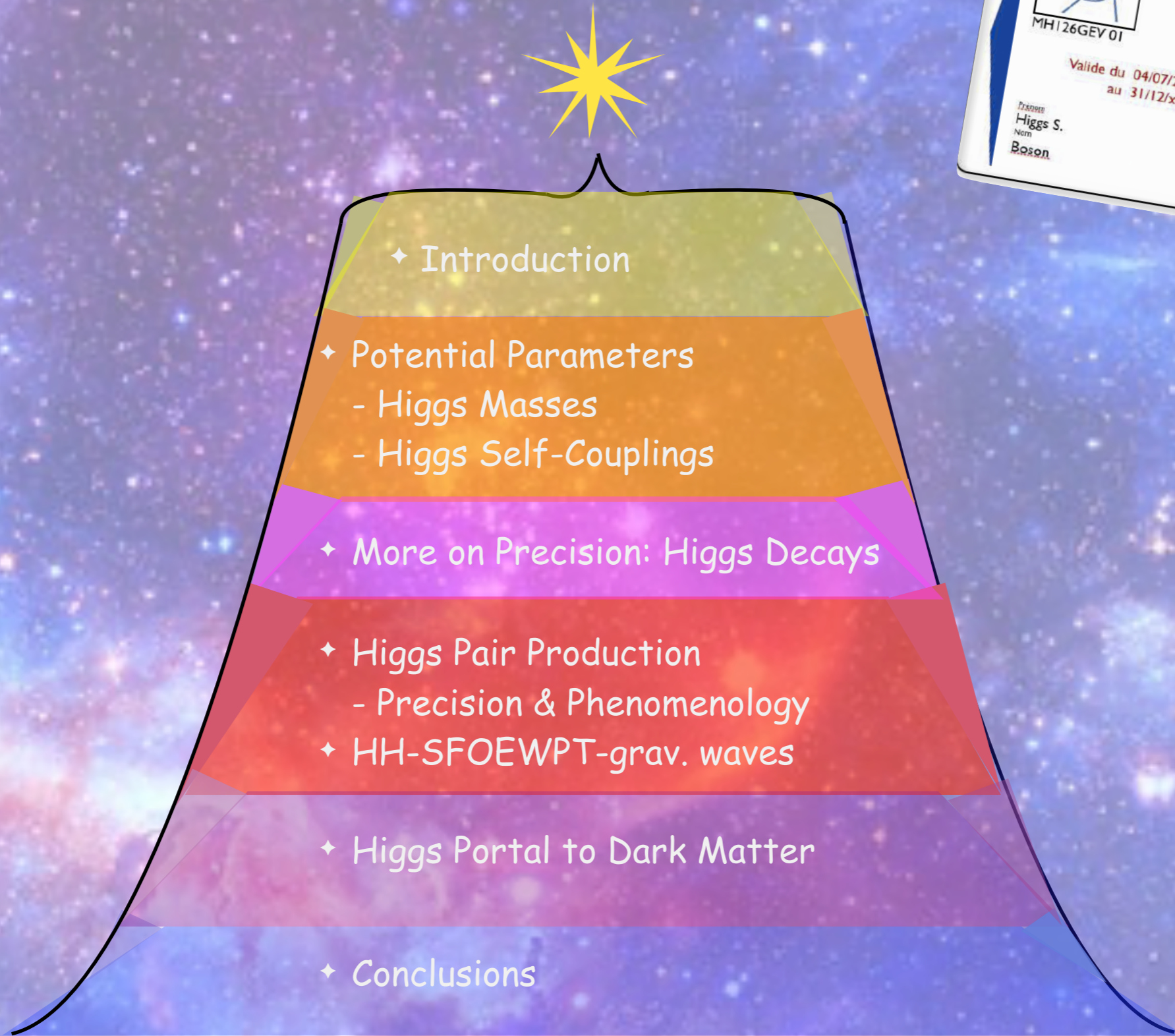
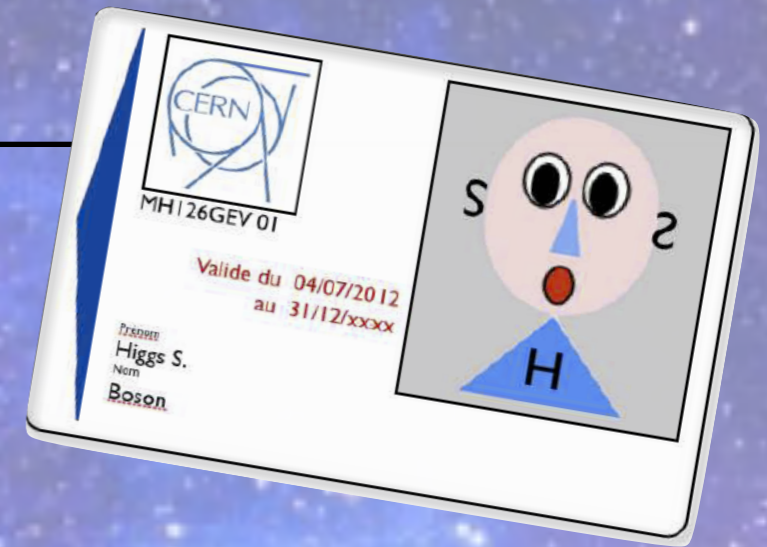


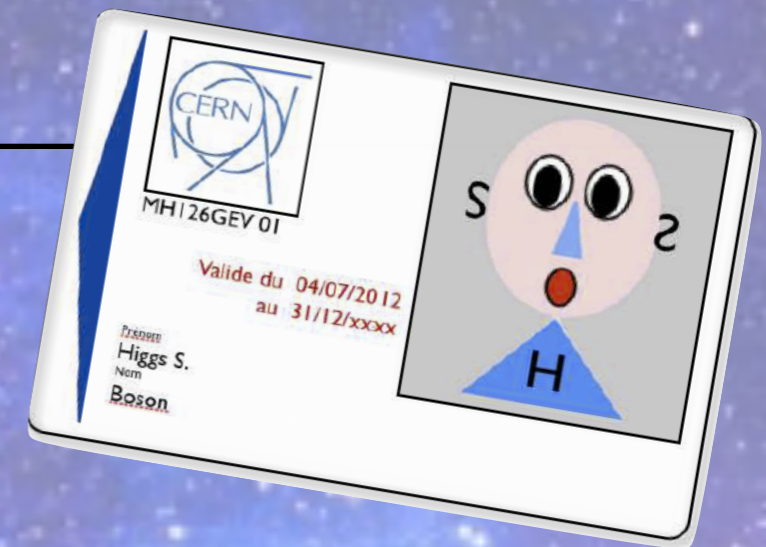
*News on the Higgs Sector or  
Cracking the Code of the Universe  
with the Higgs boson*

*M. Mühlleitner (KIT)  
Invisibles'23 Workshop  
Göttingen, 28.8.-1.9.2023*

# Outline



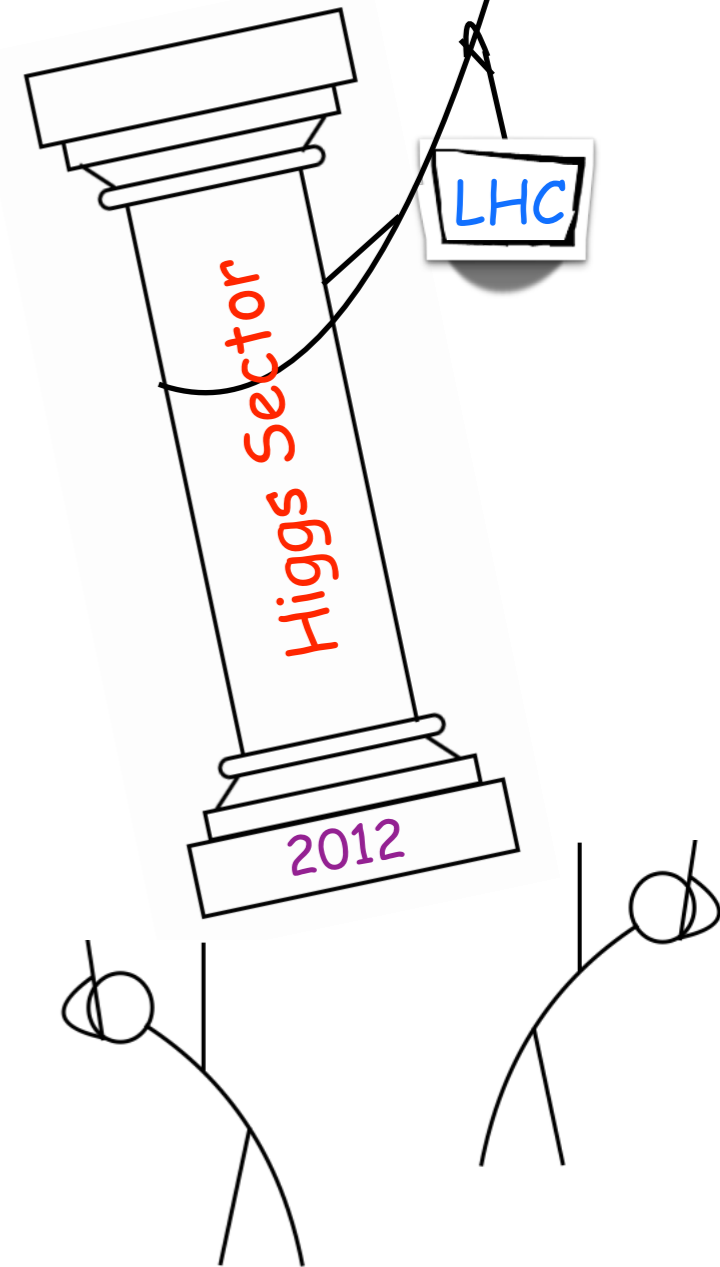
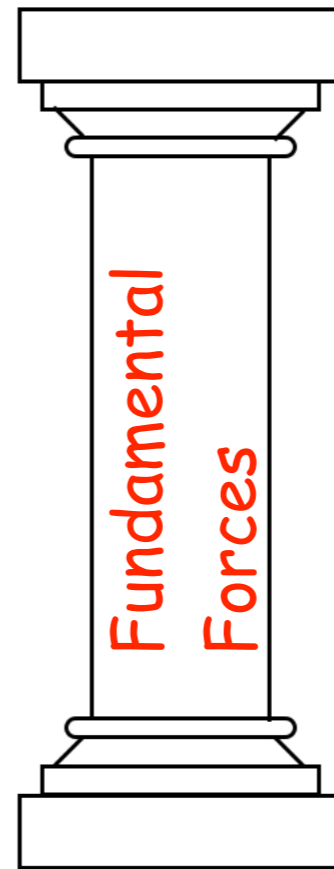
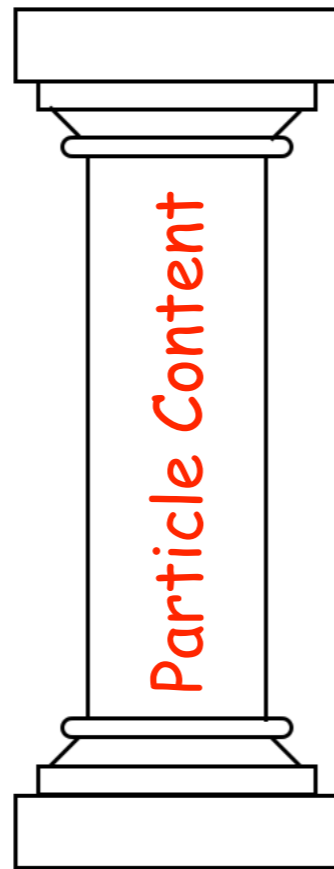
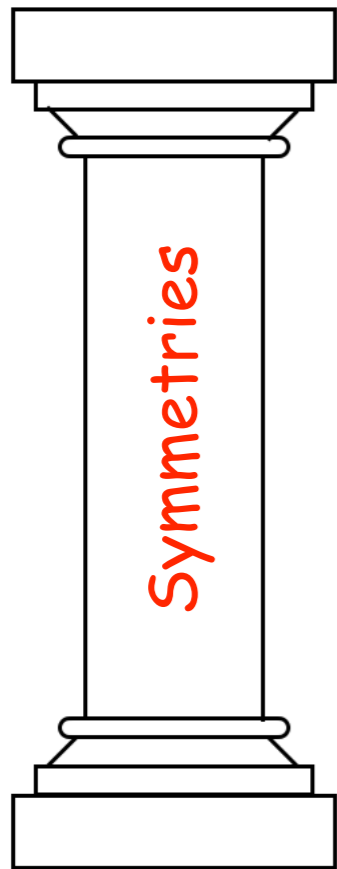
# Outline



Disclaimer: Focus on  
Beyond-Standard-Model  
Theories & Phenomenology

- ✦ Introduction
- ✦ Potential Parameters
  - Higgs Masses
  - Higgs Self-Couplings
- ✦ More on Precision: Higgs Decays
- ✦ Higgs Pair Production
  - Precision & Phenomenology
- ✦ HH-SFOEWPT-grav. waves
- ✦ Higgs Portal to Dark Matter
- ✦ Conclusions

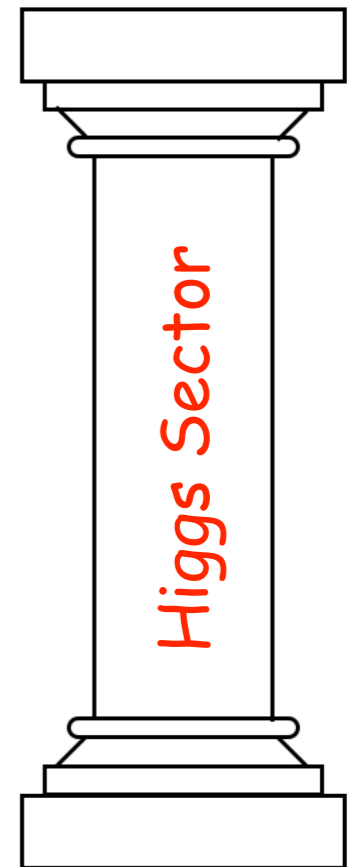
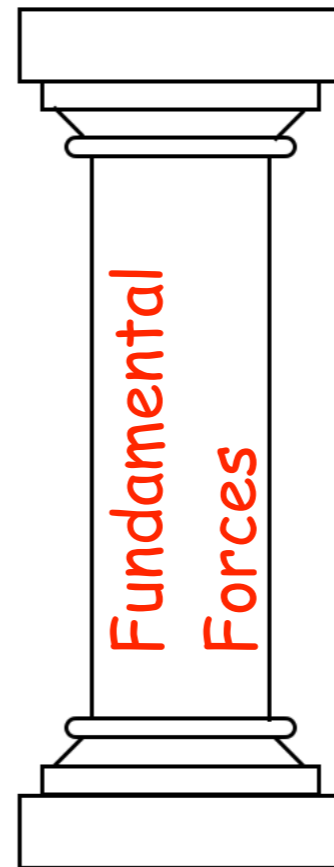
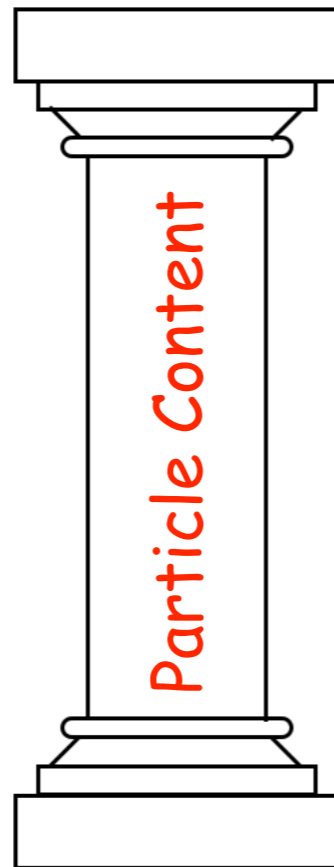
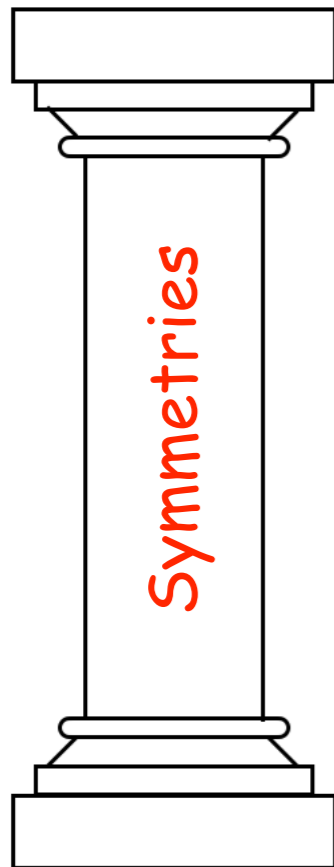
# The Four Pillars of the Standard Model



---

# The Four Pillars of the Standard Model

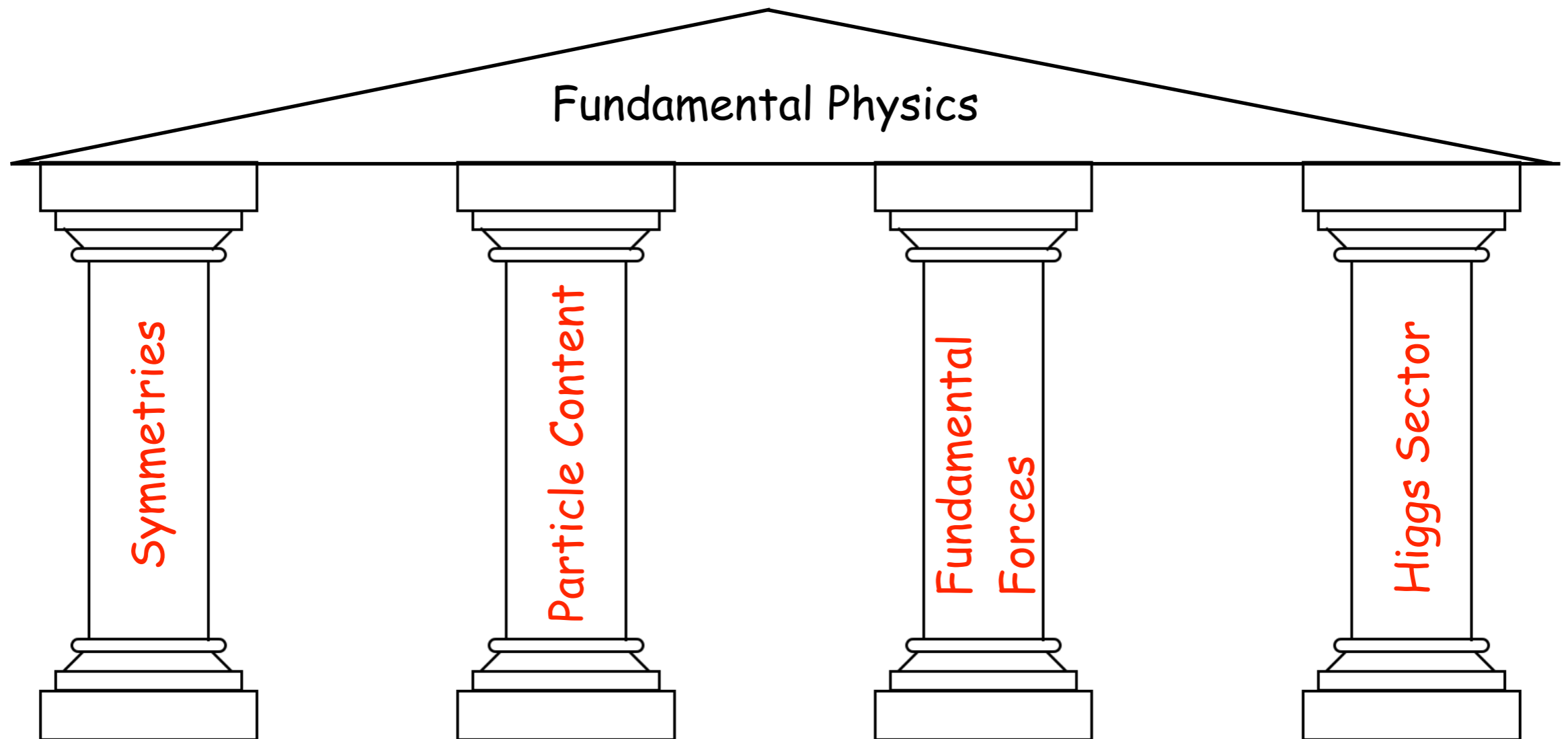
---



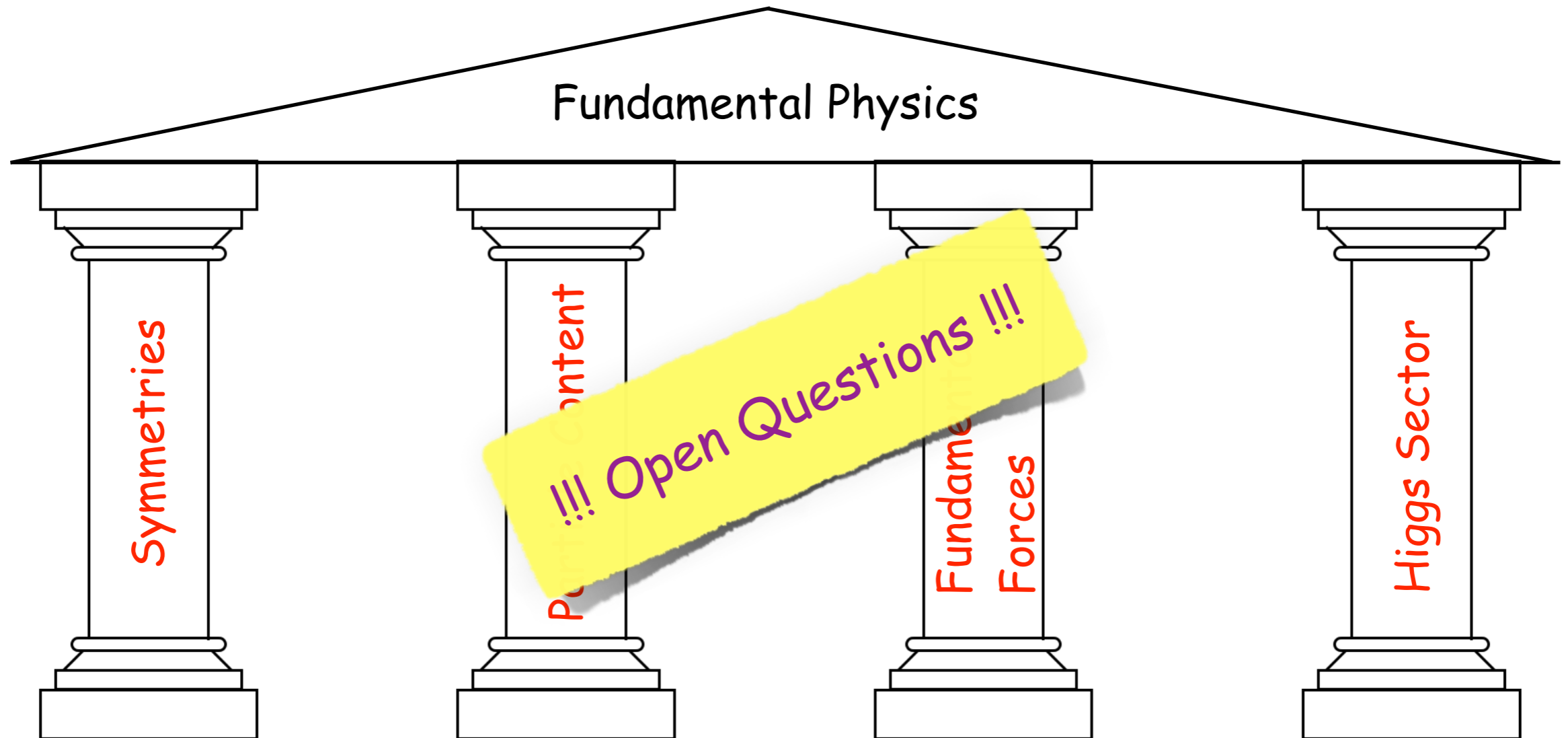
---

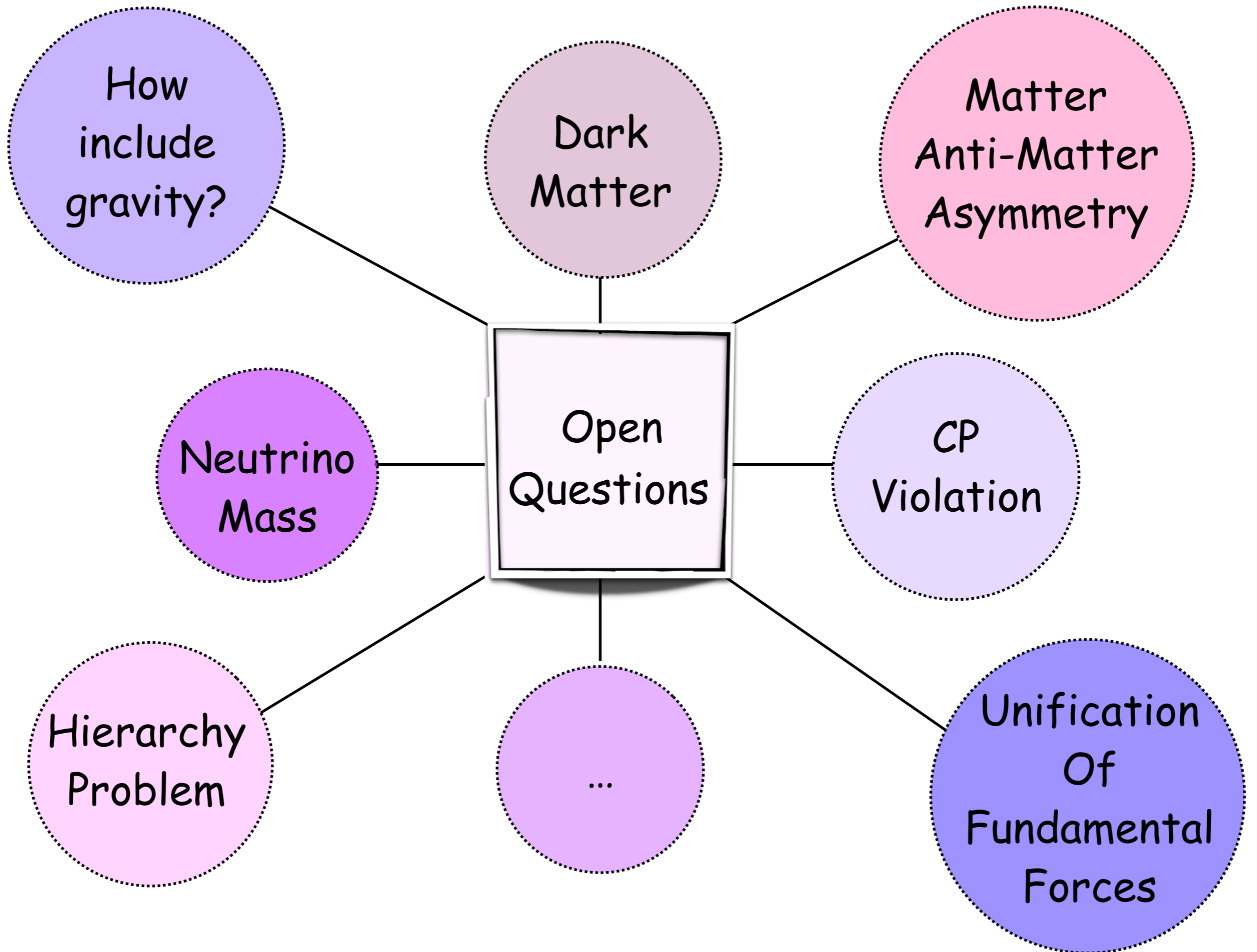
# The Standard Model is Structurally Complete

---



# The Standard Model is Structurally Complete - But





How include gravity?

Dark Matter

Matter Anti-Matter Asymmetry

Open Questions

CP Violation

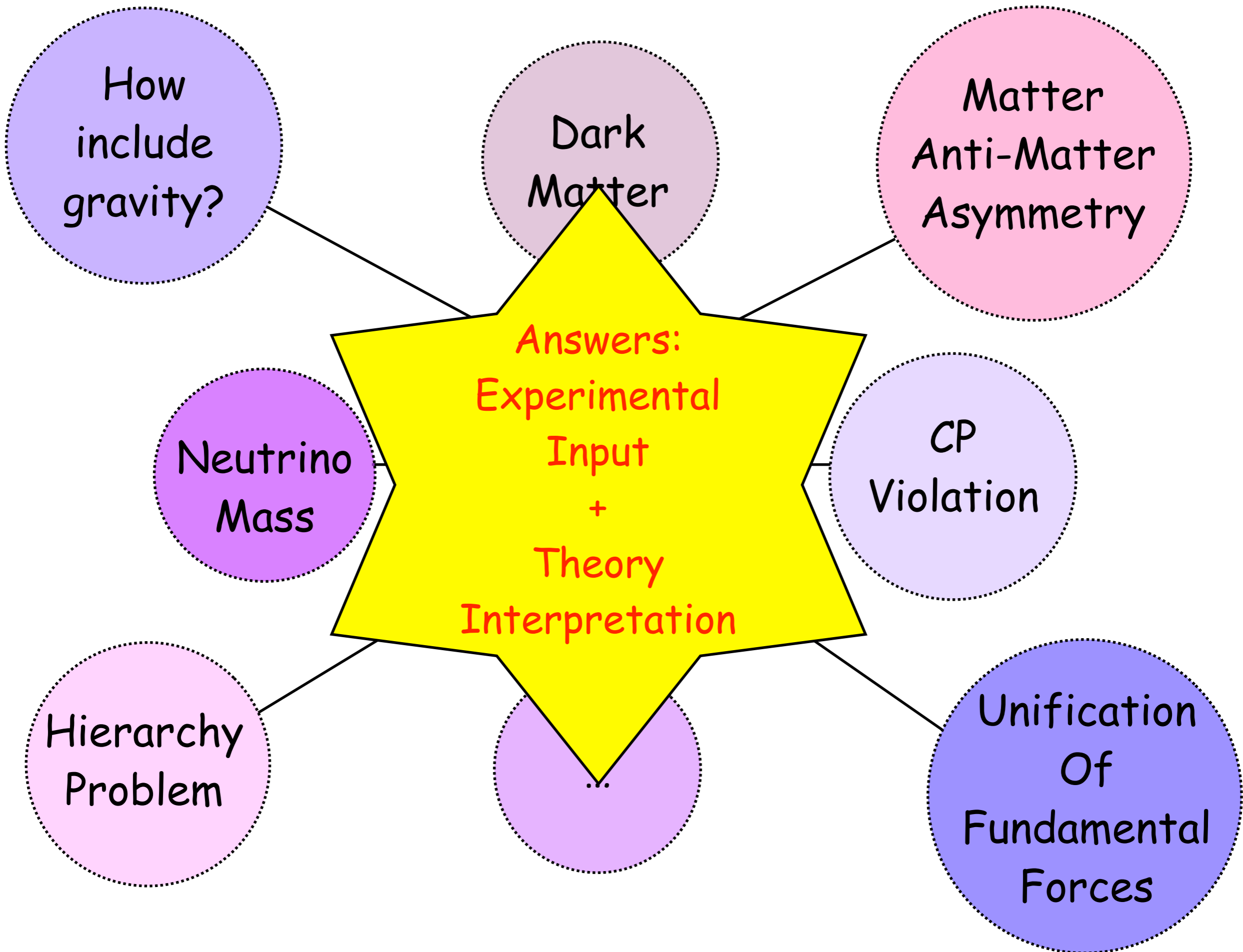
Unification Of Fundamental Forces

...

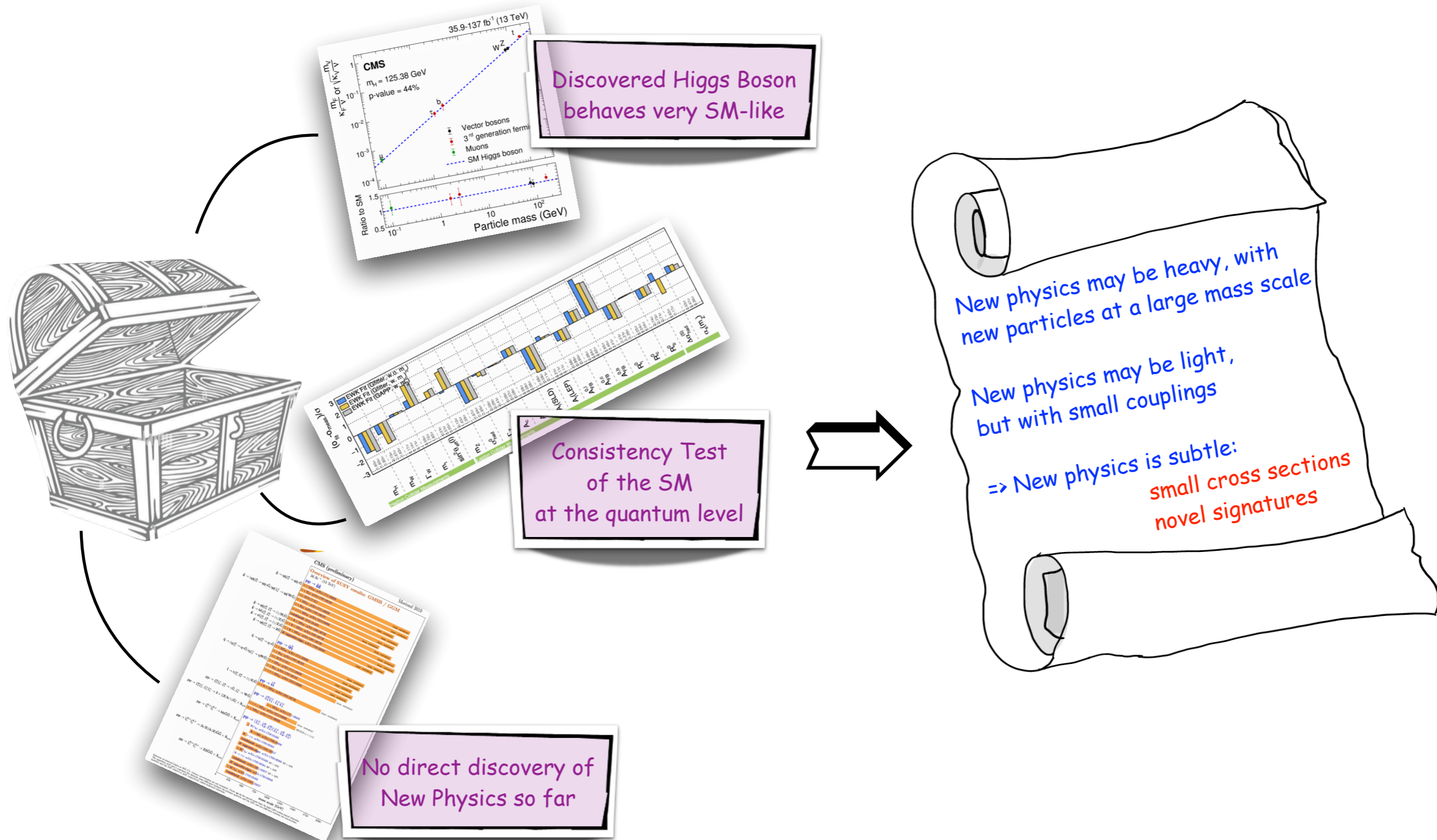
Neutrino Mass

Hierarchy Problem





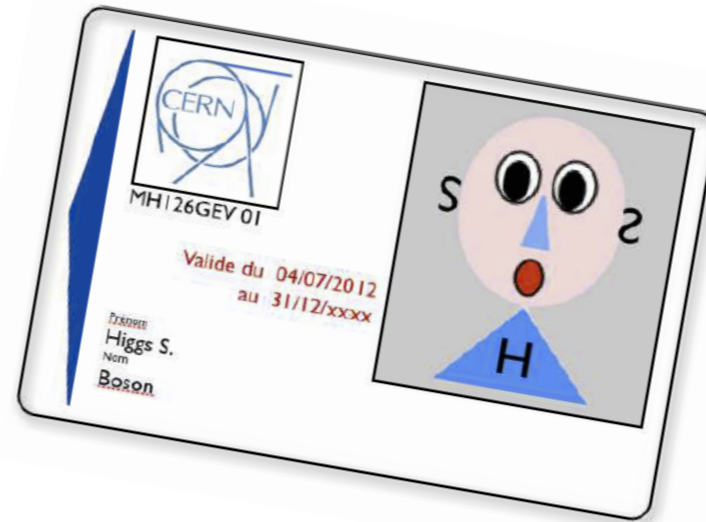
# Status



# How to corner New Physics?

- ♦ **Experimental reality:** No Beyond the Standard Model Physics discovered so far!  
Guido Altarelli, 16/1/12, KIT: „The situation is depressing, but not desperate.“

- ♦ We have the SM-like Higgs boson  
**What can we learn from Higgs physics?**



- ♦ **Corner new physics:**

**Combination of all available information** from different sectors and experiments:  
Higgs physics, Dark Matter searches, baryogenesis, astrophysics, cosmology, ...

Experiment: **Precision analyses** - new analysis techniques, ML, ...

Theory: **Precision predictions** for observables for SM, BSM (specific models, EFT)

# Higgs Potential Parameters



# The Role of the Higgs Boson Mass

## ✦ Present Accuracy:

[ATLAS,CMS]

$$M_H = 125.09 \pm 0.21 \text{ (stat)} \pm 0.11 \text{ (syst)} \text{ GeV}$$

## ✦ Why precision?

\* Self-consistency test of SM at quantum level  
(e.g.: Higgs loop corrections to **W boson mass**)

\*  $M_H \leftrightarrow$  **stability of the electroweak vacuum**

[Degrassi eal;Bednyakov eal]

\* Higgs mass uncertainty feeds back in uncertainty on **Higgs observables**

\* **Test parameter relations** in beyond-SM theories

$\Rightarrow$  **indirect constraint of viable BSM parameter space!**

# The Role of the Higgs Boson Mass

## ♦ Present Accuracy:

[ATLAS,CMS]

$$M_H = 125.09 \pm 0.21 \text{ (stat)} \pm 0.11 \text{ (syst)} \text{ GeV}$$

## ♦ Why precision?

\* Self-consistency test of SM at quantum level  
(e.g.: Higgs loop corrections to **W boson mass**)

\*  $M_H \leftrightarrow$  **stability of the electroweak vacuum**

[Degrassi eal;Bednyakov eal]

\* Higgs mass uncertainty feeds back in uncertainty on **Higgs observables**

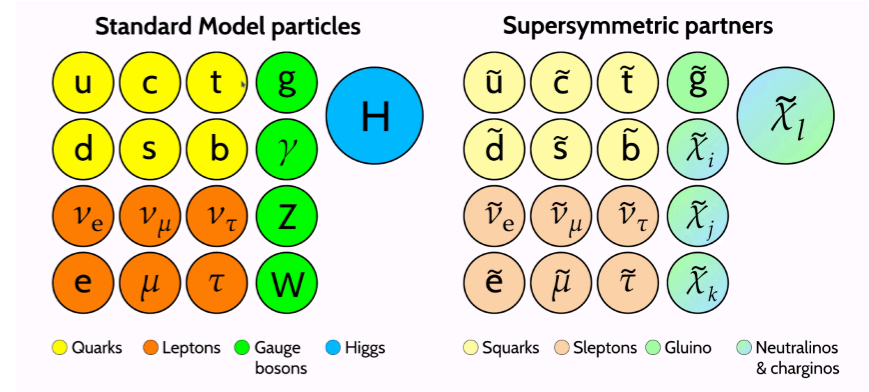
\* **Test parameter relations** in beyond-SM theories

$\Rightarrow$  **indirect constraint of viable BSM parameter space!**

# Supersymmetry

## Supersymmetry:

- enlarged particle spectrum: each SM particle has SUSY partner
- enlarged Higgs sector: requires at least 2 complex Higgs doublets



## Minimal Supersymmetric extension (MSSM): 2 complex Higgs doublets

5 Higgs bosons:  $h, H, A, H^+, H^-$

4 neutralinos:  $\tilde{\chi}_i^0 (i = 1, \dots, 4)$

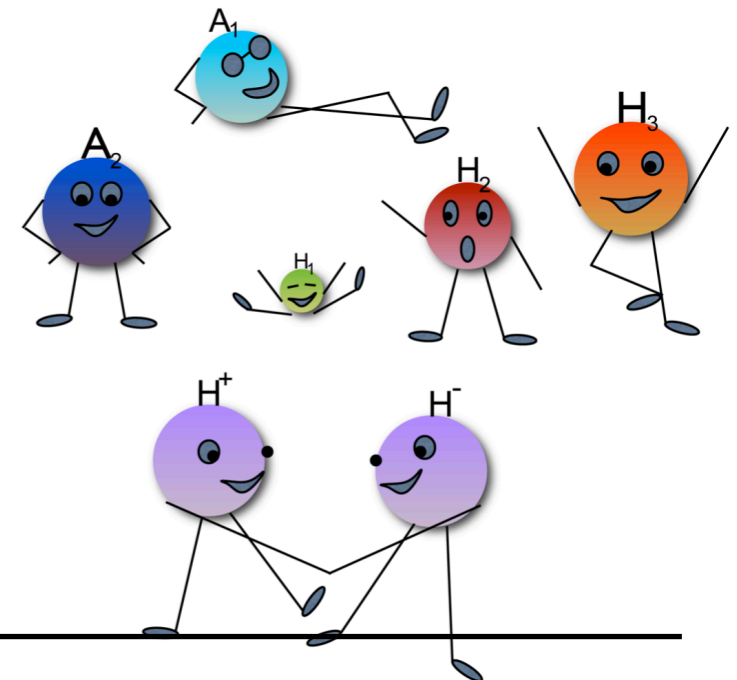
## Next-to-MSSM (NMSSM): 2 complex Higgs doublets plus complex singlet field

- enlarged Higgs and neutralino sector

7 Higgs bosons:  $H_1, H_2, H_3, A_1, A_2, H^+, H^-$

5 neutralinos:  $\tilde{\chi}_i^0 (i = 1, \dots, 5)$

- solves mu problem, interesting phenomenology



# Higgs Mass in New Physics Extensions - Supersymmetry

## Higgs boson mass:

- \* SM: fundamental parameter, not predicted by the theory
- \* Supersymmetry: calculable from input parameters; quantum corrections  $\Delta m^2_H$  are important!

$$\text{MSSM: } m_H^2 \approx M_Z^2 \cos^2 2\beta + \Delta m_H^2 \leftarrow (85 \text{ GeV})^2!$$

$$\text{NMSSM: } m_H^2 \approx M_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin^2 2\beta + \Delta m_H^2 \leftarrow (55 \text{ GeV})^2$$

## NMSSM:

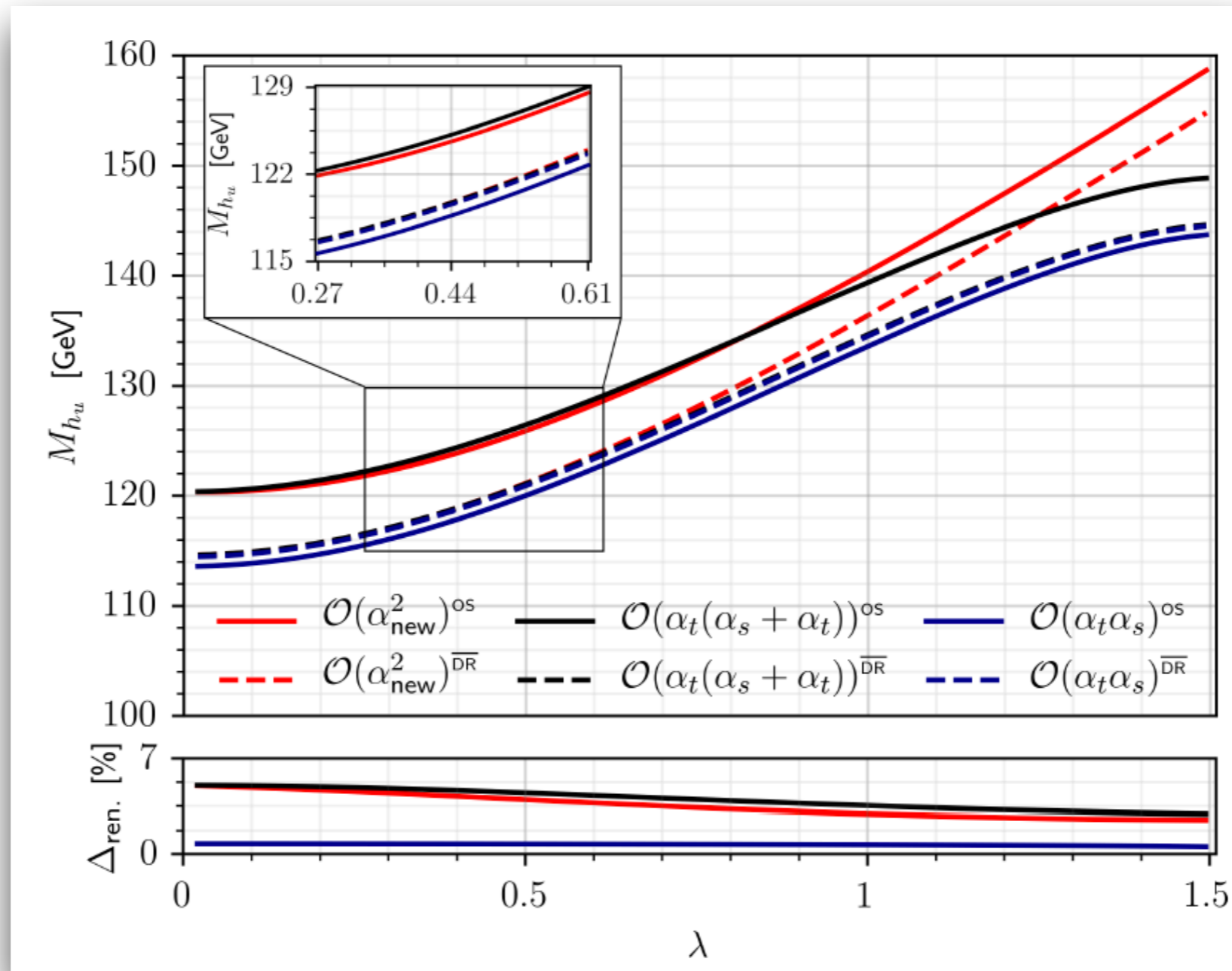
- \* less important loop corrections needed compared to the MSSM



# $\mathcal{O}(\alpha_{\text{new}}^2) \equiv \mathcal{O}((\alpha_\lambda + \alpha_K + \alpha_\dagger)^2)$ Mass Corrections in the CP-Violating NMSSM

Corrections to  $h_u$ -like Higgs ( $\hat{=}$  SM-like Higgs)

[Dao, Gabelmann, MM, Rzehak, '21]



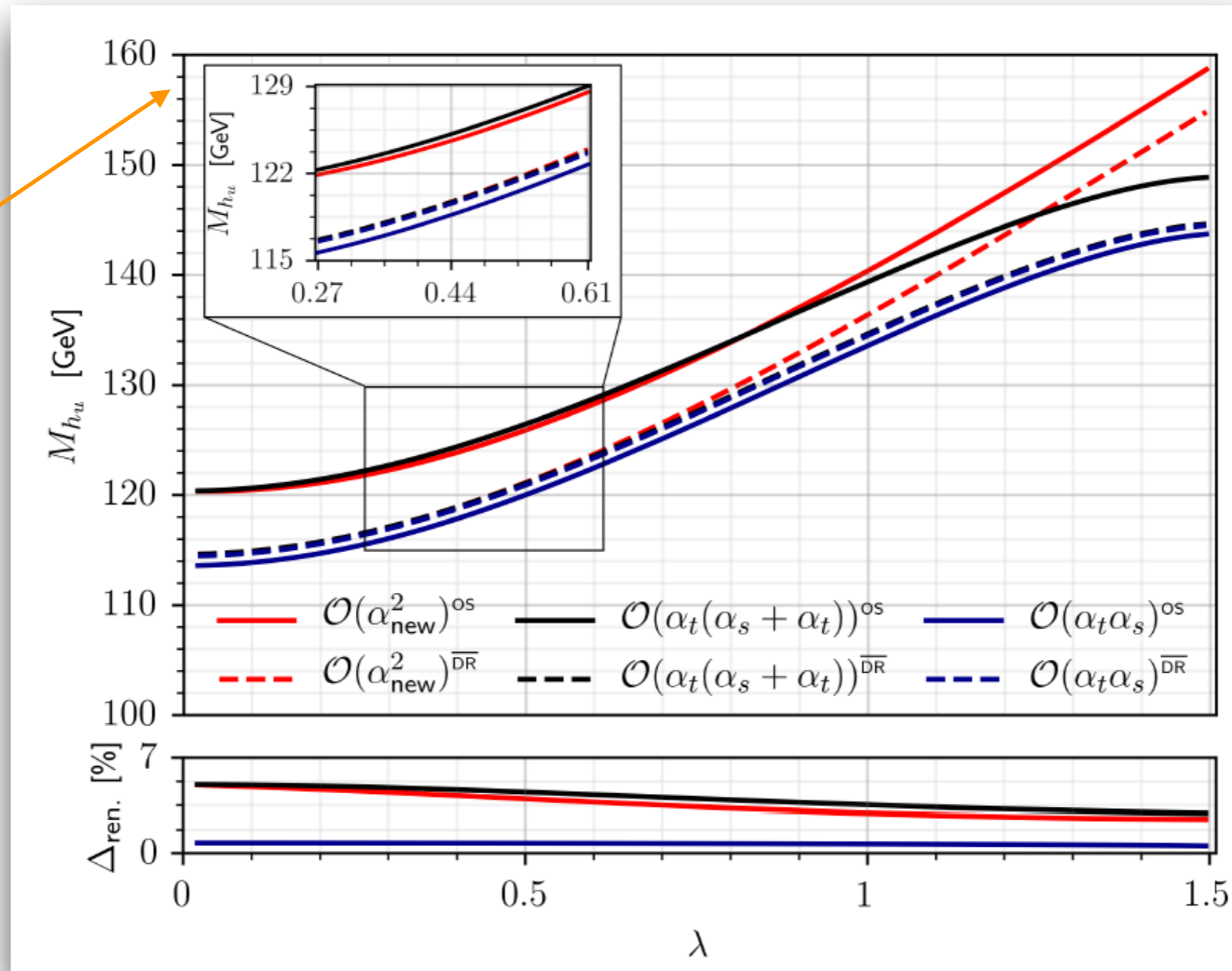
$$\Delta_{\text{ren}} = \frac{|\lambda^{m_t(\overline{\text{DR}})} - \lambda^{m_t(\text{OS})}|}{\lambda^{m_t(\overline{\text{DR}})}} : \text{remaining theoretical error: } \mathcal{O}(\text{few}\%)$$

# $\mathcal{O}(\alpha_{\text{new}}^2) \equiv \mathcal{O}((\alpha_\lambda + \alpha_K + \alpha_\dagger)^2)$ Mass Corrections in the CP-Violating NMSSM

Corrections to  $h_u$ -like Higgs ( $\hat{=}$  SM-like Higgs)

[Dao, Gabelmann, MM, Rzehak, '21]

Zoomed:  
compatible w/  
HiggsSignals after  
including the new  
correction

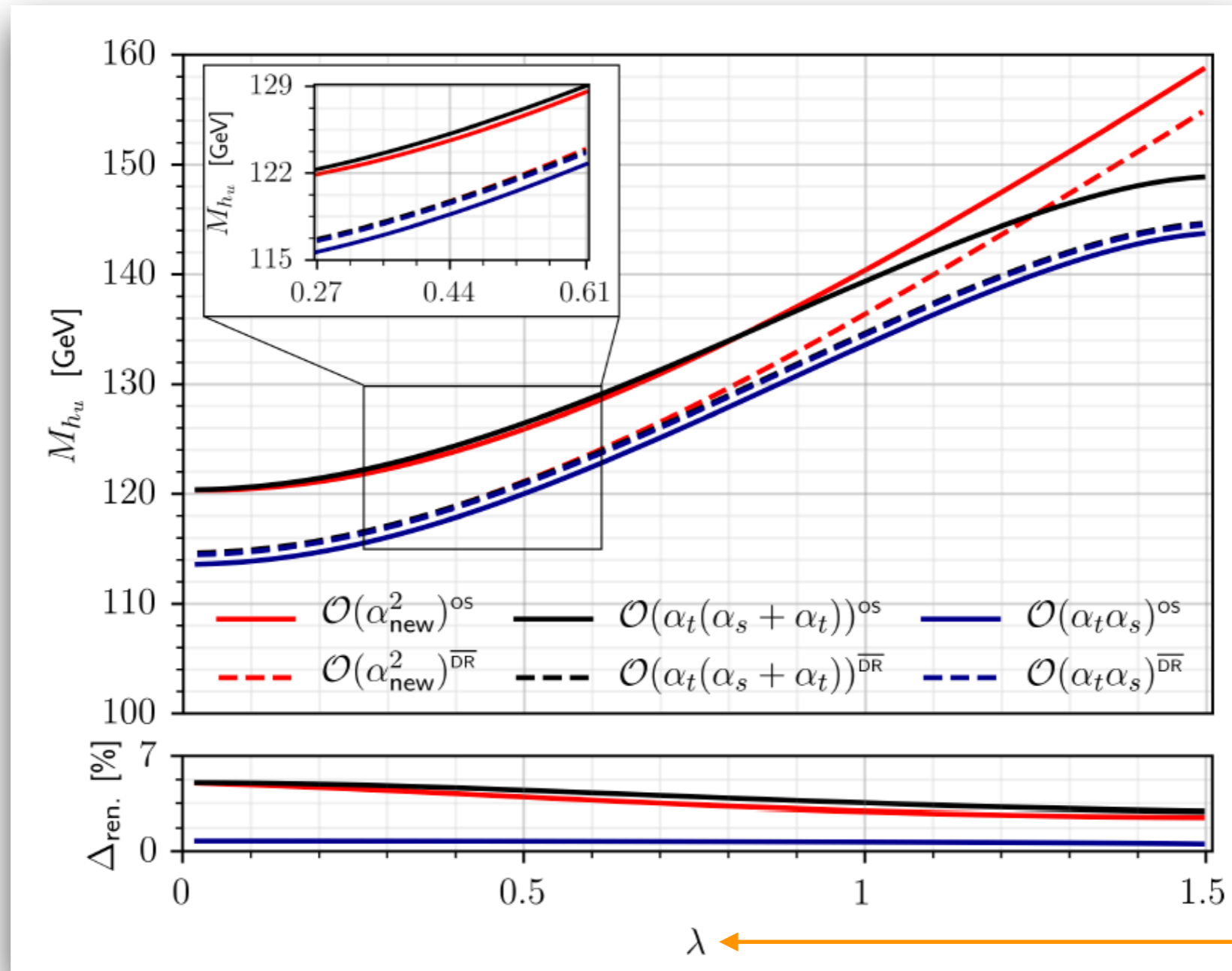


$$\Delta_{\text{ren}} = \frac{|\lambda^{m_t(\overline{\text{DR}})} - \lambda^{m_t(\text{OS})}|}{\lambda^{m_t(\overline{\text{DR}})}} : \text{remaining theoretical error: } \mathcal{O}(\text{few}\%)$$

# $\mathcal{O}(\alpha_{\text{new}}^2) \equiv \mathcal{O}((\alpha_\lambda + \alpha_\kappa + \alpha_\dagger)^2)$ Mass Corrections in the CP-Violating NMSSM

Corrections to  $h_u$ -like Higgs ( $\hat{=}$  SM-like Higgs)

[Dao, Gabelmann, MM, Rzehak, '21]



NMSSM specific couplings  $\lambda, \kappa$  related to new singlet field in superpotential

$$\Delta_{\text{ren}} = \frac{|\lambda^{m_t(\overline{\text{DR}})} - \lambda^{m_t(\text{OS})}|}{\lambda^{m_t(\overline{\text{DR}})}} : \text{remaining theoretical error: } \mathcal{O}(\text{few}\%)$$

# Loop Corrected Trilinear Higgs Self-Couplings at $\mathcal{O}(\alpha_t(\alpha_s+\alpha_t))$

- Masses  $M_{ij}=(\partial^2 V_H/\phi_i \phi_j)|_{\phi=0}$  and Higgs self-couplings  $\lambda_{ijk}=(\partial^3 V_H/\phi_i \phi_j \phi_k)|_{\phi=0}$  related through Higgs potential  $V_H \Rightarrow$  catch up in precision w/ masses

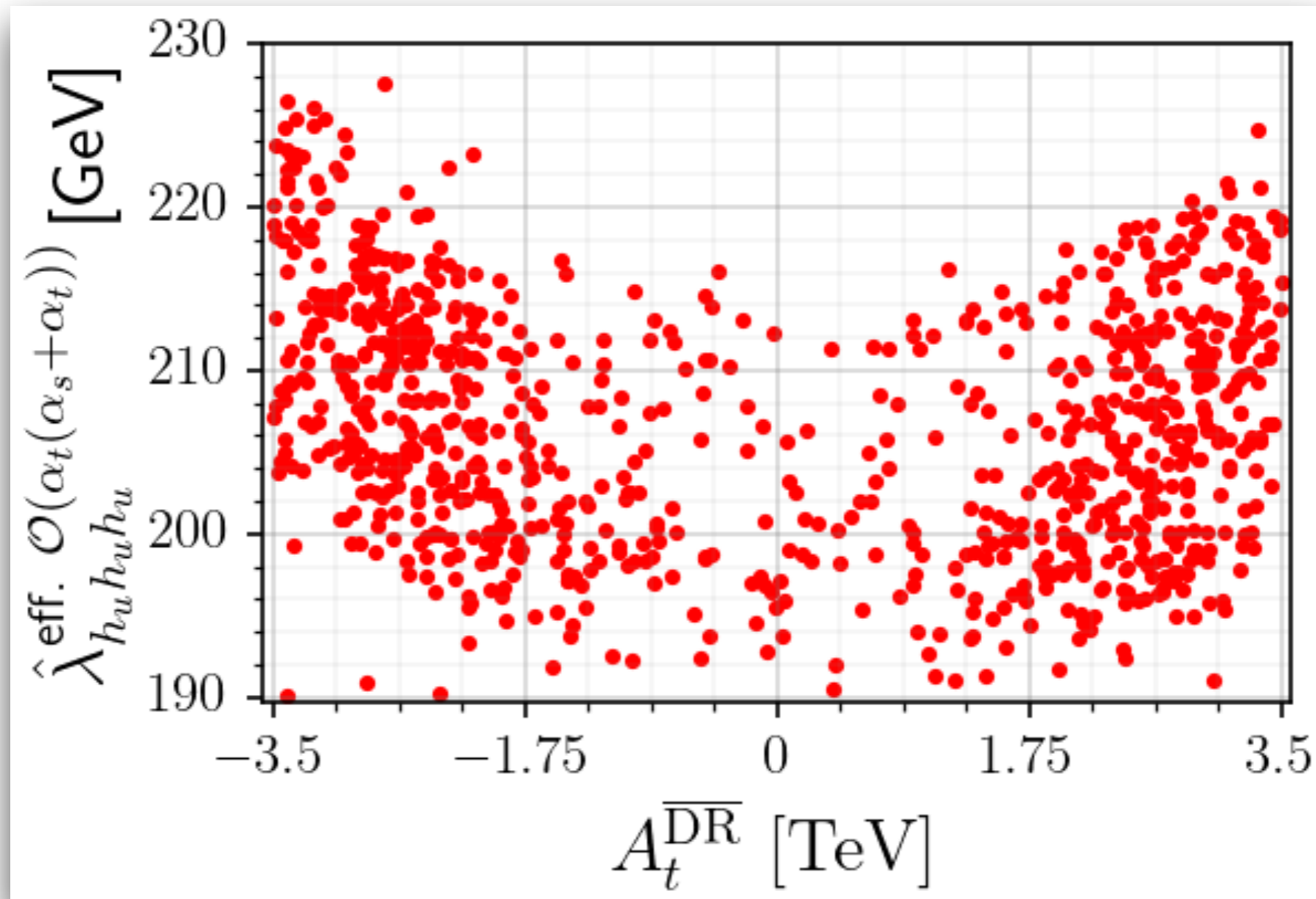


- Available in NMSSM:
  - full 1-loop [Dao,MM,Streicher,Walz,'13]
  - 2-loop  $\mathcal{O}(\alpha_t\alpha_s)$  [Dao,MM,Ziesche,'15]
  - 2-loop  $\mathcal{O}(\alpha_t(\alpha_t+\alpha_s))$  [Borschensky,Dao,Gabelmann,MM,Rzehak,'22]

# Loop Corrected Trilinear Higgs Self-Couplings at $\mathcal{O}(\alpha_t(\alpha_s+\alpha_t))$

Corrections to  $h_u$ -like Higgs ( $\hat{=}$  SM-like Higgs)

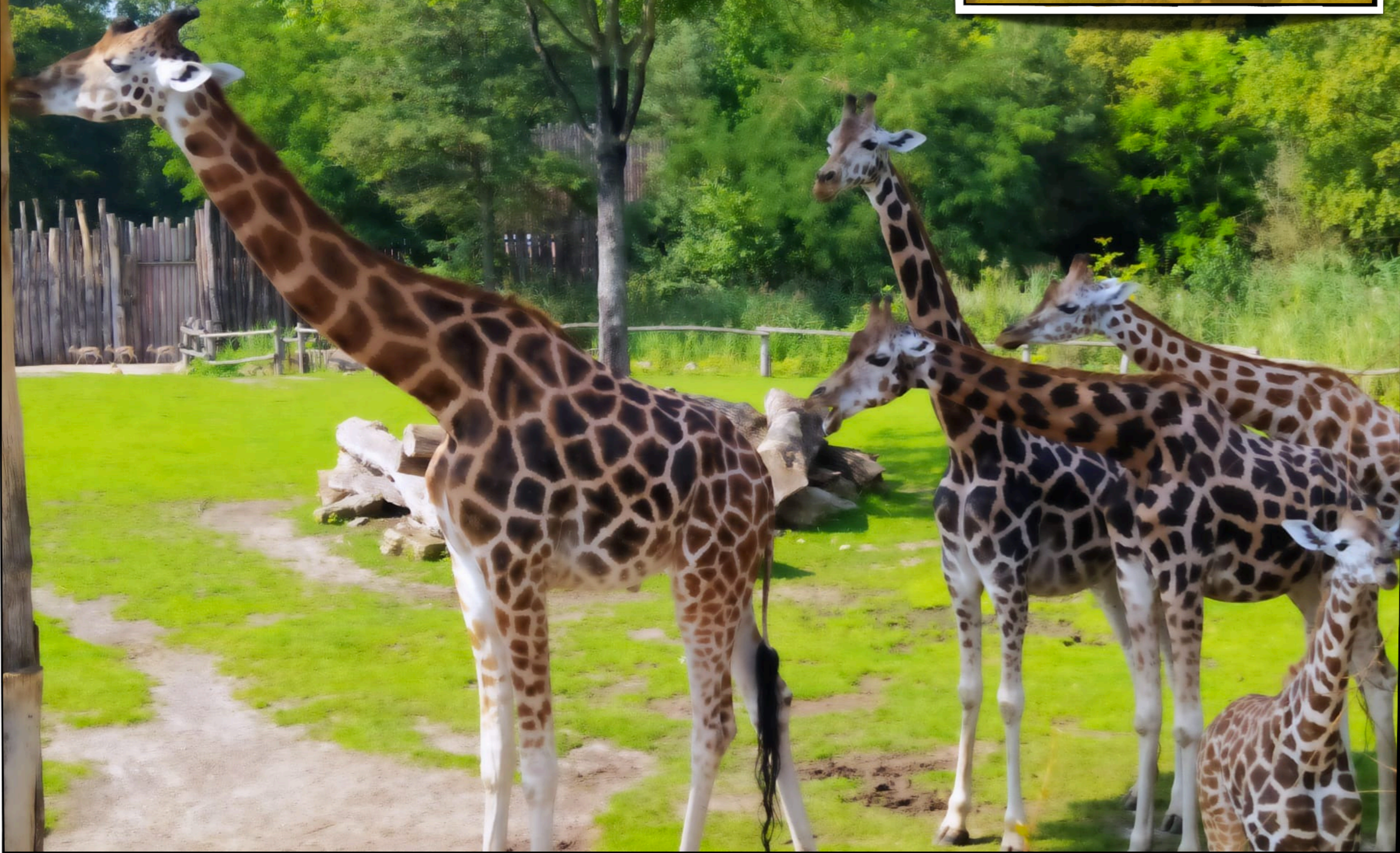
[Borschensky, Dao, Gabelmann, MM, Rzehak, '22]



Theoretical & single Higgs data constraints => trilinear coupling values are SM-like,

$$\lambda_{HHH}^{\text{SM}} = \frac{3M_H^2}{v} = 191 \text{ GeV, within theoretical uncertainty}$$

*More on Precision:  
Higgs Decays*



# Status Standard Model Decays

[Taken from talk by M. Spira]

Partial Width	QCD	Electroweak	Total	on-shell Higgs
$H \rightarrow b\bar{b}/c\bar{c}$	$\sim 0.2\%$	$\sim 0.5\%$	$\sim 0.5\%$	NNNNLO / NLO
$H \rightarrow \tau^+\tau^-/\mu^+\mu^-$		$\sim 0.5\%$	$\sim 0.5\%$	NLO
$H \rightarrow gg$	$\sim 3\%$	$\sim 1\%$	$\sim 3\%$	NNNLO approx. / NLO
$H \rightarrow \gamma\gamma$	$< 1\%$	$< 1\%$	$\sim 1\%$	NLO / NLO
$H \rightarrow Z\gamma$	$< 1\%$	$\sim 5\%$	$\sim 5\%$	(N)LO / LO
$H \rightarrow WW/ZZ \rightarrow 4f$	$< 0.5\%$	$\sim 0.5\%$	$\sim 0.5\%$	(N)NLO

Impact of EW corrections on SM Higgs branching ratios  $\Delta\text{BR} = \frac{\text{BR}^{\text{QCD\&EW}} - \text{BR}^{\text{QCD}}}{\text{BR}^{\text{QCD}}}$  [HDECAY]

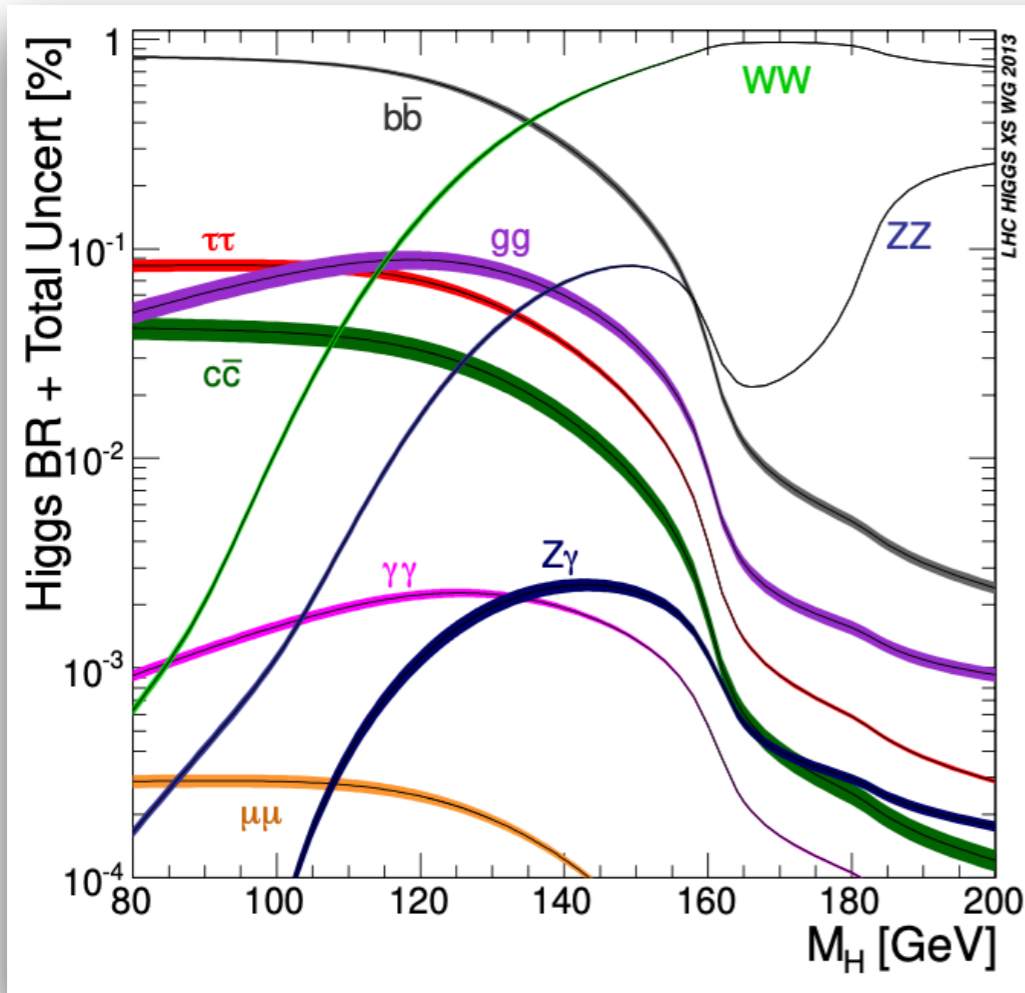
$\Delta\text{BR}$	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	$gg$	$\gamma\gamma$	$Z\gamma$	$W^+W^-$	$ZZ$
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

# Standard Model Branching Ratios

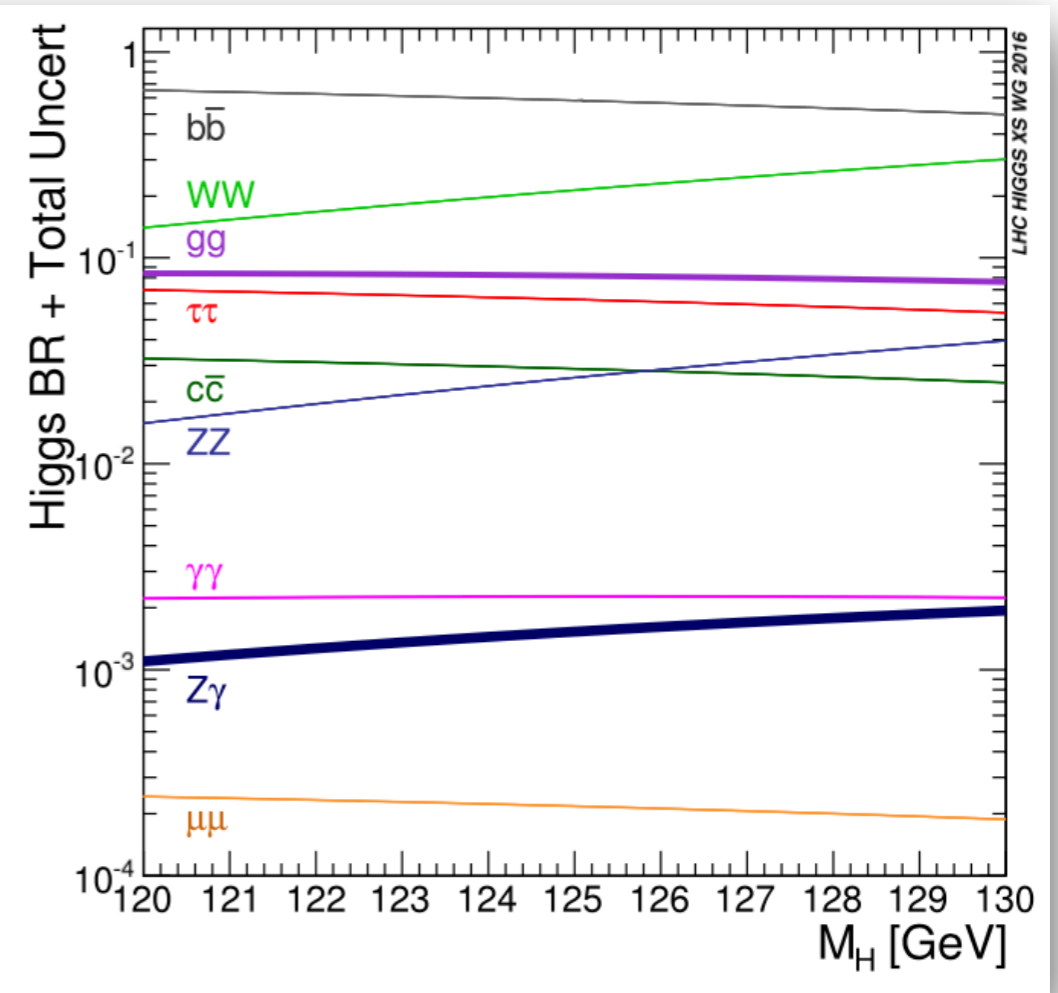
[HDECAY & Prophecy4f]

[Denner, Heinemeyer, Puljak, Rebutzi, Spira]

YR3



YR4



- Total uncertainties: parametric & theory uncertainties added linearly
- Refinements of input parameters, full NLO EW corrs. to  $H \rightarrow f\bar{f}$ , NLO quark-mass effects in  $H \rightarrow gg$





# Higher-Order Impact in Beyond-SM Theories (BSM)

Impact of EW corrections on SM Higgs branching ratios  $\Delta\text{BR} = \frac{\text{BR}^{\text{QCD\&EW}} - \text{BR}^{\text{QCD}}}{\text{BR}^{\text{QCD}}}$  [HDECAY]

$\Delta\text{BR}$	$b\bar{b}$	$\tau^+\tau^-$	$\mu^+\mu^-$	$s\bar{s}$	$c\bar{c}$	$gg$	$\gamma\gamma$	$Z\gamma$	$W^+W^-$	$ZZ$
	-1.76%	-1.59%	-3.52%	2.24%	-3.81%	4.34%	-2.29%	-0.71%	3.68%	1.61%

Example: Impact of EW corrections on branching ratios of non-SM-like 2HDM Higgs boson

Type	$\Delta\text{BR}_{H\tau^+\tau^-}^{S_1}$	$\Delta\text{BR}_{H\tau^+\tau^-}^{S_2}$	$\Delta\text{BR}_{H\tau^+\tau^-}^{S_3}$	$\Delta\text{BR}_{H\tau^+\tau^-}^{S_4}$	$\Delta\text{BR}_{H\tau^+\tau^-}^{\overline{\text{MS}}}$
I	$\lesssim 15.0\%$ (49%)	$\lesssim 15.0\%$ (51%)	$\lesssim 15.0\%$ (48%)	$\lesssim 15.0\%$ (55%)	$\lesssim 60.0\%$ (50%)
	$\lesssim 35.0\%$ (88%)	$\lesssim 35.0\%$ (88%)	$\lesssim 35.0\%$ (77%)	$\lesssim 35.0\%$ (88%)	$\gtrsim 100.0\%$ (40%)
II	$\lesssim 15.0\%$ (54%)	$\lesssim 20.0\%$ (53%)	$\lesssim 10.0\%$ (51%)	$\lesssim 25.0\%$ (47%)	$\lesssim 85.0\%$ (14%)
	$\lesssim 25.0\%$ (91%)	$\lesssim 30.0\%$ (90%)	$\lesssim 35.0\%$ (90%)	$\lesssim 40.0\%$ (86%)	$\gtrsim 100.0\%$ (84%)
LS	$\lesssim 15.0\%$ (54%)	$\lesssim 17.5\%$ (48%)	$\lesssim 7.5\%$ (46%)	$\lesssim 25.0\%$ (46%)	$\lesssim 77.5\%$ (15%)
	$\lesssim 27.5\%$ (90%)	$\lesssim 30.0\%$ (88%)	$\lesssim 30.0\%$ (88%)	$\lesssim 40.0\%$ (85%)	$\gtrsim 100.0\%$ (81%)
FL	$\lesssim 15.0\%$ (55%)	$\lesssim 17.5\%$ (48%)	$\lesssim 7.5\%$ (46%)	$\lesssim 25.0\%$ (46%)	$\lesssim 77.5\%$ (15%)
	$\lesssim 27.5\%$ (90%)	$\lesssim 30.0\%$ (88%)	$\lesssim 30.0\%$ (88%)	$\lesssim 40.0\%$ (85%)	$\gtrsim 100.0\%$ (81%)

Type	$\Delta\text{BR}_{HZA}^{S_1}$	$\Delta\text{BR}_{HZA}^{S_2}$	$\Delta\text{BR}_{HZA}^{S_3}$	$\Delta\text{BR}_{HZA}^{S_4}$	$\Delta\text{BR}_{HZA}^{\overline{\text{MS}}}$
I	$\lesssim 5.0\%$ (51%)	$\lesssim 5.0\%$ (51%)	$\lesssim 10.0\%$ (46%)	$\lesssim 10.0\%$ (53%)	$\lesssim 80.0\%$ (26%)
	$\lesssim 15.0\%$ (80%)	$\lesssim 15.0\%$ (80%)	$\lesssim 30.0\%$ (80%)	$\lesssim 22.5\%$ (83%)	$\gtrsim 100.0\%$ (52%)
II	$\lesssim 5.0\%$ (68%)	$\lesssim 5.0\%$ (69%)	$\lesssim 10.0\%$ (50%)	$\lesssim 7.5\%$ (73%)	$\lesssim 85.0\%$ (20%)
	$\lesssim 10.0\%$ (91%)	$\lesssim 12.5\%$ (94%)	$\lesssim 25.0\%$ (81%)	$\lesssim 10.0\%$ (90%)	$\gtrsim 100.0\%$ (56%)
LS	$\lesssim 5.0\%$ (65%)	$\lesssim 5.0\%$ (65%)	$\lesssim 10.0\%$ (48%)	$\lesssim 7.5\%$ (41%)	$\lesssim 85.0\%$ (29%)
	$\lesssim 10.0\%$ (86%)	$\lesssim 10.0\%$ (86%)	$\lesssim 27.5\%$ (80%)	$\lesssim 15.0\%$ (90%)	$\gtrsim 100.0\%$ (44%)
FL	$\lesssim 5.0\%$ (65%)	$\lesssim 5.0\%$ (63%)	$\lesssim 10.0\%$ (53%)	$\lesssim 7.5\%$ (51%)	$\lesssim 82.5\%$ (20%)
	$\lesssim 10.0\%$ (88%)	$\lesssim 10.0\%$ (88%)	$\lesssim 15.0\%$ (83%)	$\lesssim 10.0\%$ (84%)	$\gtrsim 100.0\%$ (30%)

Type	$\Delta\text{BR}_{HW^\pm H^\mp}^{S_1}$	$\Delta\text{BR}_{HW^\pm H^\mp}^{S_2}$	$\Delta\text{BR}_{HW^\pm H^\mp}^{S_3}$	$\Delta\text{BR}_{HW^\pm H^\mp}^{S_4}$	$\Delta\text{BR}_{HW^\pm H^\mp}^{\overline{\text{MS}}}$
I	$\lesssim 5.0\%$ (56%)	$\lesssim 5.0\%$ (55%)	$\lesssim 10.0\%$ (49%)	$\lesssim 10.0\%$ (57%)	$\lesssim 70.0\%$ (25%)
	$\lesssim 17.5\%$ (81%)	$\lesssim 17.5\%$ (81%)	$\lesssim 30.0\%$ (78%)	$\lesssim 25.0\%$ (82%)	$\gtrsim 100.0\%$ (52%)

[Krause,MM,'19]

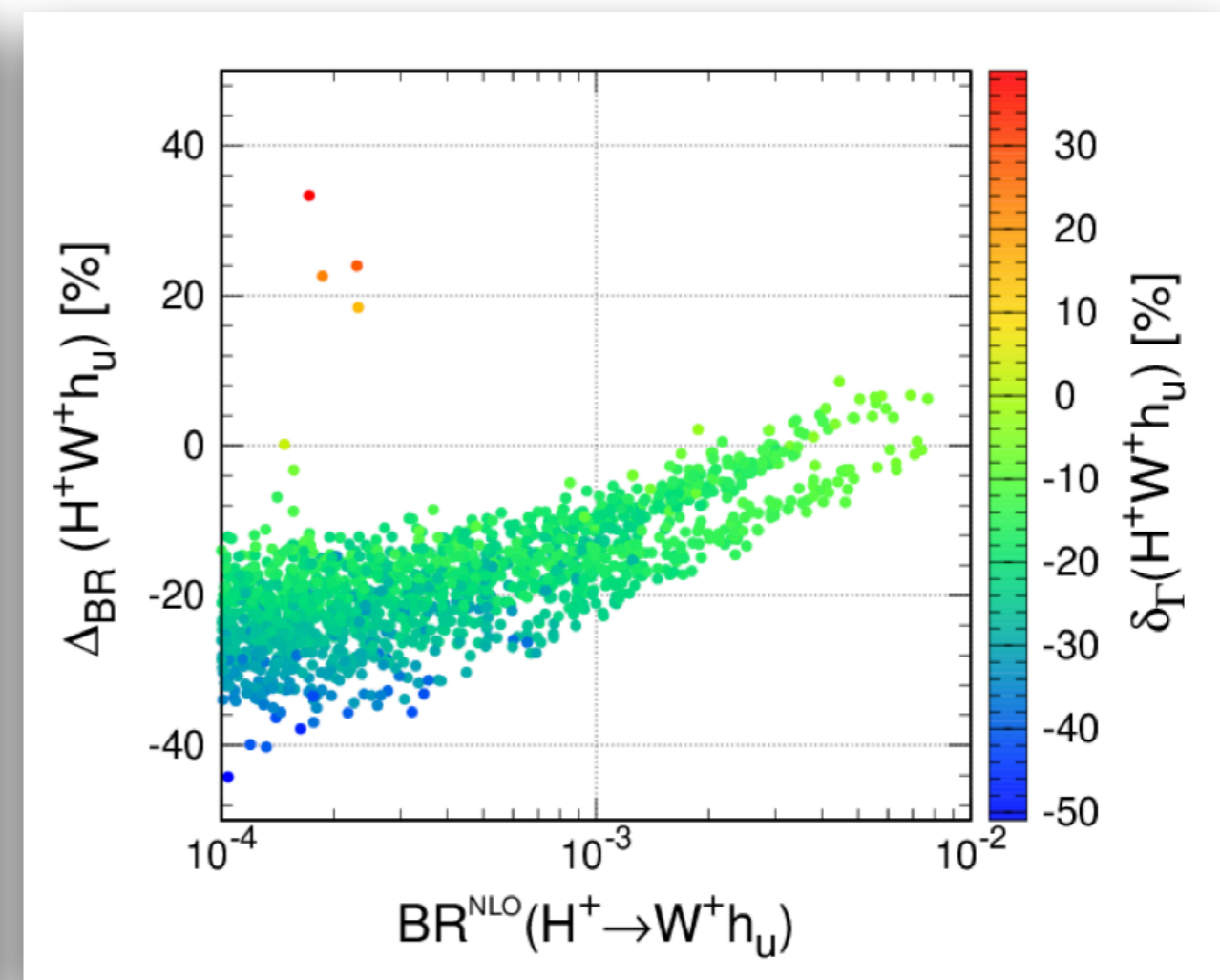
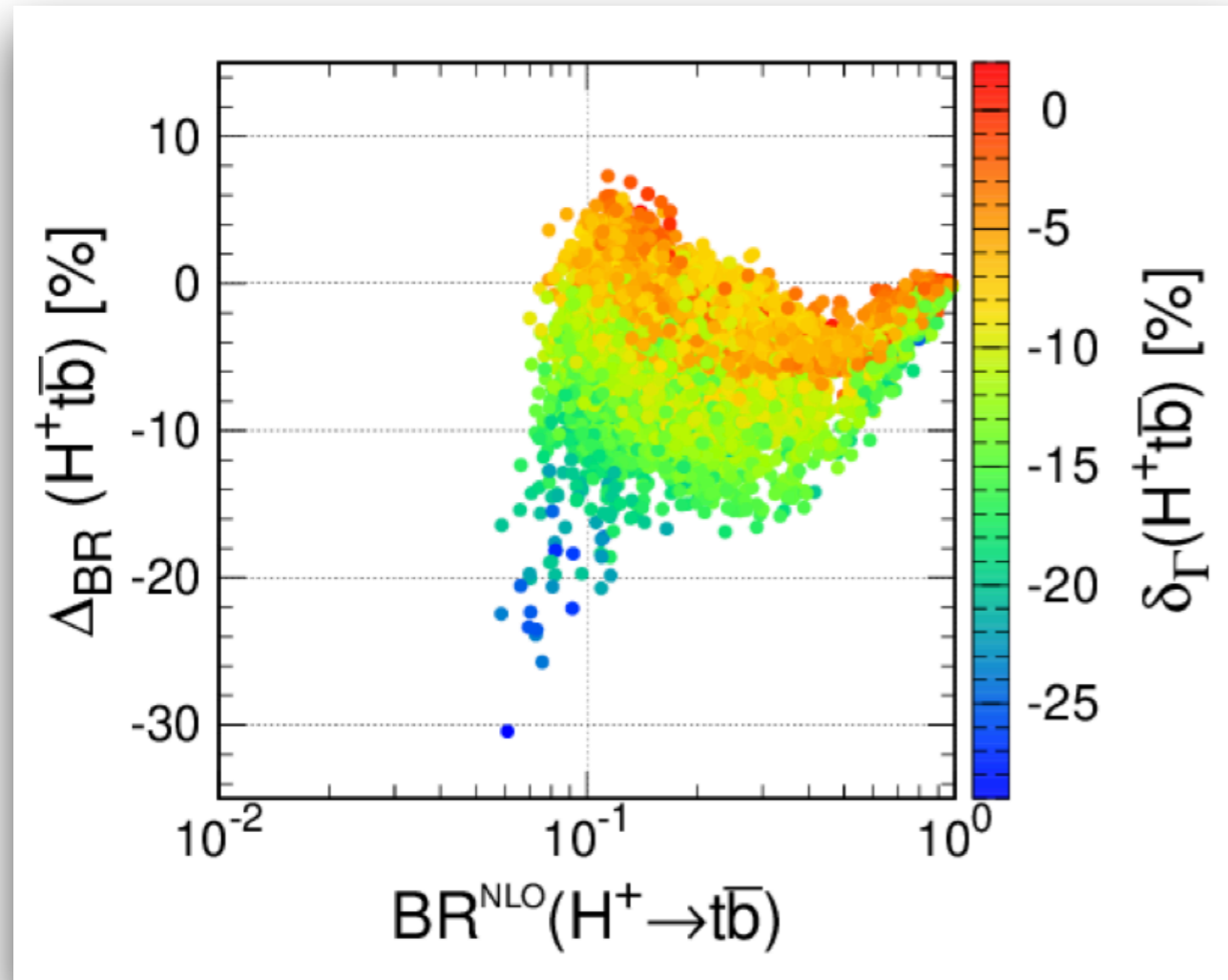
# SUSY-EW & SUSY-QCD Corrected Charged Higgs Decays

Scan points compatible w/ Higgs data

[HiggsSignals,HiggsBounds]

[Dao,Fritz,Krause,MM,Patel,'19]

[Dao,MM,Patel,Sakurai,'21]



- Corrections to charged Higgs decays:

$\Delta_{BR}$ : NLO impact on branching ratio,  $\delta_{\Gamma}$ : NLO impact on partial width

- Implemented in NMSSMCALCEW, includes also NLO neutral Higgs decays

[Dao,Baglio,MM,Patel,Sakurai]

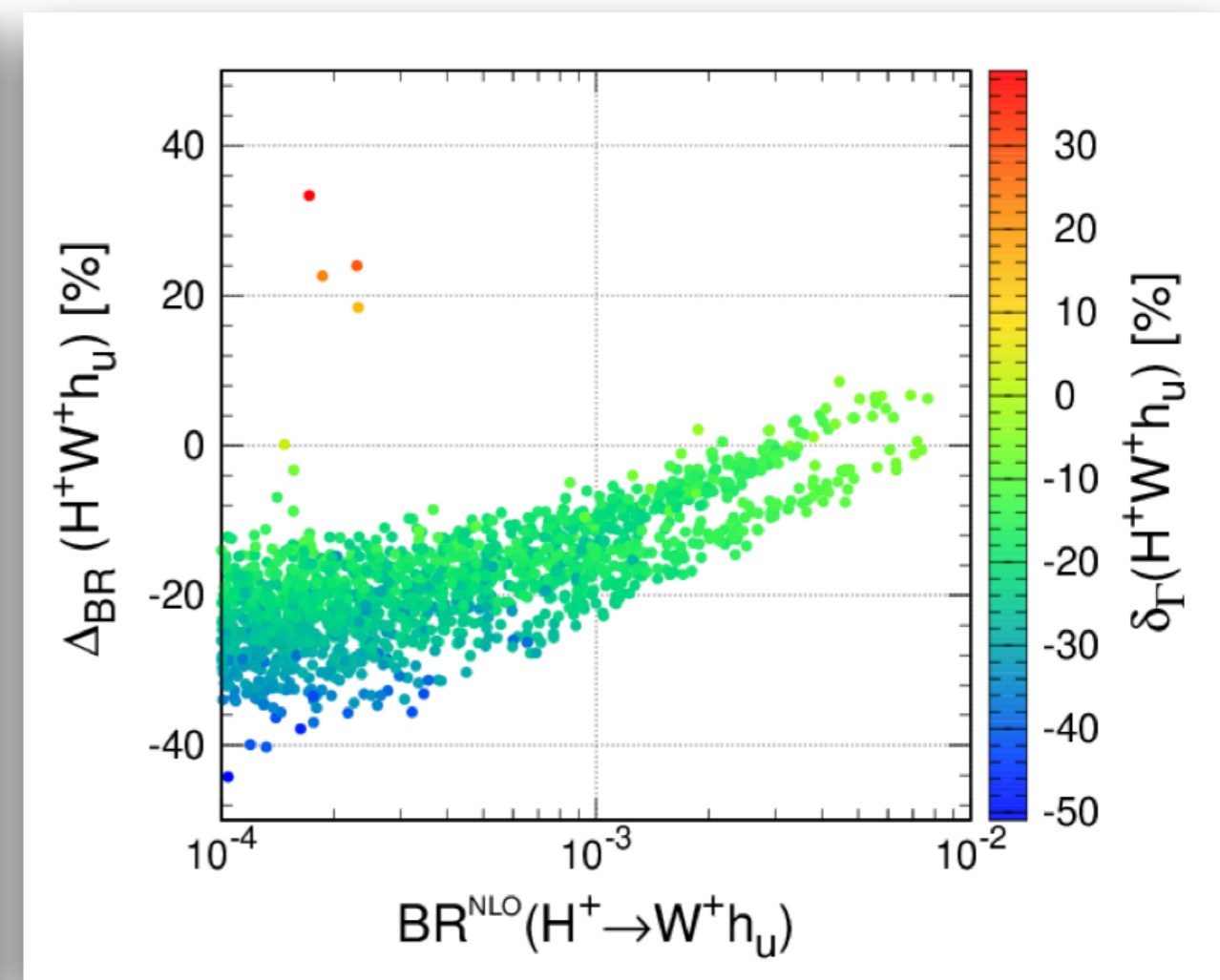
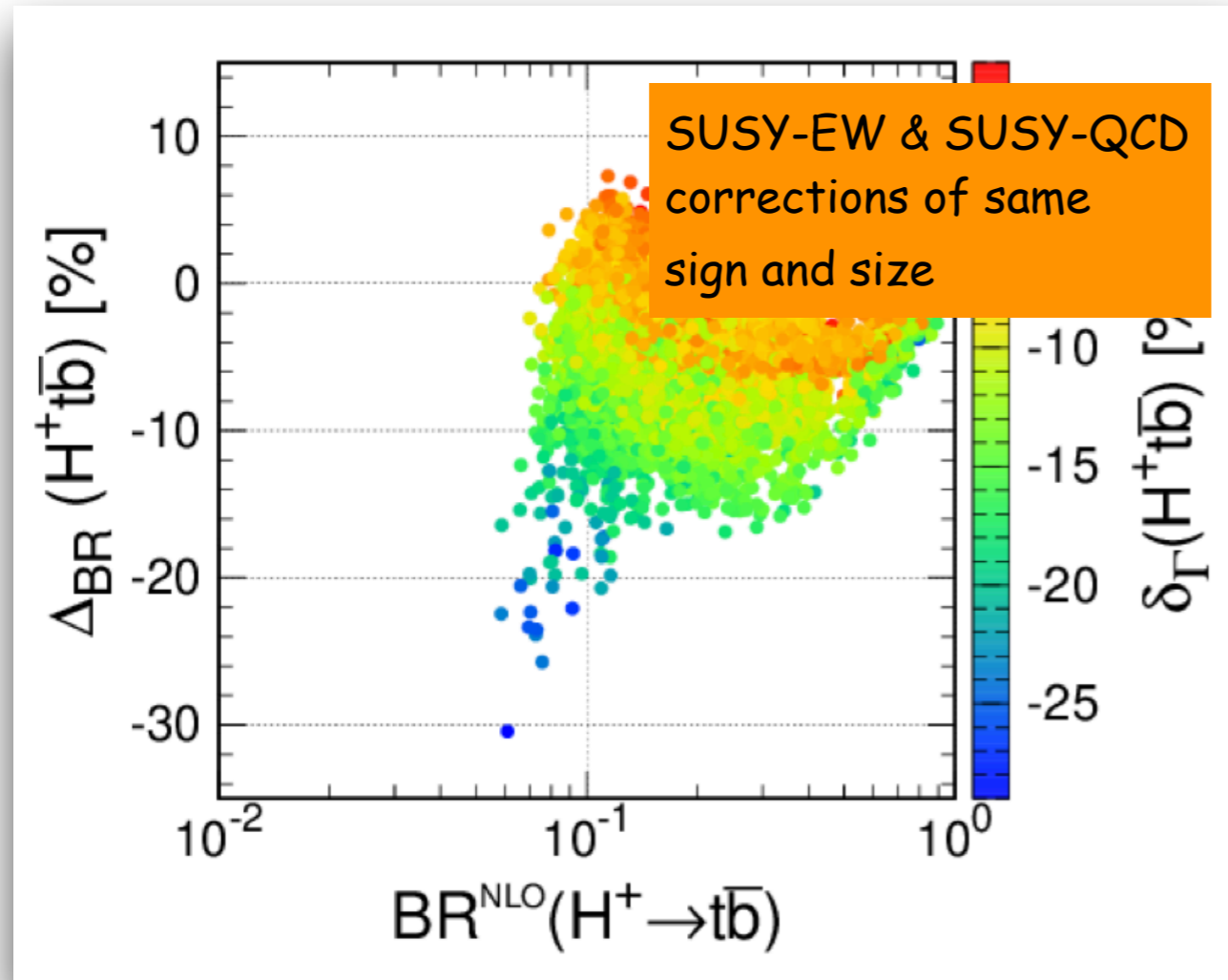
# SUSY-EW & SUSY-QCD Corrected Charged Higgs Decays

Scan points compatible w/ Higgs data

[HiggsSignals,HiggsBounds]

[Dao,Fritz,Krause,MM,Patel,'19]

[Dao,MM,Patel,Sakurai,'21]

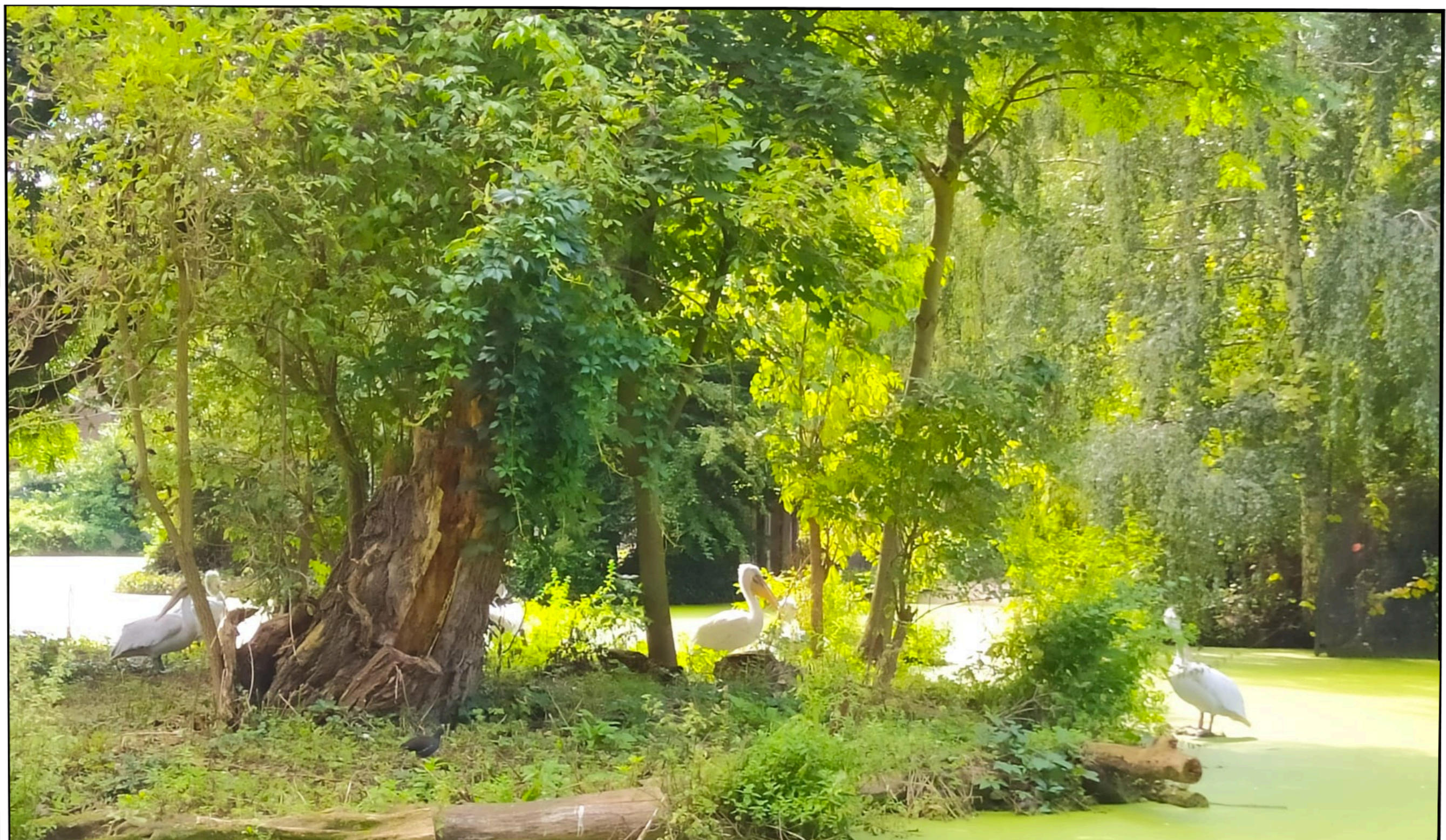


- Corrections to charged Higgs decays:

$\Delta_{BR}$ : NLO impact on branching ratio,  $\delta_{\Gamma}$ : NLO impact on partial width

- Implemented in NMSSMCALCEW, includes also NLO neutral Higgs decays



[Dao,Baglio,MM,Patel,Sakurai]



*HH Production  
Precision & Phenomenology*

# Ultimate Test of the Higgs Mechanism

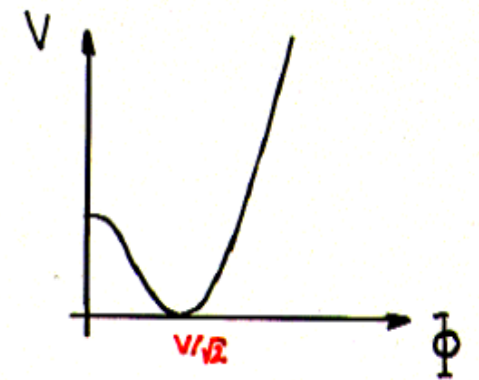
$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{M_H^2}{2v} H^3 + \frac{M_H^2}{8v^2} H^4$$

- Higgs mass :  $M_H = \sqrt{2\lambda} v$
- trilinear Higgs self-coupling :  $\lambda_{HHH} = 3M_H^2/M_Z^2$  
- quadrilinear Higgs self-coupling :  $\lambda_{HHHH} = 3M_H^2/M_Z^4$  
- (units  $\lambda_0 = 33.8 \text{ GeV}/\lambda^2$ )

$$V(\Phi) = \lambda \left( \Phi^\dagger \Phi - \frac{v}{2} \right)^2$$

$$v = 246 \text{ GeV}$$

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v+H \end{pmatrix} \sim$$

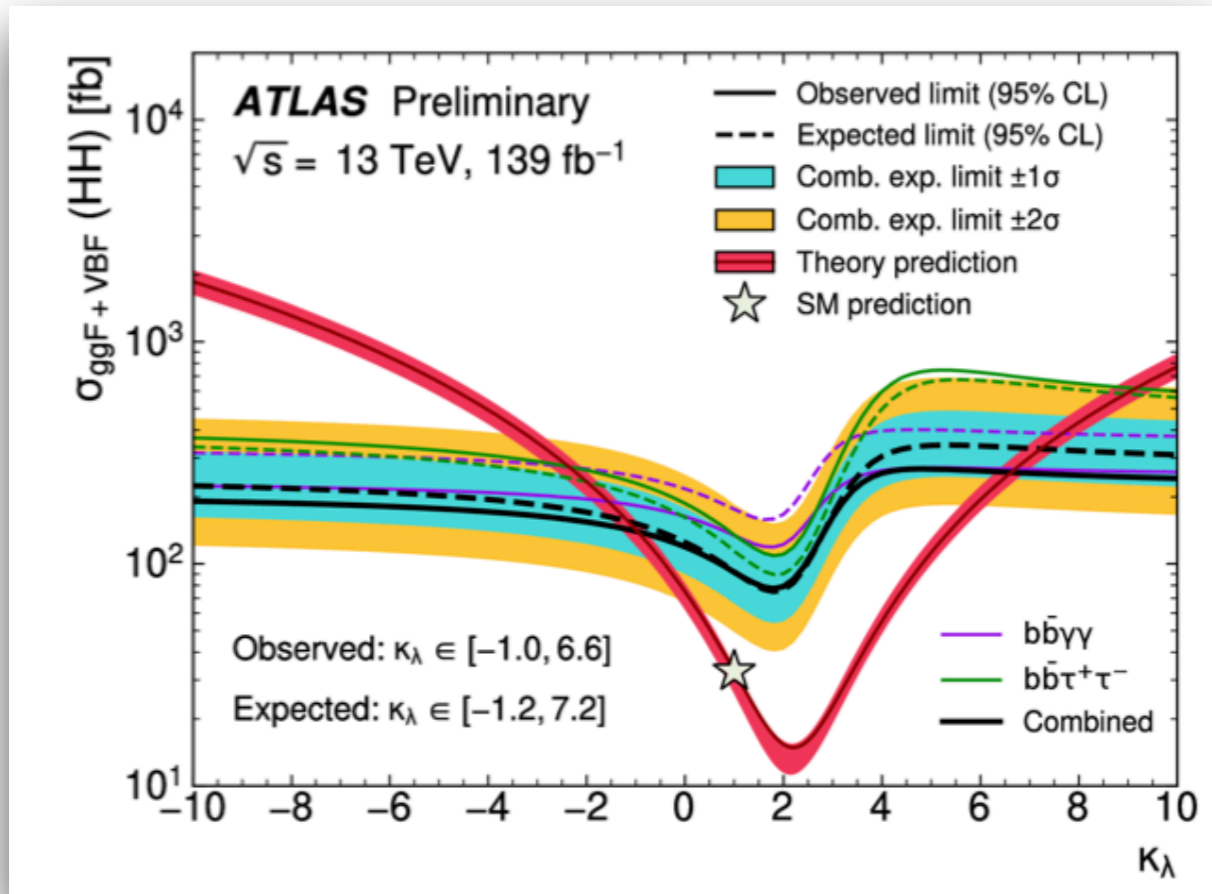


Slides from LCWS, Fermilab, 10/2000  
 [Djouadi, Kilian, MM, Zerwas, 03/99, 04/99]

- (a) trilinear coupling : via Higgs pair production
- (b) quadrilinear coupling : via triple Higgs production

measurement of the Higgs self-couplings  
 and  
 reconstruction of the Higgs potential }  $\Rightarrow$  establish the scalar  
 sector of the Higgs mechanism  
 experimentally

# Experimental Results - Limits on Trilinear Higgs Self-Coupling

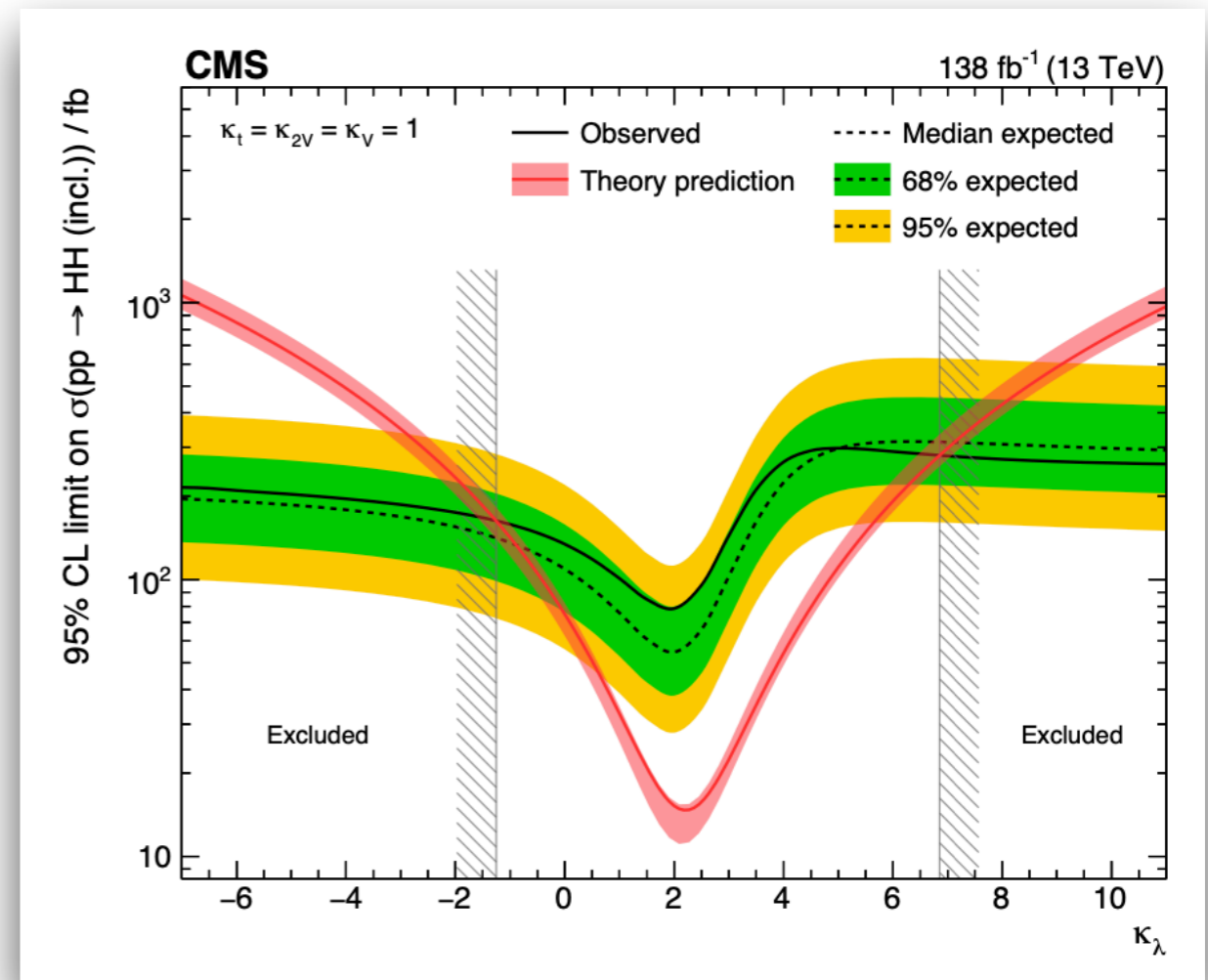


[Rui Zhang, ATLAS, HH Workshop' 22]

Observed:  $\kappa_\lambda \in [-1.0, 6.6]$

Expected:  $\kappa_\lambda \in [-1.2, 7.2]$

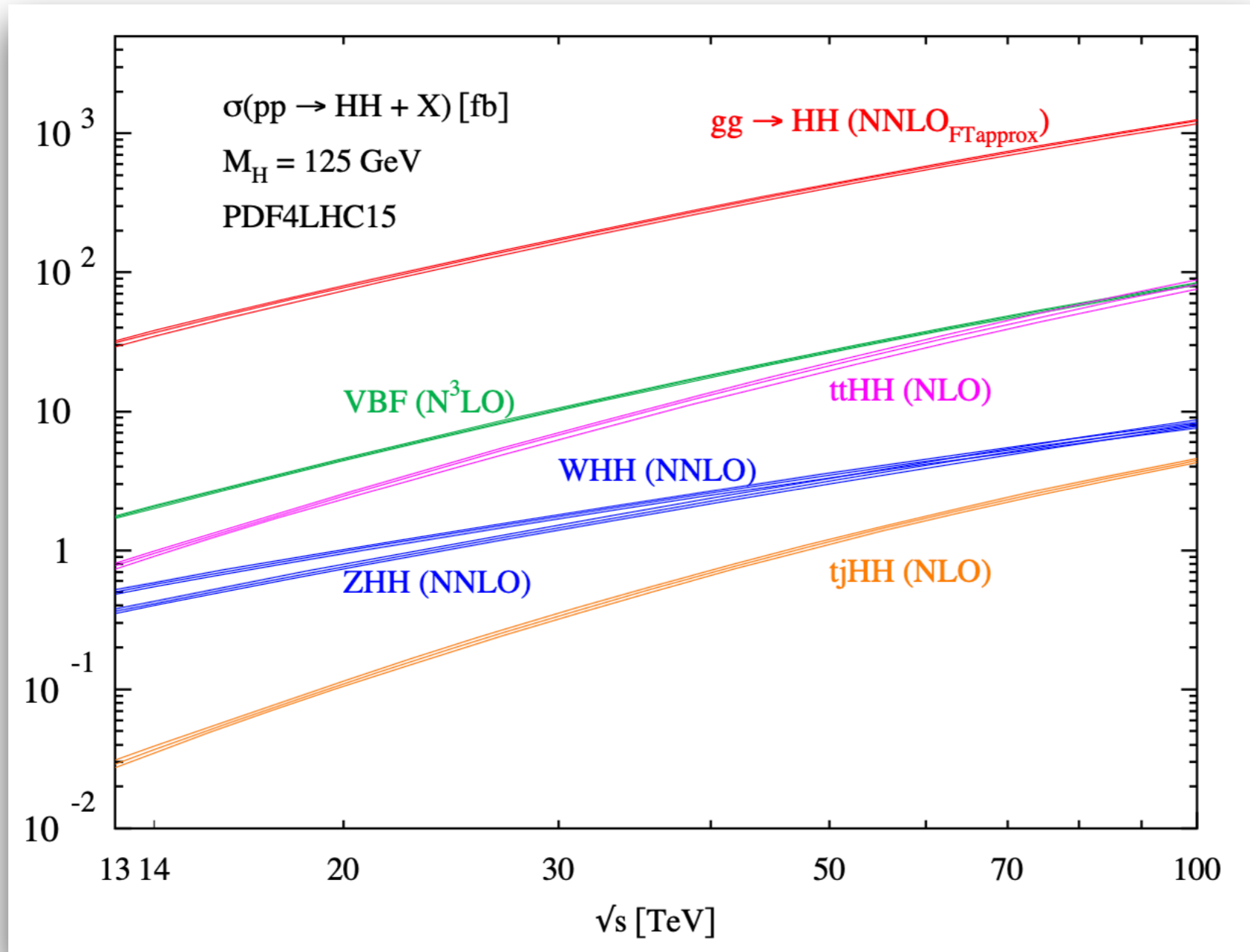
[CMS,2207.00043]



$$-1.24 \leq \kappa_\lambda \leq 6.49$$

# Double Higgs Production Processes

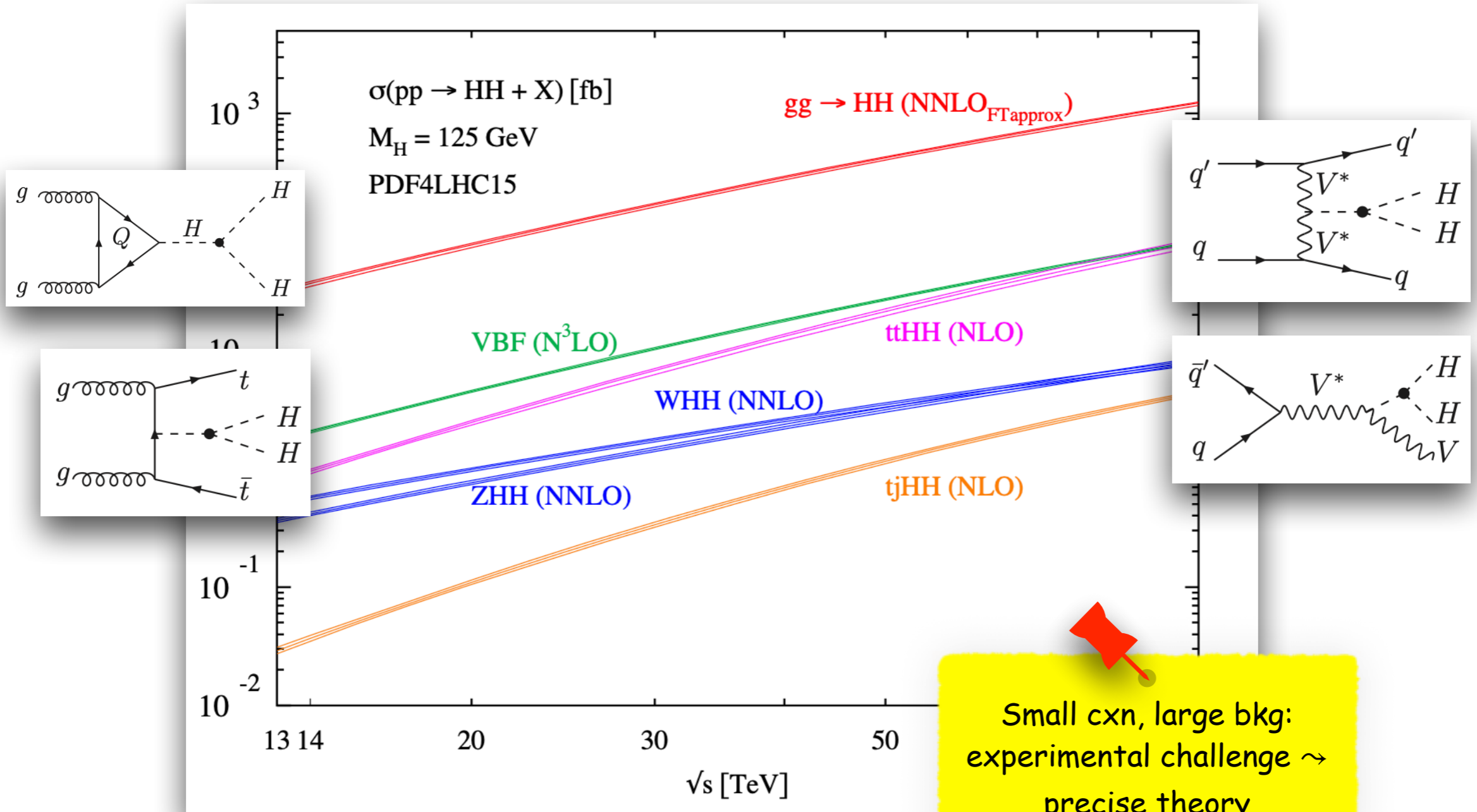
[HH, White paper]





# Double Higgs Production Processes

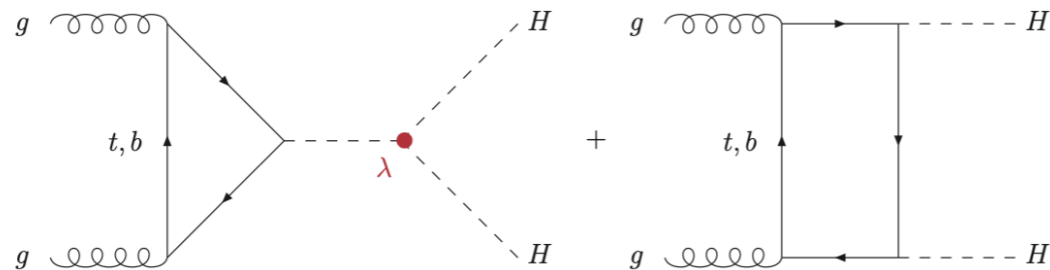
[HH, White paper]



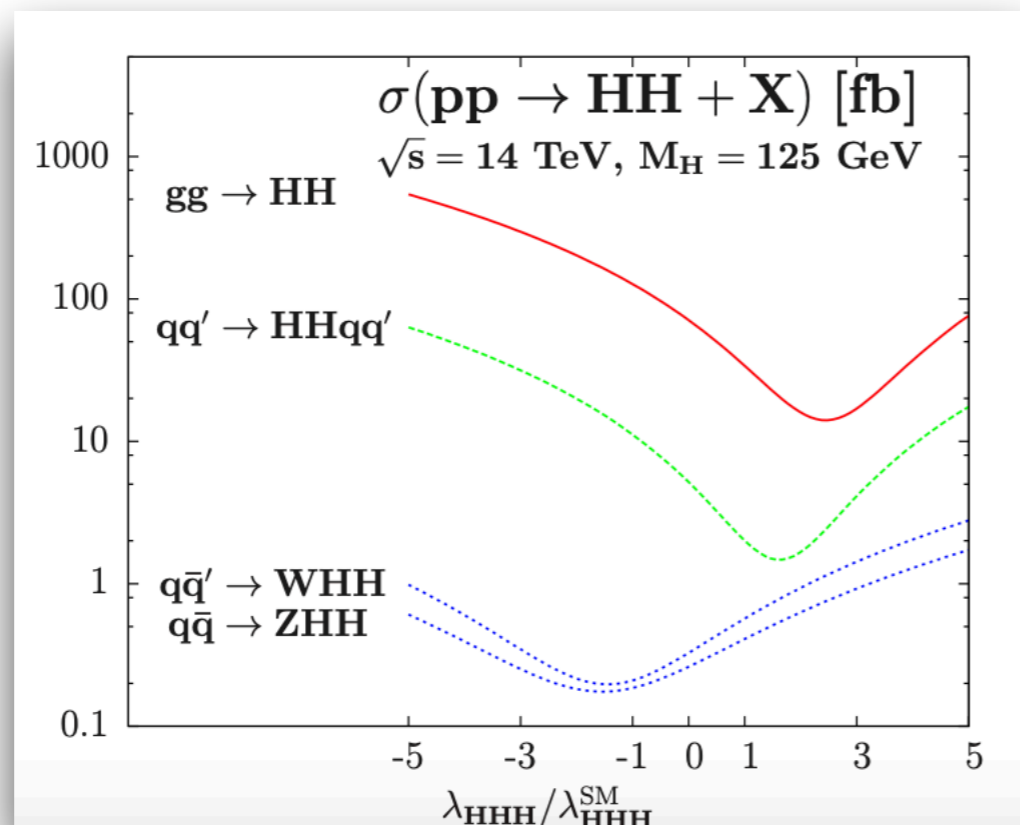
Small c<sub>xx</sub>, large bkg:  
 experimental challenge  $\leadsto$   
 precise theory  
 predictions required

# Higgs Pair Production through Gluon Fusion

- Loop mediated at leading order - SM: third generation dominant



- Threshold region sensitive to  $\lambda$ ; large  $M_{HH}$ : sensitive to new physics effects in loops



[Baglio, Djouadi, Gröber, MM, Quévillon, Spira]

$$gg \rightarrow HH : \frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$$

decreasing with  $M_{HH}$

# Higher-Order QCD Corrections to Higgs Pair Production

- ♦ 2-loop QCD corrections:  $\approx 70%$  [HTL,  $\mu=M_{HH}/2$ ] [Dawson,Dittmaier,Spira]
- ♦ 2-loop QCD corrections:  $\sigma = \sigma_0 + \sigma_1/m_t^2 + \dots + \sigma_4/m_t^8$   
[refinement: full LO at differential level] [Grigo,Hoff,Melnikov,Steinhauser]
- ♦ Mass effects @ NLO in real corrections:  $\sim -10%$   
[Frederix,Frixione,Hirschi,Maltoni,Mattelaer,Torrielli,Vryonidou,Zaro]
- ♦ NNLO QCD corrections:  $\sim 20%$  [HTL] [de Florian,Mazzitelli; Grigo,Melnikov,Steinhauser]
- ♦ N<sup>3</sup>LO QCD corrections:  $\sim 5%$  [HTL] [Chen,Li,Shao,Wang]
- ♦ NNLO Monte Carlo: inclusion of full top-mass effects @ NLO [partly at NNLO]  
[Grazzini,Heinrich,Jones,Kallweit,Kerner,Lindert,Mazzitelli]
- ♦ NLO: matching to parton showers [Heinrich,Jones,Kerner,Luisoni,Vryonidou]
- ♦ New expansion/extrapolation methods:
  - (i)  $1/m_t^2$  expansion + conformal mapping + Padé approximants [Gröber,Maier,Rauh]
  - (ii)  $p_T^2$  expansion [Bonciani,Degassi,Giardino,Gröber]
- ♦ NLO: small mass expansion [ $Q^2 \gg m_t^2$ ] [Davies,Mishima,Steinhauser,Wellmann]  
[Davies,Heinrich,Jones,Kerner,  
Mishima,Steinhauser,Wellmann]
- ♦ Combination of full NLO and small mass expansion
- ♦ Light fermionic 3-loop corrections [Davies,Schönwald,Steinhauser]

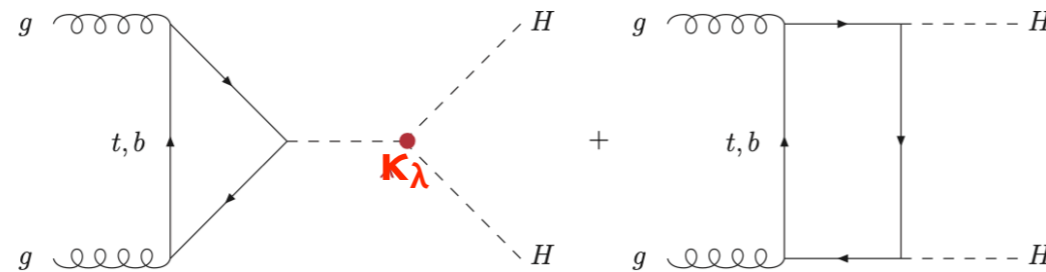
# Higher-Order QCD, EW Corrections to Higgs Pair Production

- Complete list, see e.g. twiki of LHC Higgs Working Subgroup HH and recent reviews

-> recommendations for cross sections to be used given for

- different c.m. energies
- different coupling modifiers  $\kappa_\lambda$

-> uncertainties on di-Higgs cross sections



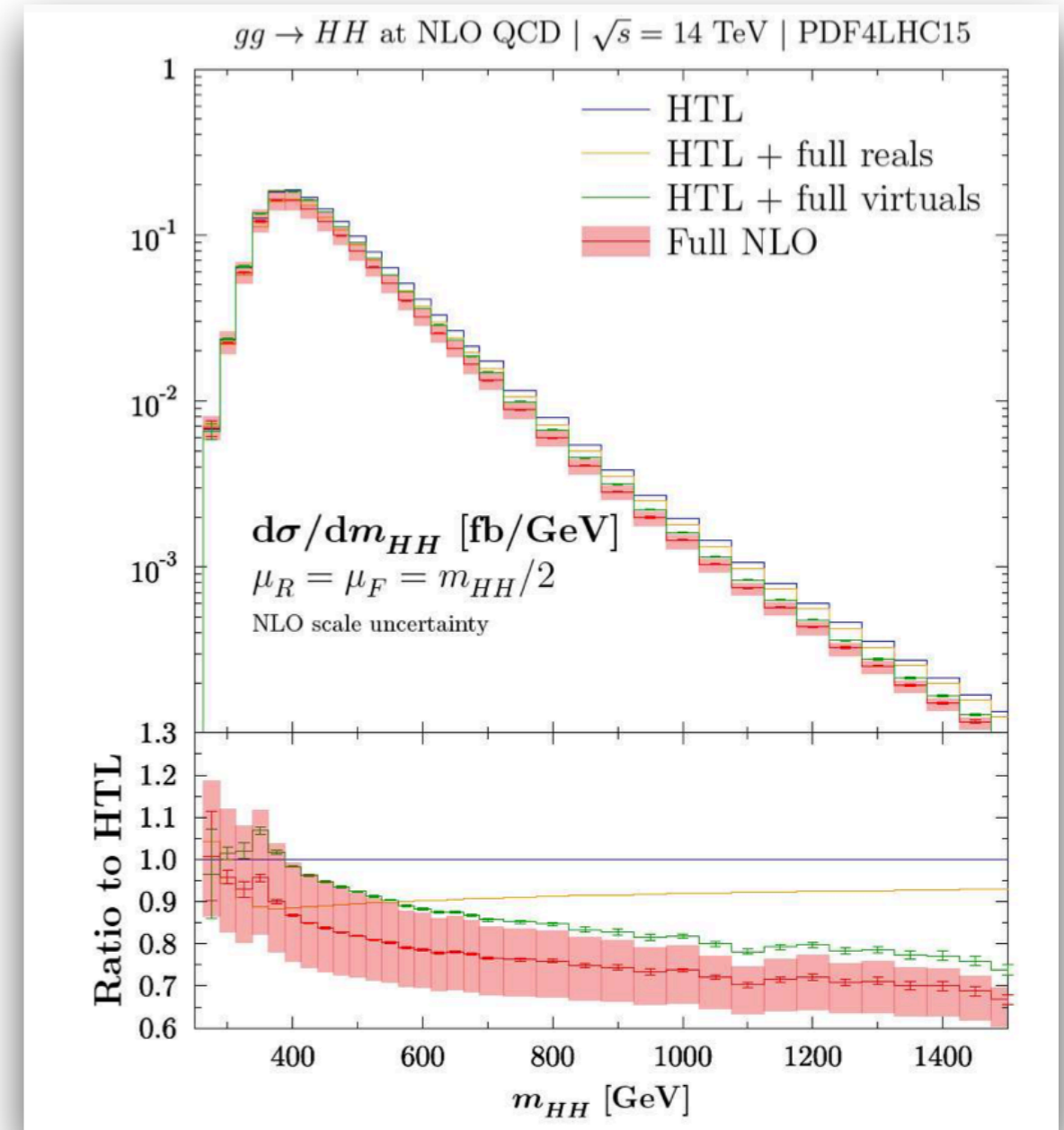
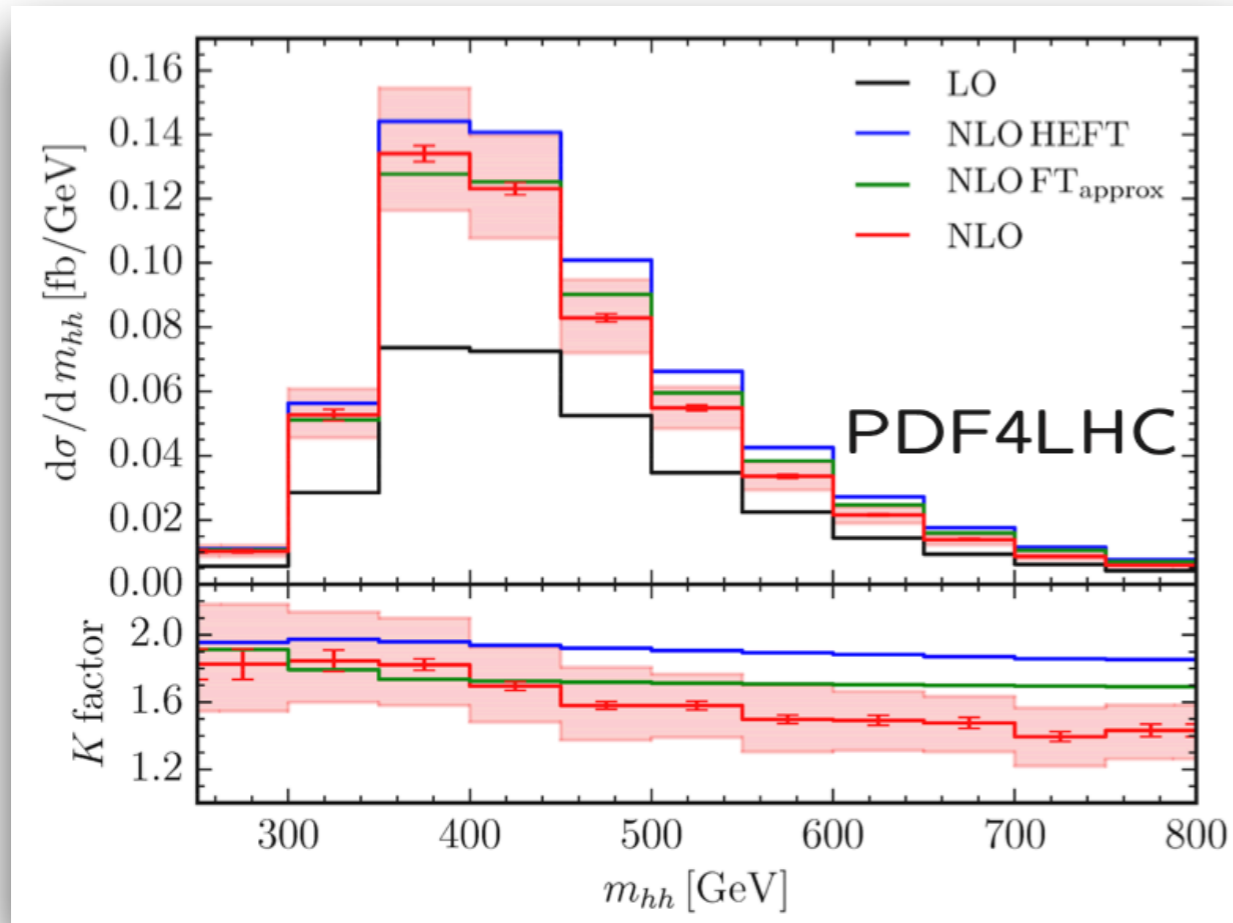
- First results on EW corrections:

- ♦ top-Yukawa induced corrections: 0.2%, not absorbable in effective trilinear coupling [MM,Schlenk,Spira,'22]
- ♦ top Yukawa corrections in the high-energy limit [Davies,Mishima,Schönwald,Steinhauser,Zhang,'22]  
large top mass expansion up to  $1/m_t^8$  or more [Davies,Schönwald,Steinhauser,Zhang,'23]

# Full NLO QCD Calculation

[Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Schubert, Zirke]

[Baglio, Campanario, Glaus, MM, Ronca, Spira, Streicher]



$$\begin{aligned} \sigma_{NLO} &= 32.91(10)_{-12.8\%}^{+13.8\%} \text{ fb} \\ \sigma_{NLO}^{HTL} &= 38.75_{-15\%}^{+18\%} \text{ fb} \\ m_t &= 173 \text{ GeV} \end{aligned}$$

$$\begin{aligned} \sigma_{NLO} &= 32.81(7)_{-12.5\%}^{+13.5\%} \text{ fb} \\ \sigma_{NLO}^{HTL} &= 38.66_{-15\%}^{+18\%} \text{ fb} \\ m_t &= 172.5 \text{ GeV} \end{aligned}$$

⇒ -15% mass effects on top of LO

20-30% for distributions

## Uncertainties at NLO QCD

### ♦ Renormalization and factorization scale uncertainties at NLO:

$$\begin{aligned}\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} &= 27.73(7)_{-12.8\%}^{+13.8\%} \text{ fb} \\ \sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} &= 32.81(7)_{-12.5\%}^{+13.5\%} \text{ fb} \\ \sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} &= 127.0(2)_{-10.7\%}^{+11.7\%} \text{ fb} \\ \sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} &= 1140(2)_{-10.0\%}^{+10.7\%} \text{ fb}\end{aligned}$$

### ♦ $m_{\tau}$ scale/scheme uncertainties at NLO:

$$\begin{aligned}\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} &= 27.73(7)_{-18\%}^{+4\%} \text{ fb} \\ \sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} &= 32.81(7)_{-18\%}^{+4\%} \text{ fb} \\ \sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} &= 127.8(2)_{-18\%}^{+4\%} \text{ fb} \\ \sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} &= 1140(2)_{-18\%}^{+3\%} \text{ fb}\end{aligned}$$

### ♦ Linear sum of uncertainties ~>

## Final Uncertainties at $FT_{\text{approx}}$

- Final combined renormalization/factorization scale and  $m_t$  scale/scheme uncertainties at  $NNLO_{FT_{\text{approx}}}$ \*

$$\begin{aligned}\sqrt{s} = 13 \text{ TeV} : \quad \sigma_{tot} &= 31.05^{+6\%}_{-23\%} \text{ fb} \\ \sqrt{s} = 14 \text{ TeV} : \quad \sigma_{tot} &= 36.69^{+6\%}_{-23\%} \text{ fb} \\ \sqrt{s} = 27 \text{ TeV} : \quad \sigma_{tot} &= 139.9^{+5\%}_{-22\%} \text{ fb} \\ \sqrt{s} = 100 \text{ TeV} : \quad \sigma_{tot} &= 1224^{+4\%}_{-21\%} \text{ fb}\end{aligned}$$

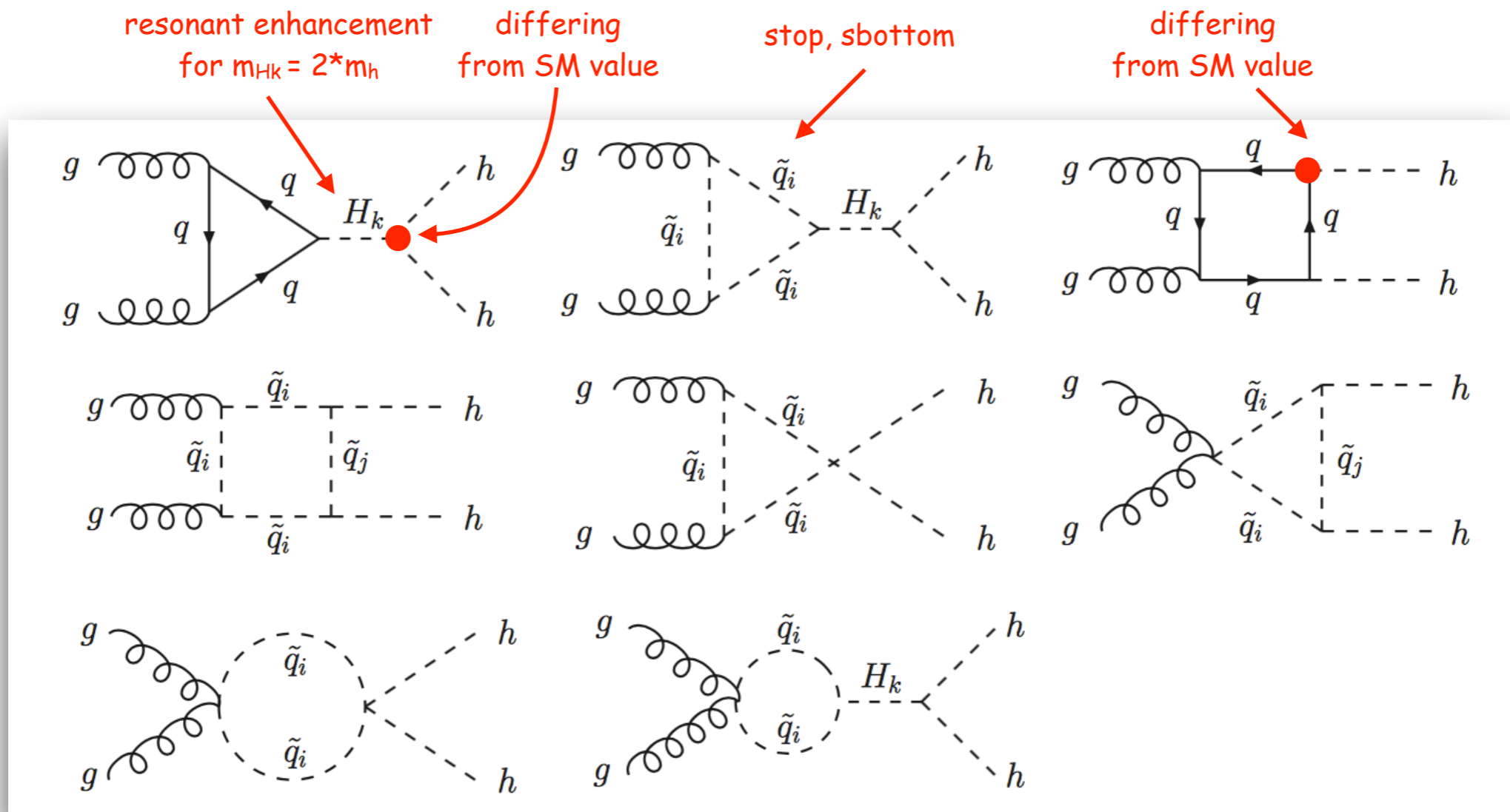
\* $FT_{\text{approx}}$ : full NNLO QCD in the heavy-top-limit with full LO and NLO mass effects and full mass dependence in the one-loop double real corrections at NNLO QCD

# New Physics Effects in Higgs Pair Production

- ♦ Cross section: - different trilinear couplings - different Yukawa couplings
- novel particles in the loops - resonant enhancement - novel couplings

## ♦ Example NMSSM:

[taken from Dao,MM,Streicher,Walz,'13]





2HDM

C2HDM

N2HDM

NMSSM

2 Higgs doublets

CP-violating

Singlet extension

Supersymmetry

$h, H, A, H^+, H^-$

$H_1, H_2, H_3, H^+, H^-$

$H_1, H_2, H_3, H^+, H^-$

$H_1, H_2, H_3, A, H^+, H^-$

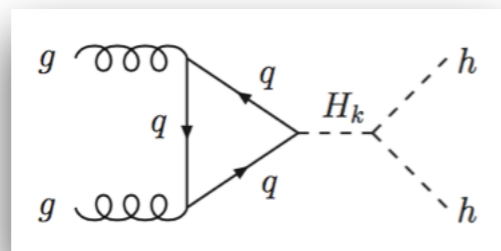
SFOEWPT, DM,  
plus charged Higgs

plus CP violation  
baryogenesis

rich pheno, DM

a lot (DM, CPviol,  
Hierarchy, ...)

Resonant Enhancement



Higgs-to-Higgs Cascade decays

♦ Following results based on:


Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MMM, Santos, „Benchmarking Di-Higgs Production in Extended Higgs Sectors“, JHEP 09 (2022) 011

# Parameter Point Samples

## ♦ Scans in parameter spaces of the models w/ ScannerS:

take into account all relevant theoretical and experimental constraints  
+ limits from di-Higgs searches

4b: [ATLAS-CONF-Note-2021-030, ATLAS,1804.06174],  
WW $\gamma\gamma$ : [ATLAS,1807.08567]; bb $\gamma\gamma$ : [ATLAS,1807.04873];  
bbWW: [ATLAS,1811.04671, bbZZ: [CMS,2006.06391]  
bb $\tau\tau$ : [ATLAS,1808.00336; ATLAS-CONF-Note-2021-035;  
ATLAS,2007.14811], 4W: [ATLAS,1811.11028]



Resonant and non-resonant  
di-Higgs limits start  
cutting in parameter space  
of the models

## ♦ Computation of Higgs pair production c $\times$ n:

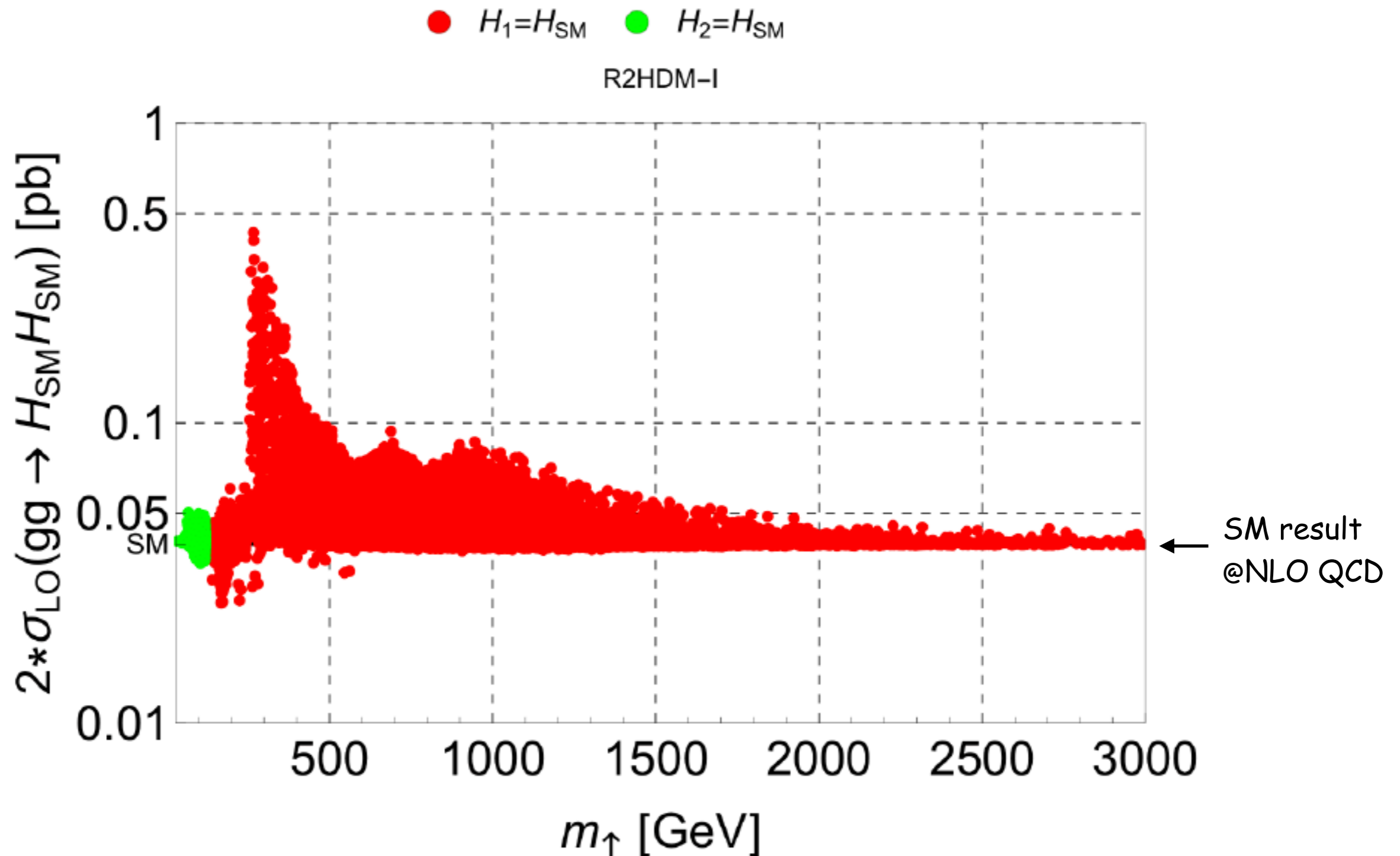
HPAIR [Spira] for C $\mathcal{2}$ HDM [Gröber,MM,Spira,'17], NMSSM [Dao,MM,Streicher,Walz,'13],  
 $\mathcal{2}$ HDM [MM], N $\mathcal{2}$ HDM [MM]: Born-improved HTL c $\times$ n; K-factors 1.4-2.1

## ♦ Scatter plots:

LO c $\times$ n times factor 2 (to approx. account for NLO QCD), benchmark points include  
NLO QCD calculated w/ HPAIR

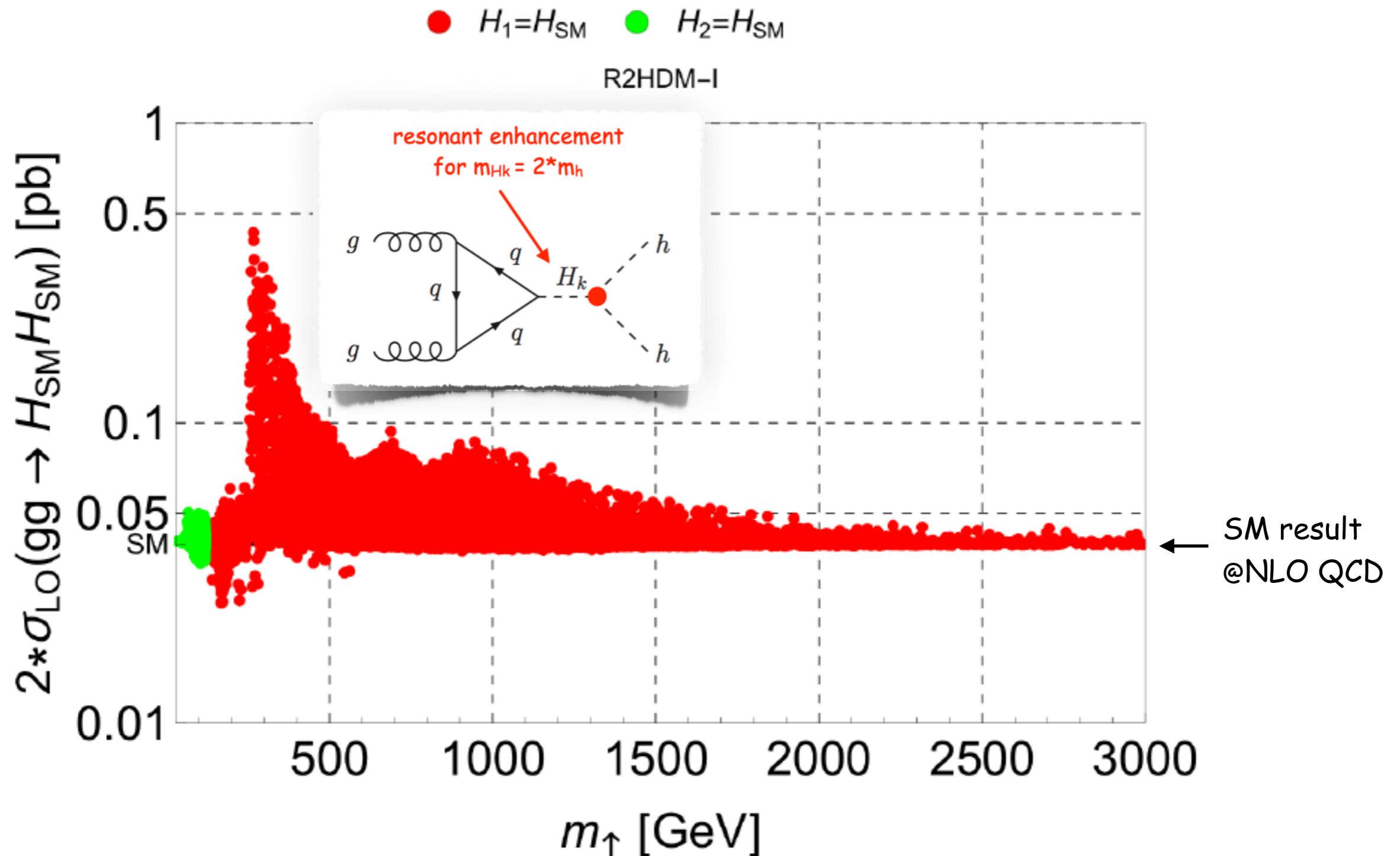
# 2-Higgs Doublet Model: SM-like Higgs Pair Production

[Abouabid,Arhrib,Azevedo,El Falaki,Ferreira,MM,Santos,'21]



# 2-Higgs Doublet Model: SM-like Higgs Pair Production

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]



# Resonant/Non-Resonant Maximum SM-Like Higgs Pair Production

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]

Resonant production  
at NLO QCD in fb

	$H_1$	$H_2$
R2HDM-I	444	n.a.
R2HDM-II	81	n.a.
C2HDM-I	387	47
C2HDM-II	130	–
N2HDM-I	376	344
N2HDM-II	188	63
NMSSM	183	65

Non-Resonant production  
at NLO QCD in fb

	$H_1$	$H_2$
R2HDM-I	92	–
R2HDM-II	59	–
C2HDM-I	98	42
C2HDM-II	75	–
N2HDM-I	151	96
N2HDM-II	112	48
NMSSM	73	65

SM value at NLO QCD 38 fb

# Di-Higgs Beats Single-Higgs

♦ **Singlet extended N2HDM, NMSSM:** non-SM-like Higgs is singlet-like and/or more down- than up-type like => suppressed direct production rate

♦ **Sample parameter point N2HDM T1:**

$m_{H_1}$ [GeV]	$m_{H_2}$ [GeV]	$m_{H_3}$ [GeV]	$m_A$ [GeV]	$m_{H^\pm}$ [GeV]	$\tan \beta$
125.09	281.54	441.25	386.98	421.81	1.990
$\alpha_1$	$\alpha_2$	$\alpha_3$	$v_s$ [GeV]	$\text{Re}(m_{12}^2)$ [GeV <sup>2</sup> ]	
1.153	0.159	0.989	9639	29769	

Final state:

$$6b: \sigma_{H_1 H_2}^{\text{NLO}} \times \text{BR}(H_2 \rightarrow H_1 H_1) \times \text{BR}(H_1 \rightarrow b\bar{b})^3 = 509 \cdot 0.37 \cdot 0.60^3 \text{ fb} = 40 \text{ fb}$$

$$4b: \sigma^{\text{NNLO}}(H_2) \times \text{BR}(H_2 \rightarrow H_1 H_1) \times \text{BR}(H_1 \rightarrow b\bar{b})^2 = 161 \cdot 0.37 \cdot 0.60^2 \text{ fb} = 21 \text{ fb}$$

**$H_2$  has tiny couplings to b-quarks => better chances to be discovered in di-Higgs than single Higgs channels**

*HH and Strong First Order EWPT  
SFOEWPT and Gravitational Waves*



# Electroweak Baryogenesis

- **Electroweak Baryogenesis (EWBG):** generation of the observed baryon-antibaryon asymmetry in the electroweak phase transition (EWPT) [Riemer-Sorensen, Jenssen '17]

$$5.8 \cdot 10^{-10} < \frac{n_B - n_{\bar{B}}}{n_\gamma} < 6.6 \cdot 10^{-10}$$

- **Sakharov Conditions:** [Sakharov '67]

- \* (i)  $B$  number violation (sphaleron processes)
- \* (ii)  $C$  and  $CP$  violation
- \* (iii) Departure from thermal equilibrium

- **Additional constraint:** EW phase transition must be strong first order PT [Quiros '94; Moore '99]

$$\xi_c \equiv \frac{\langle \Phi_c \rangle}{T_c} \geq 1$$

$\langle \Phi_c \rangle$  and  $T_c$  field configuration and temperature at phase transition



- ♦ 2HDM type II struggles to reach SFOEWPT (compared to type I)

[see e.g. Basler,Krause,MM,Wittbrodt,Wlotzka,'16]

- ♦ For 2HDM type II points with  $\xi_c < 1$ :

What extra dynamics is required to achieve SFOEWPT?

- ♦ Our model: CP-conserving 2HDM with softly broken discrete  $Z_2$  symmetry

$$V_{\text{tree}}(\Phi_1, \Phi_2) = m_{11}^2(\Phi_1^\dagger \Phi_1) + m_{22}^2(\Phi_2^\dagger \Phi_2) - m_{12}^2(\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \lambda_1(\Phi_1^\dagger \Phi_1)^2 + \lambda_2(\Phi_2^\dagger \Phi_2)^2 \\ + \lambda_3(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4(\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) + \frac{1}{2}\lambda_5[(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2]$$

- ♦ Extended by (purely scalar) dim-6 EFT contributions to the Higgs potential [Anisha eal,'19]

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{2HDM}} + \sum_i \frac{C_6^i}{\Lambda^2} O_6^i \quad \Rightarrow \quad V_{\text{dim-6}} = - \sum_i \frac{C_6^i}{\Lambda^2} O_6^i$$

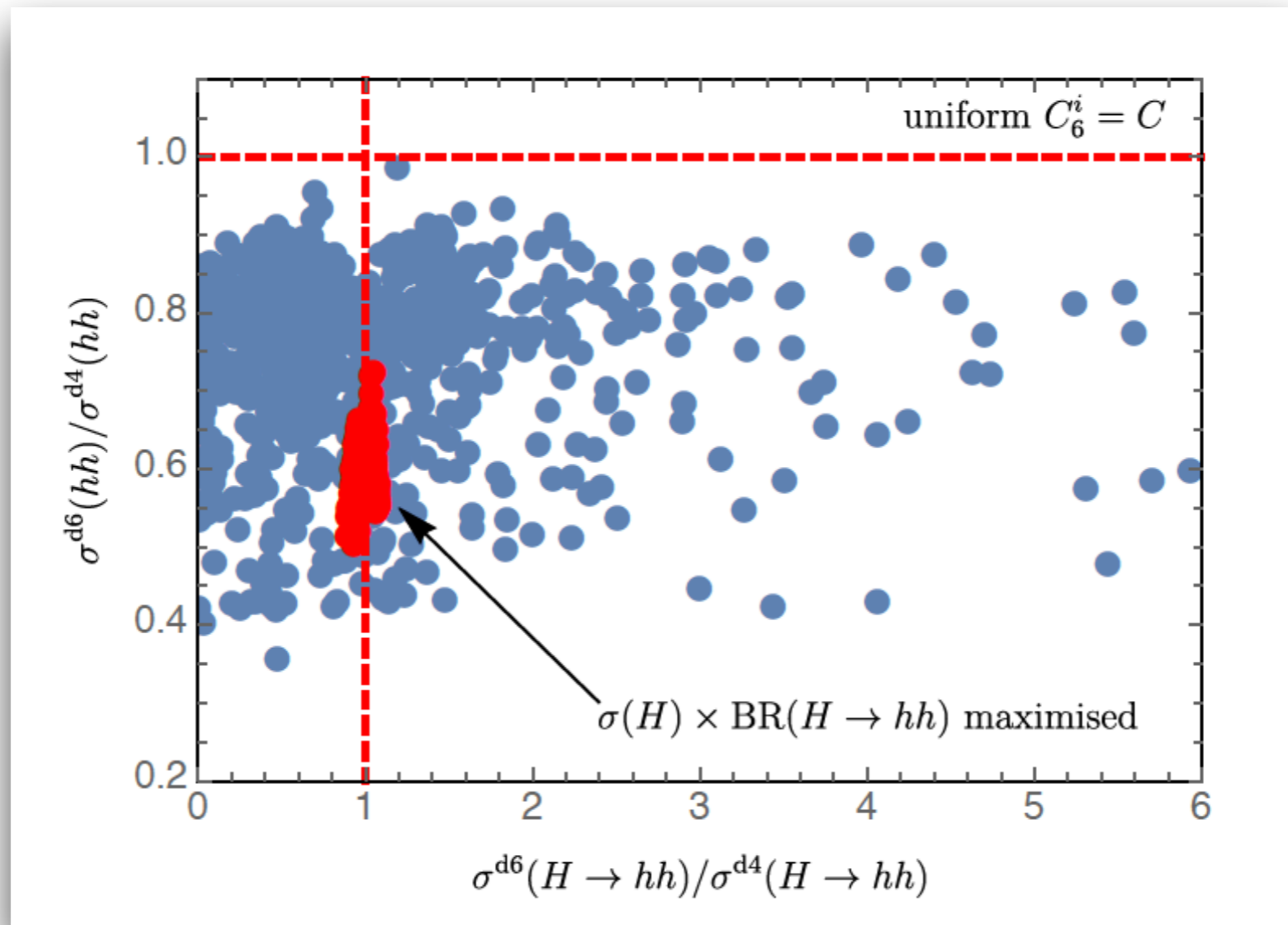
- ♦ Higgs pair production: a tool for fingerprinting an SFOEWPT?

$O_6^{111111}$	$(\Phi_1^\dagger \Phi_1)^3$	$O_6^{222222}$	$(\Phi_2^\dagger \Phi_2)^3$
$O_6^{111122}$	$(\Phi_1^\dagger \Phi_1)^2 (\Phi_2^\dagger \Phi_2)$	$O_6^{112222}$	$(\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2)^2$
$O_6^{122111}$	$(\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) (\Phi_1^\dagger \Phi_1)$	$O_6^{122122}$	$(\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2)$
$O_6^{121211}$	$(\Phi_1^\dagger \Phi_2)^2 (\Phi_1^\dagger \Phi_1) + \text{h.c.}$	$O_6^{121222}$	$(\Phi_1^\dagger \Phi_2)^2 (\Phi_2^\dagger \Phi_2) + \text{h.c.}$

- absorb dim-6 contributions (to scalar masses) in shifts  $\lambda_i \rightarrow \lambda_i + \delta\lambda_i$ ,  $m_{12}^2 \rightarrow m_{12}^2 + \delta m_{12}^2$
- ⇒ scalar mass spectrum same as for dim-4 @ LO
- ⇒ shift EFT effects into **Higgs self-couplings & multi-Higgs final states**
- Computation of  $\xi_c$  with BSMPT [Basler,Biermann,Mühlleitner,Müller]:  
 Loop-corrected effective potential at finite temperature including daisy resummation of bosonic masses; „OS“ renormalization

# Correlation of $\xi_c^{d4}$ , continuum and resonant hh production

[Anisha,Biermann,Englert,MM,'22]



- Points with  $\xi_c^{d6} \cong 1$  for  $\xi_c^{d4} \cong 0.3$  (red Higgs-philic points:  $\xi_c^{d4} > 0.15$ )
- Higgs-philic points: resonance contribution modified by  $\sim 5\text{-}10\%$ , continuum production modified by  $\sim 50\%$

## STATUS QUO: CODES ON THE MARKET

taken from Lisa Biermann

### Available codes to calculate the bounce solution:

- CosmoTransitions [Wainwright, 2011]: via path deformation
- AnyBubble [Masoumi, 2017]: via a multiple shooting algorithm
- BubbleProfiler [Athron et al., 2019]: via a semi-analytic algorithm [Akula et al., 2016]
- SimpleBounce [Sato, 2019]: via gradient flow method
- FindBounce [Guada et al., 2018/20]: via polygonal multifield method
- Opt iBounce [Bardsley, 2021]: via solving the ‘reduced’ minimization problem [Coleman, 1977]

⇒ [coming 2023]: **BSMPTv3** [BSMPTv1:Basler,MM,Müller]  
[BSMPTv2:Basler,Biermann,MM,Müller]  
[BMPTv3:Biermann,MM,Santos,Viana]

## WHY BSMPTv3?

taken from Lisa Biermann

- optimized *minimum tracing* and tracking of temperature-dependent coexisting minimum phases over any temperature interval
- numerical derivation of the *bounce solution* for any number of field dimensions
- more precise calculation of *nucleation temperature* (than implemented in CosmoTransitions)
- calculation of *percolation temperature* (not implemented in CosmoTransitions)
- calculation of *GW parameters*  $\alpha, \beta/H$
- derivation of  $f^{\text{peak}}, h^2 \Omega_{\text{GW}}^{\text{peak}}$  of (acoustic) gravitational wave spectrum
- calculation of *signal-to-noise ratio* at LISA
- ... for all models implemented (singlet-, doublet-, singlet+doublet-extensions)
- ... embedded into the framework of the existing BSMPT-code
  - easy-to-use interface to implement your own model of choice
  - designed to use input from ScannerS

## Additional Remark: Gravitational Waves from FOEWPT

- ♦ **Model CP in the Dark:** N2HDM scalar sector with one discrete  $Z_2$  symmetry

$$\Phi_1 \rightarrow +\Phi_1, \quad \Phi_2 \rightarrow -\Phi_2, \quad \Phi_S \rightarrow -\Phi_S$$

$$\begin{aligned} V^{(0)} = & m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 + \frac{m_S^2}{2} \Phi_S^2 + \left( A \Phi_1^\dagger \Phi_2 \Phi_S + h.c. \right) + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 \\ & + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{\lambda_5}{2} \left[ \left( \Phi_1^\dagger \Phi_2 \right)^2 + h.c. \right] + \frac{\lambda_6}{4} \Phi_S^4 + \frac{\lambda_7}{2} |\Phi_1|^2 \Phi_S^2 + \frac{\lambda_8}{2} |\Phi_2|^2 \Phi_S^2 \end{aligned}$$

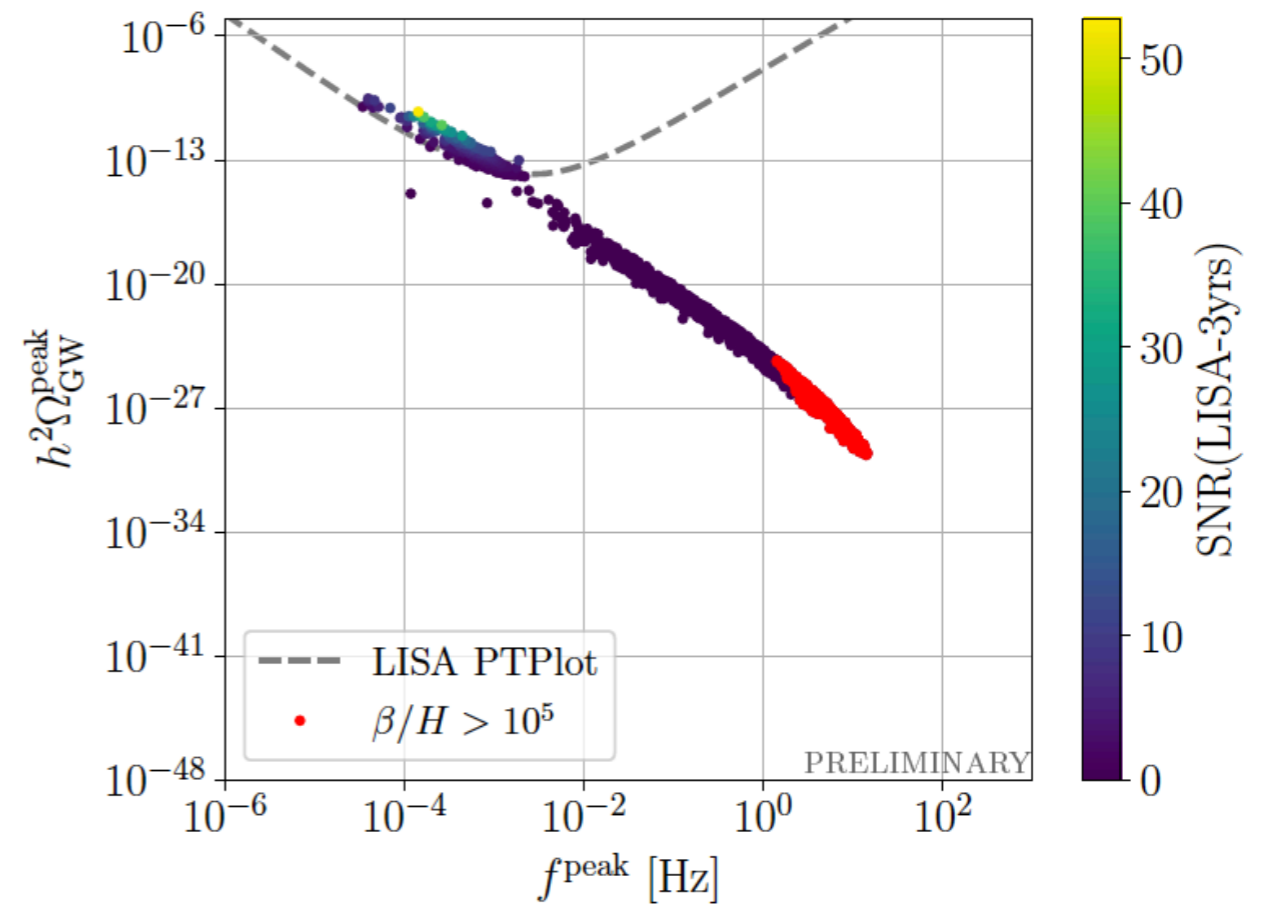
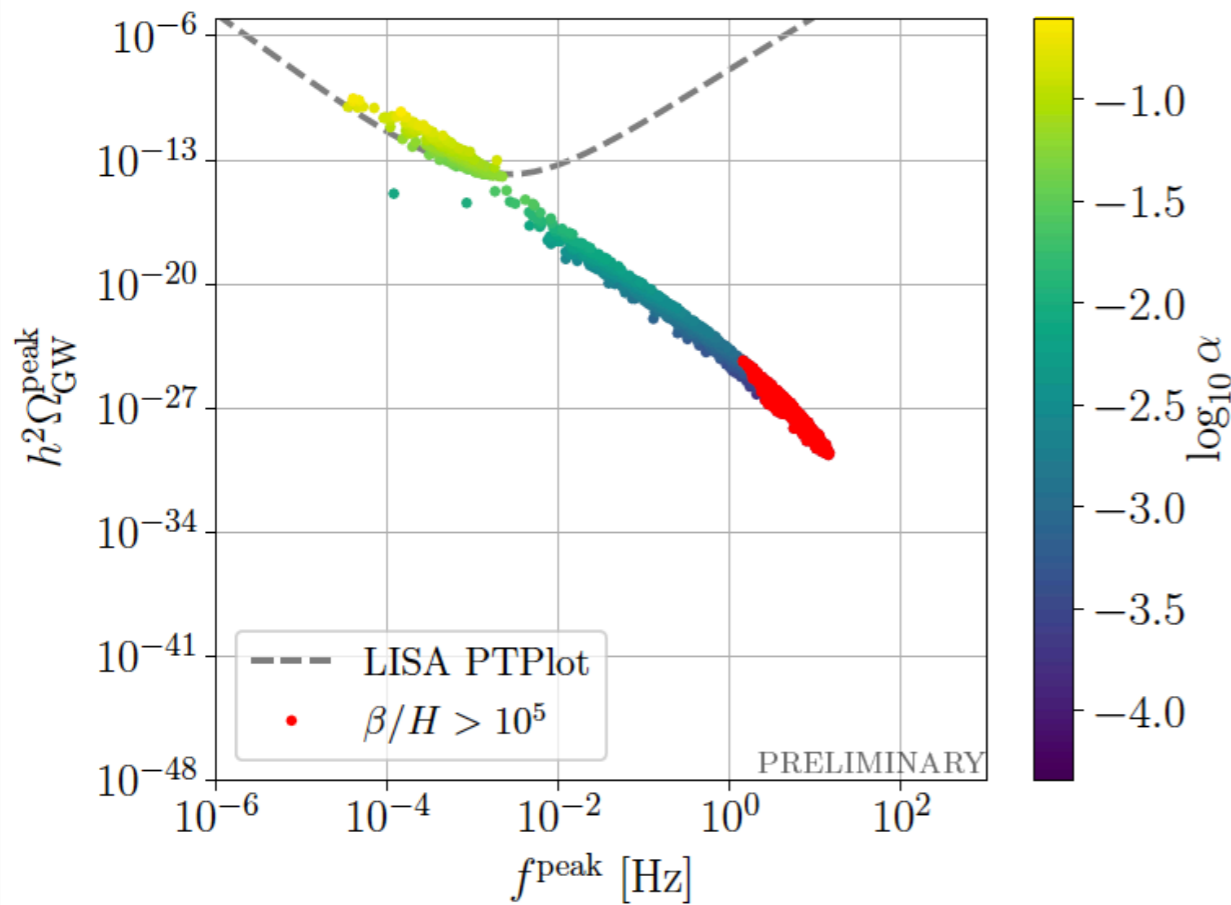
- ♦ **Spectrum:** Visible SM Higgs, Dark Sector with  $h_1, h_2, h_3, H^\pm$
- ♦  $\text{Im}(A) \neq 0 \Rightarrow$  explicit CP violation in Dark Sector

# Gravitational Waves from FOEWPT

[Biermann,MM,Santos,Viana,to appear]

PRELIMINARY

$$\text{signal-to-noise ratio SNR} = \sqrt{\mathcal{T} \int_{f_{\min}}^{f_{\max}} df \left[ \frac{h^2 \Omega_{\text{GW}}(f)}{h^2 \Omega_{\text{Sens}}(f)} \right]^2}$$



SNR(LISA-3yrs) >10 compatible w/ collider, DM, theor. constraints and have SFOEWPT

*Higgs Portal  
to Dark Matter*





# The Higgs Boson as Portal to Dark Matter

- ♦ Higgs sector extensions with discrete symmetries:

## Dark Matter candidate

- ♦ Example CxSM: SM extended by complex singlet field

$$V = \frac{m^2}{2} \Phi^\dagger \Phi + \frac{\lambda}{4} (\Phi^\dagger \Phi)^2 + \frac{\delta_2}{2} \Phi^\dagger \Phi |S|^2 + \frac{b_2}{2} |S|^2 + \frac{d_2}{4} |S|^4 + \left( \frac{b_1}{4} S^2 + c.c. \right)$$

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + H + iG^0) \end{pmatrix}, \quad S = \frac{1}{\sqrt{2}} (v_S + S + i(v_A + A)).$$

impose two separate discrete symmetries:  $S \rightarrow -S$  and  $A \rightarrow -A$

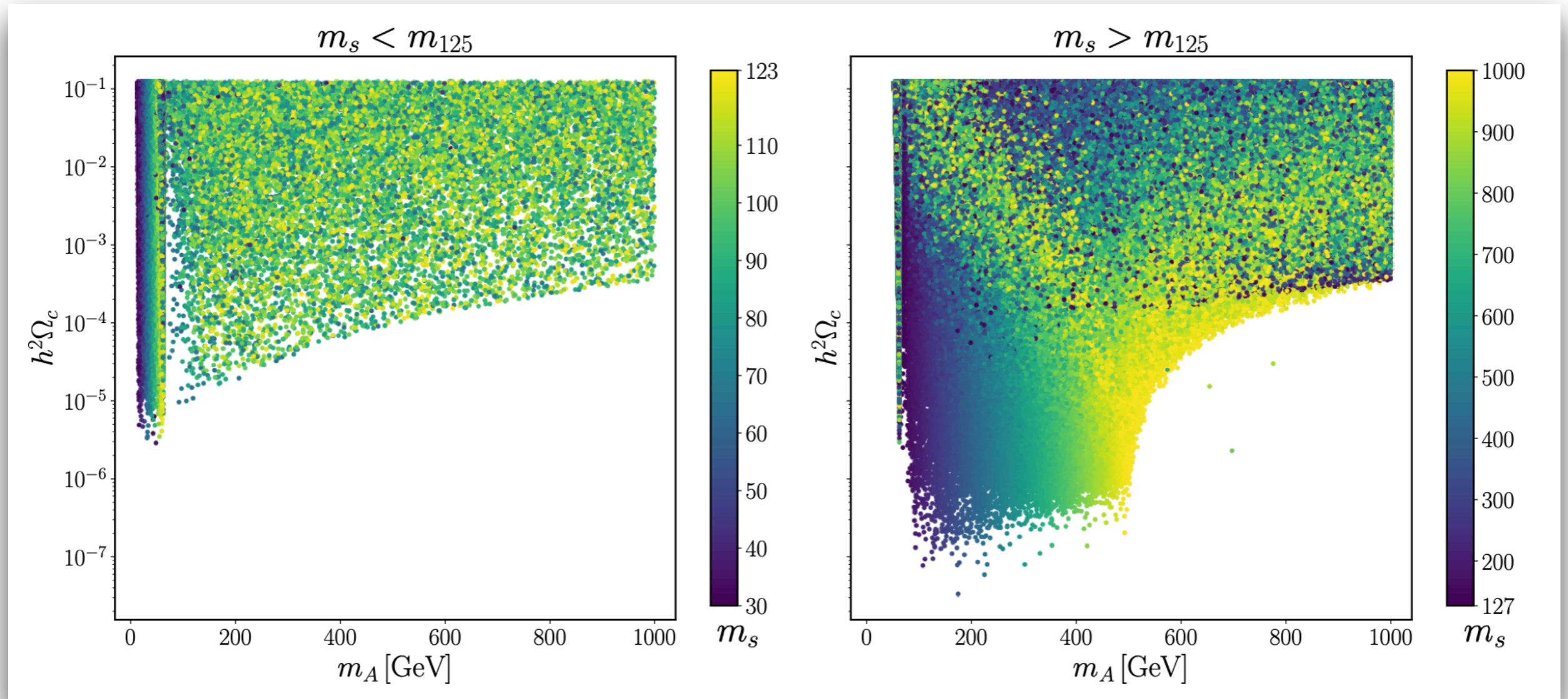
$v_A=0 \Rightarrow A \rightarrow -A$  symmetry unbroken, **A is stable  $\Rightarrow$  the Dark Matter candidate**

**Spectrum:**  $h_1, h_2, A$ ; one of the  $h_{1,2}$  is the  $h_{125}$

- ♦ Scan in parameter space of the model: keep only points compatible with relevant theoretical and experimental constraints (H&HH data, EWPT, DM observables)

# Relic Density For Allowed Parameter Points

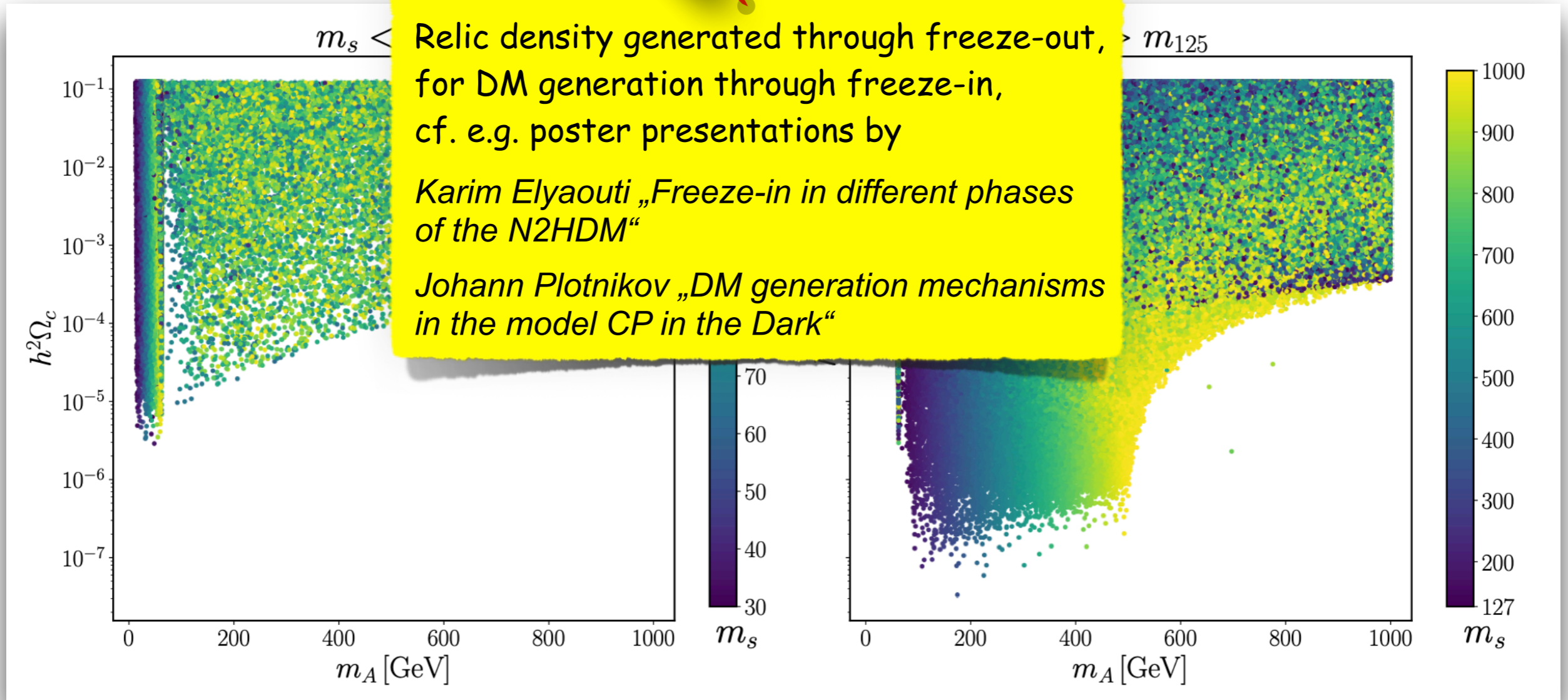
[Egle,MM,Santos,Viana,'23]



In whole scanned  $m_A$  region: allowed parameter scenarios exist saturating the relic density

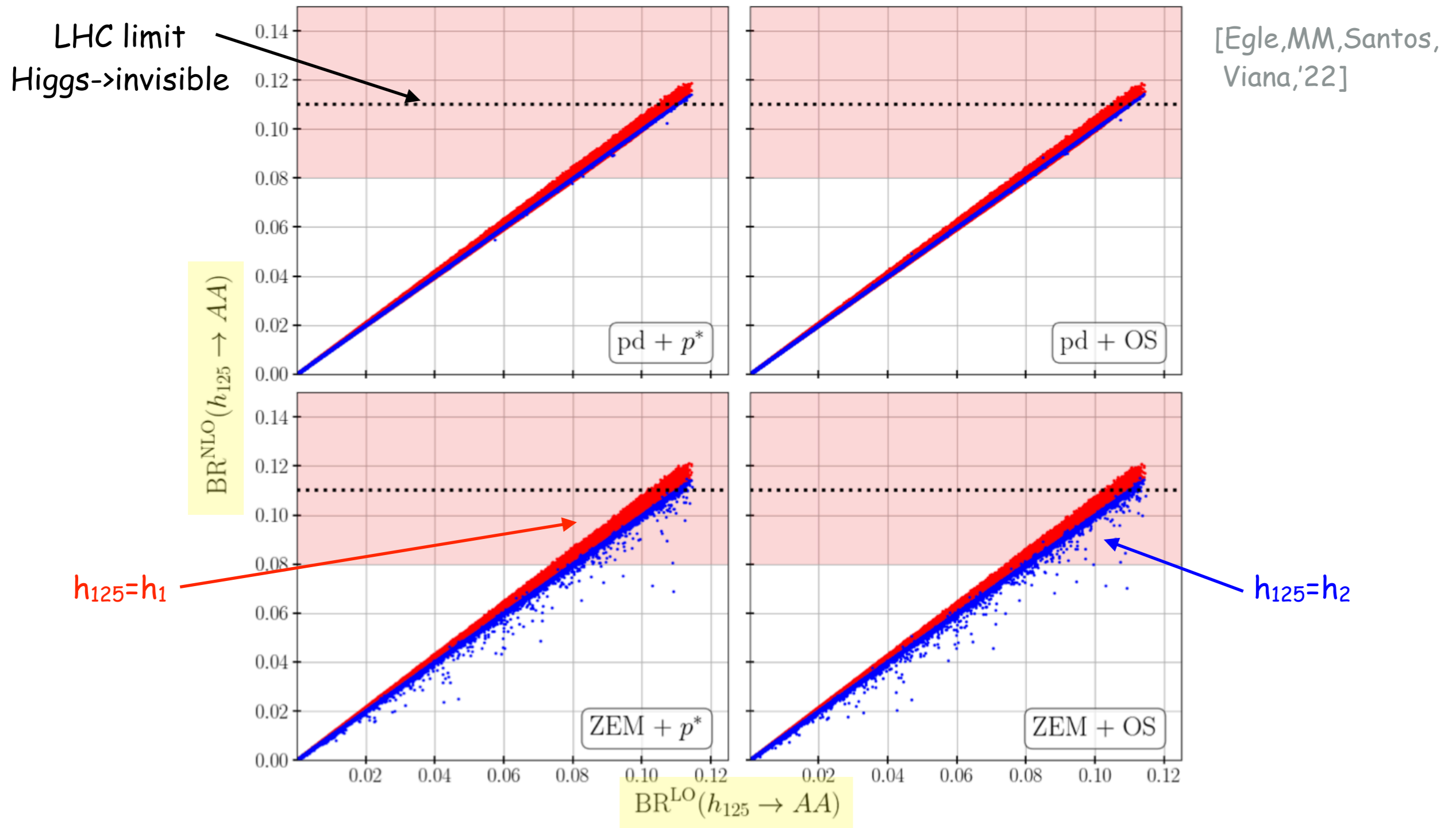
# Relic Density For Allowed Parameter Points

[Egle,MM,Santos,Viana,'23]



In whole scanned  $m_A$  region: allowed parameter scenarios exist saturating the relic density

# LHC Test: Higgs Decay into two DM Particles, $h_{125} \rightarrow AA$



Parameter point allowed at leading order may be excluded at next-to-leading order and vice versa

# Conclusions



- ◆ Flaws of **SM** call for new physics; no direct signs of new physics => **Higgs boson**
- ◆ Combine results of all available observables, **precision important** => **constrain BSM parameter space**
- ◆ Both **QCD&EW** corrections are important; corrections can be **more important in BSM models**
- ◆ **Higgs pair production** => **insights in mechanism of EWSB**  
Precision slowly catching up w/ H production  
**NLO QCD mass effects important**: -15% (inclusive), -30-40% (distribution at large  $M_{HH}$ )  
**uncertainties** from top mass scale and scheme choice are **significant**
- ◆ **HH in extended Higgs sectors**  
large cross sections due to **resonant enhancement** possible  
non-resonant&resonant searches start **testing BSM models in HH**  
interesting effects in singlet models: **di-Higgs can beat single Higgs**
- ◆ **Strong First Order EWPT (required for baryogenesis)**  
extension of 2HDM by **scalar dim-6 operators** can lead to SFOEWPT, relation to LHC pheno  
**LISA sensitive to grav. waves from SMFOEWPT** in CP in the Dark incl. exp (H) & theor constraints
- ◆ **Higgs Portal to DM**  
CxSM: compatible w/ DM constraints, **testable at LHC**, EW corrections important

Higgs boson can give many insights in BSM physics

Interesting times ahead!

*Thank you for  
your attention!*



# Uncertainties for Different Higgs Self-Coupling Values

♦ Final combined uncertainties at NNLO<sub>FTapprox</sub>:

$$\kappa_\lambda = -10 : \quad \sigma_{tot} = 1680^{+13\%}_{-14\%} \text{ fb}$$

$$\kappa_\lambda = -5 : \quad \sigma_{tot} = 598.9^{+13\%}_{-15\%} \text{ fb}$$

$$\kappa_\lambda = -1 : \quad \sigma_{tot} = 131.9^{+11\%}_{-16\%} \text{ fb}$$

$$\kappa_\lambda = 0 : \quad \sigma_{tot} = 70.38^{+8\%}_{-18\%} \text{ fb}$$

$$\kappa_\lambda = 1 : \quad \sigma_{tot} = 31.05^{+6\%}_{-23\%} \text{ fb}$$

$$\kappa_\lambda = 2 : \quad \sigma_{tot} = 13.81^{+3\%}_{-28\%} \text{ fb}$$

$$\kappa_\lambda = 2.4 : \quad \sigma_{tot} = 13.10^{+6\%}_{-27\%} \text{ fb}$$

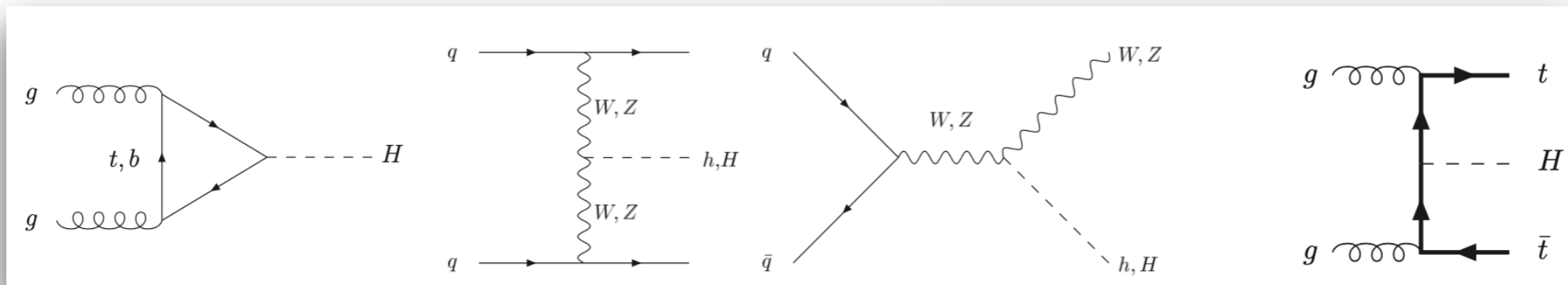
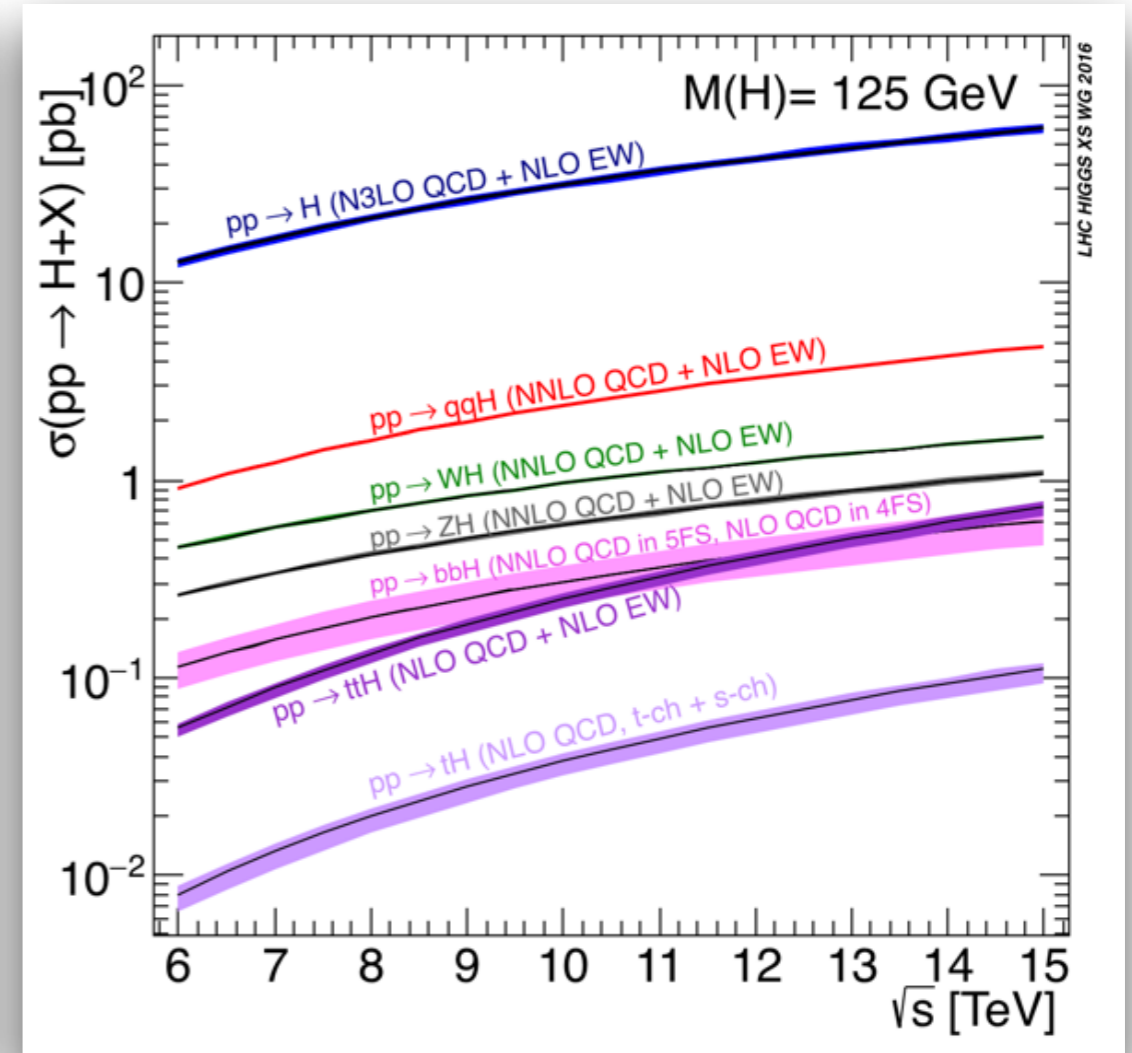
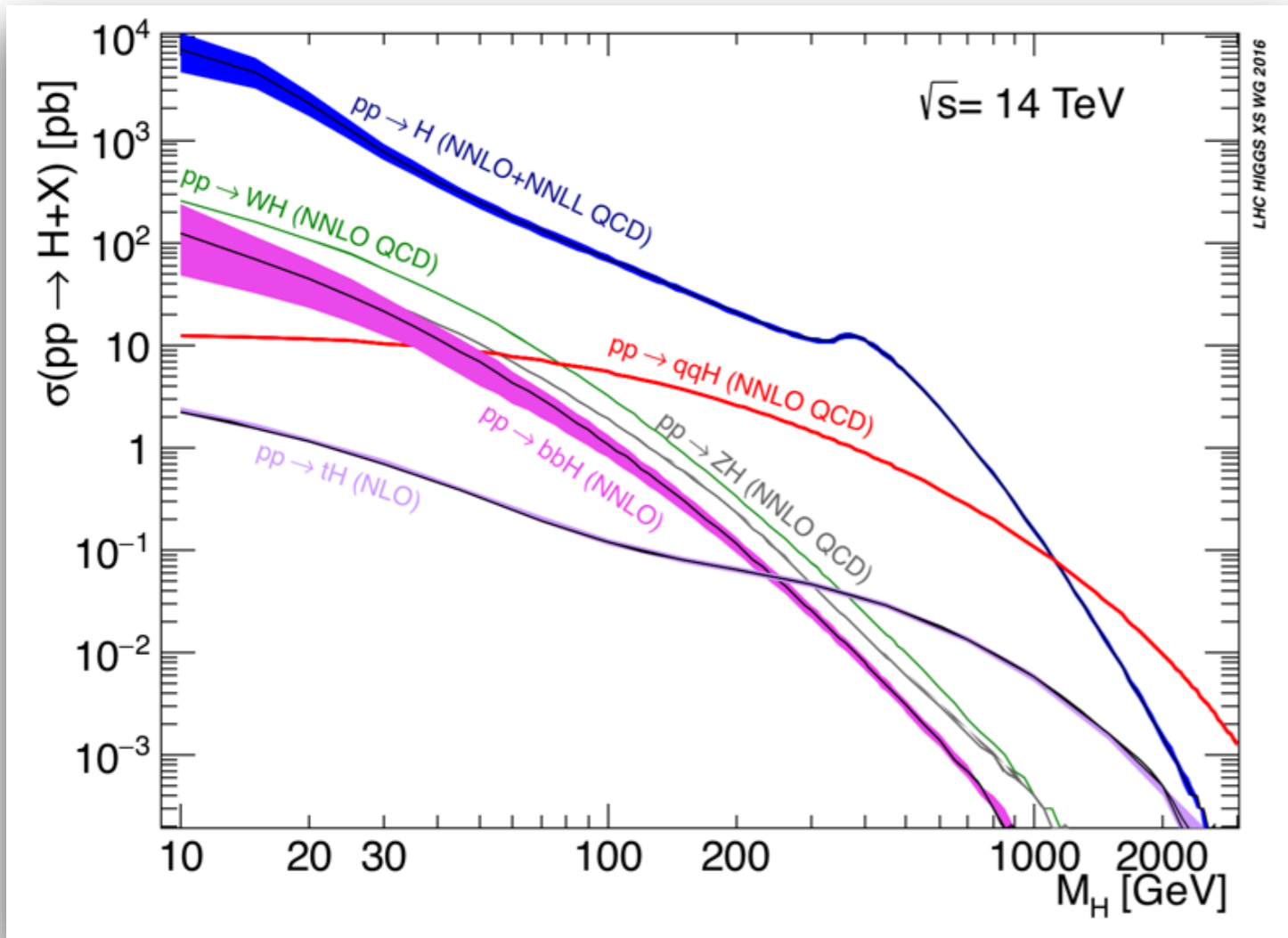
$$\kappa_\lambda = 3 : \quad \sigma_{tot} = 18.67^{+12\%}_{-22\%} \text{ fb}$$

$$\kappa_\lambda = 5 : \quad \sigma_{tot} = 94.82^{+18\%}_{-13\%} \text{ fb}$$

$$\kappa_\lambda = 10 : \quad \sigma_{tot} = 672.2^{+16\%}_{-13\%} \text{ fb}$$

# Standard Model Higgs Production

[Higgs Working Group, YR4]

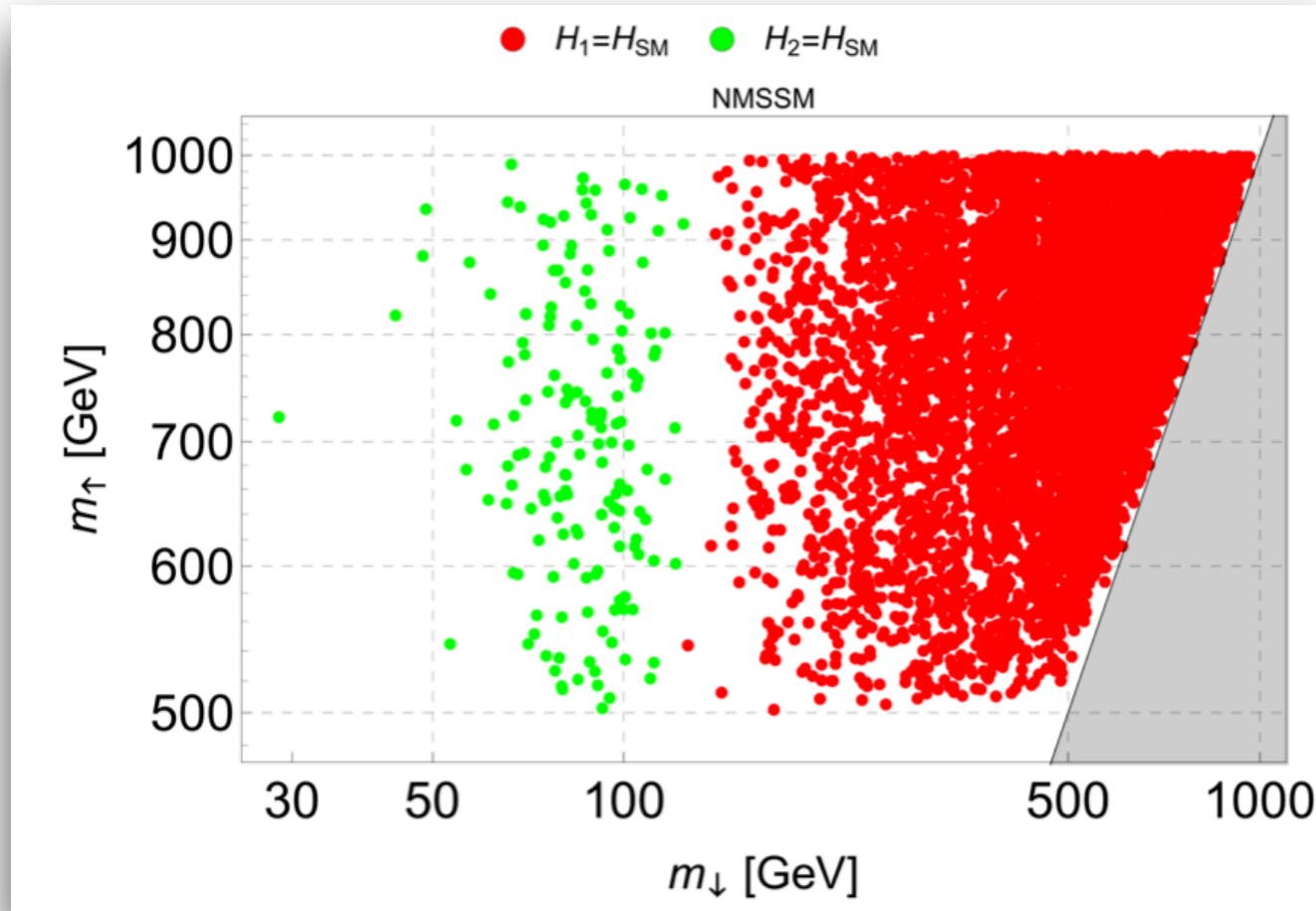




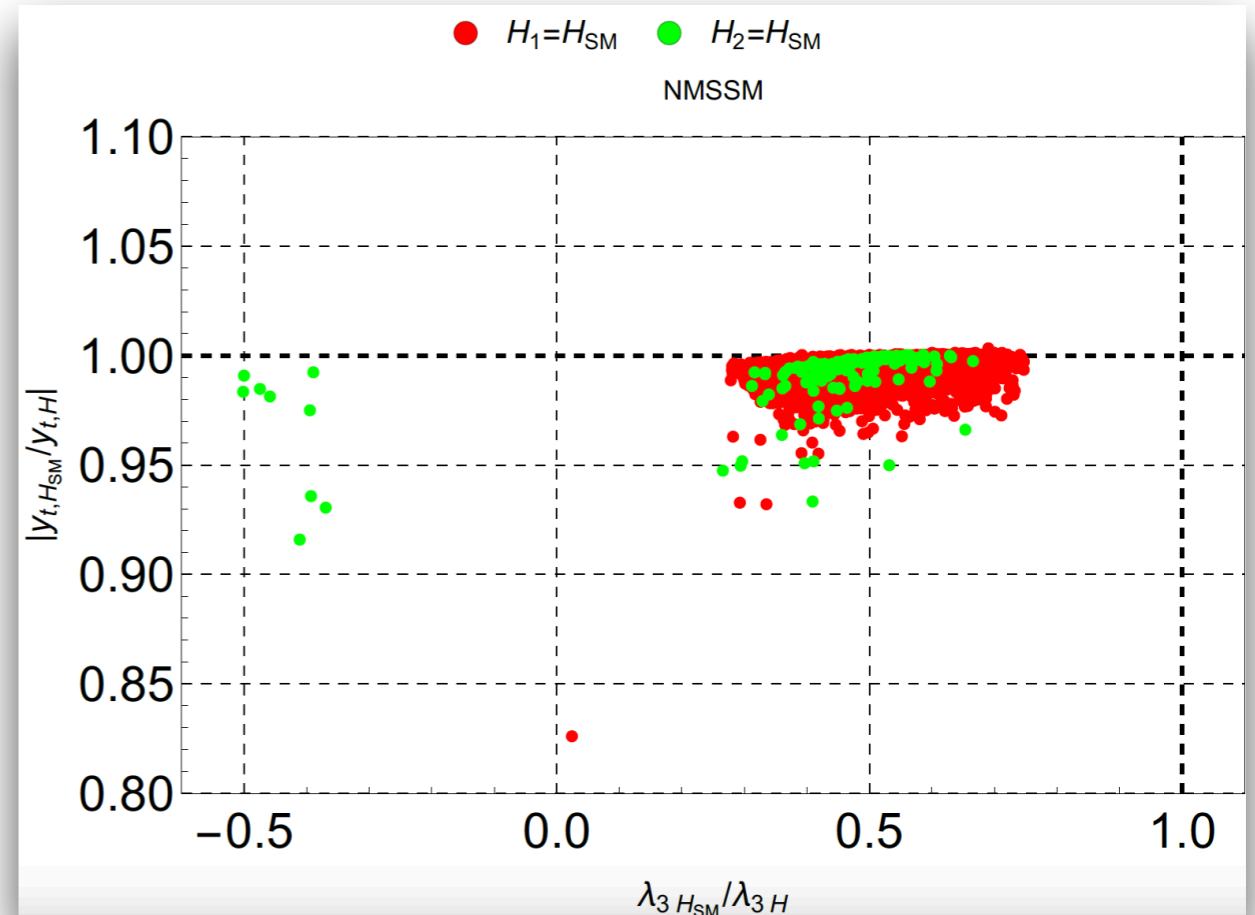
# Scan Result: Mass and Couplings Distributions

[Abouabid, Arhrib, Azevedo, El Falaki, Ferreira, MM, Santos, '21]

## Masses



## Couplings



Non-SM-like heavier versus non-SM-like lighter

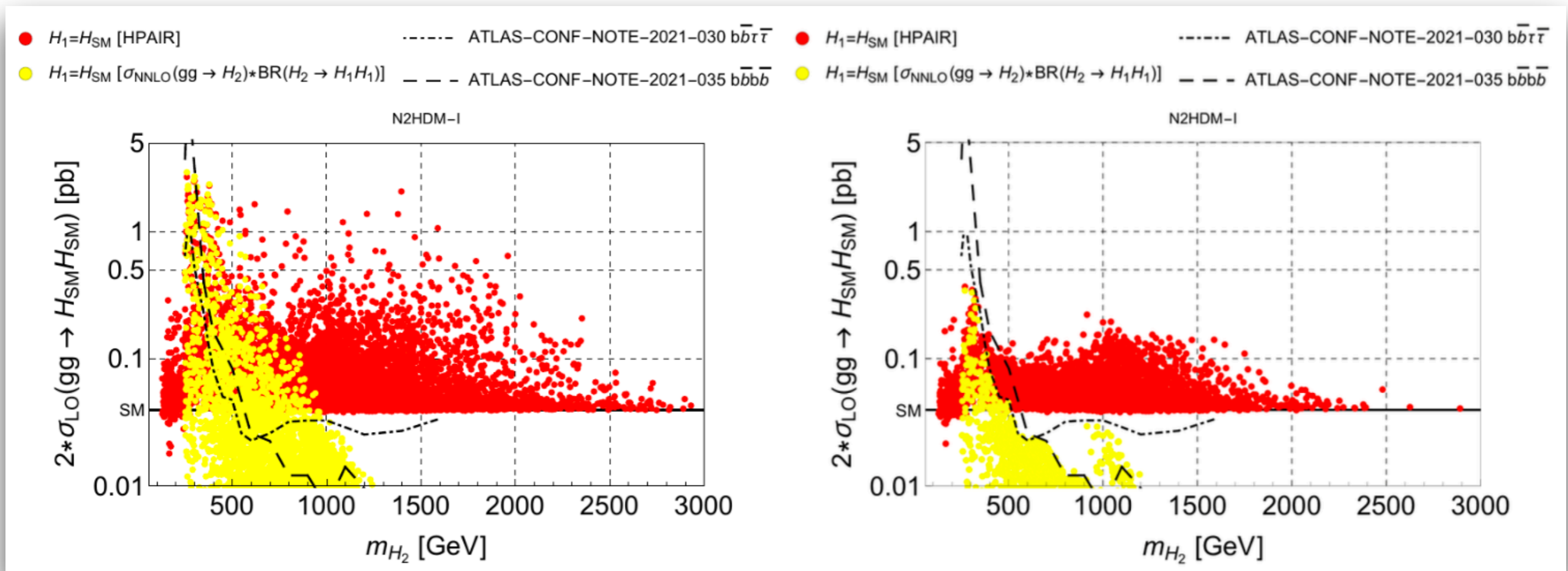
Yukawa  $y_{top}$  versus  $\lambda_{3H_{SM}}$

Red:  $H_1=H_{SM}$ , Green:  $H_2=H_{SM}$

# Impact of Constraints - Example N2HDM Type I $H_{SM} H_{SM}$ Production

[Abouabid,Arhrib,Azevedo,El Falaki,Ferreira,MM,Santos,'21]

Yellow - Resonant Prod:  $\sigma_{NNLO}(H_2) * BR(H_2 \rightarrow H_{SM} H_{SM})$  Red - Continuum Prod:  $2 * \sigma_{LO}(H_{SM} H_{SM})$



- Factor 2 roughly accounts for NLO QCD corrections (benchmark points w/ HPAIR at NLO QCD in heavy-top-limit)
- Resonant searches start constraining BSM models

---

# Impact of Non-resonant Searches

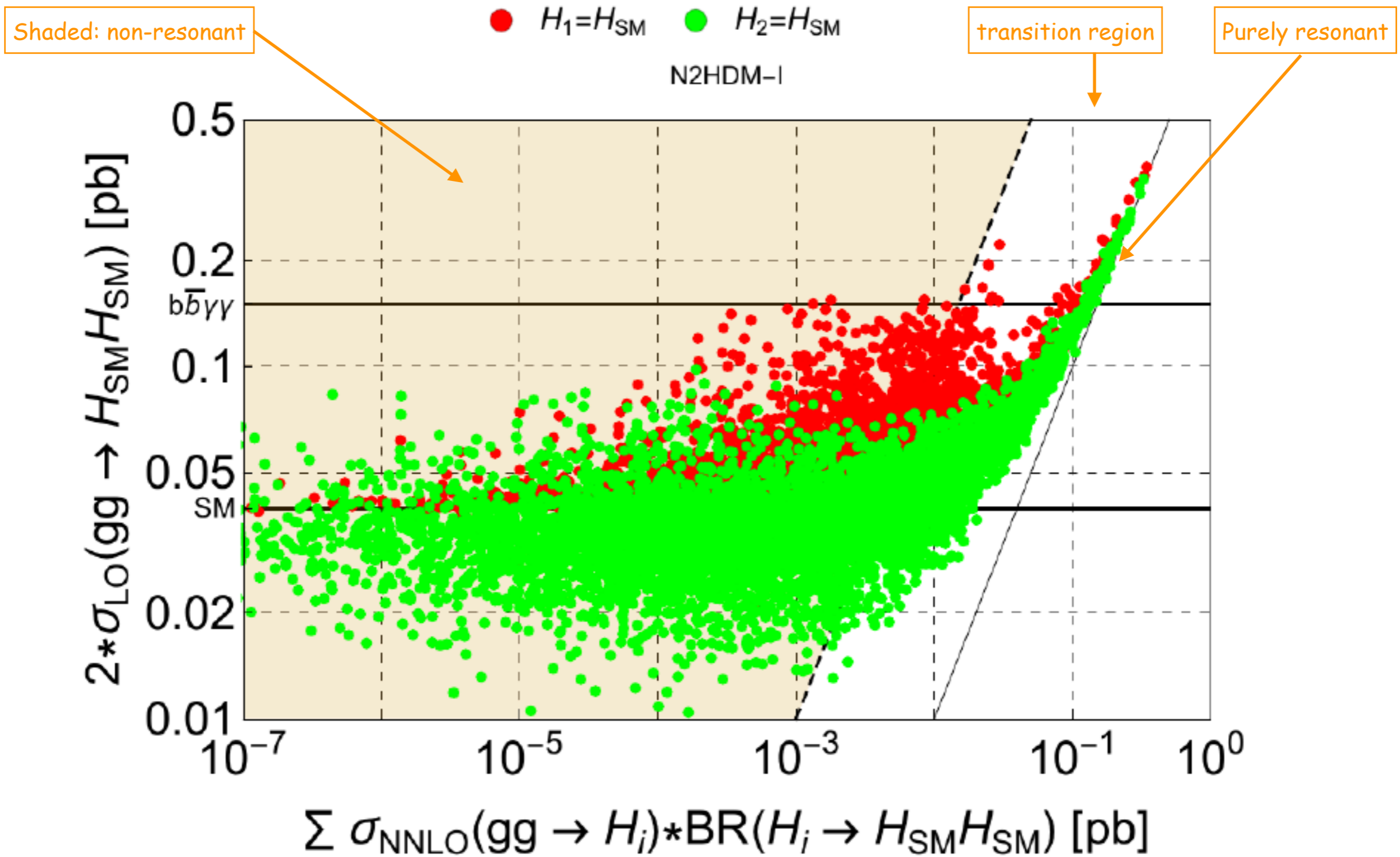
---

✦ Our definition:

take into account all relevant theoretical and experimental constraints  
+ limits from di-Higgs searches

$$\sigma_{\text{res}}^{\text{HH}} < 0.1 * \sigma_{\text{full}} \rightarrow \text{non-resonant production}$$

# Impact of Non-resonant Searches - Example N2HDM



# Allowed values of the trilinear Higgs self-coupling

	R2HDM		C2HDM	
	$y_{t,H_{SM}}^{R2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{R2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{C2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{C2HDM} / \lambda_{3H}$
light I	0.893...1.069	-0.096...1.076	0.898...1.035	-0.035...1.227
medium I	n.a.	n.a.	0.889...1.028	0.251...1.172
heavy I	0.946...1.054	0.481...1.026	0.893...1.019	0.671...1.229
light II	0.951...1.040	0.692...0.999	0.956...1.040	0.096...0.999
medium II	n.a.	n.a.	–	–
heavy II	–	–	–	–
	N2HDM		NMSSM	
	$y_{t,H_{SM}}^{N2HDM} / y_{t,H}$	$\lambda_{3H_{SM}}^{N2HDM} / \lambda_{3H}$	$y_{t,H_{SM}}^{NMSSM} / y_{t,H}$	$\lambda_{3H_{SM}}^{NMSSM} / \lambda_{3H}$
light I	0.895...1.079	-1.160...1.004	n.a.	n.a.
medium I	0.874...1.049	-1.247...1.168	n.a.	n.a.
heavy I	0.893...1.030	0.770...1.112	n.a.	n.a.
light II	0.942...1.038	-0.608...0.999	0.826...1.003	0.024...0.747
medium II	0.942...1.029	0.613...0.994	0.916...1.000	-0.502...0.666
heavy II	–	–	–	–

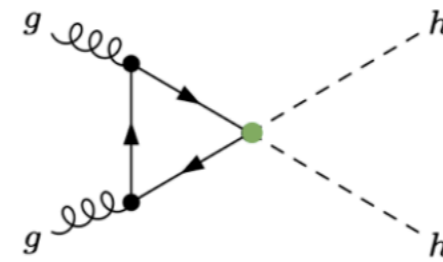
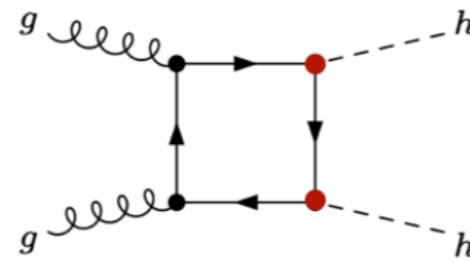
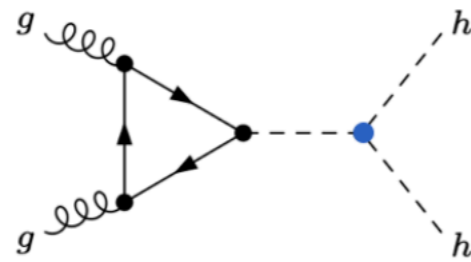
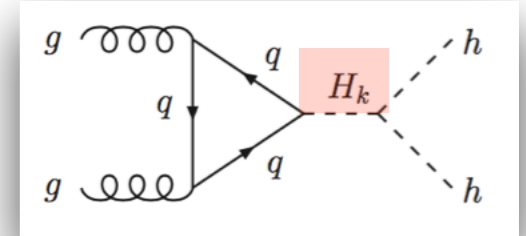
# Comparison with EFT

♦ **Effective Lagrangian:**  $\Delta\mathcal{L}_{\text{non-lin}} \supset -m_t t\bar{t} \left( c_t \frac{h}{v} + c_{tt} \frac{h^2}{2v^2} \right) - c_3 \frac{1}{6} \left( \frac{3M_h^2}{v} \right) h^3$

$c_3$ : trilinear coupling modification;  $c_t$ : top-Yukawa coupling modification;

$c_{tt}$ : effective two-Higgs-two-fermion coupling

no  $c_g, c_{gg}$ : no new heavy colored BSM particles assumed



♦ **Matching relations of our specific BSM models:**

Higgs-top Yukawa coupling	:	$g_t^{H_{\text{SM}}}(\alpha_i, \beta)$	$\rightarrow$	$c_t$
trilinear Higgs coupling	:	$\frac{g_3^{H_{\text{SM}}H_{\text{SM}}H_{\text{SM}}}(p_i)}{3M_{H_{\text{SM}}}^2/v}$	$\rightarrow$	$c_3$
two-Higgs-two-top quark coupling	:	$\sum_{k=1}^{k_{\text{max}}} \left( \frac{-v}{m_{H_k}^2} \right) g_3^{H_k H_{\text{SM}} H_{\text{SM}}}(p_i) g_t^{H_k}(\alpha_i, \beta)$	$\rightarrow$	$c_{tt}$

# 2HDM versus EFT

♦ R2HDM T2 sample parameter point:

$m_{H_1}$ [GeV]	$m_{H_2}$ [GeV]	$m_A$ [GeV]	$m_{H^\pm}$ [GeV]	$\alpha$	$\tan \beta$	$m_{12}^2$ [GeV <sup>2</sup> ]
125.09	1131	1082	1067	-0.924	0.820	552749

♦ corresponding EFT values:

$$g_t^{H_2} = -1.126$$

$$c_3 = 0.782, \quad c_t = 0.951, \quad c_{tt} = -0.122$$

♦ goodness of approximation?:

$m_{H_2}$ [GeV]	$\Gamma_{H_2}$ [GeV]	$c_{tt}$	$g_3^{H_2 H_1 H_1}$ [GeV]	$\sigma_{\text{R2HDM}}^{\text{w/ res}}$ [fb]	$\sigma_{\text{SMEFT}}^{c_{tt} \neq 0}$ [fb]	ratio
1131	78.80	-0.1222	-504.52	30.5	26.1	86%
1200	89.74	-0.1031	-479.29	27.7	24.8	90%
1500	470.2	$-4.853 \cdot 10^{-2}$	-352.42	21.8	21.4	98%

♦ Remark:

$$\sigma_{\text{R2HDM}}^{\text{w/o res}} = 18.6 \text{ fb} \quad \text{and} \quad \sigma_{\text{SMEFT}}^{c_{tt}=0} = 18.6 \text{ fb}$$

# N2HDM versus EFT

♦ N2HDM T1 sample parameter point:

$m_{H_1}$ [GeV]	$m_{H_2}$ [GeV]	$m_{H_3}$ [GeV]	$m_A$ [GeV]	$m_{H^\pm}$ [GeV]	$\tan \beta$
125.09	269	582	390	380	4.190
$\alpha_1$	$\alpha_2$	$\alpha_3$	$v_s$ [GeV]	$\text{Re}(m_{12}^2)$ [GeV <sup>2</sup> ]	
1.432	-0.109	0.535	1250	28112	

$$g_t^{H_2} = 0.179 \quad \text{and} \quad g_t^{H_3} = 2.337 \times 10^{-2}$$

♦ corresponding EFT values:

$$c_3 = 0.877, \quad c_t = 1.012, \quad c_{tt} = 4.127 \times 10^{-2}$$

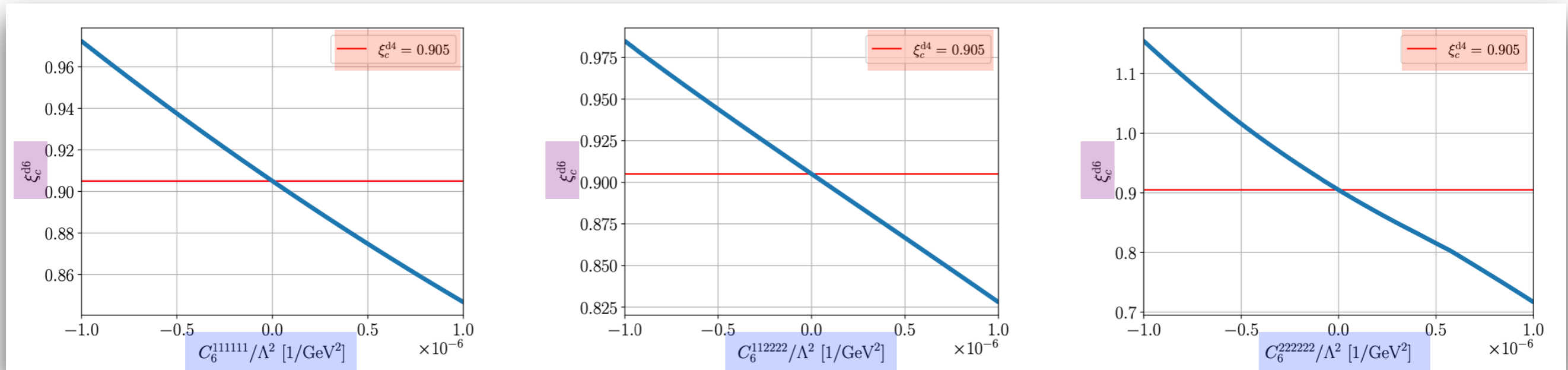
♦ goodness of approximation?: ( $m_{H_3}$  kept fixed)

$m_{H_2}$	$\Gamma_{H_2}$	$c_{tt}^{H_2}$	$c_{tt}$	$g_3^{H_2 H_1 H_1}$	$\sigma_{\text{N2HDM}}^{\text{w/ res}}$ [fb]	$\sigma_{\text{SMEFT}}^{c_{tt} \neq 0}$ [fb]	ratio
269	0.075	$4.410 \times 10^{-2}$	$4.127 \times 10^{-2}$	-72.42	183.70	20.56	11%
300	0.083	$3.170 \times 10^{-2}$	$2.877 \times 10^{-2}$	-64.80	162.80	21.28	13%
400	0.177	$9.544 \times 10^{-3}$	$6.721 \times 10^{-3}$	-34.68	43.33	22.60	52%
420	0.229	$6.895 \times 10^{-3}$	$4.063 \times 10^{-3}$	-27.62	31.70	22.76	72%
440	0.284	$4.600 \times 10^{-3}$	$1.767 \times 10^{-3}$	-20.22	26.26	22.90	87%
450	0.315	$3.564 \times 10^{-3}$	$7.323 \times 10^{-4}$	-16.39	24.84	22.96	92%
500	2.567	$-7.132 \times 10^{-4}$	$-3.545 \times 10^{-3}$	4.05	23.56	23.22	99%



# Effect of Dim-6 Operators

[Anisha,Biermann,Englert,MM,'22]



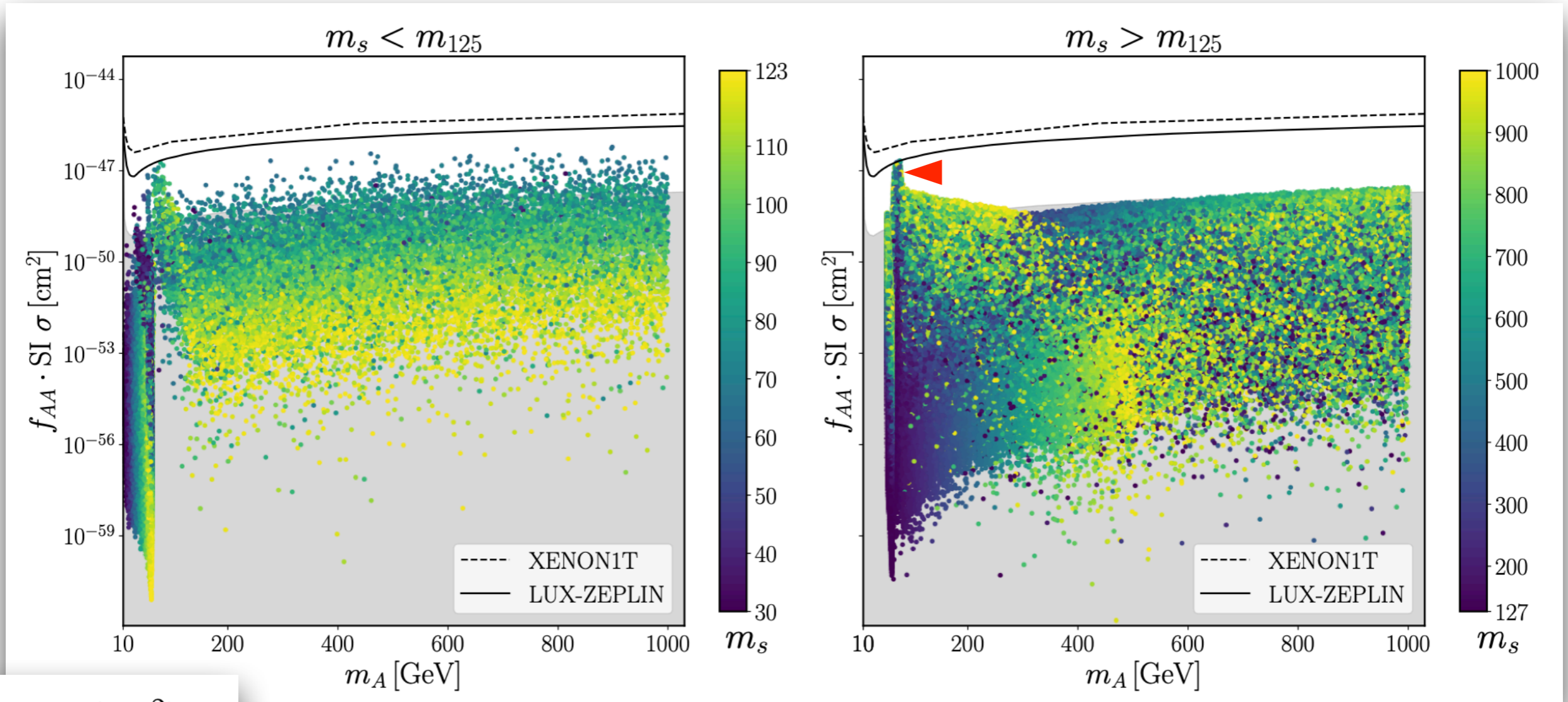
impact of individual Wilson coefficients on  $\xi_c^{d6}$  for  $\xi_c^{d4} \cong 0.9$ :

- linear response  $\sim C_{i6}$  -> perturbativity ok
- SFOEWPT achievable in agreement with experimental constraints

interference effects in heavy Higgs production in  $t\bar{t}$  final state are width dependent  
-> sensitive to EFT modifications: overall effect is small after taking the Higgs data constraints into account =>  $h h$  production important tool for fingerprinting SFOEWPT

# Dark Matter Direct Detection

[Egle,MM,Santos,Viana,'23]



$$f_{AA} = \frac{(\Omega h^2)_A}{(\Omega h^2)_{DM}^{obs}}$$

◀ : LZ sensitive to  $66 \text{ GeV} \leq m_A \leq 78 \text{ GeV}$  region (not testable through  $H(125 \text{ GeV}) \rightarrow AA$  decay)