

LQG suggest the existence of

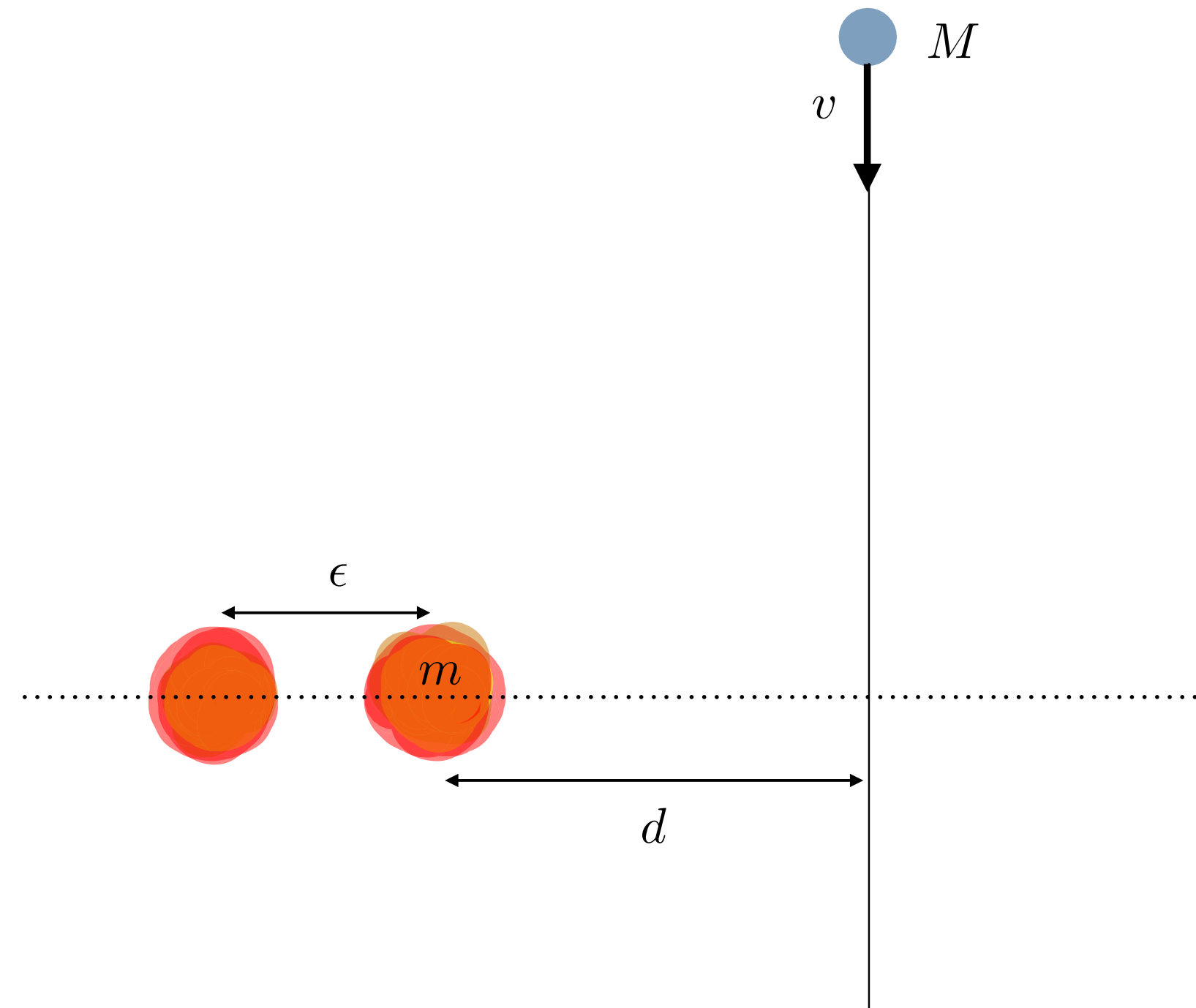
a quasi-stable particle with mass $\sim 20\mu\text{g}$

which can interact gravitationally only

- 1) LQG suggest the existence of a quasi-stable particle with mass $\sim 20\mu\text{g}$
- 2) This particle can be detected
- 3) It is a natural candidate for Dark Matter
- 4) It can be generated by the complete evaporation of an old black hole

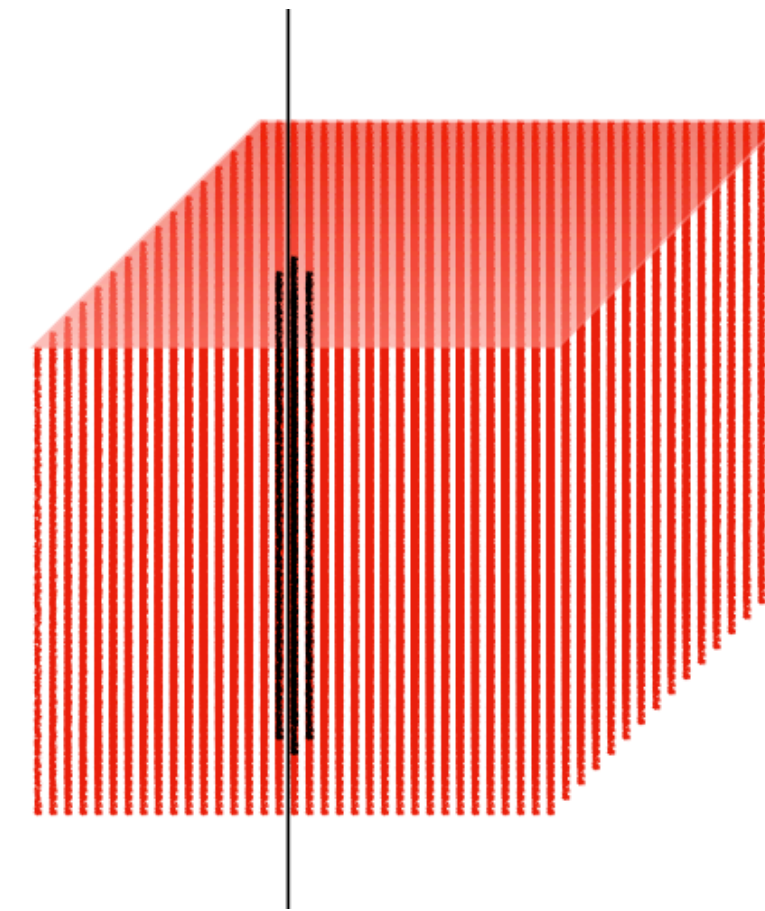
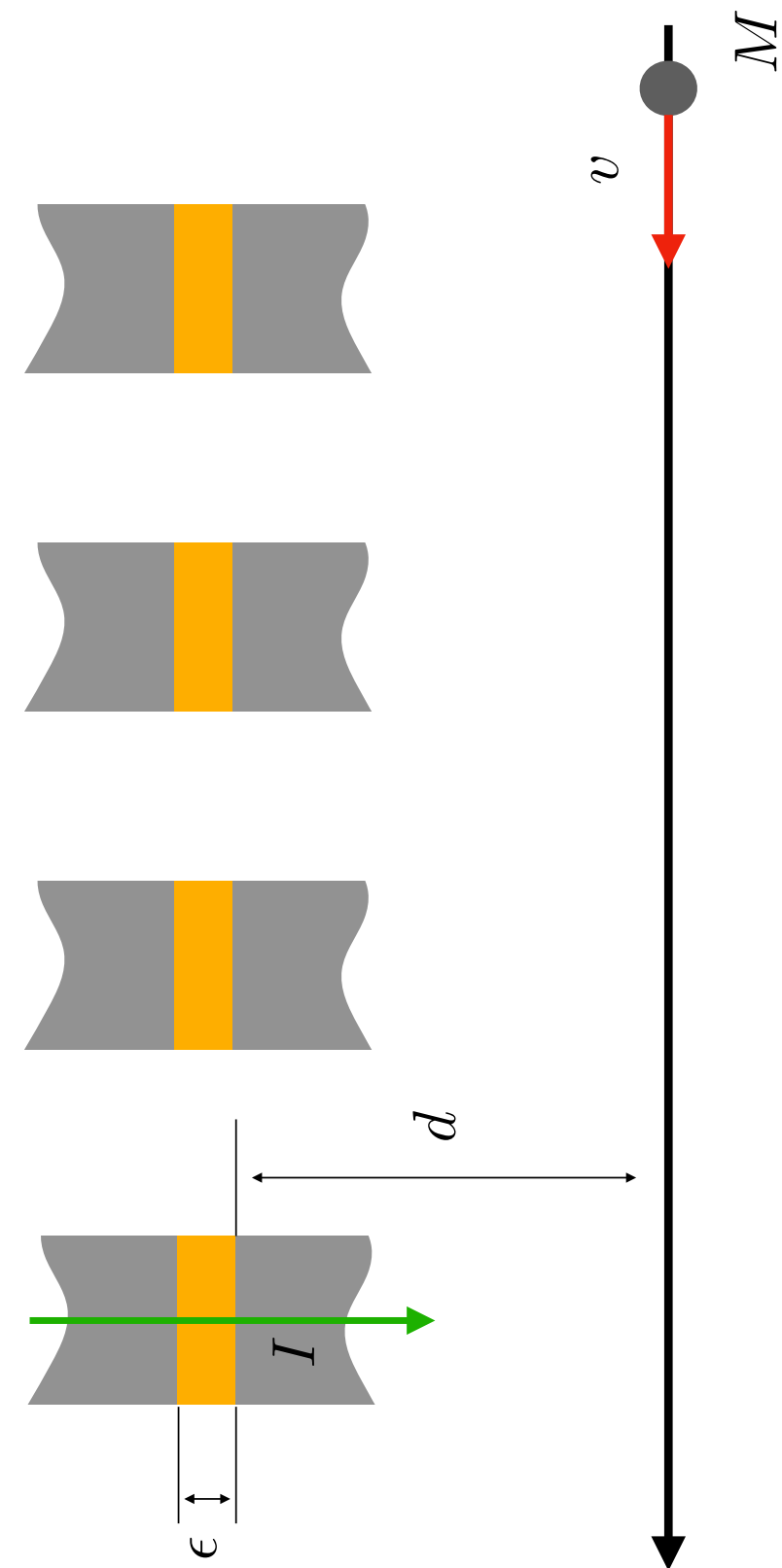
$$m_{Plank} = \sqrt{\frac{\hbar c}{G}} \sim 22\mu g$$

Direct detection. In Principle

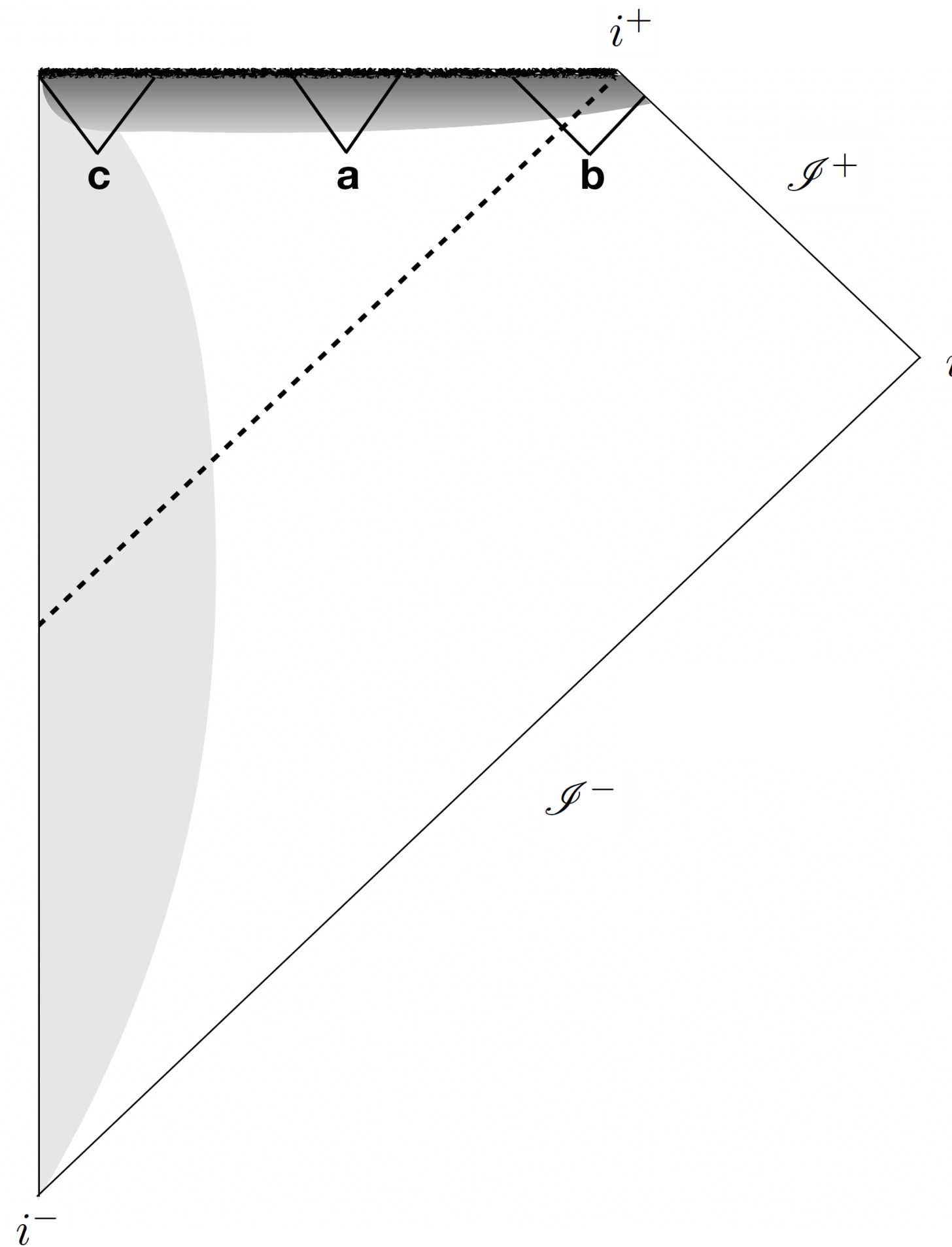


A Perez, M Christodoulou, CR,
Detecting Gravitationally Interacting Dark Matter with Quantum Interference,
2024

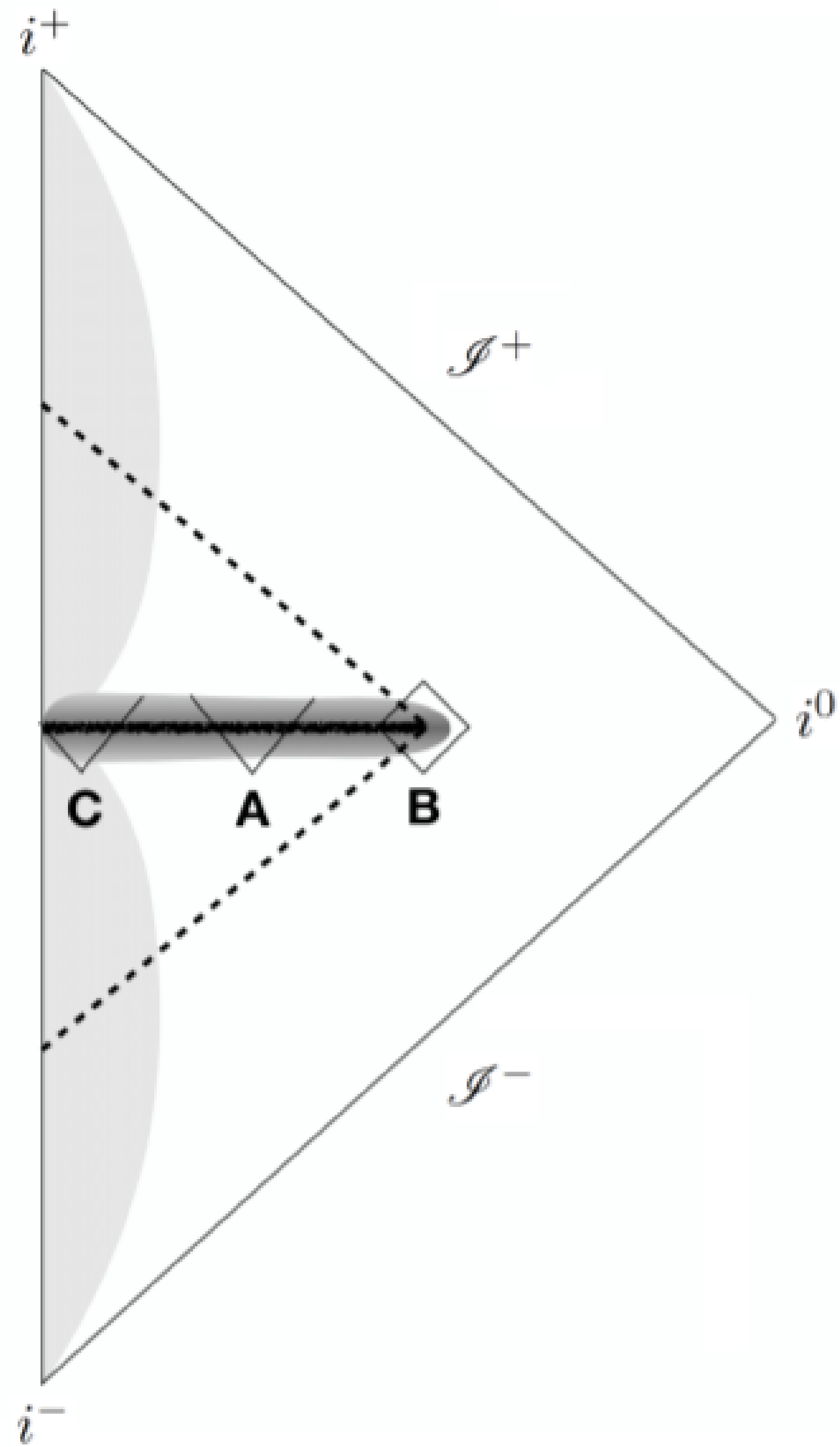
Direct detection. In Practice: Piles of Josephson Junctions



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There are three independent physical phenomena happening at the end of the BH evaporation



A. Ashtekar, B. Bojowald, 2005

F. Vidotto, CR, 2014

H. Haggard, CR, 2015

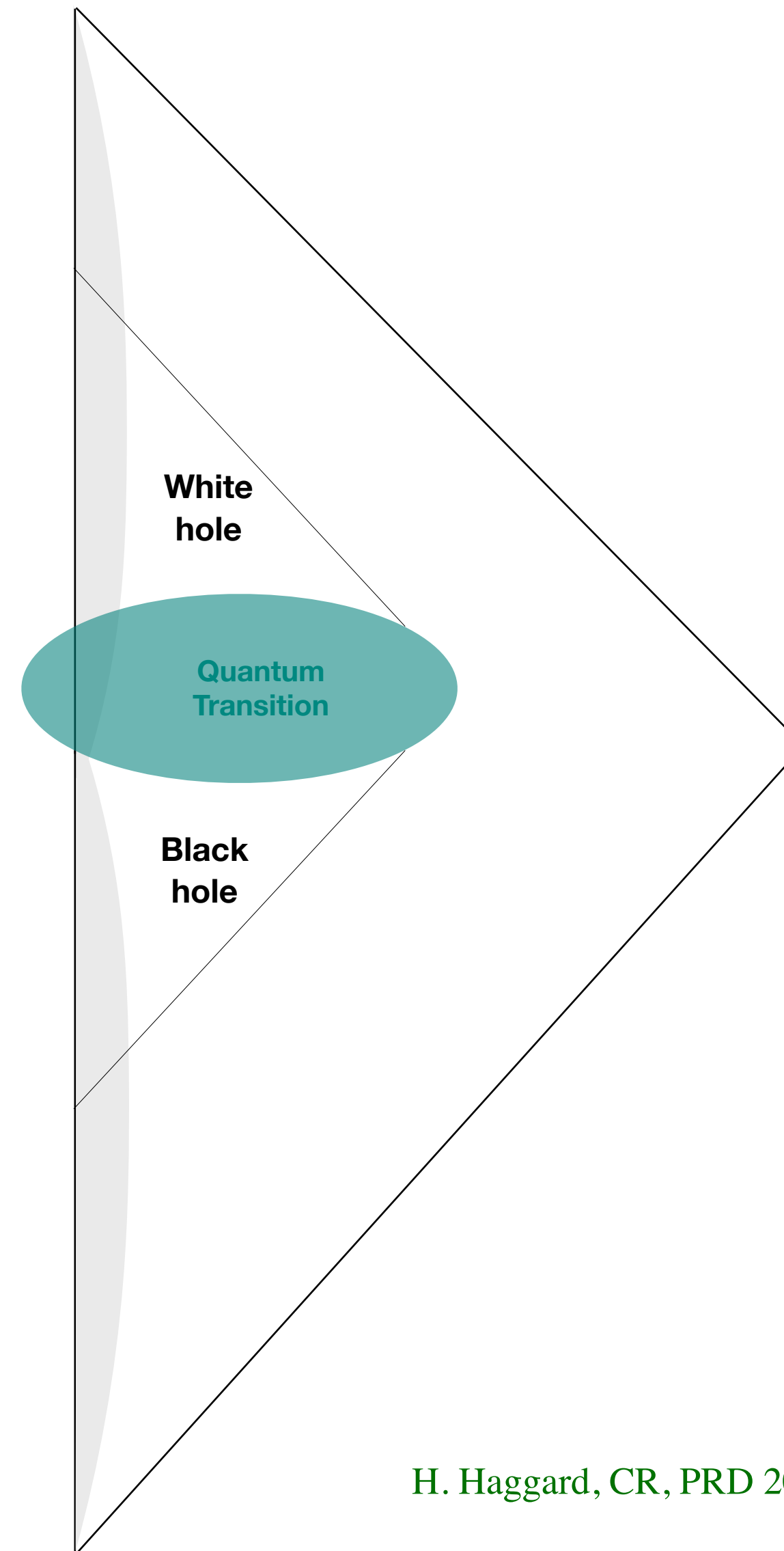
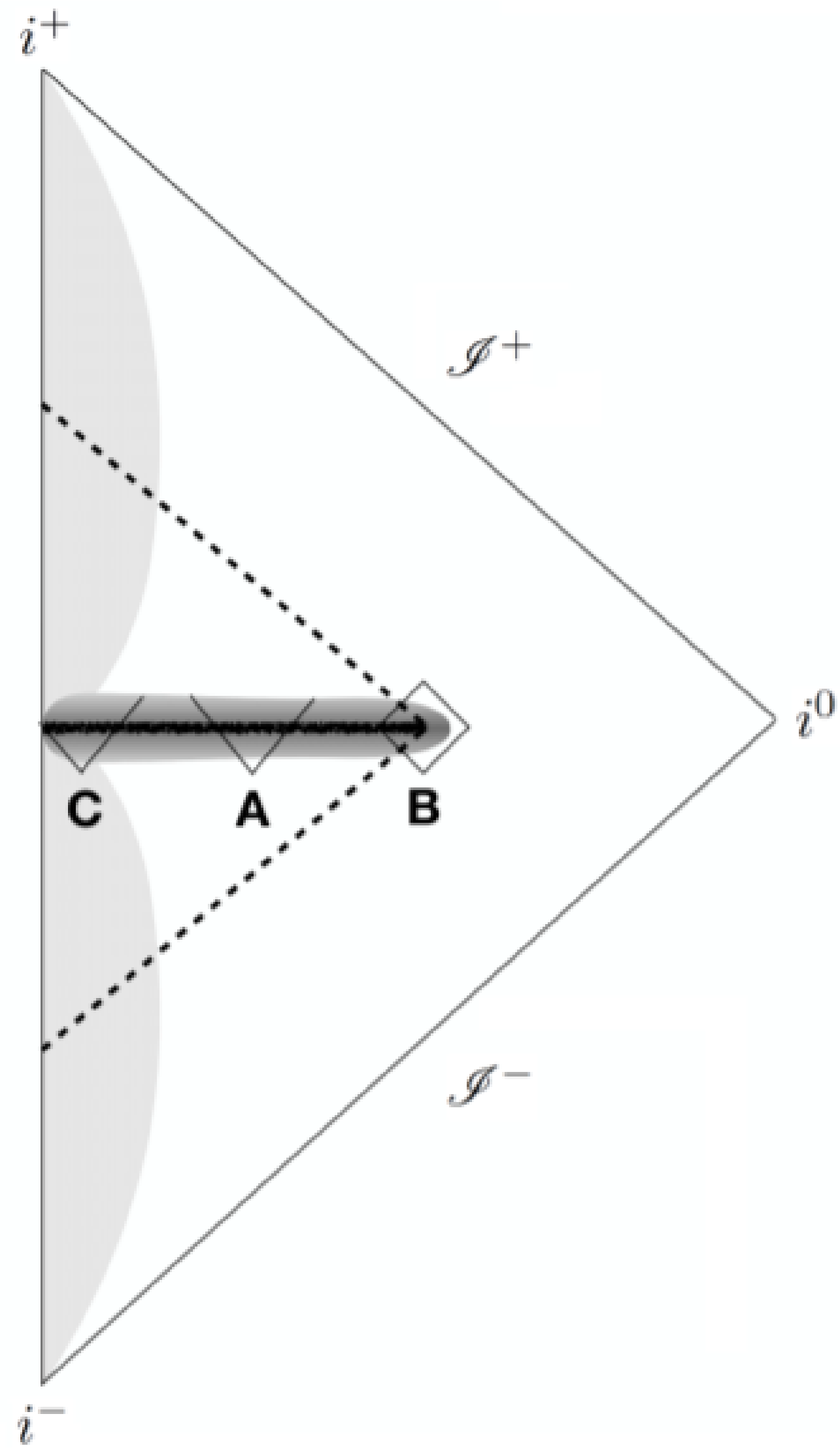
E. Bianchi, M. Christodoulou, F. D'Ambrosio, H. M. Haggard, CR, 2018

Lewandowski, Ma, Yang, Zhang, 2023

Husain, Kelly, Santacruz, Wilson-Ewing, 2022

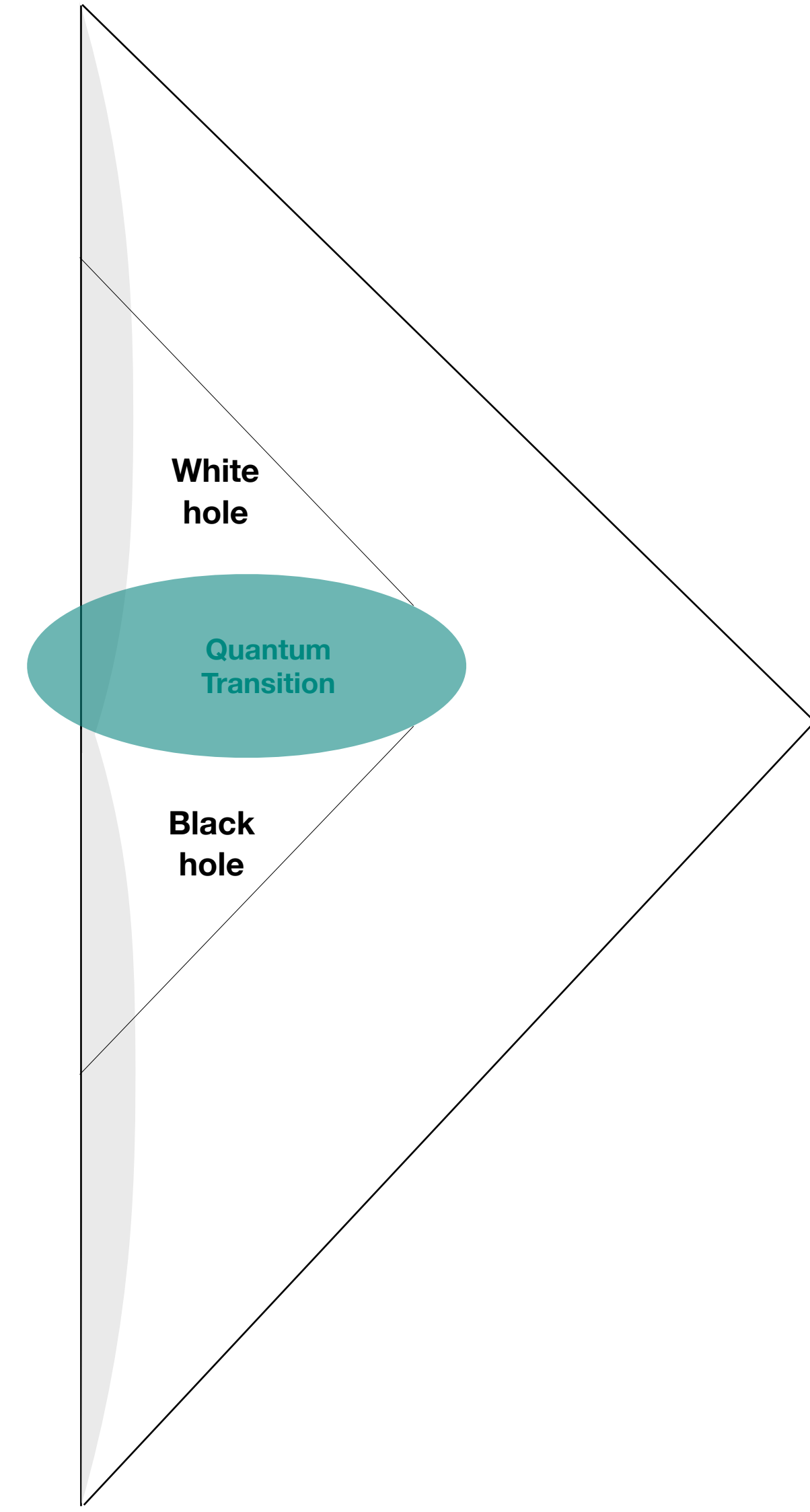
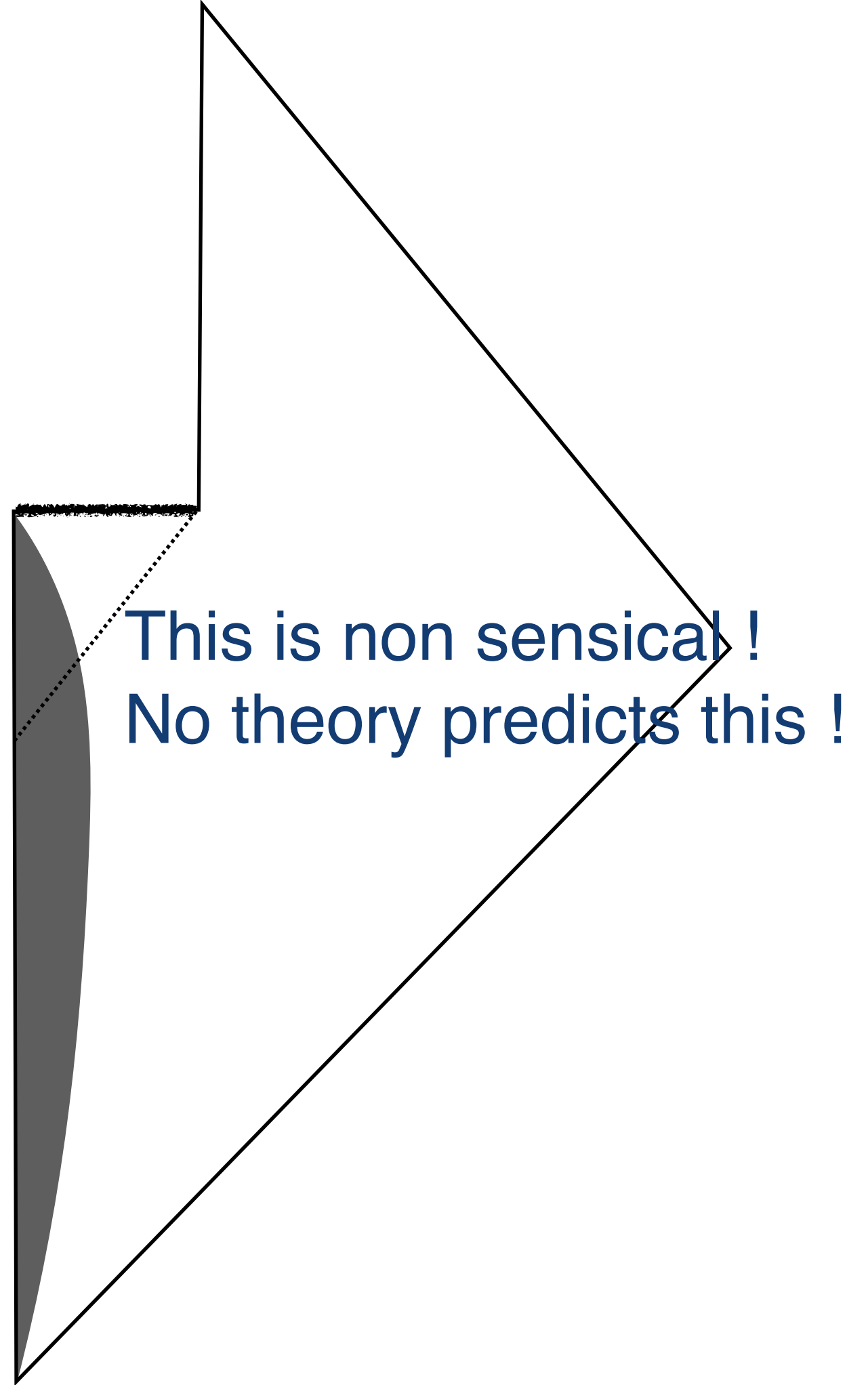
A Rignon-Bret, CR, 2021

M Han, CR, F. Soltani 2023



H. Haggard, CR, PRD 2015, arXiv:1407.0989

E. Bianchi, M. Christodoulou, F. D'Ambrosio, H. M. Haggard, CR,
 "White holes as remnants: A surprising scenario for the end of a black hole,"
 CQG 2018, arXives: 1802.04264.



Good coordinates for past patch

$$ds^2 = -F(r)dv^2 + 2dvdr + r^2d\Omega^2$$

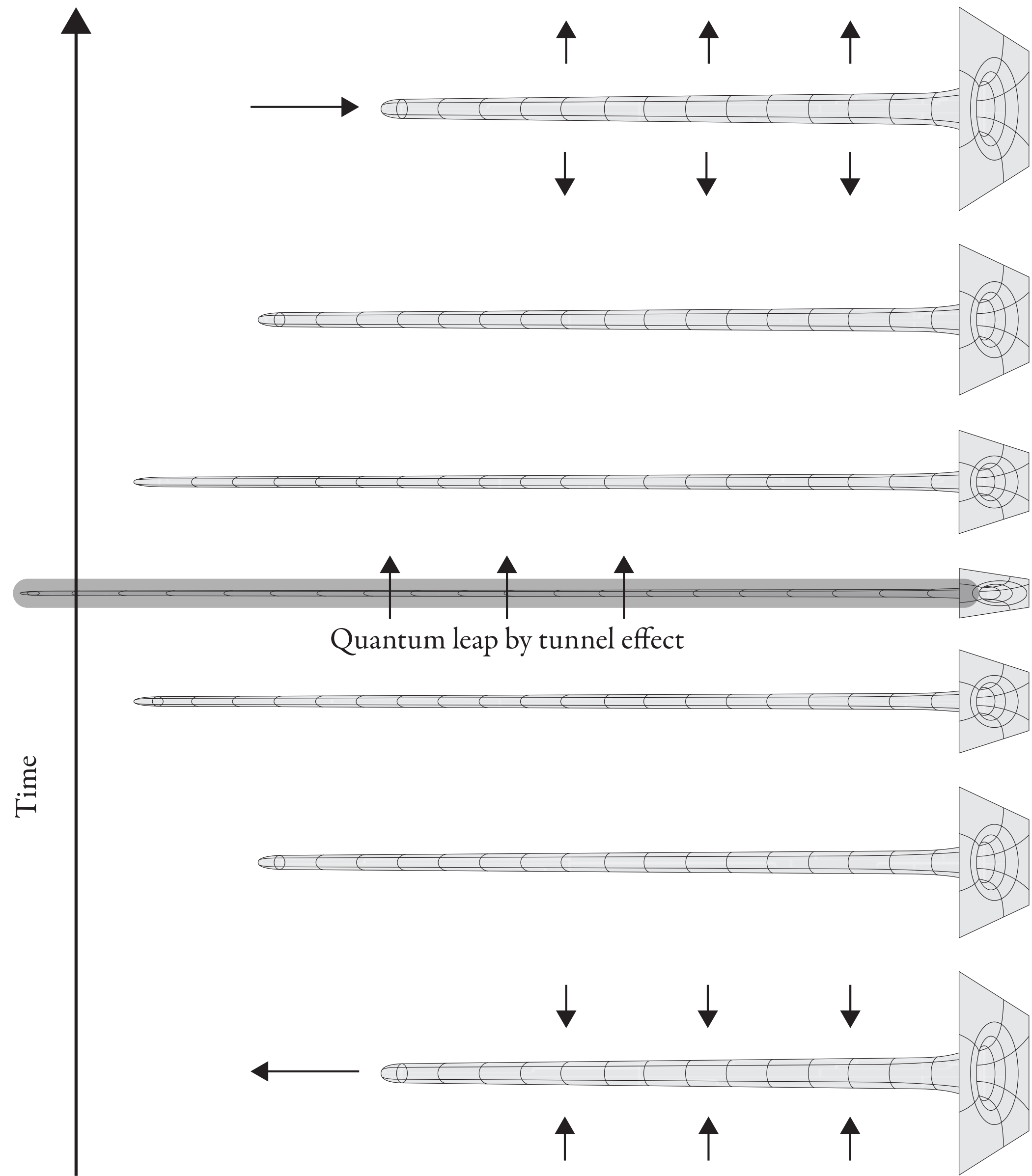
Good coordinates for future patch

$$ds^2 = -F(r)du^2 - 2dudr + r^2d\Omega^2$$

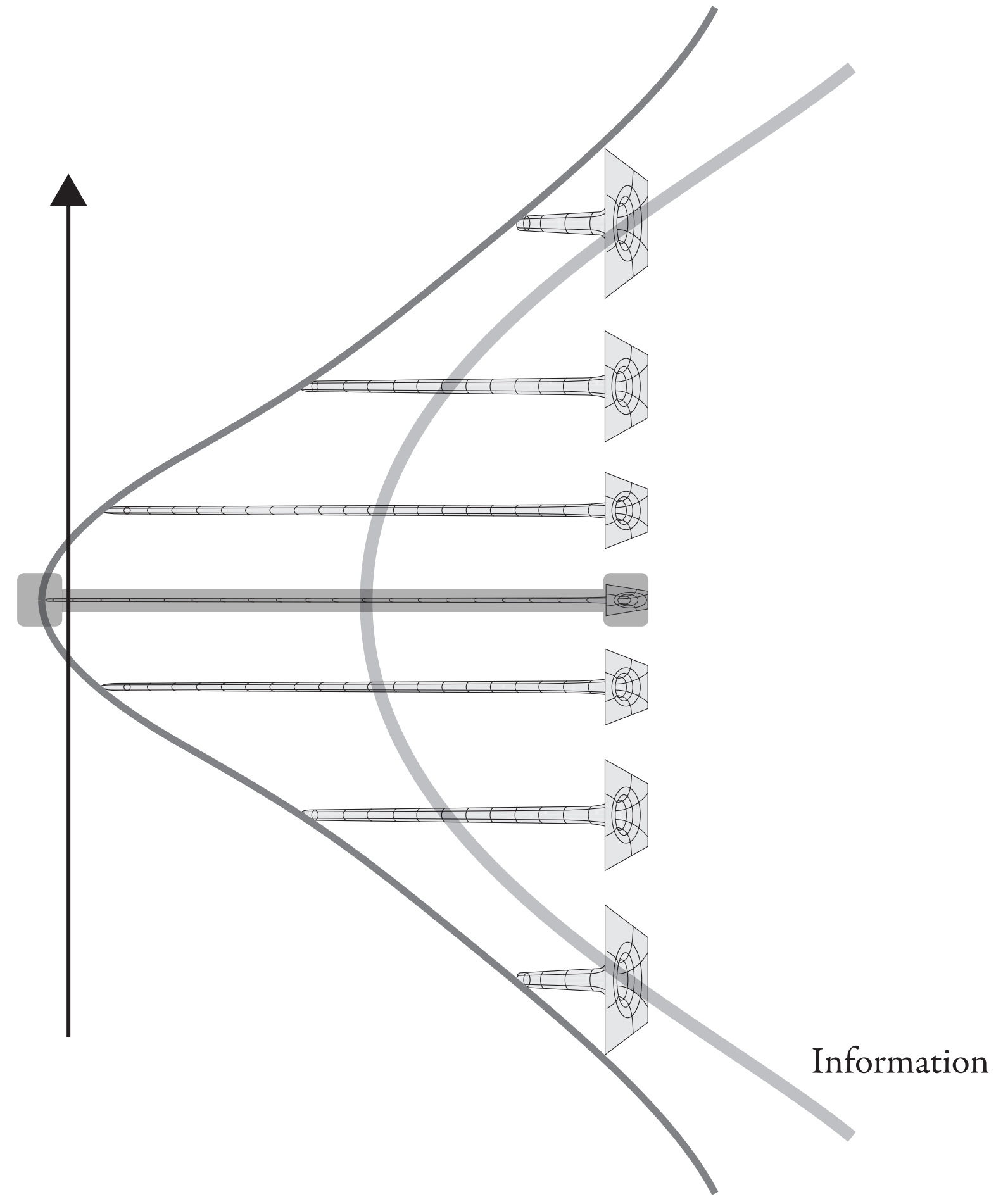
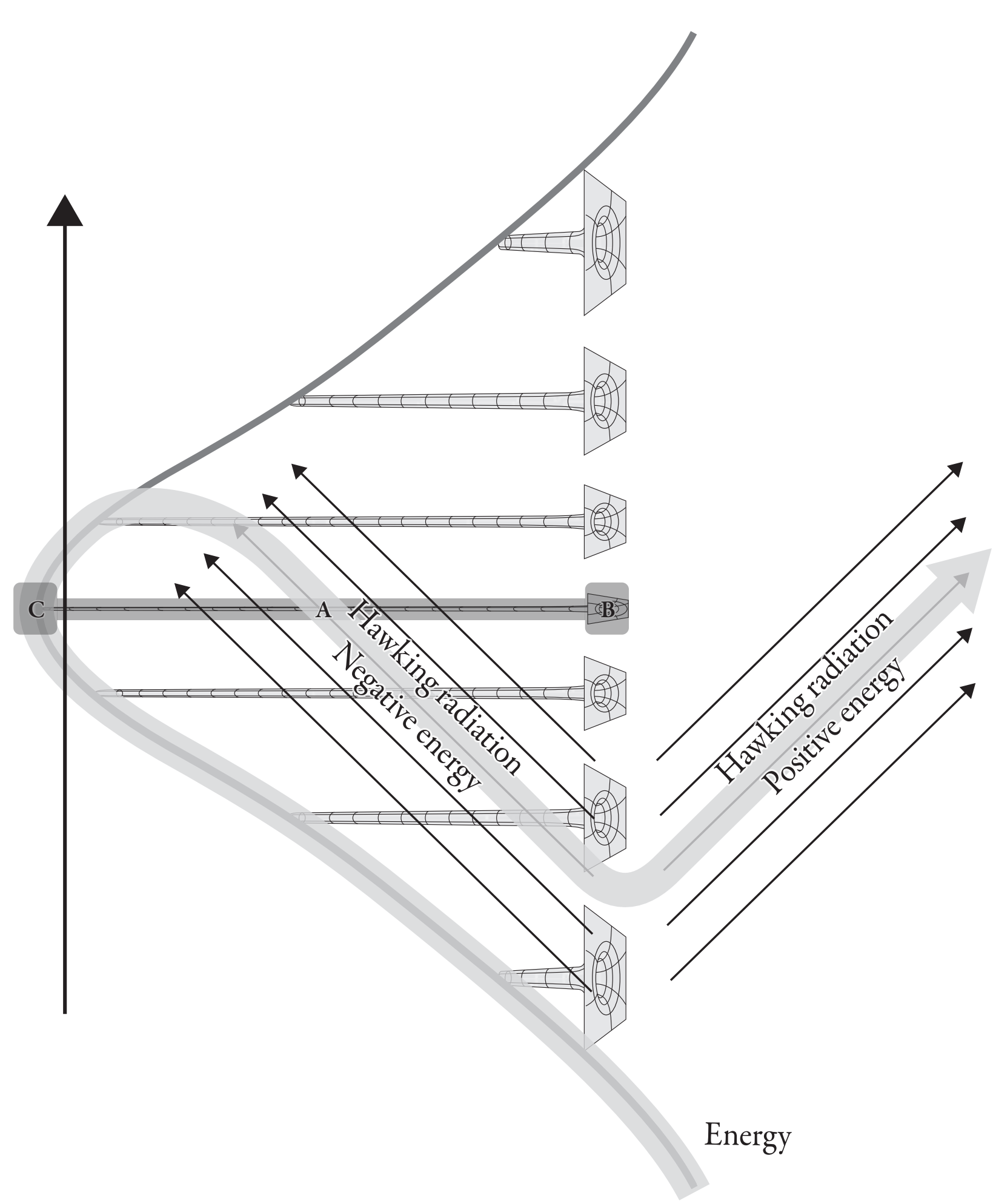
$$F(r) = 1 - \frac{2m}{r} + \frac{Am^2}{r^4}$$

Overlap

$$2r_*(r) = v + u \qquad dr_* = \frac{dr}{F(r)}$$



M Christodoulou, CR, How big is a black hole? PRD 2015.



The non existence of the information paradox

The **thermodynamical** entropy

$$\Delta S_T = \int \frac{dQ}{T}$$

measures the number of states

$$S_T = k \log W \quad S_T = k \log \dim \mathcal{H} = k \log N$$

The **von Neumann** entropy measures entanglement

$$\rho_A = \text{Tr}_B \left[|\Psi_{AB}\rangle \langle \Psi_{AB}| \right]$$

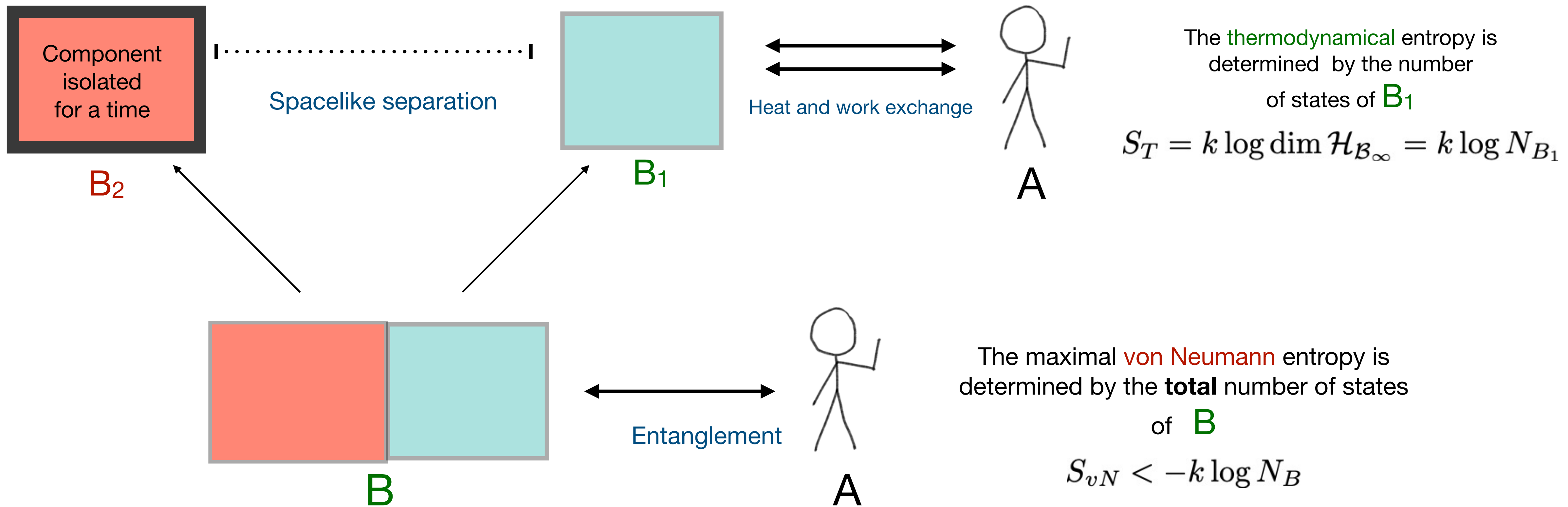
$$S_{vN} = -k \text{Tr}[\rho_A \log \rho_A]$$

It is maximized by $\rho_a = \frac{1}{N} \mathbb{1}$ $S_{vN} < k \log N$

$$S_{vN} \leq S_T$$

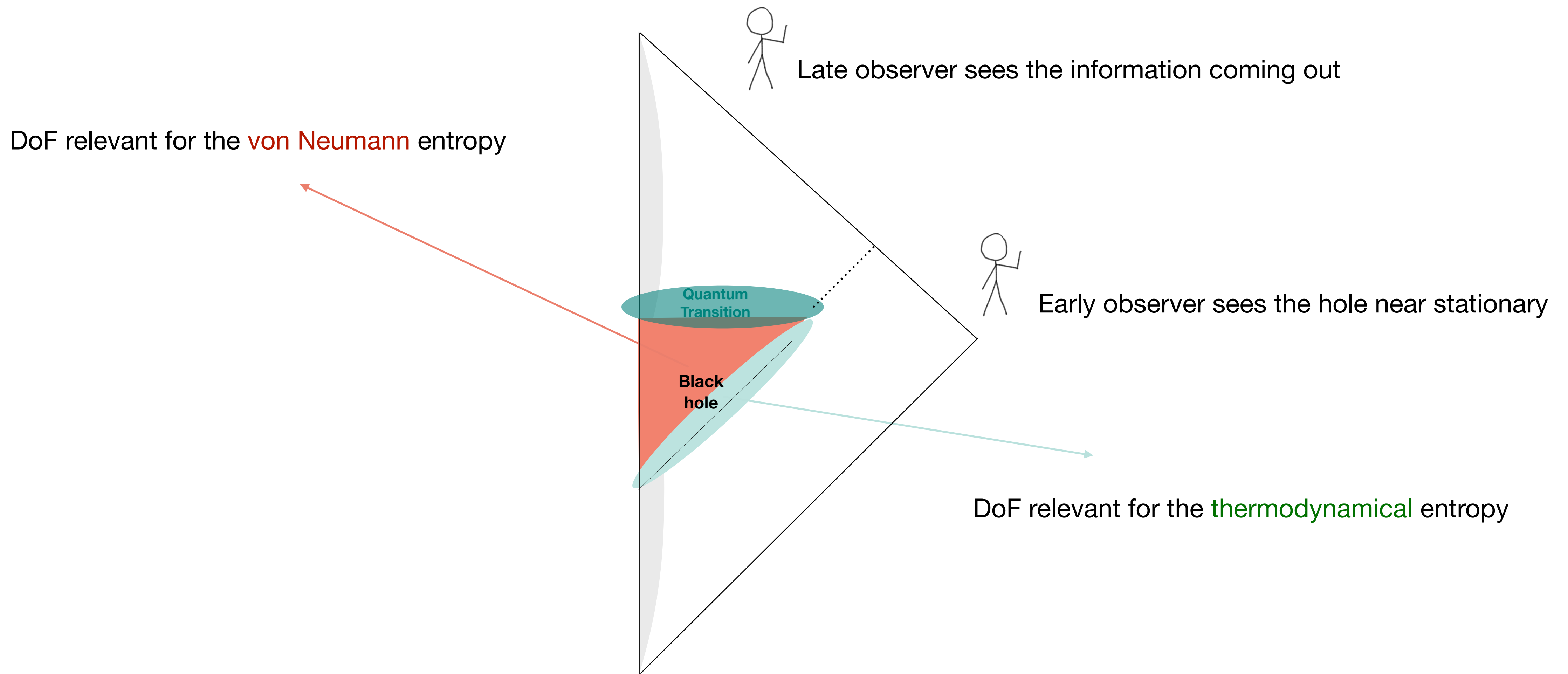


**This is only true under
(severe) conditions !**



$S_{vN} \leq S_T$ Does not hold anymore!

The **von Neumann** can be higher than the **thermodynamical** entropy.



CR, The subtle unphysical hypothesis of the firewall theorem, Entropy 2019.

CR, Black holes have more states than those giving the Bekenstein-Hawking entropy: a simple argument, CQG 2018, arXives:1710.00218

Transition probability

$$A \sim e^{-\frac{Gm^2}{c\hbar}}$$

How to think about this:

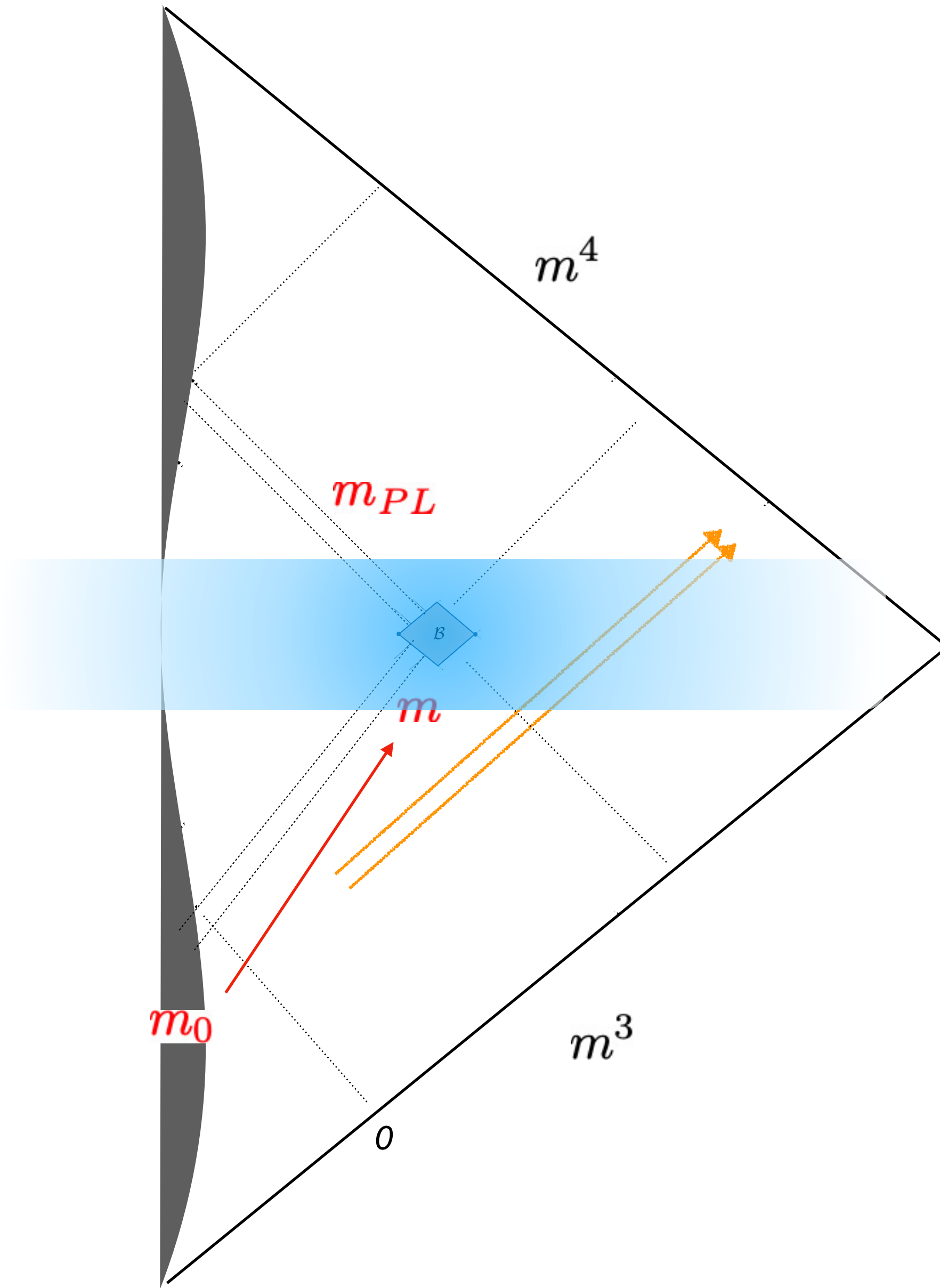
- A quantum tunnelling effect [Hal Haggard at Loop24]

P Donà , H Haggard, CR, F Vidotto, arXives: 2402.09038

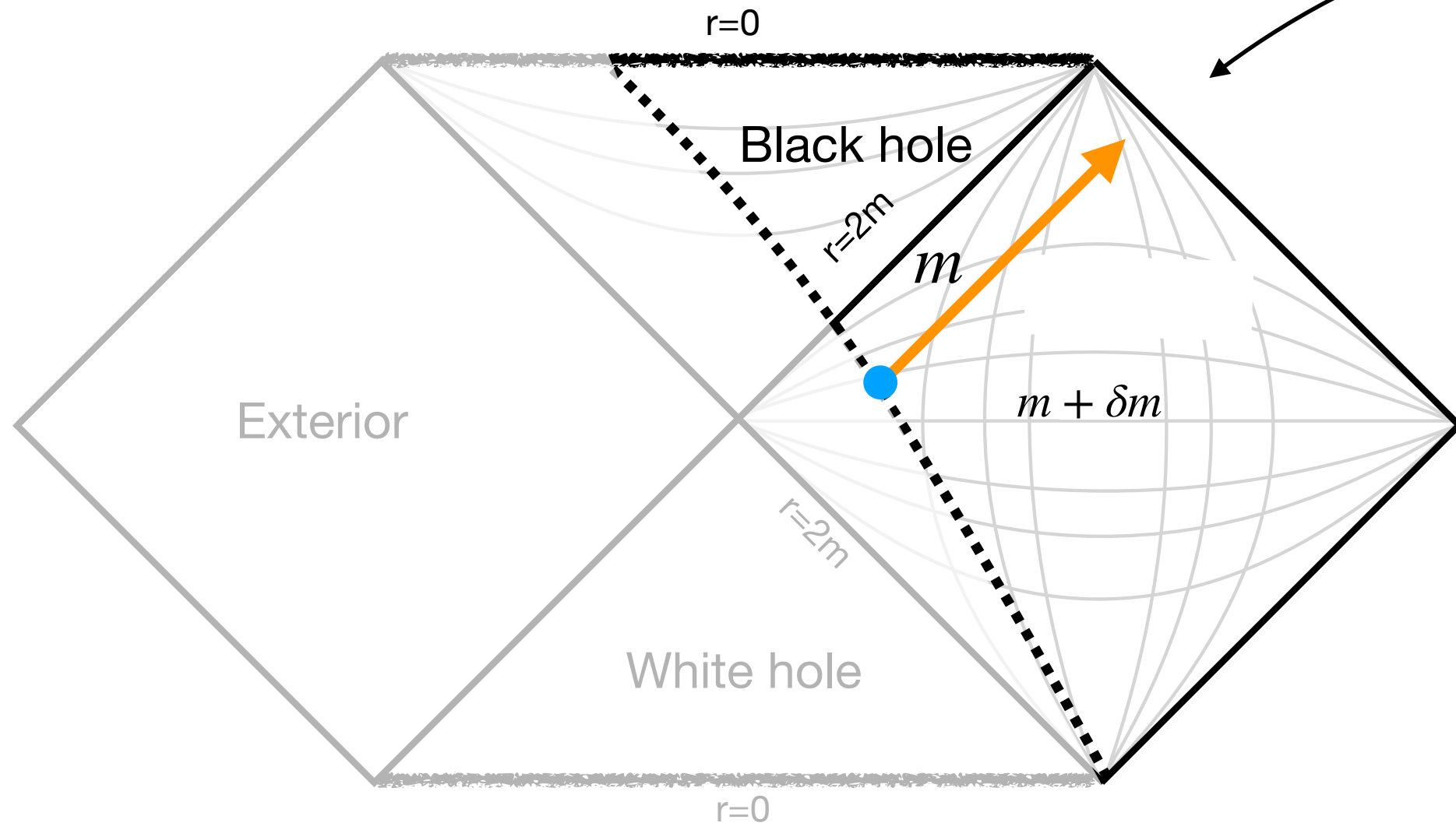
- The amplitude is approximated in the semiclassical regime by

$$A \sim e^{i S_{Regge}} \sim e^{i \sum_f j_f \theta(j_j)} \sim e^{-\sum_f Area_f}$$

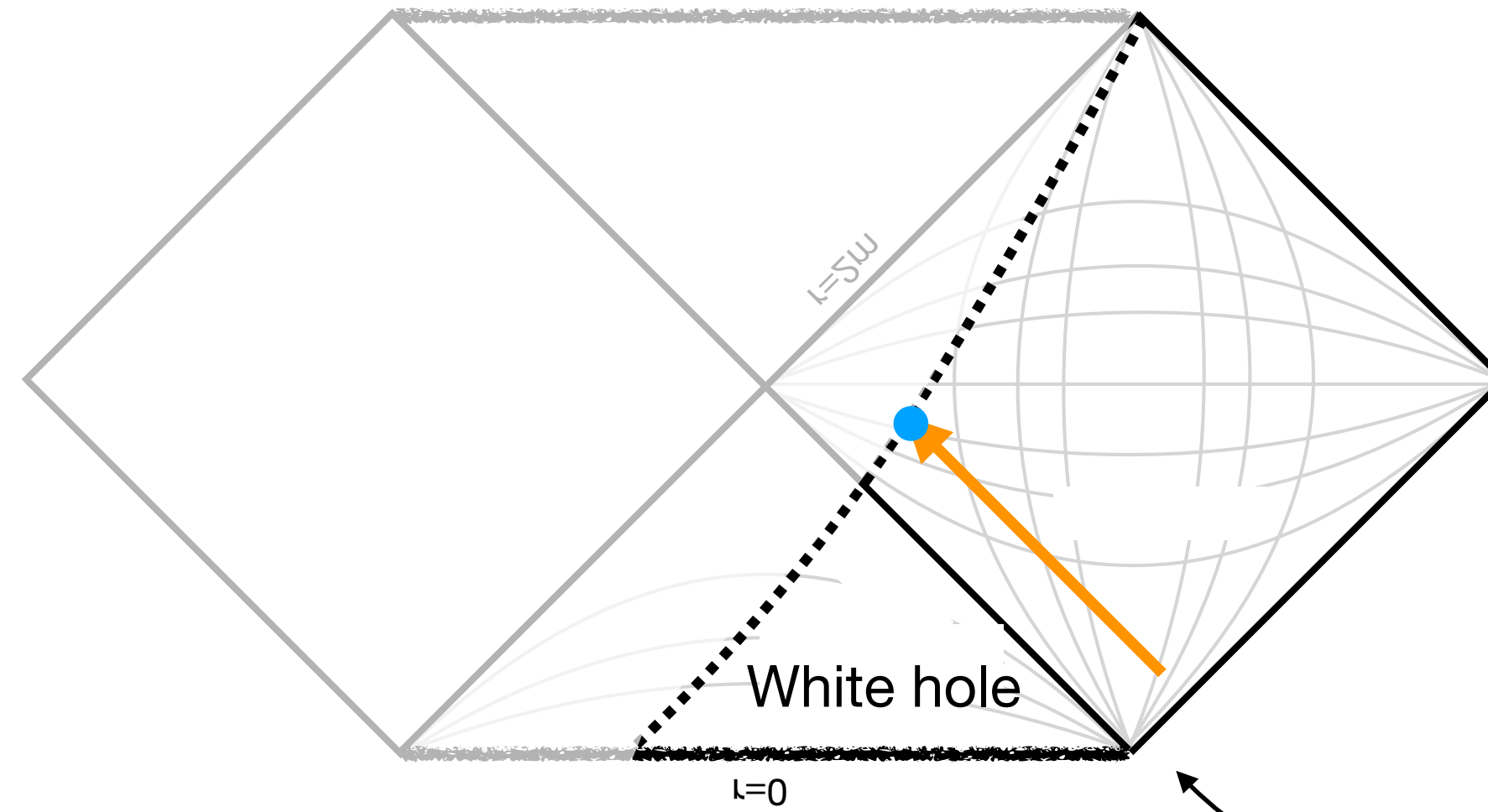
The transition is suppressed for large BH !



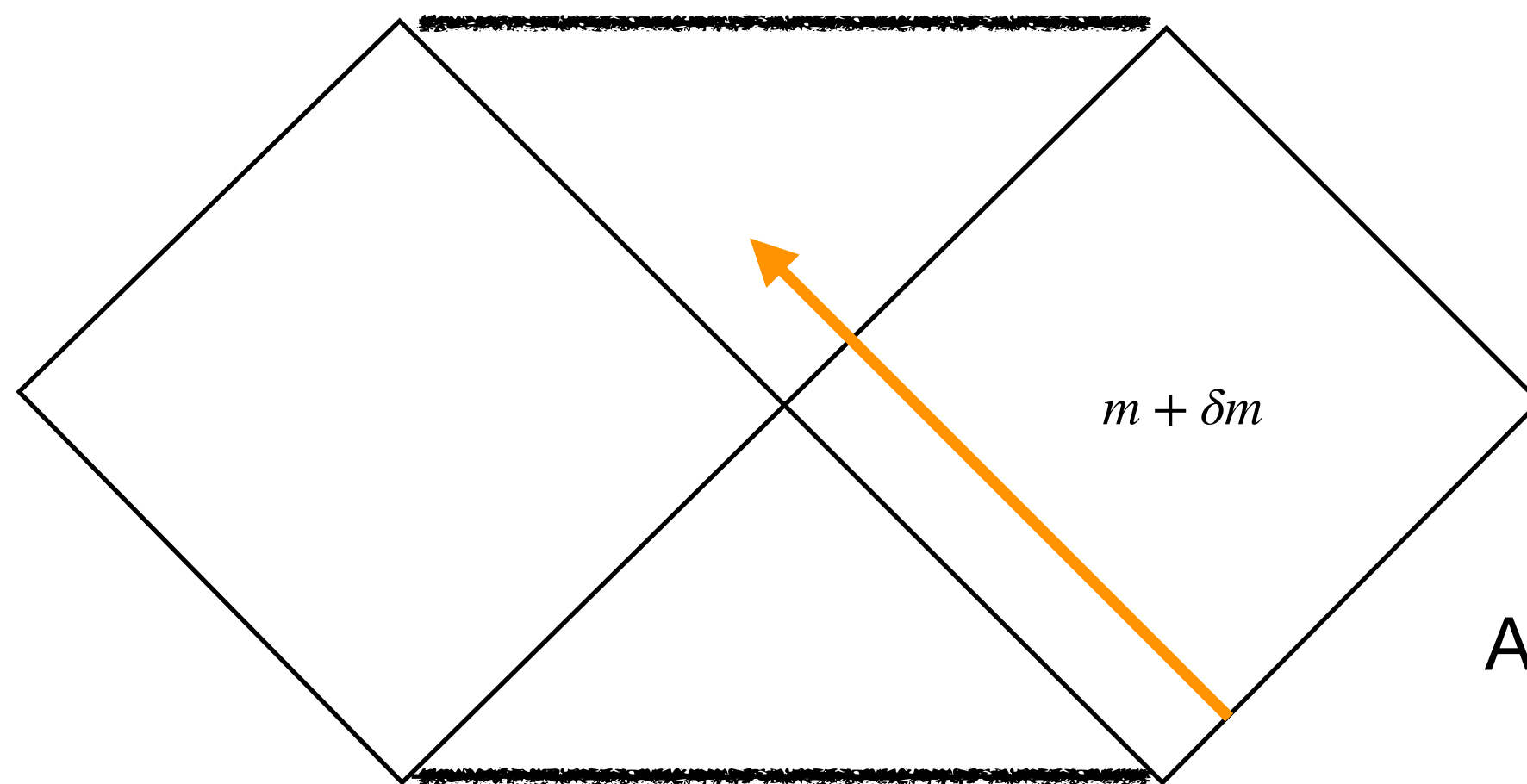
White holes are unstable



The energy pulse cannot be too much in the future

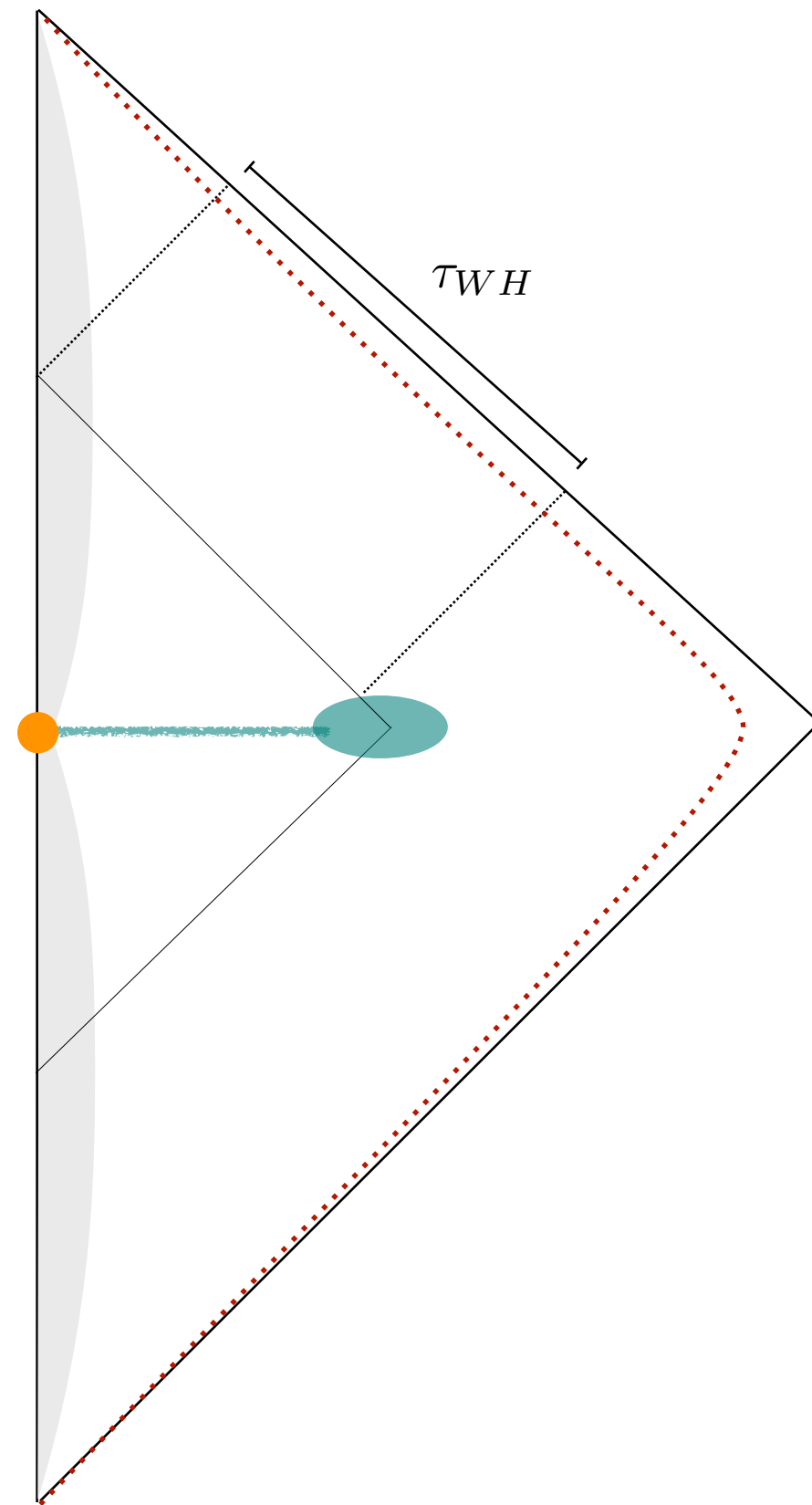


The energy pulse cannot be too much in the past



A white hole is unstable toward becoming a black hole

Are remnants stable?
They are stabilized by quantum gravity



$$|m_o, m\rangle_B \xrightarrow{\text{tunnelling}} |m_o, m\rangle_W$$

$$|m_o, m\rangle_W \xrightarrow{\text{instability}} |m_o, m\rangle_B$$

$$|\psi\rangle = \begin{pmatrix} B(m, v) \\ W(m, v) \end{pmatrix}$$

$$|m_o, m\rangle = \alpha |m_o, m\rangle_W + \beta |m_o, m\rangle_B$$

Area gap = minimum
 non vanishing mass

$$A_{min} = 4 \frac{\sqrt{3}}{\pi} \gamma \hbar G / c^3$$

$$H = \begin{pmatrix} m + 3\sqrt{3} i \pi m_o^2 \frac{\partial}{\partial v} - i \frac{\hbar^2}{m^2} \frac{\partial}{\partial m} & b \frac{\hbar}{m} \\ c \frac{\hbar}{m} e^{-m^2/\hbar} & m - 3\sqrt{3} i \pi m_o^2 \frac{\partial}{\partial v} \end{pmatrix}$$

$$|R\rangle = \frac{\sqrt{\frac{a}{b}} |B, \mu\rangle - |W, \mu\rangle}{\sqrt{1 + \frac{a}{b}}}$$

Vidotto, CR 2018.

Quasi stable
 remnants of
 Mass $\sim 1\mu\text{g}$

Dark matter?

Are remnants stable?
They are stabilized by quantum gravity

Area gap = minimum
non vanishing mass

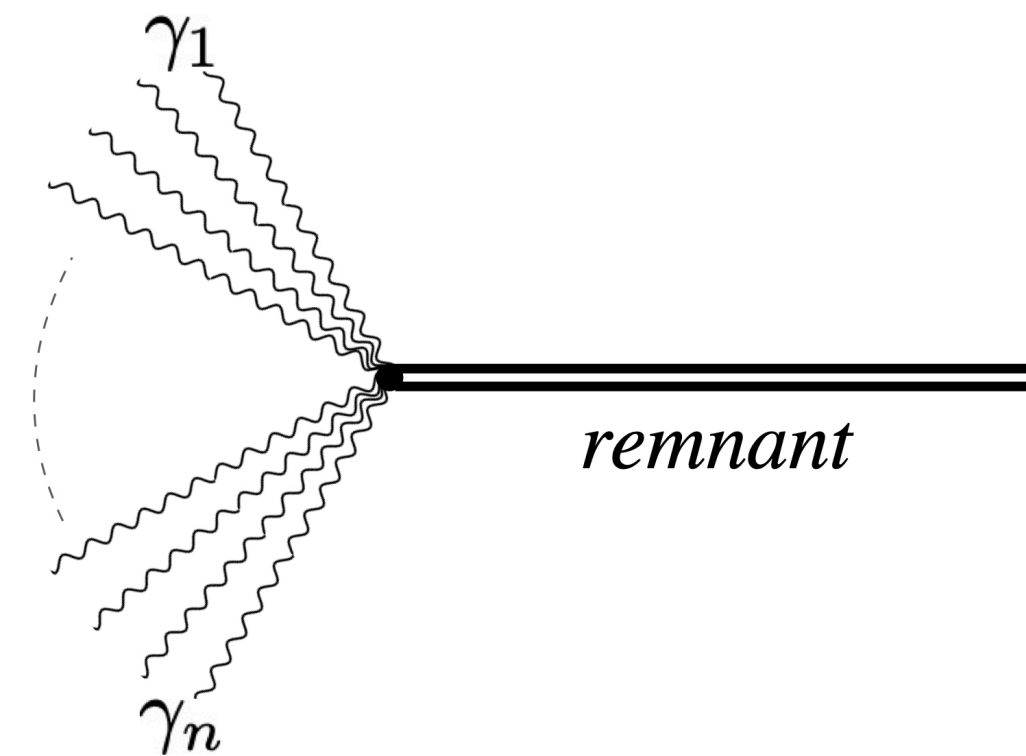
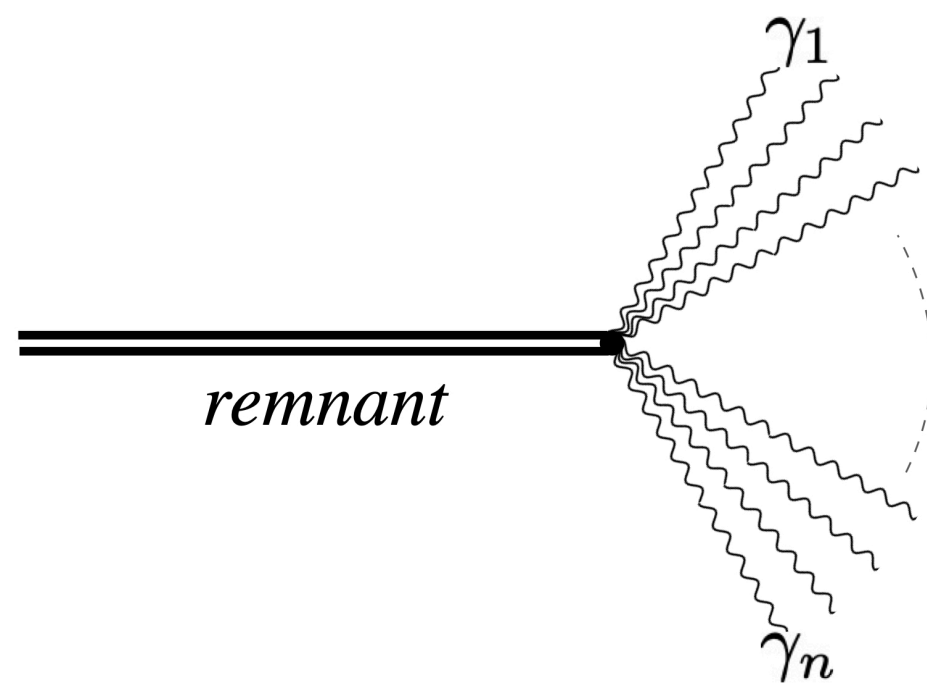
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Quasi stable
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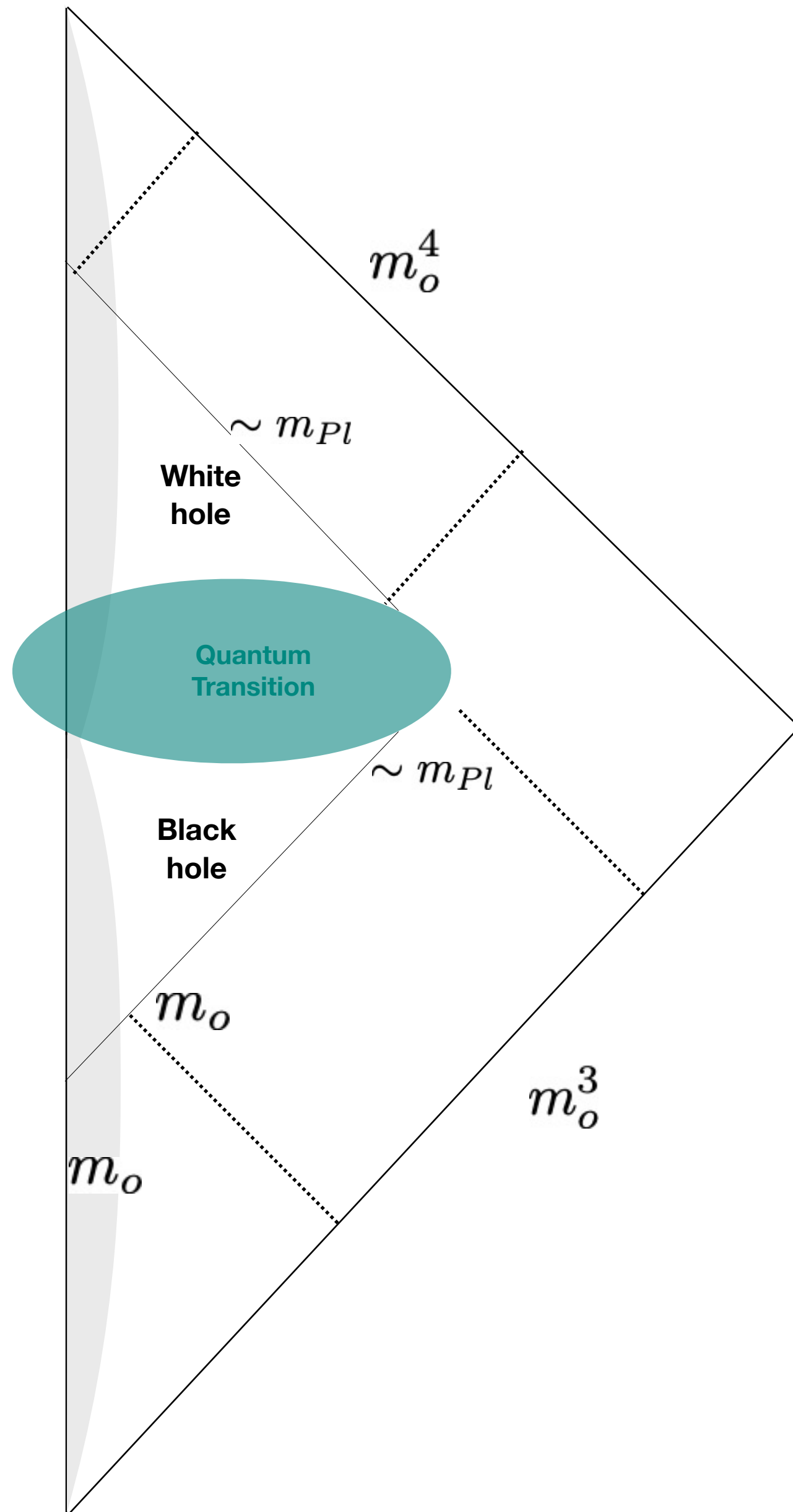
Dark matter?

$$\xrightarrow{\text{collapse}} |m_o, m_o\rangle_B \xrightarrow[\text{black hole}]{\tau_{WH} \sim m_o^3} |m_o, m_{Pl}\rangle_B \xrightarrow[\text{tunnelling}]{\tau_T \sim m_{Pl}} |m_o, m_{Pl}\rangle_W \xrightarrow[\text{white hole}]{\tau_{WH} \sim m_o^4} |m_{Pl}, m_{Pl}\rangle_W \xrightarrow{\text{end}} .$$

$|m_o, m_P\rangle \rightarrow |0\rangle$ suppressed!



This also solve the old problem:
Why WH are not easily produced?



E. Bianchi, M. Christodoulou, F. D'Ambrosio, H. M. Haggard, CR,
 "White holes as remnants: A surprising scenario for the end of a black hole," CQG 2018, arXives: 1802.04264.

$$S \sim \frac{A}{4} = 4\pi m^2$$

$$S = \frac{2\pi}{3} LT, \quad E = \frac{1}{6} LT^2.$$

$$L = \frac{3S^2}{8\pi^2 E} = 6m^4, \quad T = \frac{4\pi E}{S} = \frac{1}{m^2}$$

$$\tau_W \sim 6m^4$$

S. Kazemian, M Pascual, F Vidotto, 2022, arXiv:2207.06978.

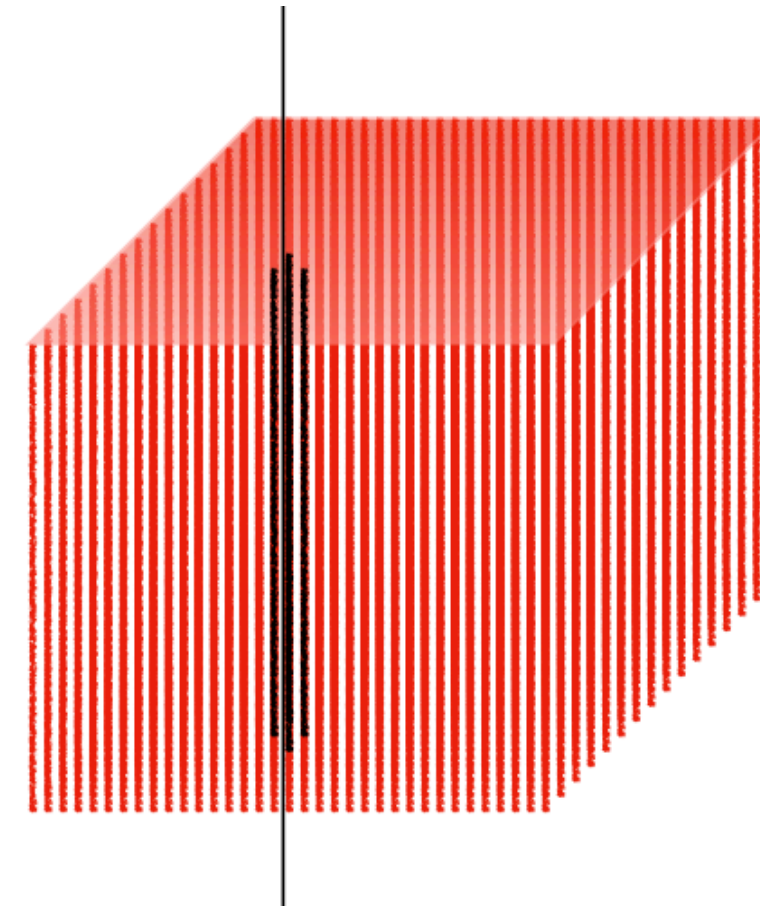
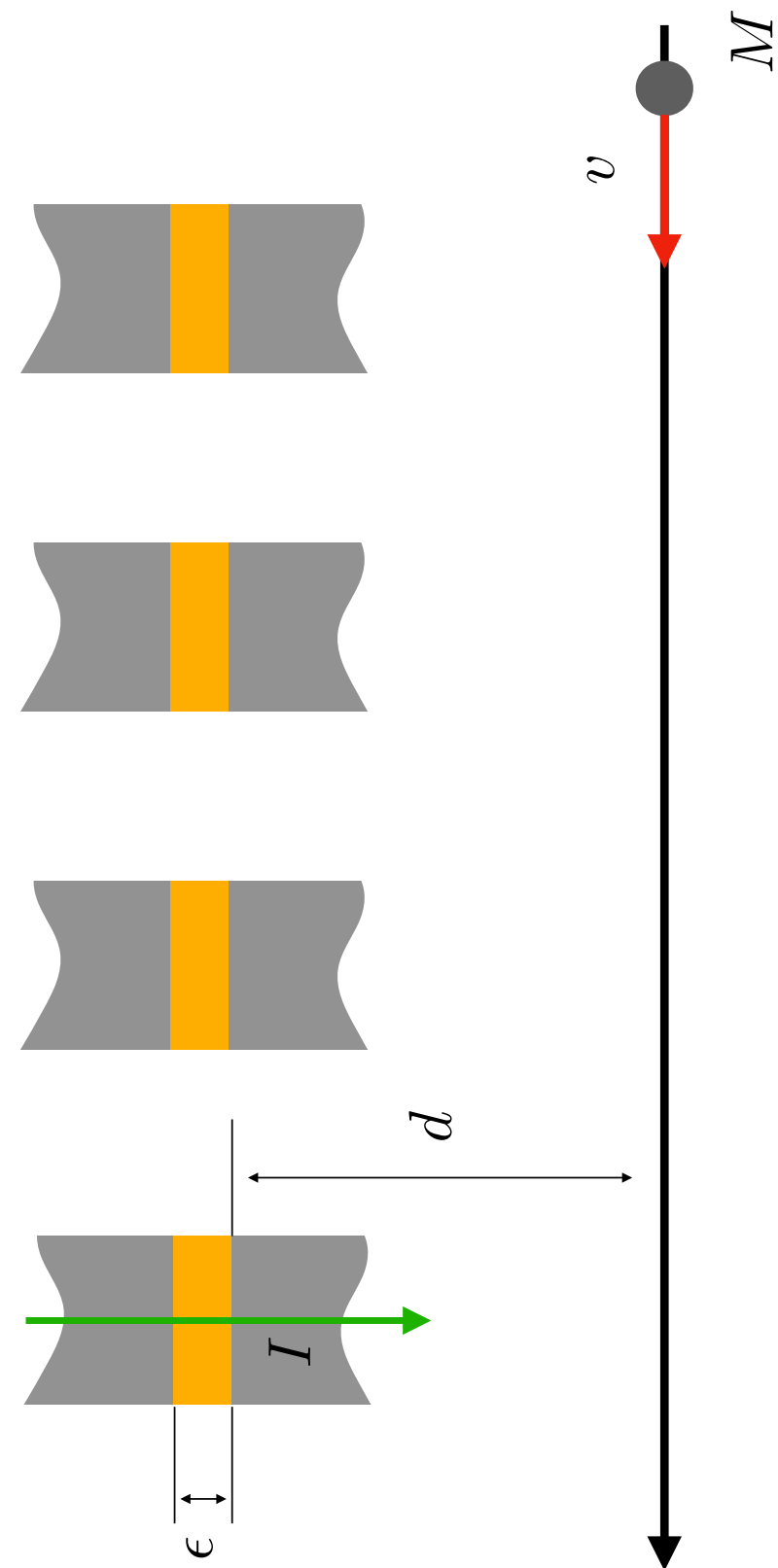
Emission

$$m = 10^{x-5} gr, \quad \nu = 10^{-2x+32} Hz, \quad \rho_{rad} = \sinh \left(\frac{10^{61} - 10^{3x}}{10^{4x} - 10^{3x}} \right) \rho_{rem}$$

$$x = \log_{10}(m/m_{Pl}) \in [15, 20]$$

S. Kazemian, M. Pascual, CR, F. Vidotto, "Diffuse emission from black hole remnants," CQG 2023.

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