

UPC 2023: International workshop on the physics of Ultra Peripheral Collisions  
December 10-15, Playa del Carmen, Mexico

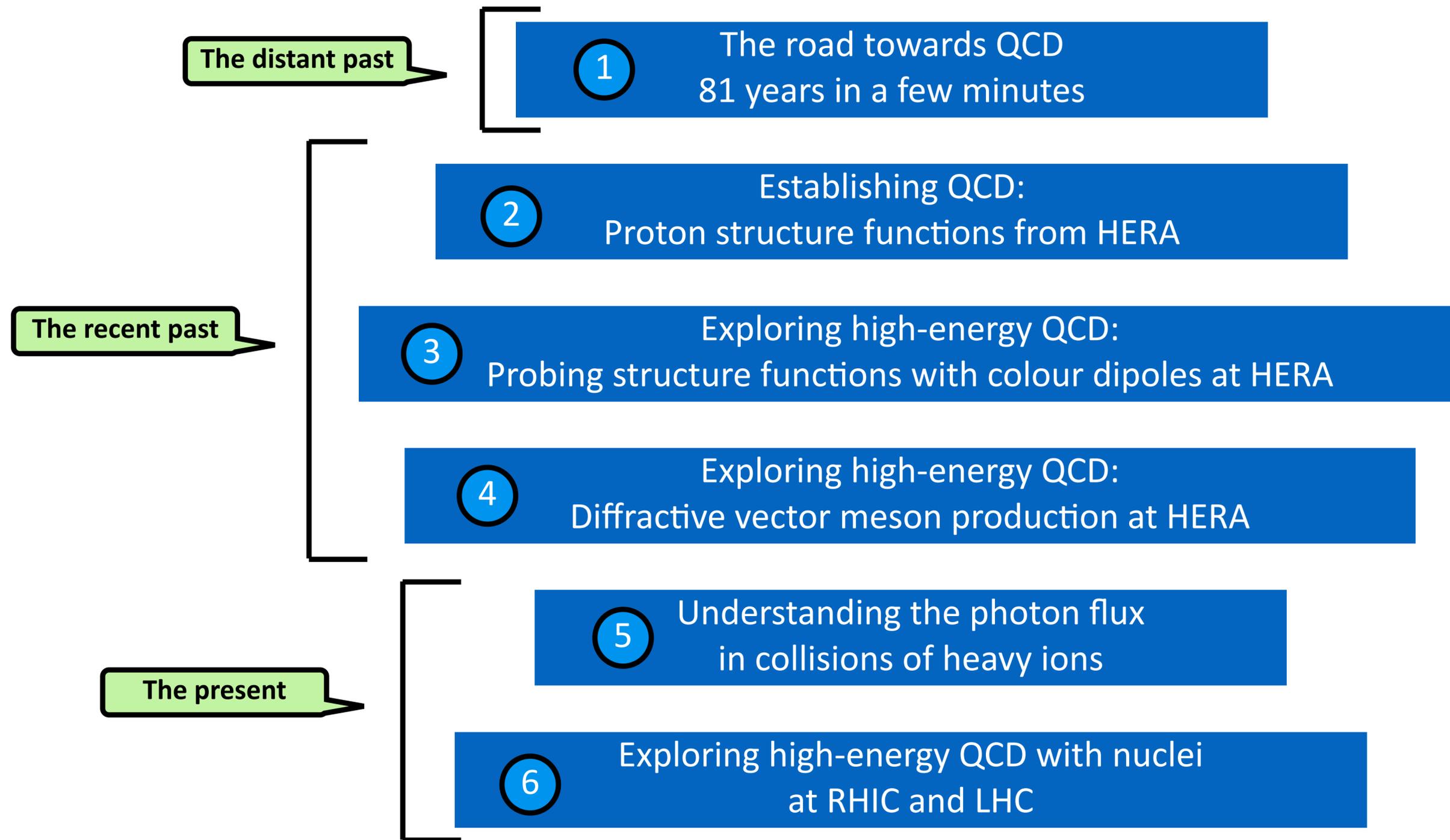
## Photon-induced process to understand QCD (Mainly from the point of view of experiments)

Guillermo Contreras

Czech Technical University in Prague



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The road towards QCD  
81 years in a few minutes

Science is a conversation amongst people  
that takes place through articles

We have arrived late to this conversation, so let's have a look at what people have been talking about in the past

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In order to understand a bit better what we will discuss during this week

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Homework:

try to read at least one of the original papers in the next few pages

Photon-induced processes to understand the QCD structure of hadrons

Hadrons?

Photon-induced processes to understand the QCD structure of hadrons

Photon-induced processes to understand the QCD structure of hadrons

Hadrons?

structure?

Photon-induced processes to understand the QCD structure of hadrons

QCD?

Hadrons?

structure?

# The first hadrons

Before we knew they were hadrons!

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Atoms have nuclei

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Some of the first models for the new force

New force and new particle carrying the force

**1932: Nuclei of protons and neutrons (Heisenberg)**

<https://link.springer.com/article/10.1007/BF01342433>

**1935: A model for the nuclear force (Yukawa)**

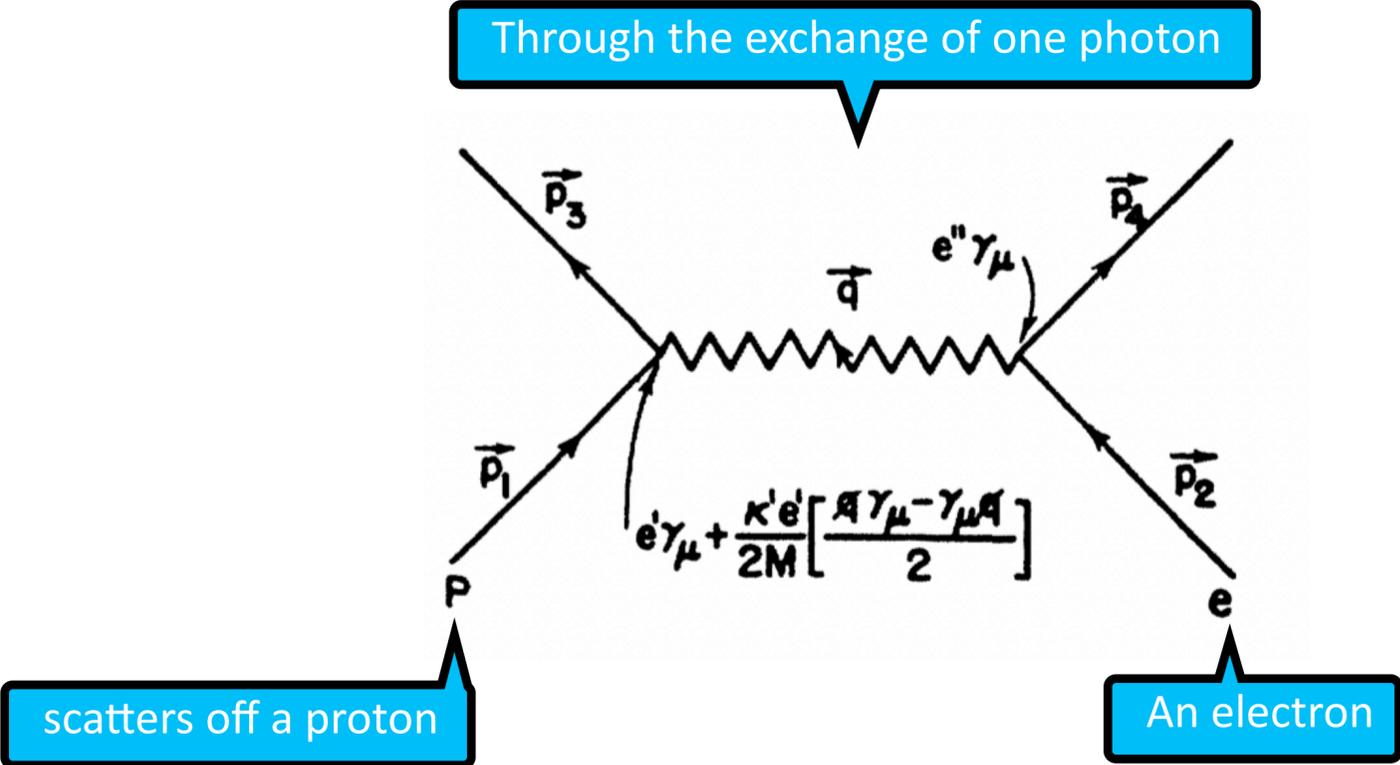
<https://academic.oup.com/ptps/article/doi/10.1143/PTPS.1.1/1878532>

At this point in time, we have hadrons and a new force

# Studying hadrons with light

1950: High energy ep elastic scattering (Rosenbluth)

<https://journals.aps.org/pr/abstract/10.1103/PhysRev.79.615>



# Studying hadrons with light

.... many other papers ...

1926: Collisions in QM (Born)

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1928: Relativistic QM (Dirac)

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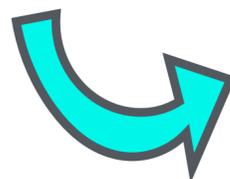
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1946-1948-: QED (Tomonaga, Schingwer, Feynman)

<https://academic.oup.com/ptp/article/1/2/27/1877120>

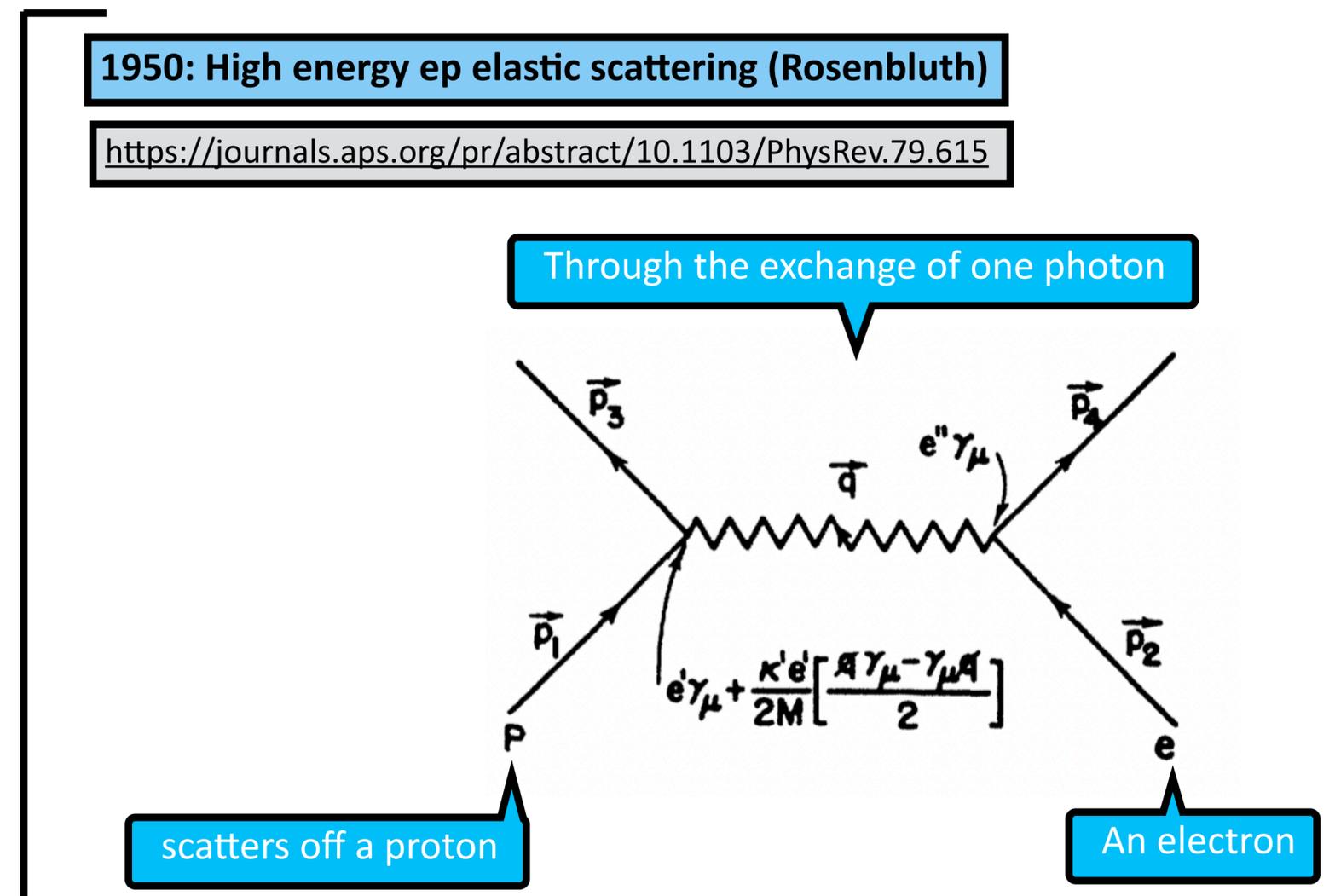
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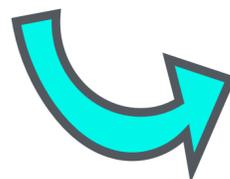
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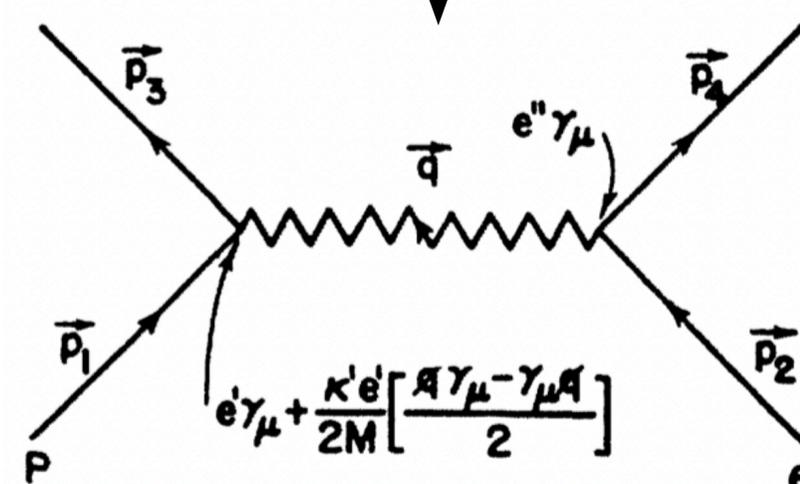
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Through the exchange of one photon

scatters off a proton

An electron



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Experiments to be performed with accelerators

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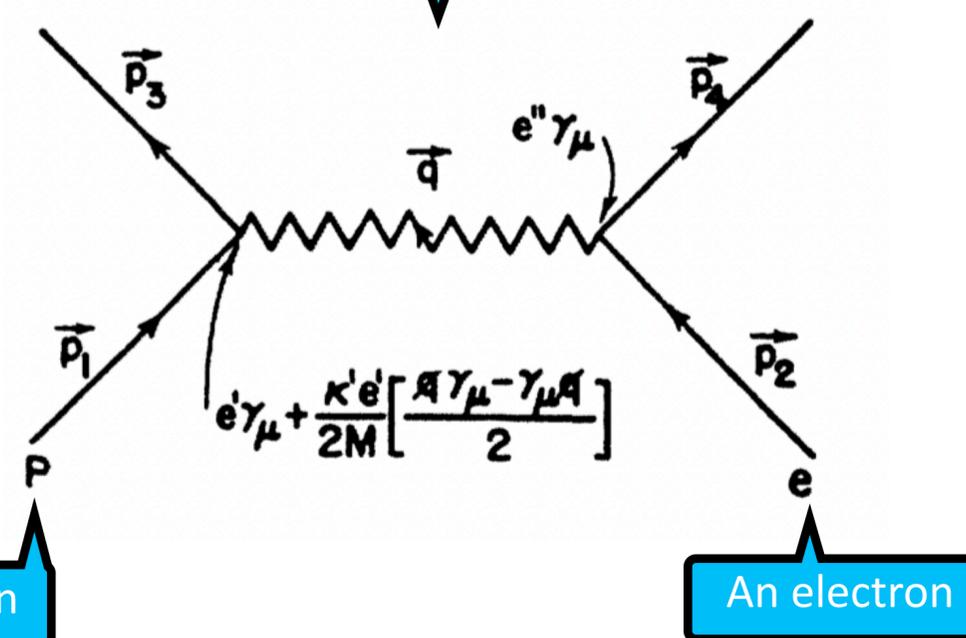
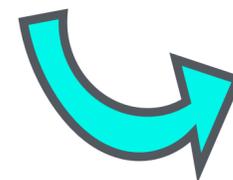
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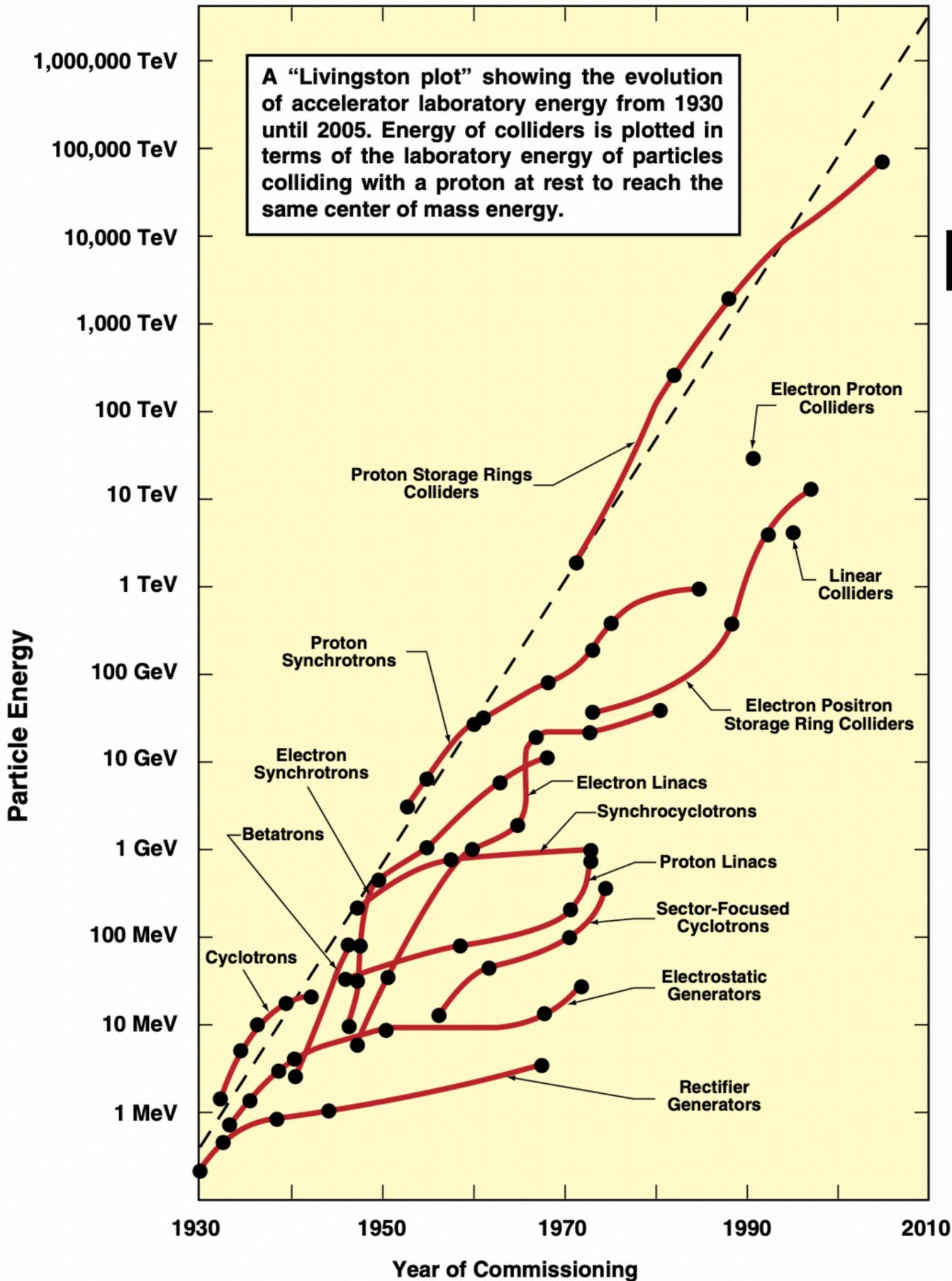
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... and we also have accelerators ...

To study the proton, probes at high energies (small de Broglie wave length) are needed

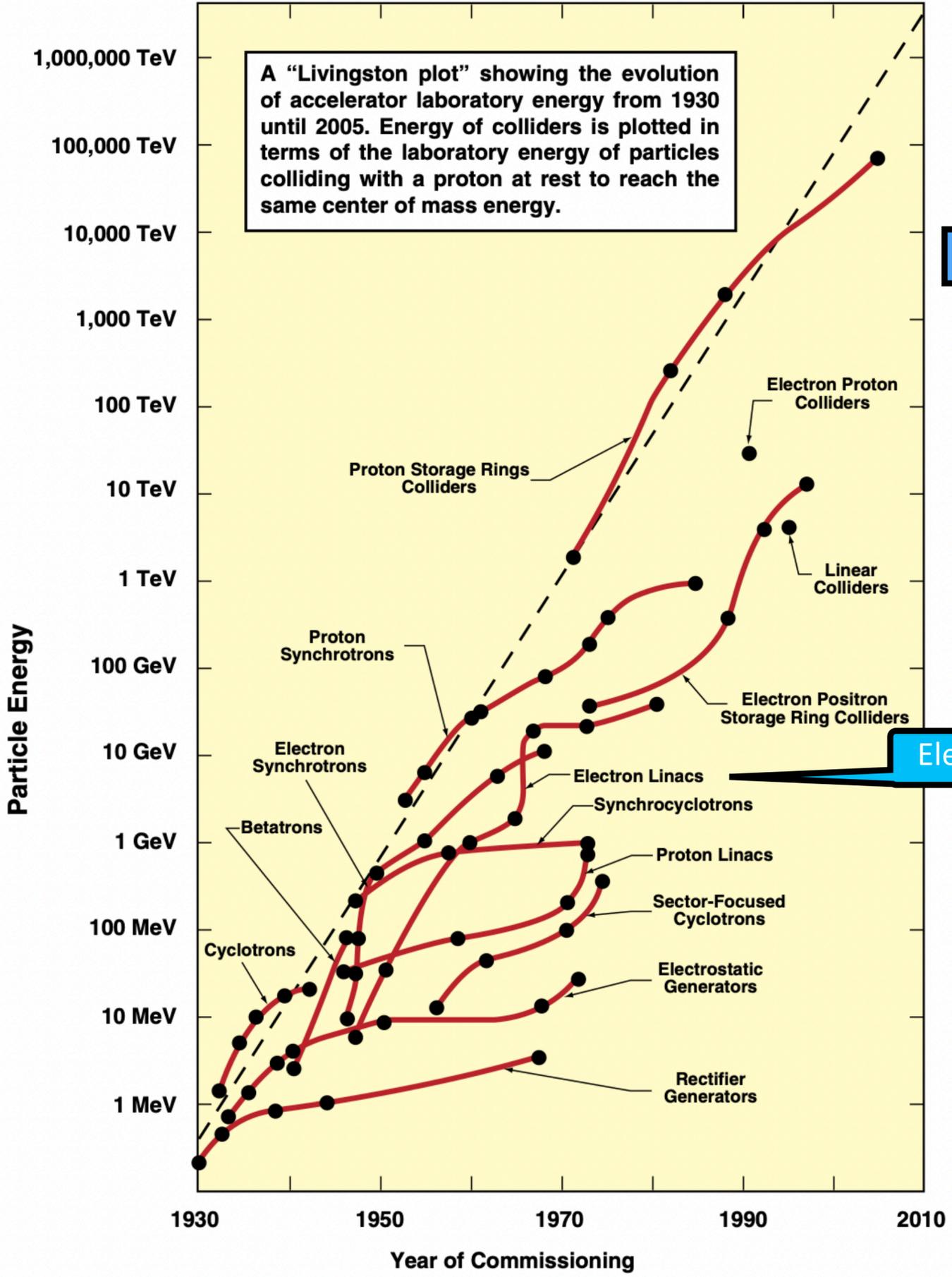
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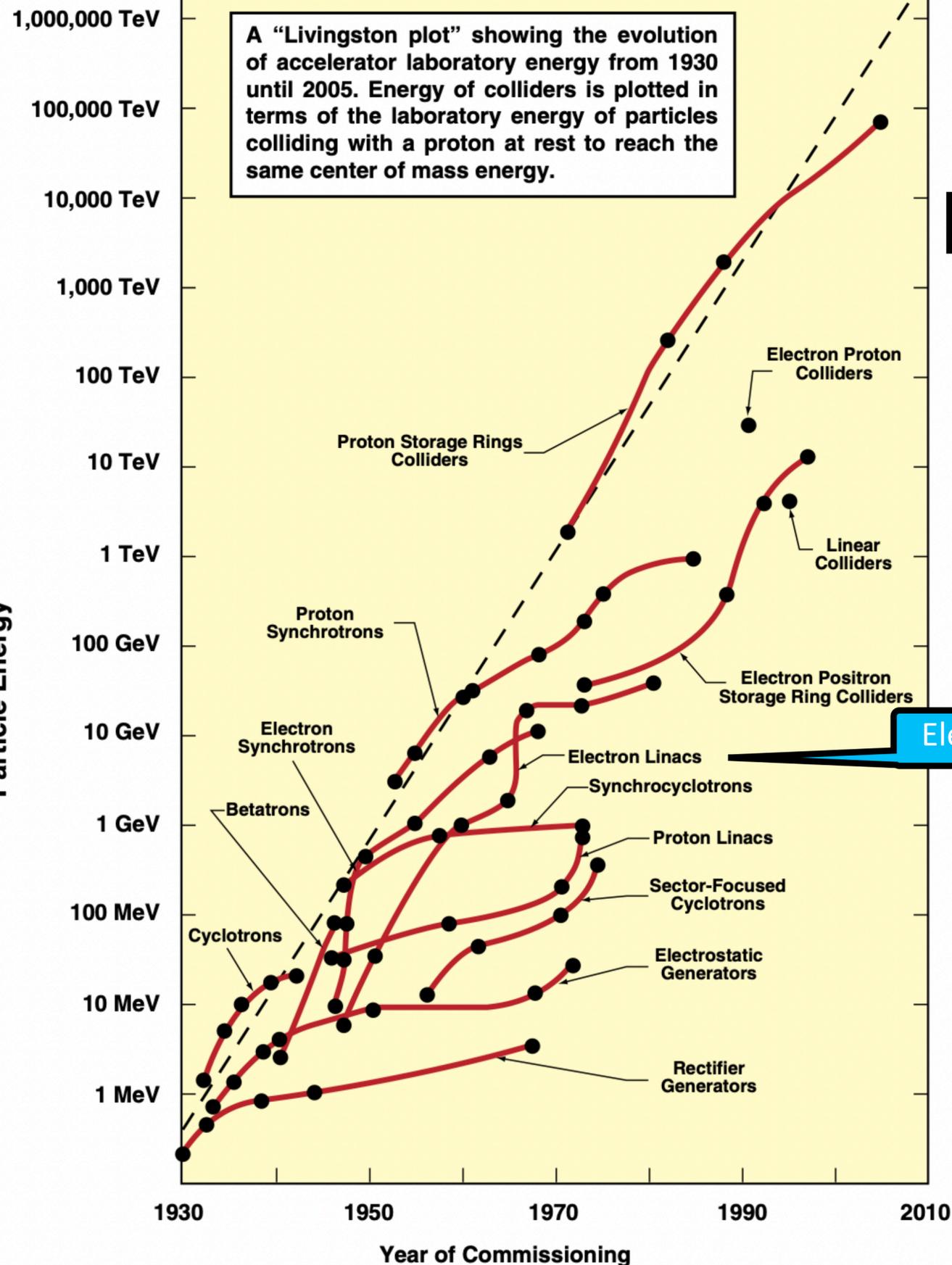
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Electron linear accelerators were used for the experiments discussed in the next slides

Snowmass 2001 <https://inspirehep.net/literature/572688>

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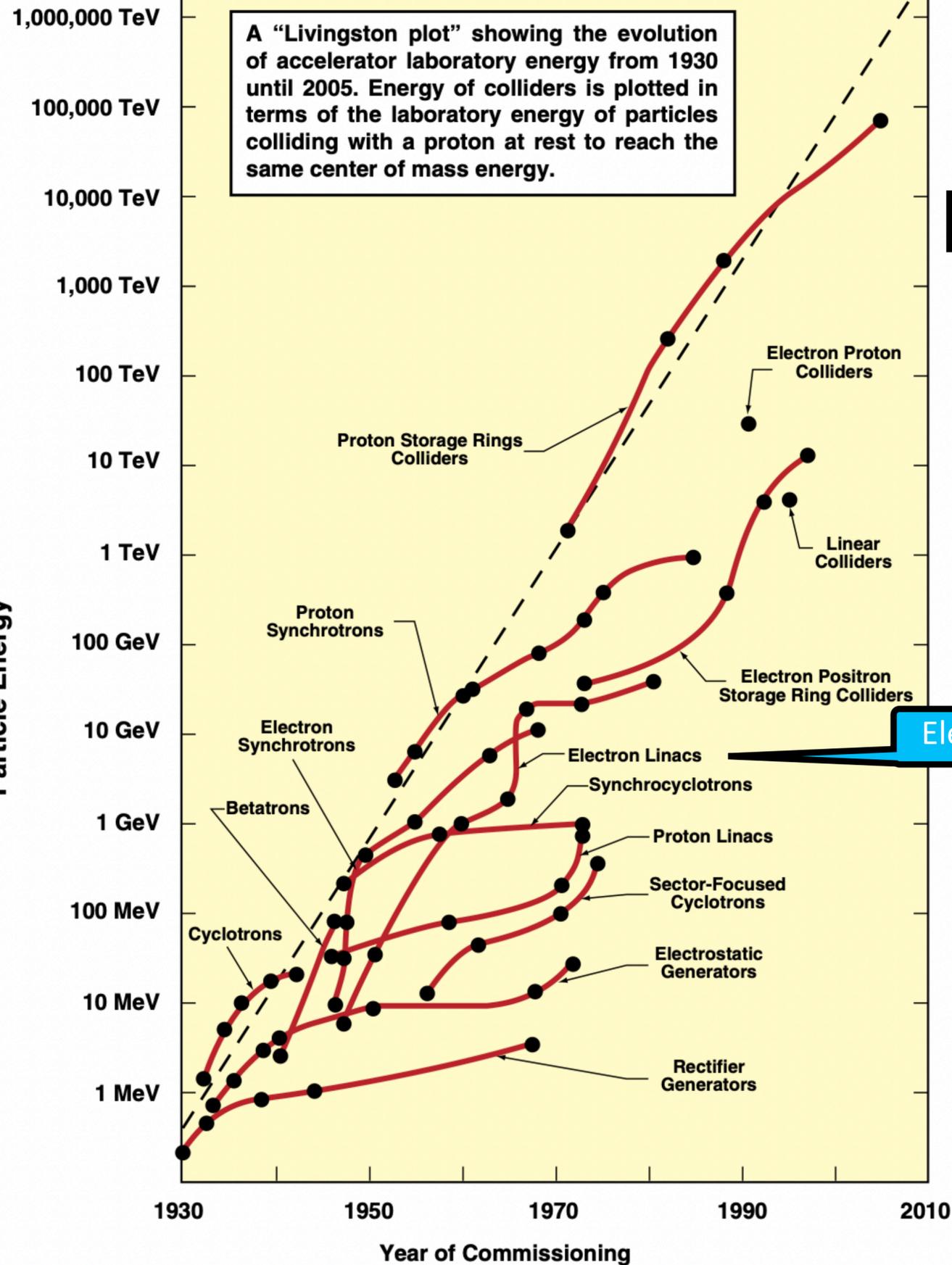


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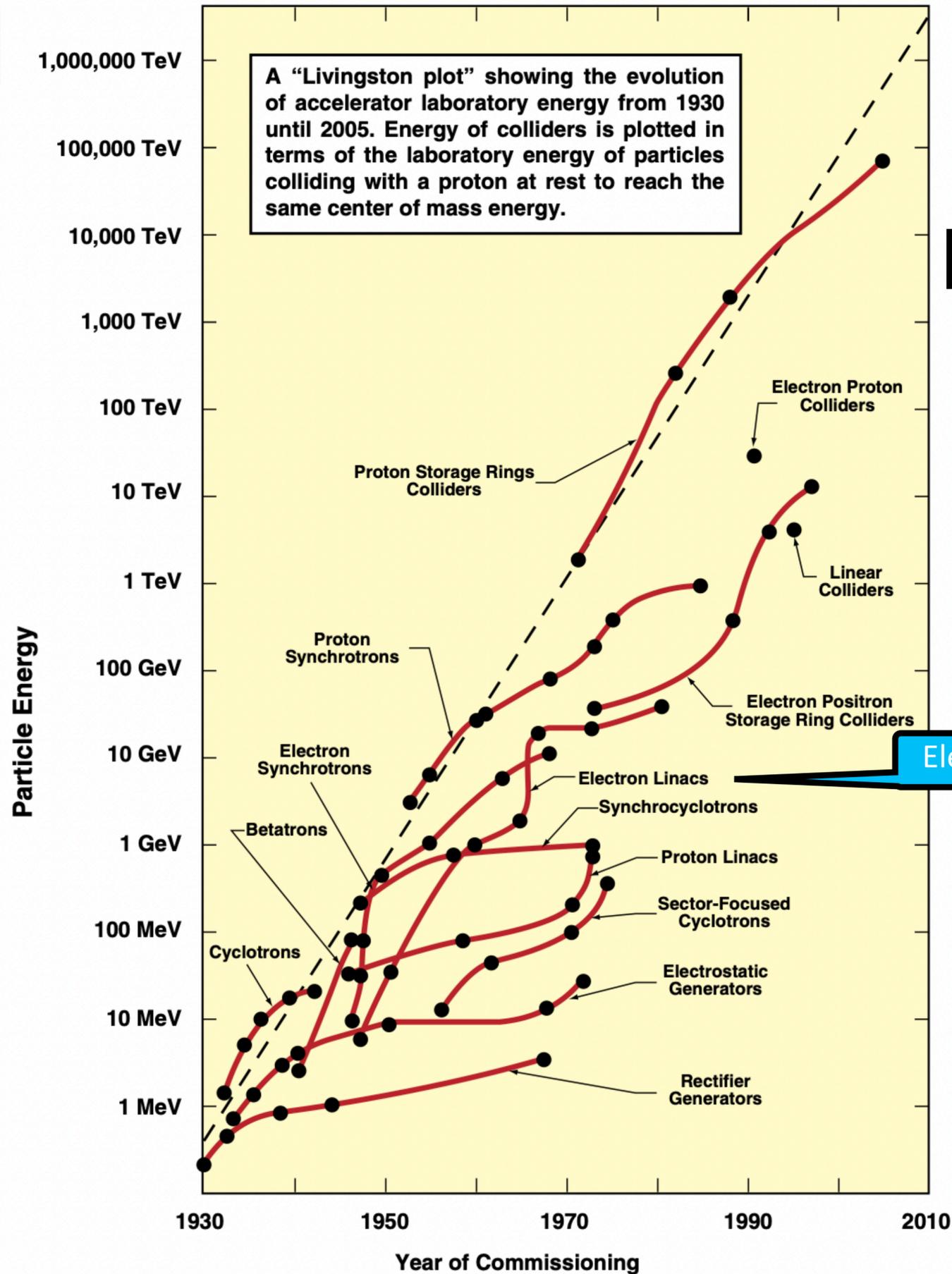
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Electron beams of up to 20 GeV

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Alpha particles from Ra reach less than 6 MeV

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# Protons have structure

**1955: Elastic scattering (Hofstadter and McAllister)**

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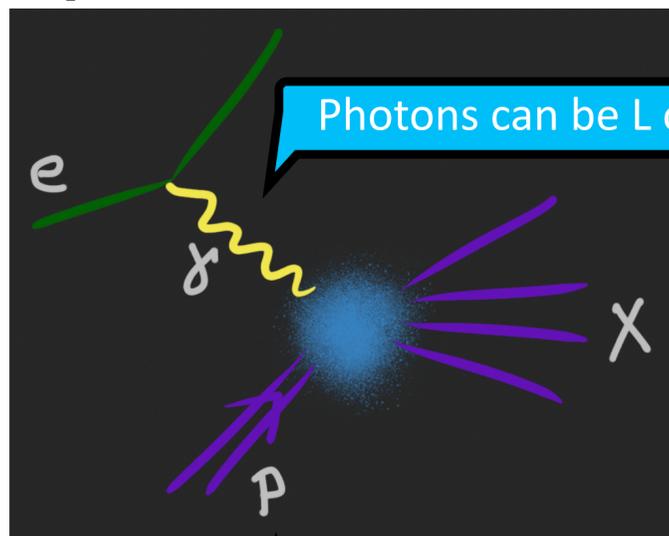
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Photons can be L or T

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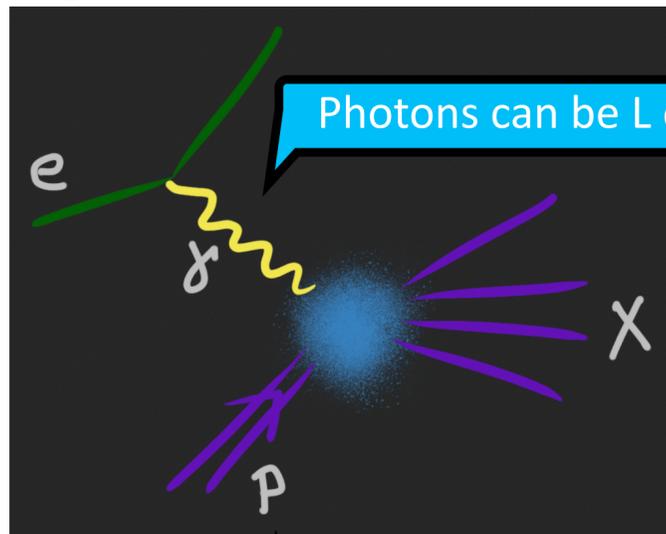
LOW  $q^2$  ELECTRODYNAMICS, ELASTIC AND INELASTIC ELECTRON (AND MUON)  
SCATTERING

No link for this one: I got it scanned thanks to the CERN Library :)

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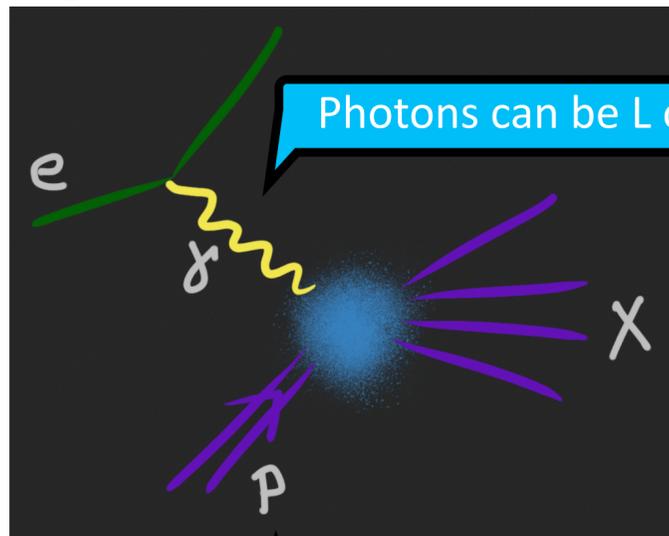
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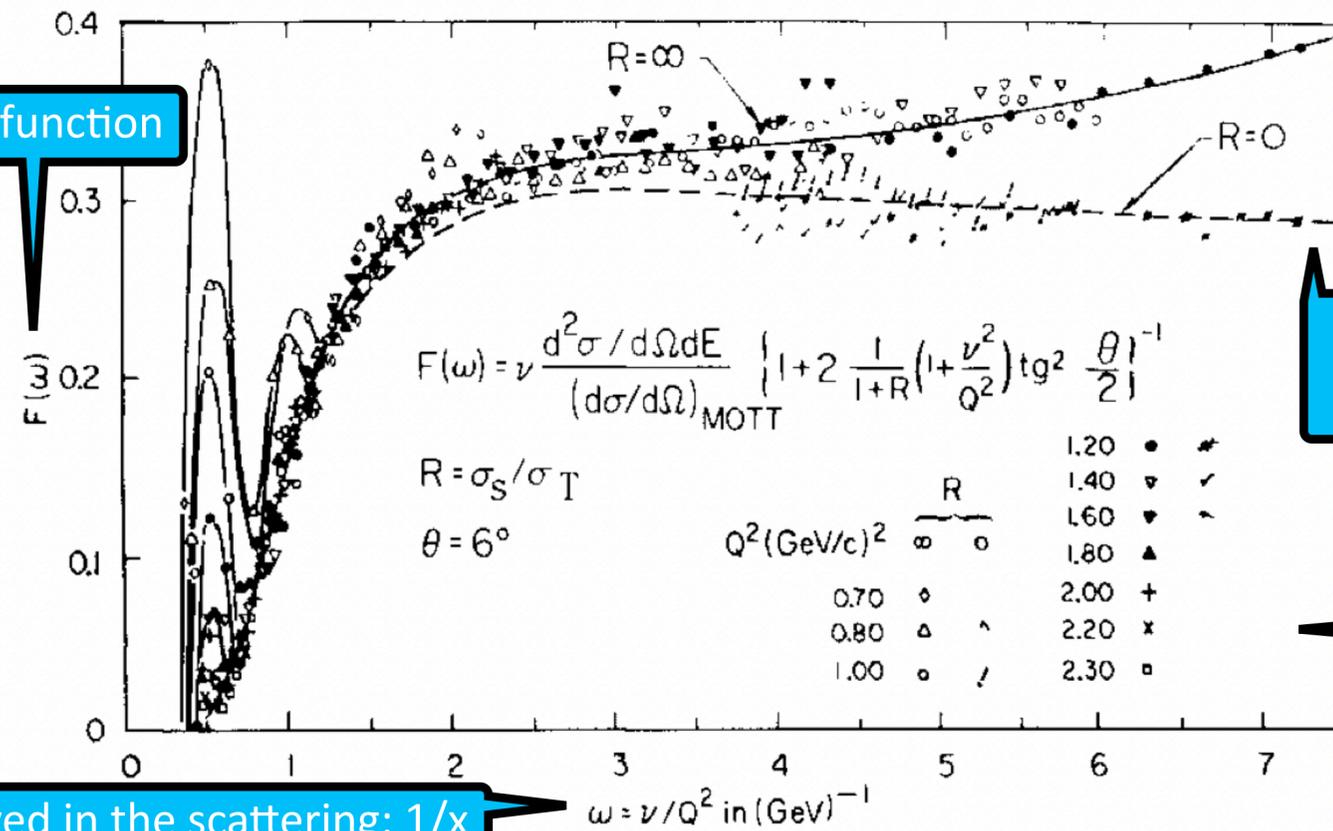
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2 options on the behaviour of R: the ratio of L to T contributions

Different  $Q^2$  values (virtuality/resolution of the photon)

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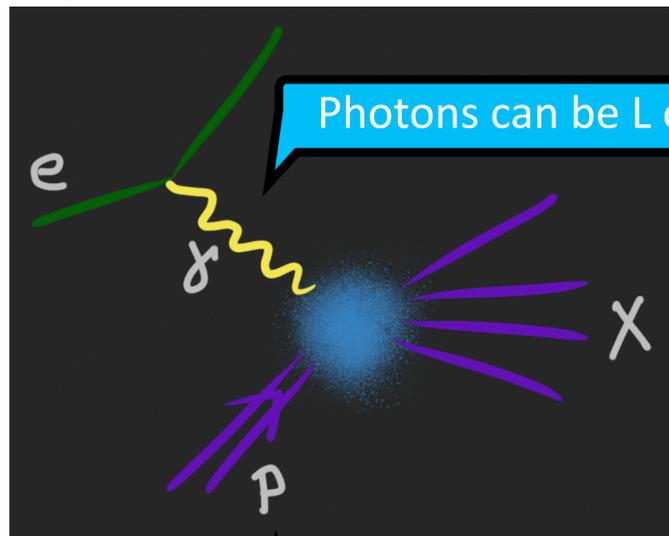
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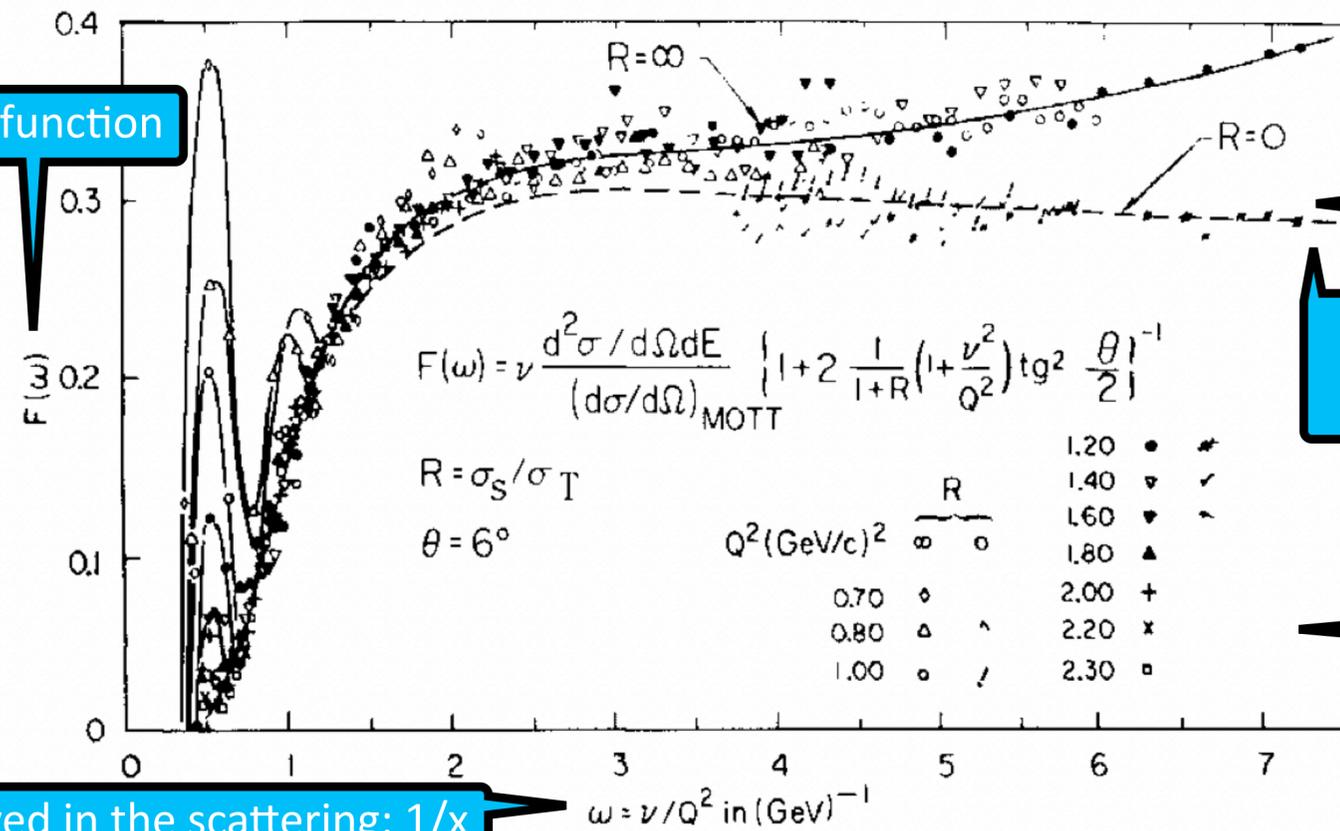
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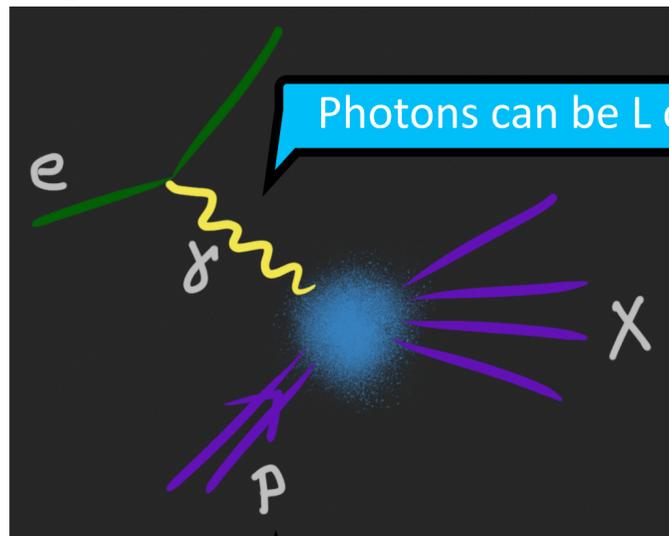
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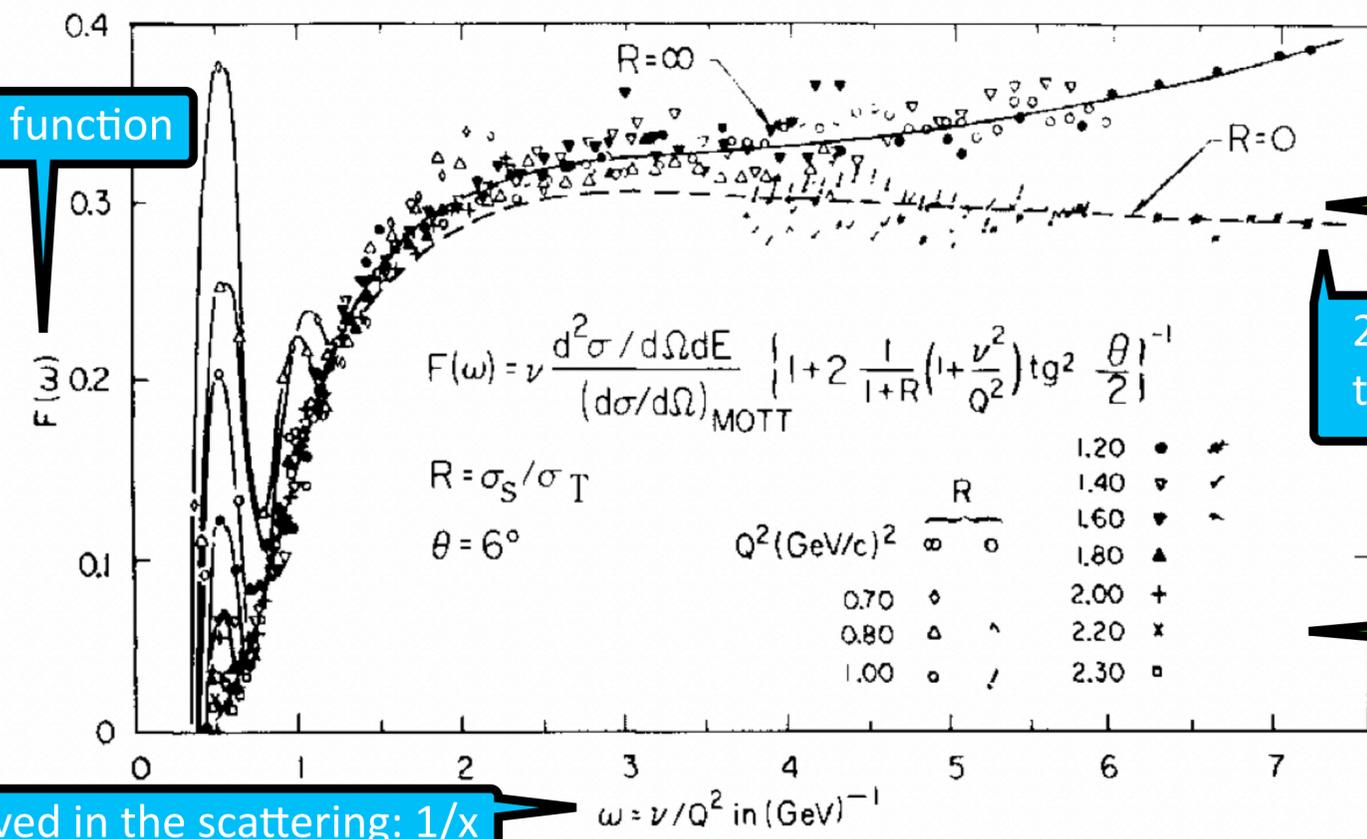
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point-like  
constituents

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<https://doi.org/10.1103/PhysRev.179.1547>

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point-like constituents

Picture only valid in the (proton) infinite-momentum frame

Partons are free during the interaction

Asymptotic freedom

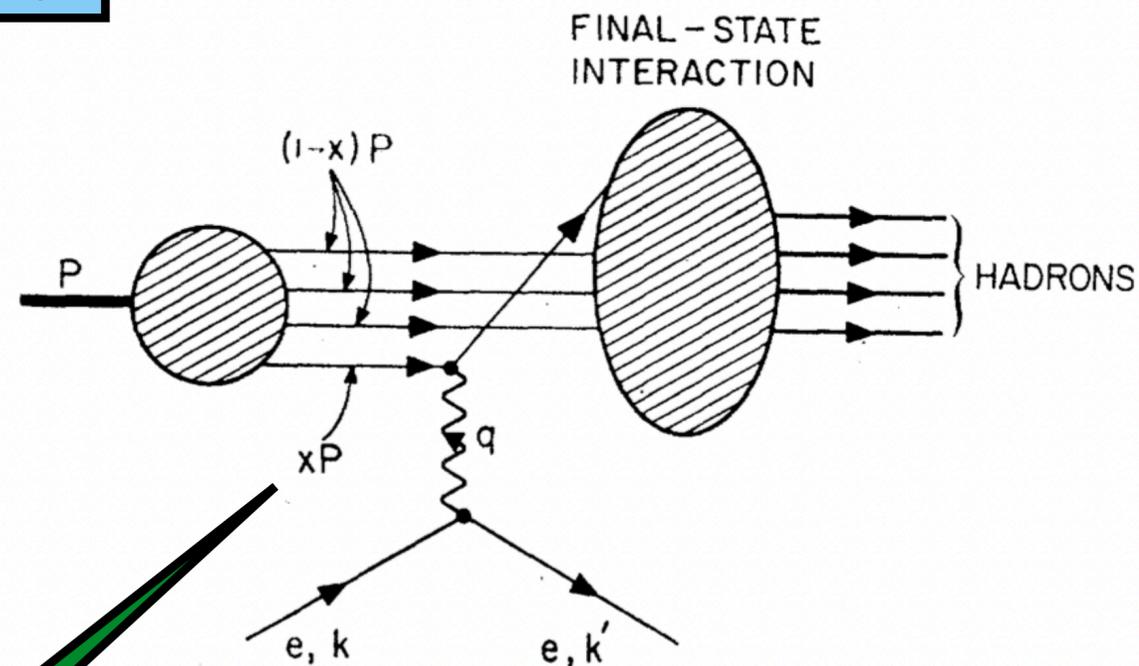


FIG. 1. Kinematics of lepton-nucleon scattering in the parton model.

Bjorken- $x$ : fraction of the proton momentum carried by the struck parton

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**1969: Callen-Gross relation**

<https://doi.org/10.1103/PhysRevLett.22.156>

**1972: Partons have spin 1/2 (Miller et al)**

<https://doi.org/10.1103/PhysRevD.5.528>

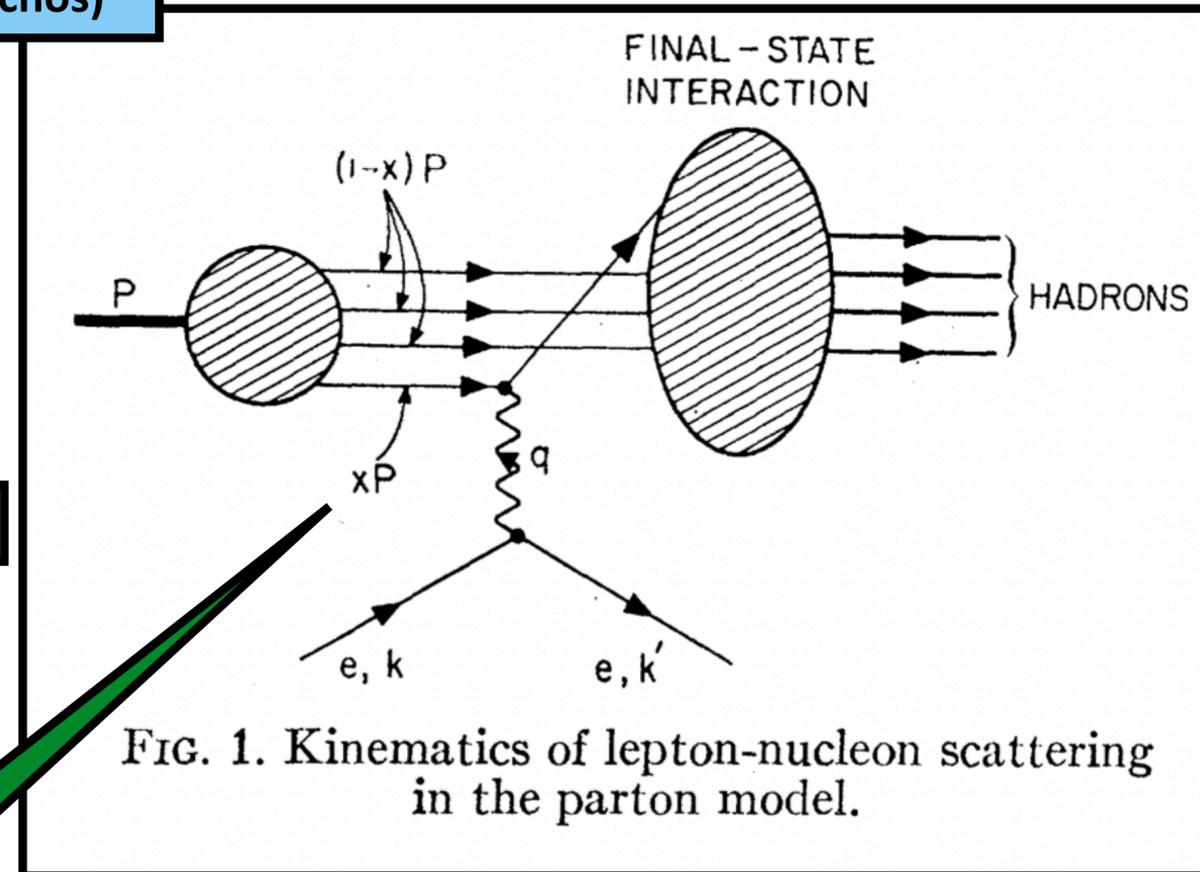
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How could there be 'free' constituents in the proton?

Needed to explain scaling

# QCD

**1973: Price of asymptotic freedom (Coleman, Gross)**

<https://doi.org/10.1103/PhysRevLett.31.851>

No renormalizable field theory without non-Abelian gauge field can be asymptotically free

**1973: Asymptotic freedom (Politzer, Gross and Wilczek)**

<https://doi.org/10.1103/PhysRevLett.30.1346>

<https://doi.org/10.1103/PhysRevLett.30.1343>

Non-Abelian gauge field theories can be asymptotically free

**1973: SU(3) color (Fritzsch, Gell-mann, Leutwyler)**

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QCD

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QCD

Charm to accept QCD

1964: Charm (Bjorken and Glashow)

[https://doi.org/10.1016/0031-9163\(64\)90433-0](https://doi.org/10.1016/0031-9163(64)90433-0)

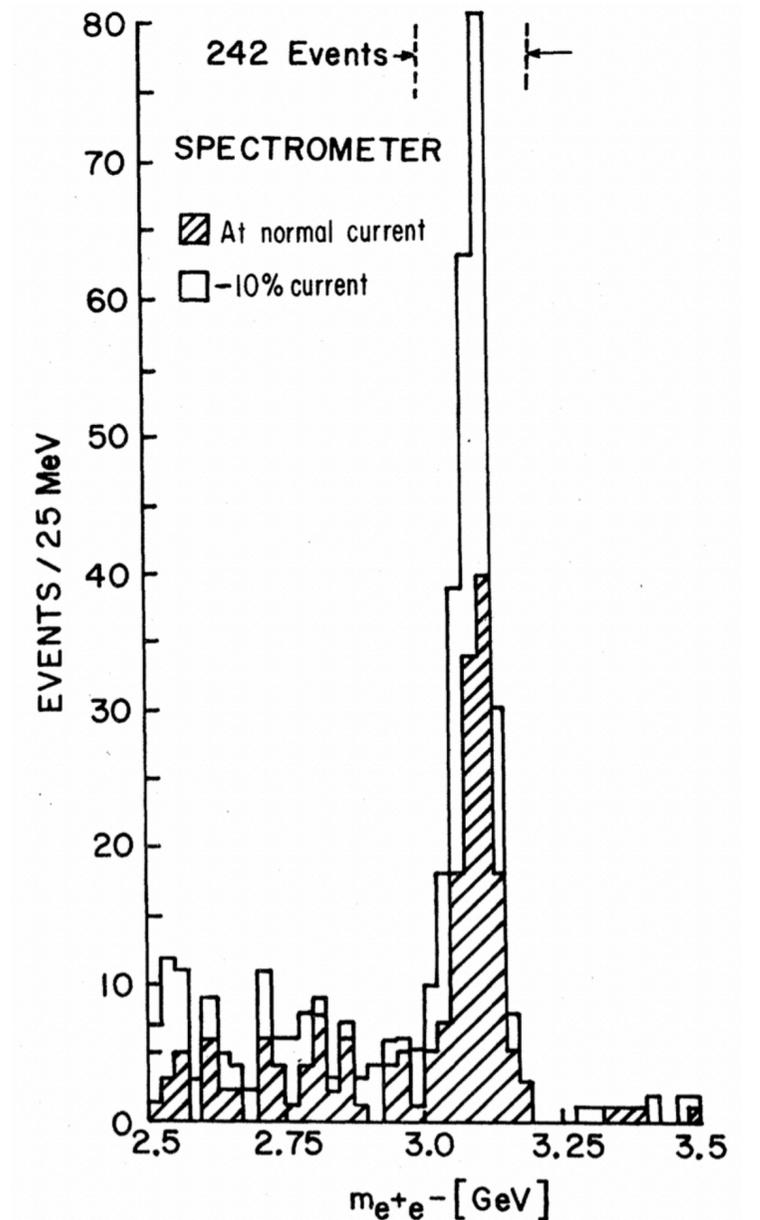
1974: J/ $\psi$  and the November revolution (Richter et al, Ting et al)

<https://doi.org/10.1103/PhysRevLett.33.1406>

1974: charmonium (Appelquist, Politzer)

<https://doi.org/10.1103/PhysRevLett.34.43>

<https://doi.org/10.1103/PhysRevLett.33.1404>



**Nobel prize 1961**

<https://www.nobelprize.org/prizes/physics/1961/>  
<https://www.nobelprize.org/uploads/2018/06/hofstadter-lecture.pdf>

**Nobel prize 1990**

<https://www.nobelprize.org/prizes/physics/1990/>  
<https://www.nobelprize.org/uploads/2018/06/taylor-lecture.pdf>  
<https://www.nobelprize.org/uploads/2018/06/kendall-lecture-1.pdf>  
<https://www.nobelprize.org/uploads/2018/06/friedman-lecture.pdf>

To be read in this order

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**Homework:**

try to read at least the 1990 lectures

At this point in time, we have a theory to explain scaling  
But QCD is a lot more than scaling ...

2

## Establishing QCD: Proton structure functions from HERA

Reminder: how do data tell us about QCD?

# Deep-inelastic scattering: QED and Lorentz invariance

This is the cross section to be measured

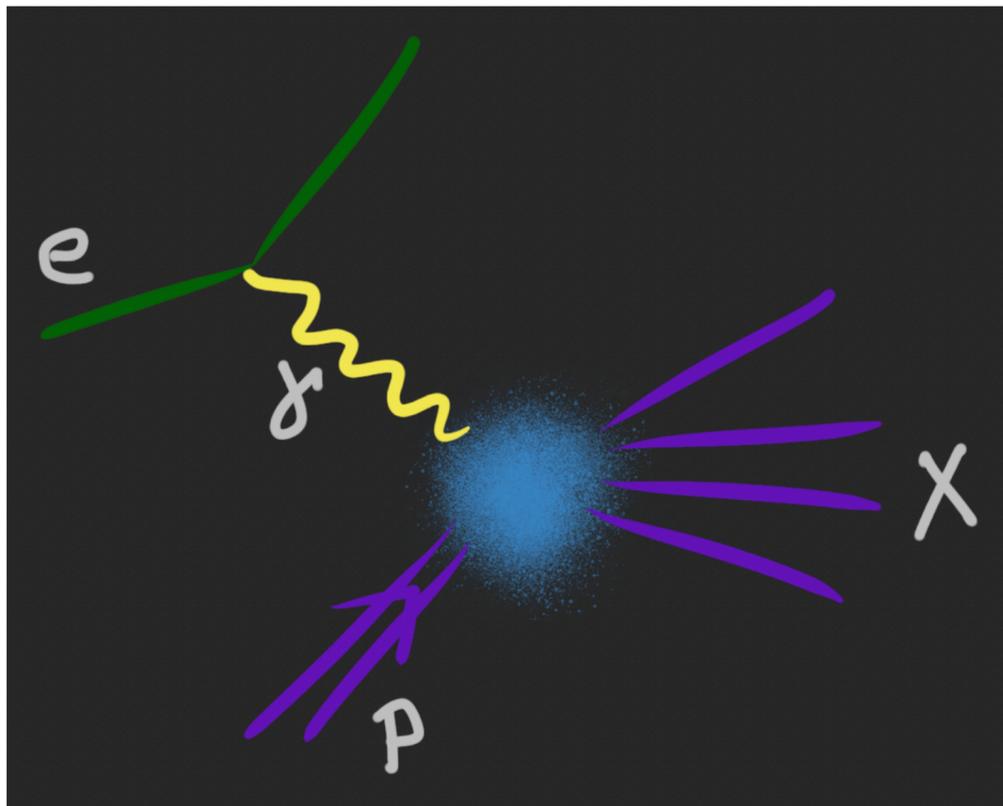
$$\frac{d\sigma^{ep}}{dx dQ^2}$$

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One photon exchange



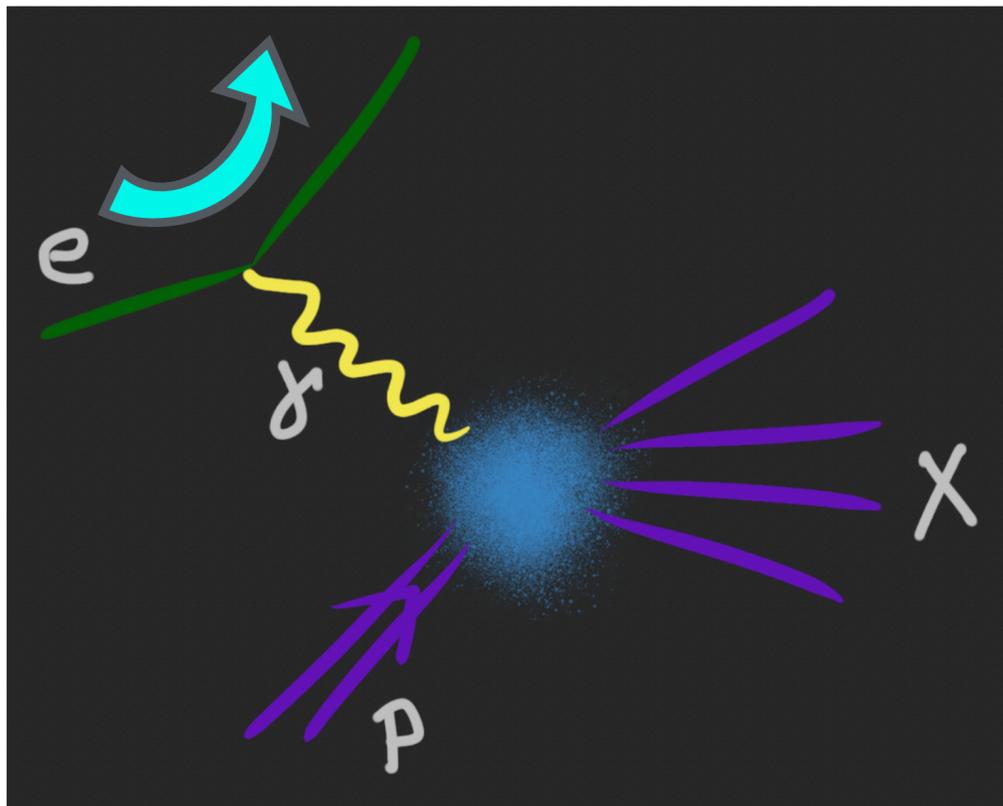
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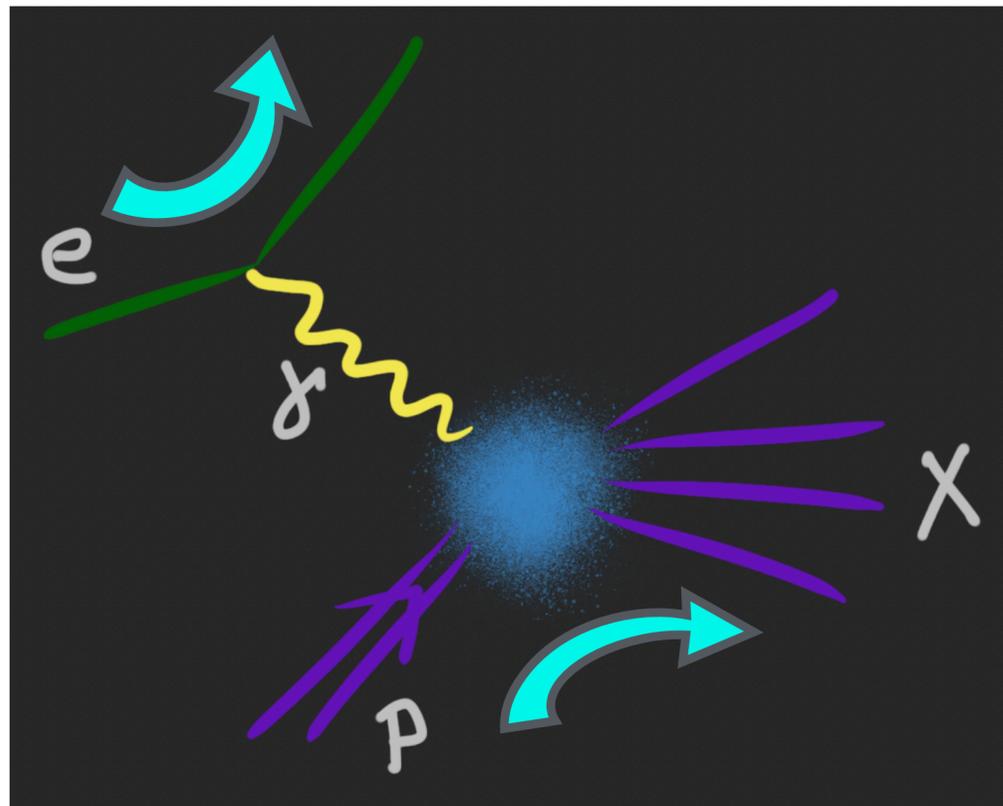
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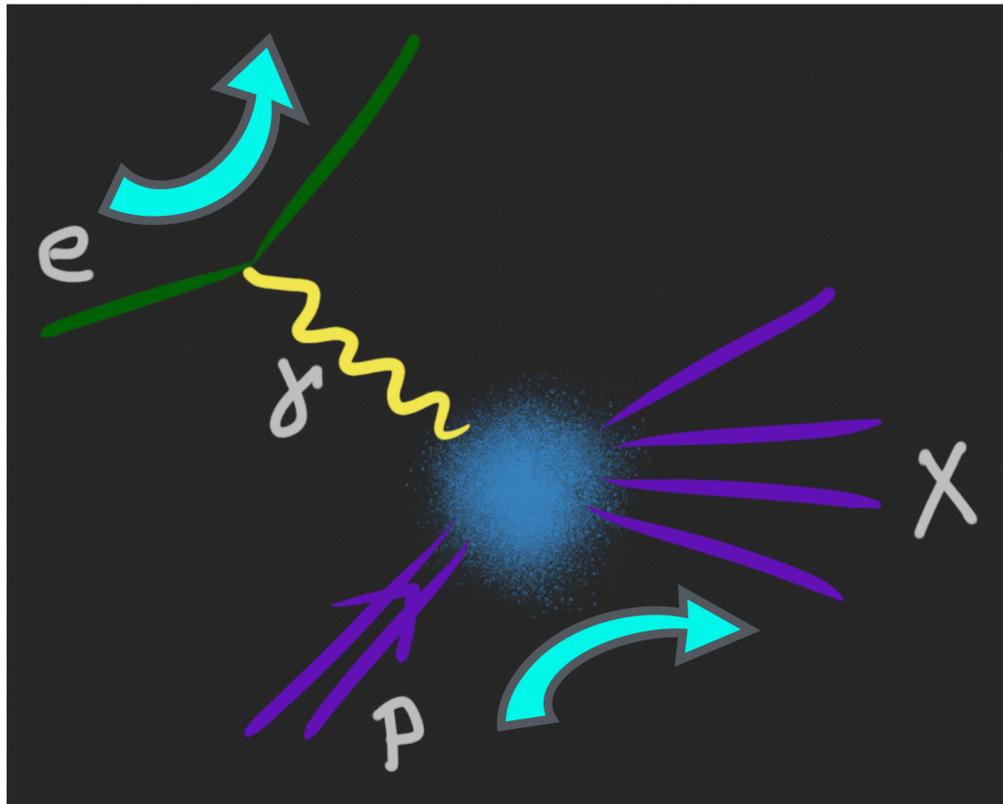
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Noting that:

- ✓ The lepton tensor is symmetric
- ✓ Photon exchange conserves parity
- ✓ The current is conserved
- ✓ Summing and averaging over spins

The most general tensor can be expressed as

$$W^{\mu\nu} = W_1 \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) + W_2 \frac{1}{M^2} \left( p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) \left( p^\nu - \frac{p \cdot q}{q^2} q^\nu \right)$$



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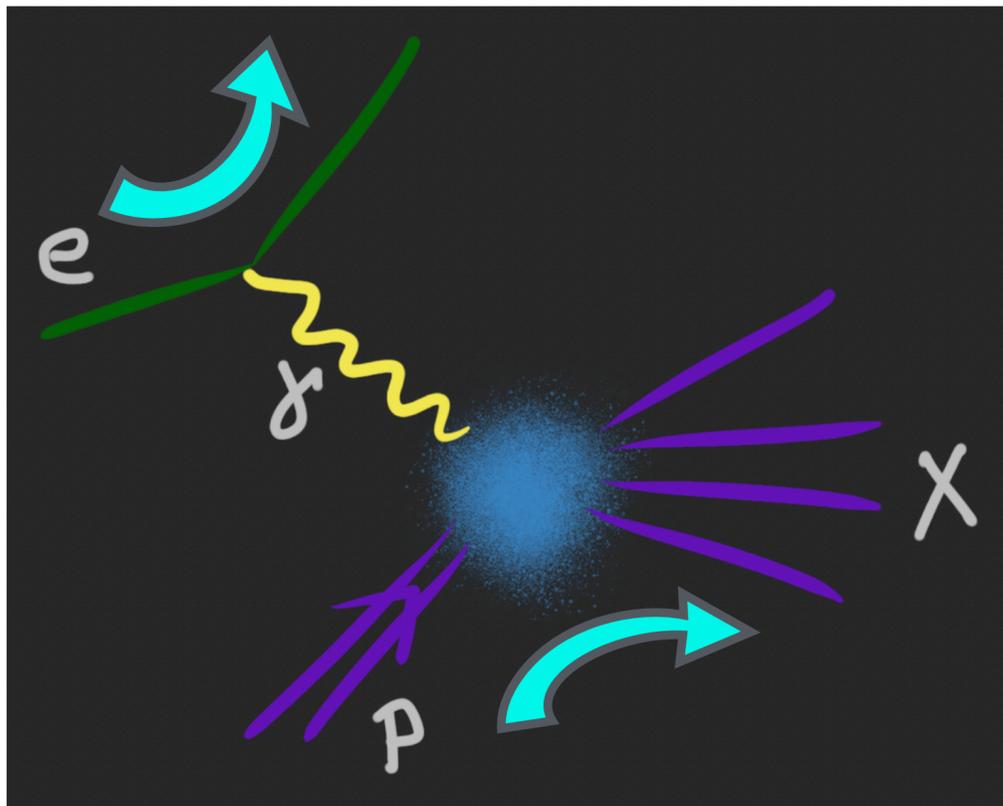
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For large photon virtualities and in a frame where the proton is moving infinitely fast

$$MW_1 \rightarrow F_1 \quad \text{and} \quad \nu W_2 \rightarrow F_2$$

Structure functions



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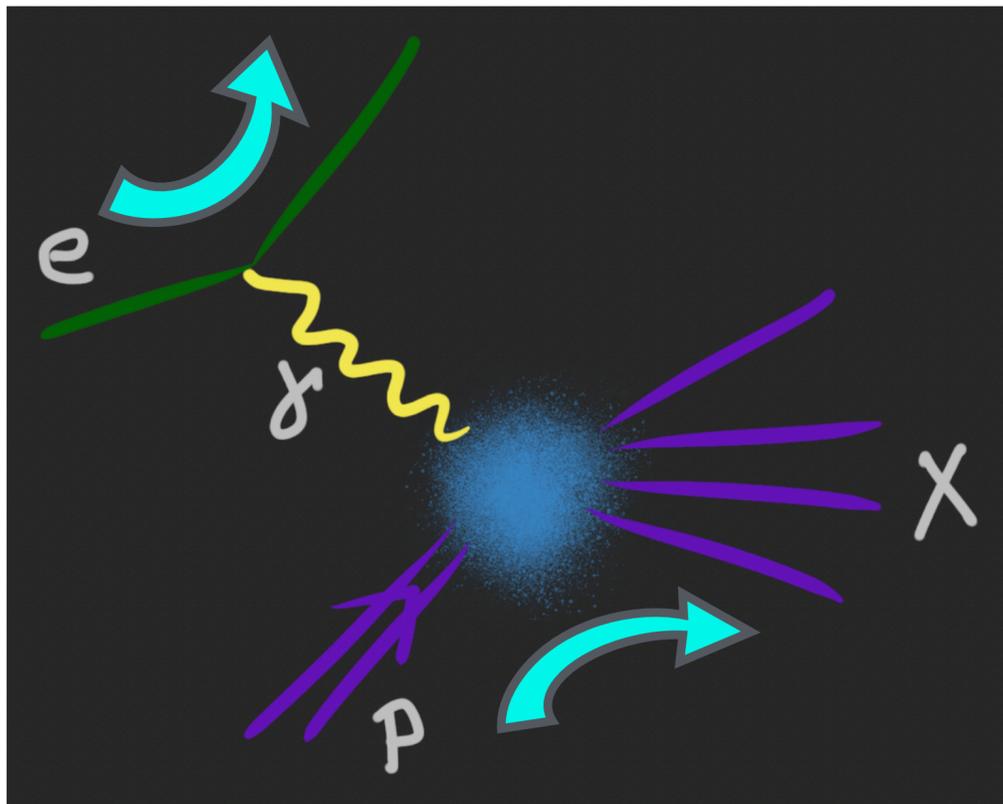
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If the constituents have spin one half

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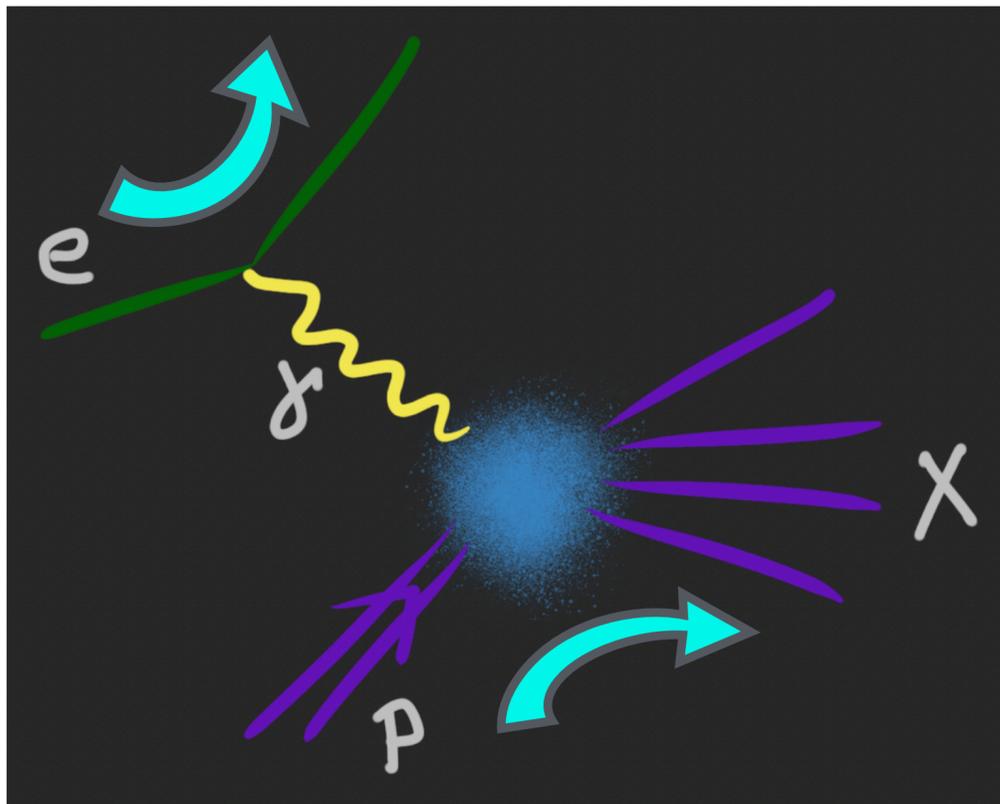
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Note that up to this point there is no QCD involved



# Deep inelastic scattering: quarks in the Bjorken limit

For large photon virtualities, thinking about point like constituents (partons), and in a frame where the proton is moving infinitely fast

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QCD enters when we identify the partons with quarks

At this point in time we have a theory and an understanding how to learn about QCD from measurements  
... now, we need a new accelerator to perform the measurements and look deeper into the proton ...

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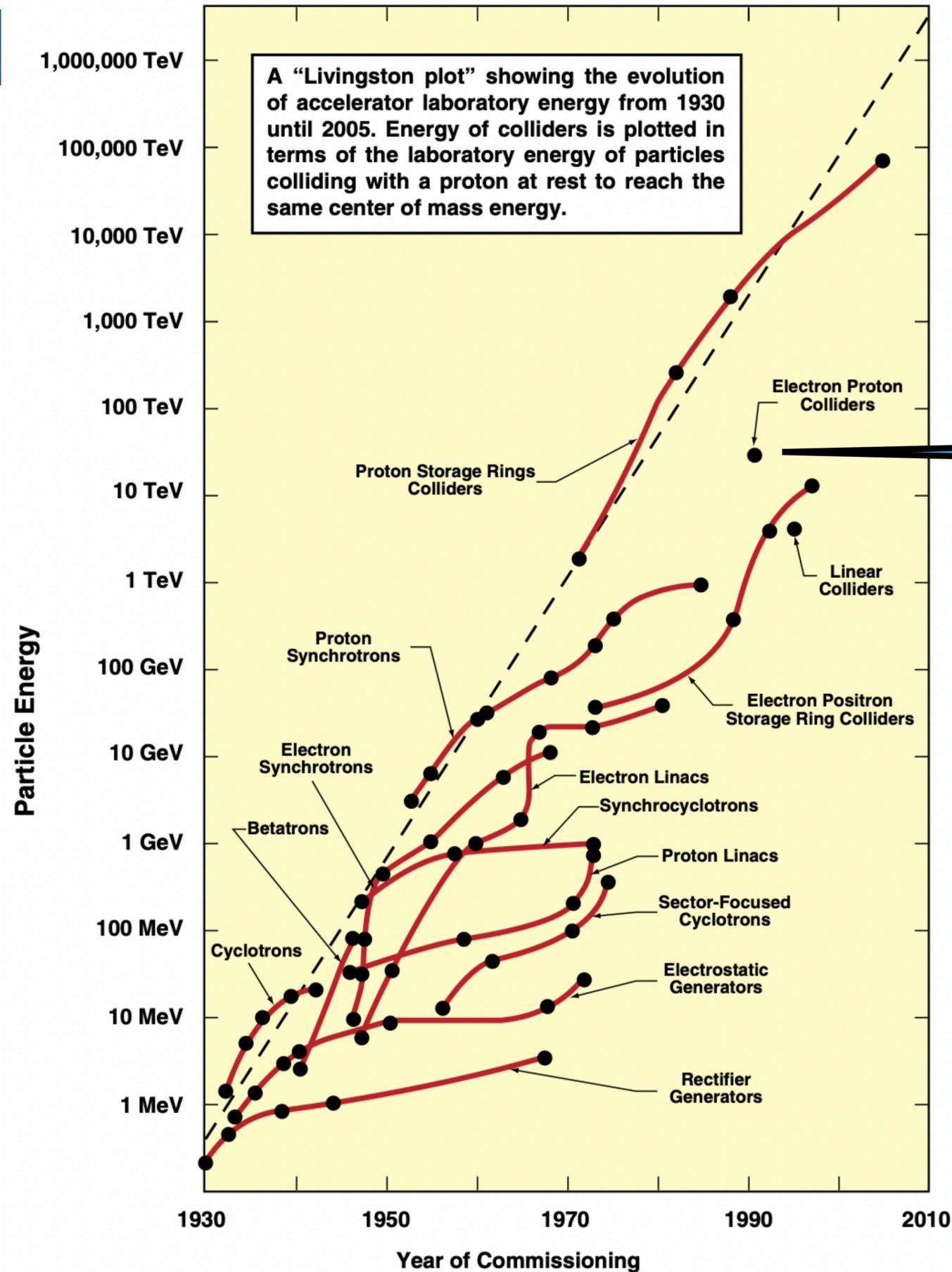
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HERA



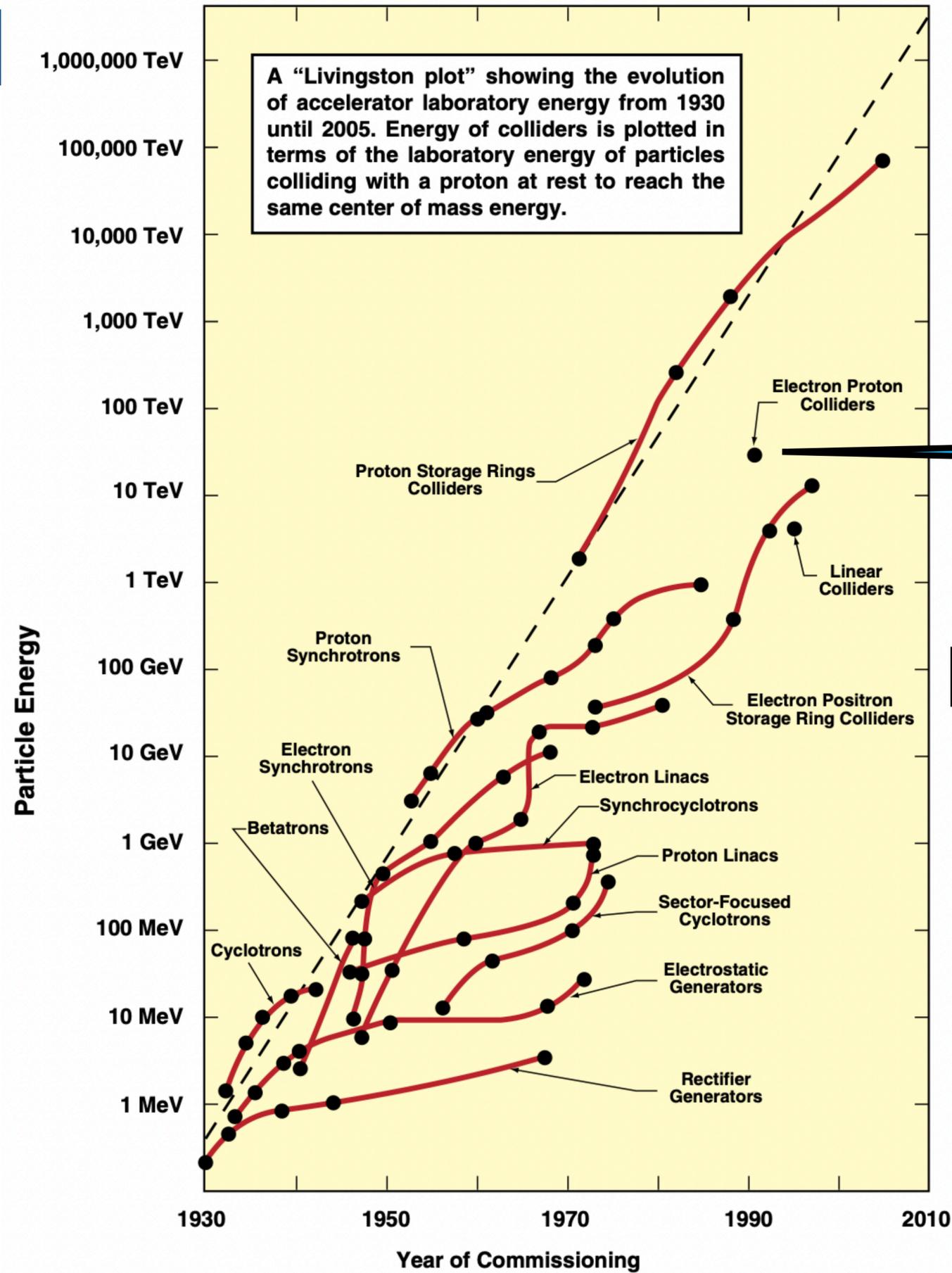
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HERA

Hopefully, we will add another ep collider in a few years when EIC enters operation



# HERA



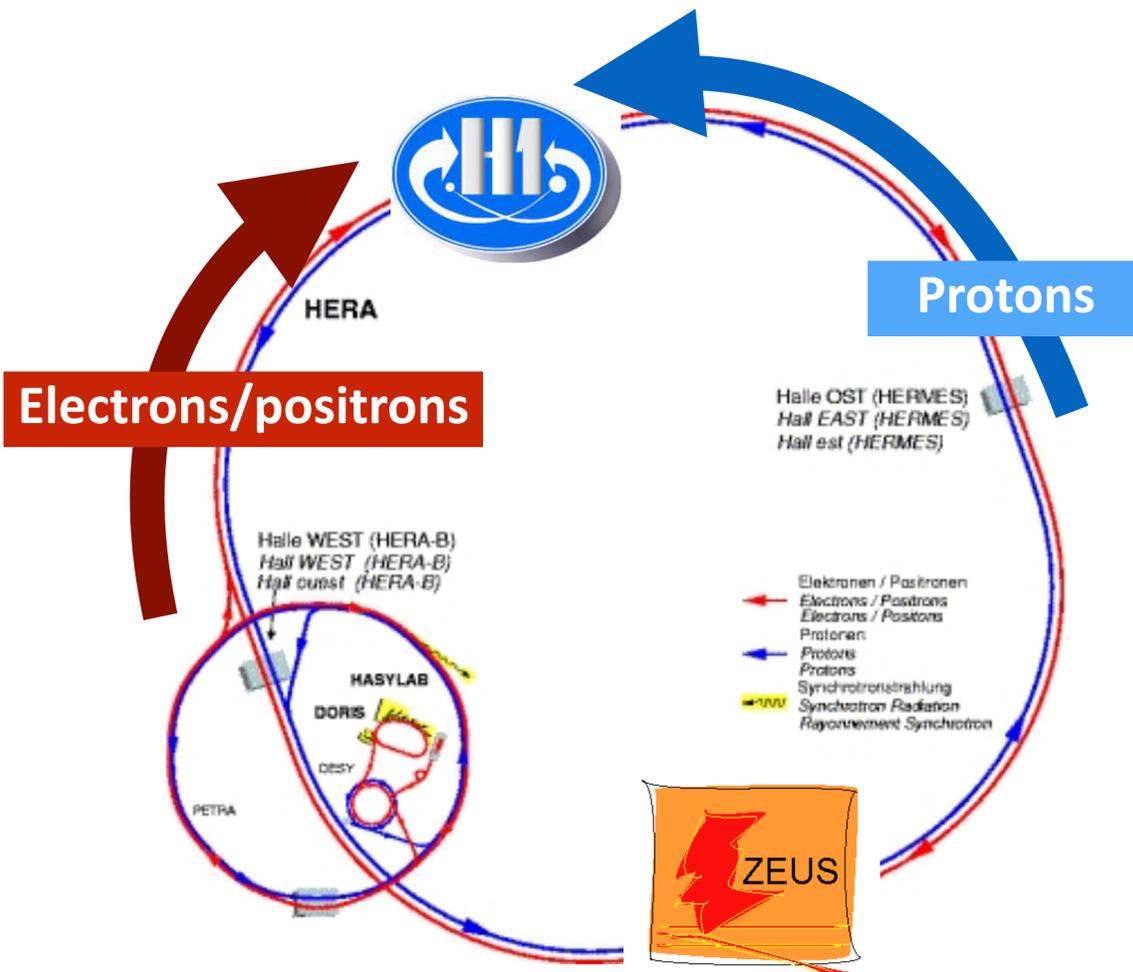
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6.3 km of circumference  
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Two beam-target experiments, HERMES, HERA-B  
Two collider experiments, H1 and ZEUS

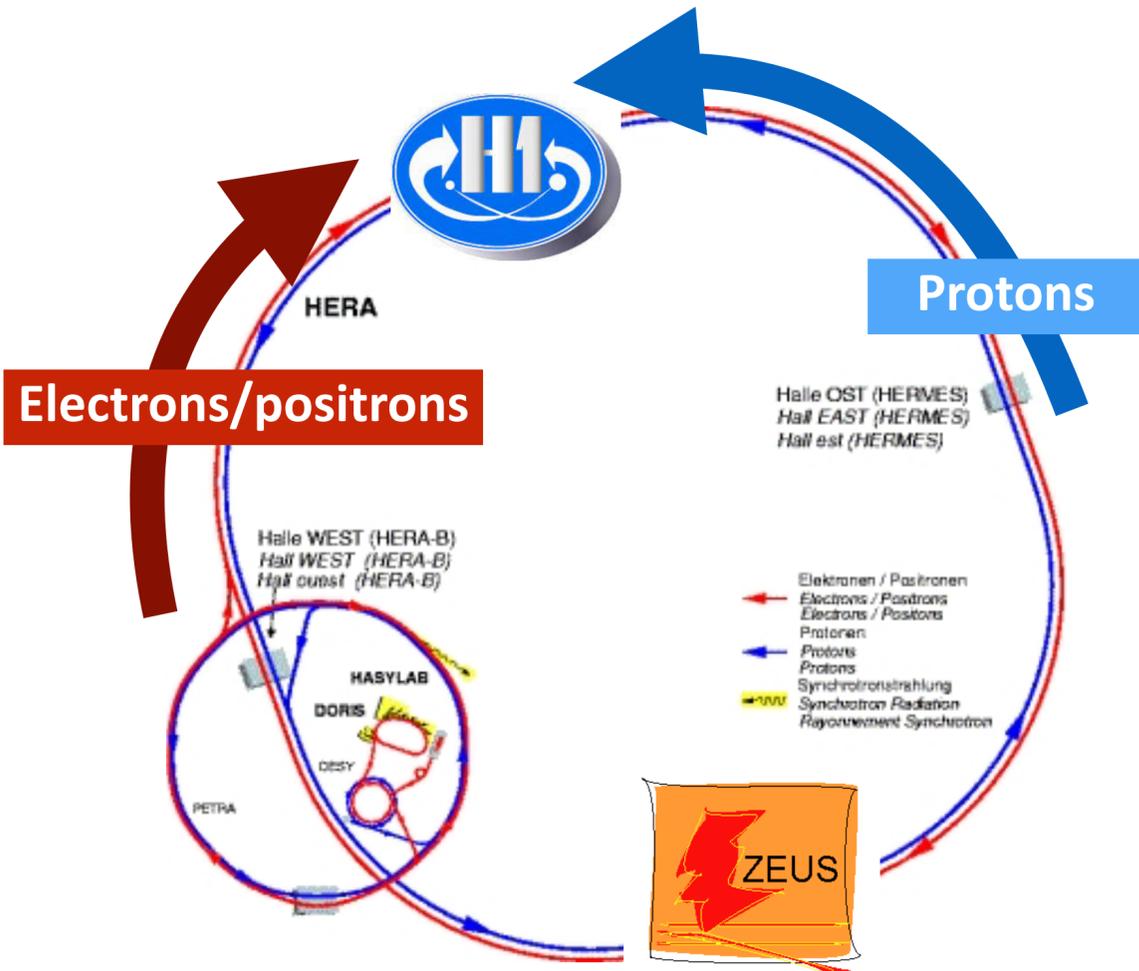


# HERA



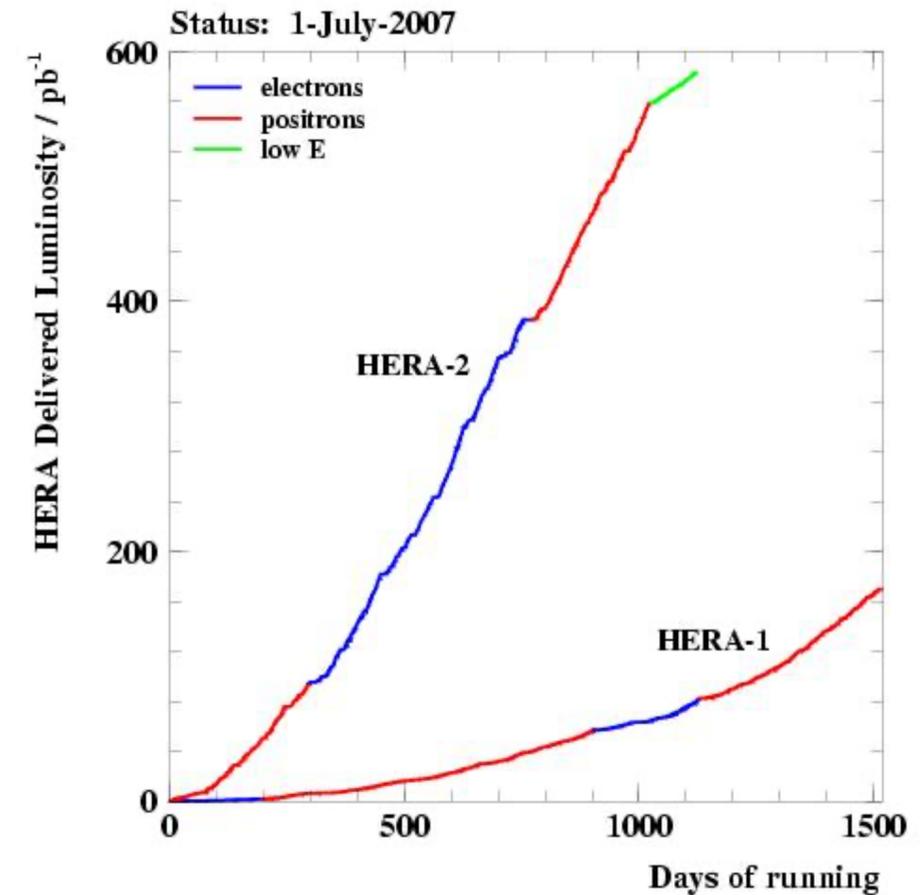
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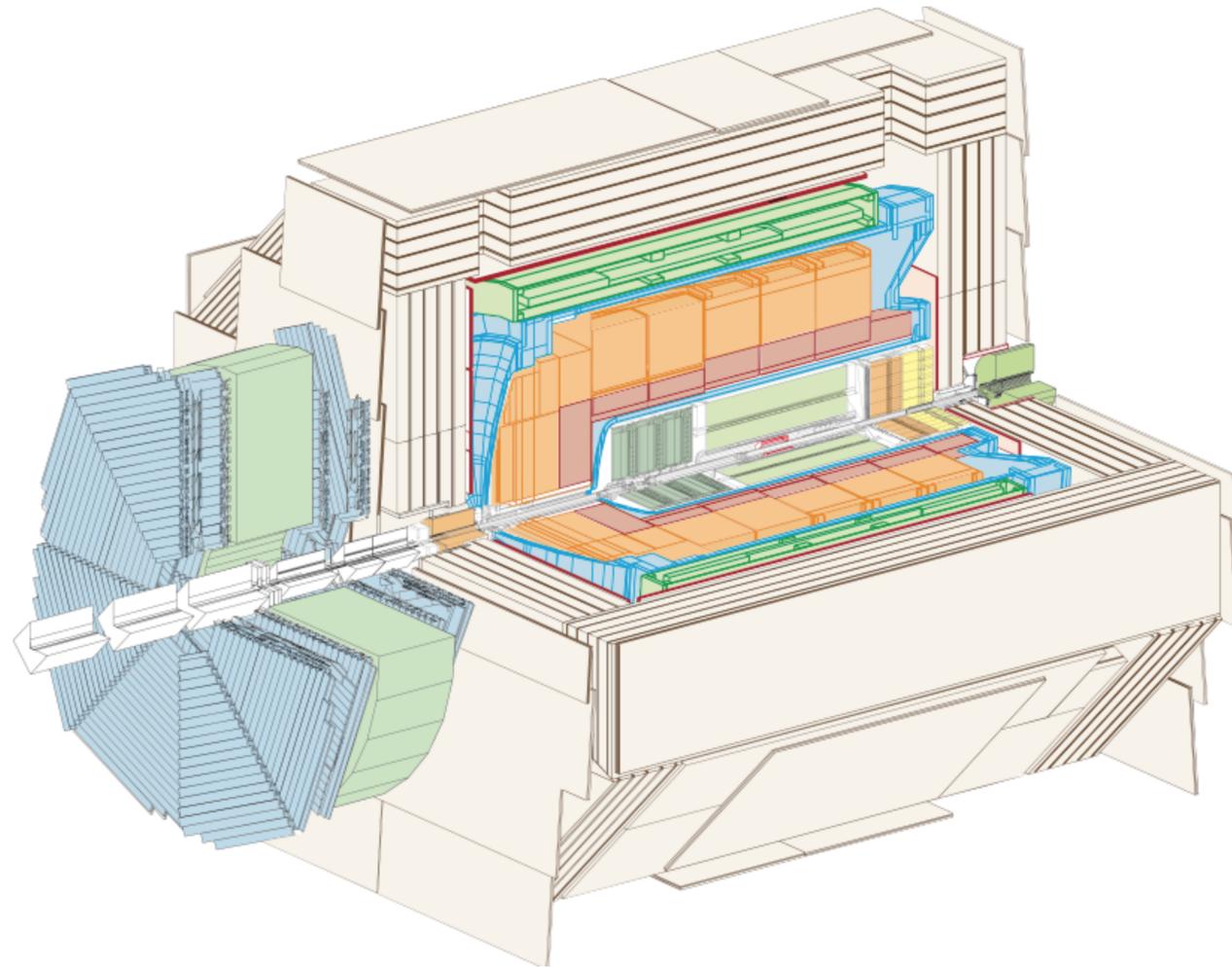
HERA-I, 1992–2000  
 $e^\pm$  beam 27.5 GeV, p beam 820 GeV (1992–1997)  
 p beam 920 GeV (1998–2000)

HERA-II, 2002–2007  
 $e^\pm$  longitudinally polarised, p beam 920 GeV  
 also p beam at 575 and 460 GeV



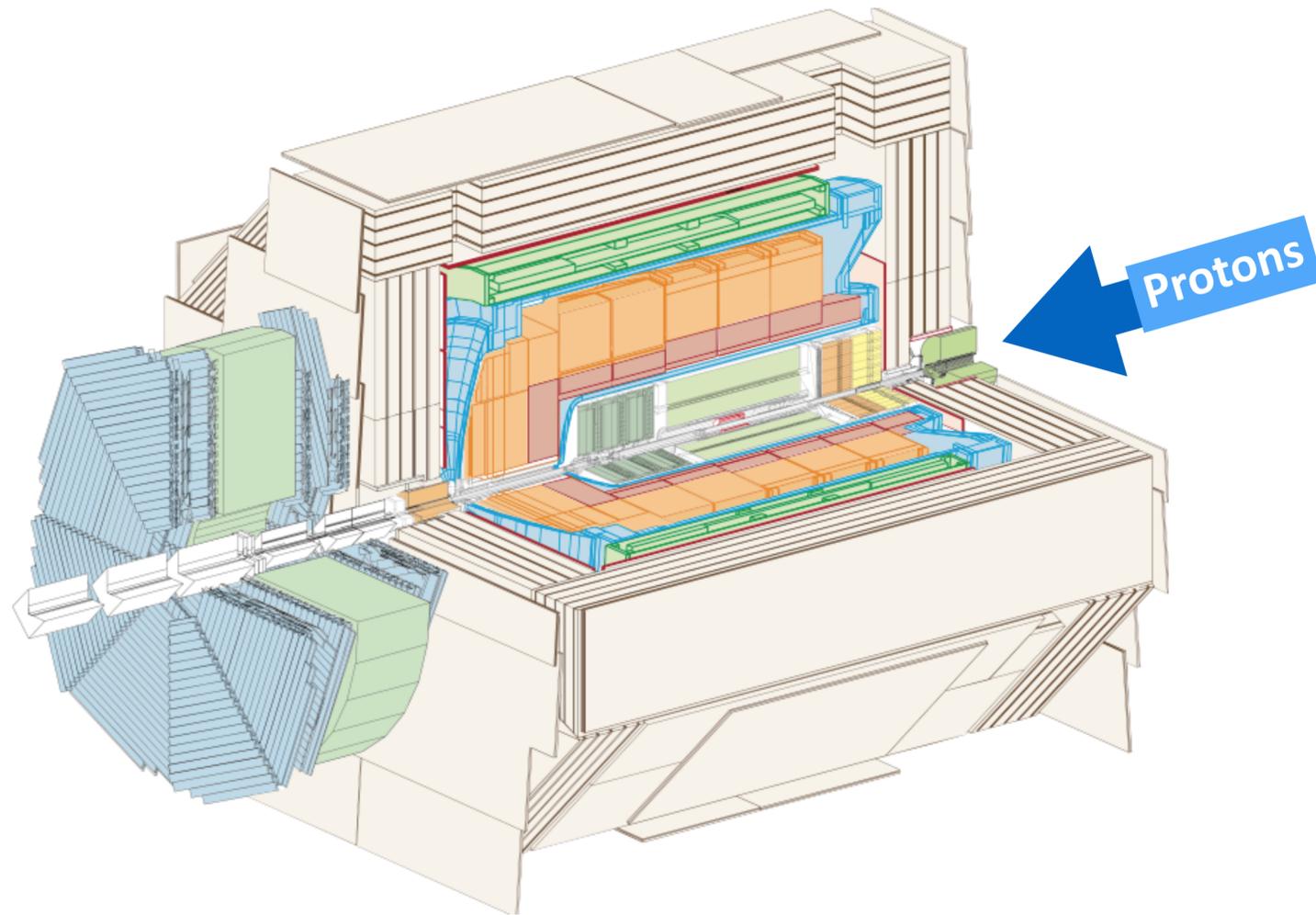
Guillermo Contreras, CTU in Prague

# H1 detector: central detectors



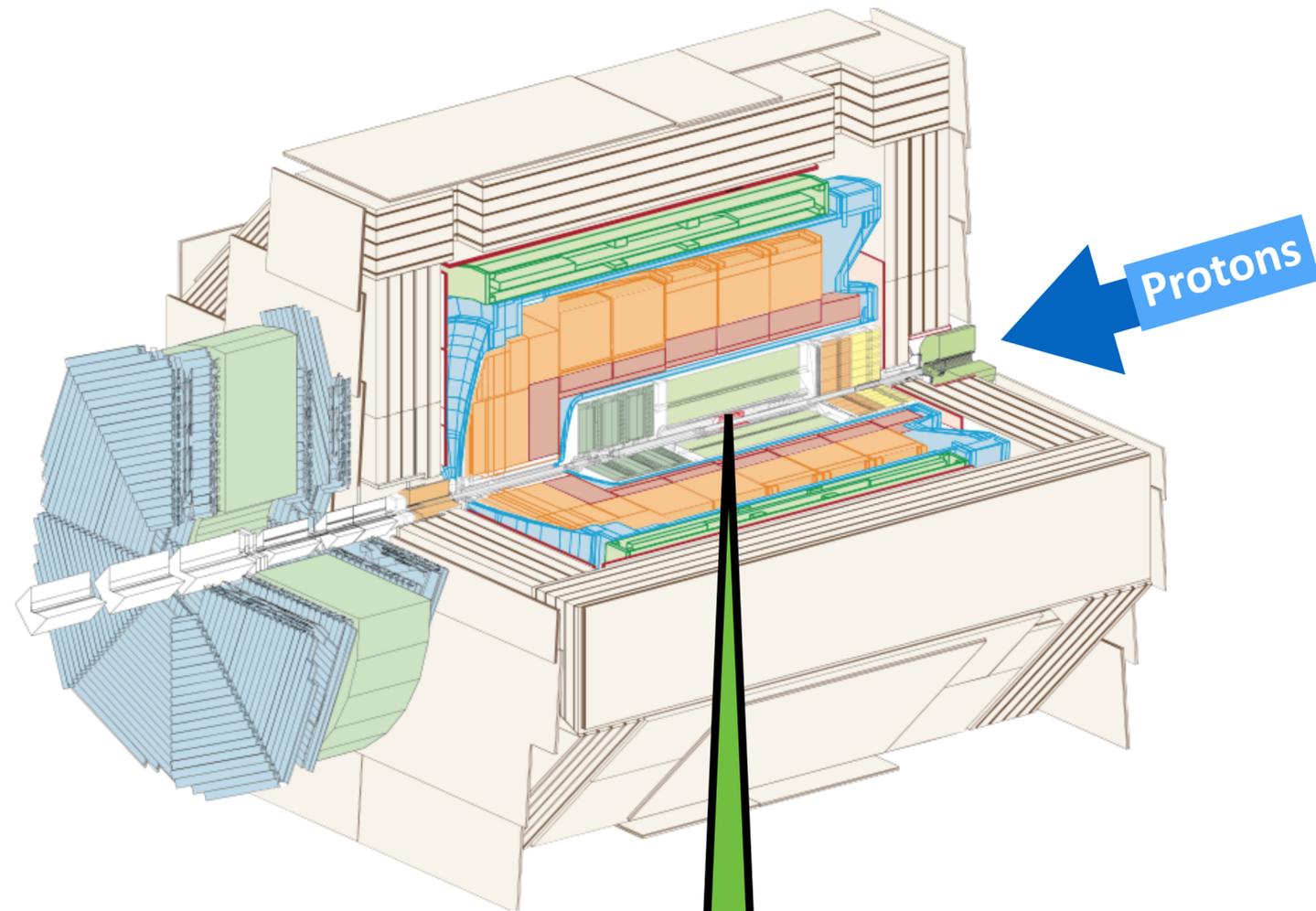
Asymmetric detector

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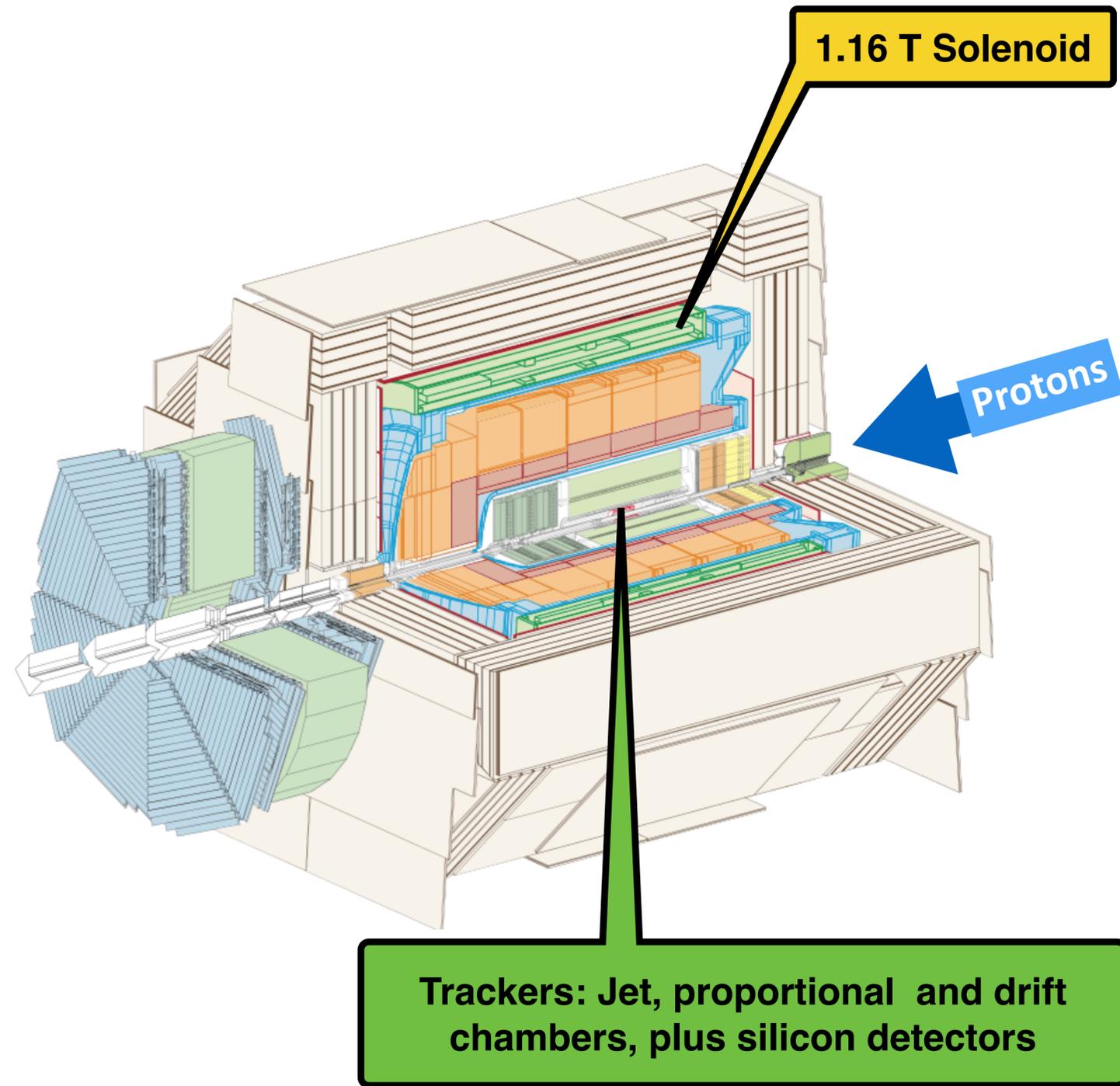
# H1 detector: central detectors



**Trackers: Jet, proportional and drift chambers, plus silicon detectors**

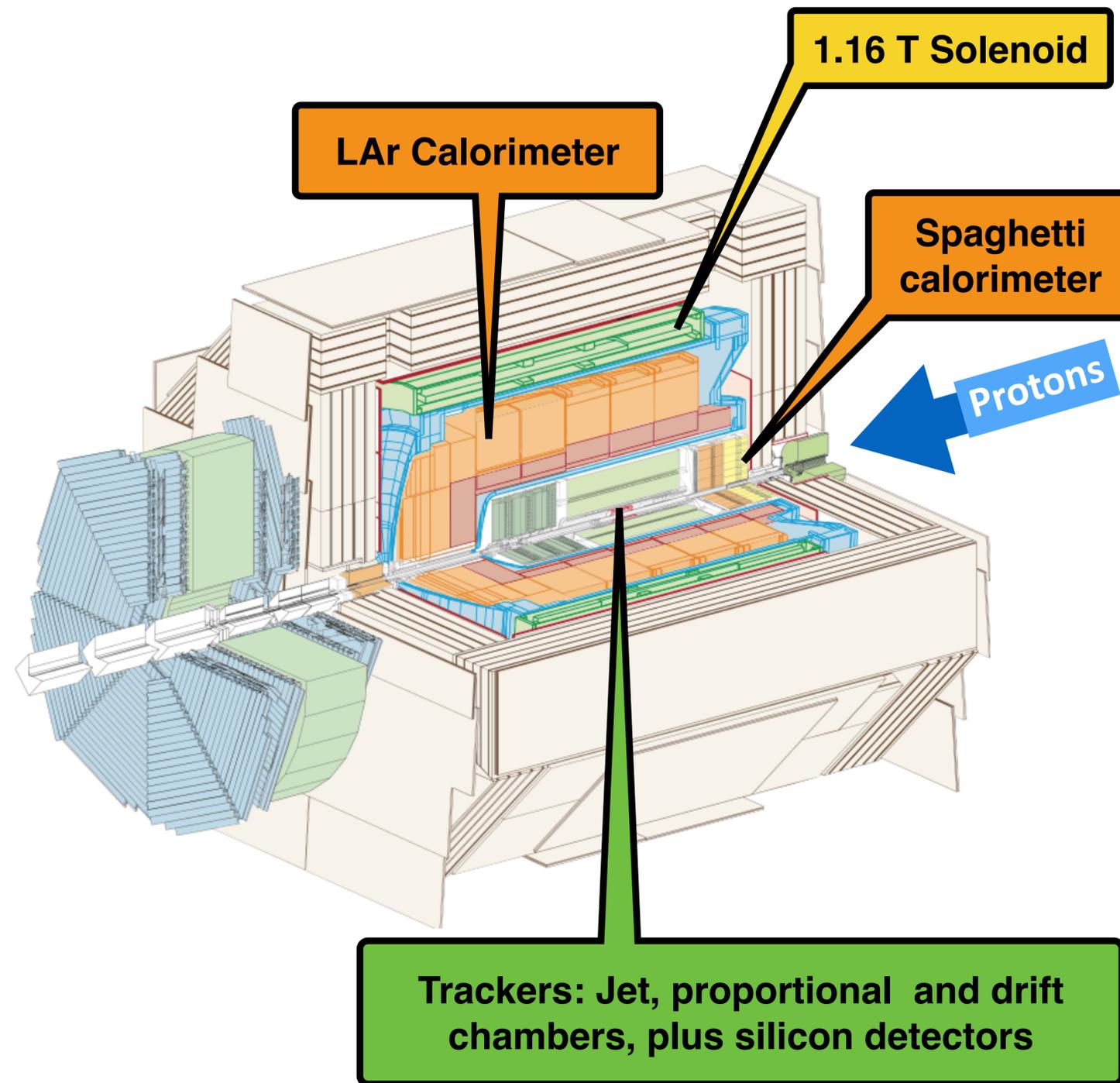
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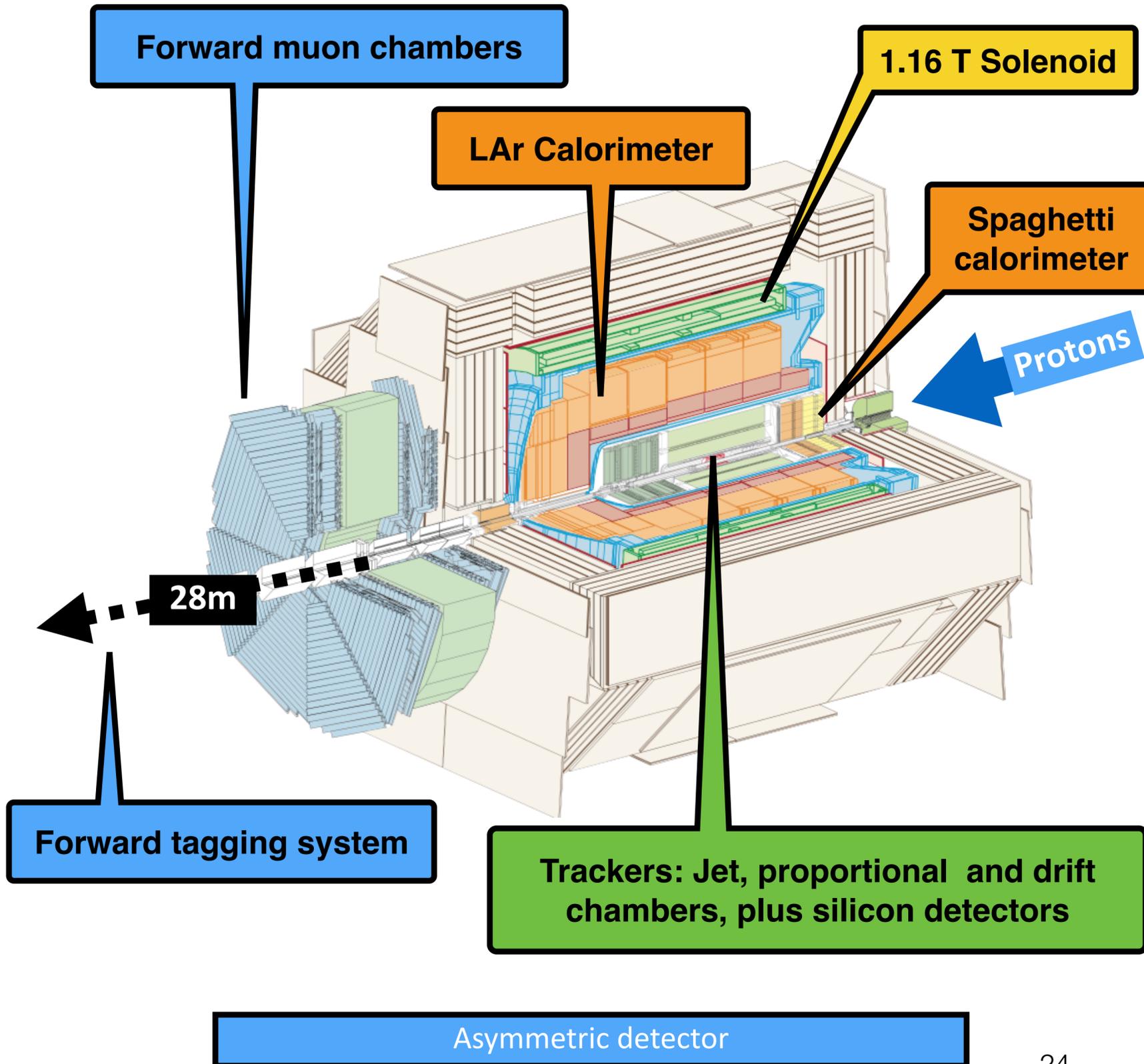
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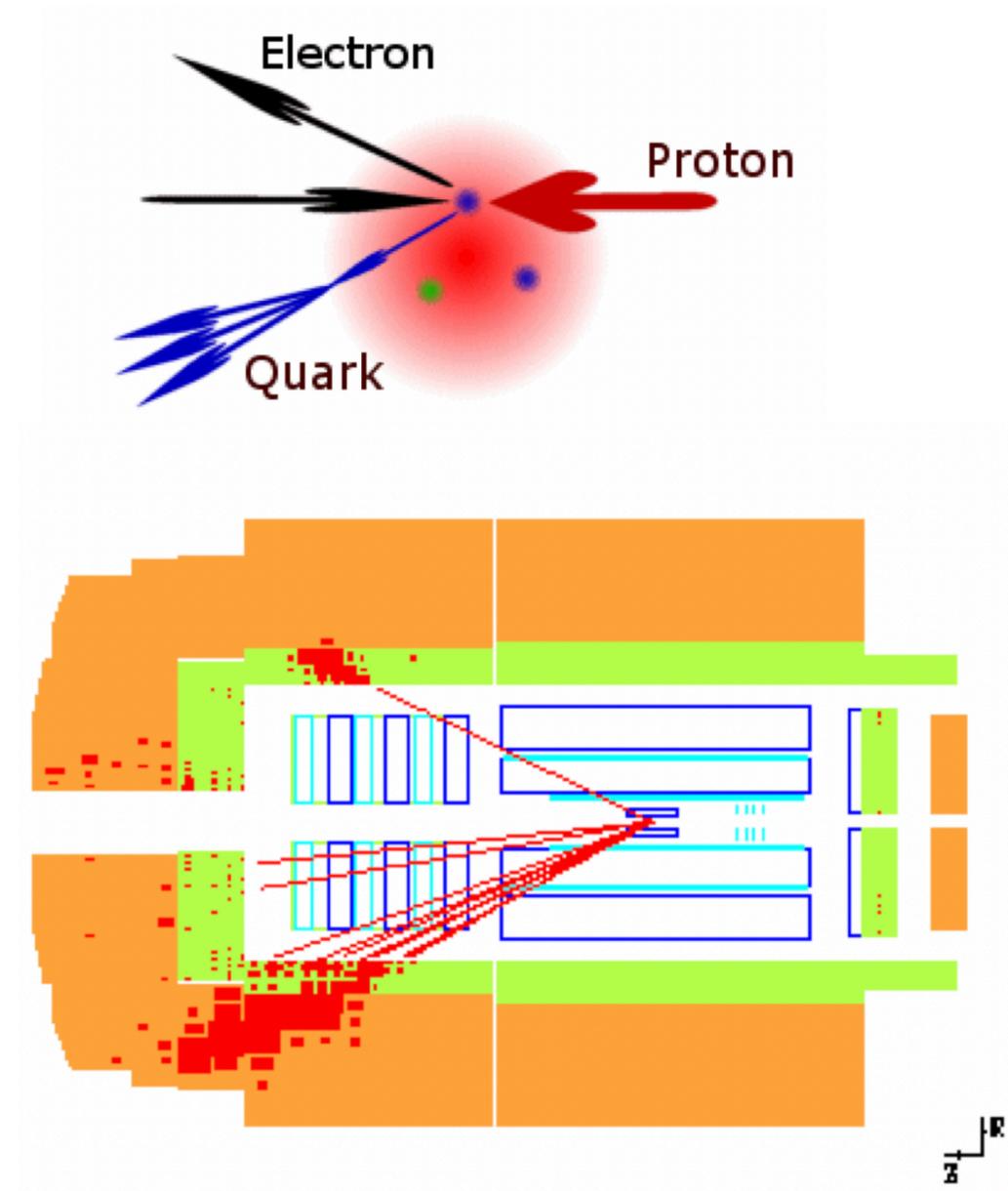
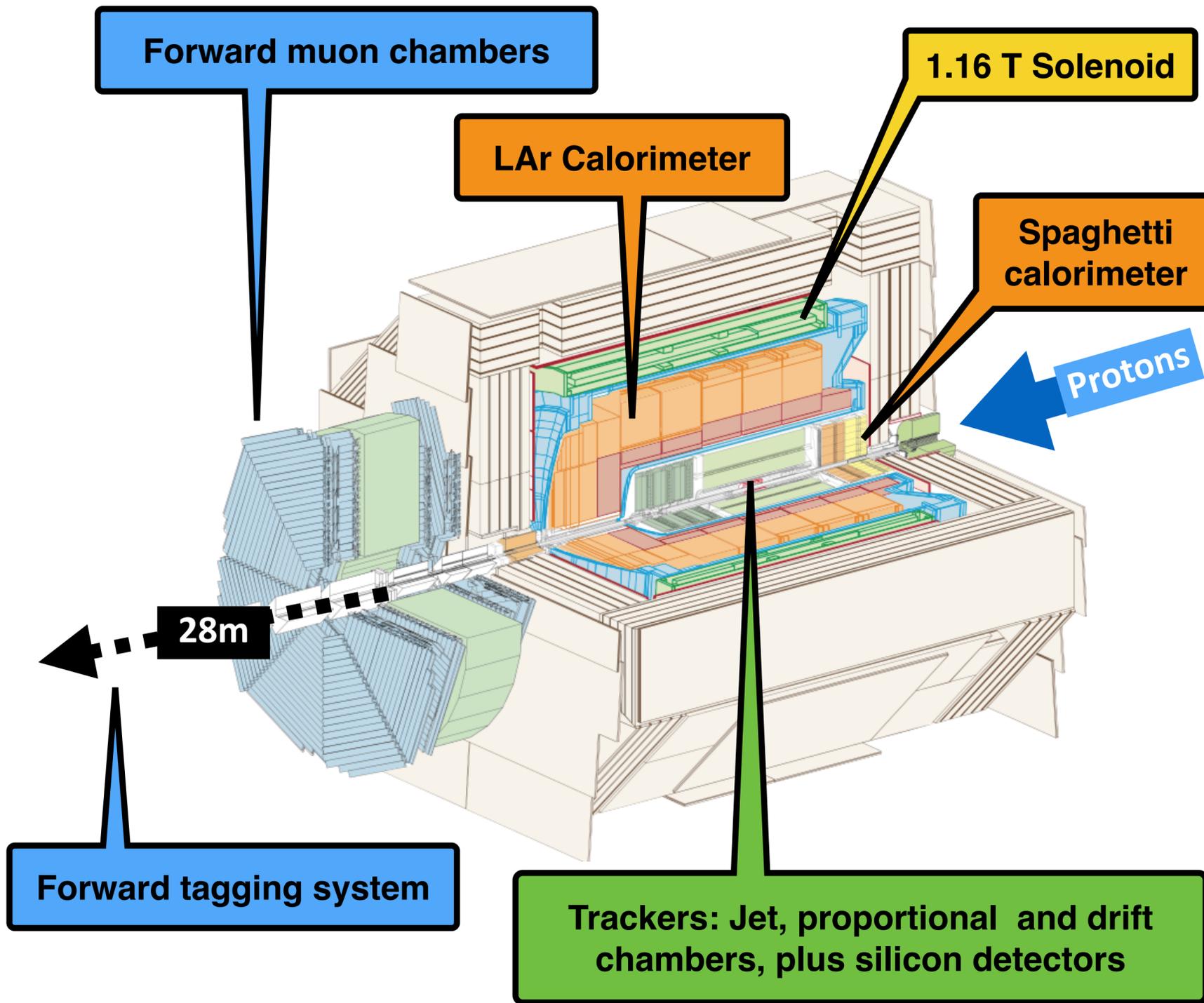


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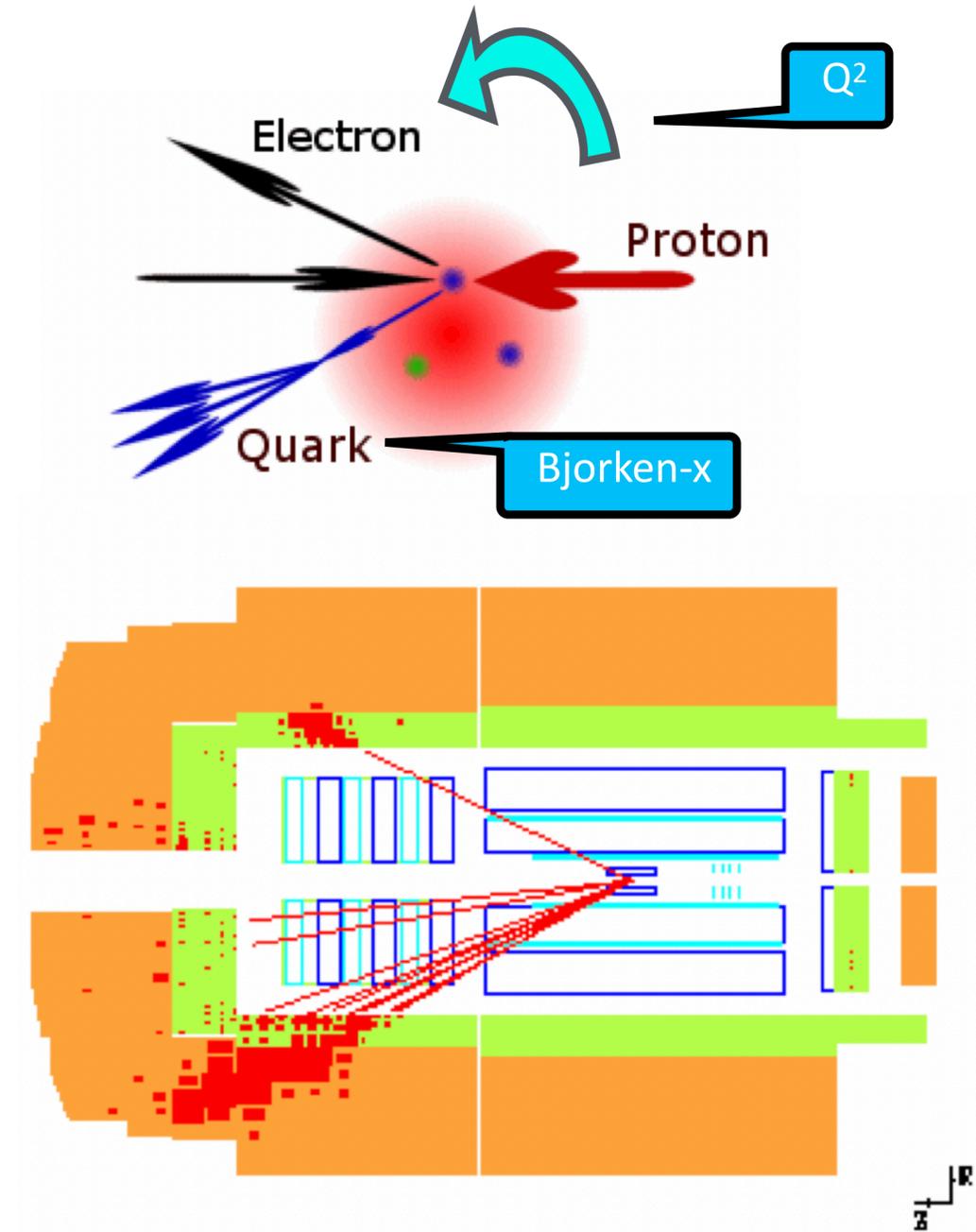
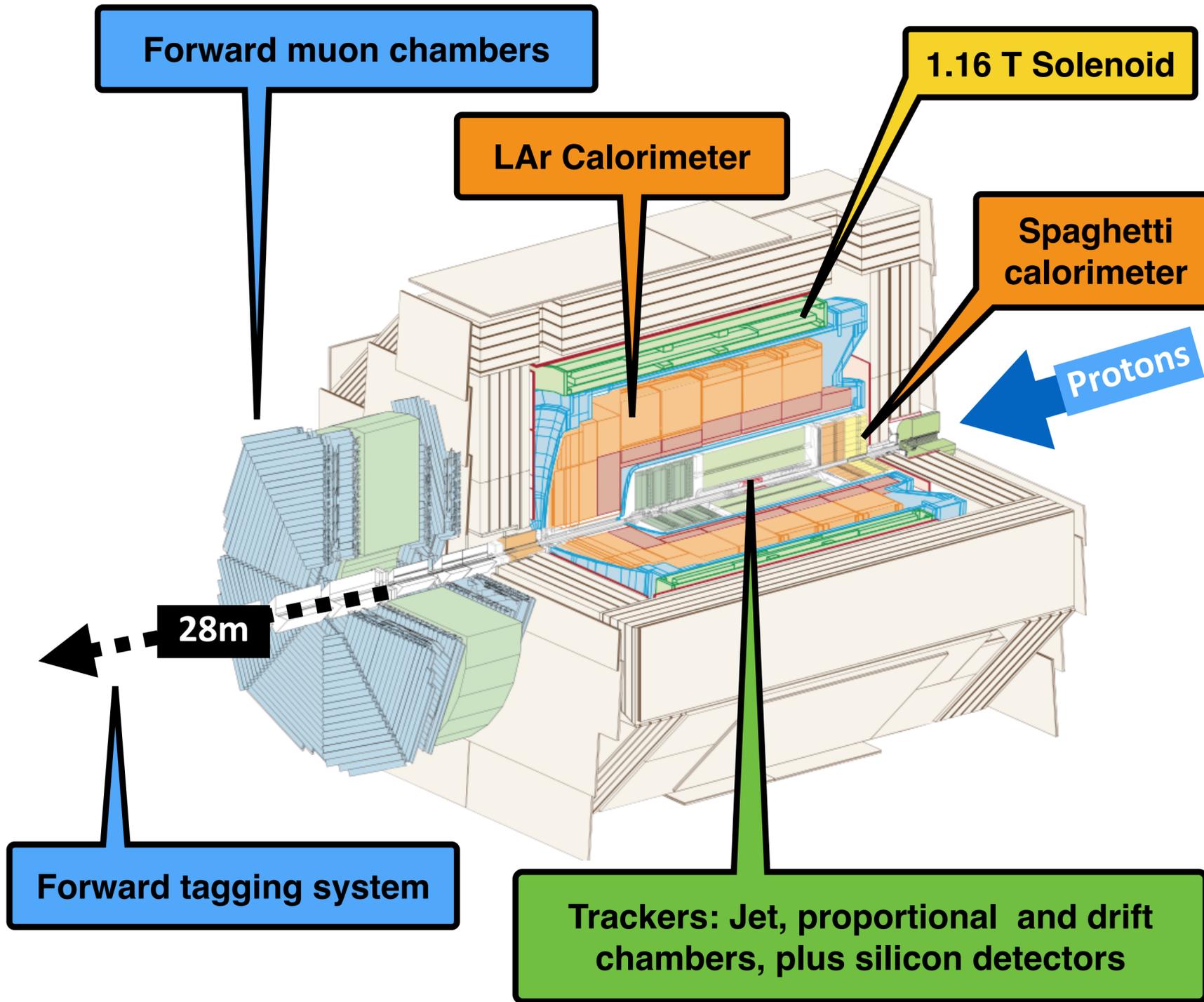
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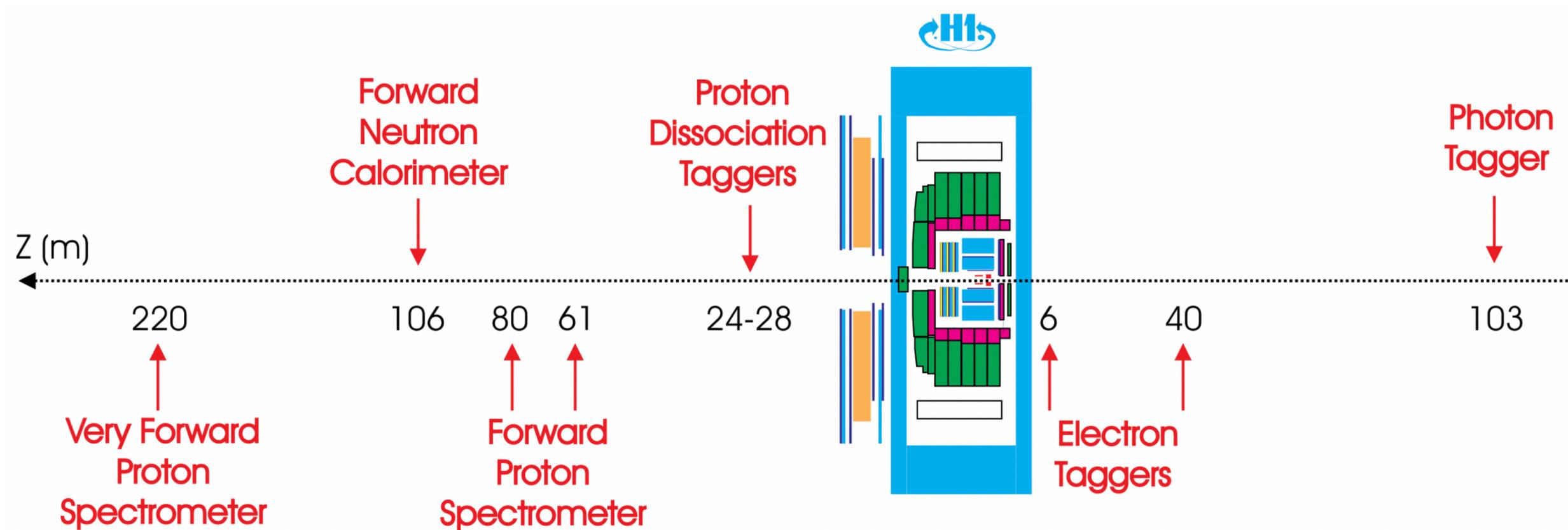
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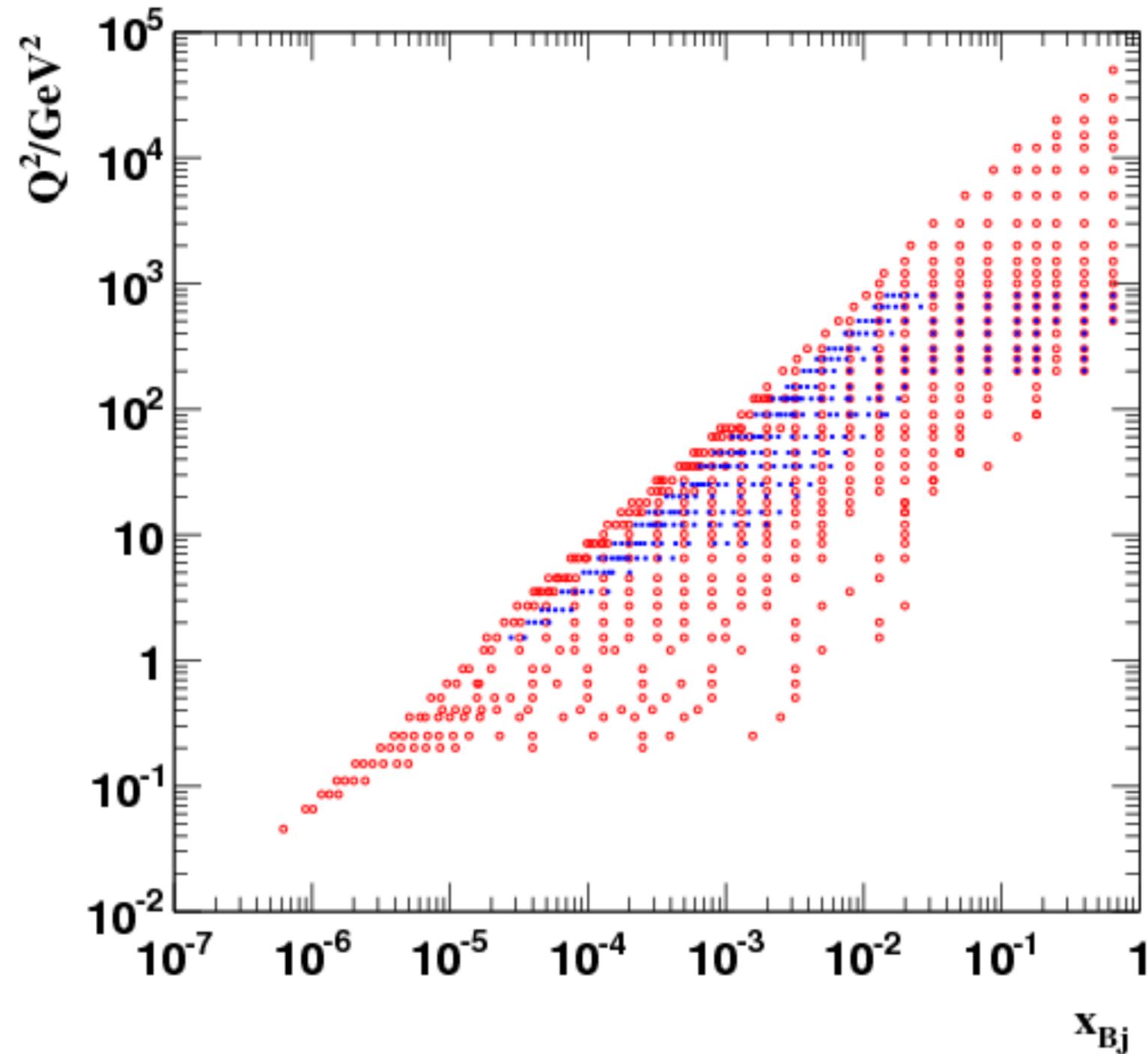
# H1 detector: forward detectors



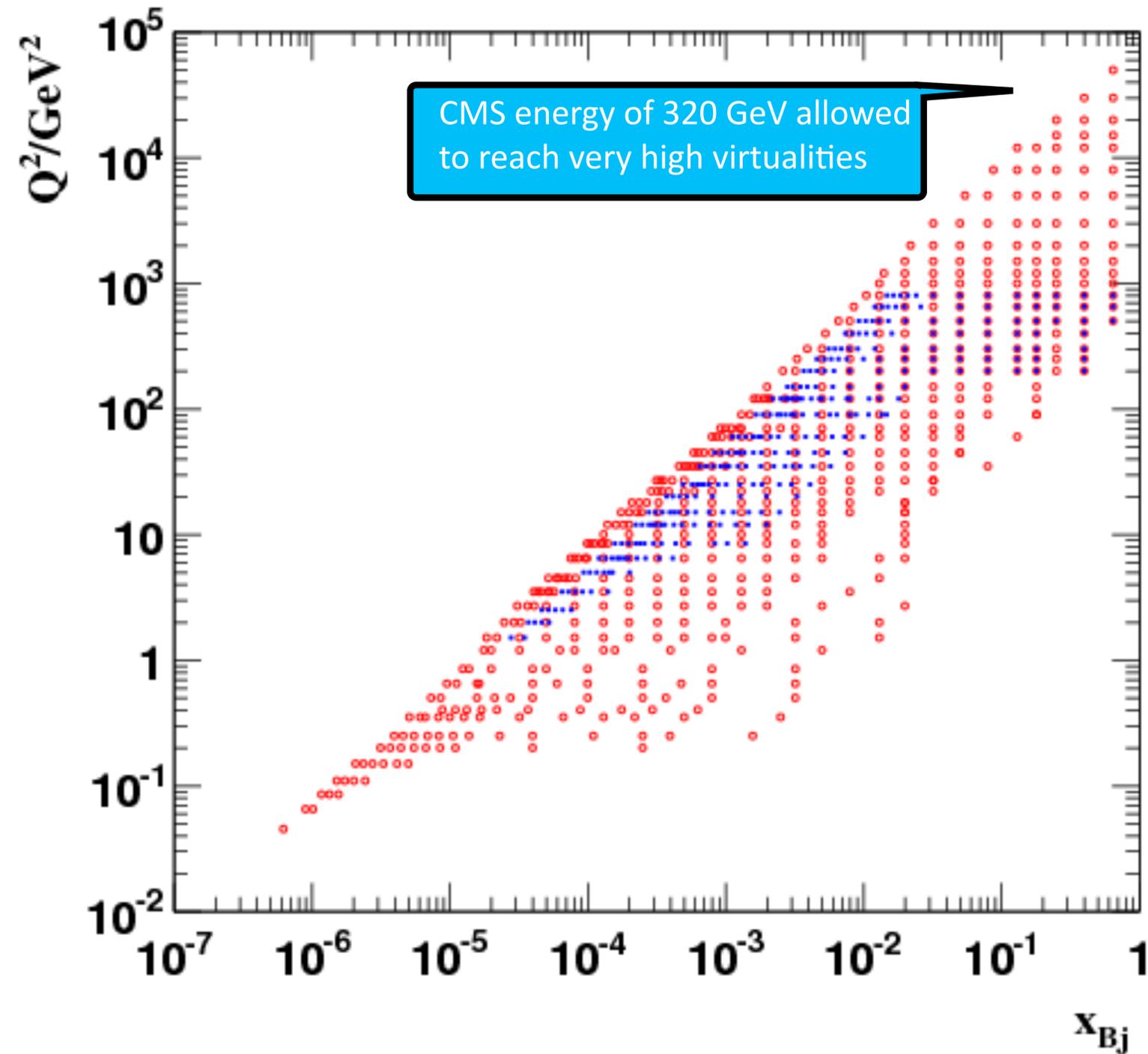
Tag diffractive processes

Luminosity (BH process) and photoproduction

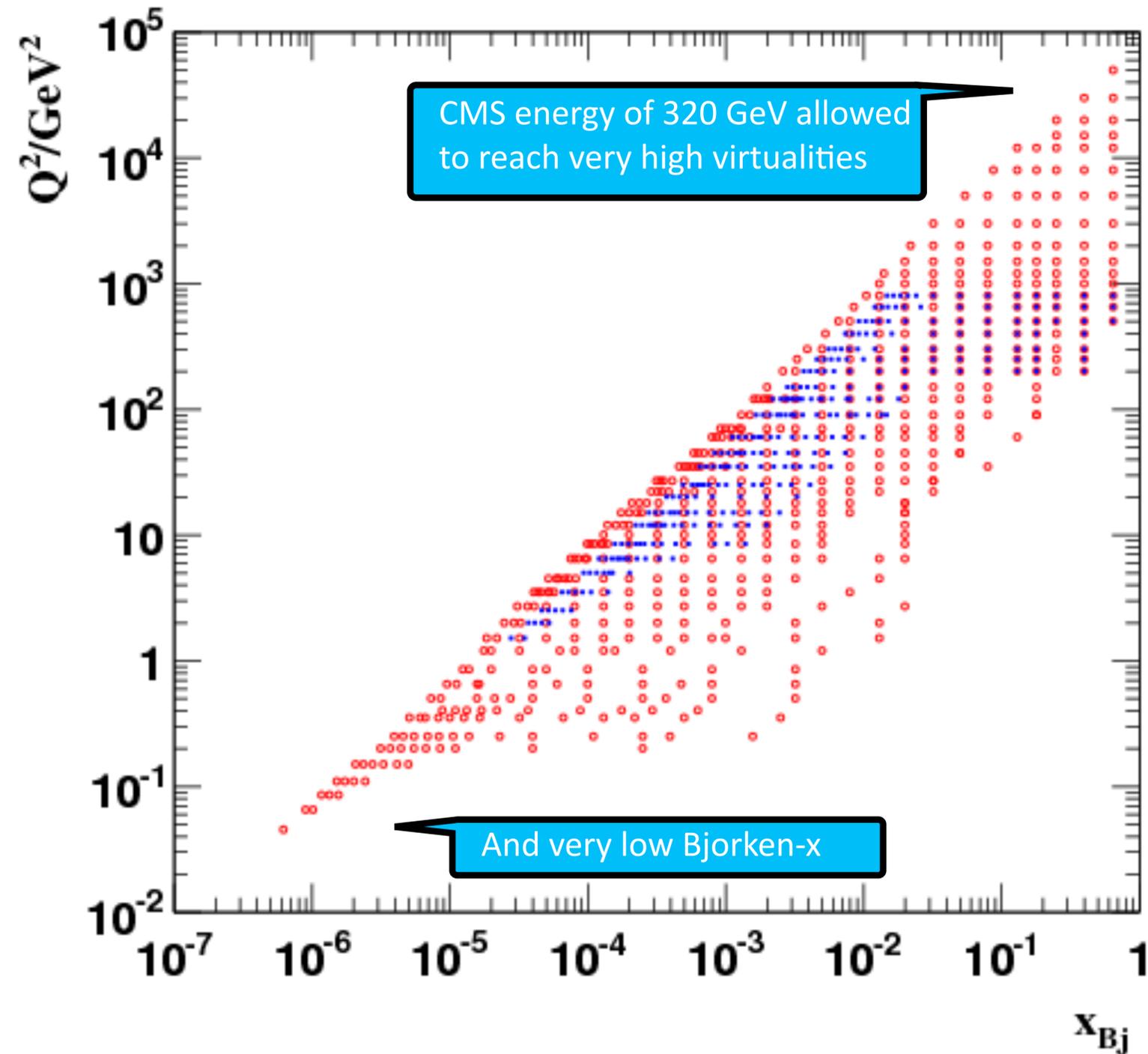
## H1 and ZEUS



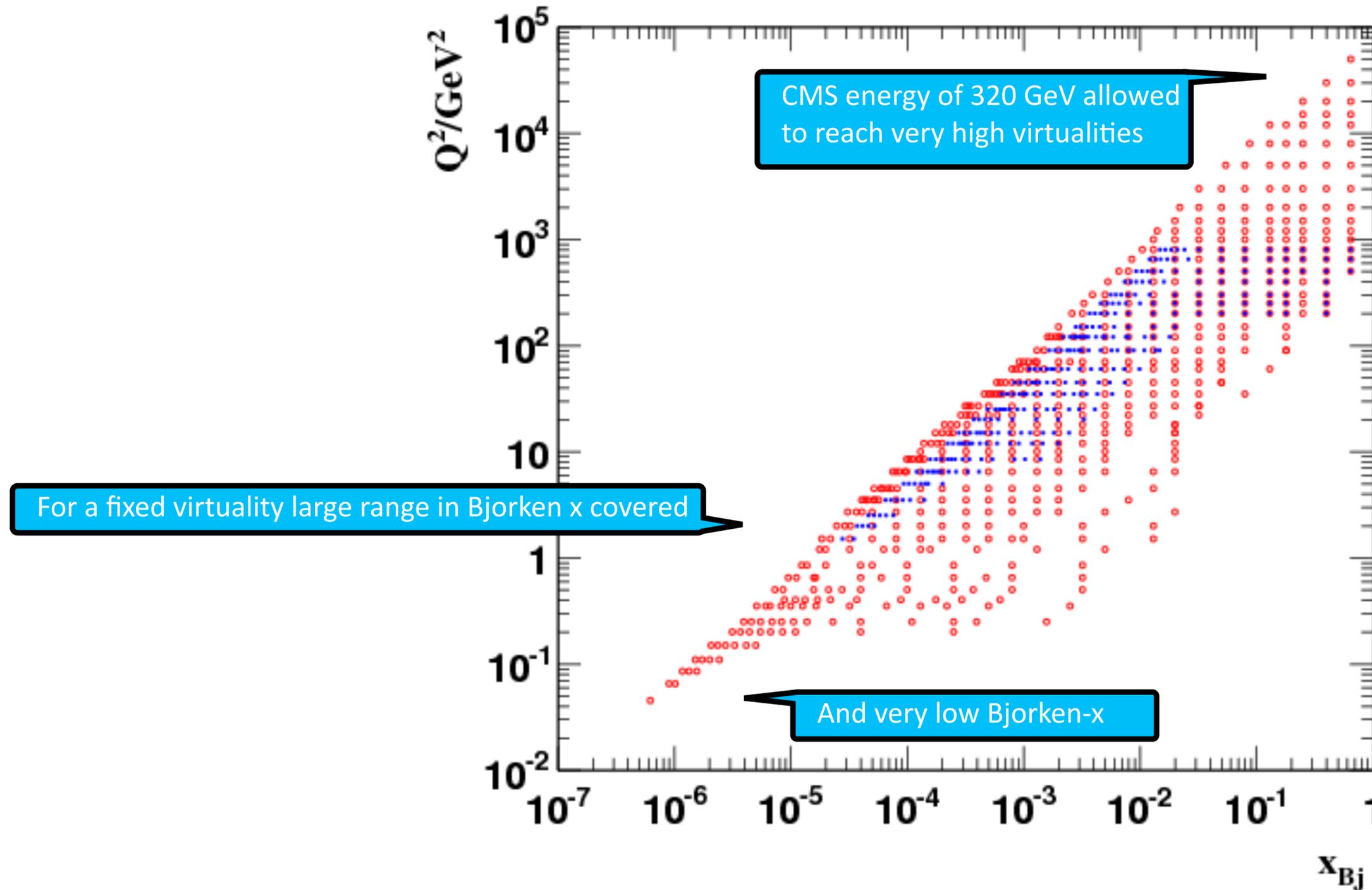
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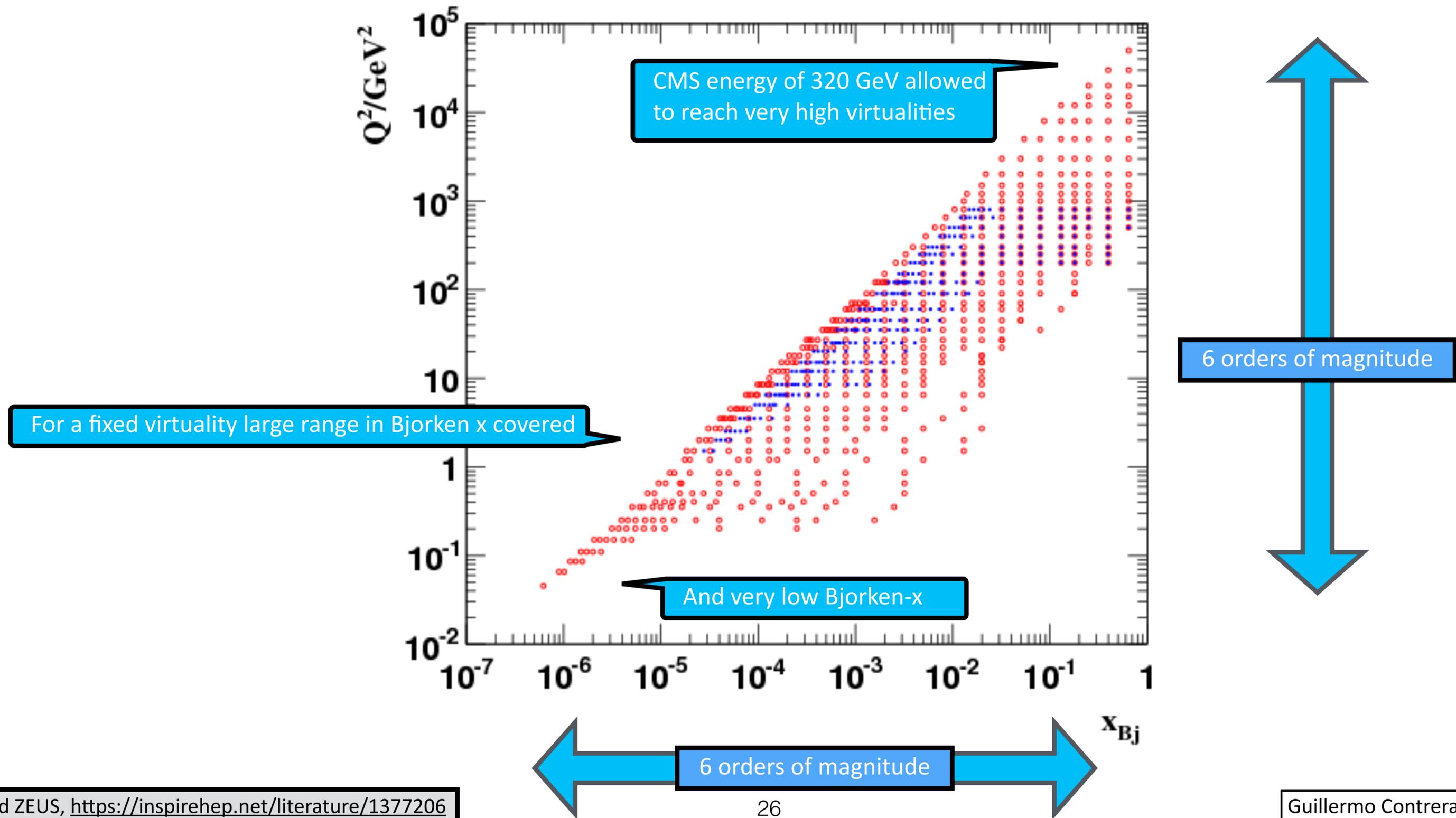


## H1 and ZEUS



# HERA: Kinematic coverage

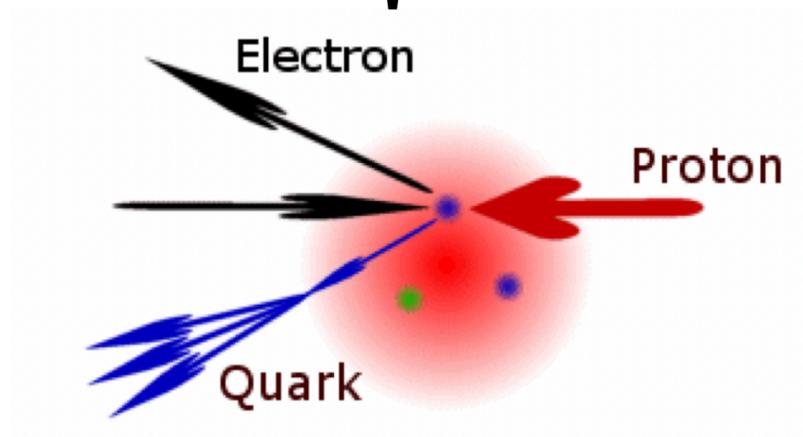
## H1 and ZEUS



At this point in time, we have an accelerator and detectors with a huge range in kinematics  
and we know how to extract QCD information from the measurements.  
Let's look at HERA data to extract the behaviour of quarks and gluons inside hadrons ...

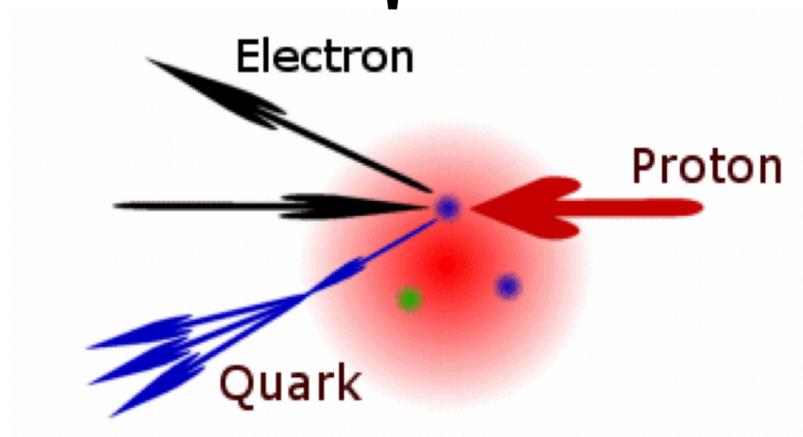
# Reconstructing the kinematics

Kinematics could be determined using only the scattered electron



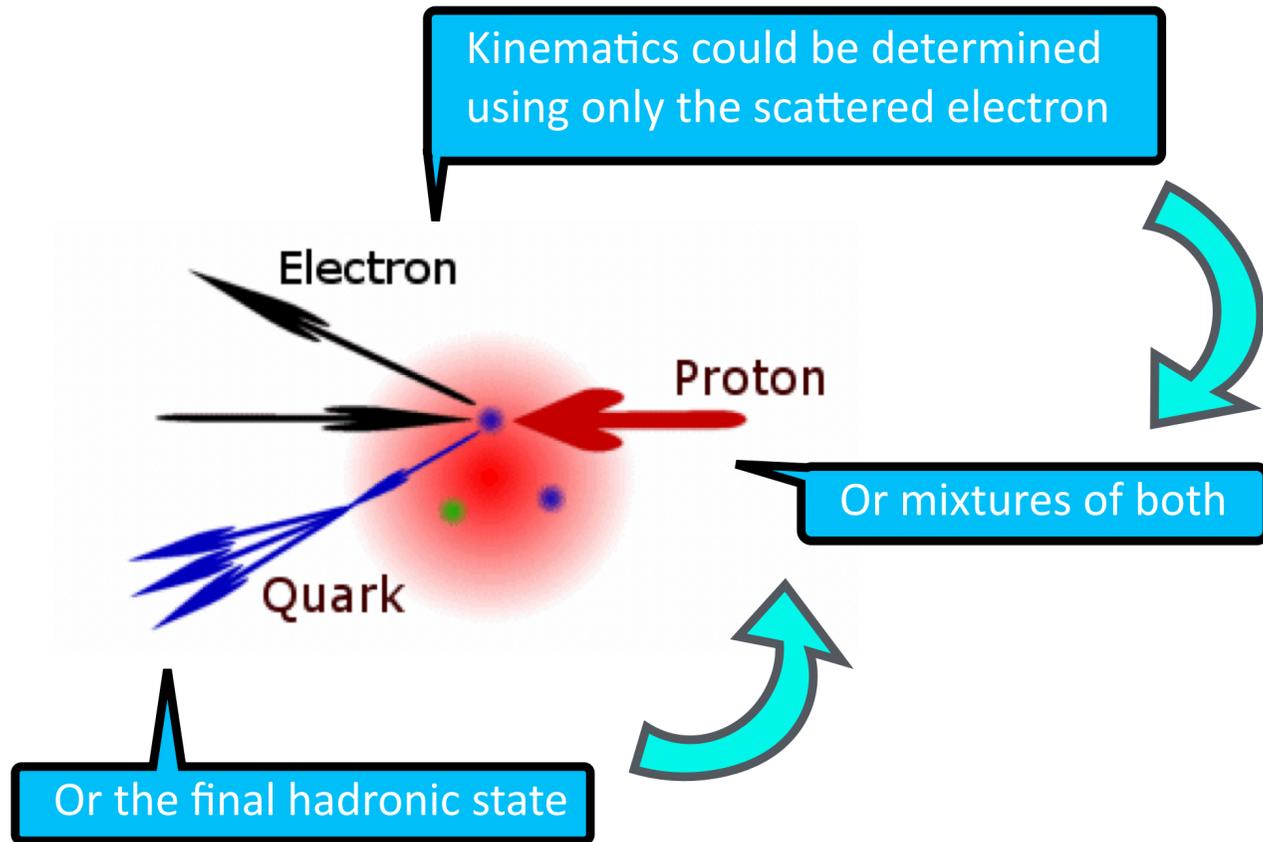
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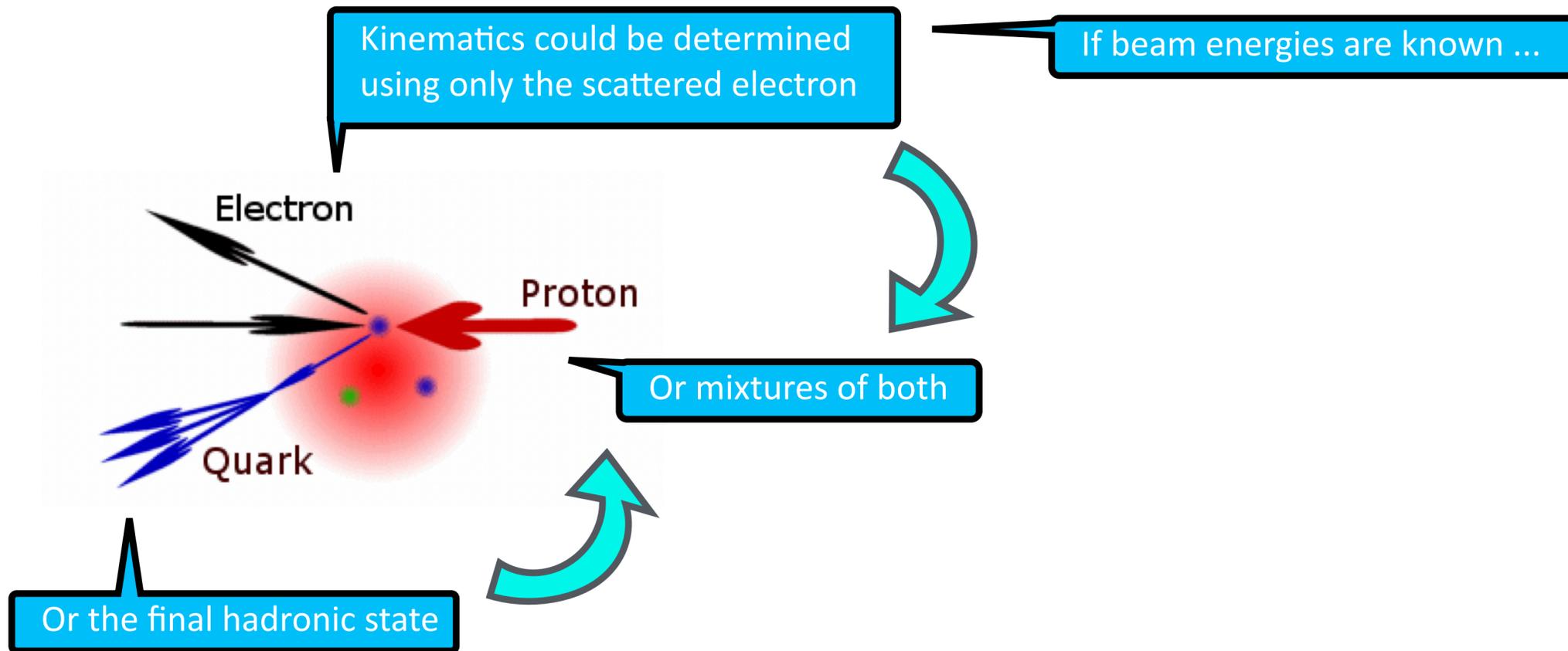


Or the final hadronic state

# Reconstructing the kinematics



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# Reconstructing the kinematics

Kinematics could be determined using only the scattered electron

If beam energies are known ...

Or mixtures of both

Or the final hadronic state

Not an exhaustive list

Method	$y$	$Q^2$	$x$
e	$1 - \frac{E}{E^e} \sin^2 \theta/2$	$4E^e E \cos^2 \theta/2$	$Q^2 / y_s$
h	$\Sigma / 2E^e$	$\frac{T^2}{1 - y_h}$	$Q^2 / y_s$
m	$y_h$	$Q_e^2$	$Q^2 / y_s$
DA	$\frac{\tan \gamma/2}{\tan \gamma/2 + \tan \theta/2}$	$4E^{e2} \frac{\cot \theta/2}{\tan \gamma/2 + \tan \theta/2}$	$Q^2 / y_s$
$\Sigma$	$\frac{\Sigma}{\Sigma + E(1 - \cos \theta)}$	$\frac{E^2 \sin^2 \theta}{1 - y_\Sigma}$	$Q^2 / y_s$
IDA	$y_{DA}$	$E^2 \tan \theta/2 \frac{\tan \gamma/2 + \tan \theta/2}{2 \cot \theta/2 + \tan \theta/2}$	$\frac{E \cot \gamma/2 + \cot \theta/2}{E^p \cot \theta/2 + \tan \theta/2}$
$1\Sigma$	$y_\Sigma$	$Q_\Sigma^2$	$\frac{E \cos^2 \theta/2}{E^p y_\Sigma}$

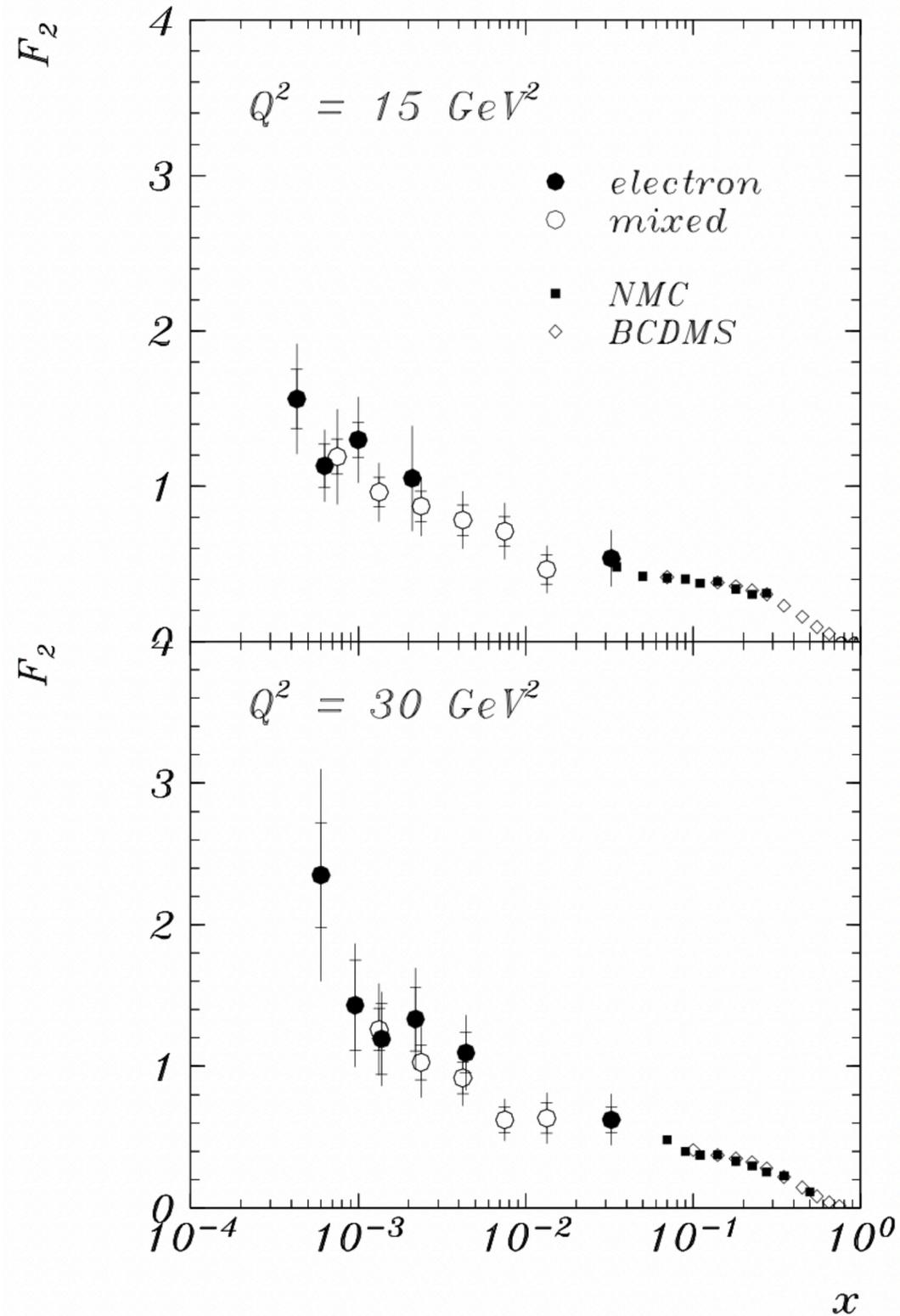
# Reconstructing the kinematics

The diagram shows an electron (black arrow) and a proton (red arrow) colliding. A quark (blue arrow) is shown being struck by the electron. Callouts indicate that kinematics can be determined from the scattered electron, or from the final hadronic state, or from mixtures of both. A homework assignment asks to deduce formulas from a table. A note states that the table is not an exhaustive list.

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$1\Sigma$	$y_\Sigma$	$Q_\Sigma^2$	$\frac{E}{E^p} \frac{\cos^2 \theta/2}{y_\Sigma}$

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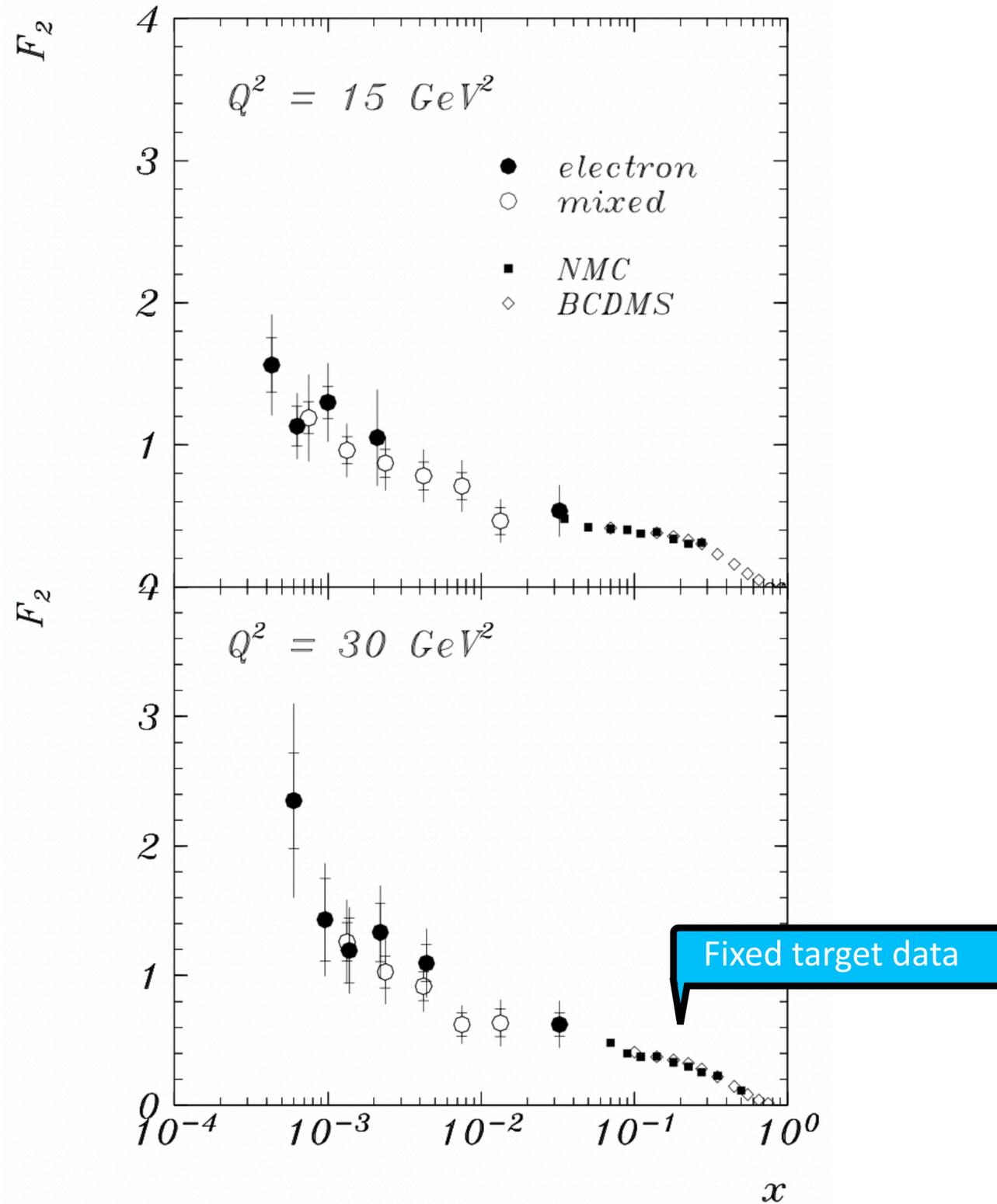
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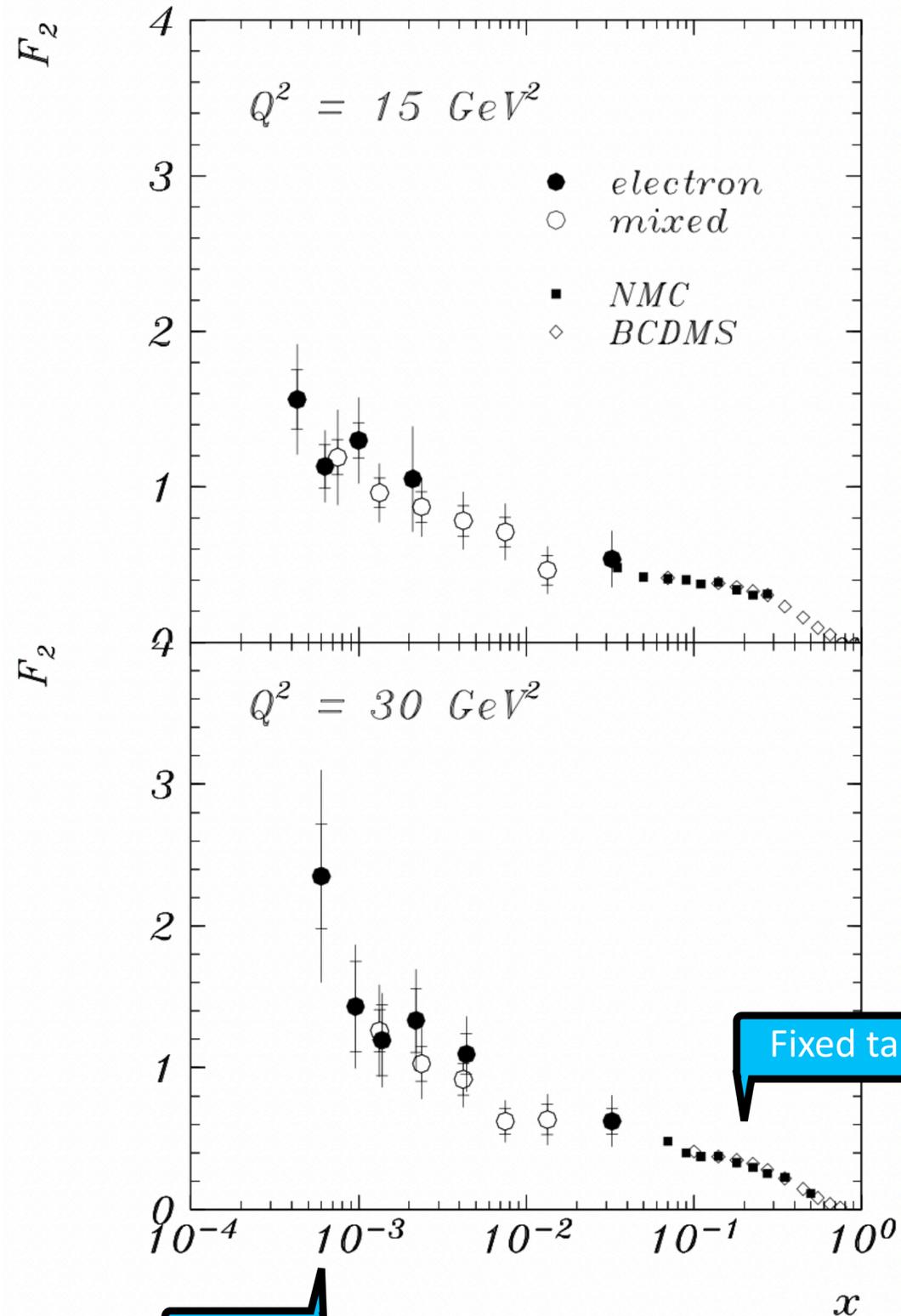
H1, <https://inspirehep.net/literature/357797>

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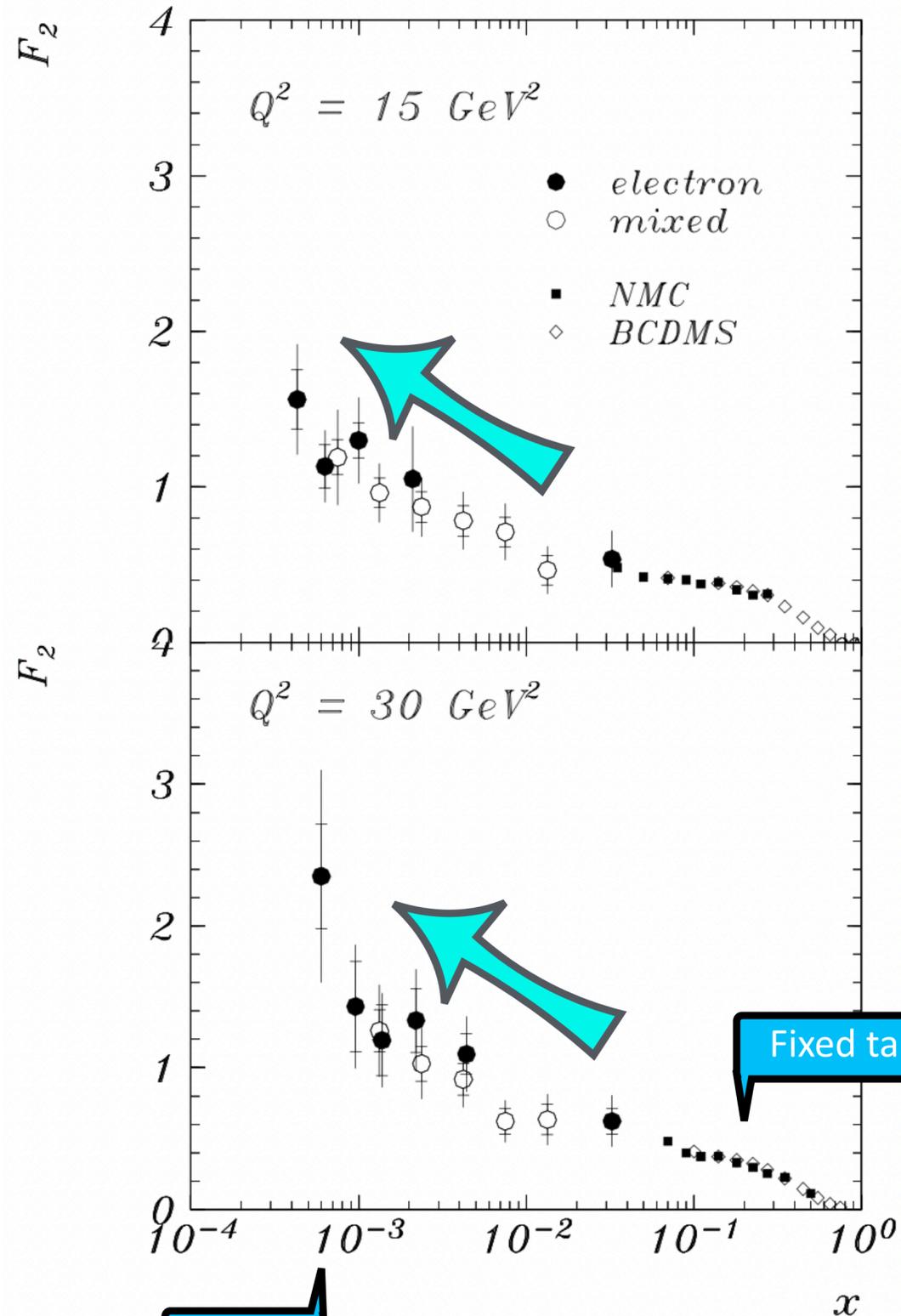
Data reach 2 orders of magnitude smaller Bjorken-x than fixed target experiments

Fixed target data

Low x

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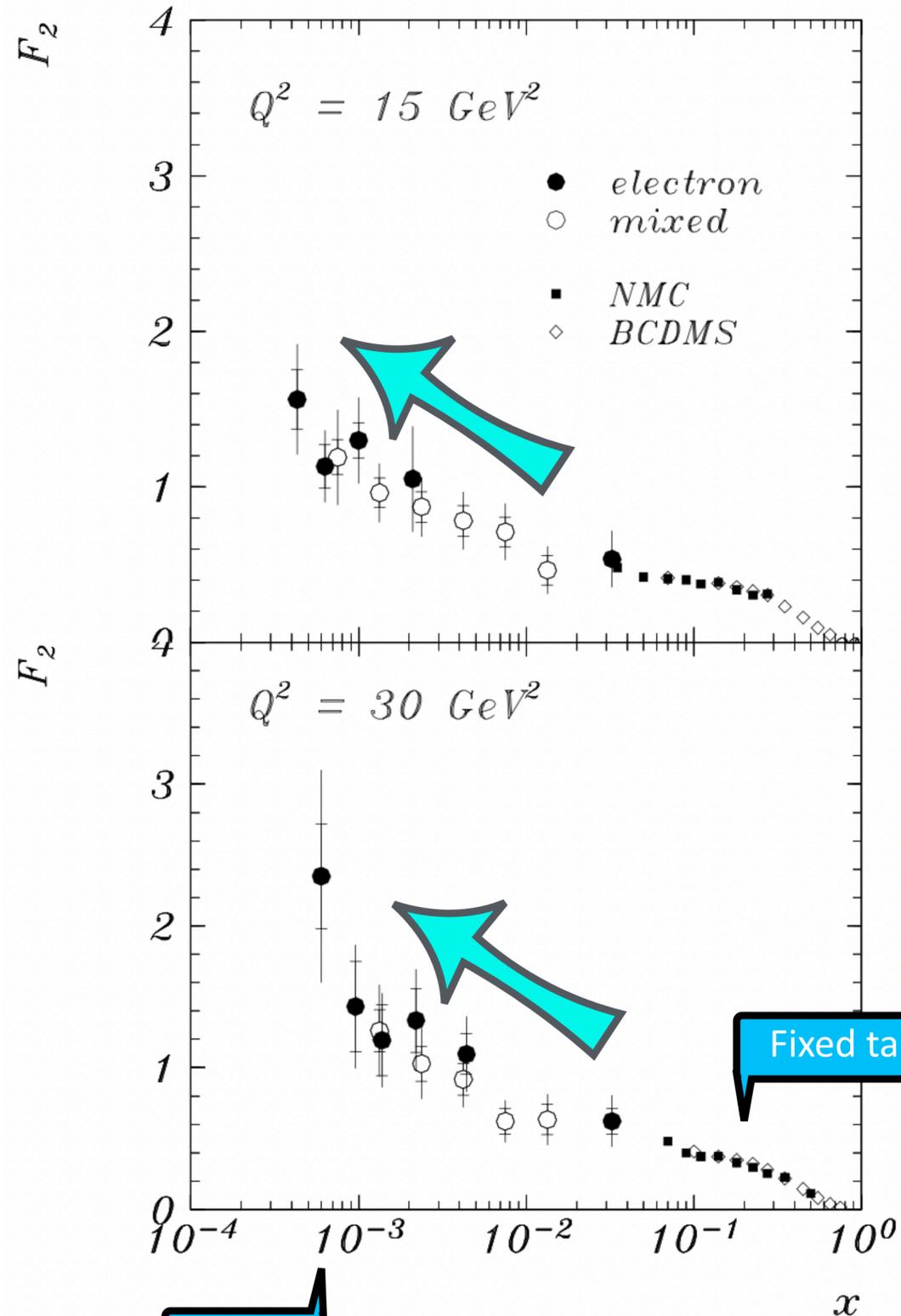
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How does  $F_2$  change with the photon virtuality?

Low x

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The evolution of hadron structure is predicted within pQCD in the form of differential equations

# Parenthesis: Altarelli-Parisi equations

1977: Evolution equations

## ASYMPTOTIC FREEDOM IN PARTON LANGUAGE

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*Institut des Hautes Etudes Scientifiques, Bures-sur-Yvette, France*

Received 12 April 1977

[https://doi.org/10.1016/0550-3213\(77\)90384-4](https://doi.org/10.1016/0550-3213(77)90384-4)

In this paper we show that an alternative derivation of all results of current interest for the  $Q^2$  behaviour of deep inelastic structure functions is possible. In this approach all stages of the calculation refer to parton concepts and offer a very illuminating physical interpretation of the scaling violations. In our opinion the present approach, although less general, is remarkably simpler than the usual one since all relevant results can be derived in a direct way from the basic vertices of QCD, with no loop calculations being involved (the only exception is the lowest order expression for the running coupling constant which we do not rederive).

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$t \equiv \ln Q^2/Q_0^2$

$$\frac{dq^i(x, t)}{dt} = \frac{\alpha(t)}{2\pi} \int_x^1 \frac{dy}{y} \left[ q^i(y, t) P_{qq}\left(\frac{x}{y}\right) + G(y, t) P_{qG}\left(\frac{x}{y}\right) \right],$$

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Probability density per unit  $t$ , at order  $\alpha$ , of finding a gluon inside a quark with a fraction  $x/y$  of the quark momentum

Density of gluons inside the proton in the infinite momentum frame

The evolution of hadron structure is predicted within pQCD in the form of differential equations

# Parenthesis: Altarelli-Parisi equations

1977: Evolution equations

ASYMPTOTIC FREEDOM IN PARTON LANGUAGE

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Received 12 April 1977

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In this paper we show that an alternative derivation of all results of current interest for the  $Q^2$  behaviour of deep inelastic structure functions is possible. In this approach all stages of the calculation refer to parton concepts and offer a very illuminating physical interpretation of the scaling violations. In our opinion the present approach, although less general, is remarkably simpler than the usual one since all relevant results can be derived in a direct way from the basic vertices of QCD, with no loop calculations being involved (the only exception is the lowest order expression for the running coupling constant which we do not rederive).

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Scaling violations

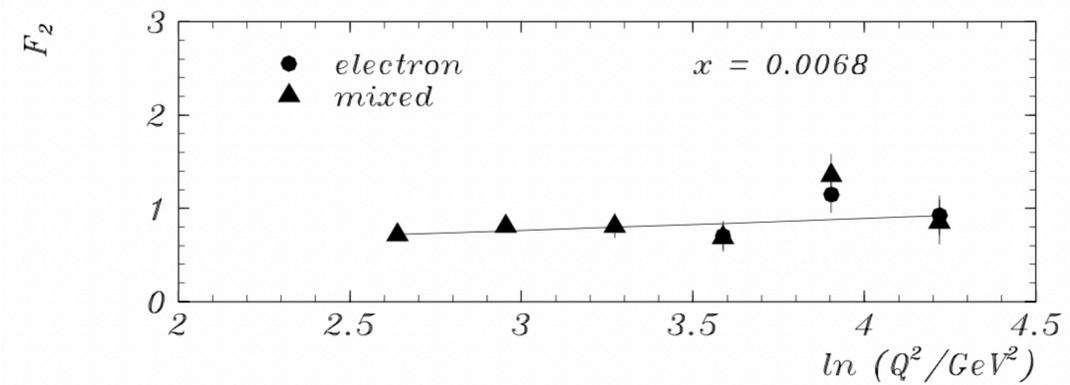
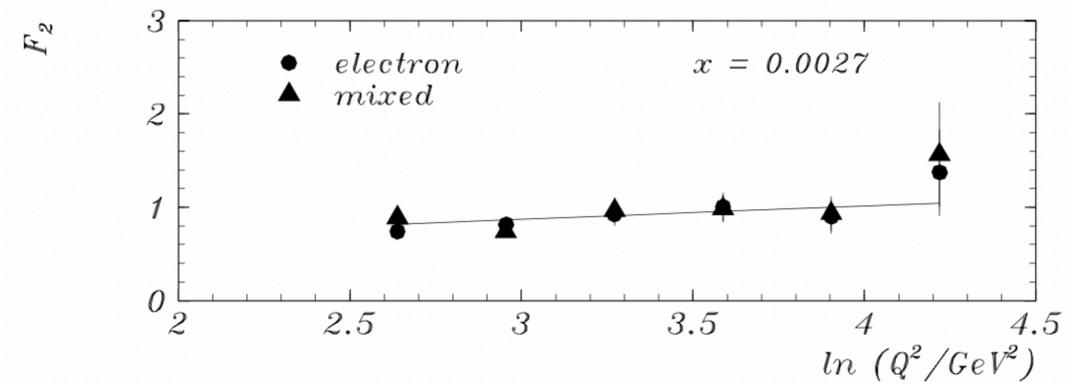
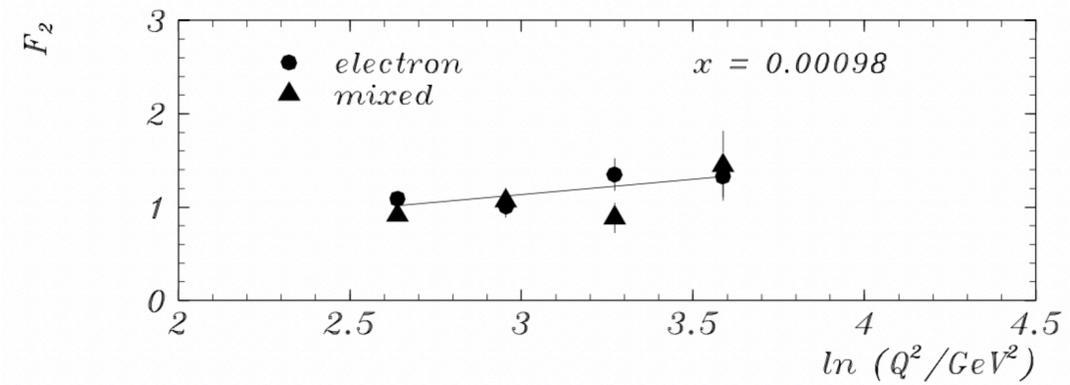
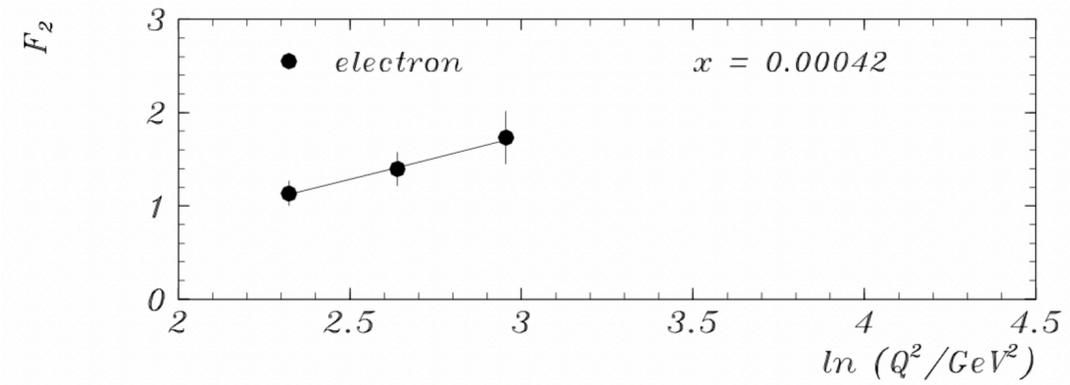
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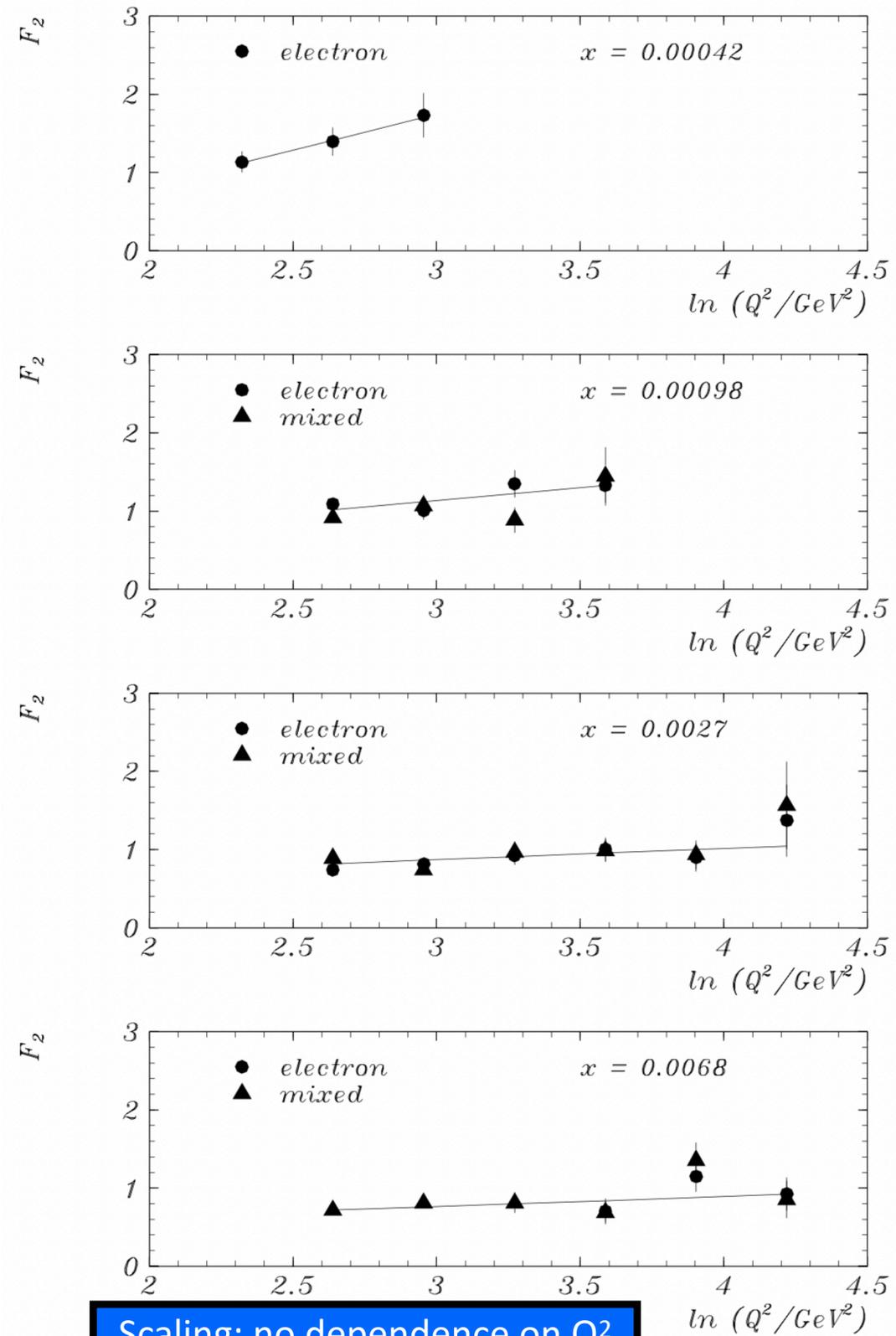
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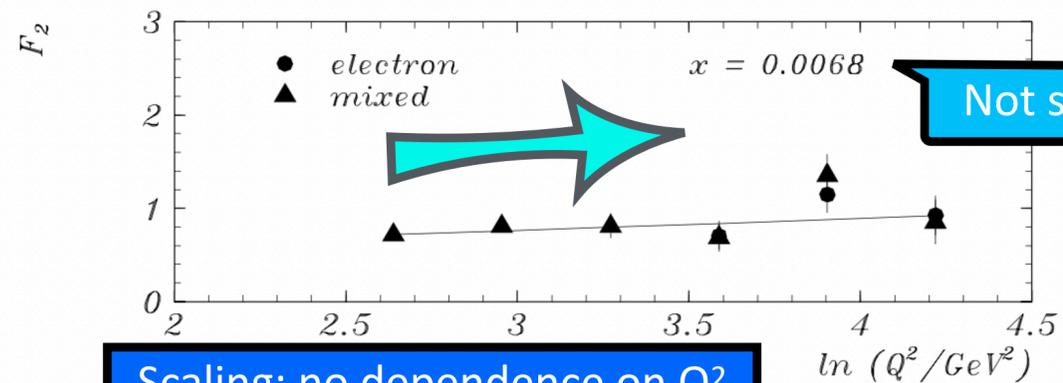
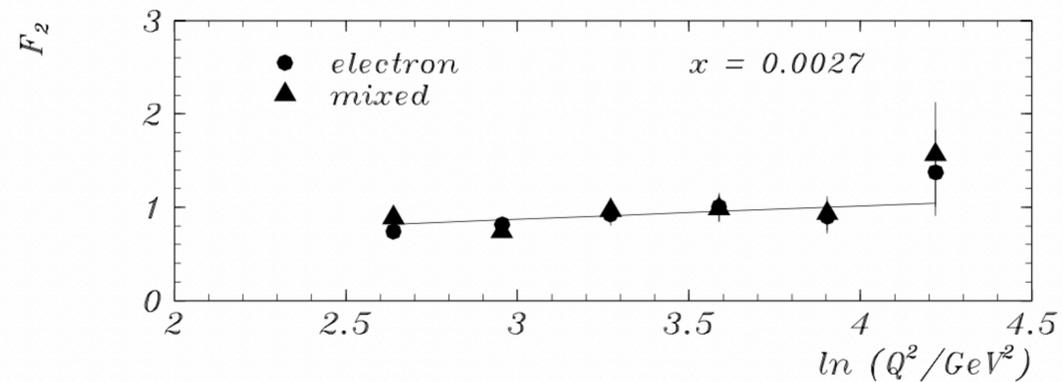
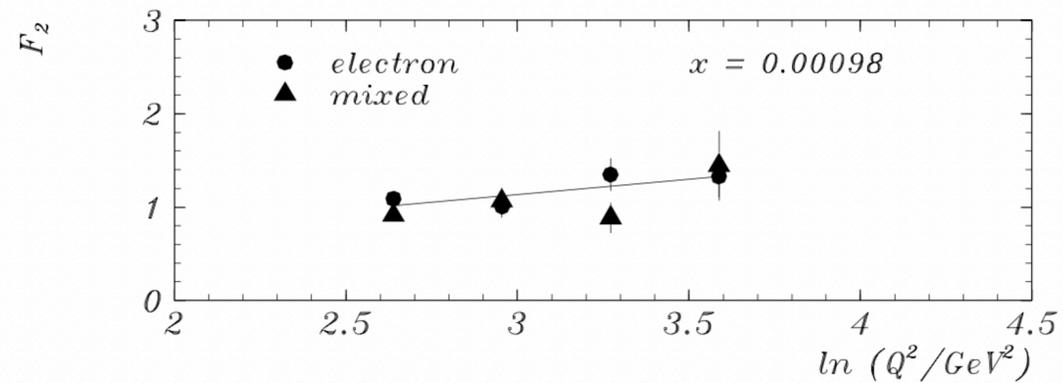
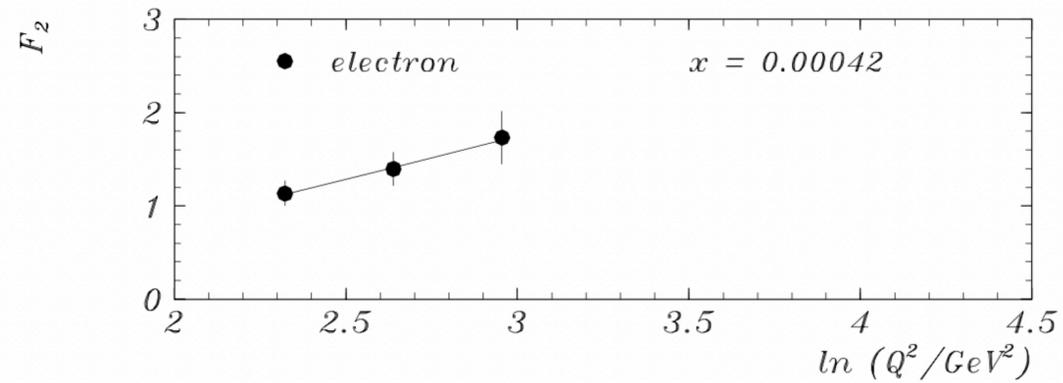
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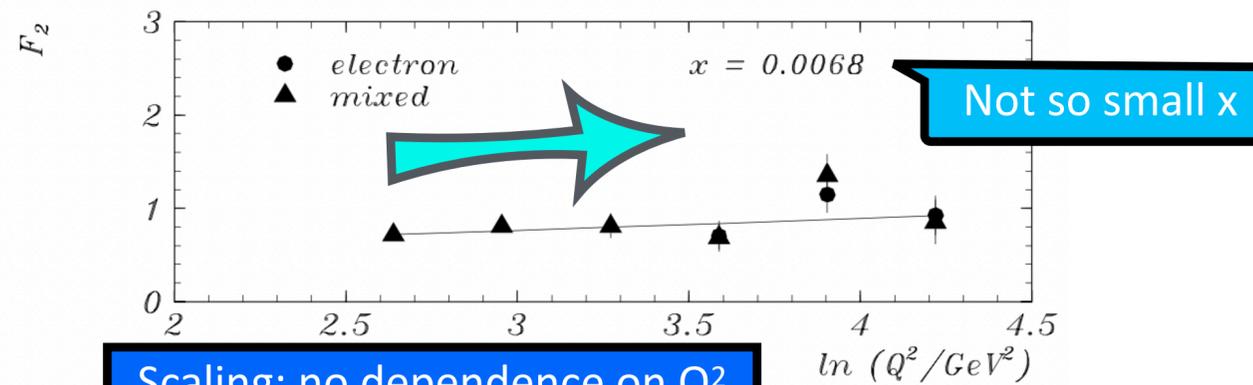
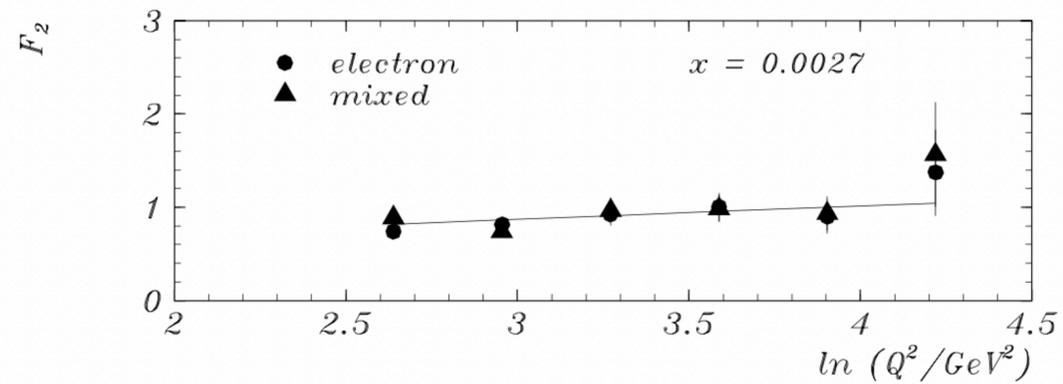
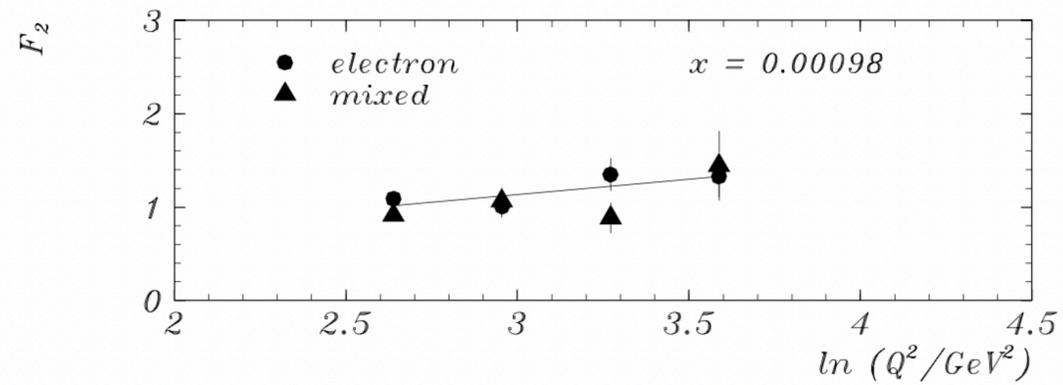
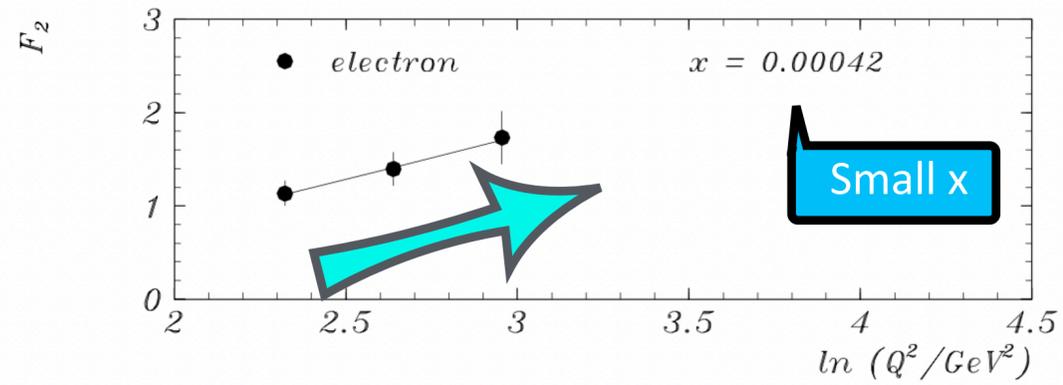
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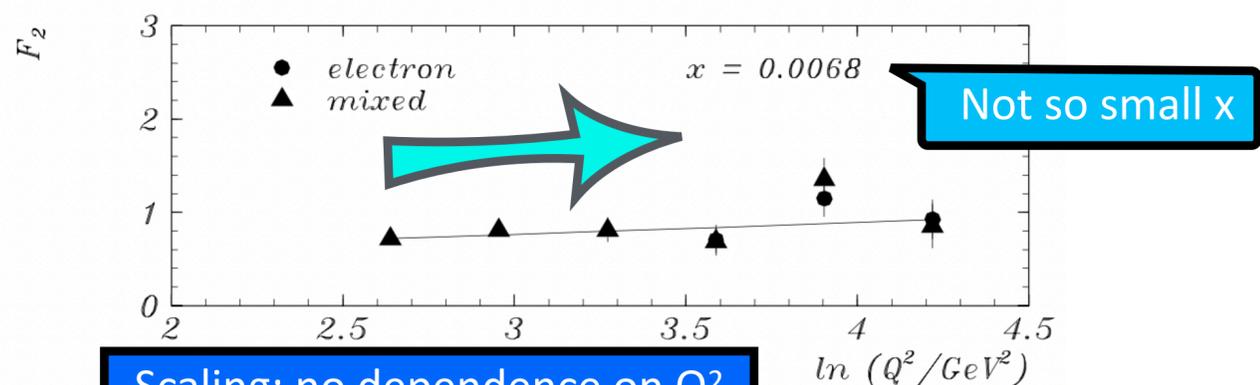
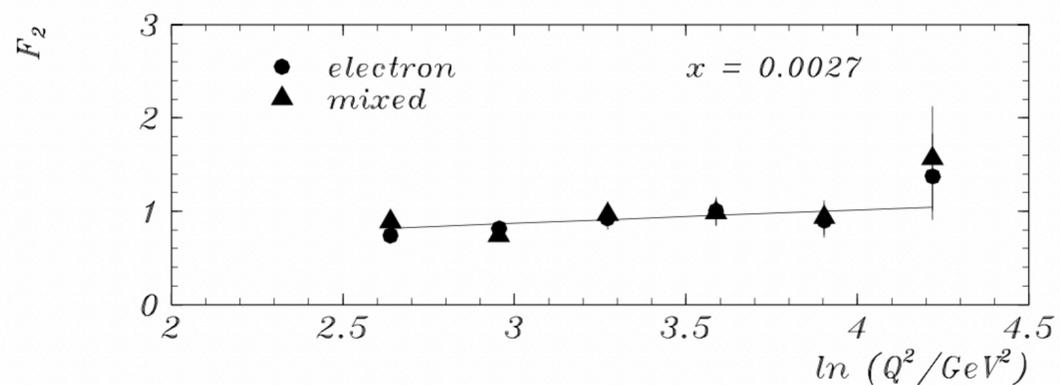
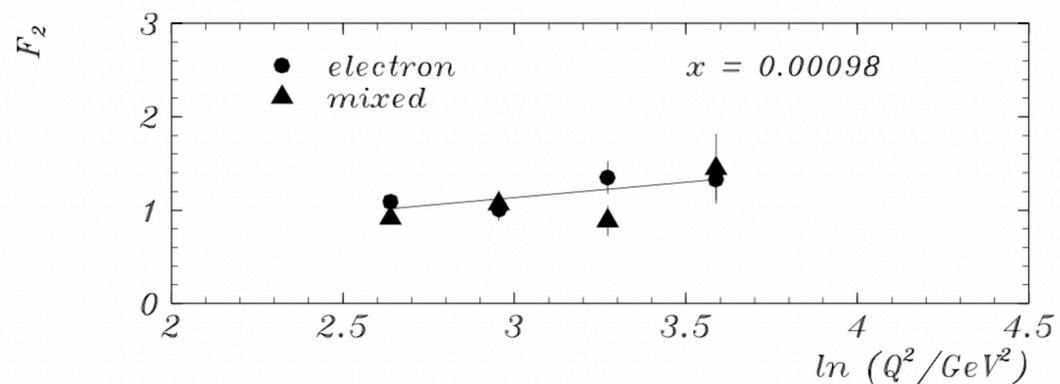
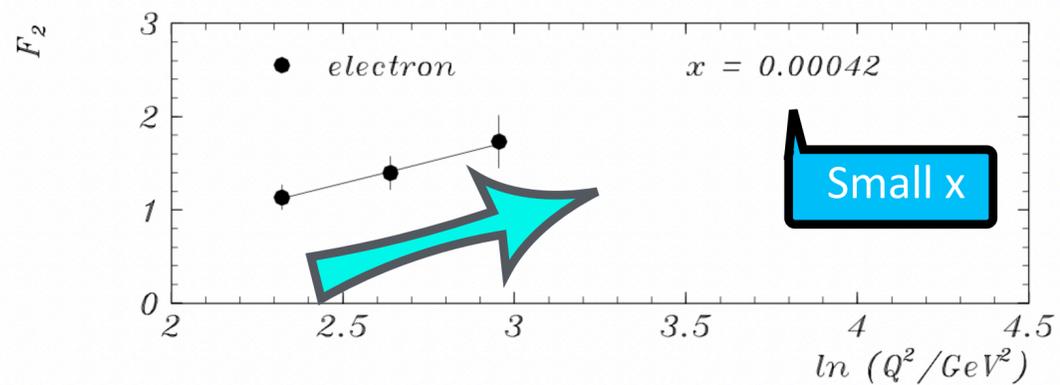
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Scaling violations logarithmic in virtuality

Violations more severe at small Bjorken x



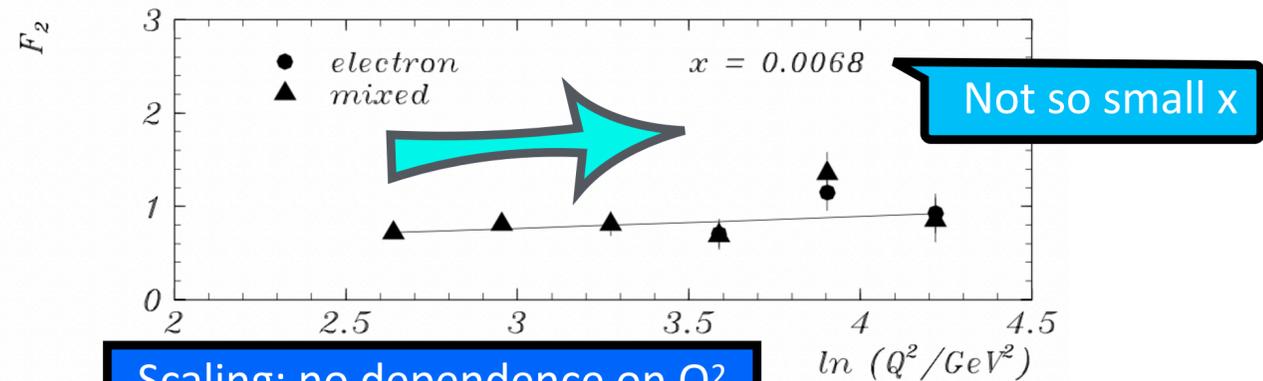
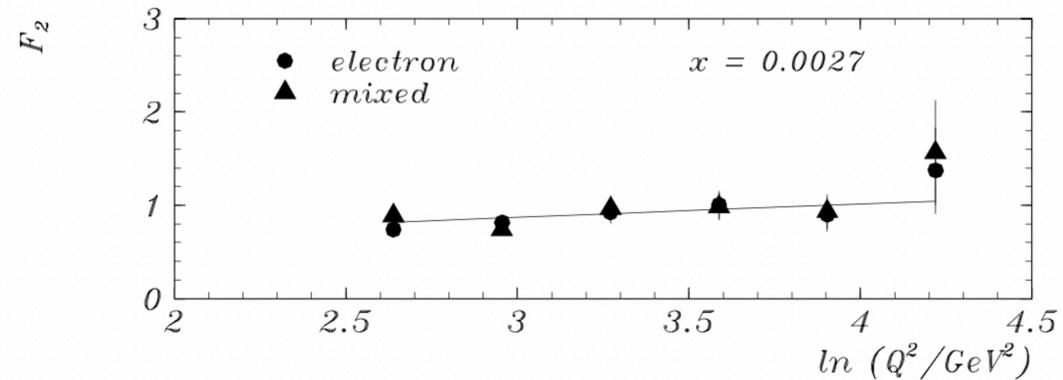
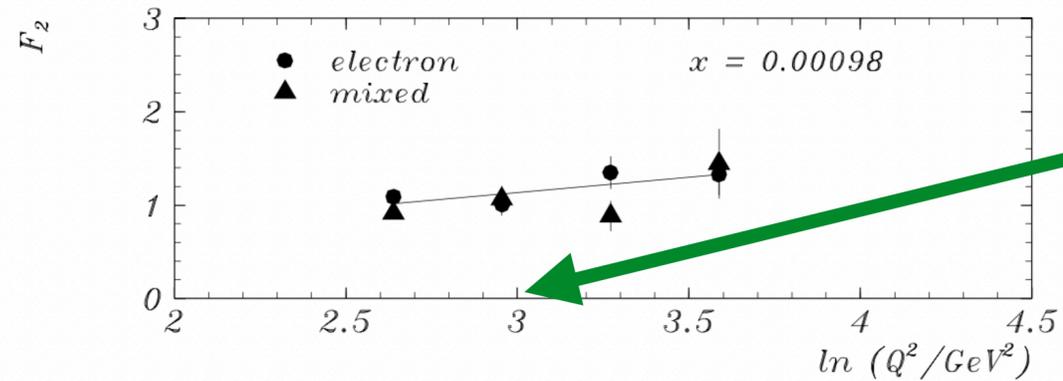
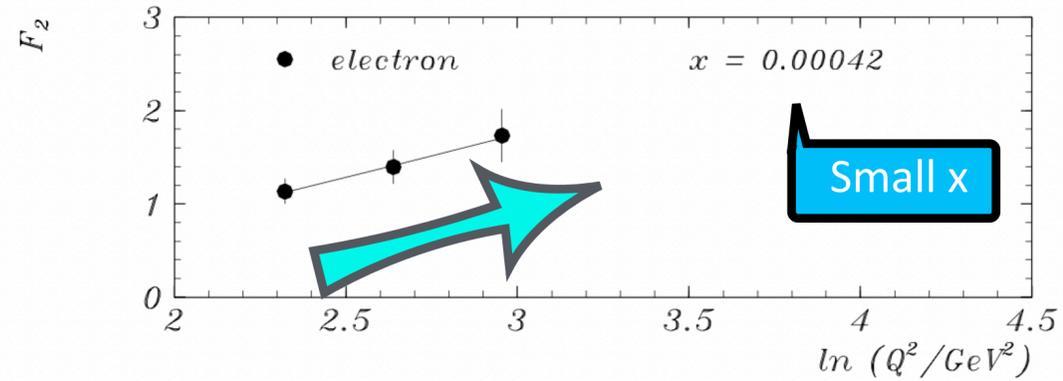
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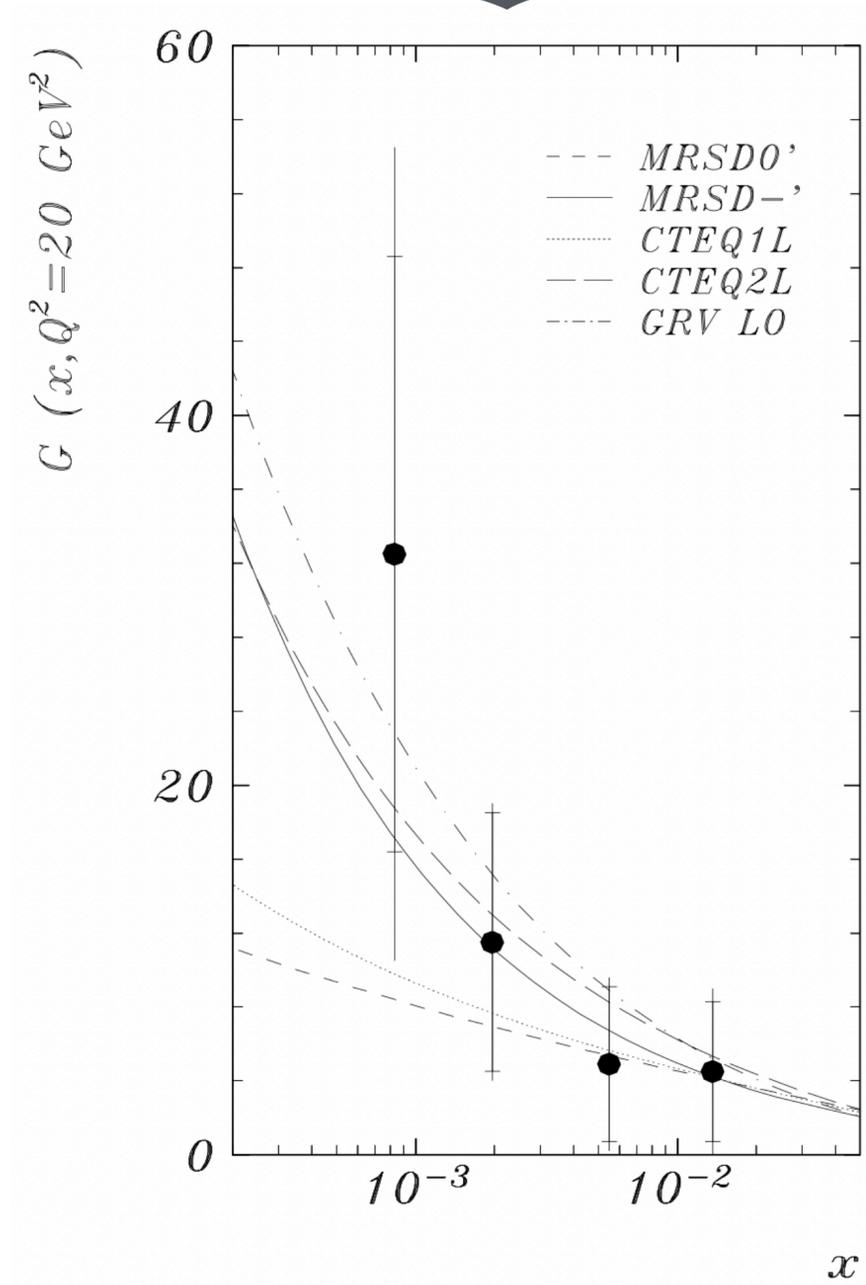
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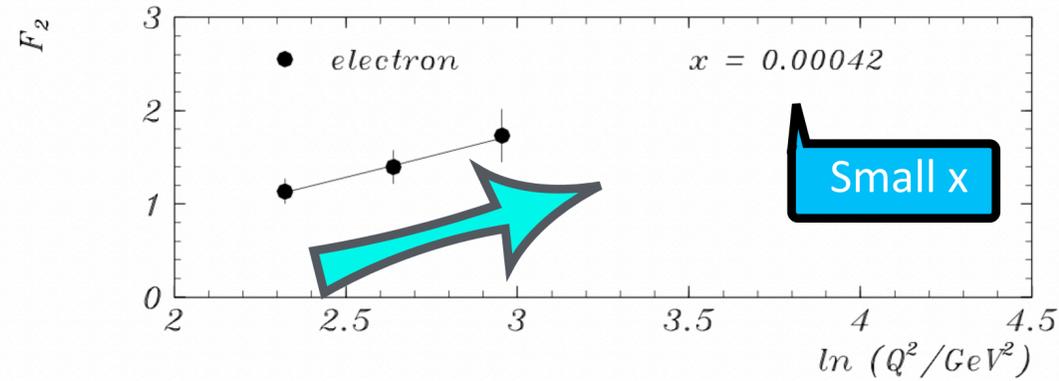


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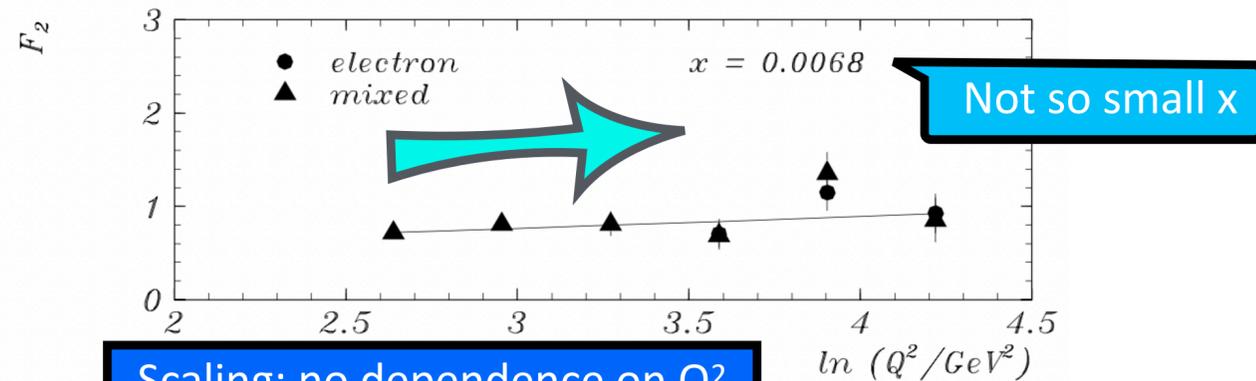
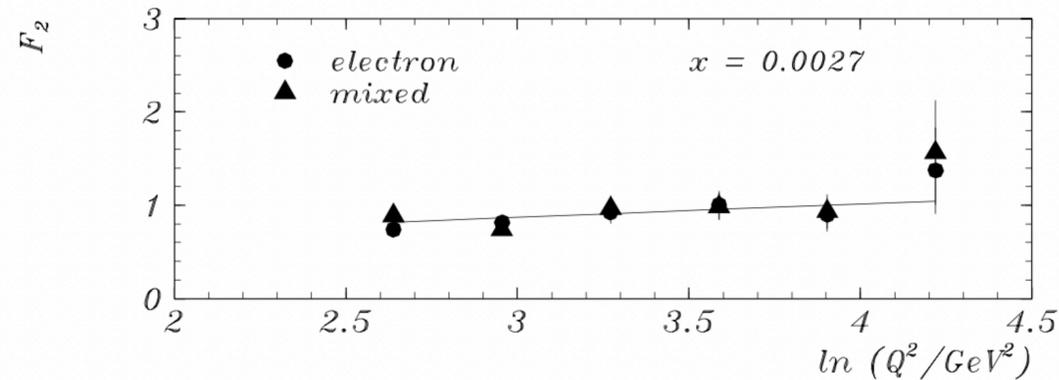
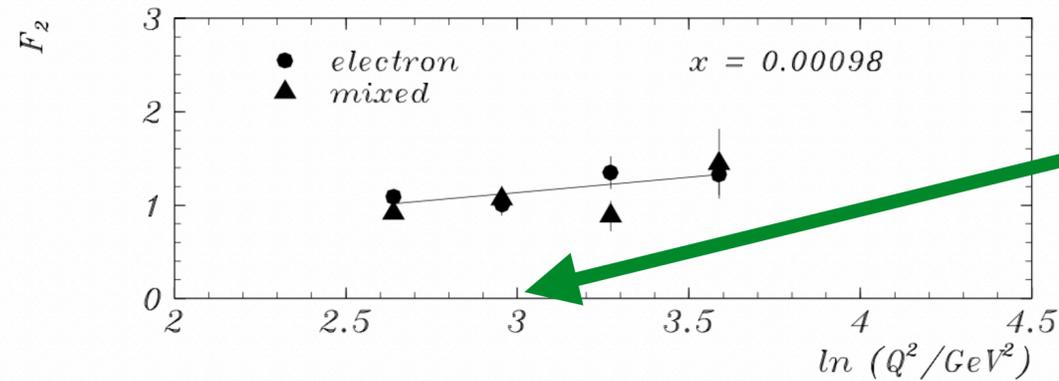
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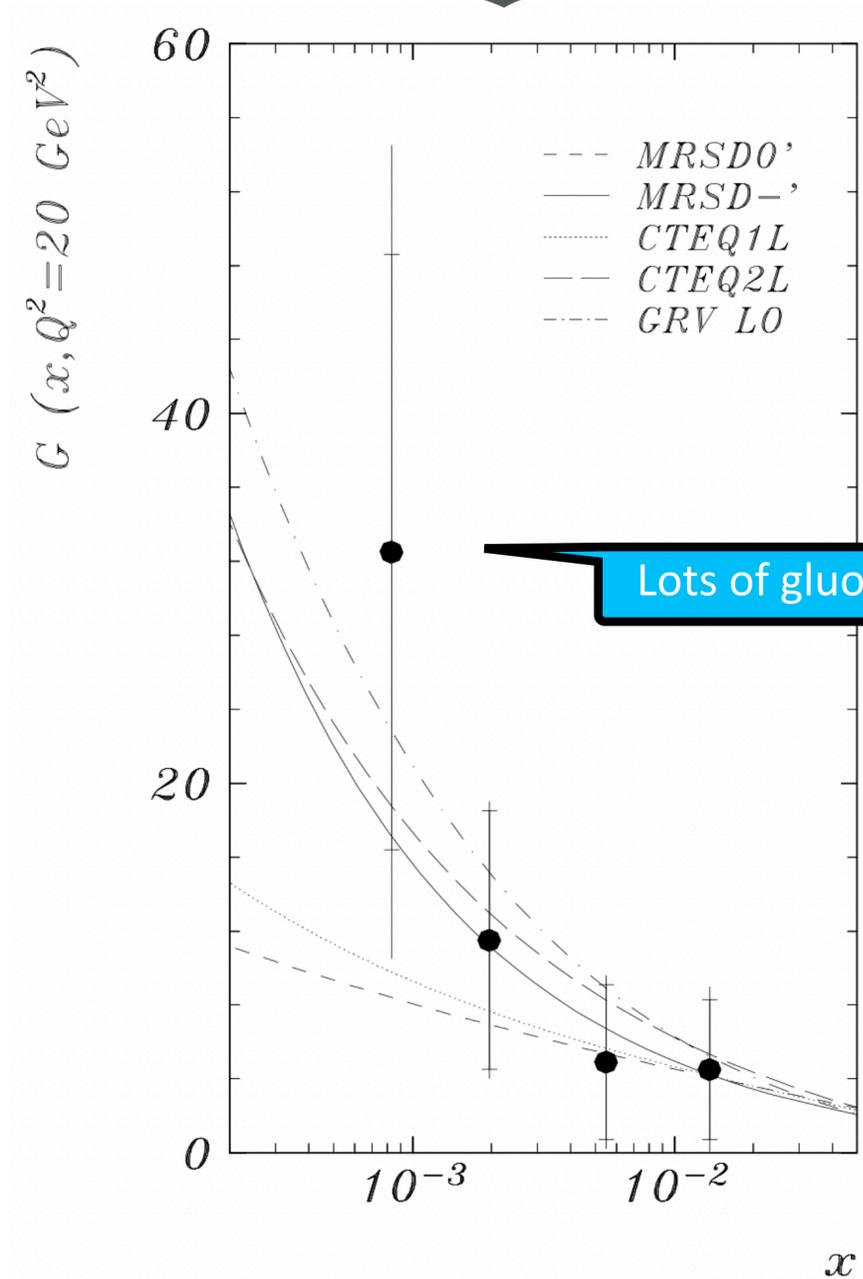


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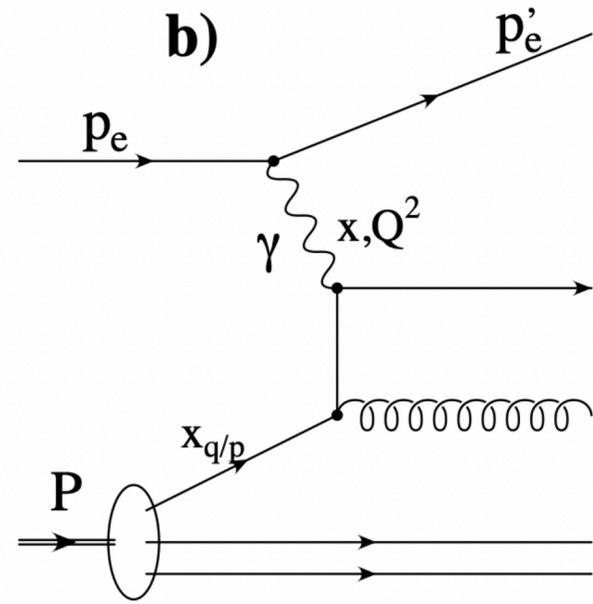
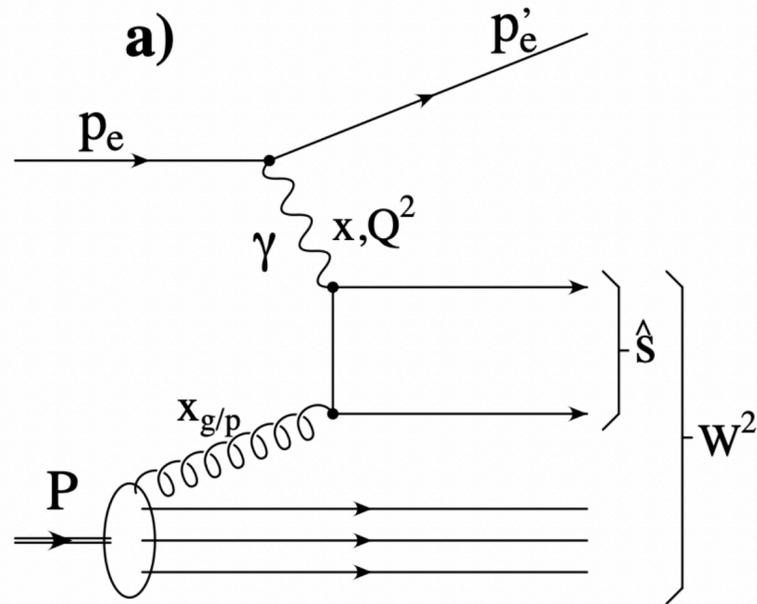
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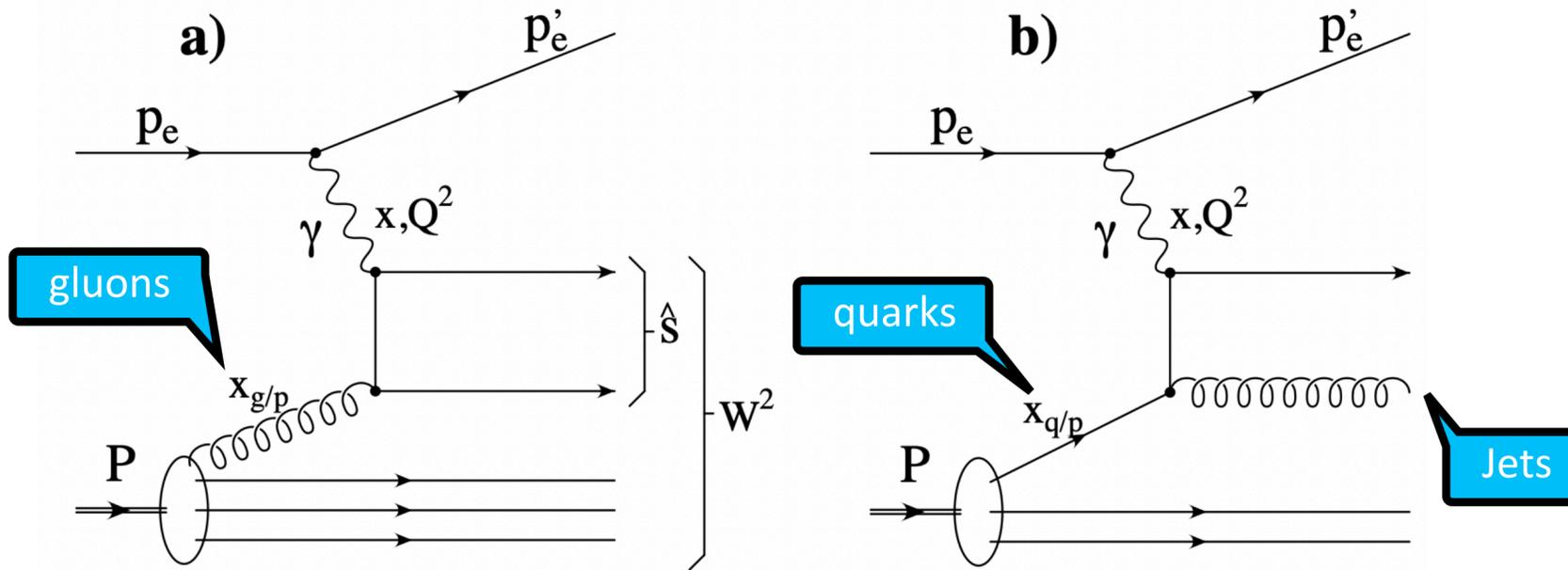
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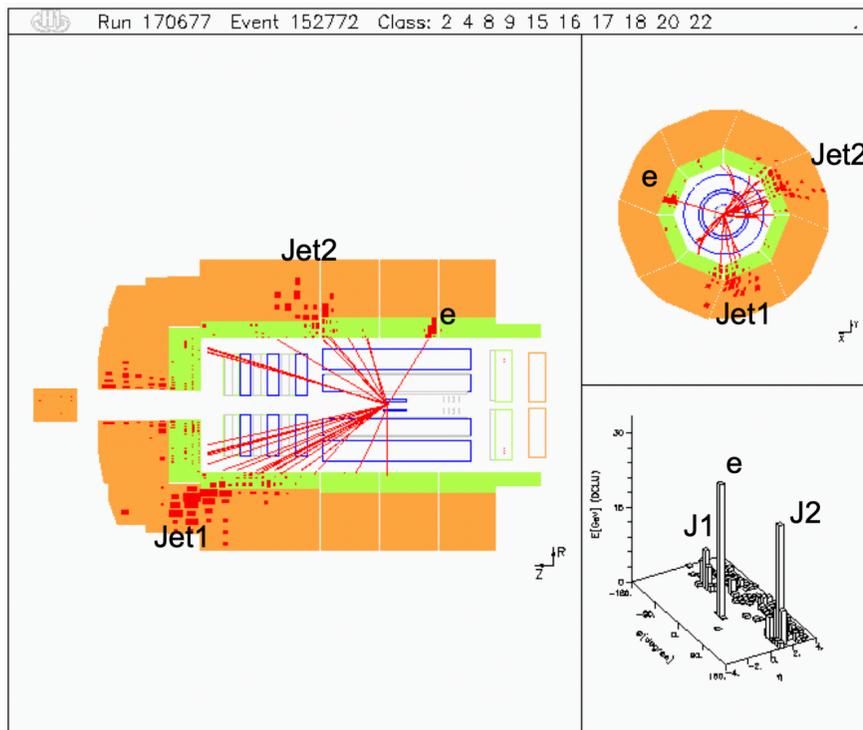
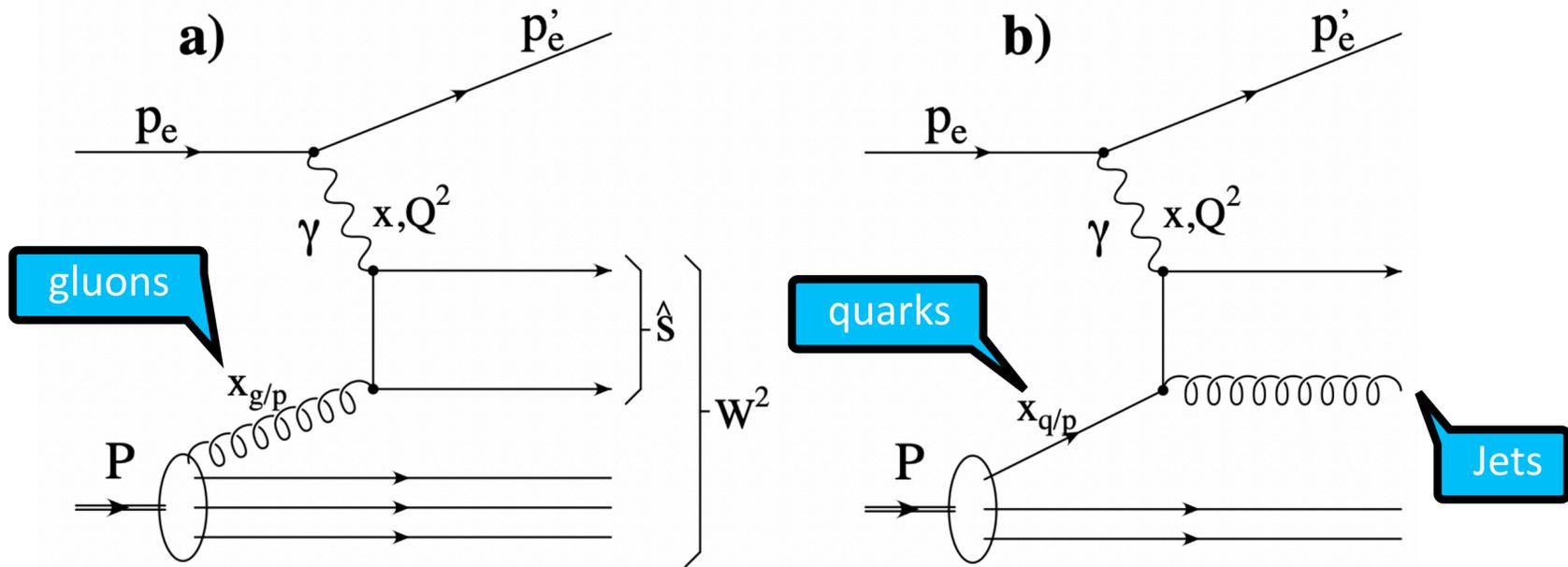
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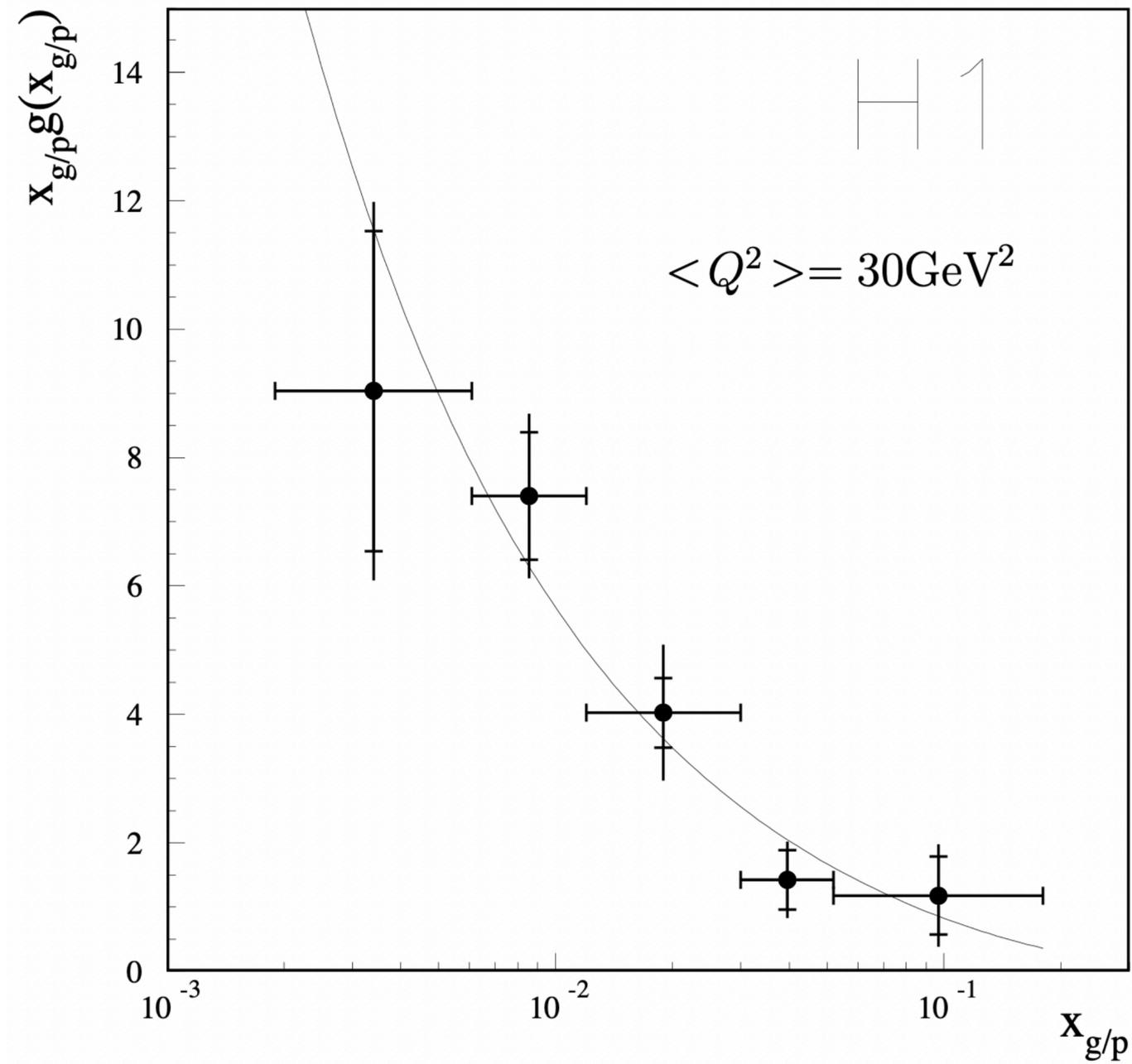
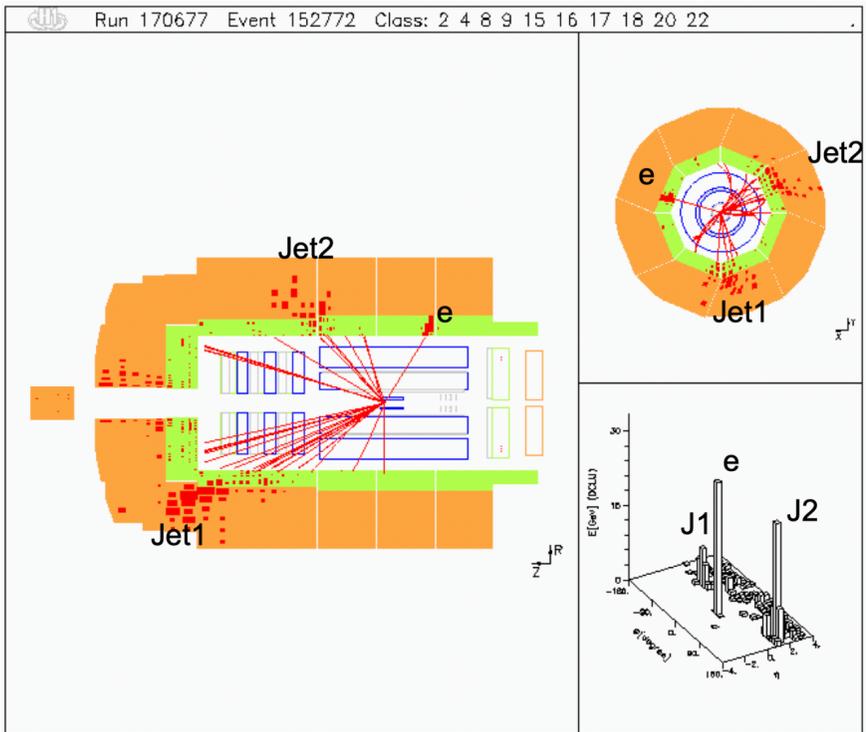
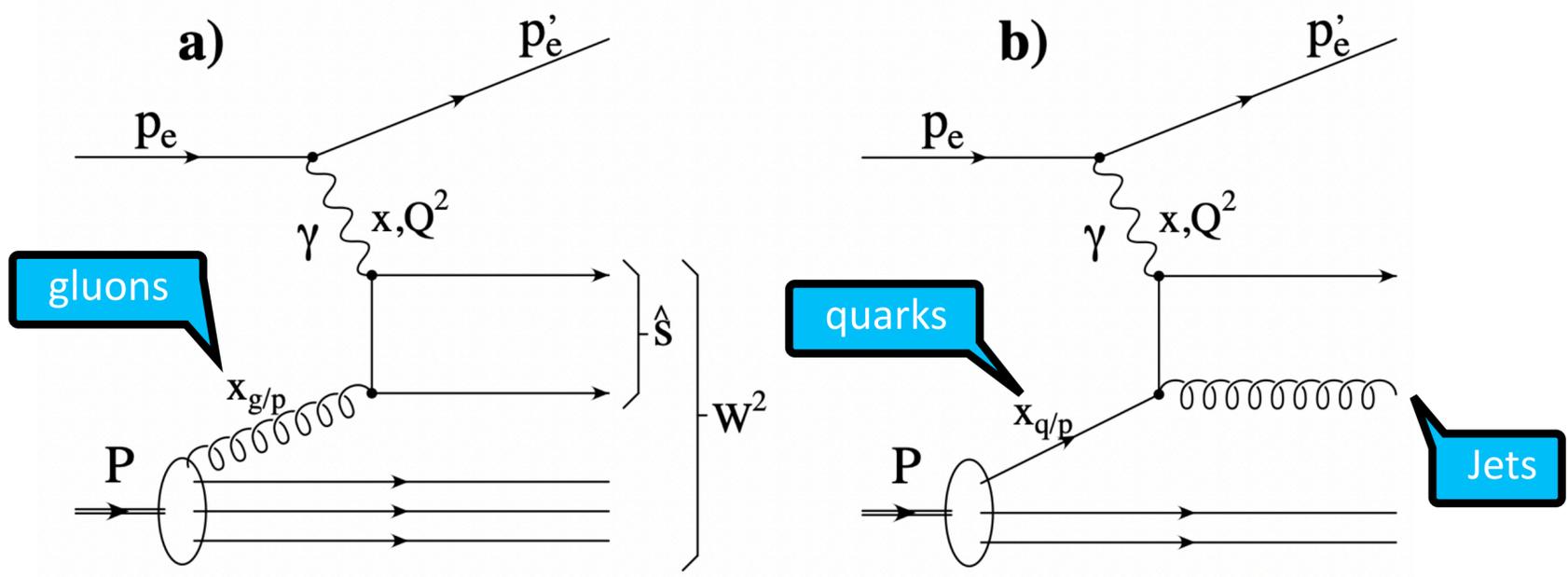
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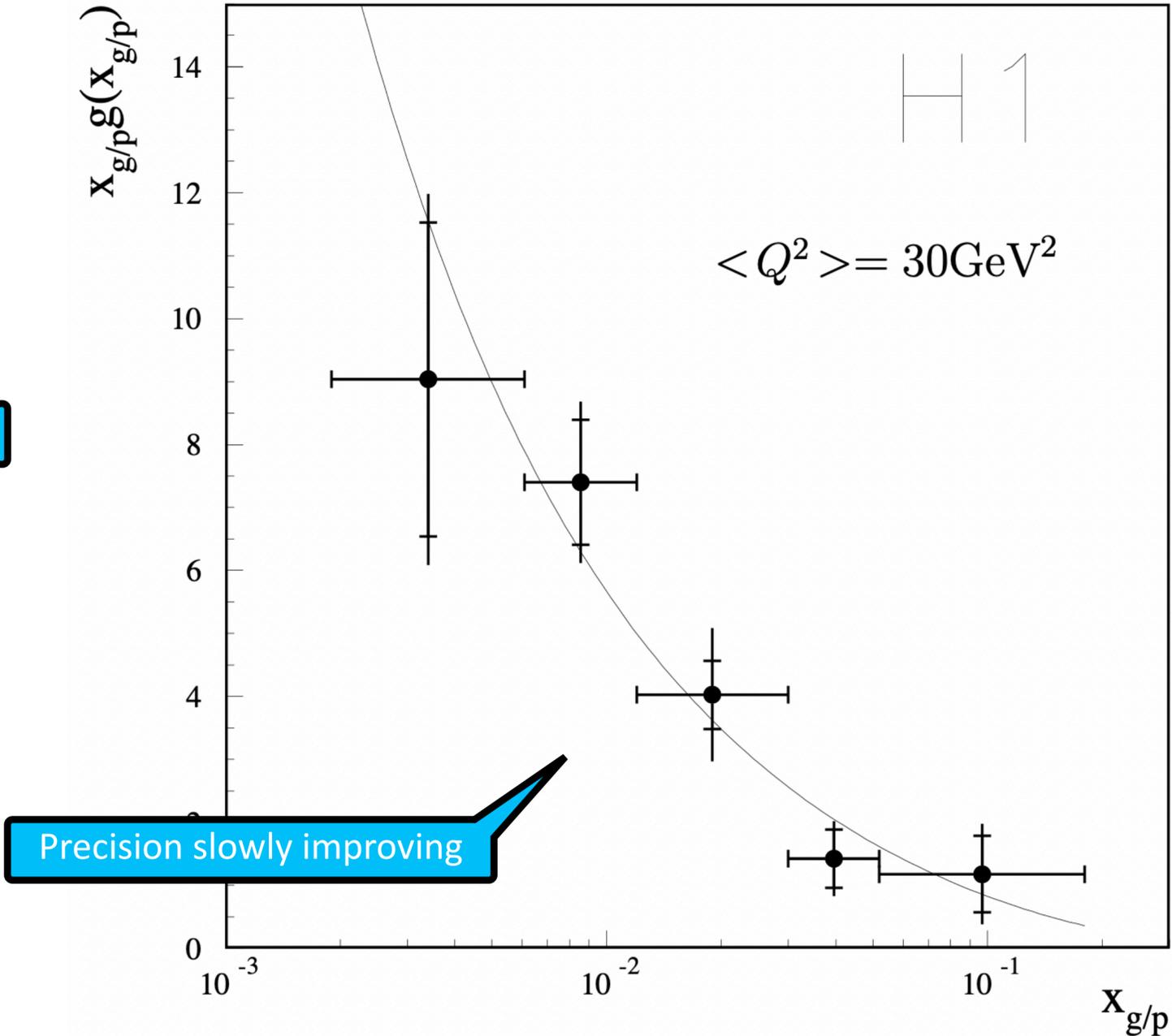
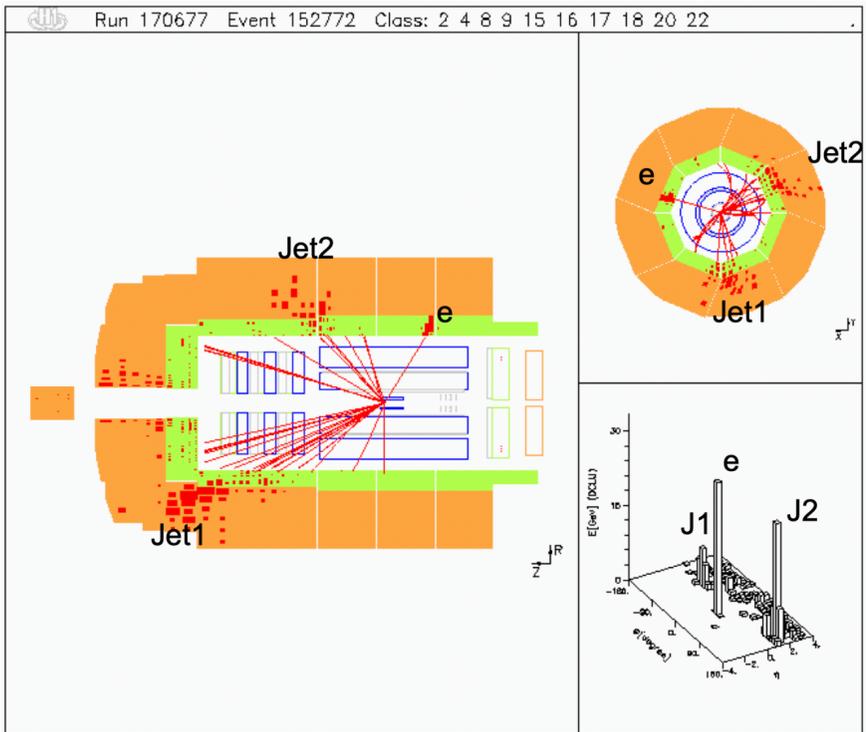
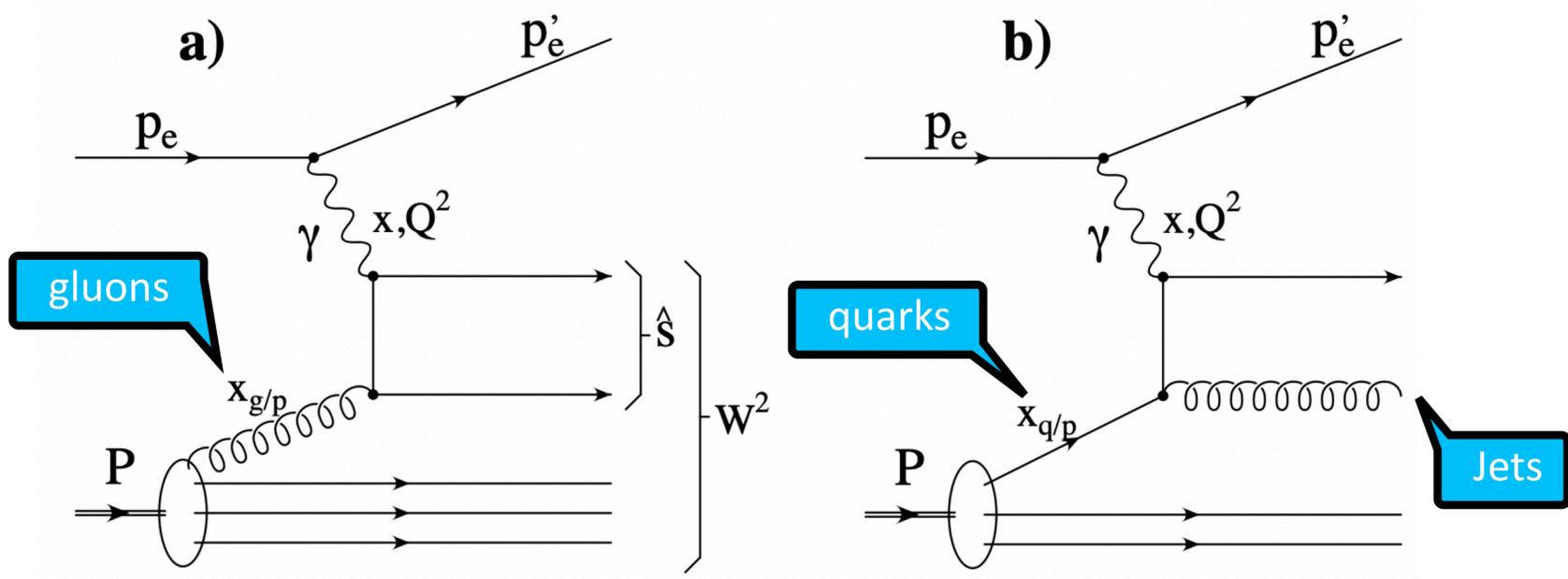
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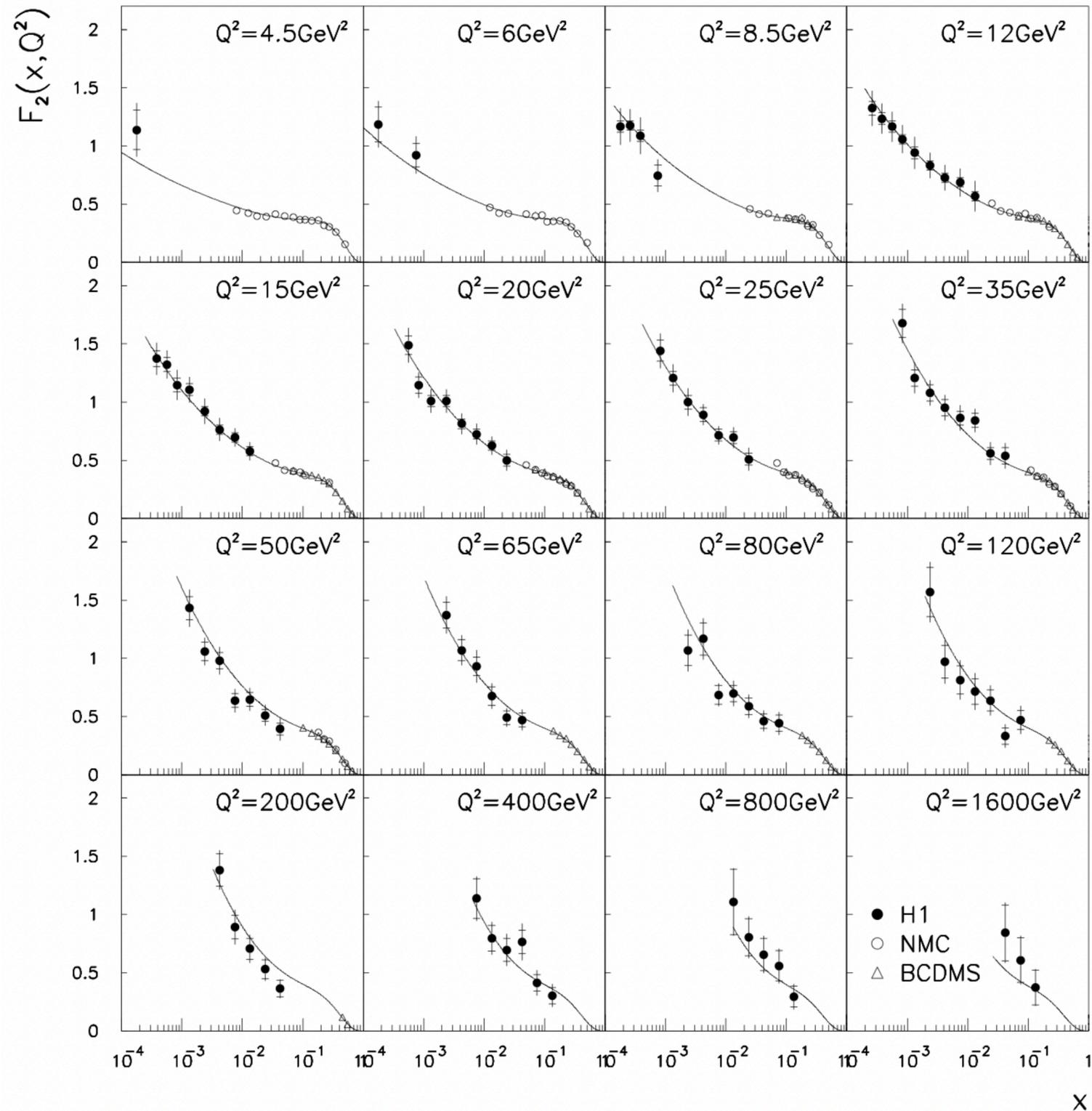
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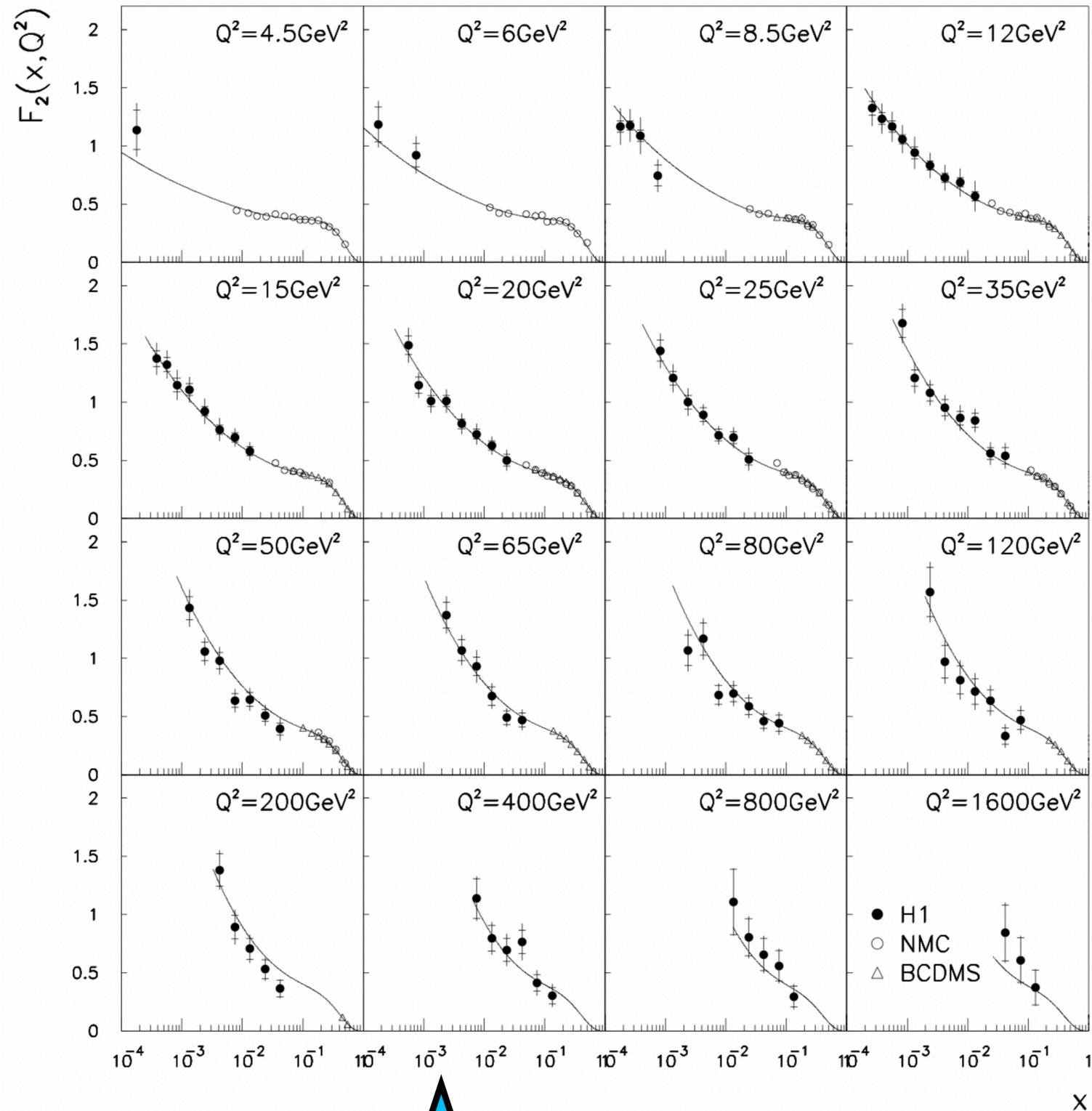
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x

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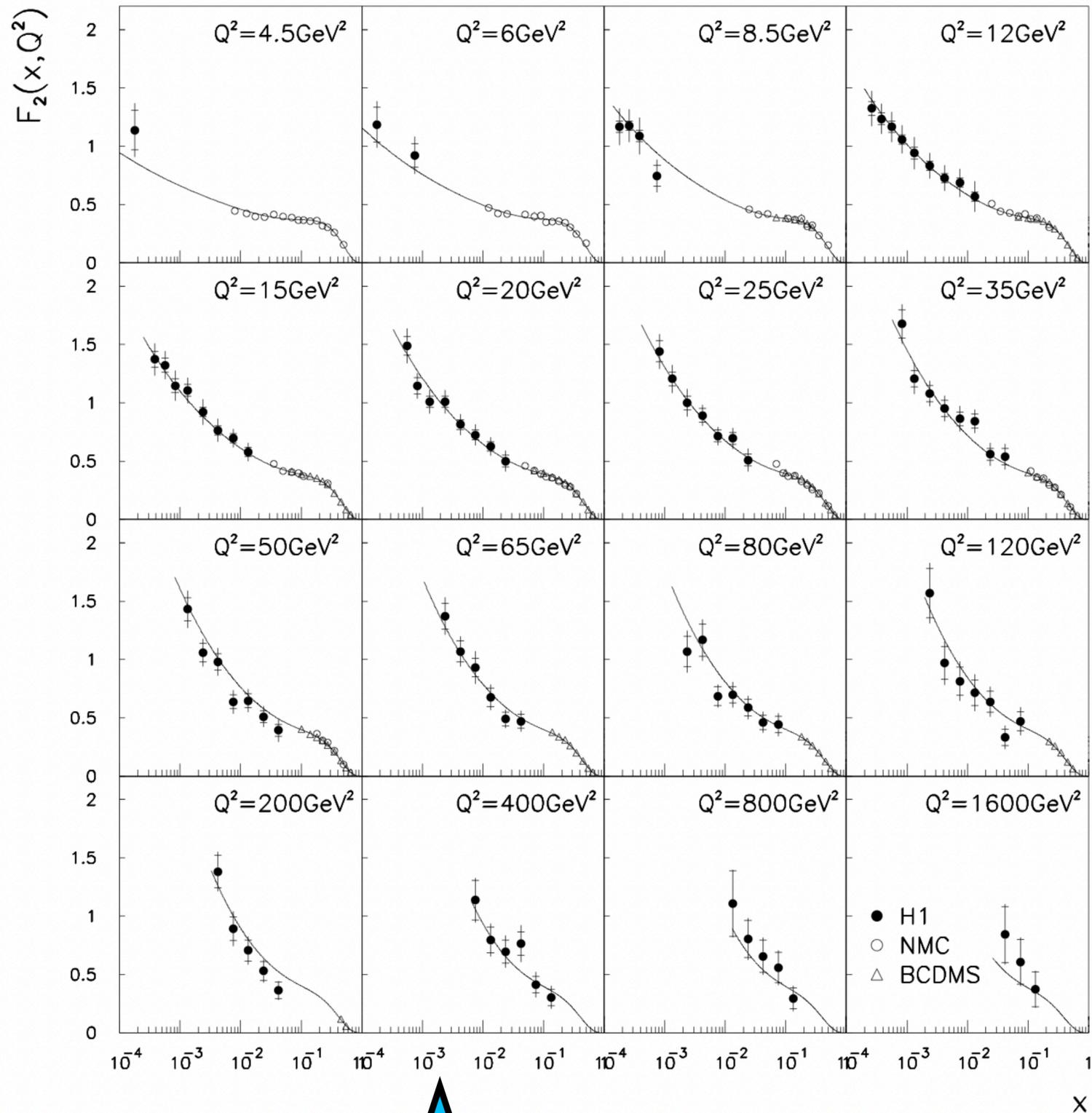
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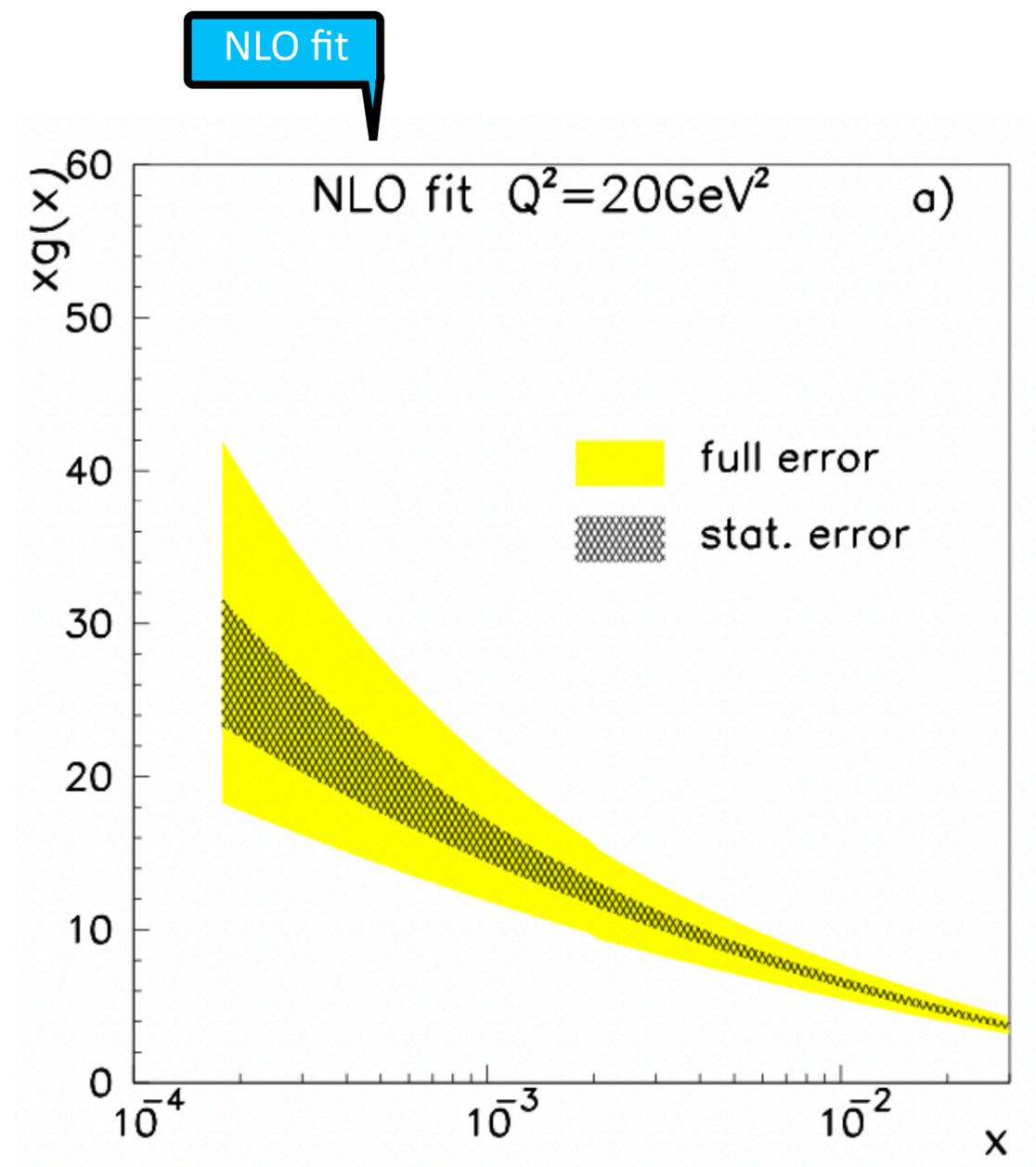
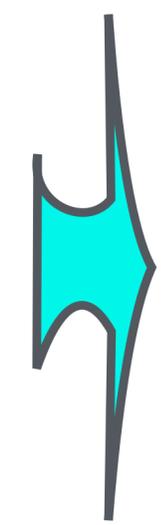
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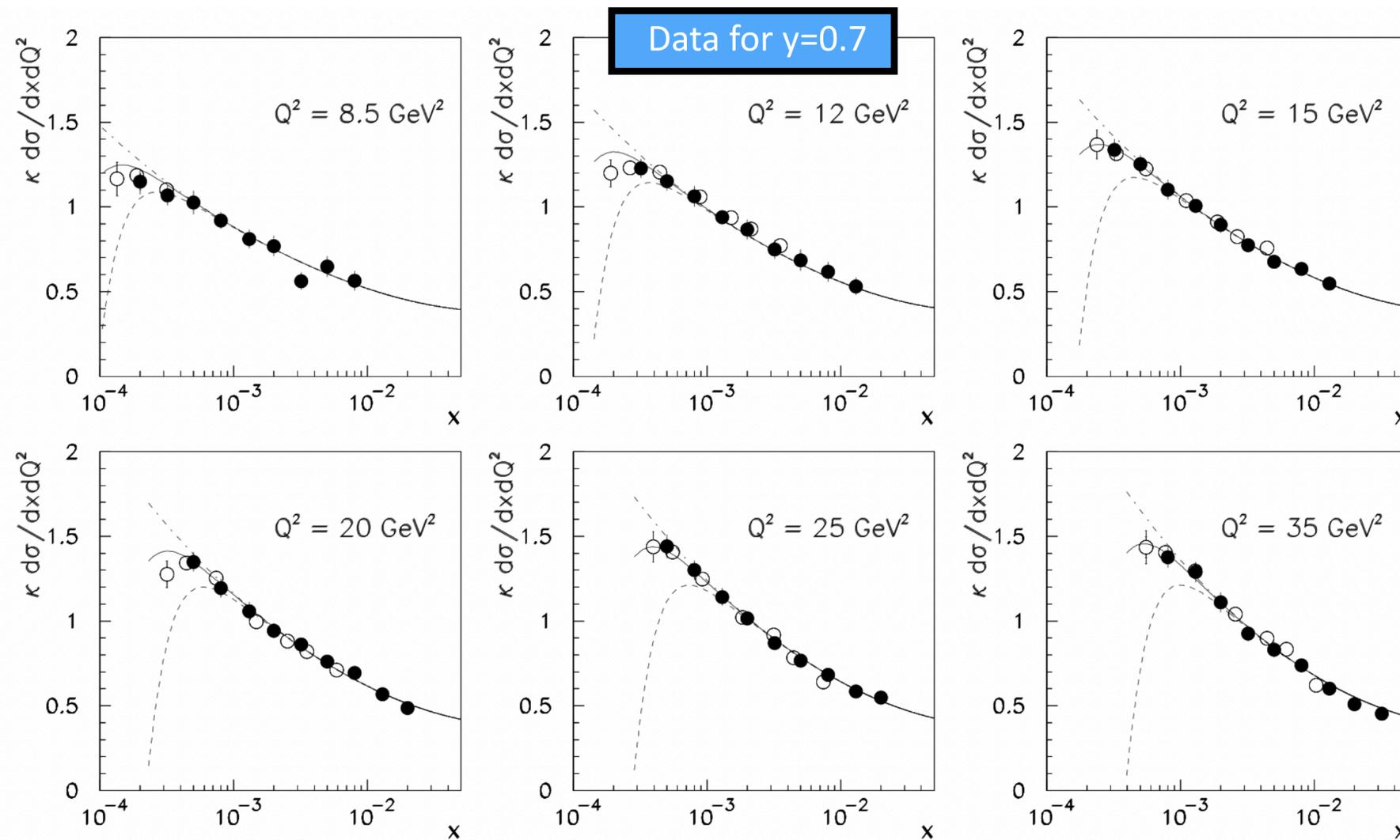
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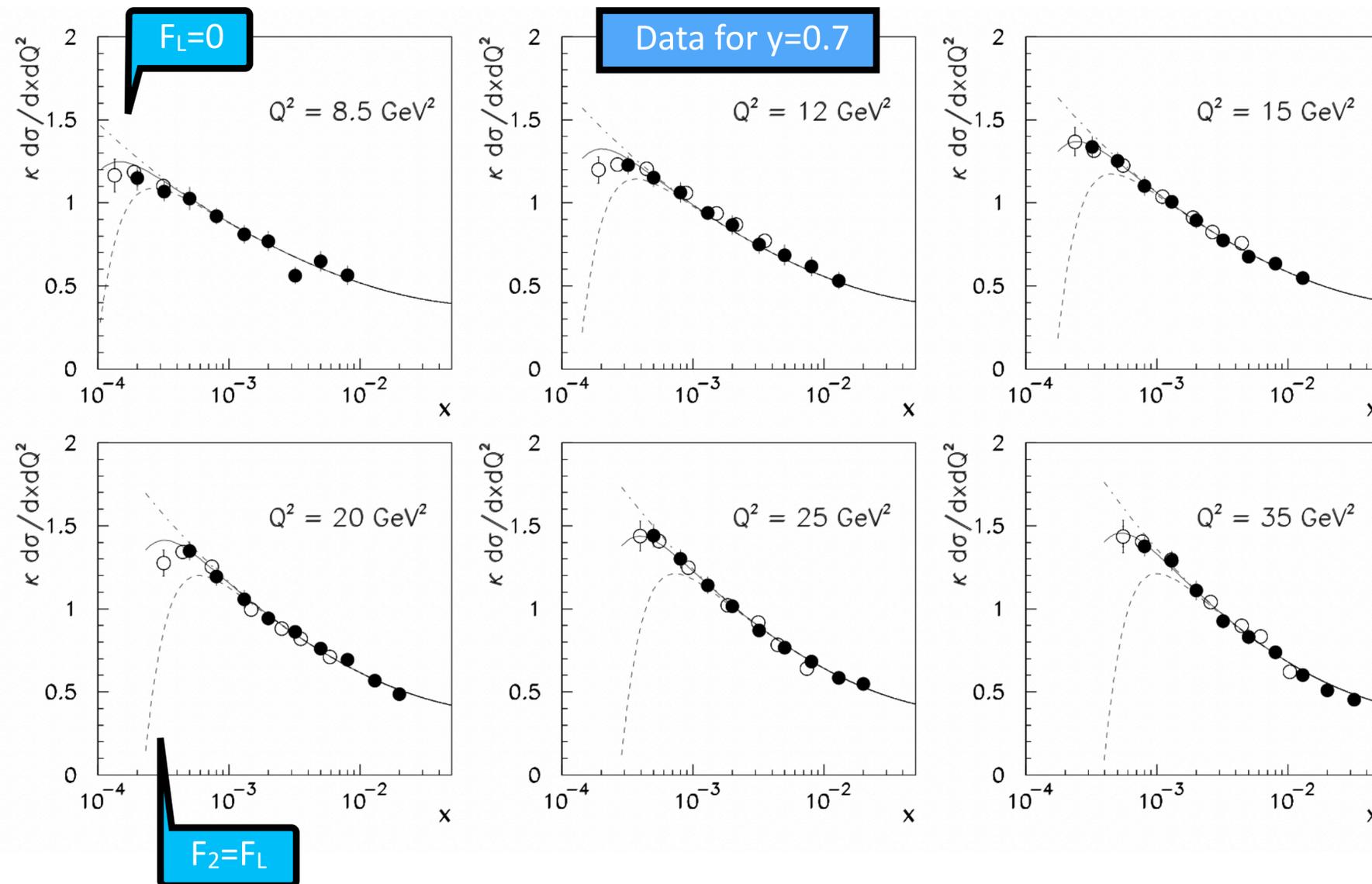


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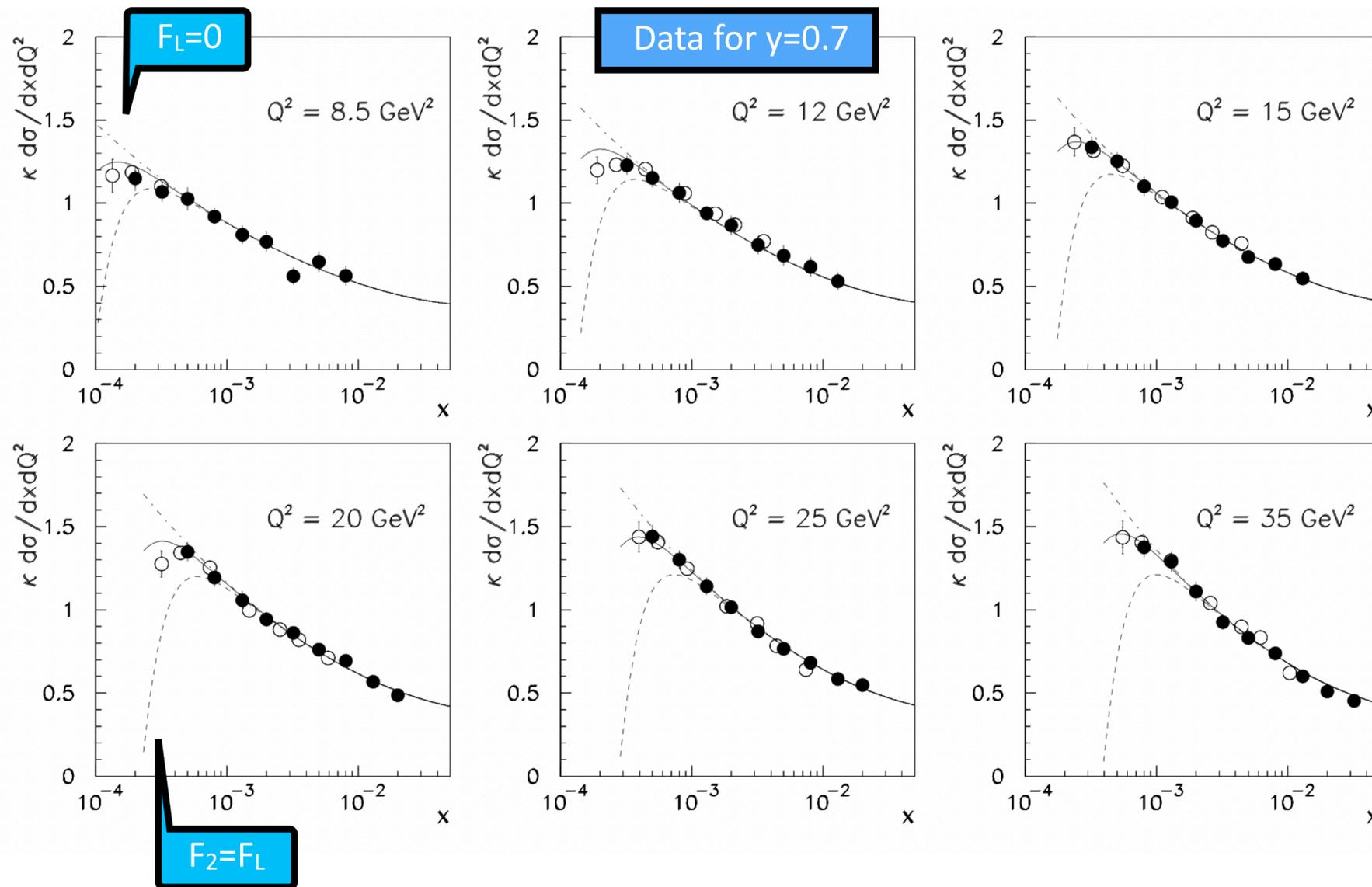


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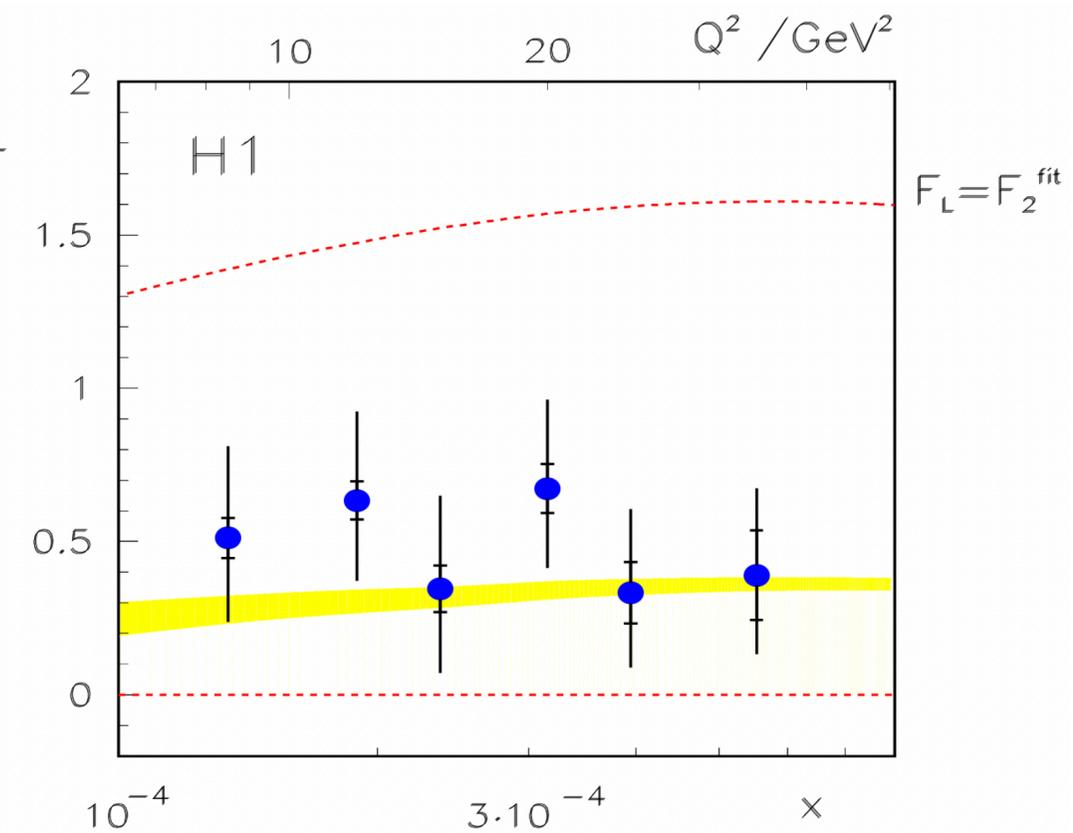
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Measure  $F_2$  at low  $y$ , use fits to get it at  $y=0.7$  and get  $F_L$

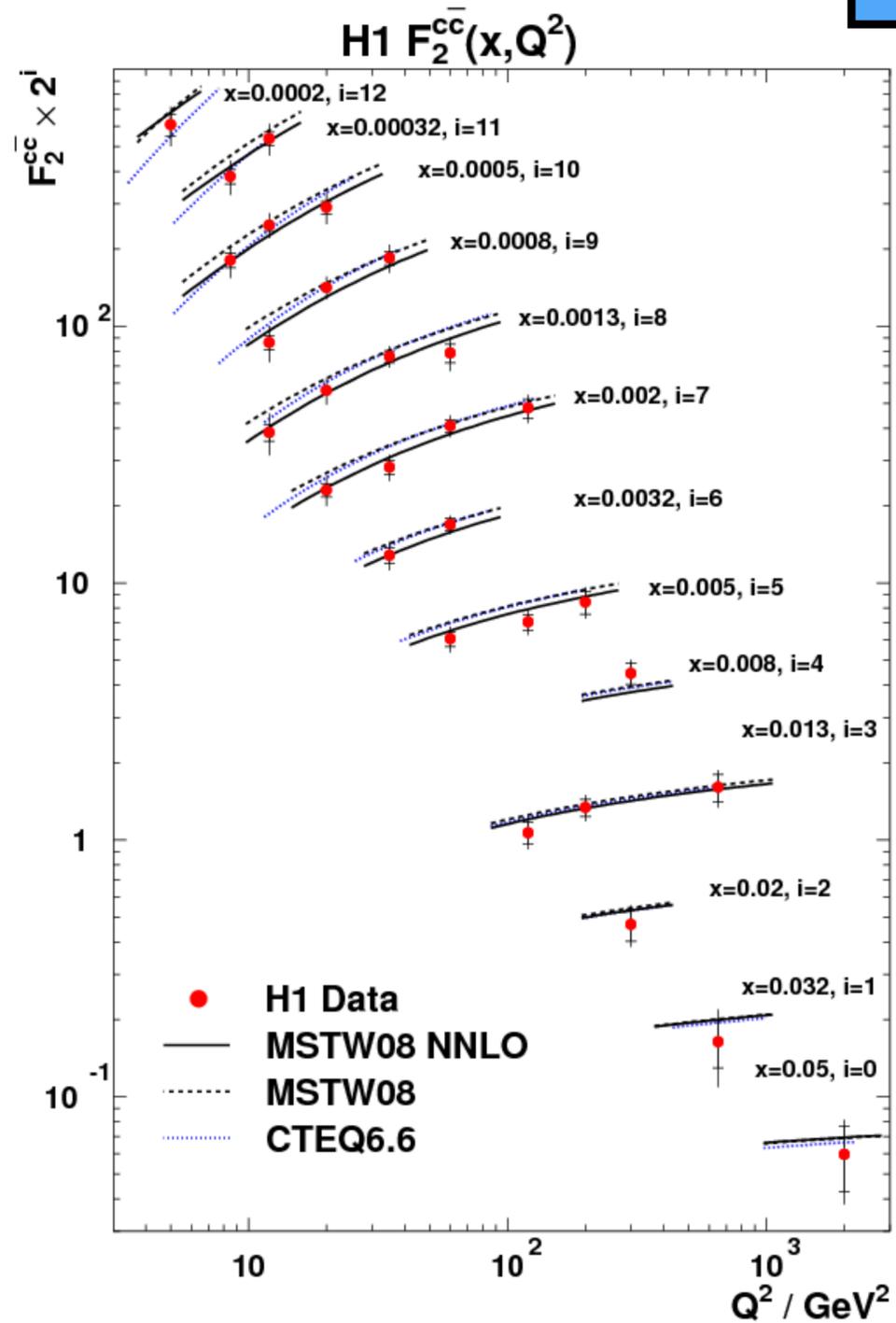


# Heavy-quark structure functions (2010)

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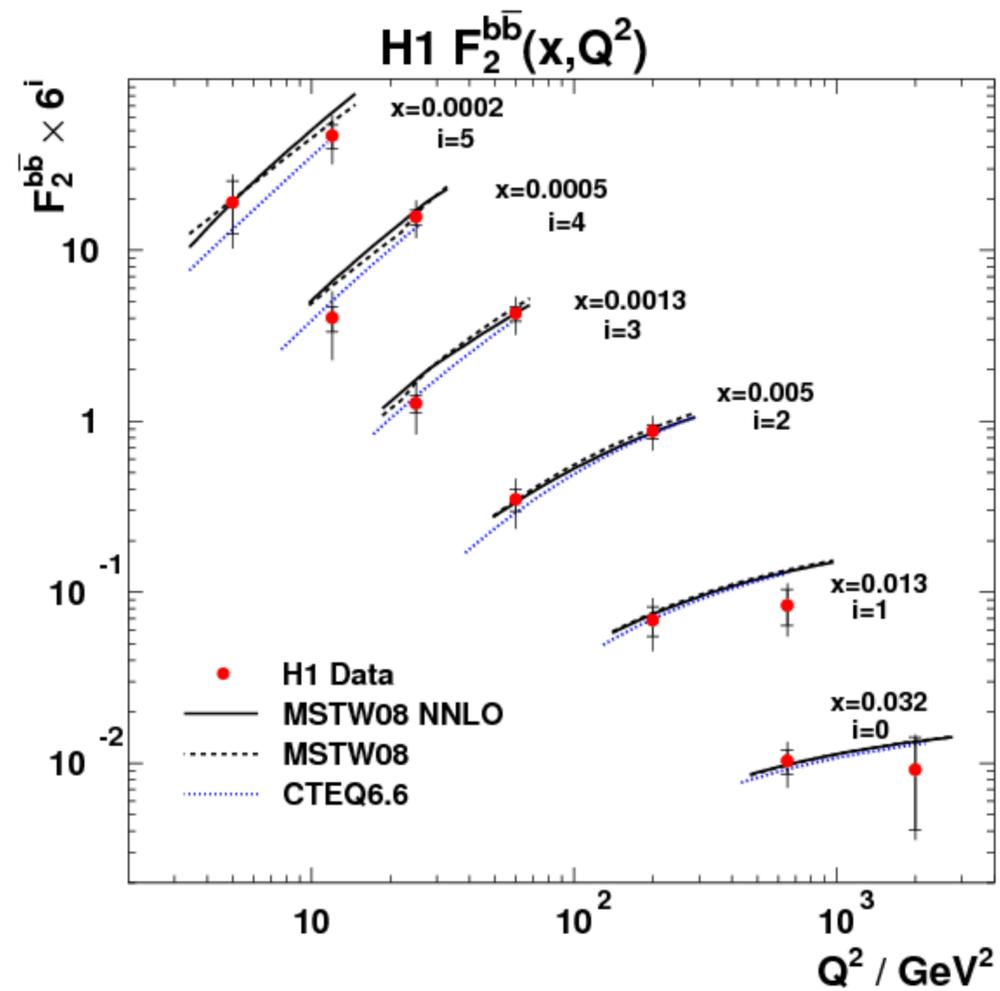
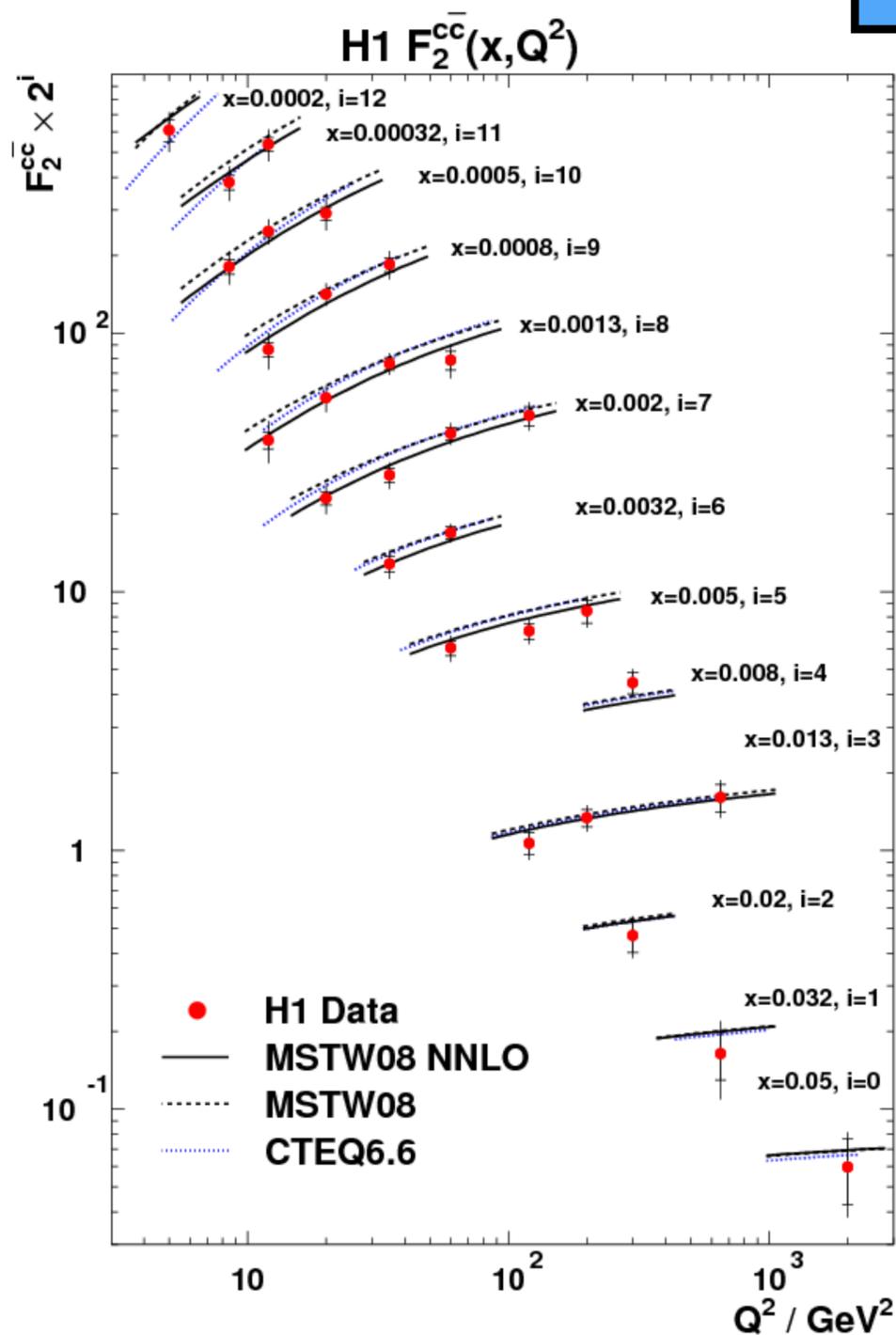
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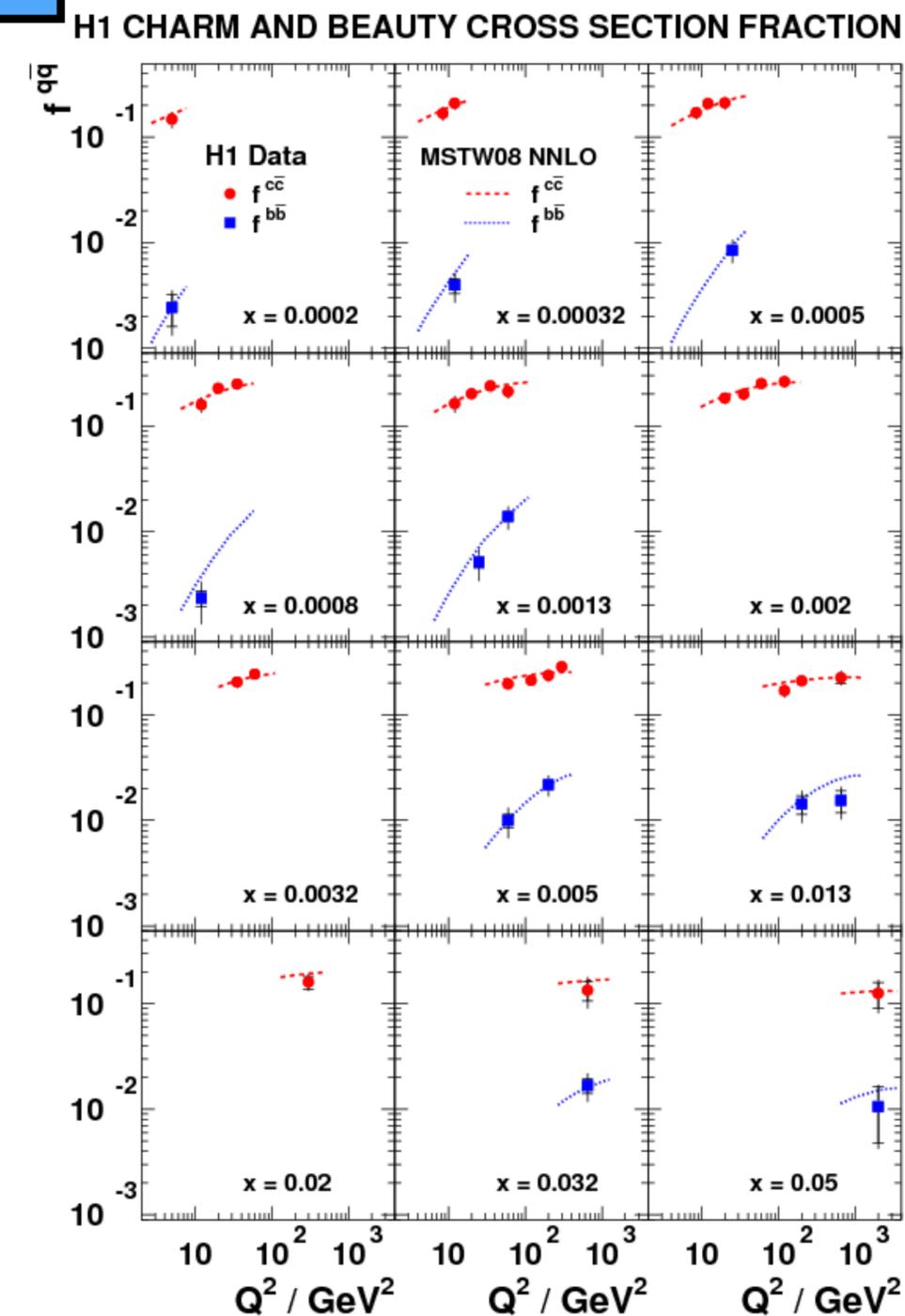
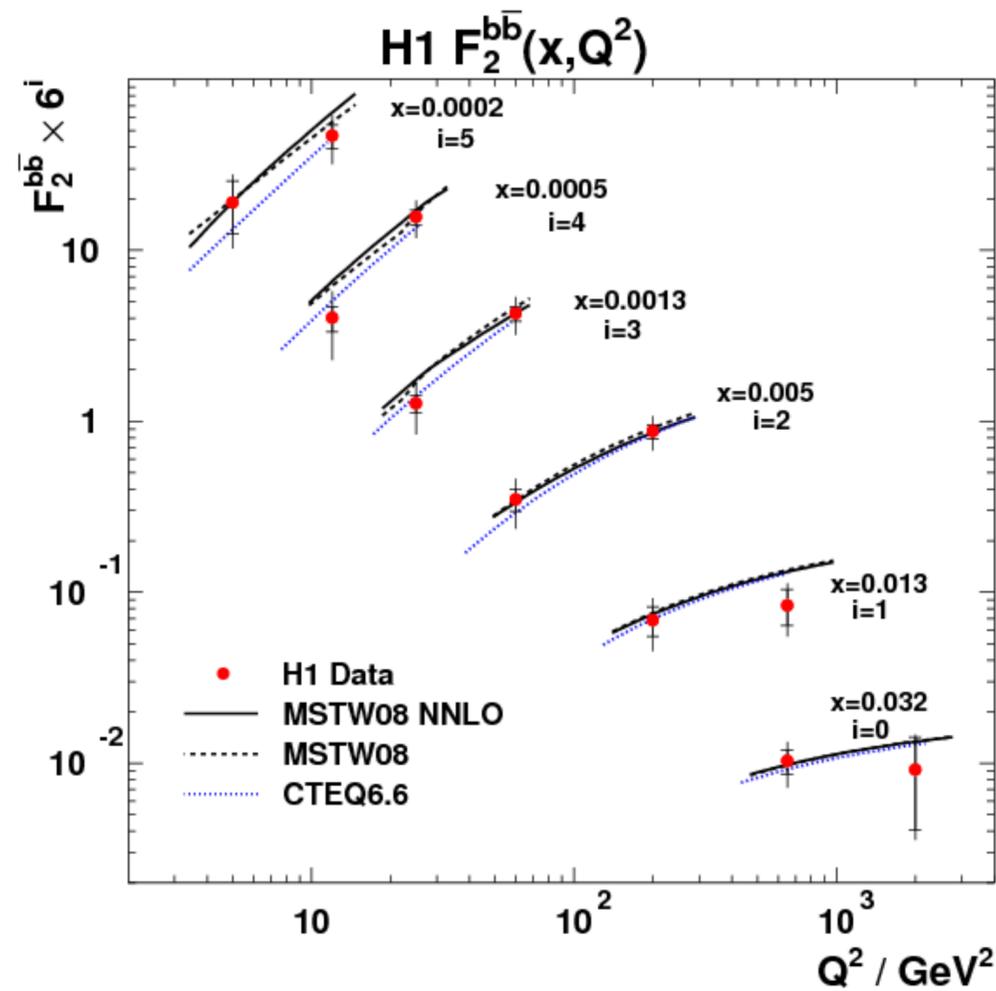
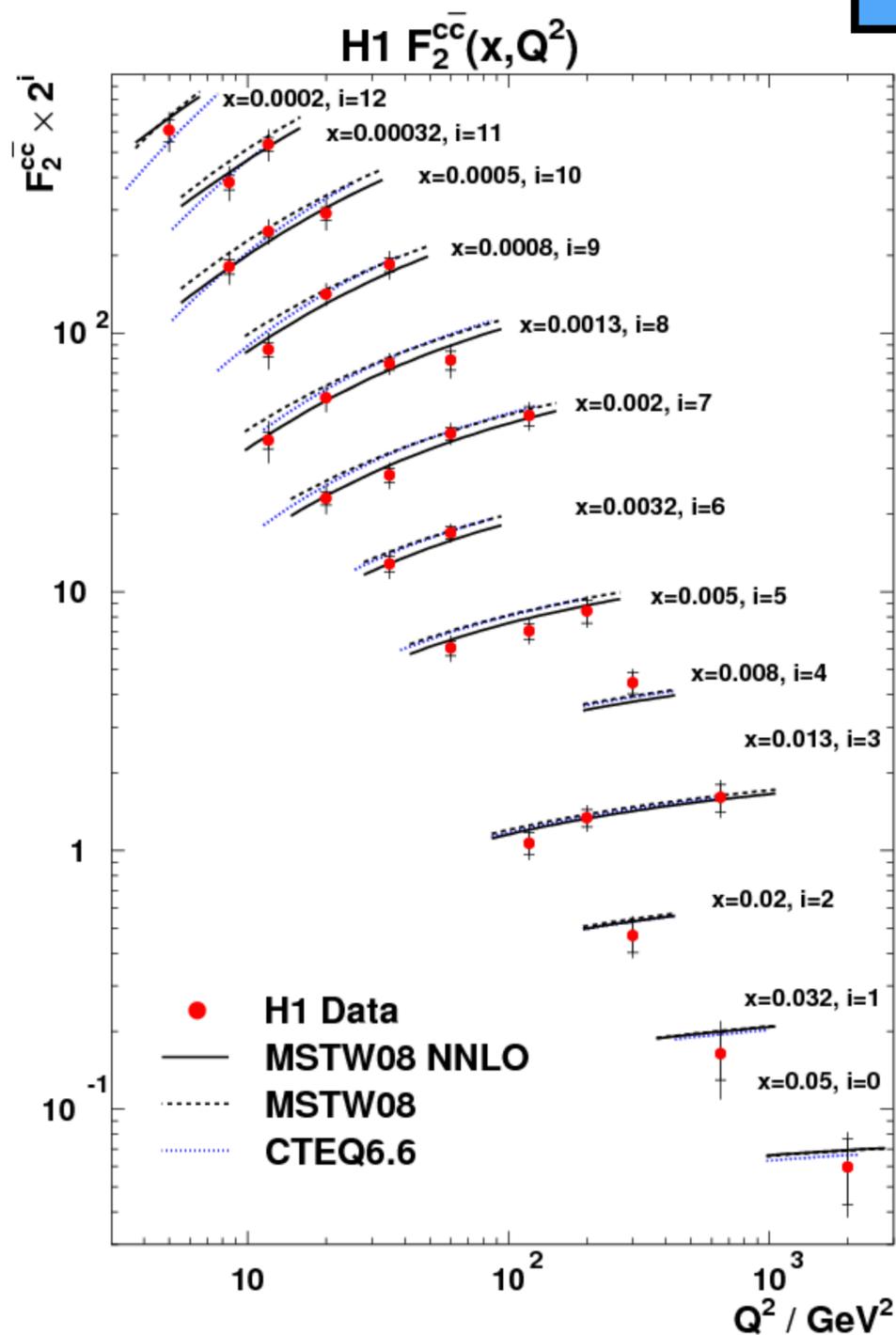
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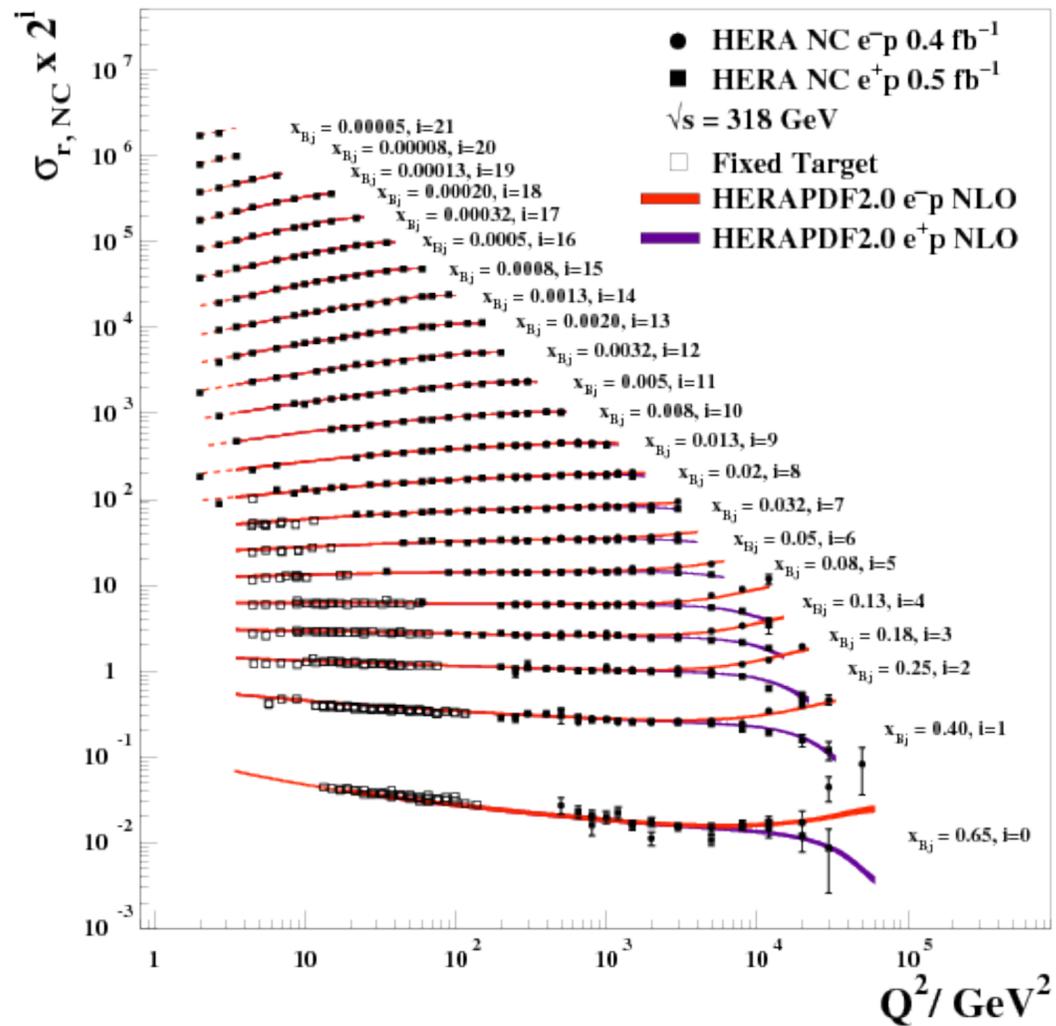
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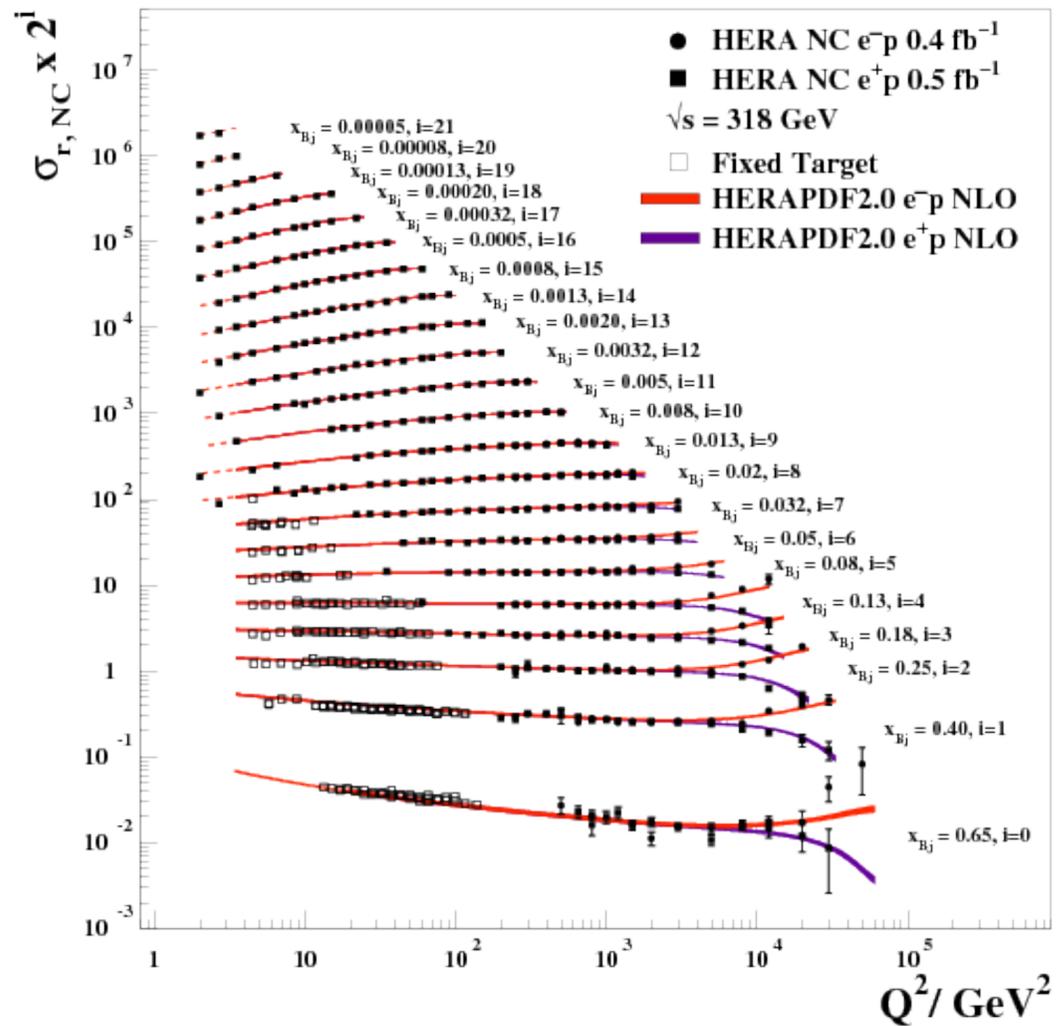
## H1 and ZEUS



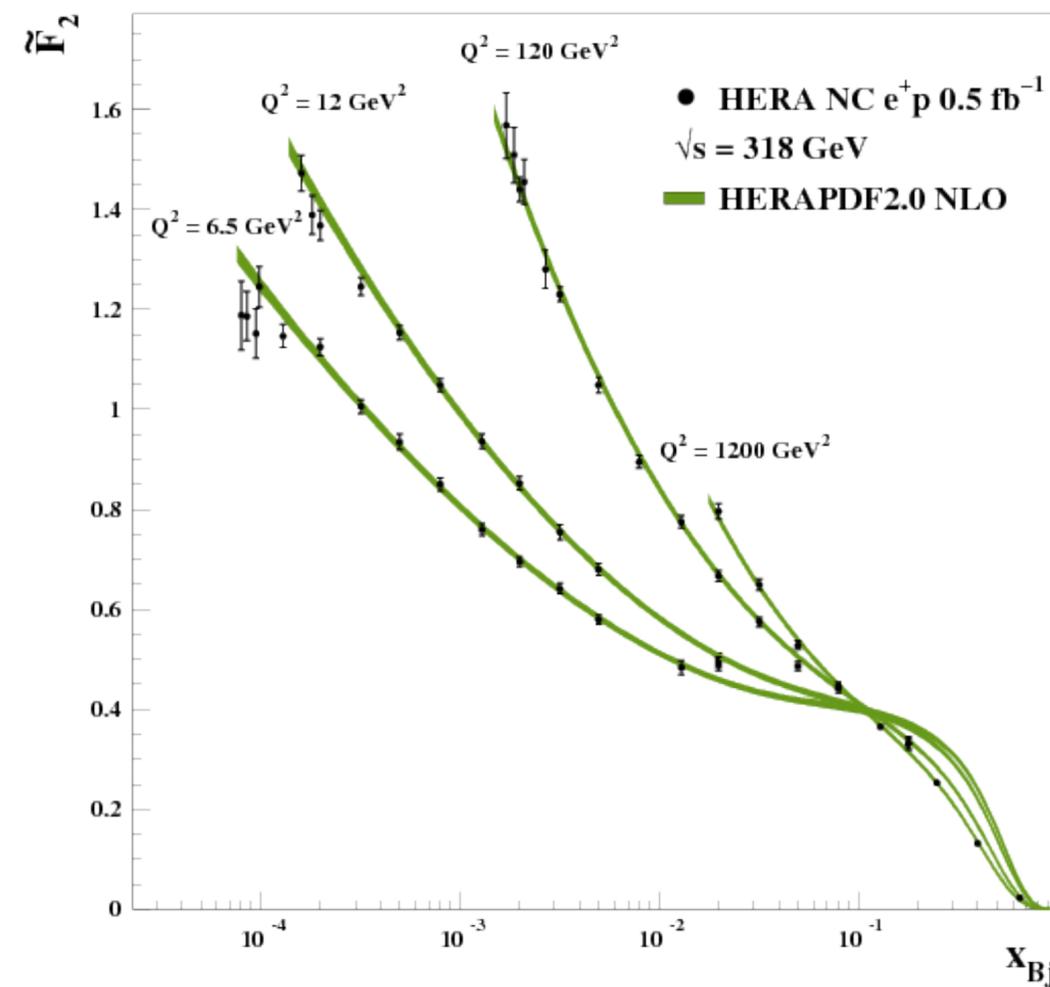
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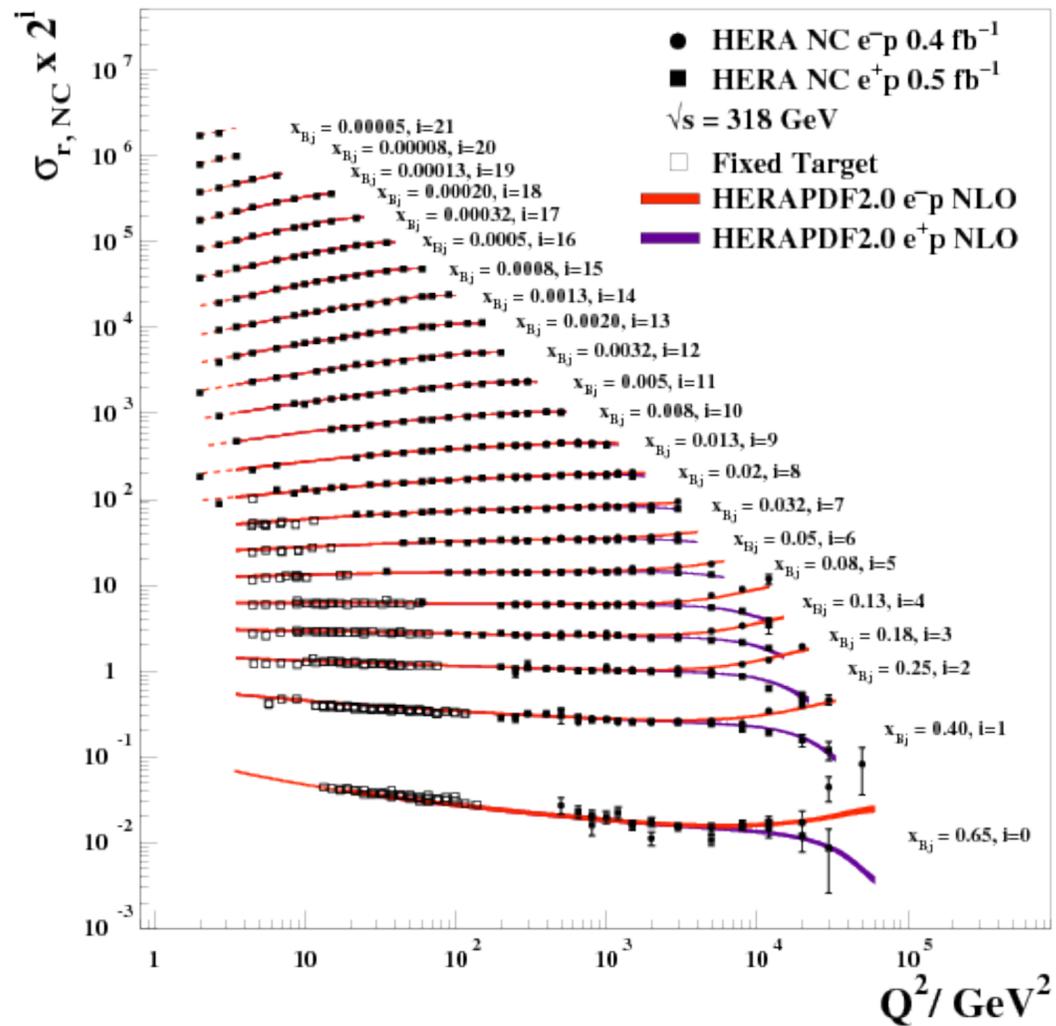
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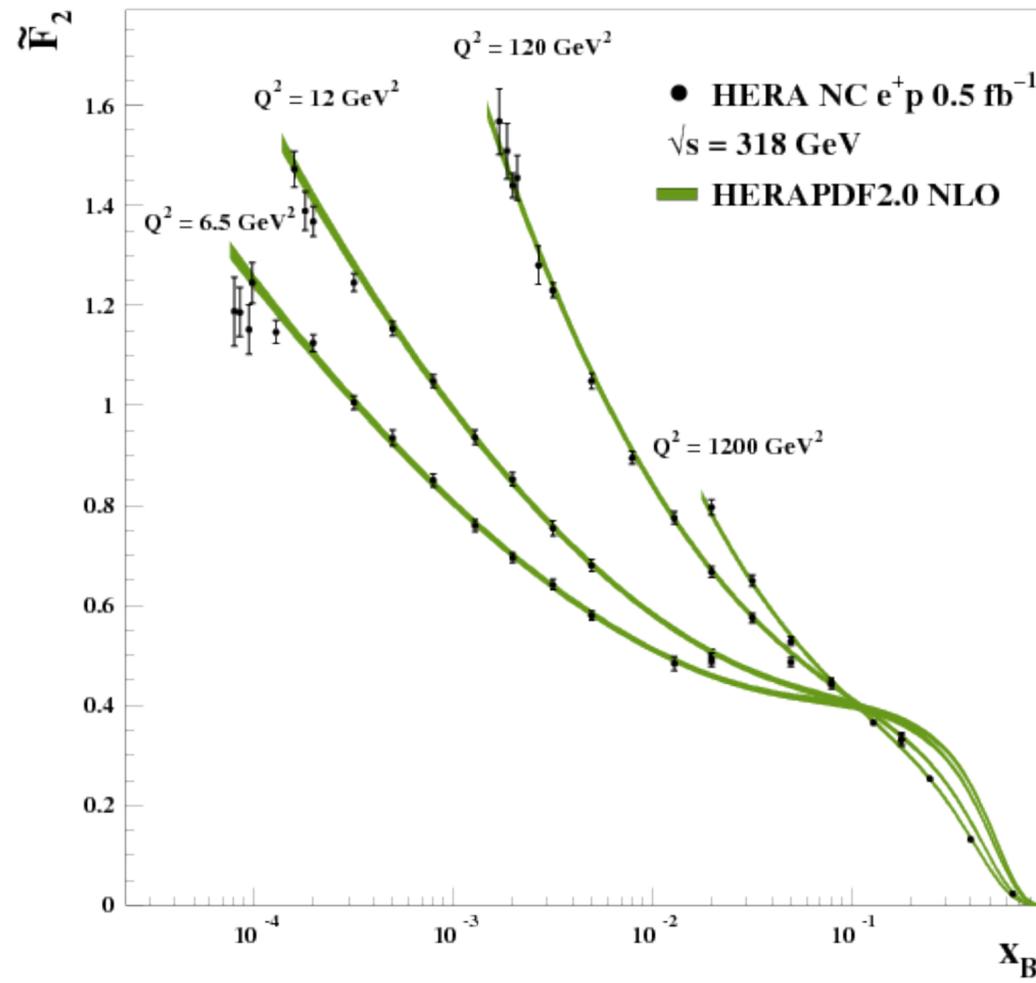
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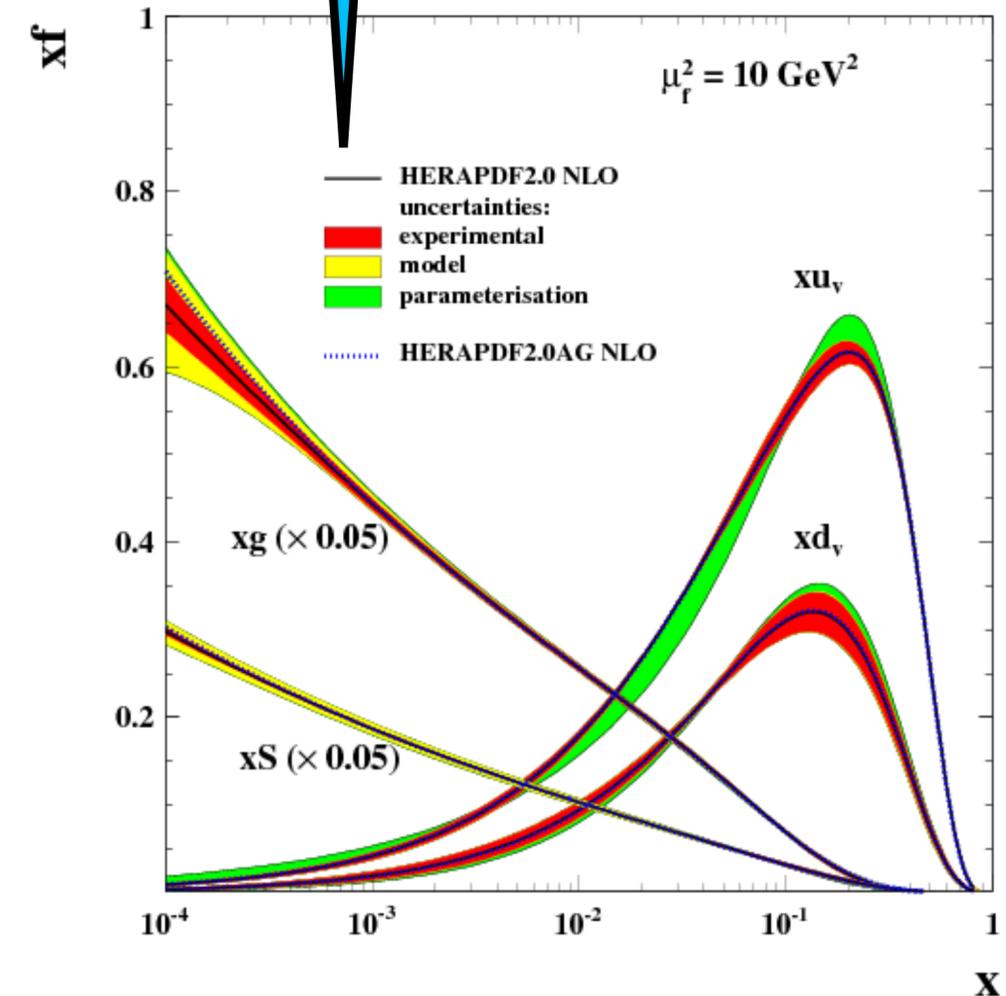


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There also are NNLO fits

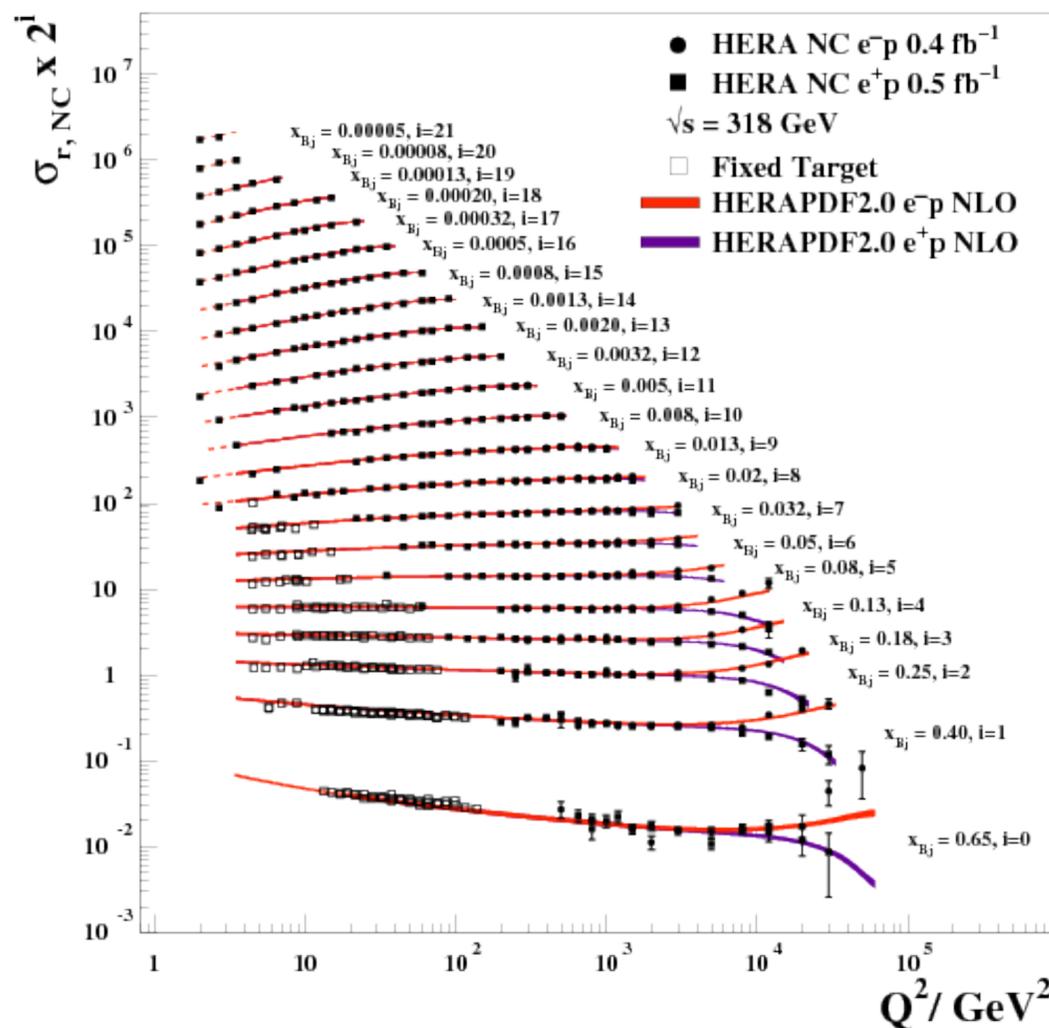
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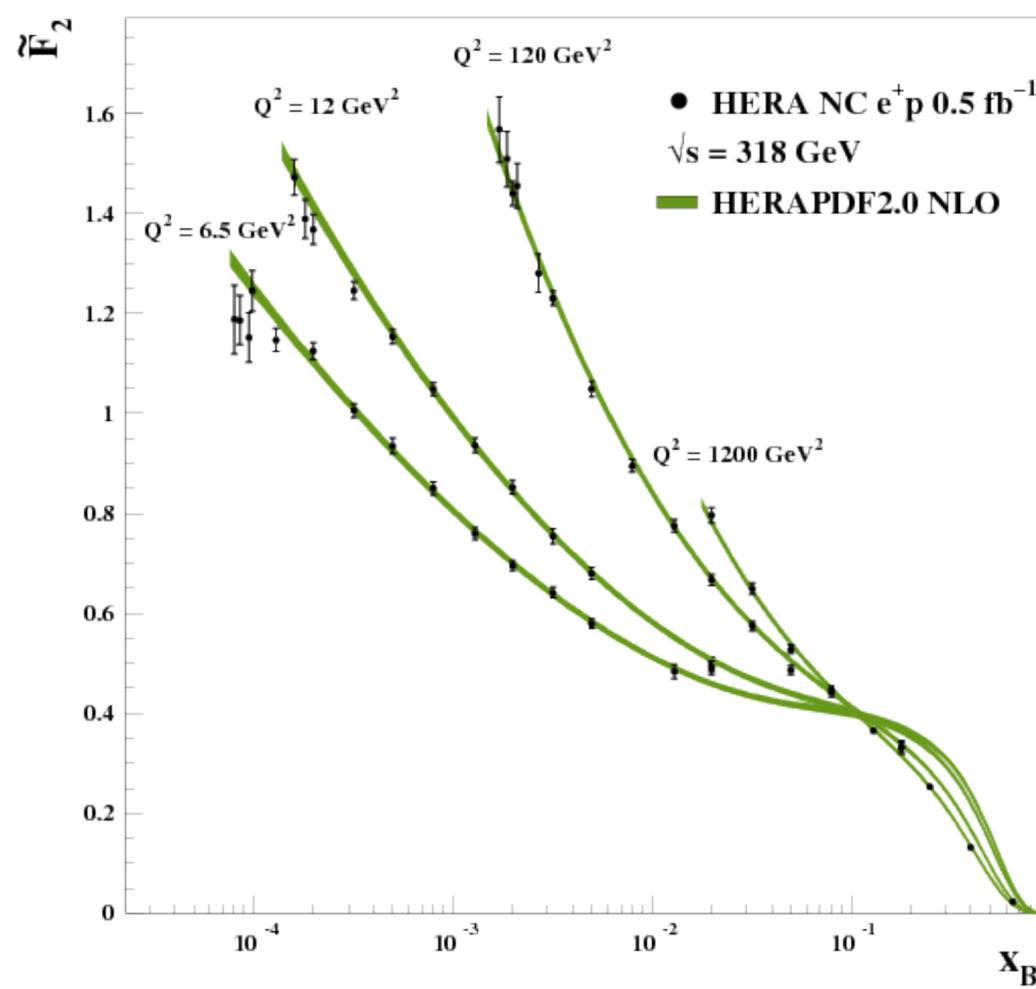
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H1 and ZEUS

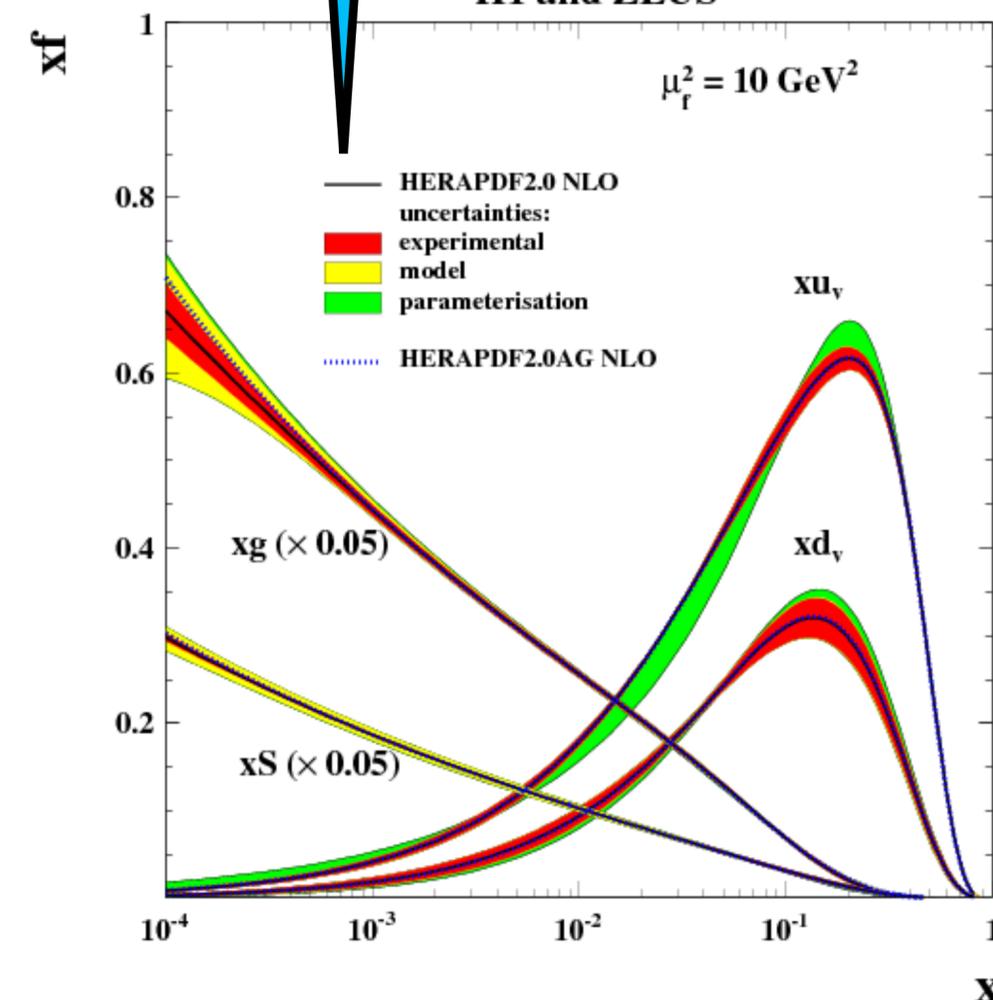


H1 and ZEUS



There also are NNLO fits

H1 and ZEUS



The QCD analysis of HERA data give us a deep and detailed view of the structure of the proton

We are interested in the high-energy limit of QCD

Reminder: small Bjorken- $x$  corresponds to large interaction energy

At this point in time, HERA data show that the structure function grows fast as Bjorken- $x$  decreases.  
Let's look at data in more detail and from different perspectives

3

## Exploring high-energy QCD: Probing structure functions with colour dipoles at HERA

# Growth of the cross section at fixed virtuality (2001)

In the BFKL approach, it is expected that the structure function at fixed virtuality grows as a power law

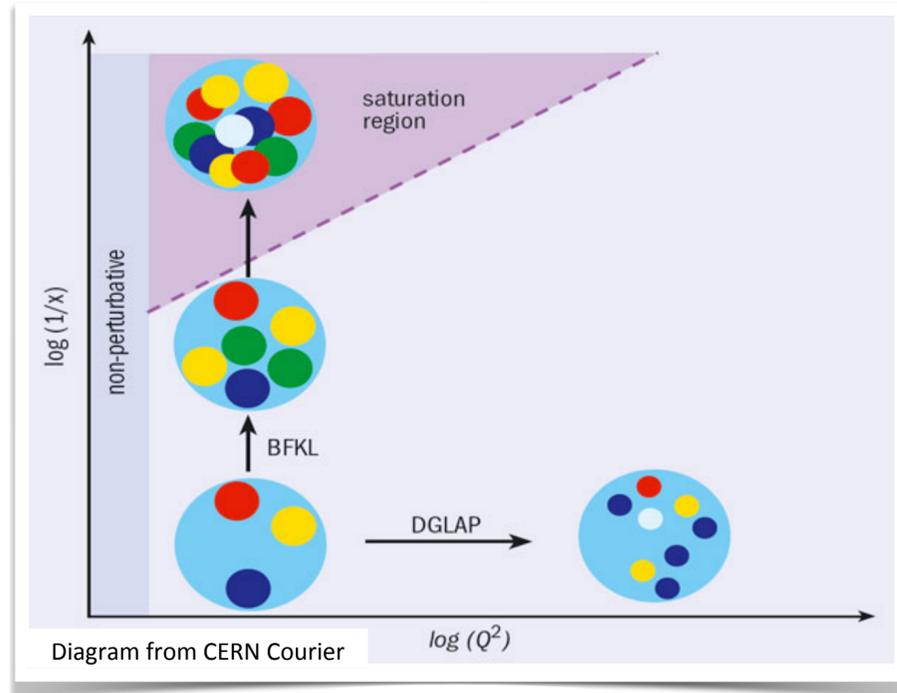
Fix the scale and  
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<https://inspirehep.net/literature/561805>

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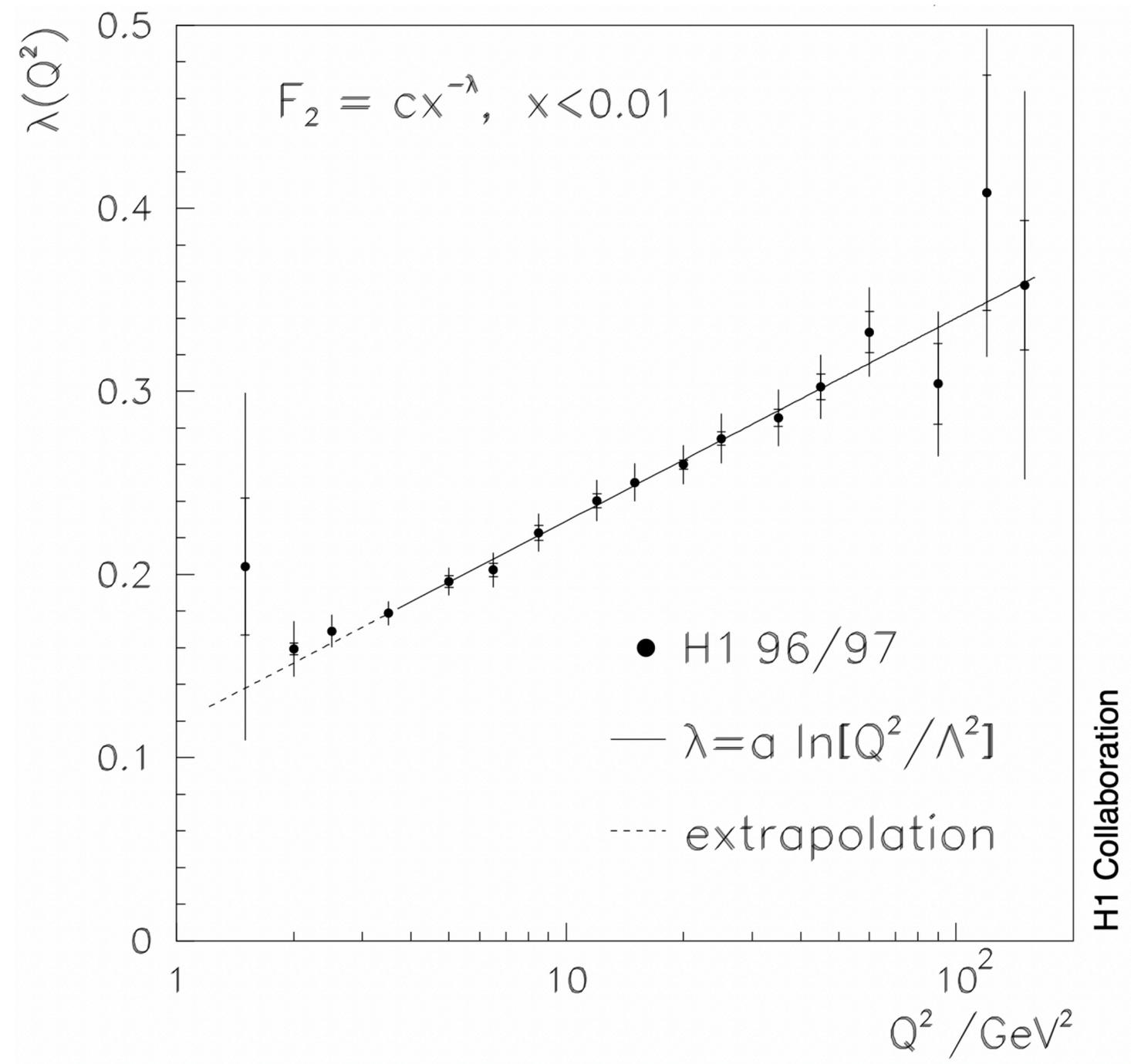
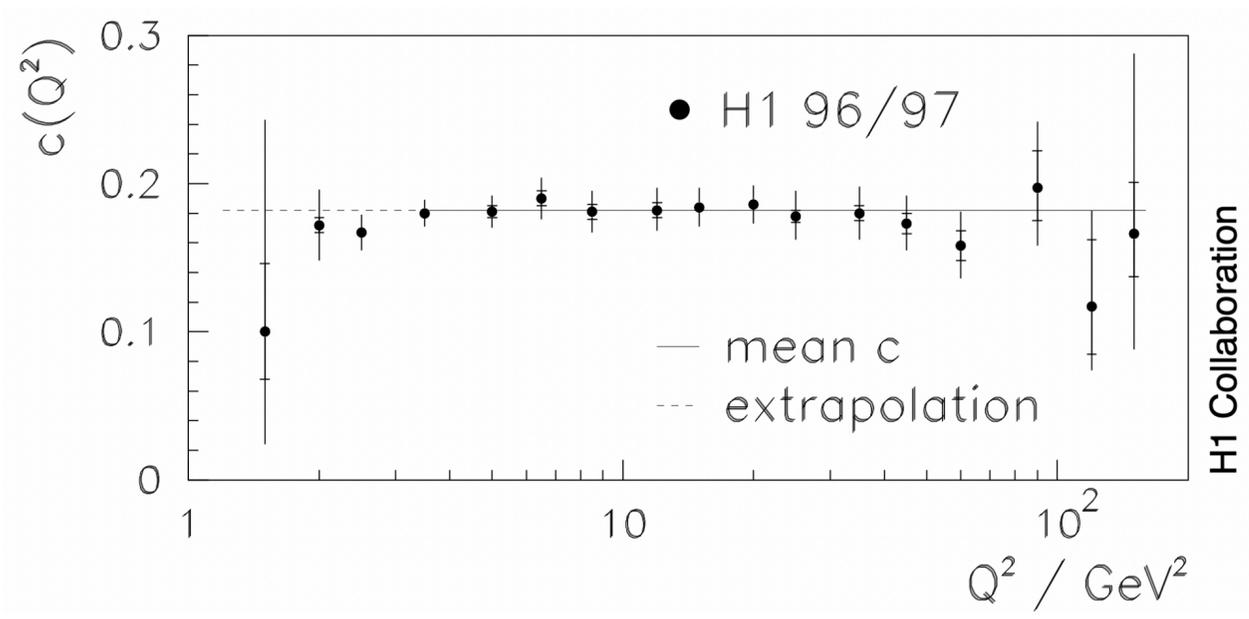
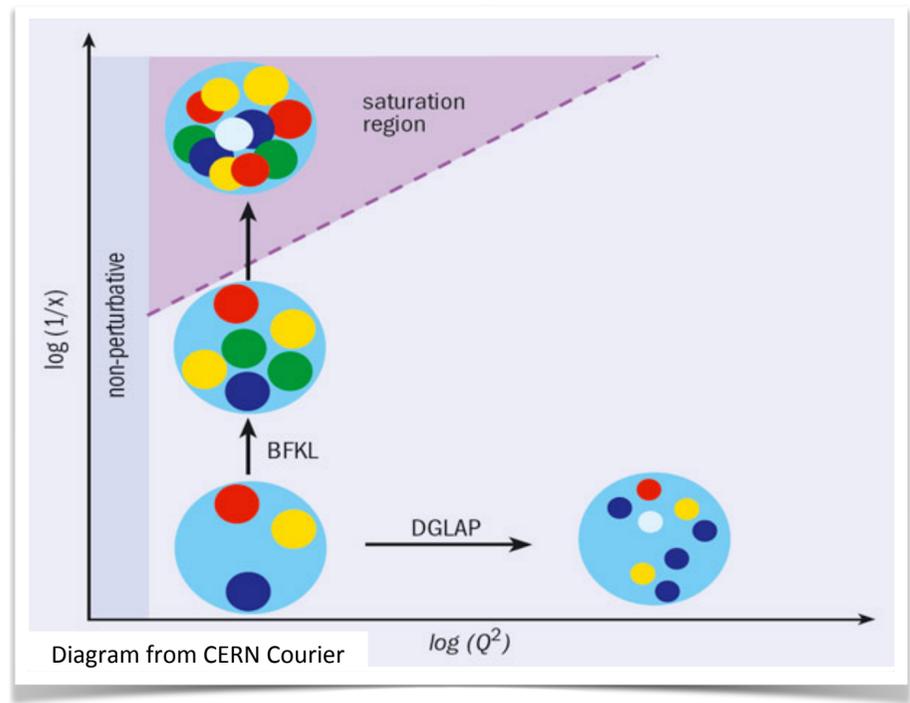


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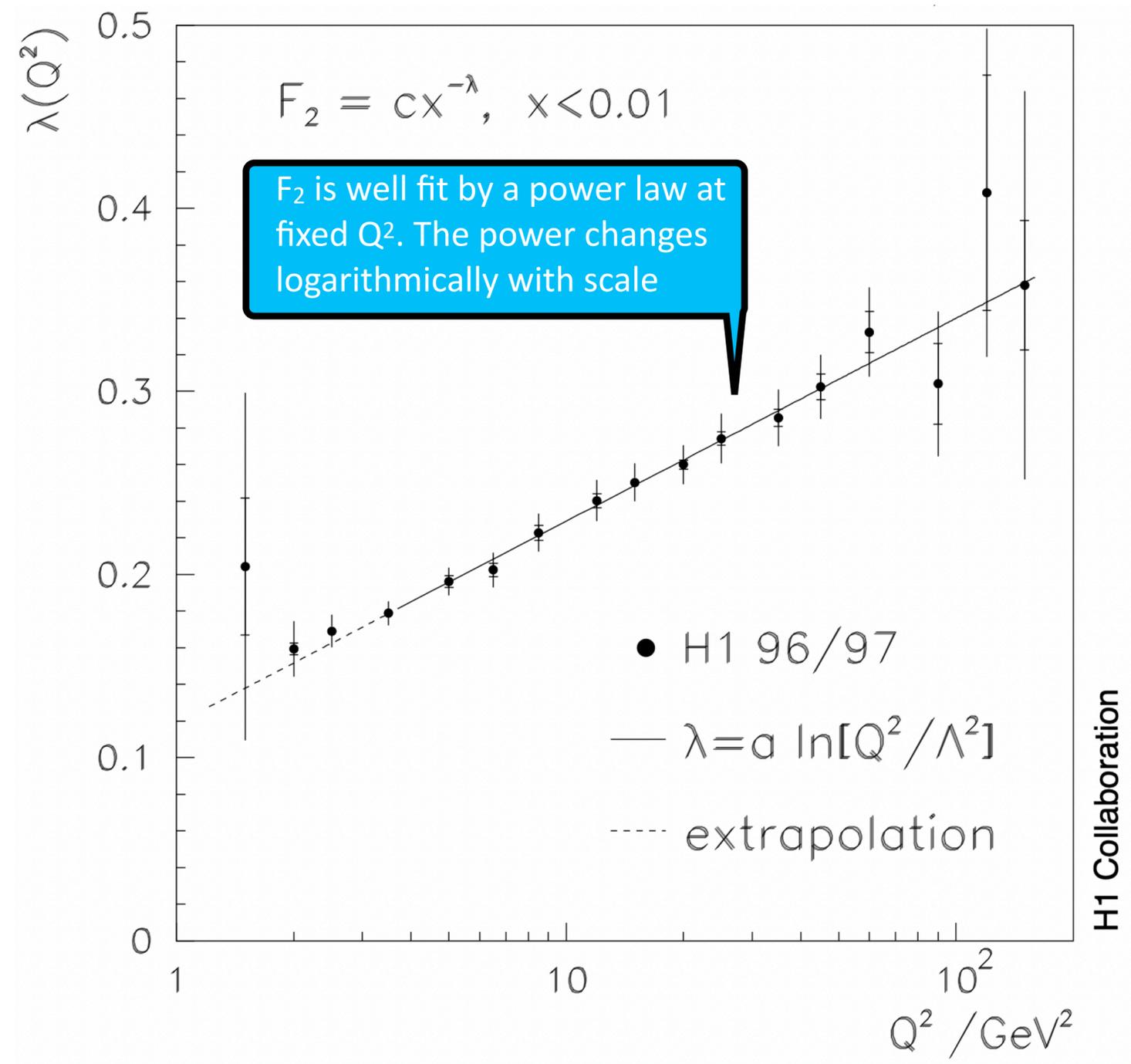
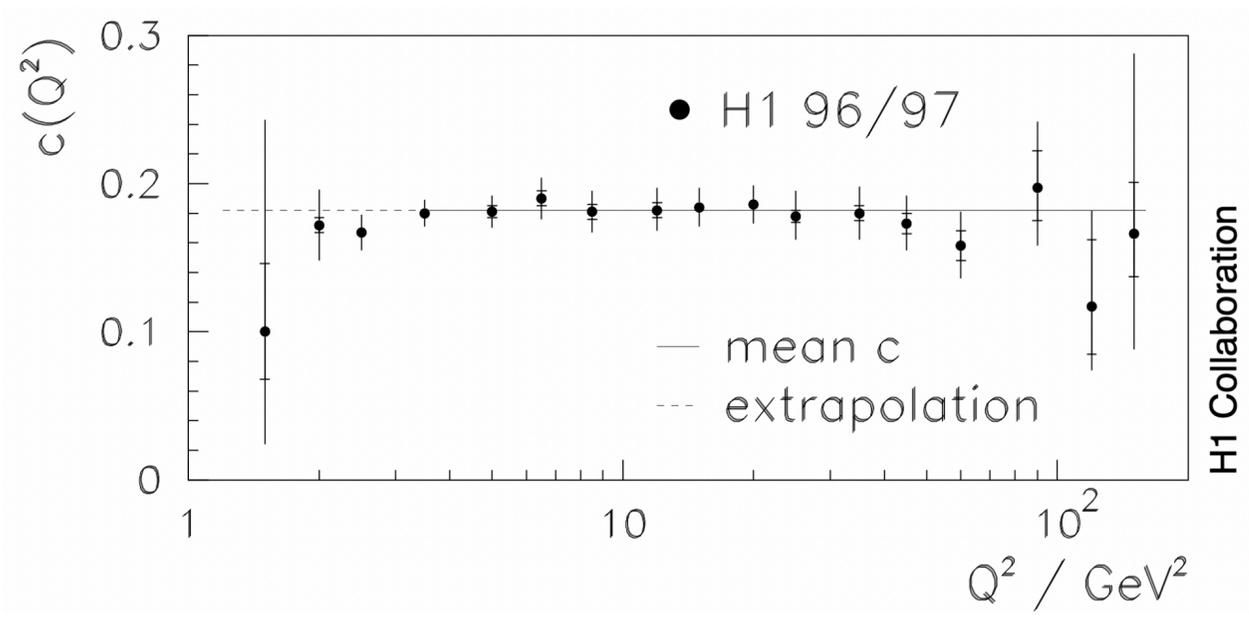
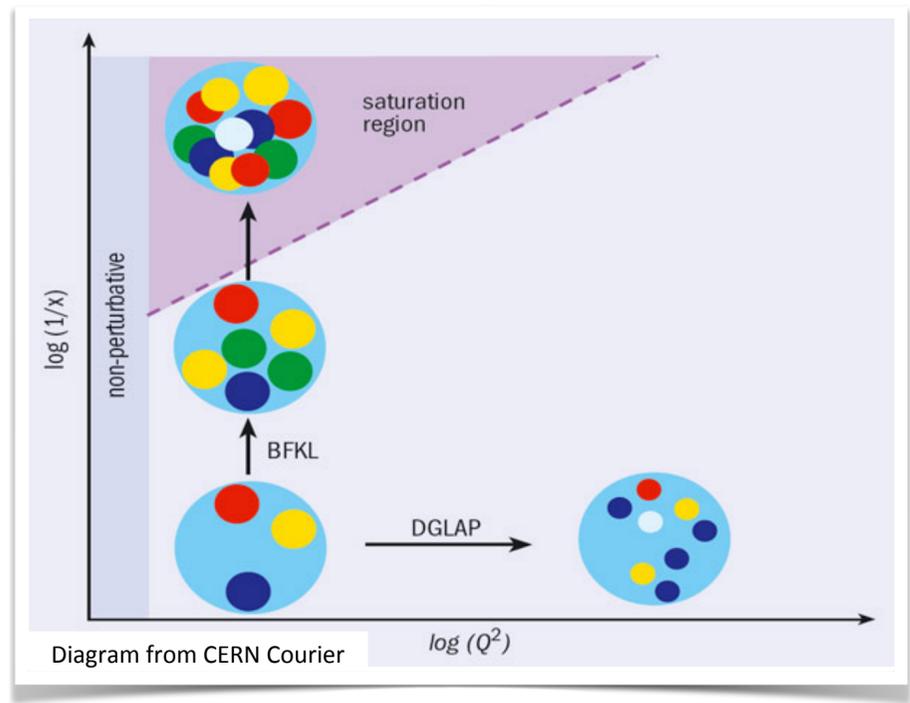


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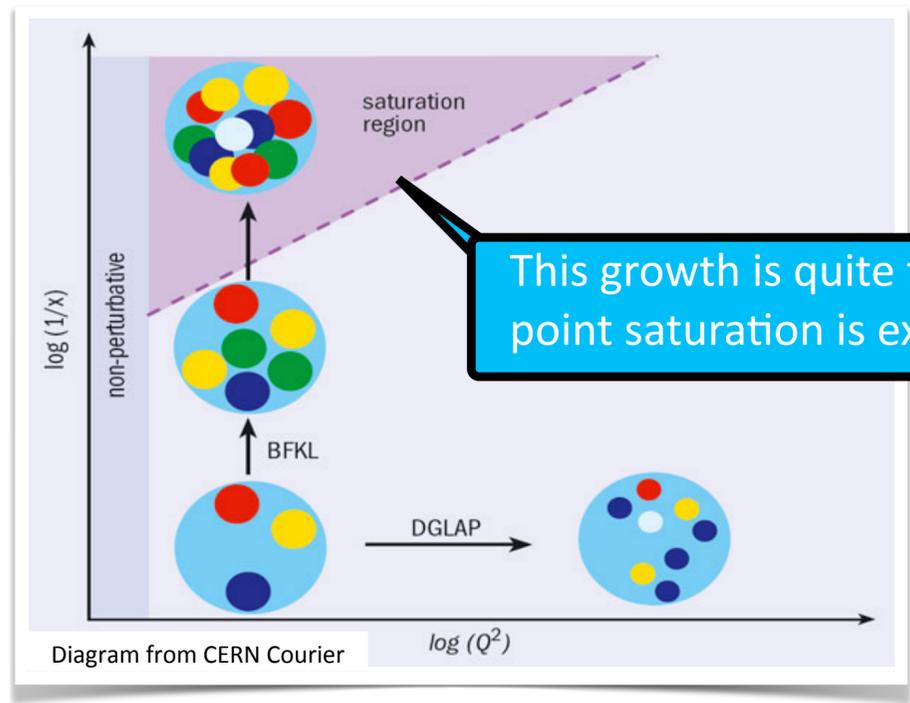


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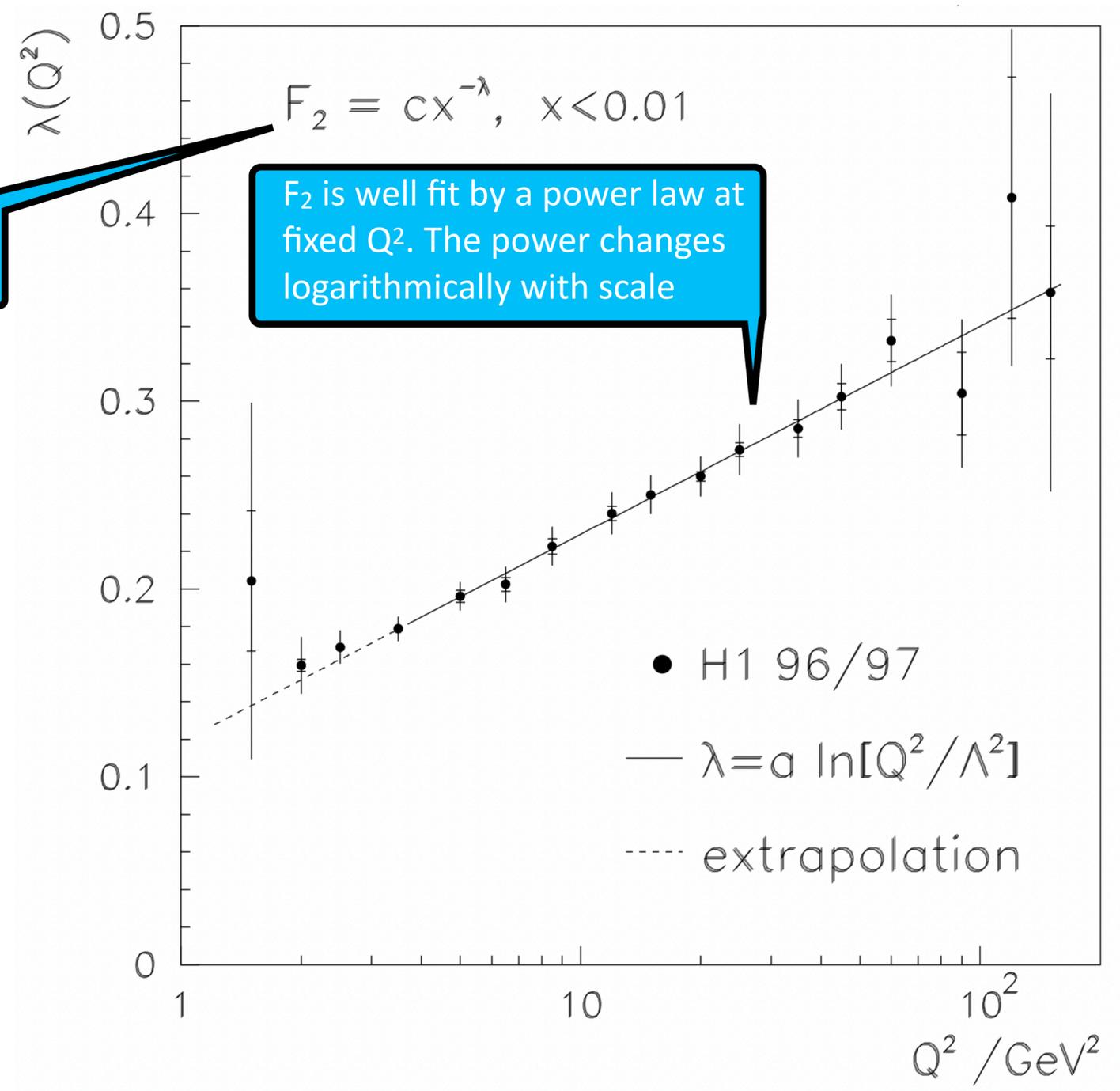
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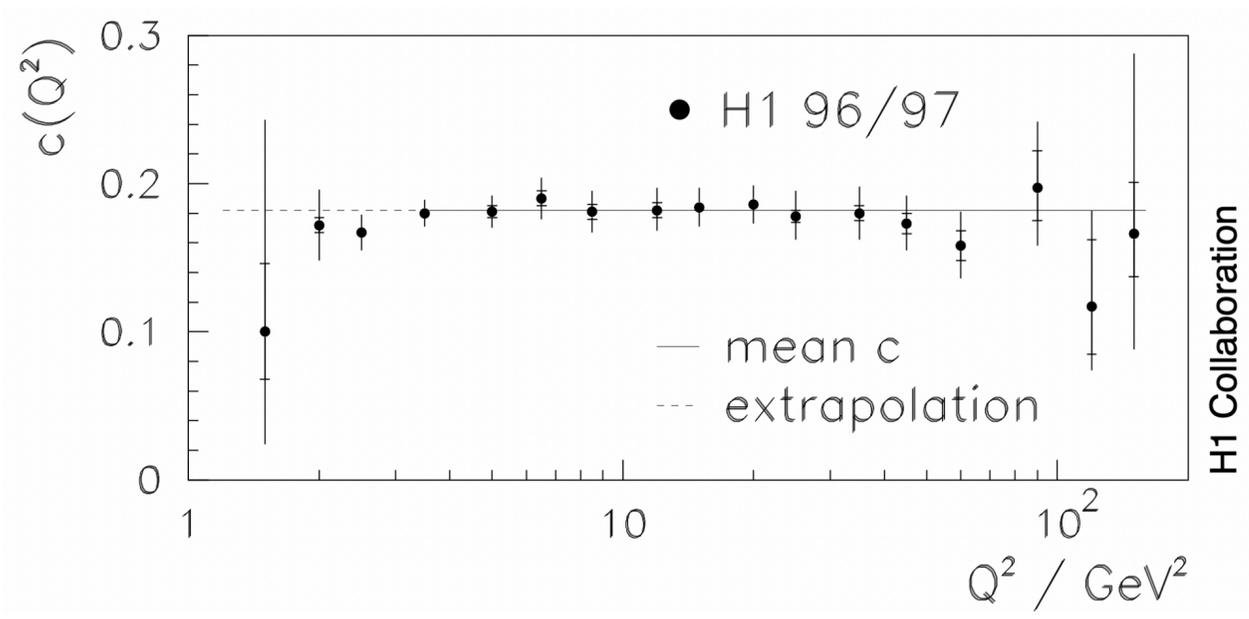
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This growth is quite fast, at some point saturation is expected



$F_2$  is well fit by a power law at fixed  $Q^2$ . The power changes logarithmically with scale



H1 Collaboration

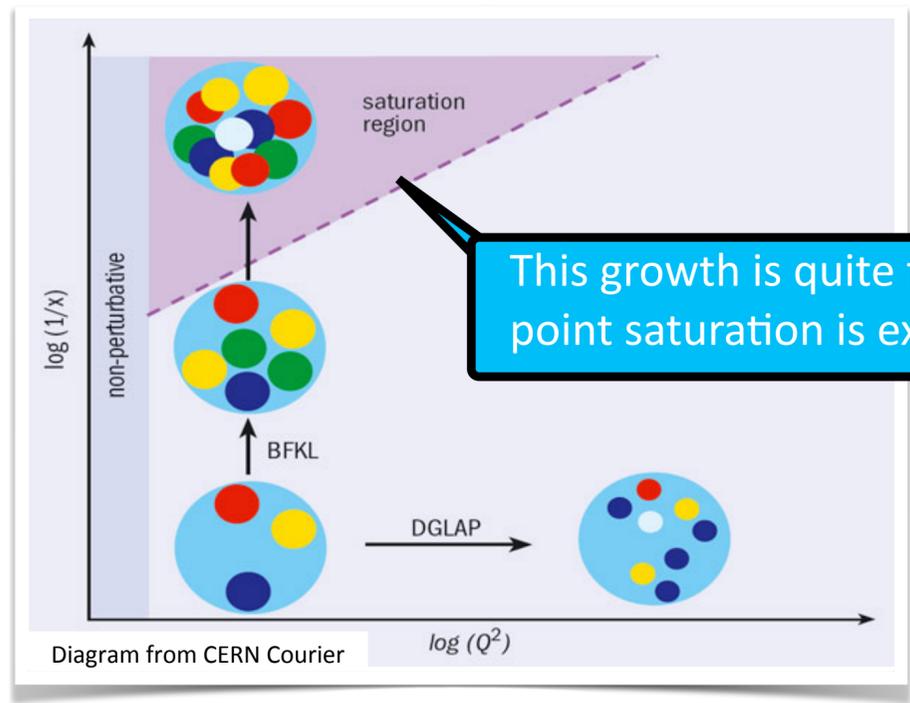
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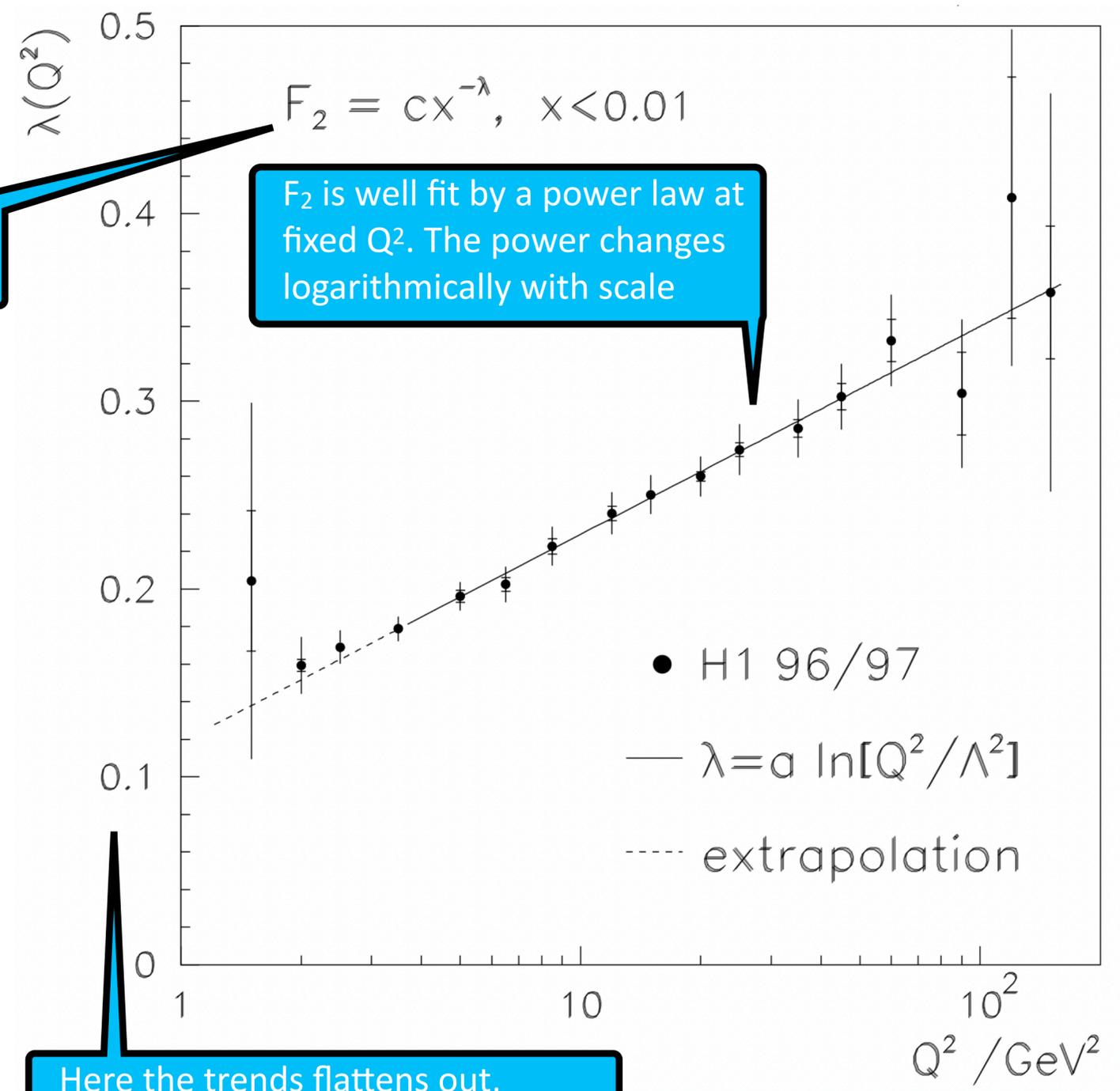
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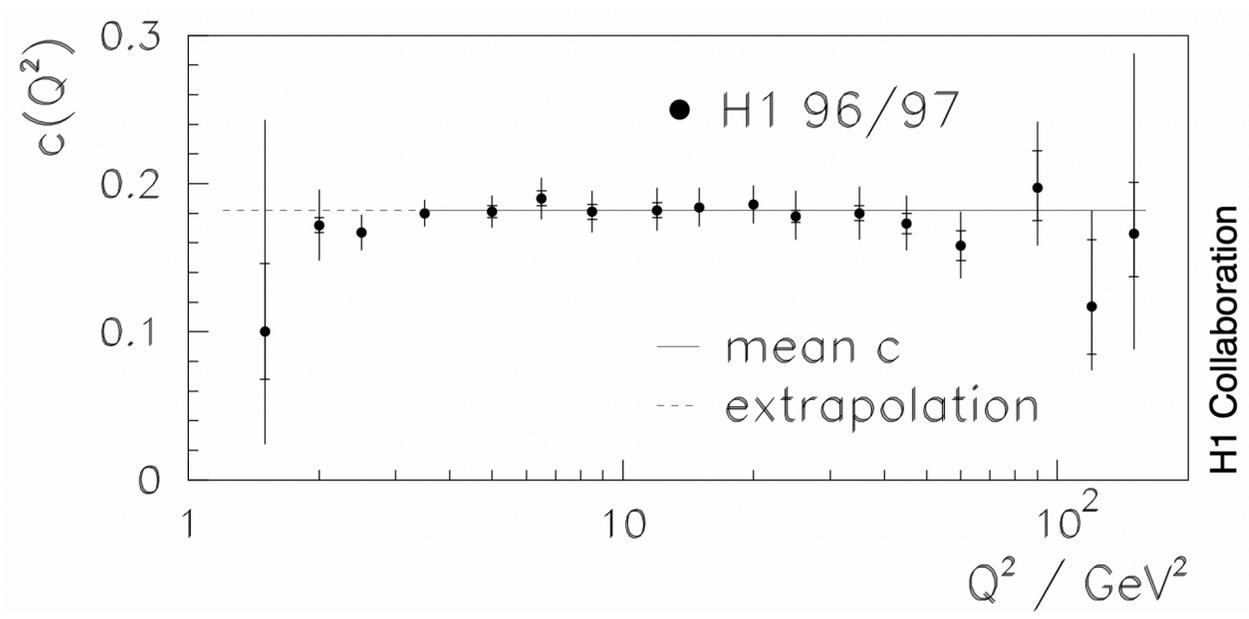


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Here the trends flattens out, consistent with total cross sections



H1 Collaboration

H1 Collaboration

The determination of the onset of saturation is one of the prime tasks of experimental pQCD nowadays

# Photo-production cross section (1997)

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4 x} \left(2 - 2y + \frac{y^2}{1+R}\right) F_2(x, Q^2) = \Gamma[\sigma_T(x, Q^2) + \epsilon(y)\sigma_L(x, Q^2)] \equiv \Gamma\sigma_{\gamma^*p}^{eff}(x, y, Q^2)$$

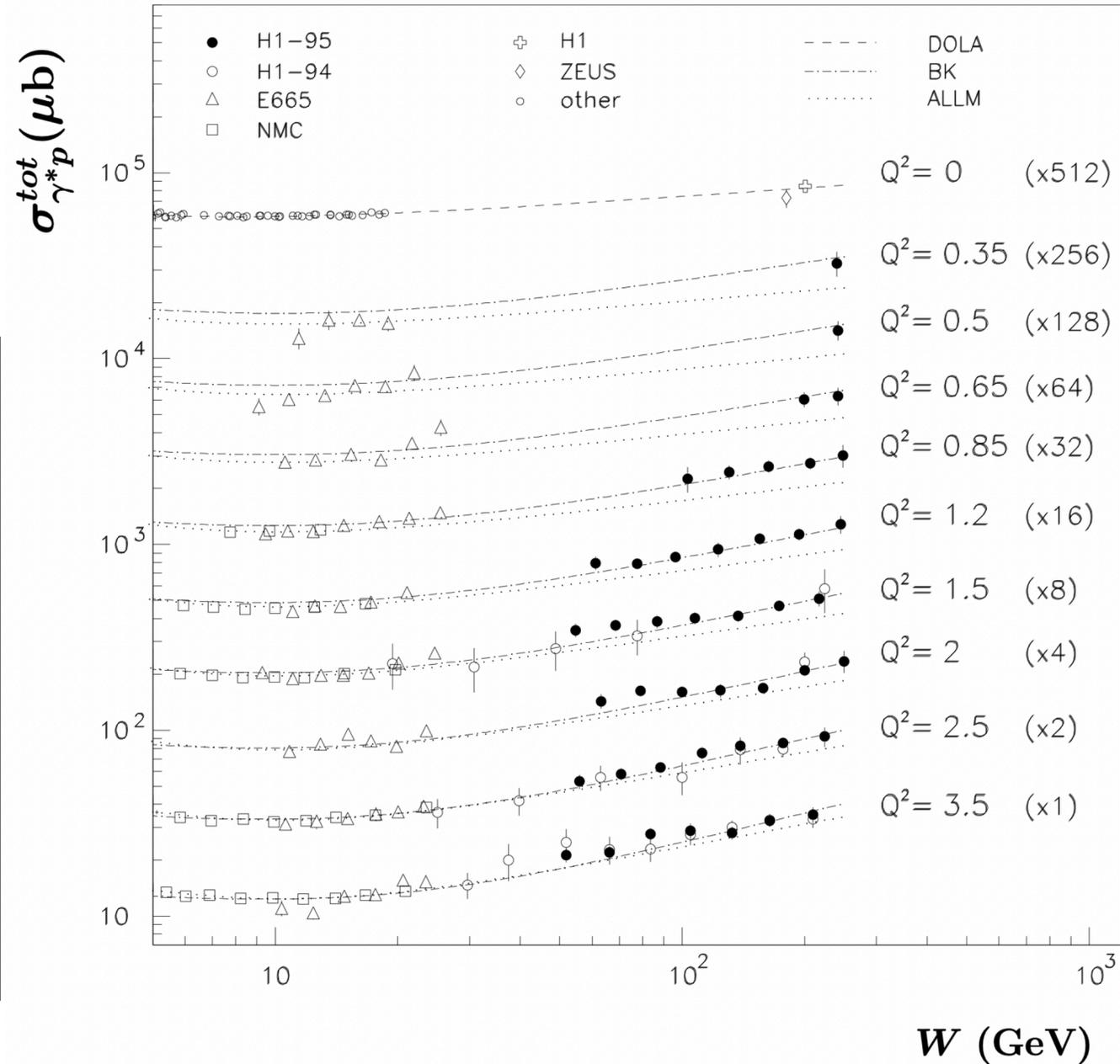
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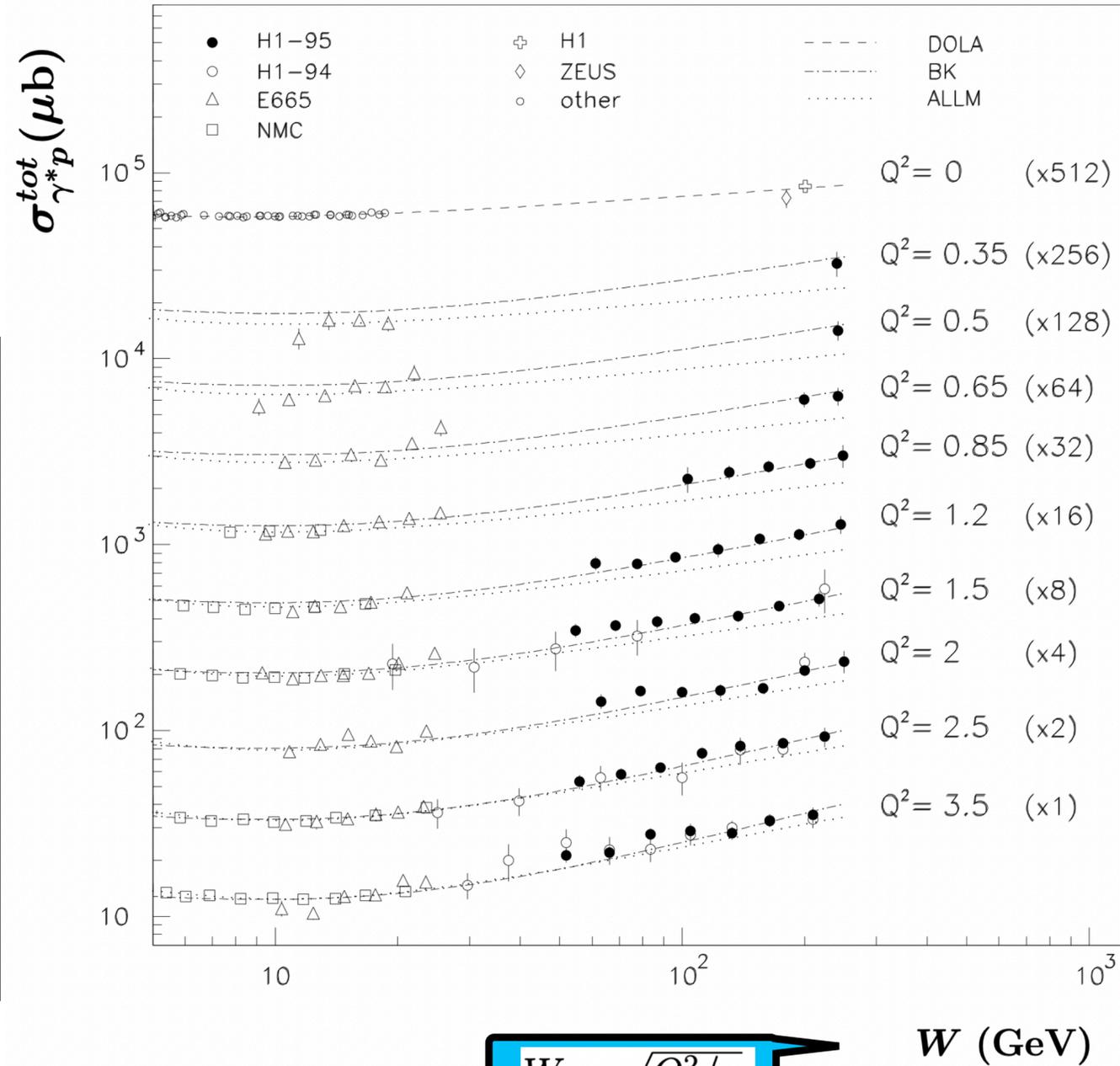
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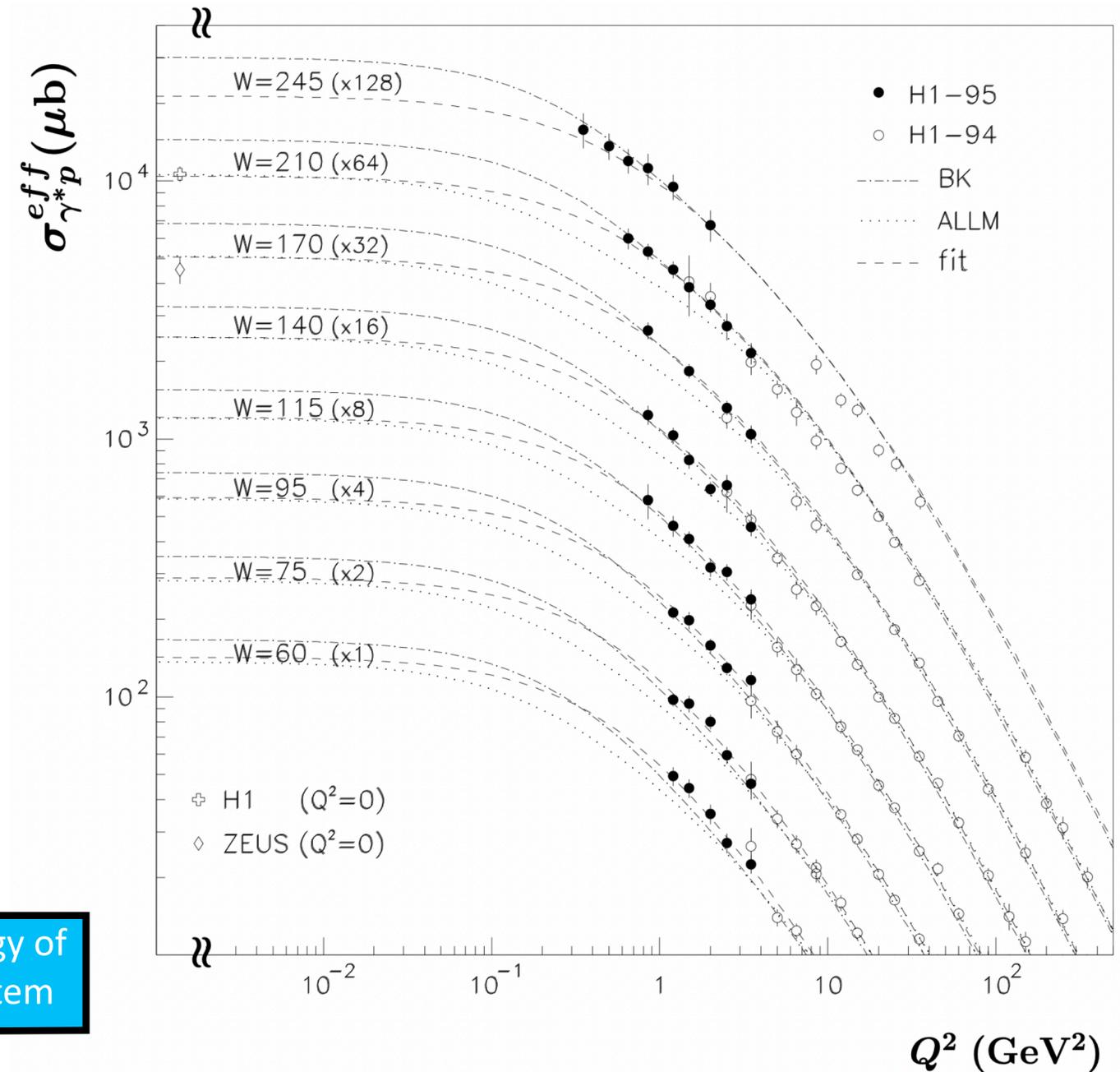
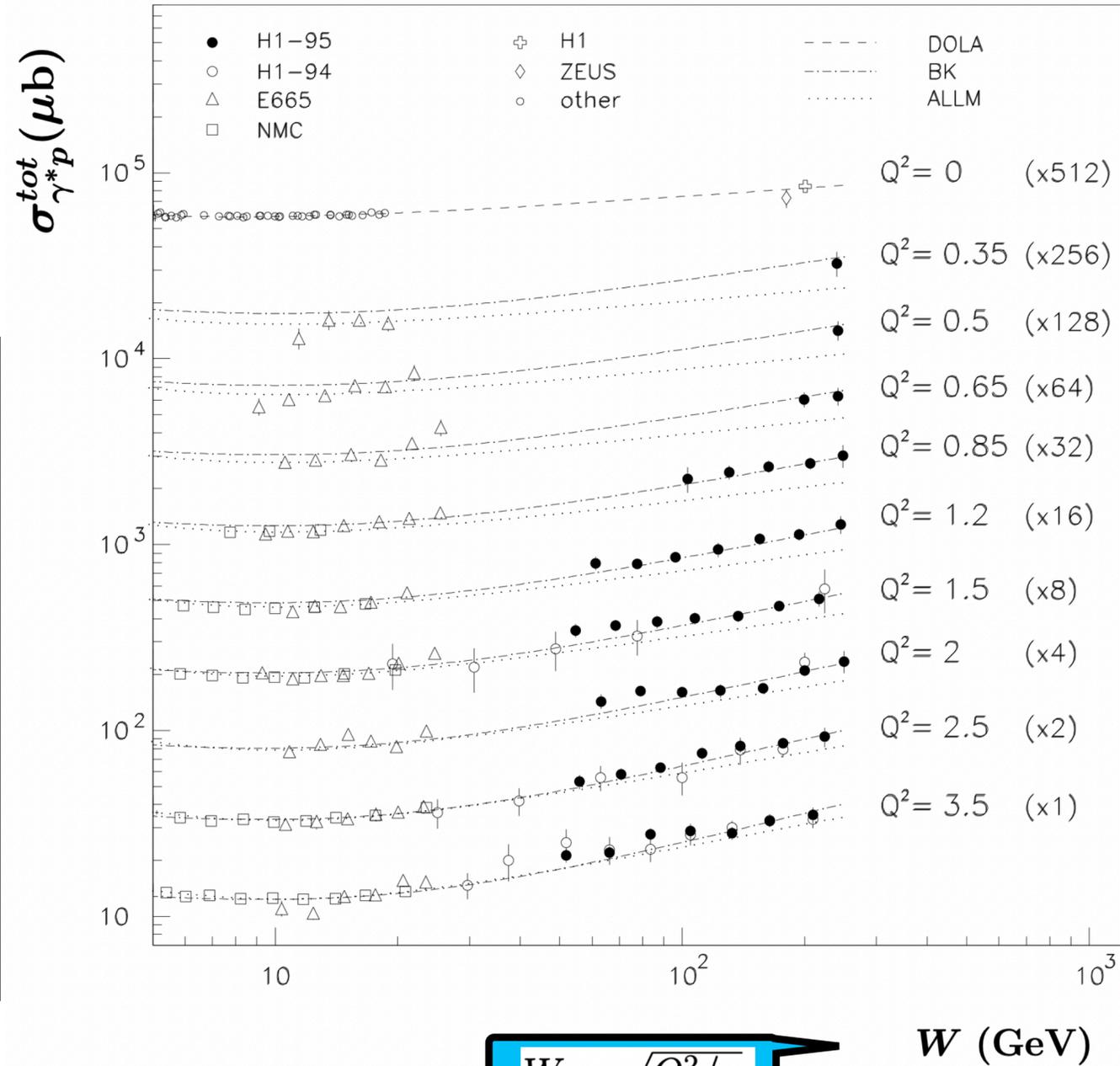
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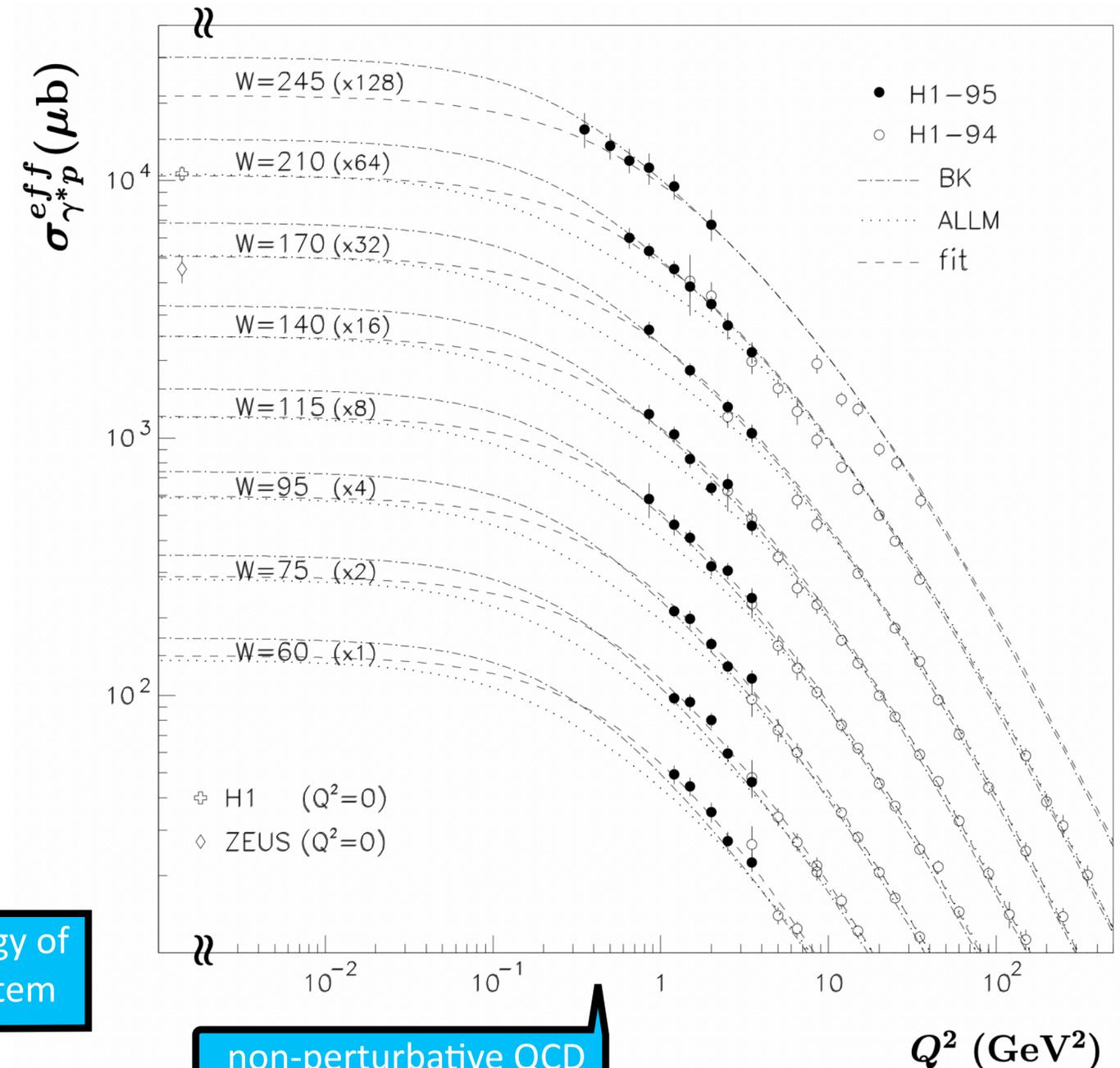
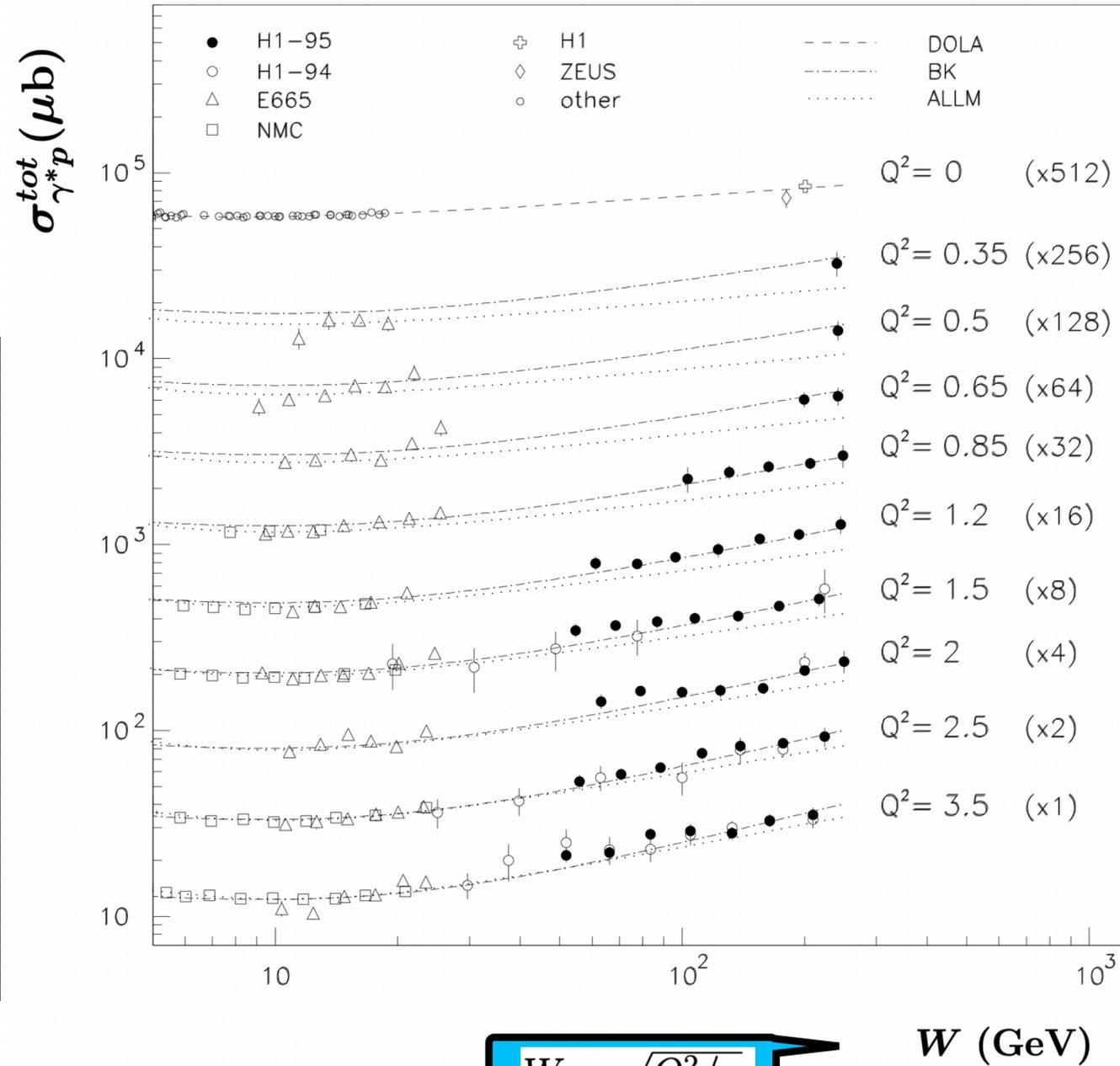
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non-perturbative QCD starts around here

Guillermo Contreras, CTU in Prague

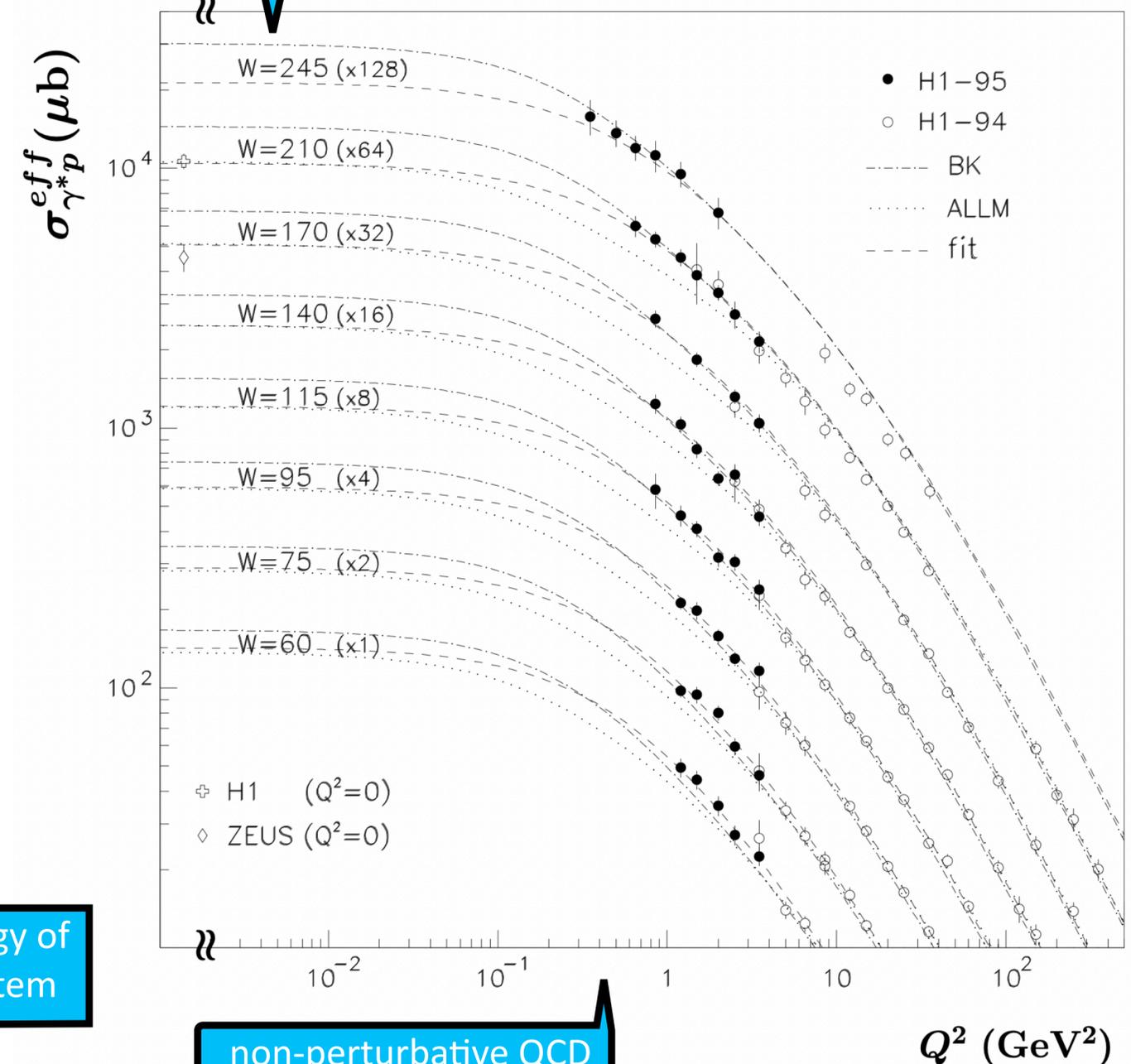
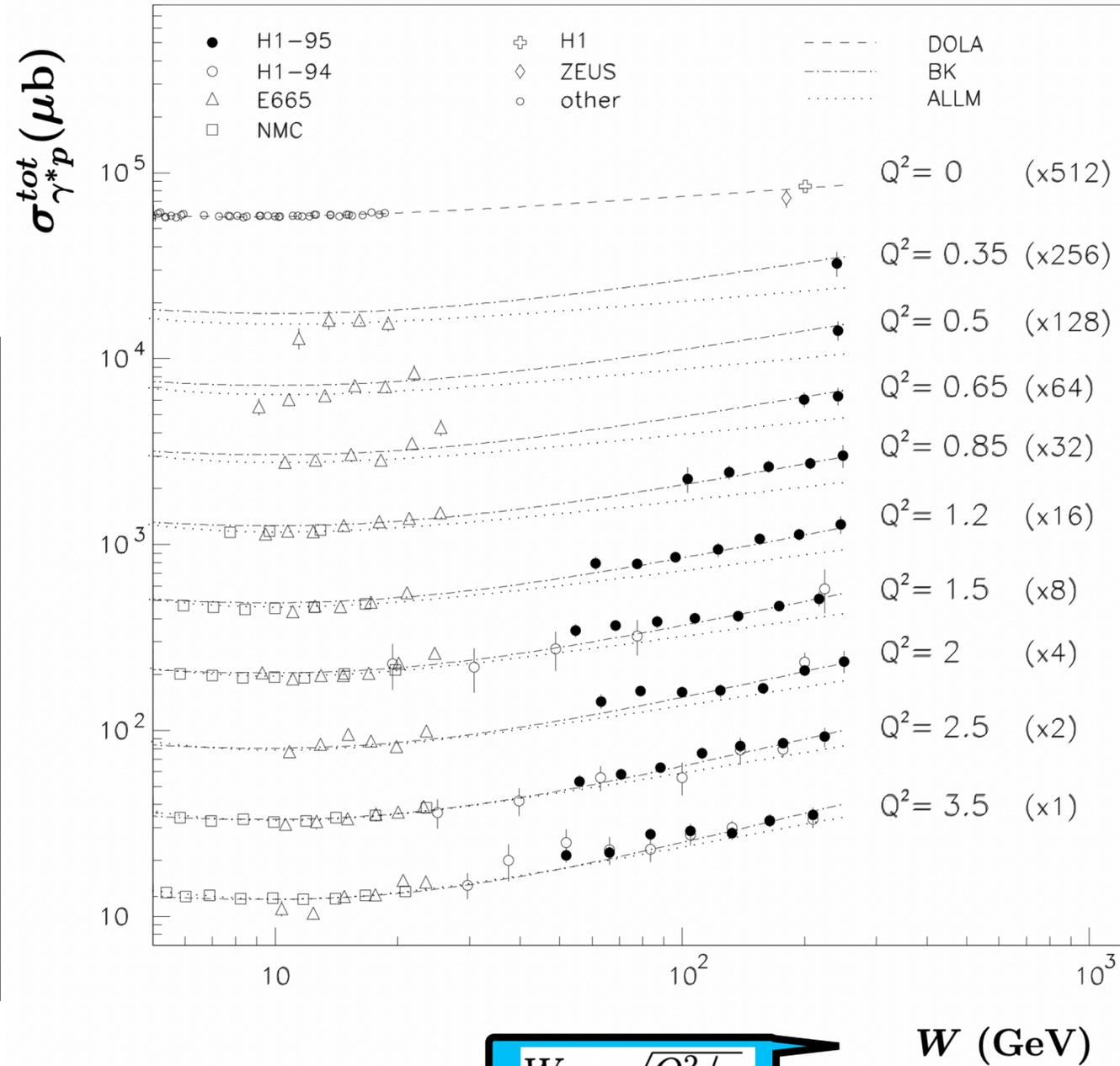
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This is a different type of saturation than the one mentioned in the previous page

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The GBW (Golec-Biernart and Wüsthoff) model

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Homework:

try to implement this model and reproduced the results in the next pages

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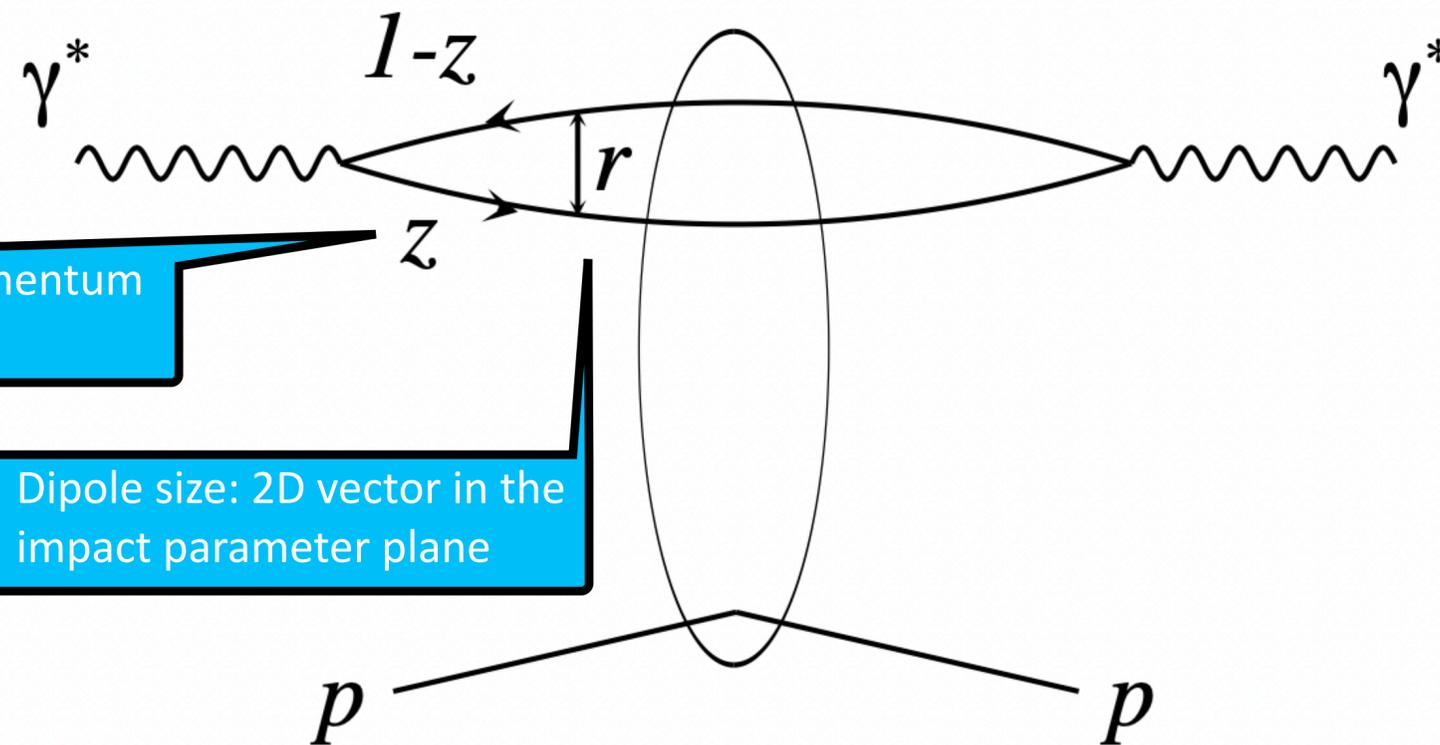
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Fraction of the photon momentum carried by the quark

Dipole size: 2D vector in the impact parameter plane

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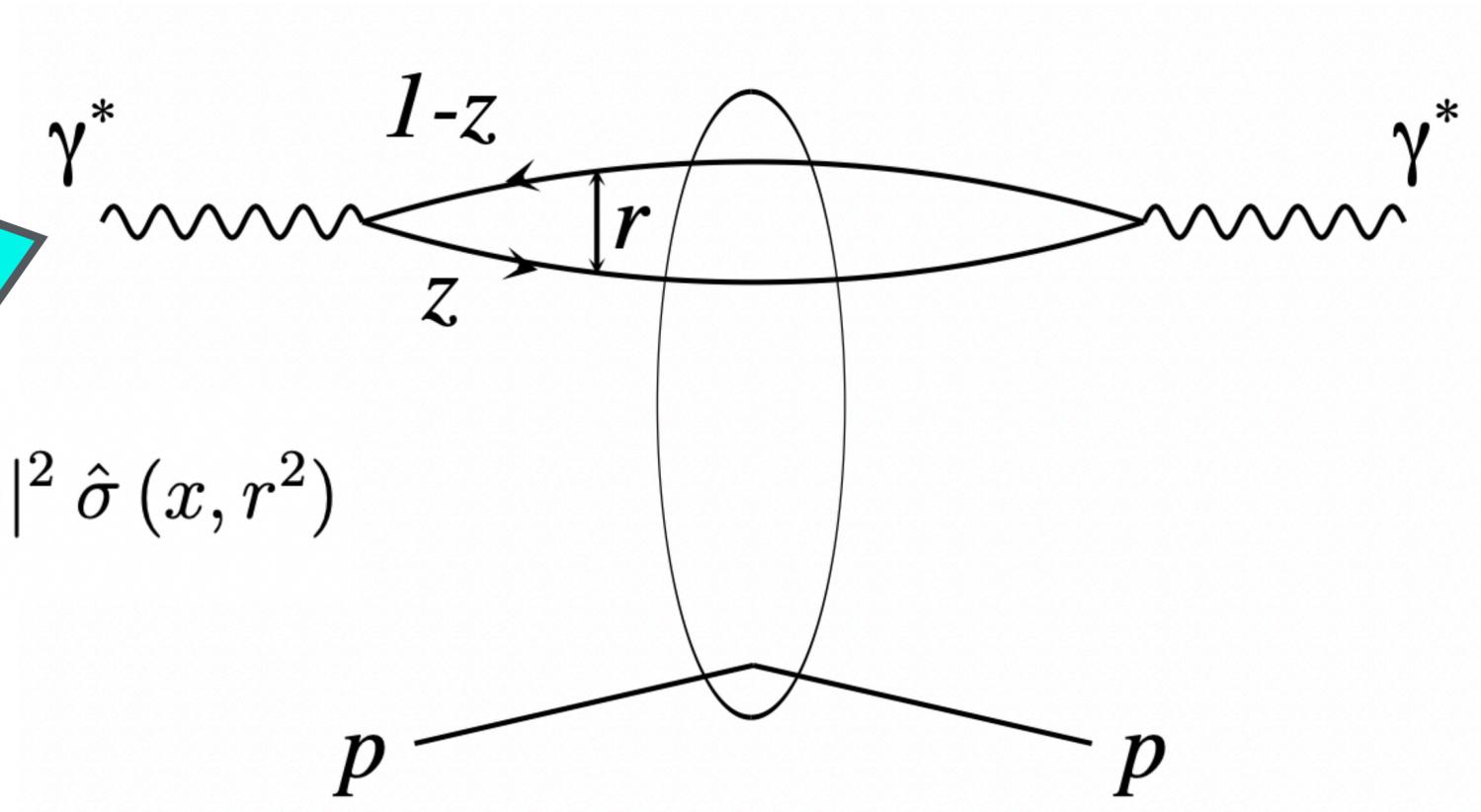
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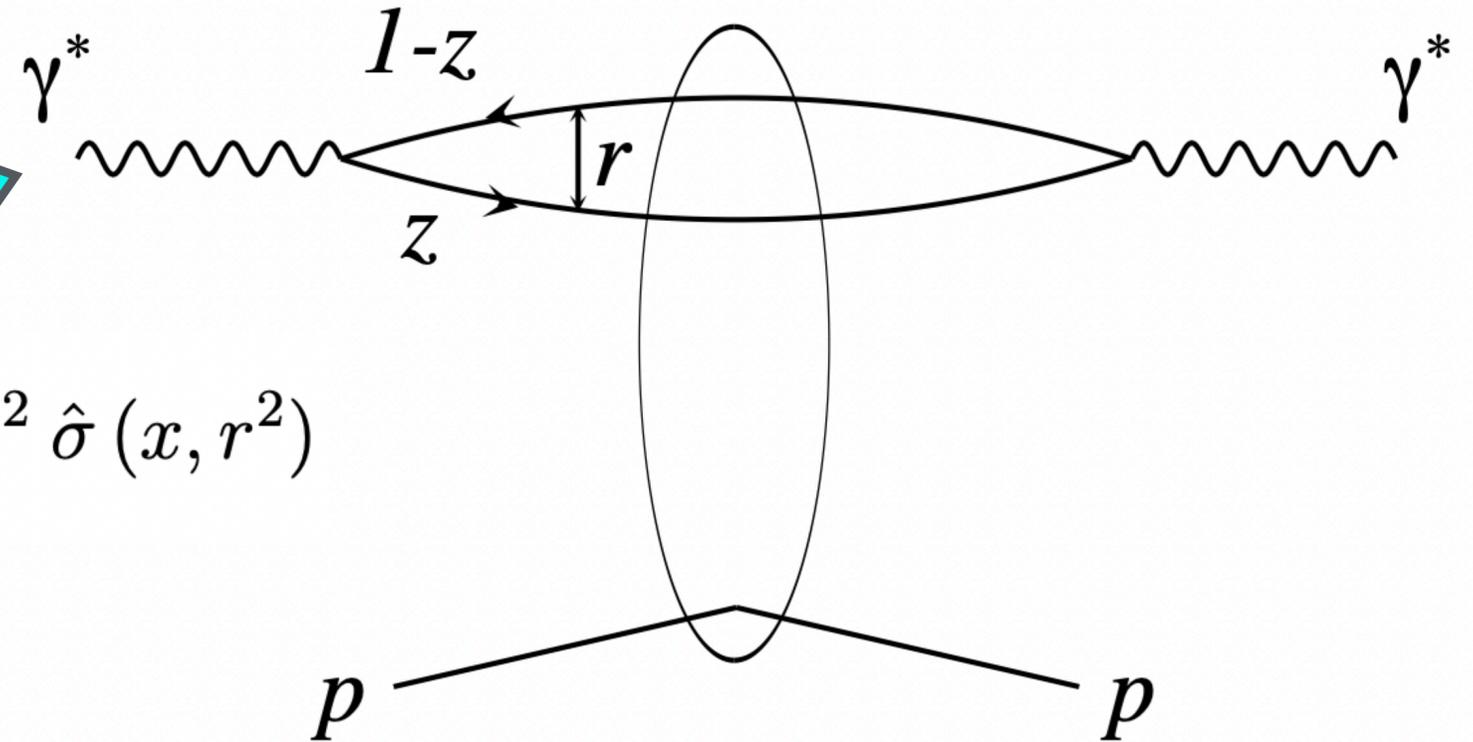


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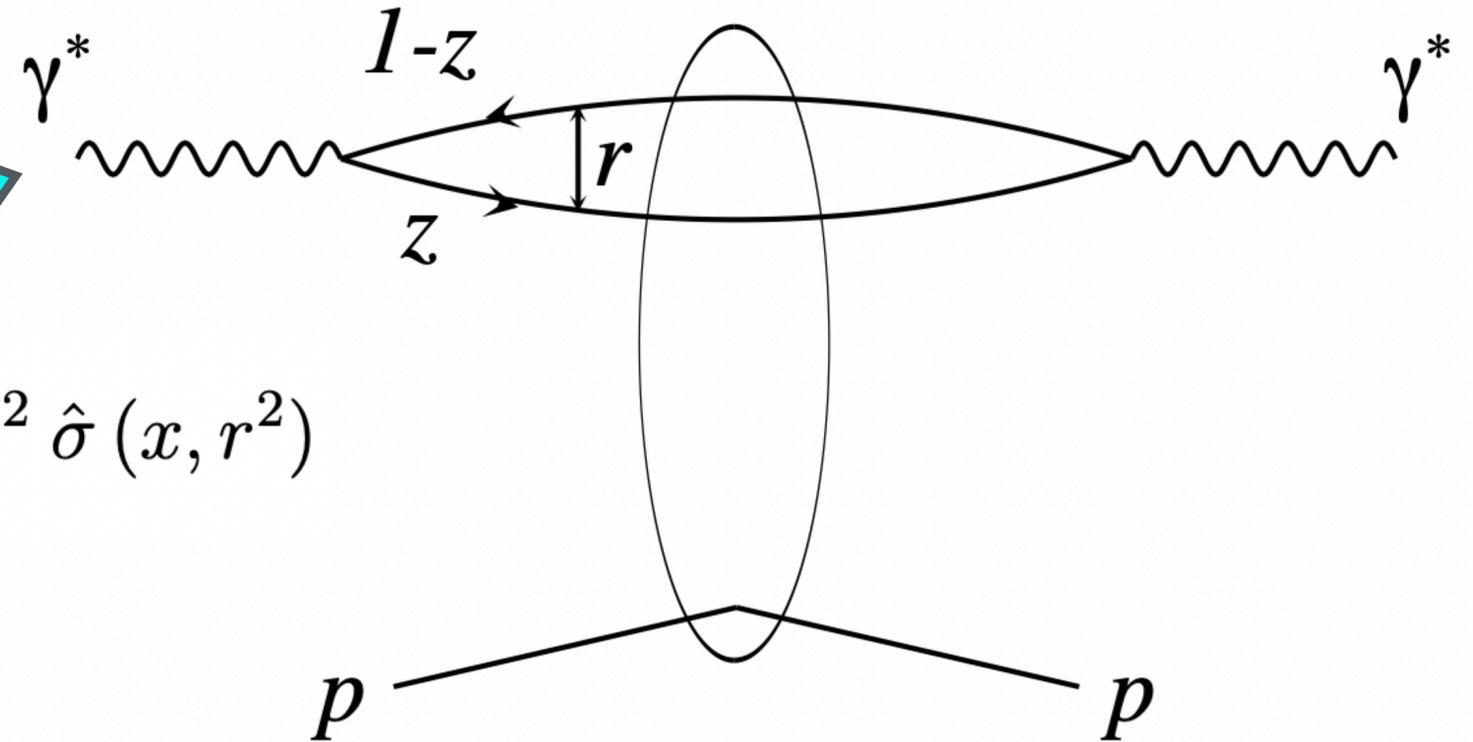
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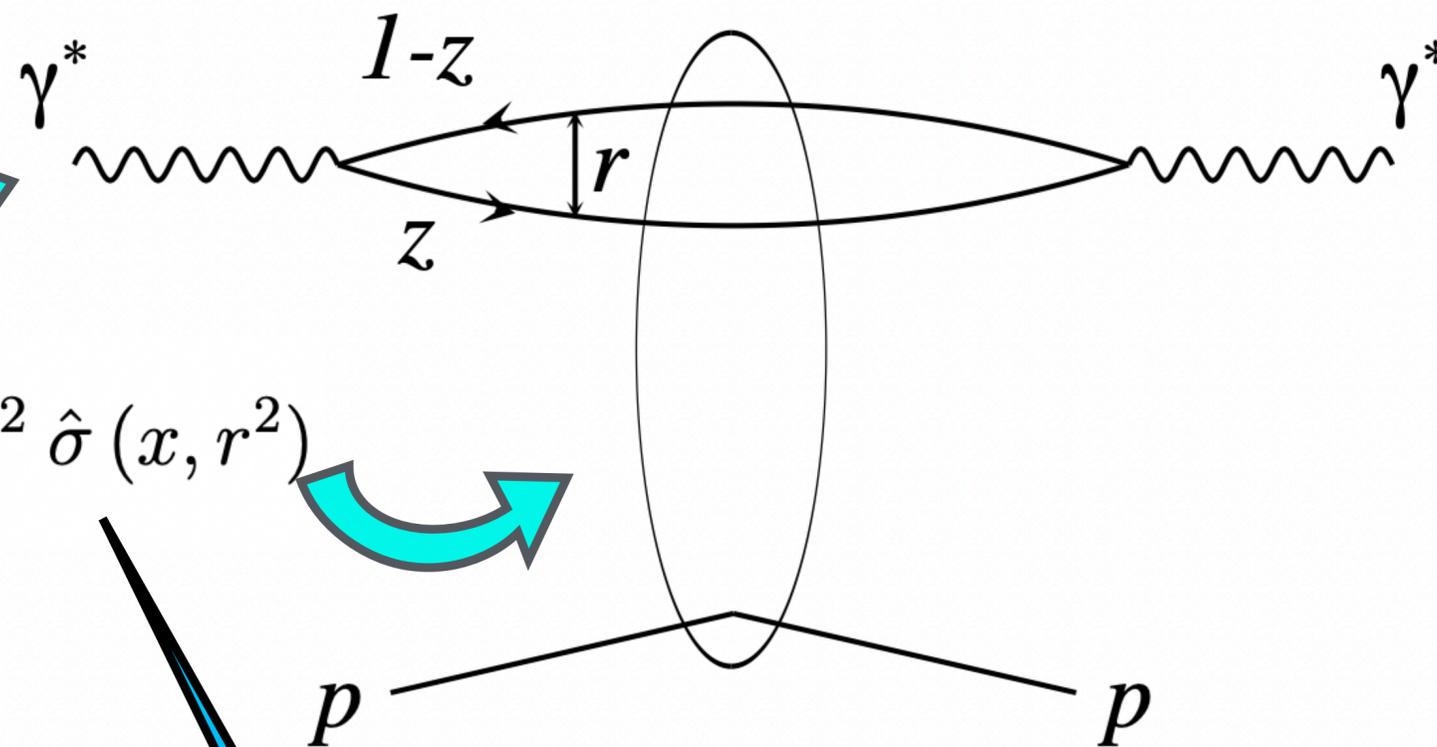
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Dipole cross section

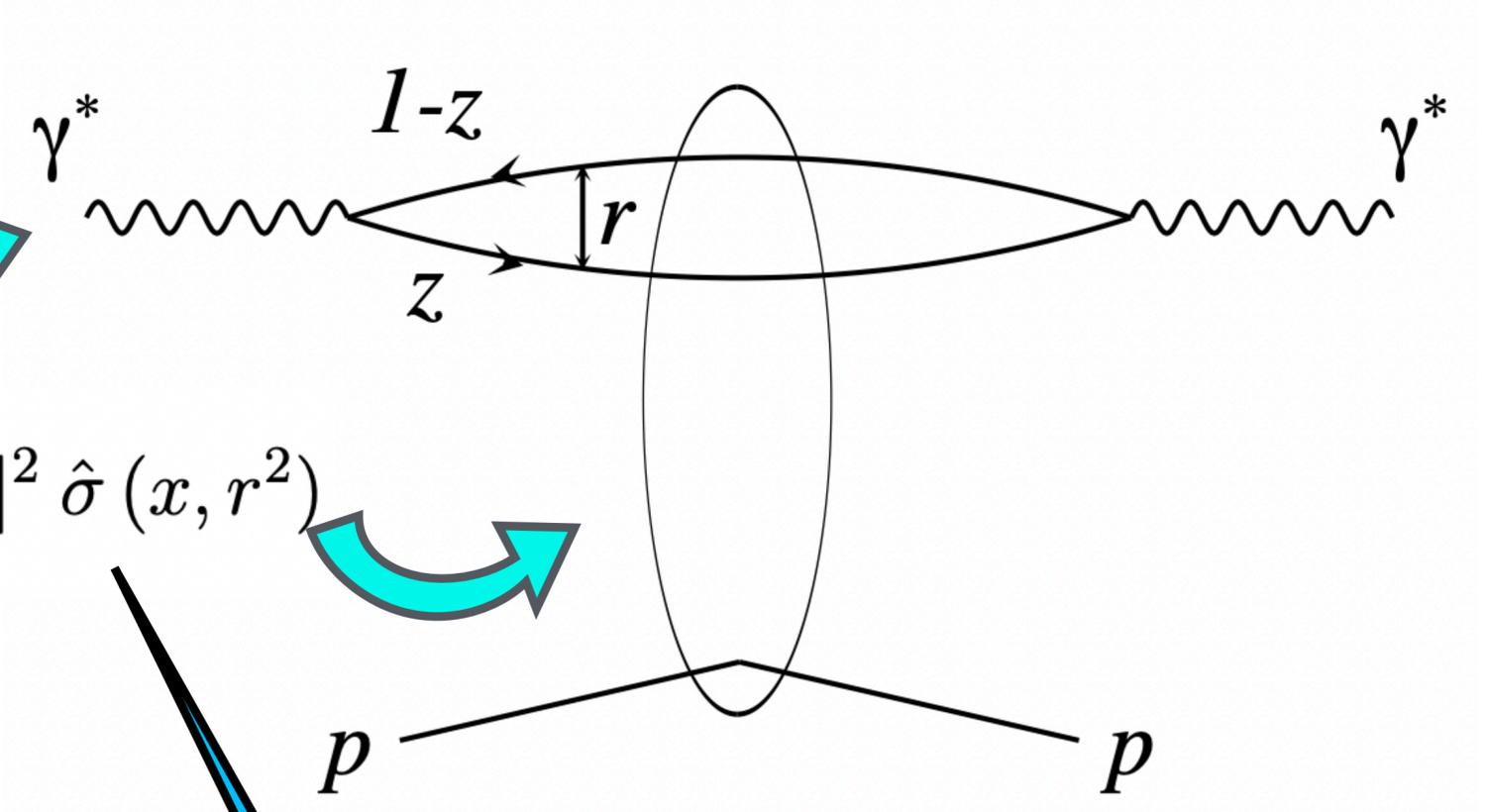
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Dipole cross section

QCD is here

Golec-Biernat, Wüsthoff <https://inspirehep.net/literature/473813>

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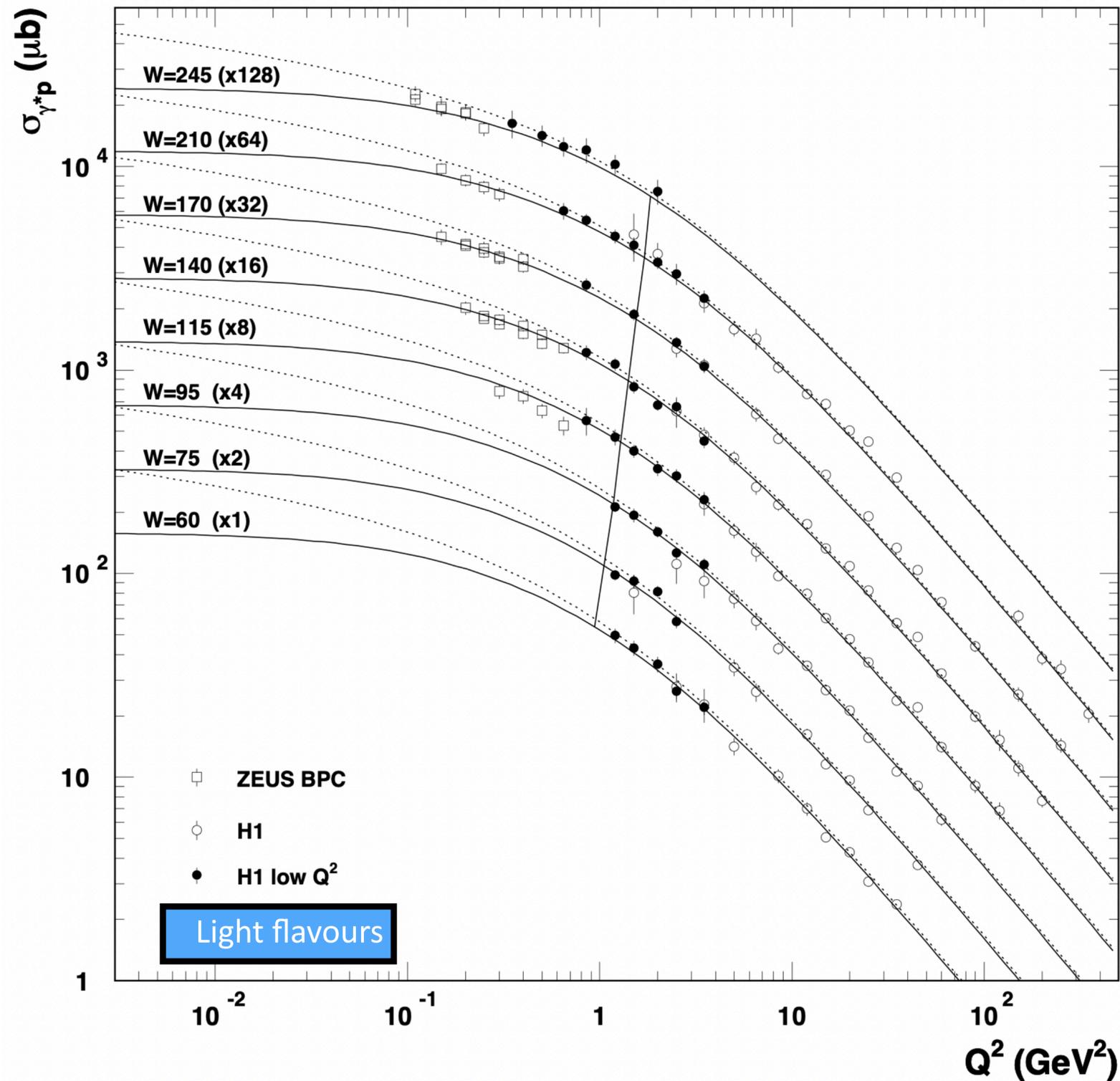
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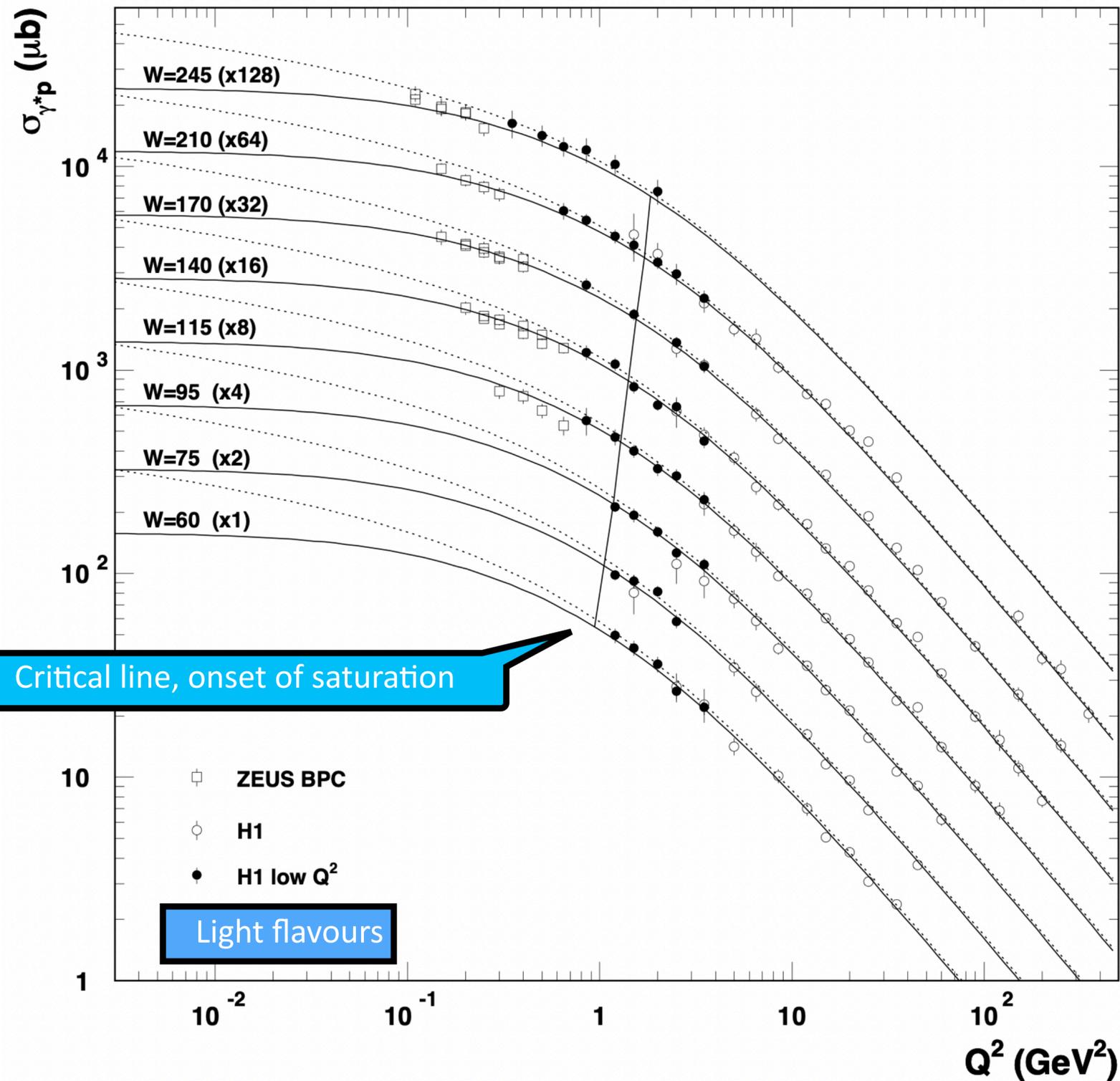
GBW define the critical line as:

$$R_0^2(x) = \frac{1}{Q^2}$$

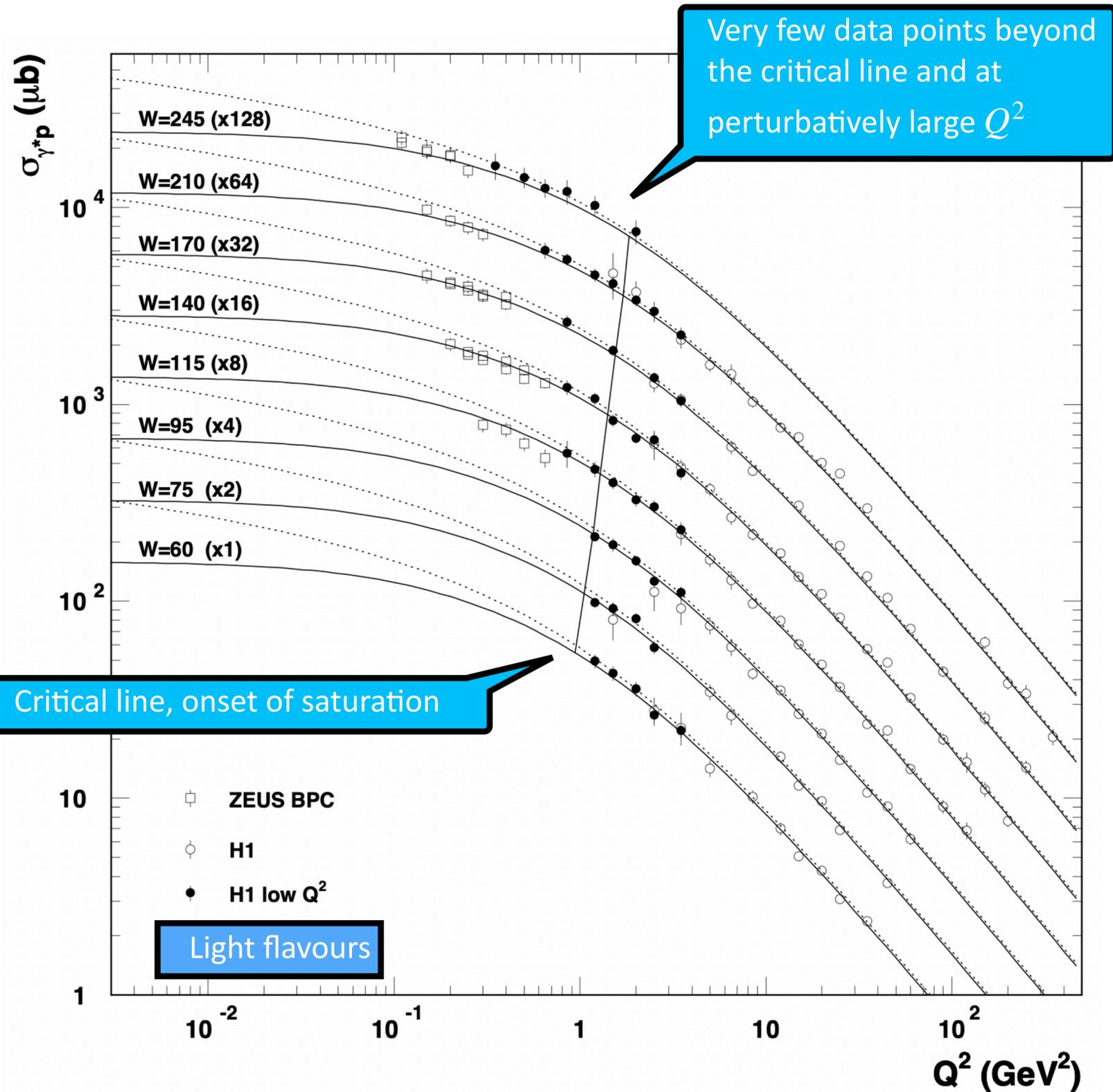
# 1998: The GBW model. (4) Fit results



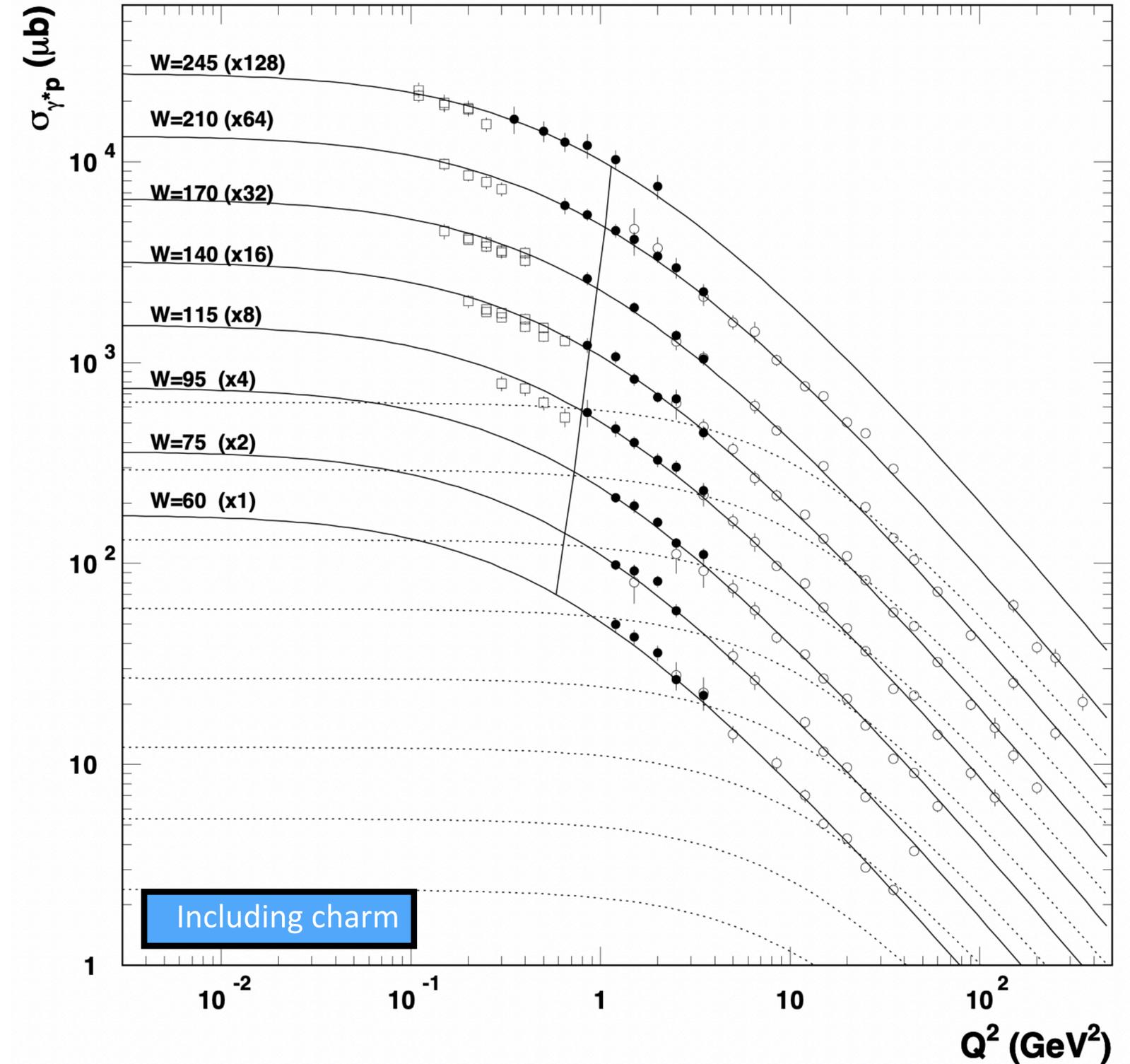
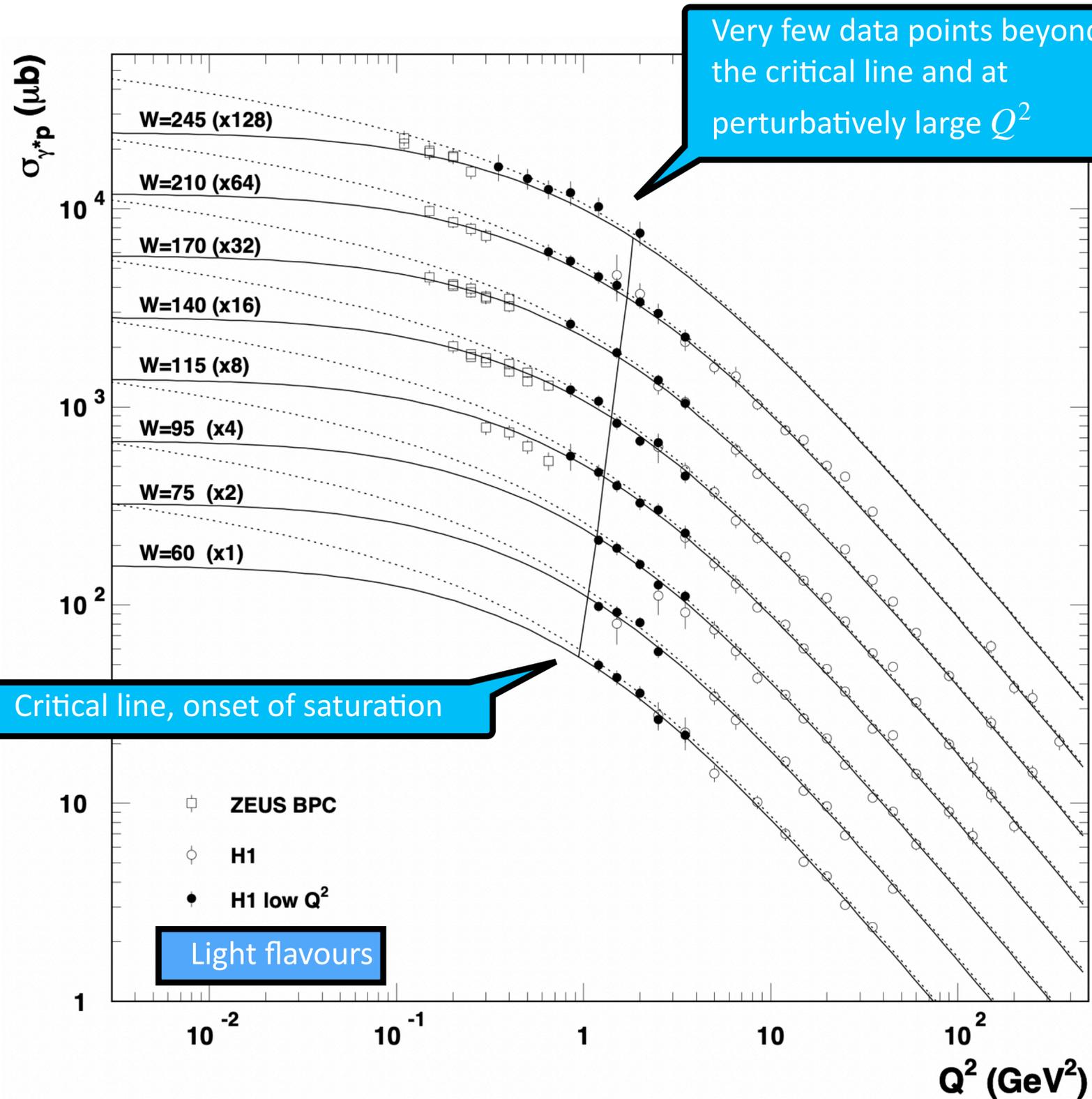
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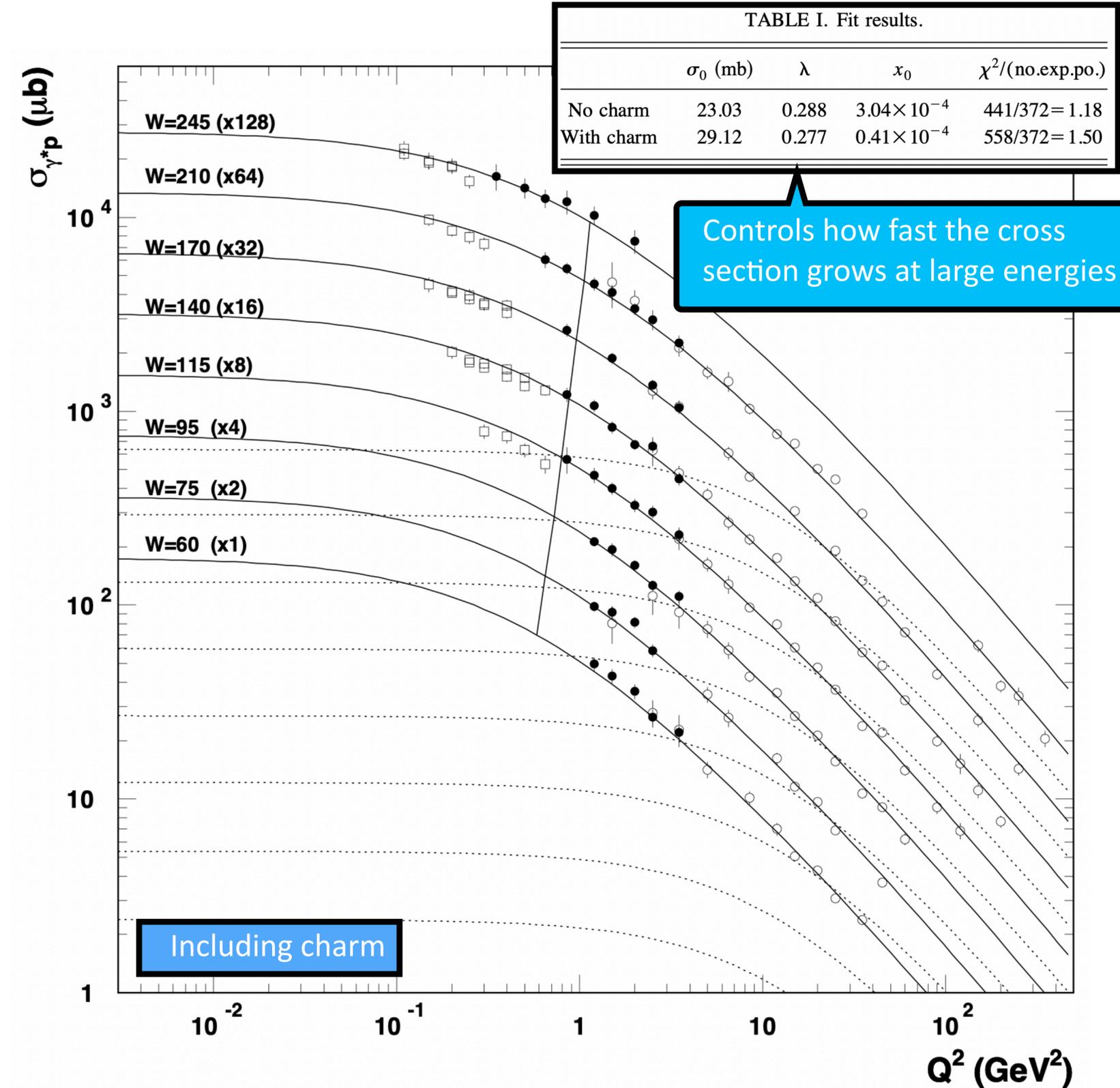
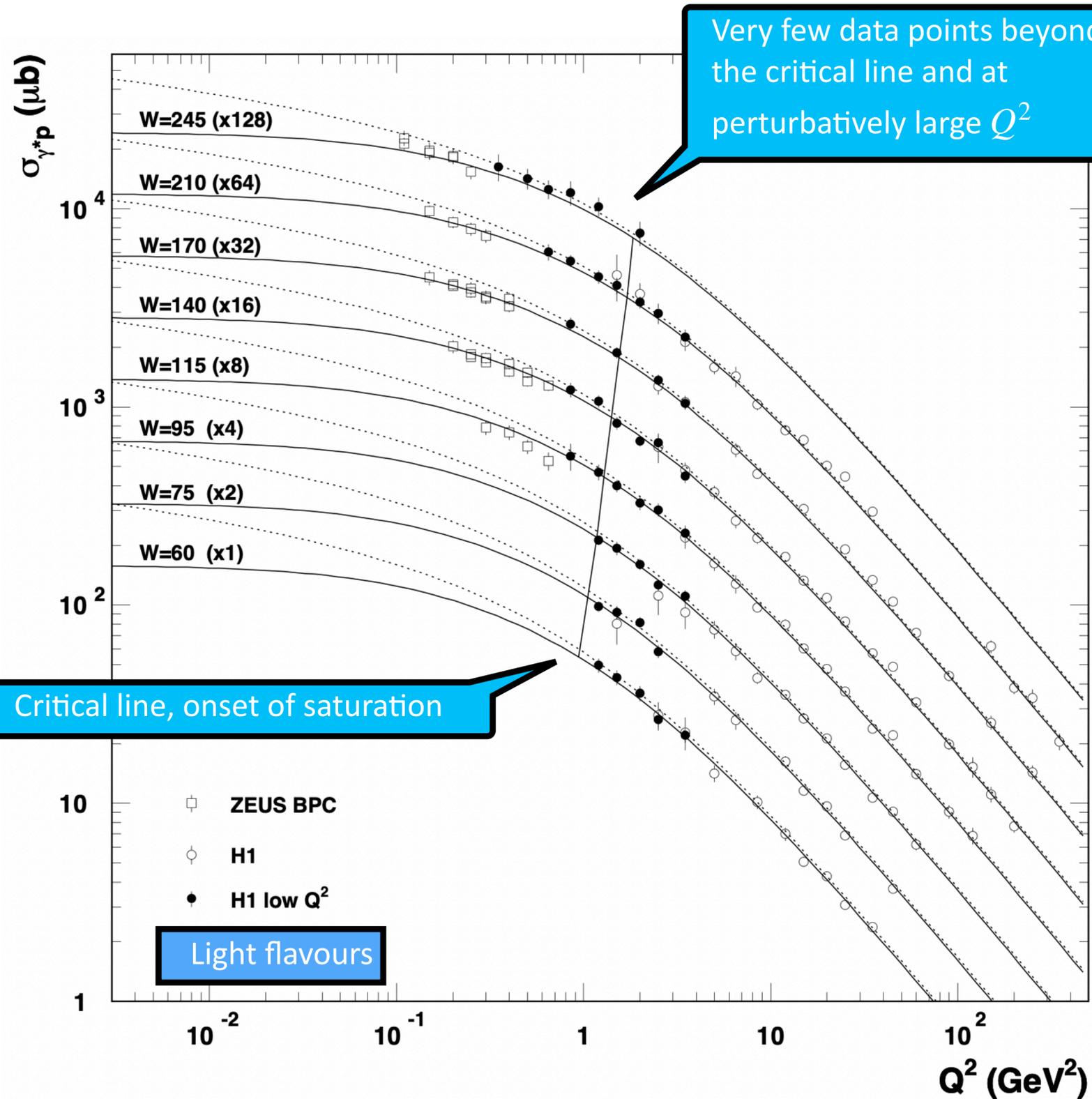
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The GBW model introduced a new scale  
Can we use it?

Geometric scaling

# 2001: Geometric scaling. (1) The formalism

## Abstract

We observe that the saturation model of deep inelastic scattering predicts a geometric scaling of the total  $\gamma^* p$  cross section in the region of small Bjorken variable  $x$ . The geometric scaling in this case means that the cross section is a function of only one dimensionless variable  $\tau = Q^2 R_0^2(x)$ , where the function  $R_0(x)$  decreases with decreasing  $x$ . We show that the experimental data from HERA in the region  $x < 0.01$  confirm the expectations of this scaling over a very broad region of  $Q^2$ . We suggest that the geometric scaling is more general than the saturation model.

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$$\sigma_{T,L}(x, Q^2) = \int d^2\mathbf{r} \int_0^1 dz |\Psi_{T,L}(r, z, Q^2)|^2 \hat{\sigma}(r, x)$$

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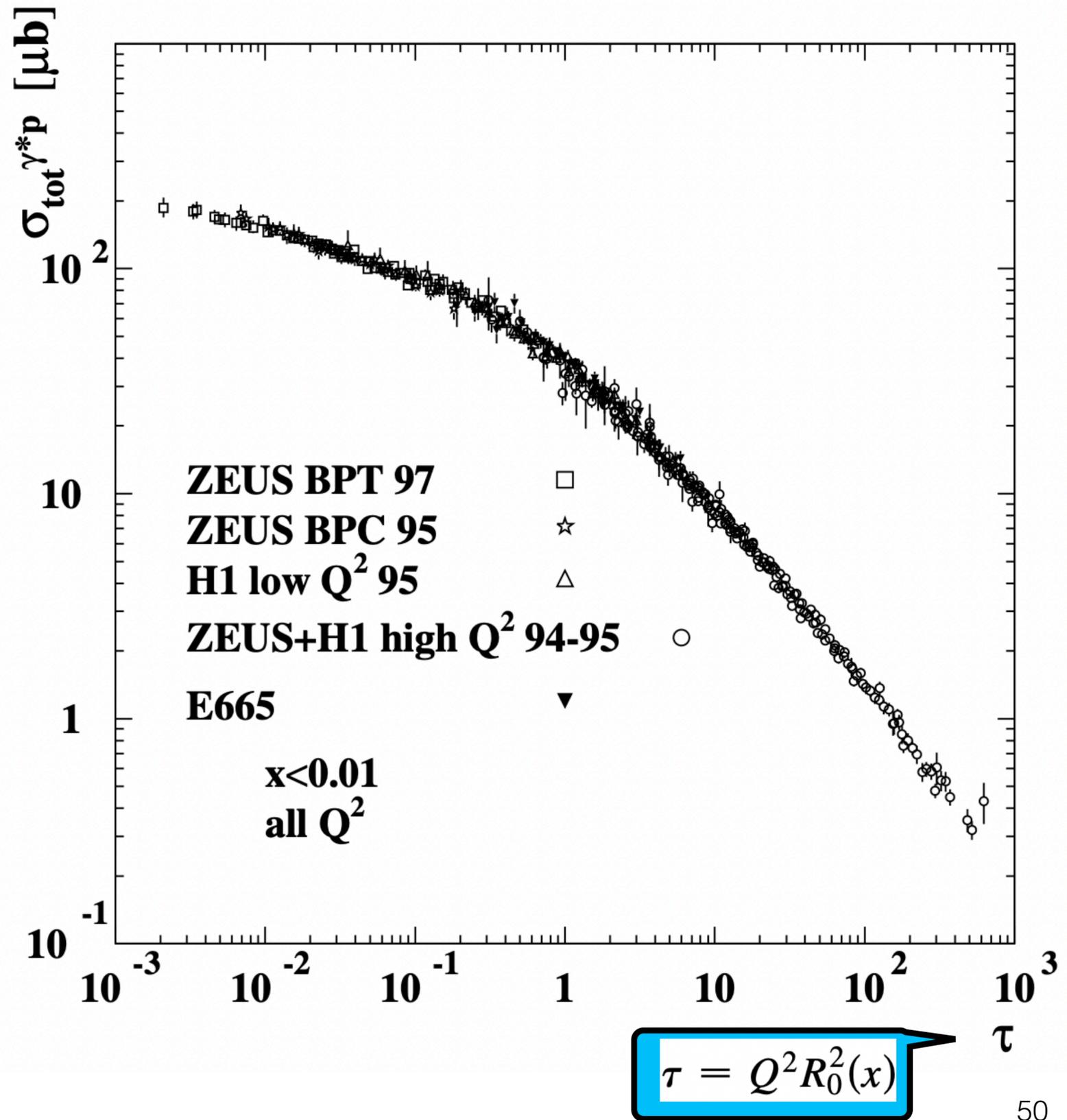
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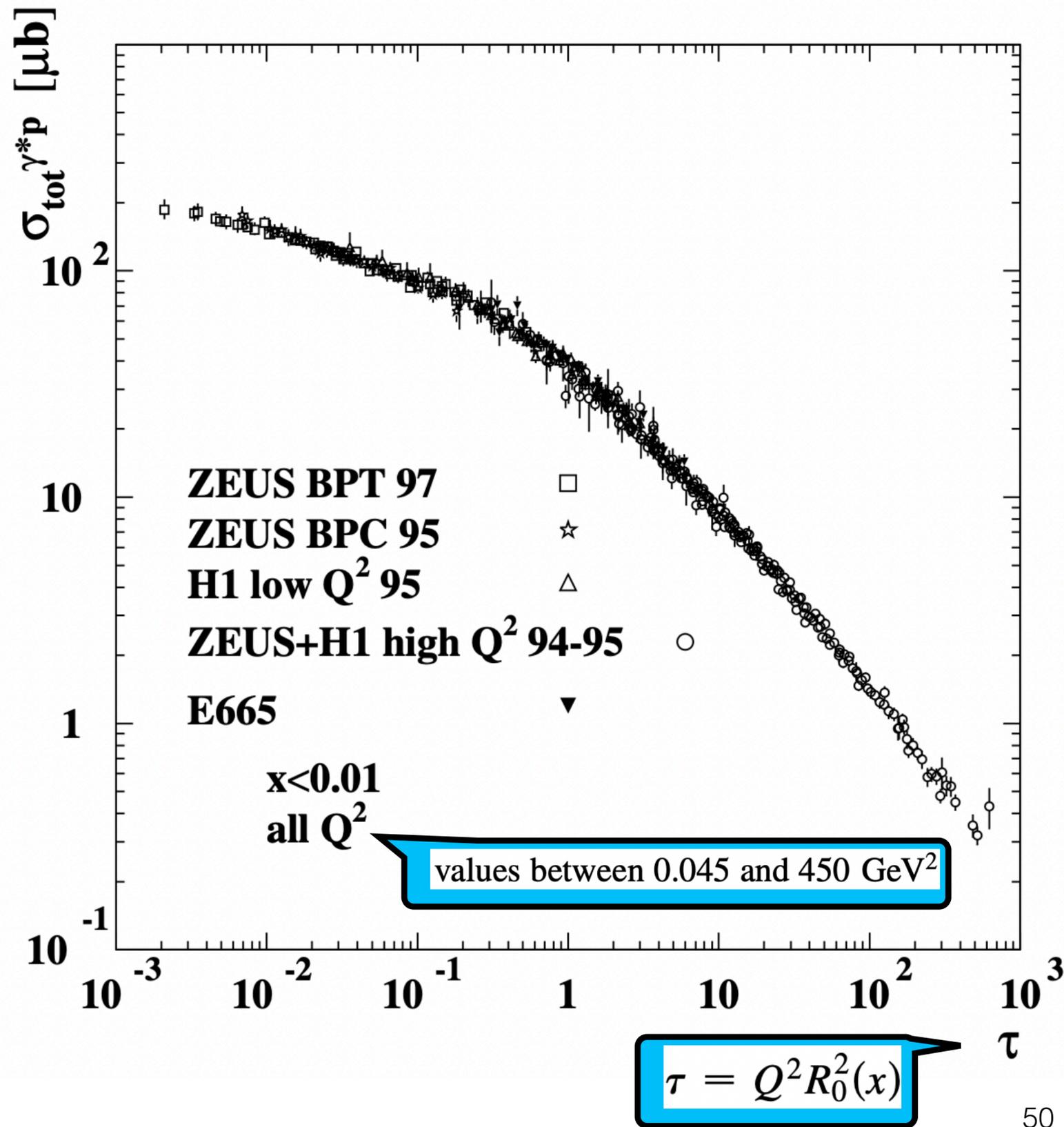
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Really?

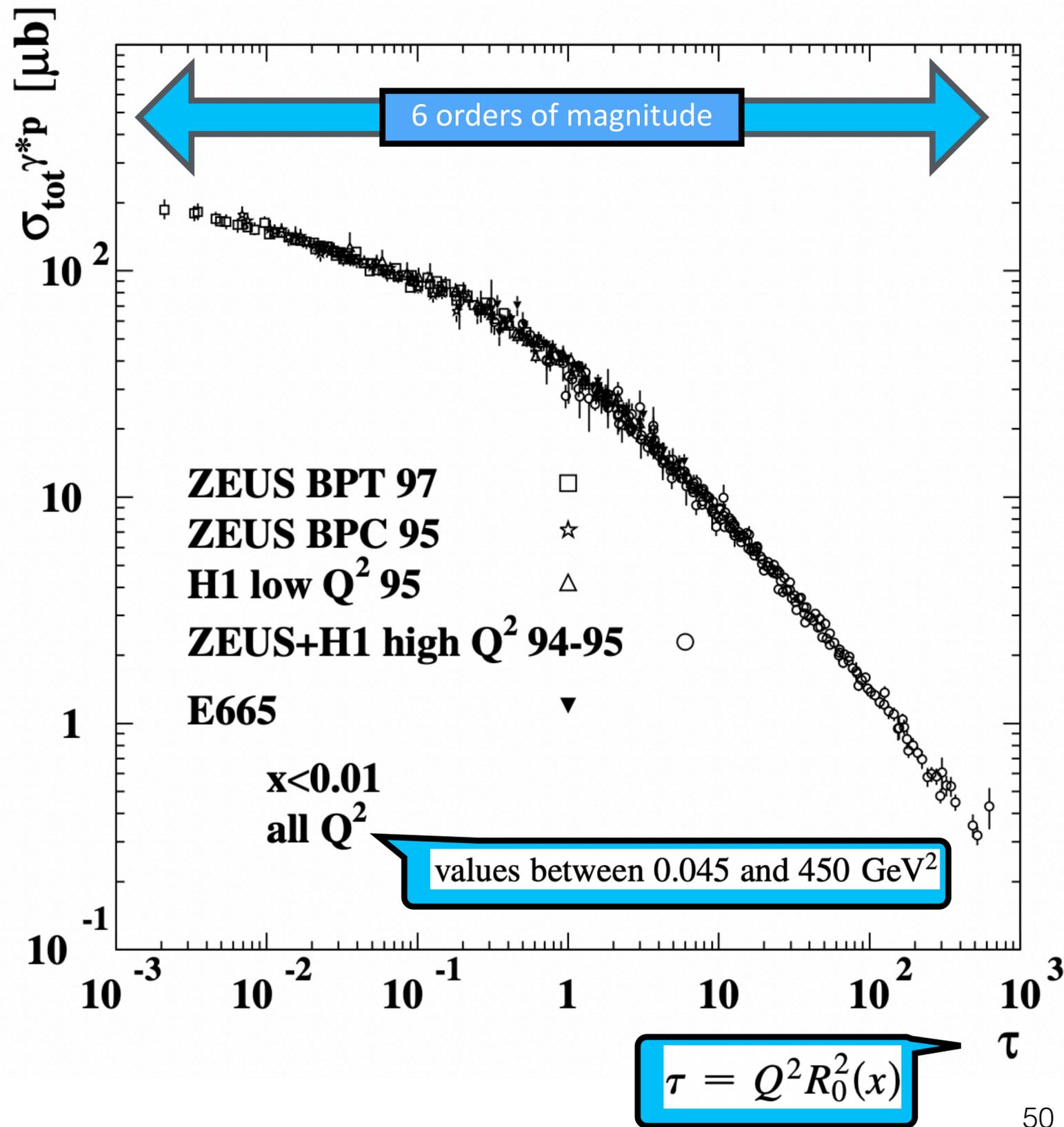
Stasto, Golec-Biernat, Kwiecinski, <http://inspirehep.net/record/530453>



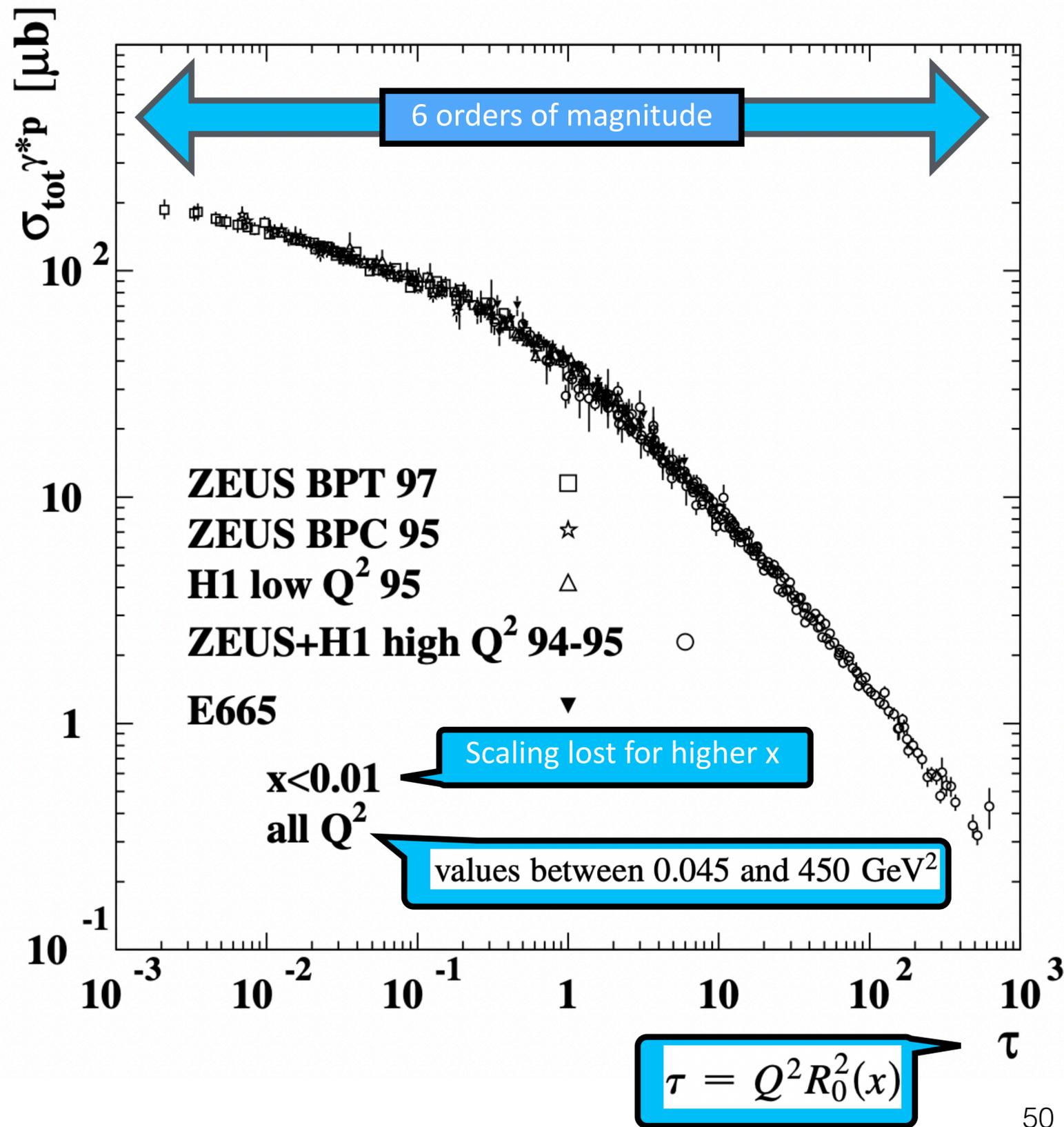
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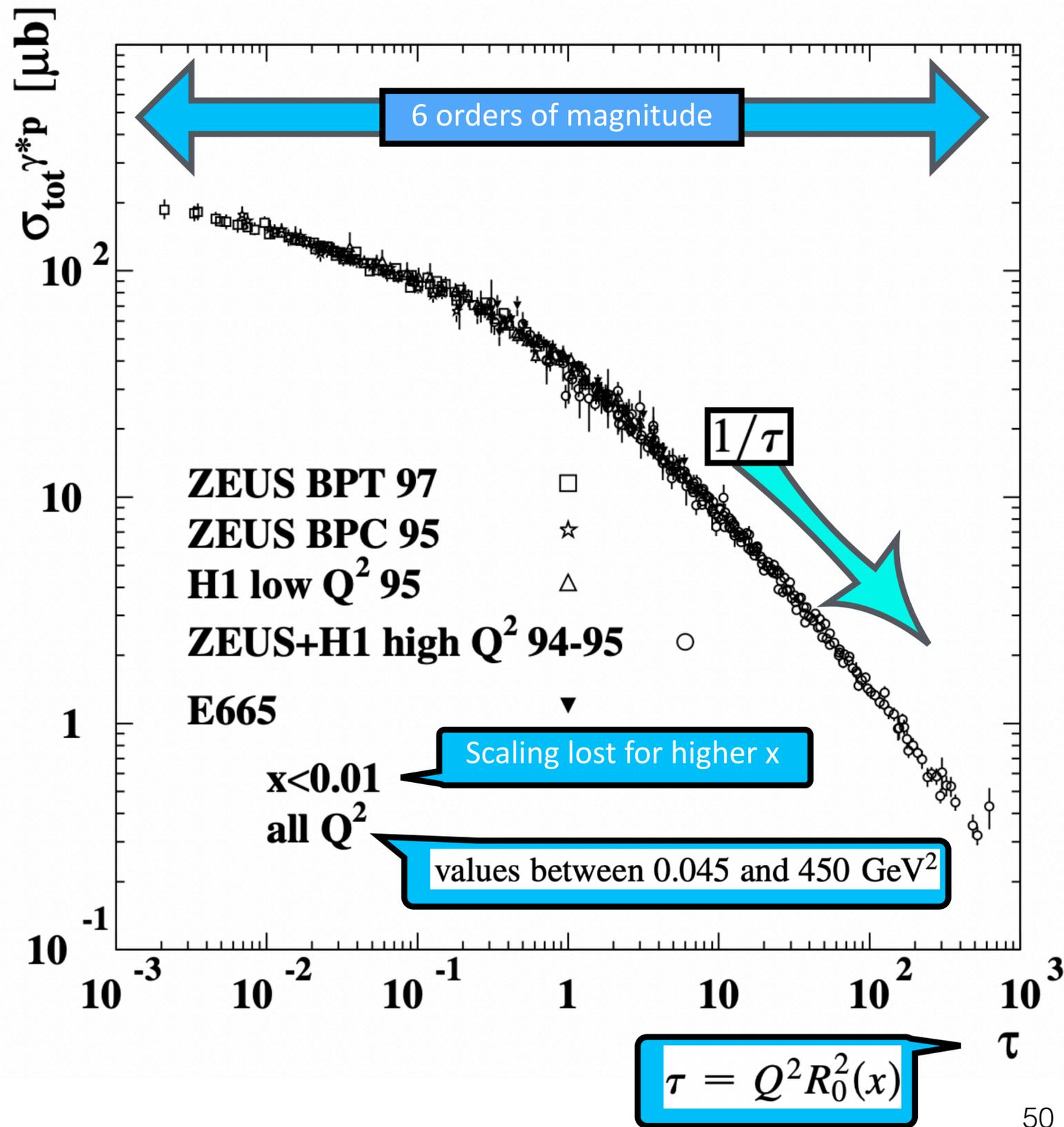
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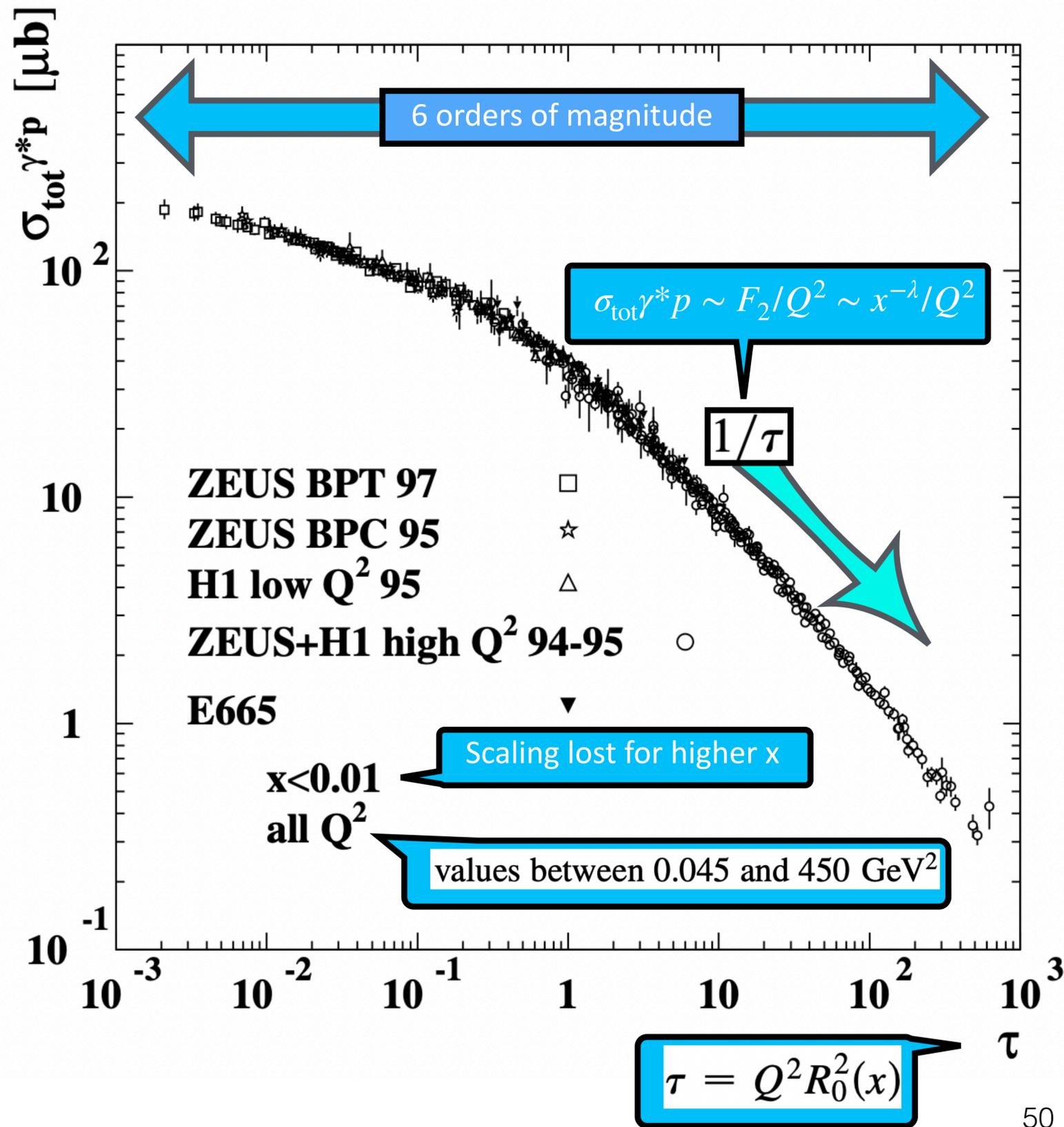
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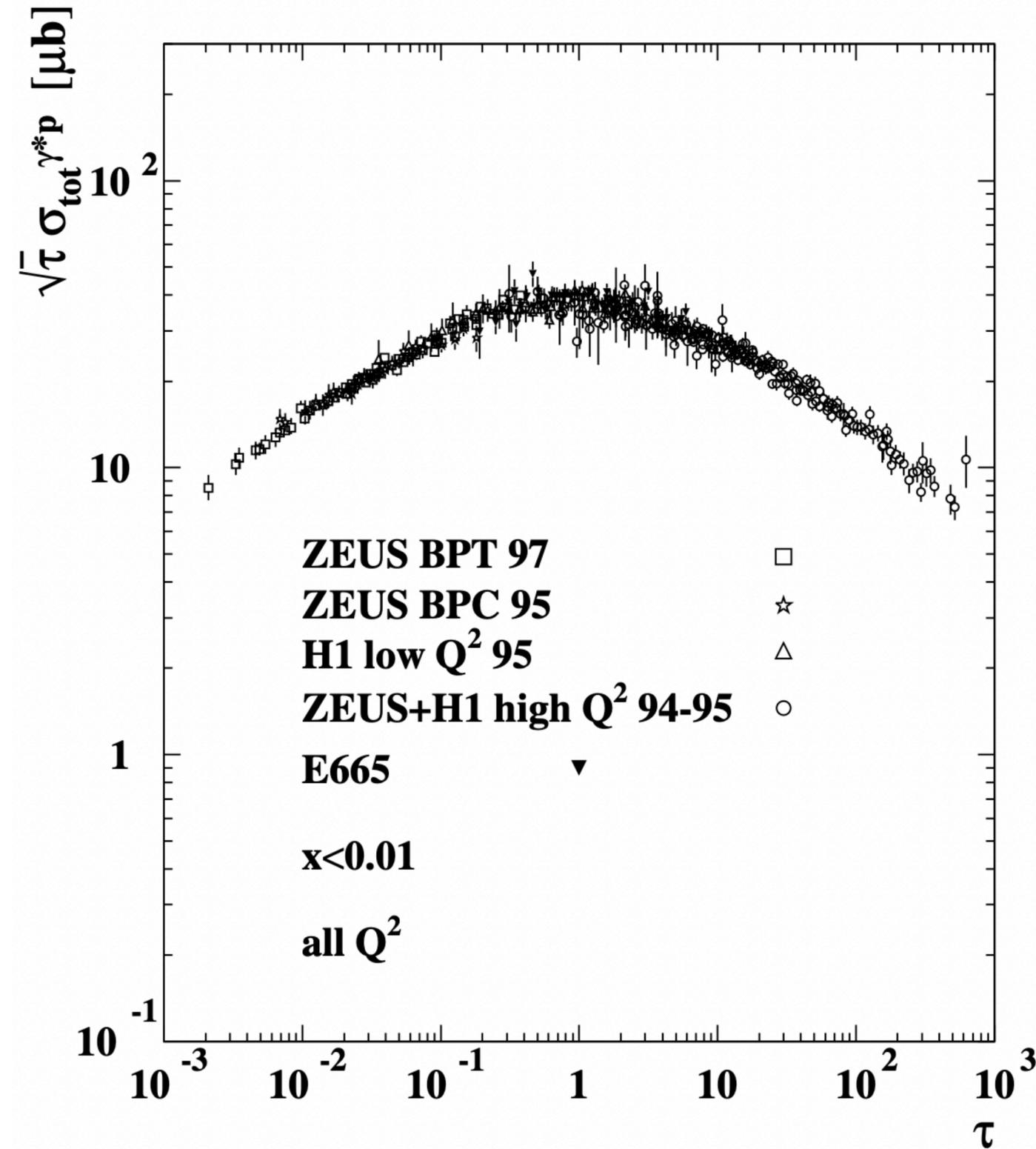
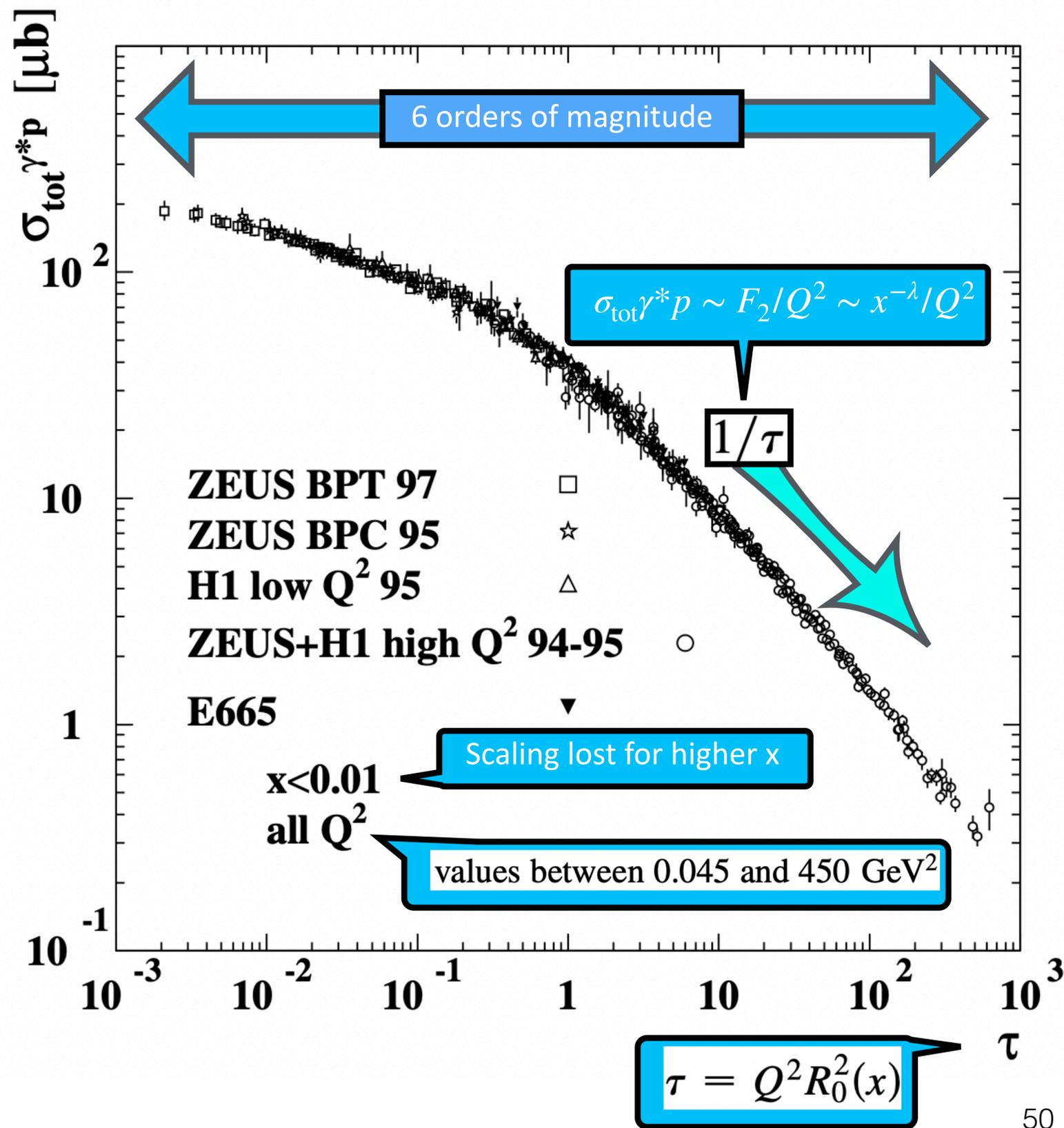
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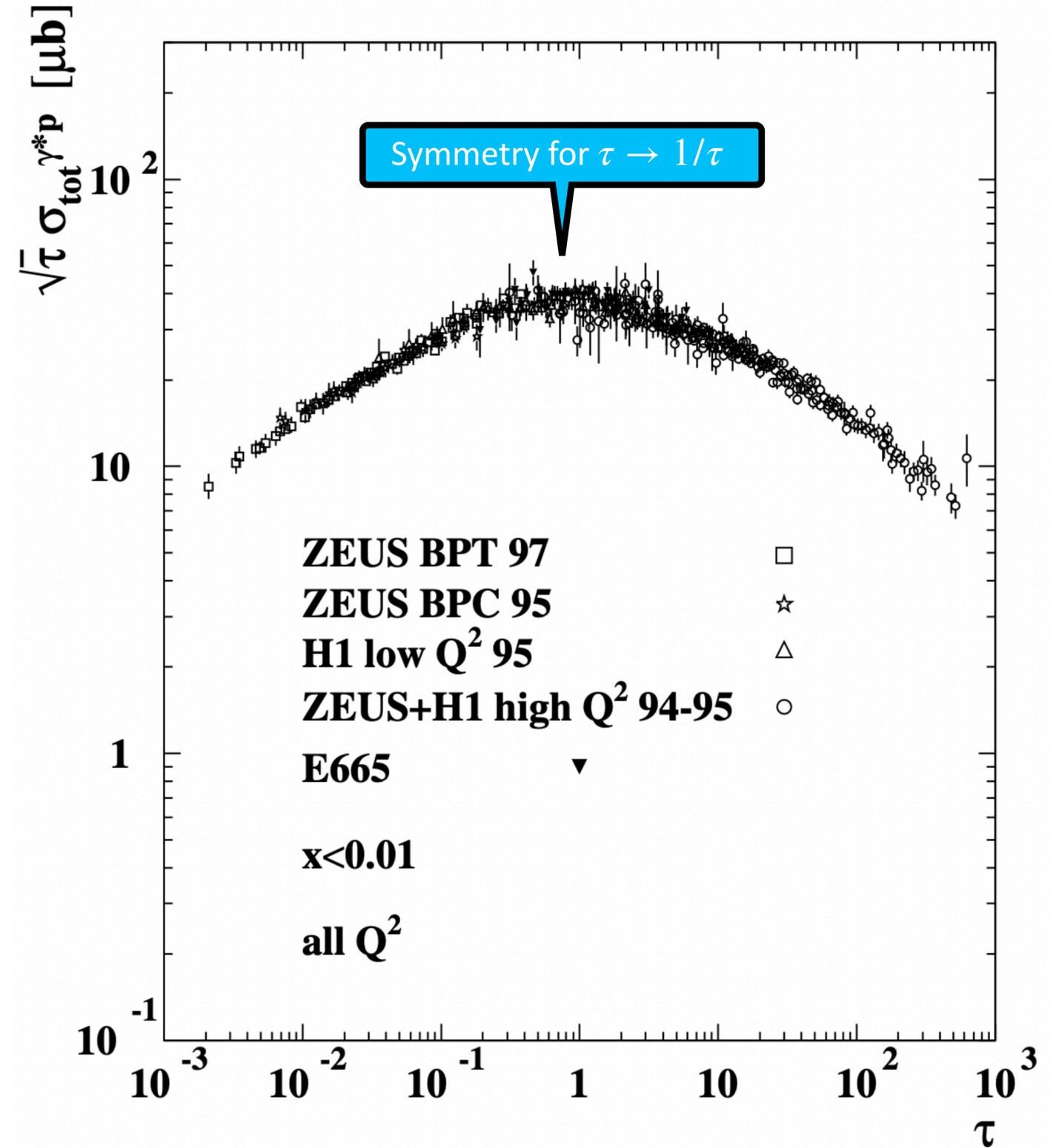
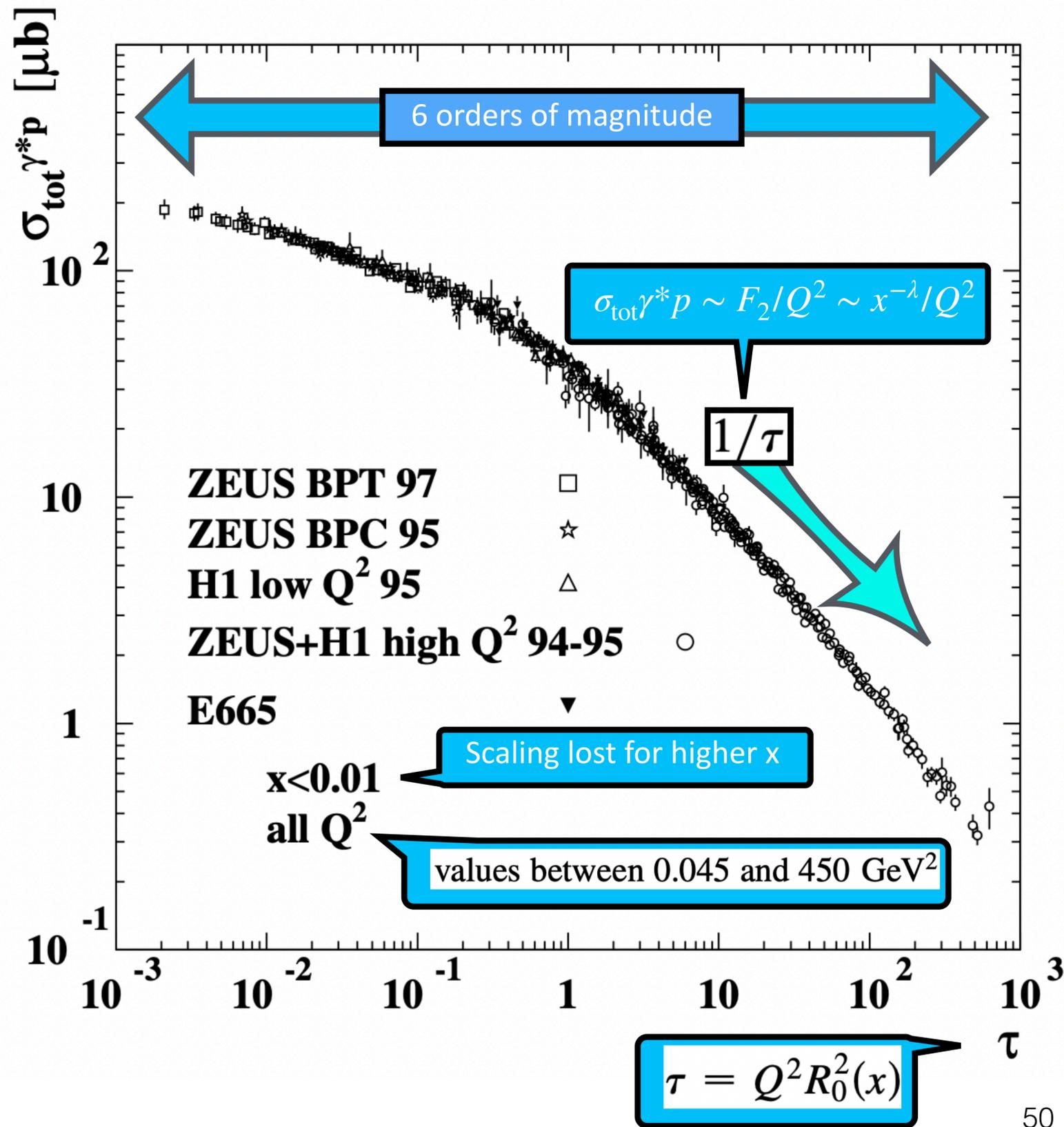
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Up to now, we have mainly used inclusive observables to study high-energy QCD  
(The exception was to look at two-jet events to 'see' the gluon directly)  
Which observables are particularly sensitive to the gluon distribution at high energies?

4

## Exploring high-energy QCD: Diffractive vector meson production at HERA

At this point in time, we know that at small Bjorken- $x$  the DIS cross section raises as a power law at high energies, we also know that this raise is driven by the gluon PDF.  
We want now to concentrate in one process that is particularly sensitive to the gluon structure of hadrons

Diffractive vector meson photoproduction

# Two experimentally important vector mesons

## EVIDENCE FOR A $\pi$ - $\pi$ RESONANCE IN THE $I=1, J=1$ STATE\*

A. R. Erwin, R. March, W. D. Walker, and E. West

Brookhaven National Laboratory, Upton, New York and University of Wisconsin, Madison, Wisconsin  
(Received May 11, 1961)

<https://inspirehep.net/literature/28197>  
<https://inspirehep.net/literature/48851>

### The $\rho(770)$

- ✓ Discovered in 1961
- ✓ Decays mainly to  $\pi\pi$  pairs
- ✓ Large width, strong interference with continuum

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### The $J/\psi$ (mass $3.097 \text{ GeV}/c^2$ )

- ✓ Discovered in 1974 (November revolution)
- ✓ Useful decays into lepton pairs
- ✓ Very small width (clean signature)

## Experimental Observation of a Heavy Particle $J^\dagger$

J. J. Aubert, U. Becker, P. J. Biggs, J. Burger, M. Chen, G. Everhart, P. Goldhagen, J. Leong, T. McCorrison, T. G. Rhoades, M. Rohde, Samuel C. C. Ting, and Sau Lan Wu  
*Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

and

Y. Y. Lee

*Brookhaven National Laboratory, Upton, New York 11973*  
(Received 12 November 1974)

## Discovery of a Narrow Resonance in $e^+e^-$ Annihilation\*

J.-E. Augustin,† A. M. Boyarski, M. Breidenbach, F. Bulos, J. T. Dakin, G. J. Feldman, G. E. Fischer, D. Fryberger, G. Hanson, B. Jean-Marie,† R. R. Larsen, V. Lüth, H. L. Lynch, D. Lyon, C. C. Morehouse, J. M. Paterson, M. L. Perl, B. Richter, P. Rapidis, R. F. Schwitters, W. M. Tanenbaum, and F. Vannucci‡

*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

and

G. S. Abrams, D. Briggs, W. Chinowsky, C. E. Friedberg, G. Goldhaber, R. J. Hollebeek, J. A. Kadyk, B. Lulu, F. Pierre,§ G. H. Trilling, J. S. Whitaker, J. Wiss, and J. E. Zipse

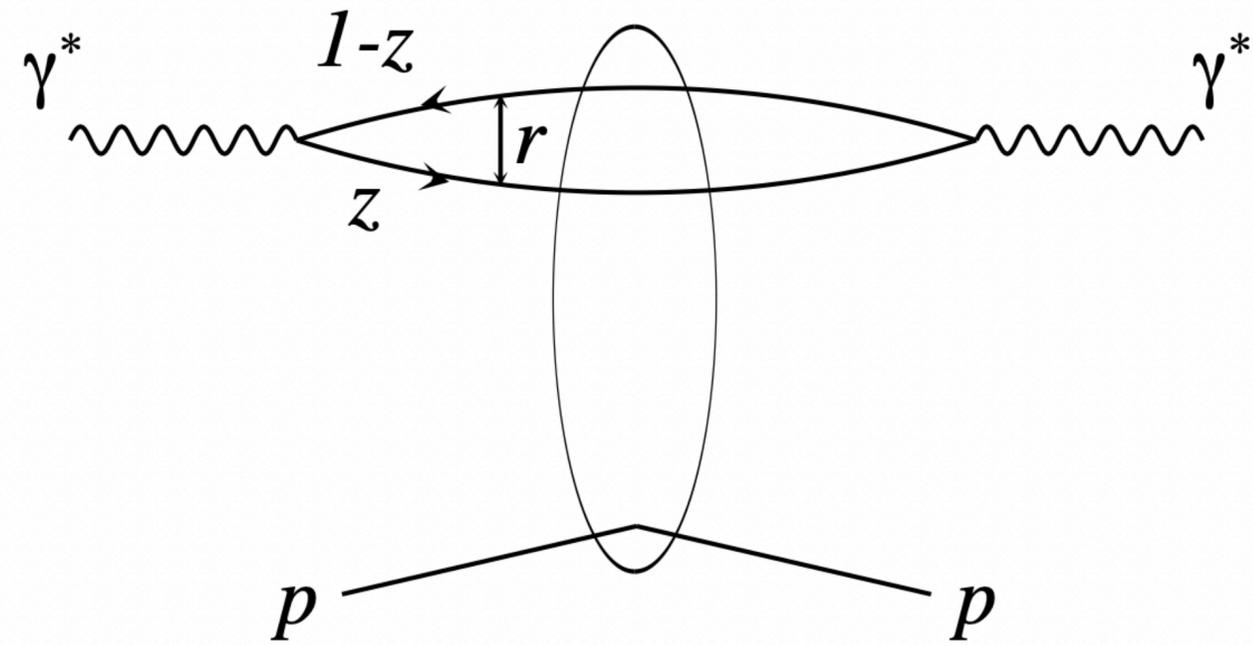
*Lawrence Berkeley Laboratory and Department of Physics, University of California, Berkeley, California 94720*  
(Received 13 November 1974)

<https://inspirehep.net/literature/90773>

<https://inspirehep.net/literature/91761>

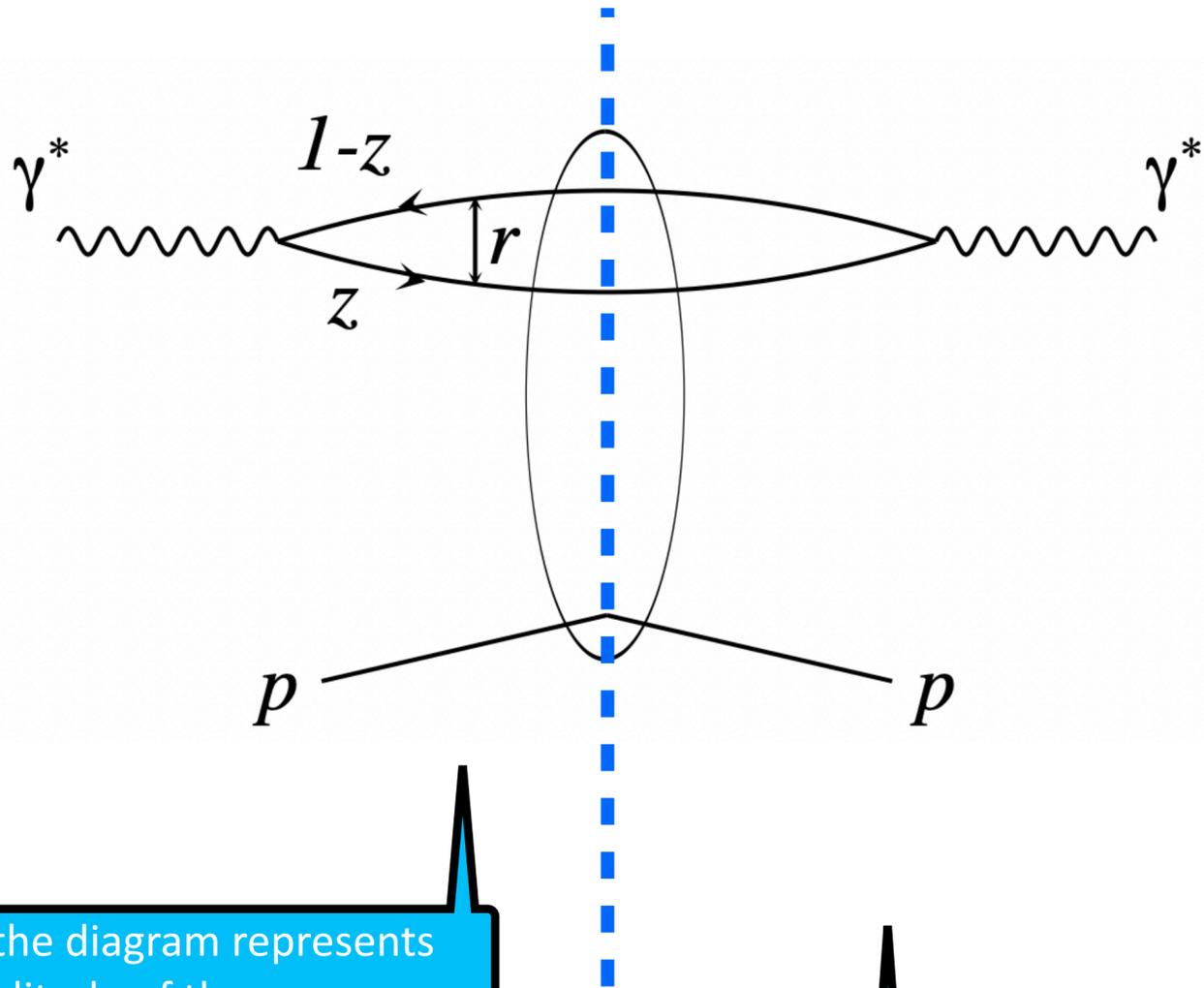
# Diffractive vector meson production: a process close to DIS

A representation of the DIS cross section



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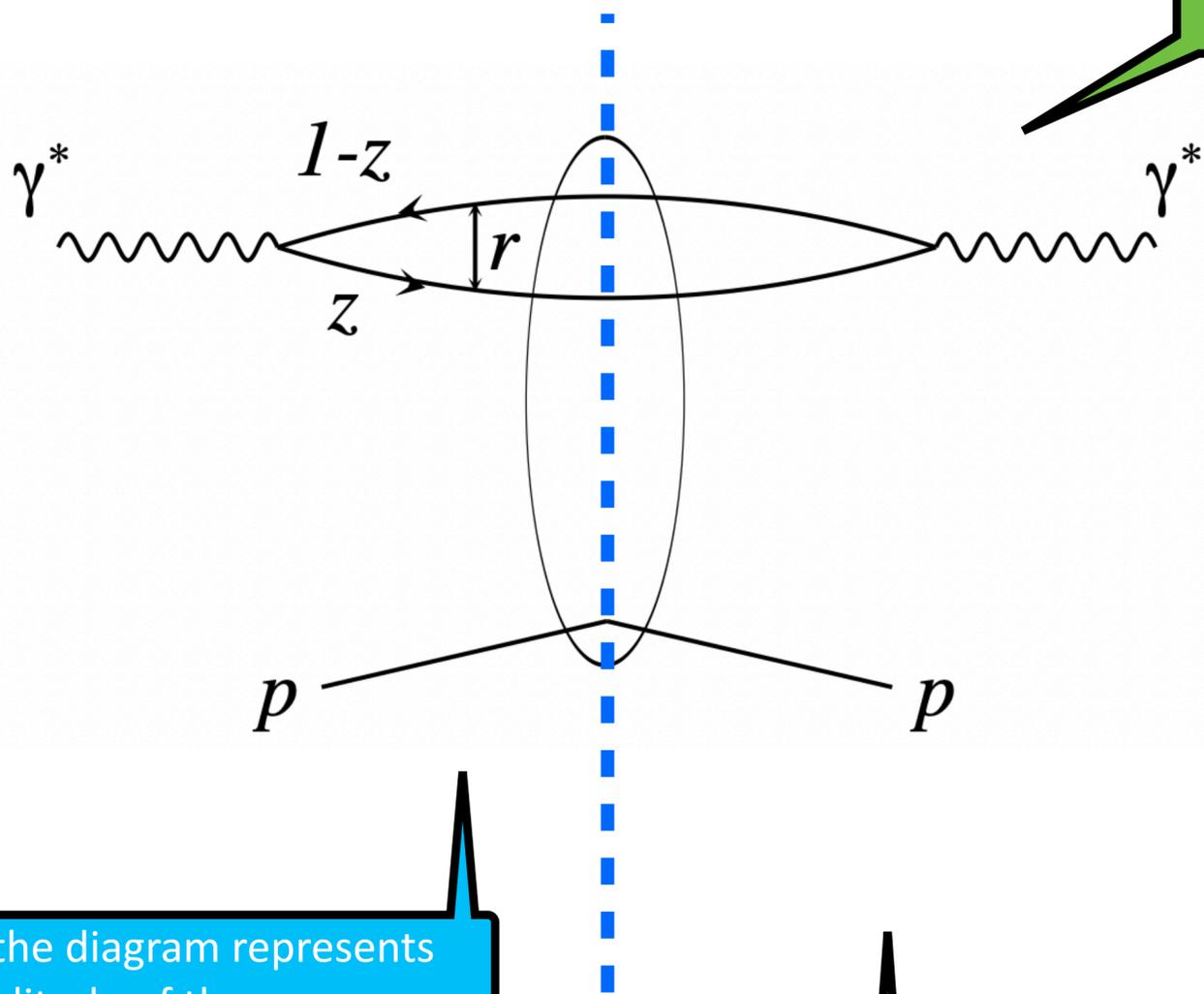
Half of the diagram represents the amplitude of the process

The other half the conjugate of the amplitude

# Diffractive vector meson production: a process close to DIS

A representation of the DIS cross section

Now consider the full diagram to represent an amplitude, not a cross section ... then ...

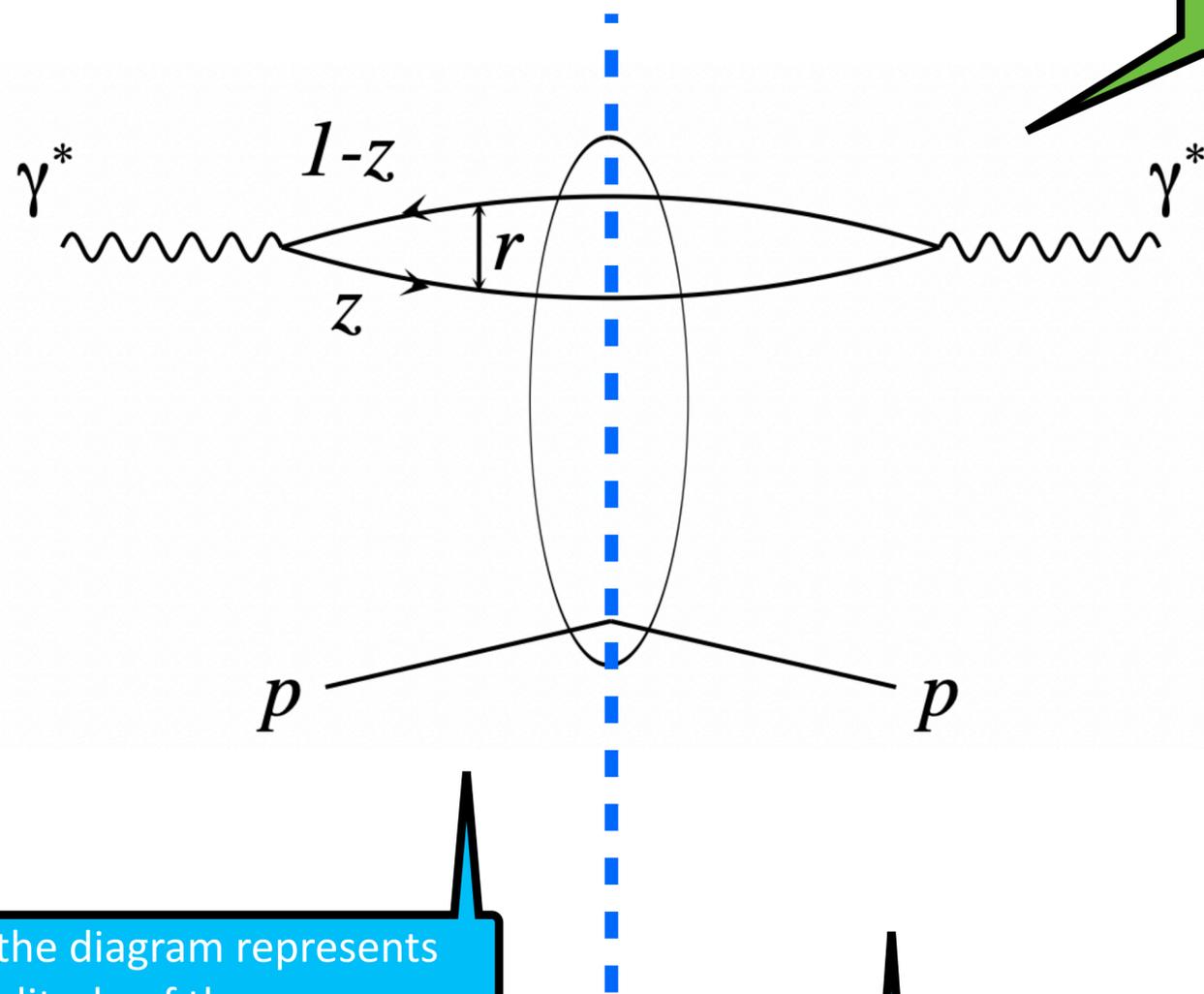


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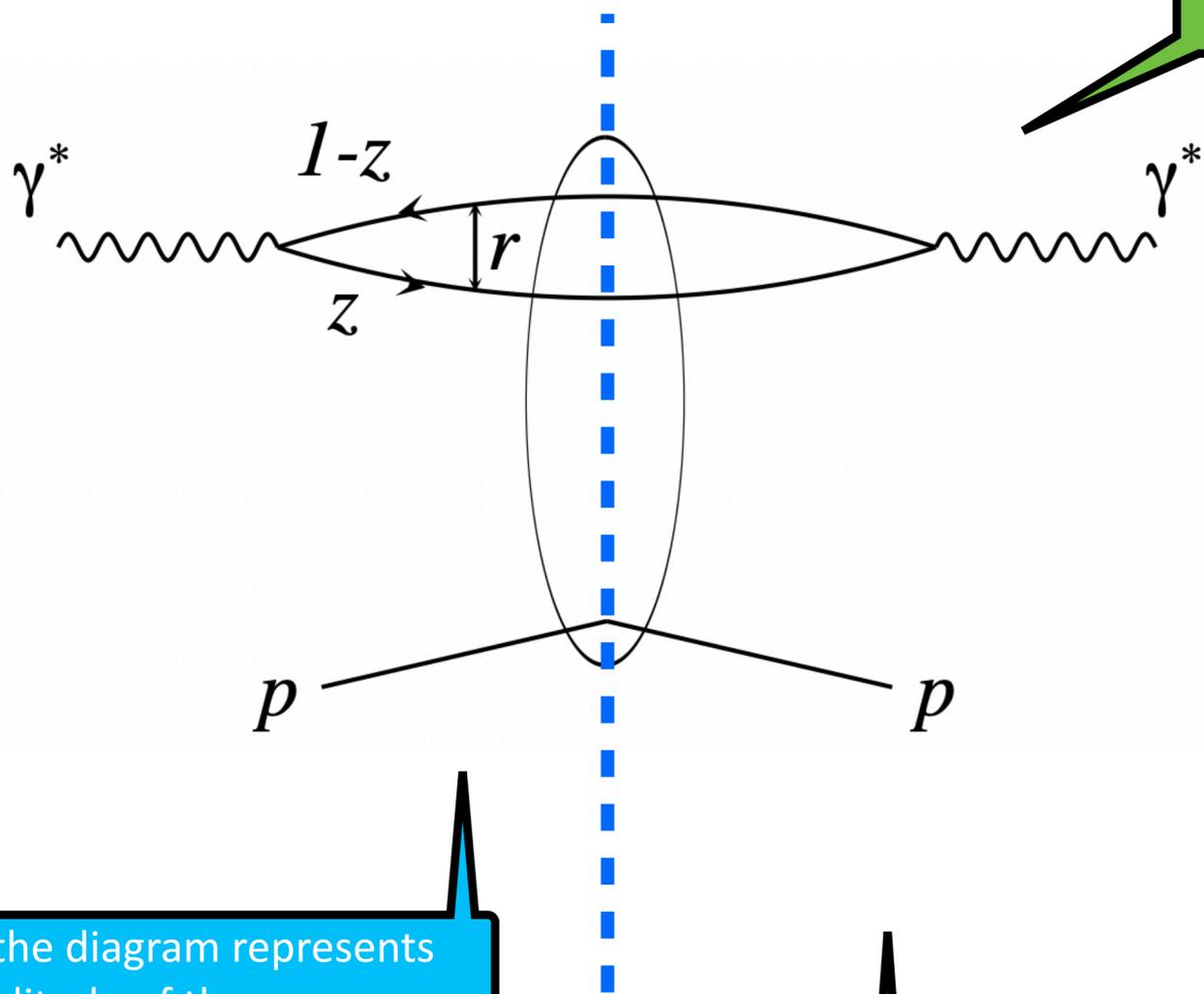
... exchange the photon for another particle with the same quantum numbers, e. g. a vector meson

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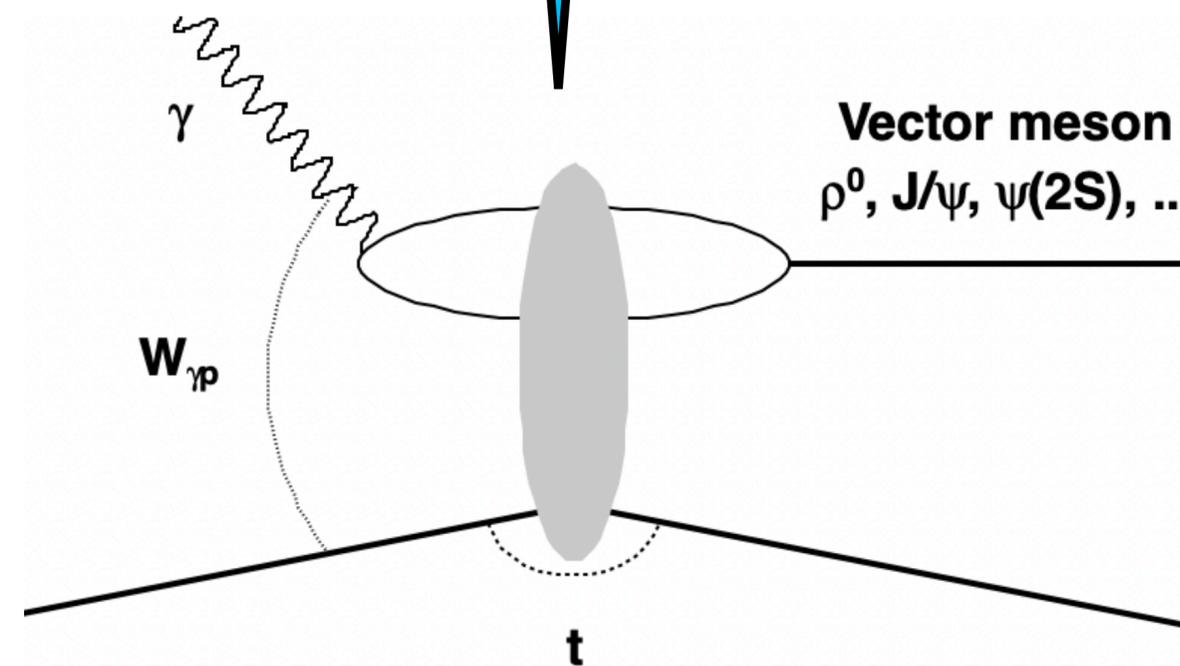
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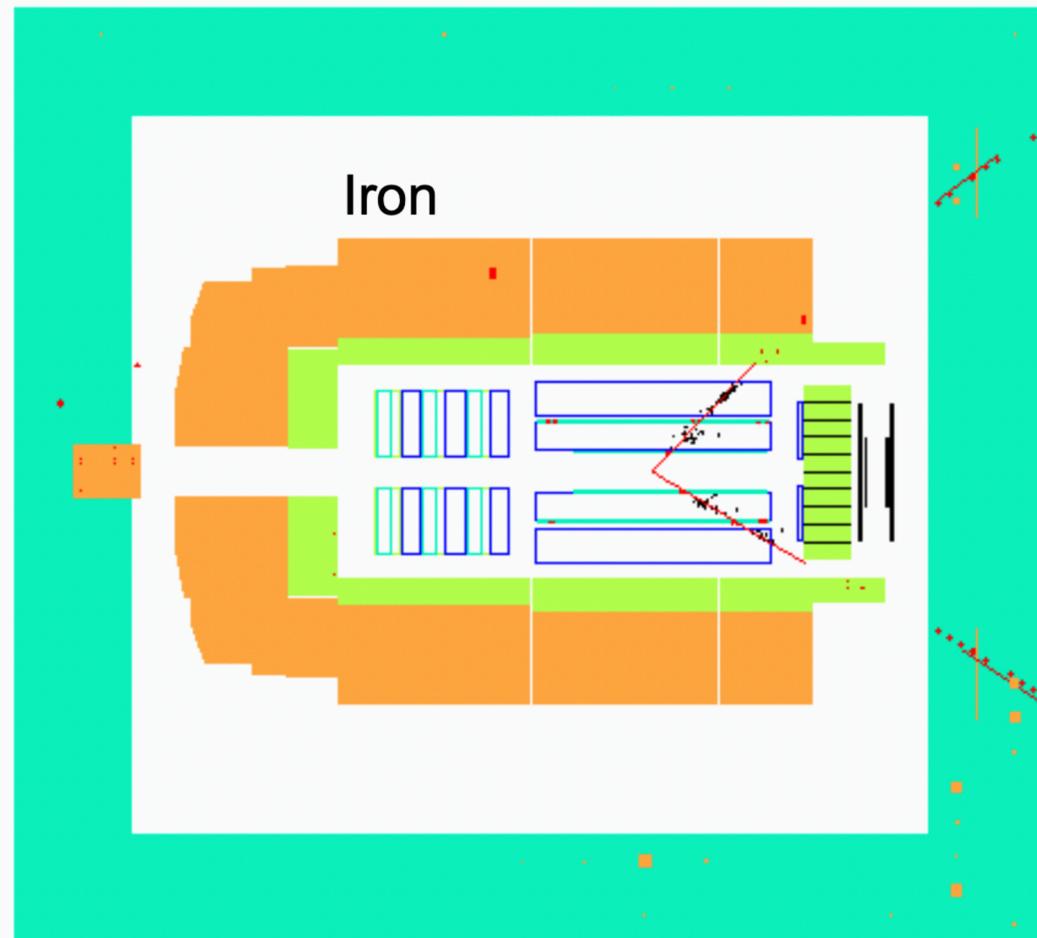
This would be a diffractive process where the protons remains intact after the interaction



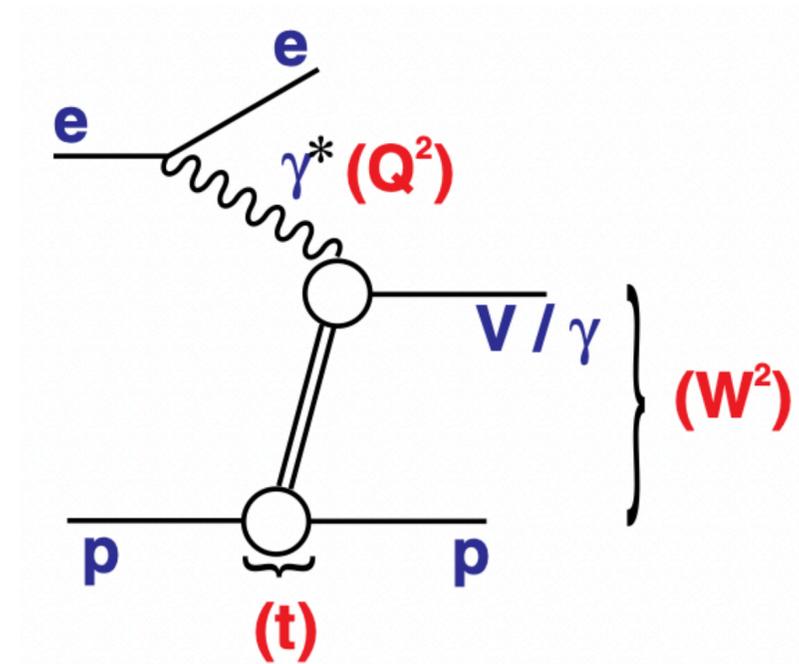
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Photoproduction  $J/\Psi \rightarrow \mu \mu$

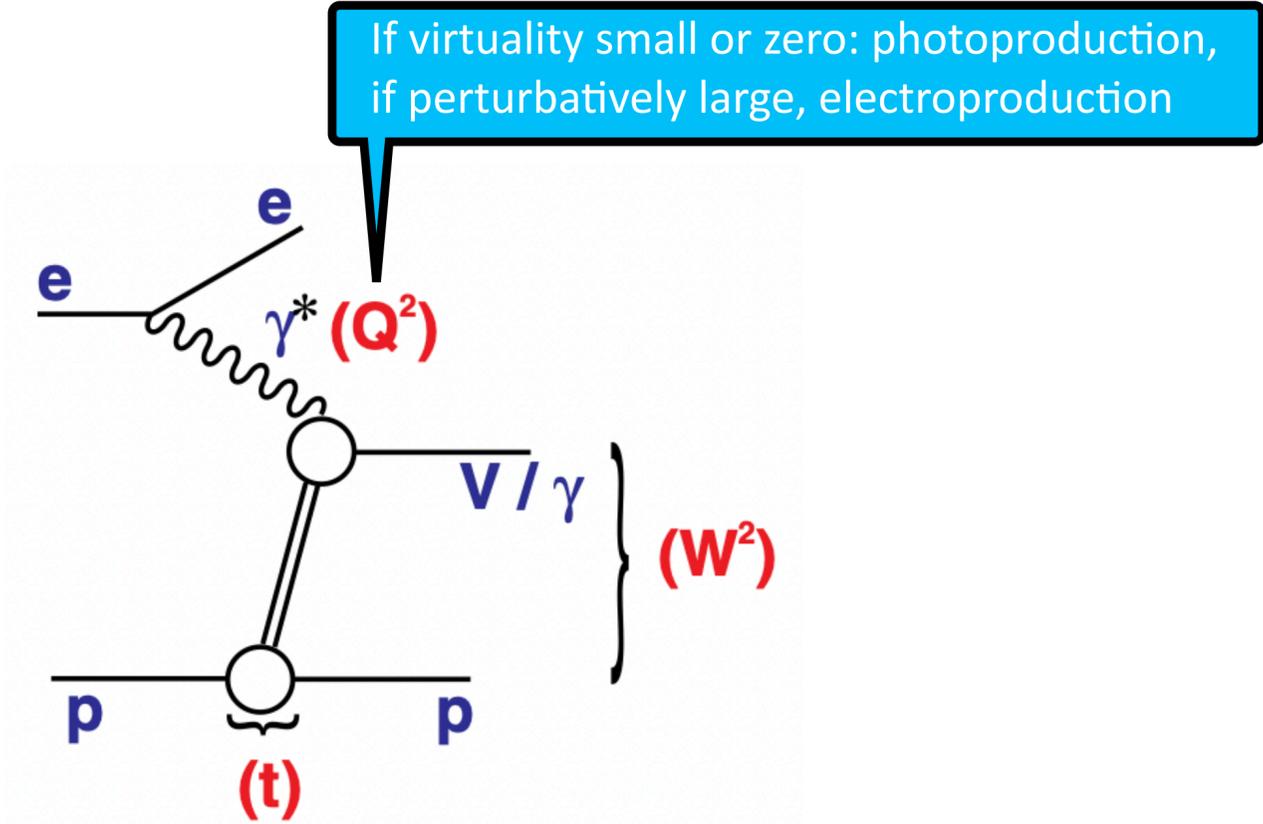


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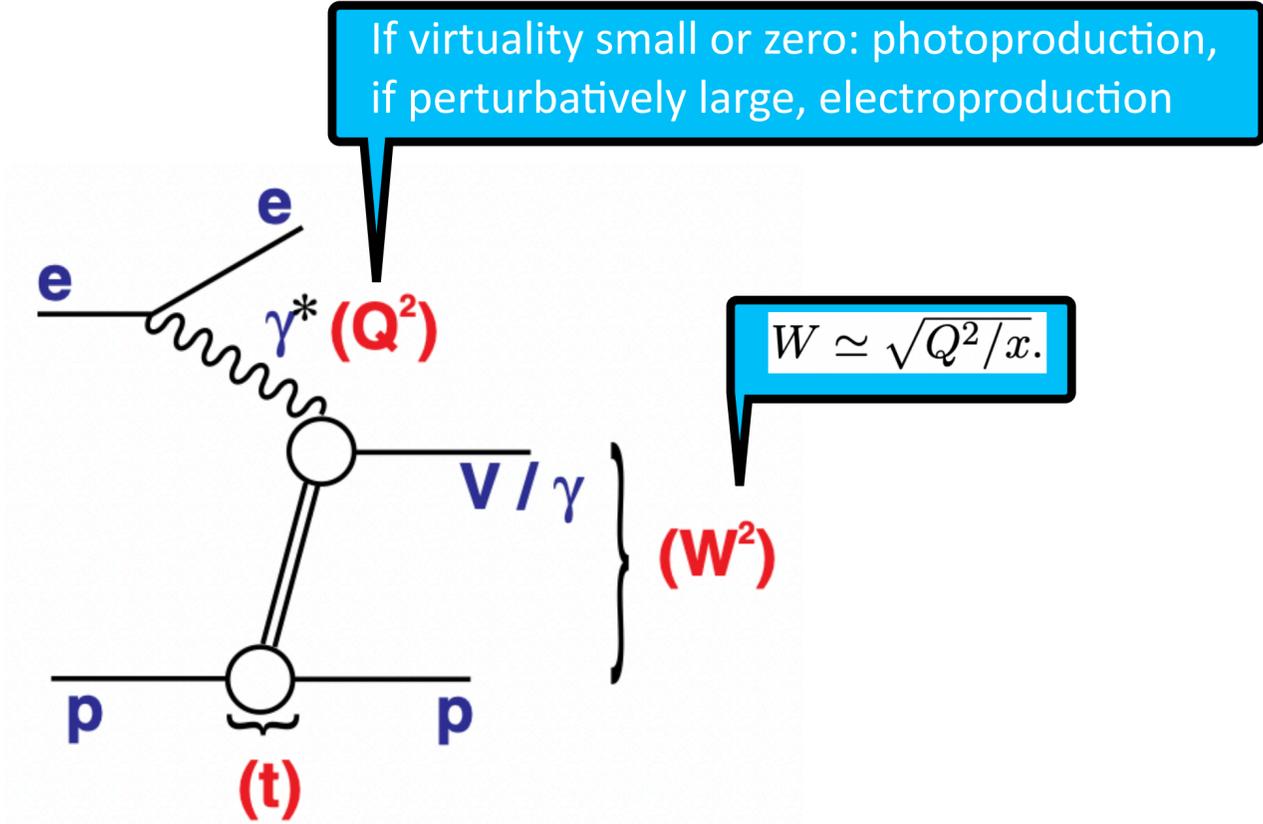
Newman, Wing, <https://inspirehep.net/literature/1247974>

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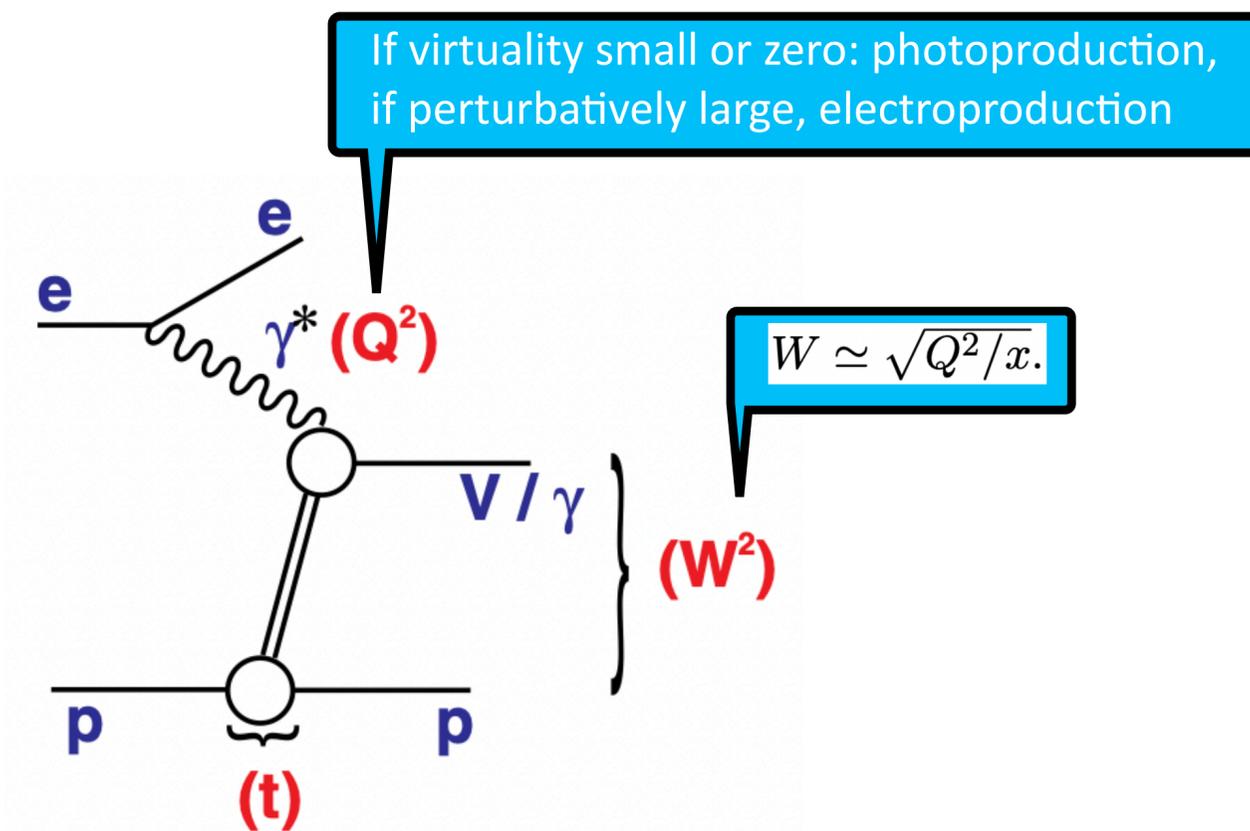
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If virtuality small or zero: photoproduction, if perturbatively large, electroproduction

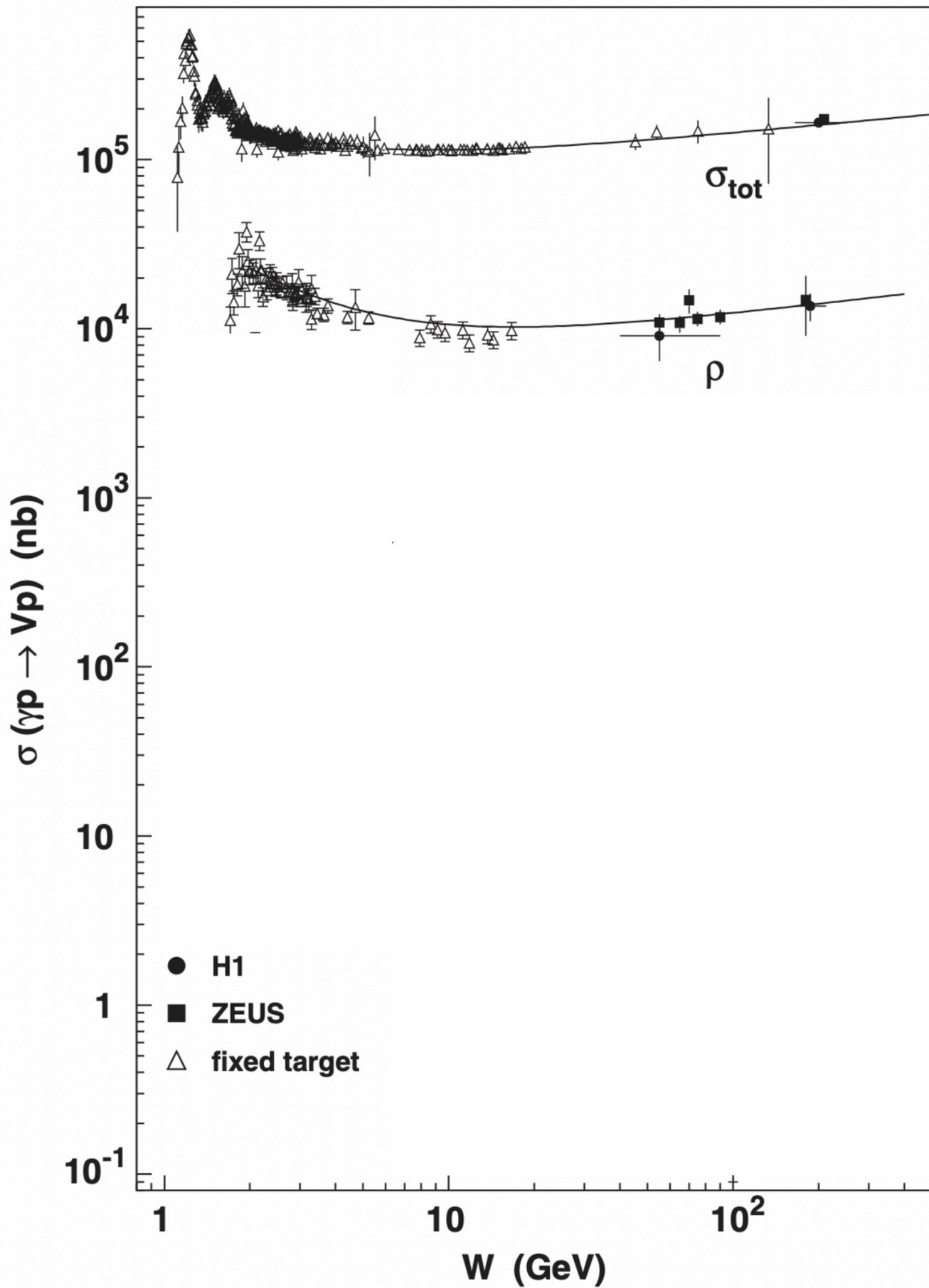
$$W \simeq \sqrt{Q^2/x}$$

Related, through a Fourier transform, to the distribution of colour fields in the transverse plane

Newman, Wing, <https://inspirehep.net/literature/1247974>

Guillermo Contreras, CTU in Prague

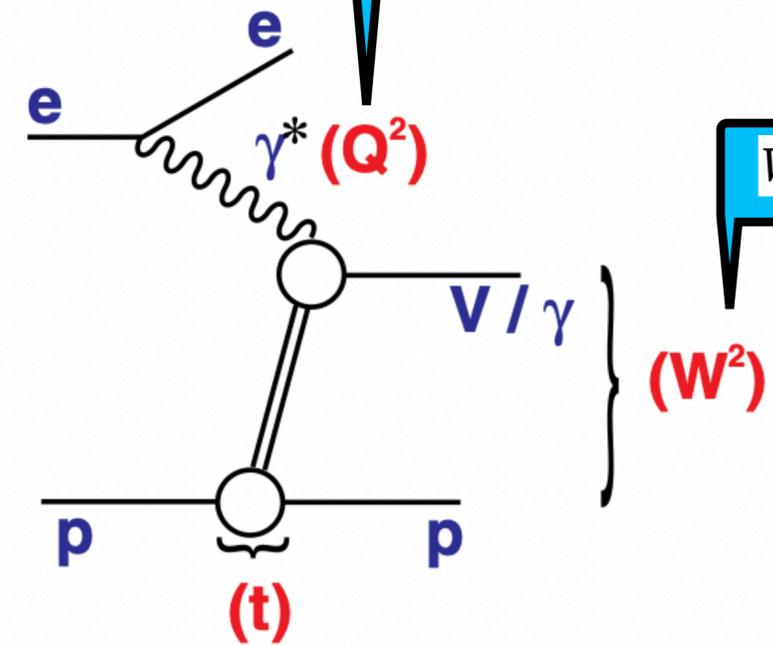
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Total photoproduction cross section

$\rho(770)$  photoproduction cross section

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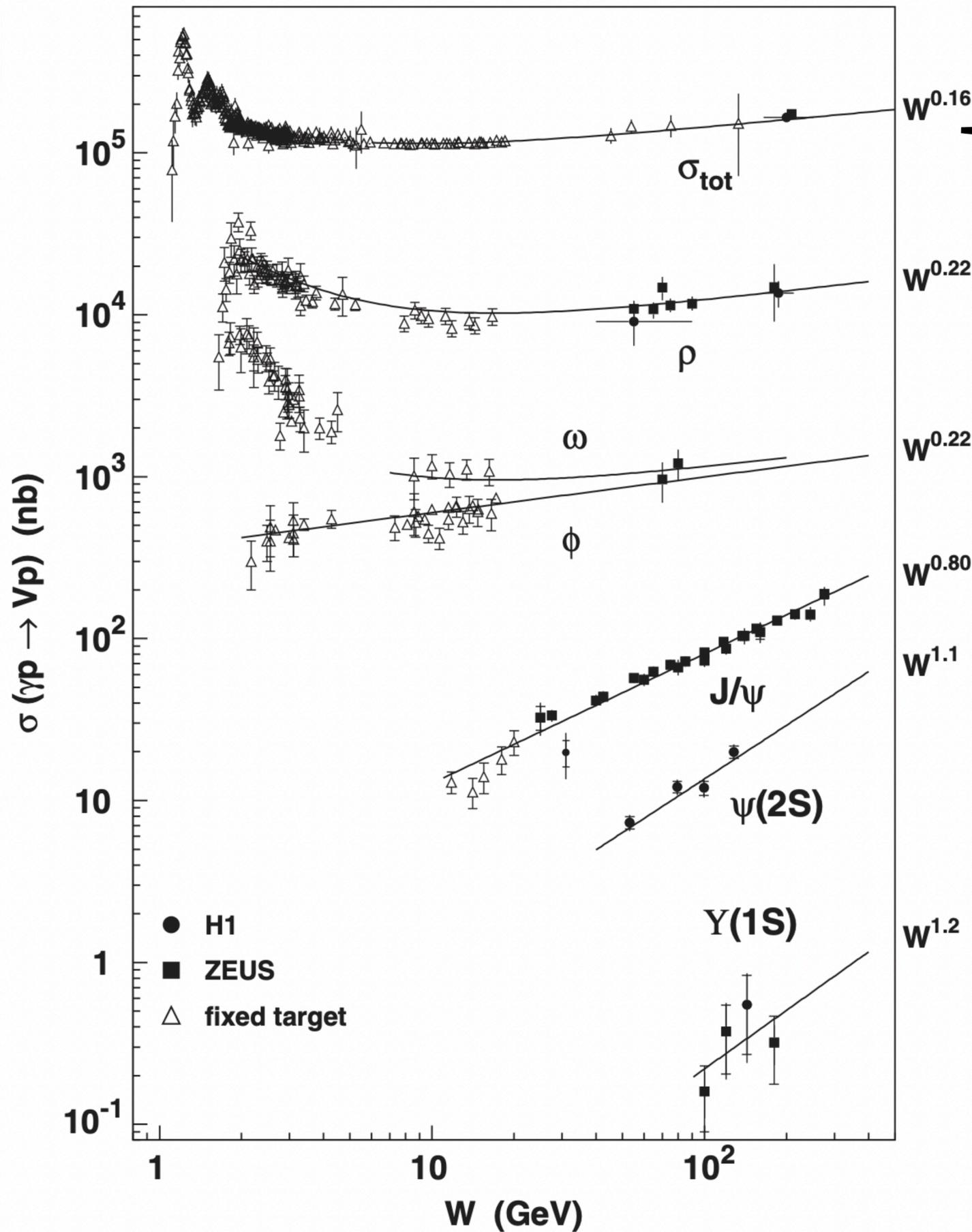


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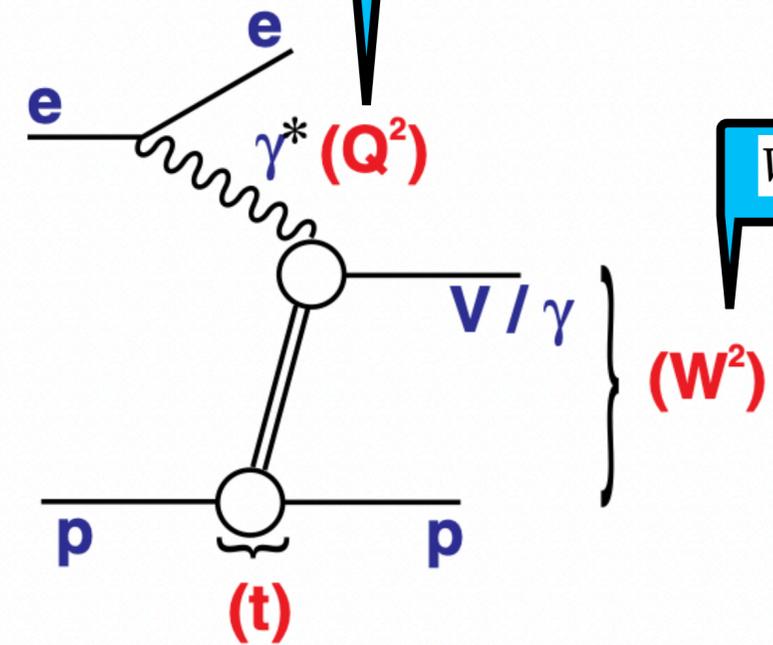
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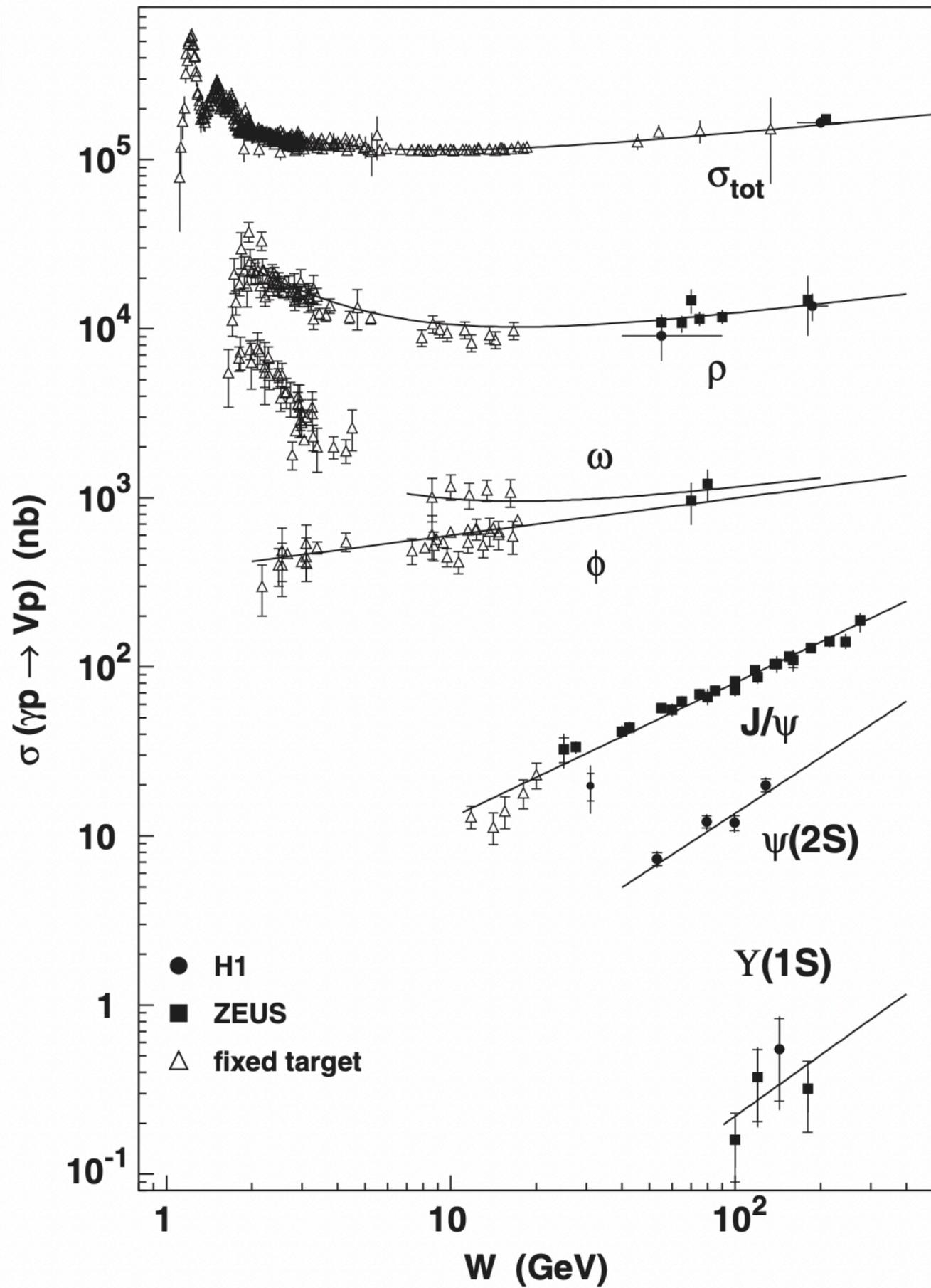


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$W^{0.16}$

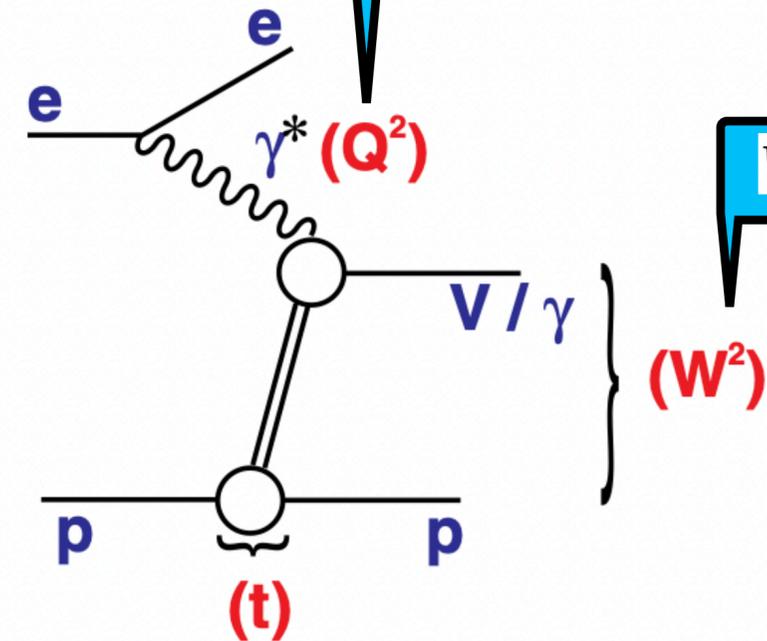
Total photoproduction cross section

$W^{0.22}$

$\rho(770)$  photoproduction cross section

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If virtuality small or zero: photoproduction, if perturbatively large, electroproduction



$W \simeq \sqrt{Q^2/x}$

$W^{0.80}$

$W^{1.1}$

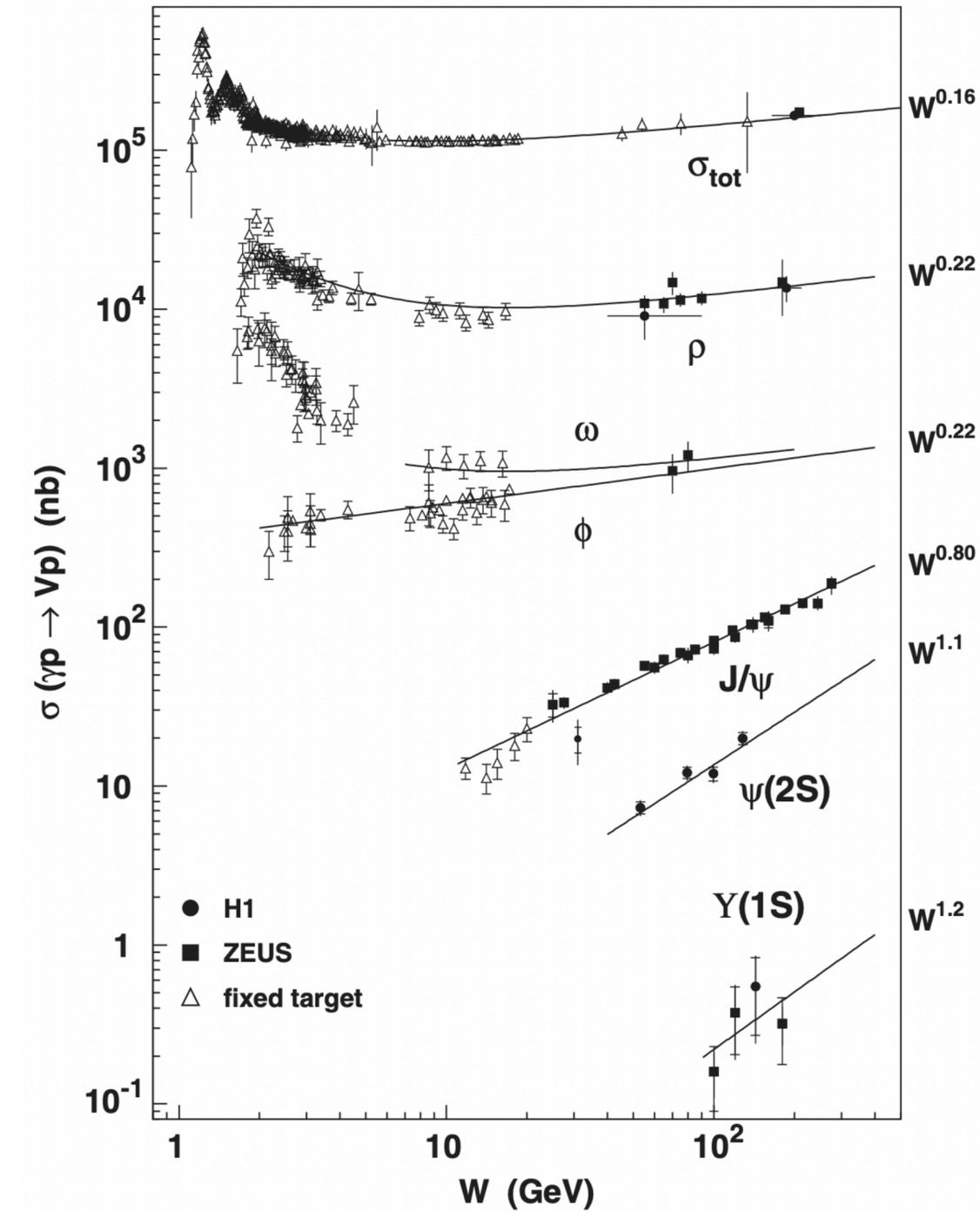
$W^{1.2}$

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Exponent grows with the scale

Newman, Wing, <https://inspirehep.net/literature/1247974>

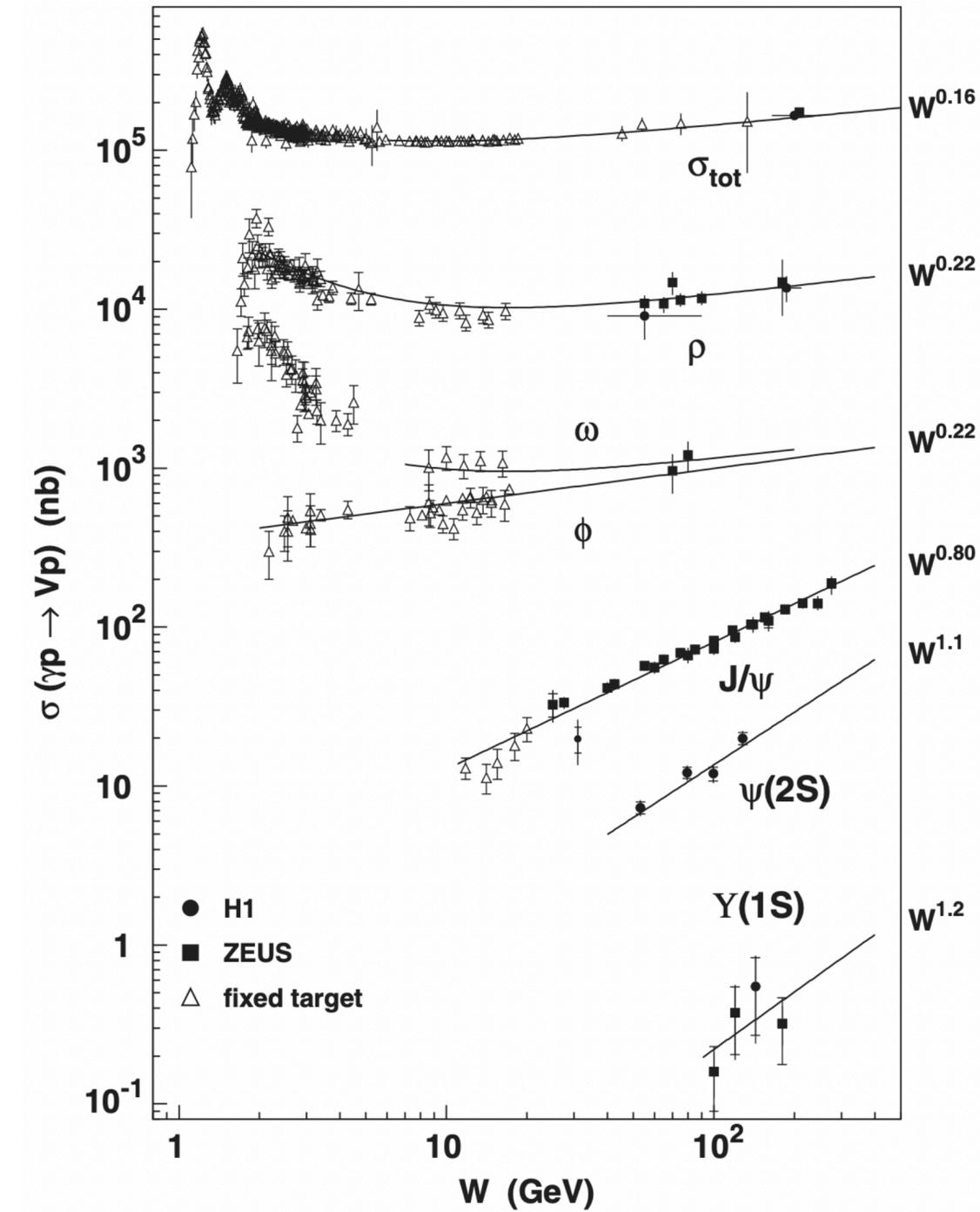
# Sensitivity to the gluon



$\sigma \propto W^\delta$

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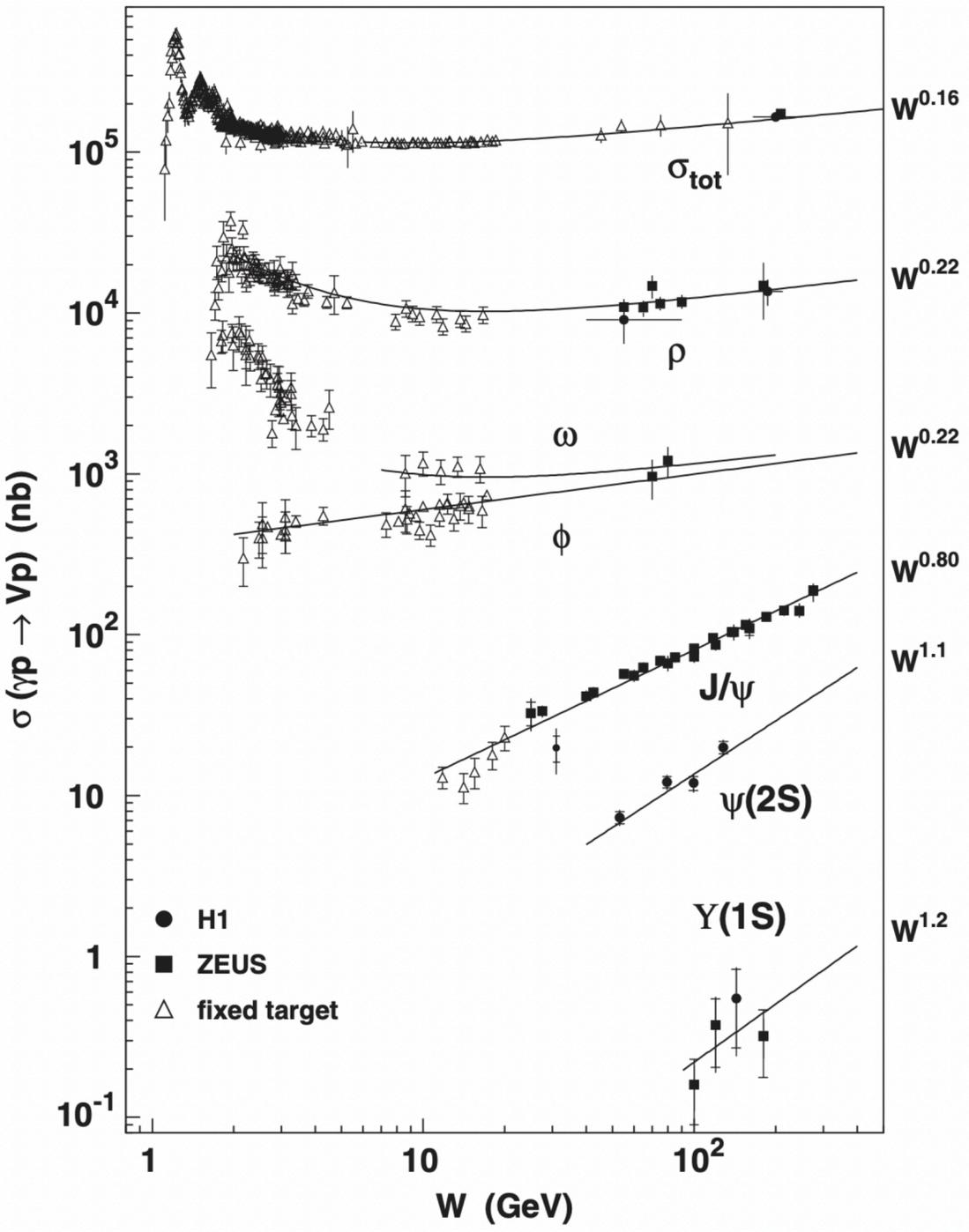


$$\sigma \propto x^{-\delta/2}$$

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Newman, Wing, <https://inspirehep.net/literature/1247974>

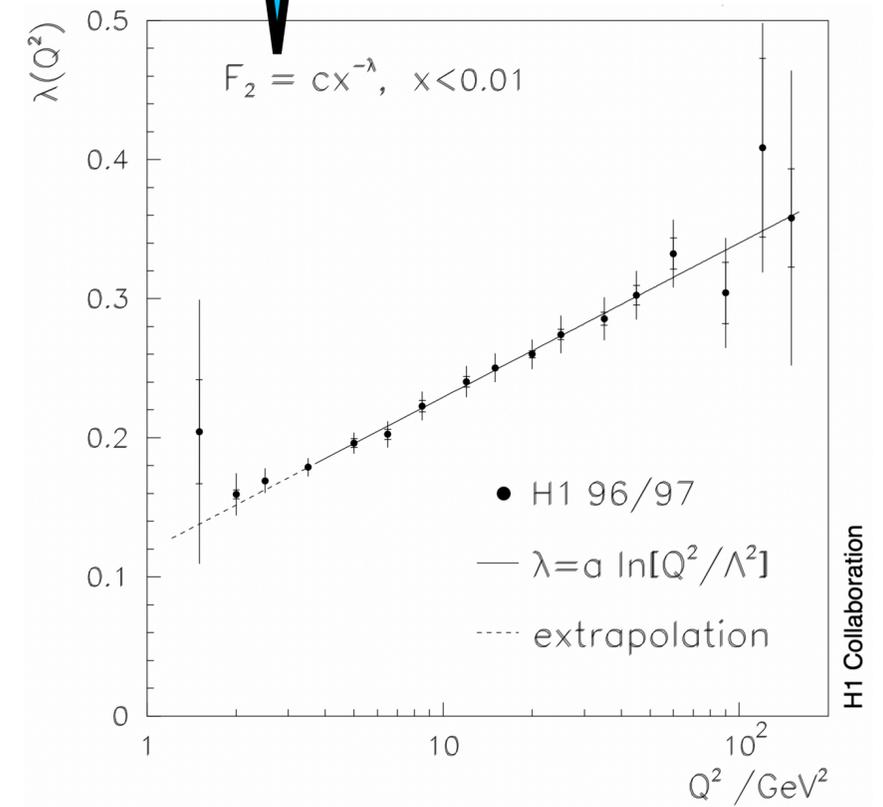
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$F_2 \propto x^{-\lambda}$

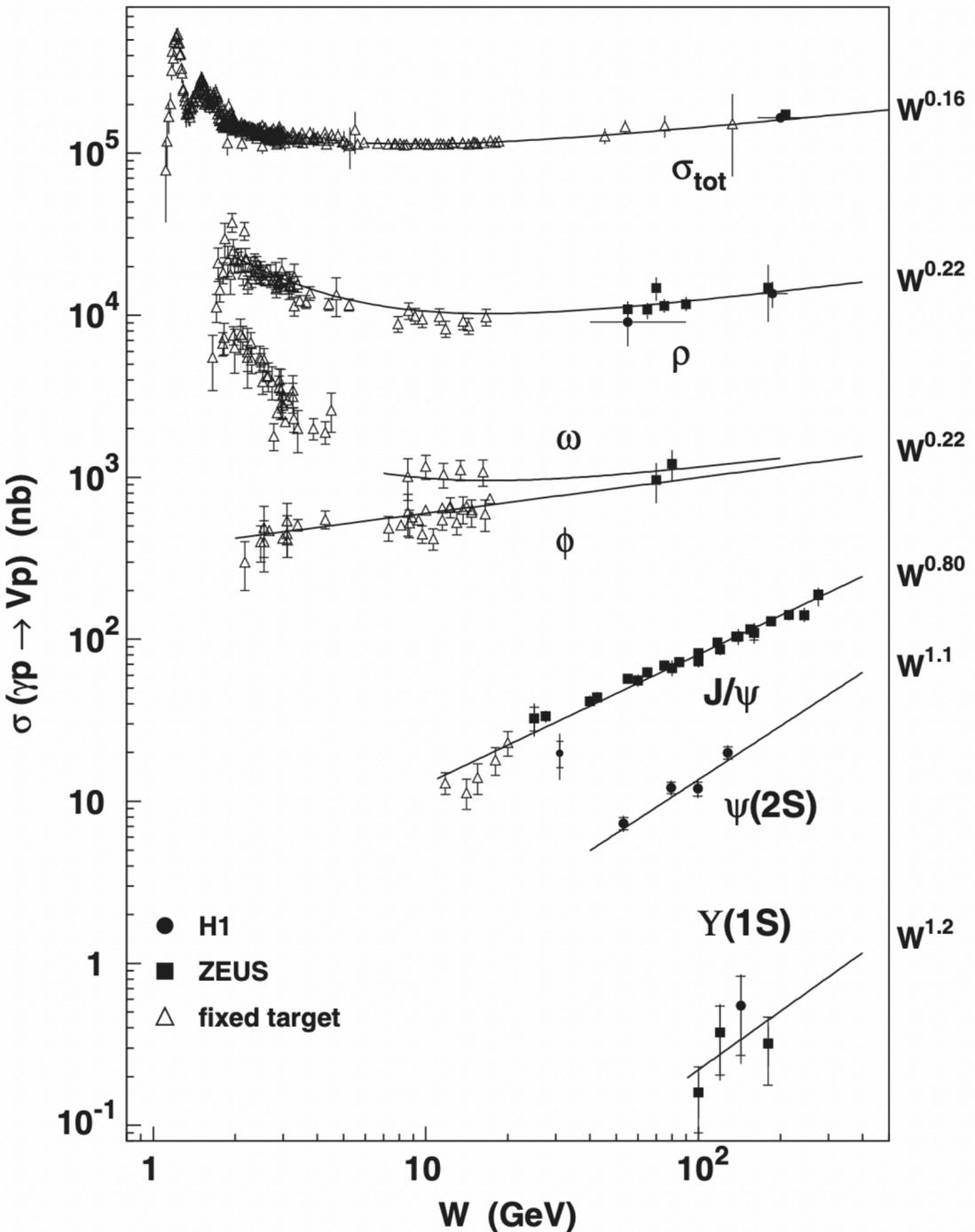


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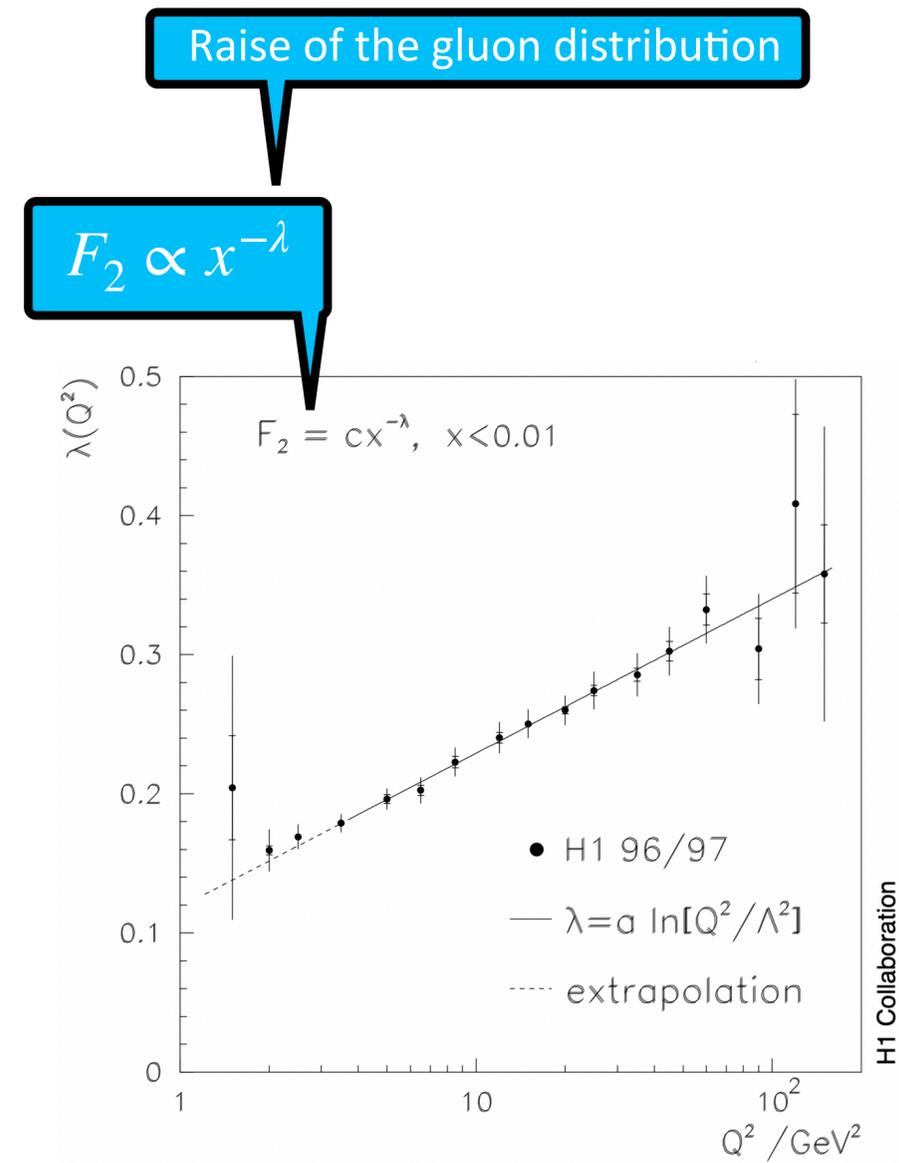
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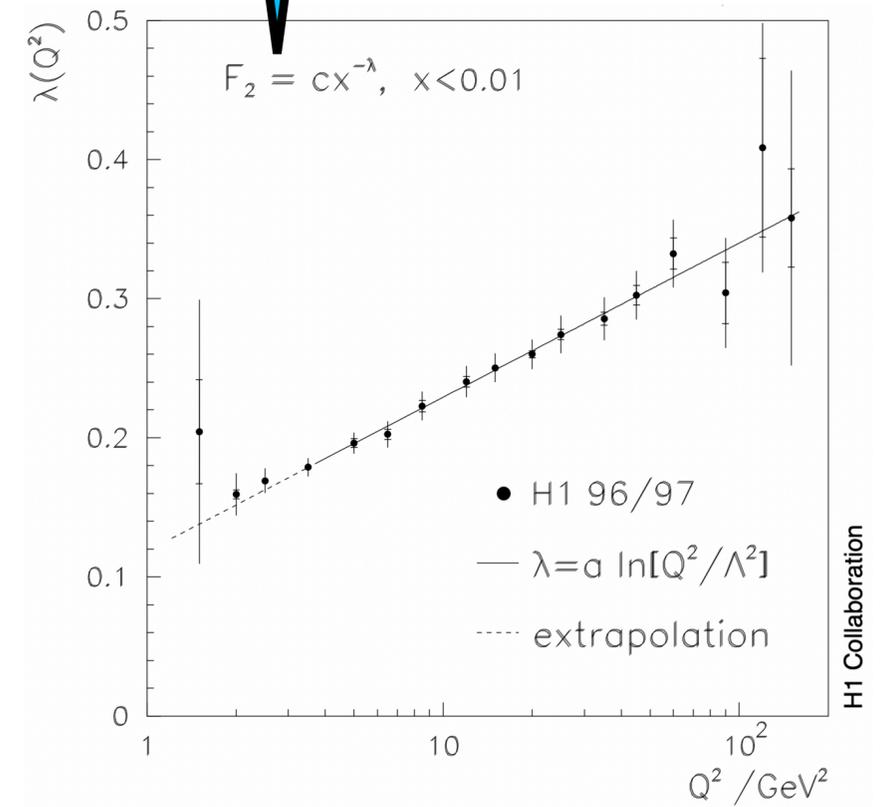
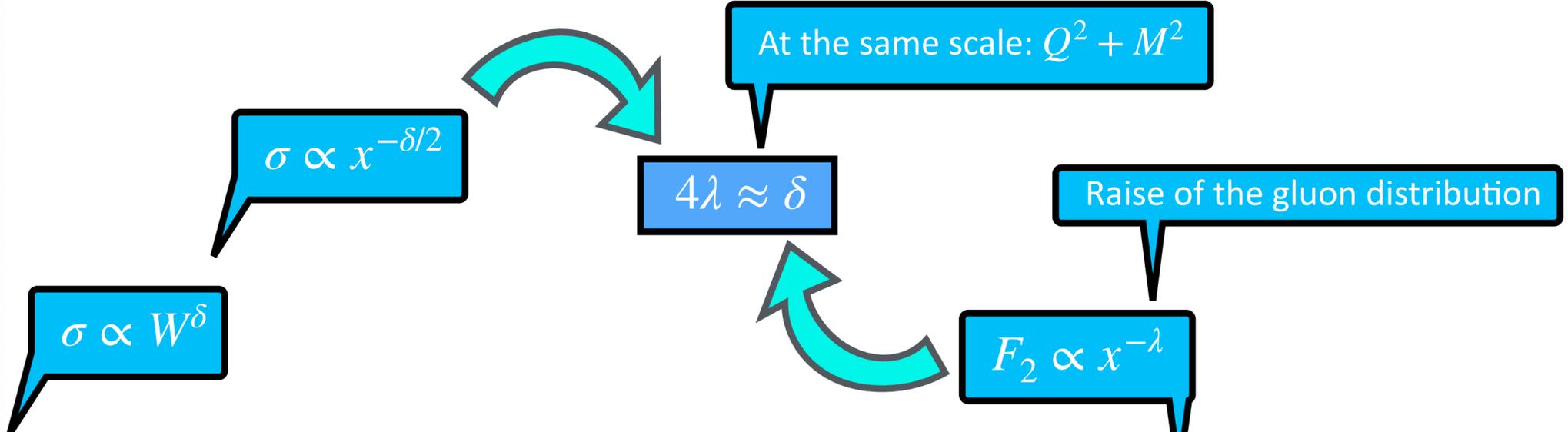
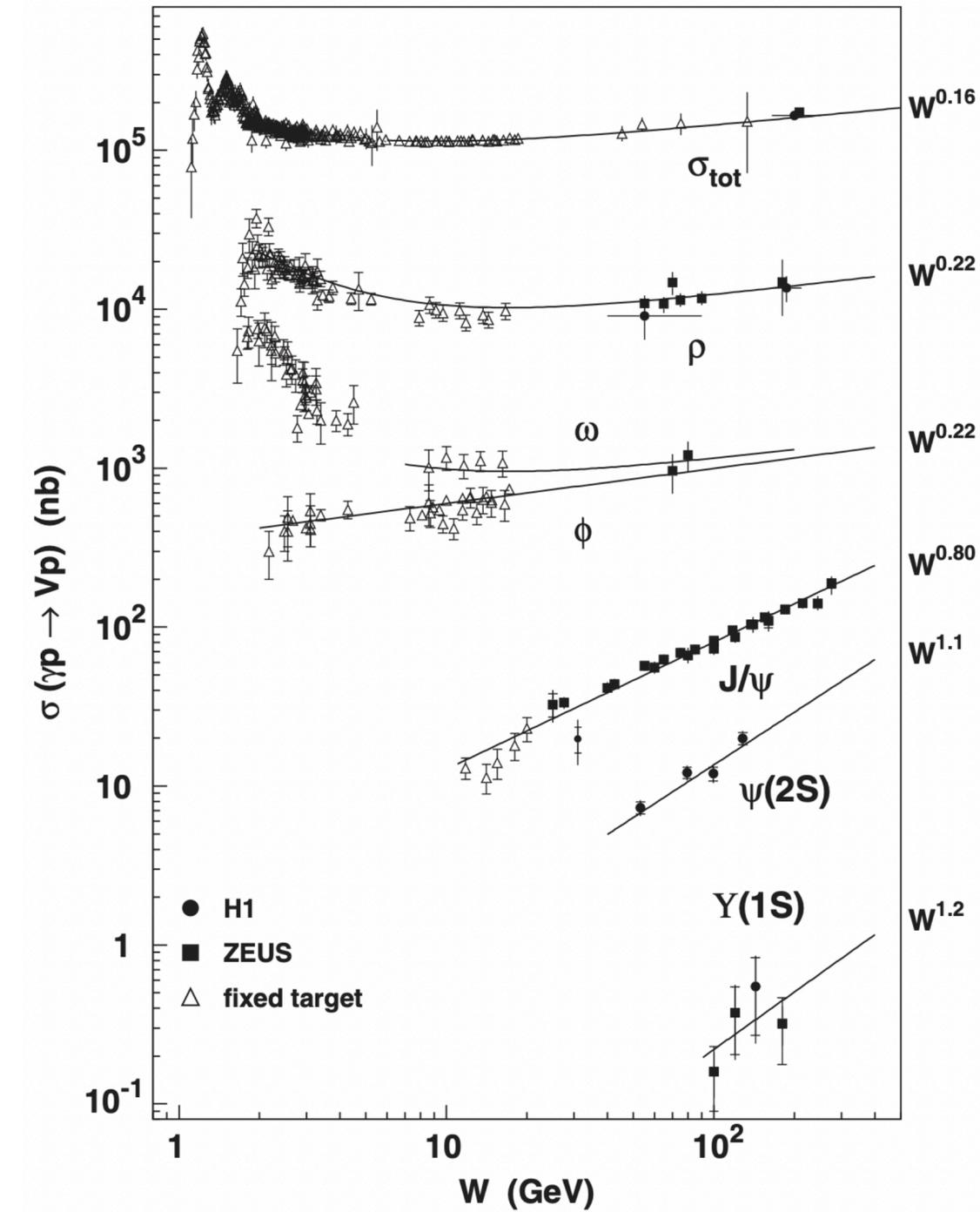
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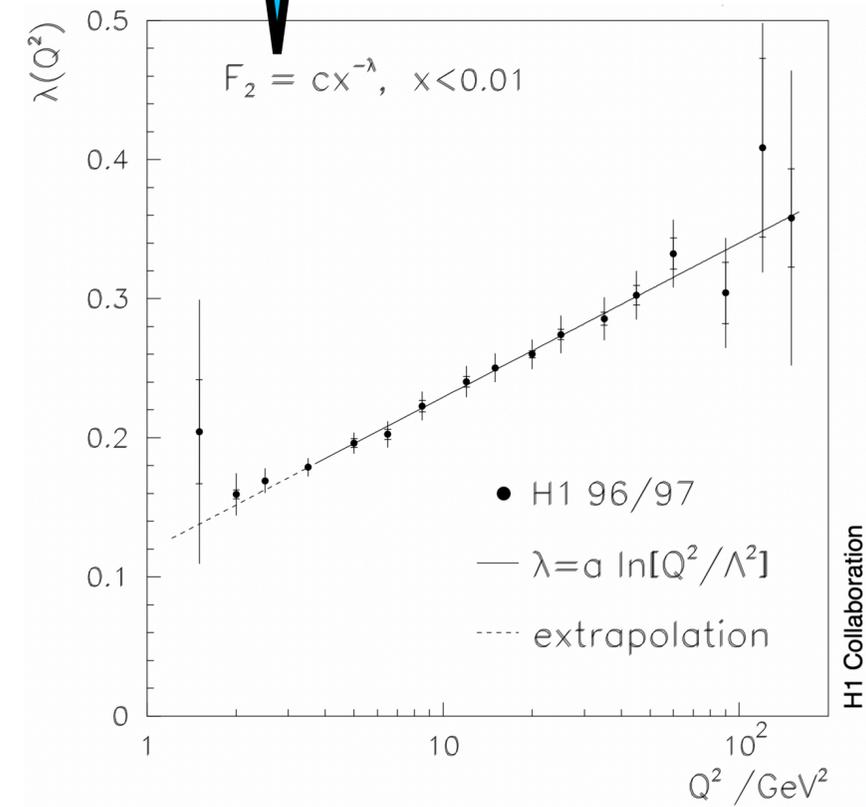
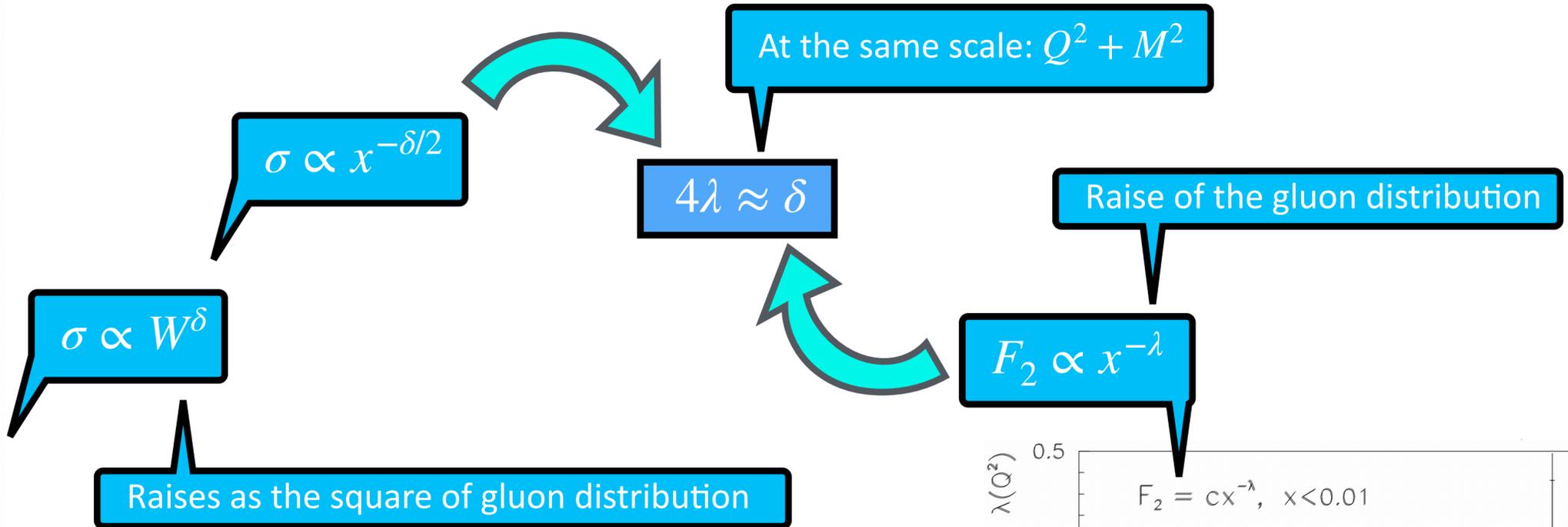
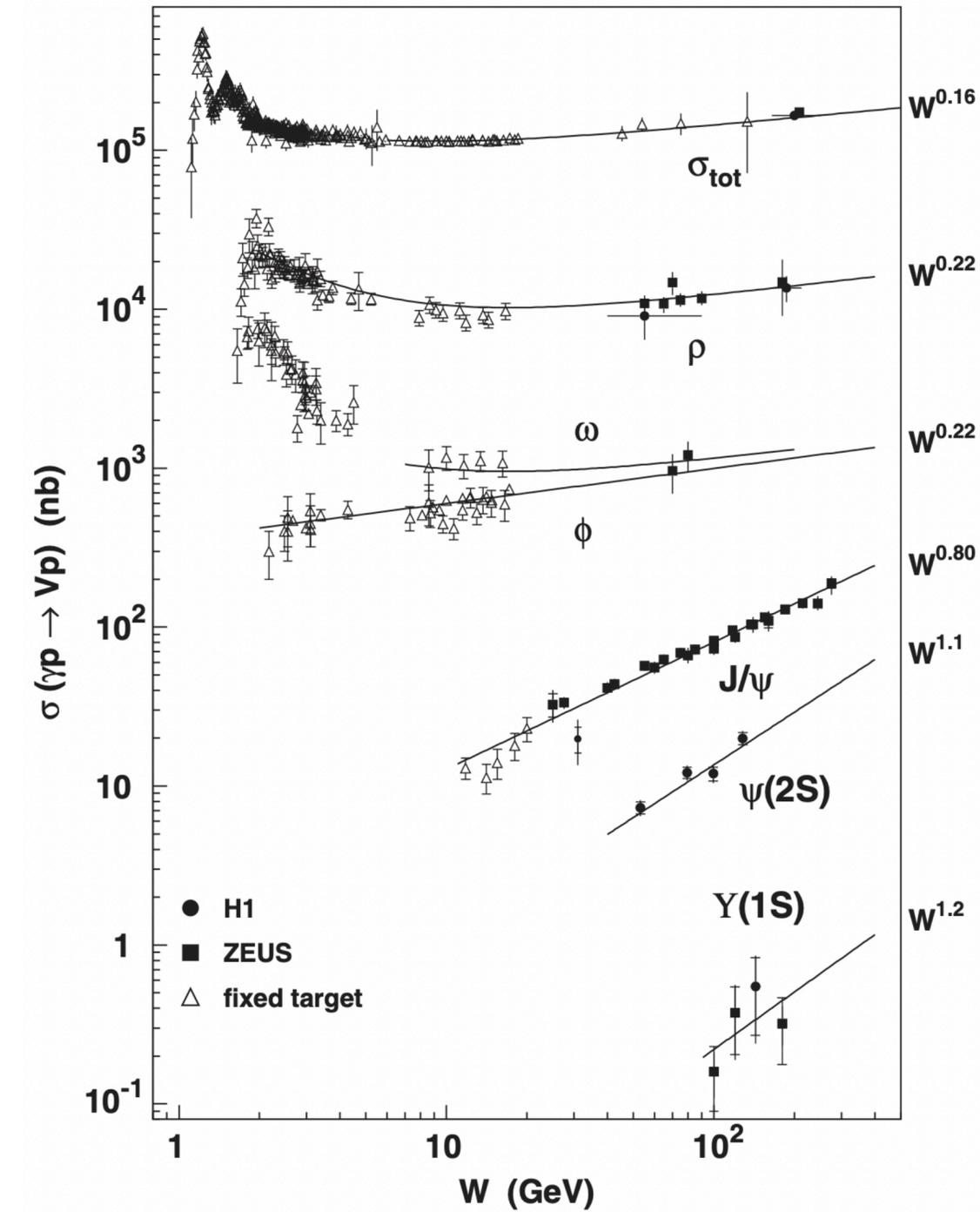
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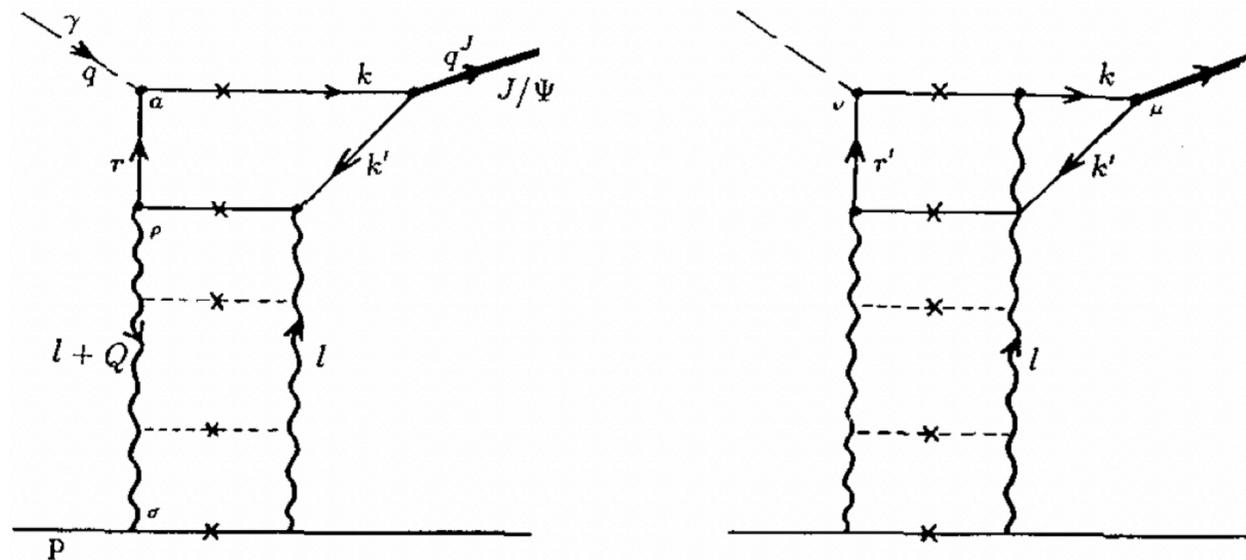
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H1, <https://inspirehep.net/literature/561805>

Guillermo Contreras, CTU in Prague

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# 1993: Diffractive vector meson production in LLA QCD

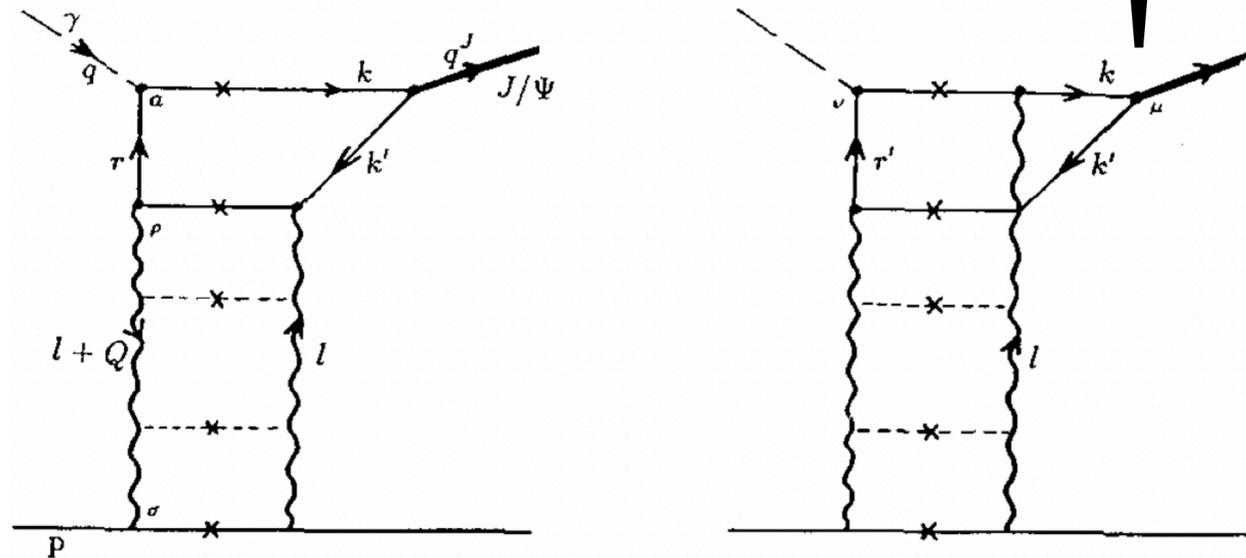


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No detailed model of the wave function of the vector meson



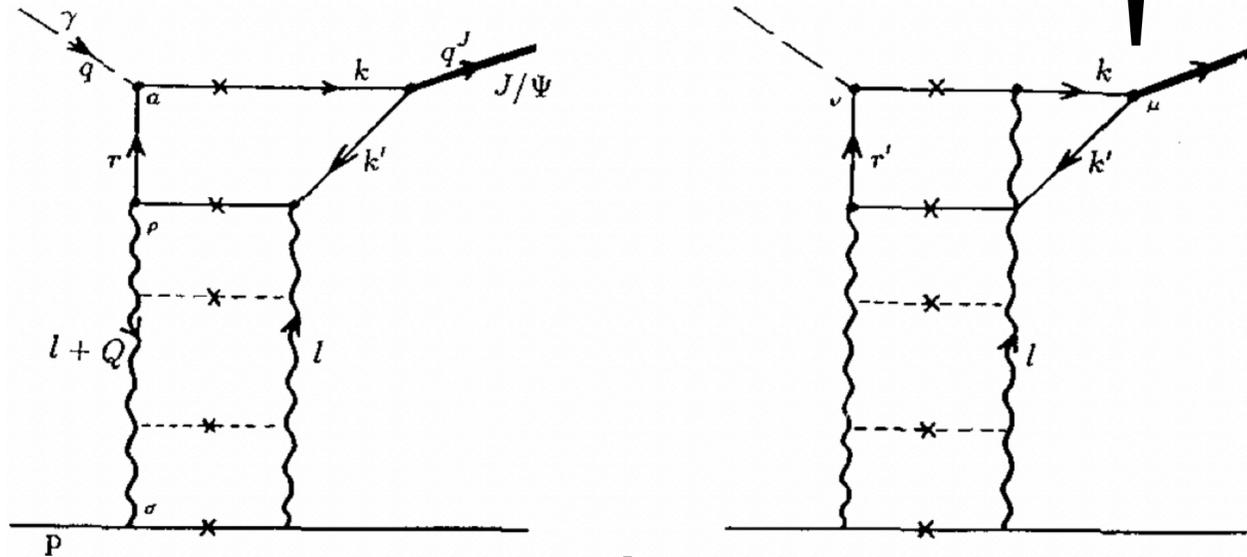
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Ryskin, <https://inspirehep.net/literature/334350>

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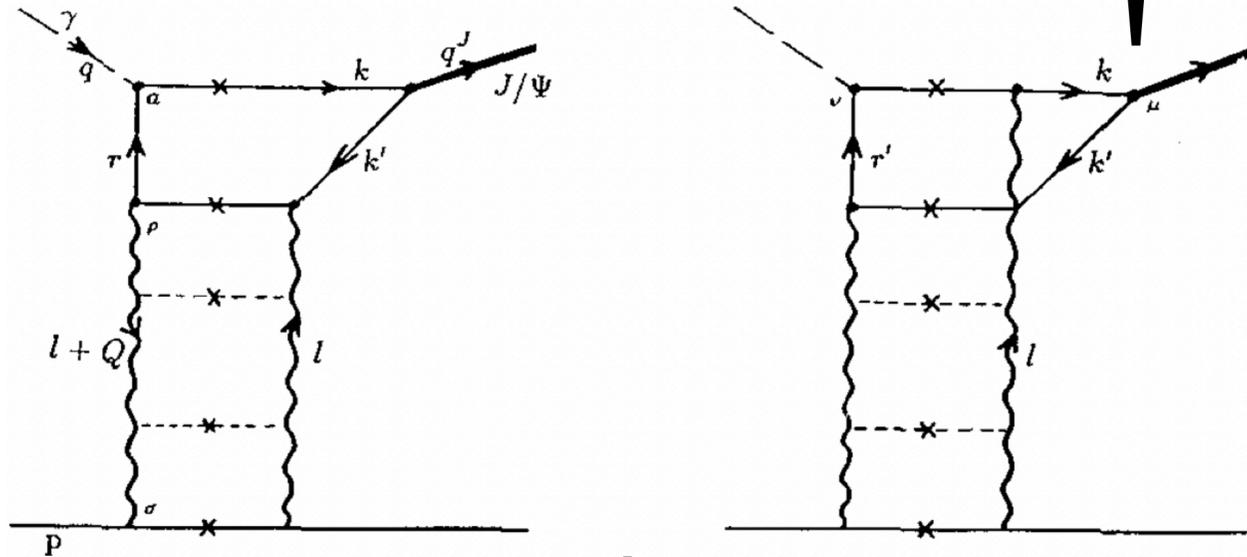
$$\begin{aligned} \frac{d\sigma^T(\gamma p \rightarrow J/\Psi + p)}{dt} &= \frac{|M|^2}{16\pi s^2} \\ &= [F_N^{2G}(t)]^2 \frac{\alpha_s^2 \Gamma_{ee}^J m_J^3}{3\alpha_{em}} \pi^3 \\ &\times \left[ \bar{x}G(\bar{x}, \bar{q}^2) \frac{2\bar{q}^2 - |q_t^J|^2}{(2\bar{q}^2)^3} \right]^2, \end{aligned}$$

Square of gluon distribution

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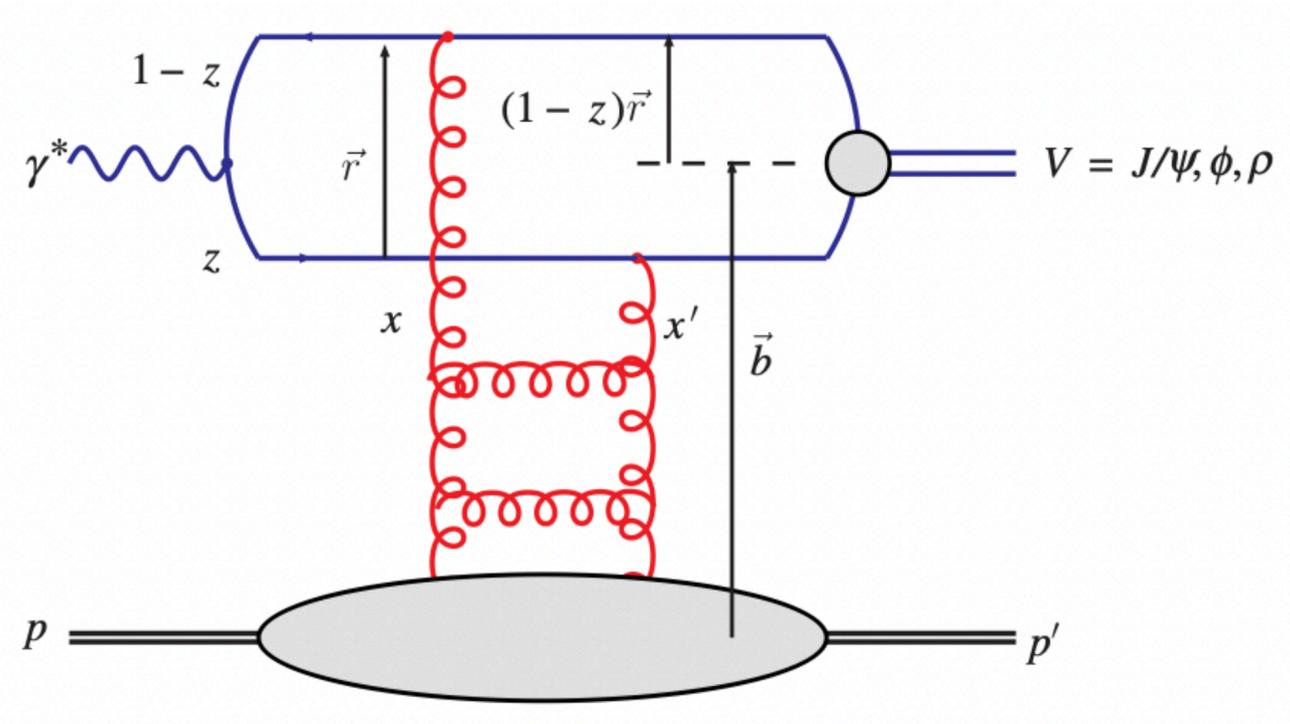
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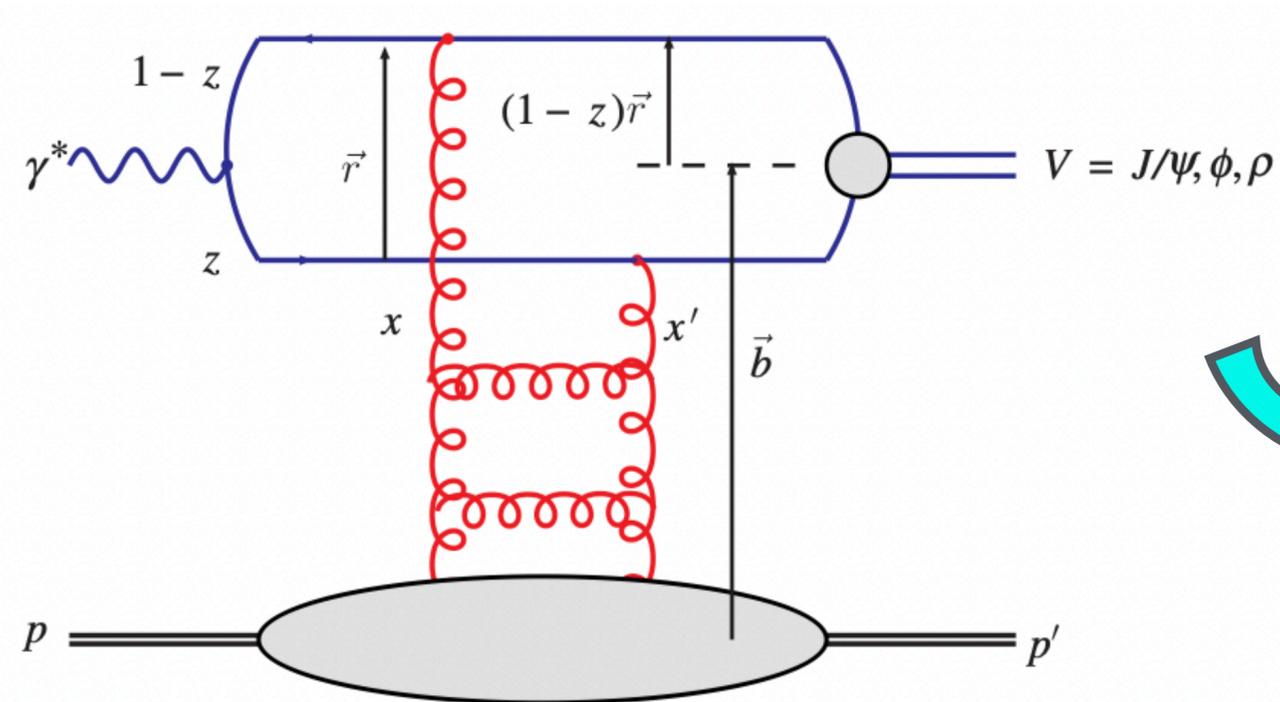
Thus, the diffractive  $J/\Psi$  production provides us with a good chance to find the real position of the saturation boundary and, hence, to answer this question.

Good process to study the approach to the saturation regime

Formalism

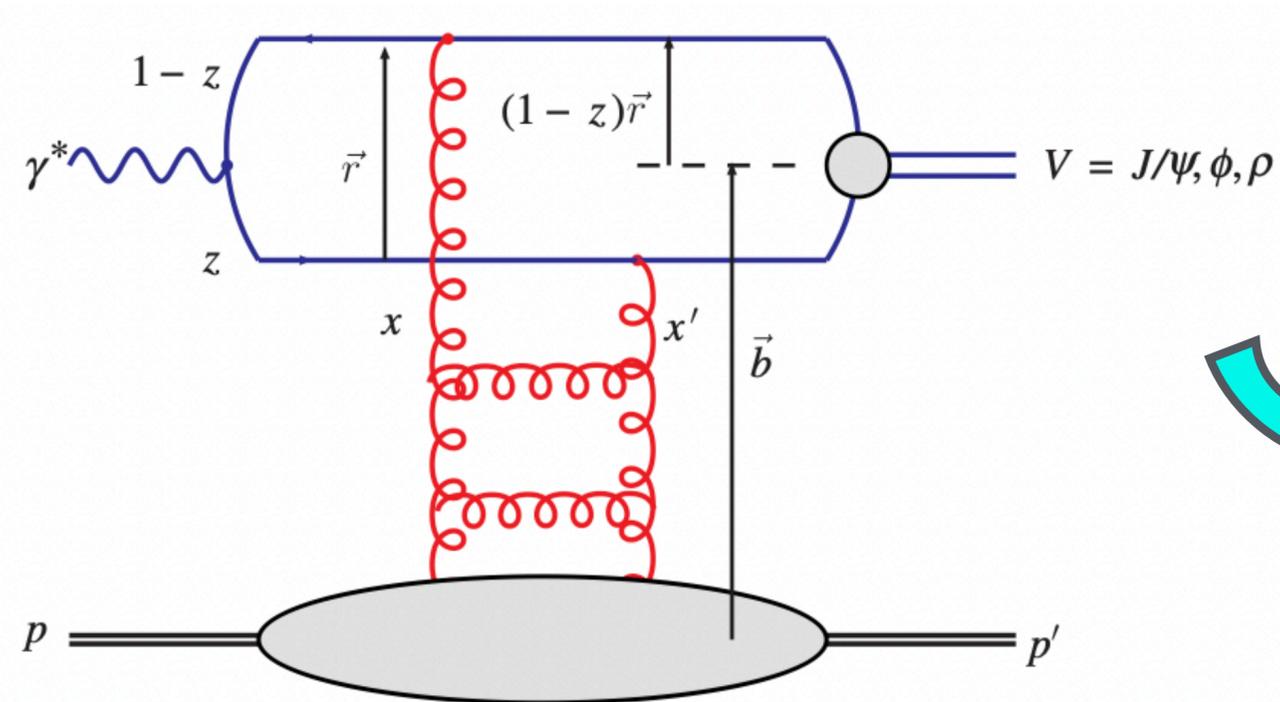


## Formalism



$$\begin{aligned}
 \frac{d\sigma_{T,L}^{\gamma^* p \rightarrow E p}}{dt} &= \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow E p}|^2 \\
 &= \frac{1}{16\pi} \left| \int d^2\mathbf{r} \int_0^1 \frac{dz}{4\pi} \right. \\
 &\quad \times \left. \int d^2\mathbf{b} (\Psi_E^* \Psi)_{T,L} e^{-i[\mathbf{b} - (1-z)\mathbf{r}] \cdot \Delta} \frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} \right|^2.
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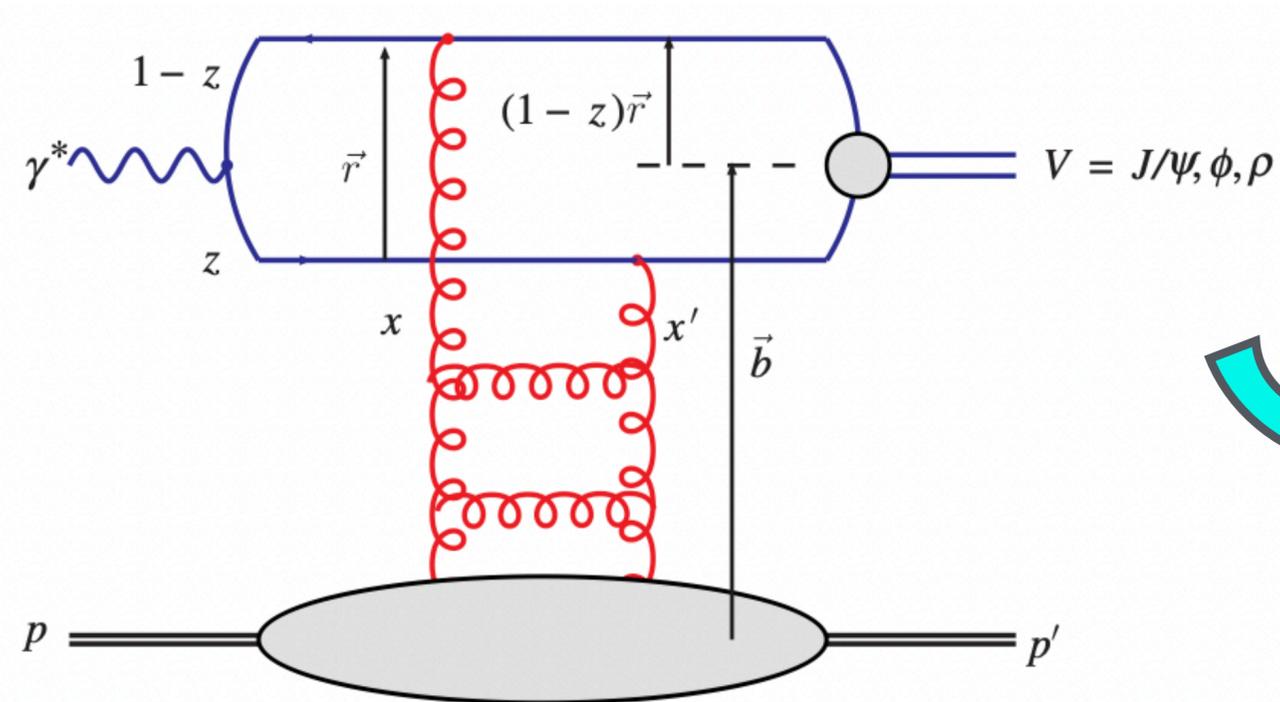
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1 Forward wave functions

## Formalism



$$\frac{d\sigma_{T,L}^{\gamma^* p \rightarrow Ep}}{dt} = \frac{1}{16\pi} |\mathcal{A}_{T,L}^{\gamma^* p \rightarrow Ep}|^2$$

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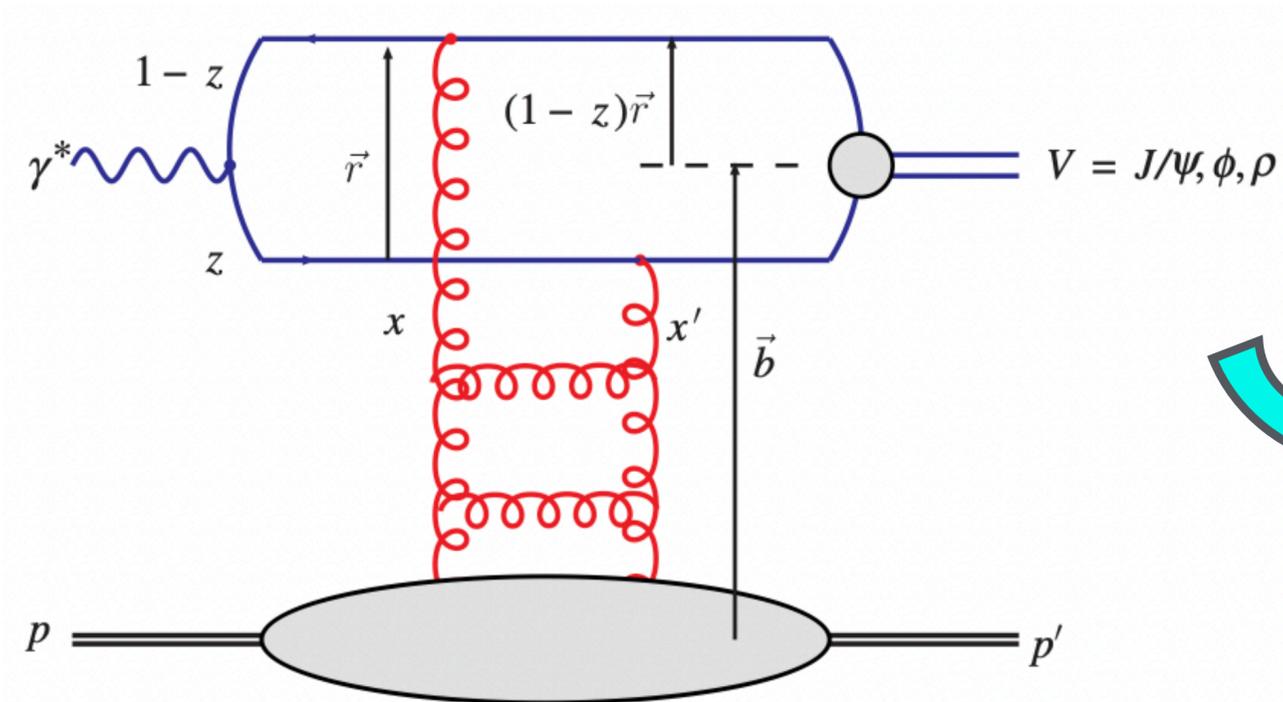
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Forward wave functions

1

$$\vec{\Delta}^2 = -t$$

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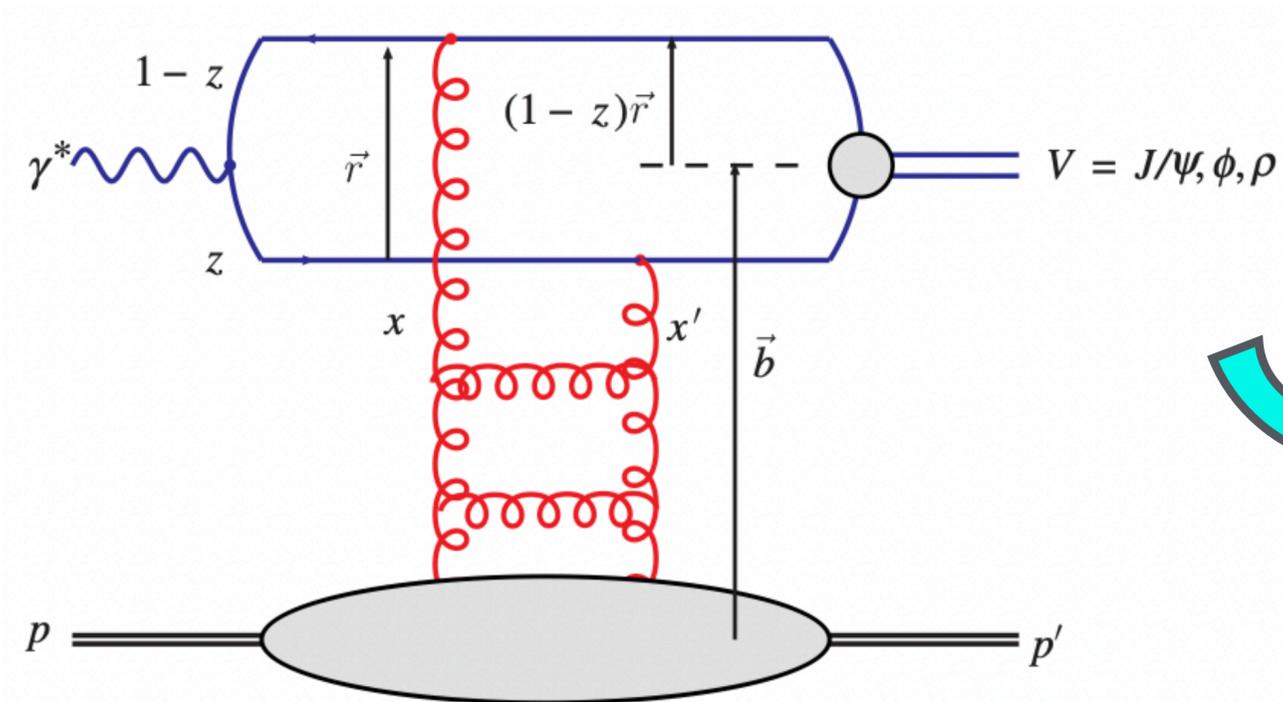
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Conjugate variable

$\vec{\Delta}^2 = -t$

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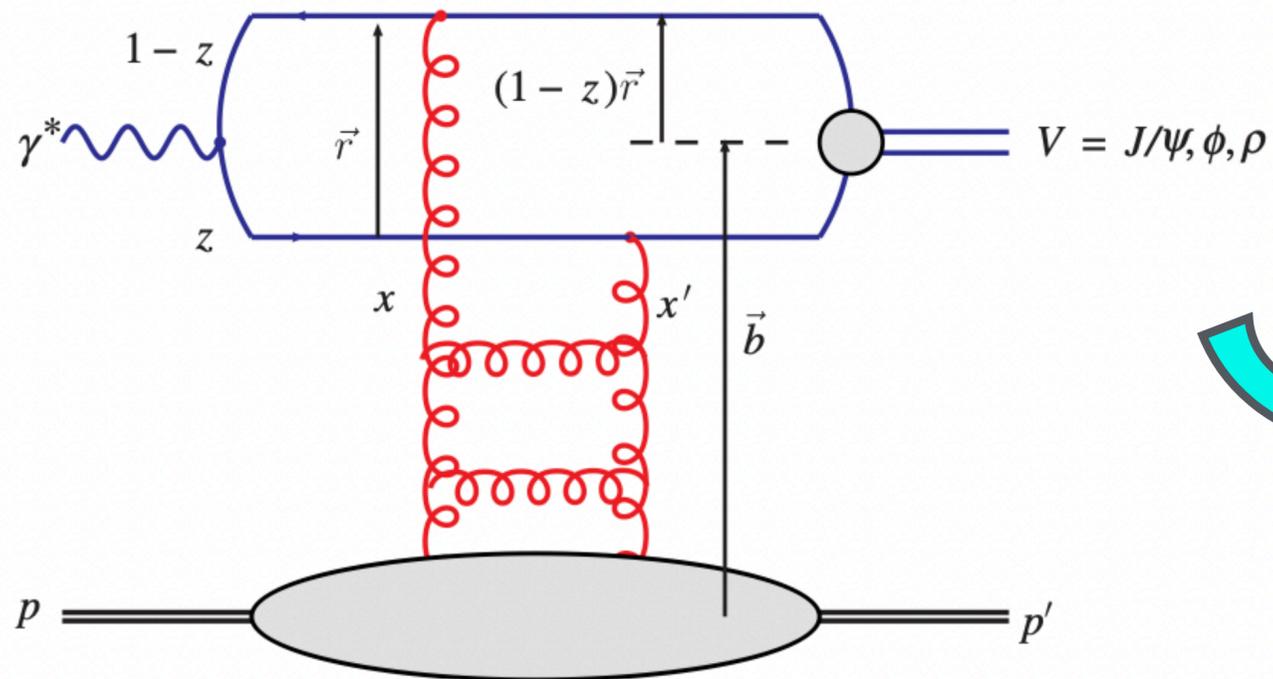
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# 2006: Diffractive vector meson production in the dipole approach (1/5)

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Slightly different form use nowadays

$$(1-z) \rightarrow \left(\frac{1}{2} - z\right)$$

Includes the effect of non-forward wave functions

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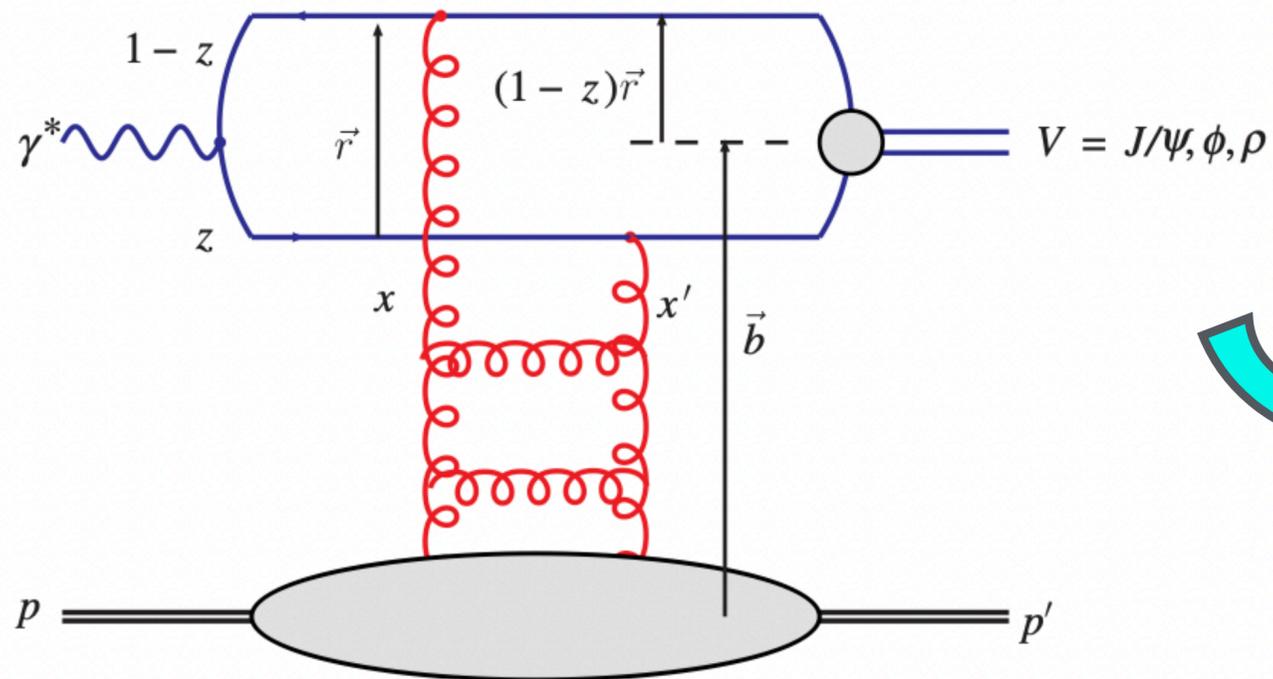
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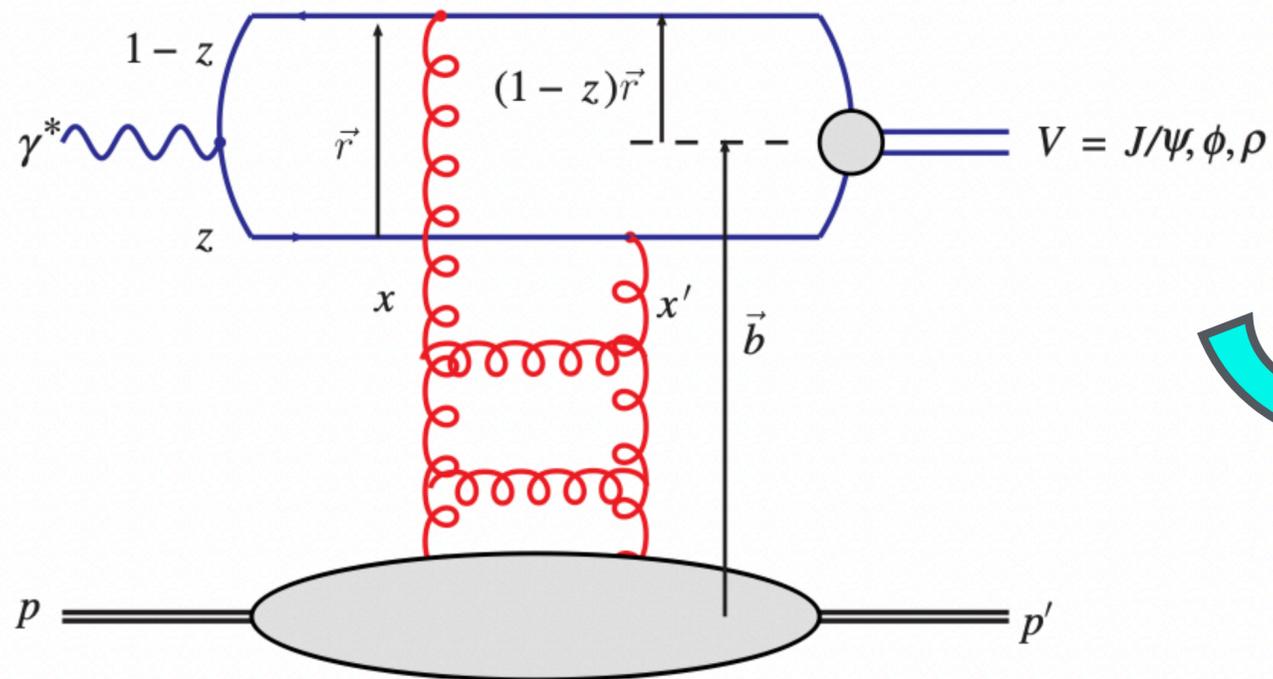
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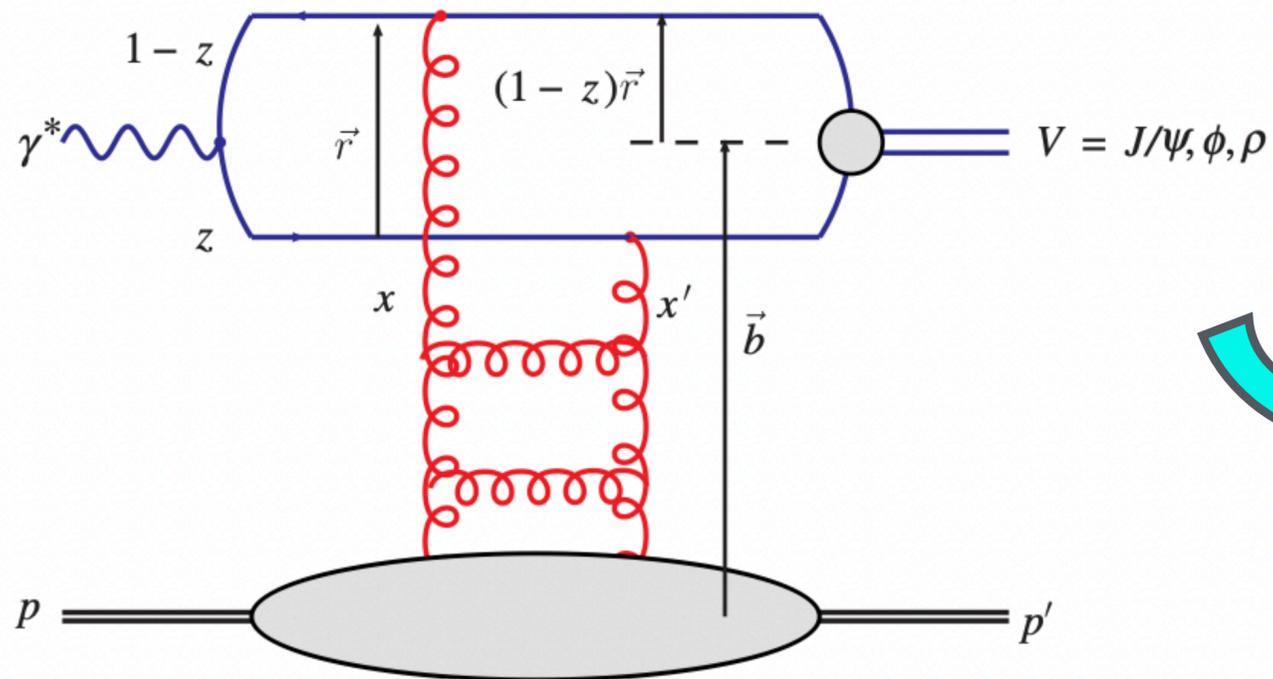
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Normally a correction is used to account for the fact that the matrix element may not be fully real

# 2006: Diffractive vector meson production in the dipole approach (1/5)

## Formalism



The fact that  $x$  and  $x'$  are not the same is taken into account with the so-called skewedness correction

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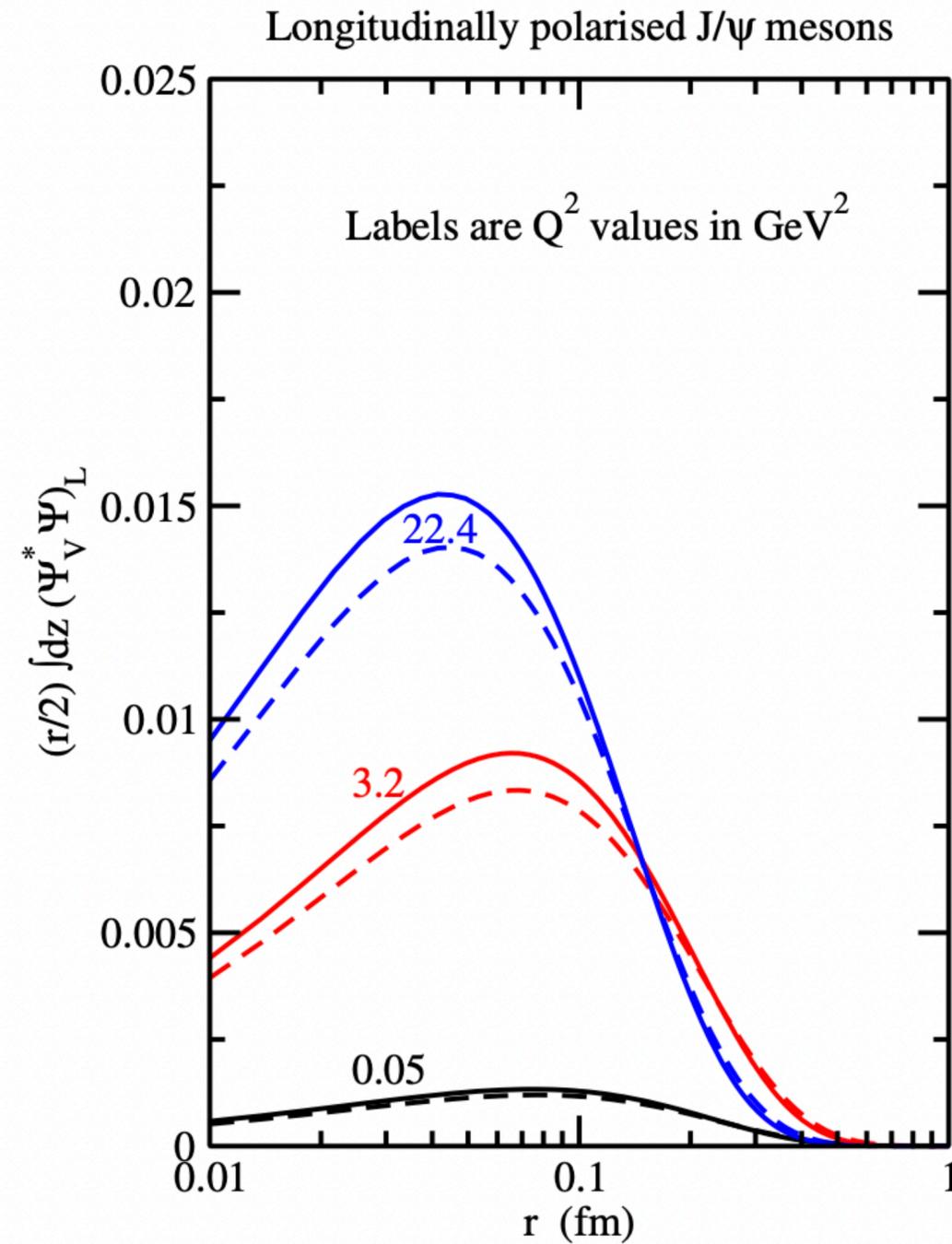
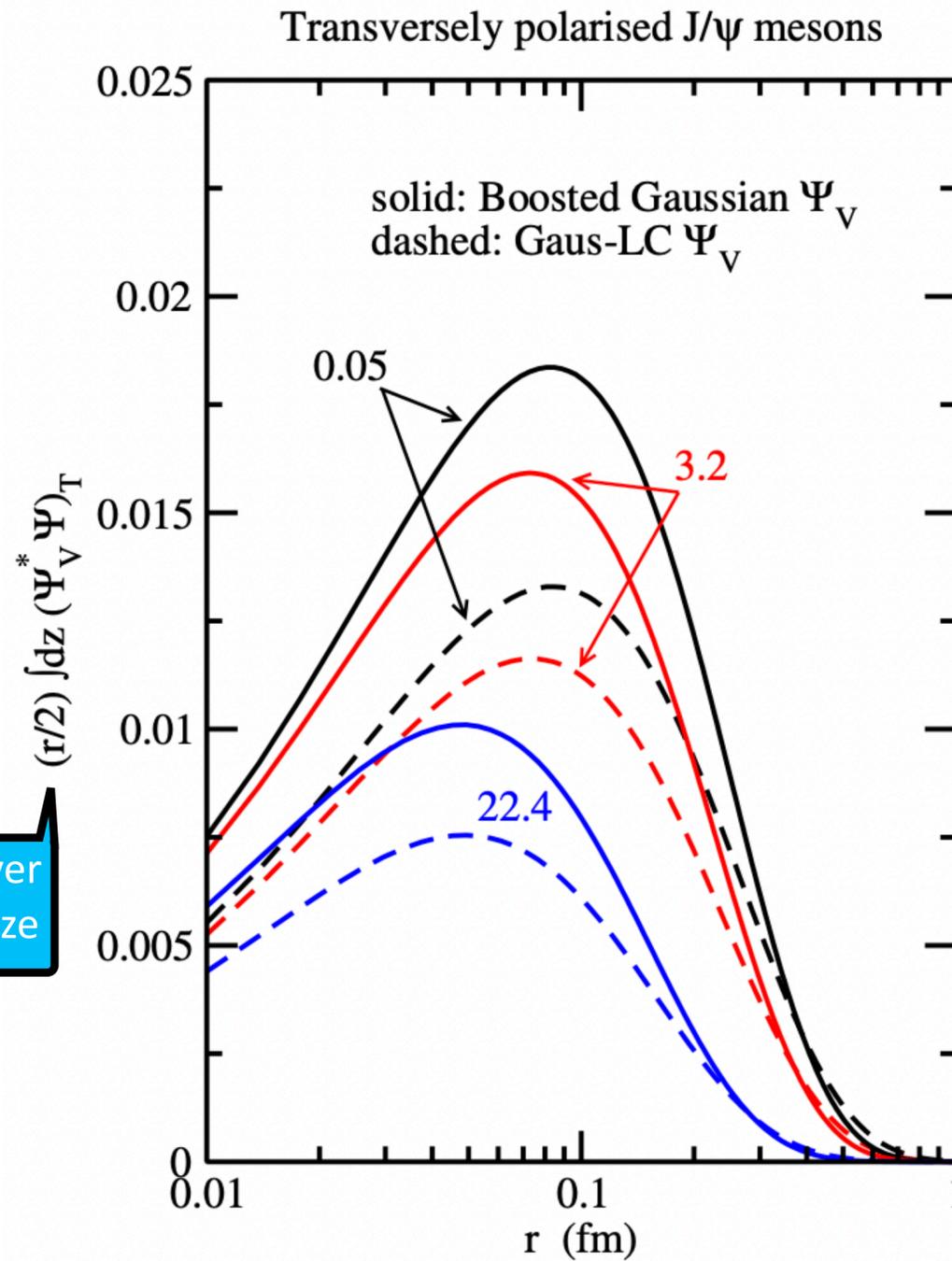
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## Forward wave functions

Forward wave functions, integrated over energy fraction and scaled by dipole size

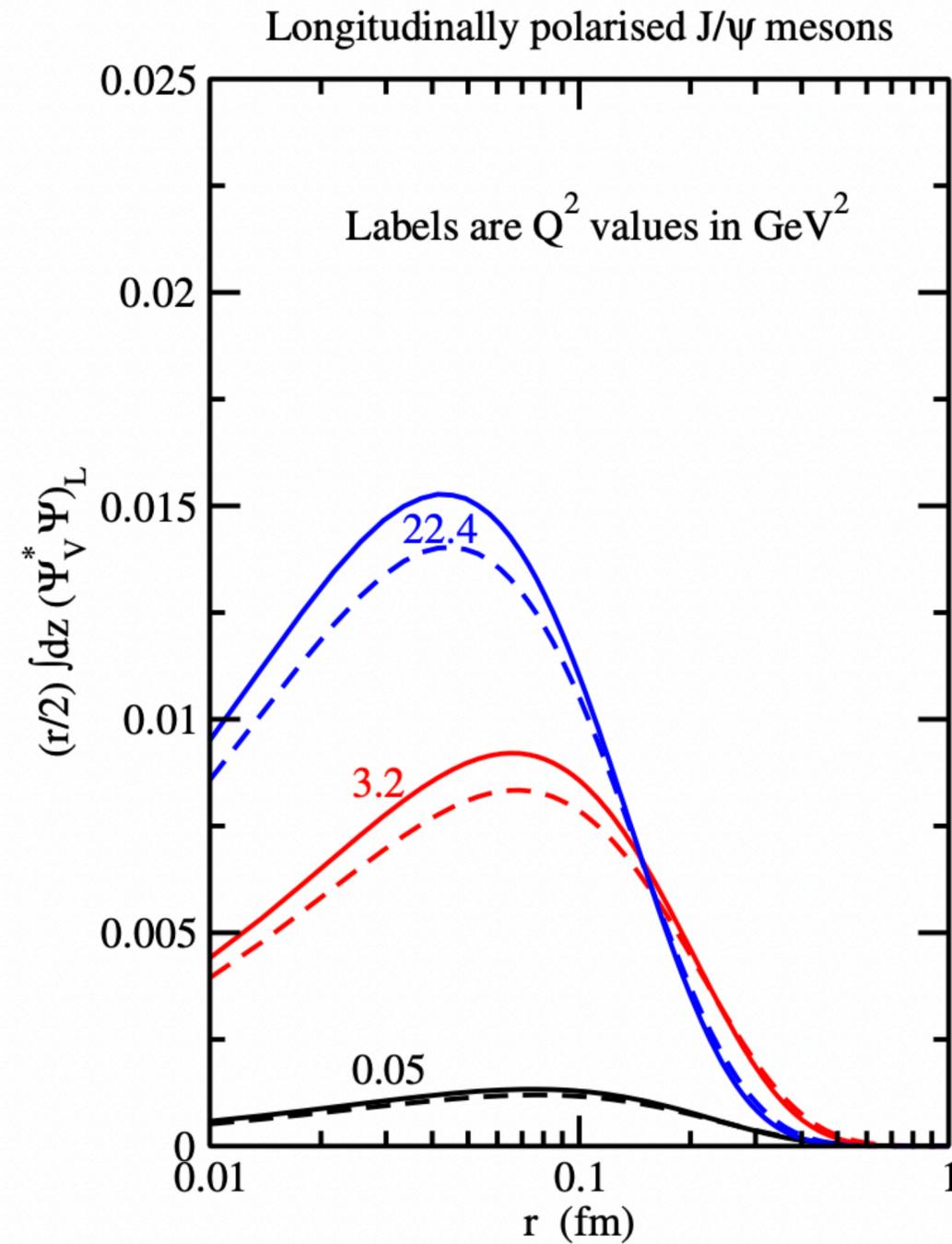
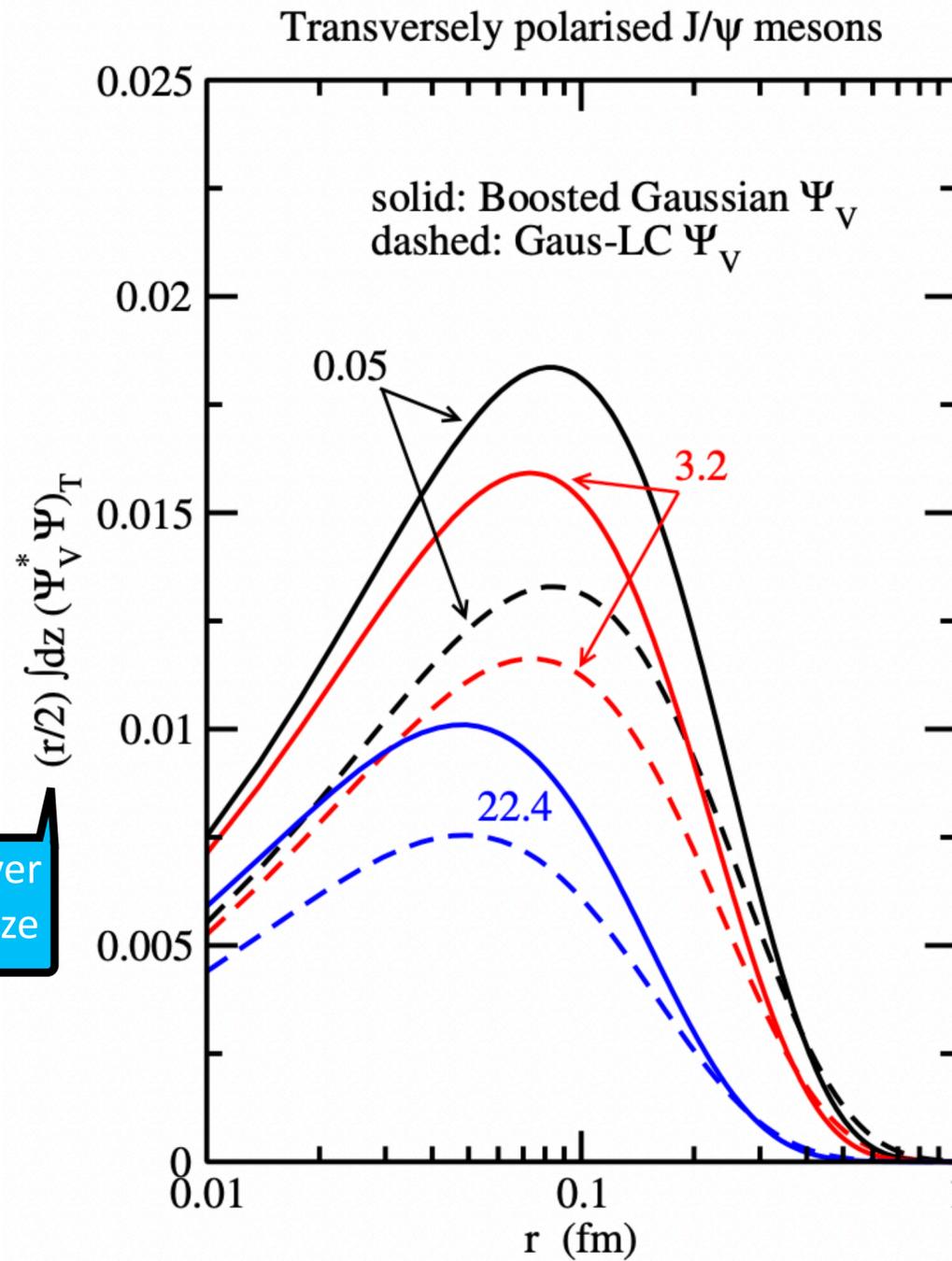


1

## Forward wave functions

Forward wave functions, integrated over energy fraction and scaled by dipole size

$$\int d\vec{r} \rightarrow \int r dr d\phi$$



# 2006: Diffractive vector meson production in the dipole approach (2/5)

1

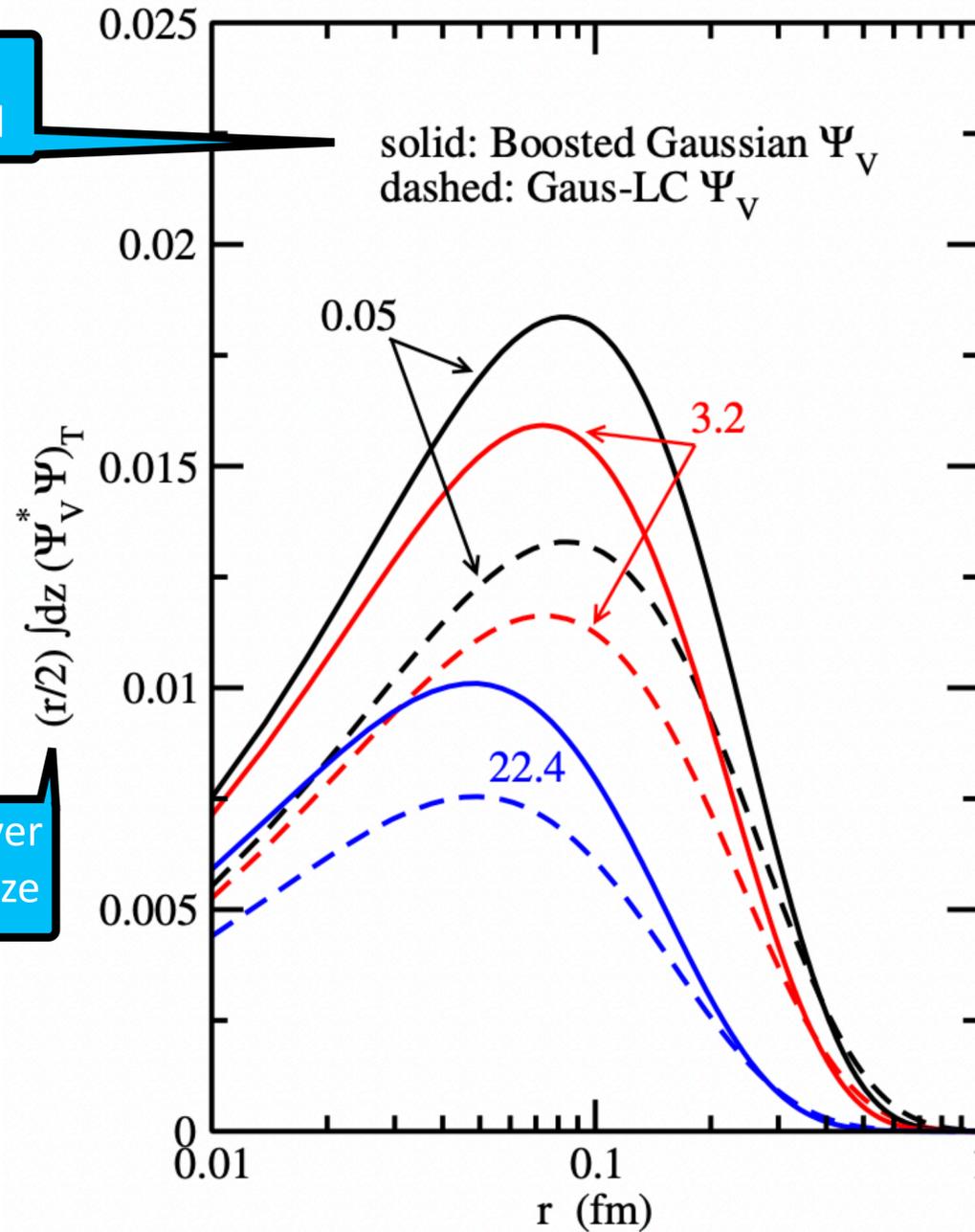
## Forward wave functions

The QED part is computable, but the vector meson part has to be modelled

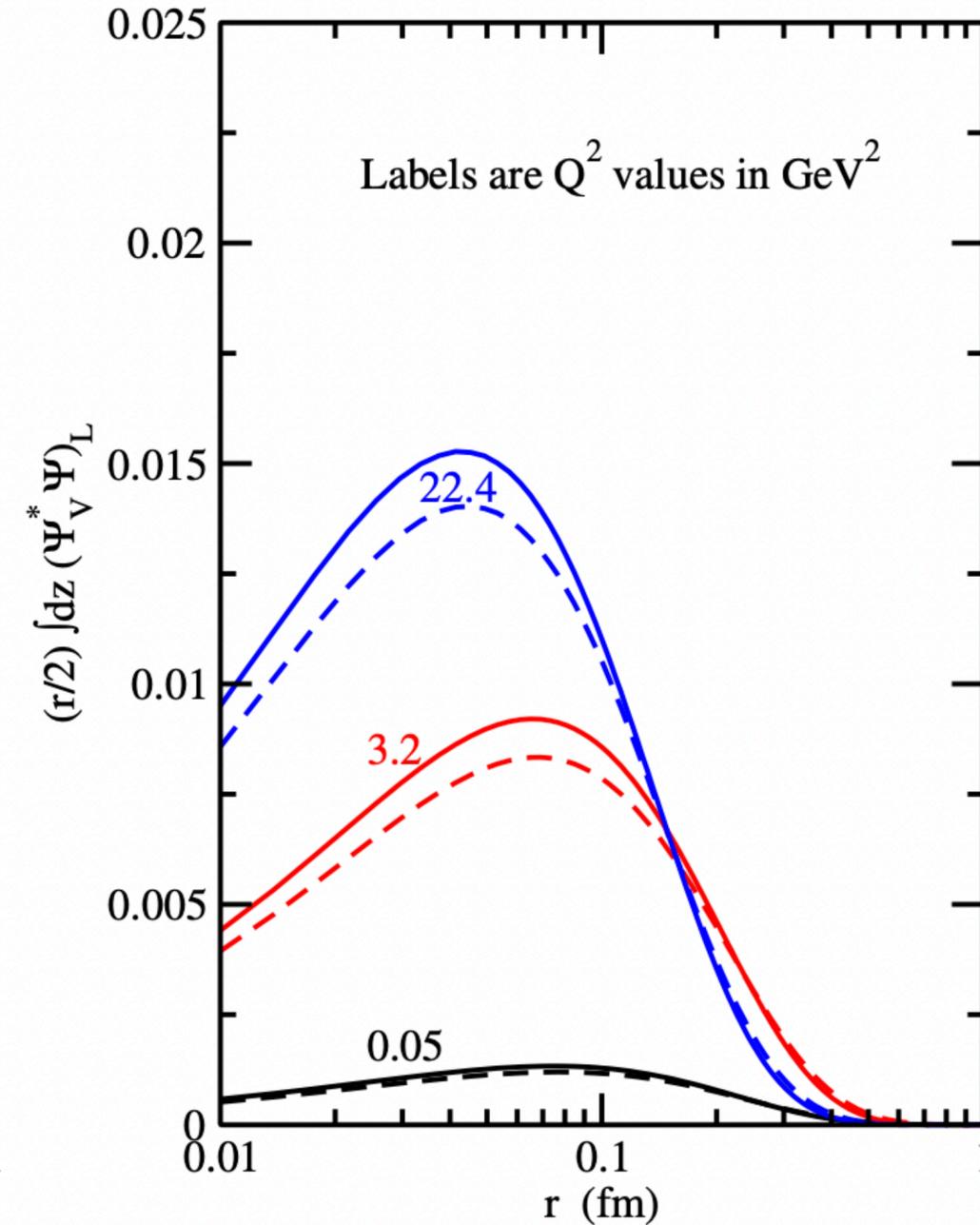
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Transversely polarised J/ψ mesons



Longitudinally polarised J/ψ mesons



# 2006: Diffractive vector meson production in the dipole approach (2/5)

1

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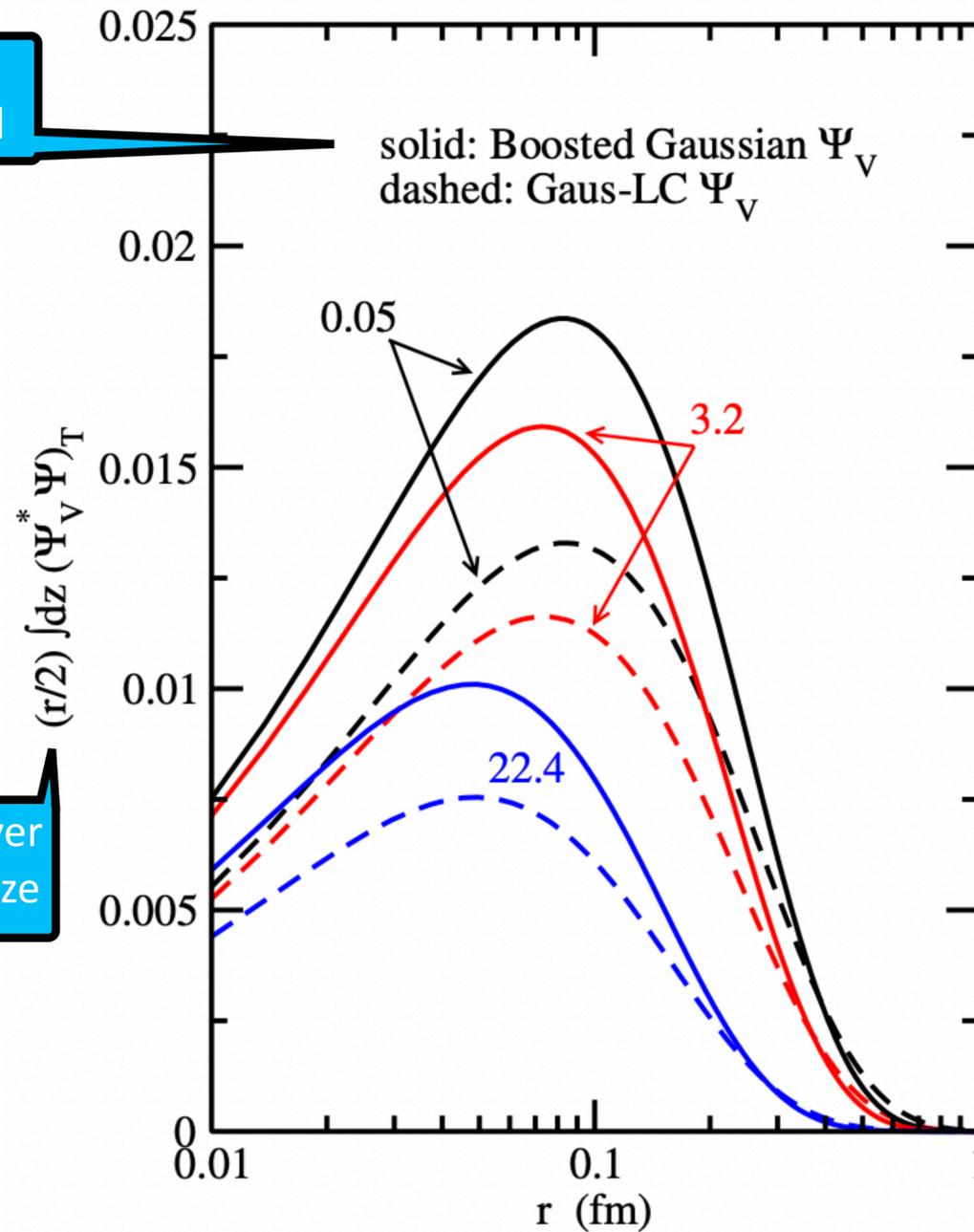
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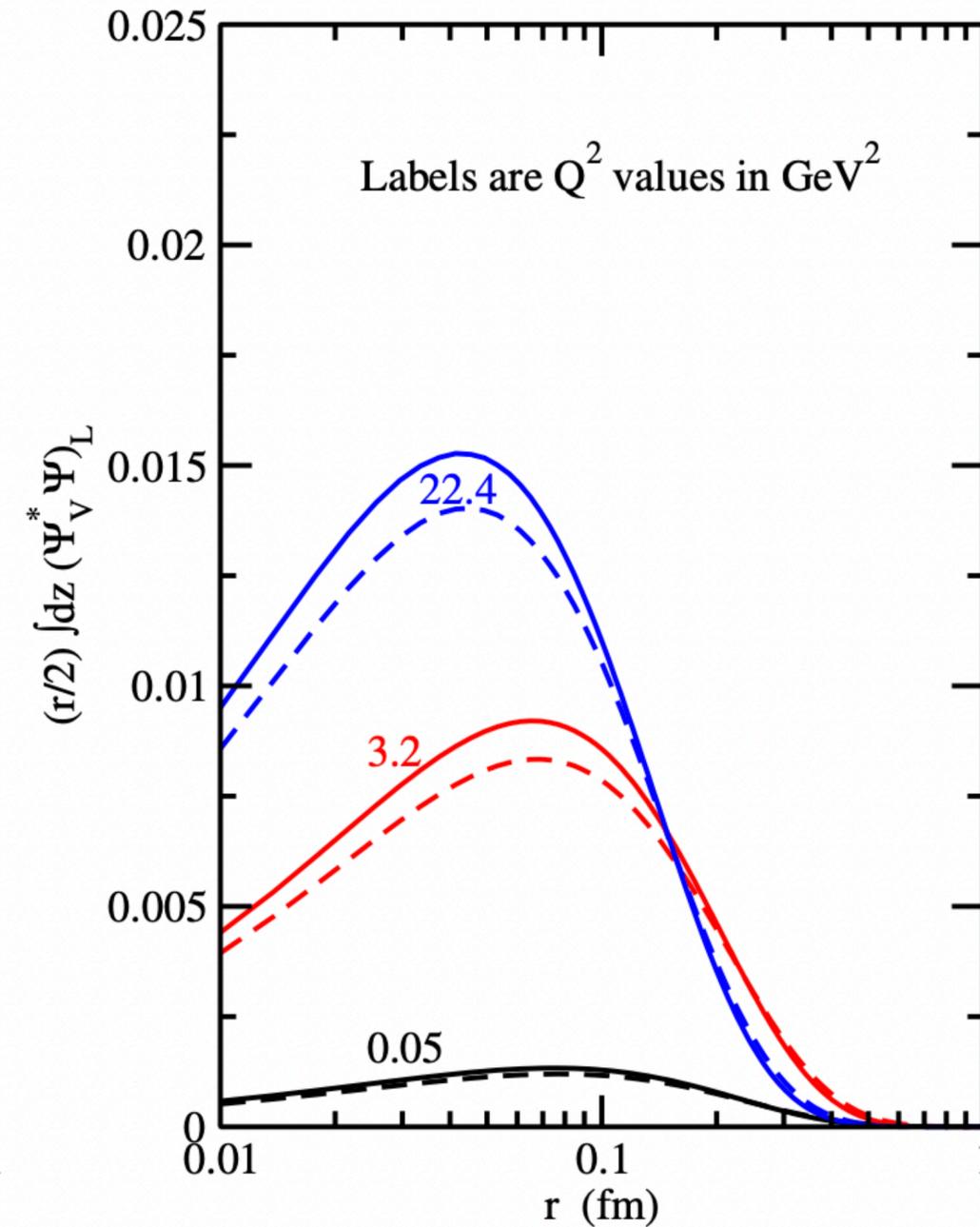
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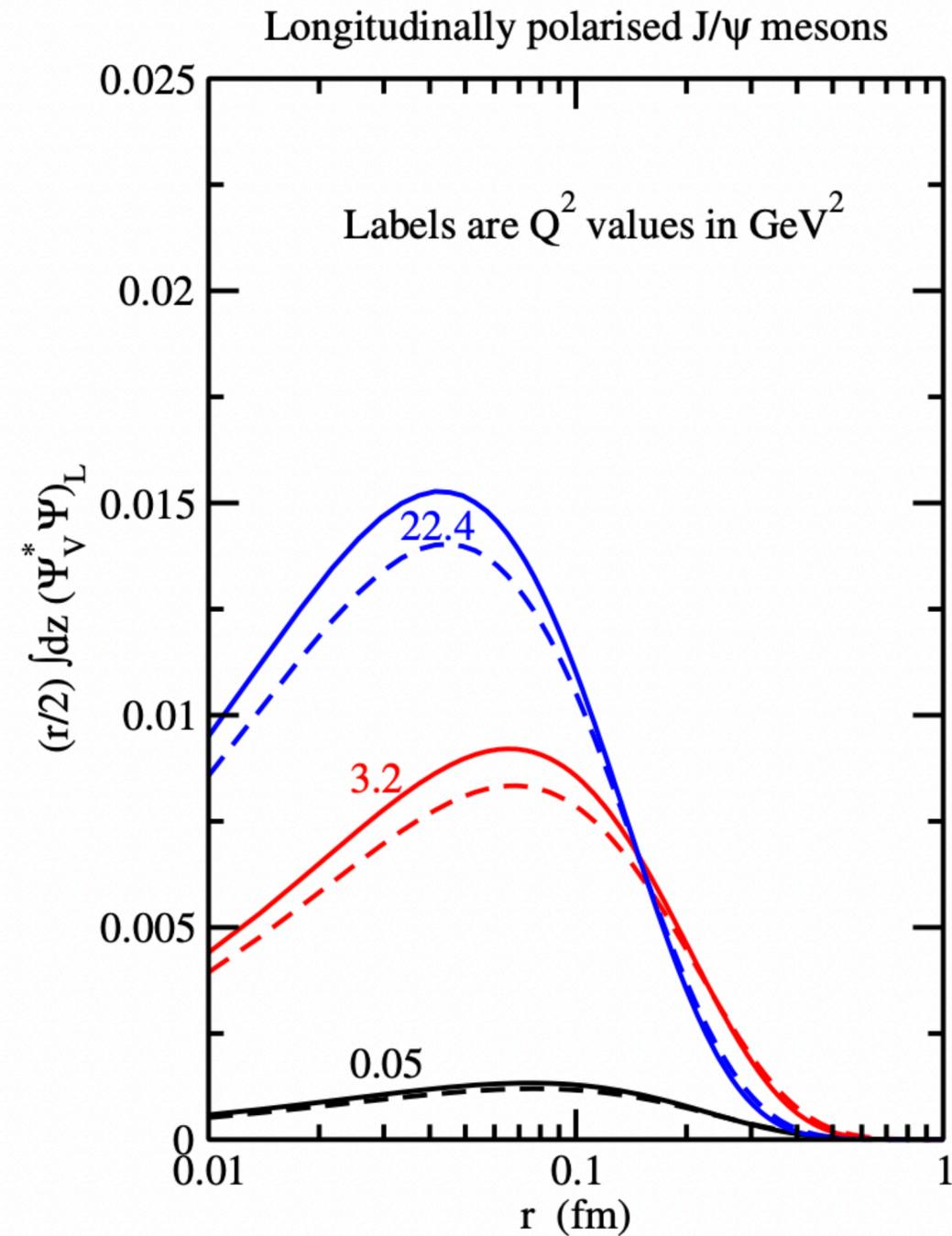
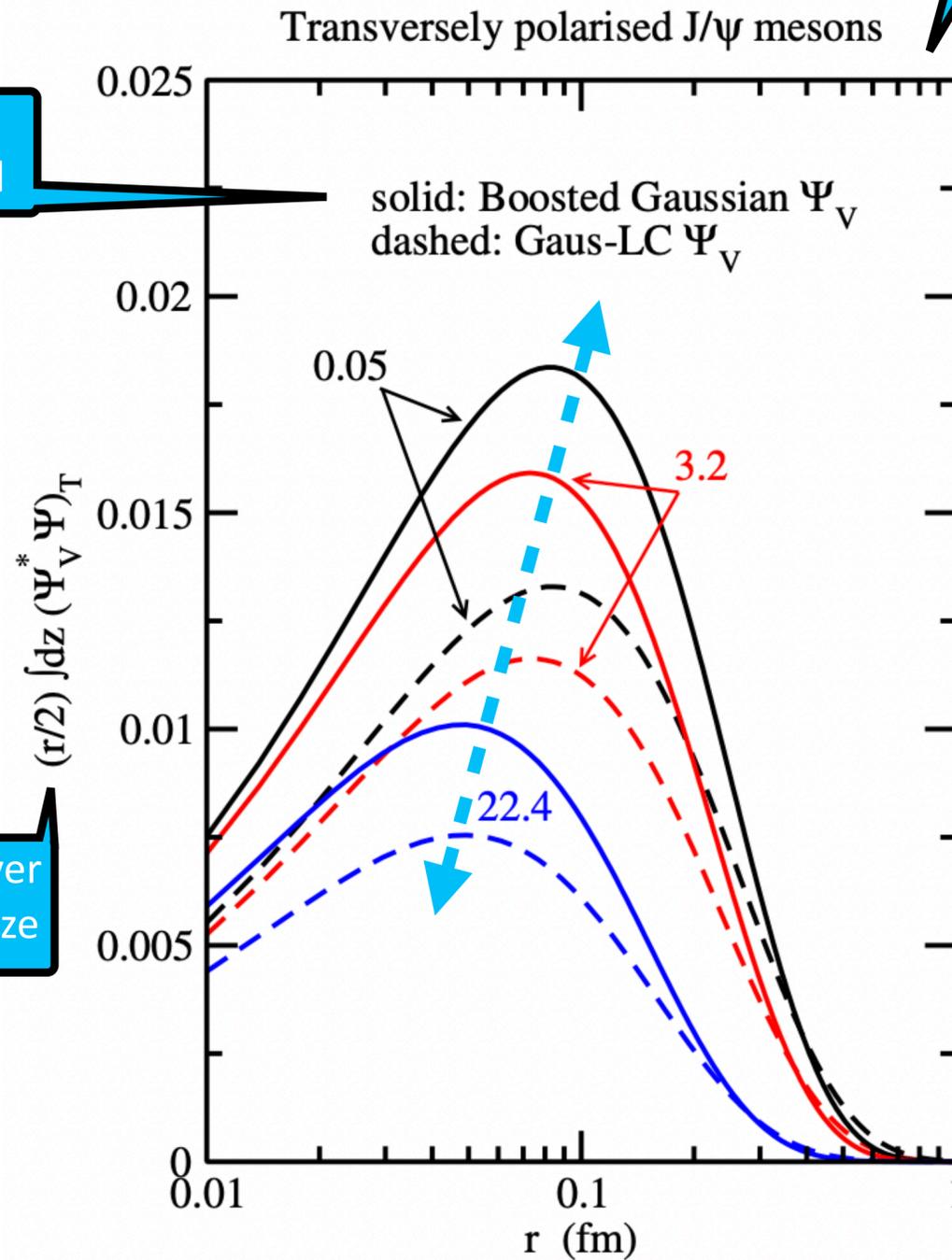
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Position of the peak moves with virtuality selecting specific dipole sizes



# 2006: Diffractive vector meson production in the dipole approach (2/5)

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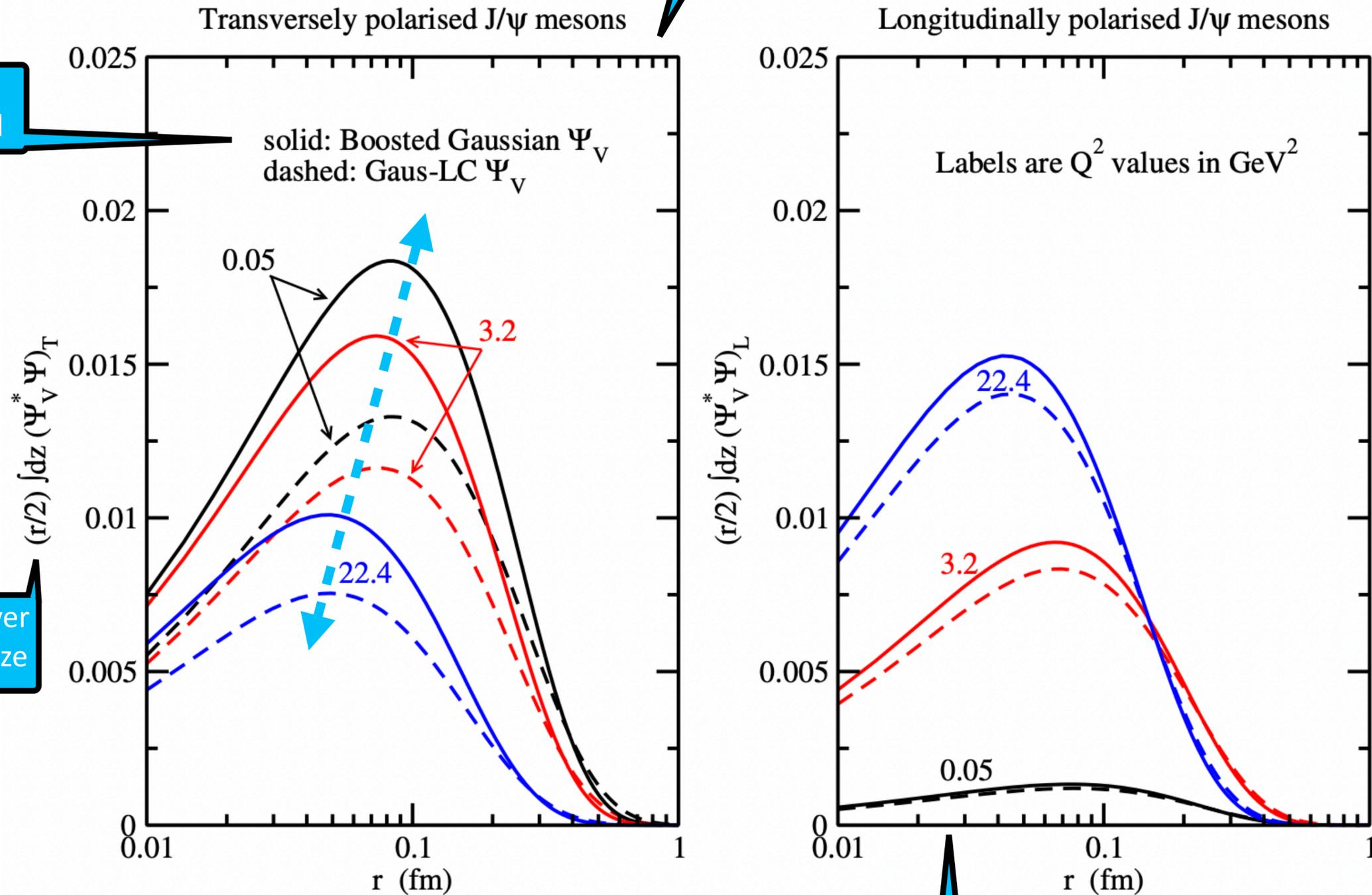
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In (quasi-) photoproduction, almost no longitudinal

# 2006: Diffractive vector meson production in the dipole approach (2/5)

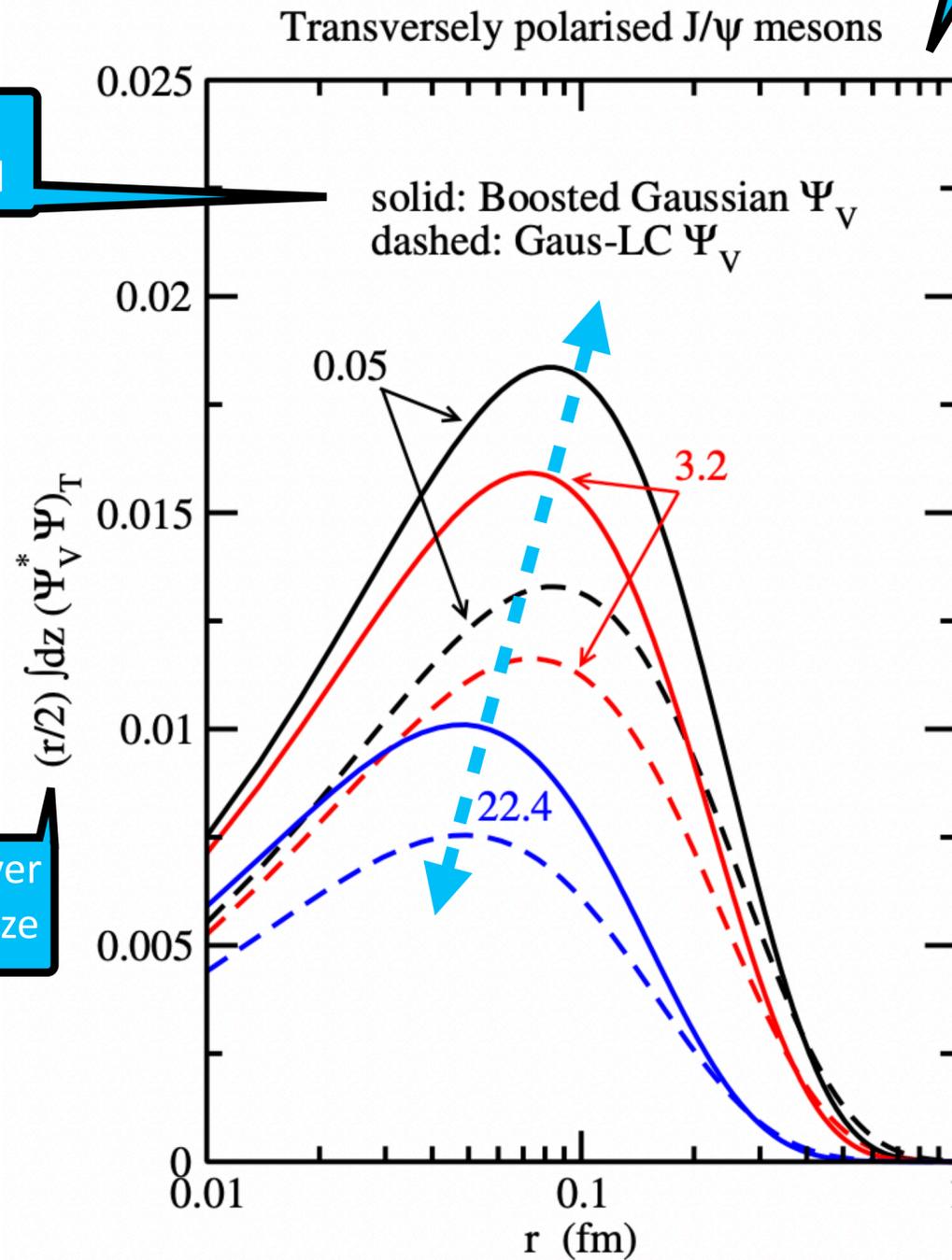
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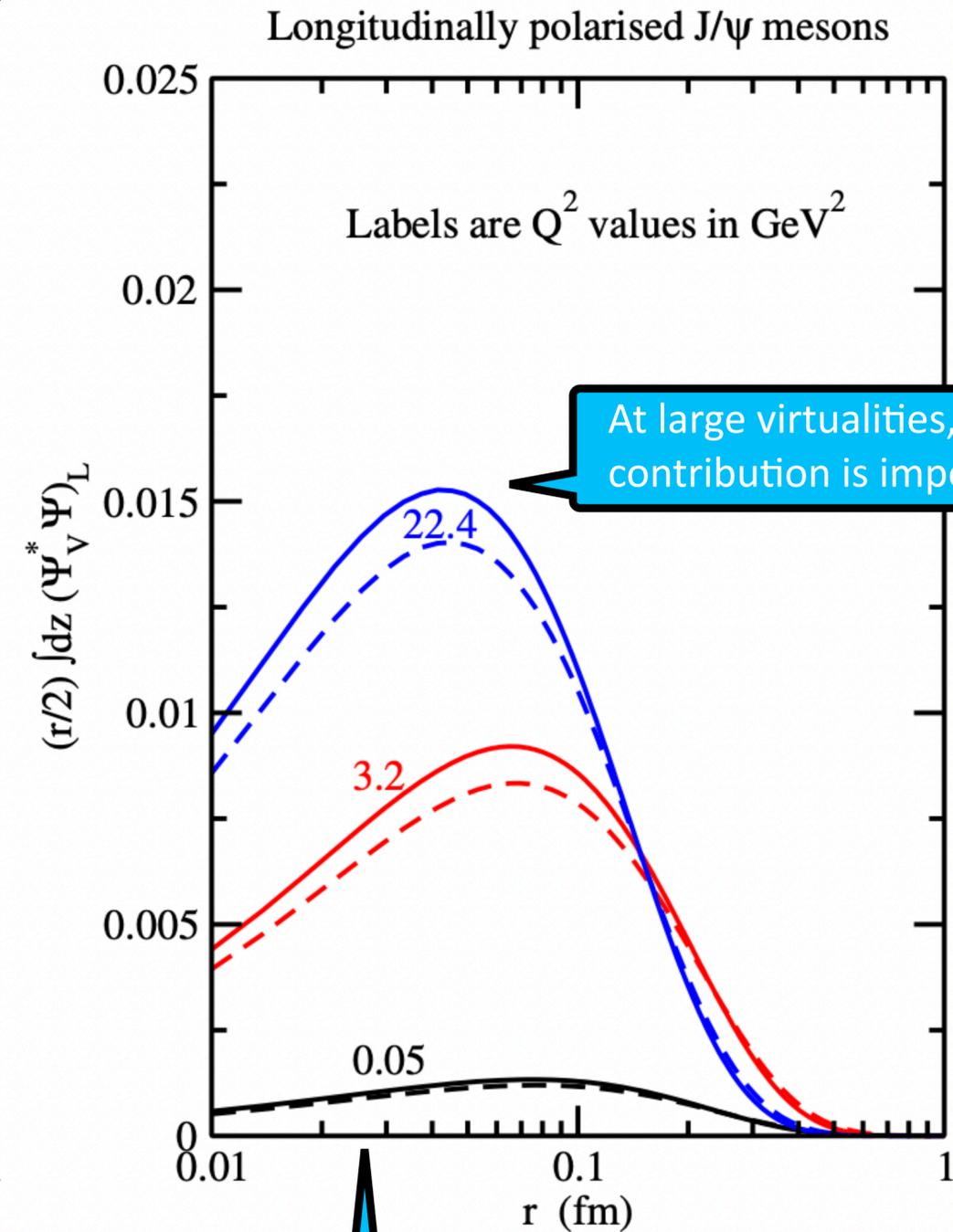
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Forward wave functions, integrated over energy fraction and scaled by dipole size

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Position of the peak moves with virtuality selecting specific dipole sizes



At large virtualities, the longitudinal contribution is important

In (quasi-) photoproduction, almost no longitudinal

2

Dipole cross sections

2

## Dipole cross sections

GBW approach

$$\begin{aligned}\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} &\equiv 2[1 - \text{Re}S(x, r, b)] \equiv 2\mathcal{N}(x, r, b) \\ &= 2\mathcal{N}(x, r)\Theta(b_S - b),\end{aligned}$$

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GBW approach

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Profile in impact parameter

$$\sigma_{q\bar{q}}(x, r) = \sigma_0\mathcal{N}(x, r),$$

$$\sigma_0 \equiv 2\pi b_S^2$$

Related to the average square radius of the target in impact parameter

2

Dipole cross sections

b-Sat approach

$$\frac{d\sigma_{q\bar{q}}}{d^2\mathbf{b}} = 2 \left[ 1 - \exp\left(-\frac{\pi^2}{2N_c} r^2 \alpha_S(\mu^2) x g(x, \mu^2) T(b)\right) \right].$$

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b-CGC approach

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$$= 2 \times \begin{cases} \mathcal{N}_0 \left(\frac{rQ_s}{2}\right)^{2(\gamma_s + (1/\kappa\lambda Y)\ln(2/rQ_s))} & : rQ_s \leq 2 \\ 1 - e^{-A\ln^2(BrQ_s)} & : rQ_s > 2 \end{cases},$$

# 2006: Diffractive vector meson production in the dipole approach (3/5)

2

Dipole cross sections

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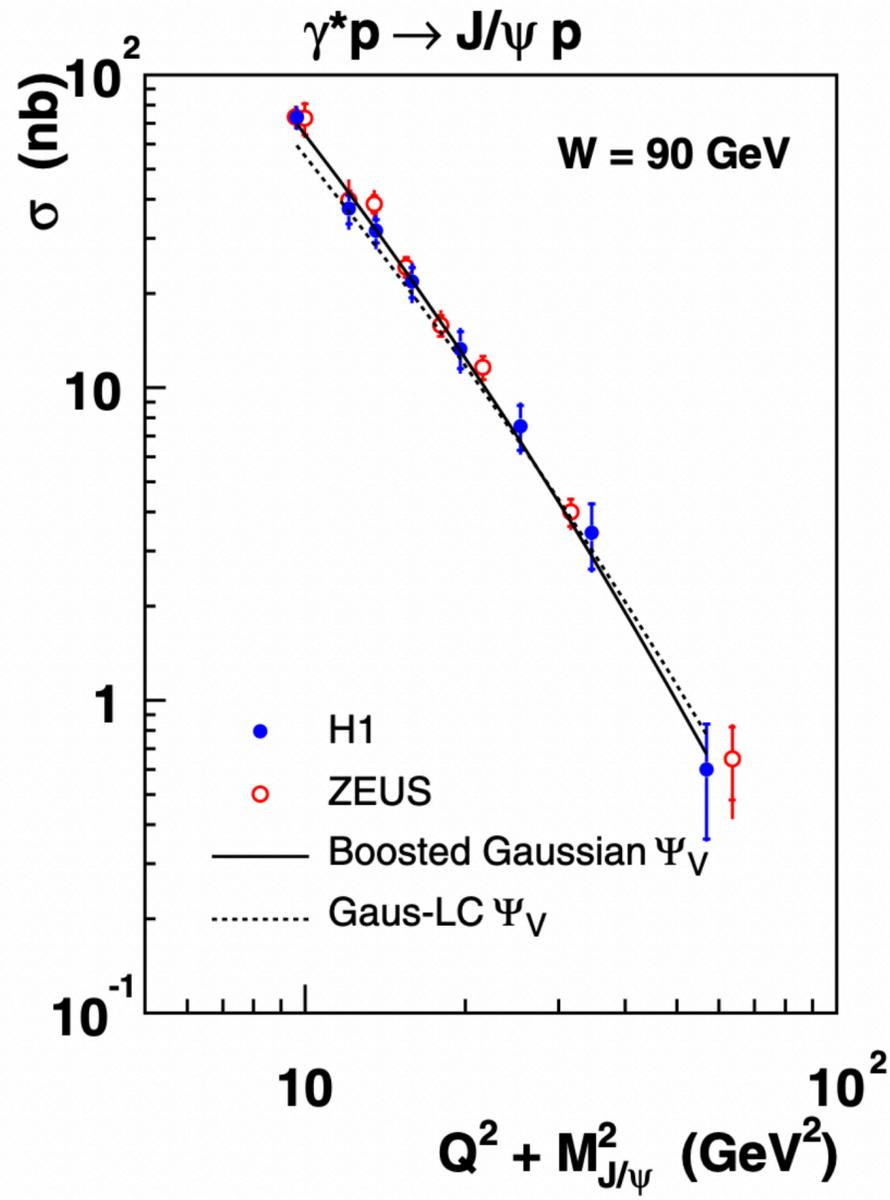
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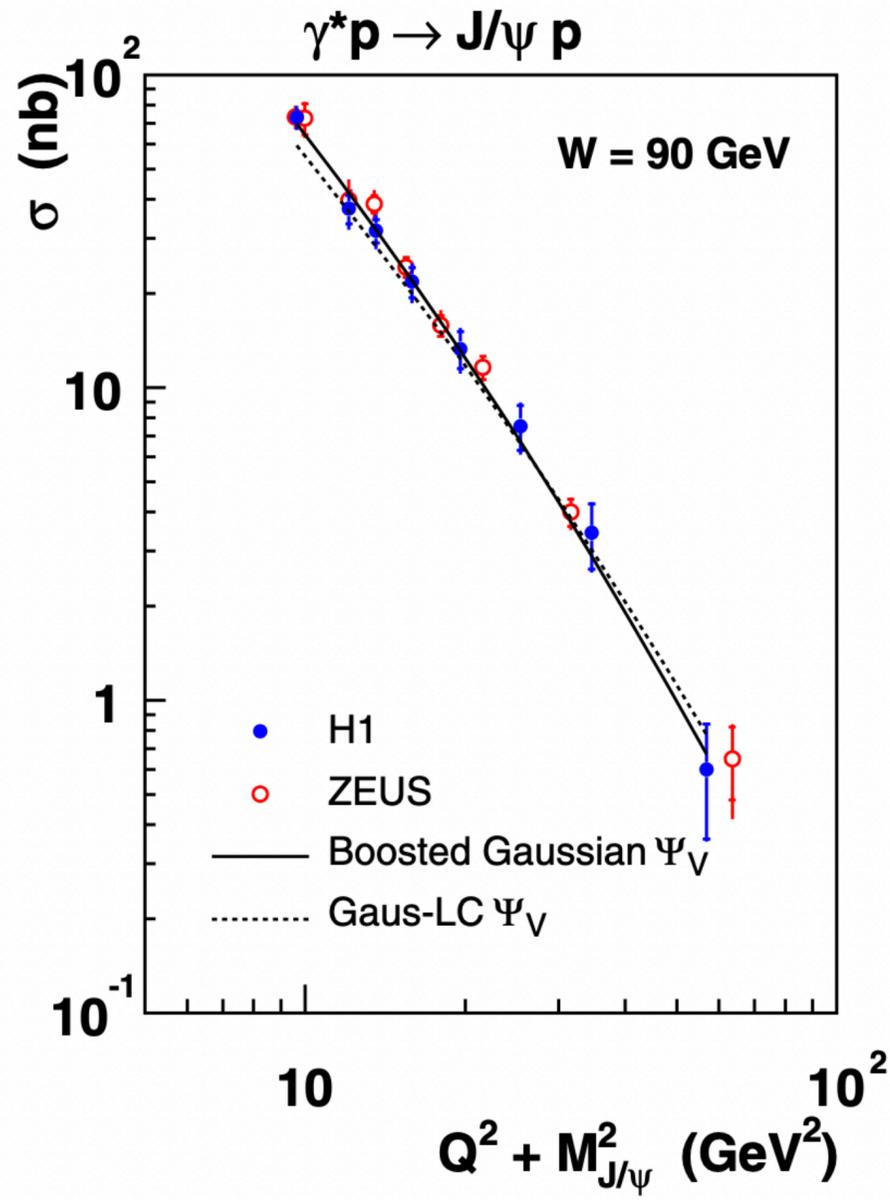
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Results

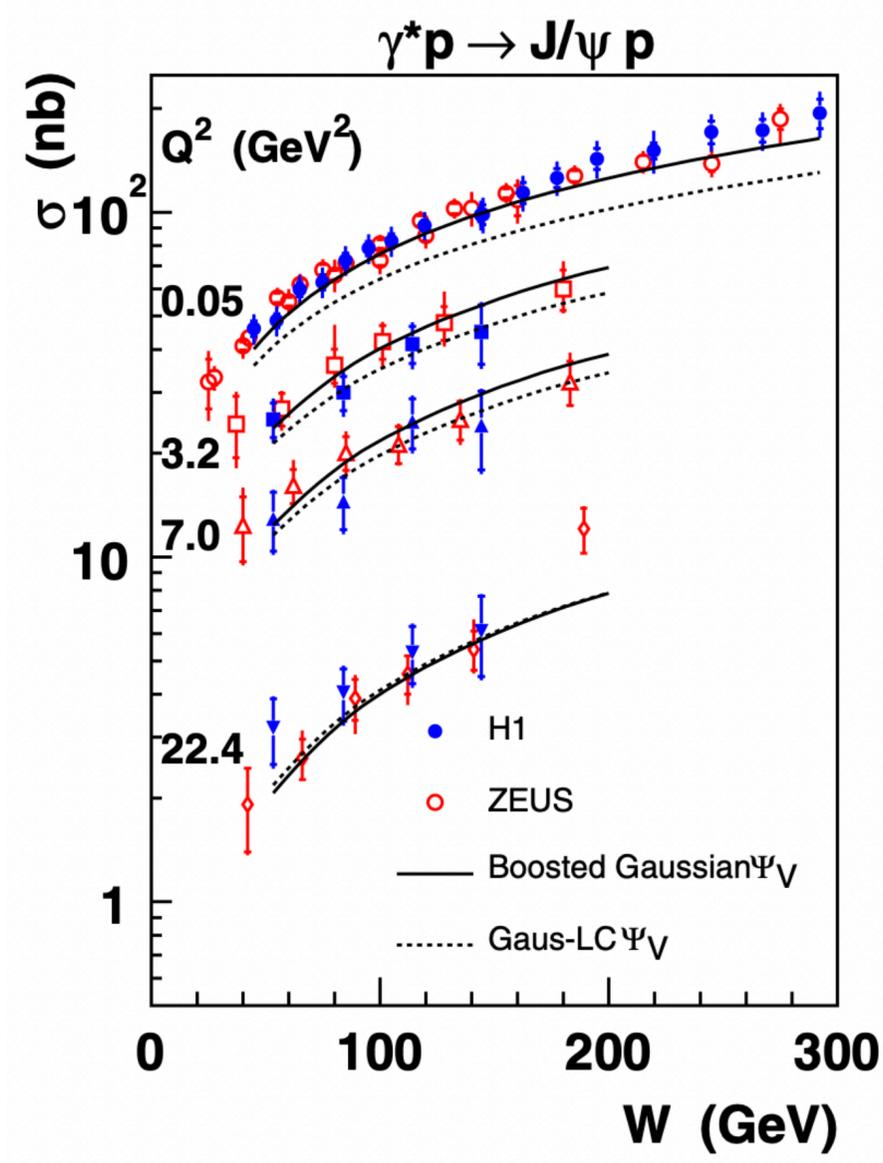


Cross section decreases with the scale

Results

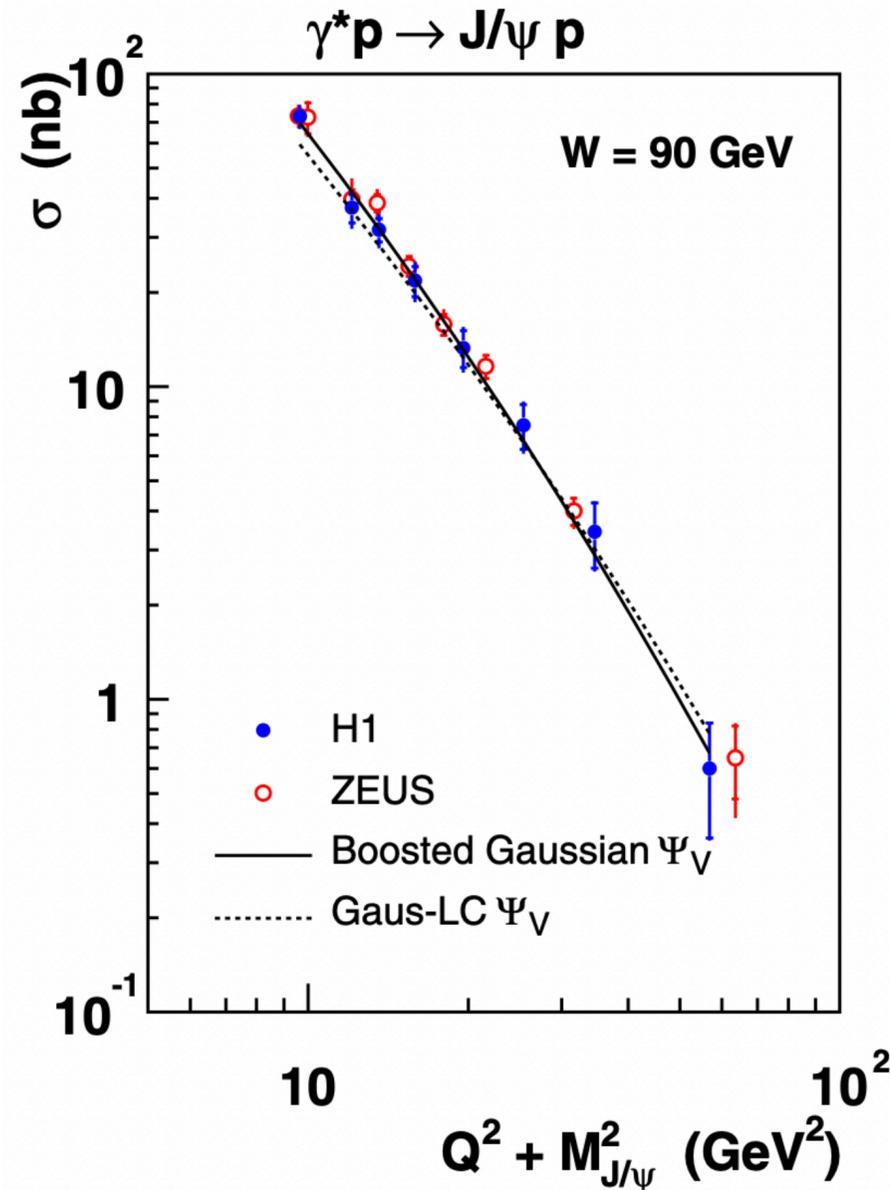


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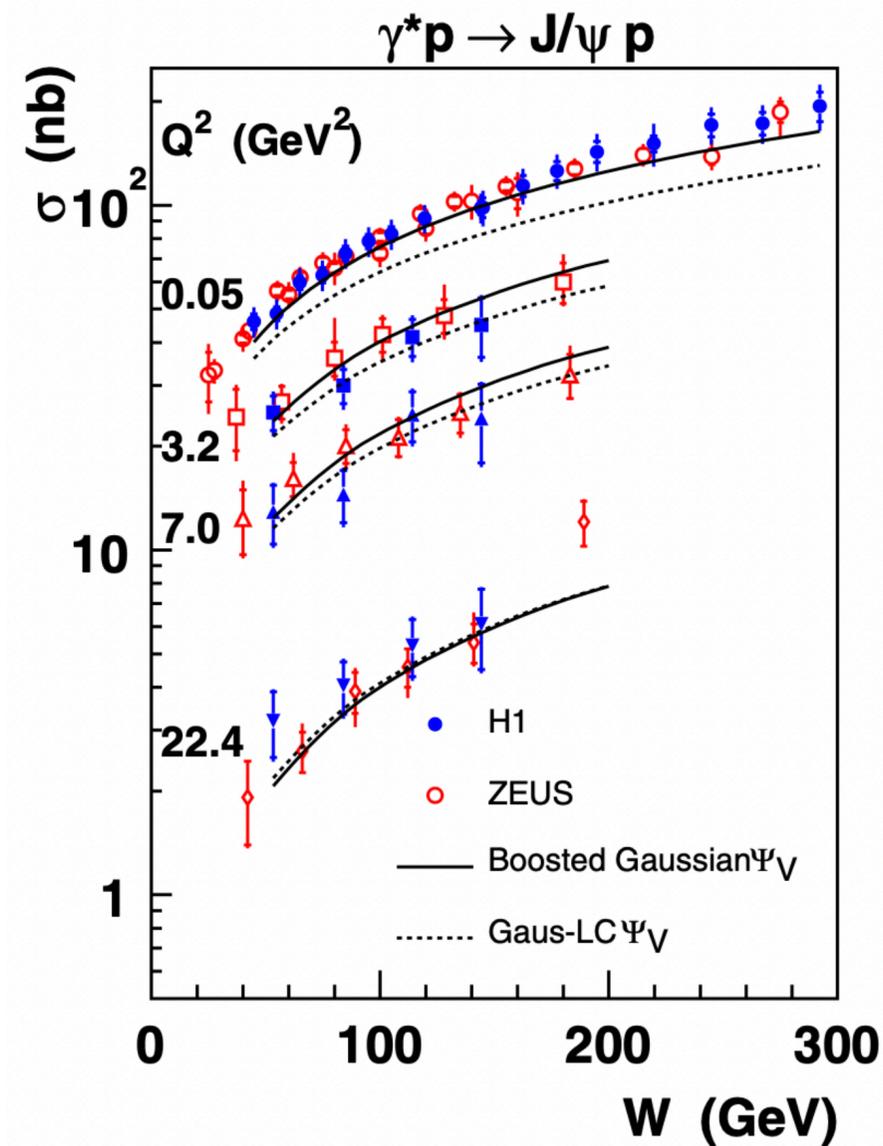


Cross section grows with energy for different virtualities

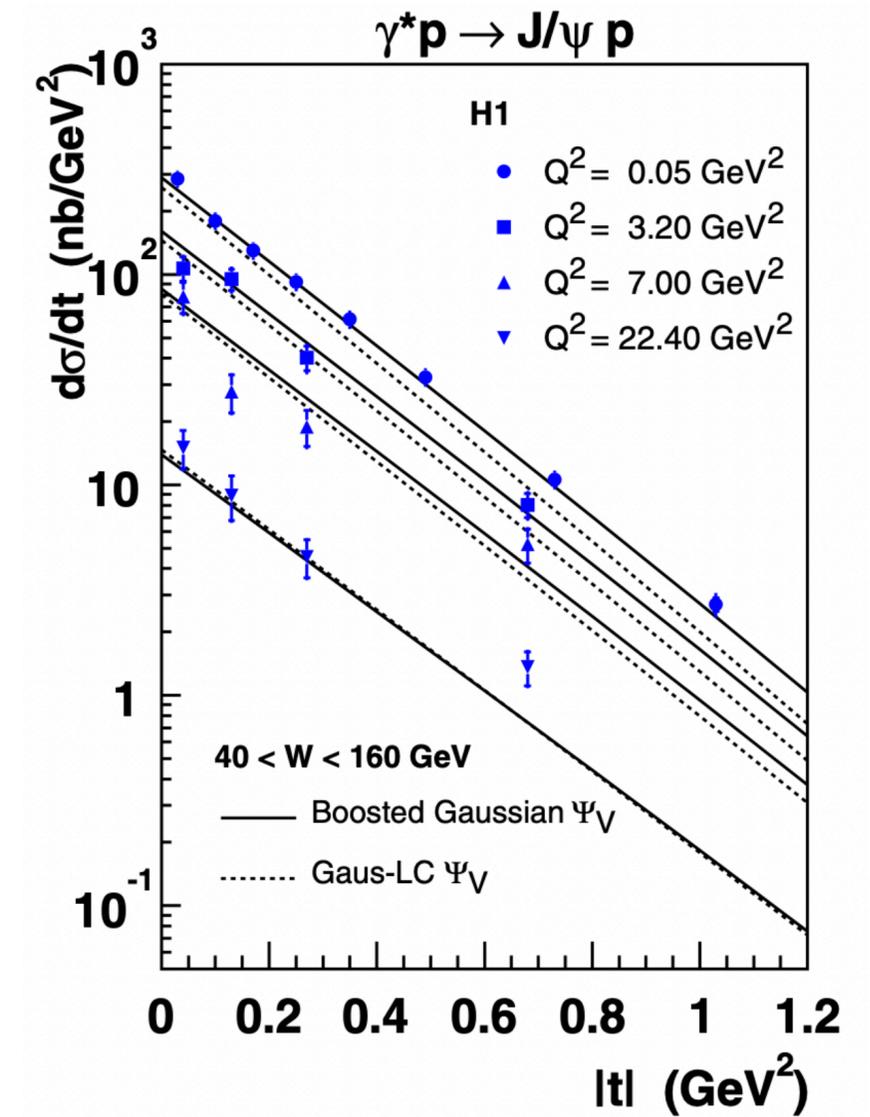
## Results



Cross section decreases with the scale

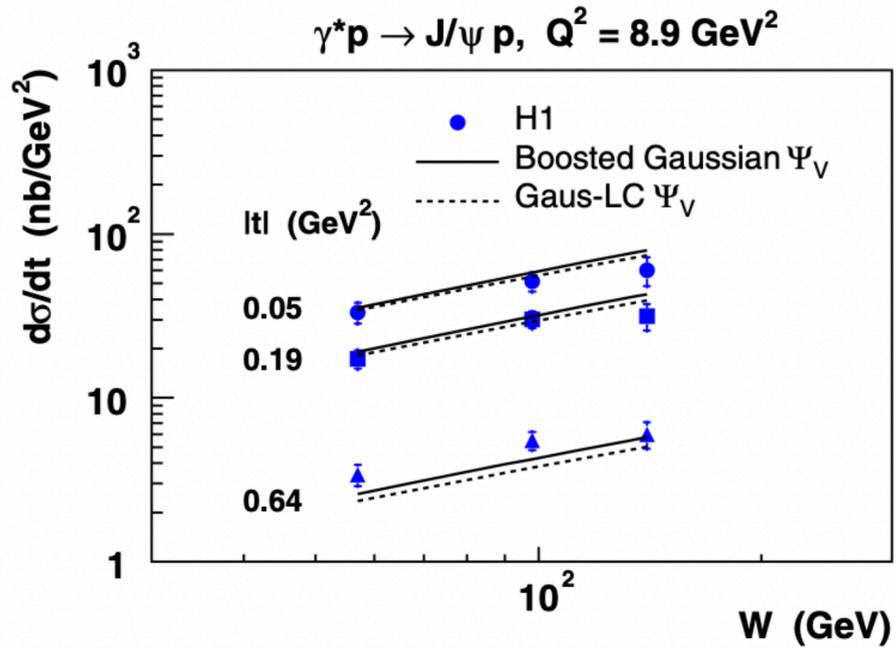
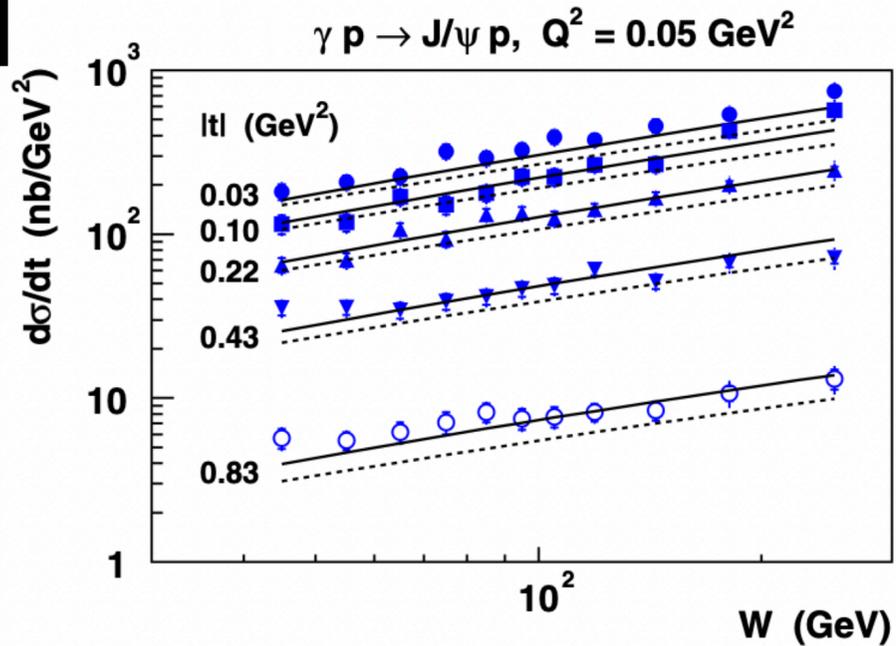


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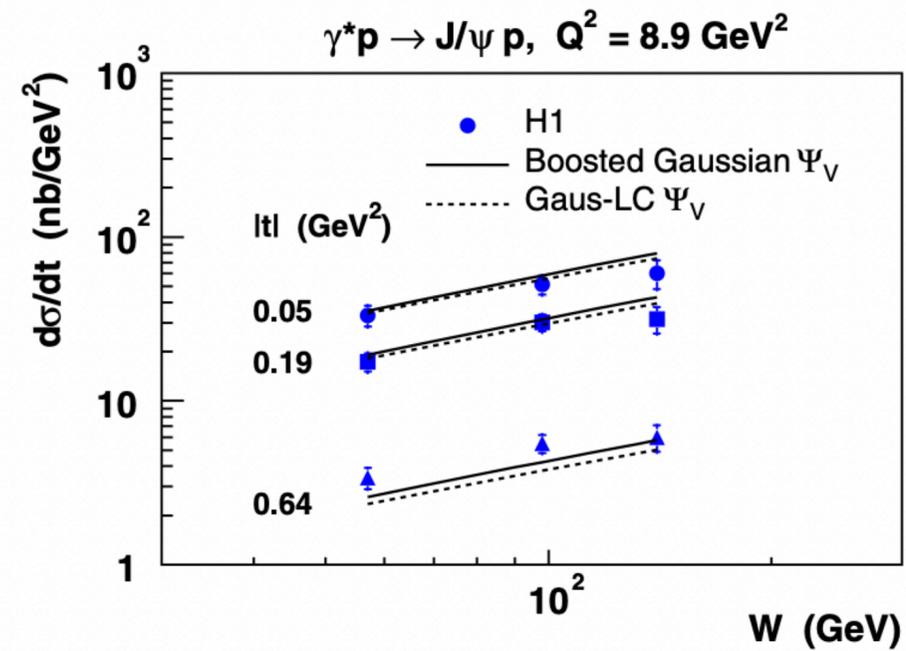
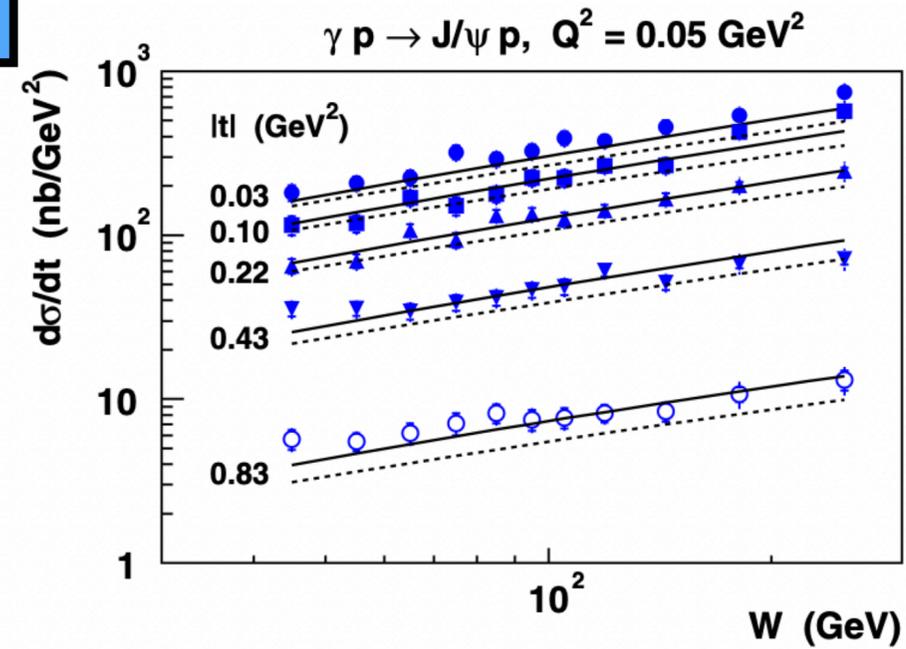
Consistent with Gaussian shape for different virtualities

## Results

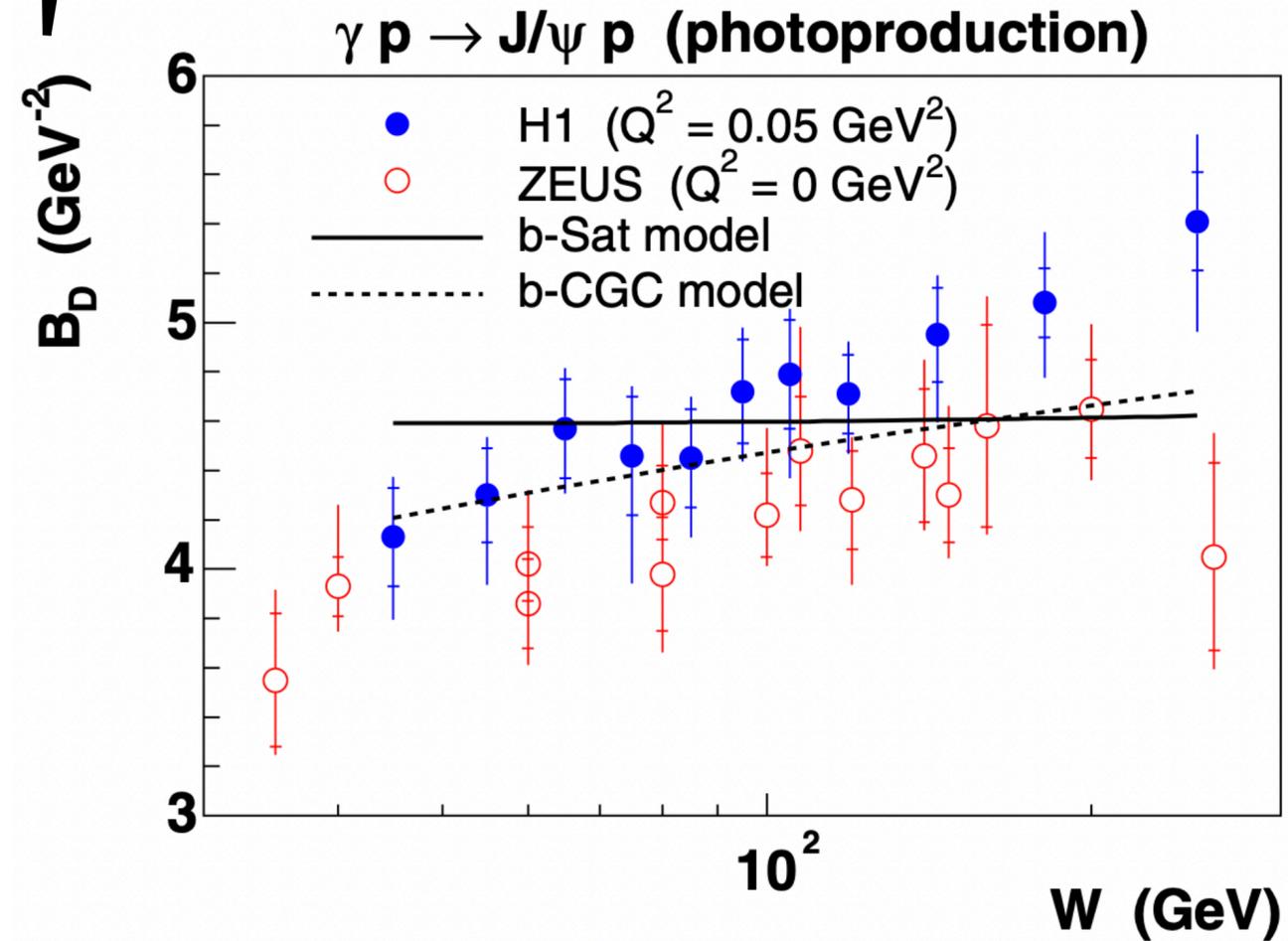


Cross section grows with energy for different momentum transfer

## Results



Gaussian profile grows with energy



Cross section grows with energy for different momentum transfer

Reminder: Geometric scaling in DIS

$$\sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(x, Q^2) = \sigma_{\text{tot}}^{\gamma^* p \rightarrow X}(\tau), \quad \tau = Q^2 / Q_s^2(x).$$

$$Q_s(x) = Q_0 \left( \frac{x}{x_0} \right)^{-\lambda/2}, \quad Q_0 \equiv 1 \text{ GeV}$$

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## Geometric scaling in diffractive VM production

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# 2006: Geometric scaling for vector mesons

## Reminder: Geometric scaling in DIS

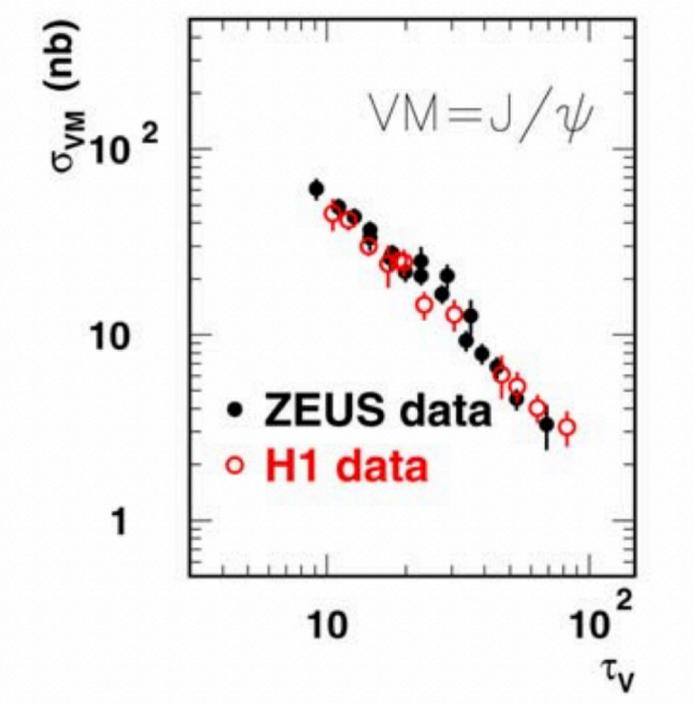
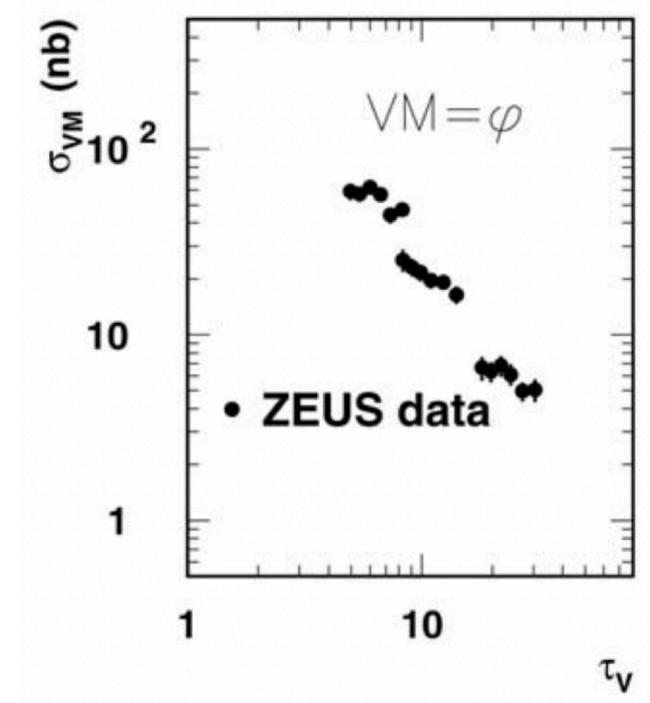
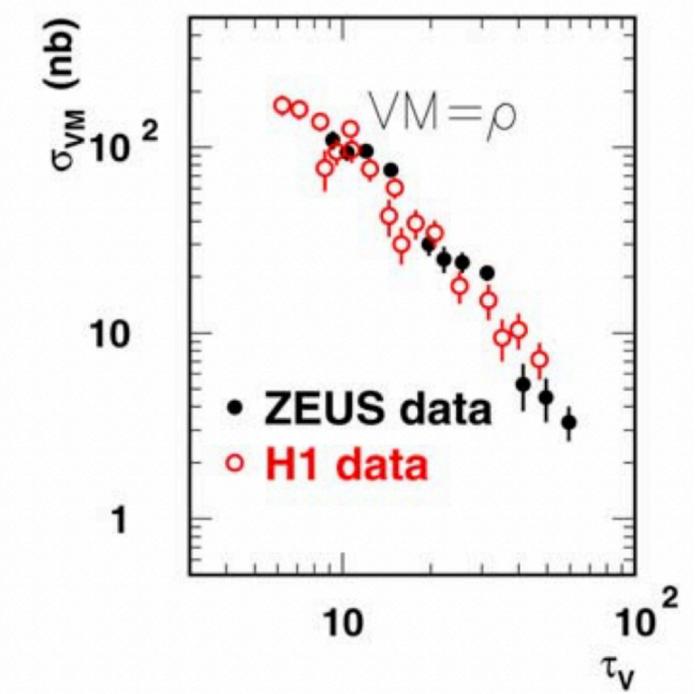
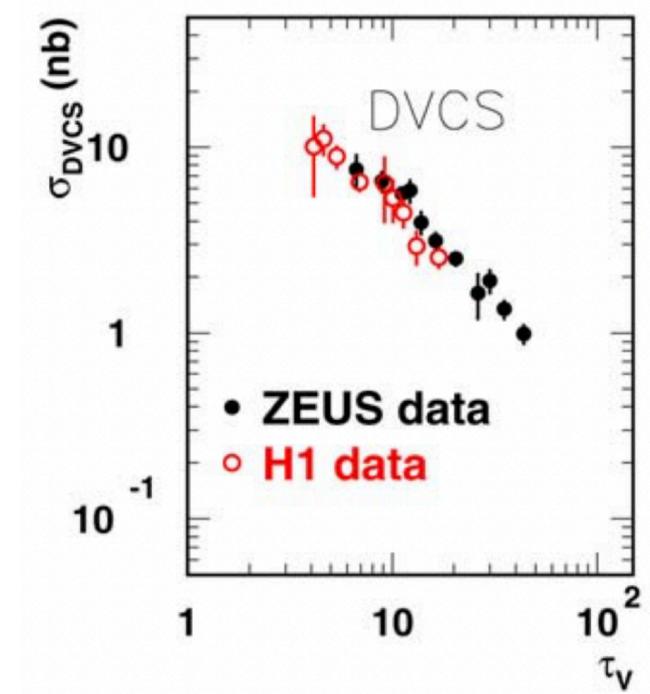
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This process has been extensively studied at HERA as a function of:

Mass of the vector meson

Virtuality of the photon

CMS energy of the photon-proton system

Mandelstam- $t$

Polarisation structure (not shown)

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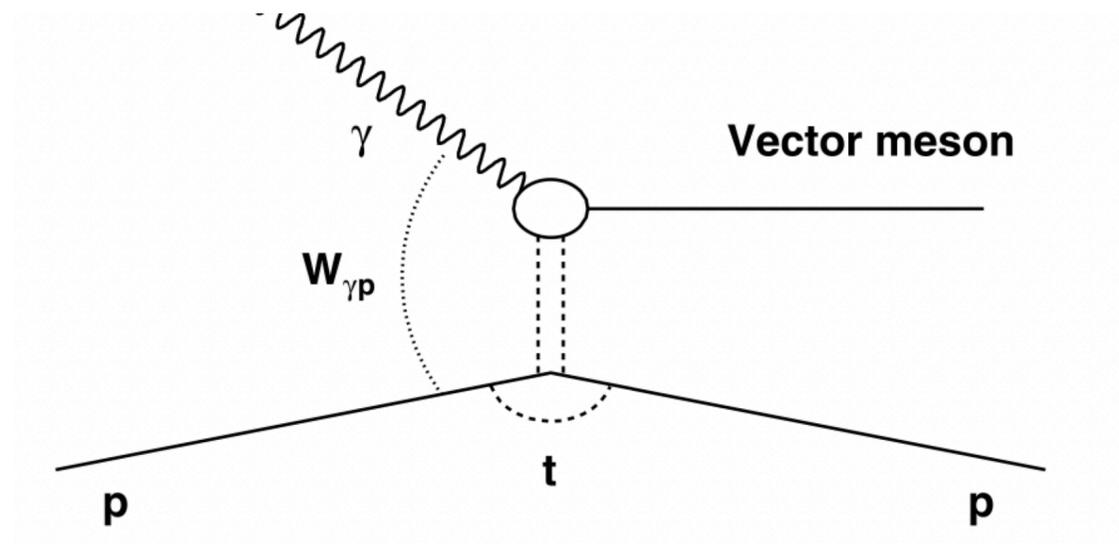
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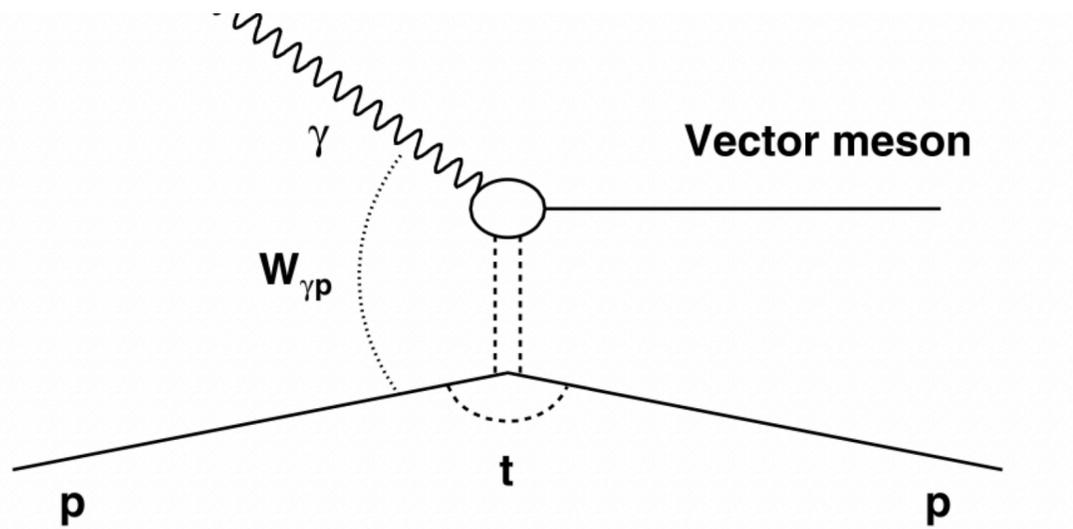
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# Dissociative vector meson production

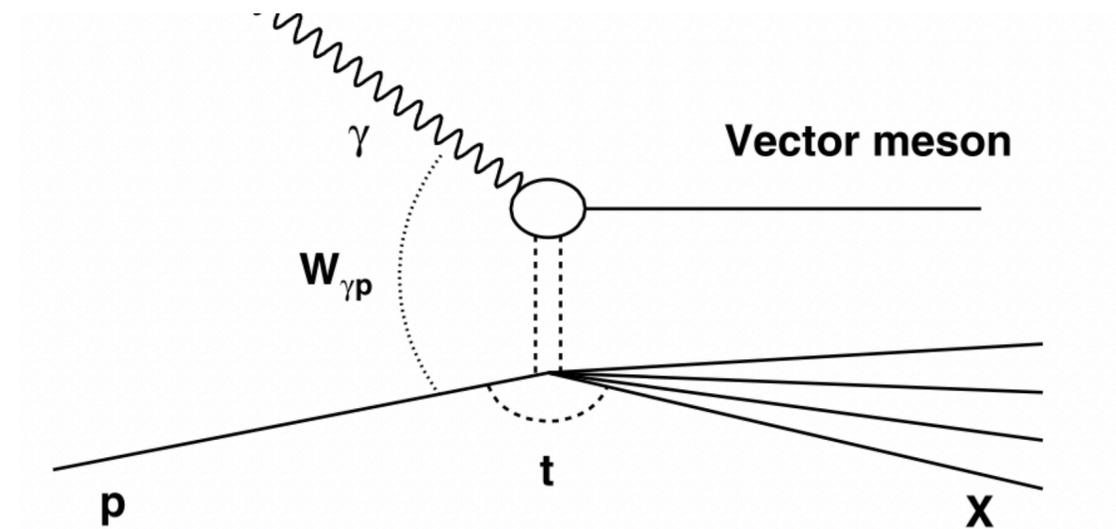


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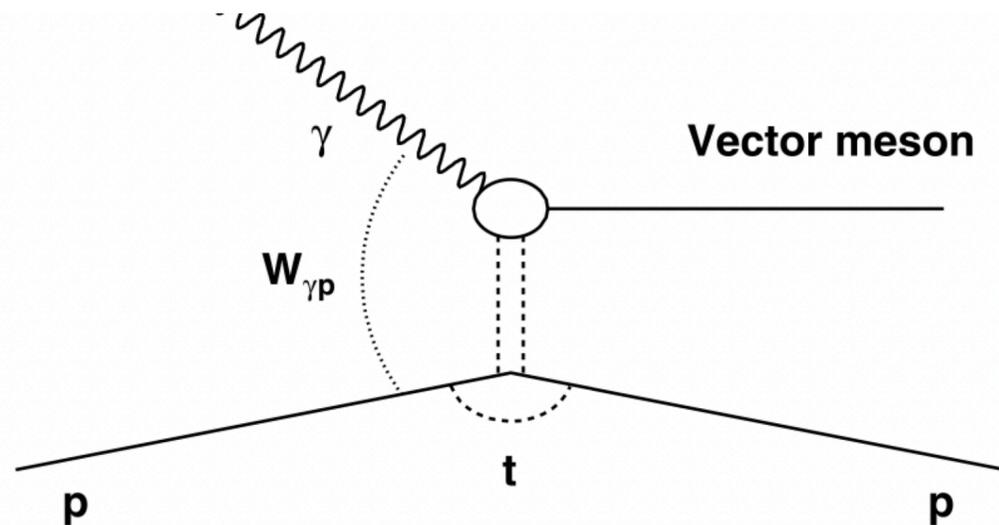


There is a similar process (called dissociation or incoherent), where the proton dissociates in a final state with the same quantum numbers as the proton

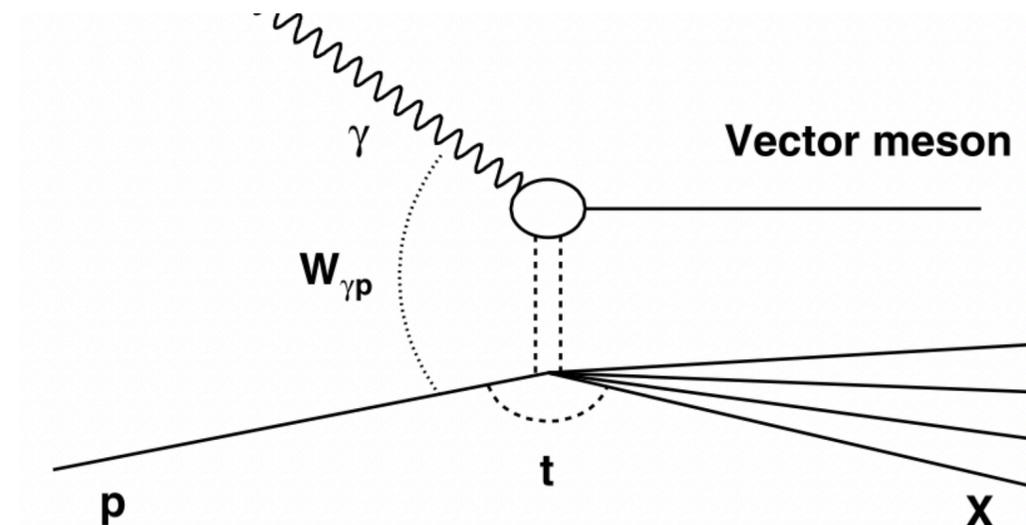
# Dissociative vector meson production

Average over target configurations

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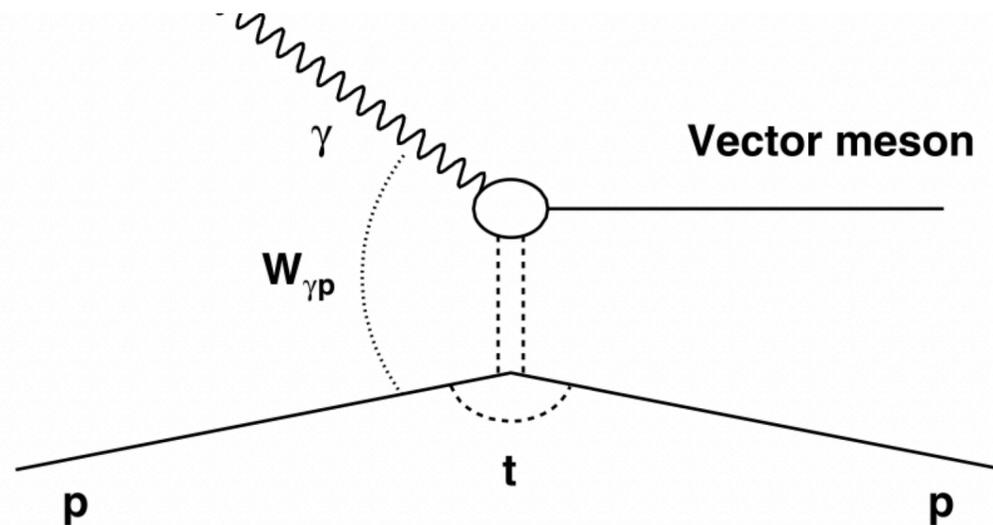
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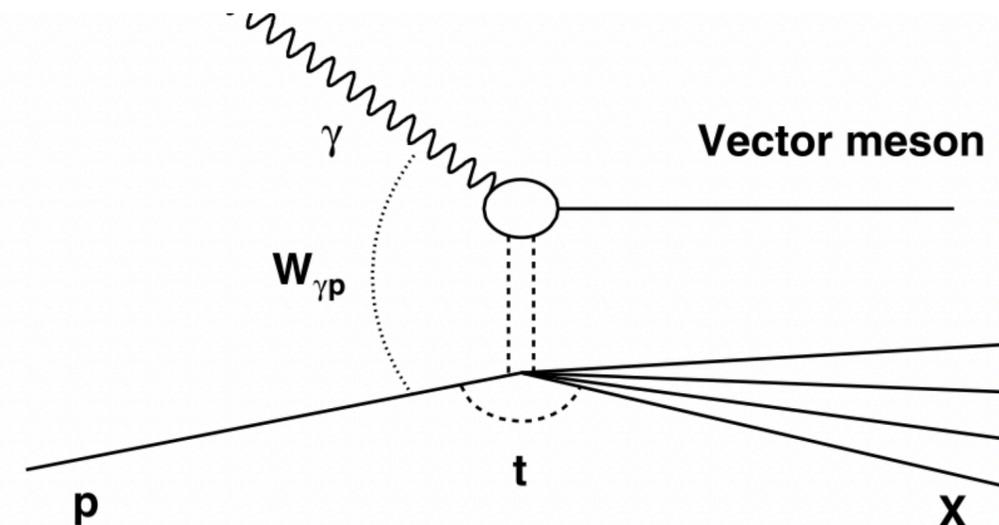
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Variance over target configurations

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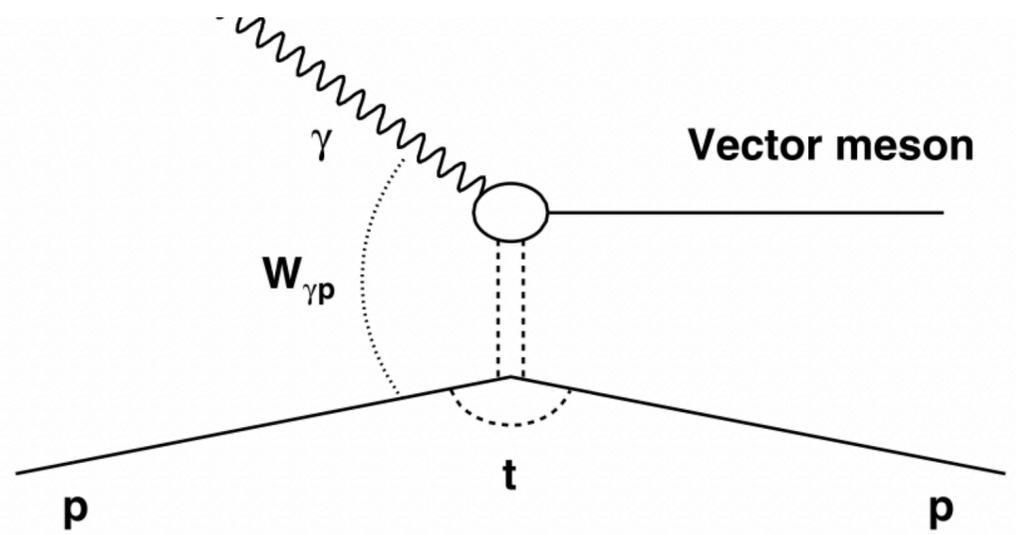
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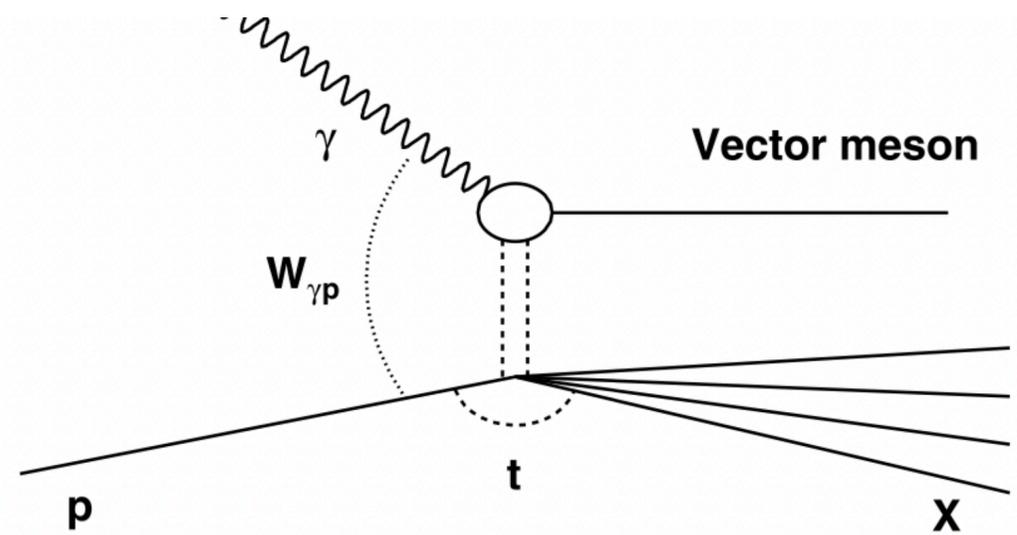
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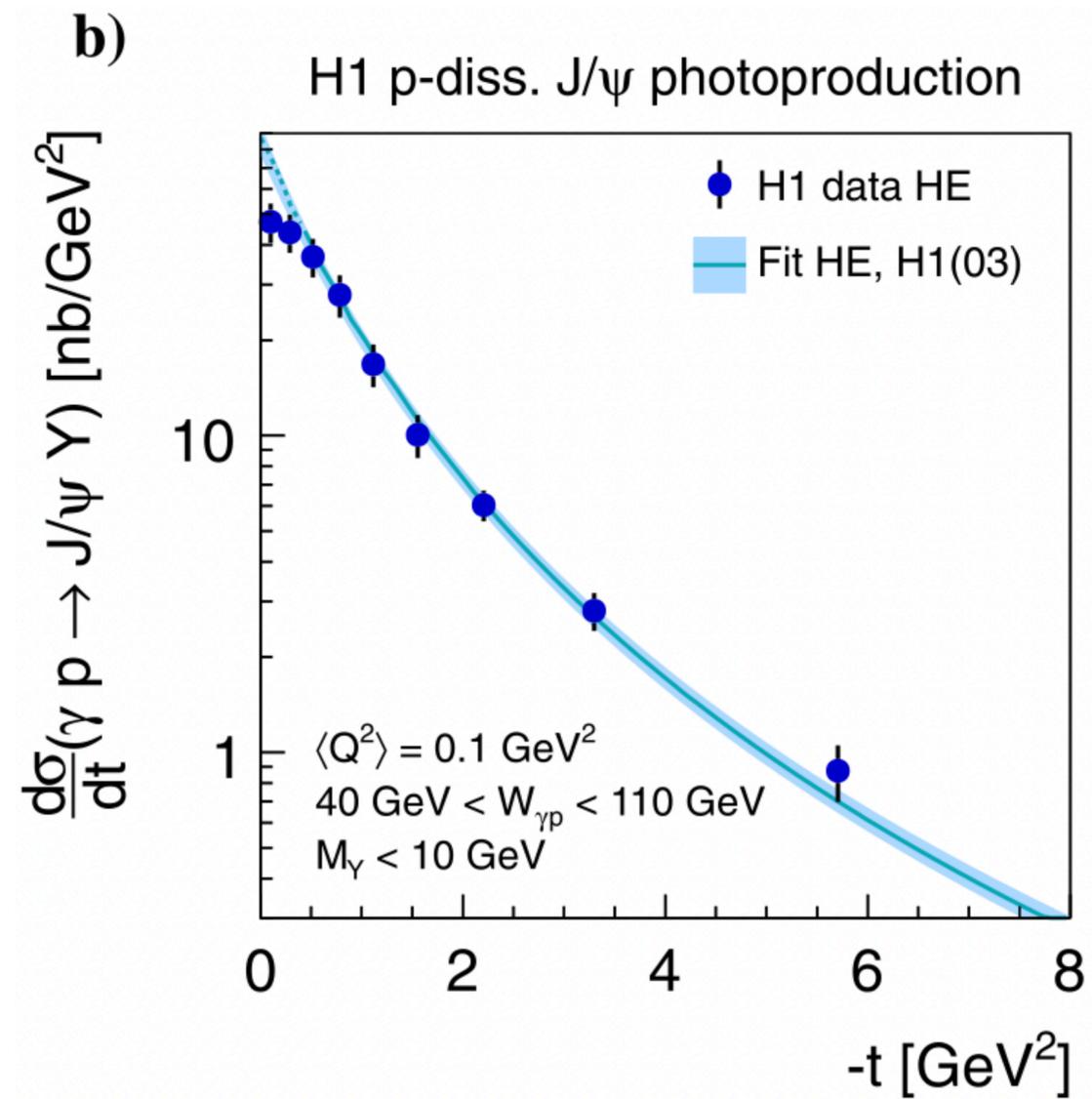


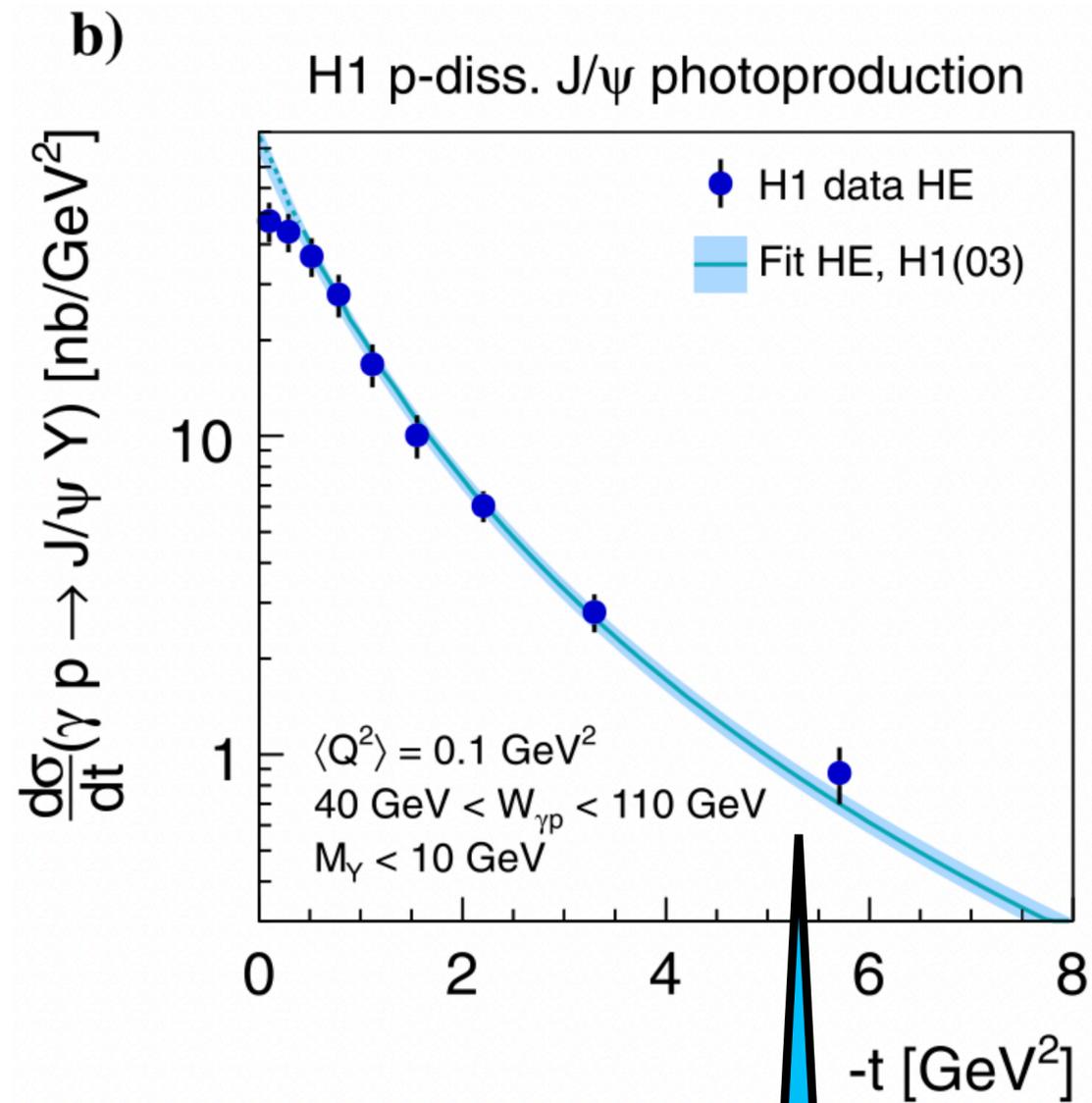
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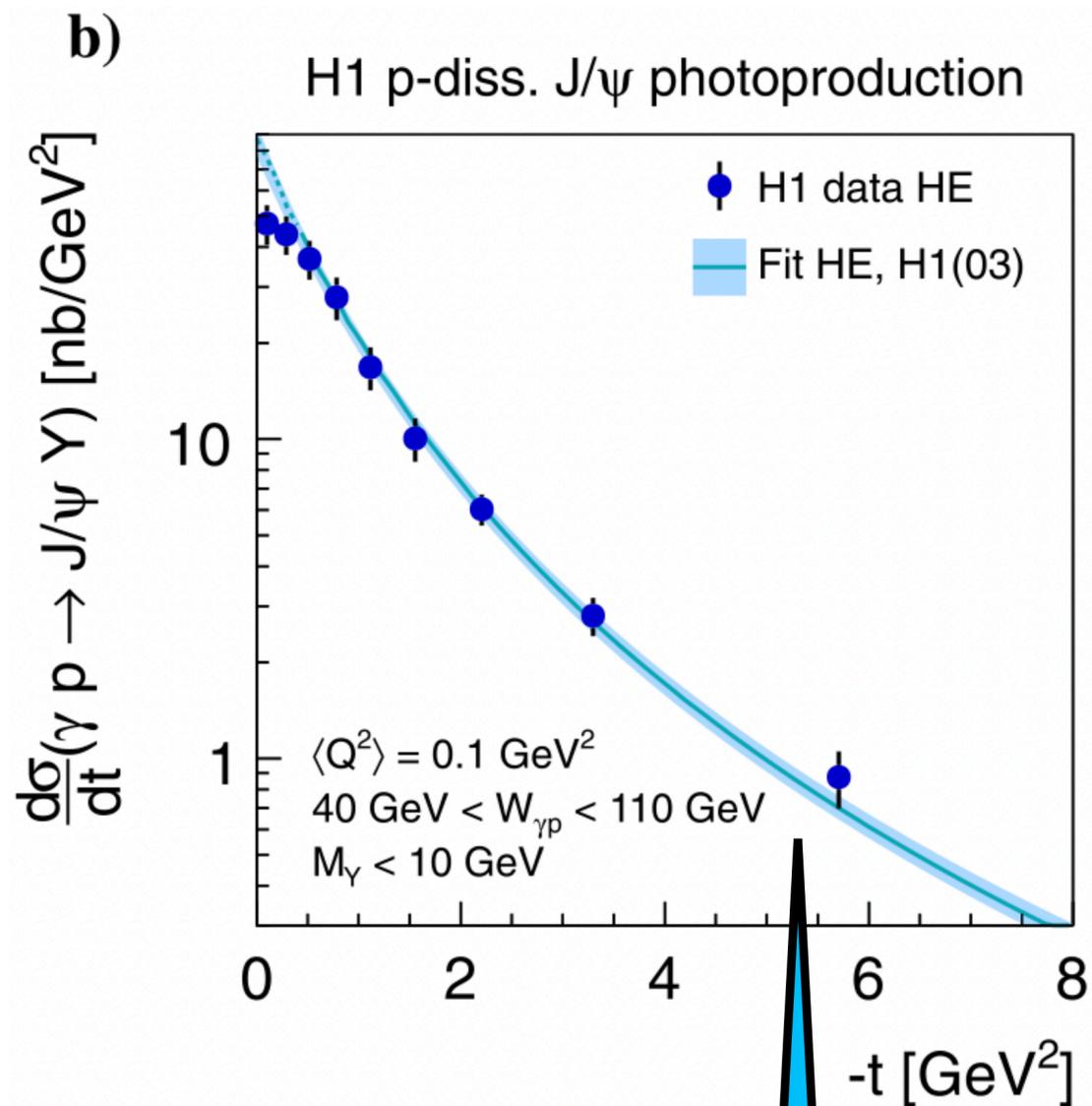




Fit:

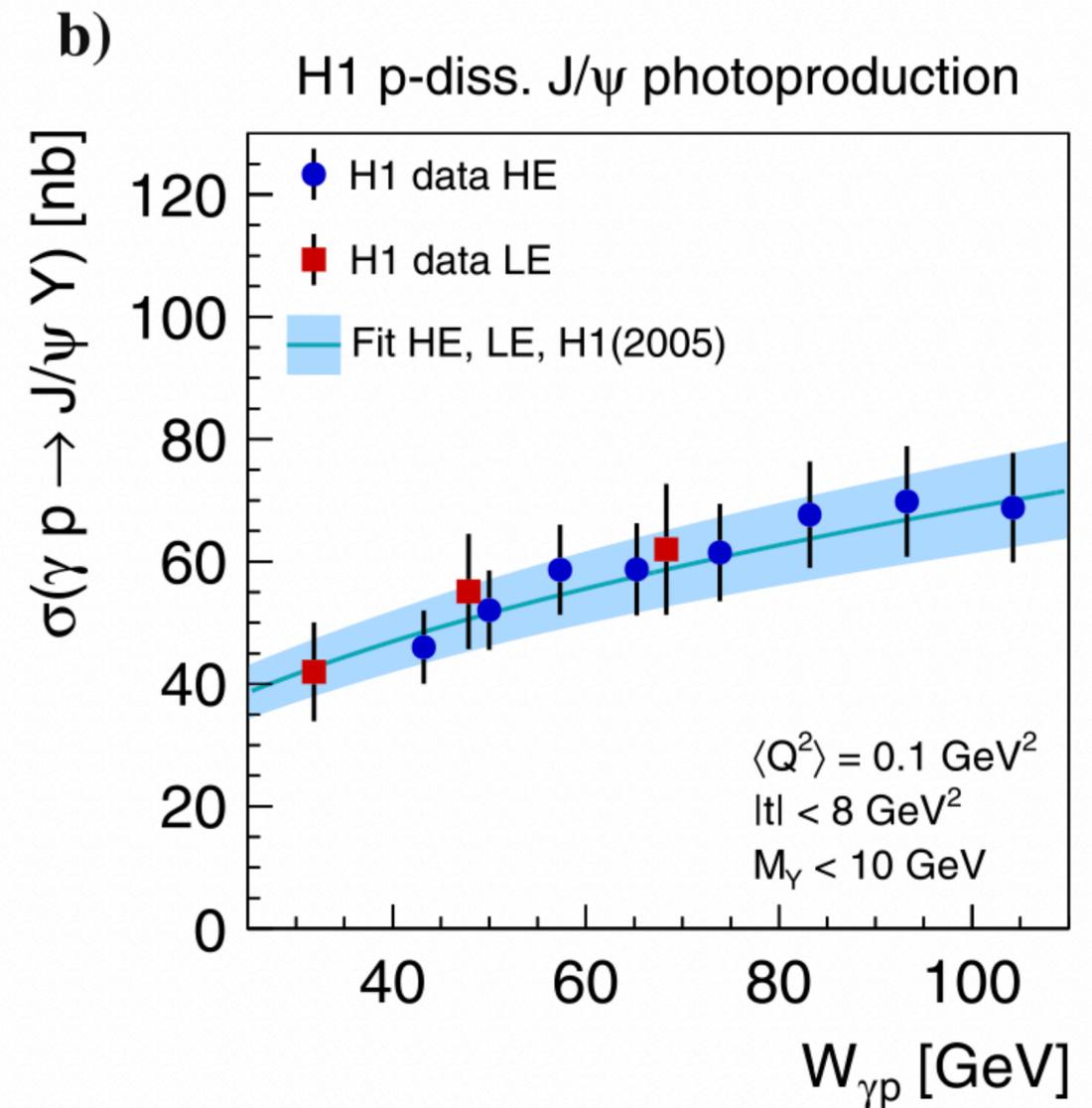
$$d\sigma/dt = N_{pd} (1 + (b_{pd}/n)|t|)^{-n}$$

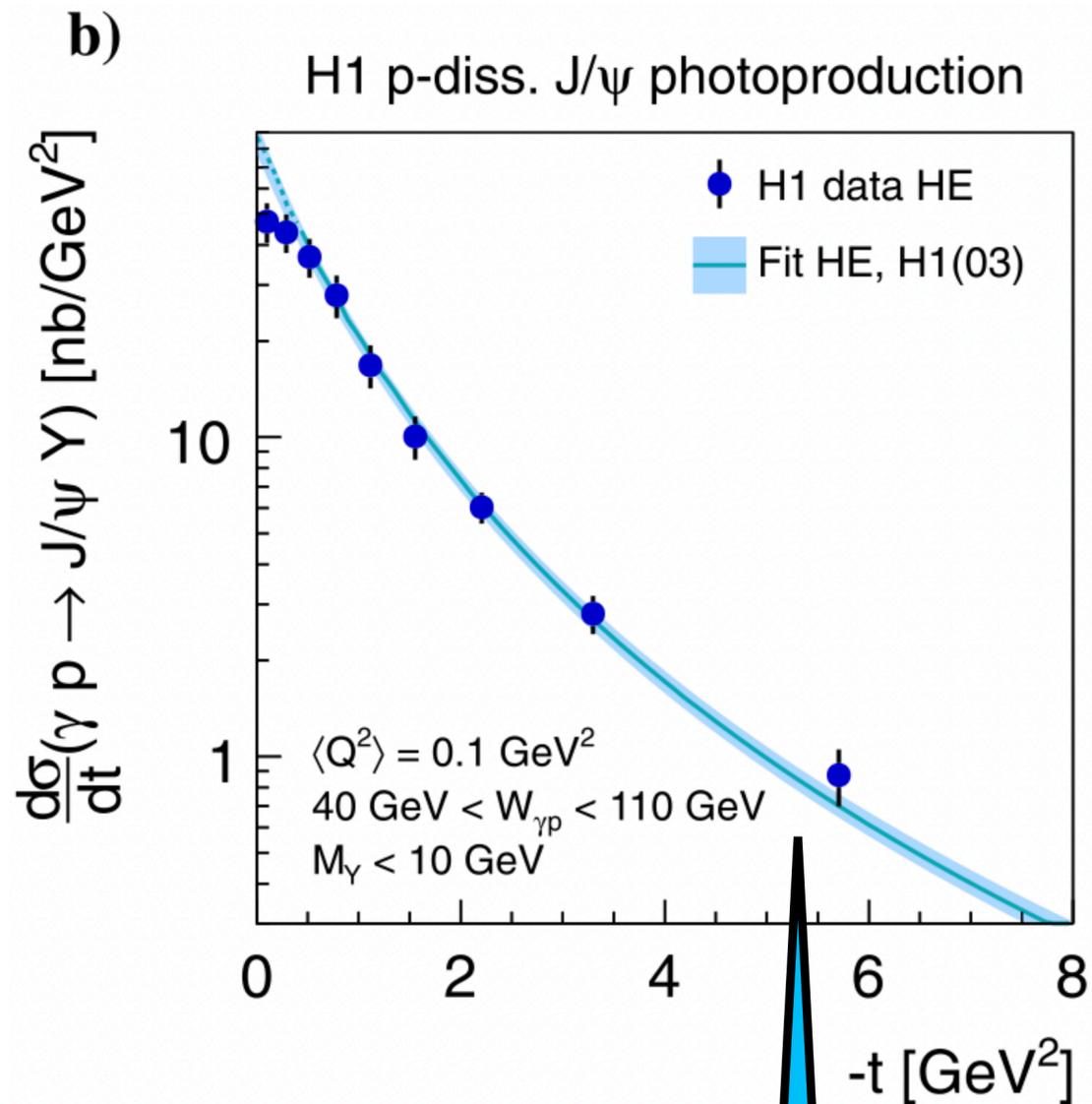
# 2013: Diffractive dissociative J/ψ photo production



Fit:

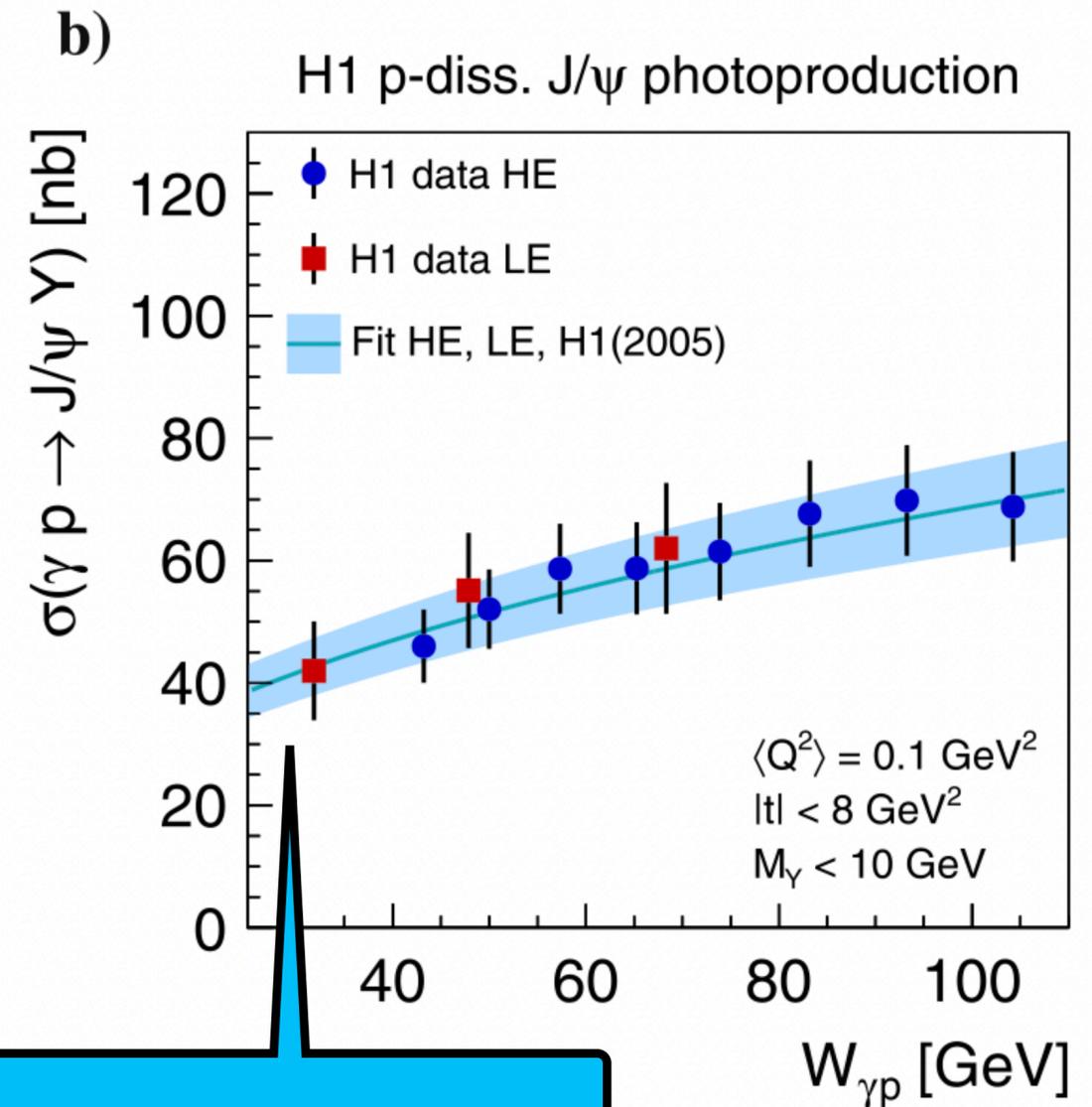
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Fit:

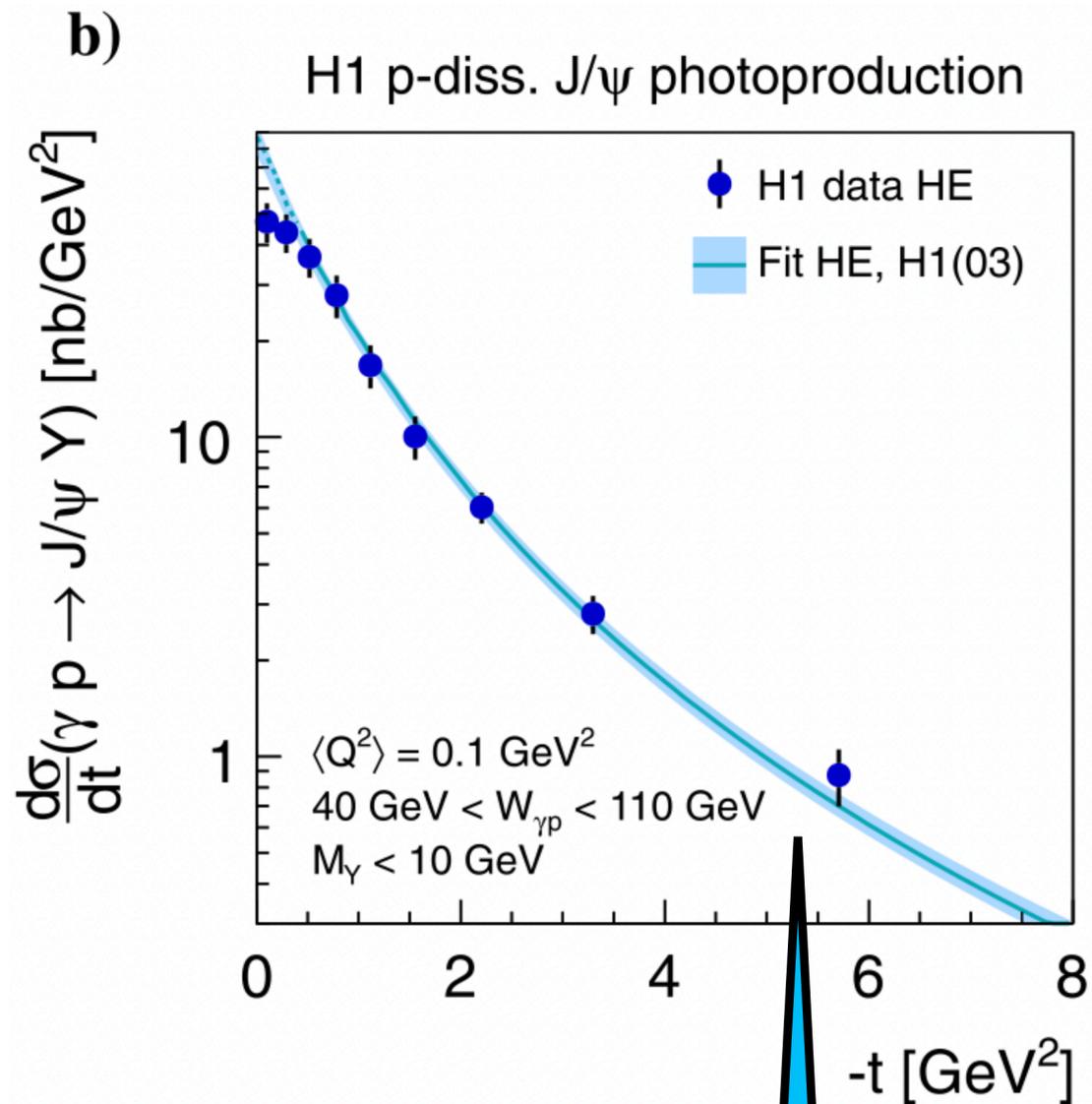
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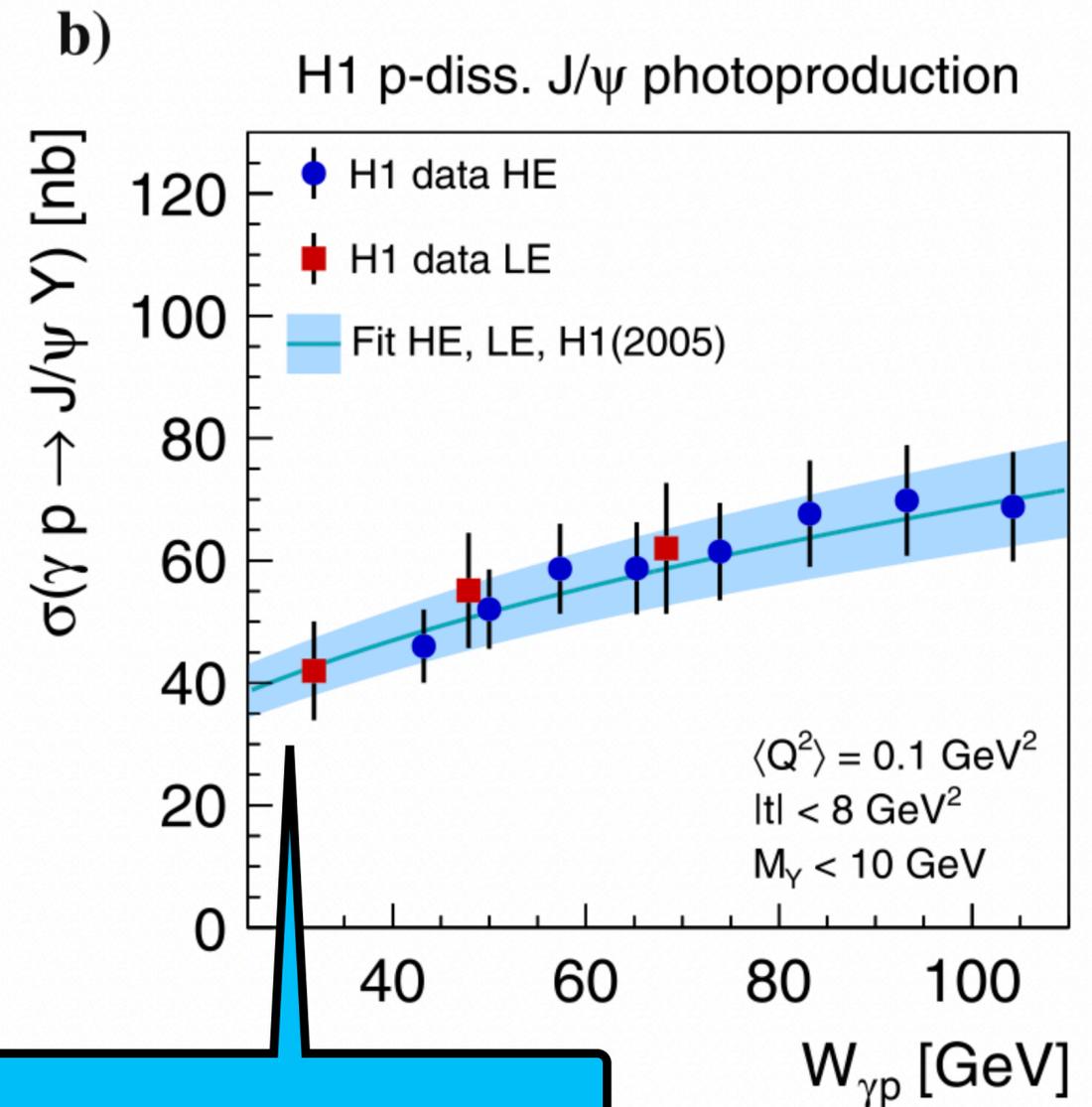
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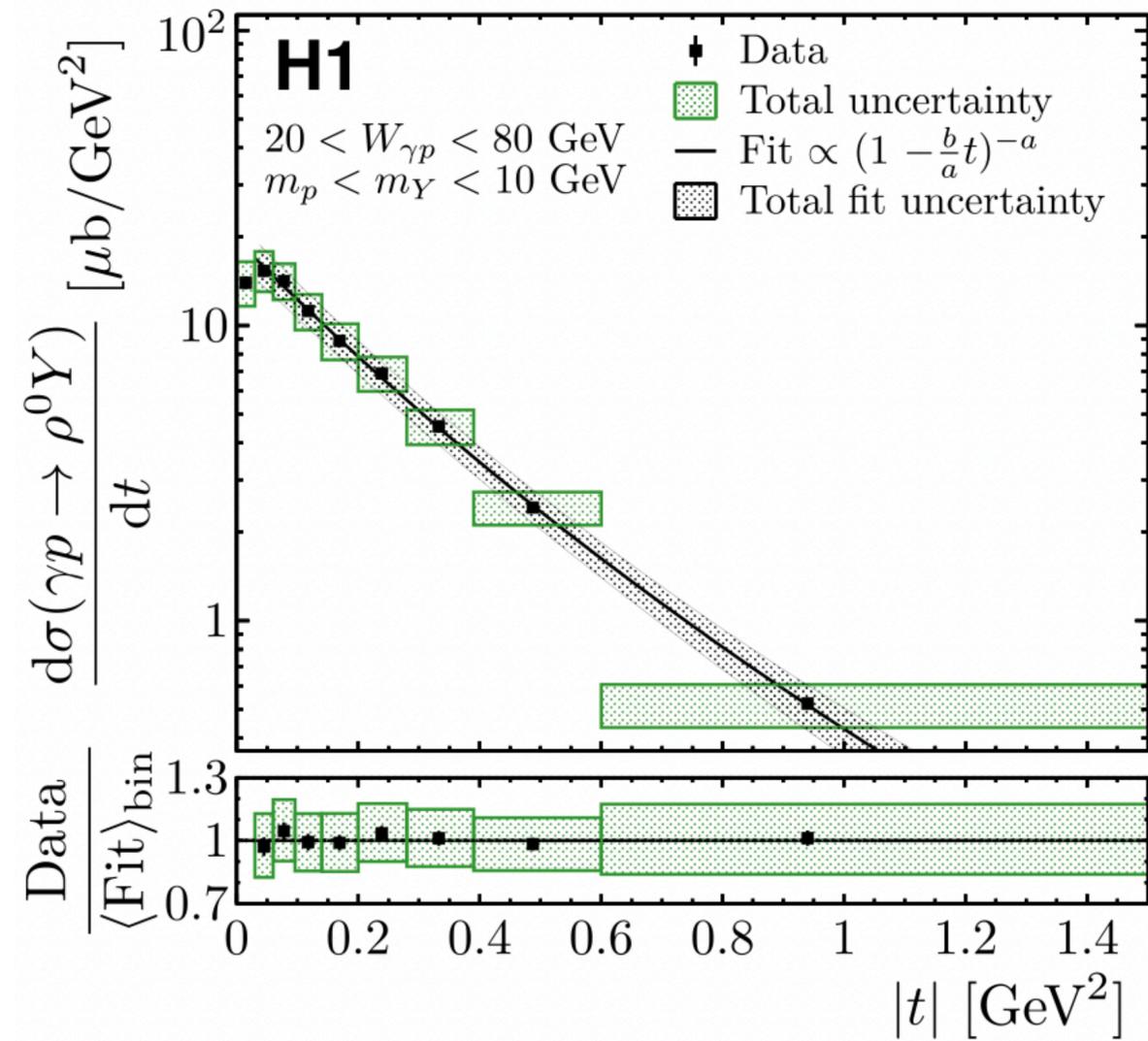


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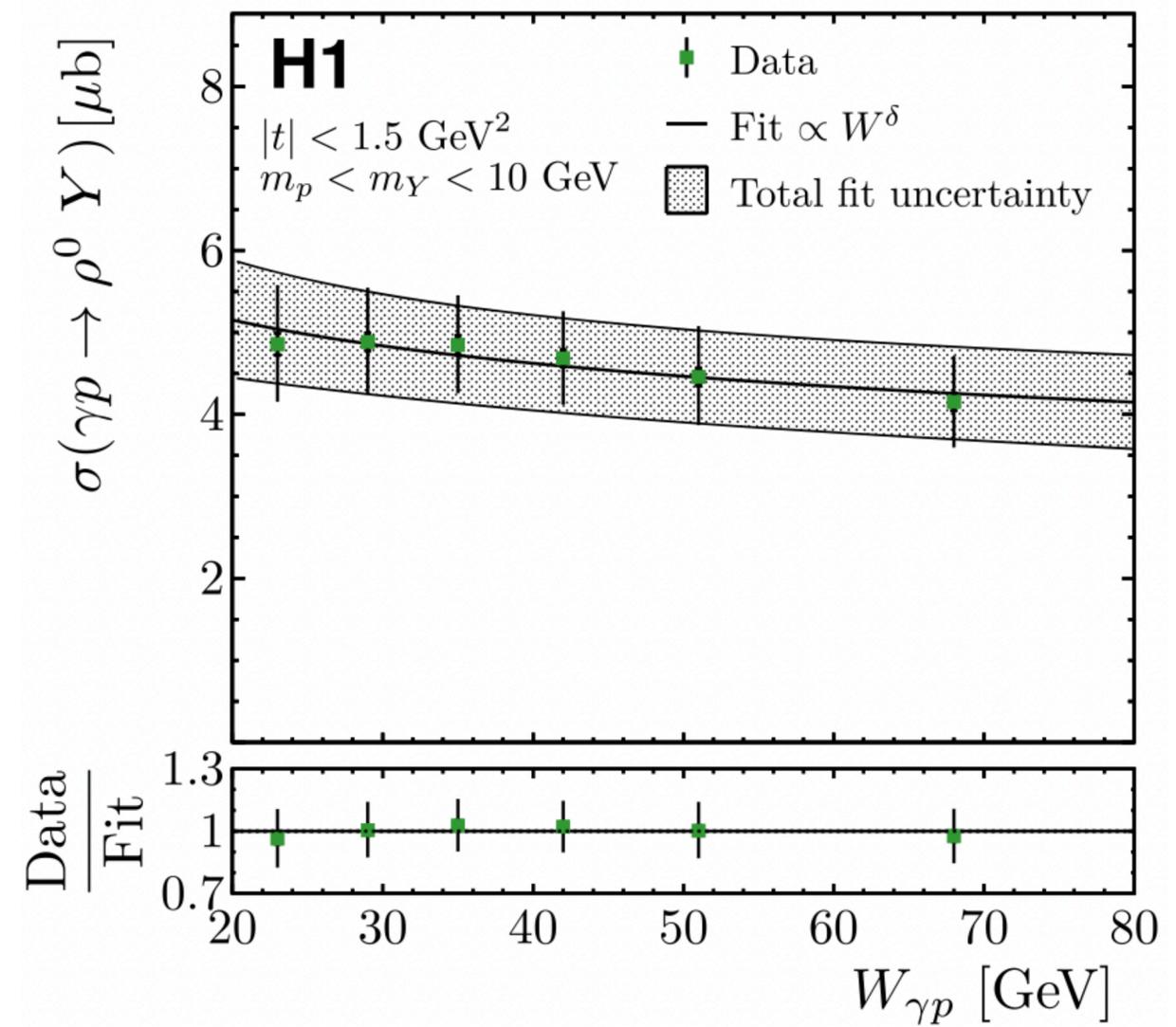
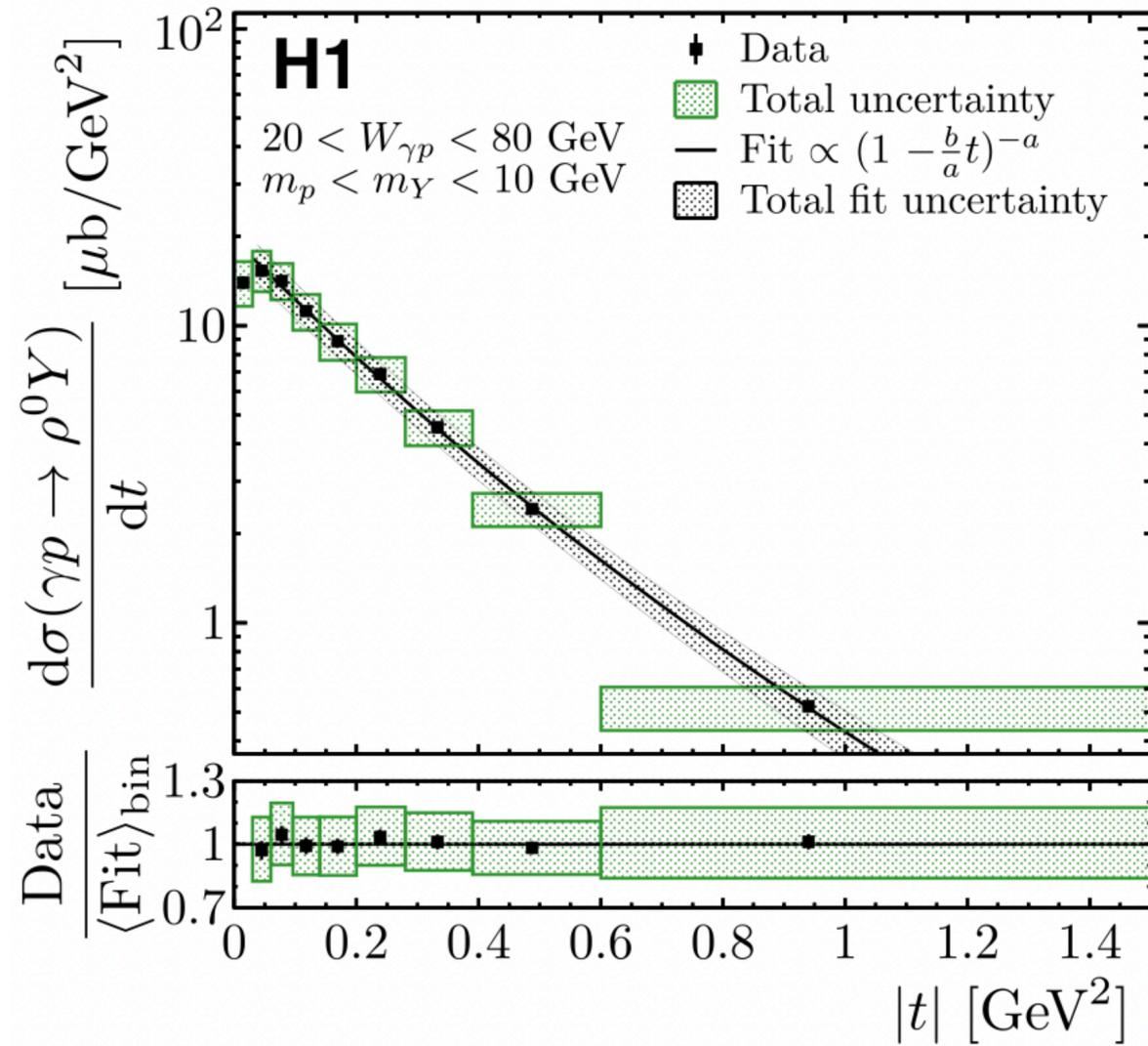
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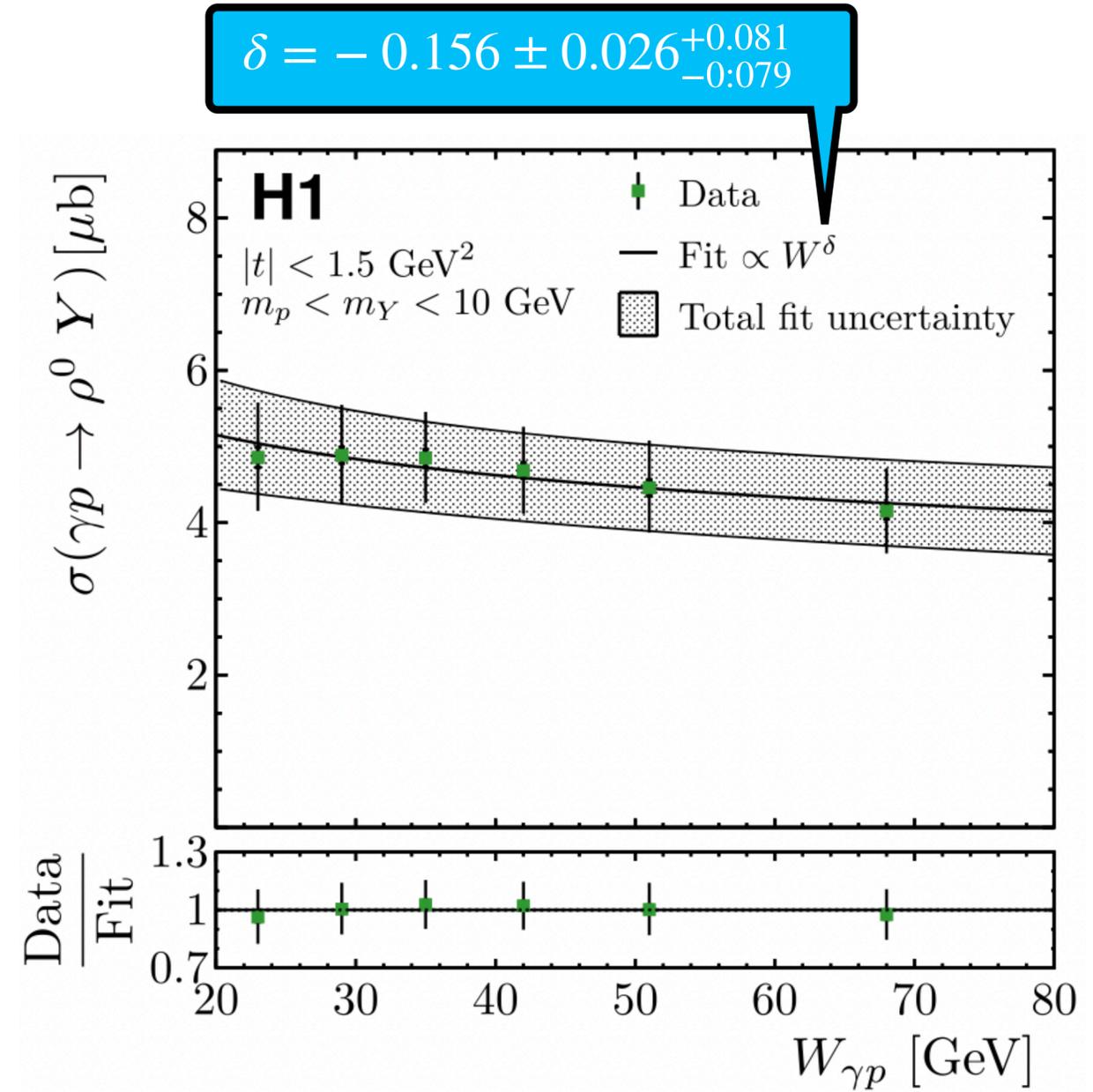
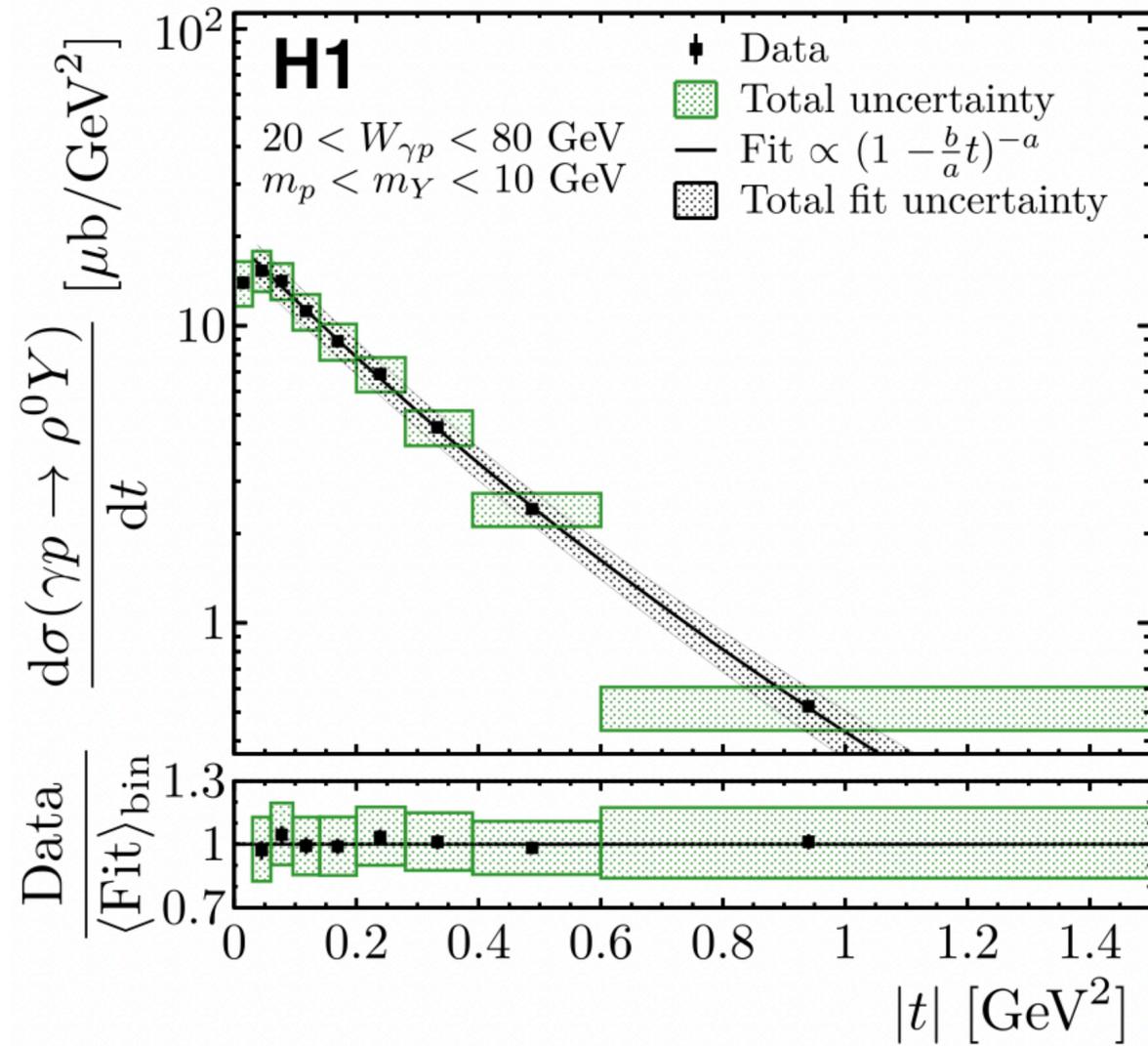
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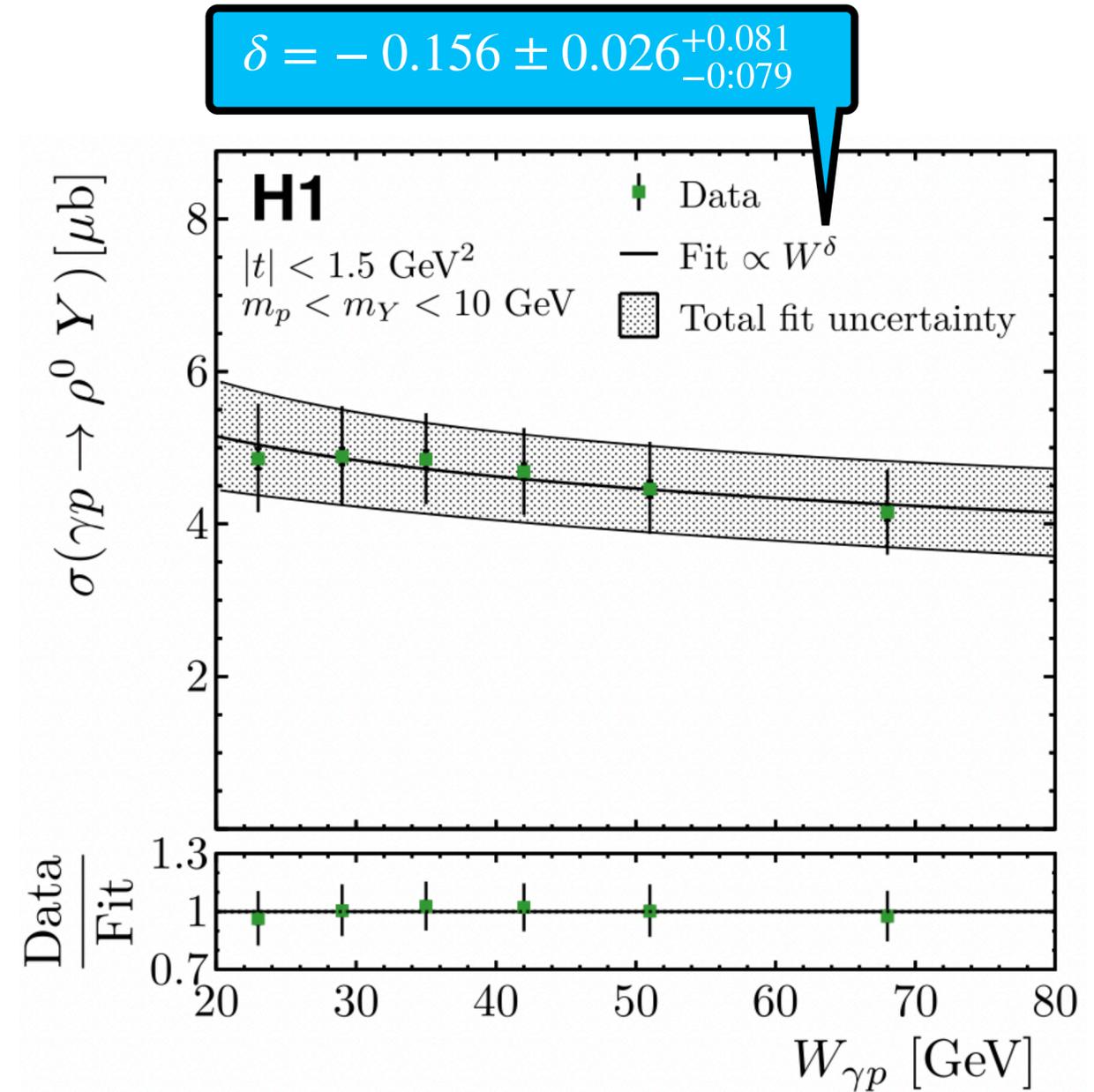
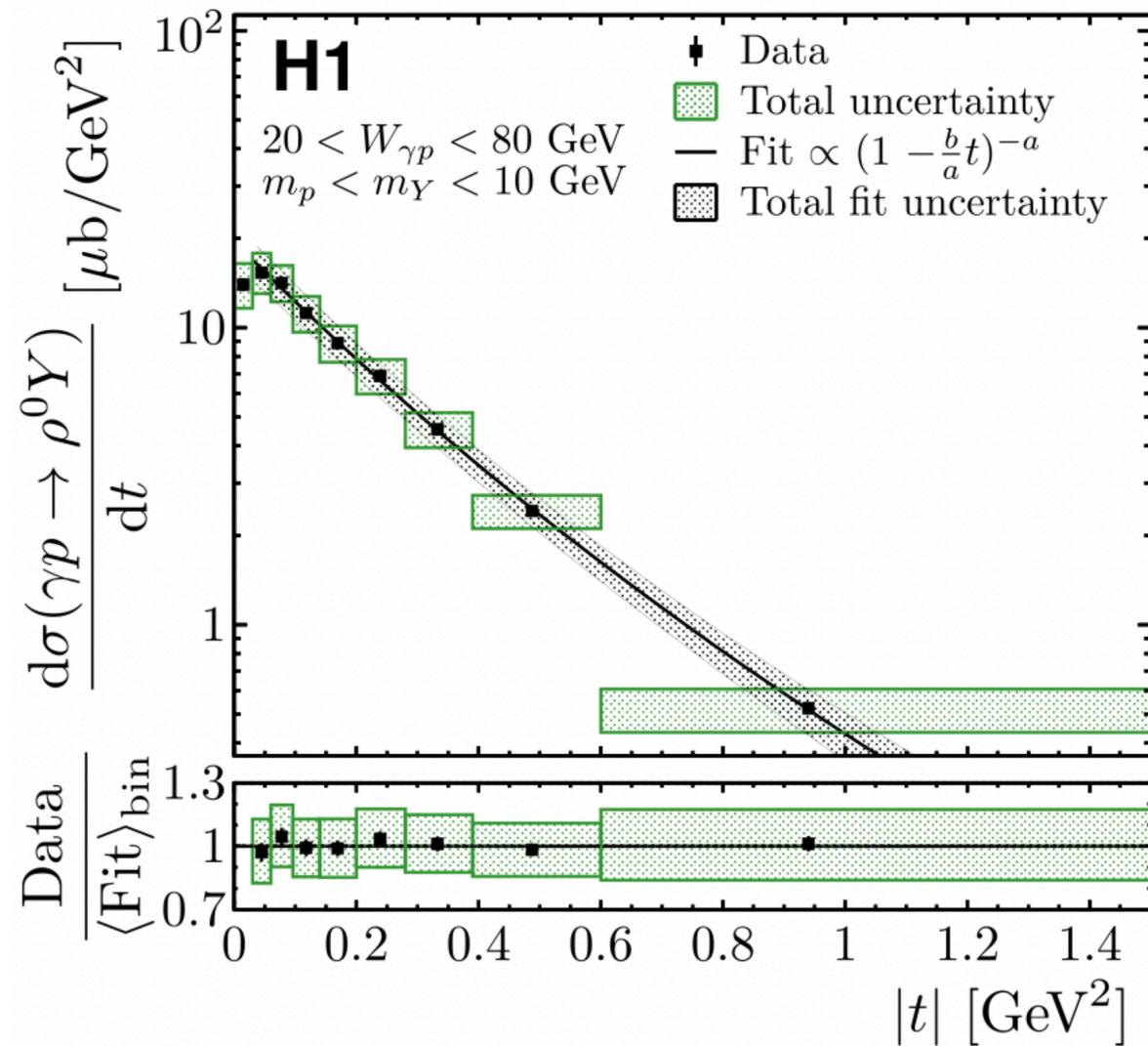
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The cross section decreases!  
 How can this be interpreted?

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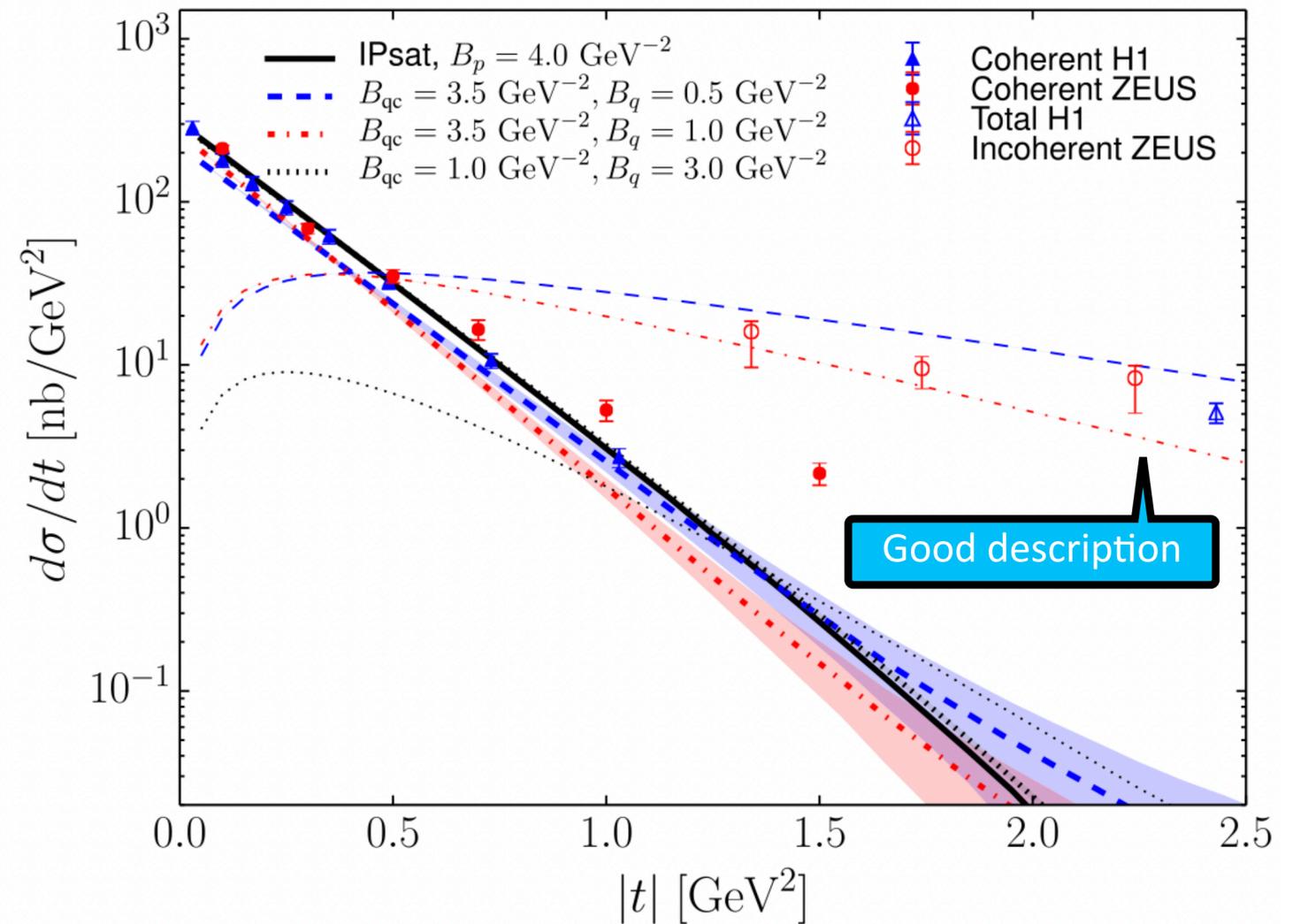
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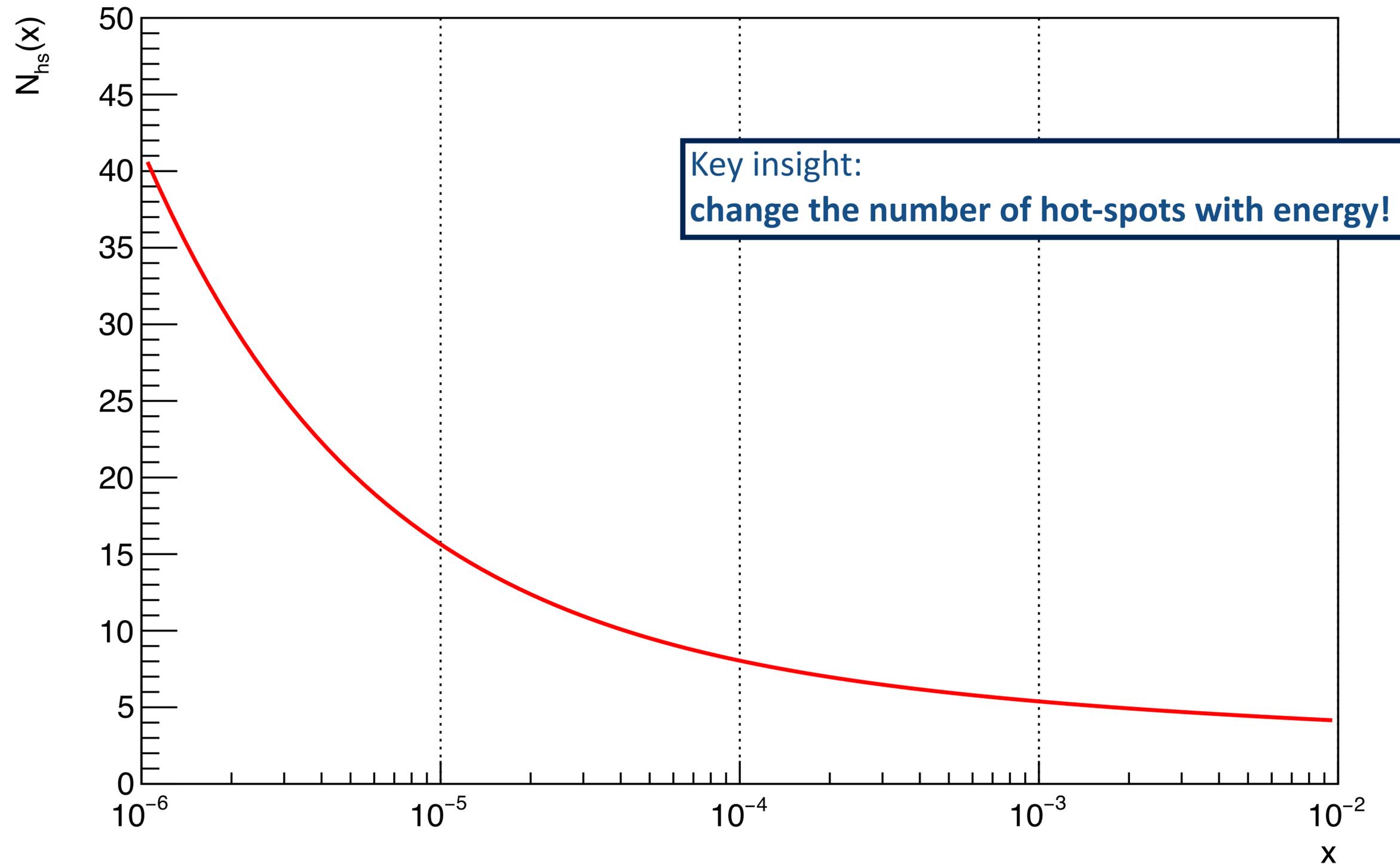
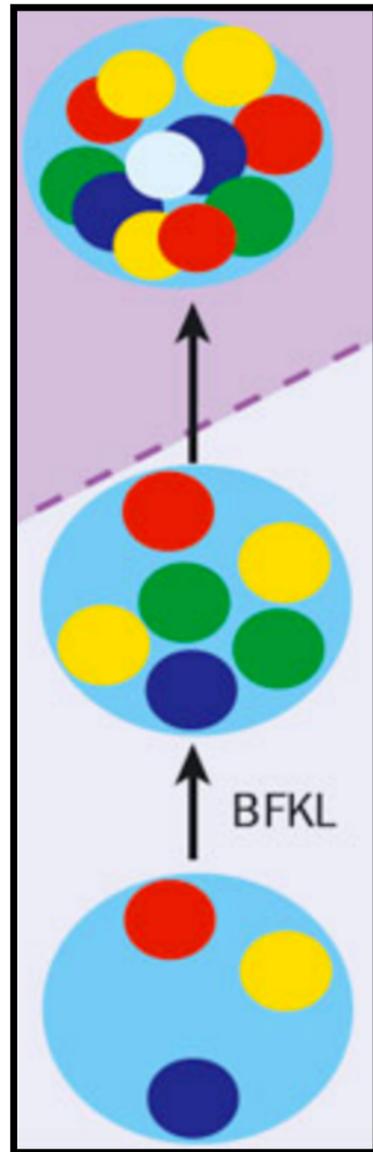
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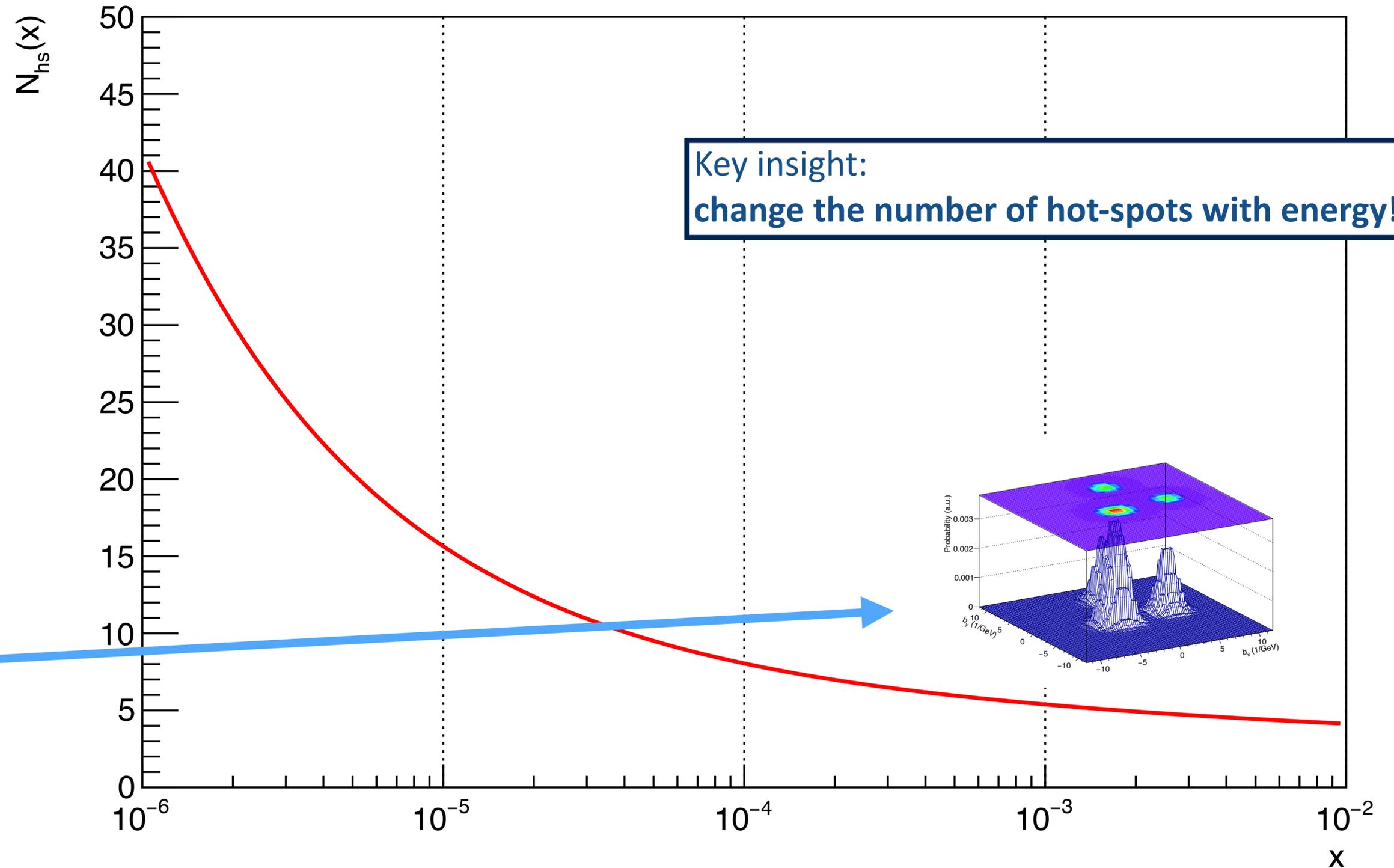
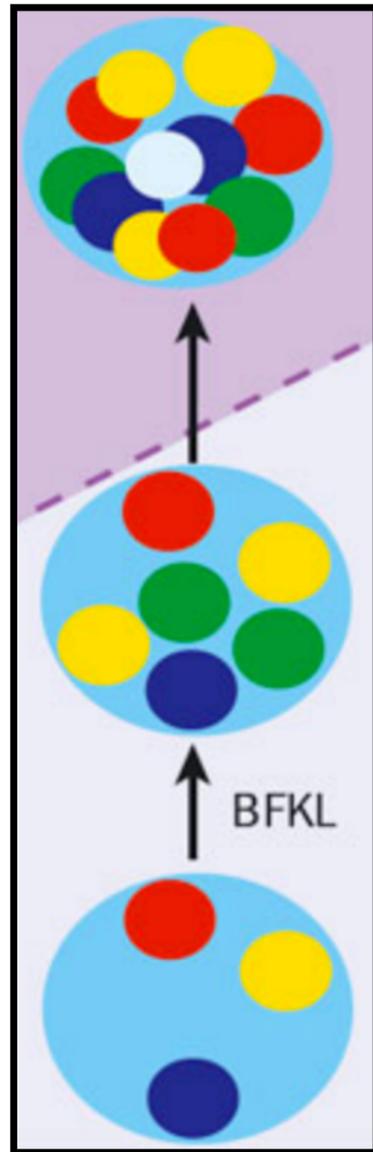
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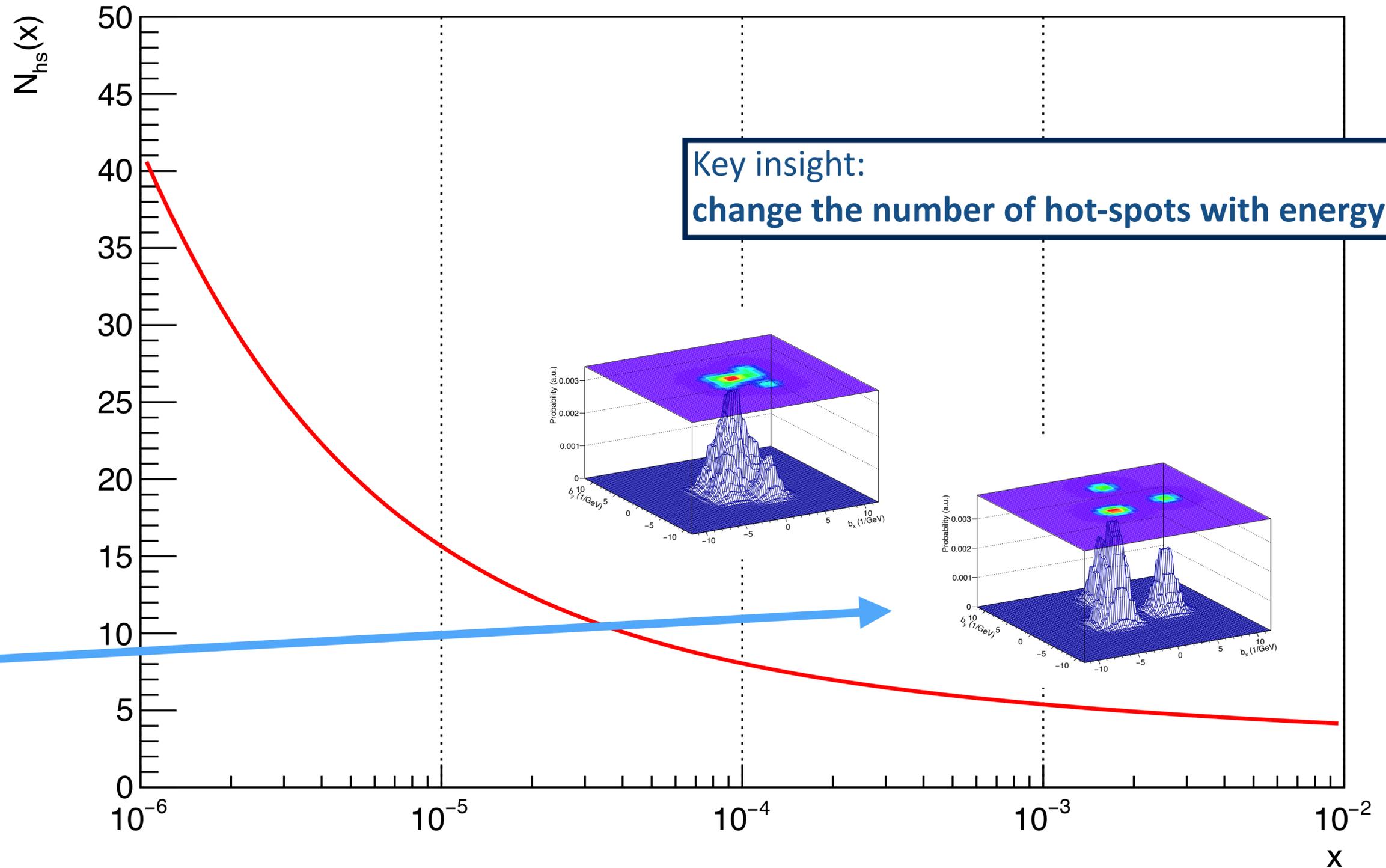
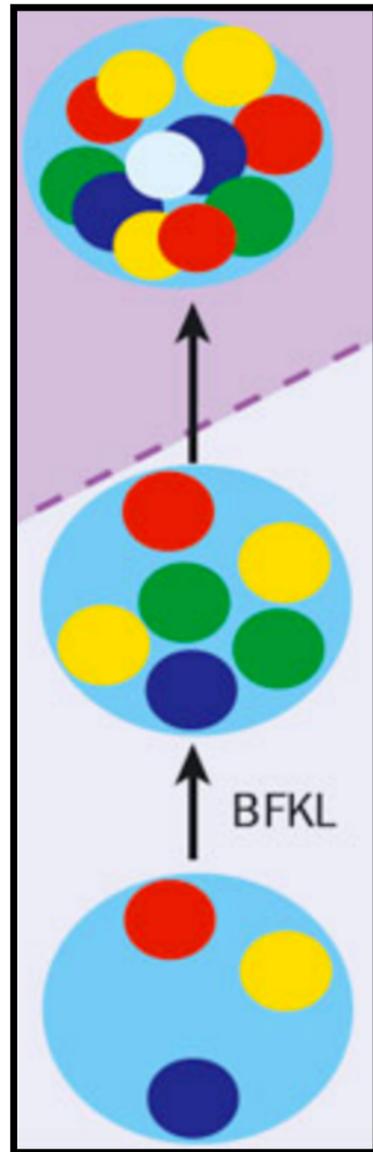
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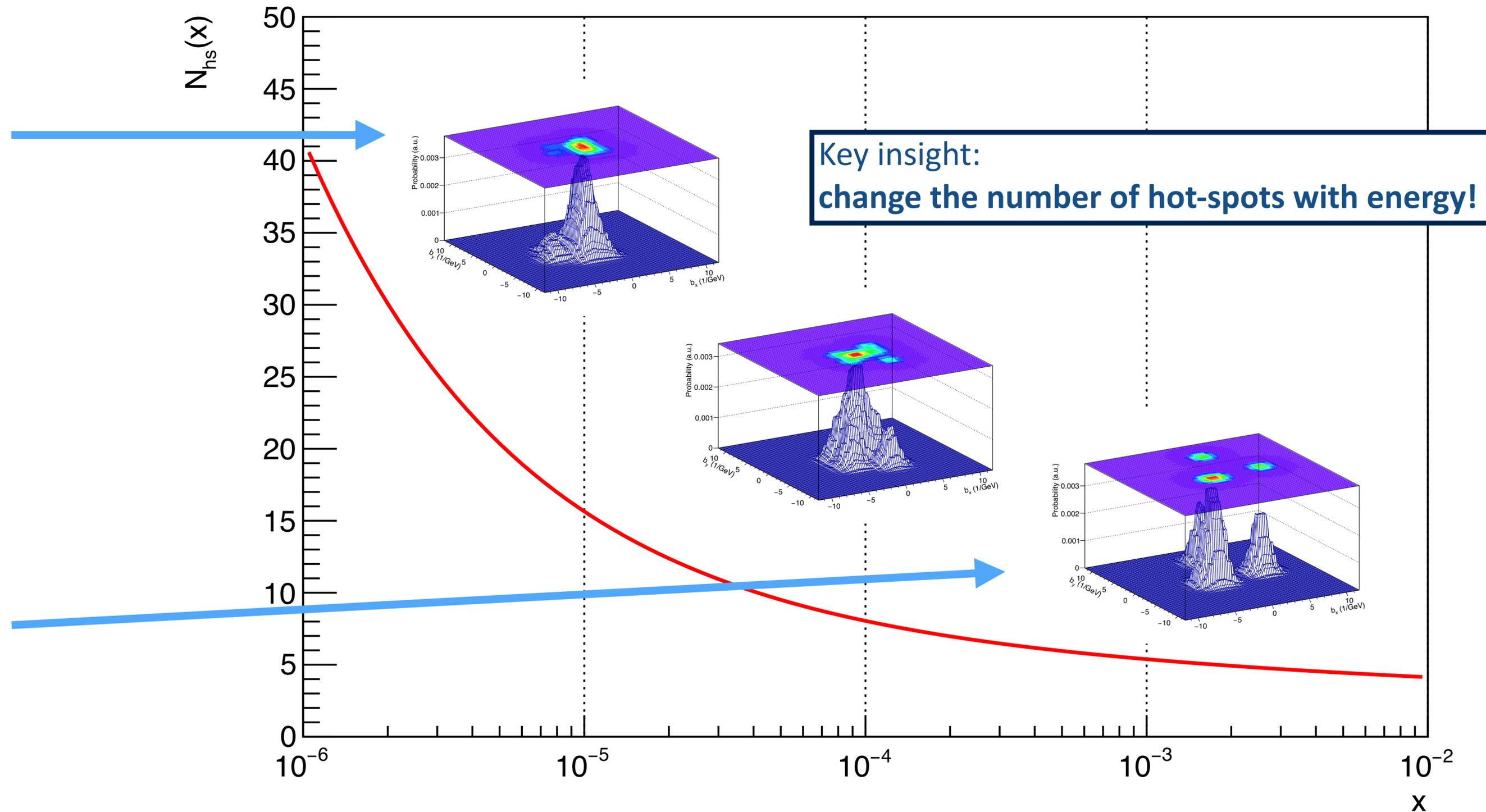
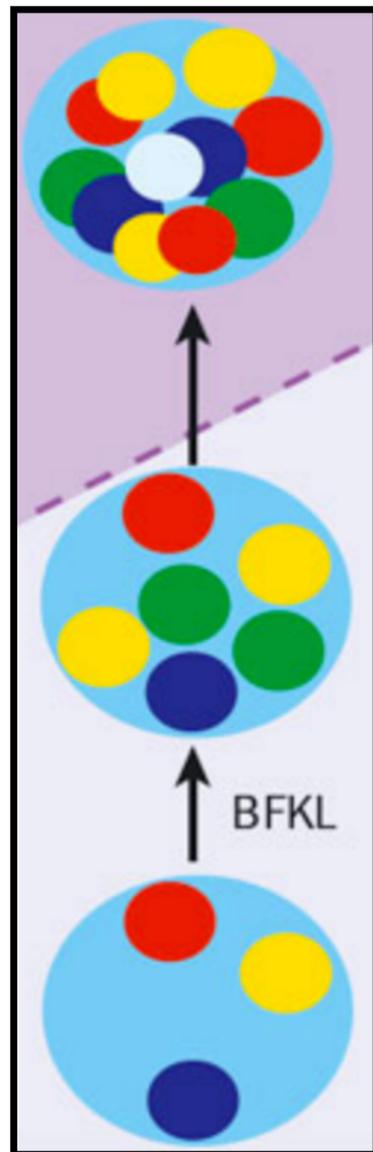
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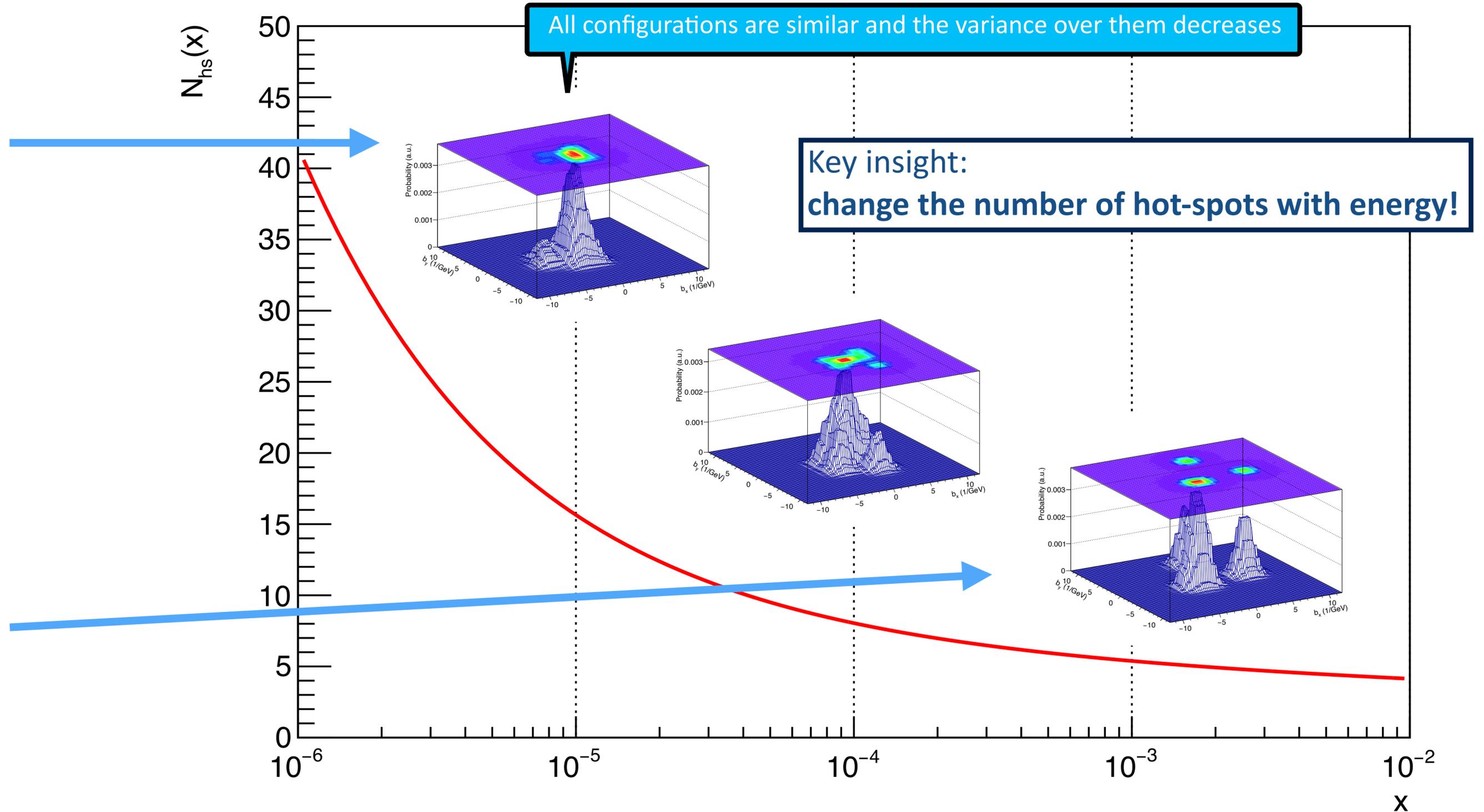
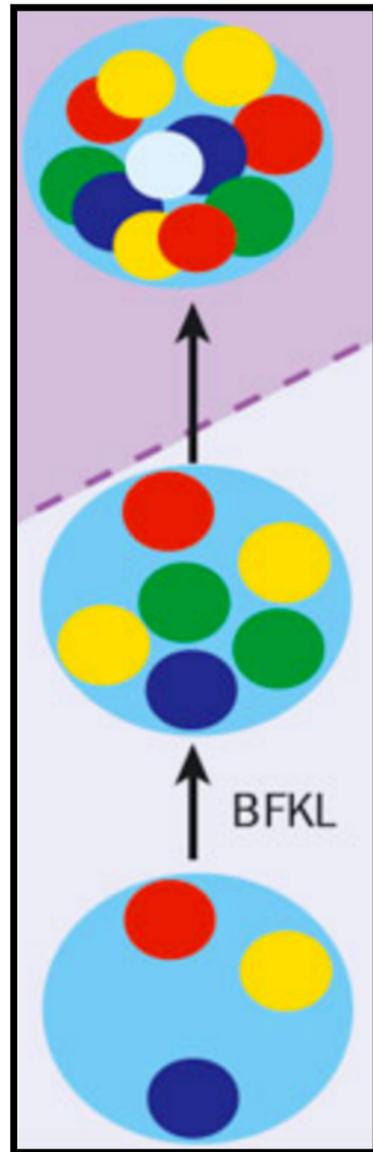
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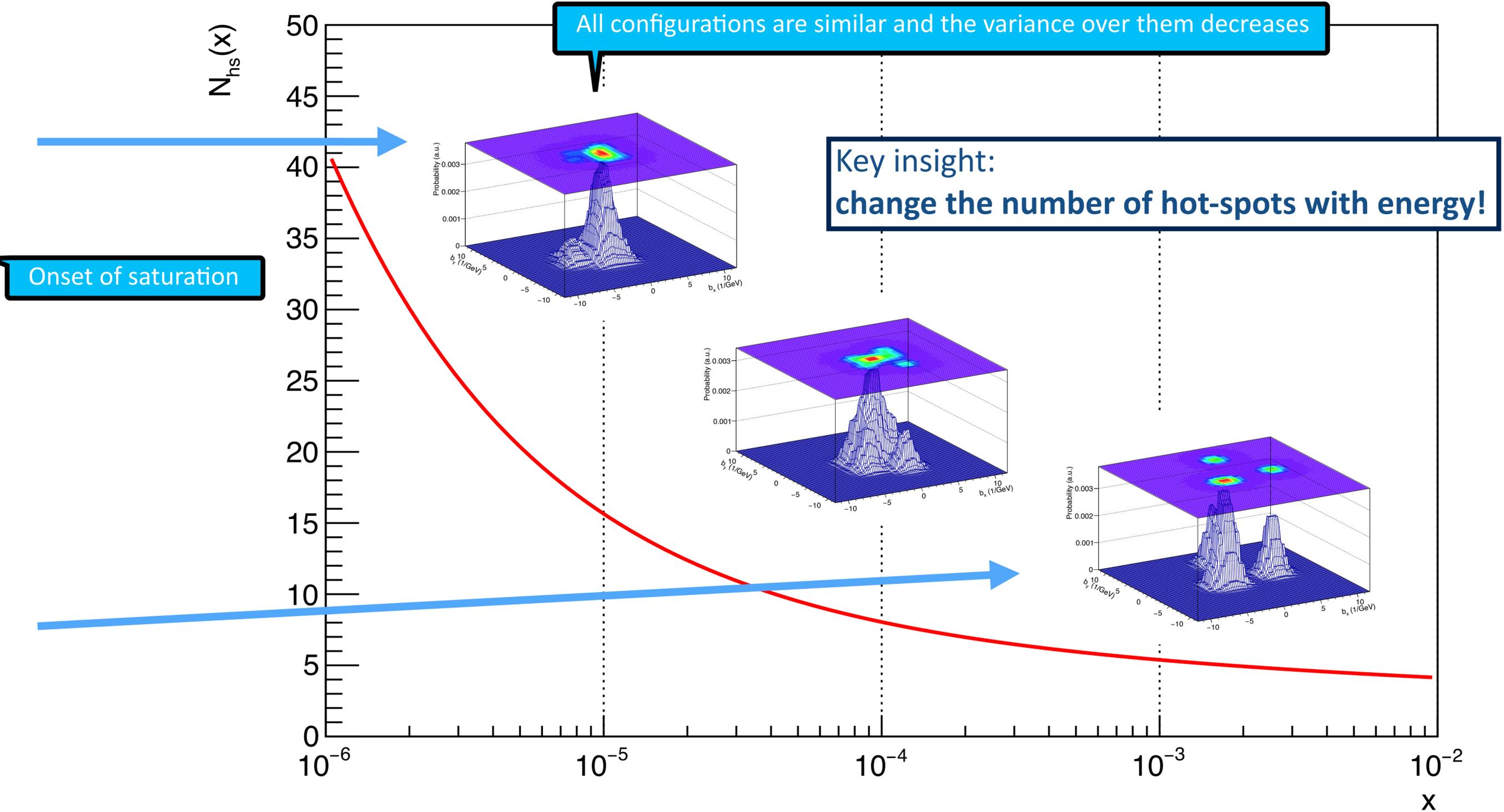
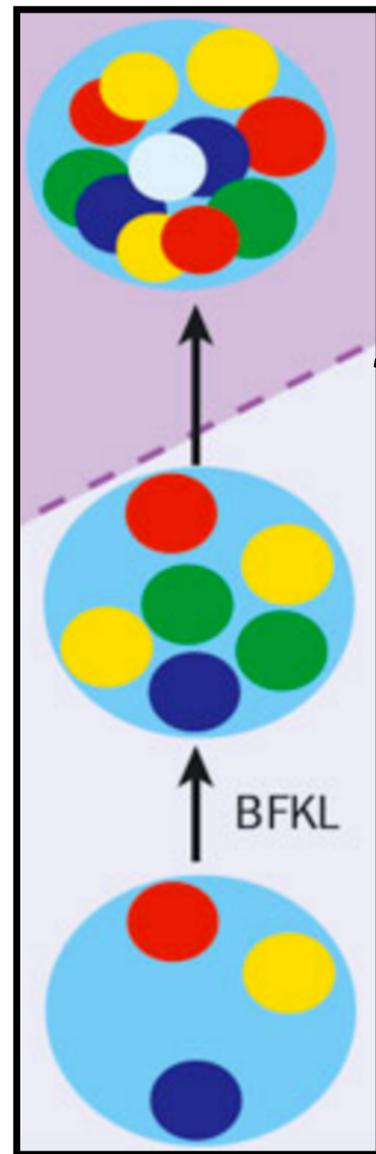
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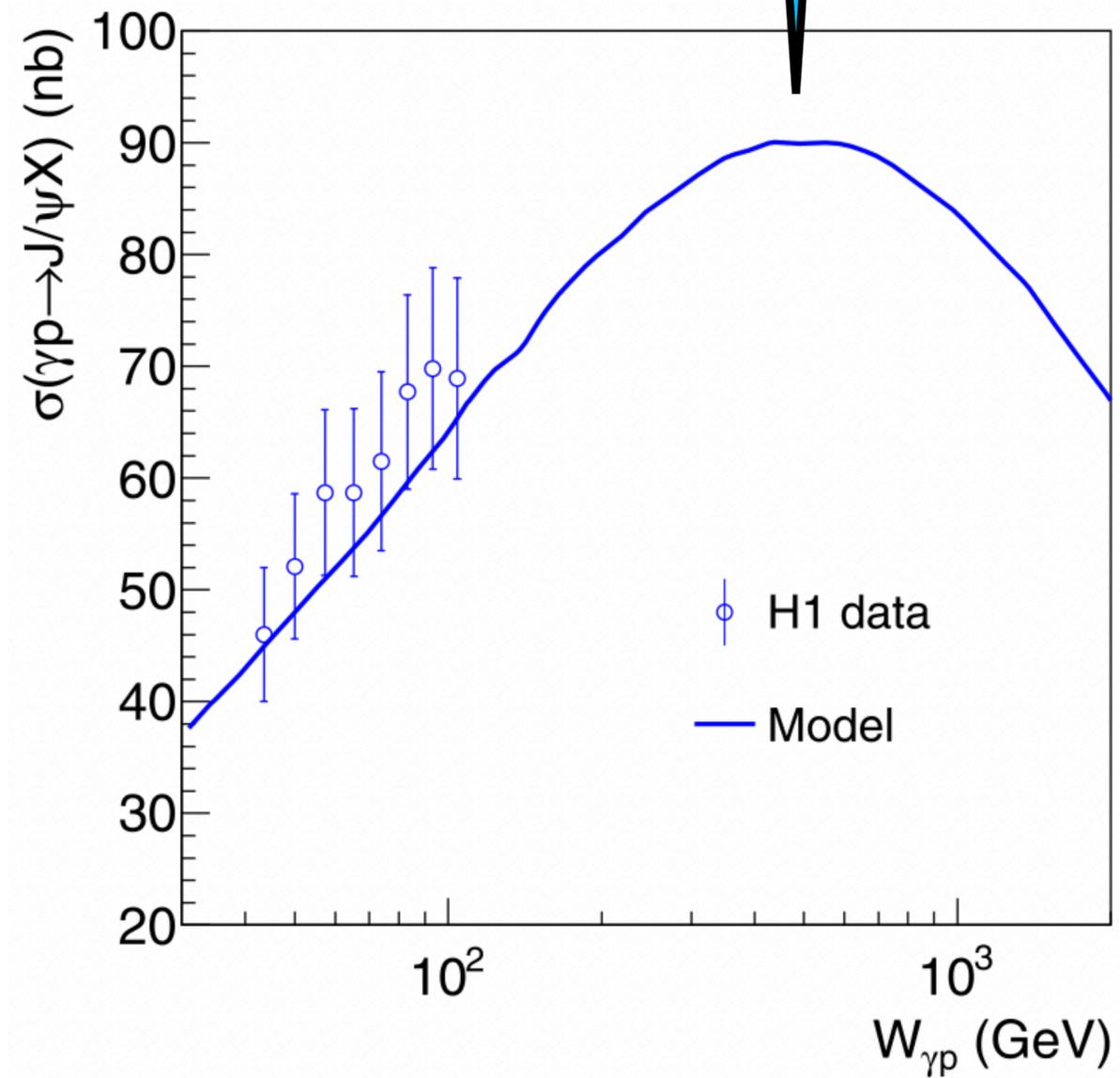


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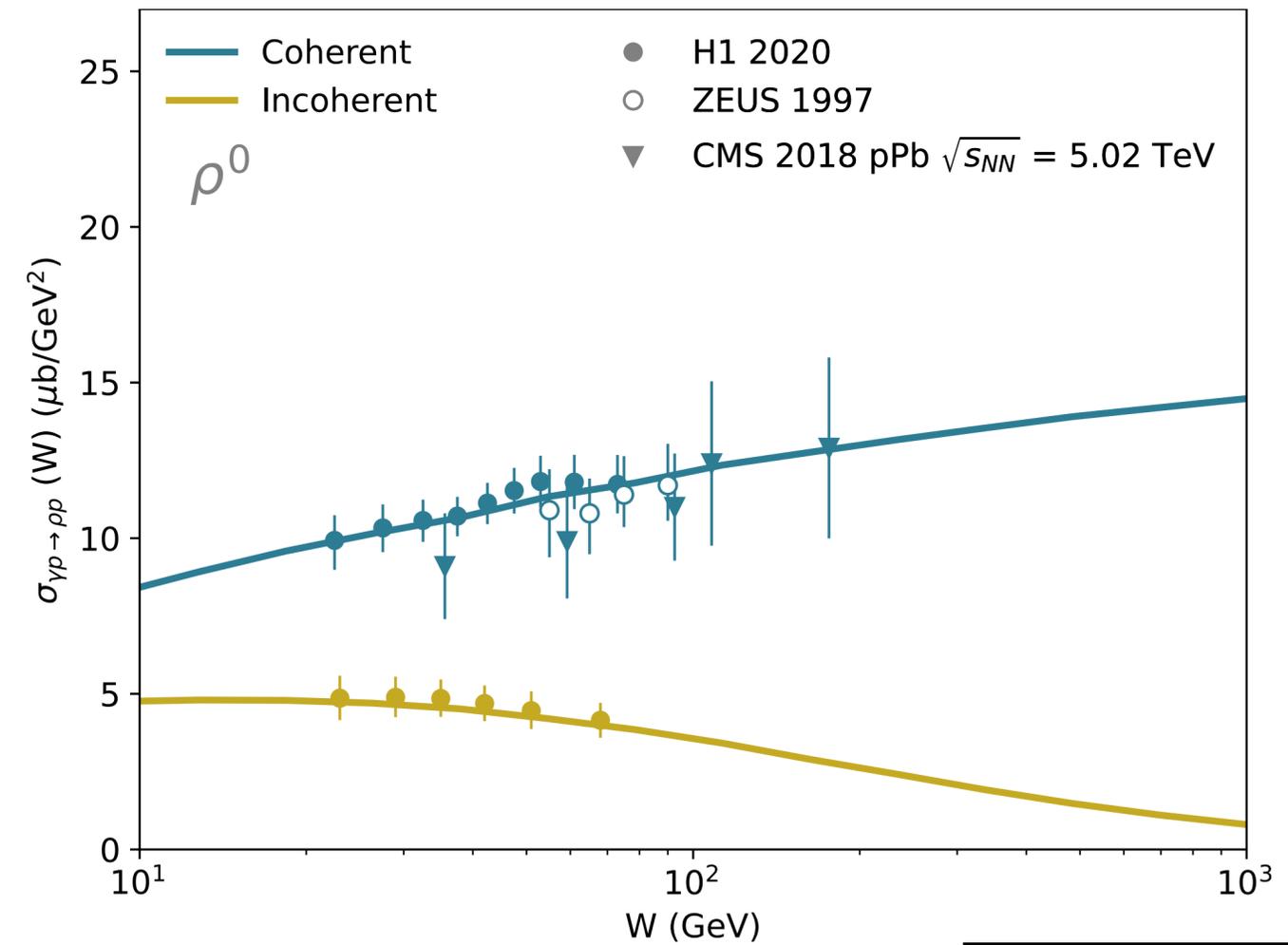
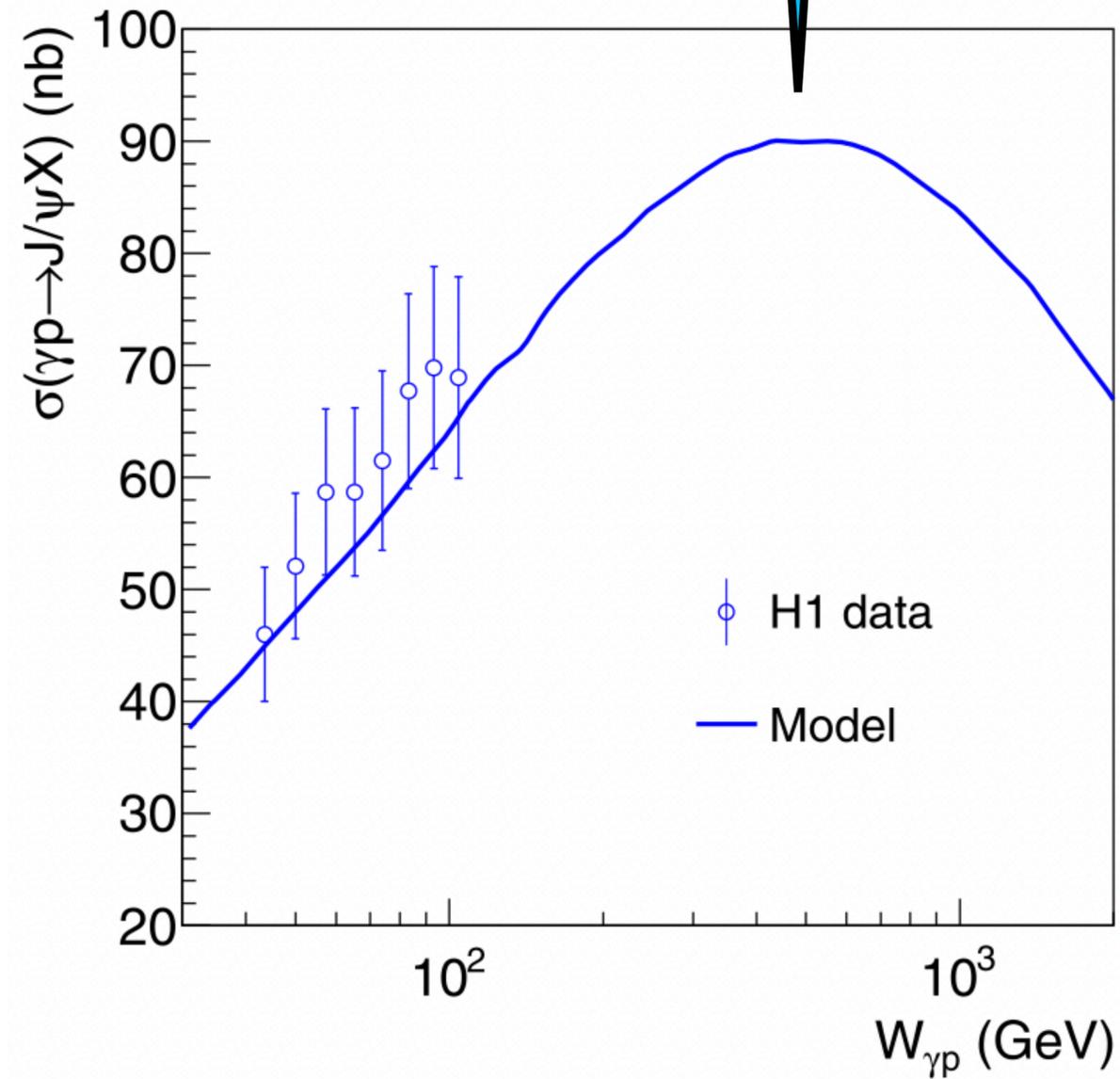
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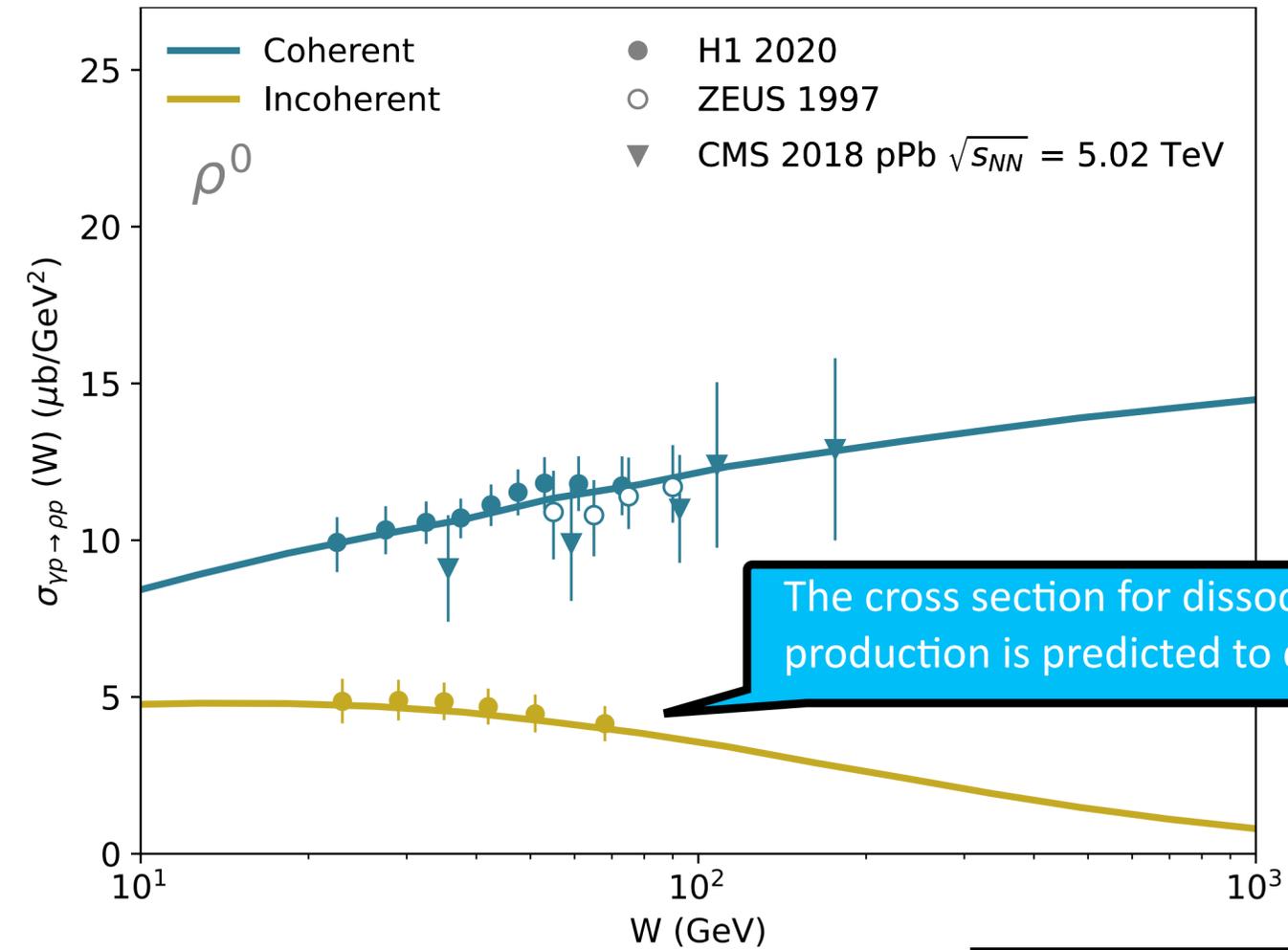
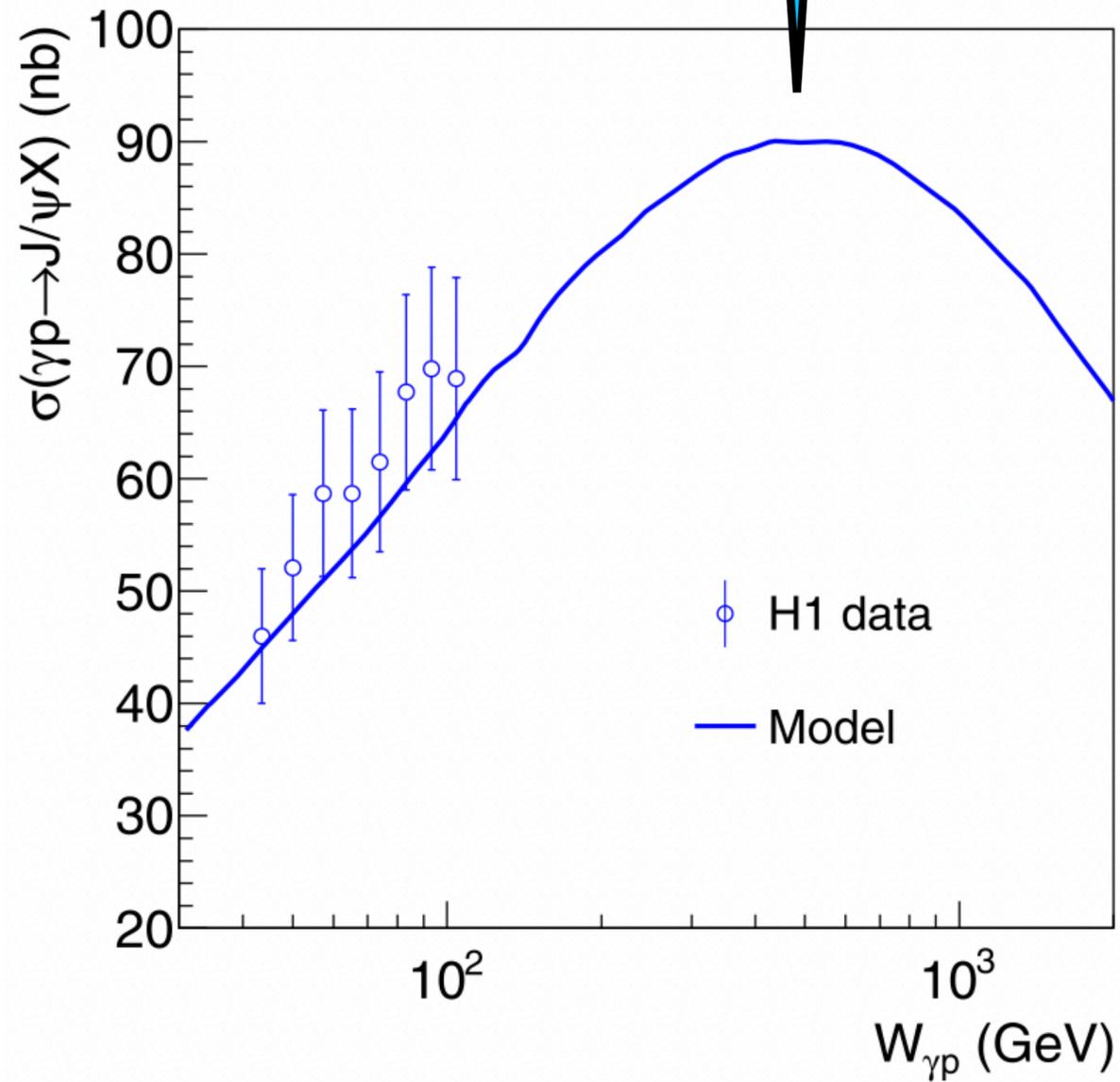
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Cepila et al, arXiv 2312.#####

# Energy-dependent hot-spot model (2/2)

In this model the onset of saturation is here



The cross section for dissociative  $\rho$  photo-production is predicted to decrease

Cepila et al, arXiv 2312.#####

Dissociative  $\rho$  photoproduction offers some tantalising results ....  
But the  $\rho$  mass-scale is low, so the application of perturbative ideas to interpret data is in question  
The  $J/\psi$  dissociative cross section is still growing at HERA energies,  
Where and how can we study this type of processes at even higher energies?

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Enter RHIC and the LHC where we can  
study photon-induced processes off nuclei

5

## Understanding the photon flux in collisions of heavy ions

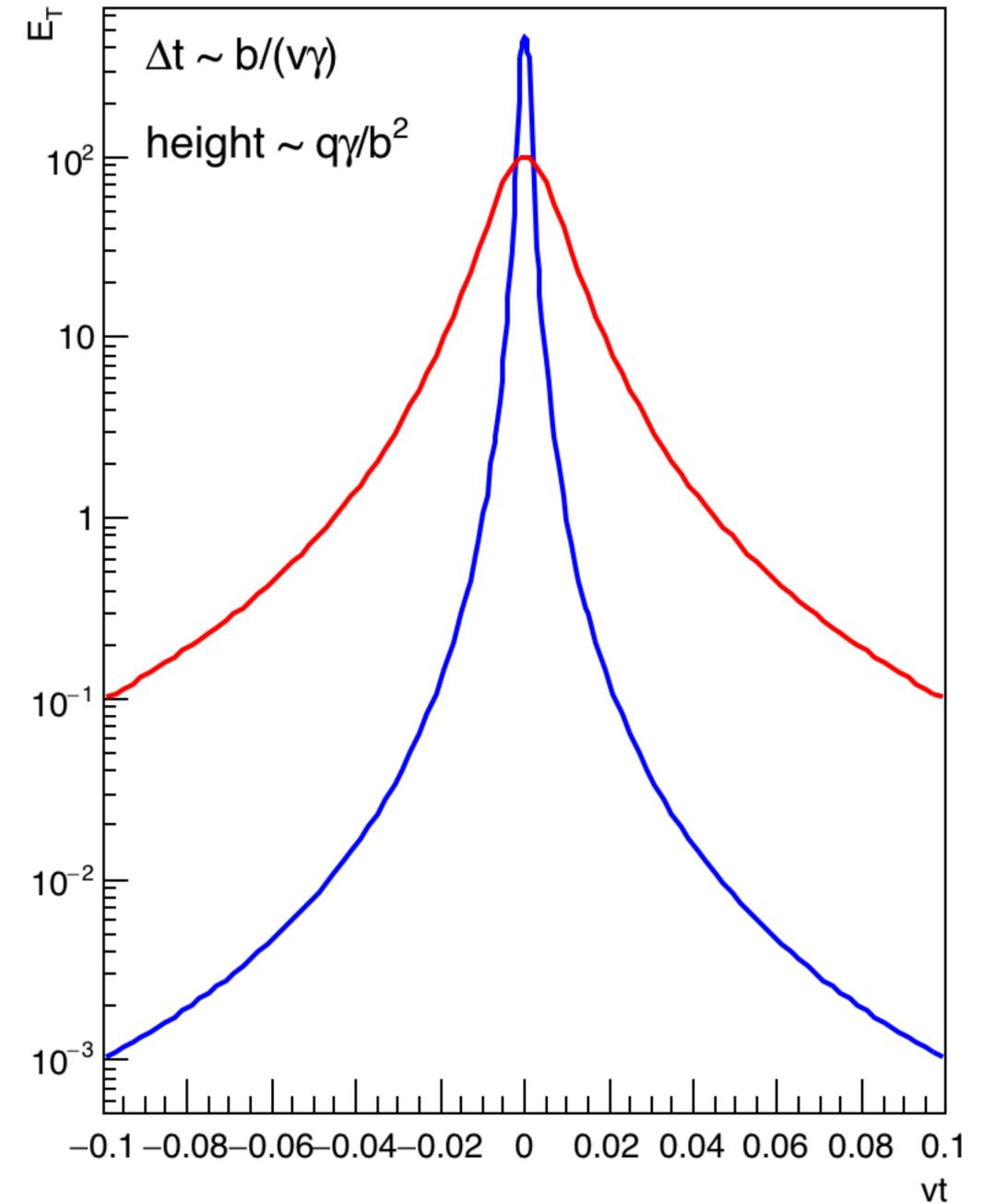
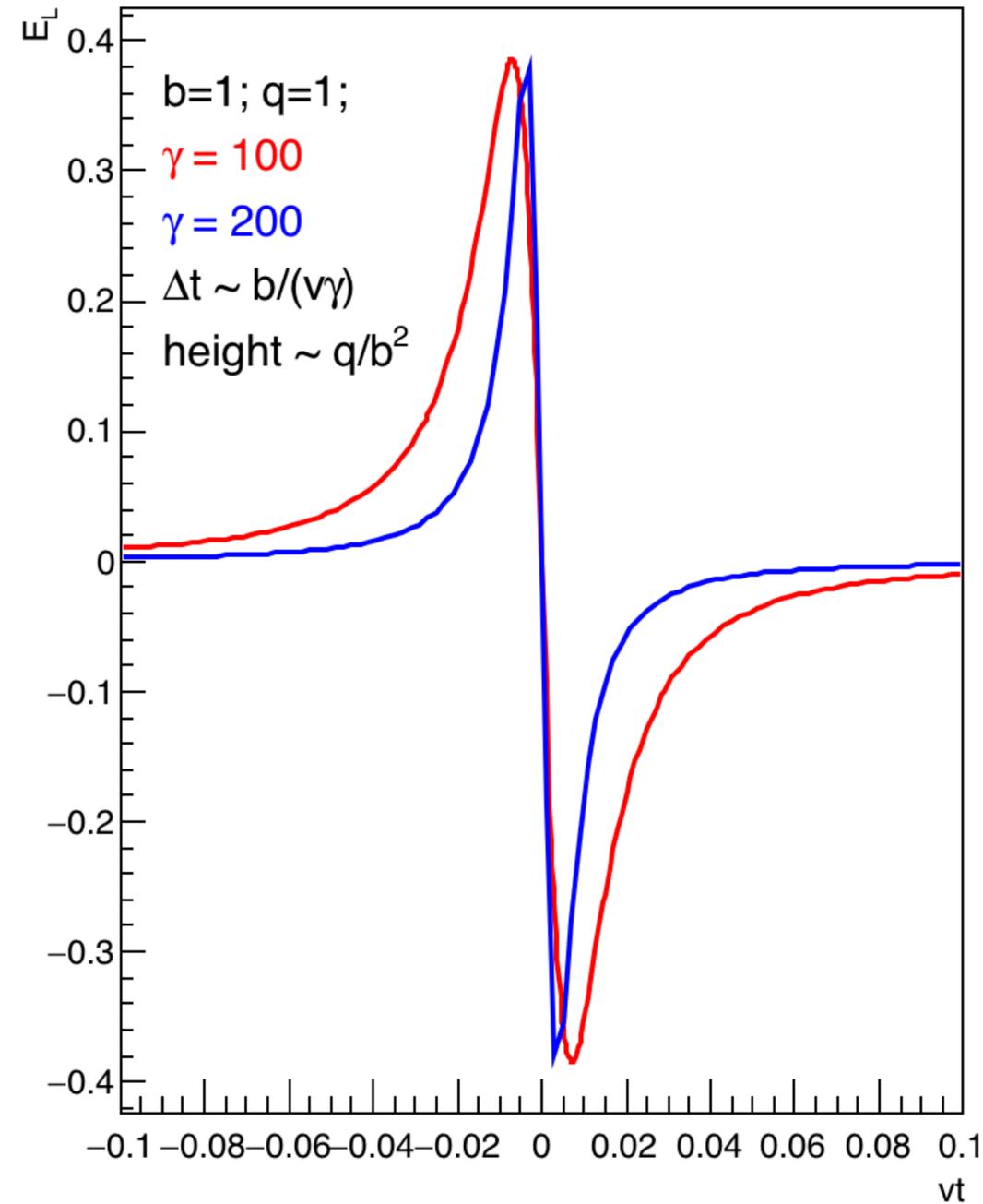
proportional to  $Z^2$

Heavy ions have intense electromagnetic fields that can be used to study photon-induced interactions

# The photon flux: field of a point charge

# The photon flux: field of a point charge

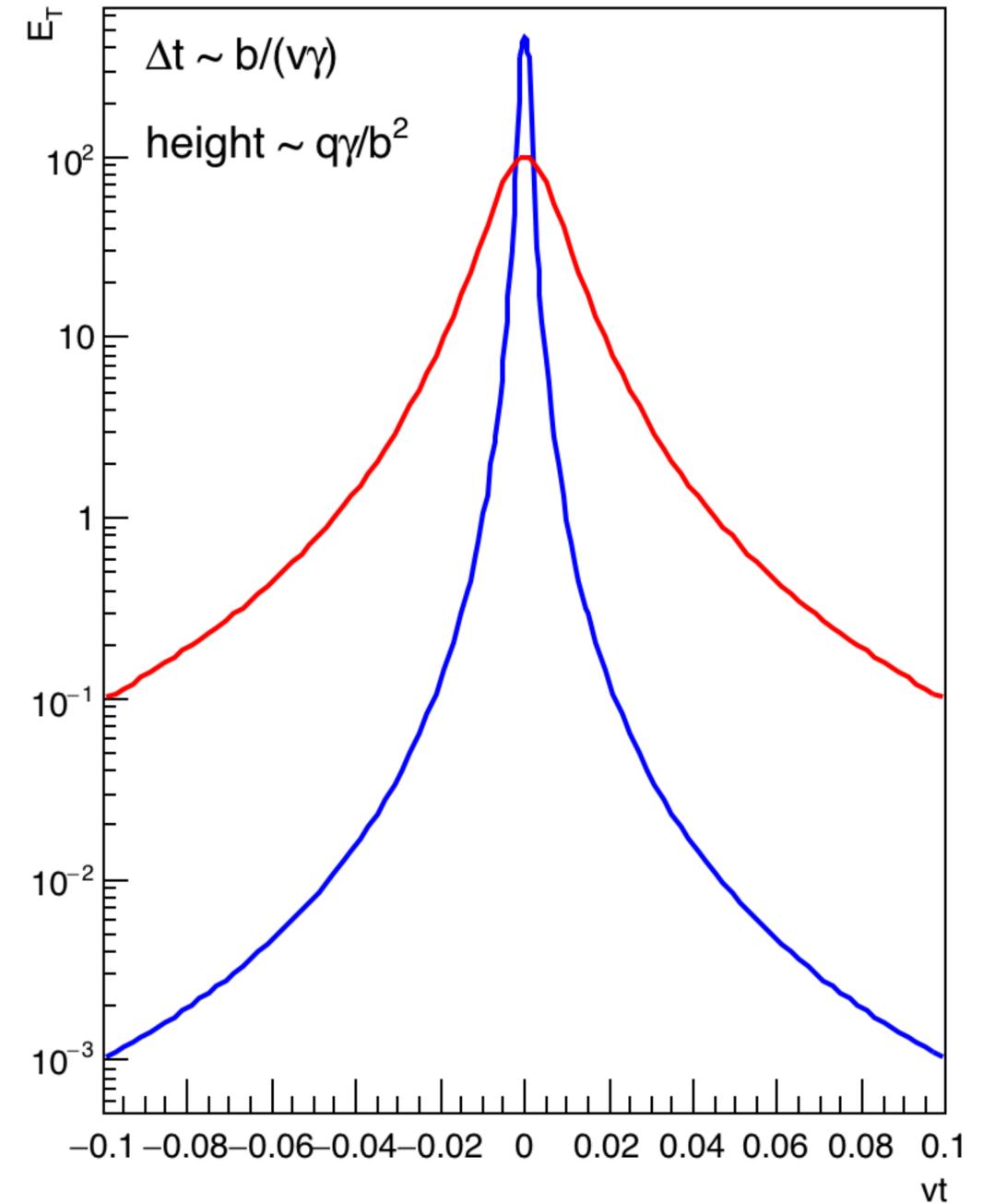
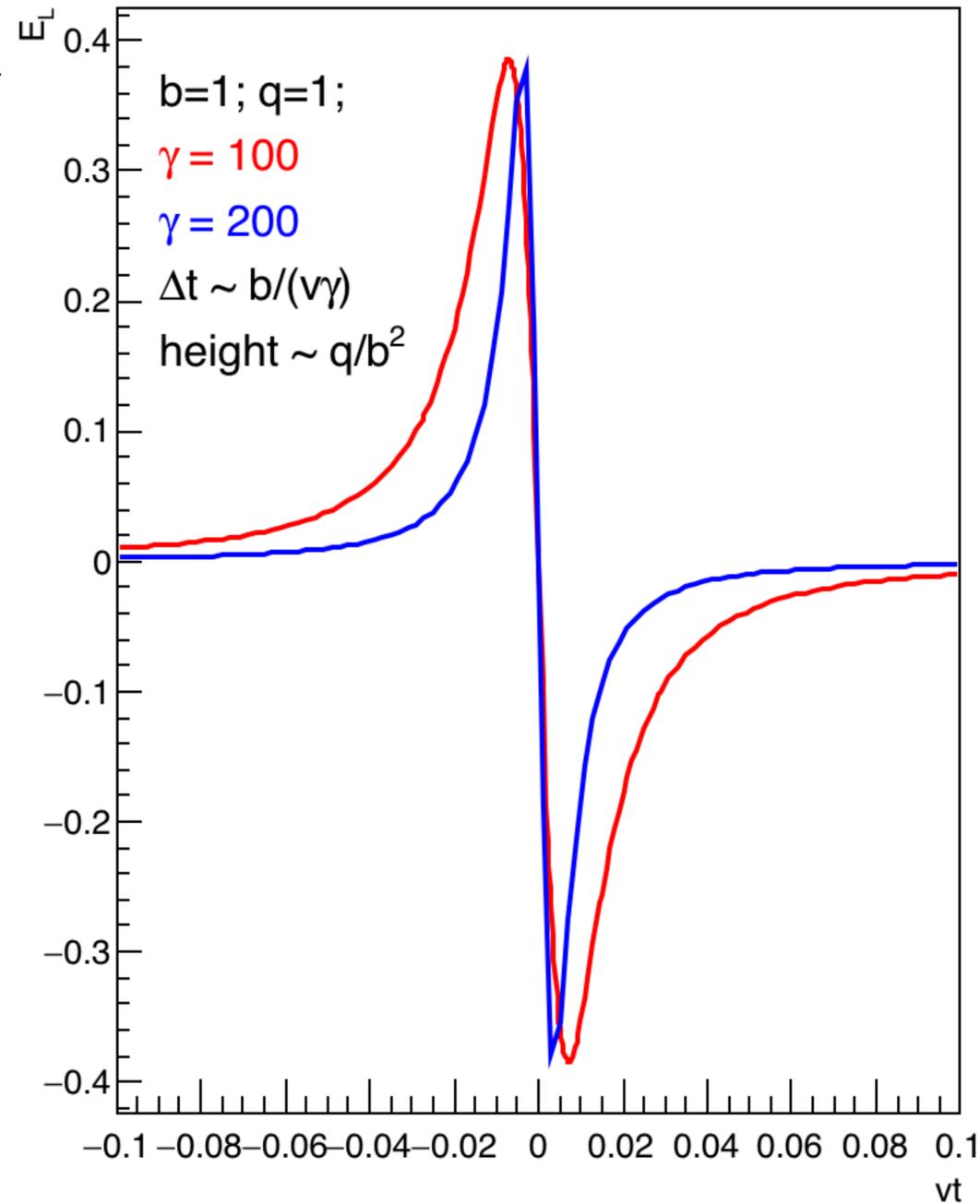
Take the electric field of the particle at rest and boost it to the collider frame



# The photon flux: field of a point charge

Take the electric field of the particle at rest and boost it to the collider frame

Longitudinal component

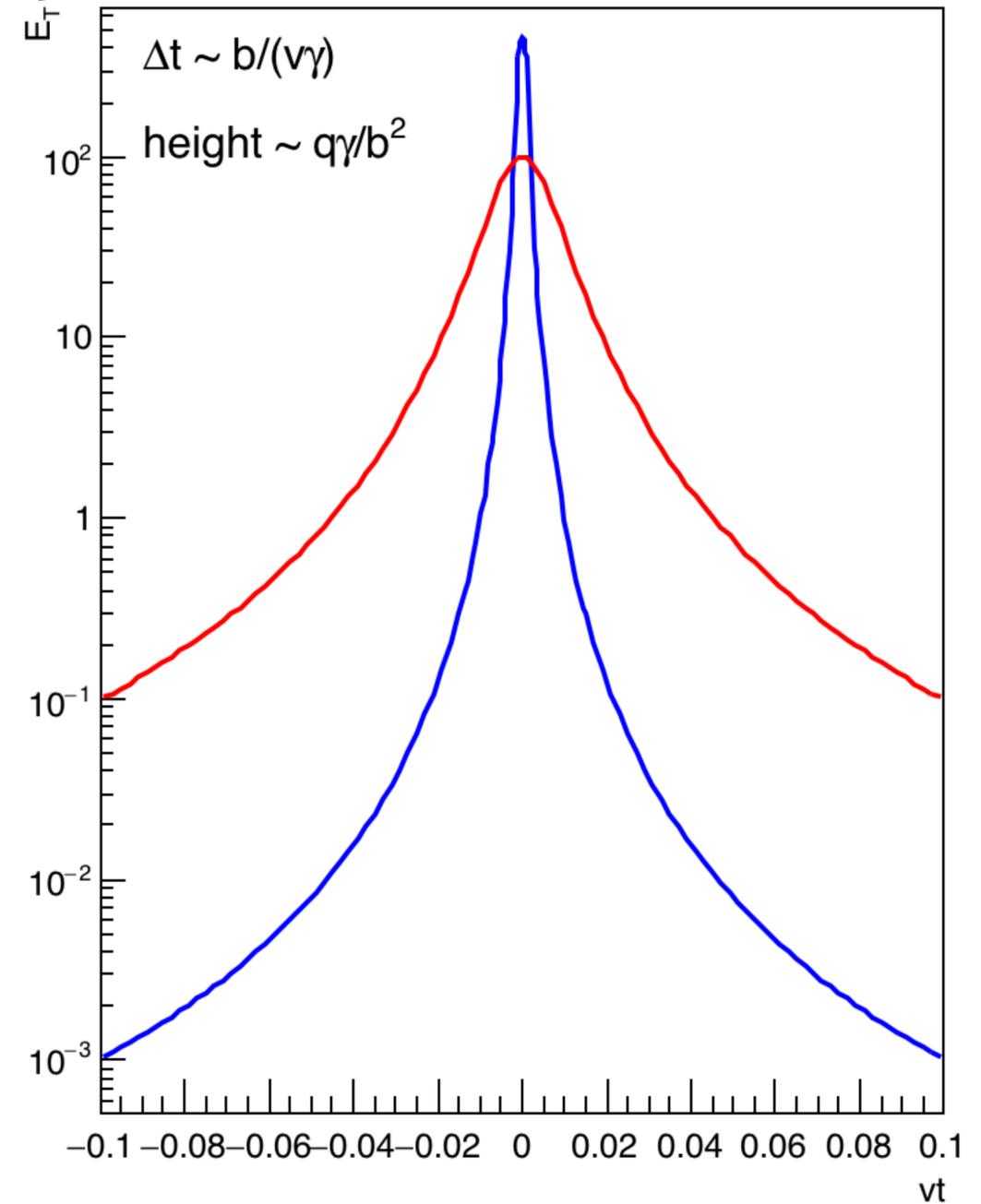
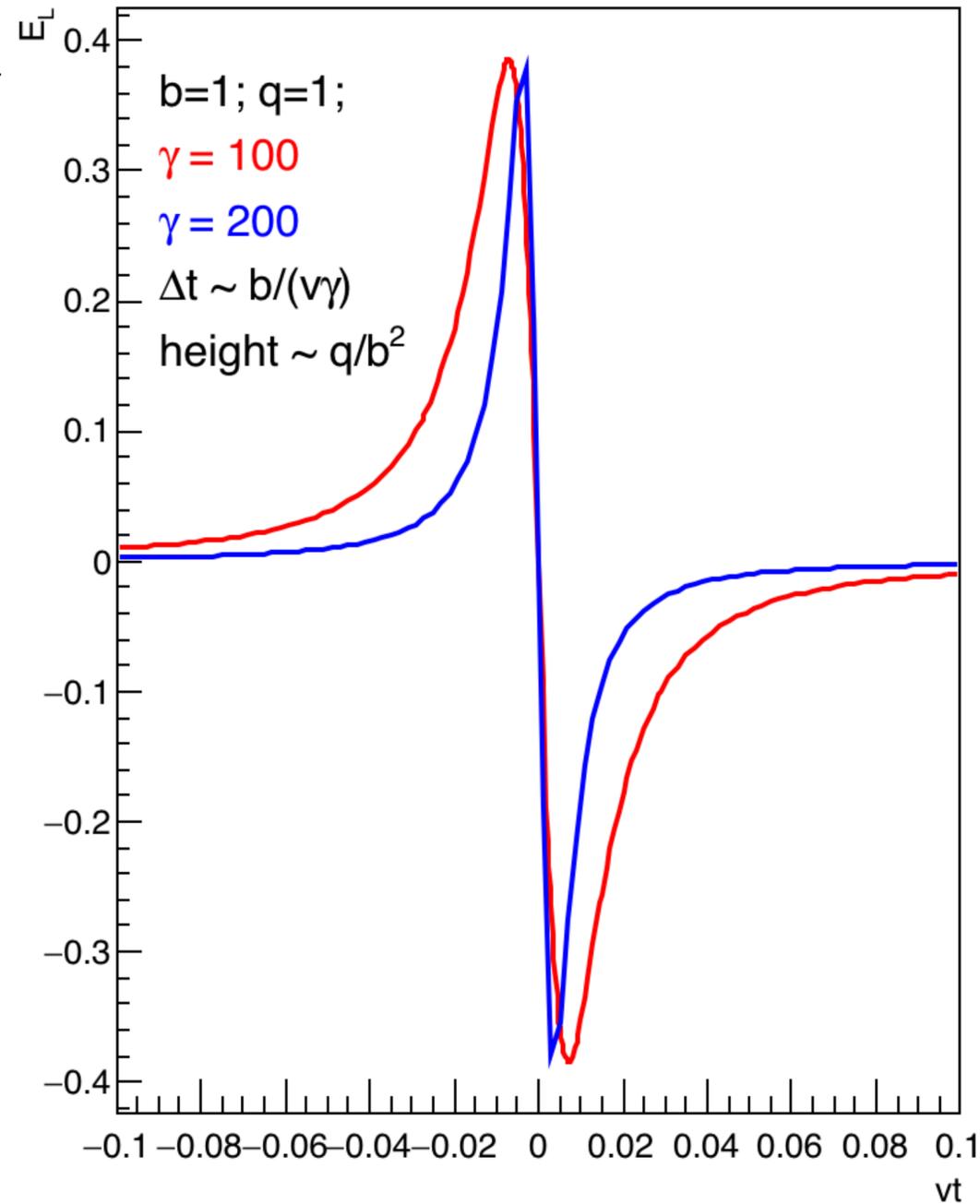


# The photon flux: field of a point charge

Take the electric field of the particle at rest and boost it to the collider frame

Transverse component

Longitudinal component

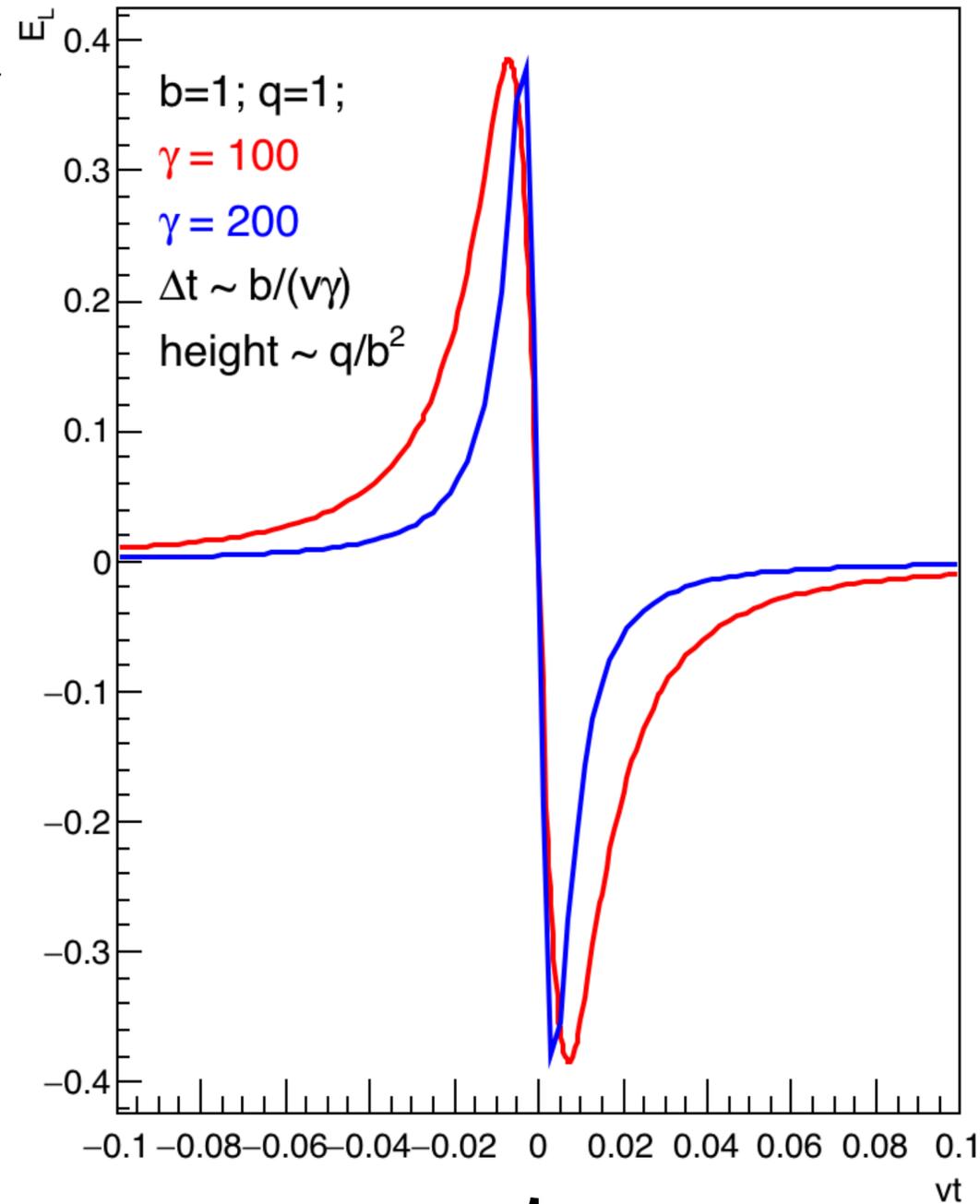


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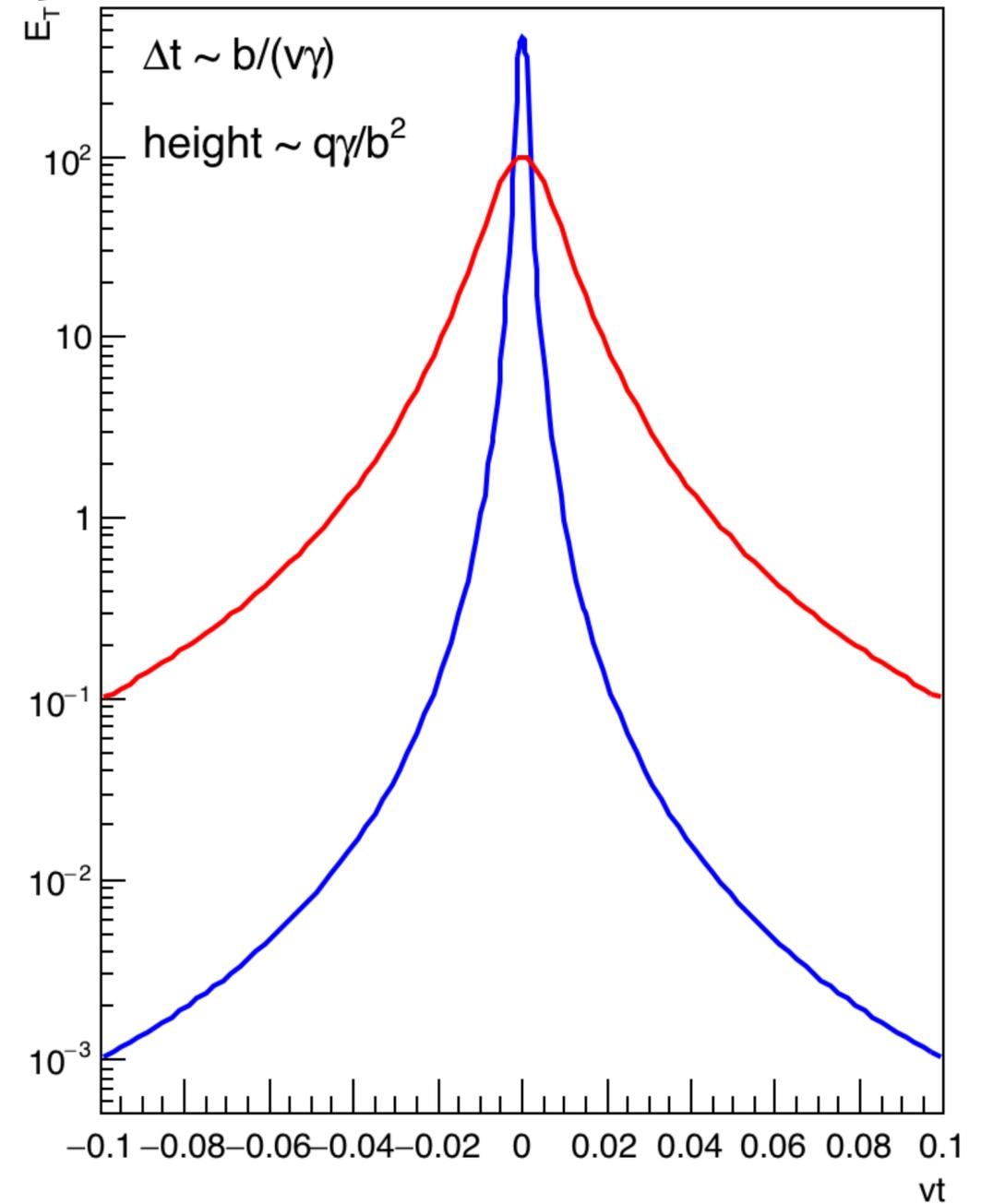
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Transverse component

Longitudinal component



Observation point

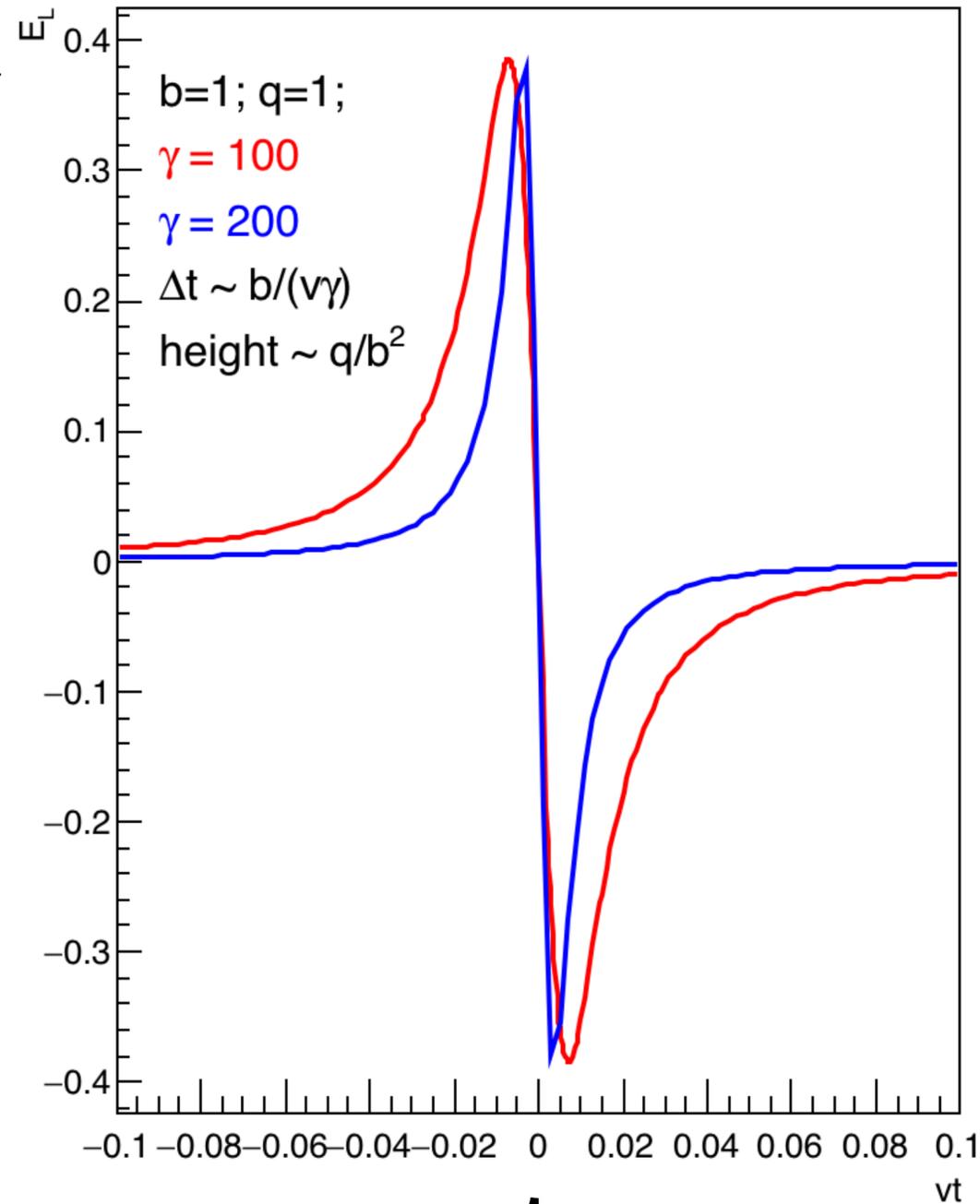


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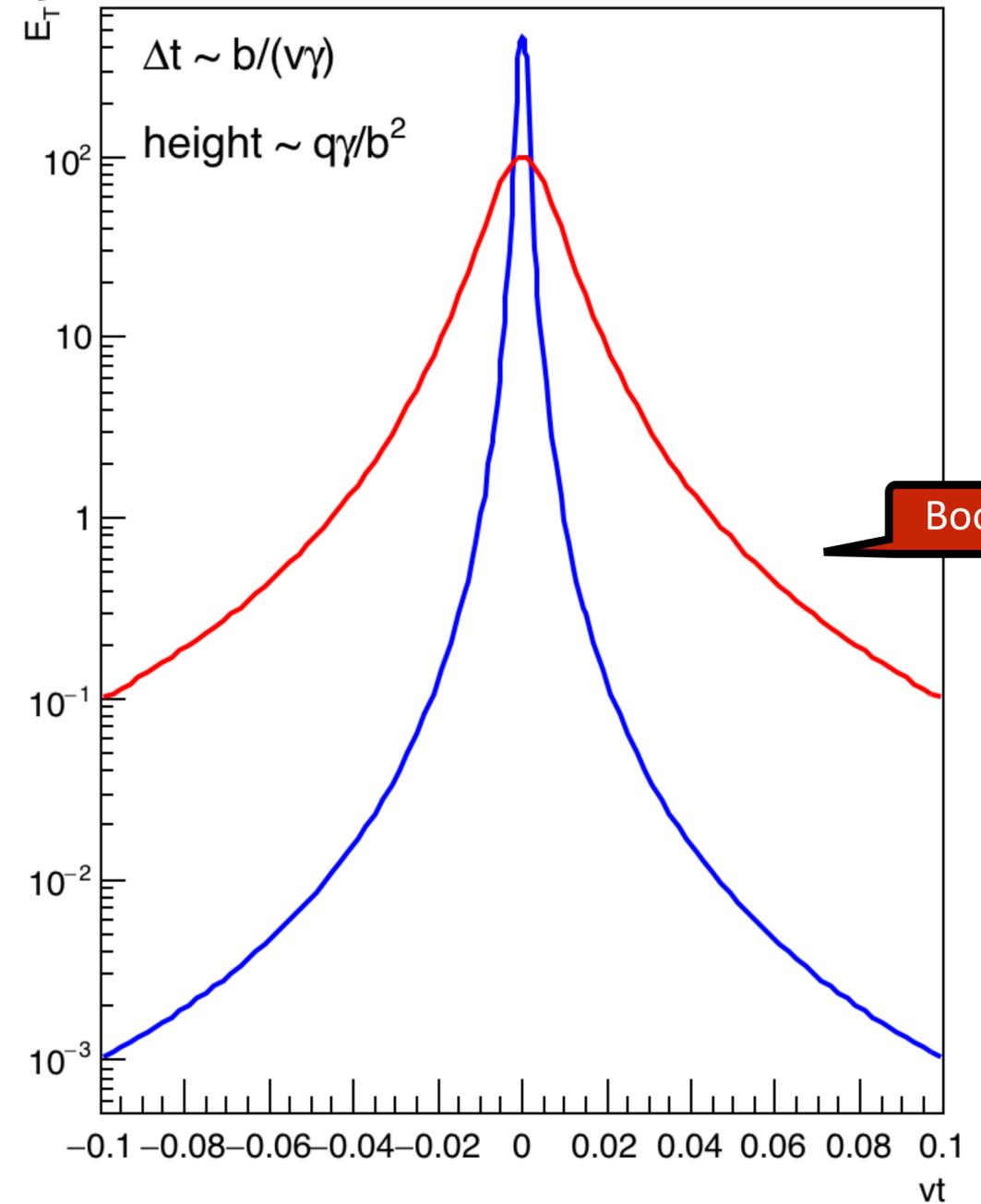
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Transverse component

Longitudinal component



Observation point



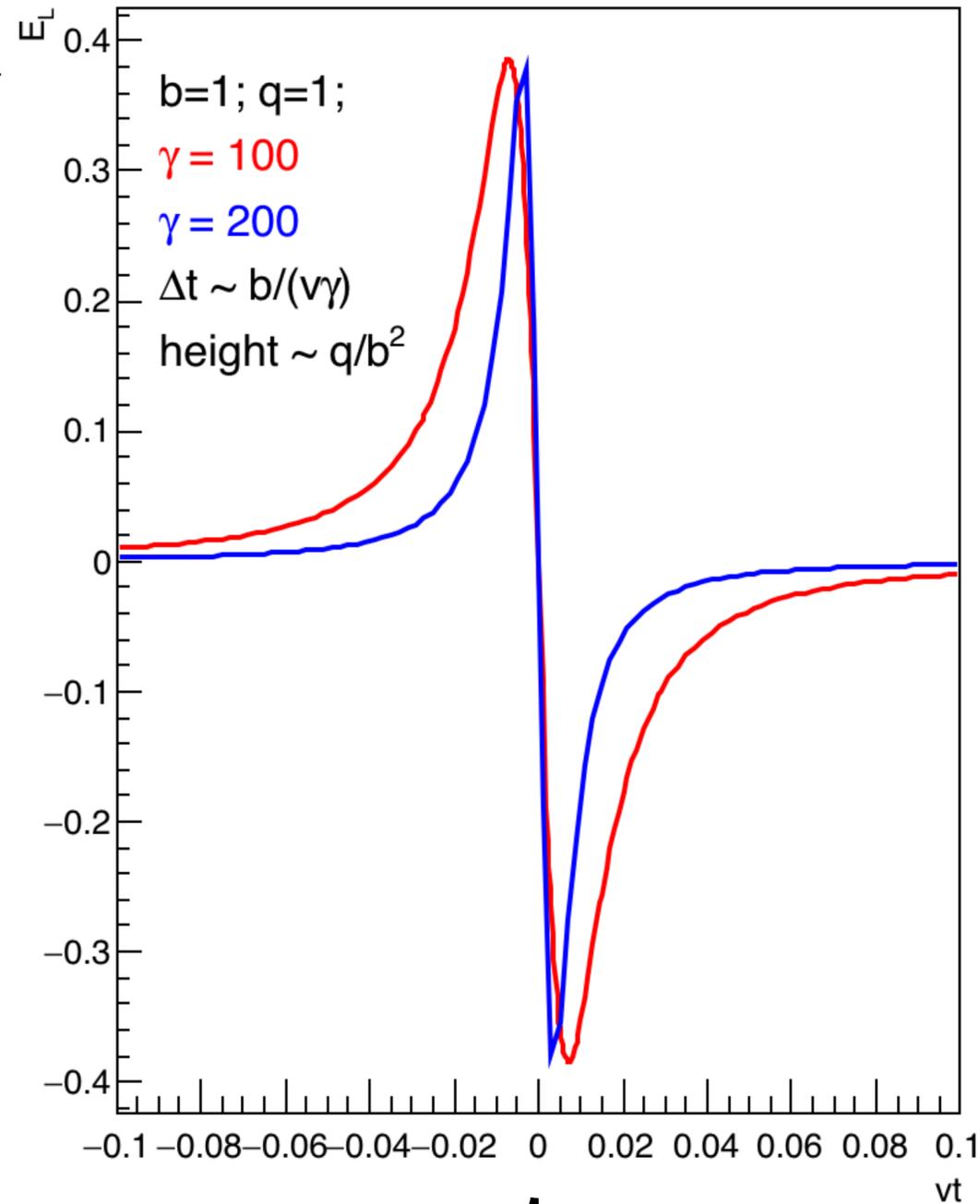
Boost = 100

# The photon flux: field of a point charge

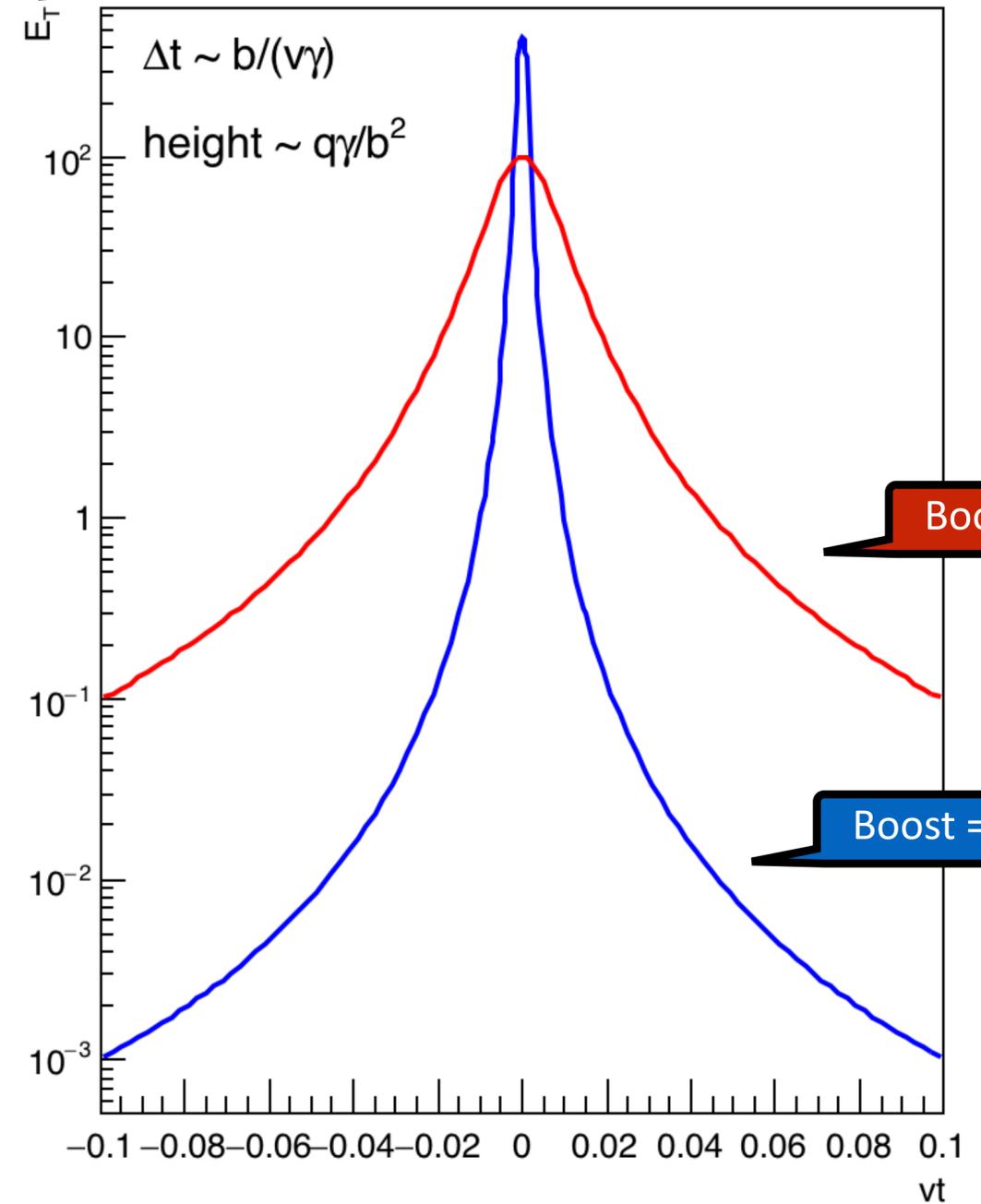
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Transverse component

Longitudinal component



Observation point

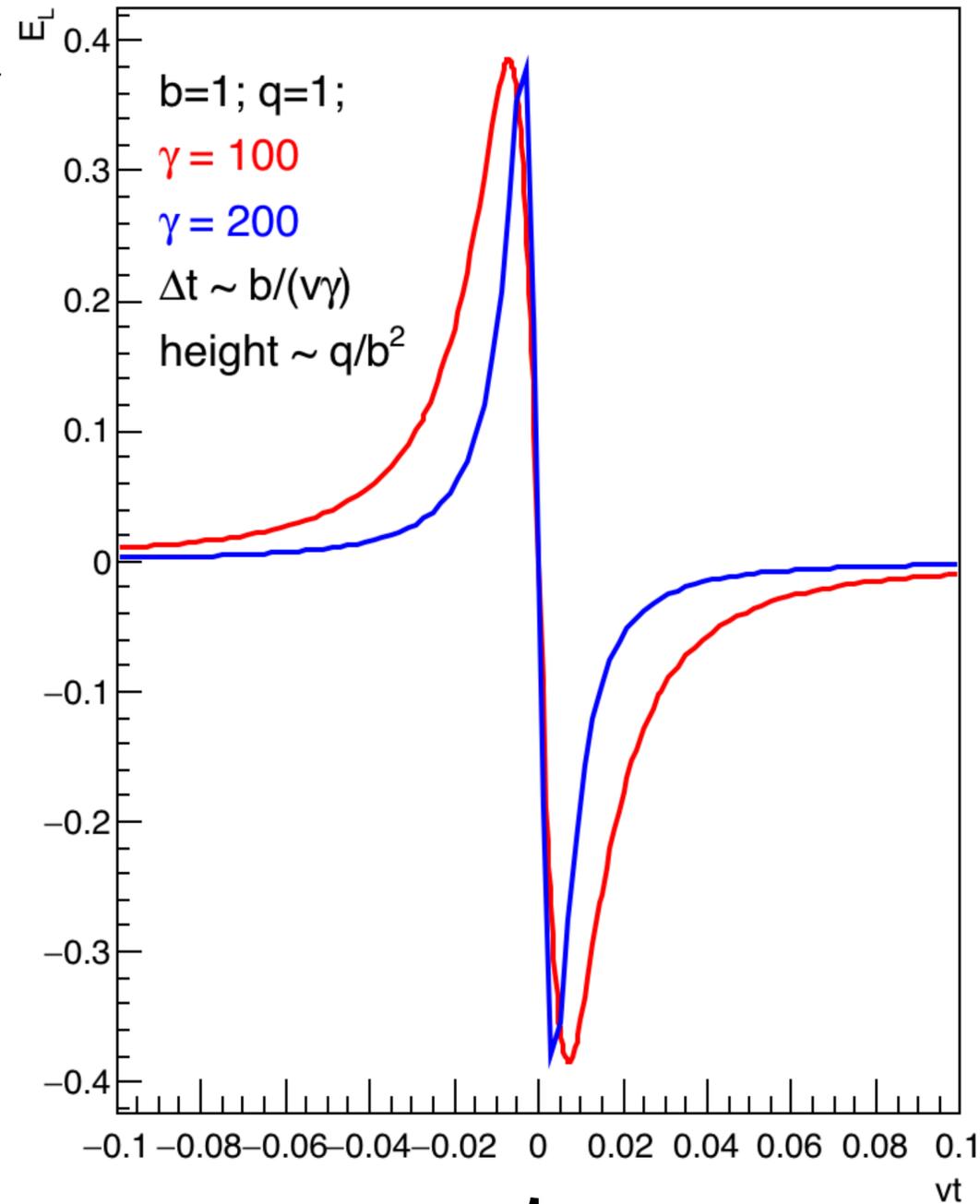


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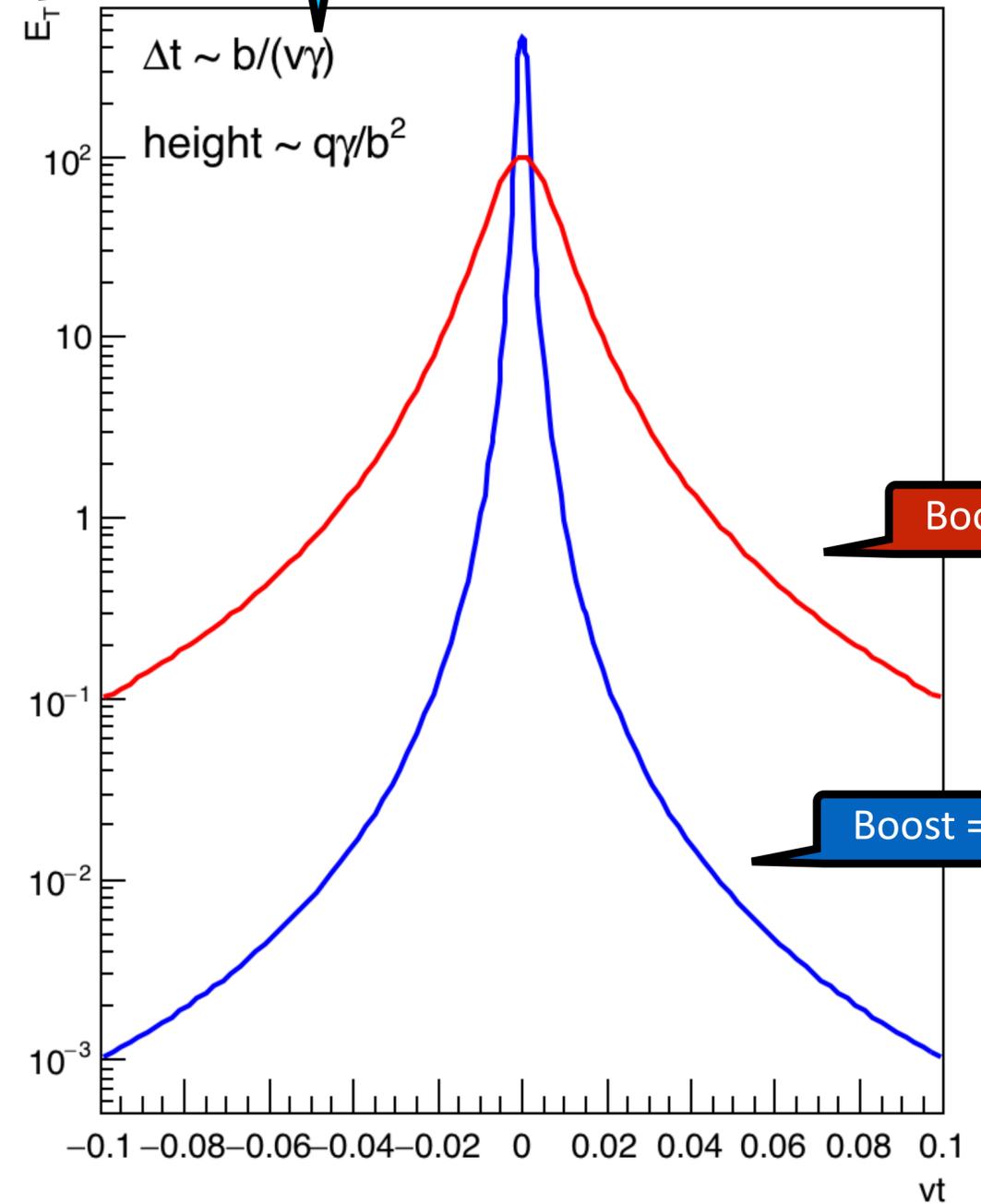
Transverse component

Longitudinal component



Observation point

Narrowness and height driven by boost factor



# The photon flux: field of a point charge

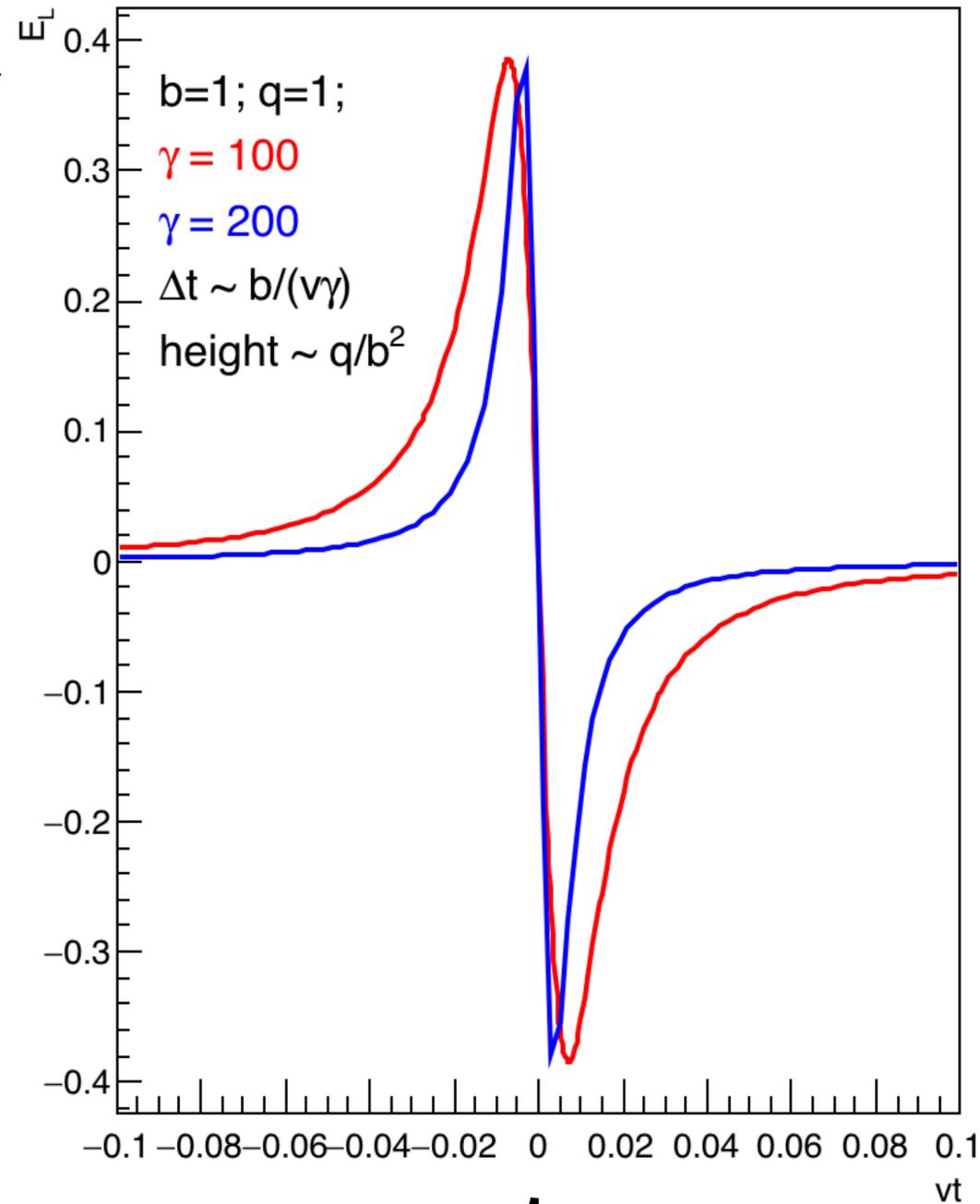
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Transverse component

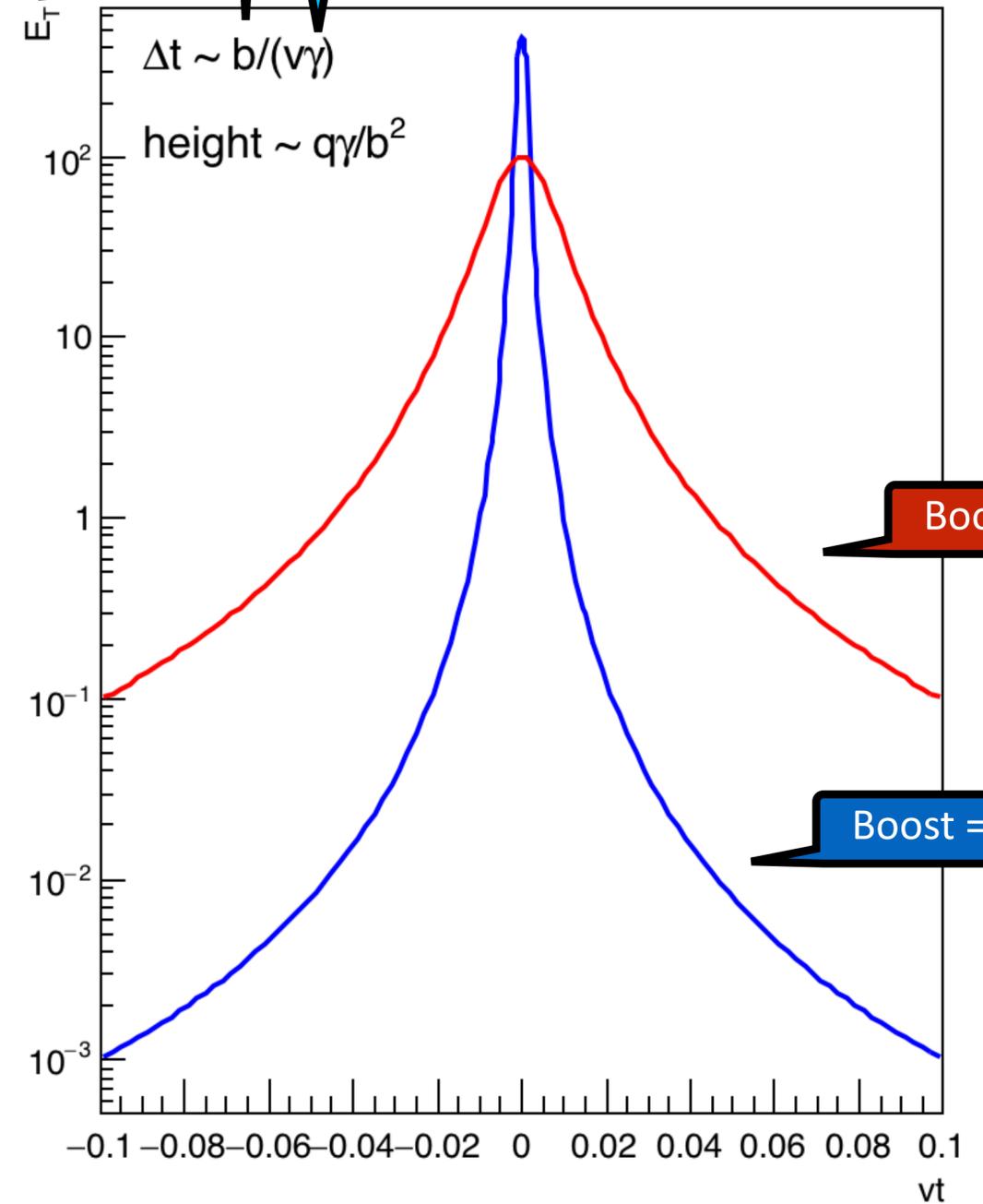
... and distance from the charge

Narrowness and height driven by boost factor

Longitudinal component



Observation point



Boost = 100

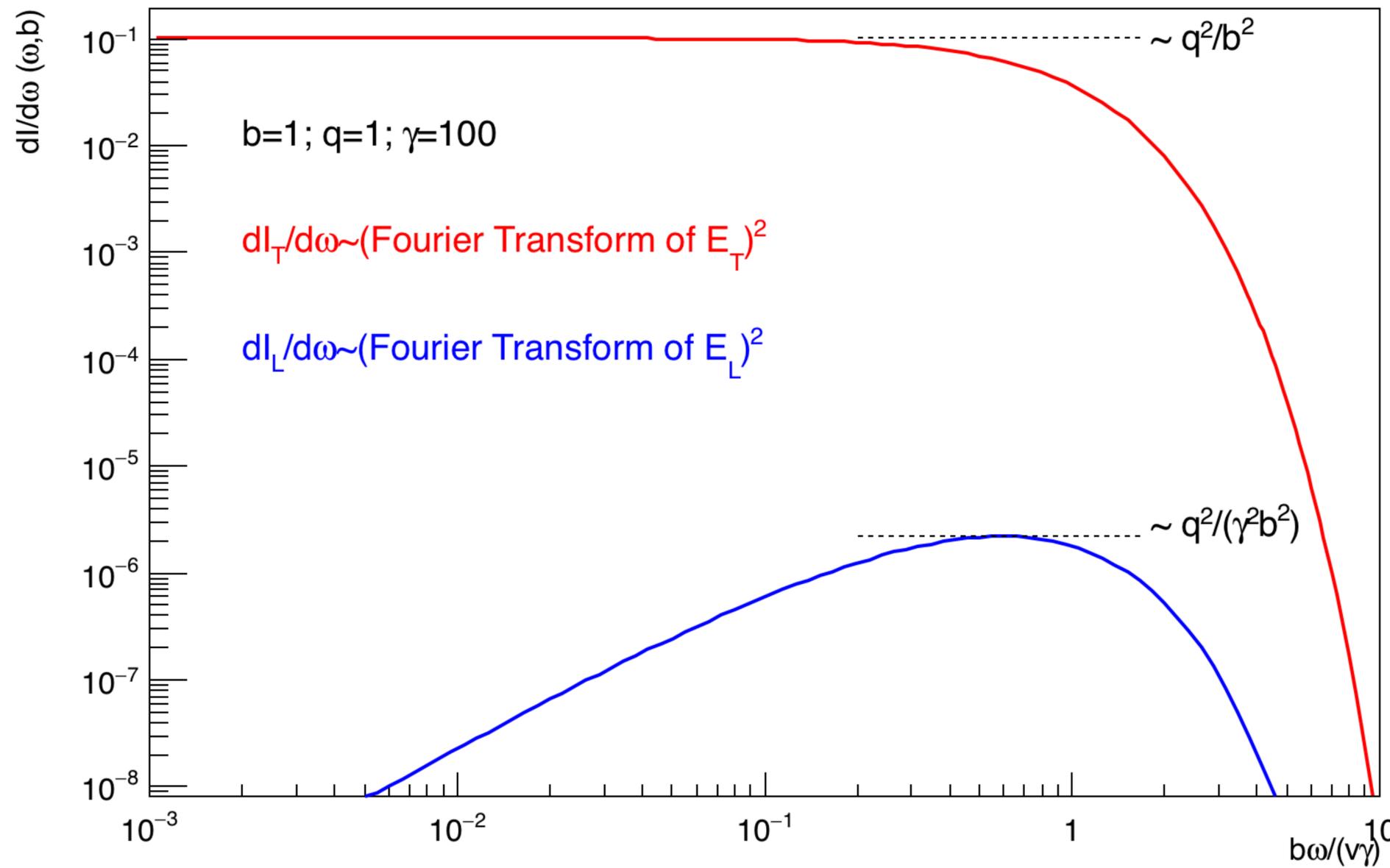
Boost = 200

# The photon flux: Fourier transform for the field of a point charge

Take the square of the Fourier transform of the electric field into frequency space

# The photon flux: Fourier transform for the field of a point charge

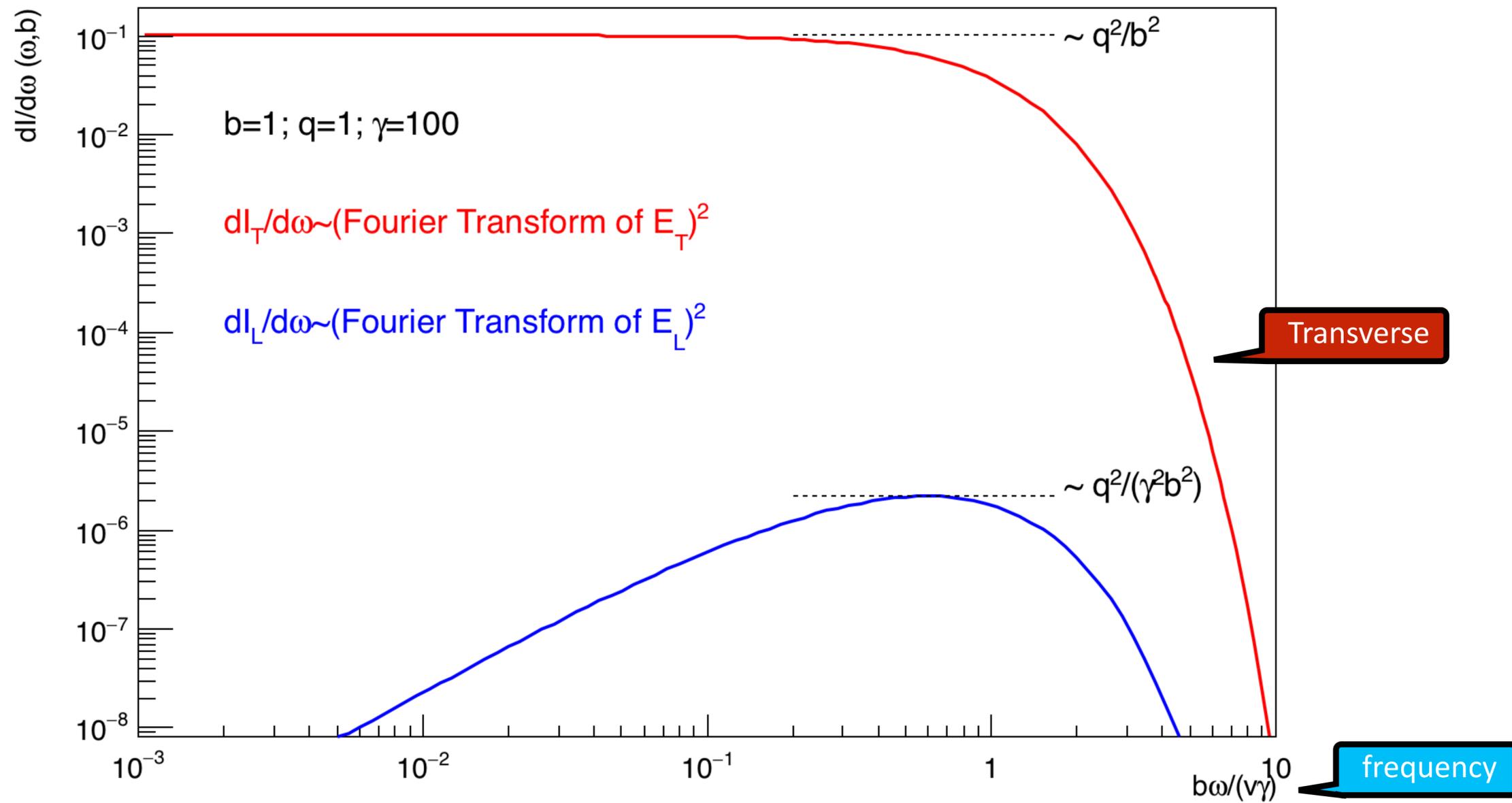
Take the square of the Fourier transform of the electric field into frequency space



frequency

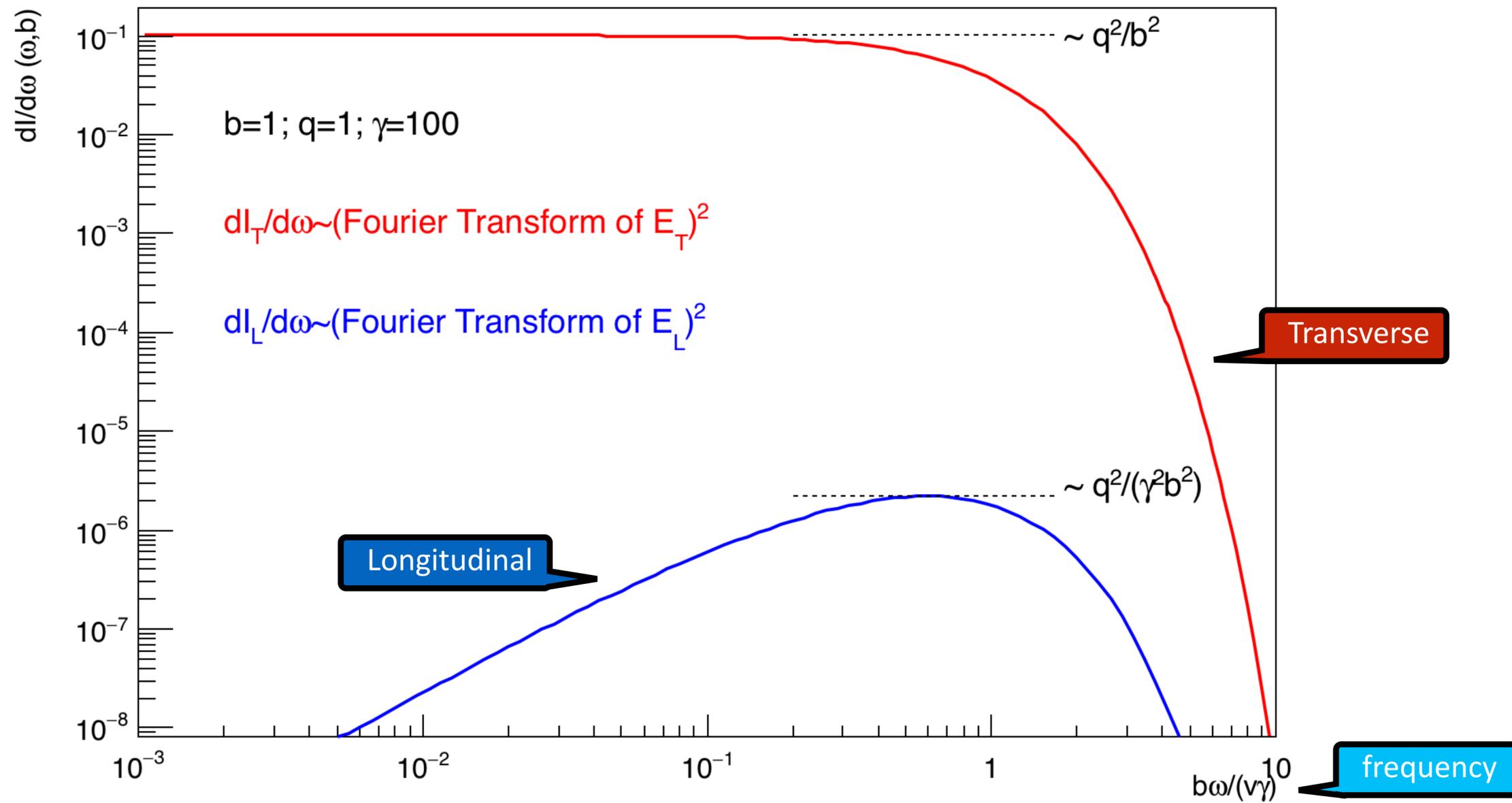
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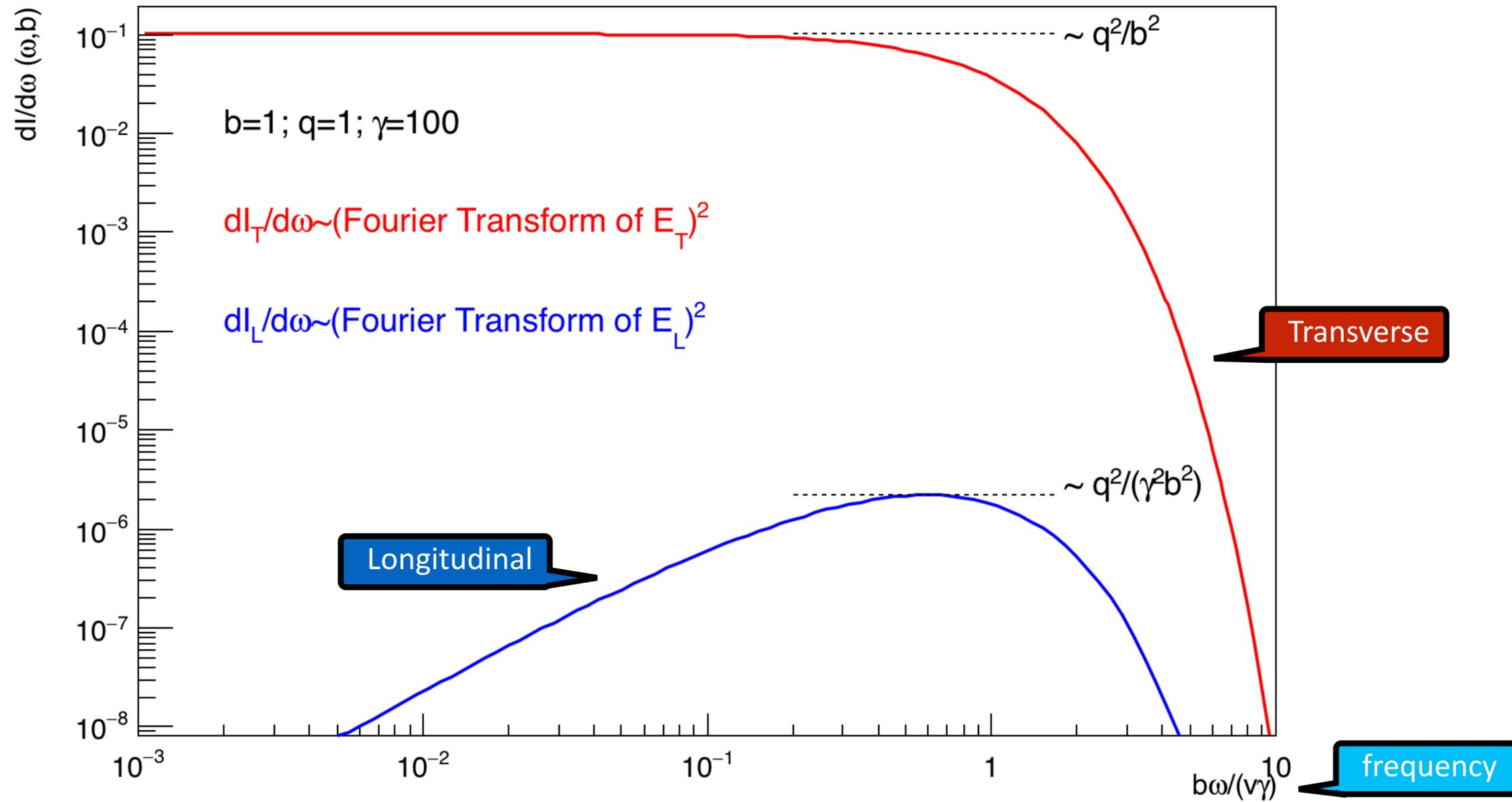
Take the square of the Fourier transform of the electric field into frequency space



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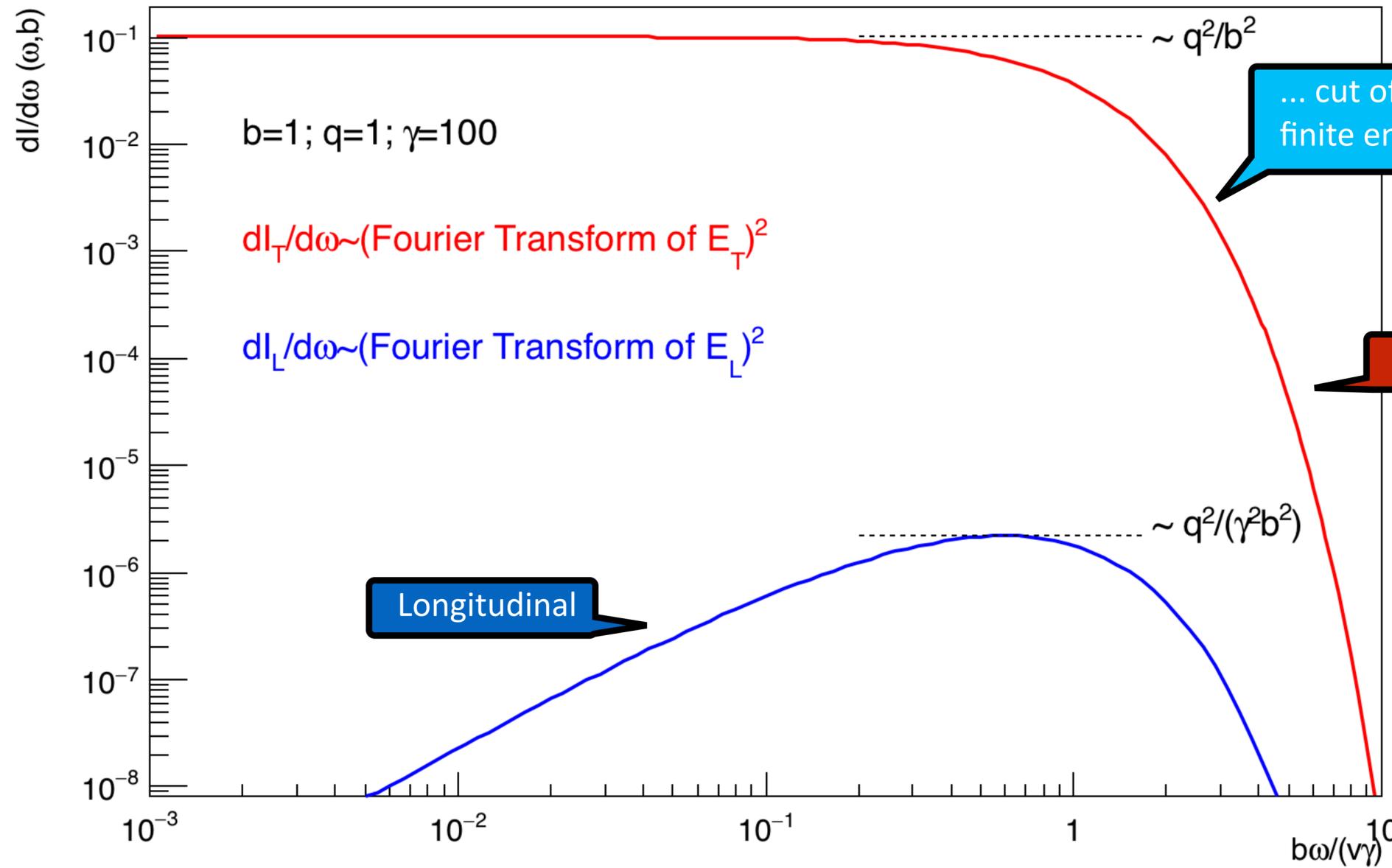
Flat behaviour due to the Dirac-delta-like shape of the field



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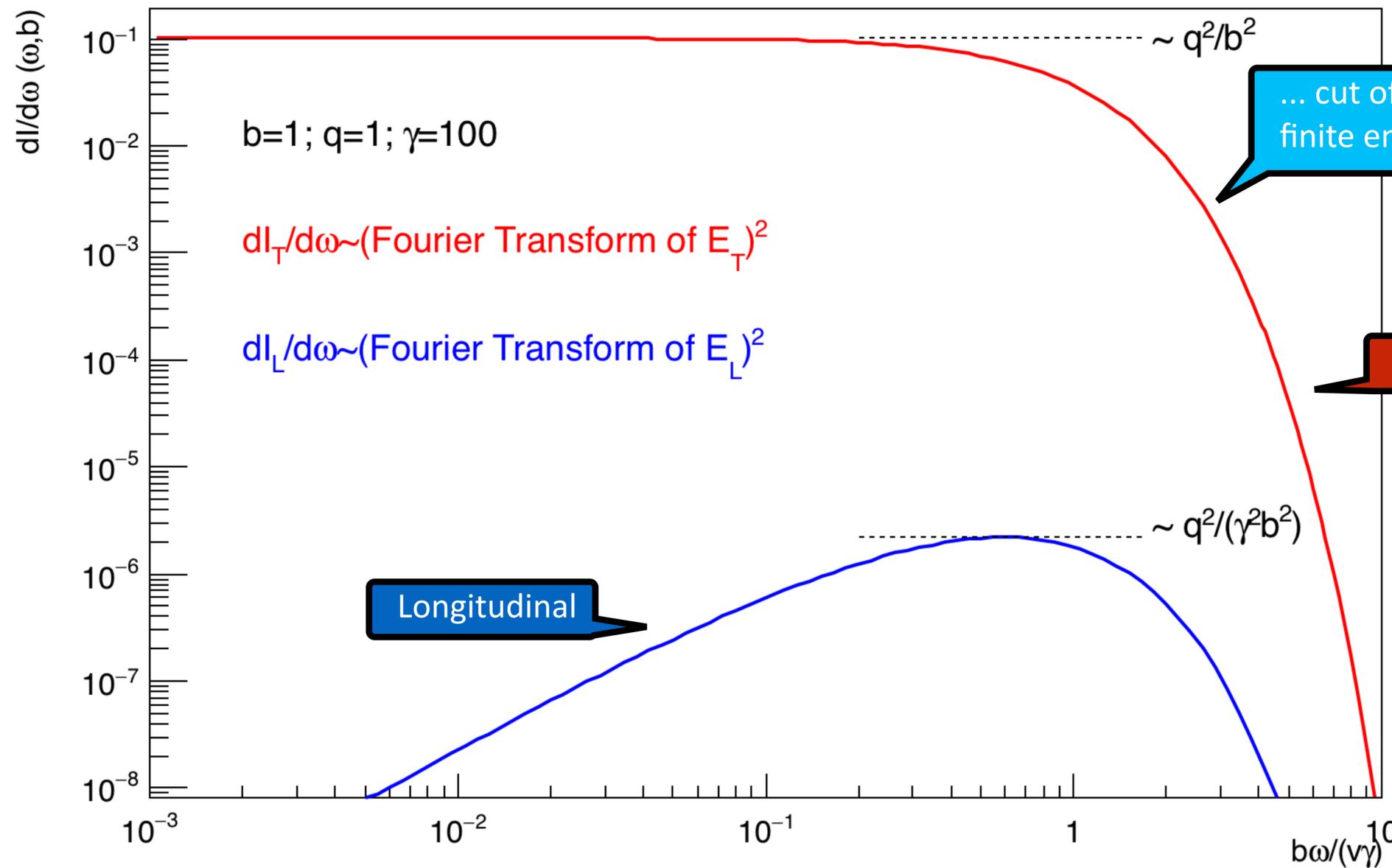


... cut off at large frequencies due to the finite energy (the pulse is not a Dirac delta)

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Take the square of the Fourier transform of the electric field into frequency space

Flat behaviour due to the Dirac-delta-like shape of the field



... cut off at large frequencies due to the finite energy (the pulse is not a Dirac delta)

Transverse

Longitudinal

frequency

This intensity is interpreted as the number of photons with a given energy and at a given transverse distance from the charge.

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

# The photon flux: a bit more general approach

The number of photons  
(known as the photon flux)

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Energy of photon

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Energy of photon

Distance from the centre  
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Particle charge

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Energy of photon

boost

Distance from the centre  
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# The photon flux: a bit more general approach

The number of photons  
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Particle charge

Form factor

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2) J_1(x_\perp k_\perp)}{k_\perp^2 + (k/\gamma)^2} \right|^2$$

Energy of photon

boost

Distance from the centre  
of the charged particle

# The photon flux: a bit more general approach

Point charge

The number of photons  
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Particle charge

Form factor

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Energy of photon

boost

Distance from the centre  
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# The photon flux: a bit more general approach

The number of photons (known as the photon flux)

Particle charge

Point charge

Form factor

Fourier-Bessel transform of a Woods-Saxon distribution

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

Energy of photon

Distance from the centre of the charged particle

boost

# The photon flux: a bit more general approach

STARlight <https://inspirehep.net/literature/1475495>

STARlight: convolution of a Yukawa potential and a hard sphere

Point charge

Fourier-Bessel transform of a Woods-Saxon distribution

The number of photons  
(known as the photon flux)

Particle charge

Form factor

$$n(k, \vec{x}_\perp) = \frac{Z^2 \alpha_{\text{QED}}}{\pi^2 k} \left| \int_0^\infty dk_\perp k_\perp^2 \frac{F(k_\perp^2 + (k/\gamma)^2)}{k_\perp^2 + (k/\gamma)^2} J_1(x_\perp k_\perp) \right|^2$$

Energy of photon

boost

Distance from the centre  
of the charged particle

# Form factor of a point charge

Form factor

$$F_{pc}(q) = 1$$

Integral can be done analytically

$$n_{pc}(k, \vec{x}_{\perp}) = \frac{Z^2 \alpha_{\text{QED}} k}{\pi^2 \gamma^2} K_1^2(k x_{\perp} / \gamma)$$

## Other form factors

Used in STARlight

$$F_{hsY}(q) = \frac{4\pi d_0}{Aq^3} [\sin(qR_A) - qR_A \cos(qR_A)] \left( \frac{1}{1 + a^2q^2} \right)$$

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$$F_{WS}(q) = \frac{4\pi}{qA} \int \rho(r) \sin(rq) r dr$$

Woods-Saxon distribution

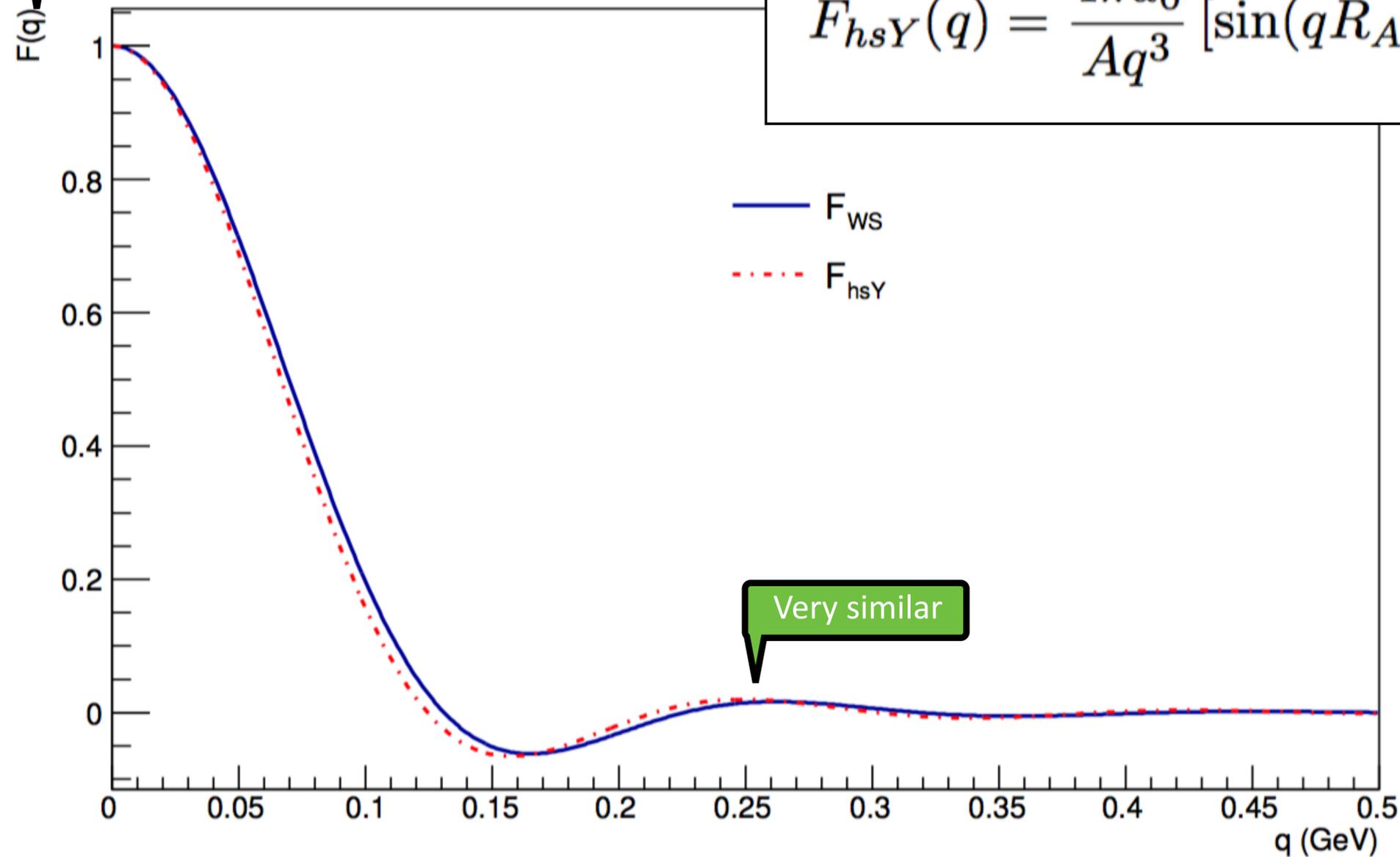
$$\rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-r_A}{z}\right)}$$

# Other form factors

Form factor

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Very similar

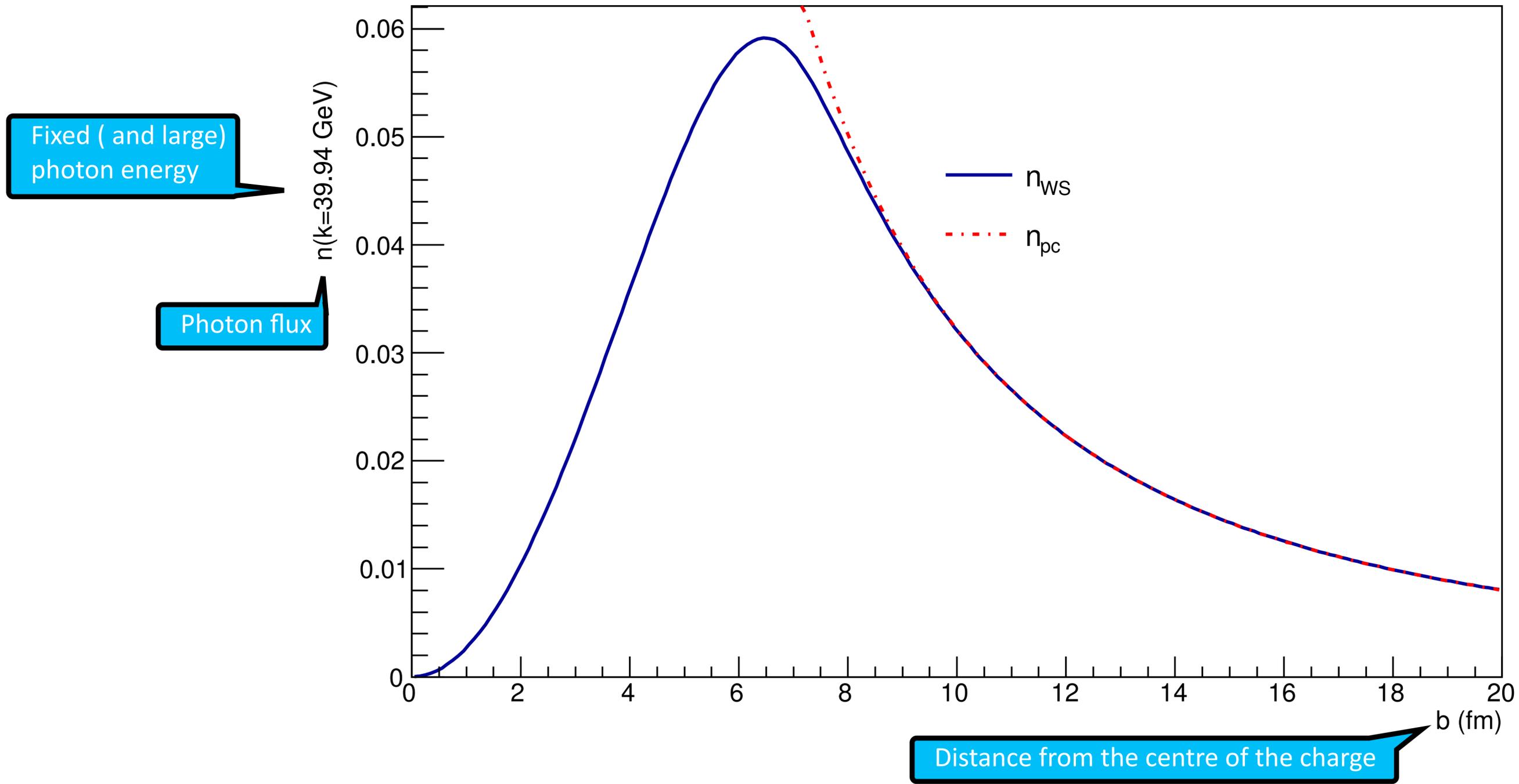
Magnitude of the transferred momentum

$$F_{WS}(q) = \frac{4\pi}{qA} \int \rho(r) \sin(rq) r dr$$

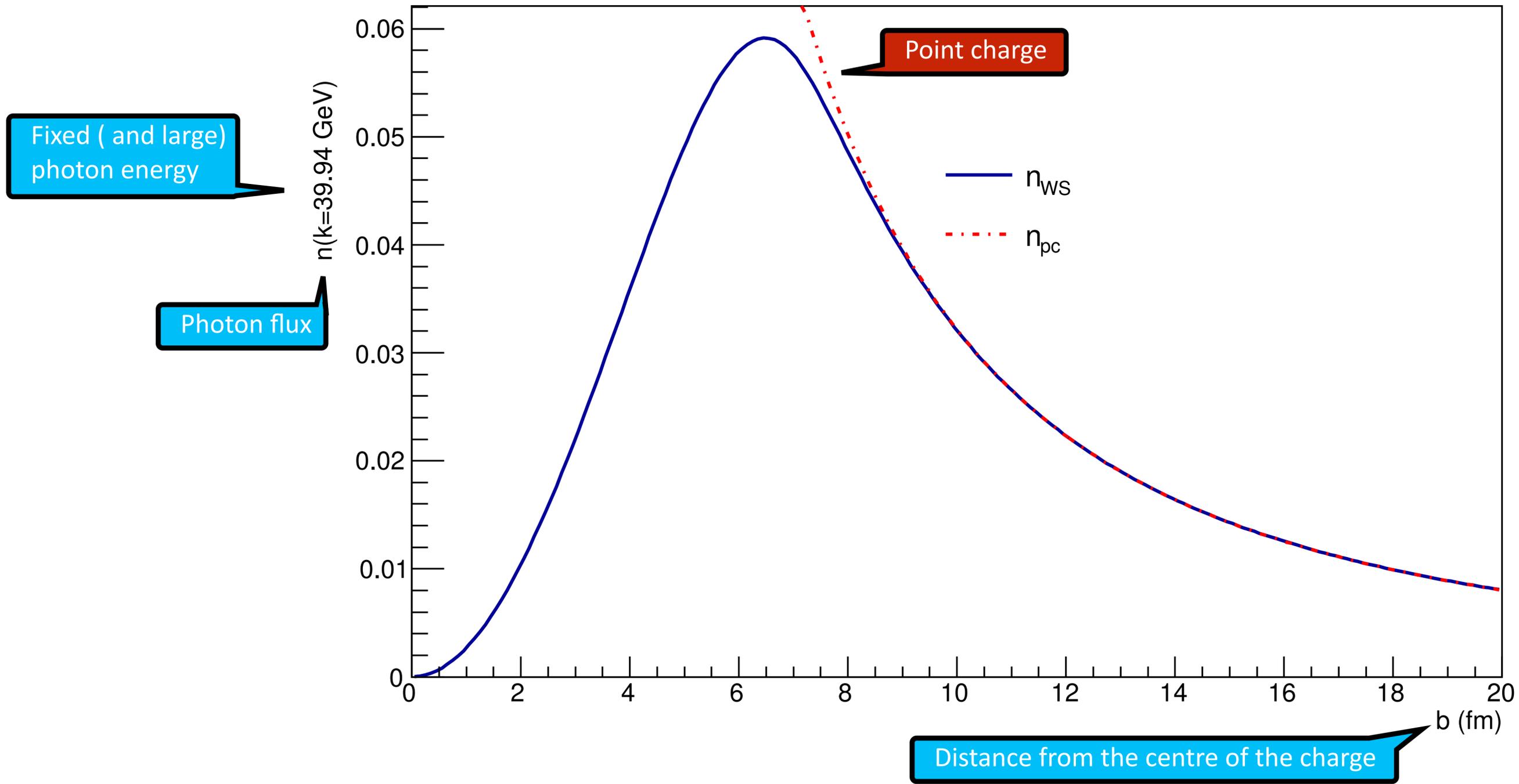
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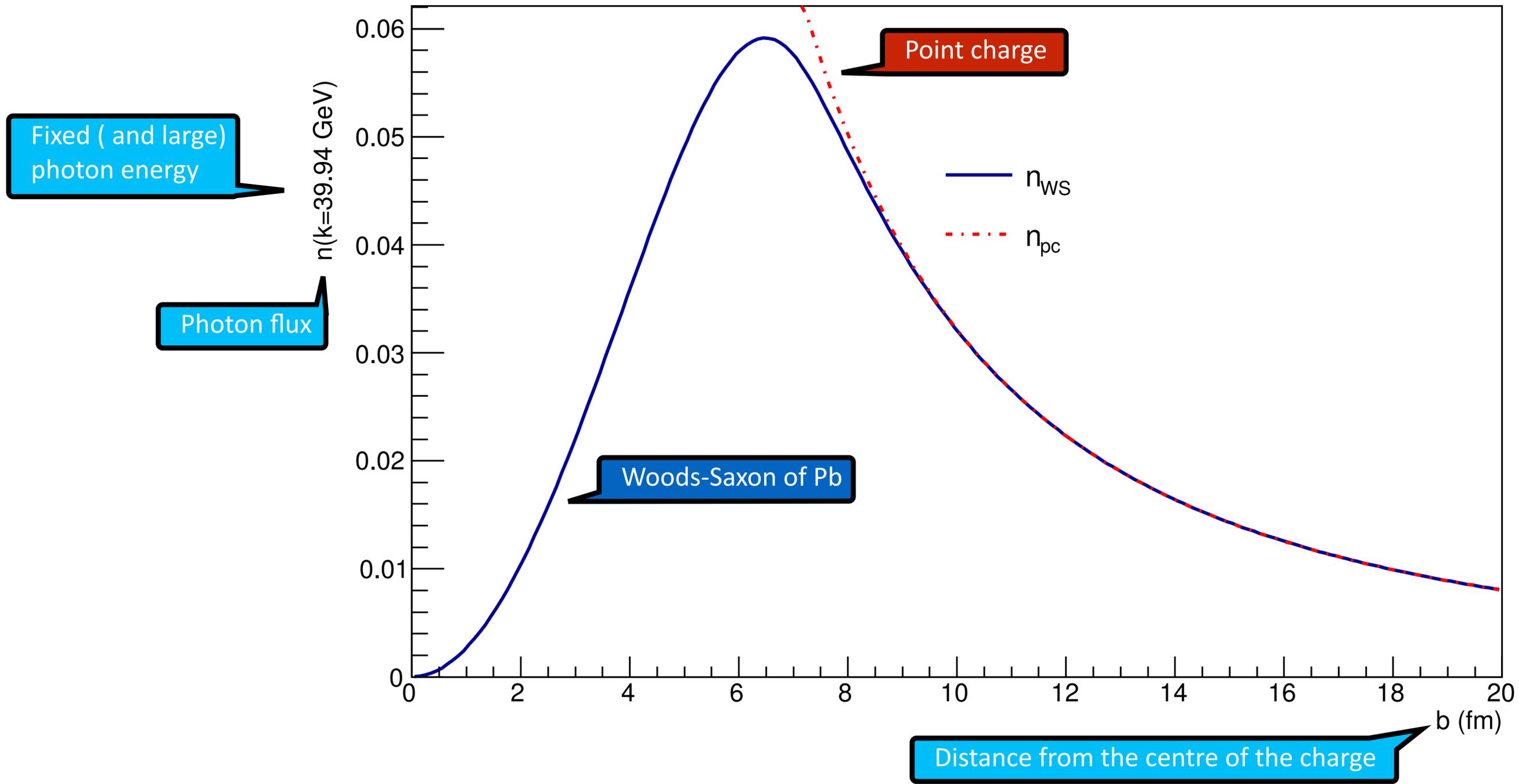
# Comparing fluxes



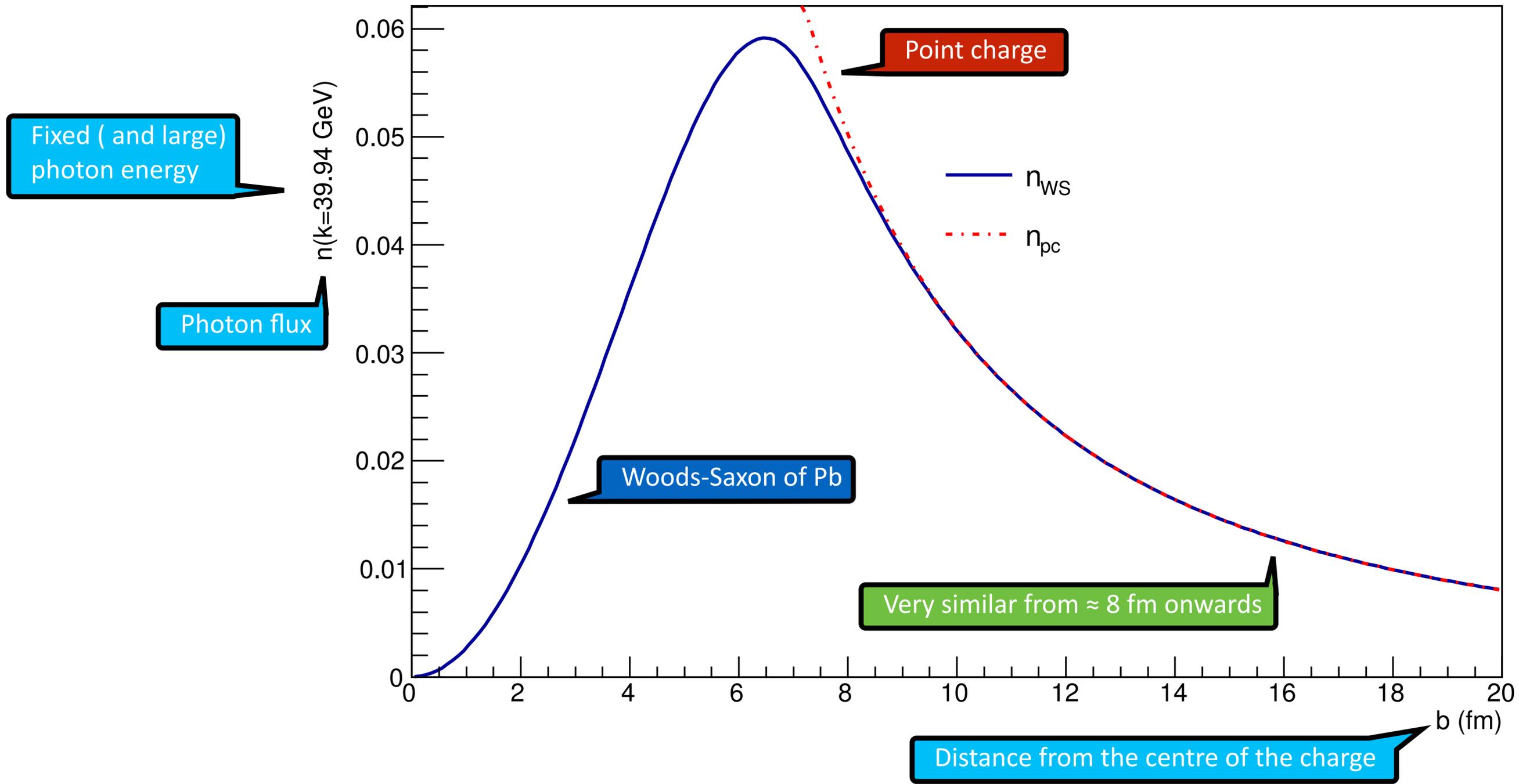
# Comparing fluxes



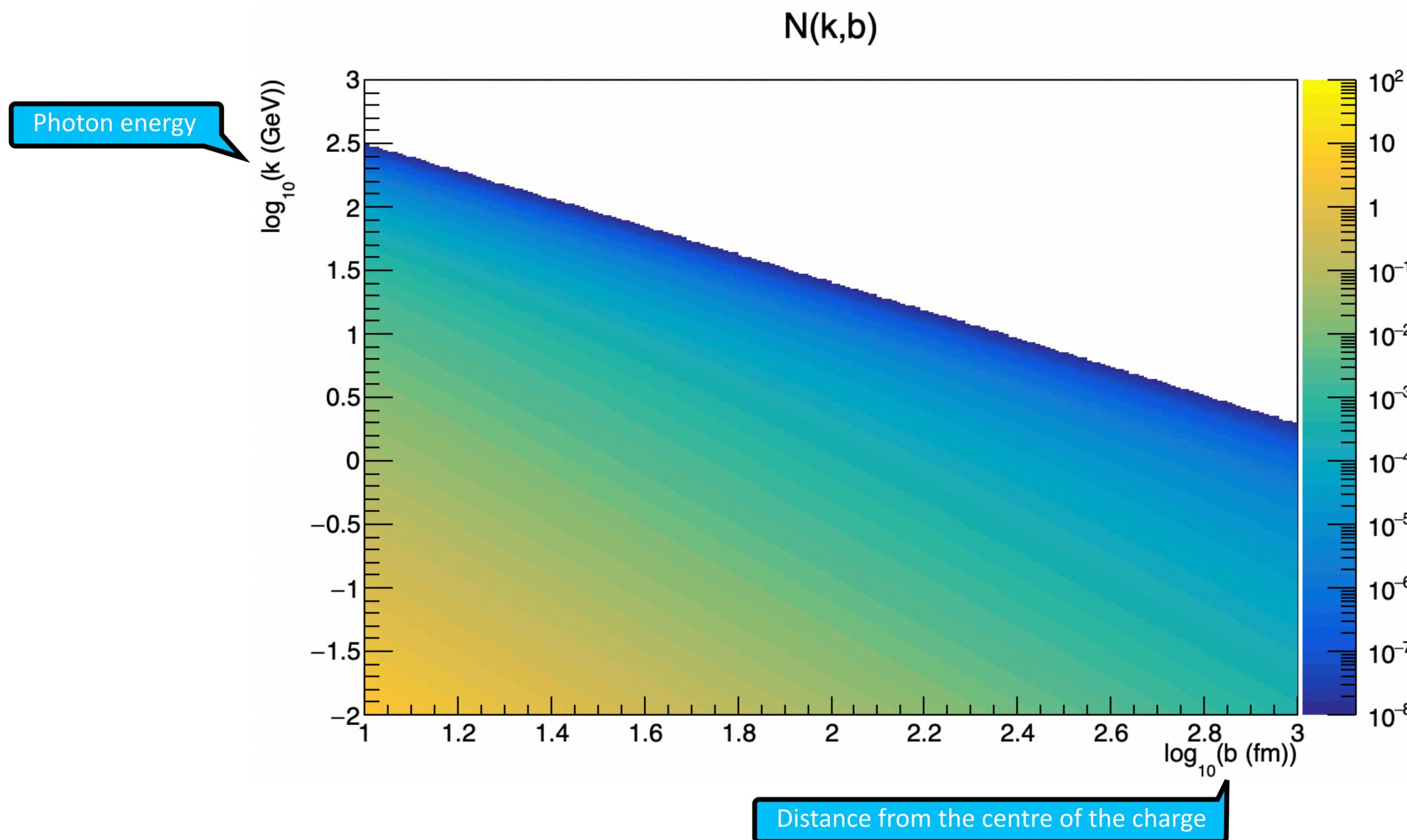
# Comparing fluxes



# Comparing fluxes



# Photon flux of a point charge

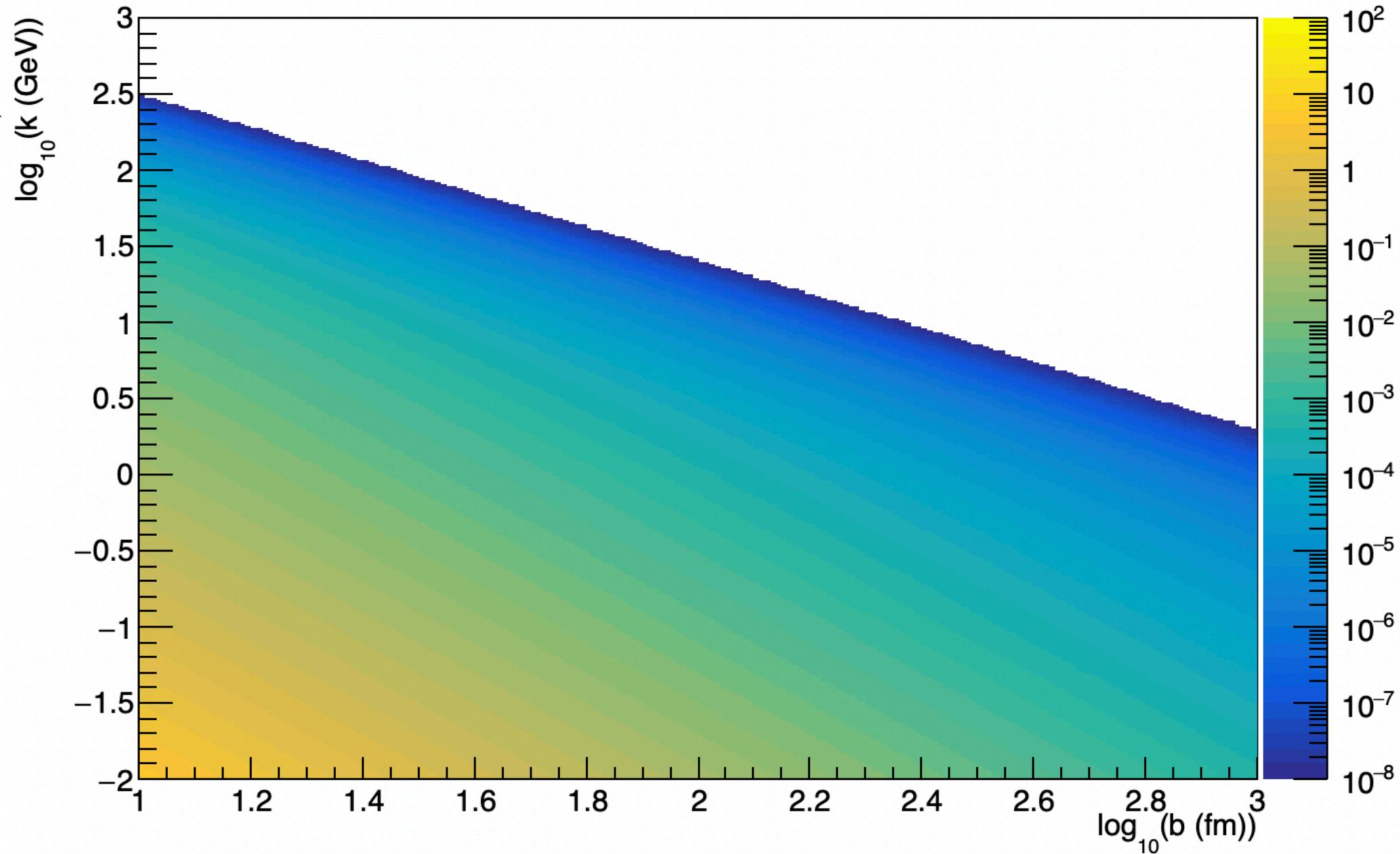


# Photon flux of a point charge

Using LHC relevant parameters and ranges for k and b

$N(k,b)$

Photon energy



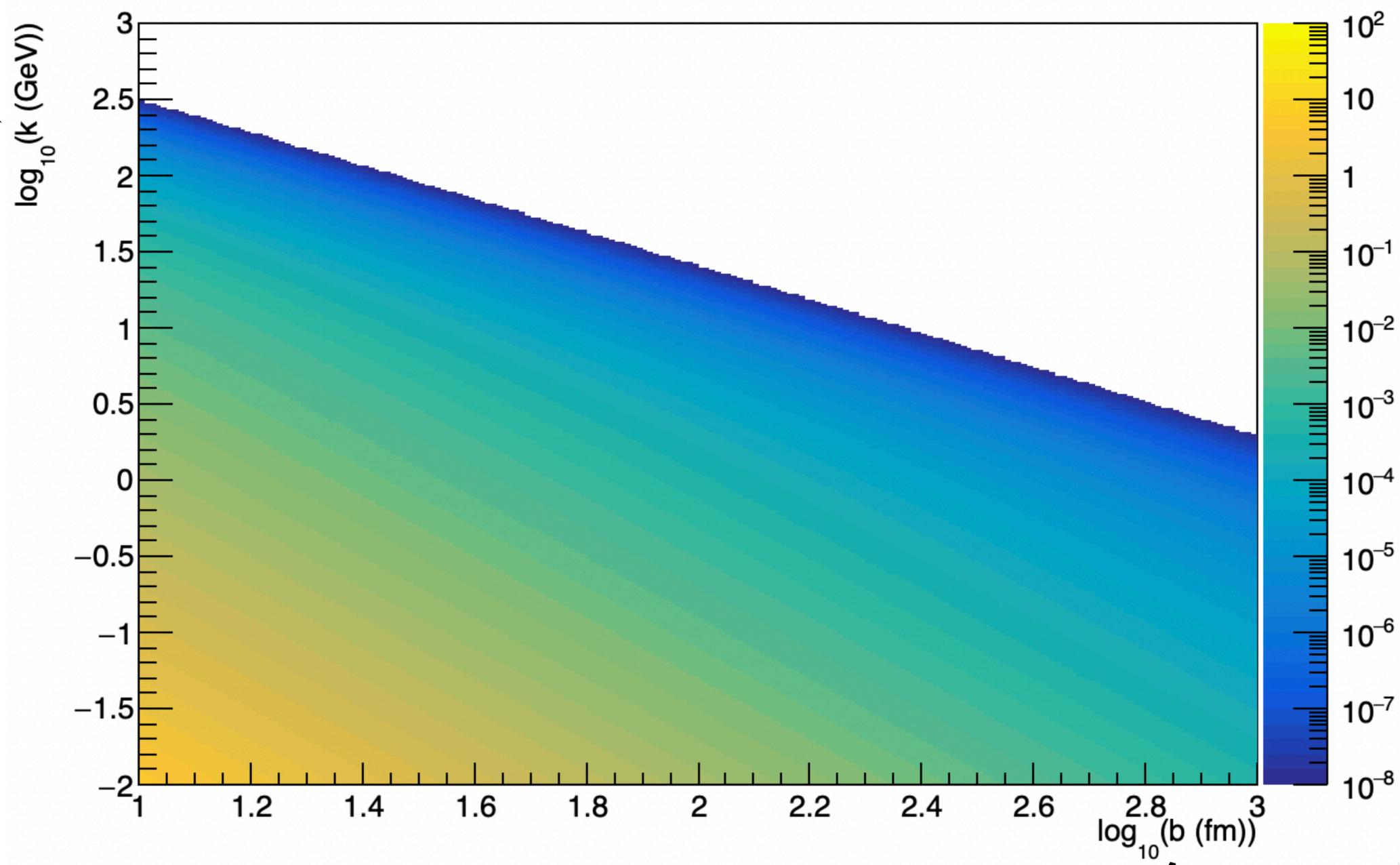
Distance from the centre of the charge

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10 orders of magnitude

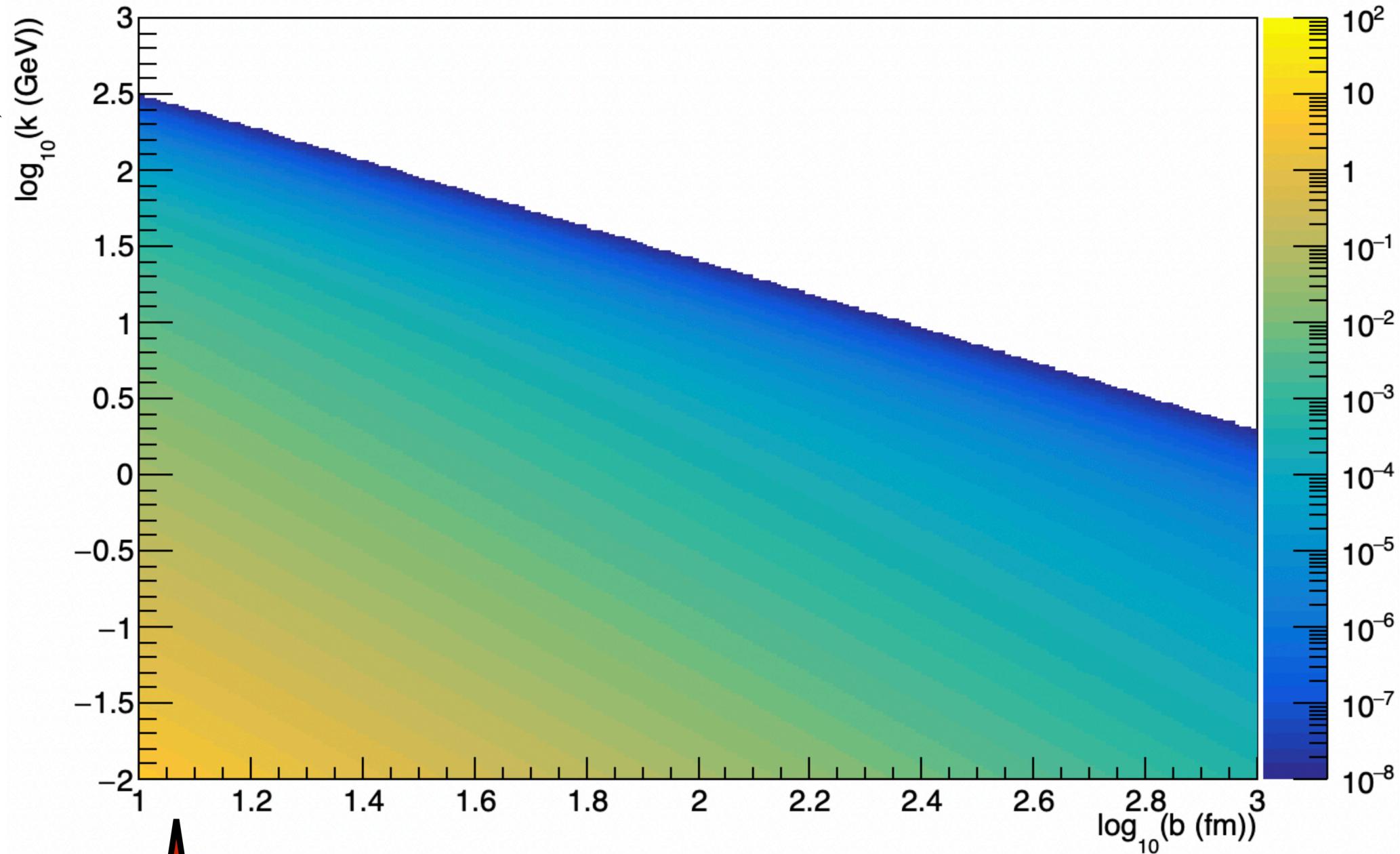
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Large photon energies are more probable at small distances

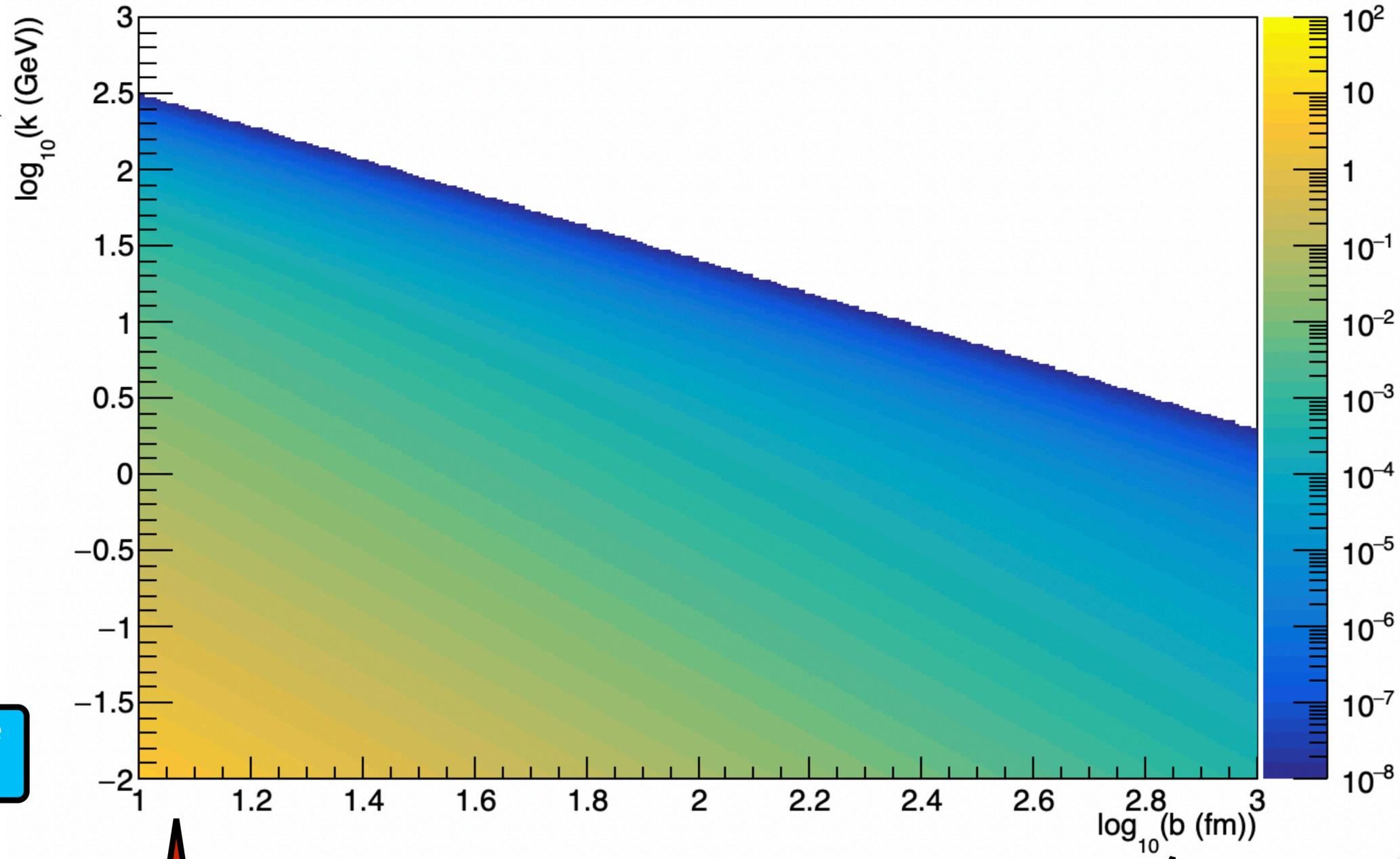
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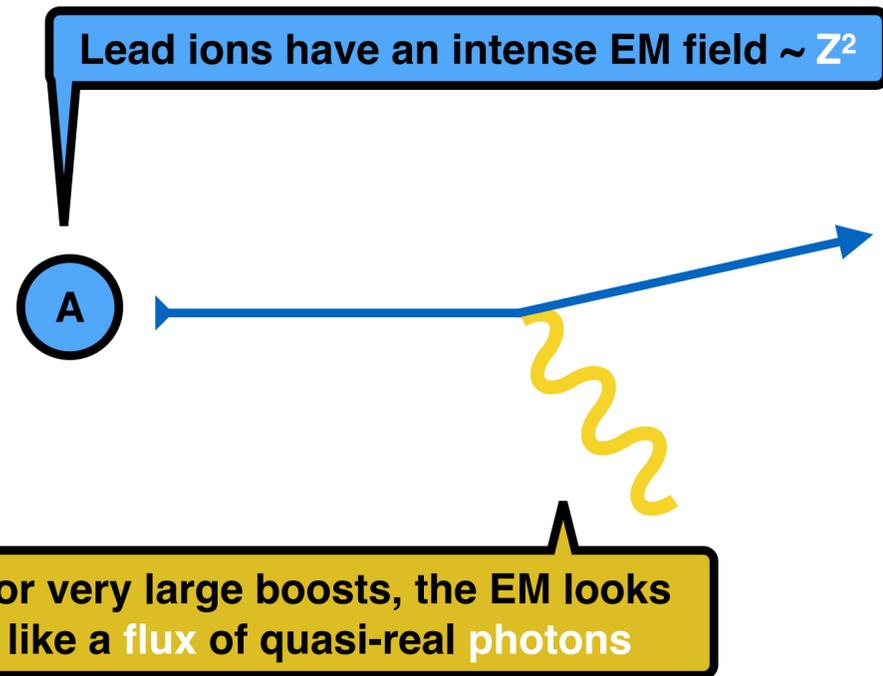
Different final states sample different parts of this plot

Large photon energies are more probable at small distances

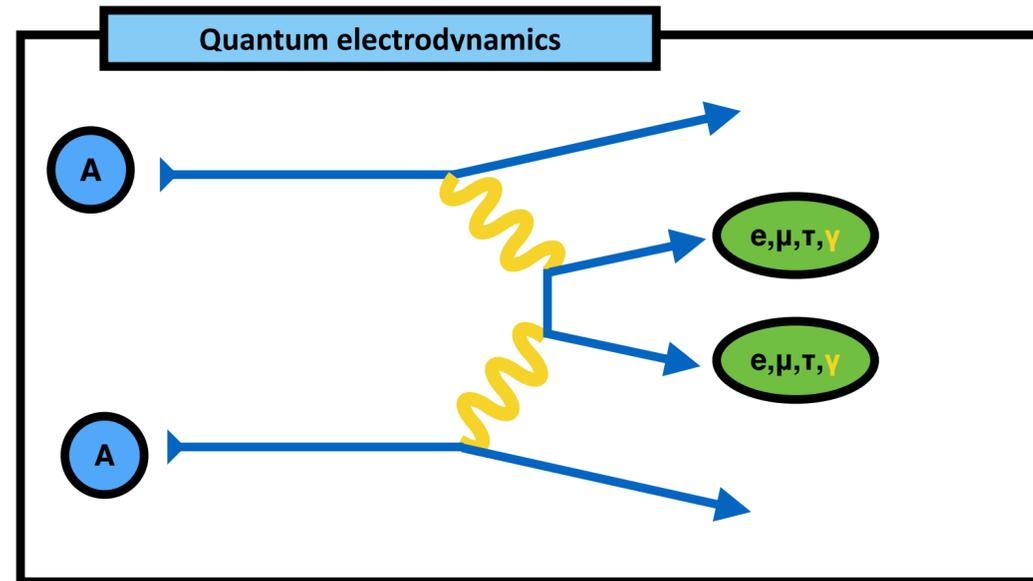
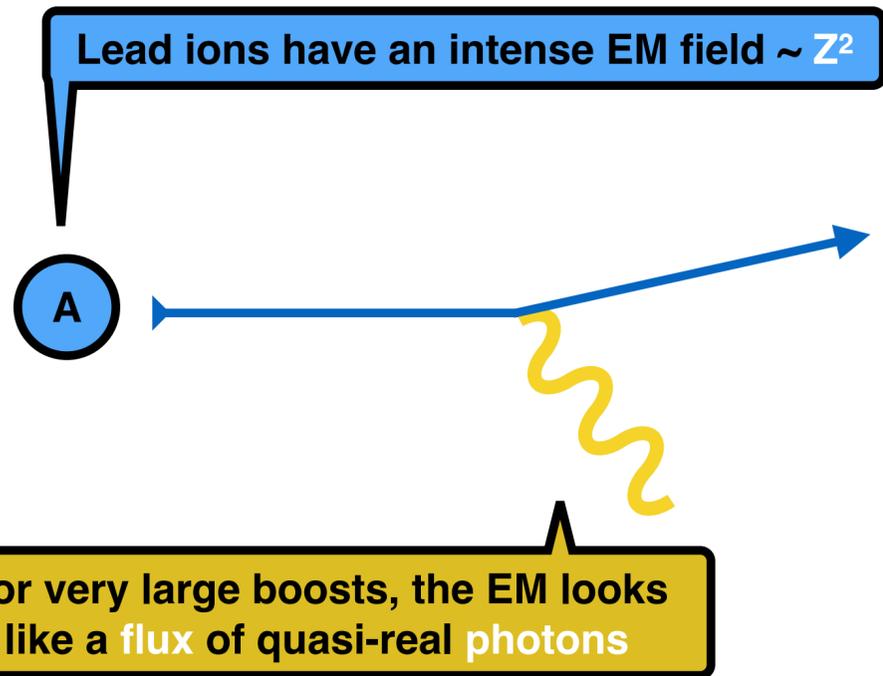
Distance from the centre of the charge

Now that we have the photons, what can we do with them?

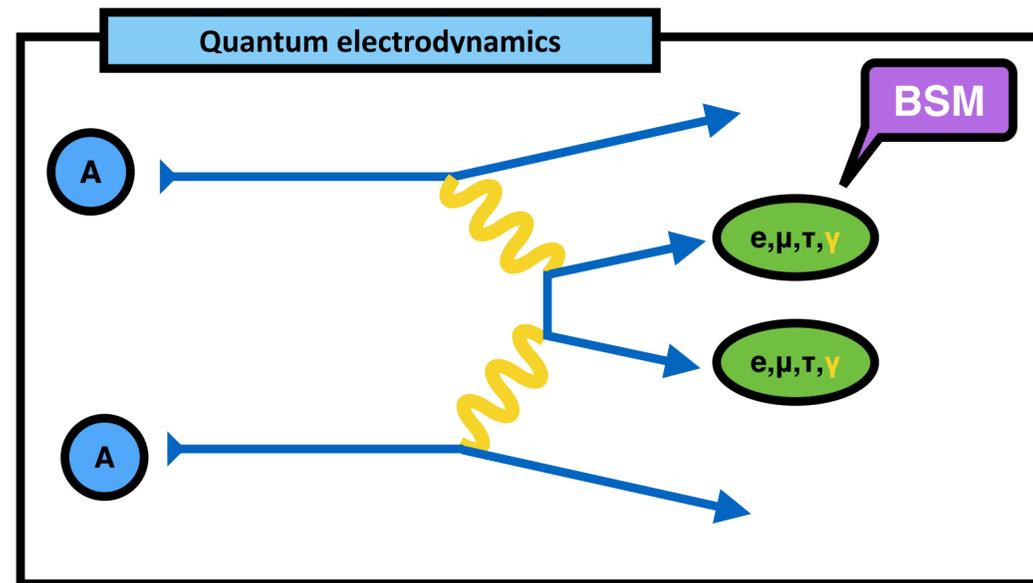
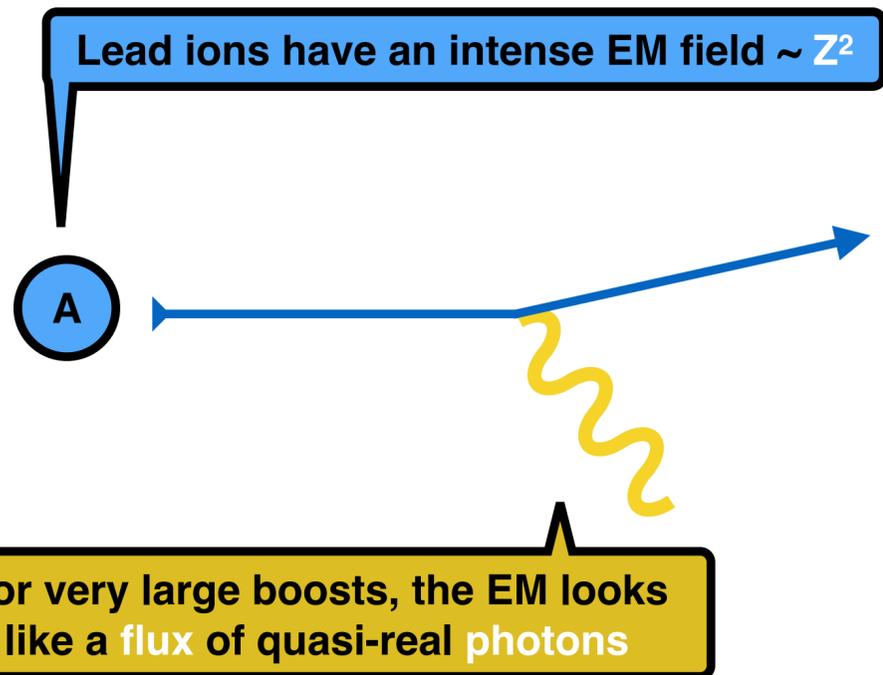
# Photons at the ion colliders: examples of what can be done



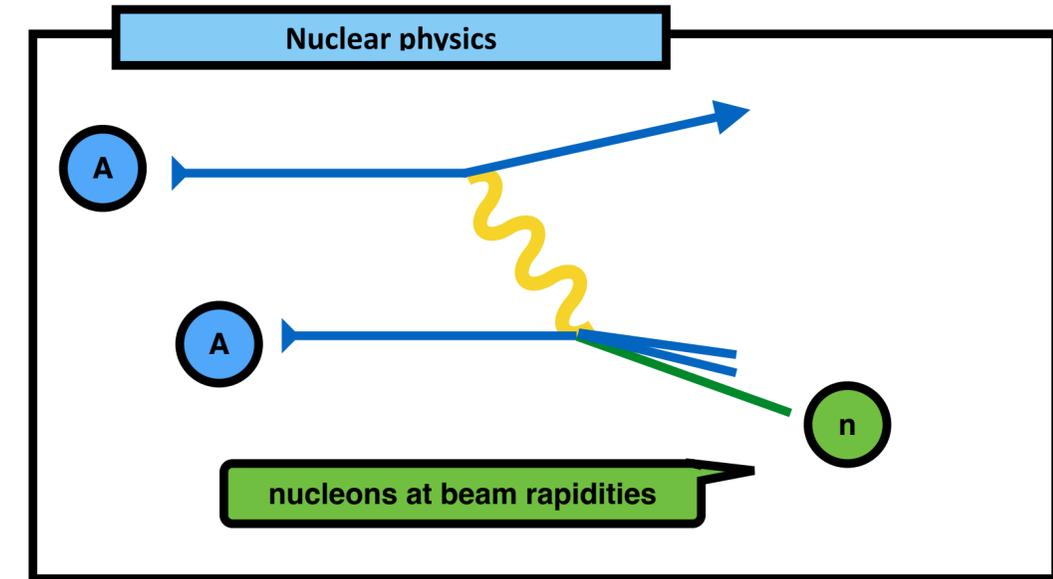
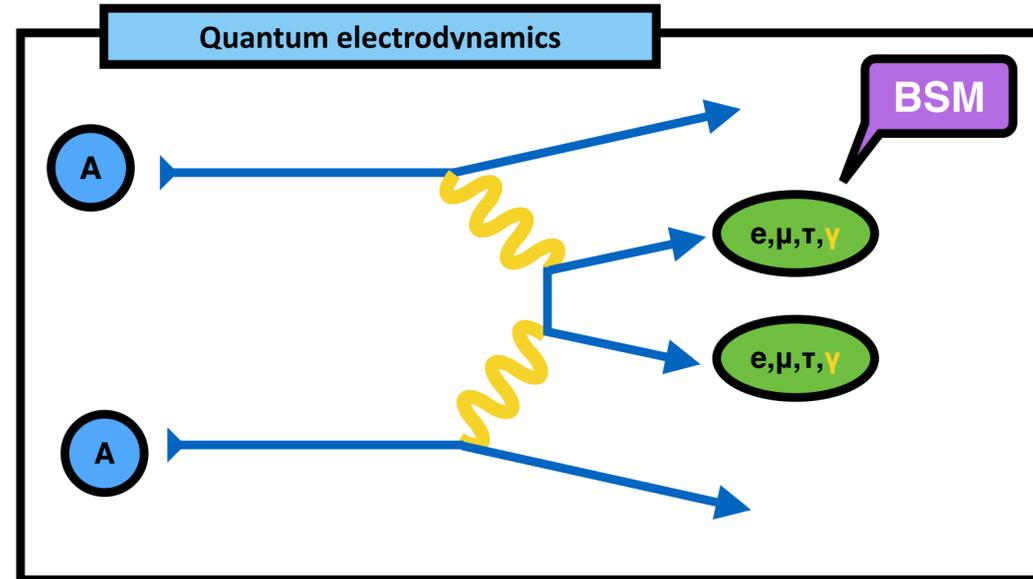
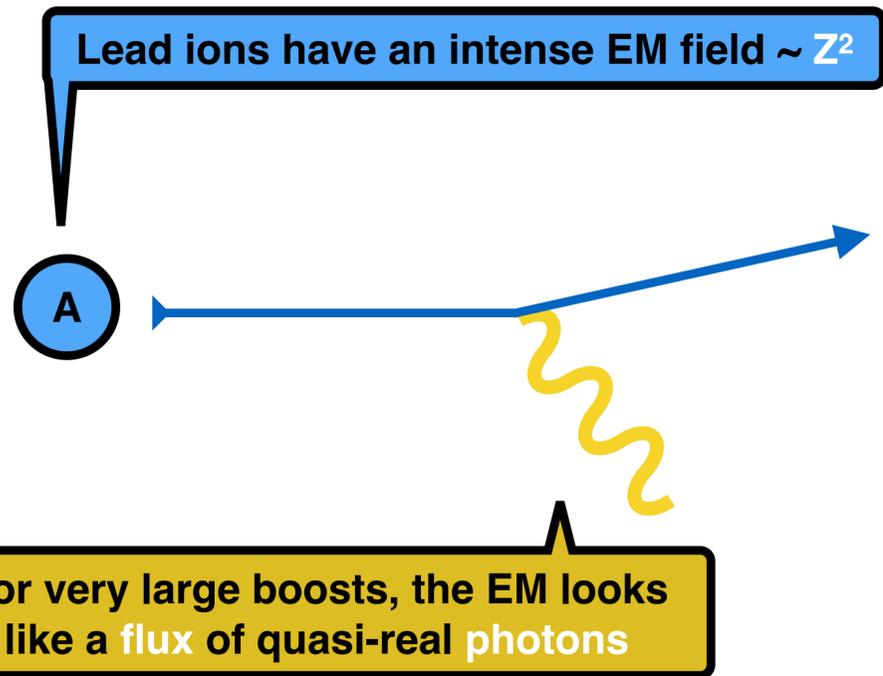
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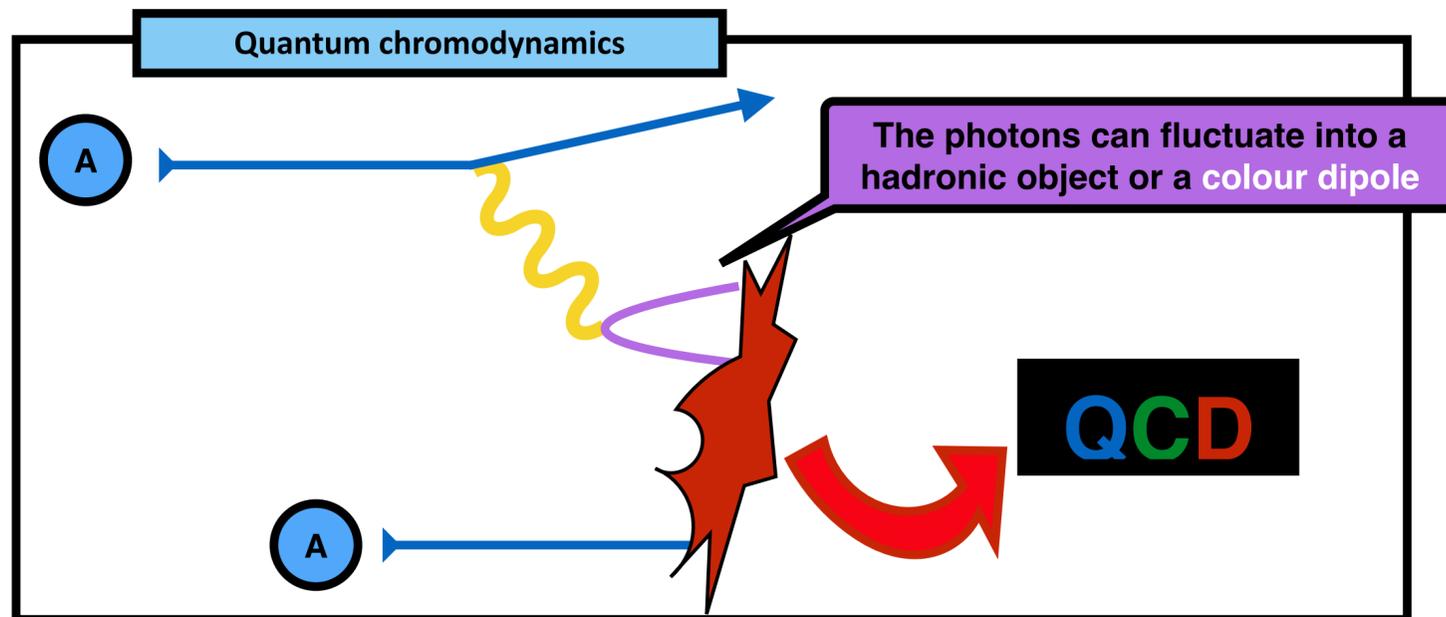
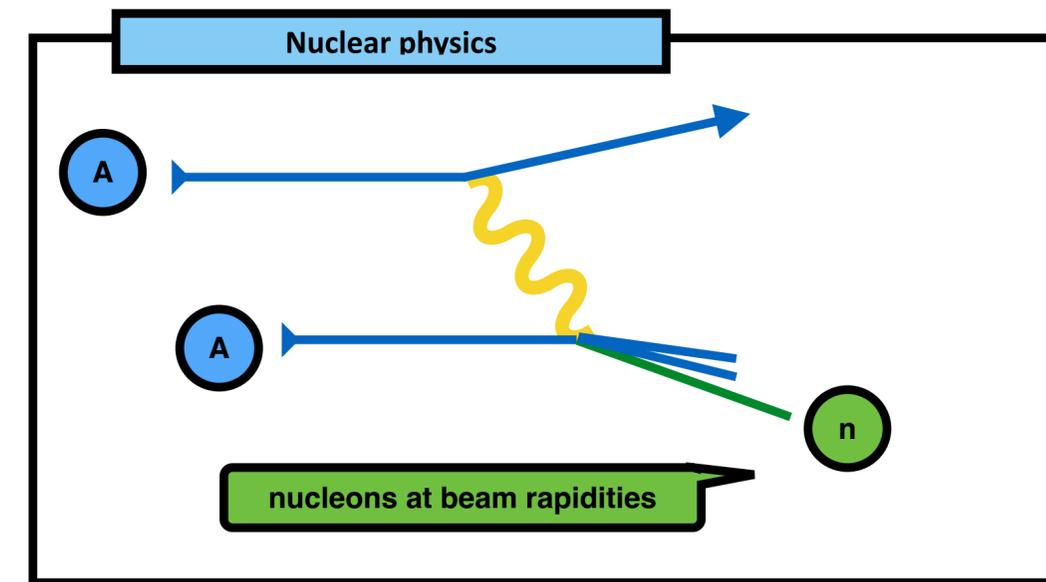
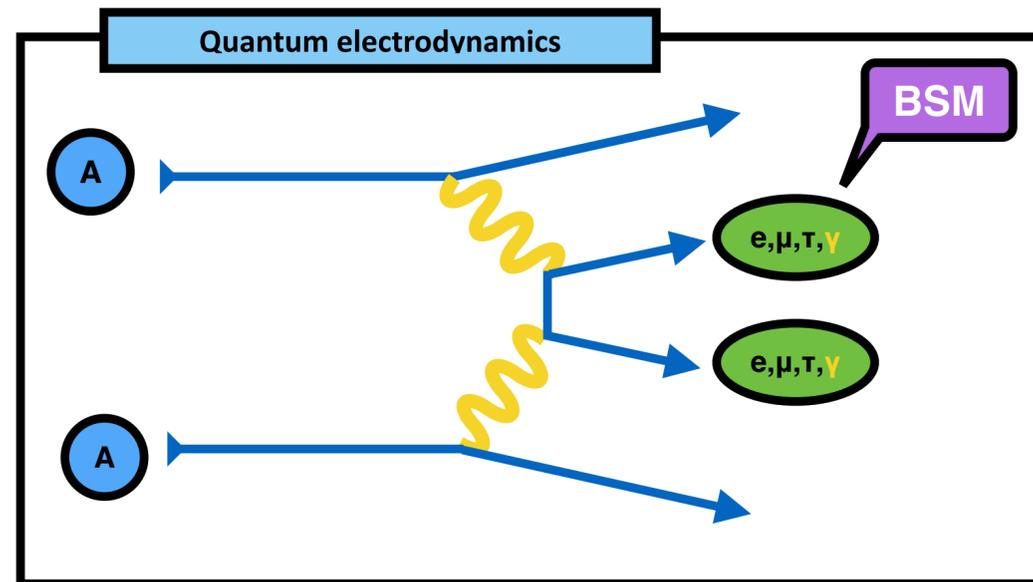
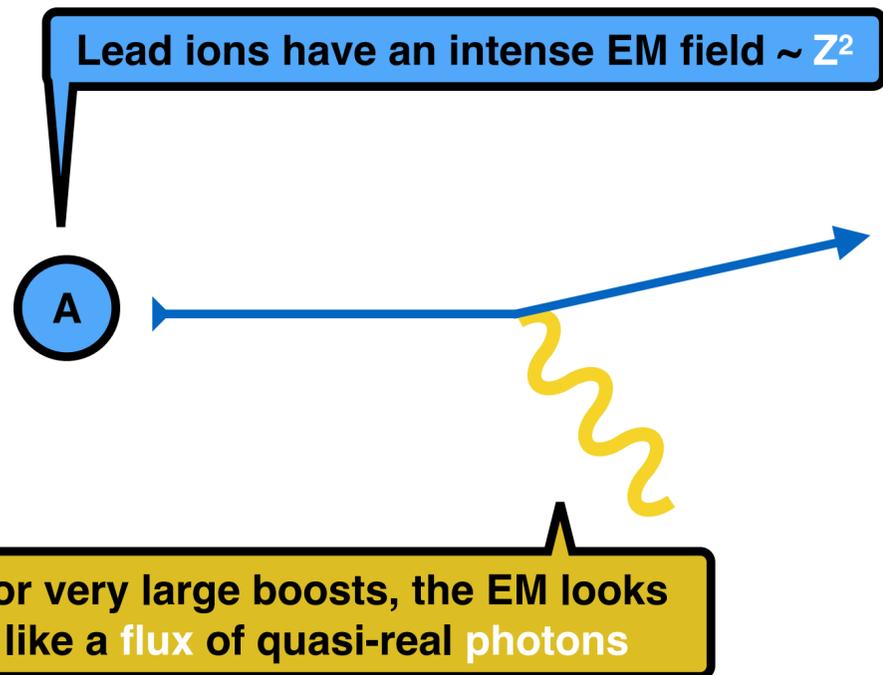
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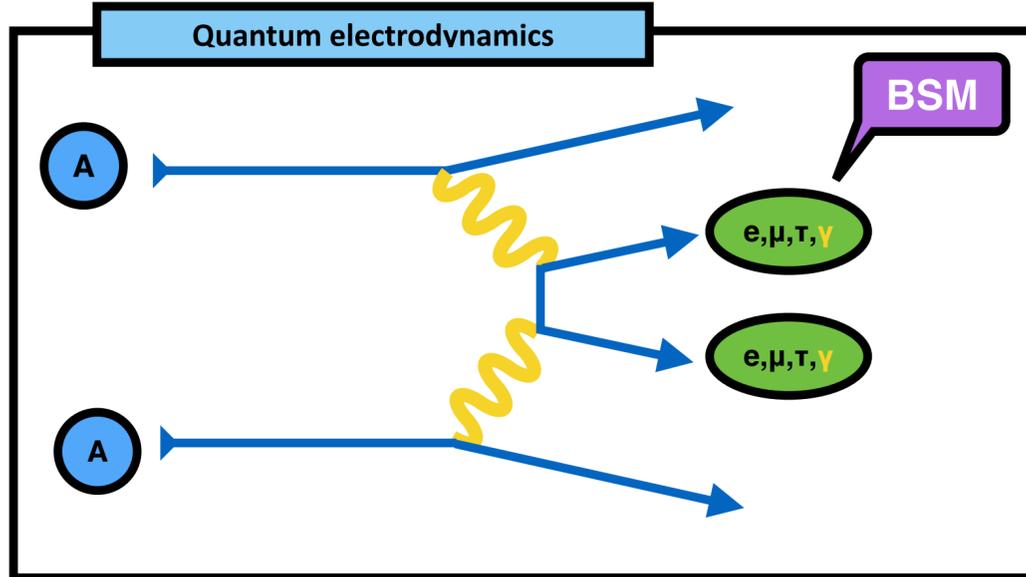
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Lead ions have an intense EM field  $\sim Z^2$

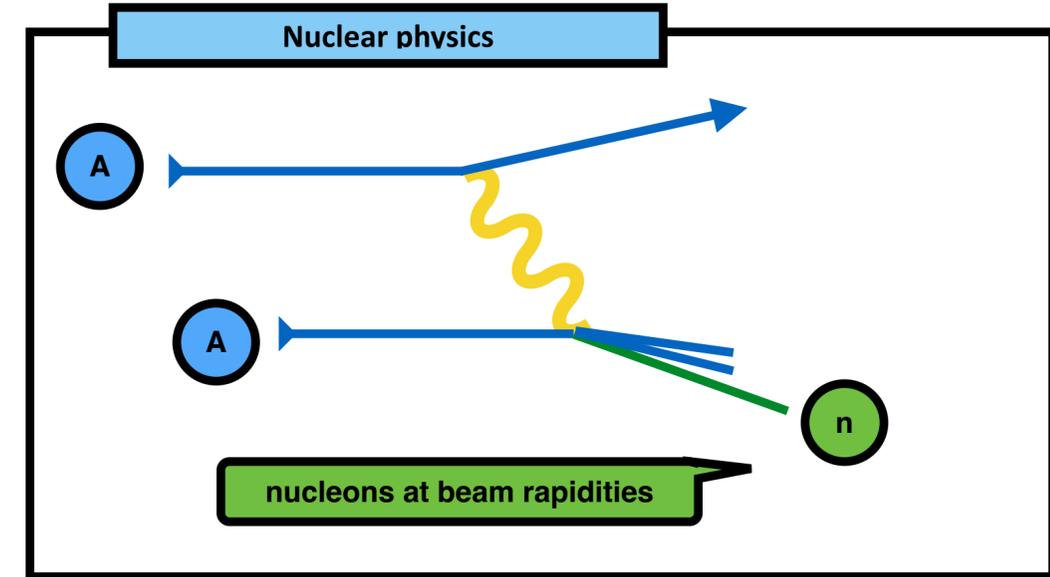


For very large boosts, the EM looks like a flux of quasi-real photons

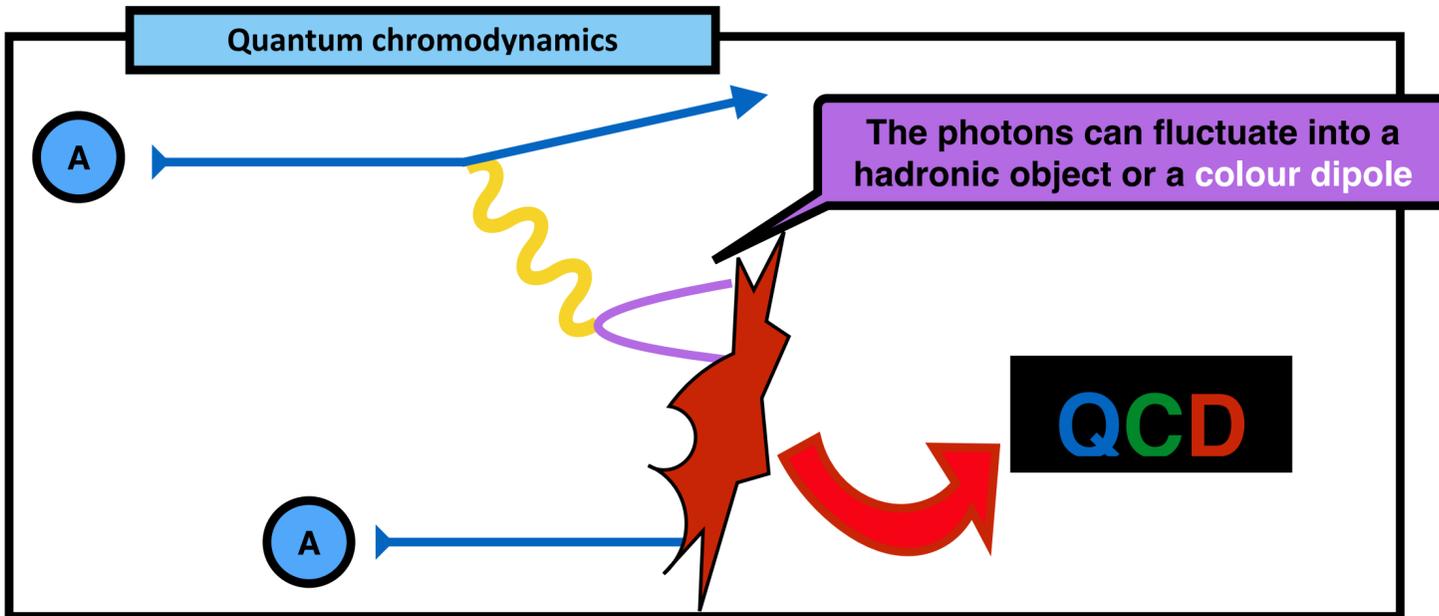
Quantum electrodynamics



Nuclear physics

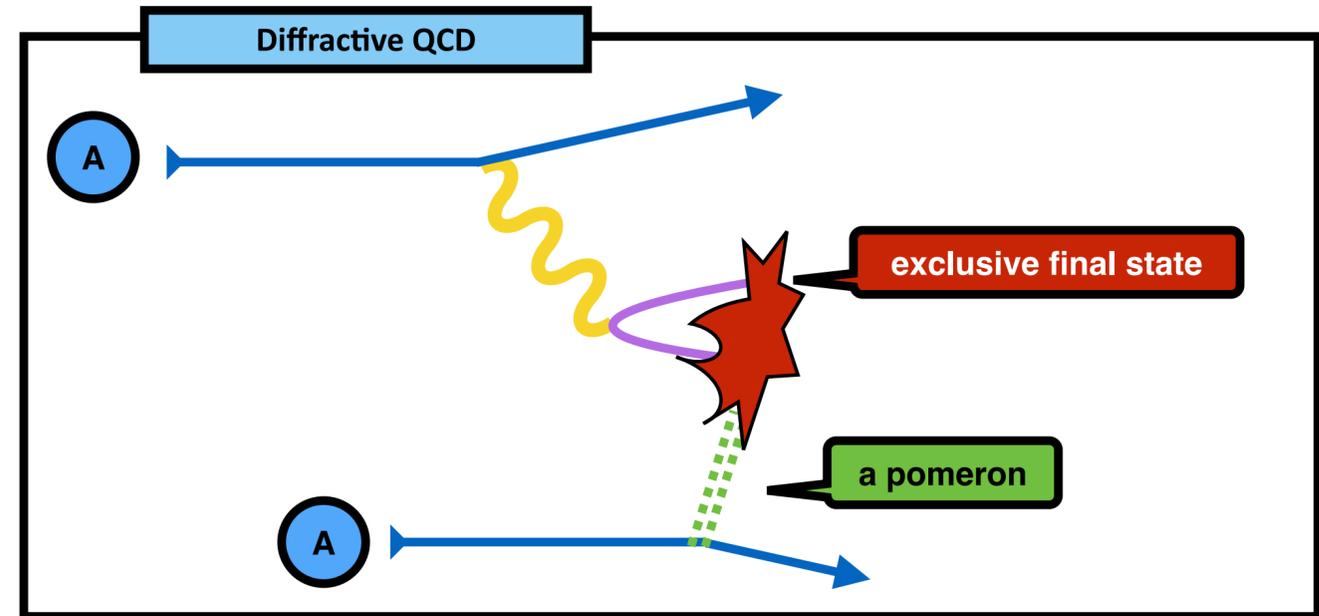


Quantum chromodynamics

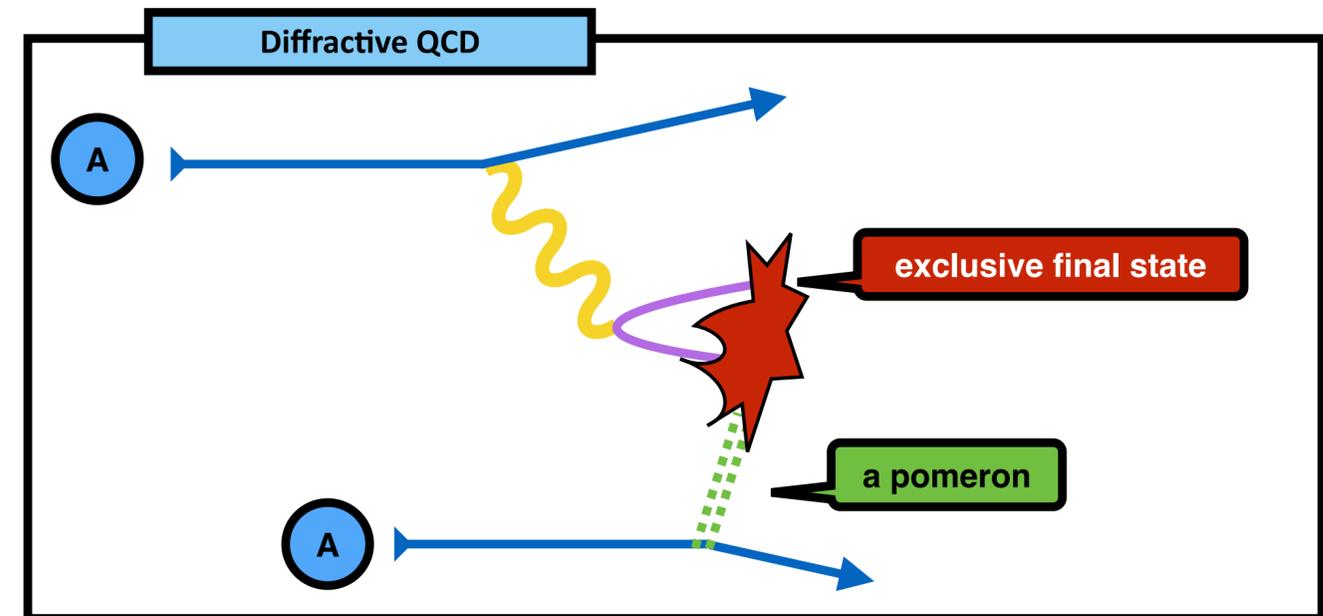
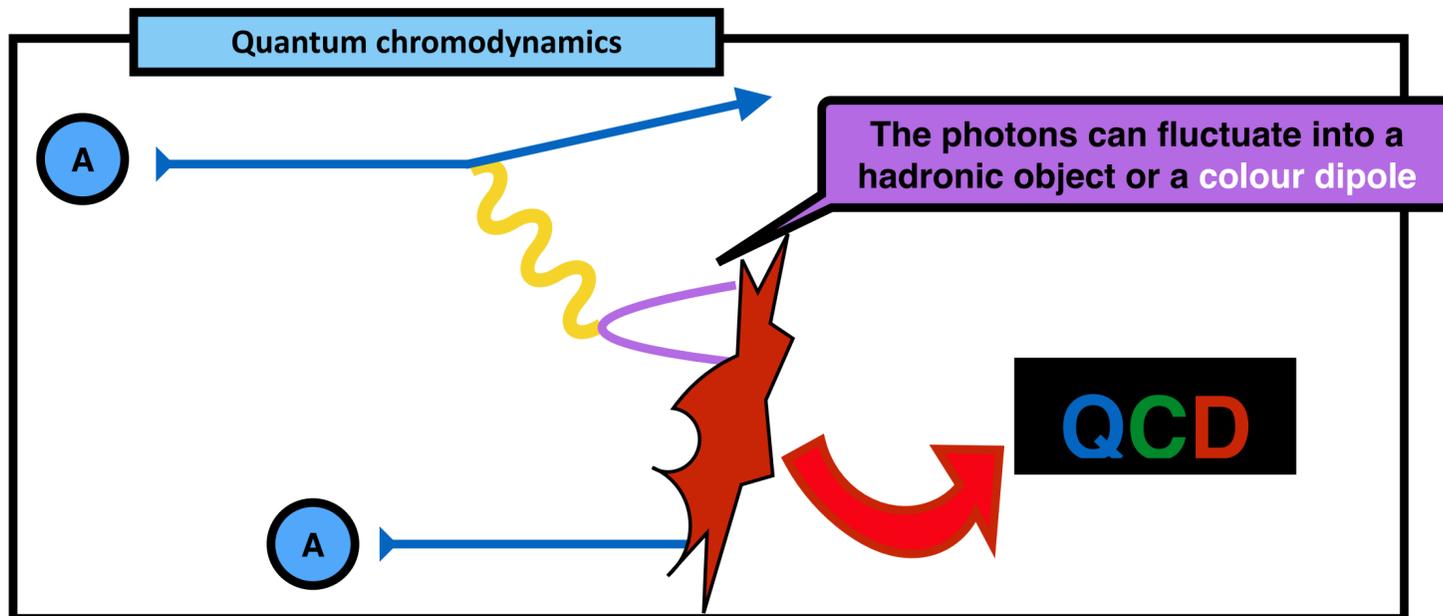
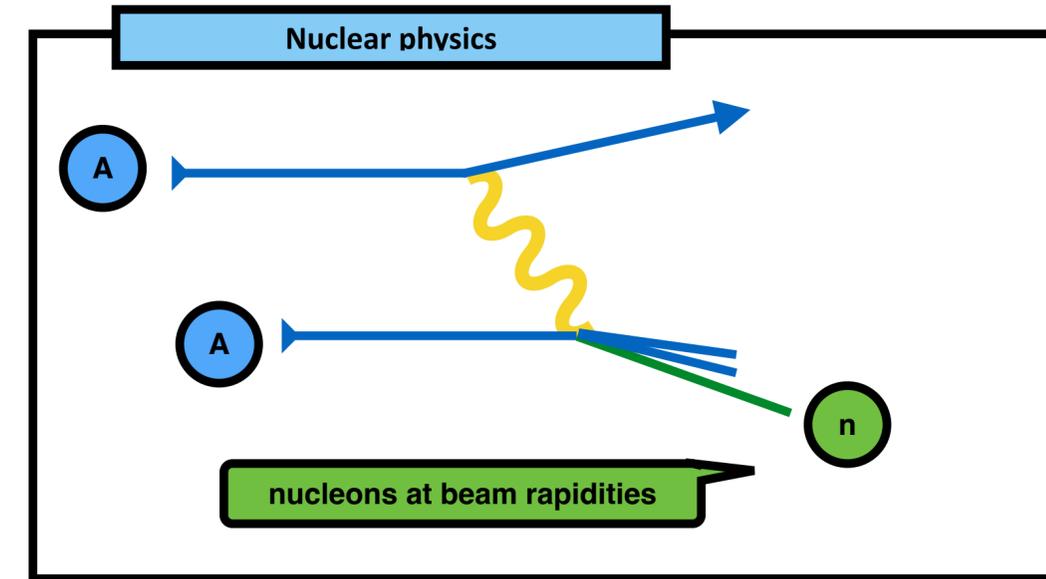
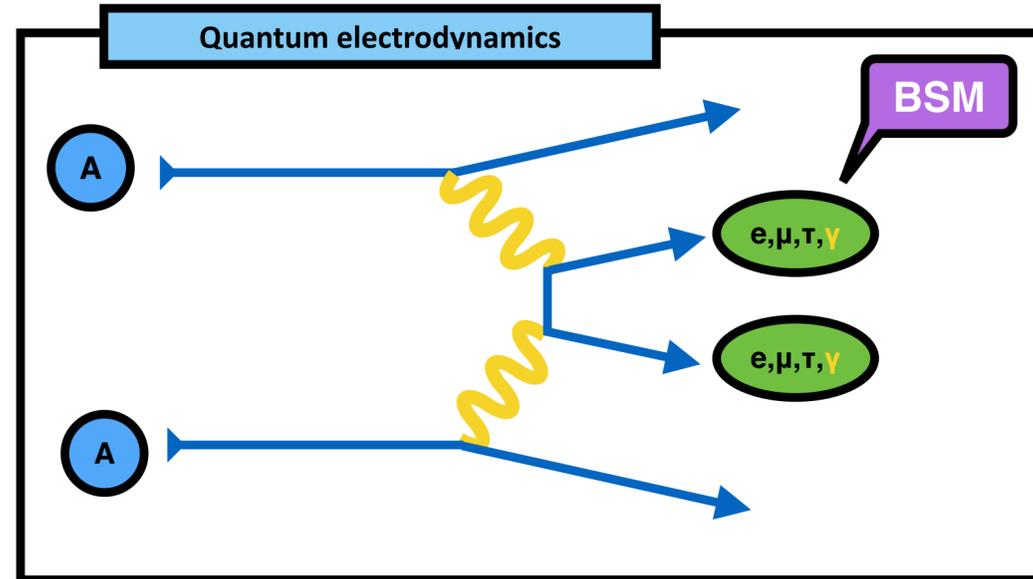
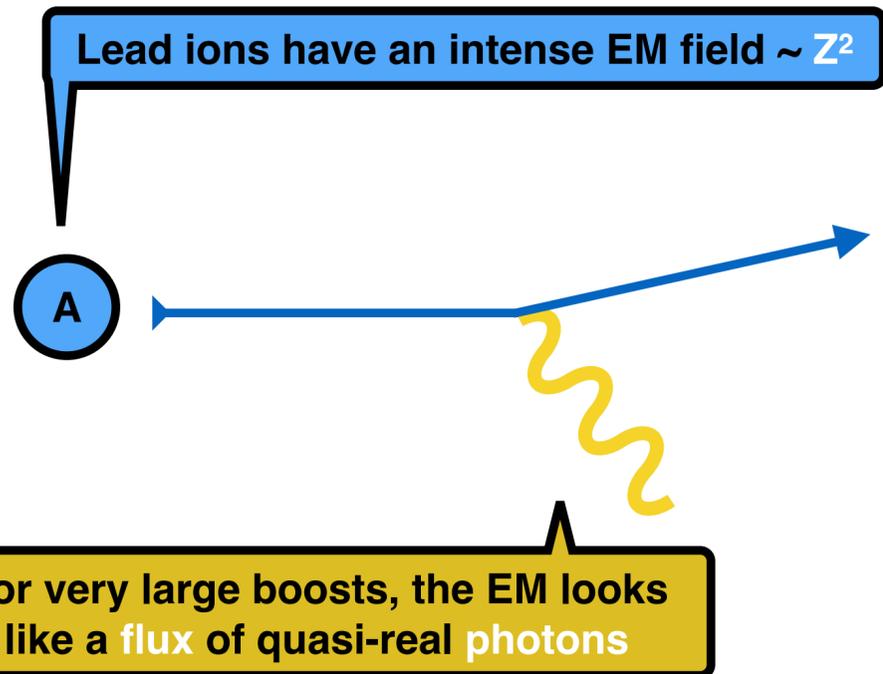


The photons can fluctuate into a hadronic object or a colour dipole

Diffractive QCD



# Photons at the ion colliders: examples of what can be done



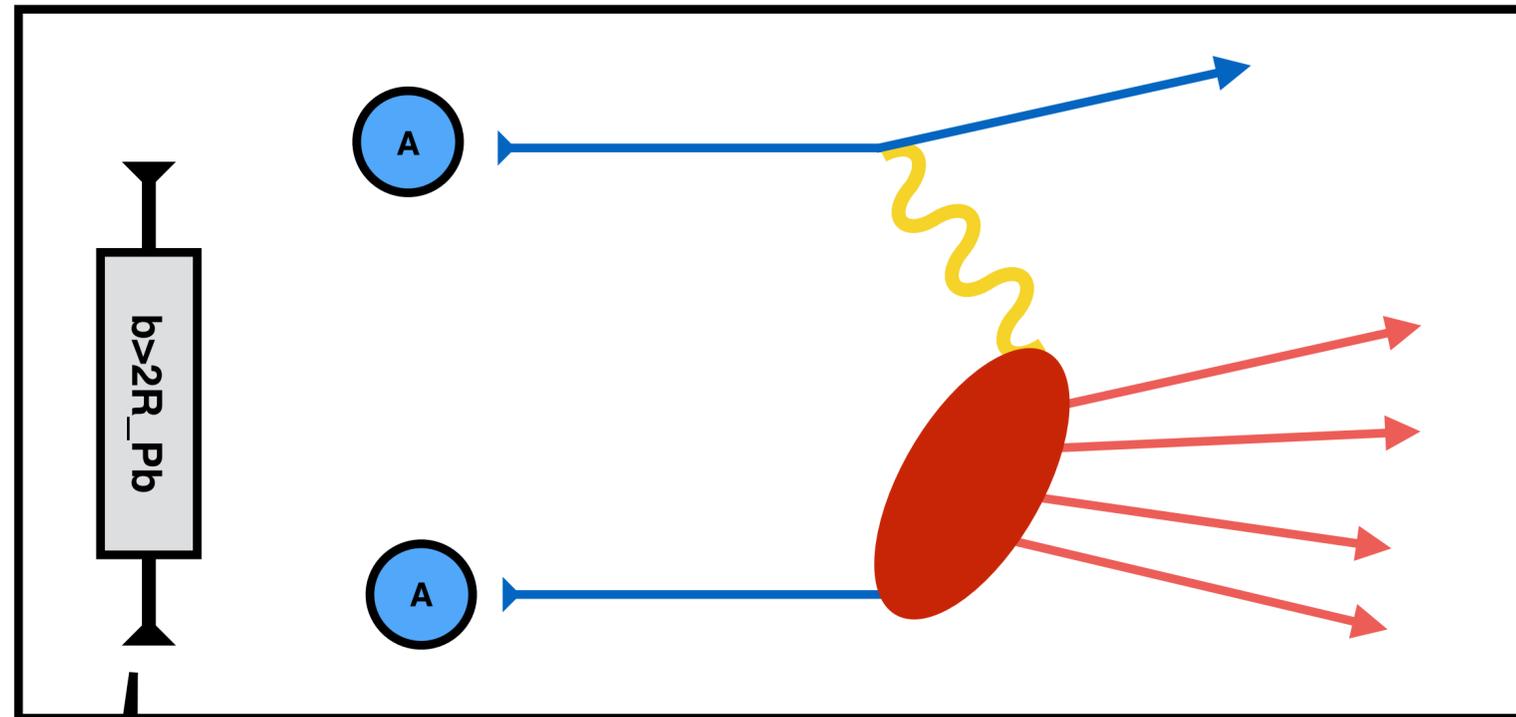
Finding these processes in hadron colliders requires specific search techniques tailored to the environment and the available detectors

# How to find photon-induced interactions in hadron colliders (1/4)

For inclusive observables one has to use ultra-peripheral collisions (UPC)

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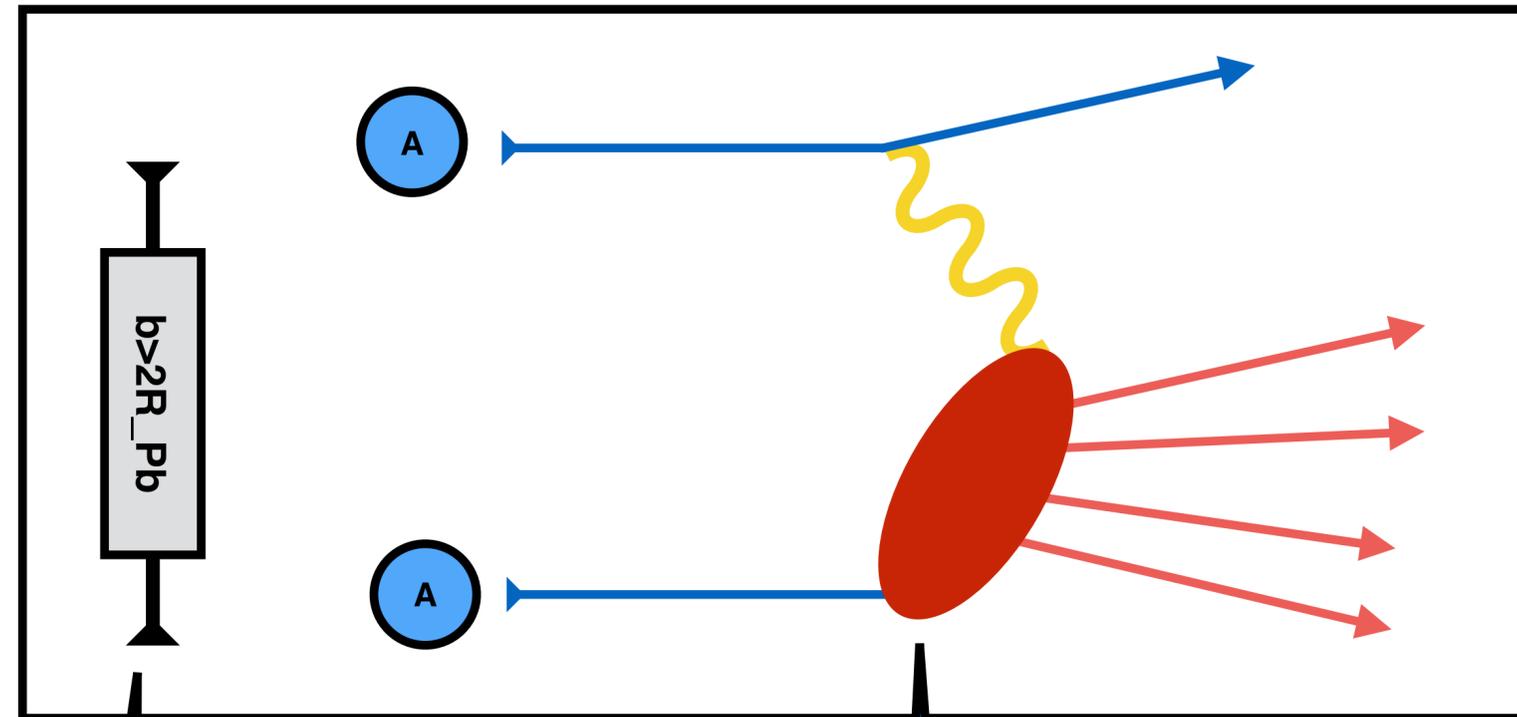
For inclusive observables one has to use ultra-peripheral collisions (UPC)



Choose interactions at large impact parameters

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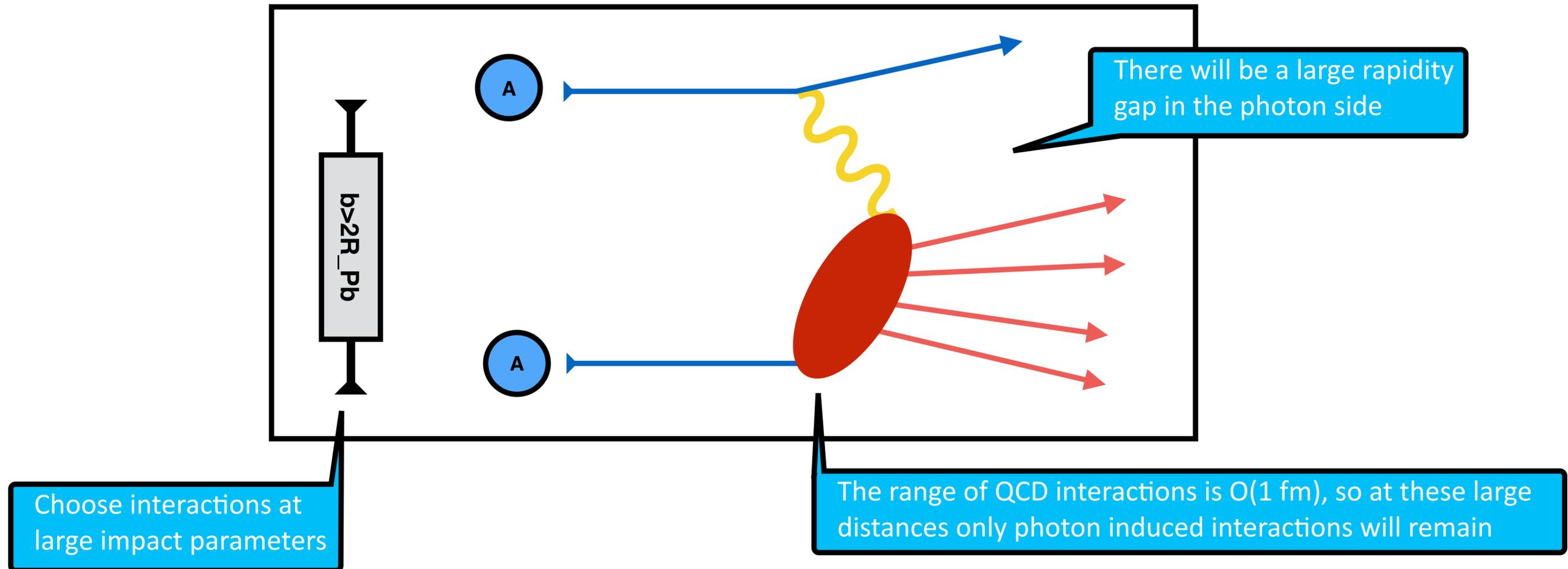


Choose interactions at large impact parameters

The range of QCD interactions is  $O(1 \text{ fm})$ , so at these large distances only photon induced interactions will remain

# How to find photon-induced interactions in hadron colliders (1/4)

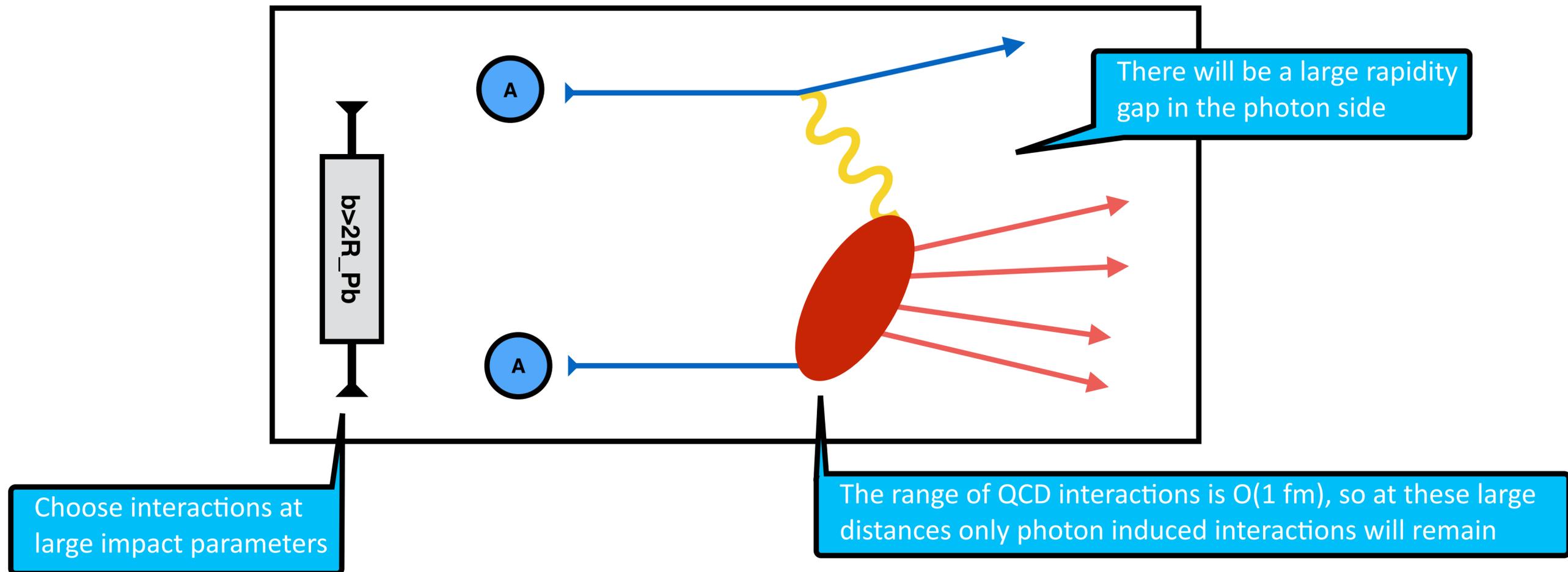
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# How to find photon-induced interactions in hadron colliders (1/4)

For inclusive observables one has to use ultra-peripheral collisions (UPC)

Signature: Look for a large rapidity gap in one side of the detector

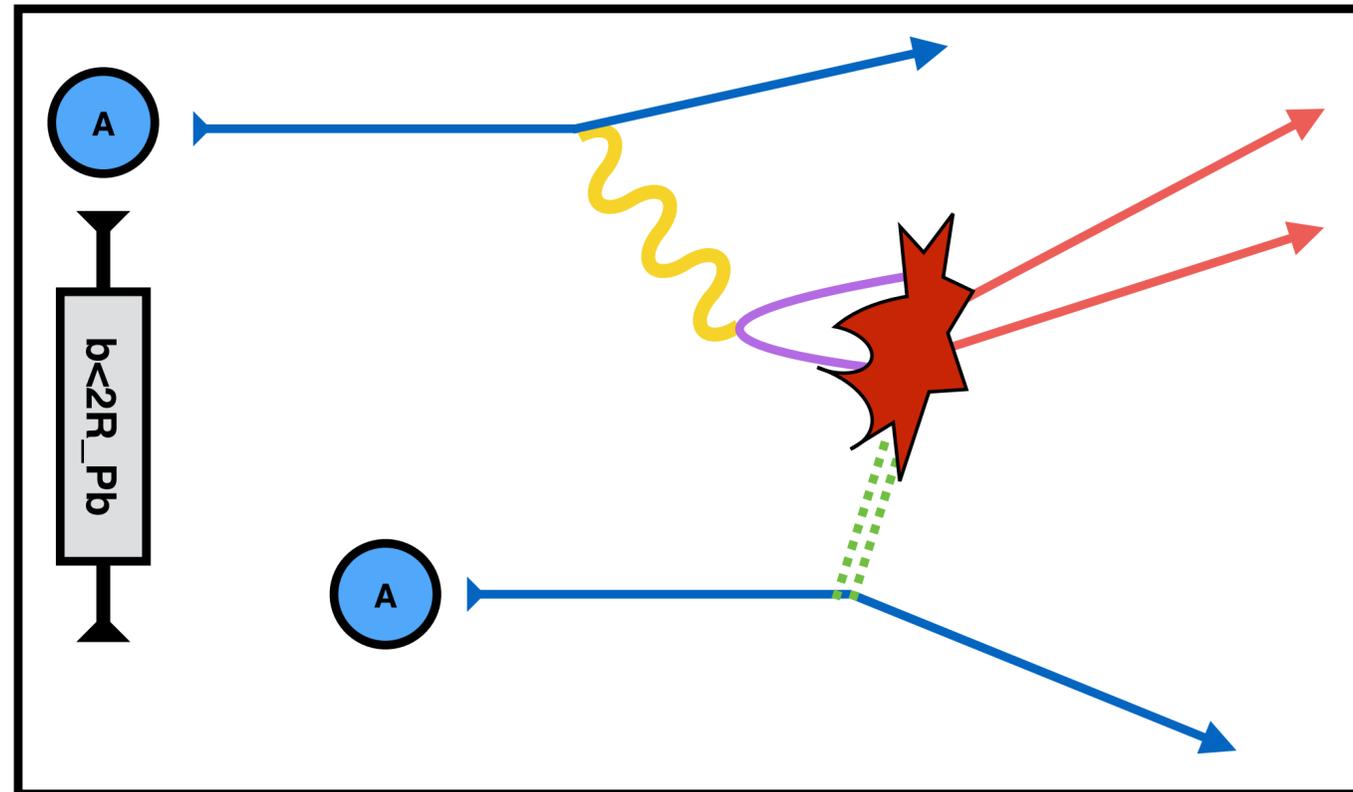


# How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions

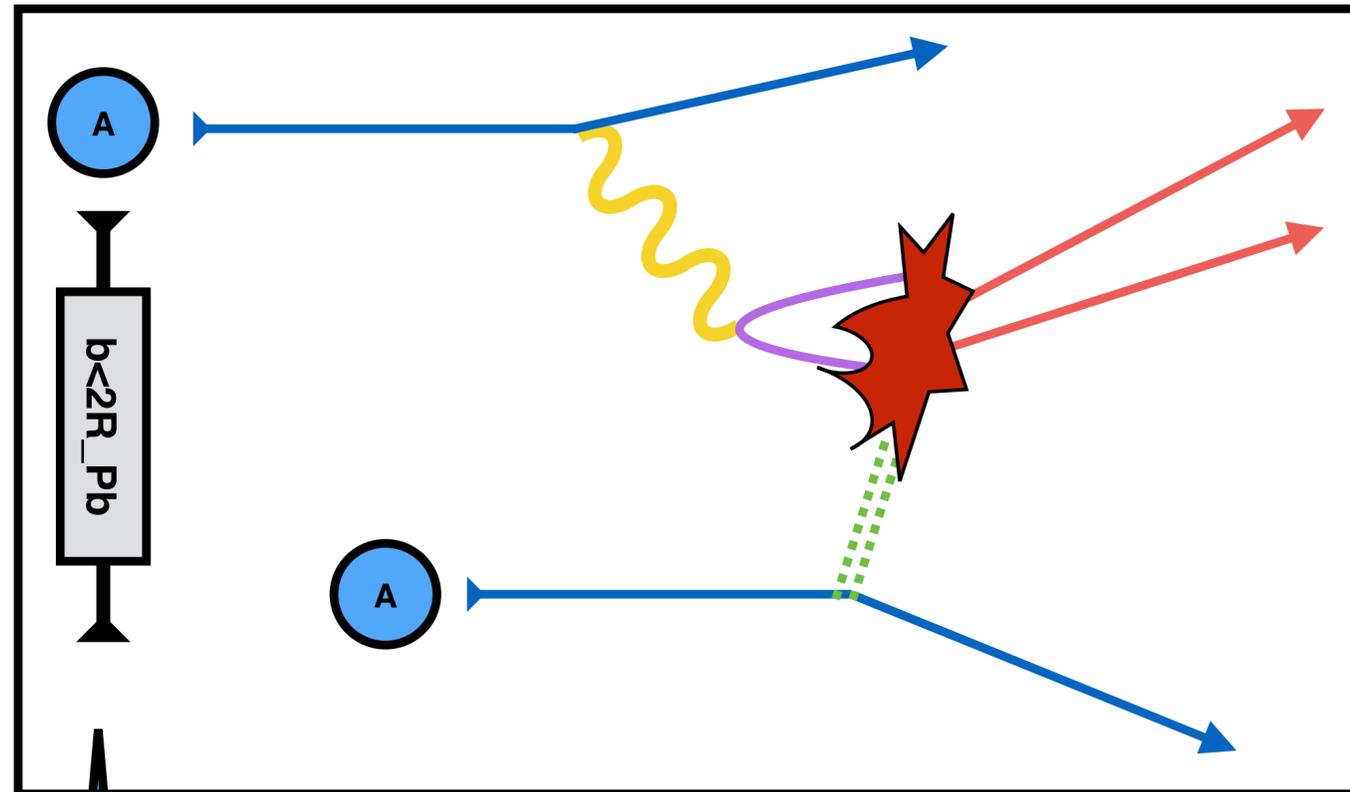
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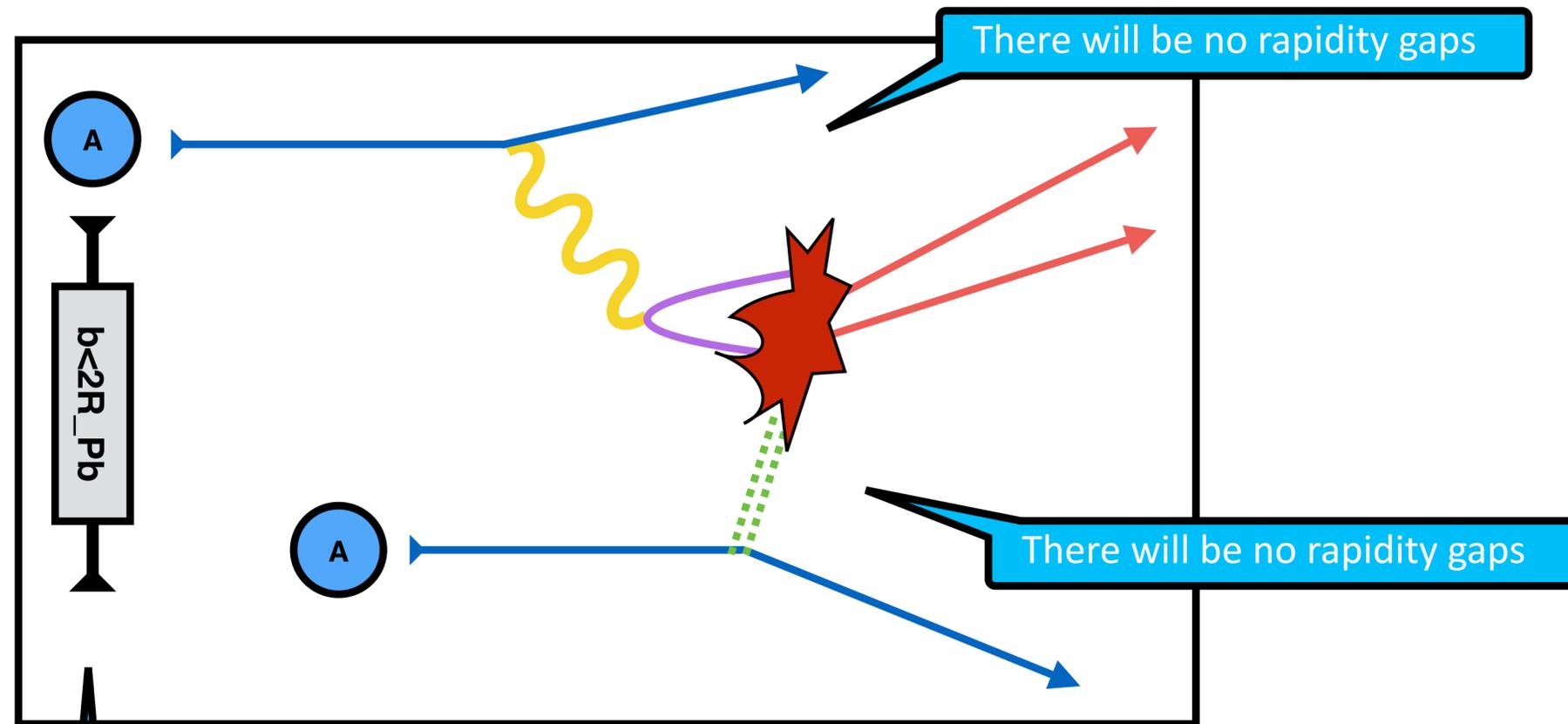
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For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

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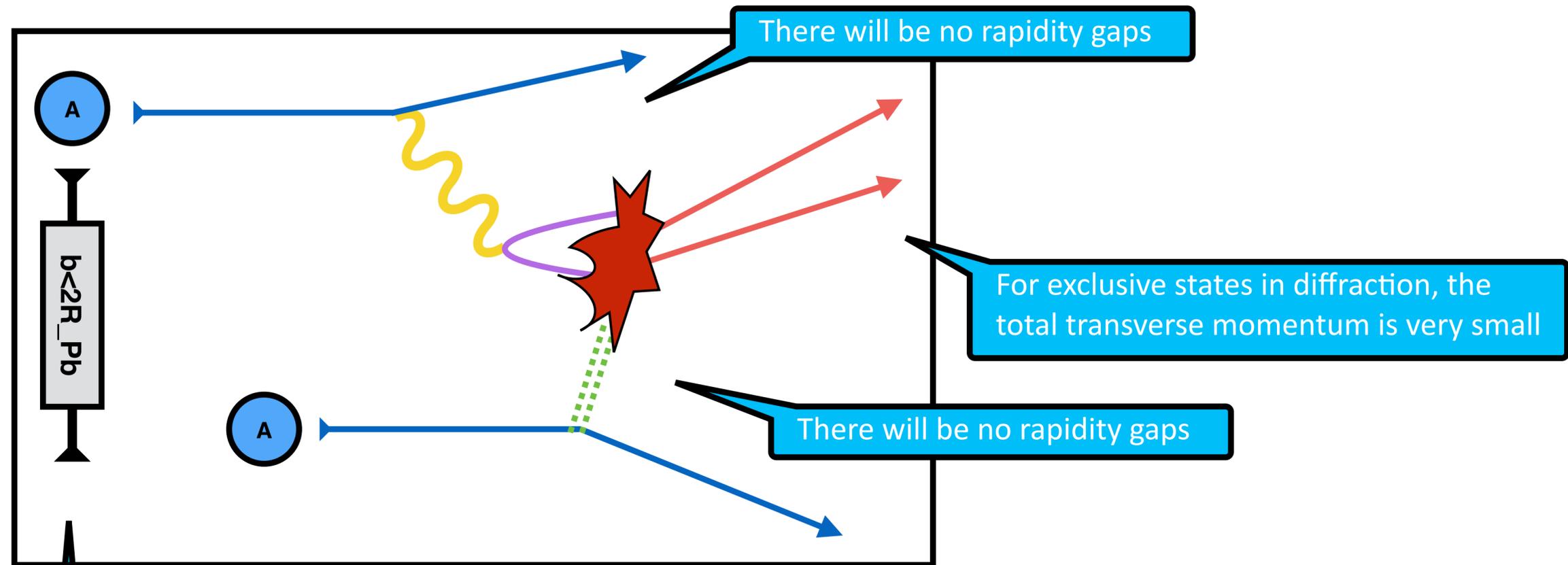
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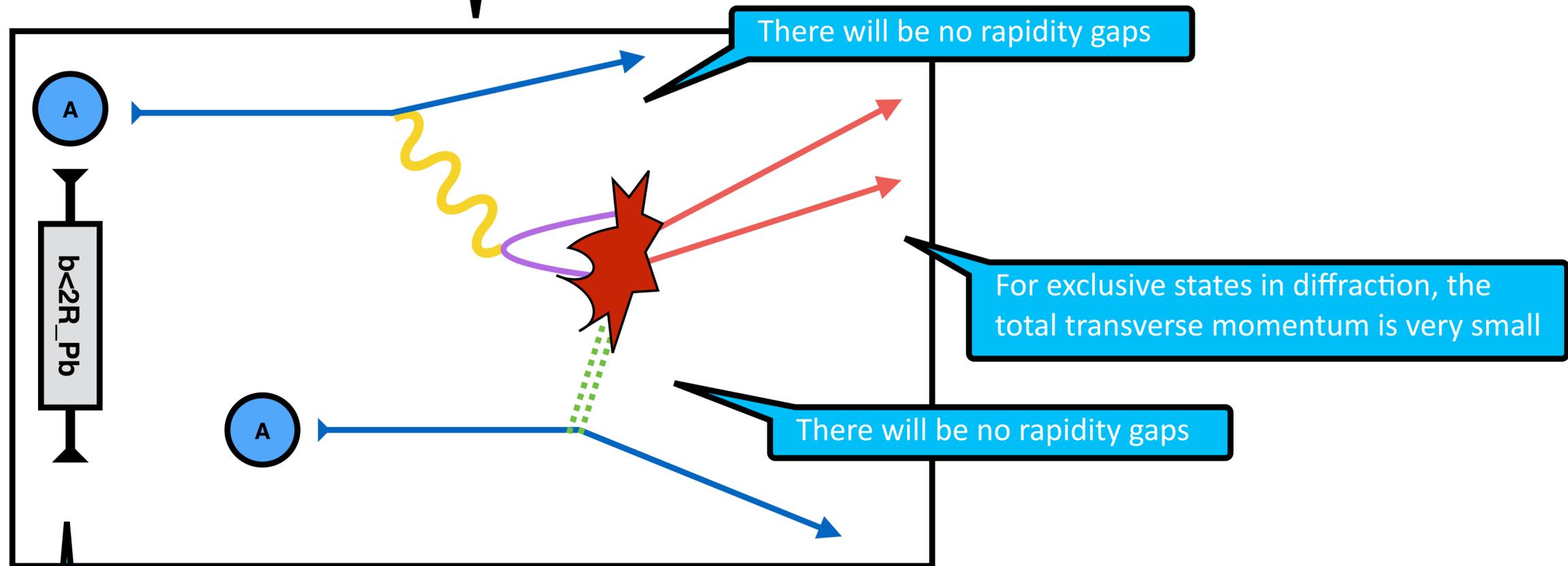


For peripheral collisions the photon-induced process will overlap with hadronic inelastic interactions

# How to find photon-induced interactions in hadron colliders (2/4)

For exclusive diffractive observables, one can use peripheral collisions

Signature: Look for a low  $p_T$  final state (eg. a dijet or a vector meson)



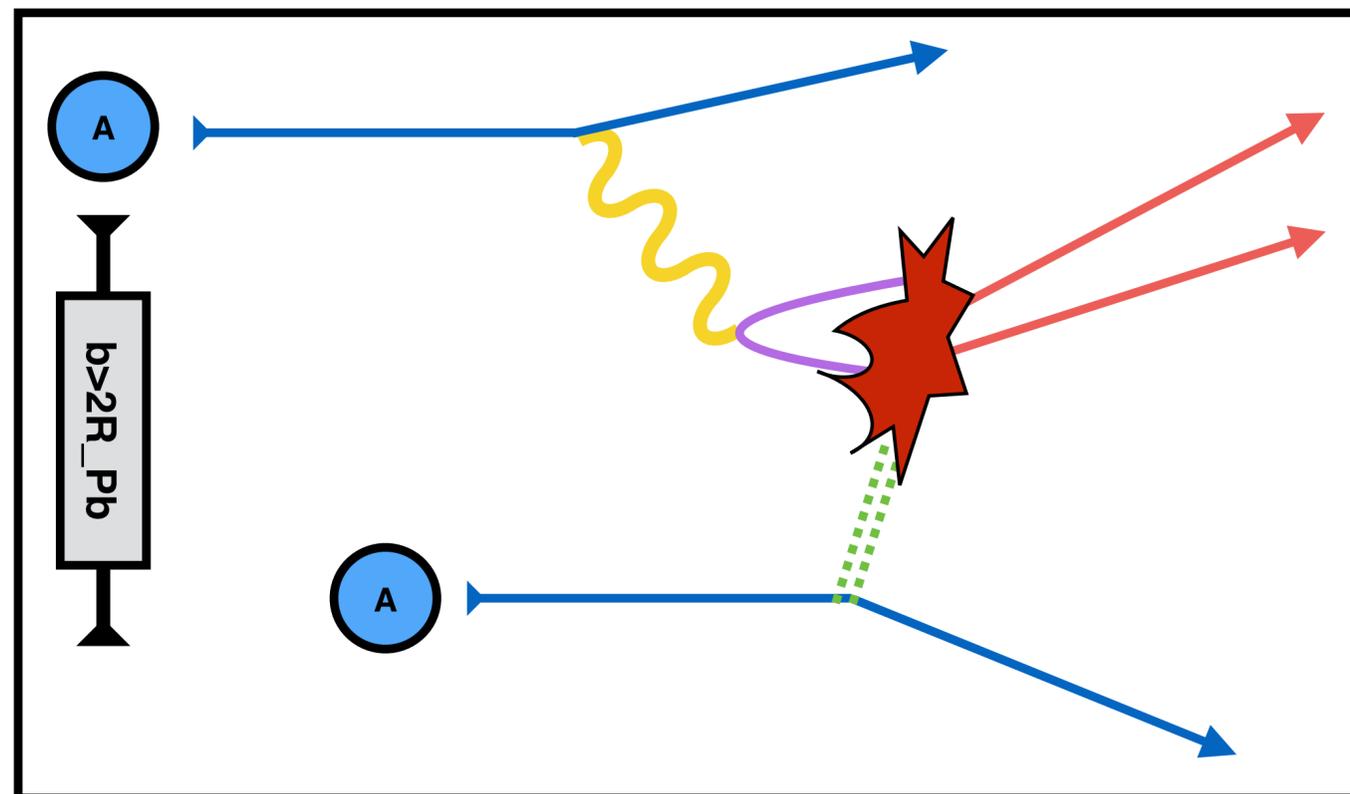
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# How to find photon-induced interactions in hadron colliders (3/4)

For exclusive diffractive observables, one can also use UPC

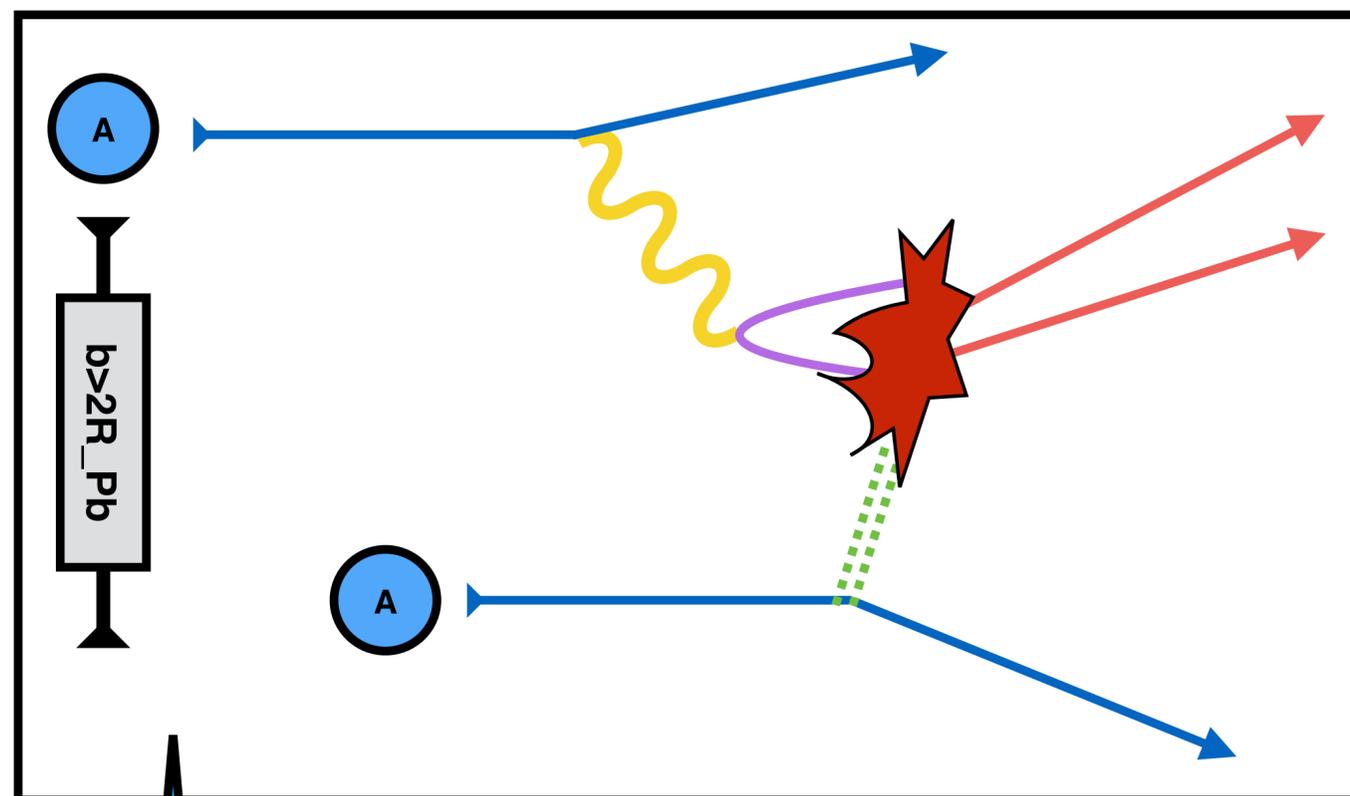
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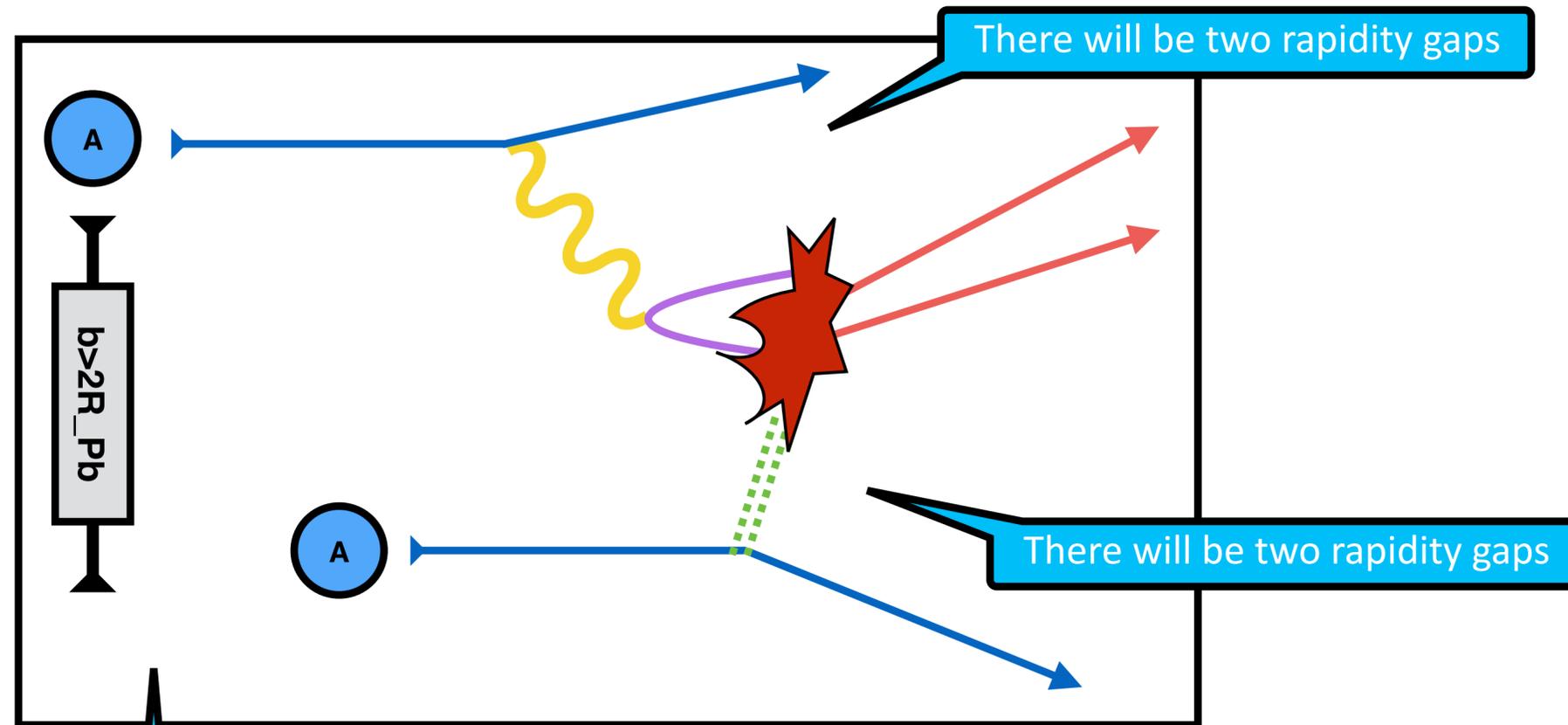
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For UPC the photon-induced process there is no overlap of the incoming hadrons within the range of QCD

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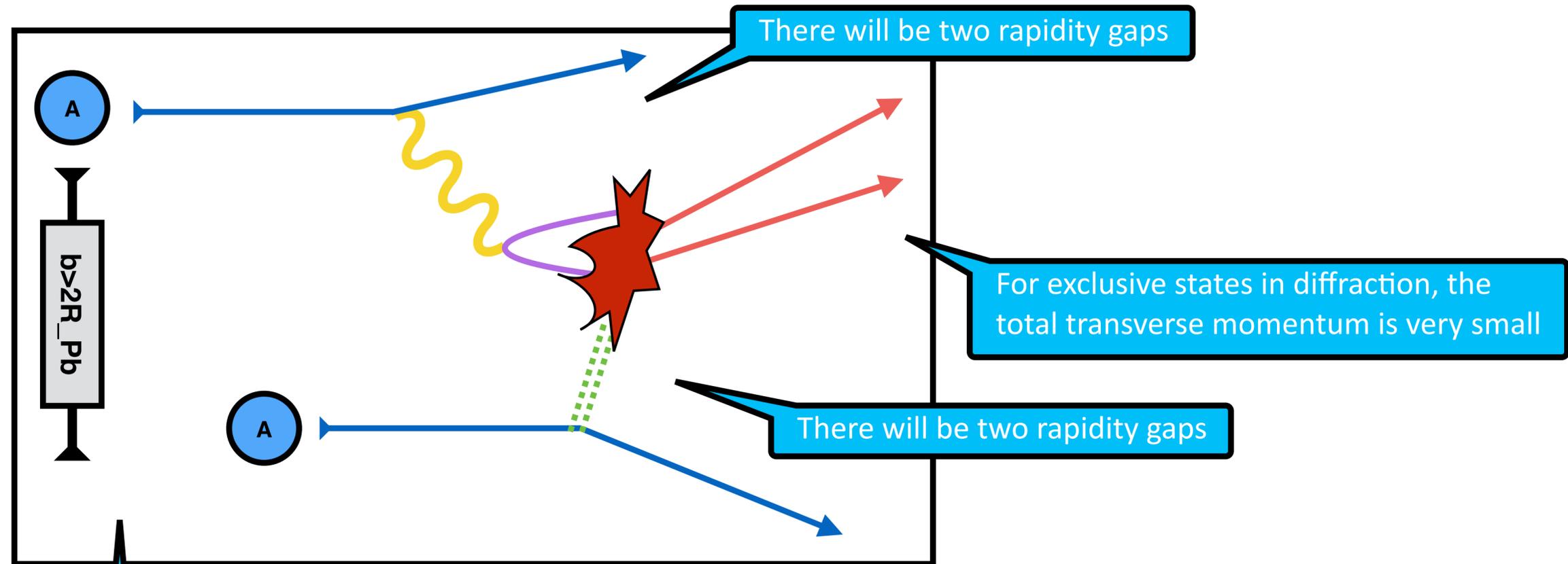
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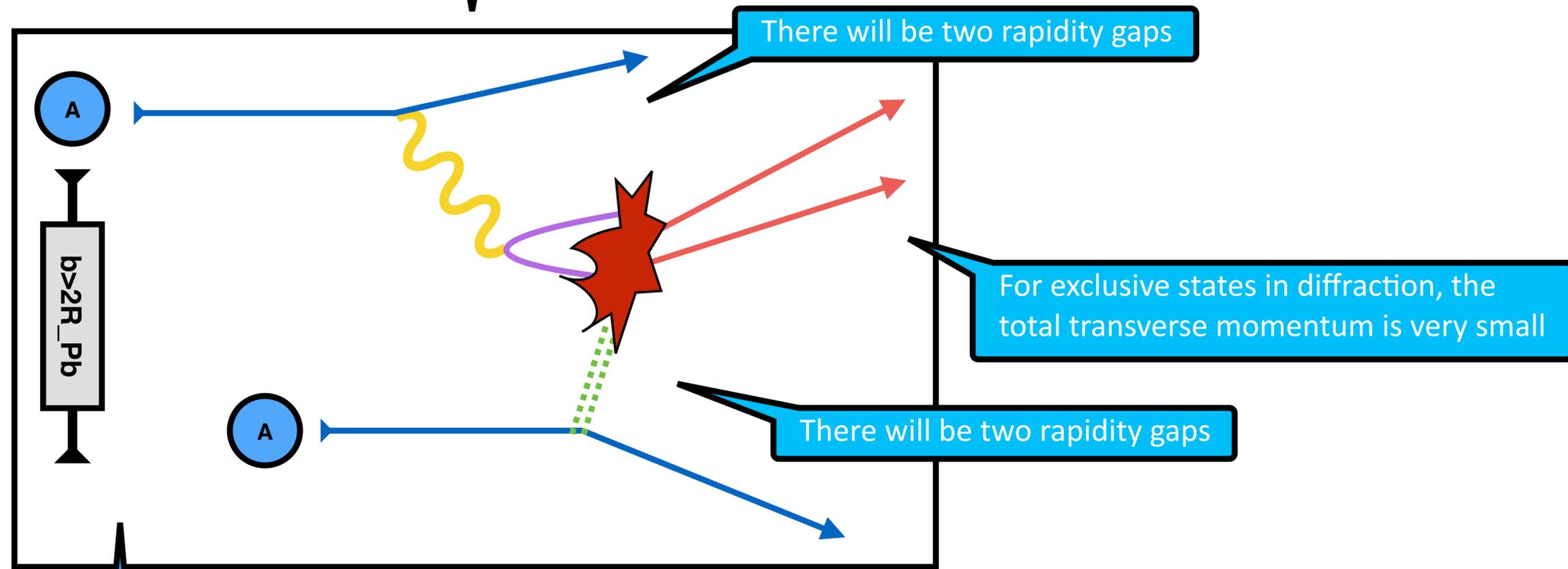


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# How to find photon-induced interactions in hadron colliders (3/4)

For exclusive diffractive observables, one can also use UPC

Signature: Look for a low  $p_T$  final state (eg. a dijet or a vector meson) in an otherwise empty detector



For UPC the photon-induced process there is no overlap of the incoming hadrons within the range of QCD

Imposing conditions to select events may select a subset of the total flux  
Let's look at two variations of the flux formalism to account for this effect:  
Selecting UPC coherent processes  
Selecting EMD processes

# The photon flux in coherent UPC according to STARlight

Use a Glauber description of the target to ensure the absence of hadronic inelastic collisions

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$$n^U(y) = k \int_0^\infty db 2\pi b P_{NH}(b) \int_0^{r_A} \frac{r dr}{\pi r_A^2} \int_0^{2\pi} d\phi n(k, b + r \cos(\phi))$$

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Position in the target

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Rapidity of the final state

$$k = \frac{M}{2} e^y$$

Average over all possible positions in the target

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Photon energy

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Use a Glauber description of the target to ensure the absence of hadronic inelastic collisions

In a Poissonian model

$$P_{NH}(b) = \exp(-T_{AA}\sigma_{NN})$$

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$$P_{NH}(b) = \exp(-T_{AA}\sigma_{NN})$$

cross section of a nucleon-nucleon inelastic hadronic interaction

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Nucleus-nucleus interaction probability

$$T_{AA}(|\vec{b}|) = \int d^2\vec{r} T_A(\vec{r}) T_A(\vec{r} - \vec{b})$$

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Rapidity of the final state

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Probability of no inelastic hadronic interactions at this impact parameter

Average over all possible positions in the target

Flux

Position in the target

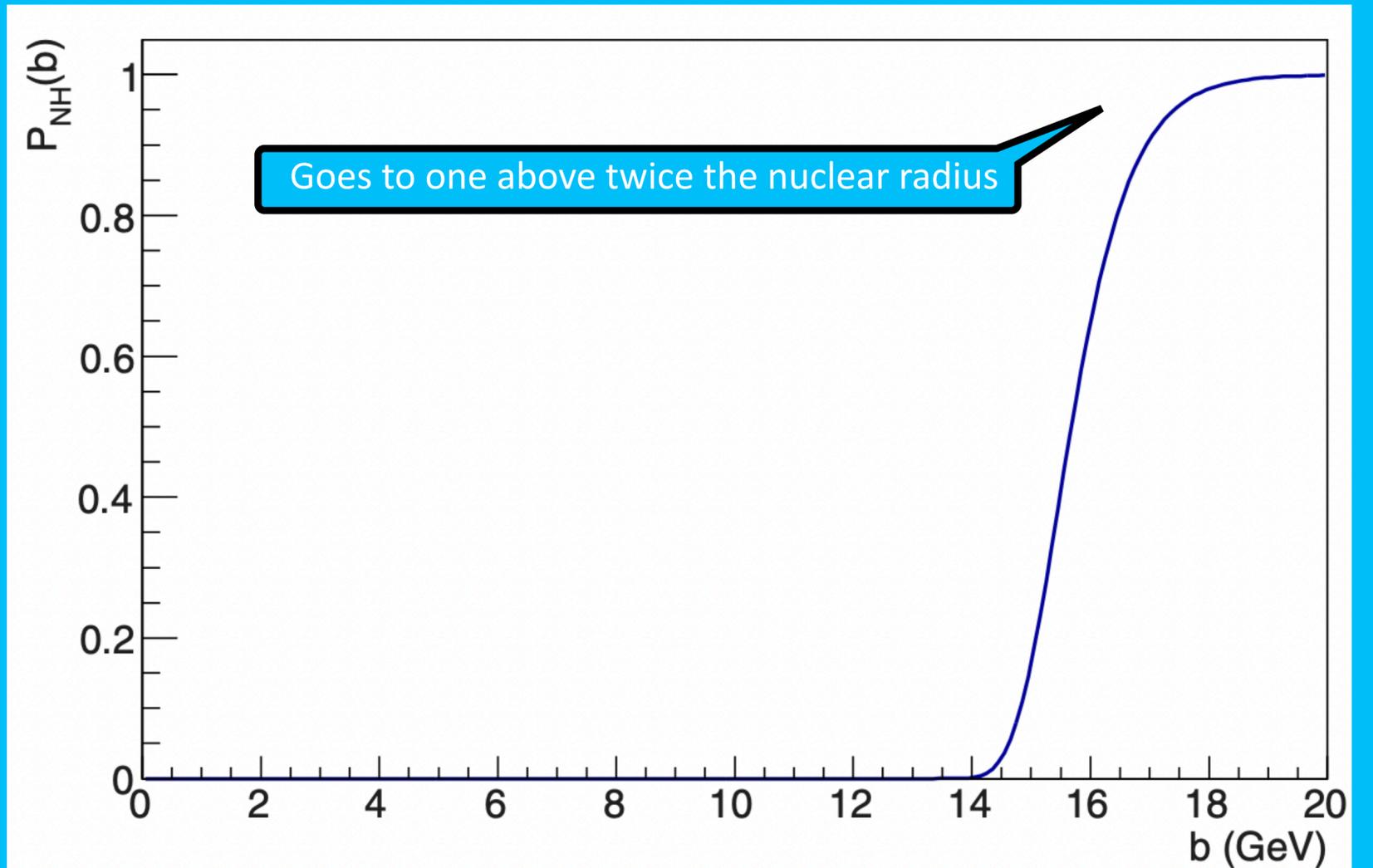
impact parameter

Homework:

try to implement these formulas

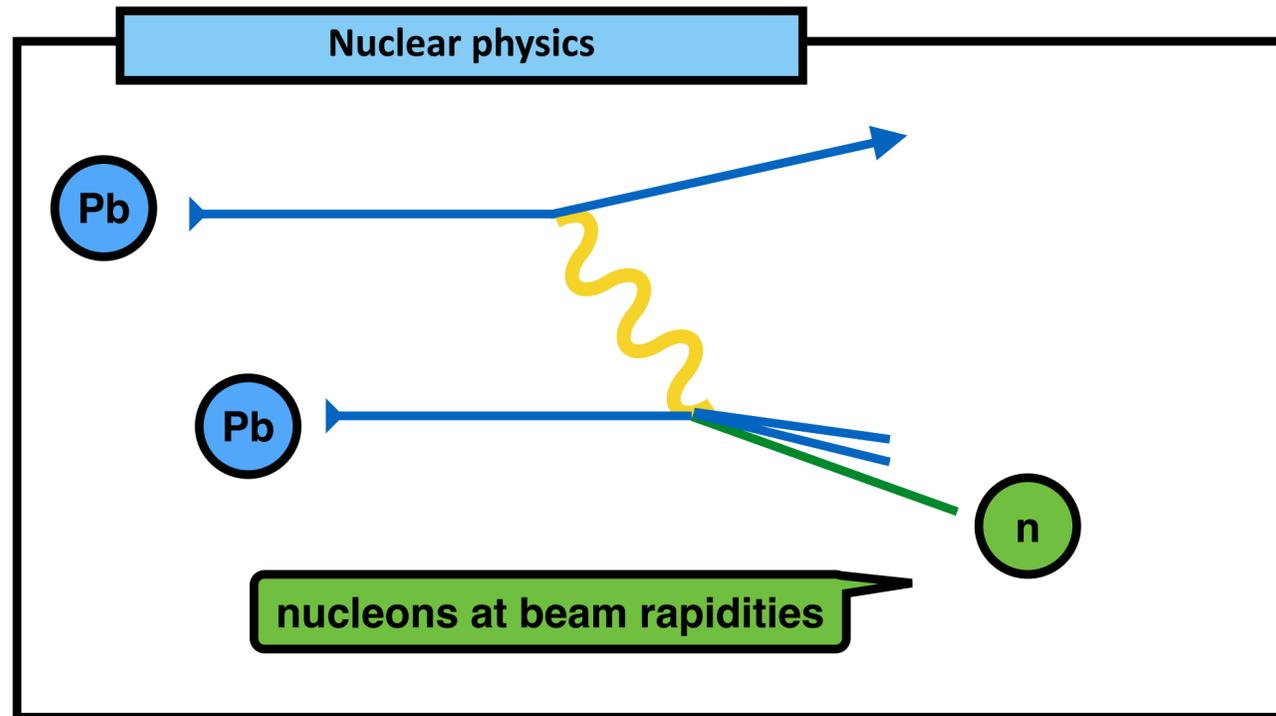
# Probability of no inelastic hadronic interaction

Probability of no hadronic inelastic interaction for Pb-Pb collisions

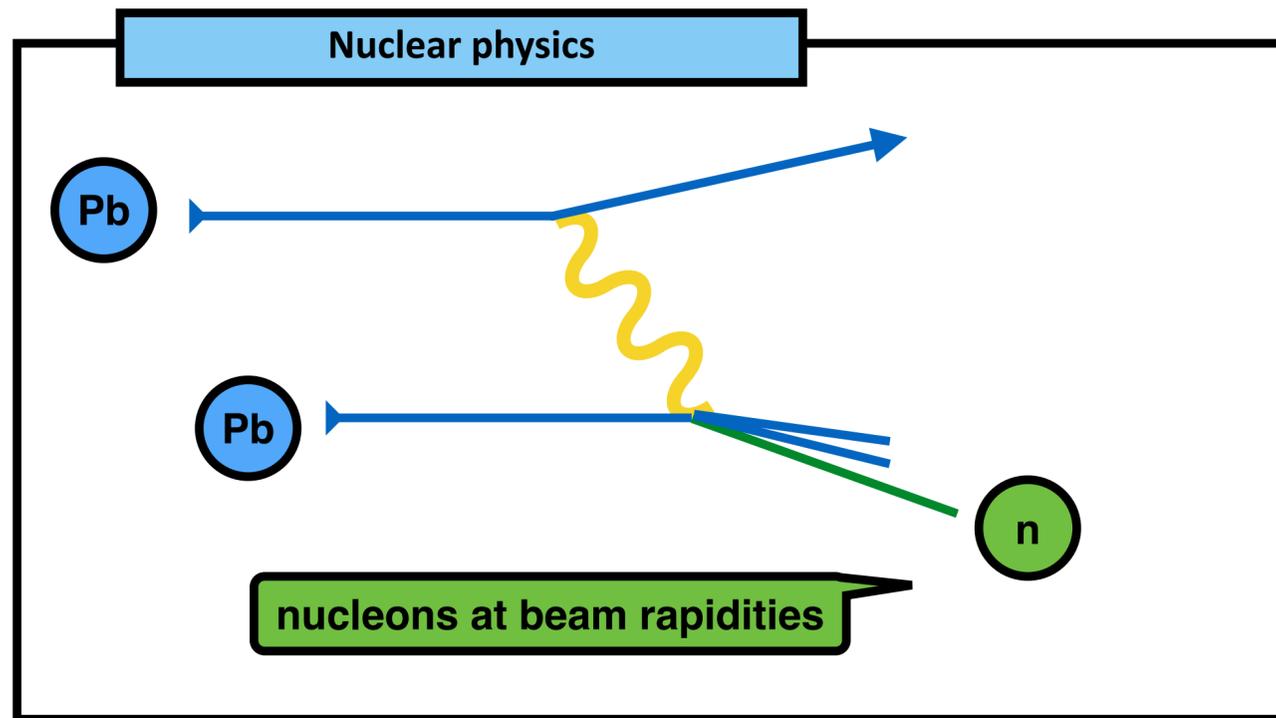


$$n^U(y) = k \int_0^\infty db 2\pi b P_{NH}(b) \int_0^{r_A} \frac{r dr}{\pi r_A^2} \int_0^{2\pi} d\phi n(k, b + r \cos(\phi))$$

# Electromagnetic dissociation (EMD)

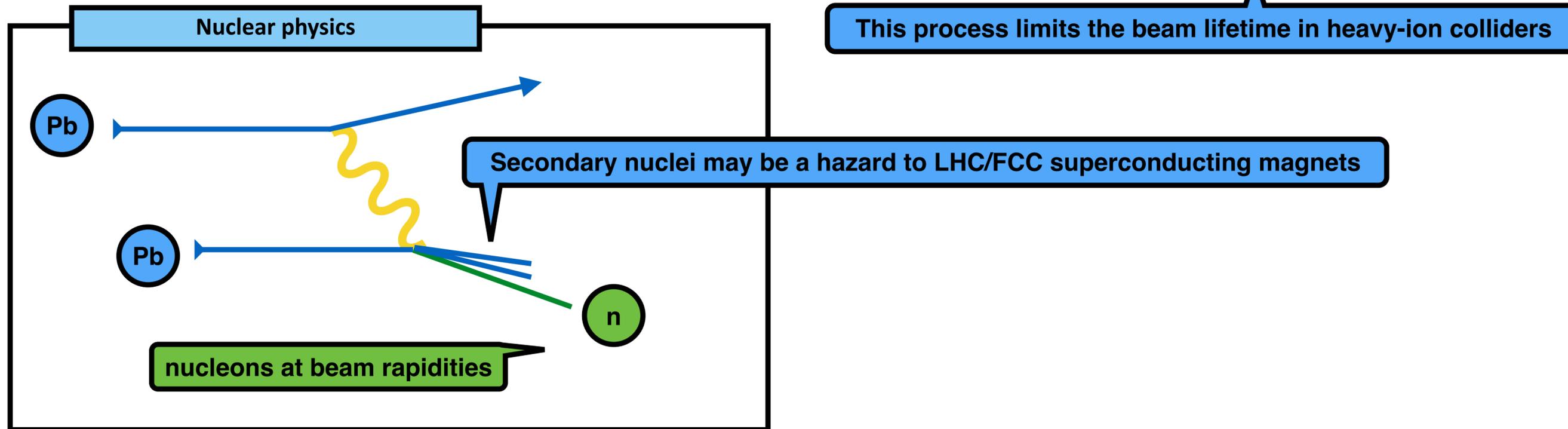


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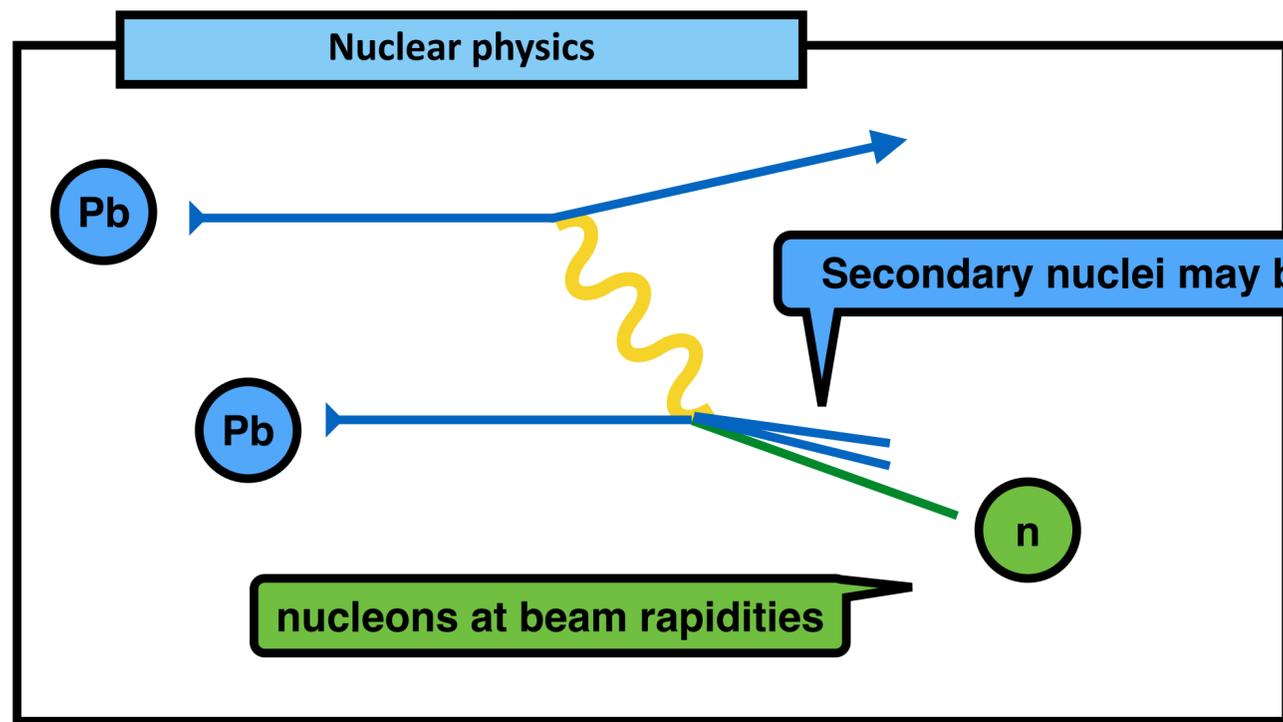


This process limits the beam lifetime in heavy-ion colliders

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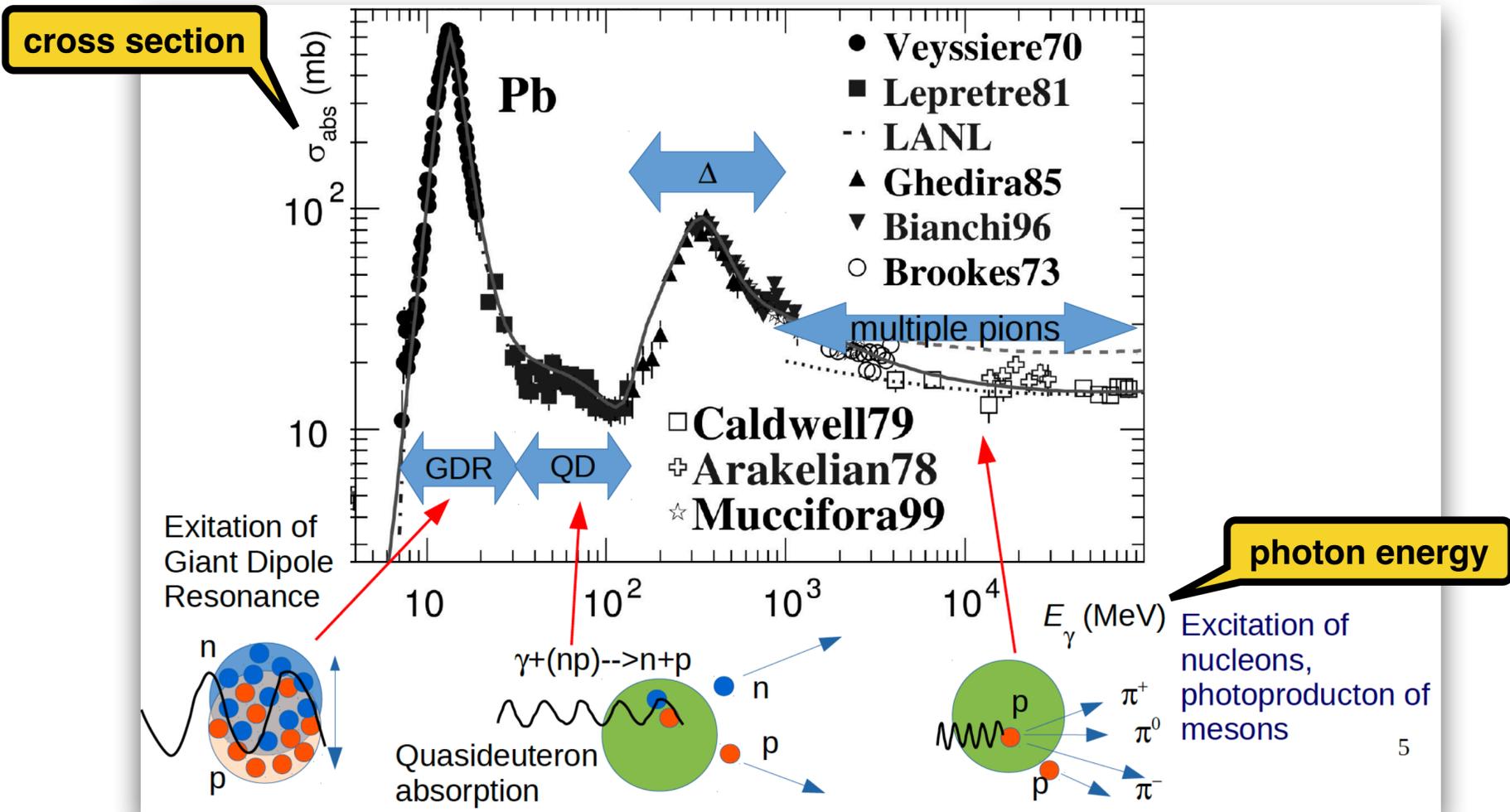
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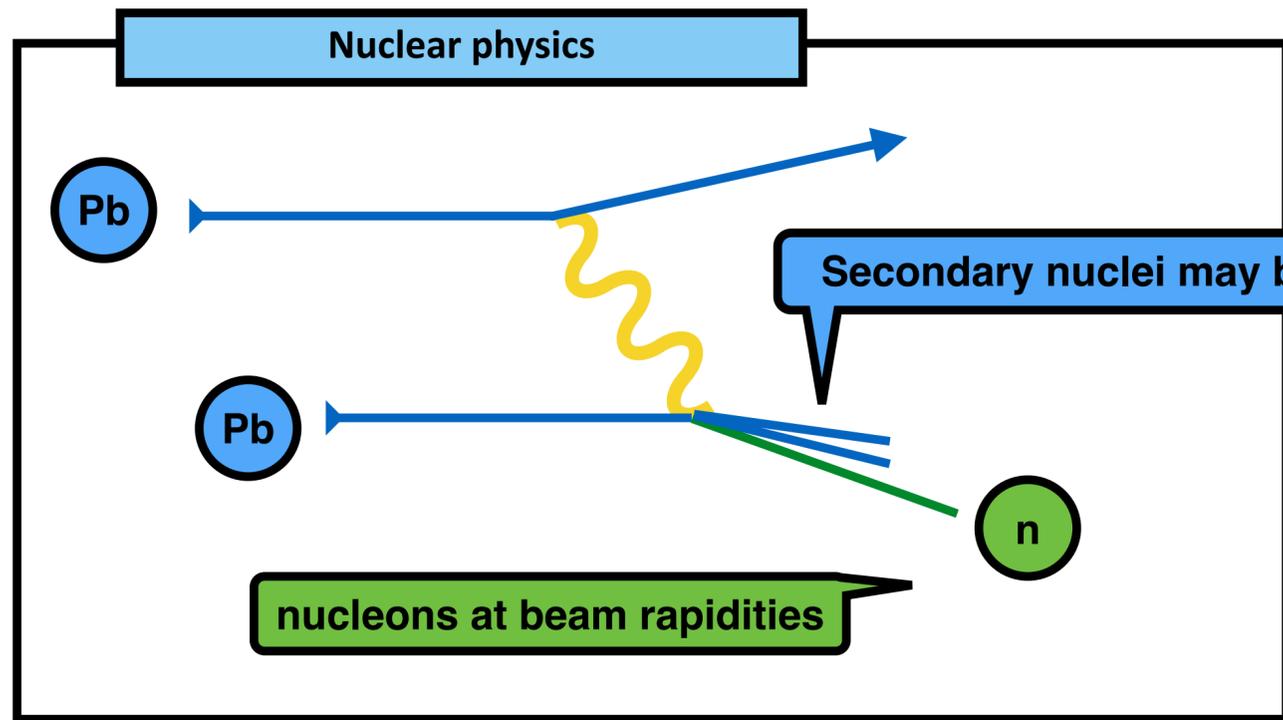
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Slide from Igor Pshenichnov



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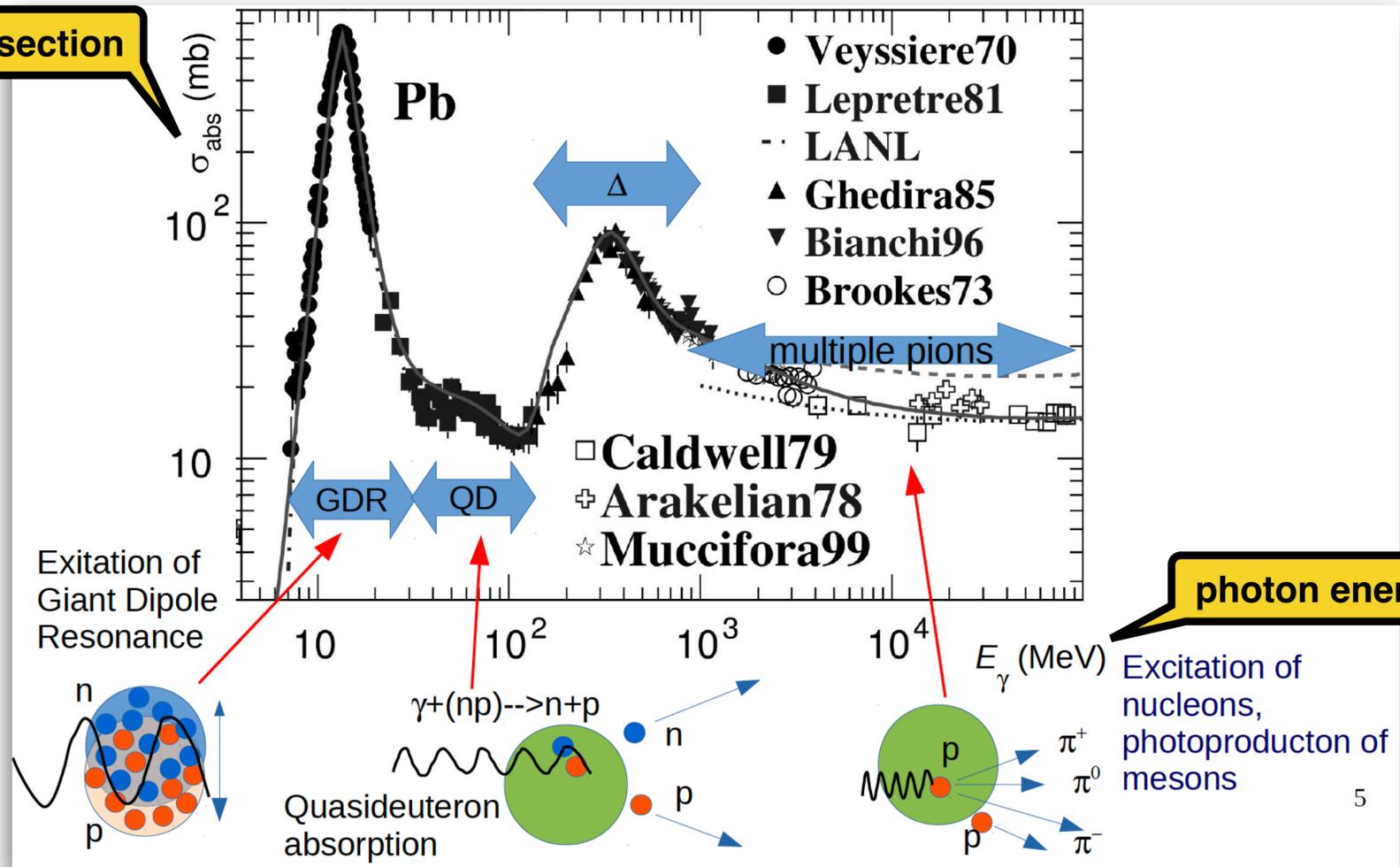


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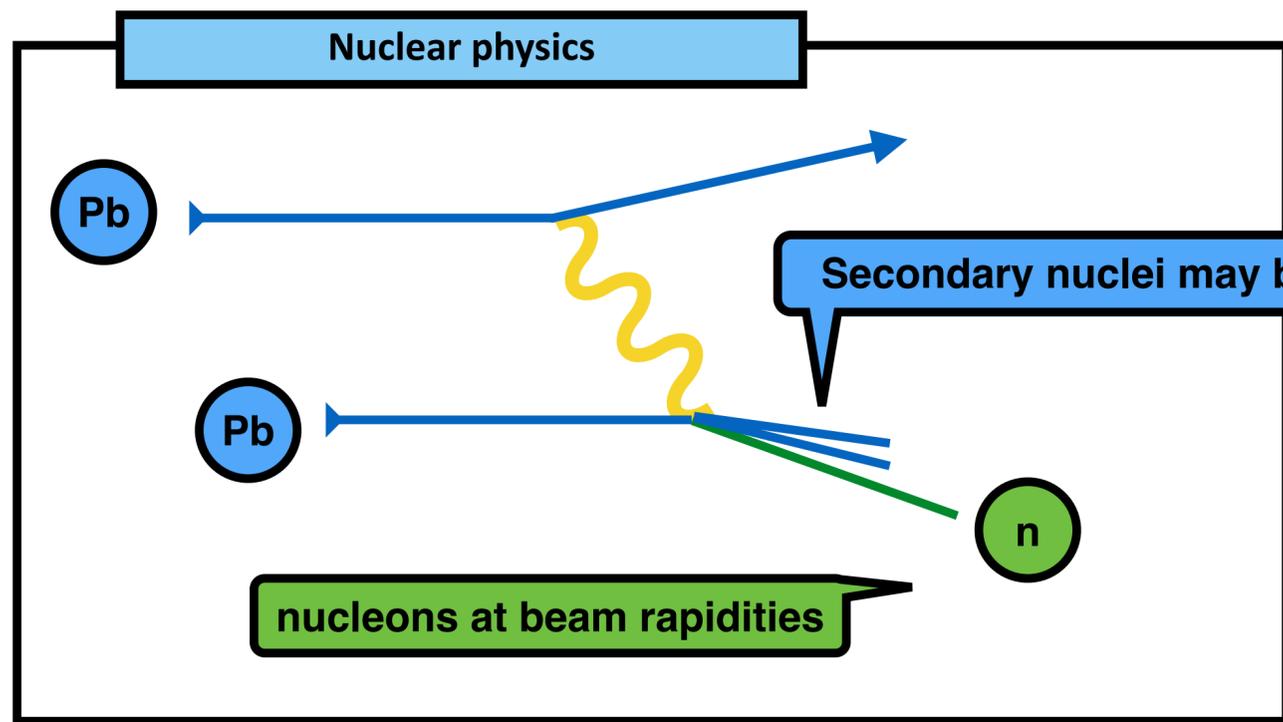
cross section



photon energy

At larger photon energies, charged particles are produced: may affect the efficiency of vetos at forward rapidities

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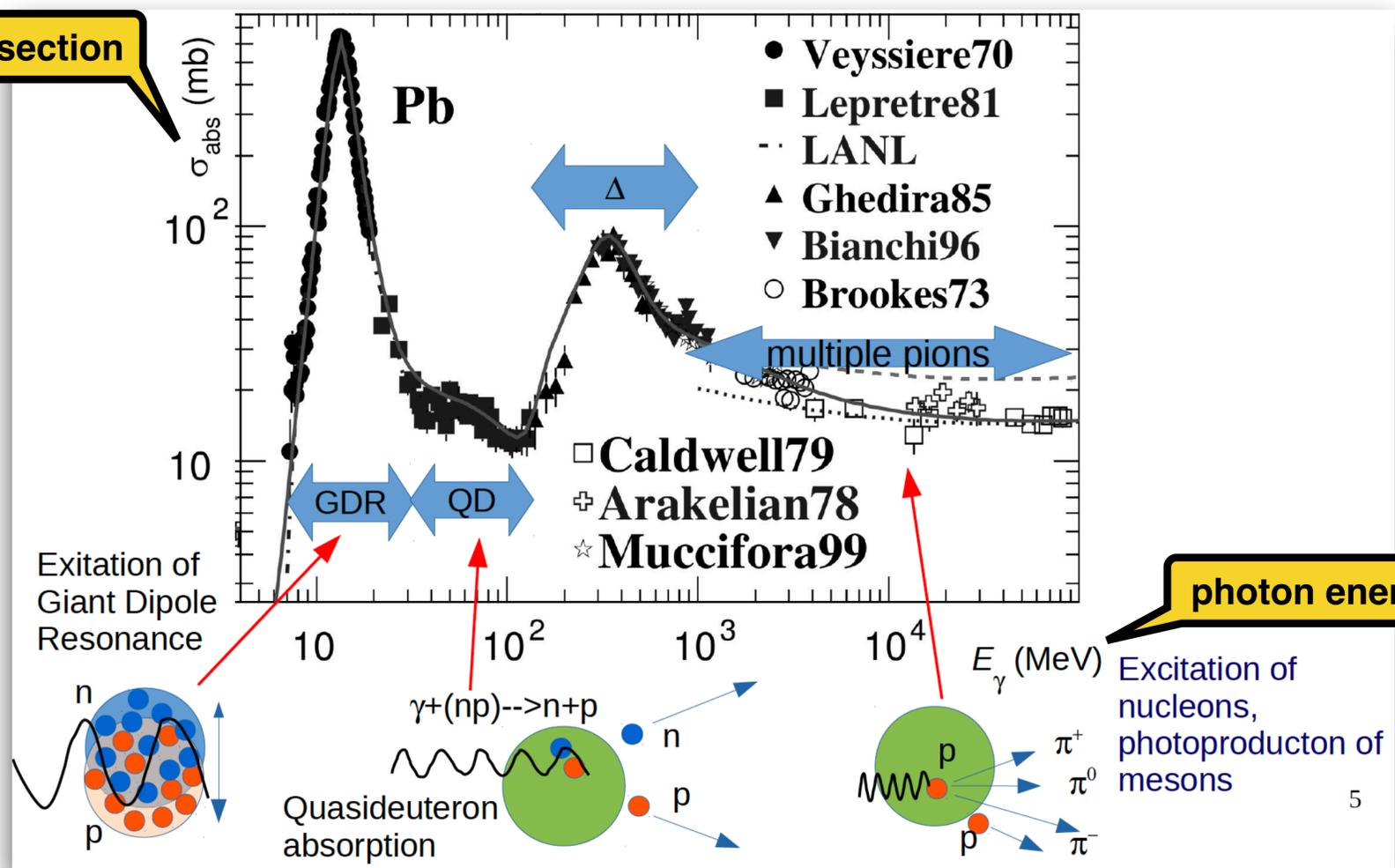
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$\sim(10)$  MeVs (in target rest frame) needed to excite the GDP

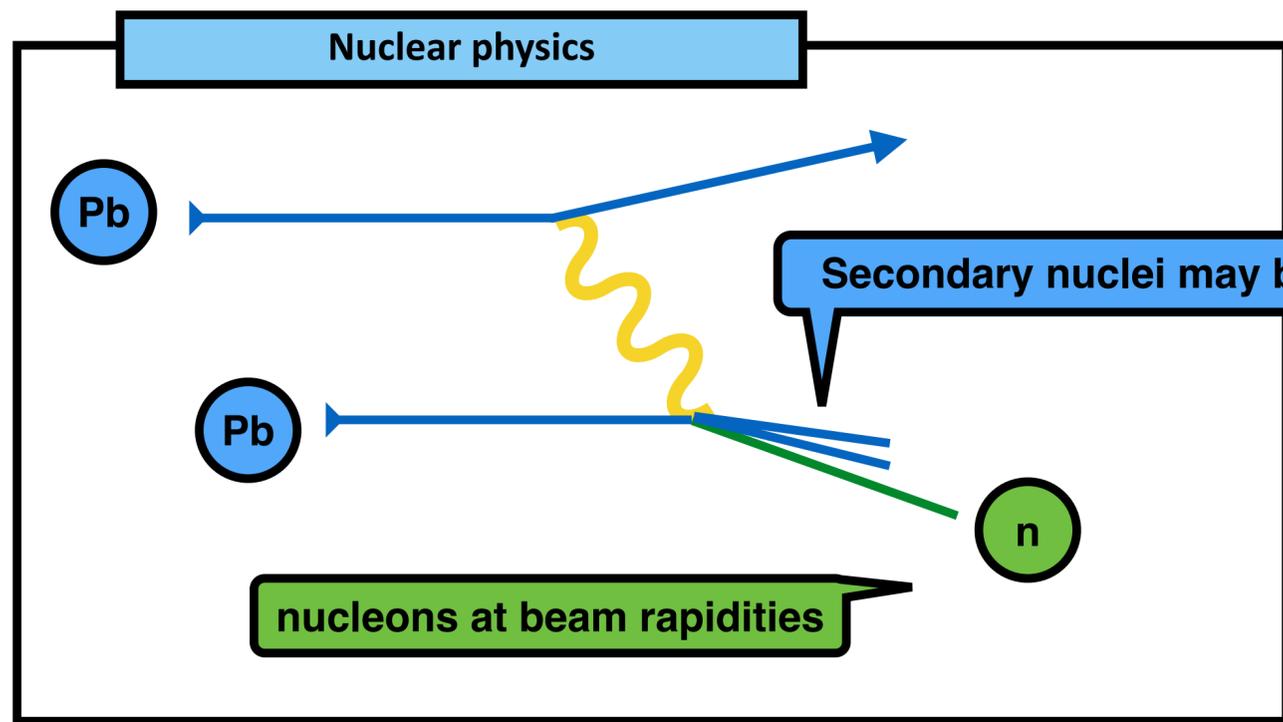
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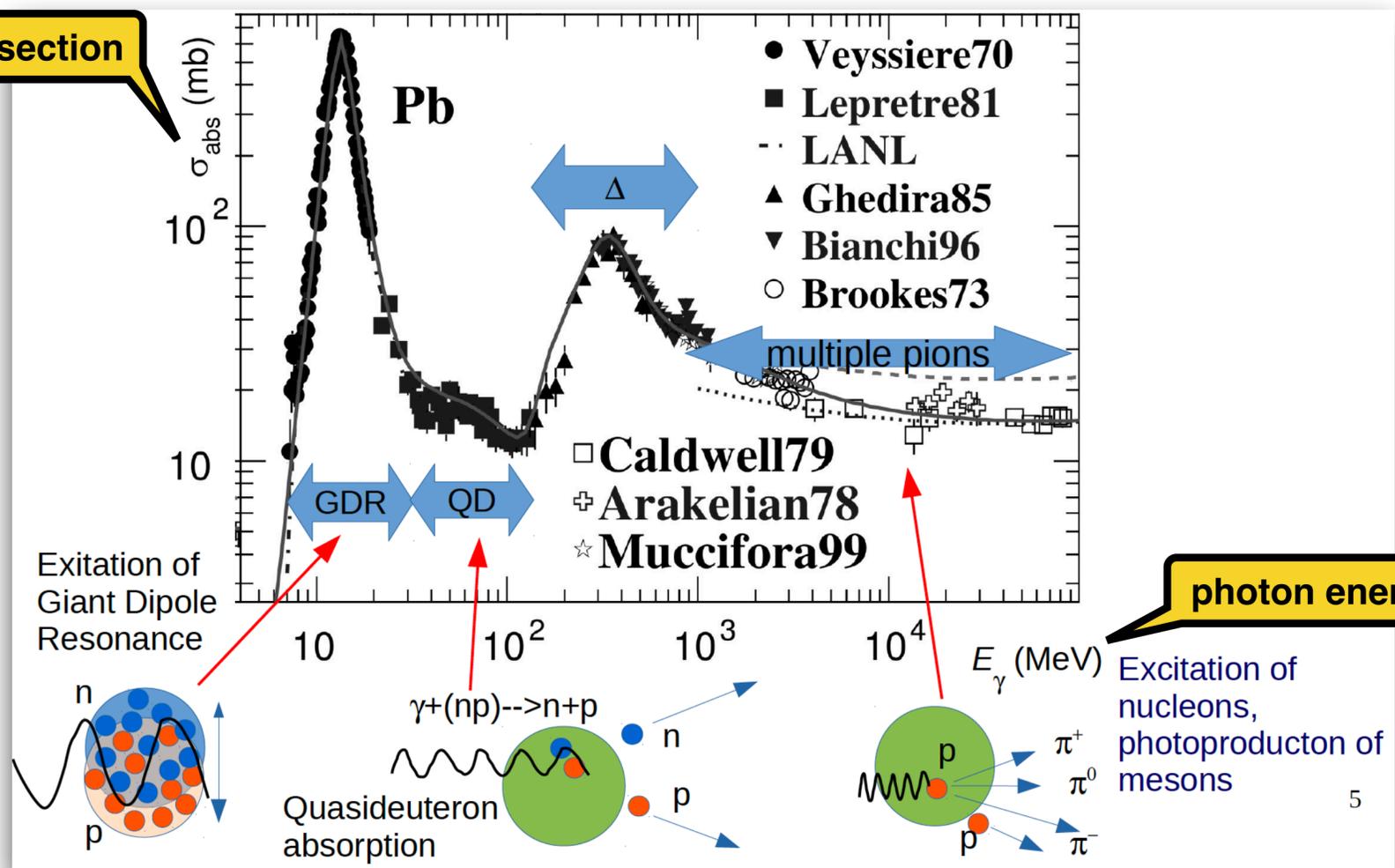


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cross section



$\sim 10$  MeVs (in target rest frame) needed to excite the GDP

This process can be used to select small impact parameters

photon energy

At larger photon energies, charged particles are produced: may affect the efficiency of vetos at forward rapidities

# Flux including EMD in n00n

Use data to describe the neutron emission in EMD processes to tag different impact-parameter ranges

# Flux including EMD in nOOn

Use data to describe the neutron emission in EMD processes to tag different impact-parameter ranges

UPC of process P with EMD

$$\sigma(AA \rightarrow PA'_i A'_j) \propto \int d^2\vec{b} P_P(b) P_{ij}(b) \exp(-P_H(b)),$$

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Probability of no inelastic hadronic interactions at this impact parameter

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$$P_{ij}(b) = P_i(b) \times P_j(b).$$

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Two one-neutron or one two-neutron emission

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Use data to describe the neutron emission in EMD processes to tag different impact-parameter ranges

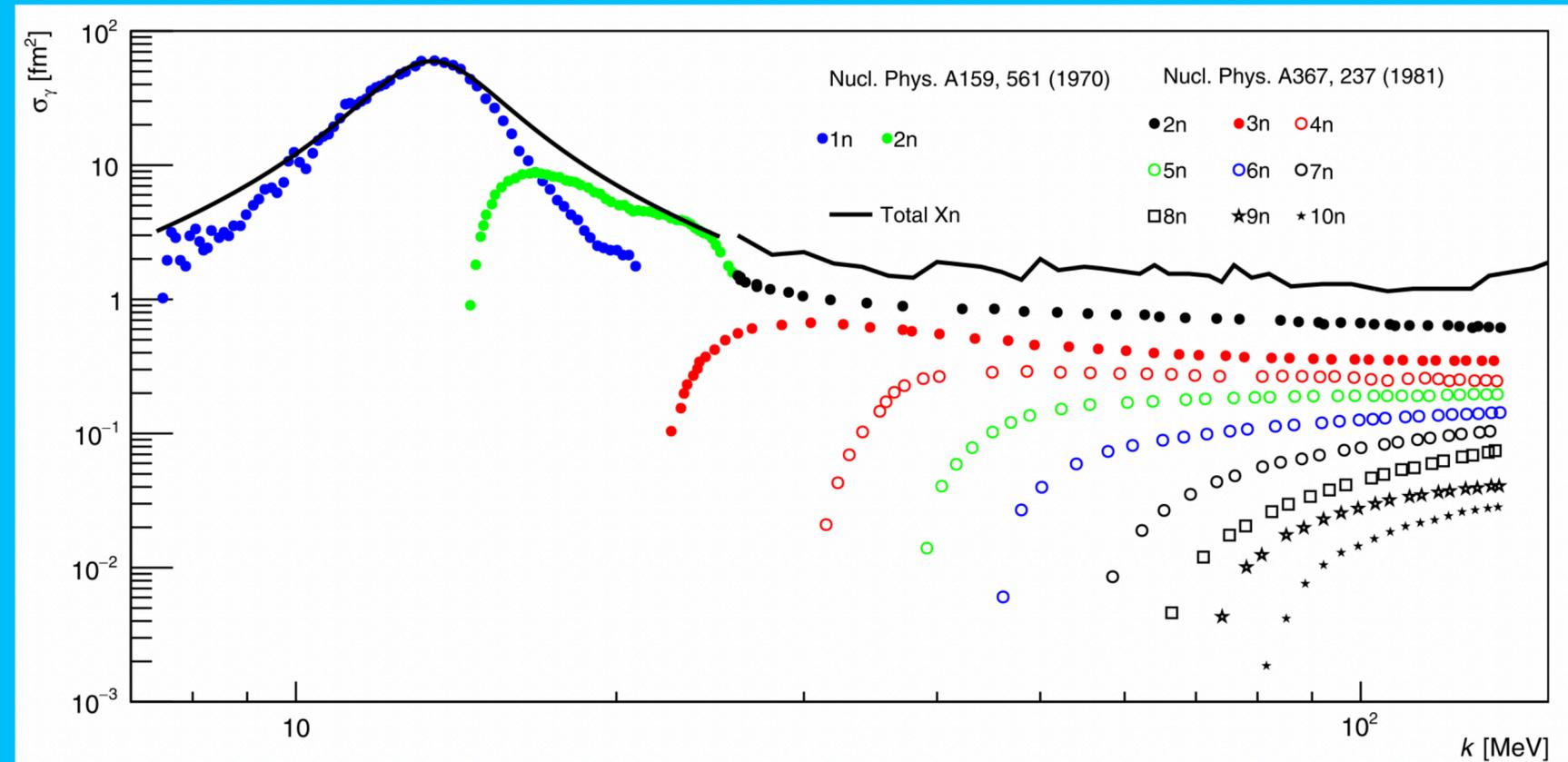
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Formalism fit to EMD data sets, e. g.



Probability of emission of i neutrons by one ion and j neutrons by the other

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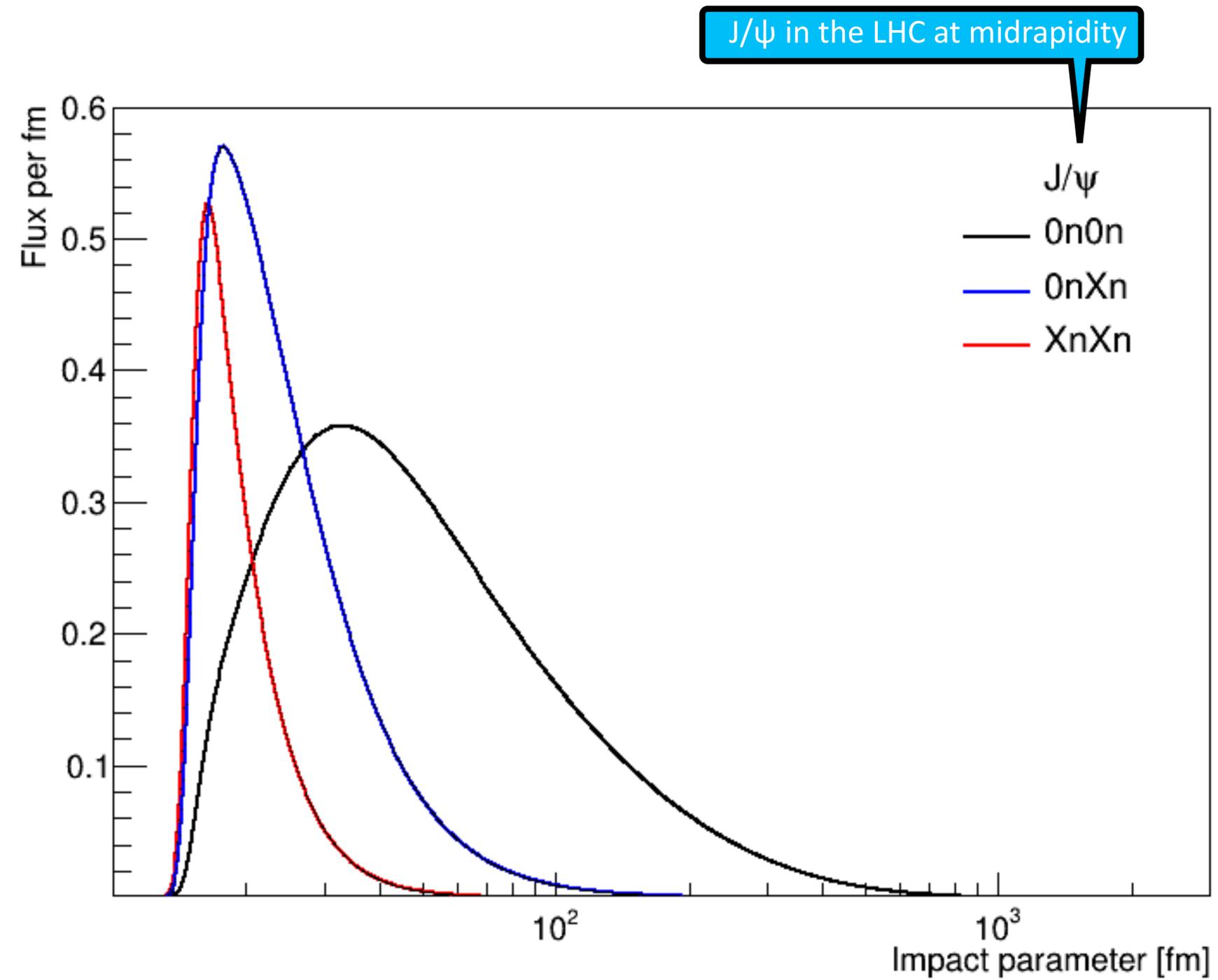
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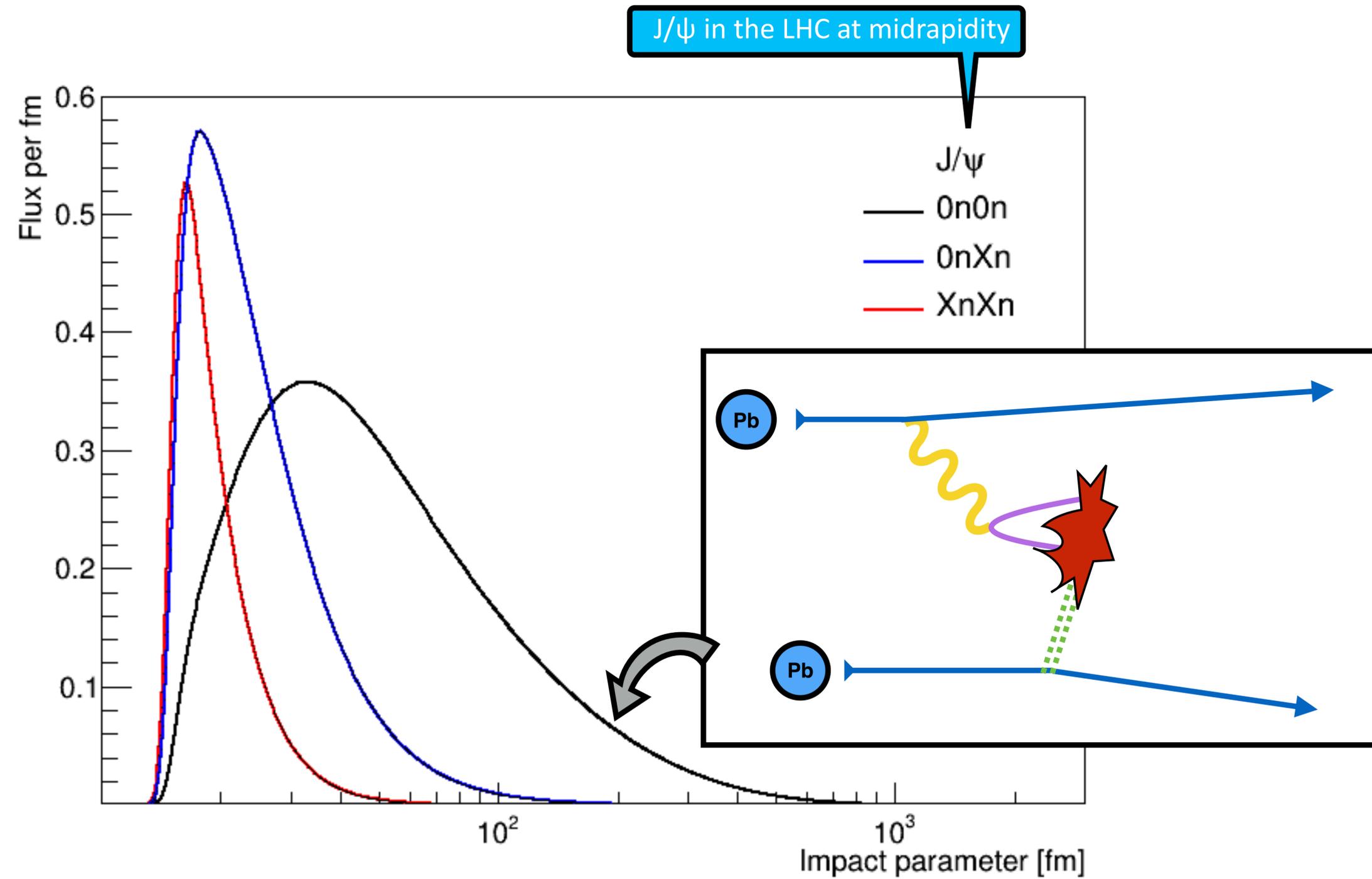
# Example of impact-parameter dependence of the flux



Plot made with n00n, provided by Michal Broz

Guillermo Contreras, CTU in Prague

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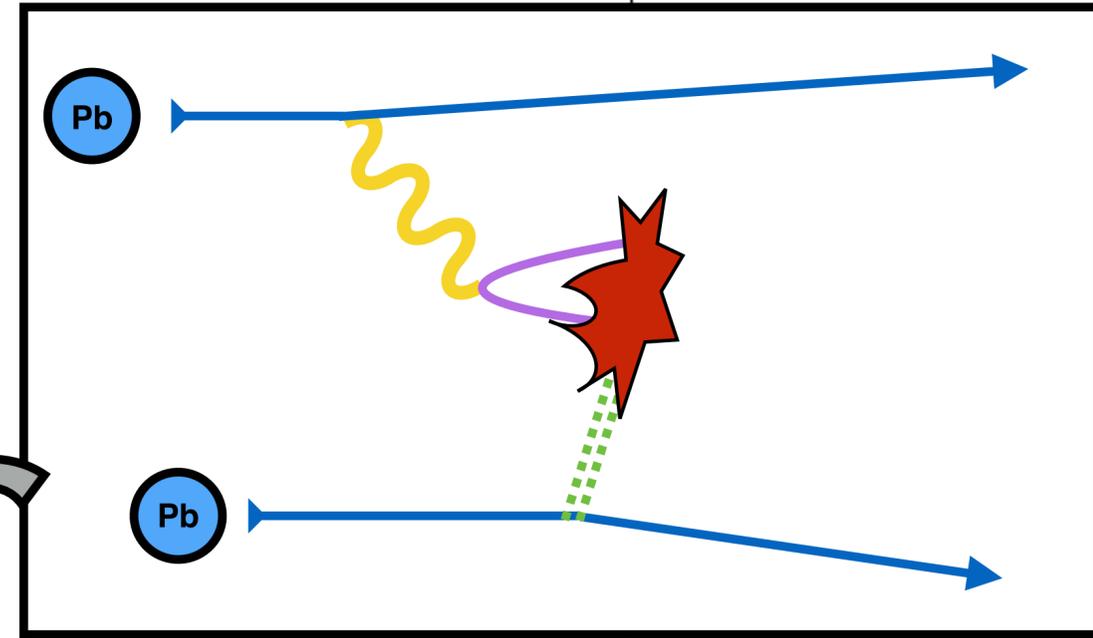
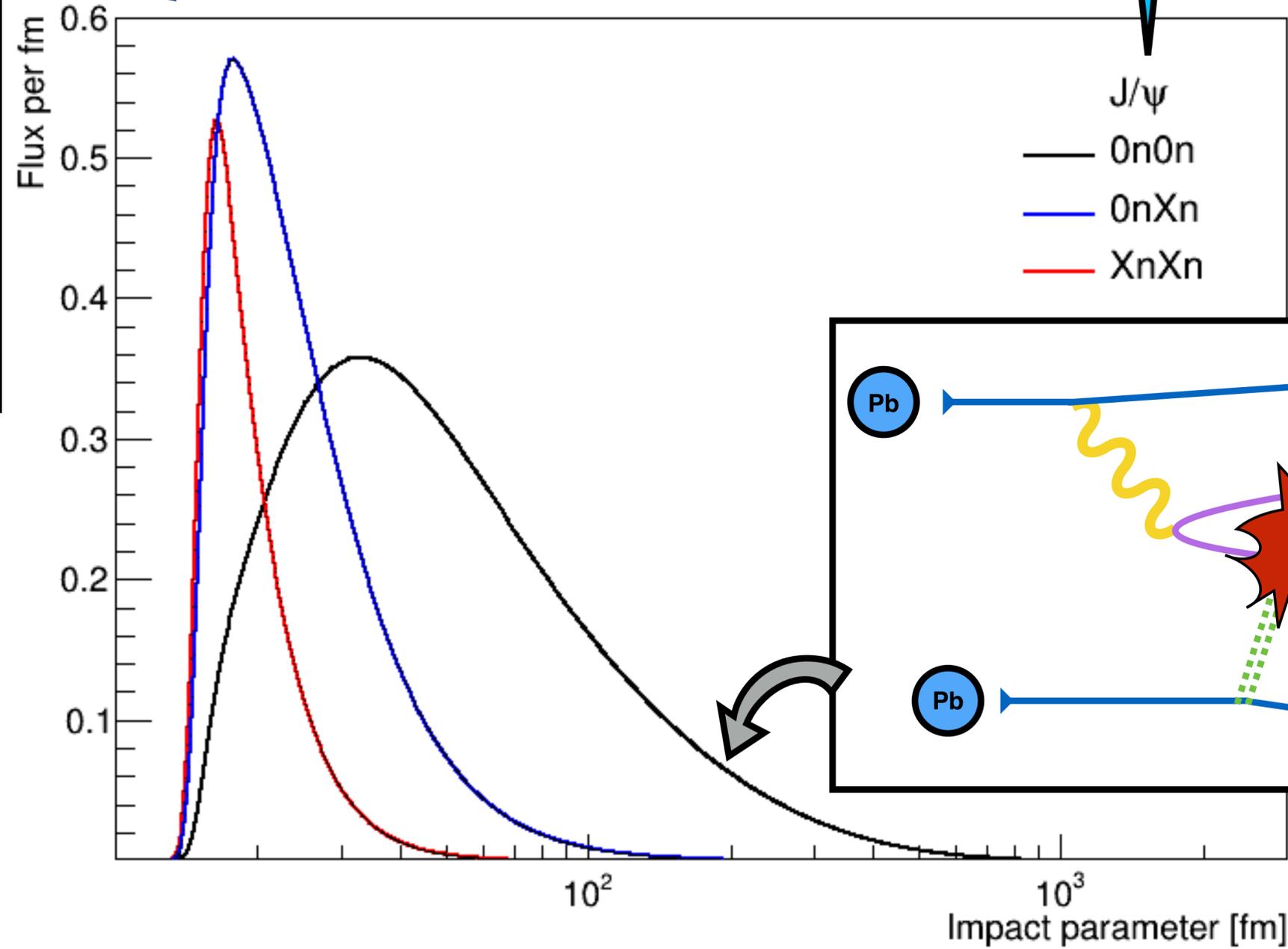
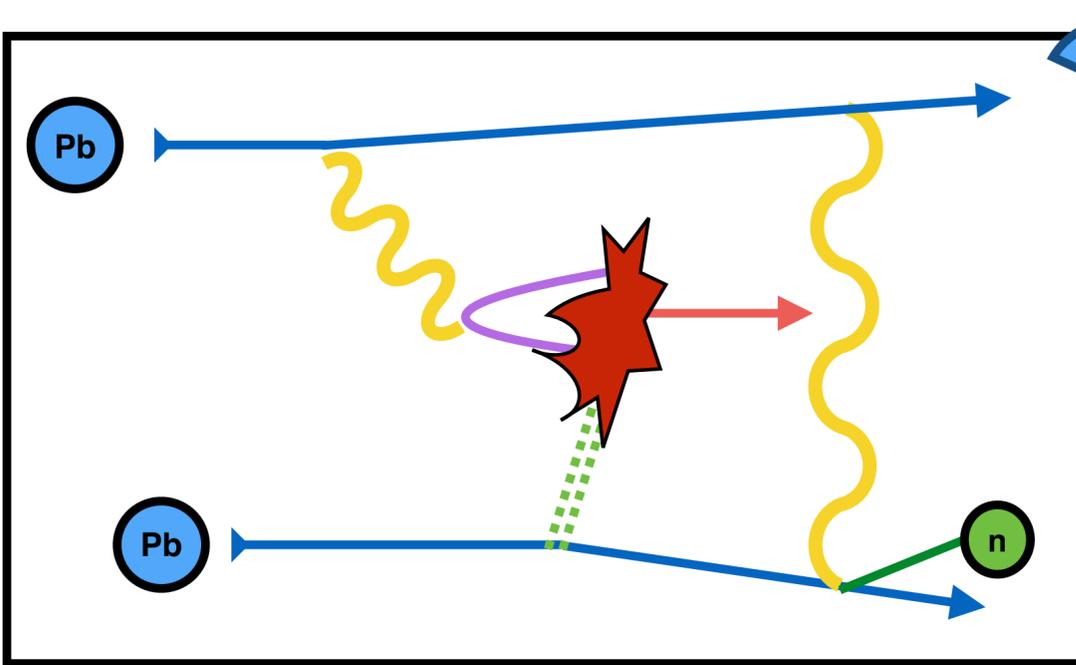


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J/ $\psi$  in the LHC at midrapidity

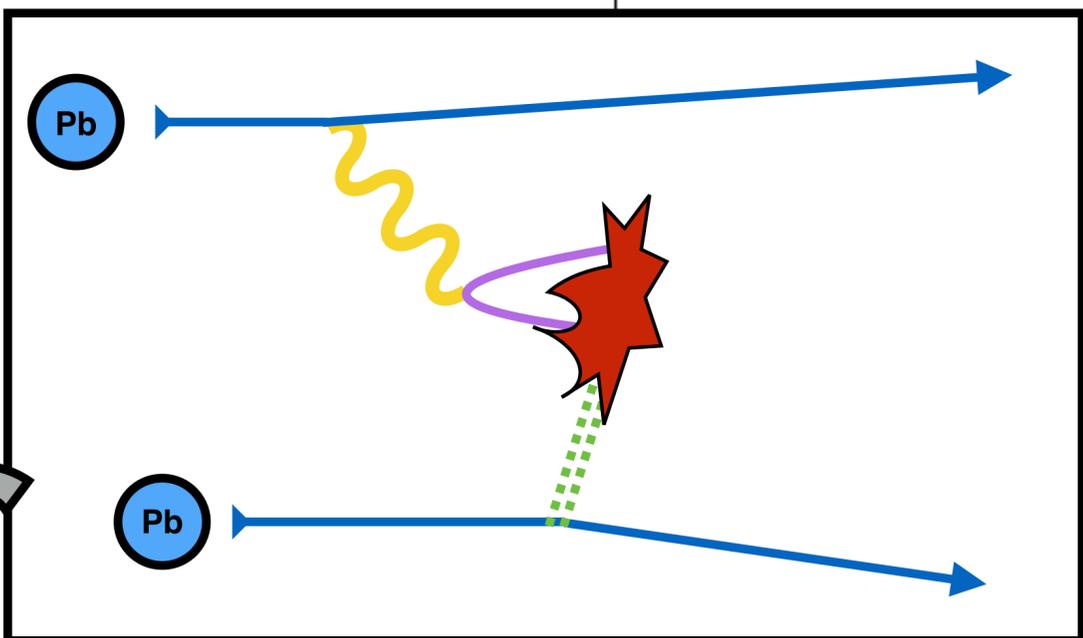
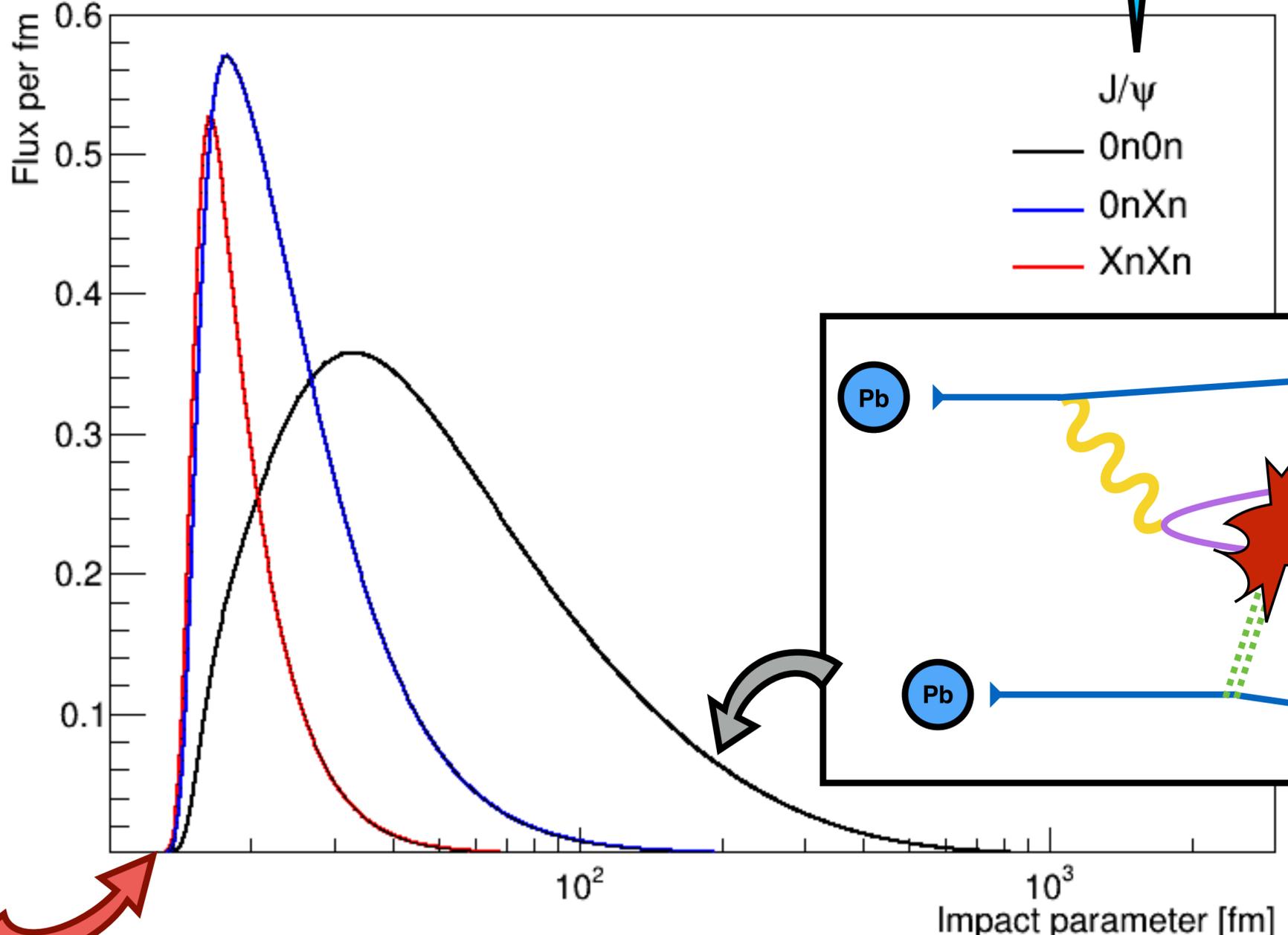
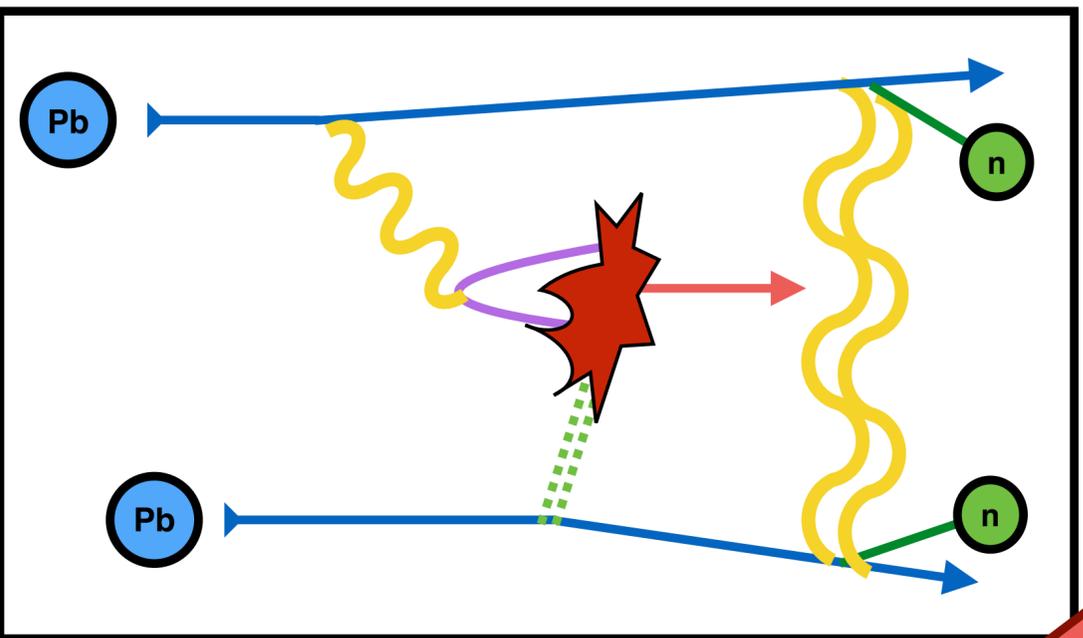
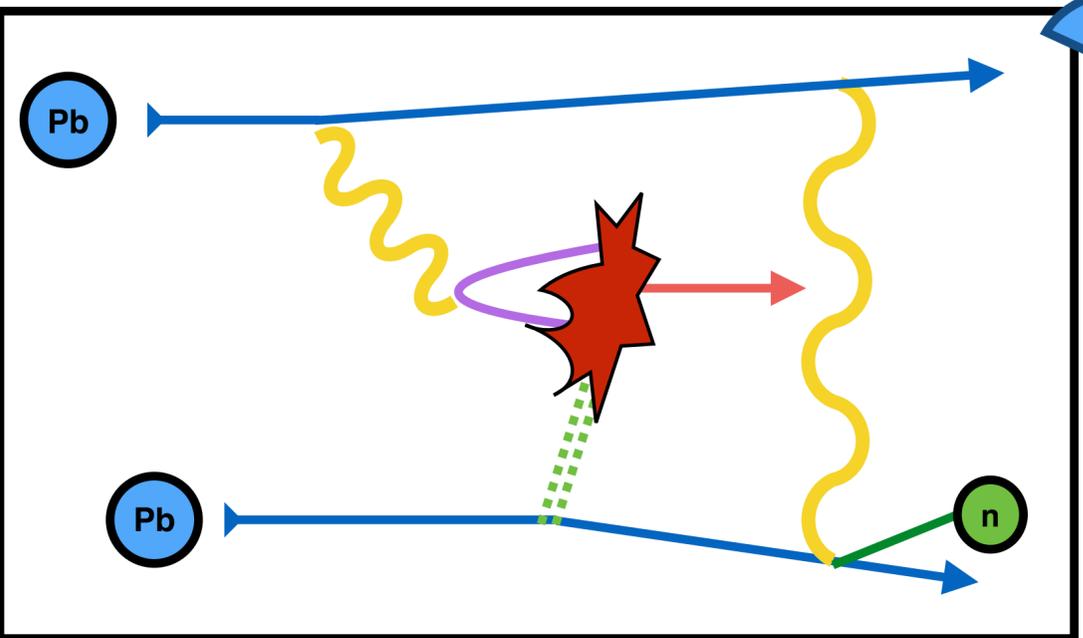


Plot made with nOOn, provided by Michal Broz

Guillermo Contreras, CTU in Prague

# Example of impact-parameter dependence of the flux

J/ $\psi$  in the LHC at midrapidity

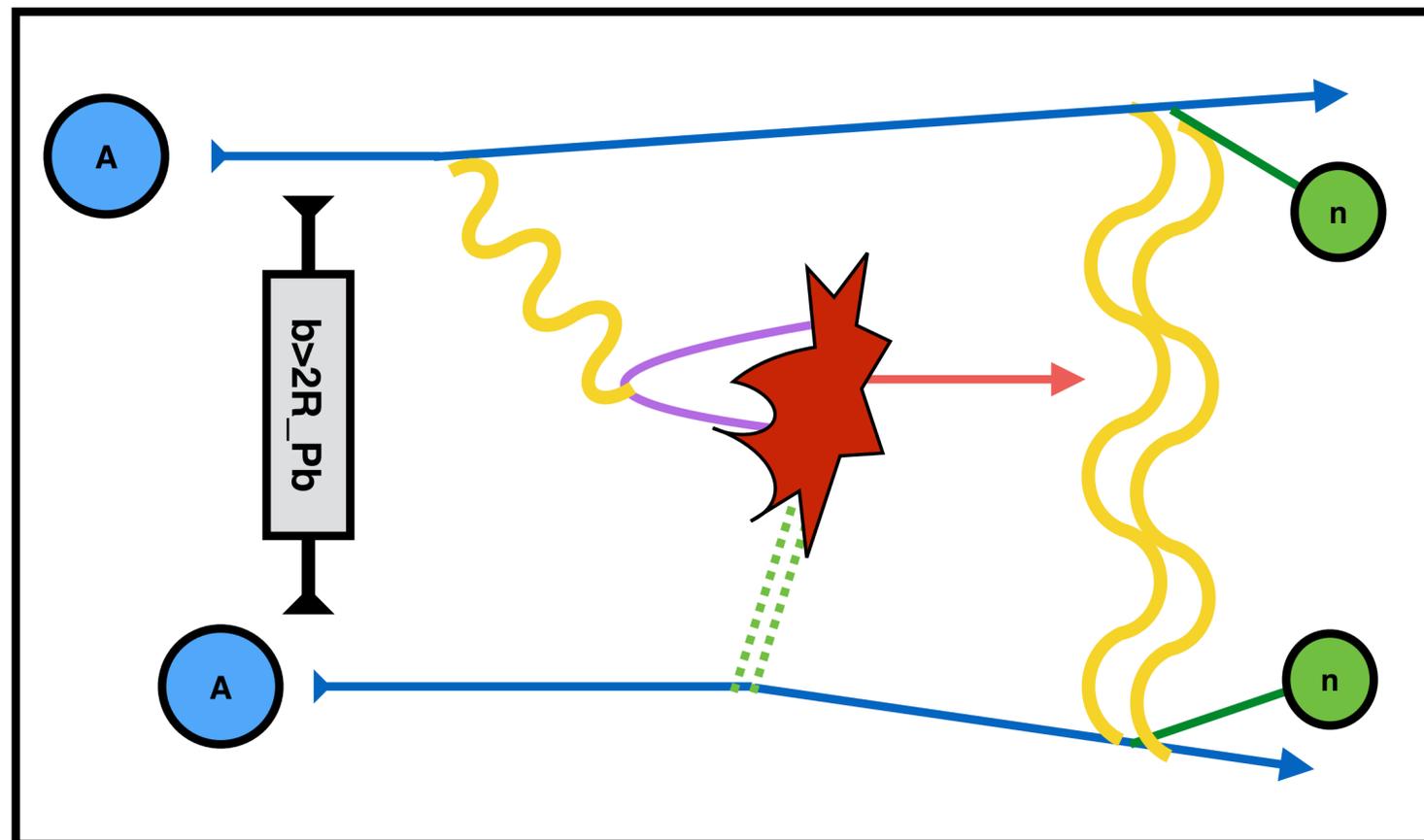


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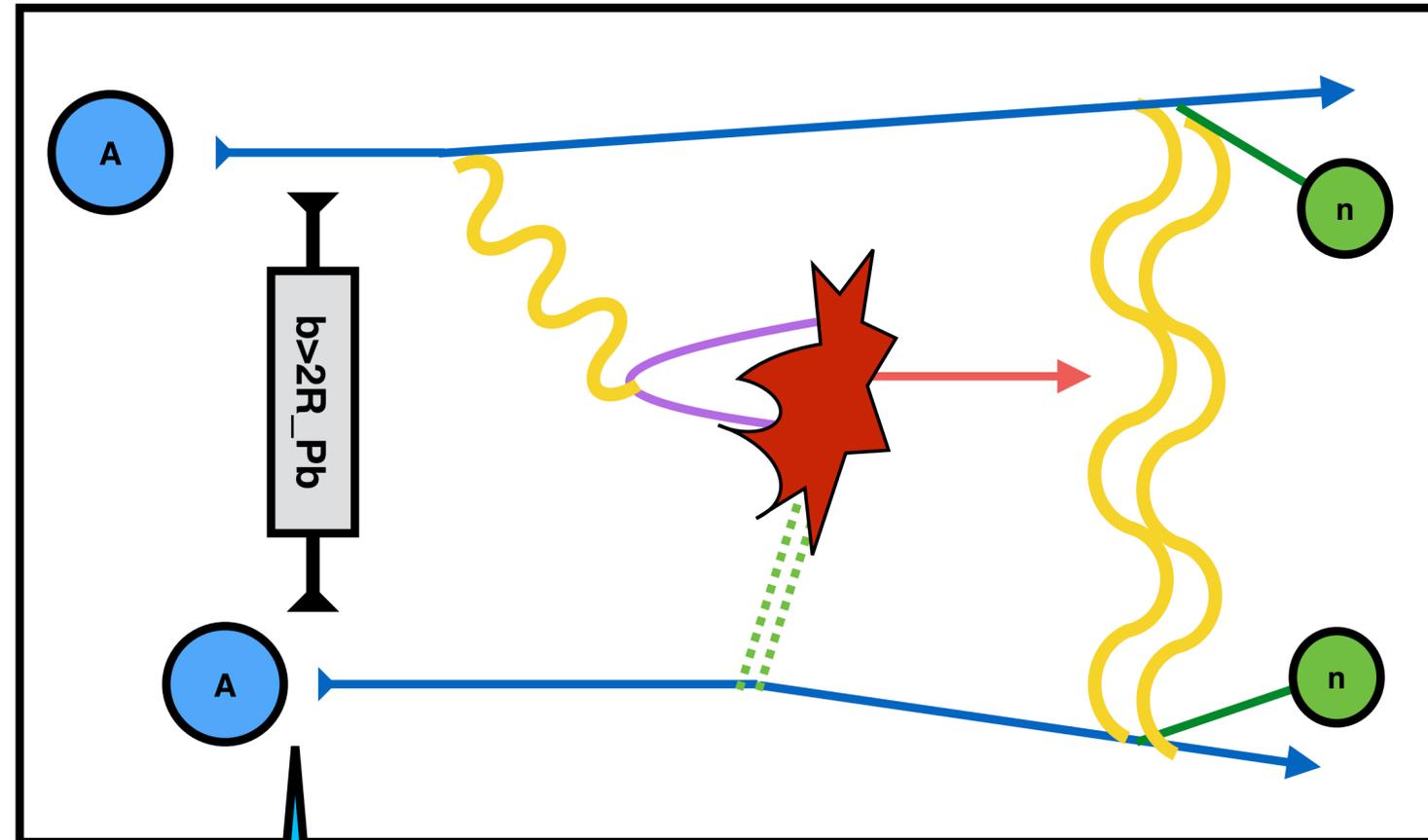
# How to find photon-induced interactions in hadron colliders (4/4)

Sometimes, for exclusive diffractive observables in UPC an overlap with EMD is required in the trigger



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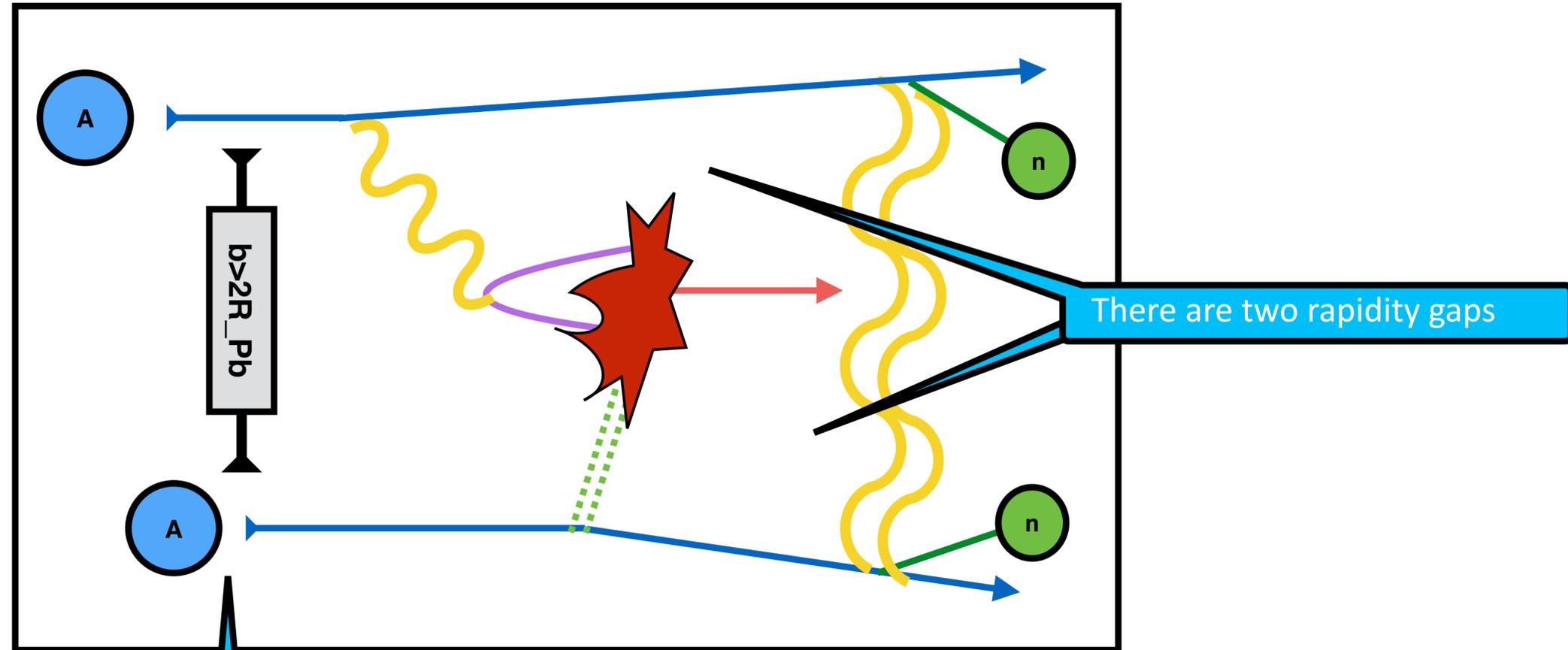
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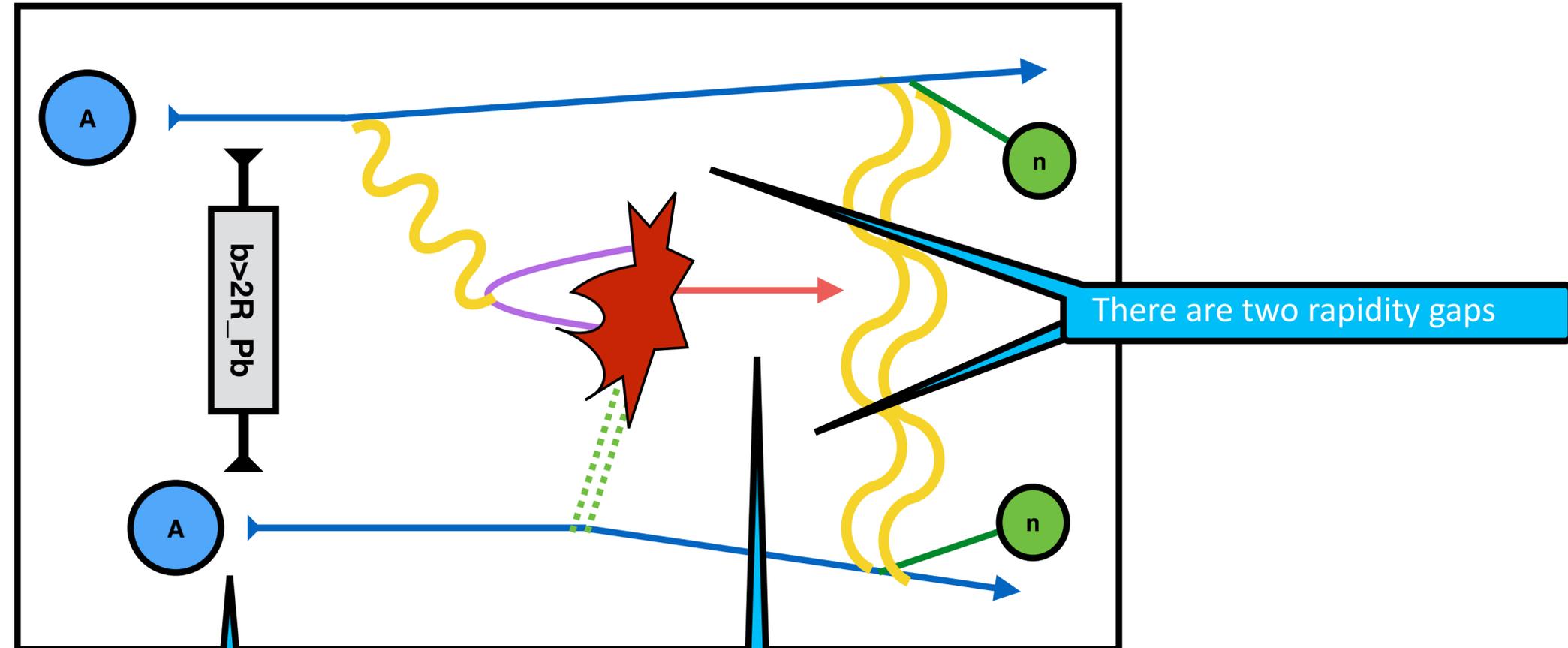
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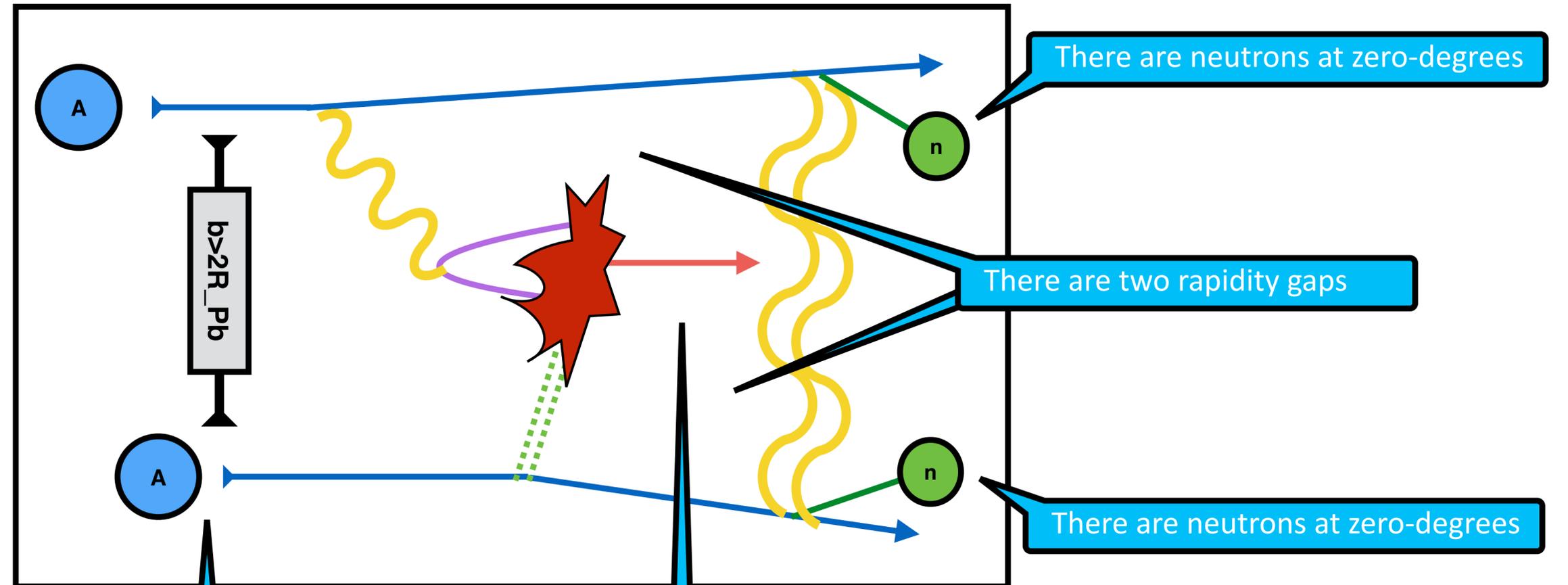


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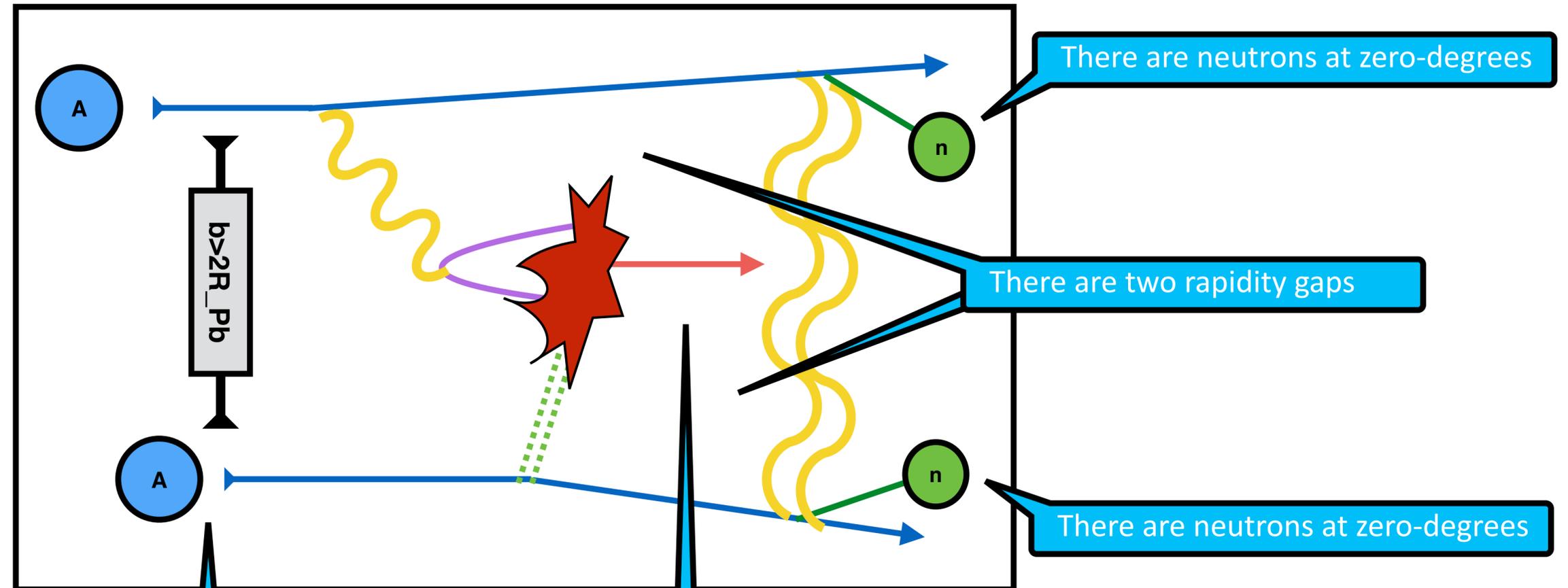
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Sometimes, for exclusive diffractive observables in UPC an overlap with EMD is required in the trigger

Signature: Look for a low  $p_T$  final state and neutrons at zero-degrees in an otherwise empty detector



For UPC the photon-induced process there is no overlap of the incoming hadrons within the range of QCD

For exclusive states in diffraction, the total transverse momentum is very small

The formalism to obtain the photon flux should be adapted to described the different types of photon induced processes

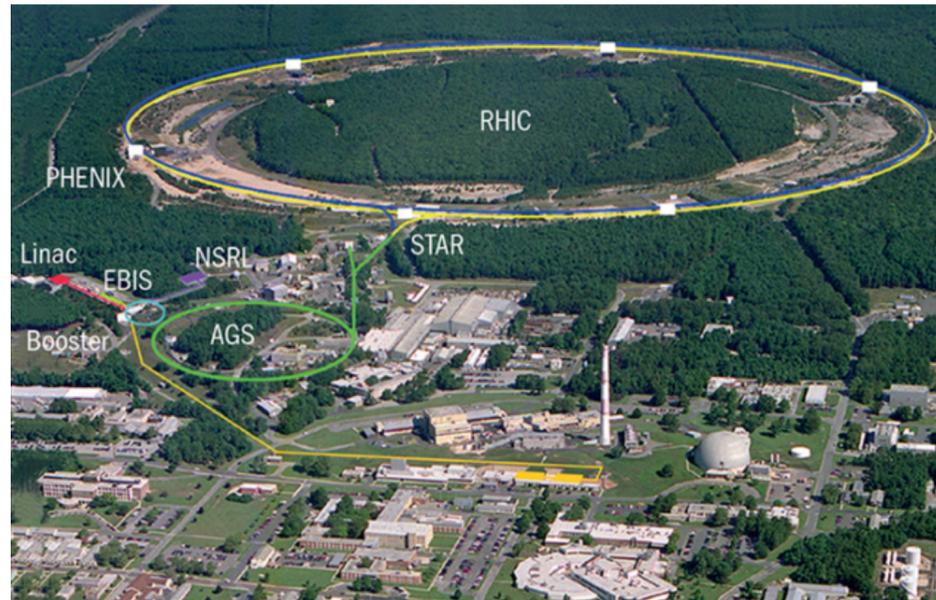
6

## Exploring high-energy QCD with nuclei at RHIC and LHC

Heavy ions have more gluons and in a denser environment than protons which makes them ideal candidates to search for saturation effects

But other effects, like shadowing may complicate the search

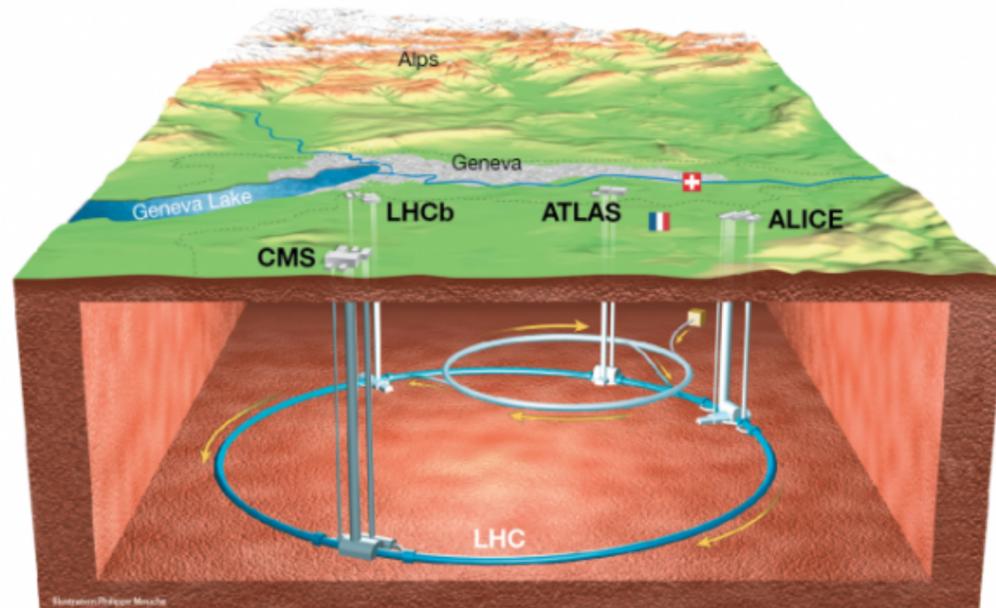
# RHIC and the LHC



Credit: BNL

Relativistic heavy ion collider (RHIC)  
Located in USA  
3834 m of circumference  
Operating since 2000  
2 independent beams  
Can accelerate different ions  
Reaches collisions at 200 GeV (per NN) for AuAu

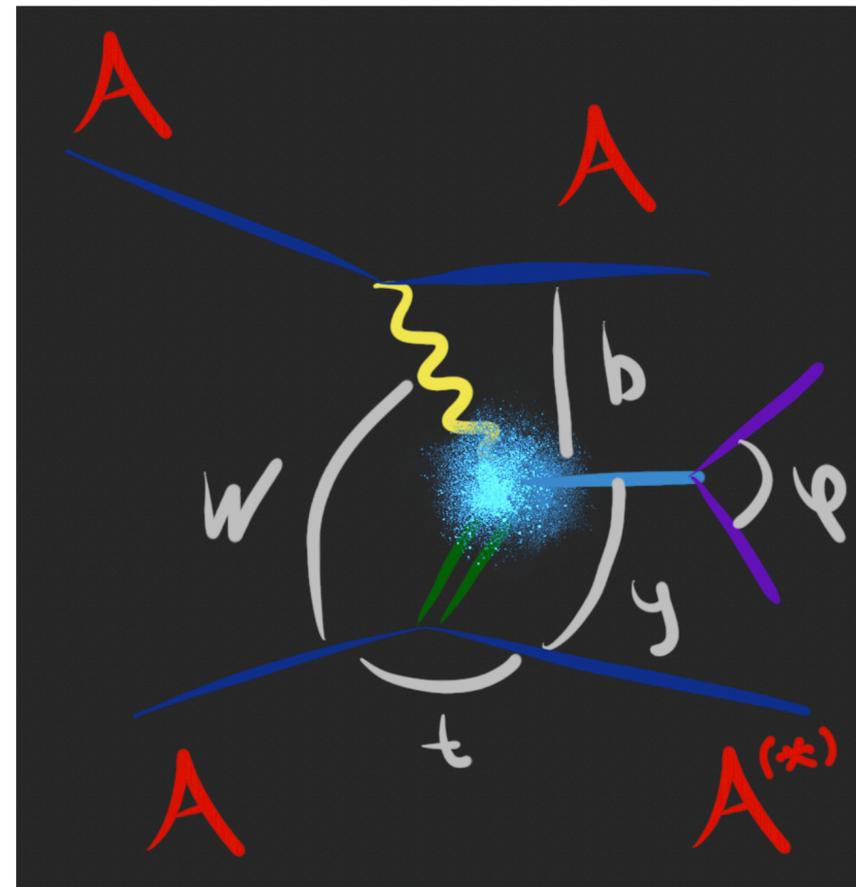
Both facilities have a very rich heavy-ion program



Credit: CERN

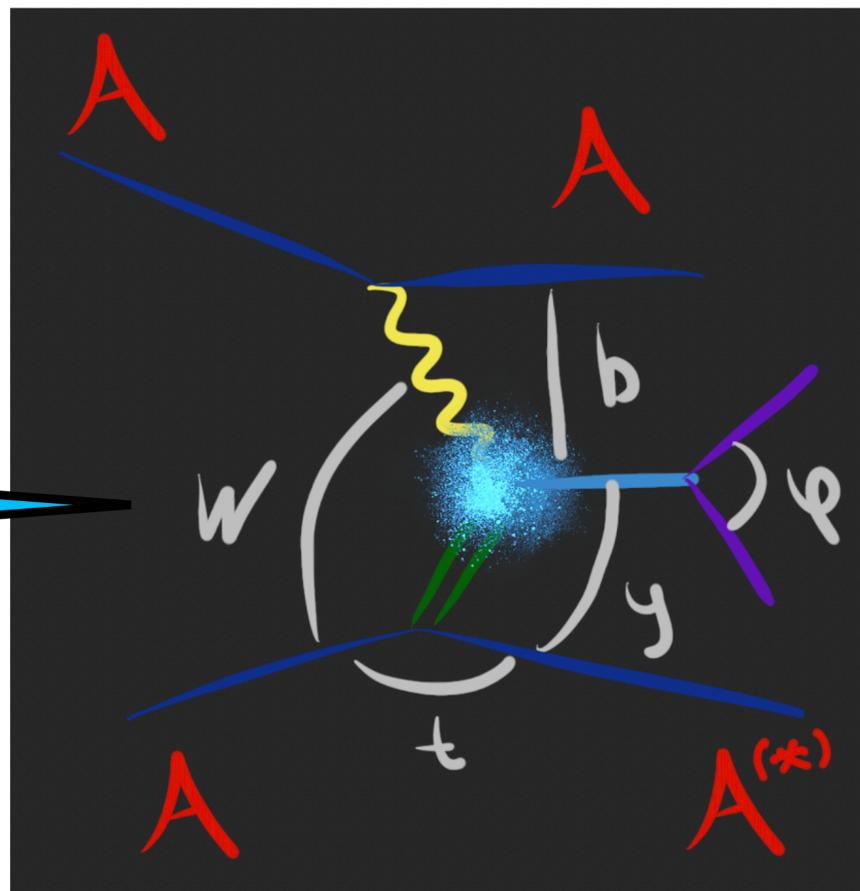
Large hadron collider (LHC)  
Located in Europe  
27 km of circumference  
Operating since 2010  
Has reached collisions at 5.36 TeV (per NN) for PbPb

There are many results, so I will concentrate on the possibilities offered by diffractive vector meson production  
I will review only a few results, you will hear a lot more about this during the conference



# Diffractive vector meson photoproduction: a Swiss army knife for QCD (1/2)

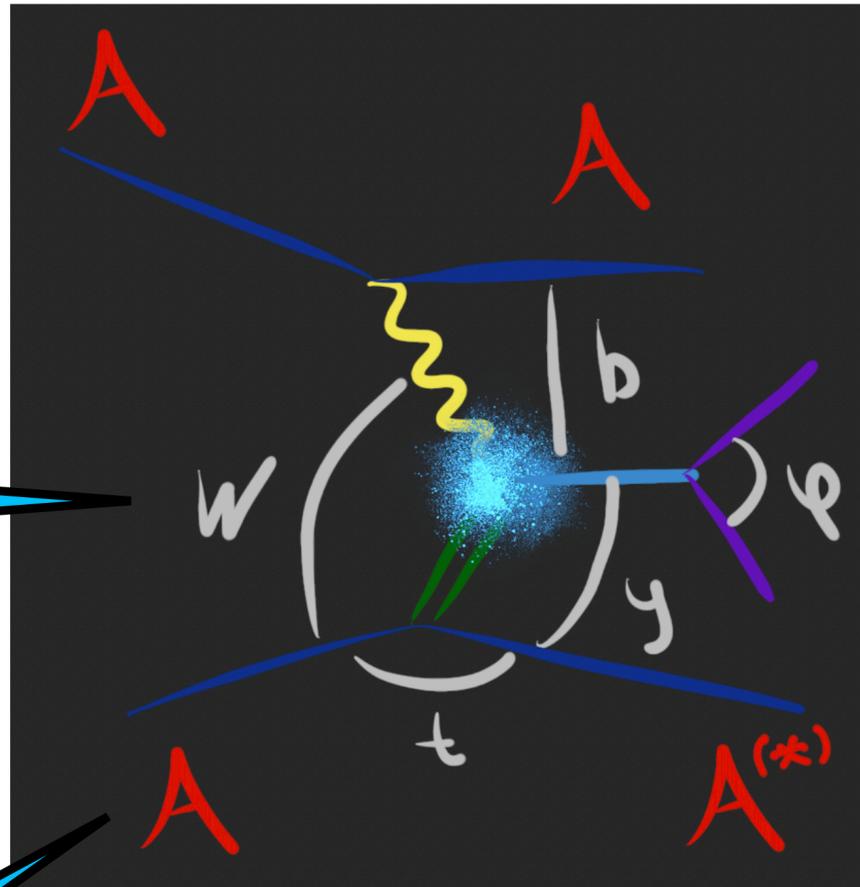
The energy dependence, gives the Bjorken-x evolution of the target



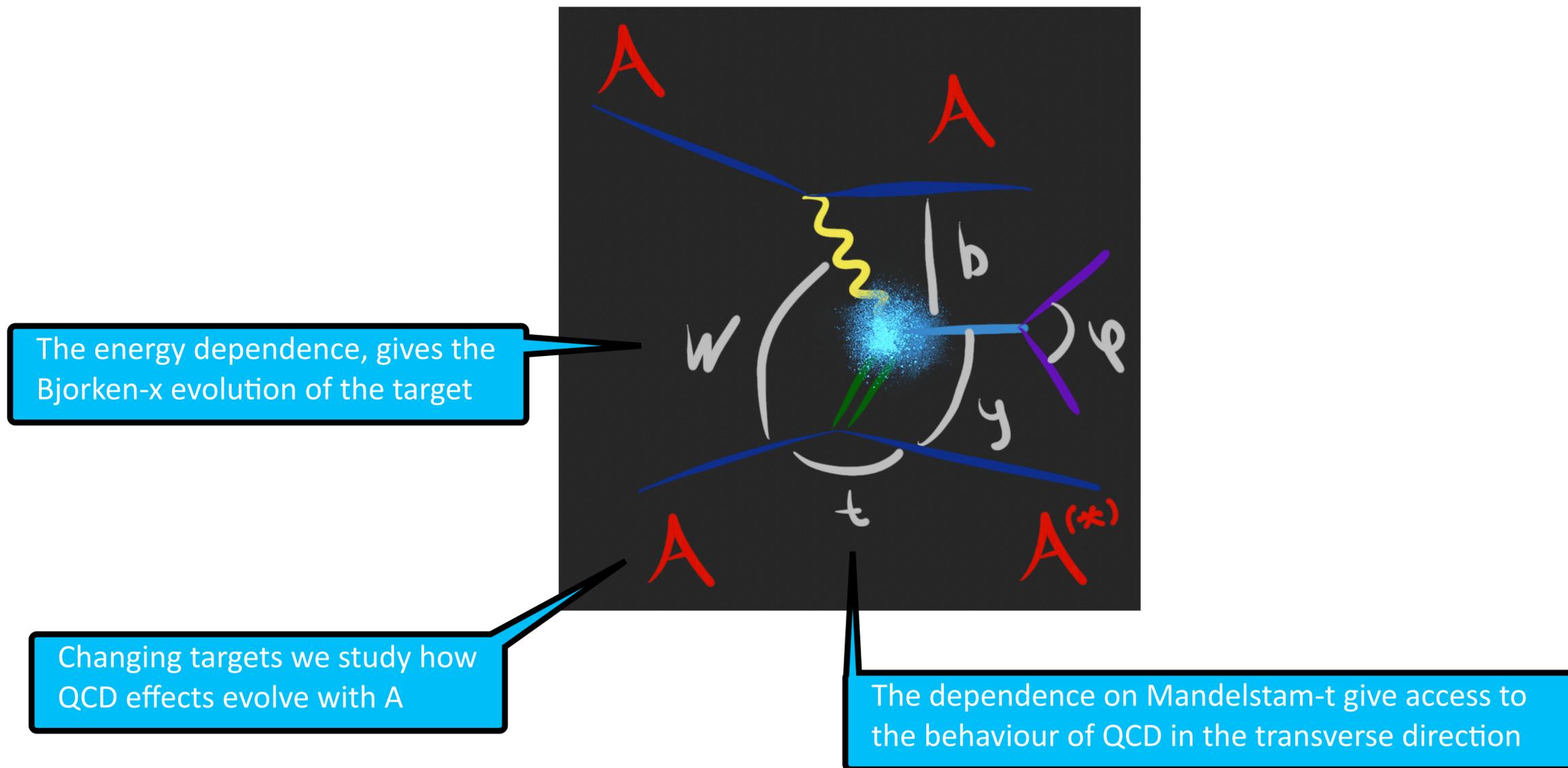
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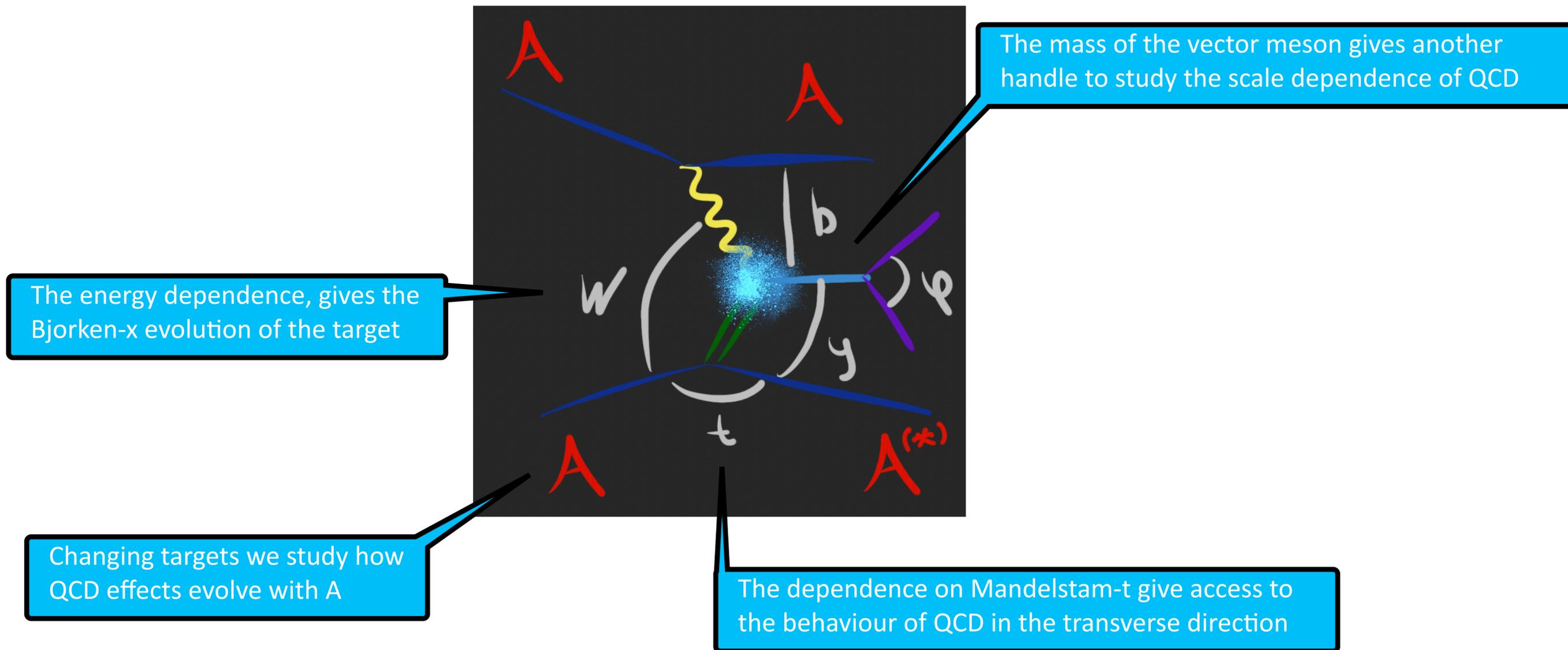
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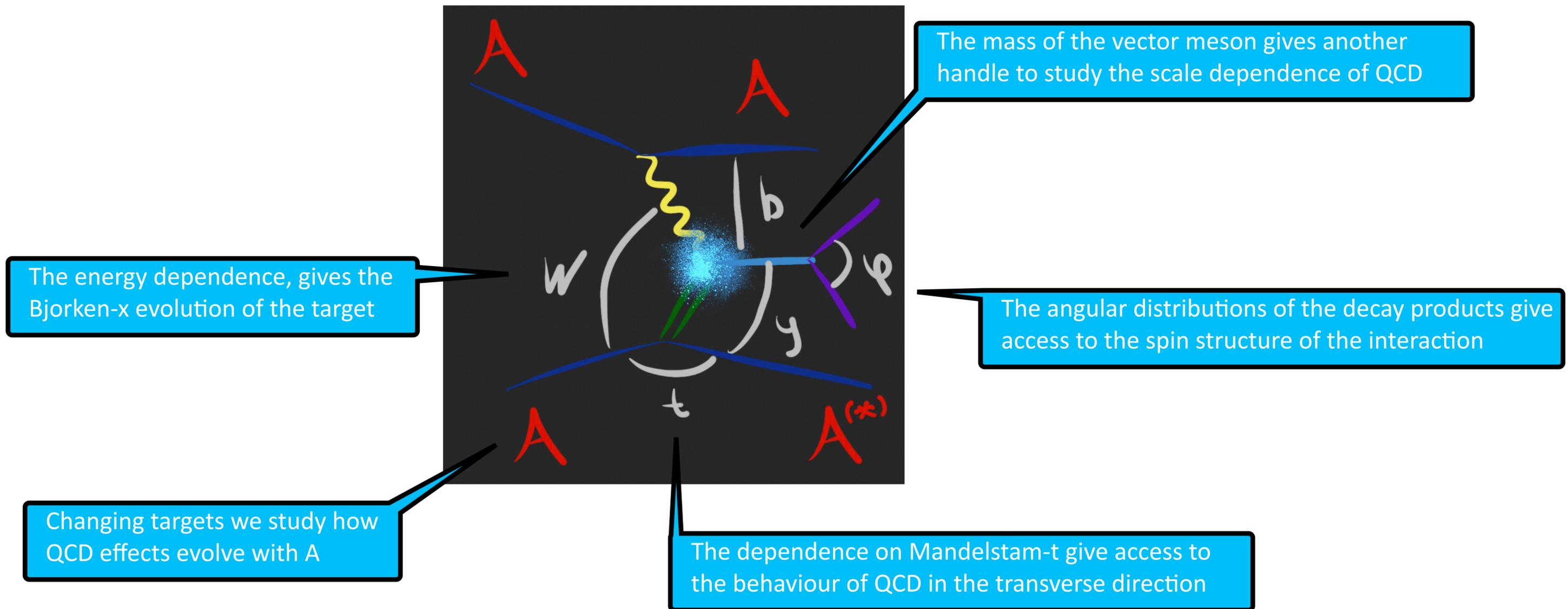
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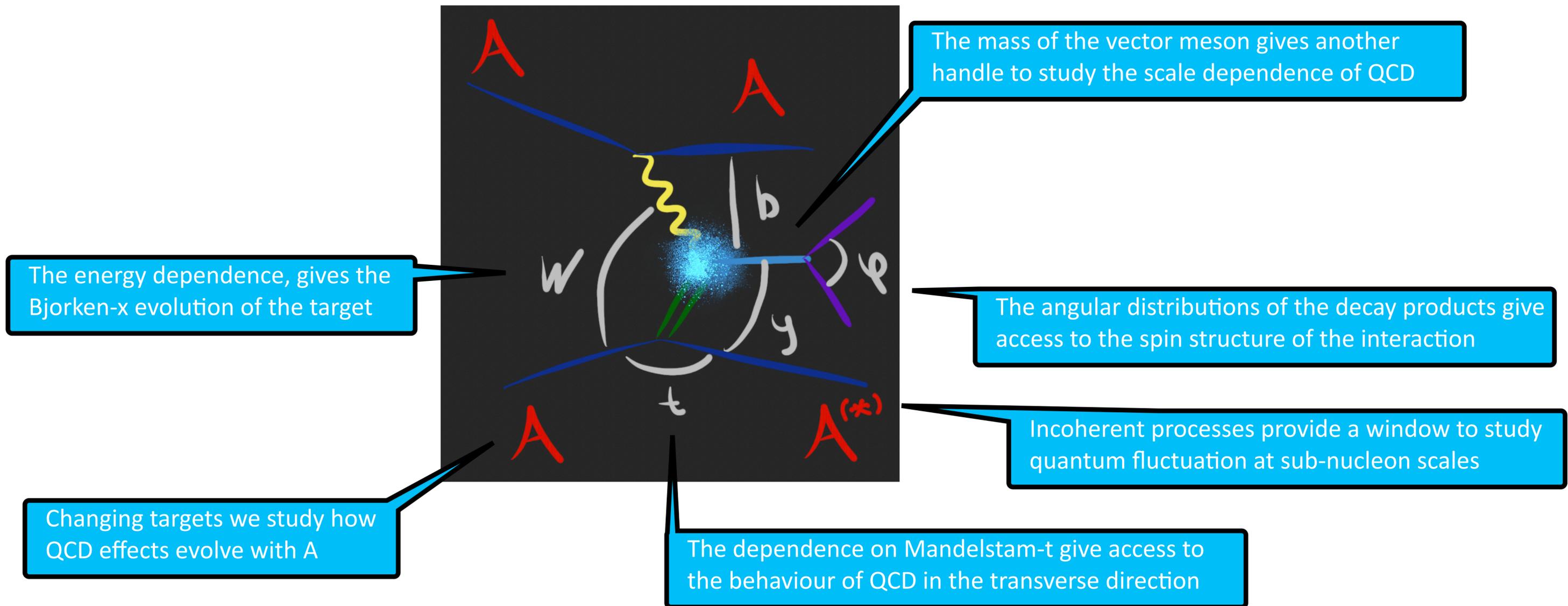
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The mass of the vector meson gives another handle to study the scale dependence of QCD

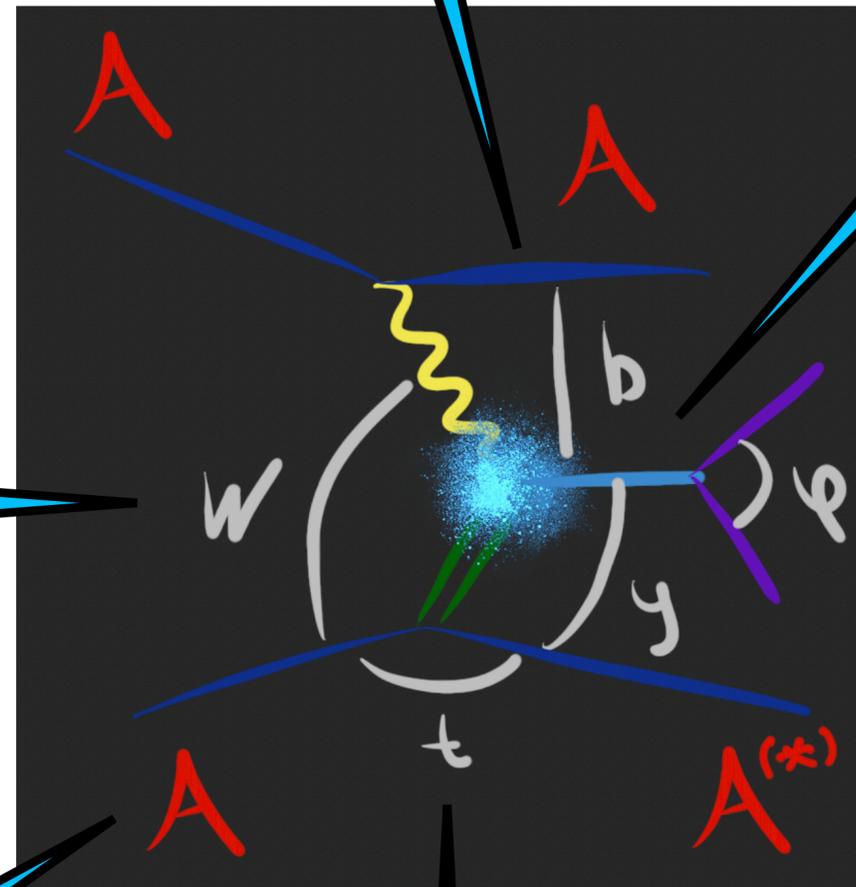
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The angular distributions of the decay products give access to the spin structure of the interaction

Incoherent processes provide a window to study quantum fluctuation at sub-nucleon scales

Changing targets we study how QCD effects evolve with A

The dependence on Mandelstam-t give access to the behaviour of QCD in the transverse direction



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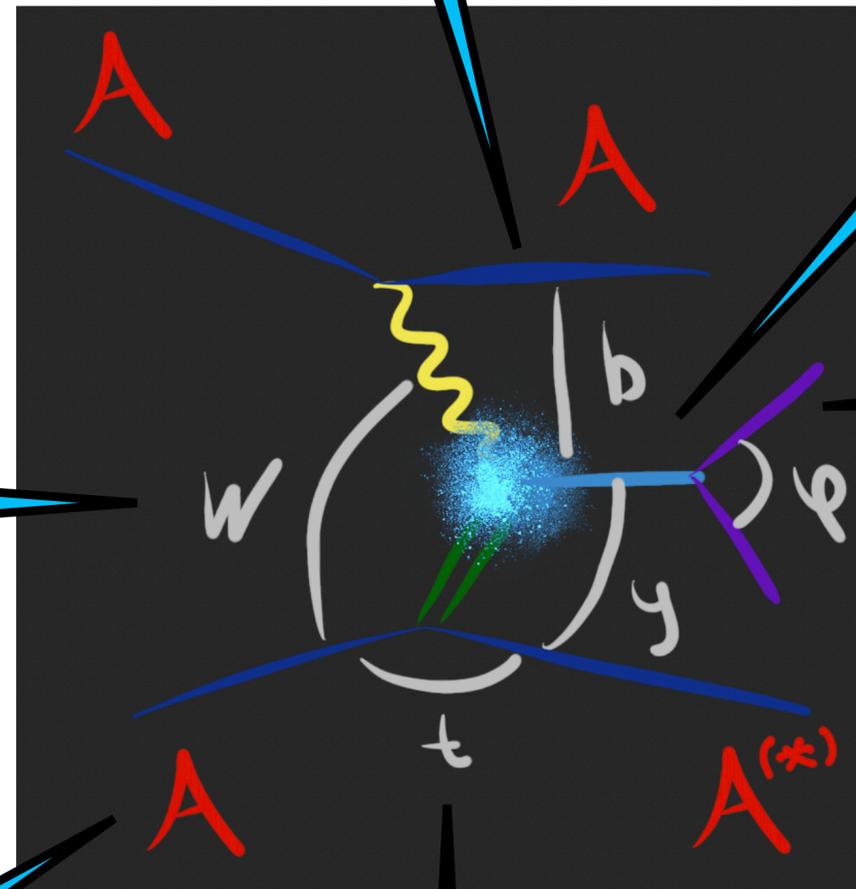
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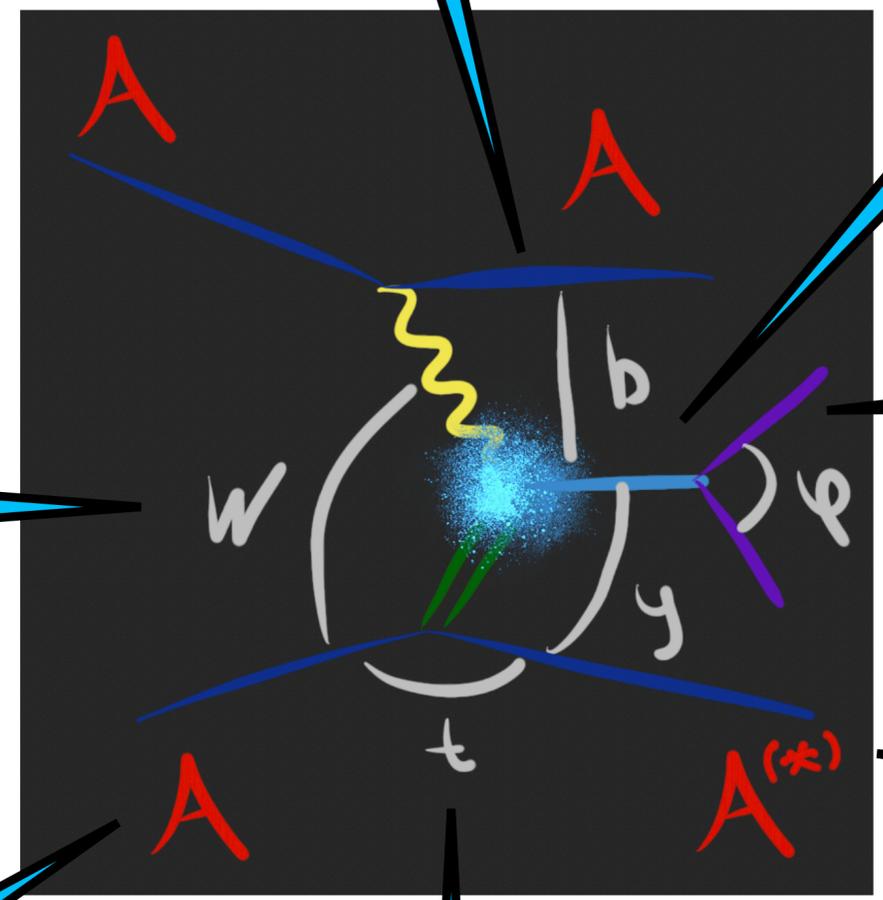
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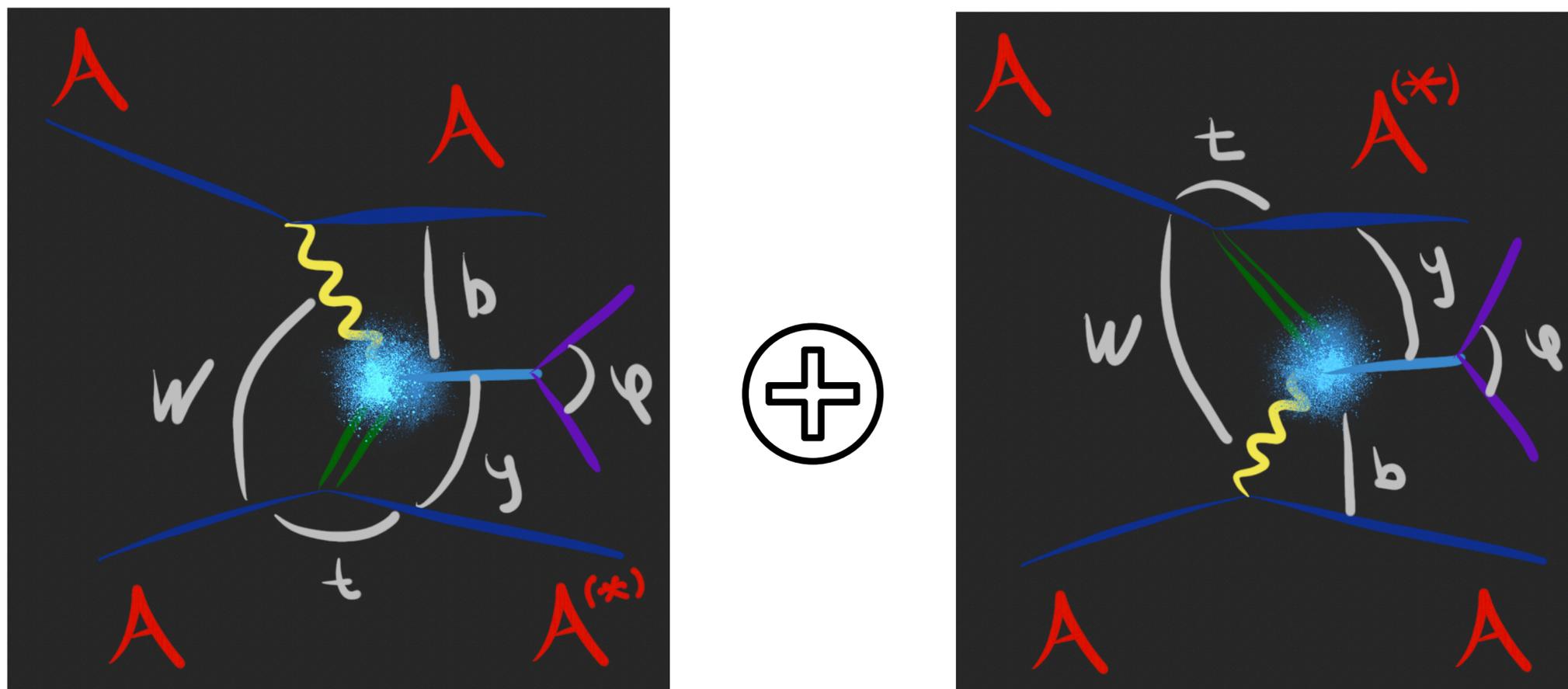
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All of these observables have been measure at RHIC+LHC 😊



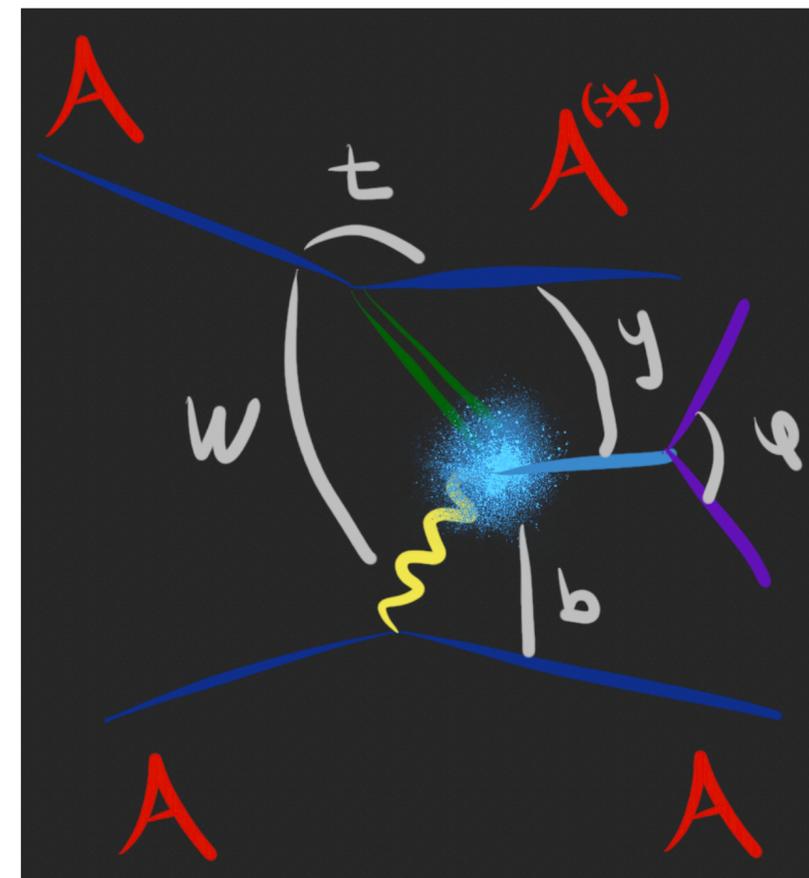
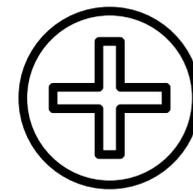
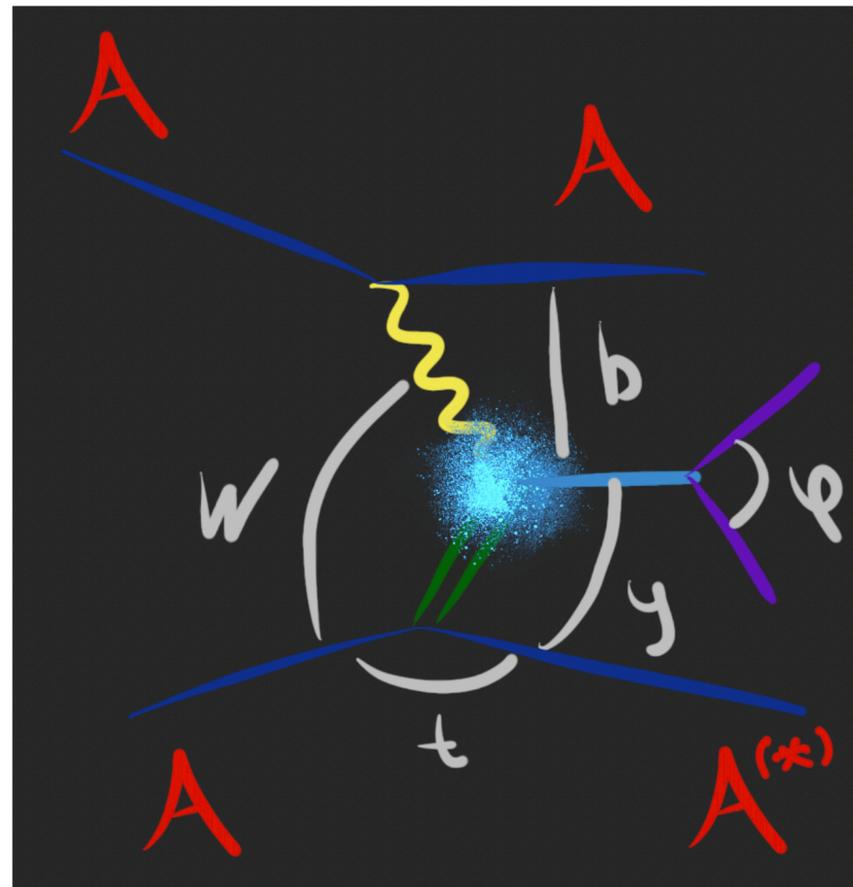
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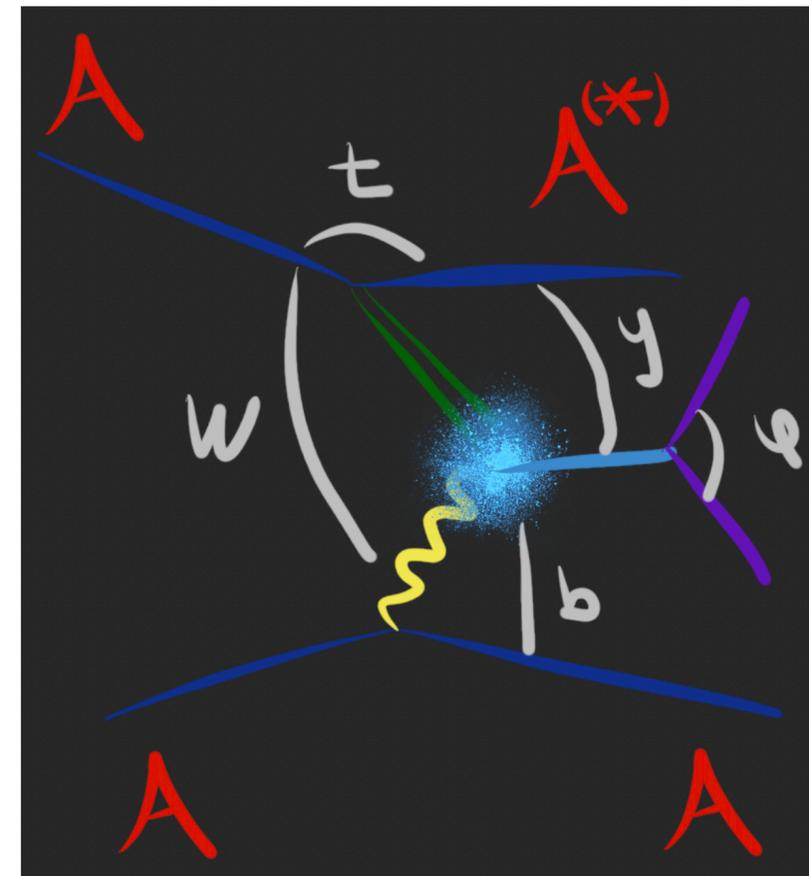
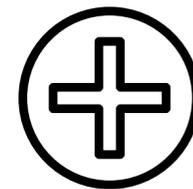
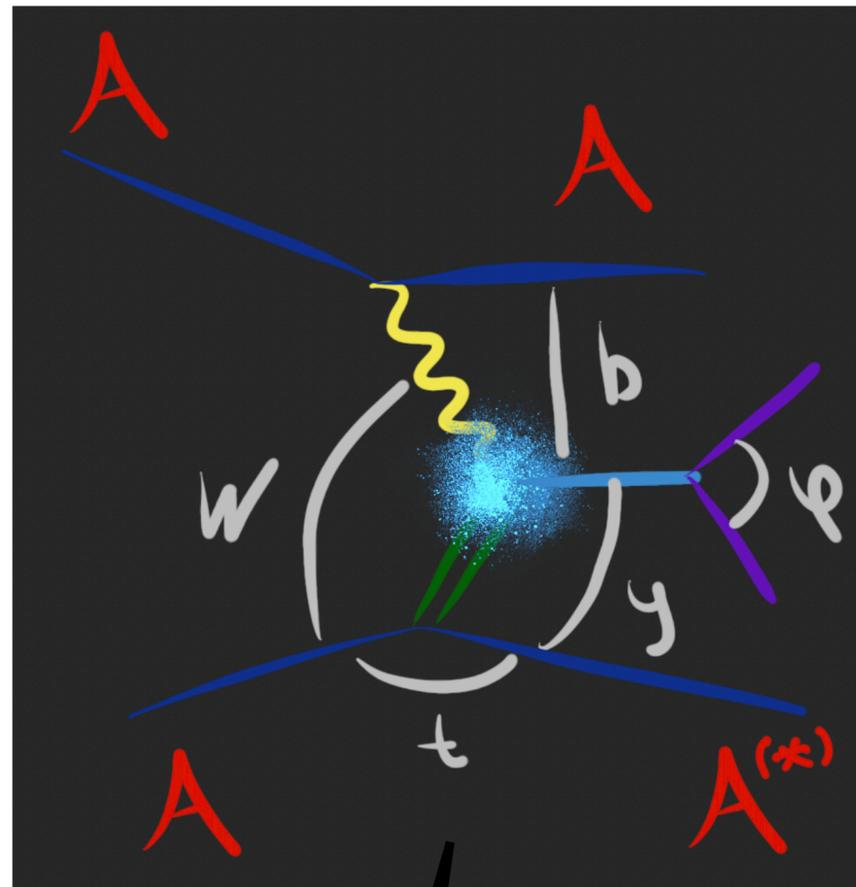
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The interference produces new angular correlations

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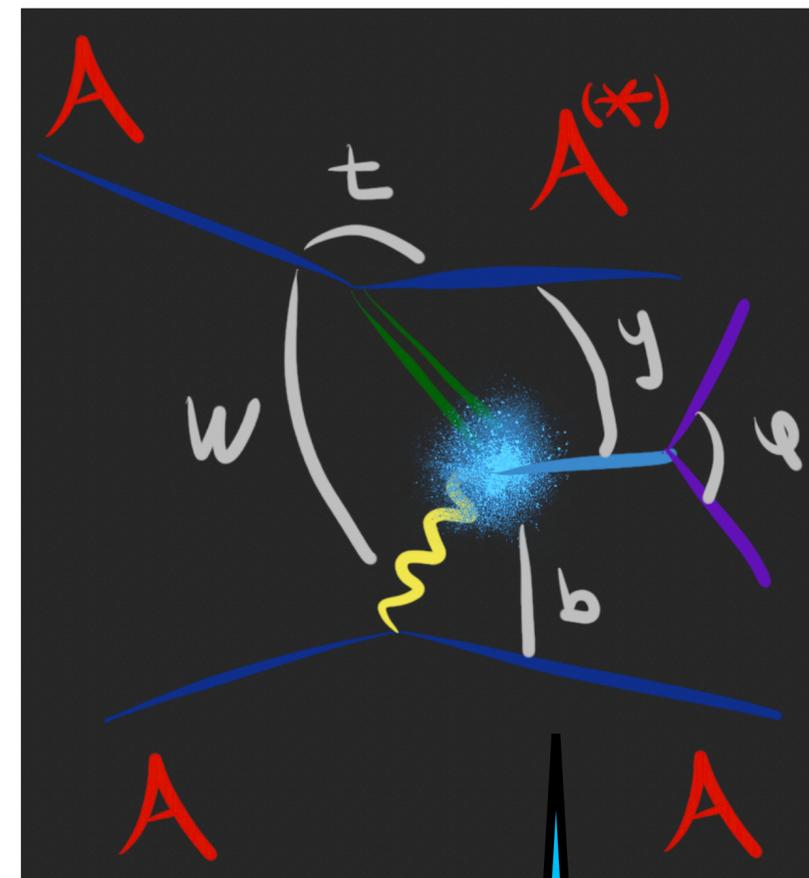
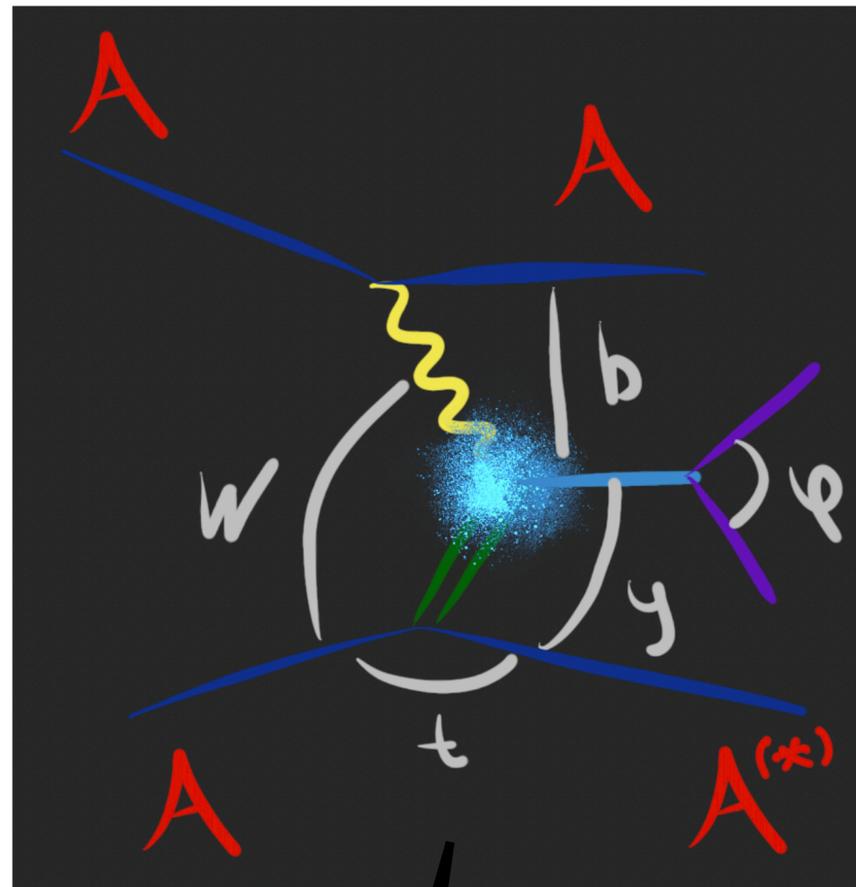


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The effects are more important at small  $|t|$  where the interference is destructive

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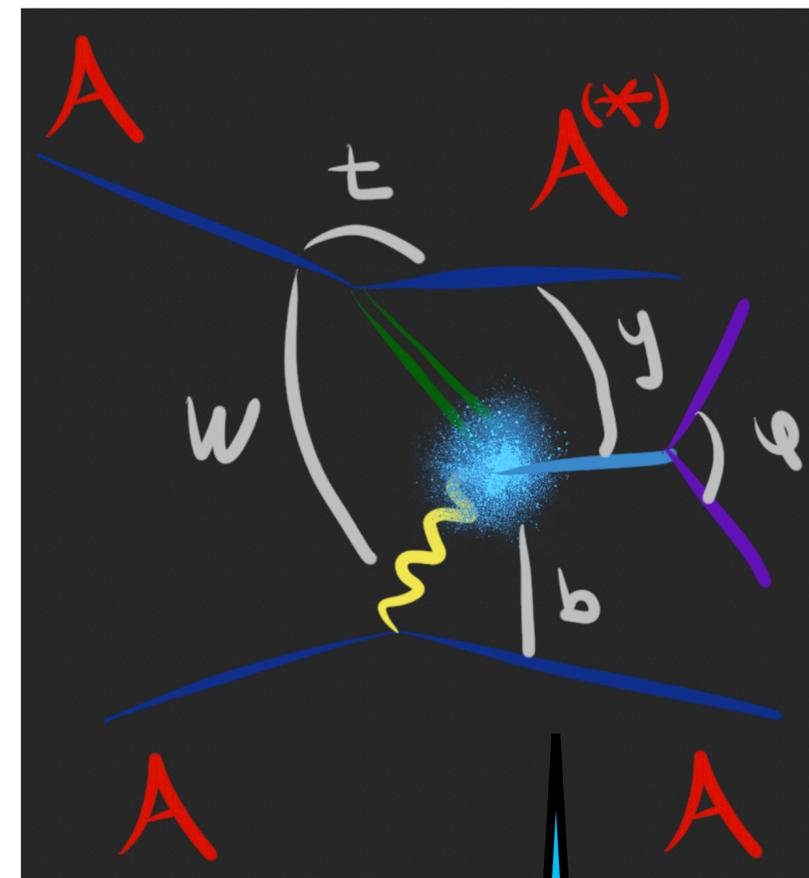
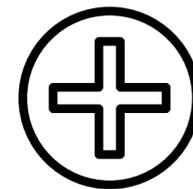
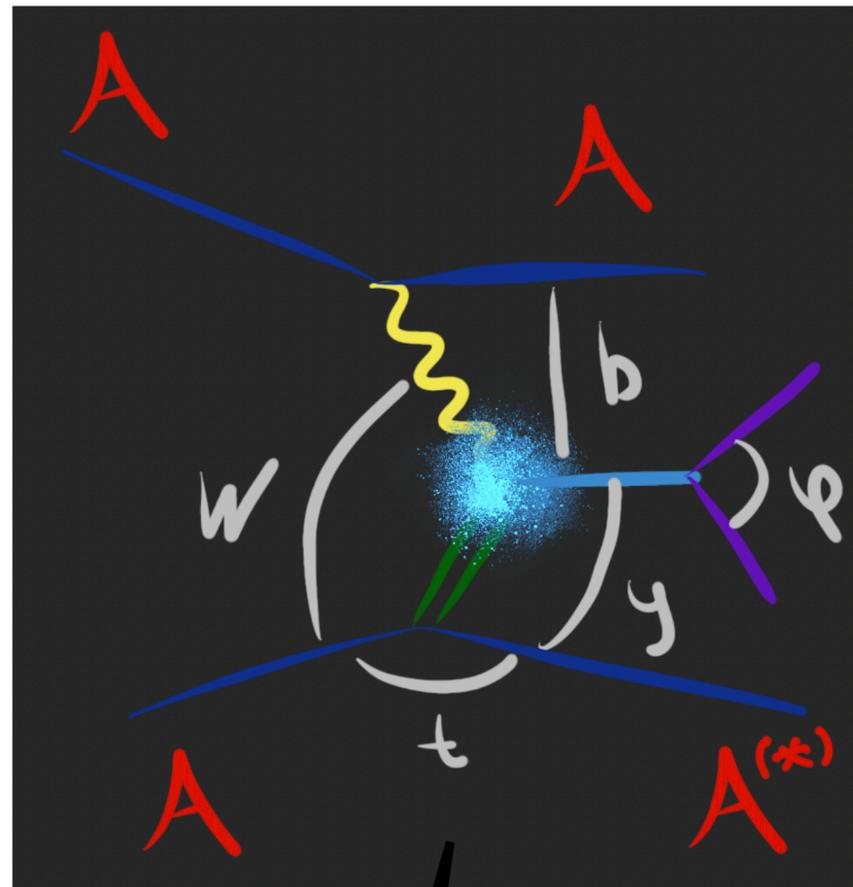
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The effects are more important at small  $|t|$  where the interference is destructive

Interference depends on the impact parameter

The interference produces new angular correlations

Also these effects been measured at RHIC+LHC 😊

As an example, I discuss here a few results that I think will not be discussed in detail during the conference

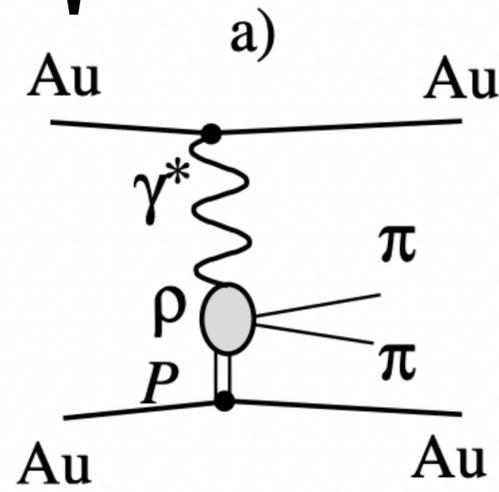
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First observation of the process at RHIC by the STAR collaboration

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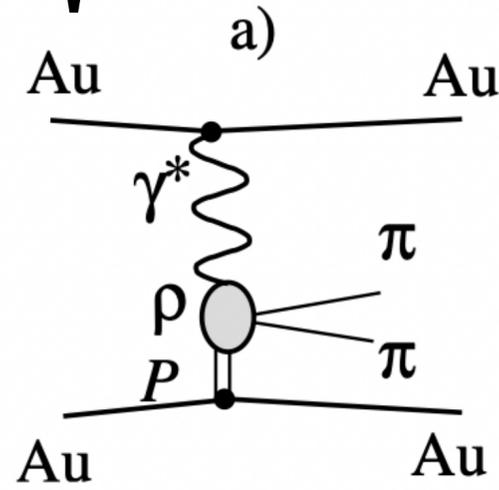
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AuAu collisions at 130 GeV per NN



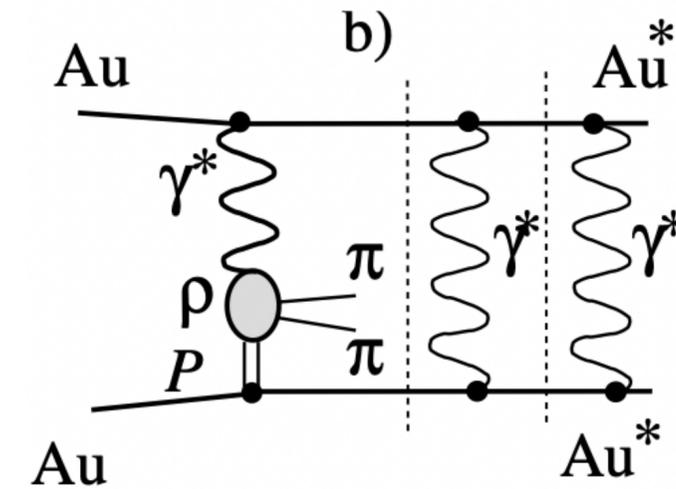
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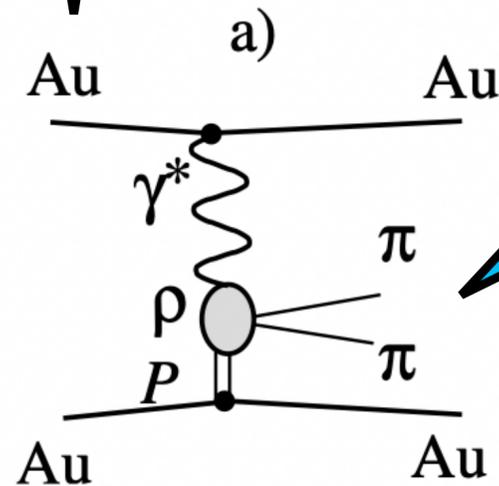
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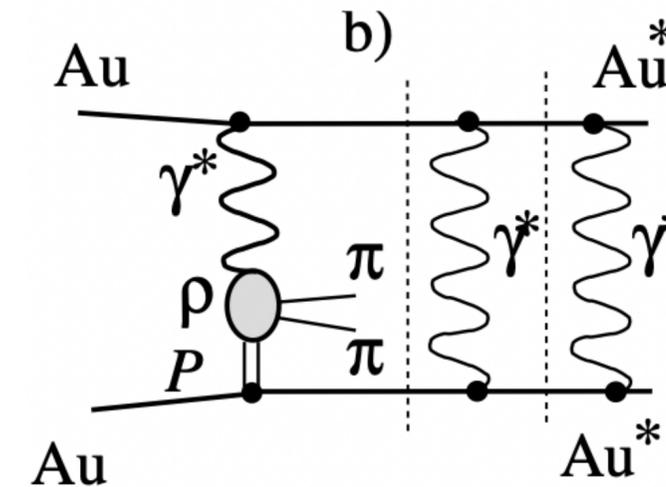
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Decay to  $\pi\pi$  almost 100% of the time

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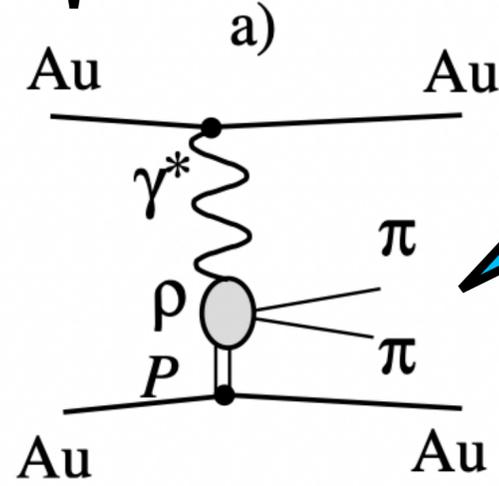


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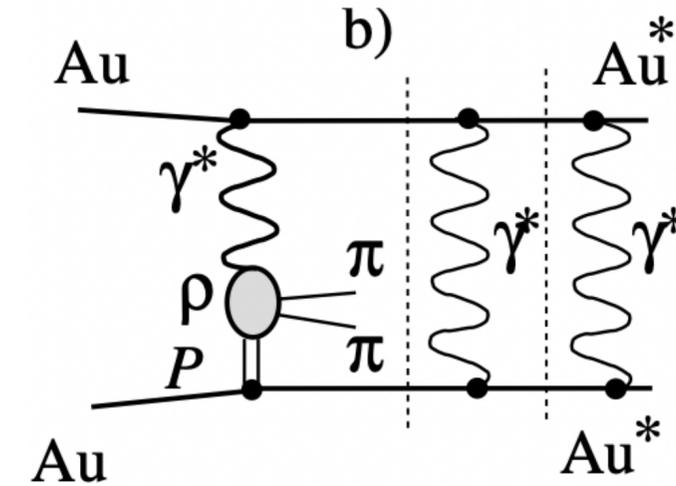
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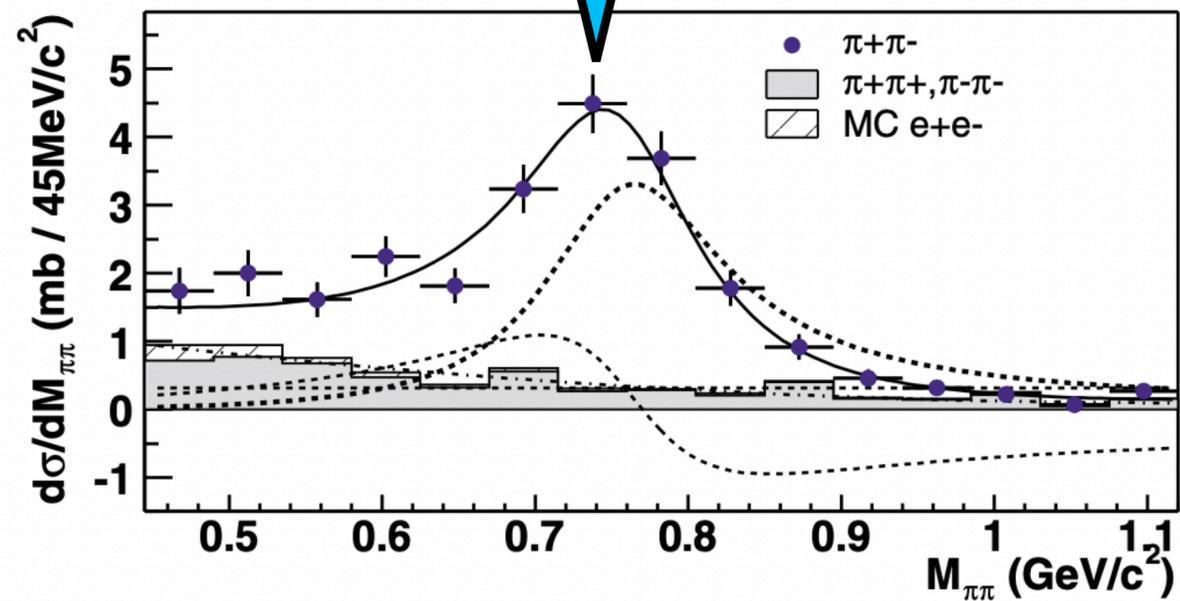
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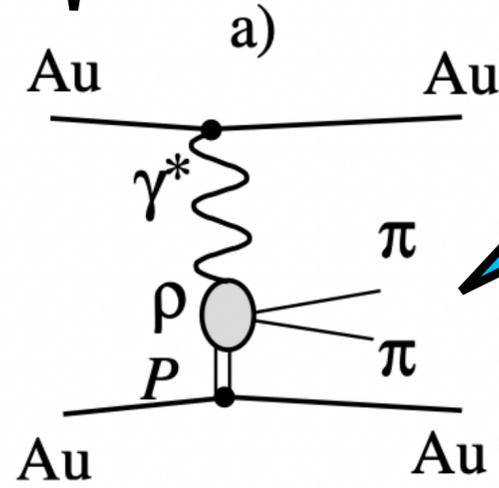
Broad resonance: need models to take into account continuum production



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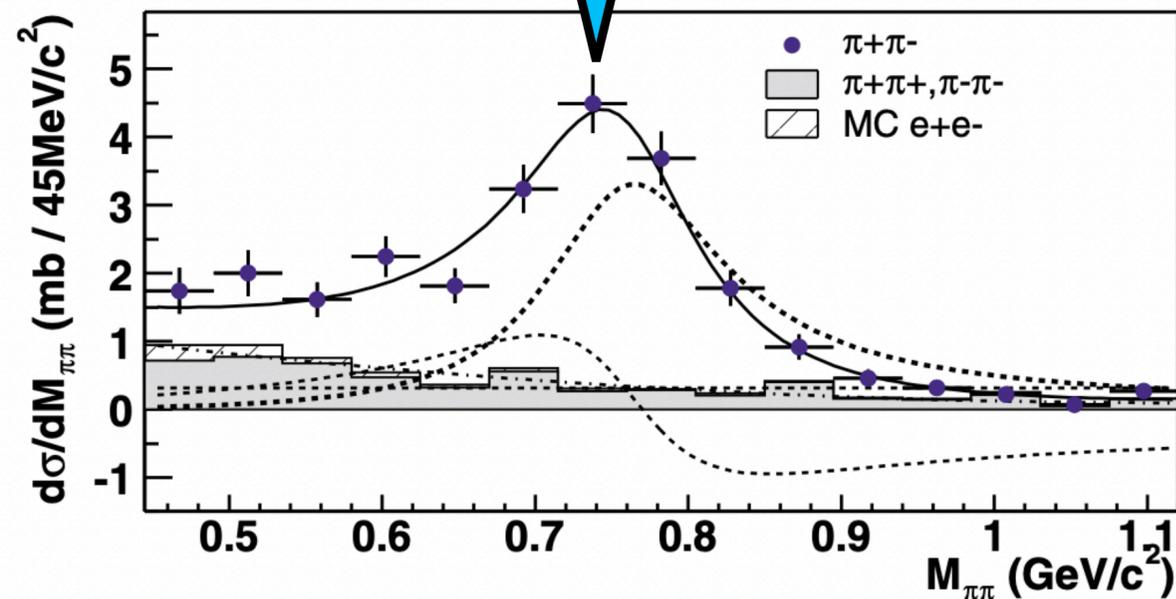


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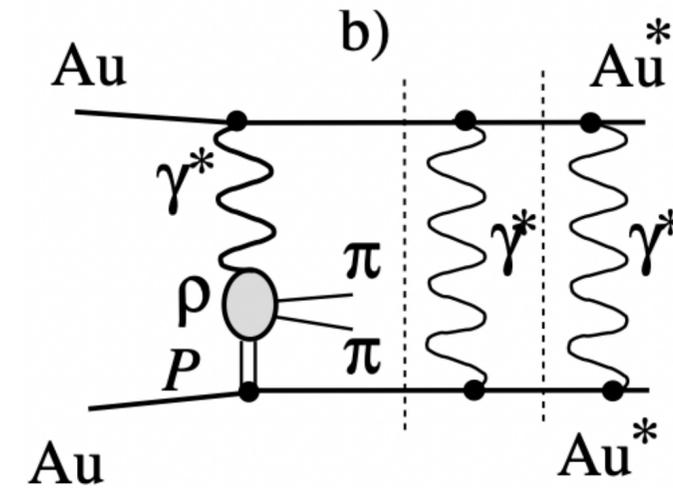
E.g. Soding or Ross-Stodolky models

Soding, P Phys.Lett. 19 (1966) 702-704  
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Broad resonance: need models to take into account continuum production



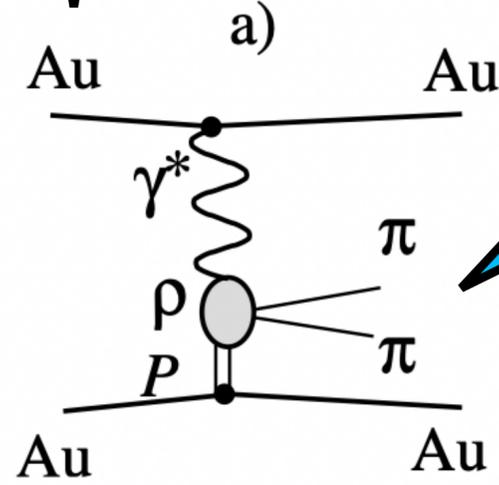
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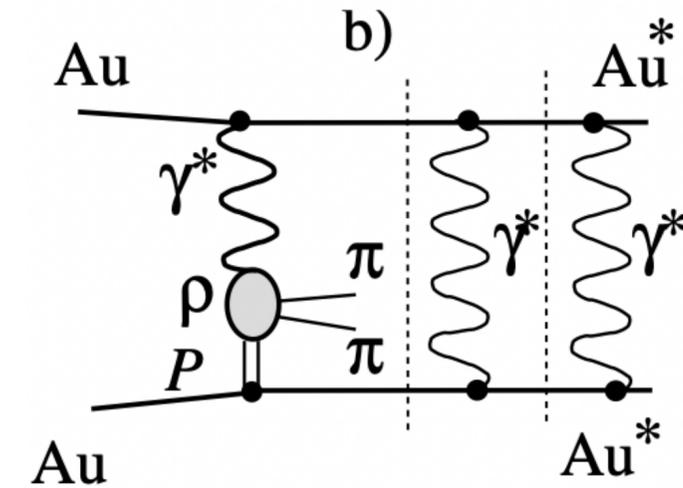
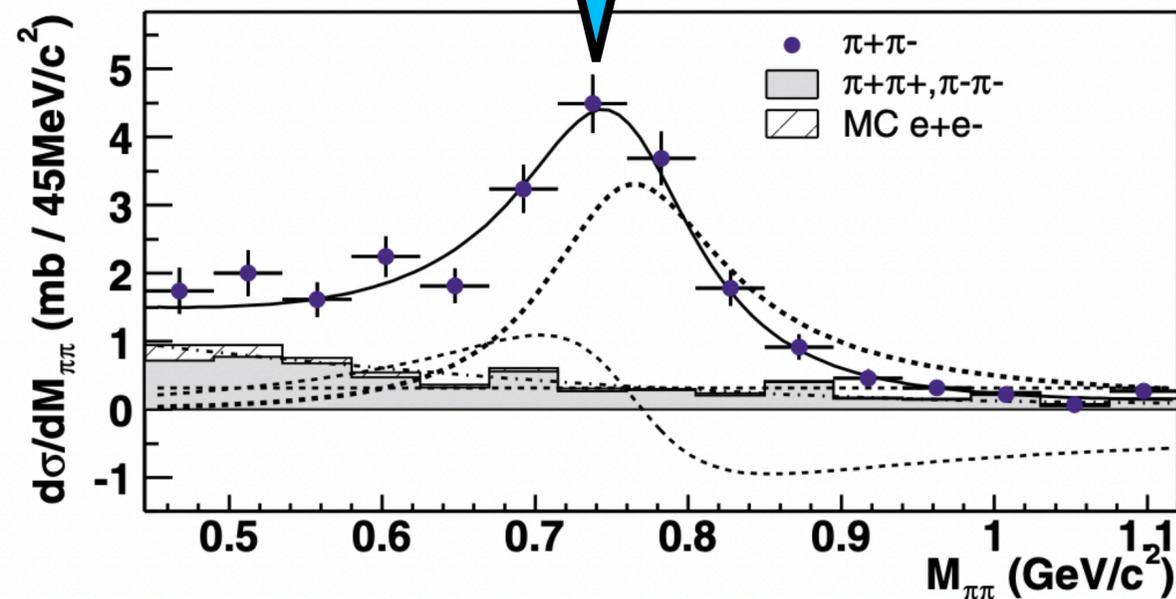


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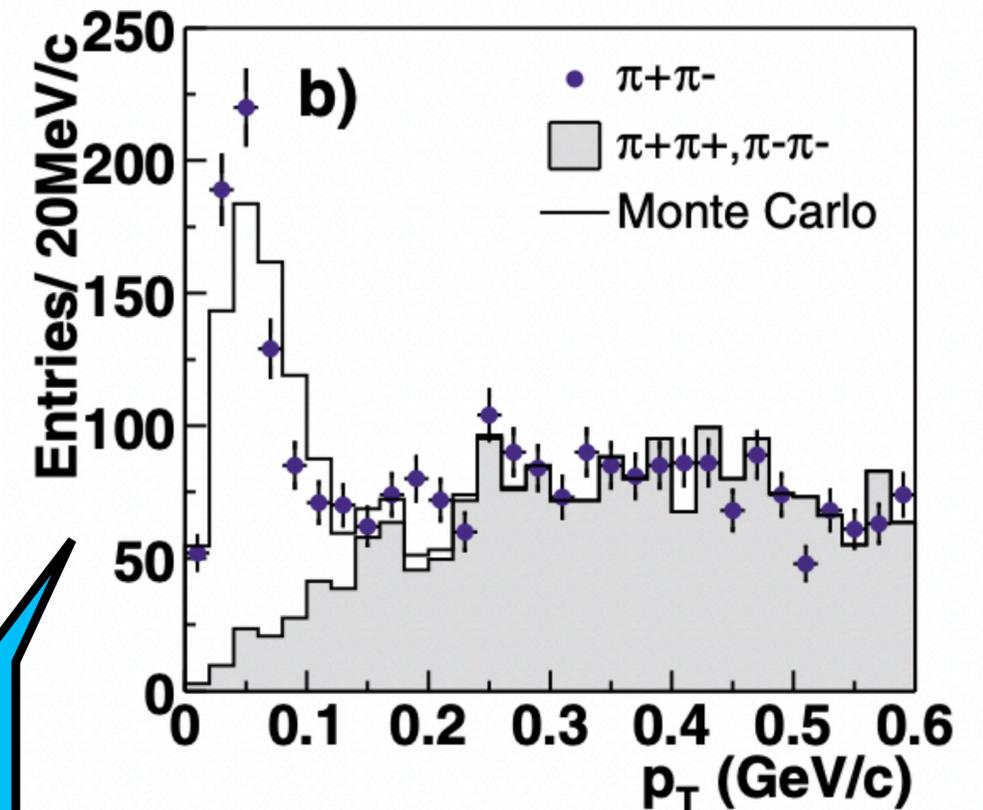
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Typical shape of the transverse momentum distribution (below 0.1 GeV/c)

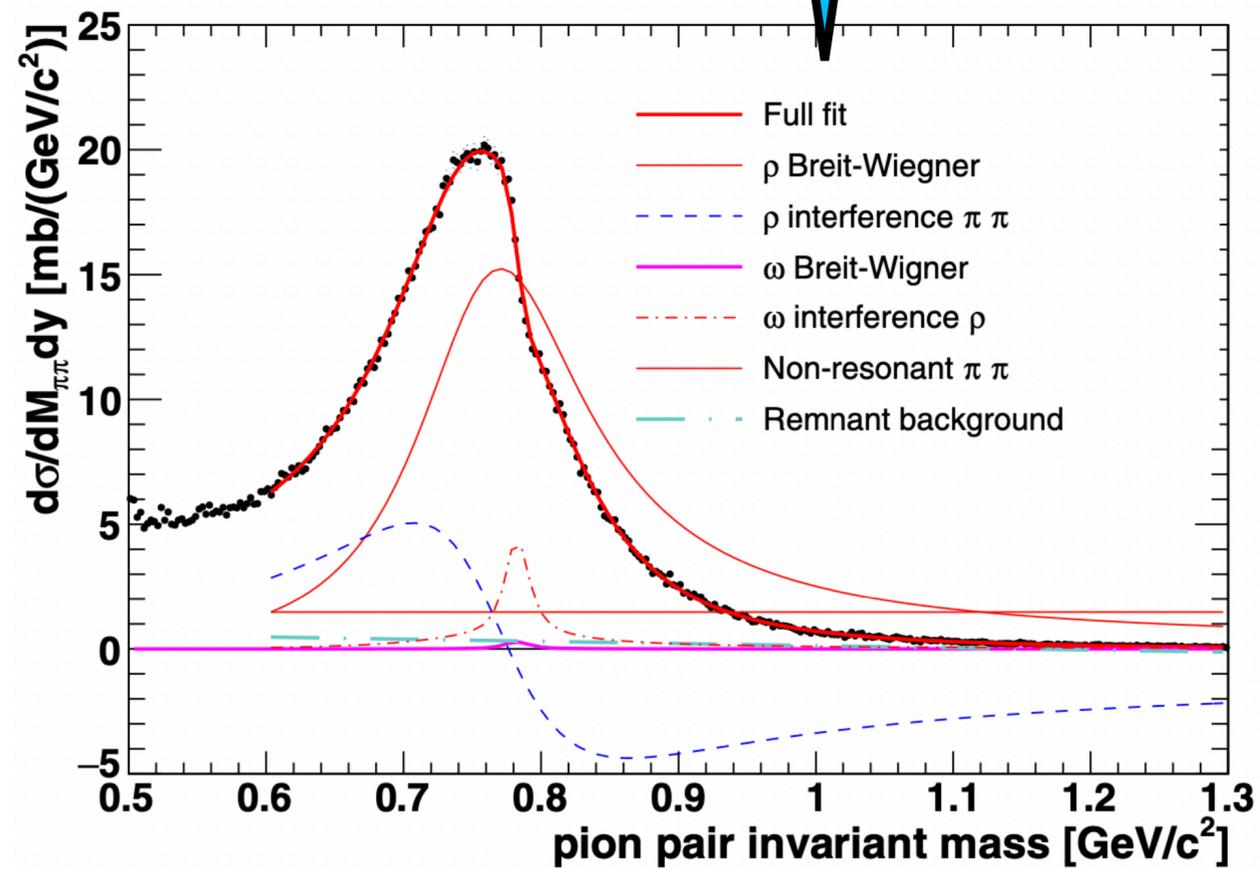
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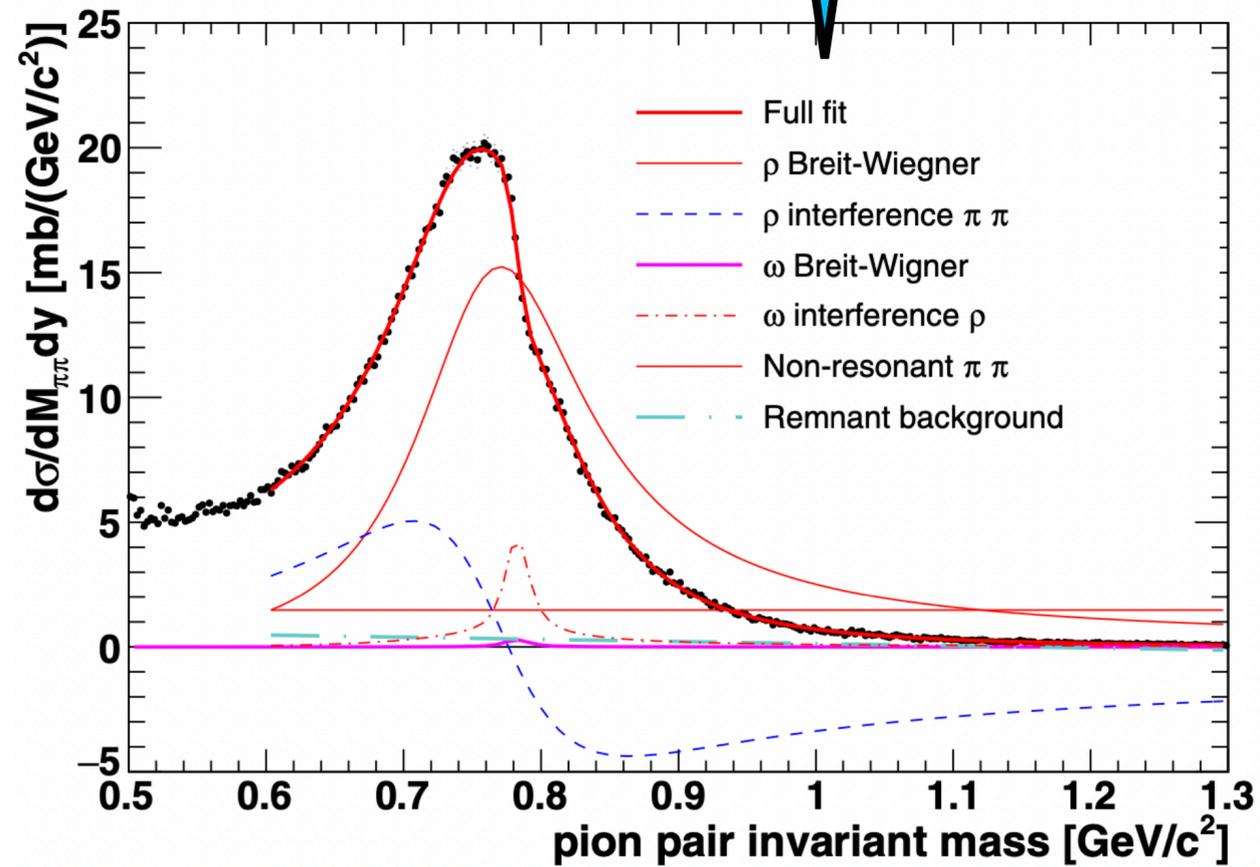
Data is sensitive to the contribution of other processes



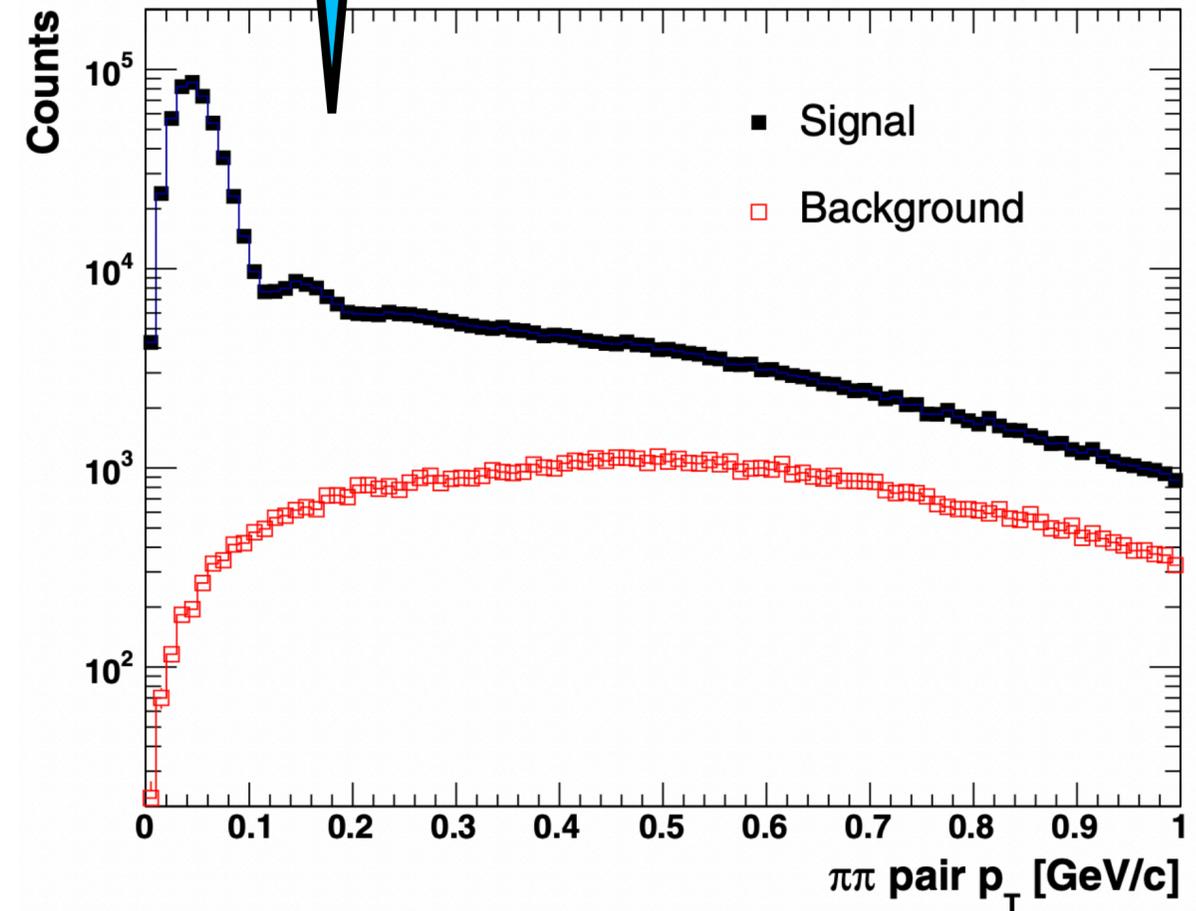
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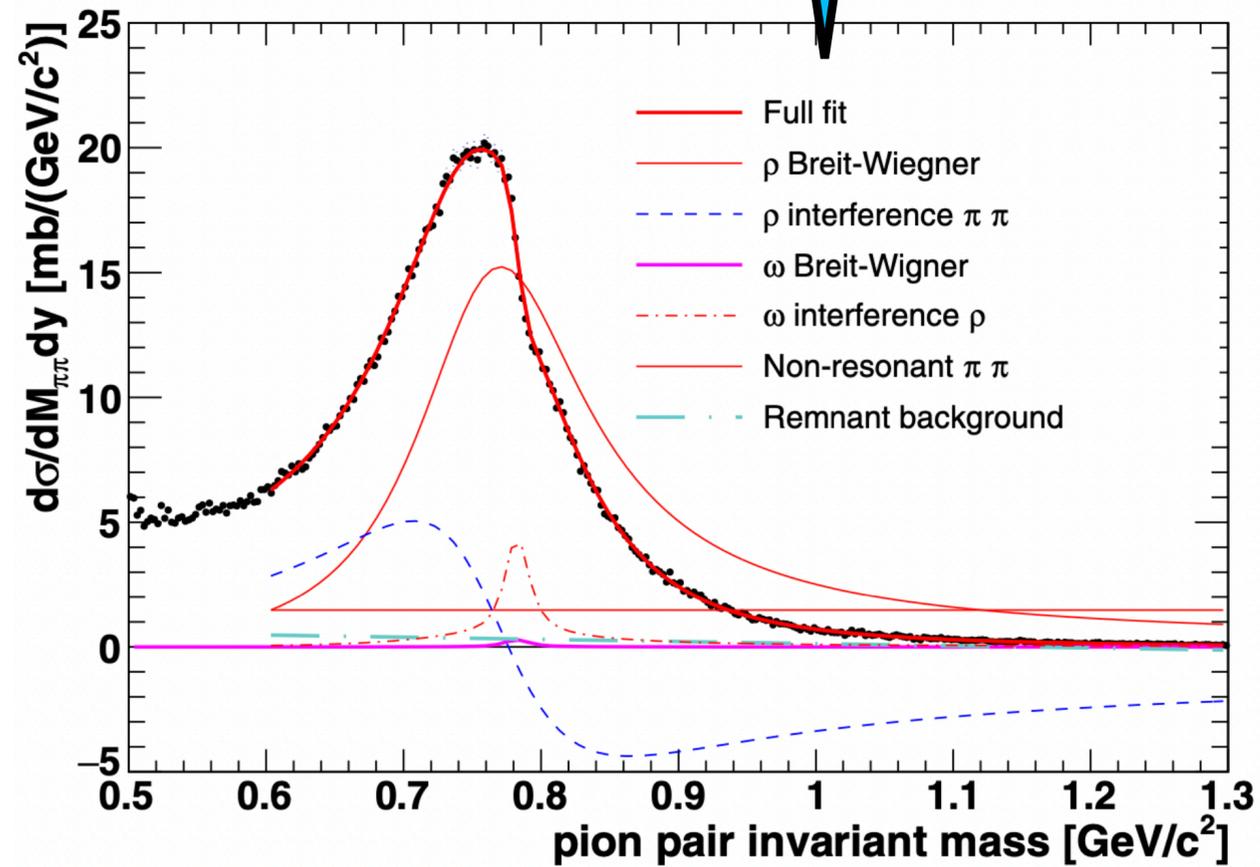
Second diffraction peak visible!



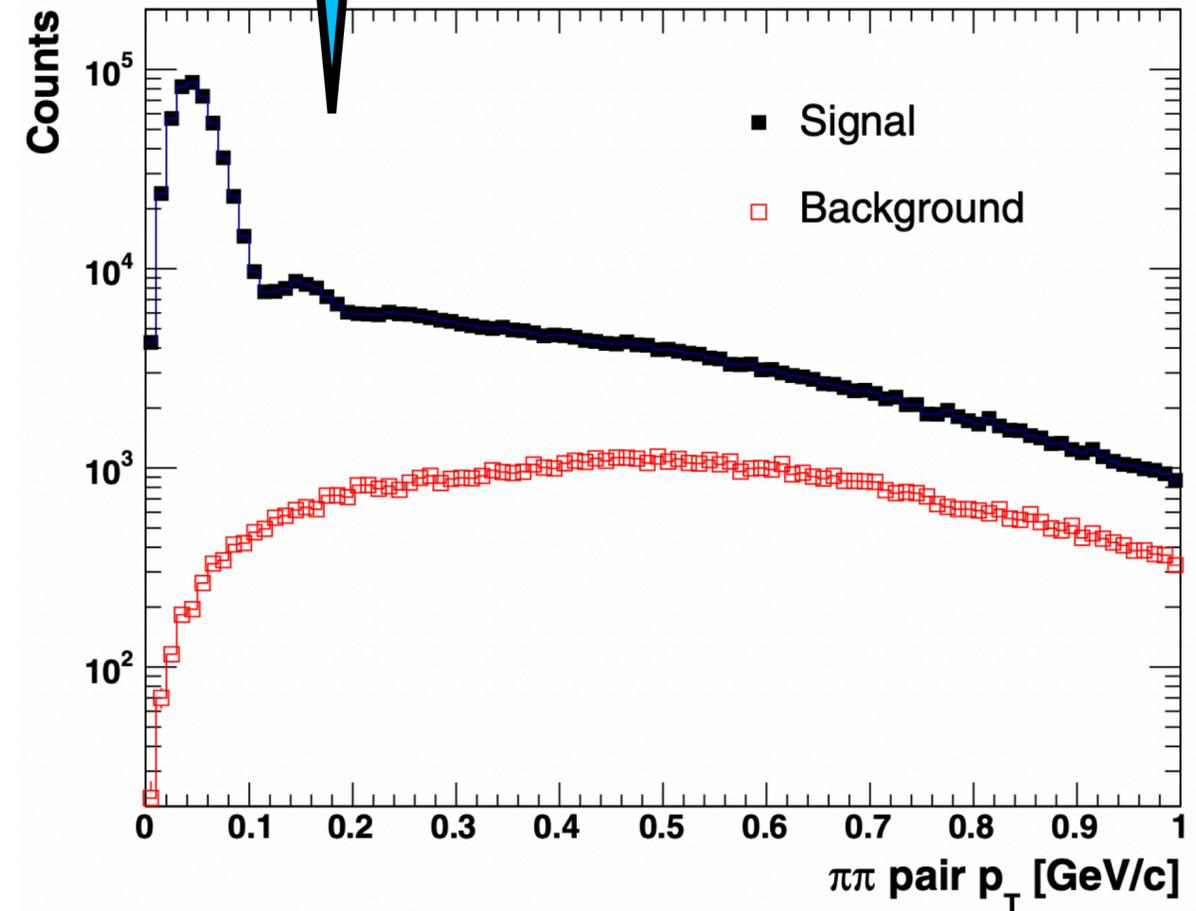
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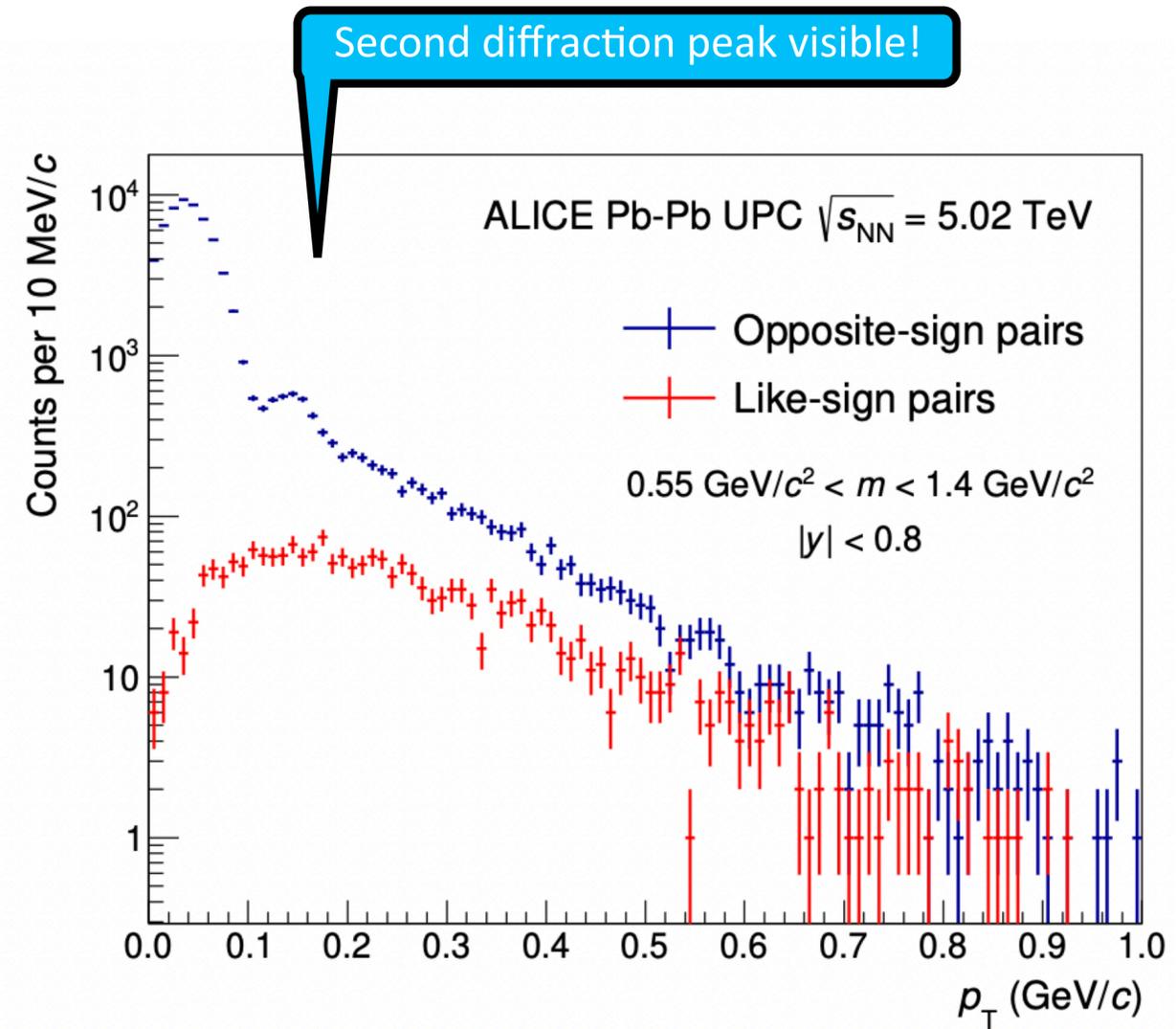
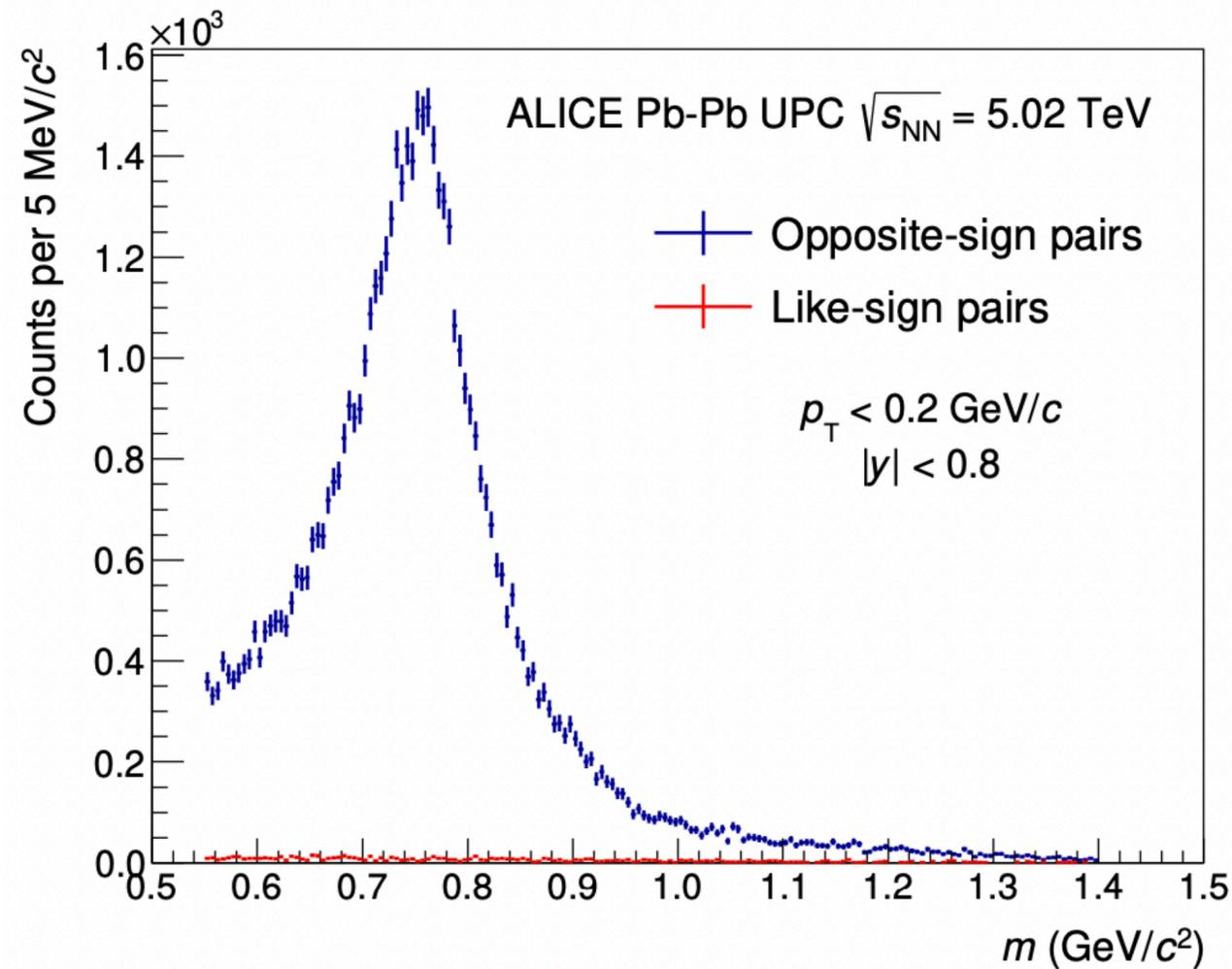
Other measurements available at 62.4 GeV per NN

# Energy dependence of coherent $\rho^0$ production: PbPb in ALICE

Coherent production in 2020: PbPb at 5.02 TeV per NN

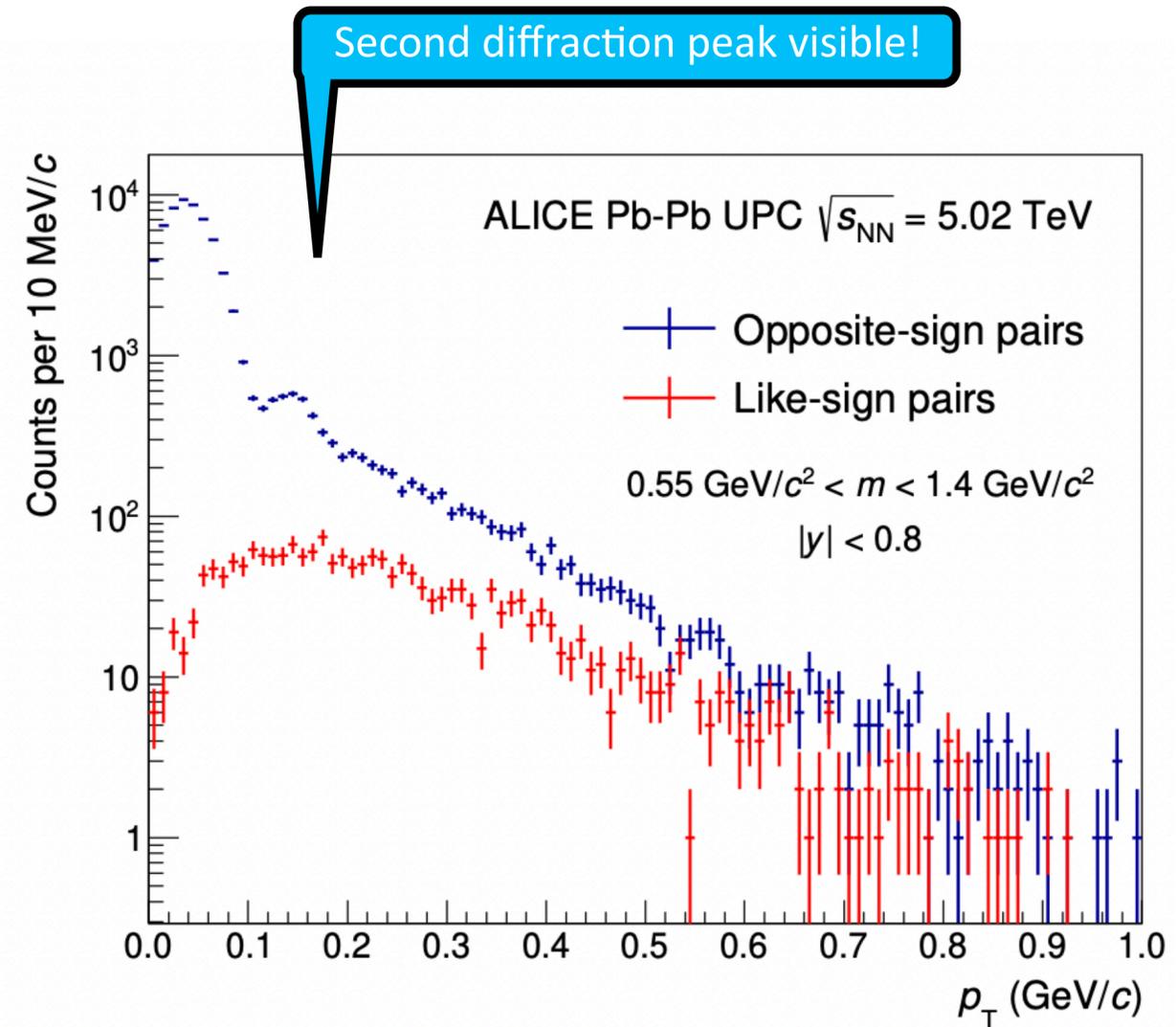
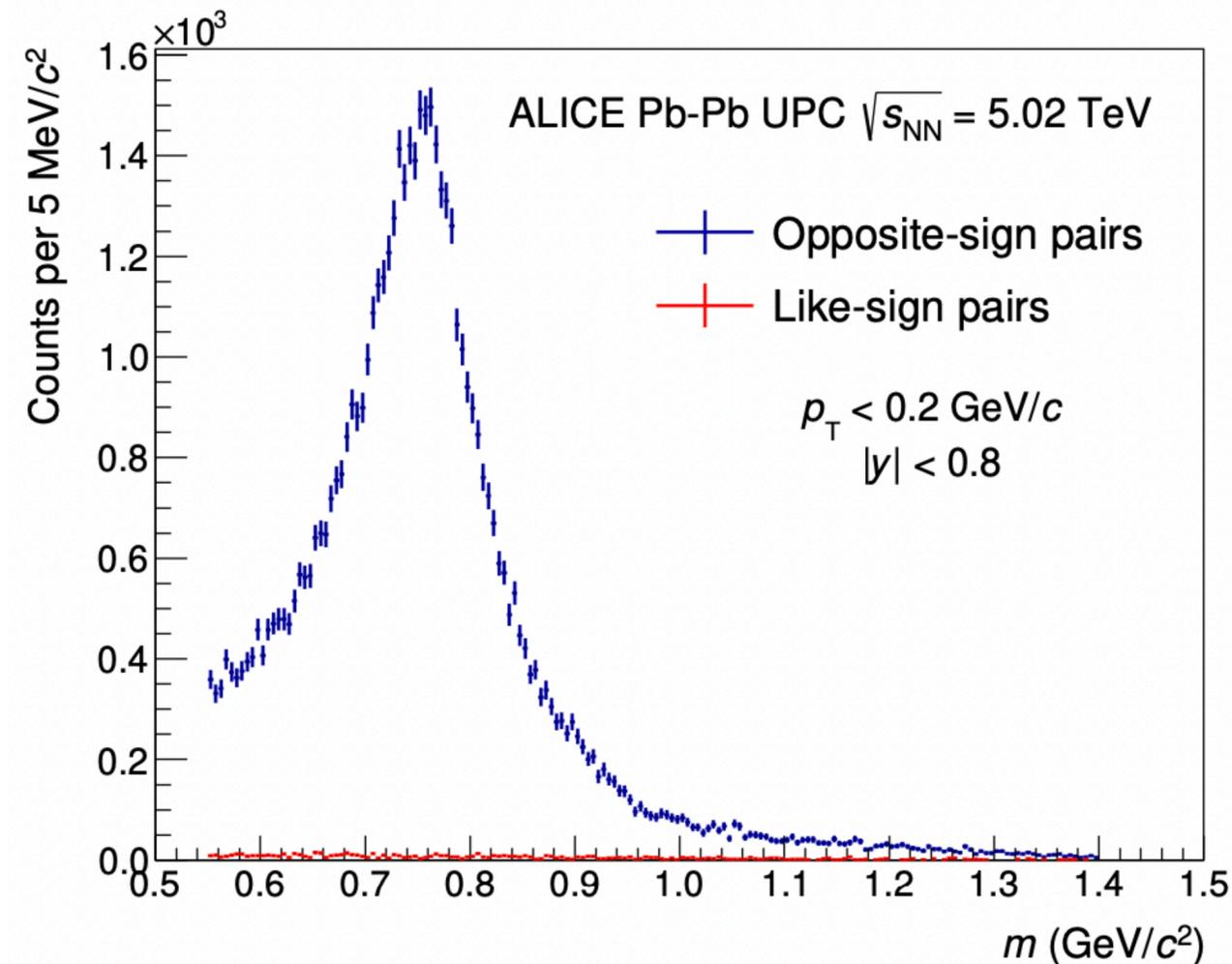
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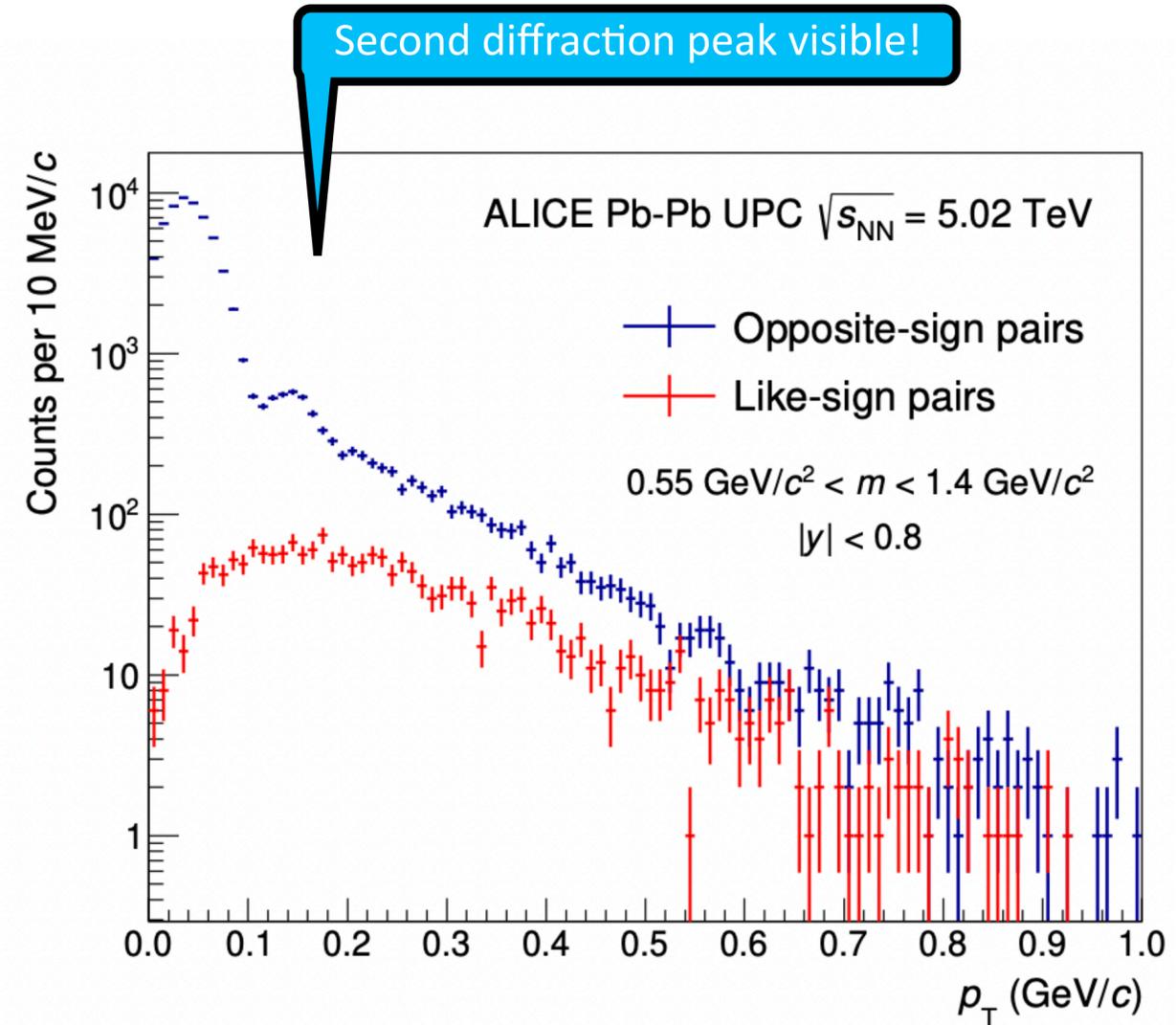
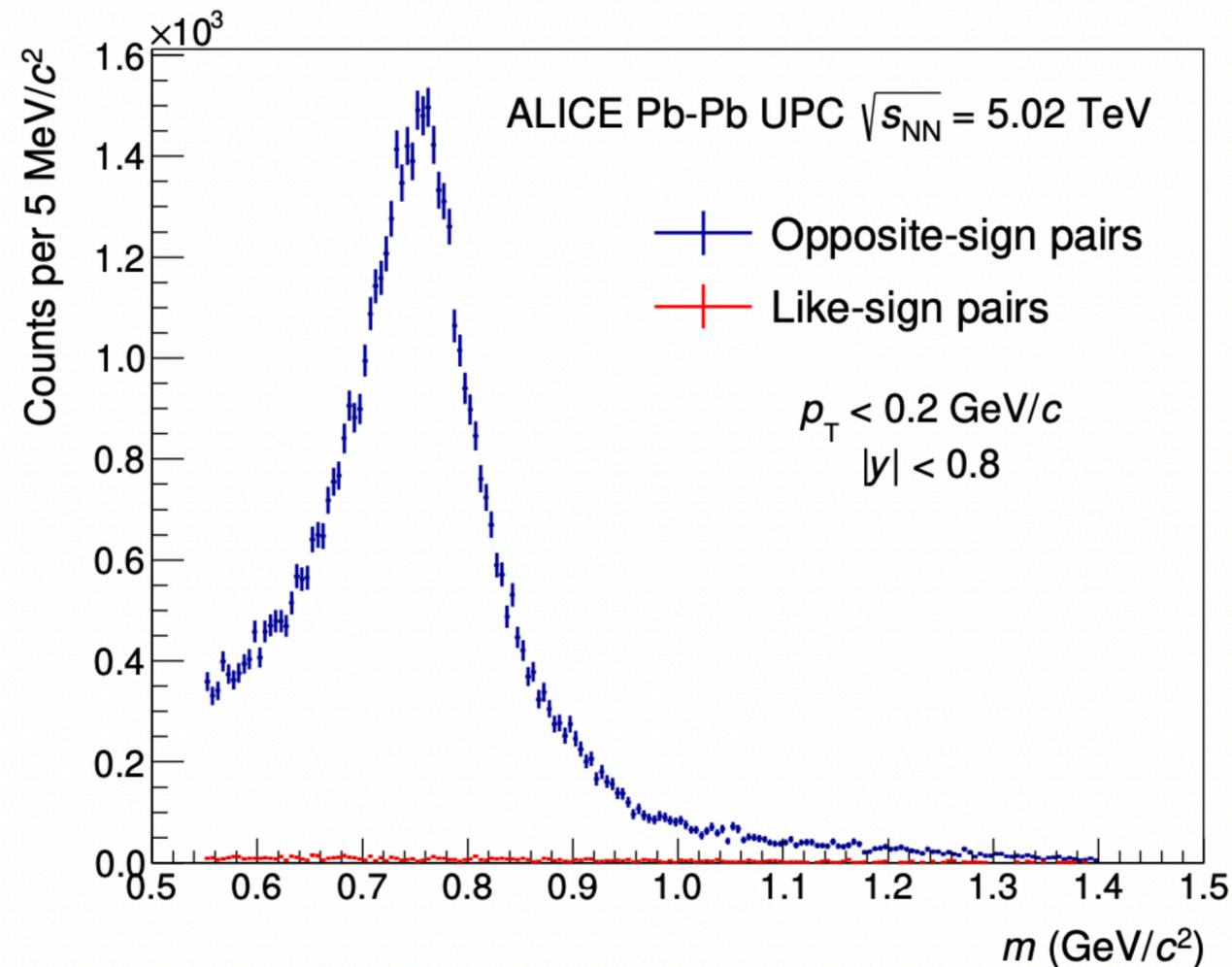
Coherent production in 2020: PbPb at 5.02 TeV per NN



Trigger on tracks and vetoes, measuring in EMD classes to test our knowledge of the photon flux

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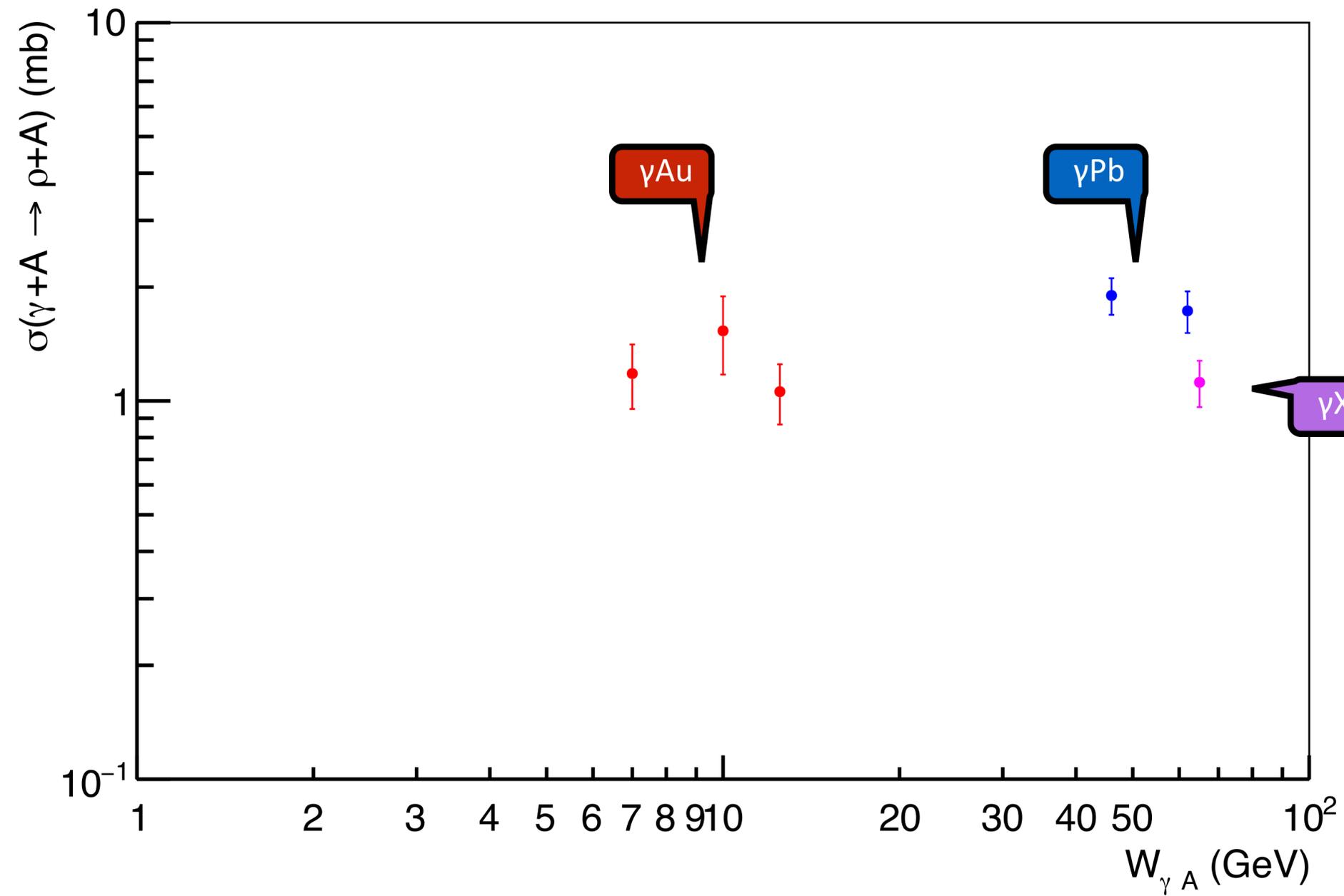
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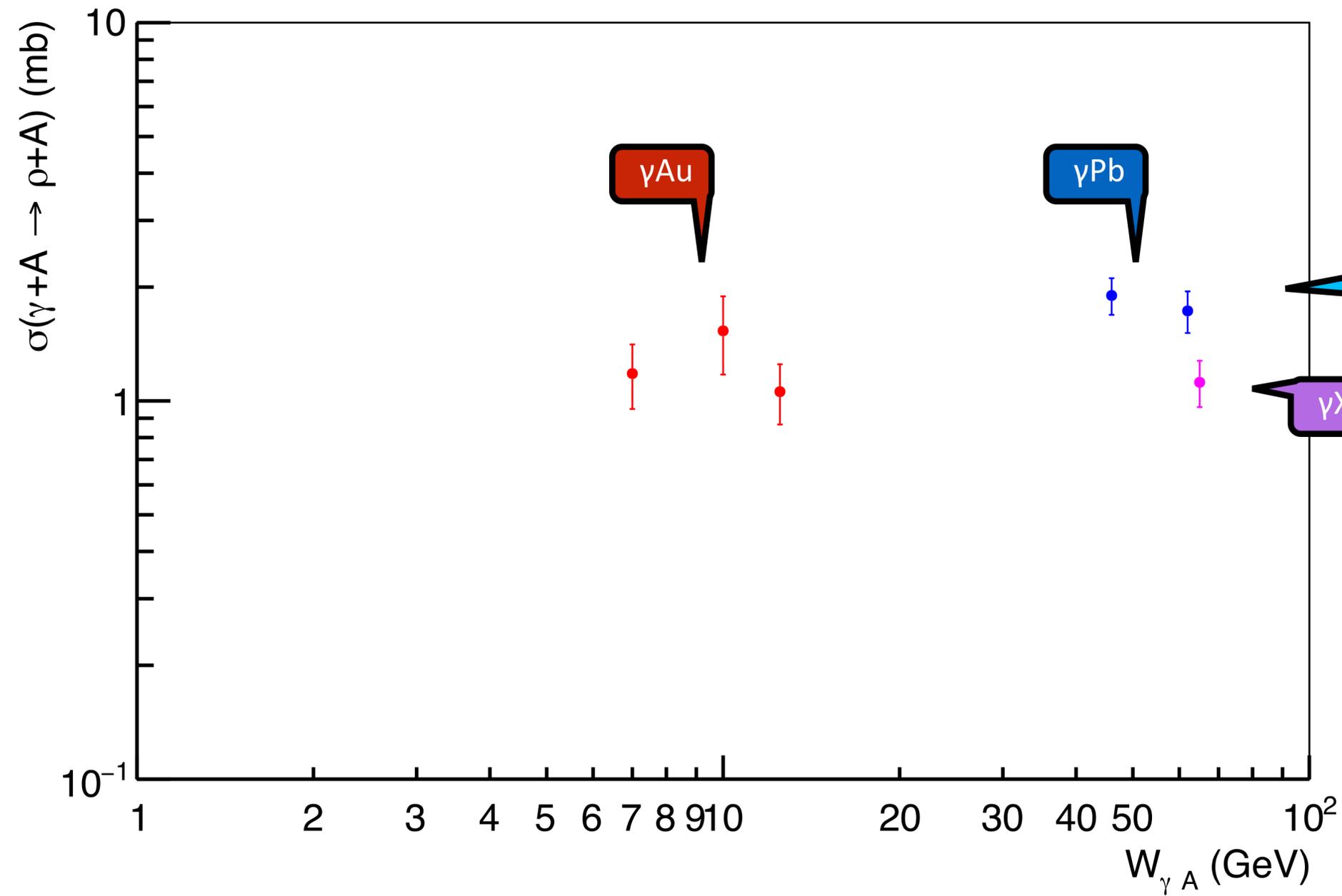
Trigger on tracks and vetoes, measuring in EMD classes to test our knowledge of the photon flux

Other measurements available at 2.76 TeV per NN

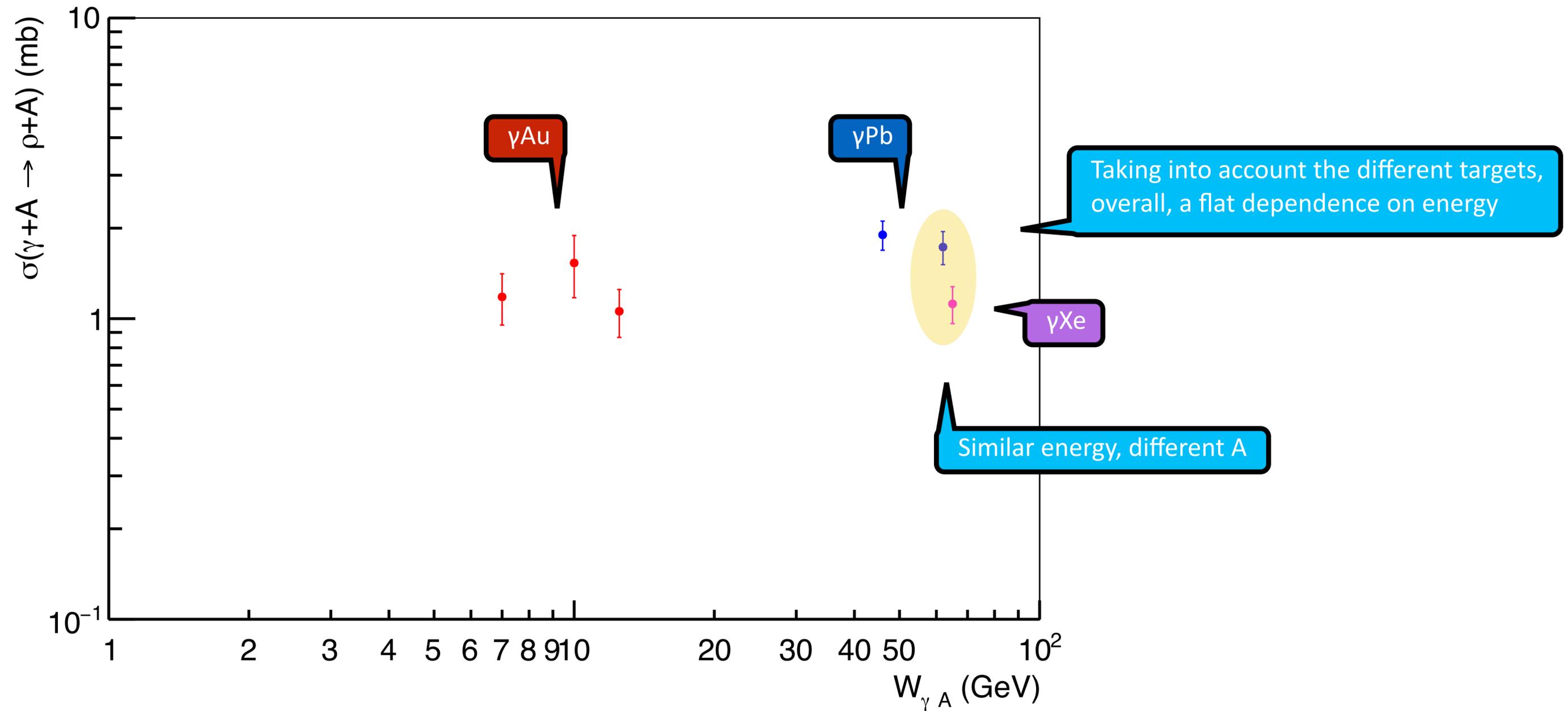
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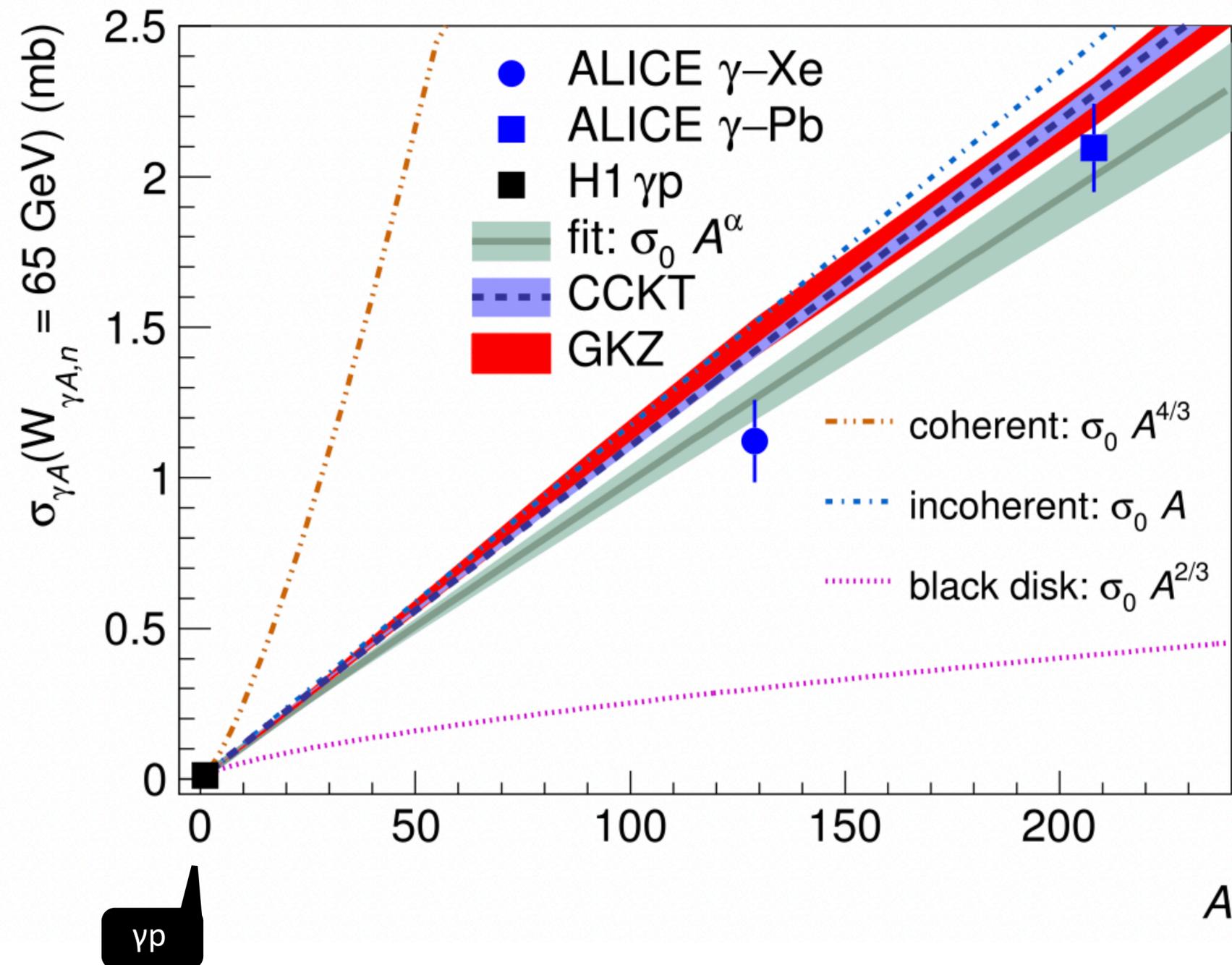
# Energy dependence of coherent $\rho^0$ production



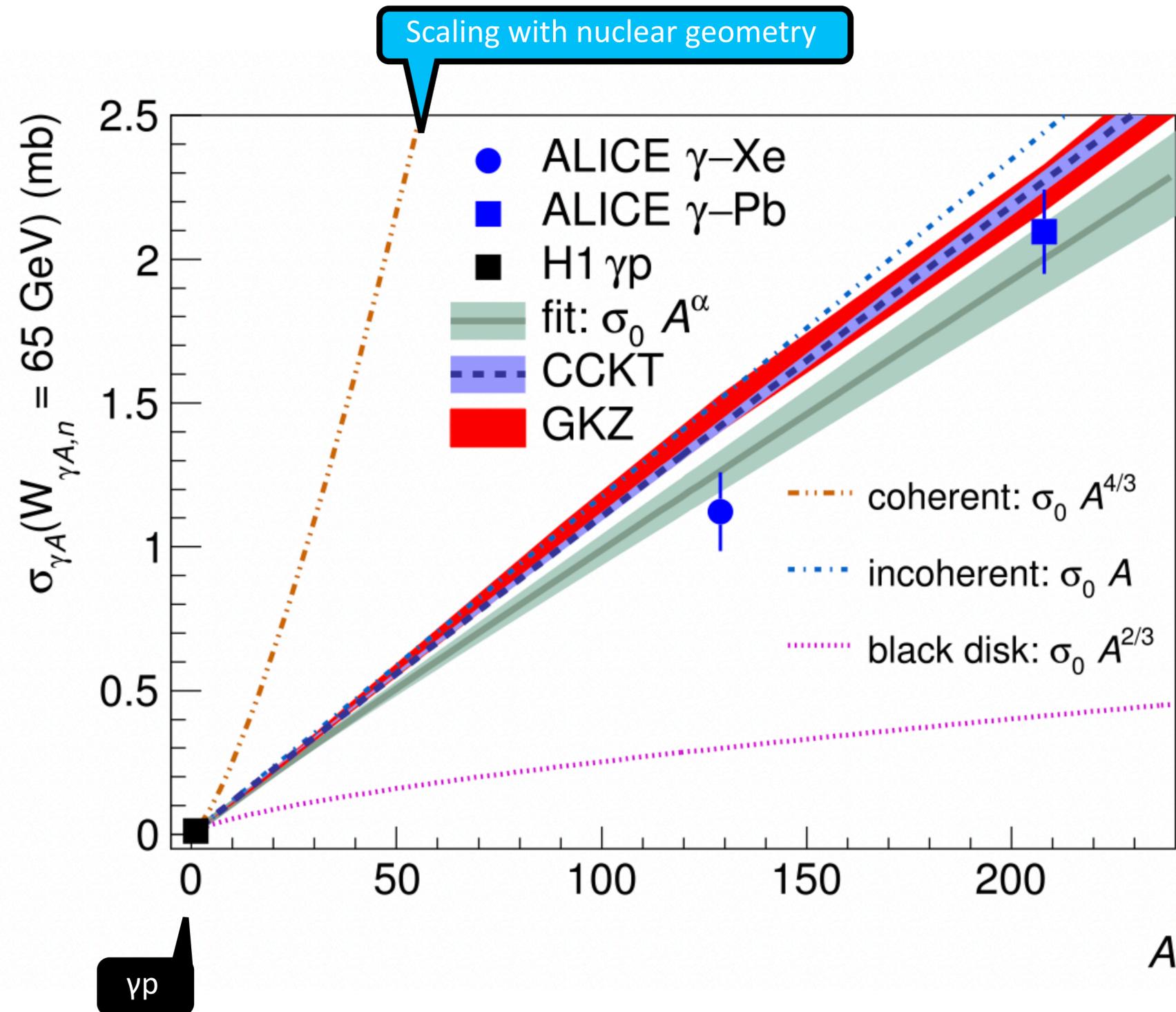
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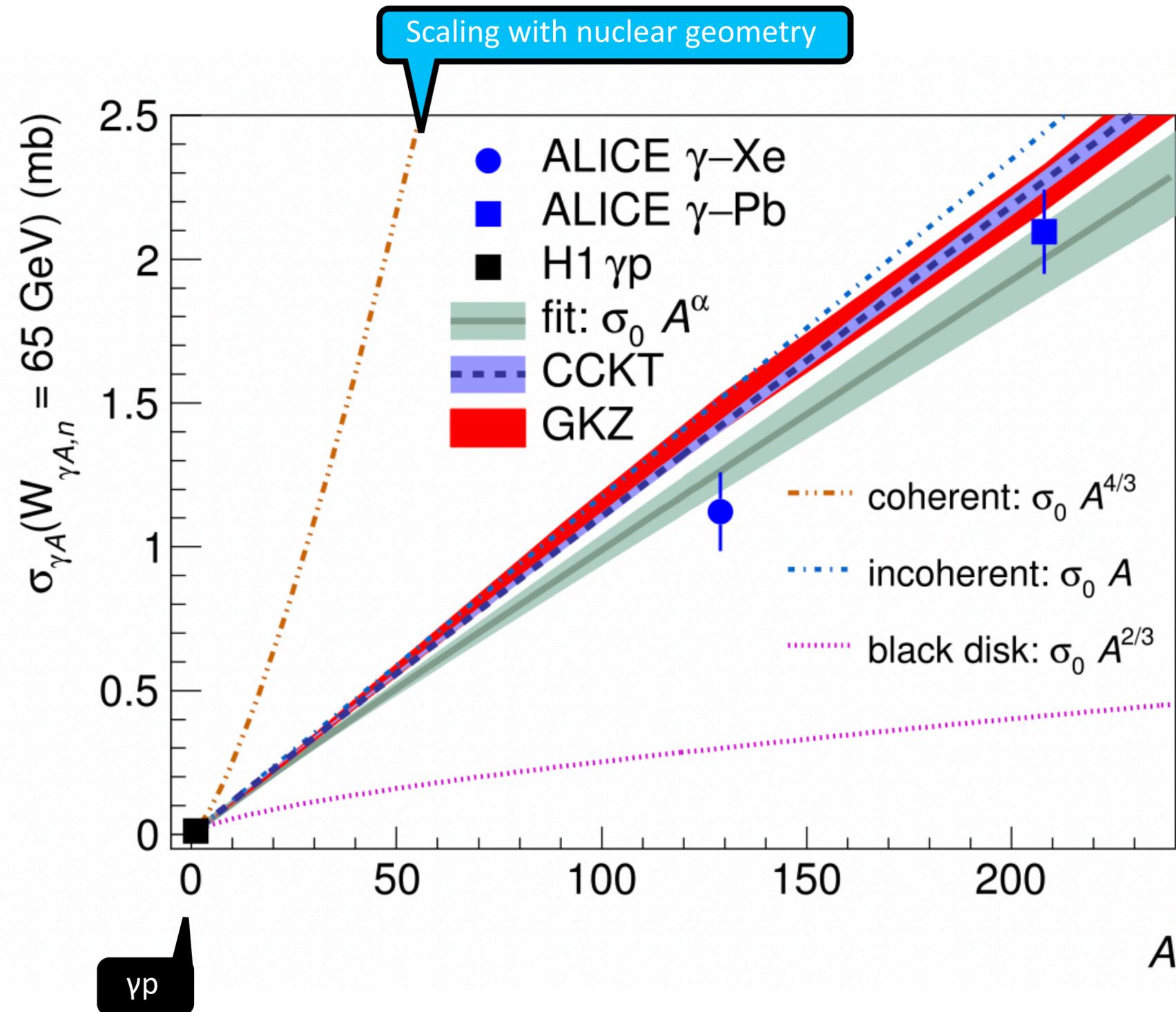
# A dependence of coherent $\rho^0$ production at high energies



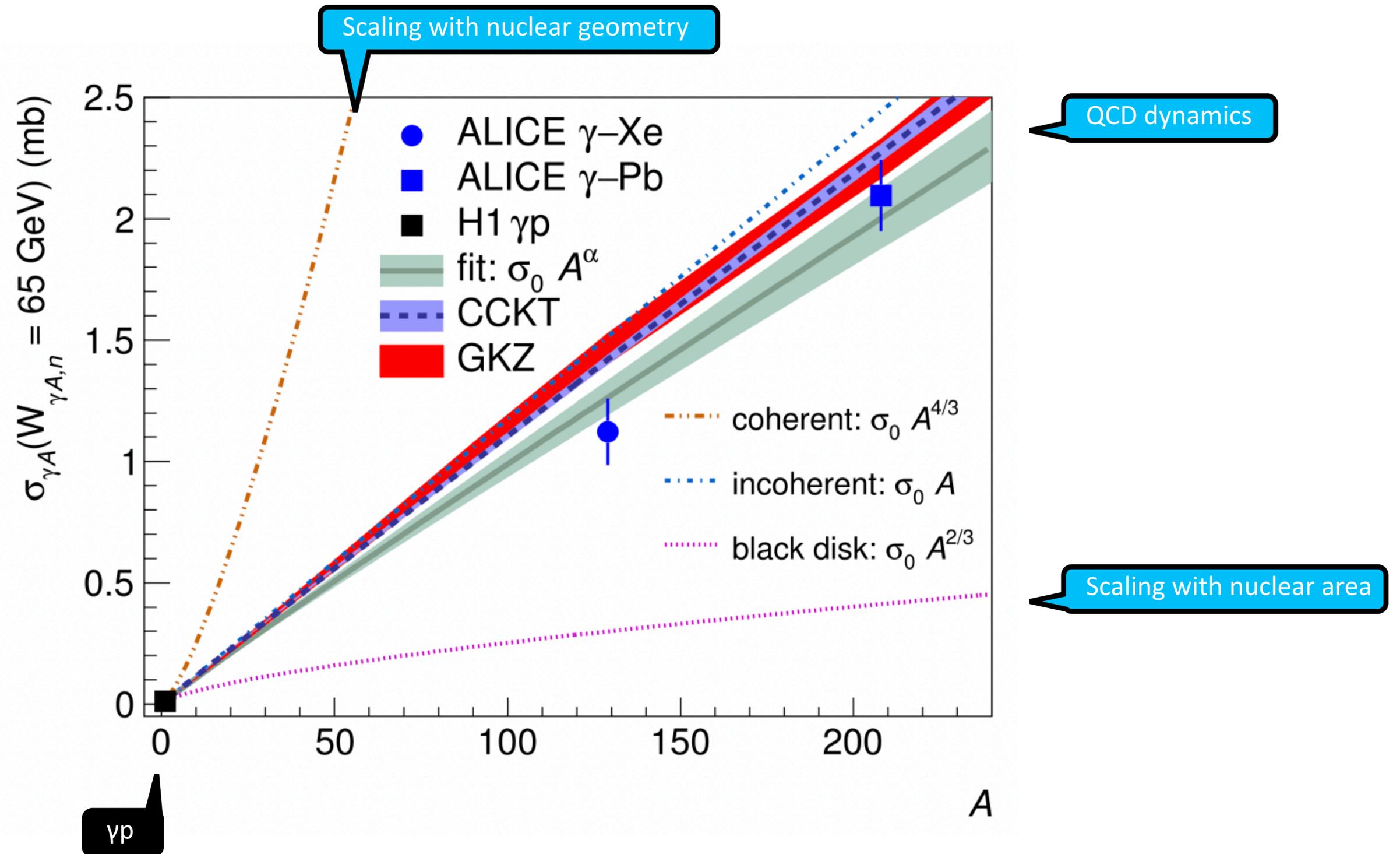
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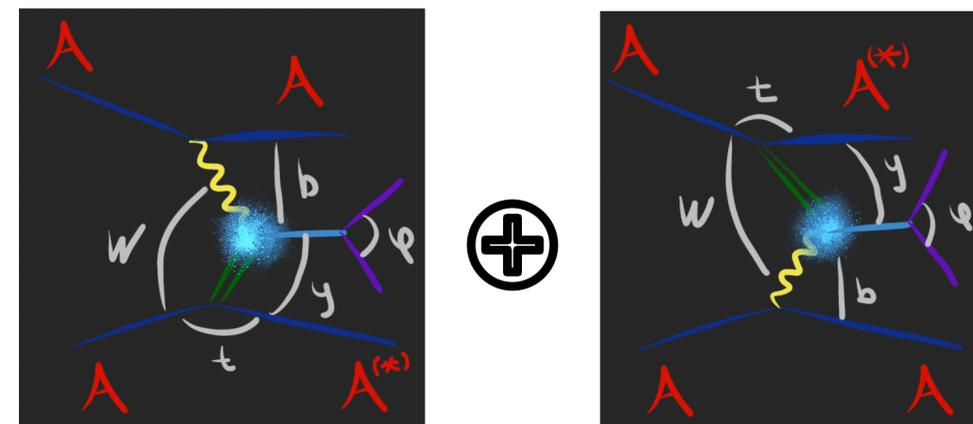
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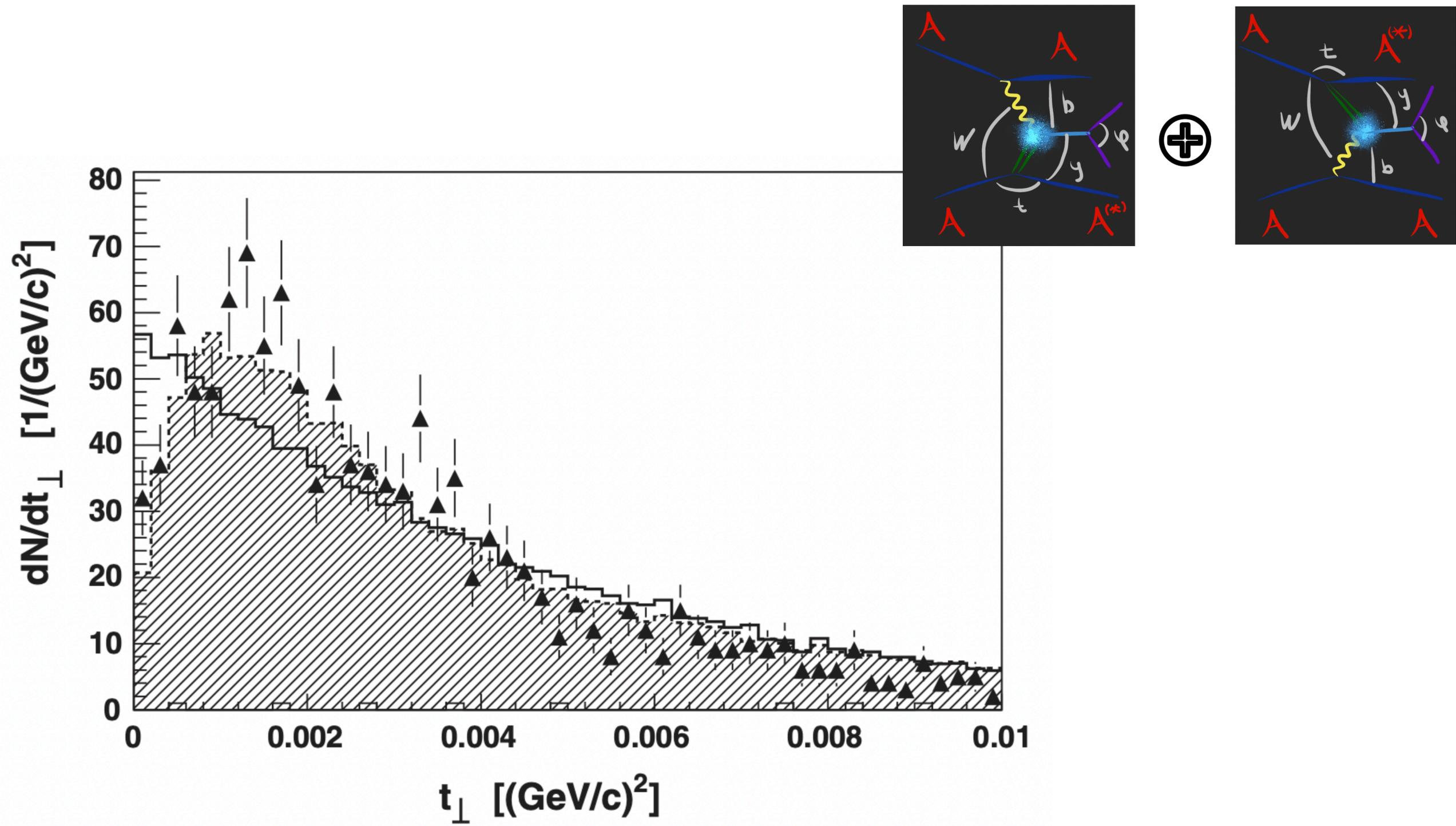
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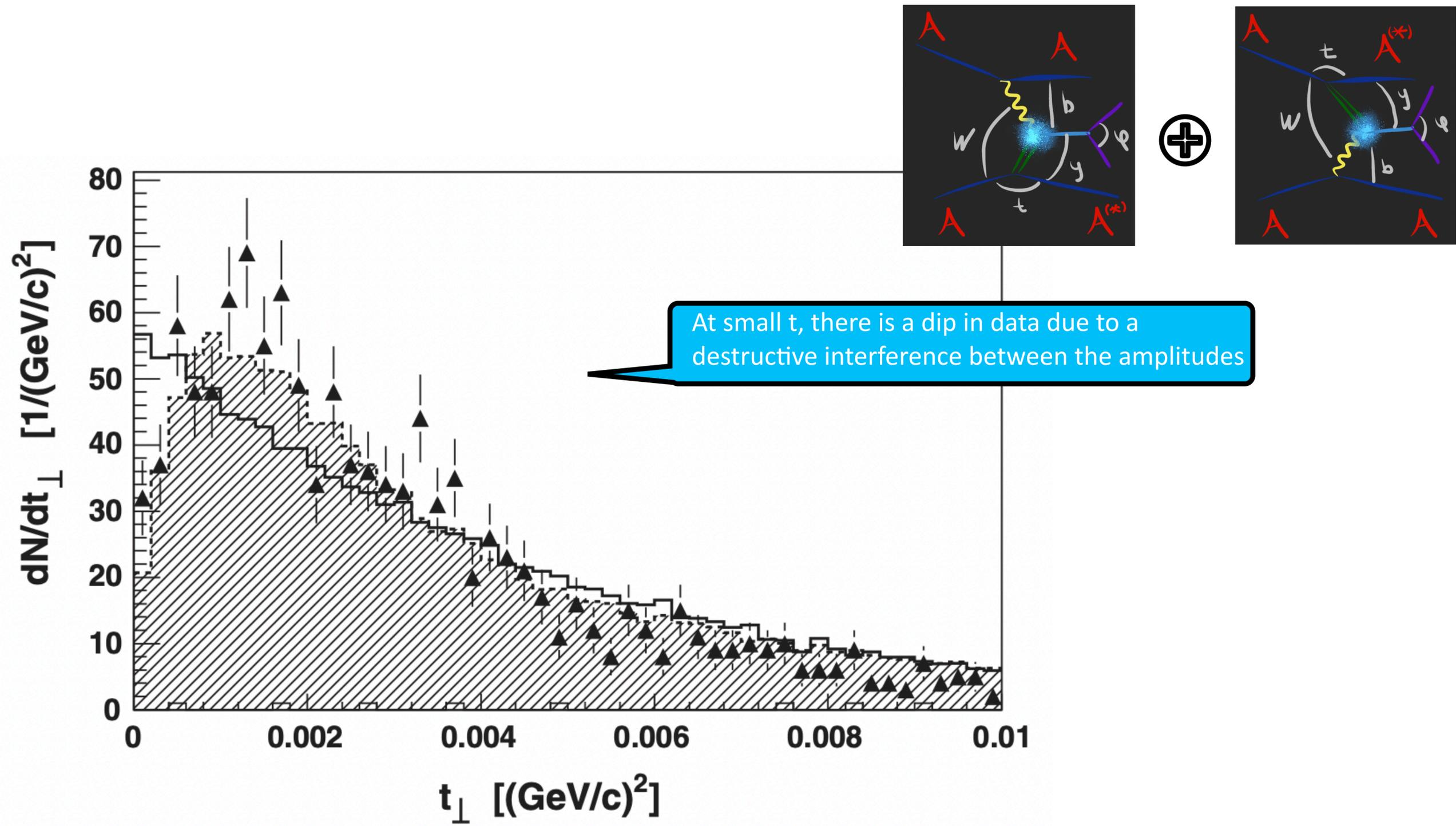
# Interference effects in coherent $\rho^0$ production: $t$ dependence



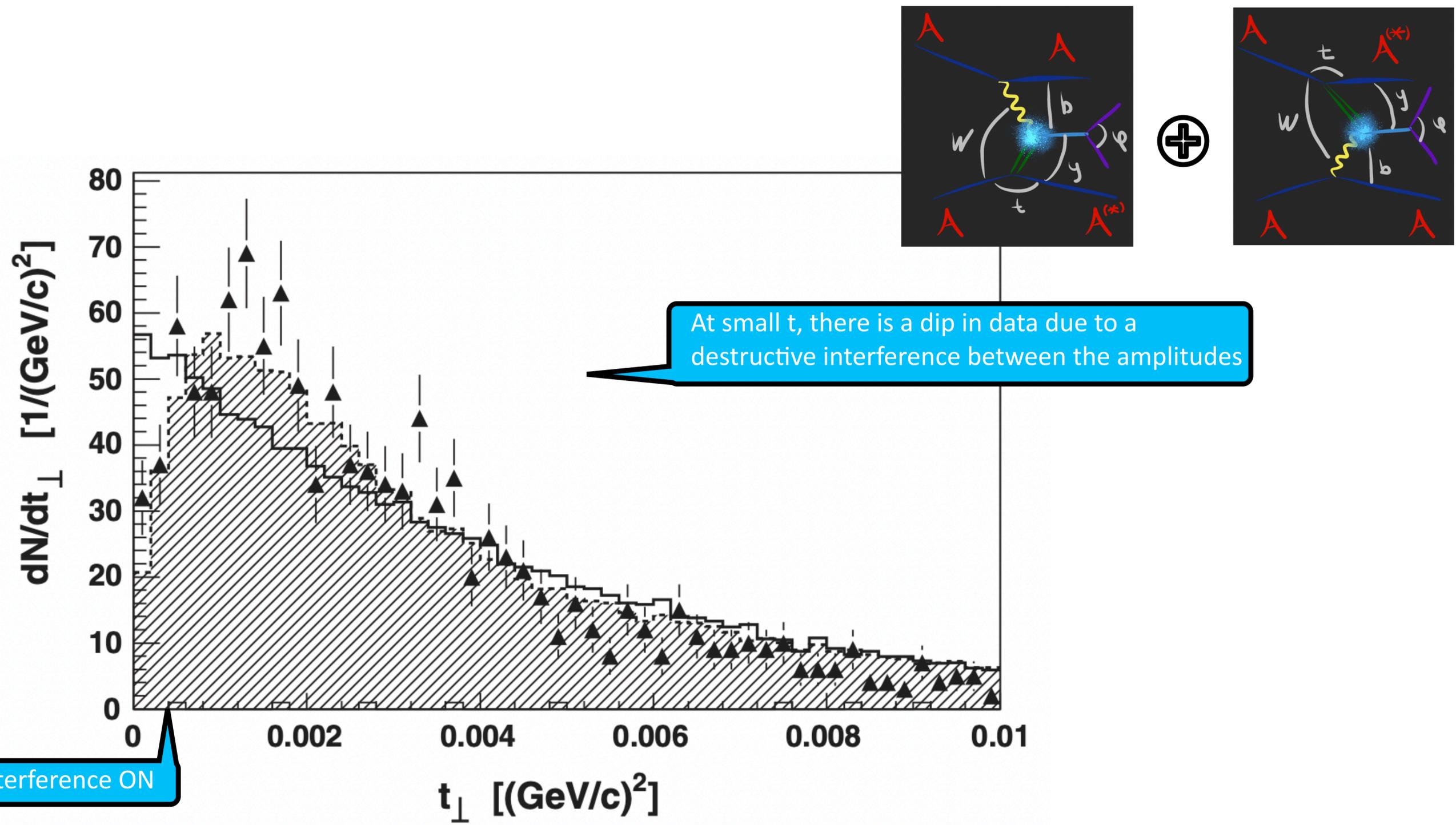
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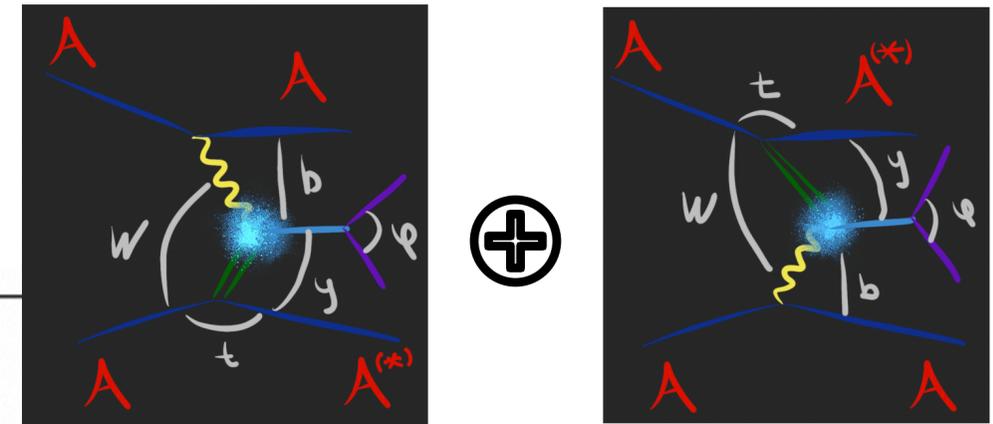
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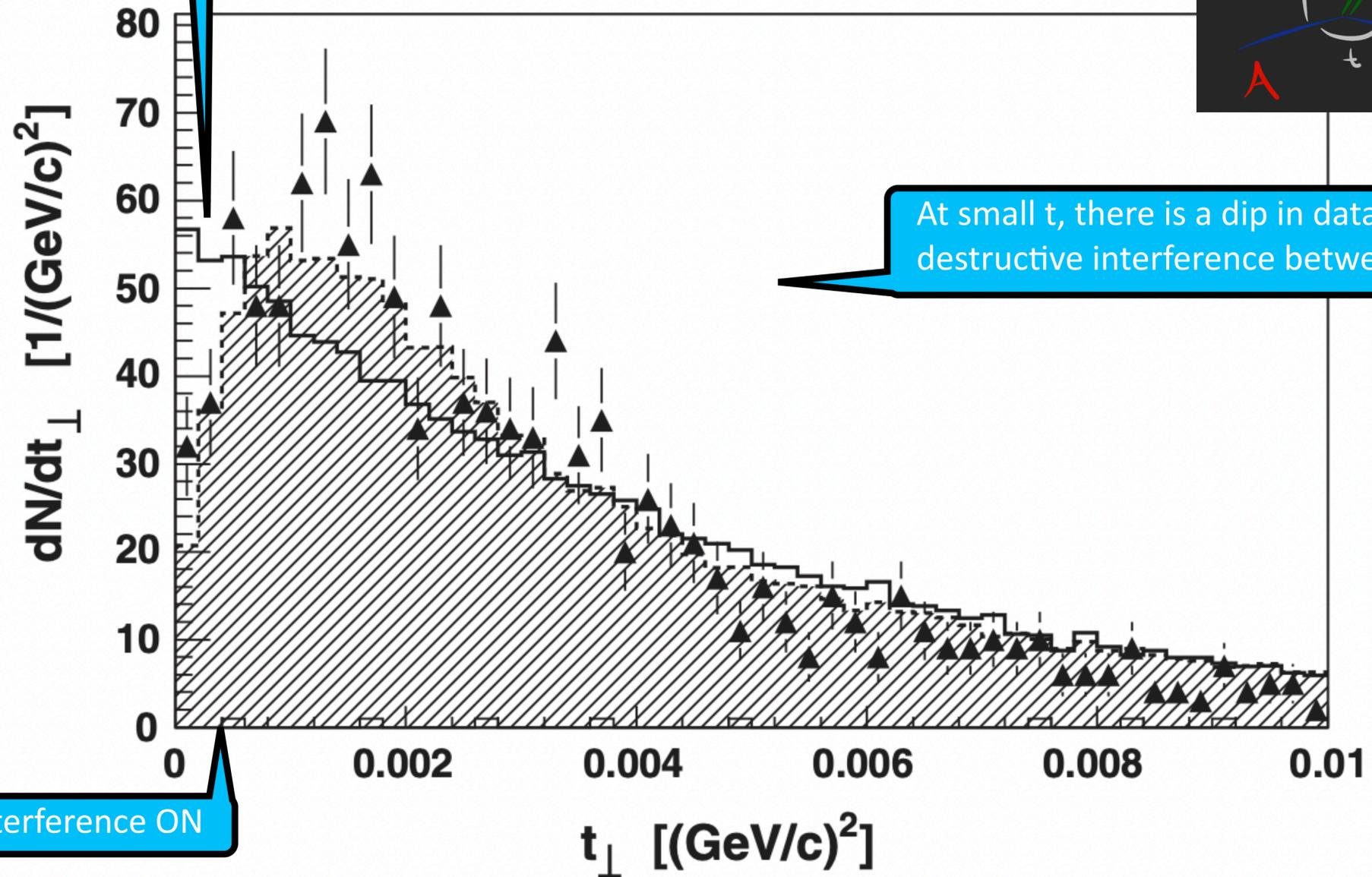
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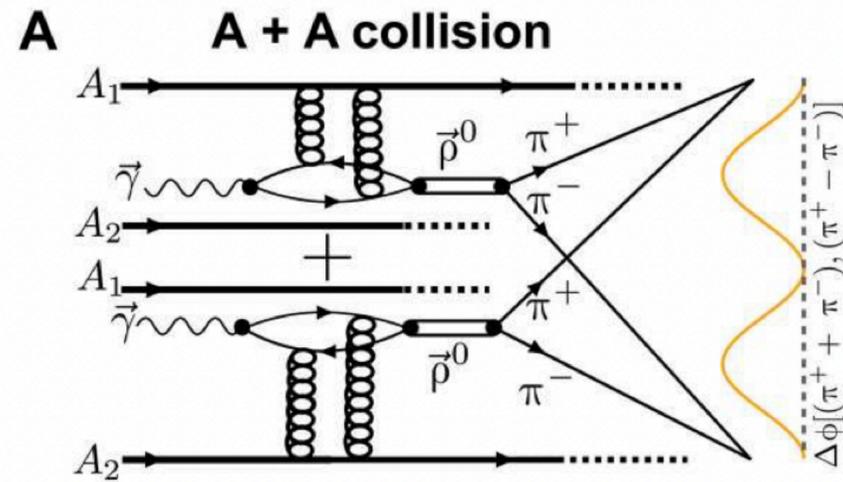
STARlight MC with interference OFF



STARlight MC with interference ON

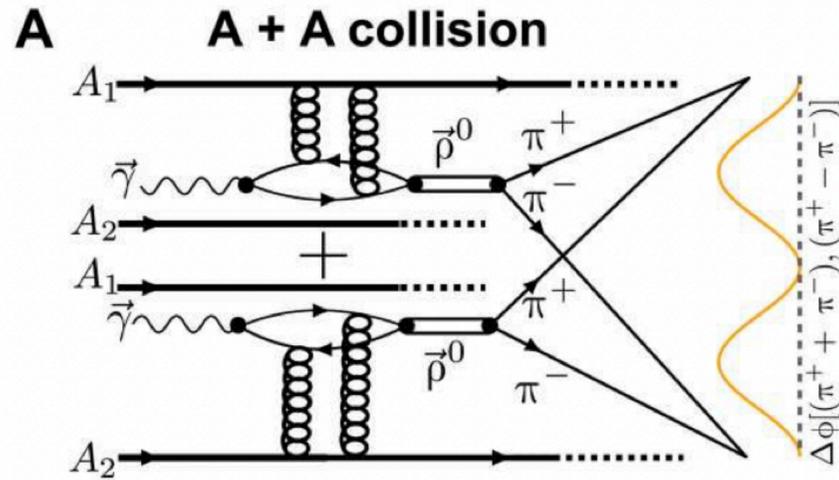
At small  $t$ , there is a dip in data due to a destructive interference between the amplitudes

# Interference effects in coherent $\rho^0$ production: azimuthal asymmetries at RHIC

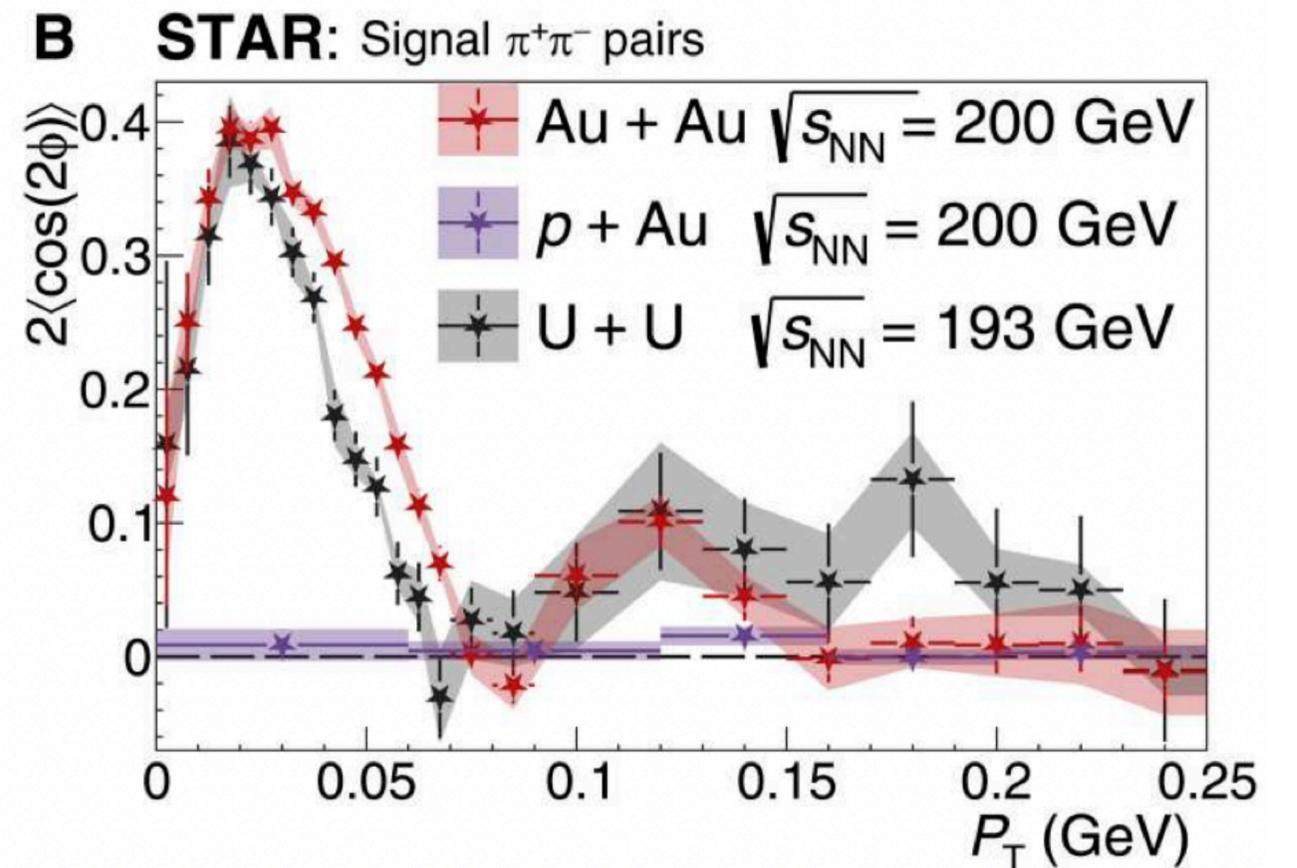
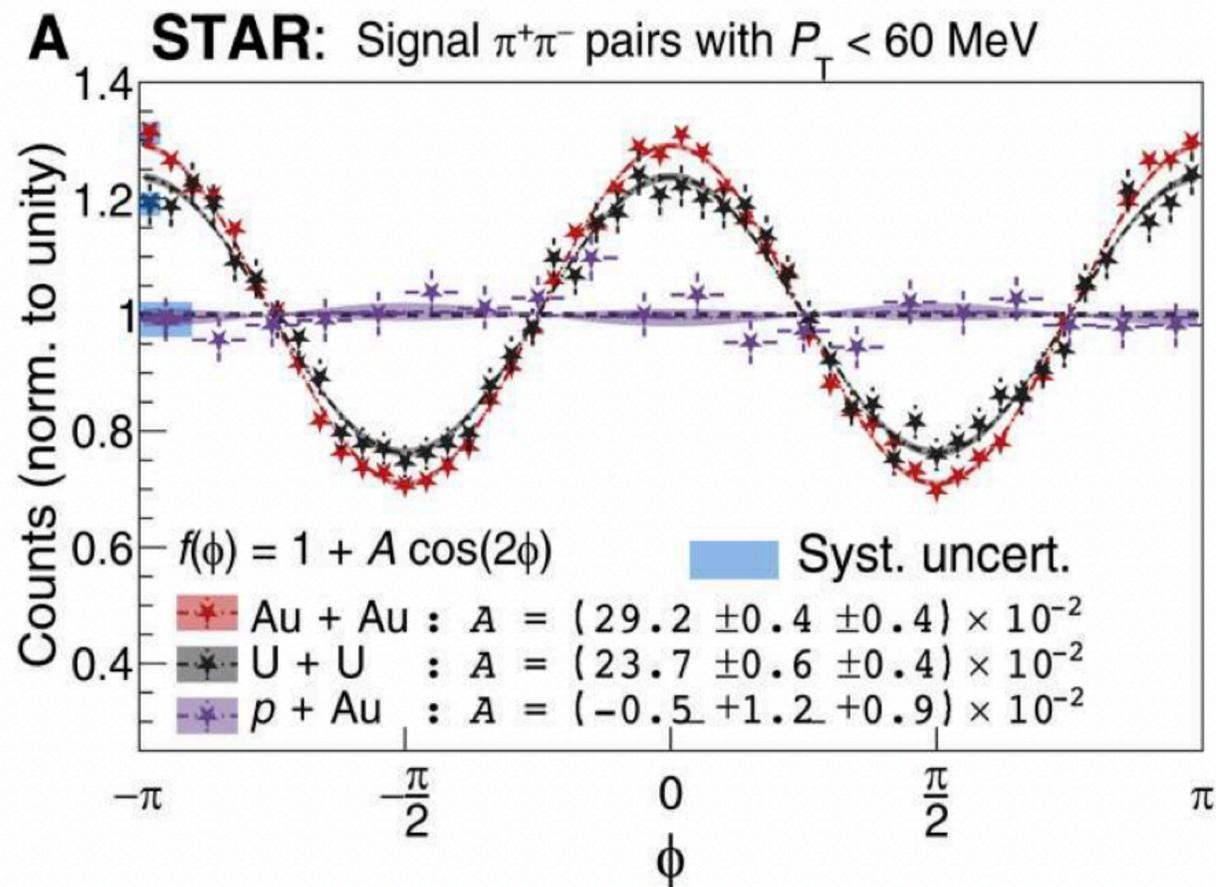


The interference between the amplitudes modifies the azimuthal correlations of the decay products

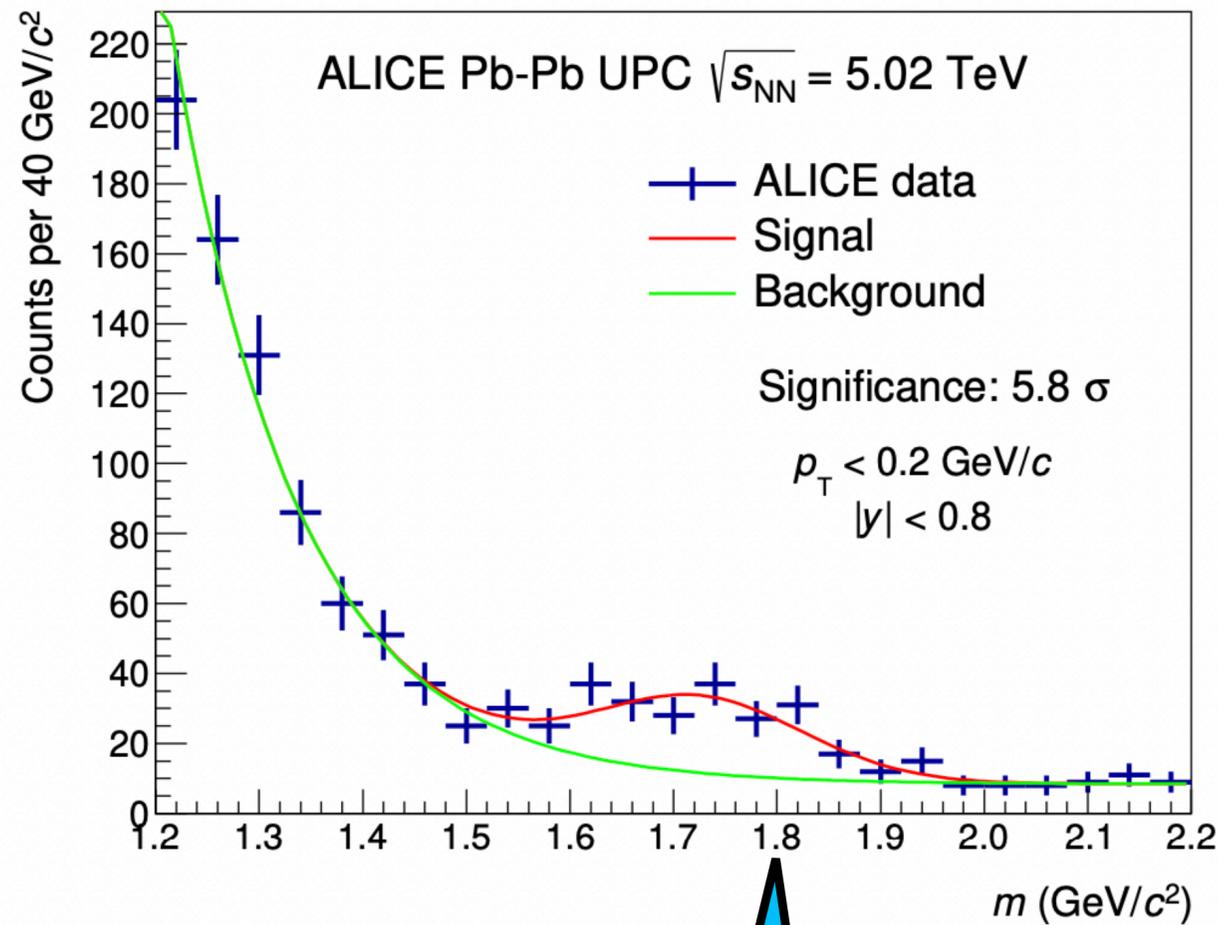
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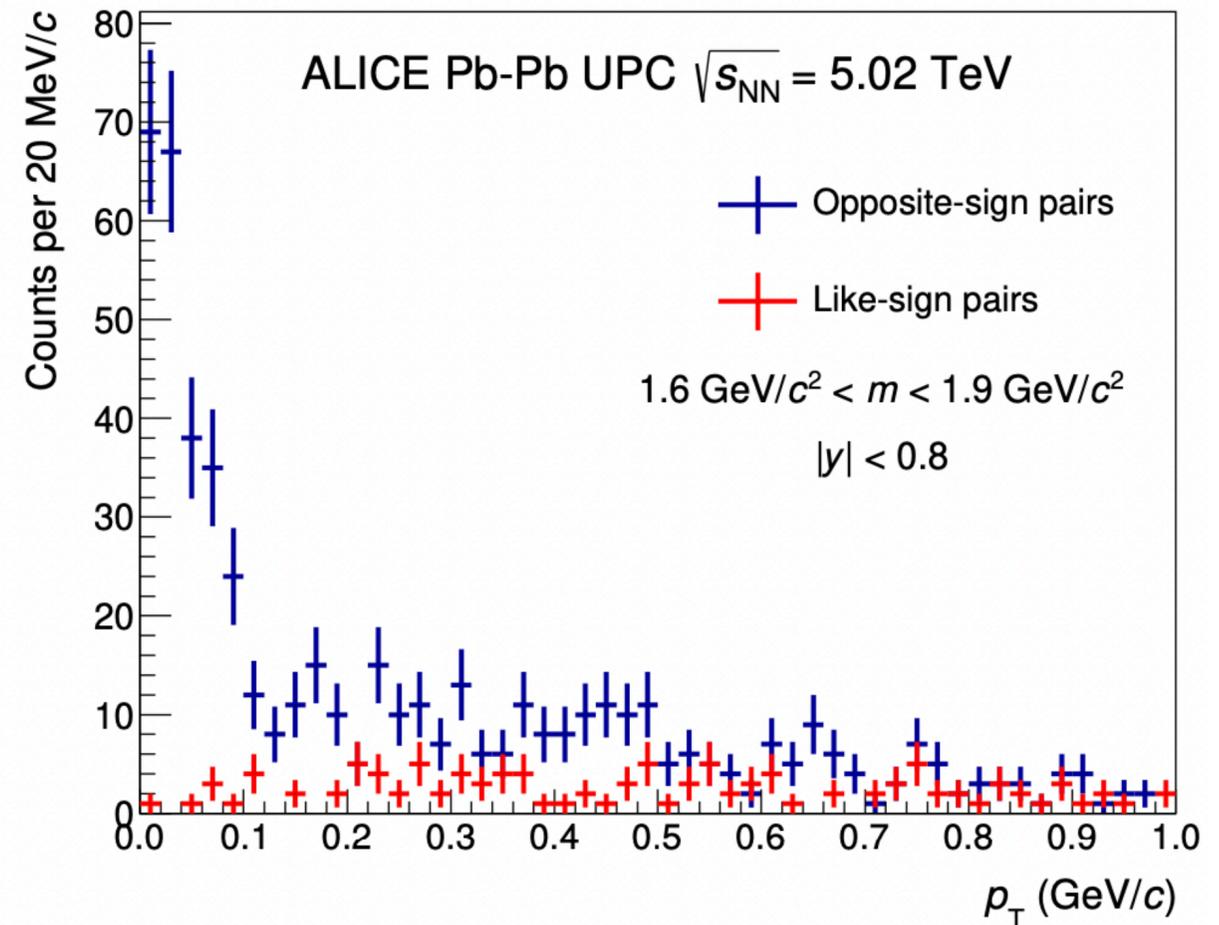


# New (?) resonances in coherent $\pi\pi$ production

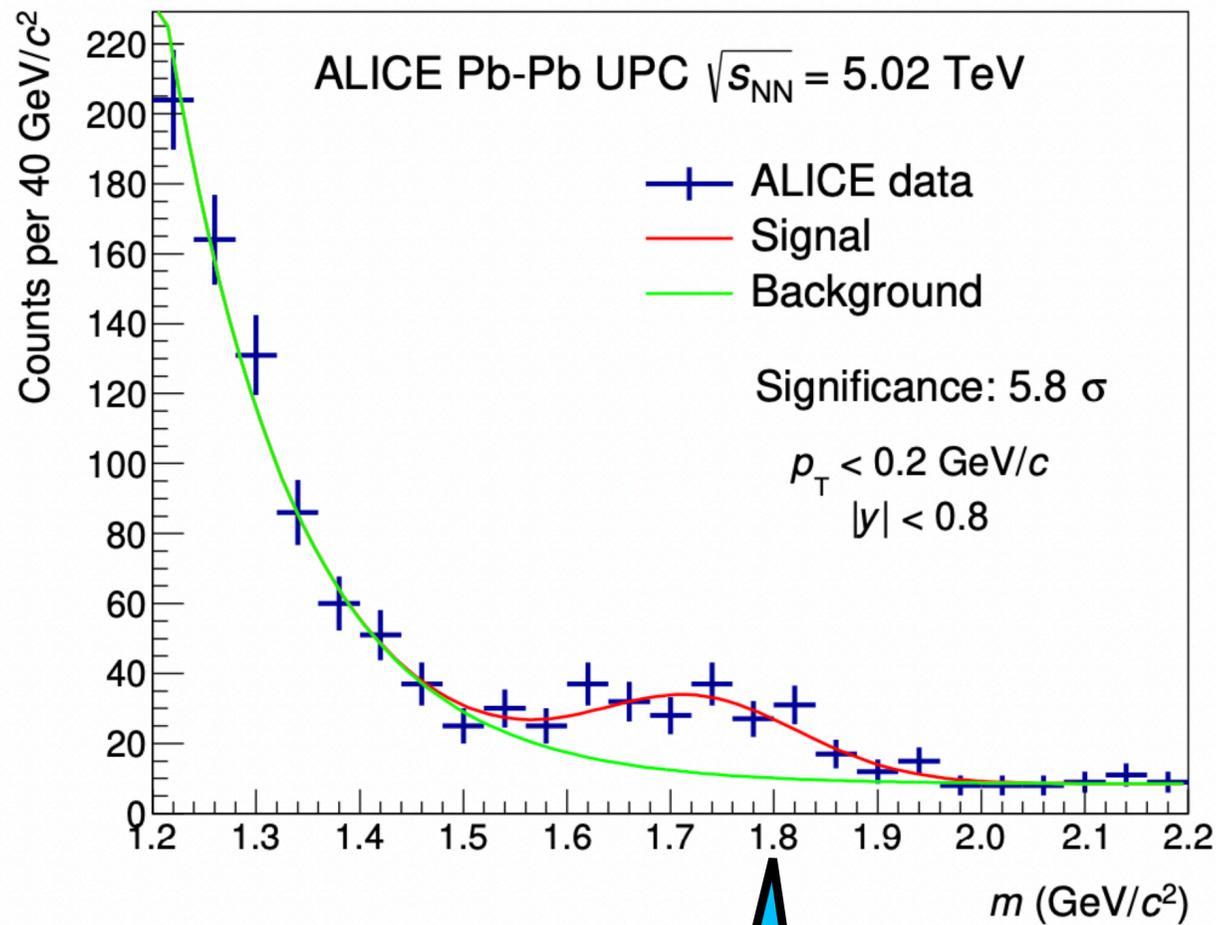


Bump in the invariance mass distribution of pion pairs

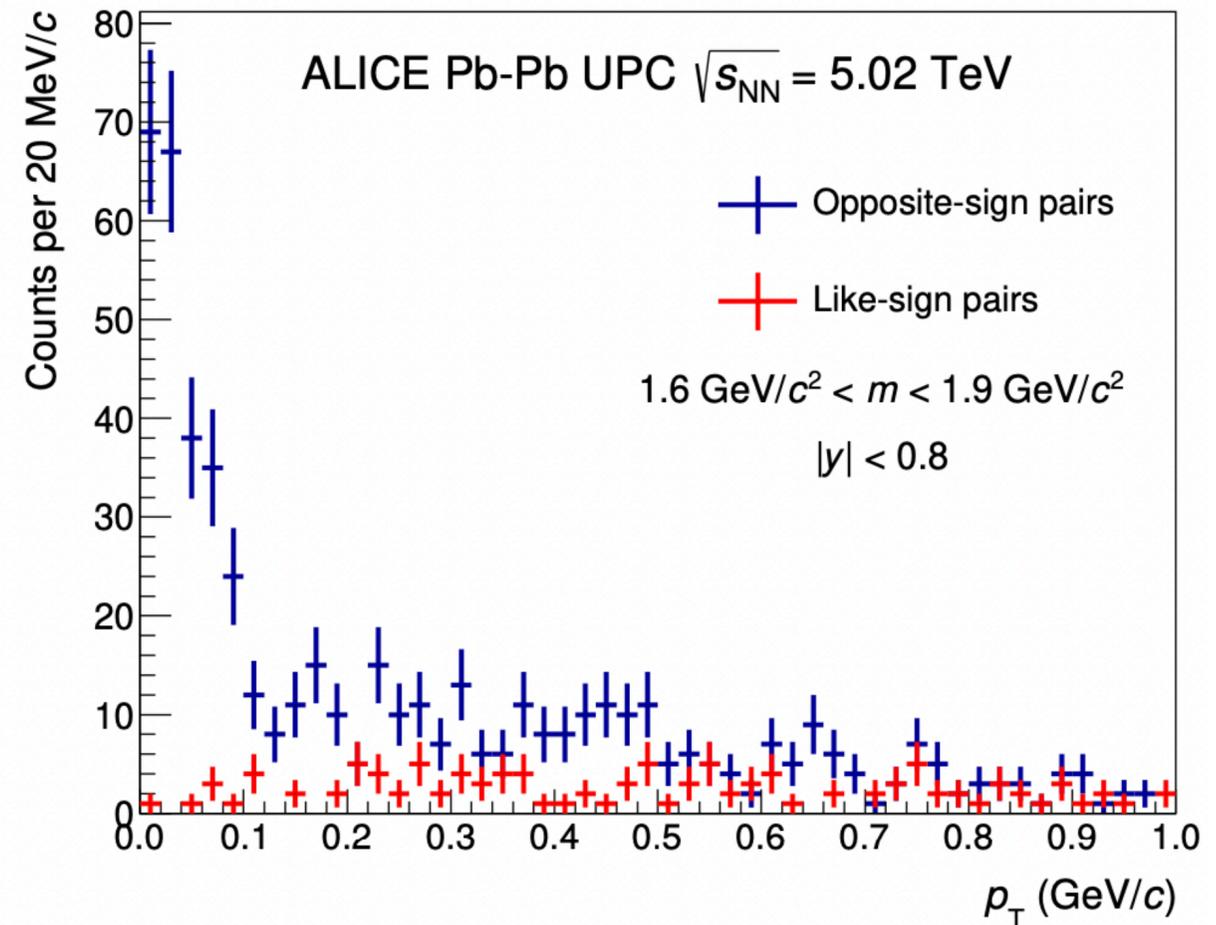
Transverse momentum distribution typical of coherent processes



# New (?) resonances in coherent $\pi\pi$ production



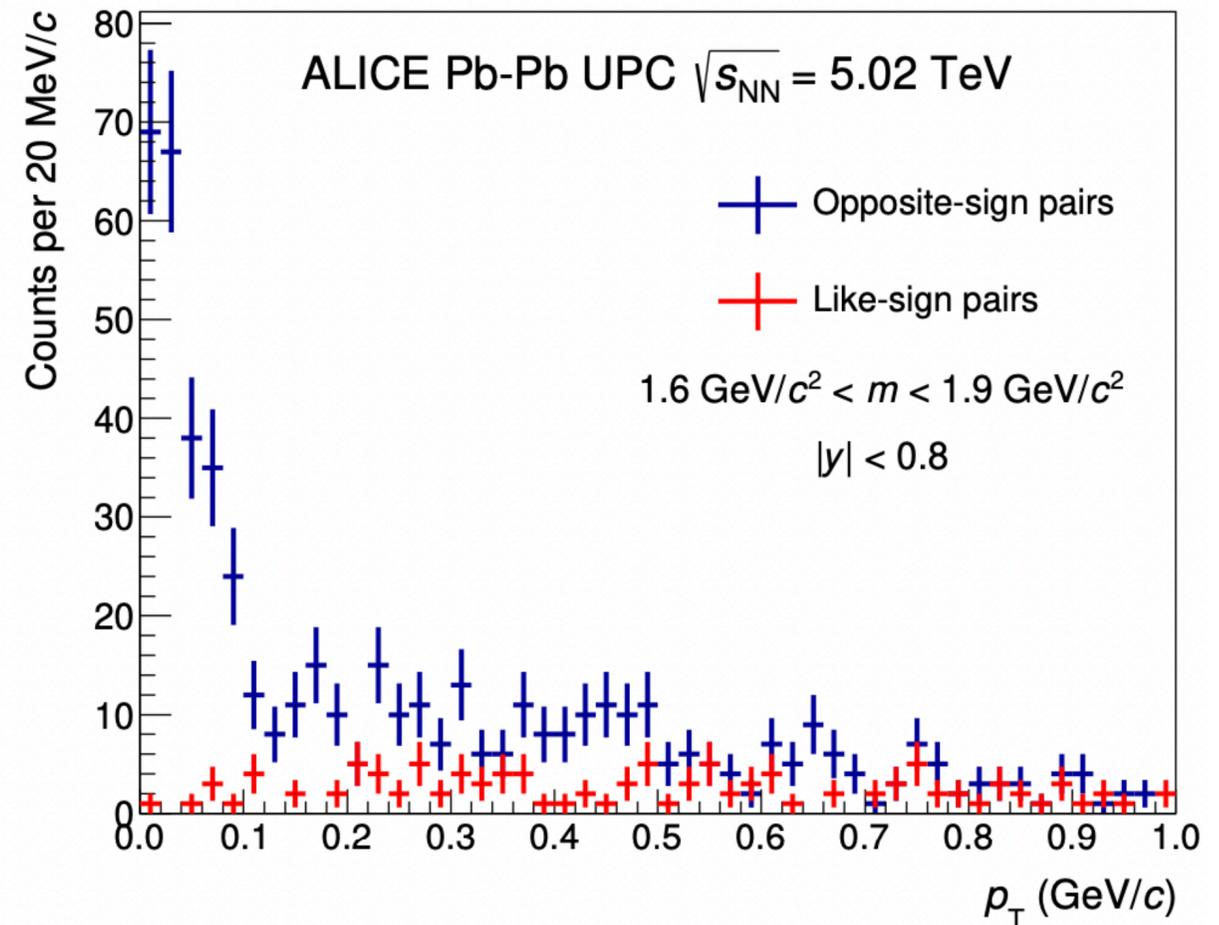
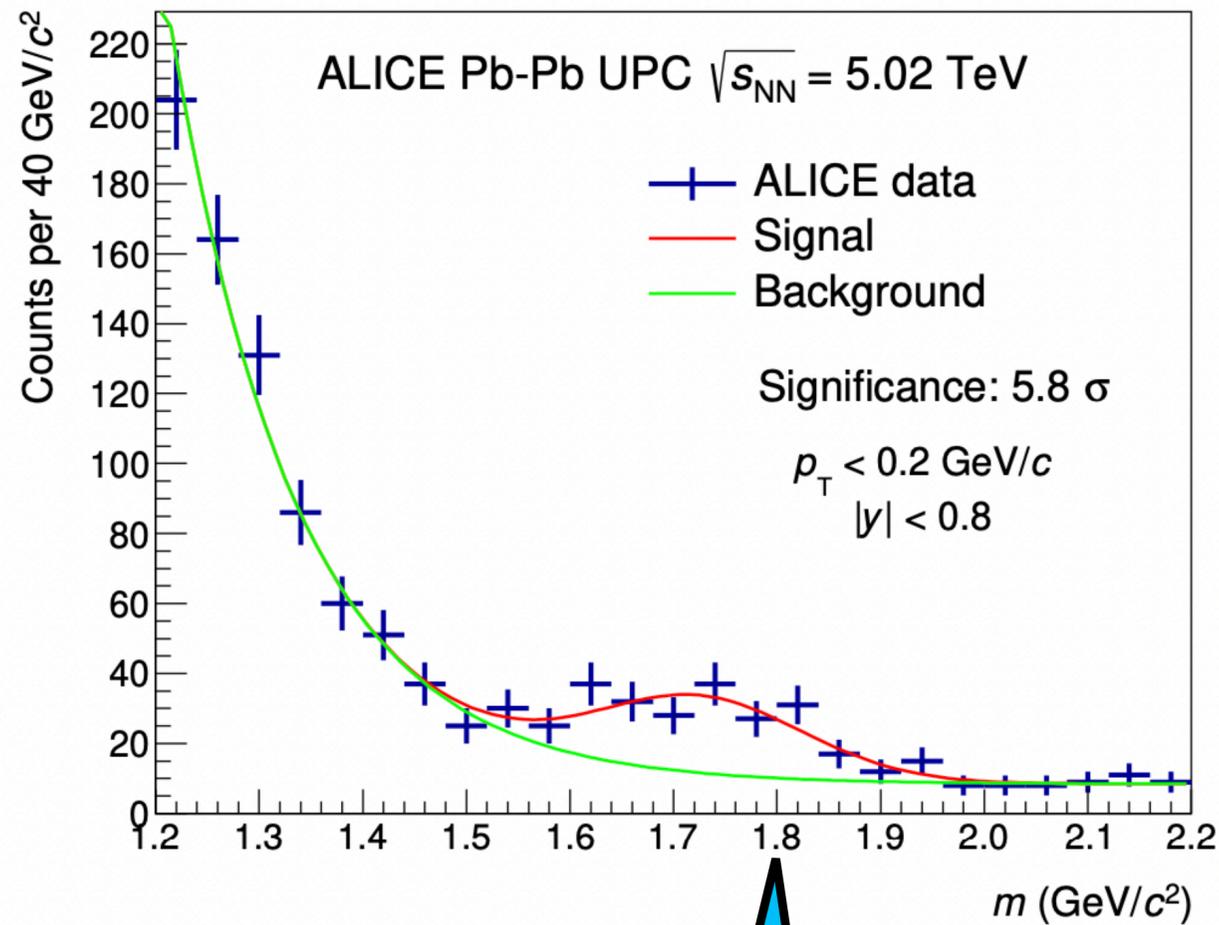
Transverse momentum distribution typical of coherent processes



Bump in the invariance mass distribution of pion pairs

Similar structures seen by H1, ZEUS, STAR

# New (?) resonances in coherent $\pi\pi$ production



Transverse momentum distribution typical of coherent processes

Bump in the invariance mass distribution of pion pairs

Similar structures seen by H1, ZEUS, STAR

The large improvement in luminosity in Run 3 may reveal more of these structures and allow for the determination of their properties

At this point you should have a rough idea of  
what was done before to use photon-induced processes to study QCD  
and what we are doing now at RHIC and LHC

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Homework:

Enjoy the meeting!