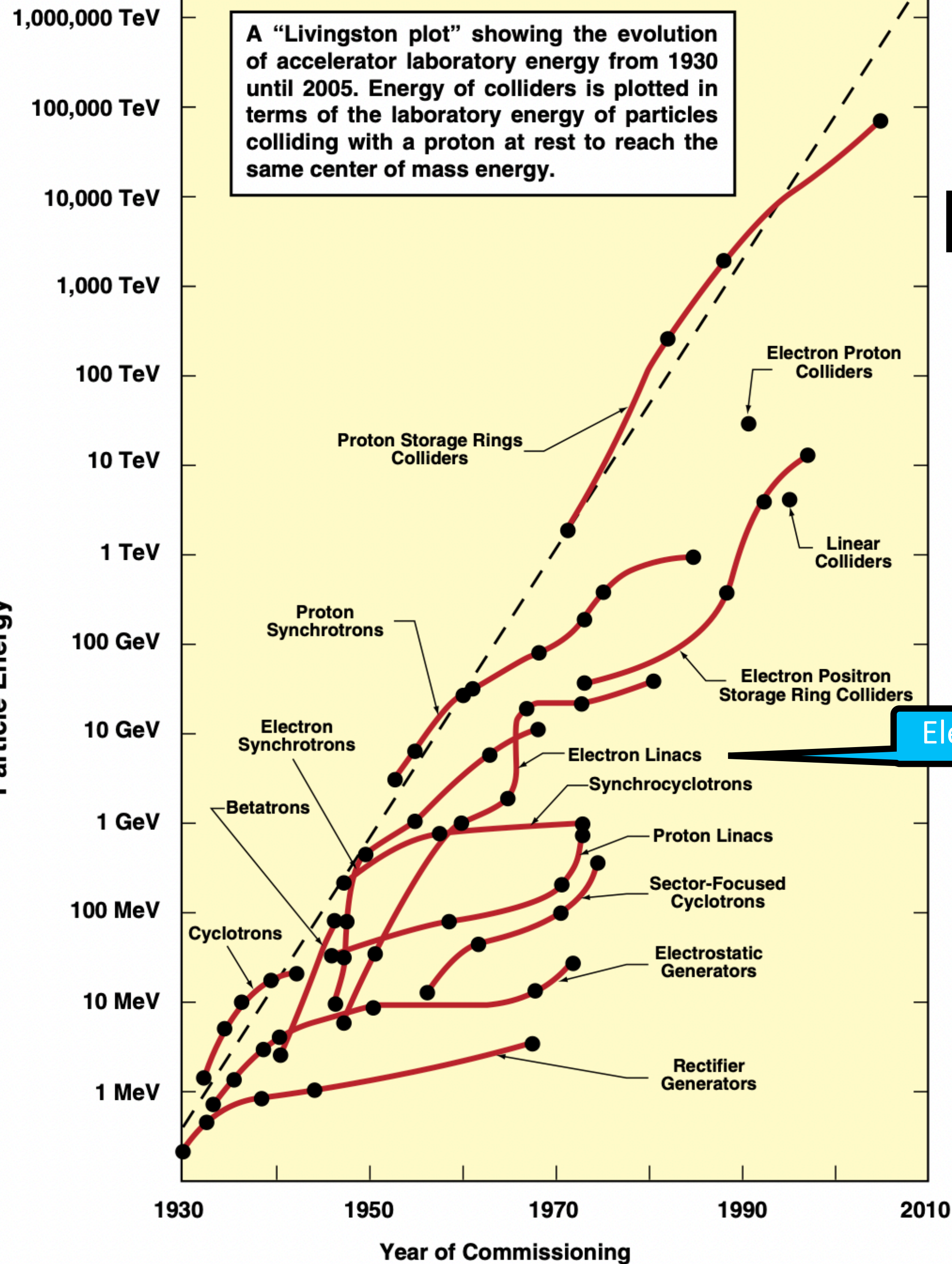
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Evolution of accelerators

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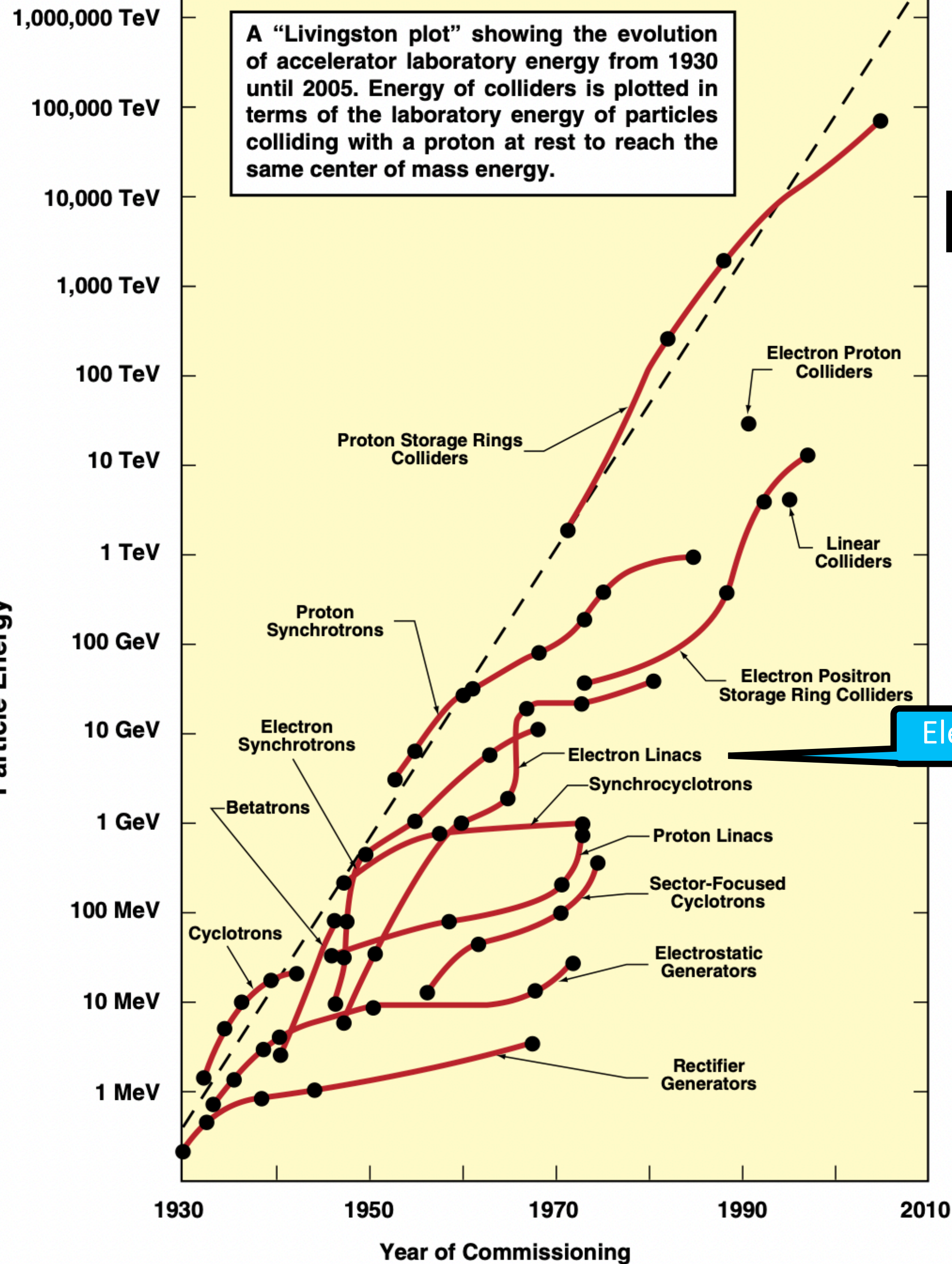
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Electron linear accelerators were used for the experiments discussed in the next slides

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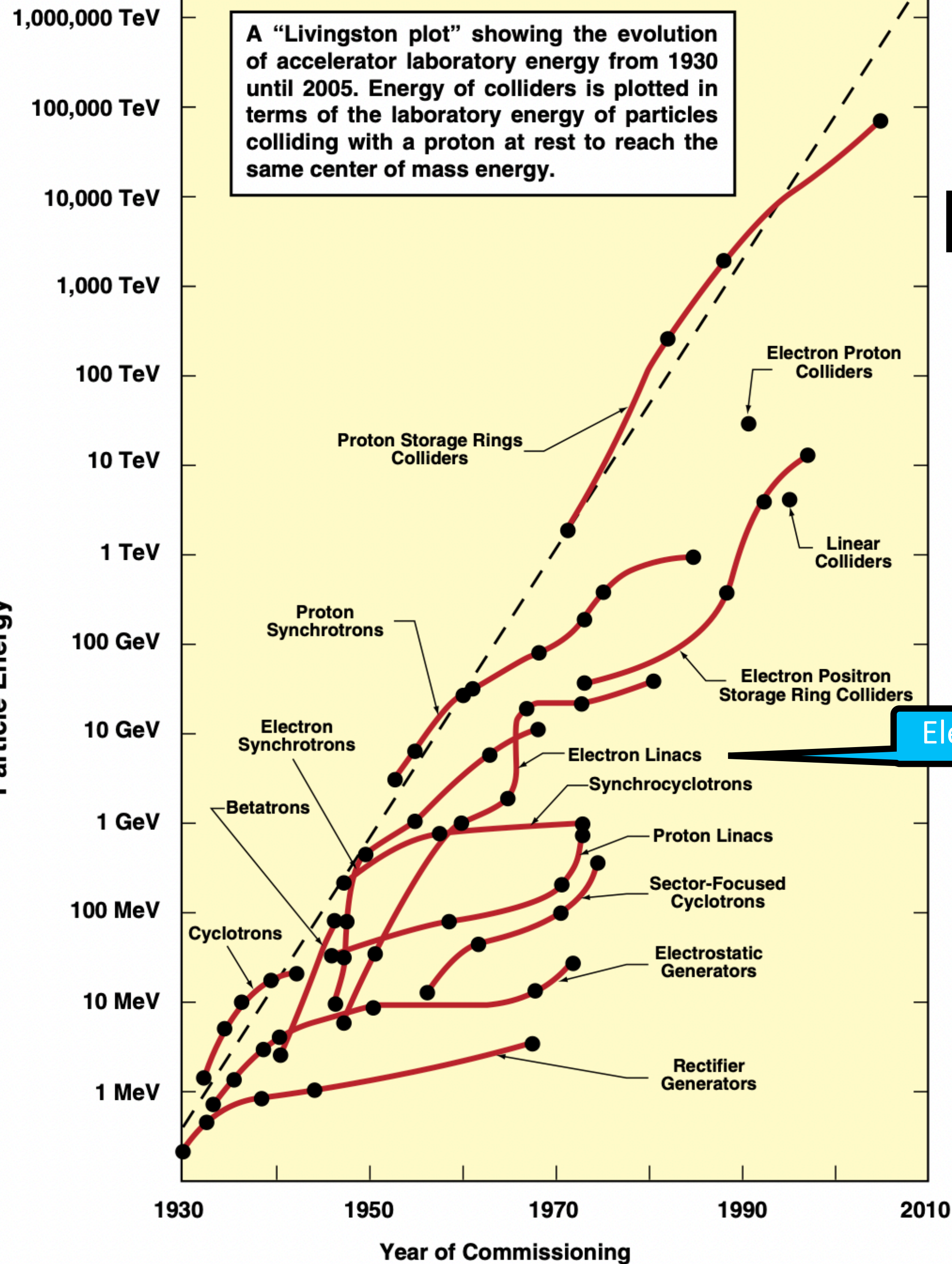


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Performed in the mid 50s, and end of 60--start of 70s

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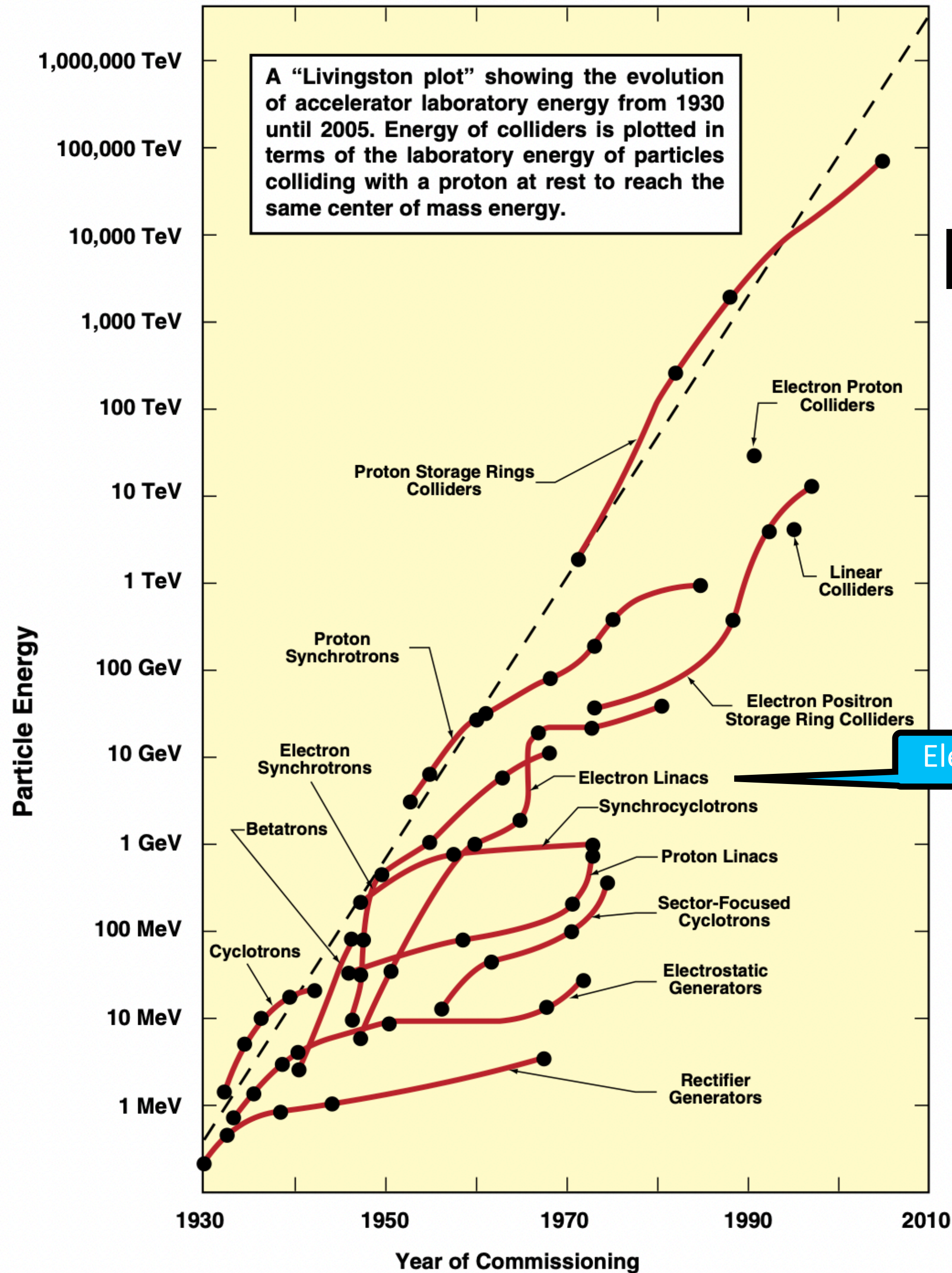
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Electron beams of up to 20 GeV

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Alpha particles from Ra reach less than 6 MeV

1966: The two-mile accelerator
Electron beams of up to 20 GeV

Protons have structure

1955: Elastic scattering (Hofstadter and McAllister)

<https://journals.aps.org/pr/abstract/10.1103/PhysRev.98.217>

Protons are not point like: RMS radius $(0.74 \pm 0.24) 10^{-13}$ cm

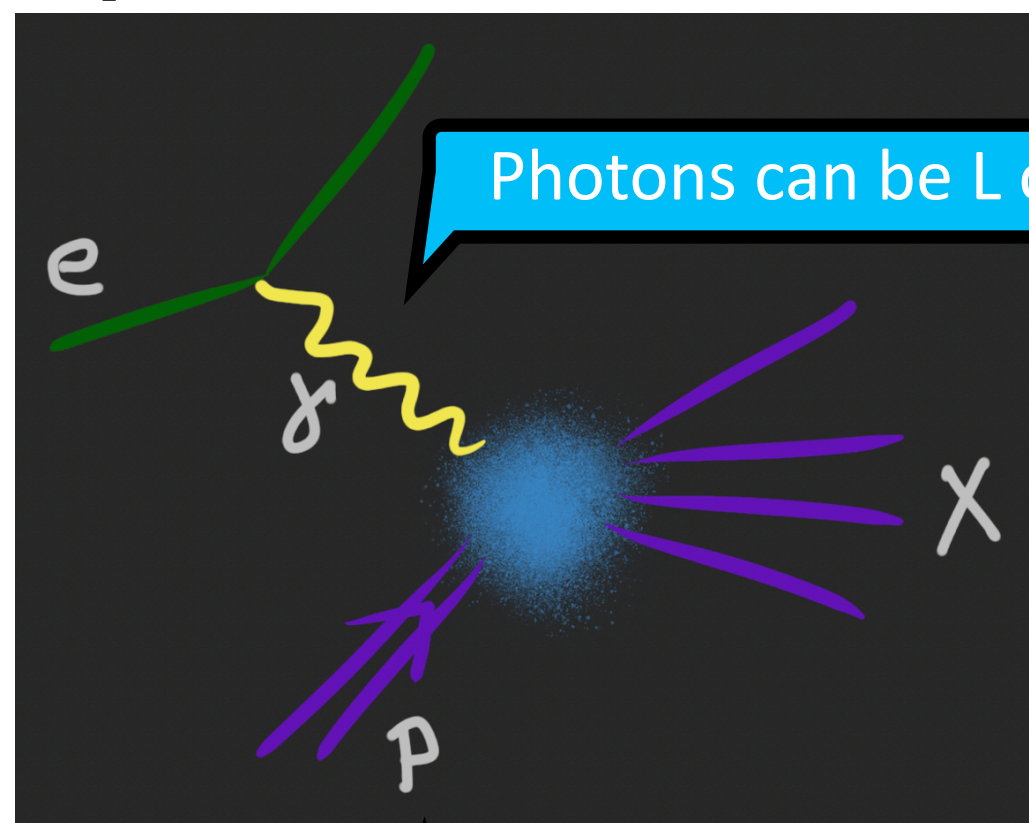
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Deep-inelastic scattering



Photons can be L or T

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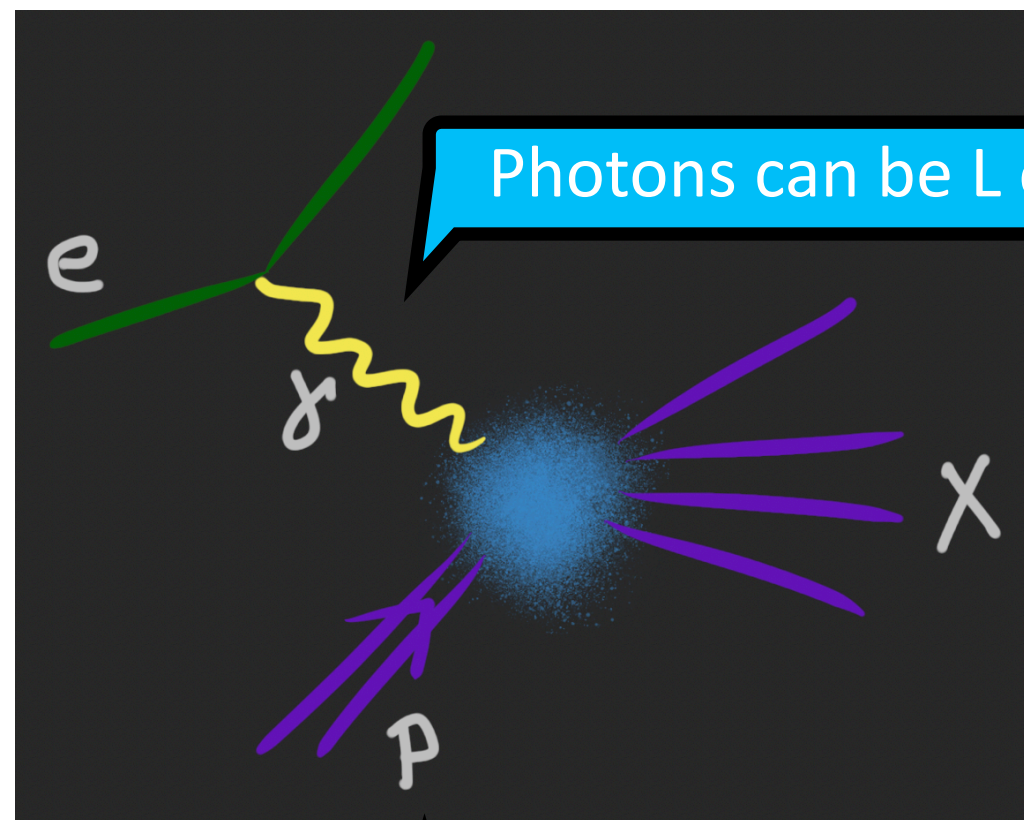
LOW q^2 ELECTRODYNAMICS, ELASTIC AND INELASTIC ELECTRON (AND MUON)
SCATTERING

No link for this one: I got it scanned thanks to the CERN Library :)

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Stanford Linear Accelerator Center, Stanford University, Stanford, Calif.

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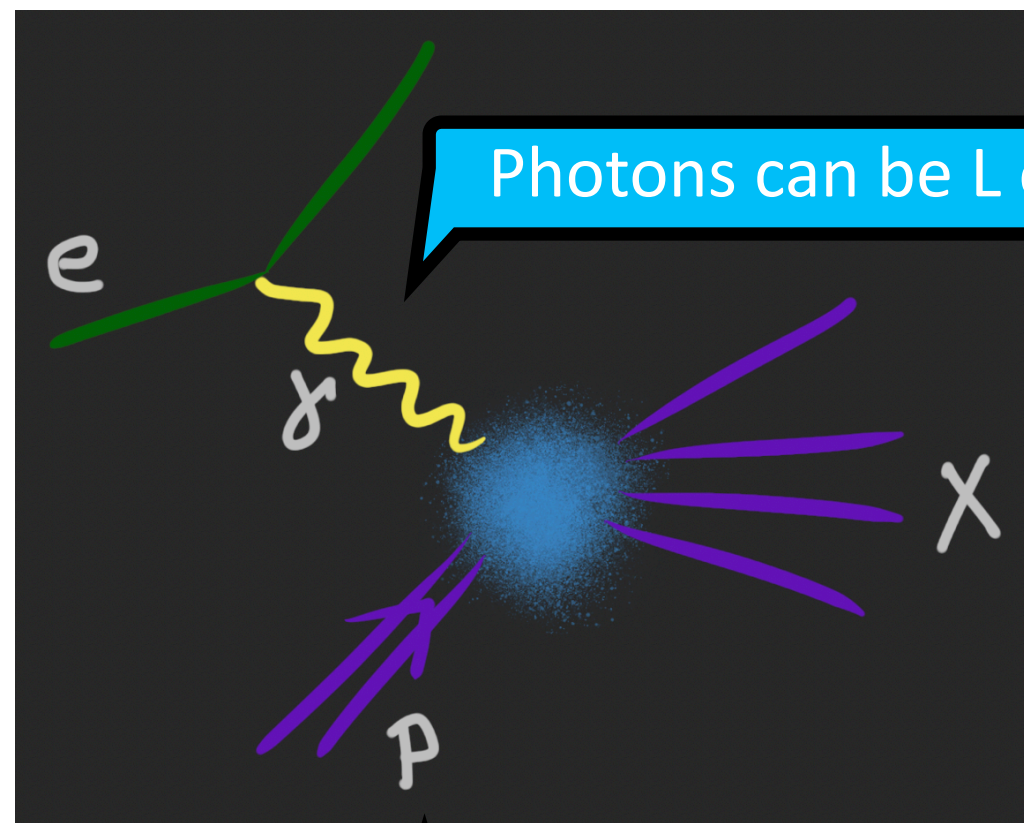
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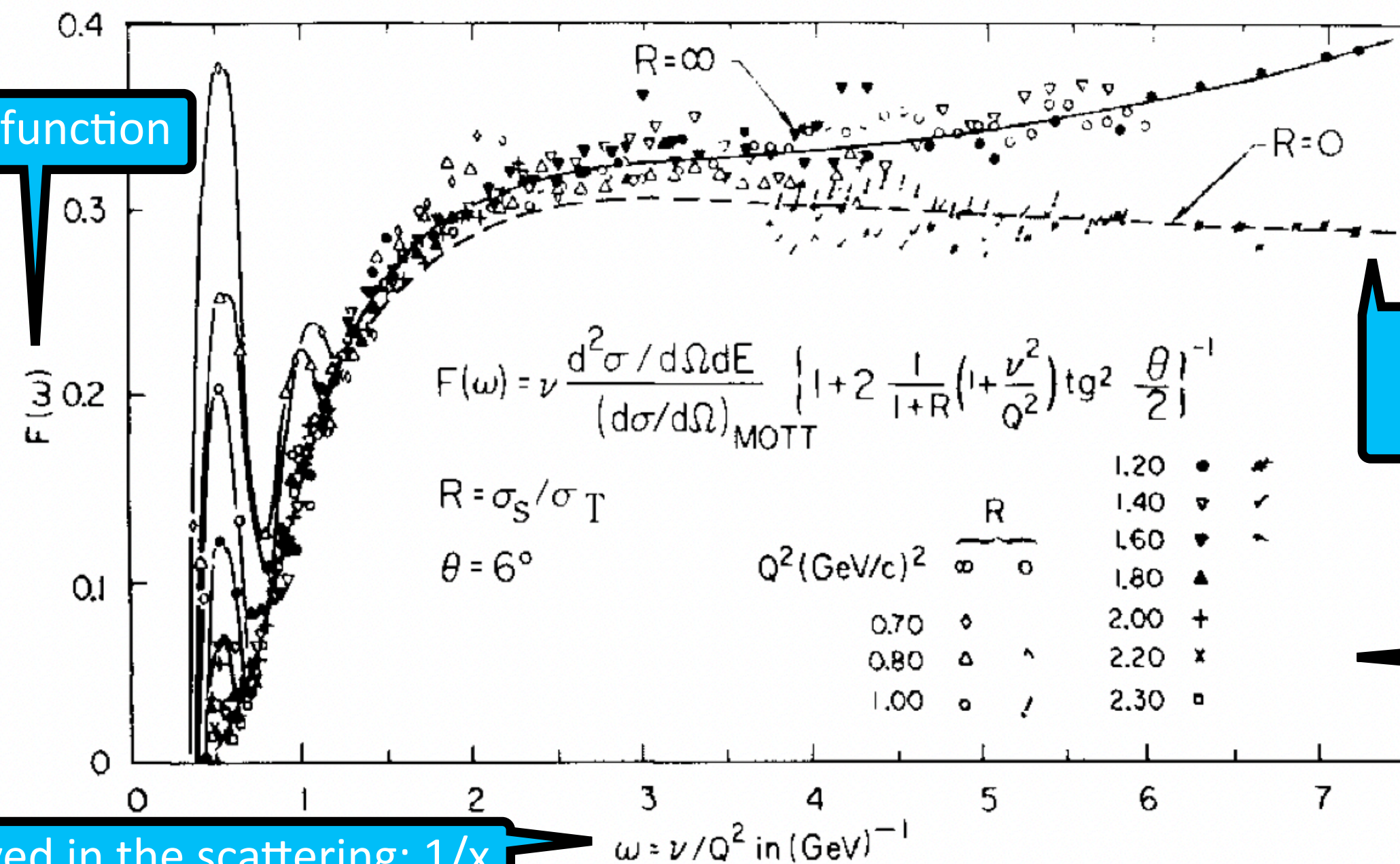
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Structure function



2 options on the behaviour of R: the ratio of L to T contributions

Different Q^2 values (virtuality/resolution of the photon)

Energy involved in the scattering: $1/x$

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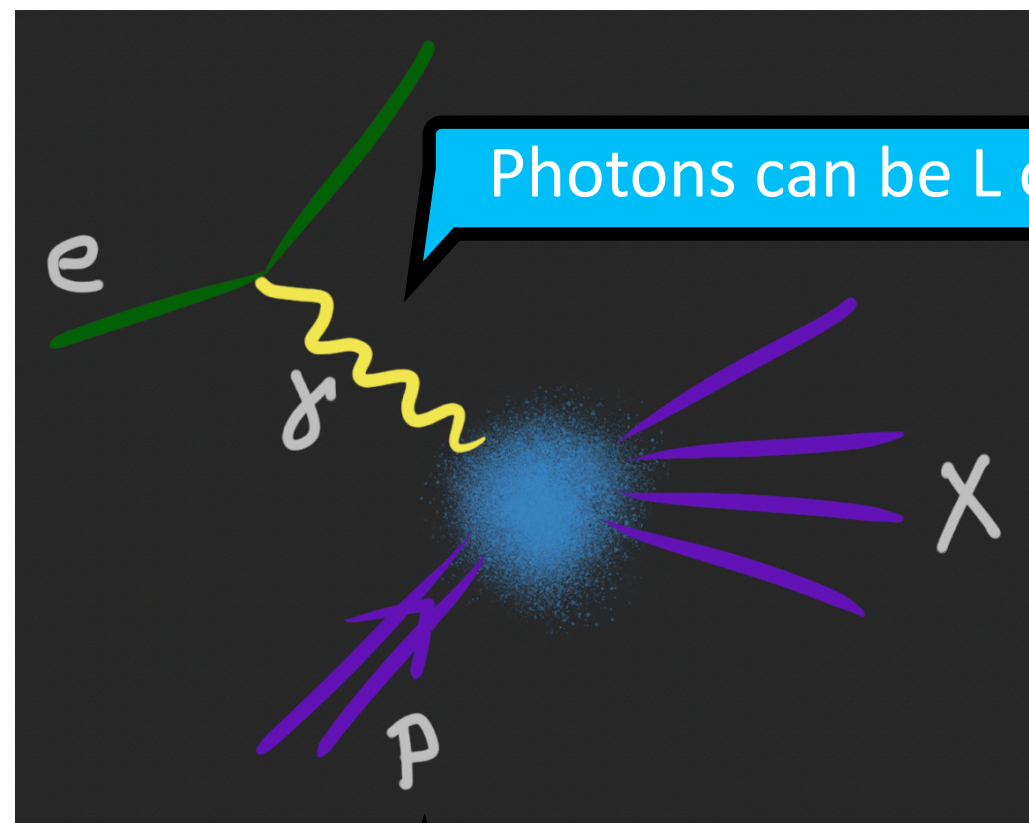
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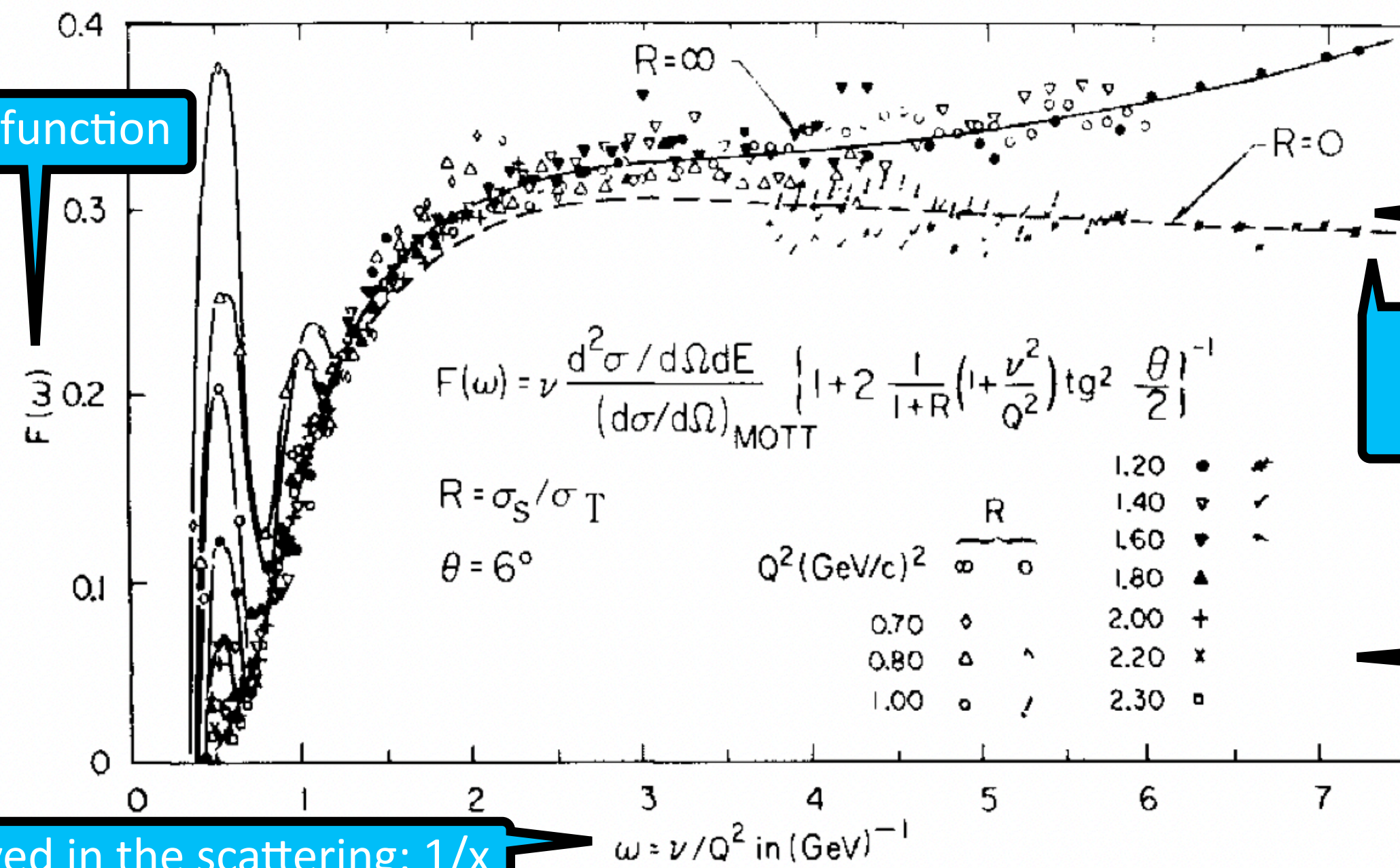
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All symbols in the same line => no dependence on the photon virtuality!

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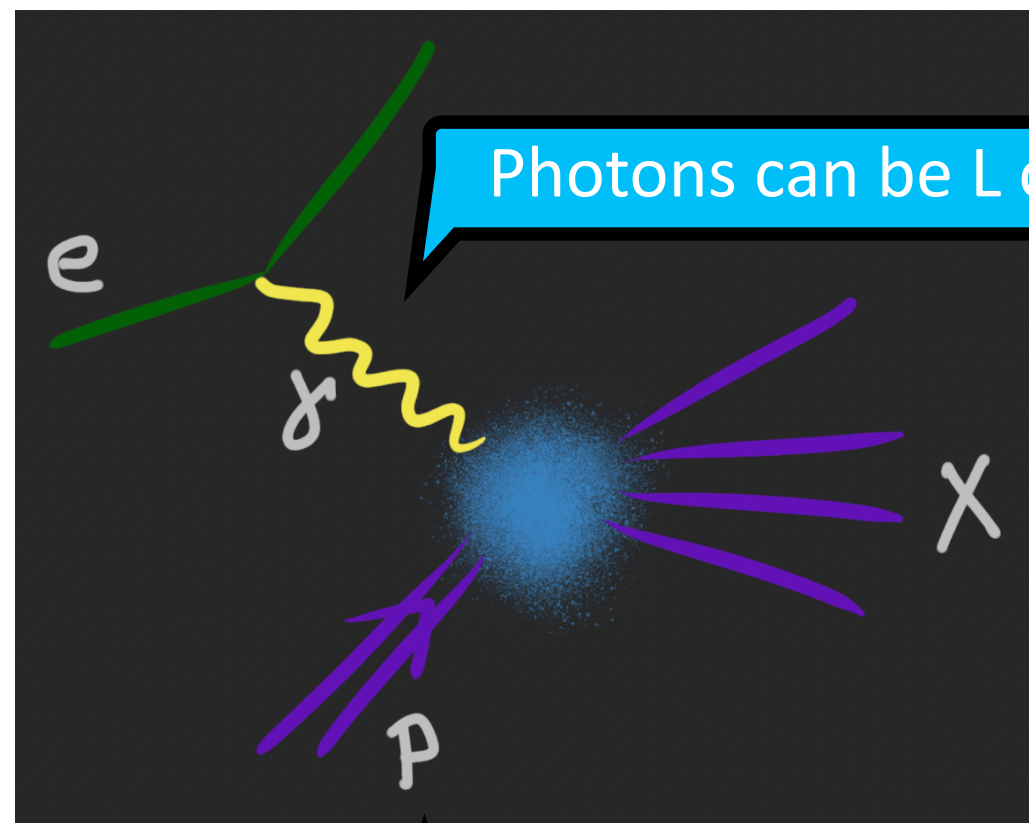
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Bjorken scaling

Deep-inelastic scattering



Structure function

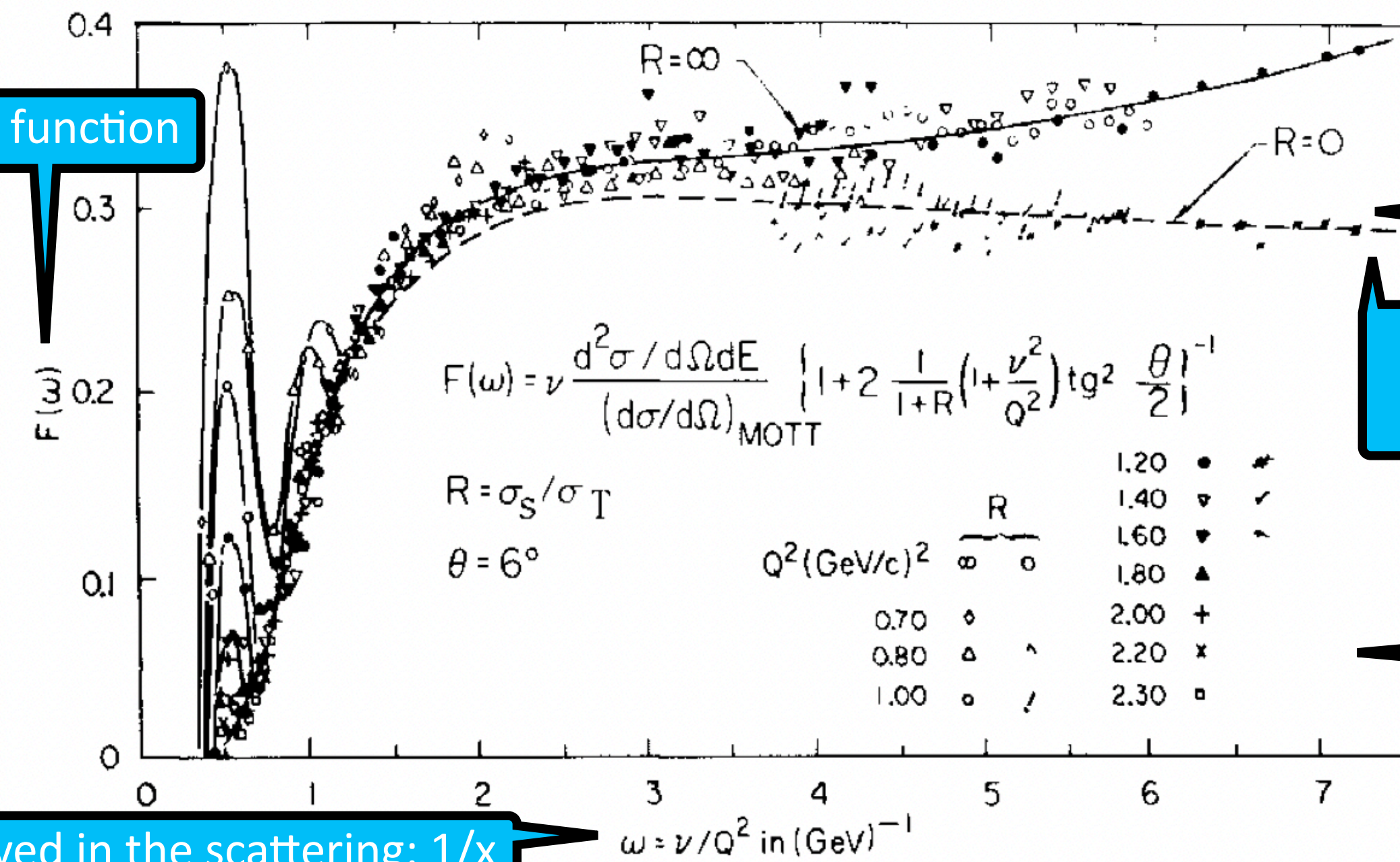
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point-like
constituents

1969: Bjorken scaling

<https://doi.org/10.1103/PhysRev.179.1547>

1969: Feynman partons

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1969: DIS in a parton picture (Bjorken and Paschos)

<https://doi.org/10.1103/PhysRev.185.1975>

DIS and partons

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point-like constituents

Picture only valid in the (proton) infinite-momentum frame

Partons are free during the interaction

Asymptotic freedom

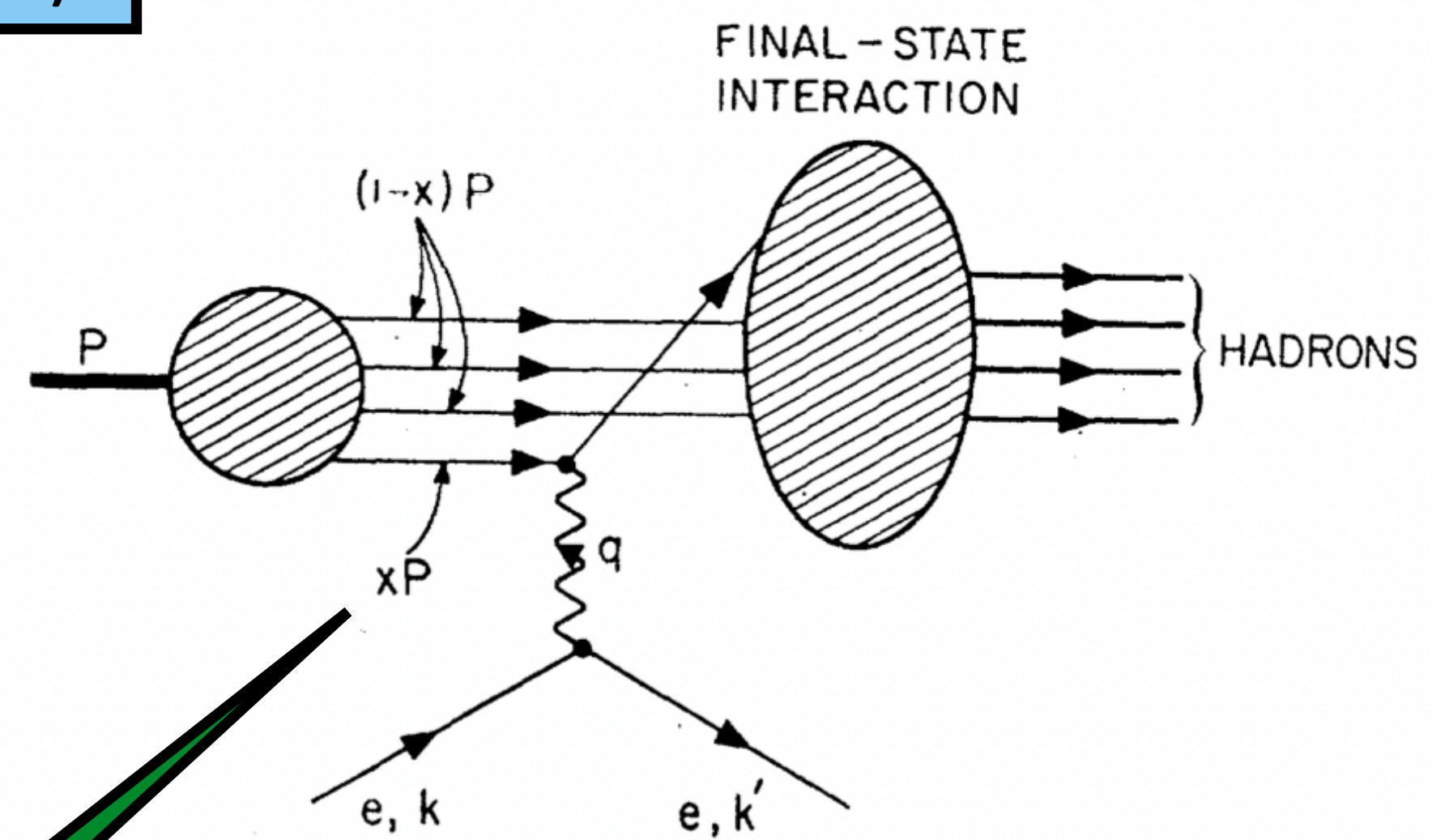


FIG. 1. Kinematics of lepton-nucleon scattering in the parton model.

Bjorken-x: fraction of the proton momentum carried by the struck parton

DIS and partons

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<https://doi.org/10.1103/PhysRev.185.1975>

1969: Callen-Gross relation

<https://doi.org/10.1103/PhysRevLett.22.156>

1972: Partons have spin 1/2 (Miller et al)

<https://doi.org/10.1103/PhysRevD.5.528>

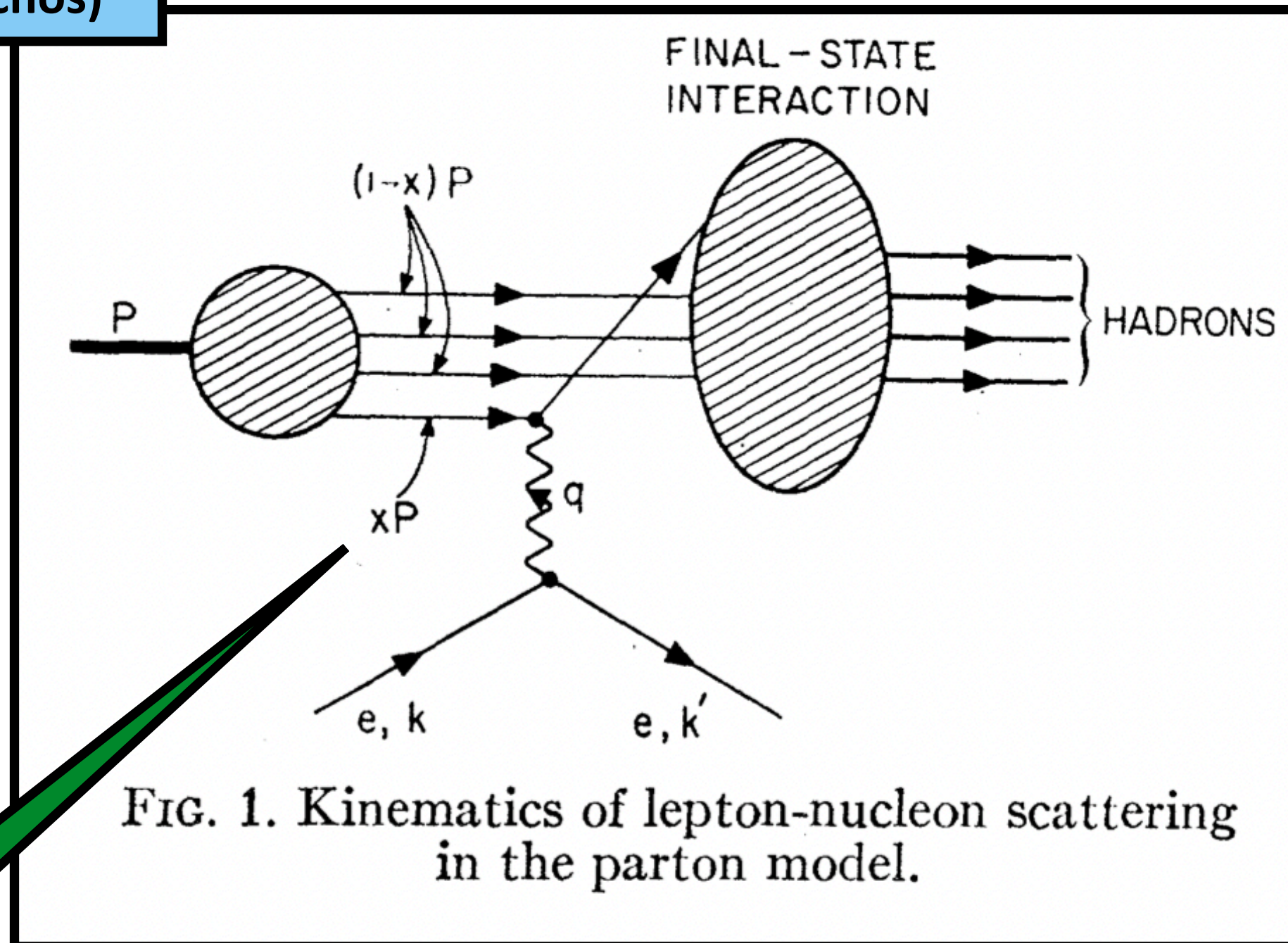
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Asymptotic freedom



At this point in time, there were many hints that protons were made of point-like constituents of spin $1/2$, but the situation in the theory front was not that clear

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How could there be 'free' constituents in the proton?

Needed to explain scaling

QCD

1973: Price of asymptotic freedom (Coleman, Gross)

<https://doi.org/10.1103/PhysRevLett.31.851>

No renormalizable field theory without non-Abelian gauge field can be asymptotically free

1973: Asymptotic freedom (Politzer, Gross and Wilczek)

<https://doi.org/10.1103/PhysRevLett.30.1346>

<https://doi.org/10.1103/PhysRevLett.30.1343>

Non-Abelian gauge field theories can be asymptotically free

1973: SU(3) color (Fritzsch, Gell-mann, Leutwyler)

[https://doi.org/10.1016/0370-2693\(73\)90625-4](https://doi.org/10.1016/0370-2693(73)90625-4)

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QCD

Charm to accept QCD

1964: Charm (Bjorken and Glashow)

[https://doi.org/10.1016/0031-9163\(64\)90433-0](https://doi.org/10.1016/0031-9163(64)90433-0)

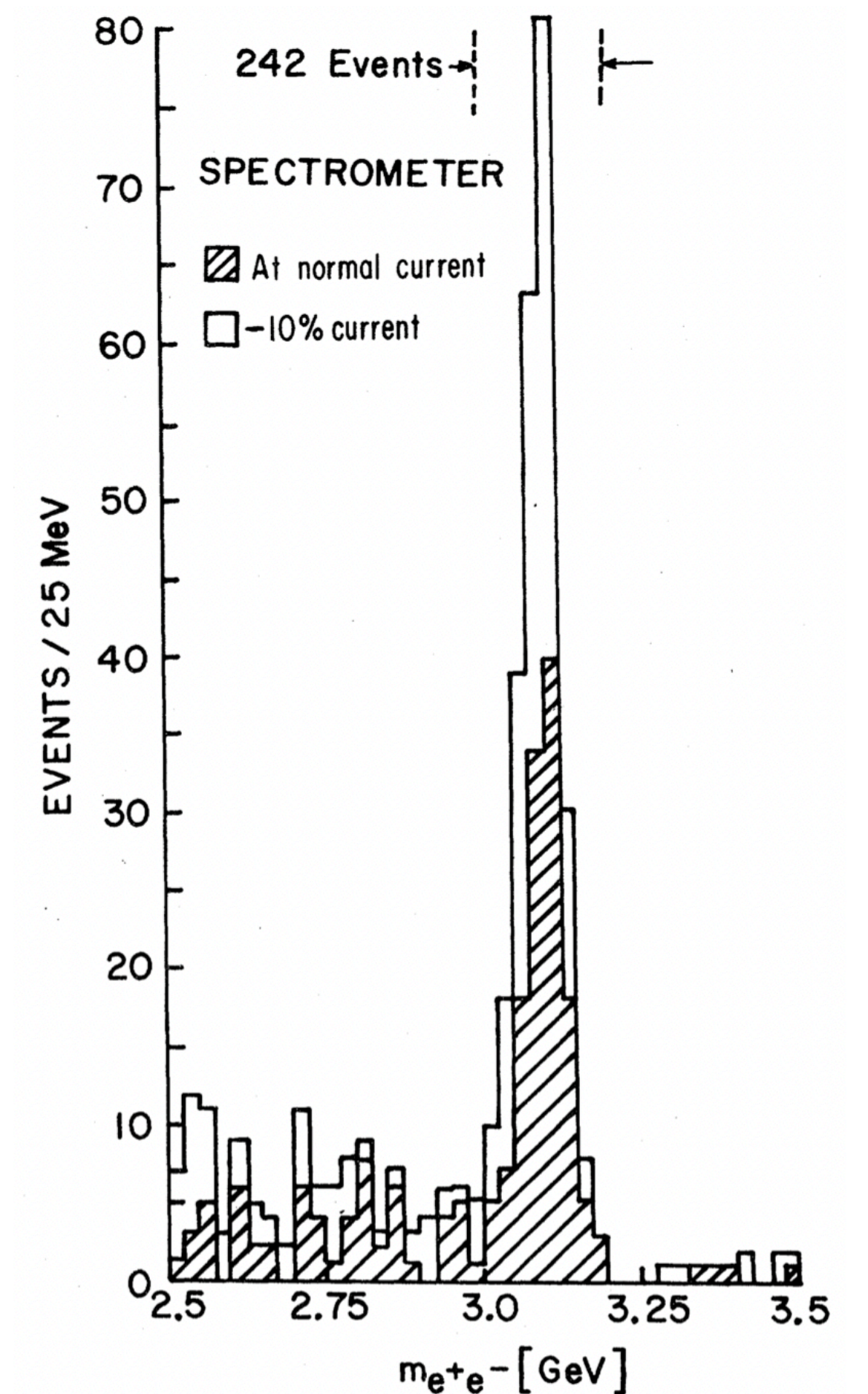
1974: J/ ψ and the November revolution (Richter et al, Ting et al)

<https://doi.org/10.1103/PhysRevLett.33.1406>

1974: charmonium (Appelquist, Politzer)

<https://doi.org/10.1103/PhysRevLett.34.43>

<https://doi.org/10.1103/PhysRevLett.33.1404>



Nobel prize 1961

<https://www.nobelprize.org/prizes/physics/1961/>
<https://www.nobelprize.org/uploads/2018/06/hofstadter-lecture.pdf>

Nobel prize 1990

<https://www.nobelprize.org/prizes/physics/1990/>
<https://www.nobelprize.org/uploads/2018/06/taylor-lecture.pdf>
<https://www.nobelprize.org/uploads/2018/06/kendall-lecture-1.pdf>
<https://www.nobelprize.org/uploads/2018/06/friedman-lecture.pdf>

To be read in this order

Nobel prize 2004

<https://www.nobelprize.org/prizes/physics/2004/>
<https://www.nobelprize.org/uploads/2018/06/gross-lecture.pdf>

Nobel prize 1961

<https://www.nobelprize.org/prizes/physics/1961/>
<https://www.nobelprize.org/uploads/2018/06/hofstadter-lecture.pdf>

Nobel prize 1990

<https://www.nobelprize.org/prizes/physics/1990/>
<https://www.nobelprize.org/uploads/2018/06/taylor-lecture.pdf>
<https://www.nobelprize.org/uploads/2018/06/kendall-lecture-1.pdf>
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<https://www.nobelprize.org/prizes/physics/2004/>
<https://www.nobelprize.org/uploads/2018/06/gross-lecture.pdf>

Homework:

try to read at least the 1990 lectures

At this point in time, we have a theory to explain scaling
But QCD is a lot more than scaling ...

2

Establishing QCD: Proton structure functions from HERA

Reminder: how do data tell us about QCD?

Deep-inelastic scattering: QED and Lorentz invariance

This is the cross section to be measured

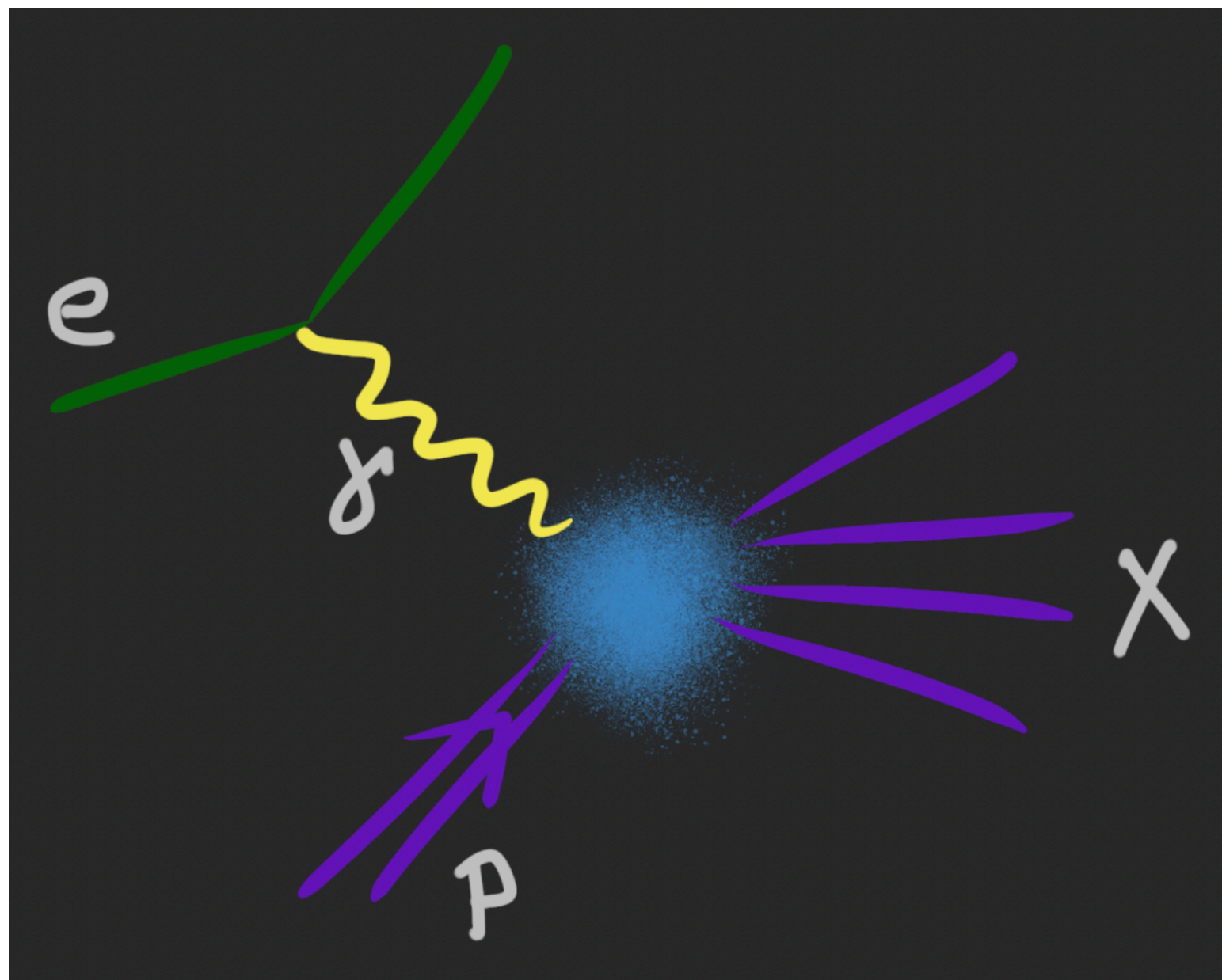
$$\frac{d\sigma^{ep}}{dx dQ^2}$$

Deep-inelastic scattering: QED and Lorentz invariance

This is the cross section to be measured

$$\frac{d\sigma^{ep}}{dx dQ^2} \sim \frac{1}{Q^4} L_{\mu\nu} W^{\mu\nu}$$

One photon exchange



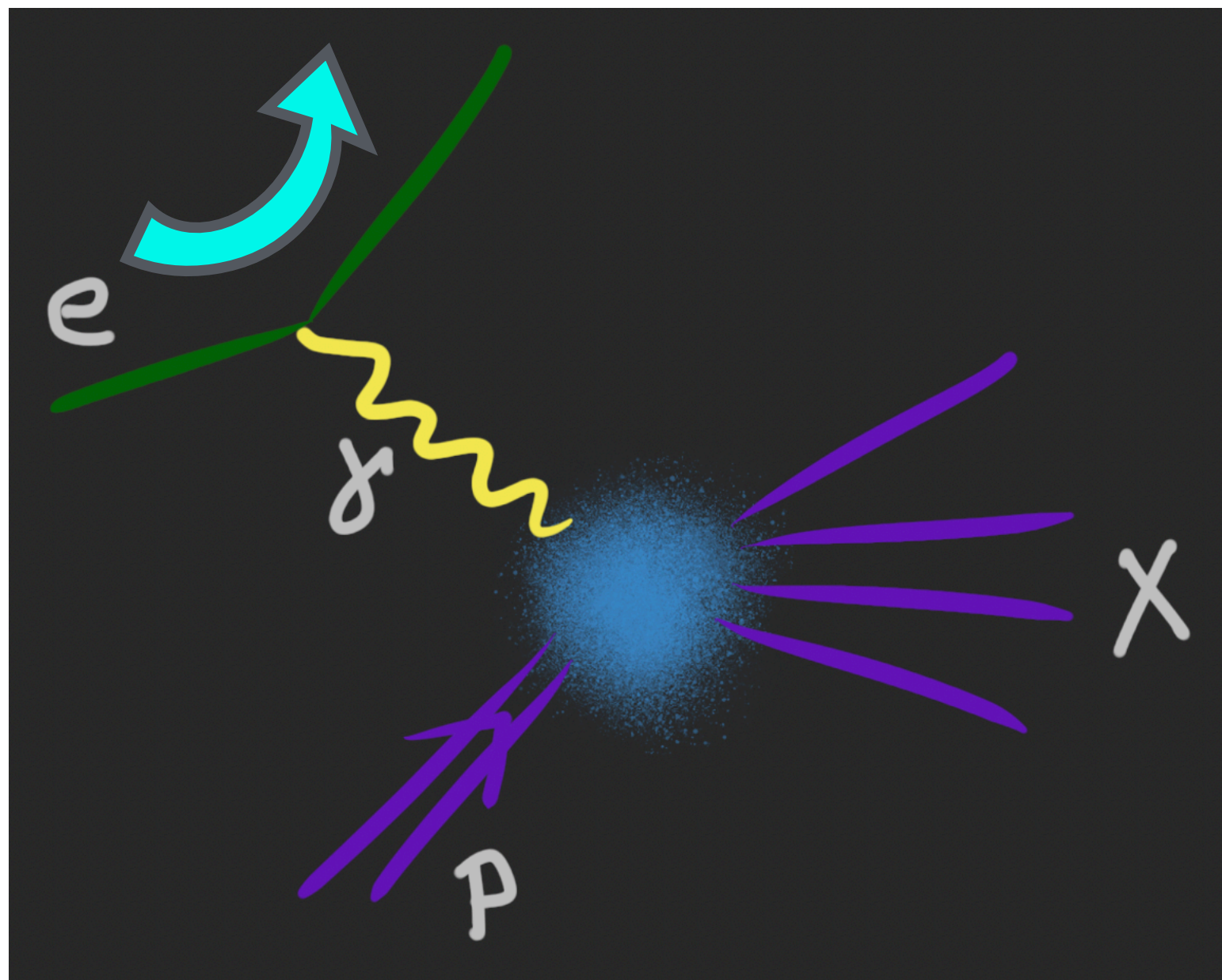
Deep-inelastic scattering: QED and Lorentz invariance

This is the cross section to be measured

The EM current gives rise to a tensor

$$\frac{d\sigma^{ep}}{dx dQ^2} \sim \frac{1}{Q^4} L_{\mu\nu} W^{\mu\nu}$$

One photon exchange



Deep-inelastic scattering: QED and Lorentz invariance

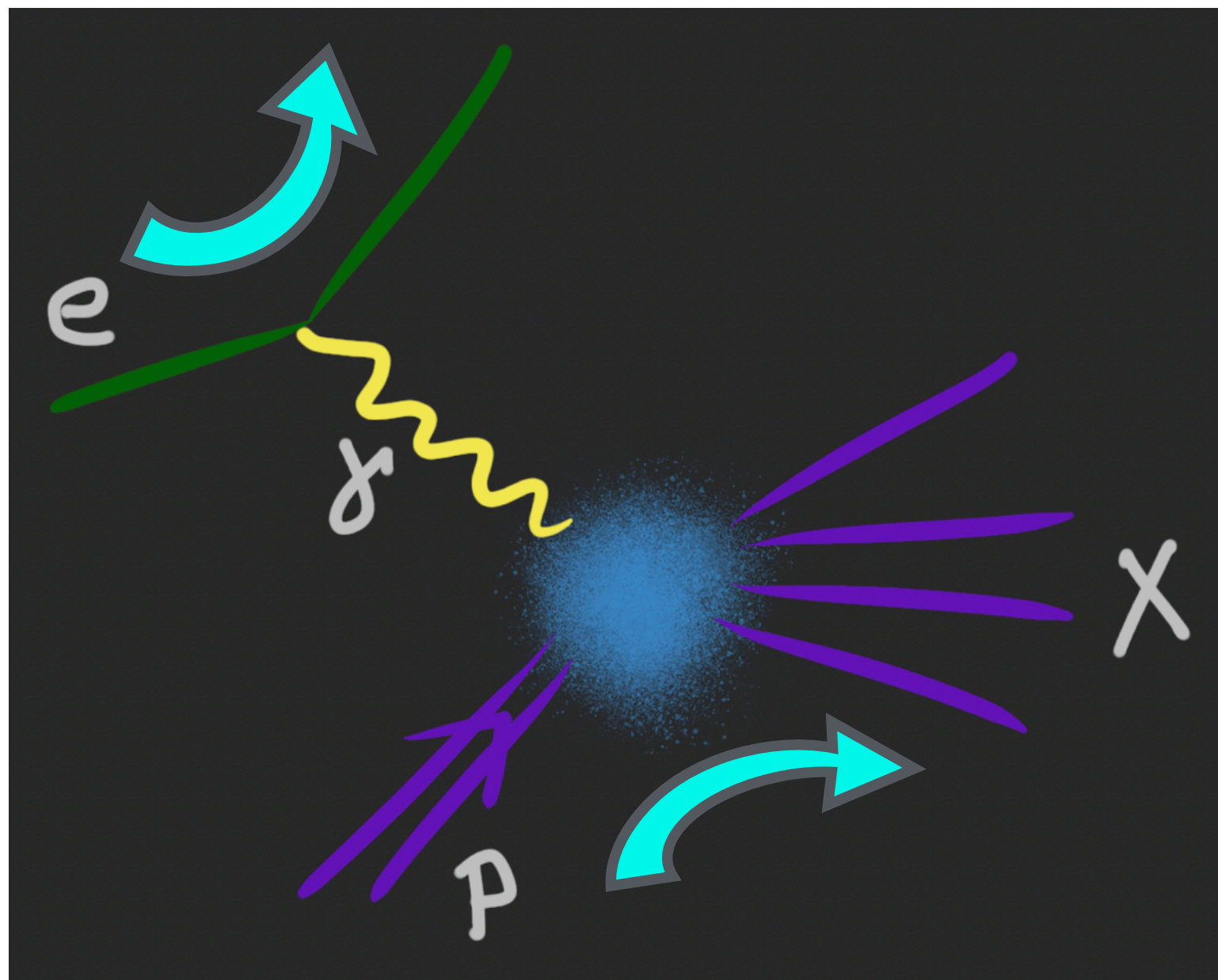
This is the cross section to be measured

$$\frac{d\sigma^{ep}}{dx dQ^2} \sim \frac{1}{Q^4} L_{\mu\nu} W^{\mu\nu}$$

The EM current gives rise to a tensor

The hadronic current then has also to be a tensor

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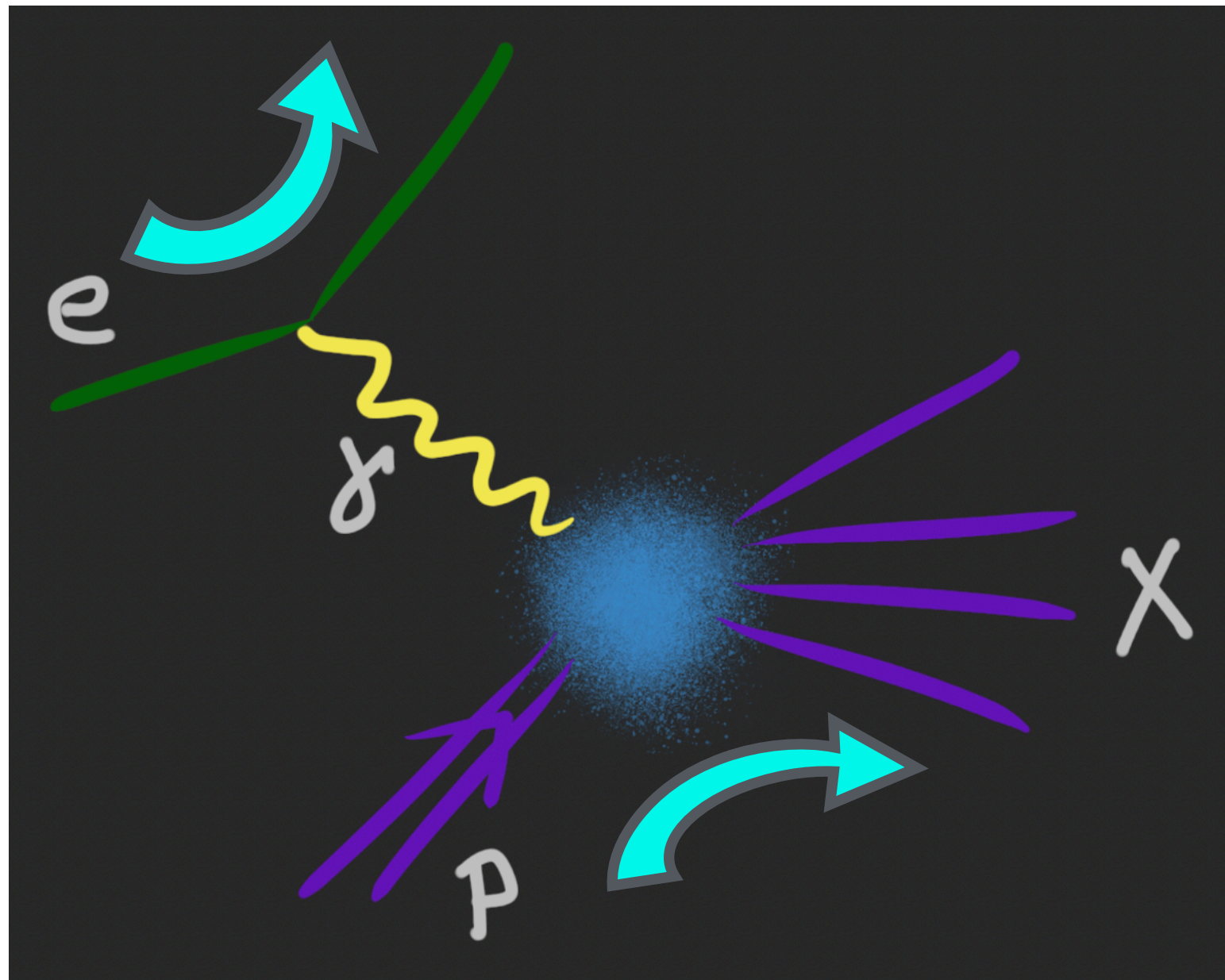
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Noting that:

- ✓ The lepton tensor is symmetric
- ✓ Photon exchange conserves parity
- ✓ The current is conserved
- ✓ Summing and averaging over spins

The most general tensor can be expressed as

$$W^{\mu\nu} = W_1 \left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) + W_2 \frac{1}{M^2} \left(p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) \left(p^\nu - \frac{p \cdot q}{q^2} q^\nu \right)$$



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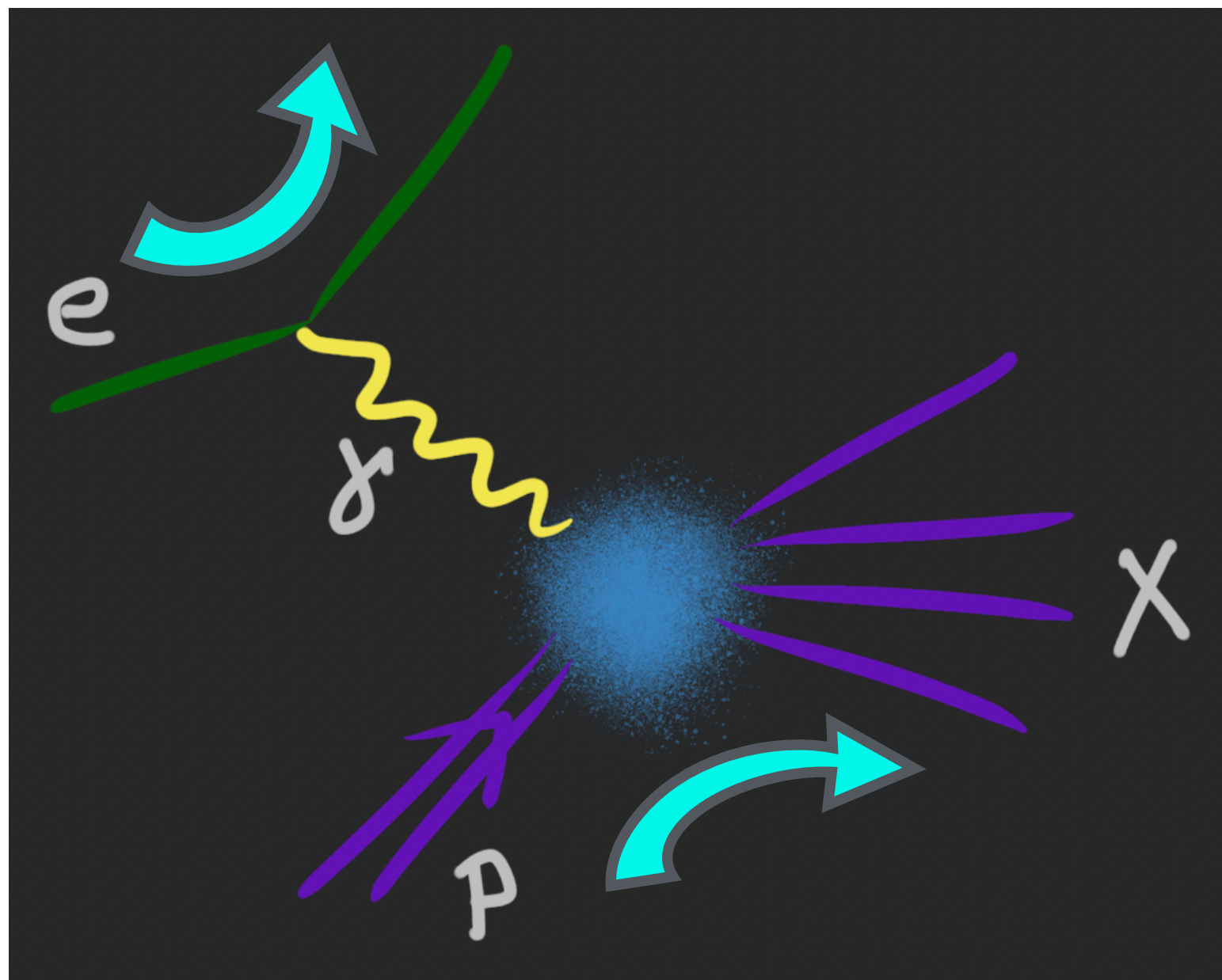
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For large photon virtualities and in a frame where the proton is moving infinitely fast

$$MW_1 \rightarrow F_1 \quad \text{and} \quad \nu W_2 \rightarrow F_2$$

Structure functions



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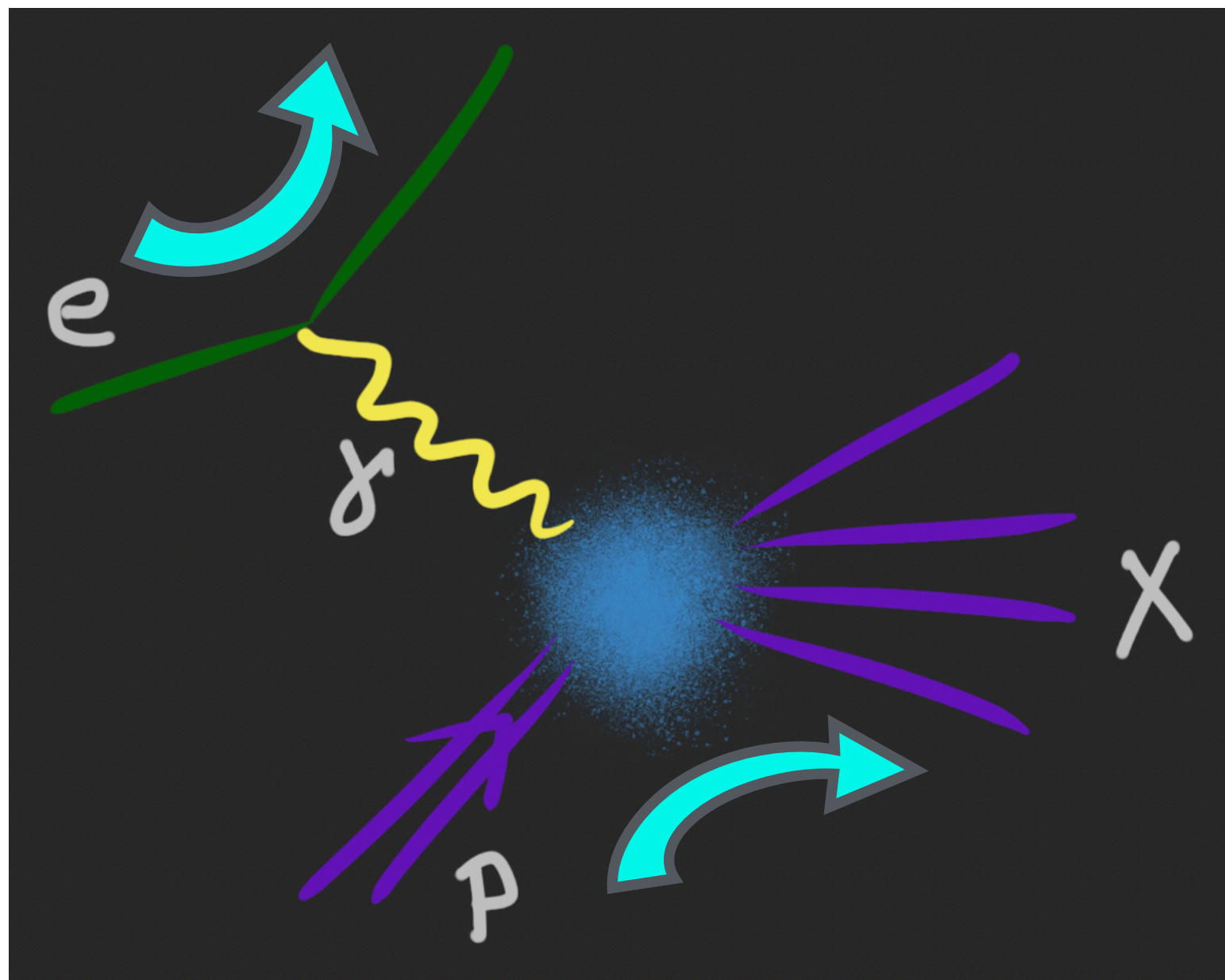
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If the constituents have spin one half

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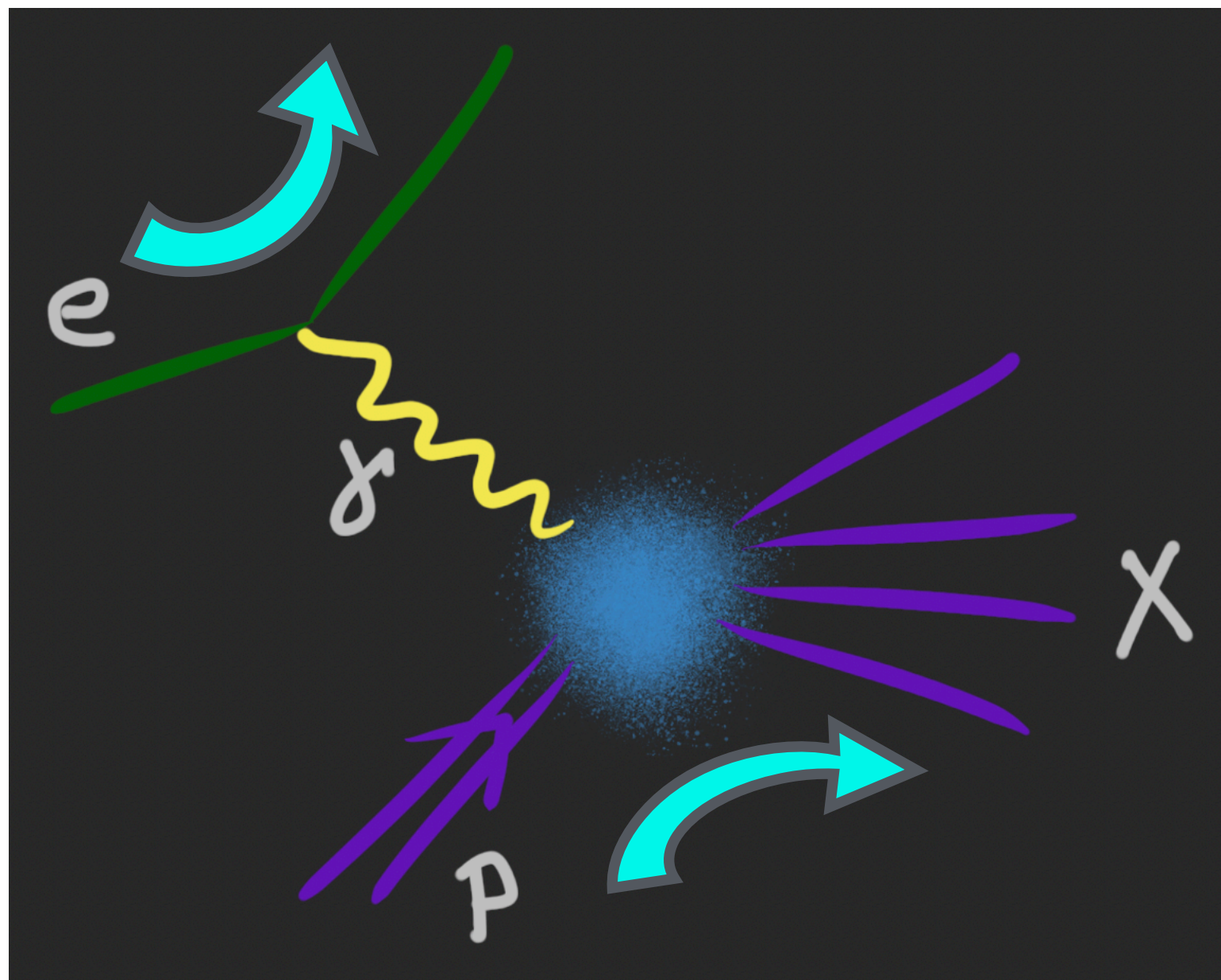
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Note that up to this point there is no QCD involved



Deep inelastic scattering: quarks in the Bjorken limit

For large photon virtualities, thinking about point like constituents (partons), and in a frame where the proton is moving infinitely fast

If the constituents are free during the interaction

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QCD enters when we identify the partons with quarks

At this point in time we have a theory and an understanding how to learn about QCD from measurements
... now, we need a new accelerator to perform the measurements and look deeper into the proton ...

To study the proton, probes at high energies (small de Broglie wave length) are needed

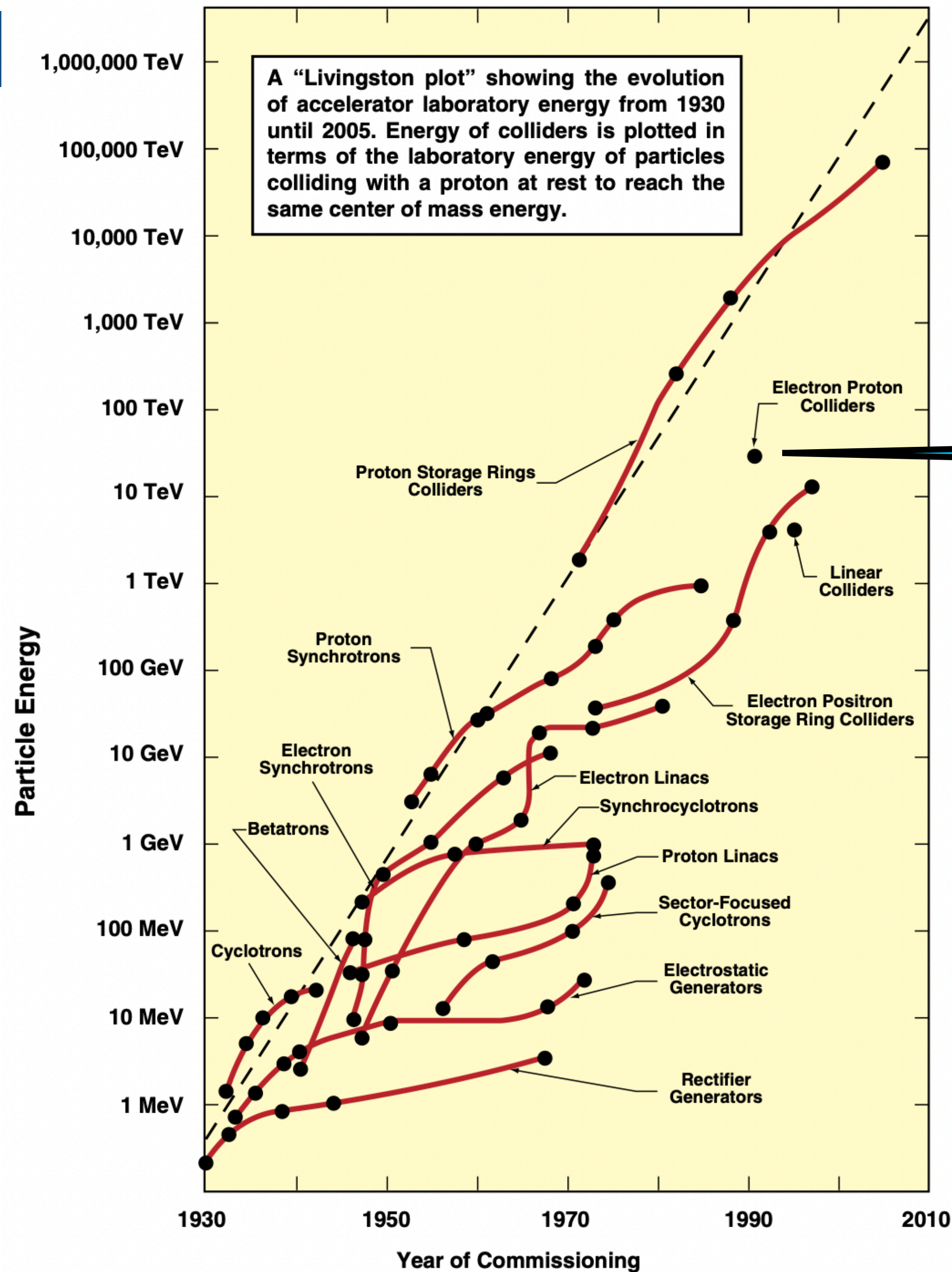
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HERA

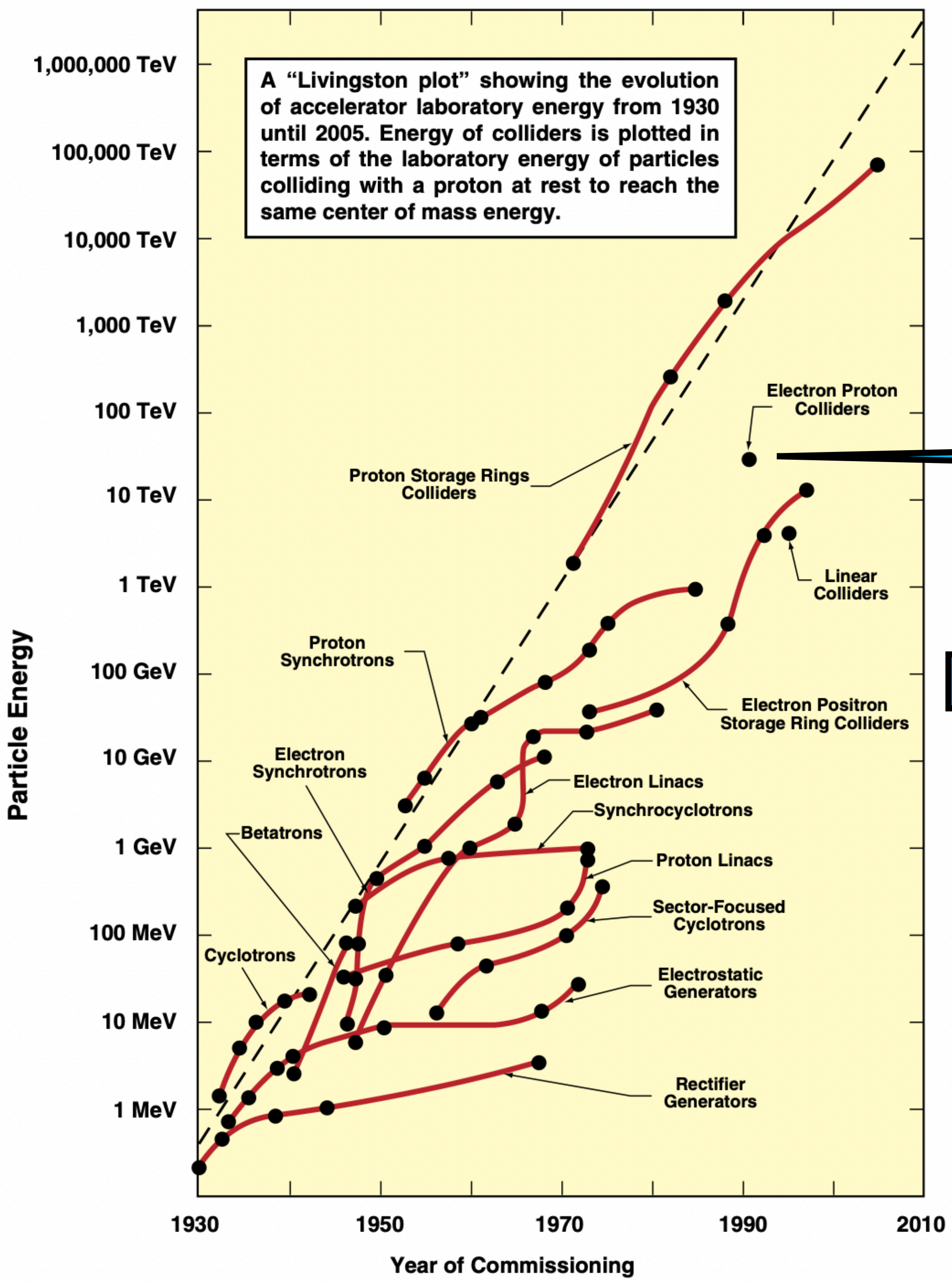
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HERA

Hopefully, we will add another ep collider in a few years when EIC enters operation



HERA



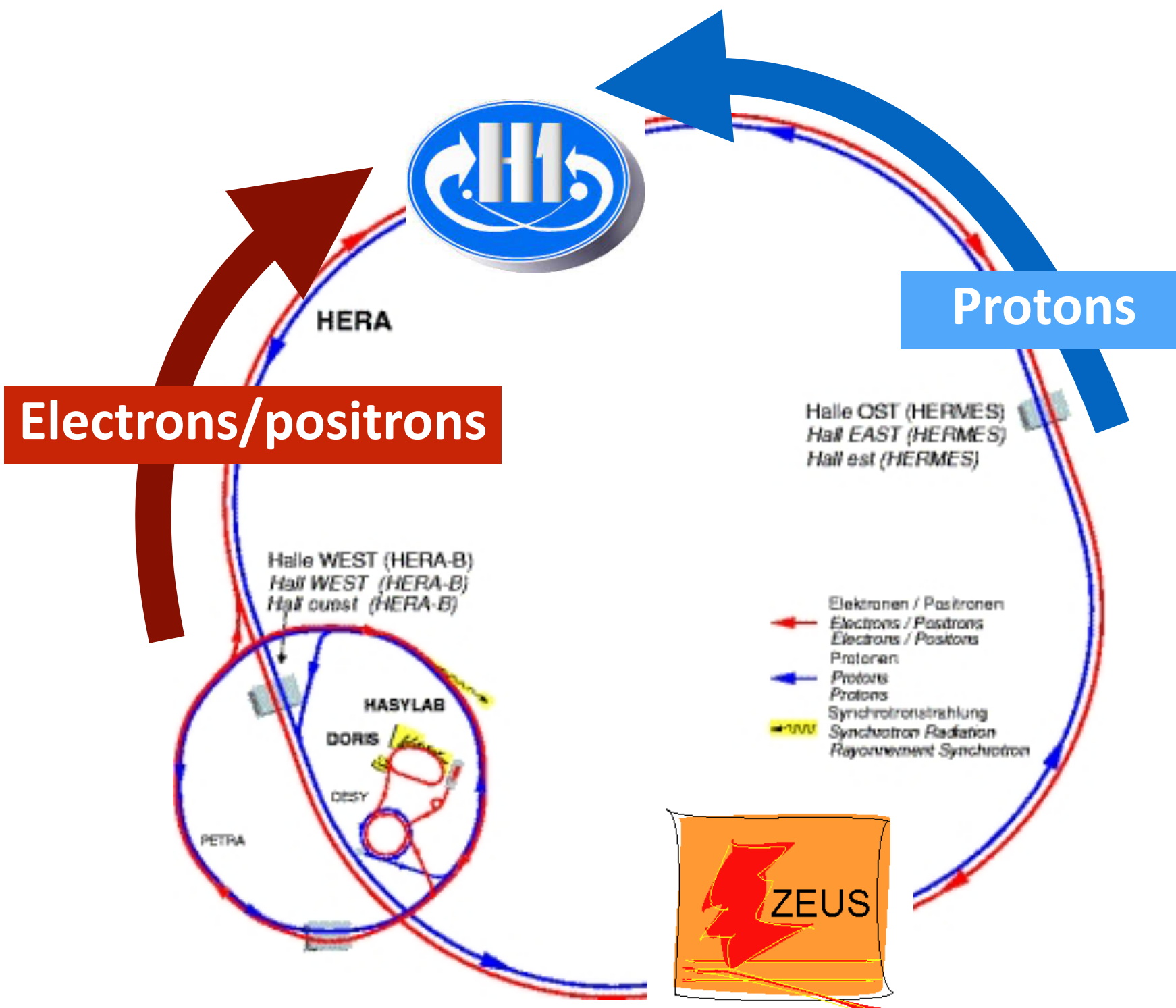
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Two beam-target experiments, HERMES, HERA-B
Two collider experiments, H1 and ZEUS

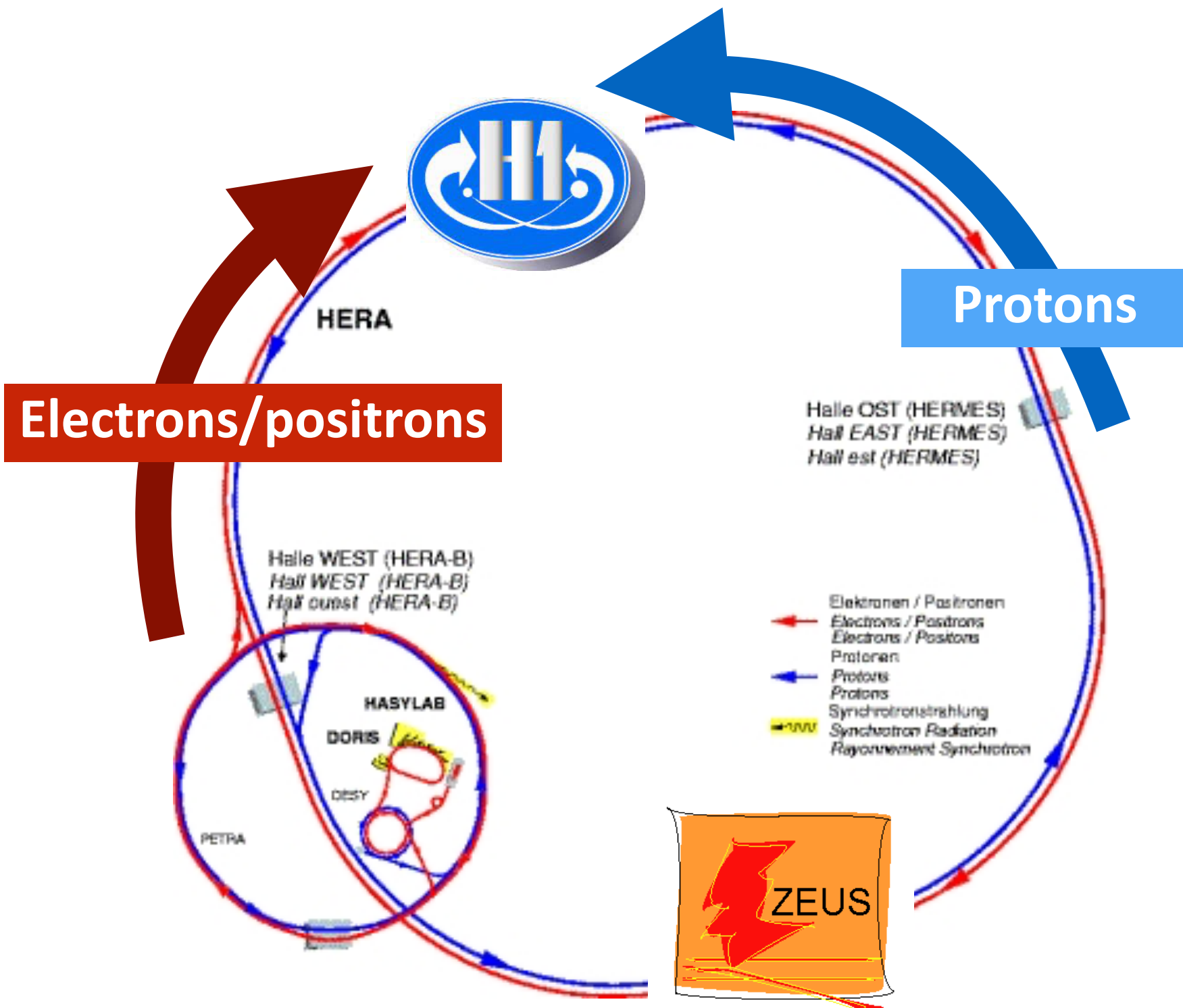


HERA



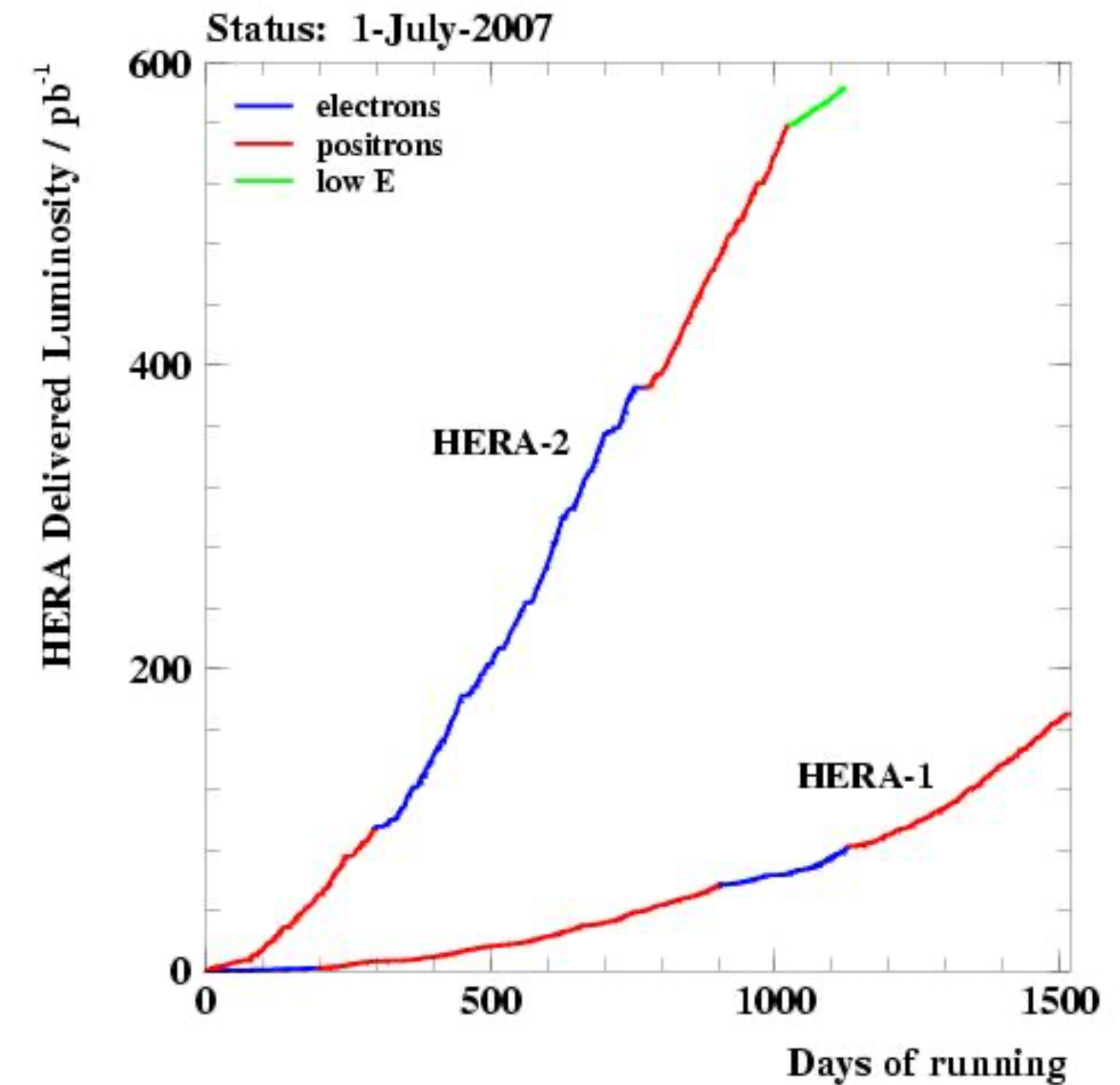
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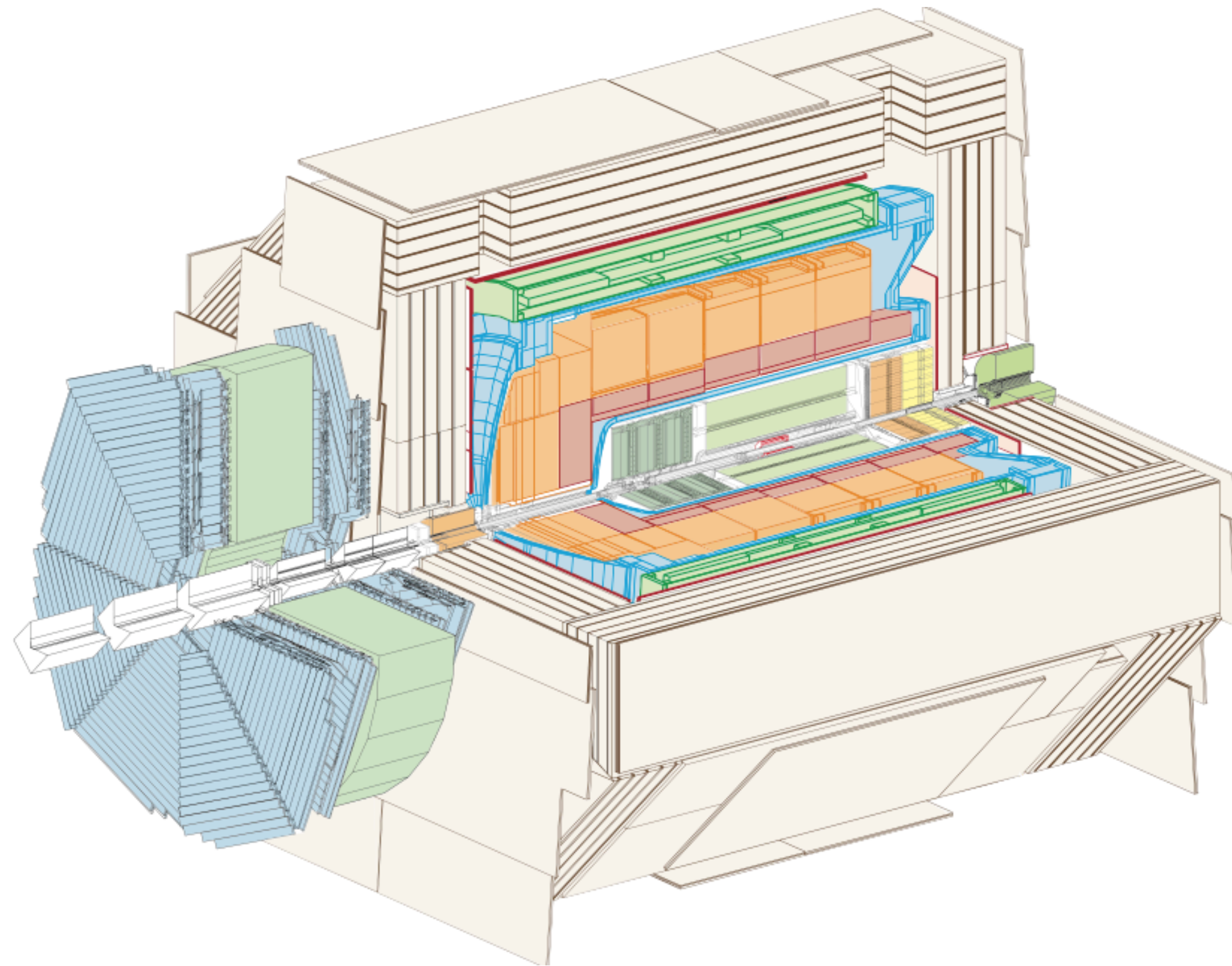
HERA-I, 1992–2000
 e^\pm beam 27.5 GeV, p beam 820 GeV (1992–1997)
 p beam 920 GeV (1998–2000)

HERA-II, 2002–2007
 e^\pm longitudinally polarised, p beam 920 GeV
 also p beam at 575 and 460 GeV



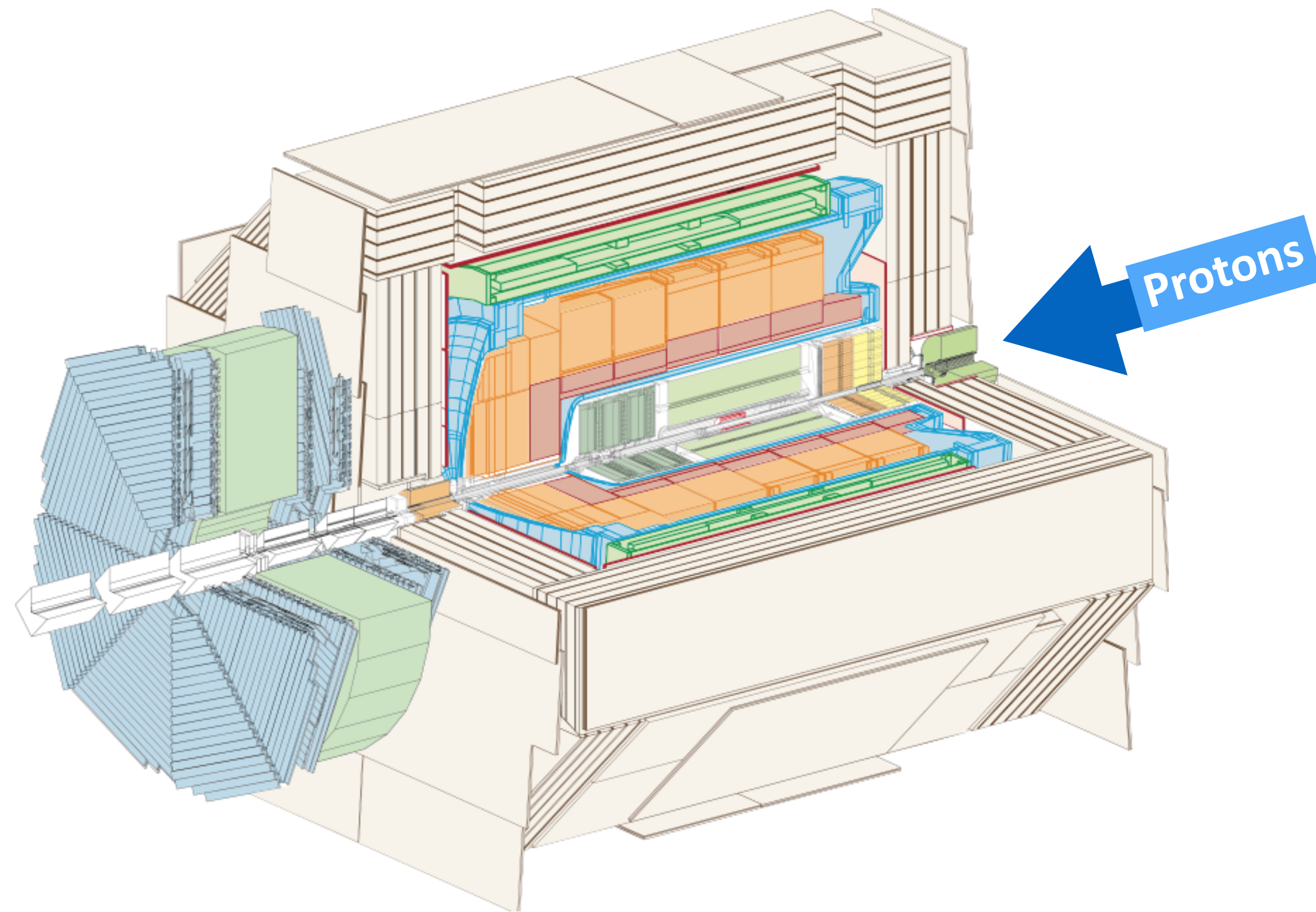
Guillermo Contreras, CTU in Prague

H1 detector: central detectors



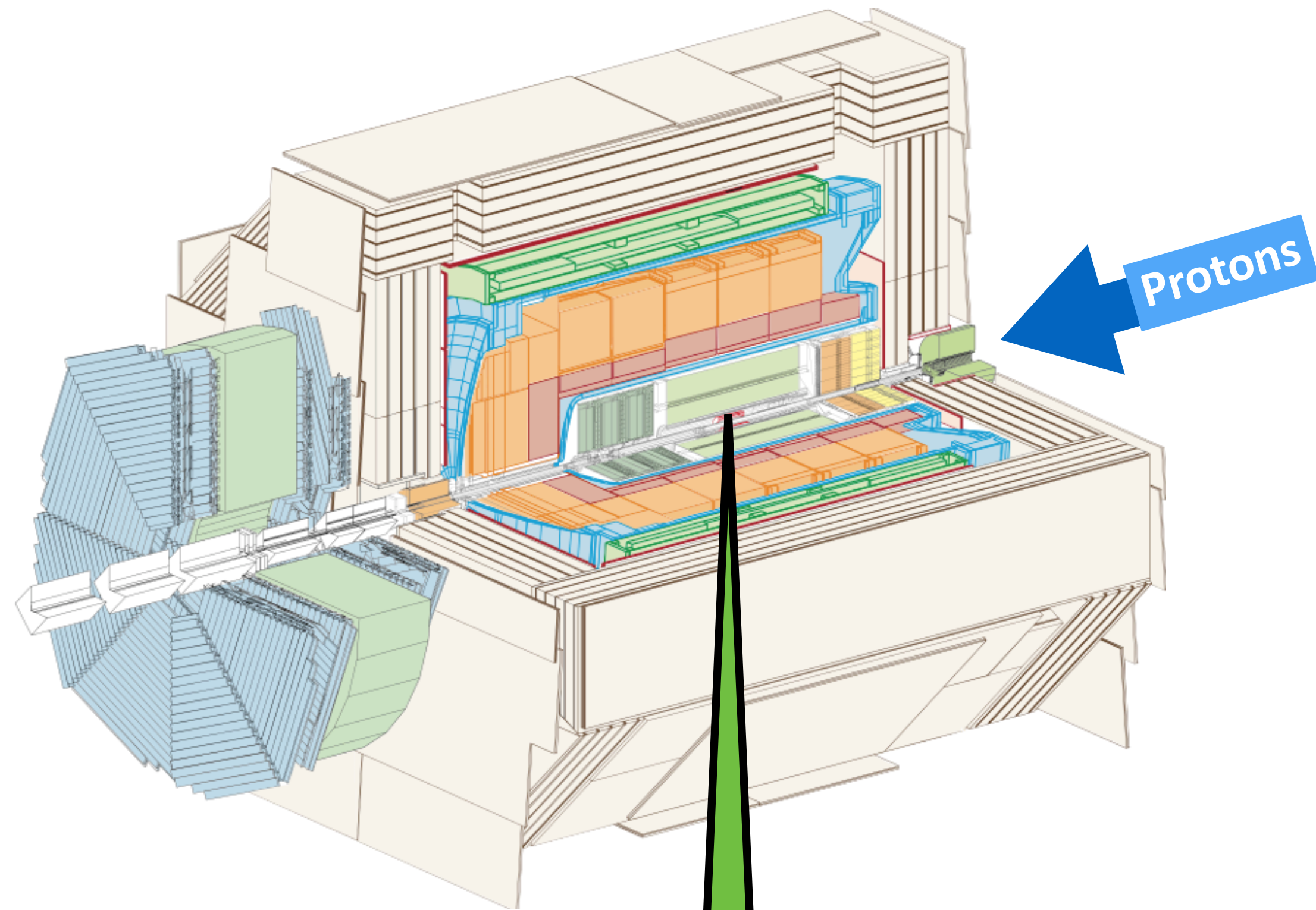
Asymmetric detector

H1 detector: central detectors



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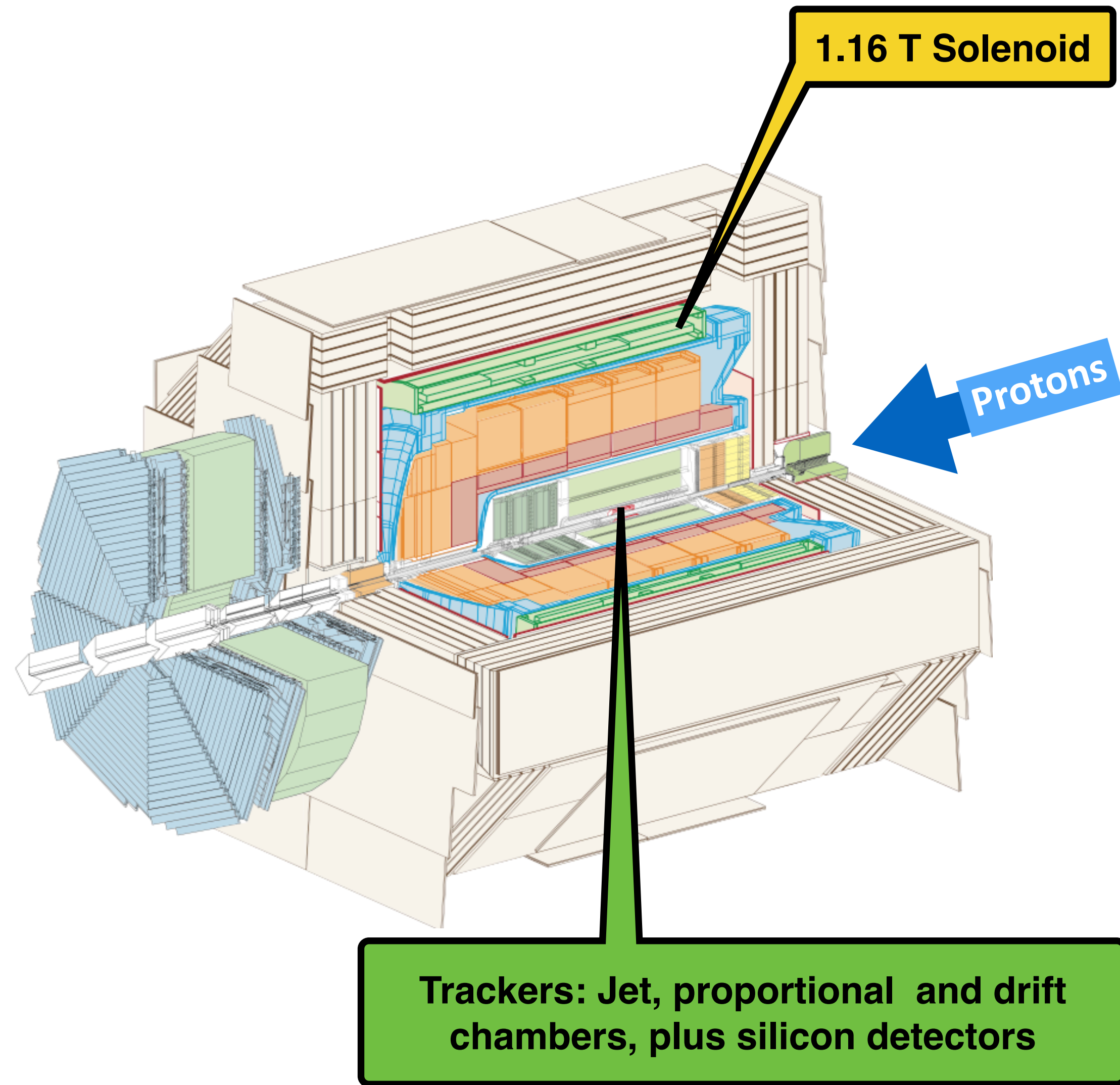
H1 detector: central detectors



Trackers: Jet, proportional and drift chambers, plus silicon detectors

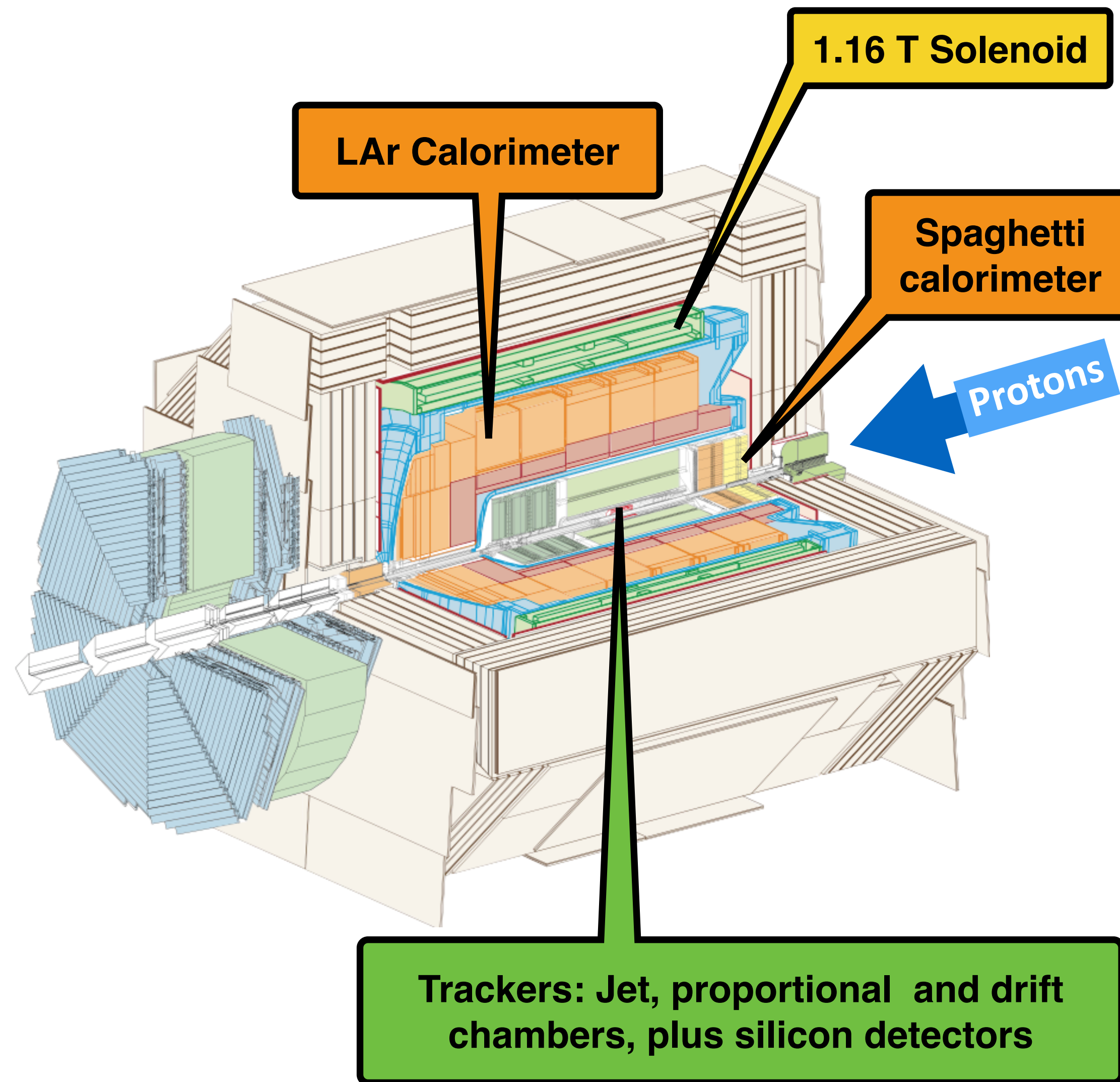
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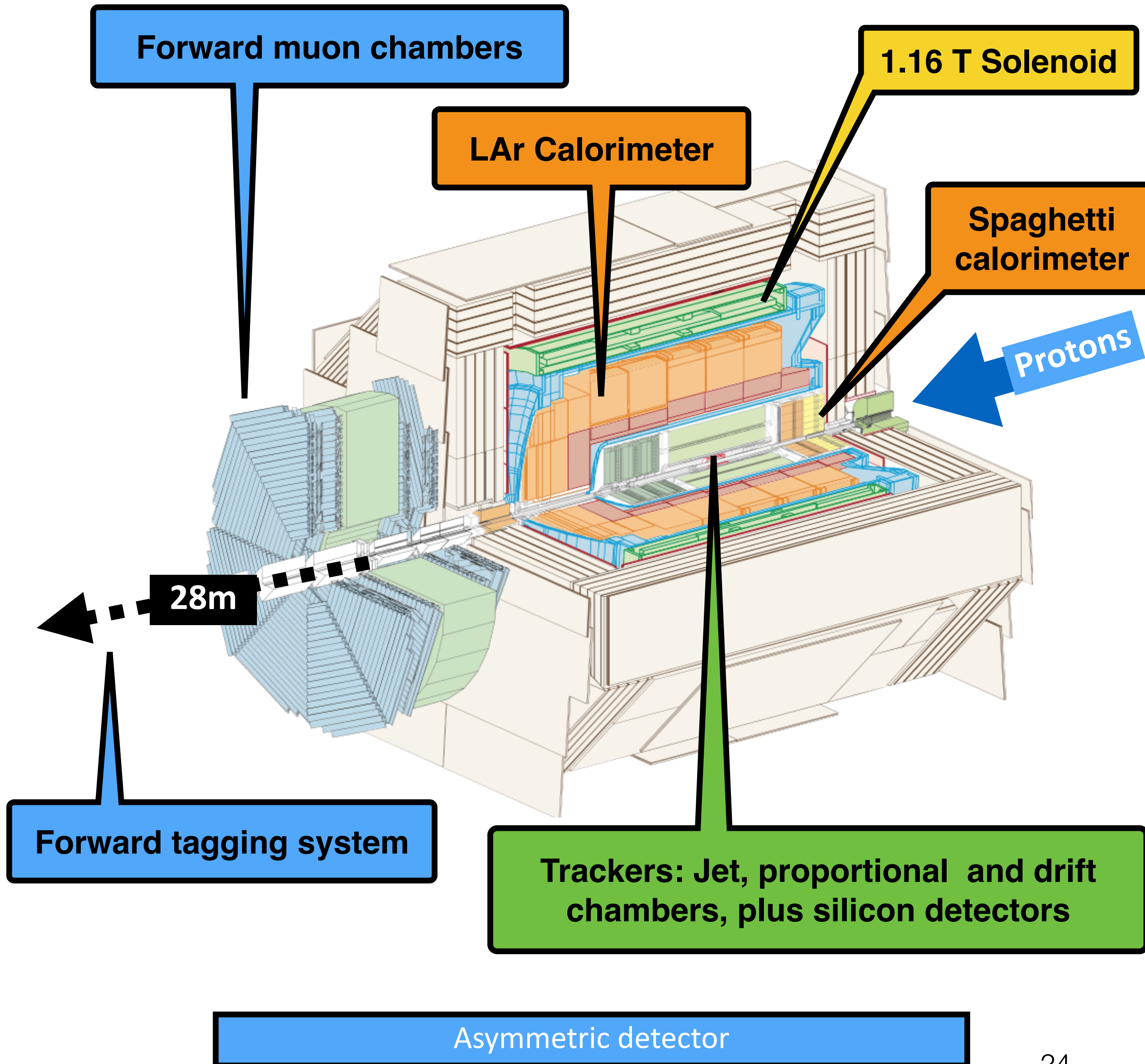
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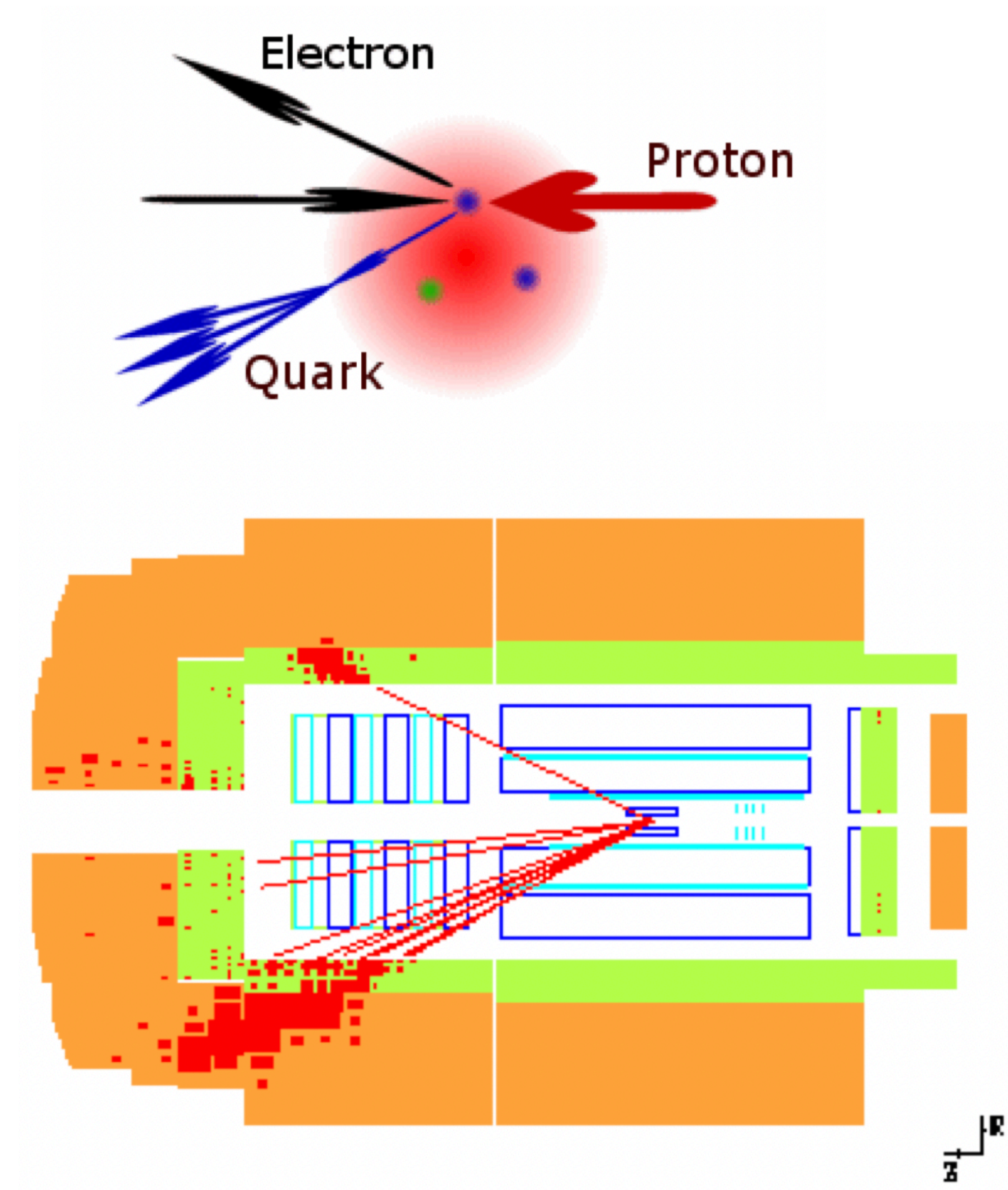
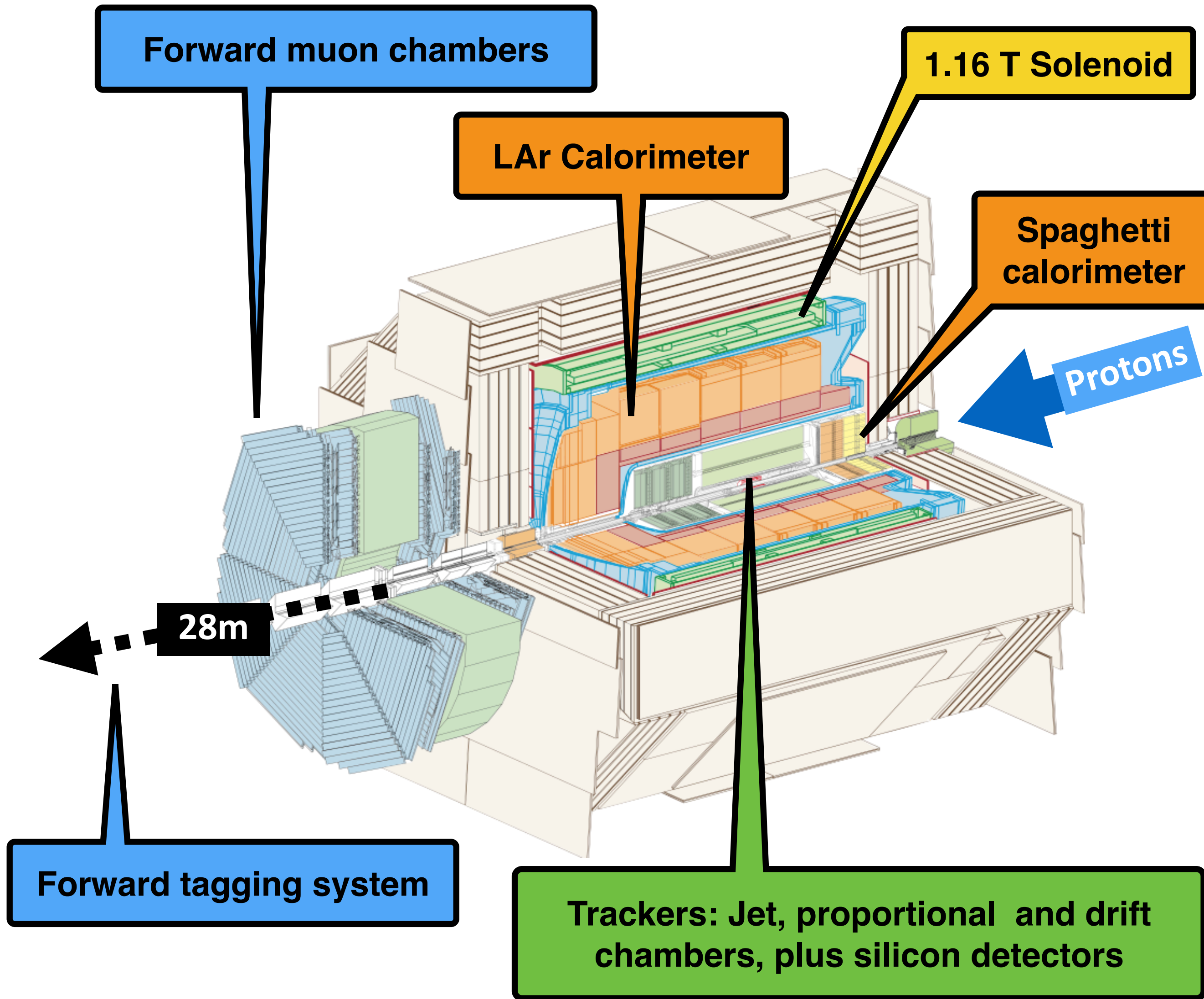


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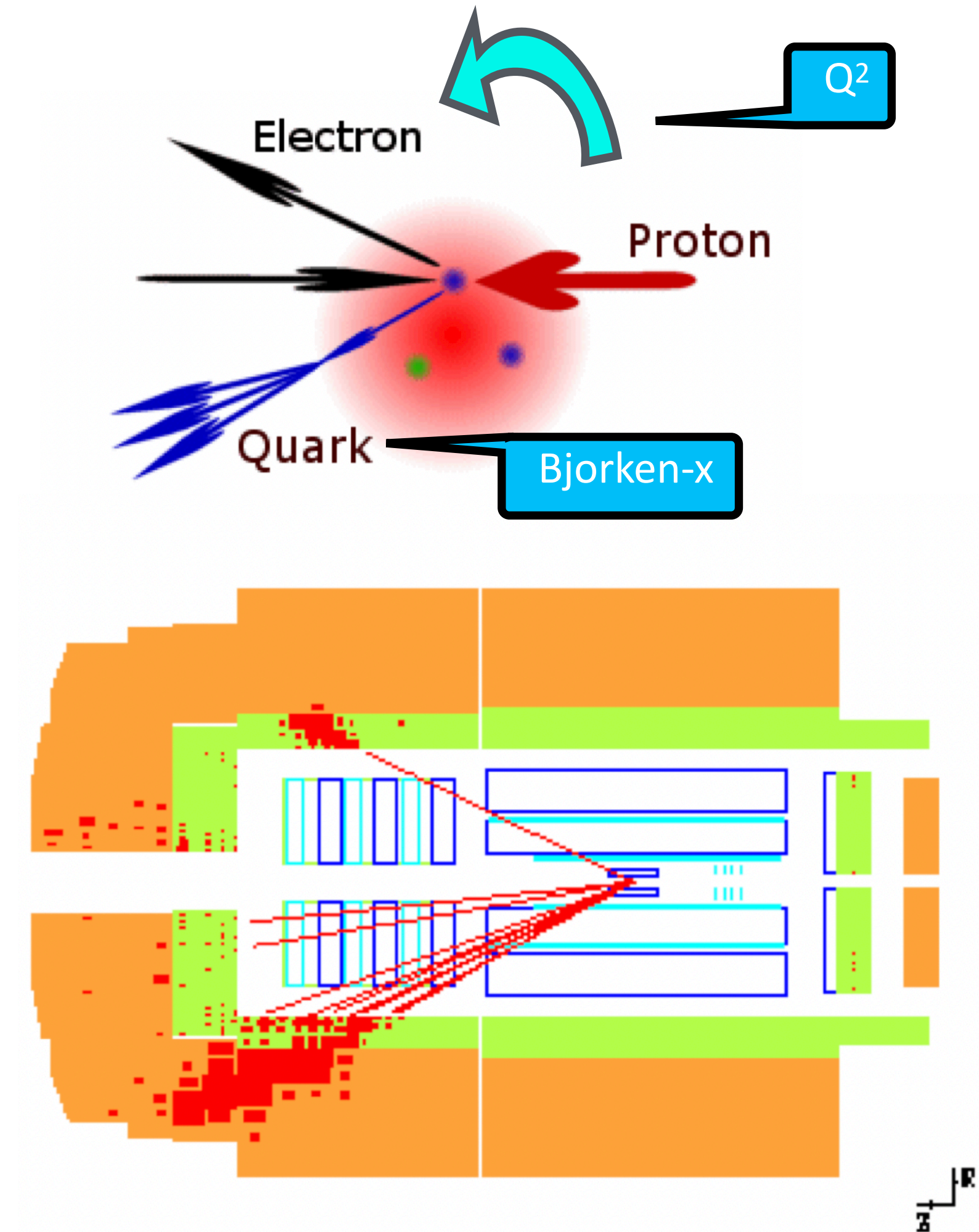
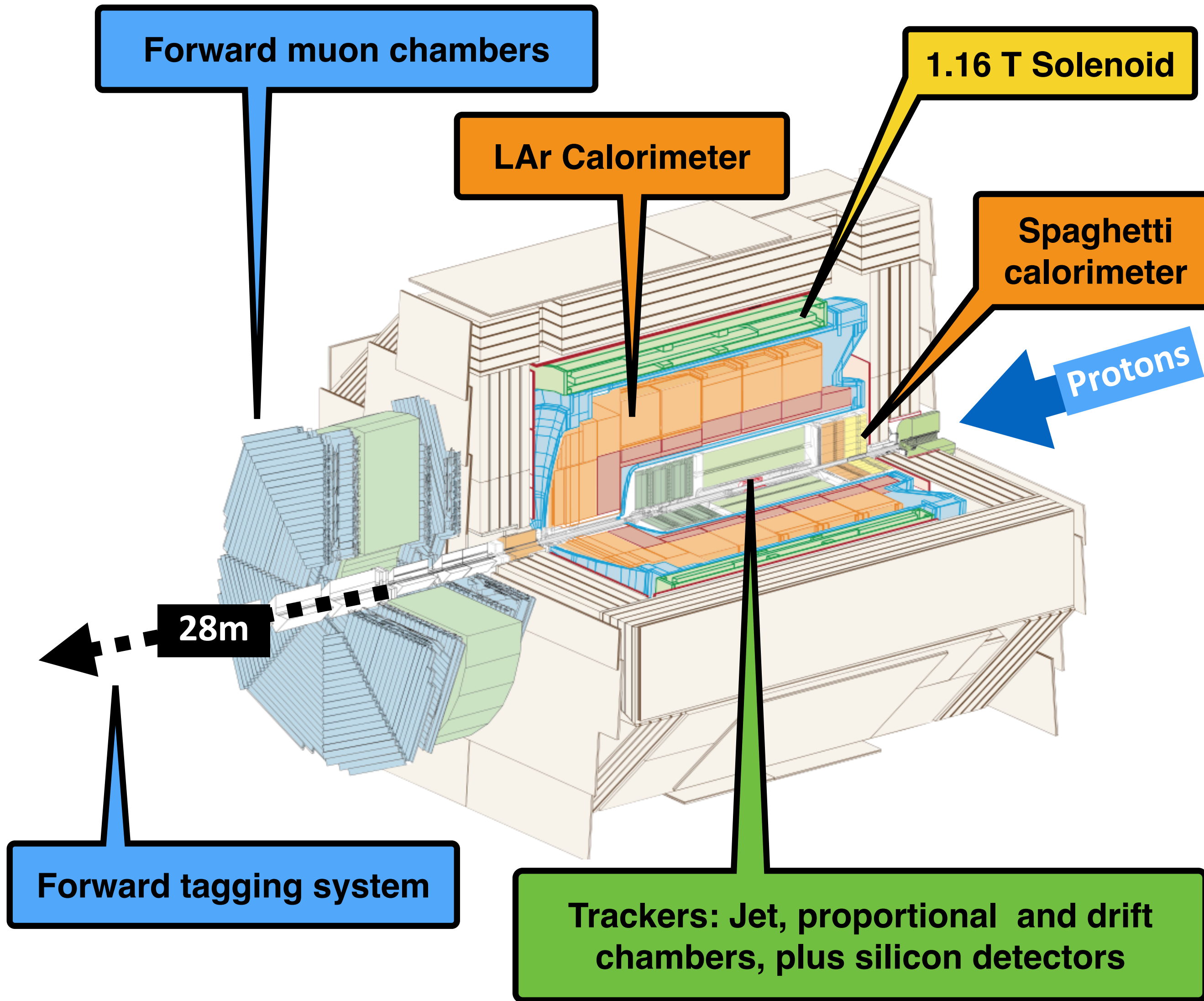
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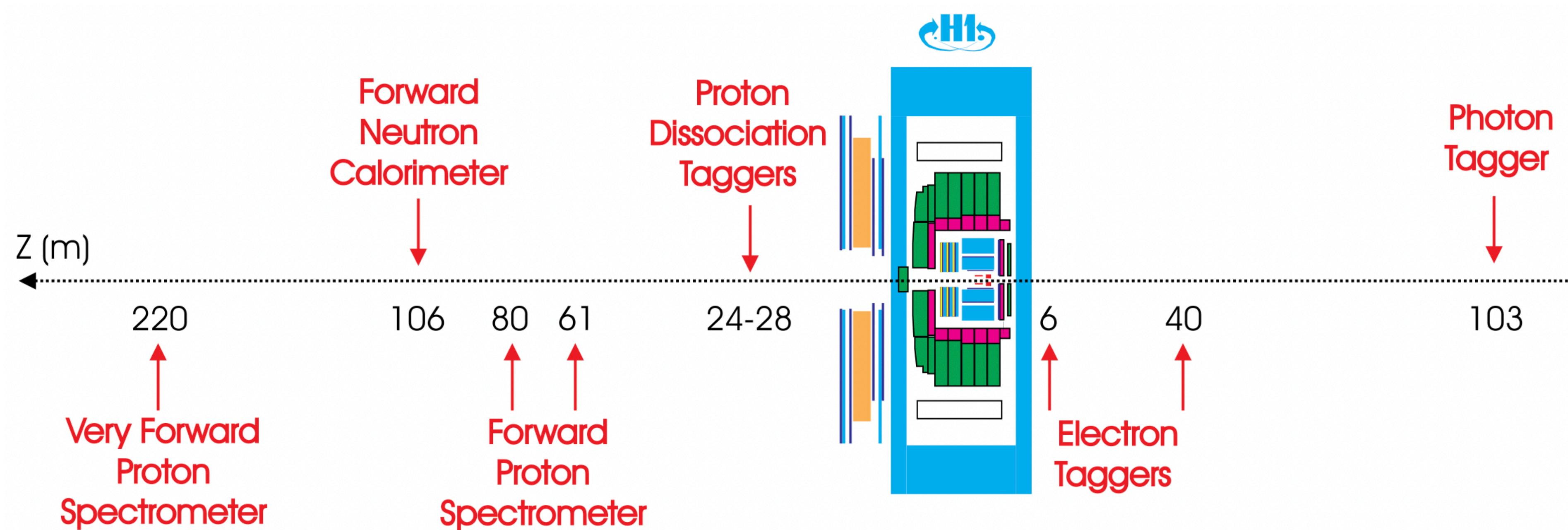
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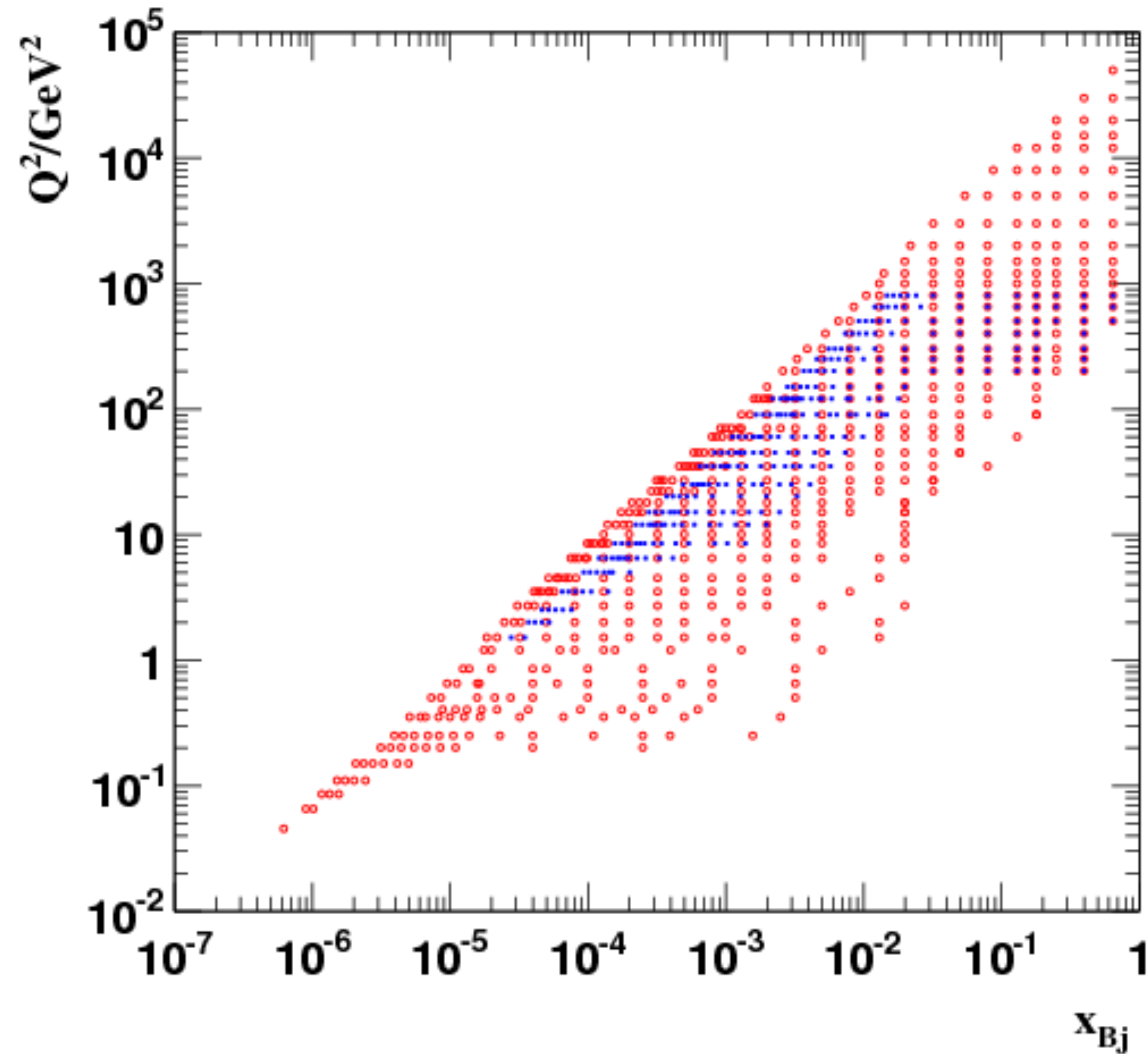
H1 detector: forward detectors



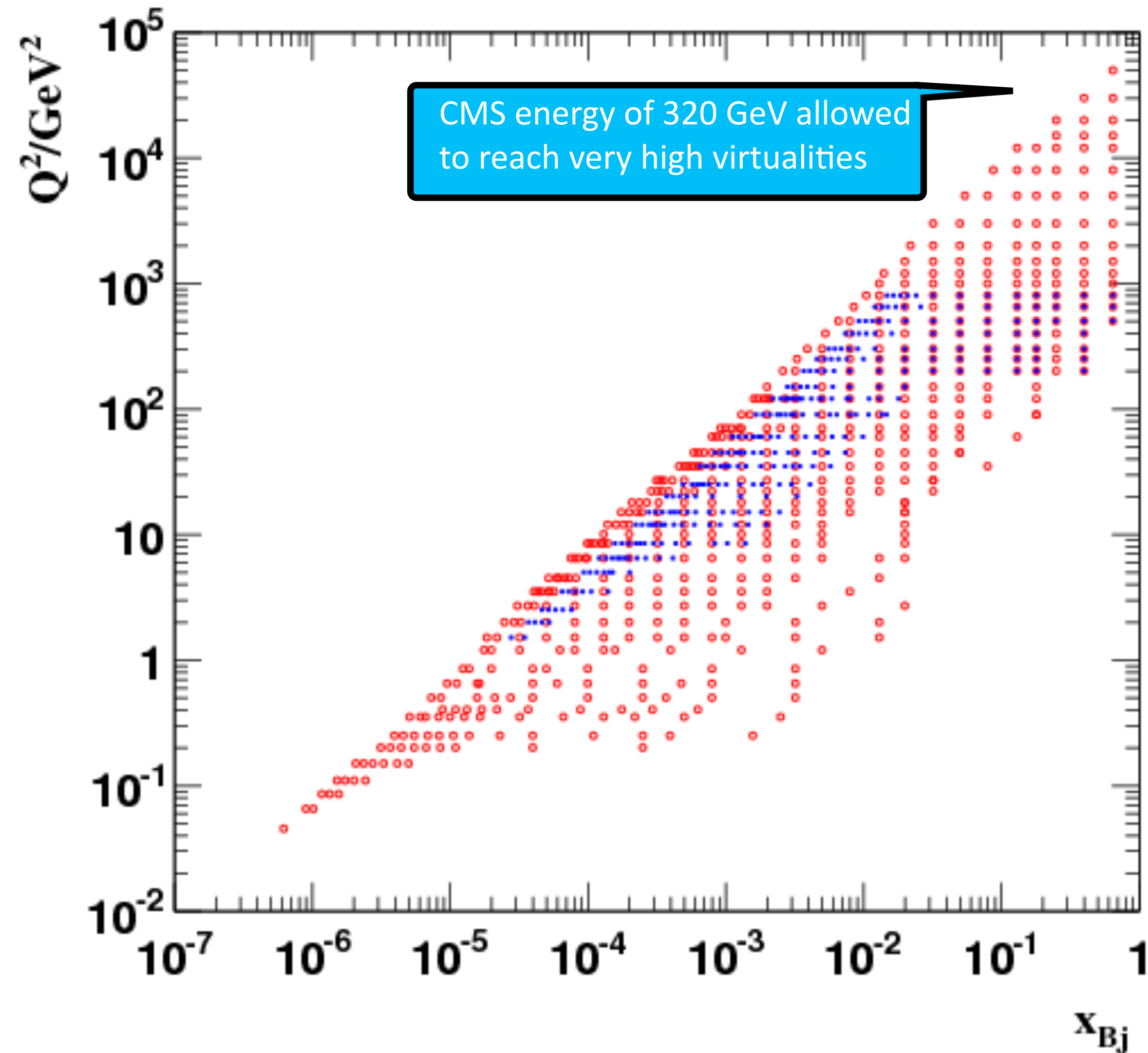
Tag diffractive processes

Luminosity (BH process) and photoproduction

H1 and ZEUS

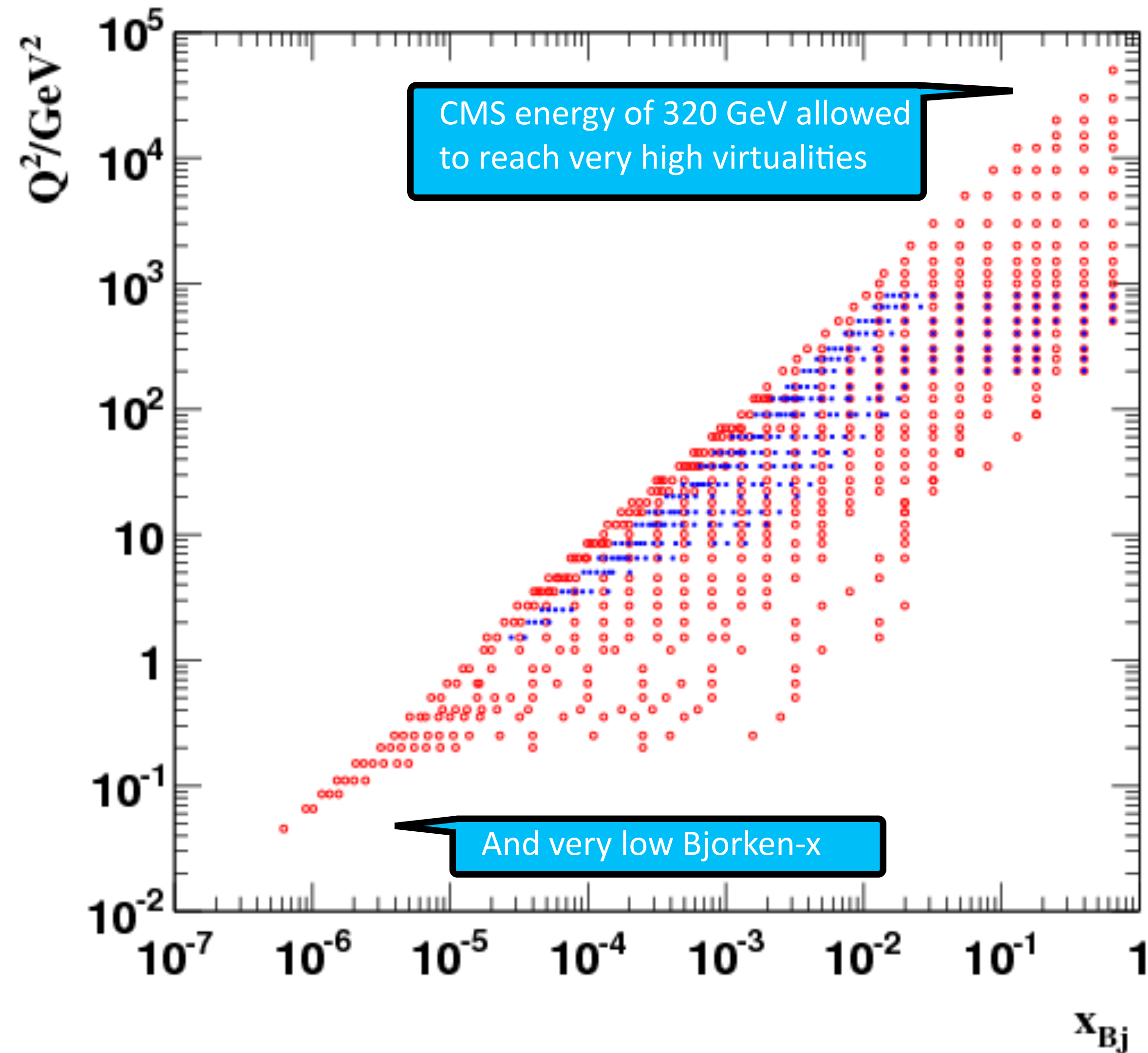


H1 and ZEUS



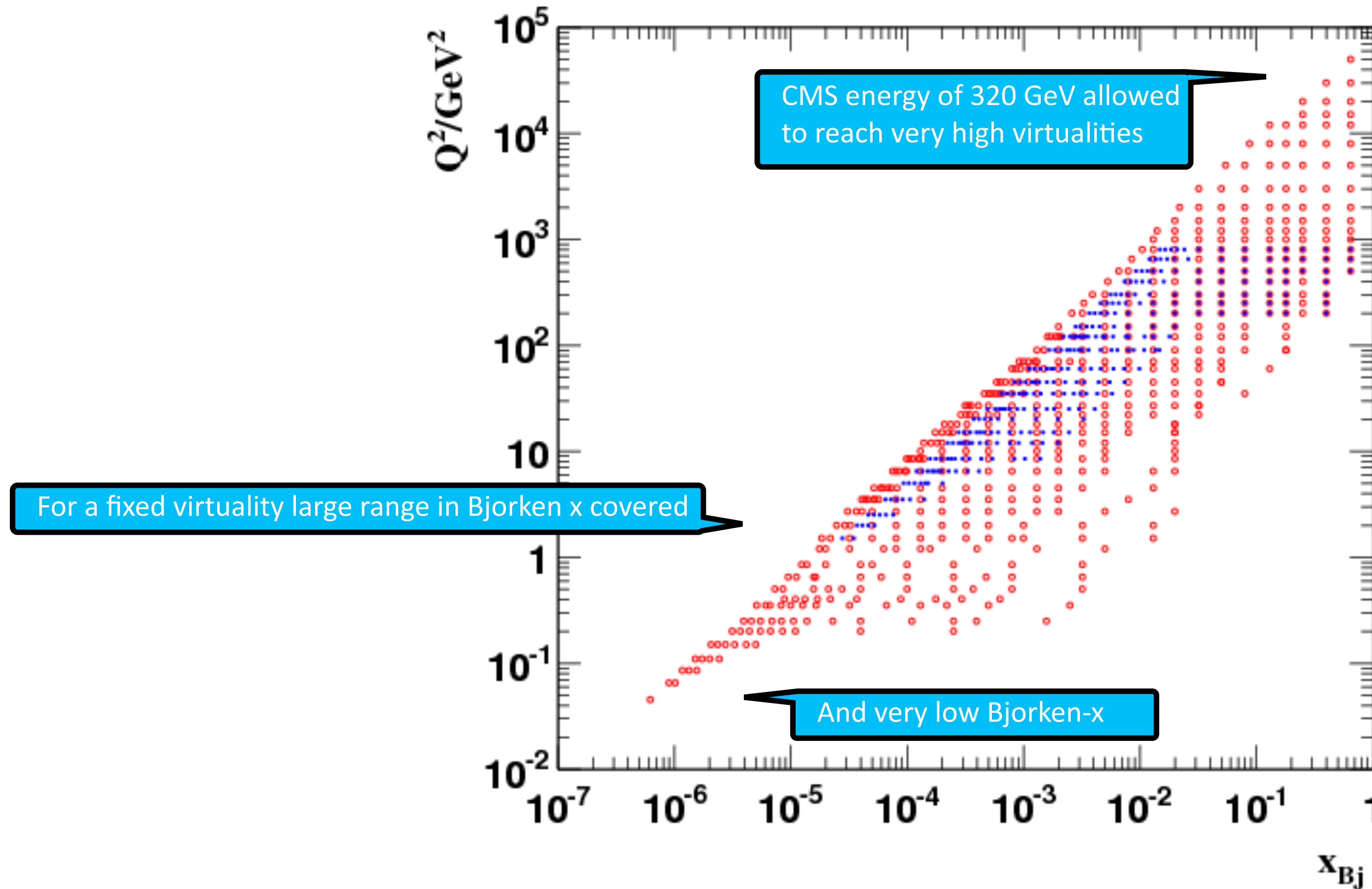
HERA: Kinematic coverage

H1 and ZEUS



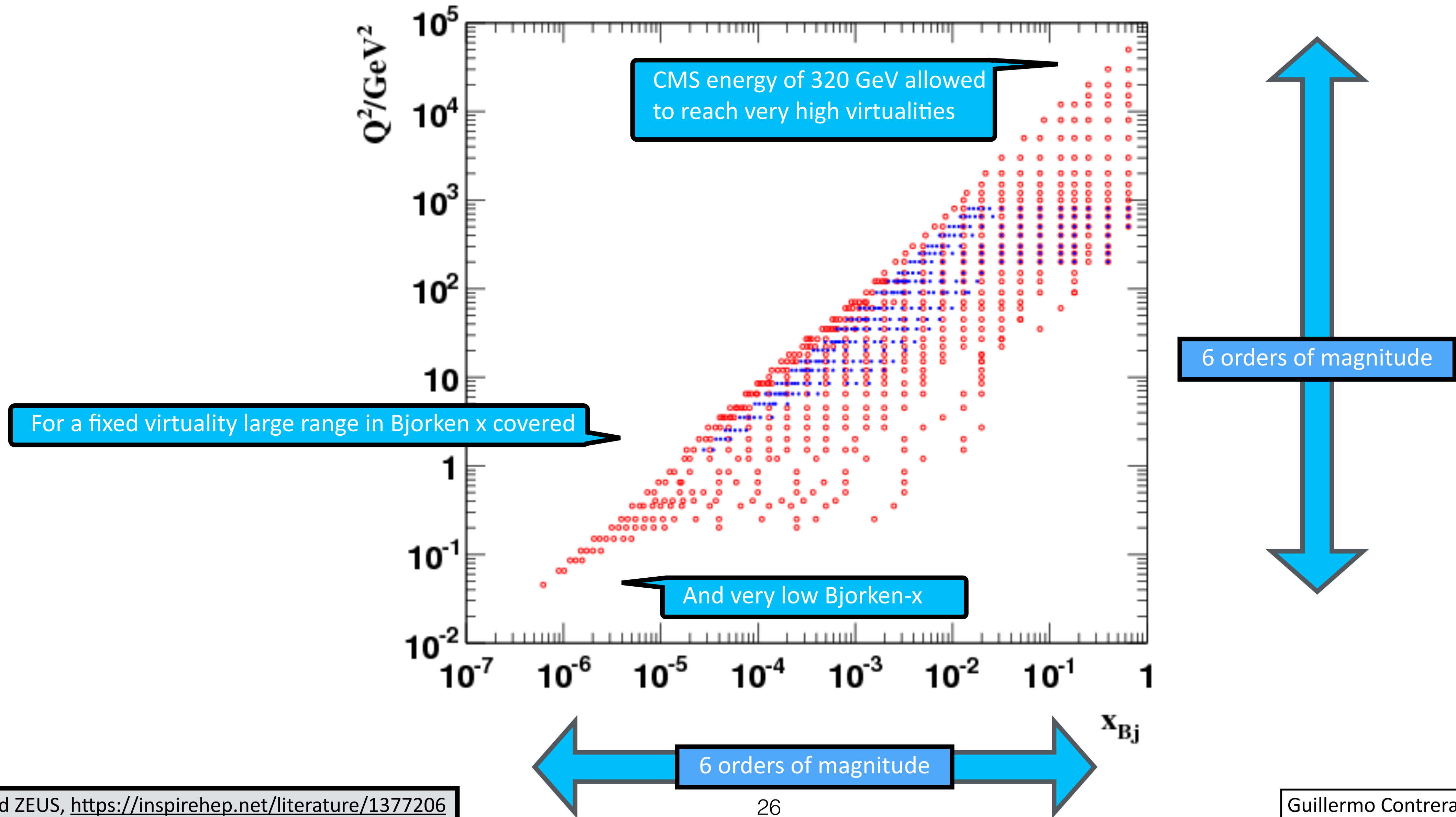
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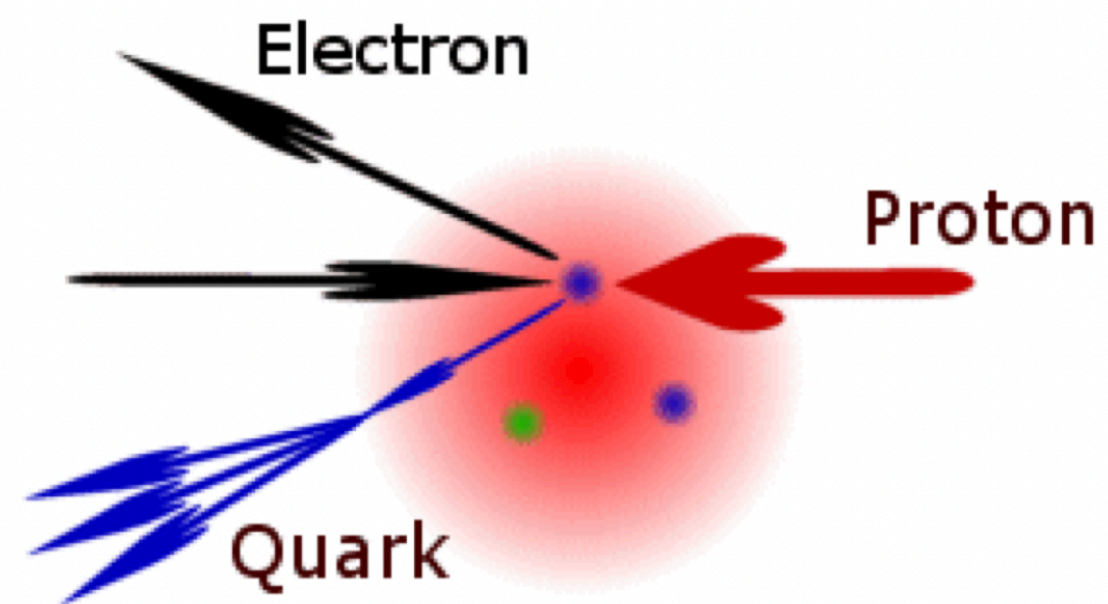
H1 and ZEUS



At this point in time, we have an accelerator and detectors with a huge range in kinematics
and we know how to extract QCD information from the measurements.
Let's look at HERA data to extract the behaviour of quarks and gluons inside hadrons ...

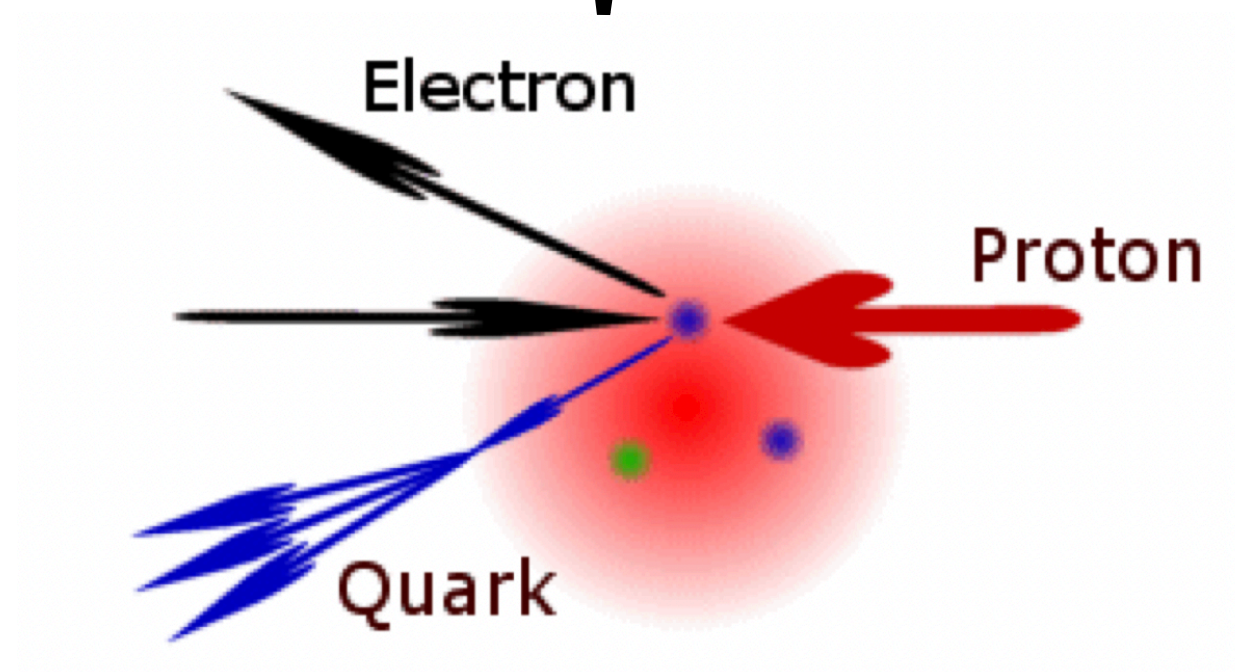
Reconstructing the kinematics

Kinematics could be determined using only the scattered electron



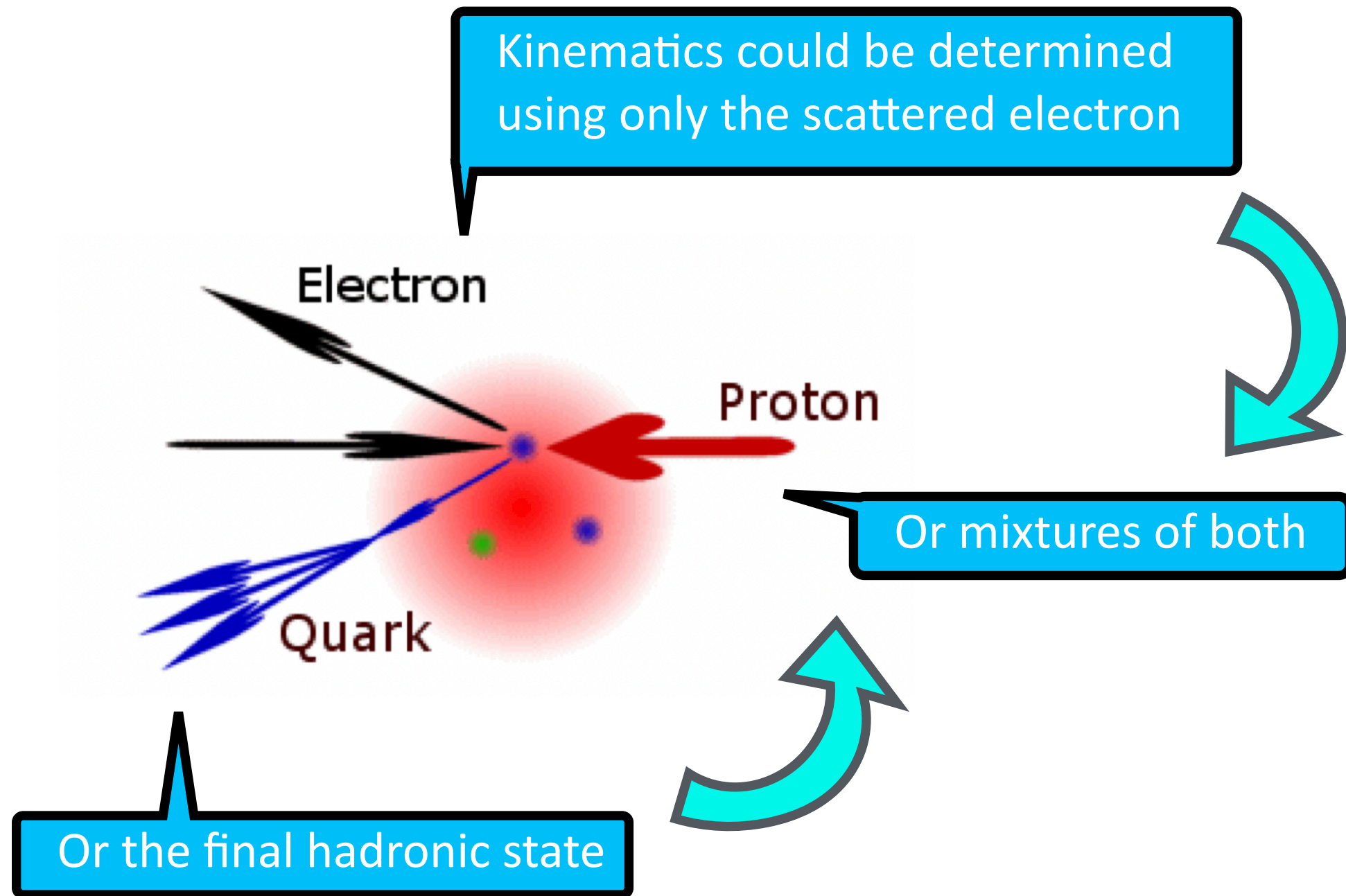
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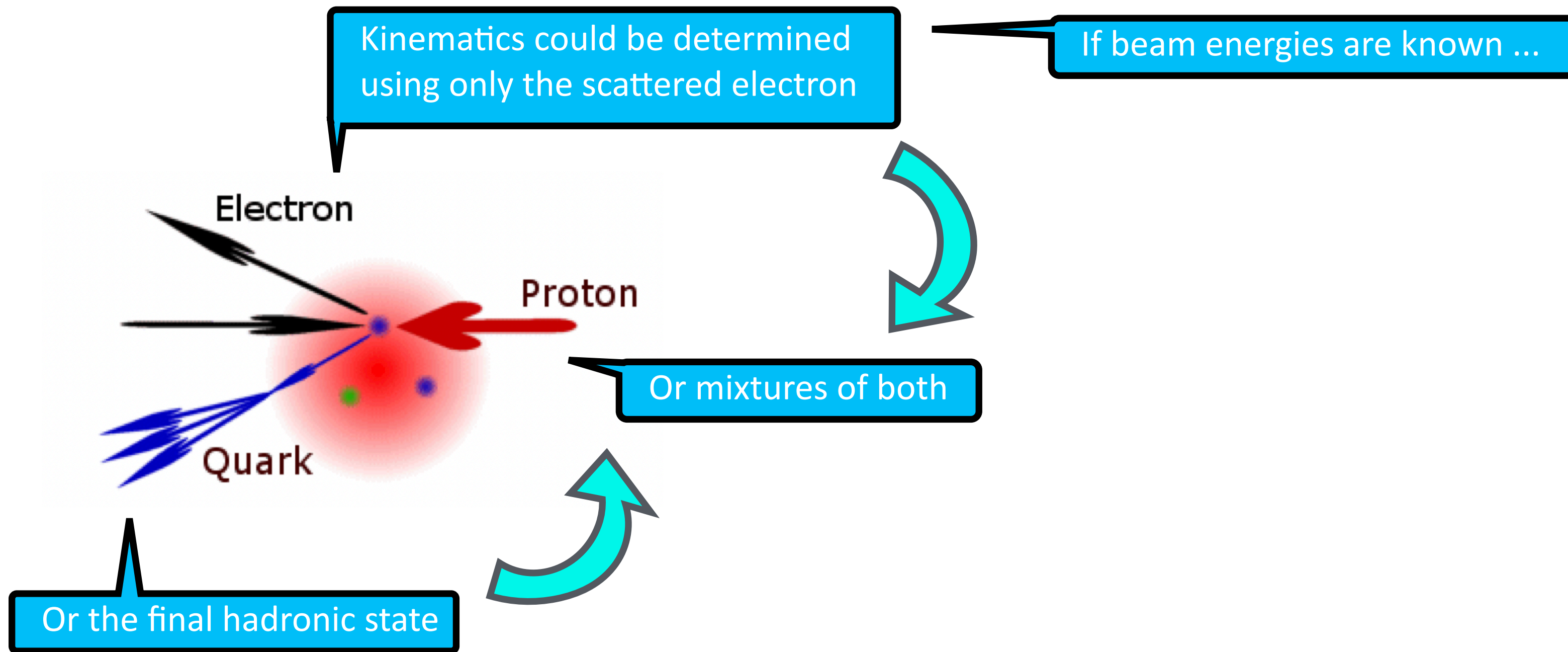


Or the final hadronic state

Reconstructing the kinematics



Reconstructing the kinematics



Reconstructing the kinematics

The diagram shows an electron (black arrow) and a proton (red arrow) colliding. A quark (blue arrow) is shown being struck by the electron. Callouts indicate: 'Kinematics could be determined using only the scattered electron' (pointing to the electron path), 'If beam energies are known ...' (pointing to the proton path), 'Or mixtures of both' (pointing to the collision region), 'Or the final hadronic state' (pointing to the quark path), and 'Not an exhaustive list' (pointing to the table).

Method	y	Q^2	x
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h	$\Sigma / 2E^e$	$\frac{T^2}{1 - y_h}$	Q^2 / y_s
m	y_h	Q_e^2	Q^2 / y_s
DA	$\frac{\tan \gamma/2}{\tan \gamma/2 + \tan \theta/2}$	$4E^{e2} \frac{\cot \theta/2}{\tan \gamma/2 + \tan \theta/2}$	Q^2 / y_s
Σ	$\frac{\Sigma}{\Sigma + E(1 - \cos \theta)}$	$\frac{E^2 \sin^2 \theta}{1 - y_\Sigma}$	Q^2 / y_s
IDA	y_{DA}	$E^2 \tan \theta/2 \frac{\tan \gamma/2 + \tan \theta/2}{2 \cot \theta/2 + \tan \theta/2}$	$\frac{E \cot \gamma/2 + \cot \theta/2}{E^p \cot \theta/2 + \tan \theta/2}$
1Σ	y_Σ	Q_Σ^2	$\frac{E \cos^2 \theta/2}{E^p y_\Sigma}$

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If beam energies are known ...

Homework: deduce some of the formulas in the table

Or mixtures of both

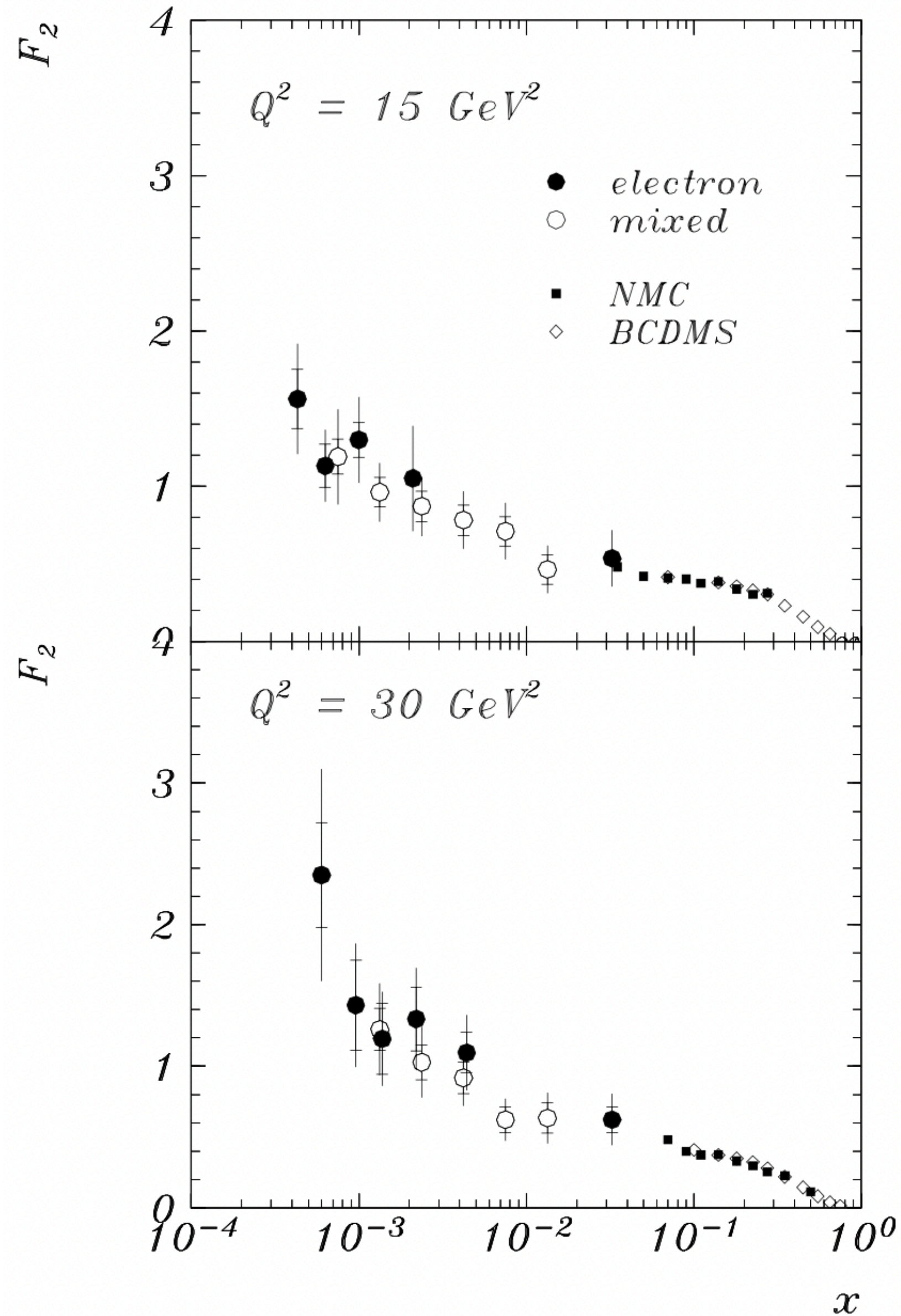
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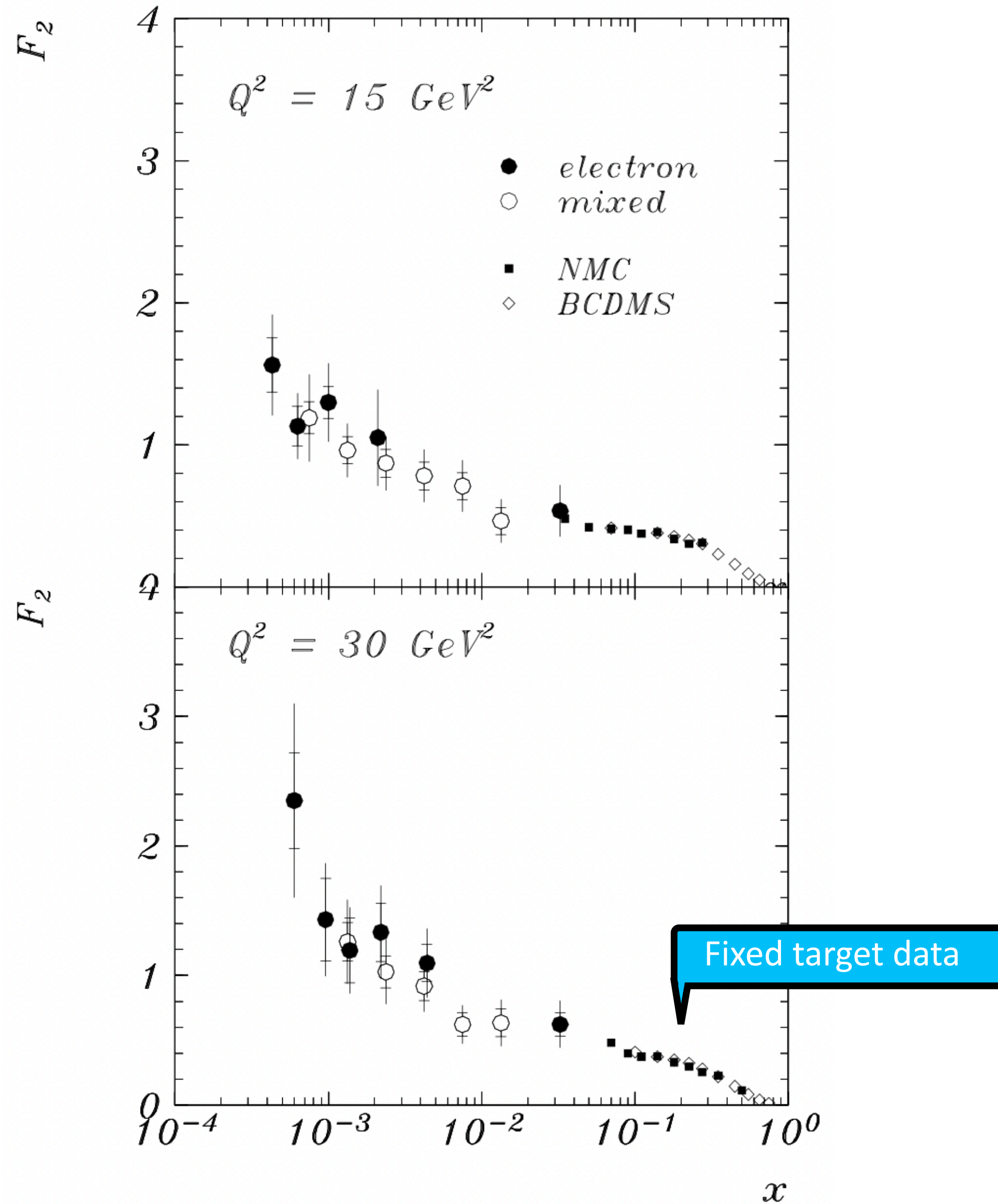
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The proton structure function with the first HERA data (1993)



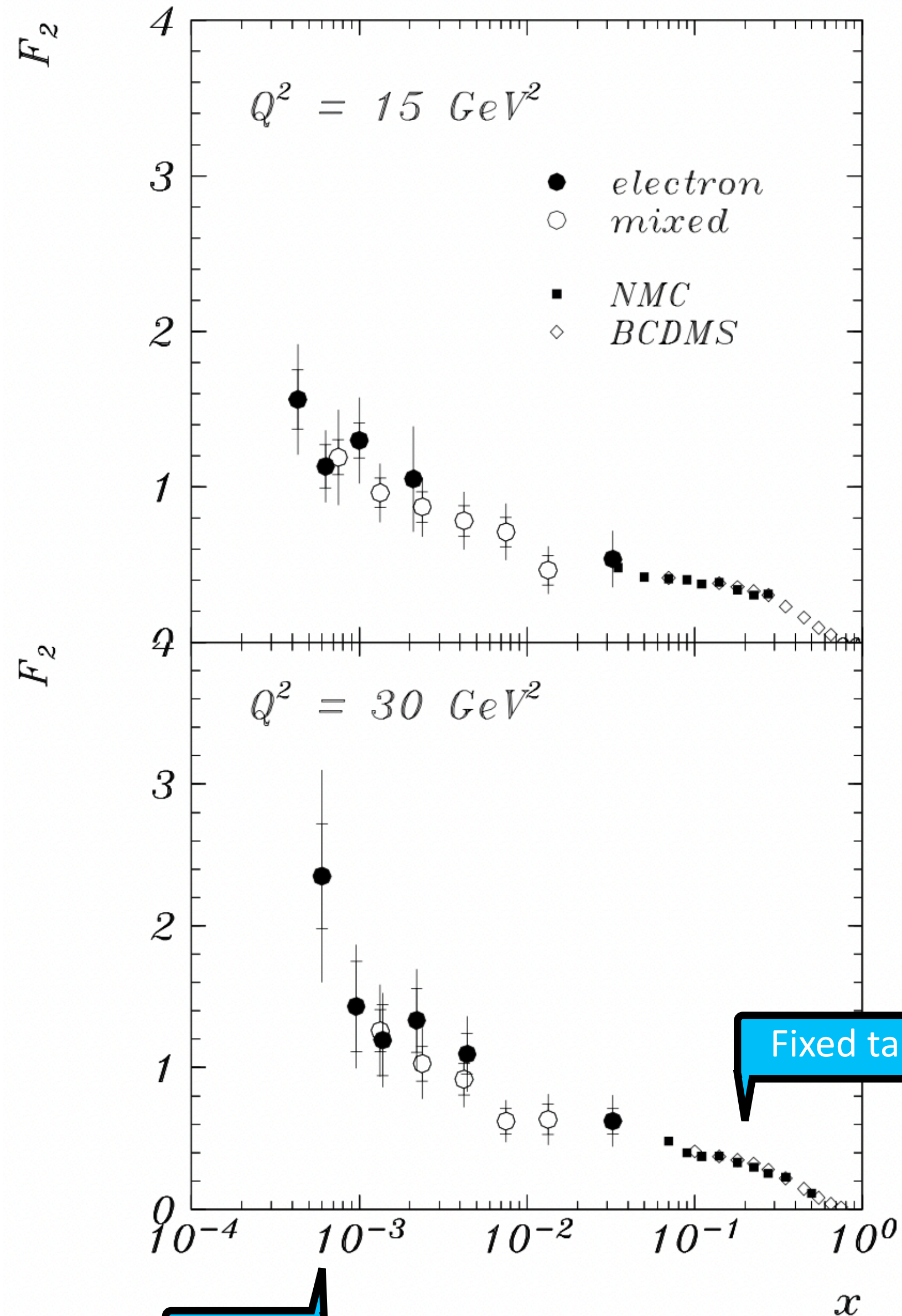
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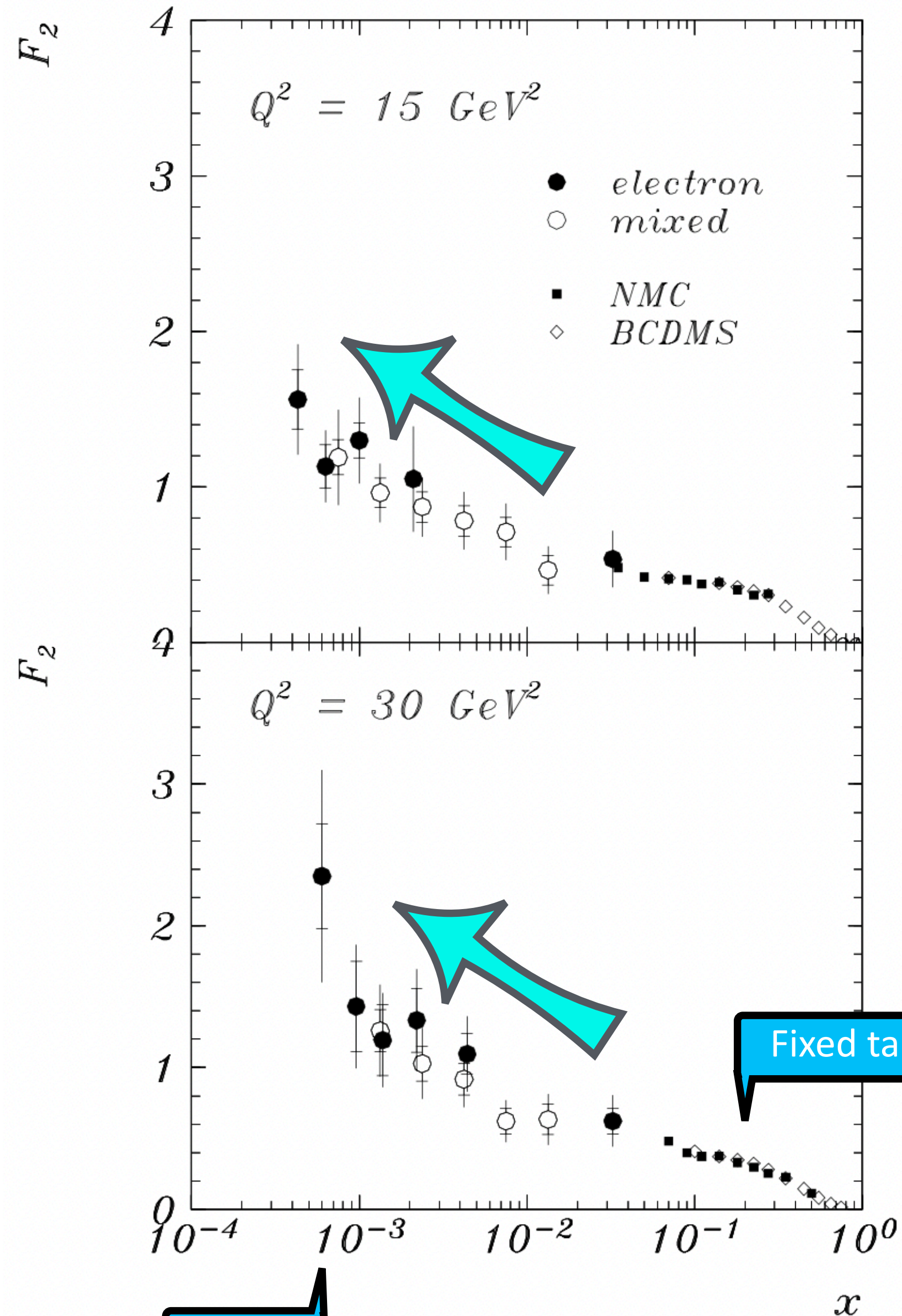
Data reach 2 orders of magnitude smaller Bjorken-x than fixed target experiments

Low x

Fixed target data

H1, <https://inspirehep.net/literature/357797>

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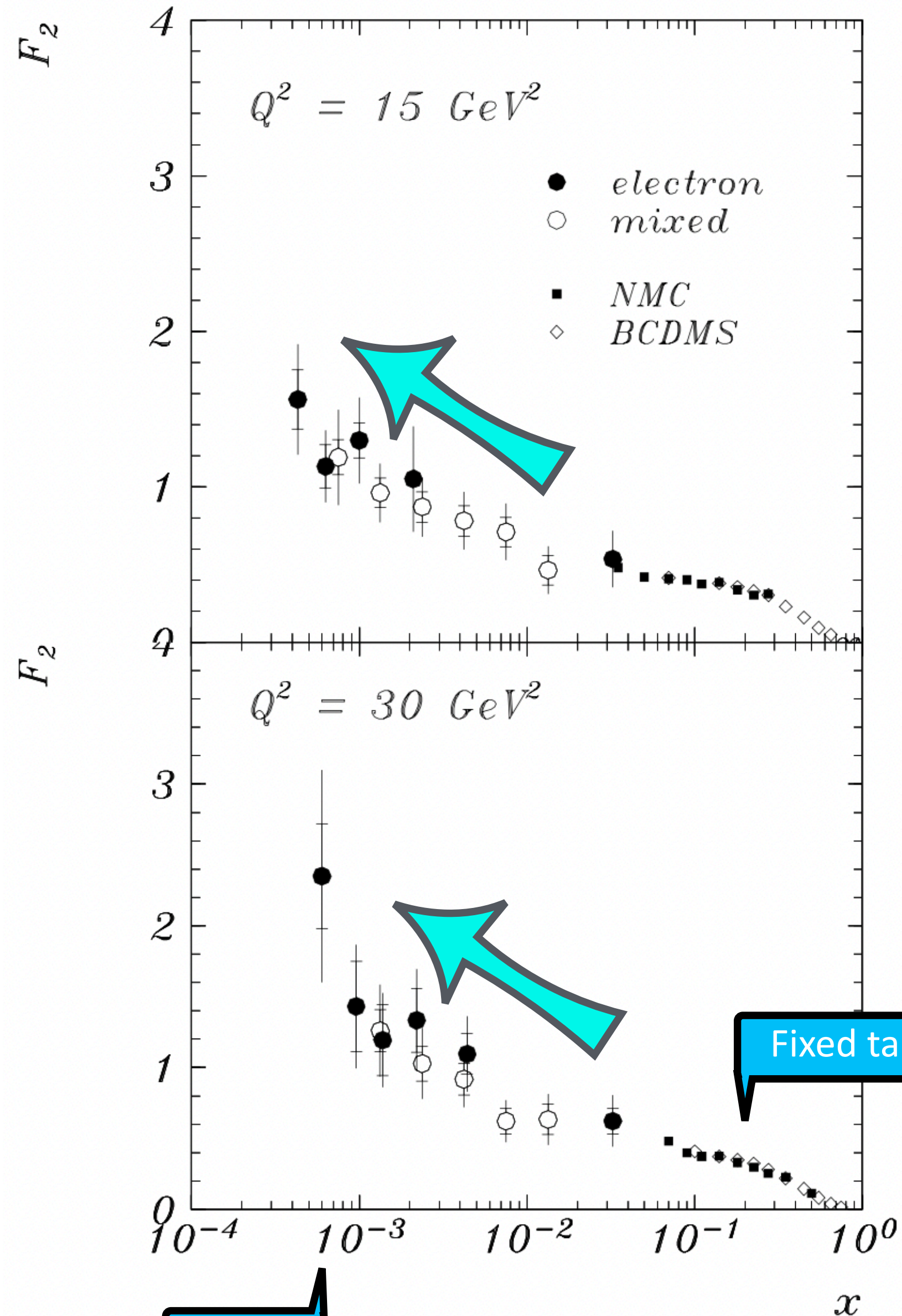
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How does F_2 change with the photon virtuality?

The evolution of hadron structure is predicted within pQCD in the form of differential equations

Parenthesis: Altarelli-Parisi equations

1977: Evolution equations

ASYMPTOTIC FREEDOM IN PARTON LANGUAGE

G. ALTARELLI *

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G. PARISI ***

Institut des Hautes Etudes Scientifiques, Bures-sur-Yvette, France

Received 12 April 1977

[https://doi.org/10.1016/0550-3213\(77\)90384-4](https://doi.org/10.1016/0550-3213(77)90384-4)

In this paper we show that an alternative derivation of all results of current interest for the Q^2 behaviour of deep inelastic structure functions is possible. In this approach all stages of the calculation refer to parton concepts and offer a very illuminating physical interpretation of the scaling violations. In our opinion the present approach, although less general, is remarkably simpler than the usual one since all relevant results can be derived in a direct way from the basic vertices of QCD, with no loop calculations being involved (the only exception is the lowest order expression for the running coupling constant which we do not rederive).

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$$\frac{dq^i(x, t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[q^i(y, t) P_{qq}\left(\frac{x}{y}\right) + G(y, t) P_{qG}\left(\frac{x}{y}\right) \right],$$

$$\frac{dG(x, t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[\sum_{i=1}^{2f} q^i(y, t) P_{Gq}\left(\frac{x}{y}\right) + G(y, t) P_{GG}\left(\frac{x}{y}\right) \right].$$

Probability density per unit t , at order α , of finding a gluon inside a quark with a fraction x/y of the quark momentum

Density of gluons inside the proton in the infinite momentum frame

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$$\frac{dG(x, t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[\sum_{i=1}^{2f} q^i(y, t) P_{Gq}\left(\frac{x}{y}\right) + G(y, t) P_{GG}\left(\frac{x}{y}\right) \right].$$

Scaling violations

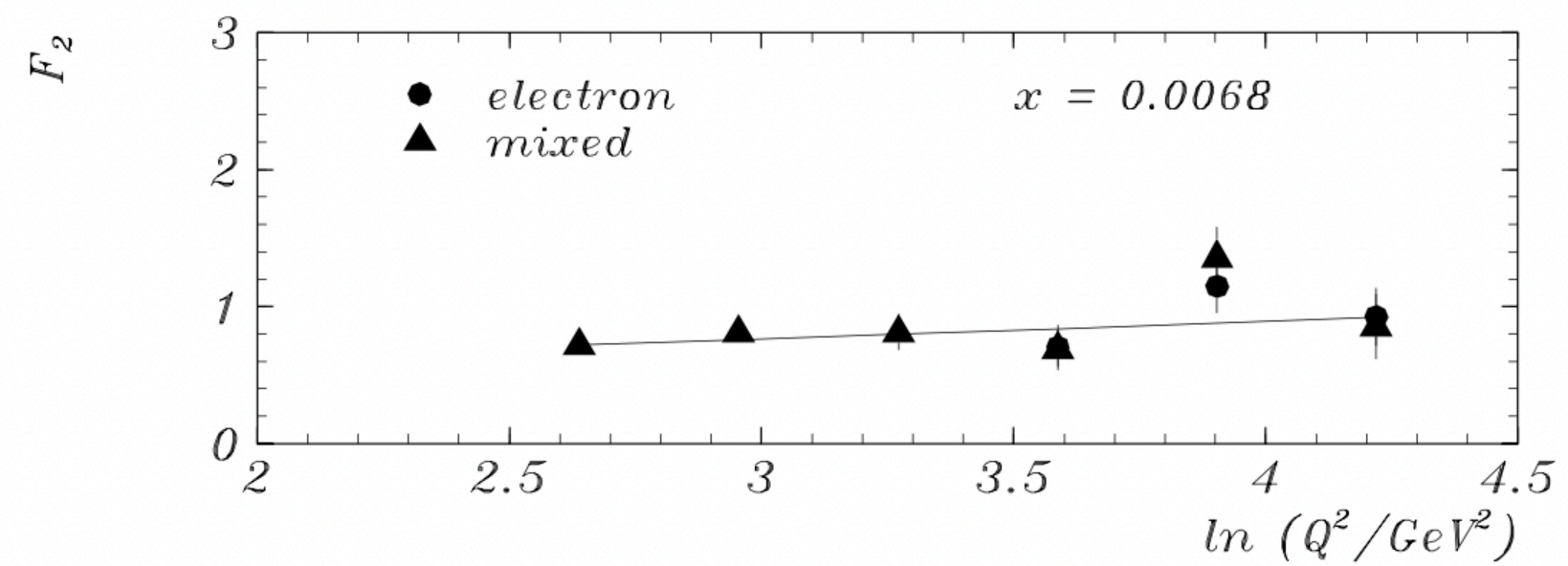
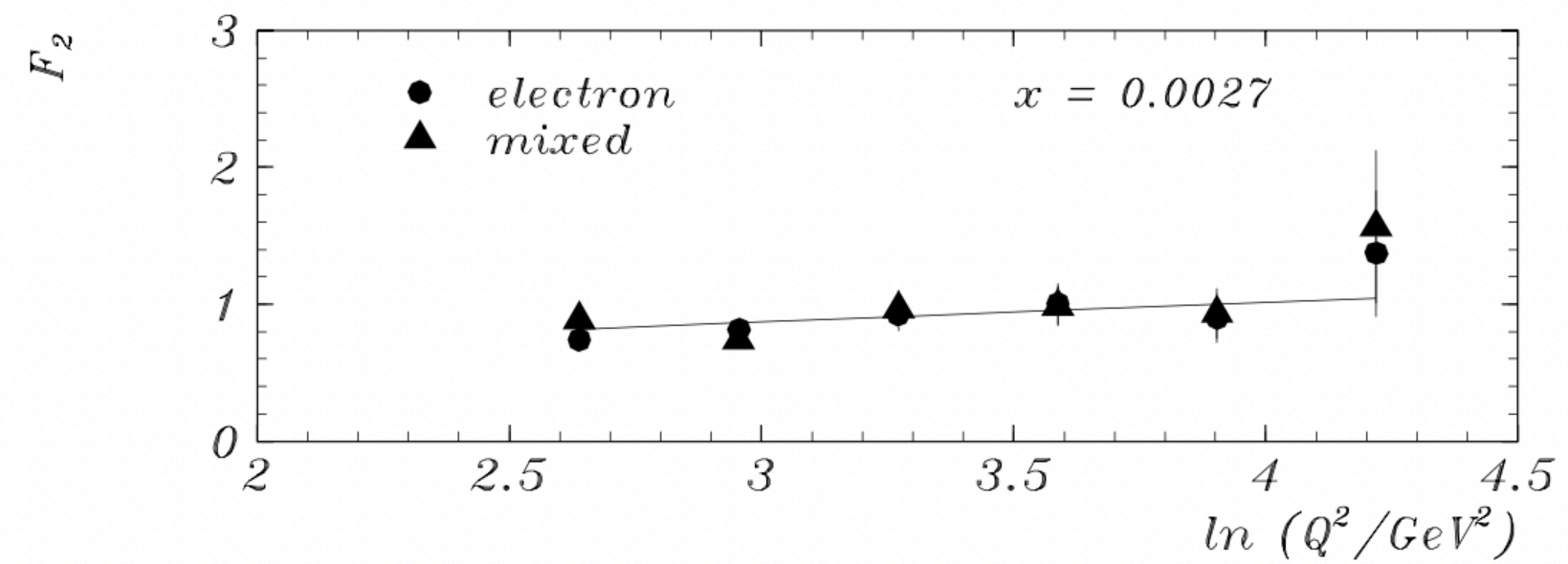
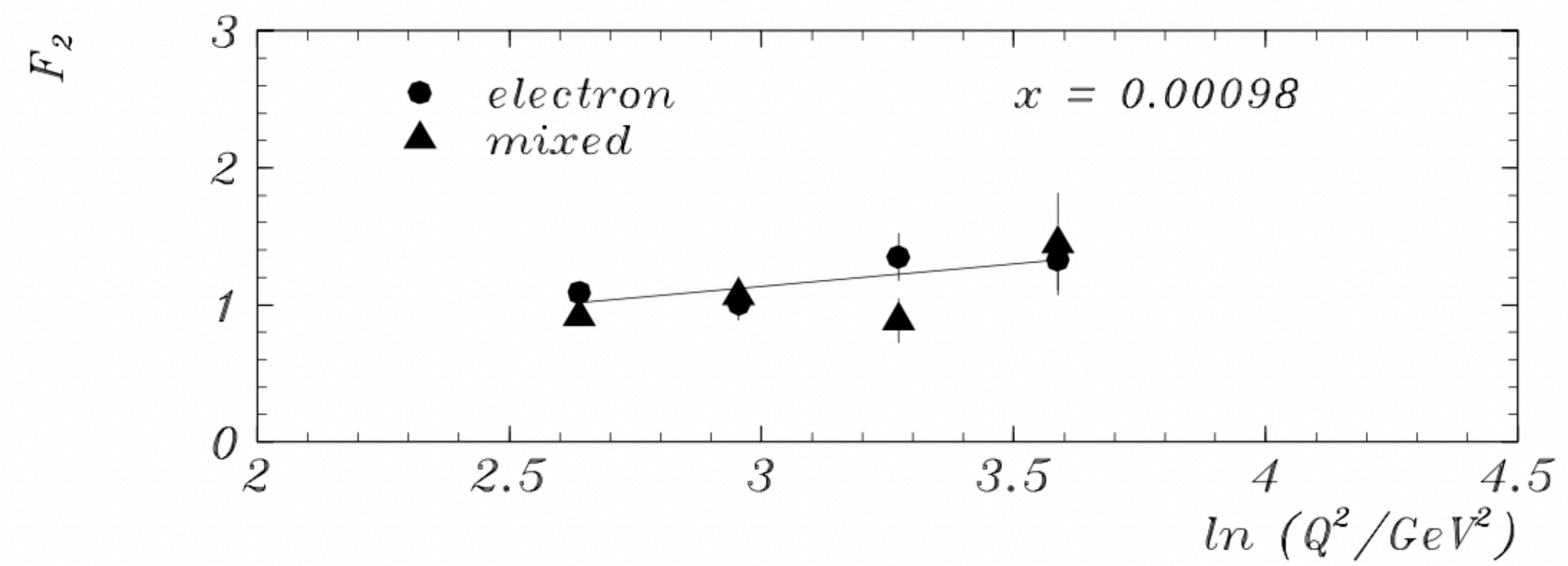
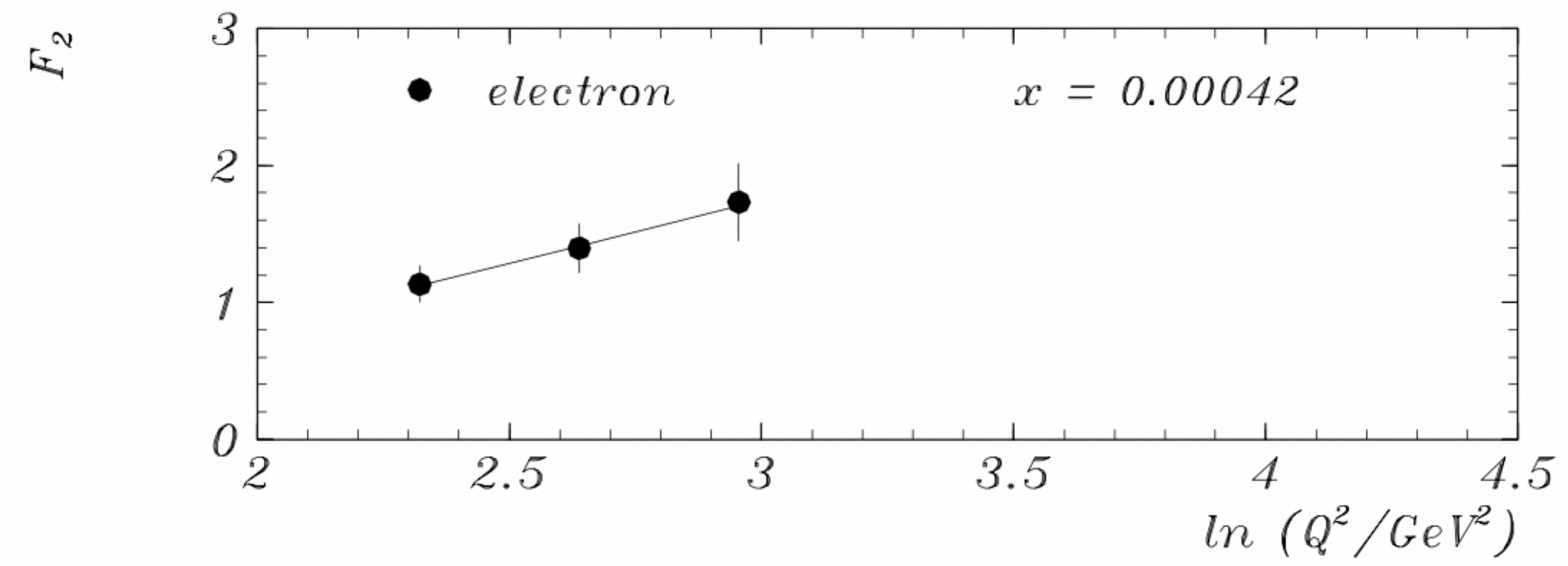
Probability density per unit t , at order α , of finding a gluon inside a quark with a fraction x/y of the quark momentum

Density of gluons inside the proton in the infinite momentum frame

The evolution of hadron structure is predicted within pQCD in the form of differential equations

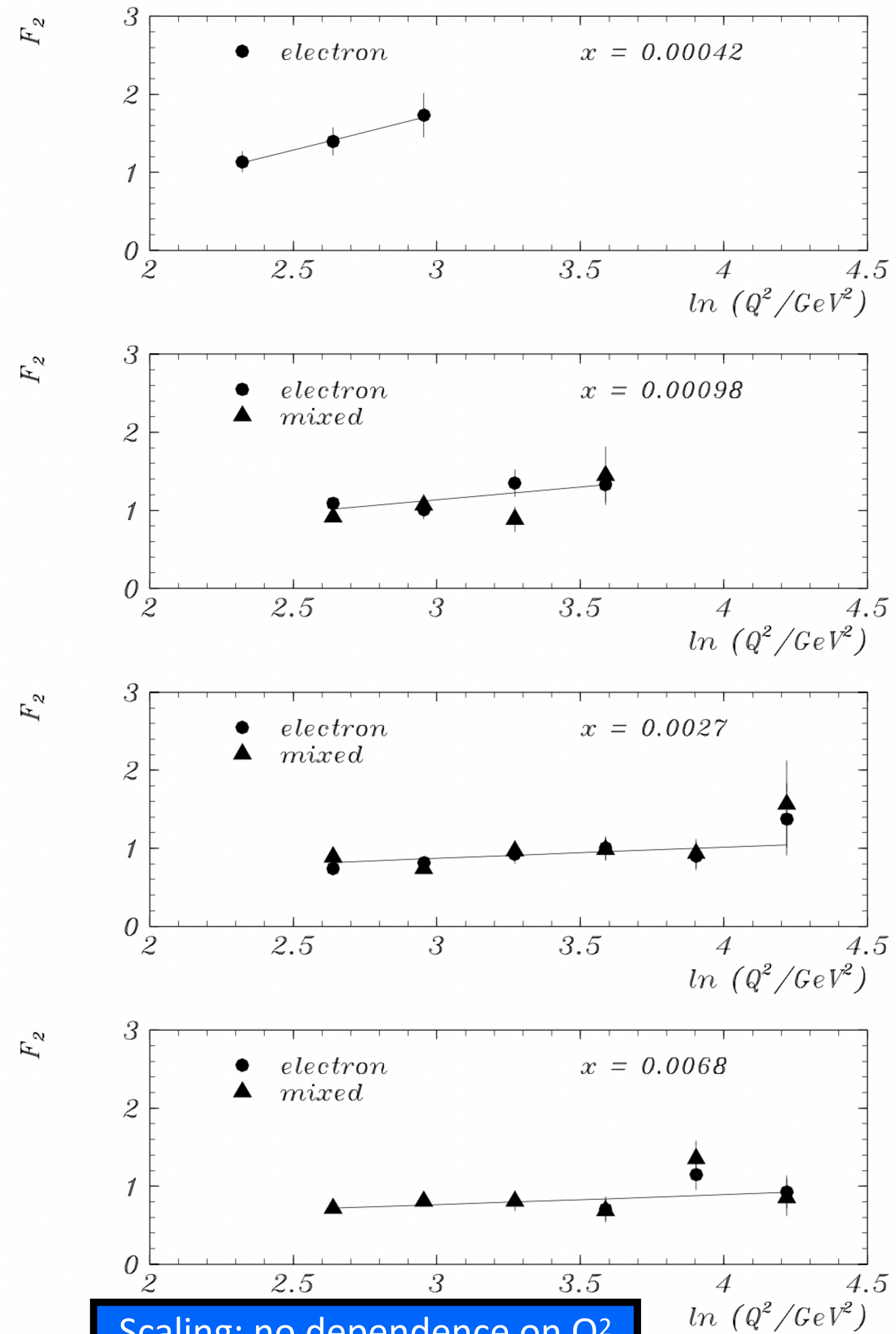
Scaling violations and the gluon in the proton (1994)

H1, <https://inspirehep.net/literature/360235>



Scaling violations and the gluon in the proton (1994)

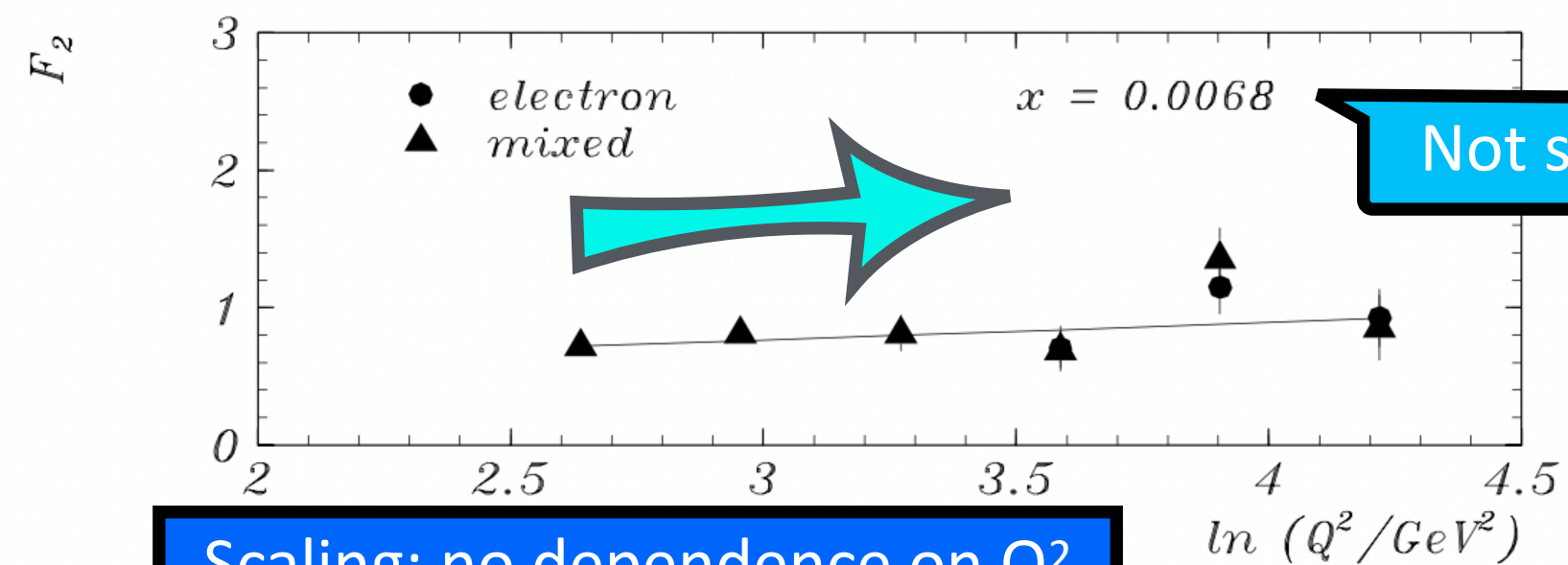
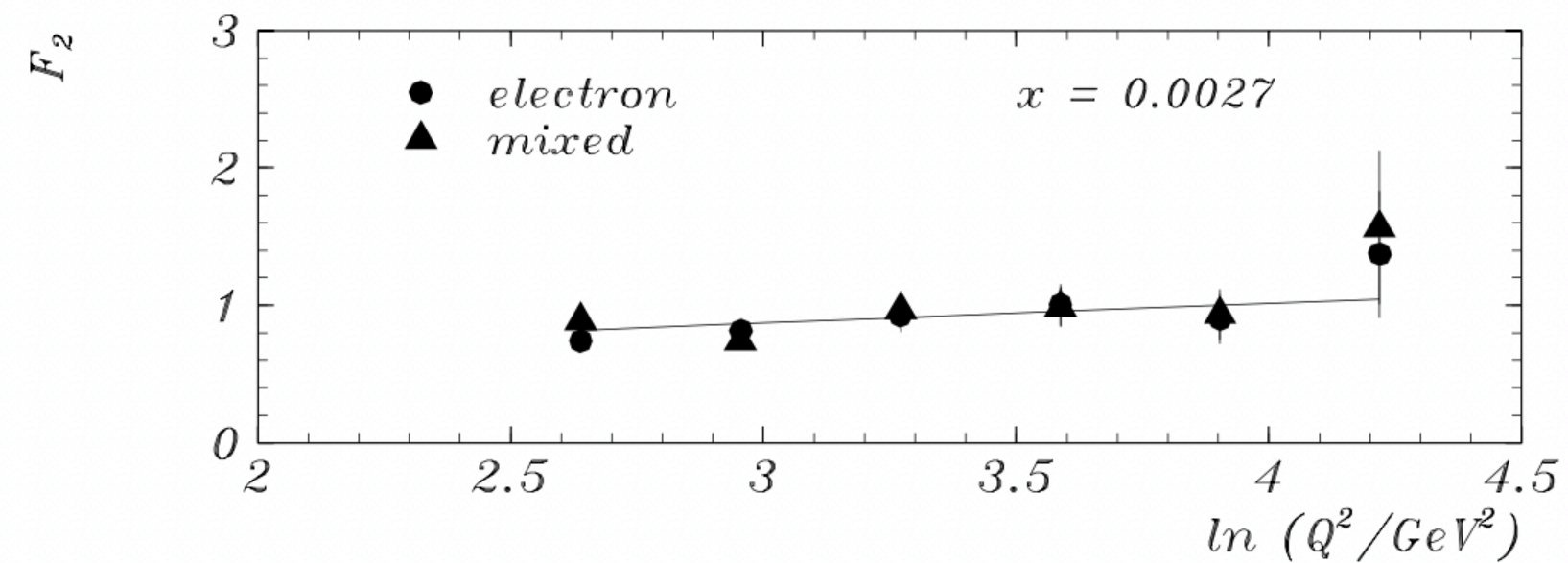
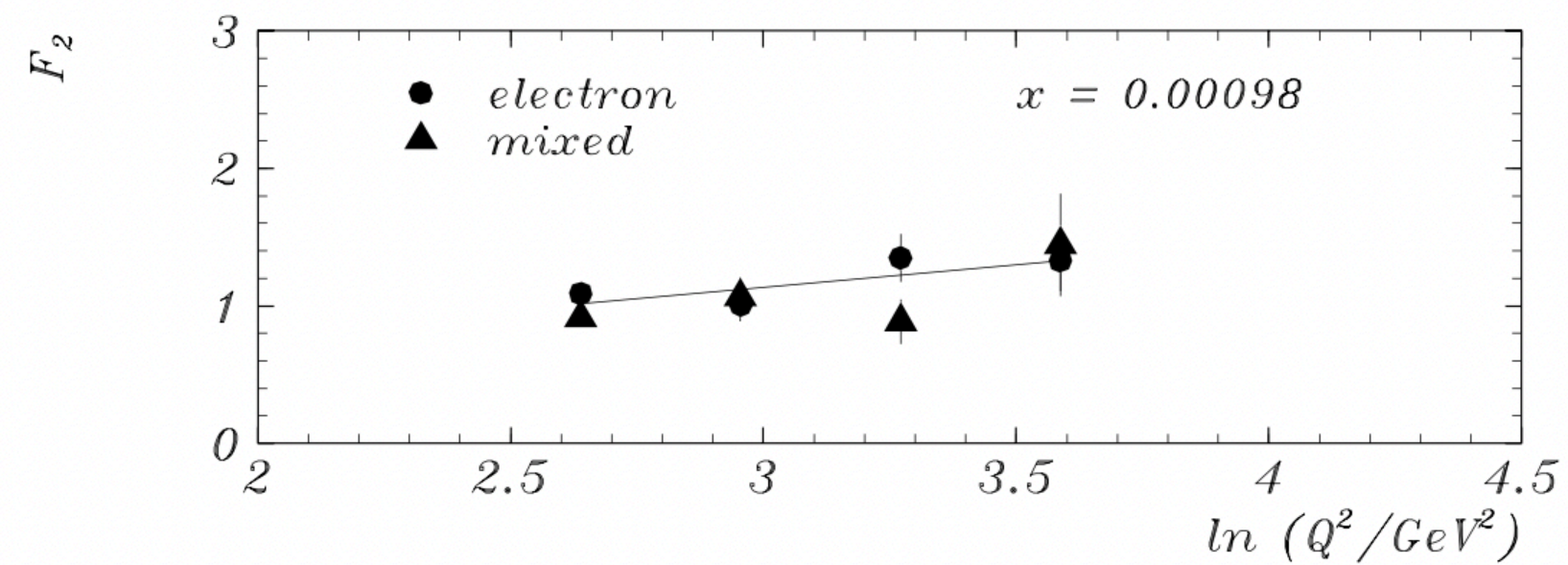
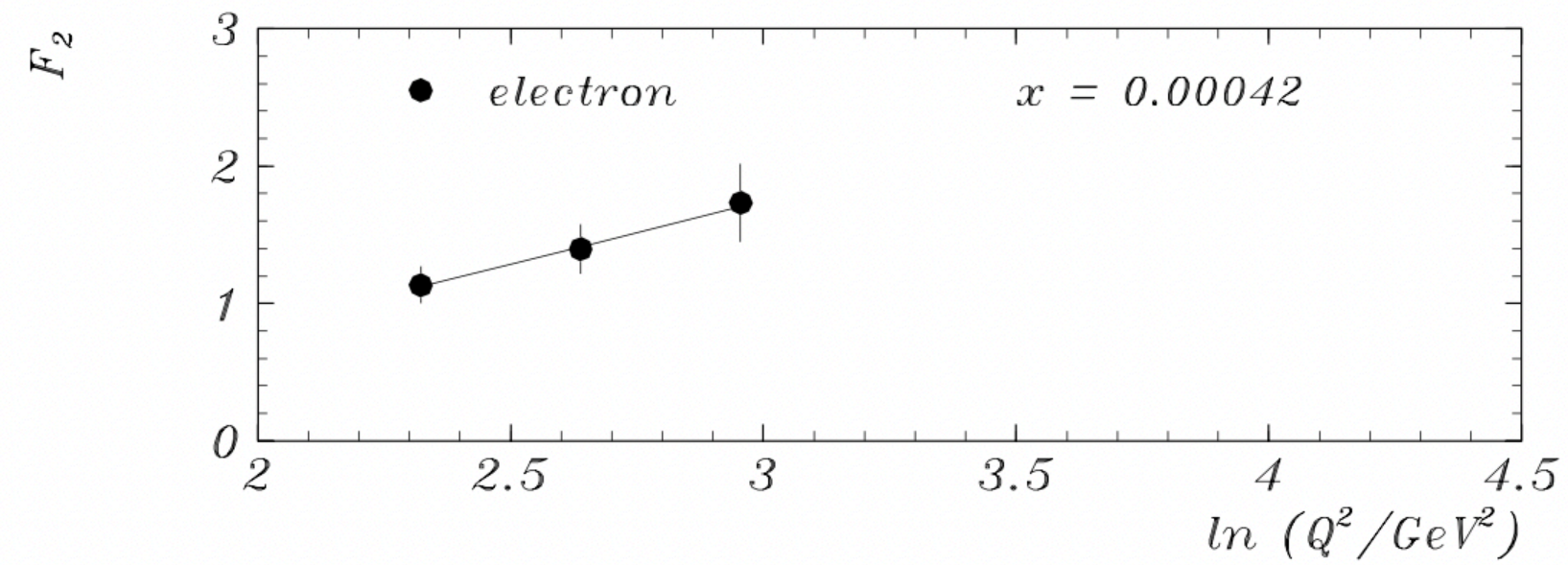
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Scaling: no dependence on Q^2

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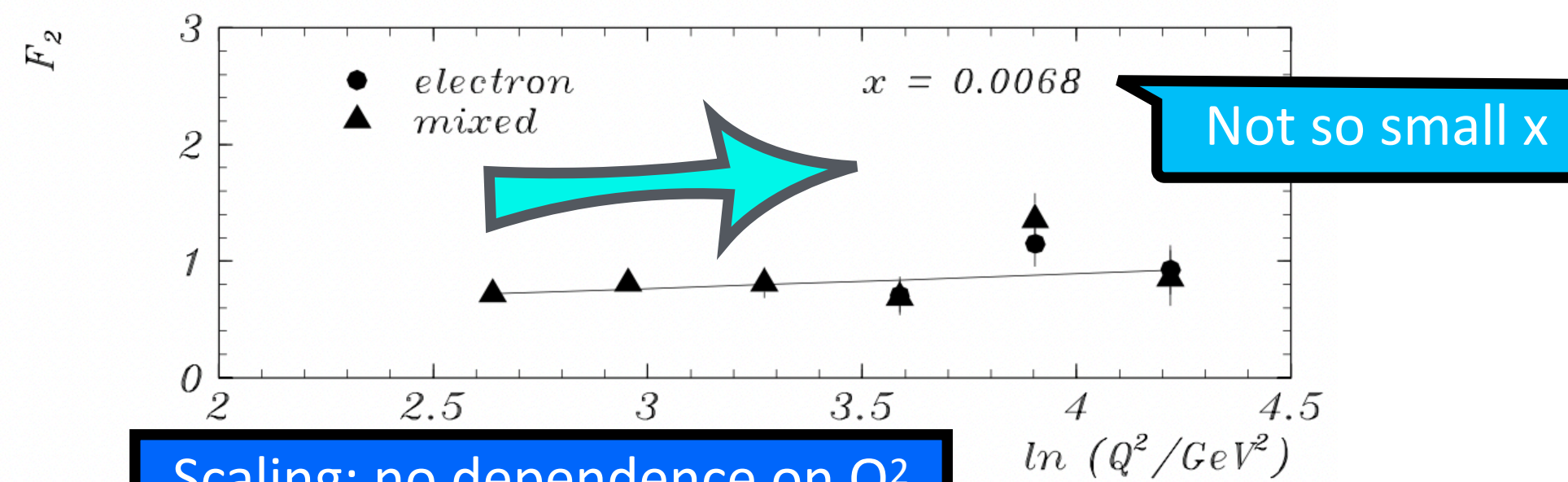
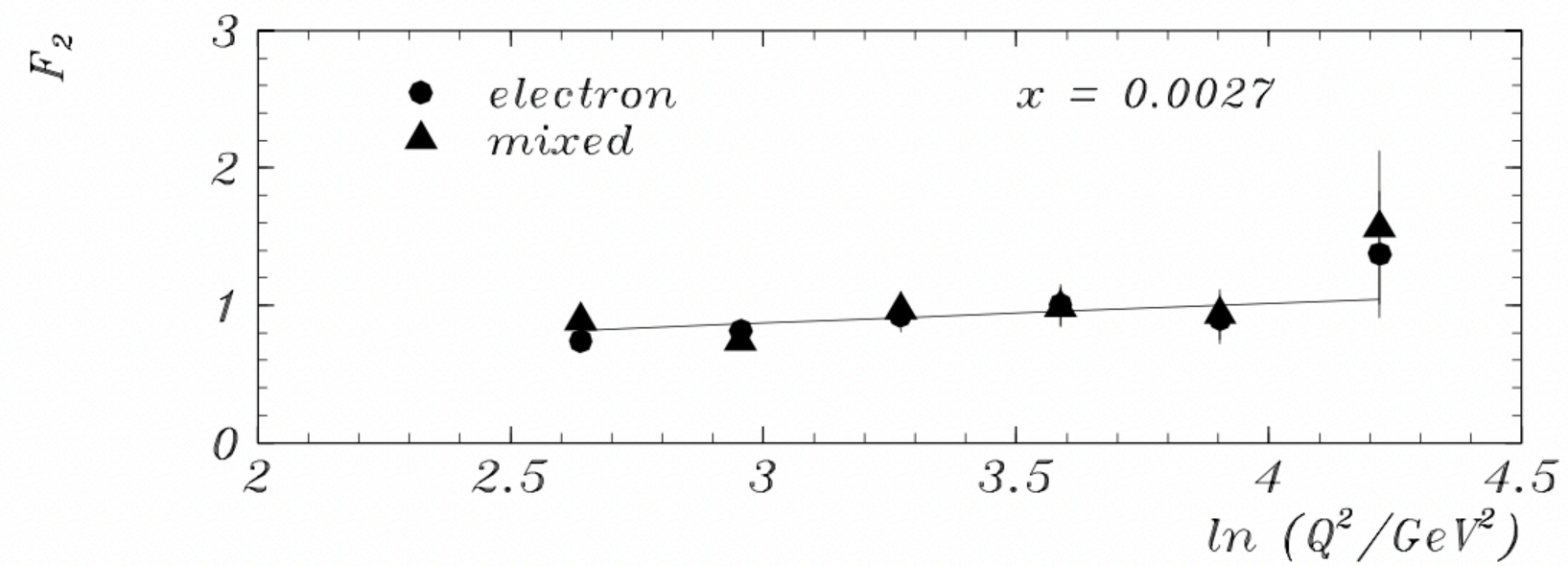
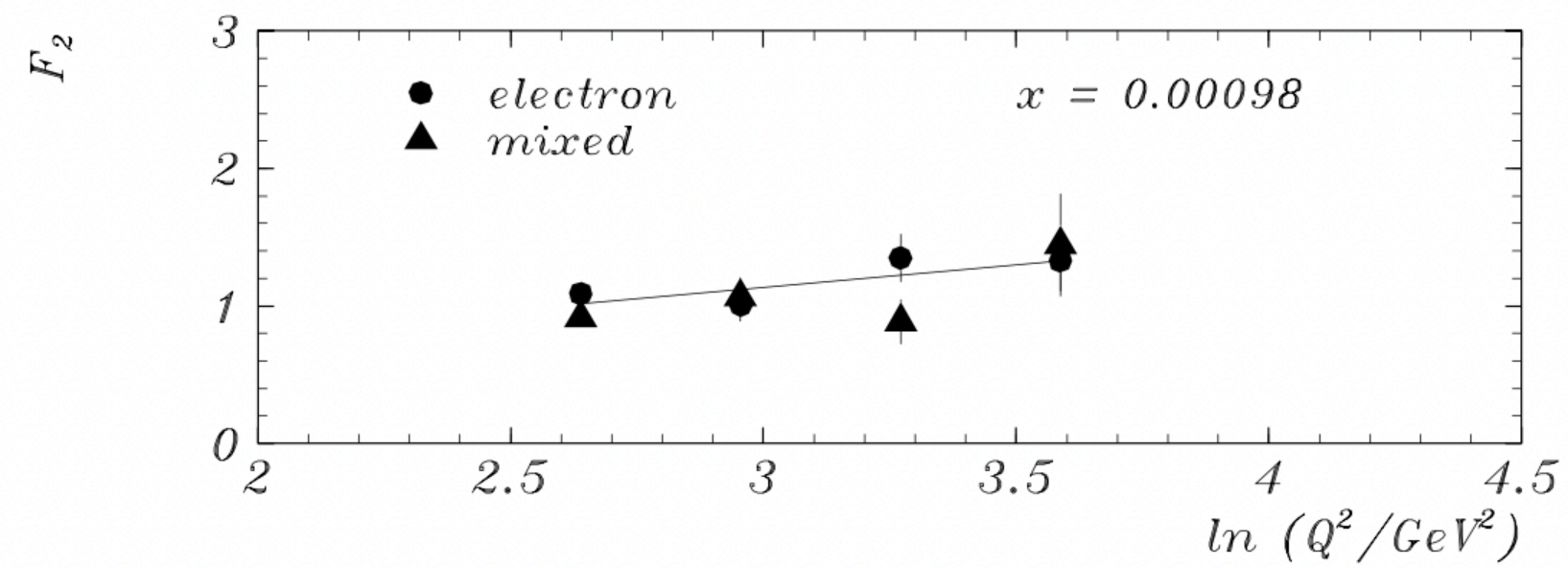
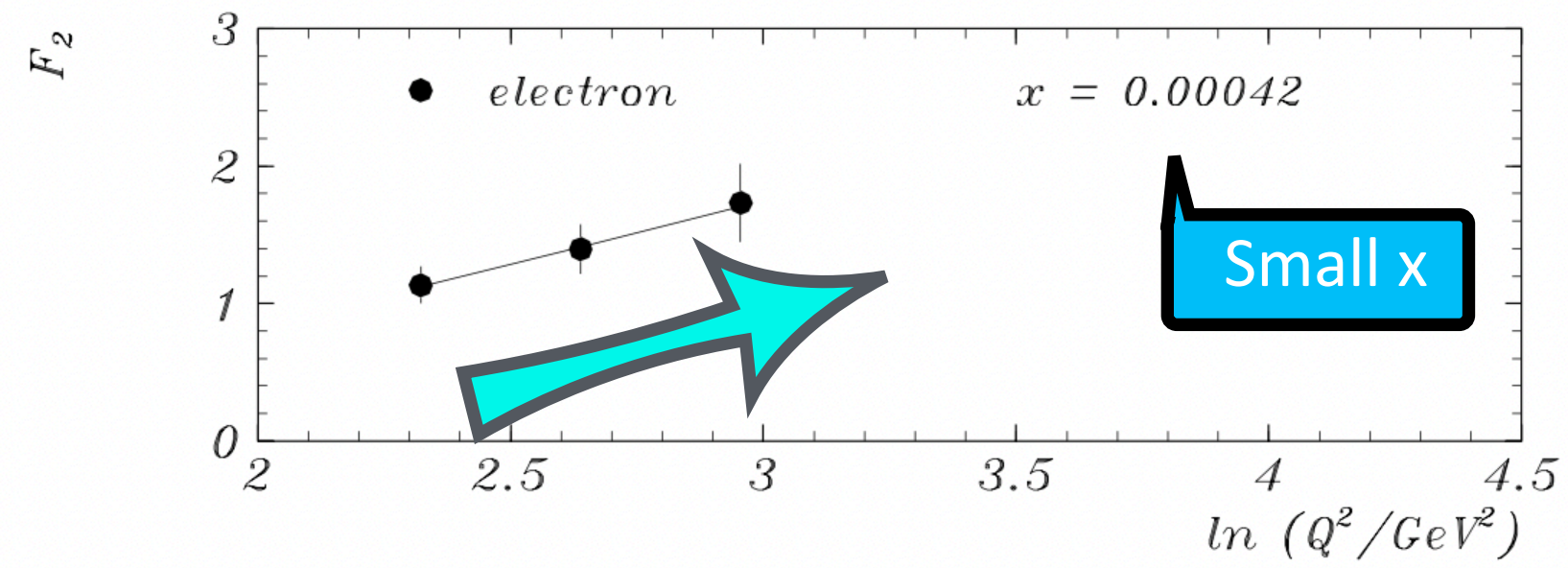


Not so small x

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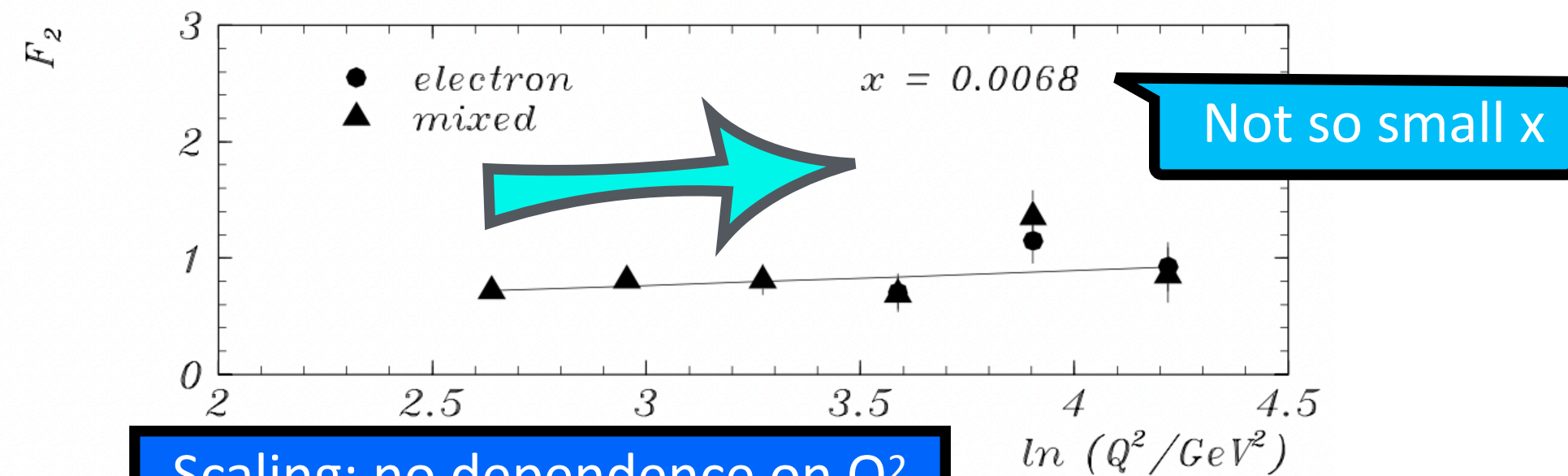
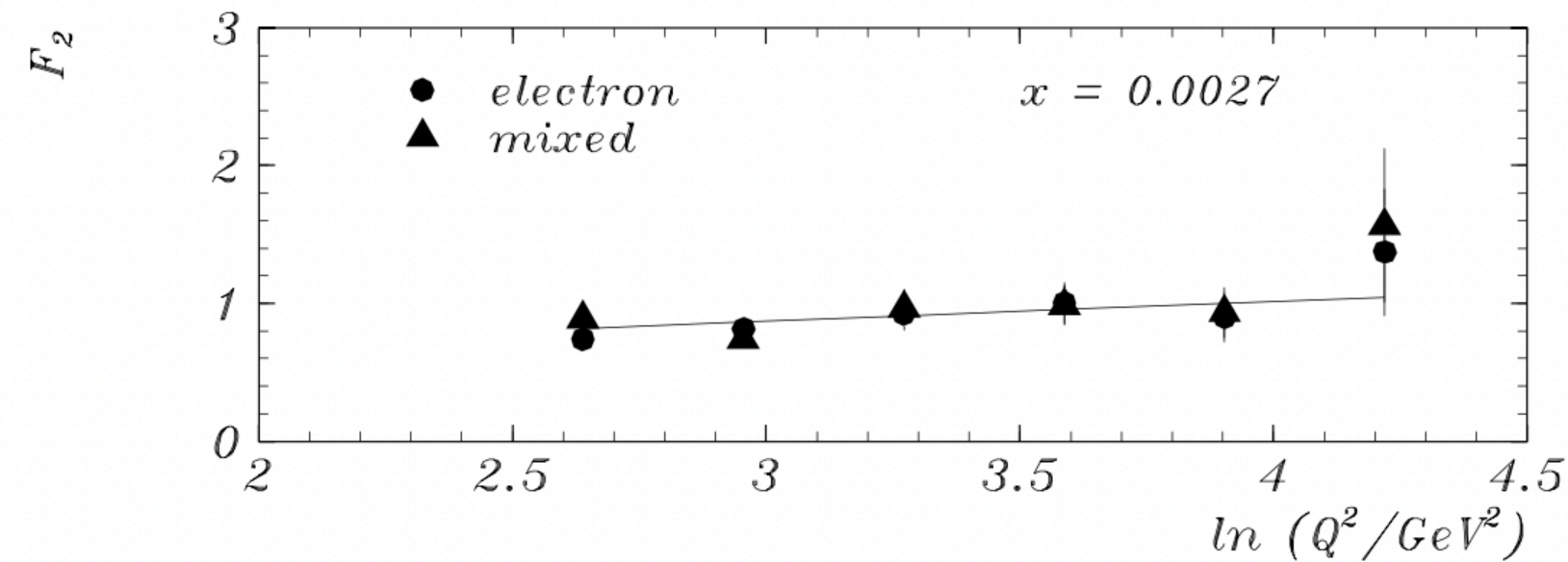
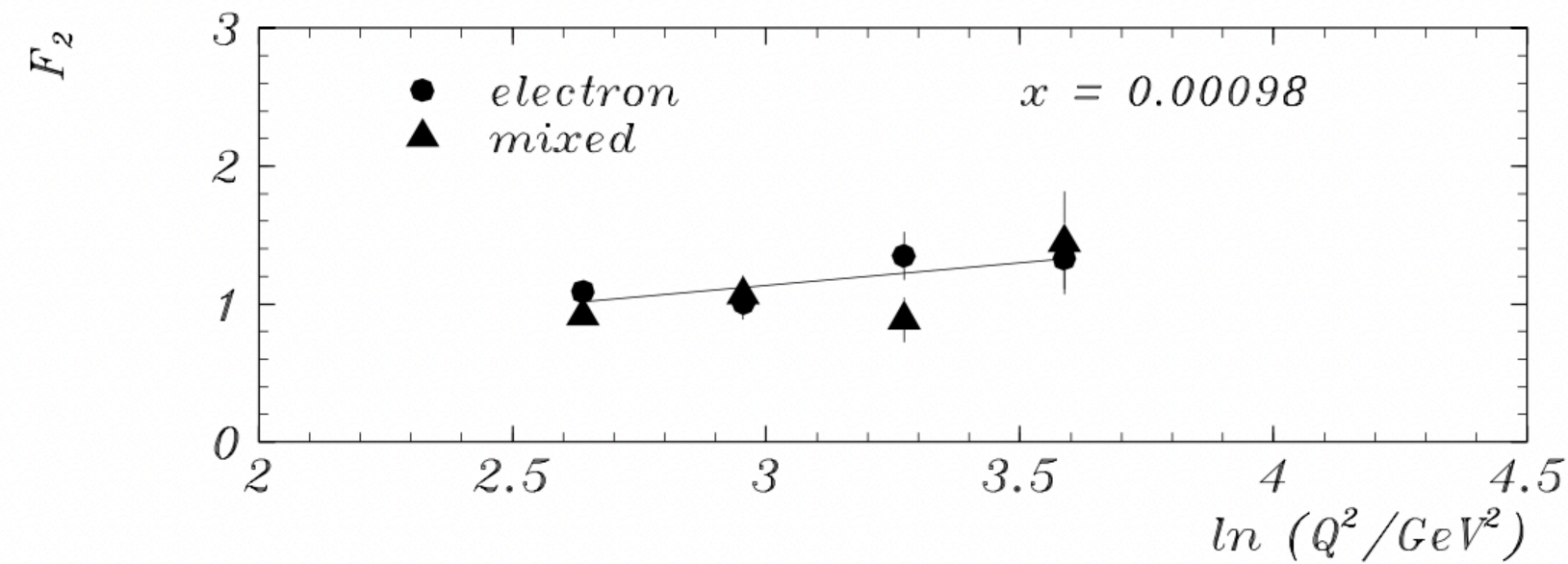
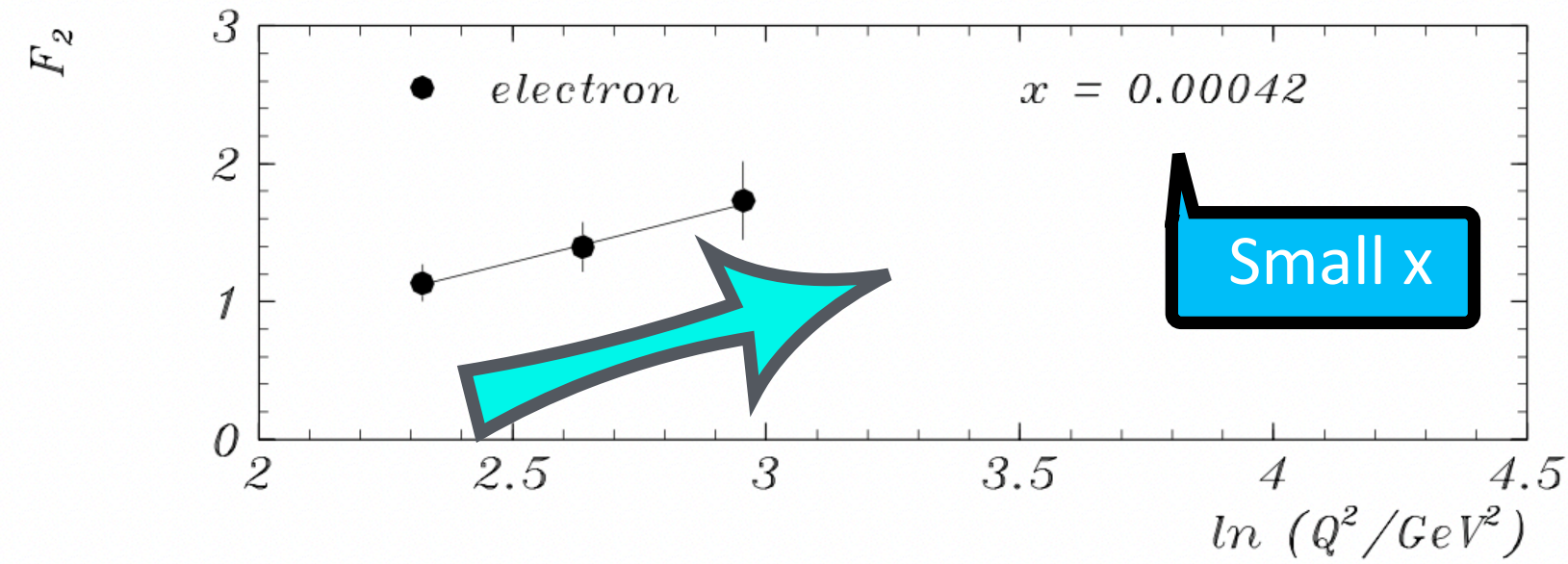
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Scaling violations logarithmic in virtuality

Violations more severe at small Bjorken x



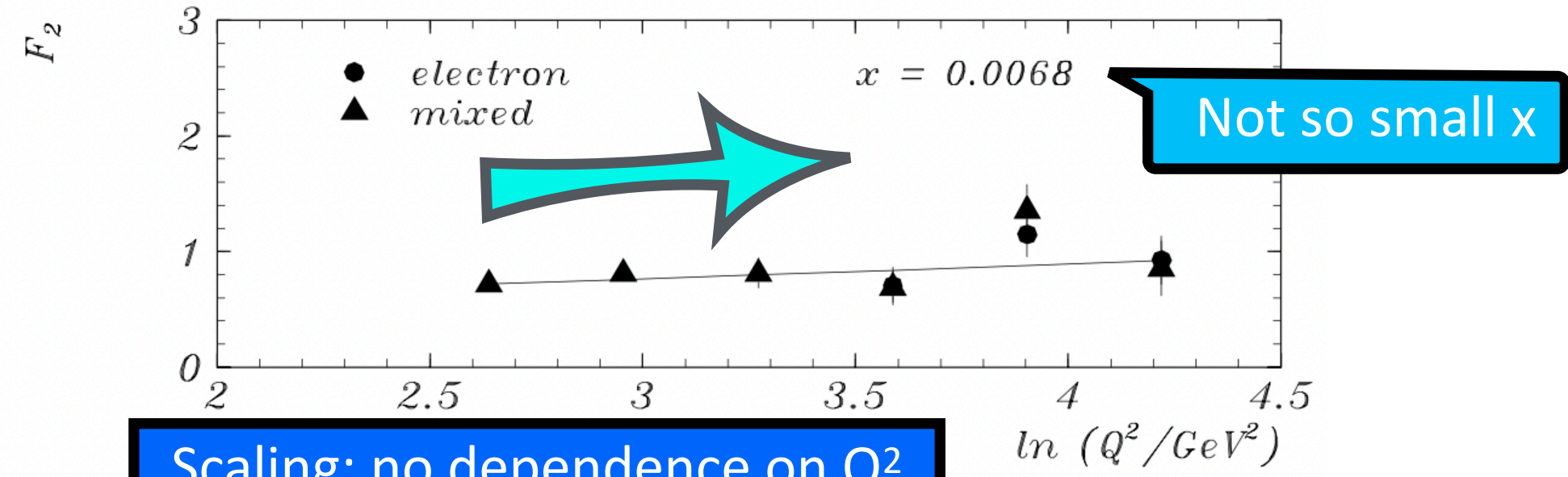
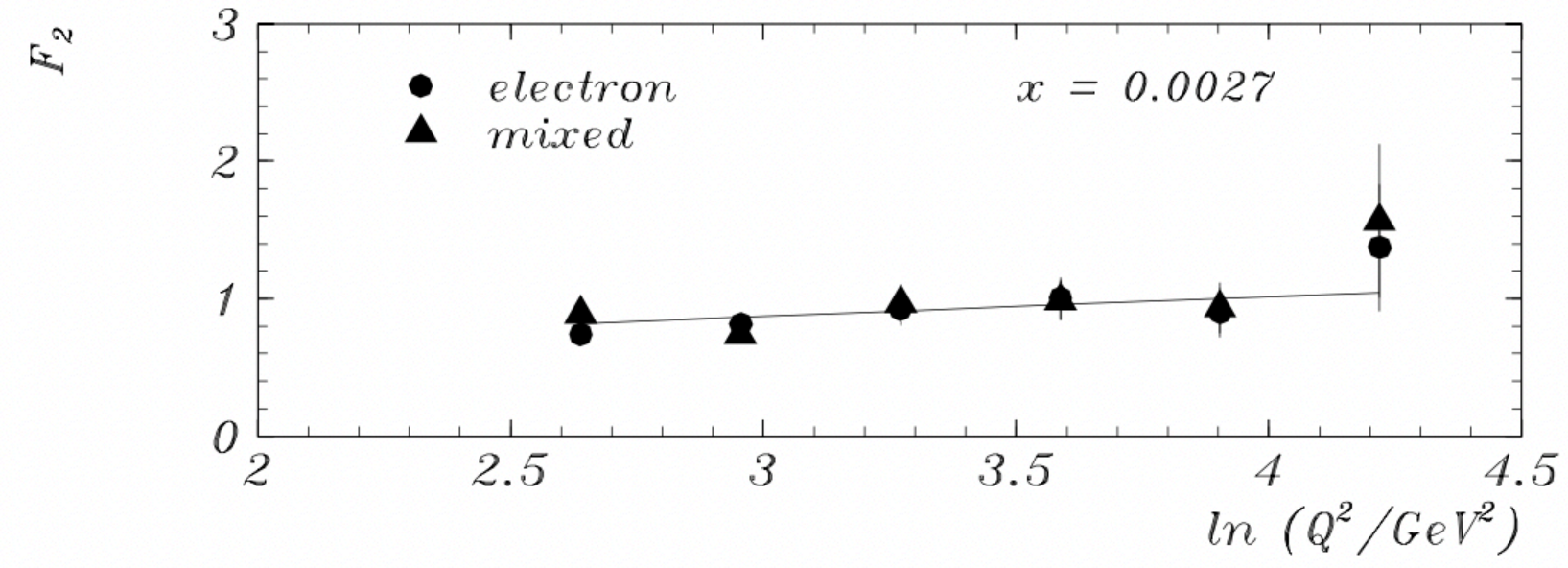
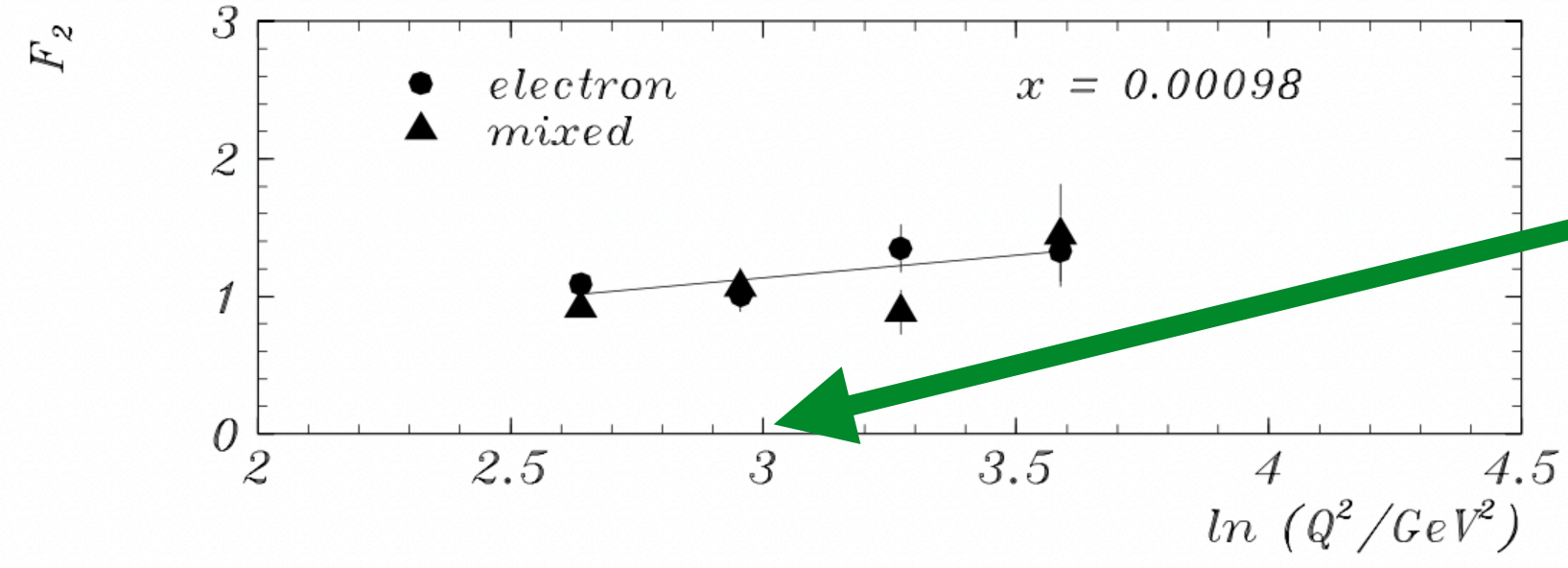
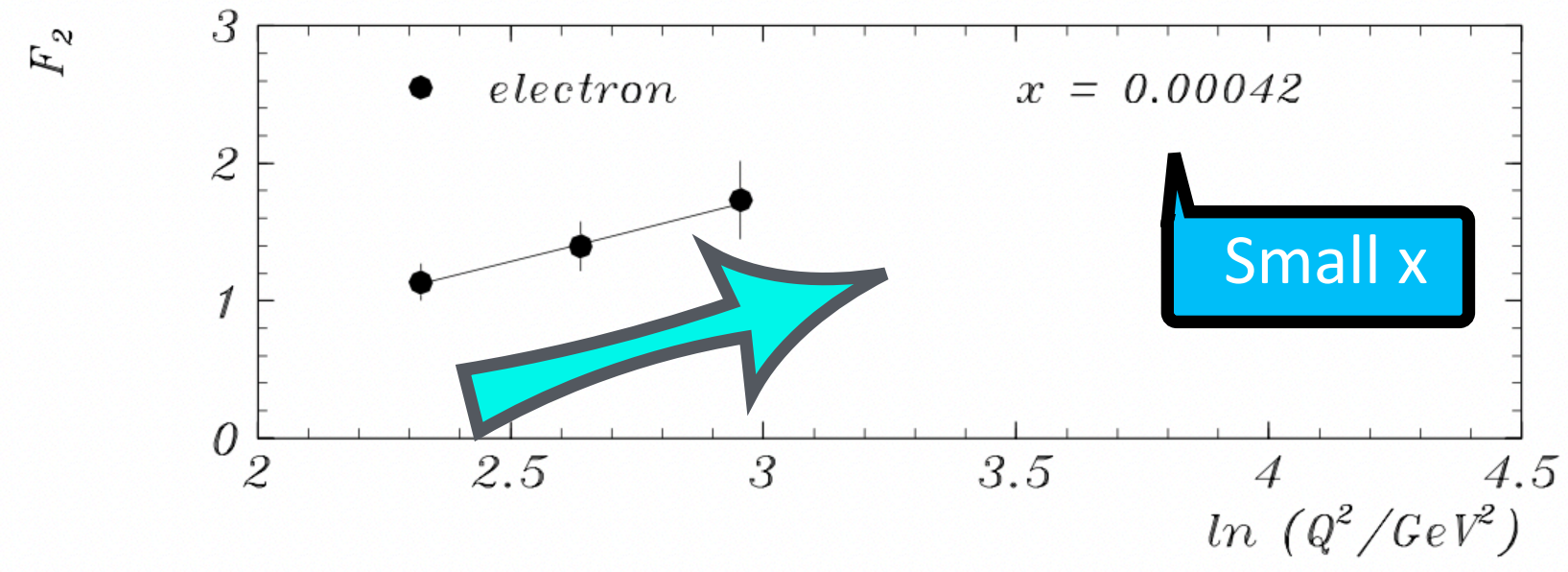
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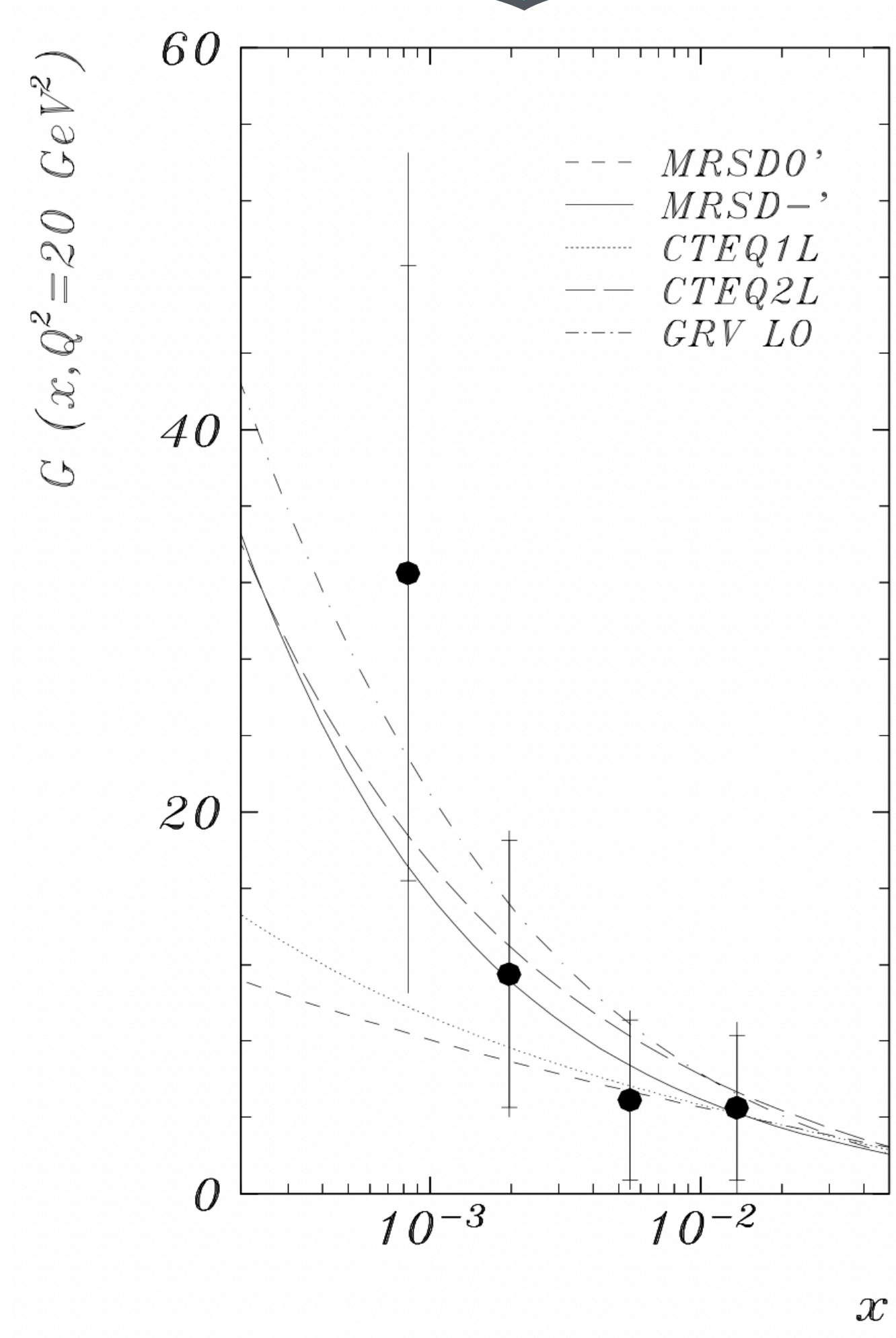
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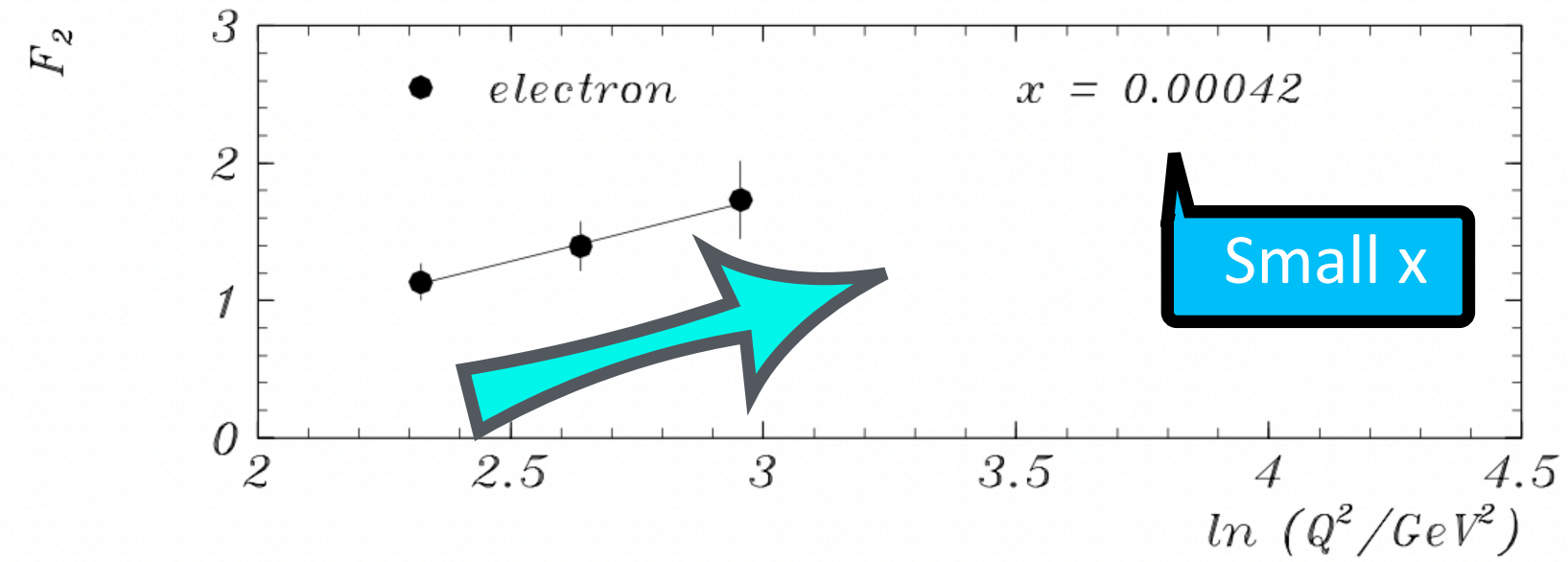


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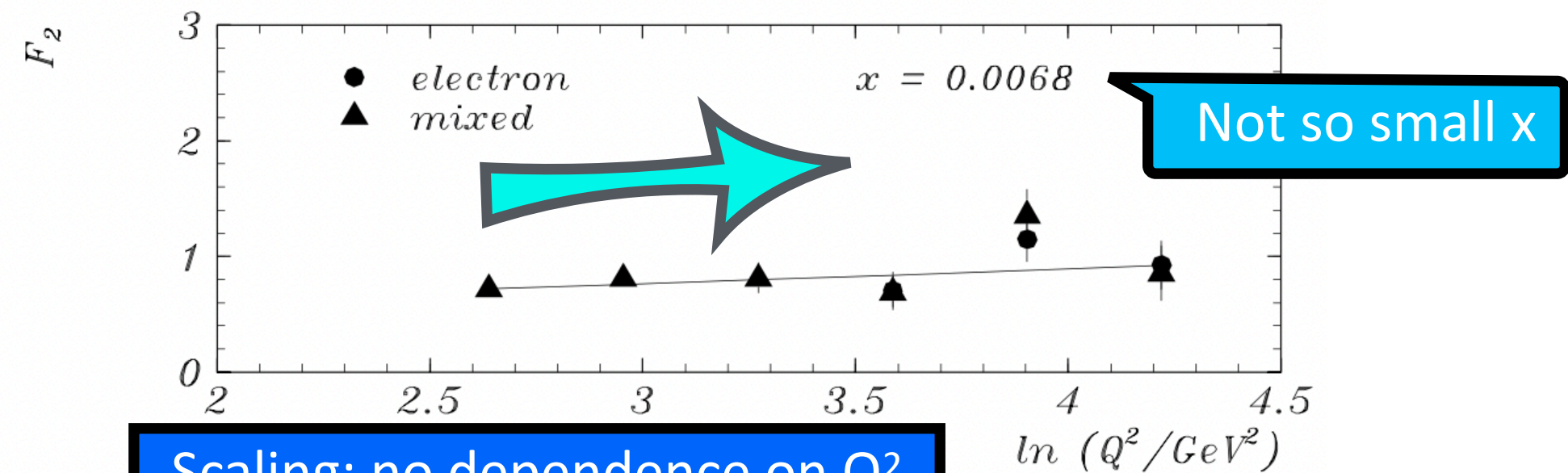
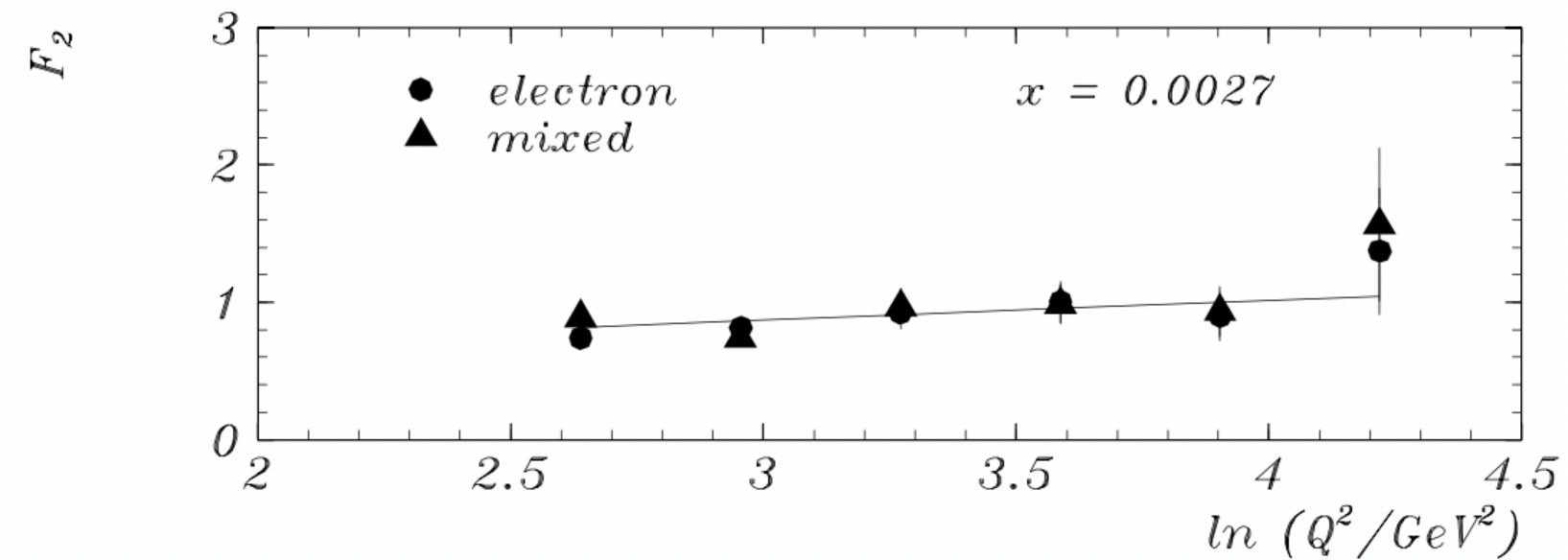
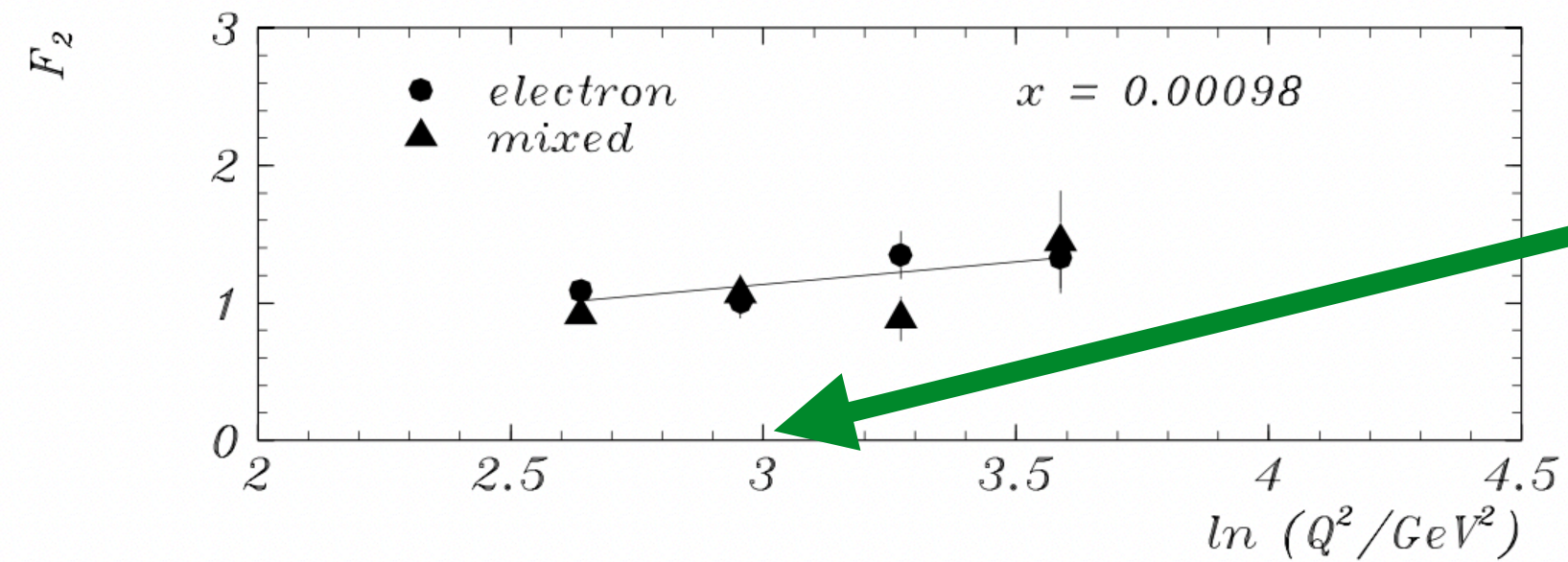
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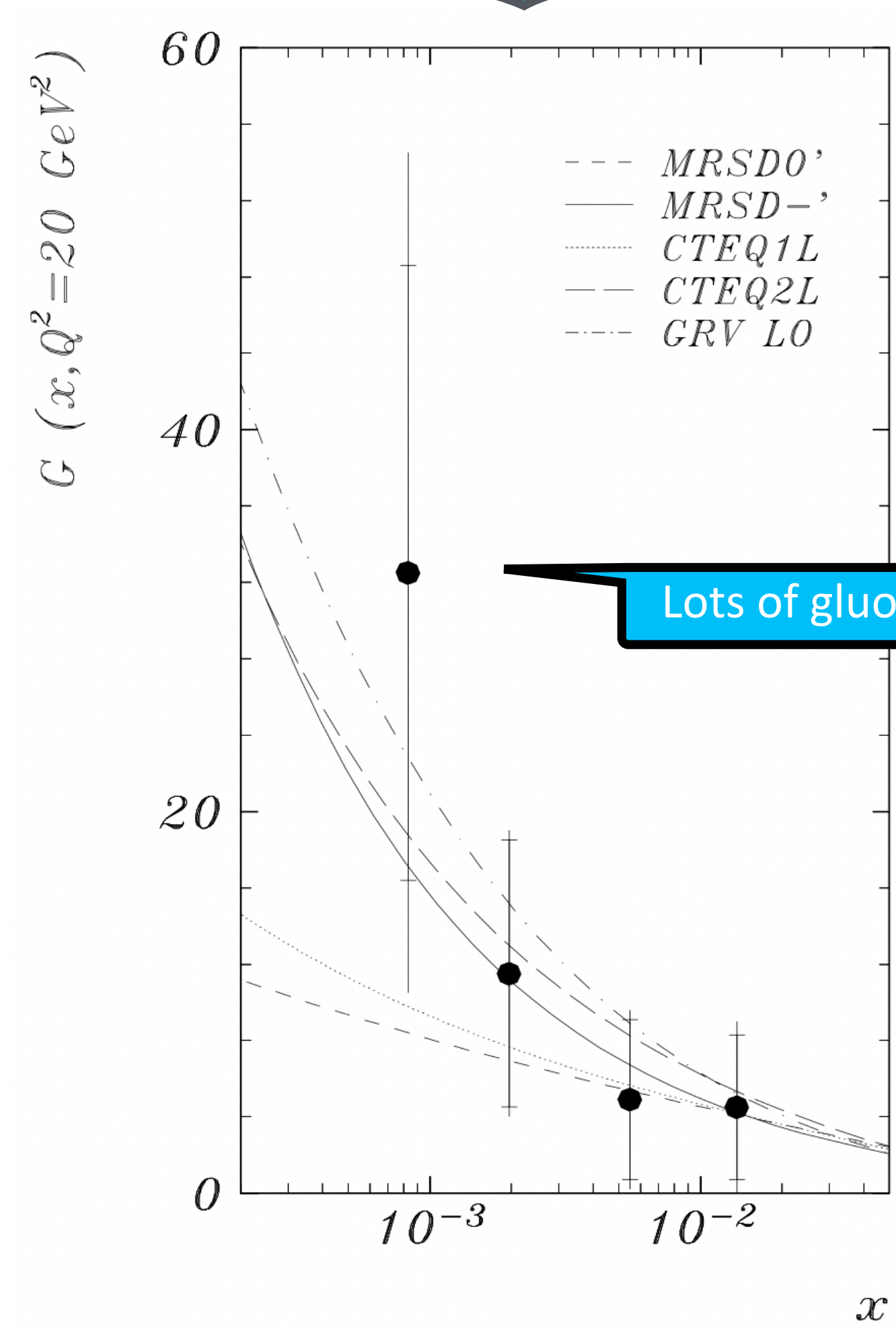


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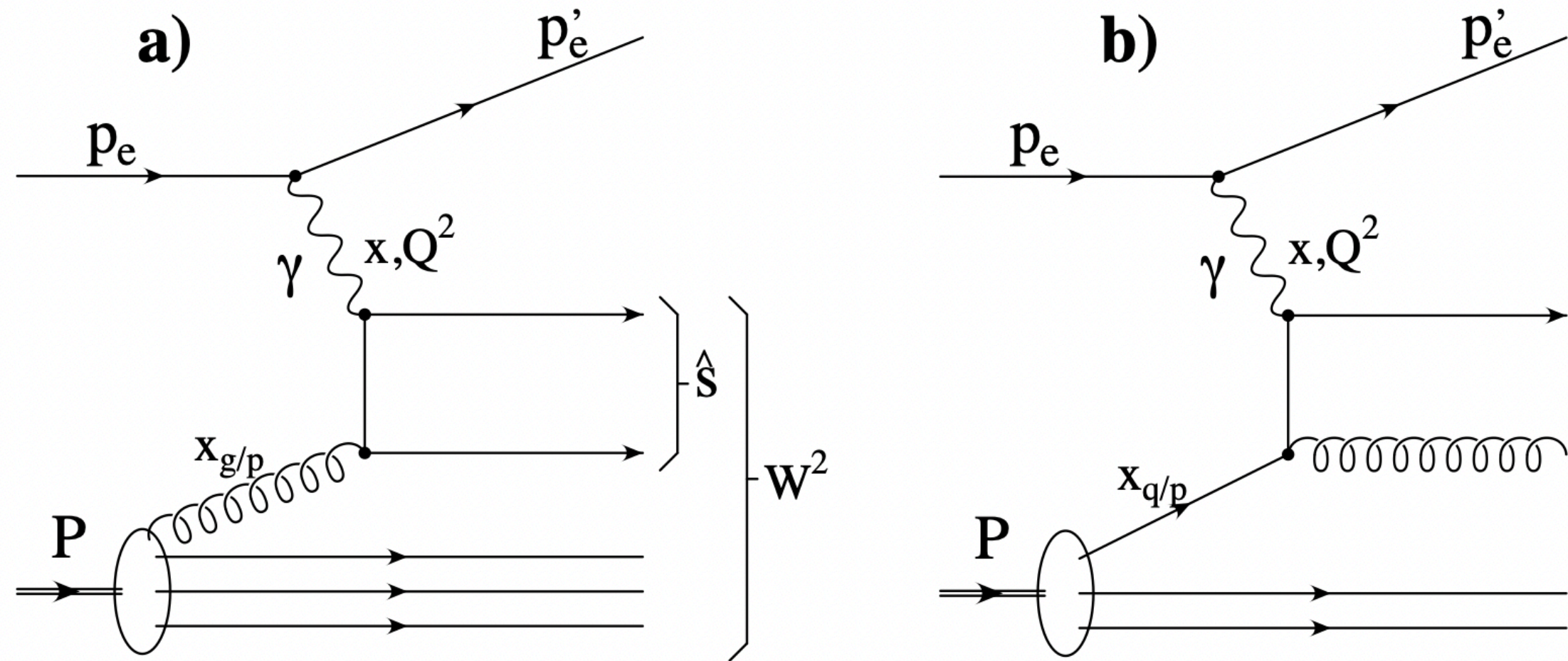
Photon-gluon fusion (1995)

Let's try to see the gluons directly!

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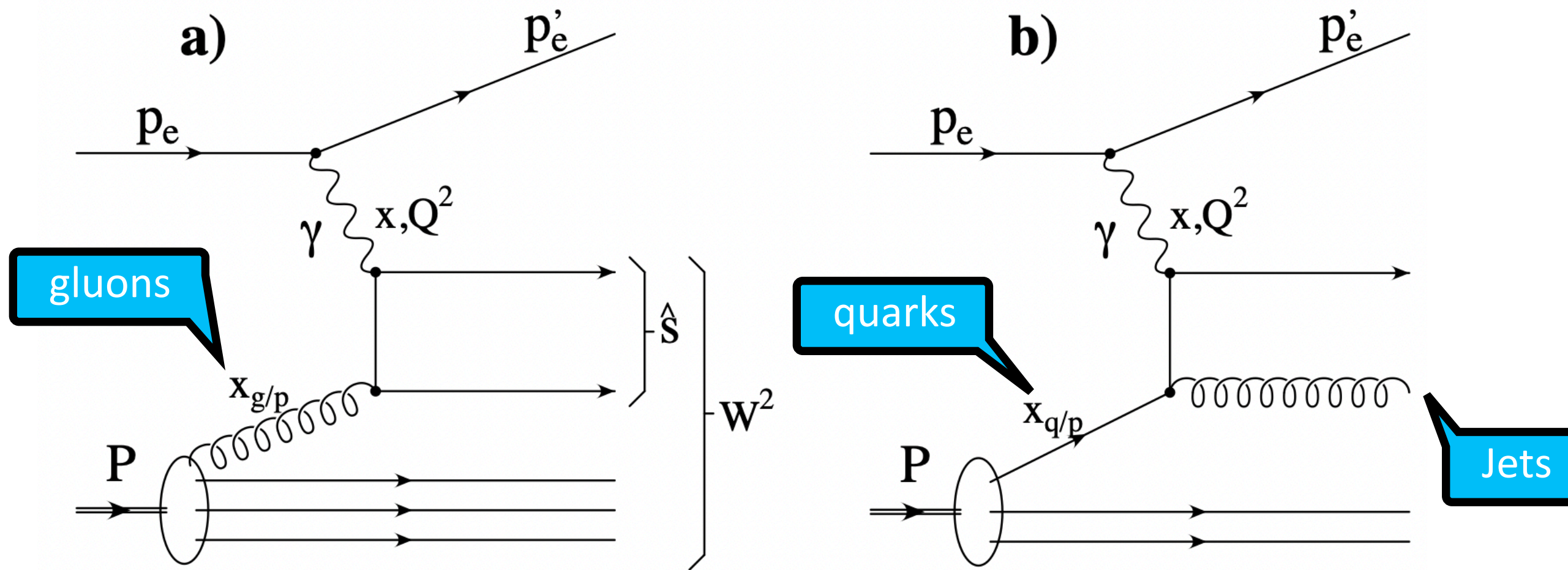
H1, <https://inspirehep.net/literature/395643>



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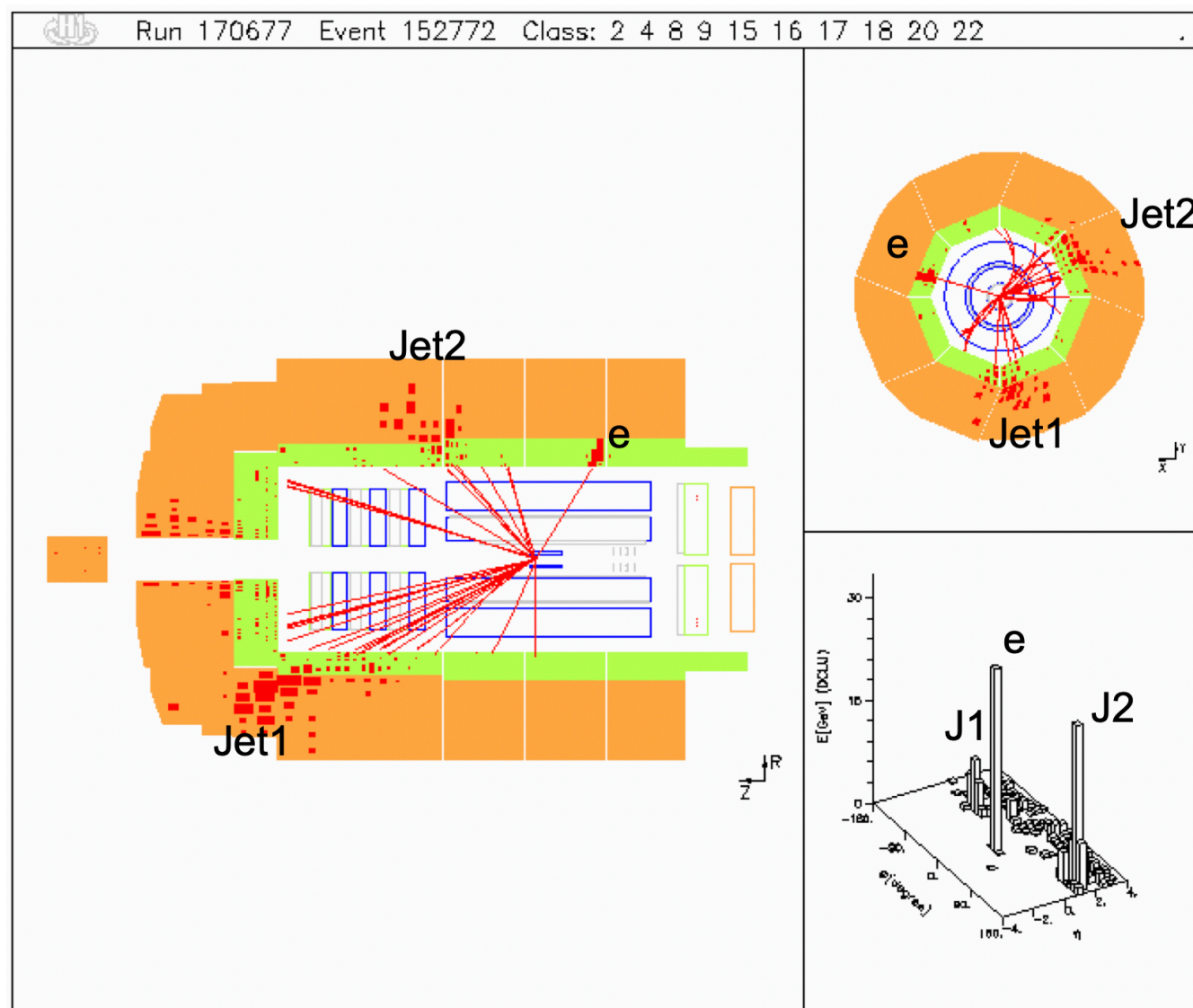
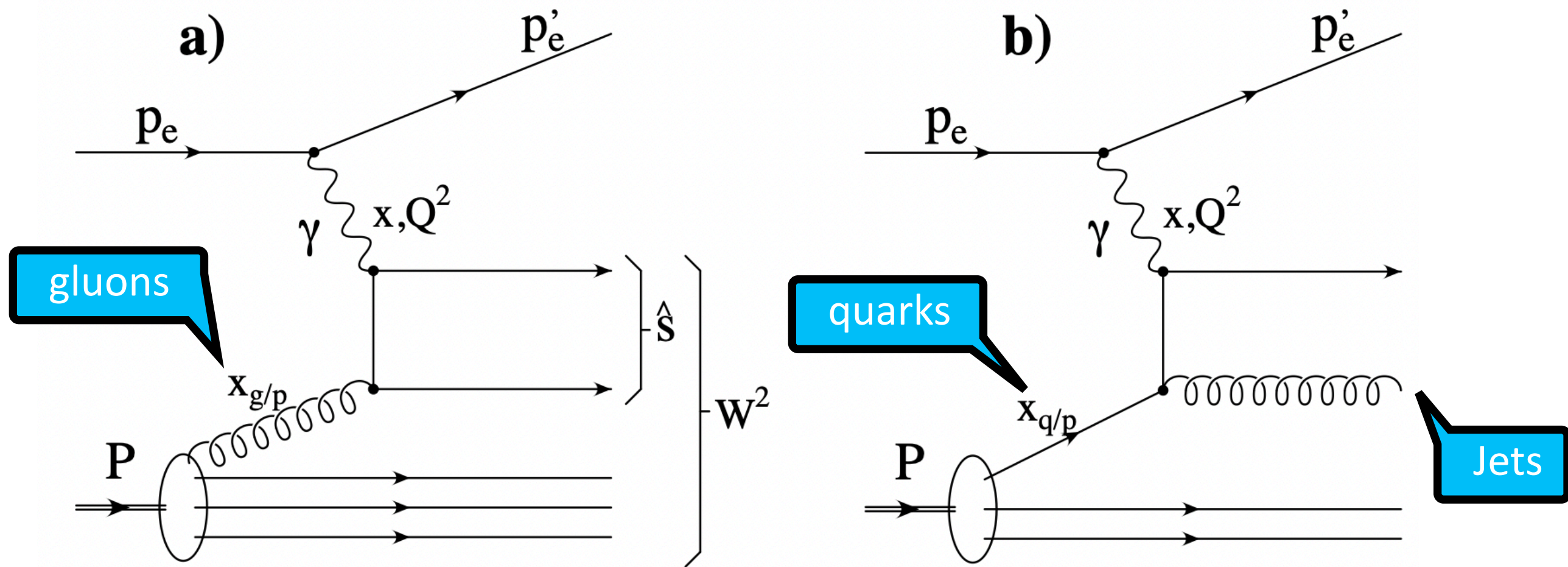
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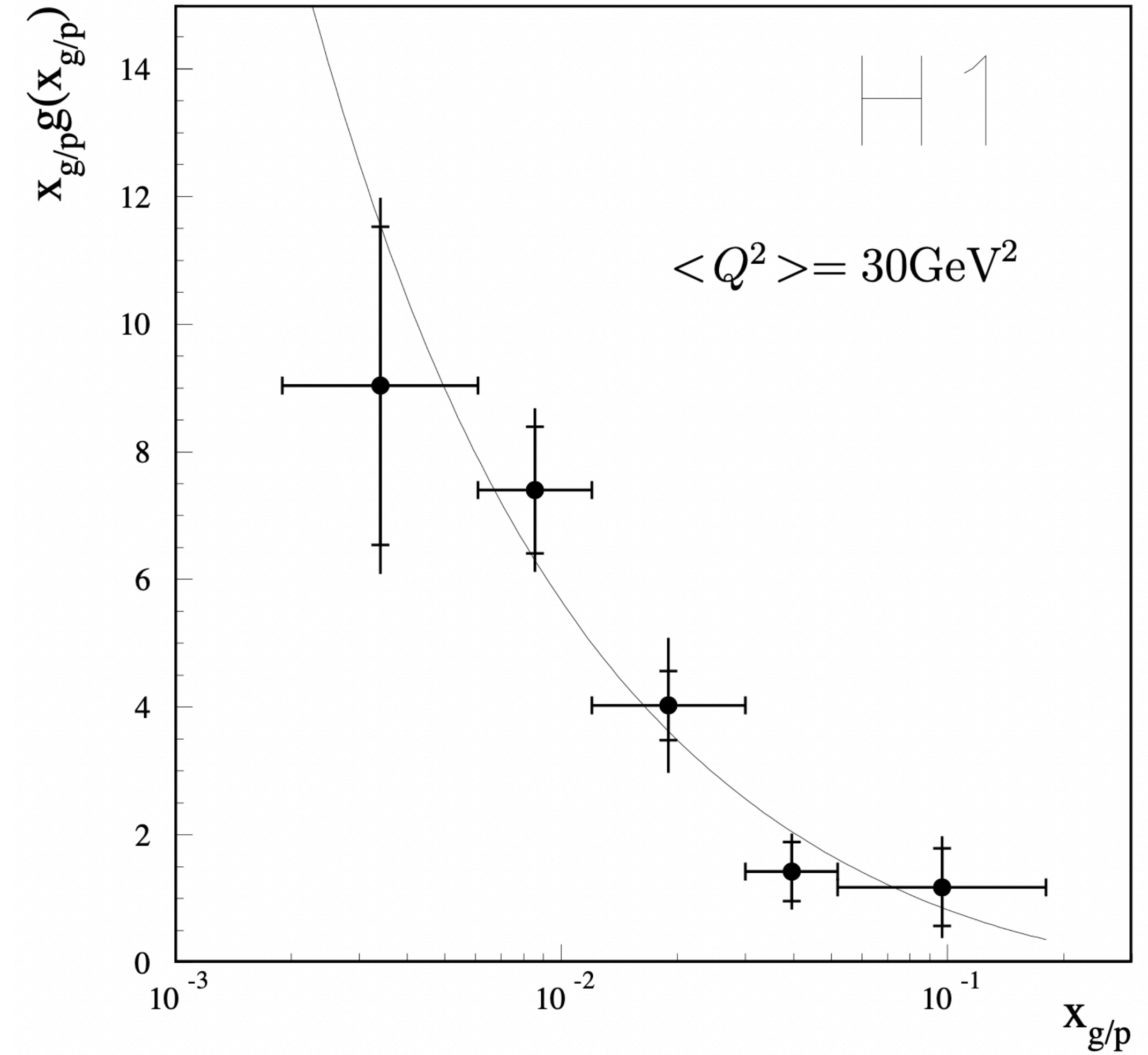
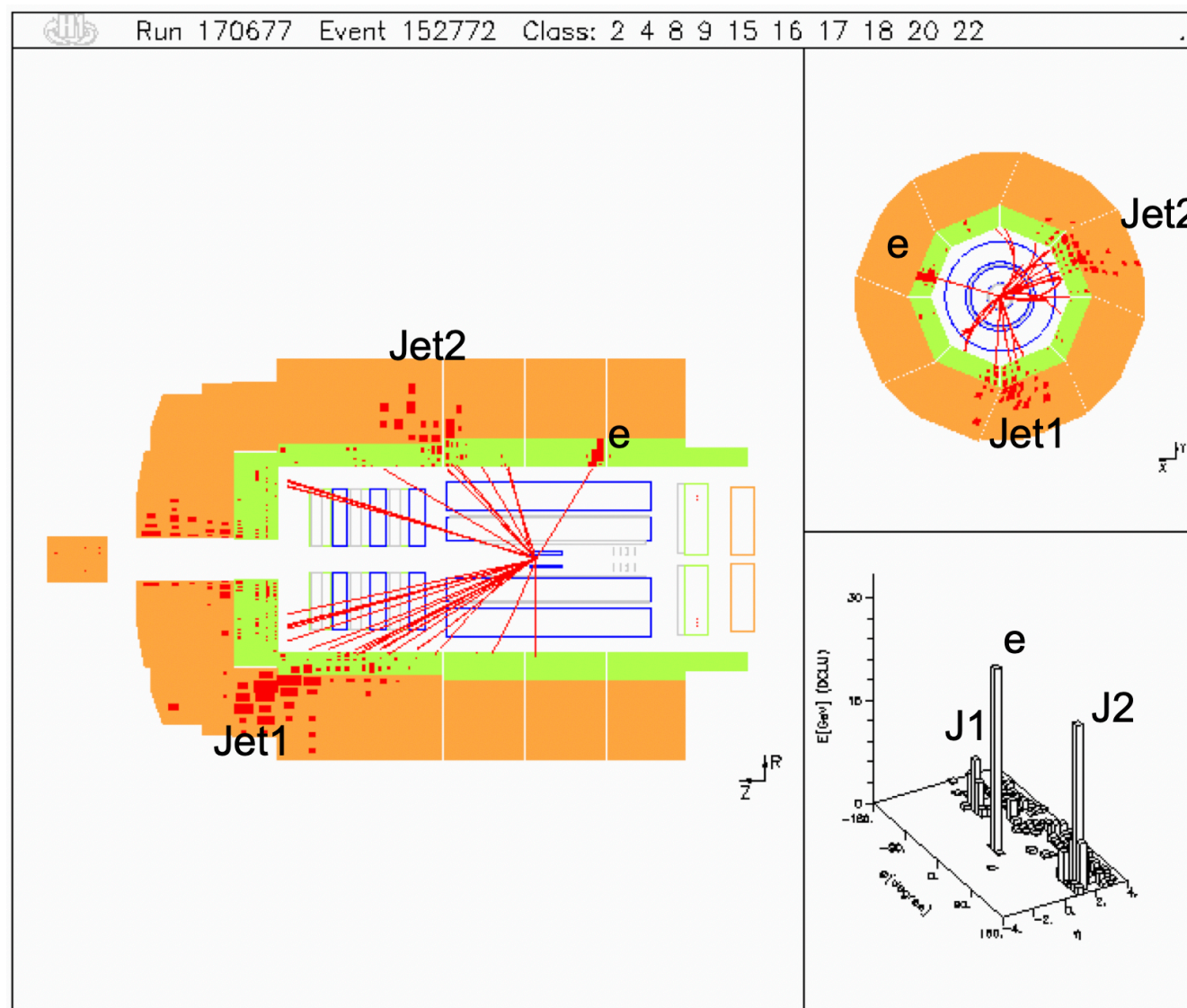
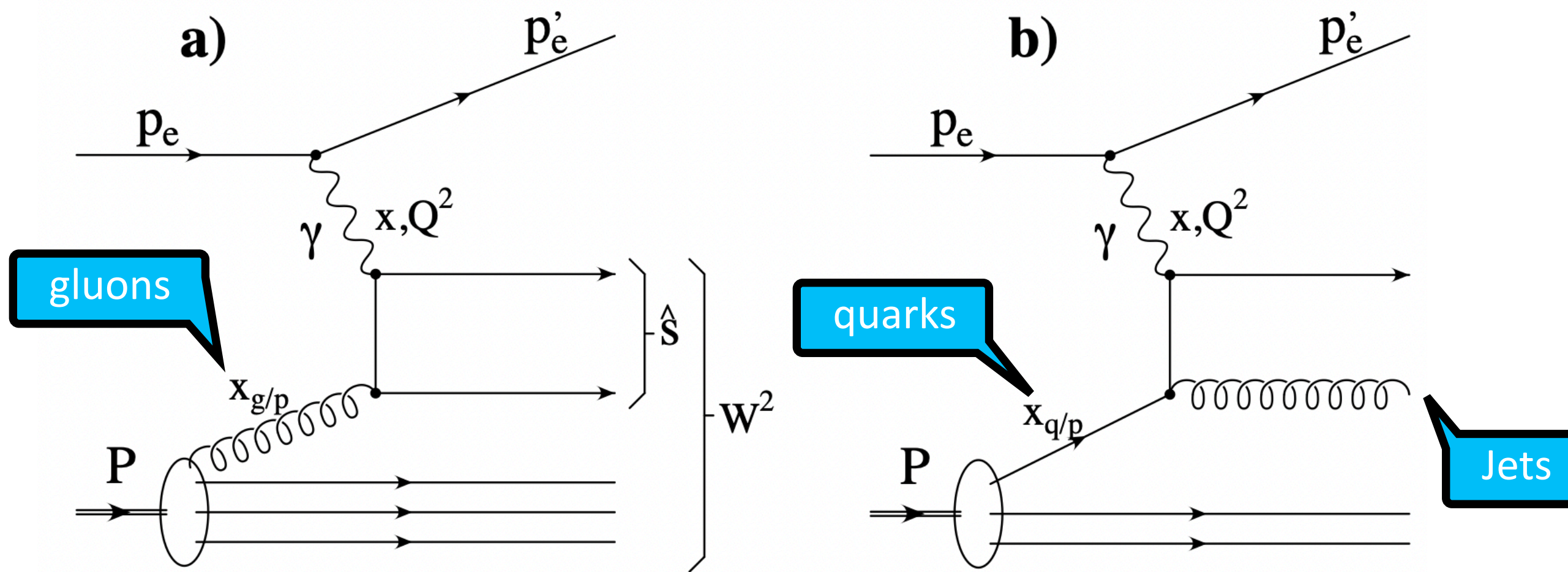
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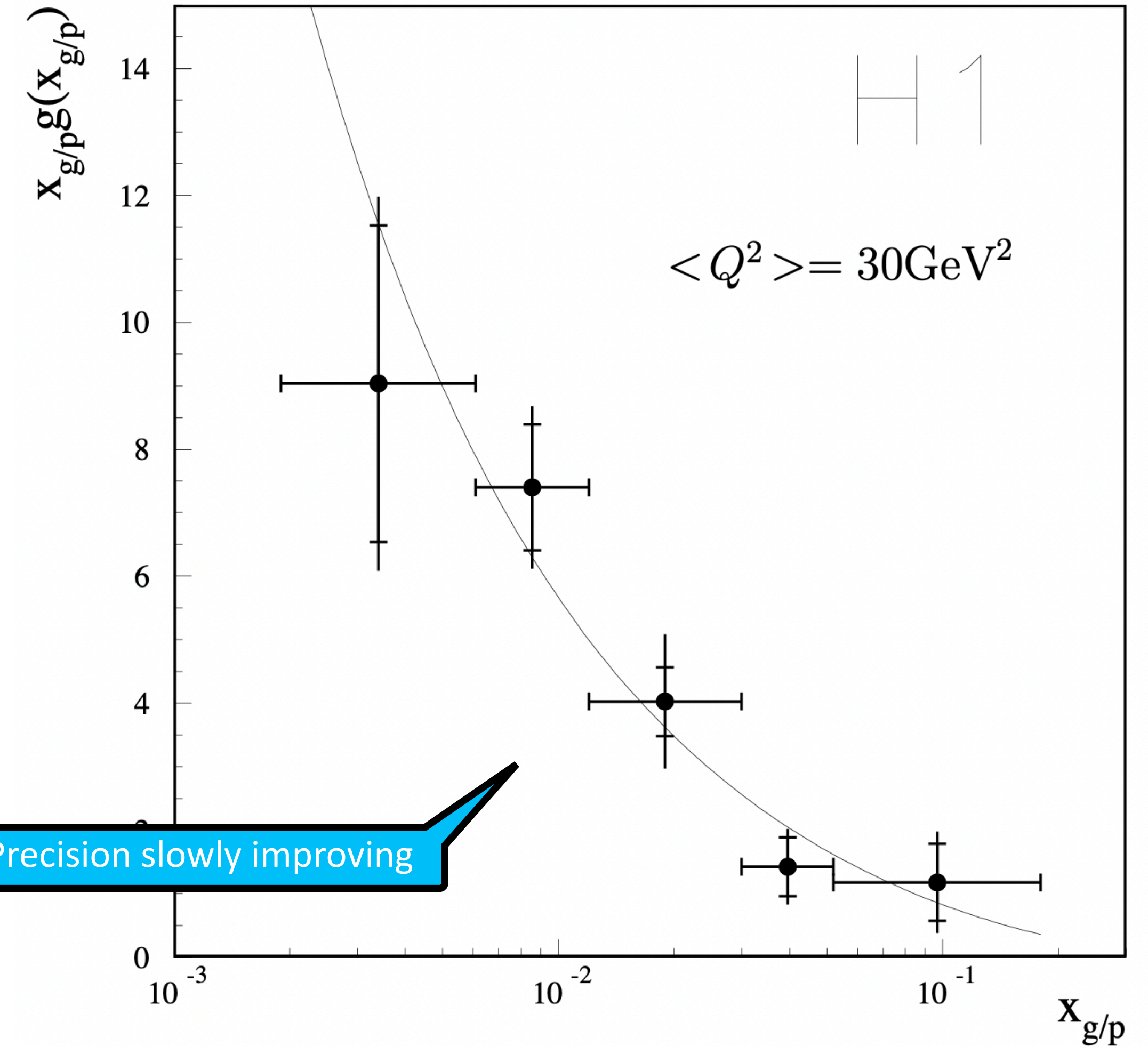
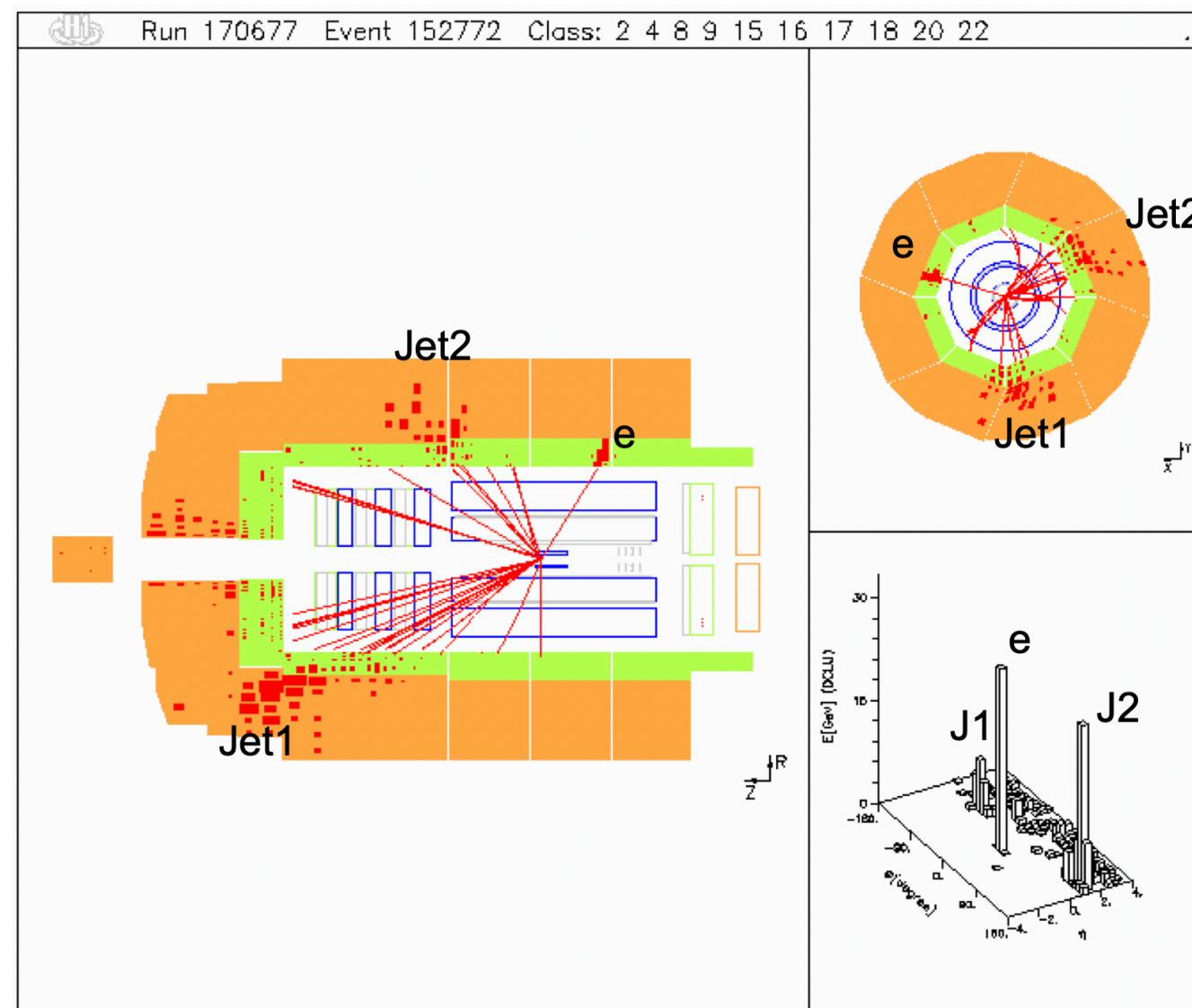
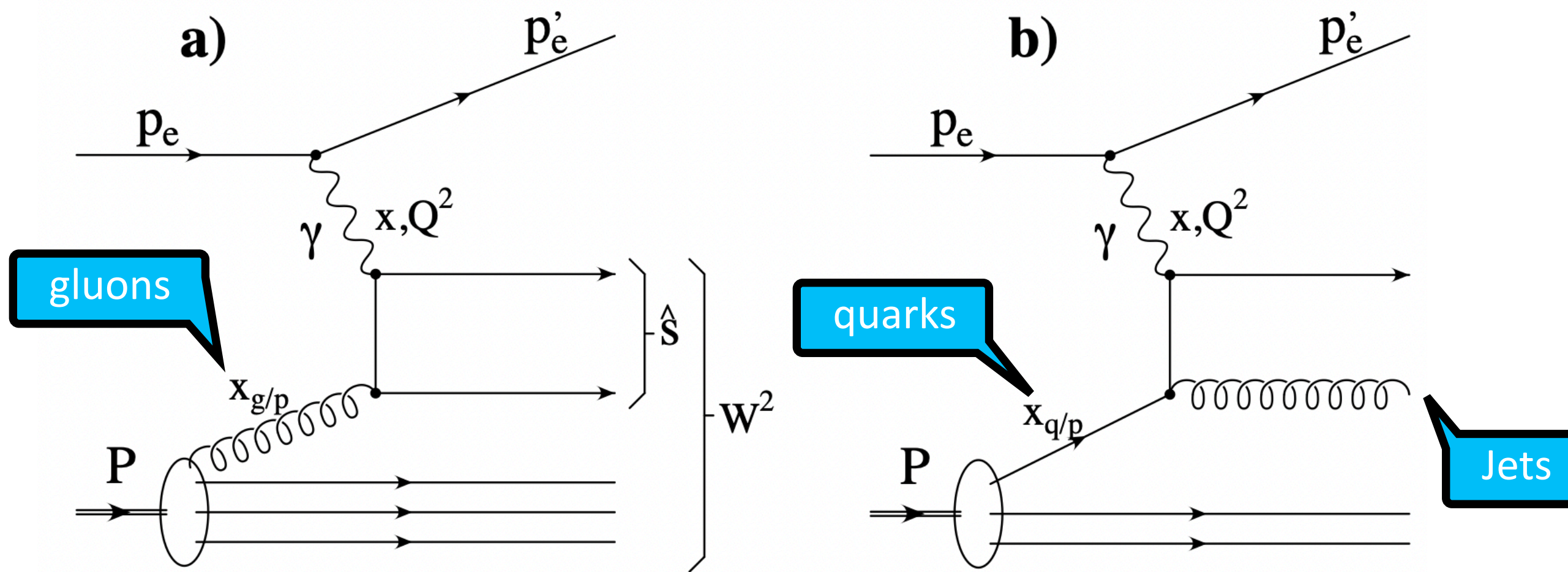
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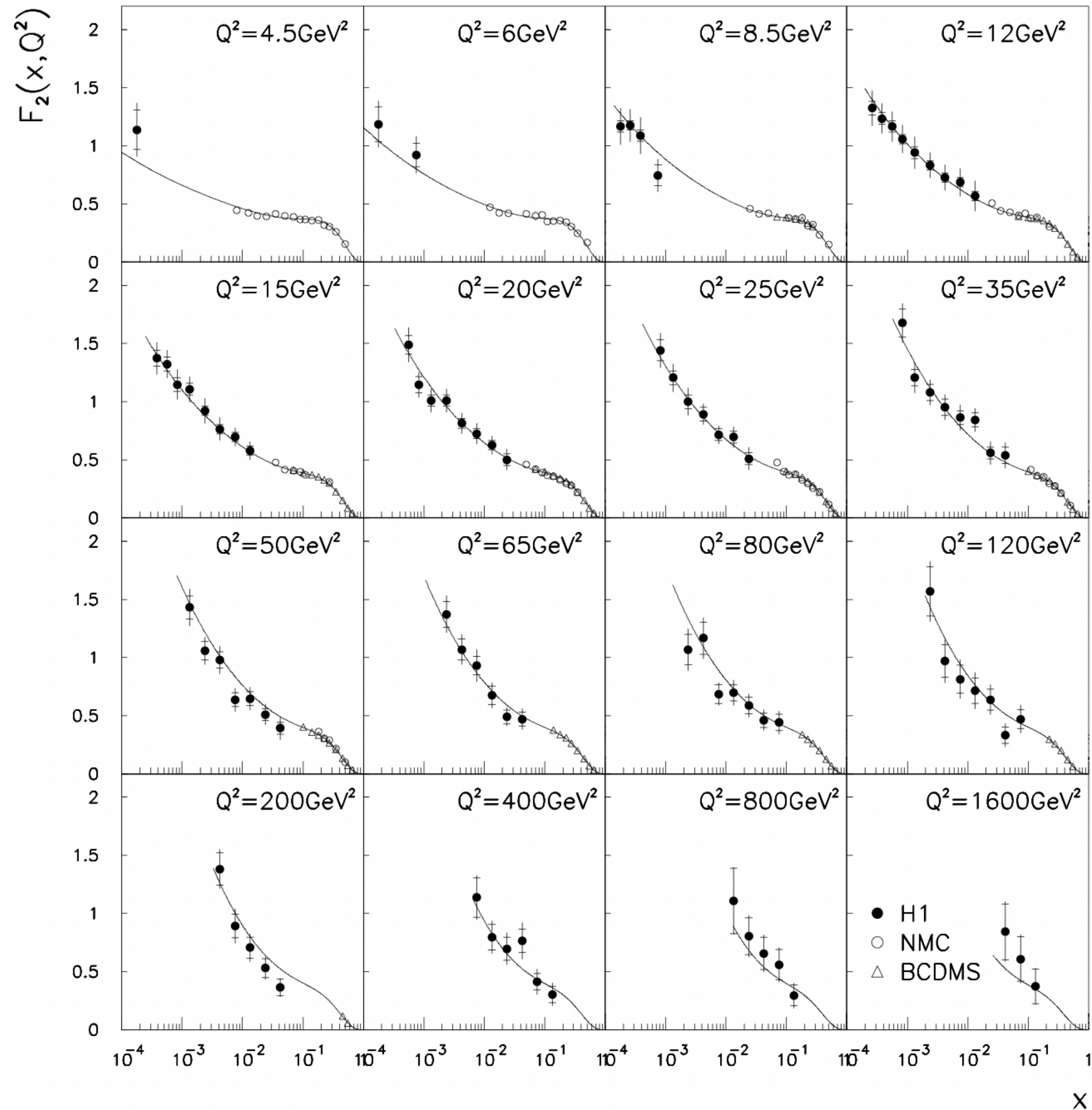
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Back to inclusive measurements: early QCD fits (1995)

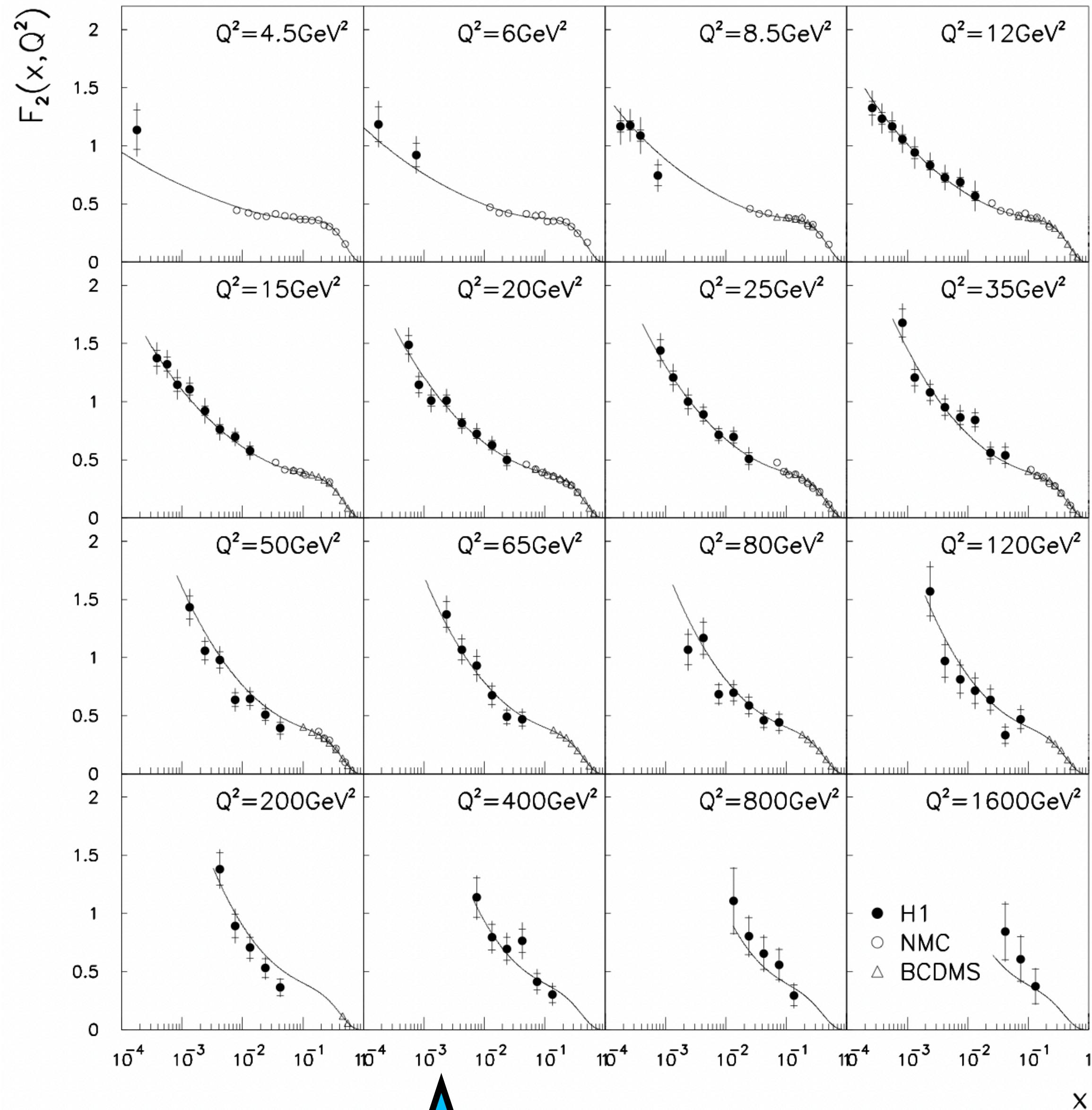
H1, <https://inspirehep.net/literature/395814>



x

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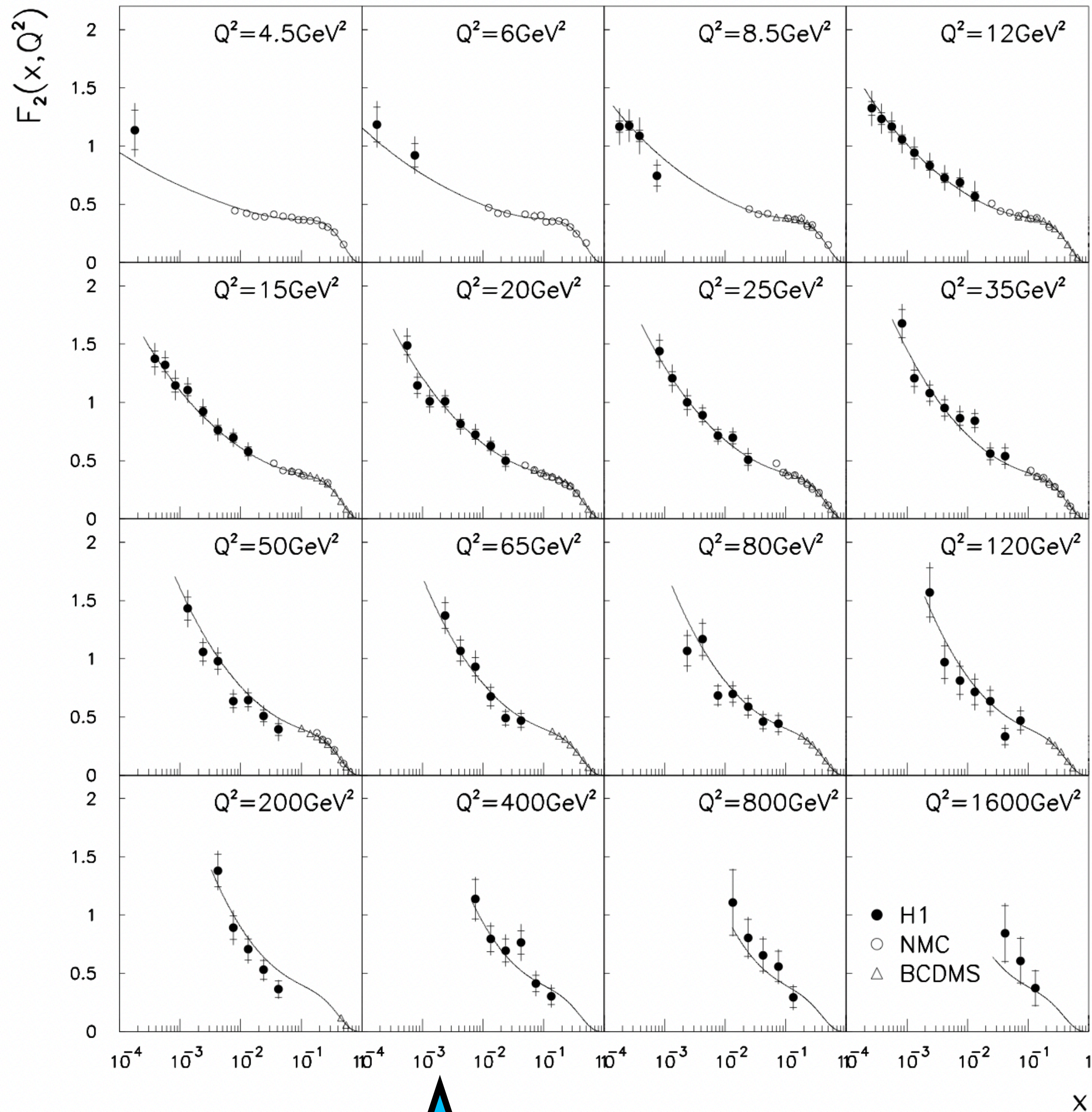
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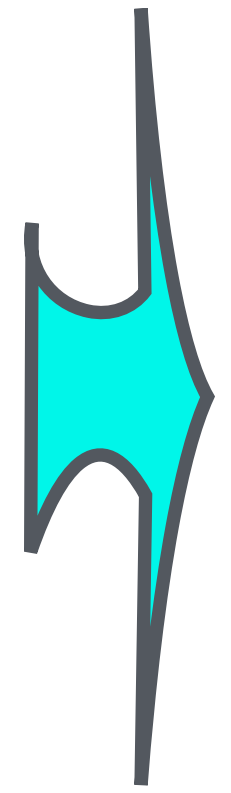
Uncertainties are getting smaller :)

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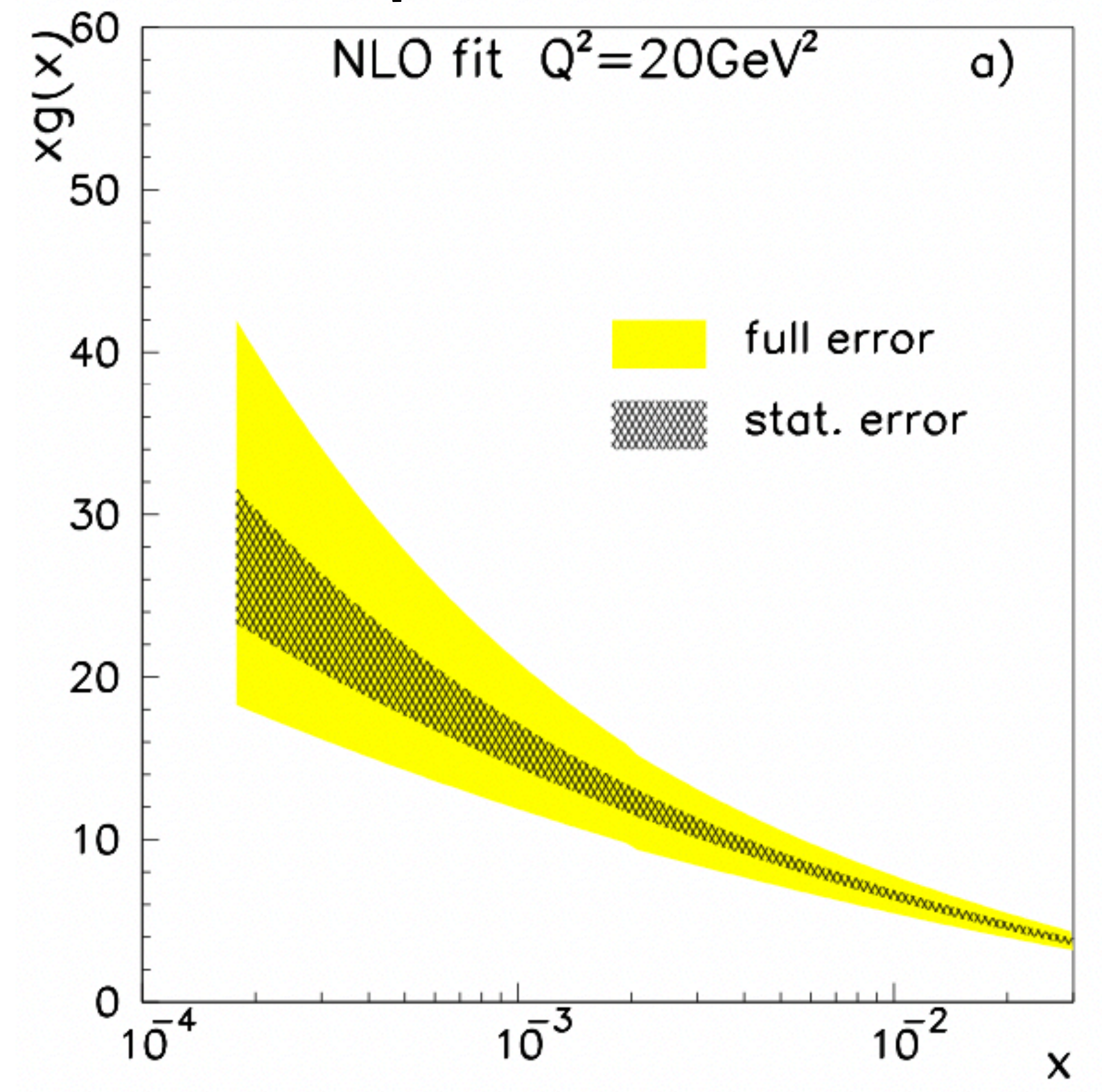
H1, <https://inspirehep.net/literature/395814>



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NLO fit



The longitudinal structure function (1997)

Once the precision is good enough, one can use the fits to extract F_L

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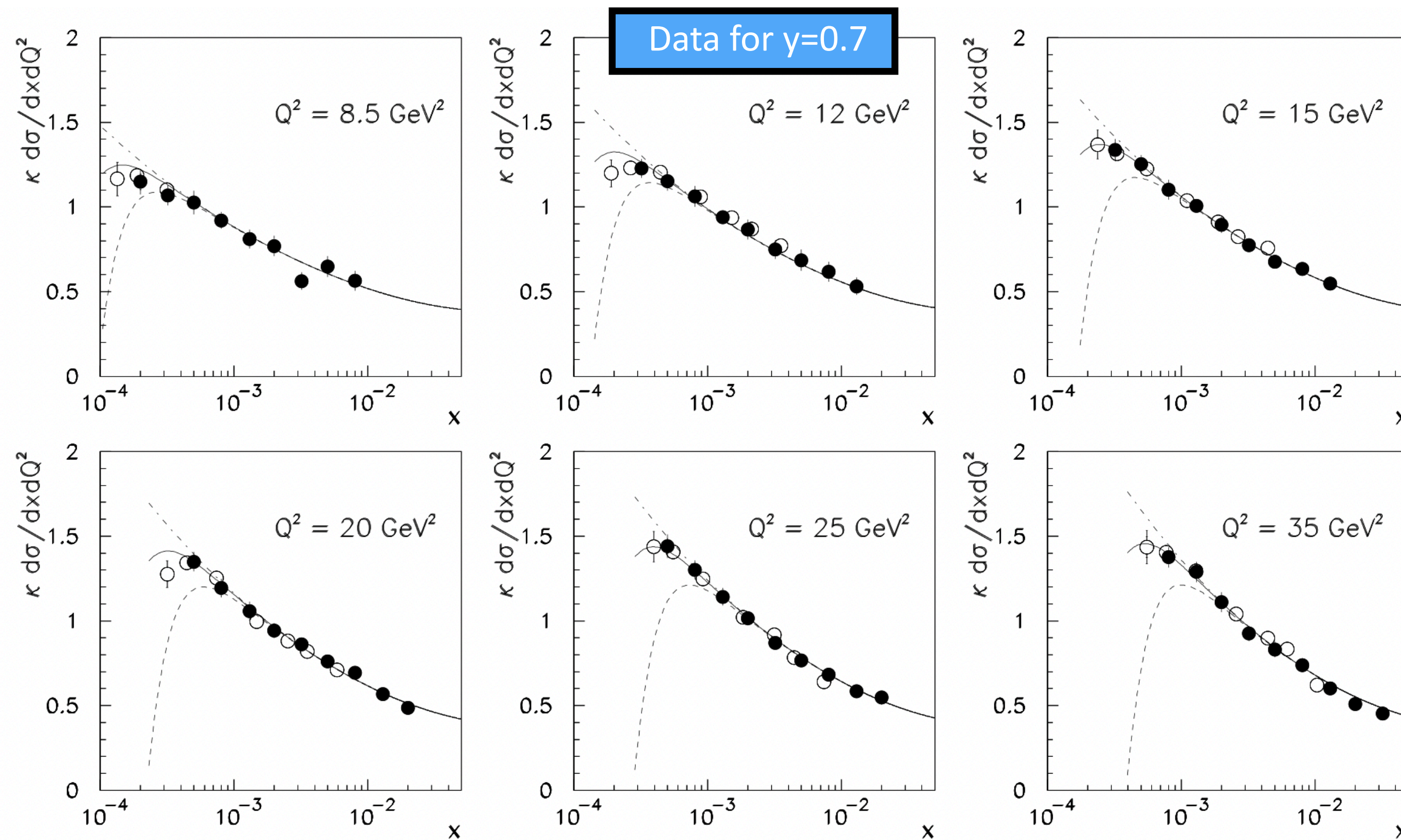
$$R = \frac{F_L}{F_2 - F_L} = \frac{\sigma_L}{\sigma_T}$$

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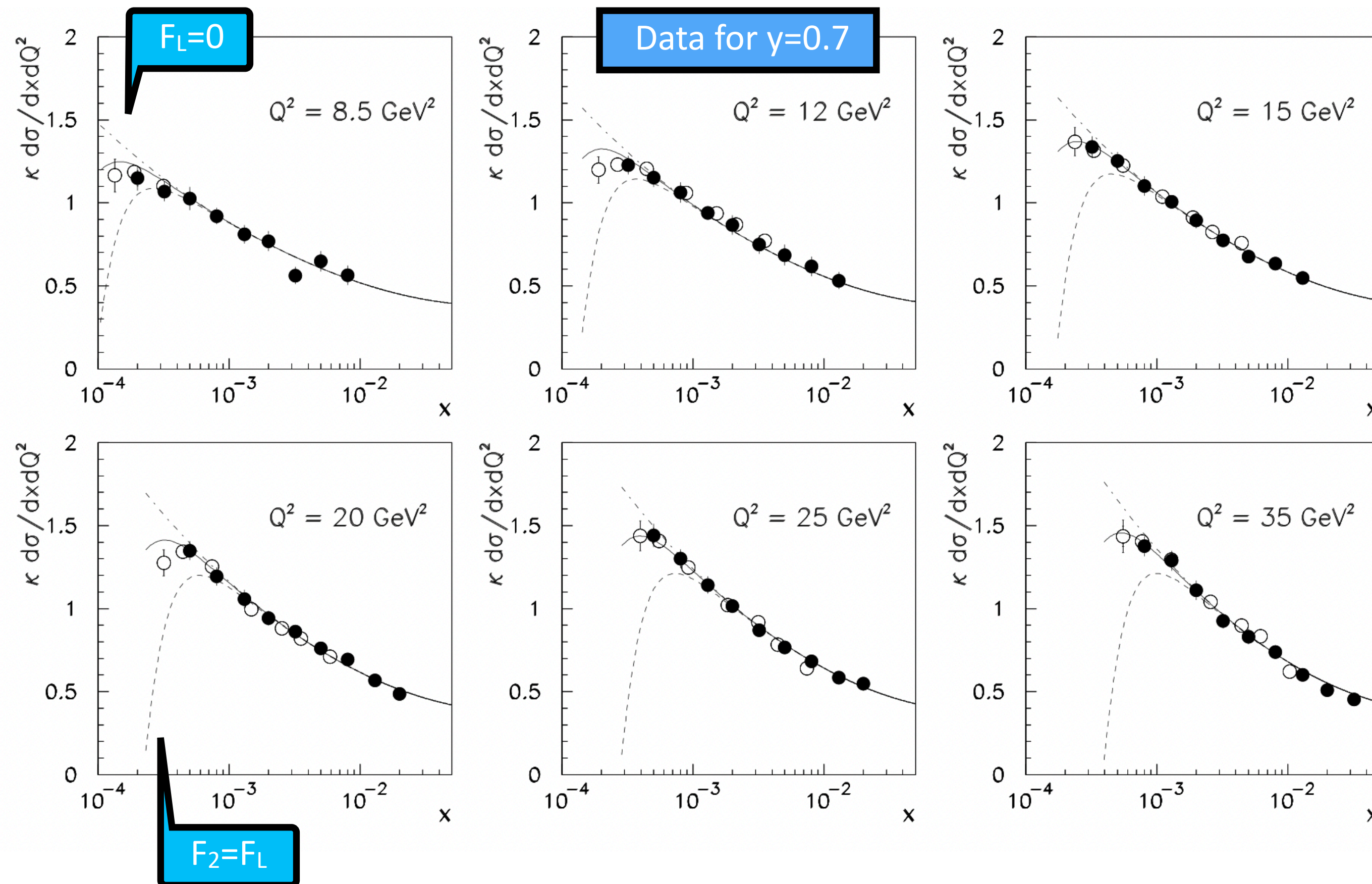


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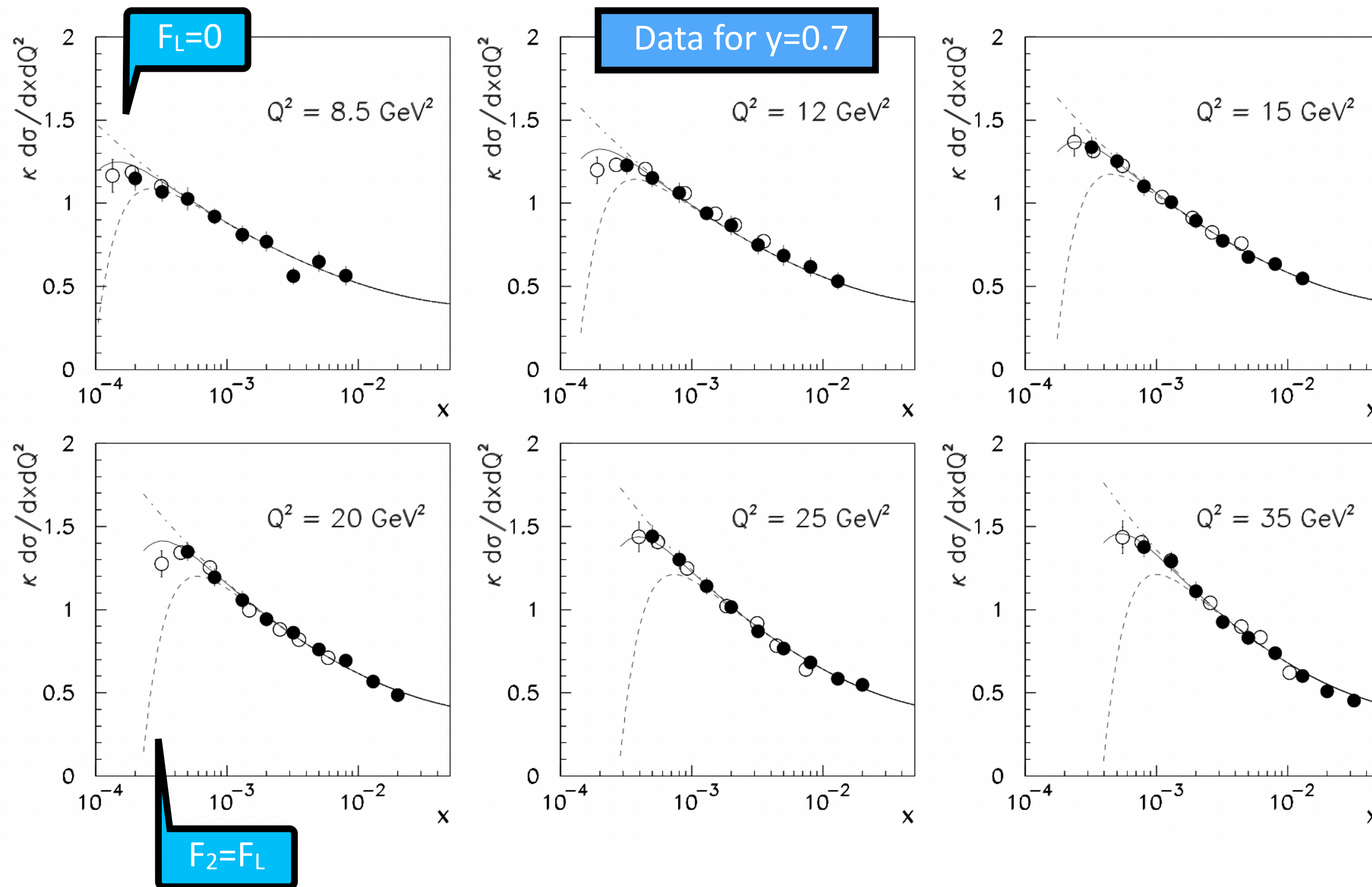


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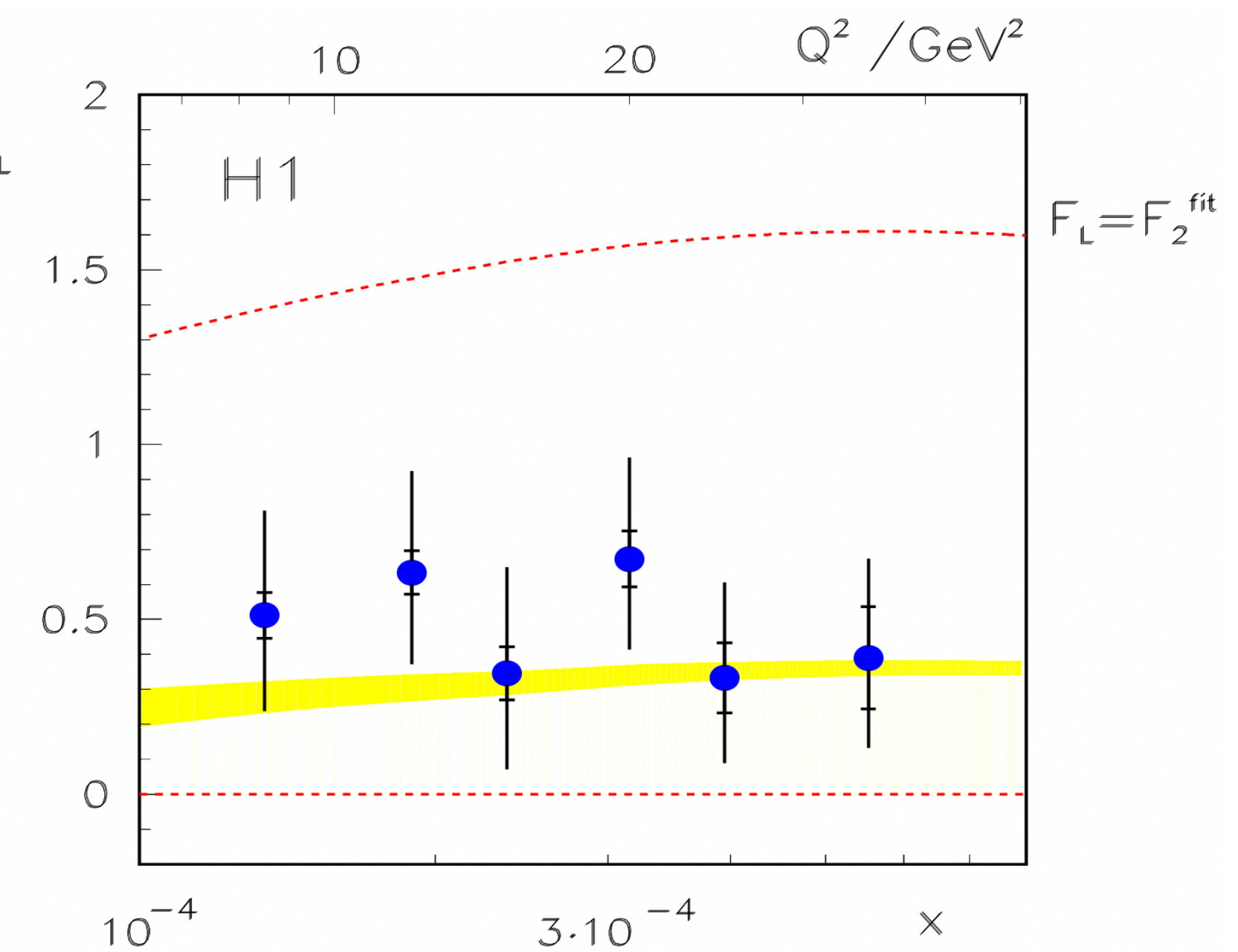
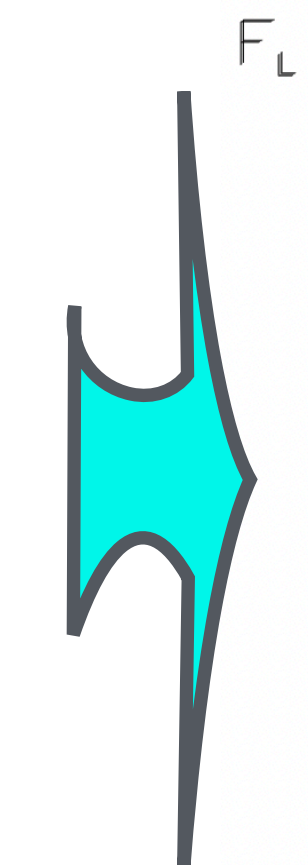
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$$R = \frac{F_L}{F_2 - F_L} = \frac{\sigma_L}{\sigma_T}$$



Measure F_2 at low y , use fits to get it at $y=0.7$ and get F_L

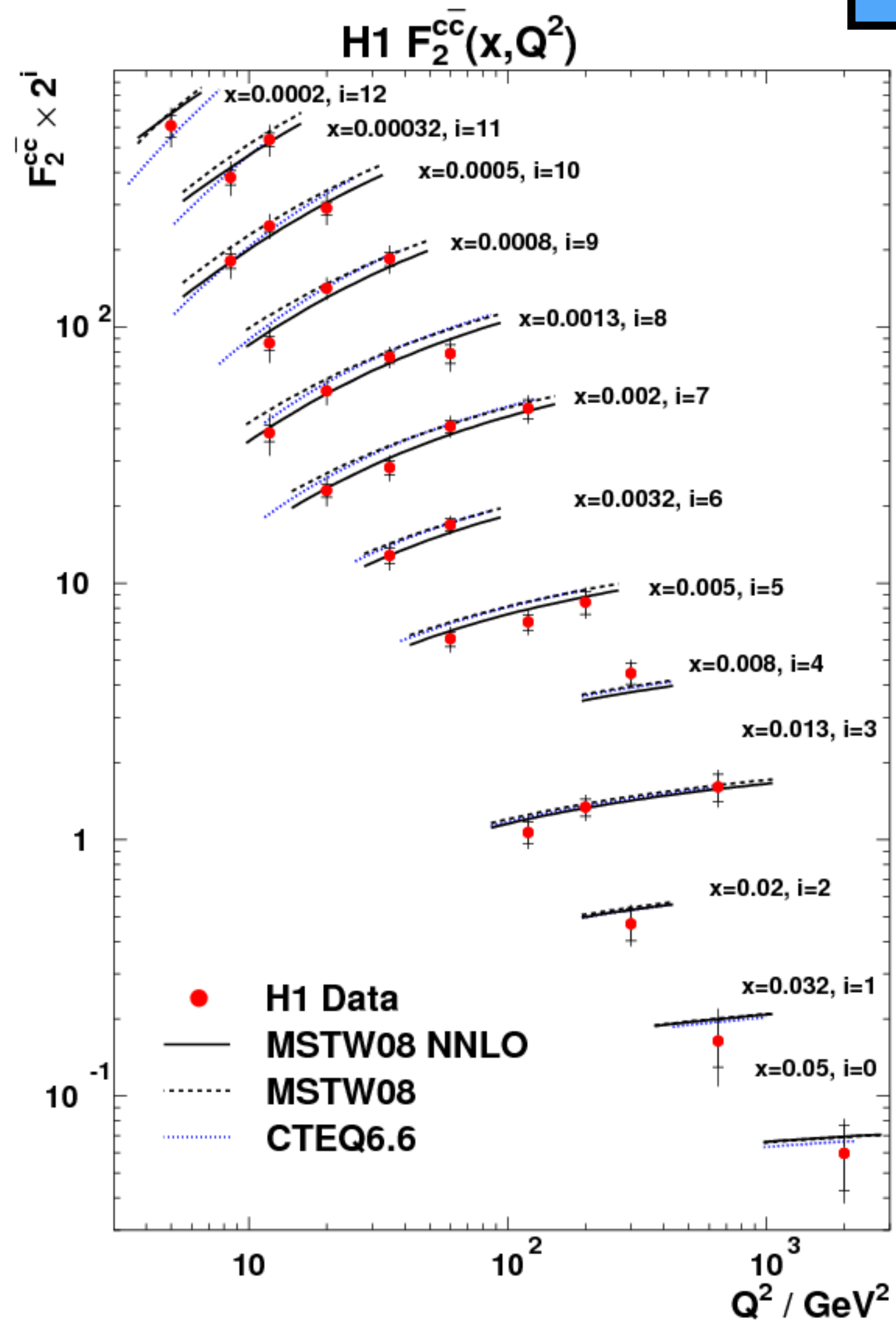


Heavy-quark structure functions (2010)

Use the longer lifetime of heavy flavour hadrons and precise tracking from silicon detectors to select charm or beauty initiated events

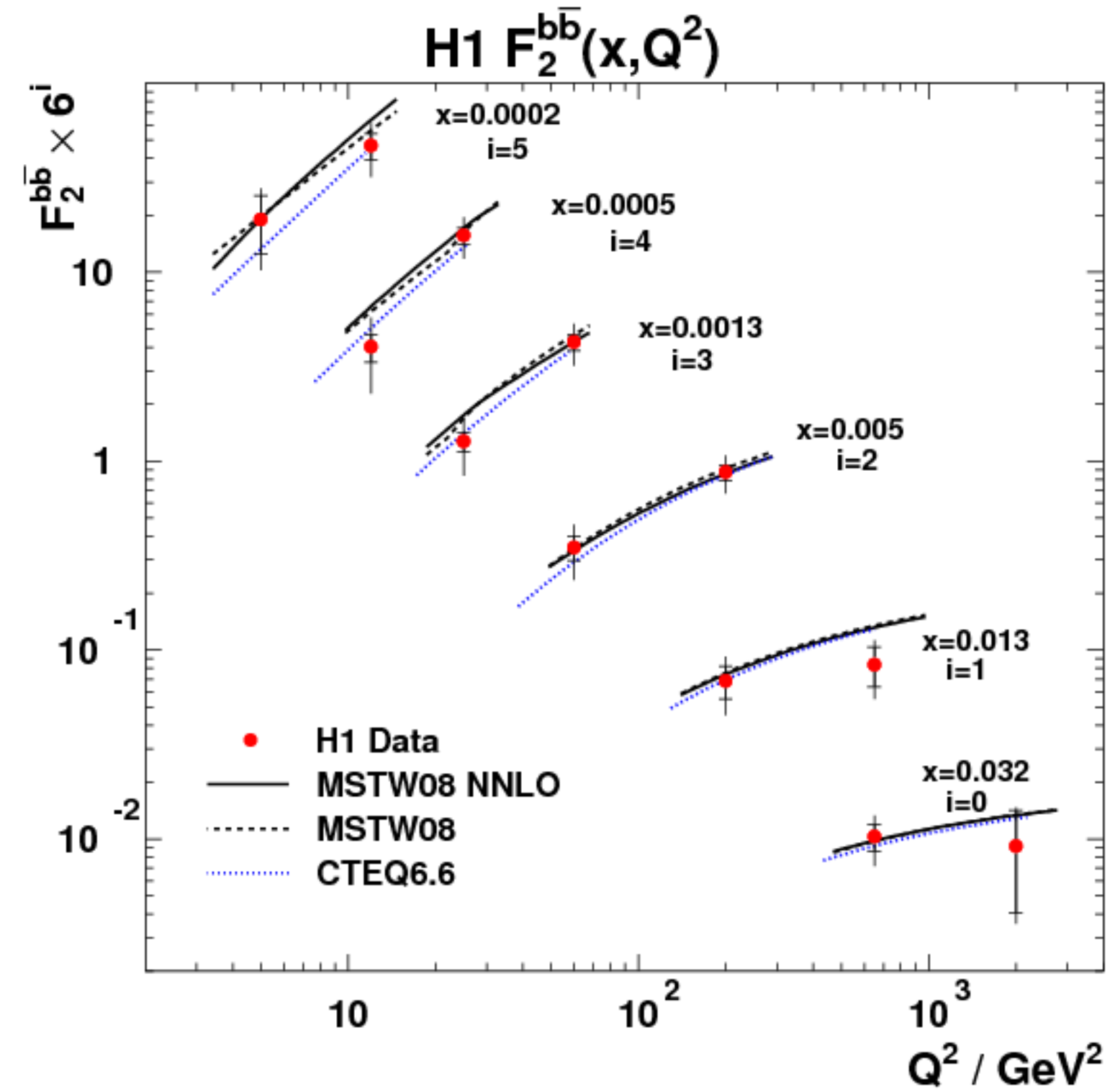
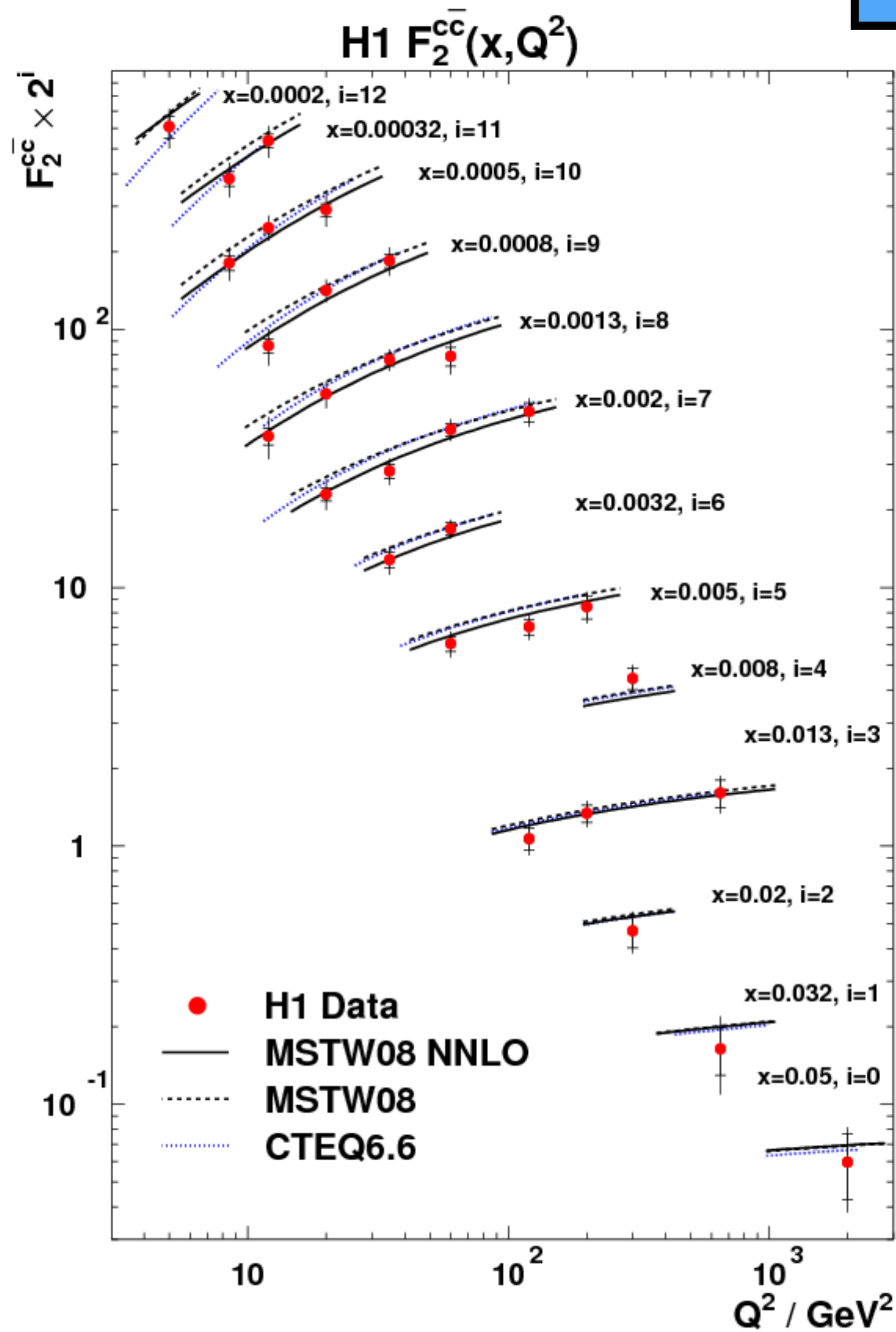
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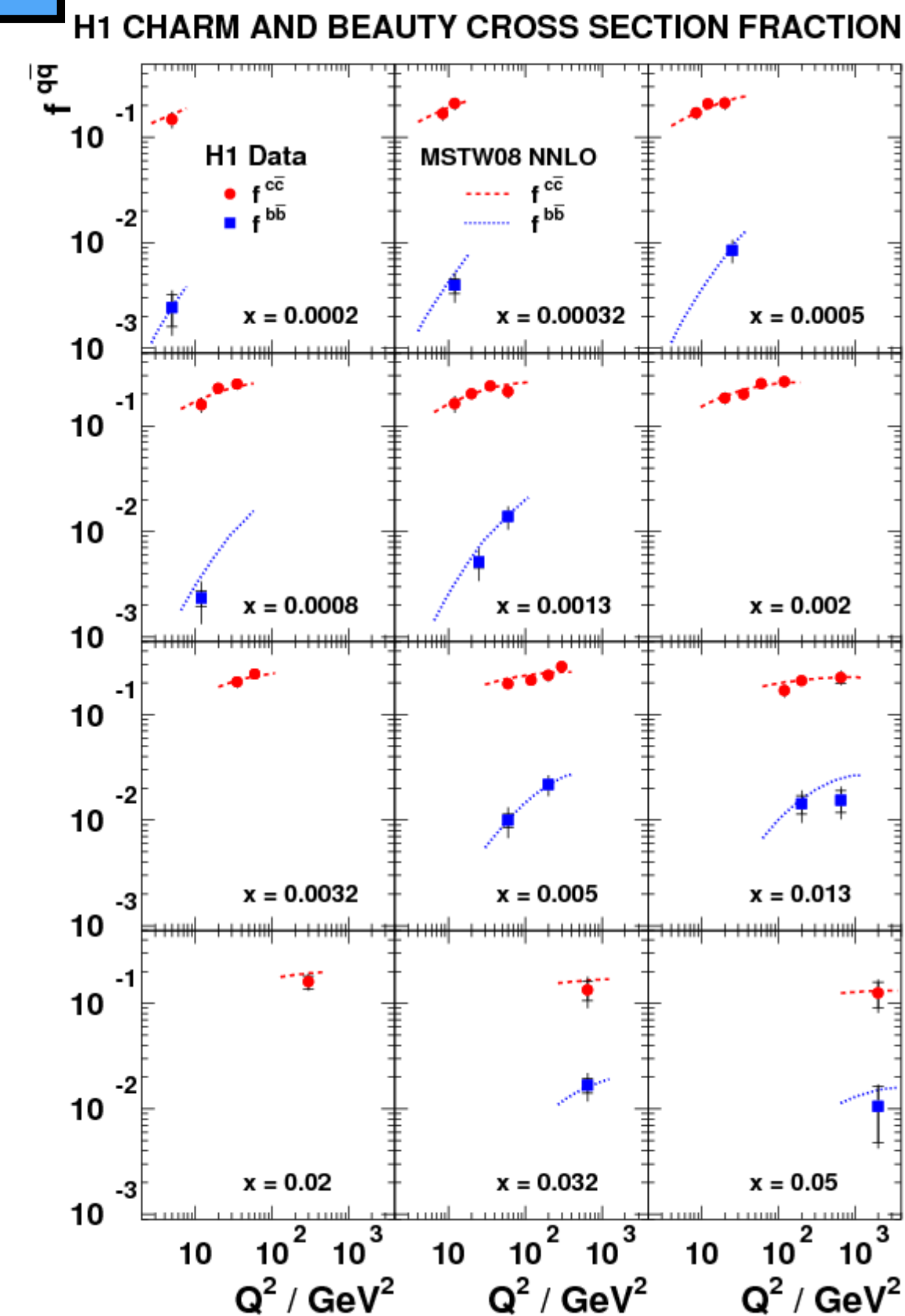
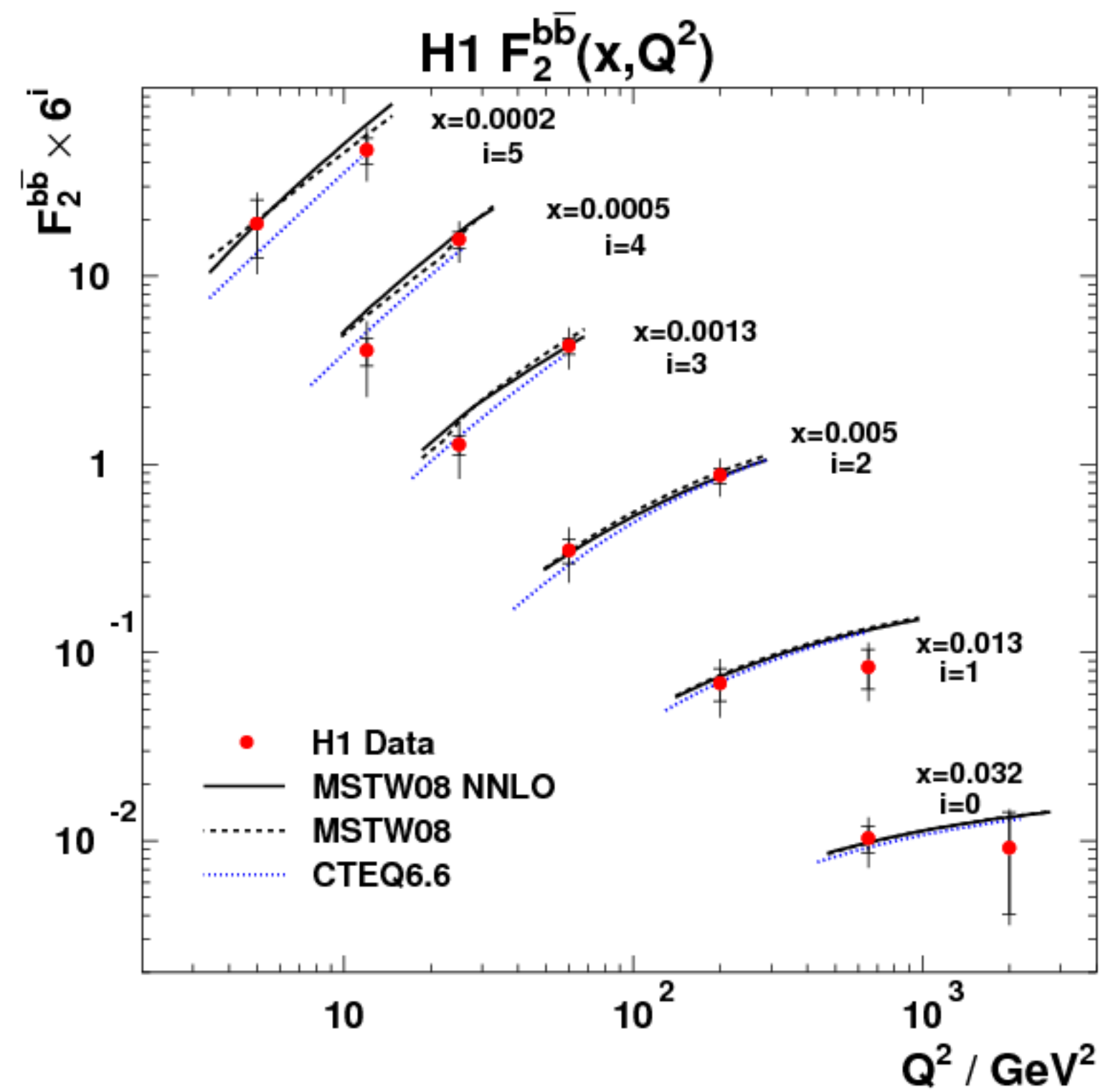
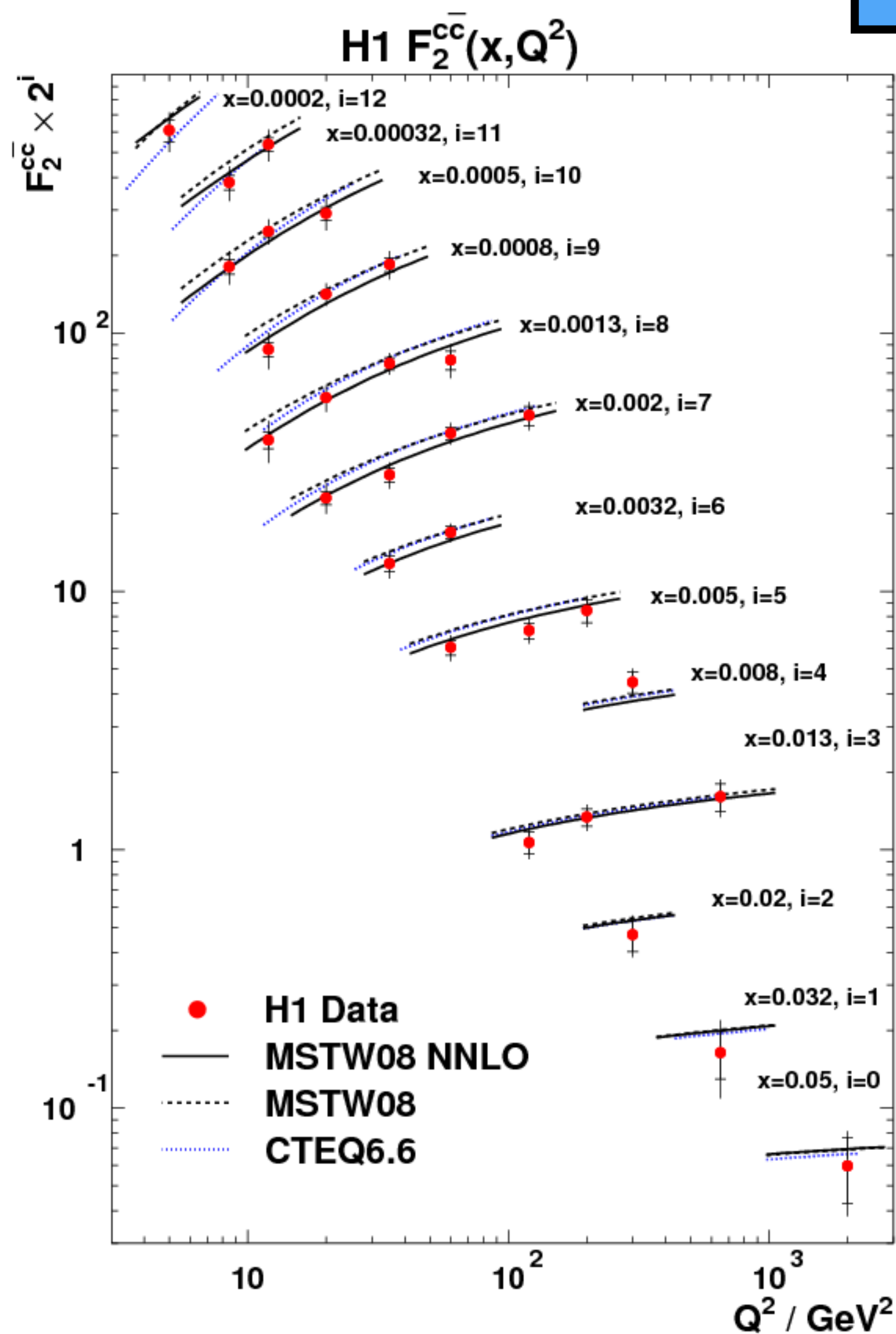
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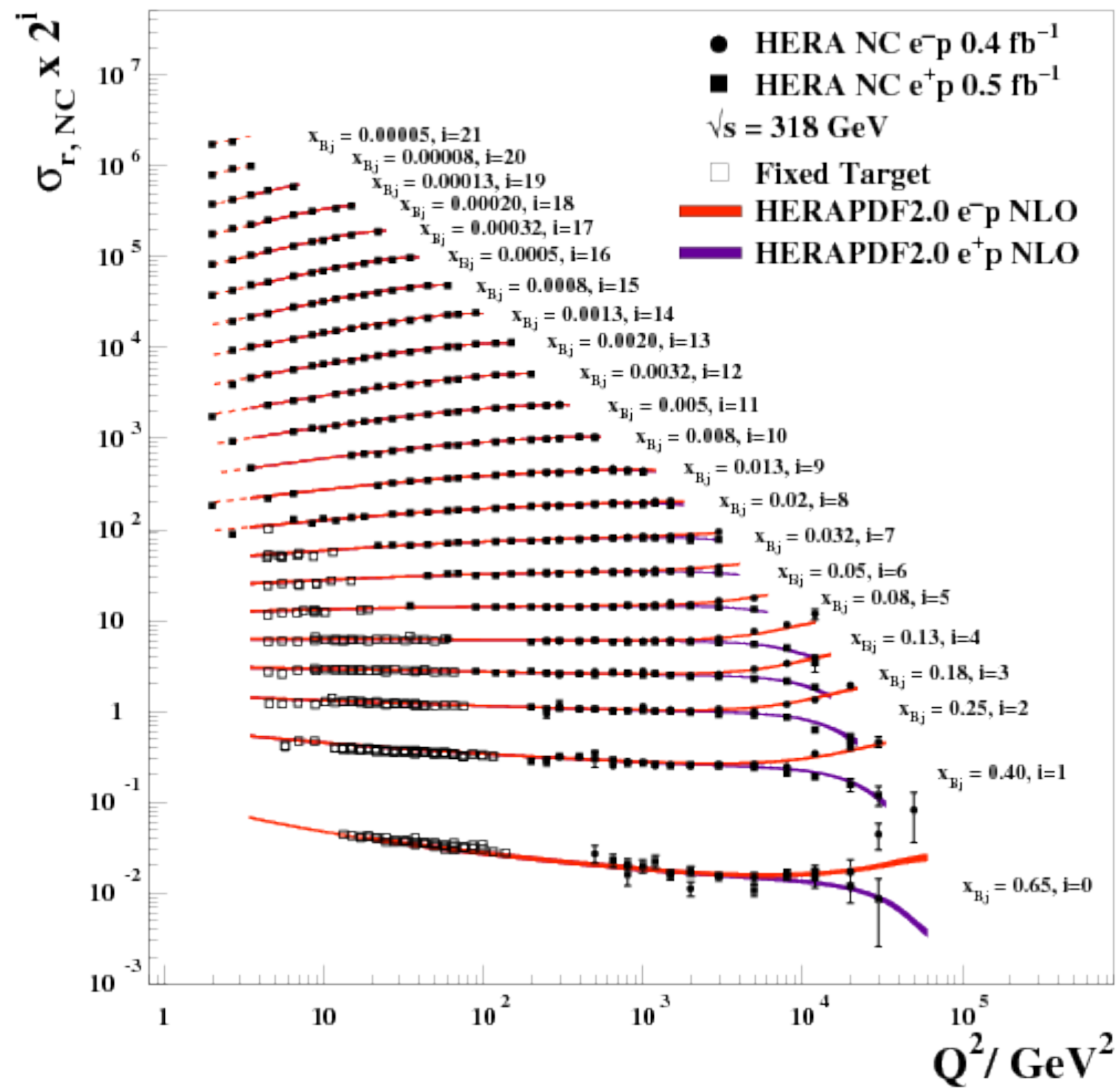
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$$\sigma_{r,NC}^{\pm} = \frac{d^2\sigma_{NC}^{e^{\pm}p}}{dx_{Bj}dQ^2} \cdot \frac{Q^4 x_{Bj}}{2\pi\alpha^2 Y_+}$$

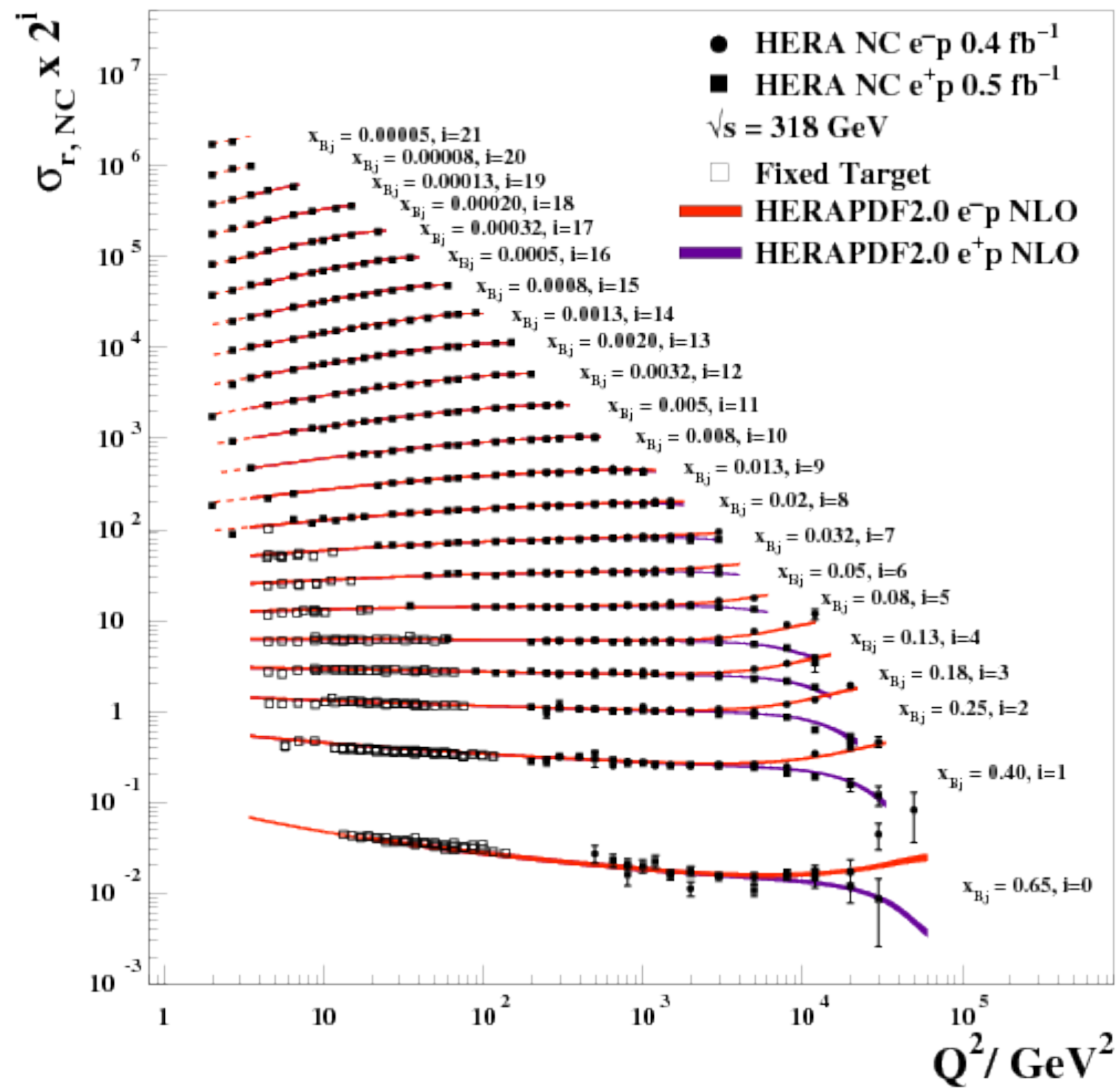
H1 and ZEUS



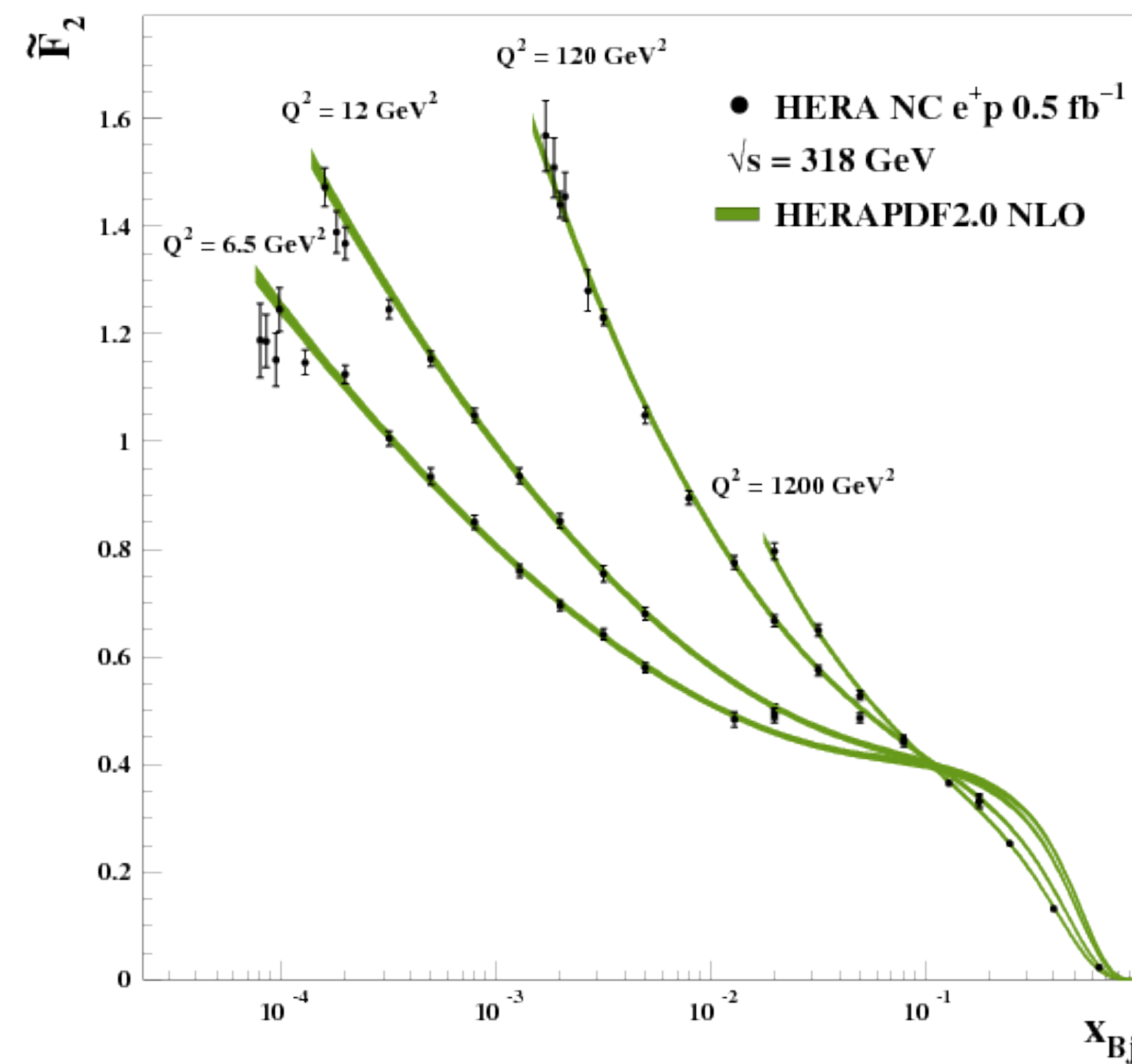
DIS data, state of the art (2015)

$$\sigma_{r,NC}^{\pm} = \frac{d^2\sigma_{NC}^{e^{\pm}p}}{dx_{Bj}dQ^2} \cdot \frac{Q^4 x_{Bj}}{2\pi\alpha^2 Y_{\pm}} = \tilde{F}_2 \mp \frac{Y_-}{Y_+} x \tilde{F}_3 - \frac{y^2}{Y_+} \tilde{F}_L, \quad \tilde{F}_2 = F_2 - \kappa_Z v_e \cdot F_2^{\gamma Z} + \kappa_Z^2 (v_e^2 + a_e^2) \cdot F_2^Z$$

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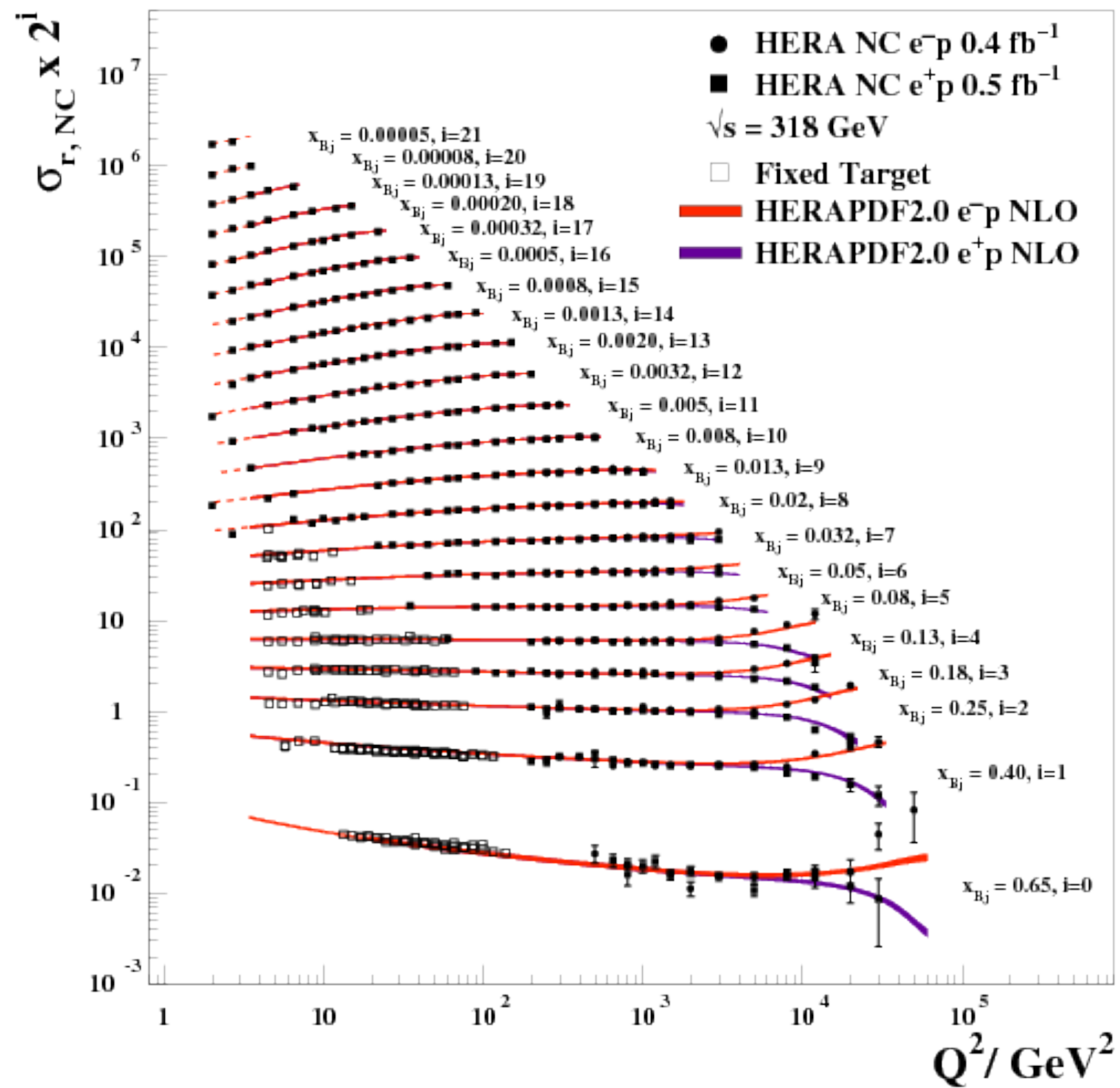
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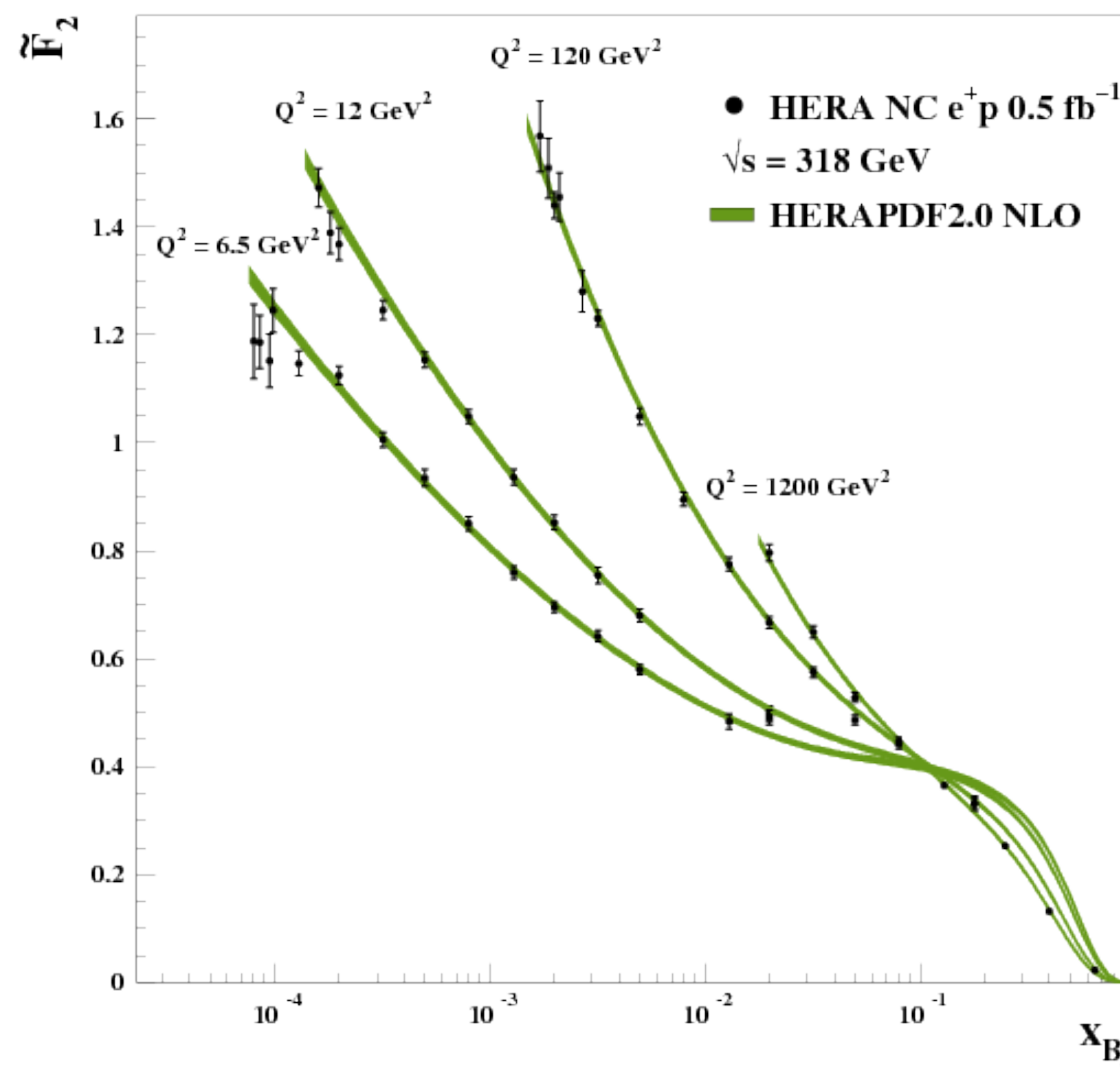
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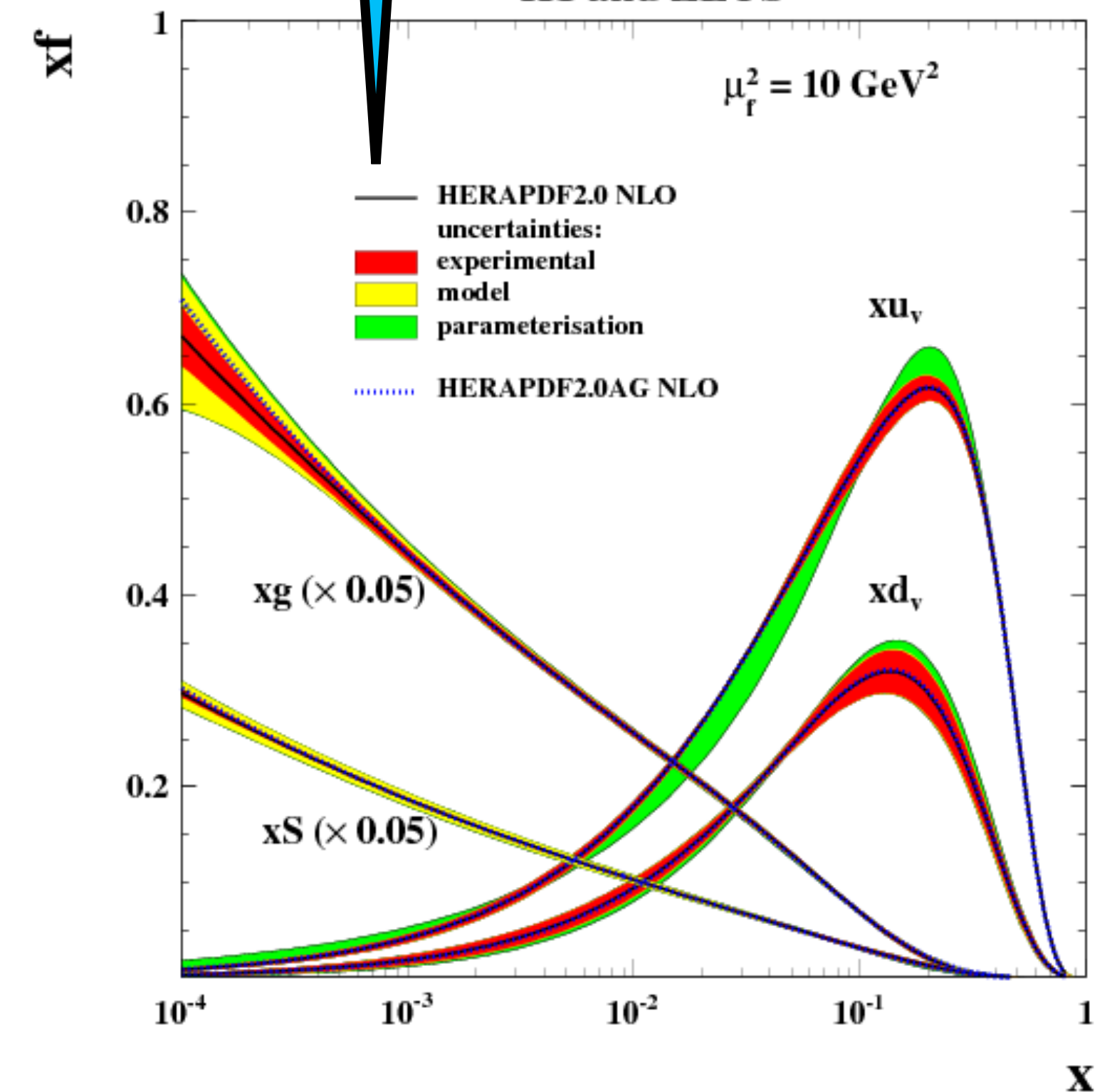


H1 and ZEUS



There also are NNLO fits

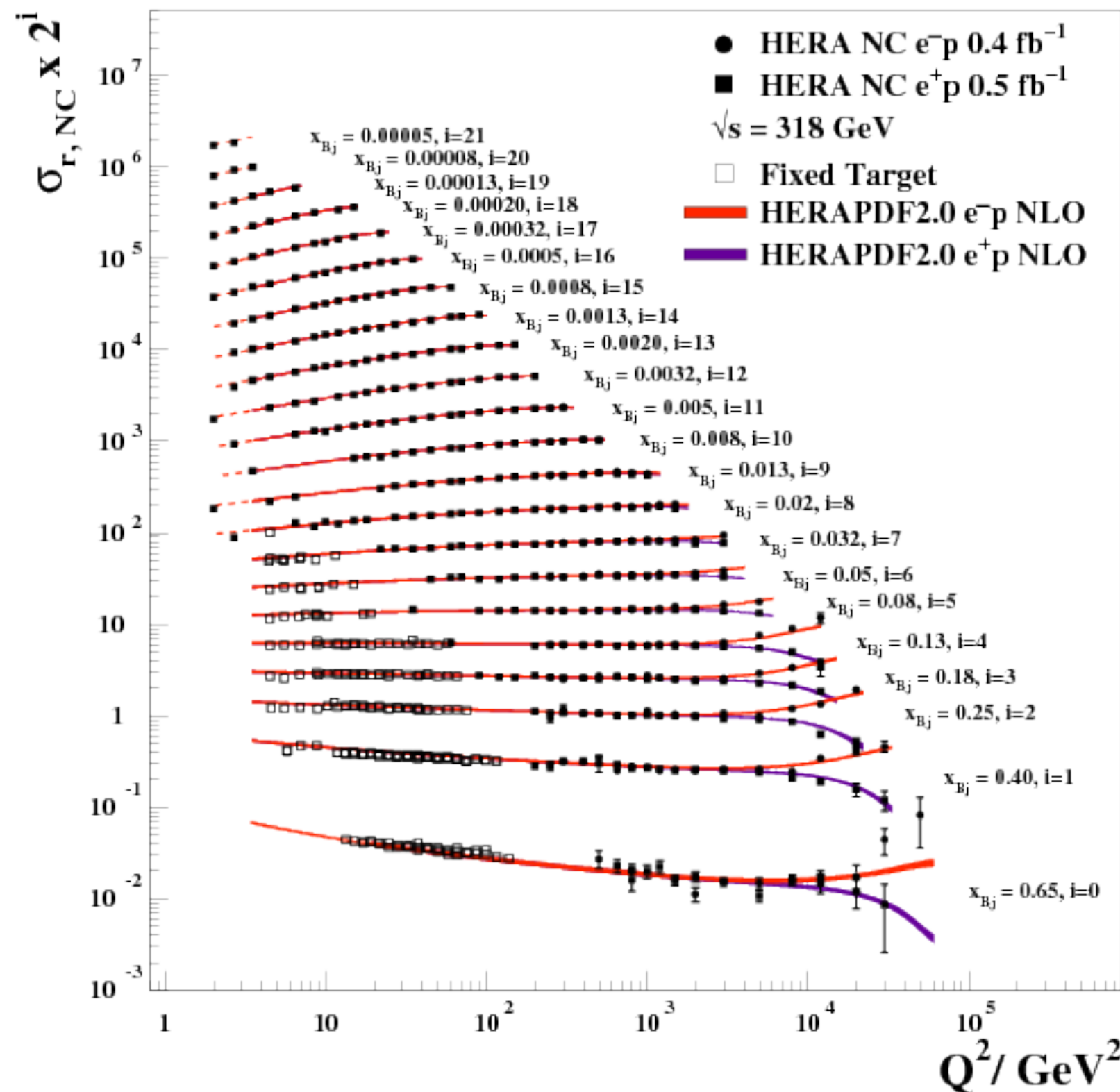
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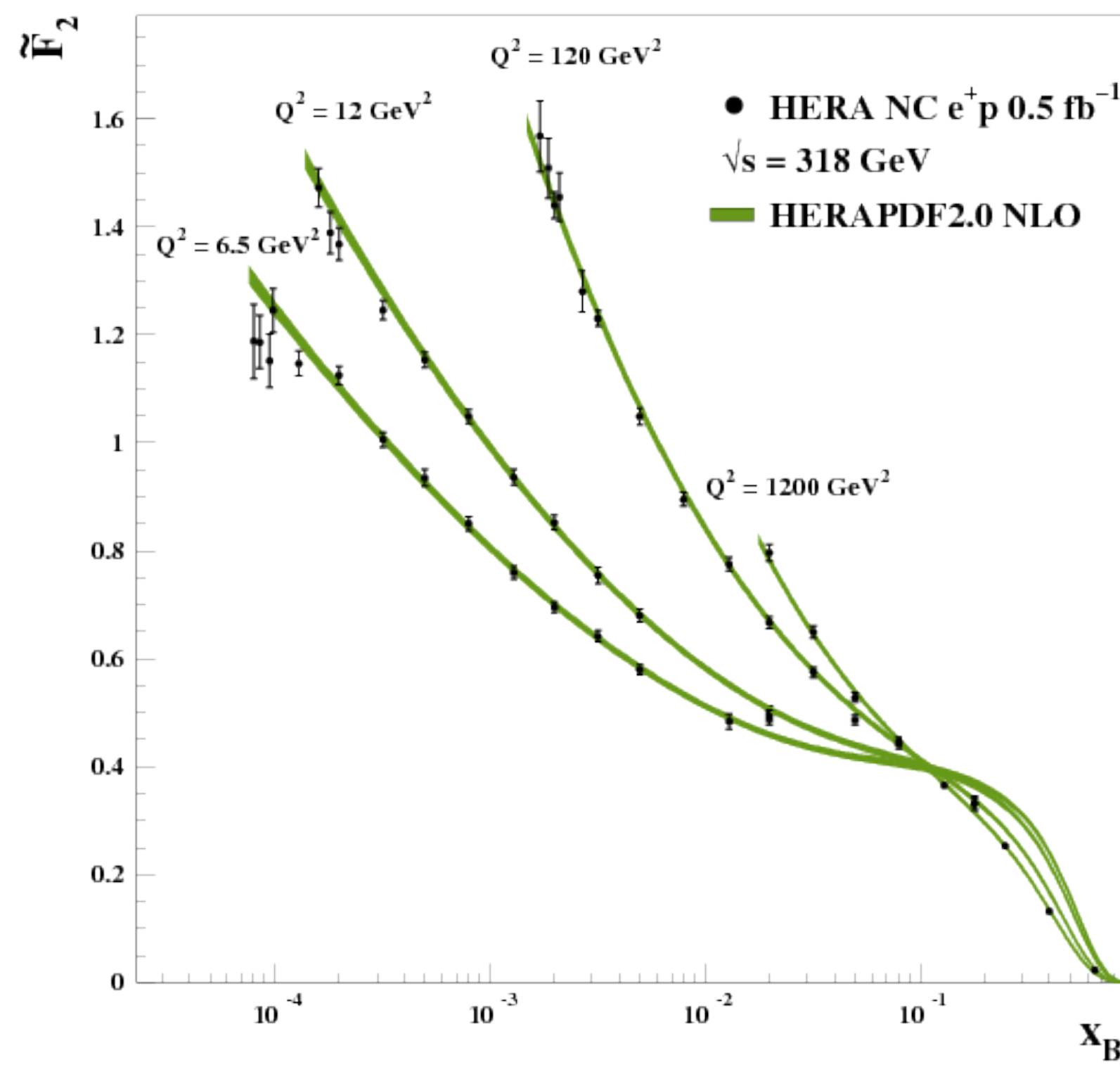
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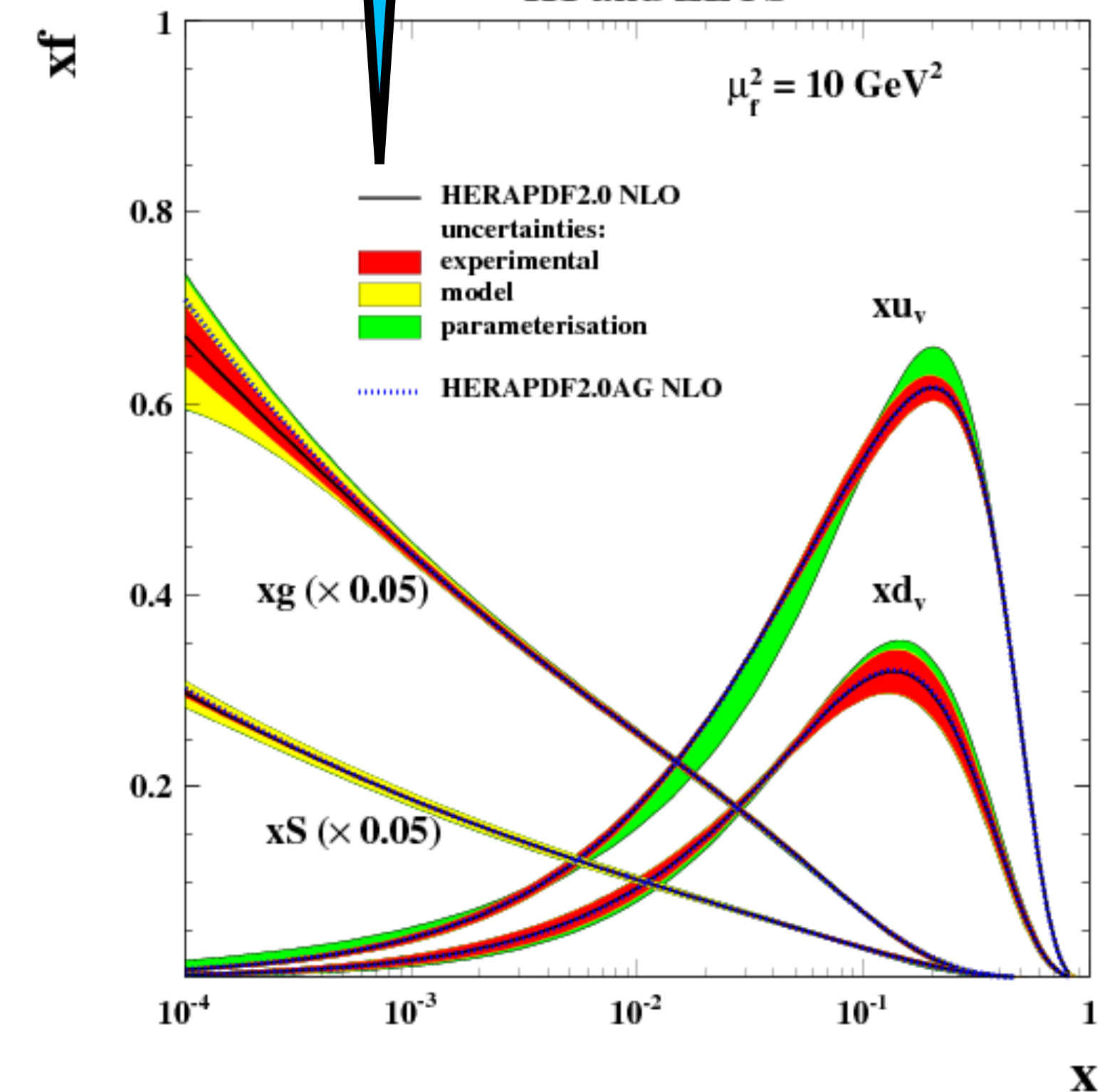


H1 and ZEUS



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H1 and ZEUS



The QCD analysis of HERA data give us a deep and detailed view of the structure of the proton

We are interested in the high-energy limit of QCD

Reminder: small Bjorken- x corresponds to large interaction energy

At this point in time, HERA data show that the structure function grows fast as Bjorken- x decreases.
Let's look at data in more detail and from different perspectives

3

Exploring high-energy QCD: Probing structure functions with colour dipoles at HERA

Growth of the cross section at fixed virtuality (2001)

In the BFKL approach, it is expected that the structure function at fixed virtuality grows as a power law

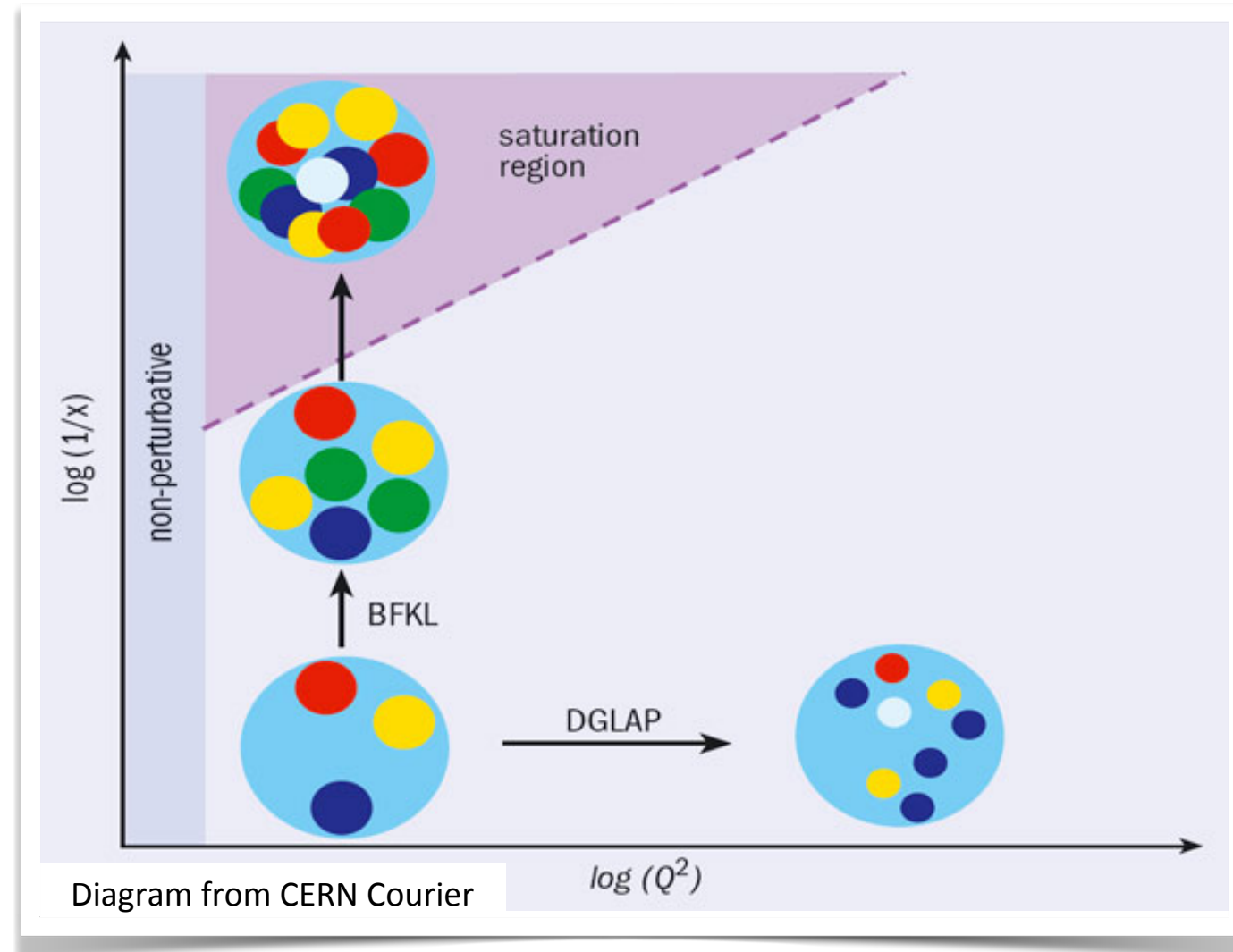
Fix the scale and
evolve in energy

<https://inspirehep.net/literature/561805>

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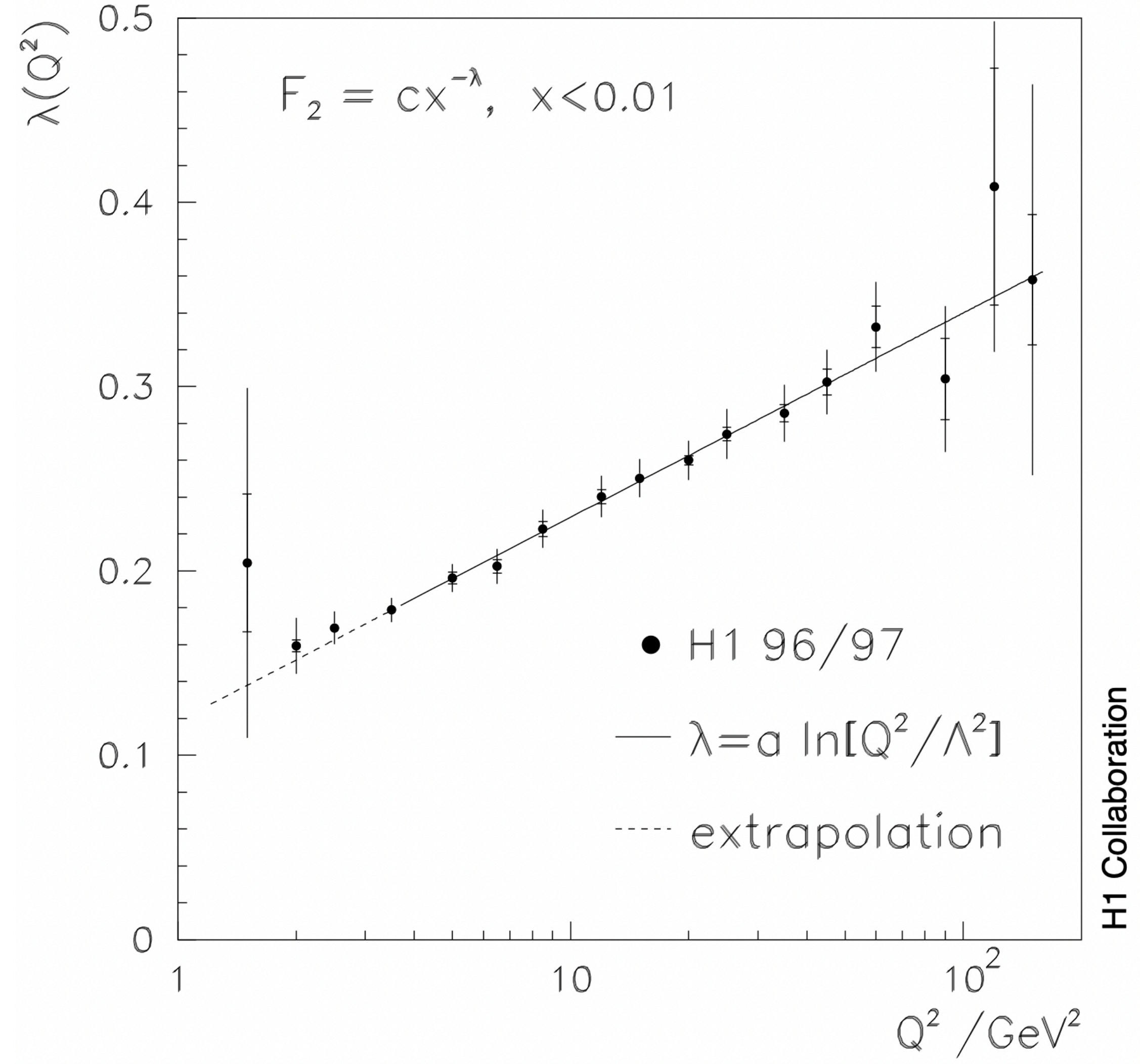
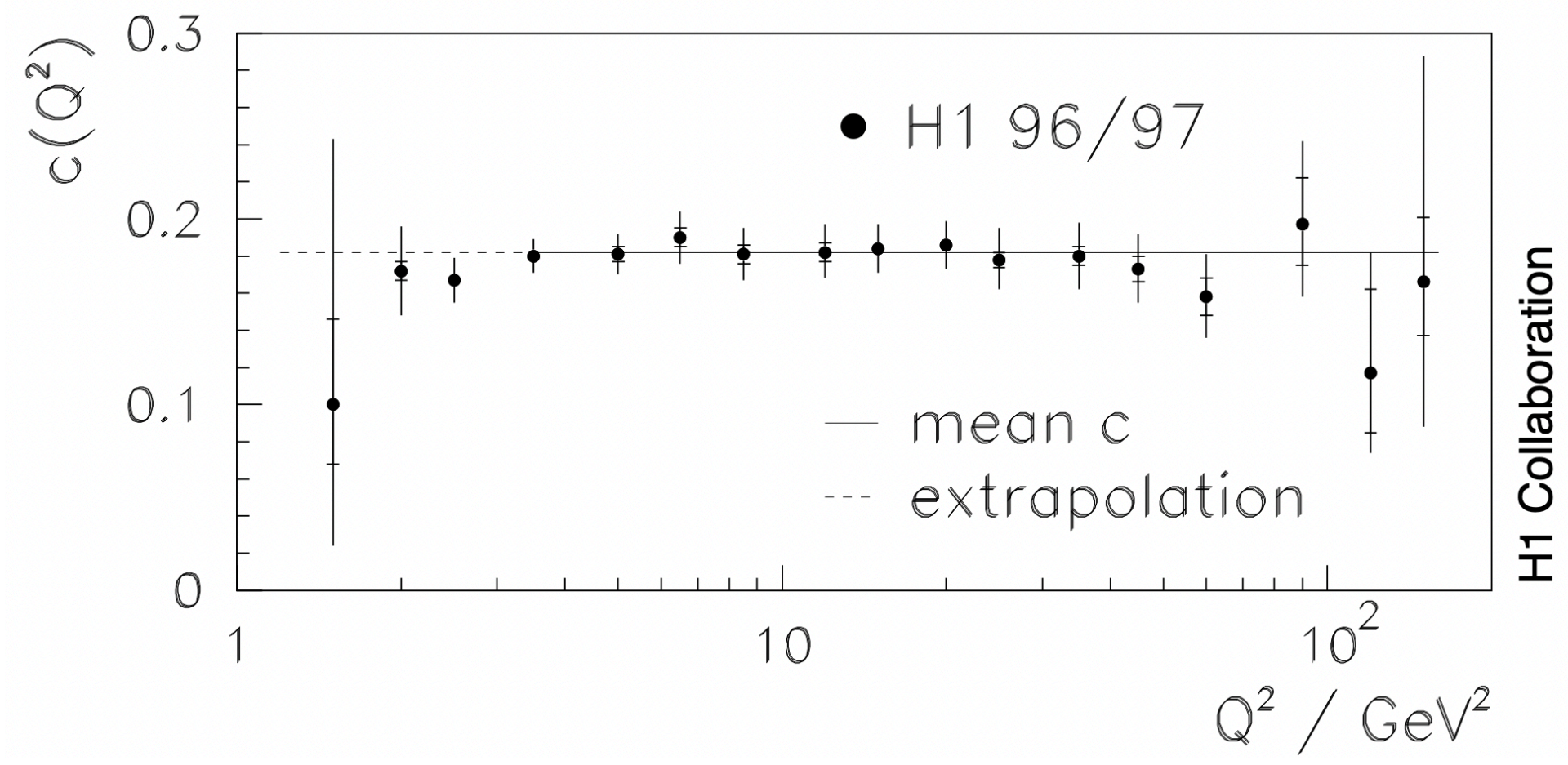
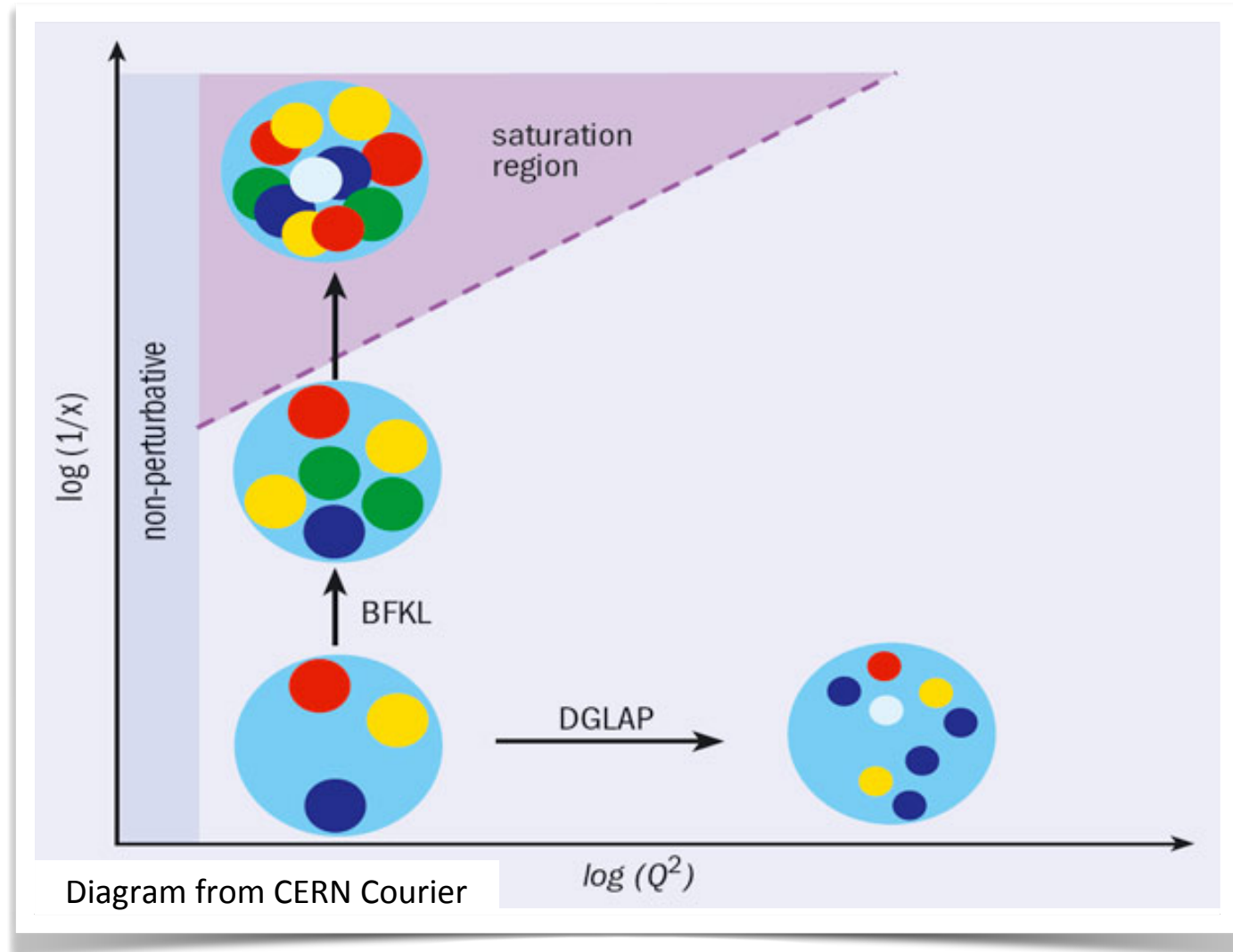


<https://inspirehep.net/literature/561805>

Growth of the cross section at fixed virtuality (2001)

In the BFKL approach, it is expected that the structure function at fixed virtuality grows as a power law

Fix the scale and evolve in energy

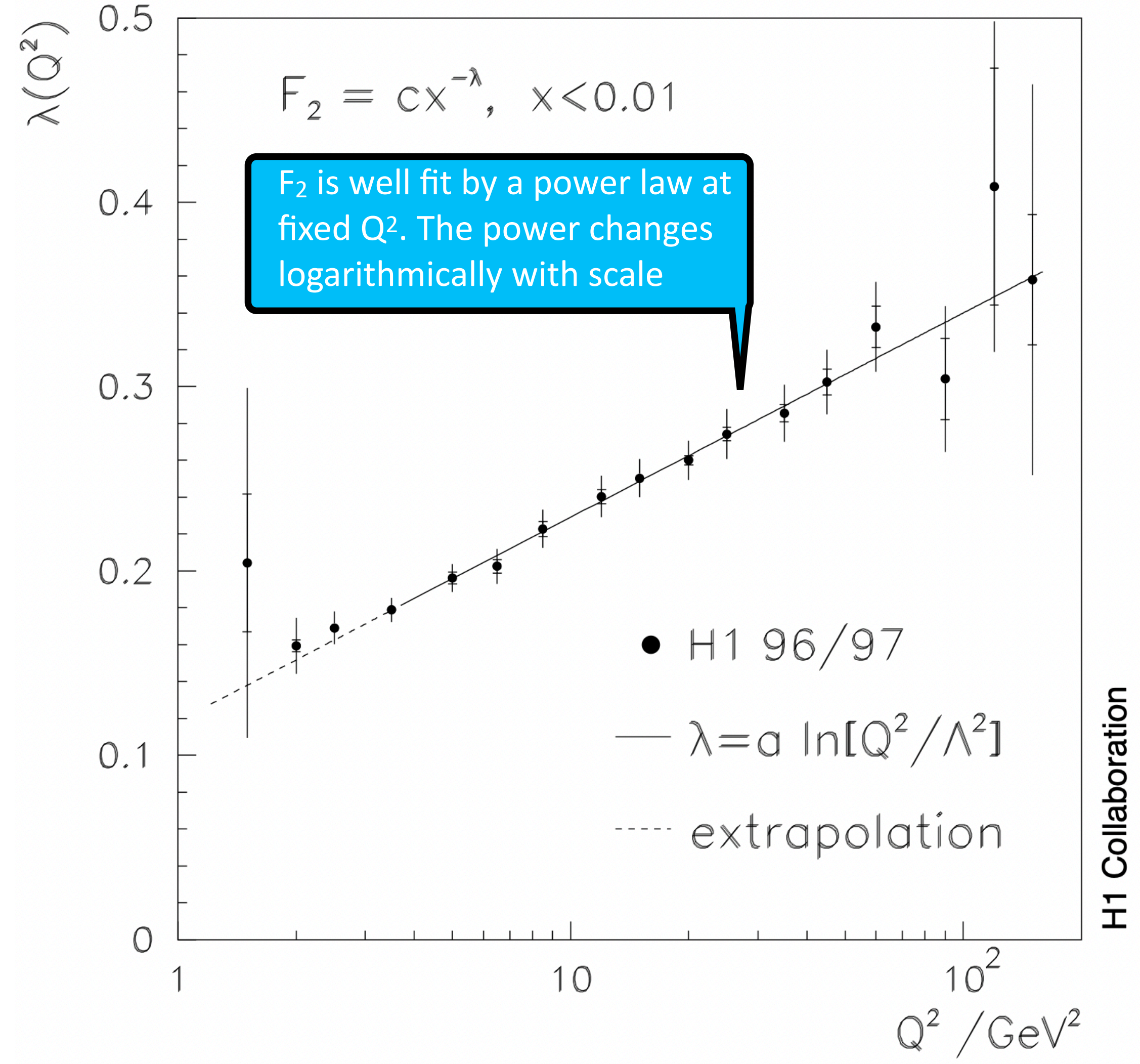
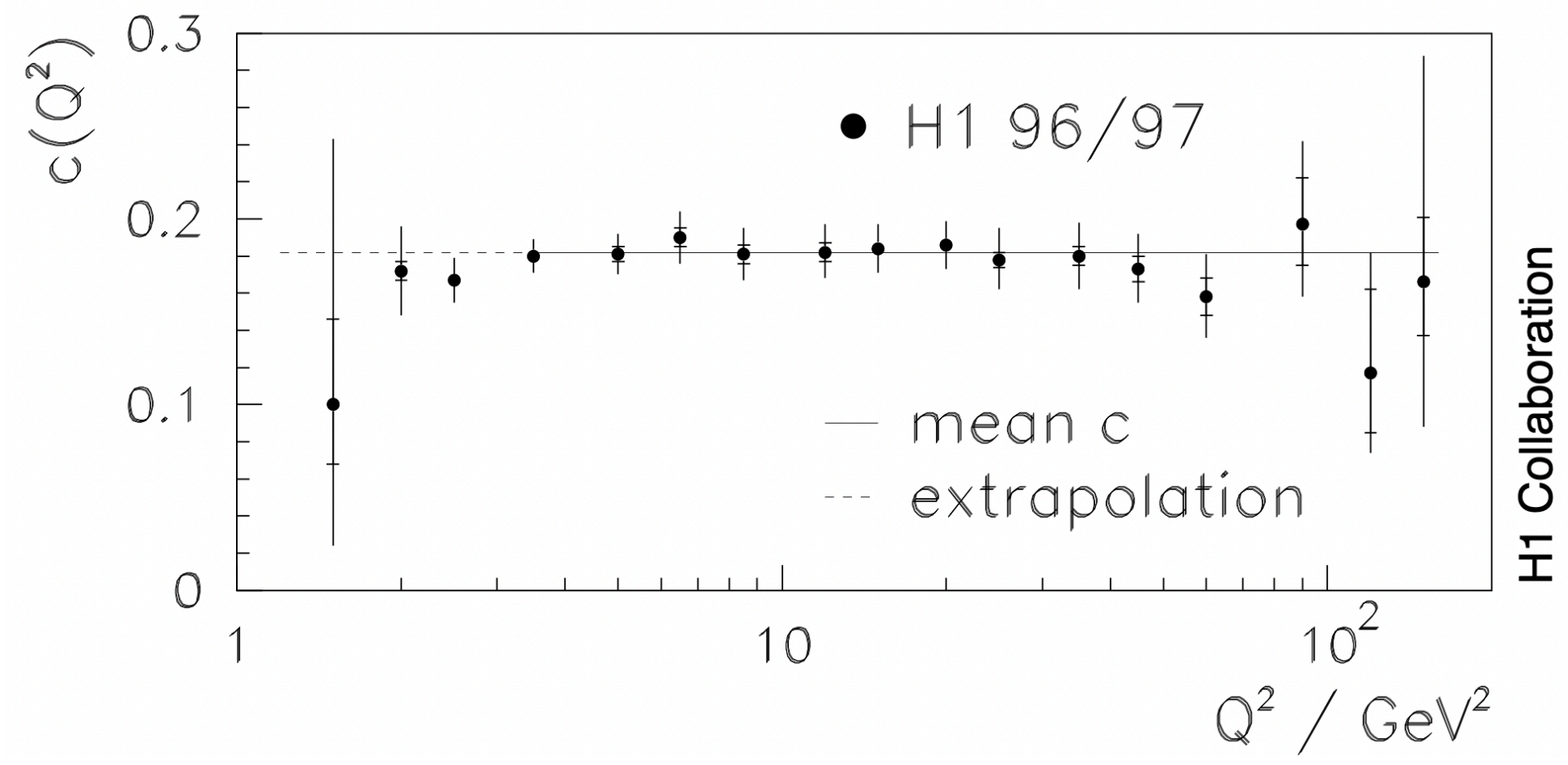
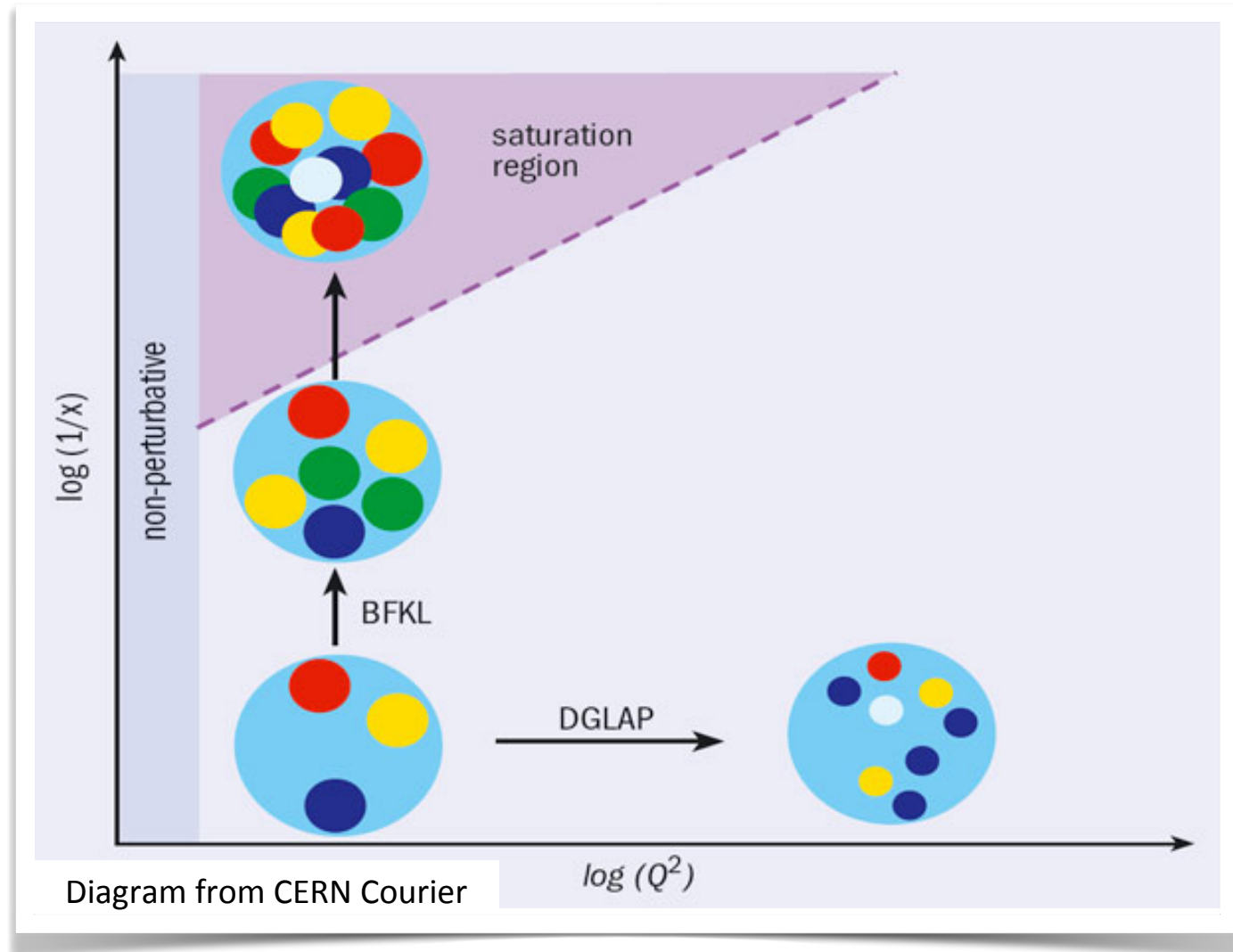


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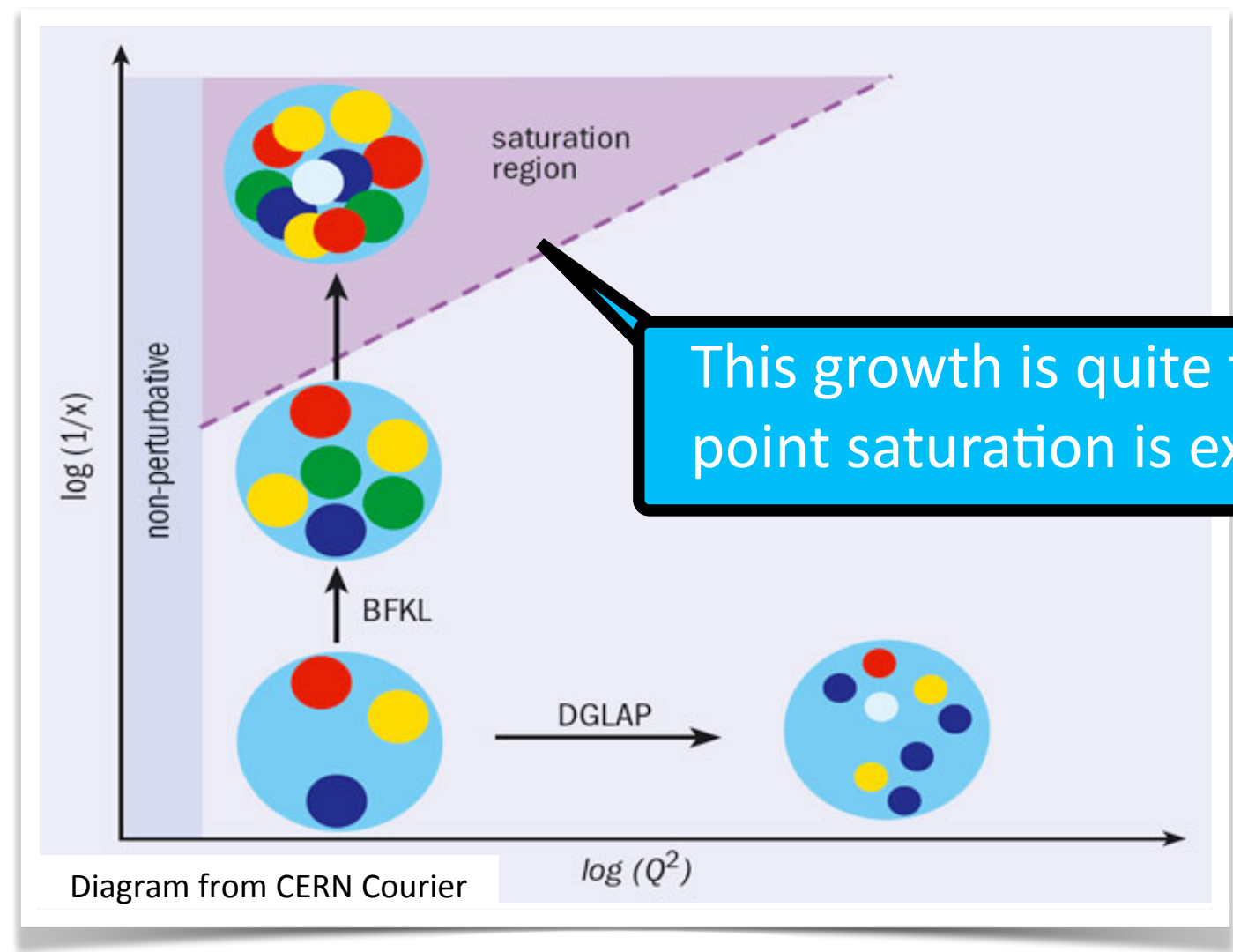


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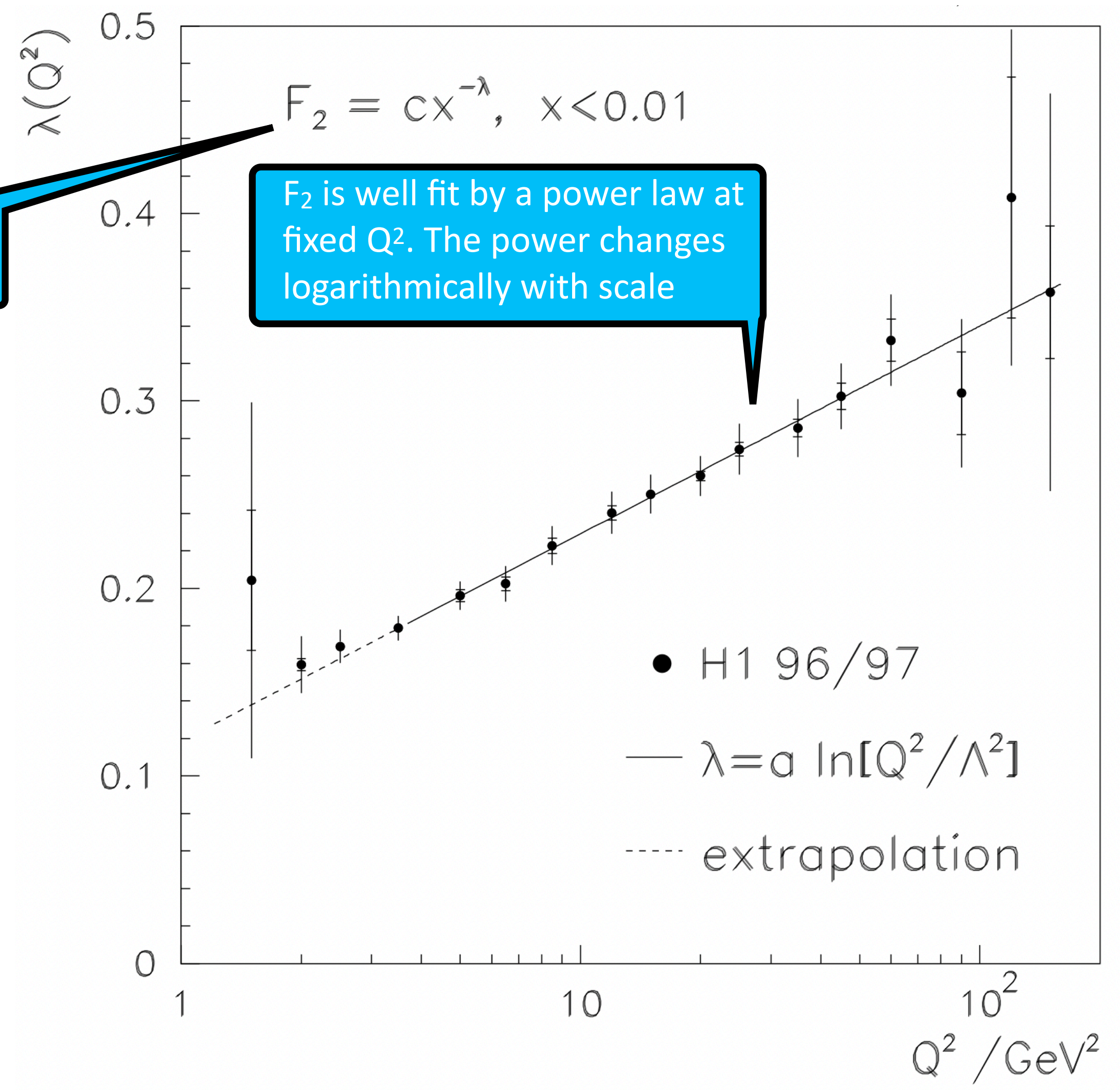
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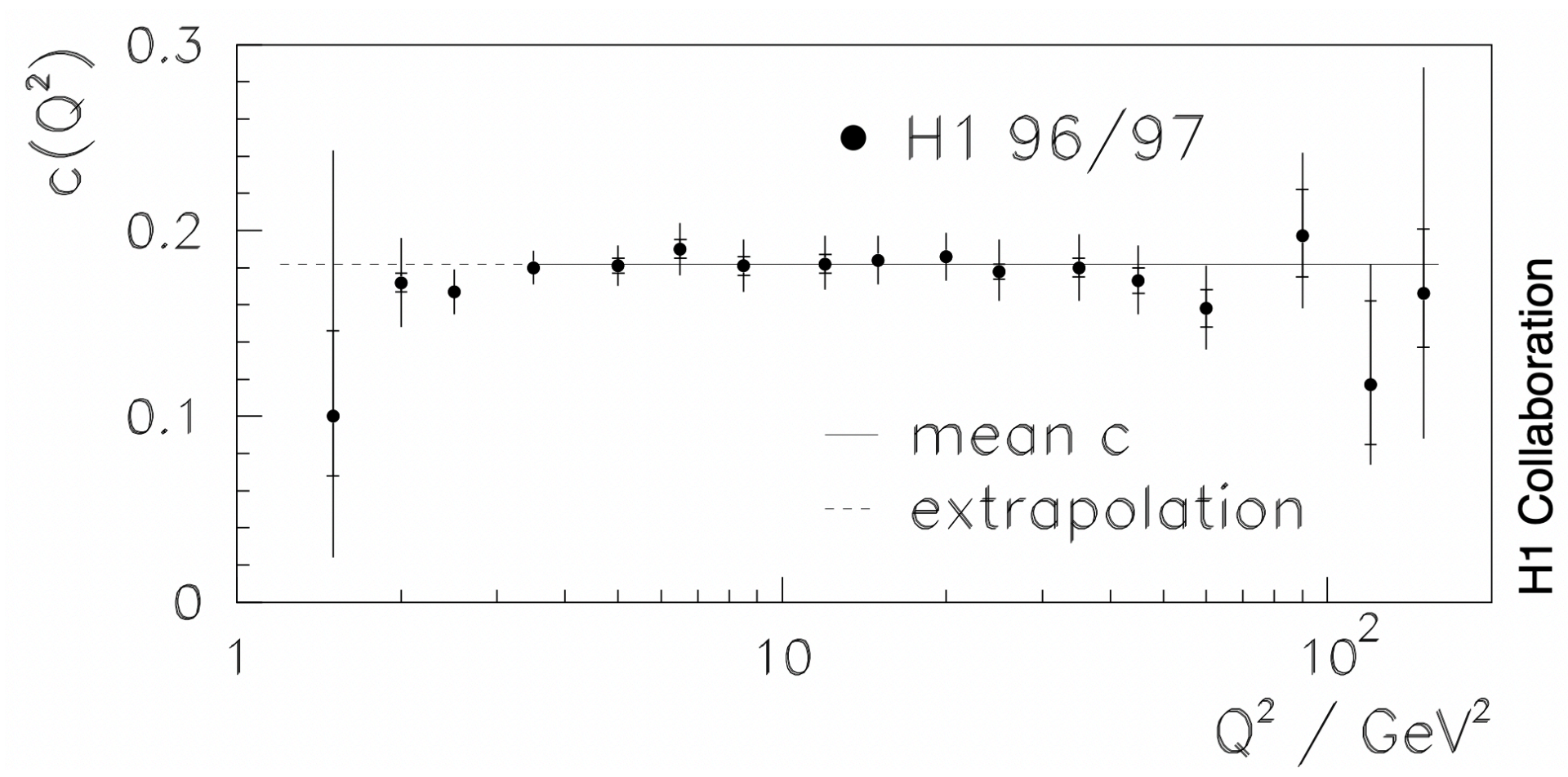
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F_2 is well fit by a power law at fixed Q^2 . The power changes logarithmically with scale



H1 Collaboration

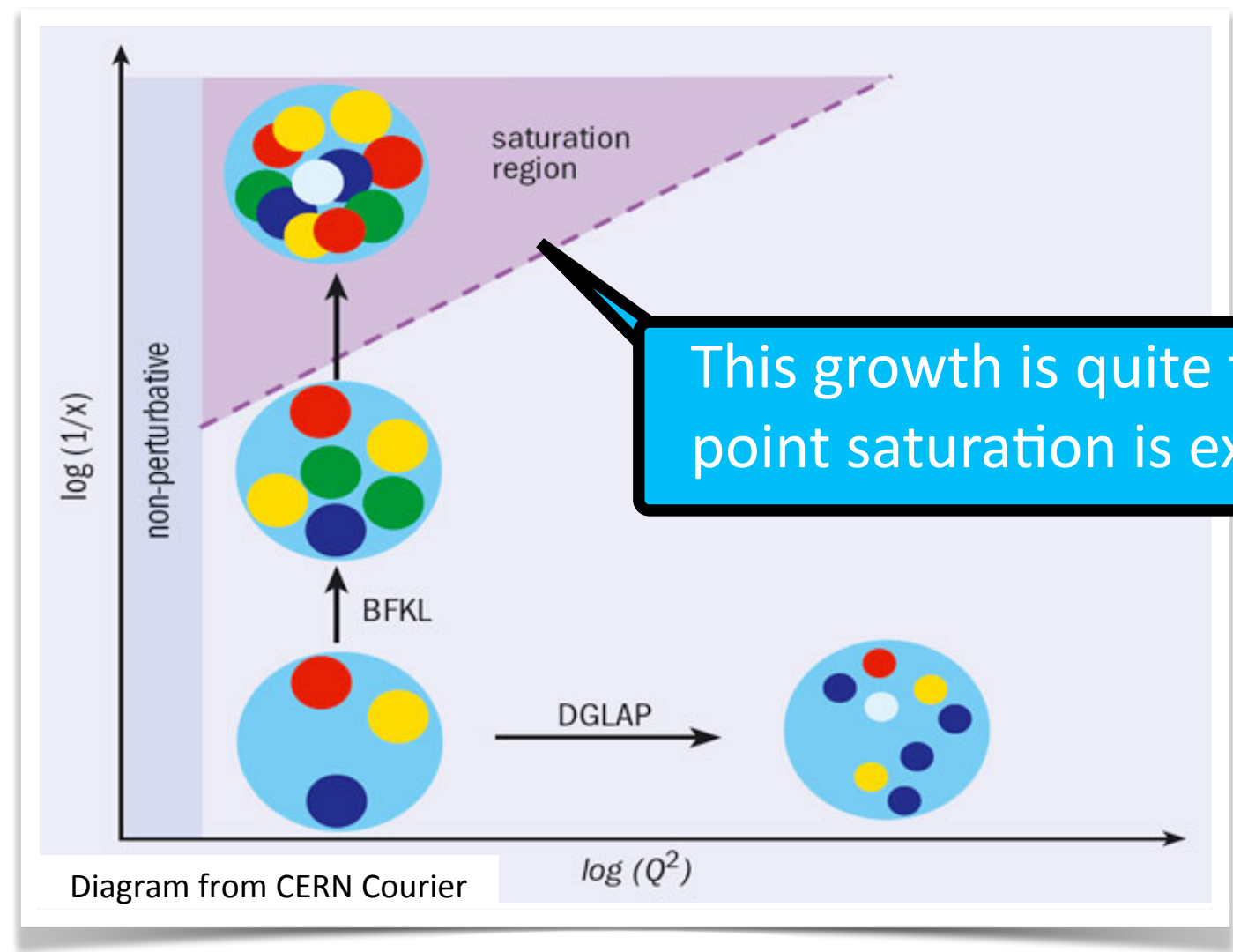
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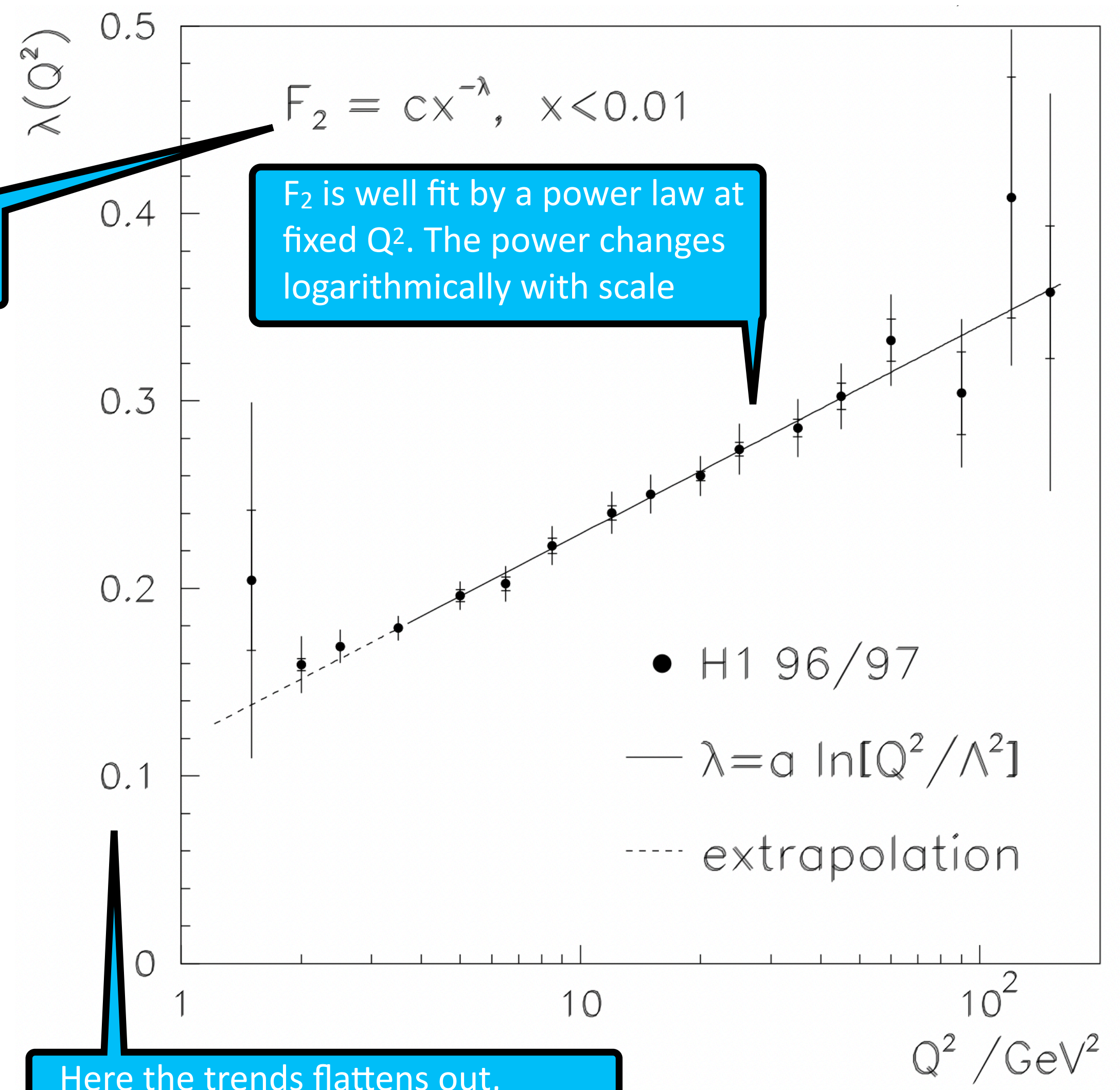
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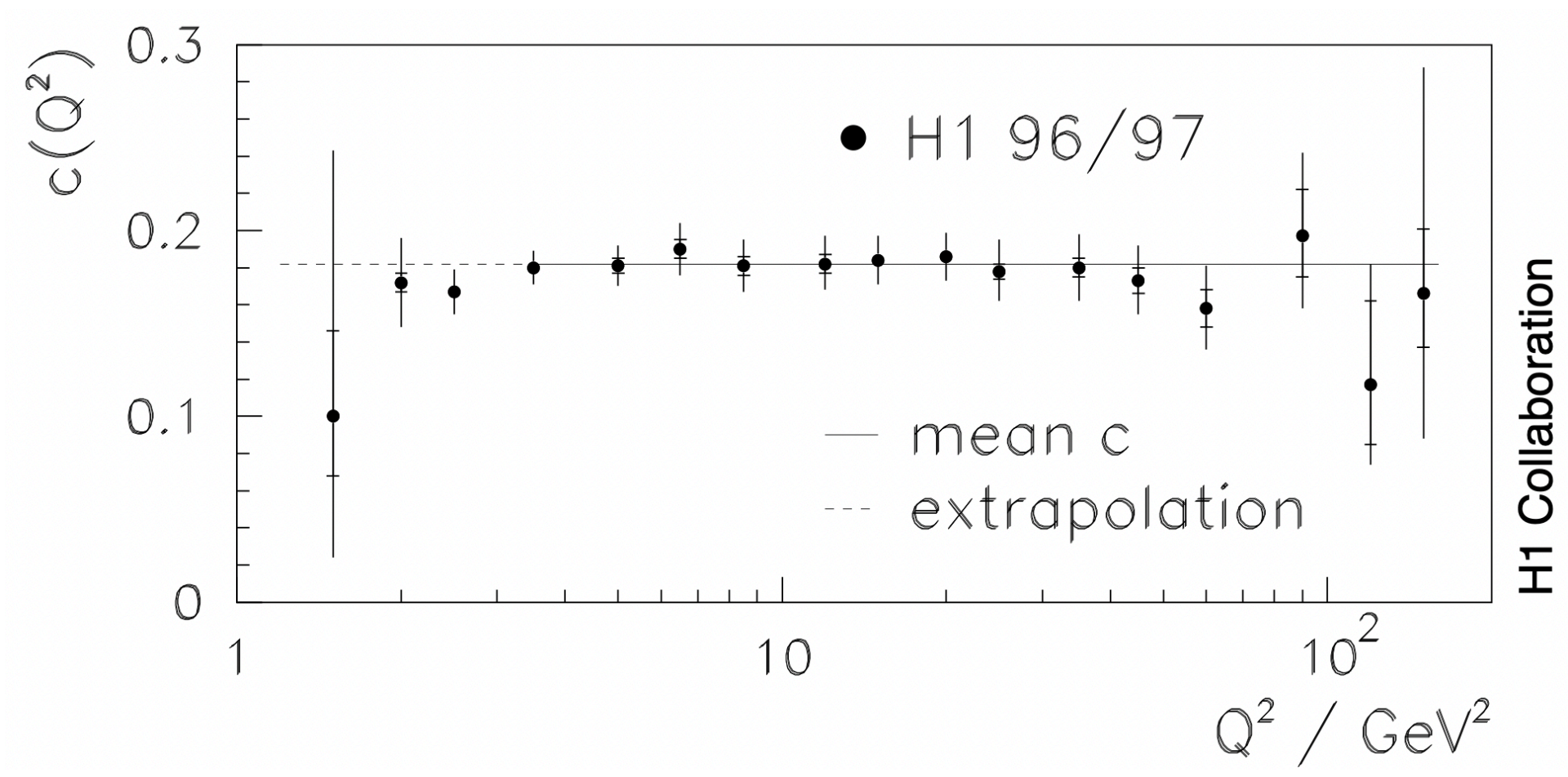


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Here the trends flattens out, consistent with total cross sections



H1 Collaboration

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The determination of the onset of saturation is one of the prime tasks of experimental pQCD nowadays

Photo-production cross section (1997)

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} \left(2 - 2y + \frac{y^2}{1+R}\right) F_2(x, Q^2) = \Gamma[\sigma_T(x, Q^2) + \epsilon(y)\sigma_L(x, Q^2)] \equiv \Gamma\sigma_{\gamma^*p}^{eff}(x, y, Q^2)$$

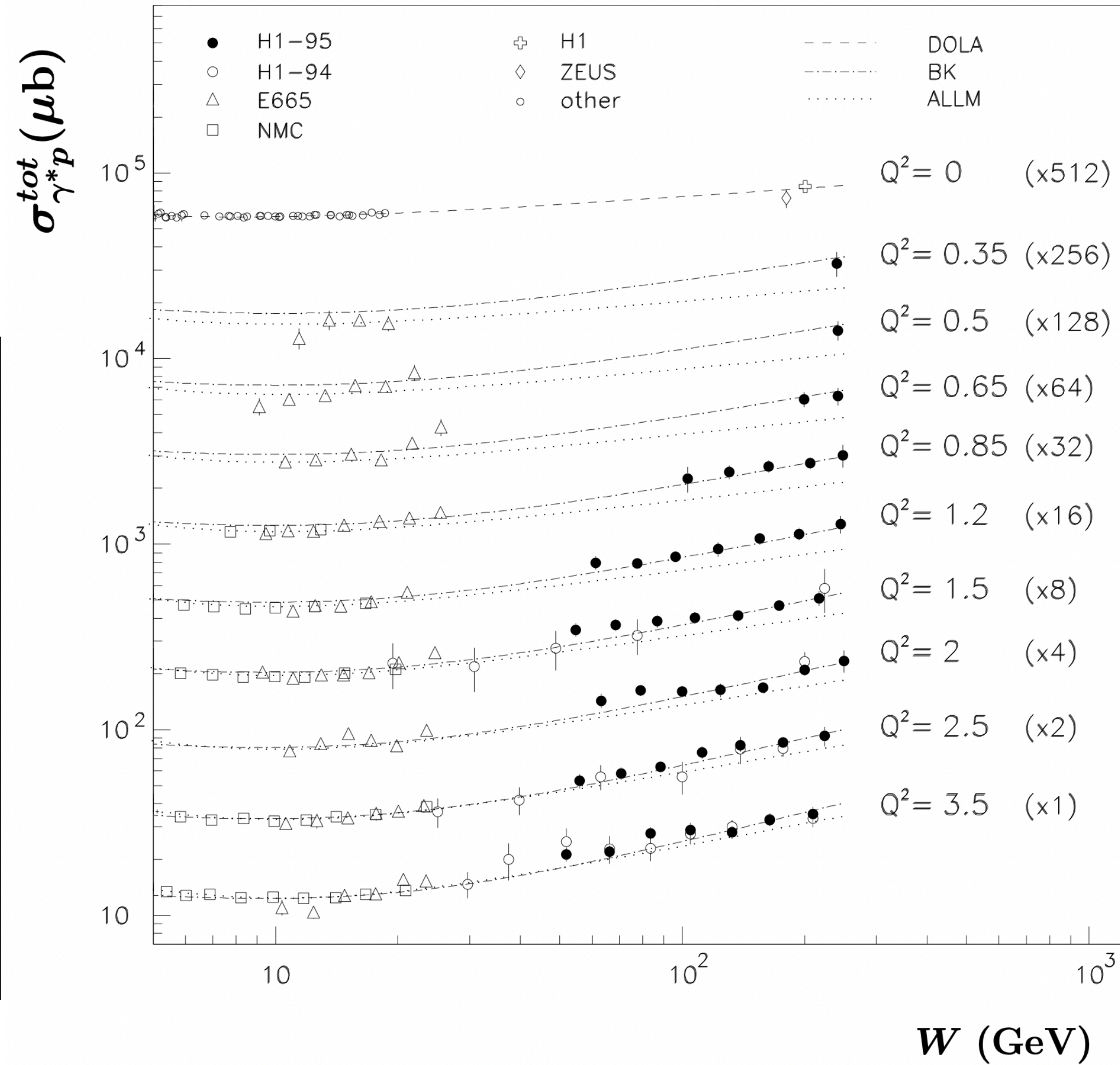
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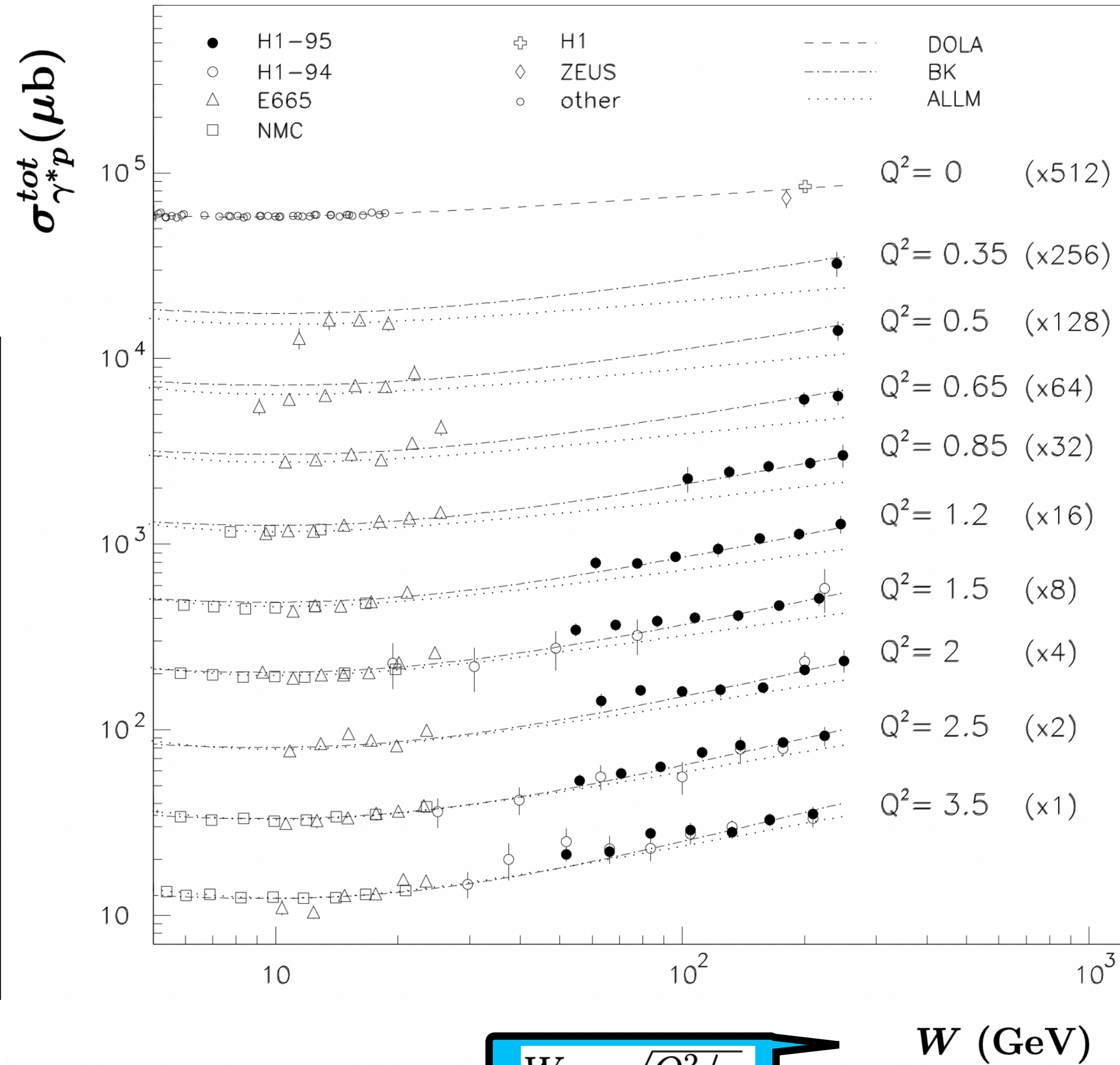


CMS energy of the γp system

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Small $x \sim$ large W

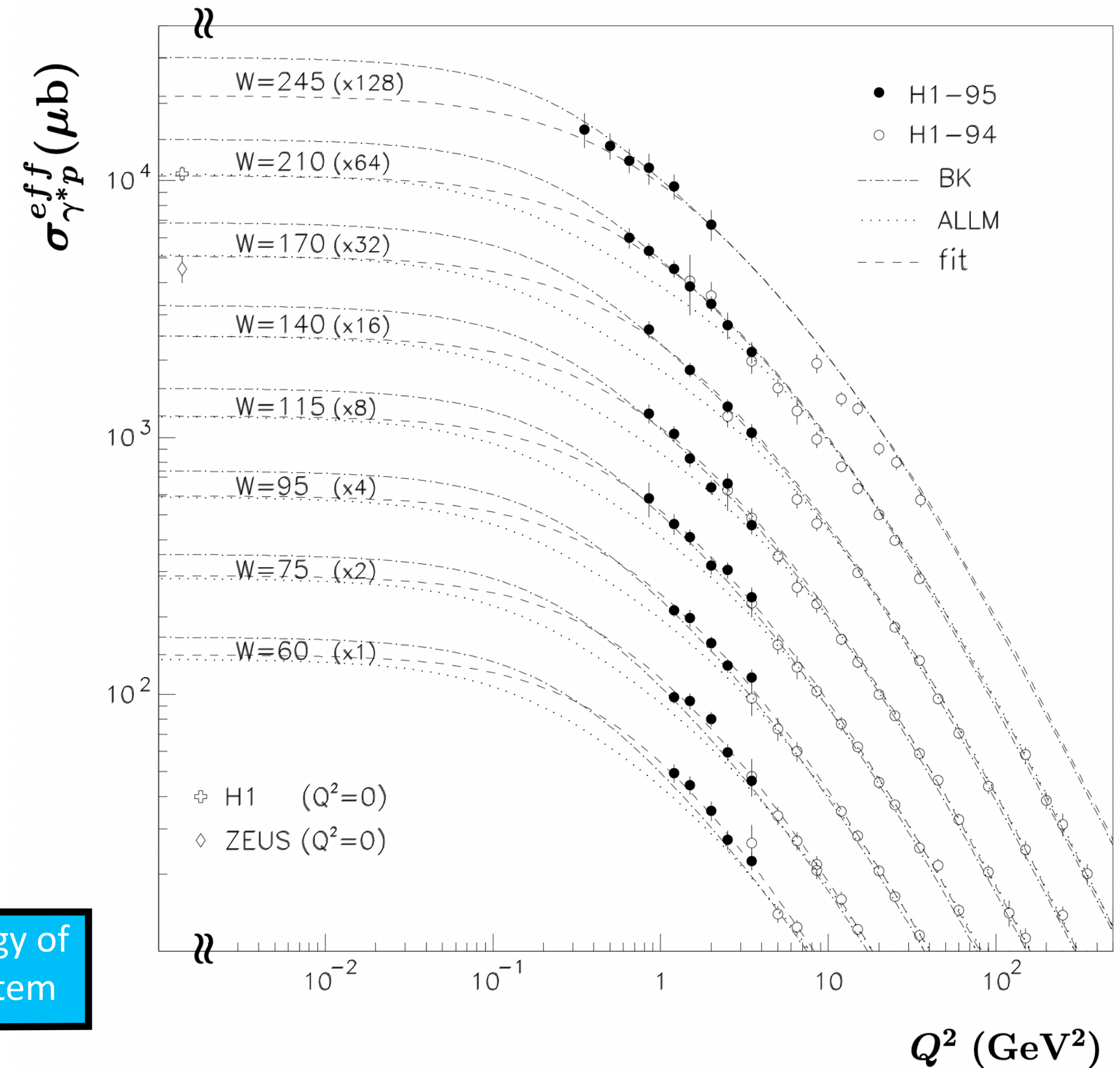
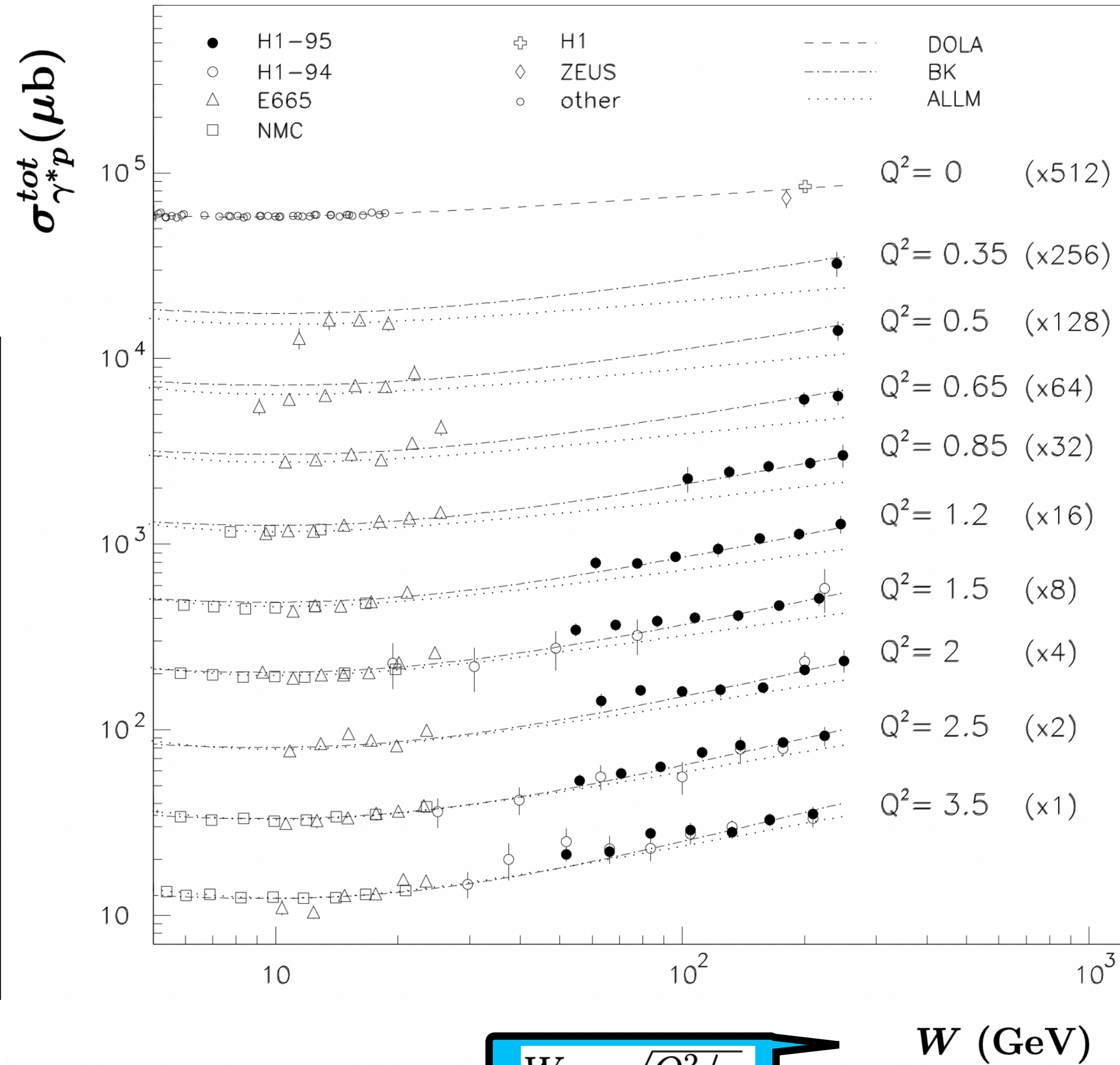
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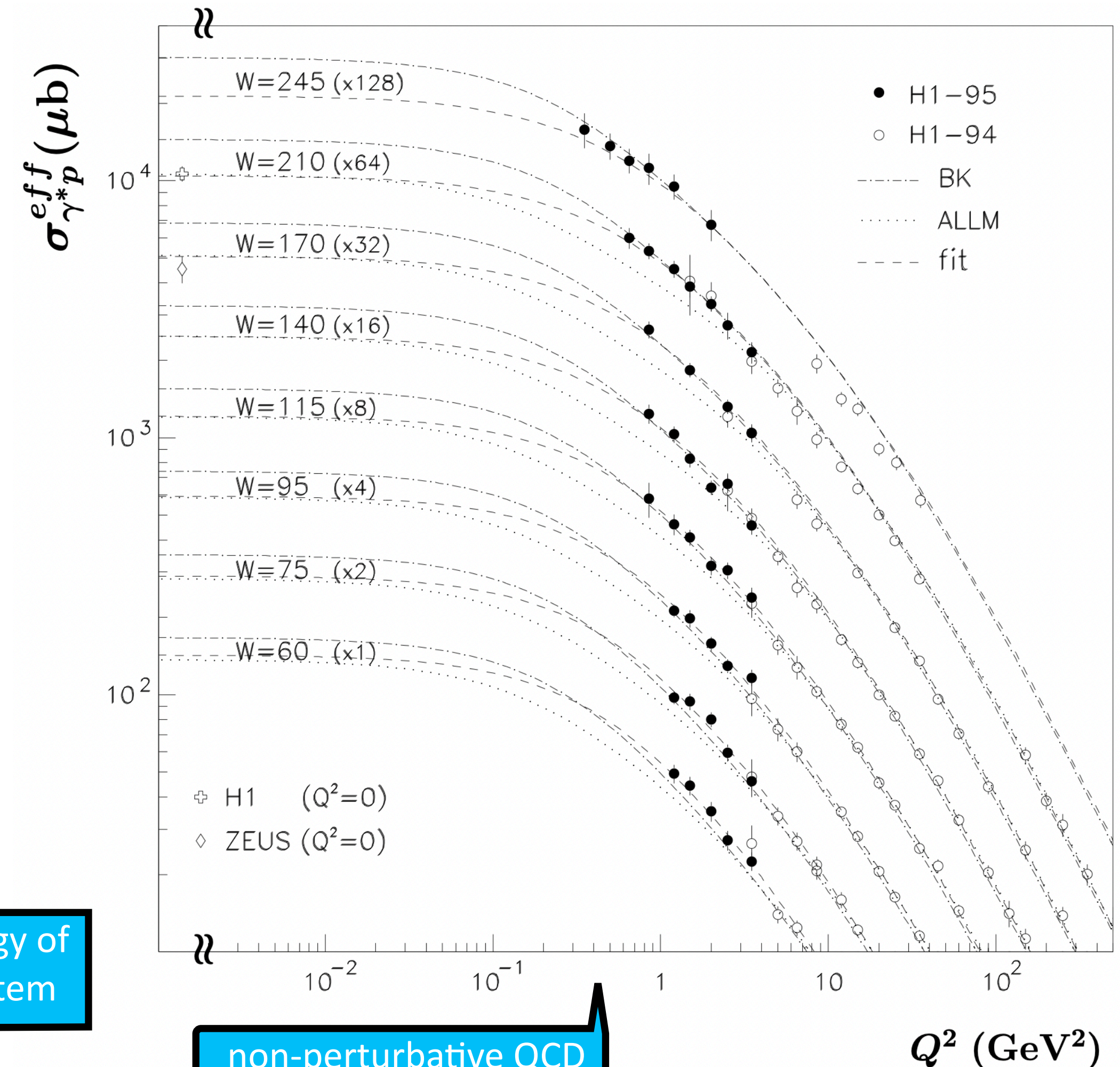
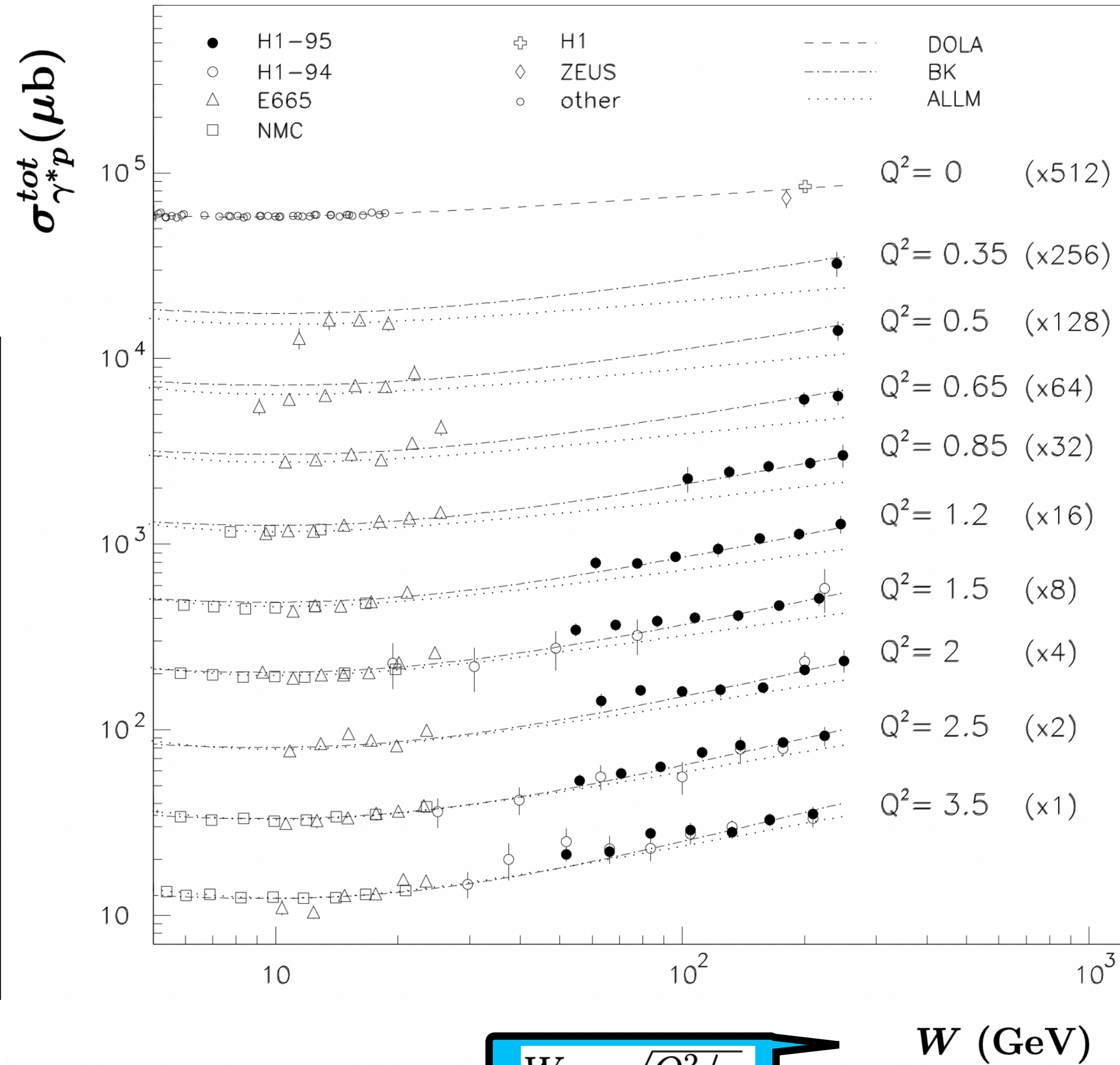
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non-perturbative QCD starts around here

Guillermo Contreras, CTU in Prague

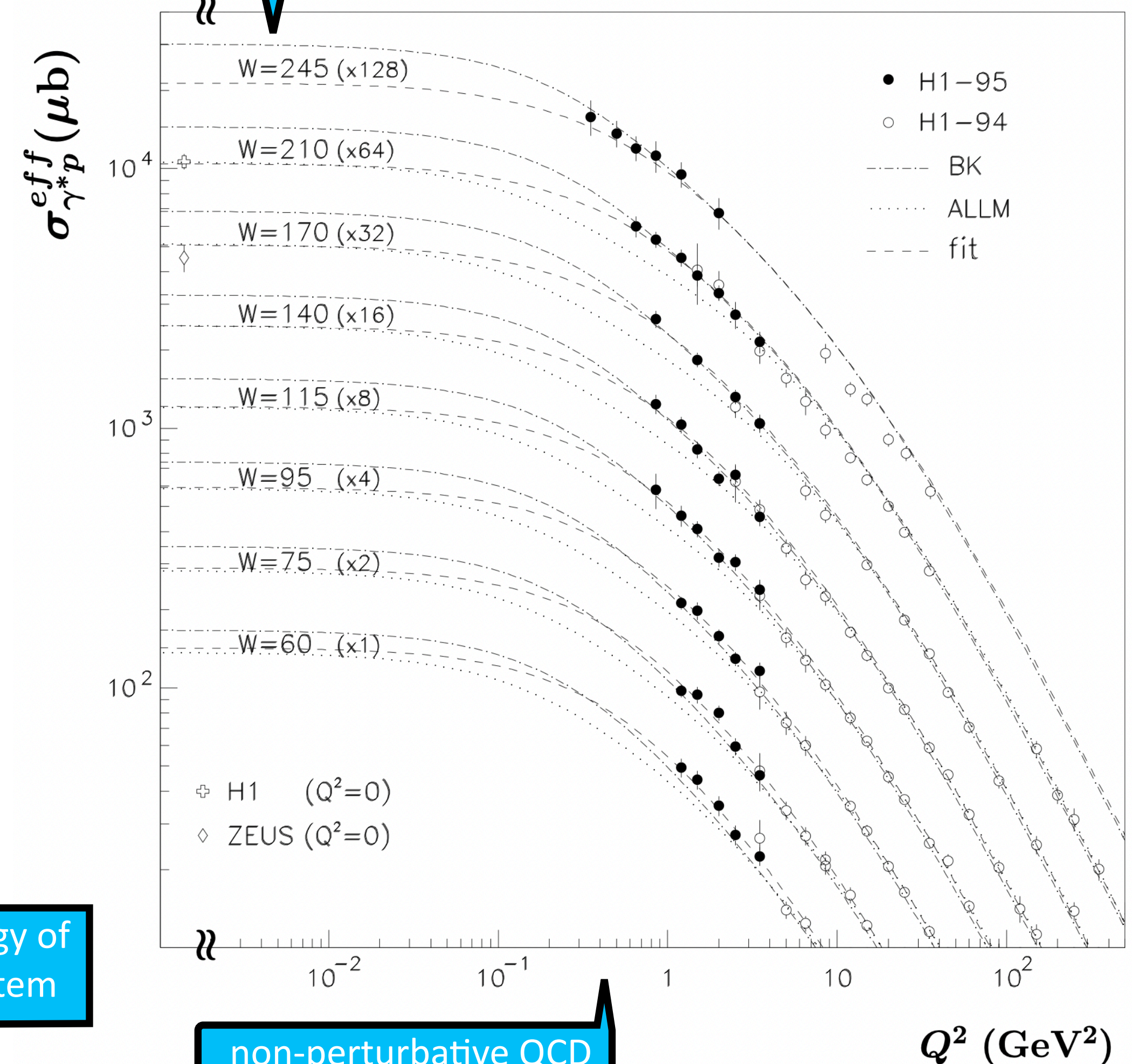
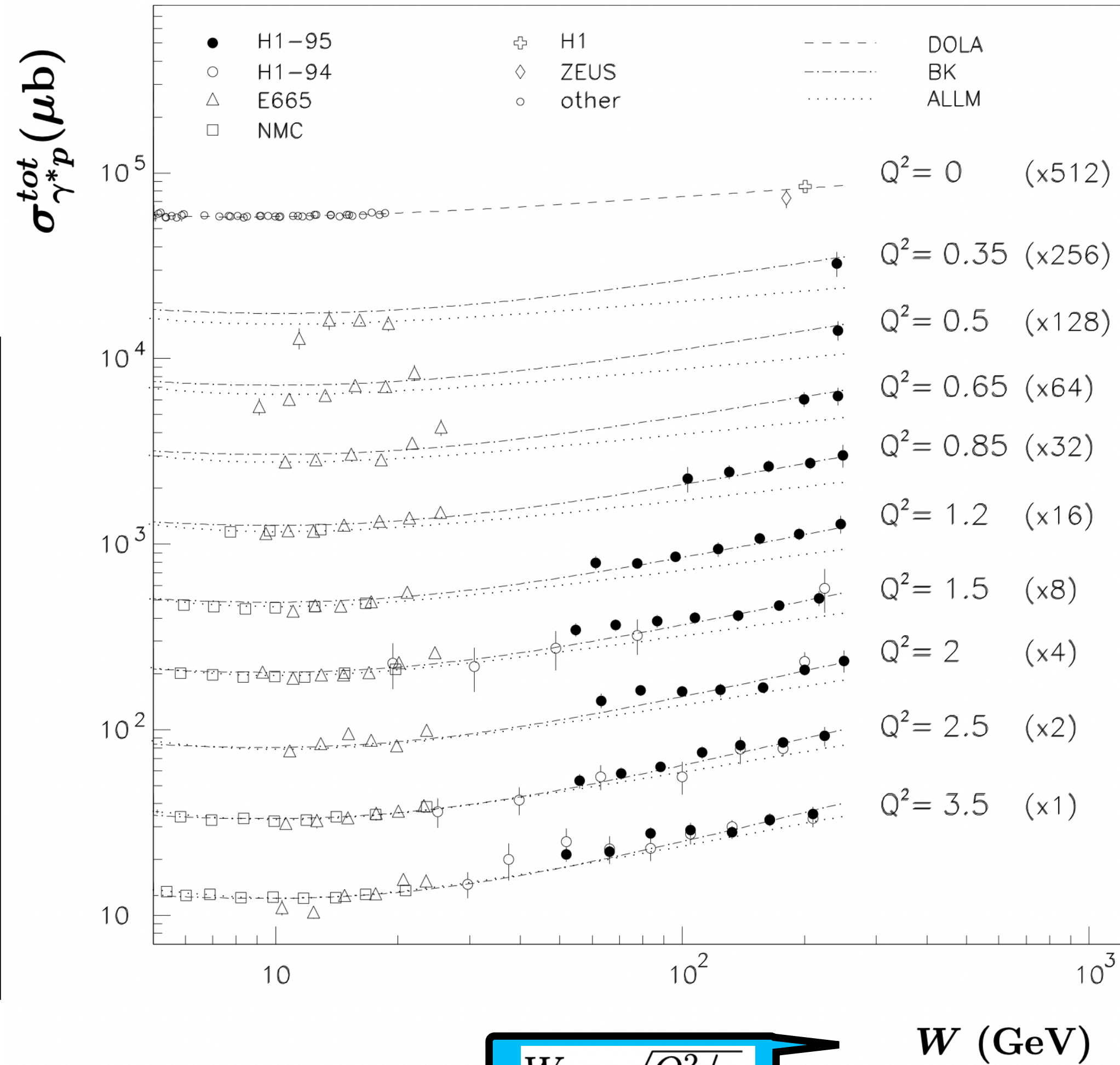
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This is a different type of saturation than the one mentioned in the previous page

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The GBW (Golec-Biernart and Wüsthoff) model

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Homework:

try to implement this model and reproduced the results in the next pages

1998: The GBW model. (1) A different reference frame

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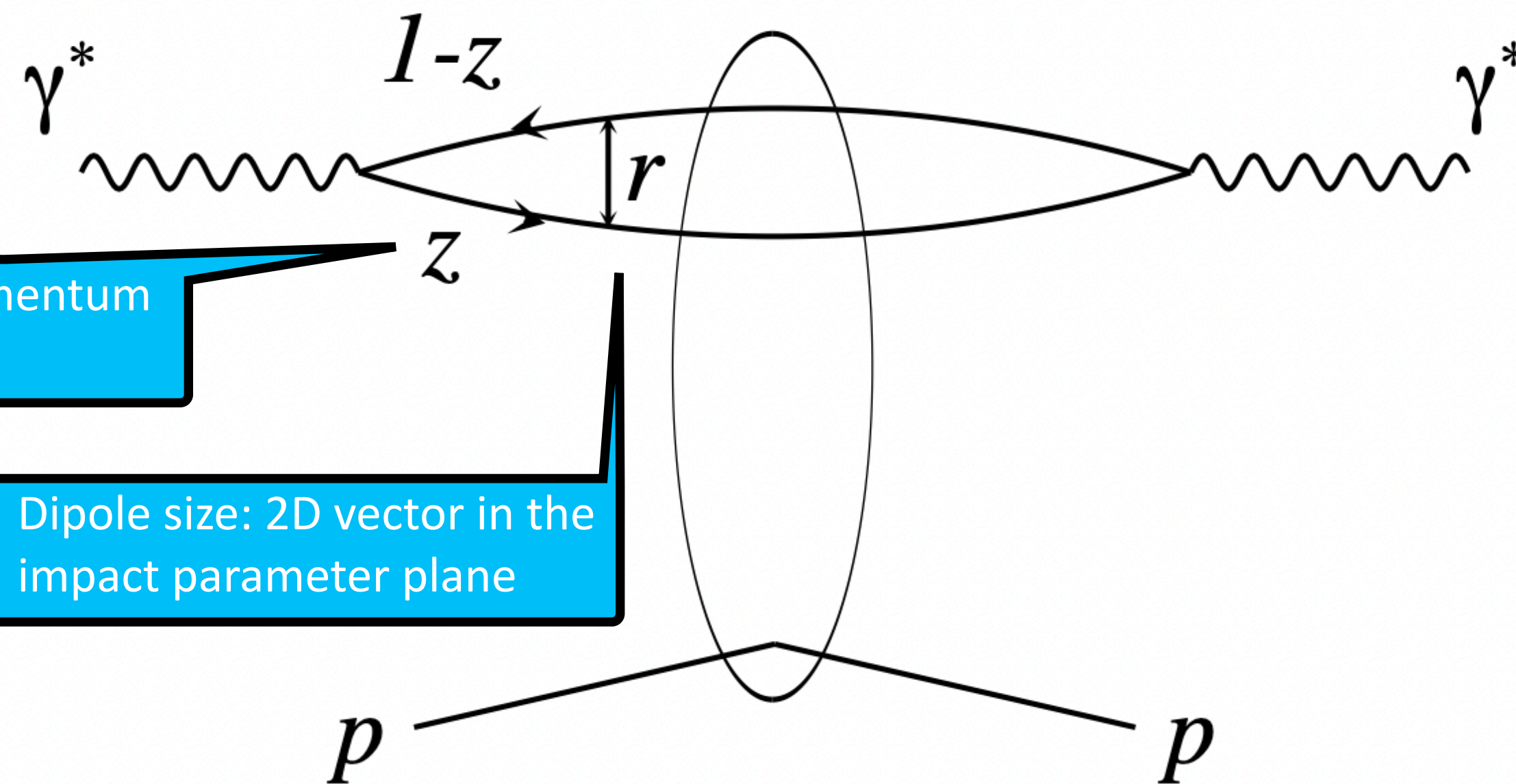
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Fraction of the photon momentum carried by the quark

Dipole size: 2D vector in the impact parameter plane

1998: The GBW model. (2) Factorisation

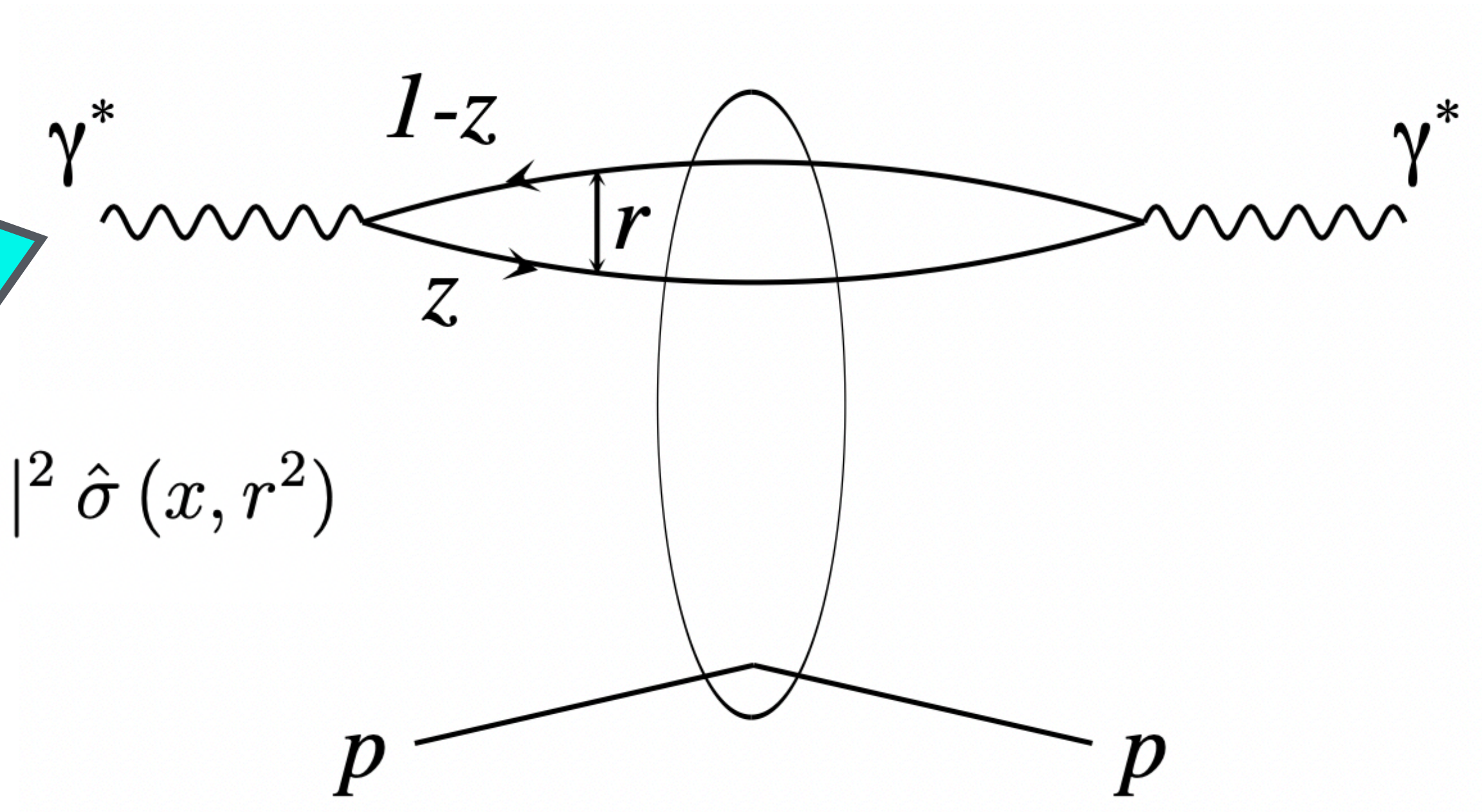
In this frame the photo-production cross section factorises in a QED and a QCD part

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Wave function for the splitting of a photon into a quark-antiquark pair

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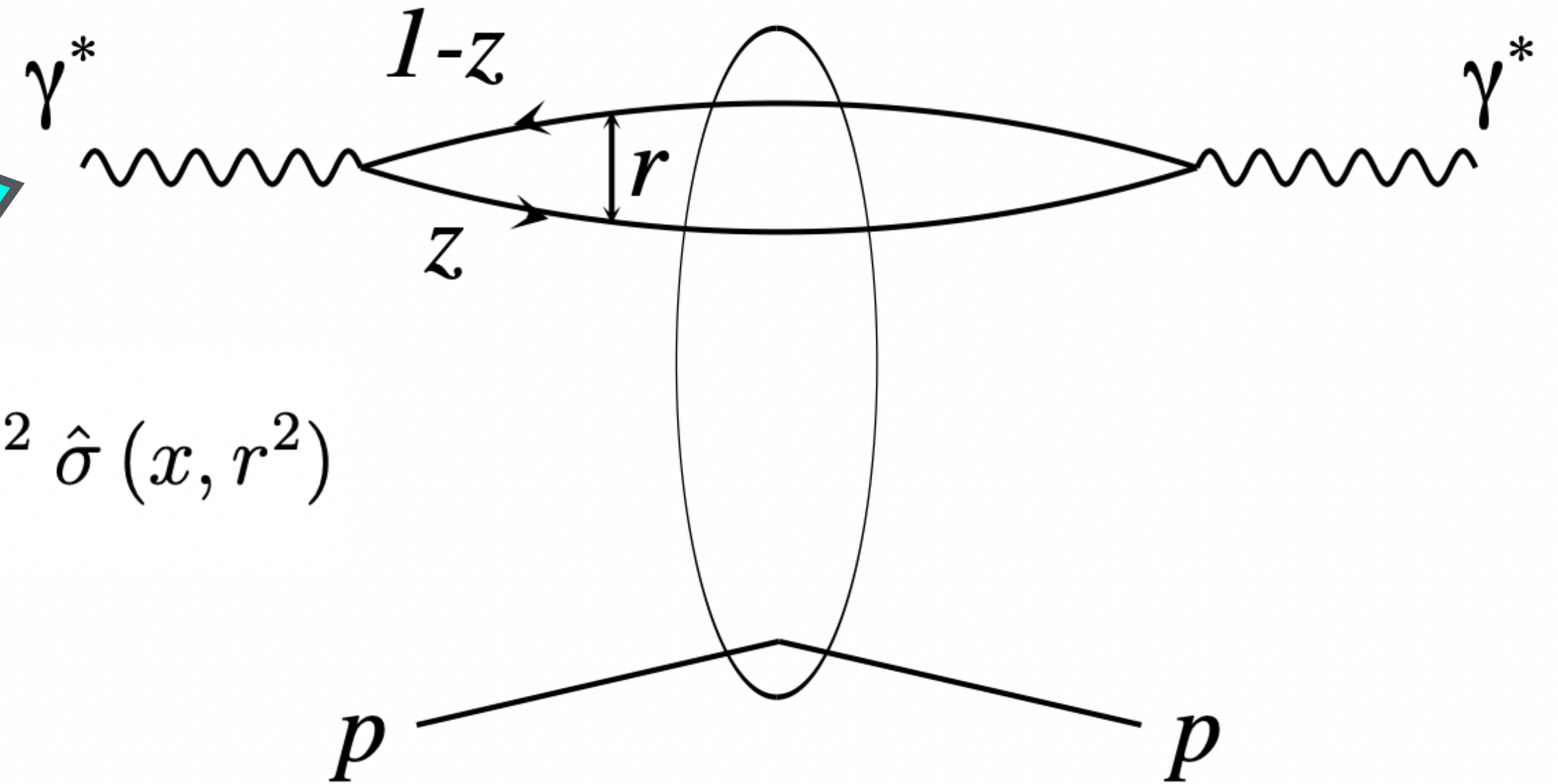


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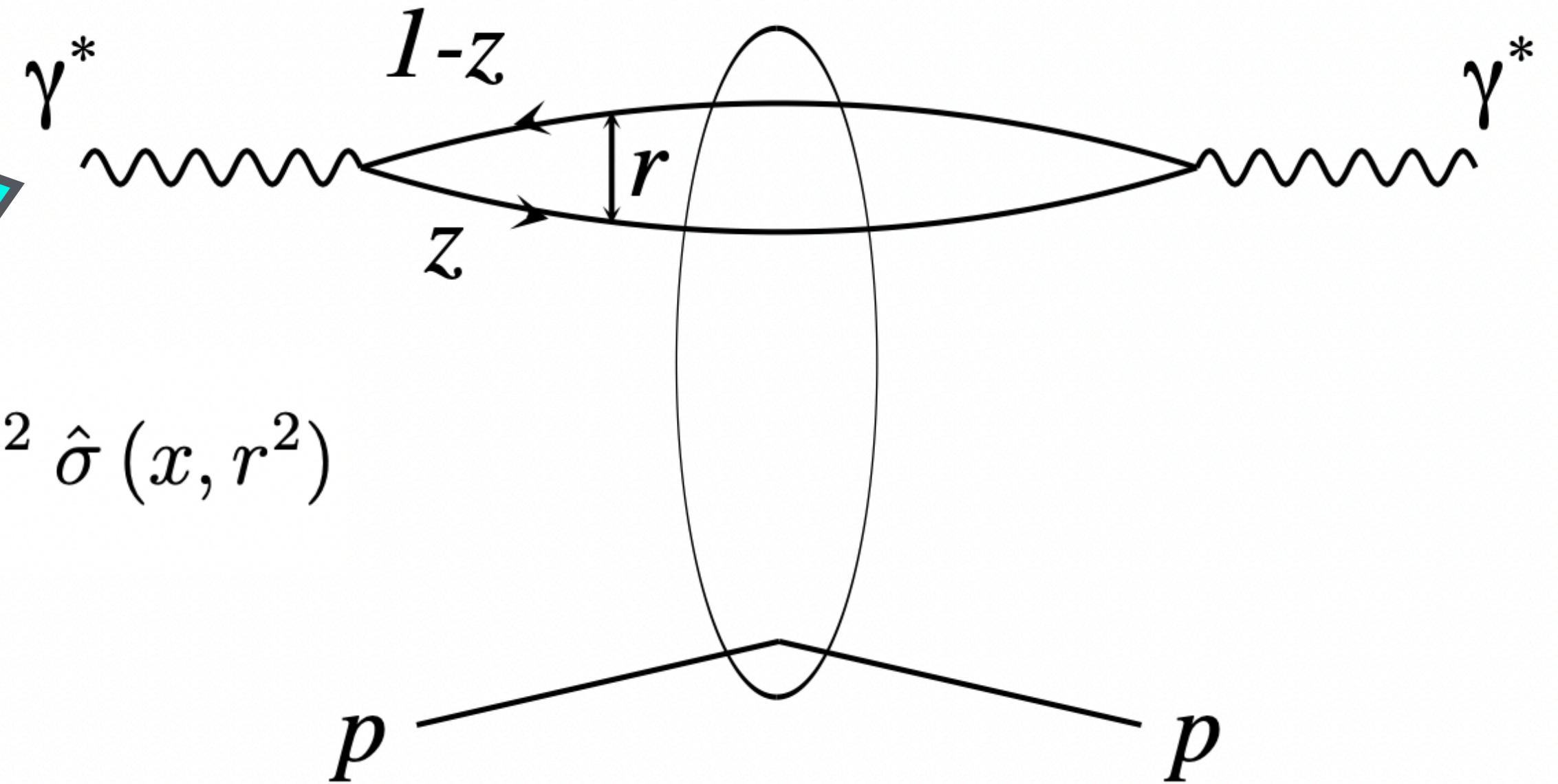
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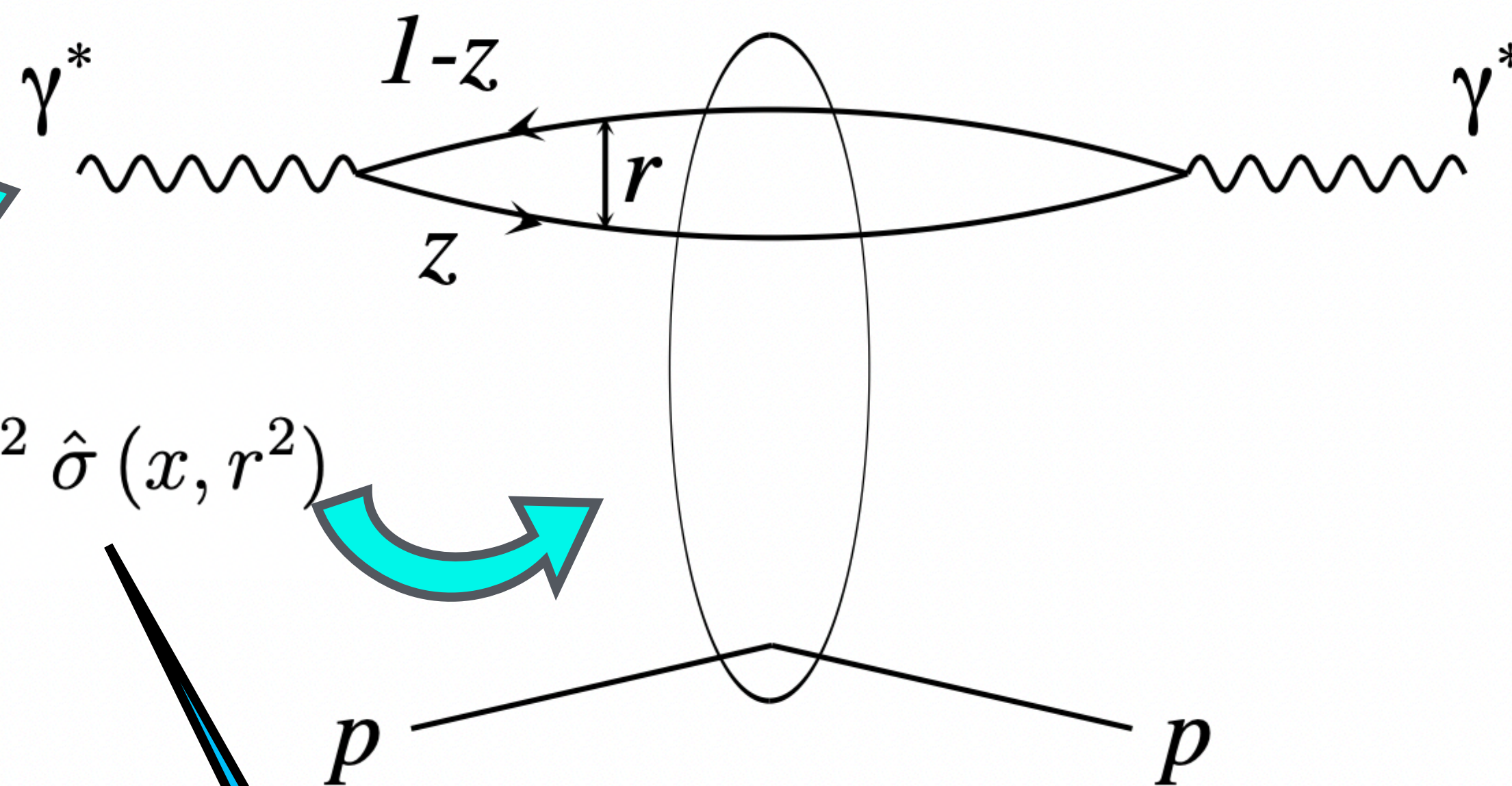
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Dipole cross section

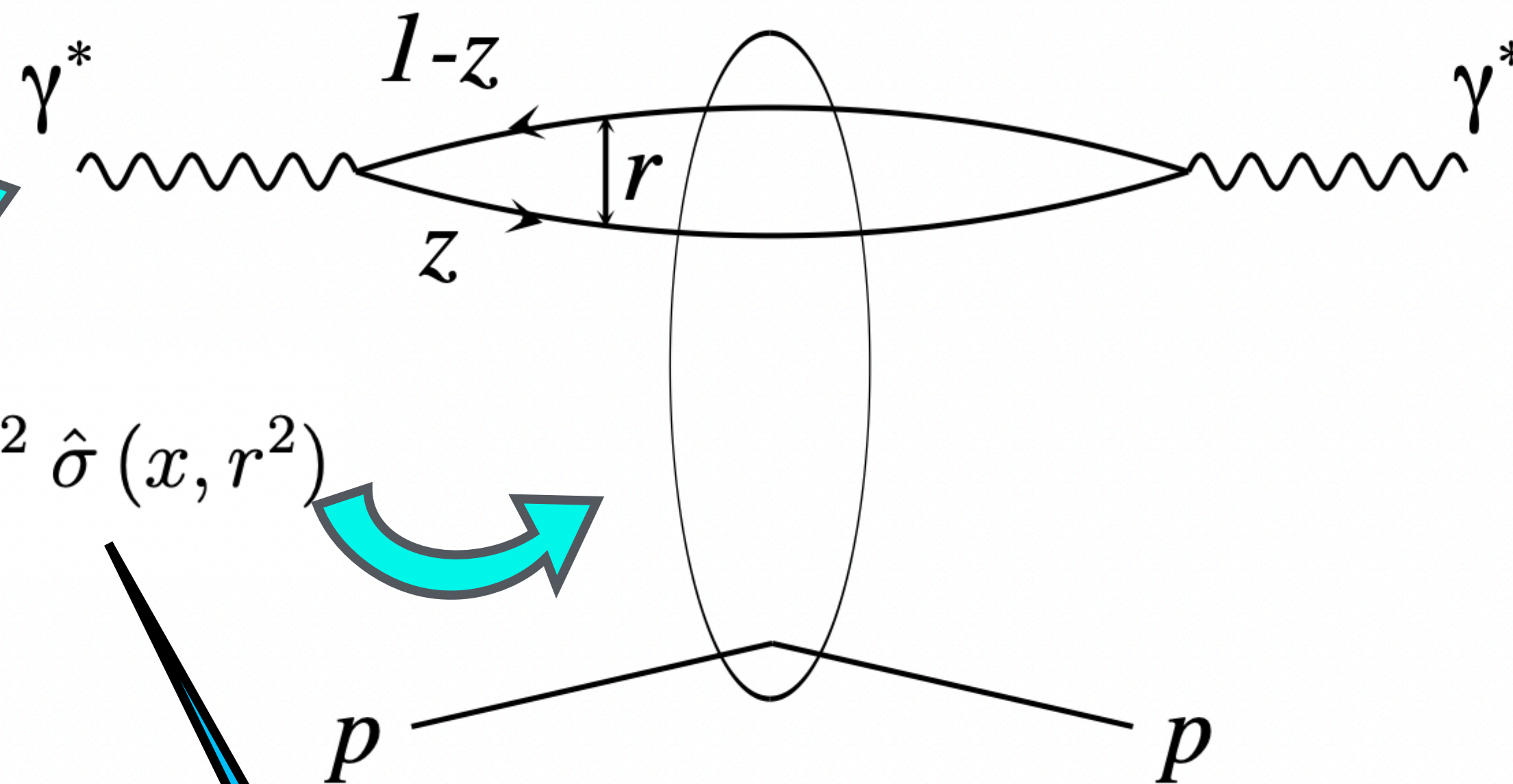
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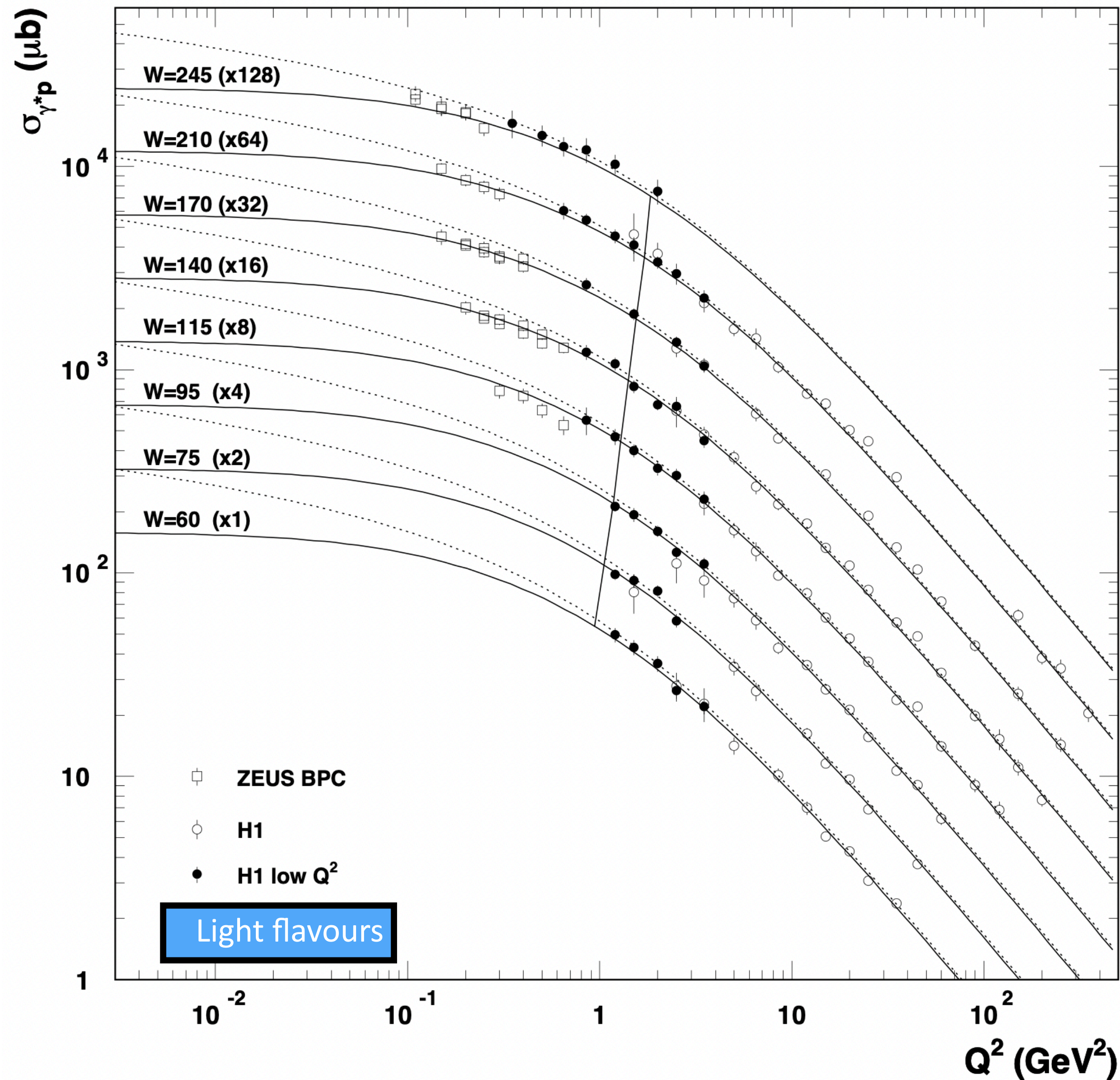
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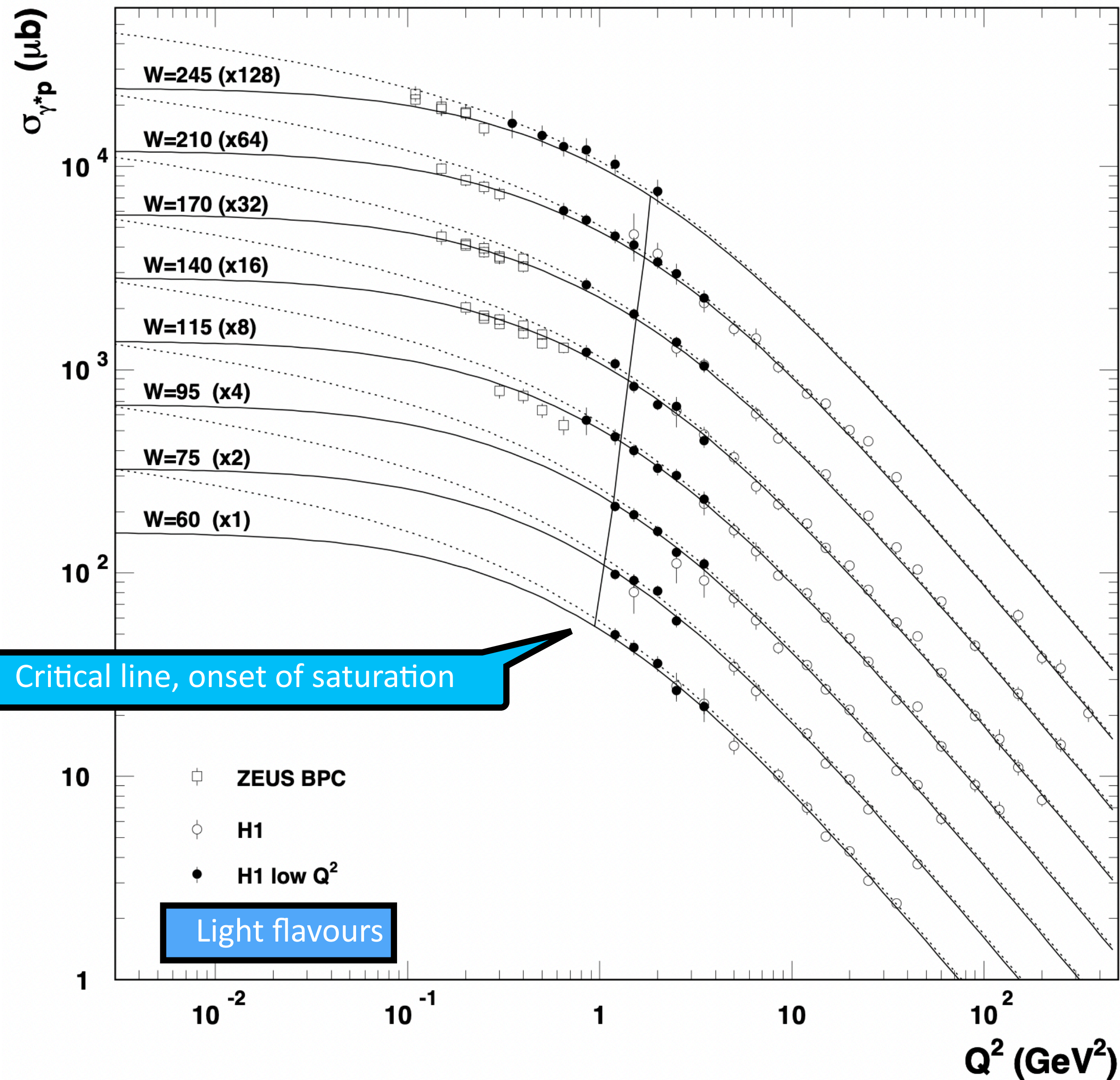
GBW define the critical line as:

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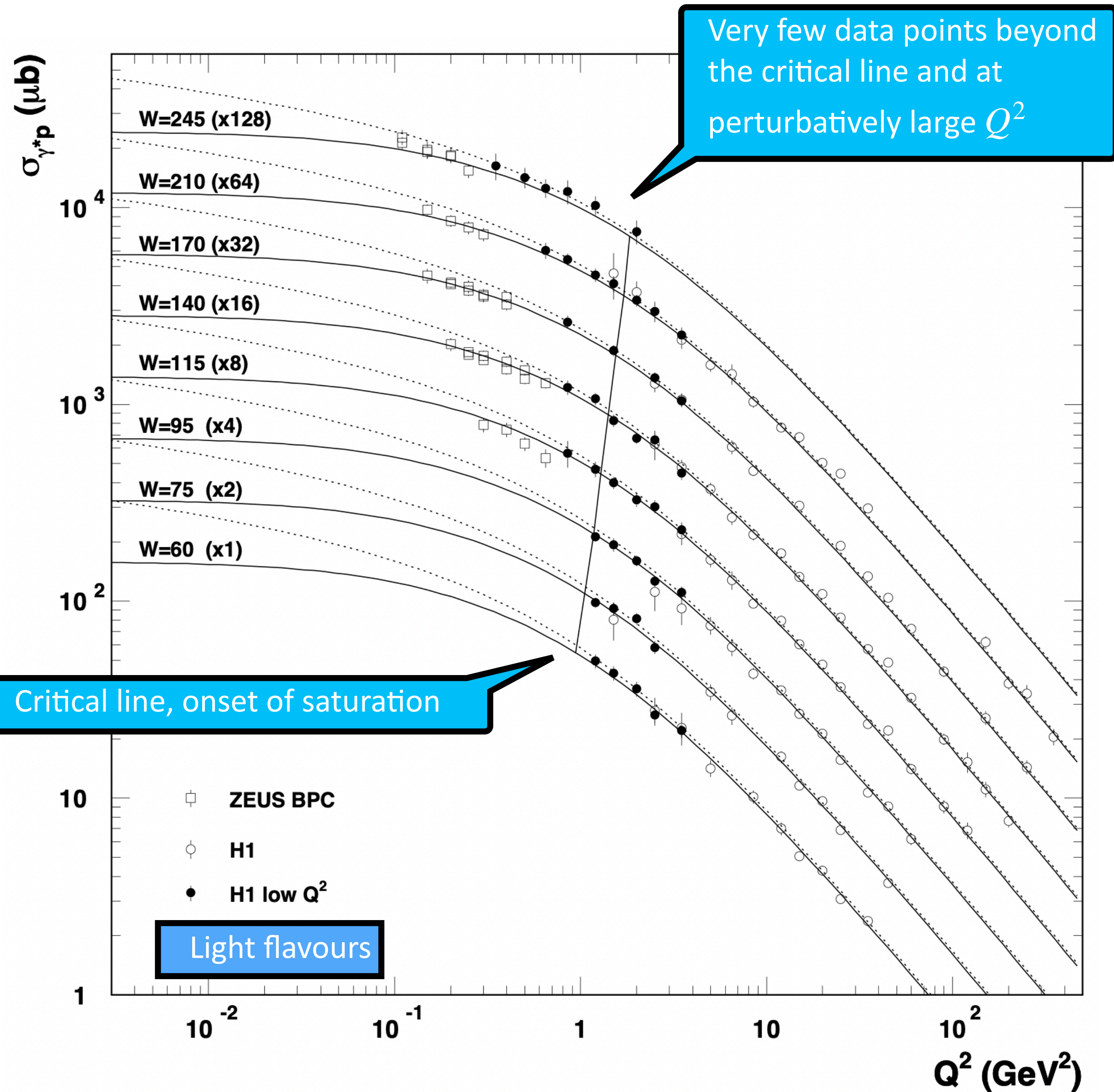
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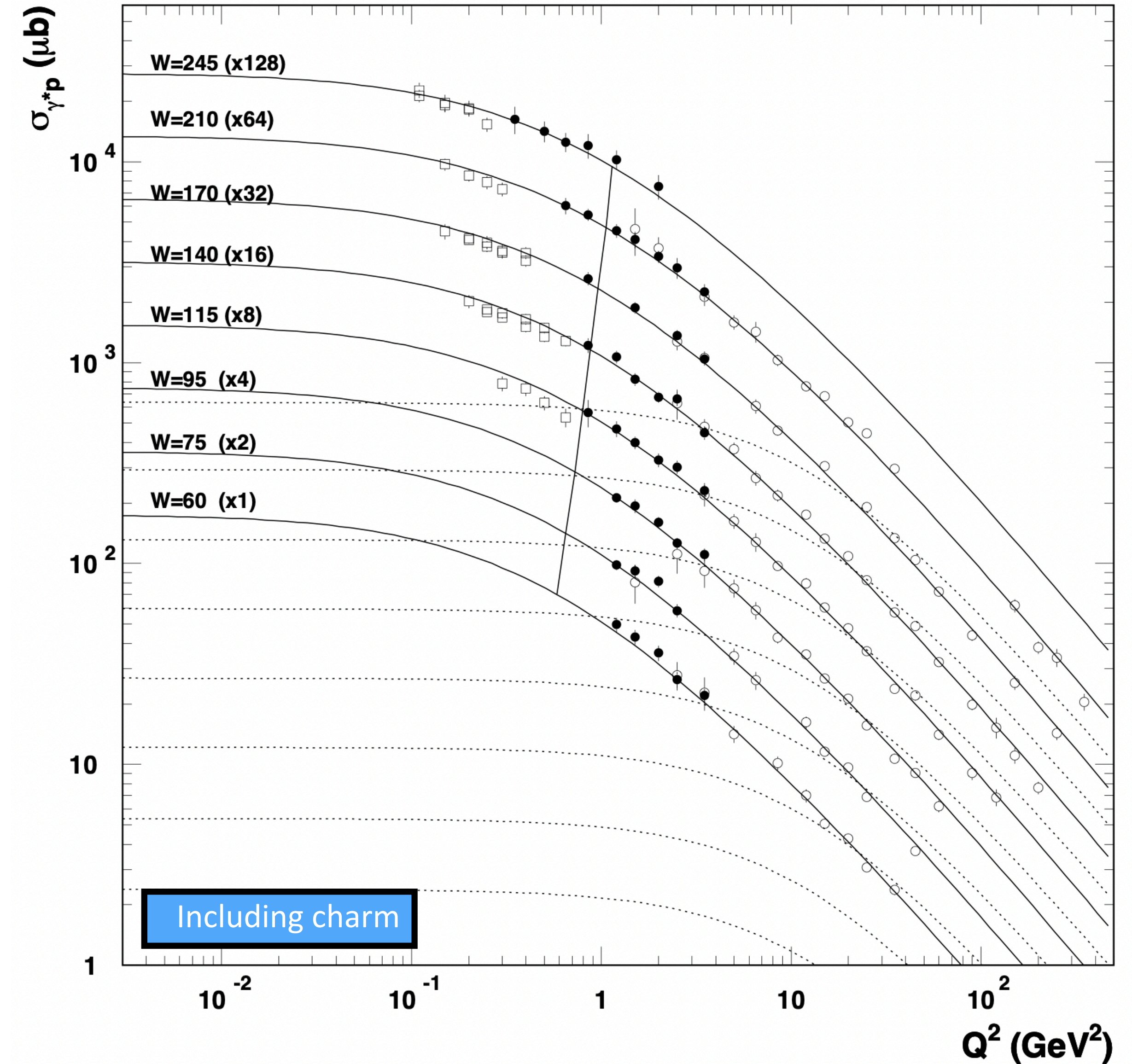
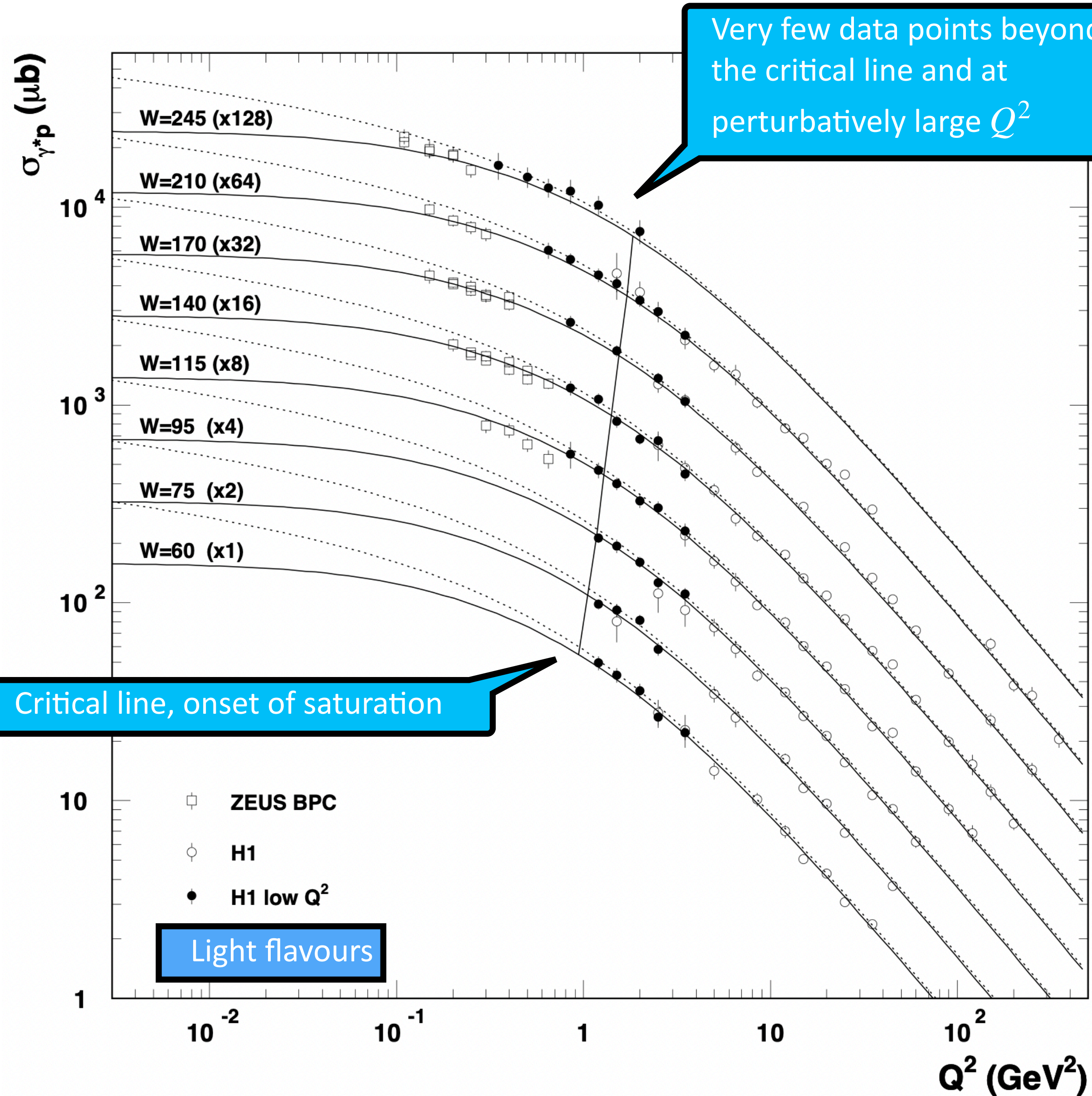
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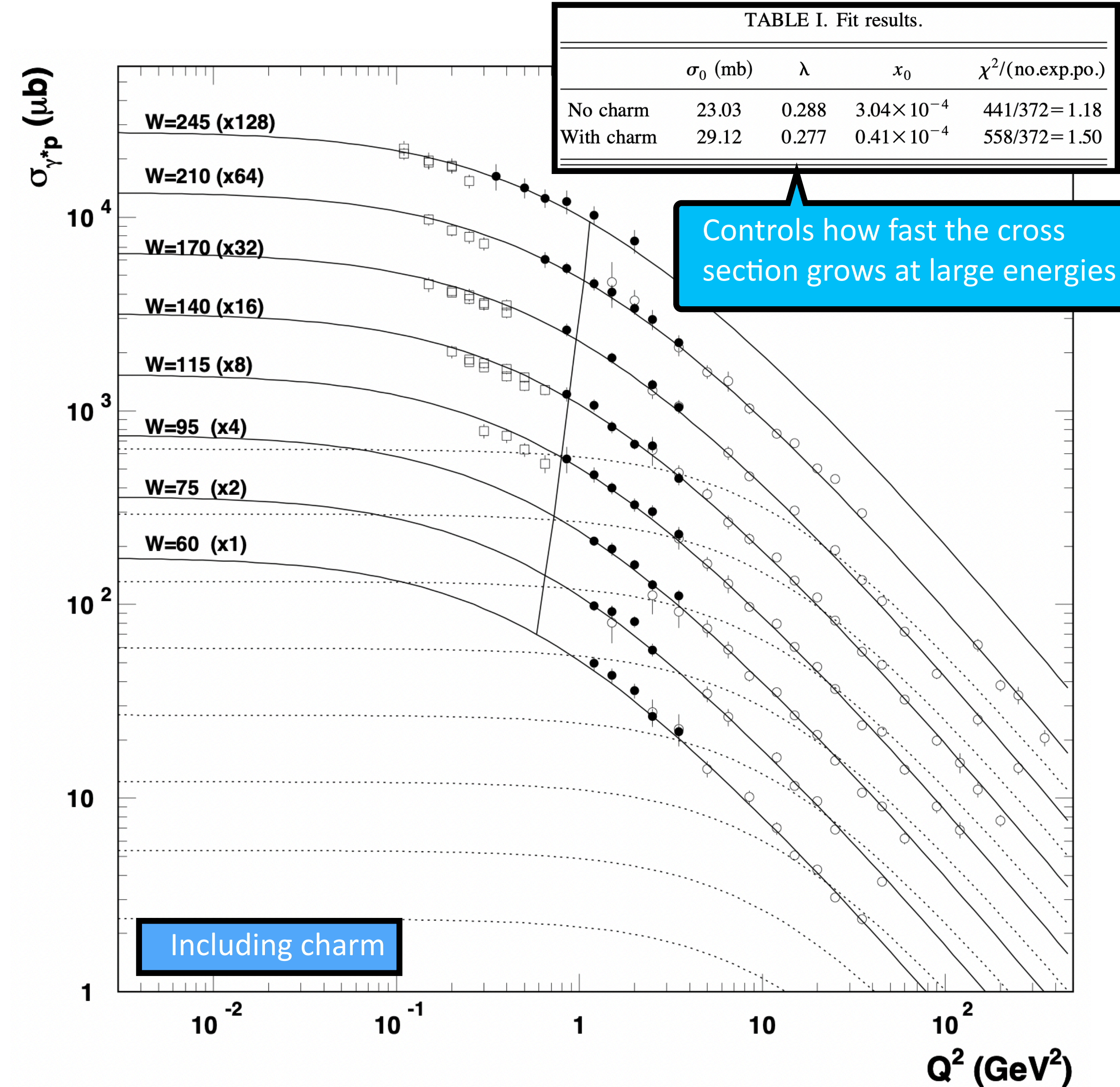
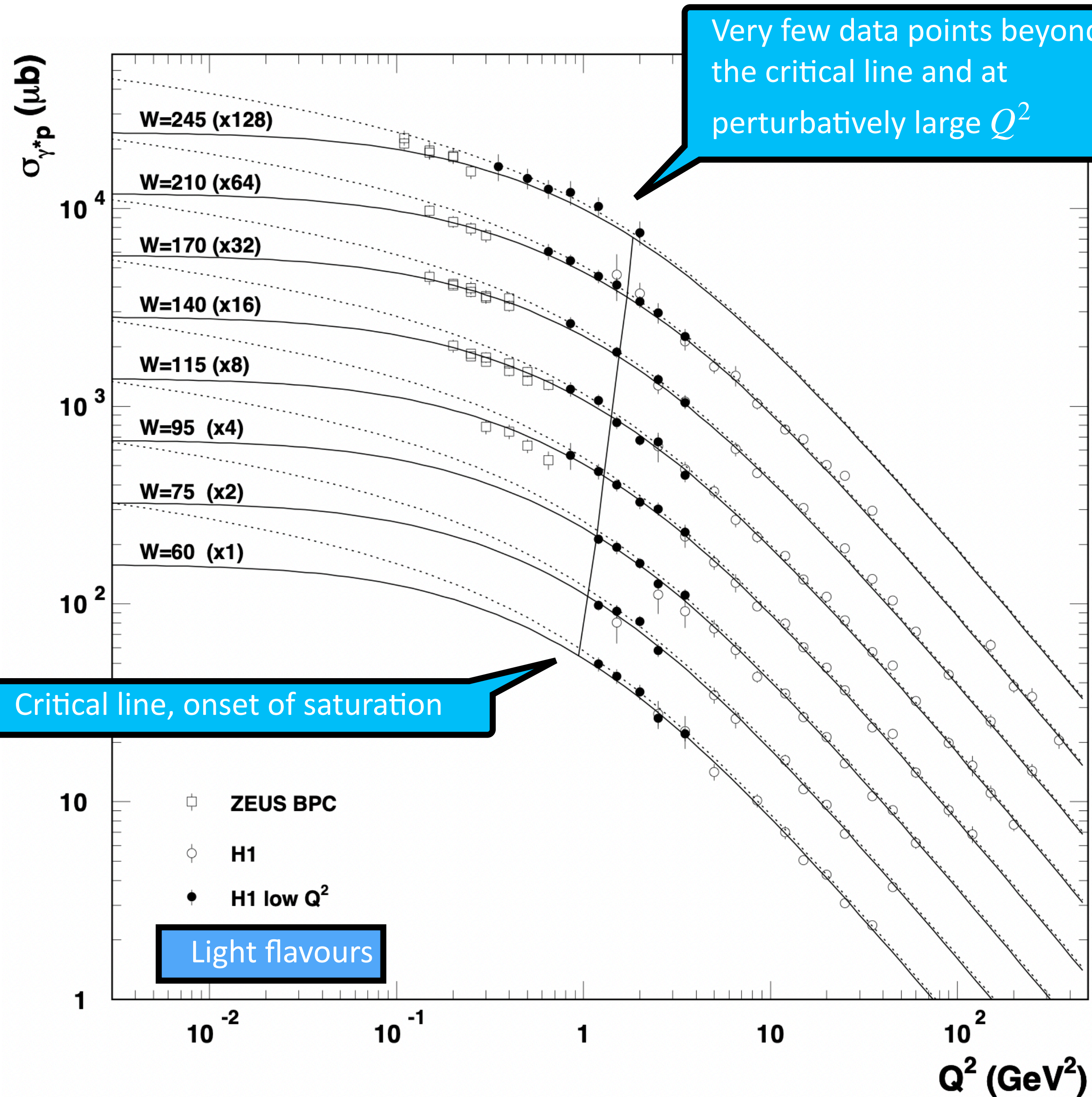
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The GBW model introduced a new scale
Can we use it?

Geometric scaling

2001: Geometric scaling. (1) The formalism

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We observe that the saturation model of deep inelastic scattering predicts a geometric scaling of the total $\gamma^* p$ cross section in the region of small Bjorken variable x . The geometric scaling in this case means that the cross section is a function of only one dimensionless variable $\tau = Q^2 R_0^2(x)$, where the function $R_0(x)$ decreases with decreasing x . We show that the experimental data from HERA in the region $x < 0.01$ confirm the expectations of this scaling over a very broad region of Q^2 . We suggest that the geometric scaling is more general than the saturation model.

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We observe that the saturation model of deep inelastic scattering predicts a geometric scaling of the total $\gamma^* p$ cross section in the region of small Bjorken variable x . The geometric scaling in this case means that the cross section is a function of only one dimensionless variable $\tau = Q^2 R_0^2(x)$, where the function $R_0(x)$ decreases with decreasing x . We show that the experimental data from HERA in the region $x < 0.01$ confirm the expectations of this scaling over a very broad region of Q^2 . We suggest that the geometric scaling is more general than the saturation model.

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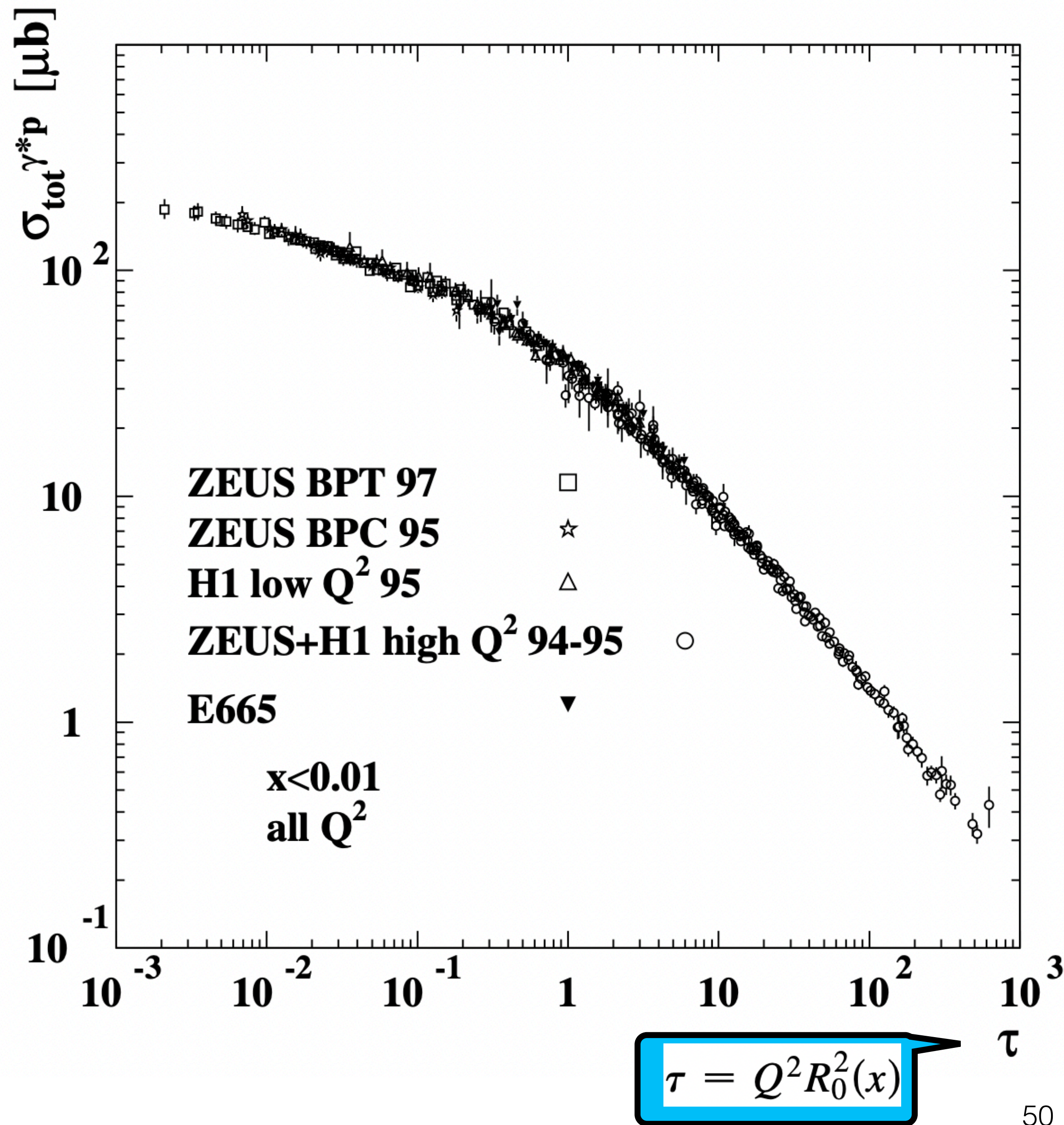
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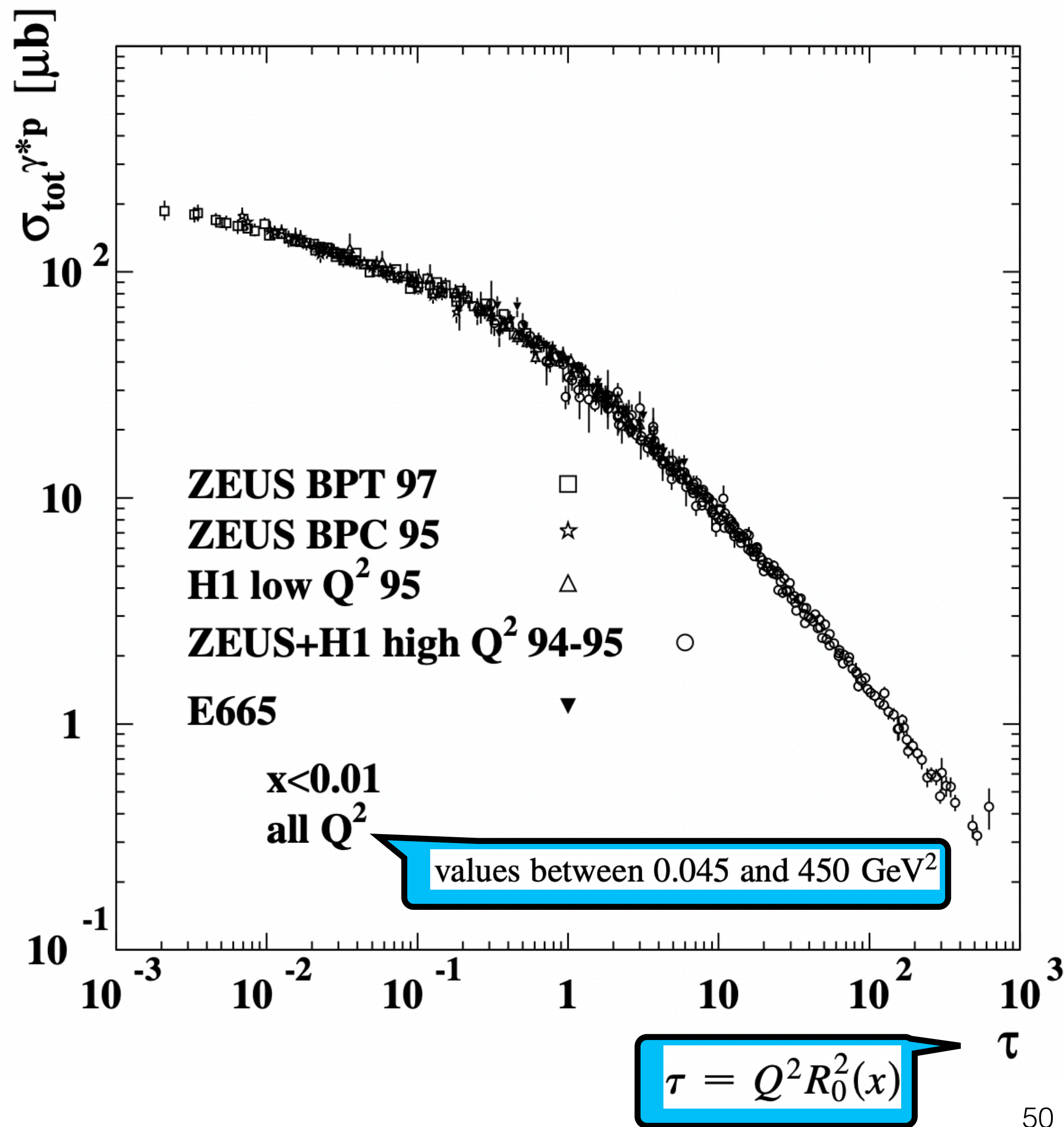
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Really?

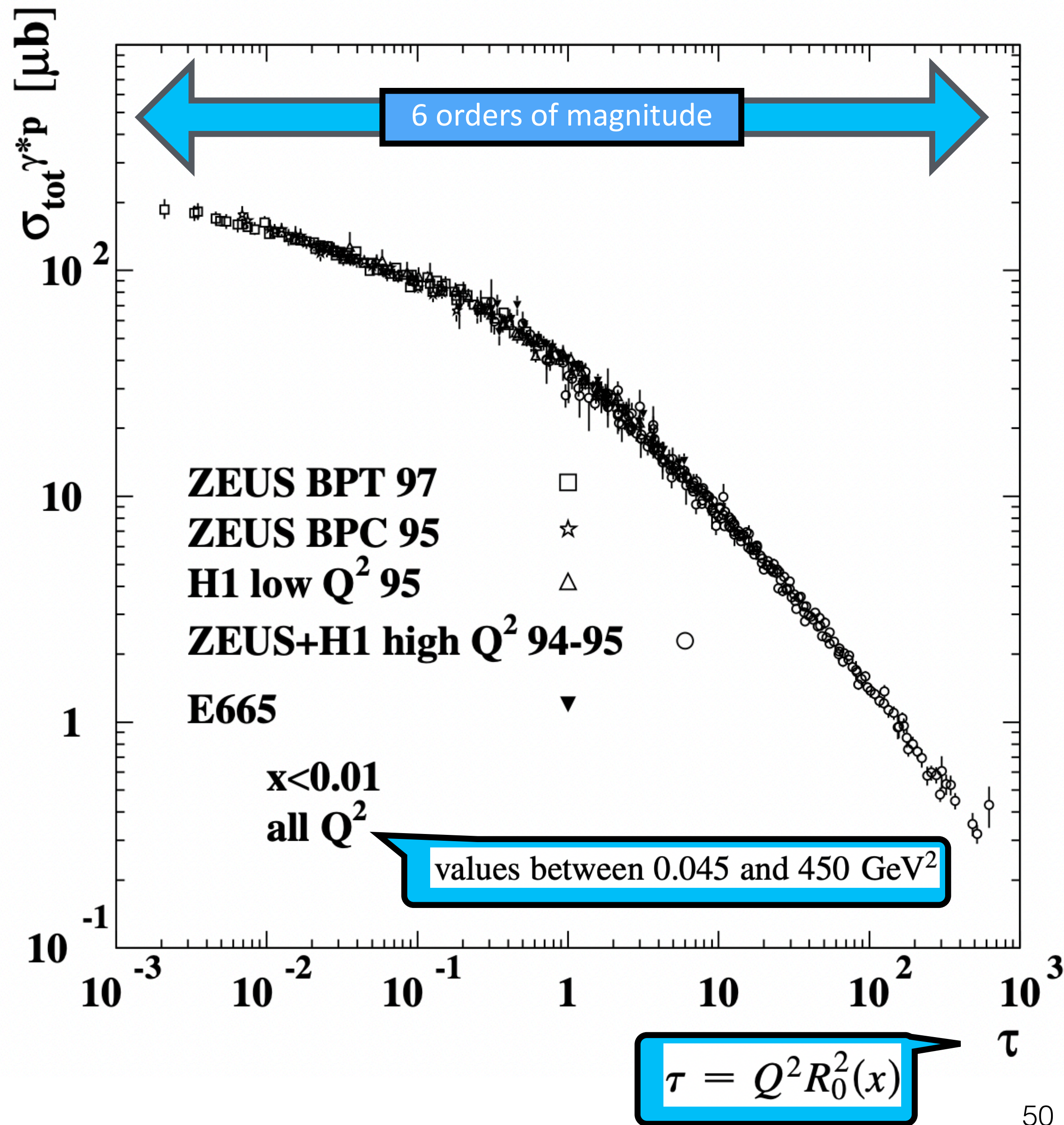
Stasto, Golec-Biernat, Kwiecinski, <http://inspirehep.net/record/530453>



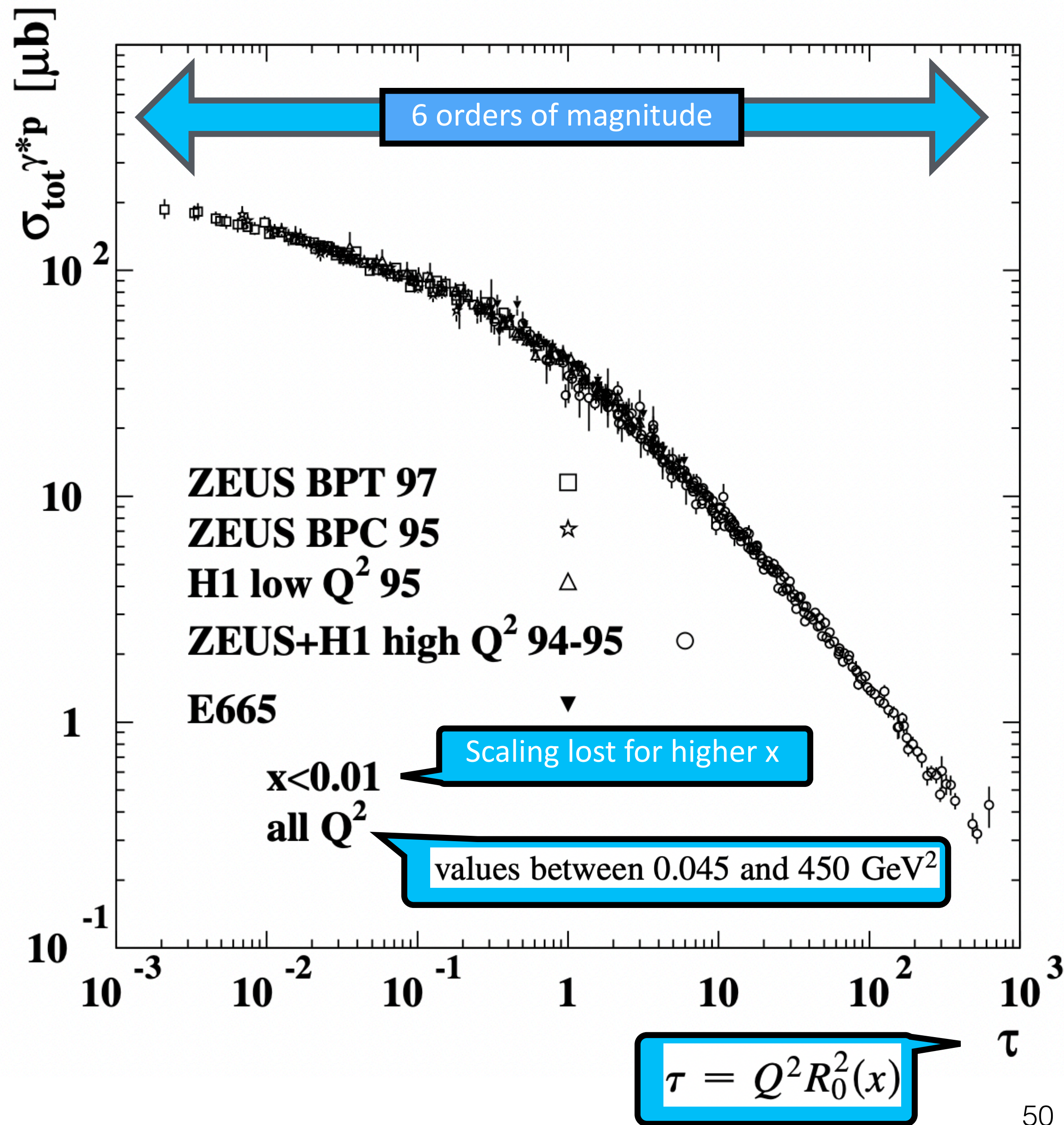
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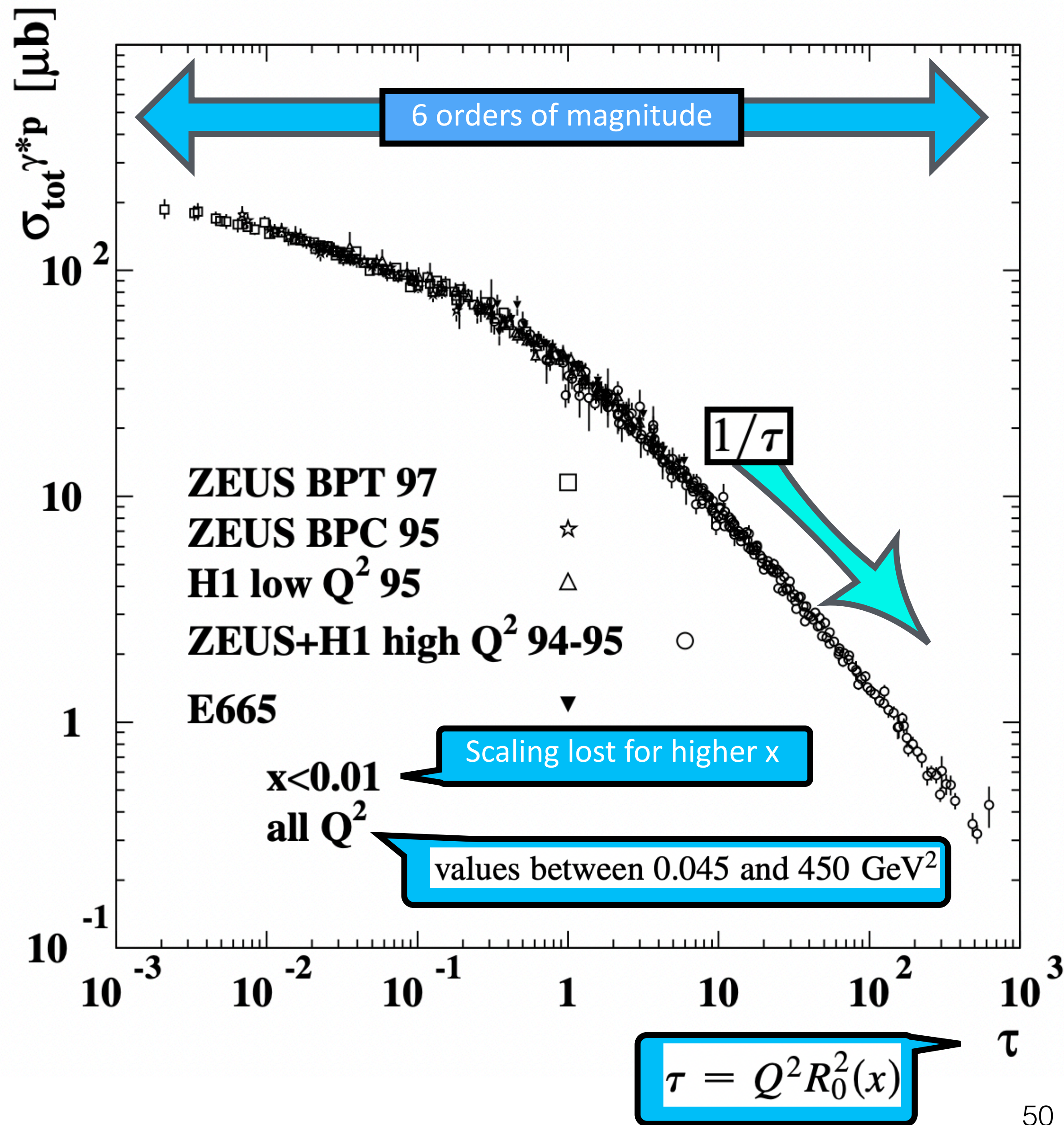
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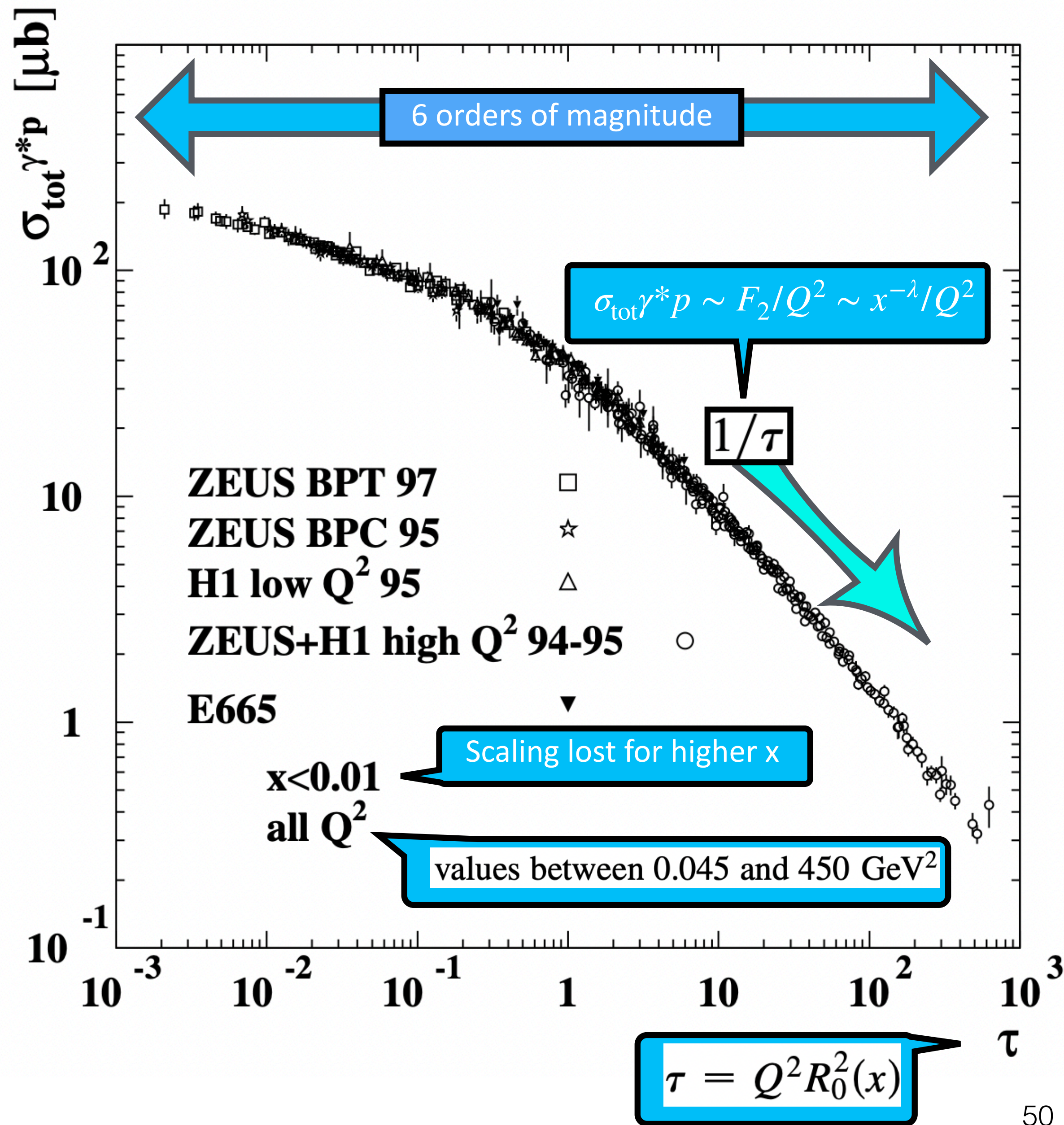
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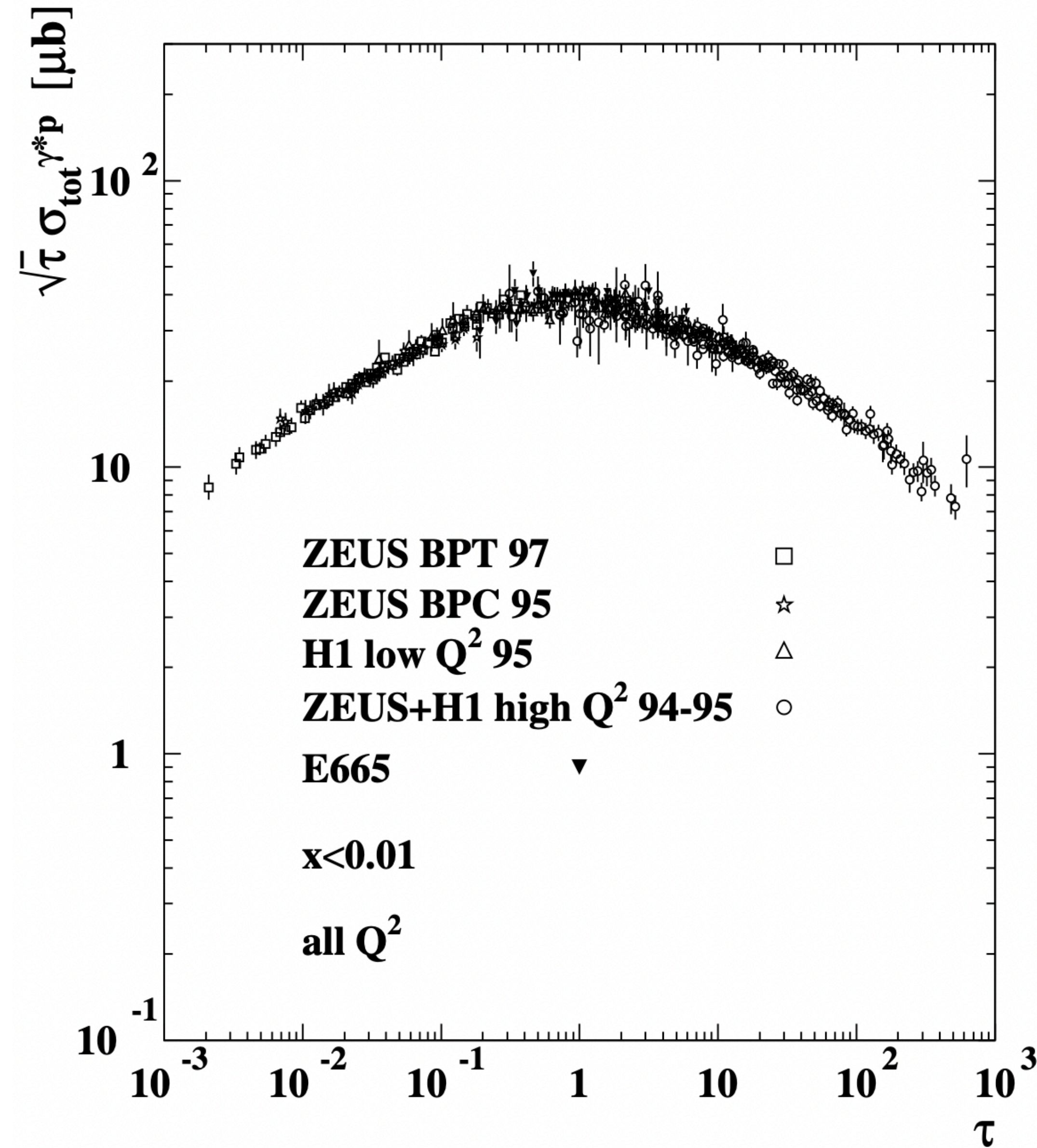
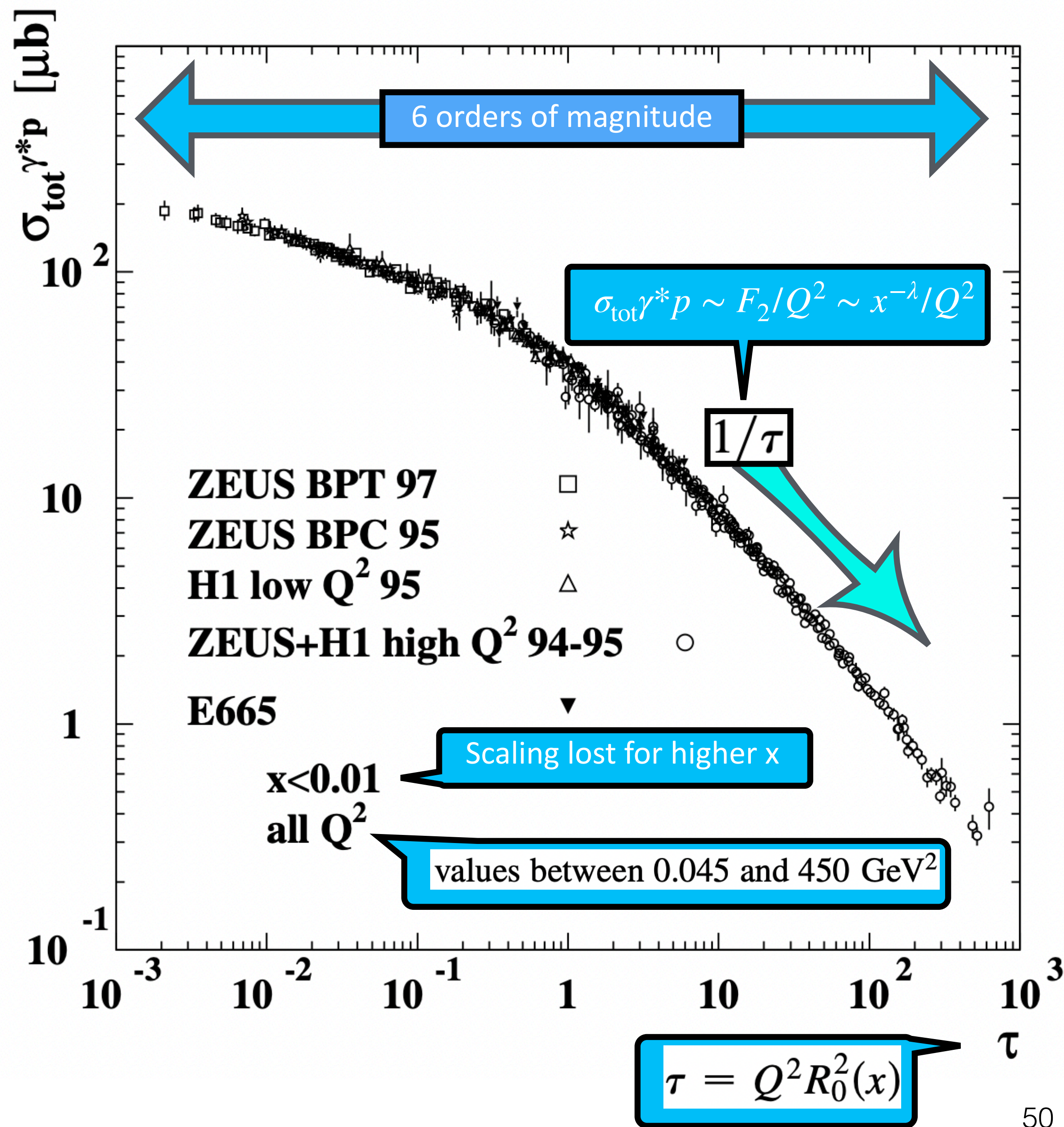


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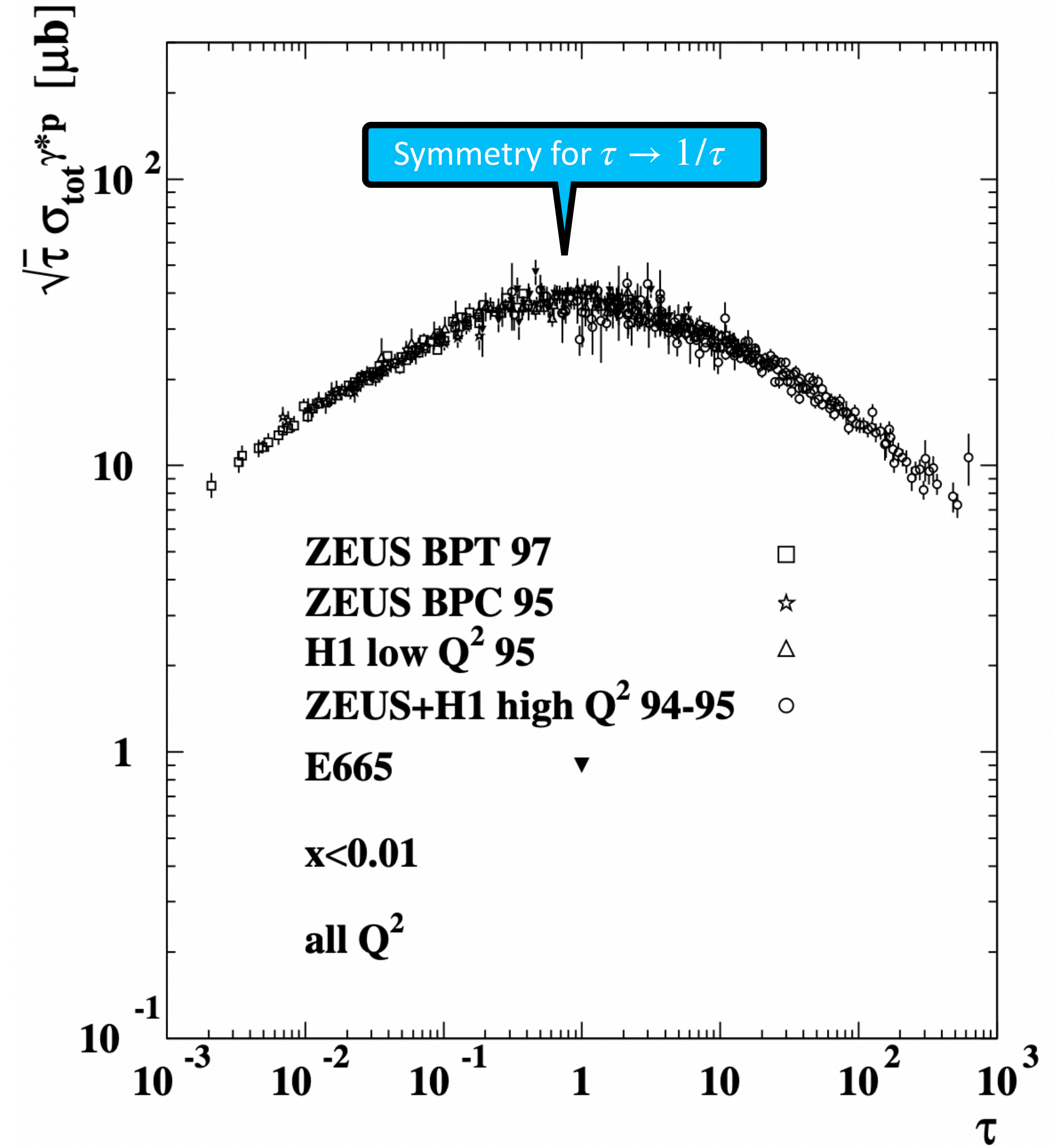
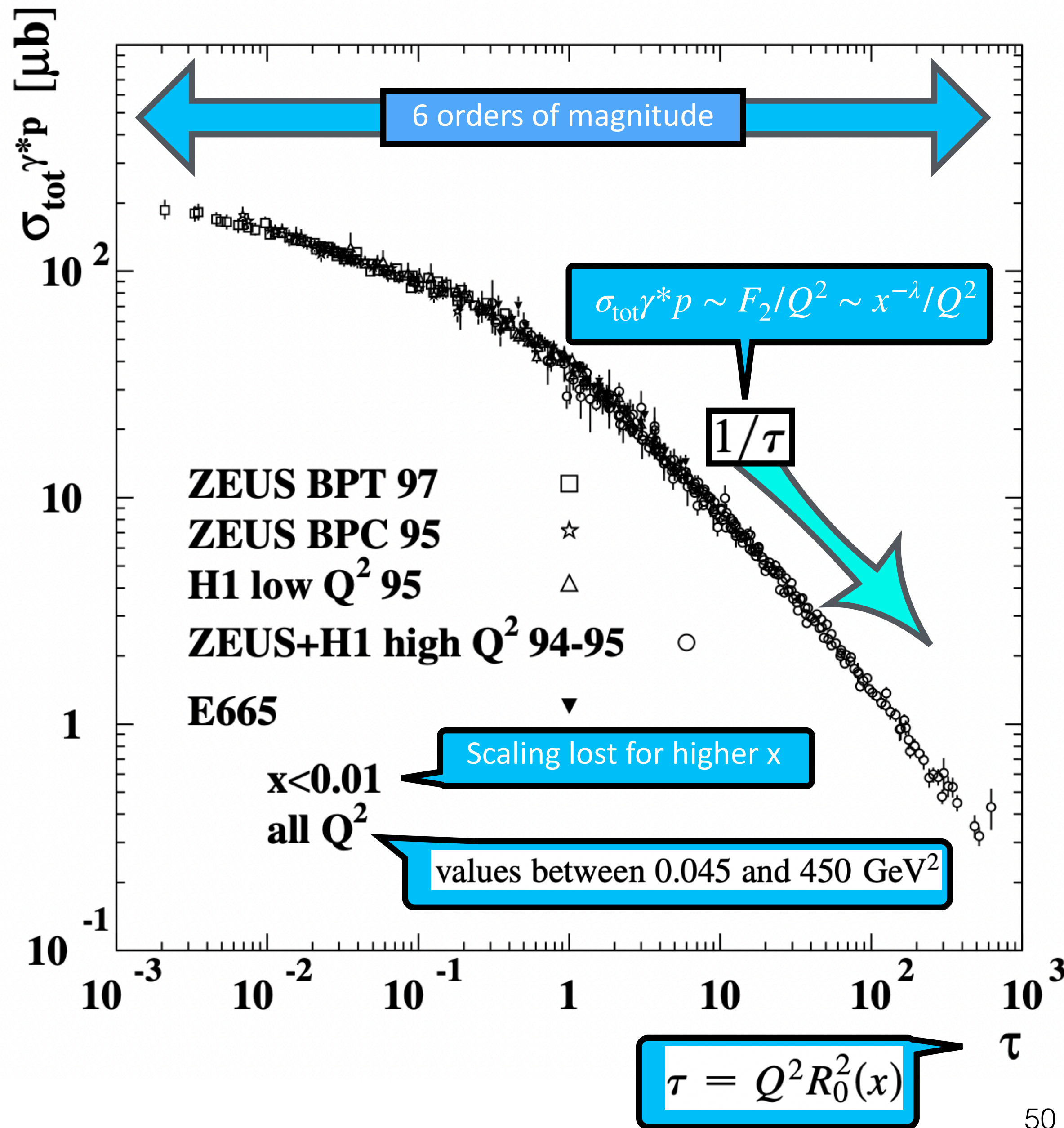


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Up to now, we have mainly used inclusive observables to study high-energy QCD
(The exception was to look at two-jet events to 'see' the gluon directly)
Which observables are particularly sensitive to the gluon distribution at high energies?

4

Exploring high-energy QCD: Diffractive vector meson production at HERA

At this point in time, we know that at small Bjorken- x the DIS cross section rises as a power law at high energies, we also know that this rise is driven by the gluon PDF.
We want now to concentrate in one process that is particularly sensitive to the gluon structure of hadrons

Diffractive vector meson photoproduction

Two experimentally important vector mesons

EVIDENCE FOR A π - π RESONANCE IN THE $I=1, J=1$ STATE*

A. R. Erwin, R. March, W. D. Walker, and E. West

Brookhaven National Laboratory, Upton, New York and University of Wisconsin, Madison, Wisconsin
(Received May 11, 1961)

<https://inspirehep.net/literature/28197>
<https://inspirehep.net/literature/48851>

The $\rho(770)$

- ✓ Discovered in 1961
- ✓ Decays mainly to $\pi\pi$ pairs
- ✓ Large width, strong interference with continuum

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P. SÖDING

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The J/ψ (mass $3.097 \text{ GeV}/c^2$)

- ✓ Discovered in 1974 (November revolution)
- ✓ Useful decays into lepton pairs
- ✓ Very small width (clean signature)

Experimental Observation of a Heavy Particle J^\dagger

J. J. Aubert, U. Becker, P. J. Biggs, J. Burger, M. Chen, G. Everhart, P. Goldhagen, J. Leong, T. McCorrison, T. G. Rhoades, M. Rohde, Samuel C. C. Ting, and Sau Lan Wu
Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139

and

Y. Y. Lee

Brookhaven National Laboratory, Upton, New York 11973
(Received 12 November 1974)

Discovery of a Narrow Resonance in e^+e^- Annihilation*

J.-E. Augustin,† A. M. Boyarski, M. Breidenbach, F. Bulos, J. T. Dakin, G. J. Feldman, G. E. Fischer, D. Fryberger, G. Hanson, B. Jean-Marie,† R. R. Larsen, V. Lüth, H. L. Lynch, D. Lyon, C. C. Morehouse, J. M. Paterson, M. L. Perl, B. Richter, P. Rapidis, R. F. Schwitters, W. M. Tanenbaum, and F. Vannucci‡

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305

and

G. S. Abrams, D. Briggs, W. Chinowsky, C. E. Friedberg, G. Goldhaber, R. J. Hollebeek, J. A. Kadyk, B. Lulu, F. Pierre,§ G. H. Trilling, J. S. Whitaker, J. Wiss, and J. E. Zipse

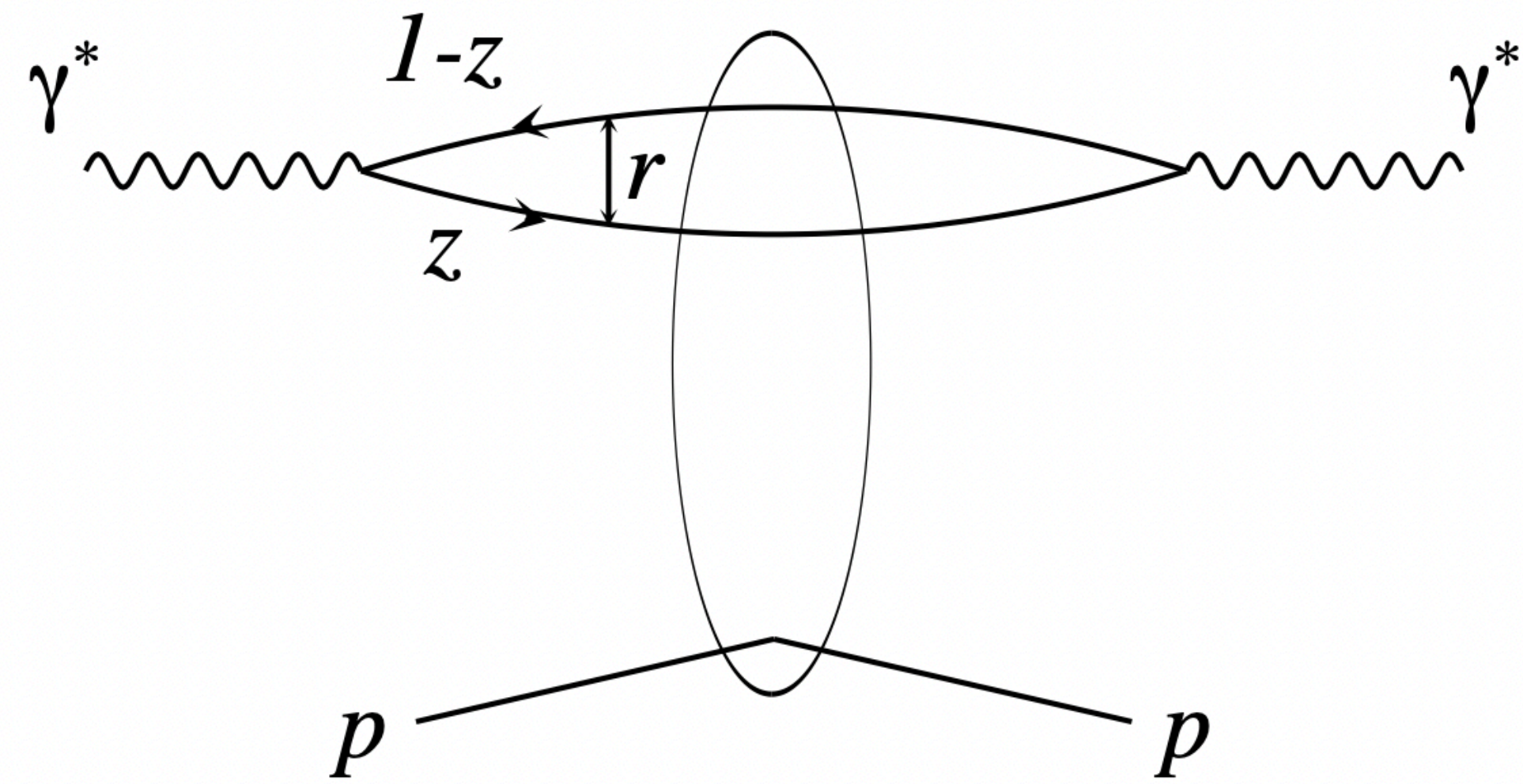
Lawrence Berkeley Laboratory and Department of Physics, University of California, Berkeley, California 94720
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<https://inspirehep.net/literature/90773>

<https://inspirehep.net/literature/91761>

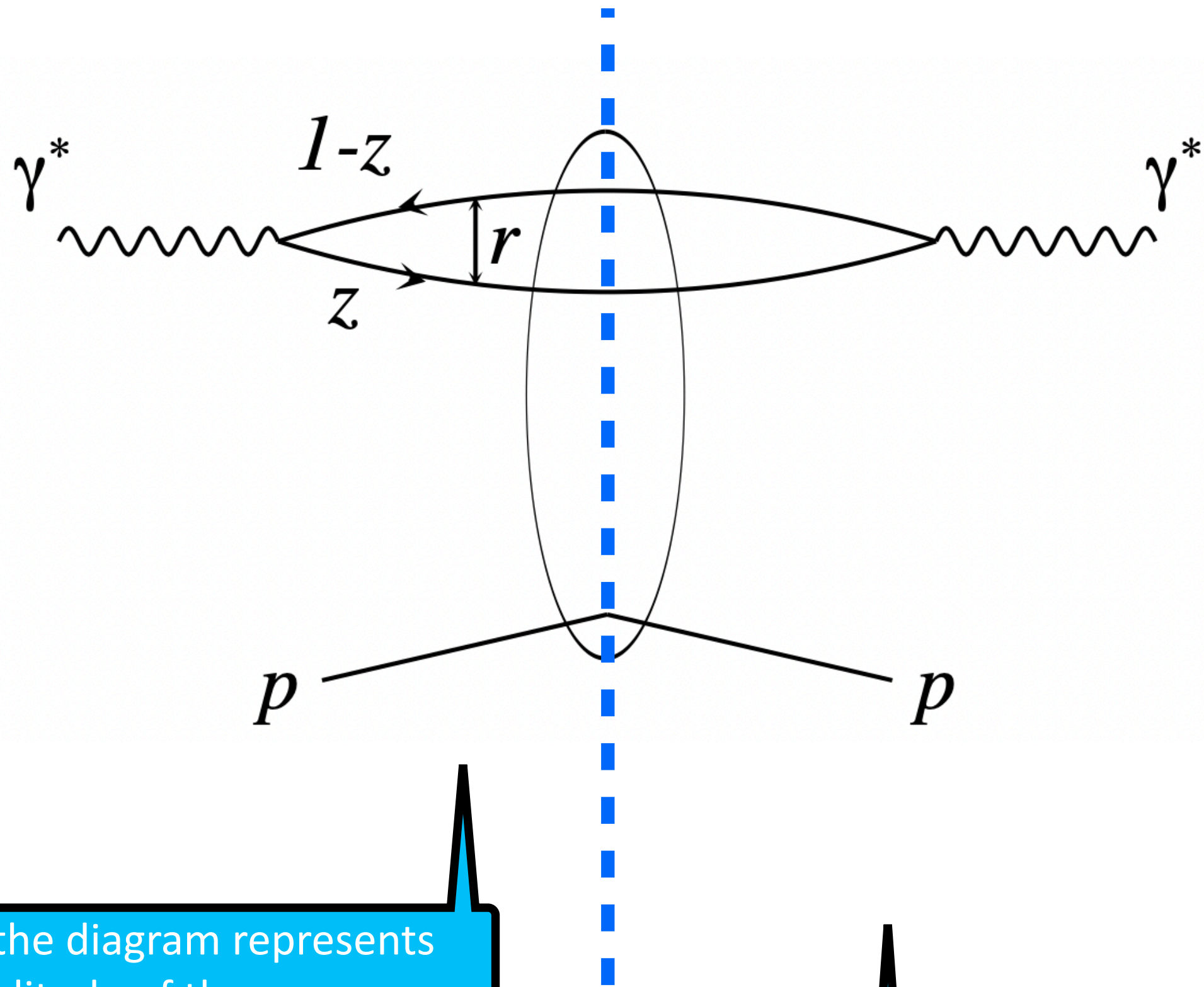
Diffractive vector meson production: a process close to DIS

A representation of the DIS cross section



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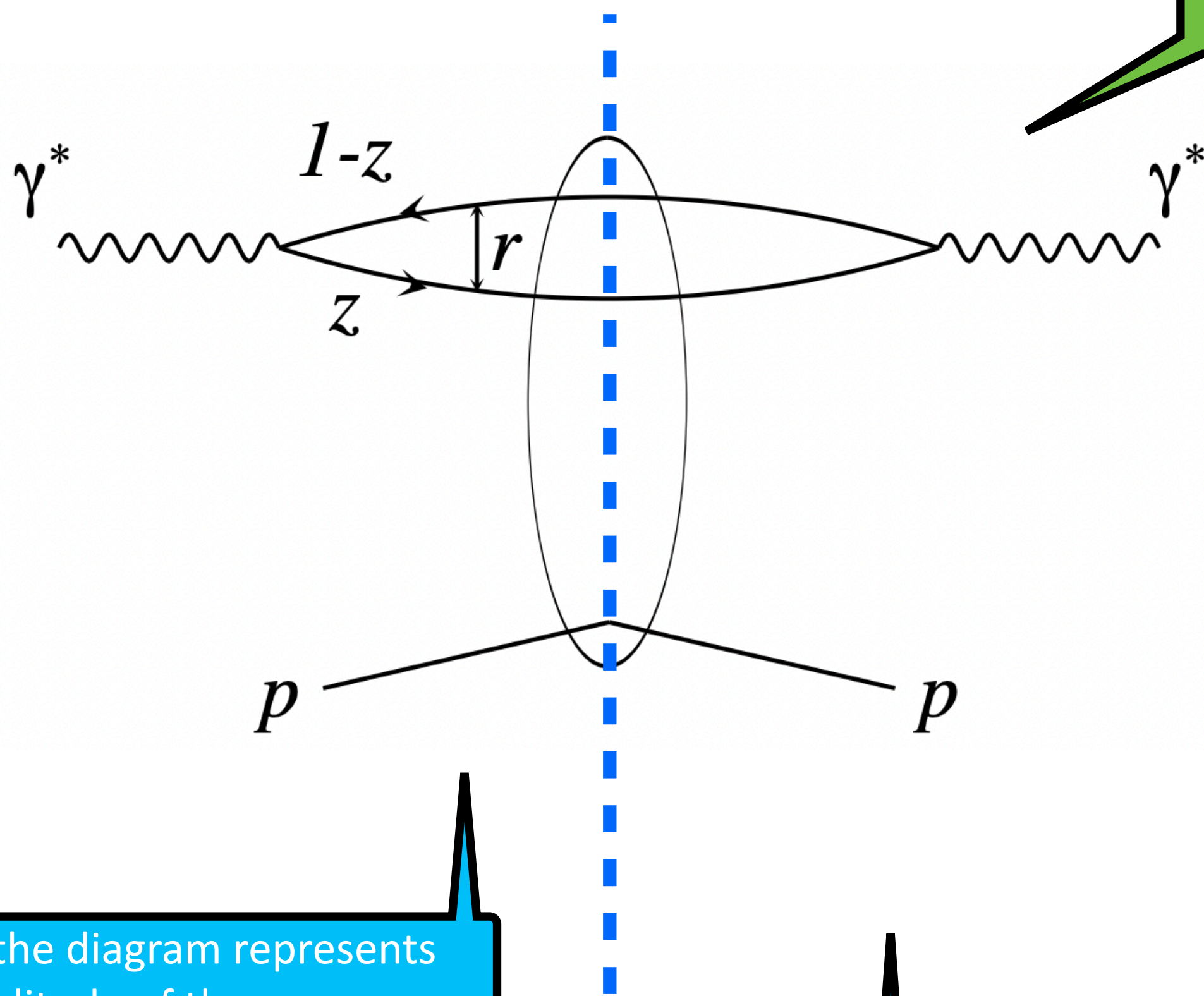
Half of the diagram represents the amplitude of the process

The other half the conjugate of the amplitude

Diffractive vector meson production: a process close to DIS

A representation of the DIS cross section

Now consider the full diagram to represent an amplitude, not a cross section ... then ...

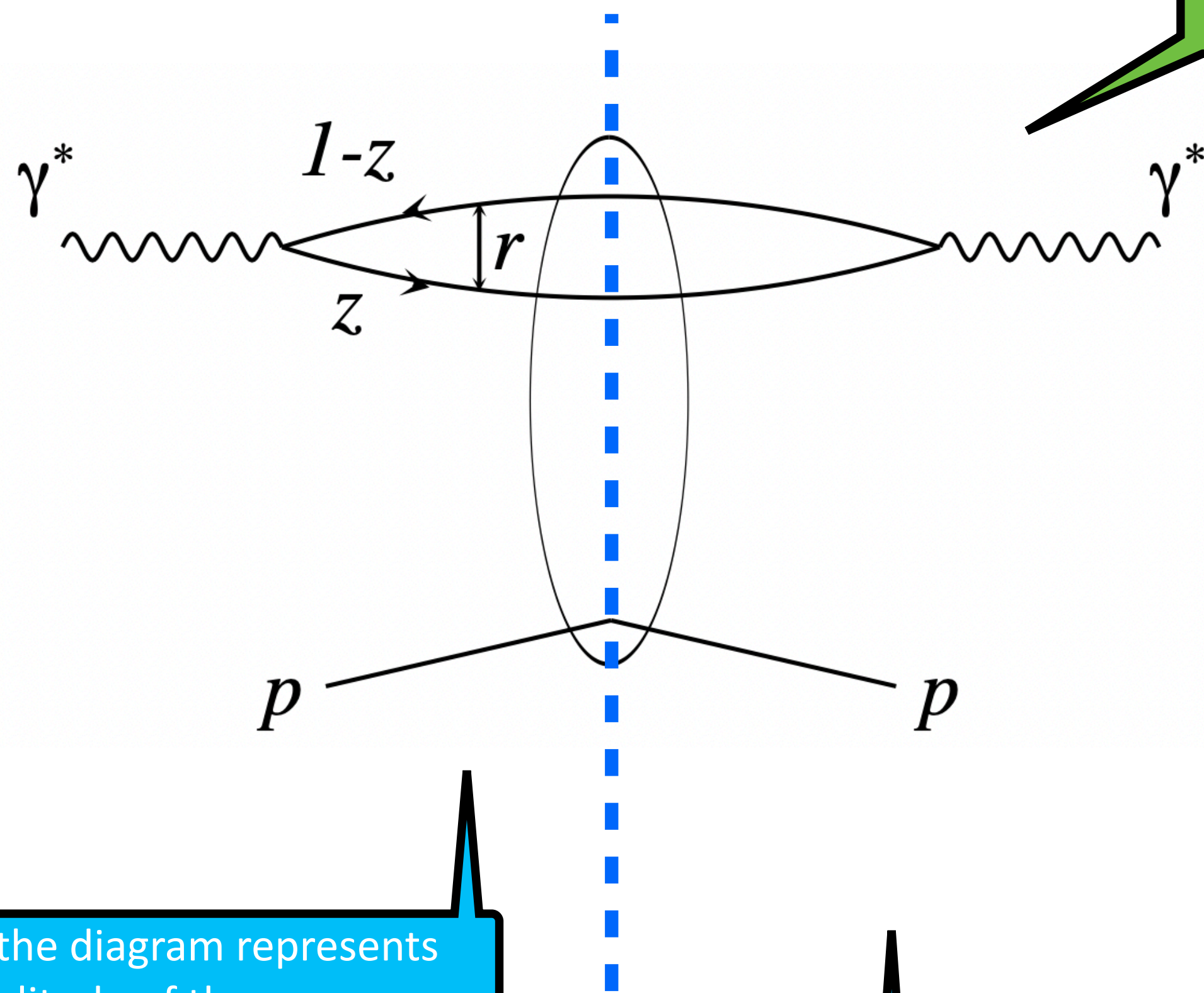


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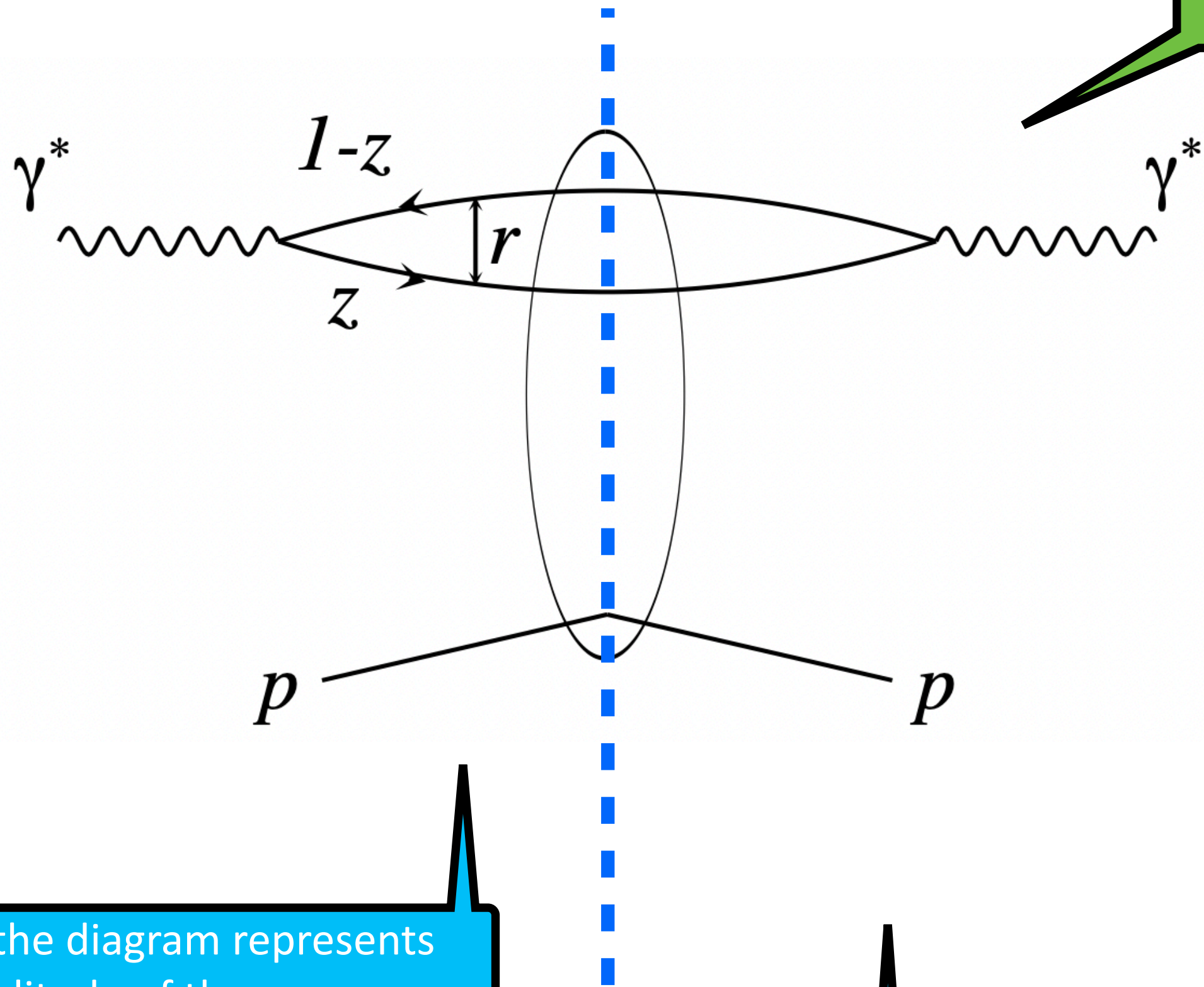
... exchange the photon for another particle with the same quantum numbers, e. g. a vector meson

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Diffractive vector meson production: a process close to DIS

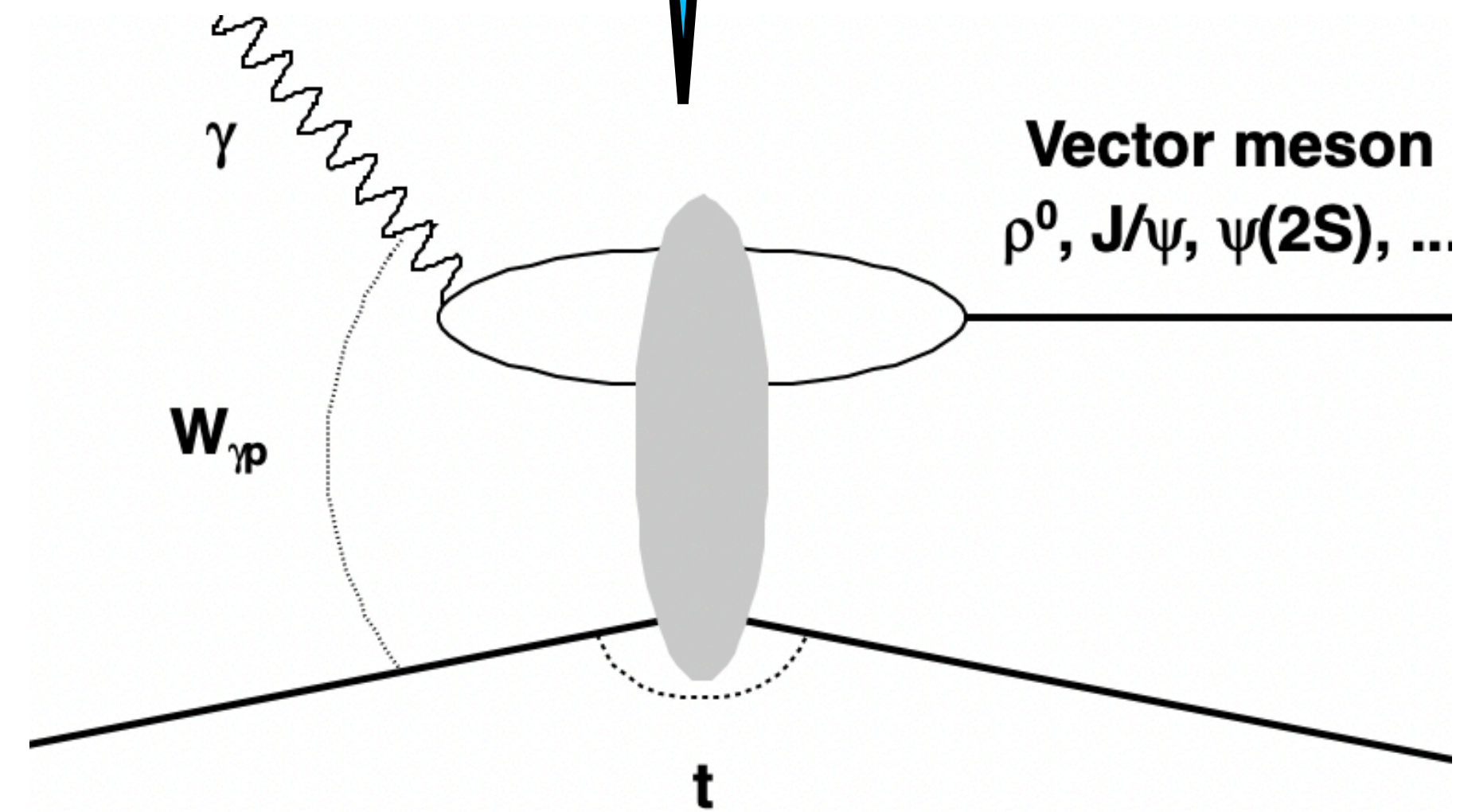
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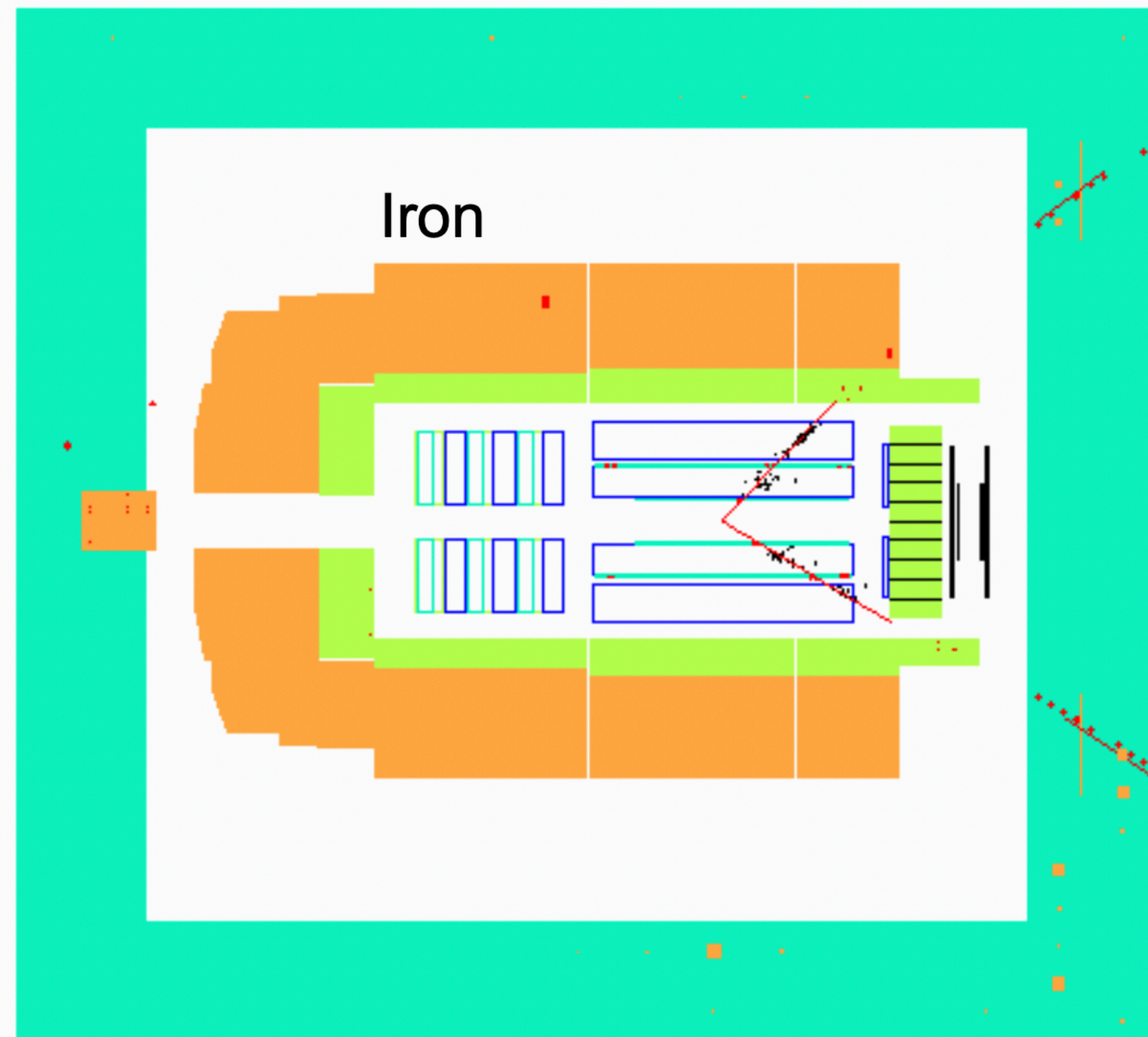
This would be a diffractive process where the protons remains intact after the interaction



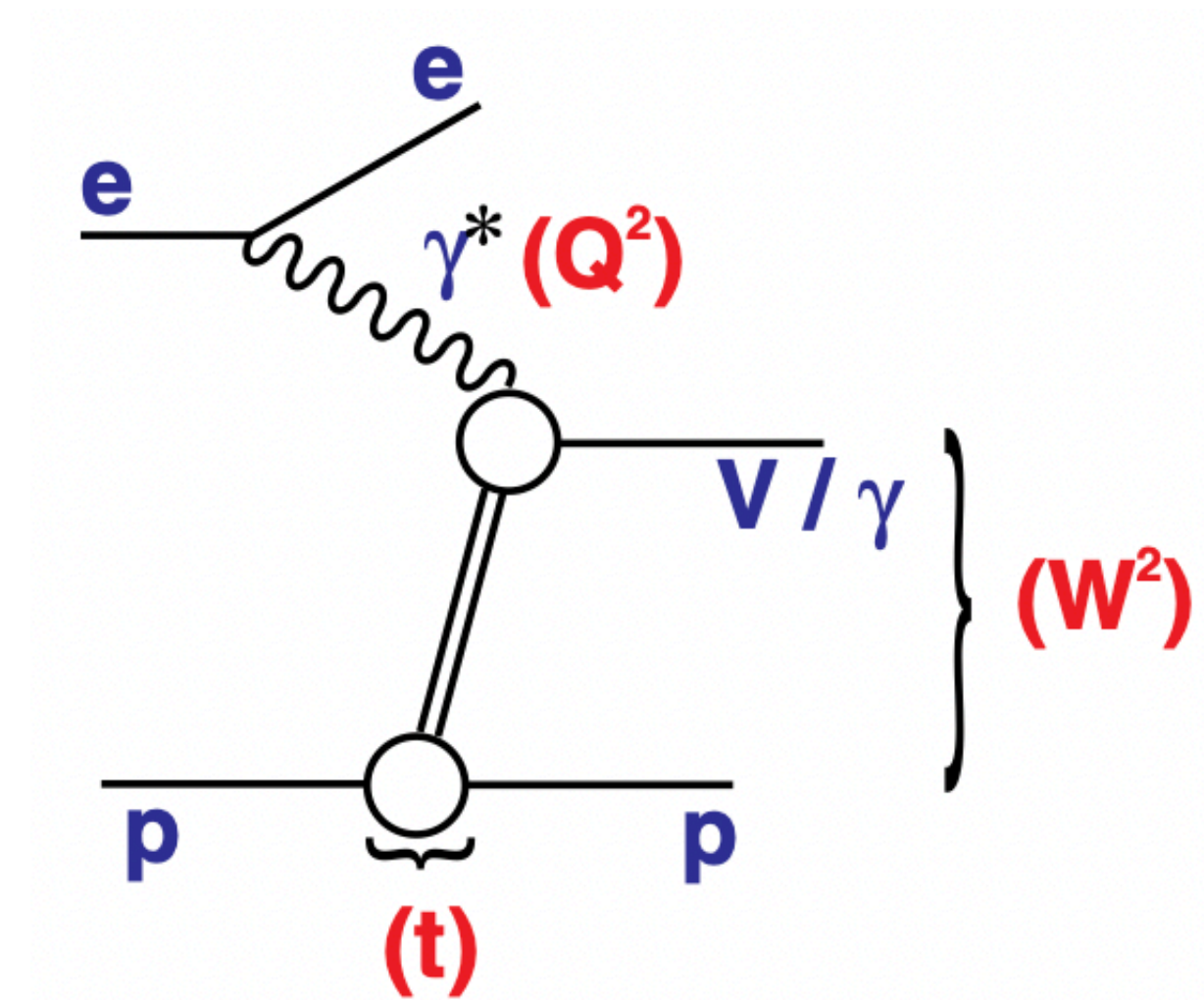
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Photoproduction $J/\Psi \rightarrow \mu \mu$

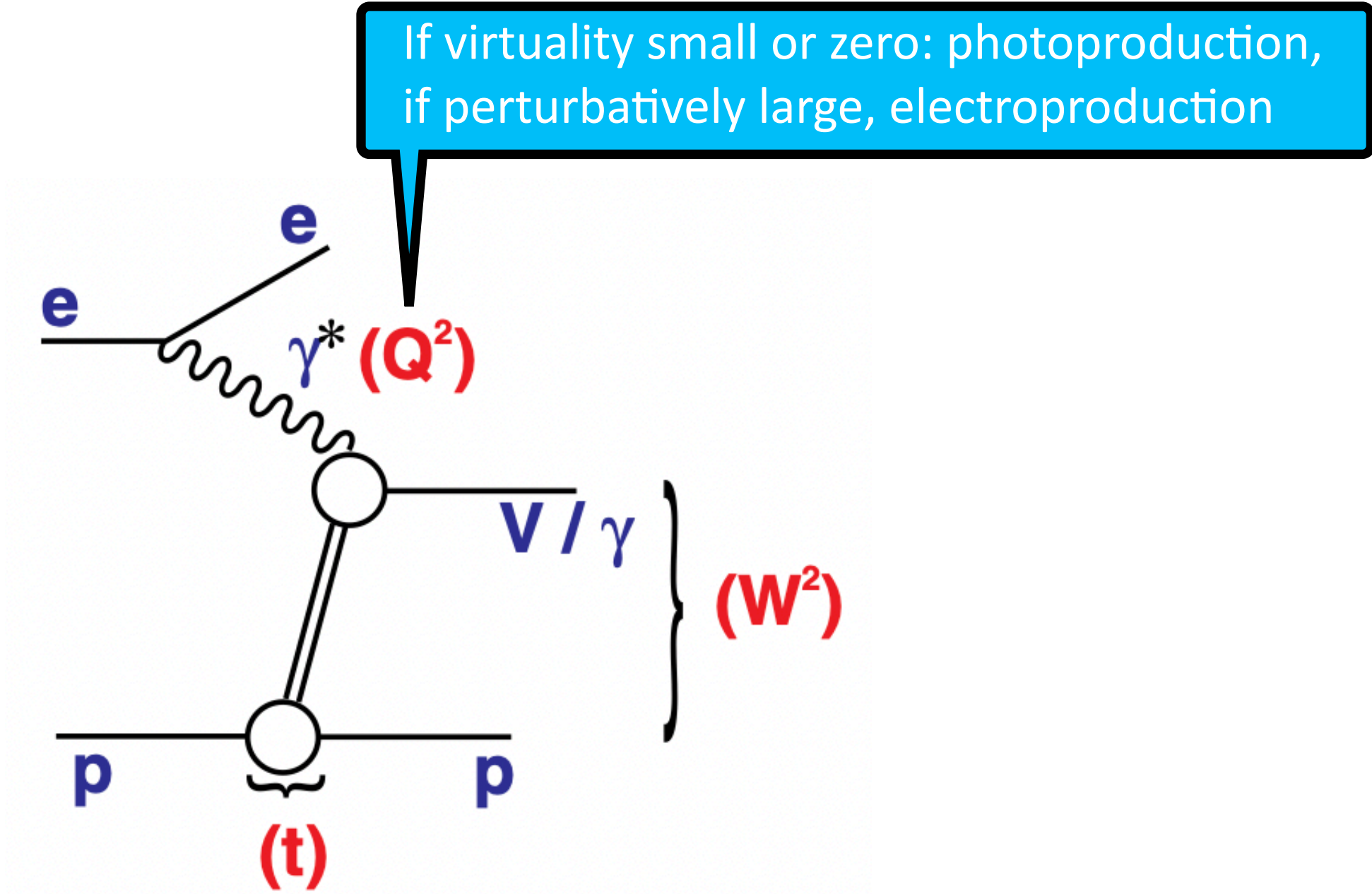


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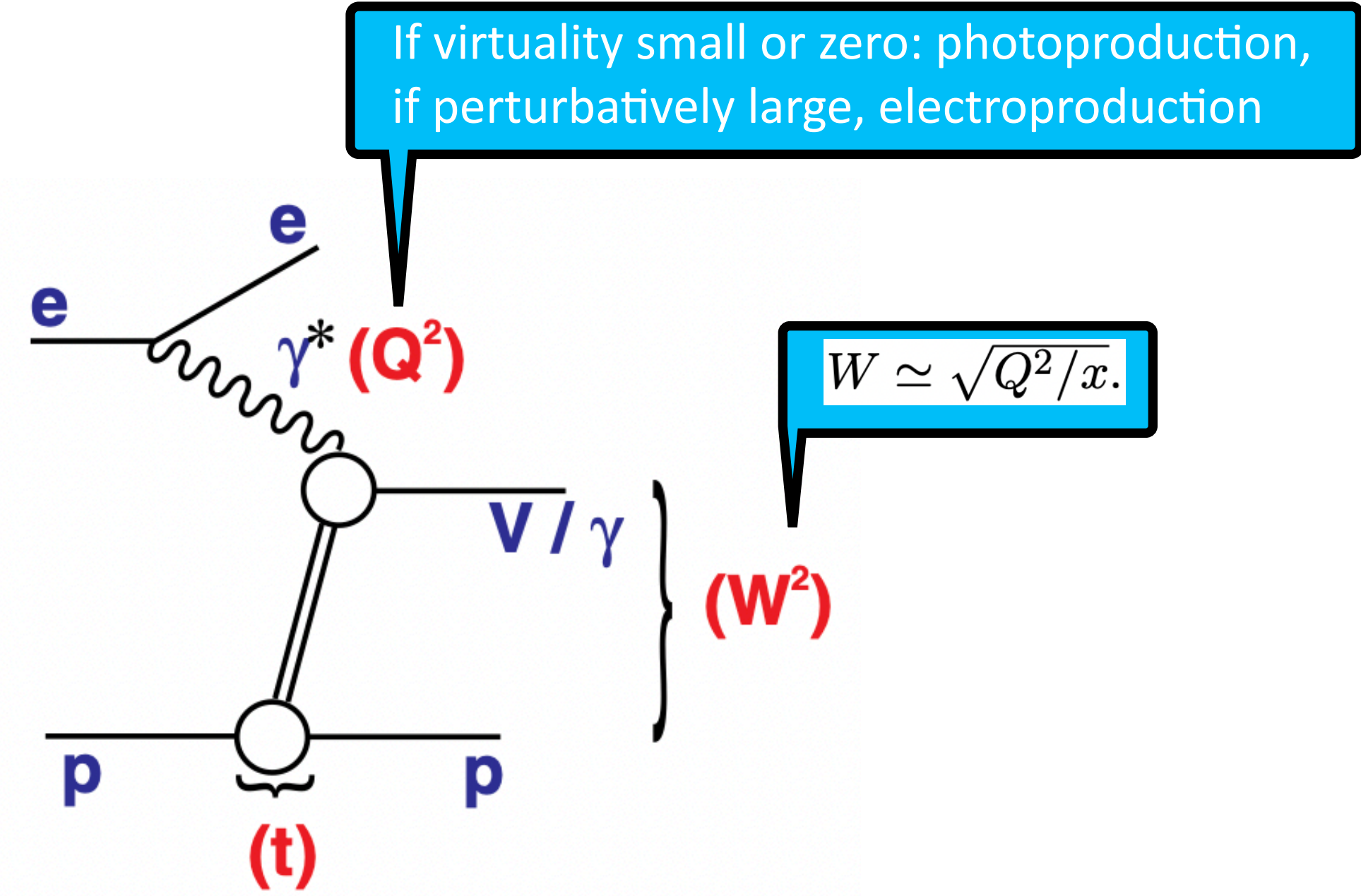
Newman, Wing, <https://inspirehep.net/literature/1247974>

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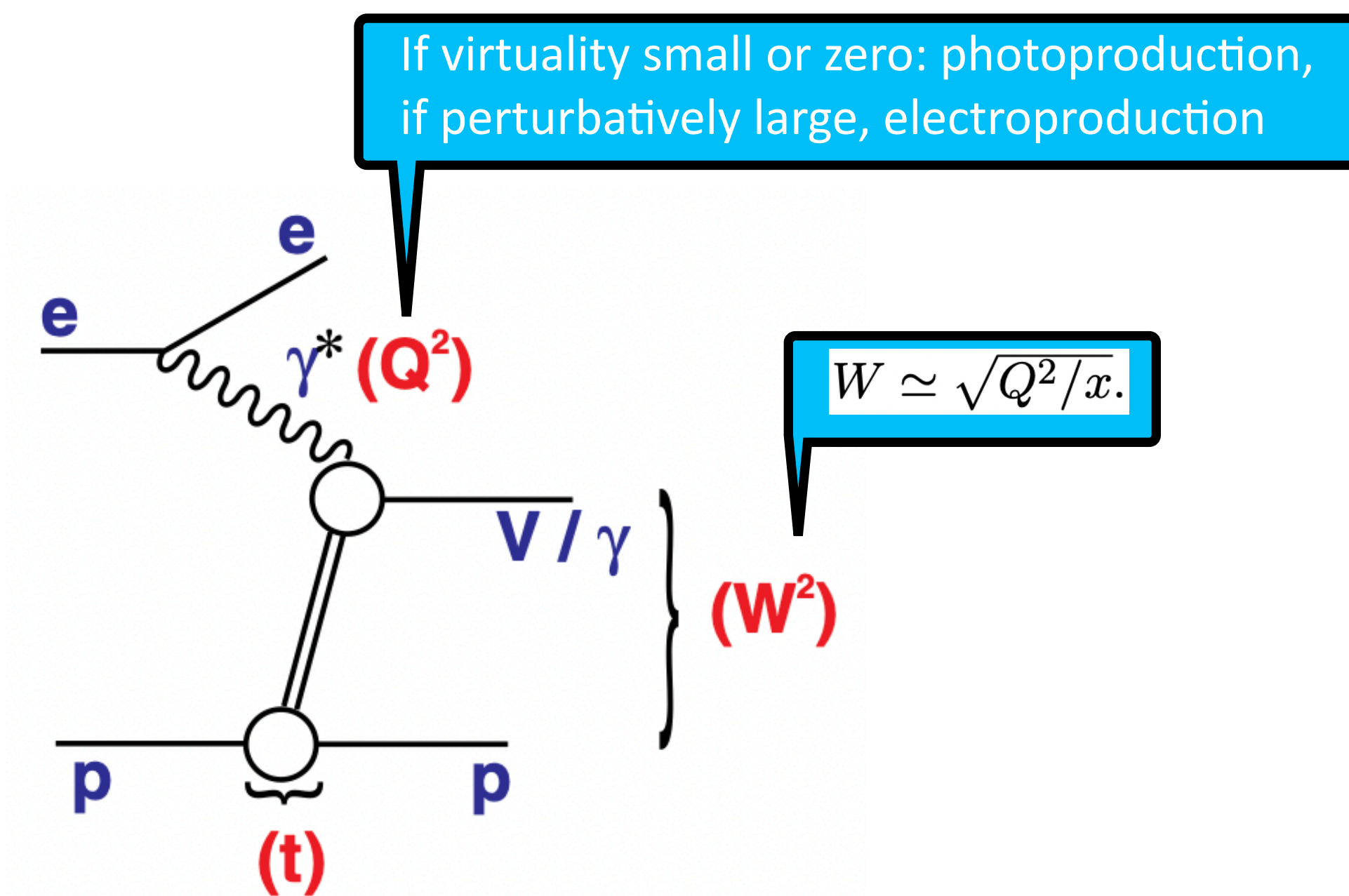
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Diffractive vector meson photoproduction



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Diffractive vector meson photoproduction



If virtuality small or zero: photoproduction, if perturbatively large, electroproduction

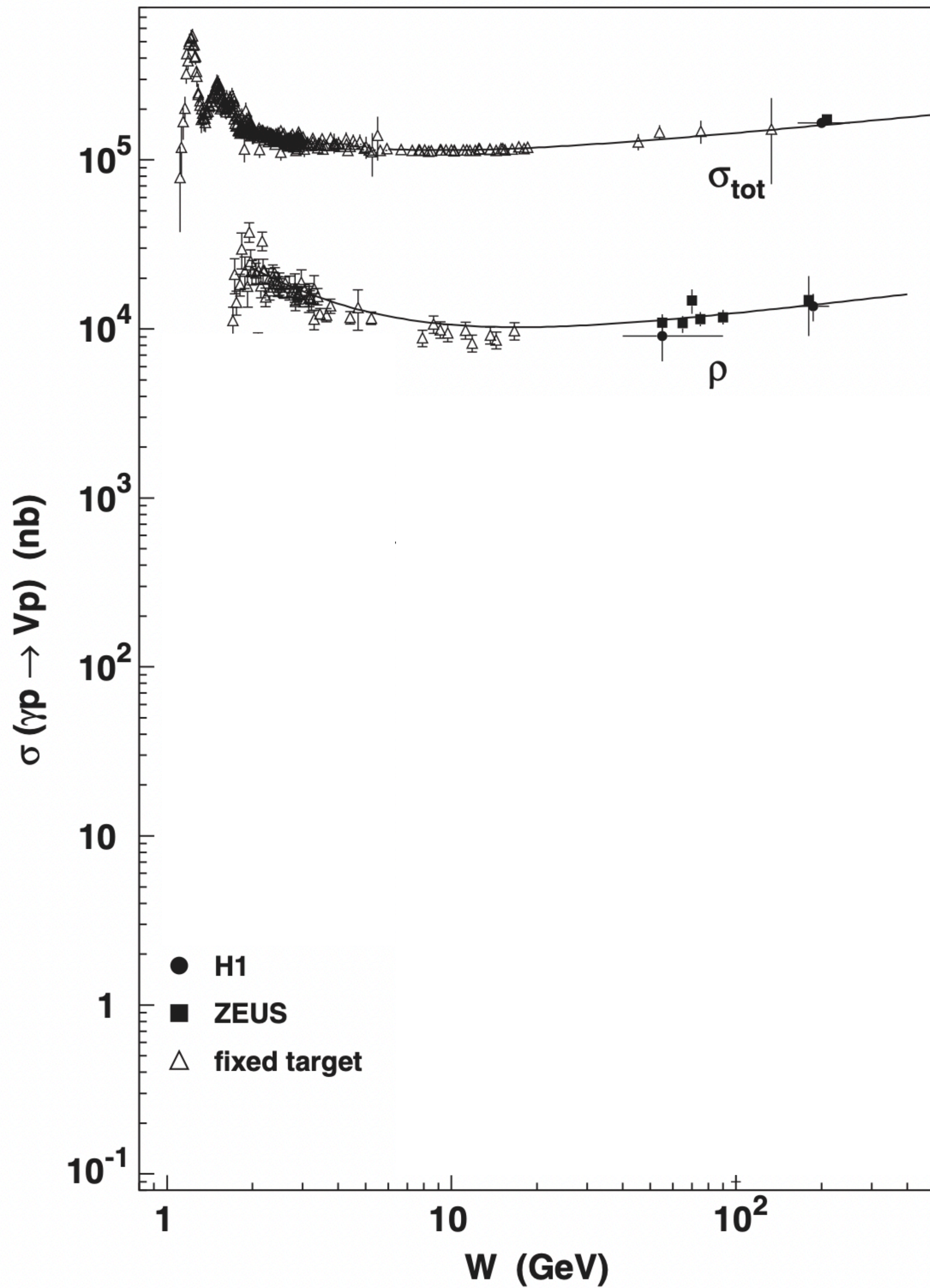
$$W \simeq \sqrt{Q^2/x}$$

Related, through a Fourier transform, to the distribution of colour fields in the transverse plane

Newman, Wing, <https://inspirehep.net/literature/1247974>

Guillermo Contreras, CTU in Prague

Diffractive vector meson photoproduction

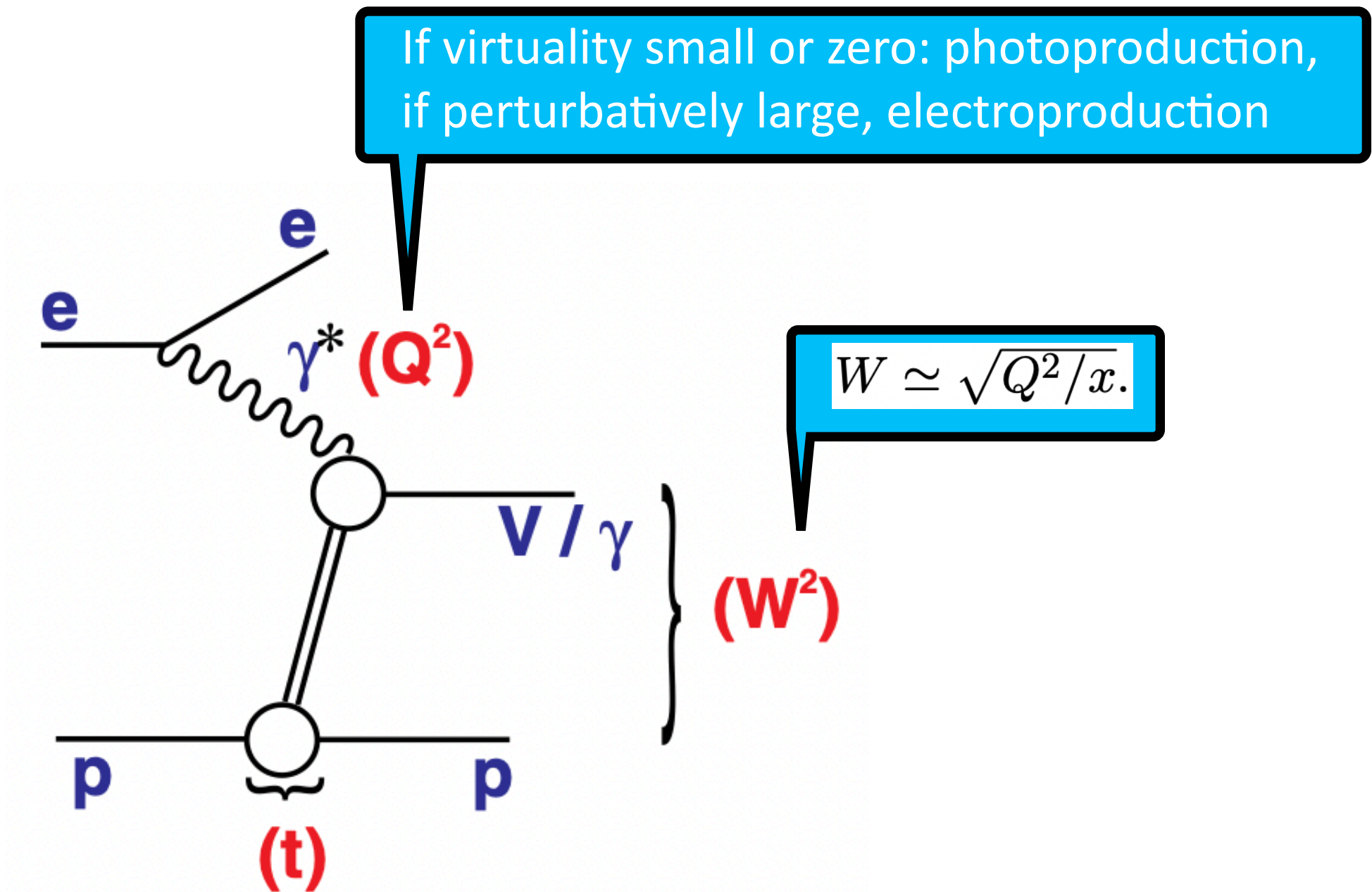


$W^{0.16}$

Total photoproduction cross section

$W^{0.22}$

$\rho(770)$ photoproduction cross section

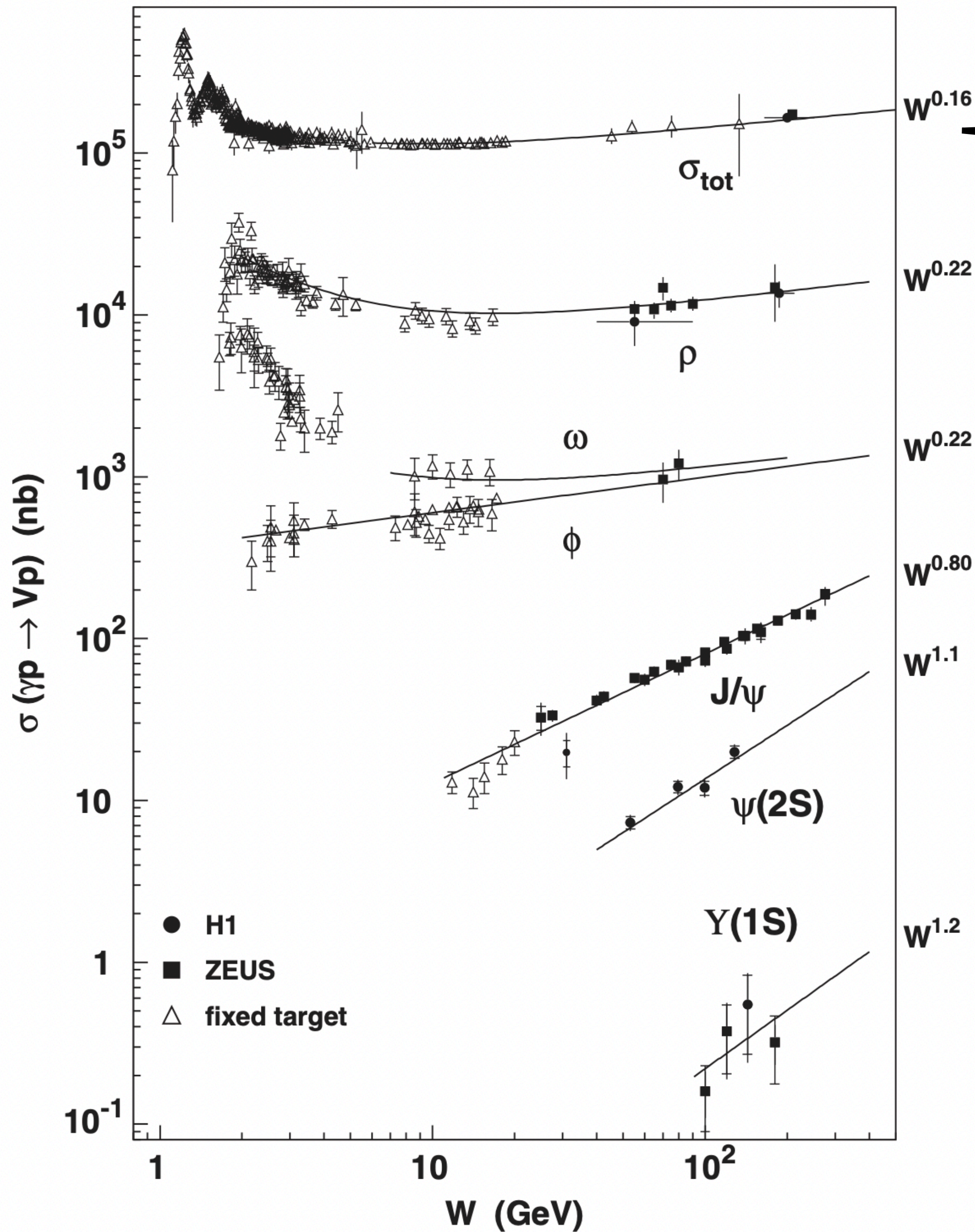


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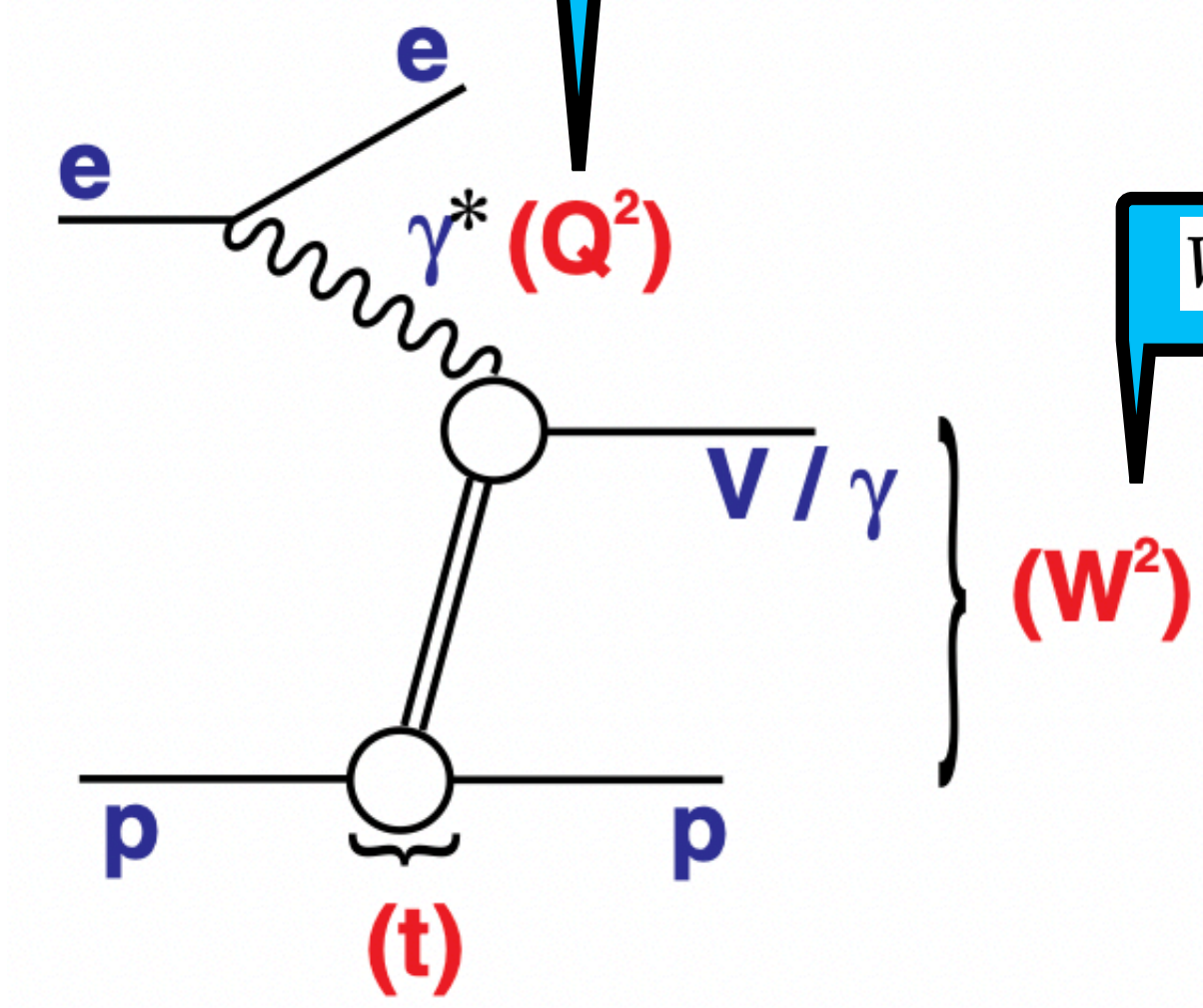
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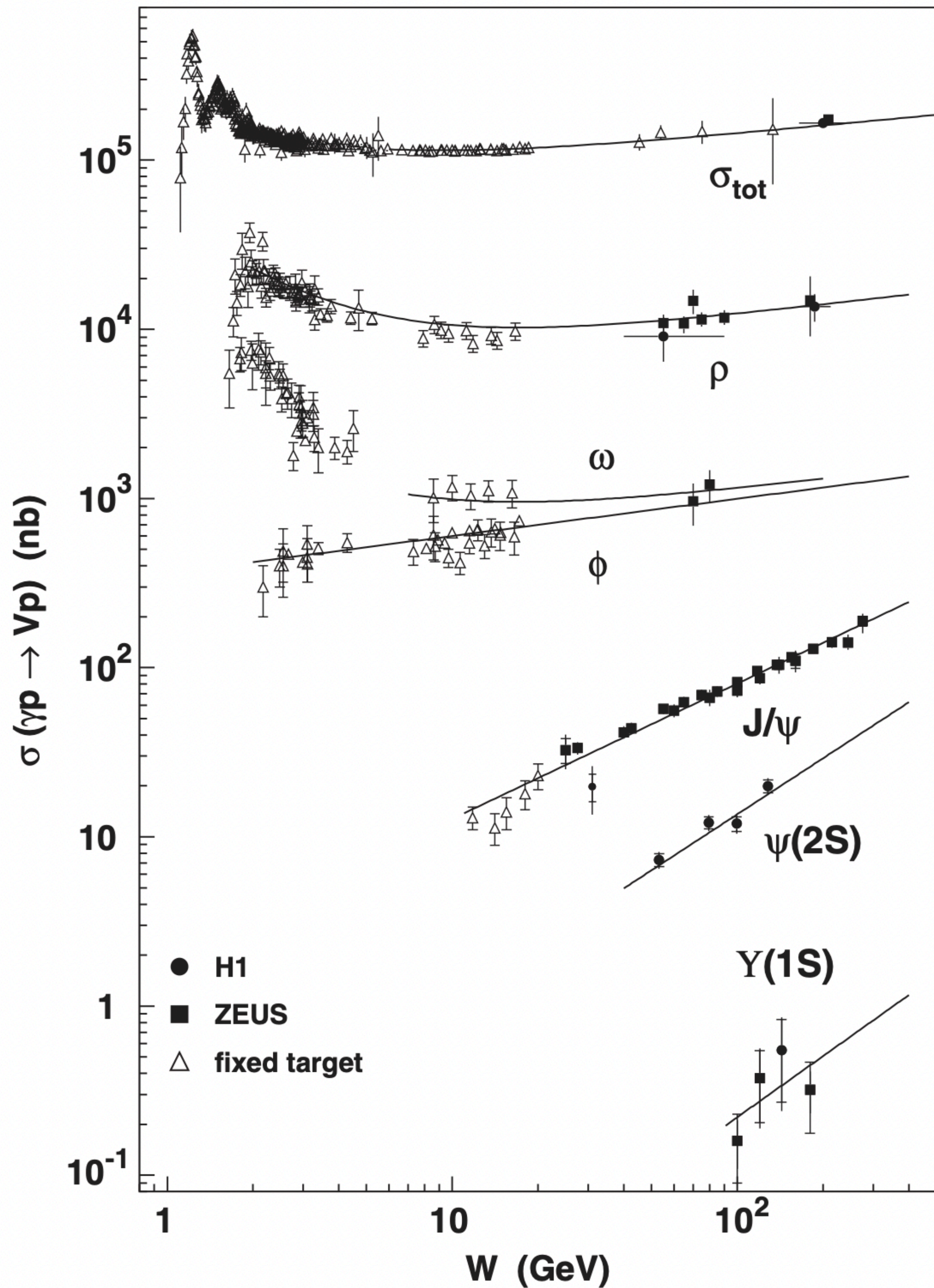


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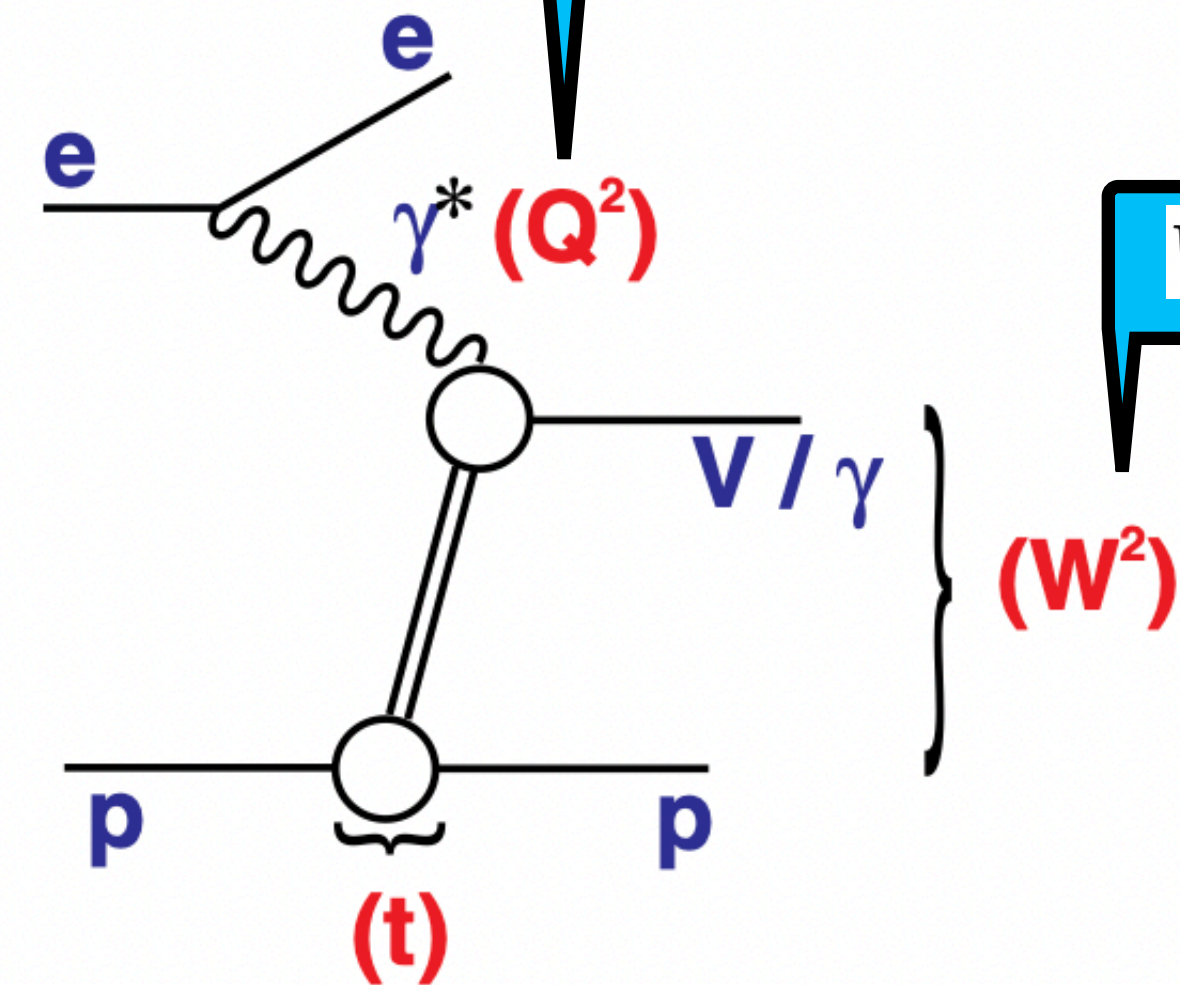
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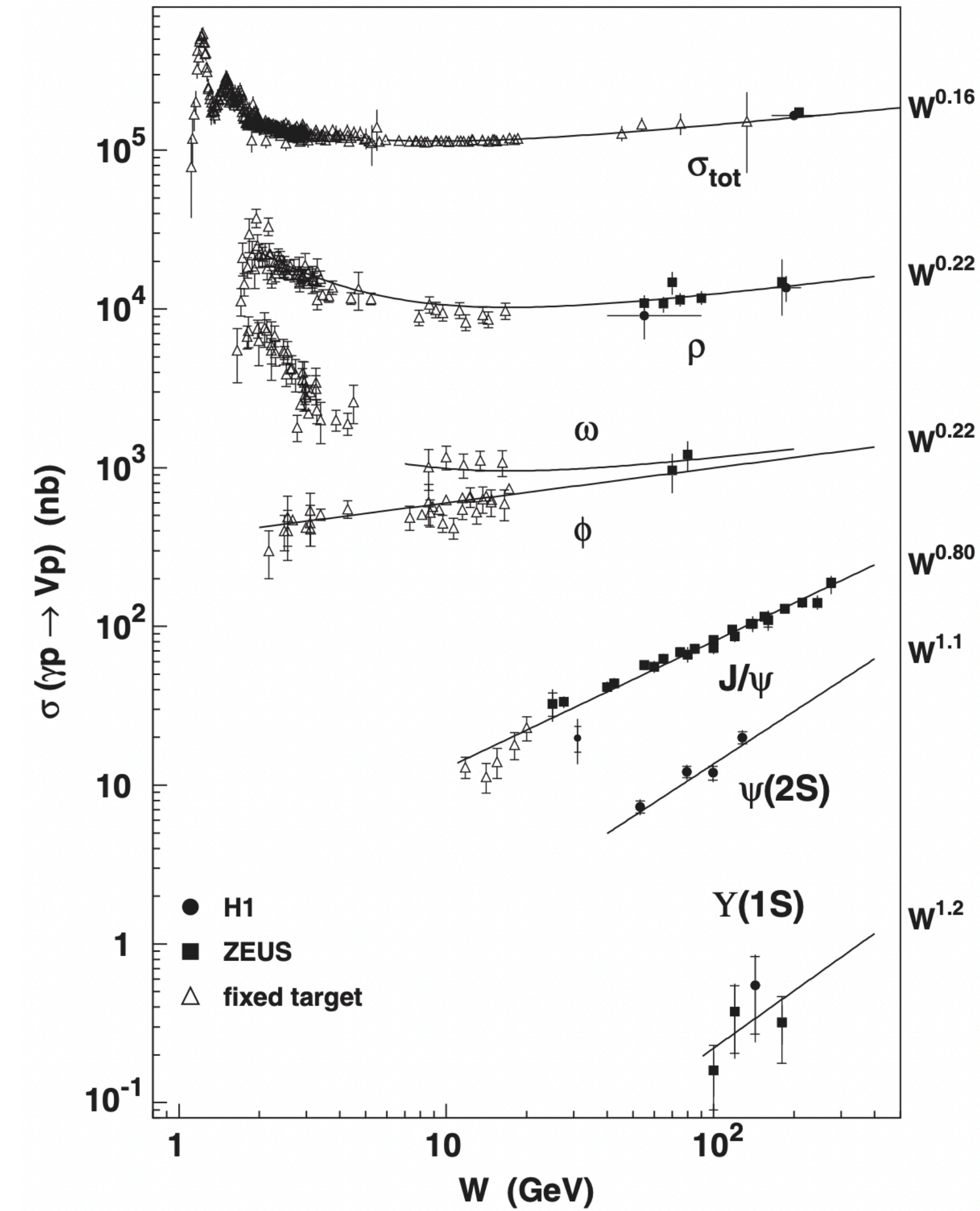
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Exponent grows with the scale

Related, through a Fourier transform, to the distribution of colour fields in the transverse plane

Newman, Wing, <https://inspirehep.net/literature/1247974>

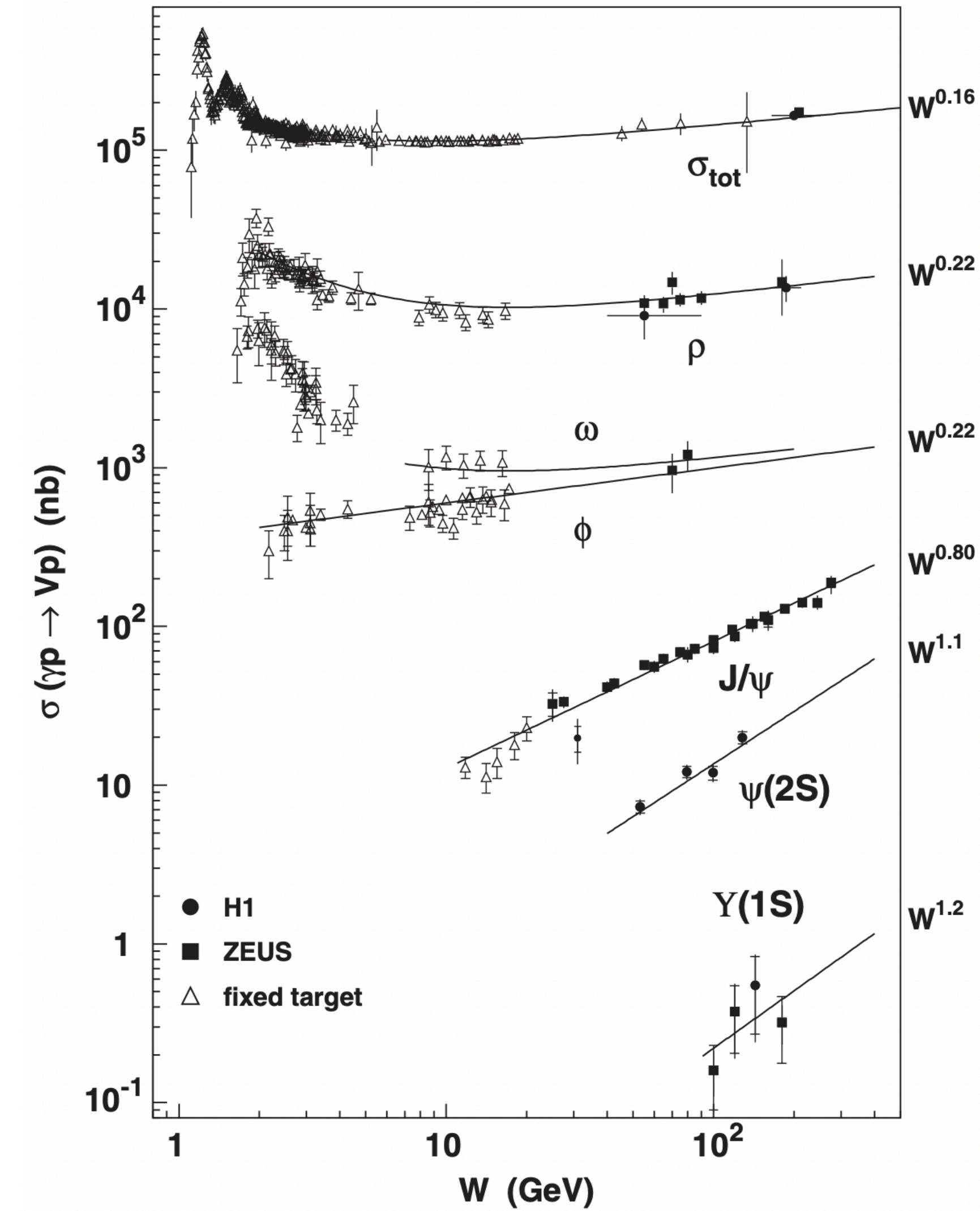
Sensitivity to the gluon



$\sigma \propto W^\delta$

Newman, Wing, <https://inspirehep.net/literature/1247974>

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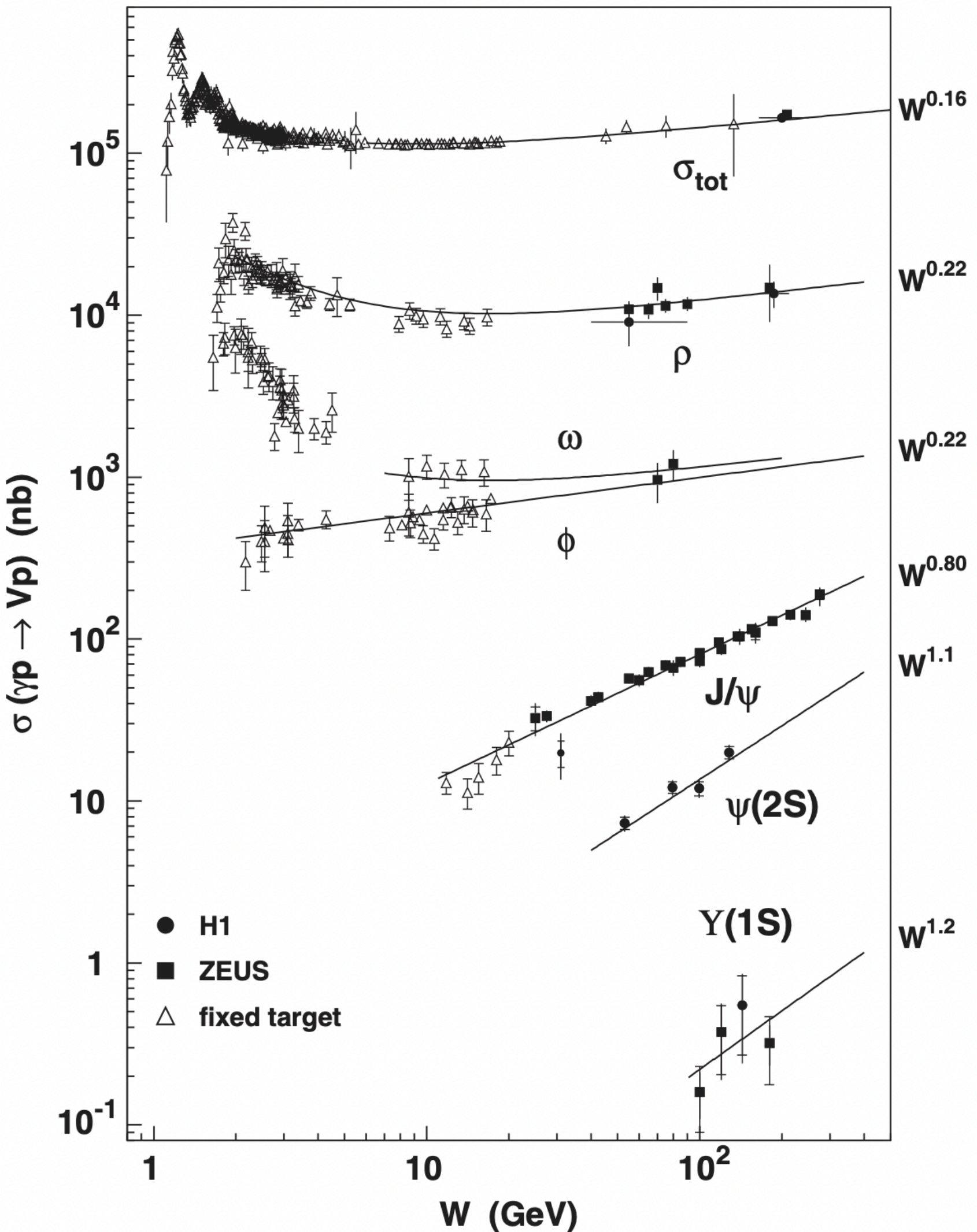


$$\sigma \propto x^{-\delta/2}$$

$$\sigma \propto W^\delta$$

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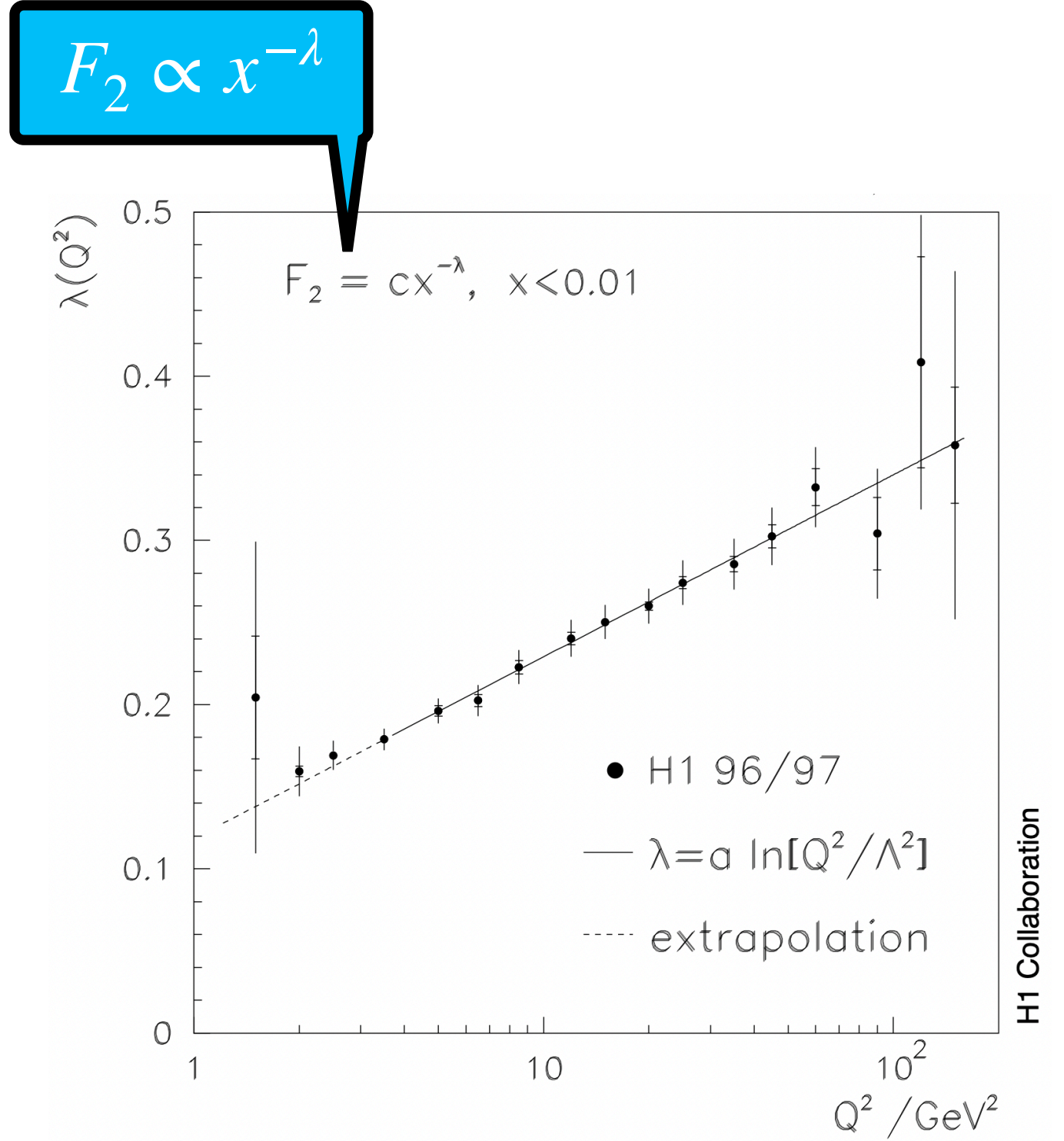
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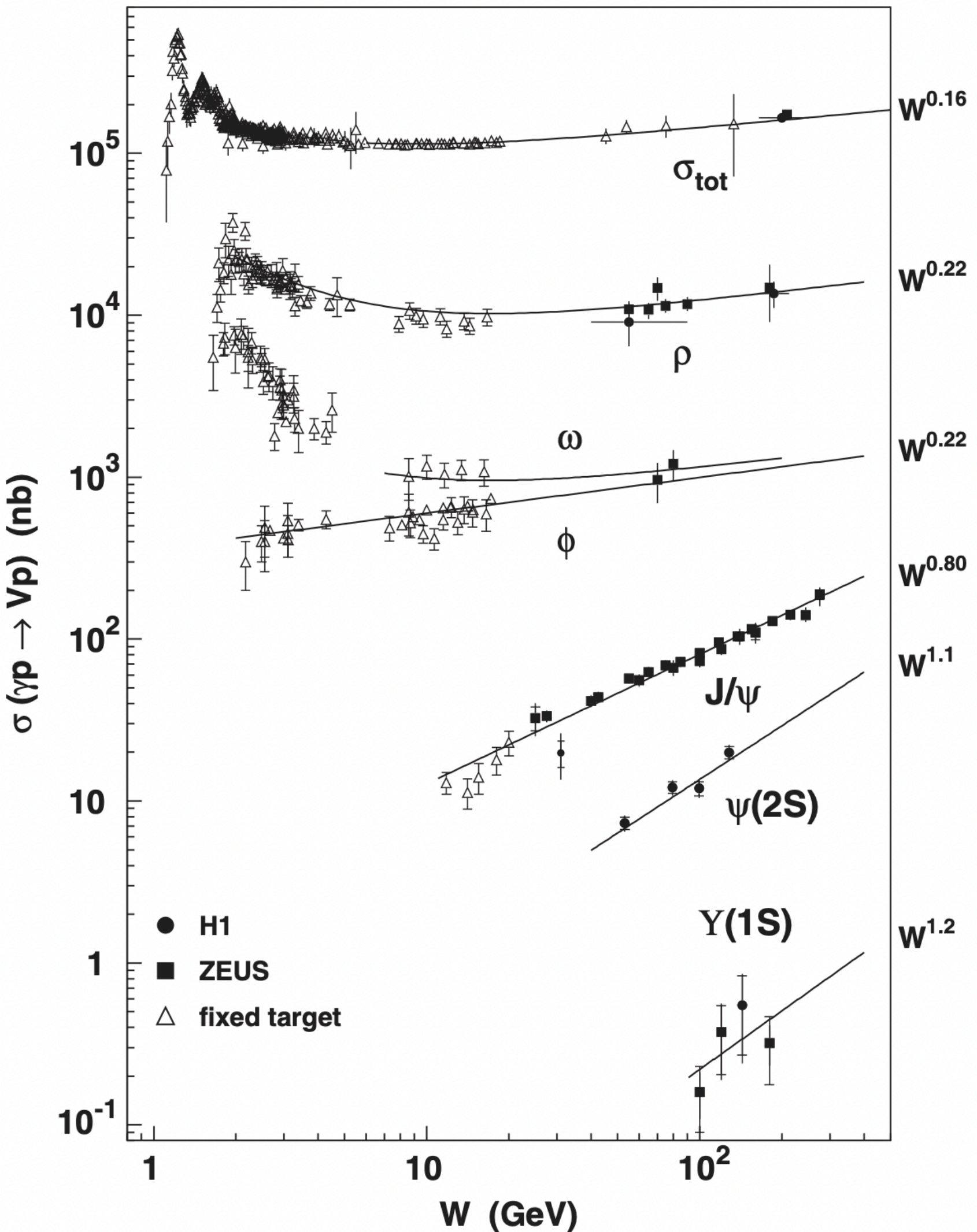
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H1, <https://inspirehep.net/literature/561805>

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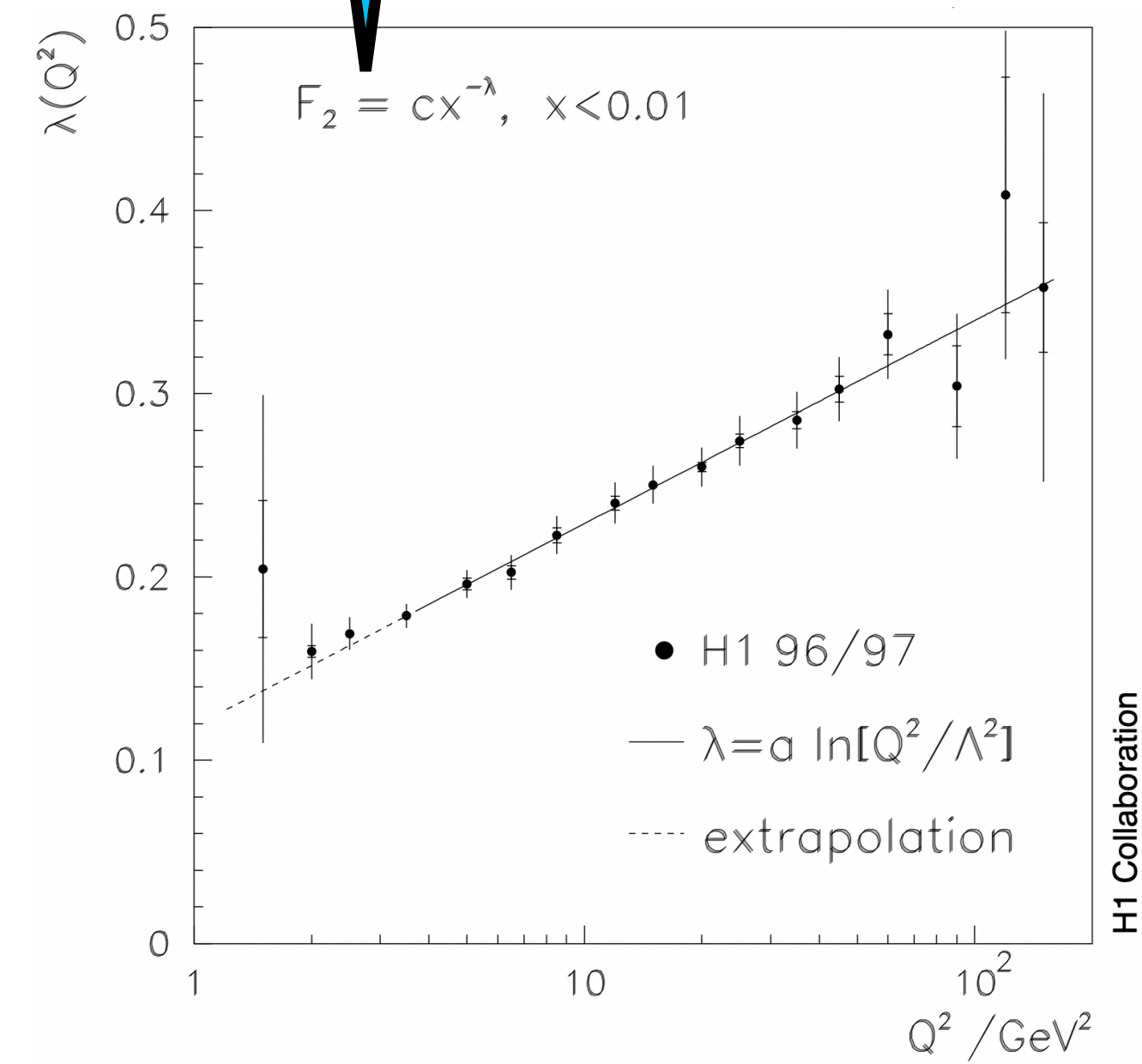


$\sigma \propto x^{-\delta/2}$

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Raise of the gluon distribution

$F_2 \propto x^{-\lambda}$

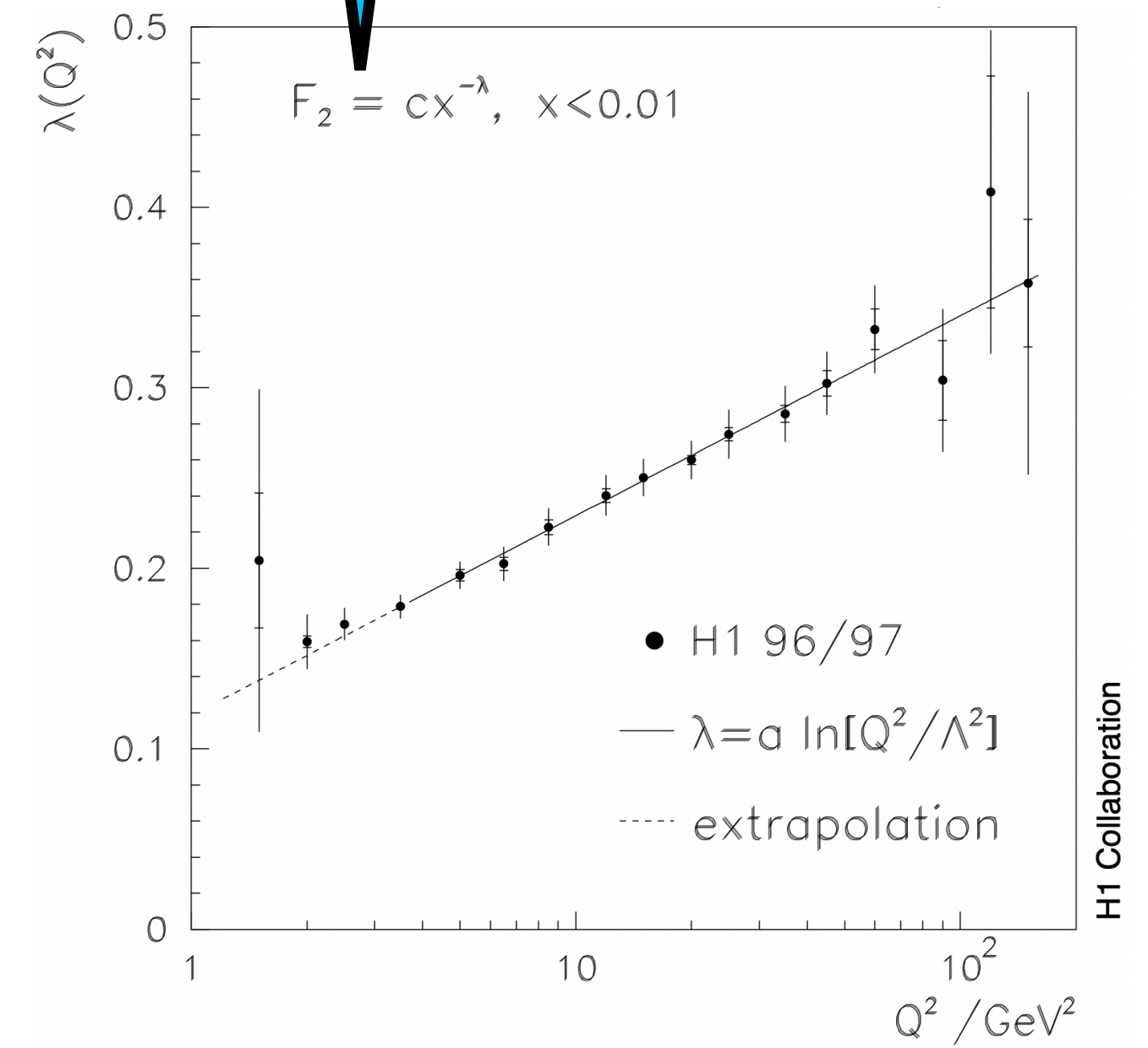
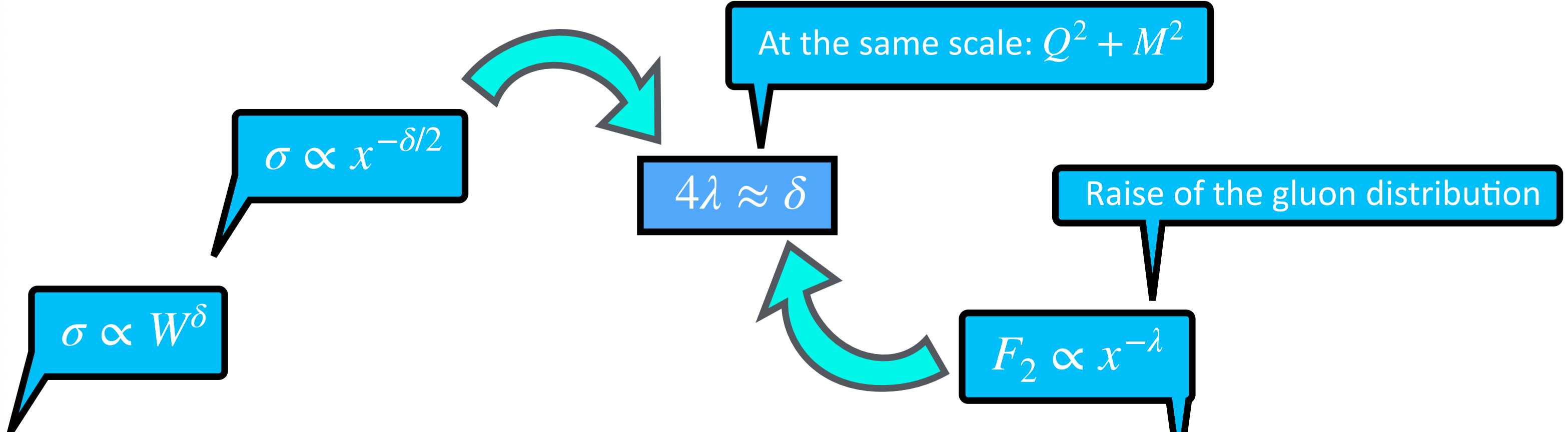
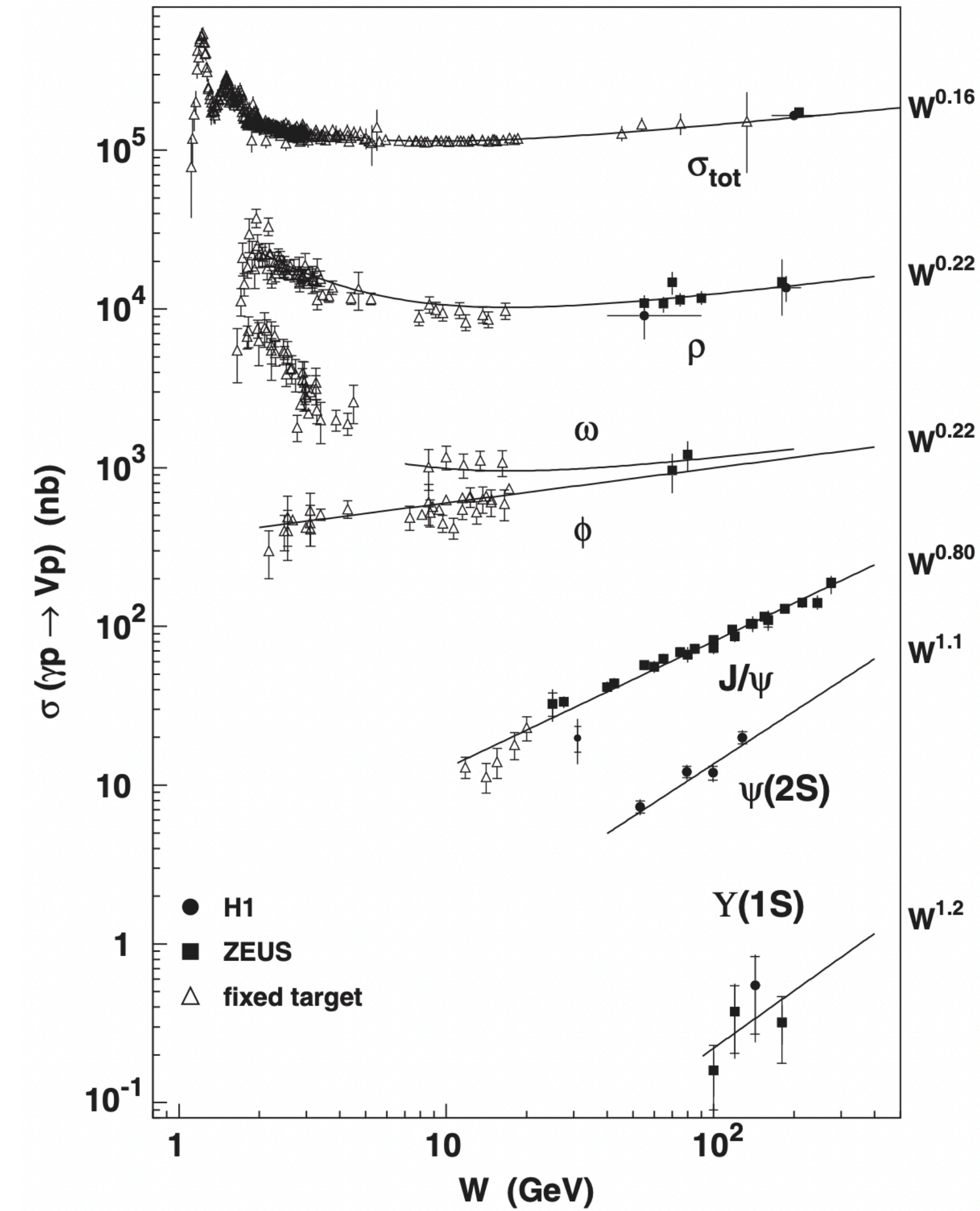


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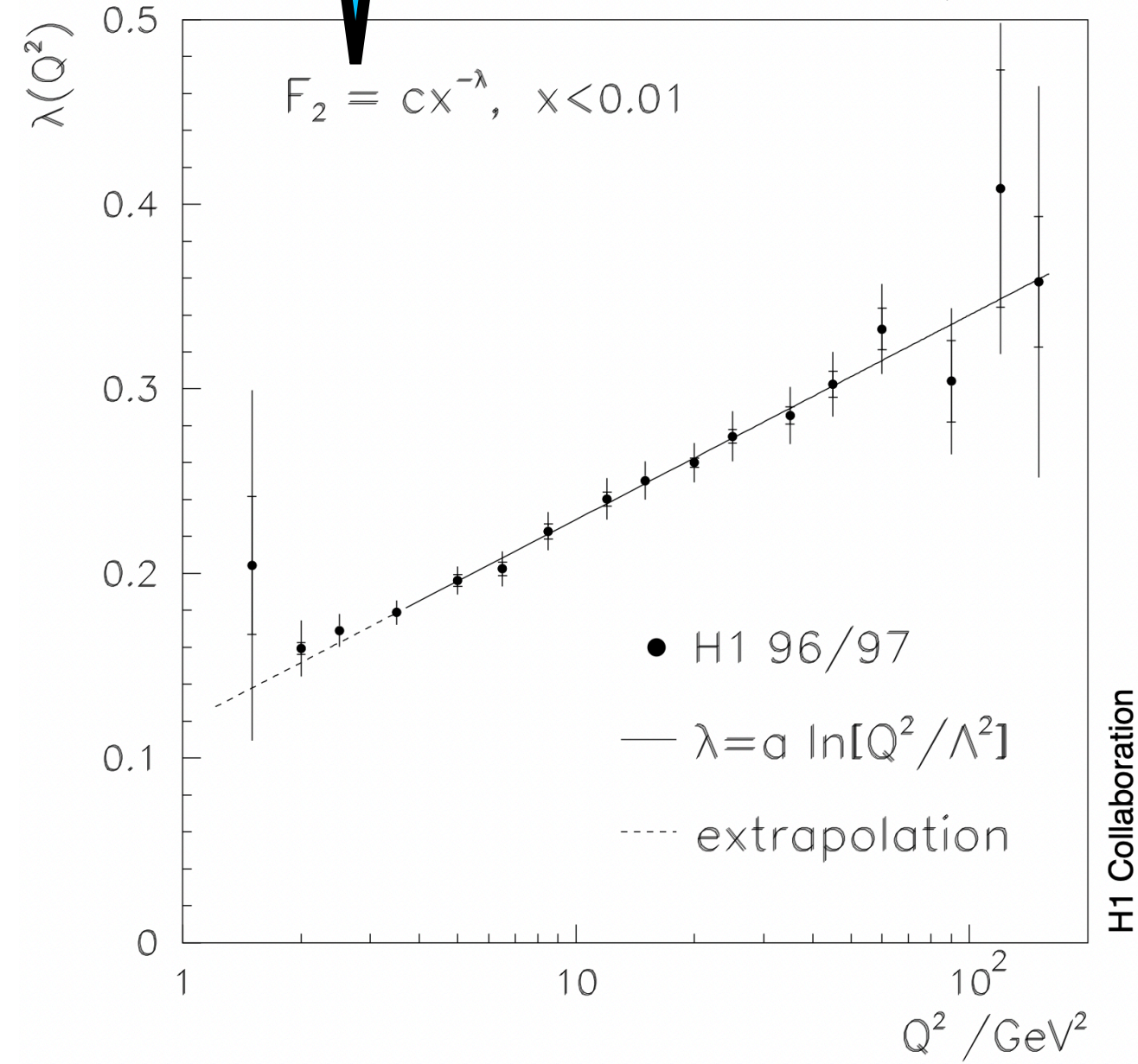
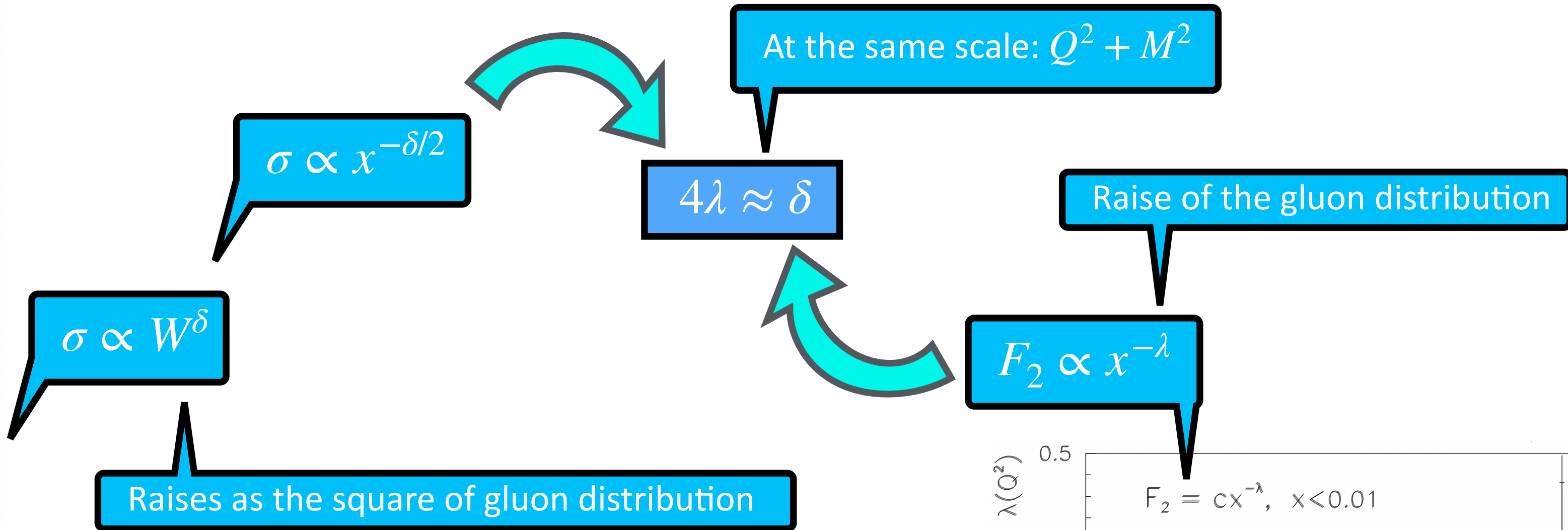
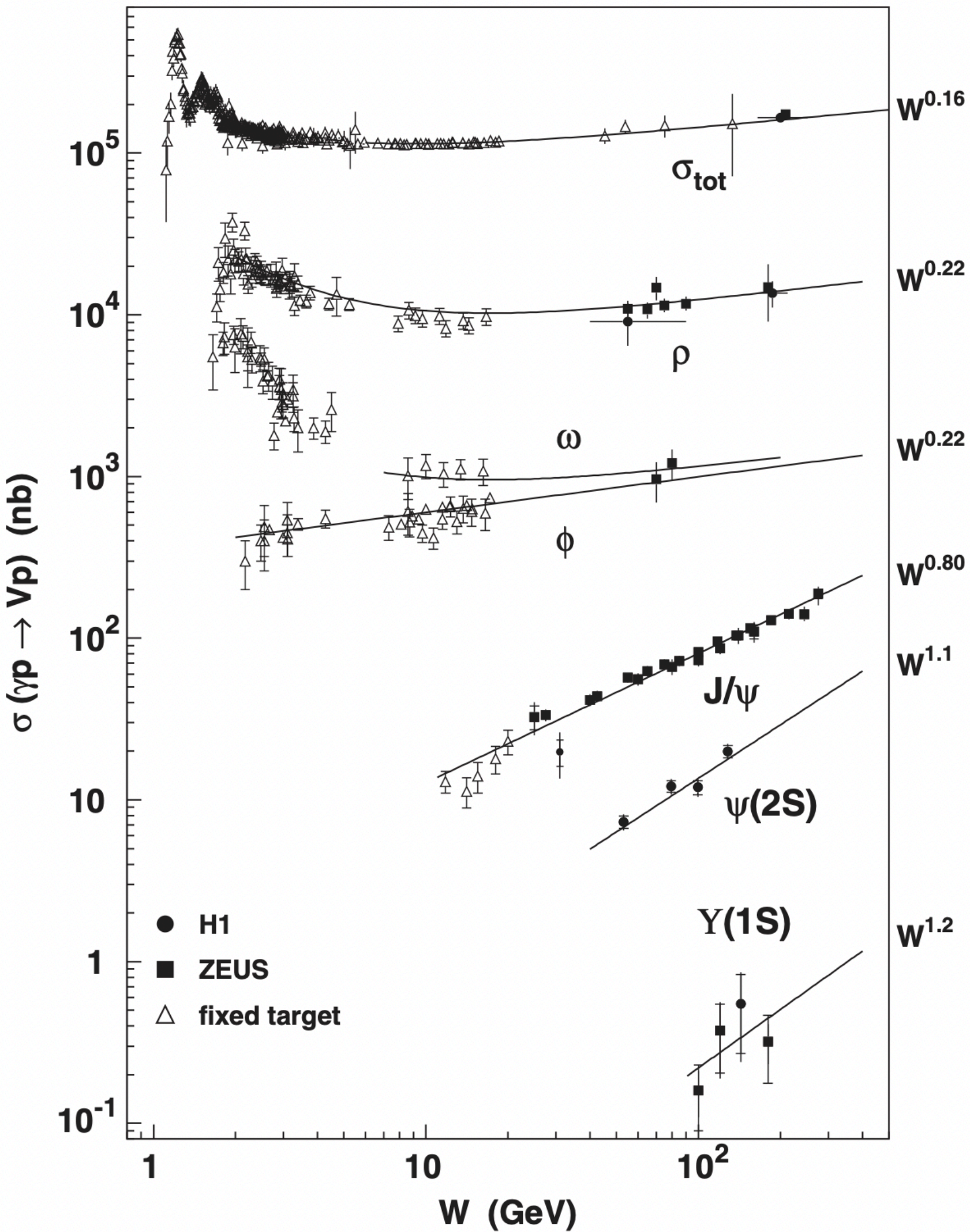
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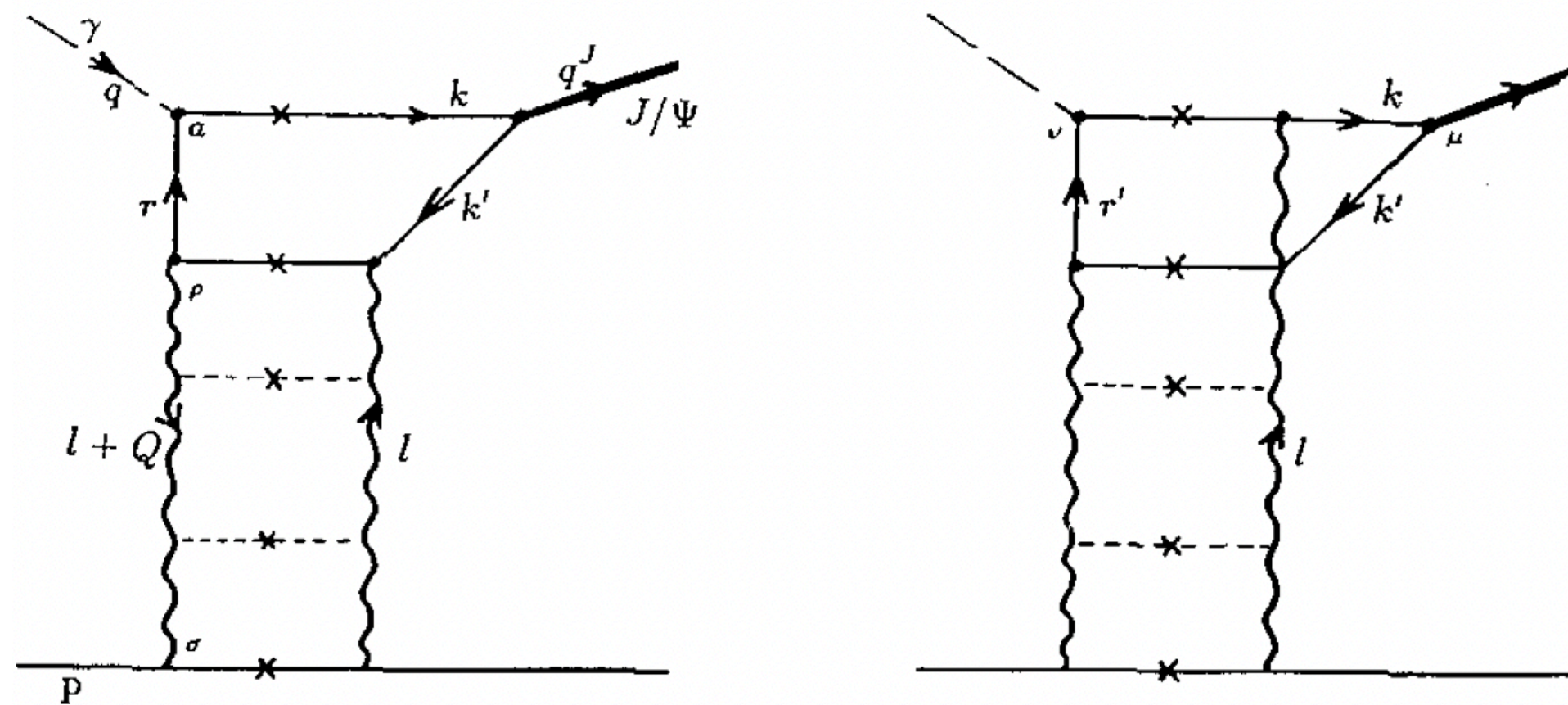


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The process of J/Ψ electroproduction arouses interest due to two reasons. First, it can be calculated within the perturbative QCD and second, its cross section is proportional to the gluon structure function. So, it is a good way to study the gluon distribution inside a proton [1, 2].

1993: Diffractive vector meson production in LLA QCD

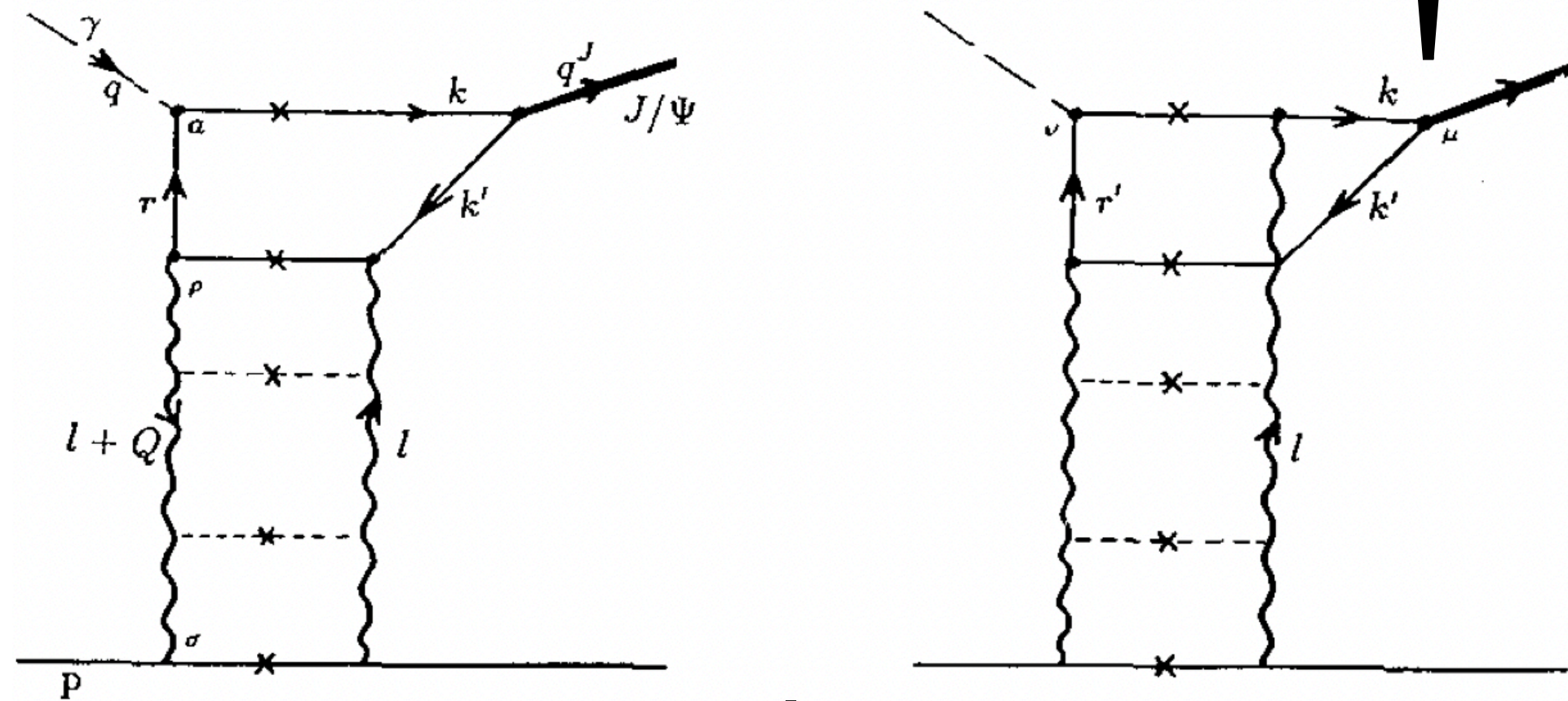


Diagrams that are considered

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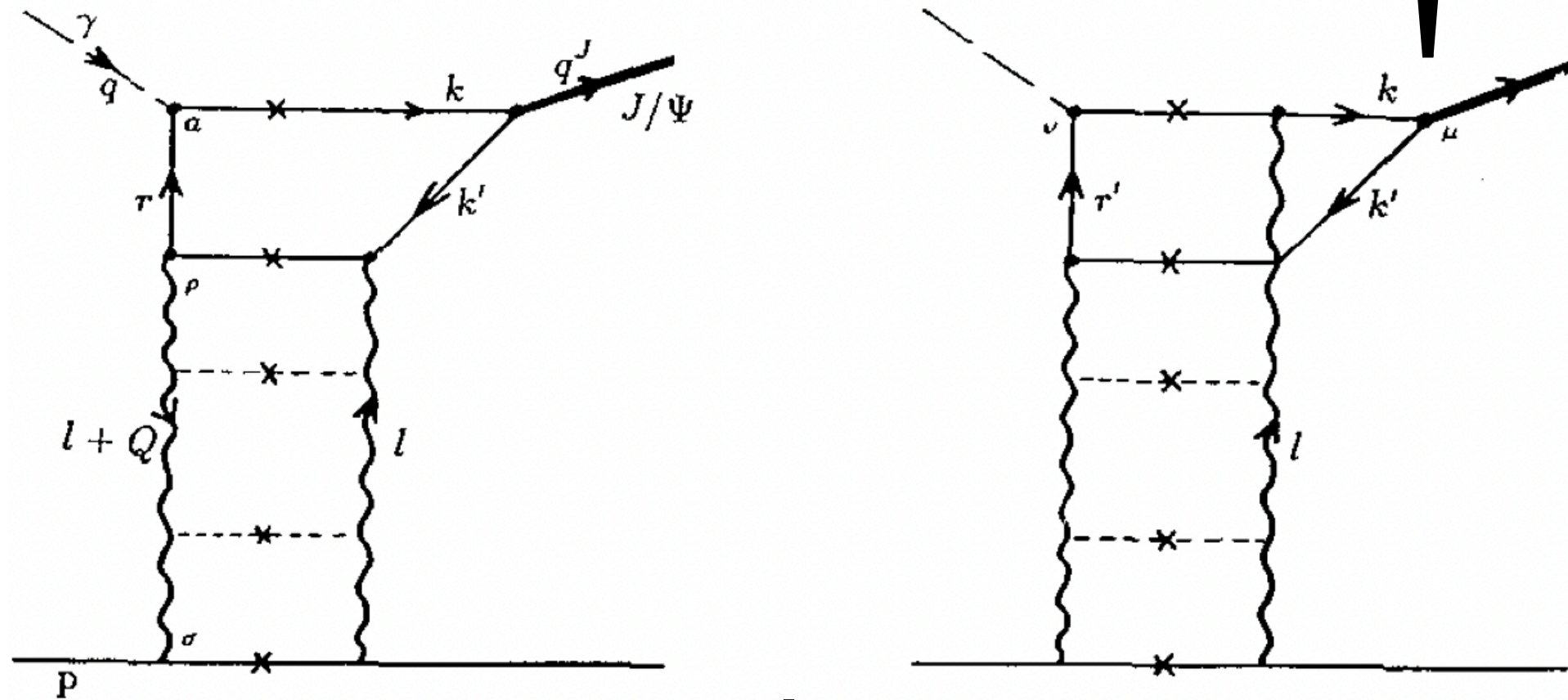
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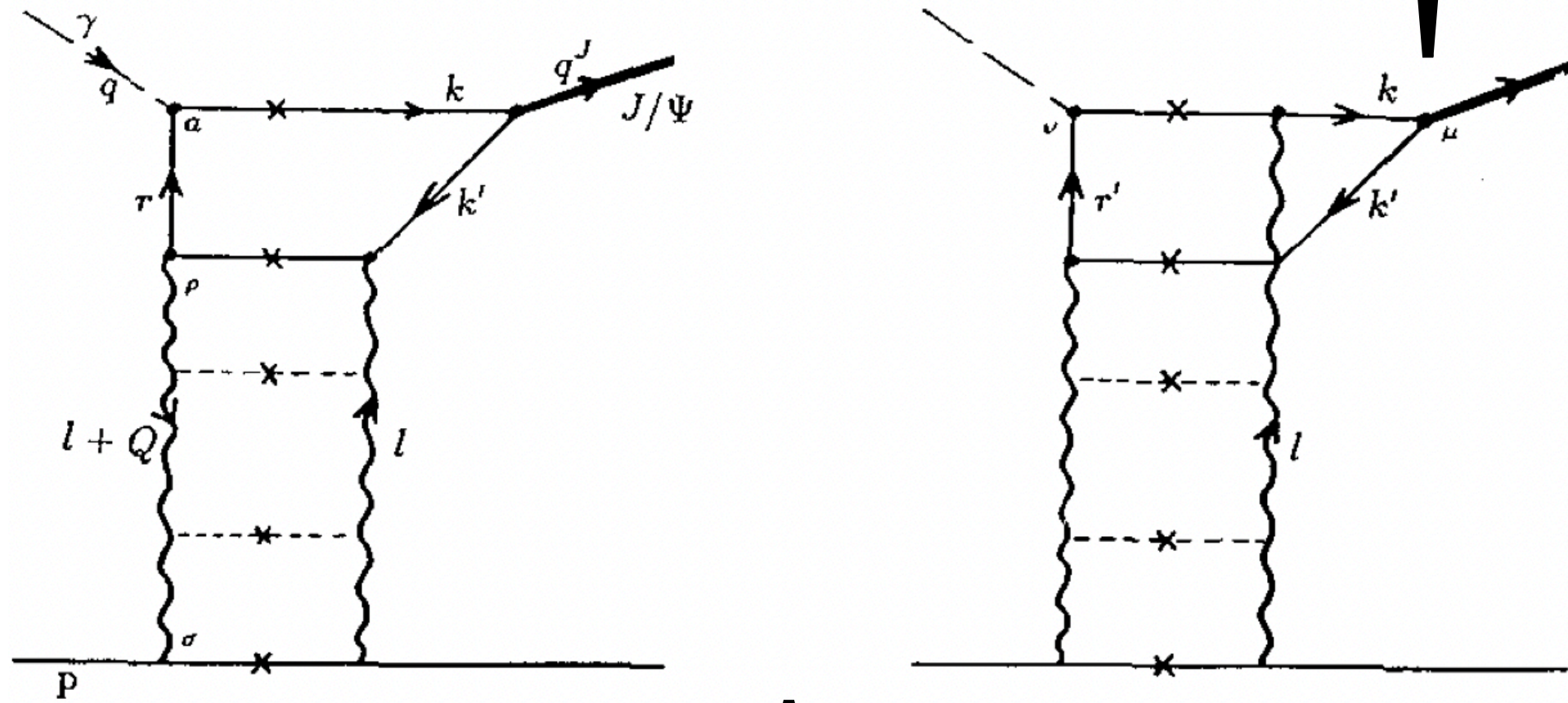
$$\begin{aligned} \frac{d\sigma^T(\gamma p \rightarrow J/\Psi + p)}{dt} &= \frac{|M|^2}{16\pi s^2} \\ &= [F_N^{2G}(t)]^2 \frac{\alpha_s^2 \Gamma_{ee}^J m_J^3}{3\alpha_{em}} \pi^3 \\ &\times \left[\bar{x}G(\bar{x}, \bar{q}^2) \frac{2\bar{q}^2 - |q_t^J|^2}{(2\bar{q}^2)^3} \right]^2, \end{aligned}$$

Square of gluon distribution

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Diagrams that are considered

The process of J/Ψ electroproduction arouses interest due to two reasons. First, it can be calculated within the perturbative QCD and second, its cross section is proportional to the gluon structure function. So, it is a good way to study the gluon distribution inside a proton [1, 2].

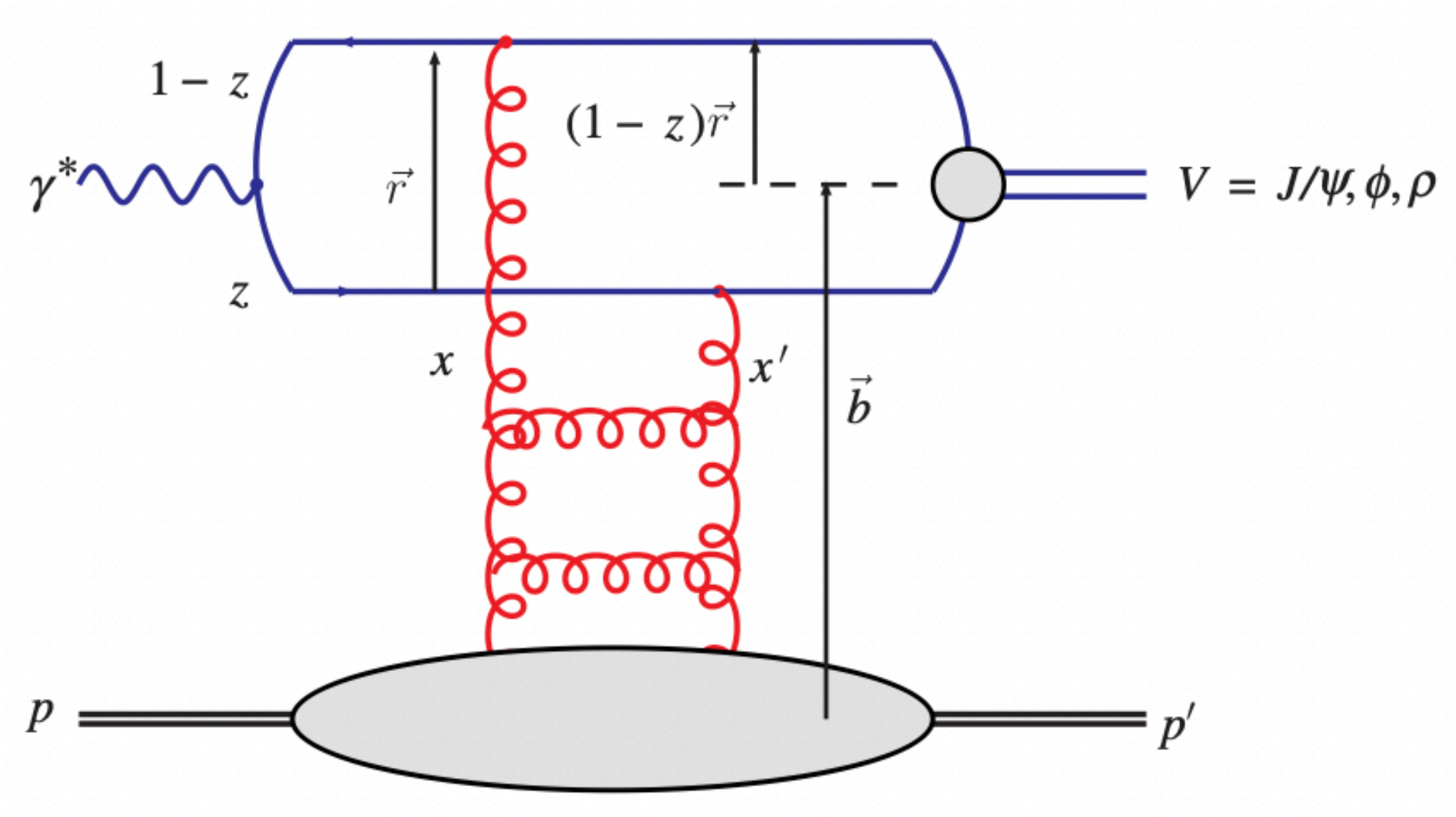
$$\begin{aligned} \frac{d\sigma^T(\gamma p \rightarrow J/\Psi + p)}{dt} &= \frac{|M|^2}{16\pi s^2} \\ &= [F_N^{2G}(t)]^2 \frac{\alpha_s^2 \Gamma_{ee}^J m_J^3 \pi^3}{3\alpha_{em}} \\ &\times \left[\bar{x} G(\bar{x}, \bar{q}^2) \frac{2\bar{q}^2 - |q_t^J|^2}{(2\bar{q}^2)^3} \right]^2, \end{aligned}$$

Square of gluon distribution

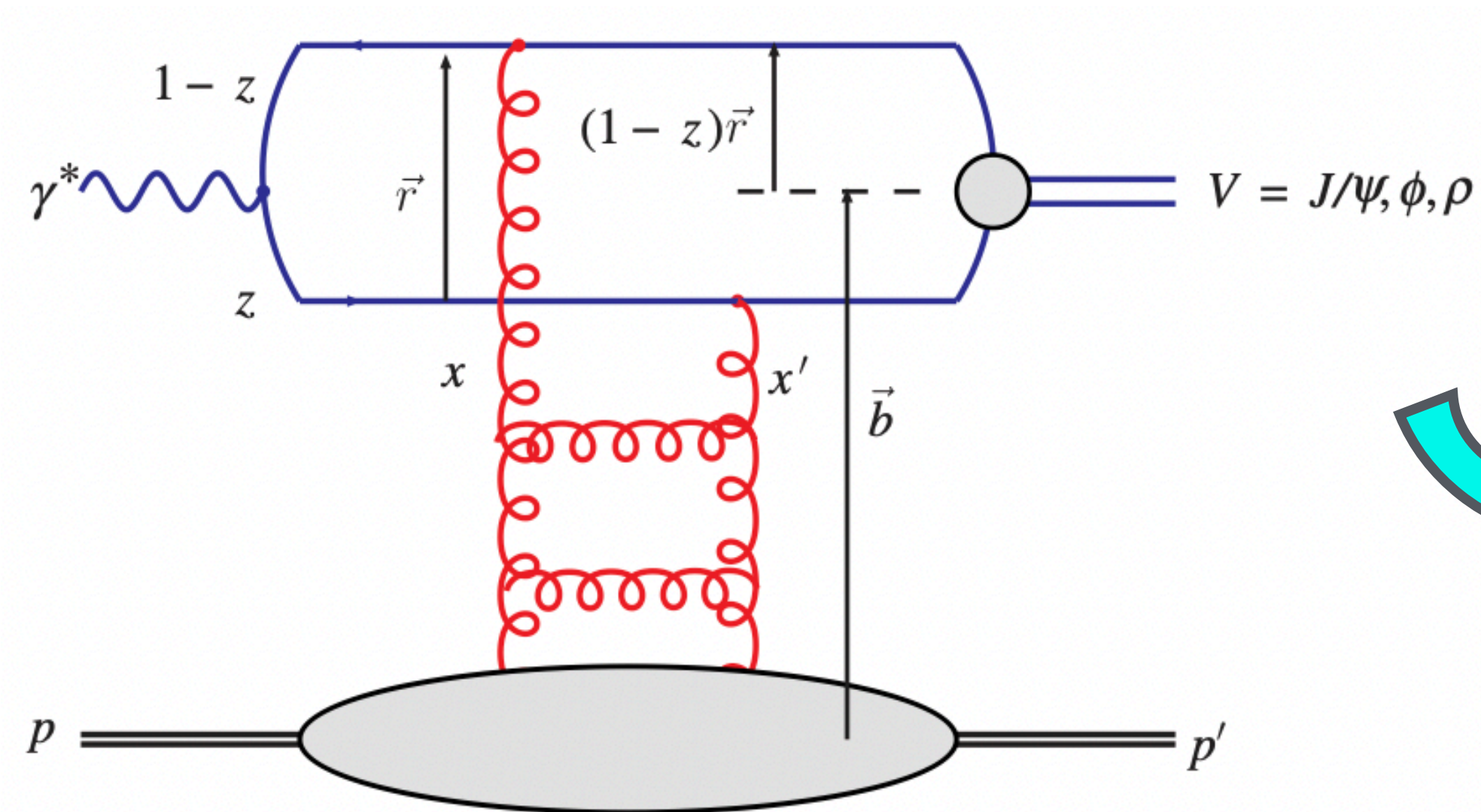
Thus, the diffractive J/Ψ production provides us with a good chance to find the real position of the saturation boundary and, hence, to answer this question.

Good process to study the approach to the saturation regime

Formalism

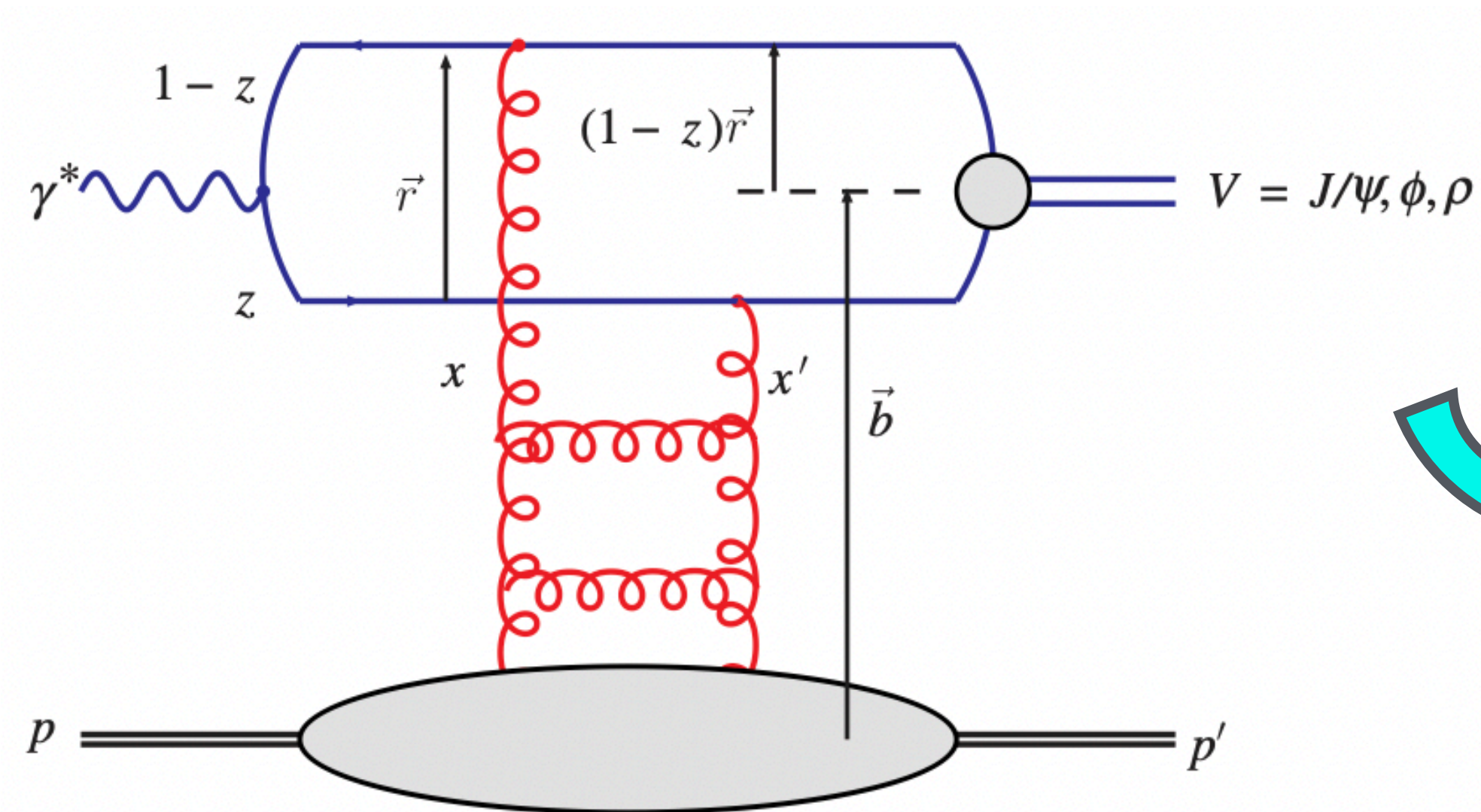


Formalism



$$\begin{aligned} \frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} &= \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2 \\ &= \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \right. \\ &\quad \left. \times \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \right|^2. \end{aligned}$$

Formalism

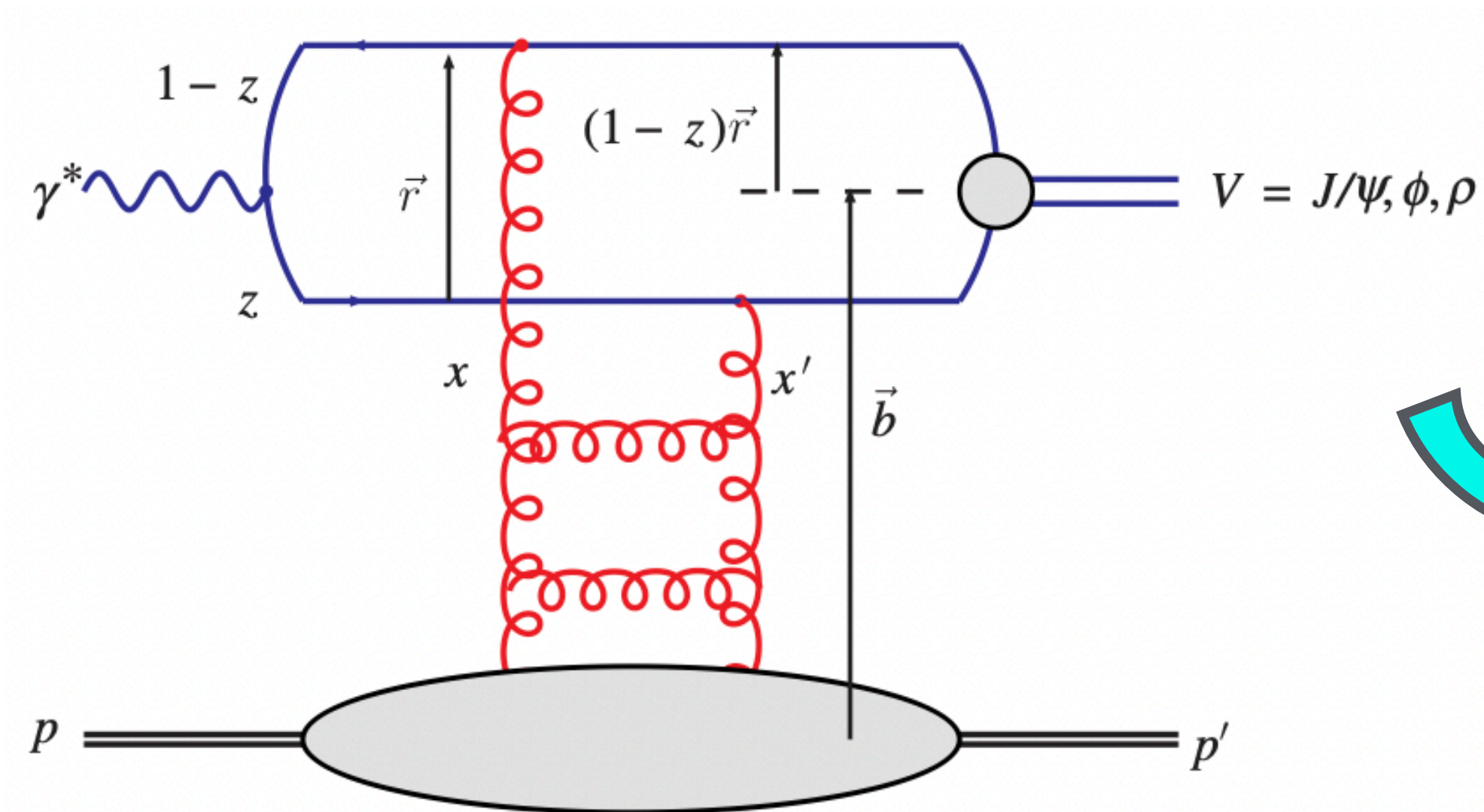


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Forward wave functions

1

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

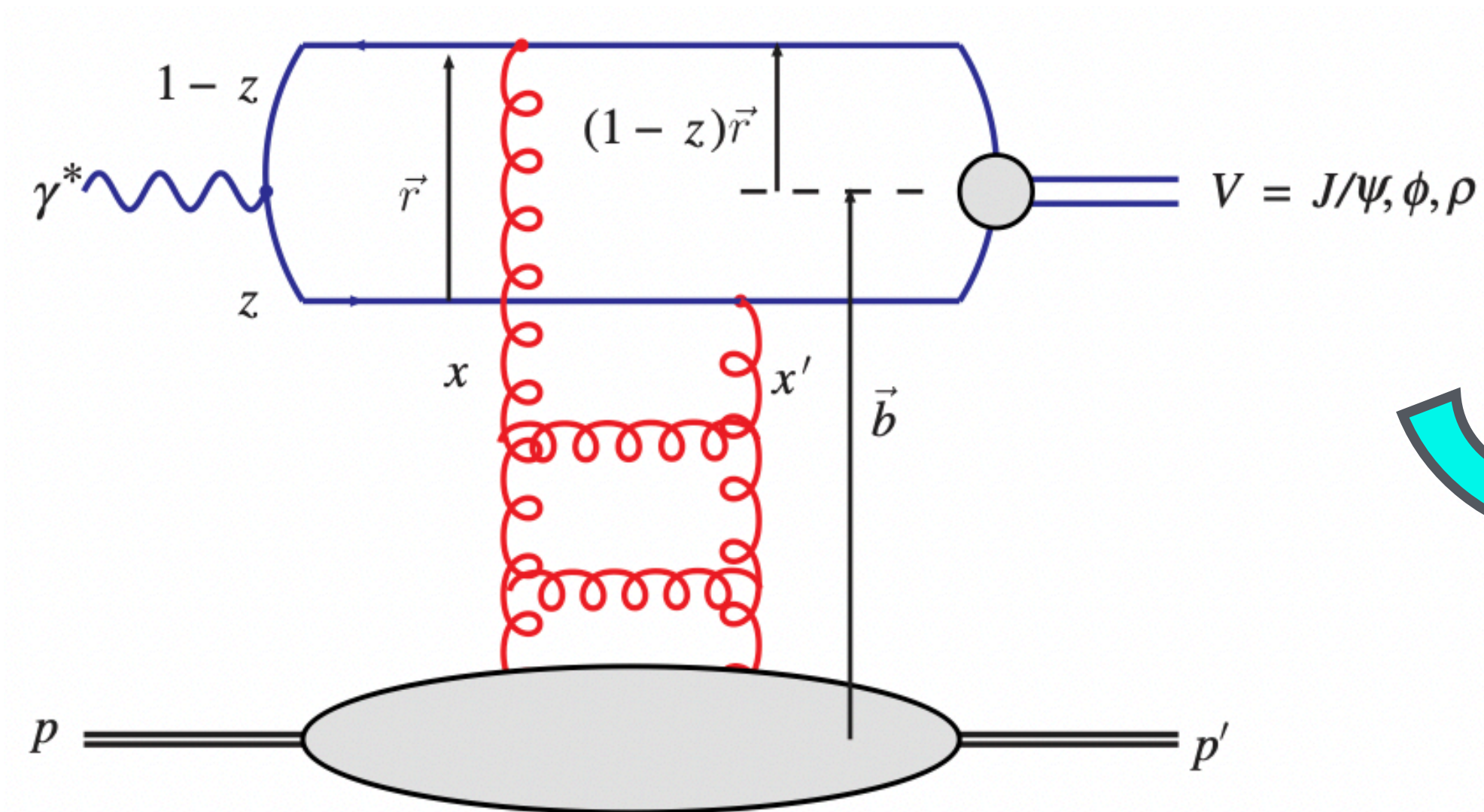
$$= \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \right.$$

$$\left. \times \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \vec{\Delta}} \frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \right|^2.$$

1 Forward wave functions

$\vec{\Delta}^2 = -t$

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

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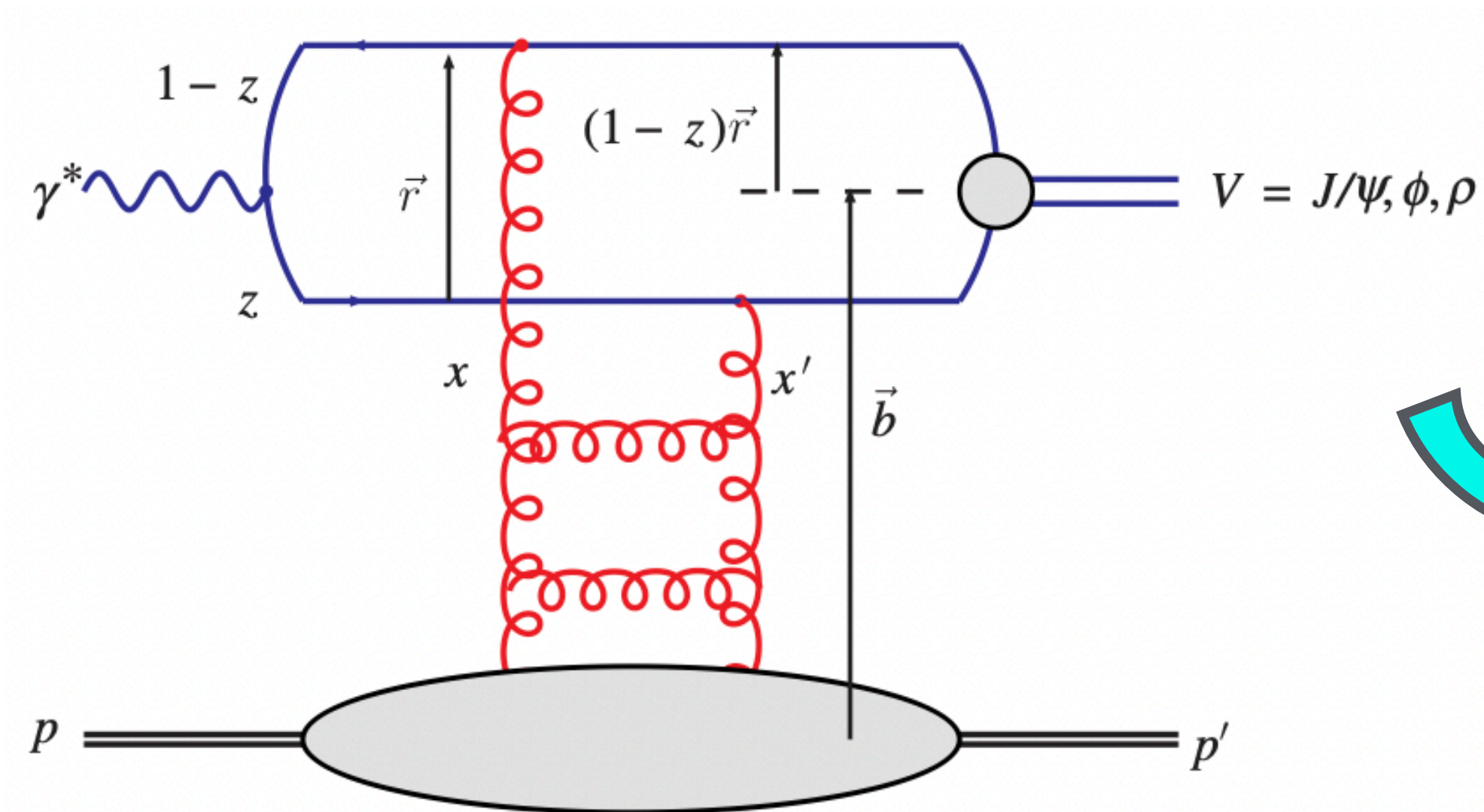
$$\times \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \vec{\Delta}} \left. \frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \right|^2.$$

Conjugate variable

$\vec{\Delta}^2 = -t$

1 Forward wave functions

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

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Includes the effect of non-forward wave functions

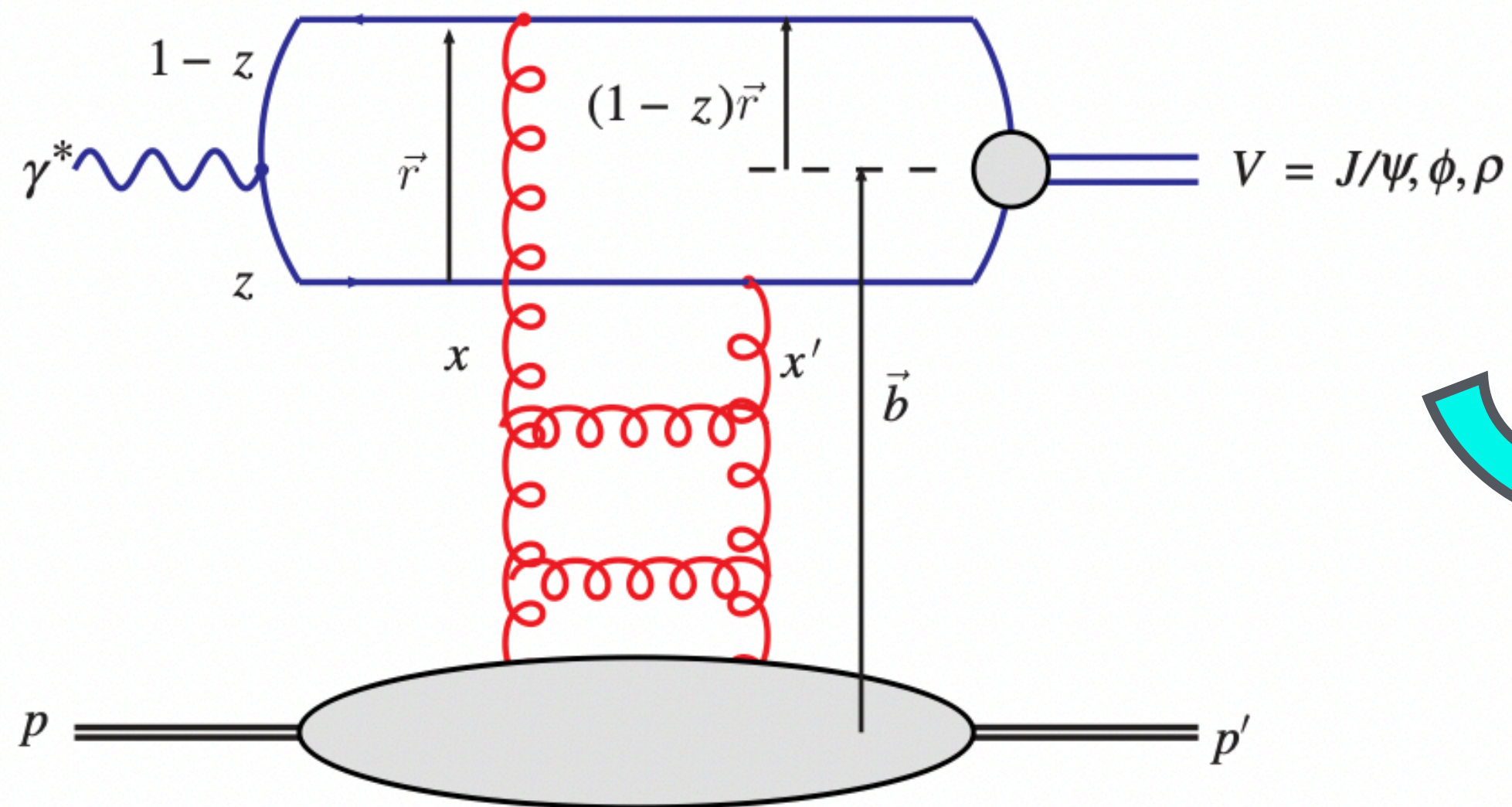
Conjugate variable

$\vec{\Delta}^2 = -t$

1 Forward wave functions

2006: Diffractive vector meson production in the dipole approach (1/5)

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow E p}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow E p}|^2$$

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Slightly different form use nowadays

$$(1-z) \rightarrow \left(\frac{1}{2} - z\right)$$

Includes the effect of non-forward wave functions

Conjugate variable

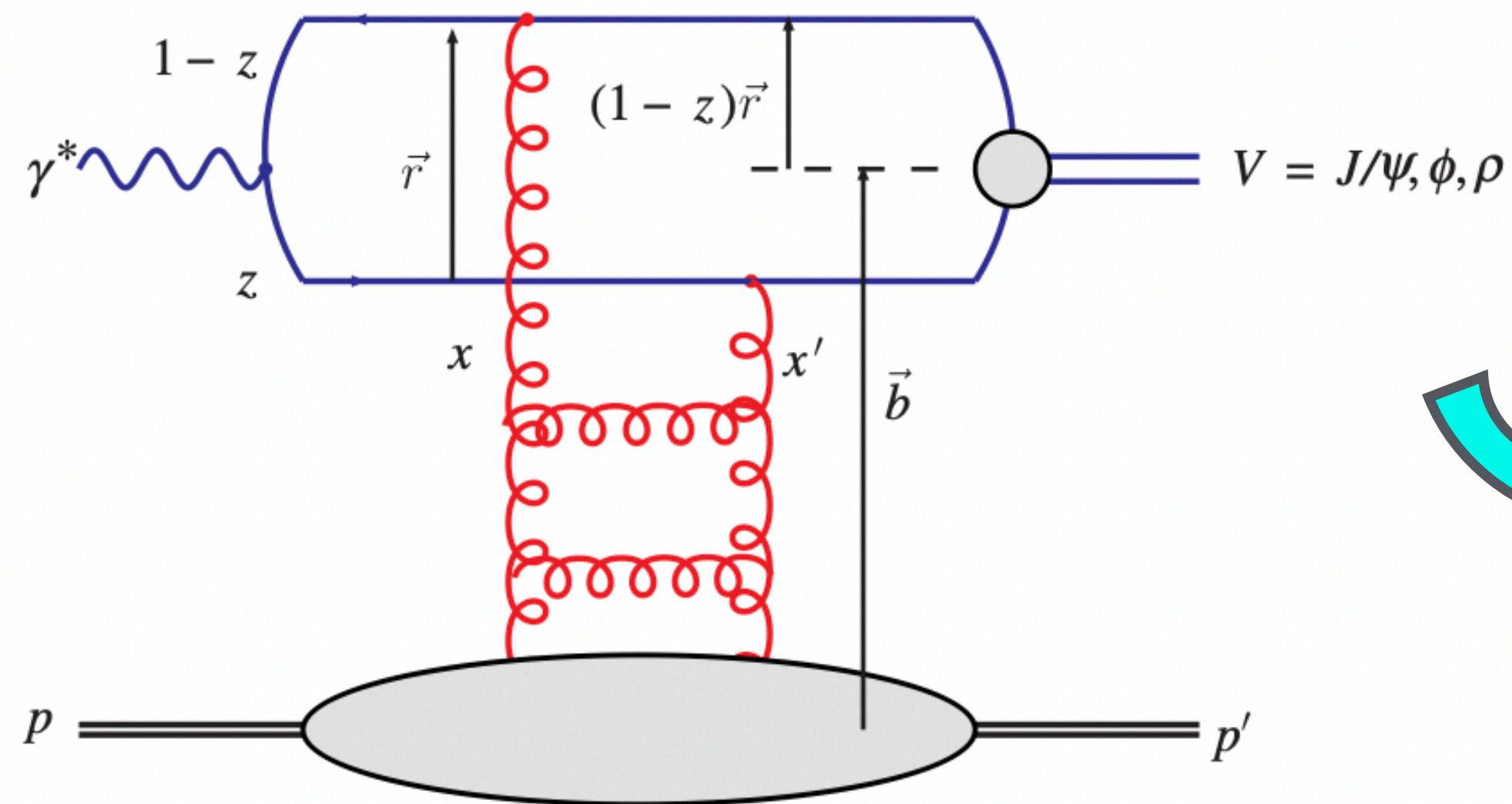
$$\vec{\Delta}^2 = -t$$

Forward wave functions

1

2006: Diffractive vector meson production in the dipole approach (1/5)

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

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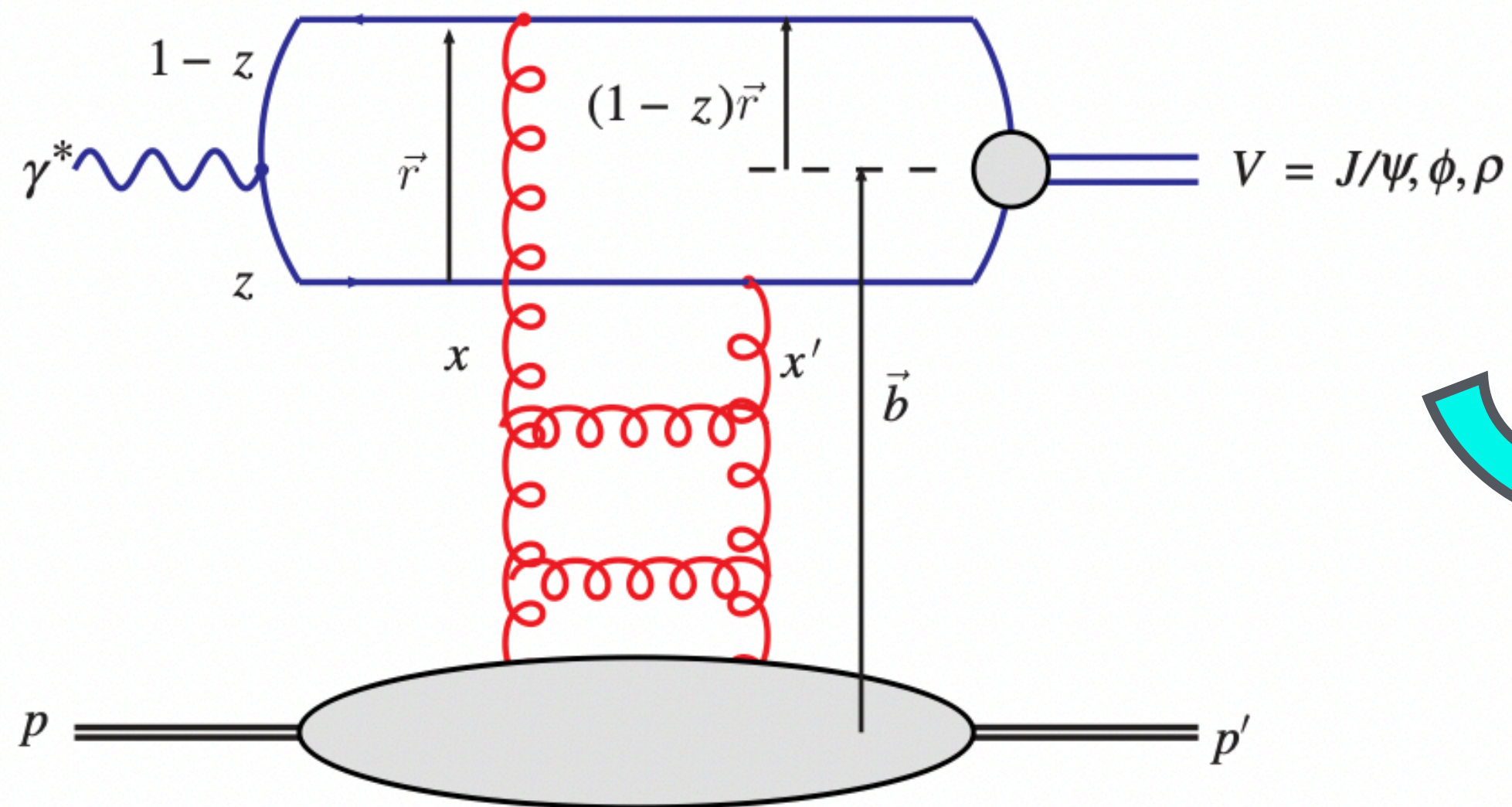
$$\vec{\Delta}^2 = -t$$

1 Forward wave functions

2 Dipole-target cross section assumes a real matrix element

2006: Diffractive vector meson production in the dipole approach (1/5)

Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow E p}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow E p}|^2$$

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 $(1-z) \rightarrow (\frac{1}{2} - z)$

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Conjugate variable

$\vec{\Delta}^2 = -t$

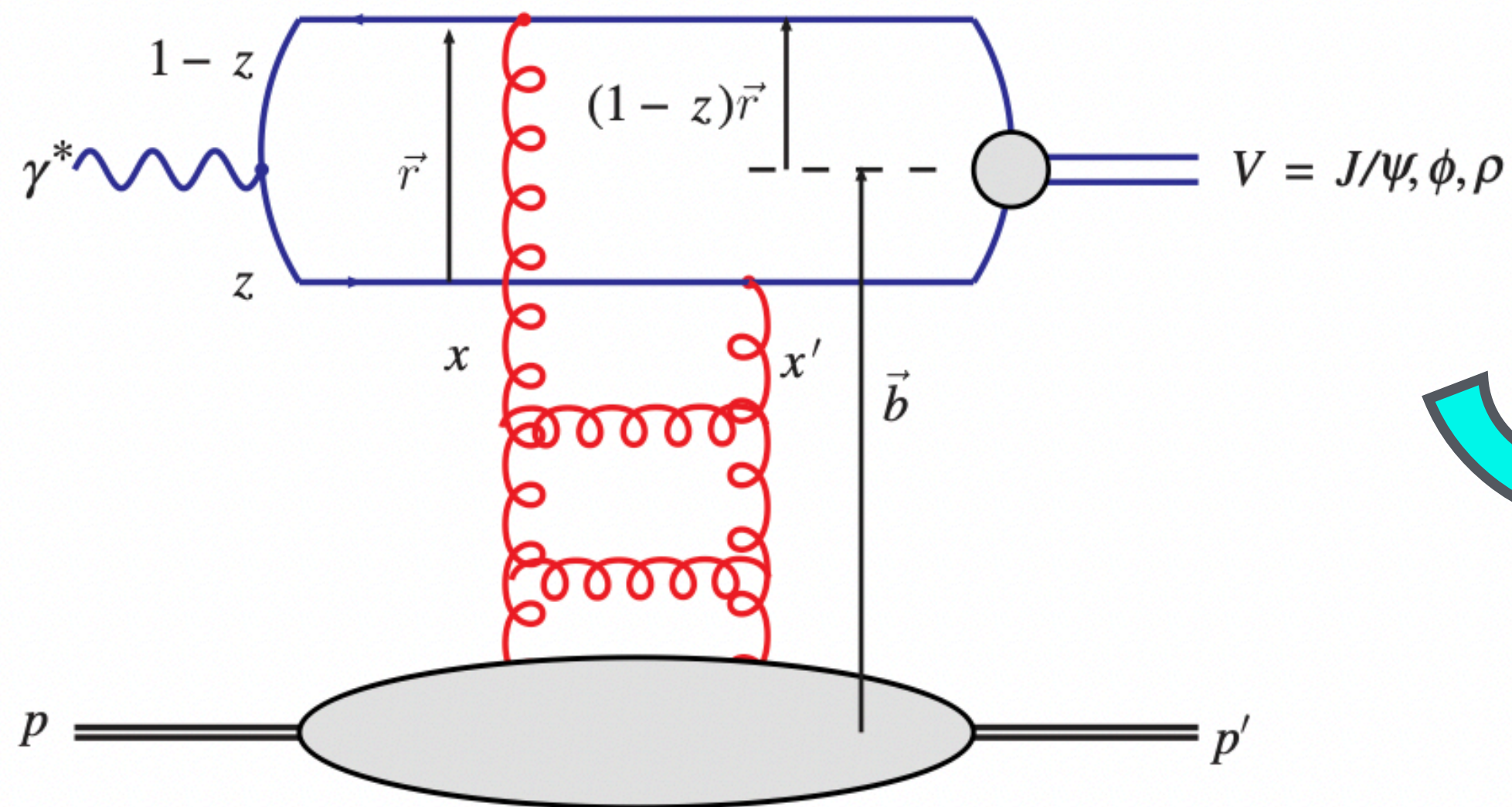
1 Forward wave functions

2 Dipole-target cross section assumes a real matrix element

Normally a correction is used to account for the fact that the matrix element may not be fully real

2006: Diffractive vector meson production in the dipole approach (1/5)

Formalism



The fact that x and x' are not the same is taken into account with the so-called skewedness correction

$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

$$= \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \right.$$

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Slightly different form use nowadays

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Includes the effect of non-forward wave functions

Conjugate variable

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1 Forward wave functions

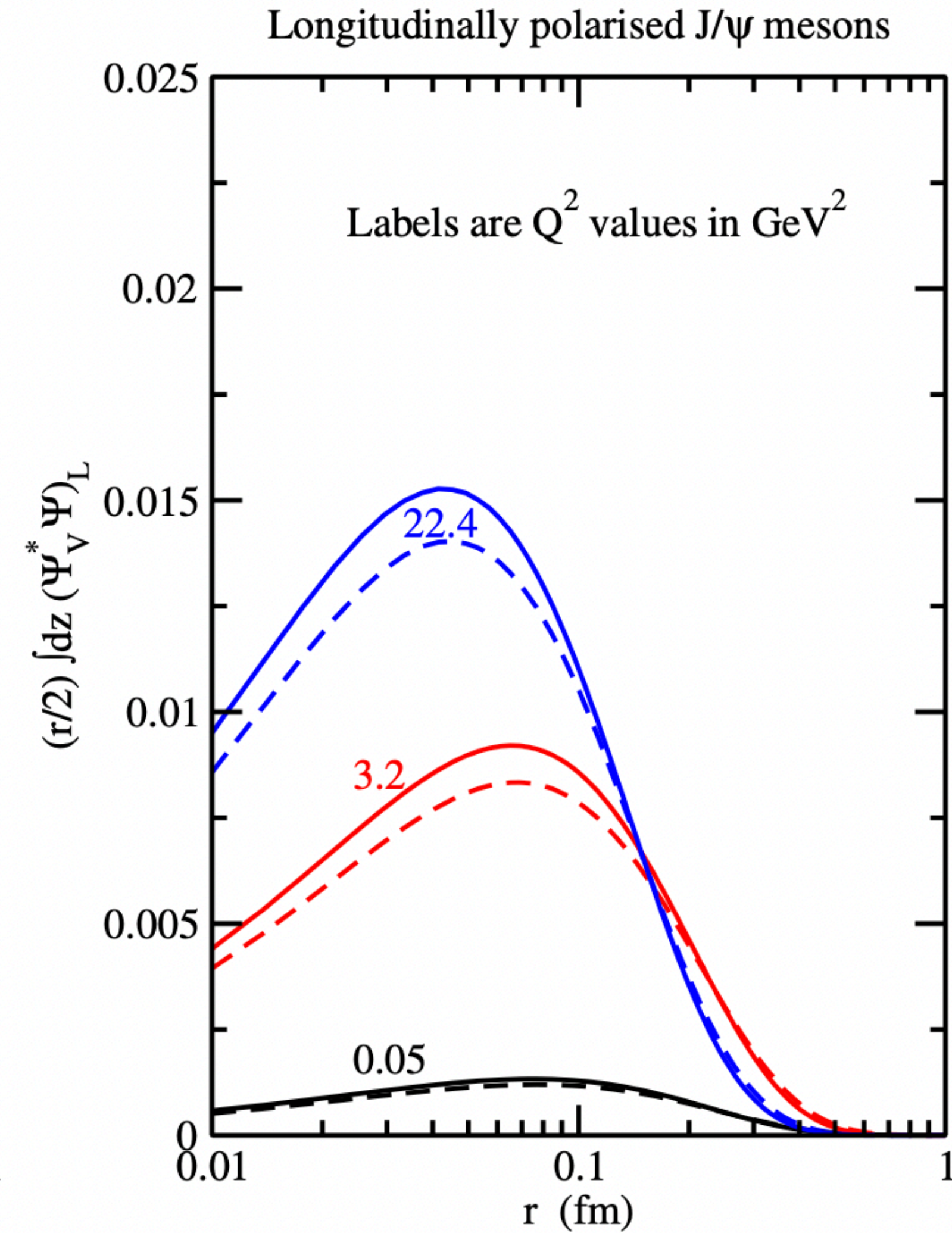
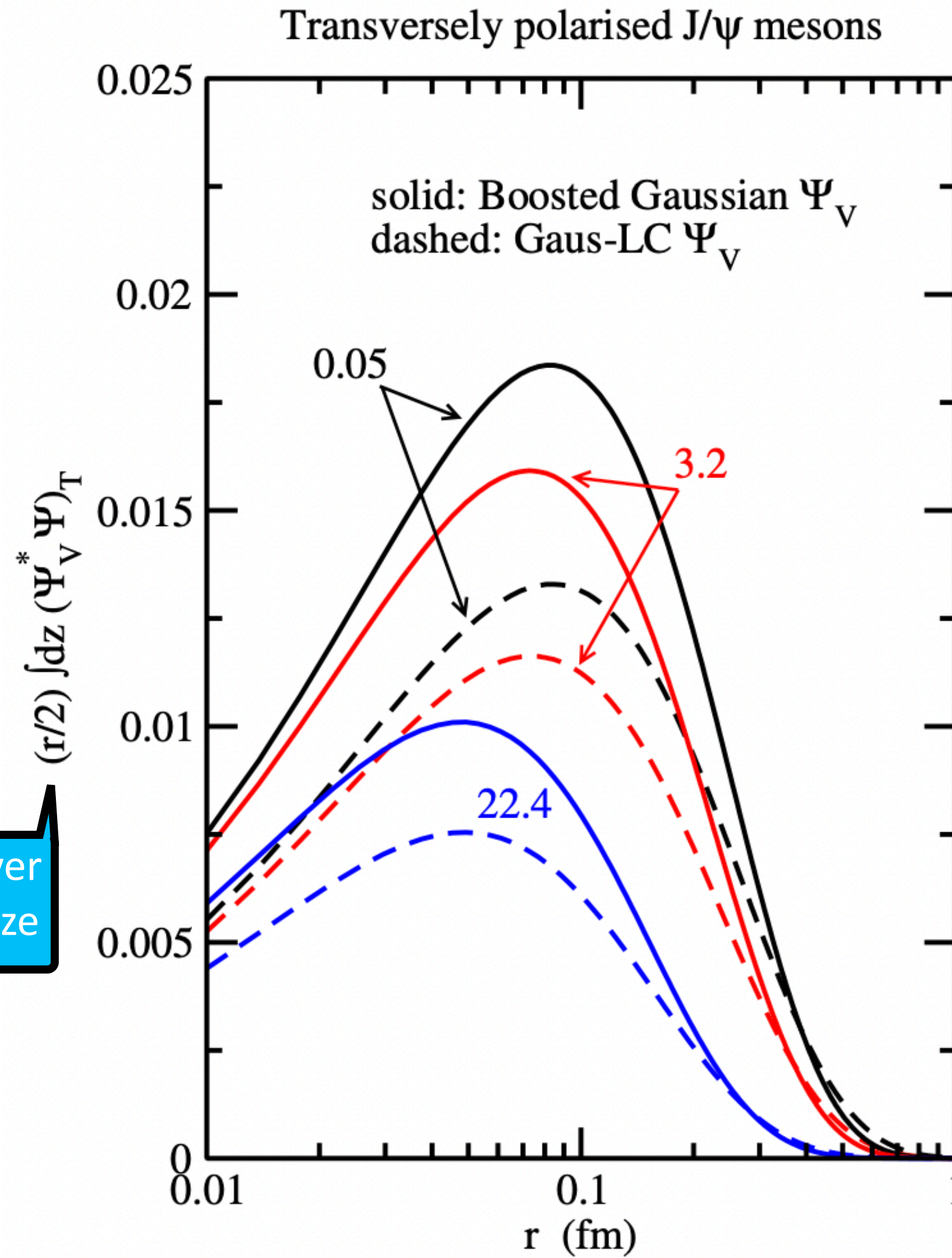
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Normally a correction is used to account for the fact that the matrix element may not be fully real

1

Forward wave functions

Forward wave functions, integrated over energy fraction and scaled by dipole size

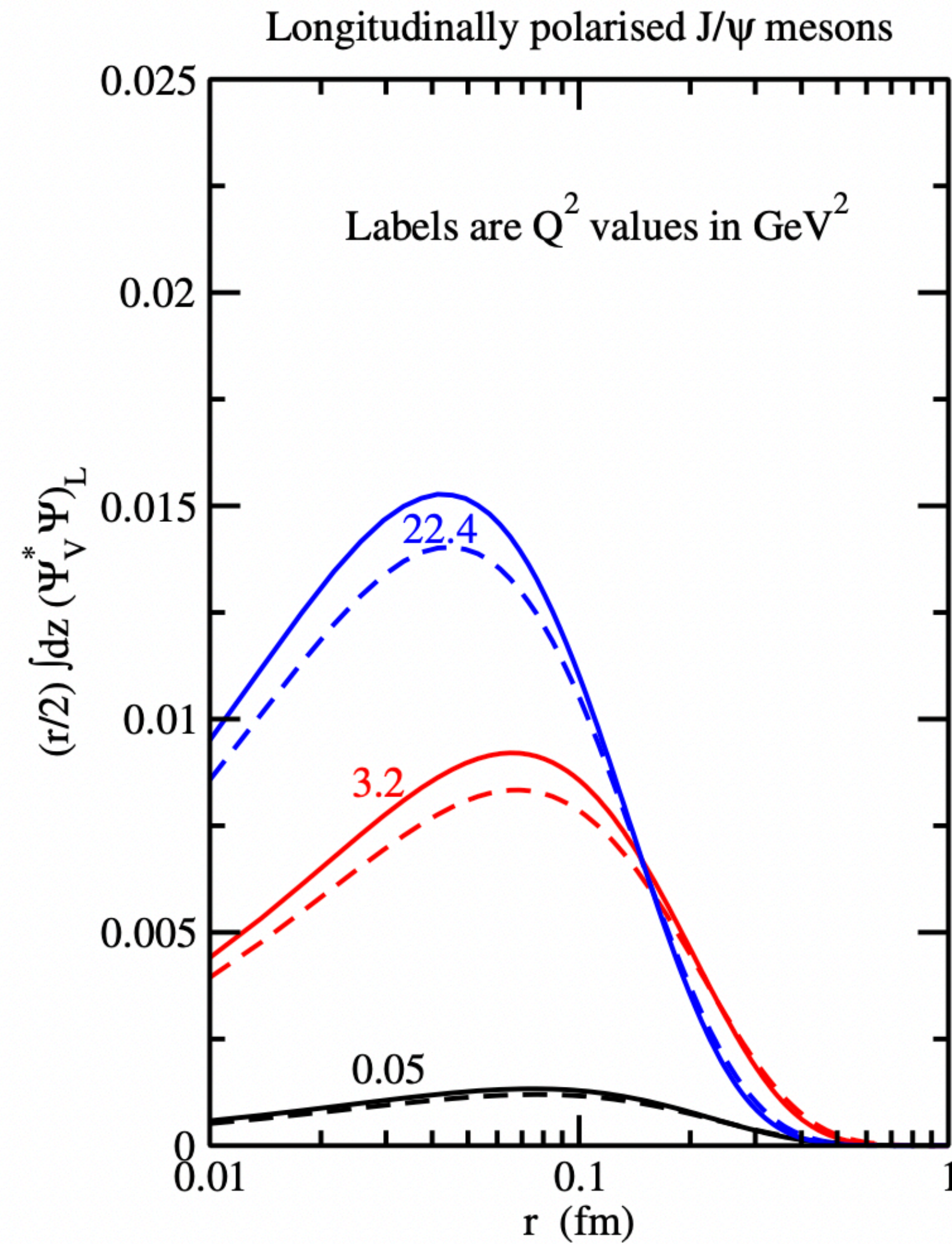
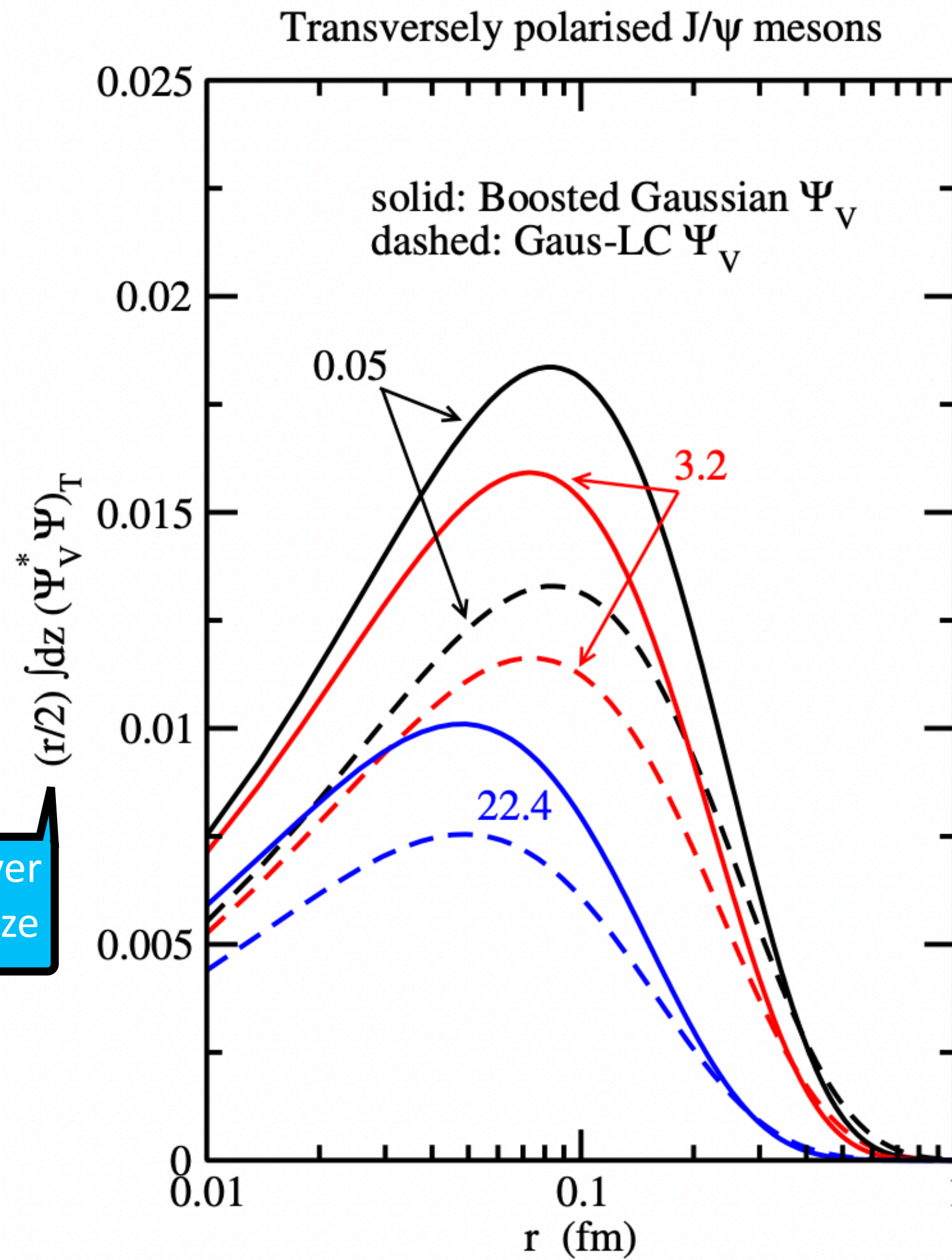


1

Forward wave functions

Forward wave functions, integrated over energy fraction and scaled by dipole size

$$\int d\vec{r} \rightarrow \int r dr d\phi$$



2006: Diffractive vector meson production in the dipole approach (2/5)

1

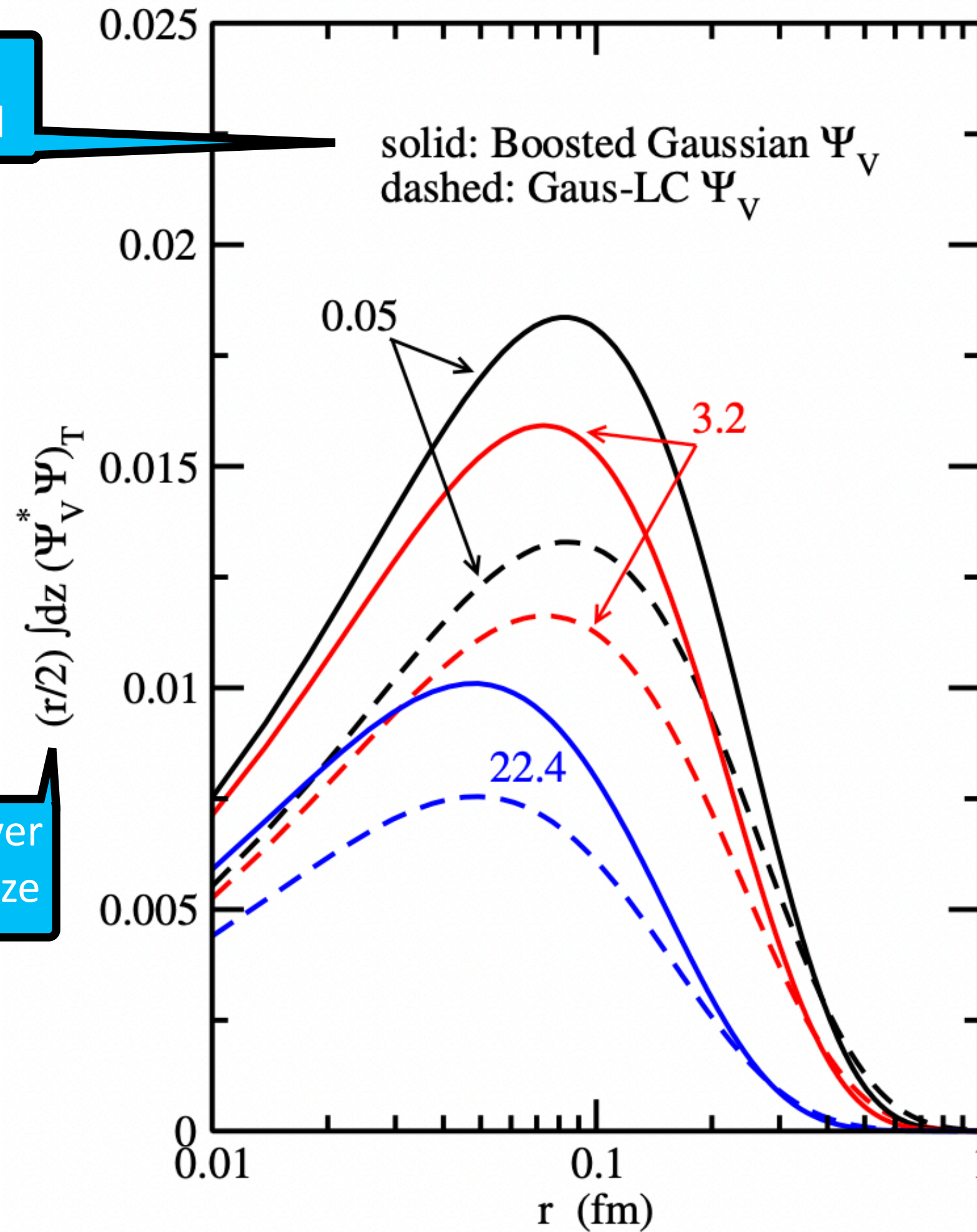
Forward wave functions

The QED part is computable, but the vector meson part has to be modelled

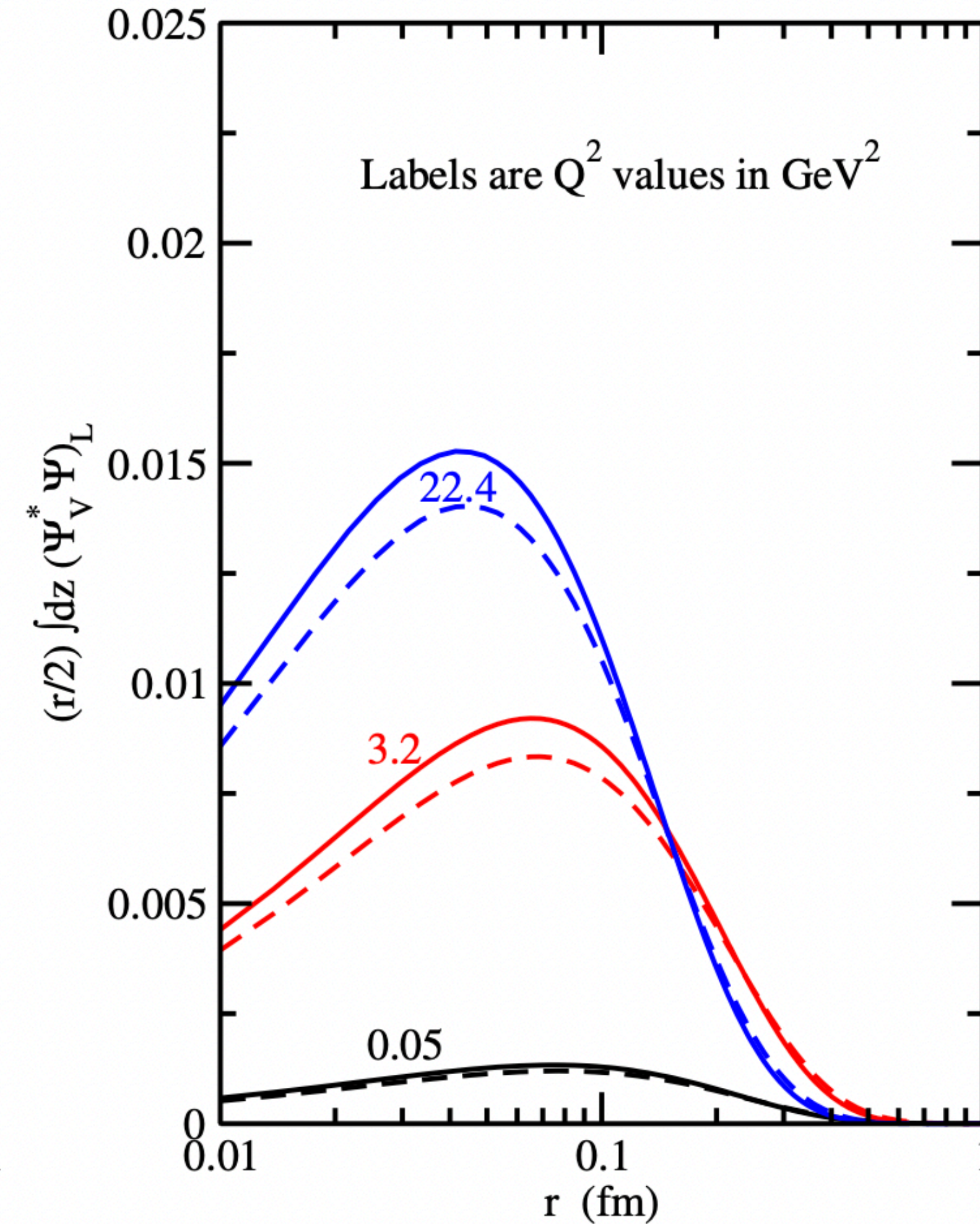
Forward wave functions, integrated over energy fraction and scaled by dipole size

$$\int d\vec{r} \rightarrow \int r dr d\phi$$

Transversely polarised J/ψ mesons



Longitudinally polarised J/ψ mesons



2006: Diffractive vector meson production in the dipole approach (2/5)

1

Forward wave functions

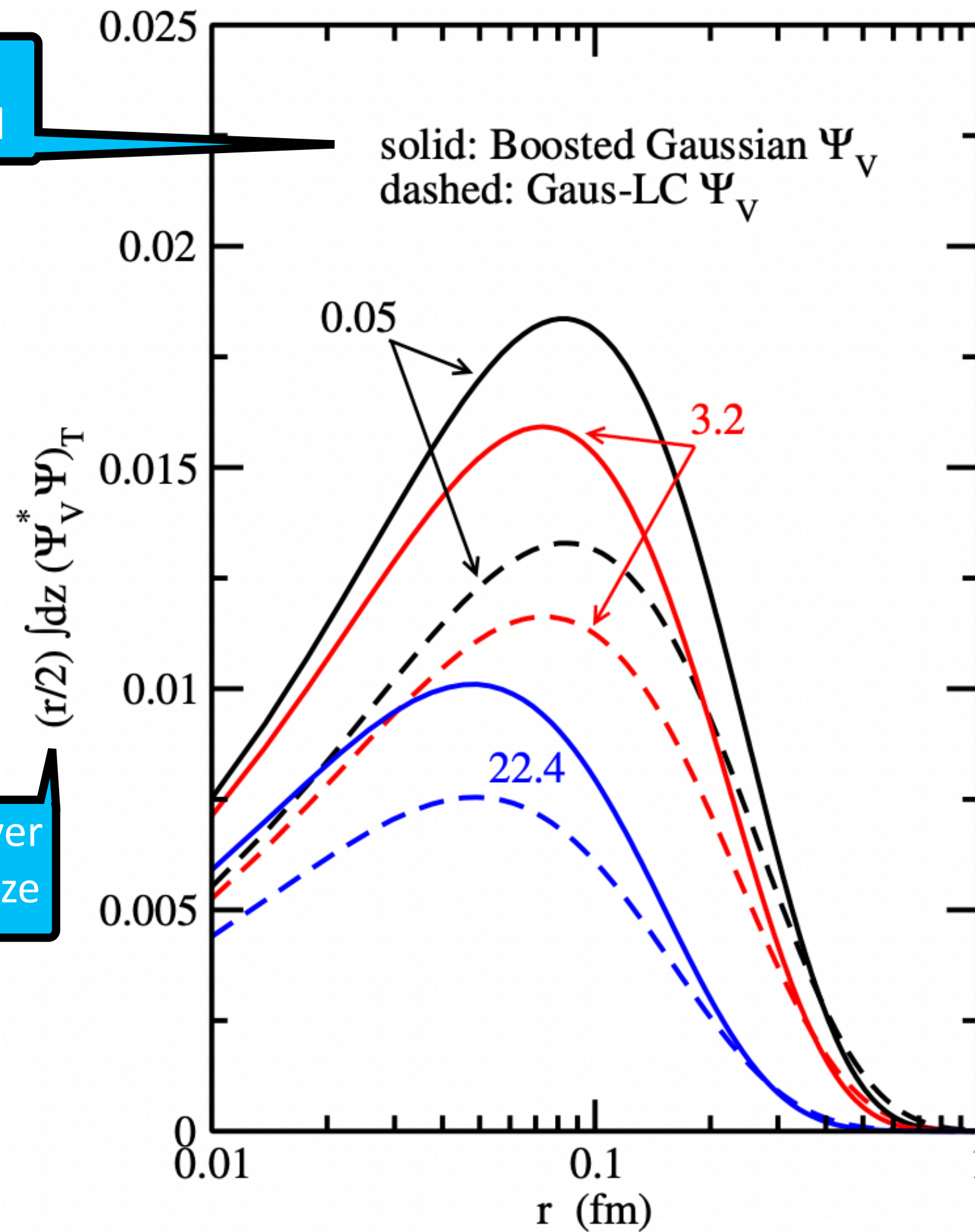
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Modelling may have a strong influence in the normalisation.

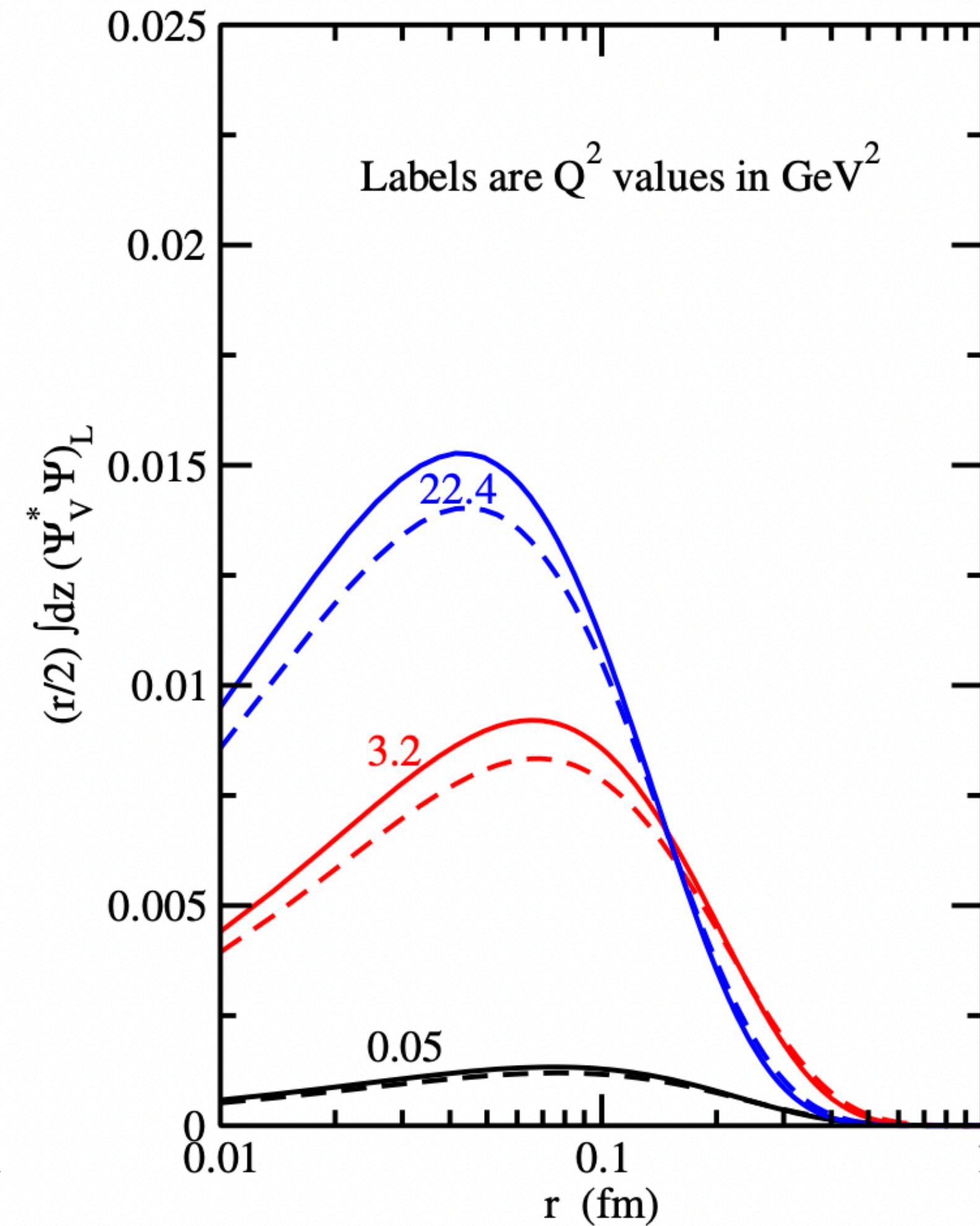
Forward wave functions, integrated over energy fraction and scaled by dipole size

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2006: Diffractive vector meson production in the dipole approach (2/5)

1 Forward wave functions

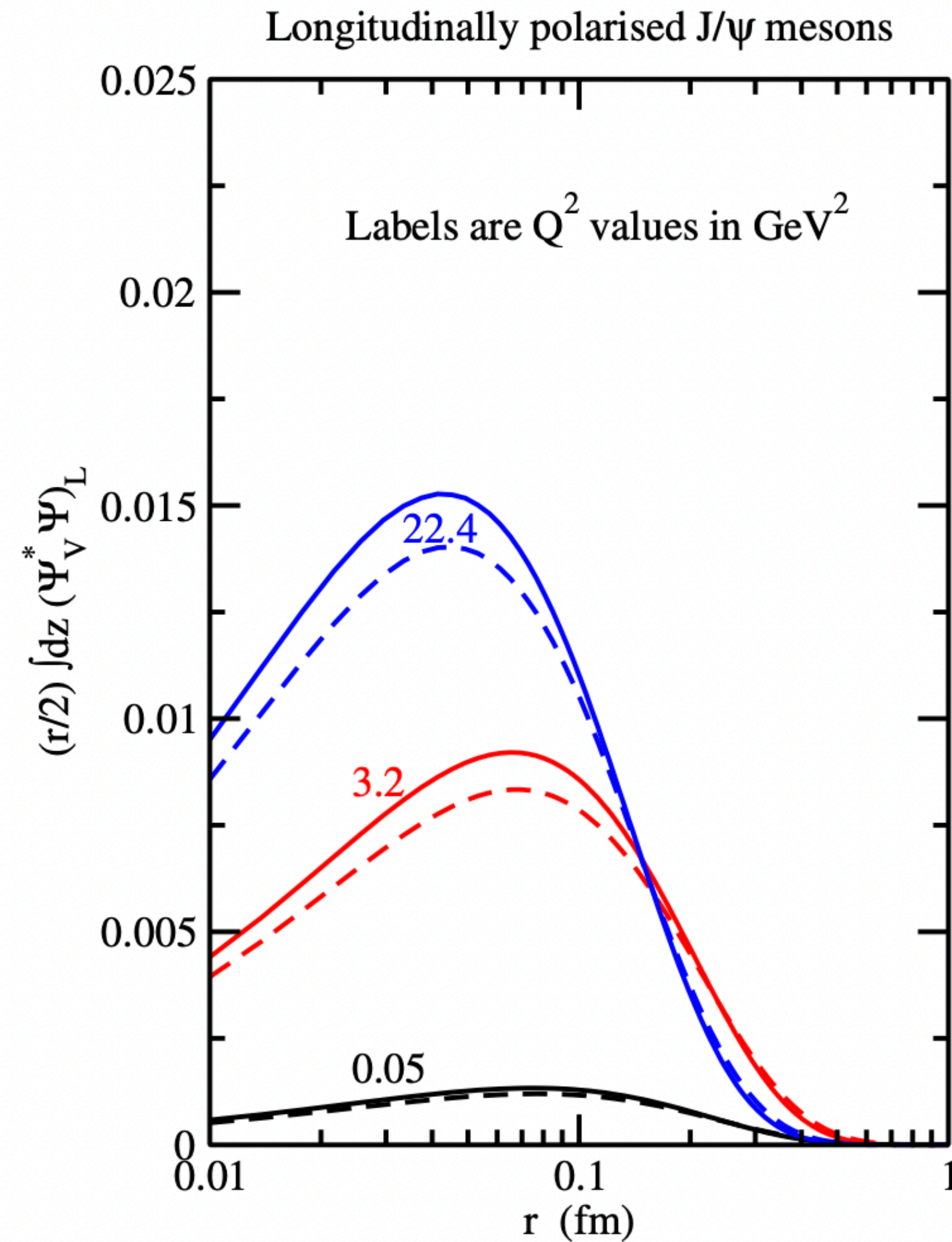
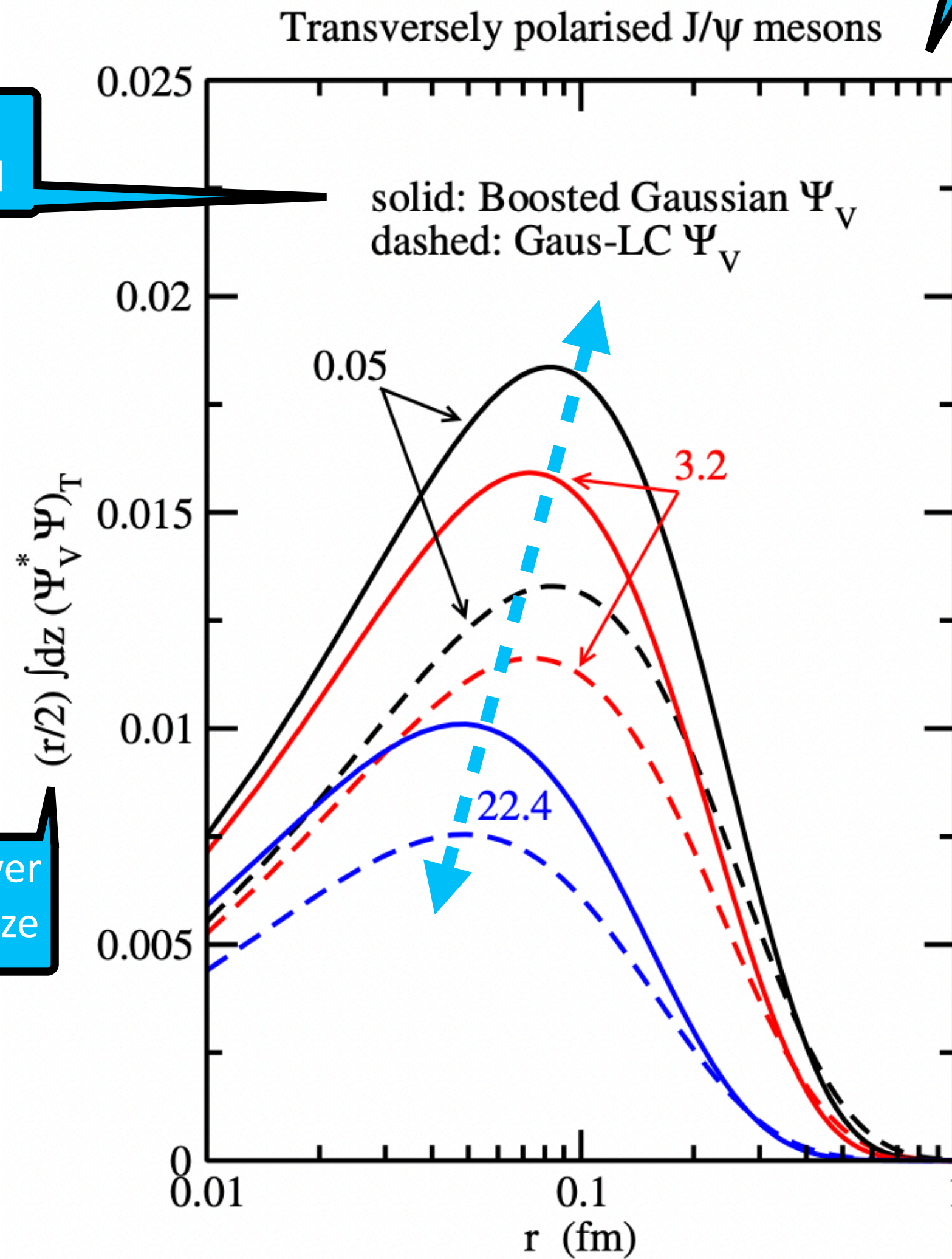
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Forward wave functions, integrated over energy fraction and scaled by dipole size

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Position of the peak moves with virtuality selecting specific dipole sizes



2006: Diffractive vector meson production in the dipole approach (2/5)

1 Forward wave functions

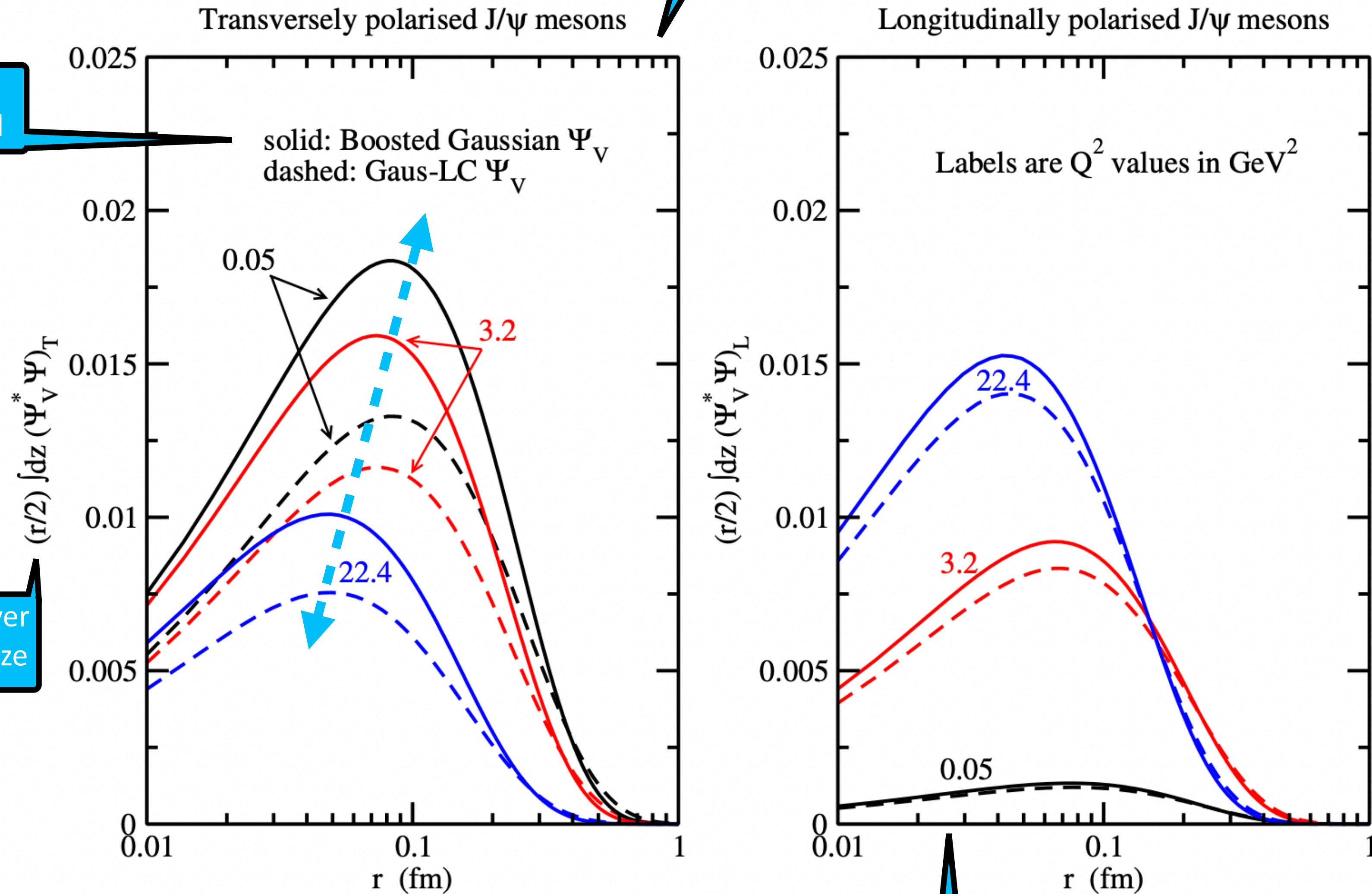
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Position of the peak moves with virtuality selecting specific dipole sizes



In (quasi-) photoproduction, almost no longitudinal

2006: Diffractive vector meson production in the dipole approach (2/5)

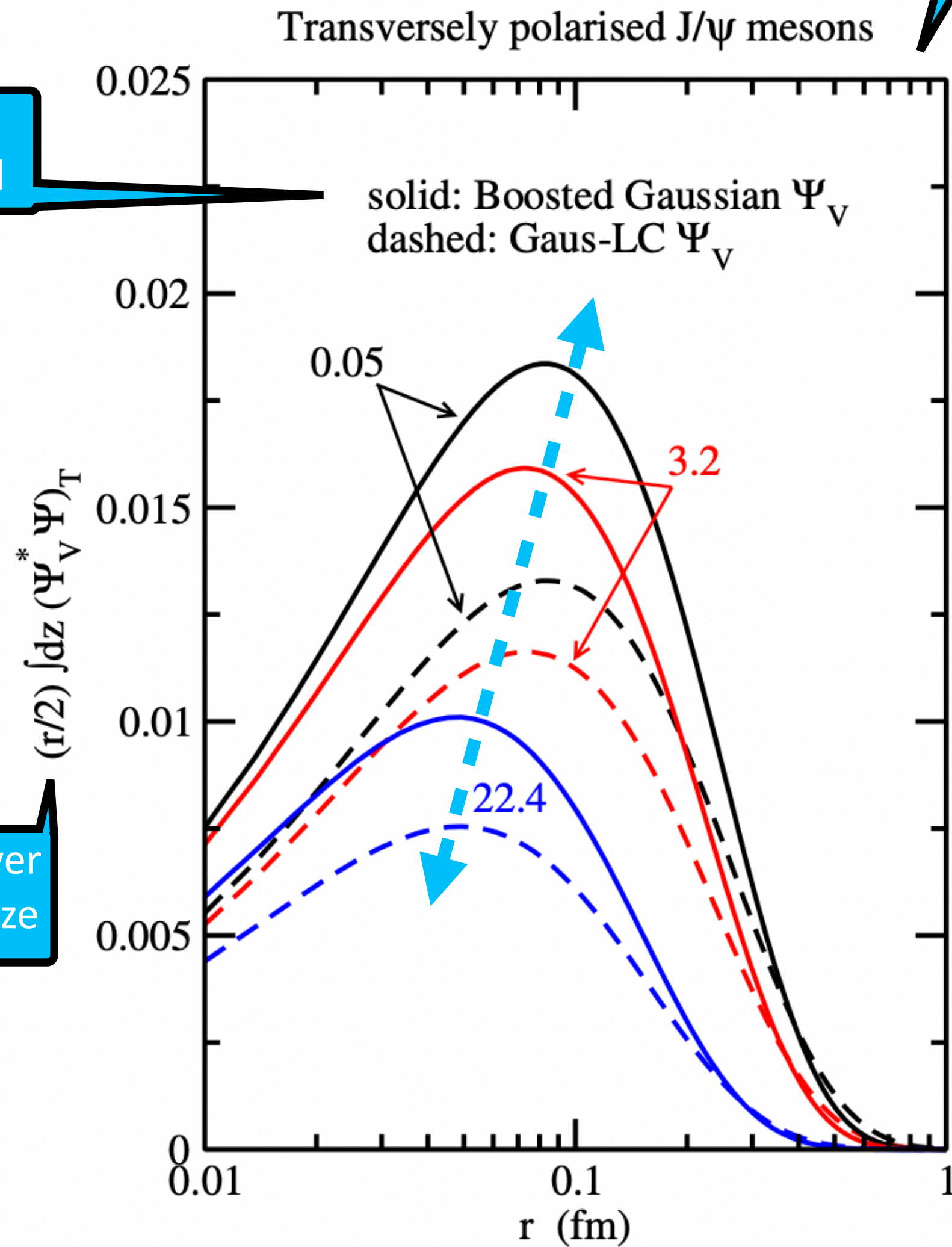
1 Forward wave functions

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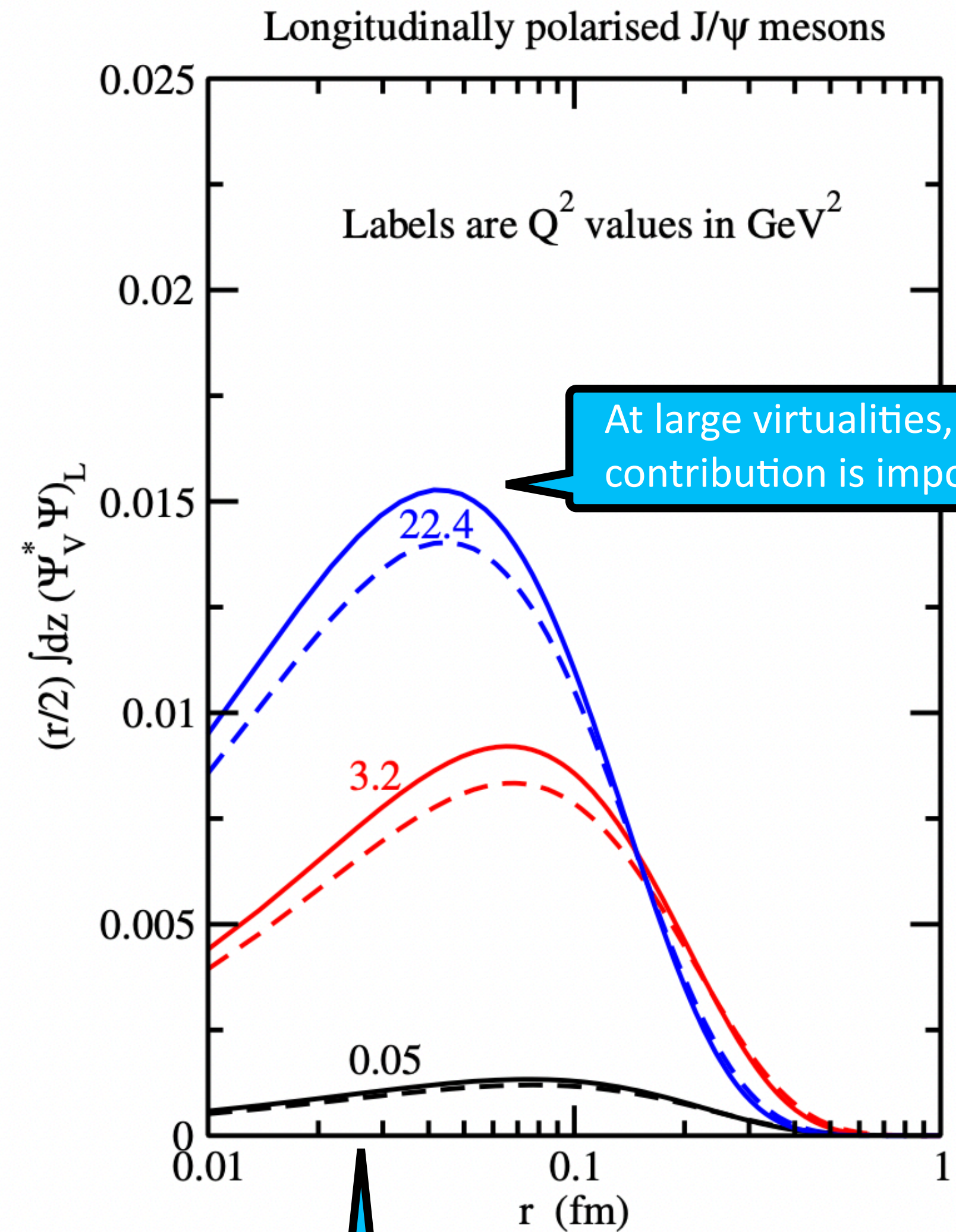
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Forward wave functions, integrated over energy fraction and scaled by dipole size

$$\int d\vec{r} \rightarrow \int r dr d\phi$$



Position of the peak moves with virtuality selecting specific dipole sizes



At large virtualities, the longitudinal contribution is important

In (quasi-) photoproduction, almost no longitudinal

2

Dipole cross sections

2

Dipole cross sections

GBW approach

$$\begin{aligned}\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} &\equiv 2[1 - \text{Re}S(x, r, b)] \equiv 2\mathcal{N}(x, r, b) \\ &= 2\mathcal{N}(x, r)\Theta(b_S - b),\end{aligned}$$

2

Dipole cross sections

GBW approach

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$$= 2\mathcal{N}(x, r)\Theta(b_S - b),$$

Profile in impact parameter

$$\sigma_{q\bar{q}}(x, r) = \sigma_0\mathcal{N}(x, r),$$

$$\sigma_0 \equiv 2\pi b_S^2$$

Related to the average square radius of the target in impact parameter

2

Dipole cross sections

b-Sat approach

$$\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} = 2 \left[1 - \exp\left(-\frac{\pi^2}{2N_c} r^2 \alpha_S(\mu^2) x g(x, \mu^2) T(b)\right) \right].$$

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Profile in impact parameter

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$$T_G(b) = \frac{1}{2\pi B_G} e^{-(b^2/2B_G)},$$

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$$\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} = 2 \left[1 - \exp\left(-\frac{\pi^2}{2N_c} r^2 \alpha_S(\mu^2) x g(x, \mu^2) T(b)\right) \right].$$

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Profile in impact parameter

$$T_G(b) = \frac{1}{2\pi B_G} e^{-(b^2/2B_G)},$$

Related to the average square radius of the target in impact parameter

Profile in impact parameter

b-CGC approach

$$\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \equiv 2\mathcal{N}(x, r, b)$$

$$= 2 \times \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2}\right)^{2(\gamma_s + (1/\kappa\lambda Y)\ln(2/rQ_s))} & : rQ_s \leq 2 \\ 1 - e^{-A\ln^2(BrQ_s)} & : rQ_s > 2 \end{cases},$$

2006: Diffractive vector meson production in the dipole approach (3/5)

2

Dipole cross sections

GBW approach

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Profile in impact parameter

b-CGC approach

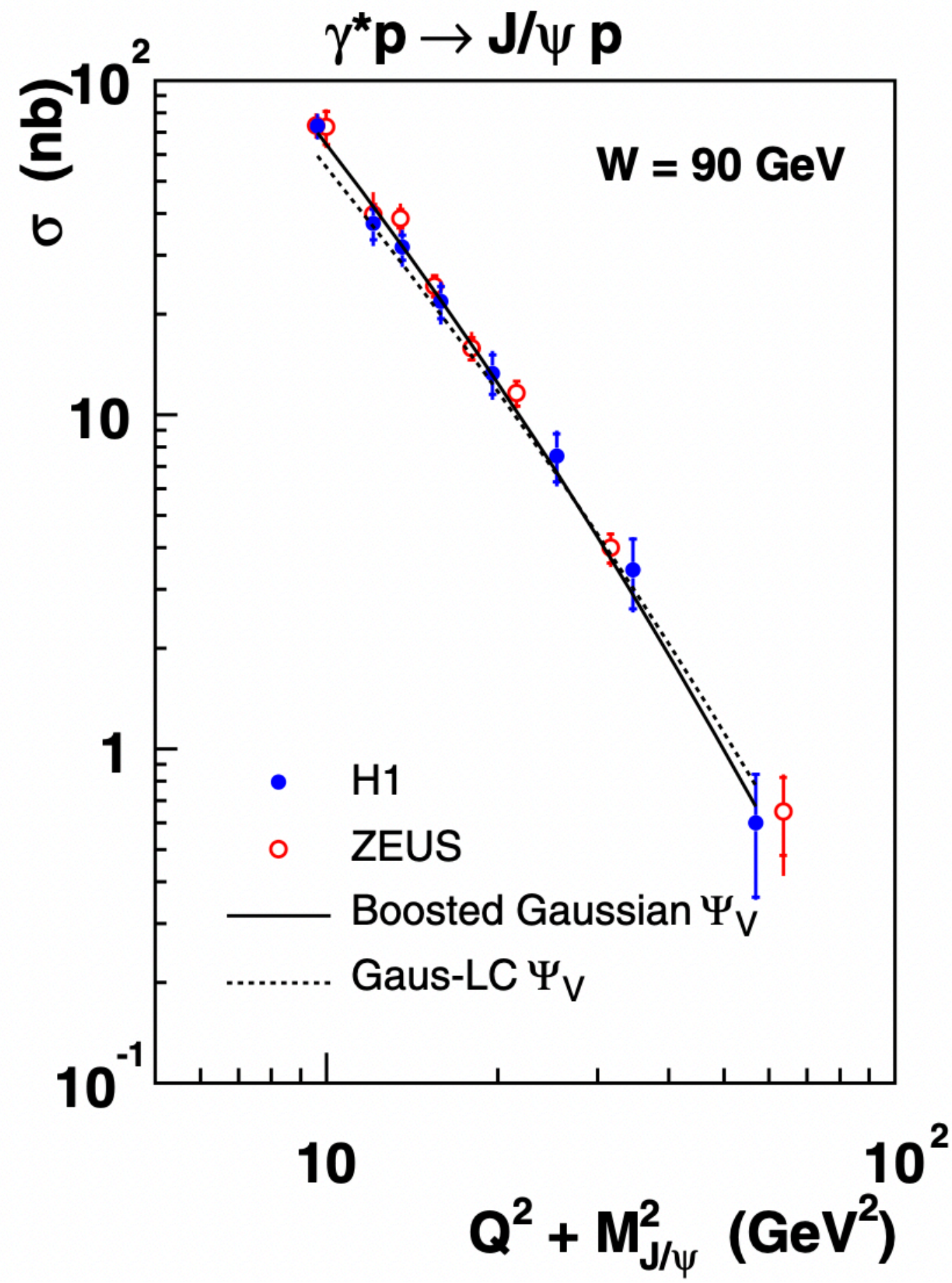
$$\frac{d\sigma_{q\bar{q}}}{d^2b} \equiv 2\mathcal{N}(x, r, b)$$

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$$Q_s \equiv Q_s(x, b) = \left(\frac{x_0}{x}\right)^{\lambda/2} \left[\exp\left(-\frac{b^2}{2B_{\text{CGC}}}\right) \right]^{1/2\gamma_s}.$$

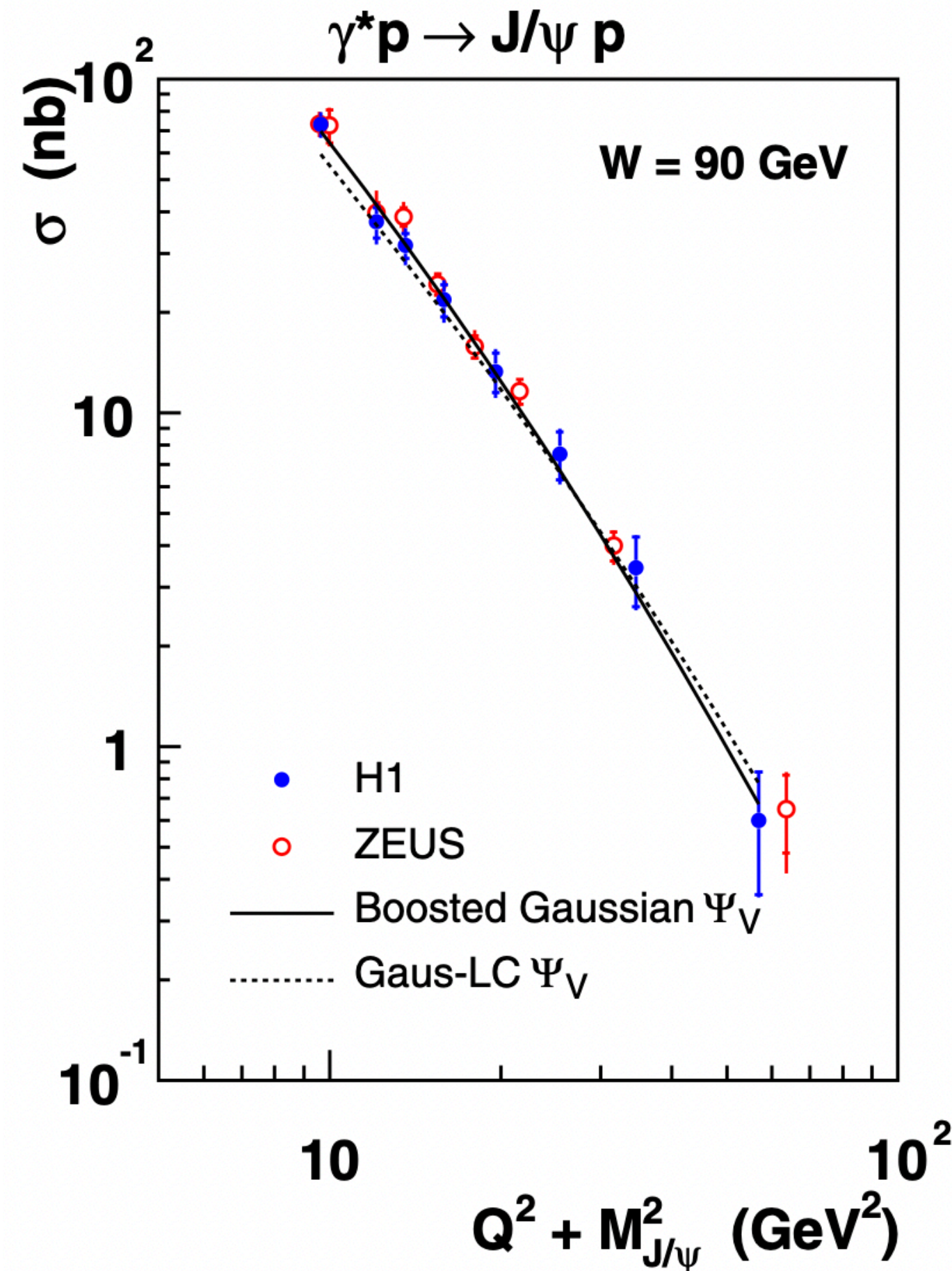
Profile in impact parameter

Results

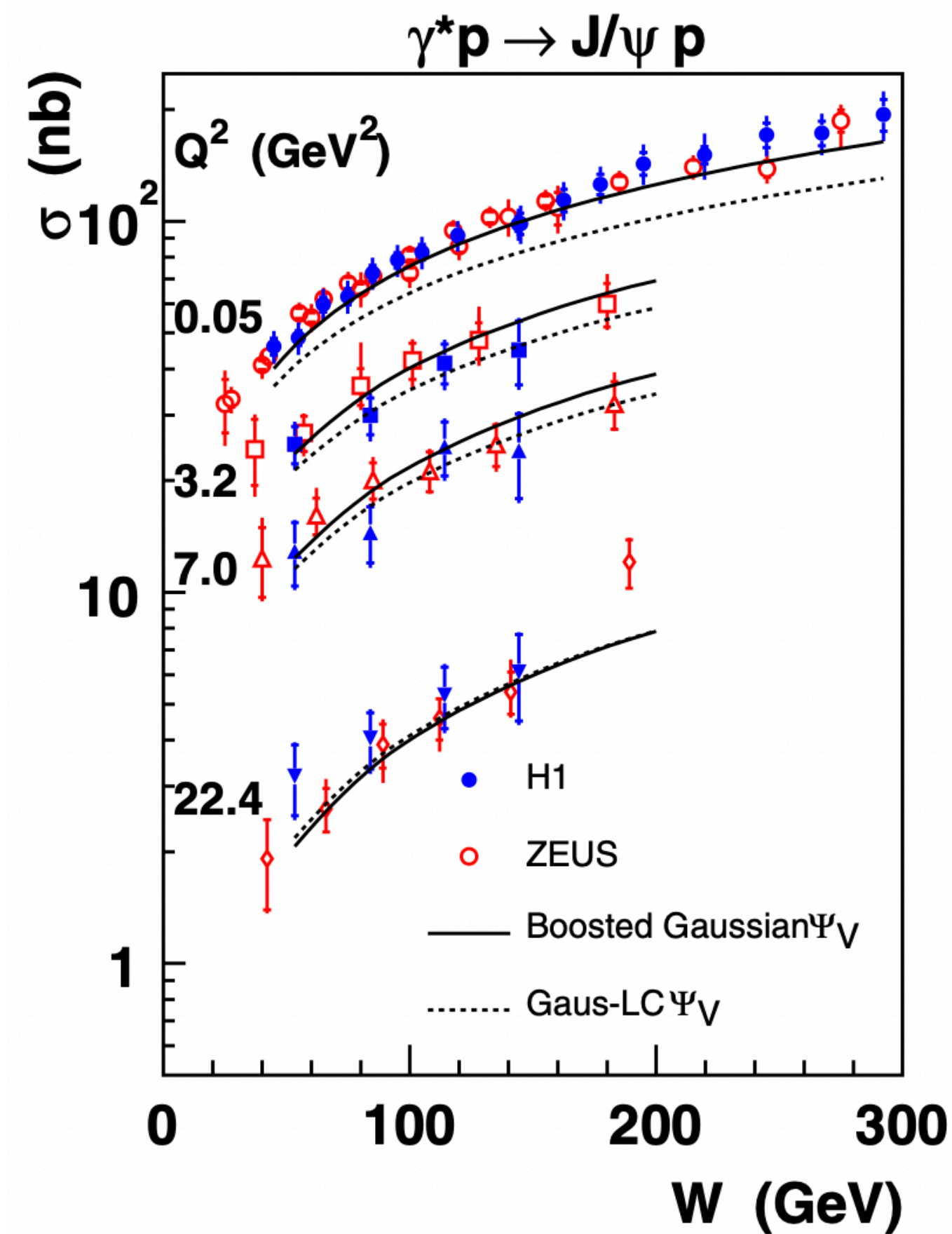


Cross section decreases with the scale

Results

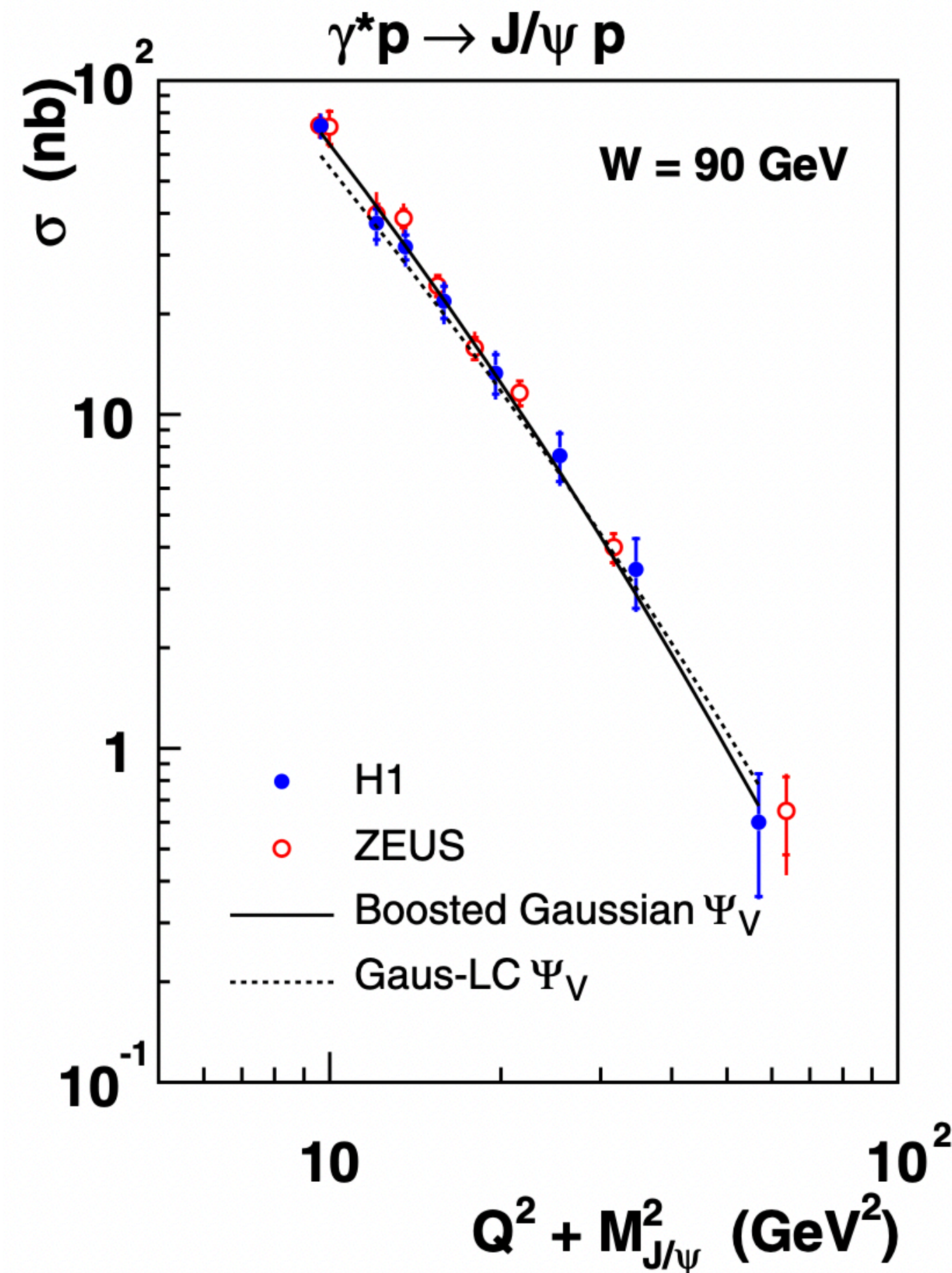


Cross section decreases with the scale

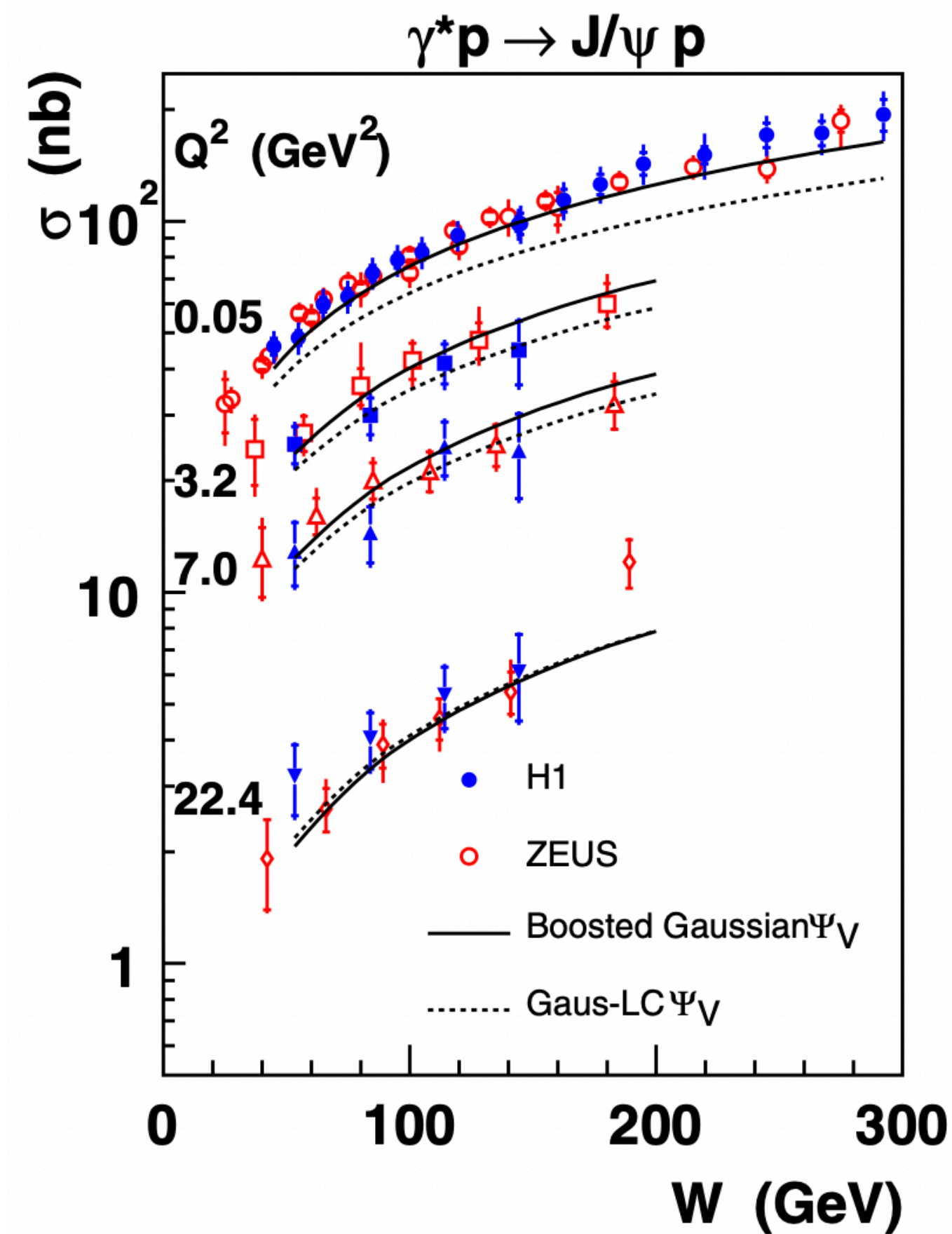


Cross section grows with energy for different virtualities

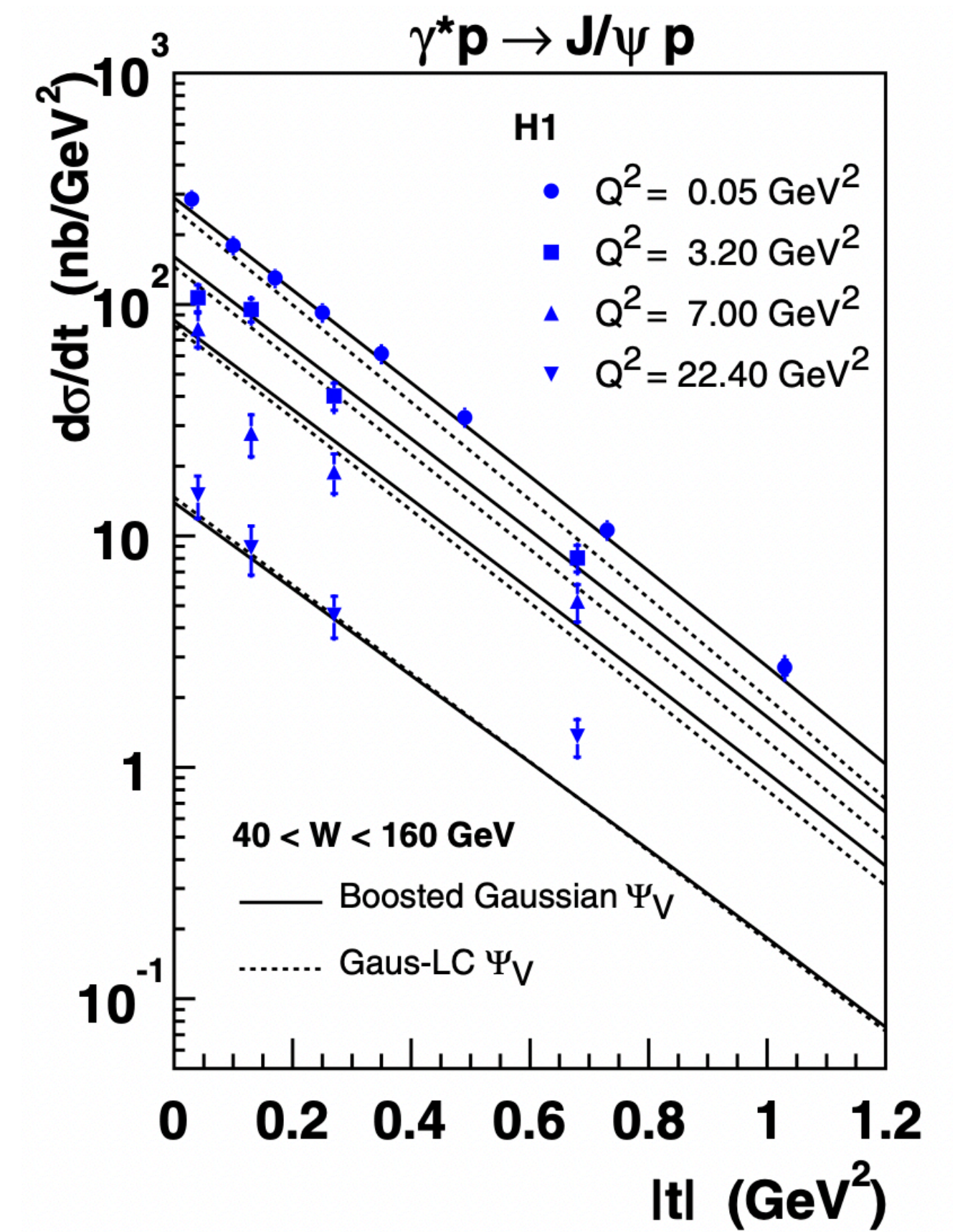
Results



Cross section decreases with the scale

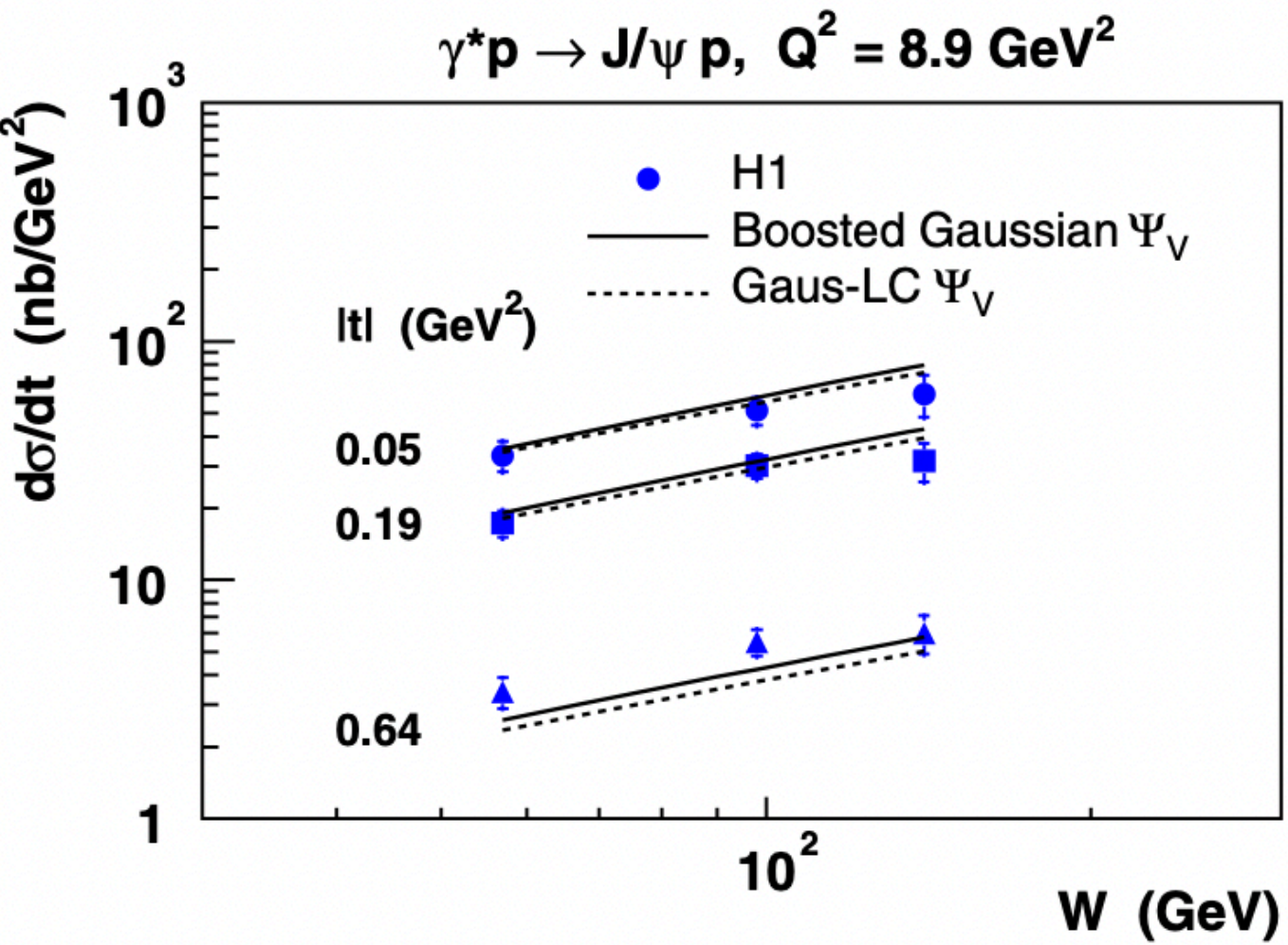
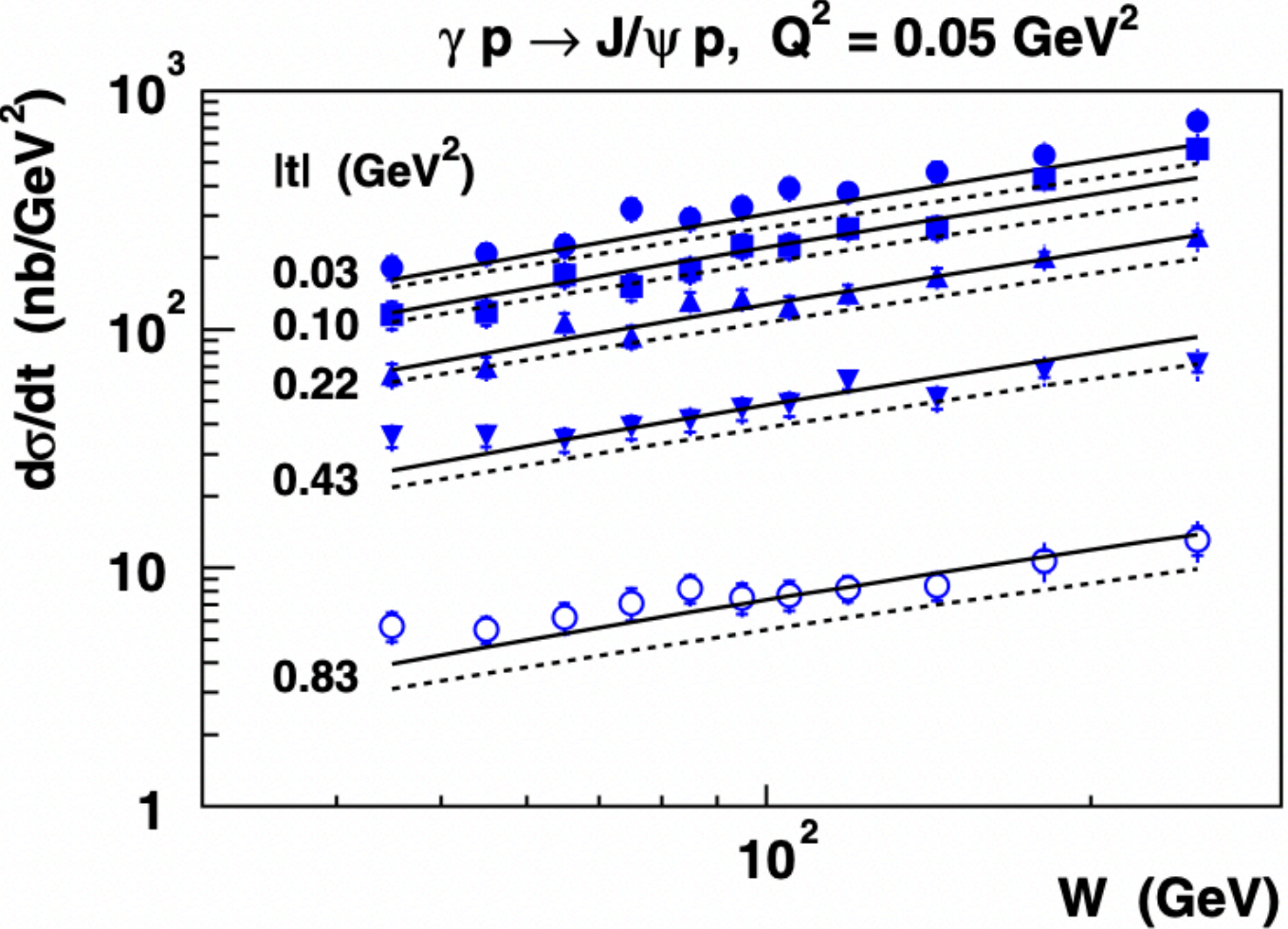


Cross section grows with energy for different virtualities



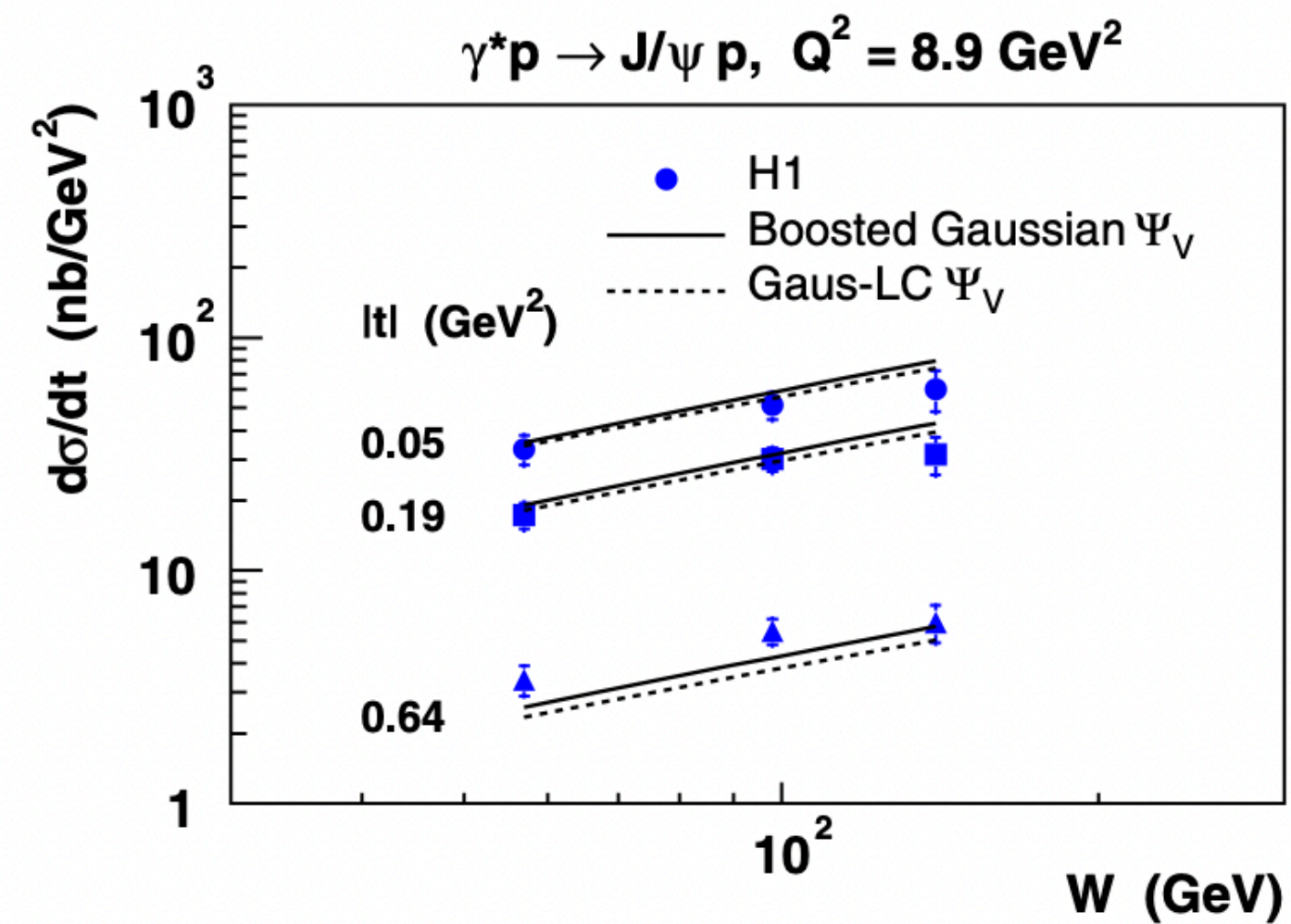
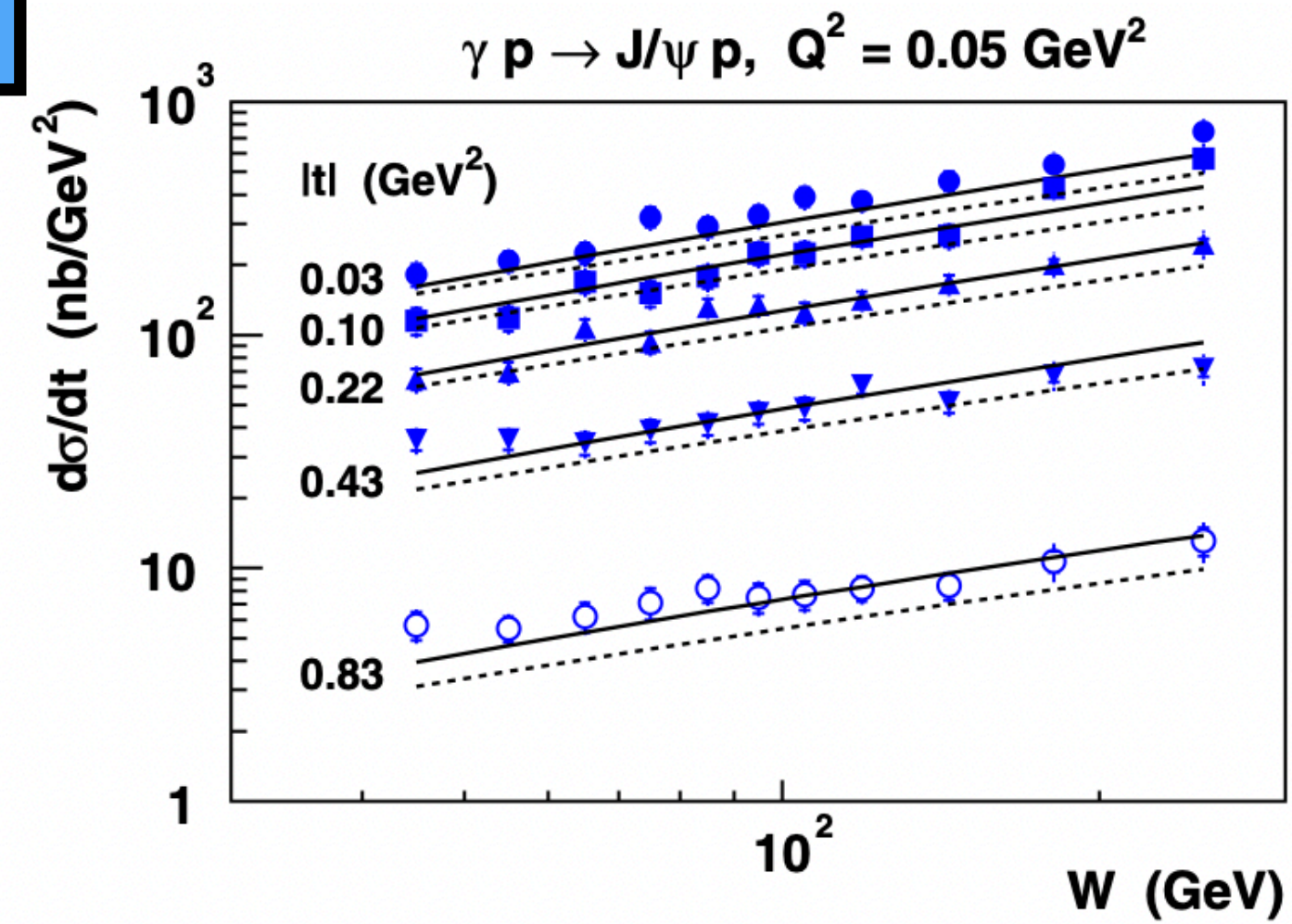
Consistent with Gaussian shape for different virtualities

Results

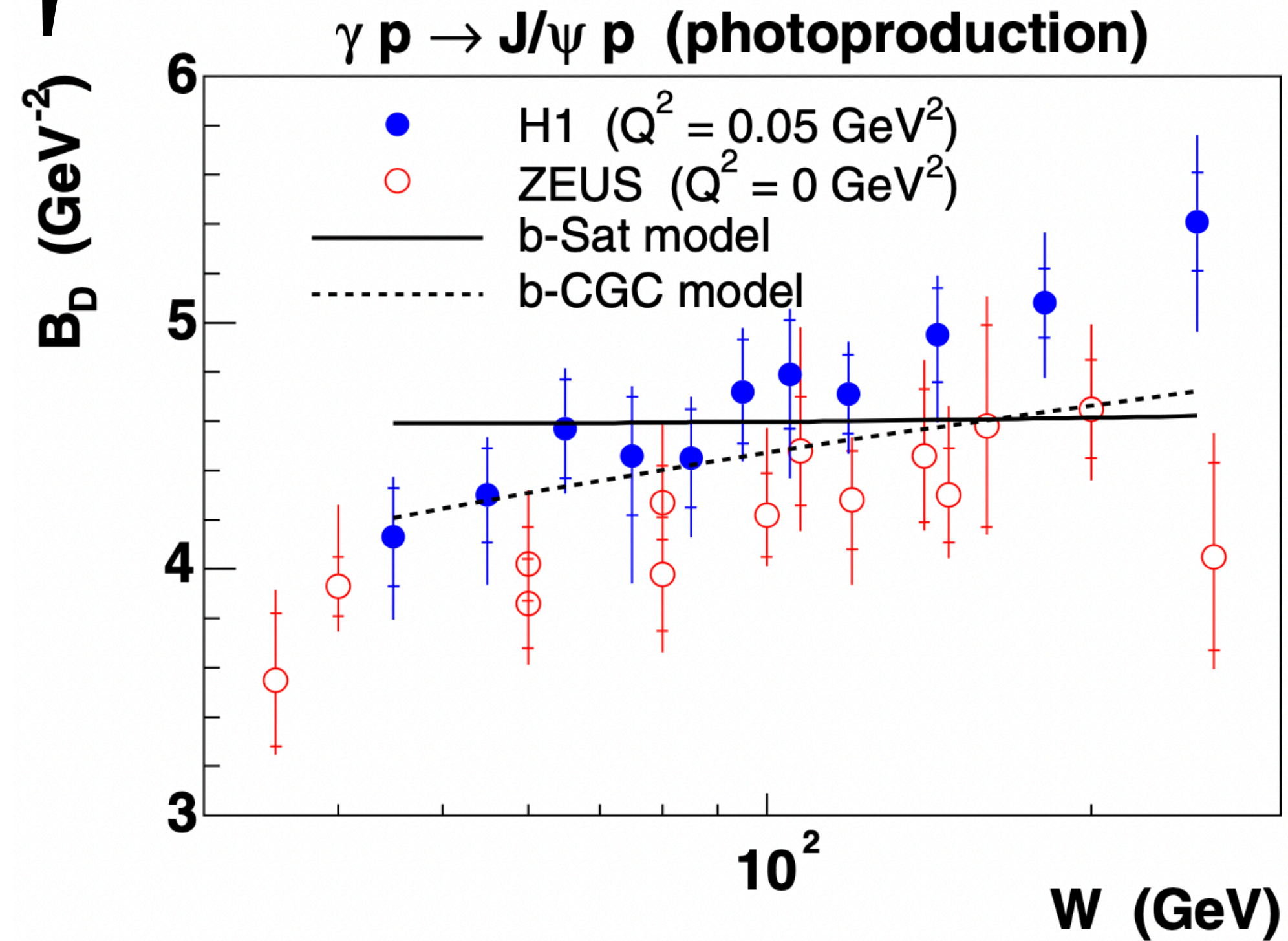


Cross section grows with energy for different momentum transfer

Results



Gaussian profile grows with energy



Cross section grows with energy for different momentum transfer

Reminder: Geometric scaling in DIS

$$\sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(x, Q^2) = \sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(\tau), \quad \tau = Q^2 / Q_s^2(x).$$

$$Q_s(x) = Q_0 \left(\frac{x}{x_0} \right)^{-\lambda/2}, \quad Q_0 \equiv 1 \text{ GeV}$$

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Geometric scaling in diffractive VM production

$$\sigma_{\text{VM}}^{\gamma^* p \rightarrow VP}(x_{\mathbb{P}}, Q^2) = \sigma_{\text{VM}}^{\gamma^* p \rightarrow VP}(\tau_V)$$

$$\tau_V = (Q^2 + M_V^2) / Q_s^2(x_{\mathbb{P}}).$$

2006: Geometric scaling for vector mesons

Reminder: Geometric scaling in DIS

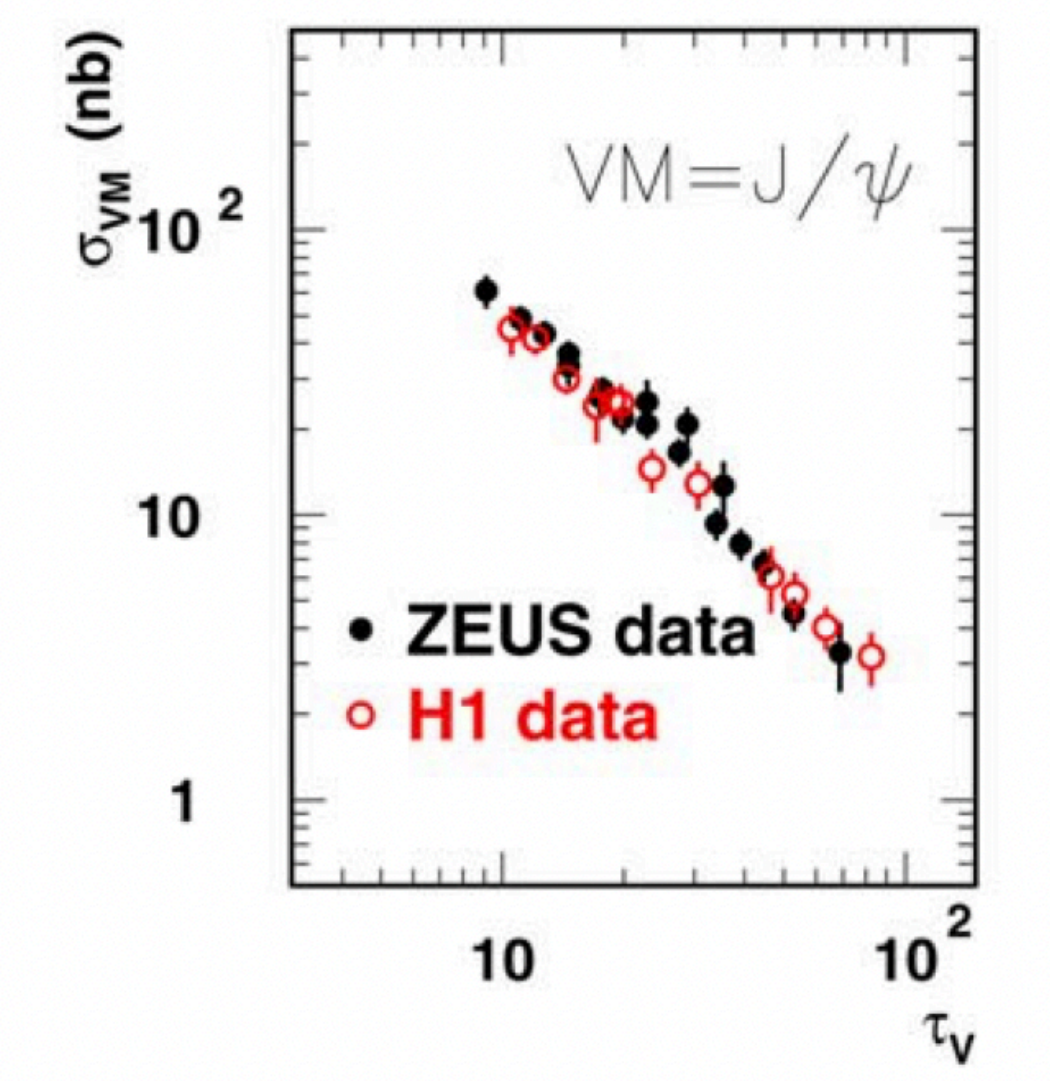
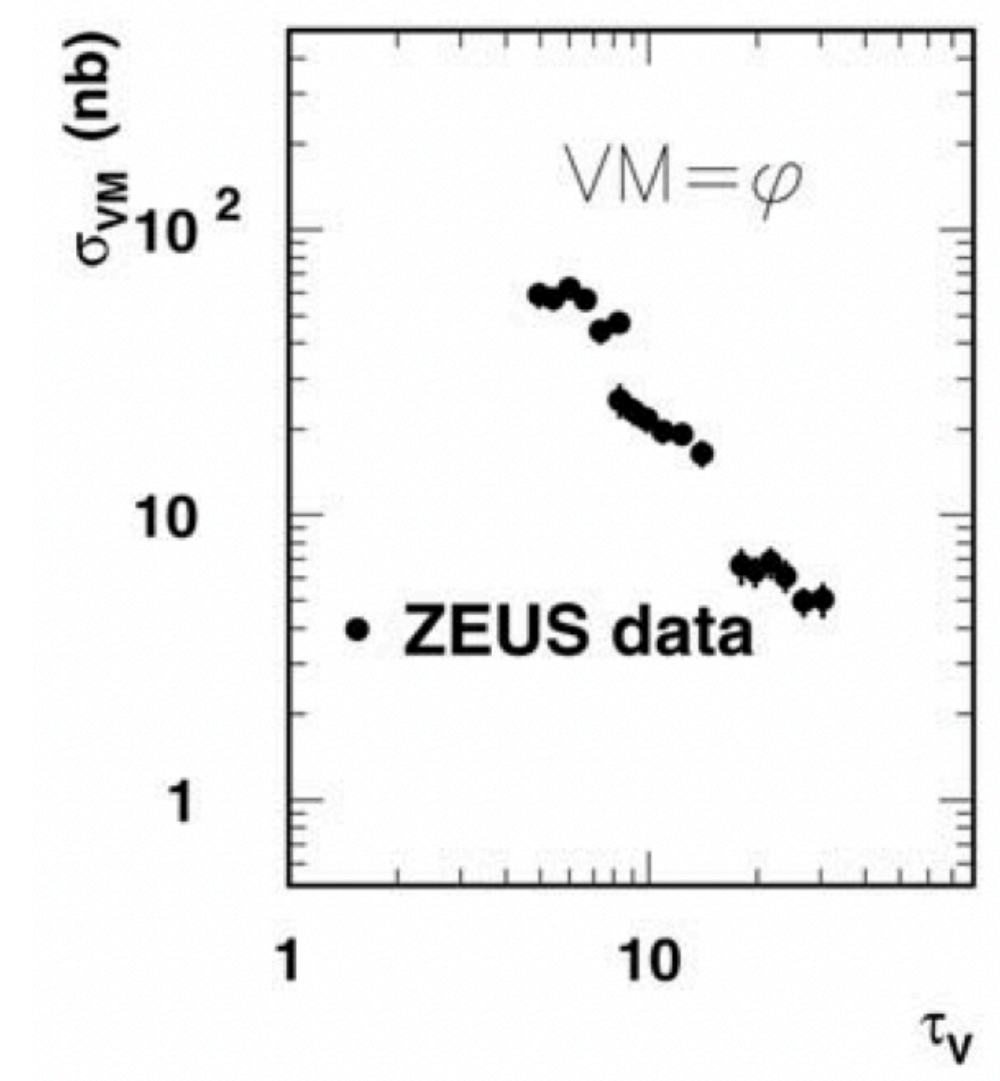
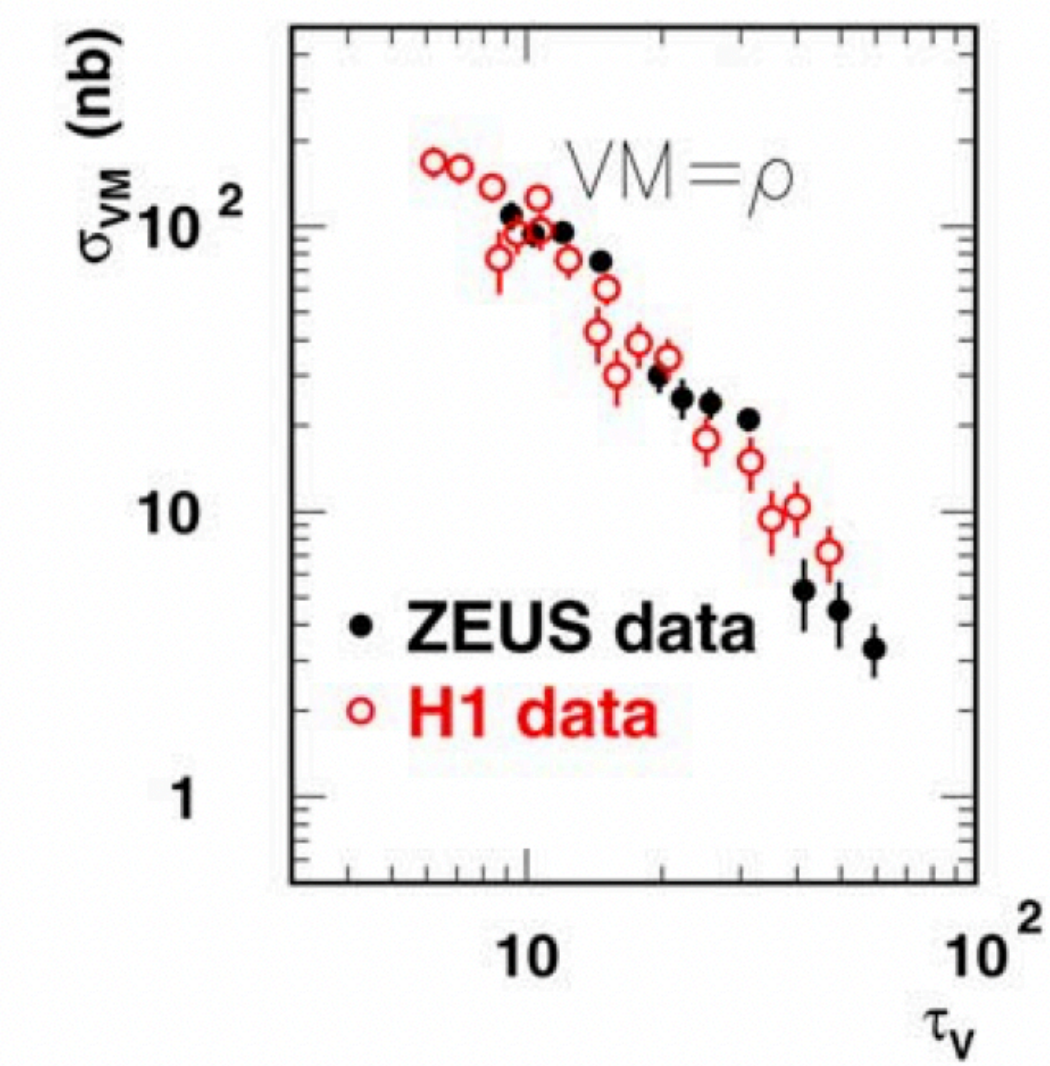
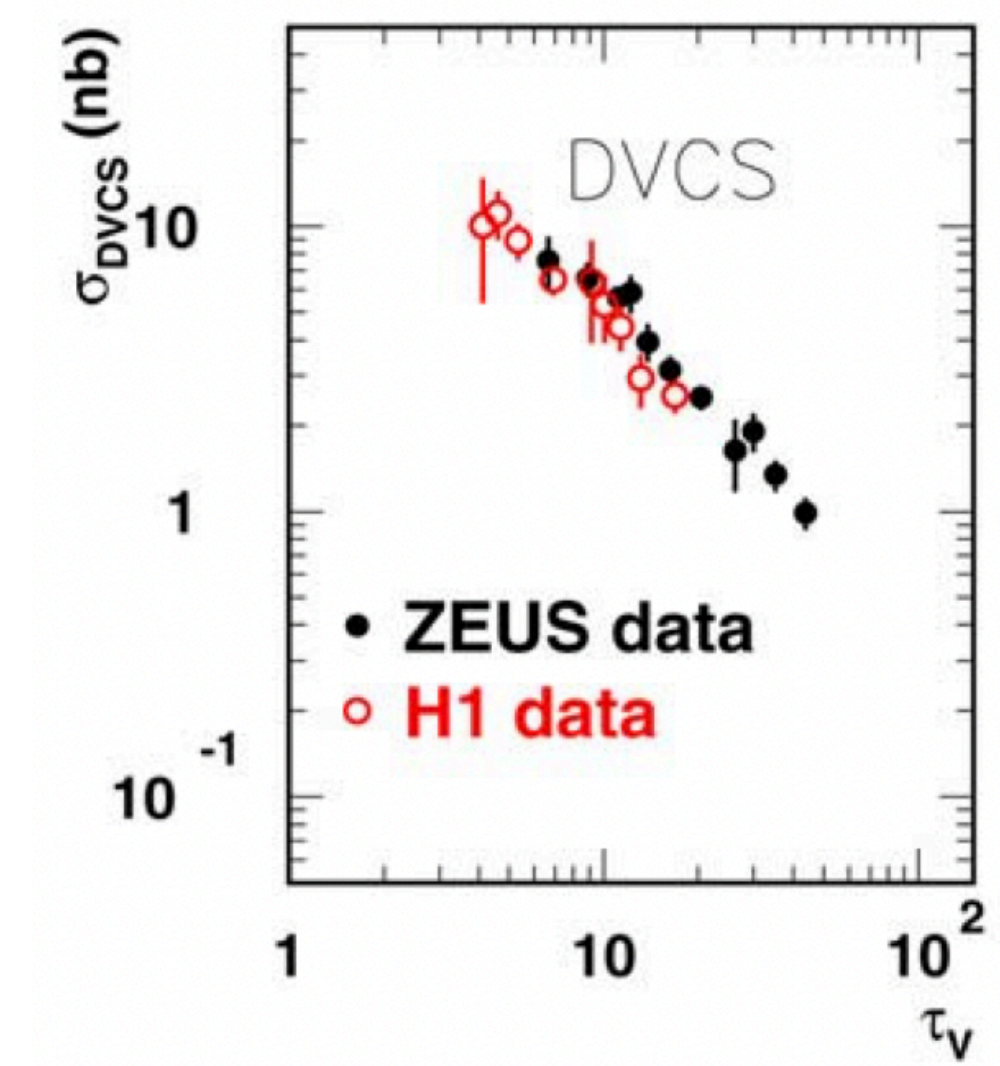
$$\sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(x, Q^2) = \sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(\tau), \quad \tau = Q^2 / Q_s^2(x).$$

$$Q_s(x) = Q_0 \left(\frac{x}{x_0} \right)^{-\lambda/2}, \quad Q_0 \equiv 1 \text{ GeV}$$

Geometric scaling in diffractive VM production

$$\sigma_{\text{VM}}^{\gamma^* p \rightarrow VP}(x_{\mathbb{P}}, Q^2) = \sigma_{\text{VM}}^{\gamma^* p \rightarrow VP}(\tau_V)$$

$$\tau_V = (Q^2 + M_V^2) / Q_s^2(x_{\mathbb{P}}).$$



Exclusive diffractive vector meson production is very sensitive to the gluon content of the proton

This process has been extensively studied at HERA as a function of:

Mass of the vector meson

Virtuality of the photon

CMS energy of the photon-proton system

Mandelstam- t

Polarisation structure (not shown)

What about dissociative production?

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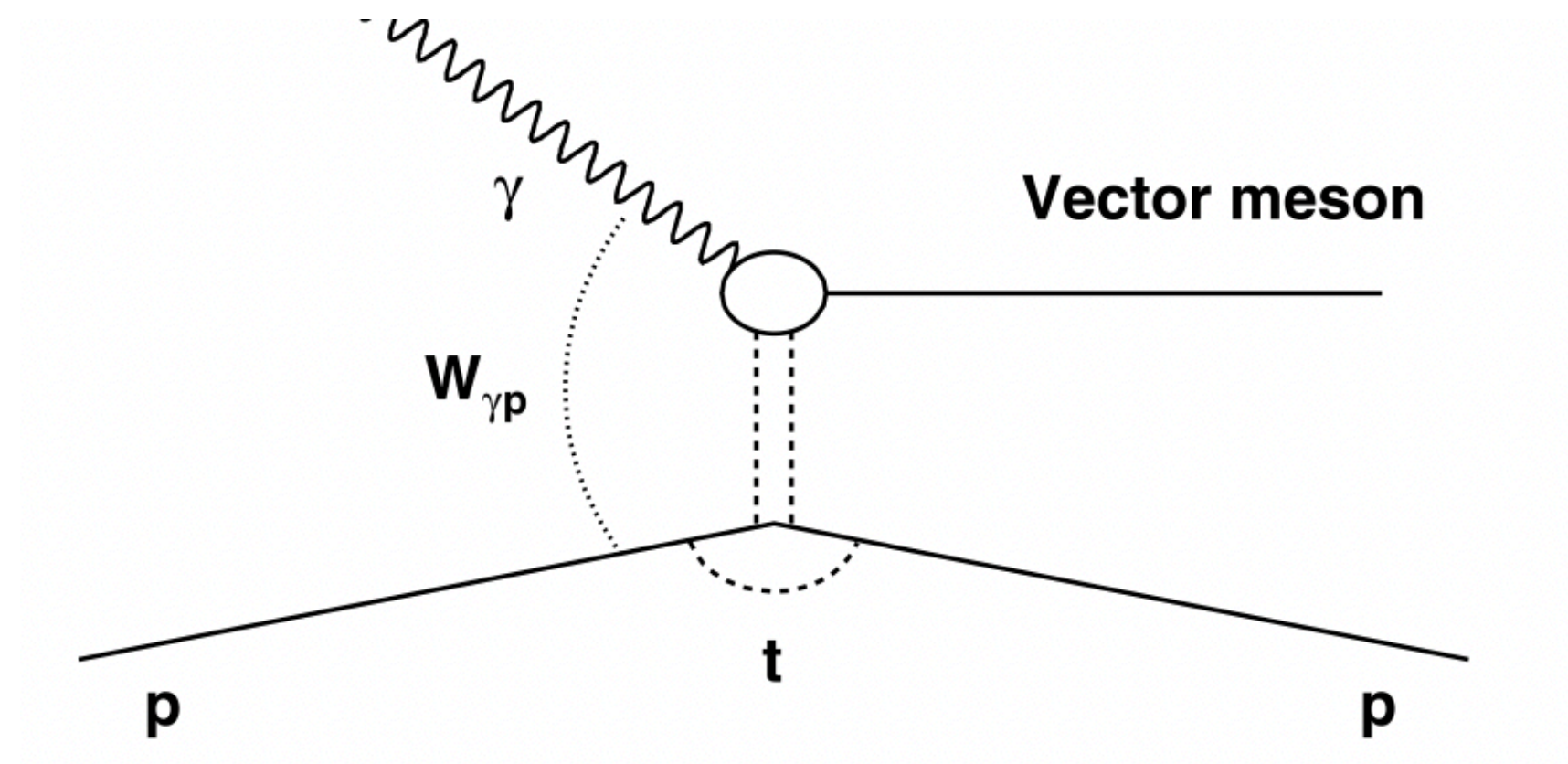
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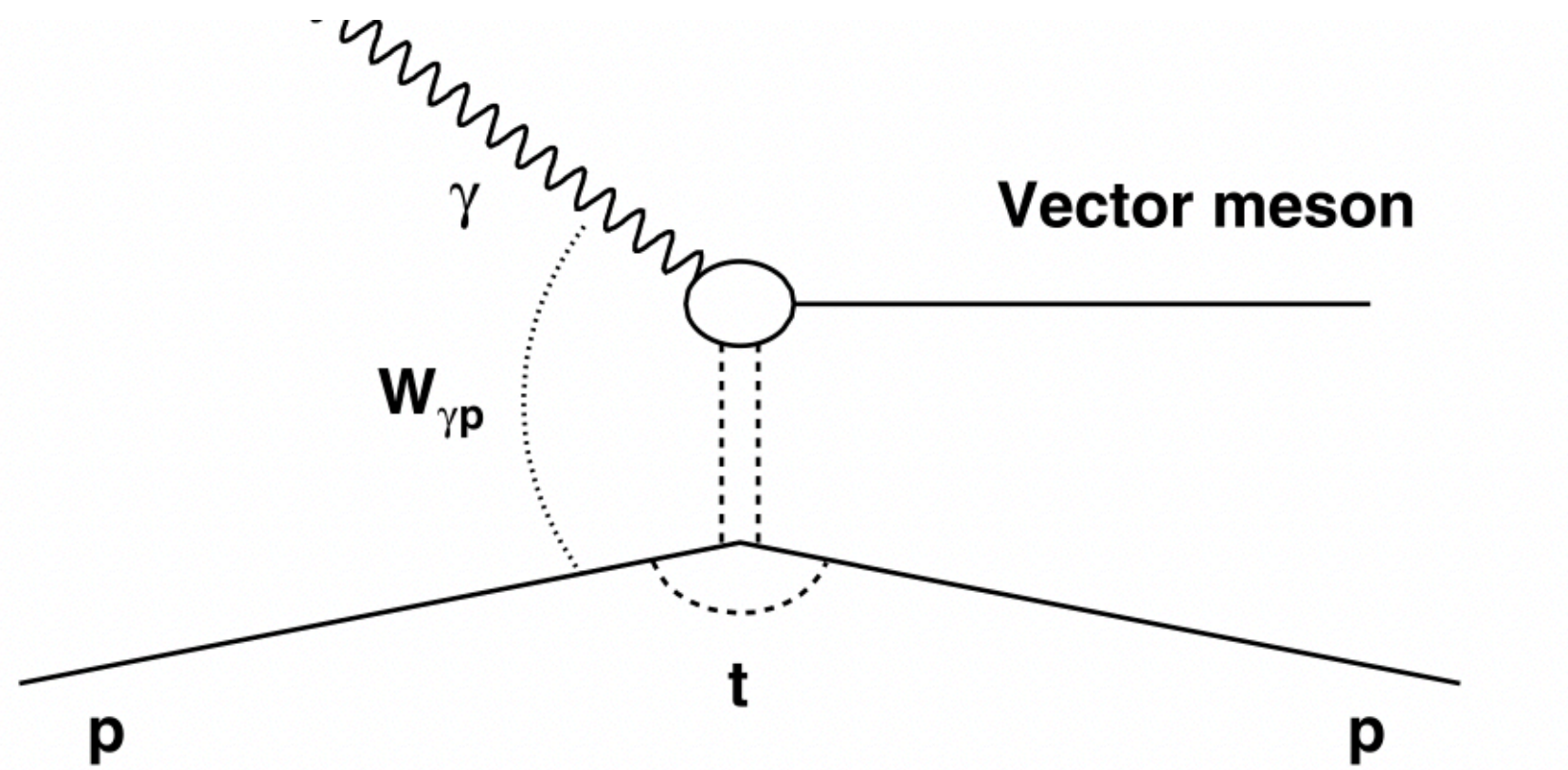
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Dissociative vector meson production

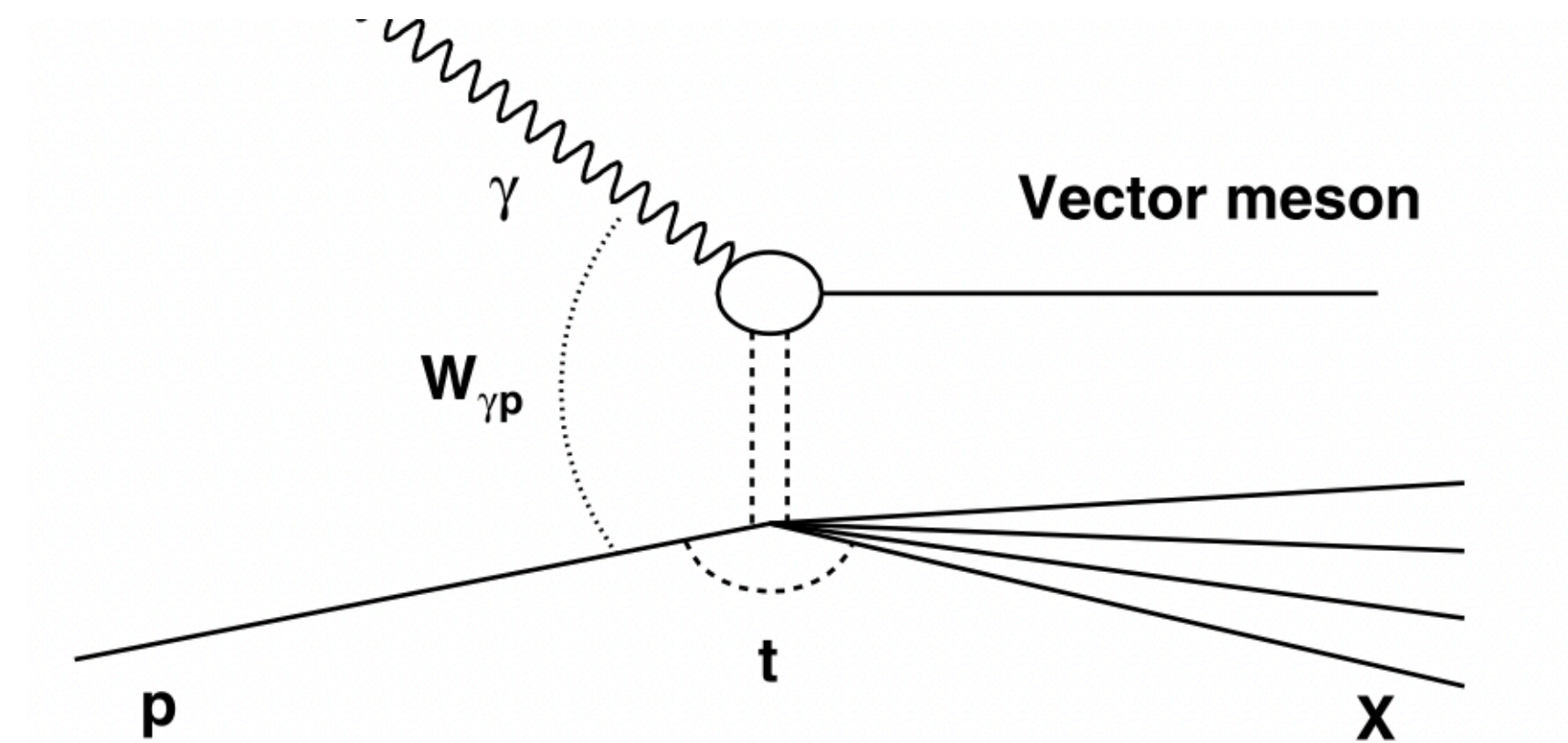


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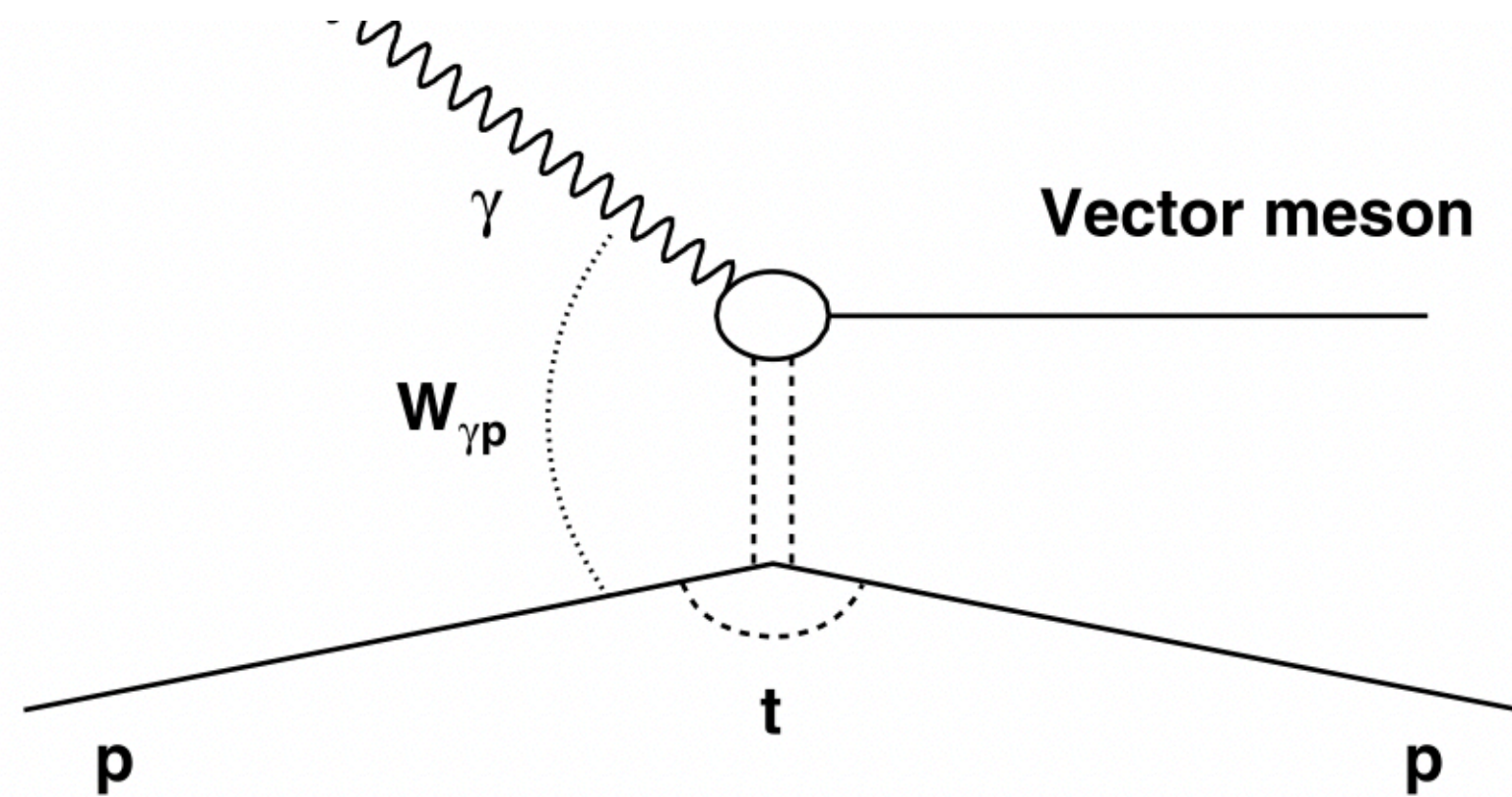


There is a similar process (called dissociation or incoherent), where the proton dissociates in a final state with the same quantum numbers as the proton

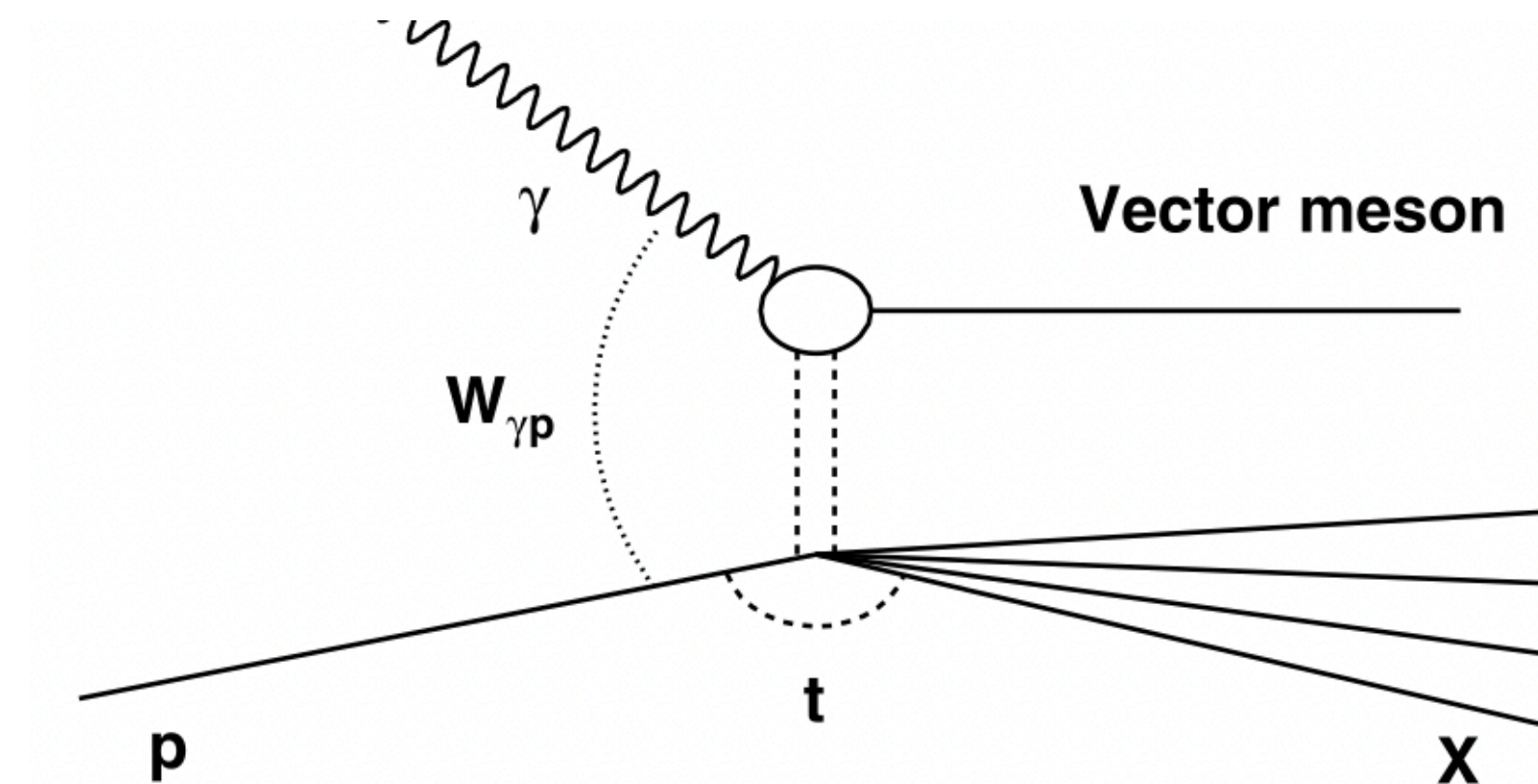
Dissociative vector meson production

Average over target configurations

$$\frac{d\sigma^{\gamma^* p \rightarrow J/\psi p}}{dt} = \frac{1}{16\pi} |\langle A(x_{\mathbb{P}}, Q^2, \Delta) \rangle|^2.$$



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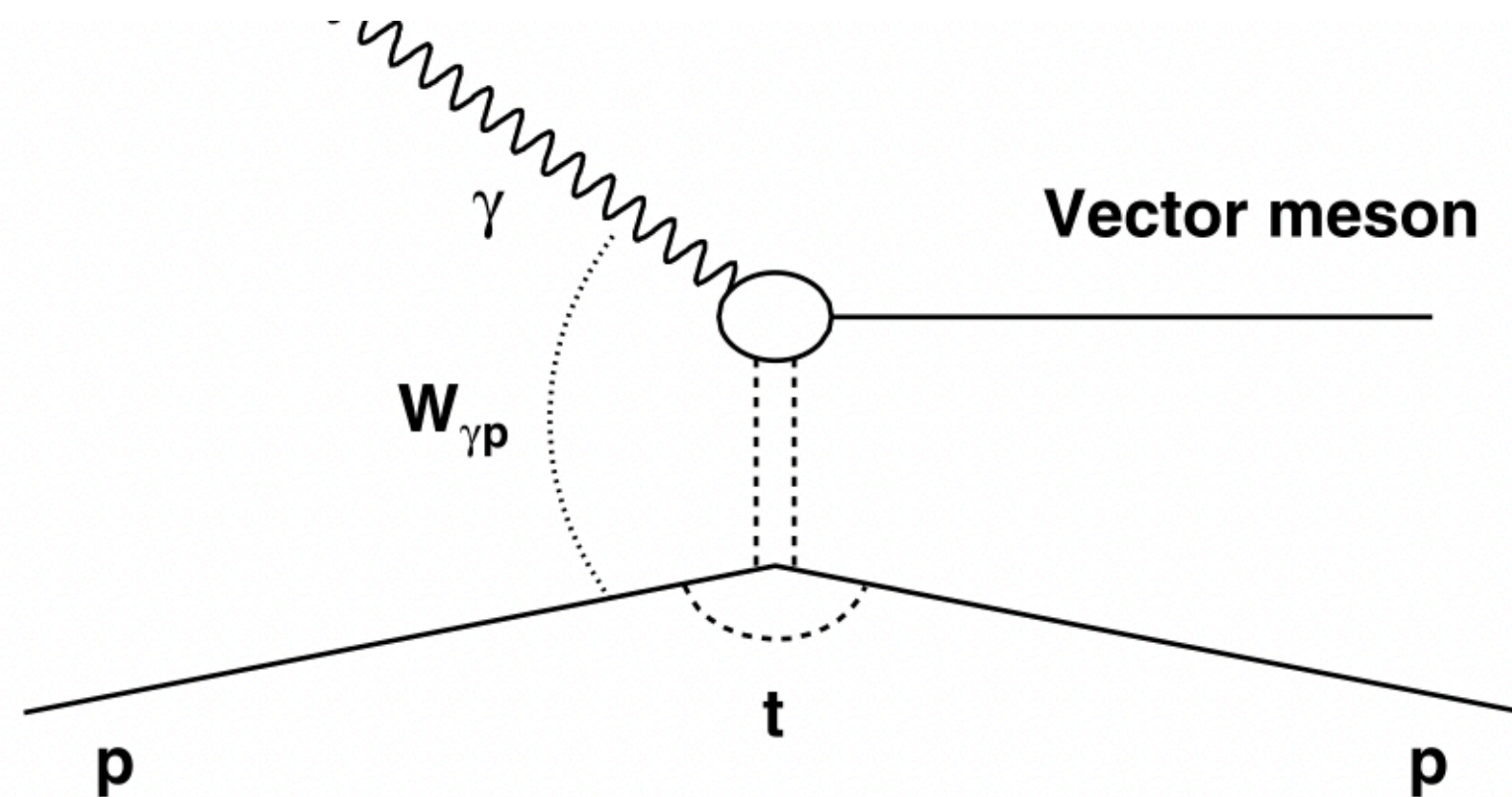
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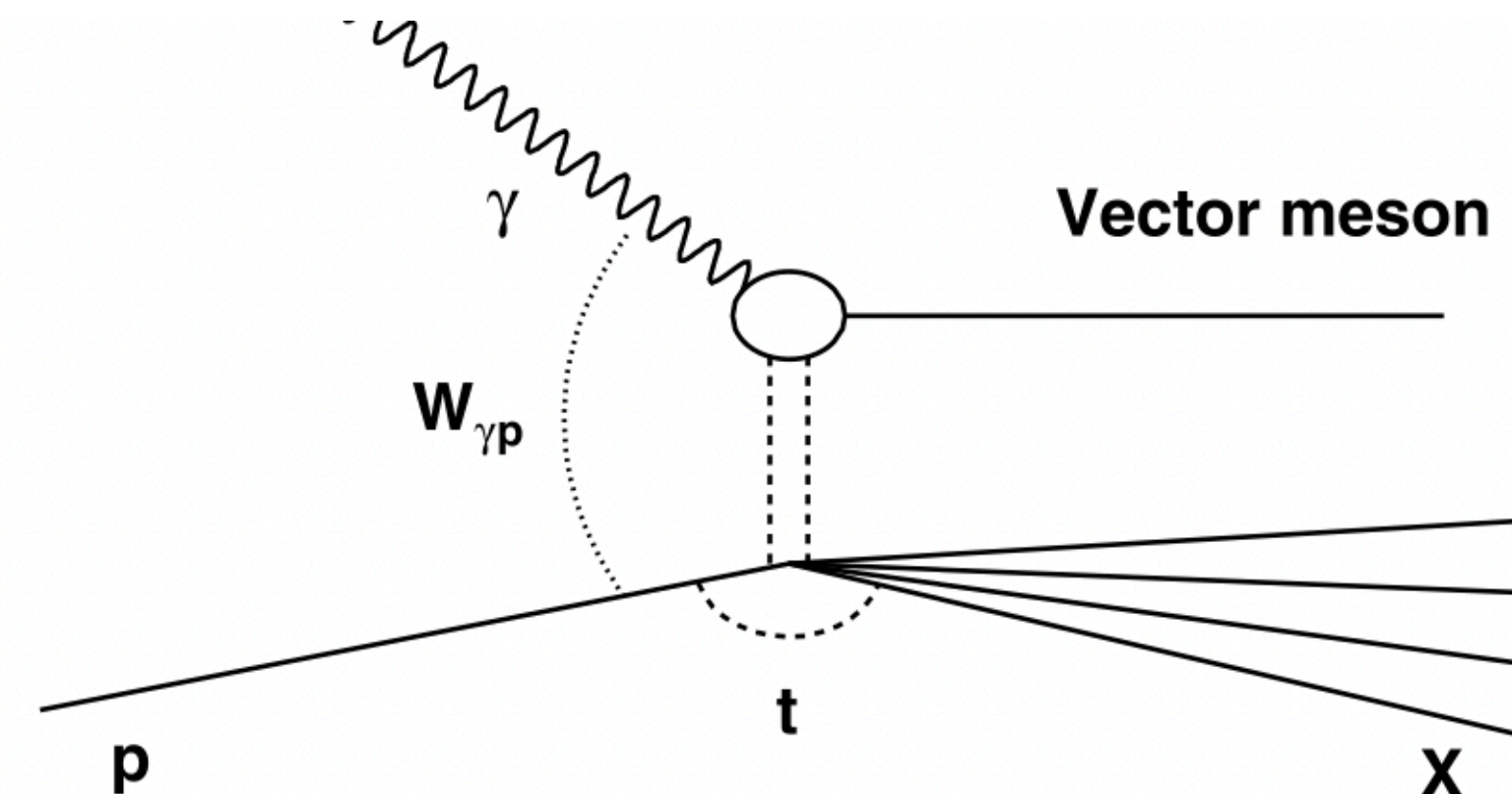
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Variance over target configurations

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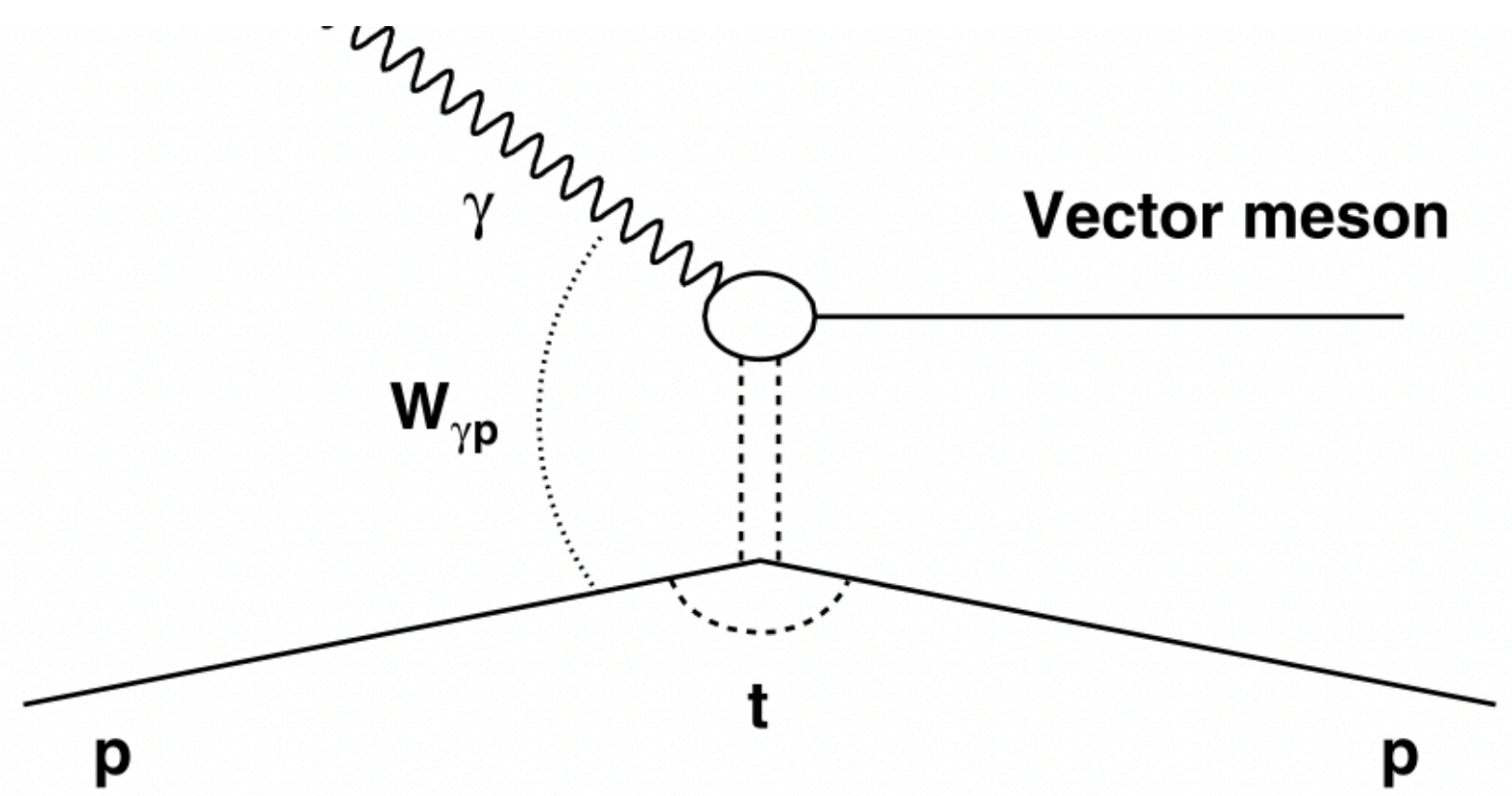
Klein, <https://inspirehep.net/literature/2620130>

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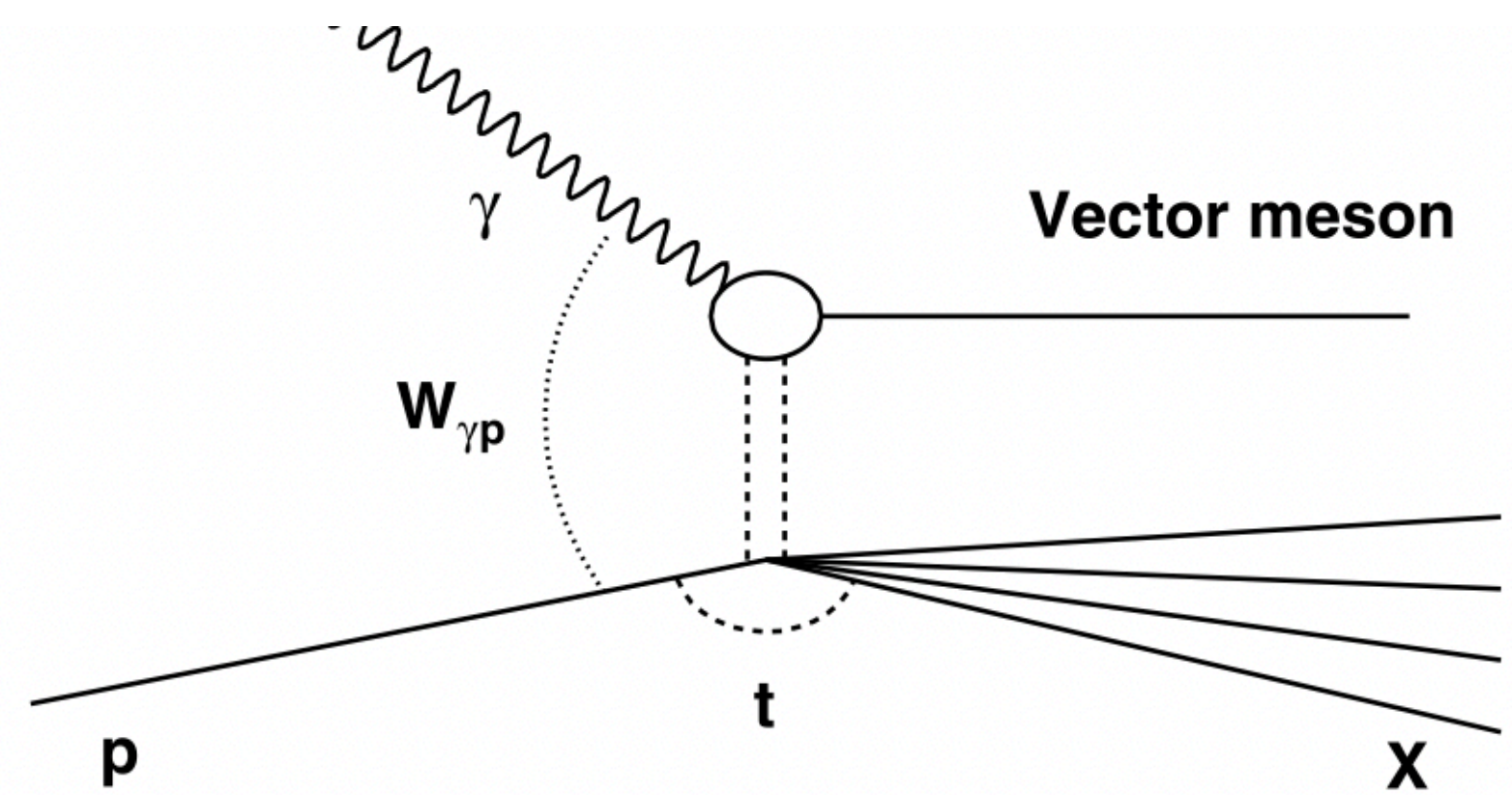
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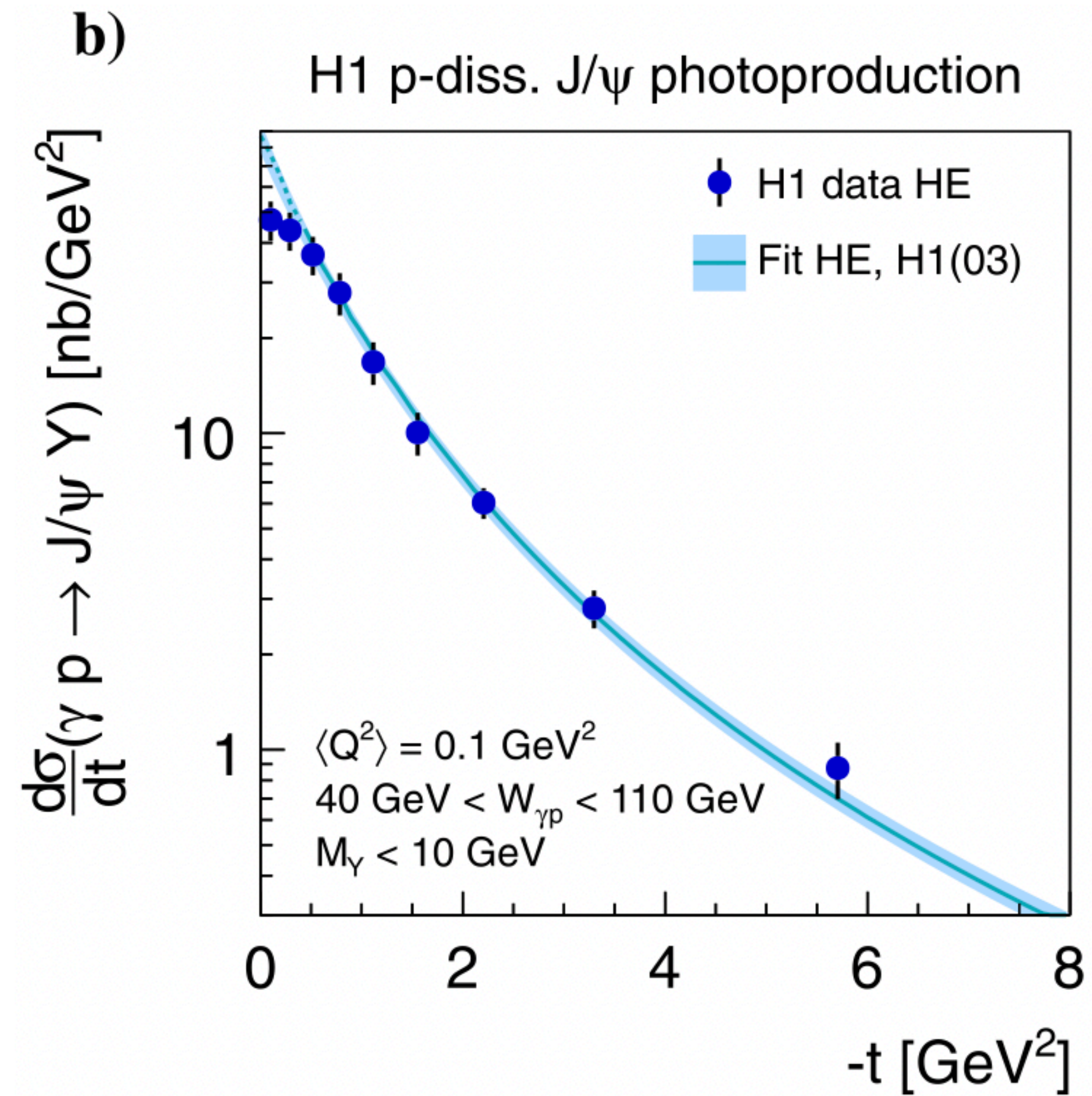


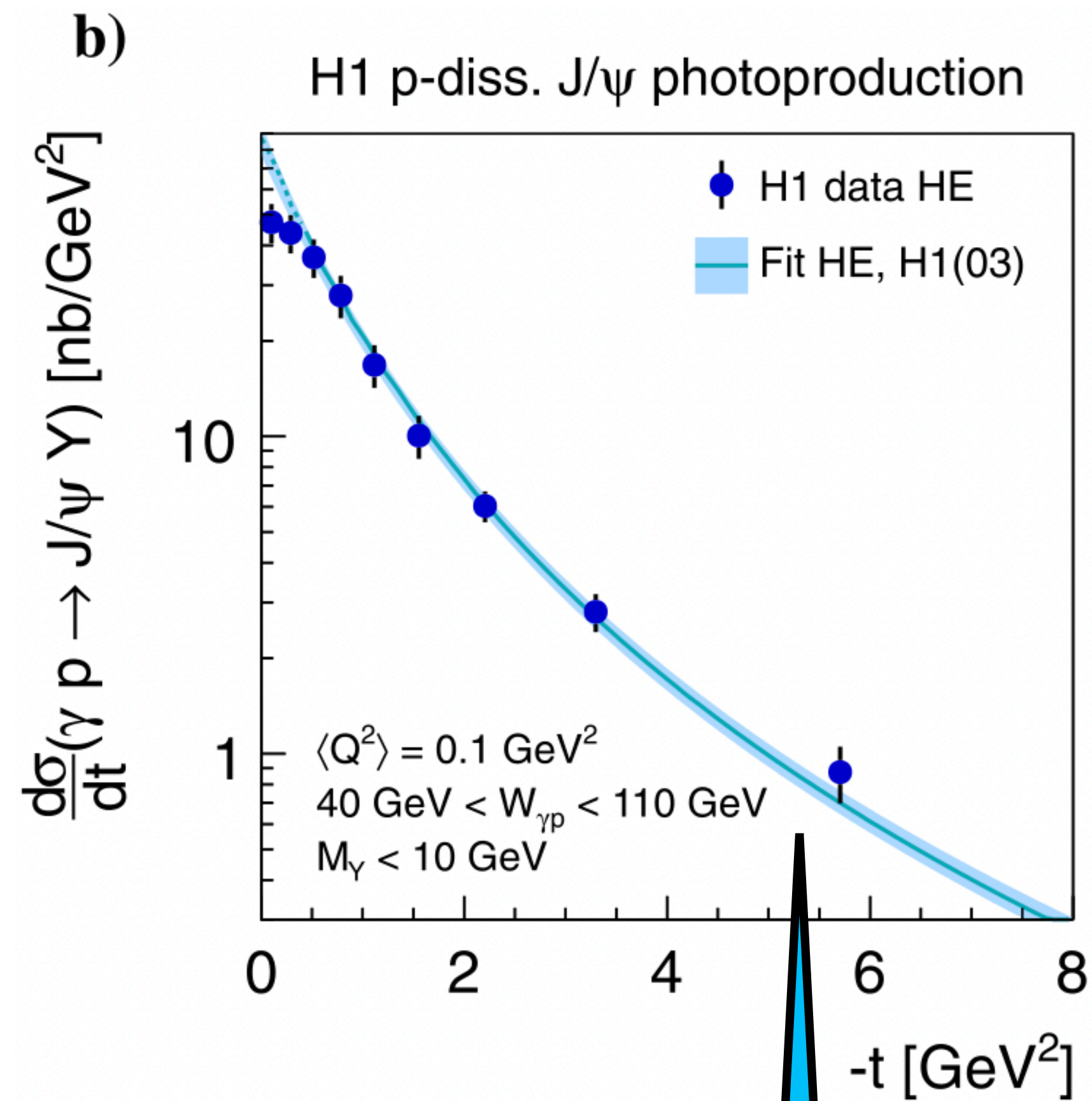
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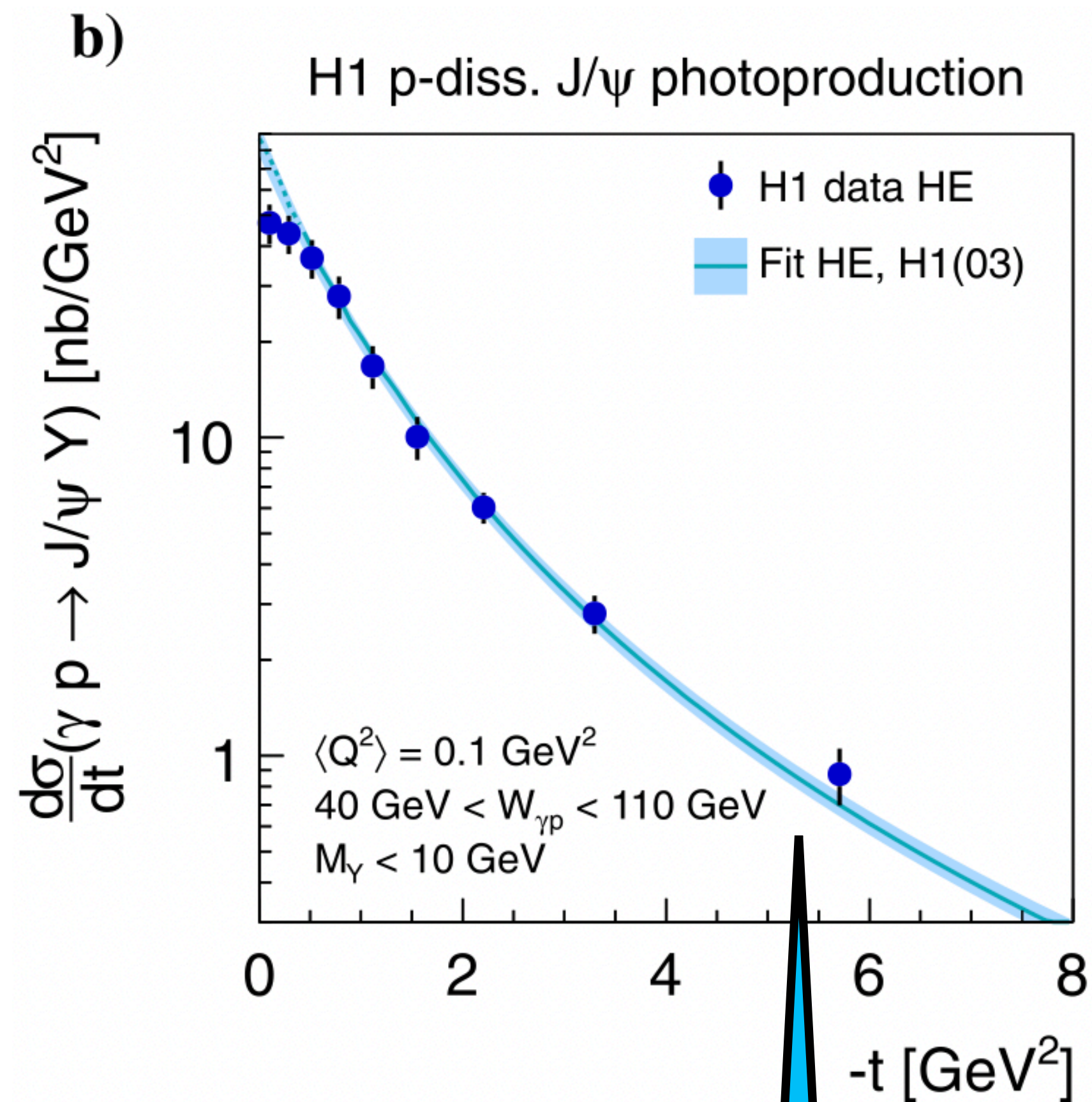




Fit:

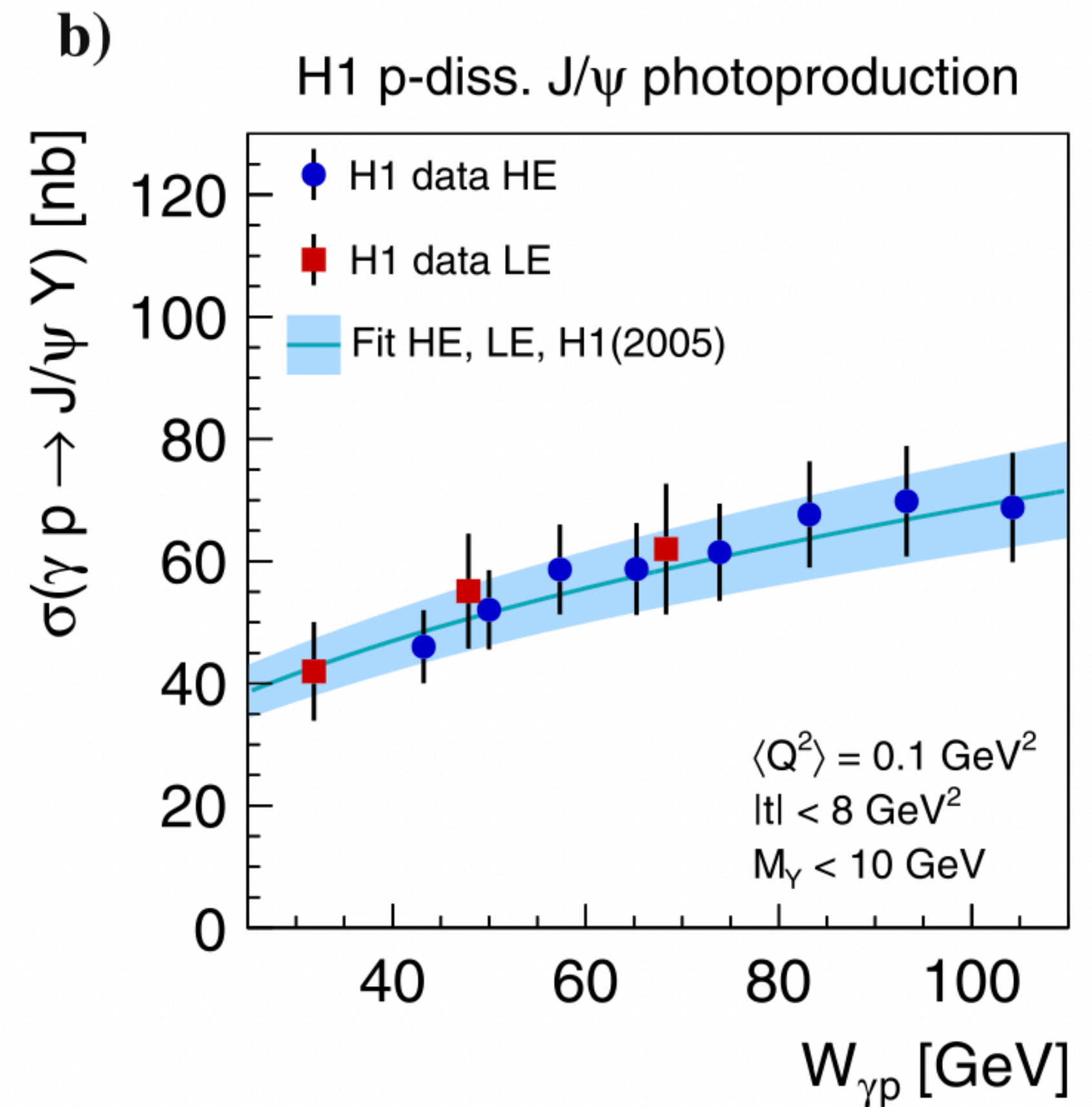
$$d\sigma/dt = N_{pd} (1 + (b_{pd}/n)|t|)^{-n}$$

2013: Diffractive dissociative J/ψ photo production

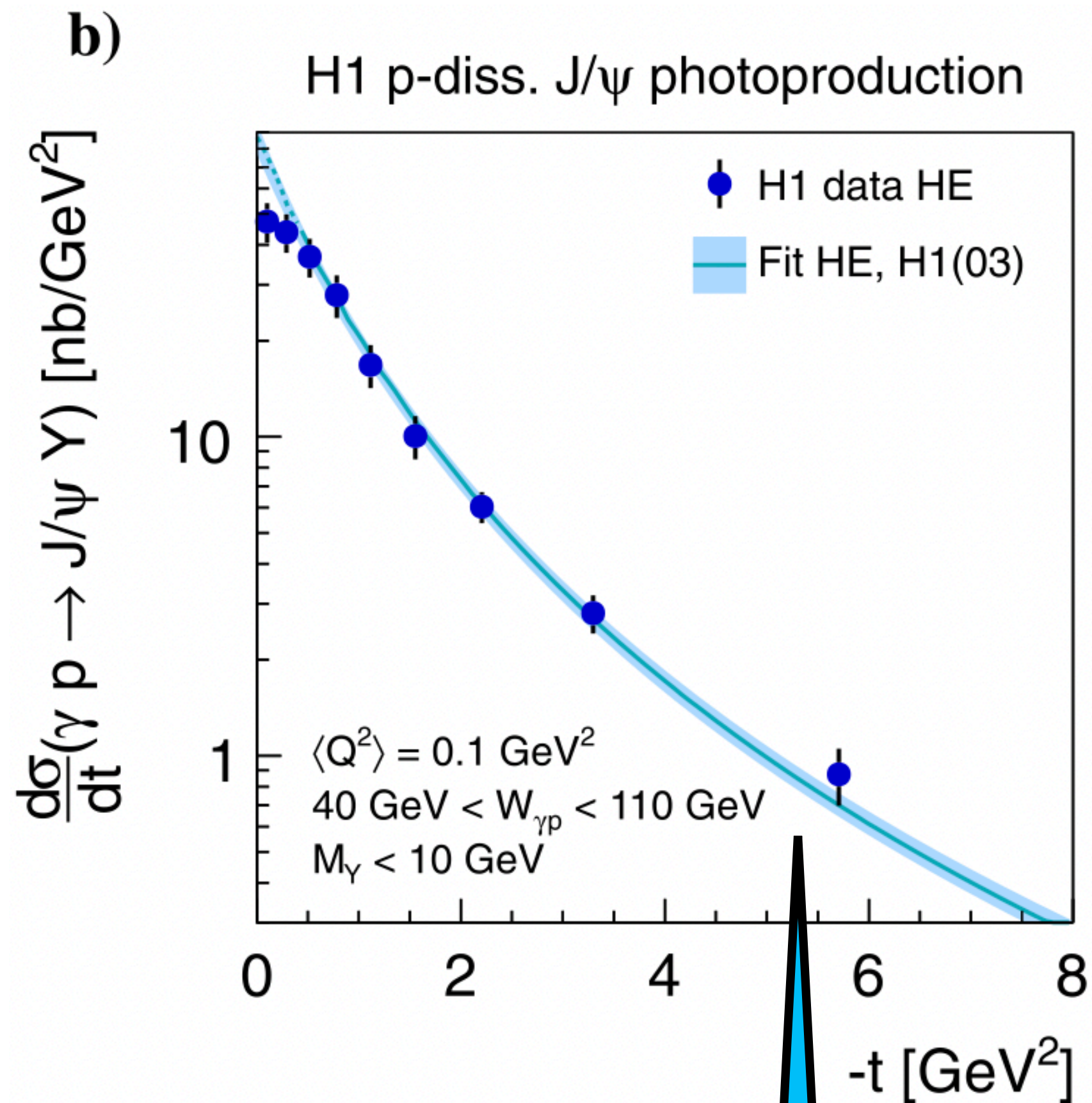


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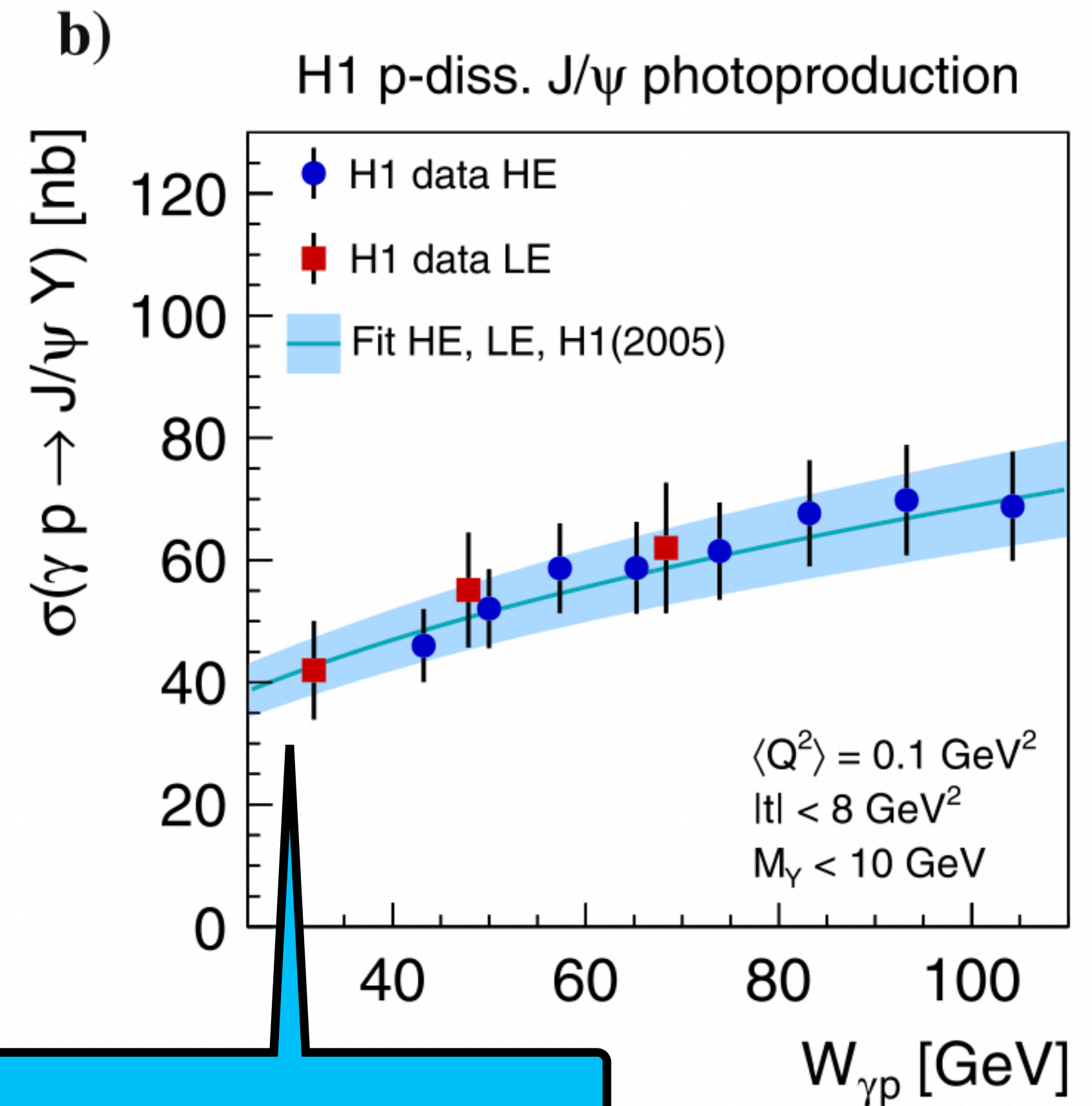


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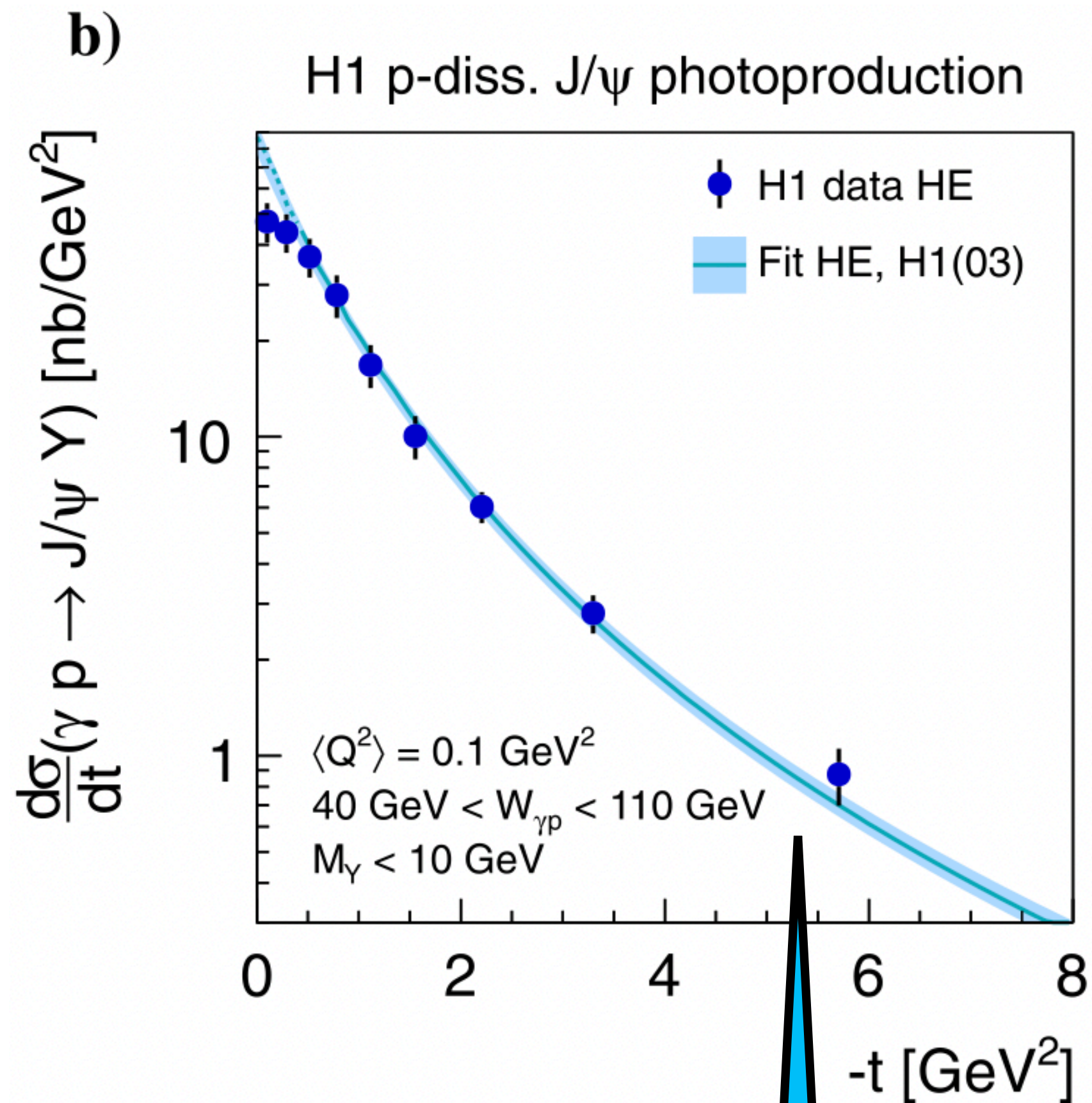
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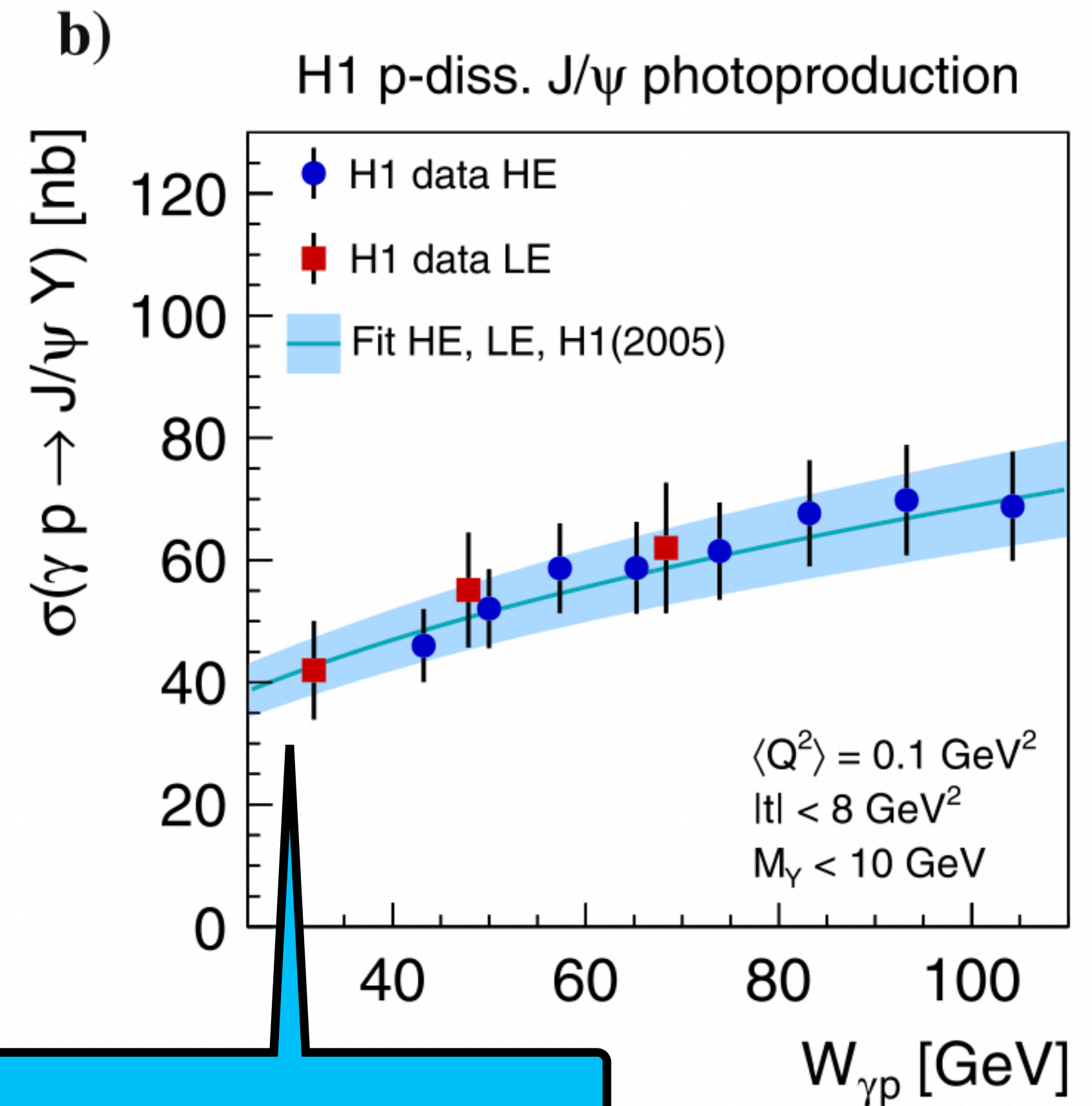
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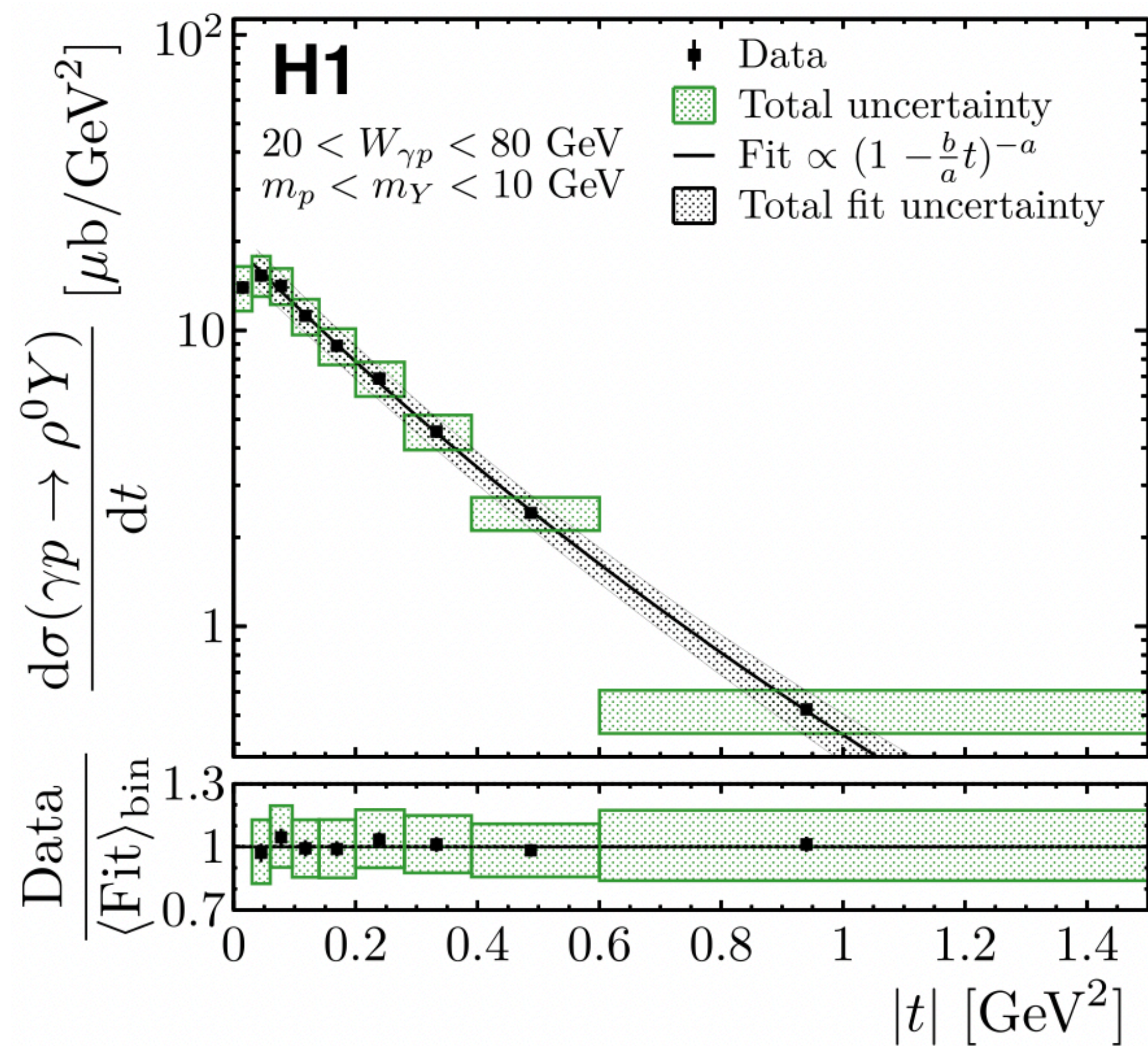


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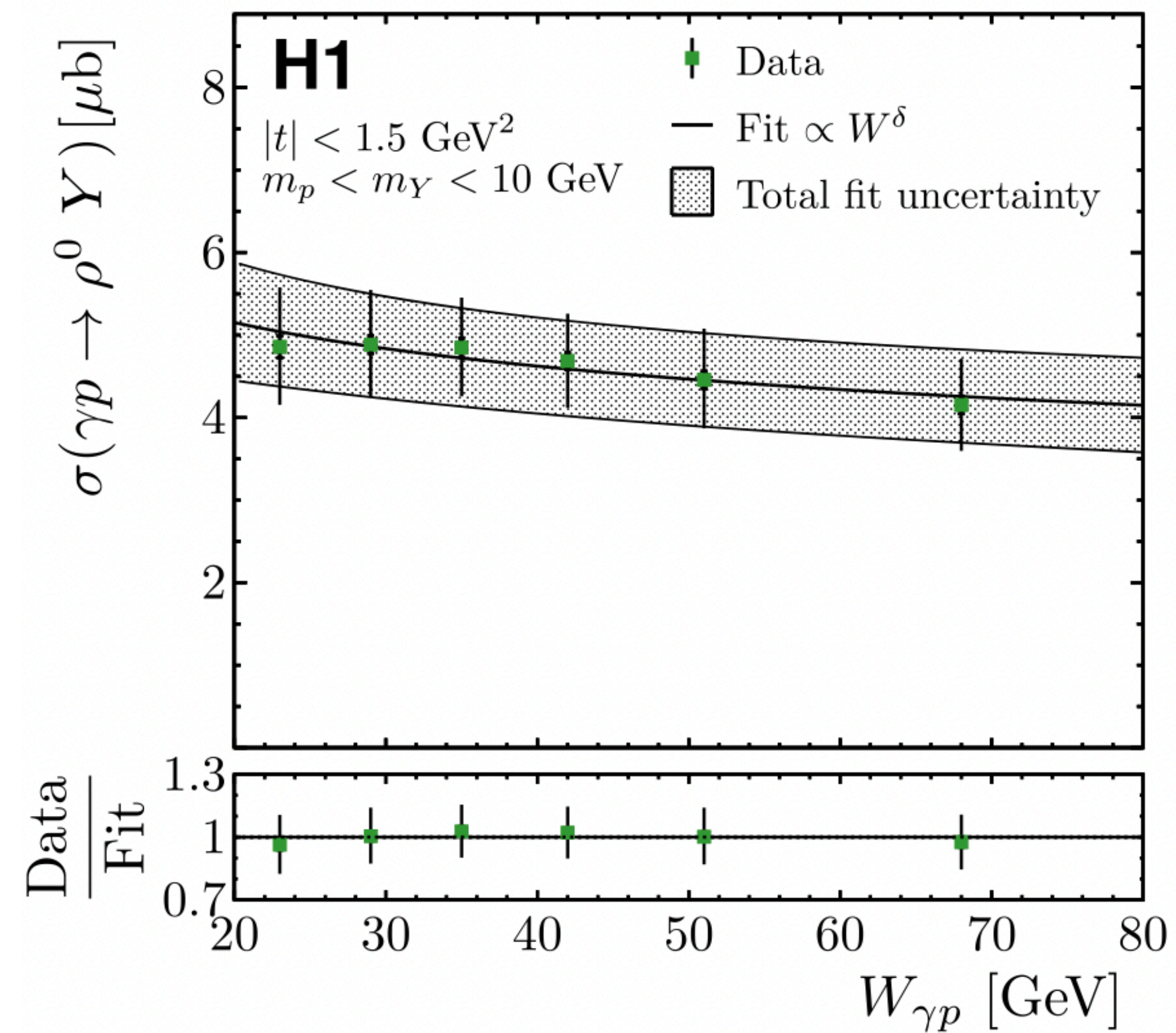
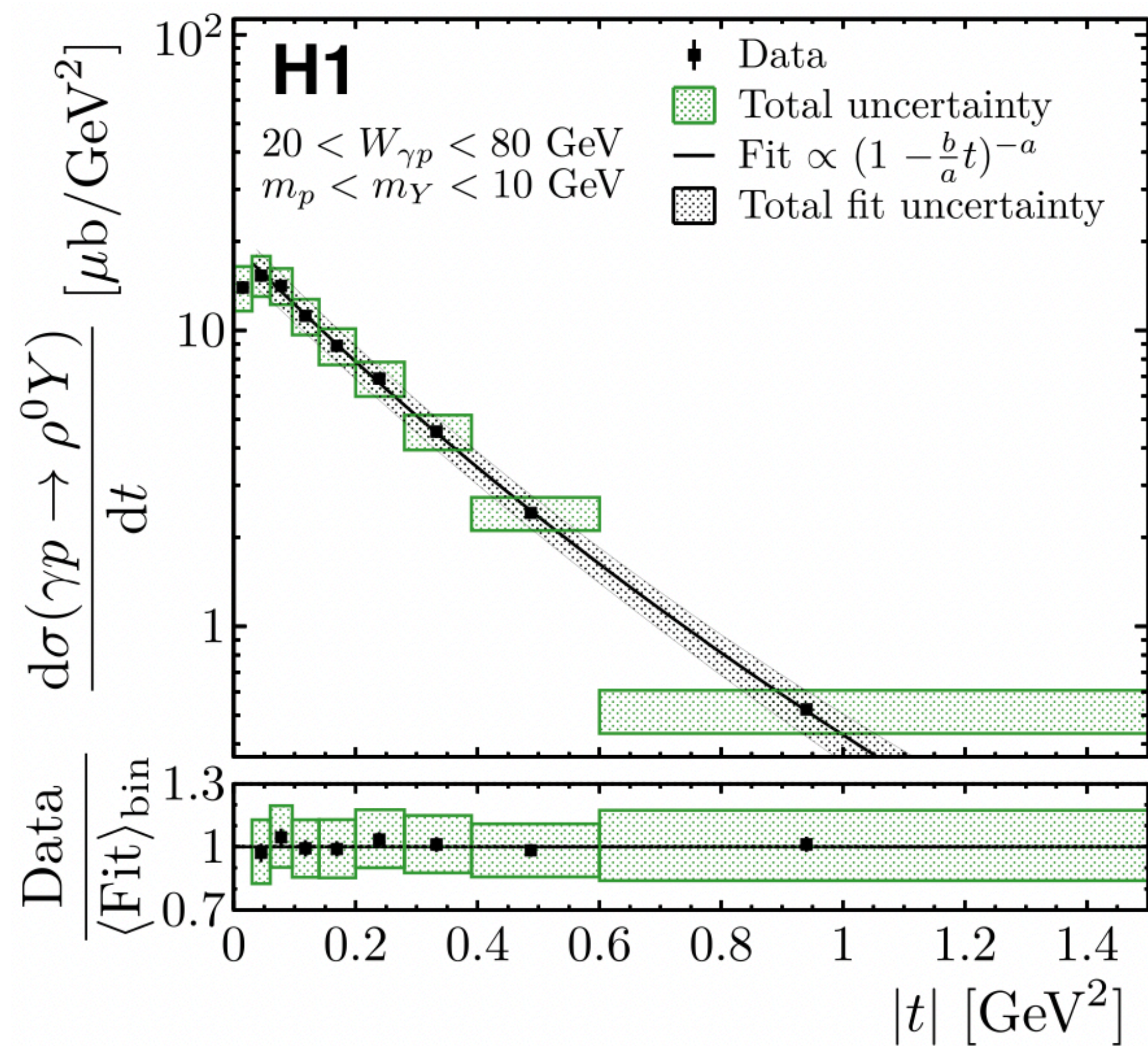
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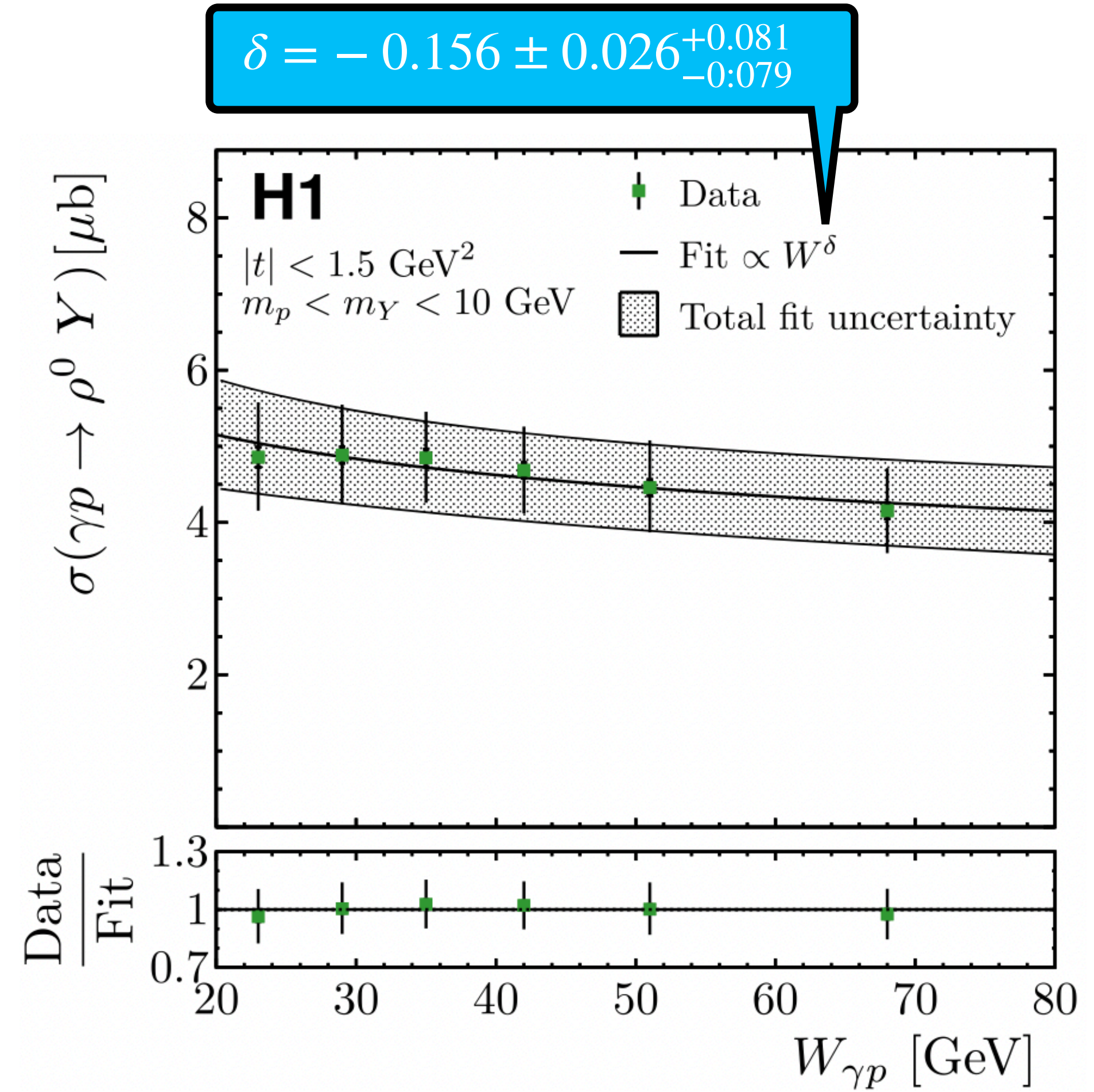
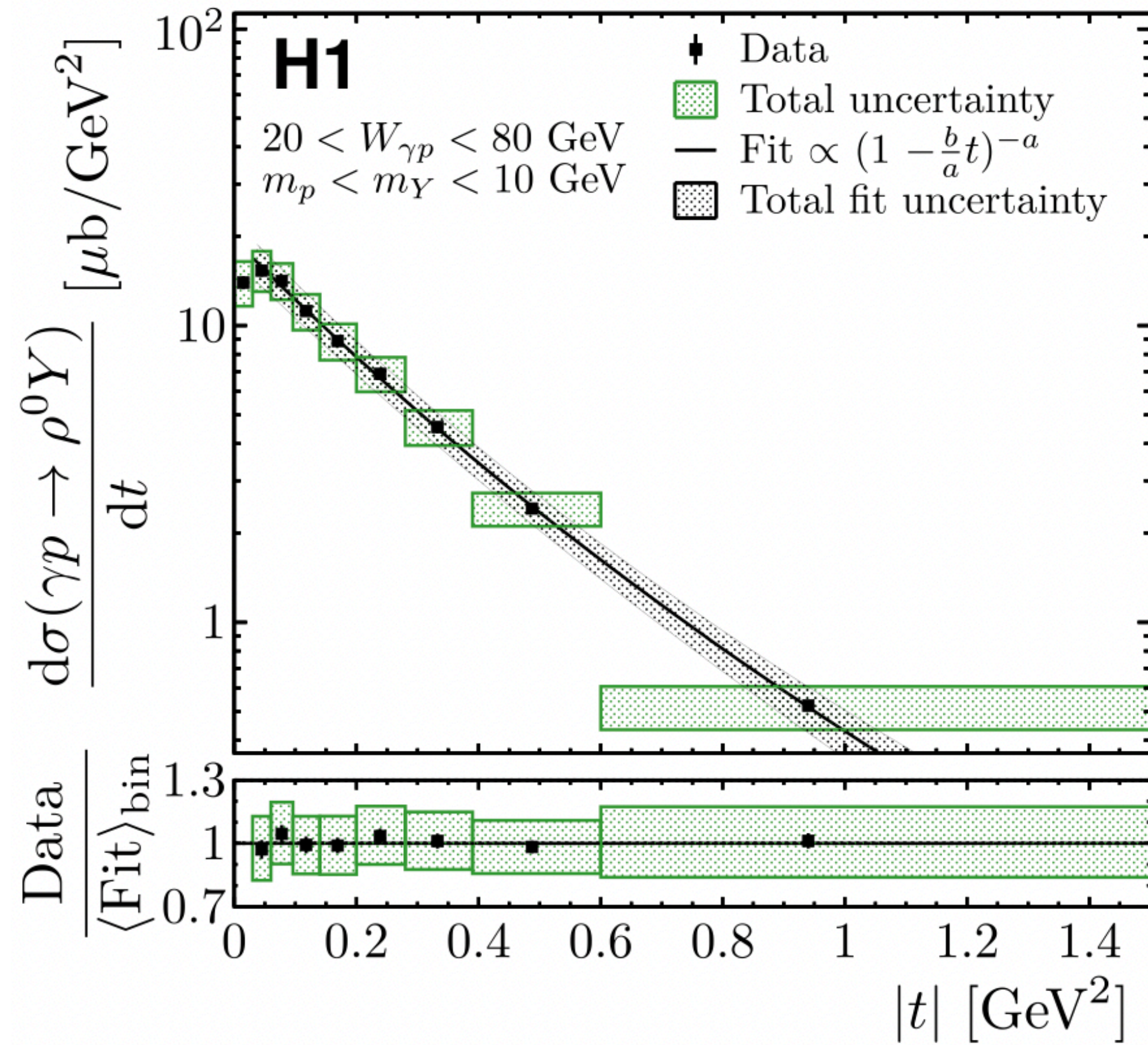
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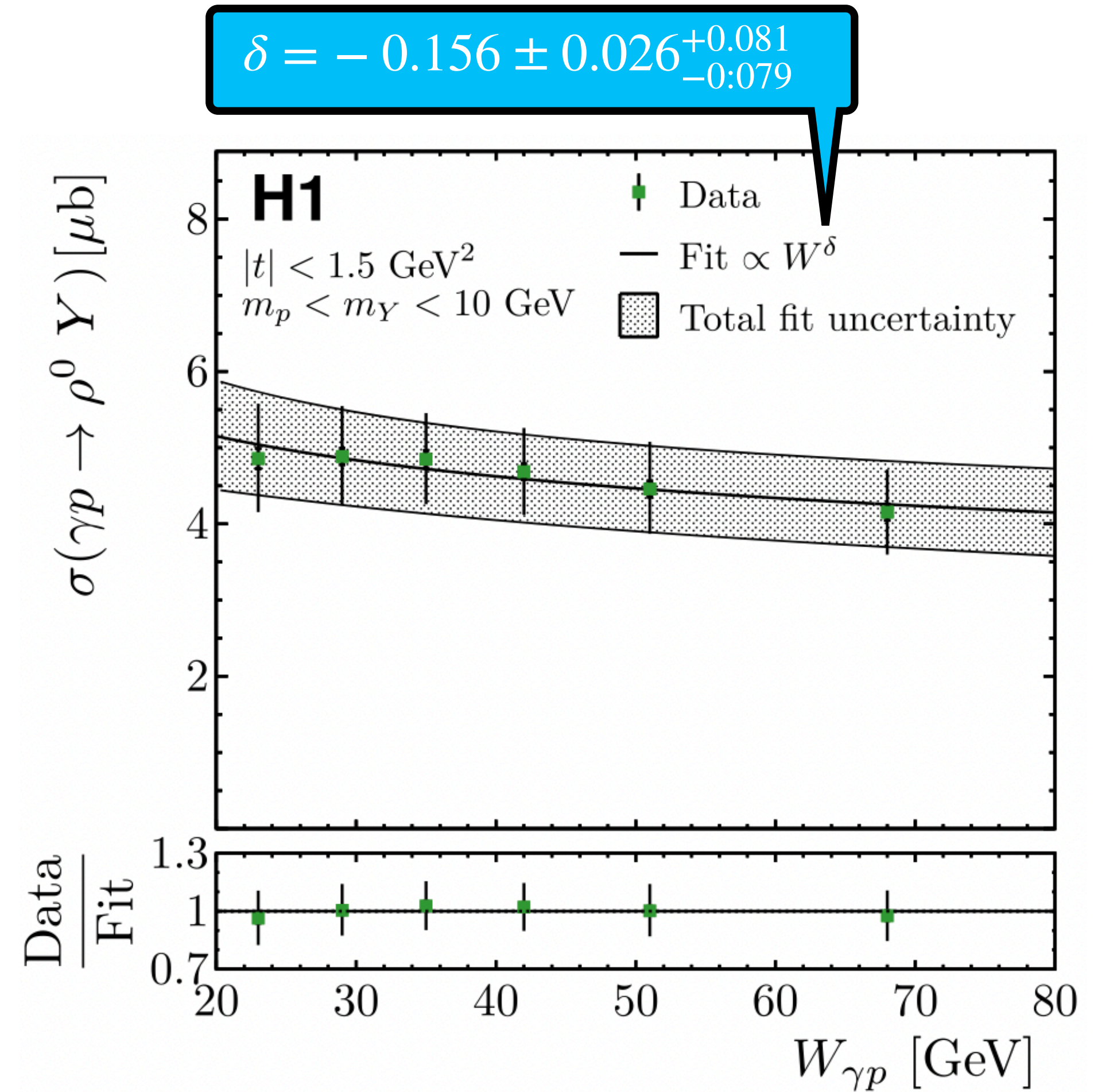
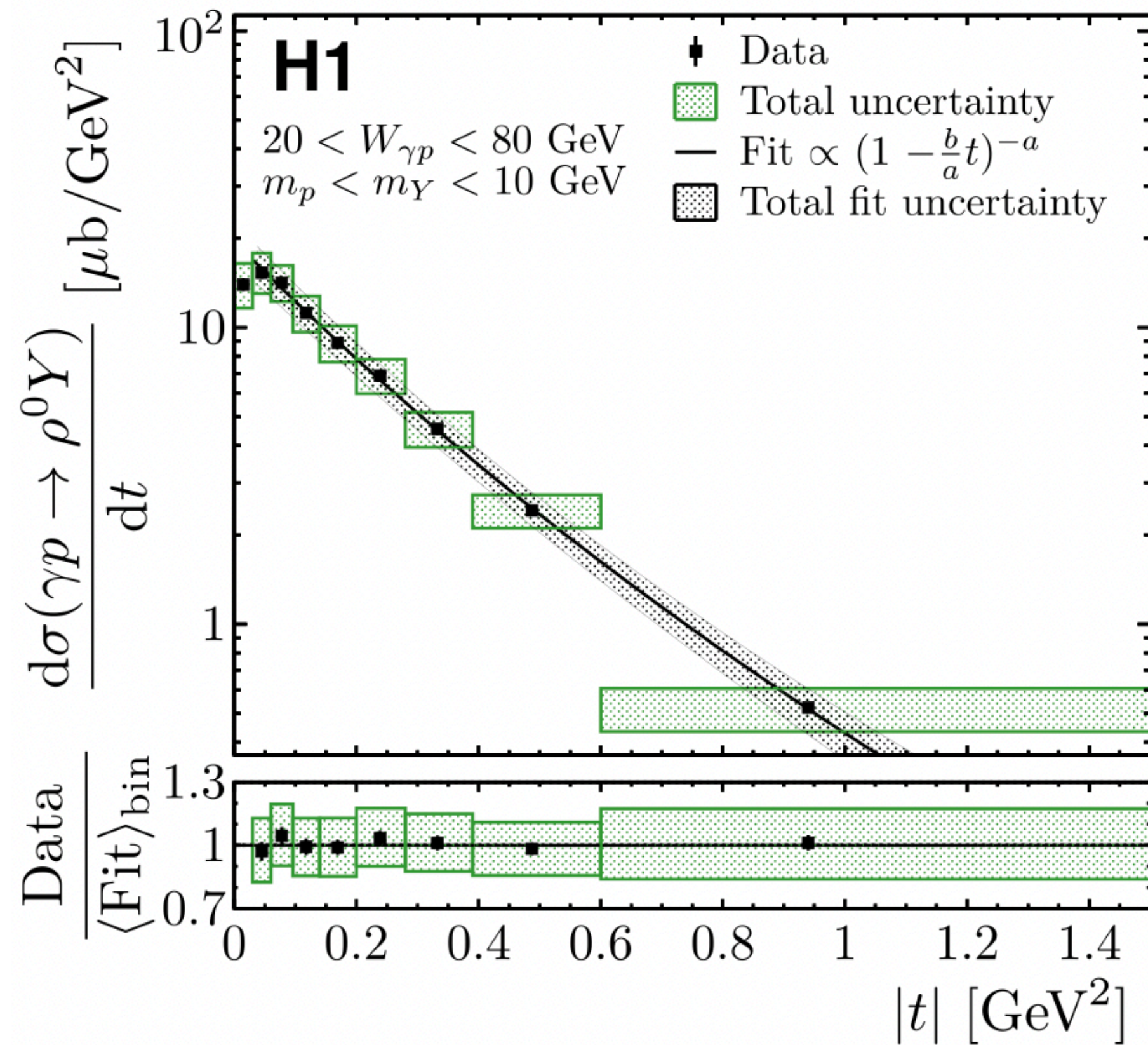
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The cross section decreases!
 How can this be interpreted?

2016: Fluctuations in the proton

In the Good-Walker approach, the dissociative cross section is related to the variance over configurations

$$\frac{d\sigma^{\gamma^* N \rightarrow J/\psi N^*}}{dt} = \frac{1}{16\pi} (\langle |A(x_{\mathbb{P}}, Q^2, \mathbf{\Delta})|^2 \rangle - |\langle A(x_{\mathbb{P}}, Q^2, \mathbf{\Delta}) \rangle|^2)$$

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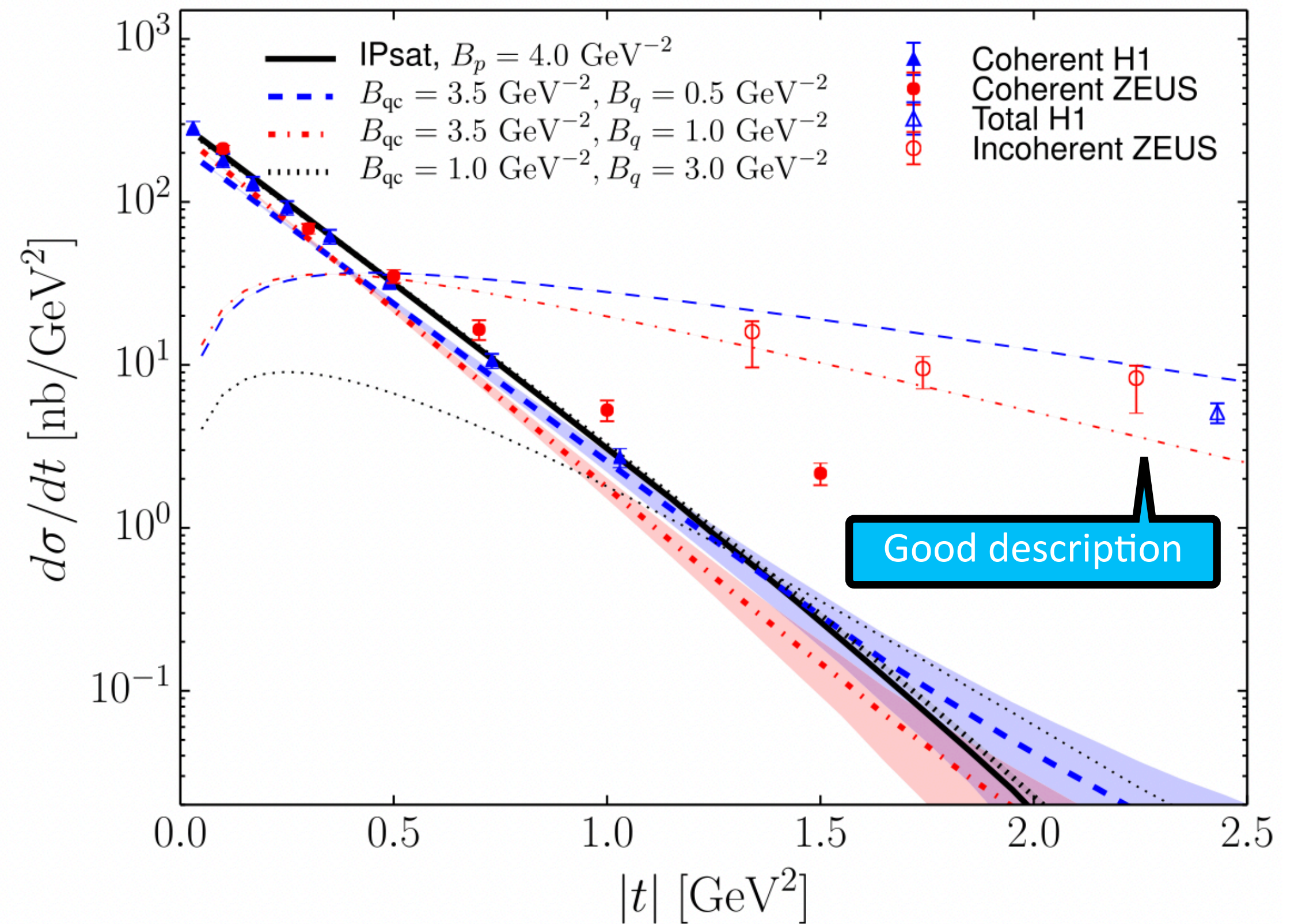
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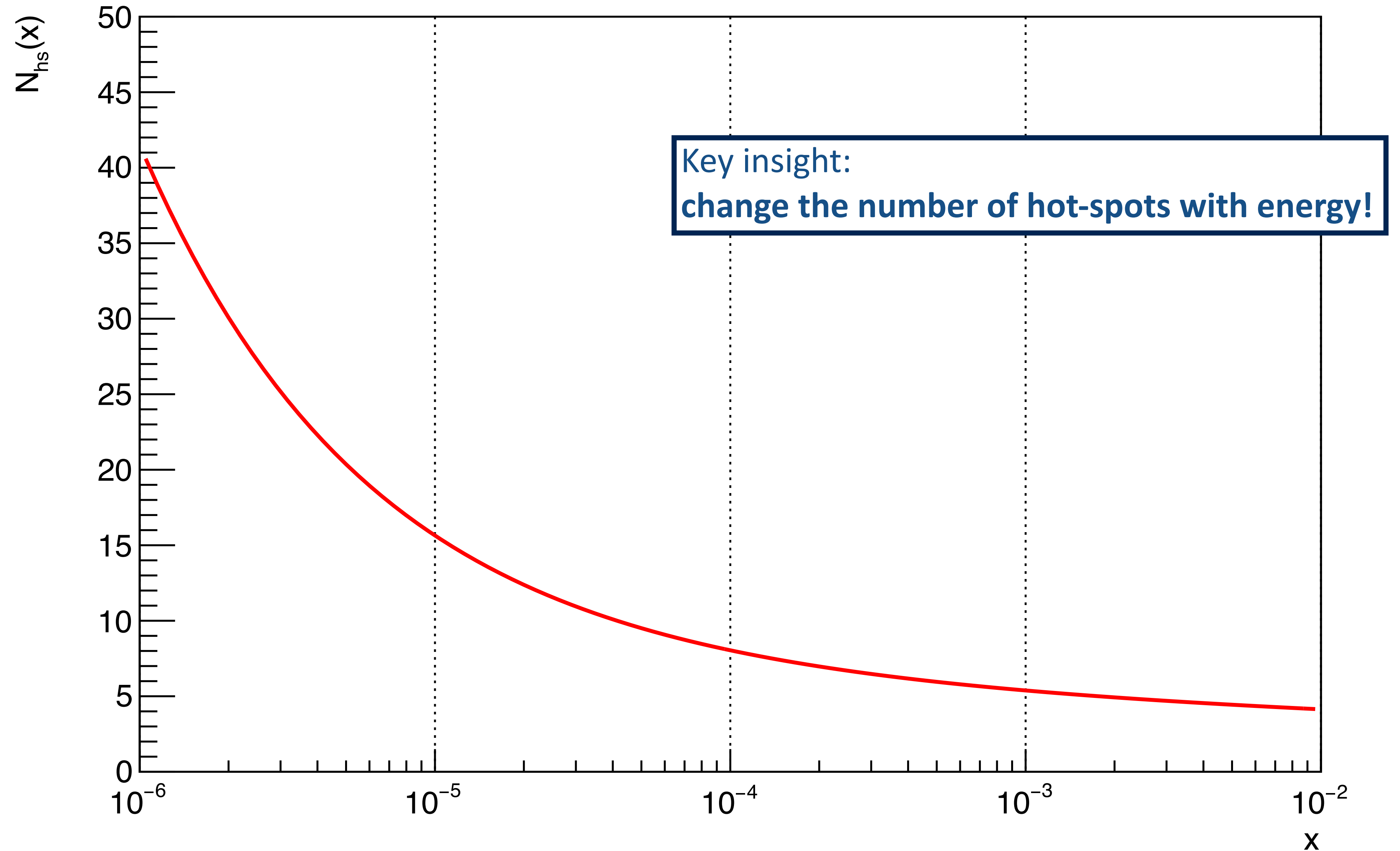
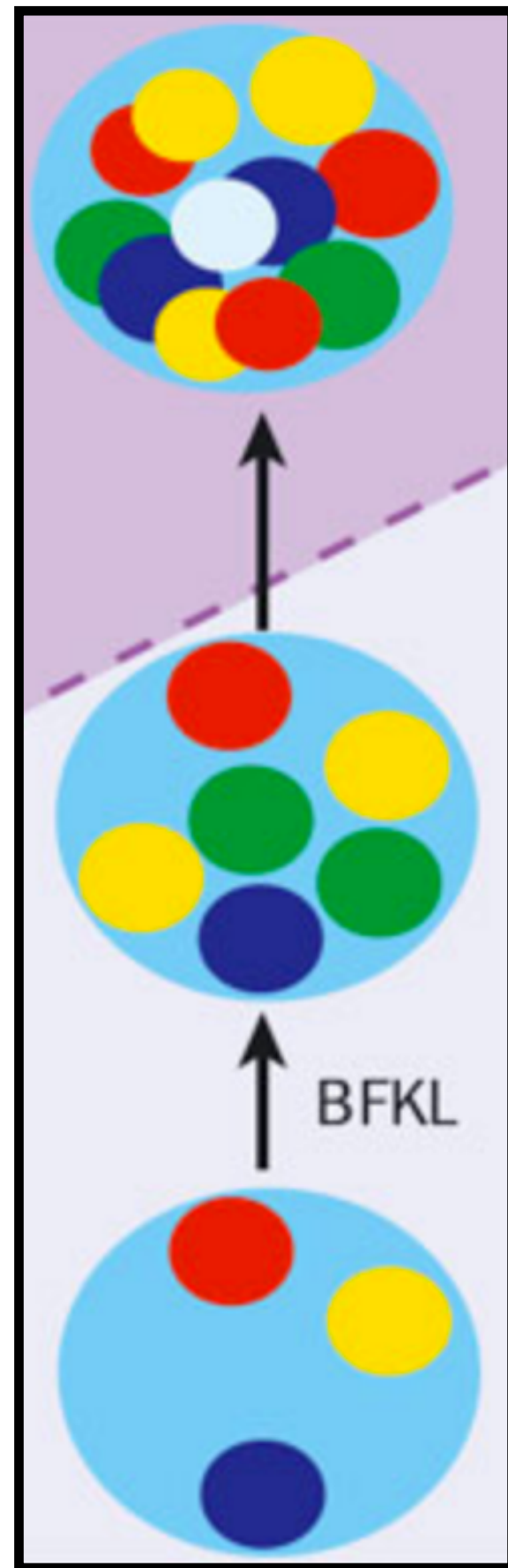
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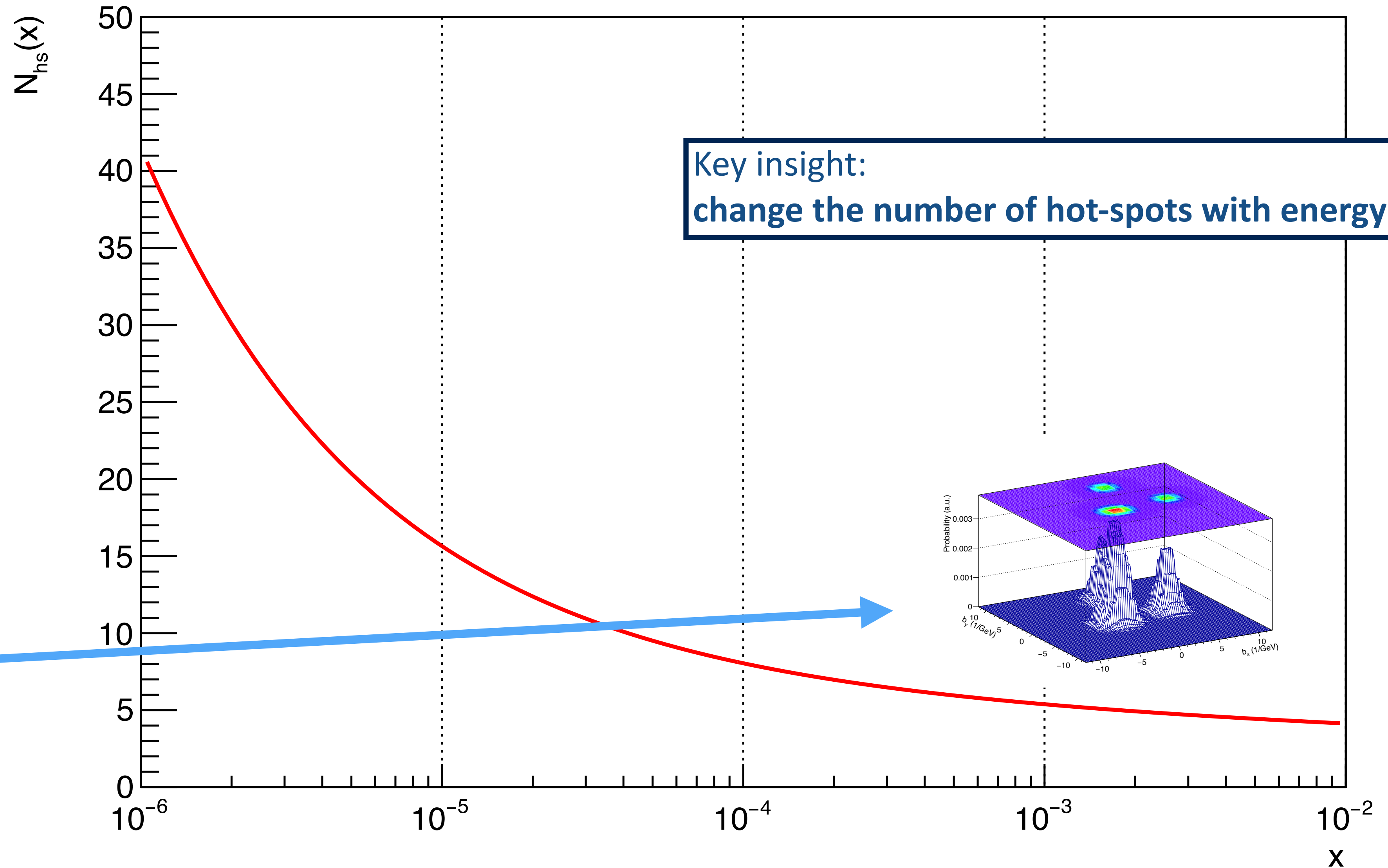
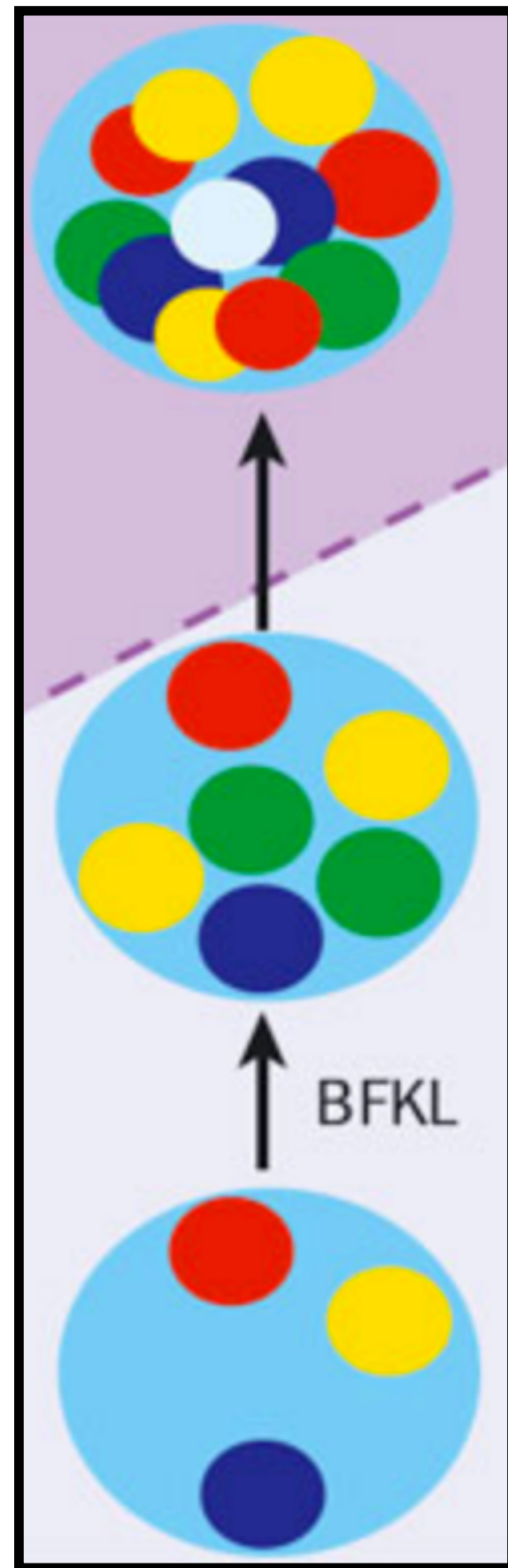
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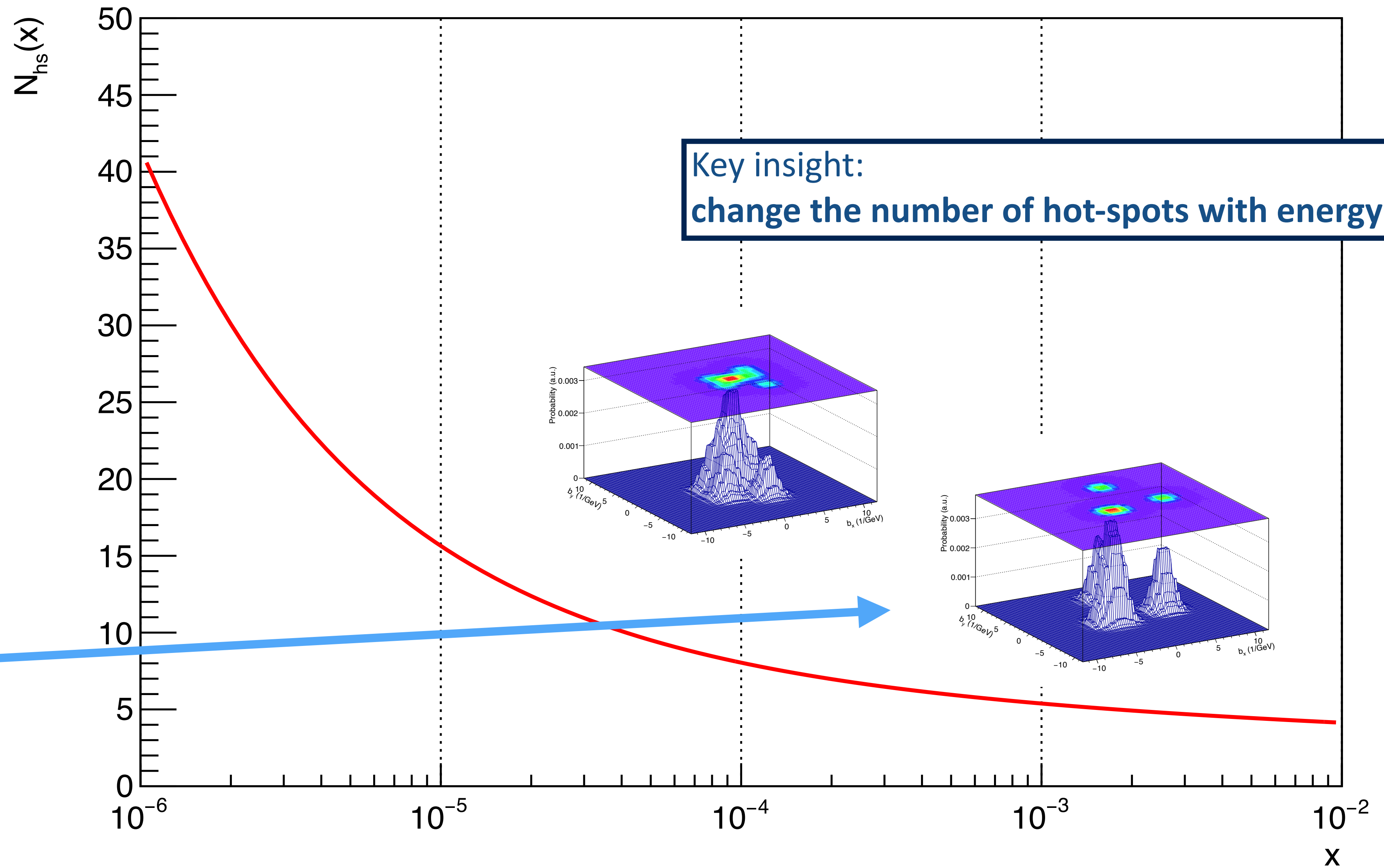
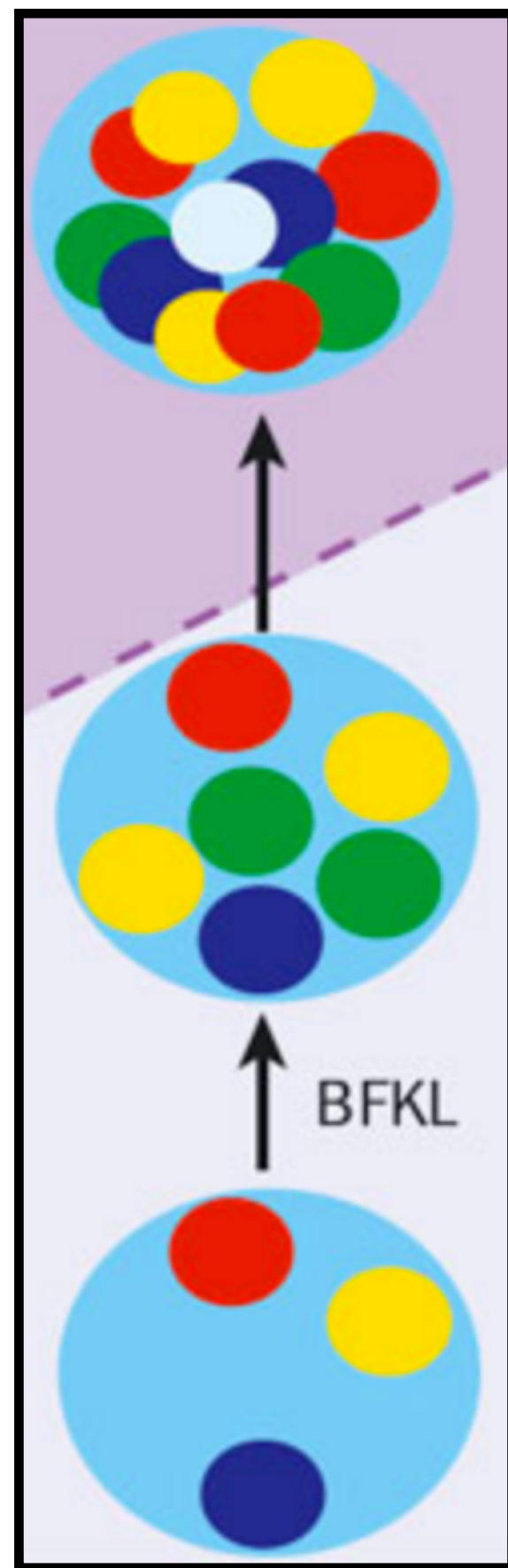
Energy-dependent hot-spot model (1/2)



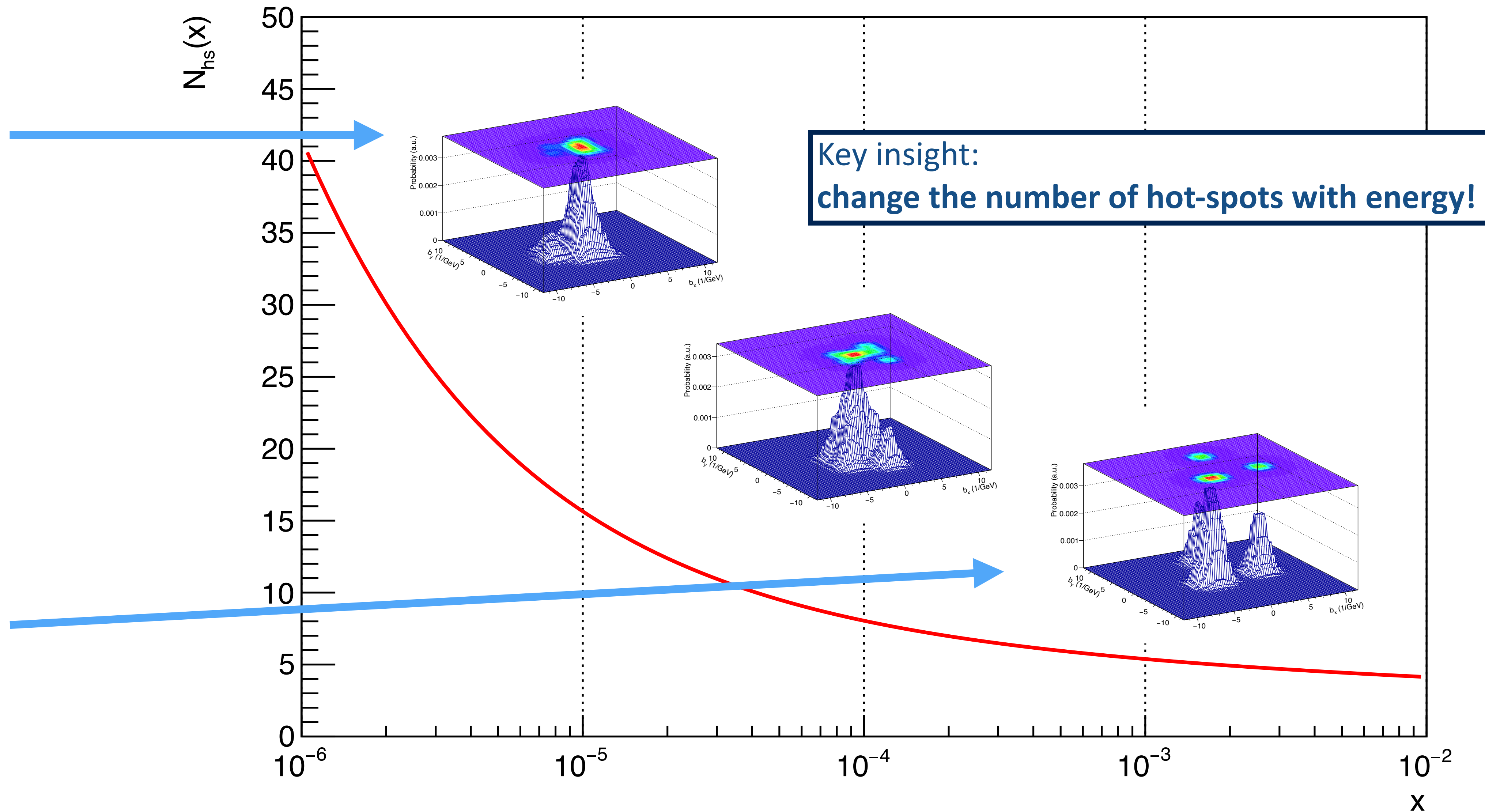
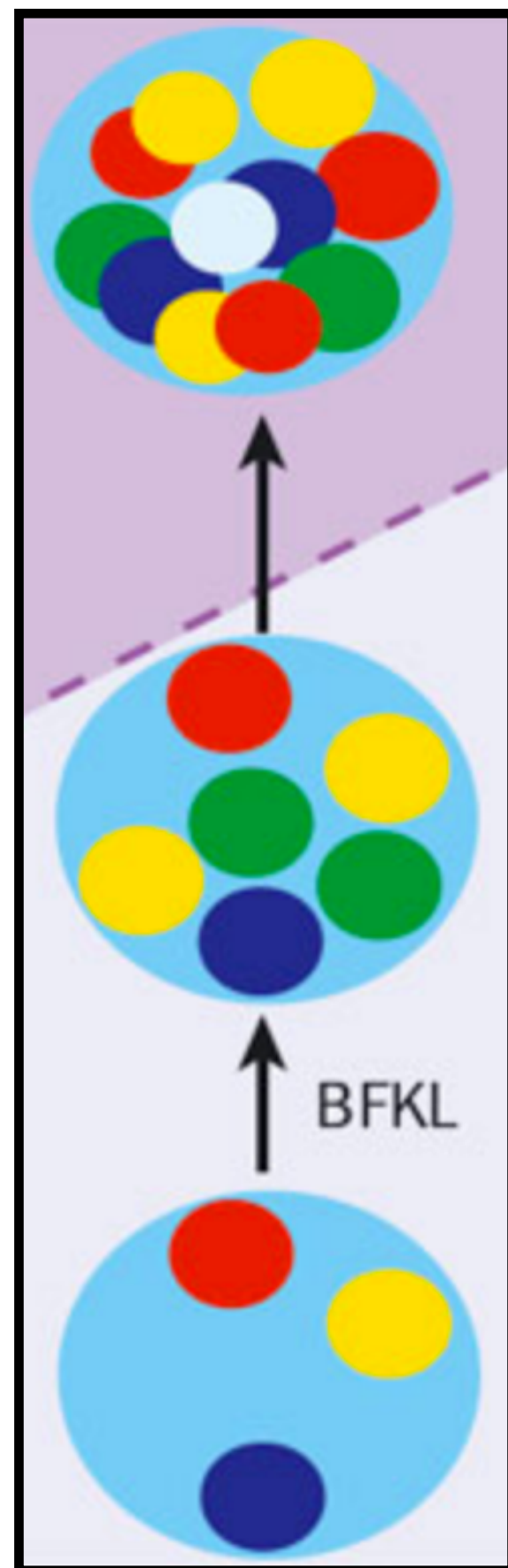
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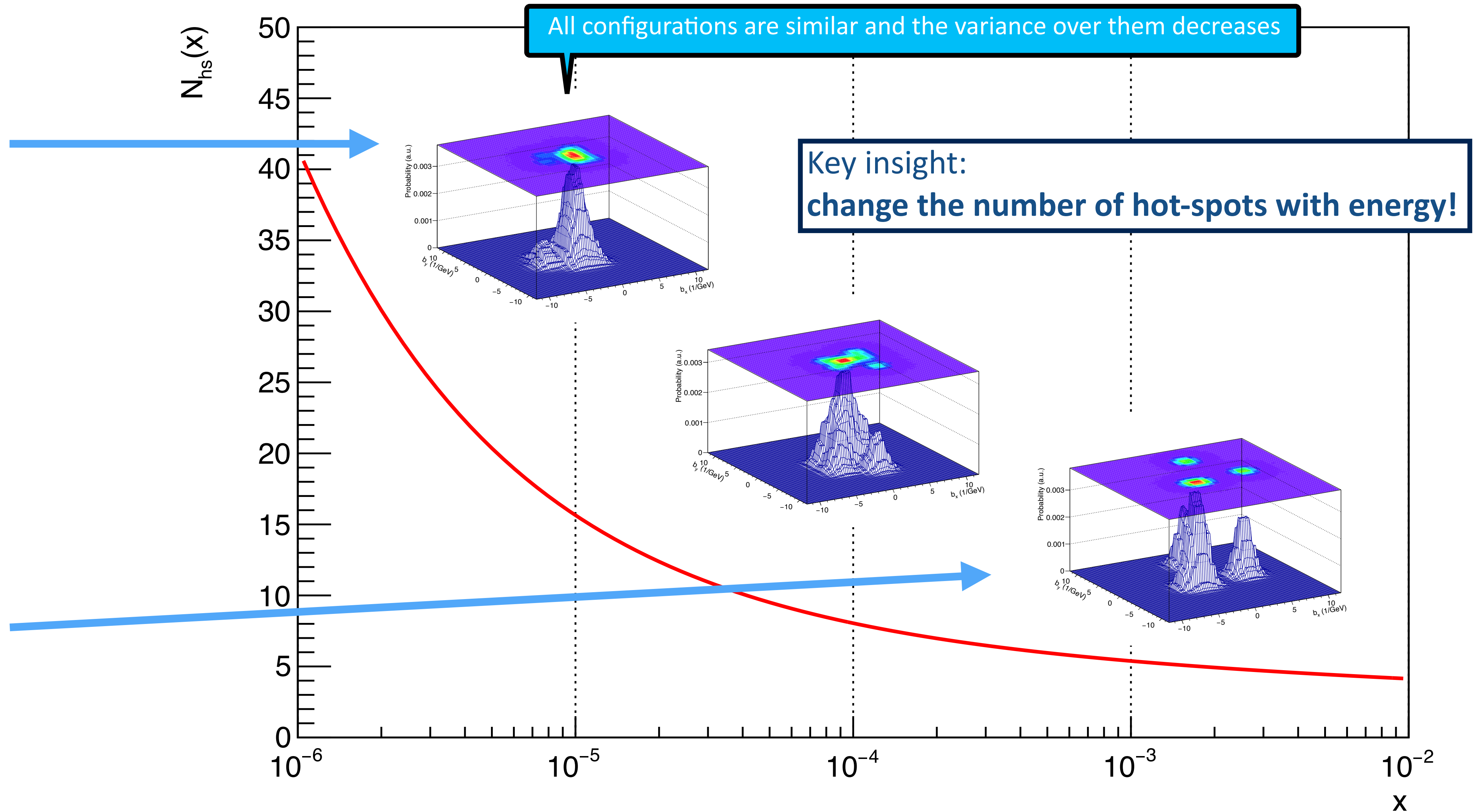
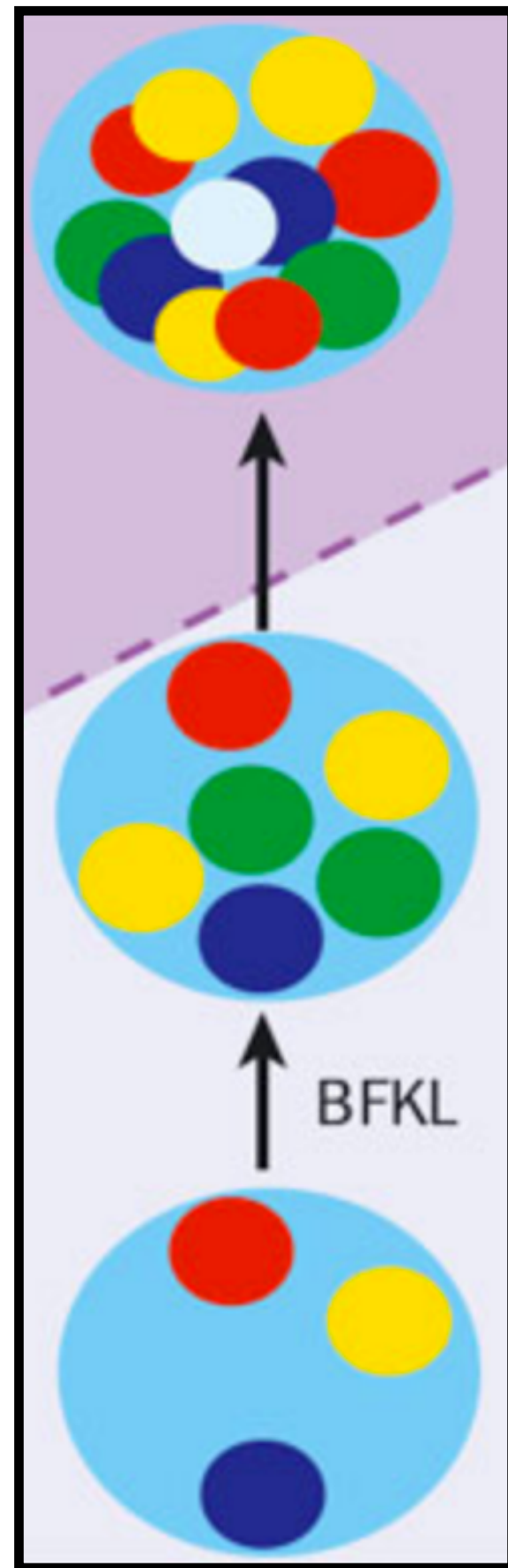
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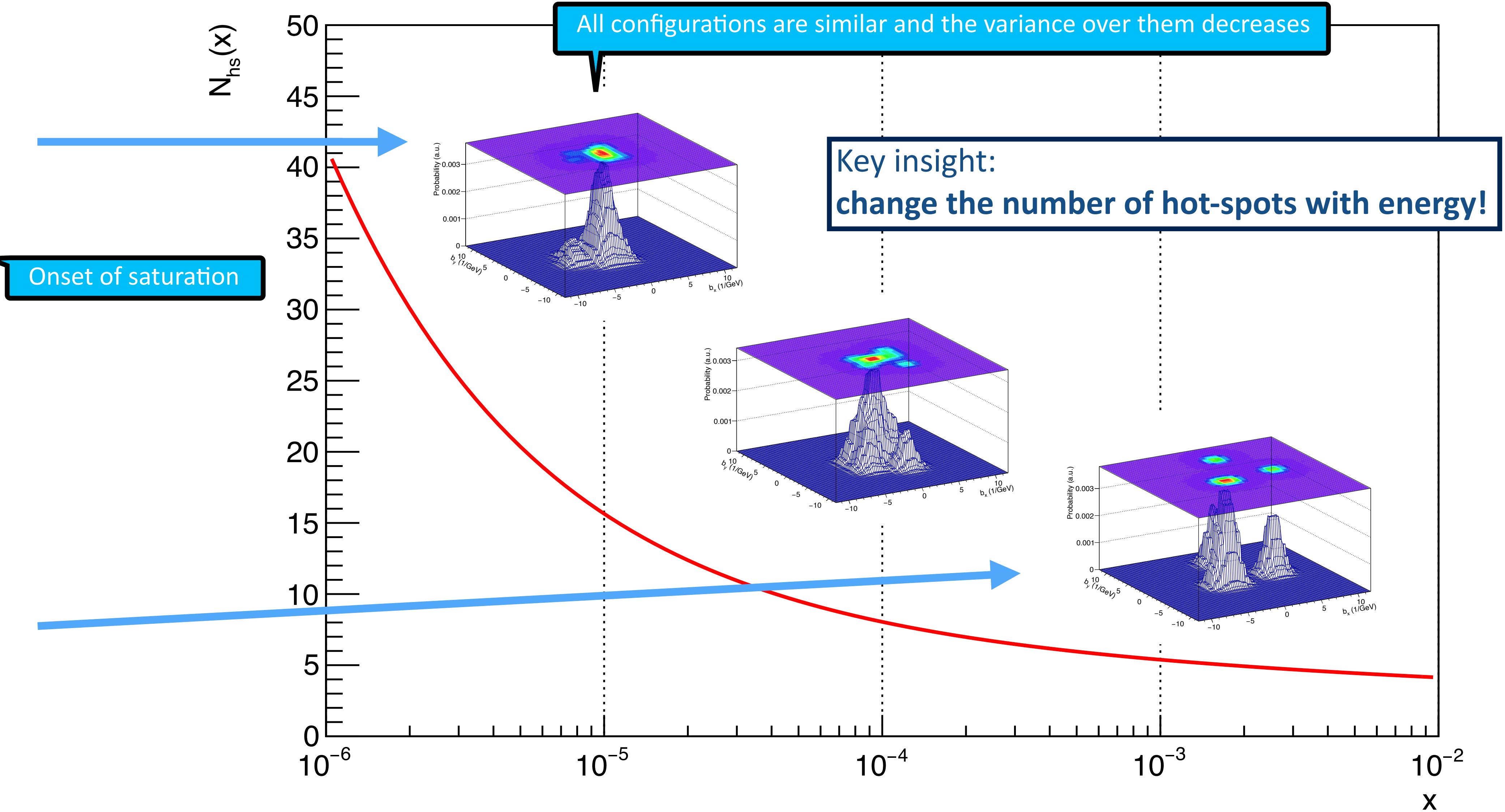
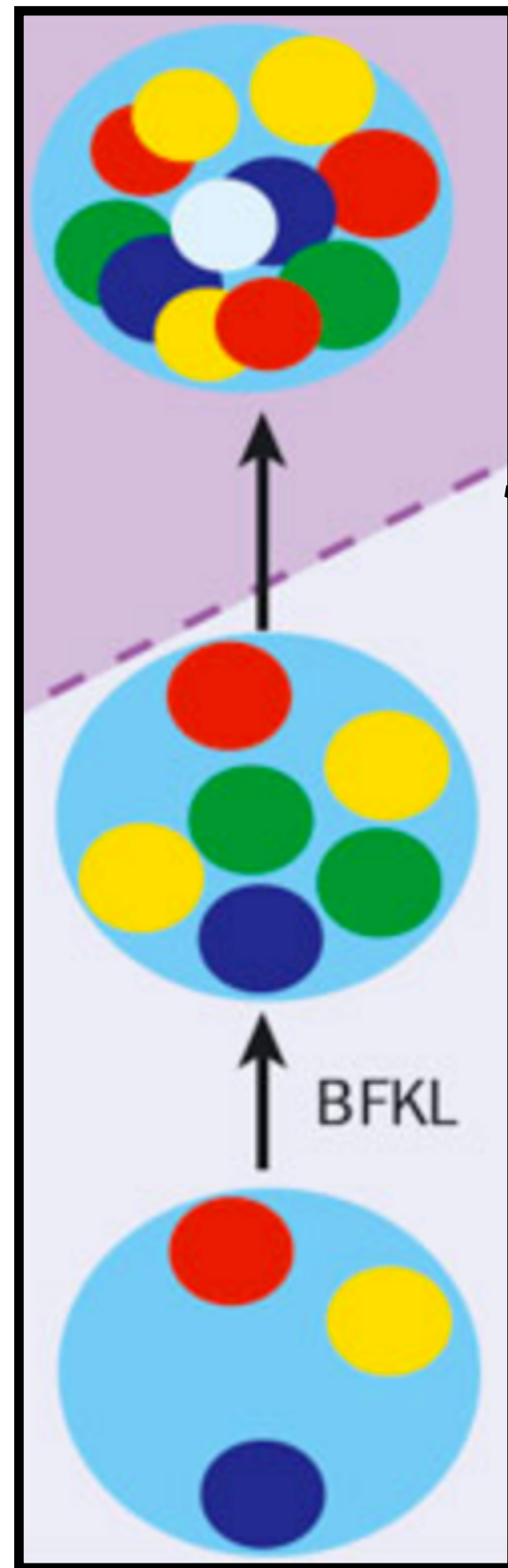
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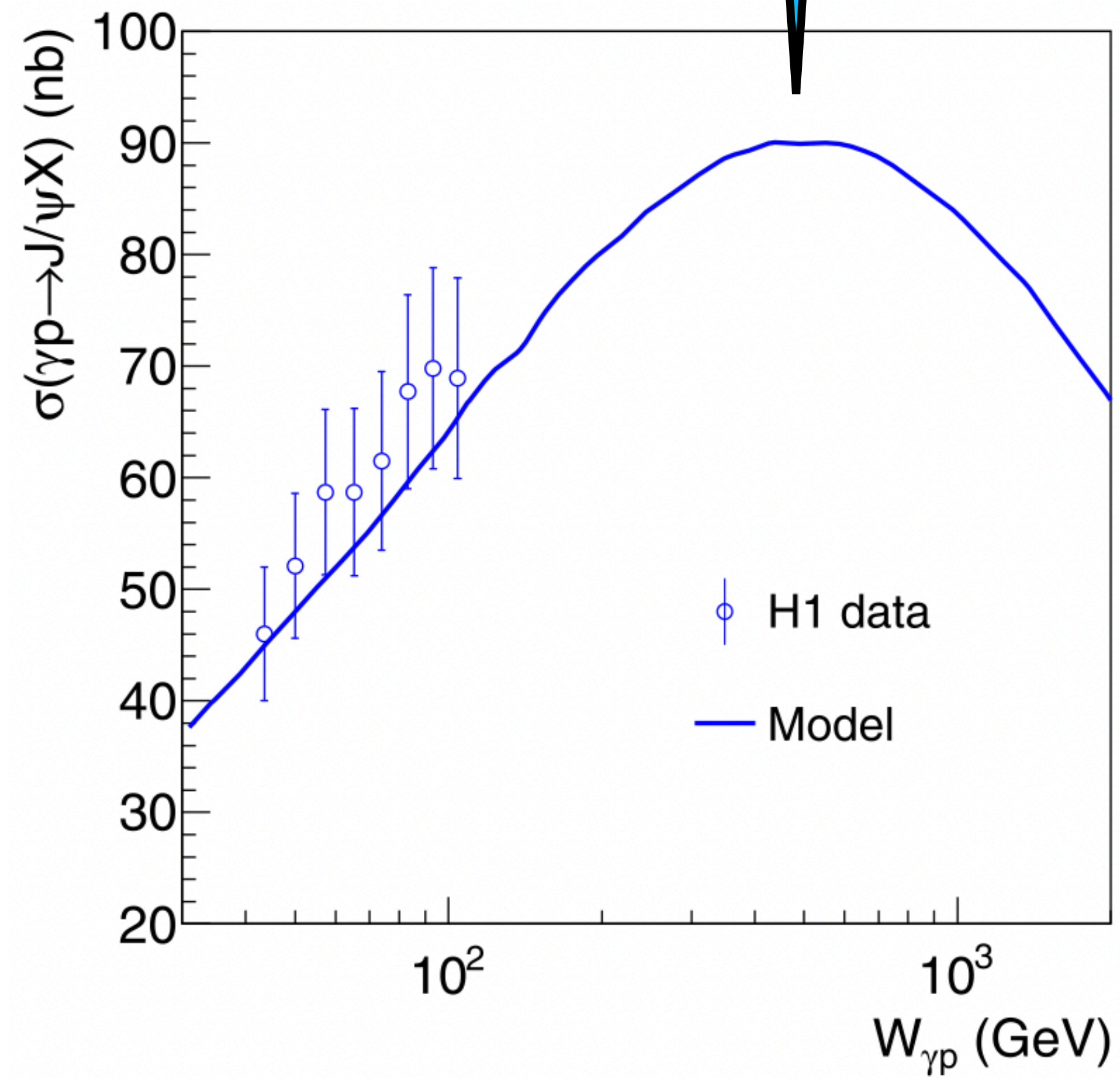


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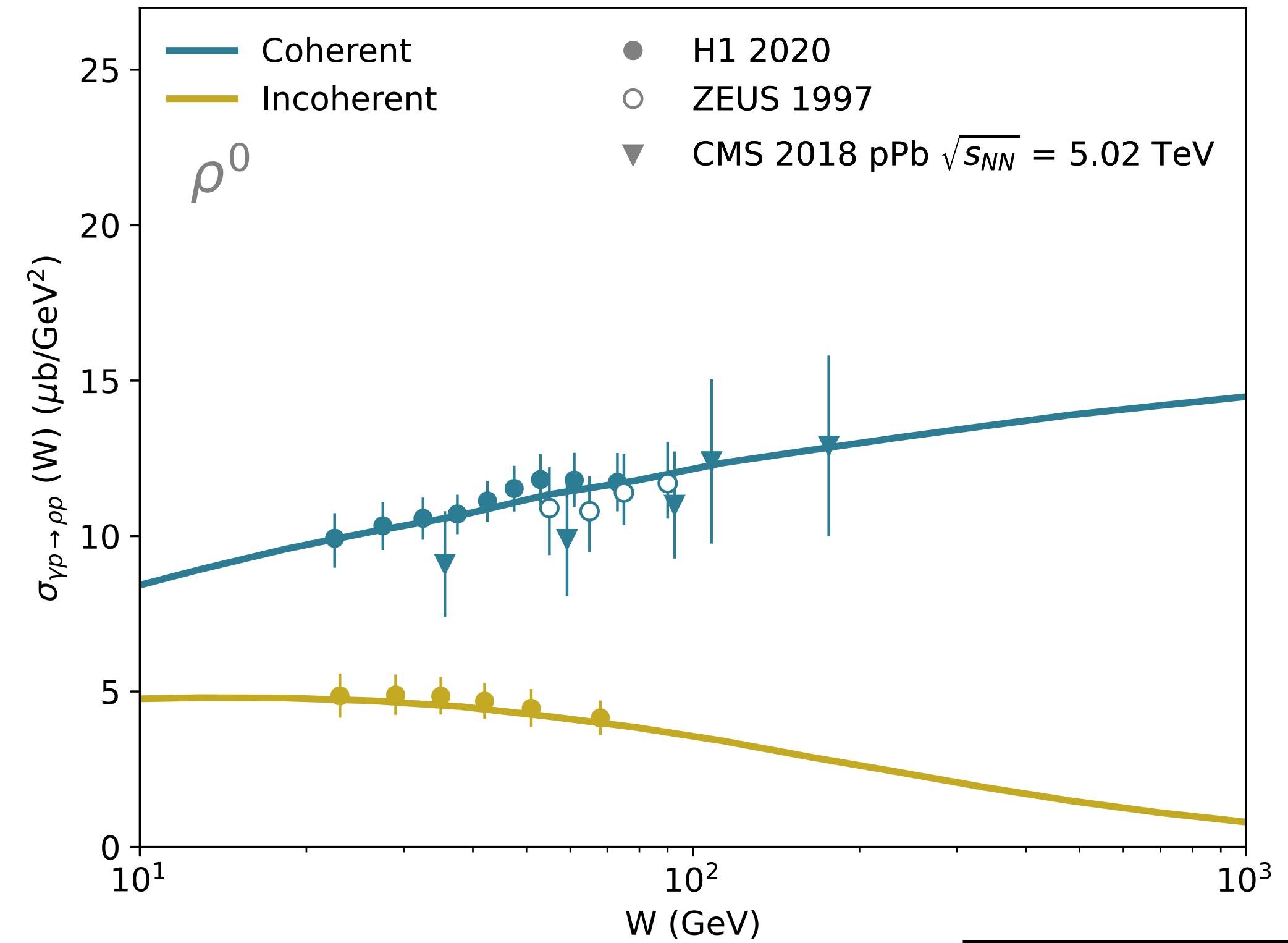
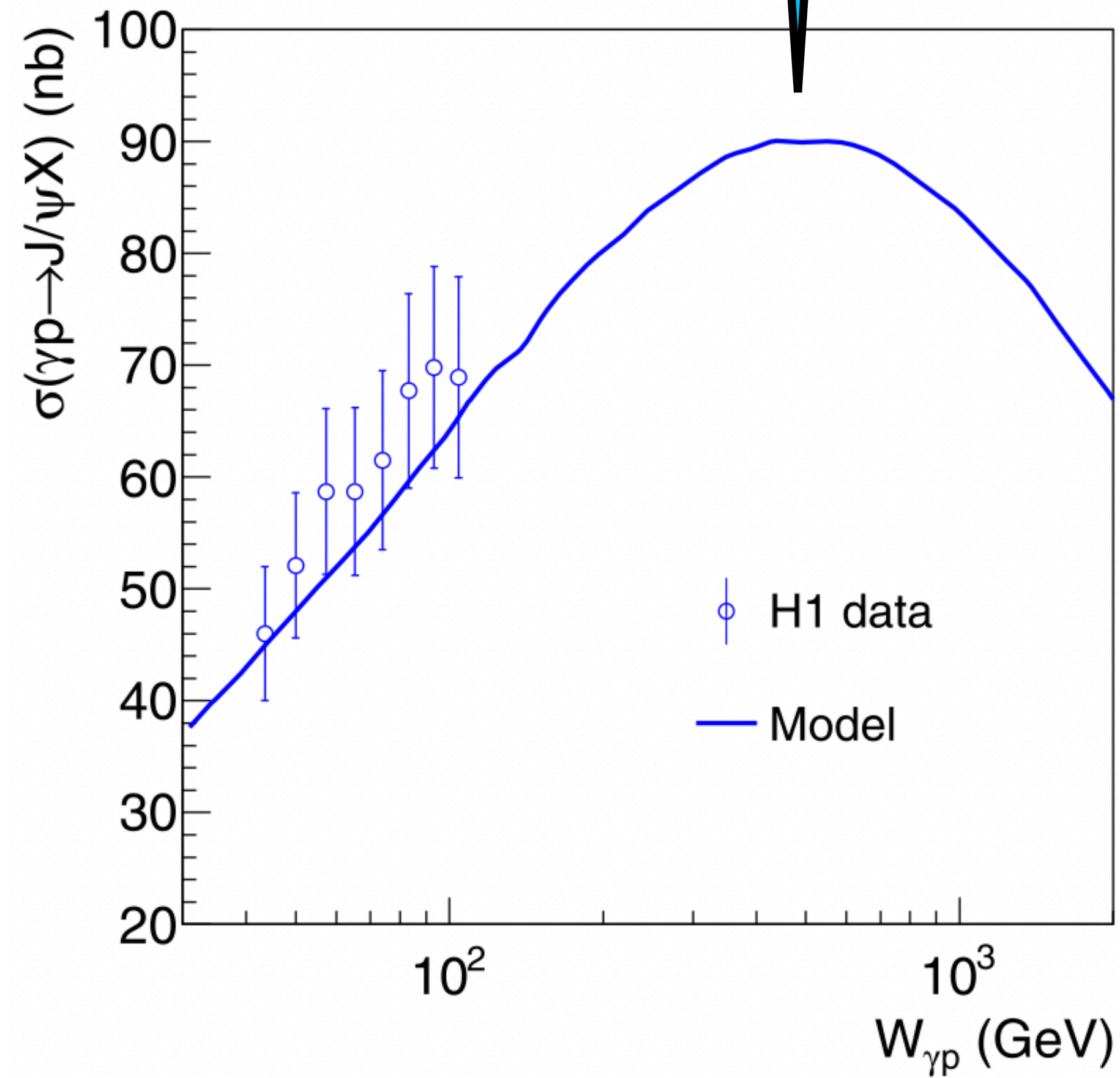
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In this model the onset of saturation is here



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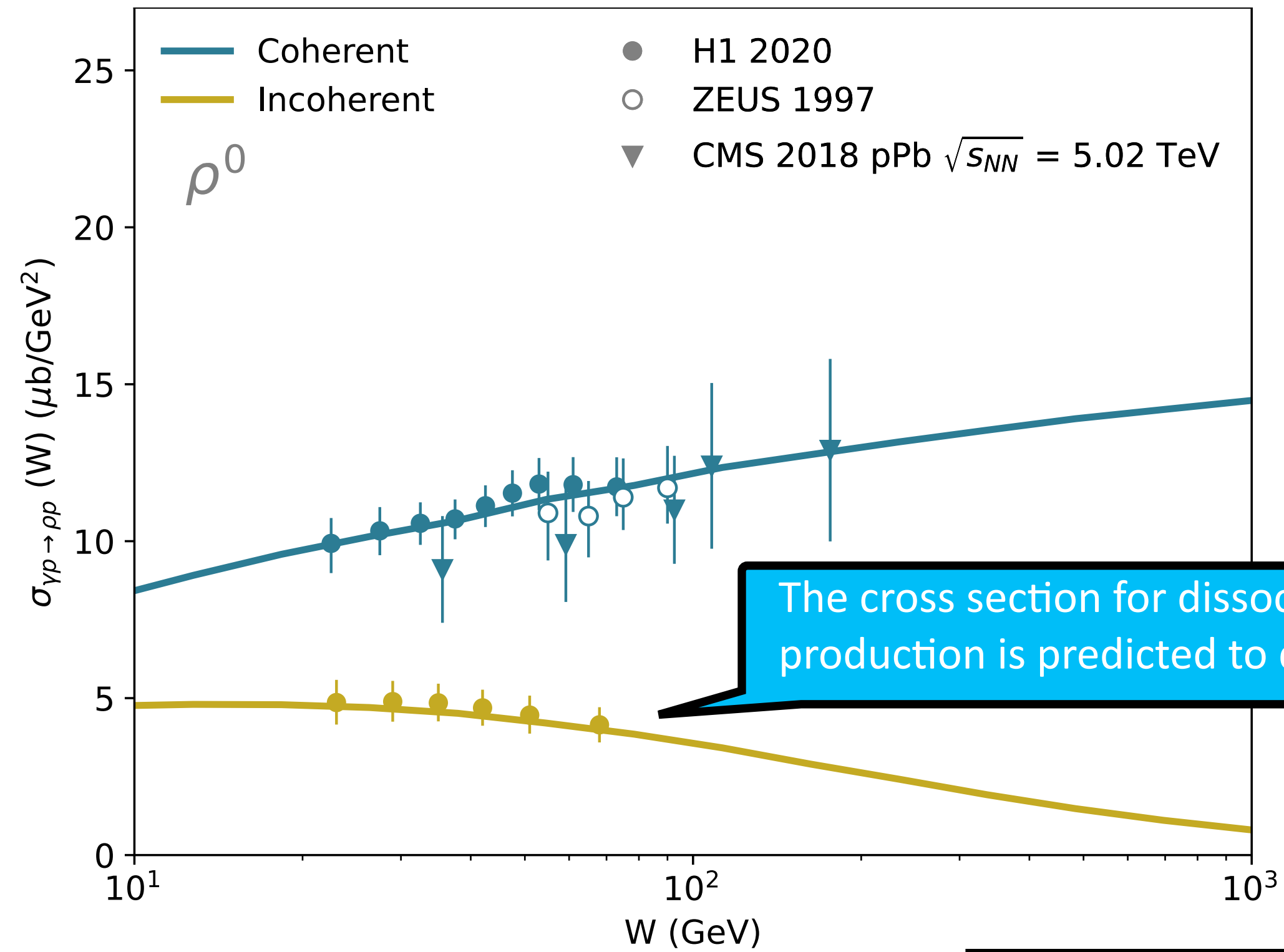
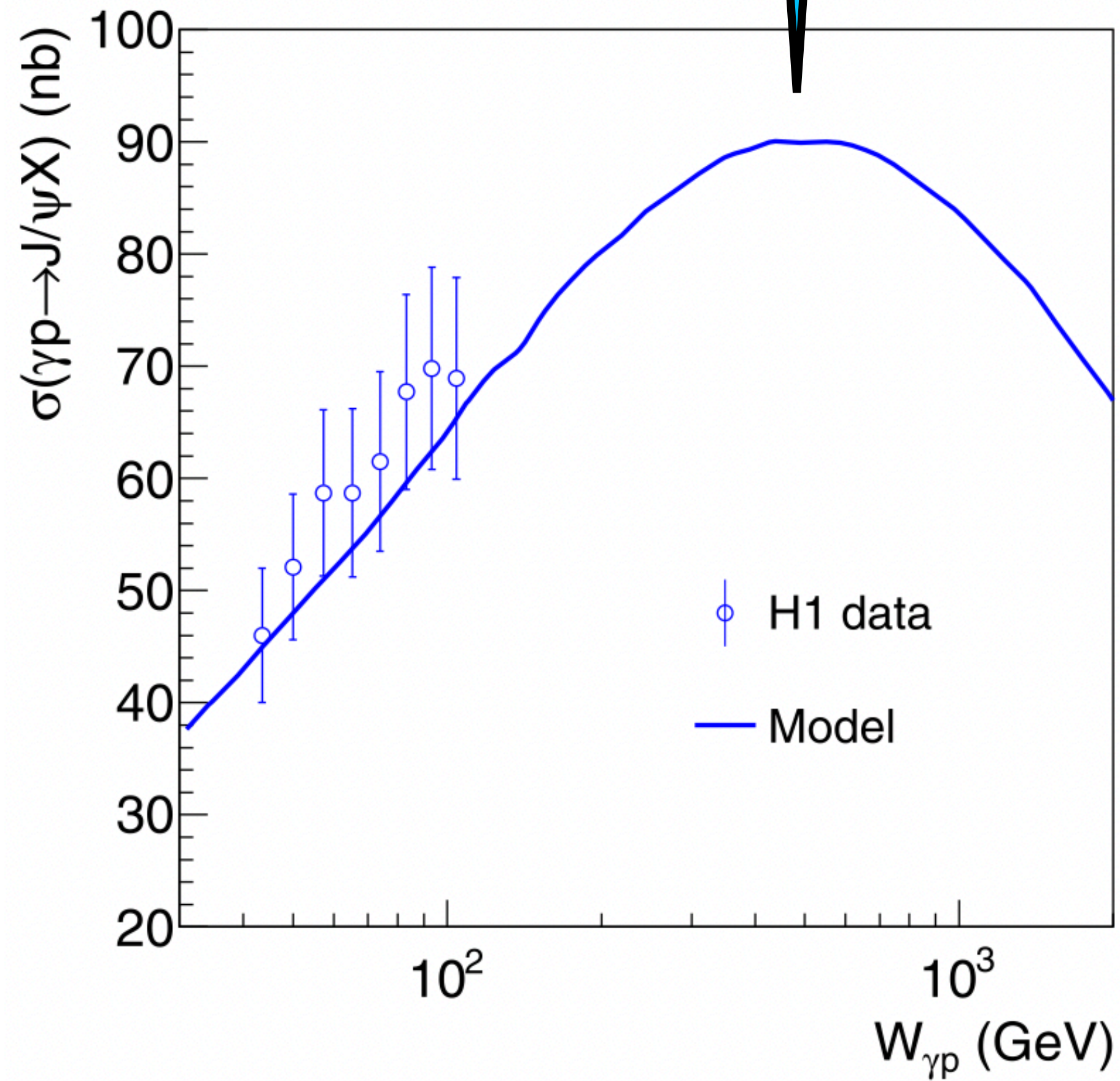
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Cepila et al, arXiv 2312.#####

Energy-dependent hot-spot model (2/2)

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The cross section for dissociative ρ photo-production is predicted to decrease

Cepila et al, arXiv 2312.#####

Dissociative ρ photoproduction offers some tantalising results
But the ρ mass-scale is low, so the application of perturbative ideas to interpret data is in question
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Where and how can we study this type of processes at even higher energies?

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Enter RHIC and the LHC where we can
study photon-induced processes off nuclei

5

Understanding the photon flux in collisions of heavy ions

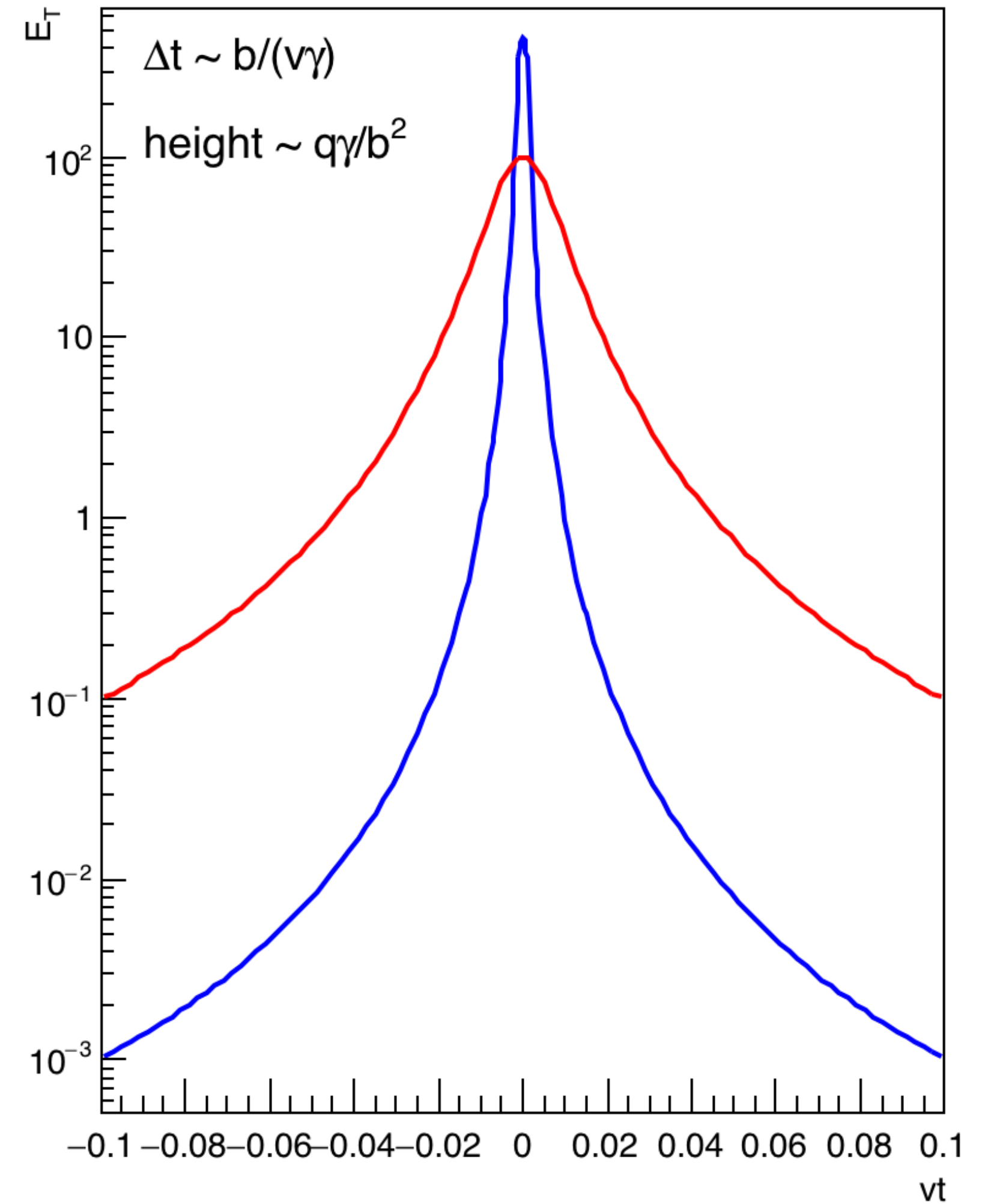
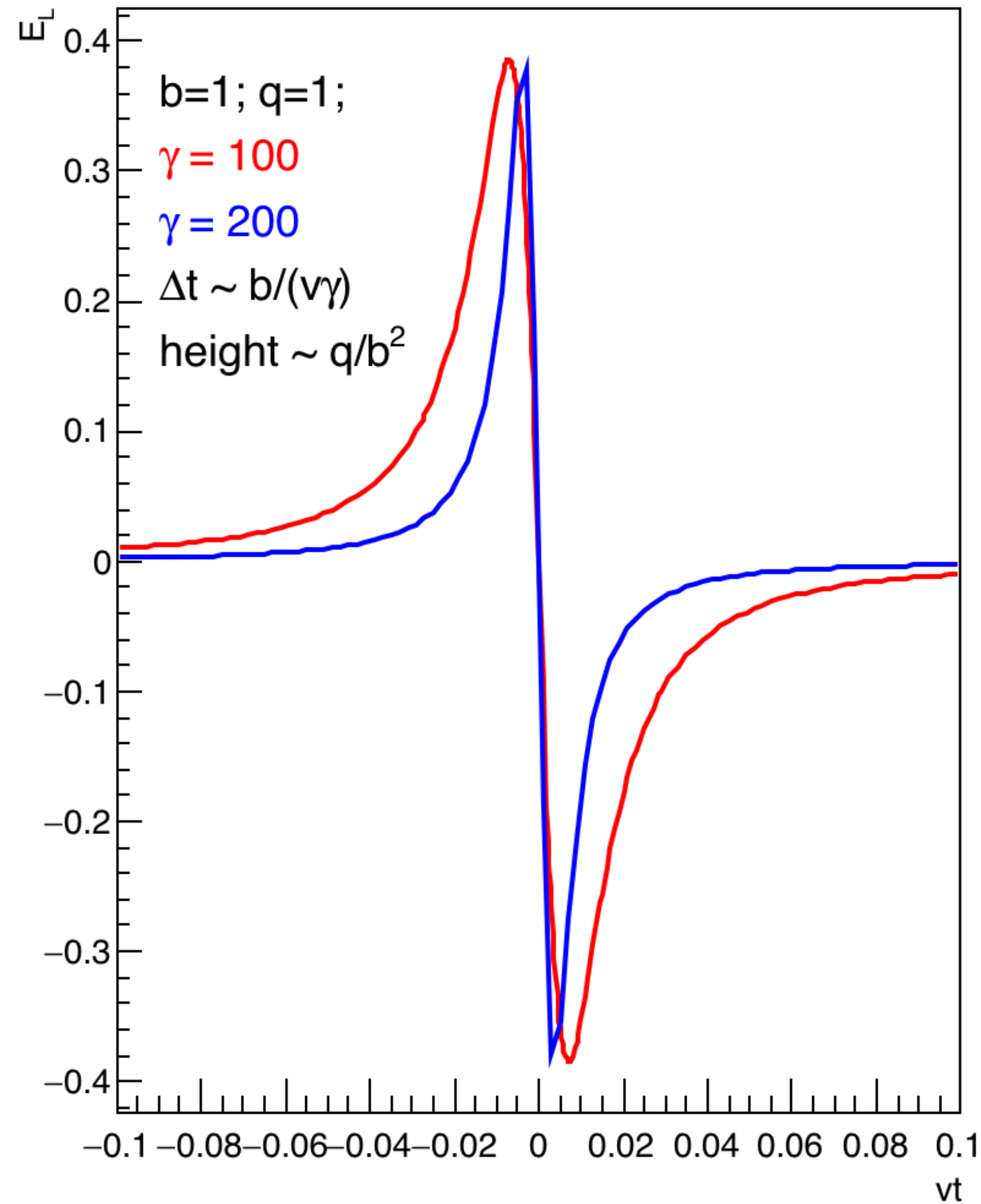
proportional to Z^2

Heavy ions have intense electromagnetic fields that can be used to study photon-induced interactions

The photon flux: field of a point charge

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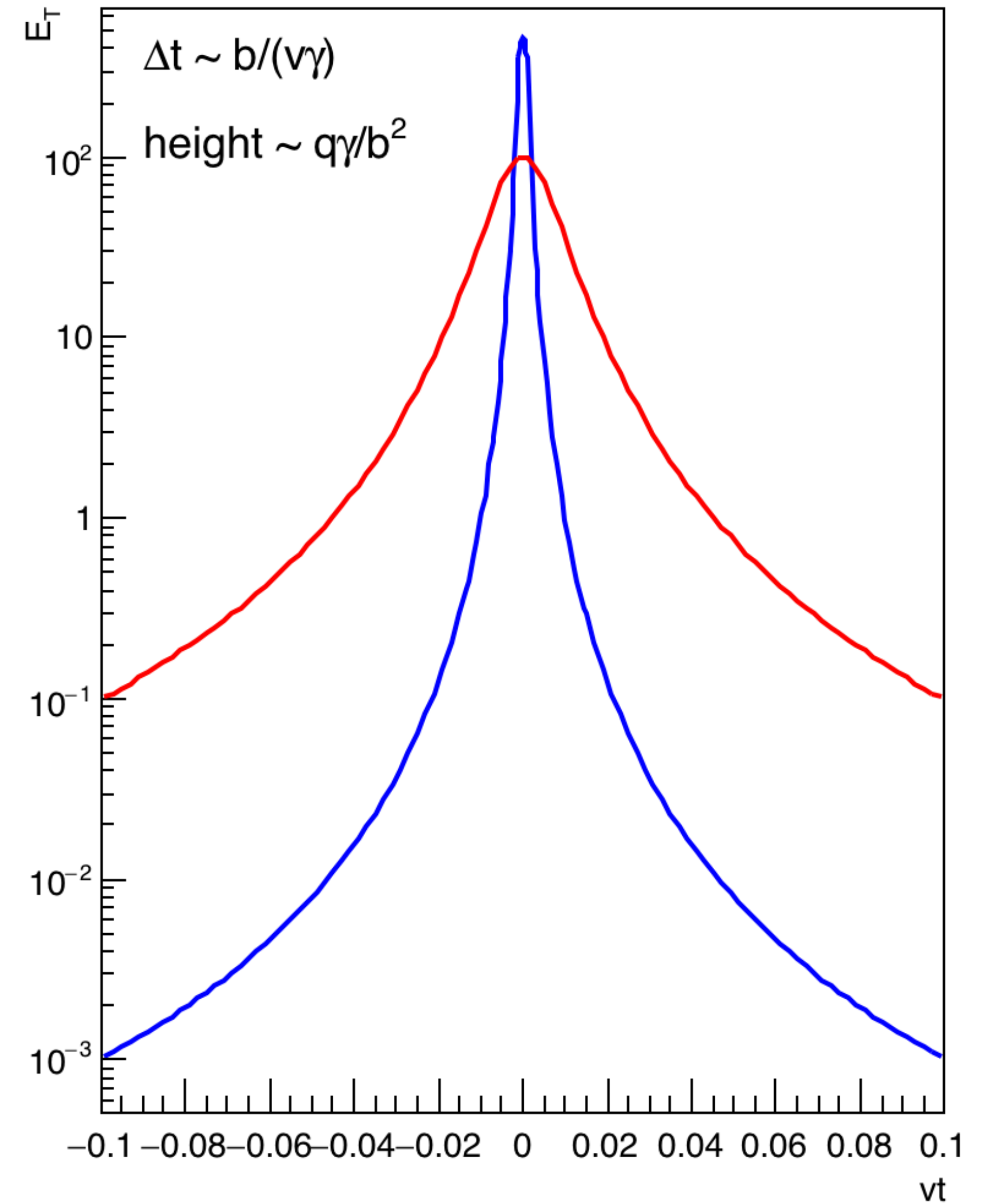
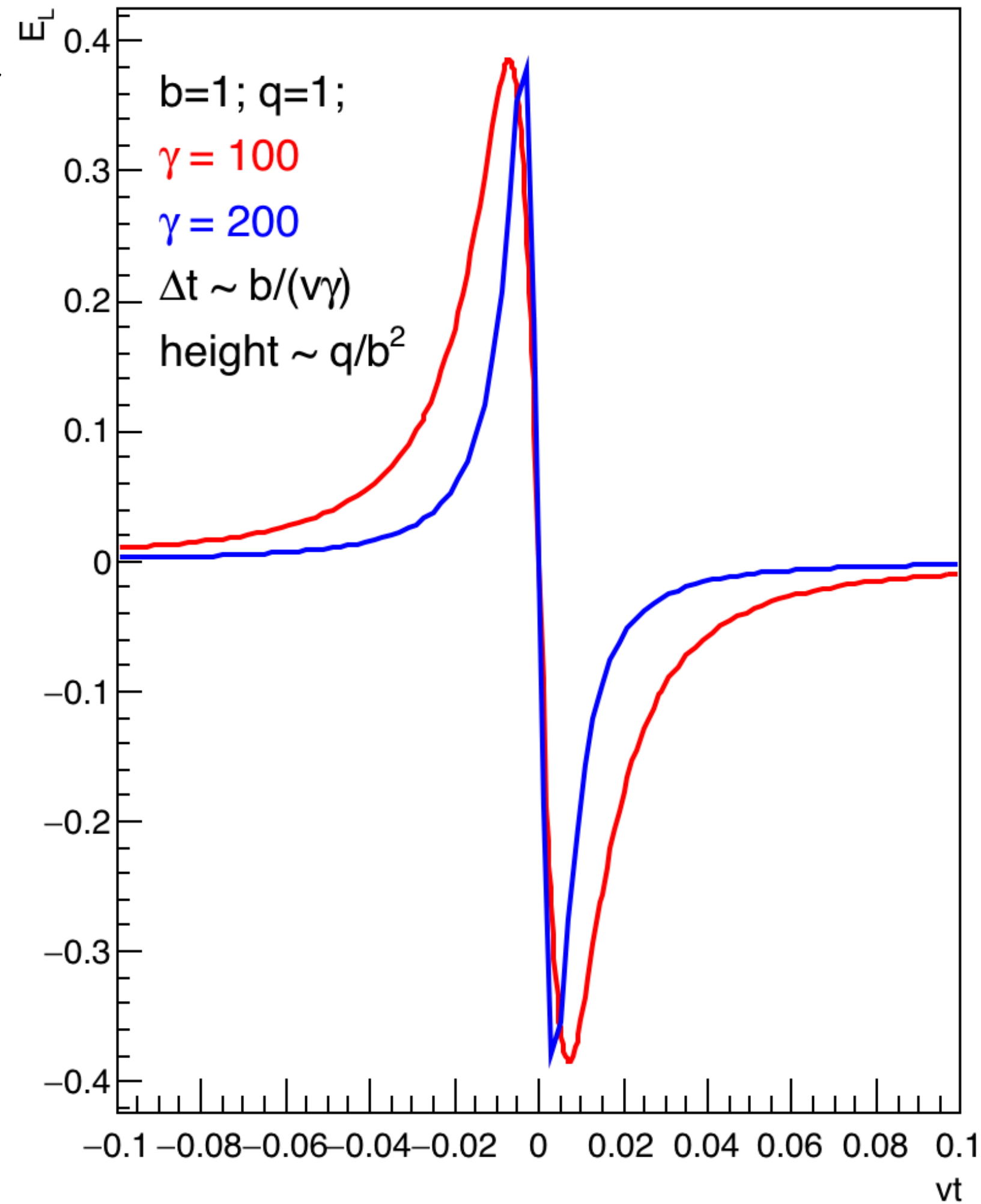
Take the electric field of the particle at rest and boost it to the collider frame



The photon flux: field of a point charge

Take the electric field of the particle at rest and boost it to the collider frame

Longitudinal component

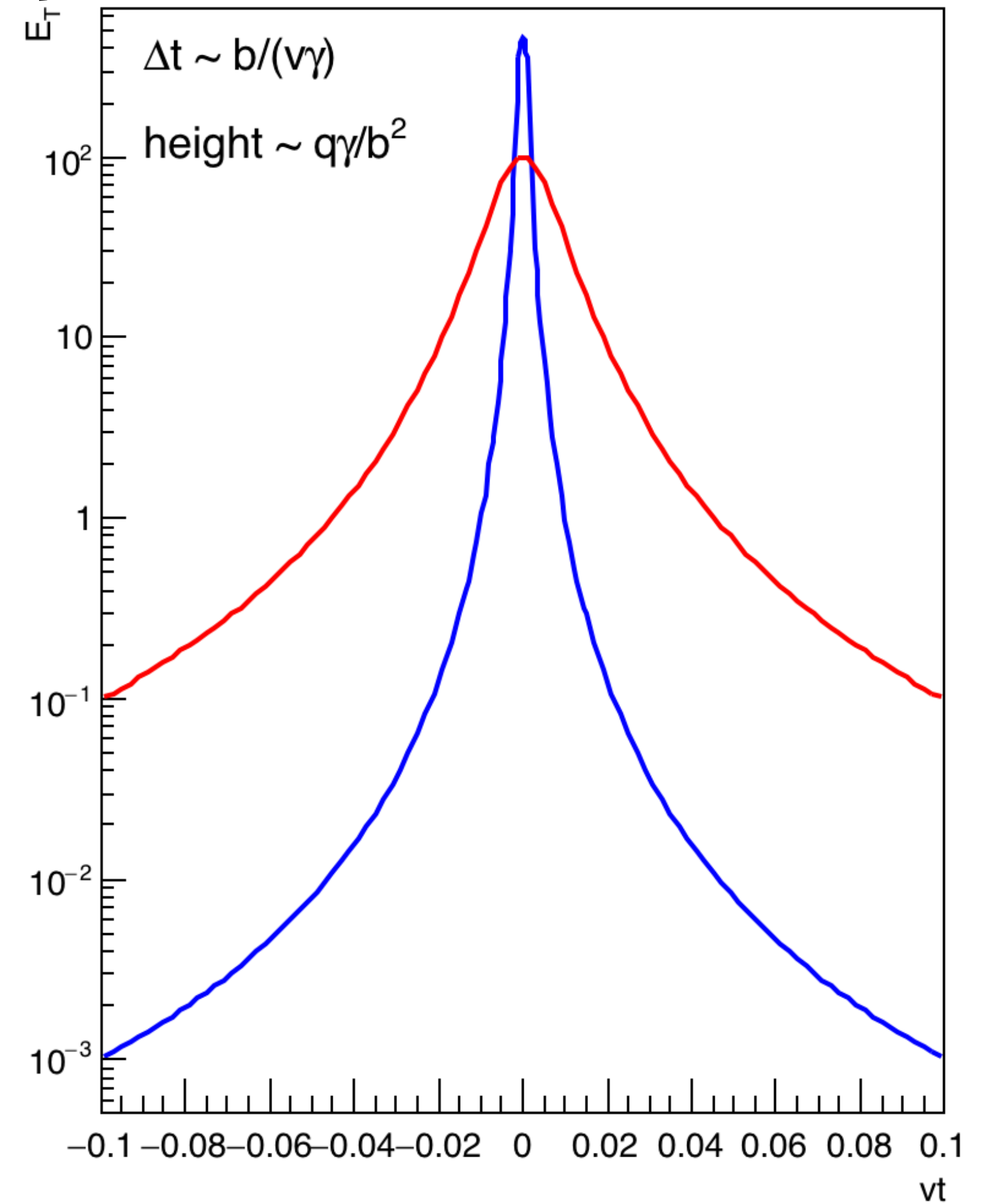
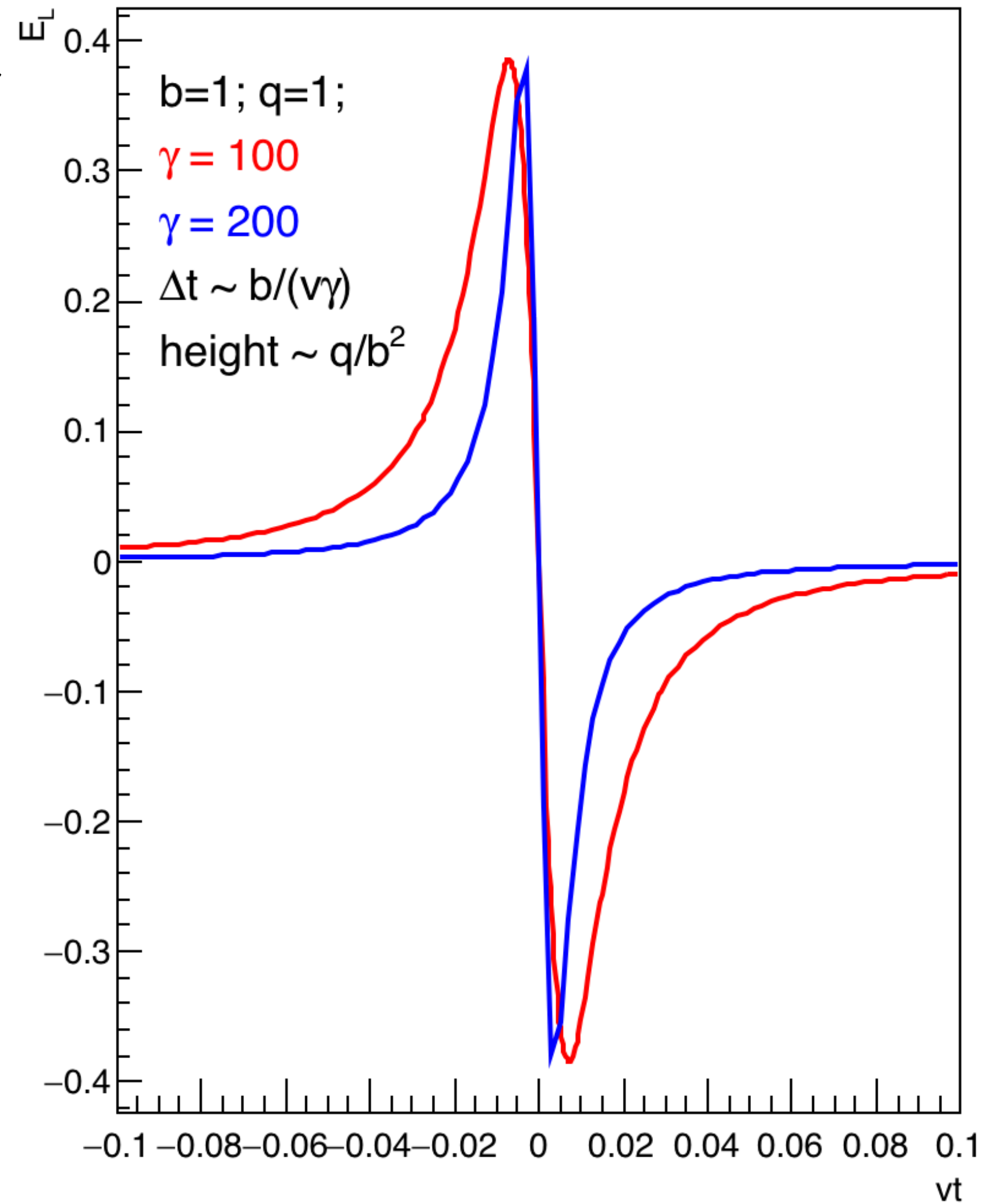


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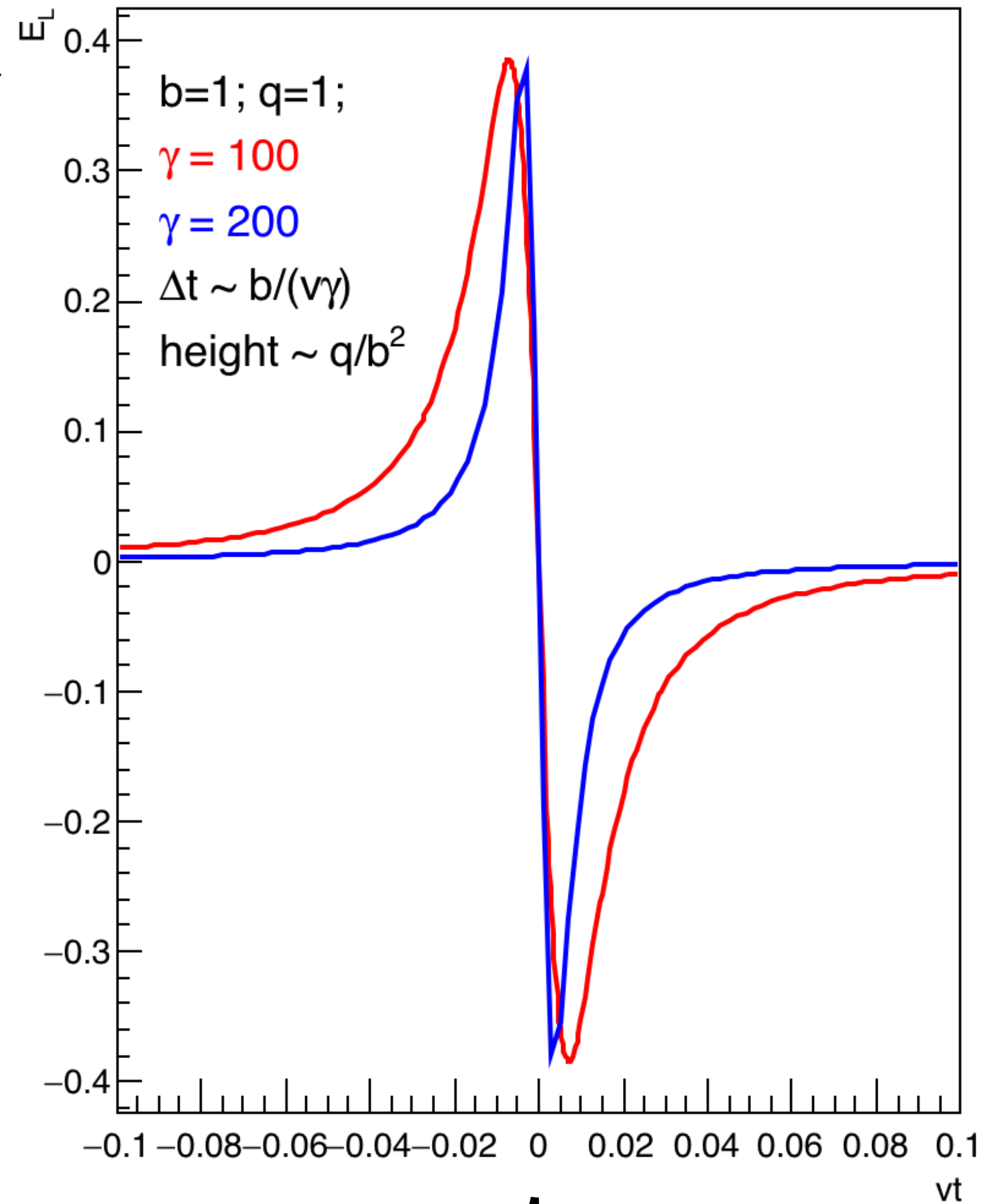


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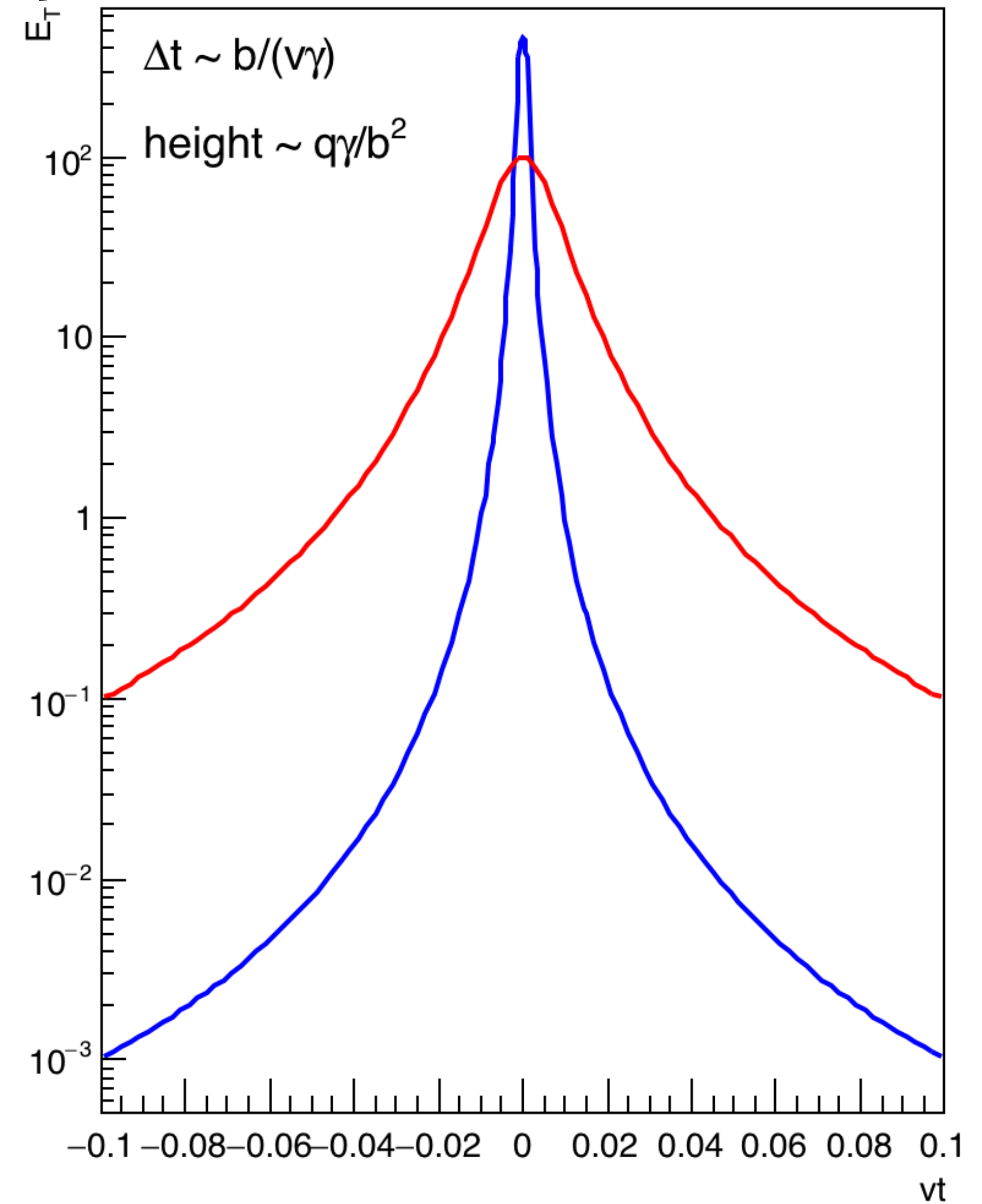
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Observation point

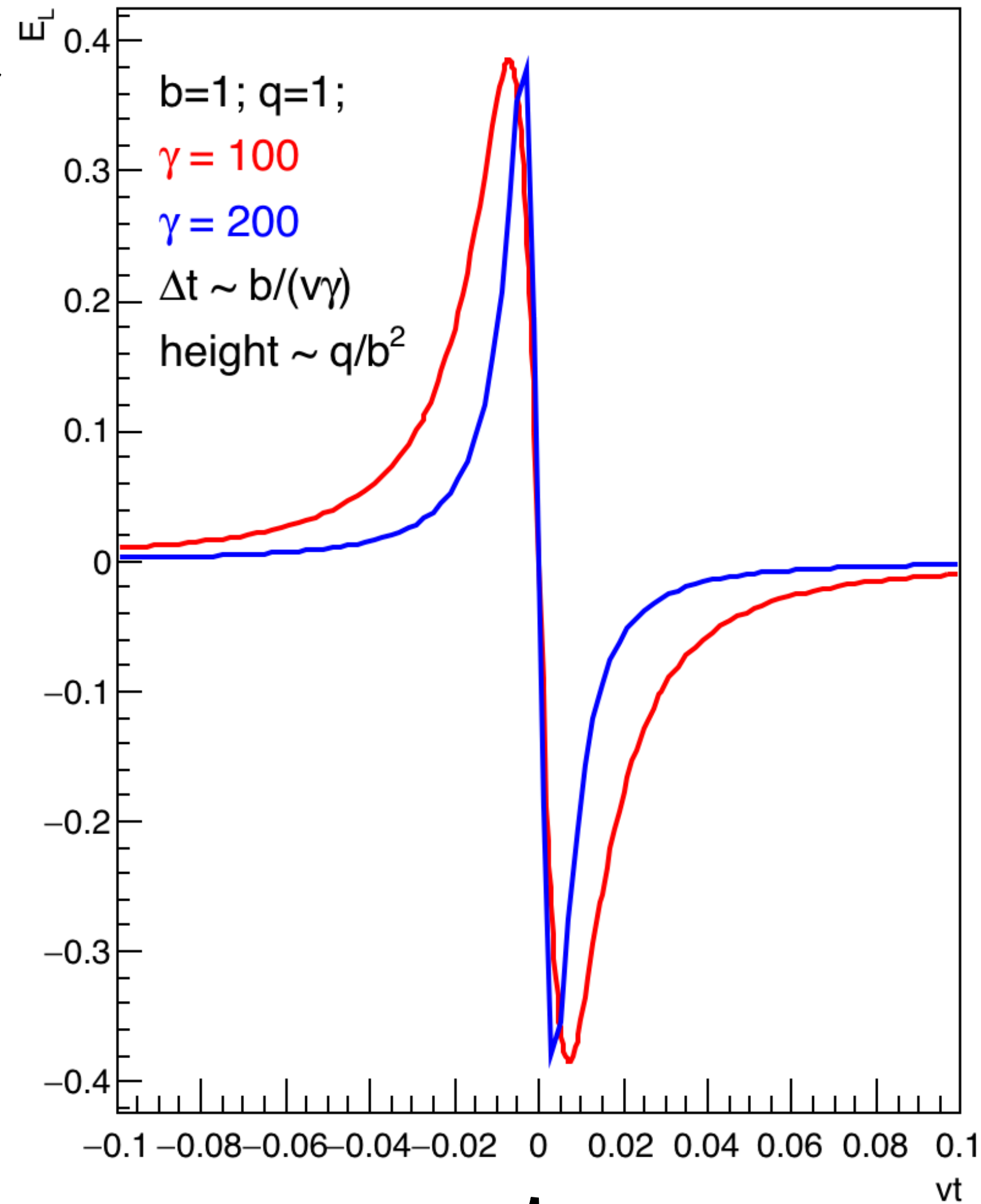


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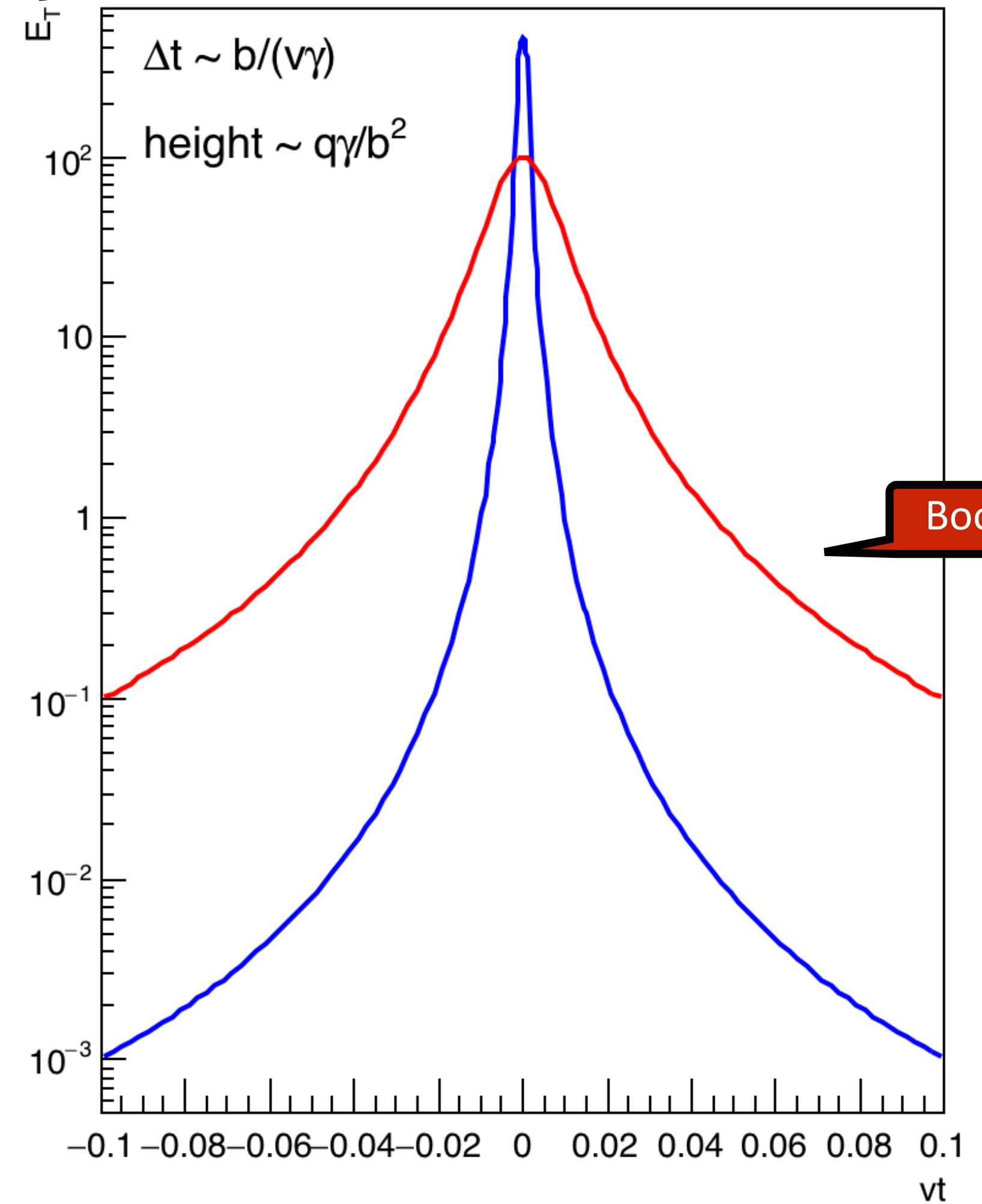
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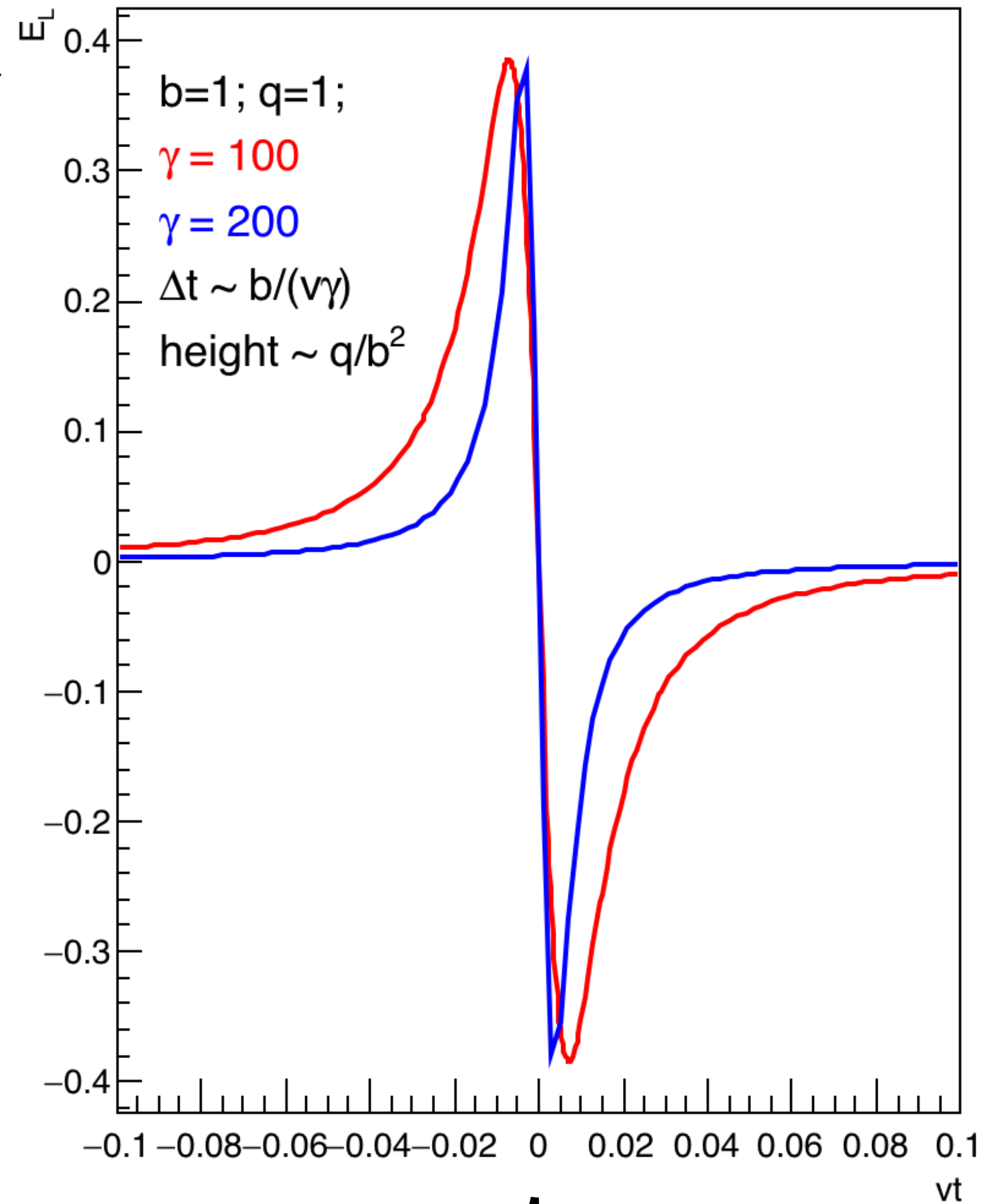
Boost = 100

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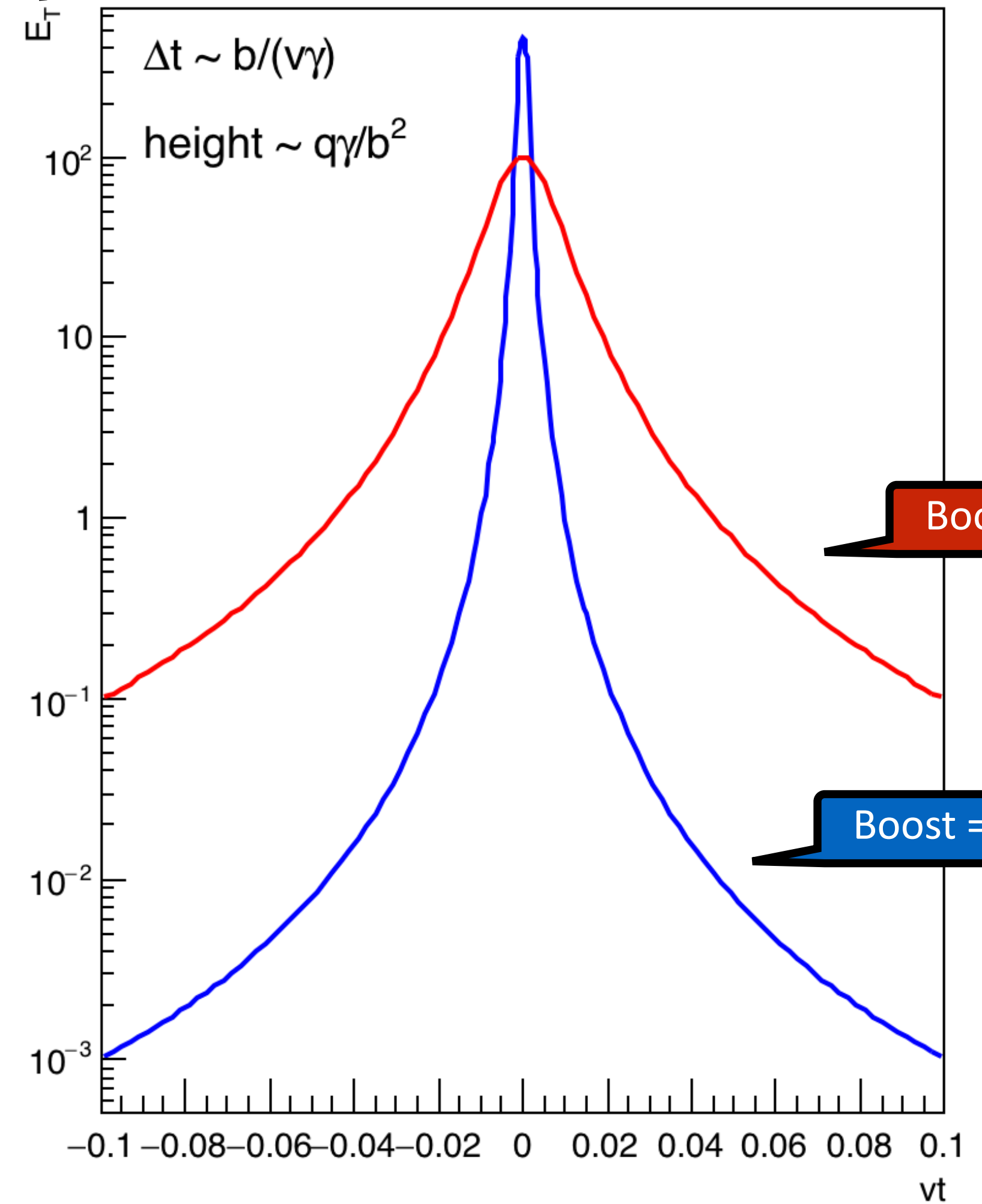
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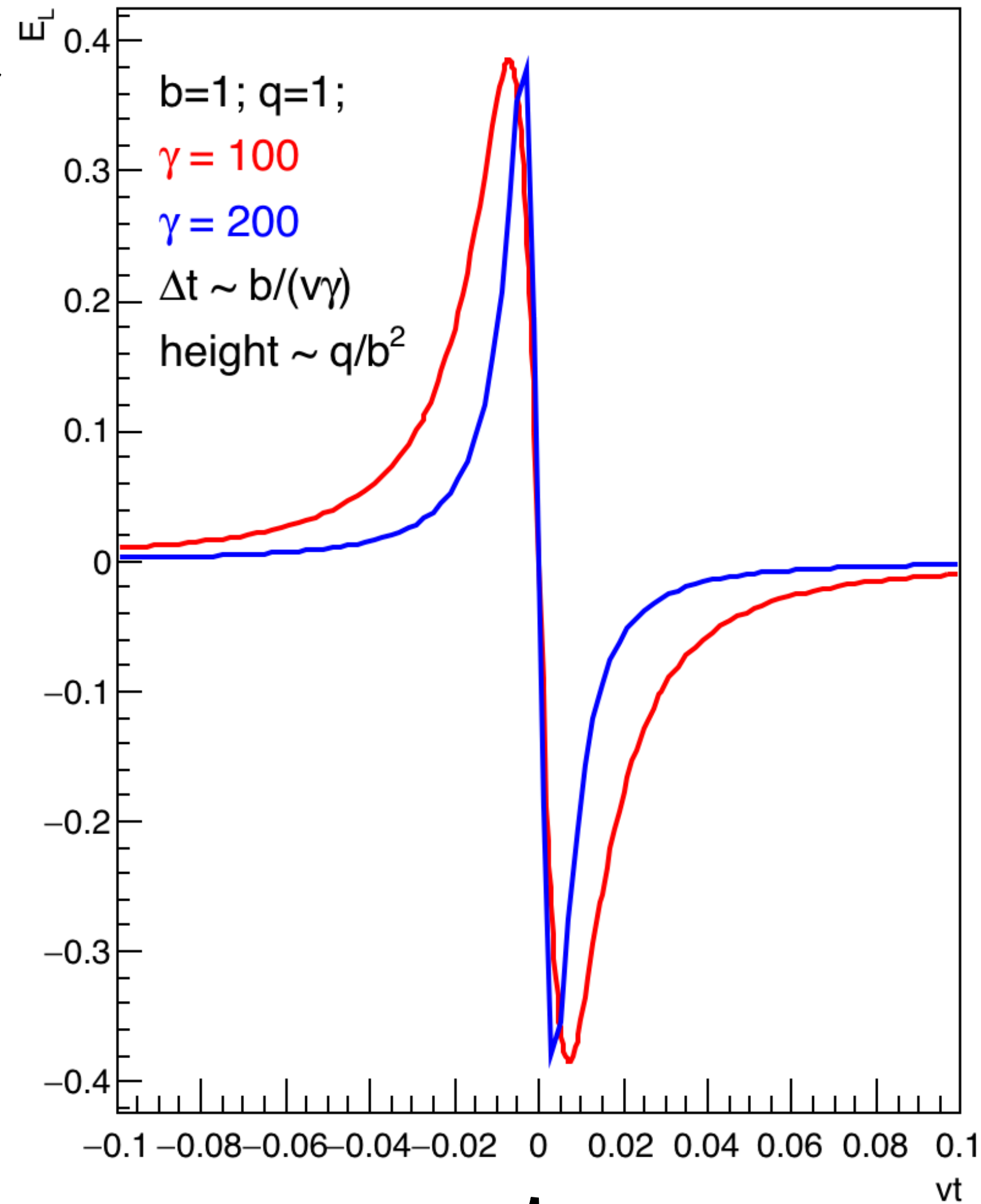


The photon flux: field of a point charge

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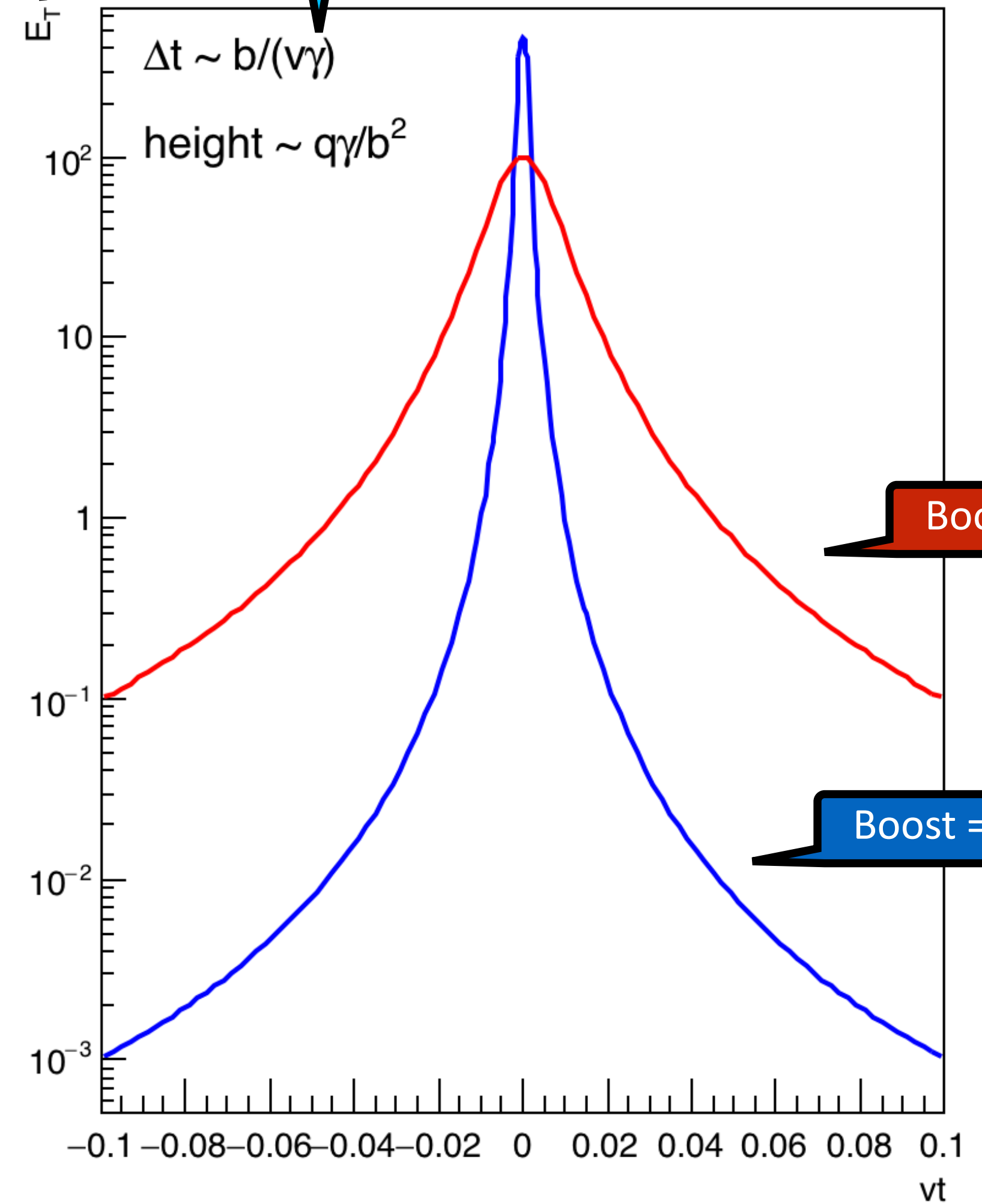
Transverse component

Longitudinal component



Observation point

Narrowness and height driven by boost factor

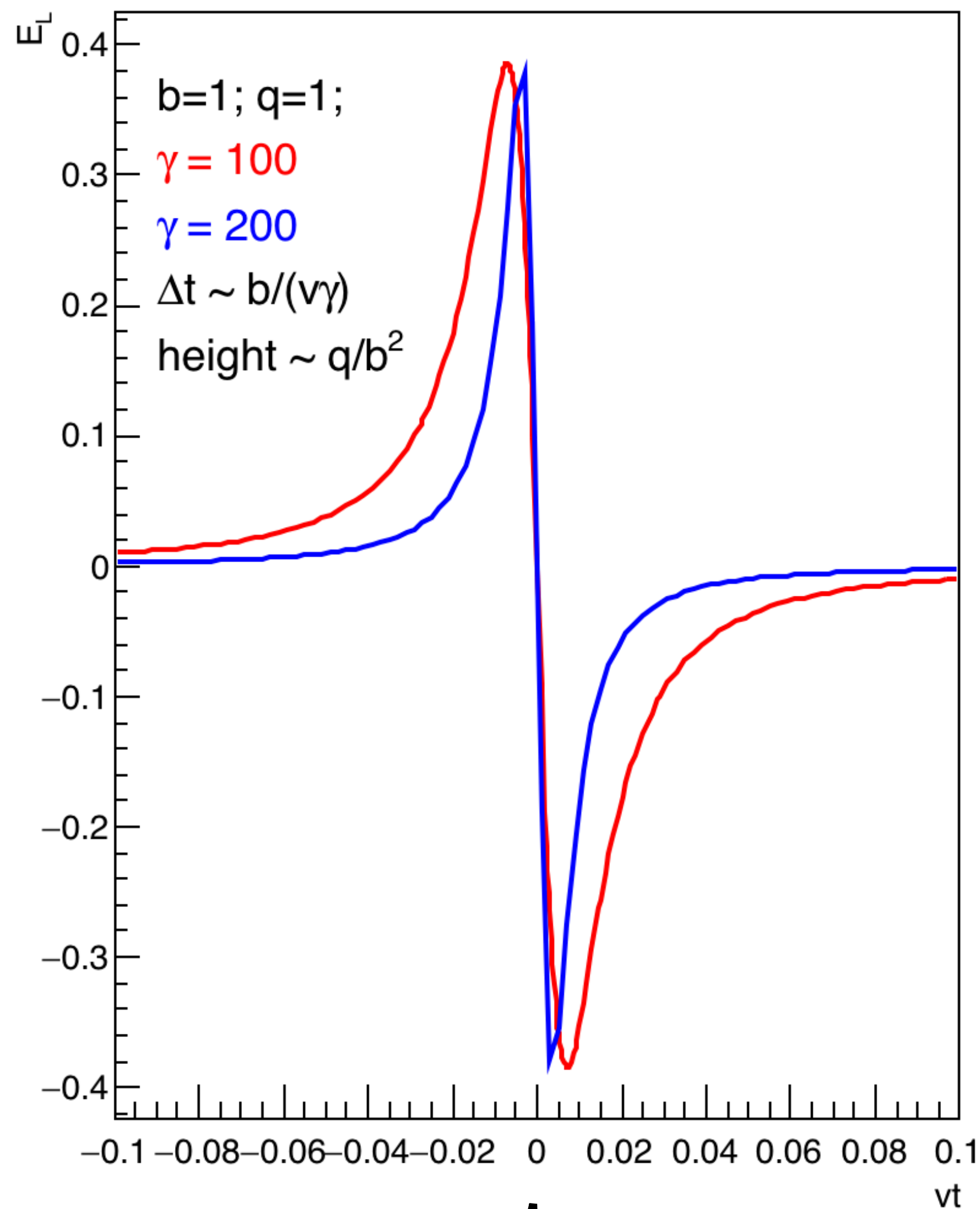


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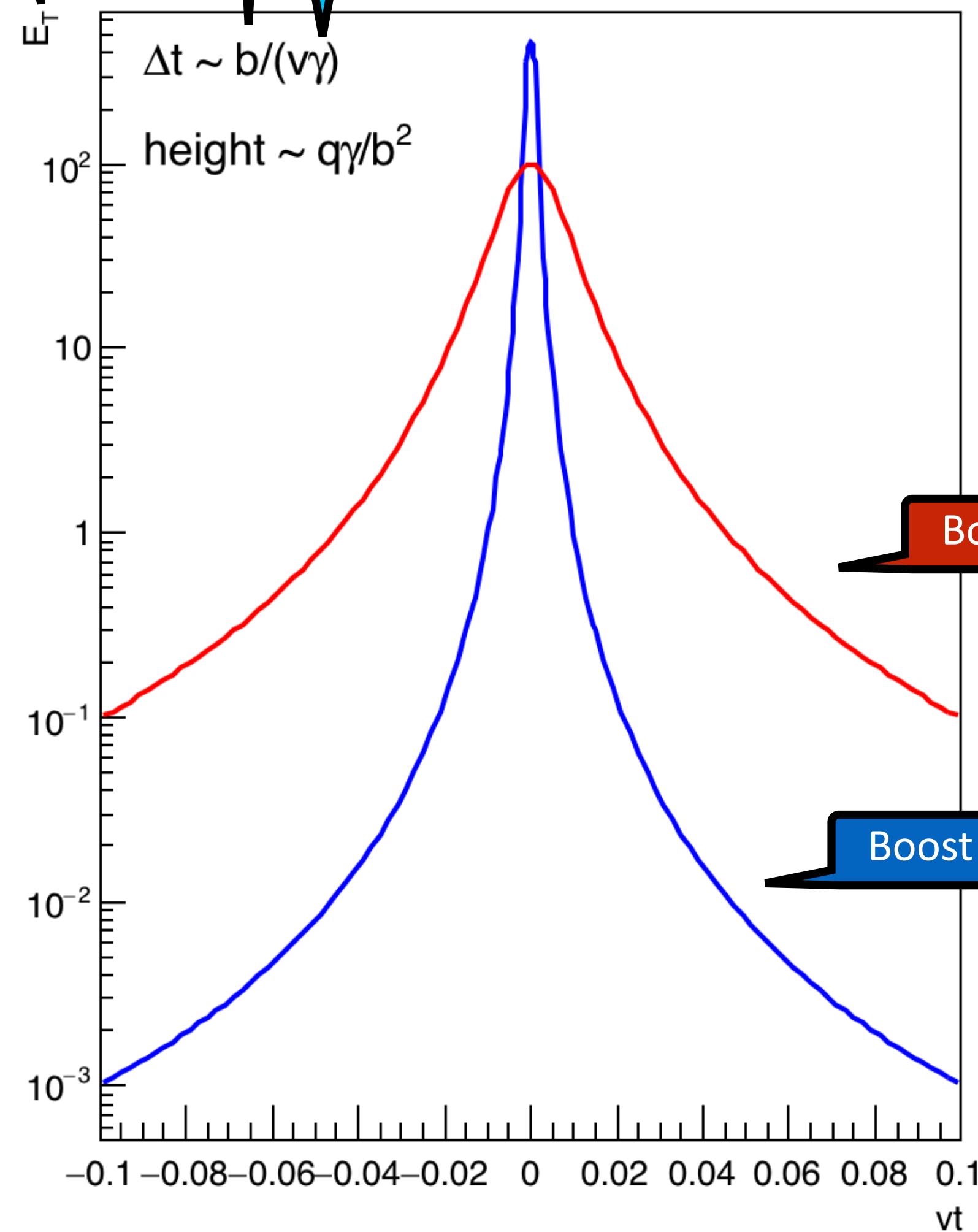
Longitudinal component



Observation point

... and distance from the charge

Narrowness and height driven by boost factor



Boost = 100

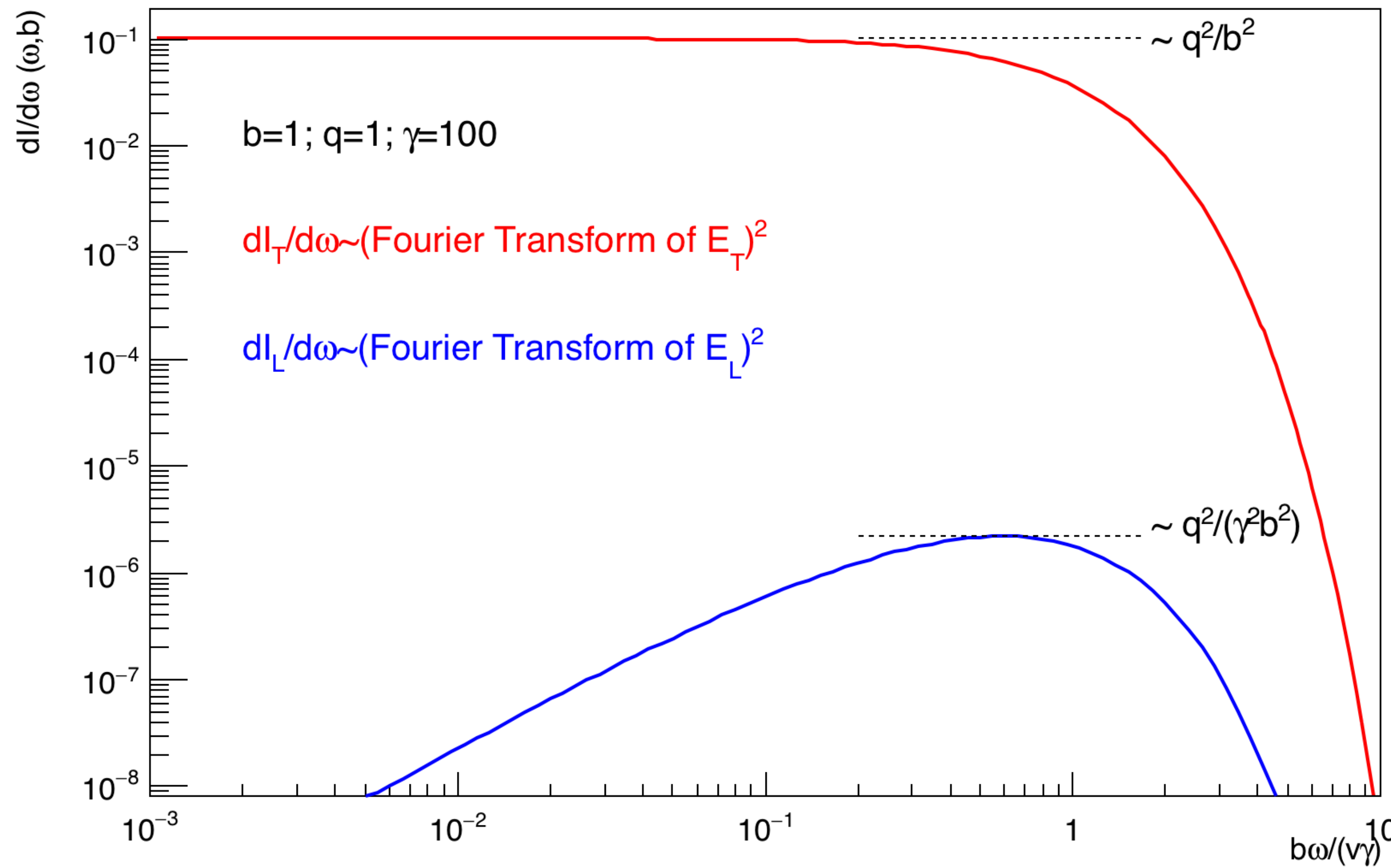
Boost = 200

The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space

The photon flux: Fourier transform for the field of a point charge

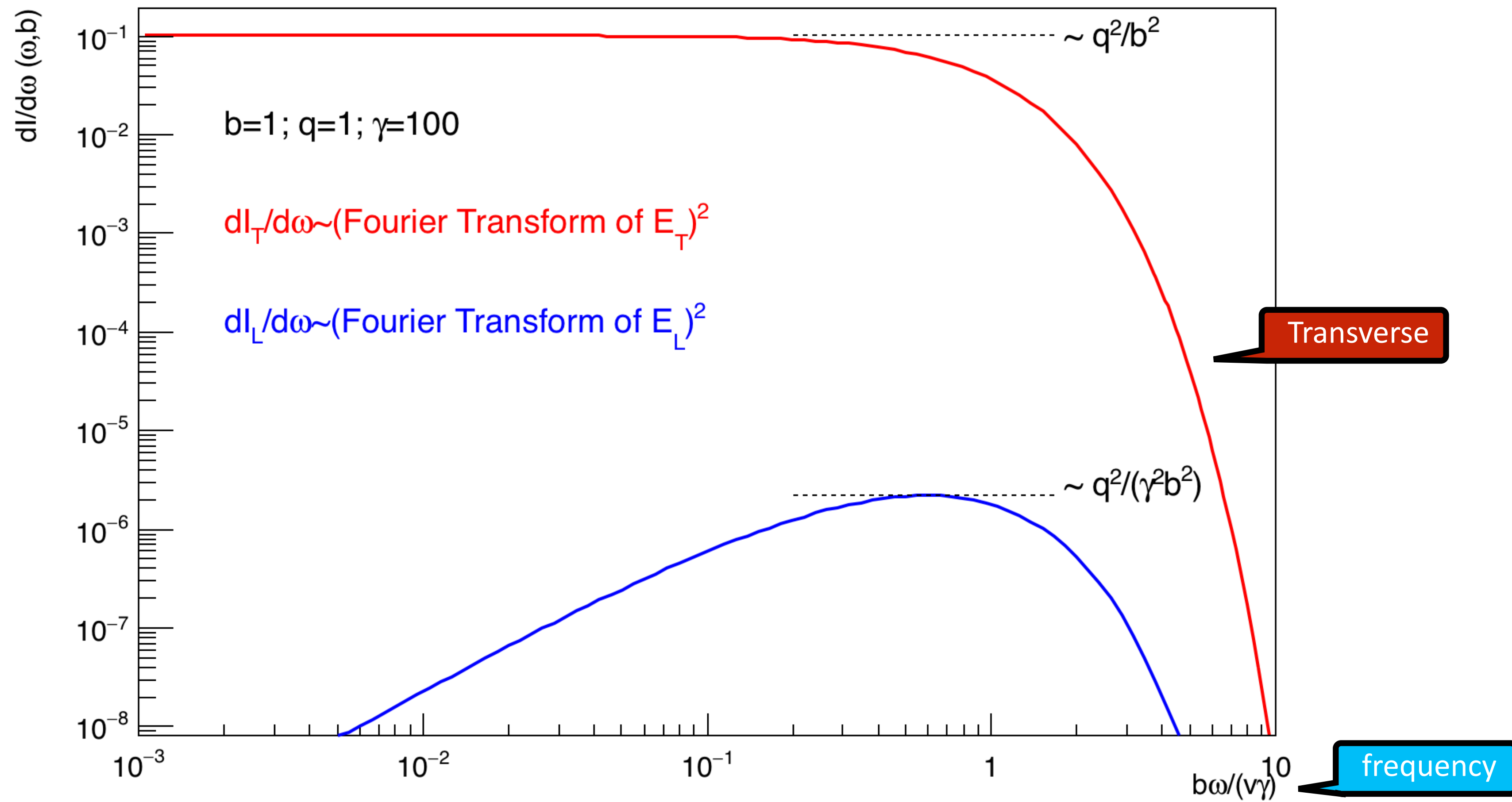
Take the square of the Fourier transform of the electric field into frequency space



frequency

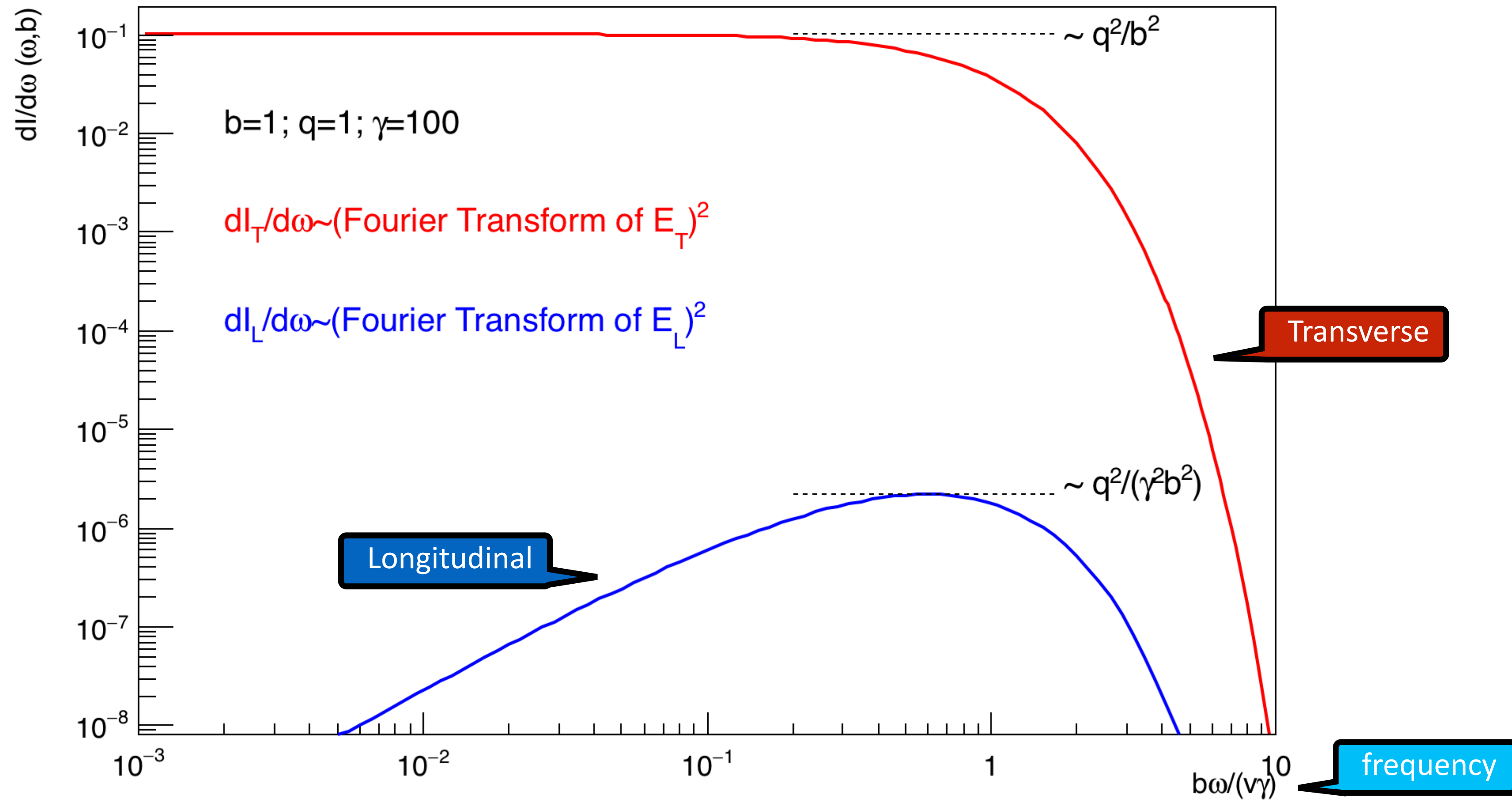
The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space



The photon flux: Fourier transform for the field of a point charge

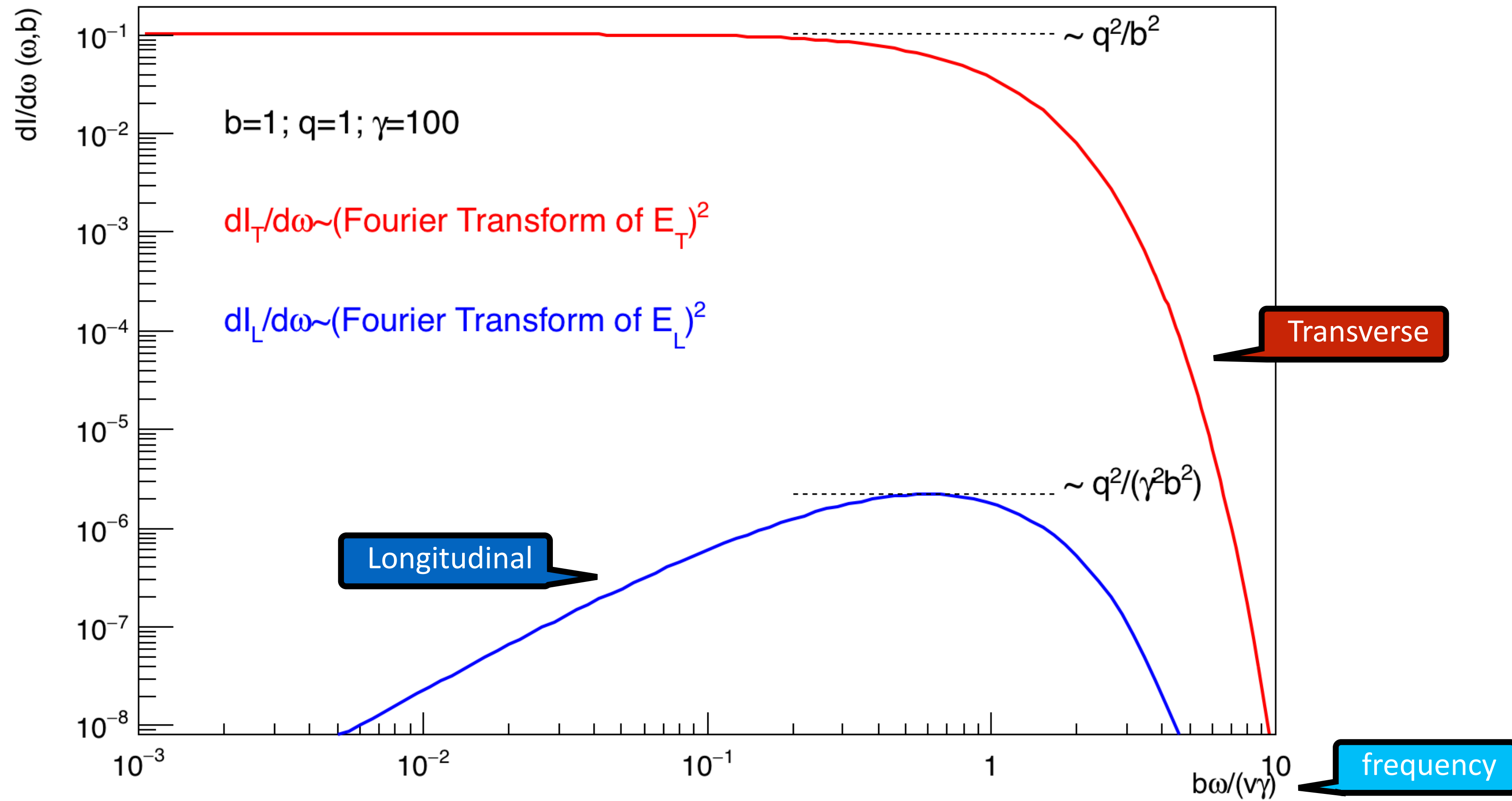
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The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space

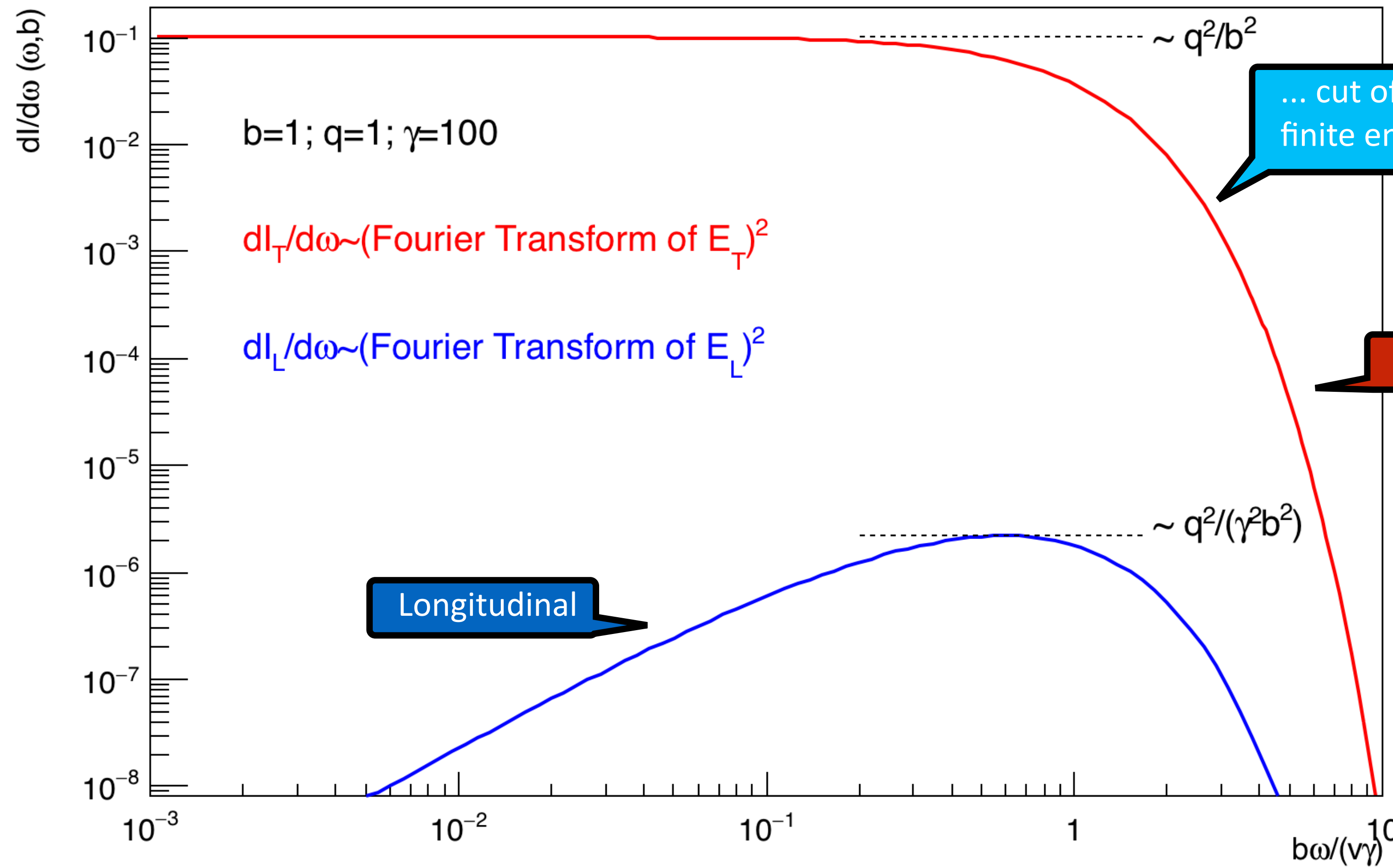
Flat behaviour due to the Dirac-delta-like shape of the field



The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space

Flat behaviour due to the Dirac-delta-like shape of the field



... cut off at large frequencies due to the finite energy (the pulse is not a Dirac delta)

Transverse

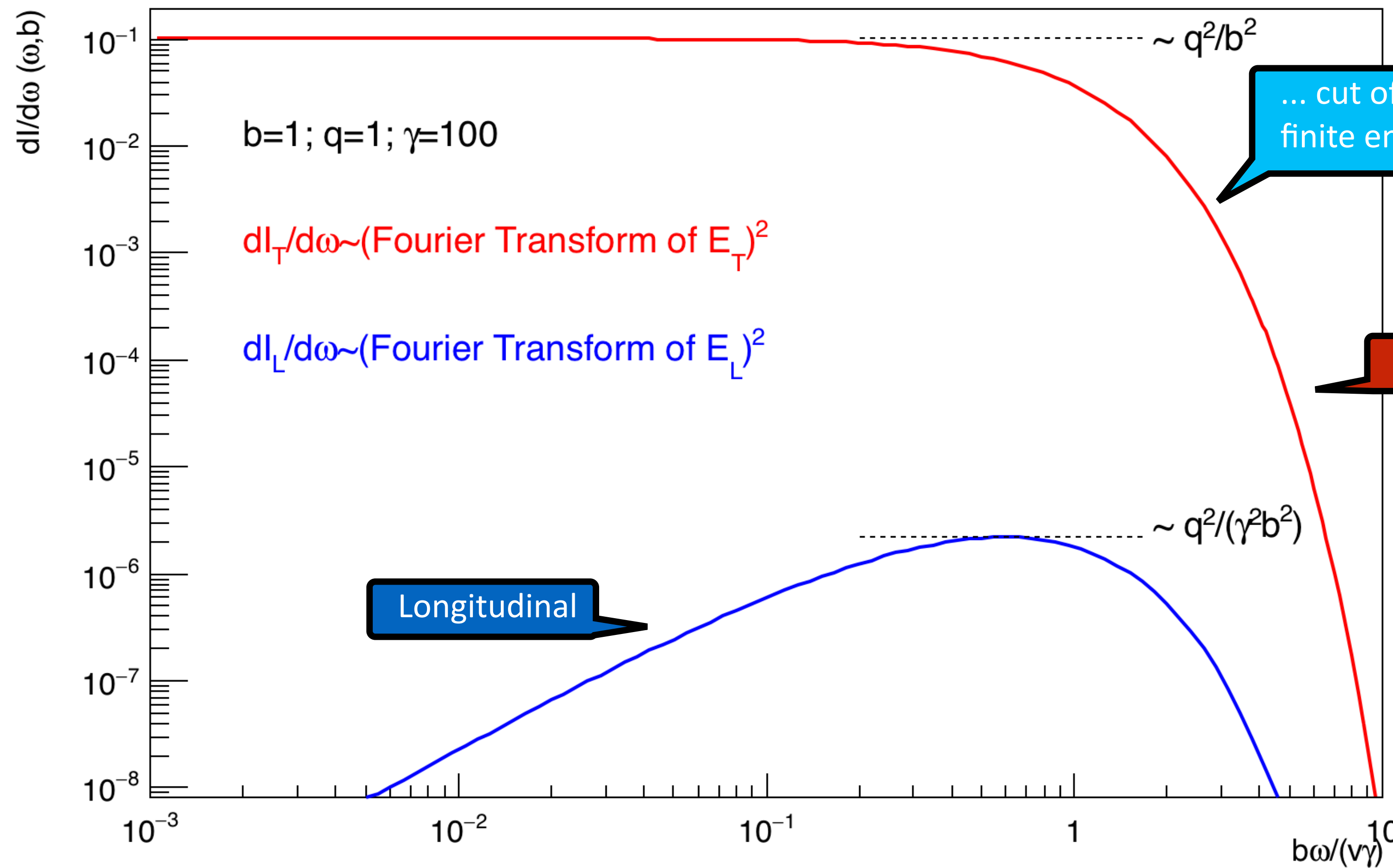
Longitudinal

frequency

The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space

Flat behaviour due to the Dirac-delta-like shape of the field



... cut off at large frequencies due to the finite energy (the pulse is not a Dirac delta)

This intensity is interpreted as the number of photons with a given energy and at a given transverse distance from the charge.

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

The photon flux: a bit more general approach

The number of photons
(known as the photon flux)

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

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Energy of photon

The photon flux: a bit more general approach

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Energy of photon

Distance from the centre
of the charged particle

The photon flux: a bit more general approach

The number of photons
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Particle charge

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

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Energy of photon

boost

Distance from the centre
of the charged particle

The photon flux: a bit more general approach

The number of photons
(known as the photon flux)

Particle charge

Form factor

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2) J_1(x_\perp k_\perp)}{k_\perp^2 + (k/\gamma)^2} \right|^2$$

Energy of photon

boost

Distance from the centre
of the charged particle

The photon flux: a bit more general approach

Point charge

The number of photons
(known as the photon flux)

Particle charge

Form factor

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2) J_1(x_\perp k_\perp)}{k_\perp^2 + (k/\gamma)^2} \right|^2$$

Energy of photon

boost

Distance from the centre
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The photon flux: a bit more general approach

The number of photons (known as the photon flux)

Particle charge

Point charge

Form factor

Fourier-Bessel transform of a Woods-Saxon distribution

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

Energy of photon

Distance from the centre of the charged particle

boost

The photon flux: a bit more general approach

STARlight <https://inspirehep.net/literature/1475495>

STARlight: convolution of a Yukawa potential and a hard sphere

Point charge

Fourier-Bessel transform of a Woods-Saxon distribution

The number of photons
(known as the photon flux)

Particle charge

Form factor

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

Energy of photon

boost

Distance from the centre
of the charged particle

Form factor of a point charge

Form factor

$$F_{pc}(q) = 1$$

Integral can be done analytically

$$n_{pc}(k, \vec{x}_{\perp}) = \frac{Z^2 \alpha_{\text{QED}} k}{\pi^2 \gamma^2} K_1^2(k x_{\perp} / \gamma)$$

Other form factors

Used in STARlight

$$F_{hsY}(q) = \frac{4\pi d_0}{Aq^3} [\sin(qR_A) - qR_A \cos(qR_A)] \left(\frac{1}{1 + a^2q^2} \right)$$

Other form factors

Used in STARlight

$$F_{hsY}(q) = \frac{4\pi d_0}{Aq^3} [\sin(qR_A) - qR_A \cos(qR_A)] \left(\frac{1}{1 + a^2q^2} \right)$$

$$F_{WS}(q) = \frac{4\pi}{qA} \int \rho(r) \sin(rq) r dr$$

Woods-Saxon distribution

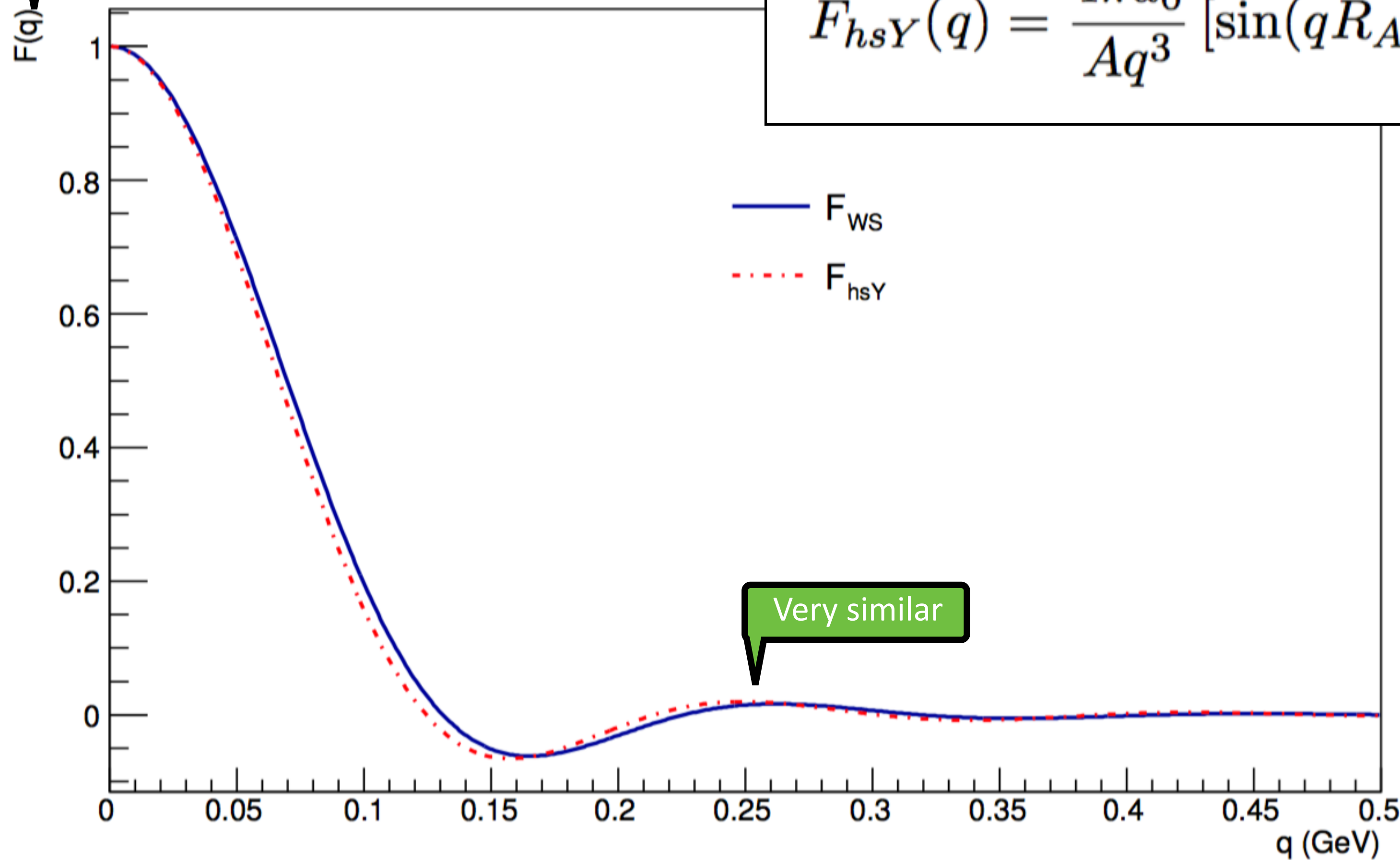
$$\rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-r_A}{z}\right)}$$

Other form factors

Form factor

Used in STARlight

$$F_{hsY}(q) = \frac{4\pi d_0}{Aq^3} [\sin(qR_A) - qR_A \cos(qR_A)] \left(\frac{1}{1 + a^2q^2} \right)$$



Very similar

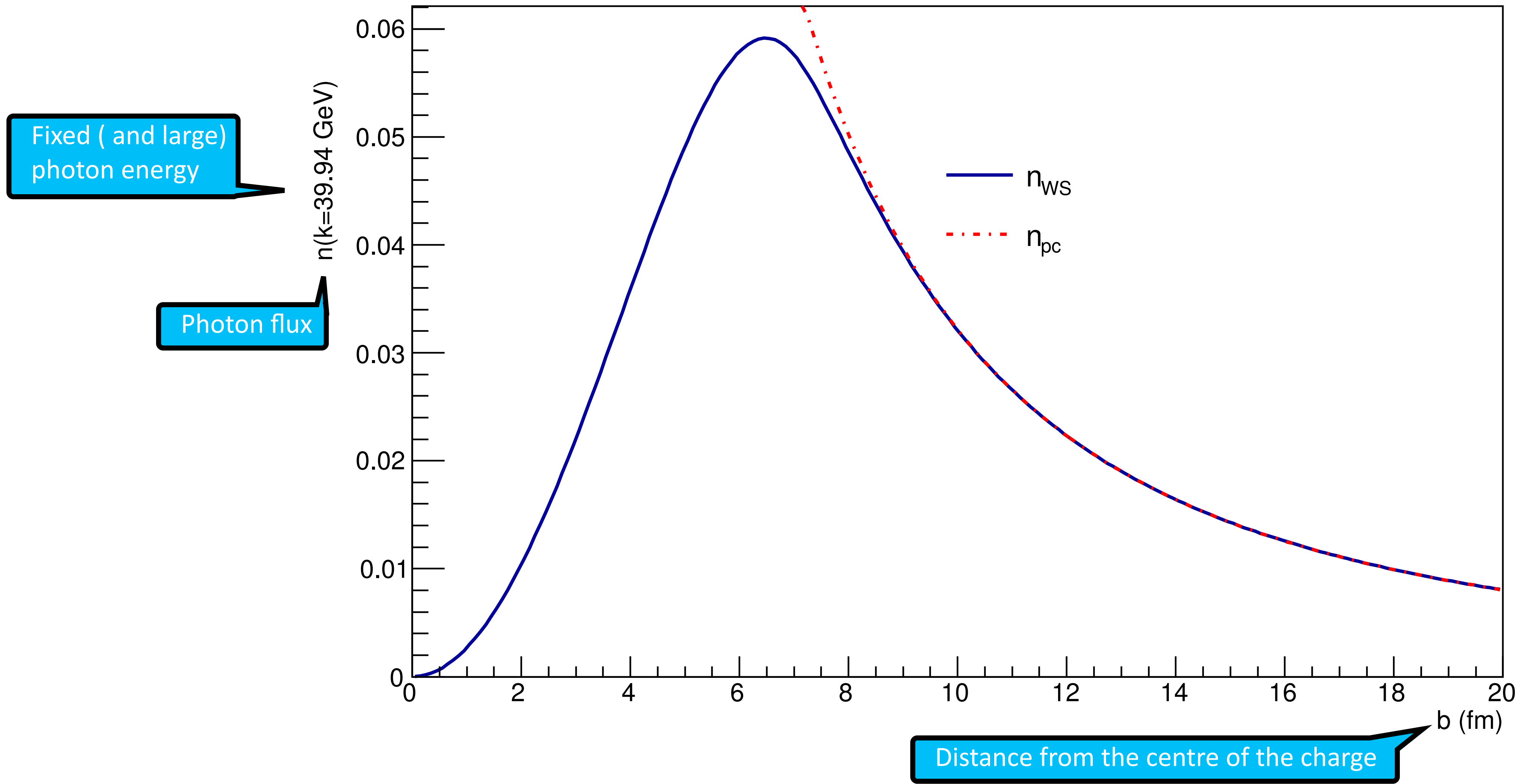
Magnitude of the transferred momentum

$$F_{WS}(q) = \frac{4\pi}{qA} \int \rho(r) \sin(rq) r dr$$

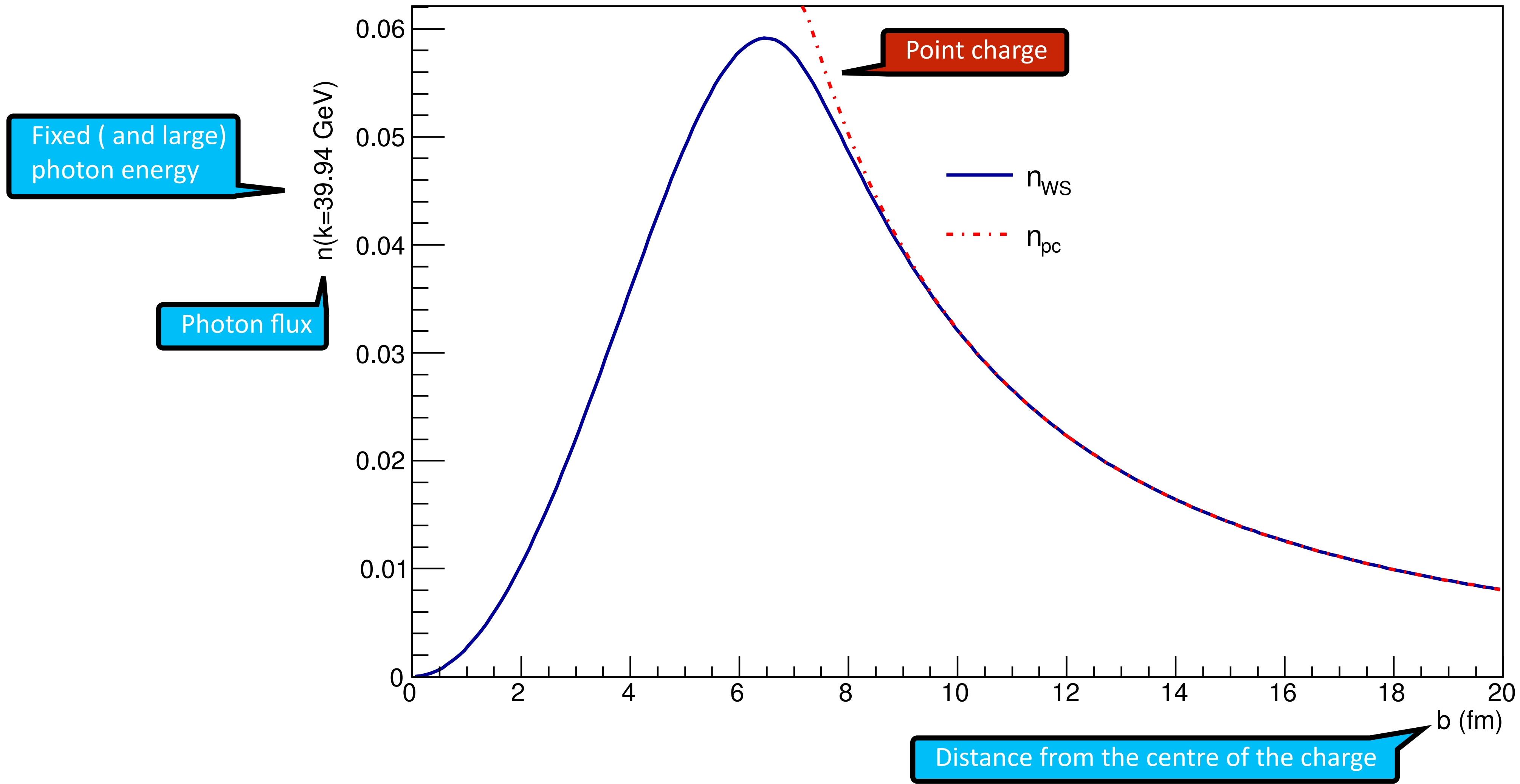
Woods-Saxon distribution

$$\rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-r_A}{z}\right)}$$

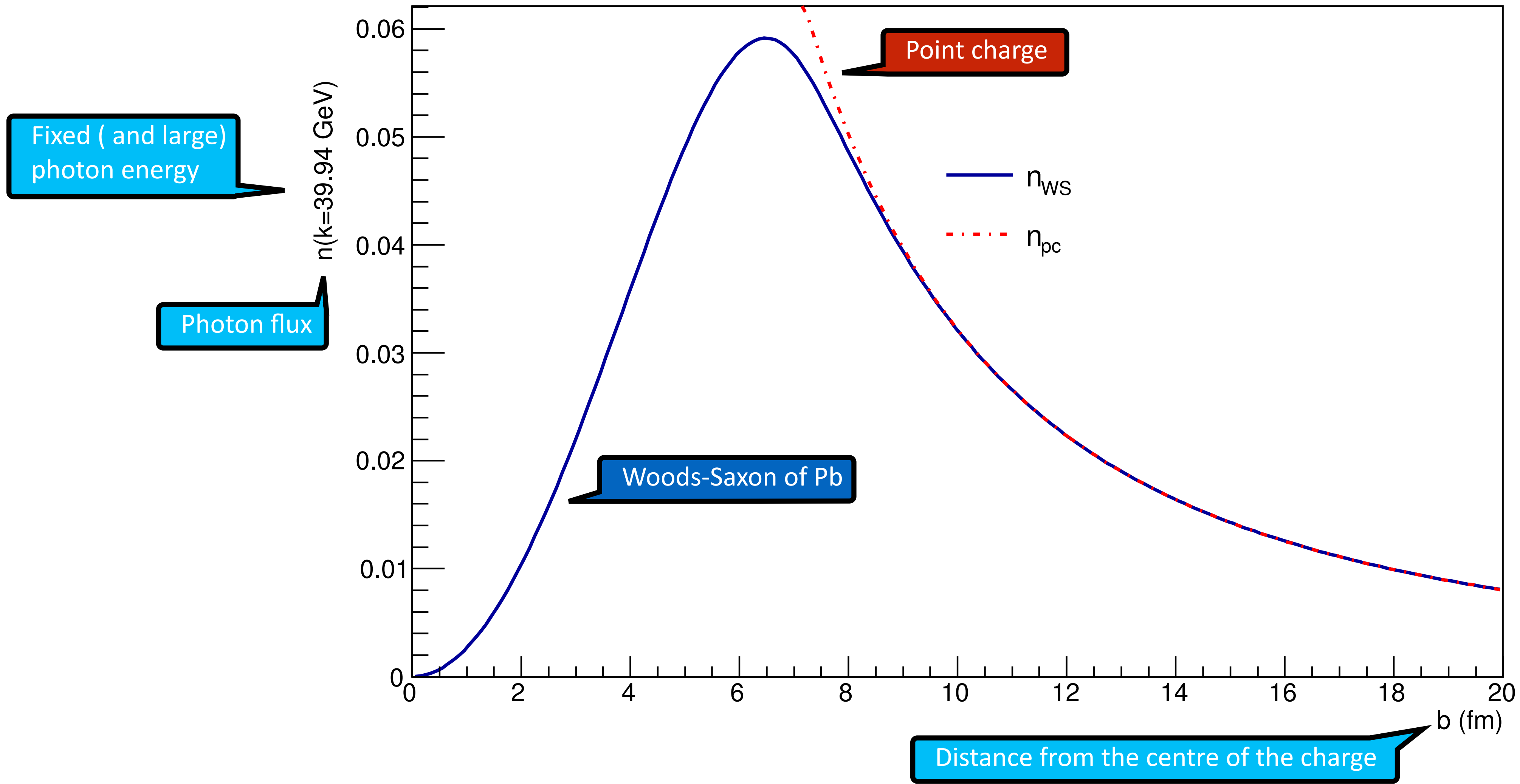
Comparing fluxes



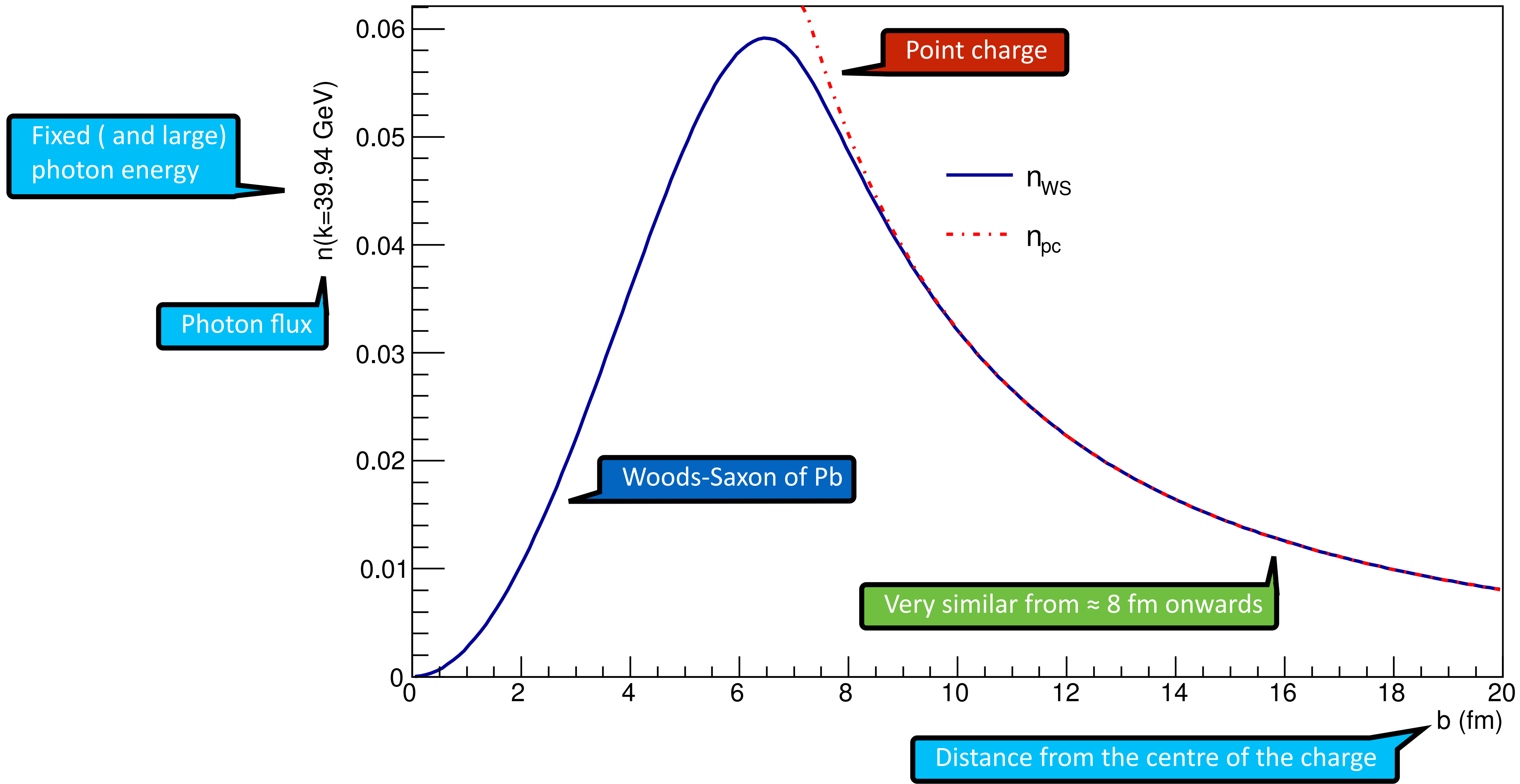
Comparing fluxes



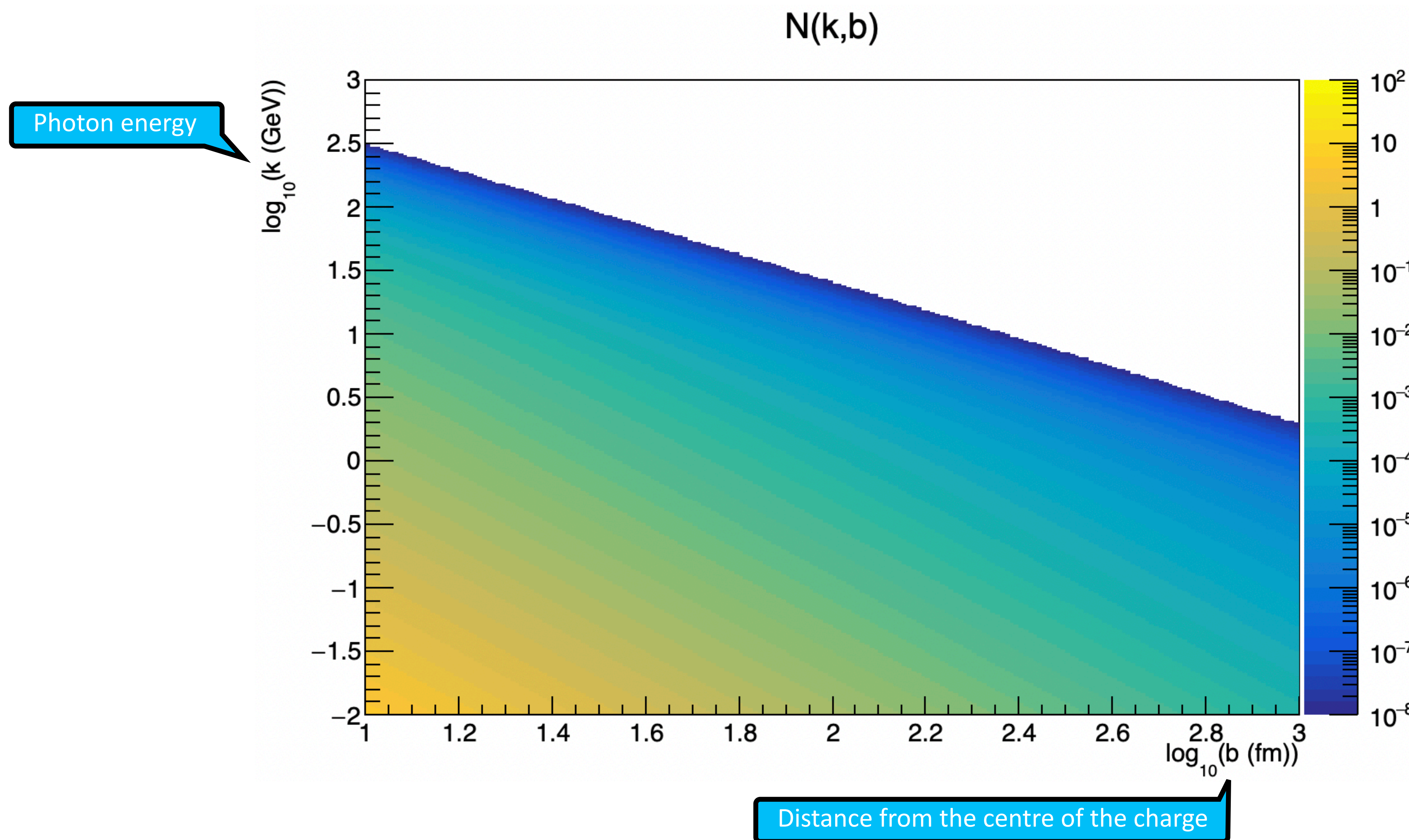
Comparing fluxes



Comparing fluxes



Photon flux of a point charge

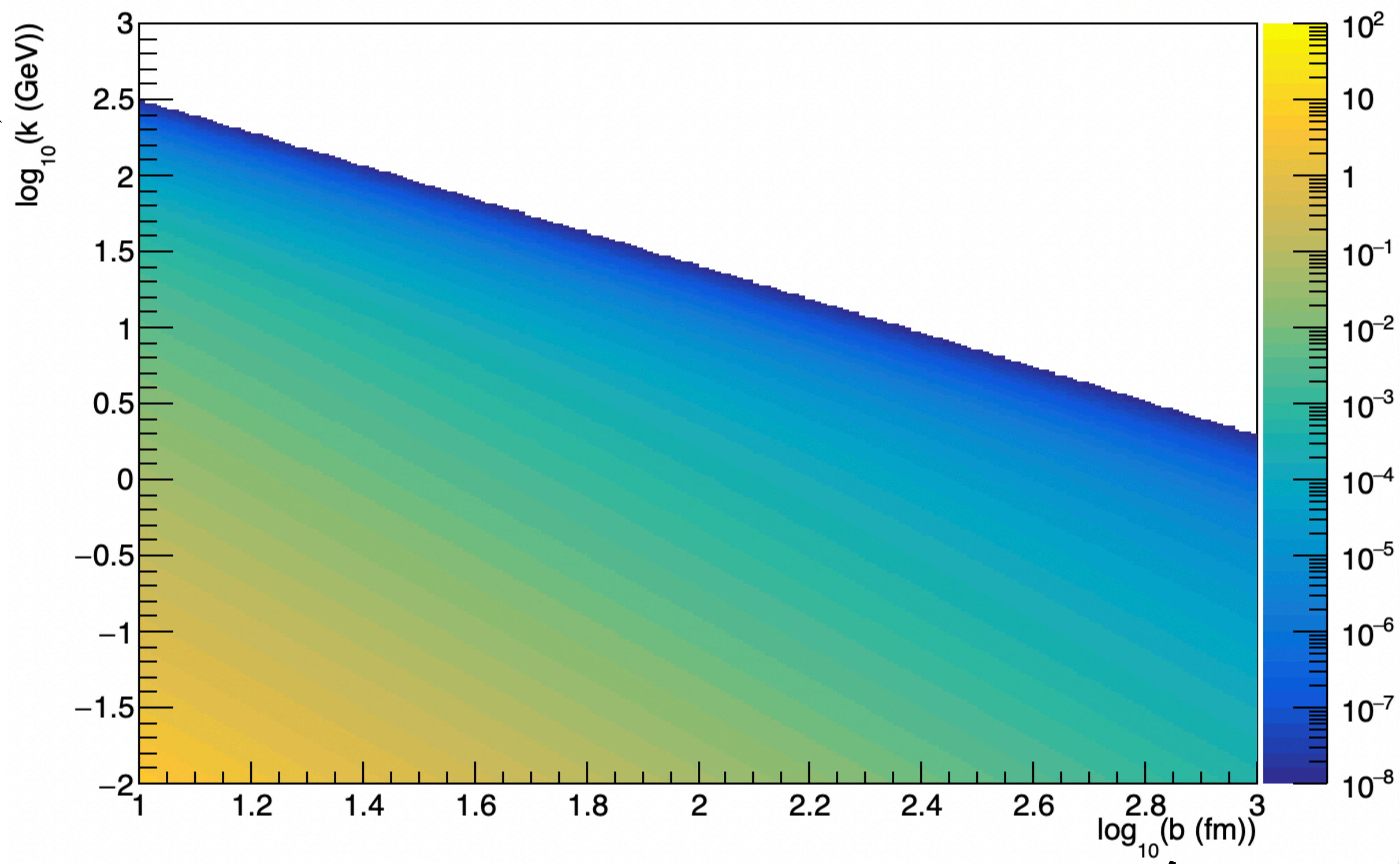


Photon flux of a point charge

Using LHC relevant parameters and ranges for k and b

$N(k,b)$

Photon energy



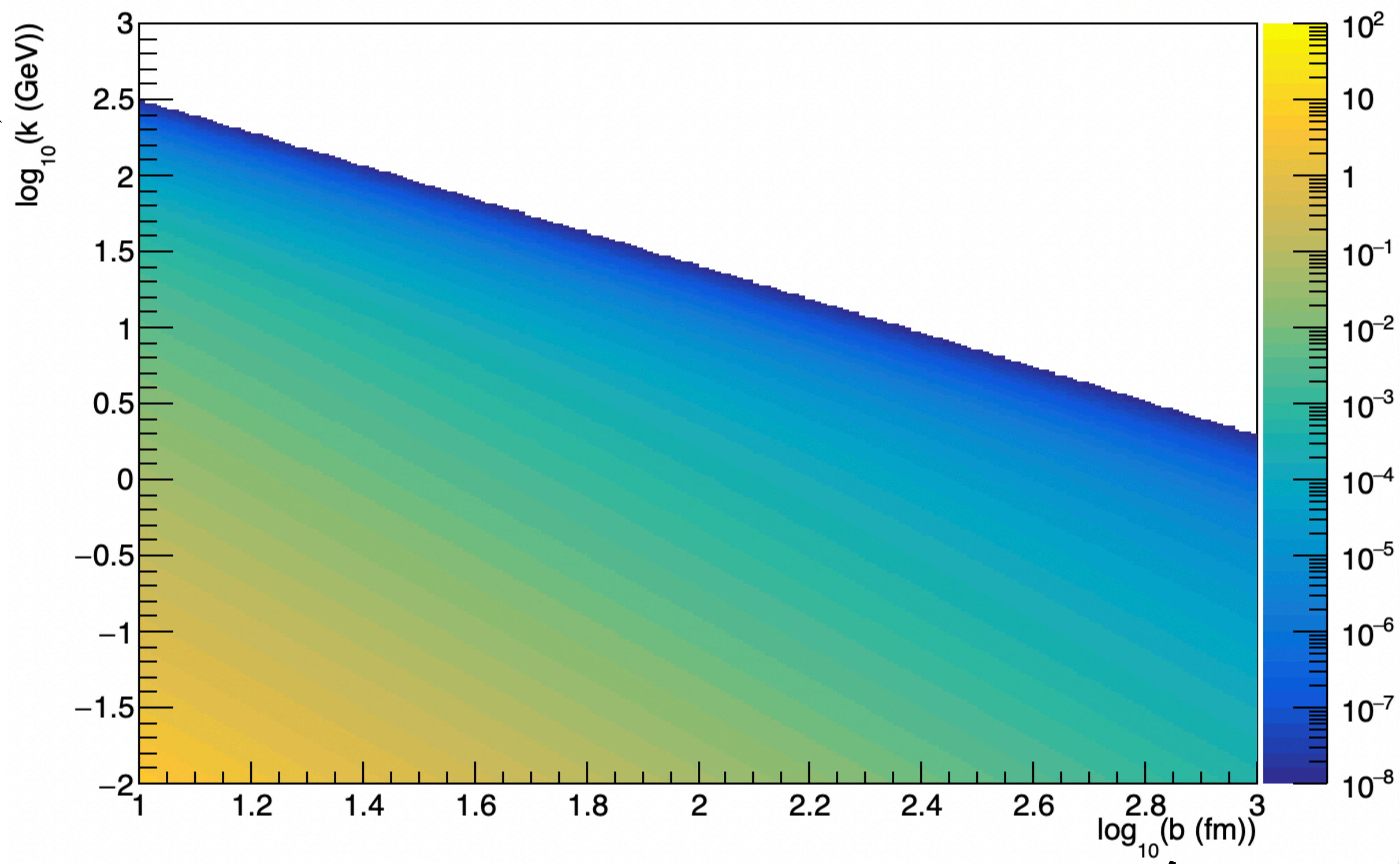
Distance from the centre of the charge

Photon flux of a point charge

Using LHC relevant parameters and ranges for k and b

$N(k,b)$

Photon energy



10 orders of magnitude

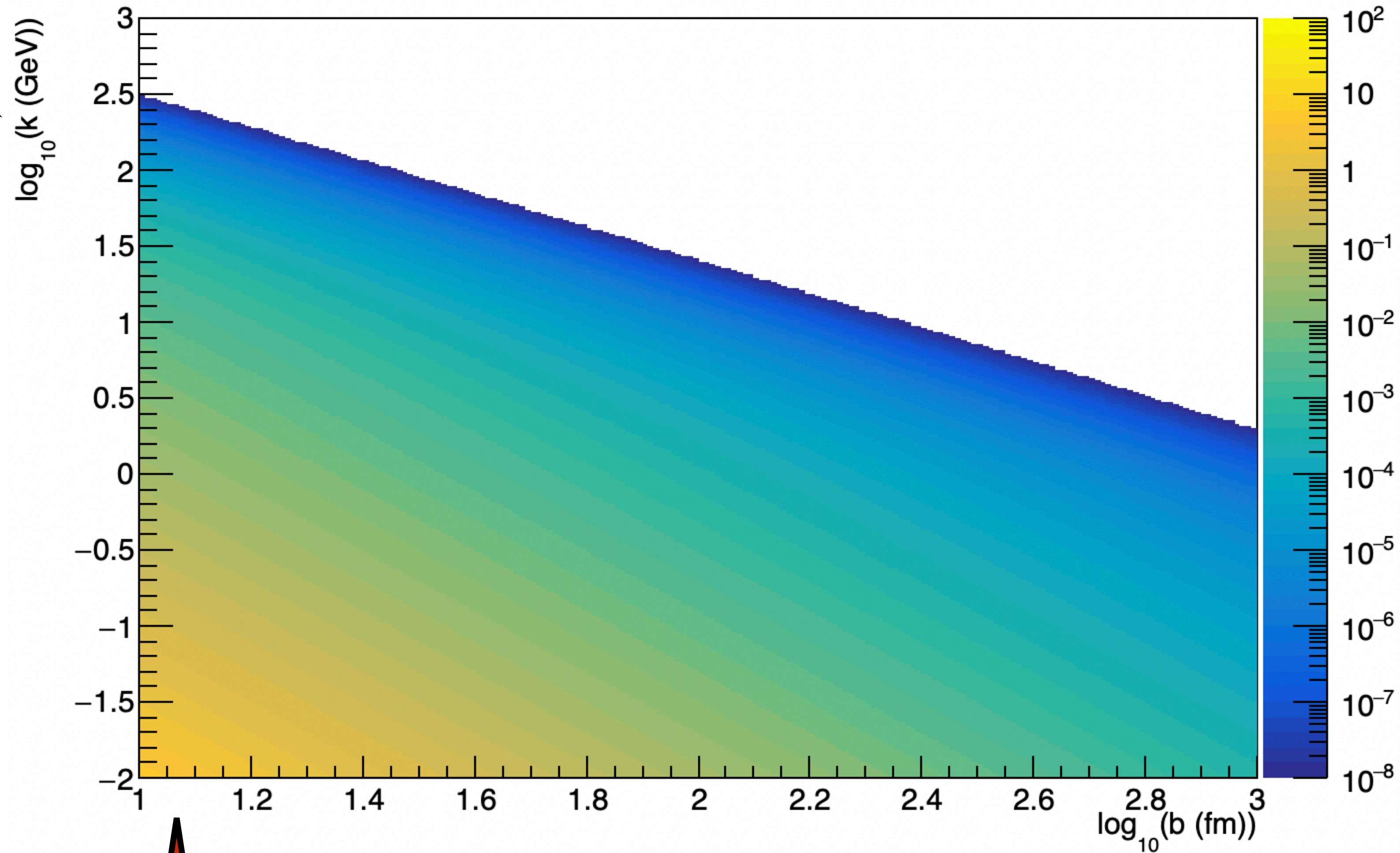
Distance from the centre of the charge

Photon flux of a point charge

Using LHC relevant parameters and ranges for k and b

$N(k,b)$

Photon energy



10 orders of magnitude

Large photon energies are more probable at small distances

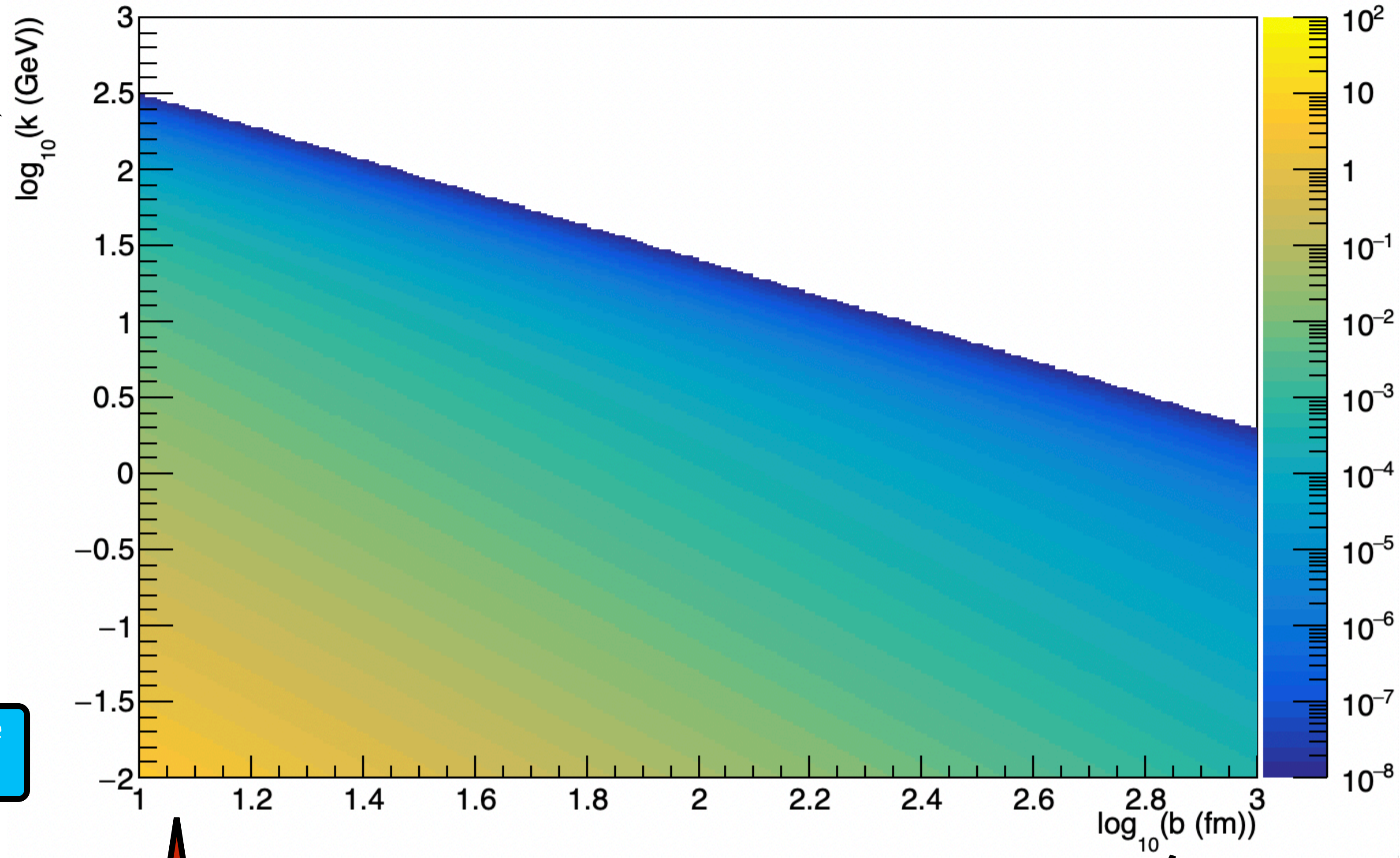
Distance from the centre of the charge

Photon flux of a point charge

Using LHC relevant parameters and ranges for k and b

$N(k,b)$

Photon energy



10 orders of magnitude

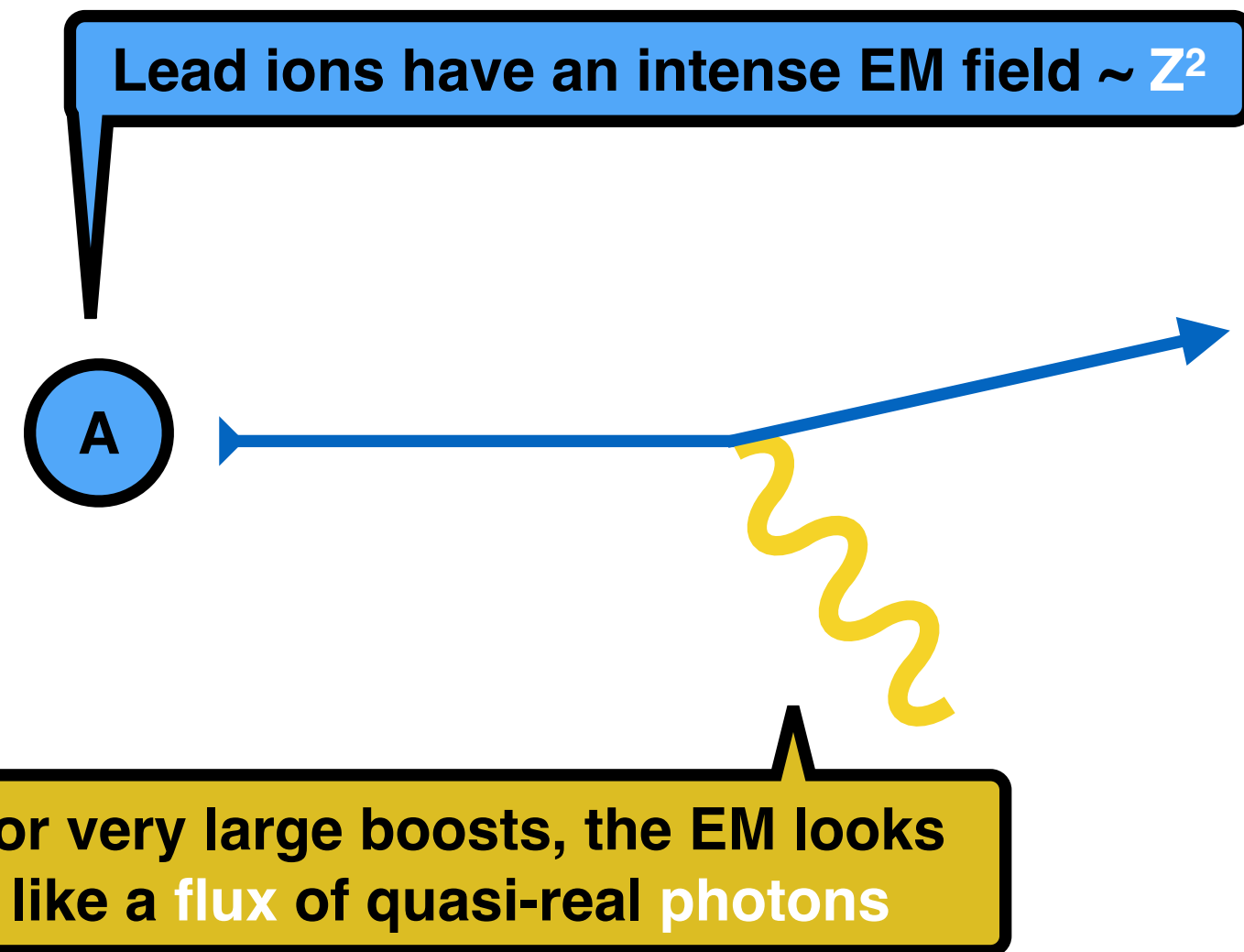
Different final states sample different parts of this plot

Large photon energies are more probable at small distances

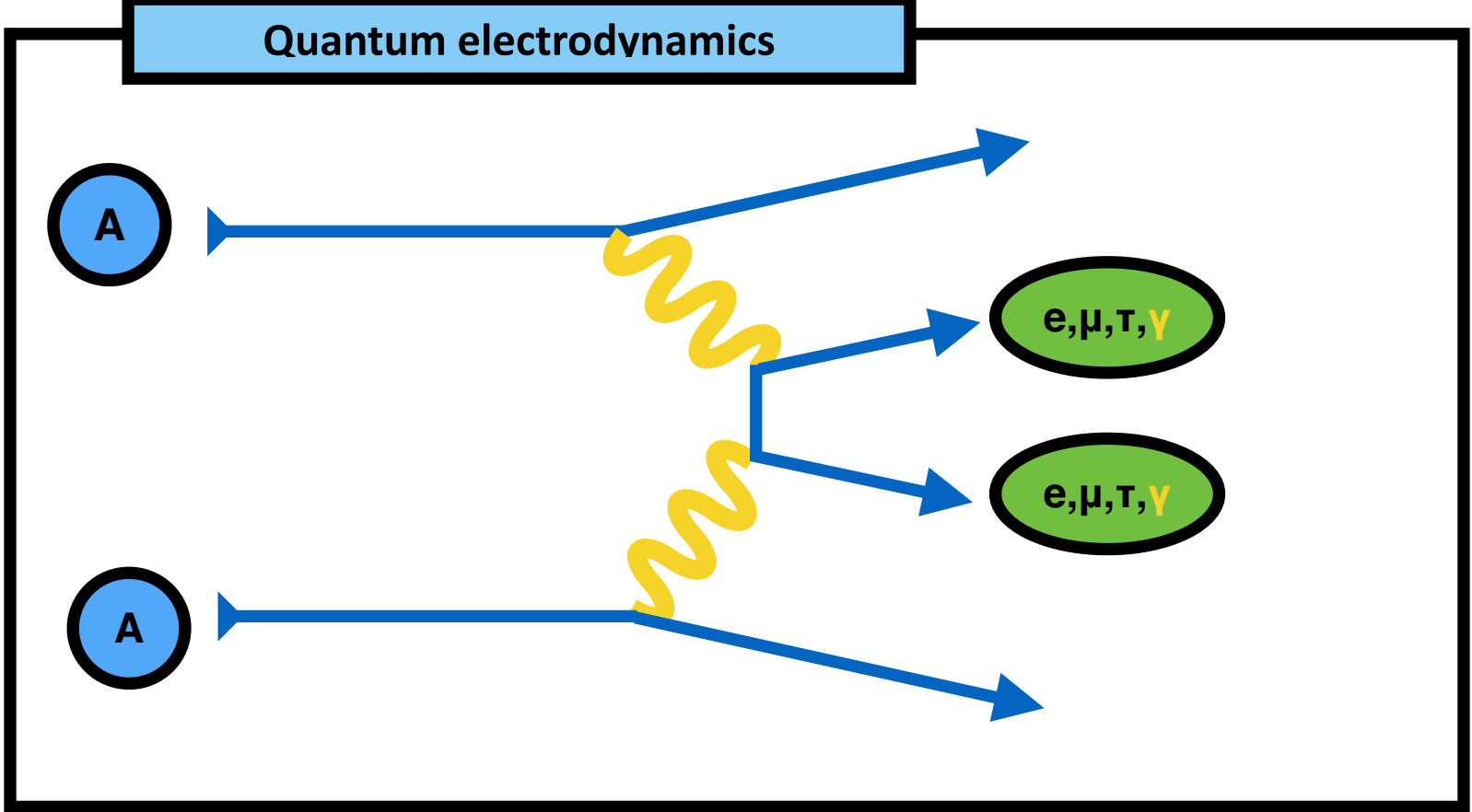
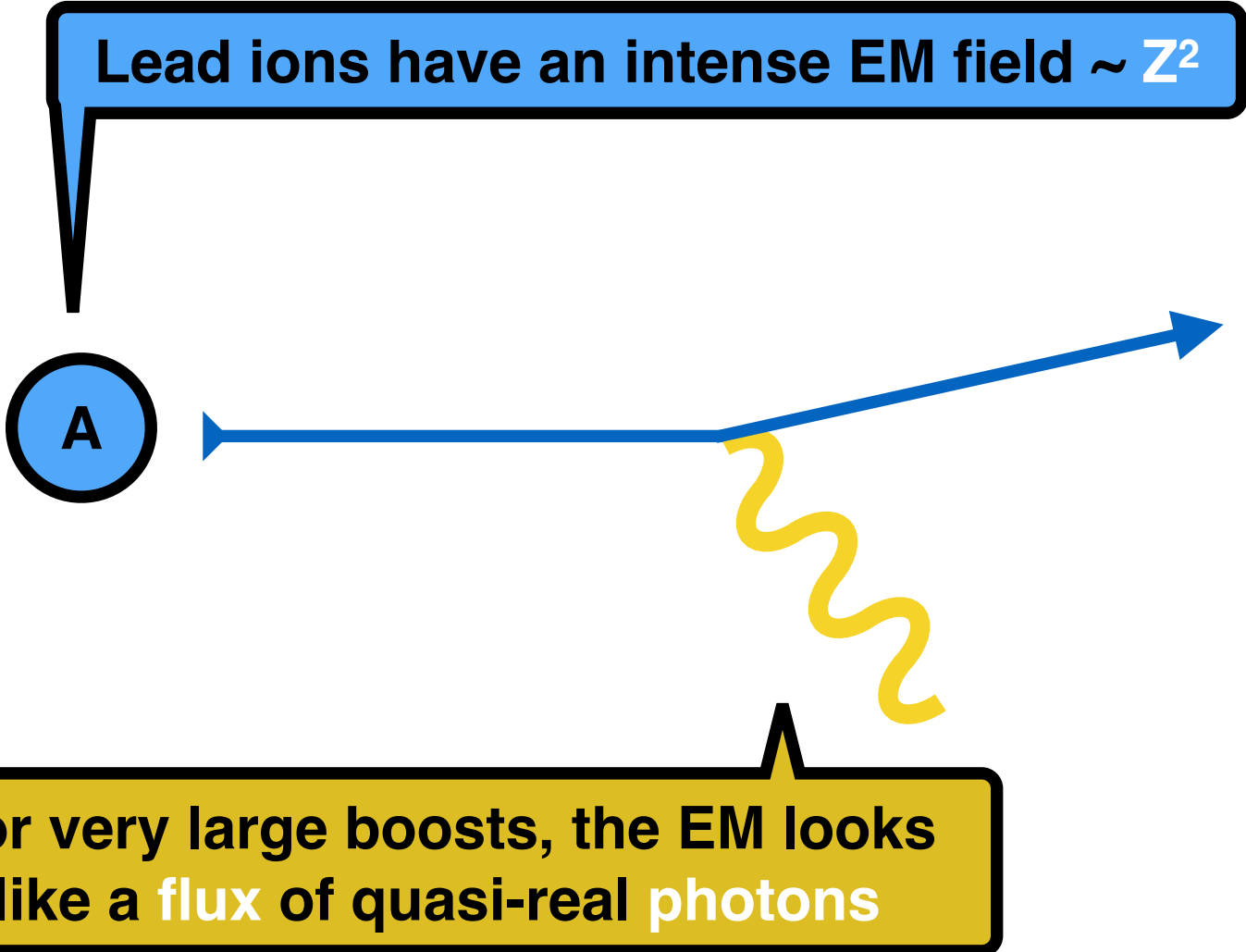
Distance from the centre of the charge

Now that we have the photons, what can we do with them?

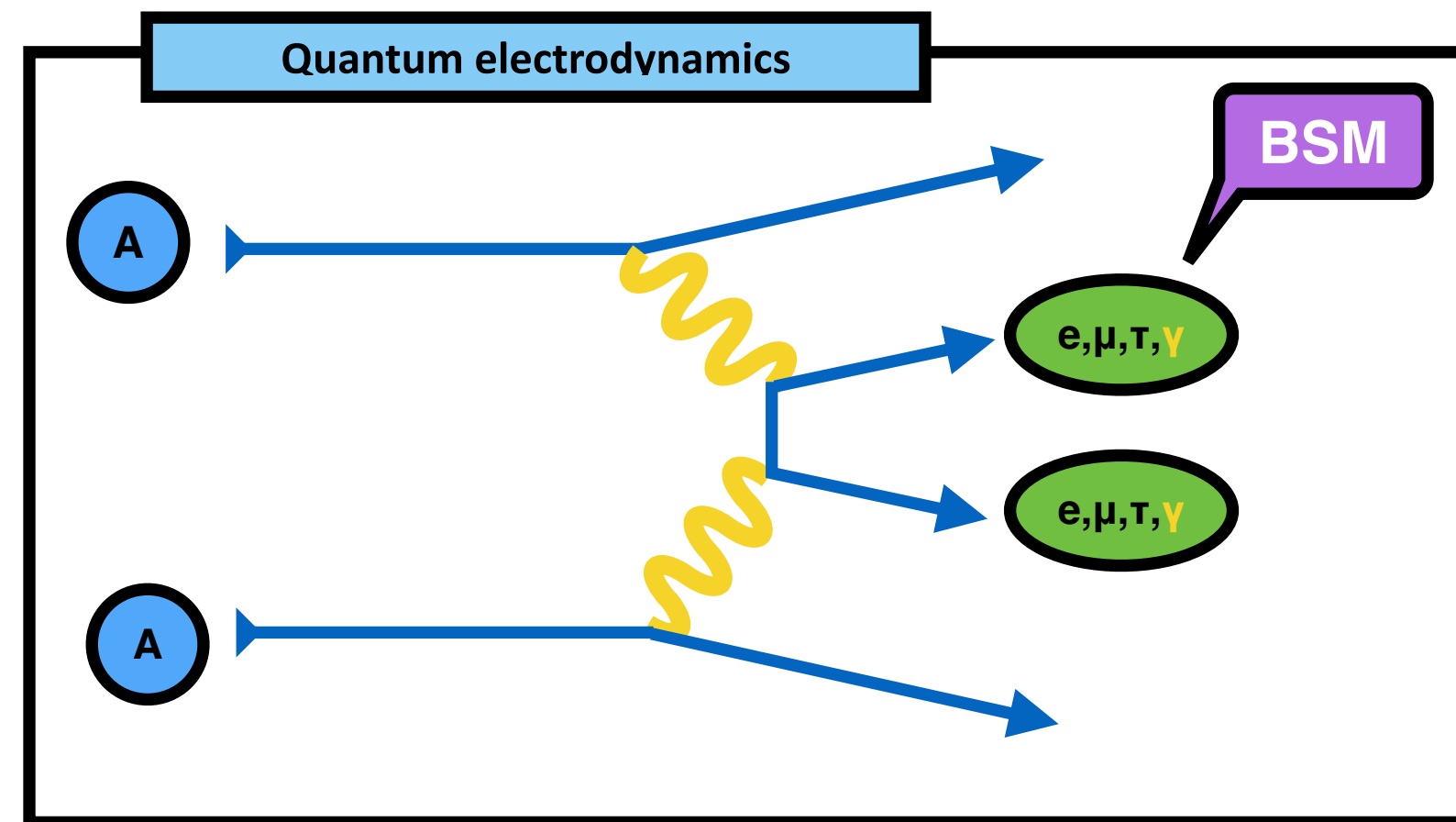
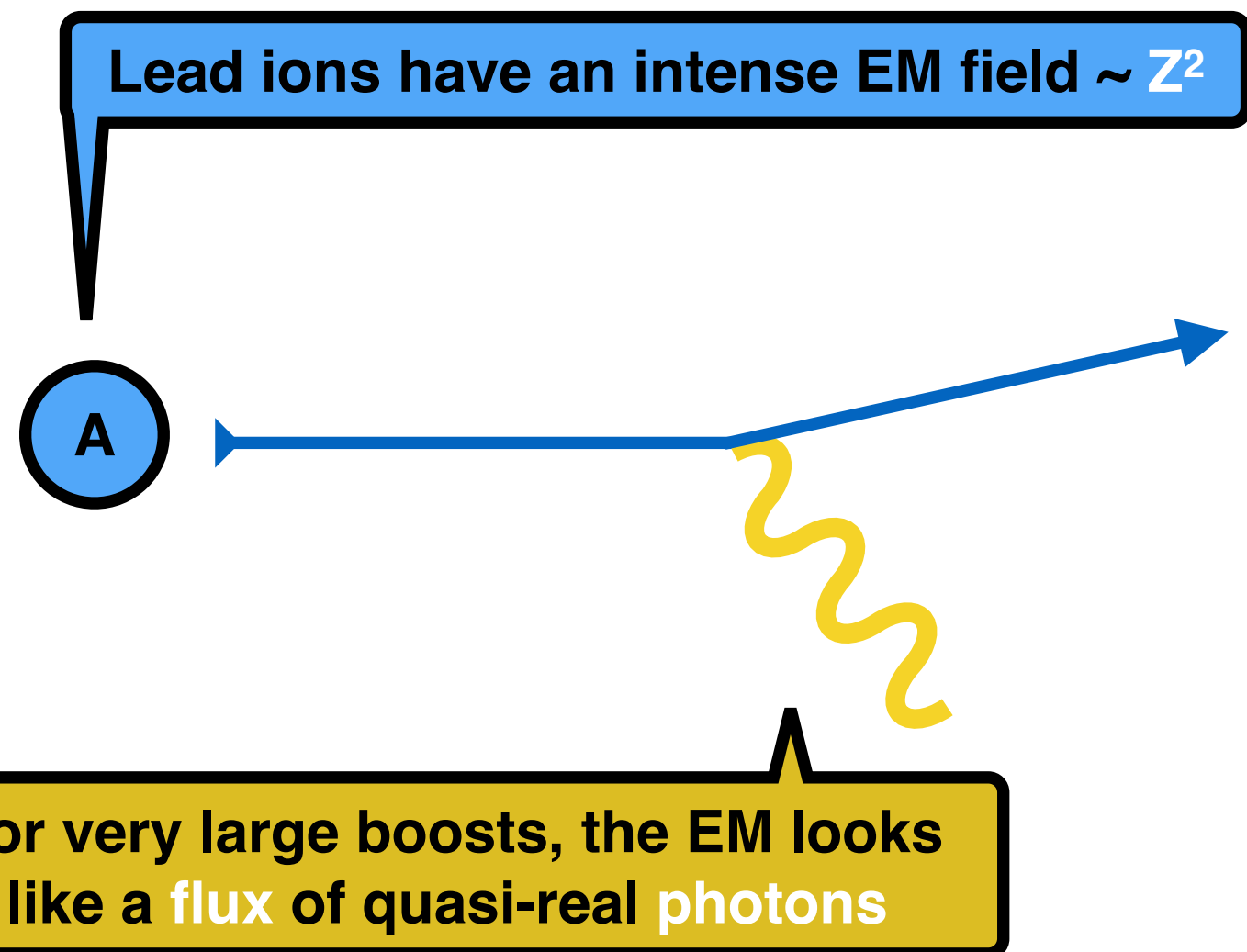
Photons at the ion colliders: examples of what can be done



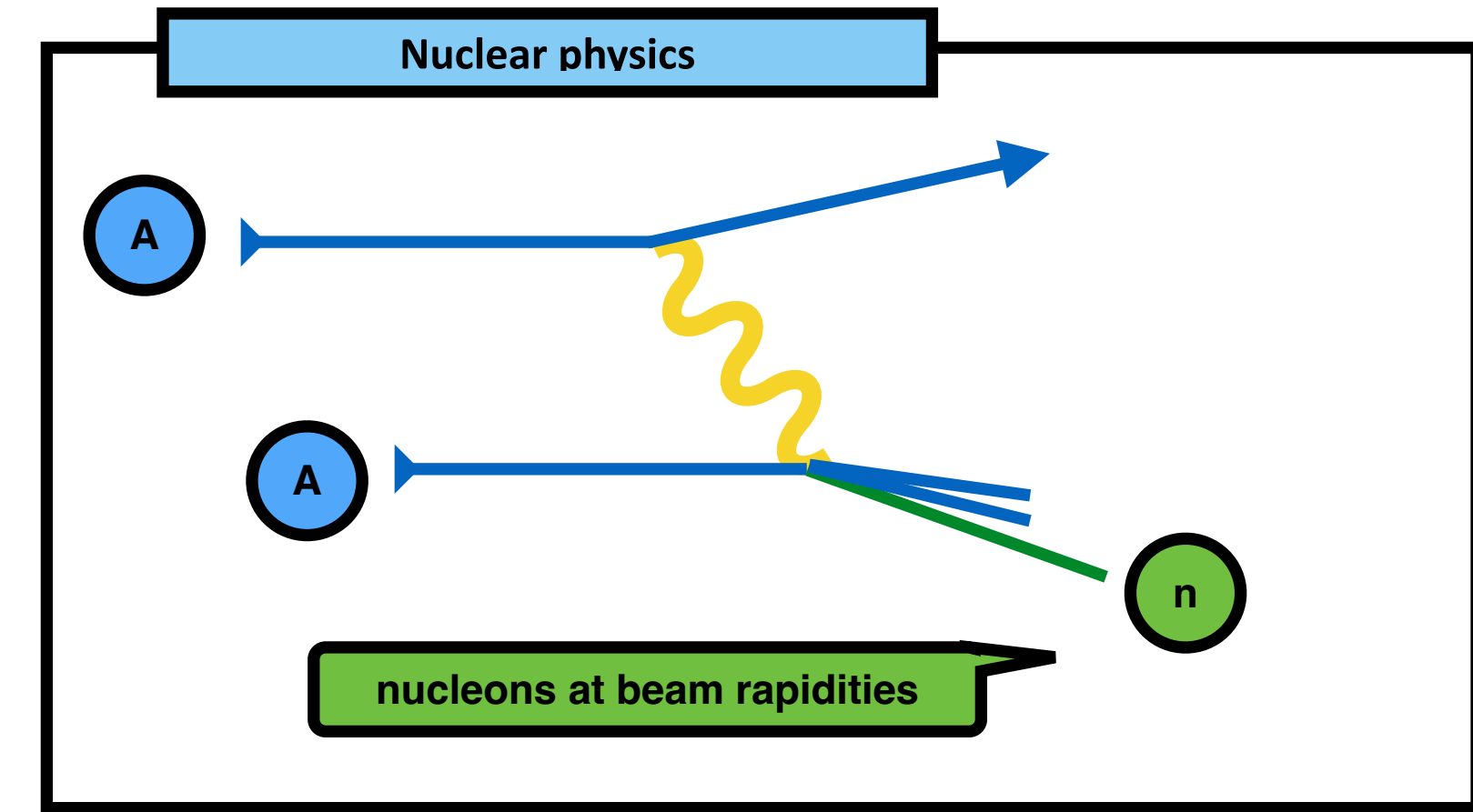
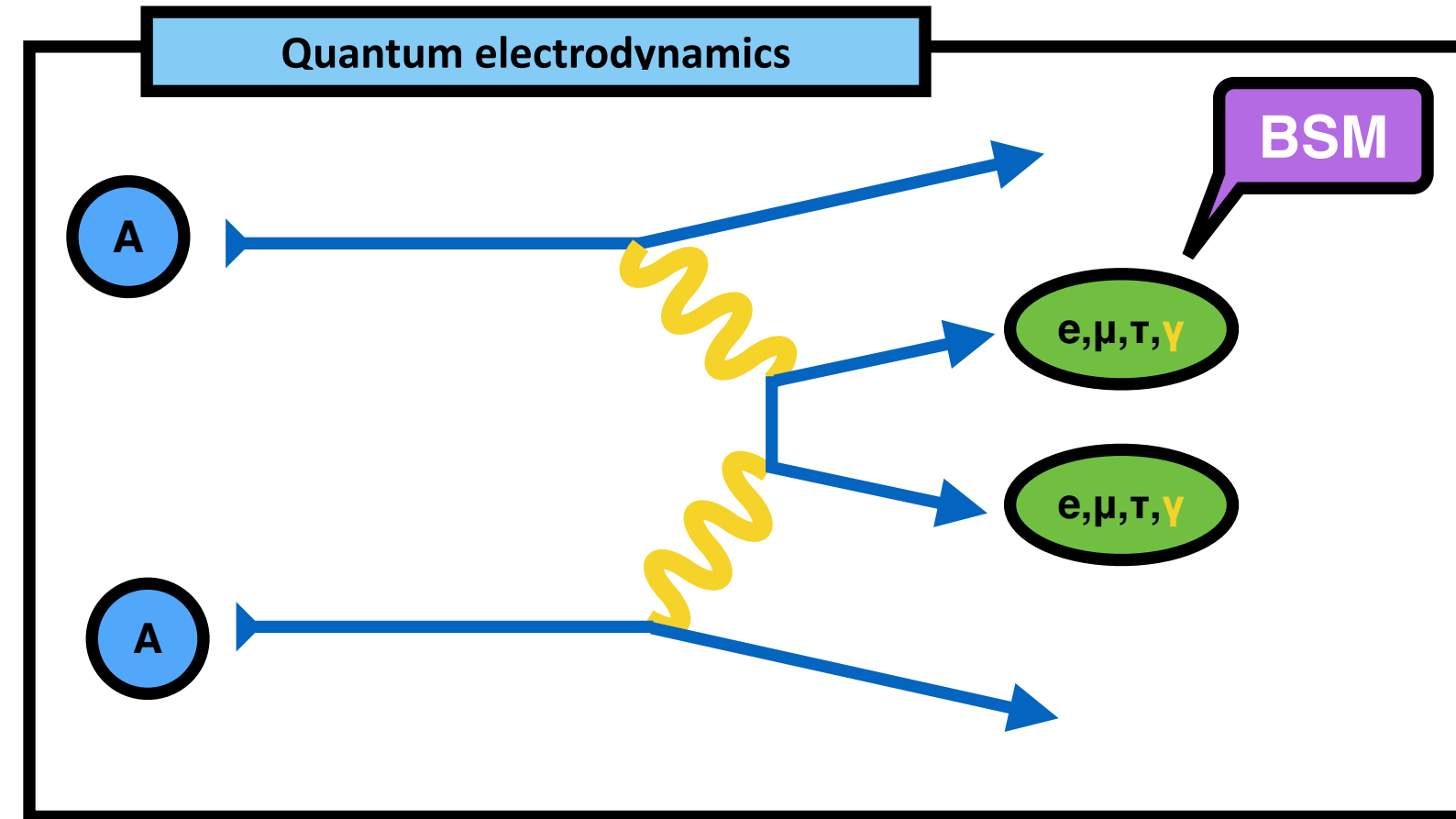
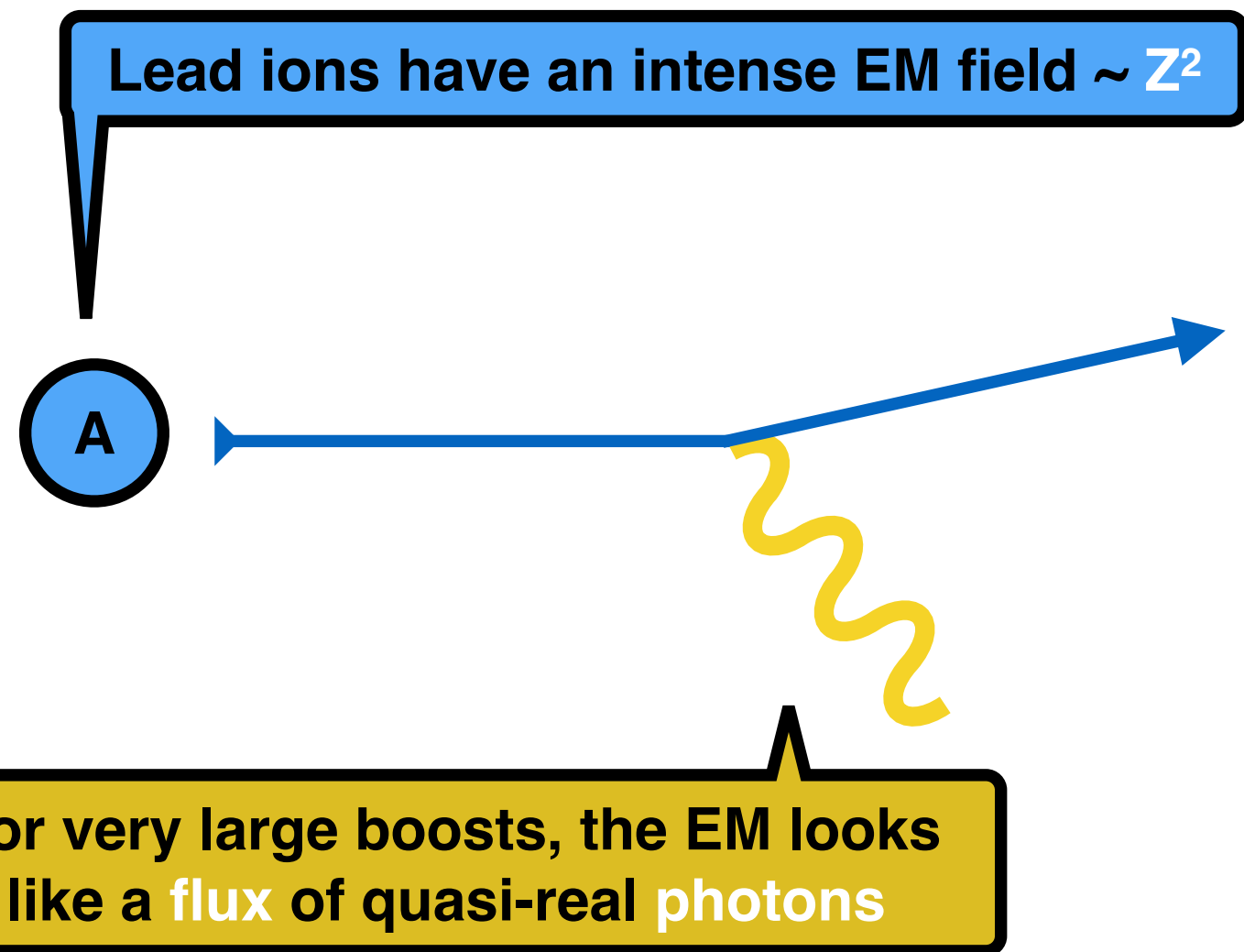
Photons at the ion colliders: examples of what can be done



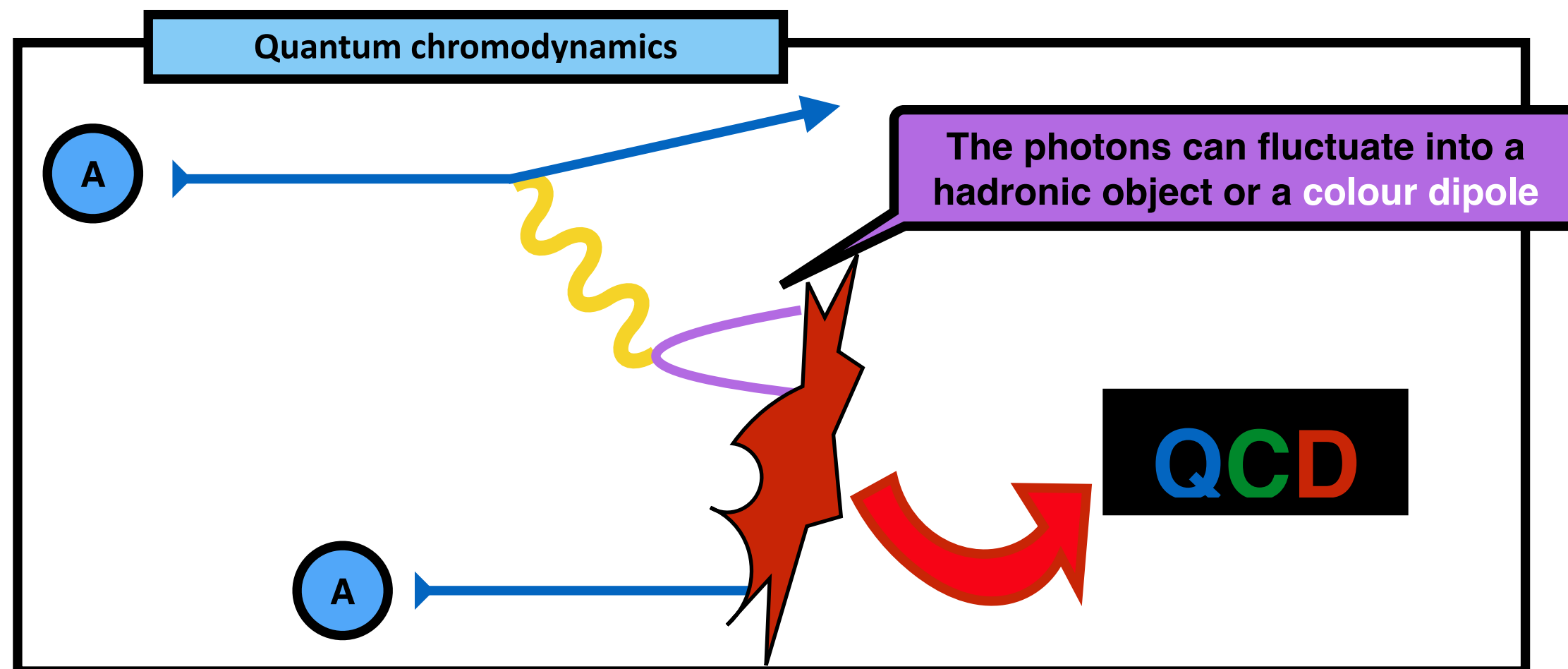
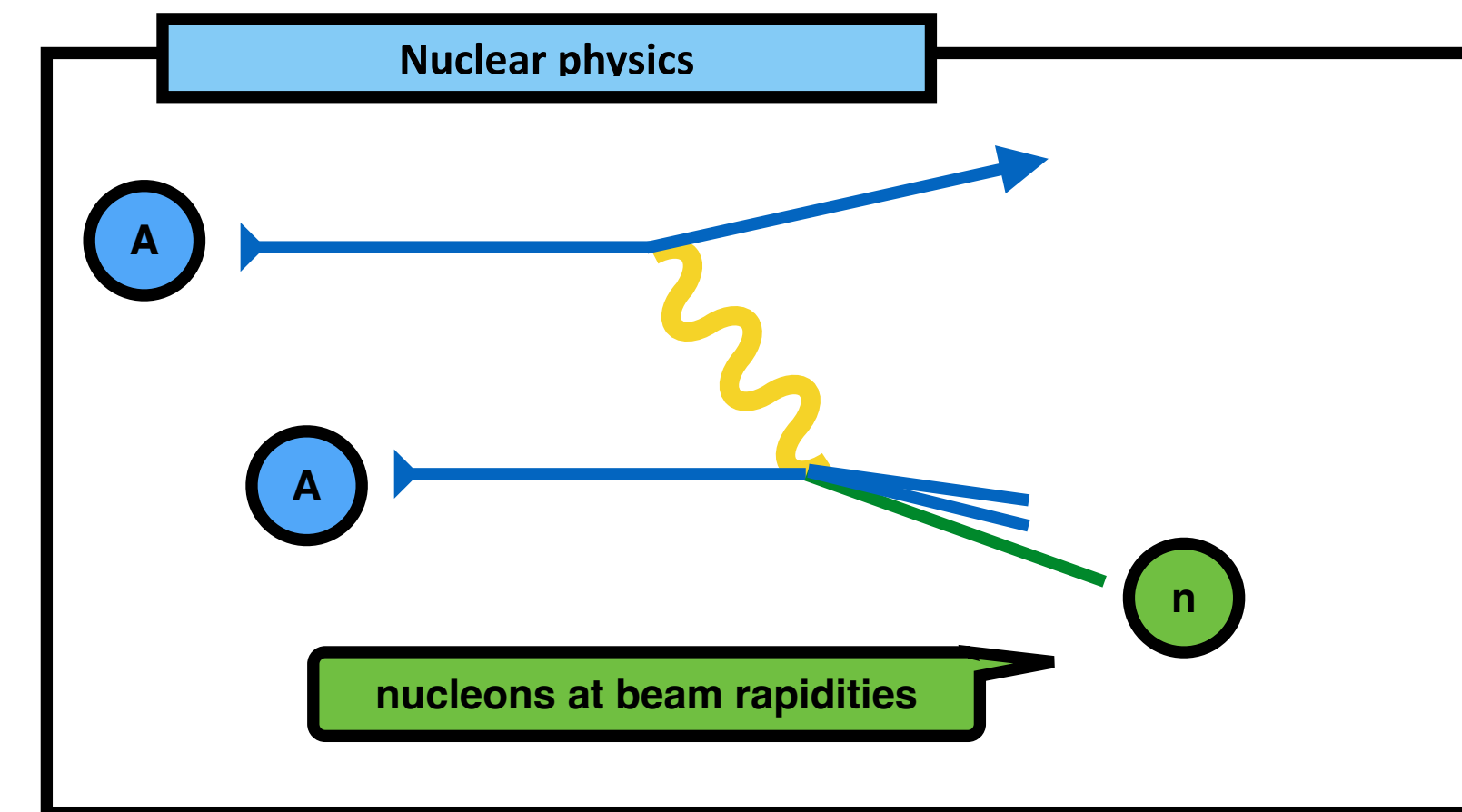
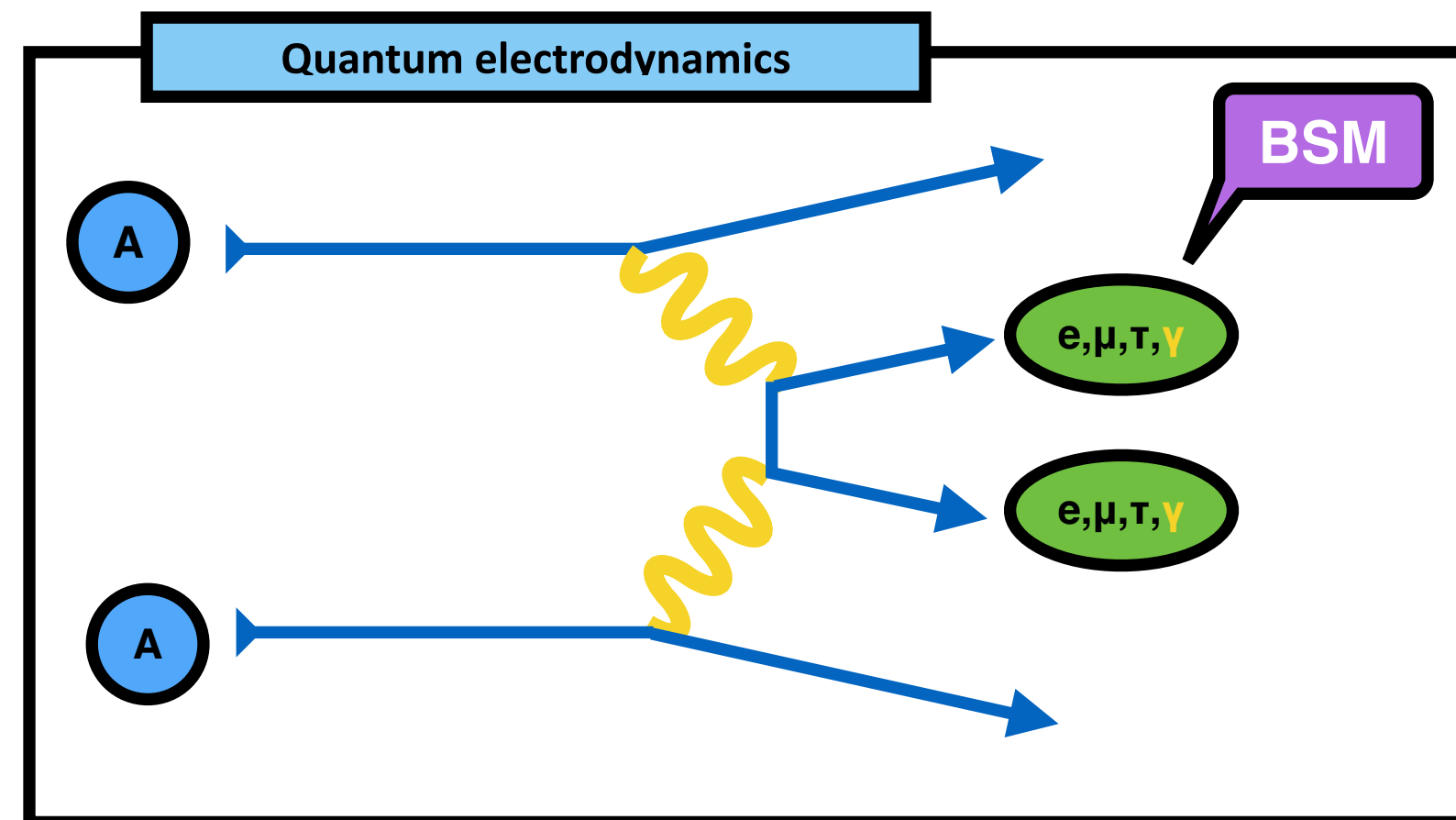
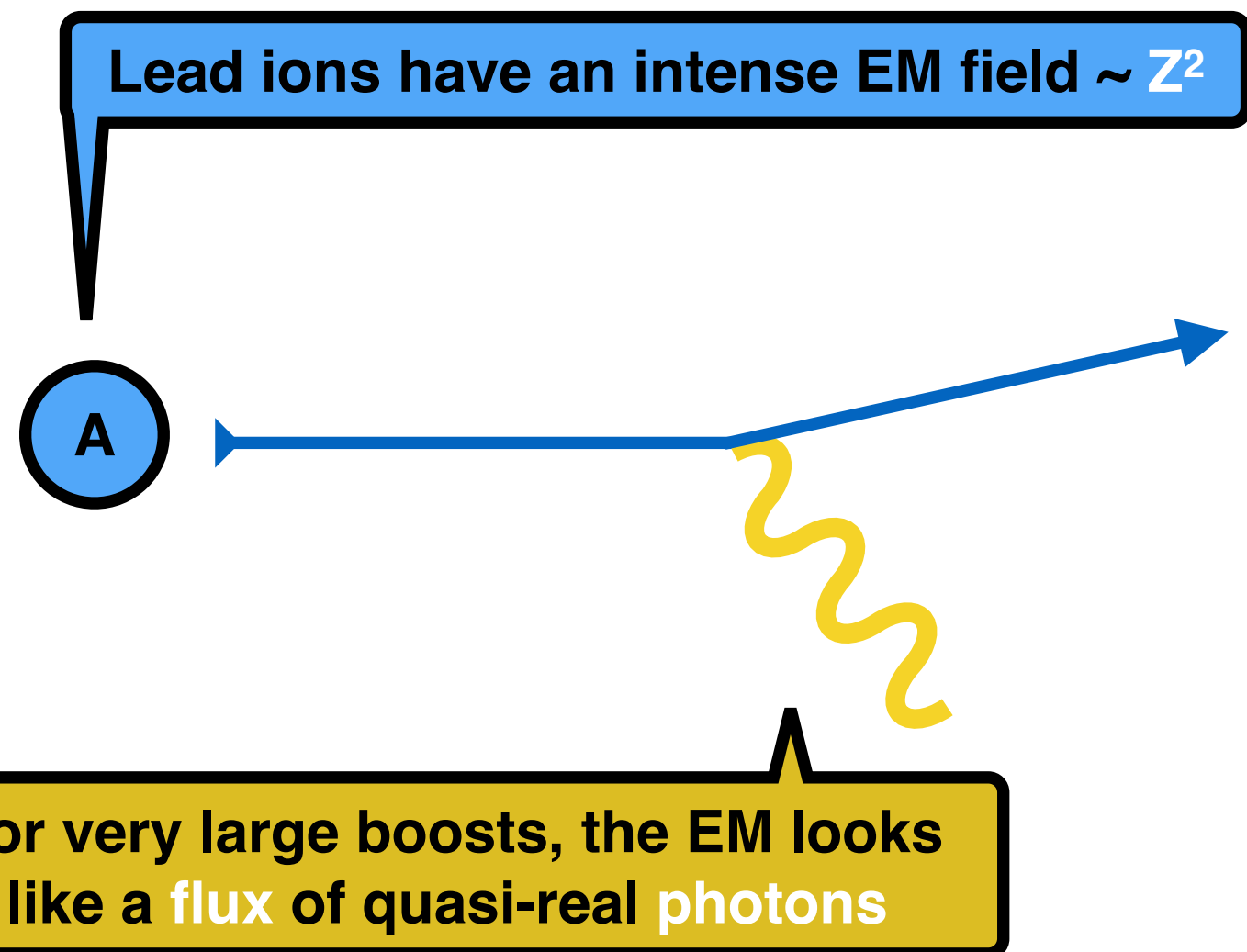
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Photons at the ion colliders: examples of what can be done

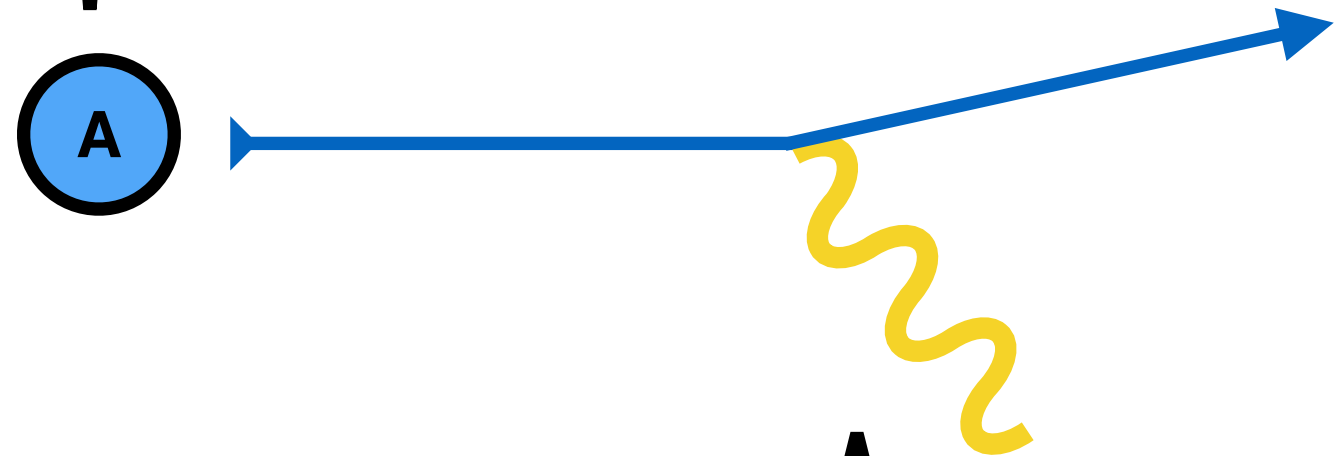


Photons at the ion colliders: examples of what can be done



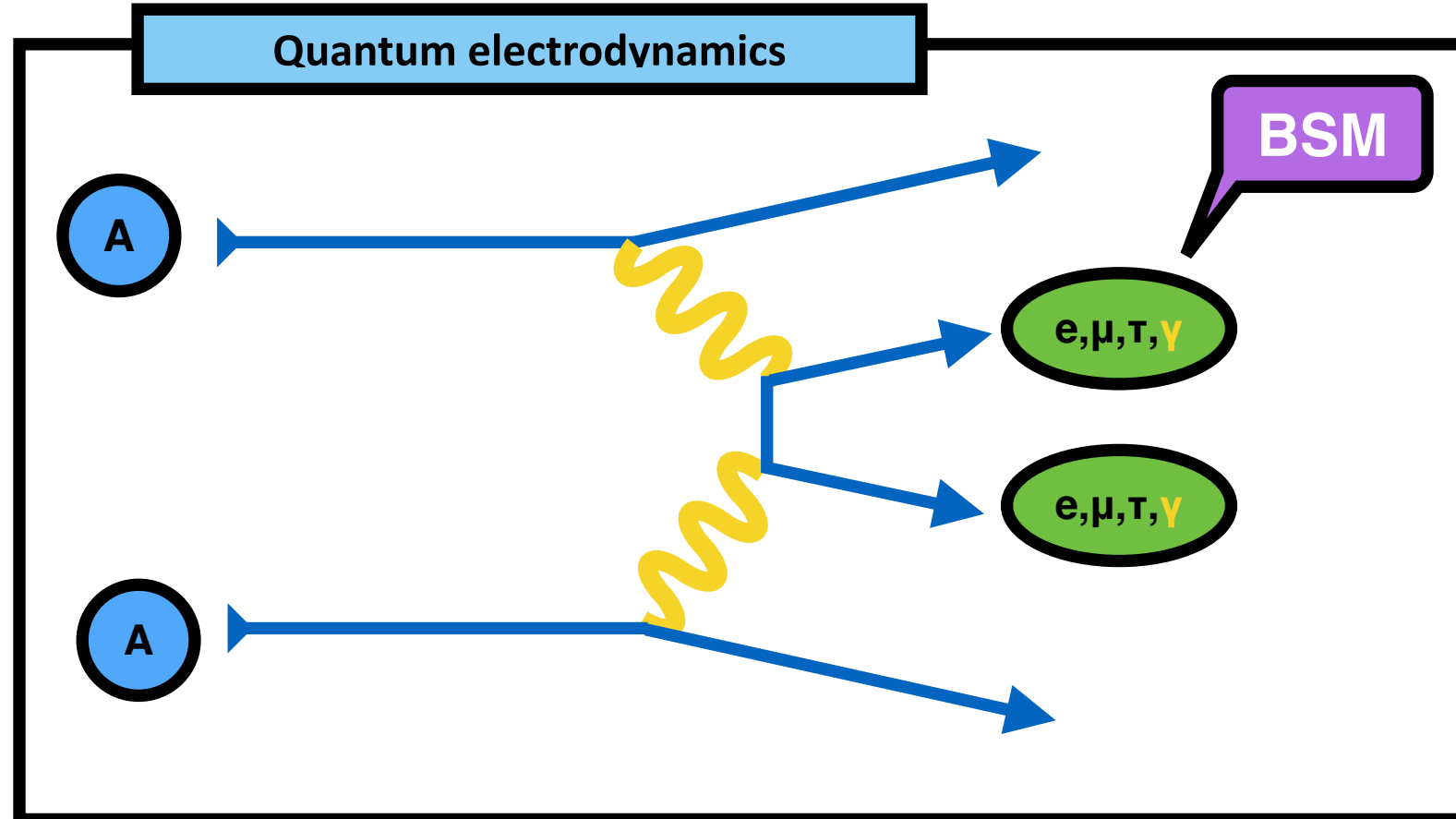
Photons at the ion colliders: examples of what can be done

Lead ions have an intense EM field $\sim Z^2$

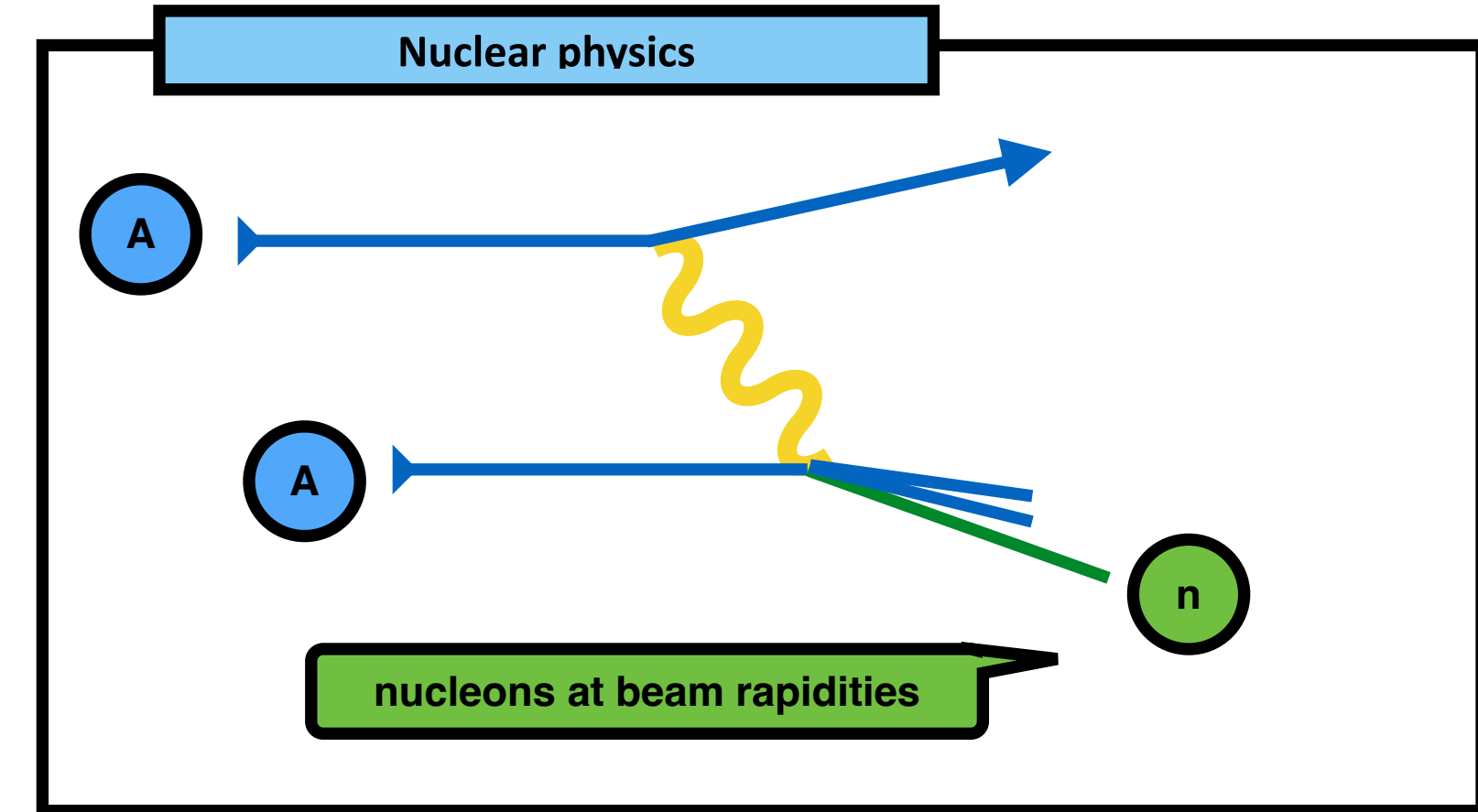


For very large boosts, the EM looks like a flux of quasi-real photons

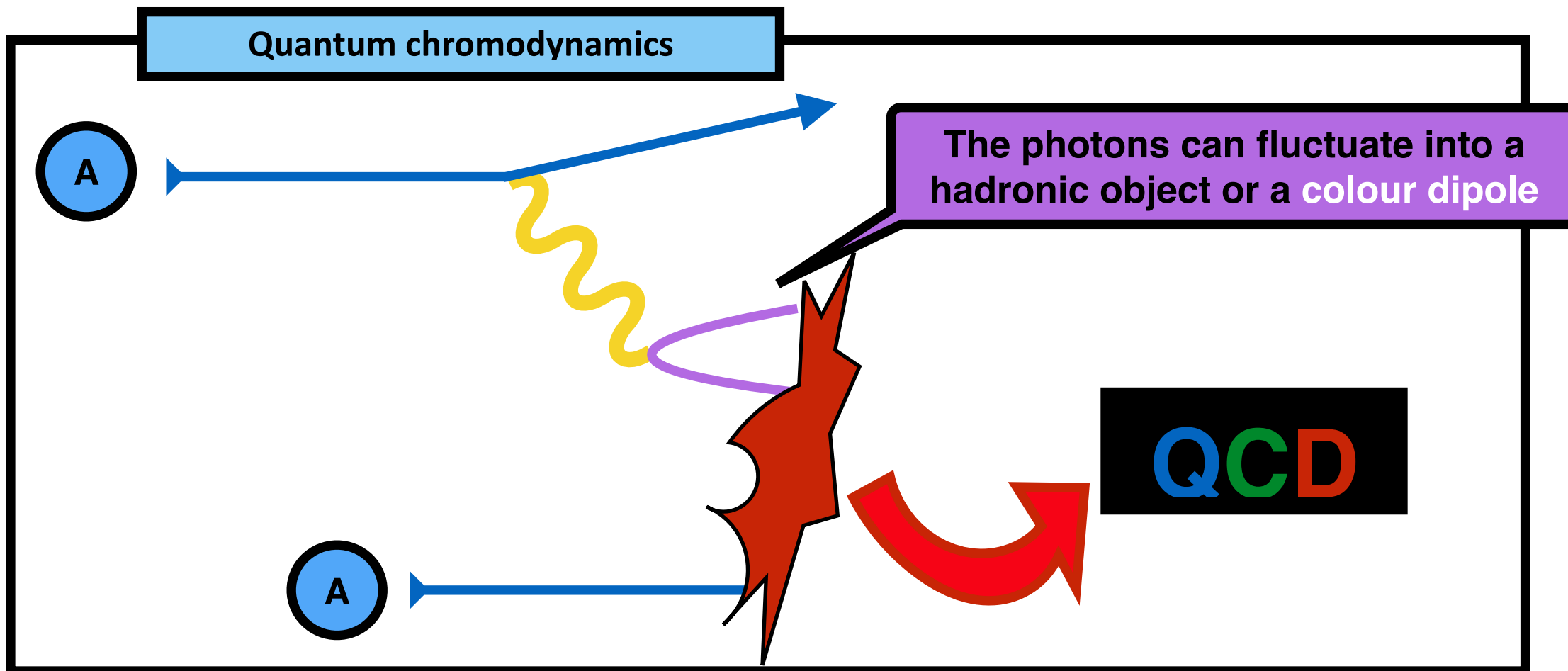
Quantum electrodynamics



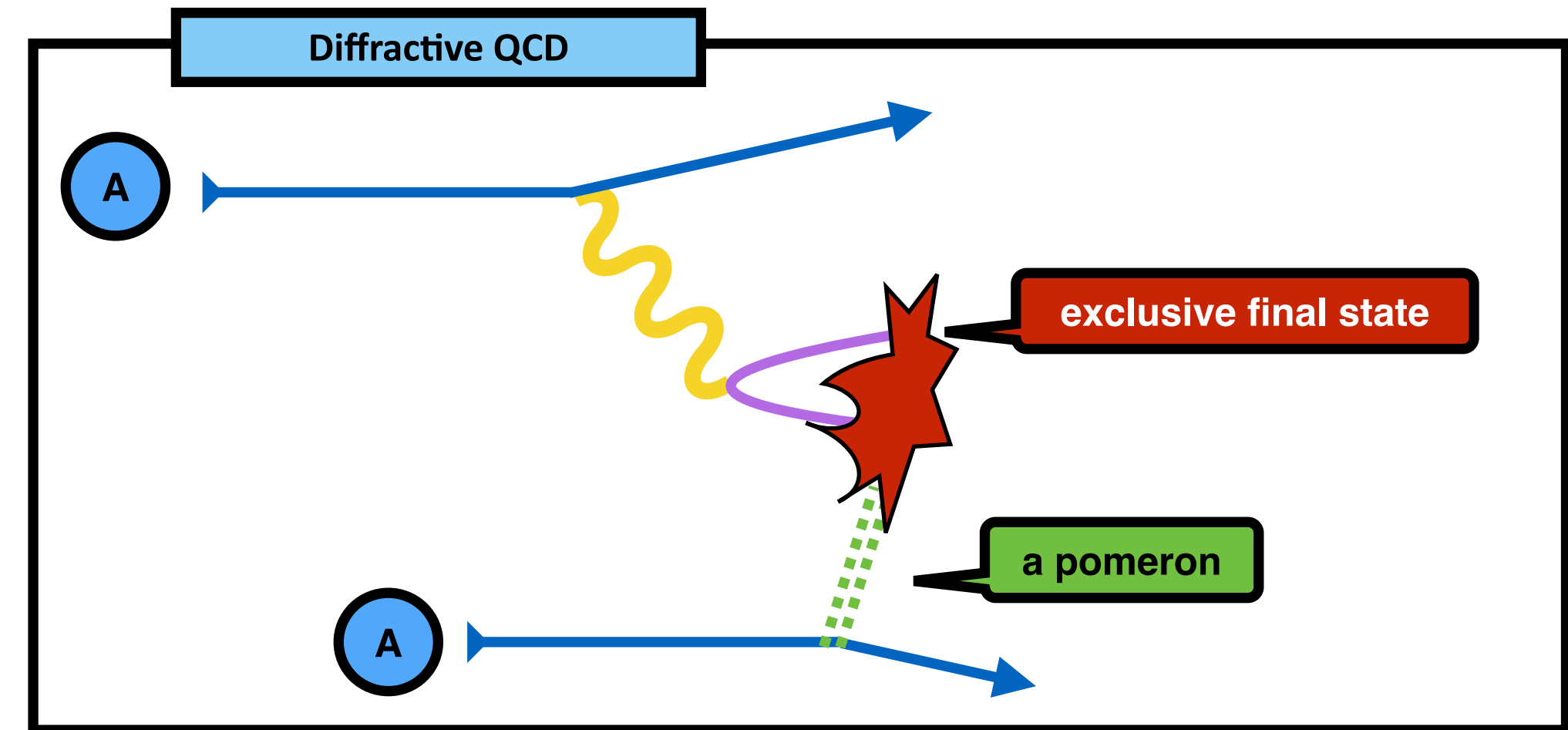
Nuclear physics



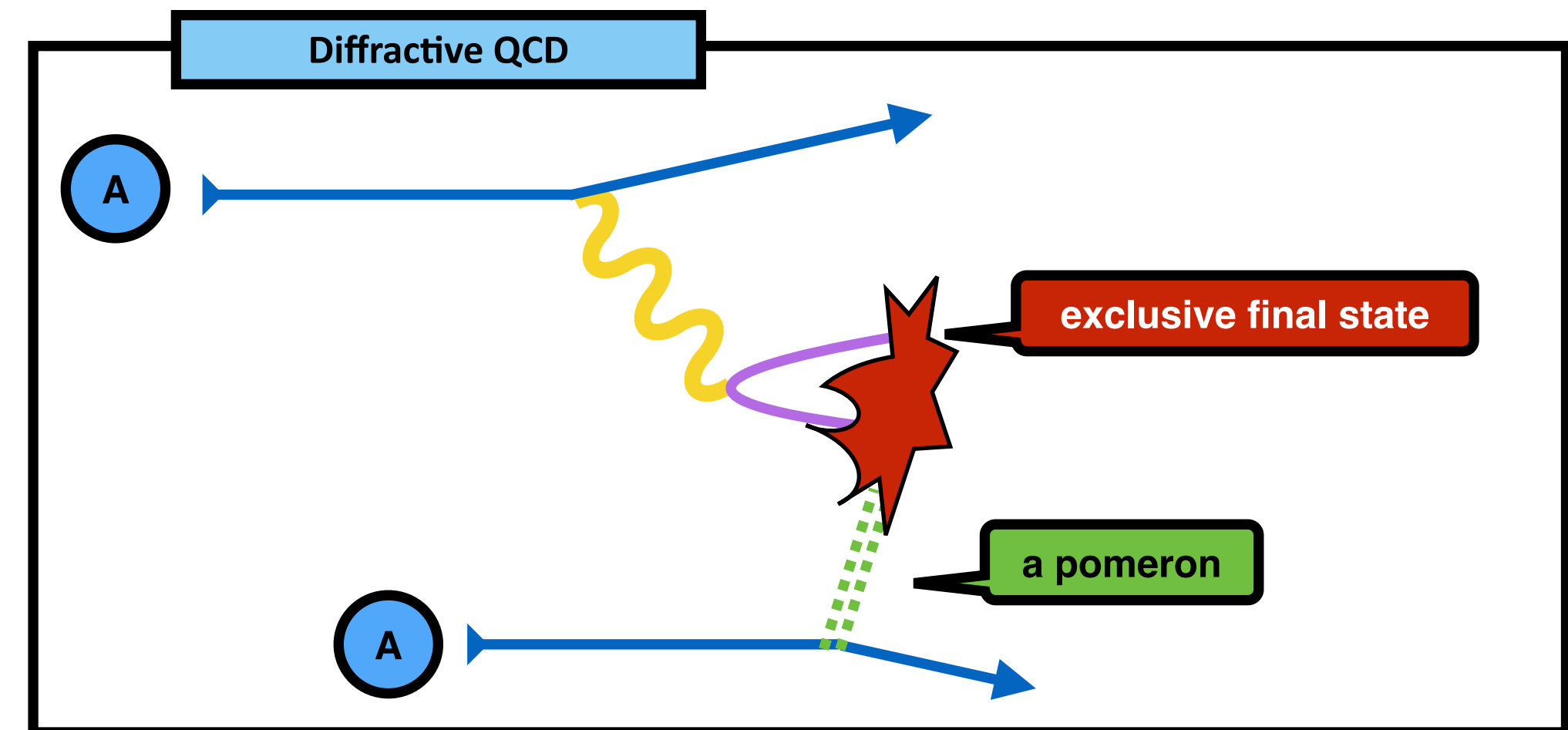
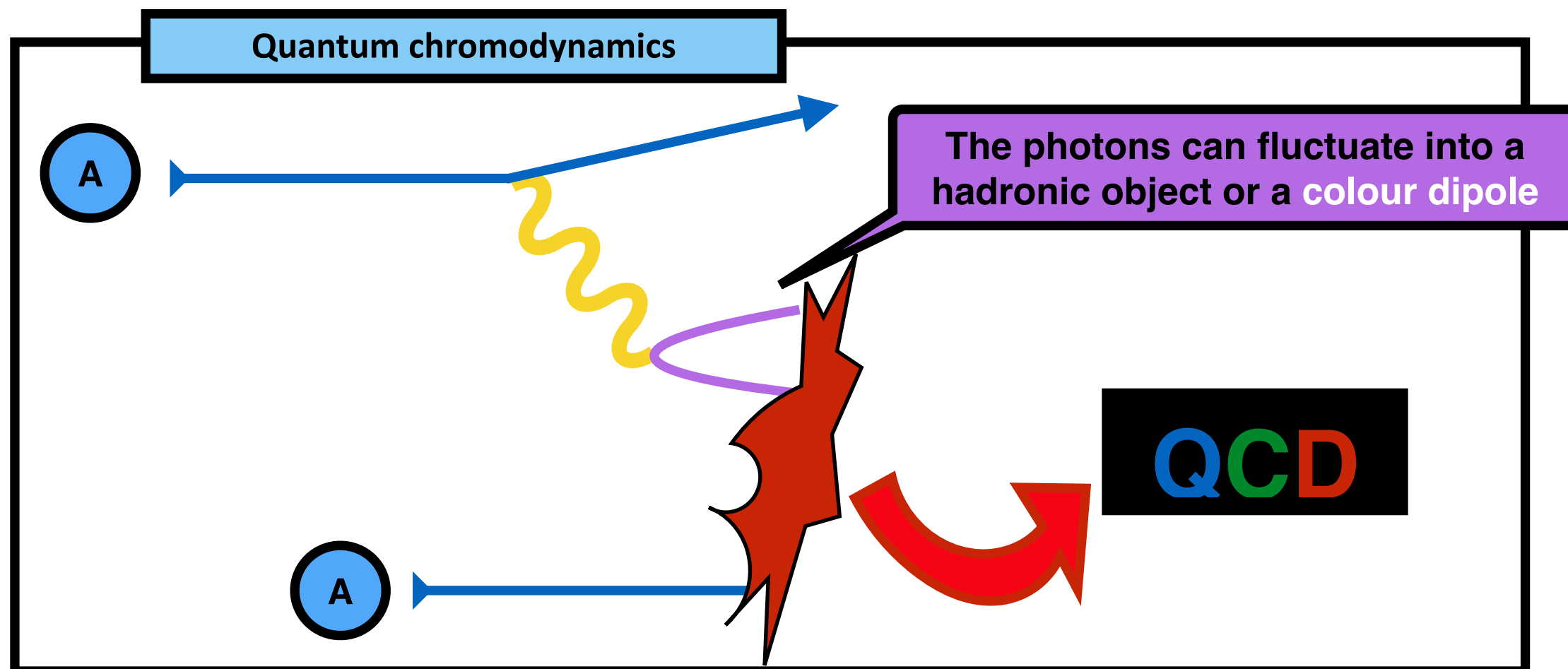
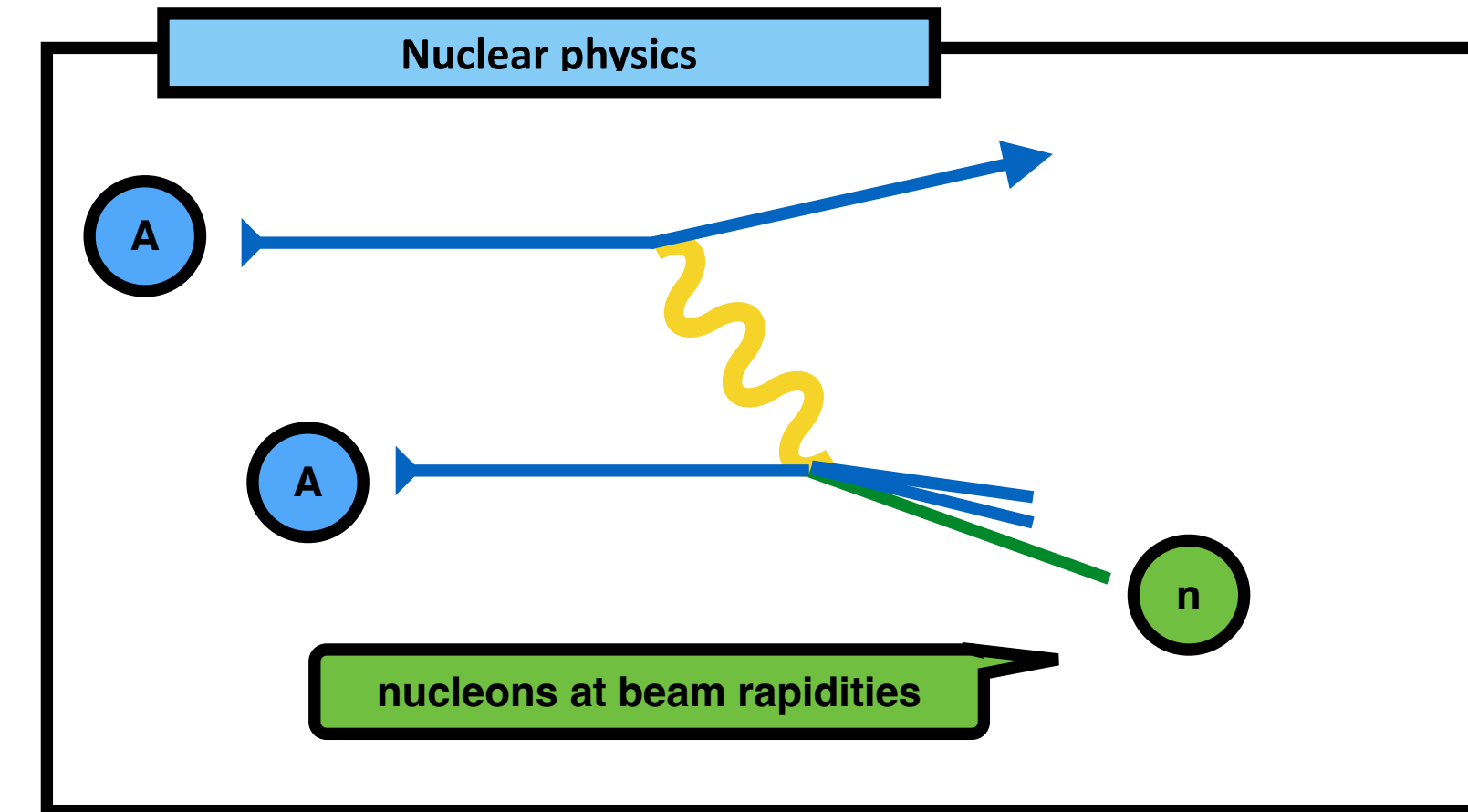
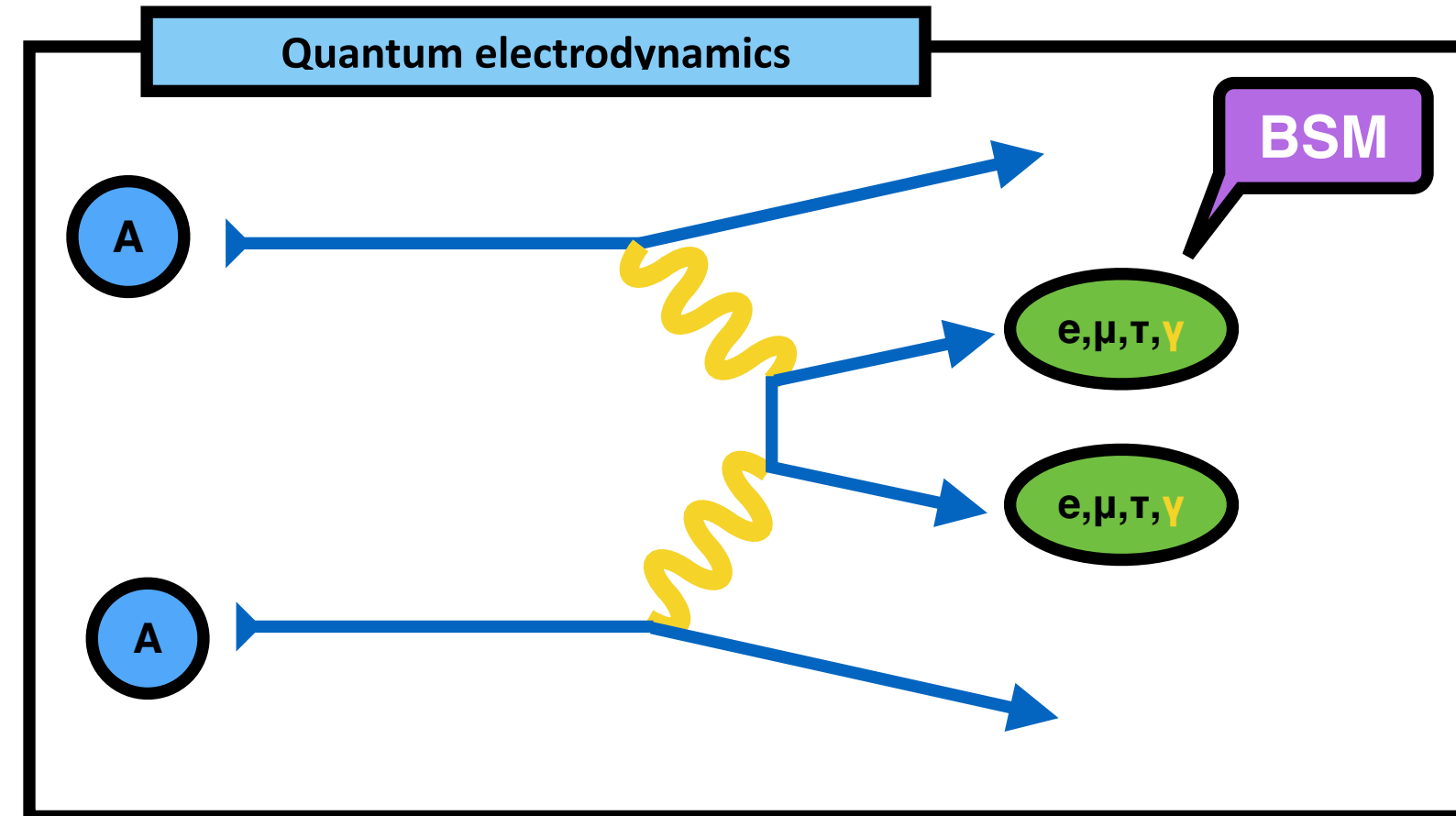
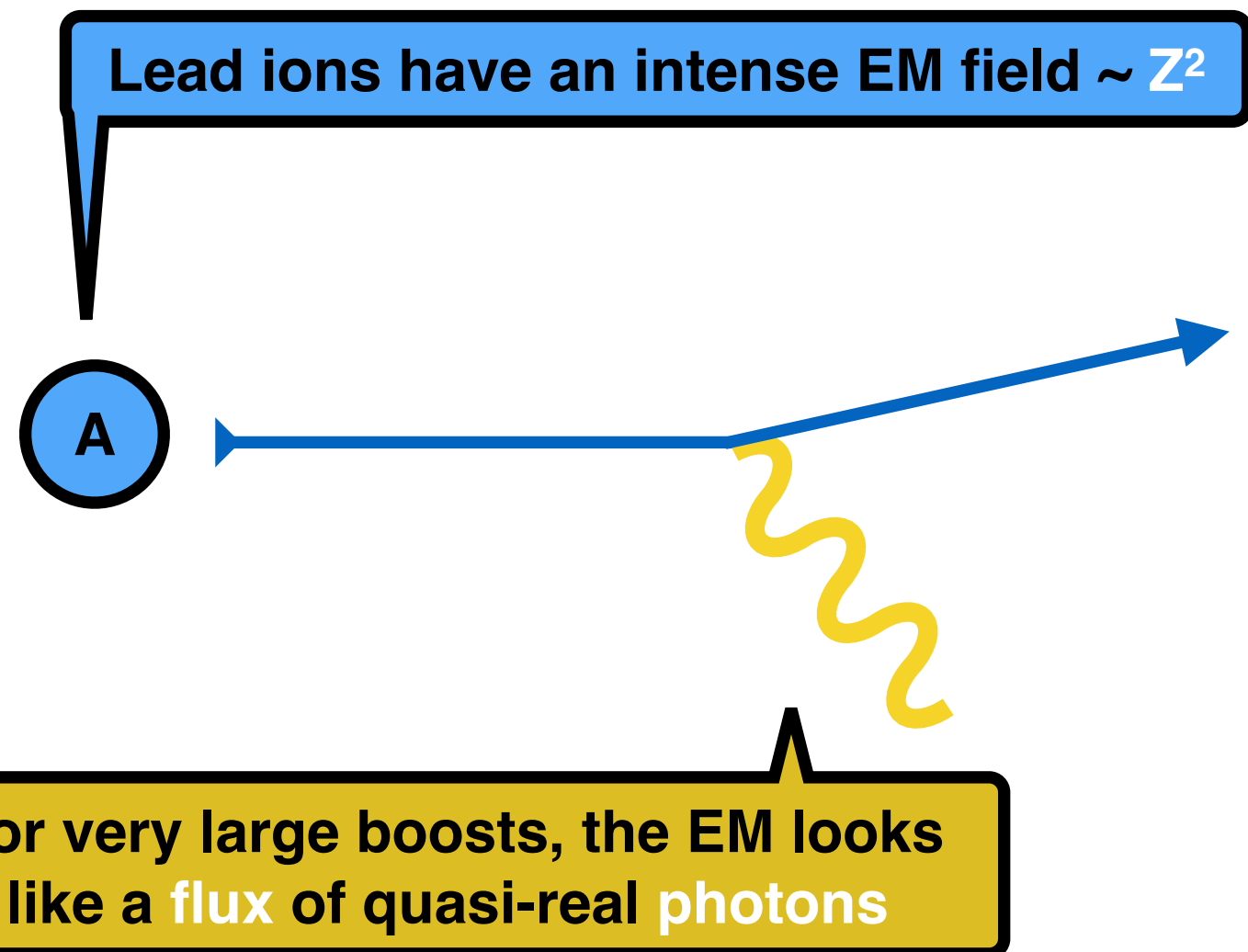
Quantum chromodynamics



Diffractive QCD



Photons at the ion colliders: examples of what can be done



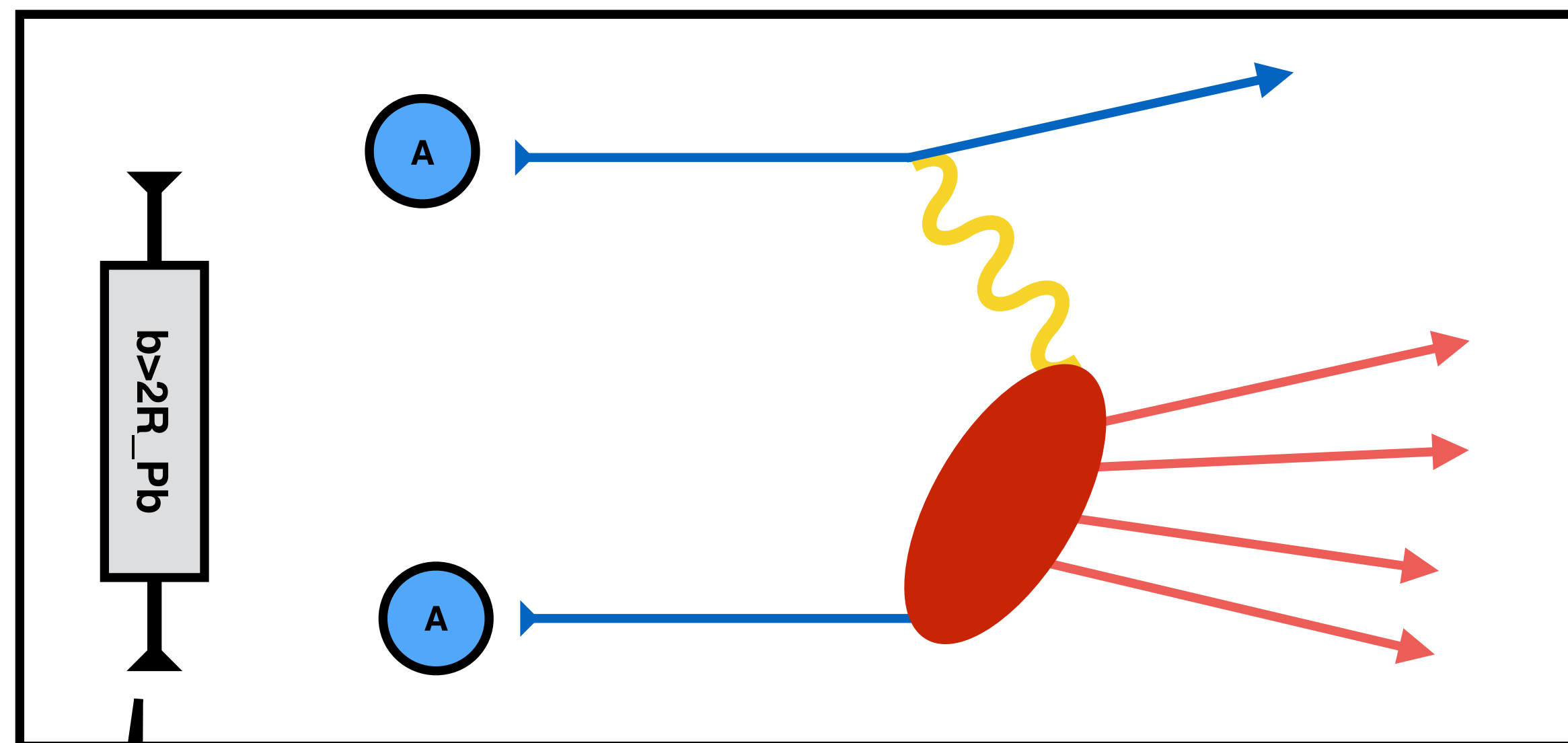
Finding these processes in hadron colliders requires specific search techniques tailored to the environment and the available detectors

How to find photon-induced interactions in hadron colliders (1/4)

For inclusive observables one has to use ultra-peripheral collisions (UPC)

How to find photon-induced interactions in hadron colliders (1/4)

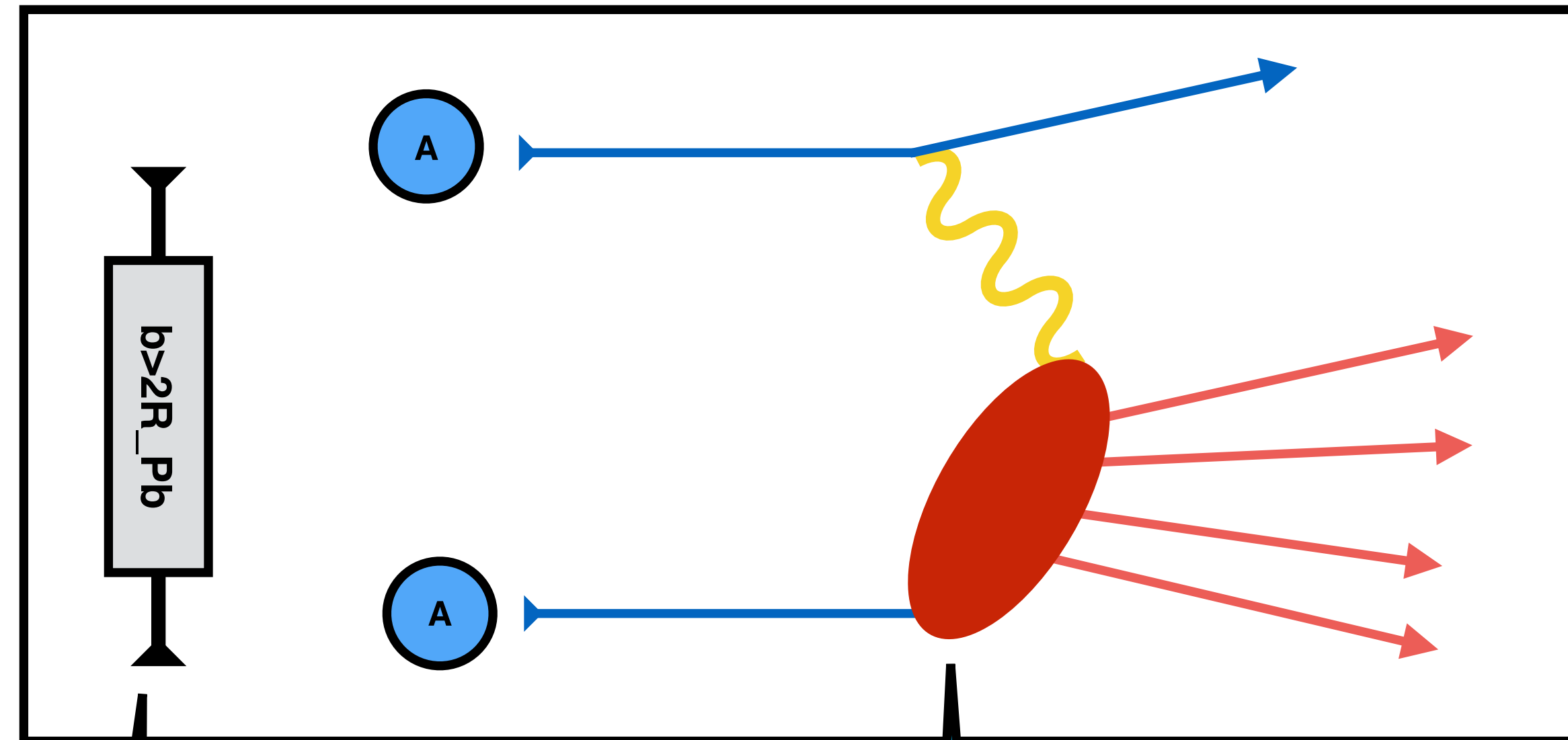
For inclusive observables one has to use ultra-peripheral collisions (UPC)



Choose interactions at large impact parameters

How to find photon-induced interactions in hadron colliders (1/4)

For inclusive observables one has to use ultra-peripheral collisions (UPC)

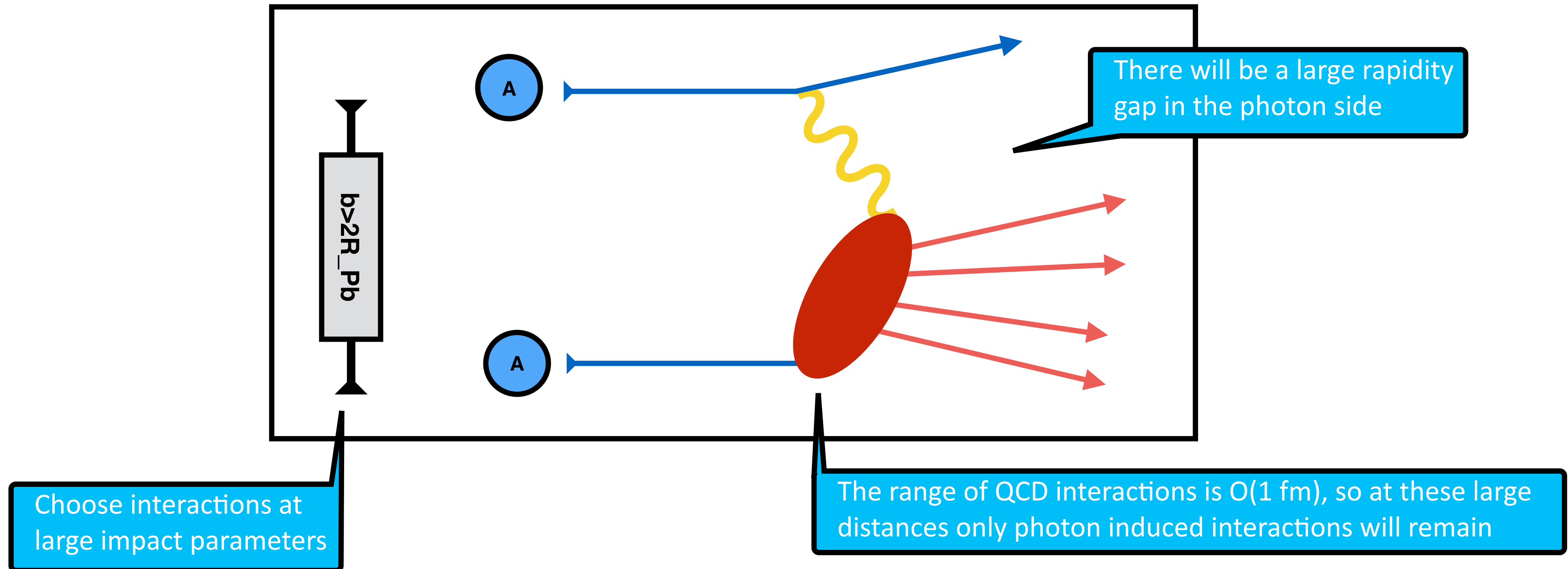


Choose interactions at large impact parameters

The range of QCD interactions is $O(1 \text{ fm})$, so at these large distances only photon induced interactions will remain

How to find photon-induced interactions in hadron colliders (1/4)

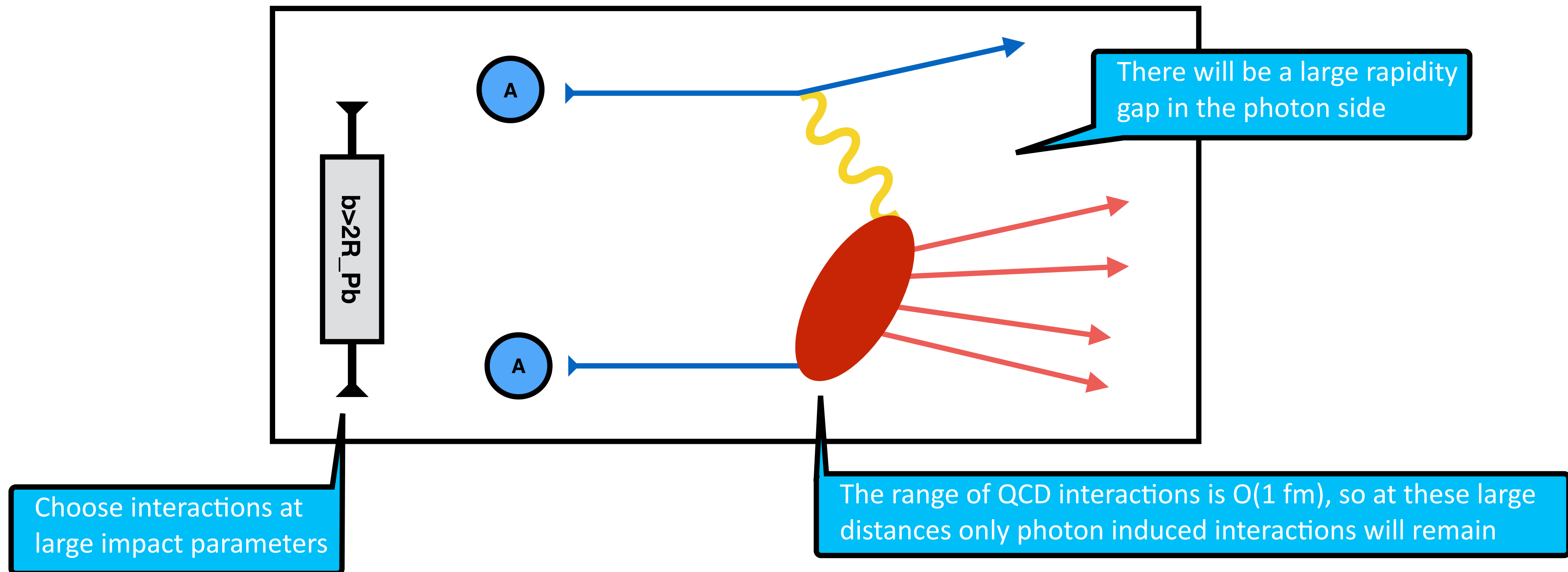
For inclusive observables one has to use ultra-peripheral collisions (UPC)



How to find photon-induced interactions in hadron colliders (1/4)

For inclusive observables one has to use ultra-peripheral collisions (UPC)

Signature: Look for a large rapidity gap in one side of the detector

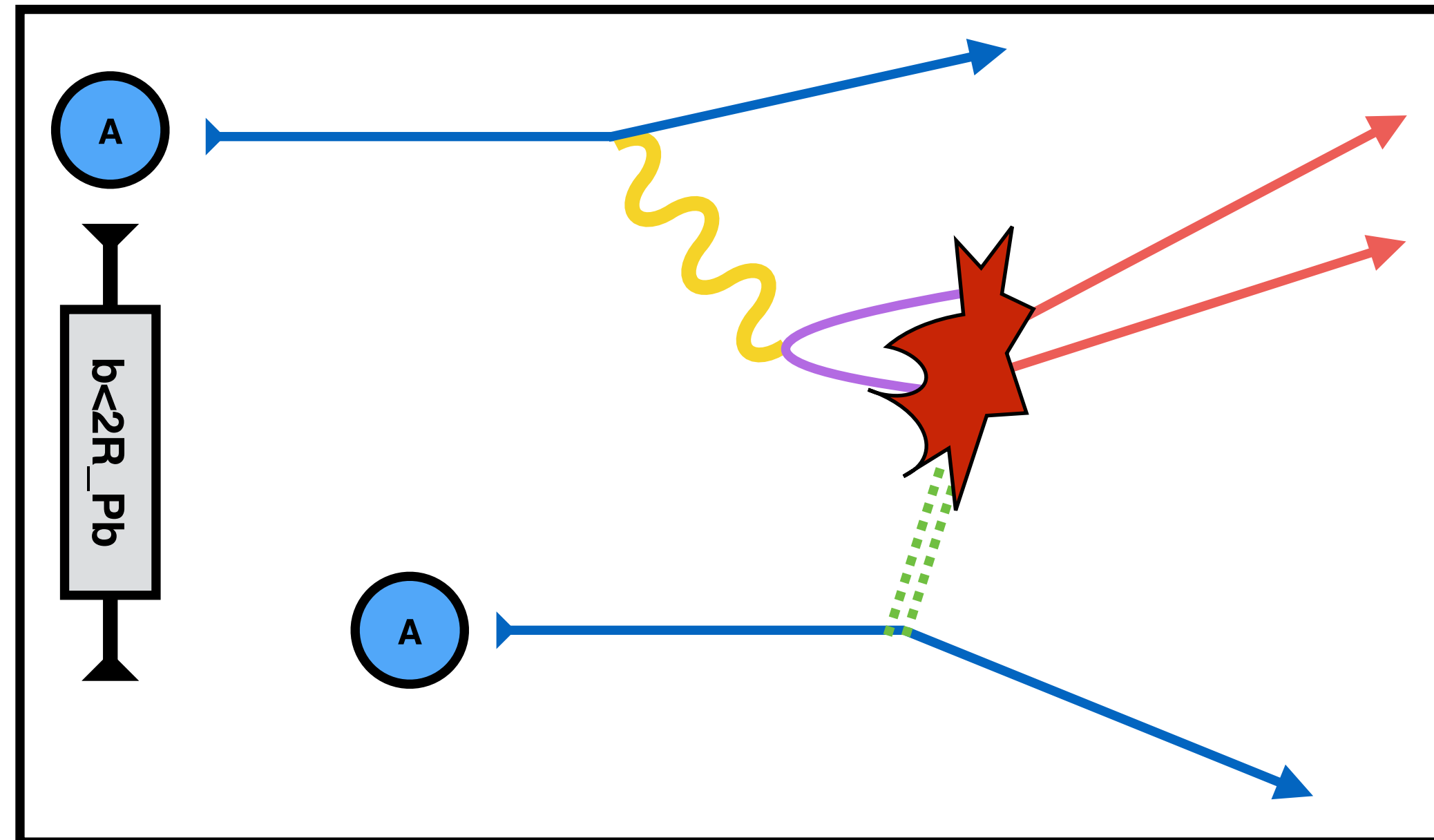


How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions

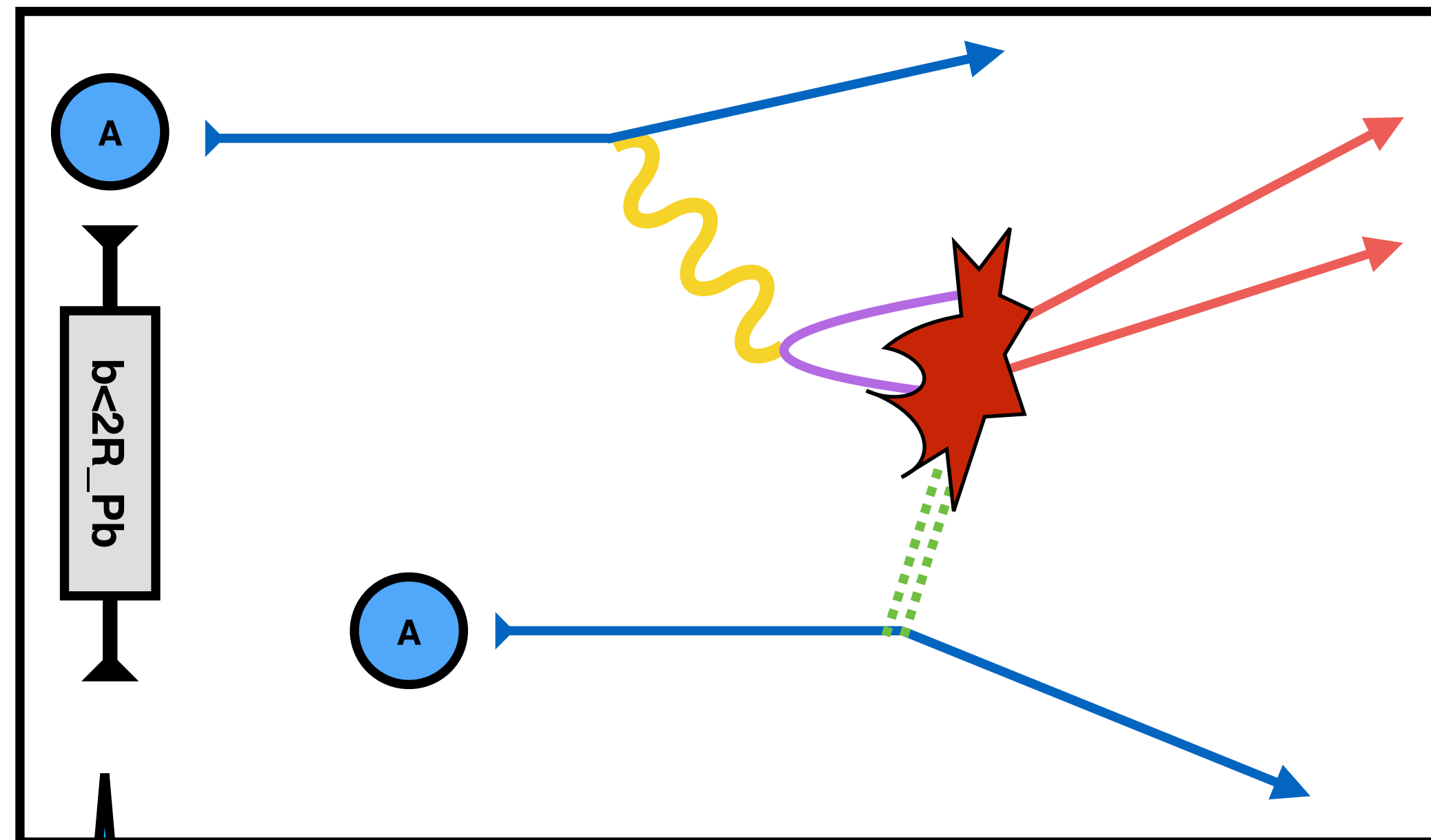
How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions



How to find photon-induced interactions in hadron colliders (2/4)

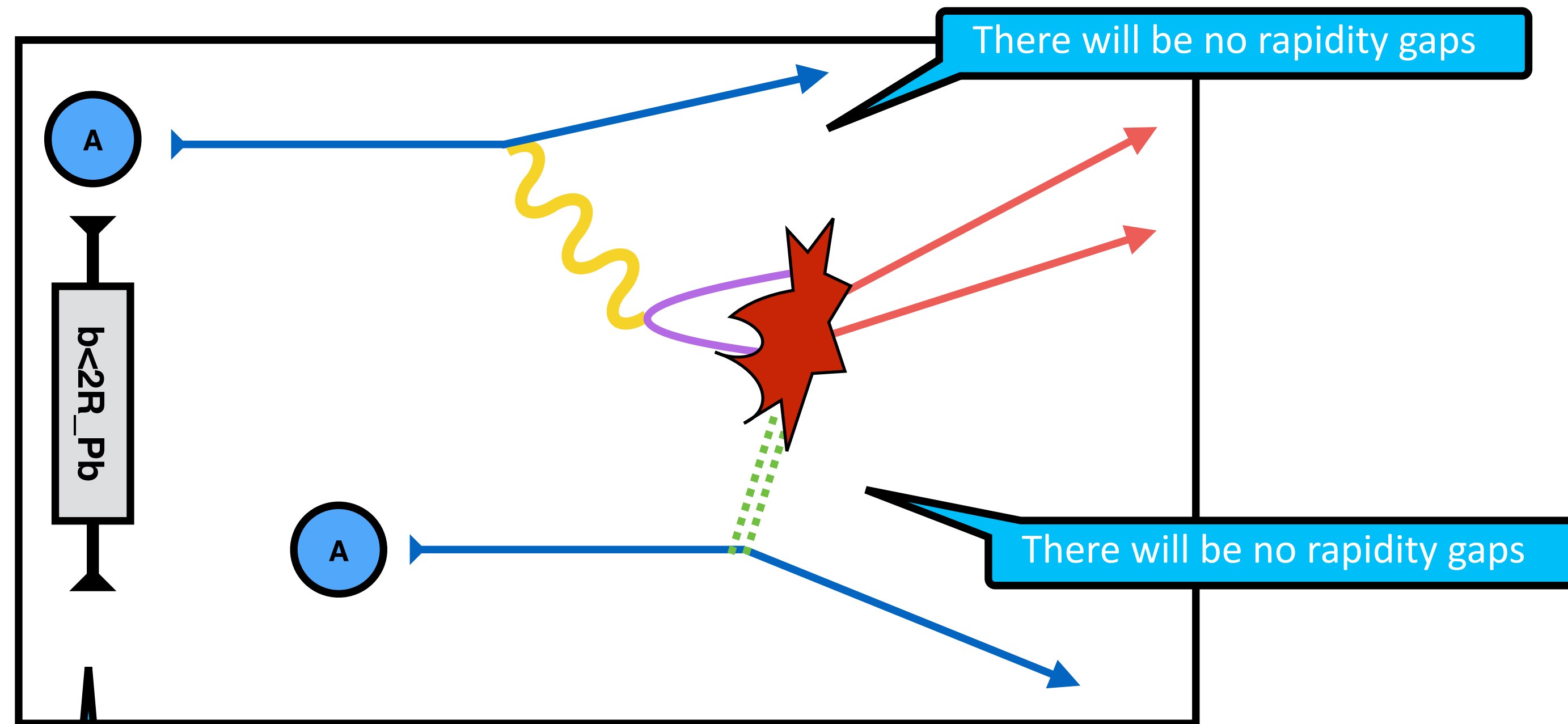
For exclusive diffractive observables, one can use peripheral collisions



For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

How to find photon-induced interactions in hadron colliders (2/4)

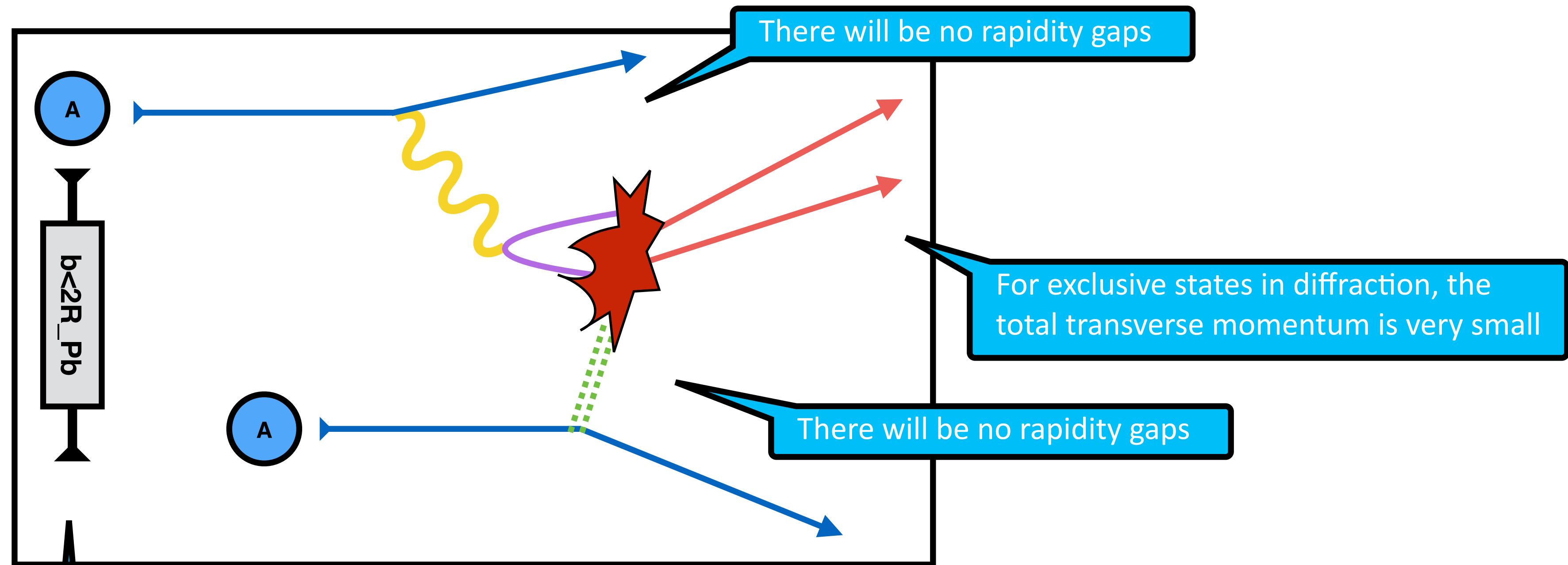
For exclusive diffractive observables, one can use peripheral collisions



For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions

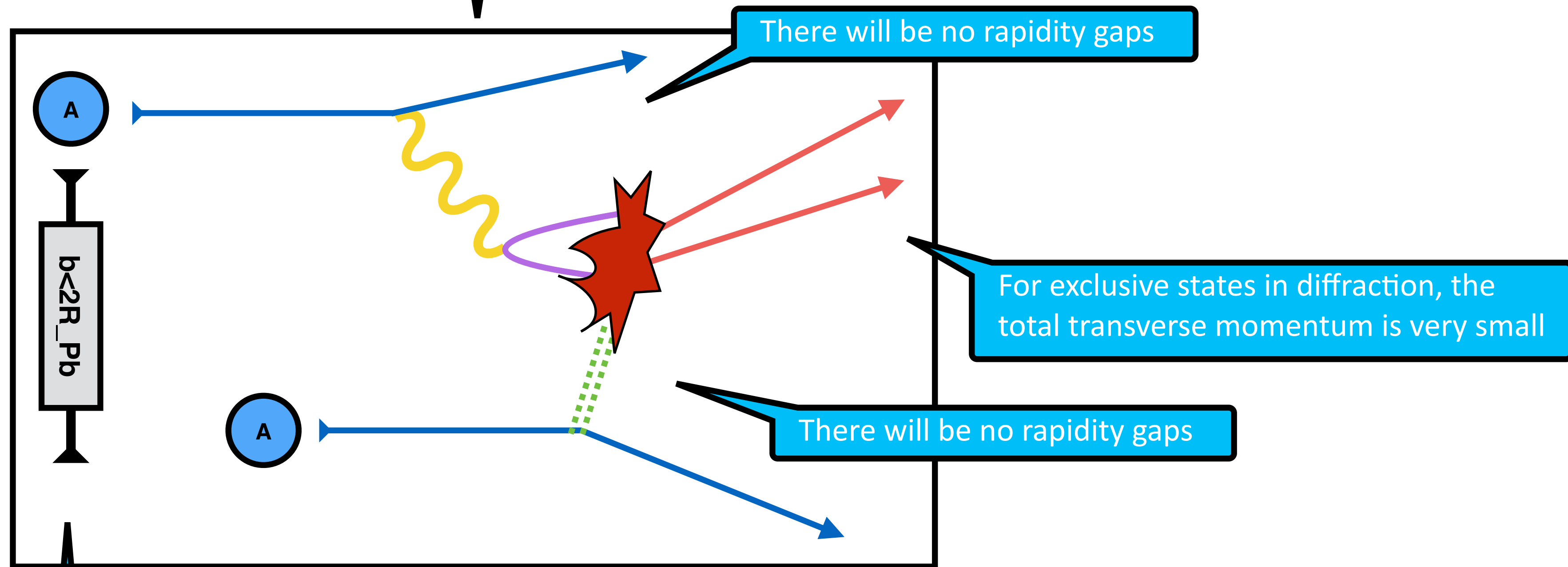


For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions

Signature: Look for a low p_T final state (eg. a dijet or a vector meson)



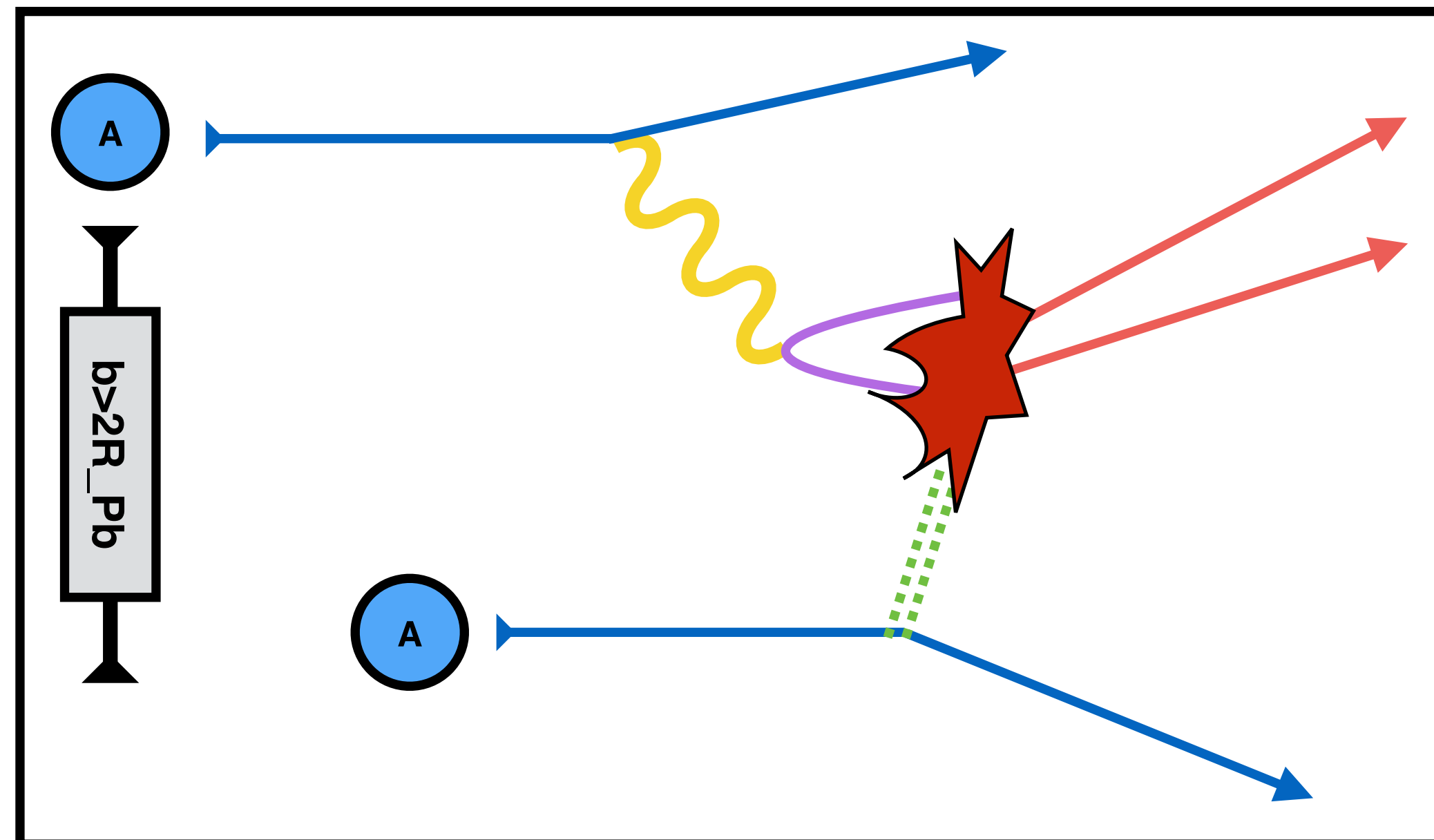
For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

How to find photon-induced interactions in hadron colliders (3/4)

For exclusive diffractive observables, one can also use UPC

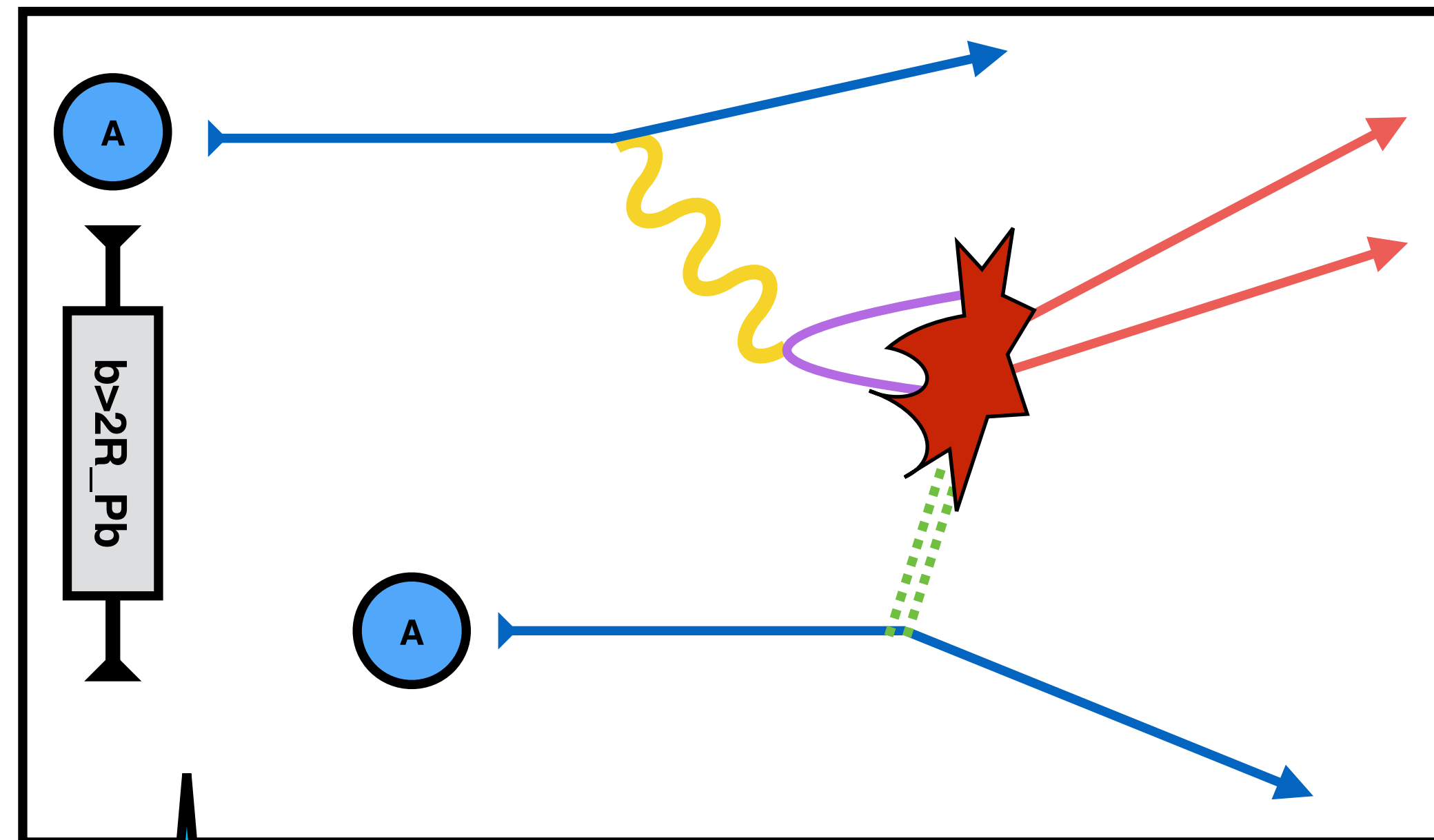
How to find photon-induced interactions in hadron colliders (3/4)

For exclusive diffractive observables, one can also use UPC



How to find photon-induced interactions in hadron colliders (3/4)

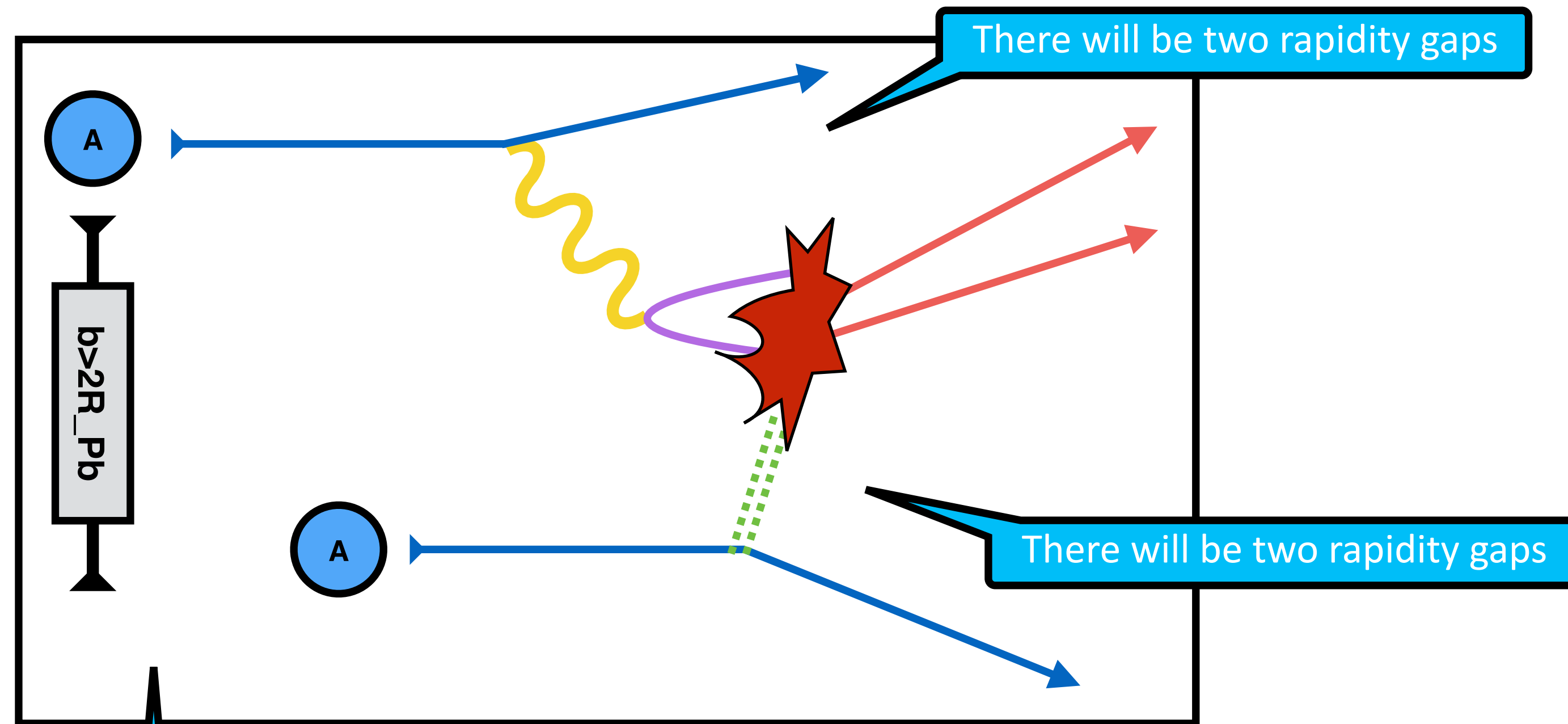
For exclusive diffractive observables, one can also use UPC



For UPC the photon-induced process there is no overlap of the incoming hadrons within the range of QCD

How to find photon-induced interactions in hadron colliders (3/4)

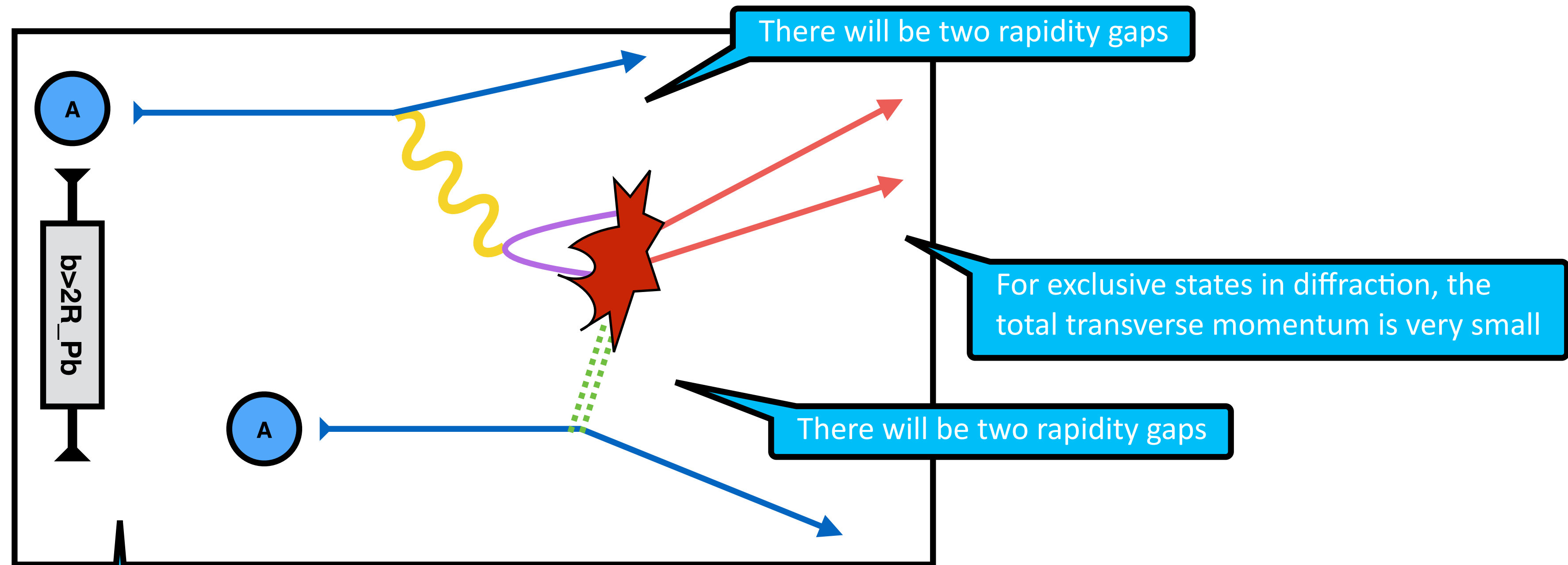
For exclusive diffractive observables, one can also use UPC



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How to find photon-induced interactions in hadron colliders (3/4)

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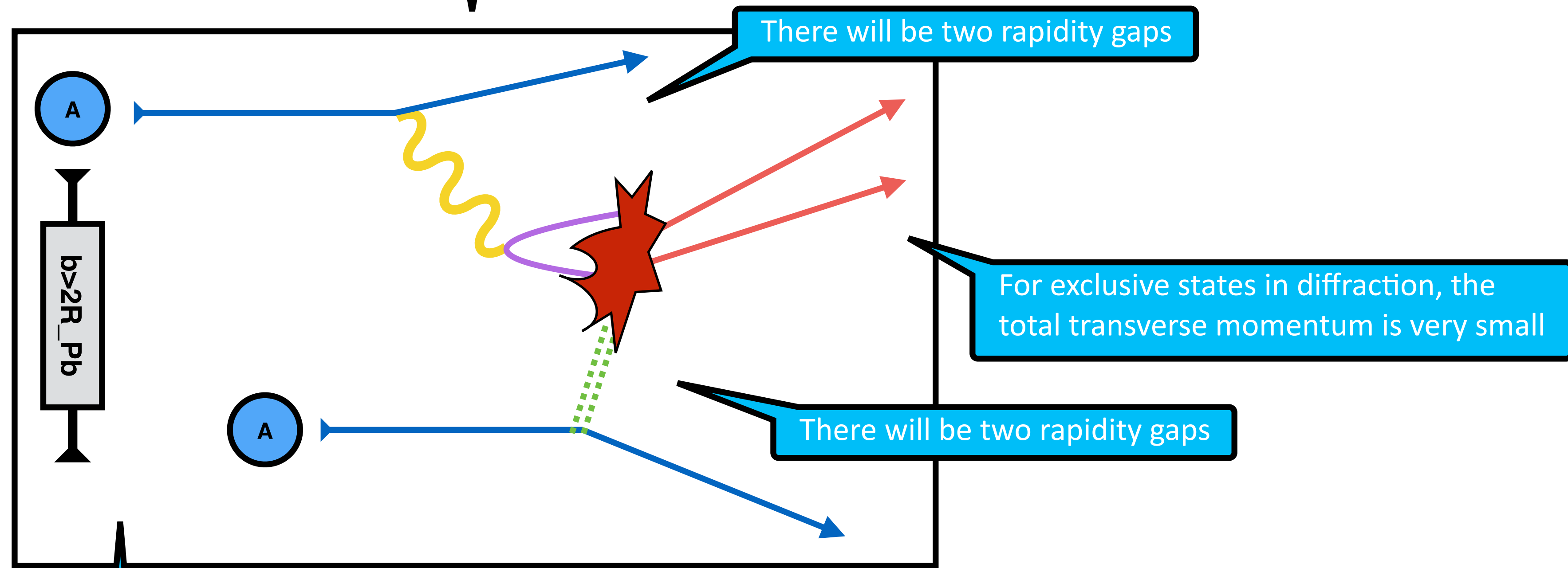


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Signature: Look for a low p_T final state (eg. a dijet or a vector meson) in an otherwise empty detector



For exclusive states in diffraction, the total transverse momentum is very small

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Imposing conditions to select events may select a subset of the total flux
Let's look at two variations of the flux formalism to account for this effect:
Selecting UPC coherent processes
Selecting EMD processes

The photon flux in coherent UPC according to STARlight

Use a Glauber description of the target to ensure the absence of hadronic inelastic collisions

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$$n^U(y) = k \int_0^\infty db 2\pi b P_{NH}(b) \int_0^{r_A} \frac{r dr}{\pi r_A^2} \int_0^{2\pi} d\phi n(k, b + r \cos(\phi))$$

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Rapidity of the final state

$$k = \frac{M}{2} e^y$$

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In a Poissonian model

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cross section of a nucleon-nucleon inelastic hadronic interaction

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Probability of no inelastic hadronic interactions at this impact parameter

Average over all possible positions in the target

Flux

Position in the target

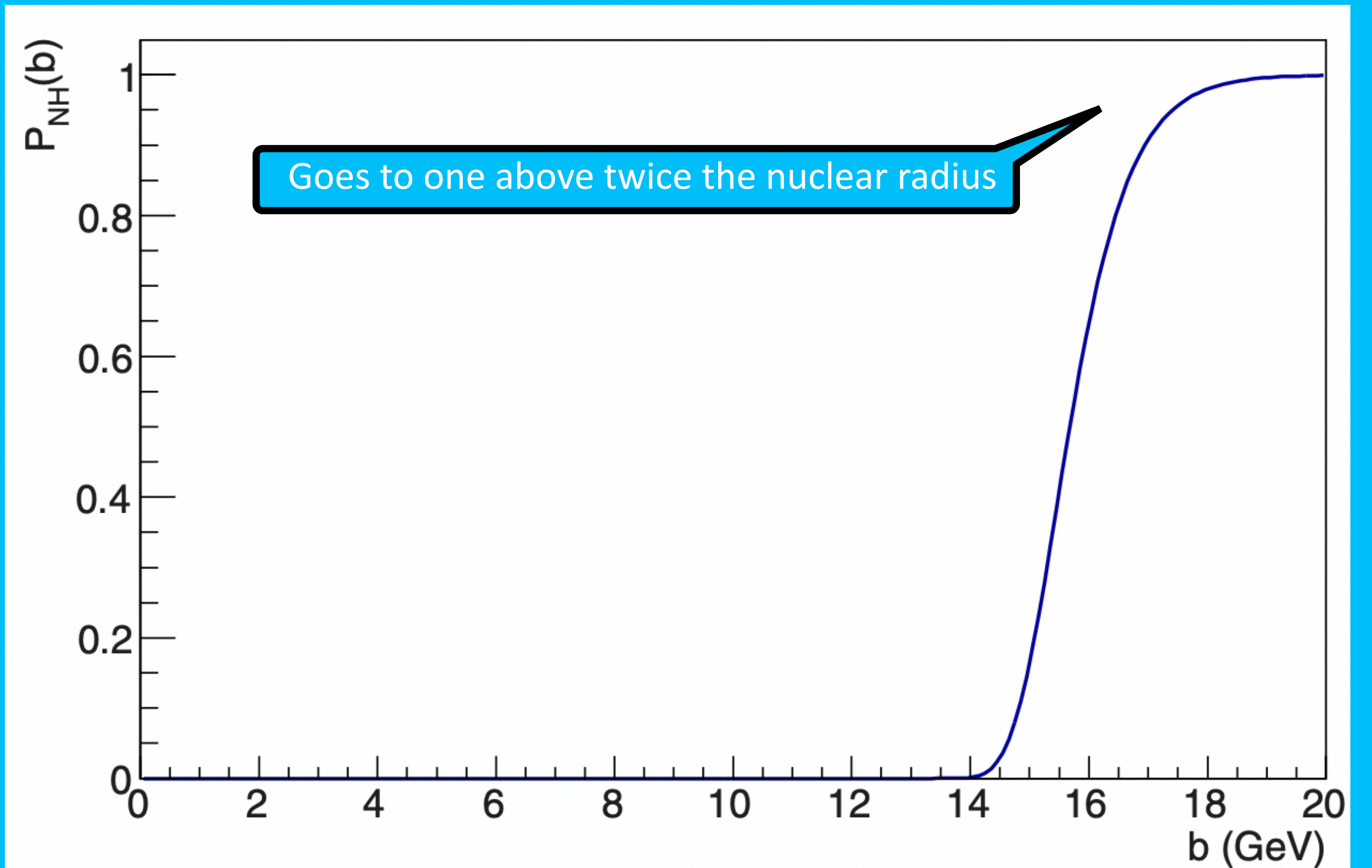
impact parameter

Homework:

try to implement these formulas

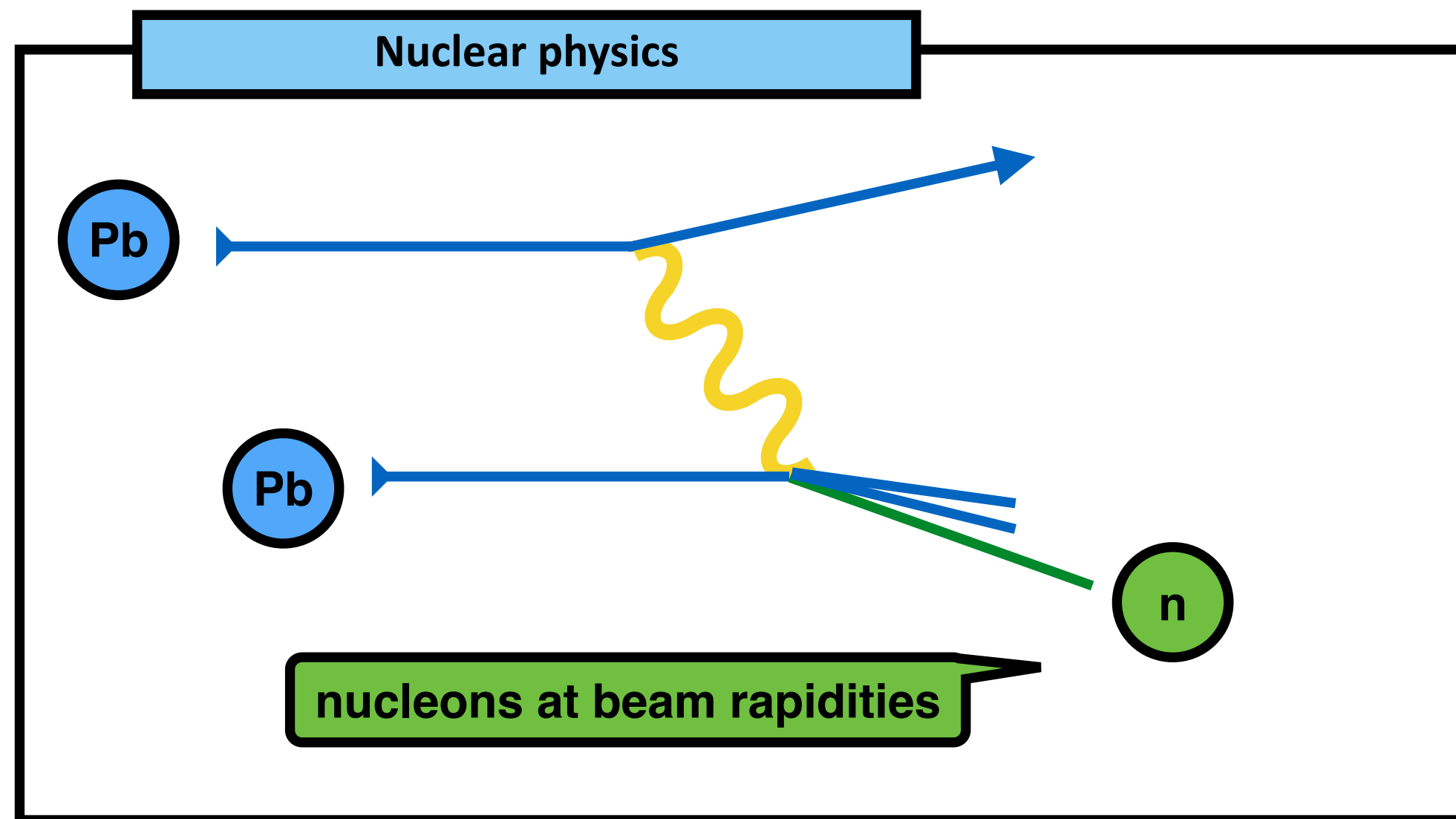
Probability of no inelastic hadronic interaction

Probability of no hadronic inelastic interaction for Pb-Pb collisions

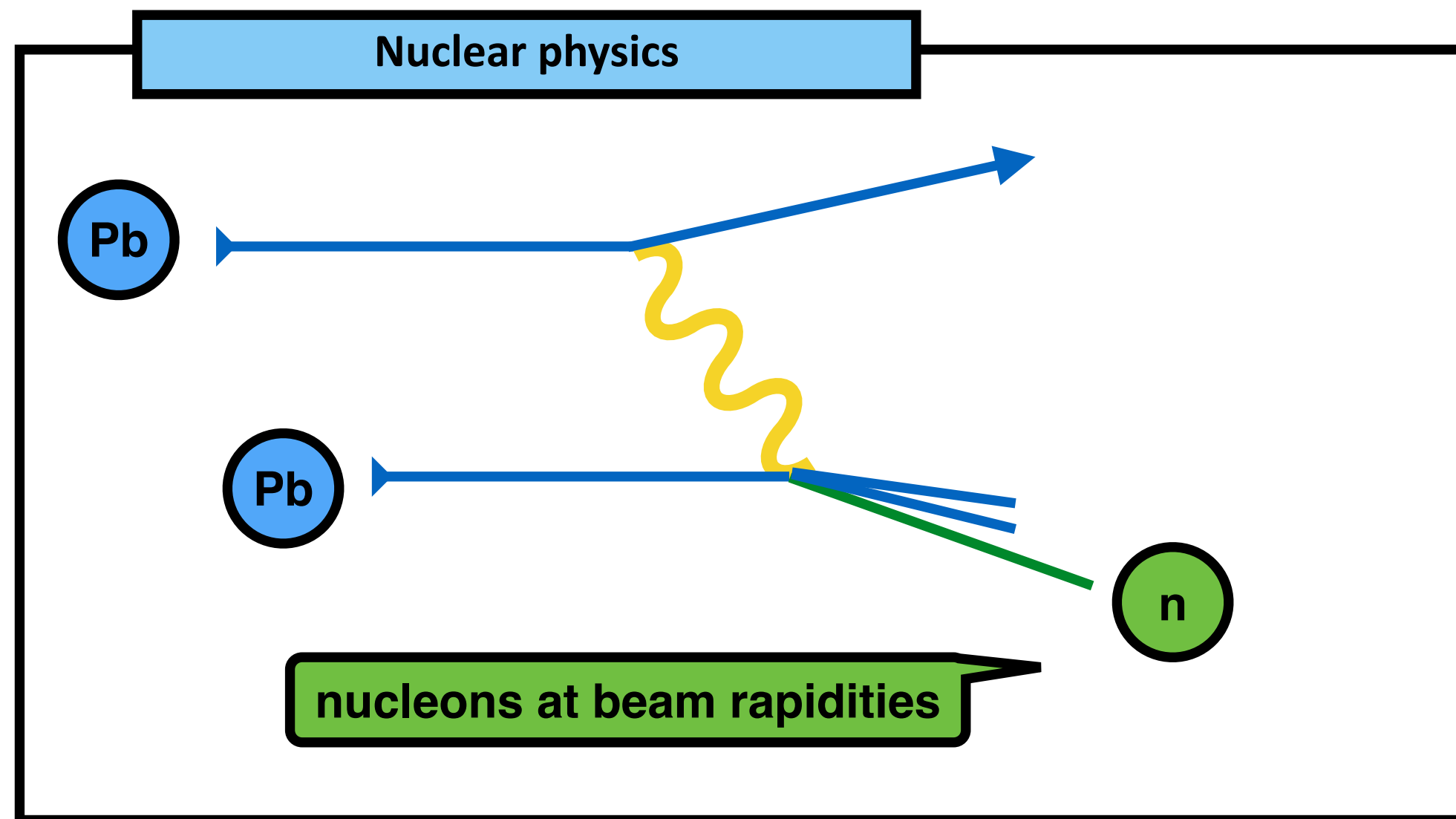


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Electromagnetic dissociation (EMD)

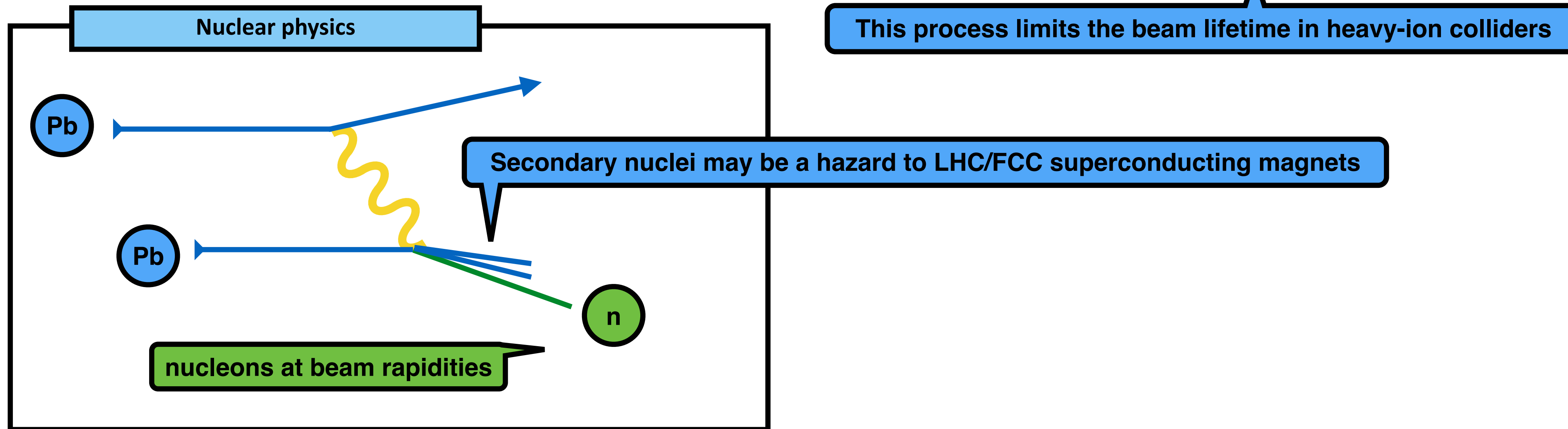


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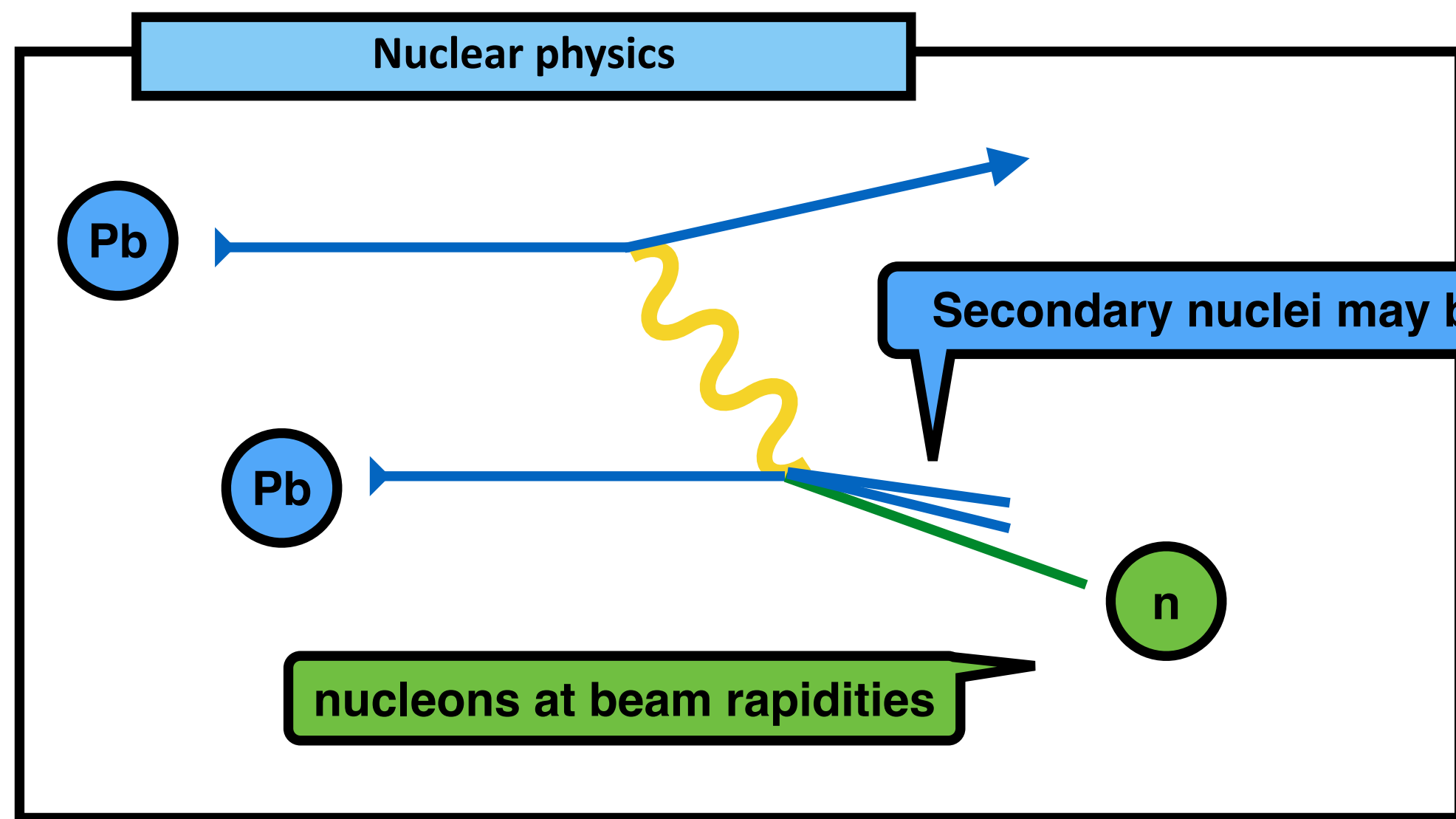


This process limits the beam lifetime in heavy-ion colliders

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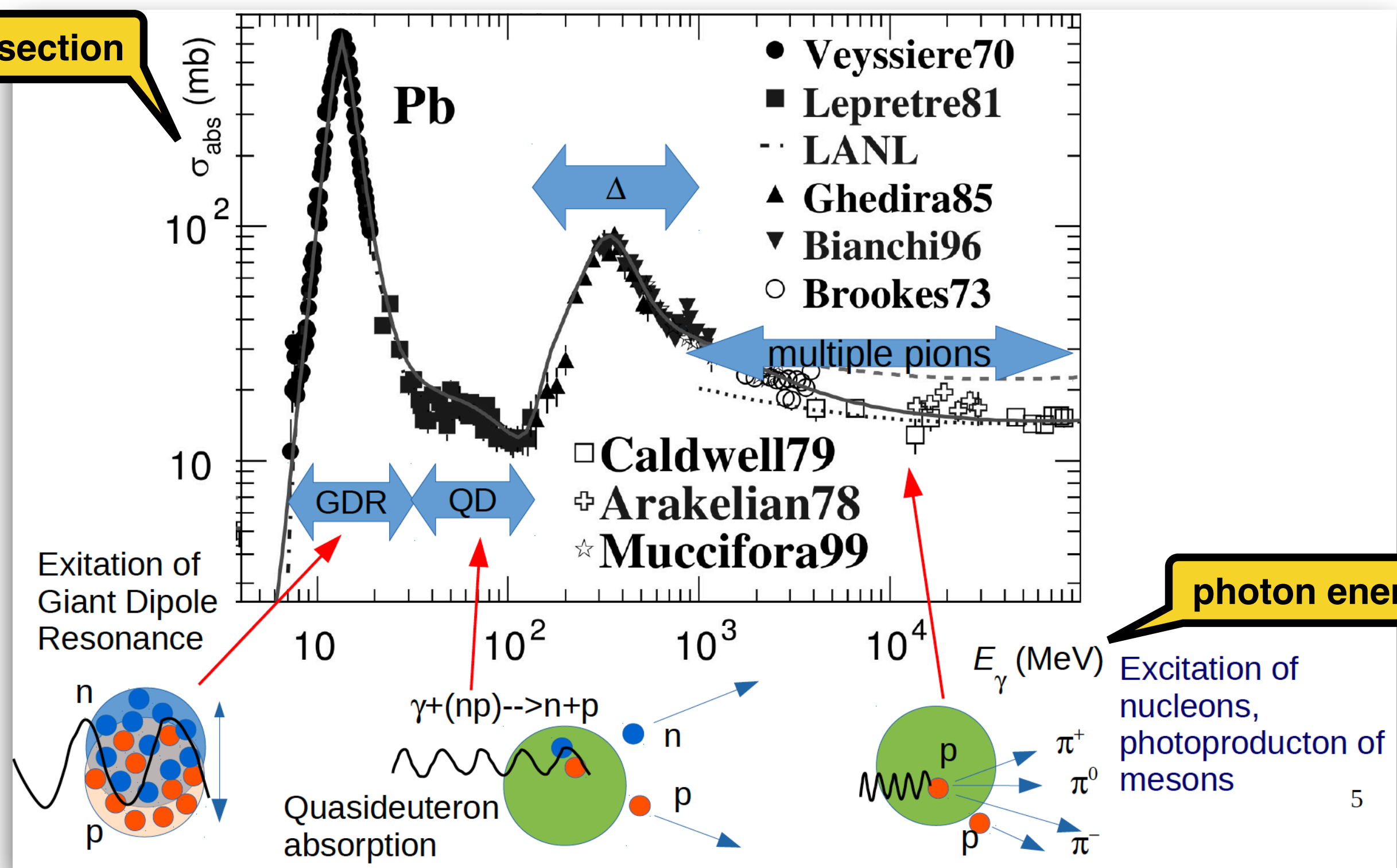


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Secondary nuclei may be a hazard to LHC/FCC superconducting magnets

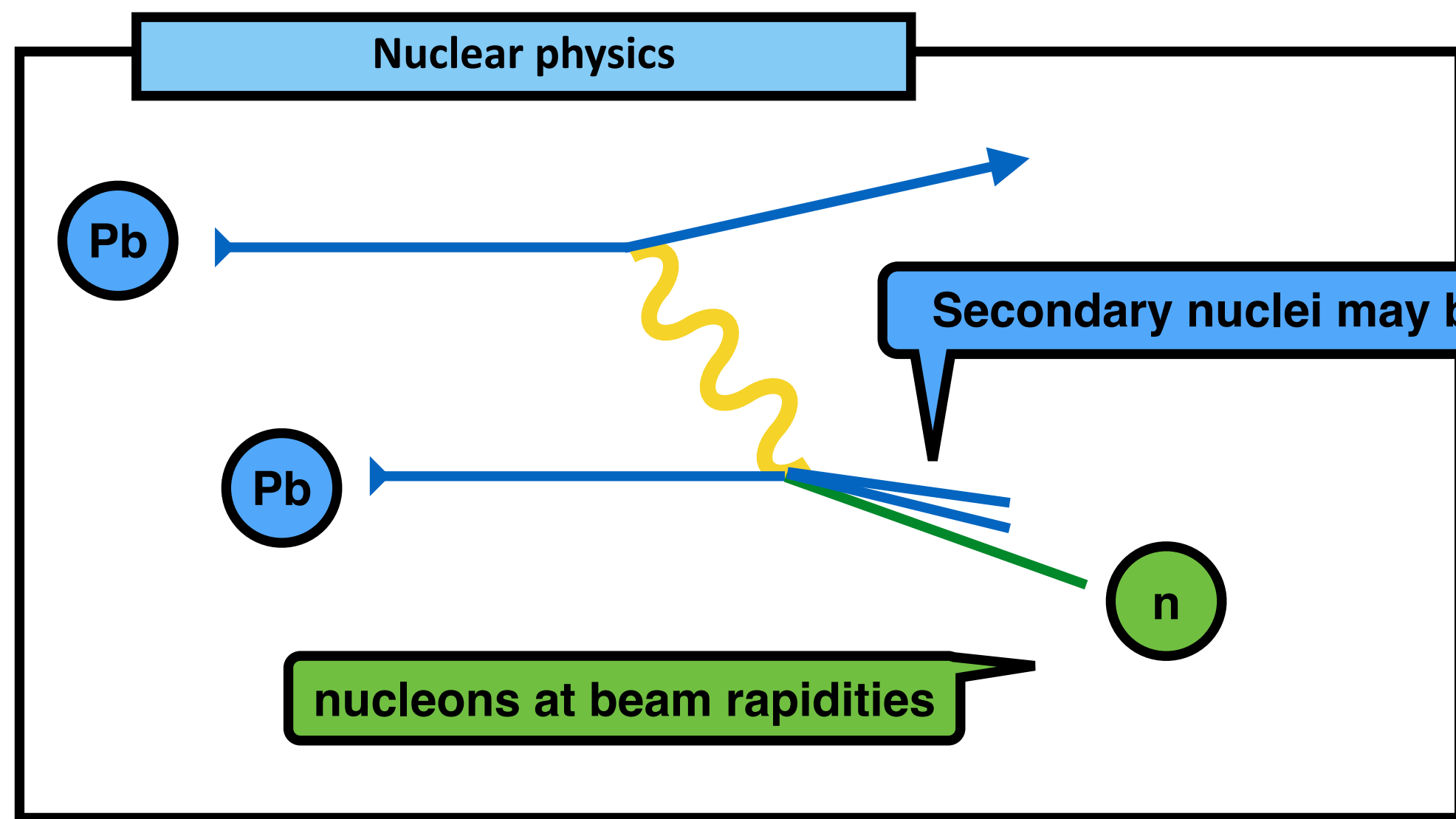
Slide from Igor Pshenichnov

cross section



photon energy

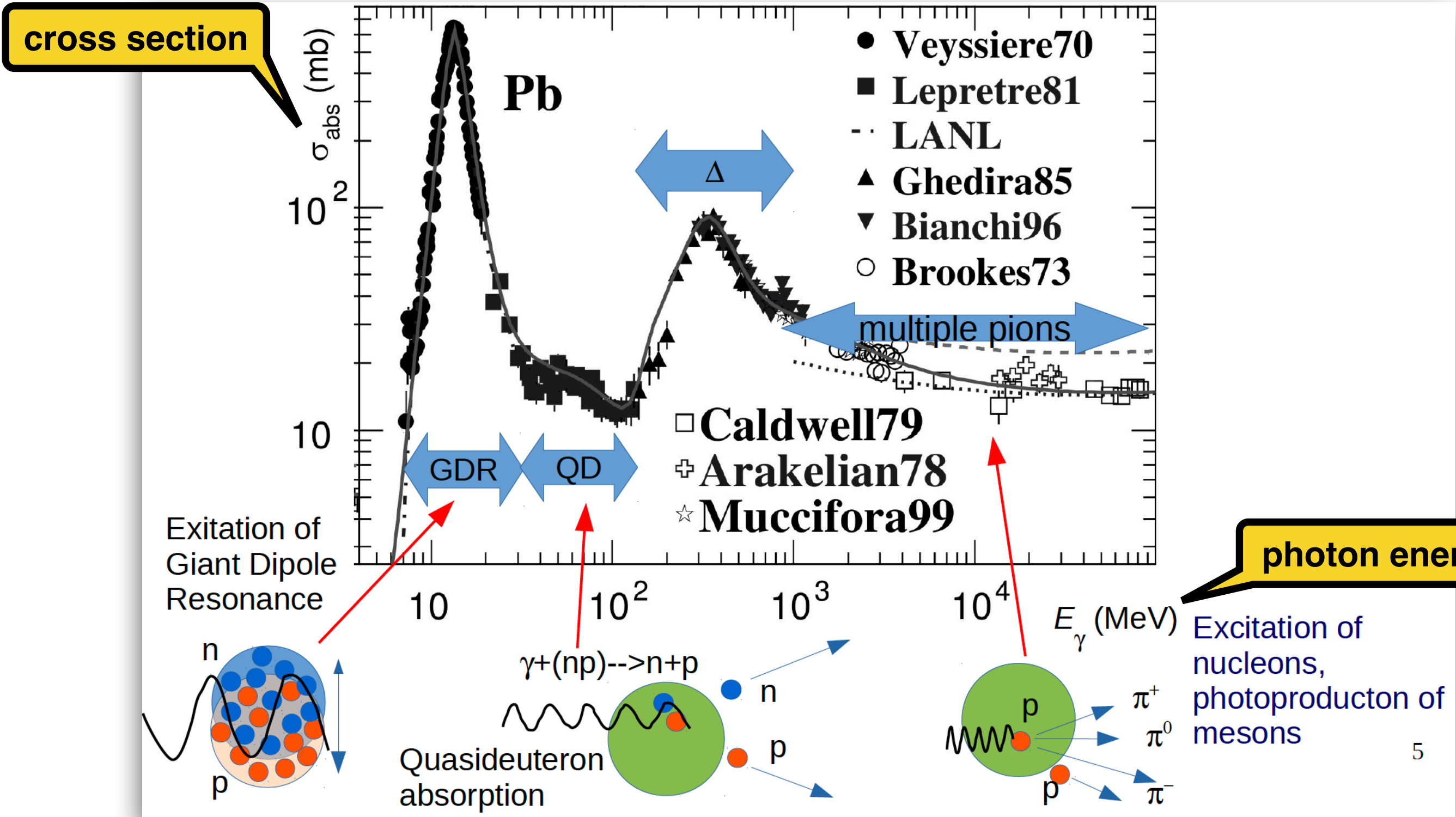
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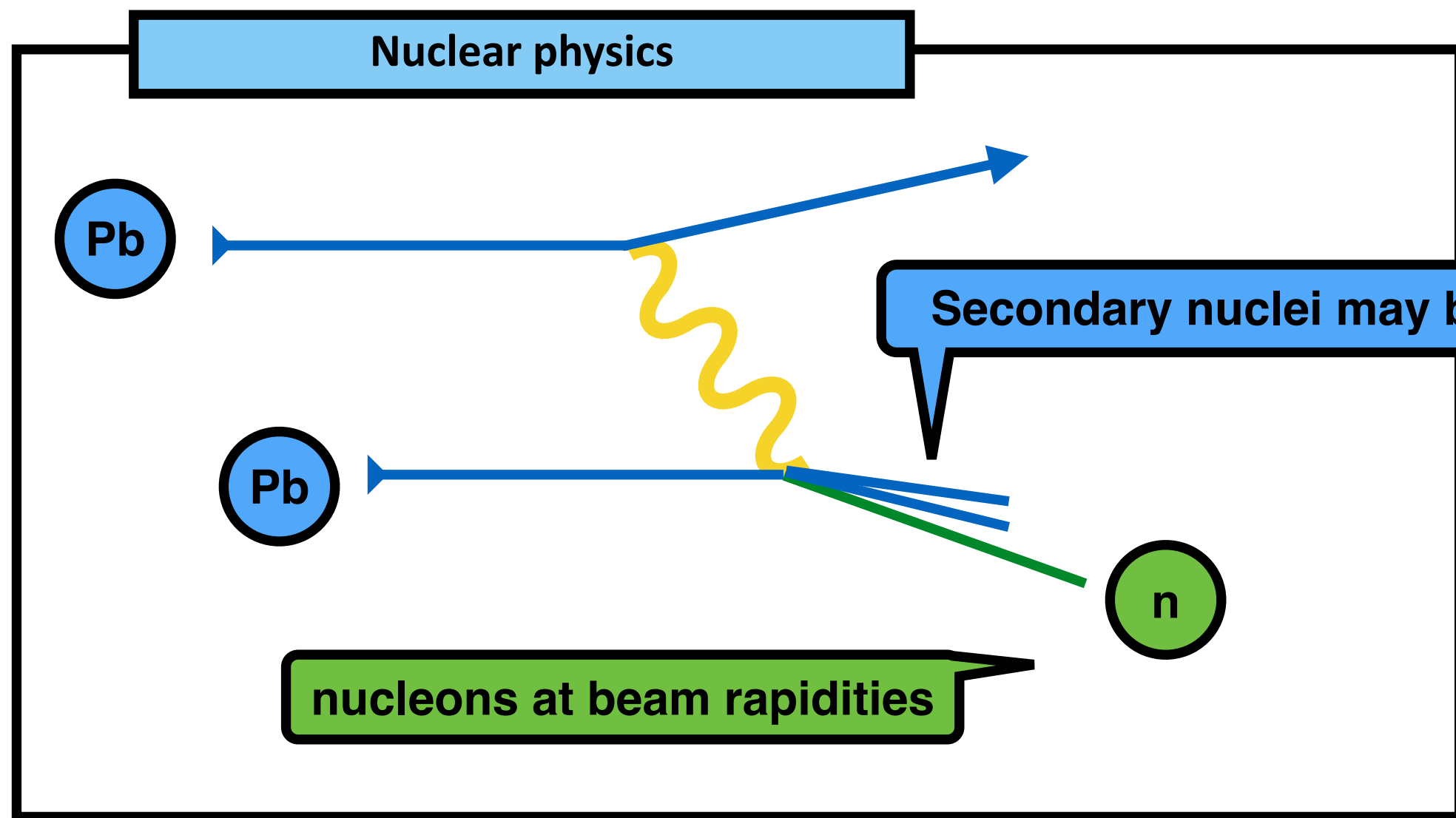
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photon energy

At larger photon energies, charged particles are produced: may affect the efficiency of vetos at forward rapidities

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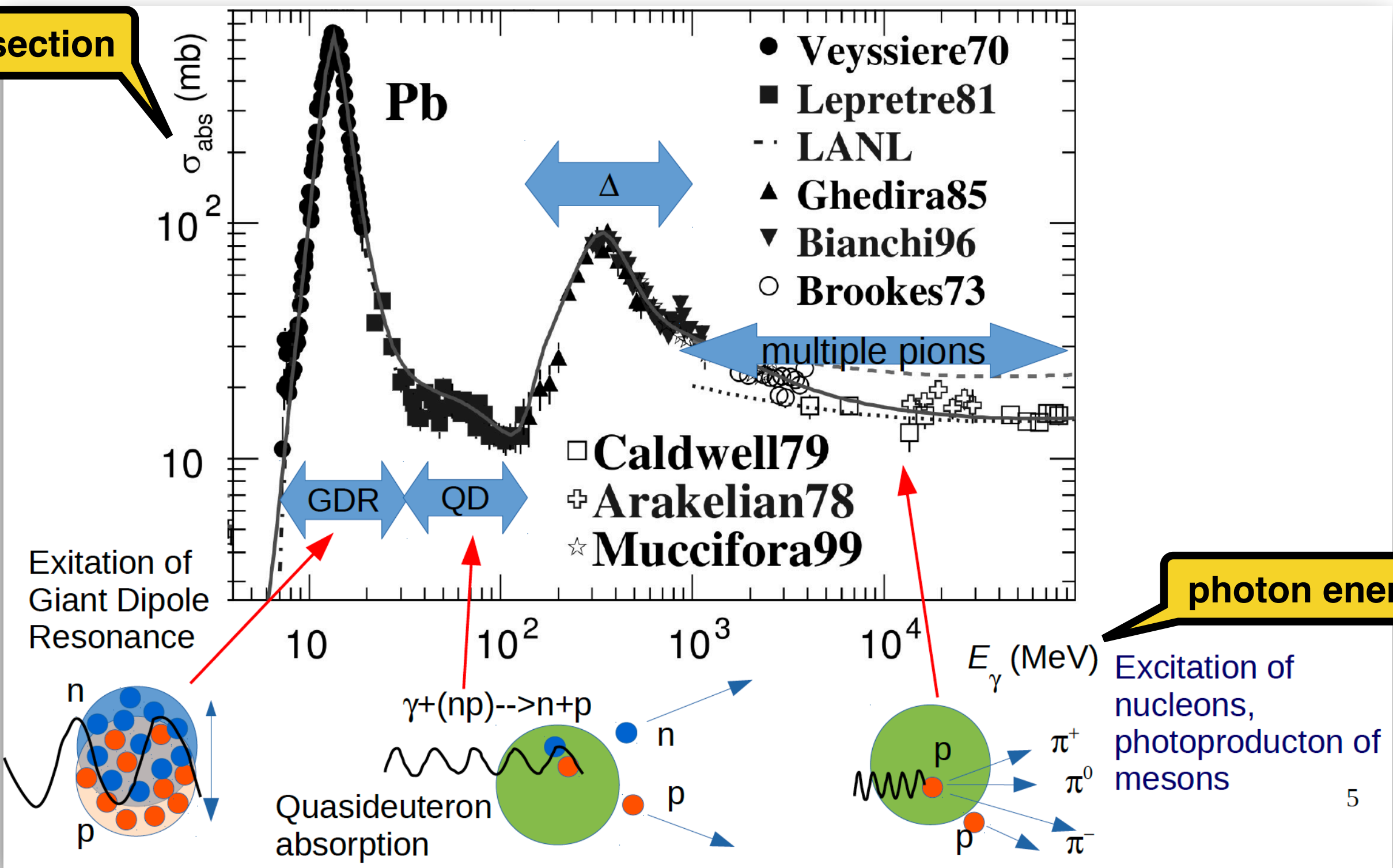
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$\sim(10)$ MeVs (in target rest frame) needed to excite the GDP

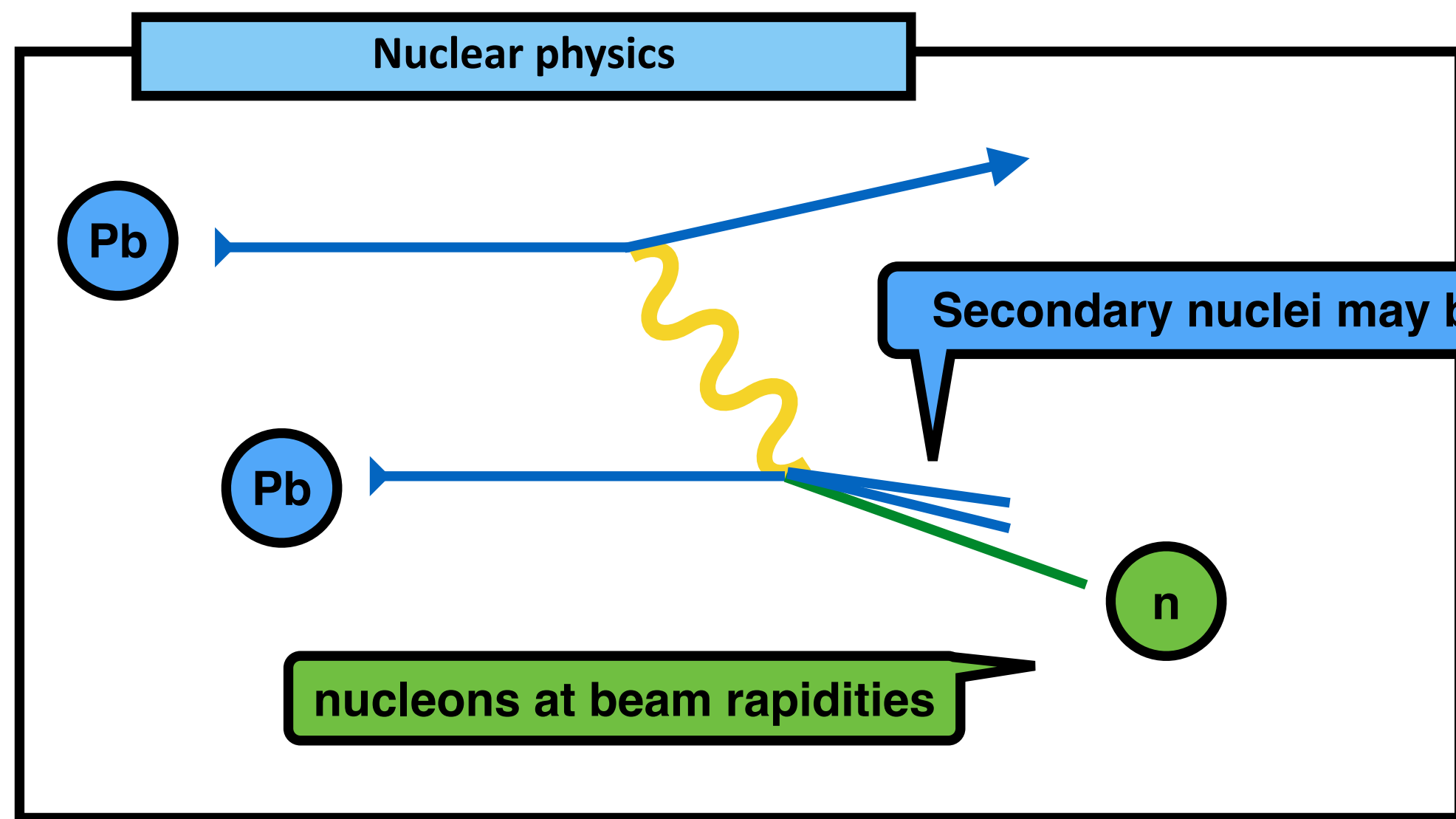
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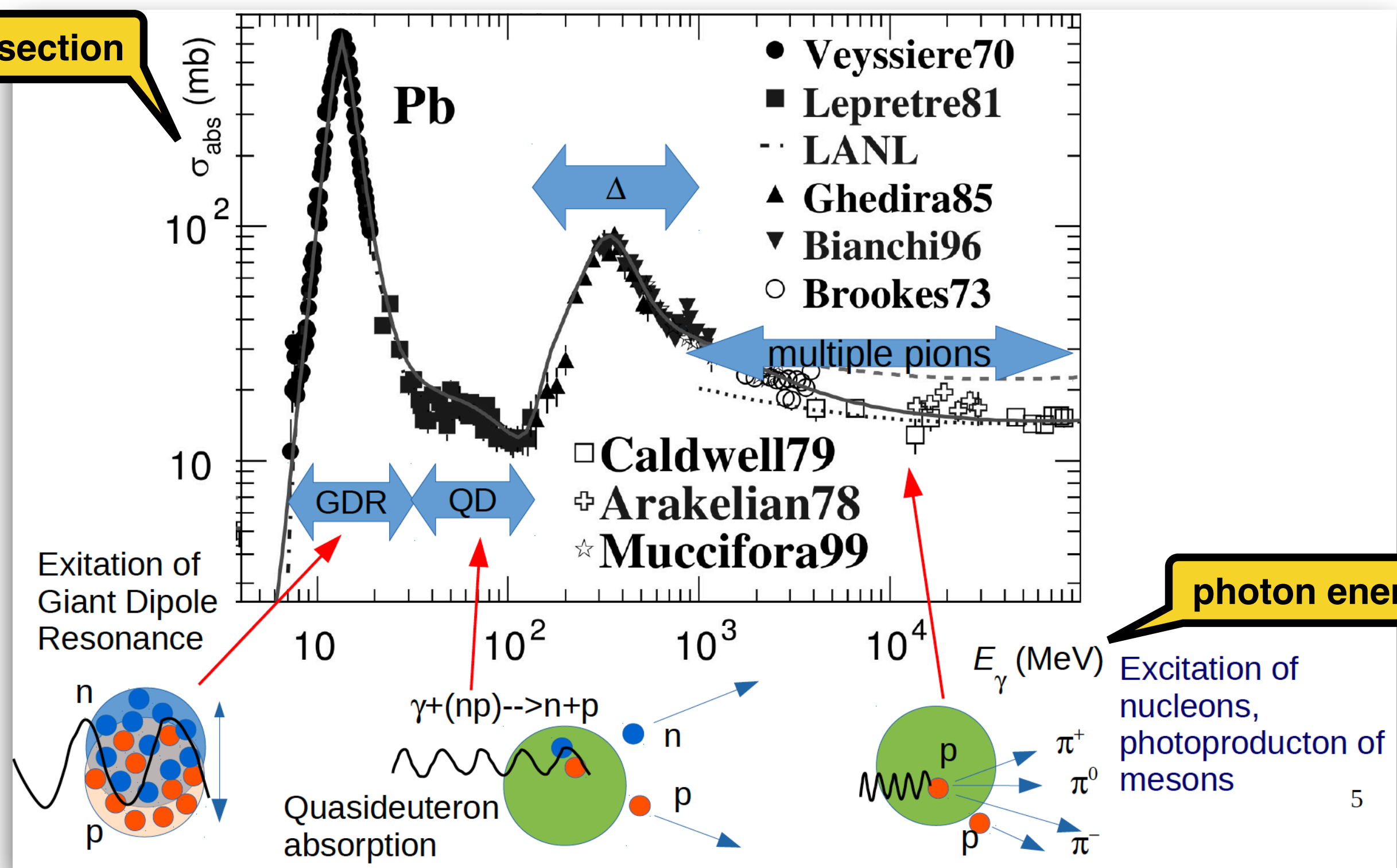


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cross section



~ 10 MeVs (in target rest frame) needed to excite the GDP

This process can be used to select small impact parameters

photon energy

At larger photon energies, charged particles are produced: may affect the efficiency of vetos at forward rapidities

Flux including EMD in n00n

Use data to describe the neutron emission in EMD processes to tag different impact-parameter ranges

Flux including EMD in nOOn

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UPC of process P with EMD

$$\sigma(AA \rightarrow PA'_i A'_j) \propto \int d^2\vec{b} P_P(b) P_{ij}(b) \exp(-P_H(b)),$$

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Two one-neutron or one two-neutron emission

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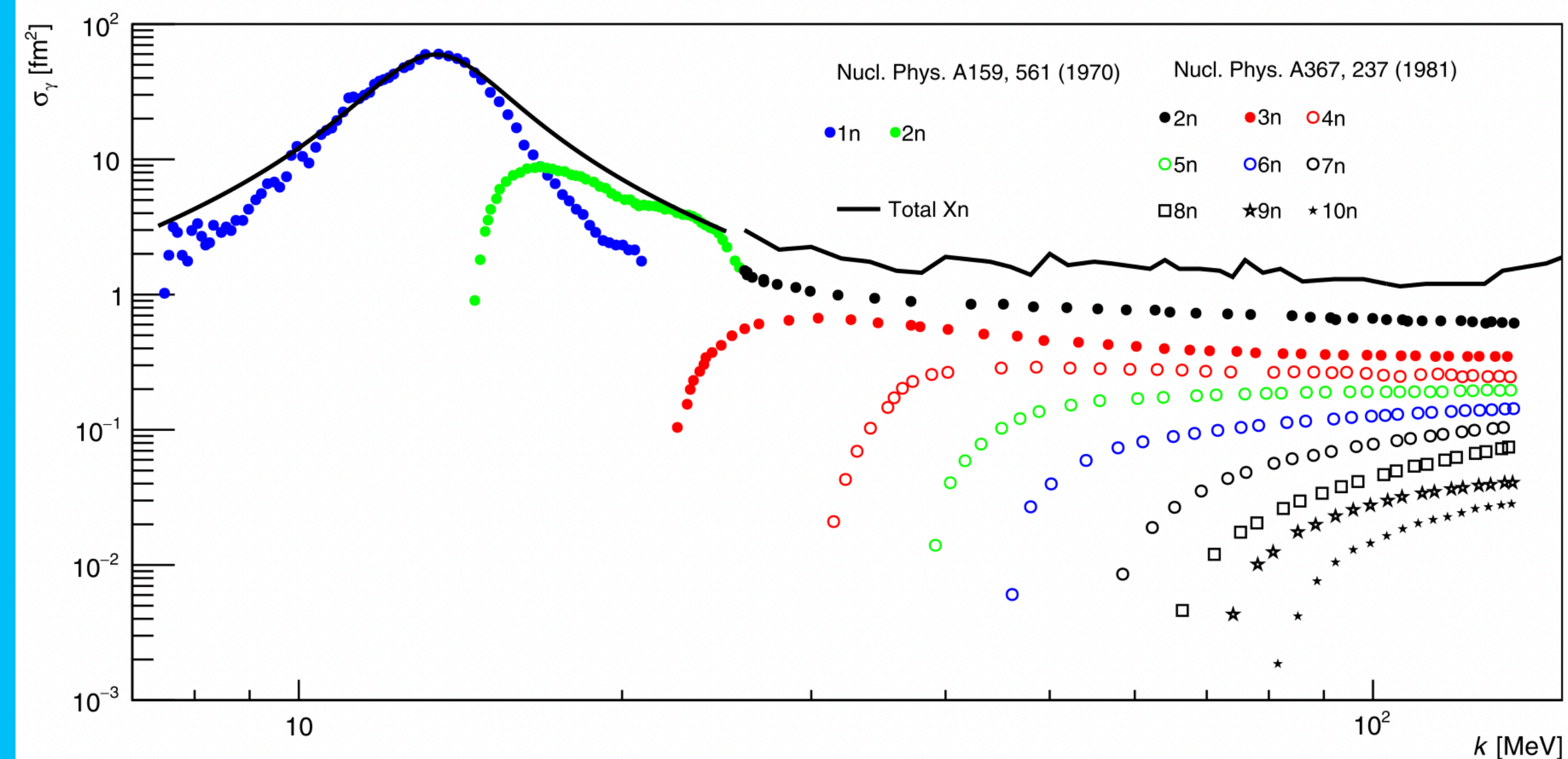
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Formalism fit to EMD data sets, e. g.



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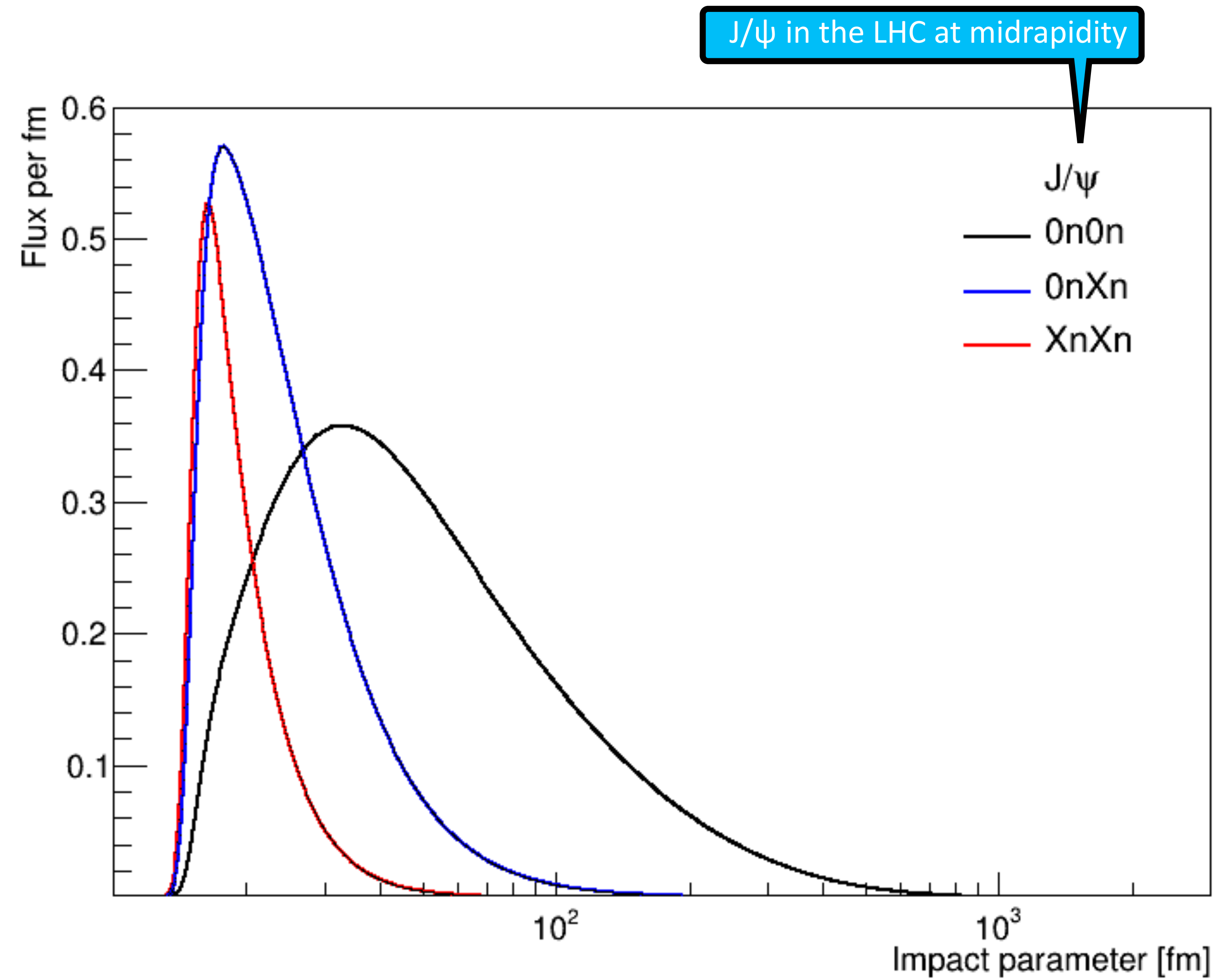
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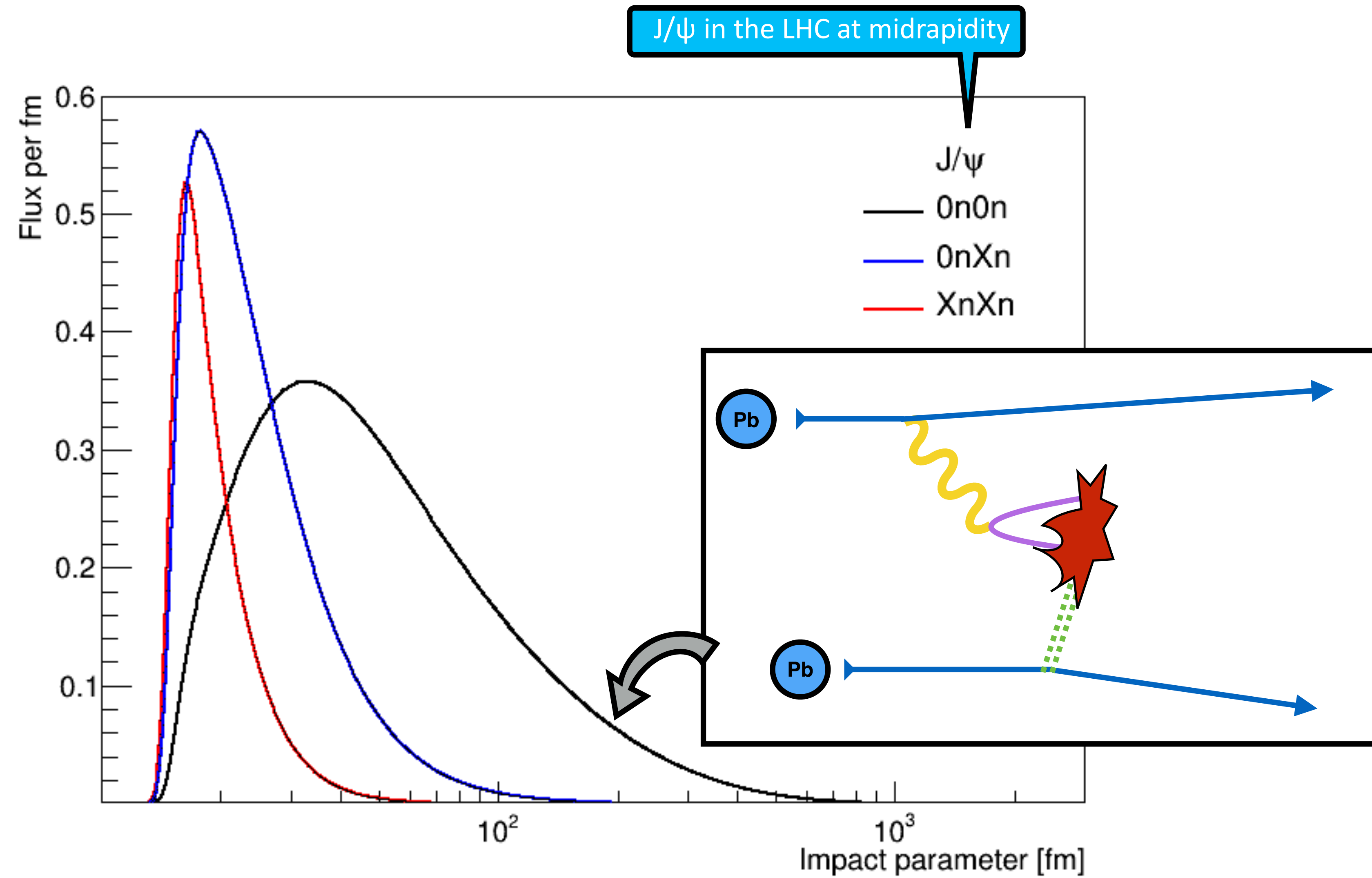
Example of impact-parameter dependence of the flux



Plot made with n00n, provided by Michal Broz

Guillermo Contreras, CTU in Prague

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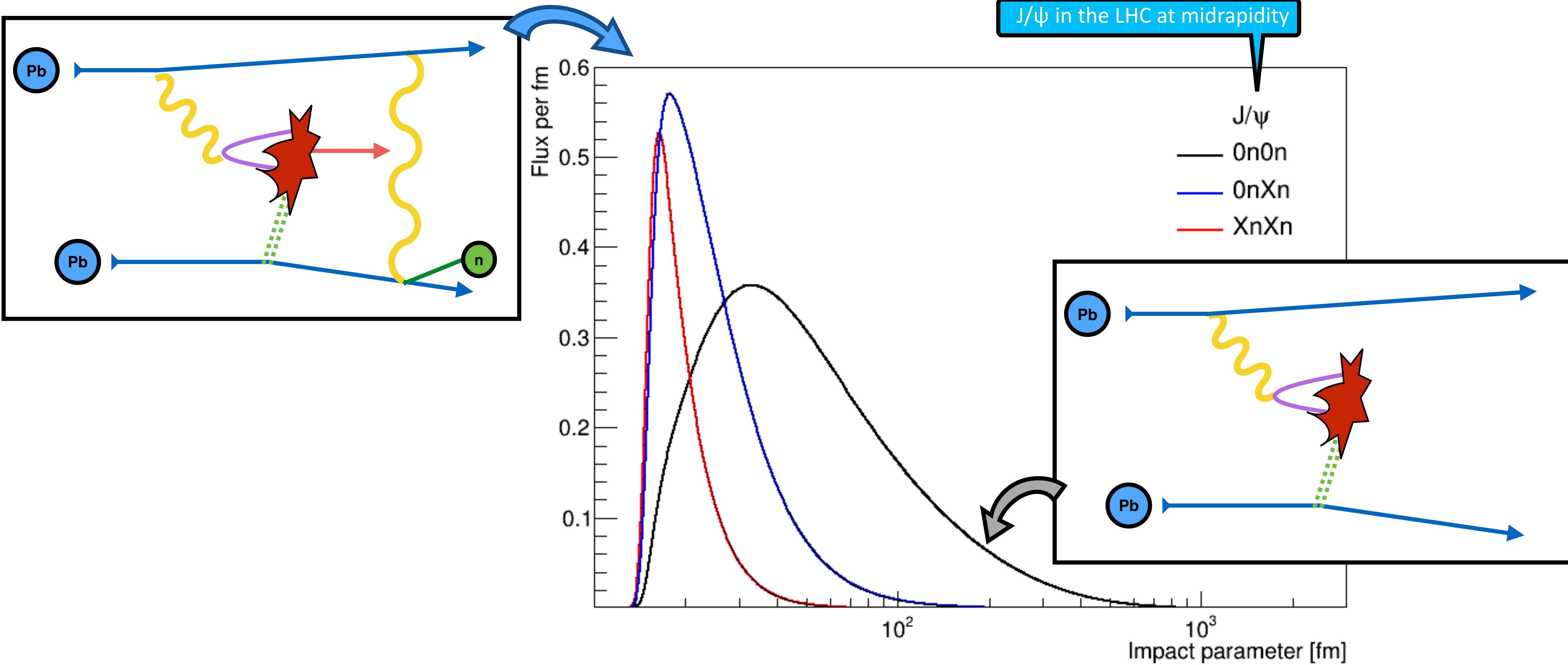


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J/ ψ in the LHC at midrapidity

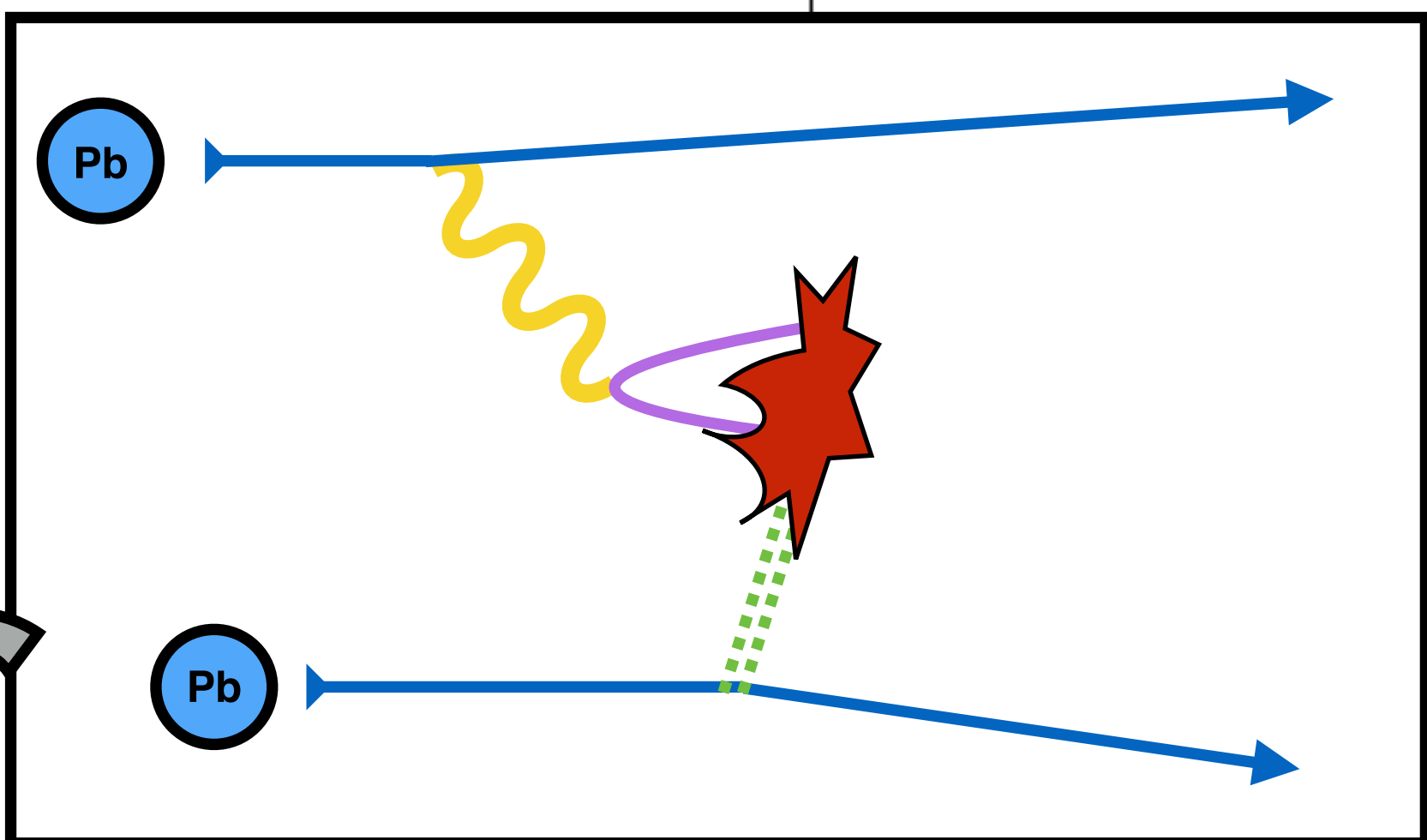
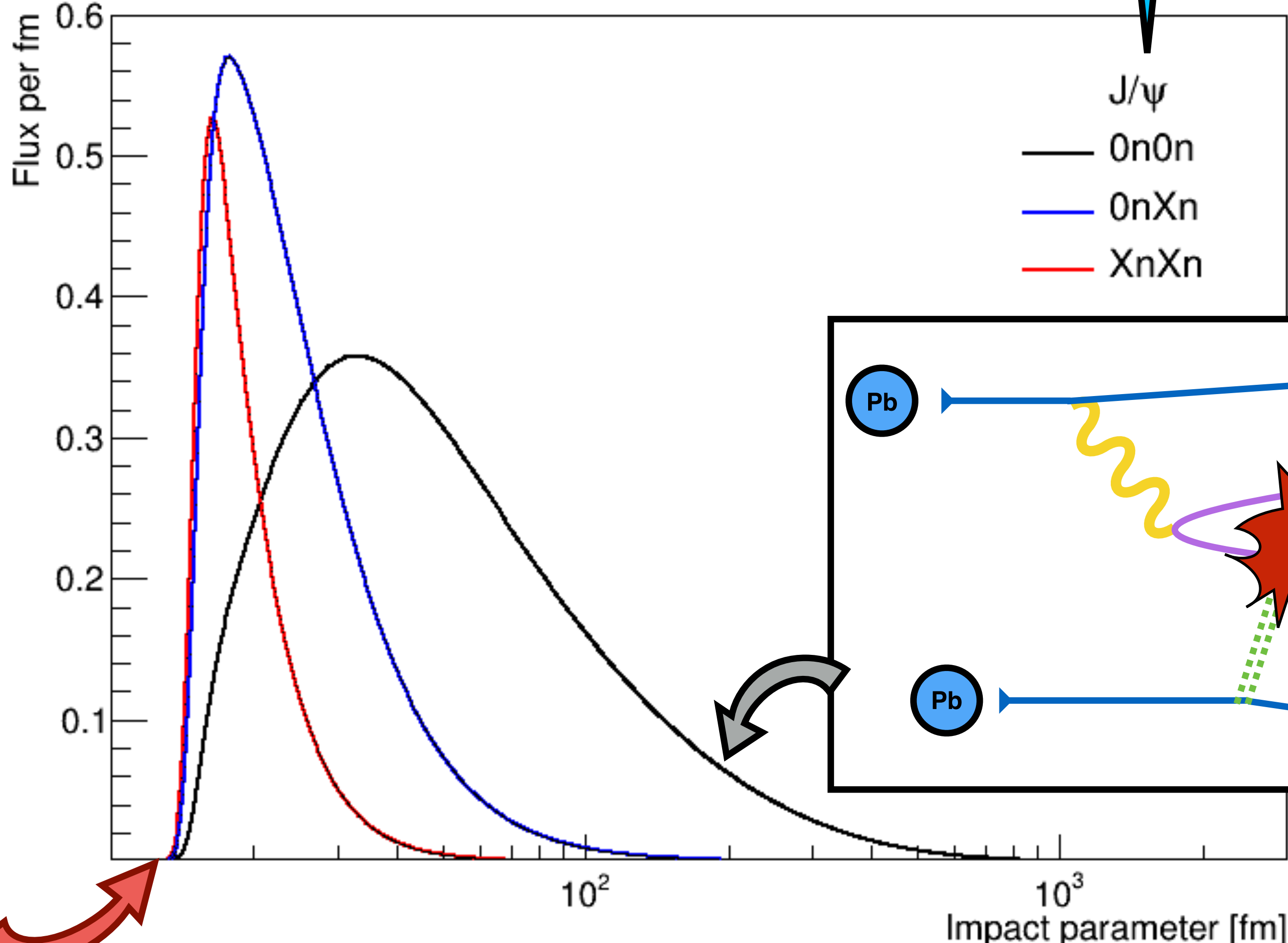
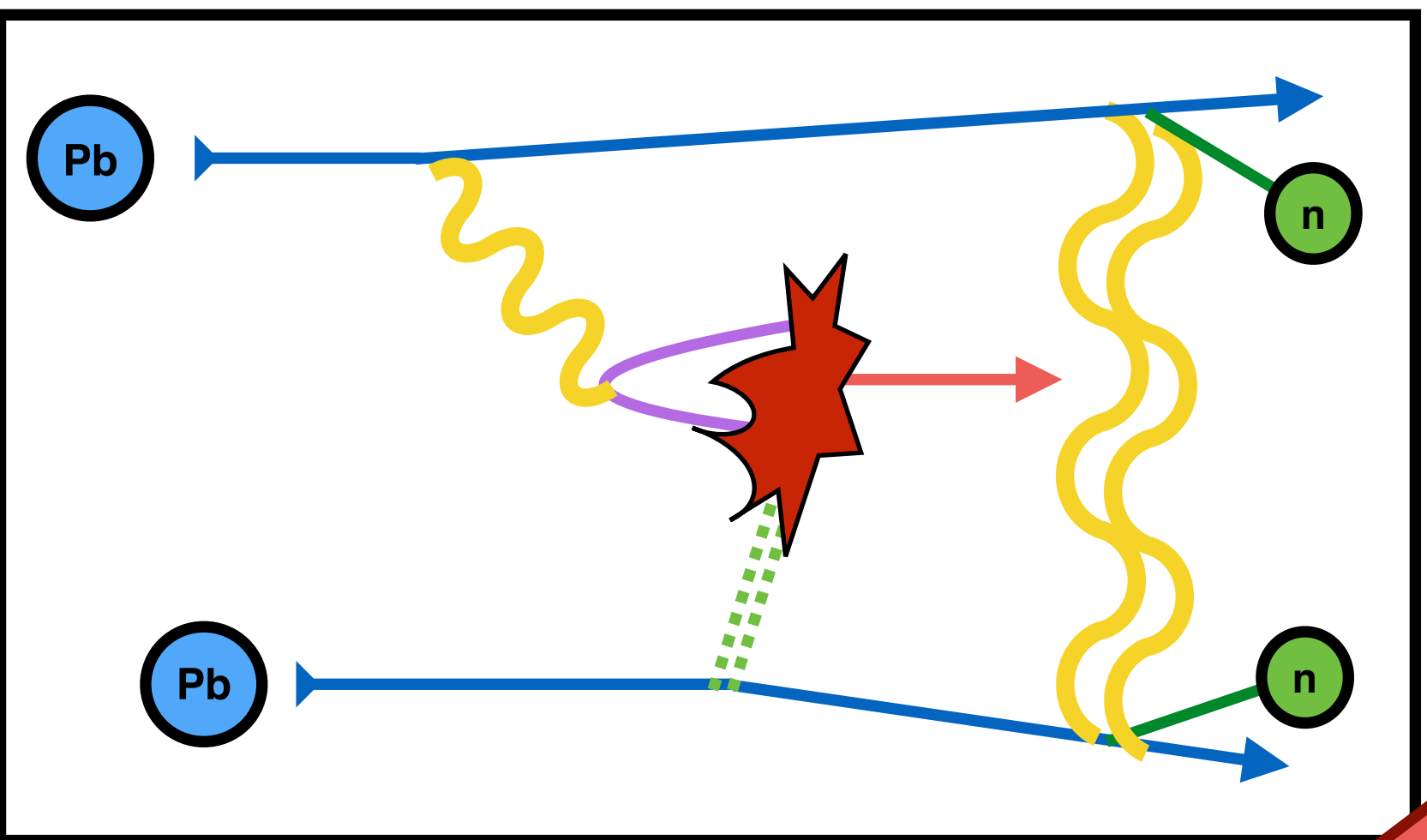
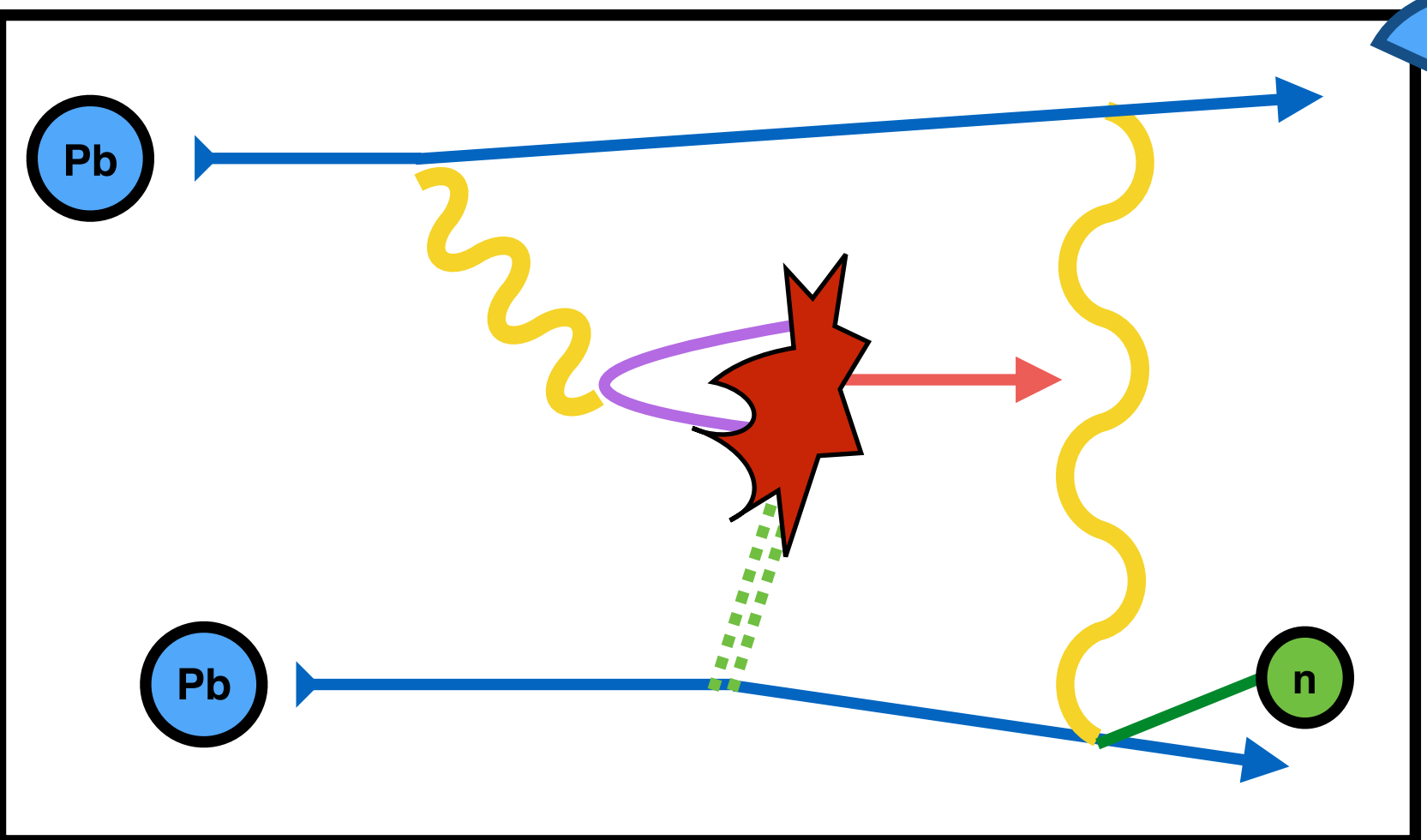


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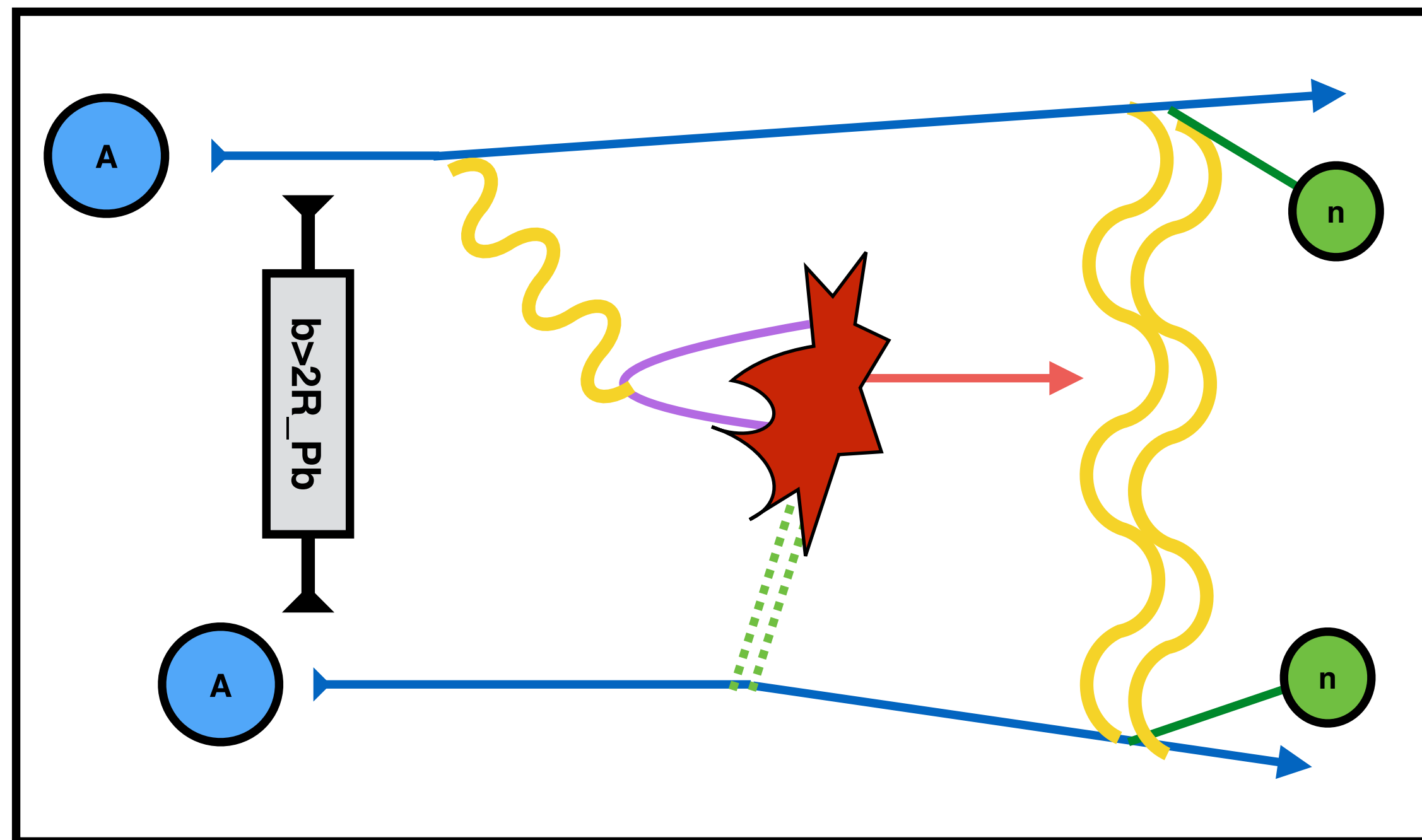


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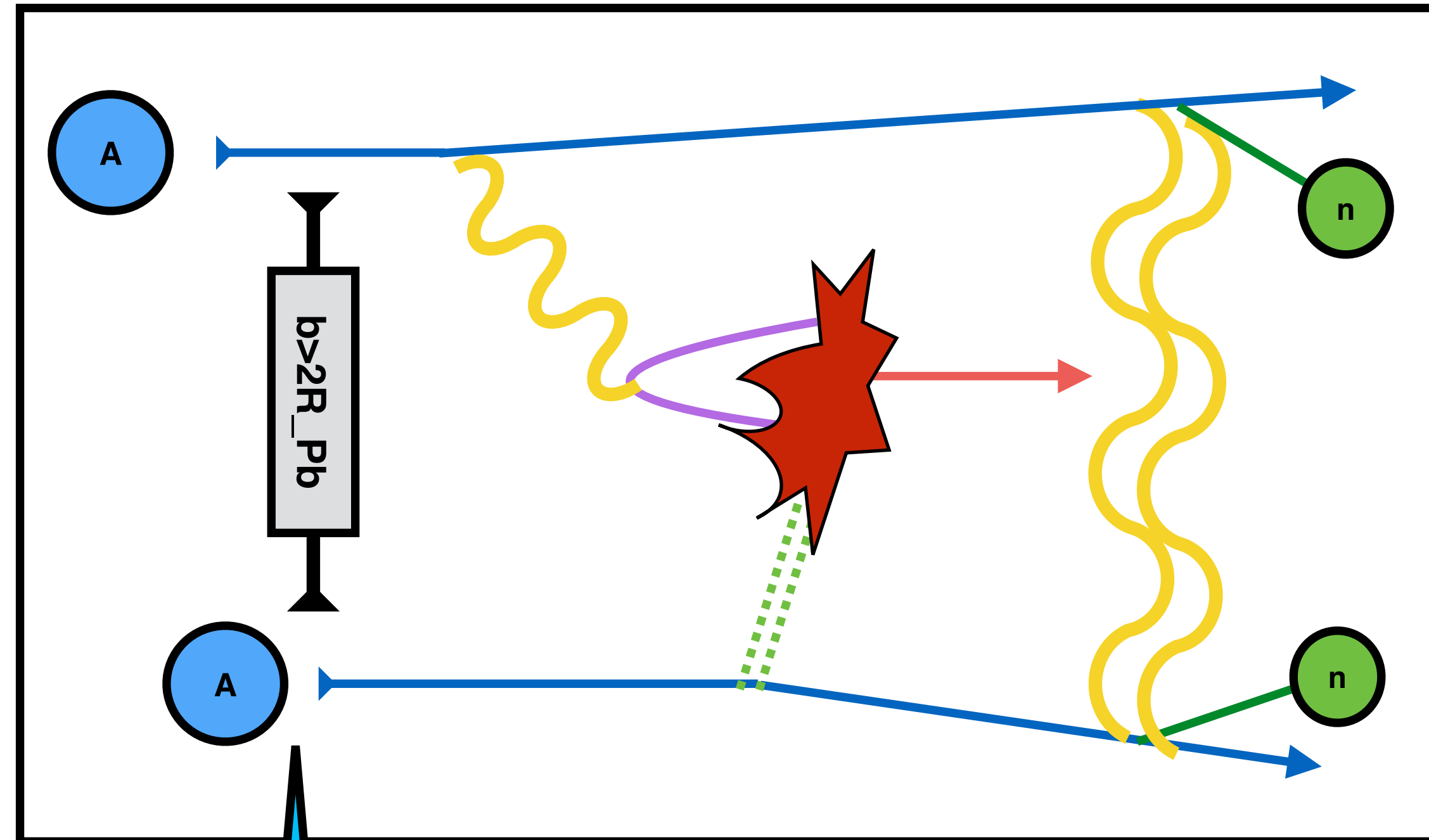
How to find photon-induced interactions in hadron colliders (4/4)

Sometimes, for exclusive diffractive observables in UPC an overlap with EMD is required in the trigger



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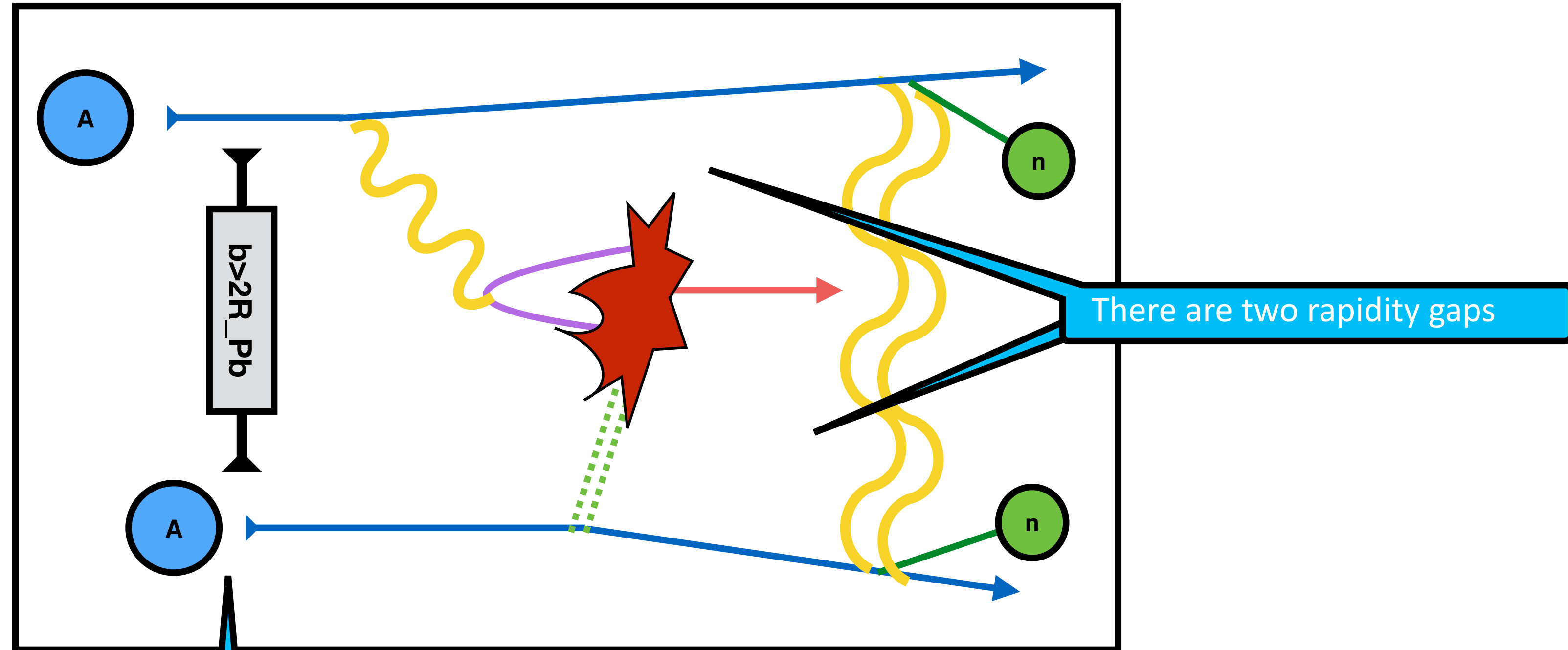
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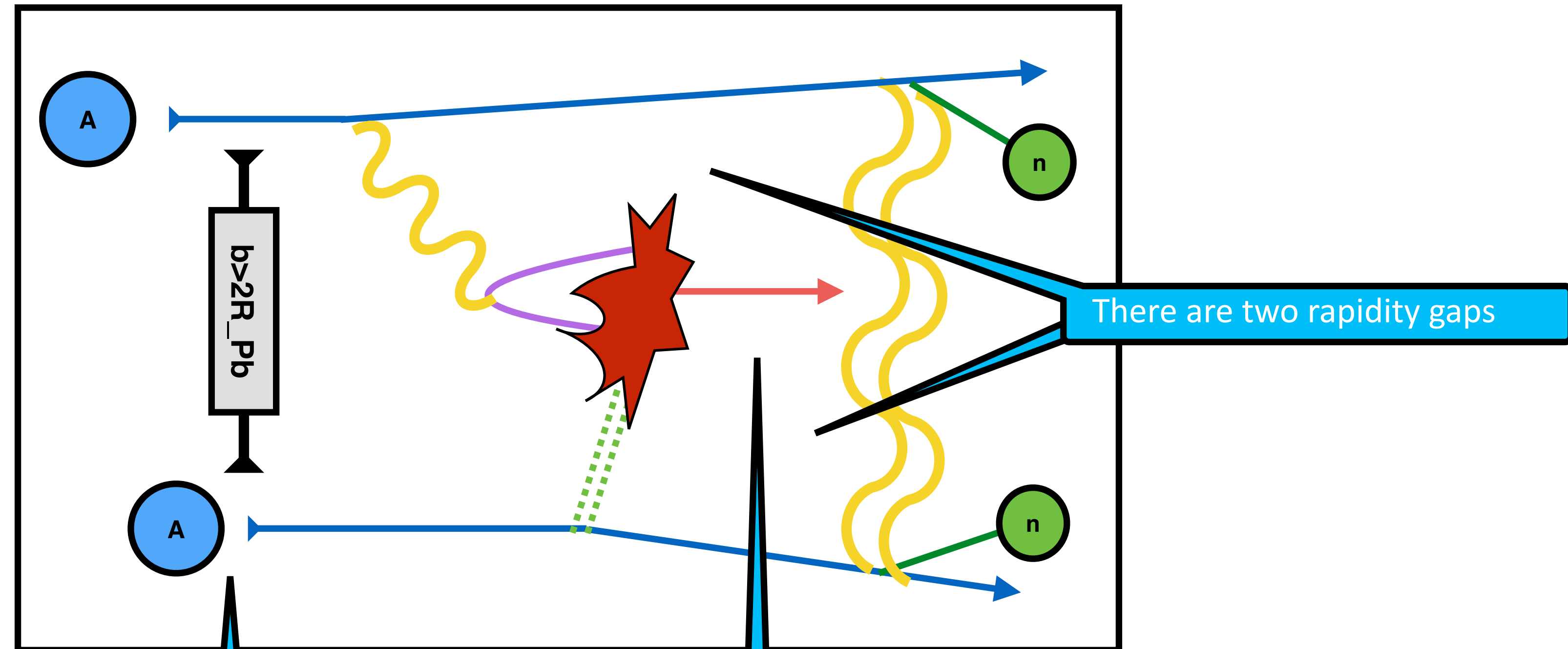
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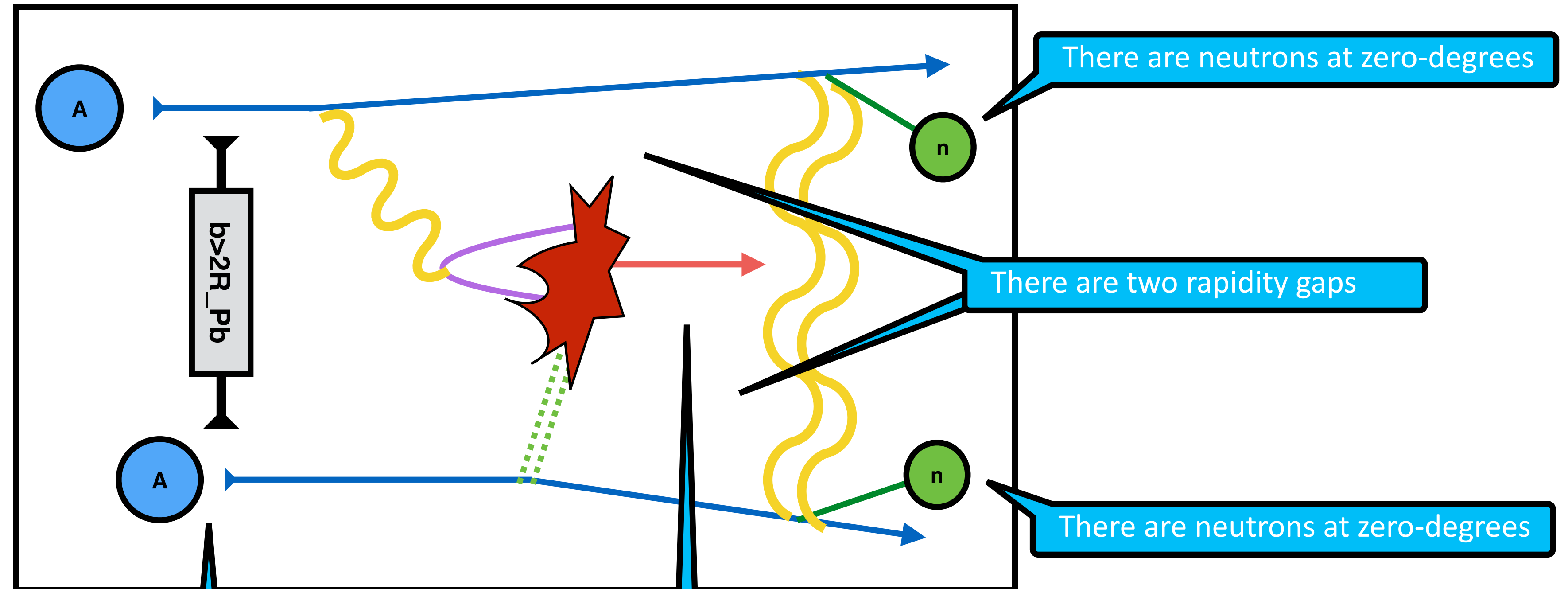
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There are two rapidity gaps

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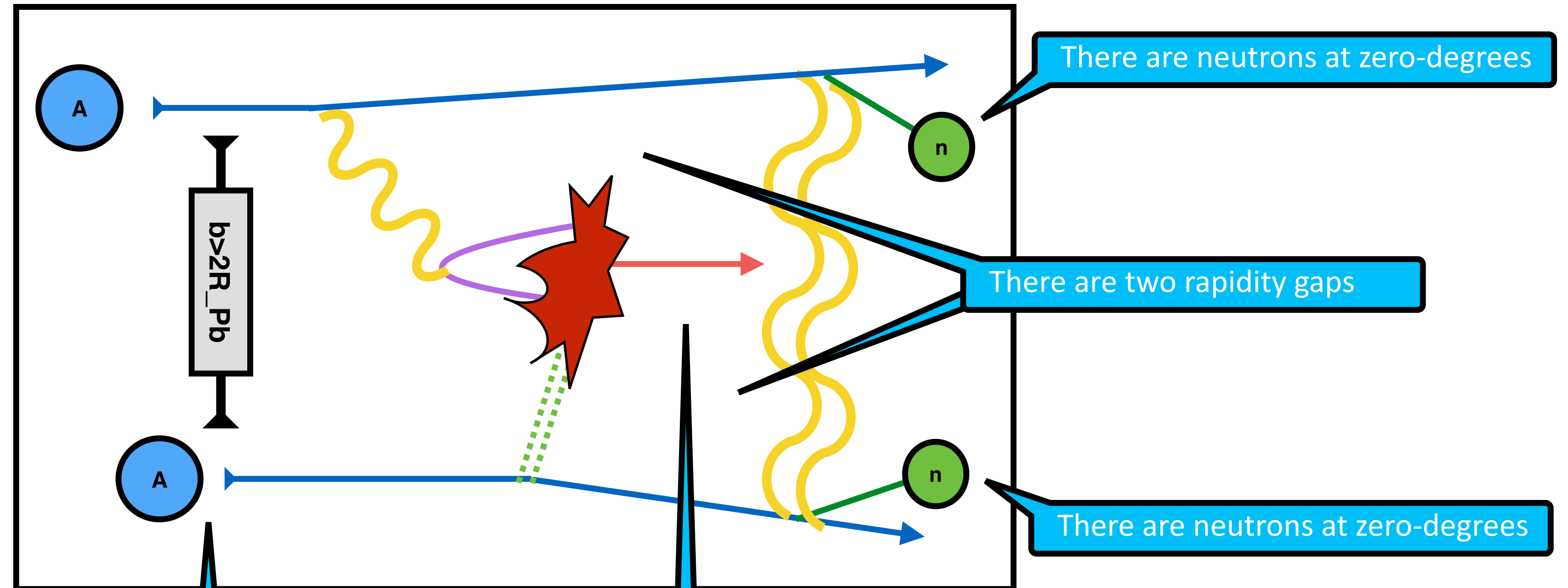
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For exclusive states in diffraction, the total transverse momentum is very small

The formalism to obtain the photon flux should be adapted to described the different types of photon induced processes

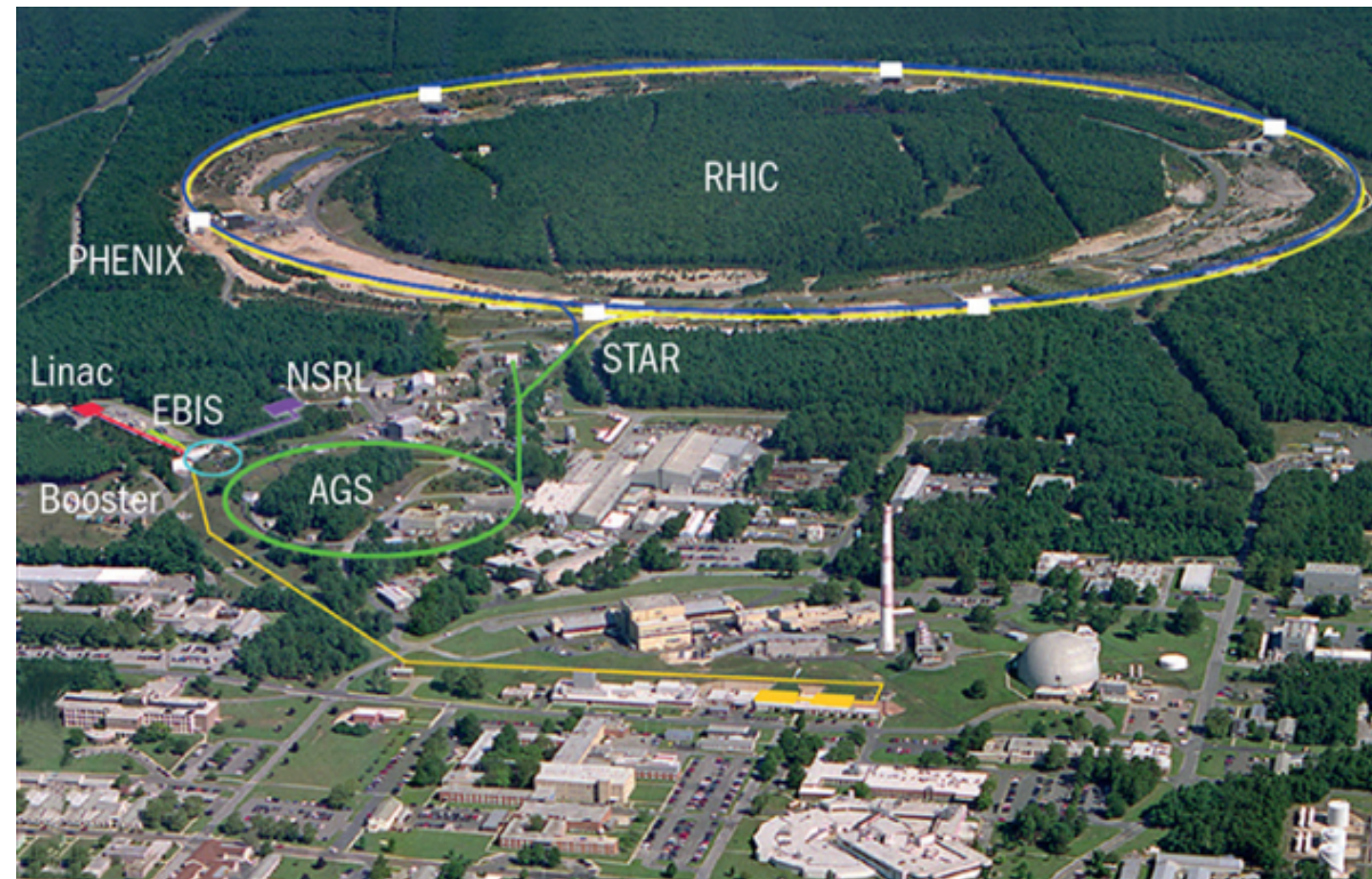
6

Exploring high-energy QCD with nuclei at RHIC and LHC

Heavy ions have more gluons and in a denser environment than protons which makes them ideal candidates to search for saturation effects

But other effects, like shadowing may complicate the search

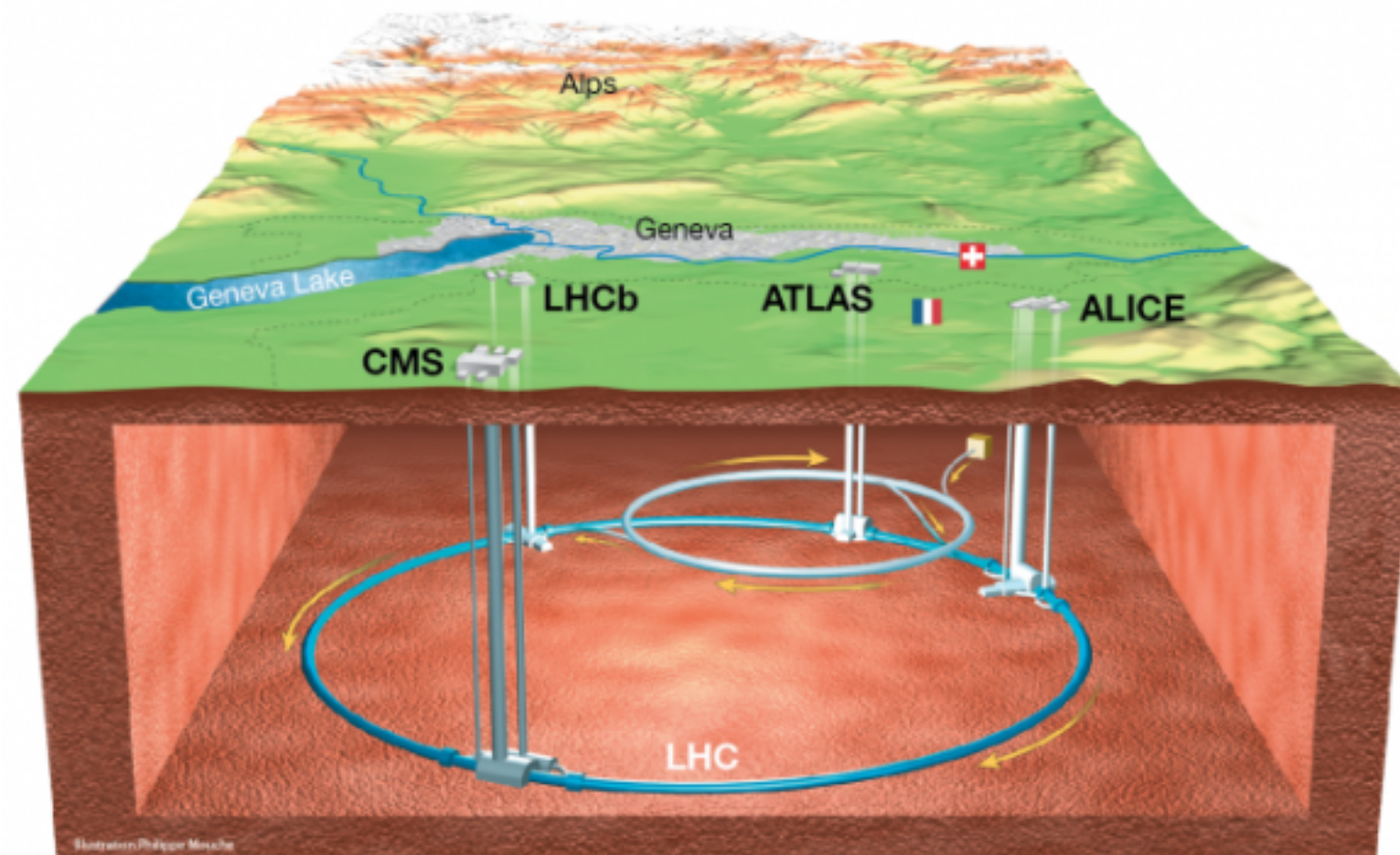
RHIC and the LHC



Credit: BNL

Relativistic heavy ion collider (RHIC)
Located in USA
3834 m of circumference
Operating since 2000
2 independent beams
Can accelerate different ions
Reaches collisions at 200 GeV (per NN) for AuAu

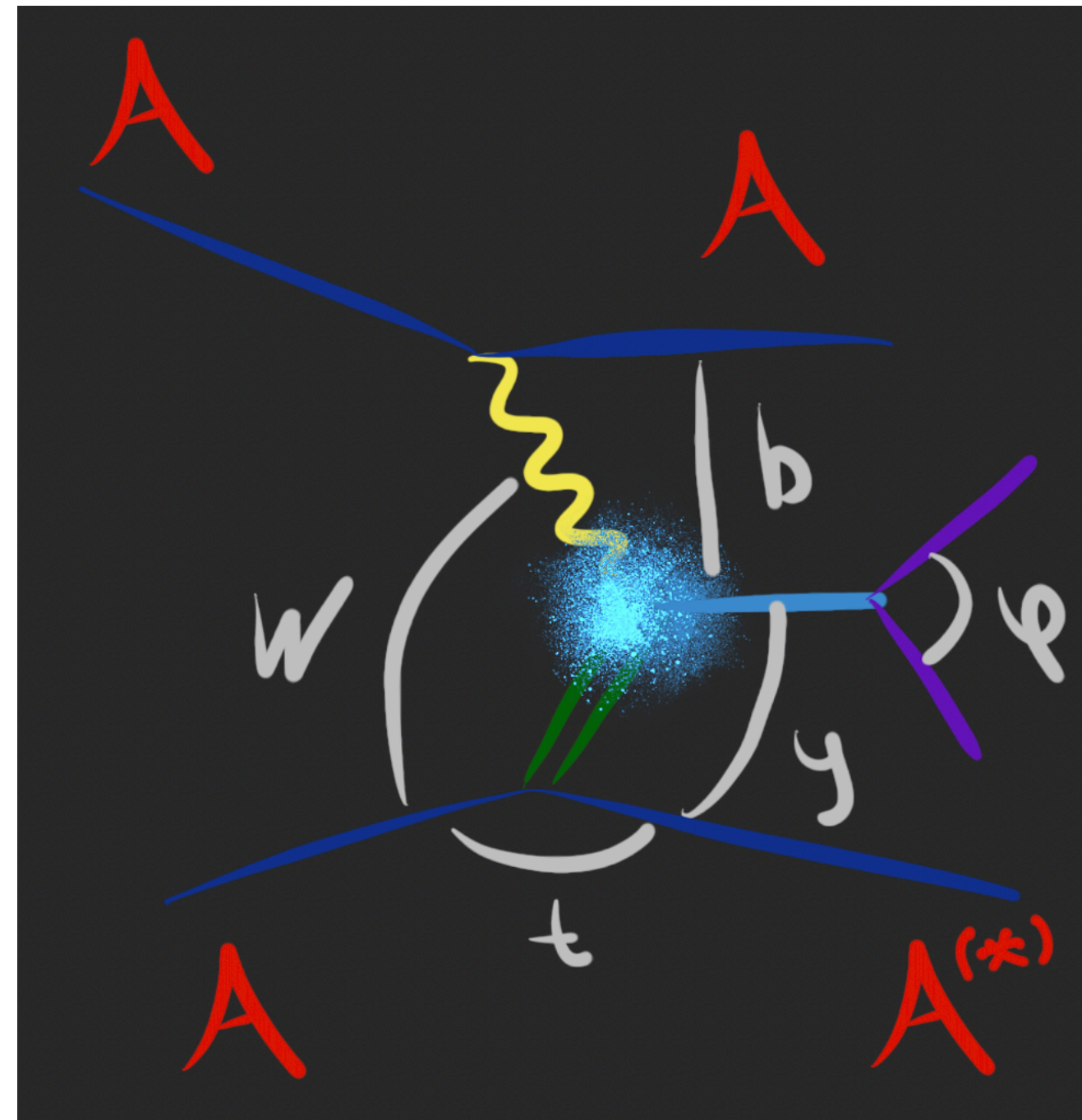
Both facilities have a very rich heavy-ion program



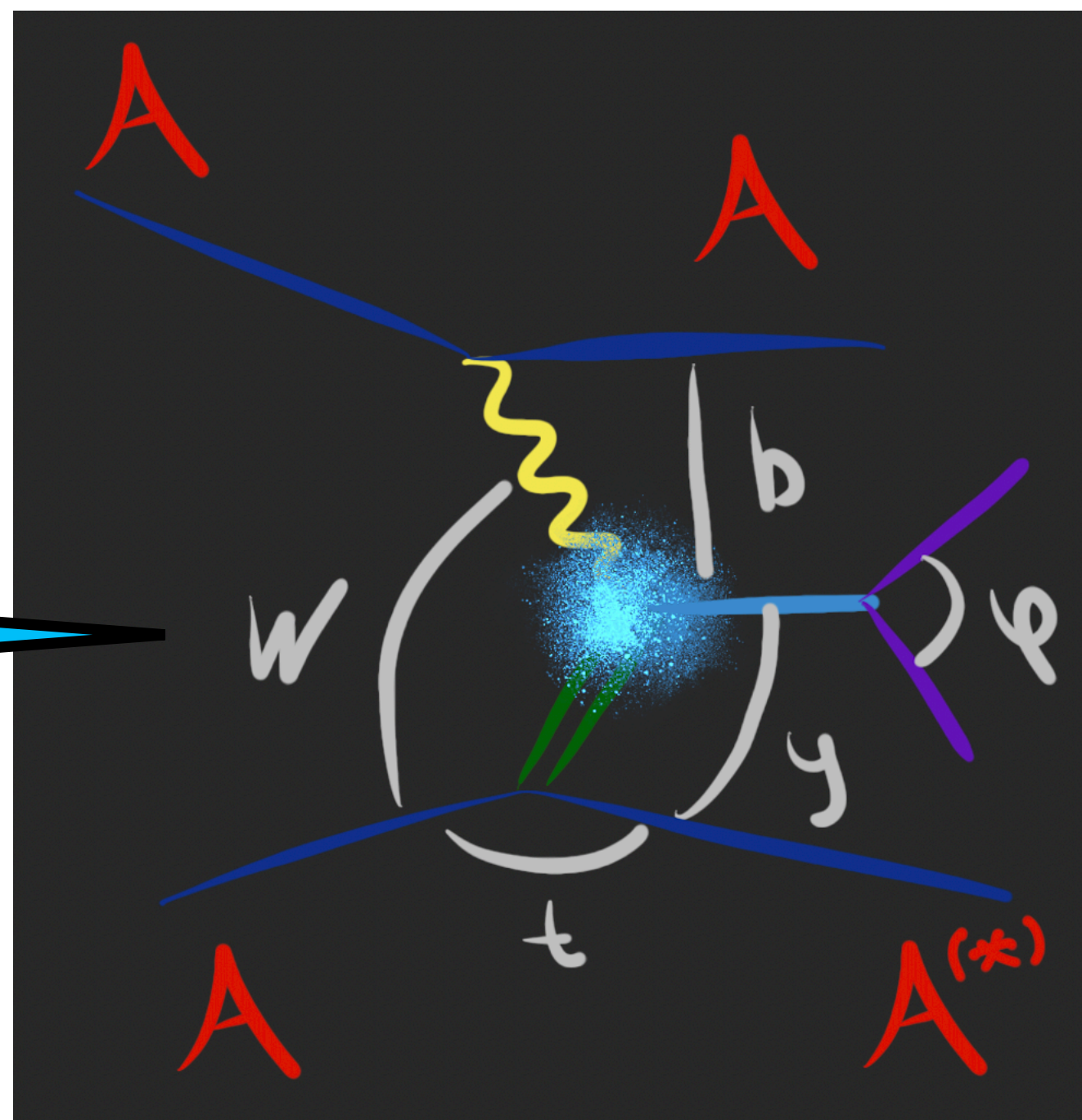
Credit: CERN

Large hadron collider (LHC)
Located in Europe
27 km of circumference
Operating since 2010
Has reached collisions at 5.36 TeV (per NN) for PbPb

There are many results, so I will concentrate on the possibilities offered by diffractive vector meson production
I will review only a few results, you will hear a lot more about this during the conference



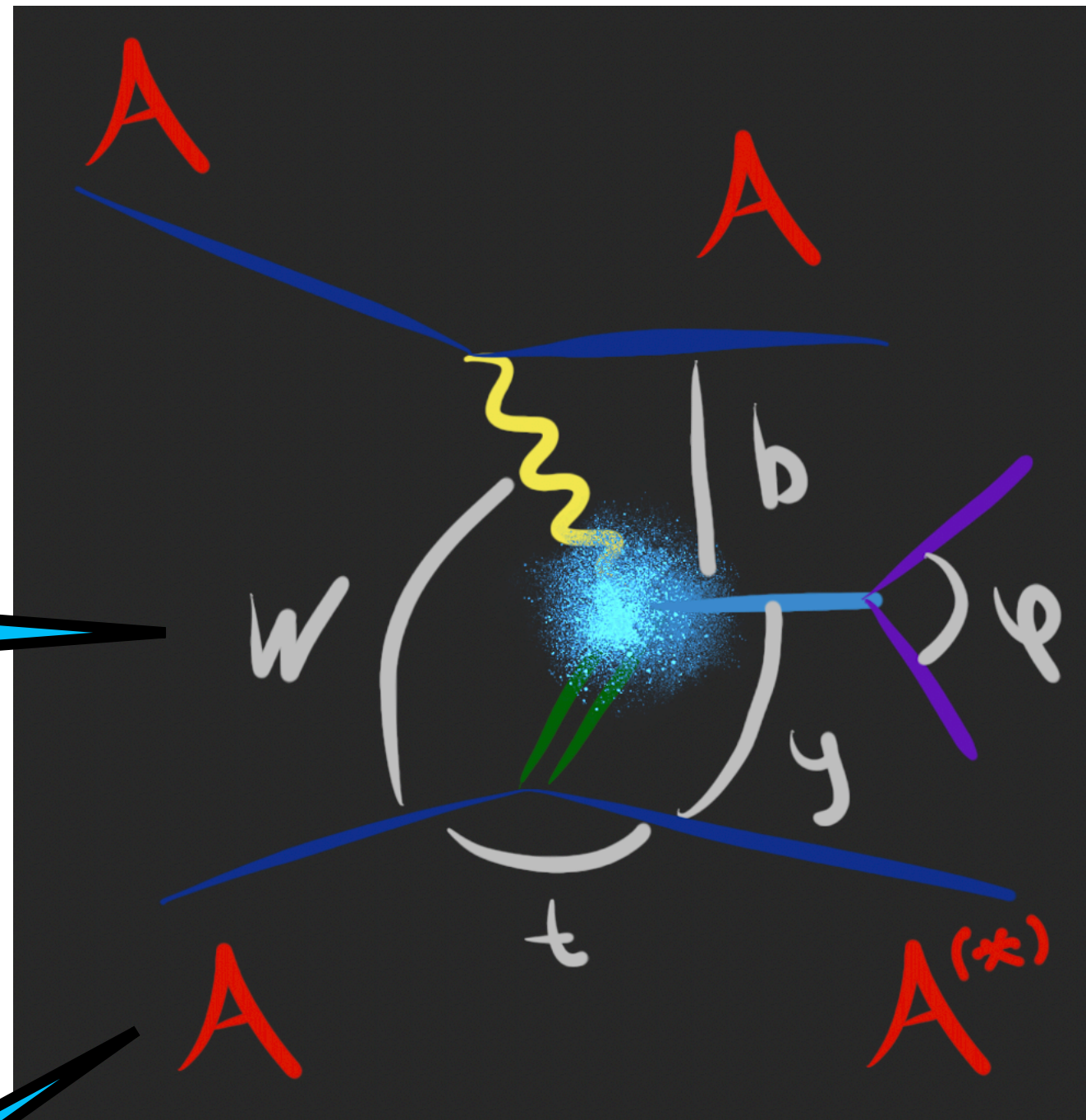
The energy dependence, gives the Bjorken-x evolution of the target



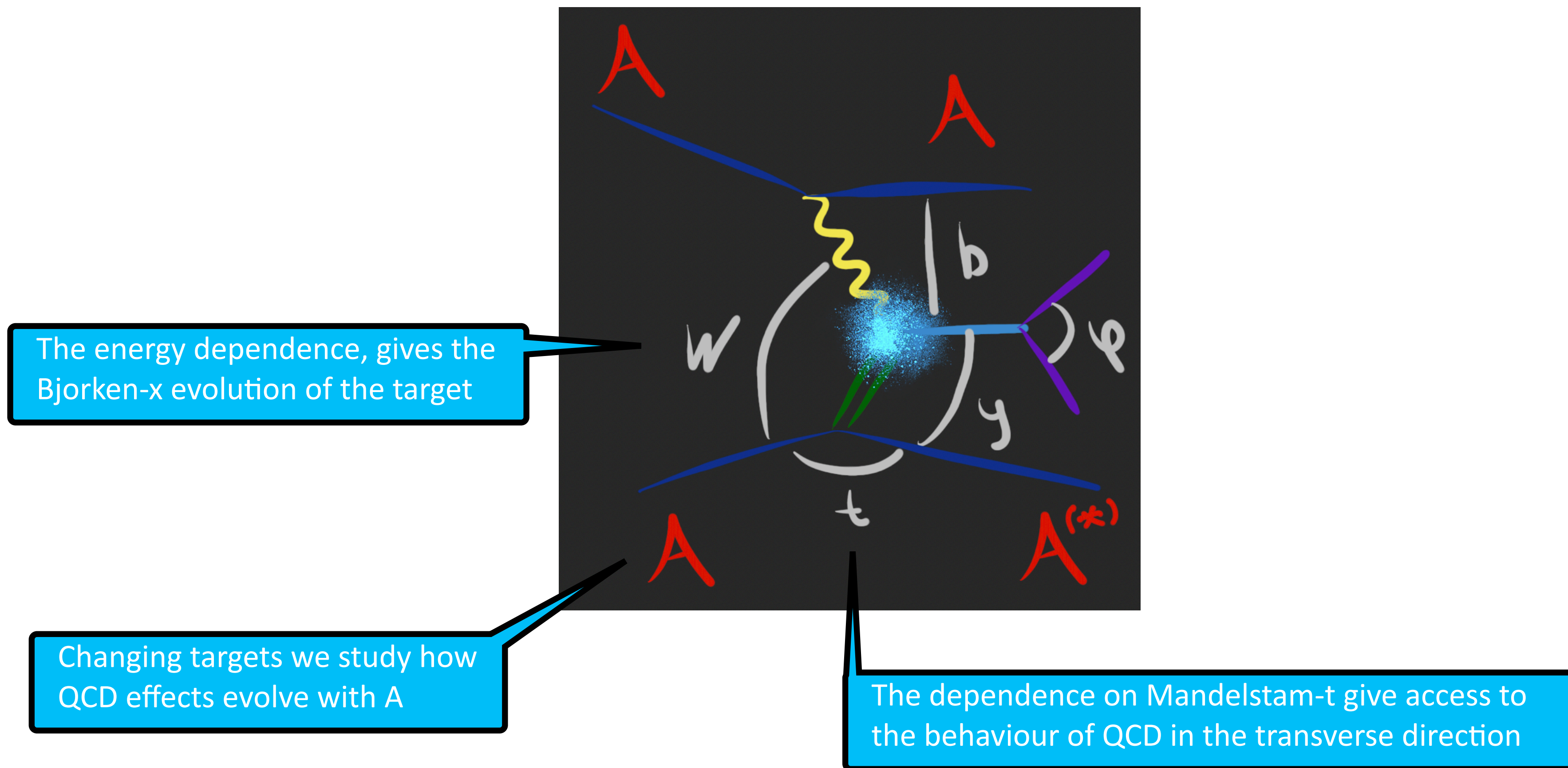
Diffractive vector meson photoproduction: a Swiss army knife for QCD (1/2)

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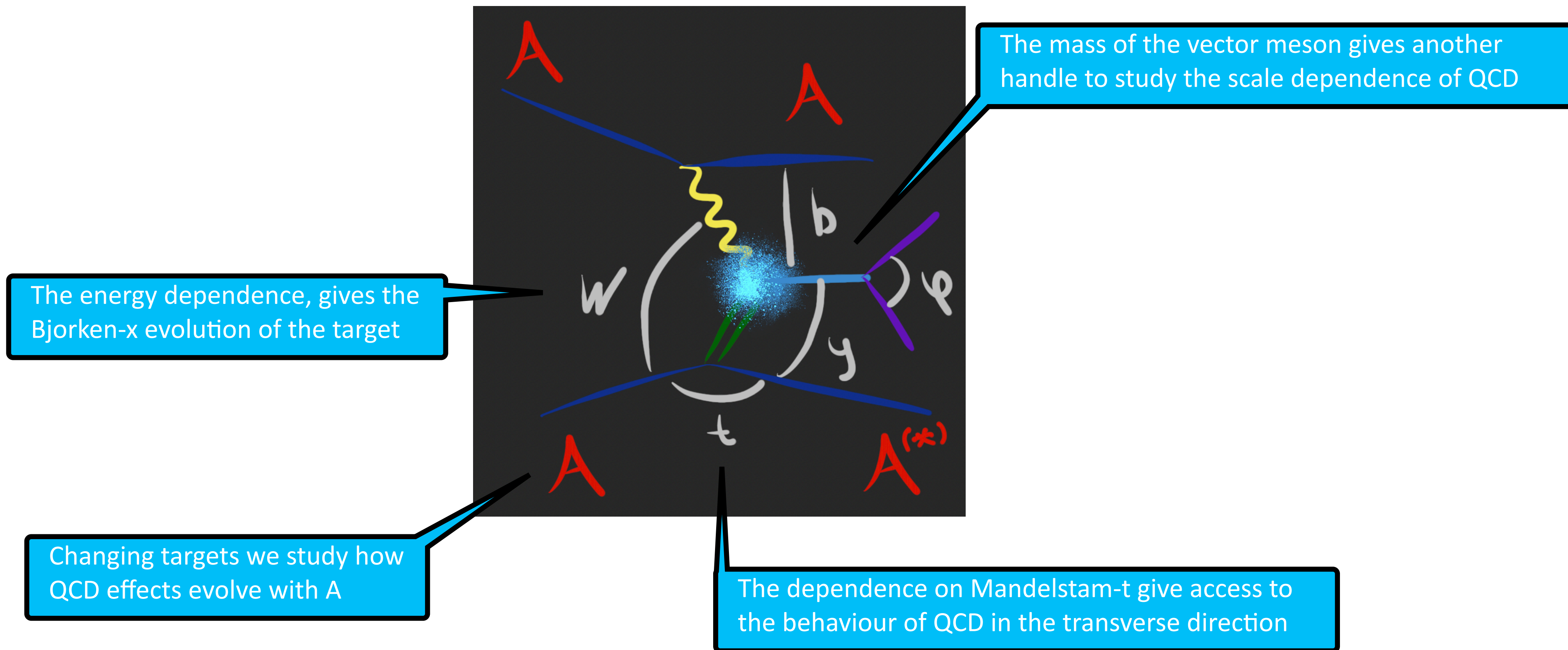
Changing targets we study how QCD effects evolve with A



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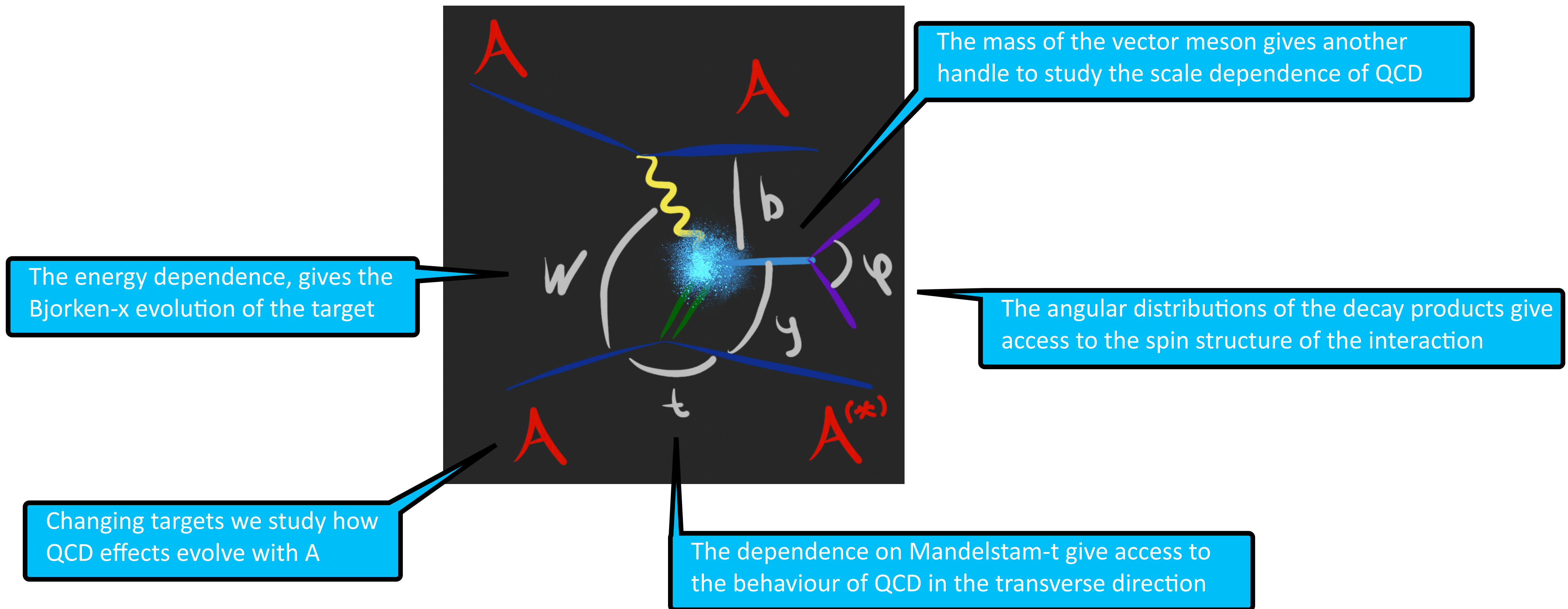
The energy dependence, gives the Bjorken-x evolution of the target

The mass of the vector meson gives another handle to study the scale dependence of QCD

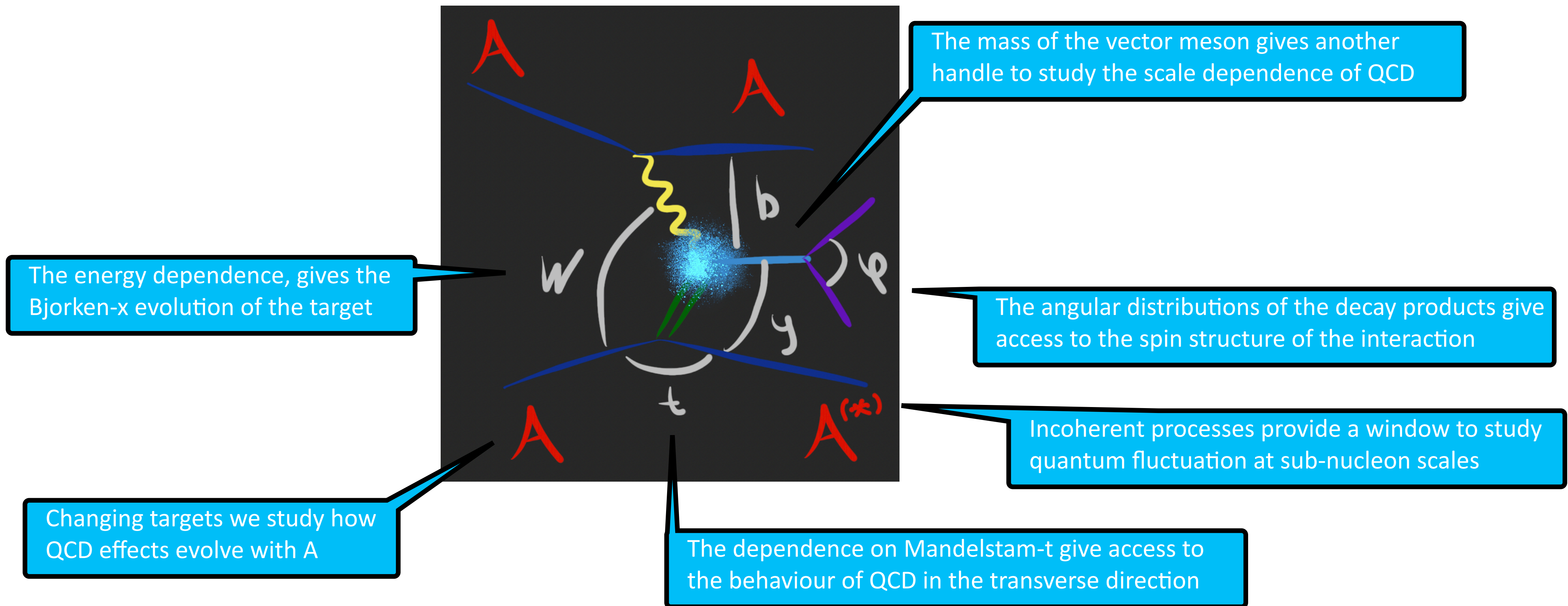
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The dependence on Mandelstam-t give access to the behaviour of QCD in the transverse direction

Diffractive vector meson photoproduction: a Swiss army knife for QCD (1/2)



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The impact-parameter dependence allows us to have independent and simultaneous measurements of the same process

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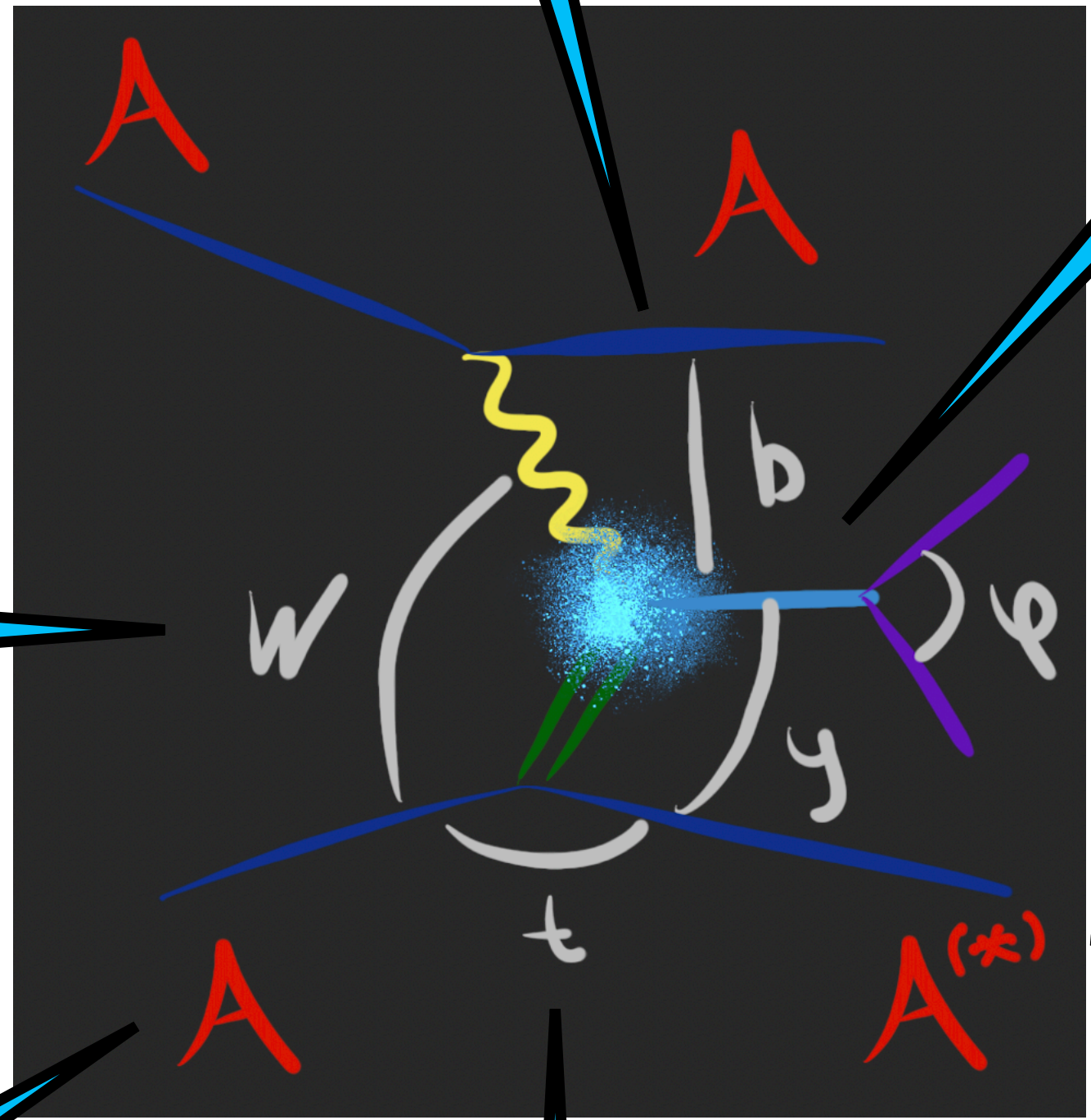
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The angular distributions of the decay products give access to the spin structure of the interaction

Incoherent processes provide a window to study quantum fluctuation at sub-nucleon scales

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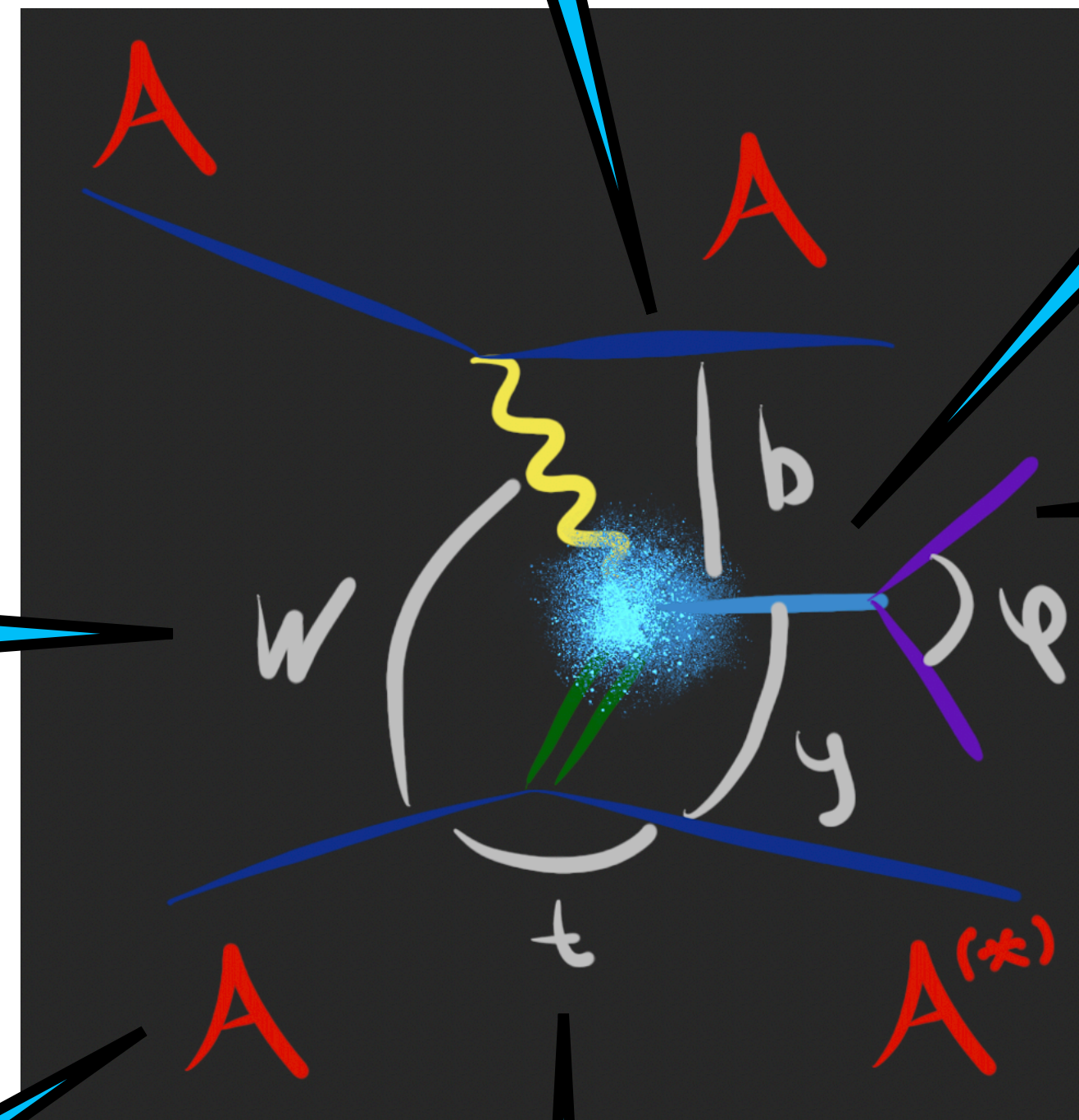
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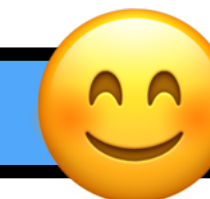
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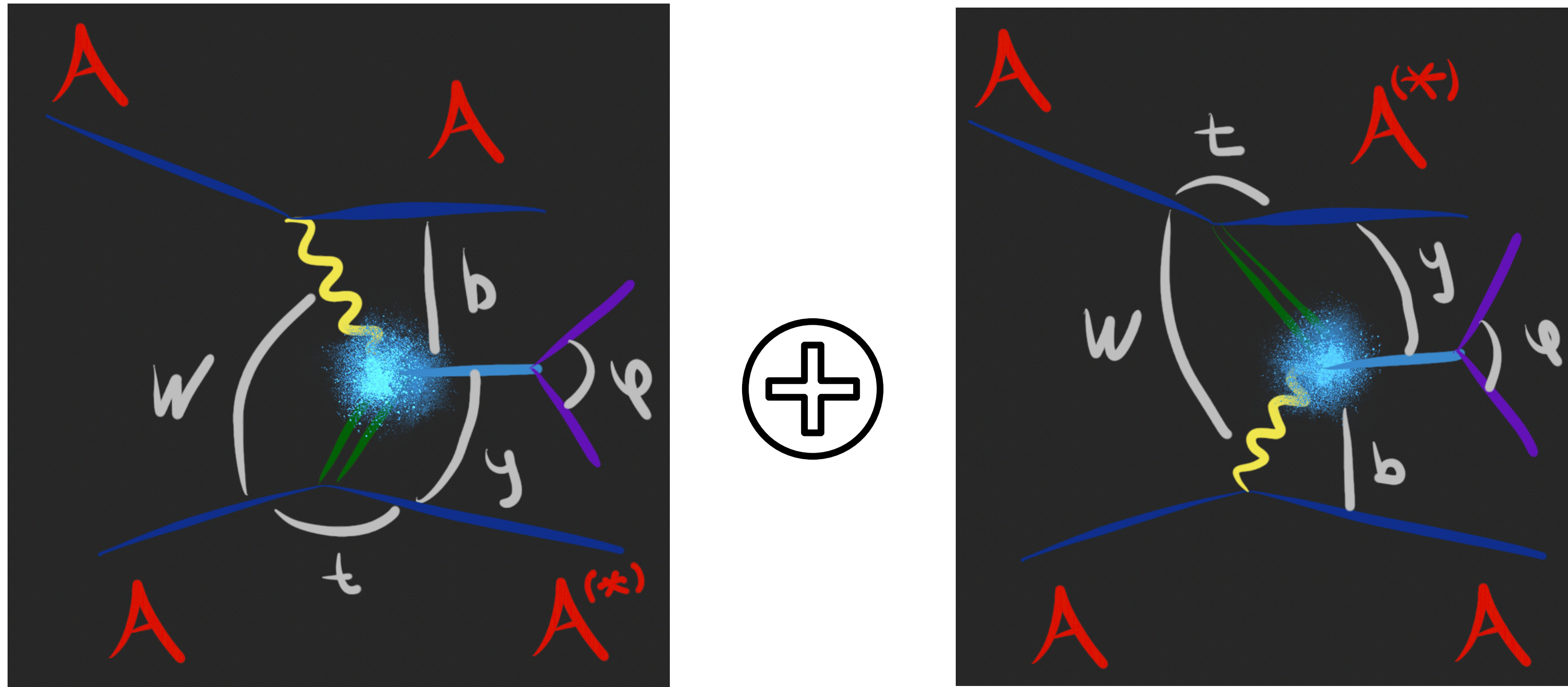
The dependence on Mandelstam-t give access to the behaviour of QCD in the transverse direction

All of these observables have been measure at RHIC+LHC



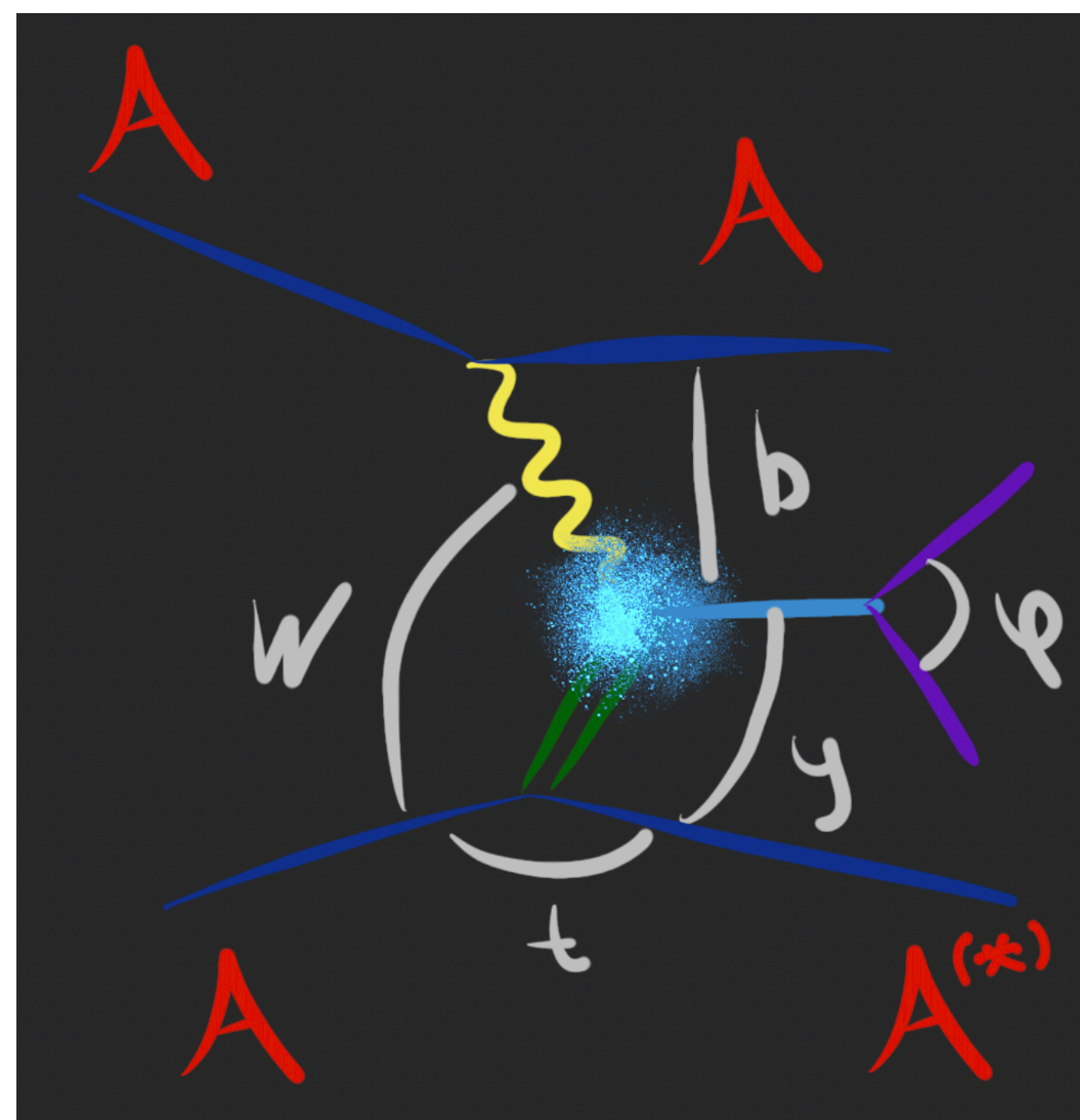
Diffractive vector meson photoproduction: a Swiss army knife for QCD (2/2)

The presence of two competing amplitudes allows for the study of QM interference effects at new scales

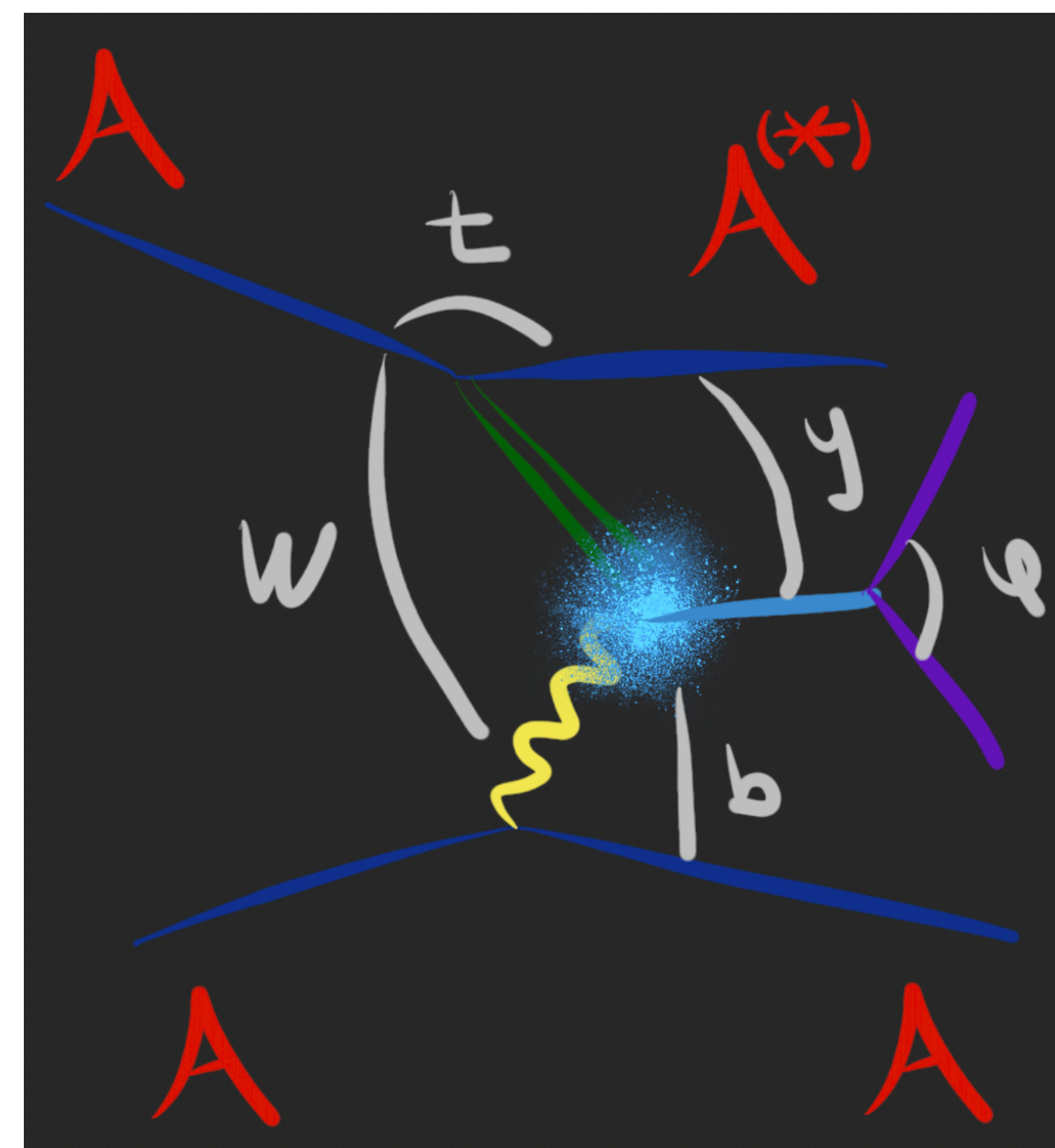


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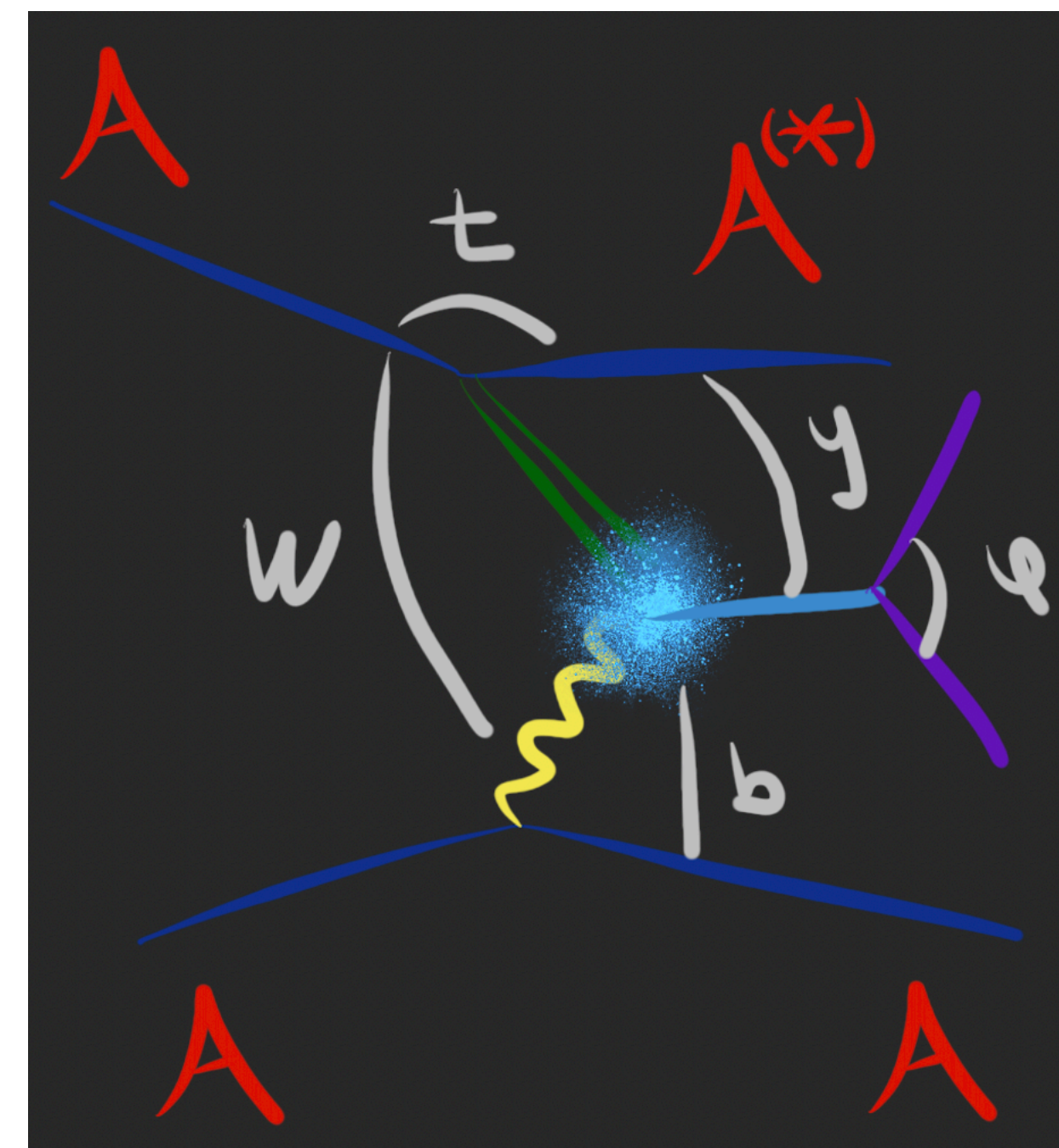
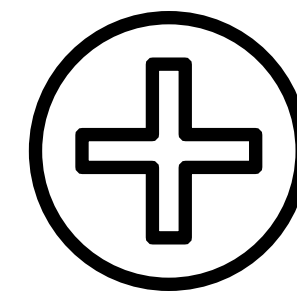
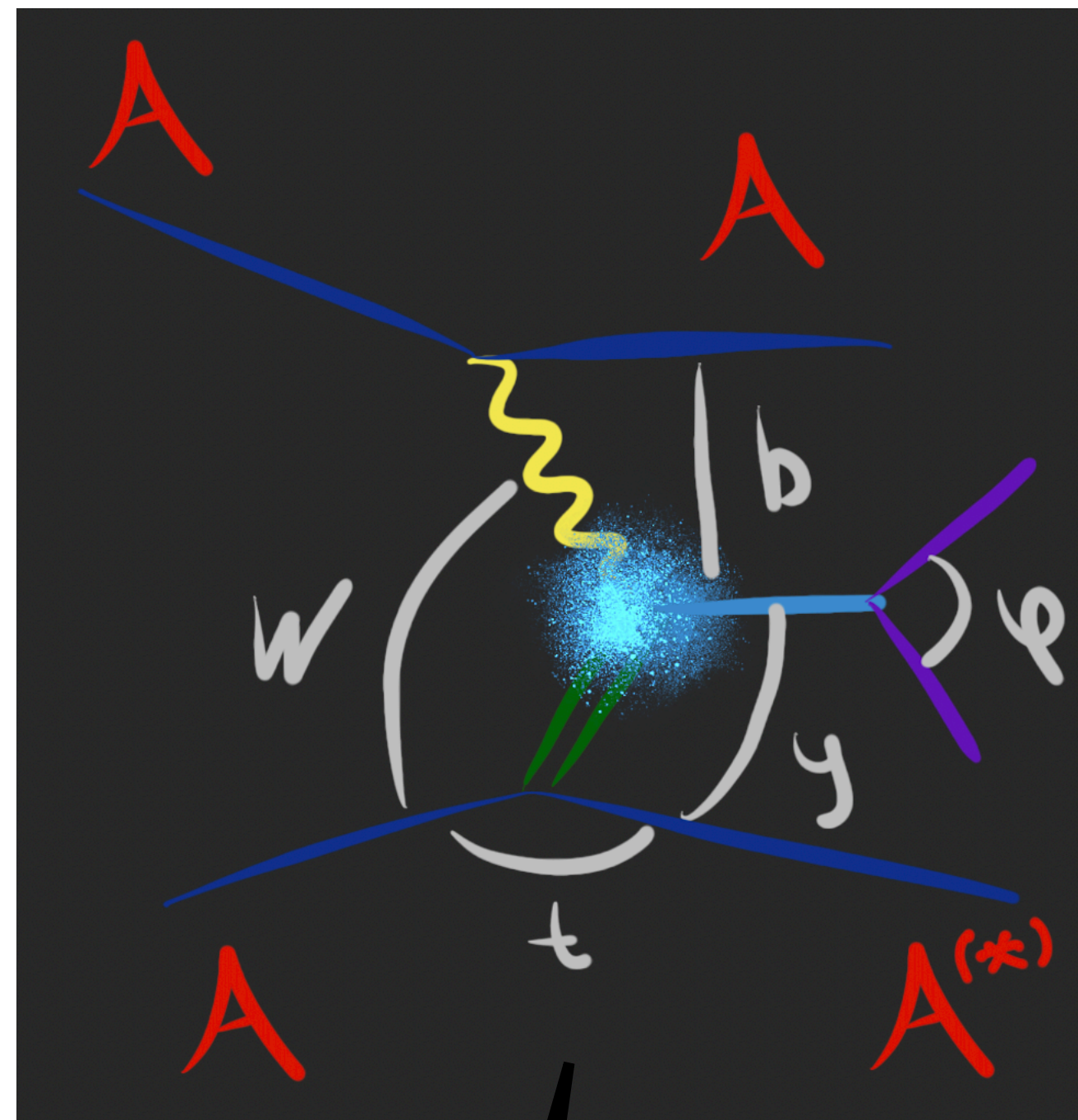
+



The interference produces new angular correlations

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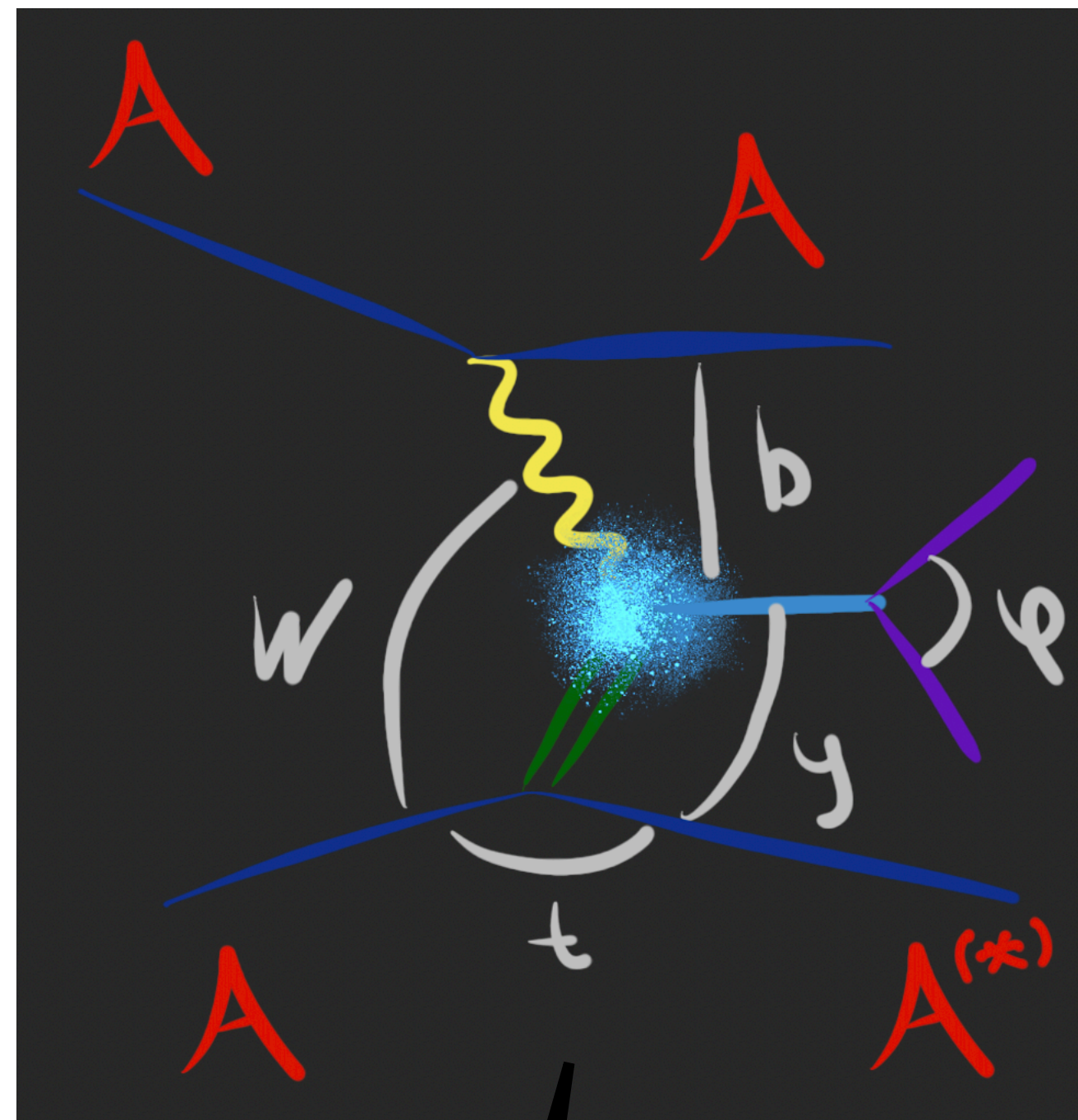


The effects are more important at small $|t|$ where the interference is destructive

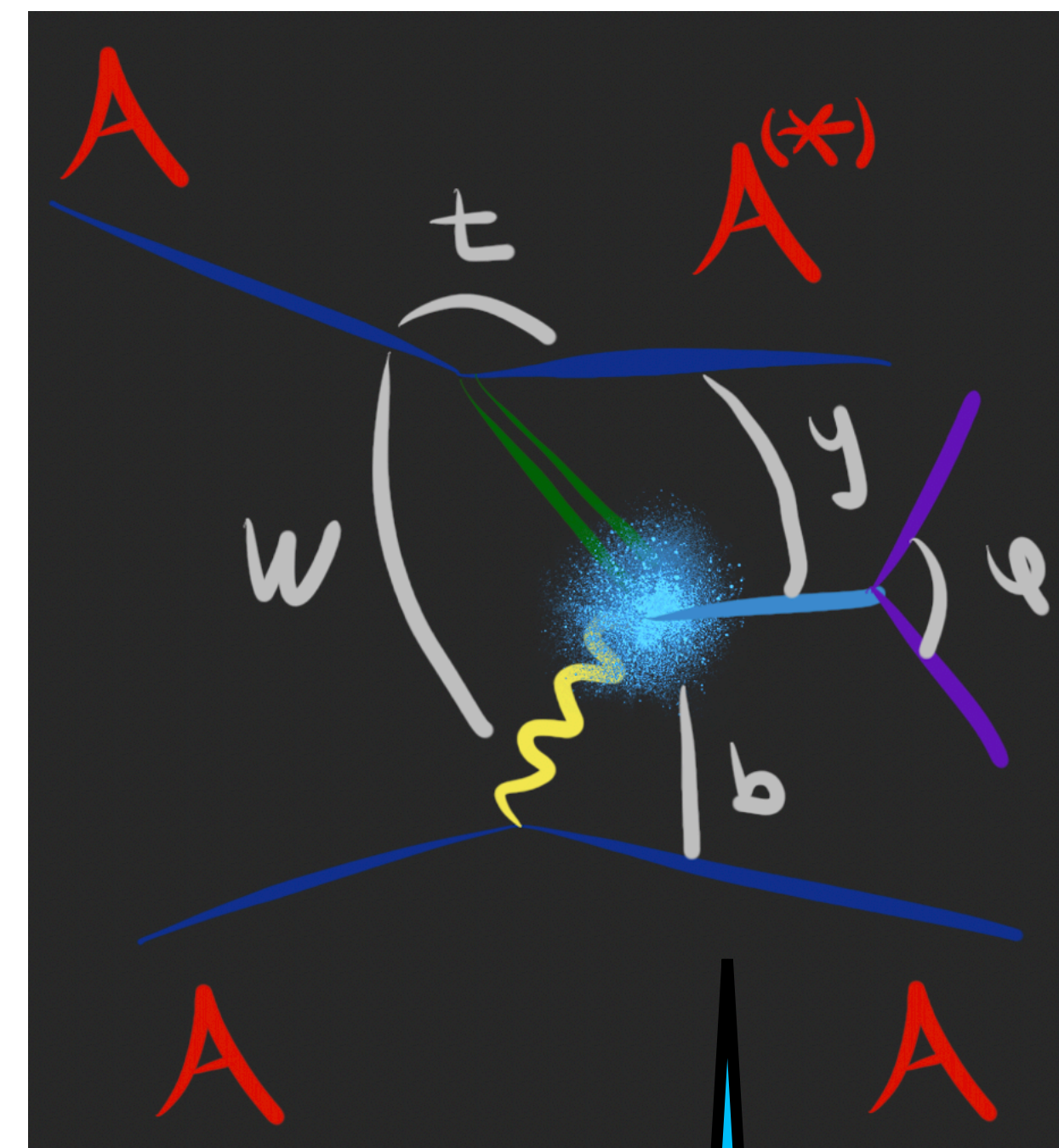
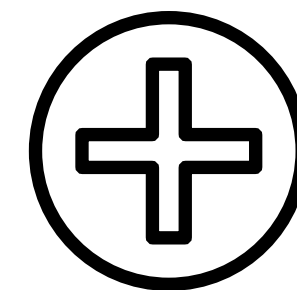
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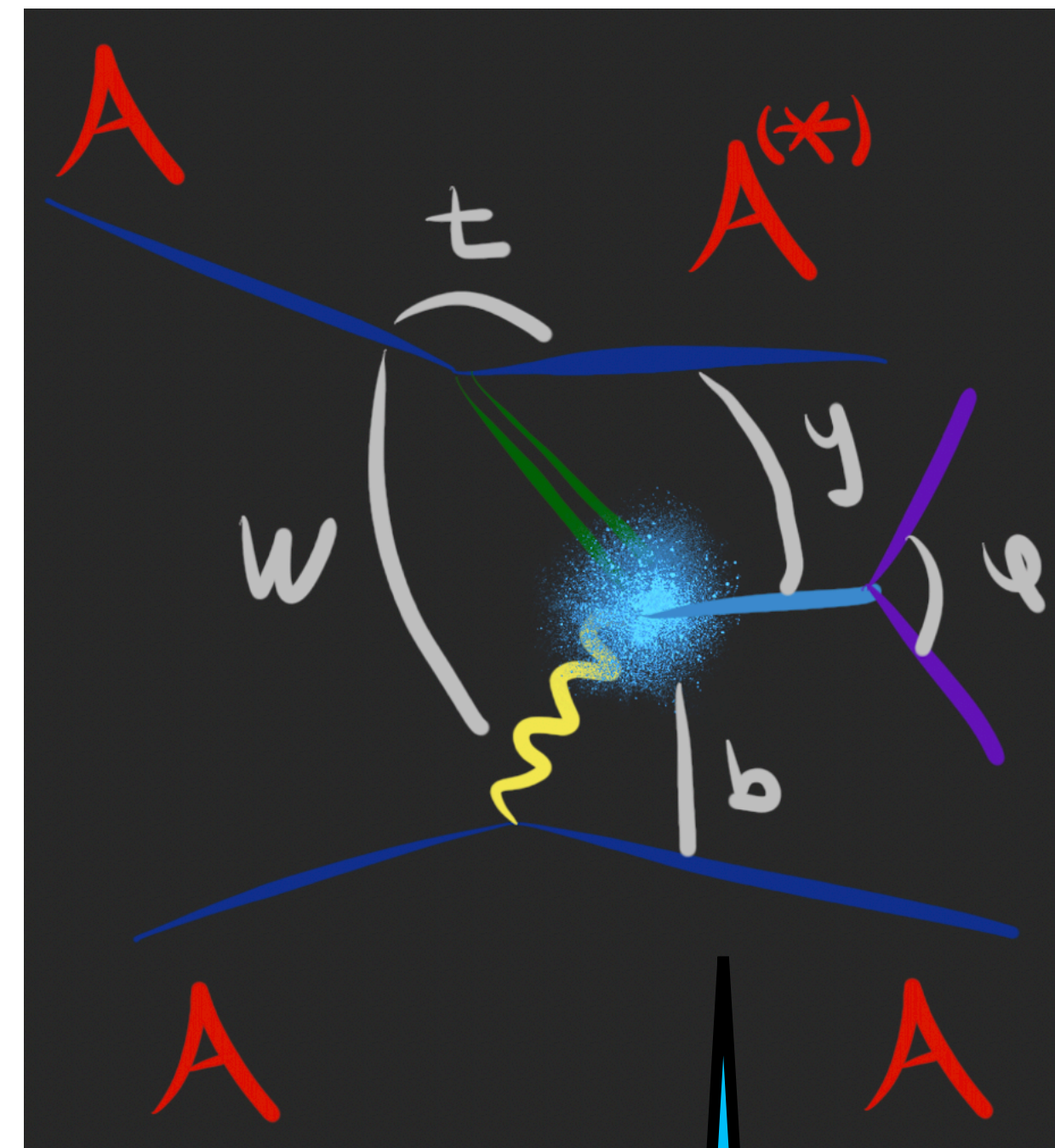
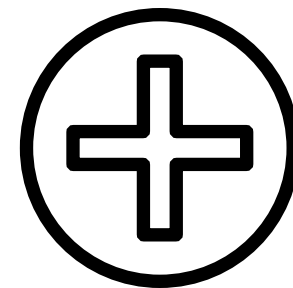
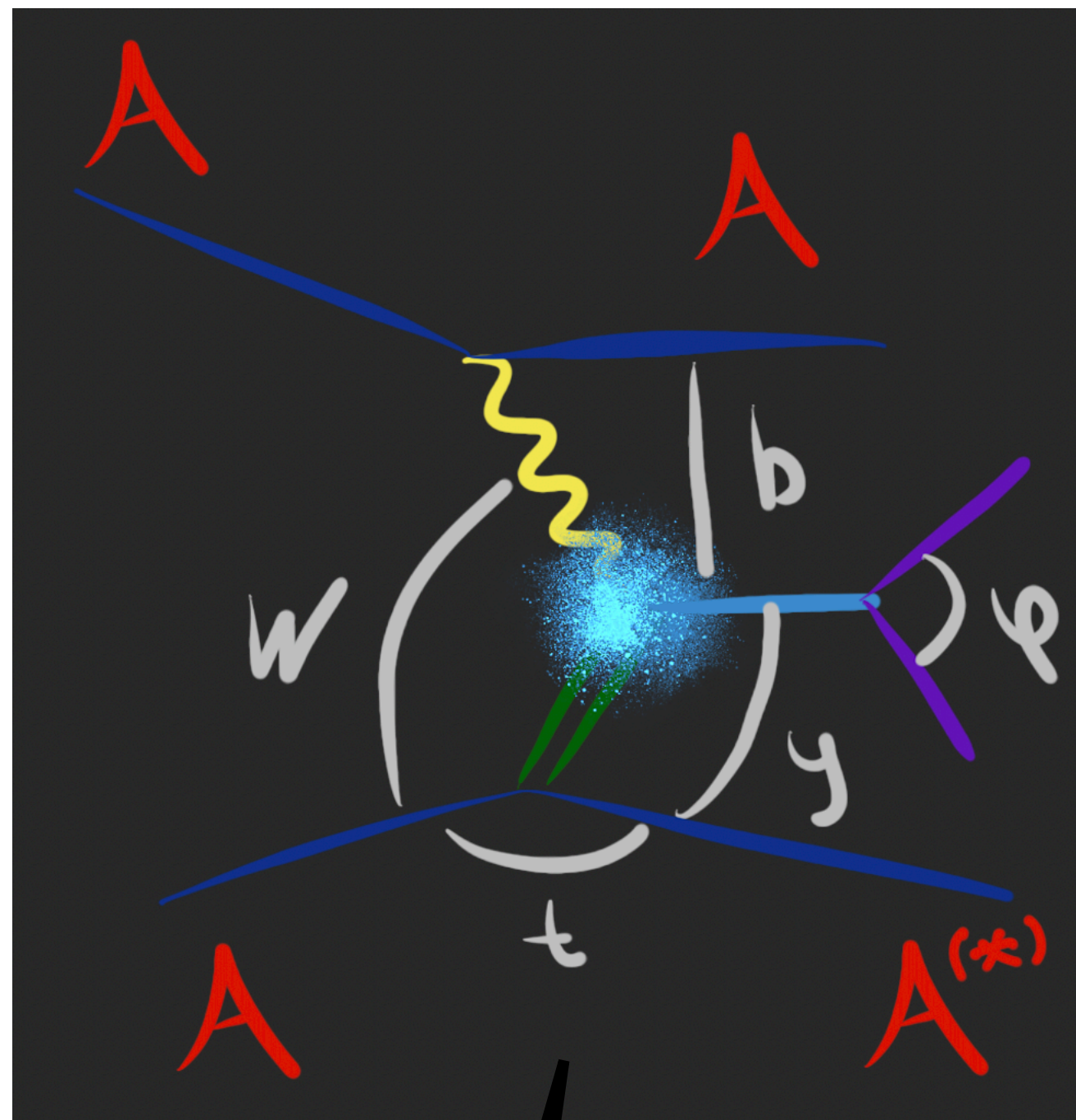


Interference depends on the impact parameter

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The presence of two competing amplitudes allows for the study of QM interference effects at new scales



The effects are more important at small $|t|$ where the interference is destructive

Interference depends on the impact parameter

The interference produces new angular correlations

Also these effects been measured at RHIC+LHC 😊

As an example, I discuss here a few results that I think will not be discussed in detail during the conference

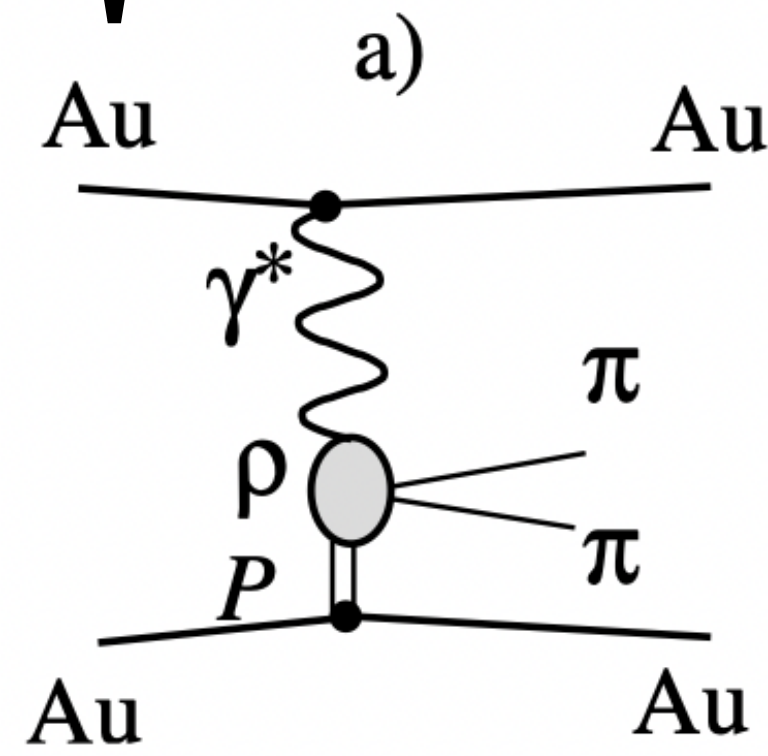
Energy dependence of coherent ρ^0 production: the first look (2002)

First observation of the process at RHIC by the STAR collaboration

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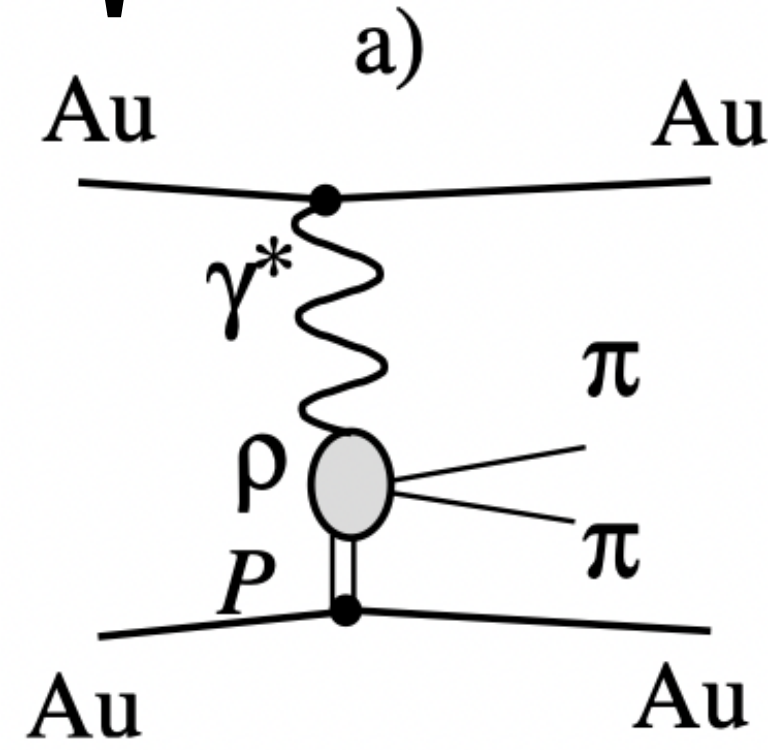
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AuAu collisions at 130 GeV per NN



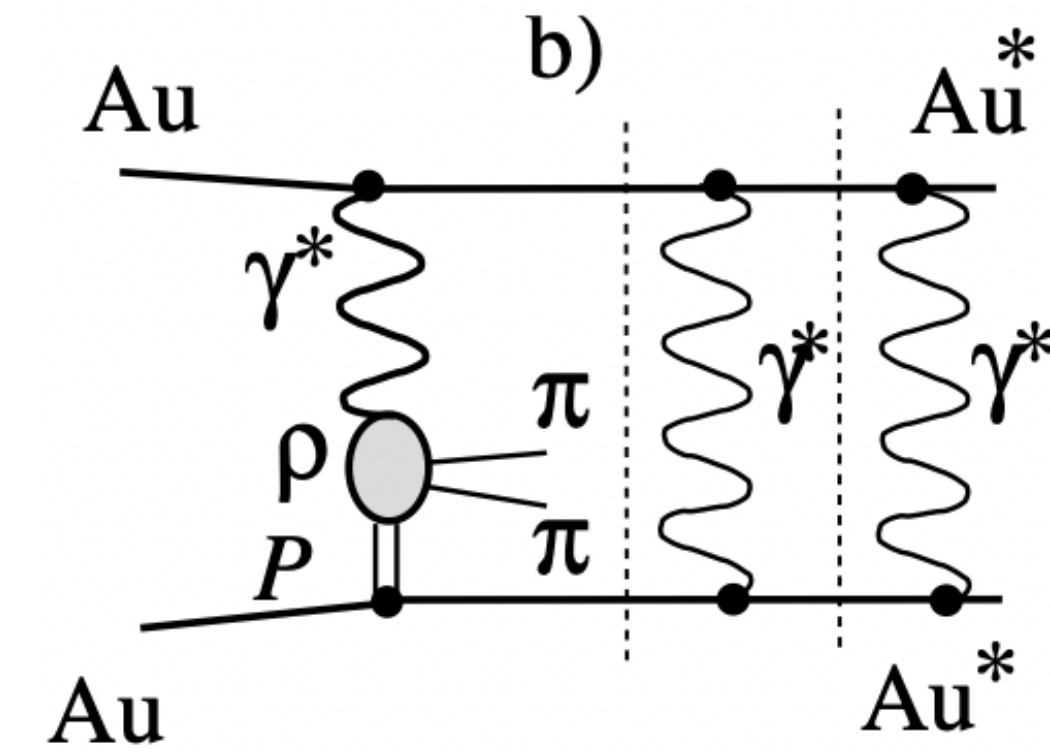
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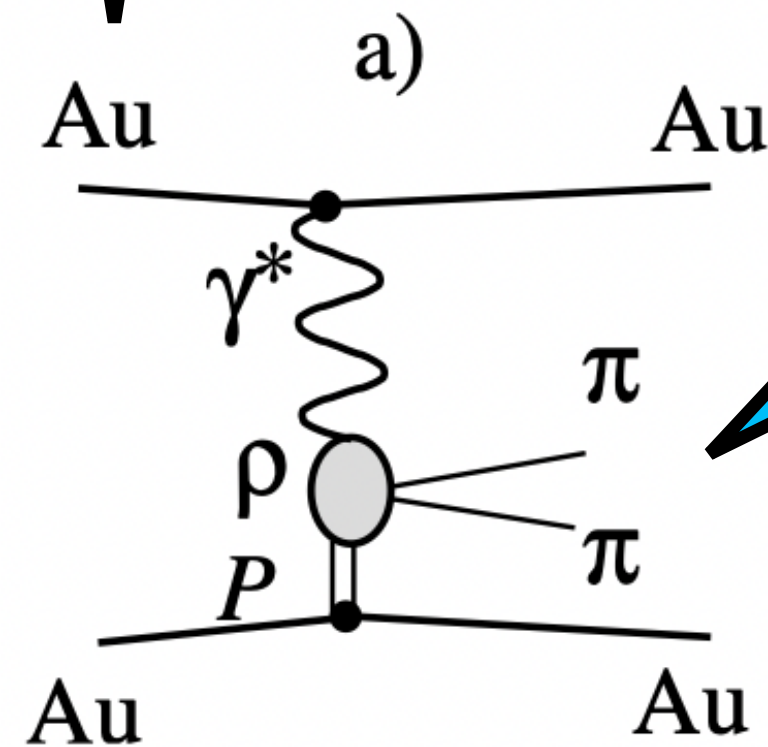
Triggering utilises EMD



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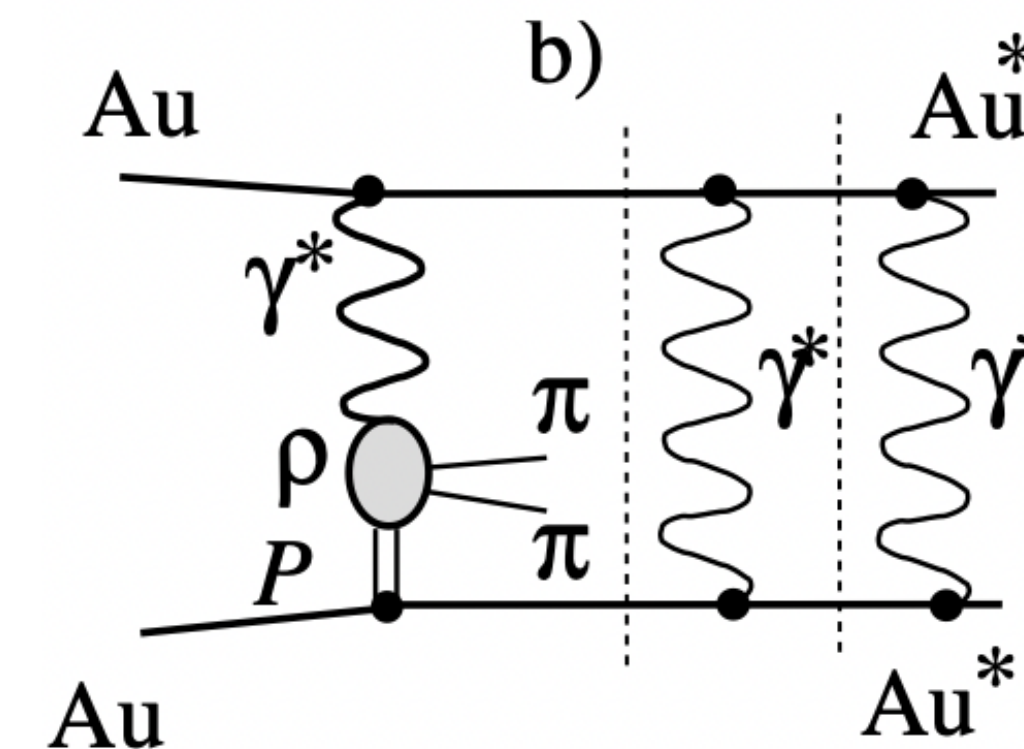
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Decay to $\pi\pi$ almost 100% of the time

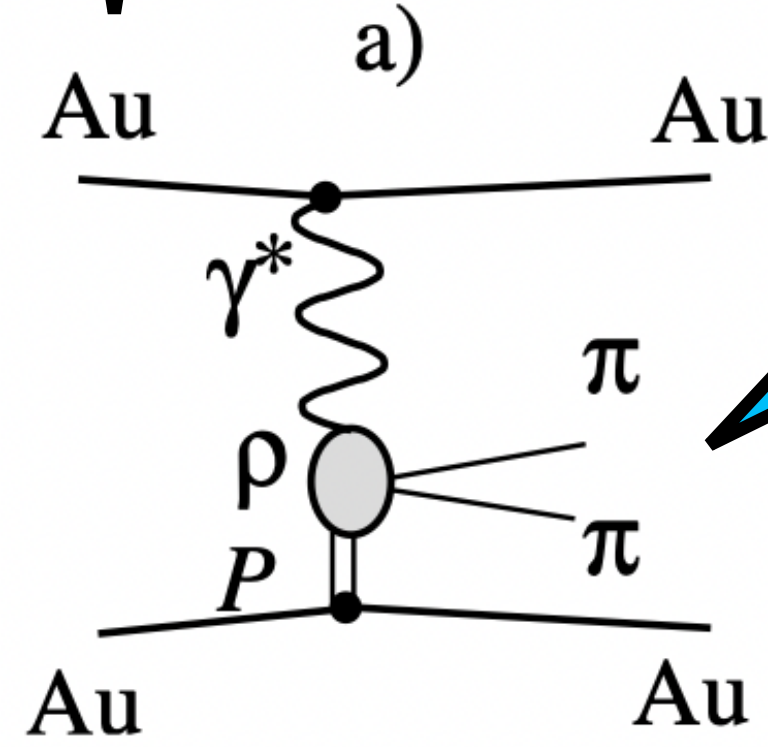
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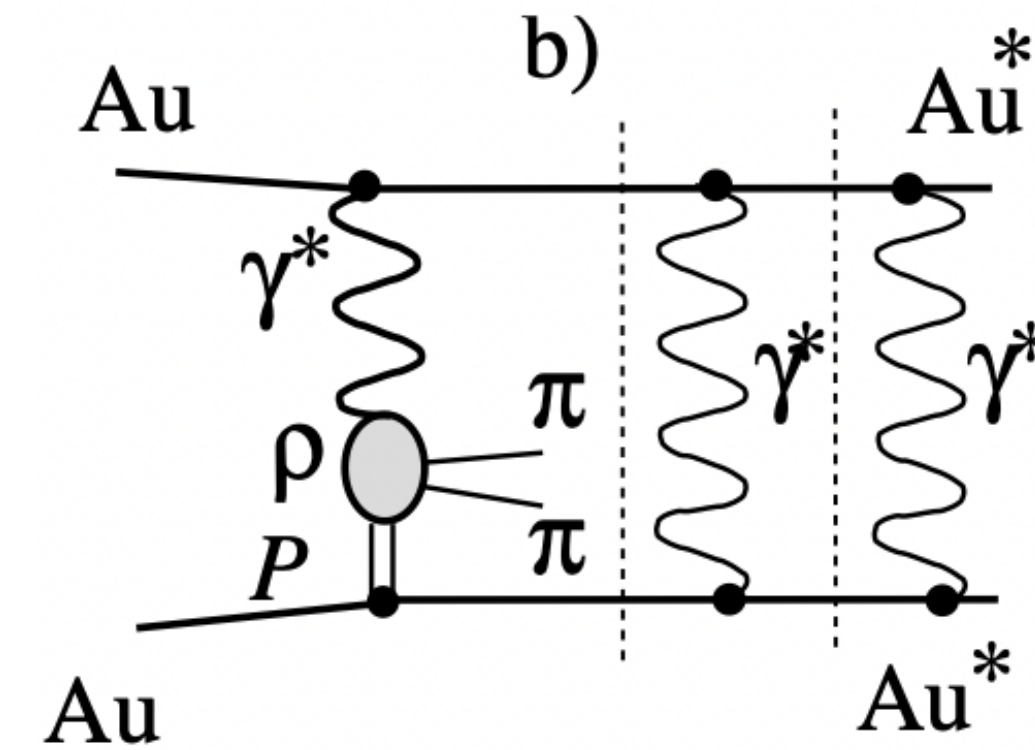
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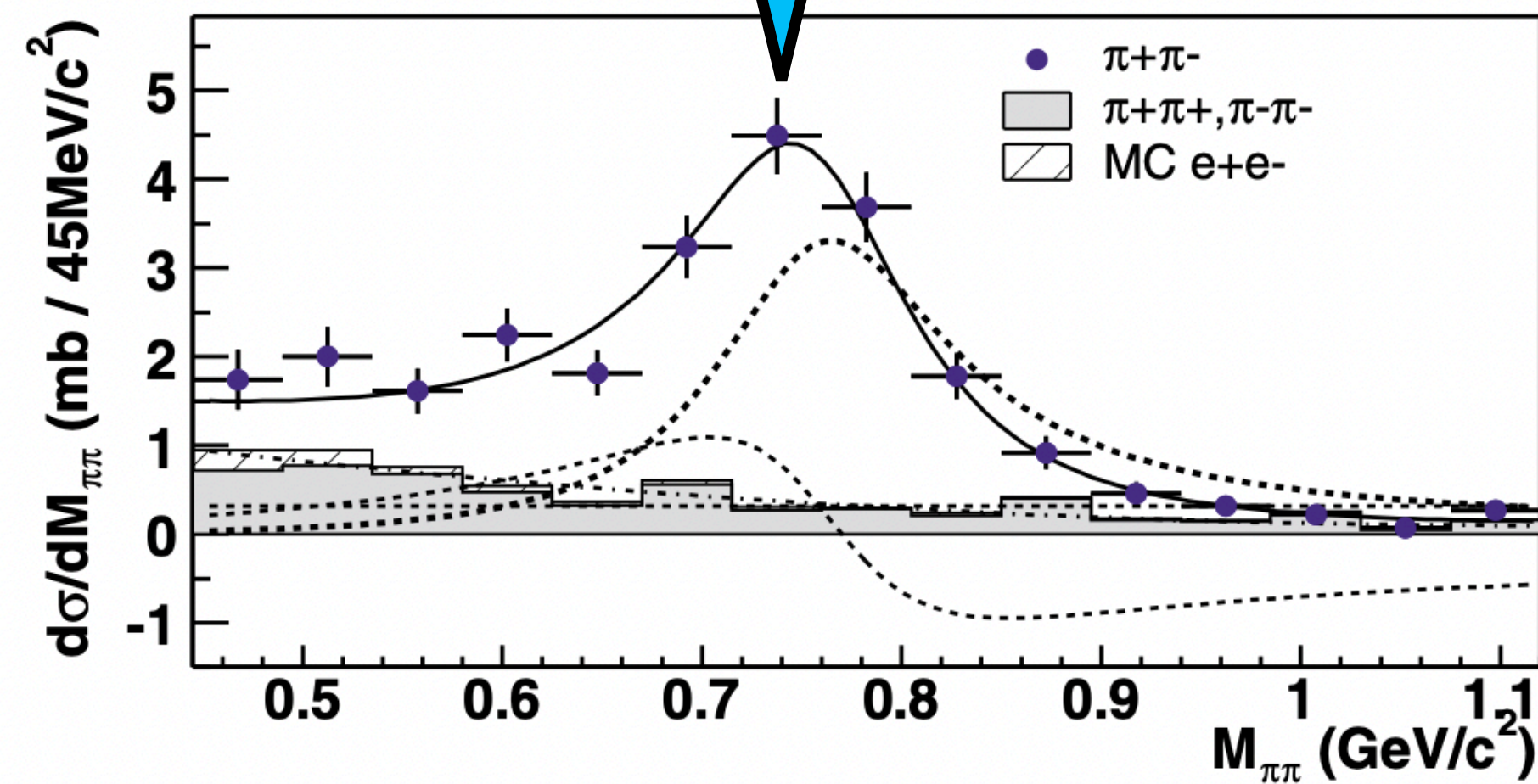


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Broad resonance: need models to take into account continuum production

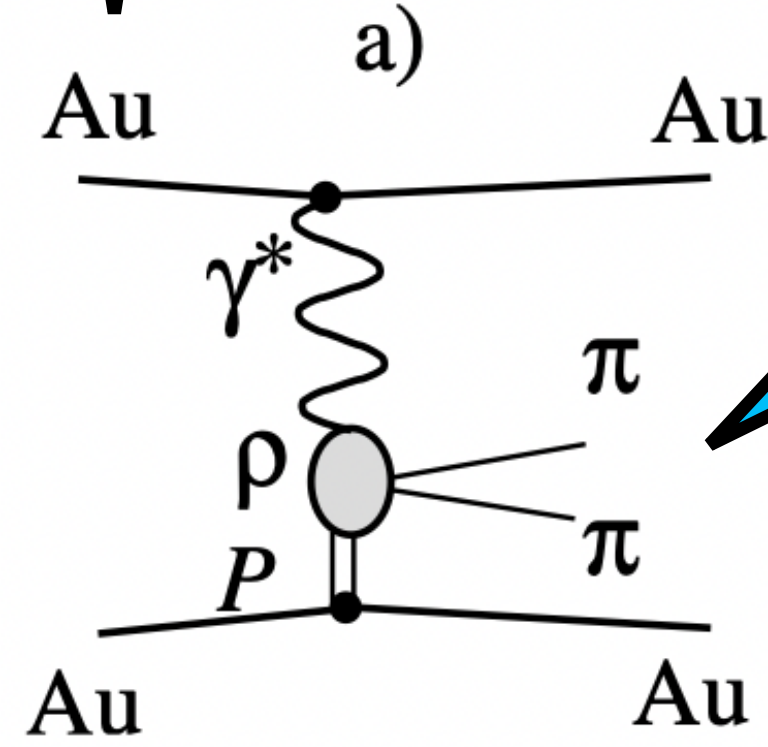


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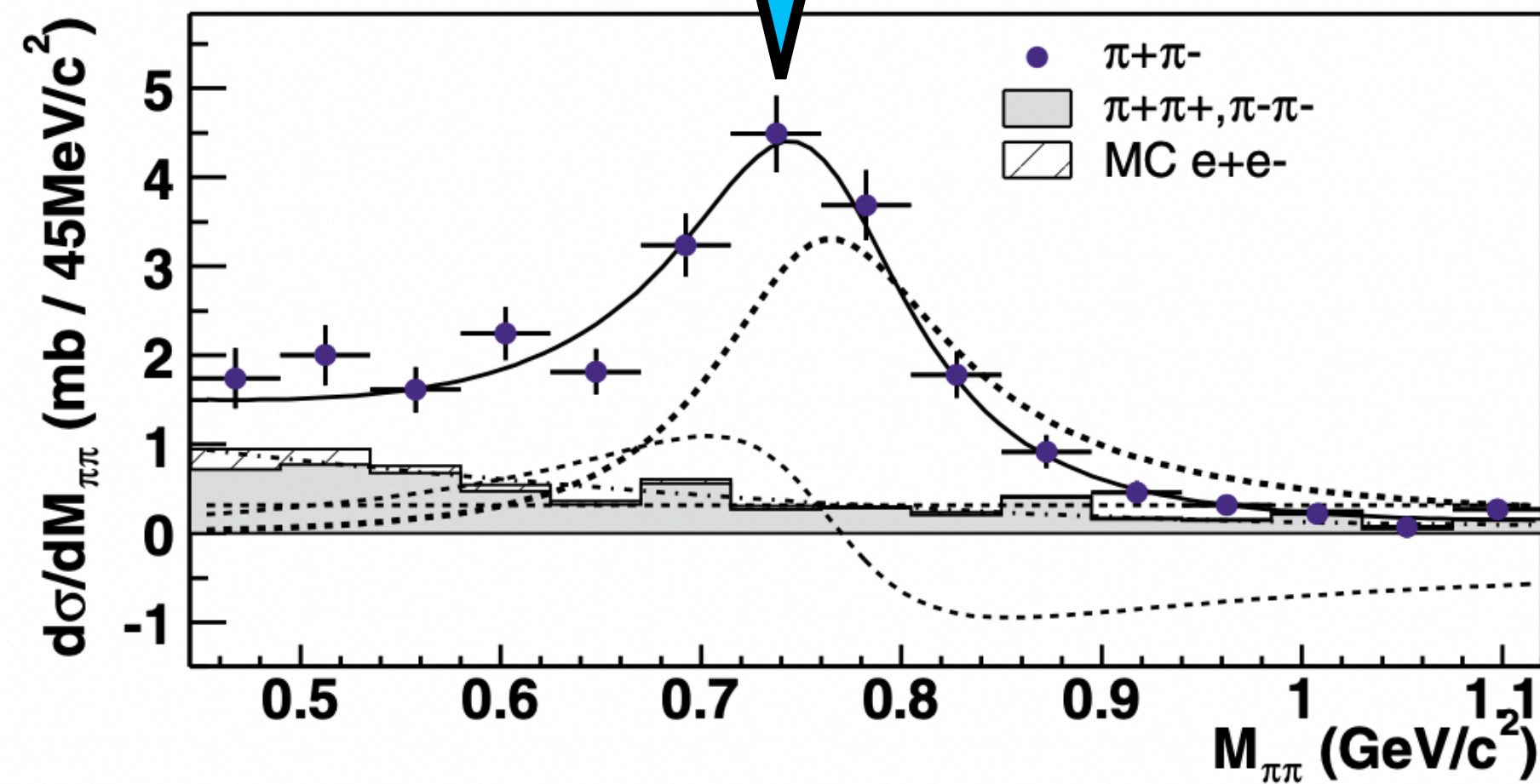
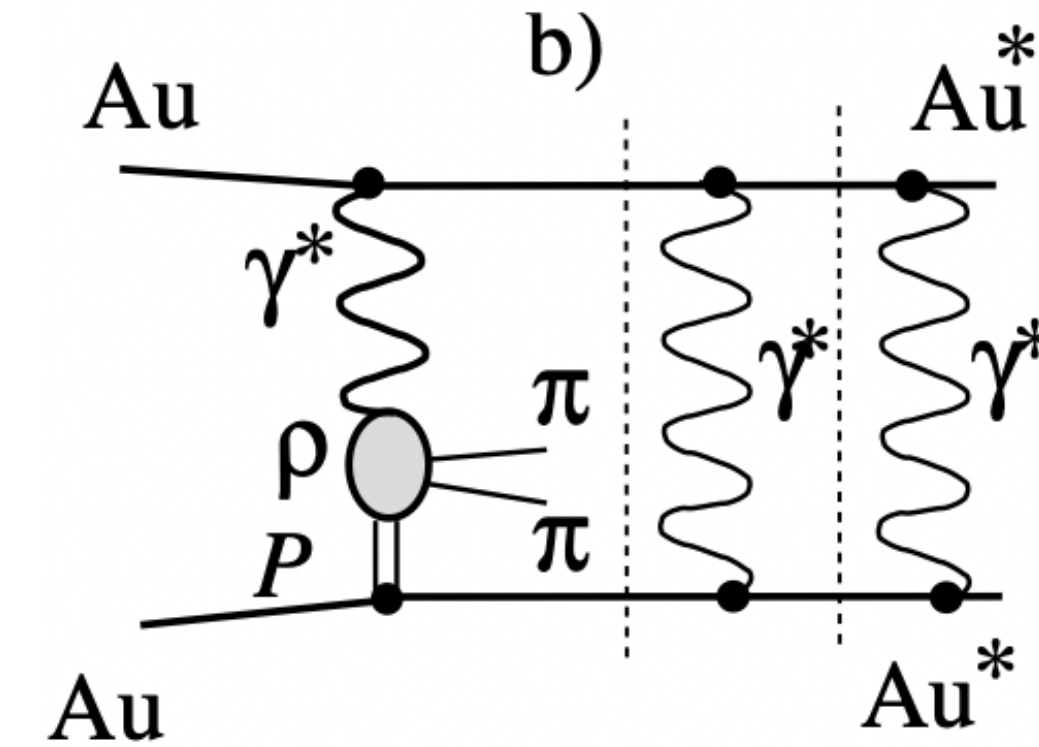


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E.g. Söding or Ross-Stodolky models

Soding, P Phys.Lett. 19 (1966) 702-704
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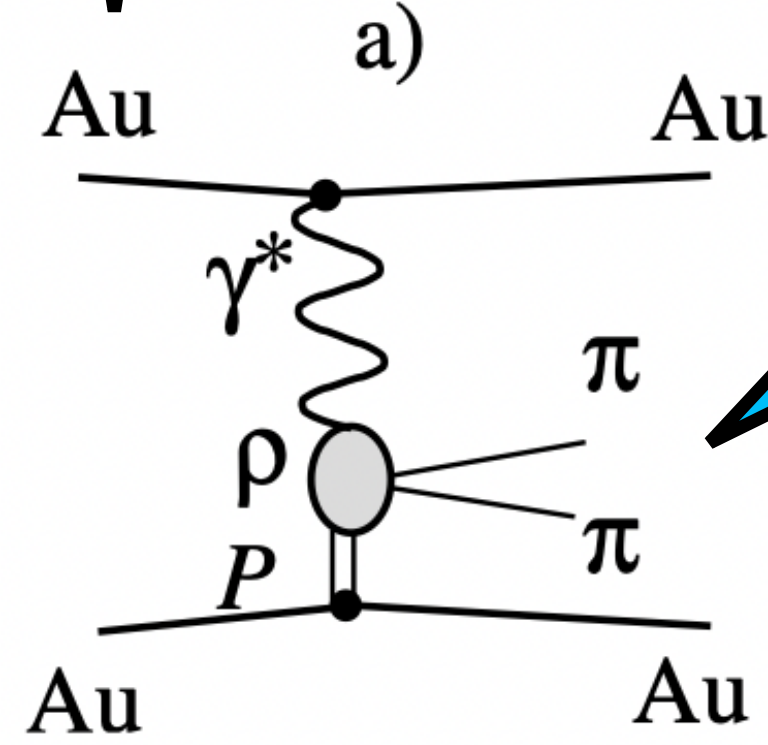
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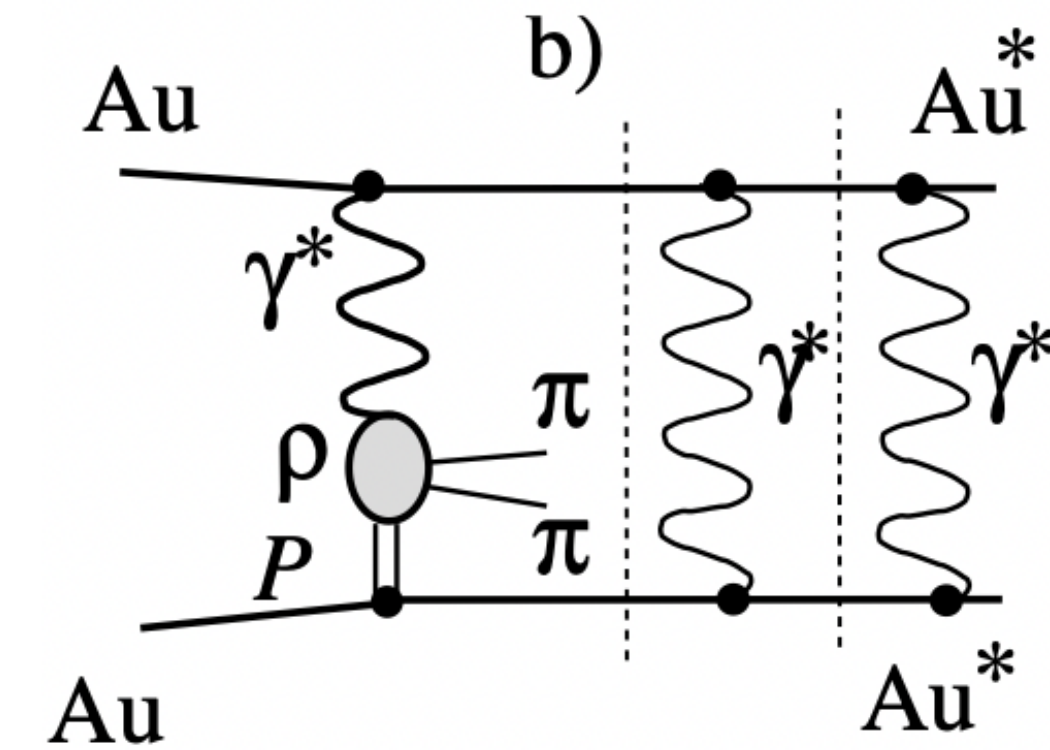
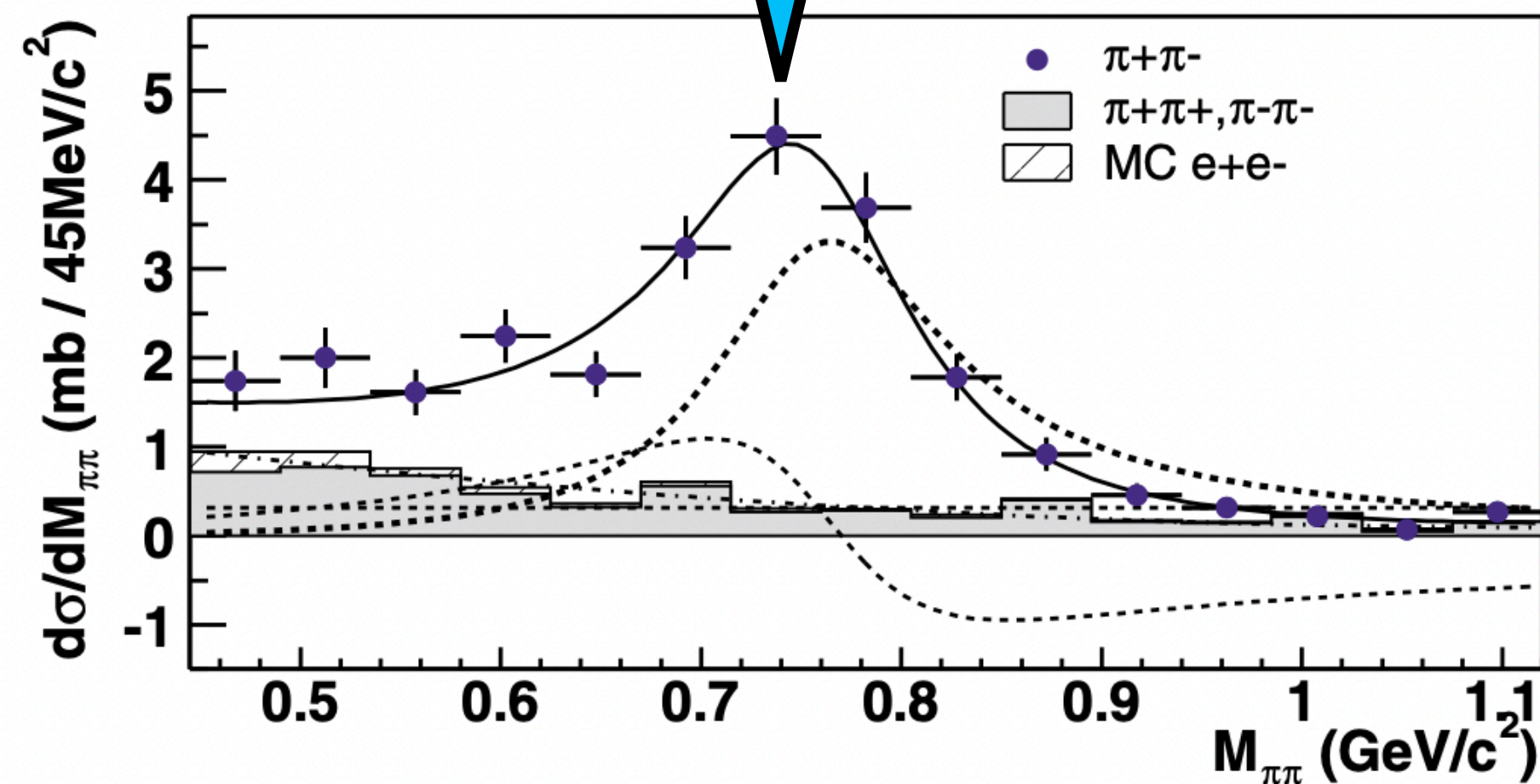


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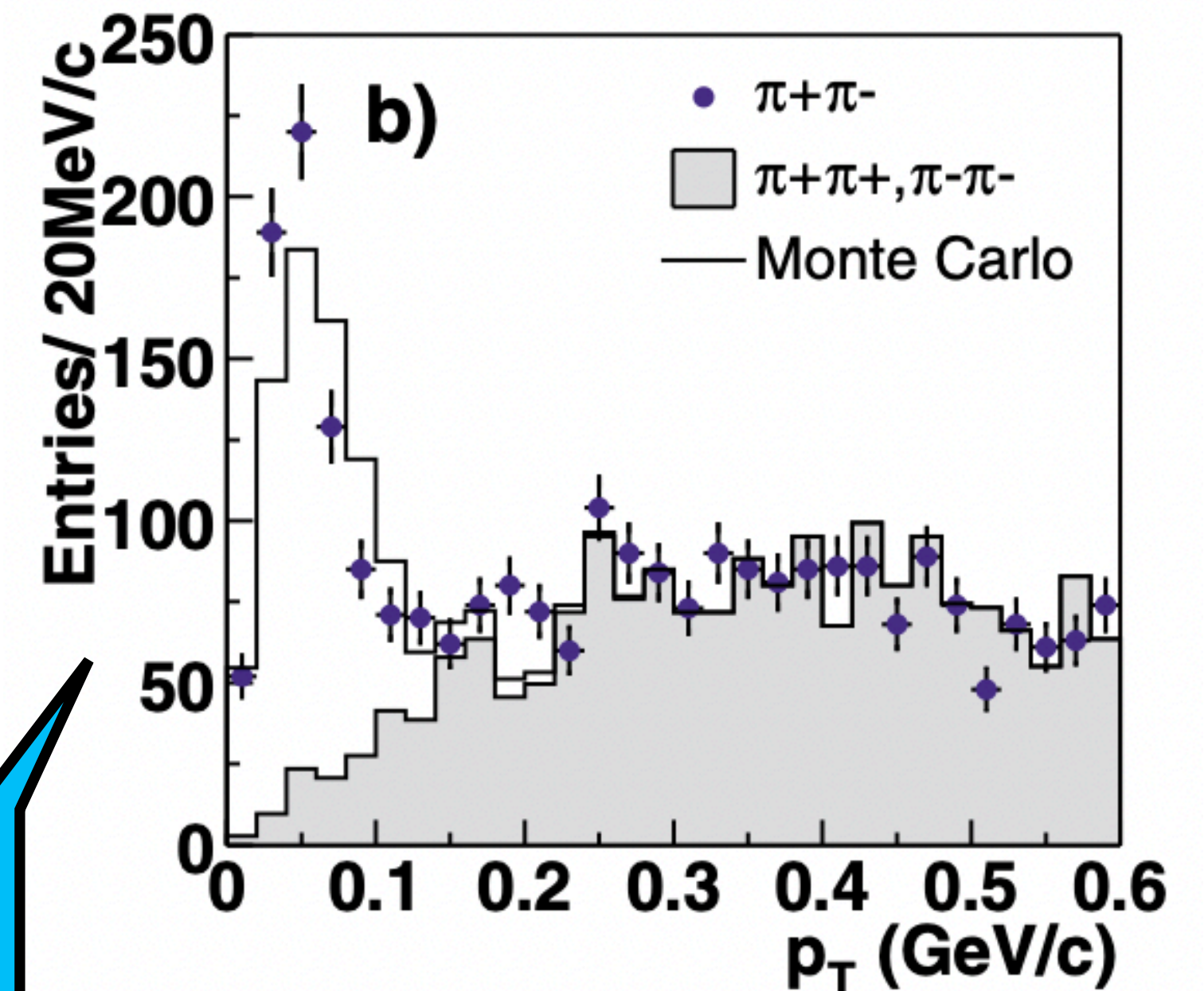
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Typical shape of the transverse momentum distribution (below 0.1 GeV/c)

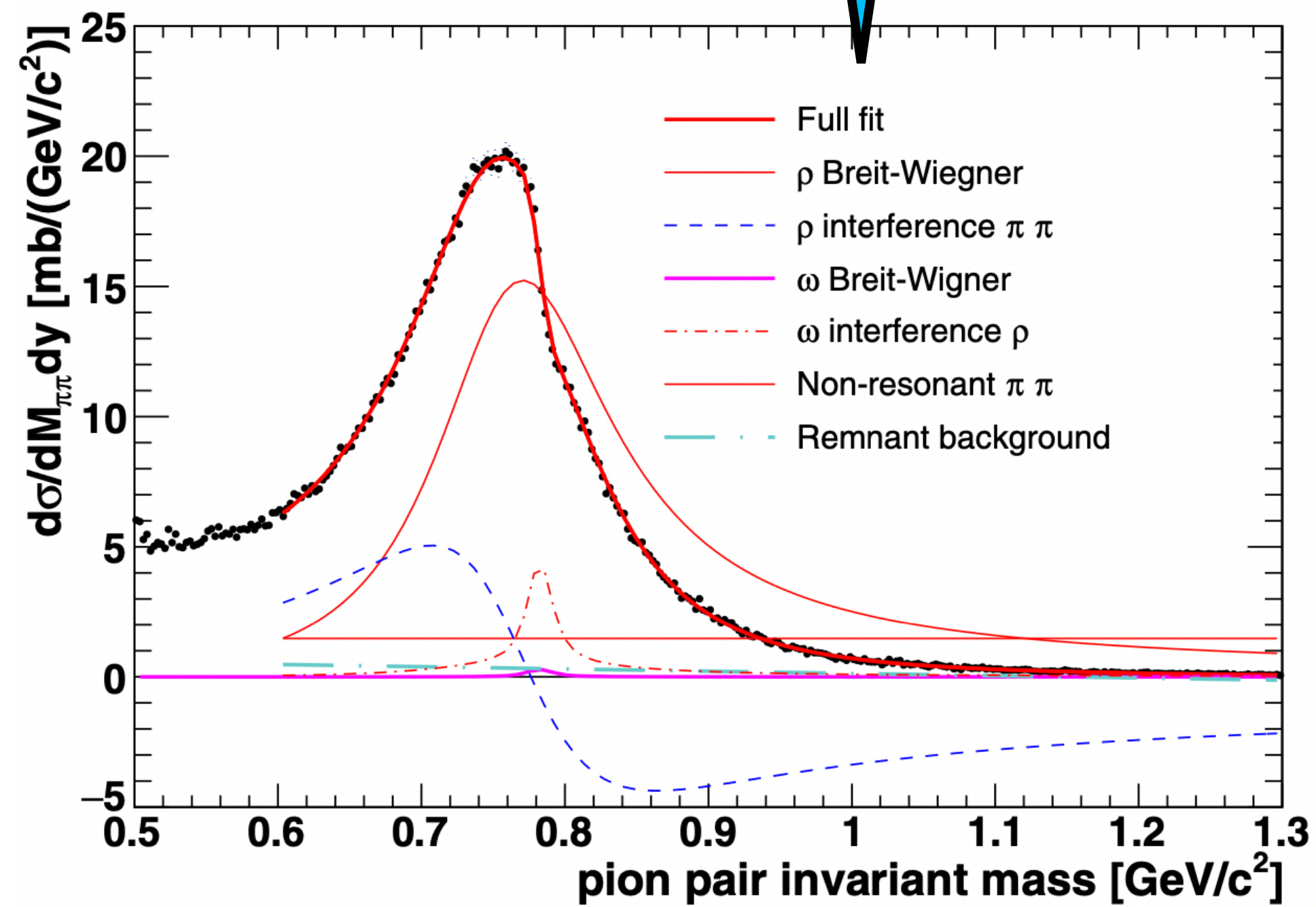
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Coherent production in 2017: AuAu at 200 GeV per NN

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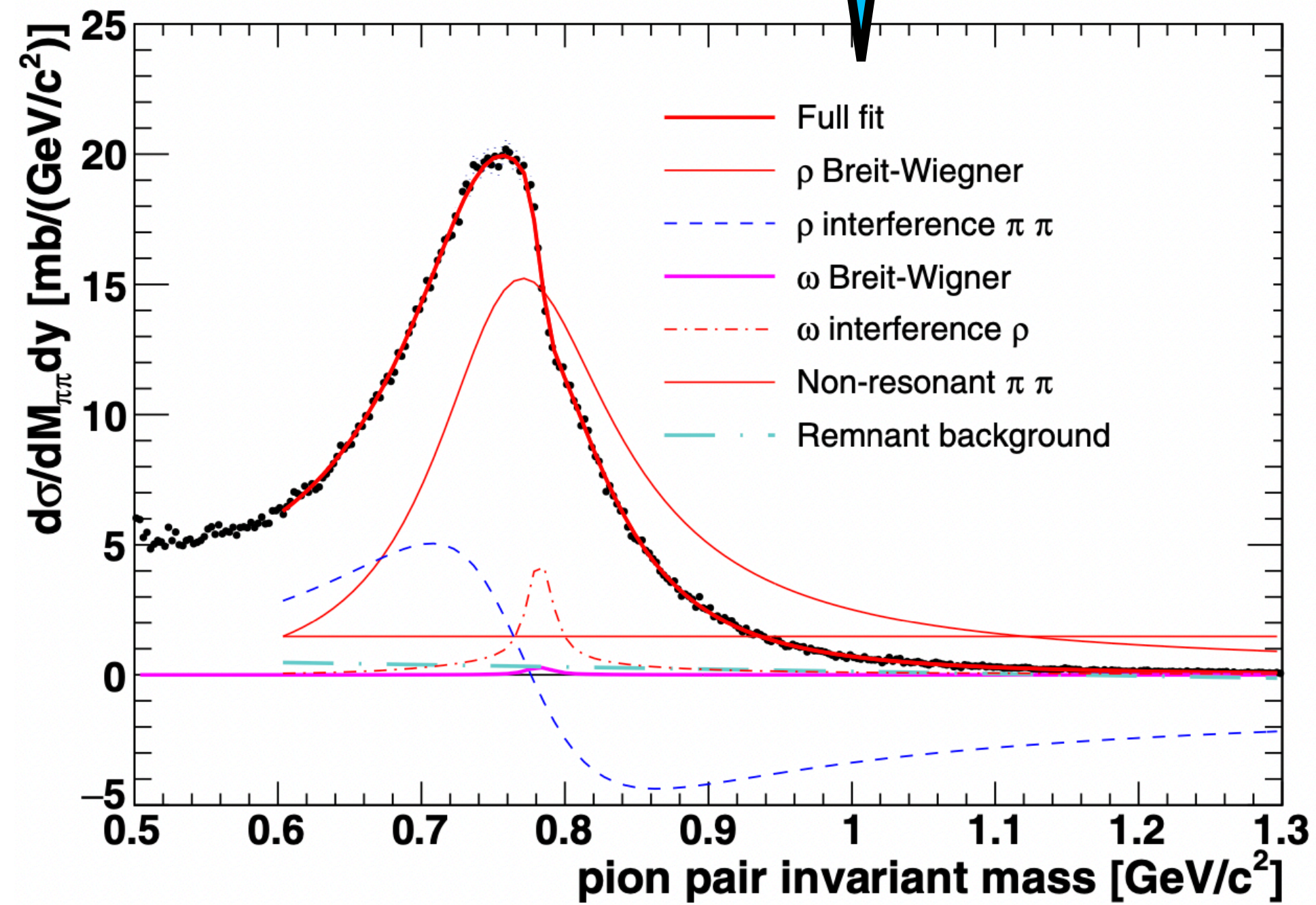
Data is sensitive to the contribution of other processes



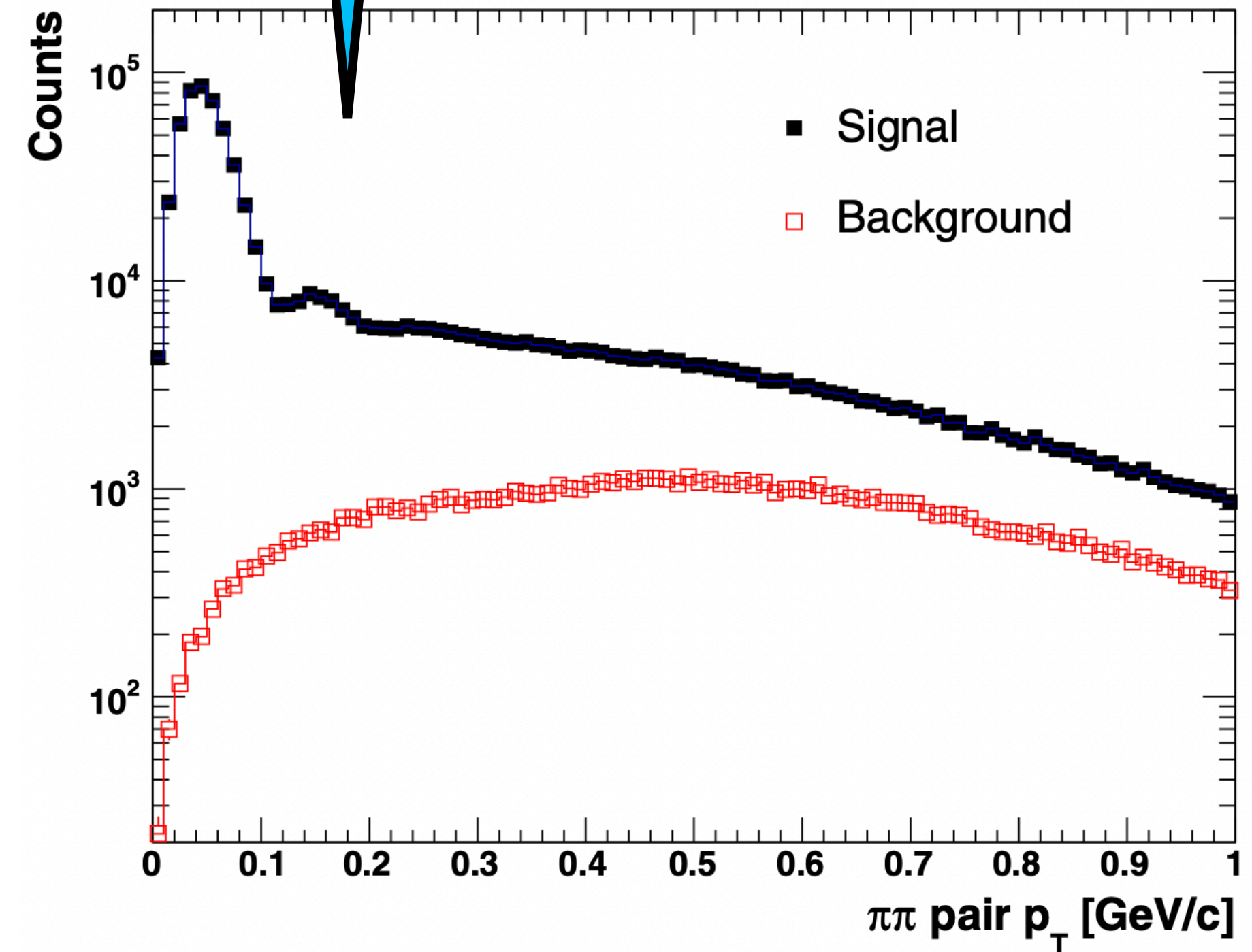
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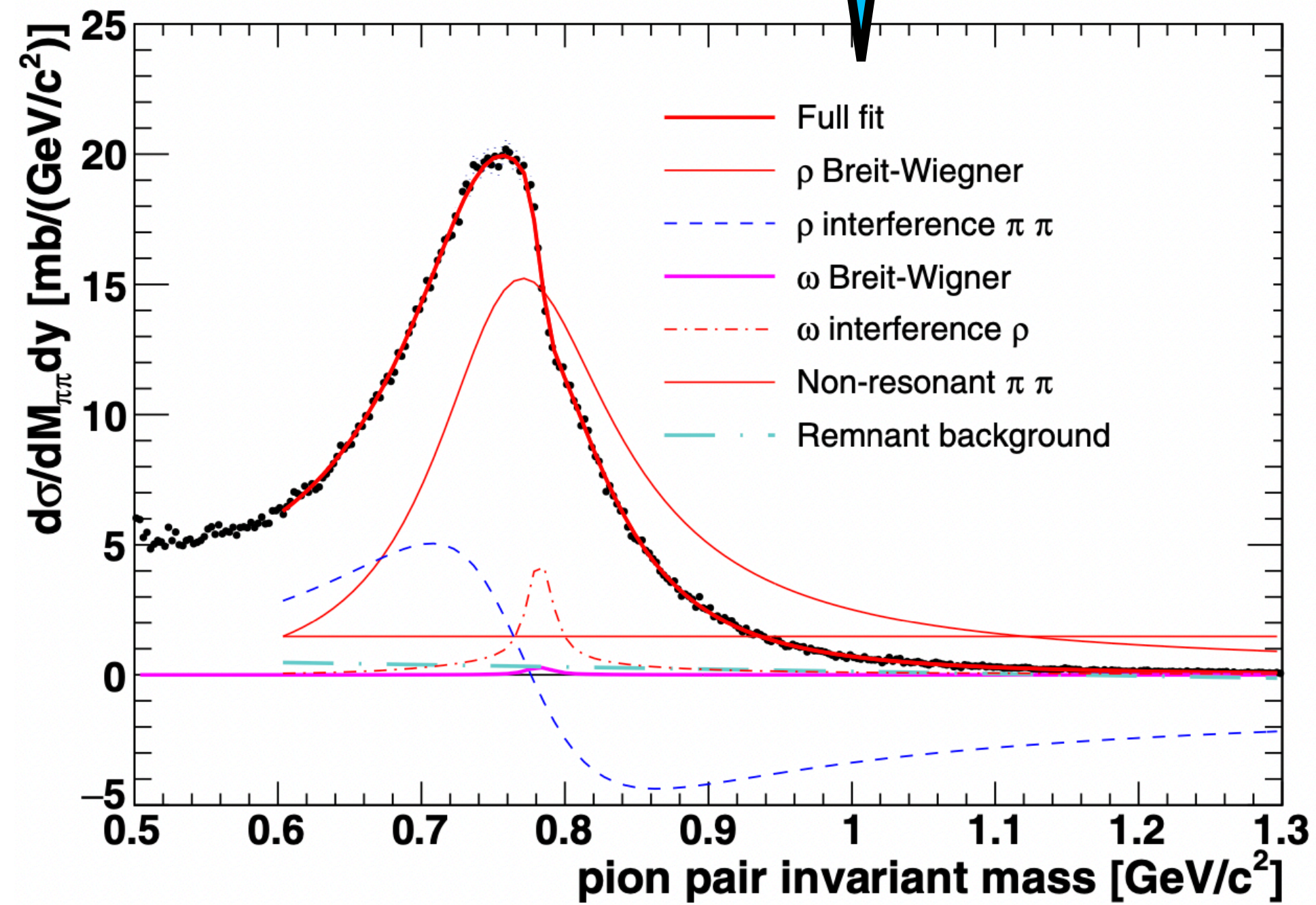
Second diffraction peak visible!



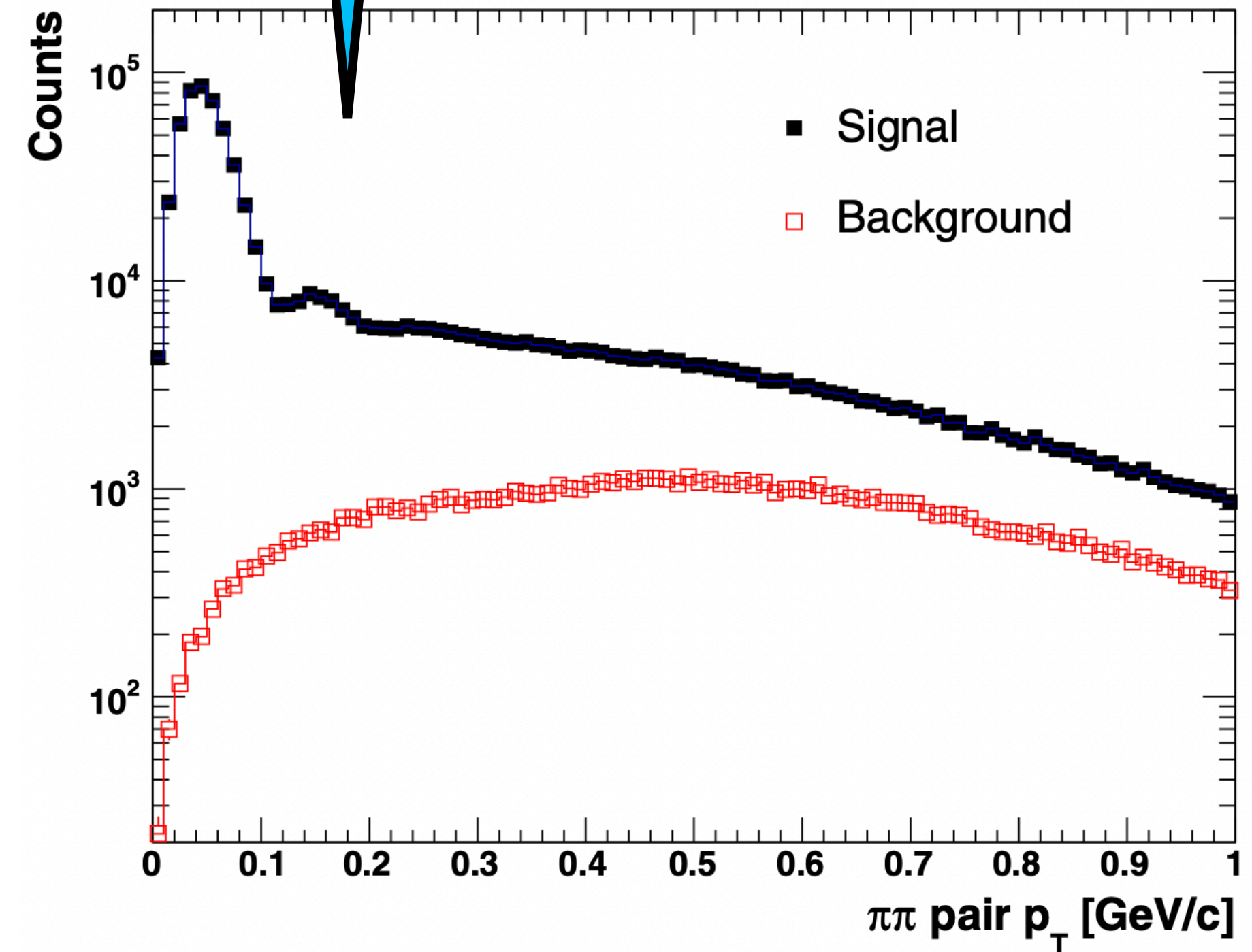
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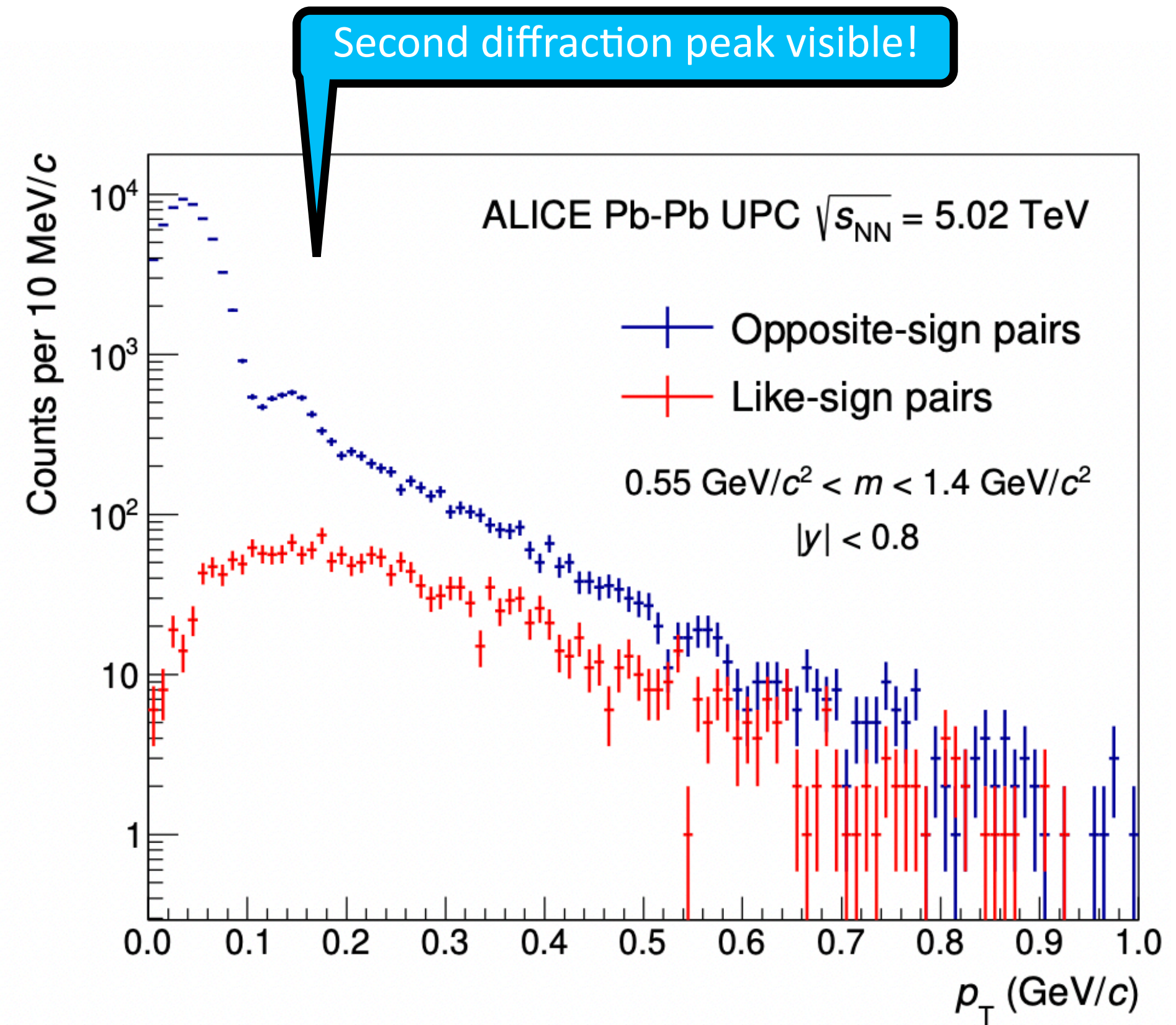
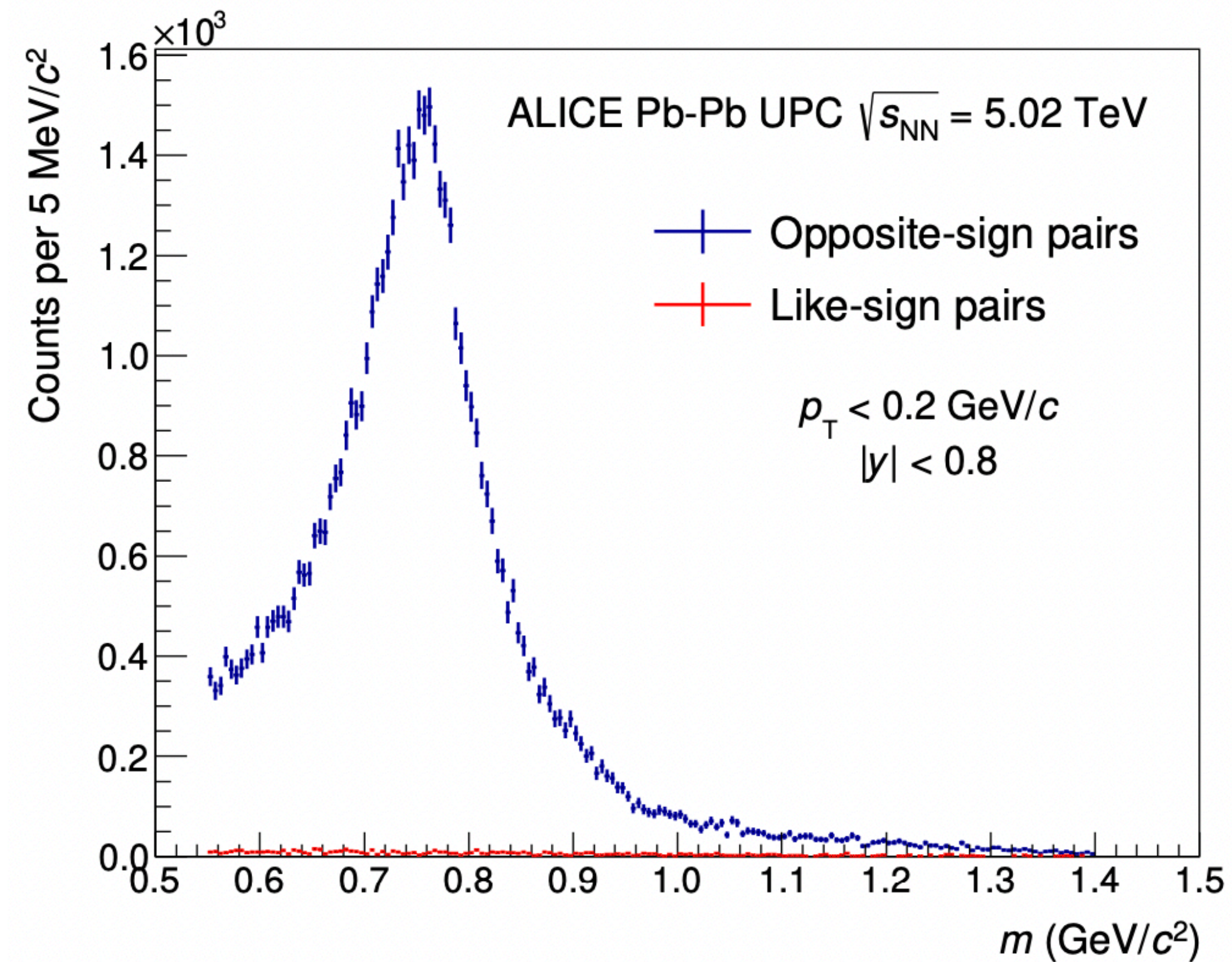
Other measurements available at 62.4 GeV per NN

Energy dependence of coherent ρ^0 production: PbPb in ALICE

Coherent production in 2020: PbPb at 5.02 TeV per NN

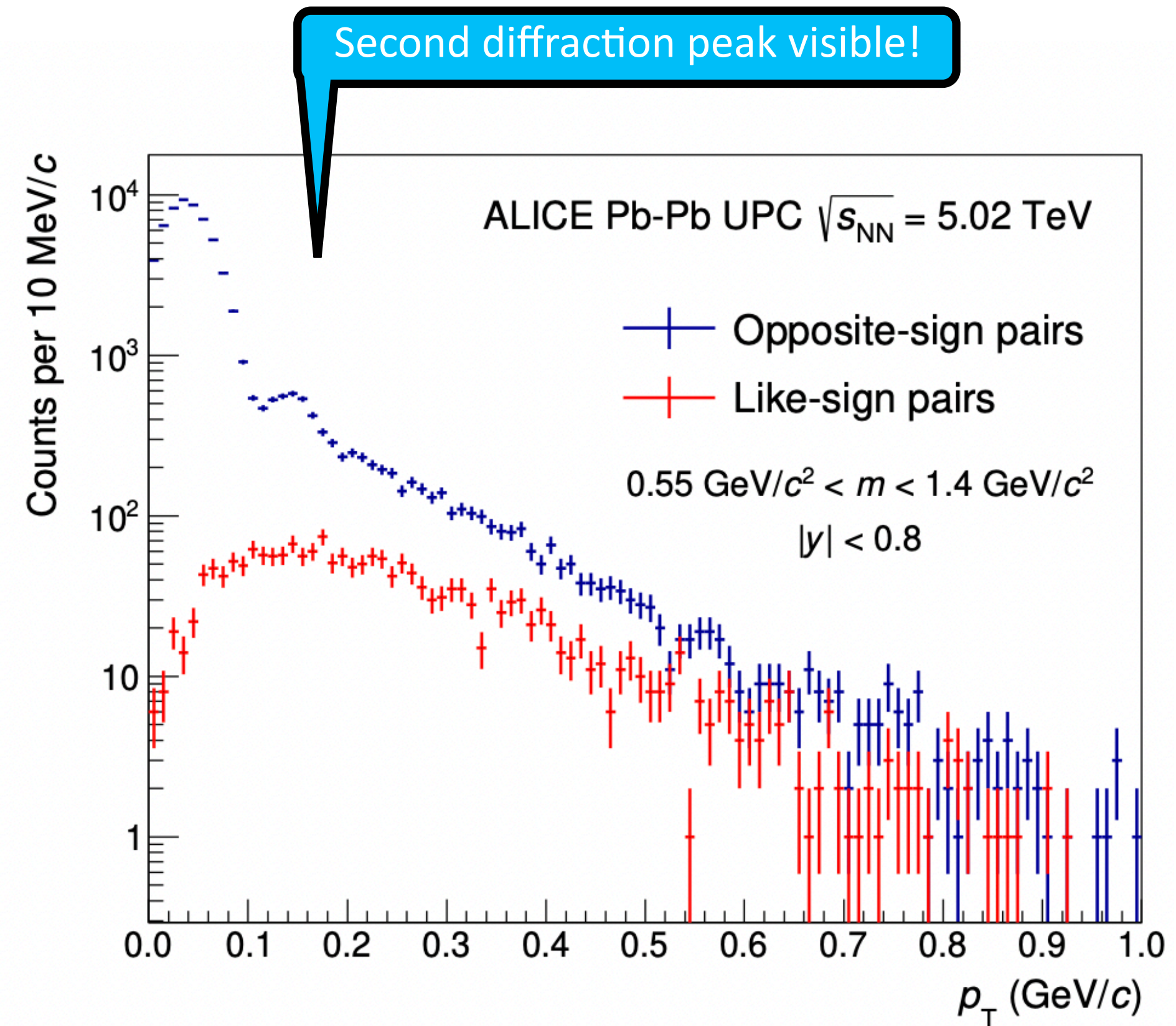
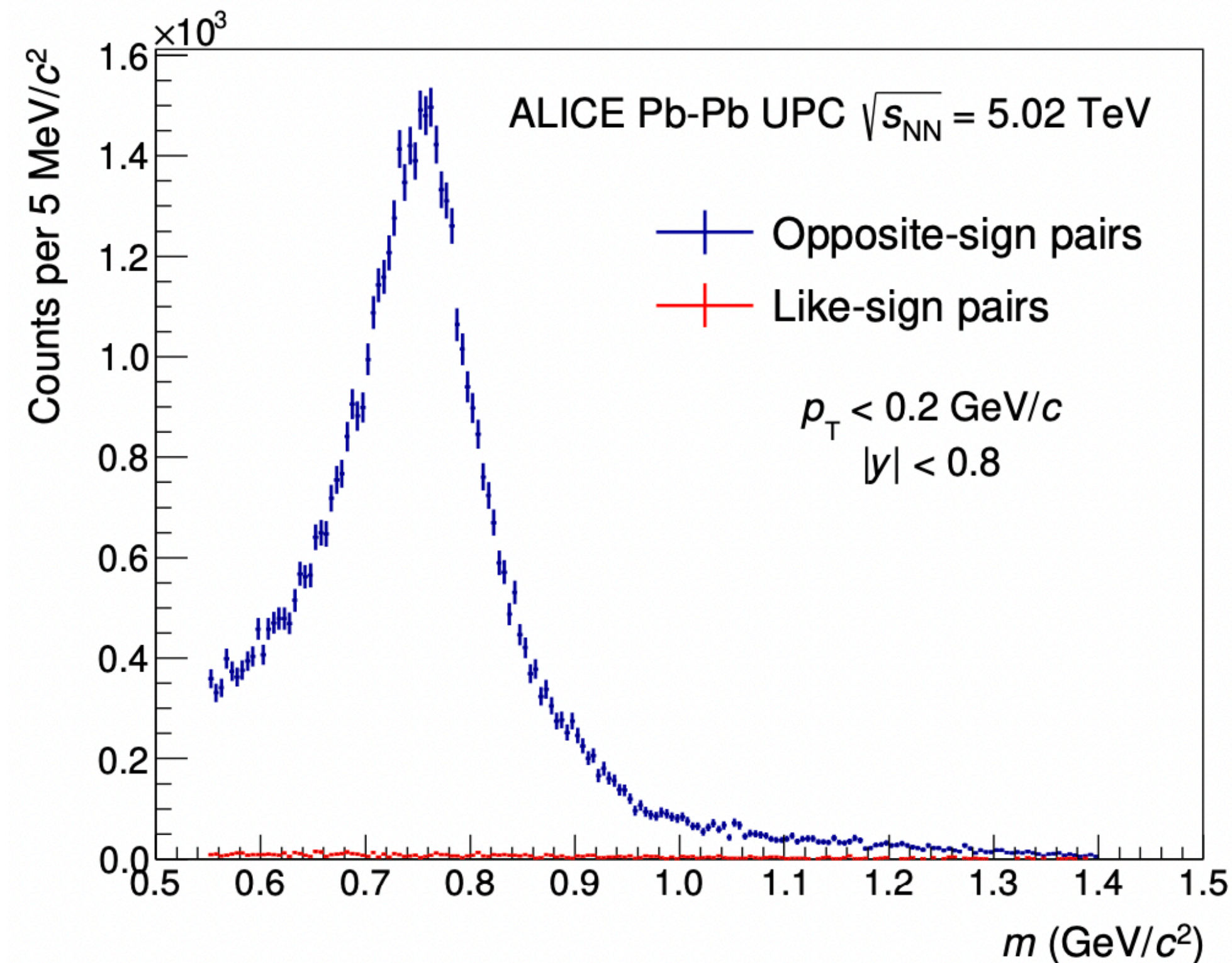
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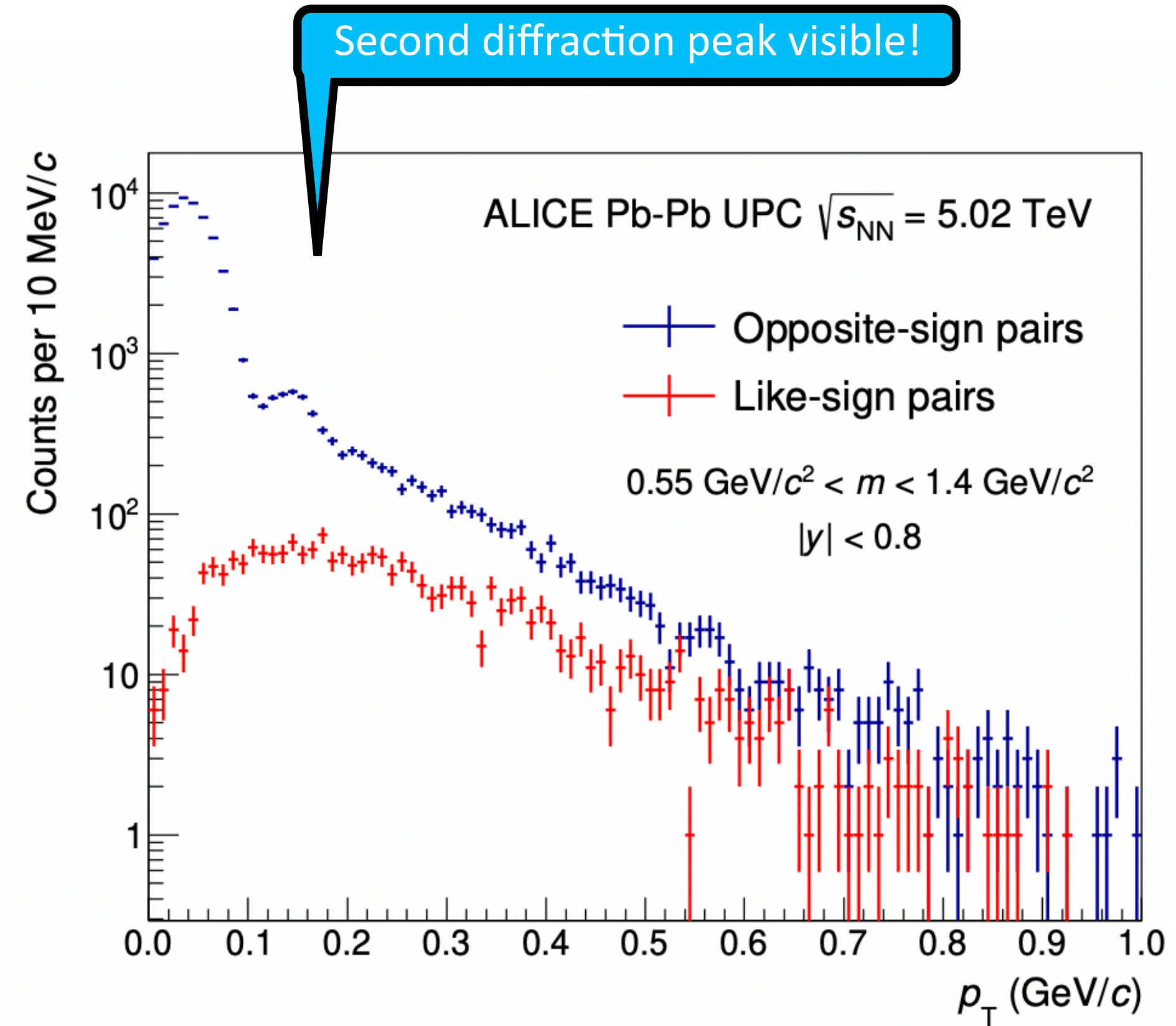
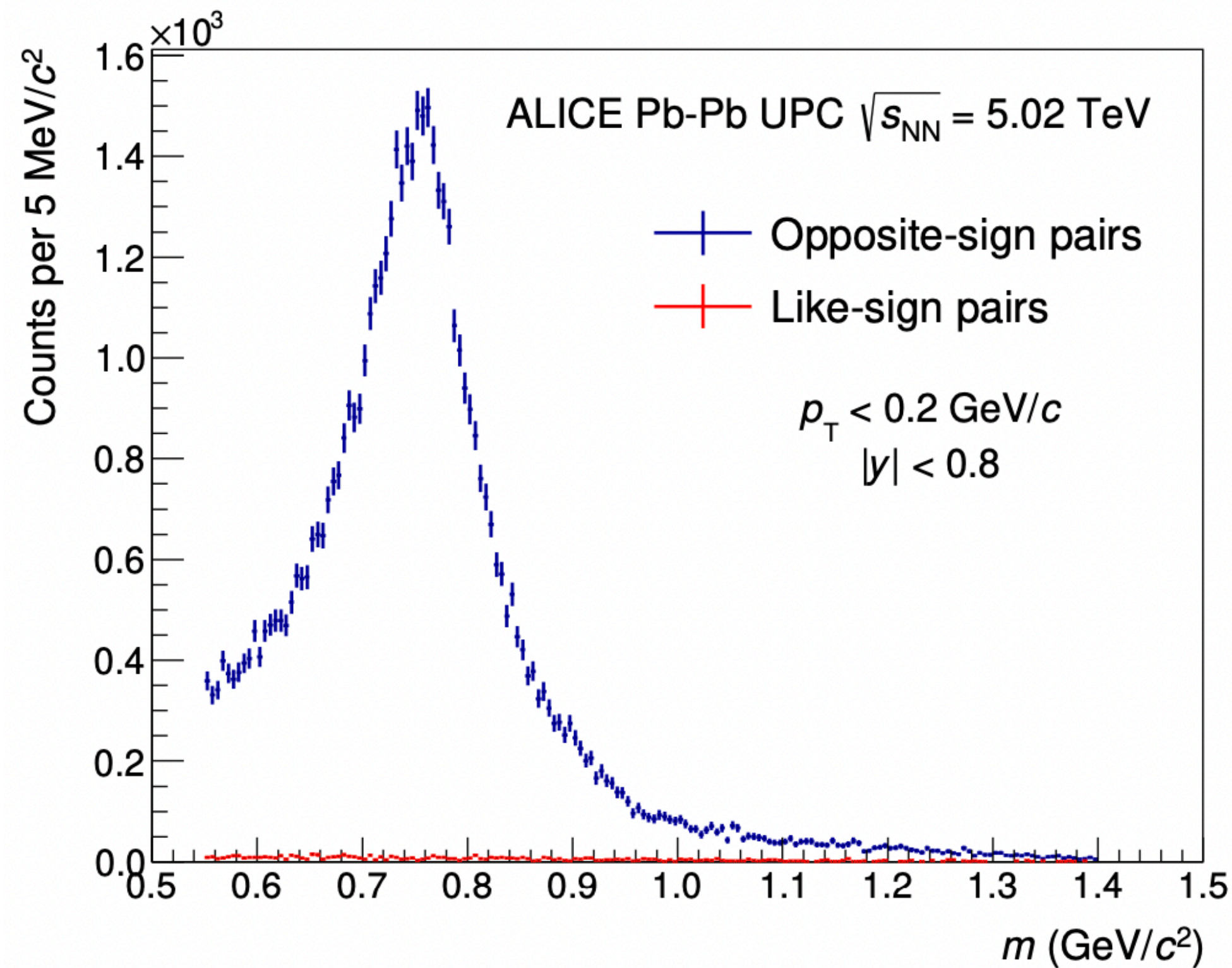
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Trigger on tracks and vetoes, measuring in EMD classes to test our knowledge of the photon flux

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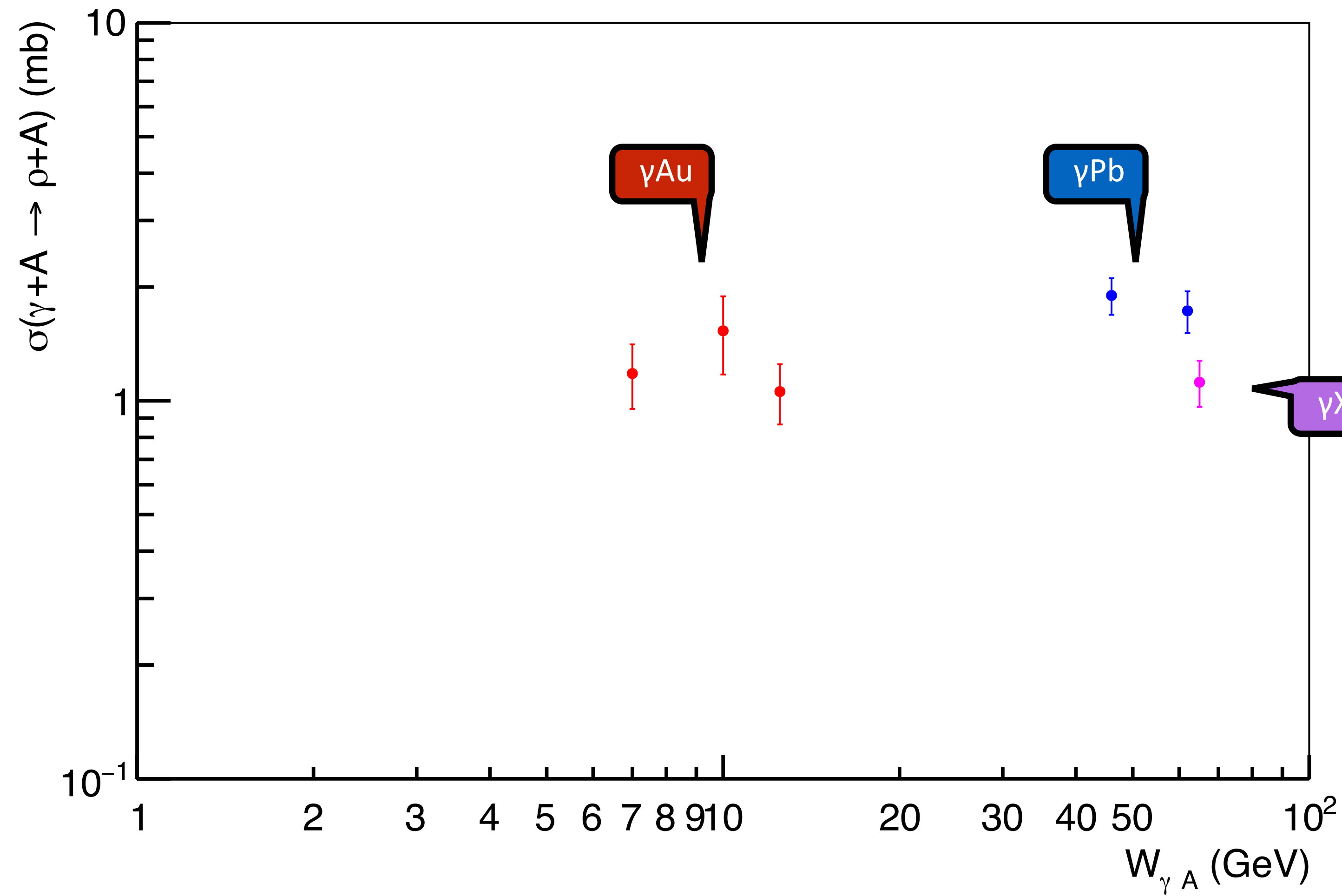
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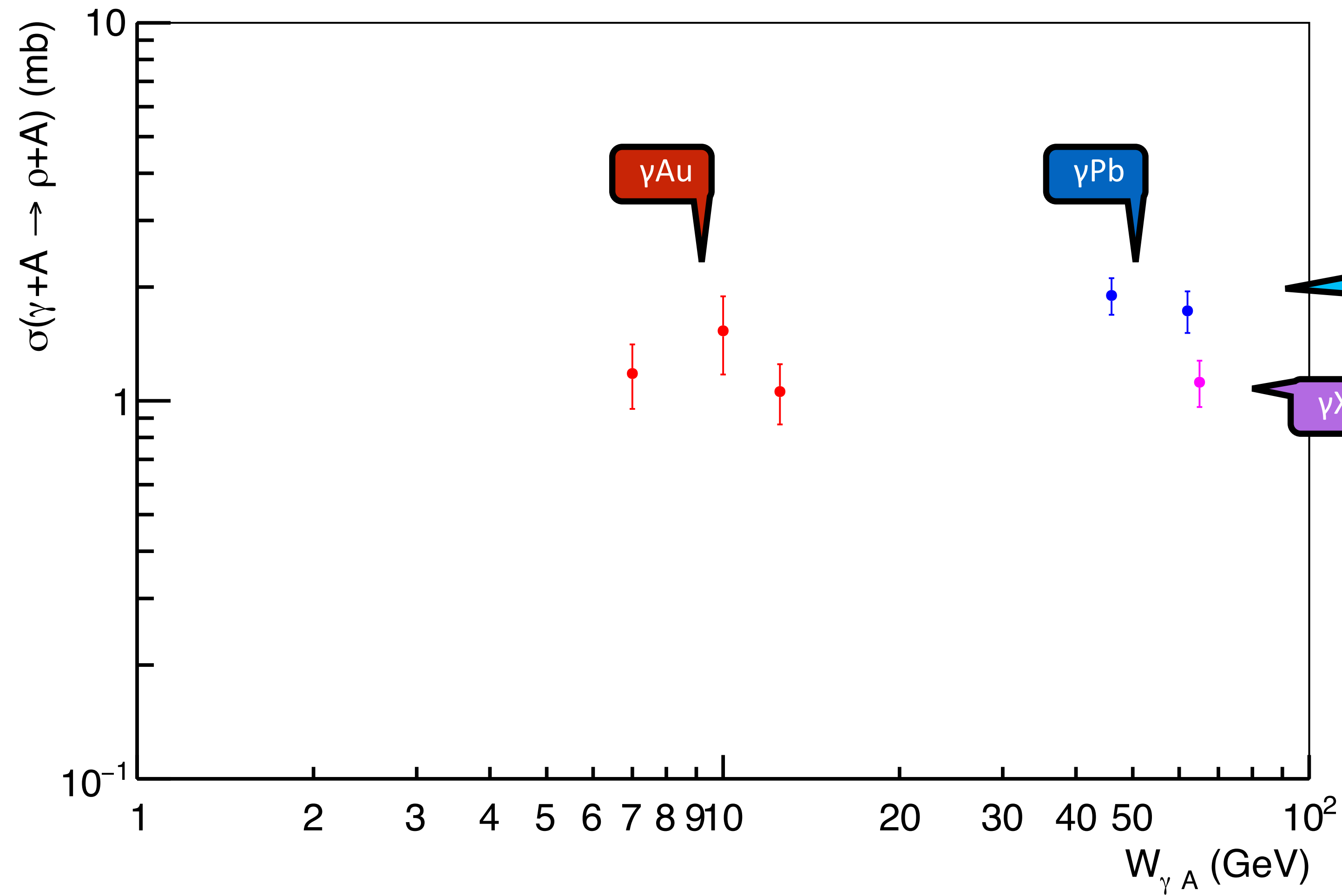
Trigger on tracks and vetoes, measuring in EMD classes to test our knowledge of the photon flux

Other measurements available at 2.76 TeV per NN

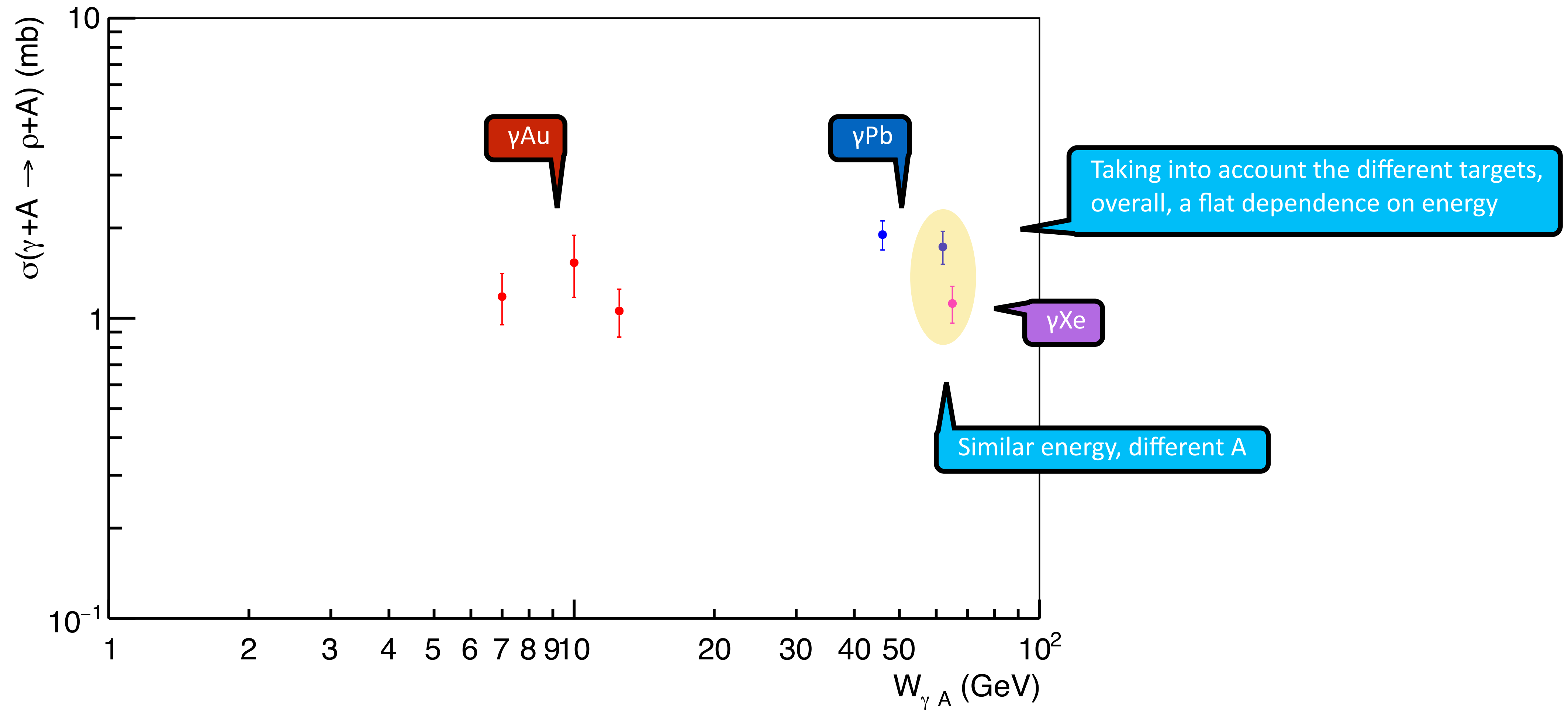
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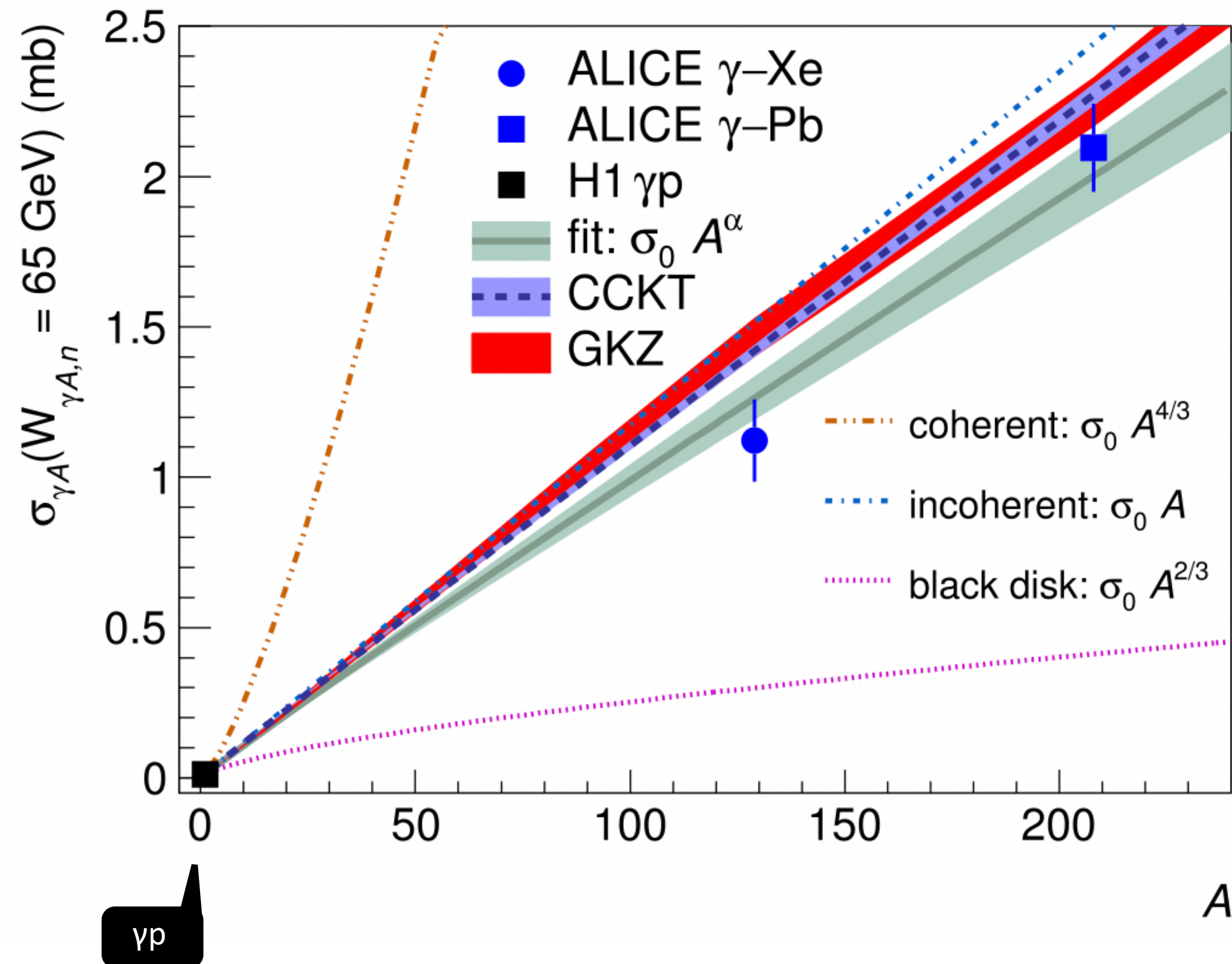
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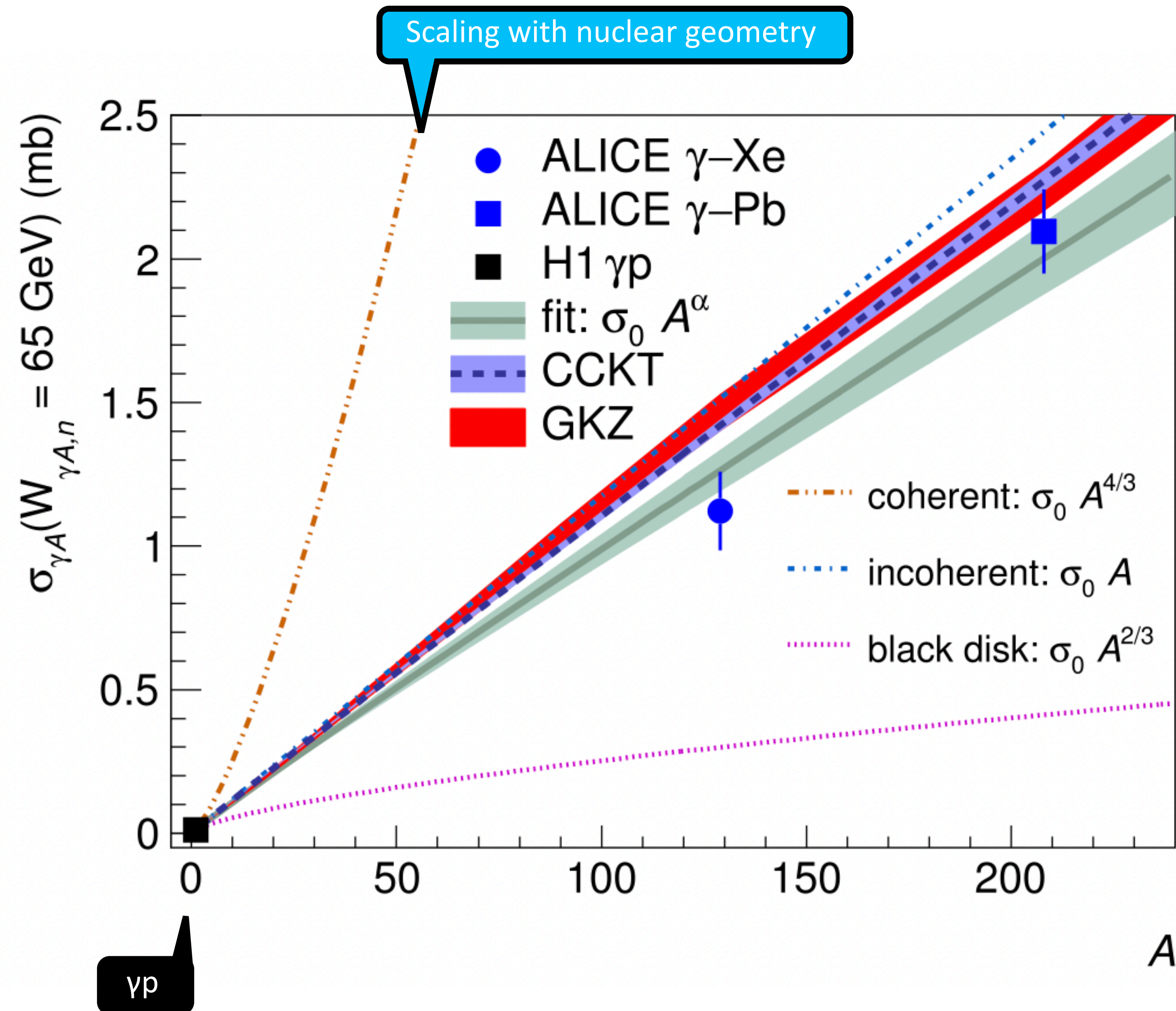
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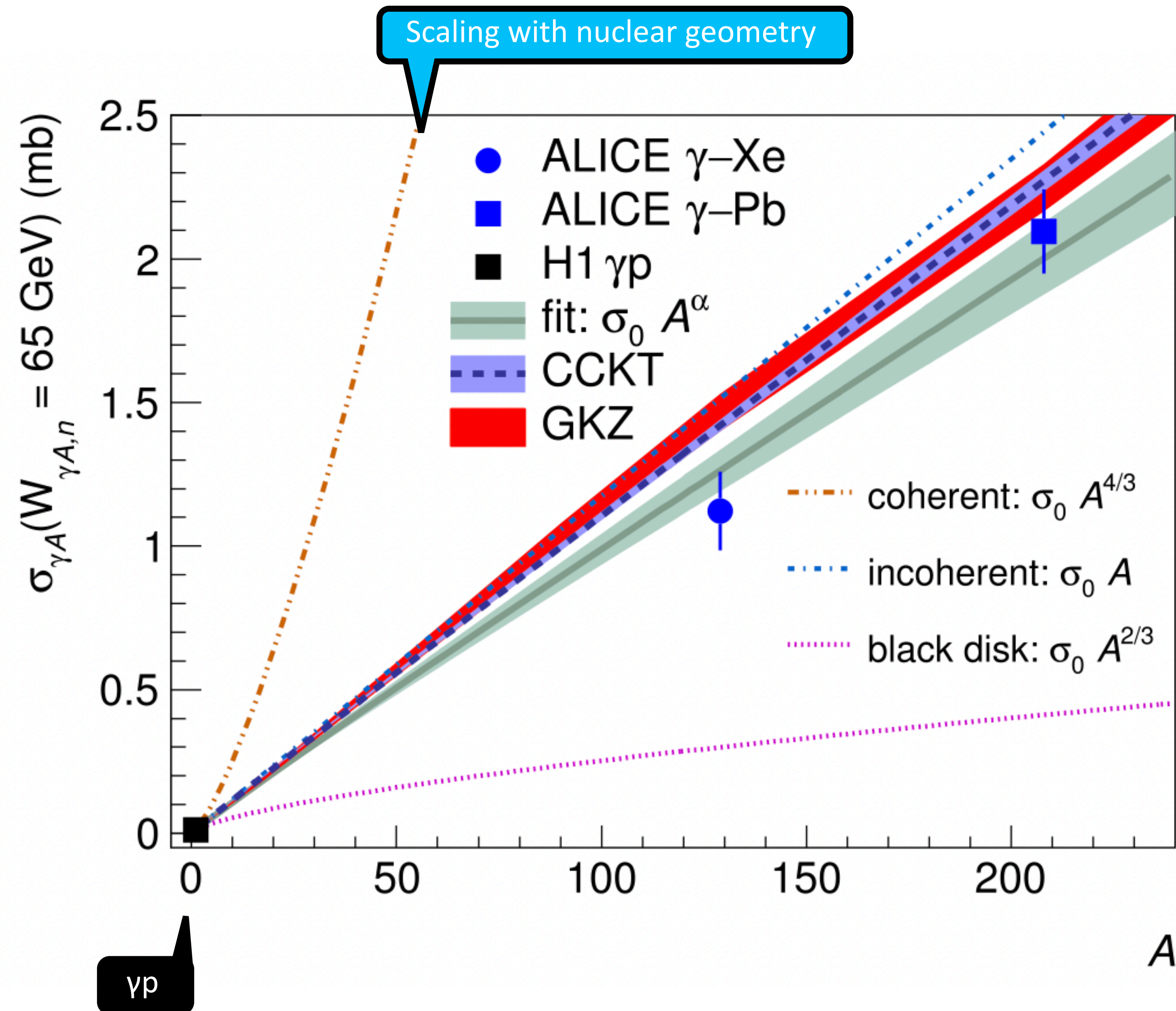
A dependence of coherent ρ^0 production at high energies



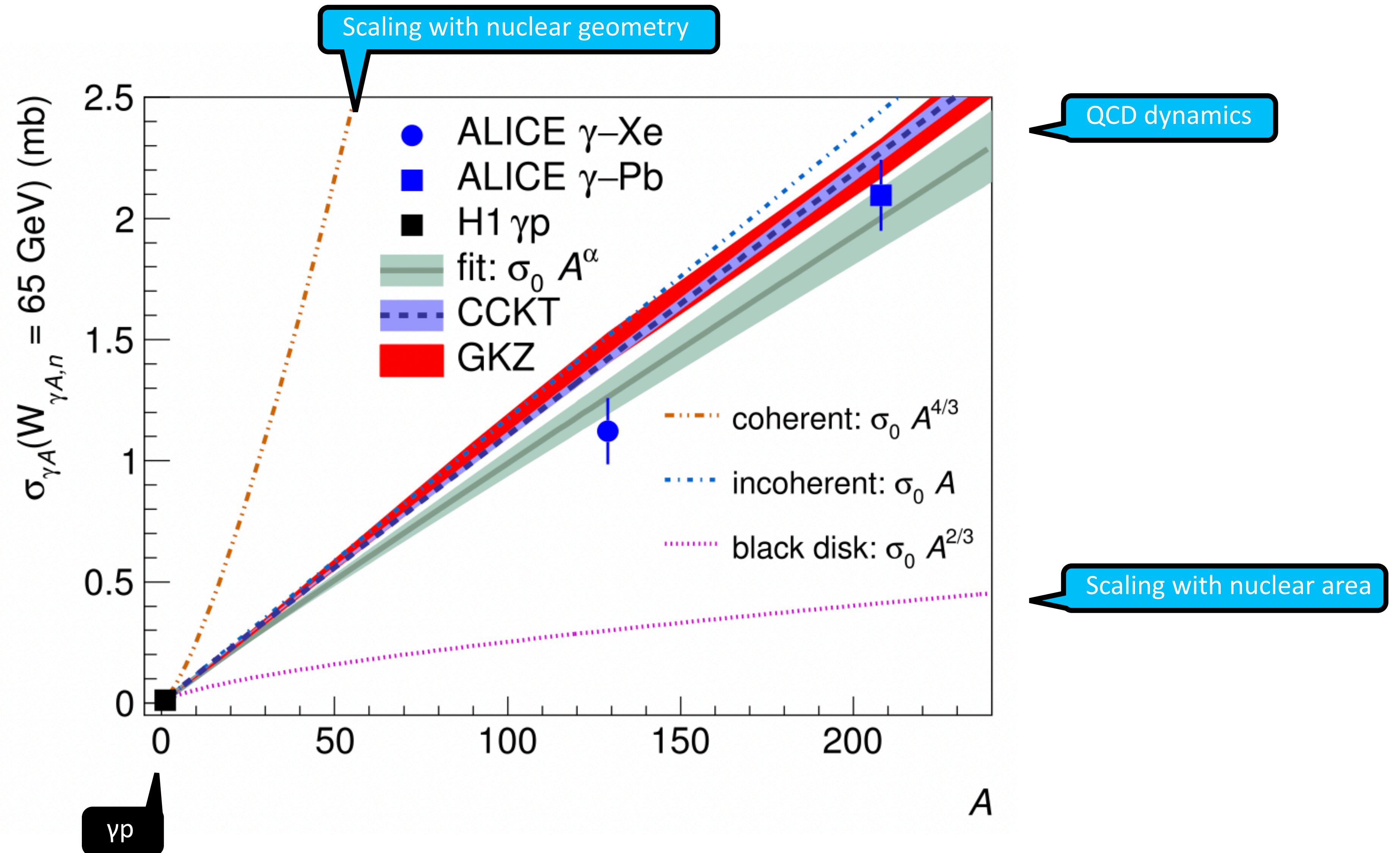
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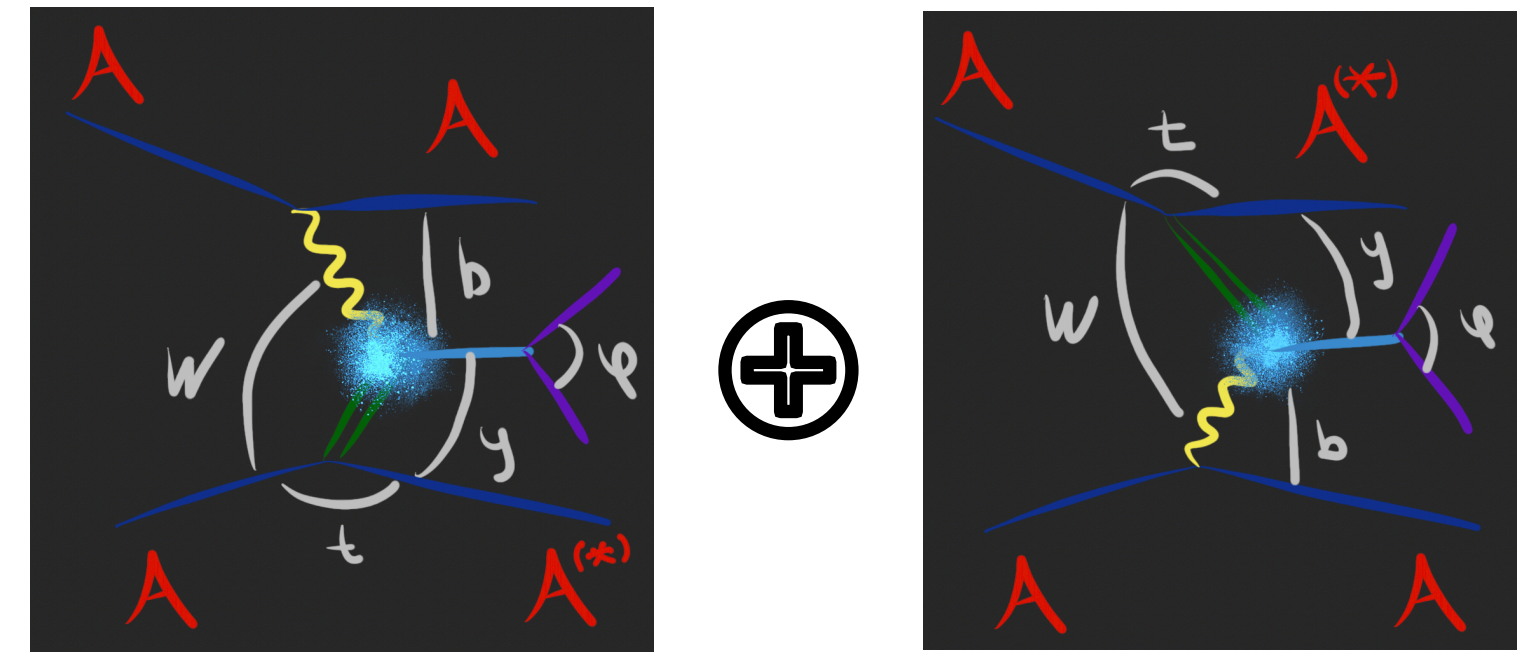
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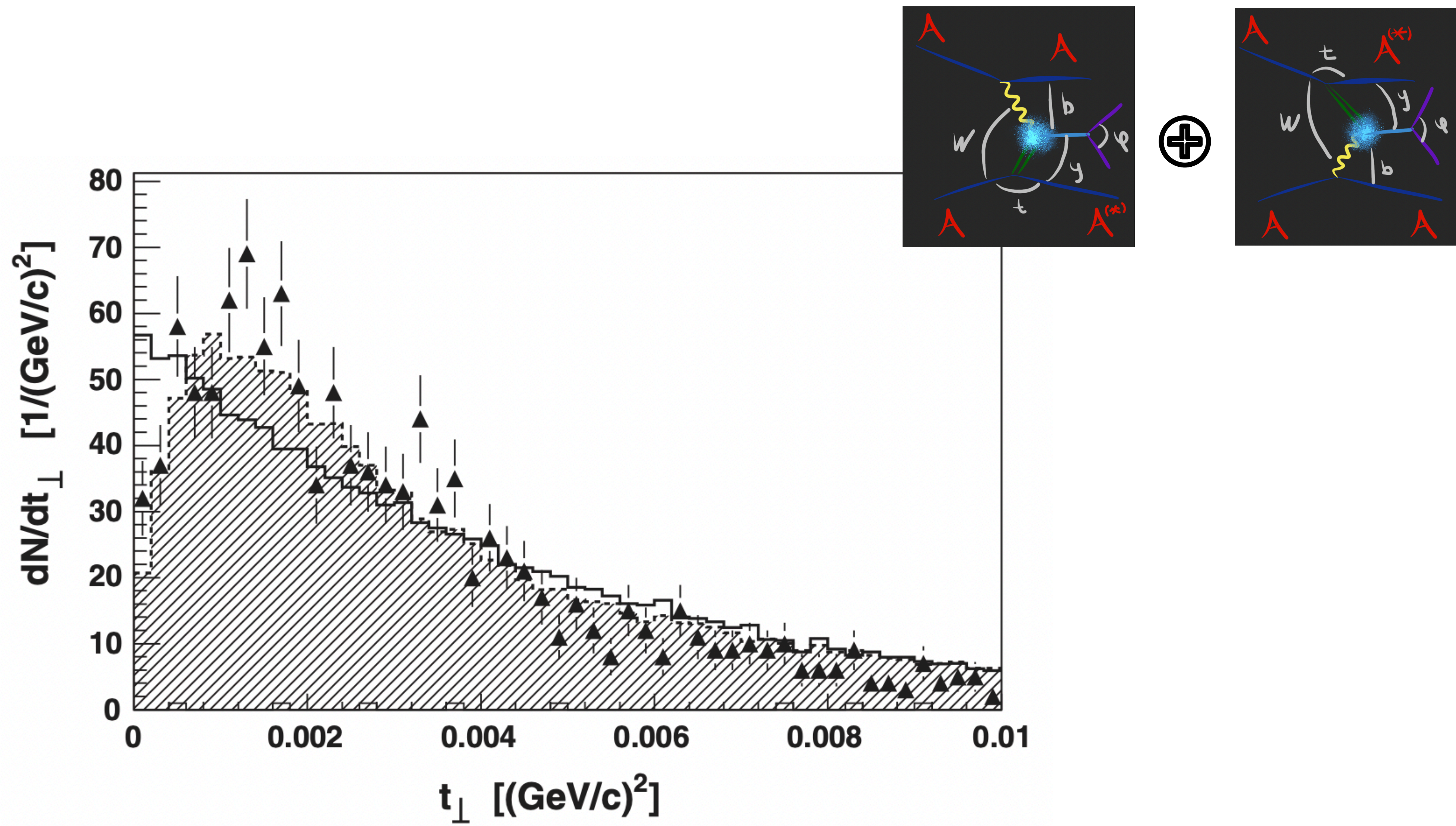
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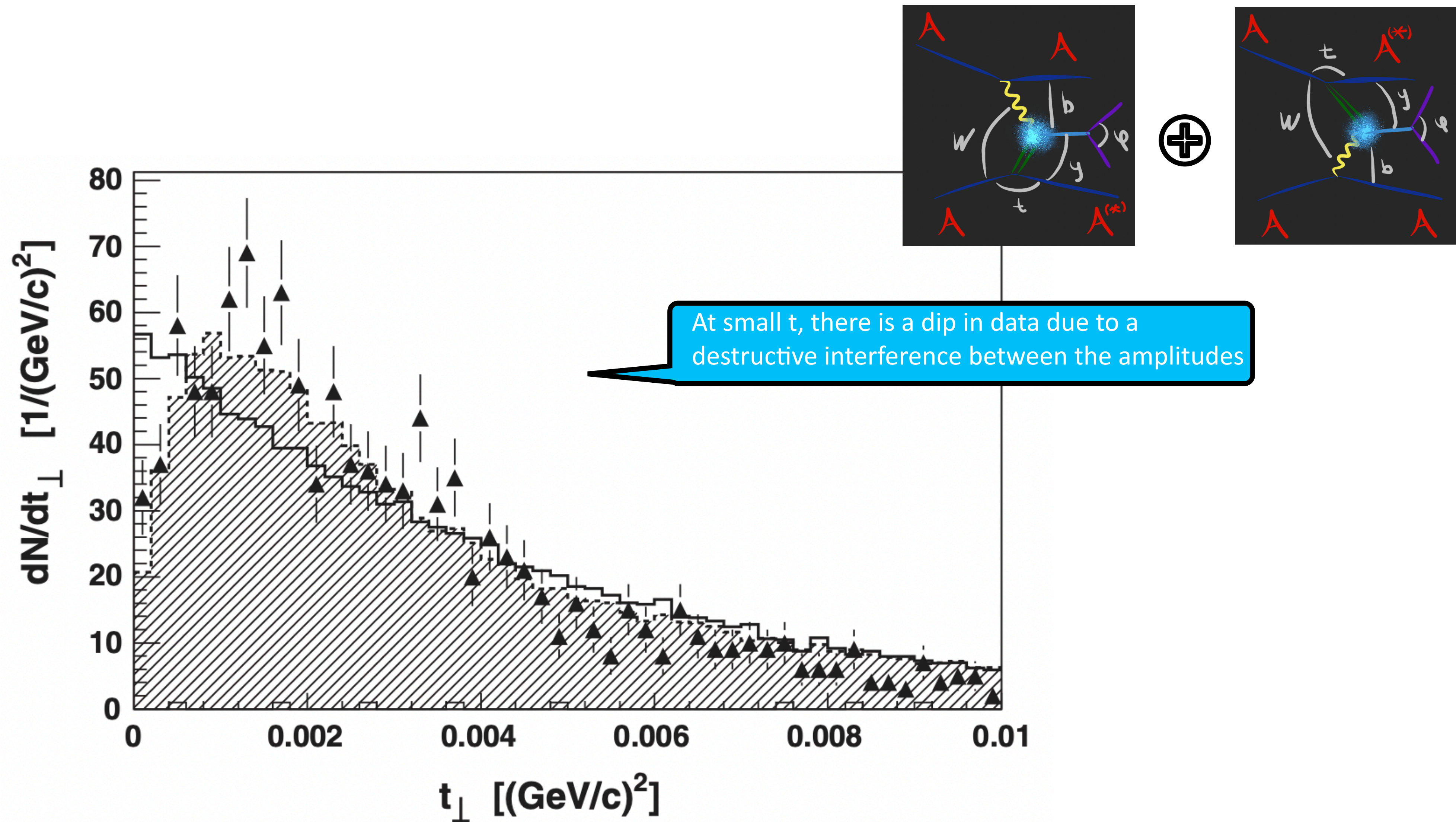
Interference effects in coherent ρ^0 production: t dependence



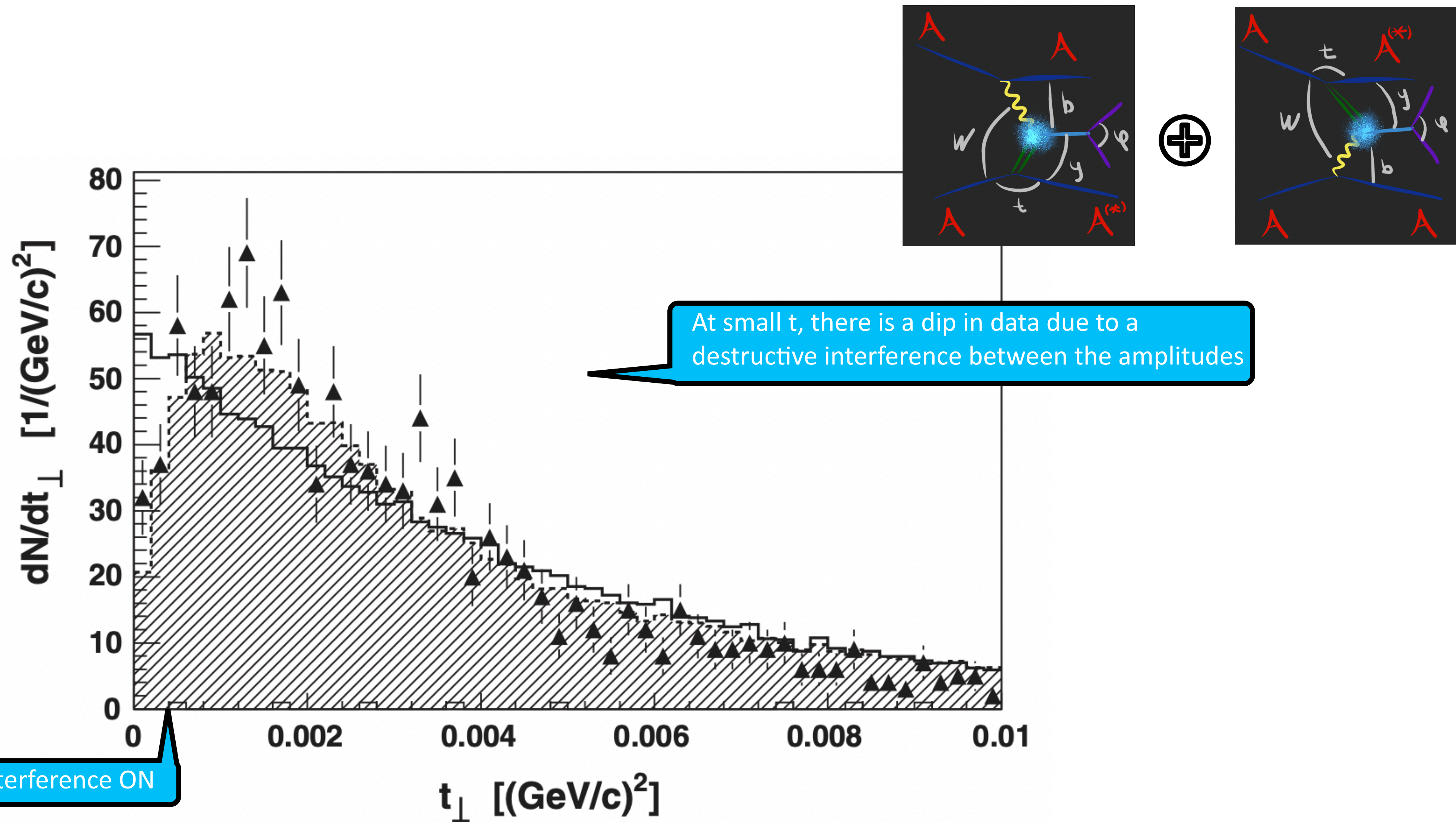
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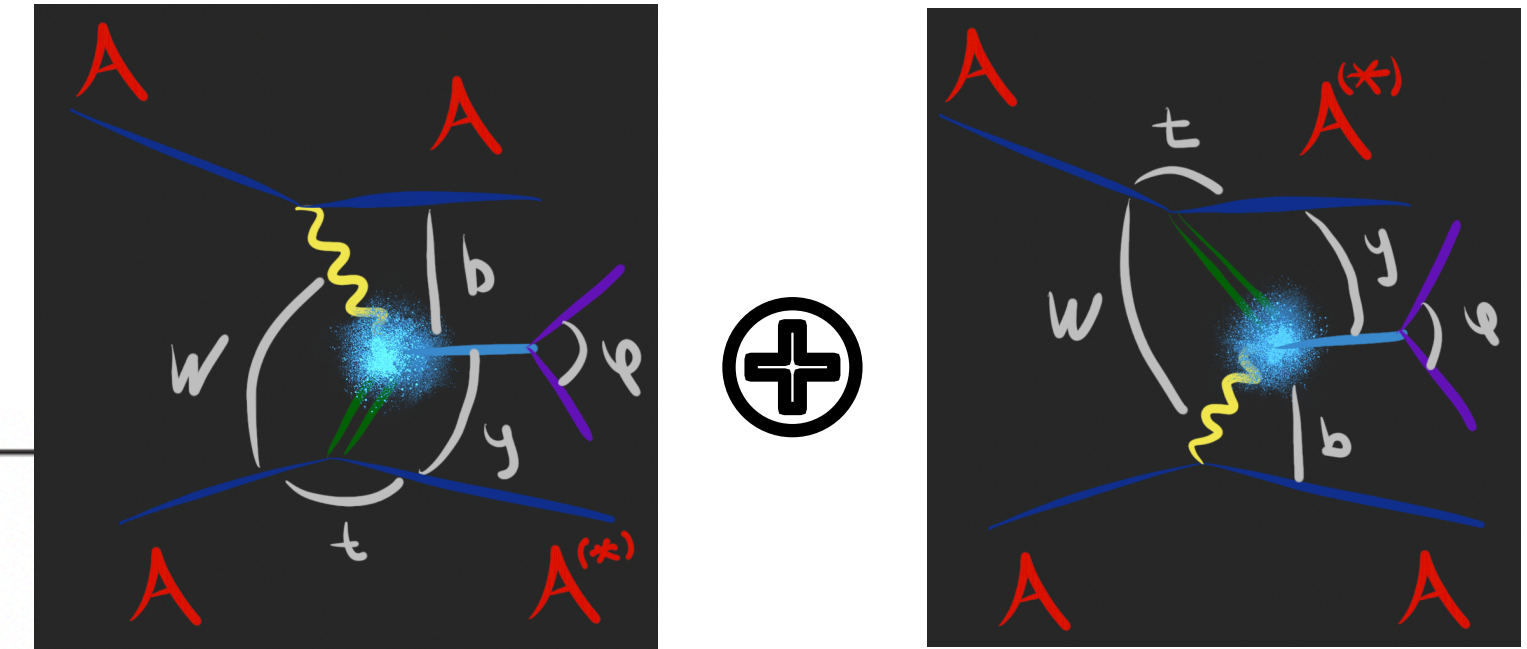
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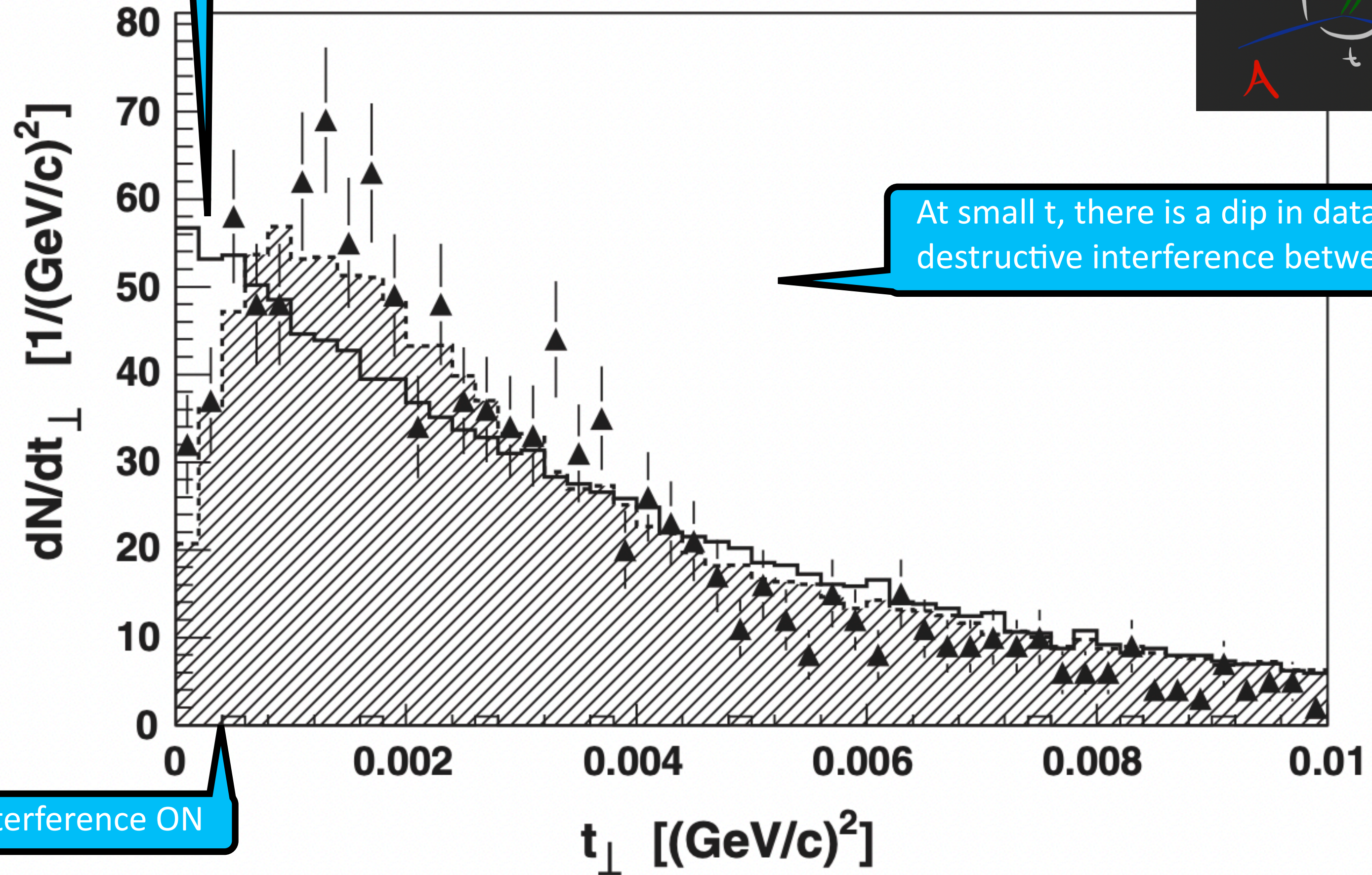
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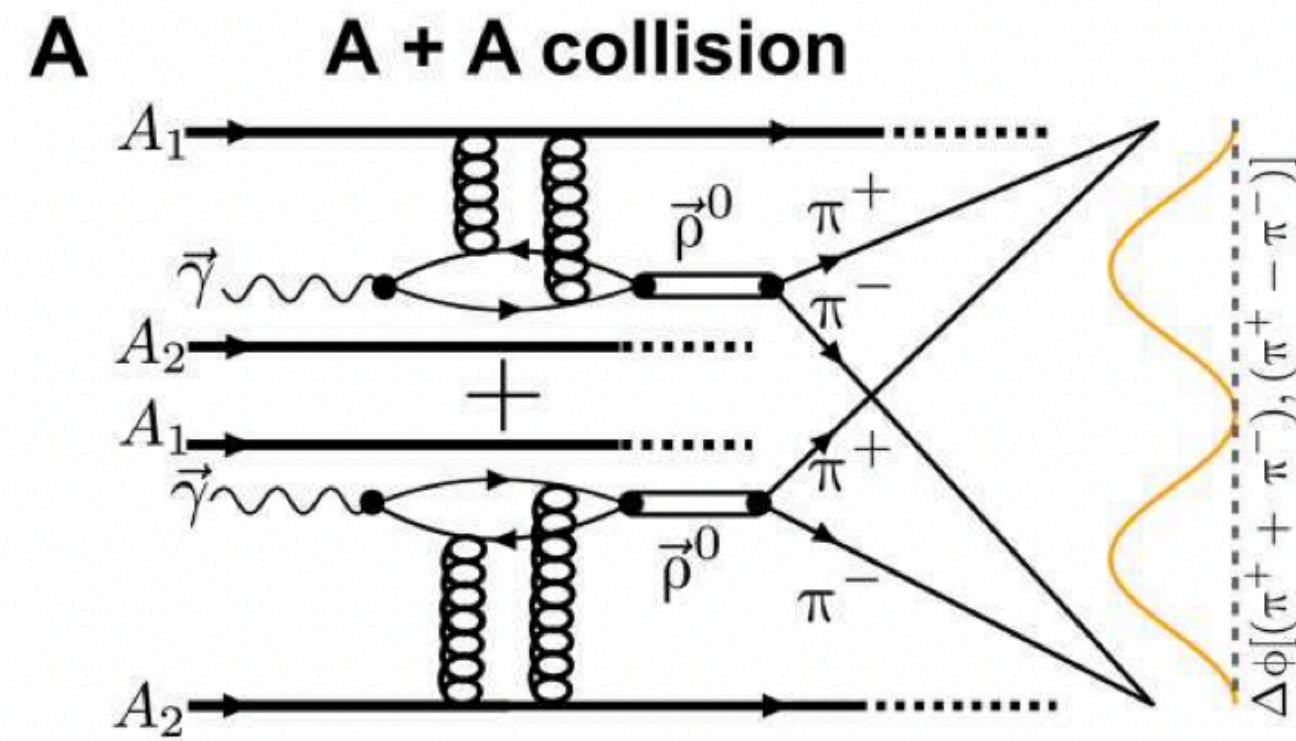
STARlight MC with interference OFF



At small t , there is a dip in data due to a destructive interference between the amplitudes

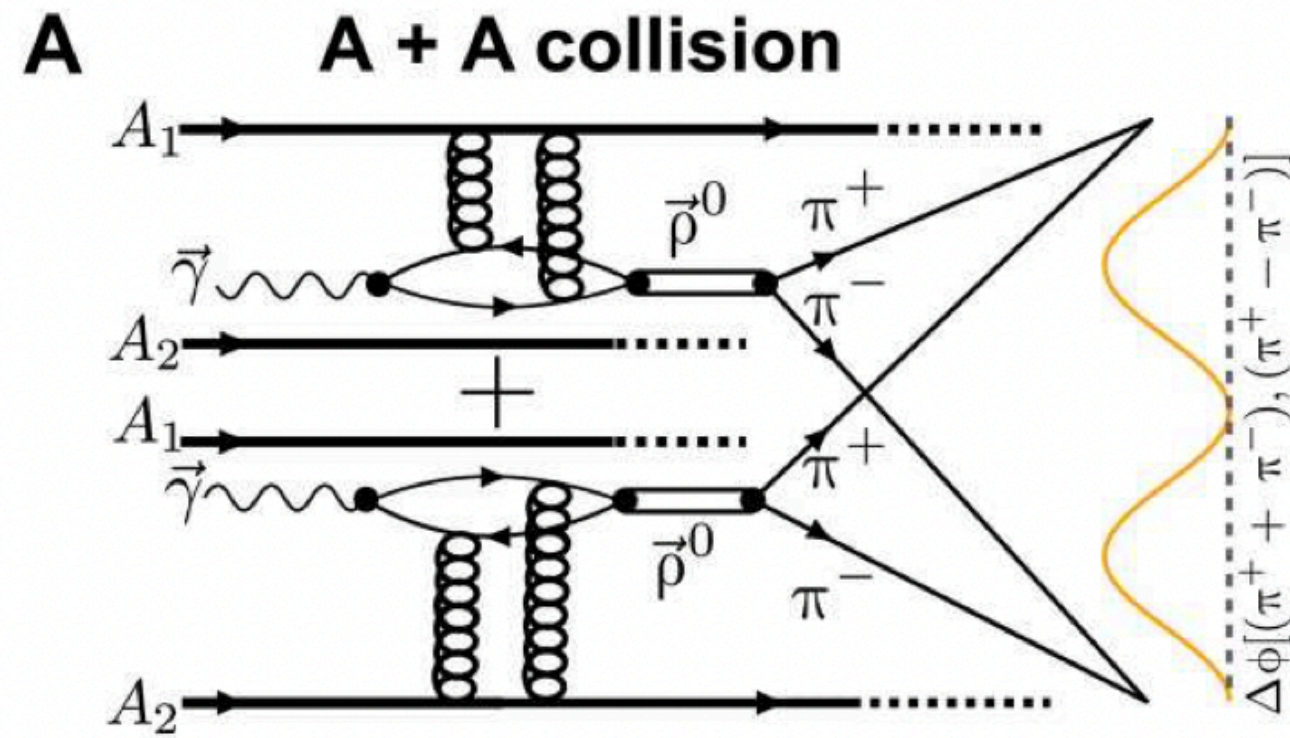
STARlight MC with interference ON

Interference effects in coherent ρ^0 production: azimuthal asymmetries at RHIC

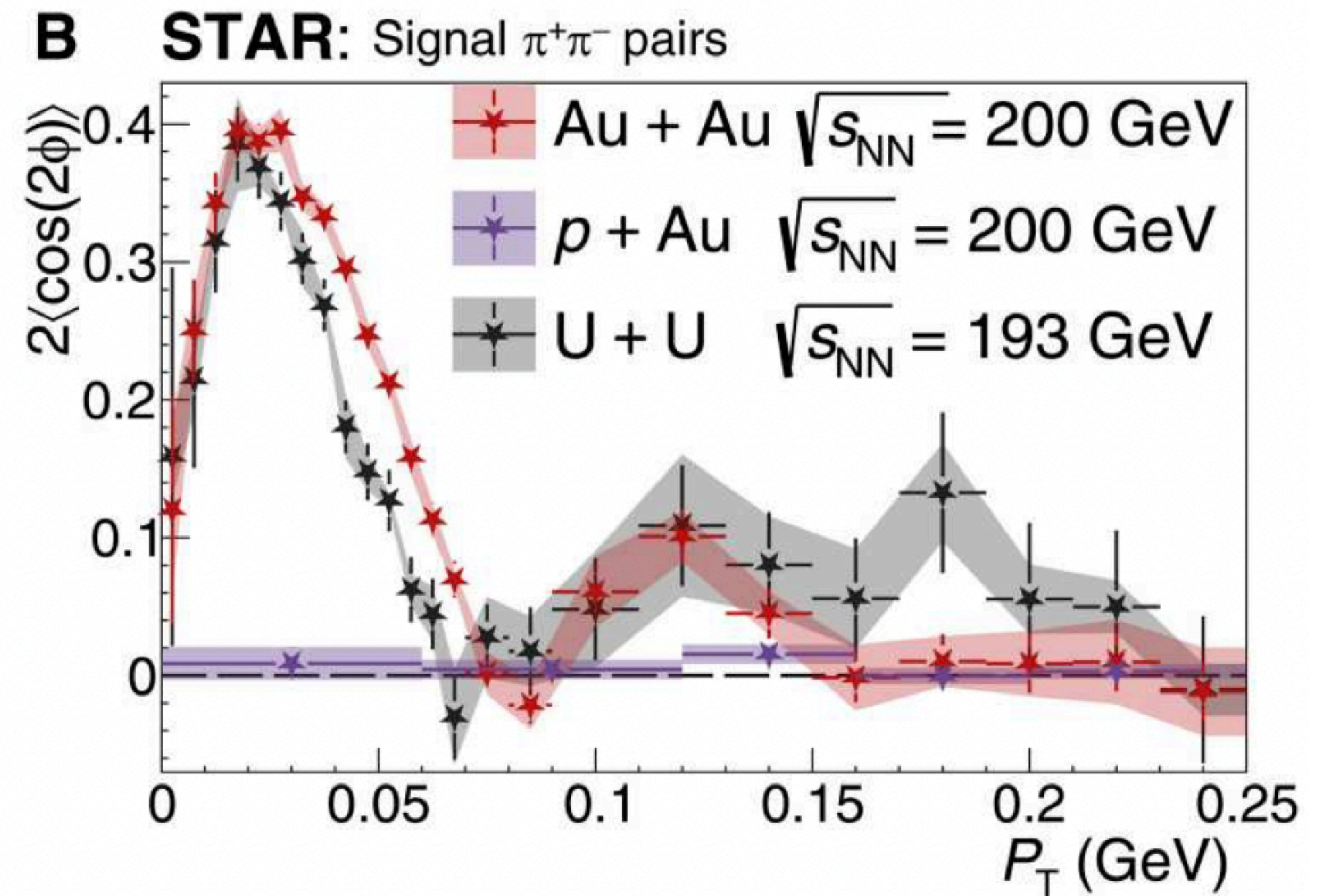
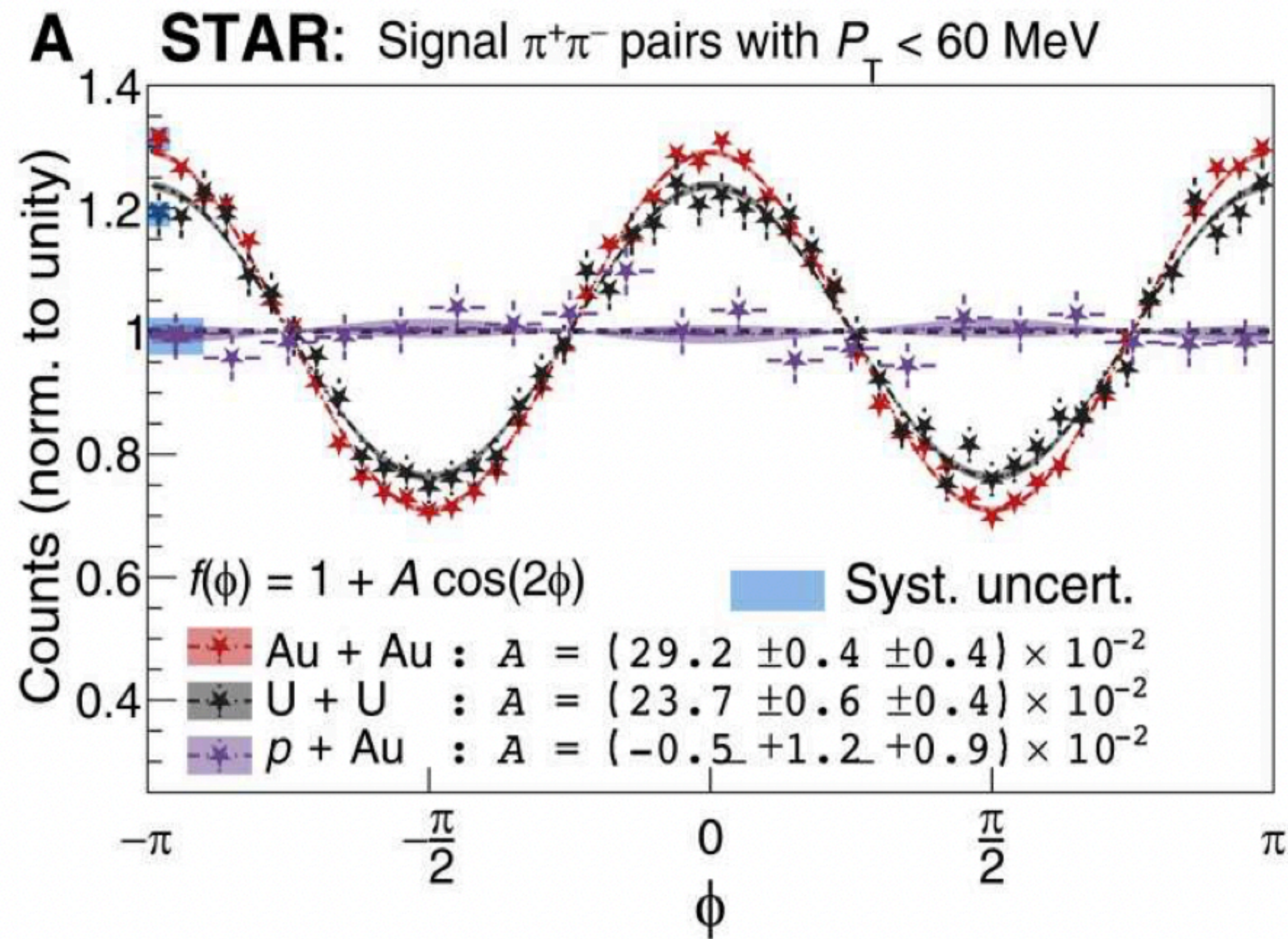


The interference between the amplitudes modifies the azimuthal correlations of the decay products

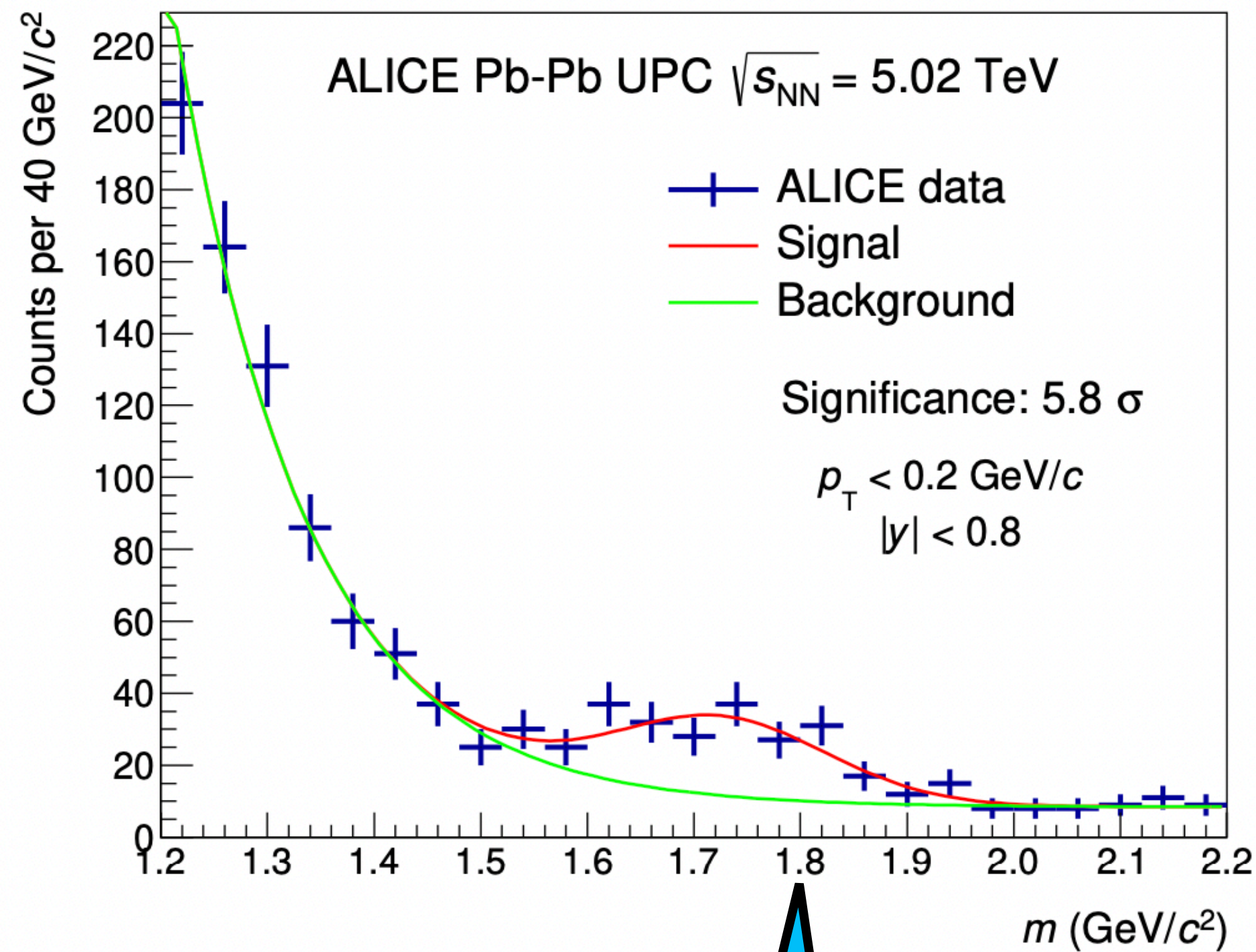
Interference effects in coherent ρ^0 production: azimuthal asymmetries at RHIC



The interference between the amplitudes modifies the azimuthal correlations of the decay products

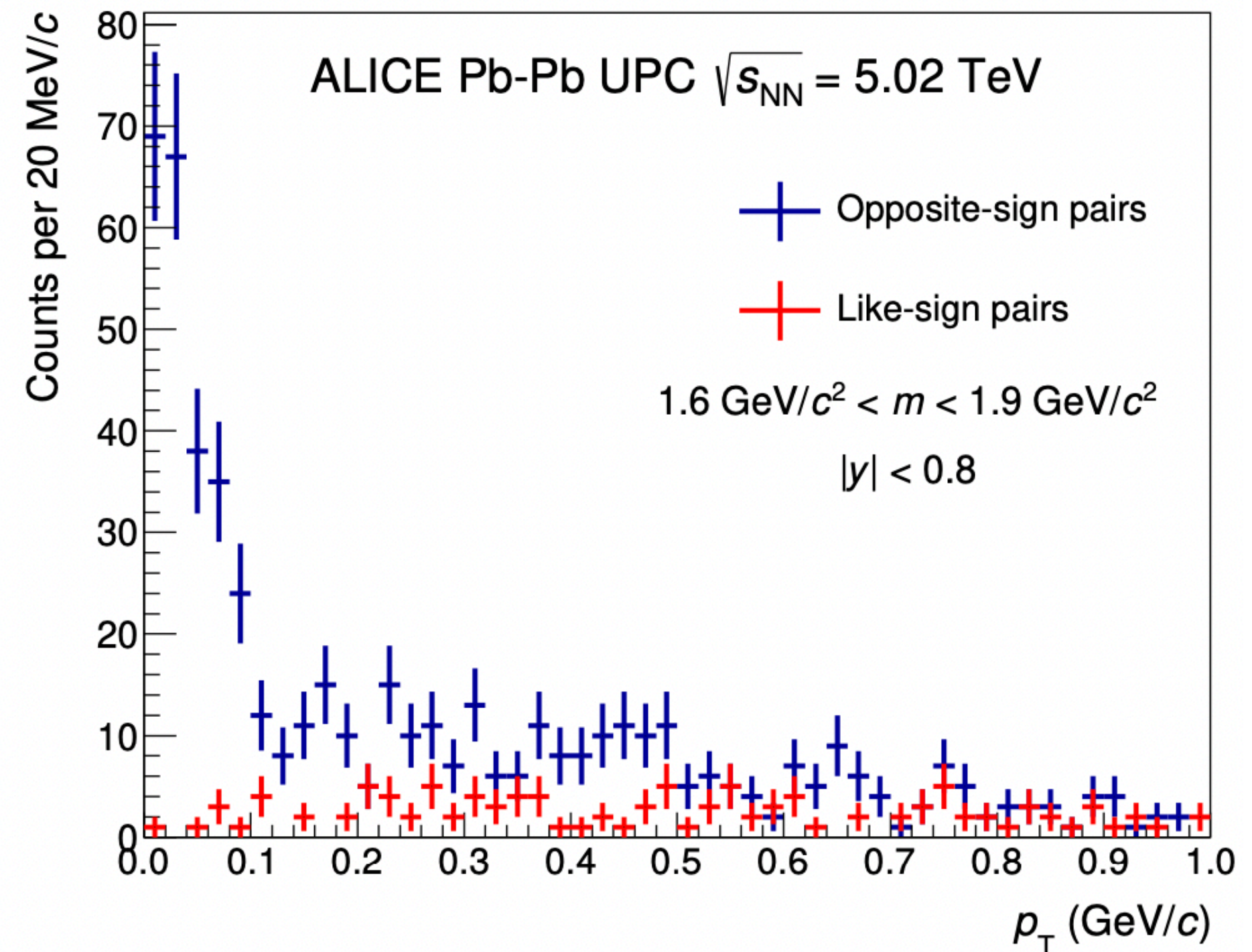


New (?) resonances in coherent $\pi\pi$ production

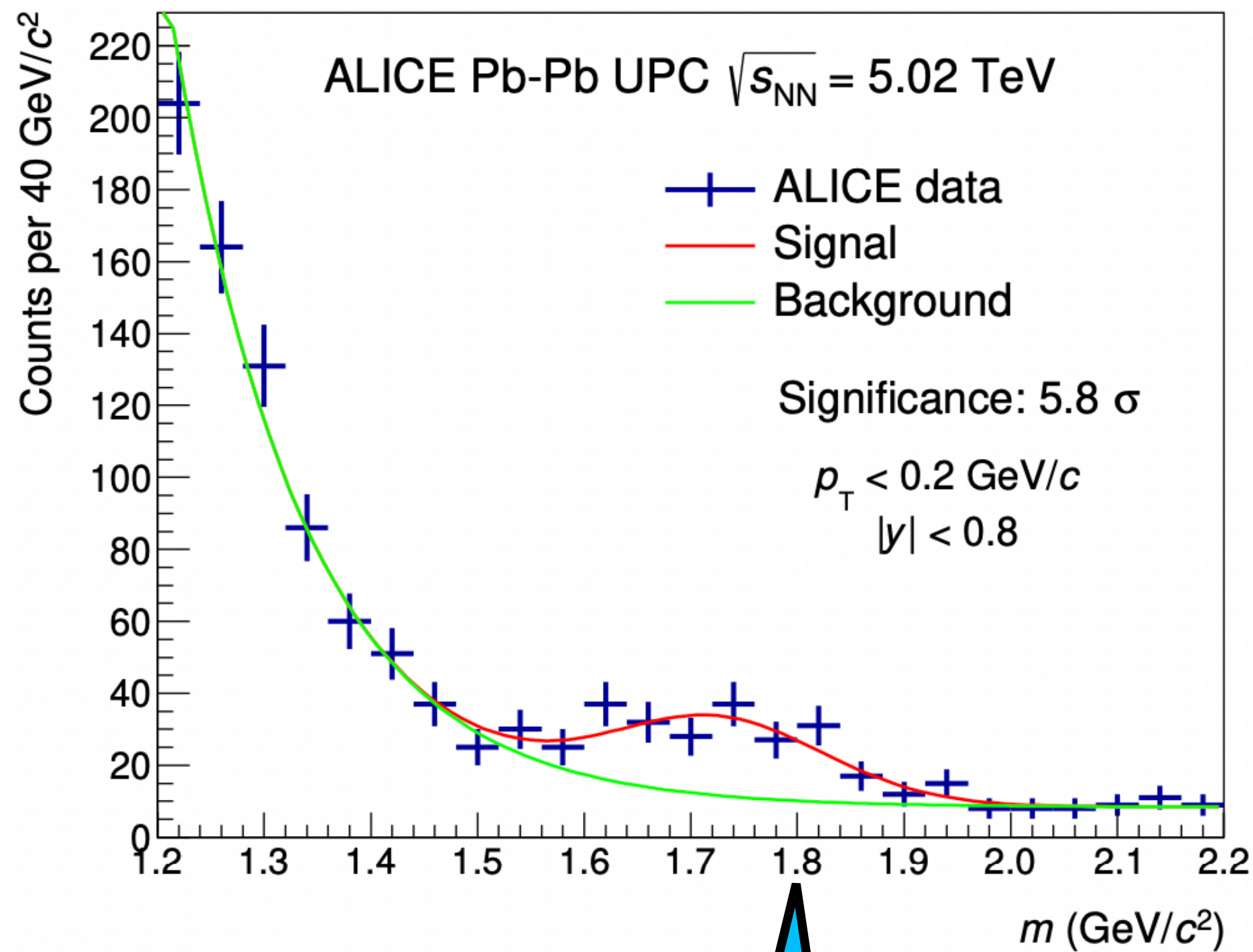


Bump in the invariance mass distribution of pion pairs

Transverse momentum distribution typical of coherent processes



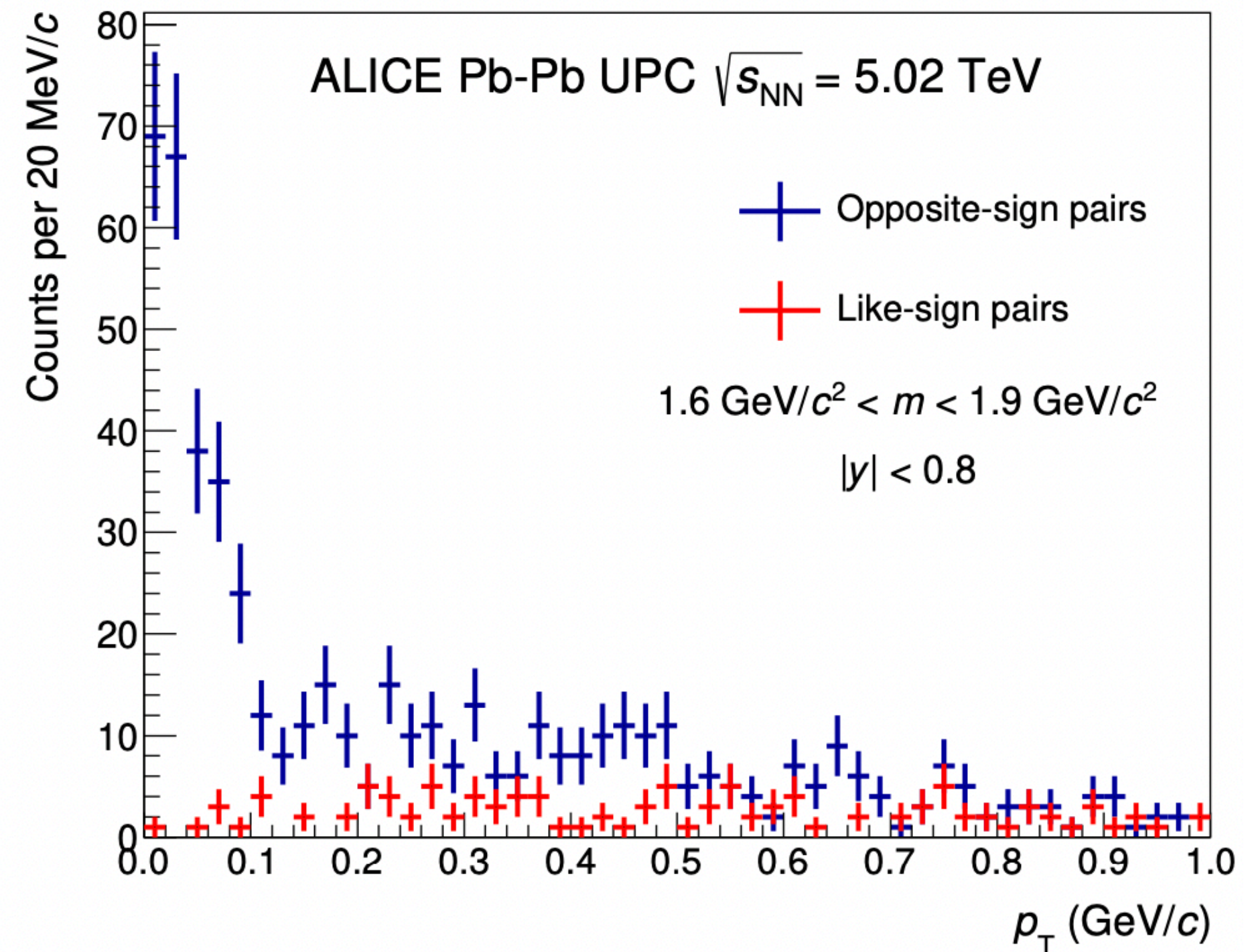
New (?) resonances in coherent $\pi\pi$ production



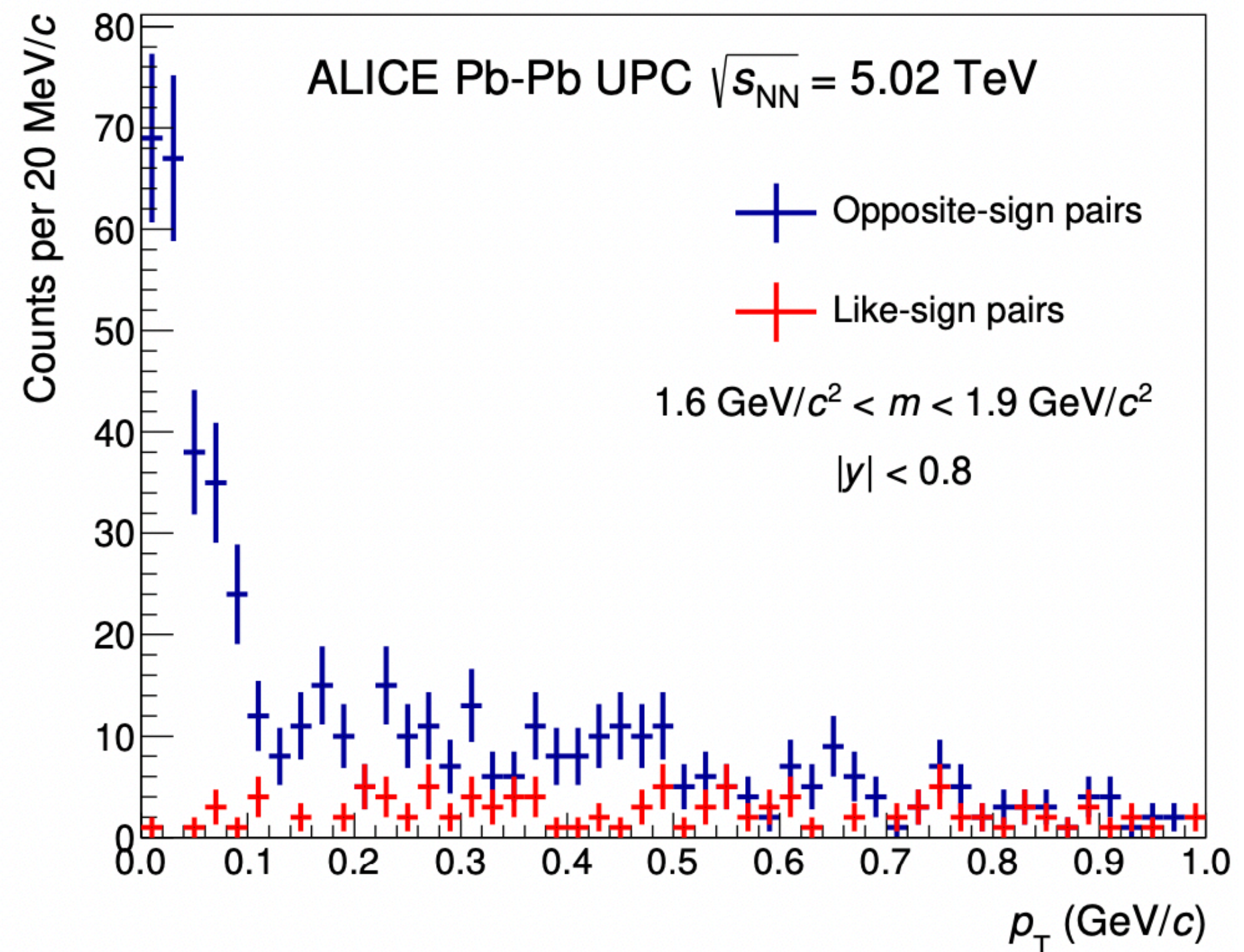
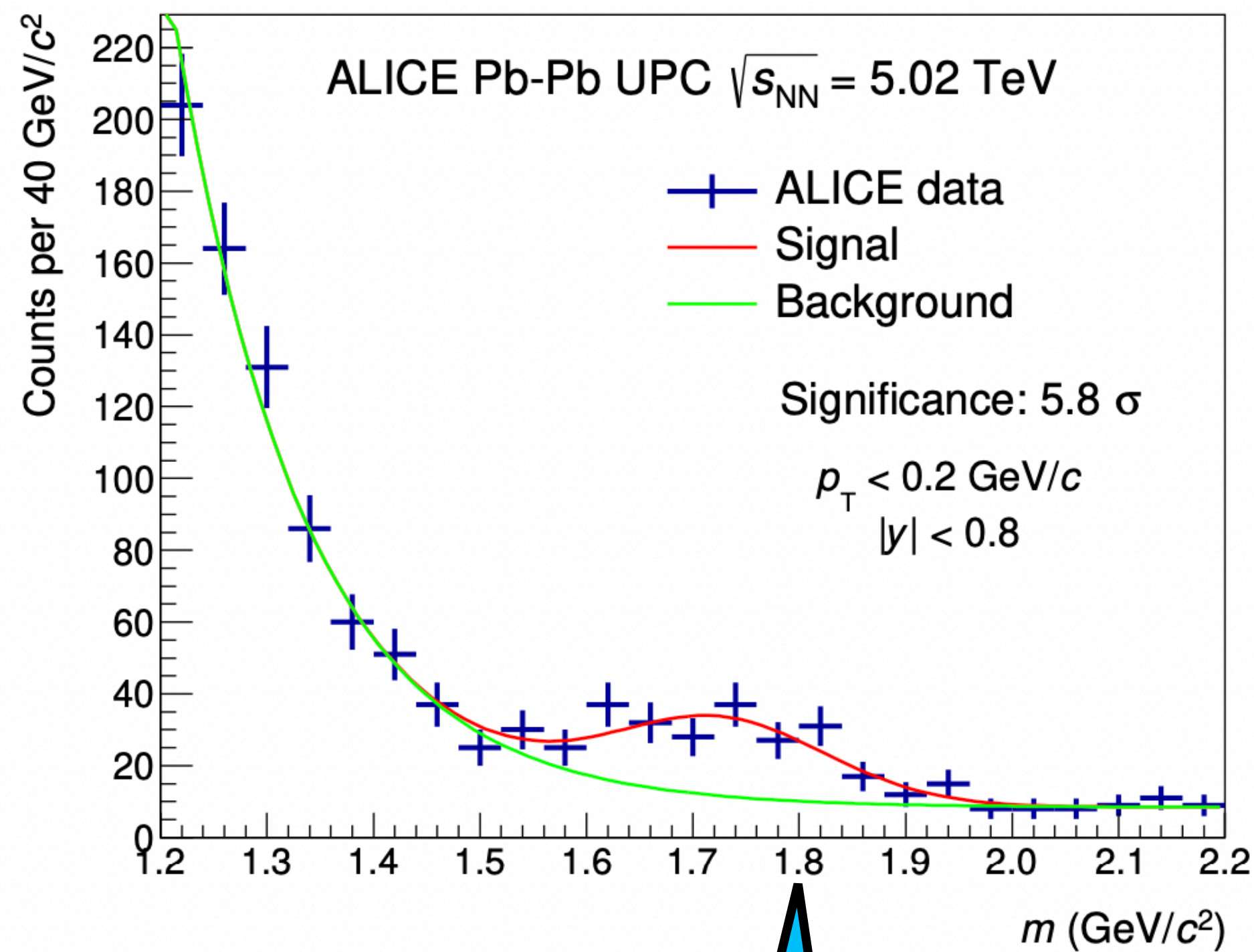
Bump in the invariance mass distribution of pion pairs

Similar structures seen by H1, ZEUS, STAR

Transverse momentum distribution typical of coherent processes



New (?) resonances in coherent $\pi\pi$ production



Transverse momentum distribution typical of coherent processes

Bump in the invariance mass distribution of pion pairs

Similar structures seen by H1, ZEUS, STAR

The large improvement in luminosity in Run 3 may reveal more of these structures and allow for the determination of their properties

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and what we are doing now at RHIC and LHC

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Homework:

Enjoy the meeting!