

Development of novel, portable matrix-element + phase space methods

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MCnet meeting 2023

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Gefördert durch



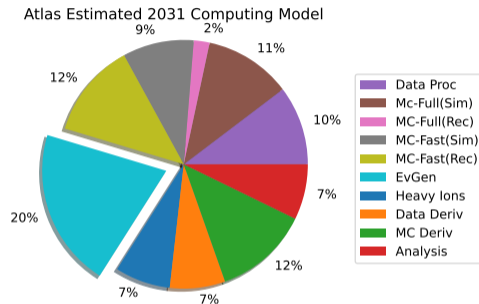
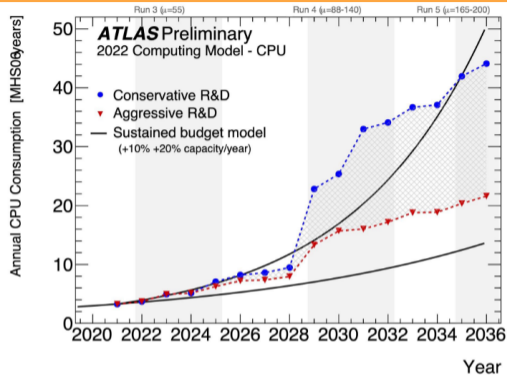


Figure and numbers taken from [CERN-LHCC-2022-005]

- Computing needs are predicted to grow faster than available resources
→ Computing budget might limit physics outcome
- Sizeable part of CPU budget spend on event generation (roughly 20%)
- Our strategy, dedicated rewrite to tackle major bottle-necks
→ Identify major bottle-necks first!

Expensive MC Samples: V+Jets with many jets

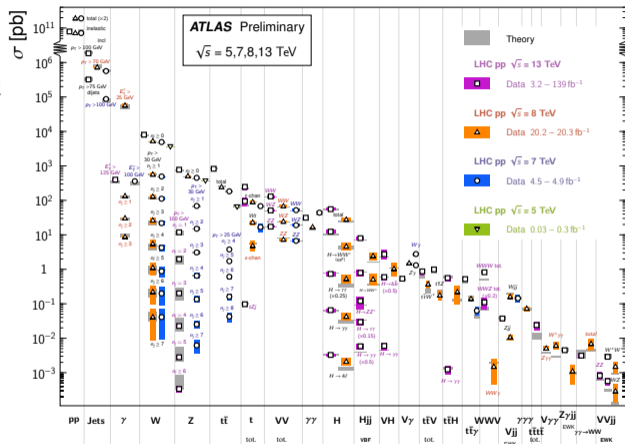
- Background to essential analysis(es), e.g. Higgs-boson and top-quark measurements
cf. [2112.09588]
- Large production cross-section \rightarrow large MC samples
- To reduce significant portion of MC budget, ensure to be efficient for these processes

Guiding Principles for the following discussion:

- 1 Good performance for bottleneck processes (for now: V+Jets, $t\bar{t}$), in particular for many jets!
- 2 Deployable in modern architectures
- 3 Useful integration in existing MC tool-chain

Standard Model Production Cross Section Measurements

Status: February 2022



twiki.cern.ch/twiki/bin/view/AtlasPublic/StandardModelPublicResults

(Some) Components of a MC Computation

$$\sigma_{pp \rightarrow X_n} = \sum_{ab} \int dx_a dx_b d\phi_n f_a(x_a, \mu_F^2) f_b(x_b, \mu_F^2) \\ \times |\mathcal{M}_{ab \rightarrow X_n}|^2 \Theta(p_1, \dots, p_n)$$

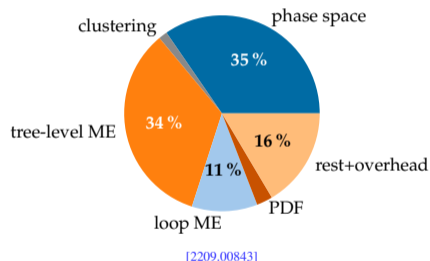
- After some optimisation: Large portion of MC time spend in ME + PS
cf. [2209.00843]
- In this talk: Re-think ME strategy
- Goal: Develop efficient strategy for the different components
- Naive treatment of helicity/color sum scales terribly with increase of multiplicity

$$|\mathcal{M}_{ab \rightarrow X_n}(1, \dots, n)|^2 = \sum_{\text{helicity}} \sum_{\text{color}} A(p_1, \dots, p_n) A(p_1, \dots, p_n)^\dagger$$

Major components we have to take care of are

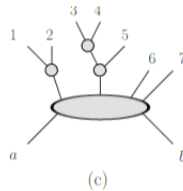
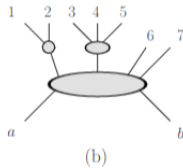
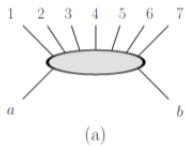
- 1 The Phase-Space generation
- 2 The helicity sum
- 3 The amplitudes
- 4 The color sum

$pp \rightarrow e^+e^- + 0,1,2j @ \text{NLO} + 3,4,5j @ \text{LO}$



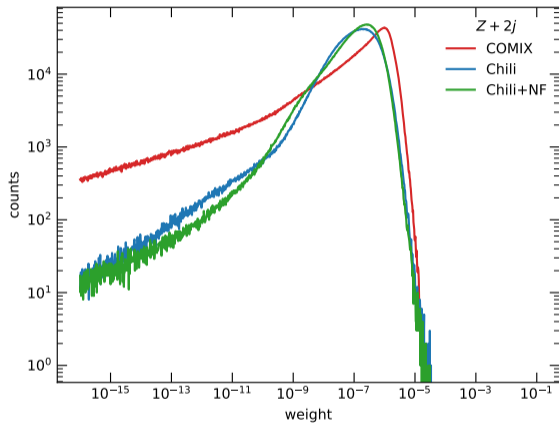
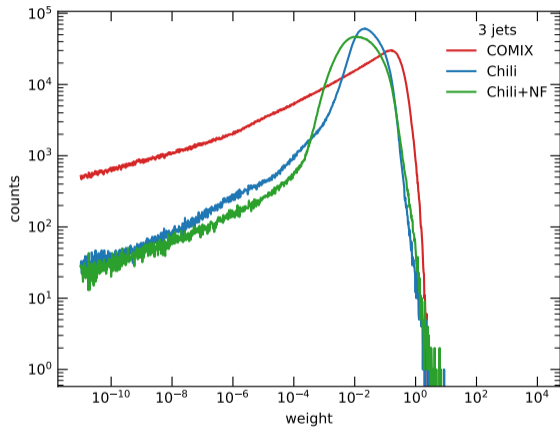
Basic building blocks:

- T-channel phase-space generator from MCFM [Fig, Giele 1806.09678]
- S-channel phase-space factorization and decays [Byckling, Kajantie NPB9(1969)568]
- Variable number of s-channel decays (user-defined) to eliminate exponential scaling



- Very simple phase space generator, but fast and portable

Chili performance compared to Sherpa default



→ Tested across a large range of processes ($W + 5j$, $Z + 5j$, $h + 5j$, $t\bar{t} + 4j$, $\gamma + 5j$, $6j$)

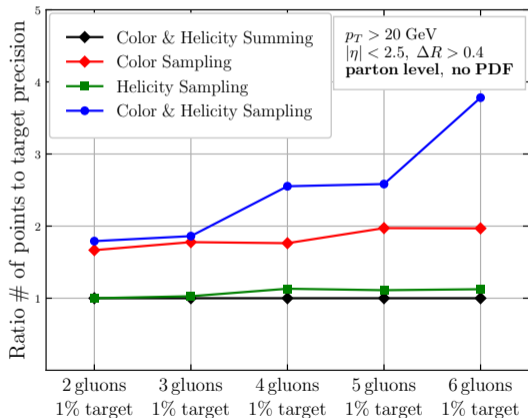
→ Overall good performance

Investigate impact of helicity-summing vs. sampling on convergence

→ How many points to we have to compute to make up for MC estimate?

- Compare convergence in realistic setup
→ Recursive PS-Sampler, ...
- Helicity sampling comes with close to zero additional points
→ This takes analytic amplitude knowledge into account
- Loss in precision increases with multiplicity for color and helicity sampling

⇒ **Algorithmic choice: Sample helicities**



- Different strategies to compute tree-level amplitudes efficiently

- 1 Berends-Giele like recursion
- 2 Scalar
- 3 MHV (CSW)
- 4 BCF

- Rely on performance studies from early 2000's

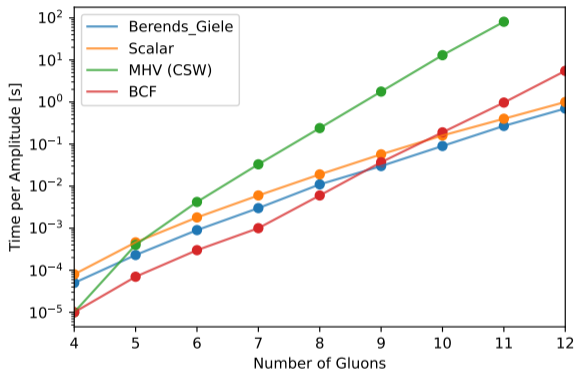
[hep-ph/0602204](https://arxiv.org/abs/hep-ph/0602204), [hep-ph/0607057](https://arxiv.org/abs/hep-ph/0607057)

- We are interested in best scaling behaviour / performance for multi-jet processes (guiding principles)

Best scaling option is the Berends-Giele recursion

⇒ **Algorithmic choice: Berends-Giele recursion**

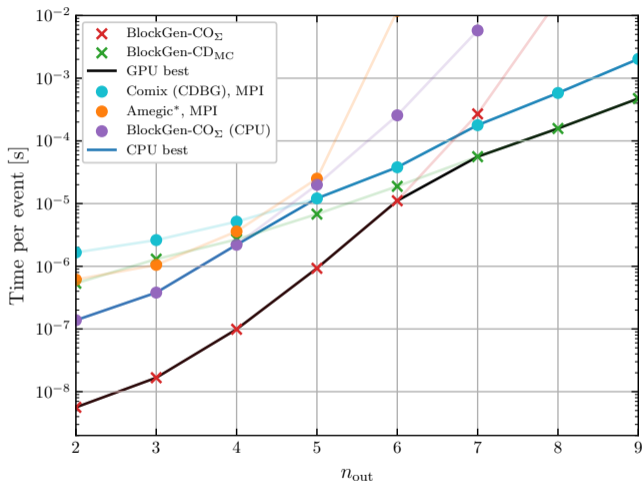
NB: BCF-like recursions show potential for intermediate multiplicities, dominant effect from (N)MHV amplitudes that can be included in current generator



Based on numbers from [hep-ph/0602204](https://arxiv.org/abs/hep-ph/0602204)

- Benchmark performance for gluon-only process
- Relevant test, since as-many-gluon-as-possible amplitudes make up largest portion of computing time for jet-processes
- Compare different color treatments: color-dressing/summing/sampling
- Color-sampled algorithms scale similar to color-summed approaches
- Color-summing scales worse than color-dressing, but faster up to roughly 5-6 outgoing jets
- Caveat: Color-sampling comes with penalty factor from slower convergence

⇒ **Algorithmic choice: Sum colors**



- Introduce spinors (Weyl for massless, Dirac for massive particles)
- Add more general QCD three point vertices
- Straight-forward for helicity-sum and Berends-Giele recursion
- First time in a code aimed for production: use minimal QCD color-basis $\{A(1, 2, \sigma), \sigma \in \text{Dyck}\}$

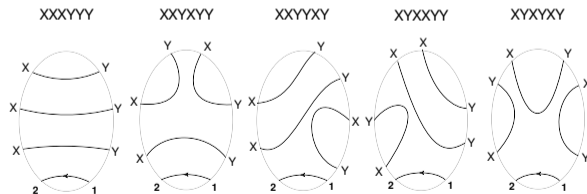
[T. Melia 1304.7809 & 1312.0599 & 1509.03297; H. Johansson, A. Ochirov, 1507.00332]

→ Allows to fix one fermion line, remaining permutations are given by Dyck-Words

→ For particle Dyck Words: $()()$, $(())$

→ Significantly less amplitudes to compute

- Include EW particles after QCD basis has been setup

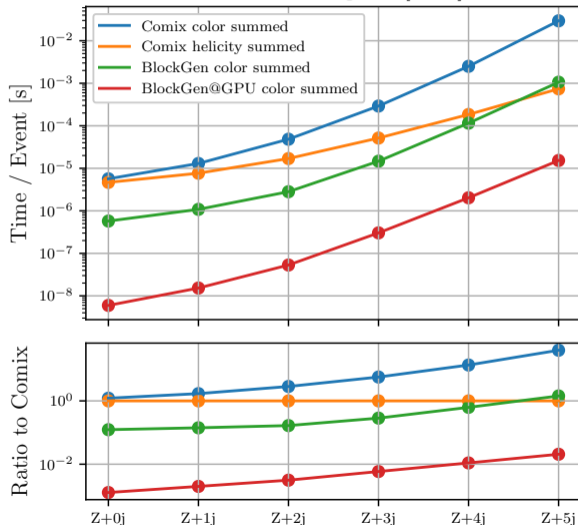


[1304.7809]

Relevant benchmark process: $pp \rightarrow Z[ee] + nj$

- Realistic setup for ME computations
 - Include all sub-processes, no PDF
 - Dominated by as-many-as-possible
- Compare dedicated C++ Version with dedicated Cuda version
- PS: Rambo
- CPU: i3-8300 CPU @ 3.70GHz, GPU: Tesla V100S
- Excellent performance compared to current Sherpa-Standard
- Almost three orders of magnitude for lower multiplicities (single CPU core vs full GPU)

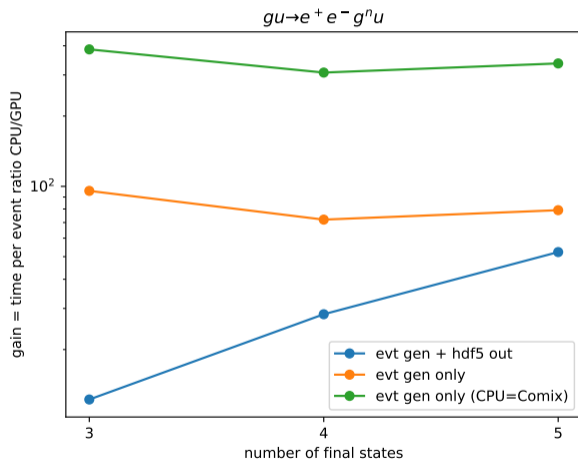
Matrix Element timing of $Z[e^+e^-] + \text{Jets}$



Results cont'd: PRELIMINARY Performance of the whole tool-chain*

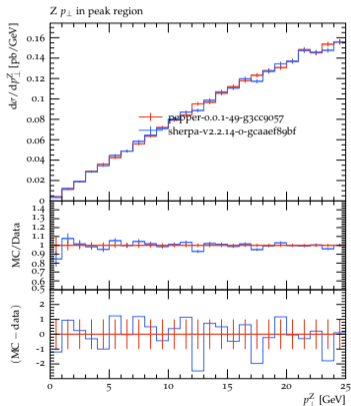
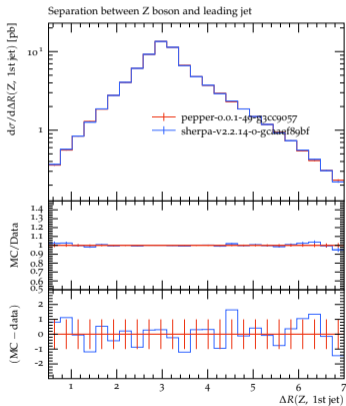
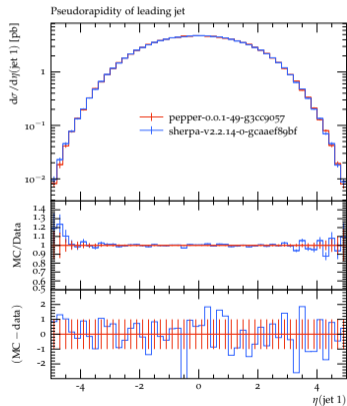
Best comparison we can currently do, but details hiding in the '**':

- Still lacking Chili@GPU
 - The only real GPU number we can compute are the ME timings
 - Remaining numbers are estimate from the CPU performance
- The gain here is measured per trial event
 - Comix' worse cut-efficiency helps
 - Eventually should measure per unweighted event
- LHAPDF is available on the GPU, but not used yet
 - Will be added once PS is there
- hdf5 can probably be hidden by asynchronous writes



Results cont'd: How to make this usable

- 1 Compute Phase-Space and Matrix-Element
- 2 Write out **unweighted** Phase-Space points
- 3 Do the remaining MC magic the usual way



- Matrix-elements show excellent performance on both CPU and GPU
 - ▶ Helps to reduce CPU time consumption but also enables more/complicated computations and use of modern GPU data-centers
- CPU Speed-up $\mathcal{O}(10)$, GPU Speed-up $\mathcal{O}(100)$
 - ▶ Color-summing/helicity sampling good choice for intermediate to high multiplicities
 - ▶ No process-specific optimisations → straight-forward extension to more processes
 - ▶ Potentially need some more fine-tuning of Cuda version
- Eventual goal: parton-level generator that delivers seed events to SHERPA for further processing
 - ▶ Proposed workflow, (ME,PS)@GPU, (Shower,Hadronisation,MPI,...)@CPU using HDF5 I/O [[Höche, Prestel, Schulz 1905.05120](#)]
→ Nearing usable product, natural inclusion in current toolchain