



Universiteit Leiden

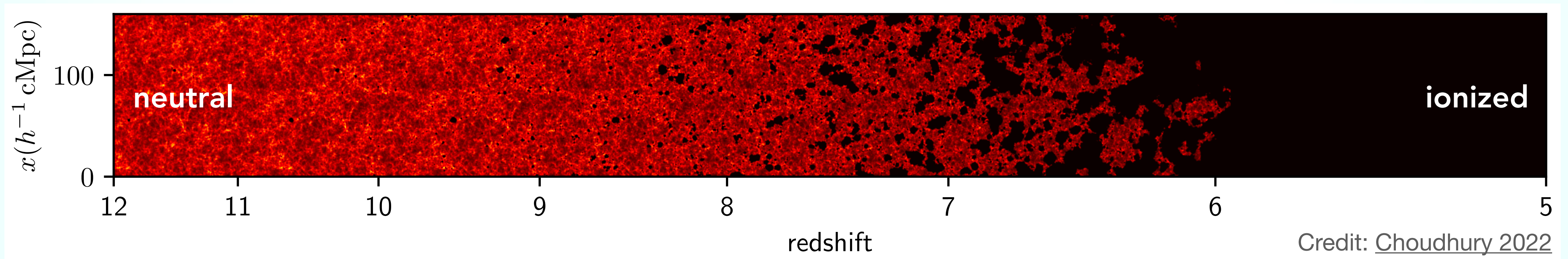


Learning Reionization History with Quasar IGM Damping Wings

Timo Kist, PhD candidate at Leiden Observatory
Supervisor: Joseph F. Hennawi

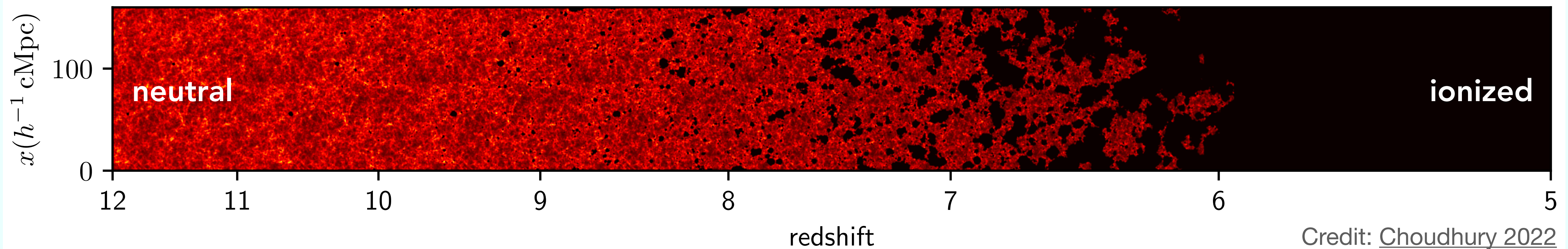
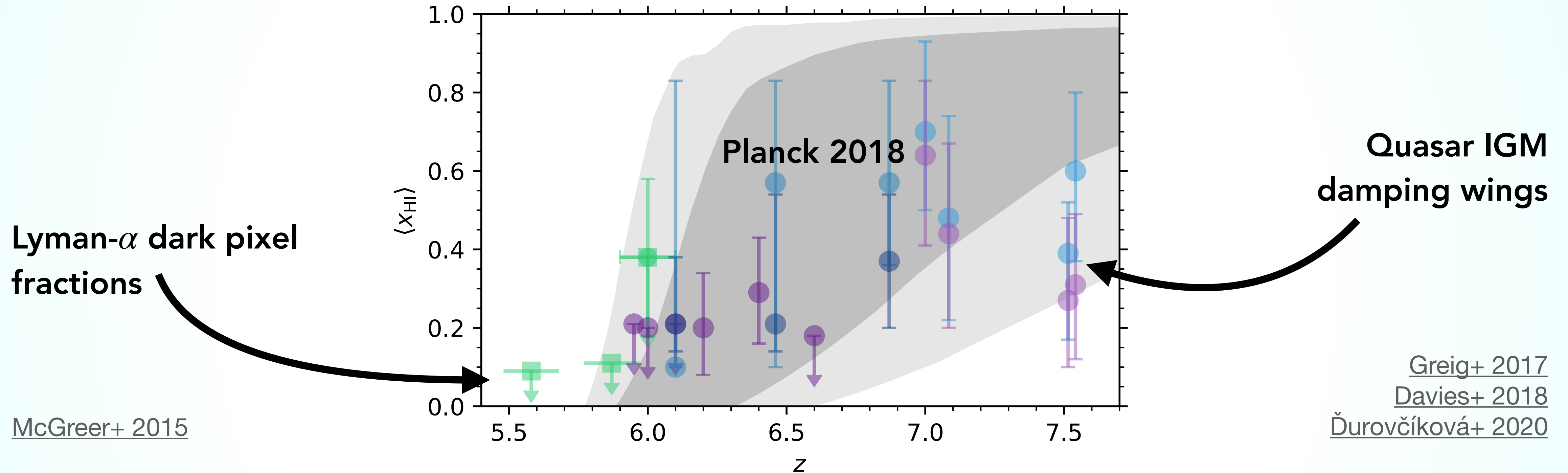
Quasars in a Reionizing Universe

Proximity Zones & IGM Damping Wings



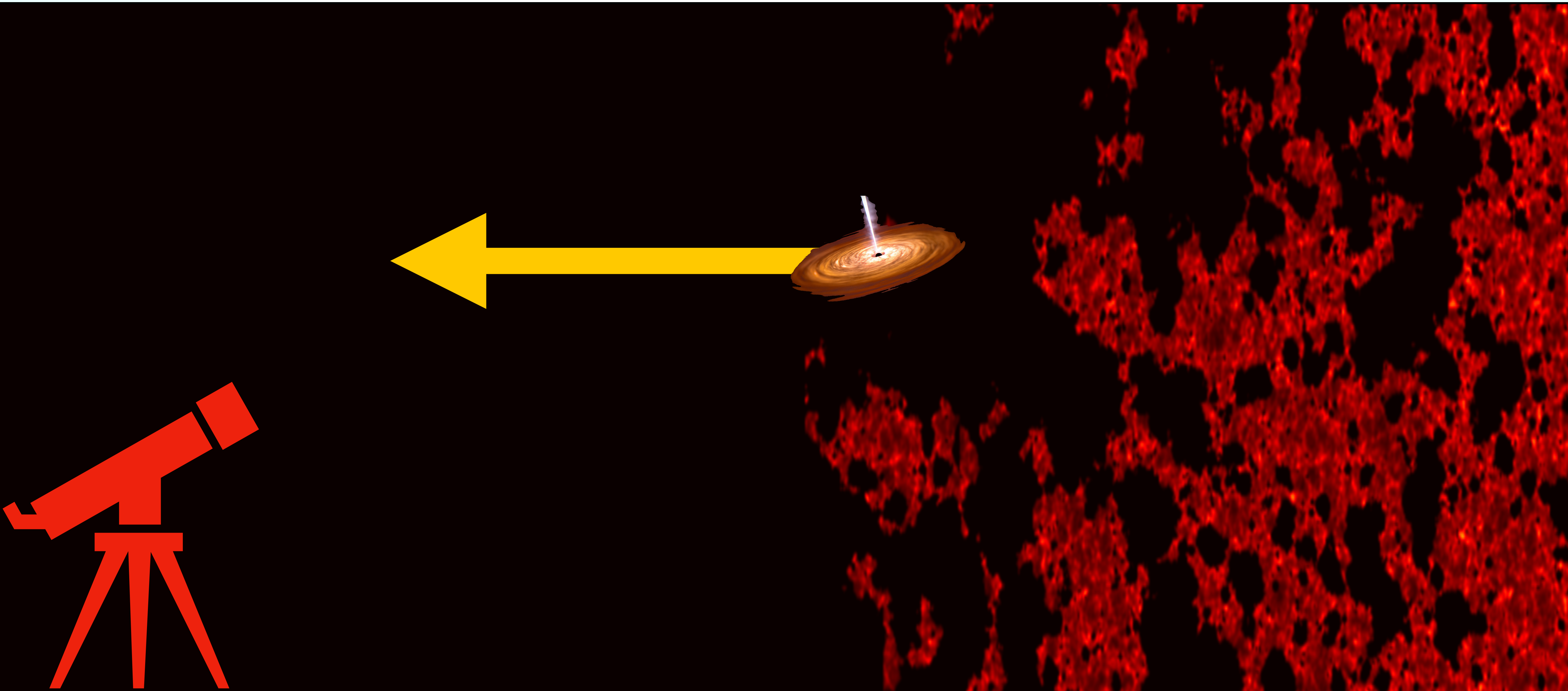
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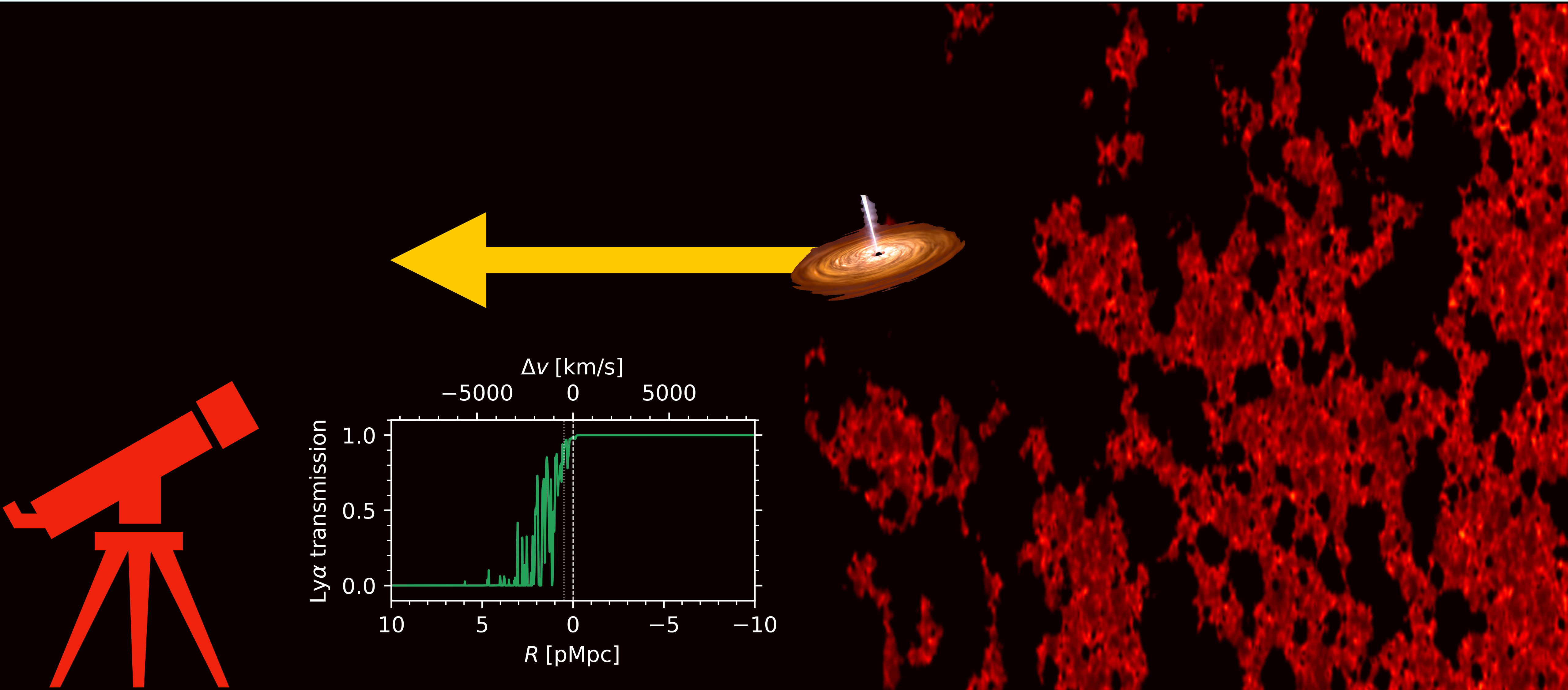
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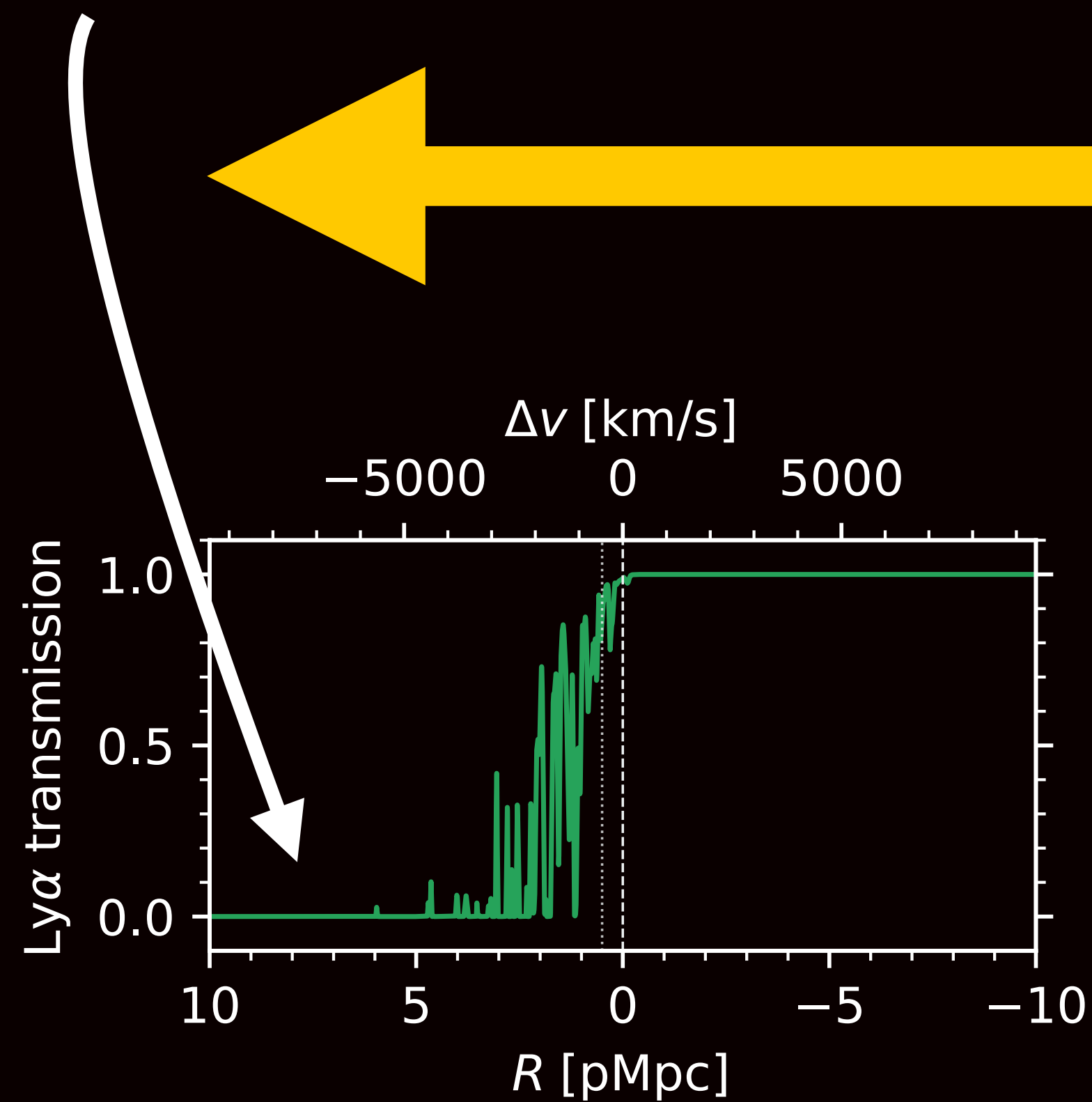


Quasars in a Reionizing Universe

Proximity Zones & IGM Damping Wings

Gunn-Peterson trough:

Complete absorption in the Ly- α forest region starting at IGM neutral fractions $\langle x_{\text{HI}} \rangle \gtrsim 10^{-4}$

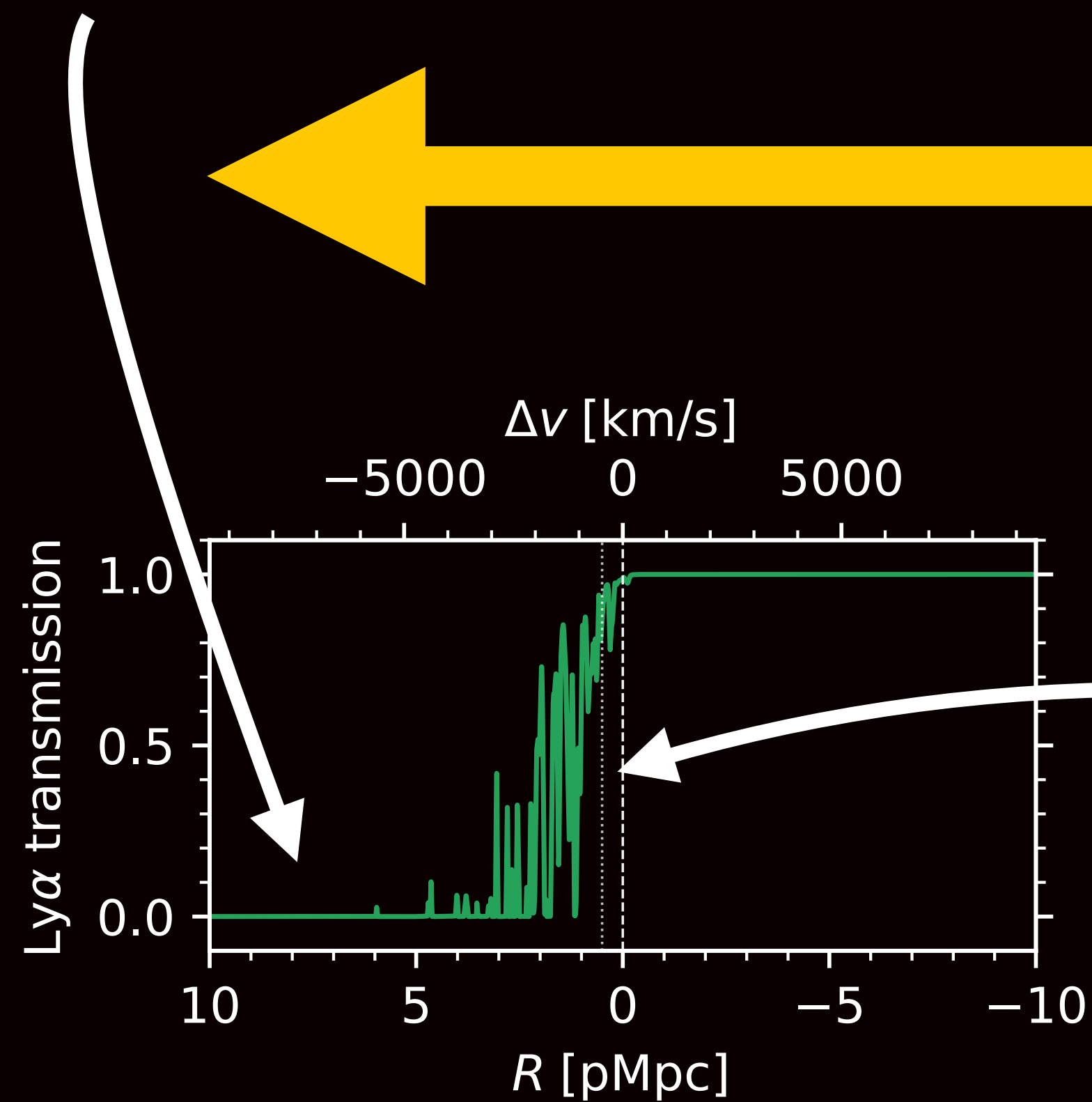


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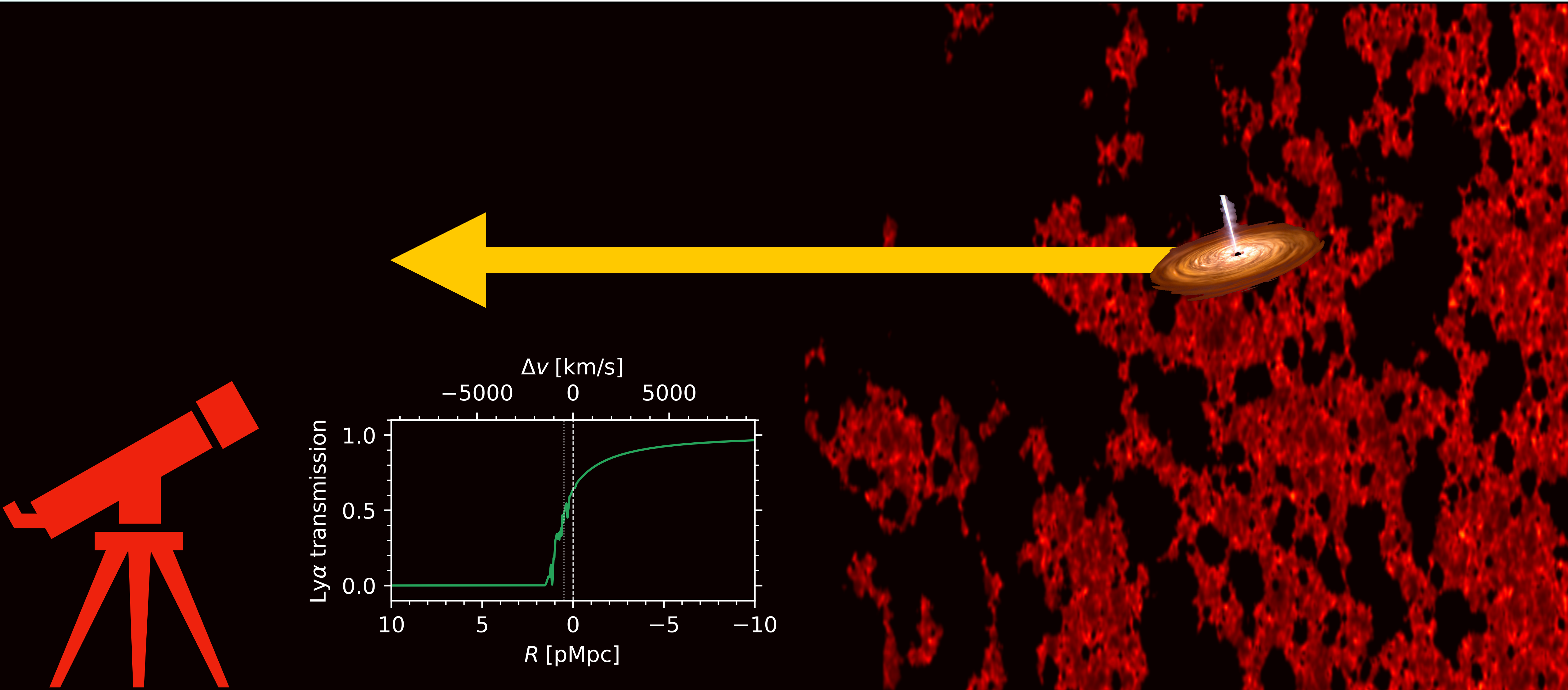


Quasar proximity zone:

The quasar carves out an ionized bubble whose size depends on its lifetime

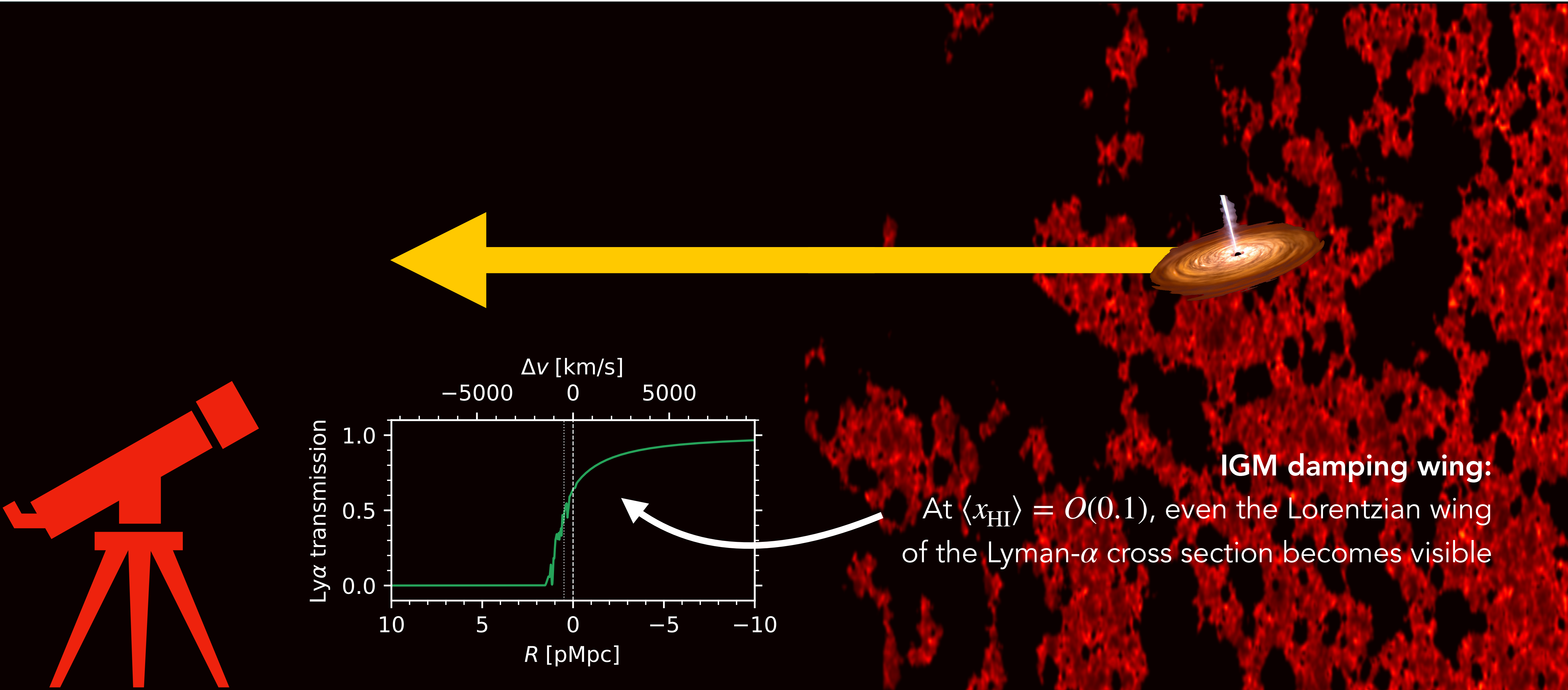
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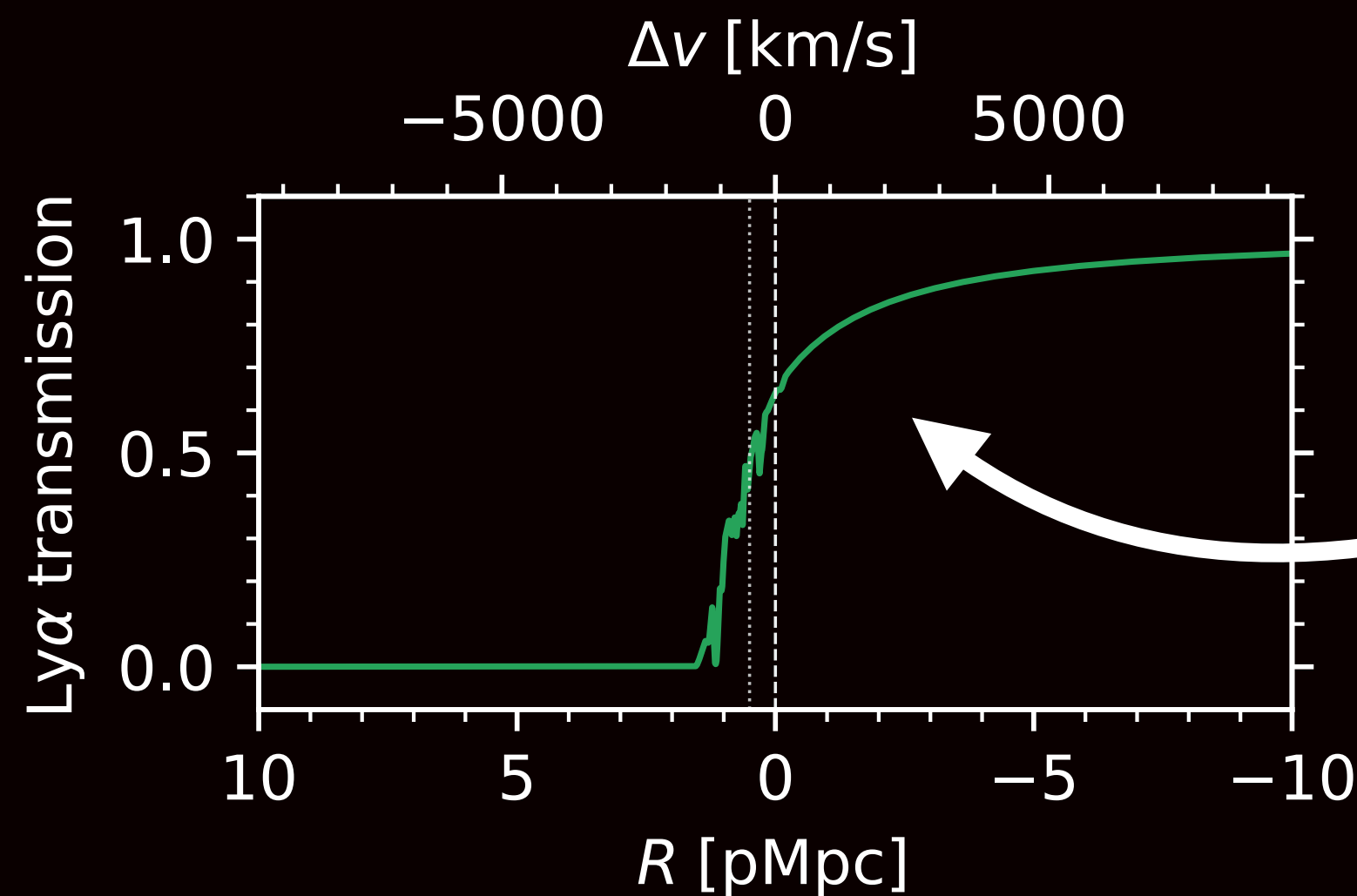
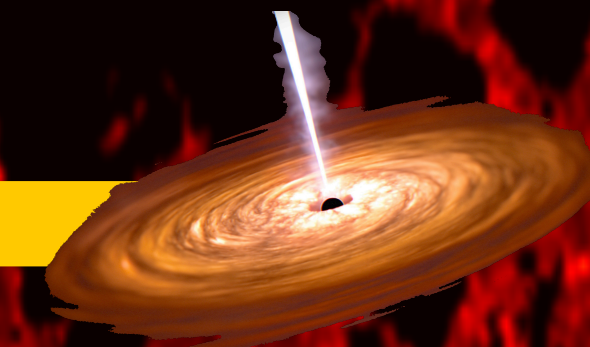
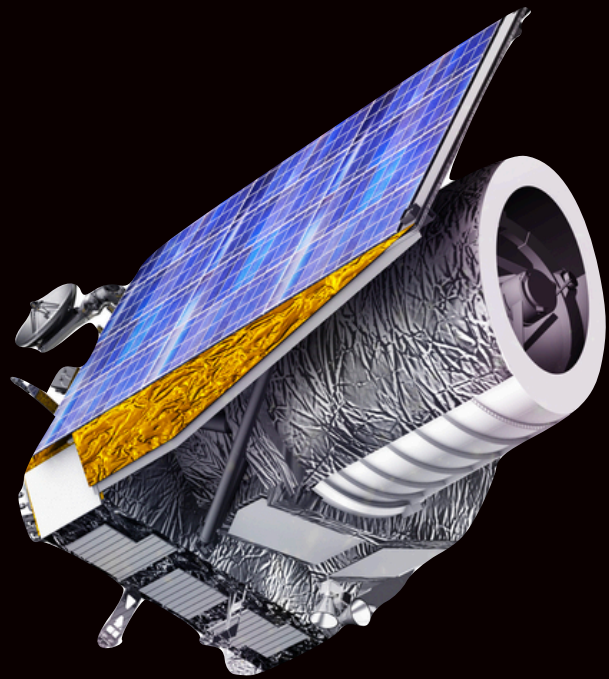
Proximity Zones & IGM Damping Wings



Quasars in a Reionizing Universe

Proximity Zones & IGM Damping Wings

Euclid will find
hundreds of QSOs at $z > 6$



IGM damping wing:
At $\langle x_{\text{HI}} \rangle = O(0.1)$, even the Lorentzian wing of the Lyman- α cross section becomes visible

Forward-Modelling Damping Wing Absorption

Constructing realistic skewers based on cosmological simulations

Nyx hydrodynamical simulations:

1200 density and temperature skewers around the most massive DM halos

21cmFast:

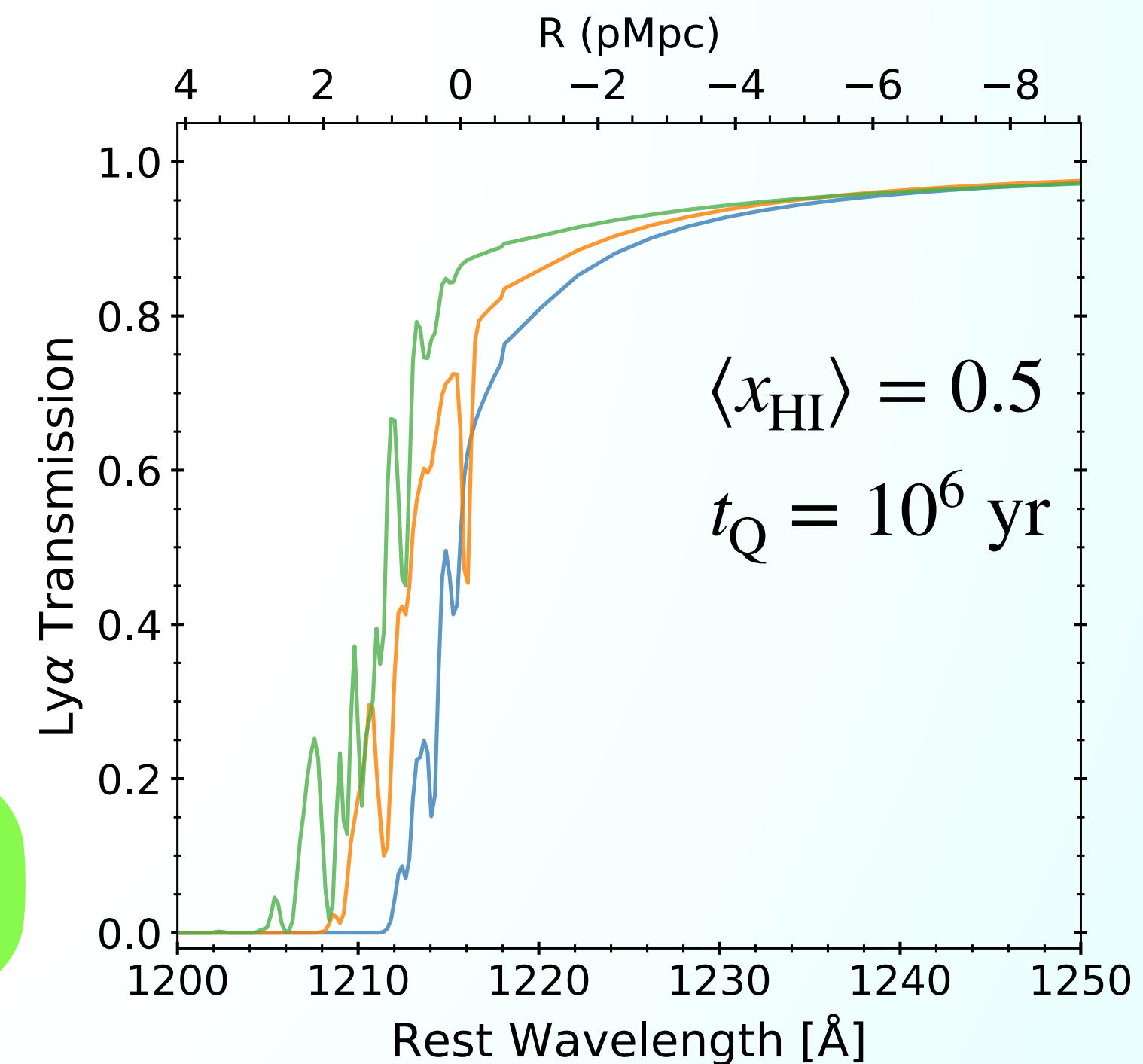
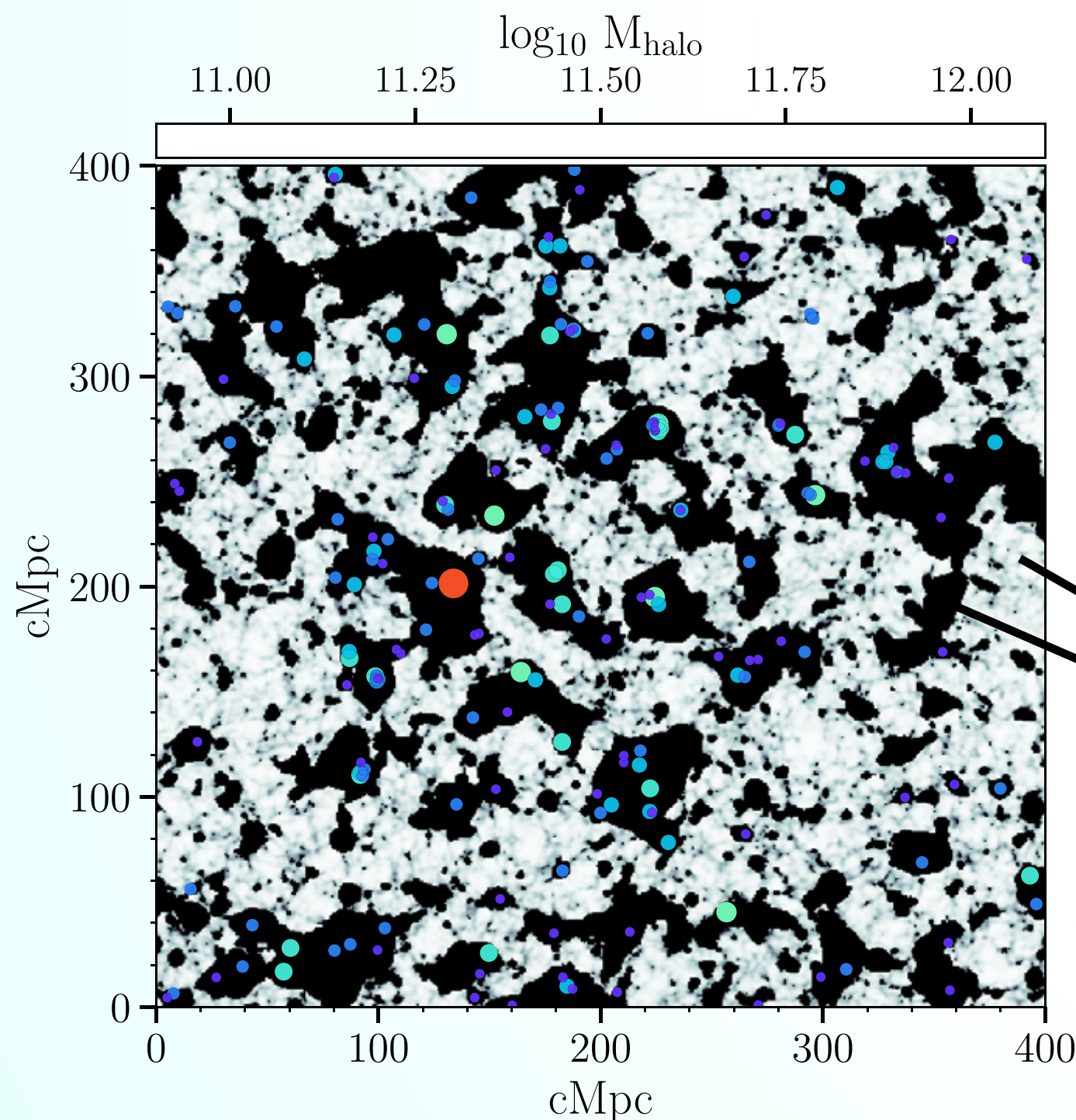
21 reionization topologies ($0 \leq \langle x_{\text{HI}} \rangle \leq 1$) with 10 000 x_{HI} skewers each

1D Radiative Transfer

51 quasar lifetimes between $10^3 \text{ yr} \leq t_Q \leq 10^8 \text{ yr}$

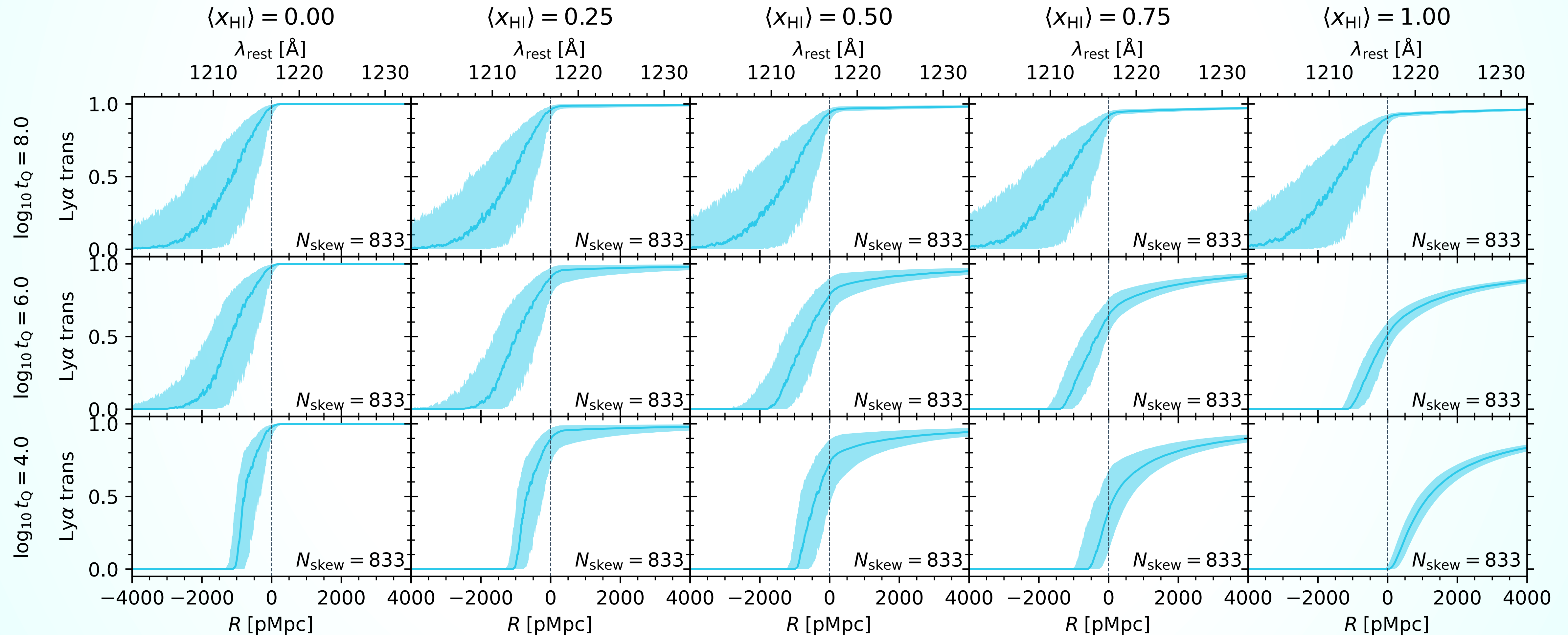
white: neutral
black: ionized

1200 x 21 x 51 grid of Ly- α transmission skewers



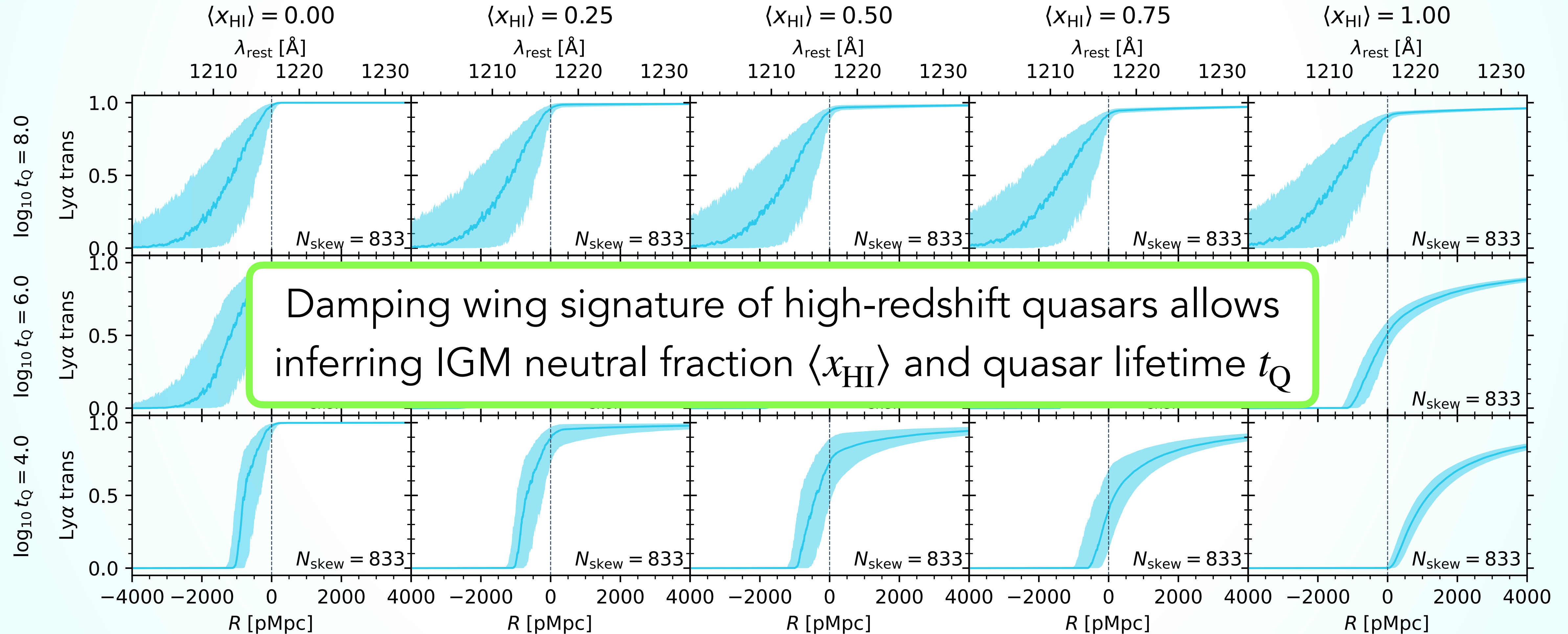
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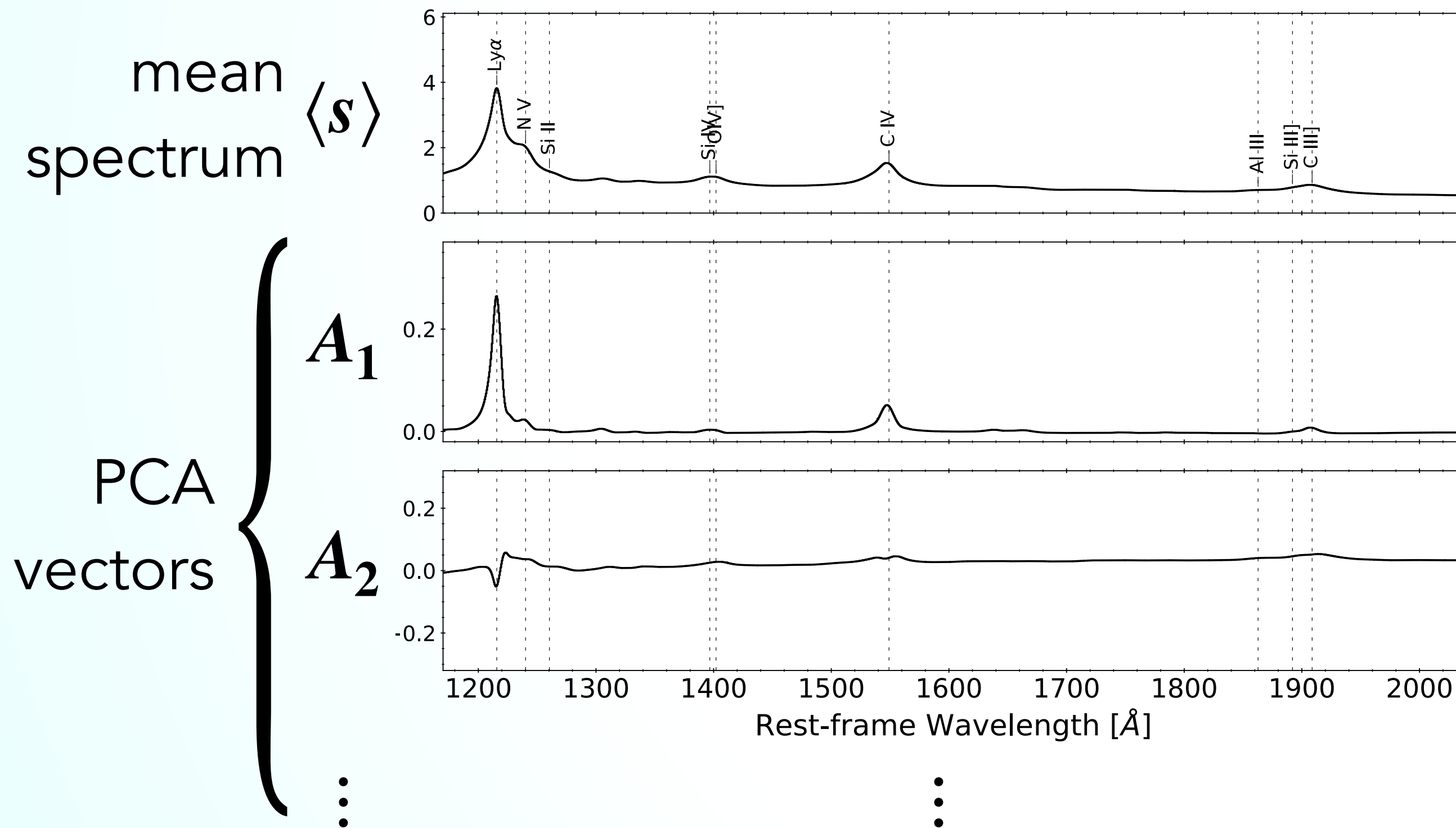


Predicting the Quasar Continuum

A low-redshift PCA model

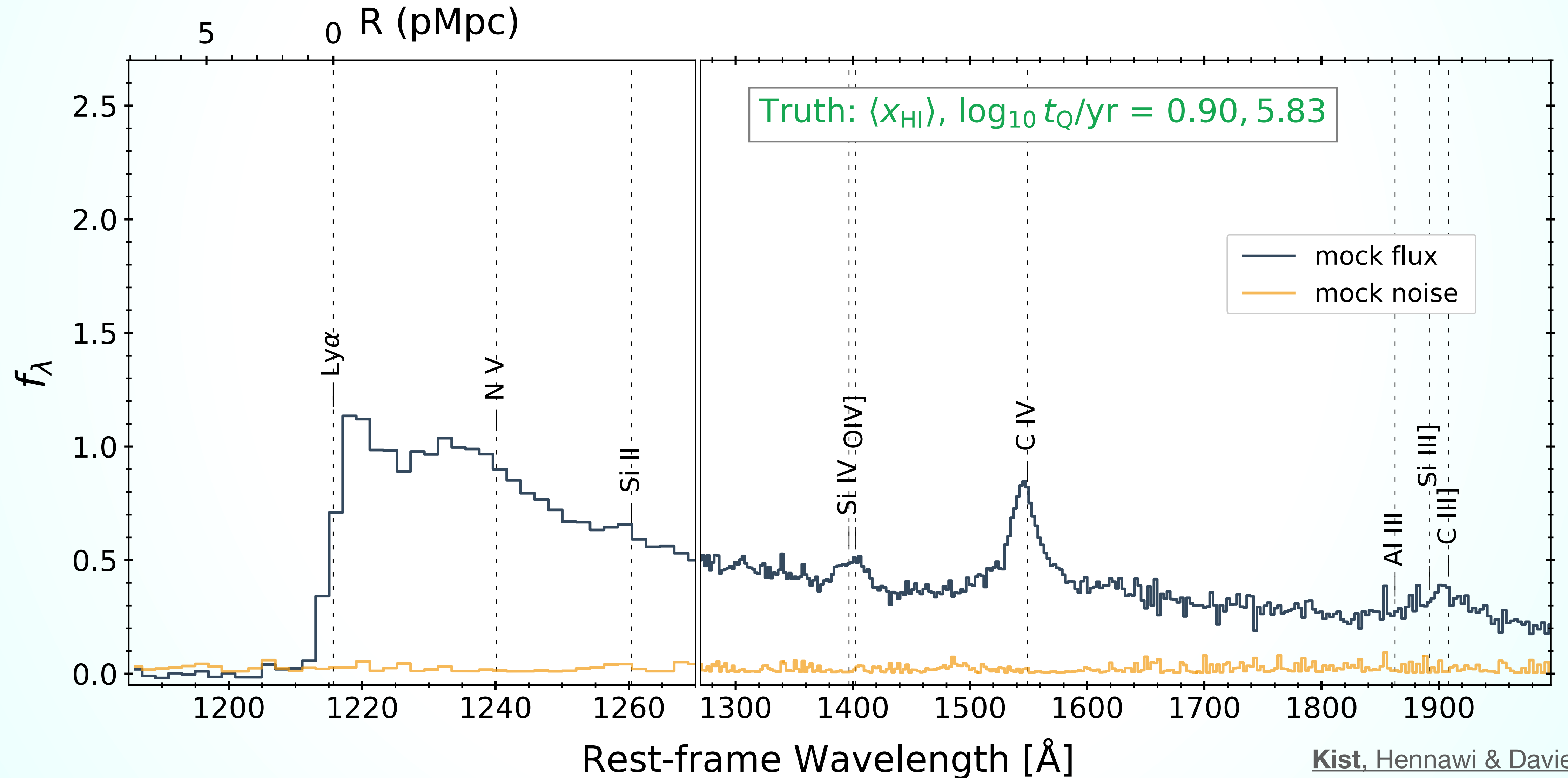
PCA decomposed continuum: $s_{\text{DR}}(\xi) = \langle s \rangle + \xi \cdot A$

- 15 559 SDSS-autofit spectra ($2.149 < z < 4$, $R \sim 2000$, $S/N > 10$)
- 95% - 5% training-test split:
 - Training set of 14 781 low-redshift spectra to build PCA model
 - Test set of 778 spectra to draw mock continua and estimate reconstruction error



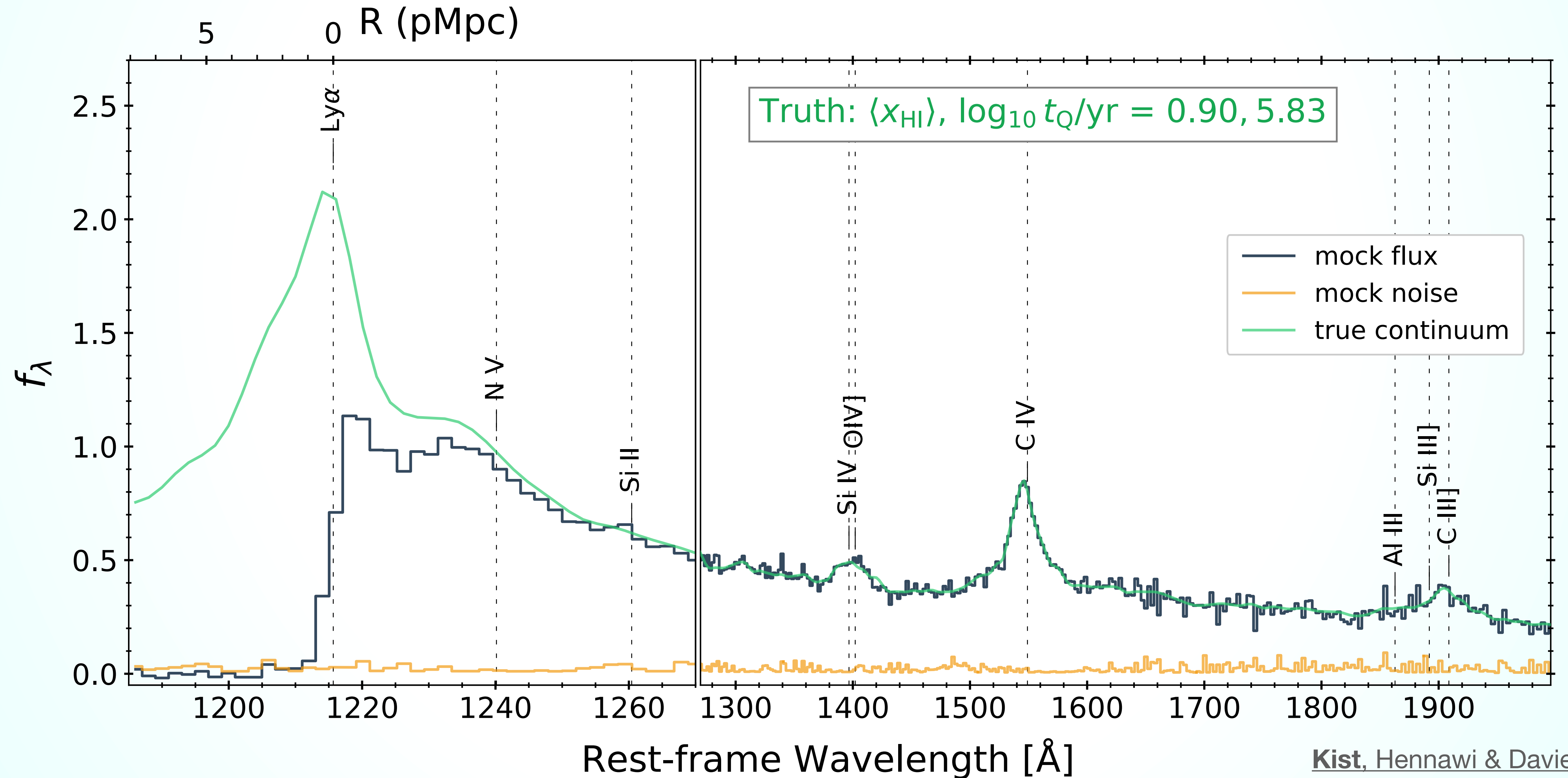
From an Observed Quasar Spectrum to $\langle x_{\text{HI}} \rangle$

A Quasar in a Neutral Environment



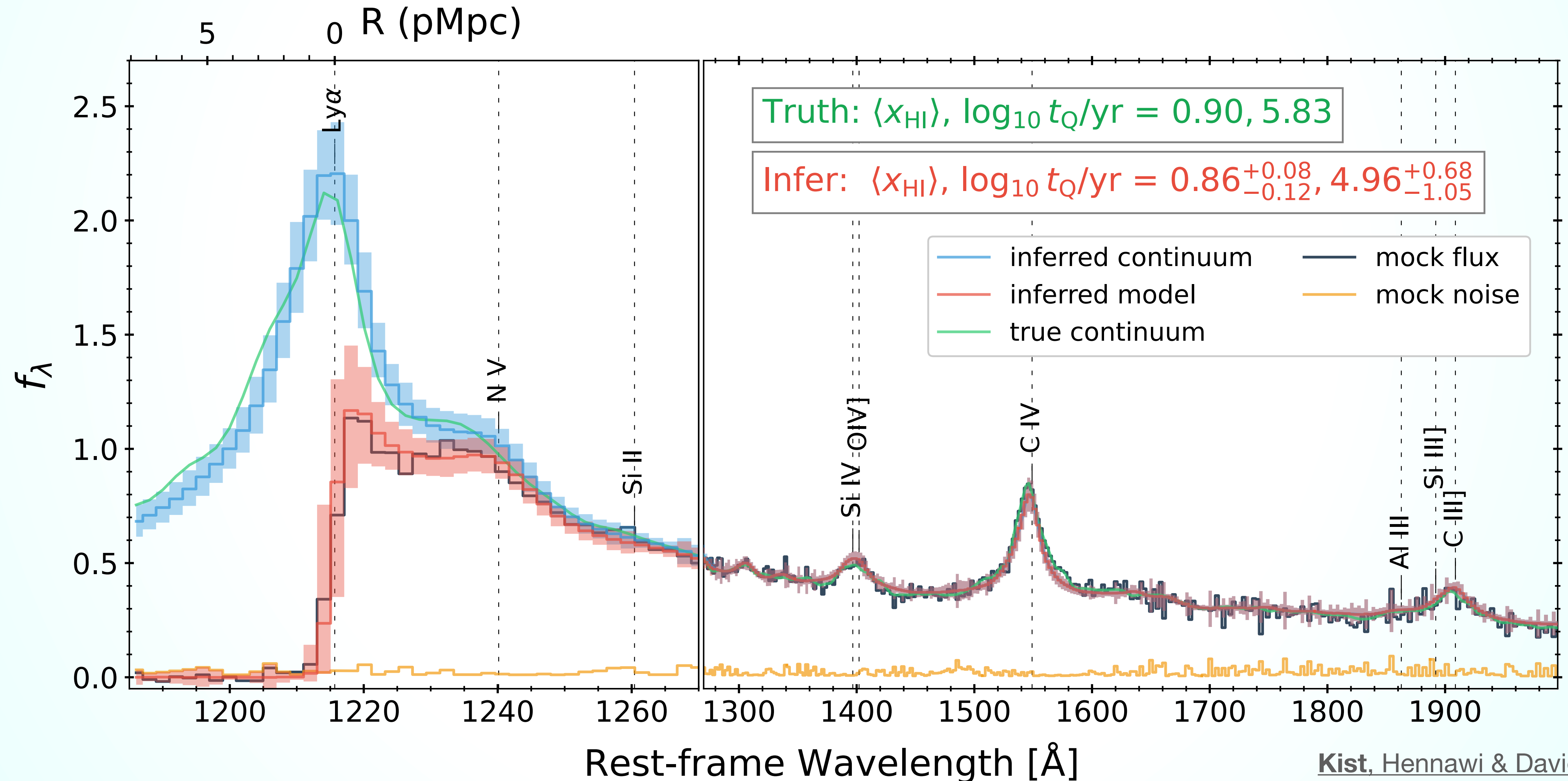
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From an Observed Quasar Spectrum to $\langle x_{\text{HI}} \rangle$

HMC Inference Pipeline

DATA

Real (or mock) quasar spectrum
with observational noise

MODEL

Quasar
continuum
model

Reconstruction
error stochastic
process

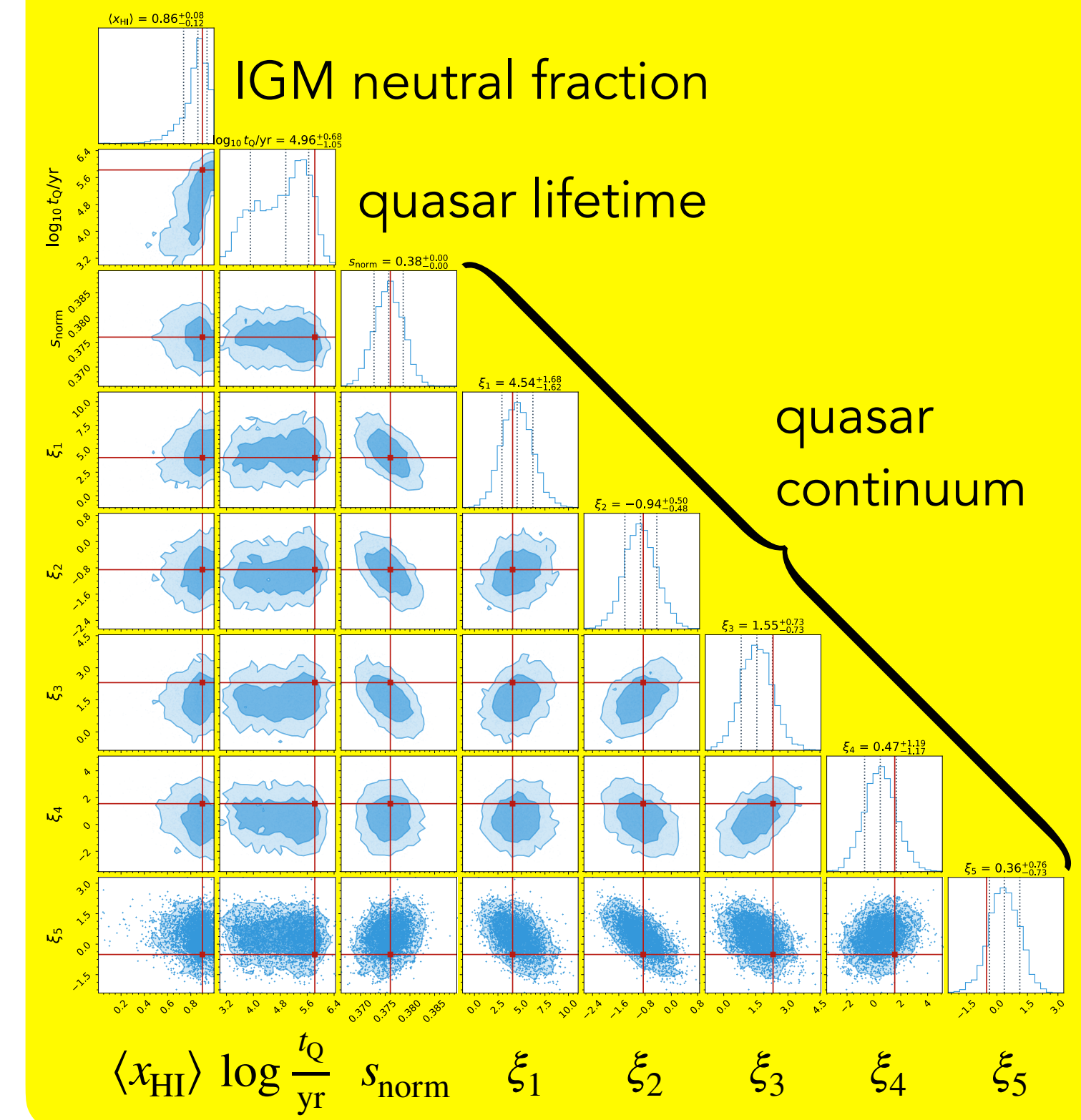
+

IGM transmission field
stochastic process

BAYESIAN INFERENCE
with a Gaussian likelihood approximation

- **Jointly** fitting the quasar continuum & IGM damping wing
- Likelihood operates on the **entire** spectrum (red- and blueward of Lyman- α)
- **Fast** GPU-accelerated JAX-based Hamiltonian Monte Carlo implementation (runtimes ~ 15 min)

POSTERIOR



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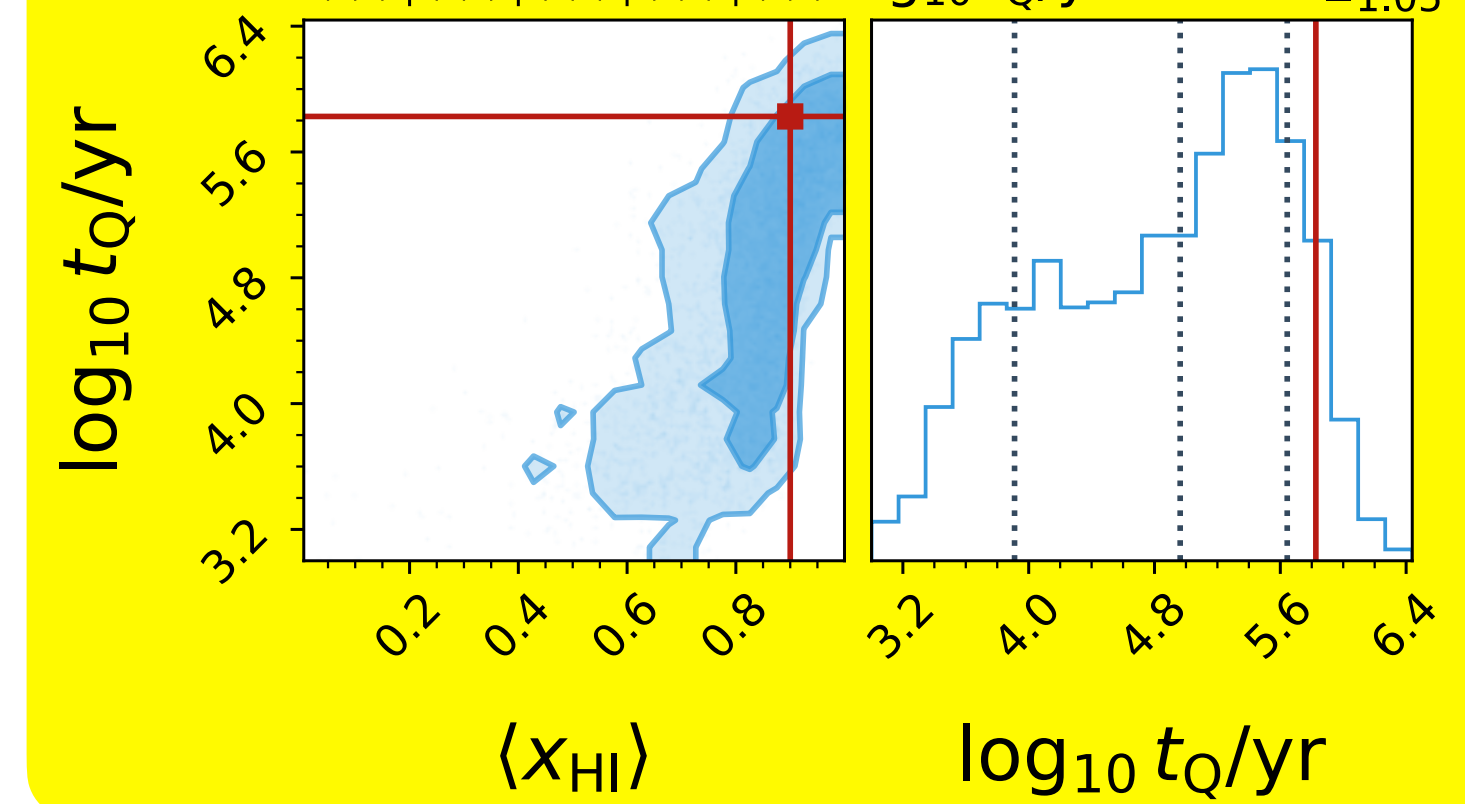
POSTERIOR

IGM neutral fraction

$$\langle x_{\text{HI}} \rangle = 0.86^{+0.08}_{-0.12}$$

quasar lifetime

$$\log_{10} t_{\text{Q}}/\text{yr} = 4.96^{+0.68}_{-1.05}$$



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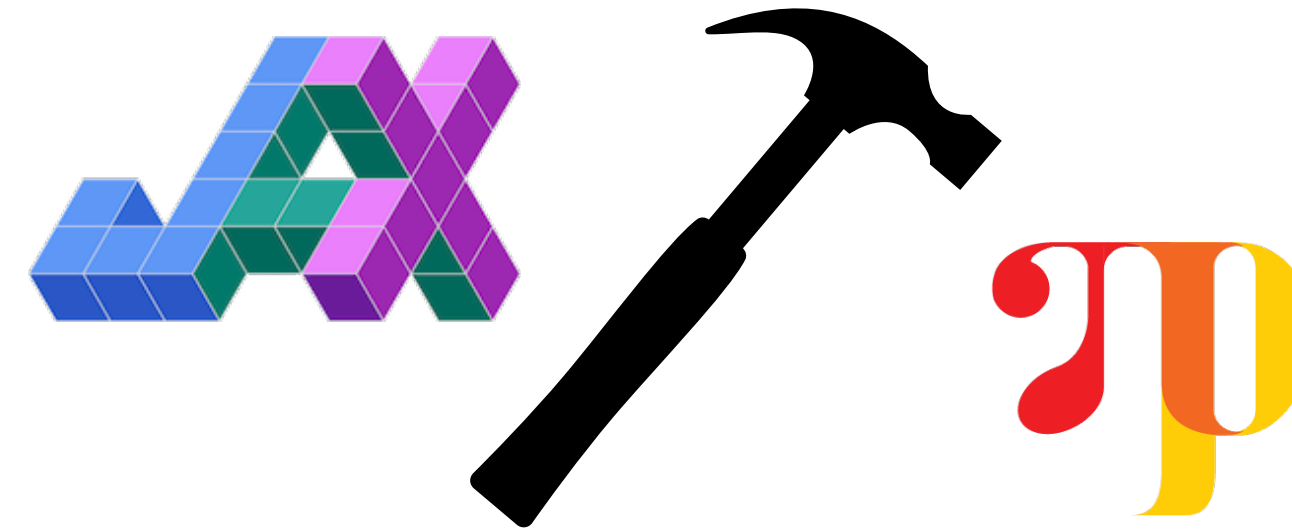
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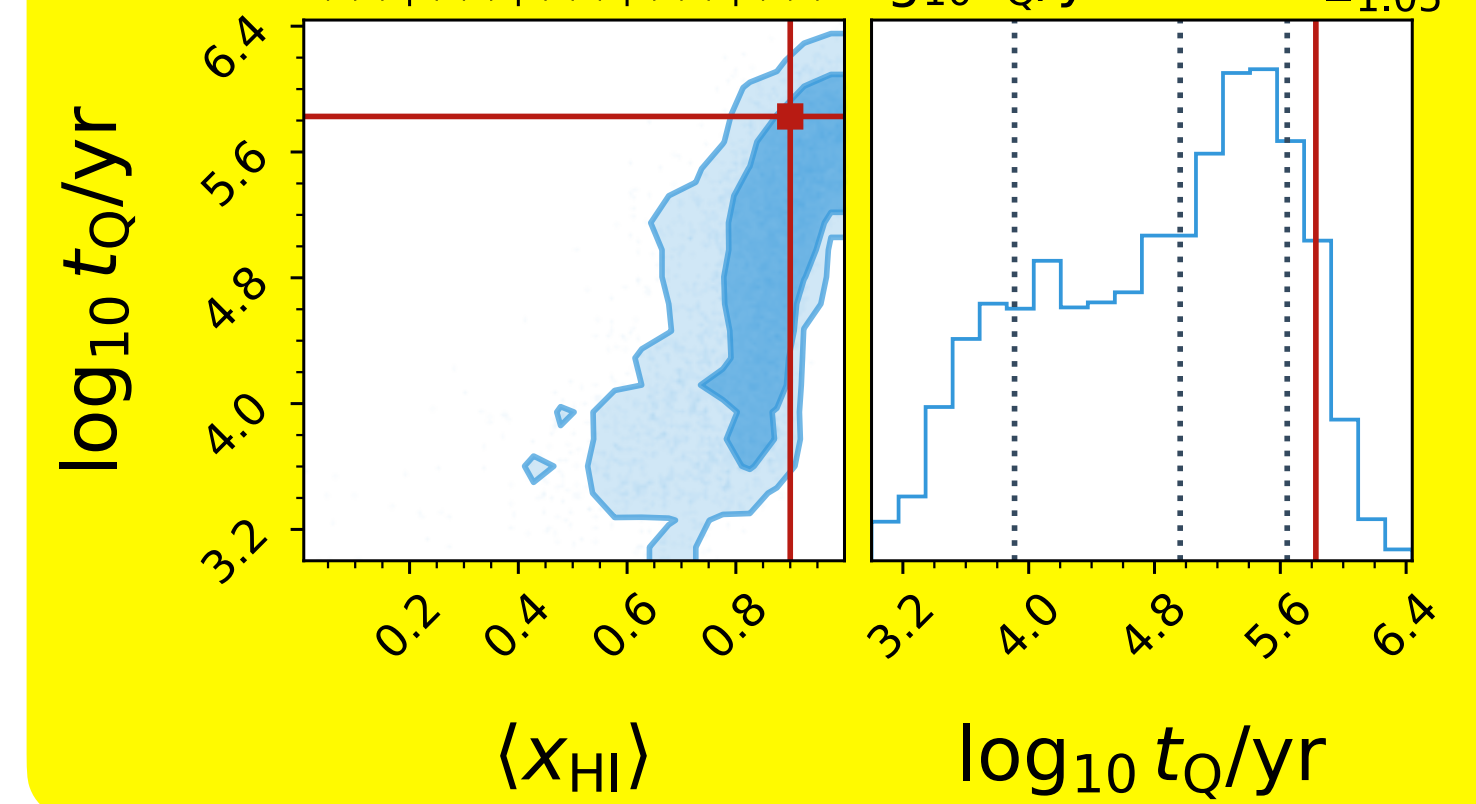
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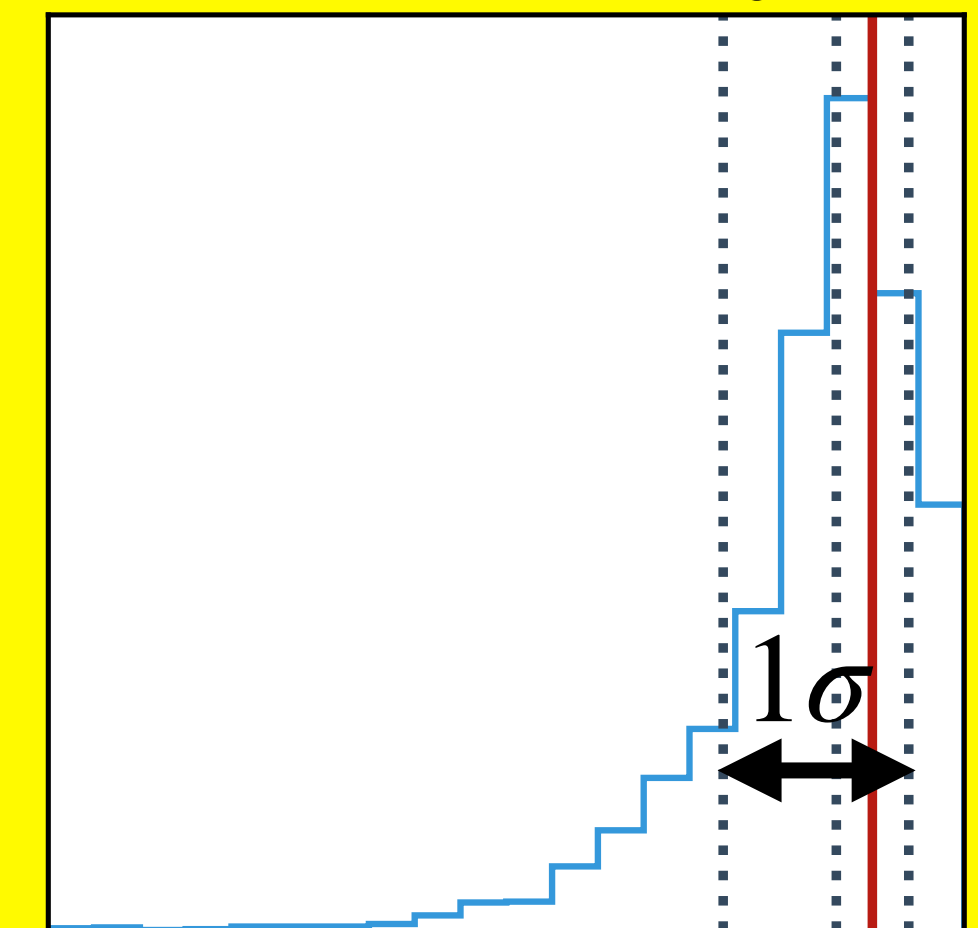
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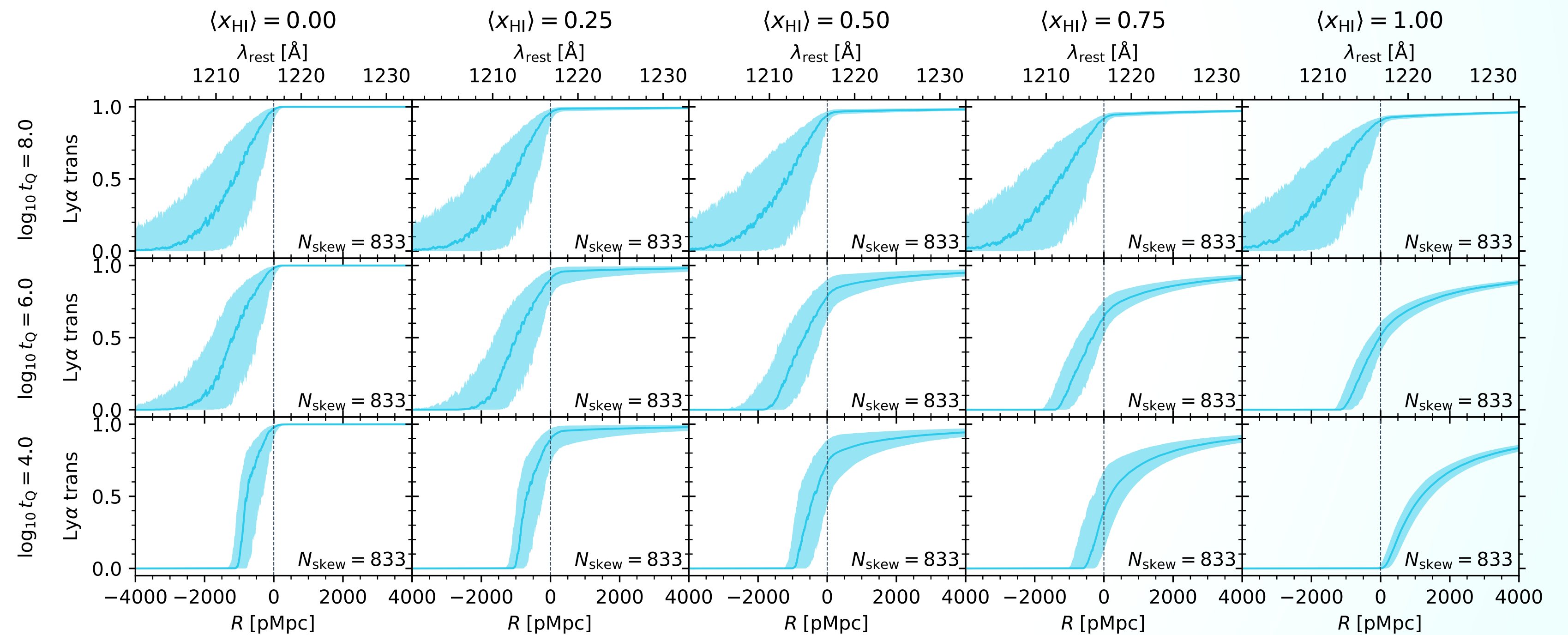
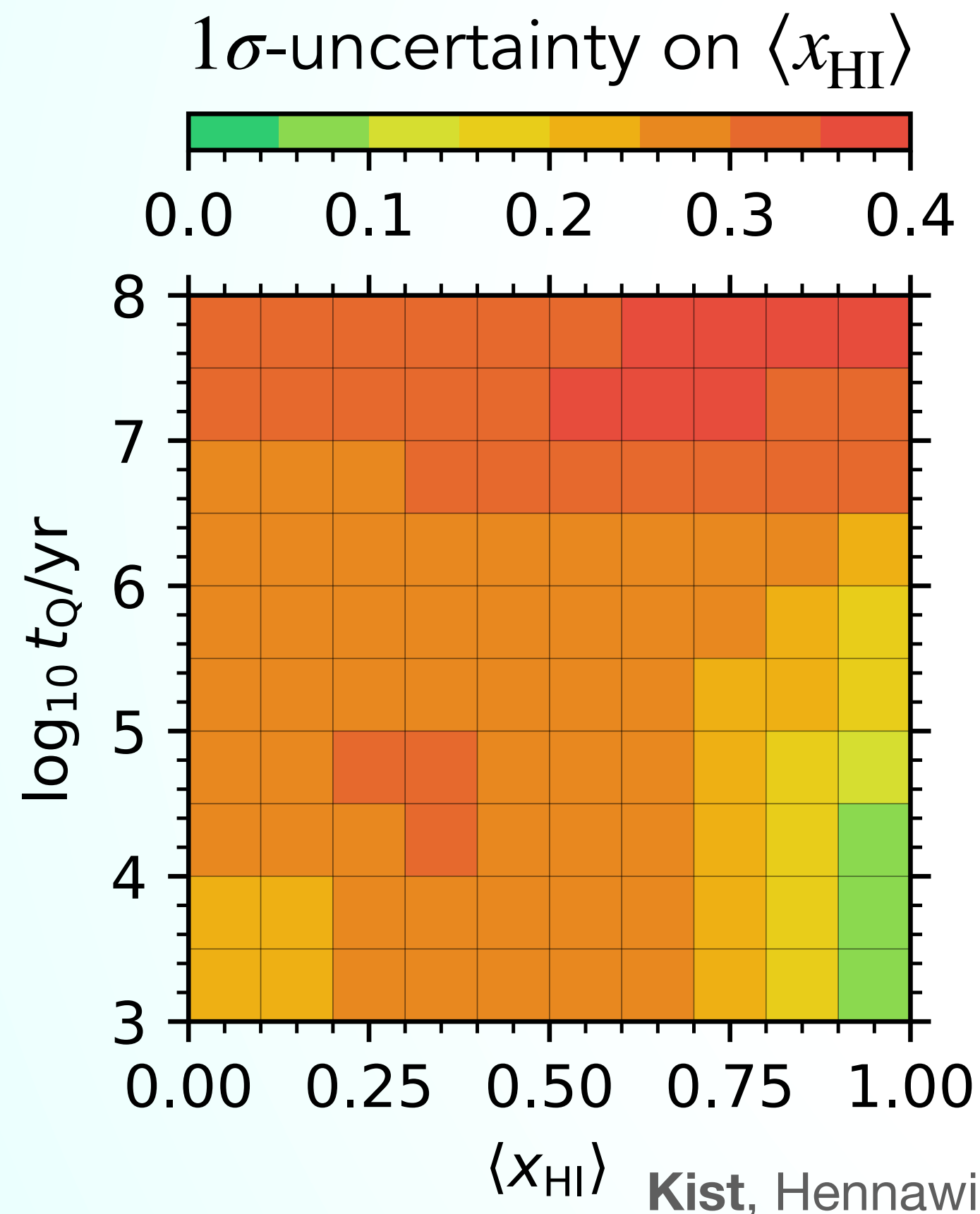


0.2 0.4 0.6 0.8

$\langle x_{\text{HI}} \rangle$

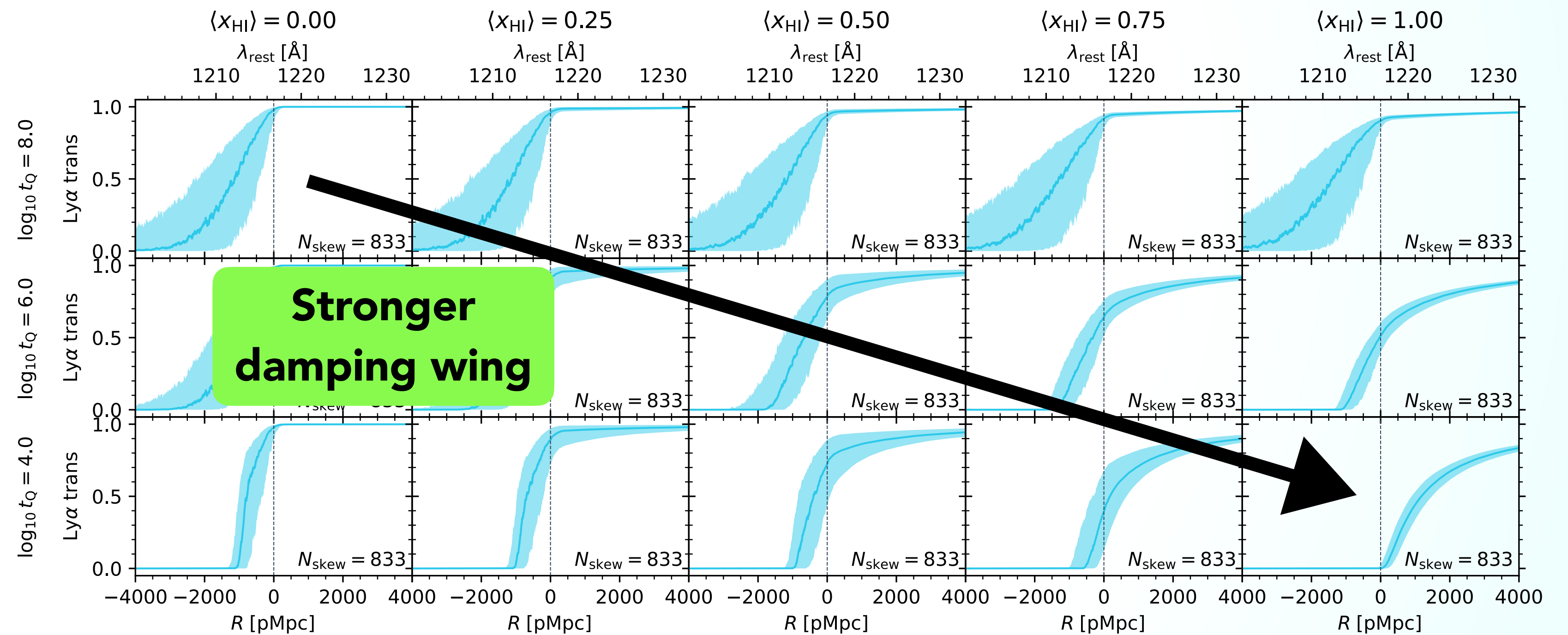
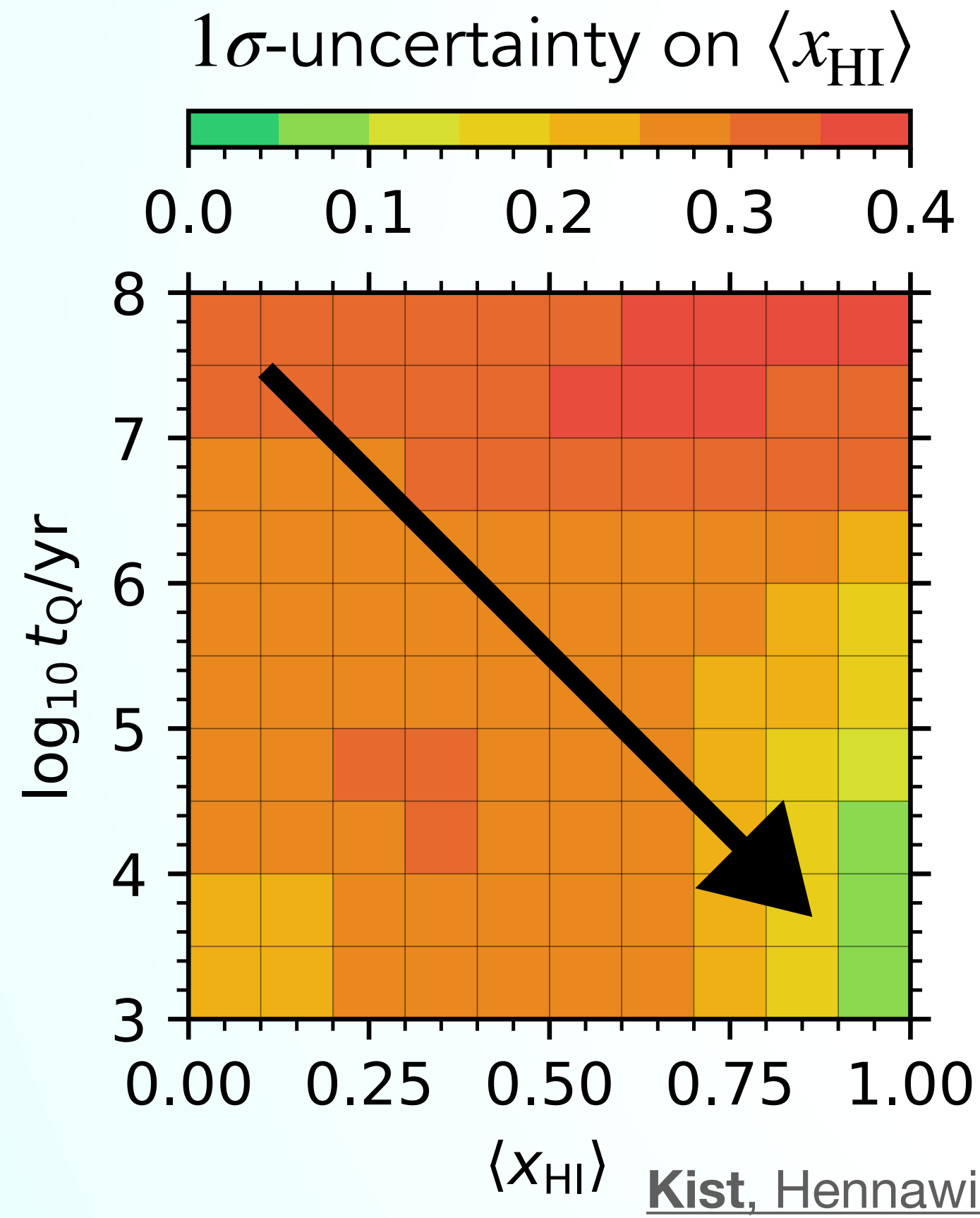
Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across parameter space



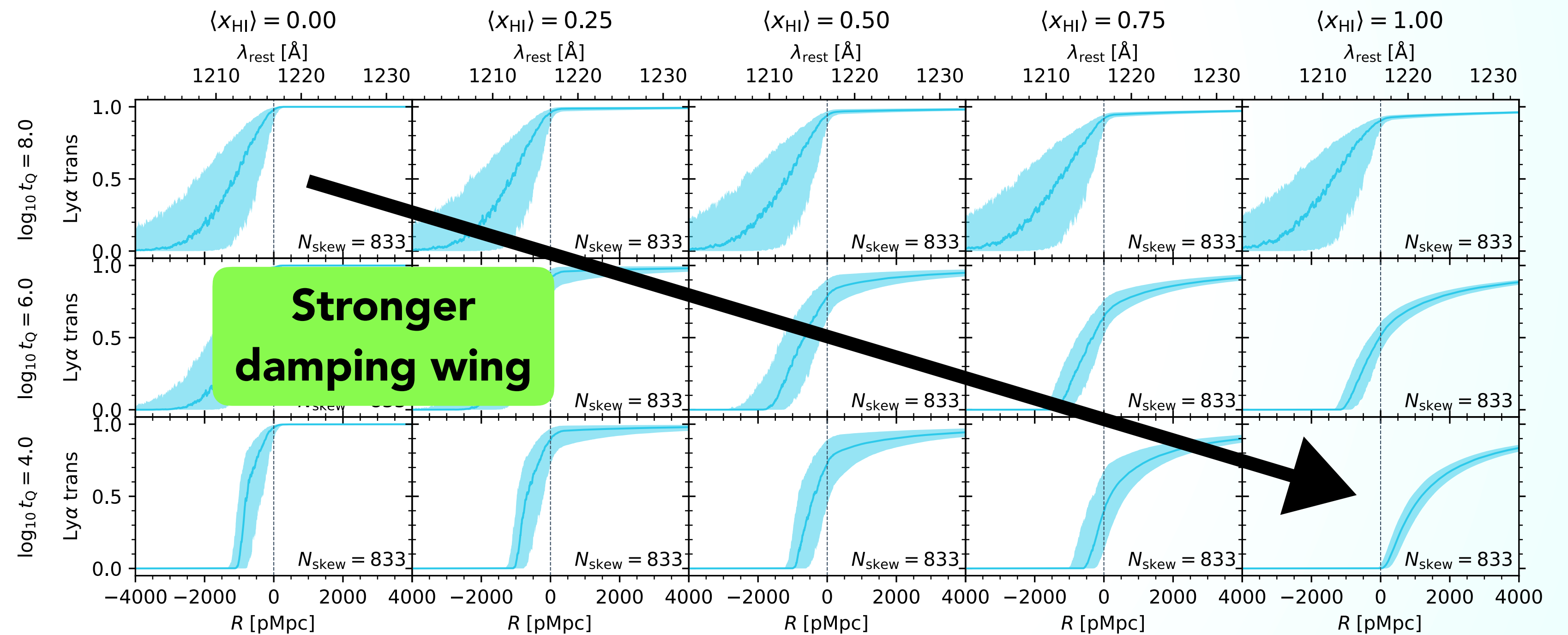
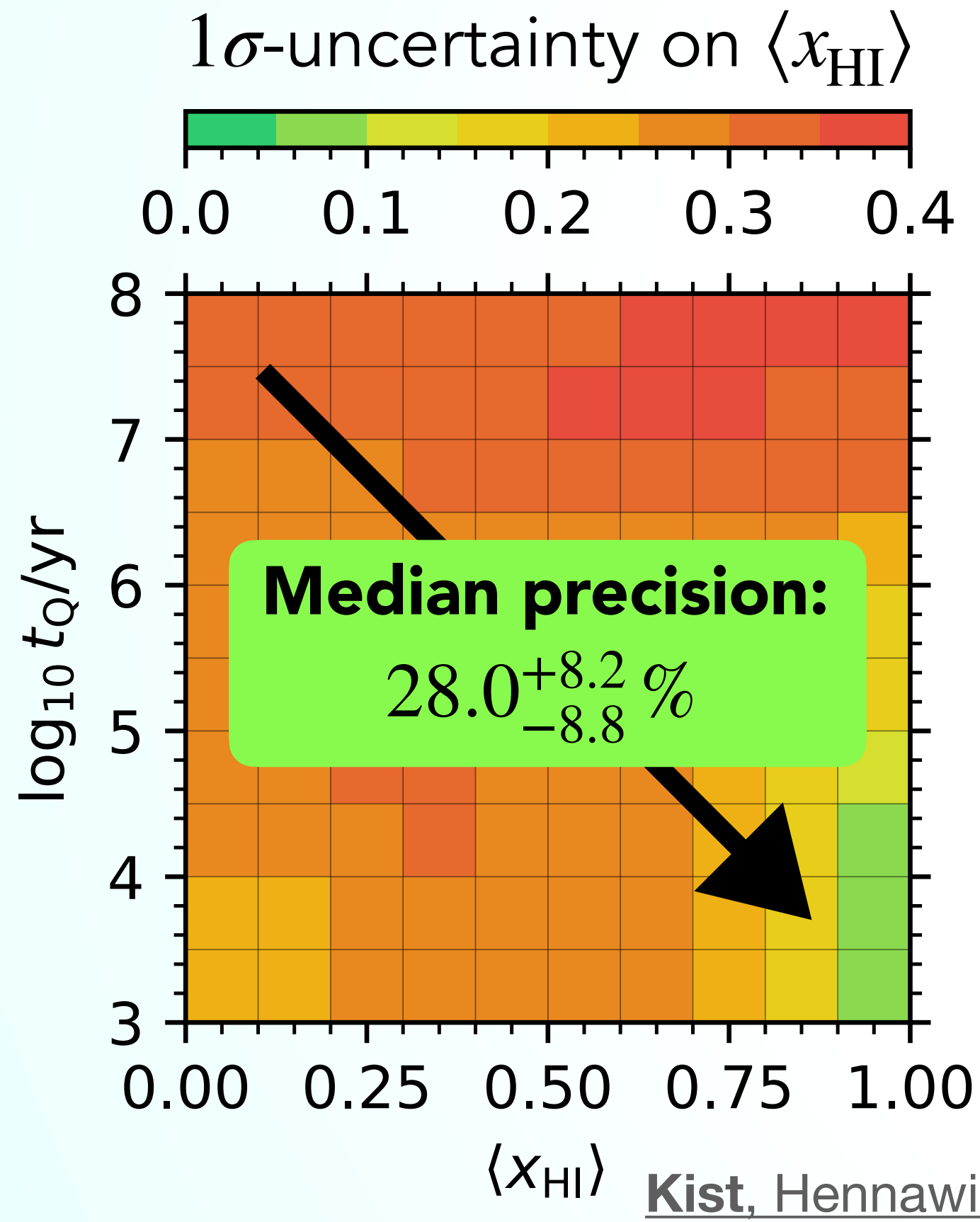
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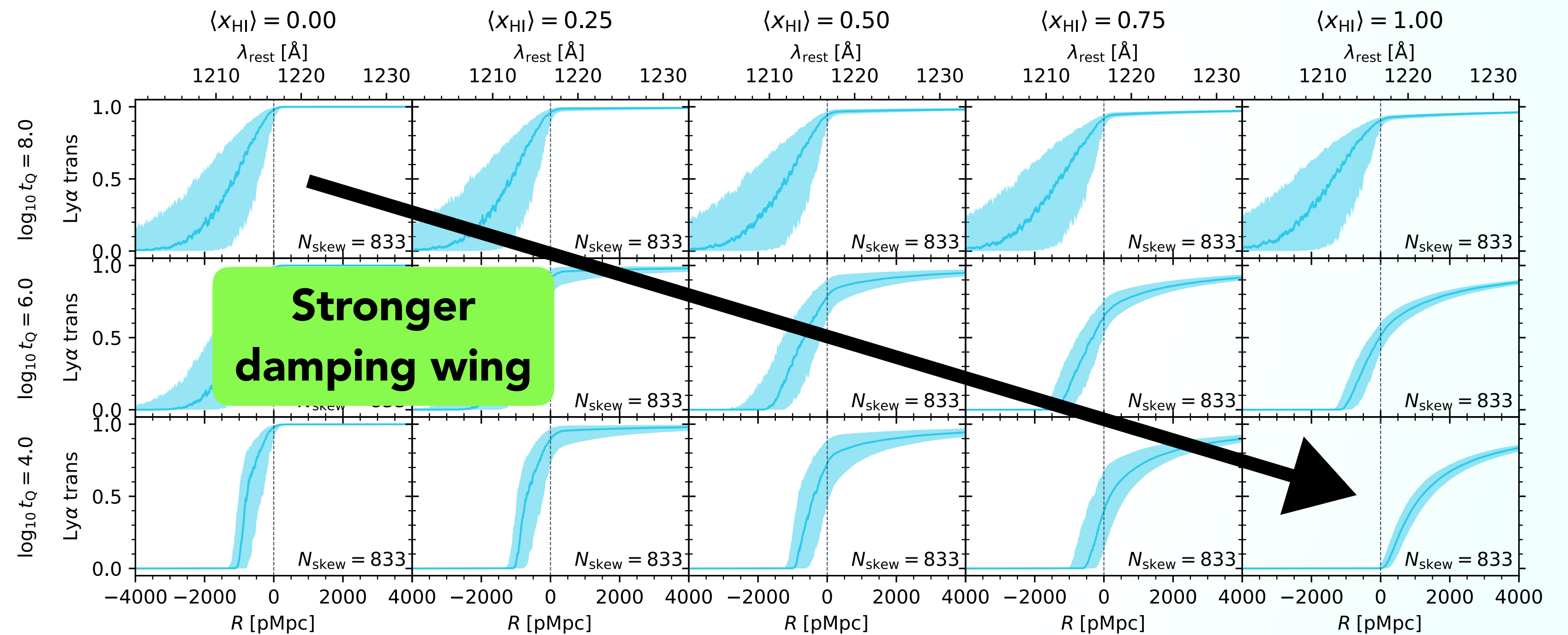
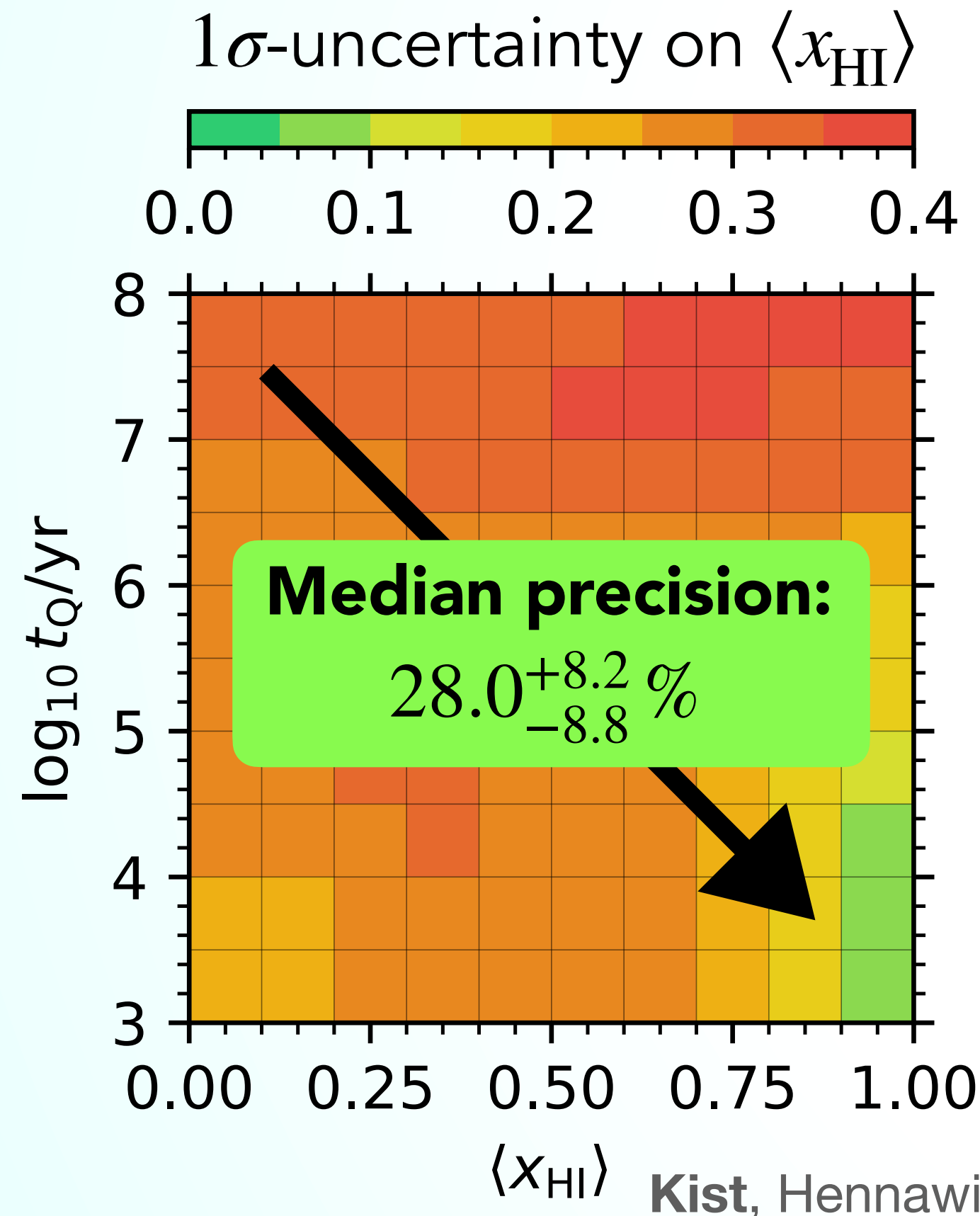
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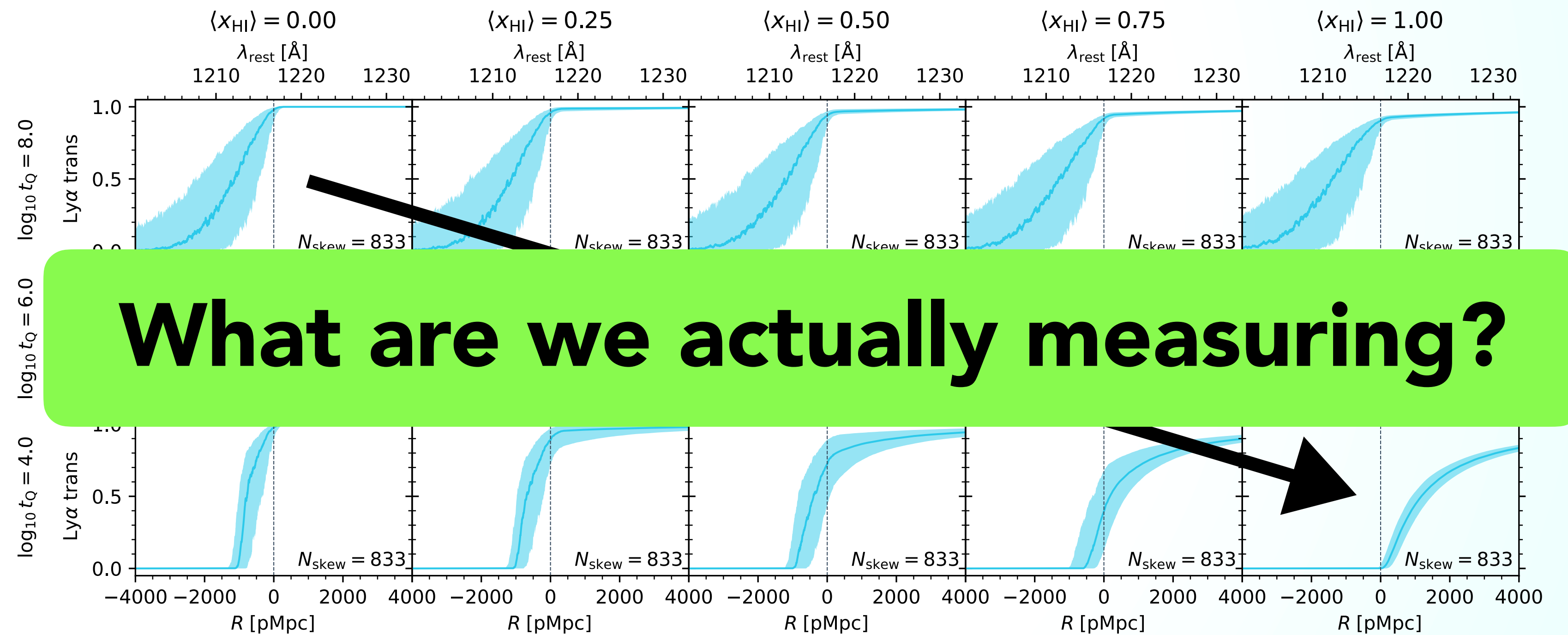
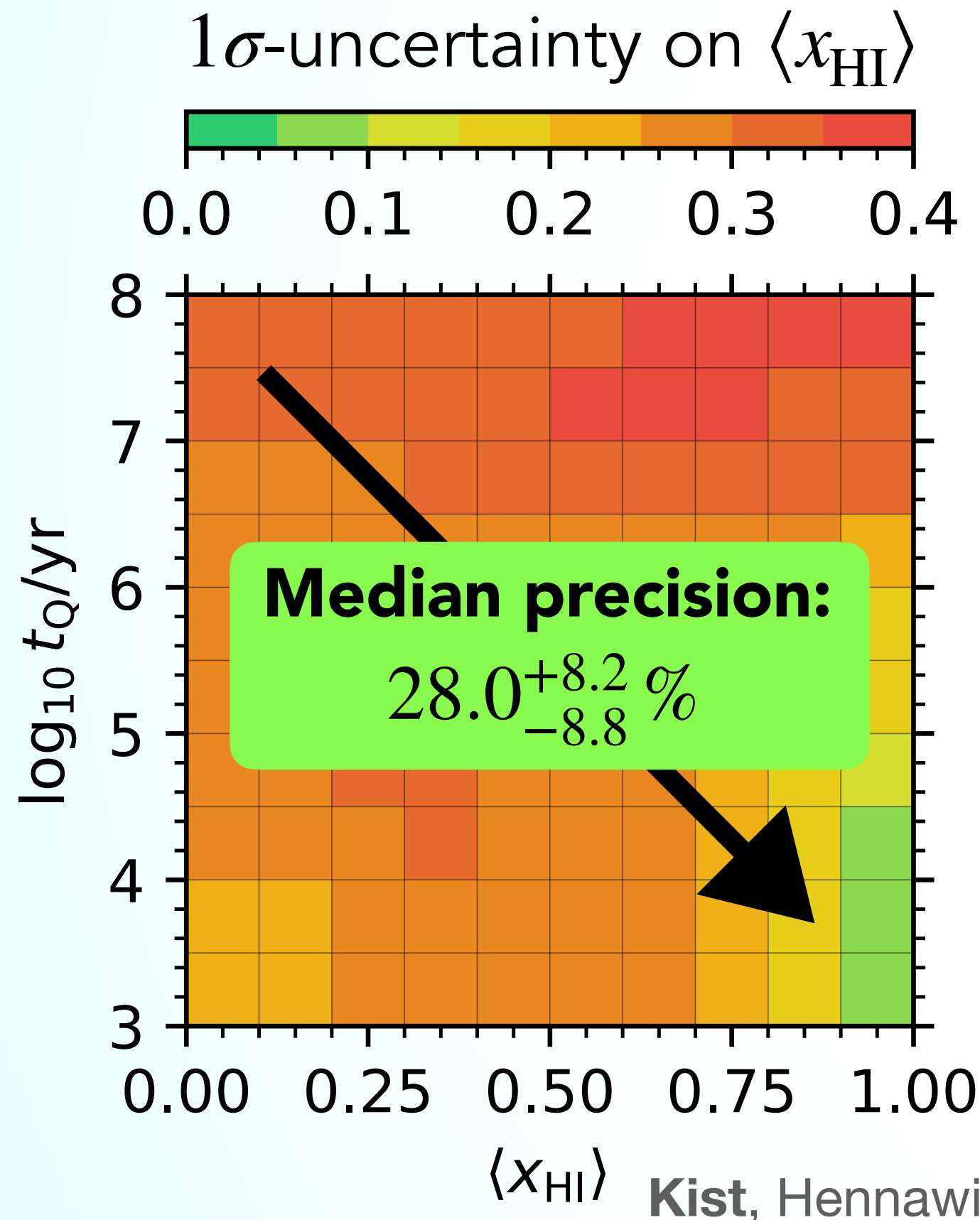
Variation across parameter space



Main sources of uncertainty: continuum reconstruction and **stochasticity of ionized bubble sizes**

Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across parameter space



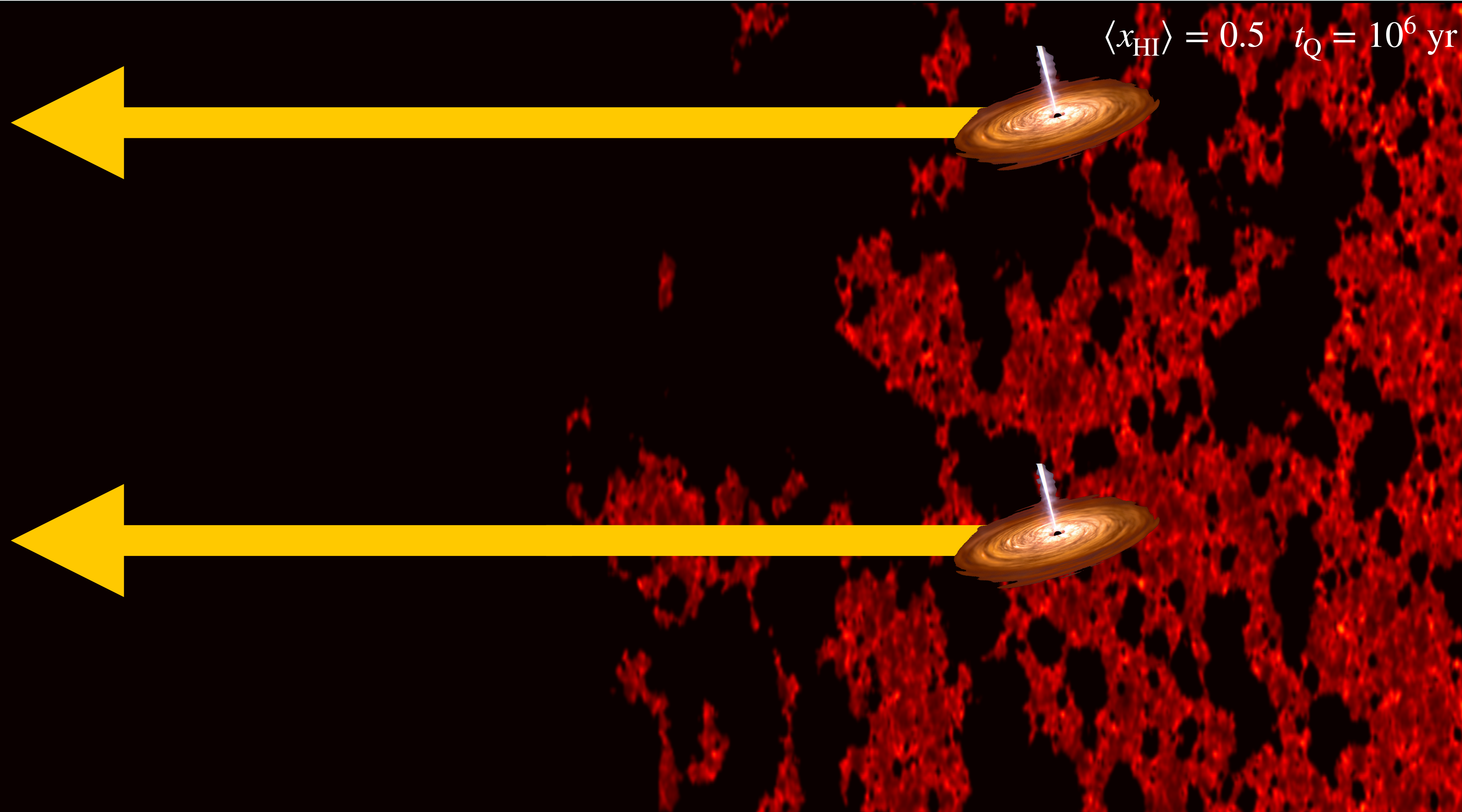
Kist, Hennawi & Davies 2024a

Kist, Hennawi & Davies 2024b (in prep.)

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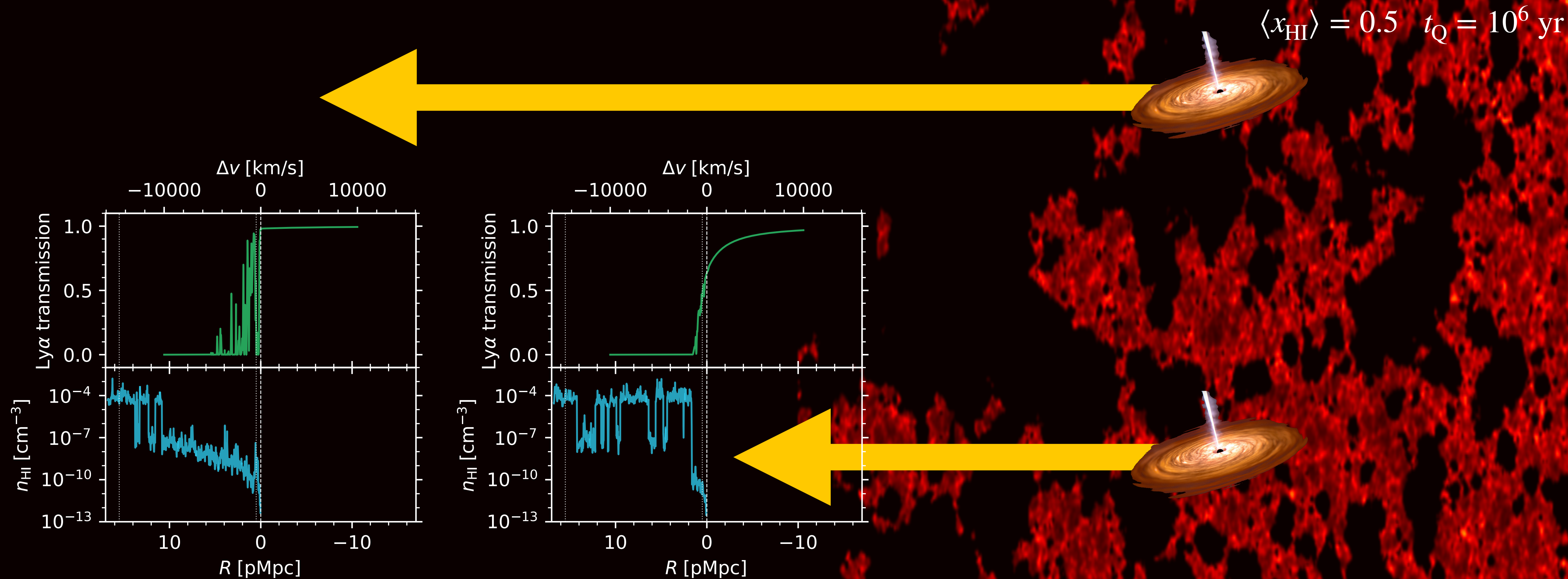
Measuring the local HI content in front of a quasar

Introducing a new label for the HI column density



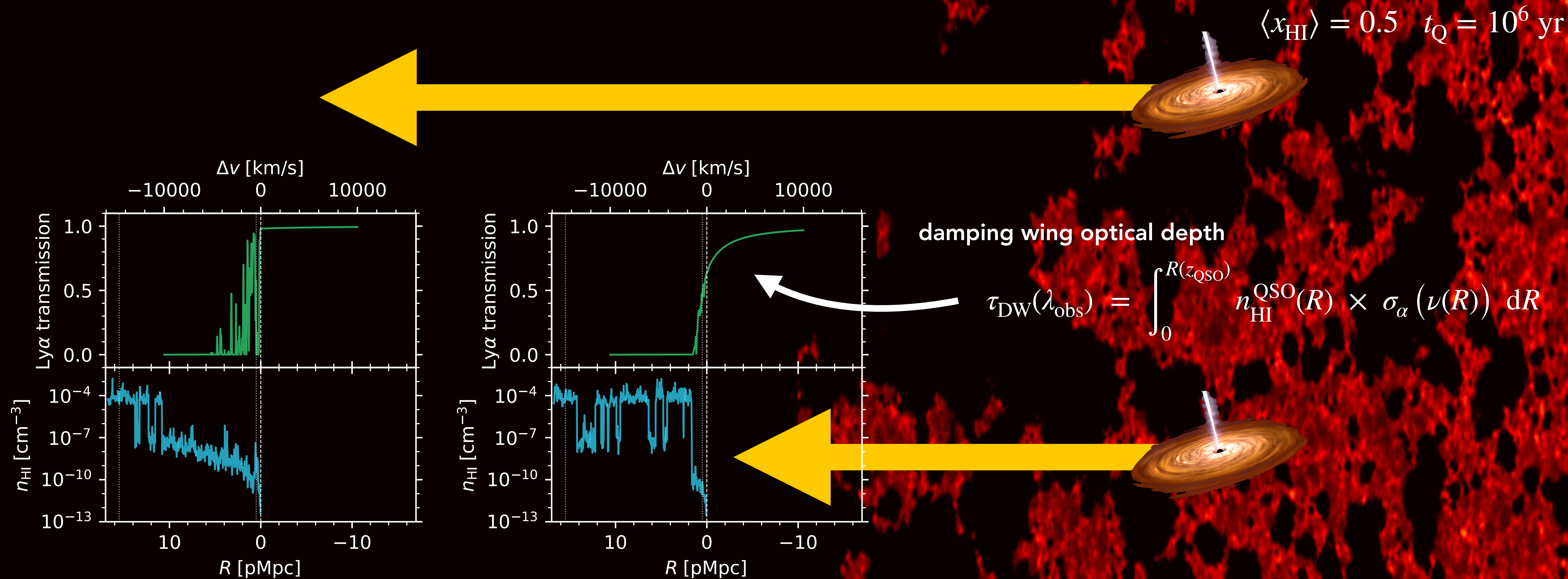
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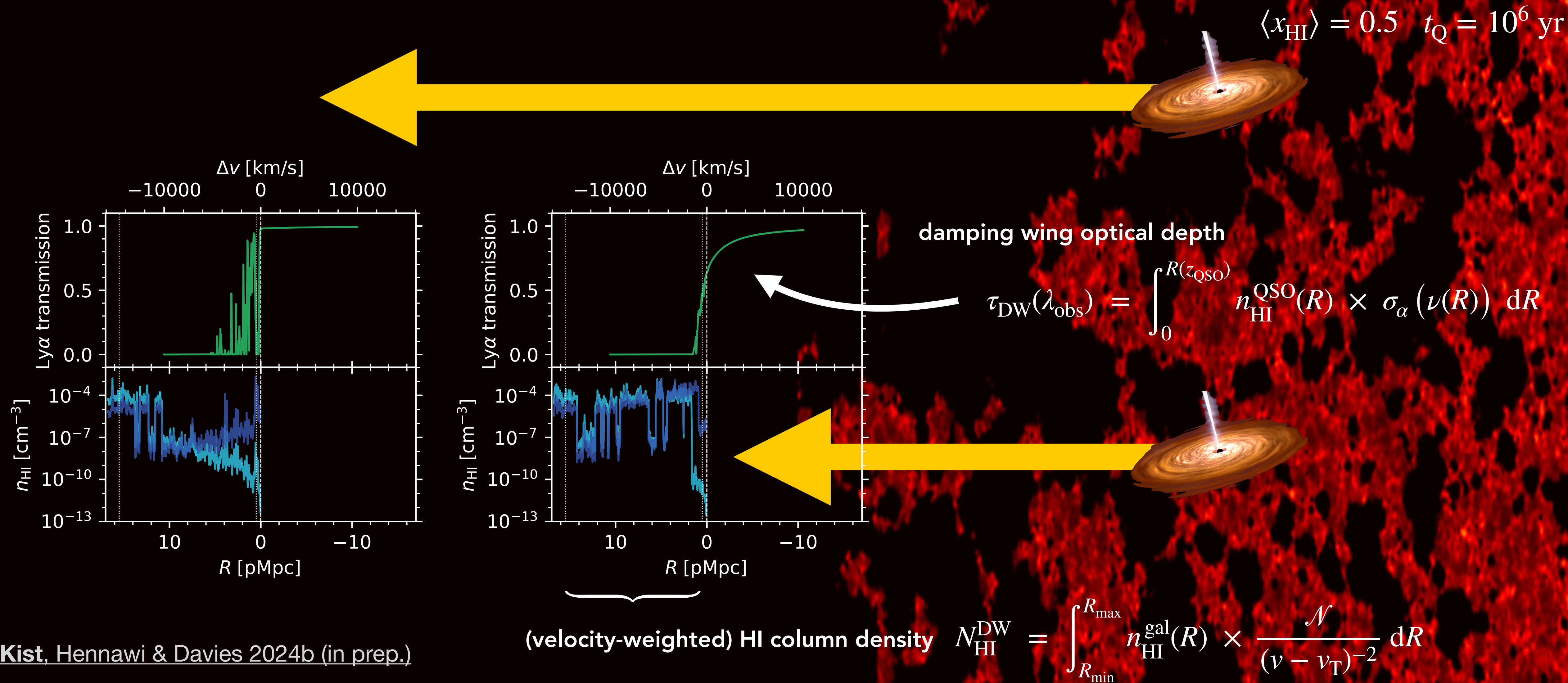
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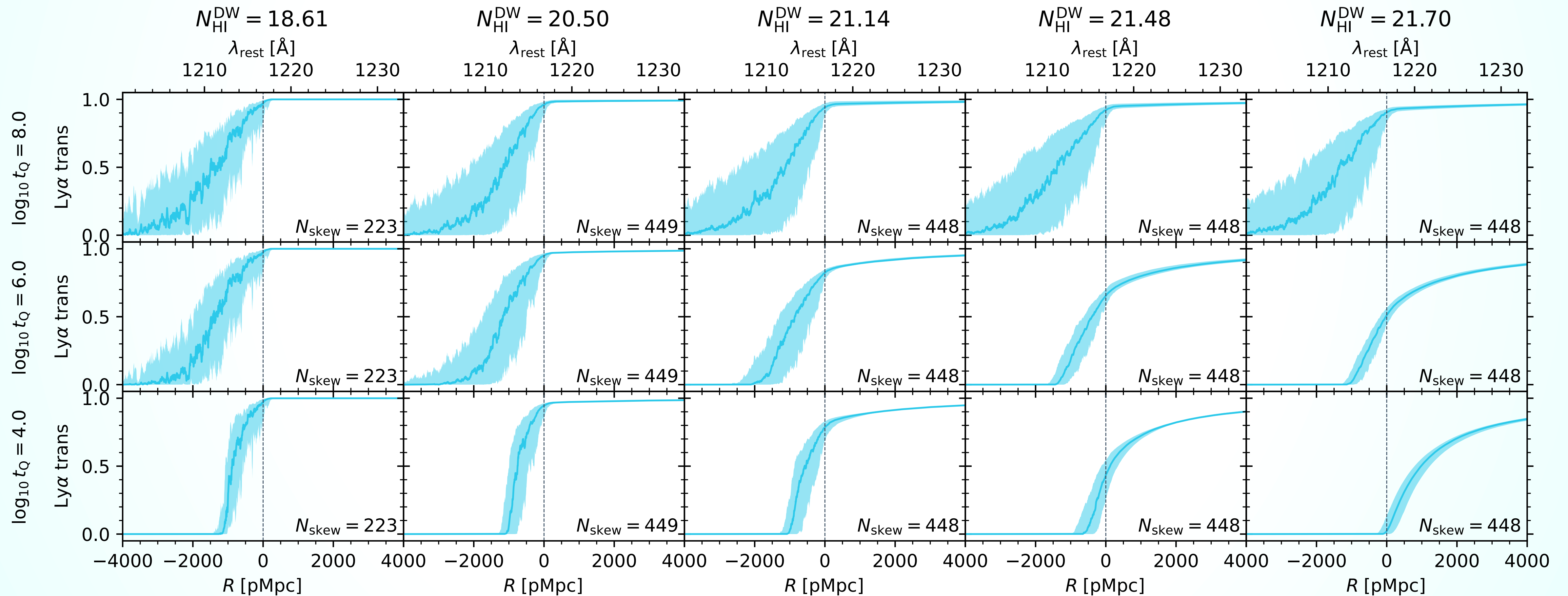
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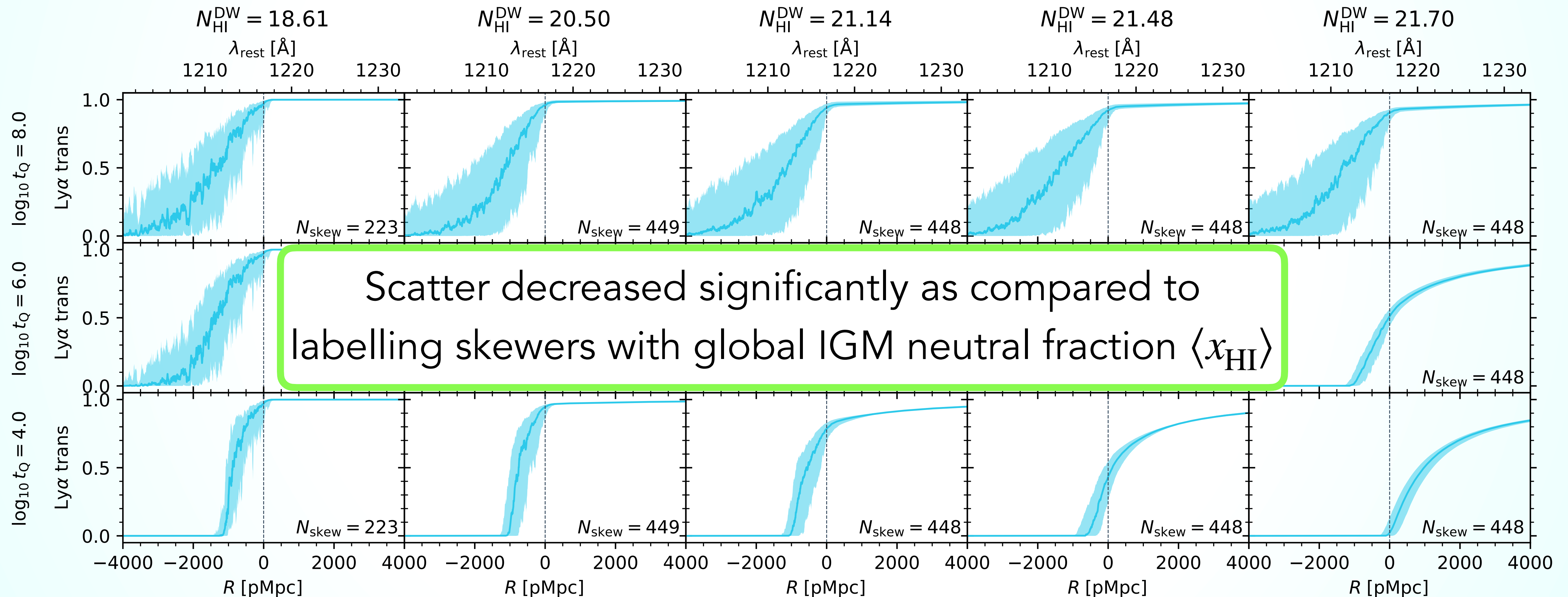
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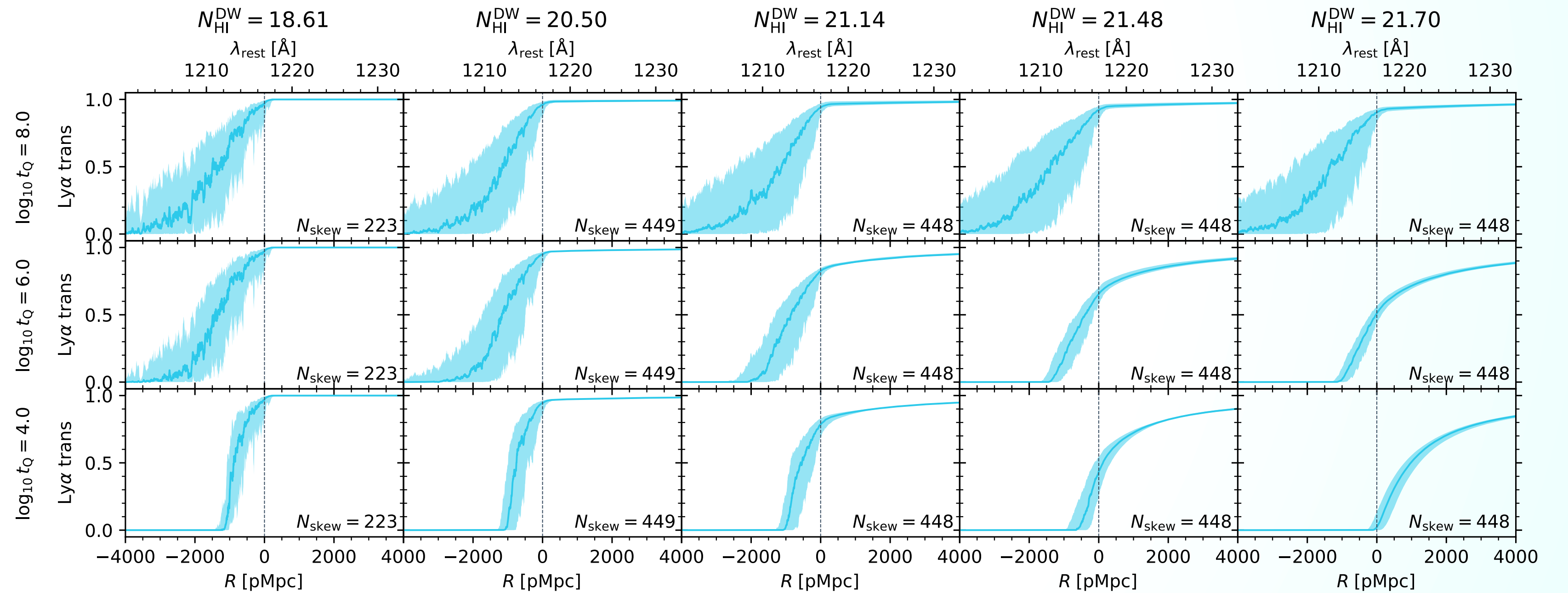
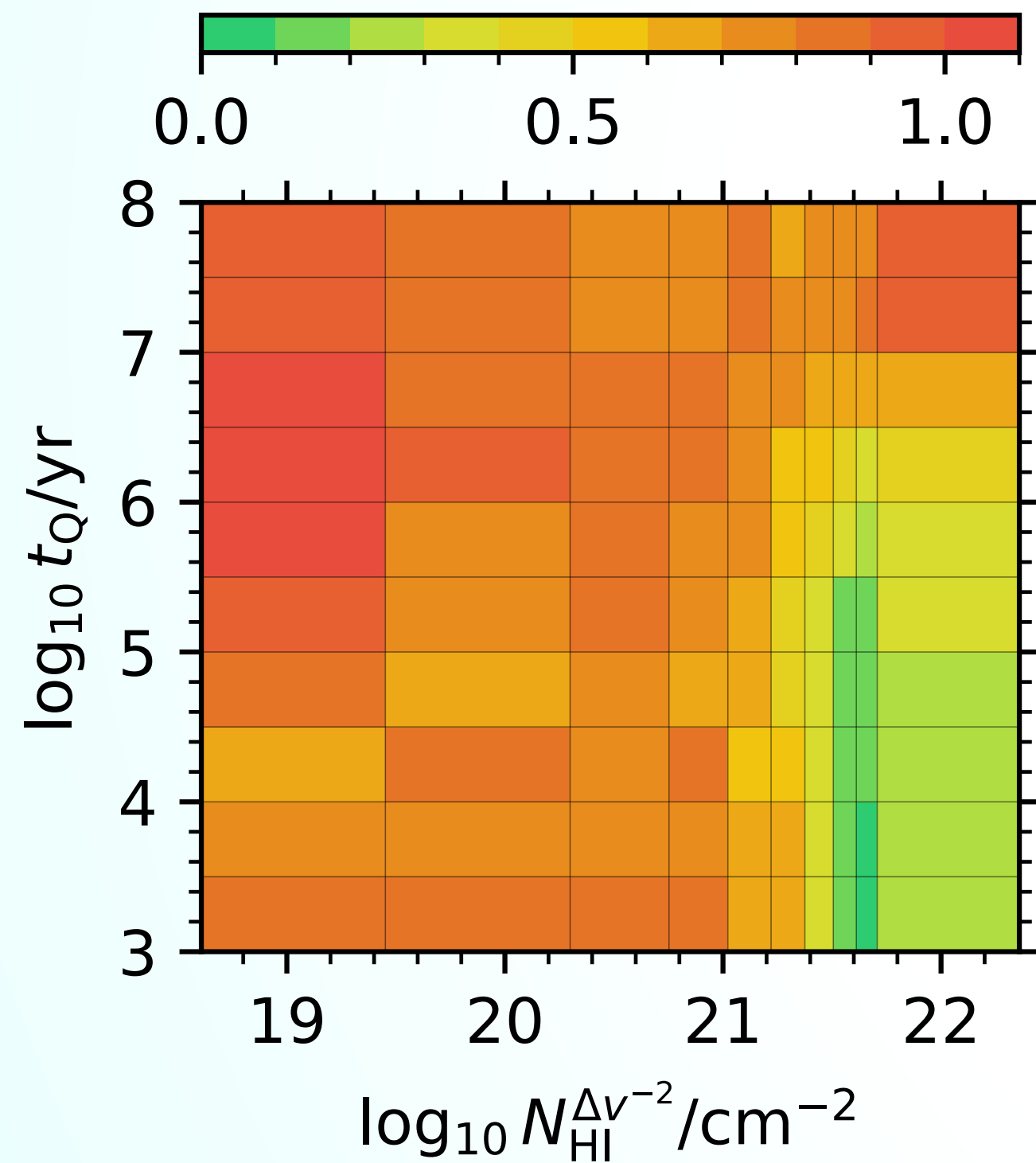
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Quantifying $N_{\text{HI}}^{\text{DW}}$ Inference Precision

Variation across parameter space

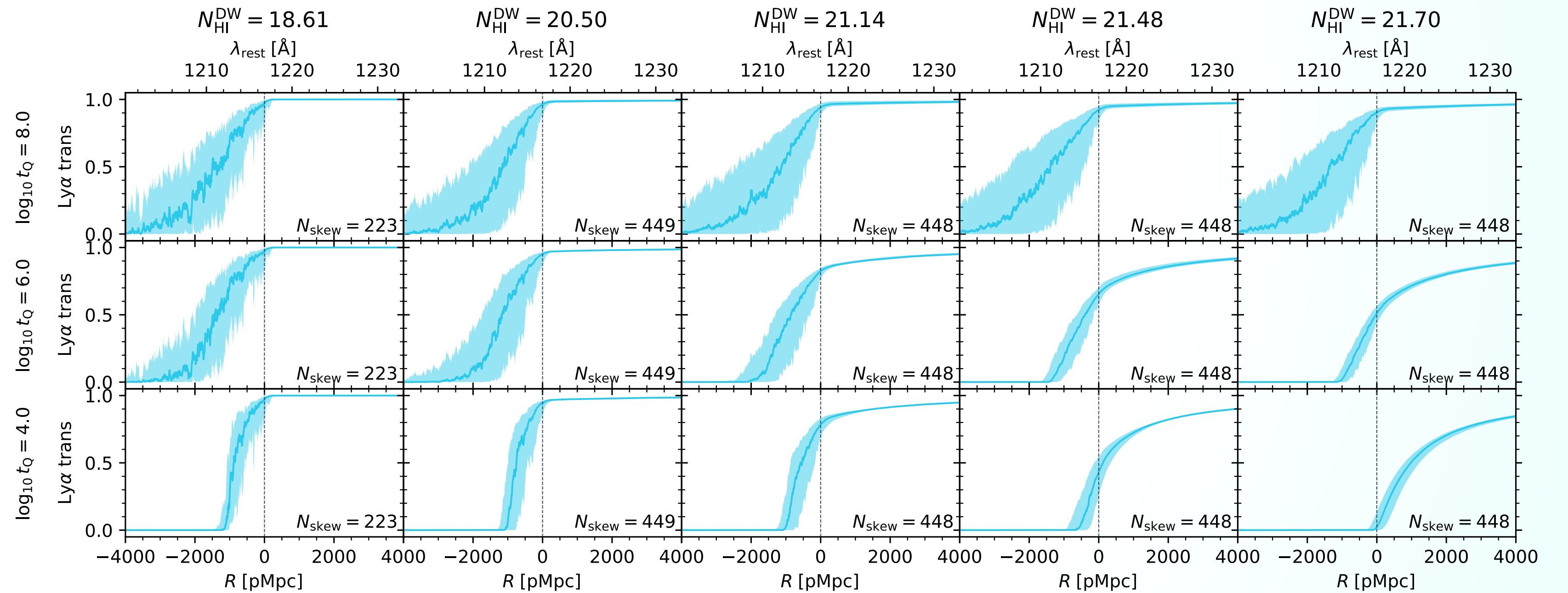
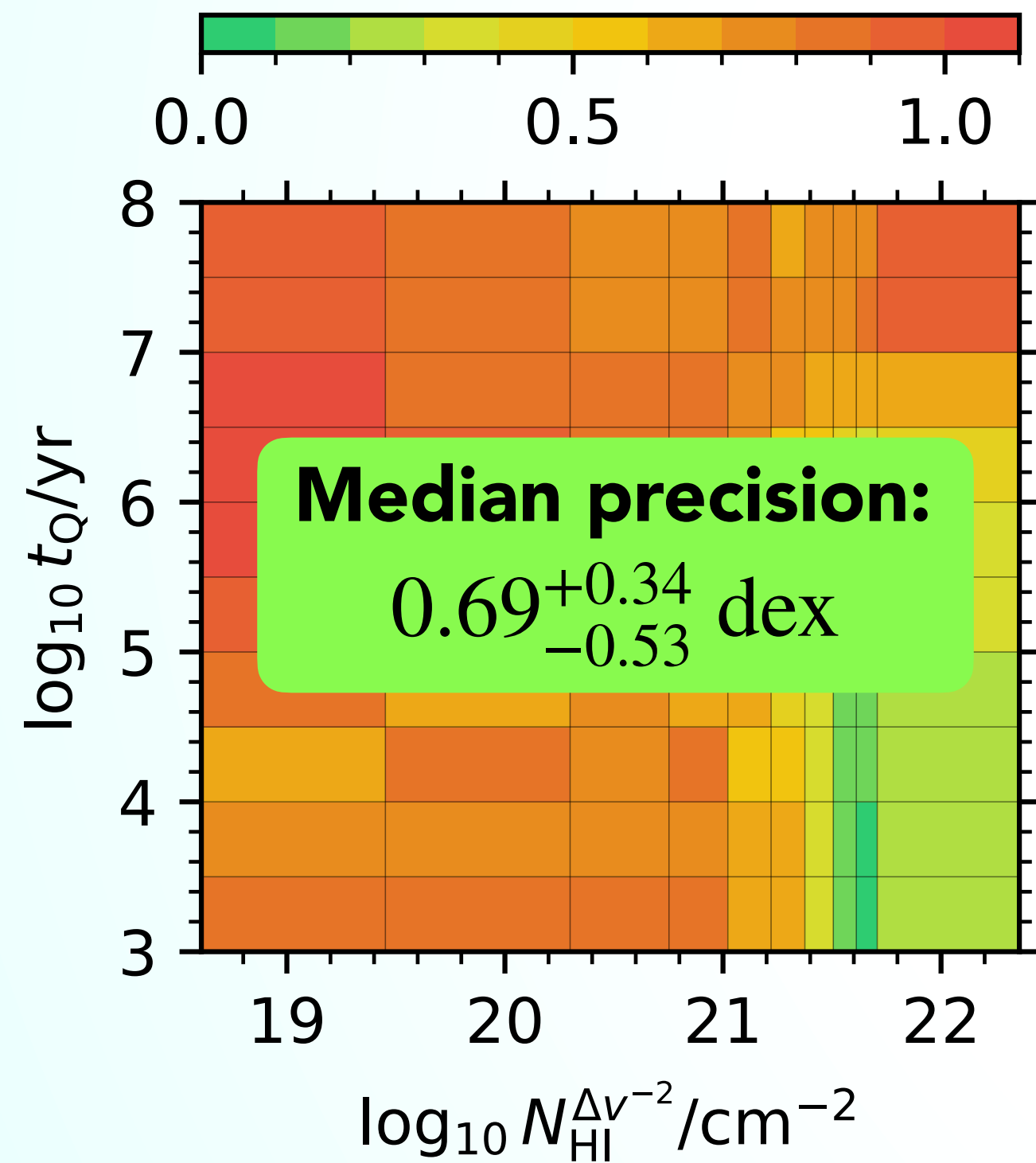
1σ -uncertainty on $\log_{10} N_{\text{HI}}^{\text{DW}}$



Quantifying $N_{\text{HI}}^{\text{DW}}$ Inference Precision

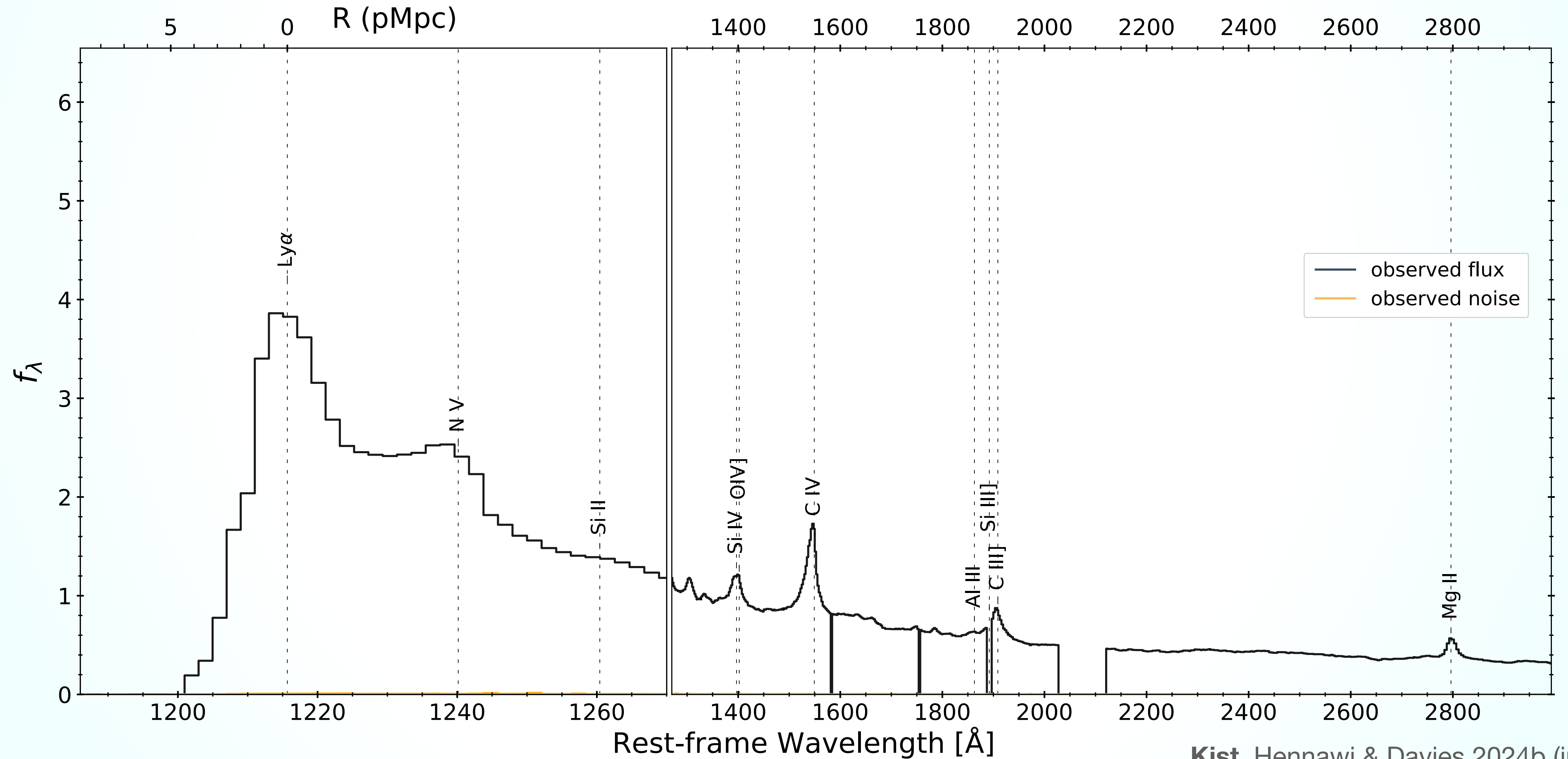
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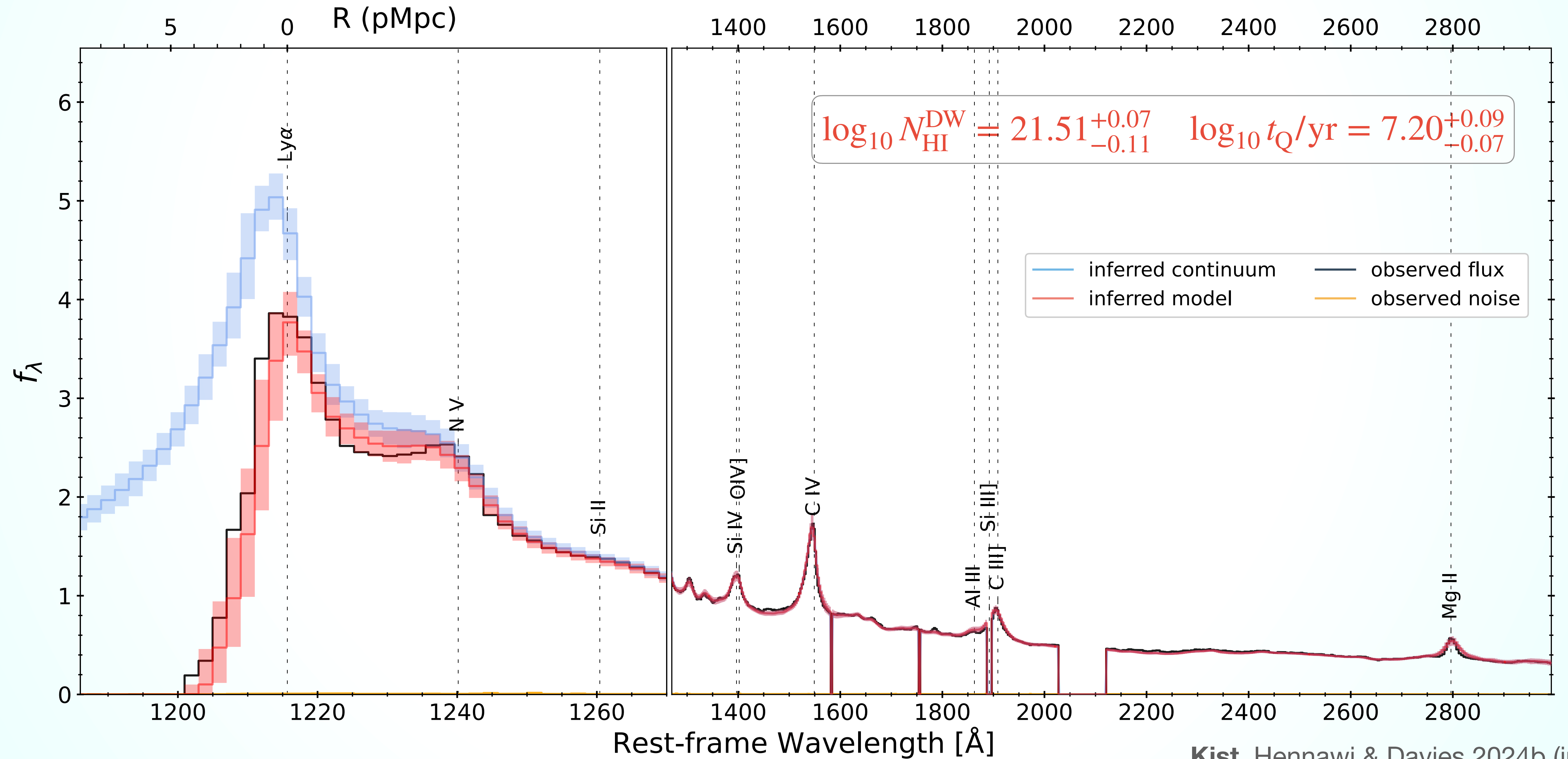
Inferring $N_{\text{HI}}^{\text{DW}}$ in front of a $z = 6.83$ quasar

A JWST spectrum of J0411-0907



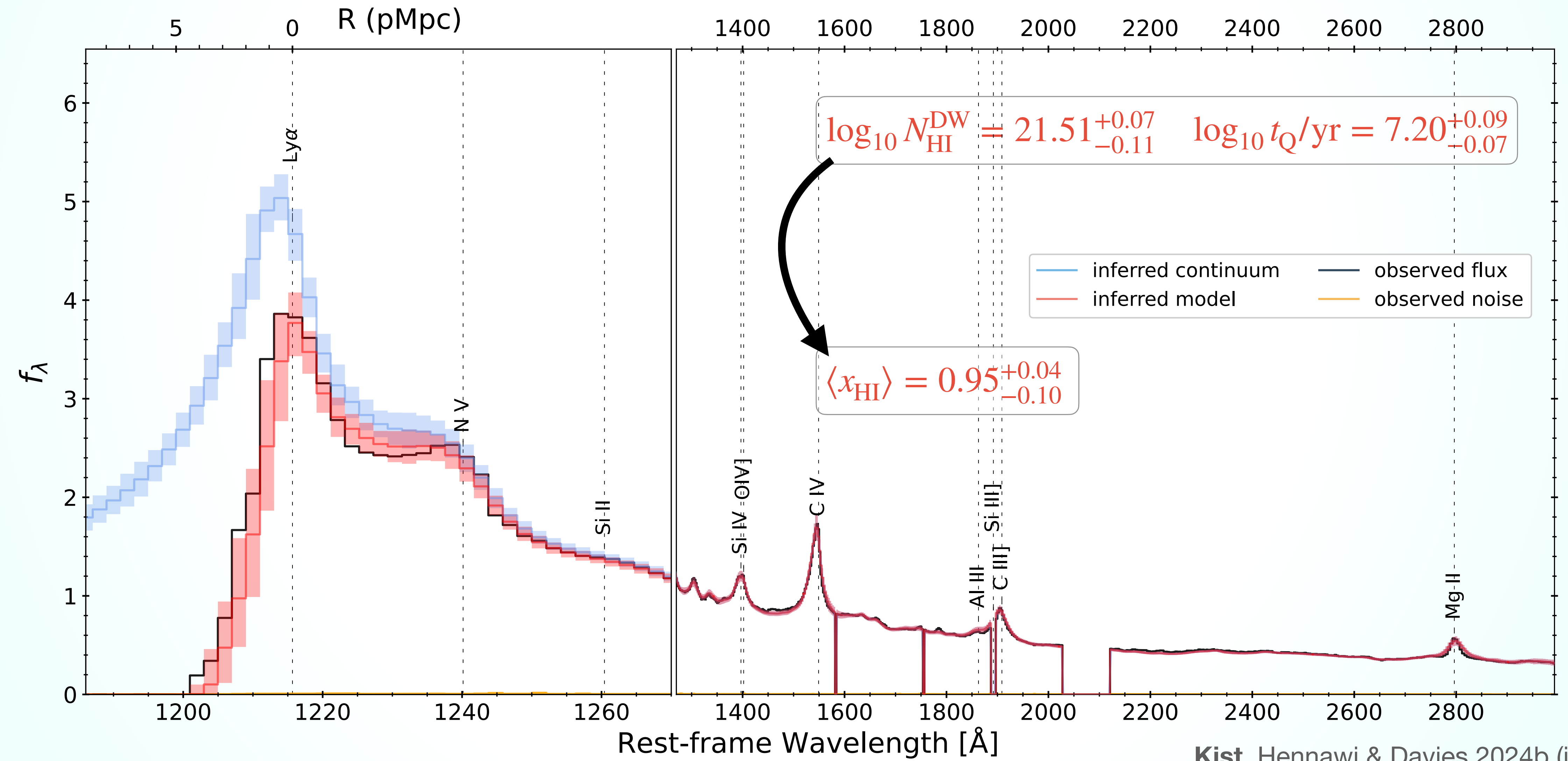
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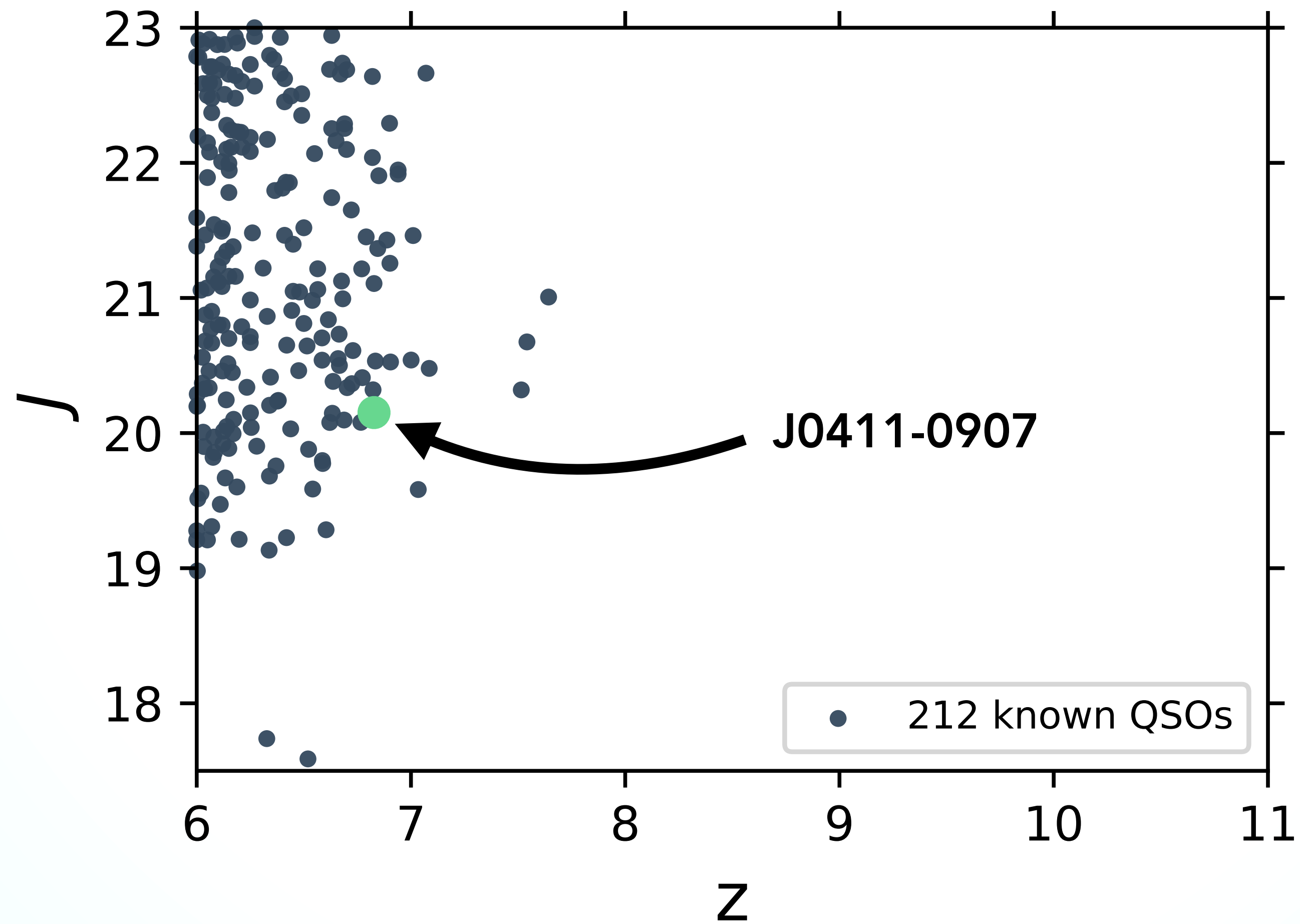
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EUCLID

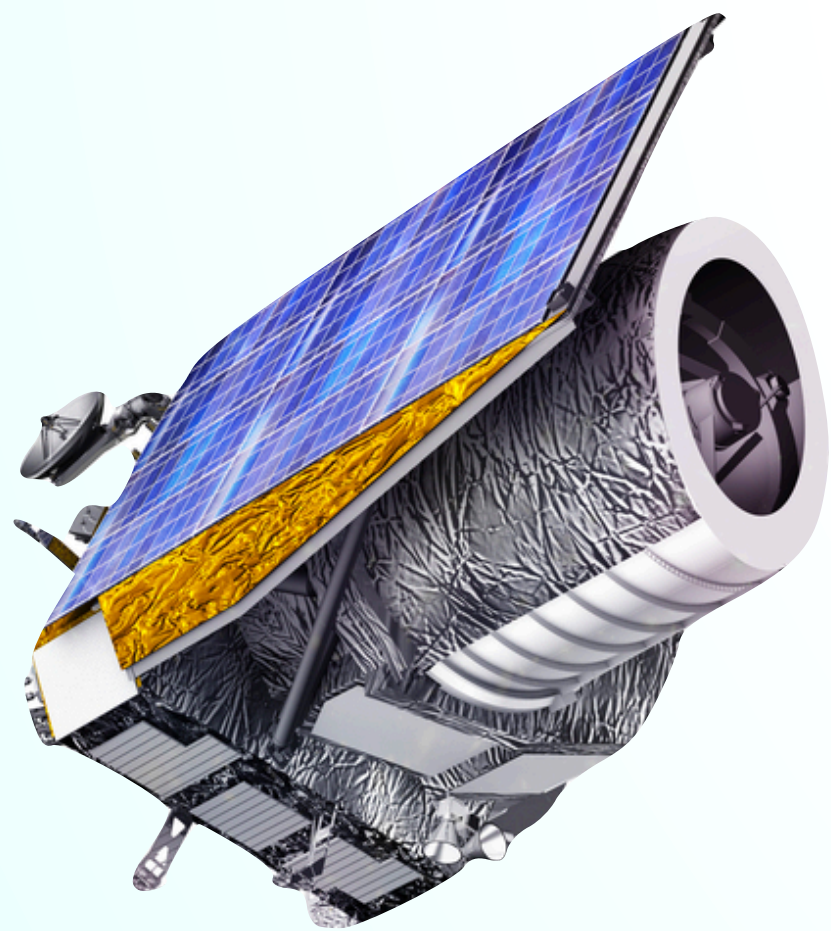
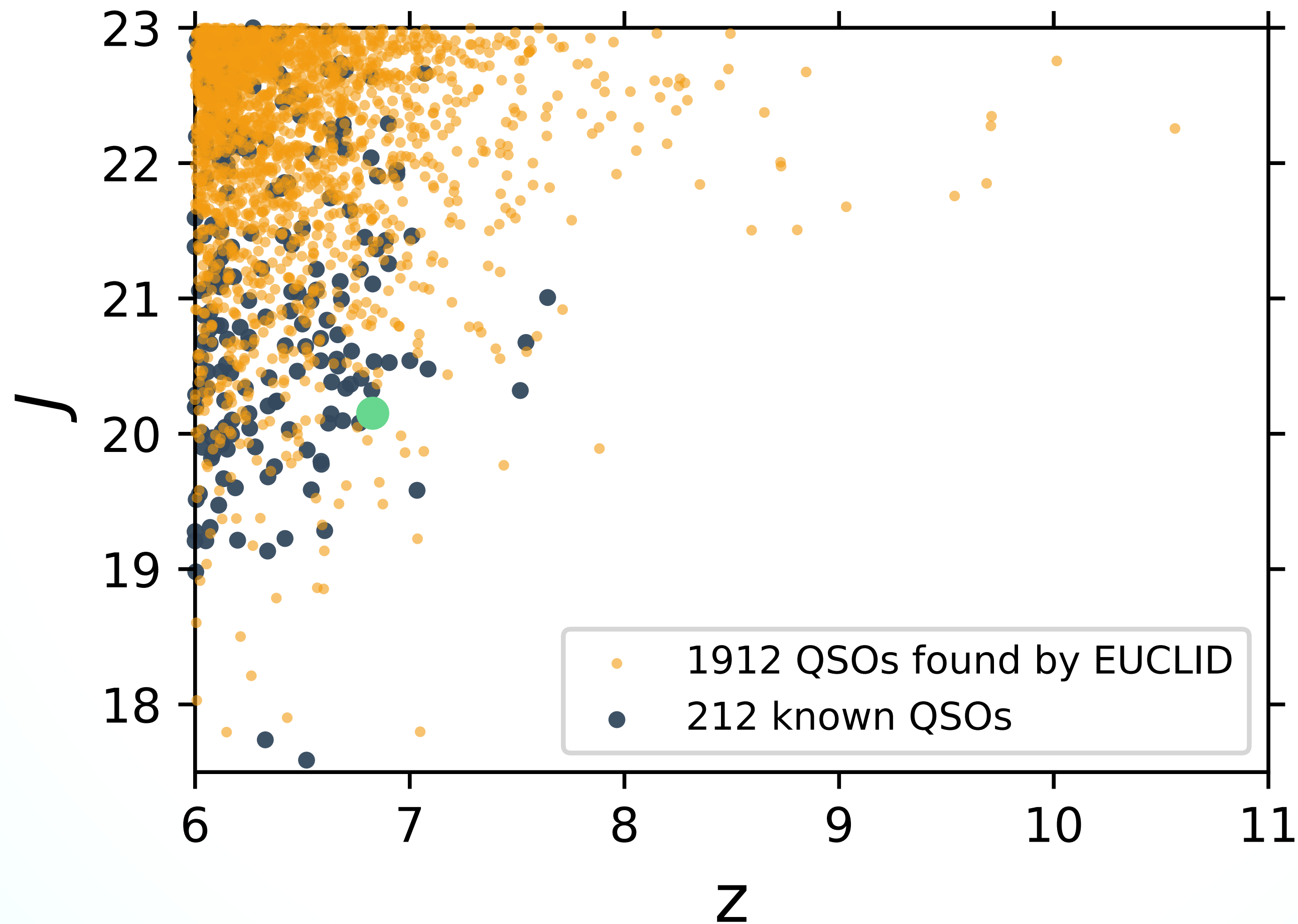
The Quasar Yield of the Wide-Field Survey



EUCLID

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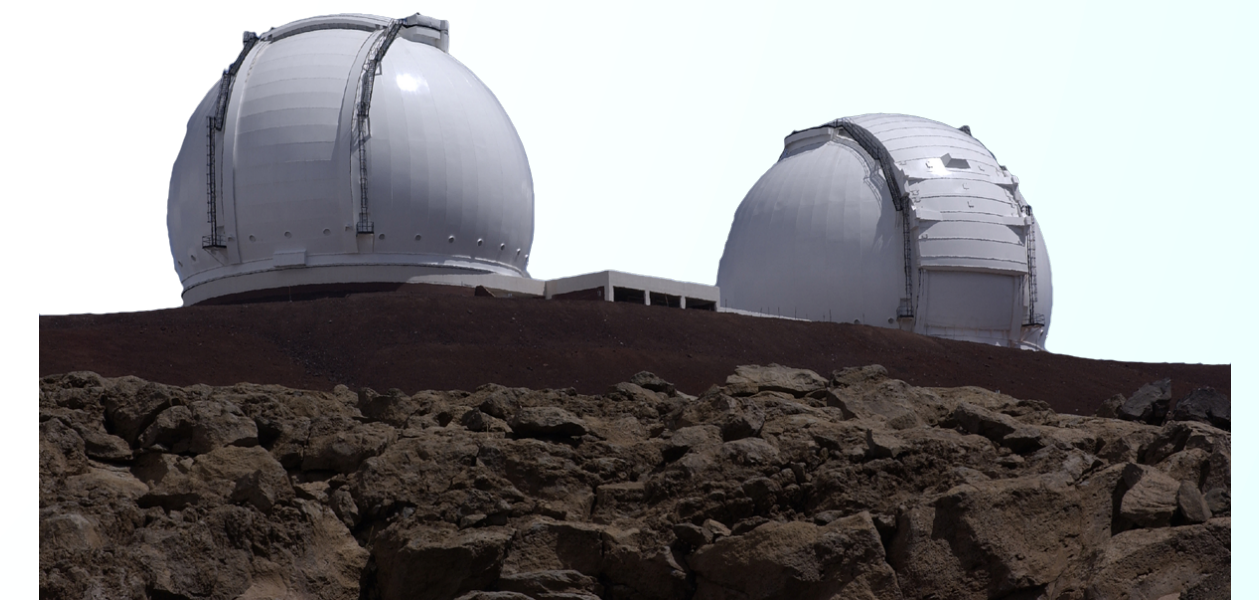
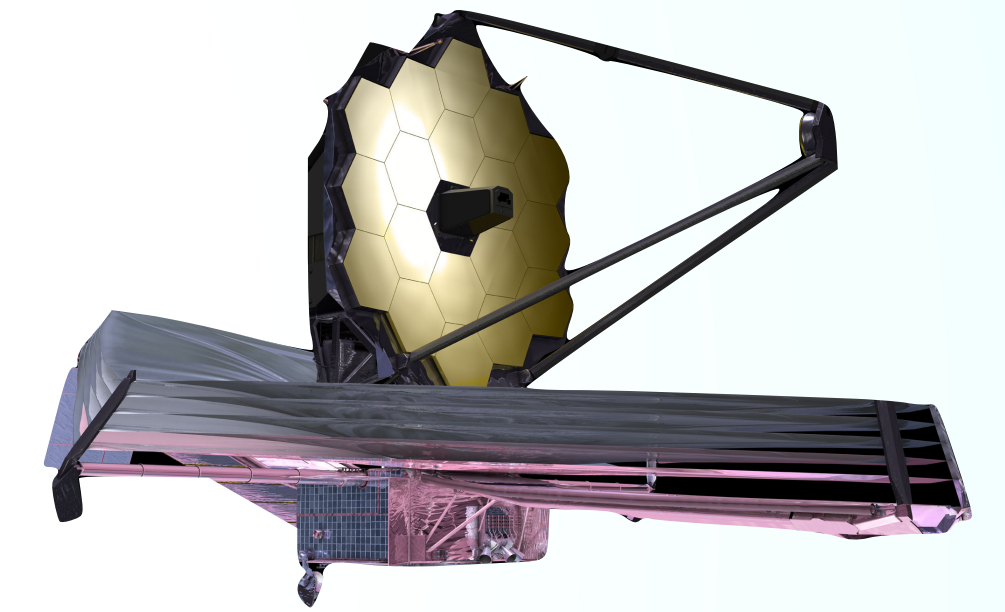
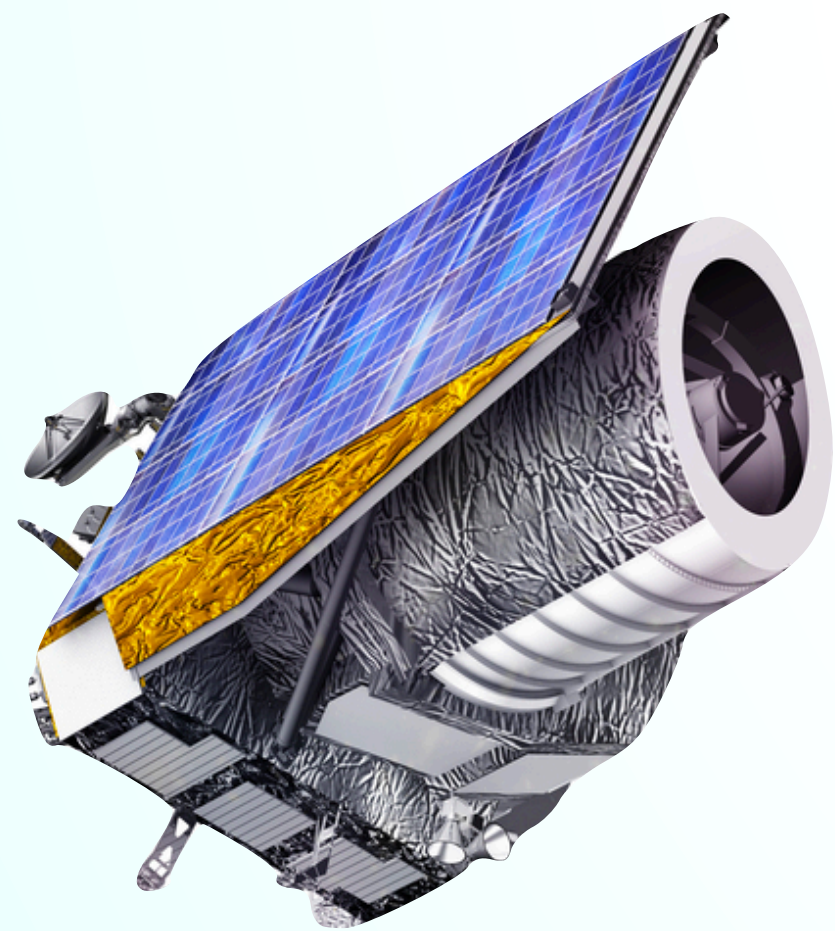
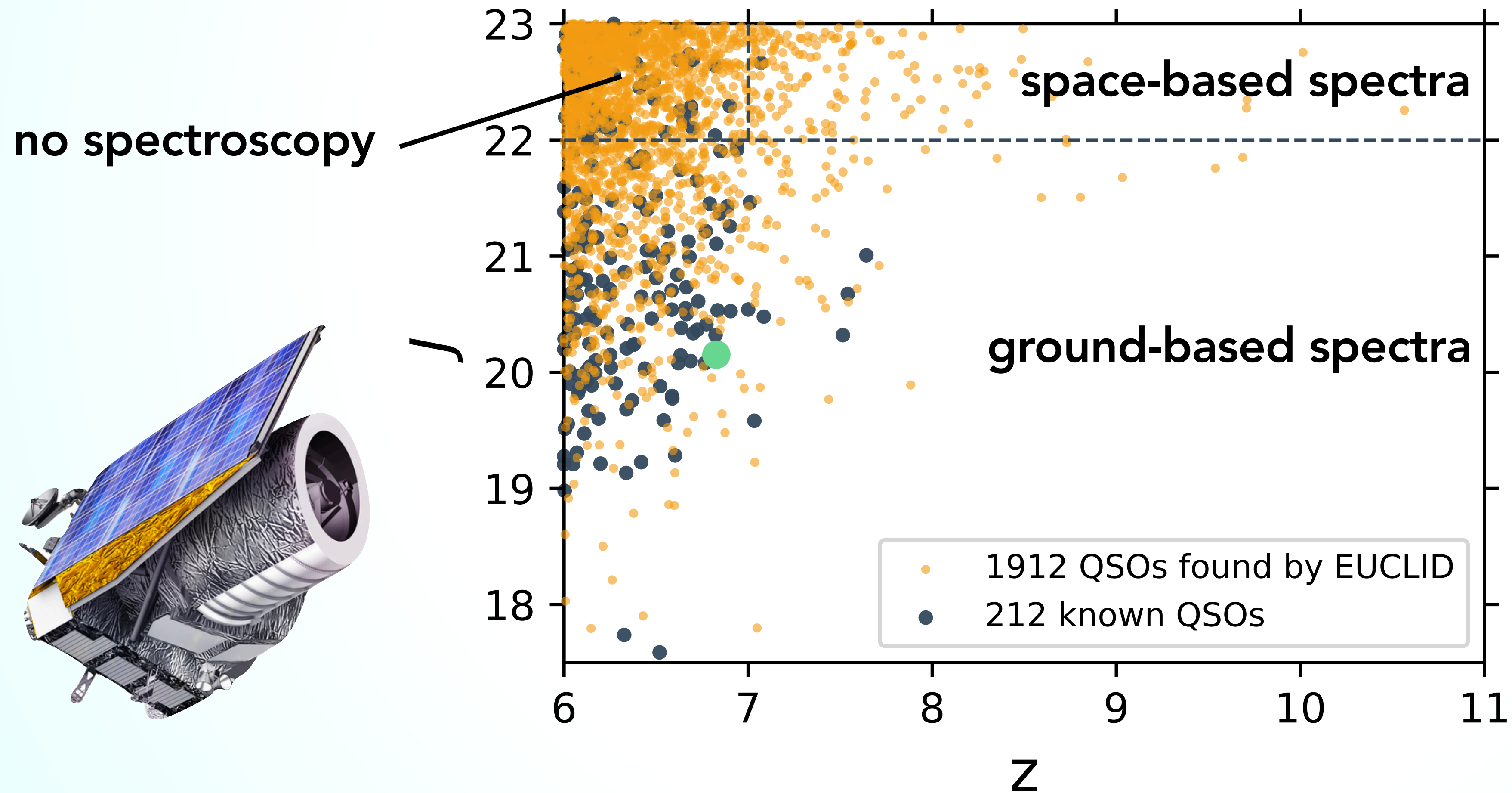
Samples from a Wang+2019 quasar luminosity function



EUCLID

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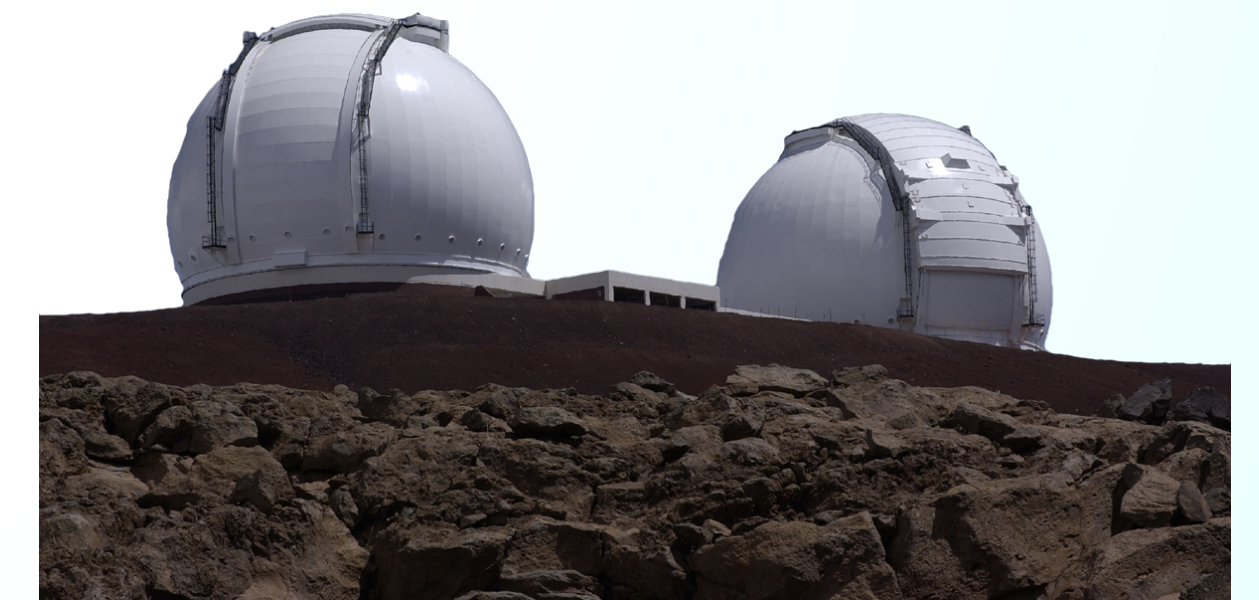
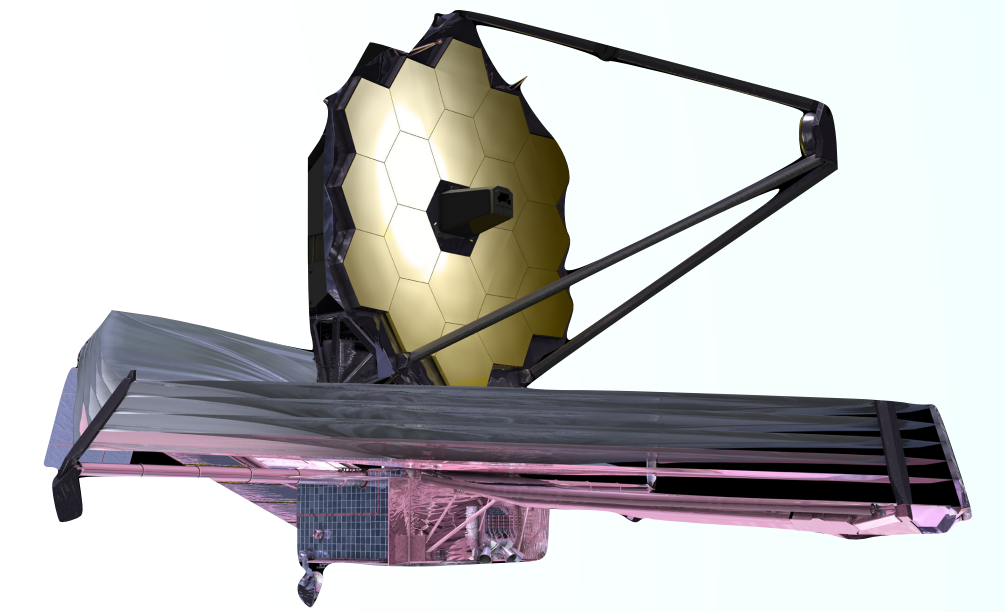
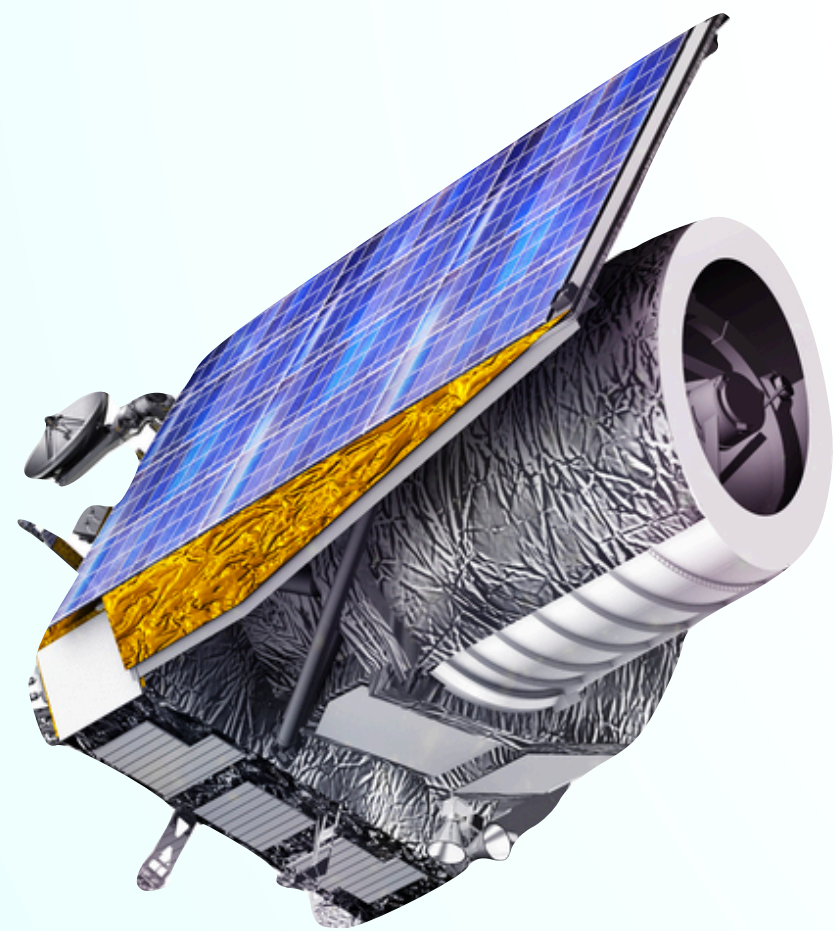
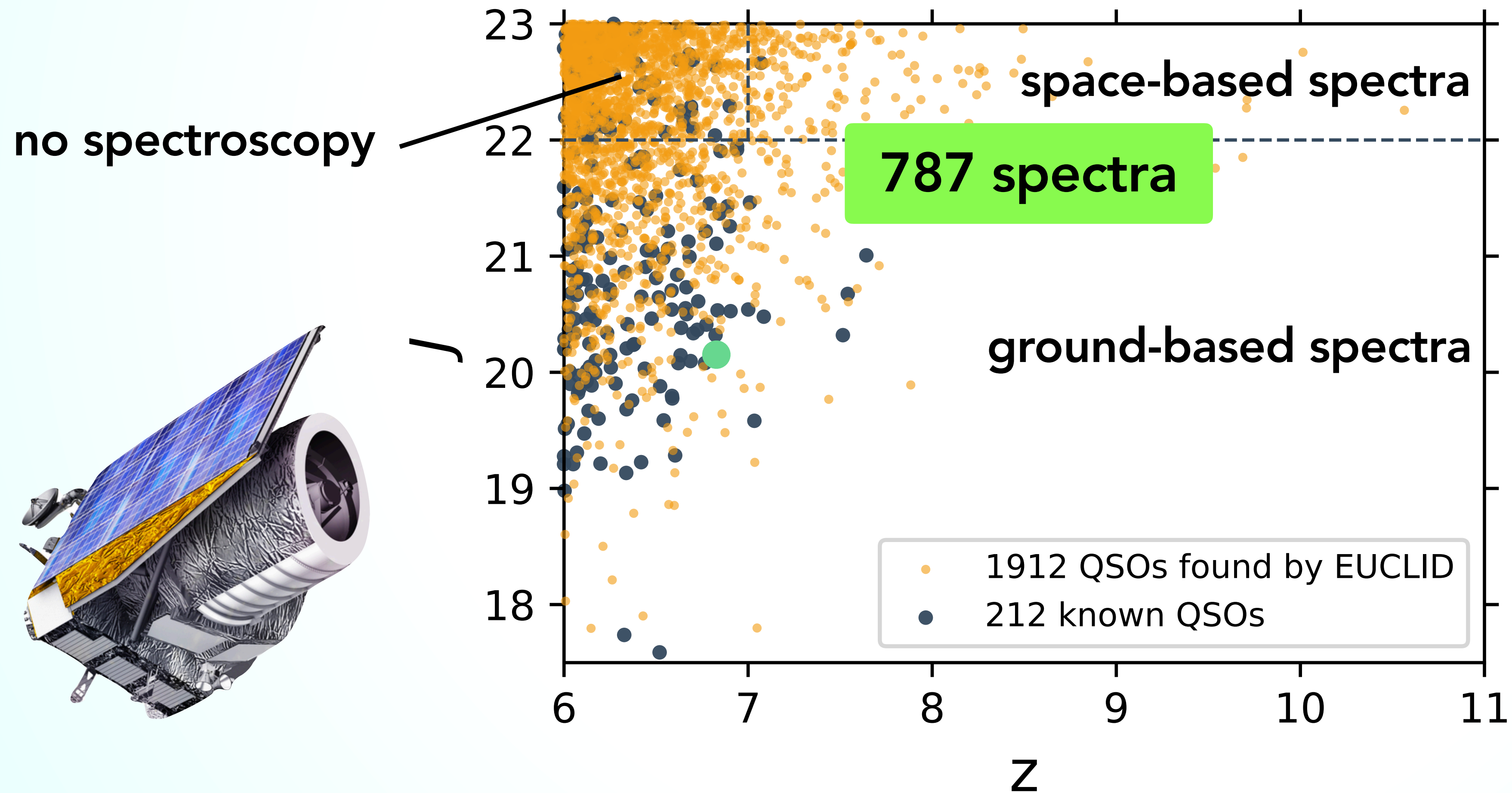
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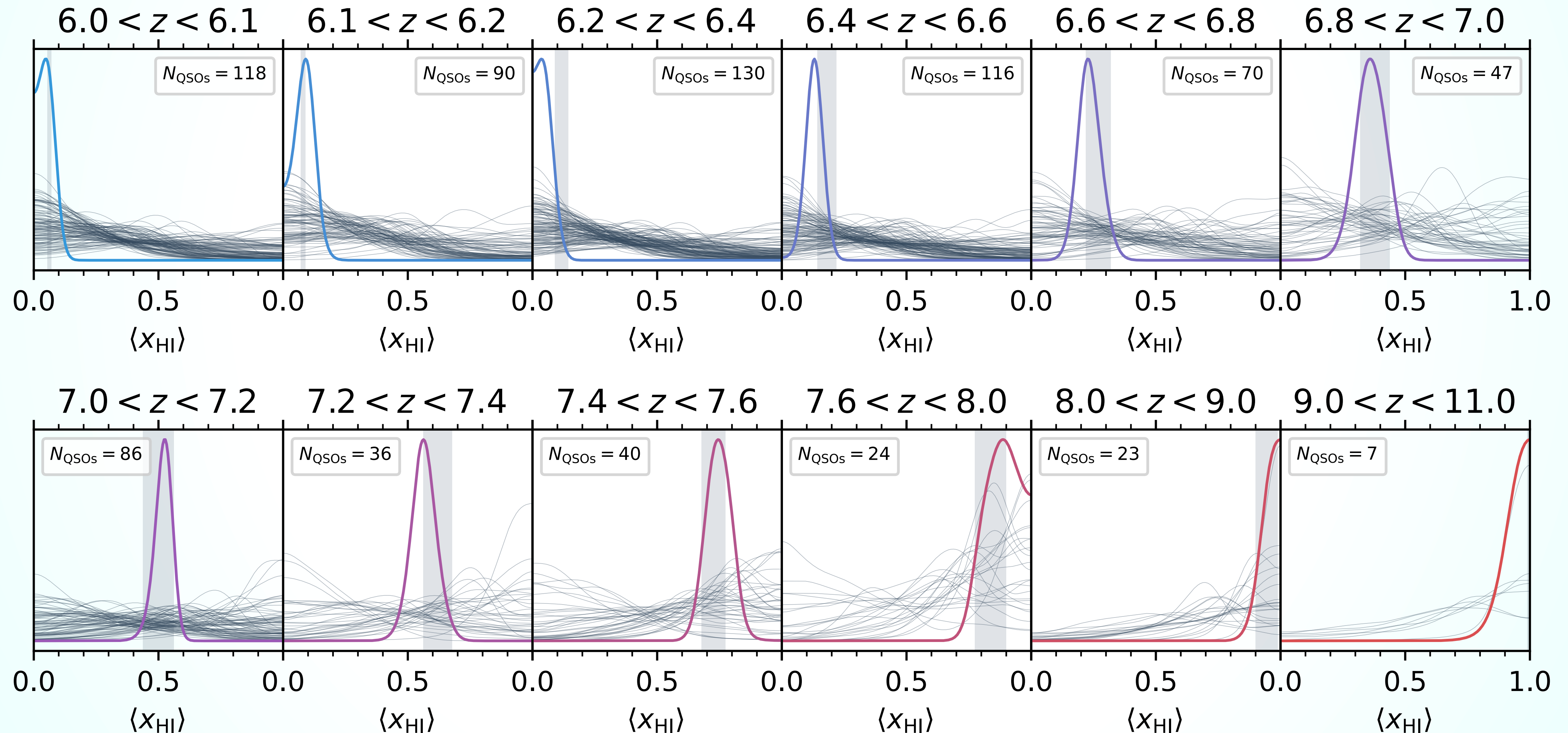
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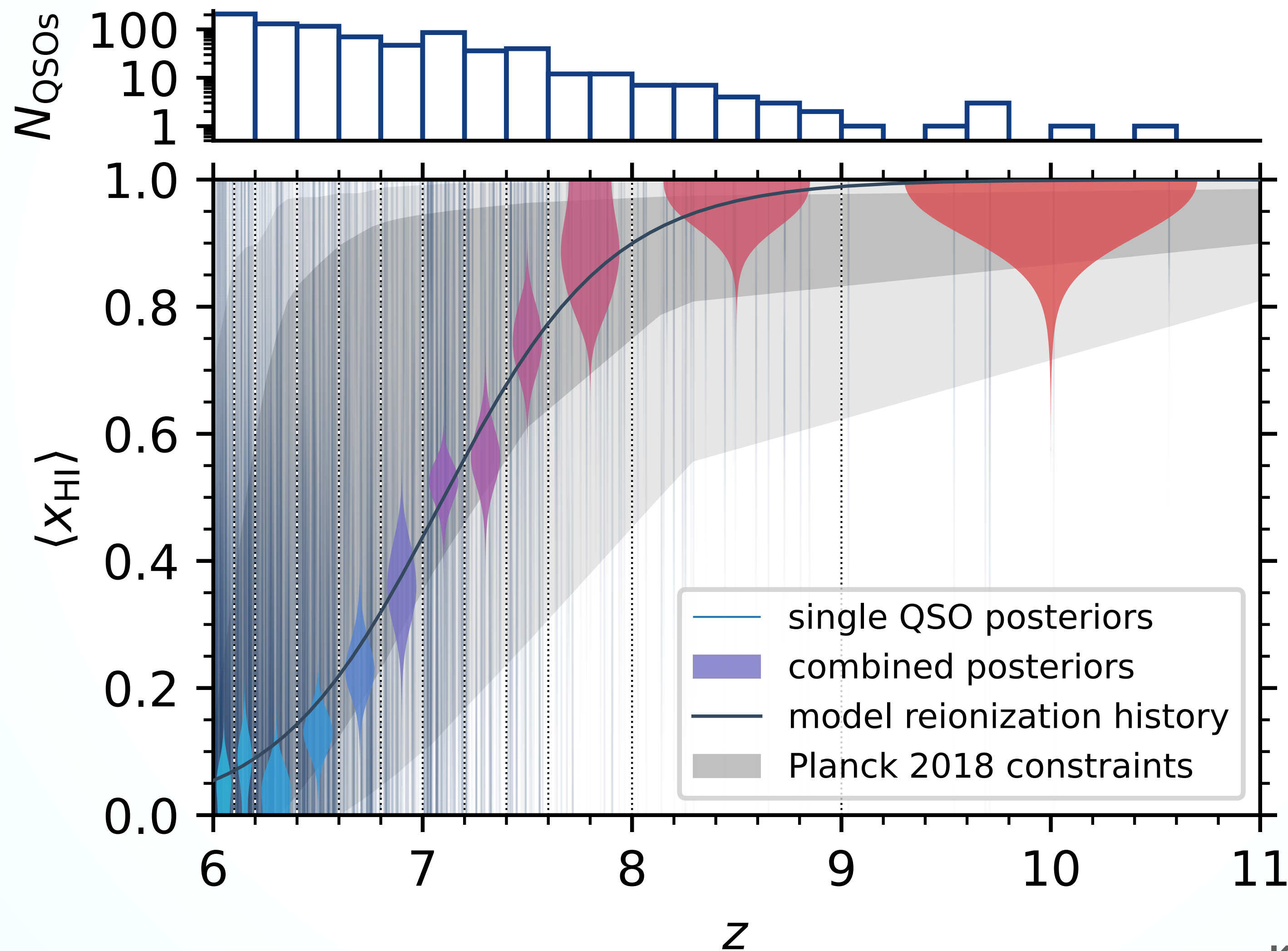
Constraining Reionization History with EUCLID & JWST

A forecast of upcoming IGM damping wing constraints



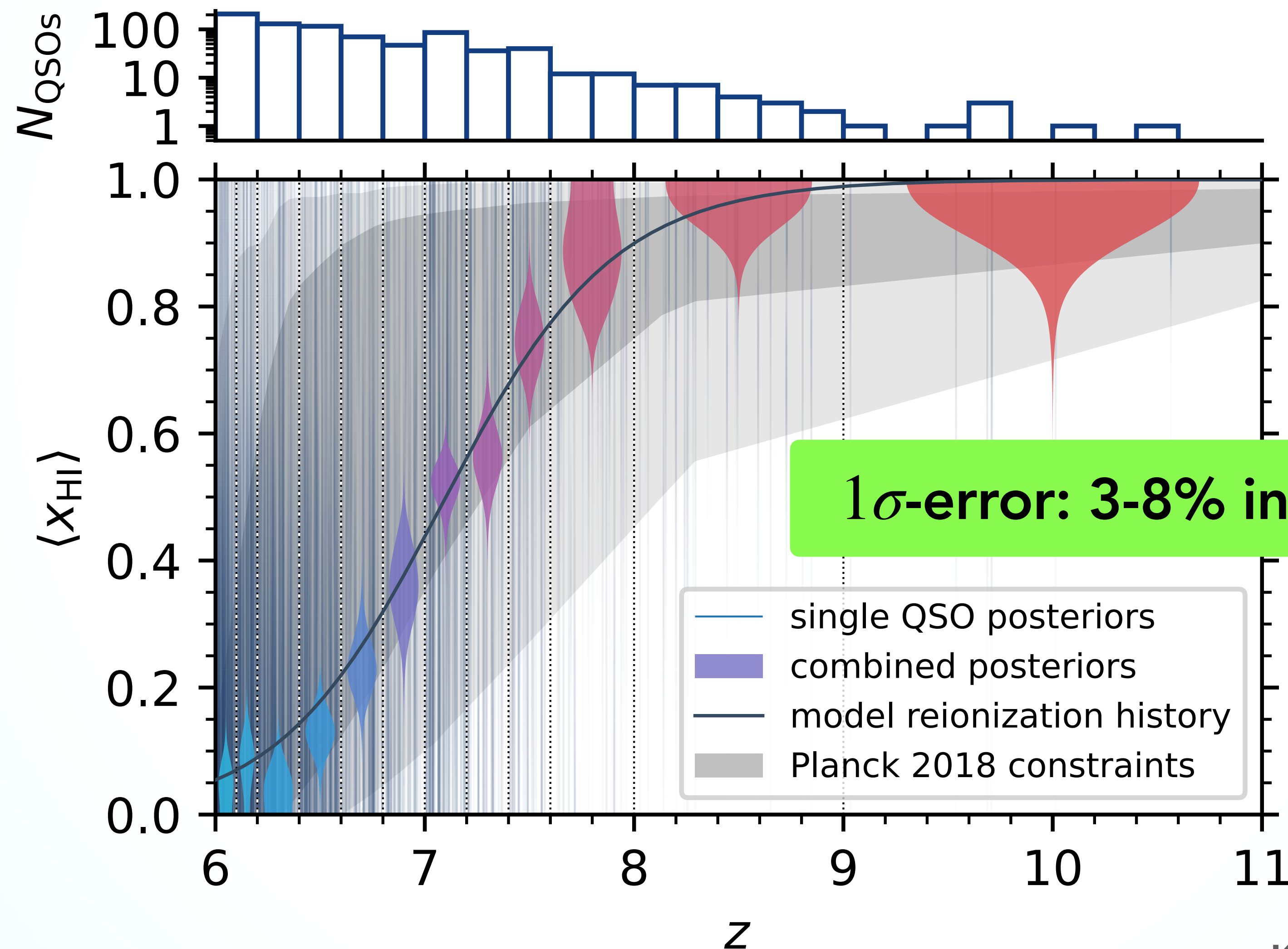
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Summary

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MODEL

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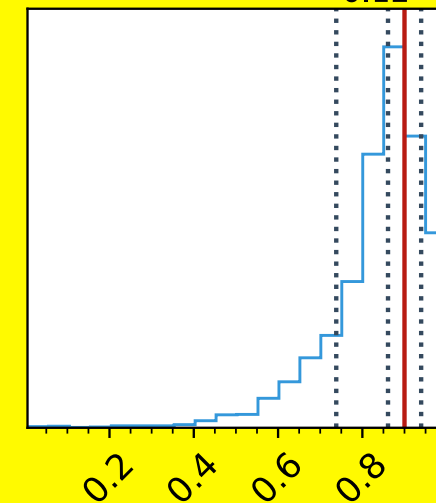
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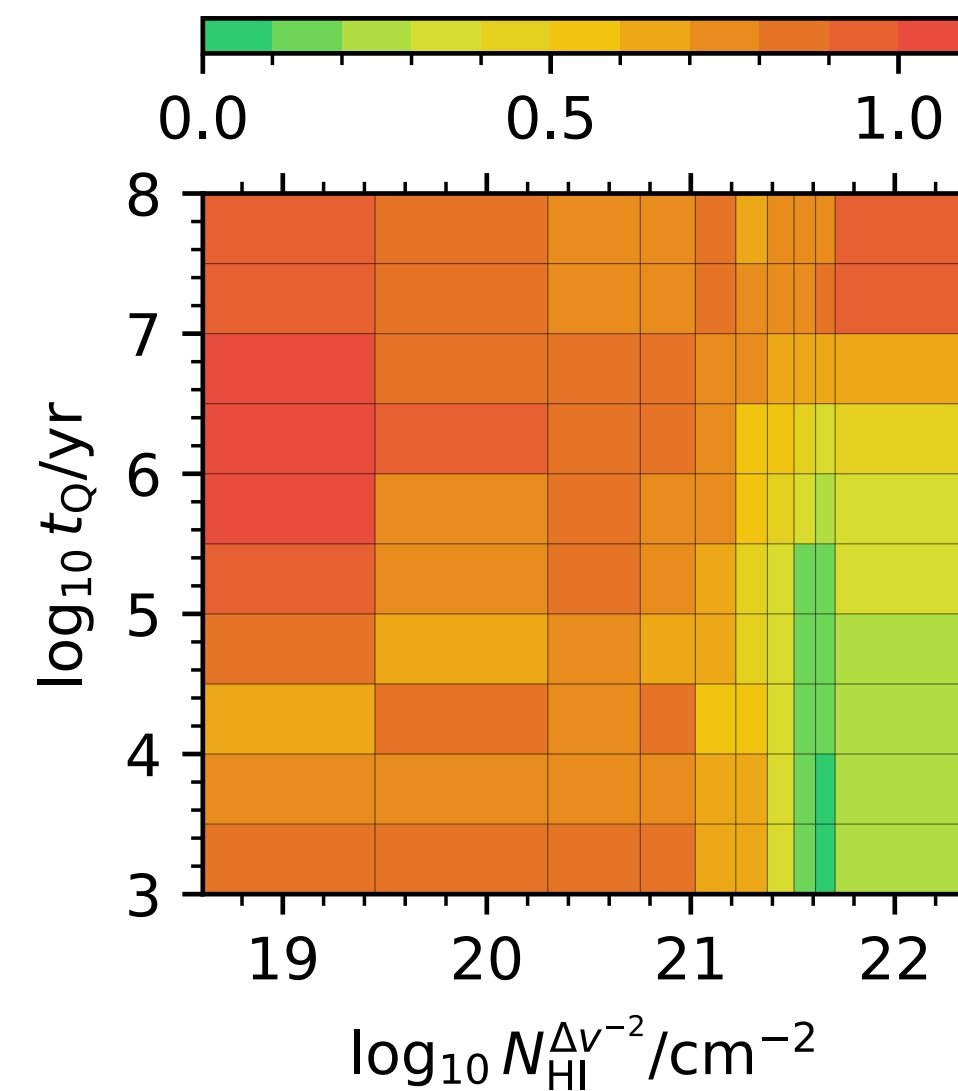
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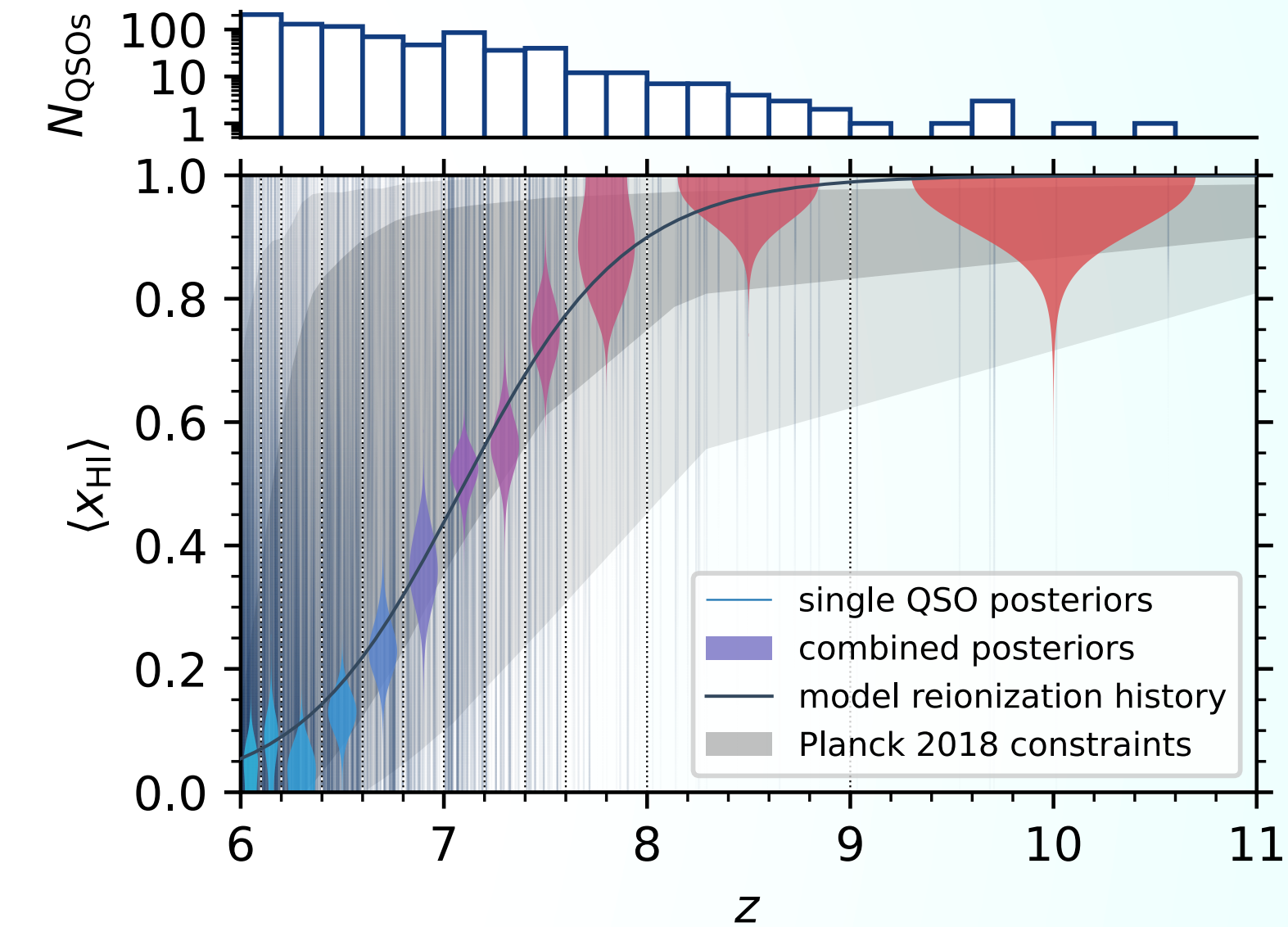


$\langle x_{\text{HI}} \rangle$



$\log_{10} t_{\text{Q}}/\text{yr}$

$\log_{10} N_{\text{HI}}^{\Delta_V^{-2}}/\text{cm}^{-2}$



Fast HMC pipeline to infer $\langle x_{\text{HI}} \rangle$ and t_{Q} using the damping wing imprint of high-redshift quasars

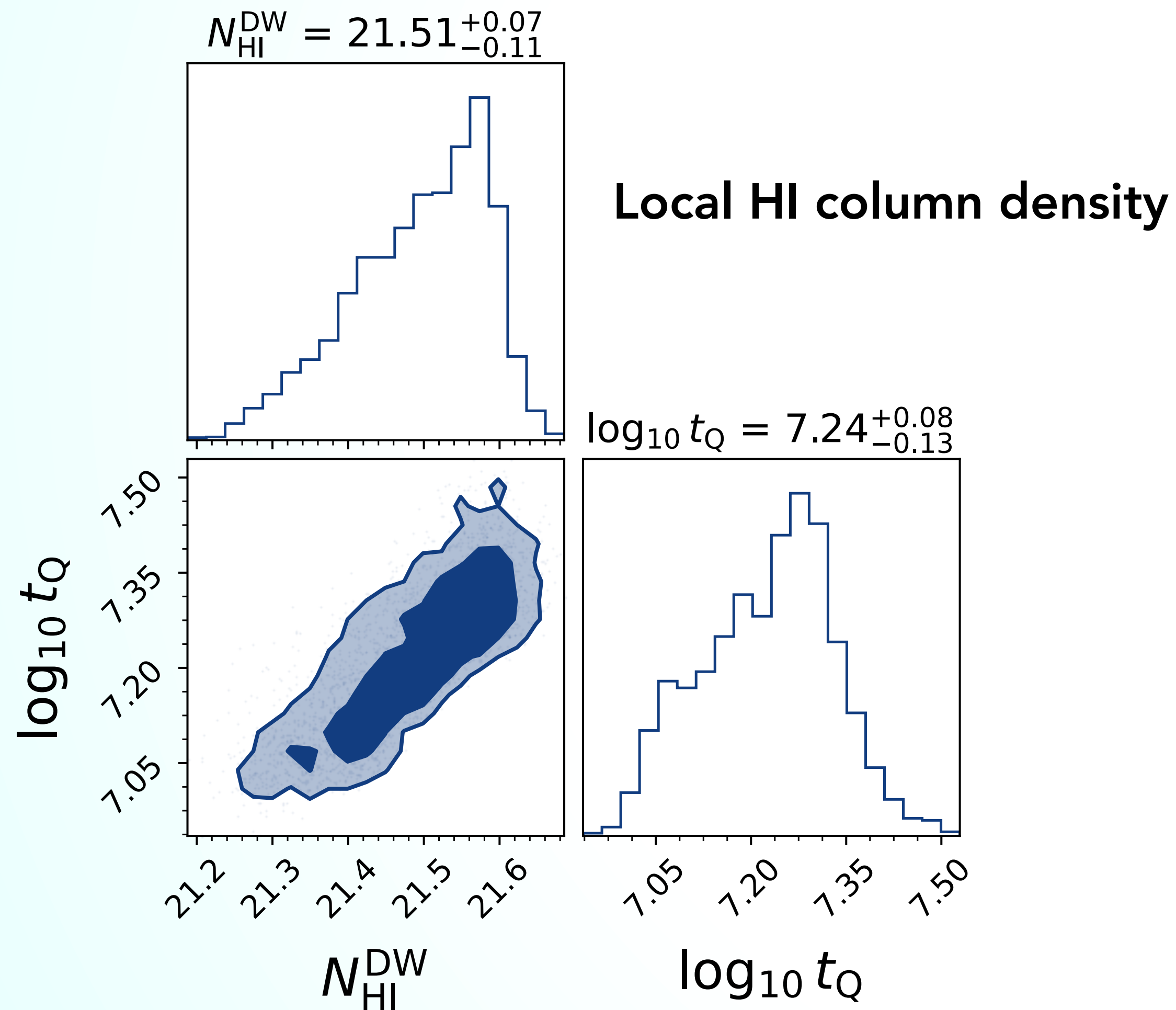
Inferring $\langle x_{\text{HI}} \rangle$ at $28.0^{+8.2}_{-8.8} \%$ precision, or even the local HI column density at $0.69^{+0.34}_{-0.53}$ dex

EUCLID & JWST:
3-8% constraints on $\langle x_{\text{HI}} \rangle(z)$ between $6 \lesssim z \lesssim 11$

Backup Slides

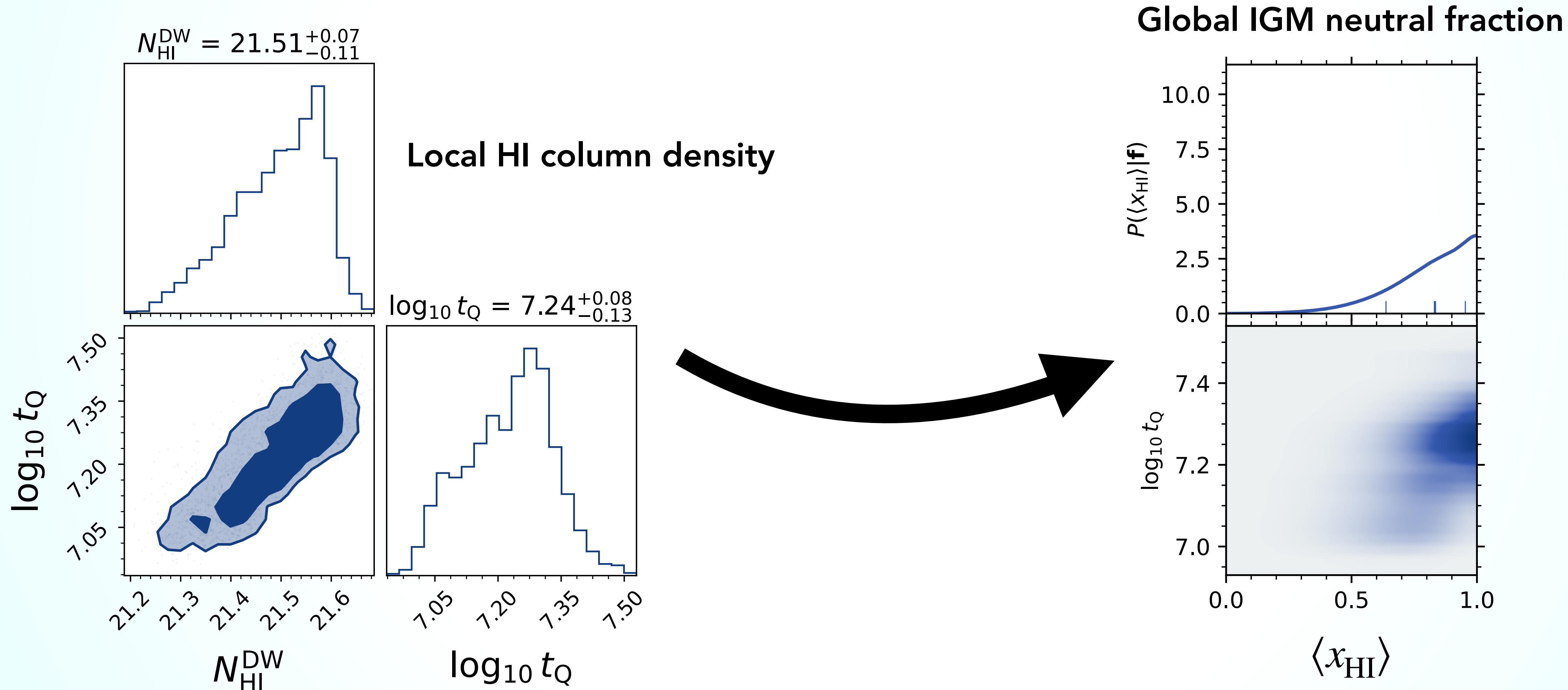
Converting the constraints

The *global* IGM neutral fraction inferred from J0411-0907



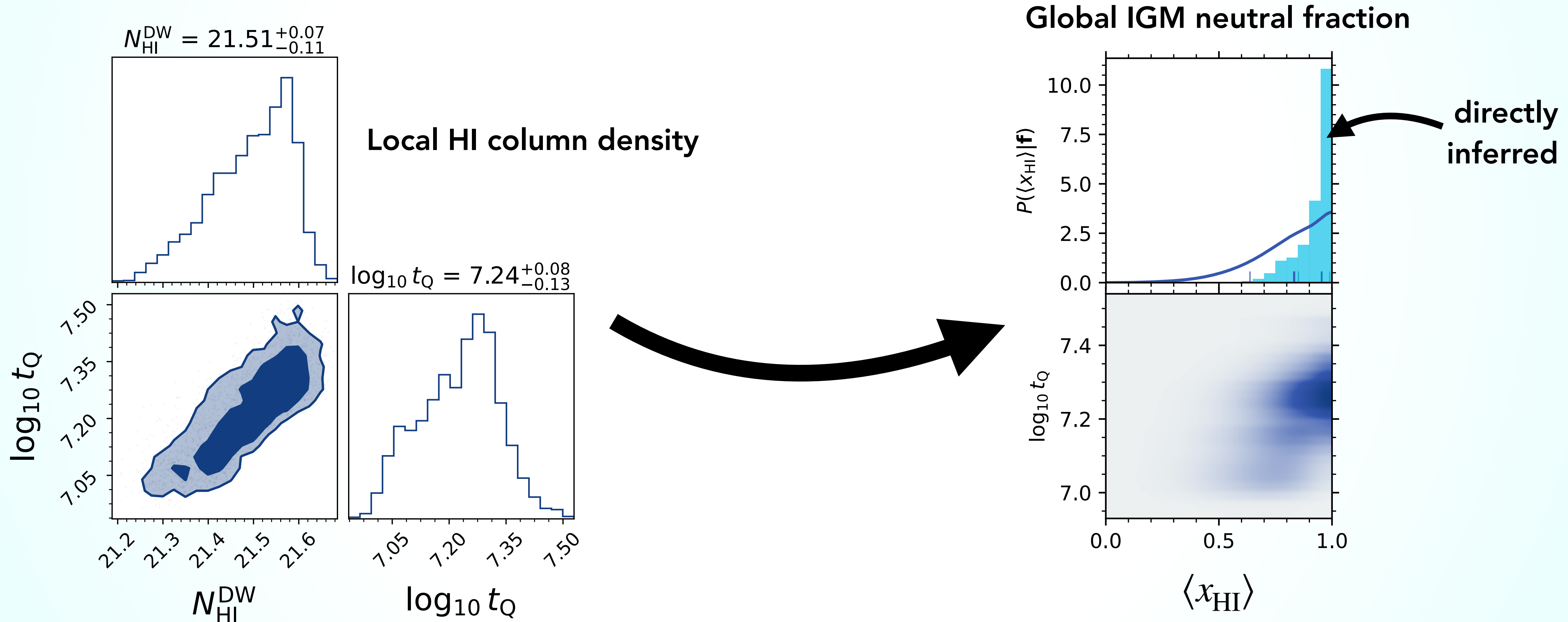
Converting the constraints

The *global* IGM neutral fraction inferred from J0411-0907



Converting the constraints

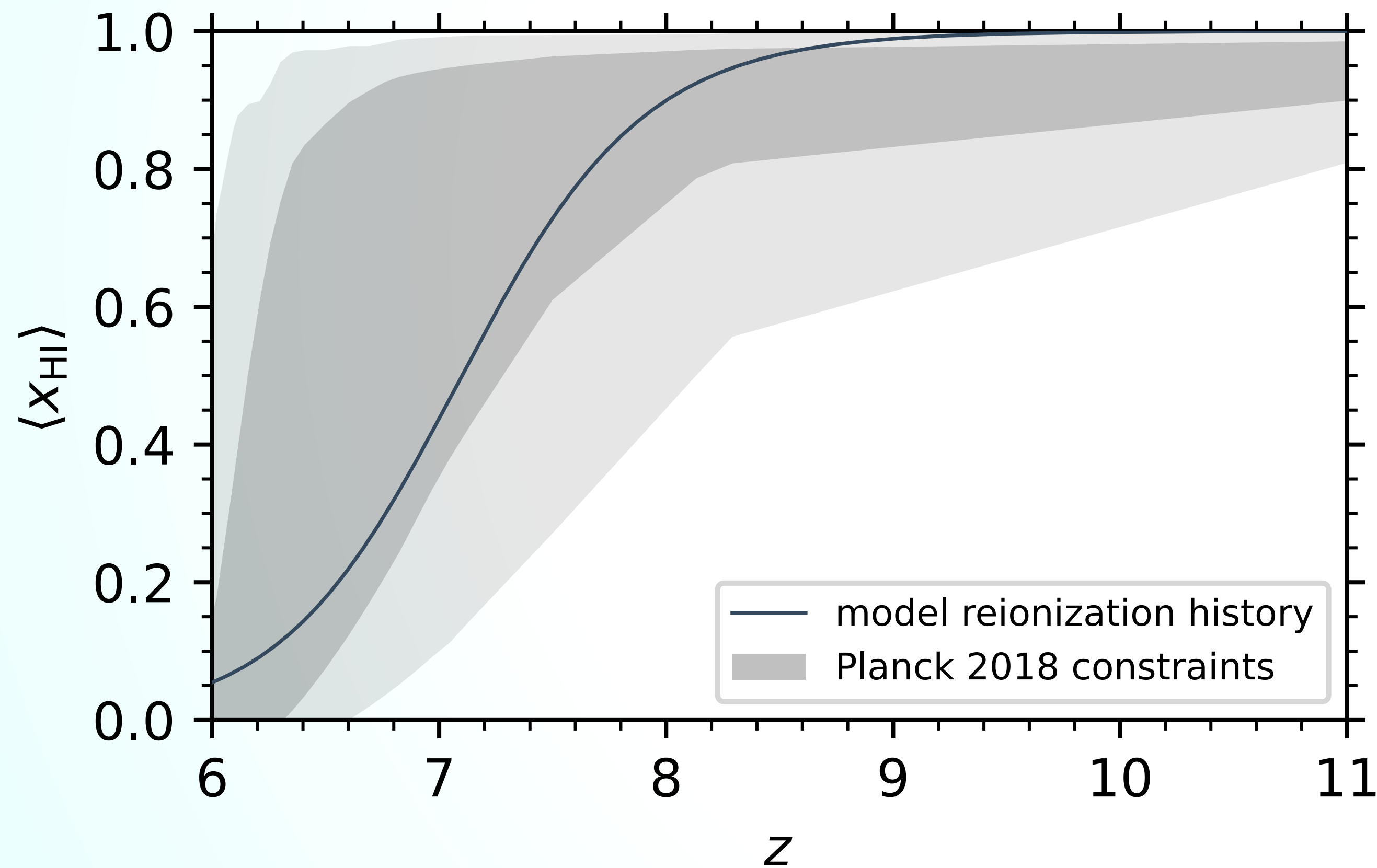
The *global* IGM neutral fraction inferred from J0411-0907



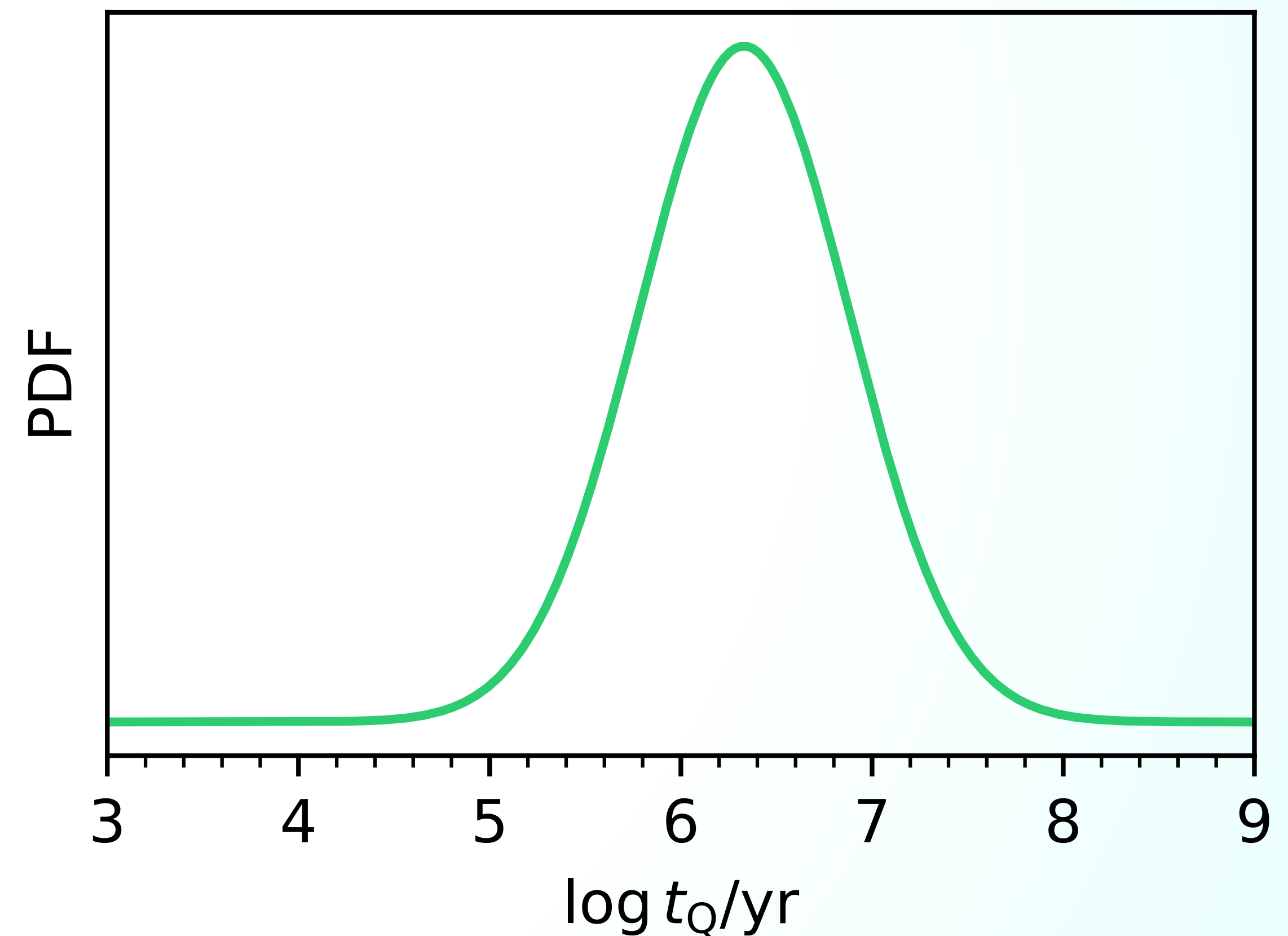
Constraining Reionization History with EUCLID & JWST

A forecast of upcoming IGM damping wing constraints

Toy model for $\langle x_{\text{HI}} \rangle(z)$



Lognormal t_Q distribution (Khrykin+ 2021)

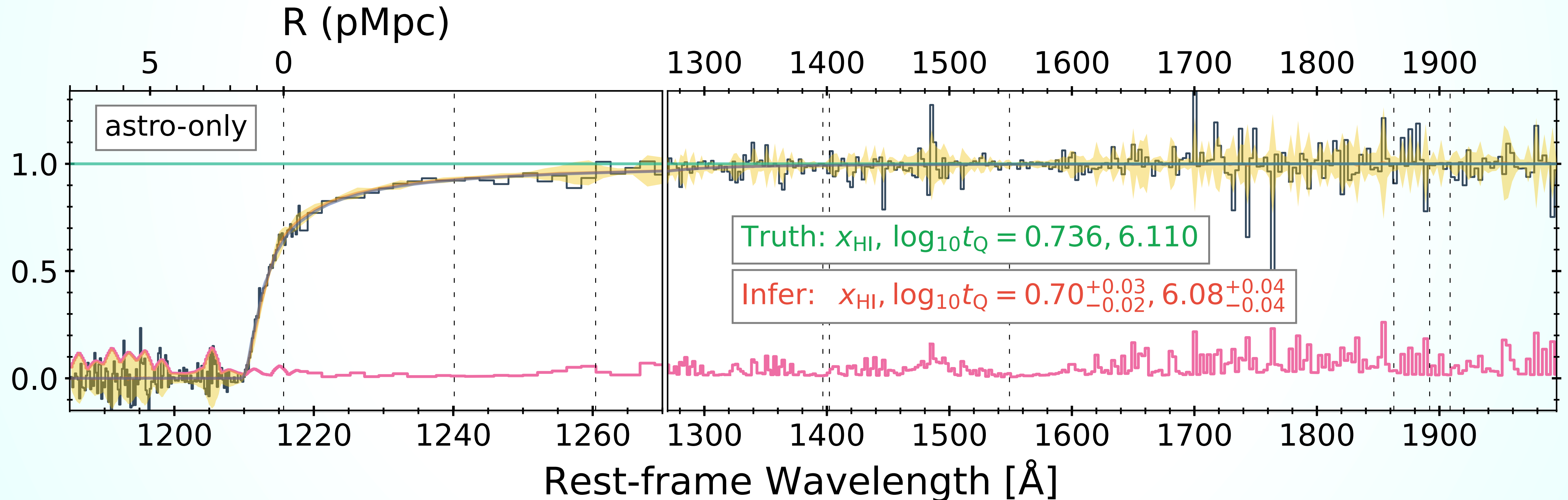


The PCA Continuum Model

Impact on Inference Precision

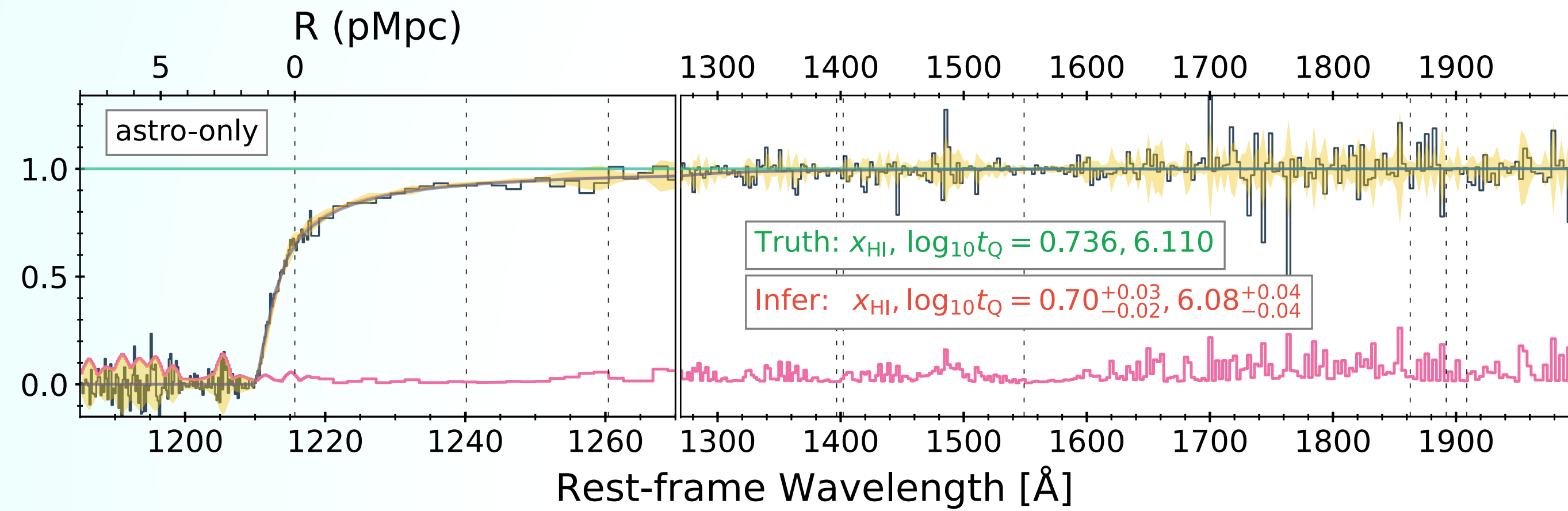
Continuum-normalized spectrum:

→ optimal bound on inferring $\langle x_{\text{HI}} \rangle$ and t_{Q} without nuisance parameters



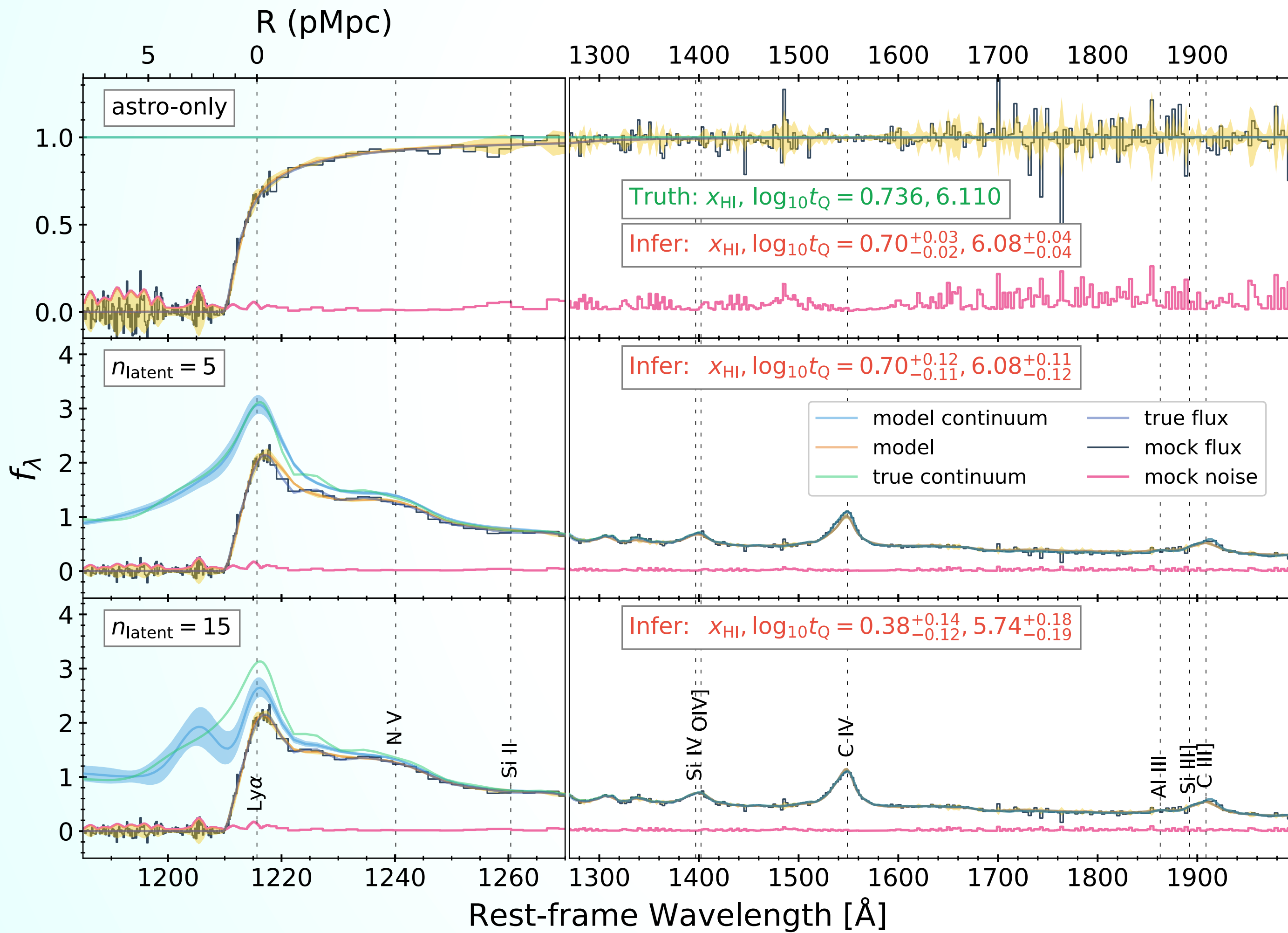
The PCA Continuum Model

Impact on Inference Precision



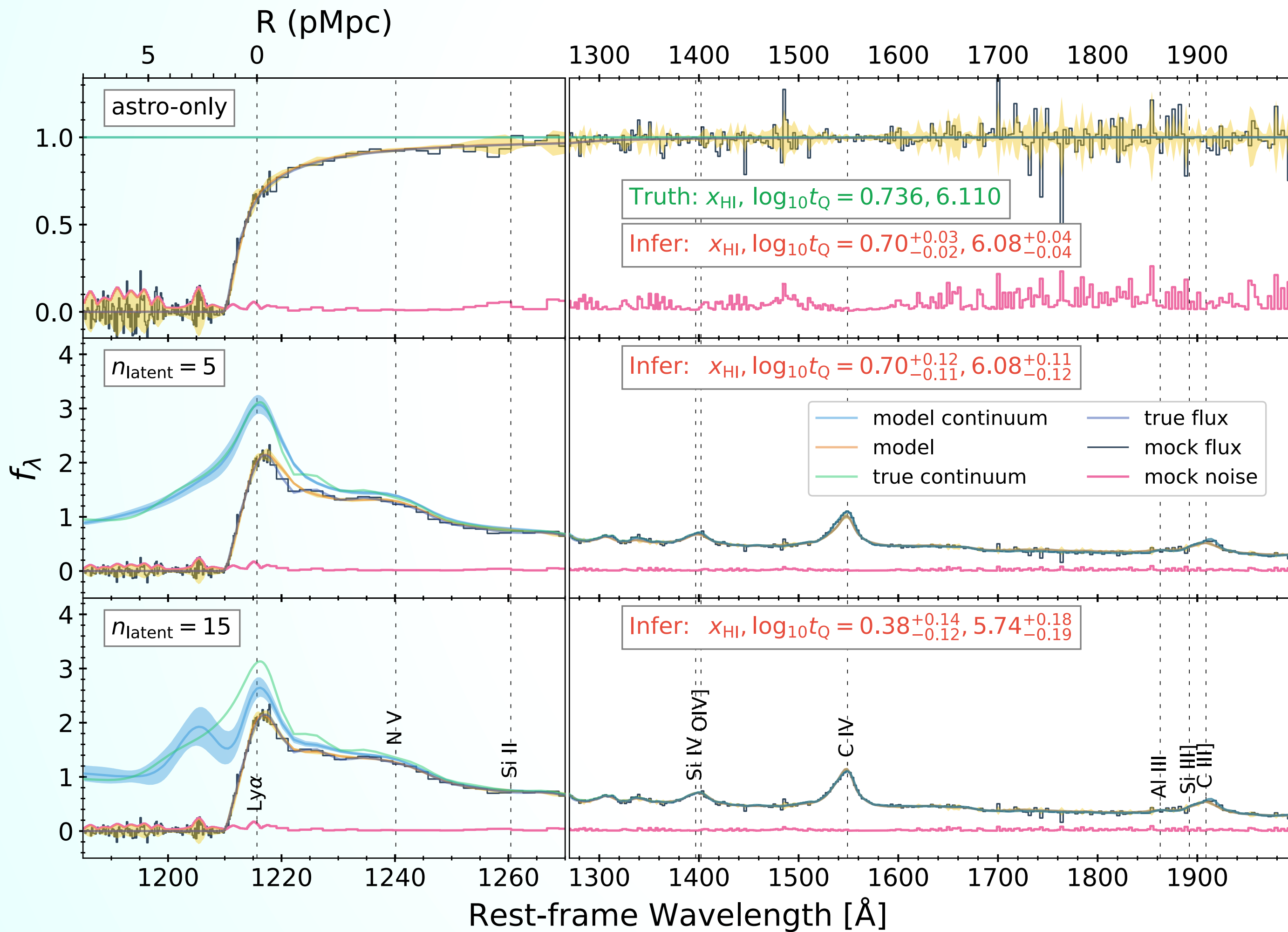
The PCA Continuum Model

Impact on Inference Precision

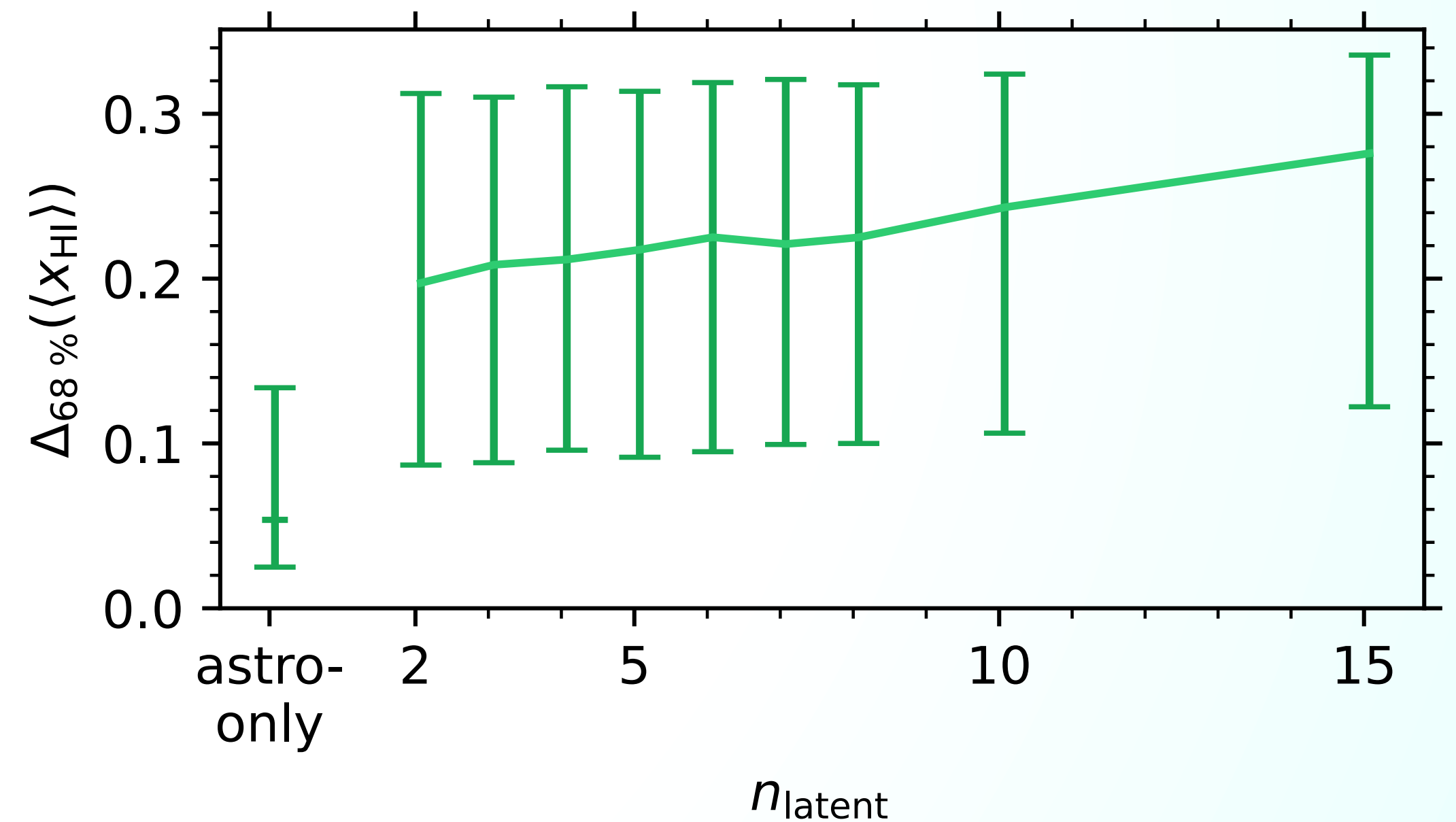


The PCA Continuum Model

Impact on Inference Precision

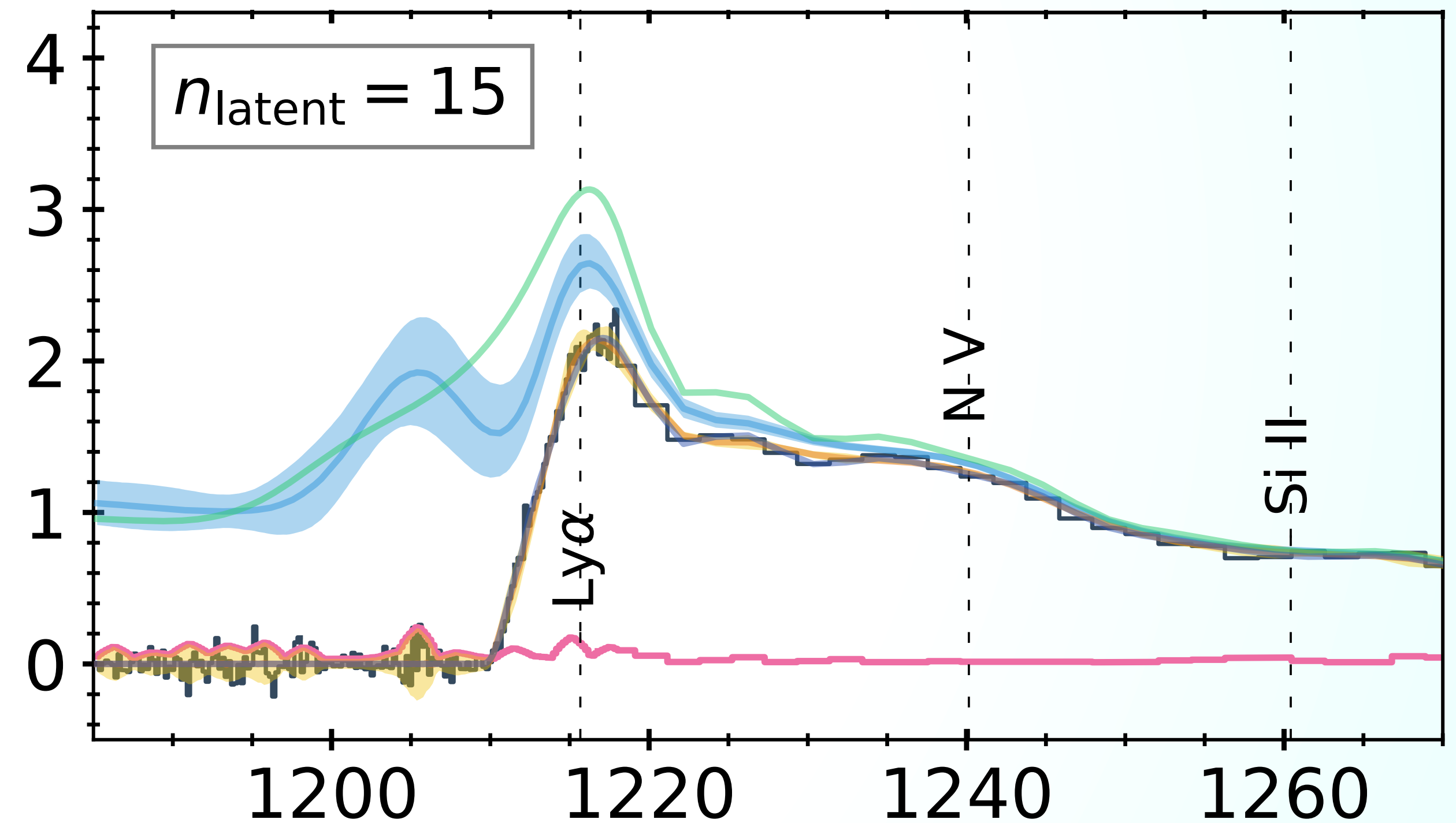


Average precision of 100 mock samples:



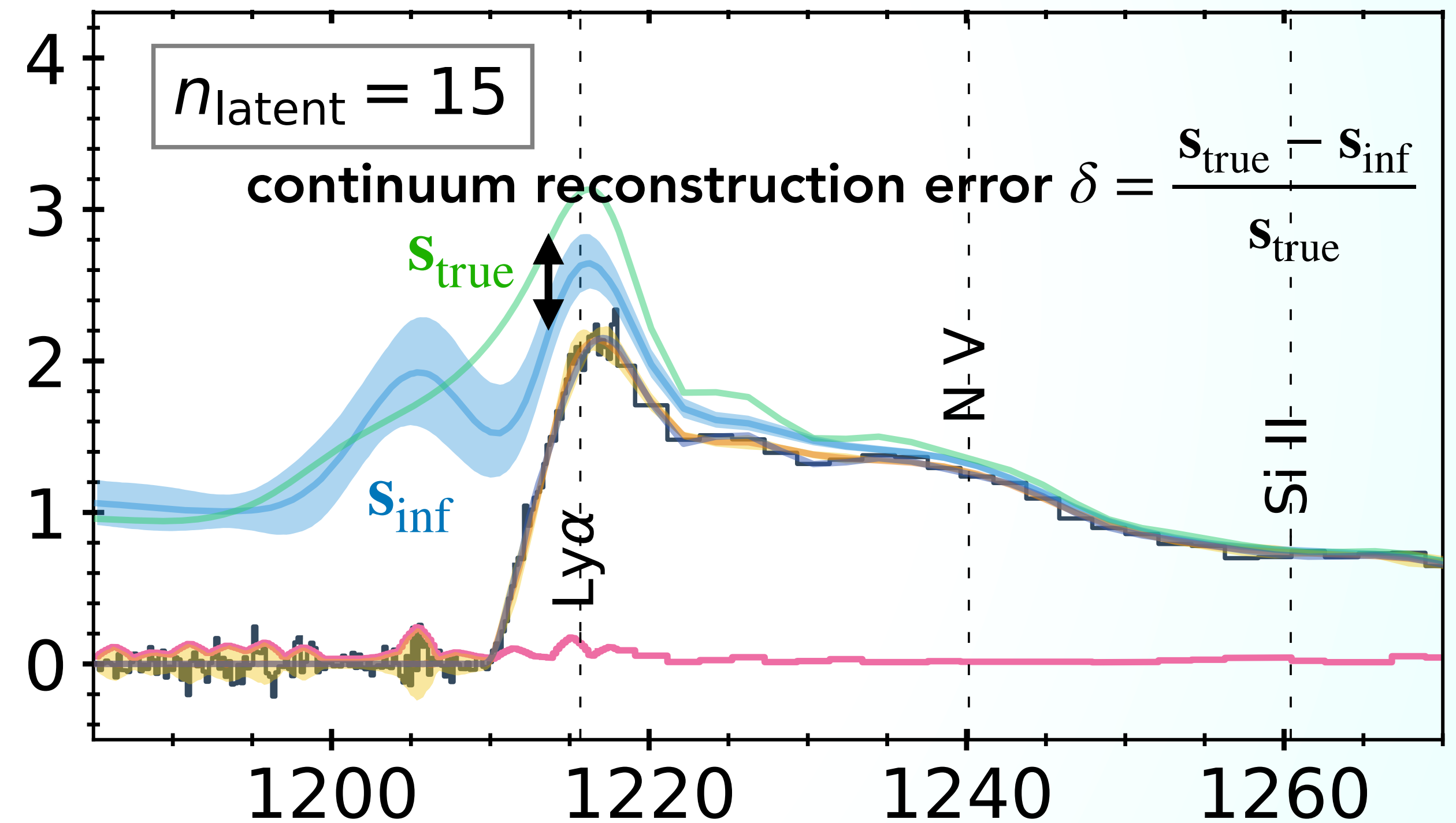
The PCA Continuum Model

Impact on Inference Precision



The PCA Continuum Model

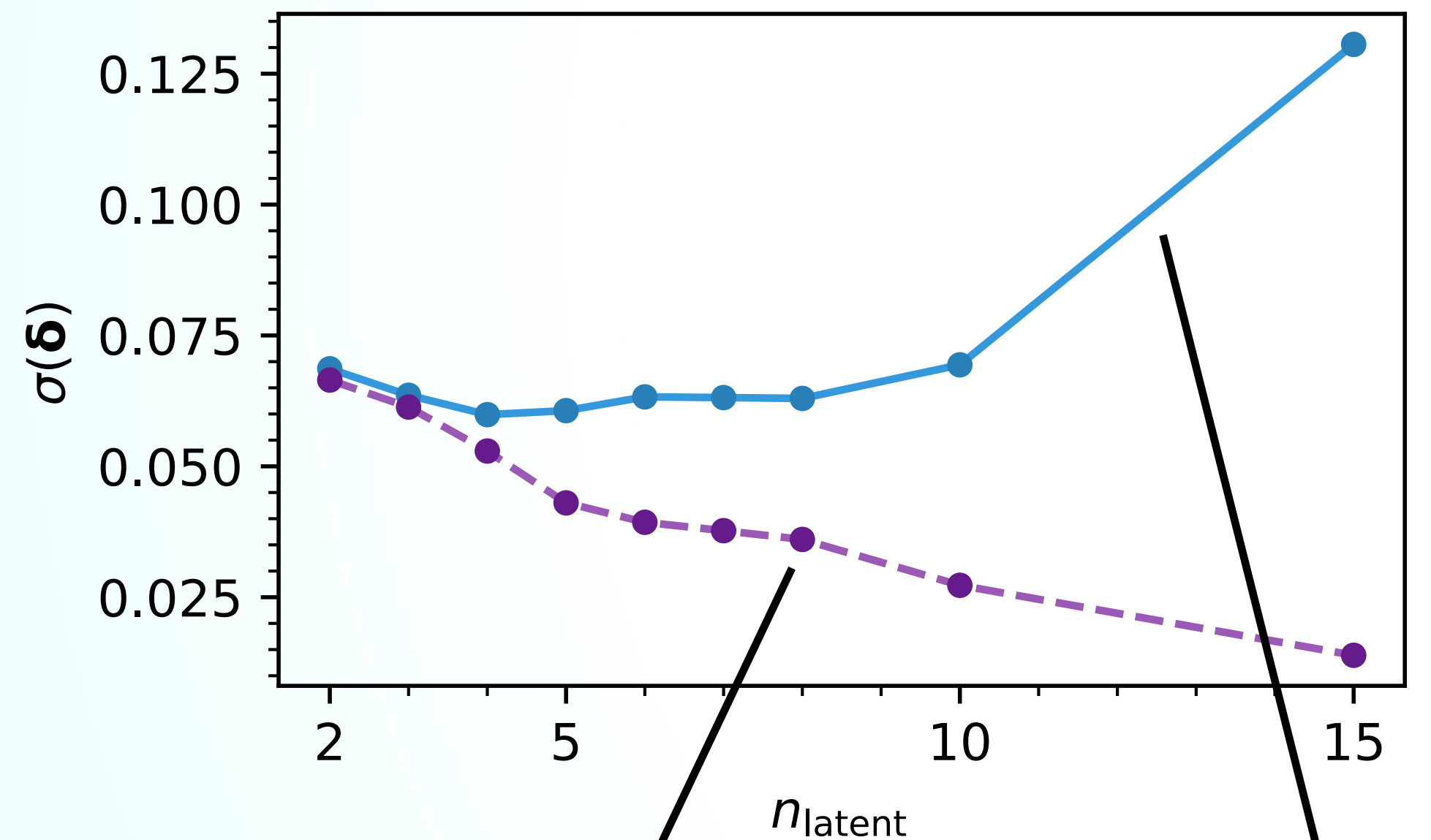
Impact on Inference Precision



The PCA Continuum Model

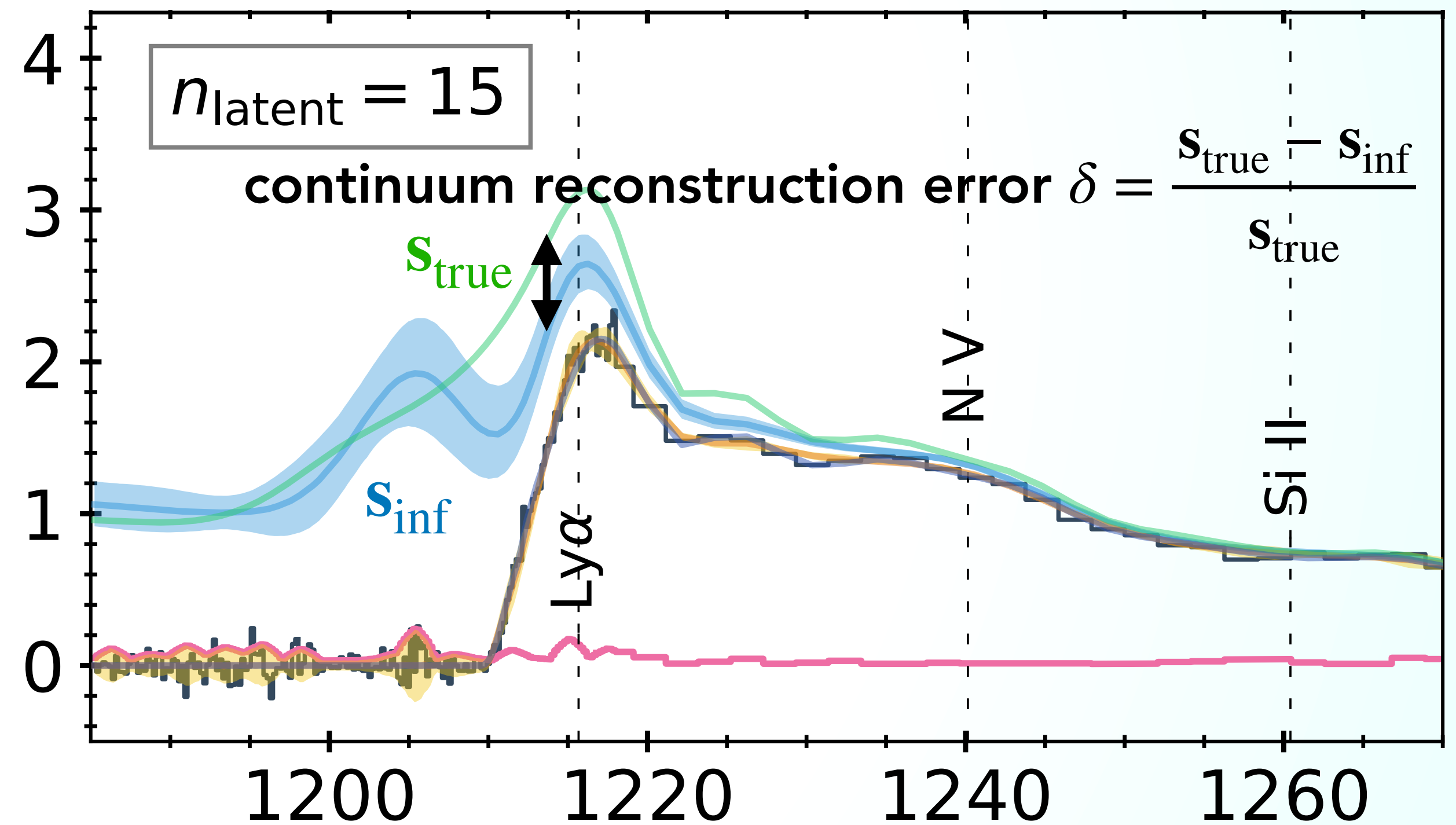
Impact on Inference Precision

Variation of the continuum reconstruction error w.r.t. 100 mock samples



pure continuum fitting error

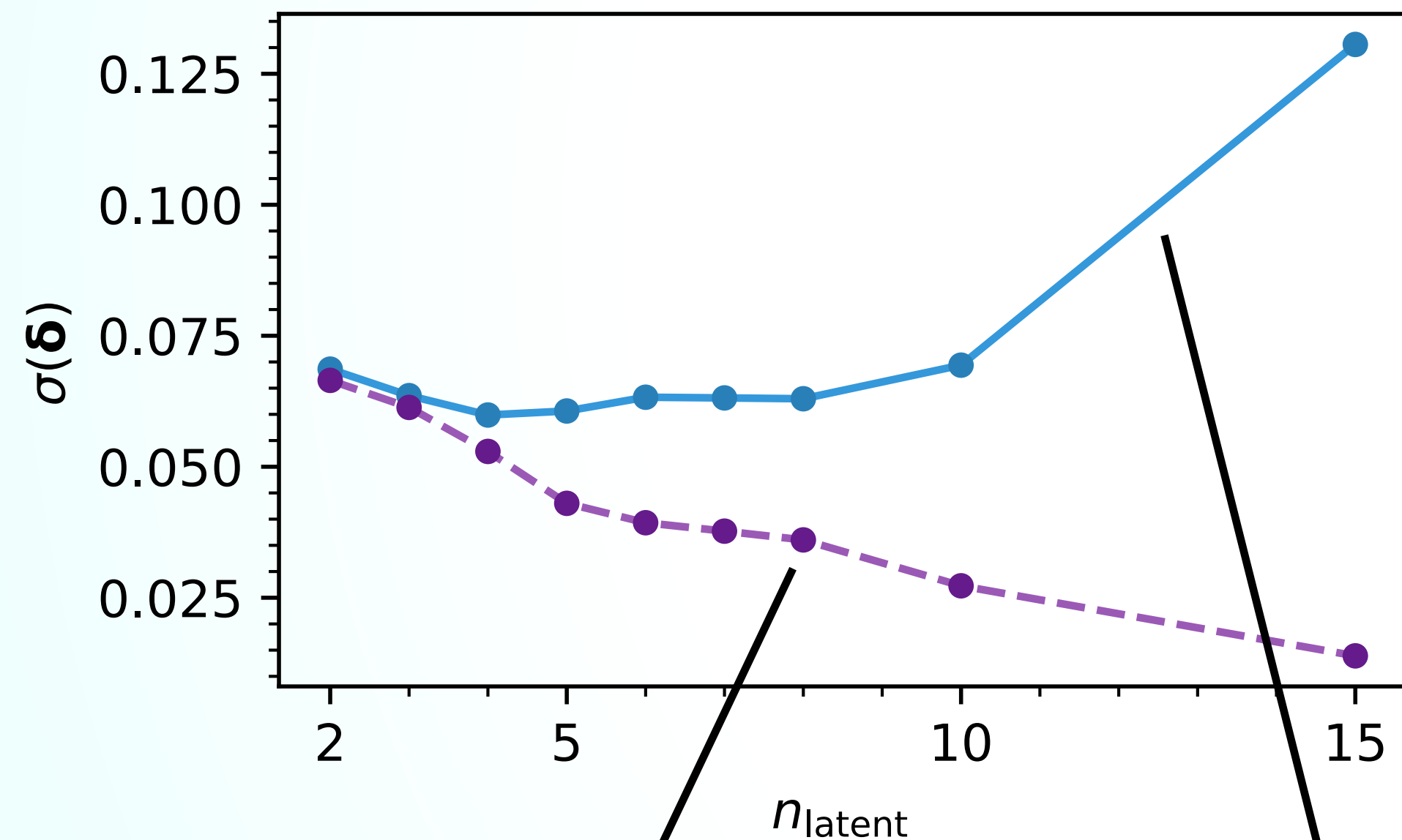
inferred continuum error



The PCA Continuum Model

Impact on Inference Precision

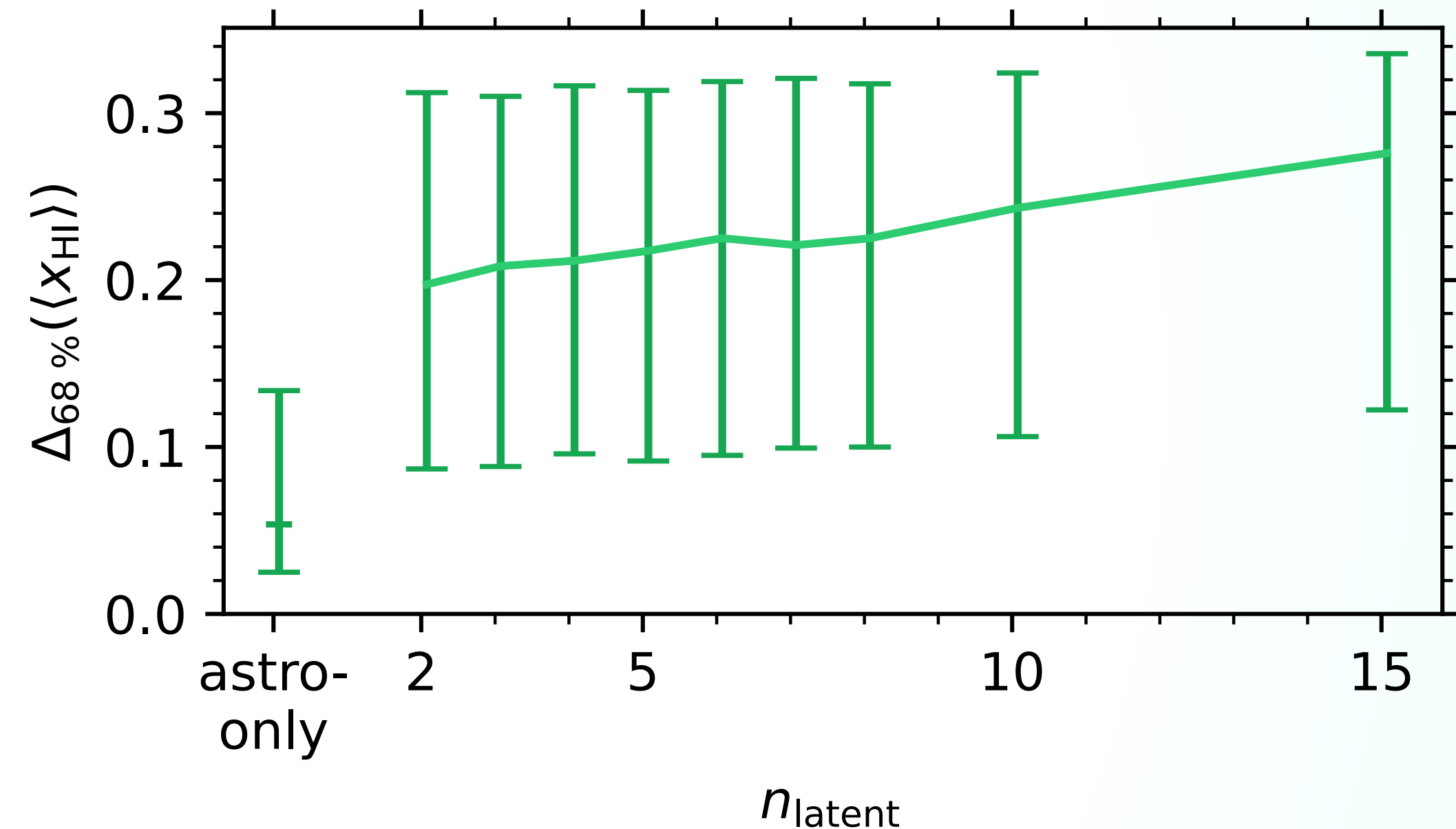
Variation of the continuum reconstruction error w.r.t. 100 mock samples



pure continuum fitting error

inferred continuum error

Average precision of 100 mock samples:

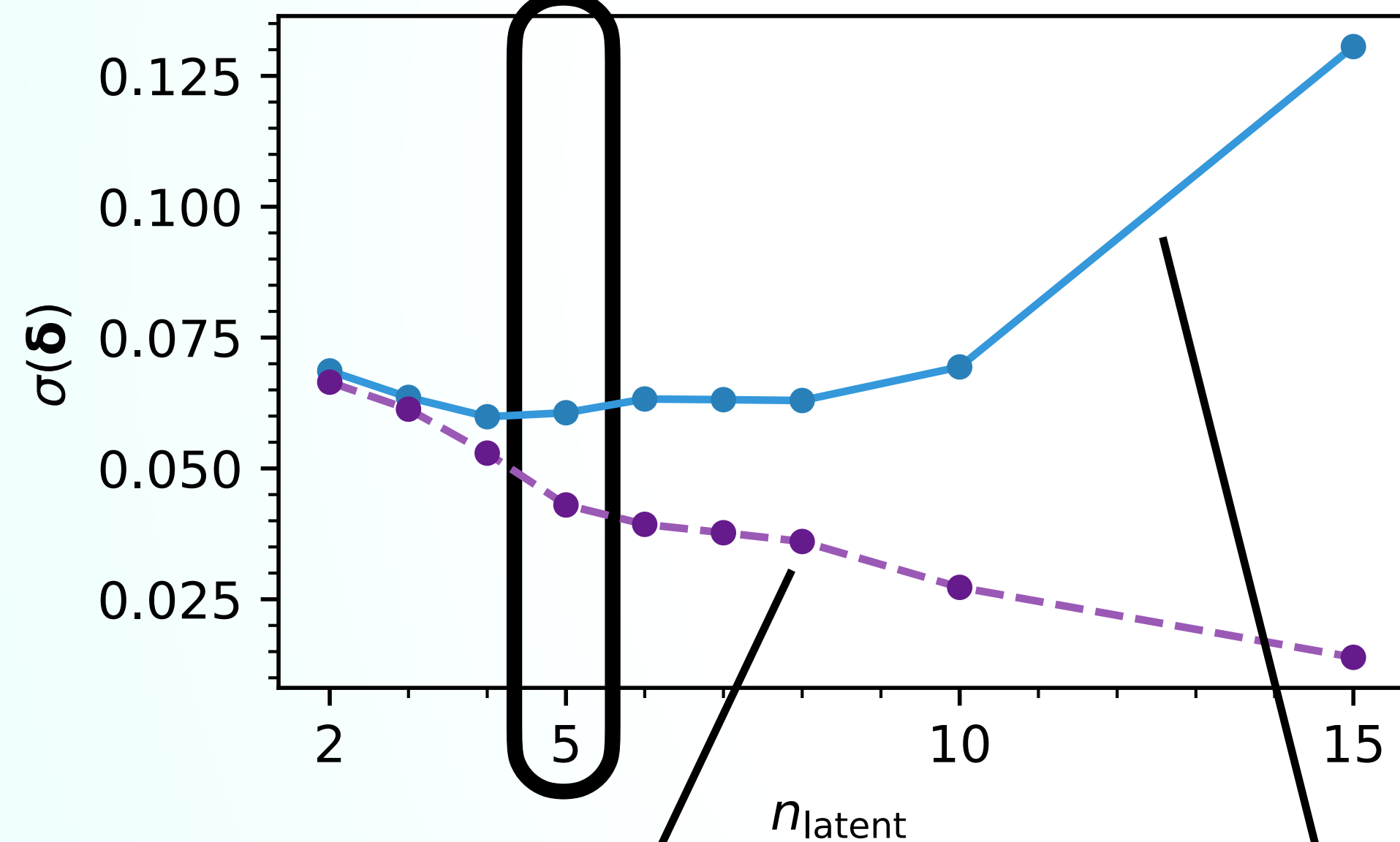


- All information about the Lyman- α forest is encoded in the first few PCA vectors
- Additional latent dimensions improve the continuum fit but lose constraining power

The PCA Continuum Model

Impact on Inference Precision

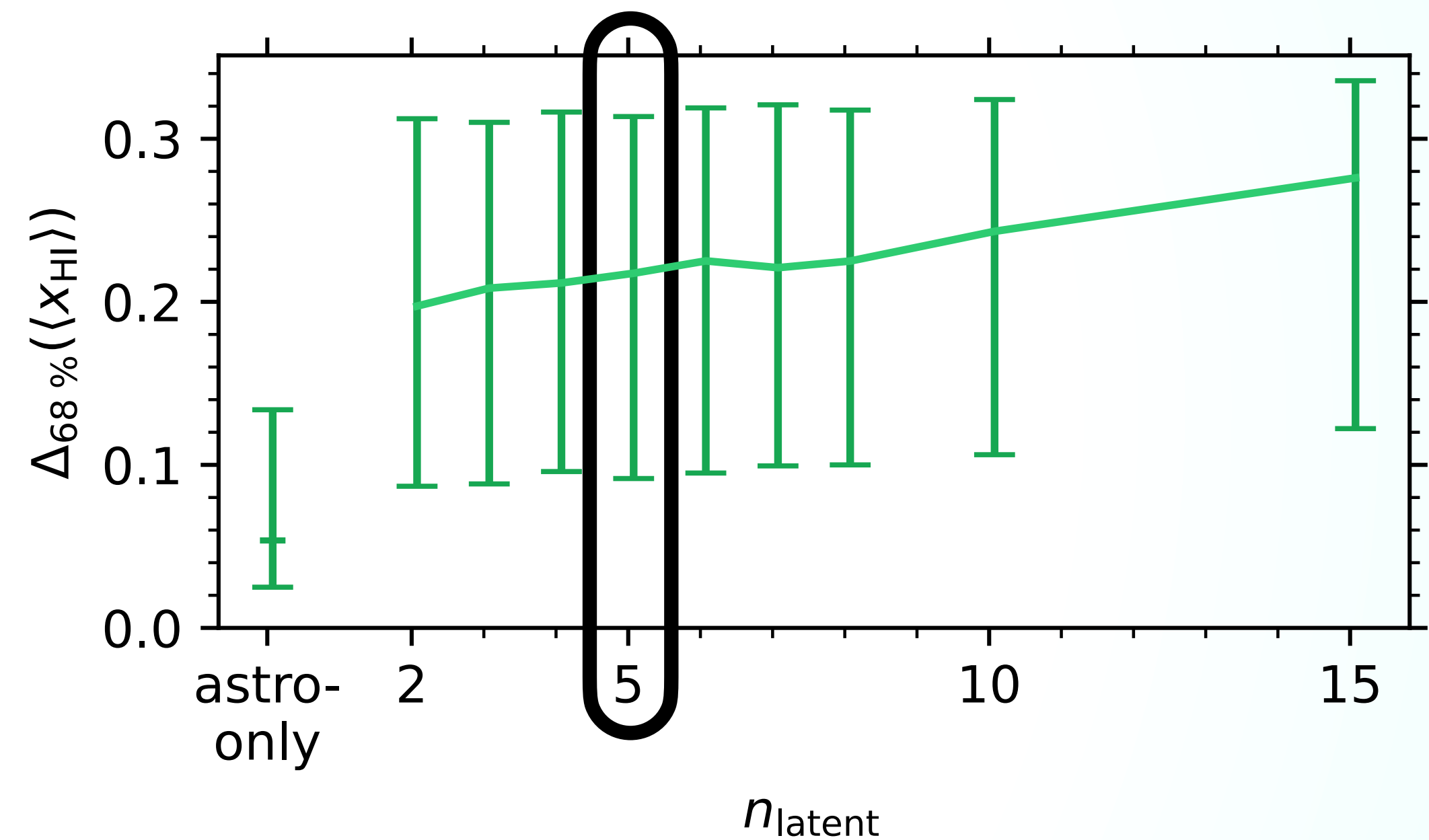
Variation of the continuum reconstruction error w.r.t. 100 mock samples



pure continuum fitting error

inferred continuum error

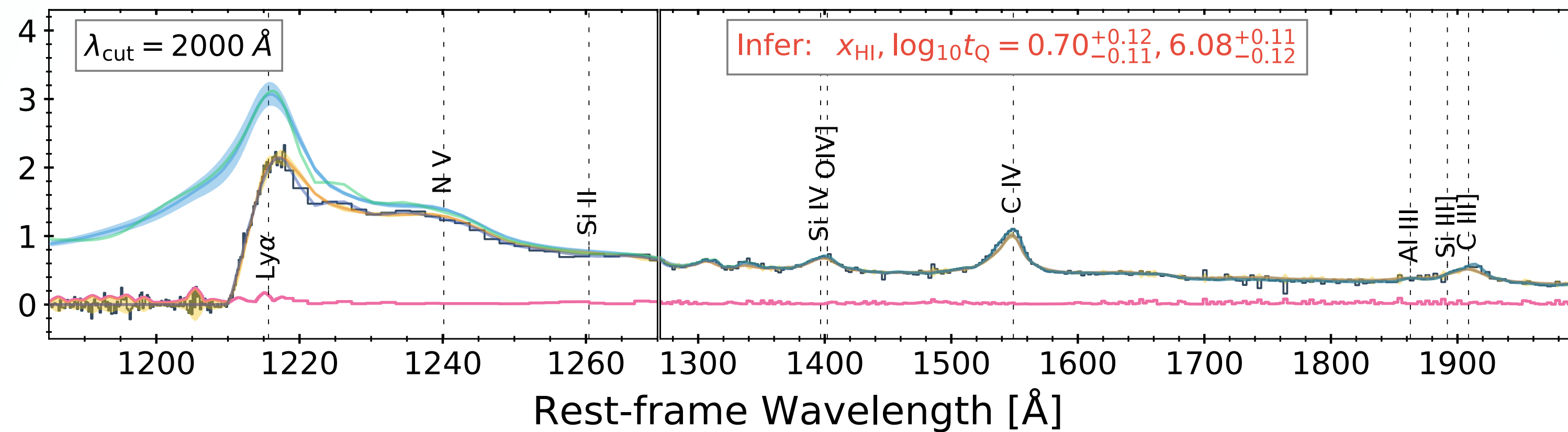
Average precision of 100 mock samples:



- All information about the Lyman- α forest is encoded in the first few PCA vectors
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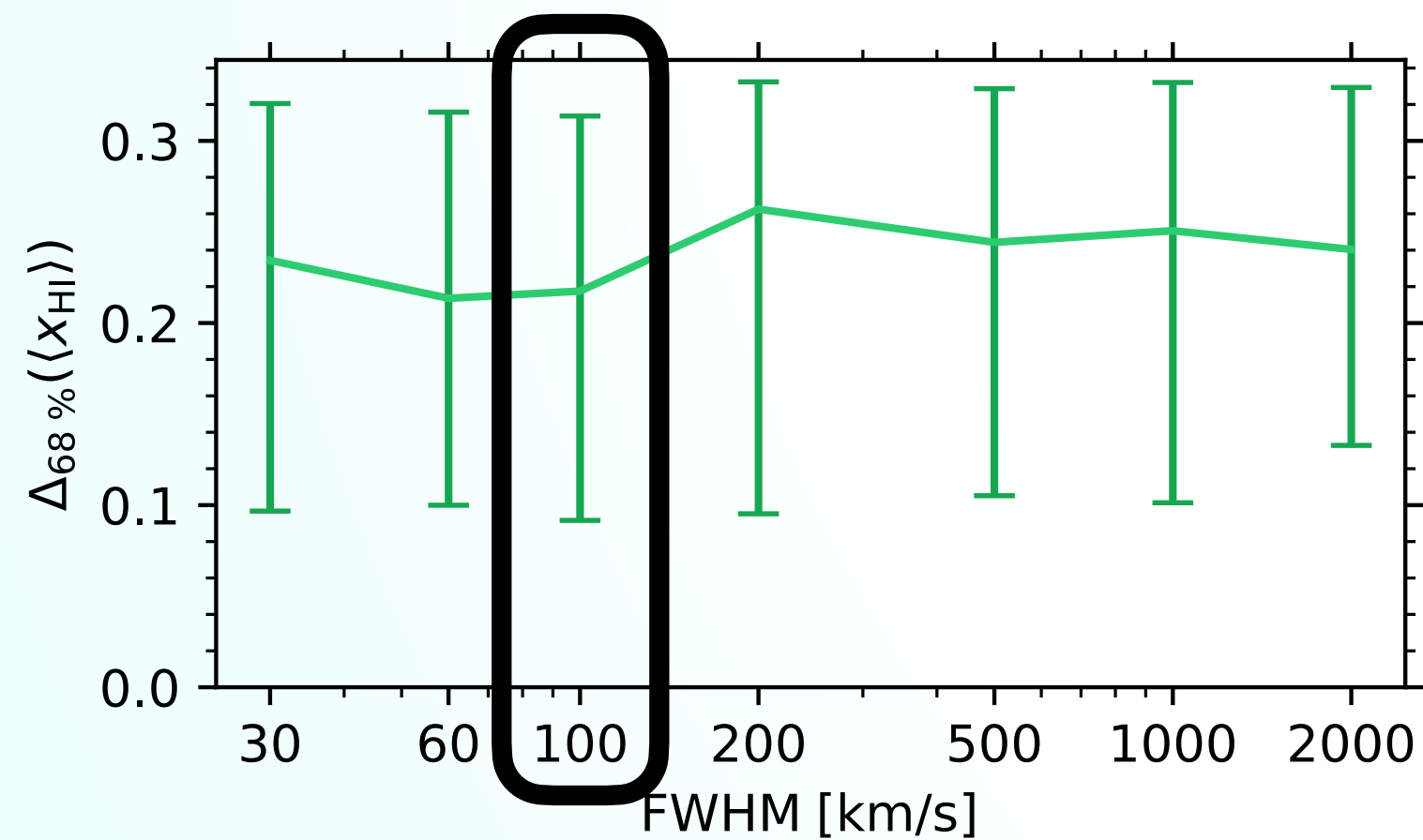
Observational Setup

Impact on Inference Precision



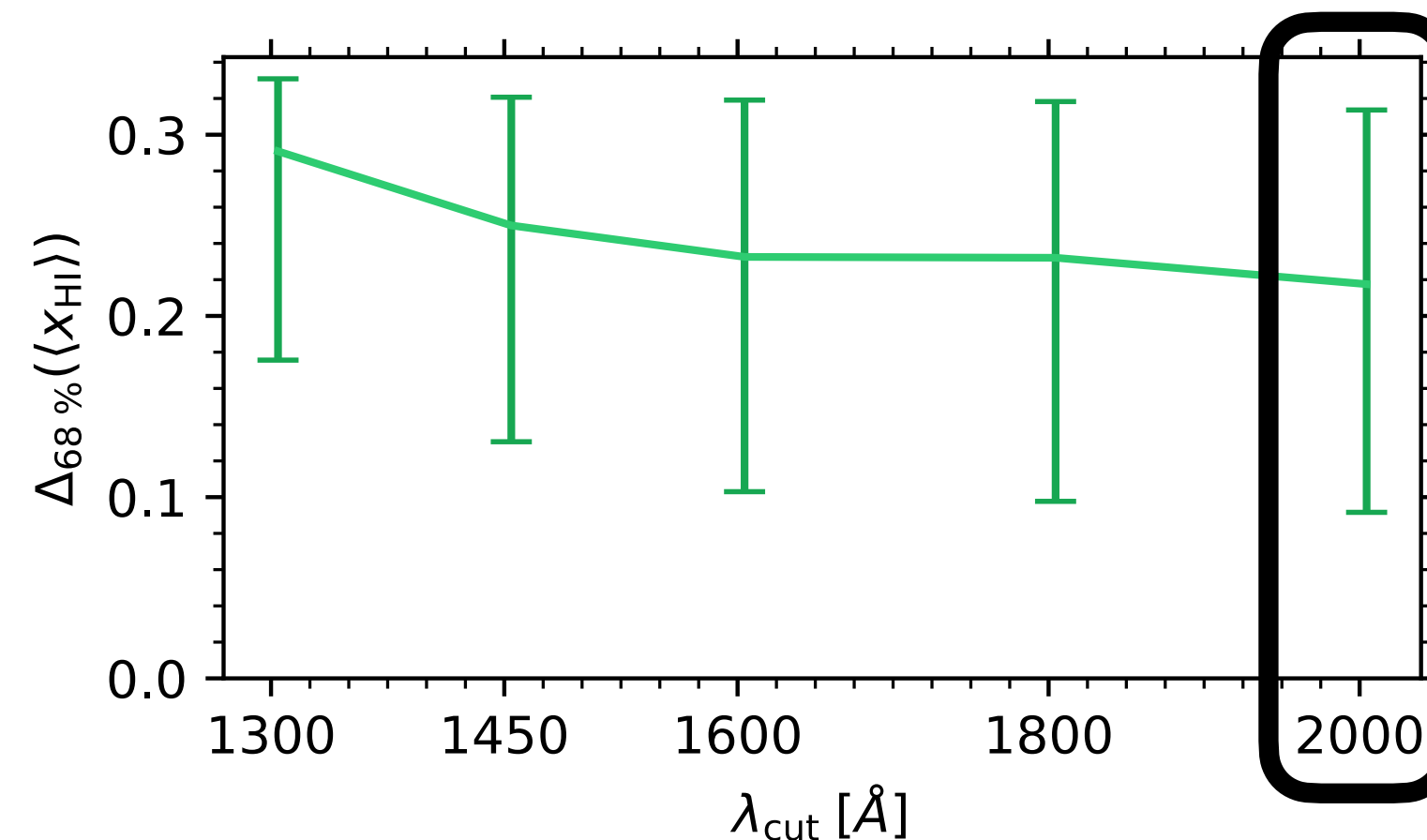
Hennawi, Kist, Davies+ 2023a
(in prep.)

Spectral resolution



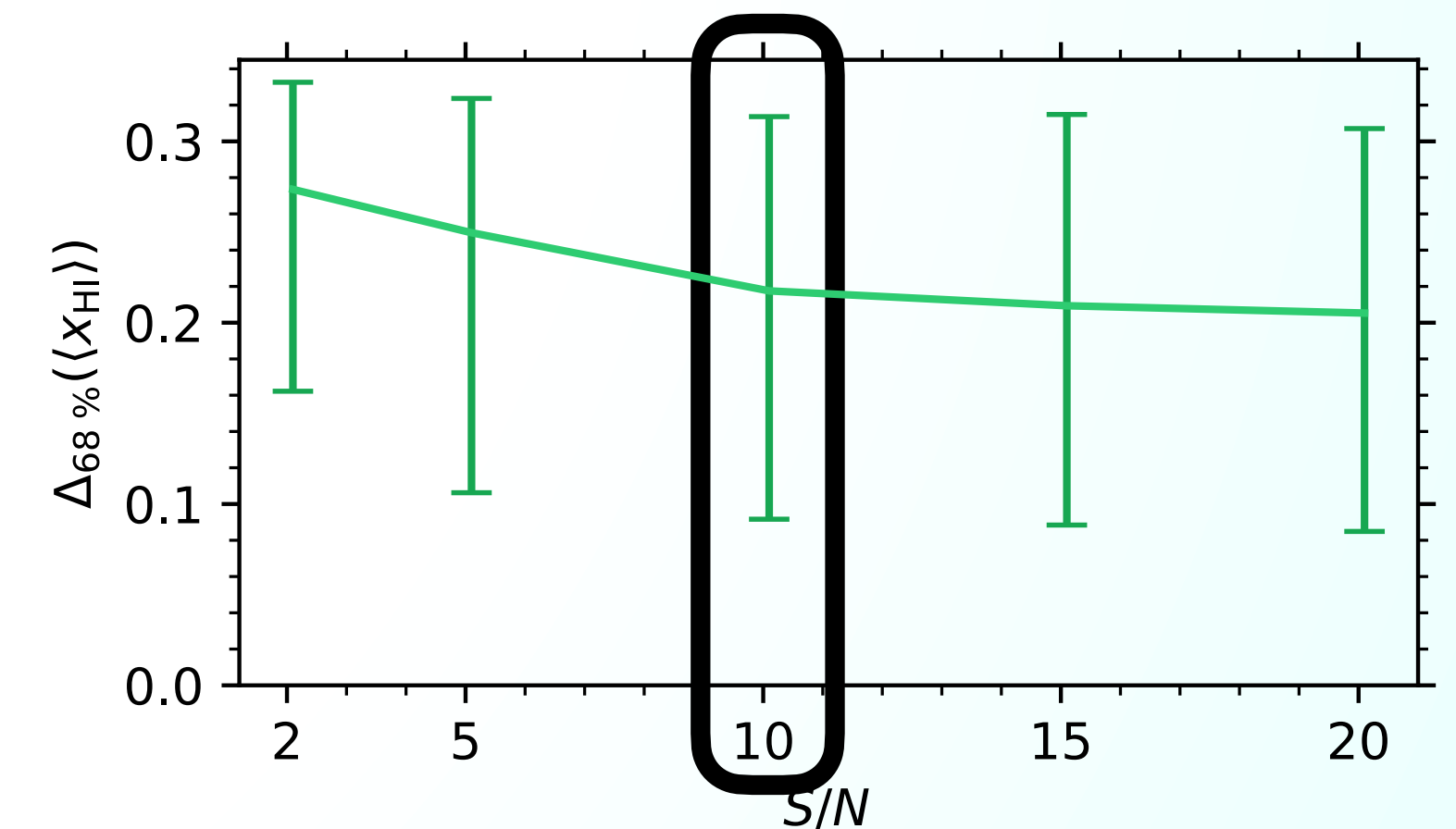
→ Precision does not vary significantly with spectral resolution

Red-side wavelength coverage



→ Covering major emission lines is important

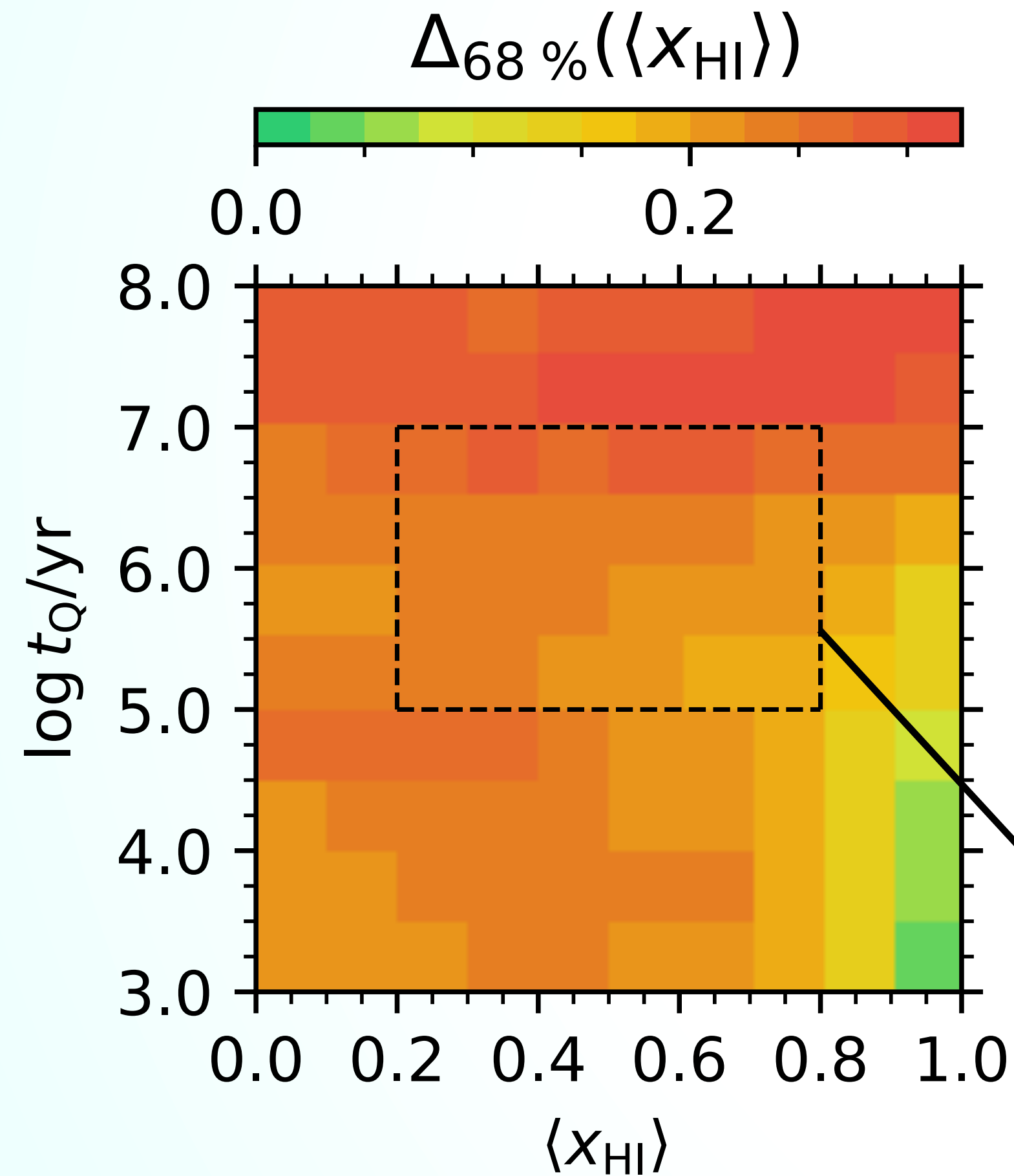
S/N per 100 km/s velocity interval



→ Covering major emission lines is important

Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

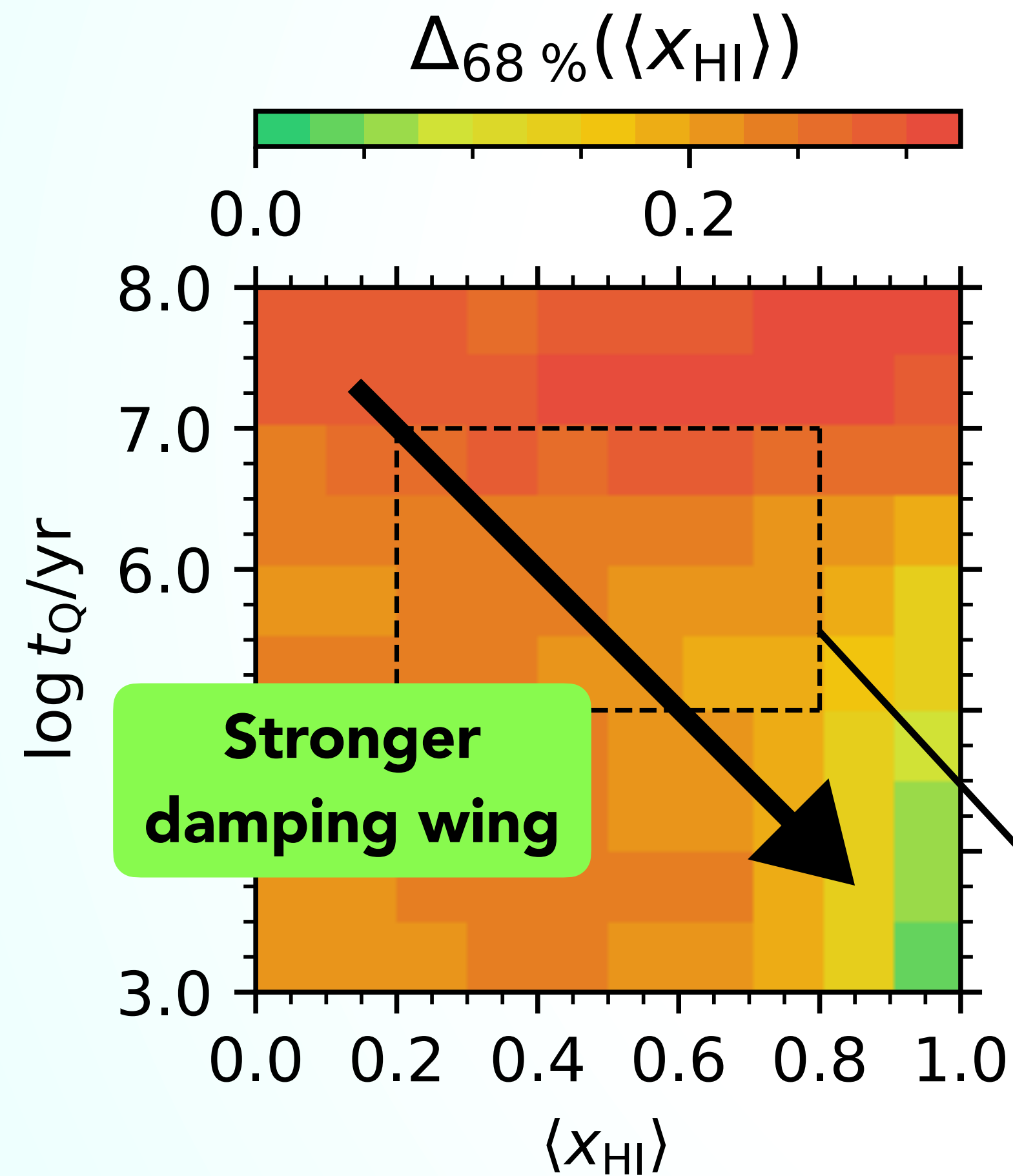


- Precision varies significantly across parameter space (between 2.6% and 39.3%)
- Median precision: 23.4%
- Stronger damping wing imprint (higher $\langle x_{\text{HI}} \rangle$, lower t_Q) improves precision

"Fiducial" region of parameter space

Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

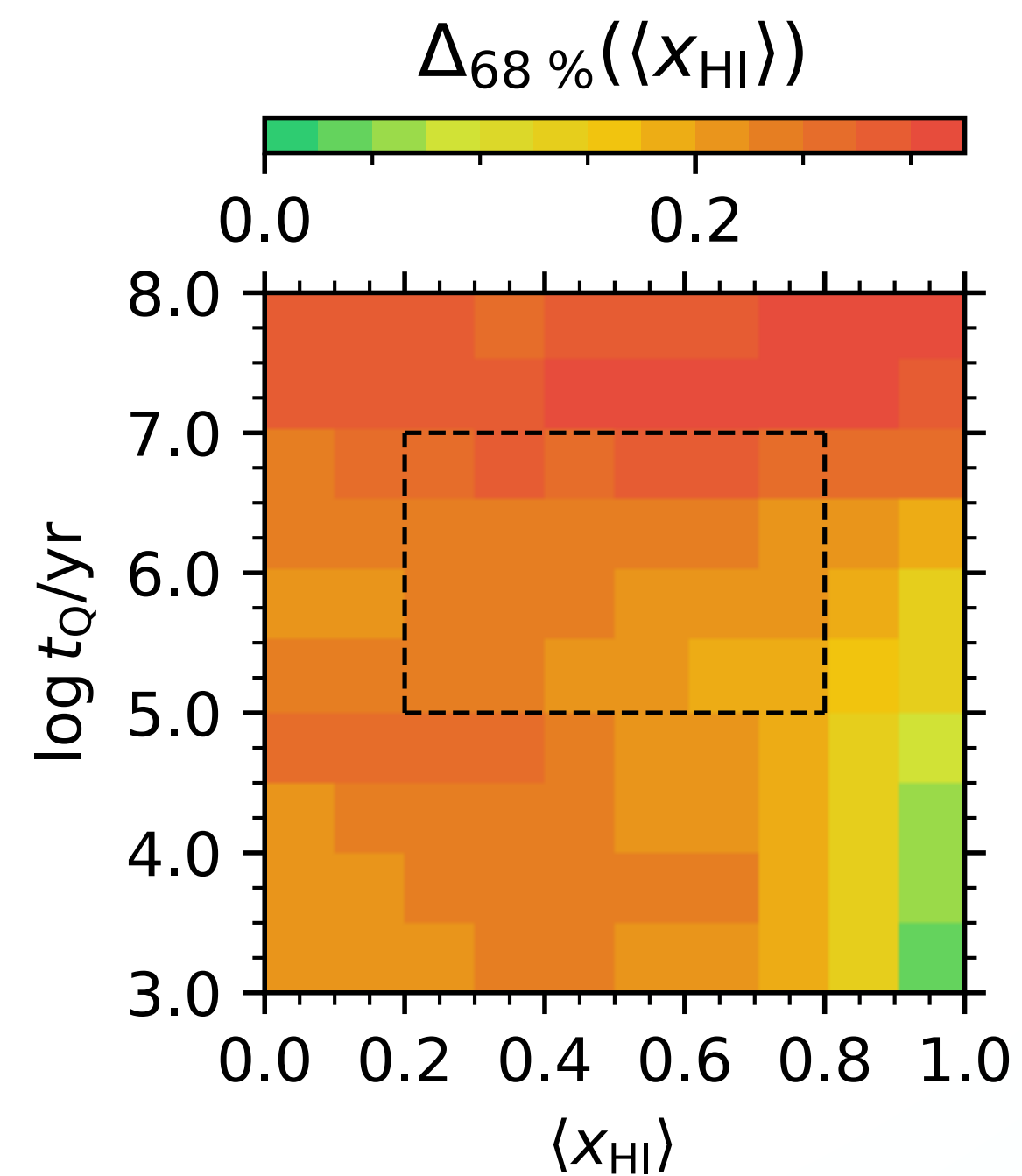


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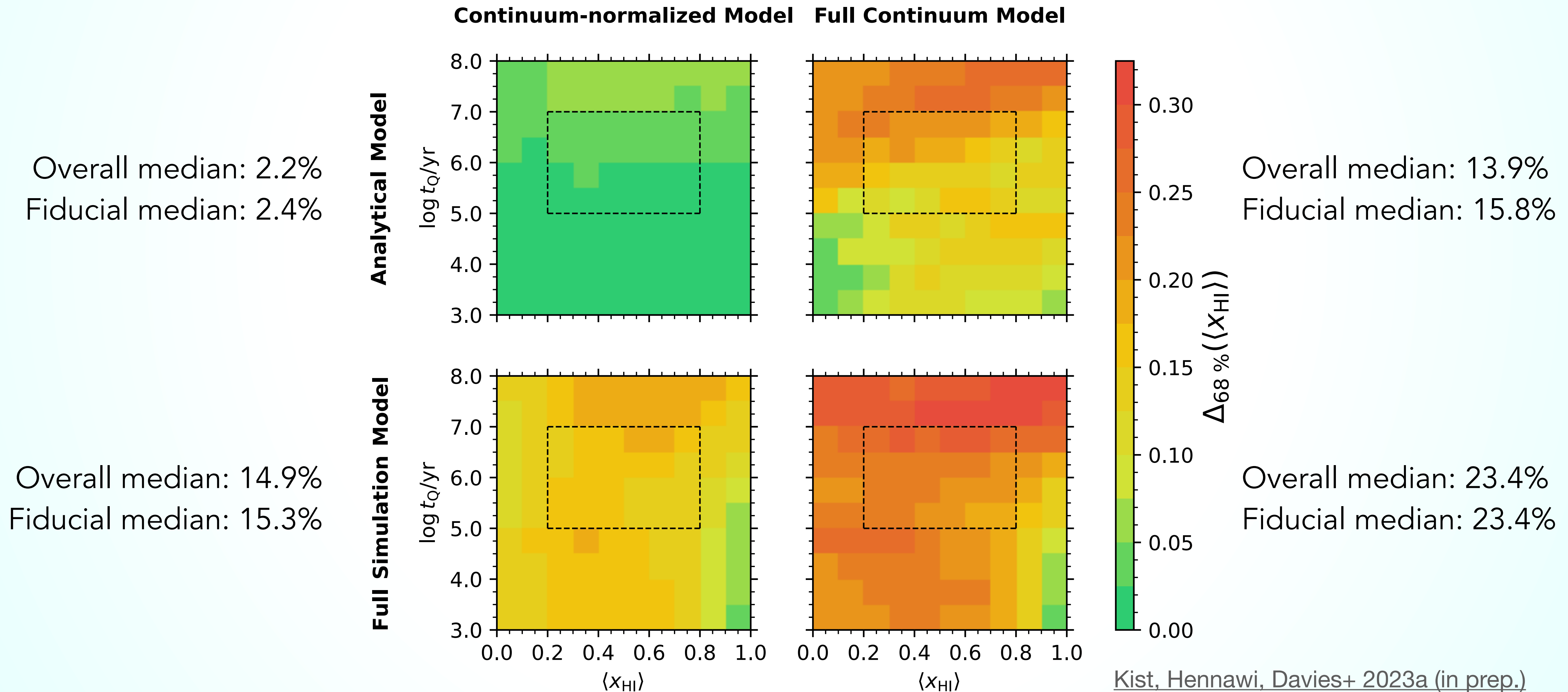
Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space



Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

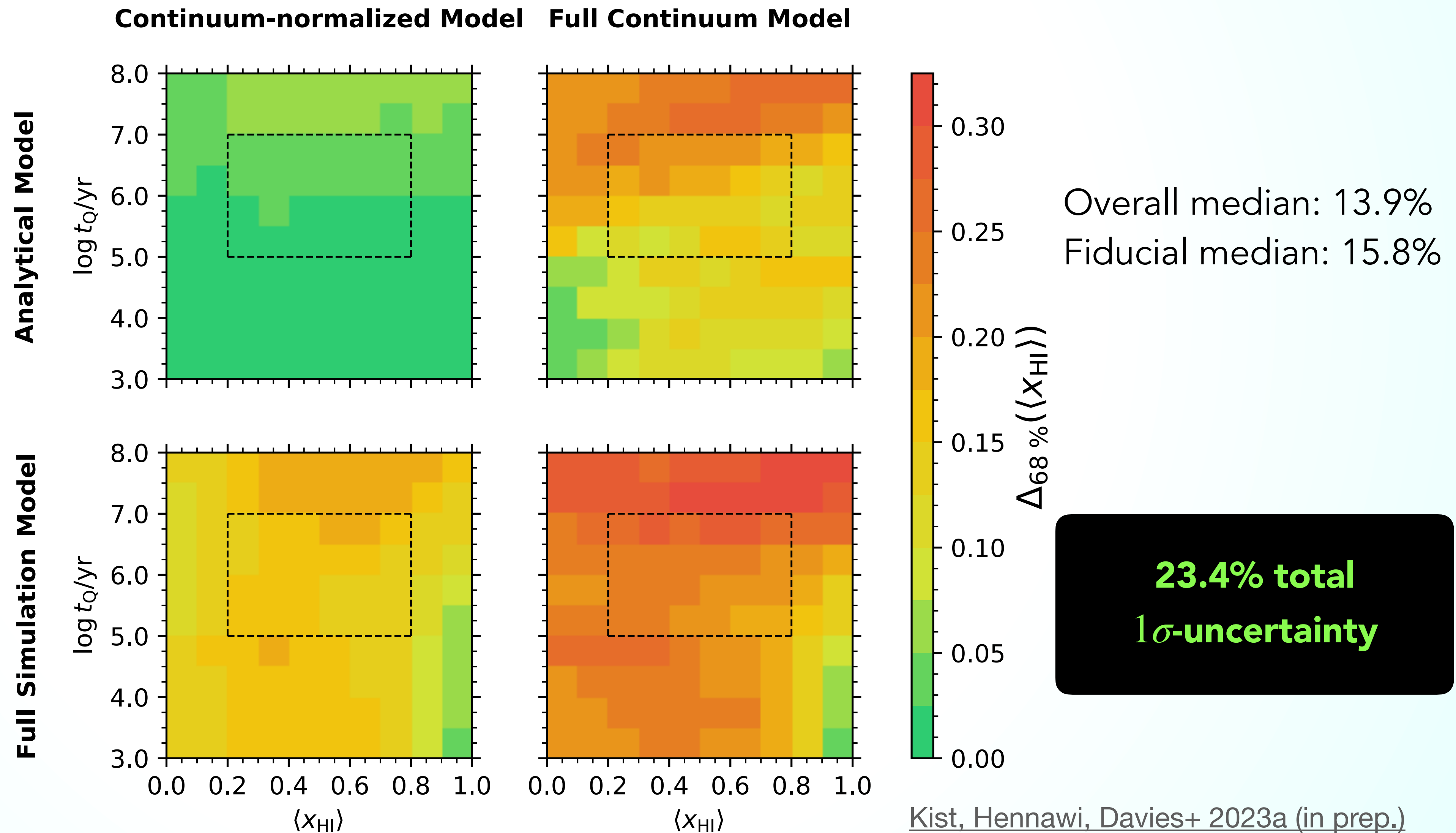


Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

Overall median: 2.2%
Fiducial median: 2.4%

Overall median: 14.9%
Fiducial median: 15.3%

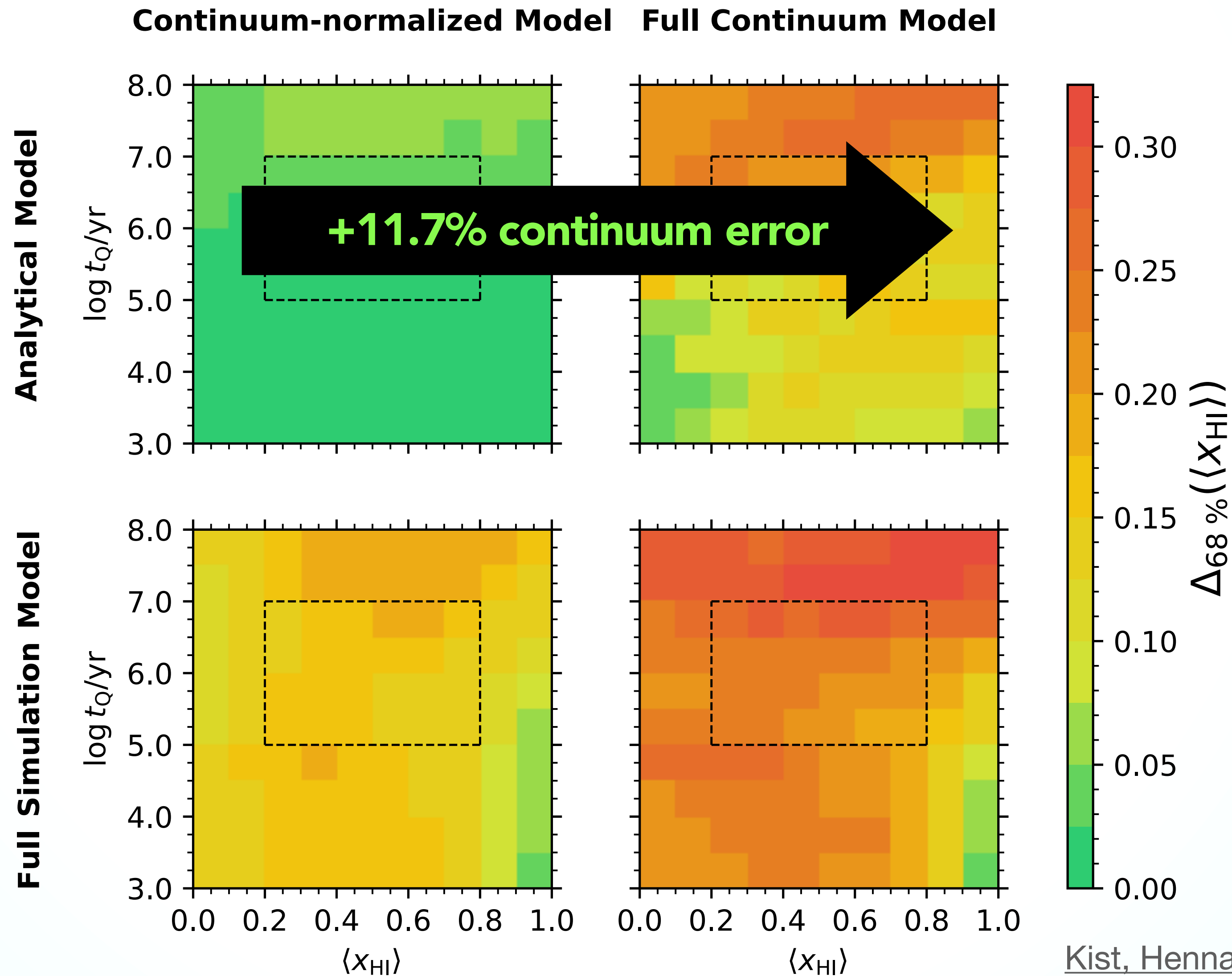


Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

Overall median: 2.2%
Fiducial median: 2.4%

Overall median: 14.9%
Fiducial median: 15.3%



Overall median: 13.9%
Fiducial median: 15.8%

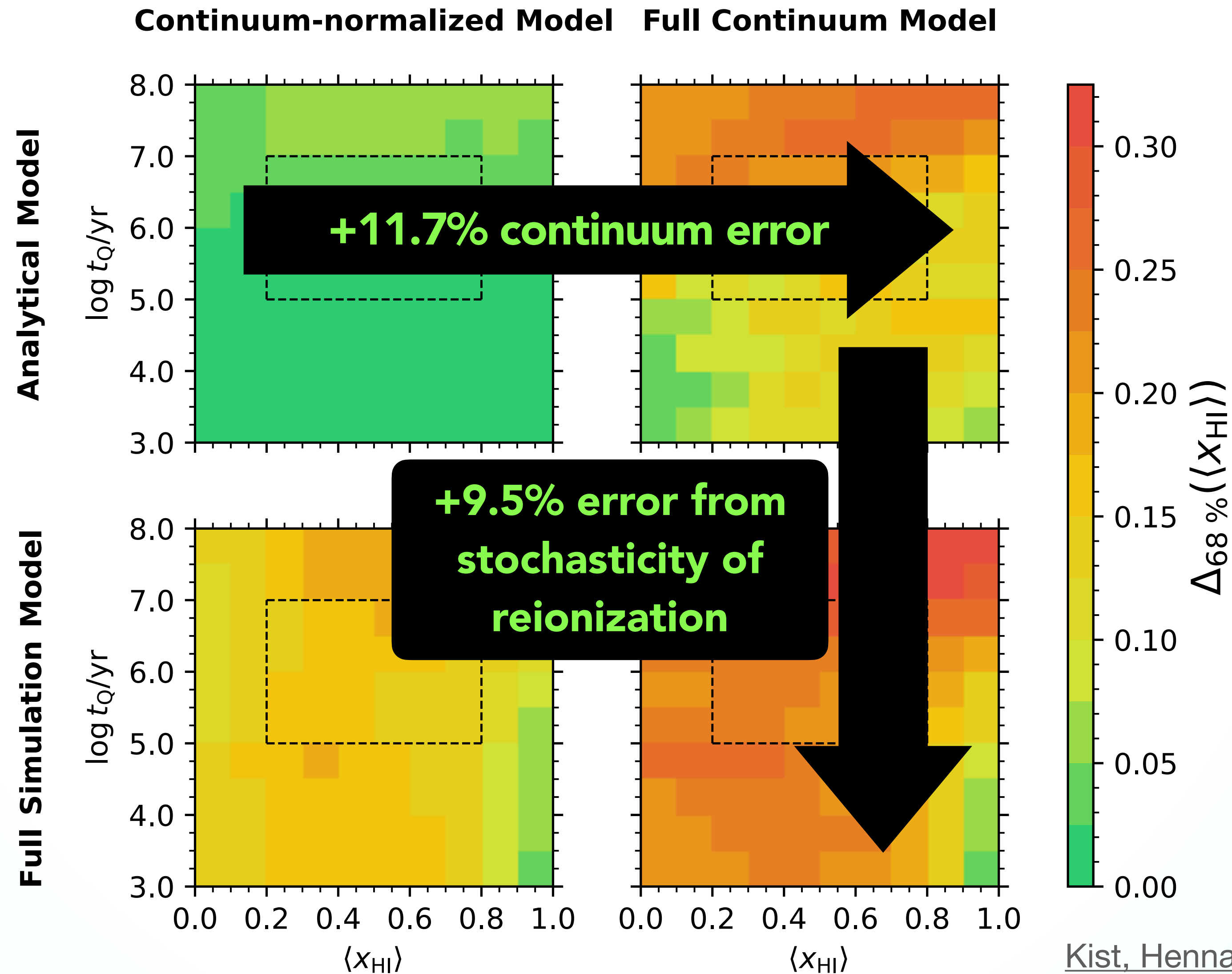
23.4% total
1 σ -uncertainty

Quantifying $\langle x_{\text{HI}} \rangle$ Inference Precision

Variation across Model Components and Parameter Space

Overall median: 2.2%
Fiducial median: 2.4%

Overall median: 14.9%
Fiducial median: 15.3%

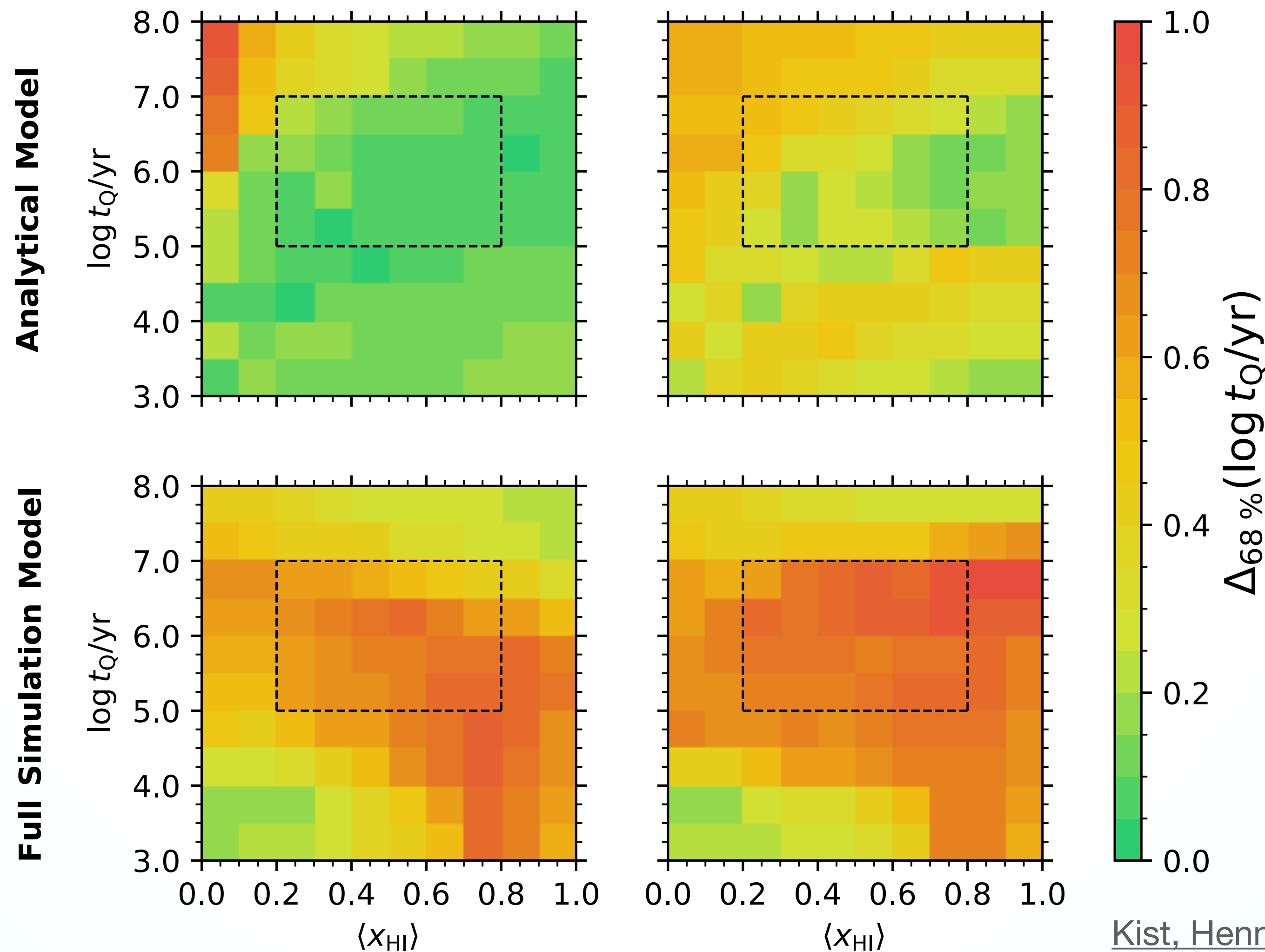


Overall median: 13.9%
Fiducial median: 15.8%

Quantifying t_Q Inference Precision

Variation across Model Components and Parameter Space

Continuum-normalized Model **Full Continuum Model**



Analytical Model

Full Simulation Model

$\Delta_{68\%}(\log t_Q/\text{yr})$

Overall median: 0.12 dex
Fiducial median: 0.08 dex

Overall median: 0.33 dex
Fiducial median: 0.26 dex

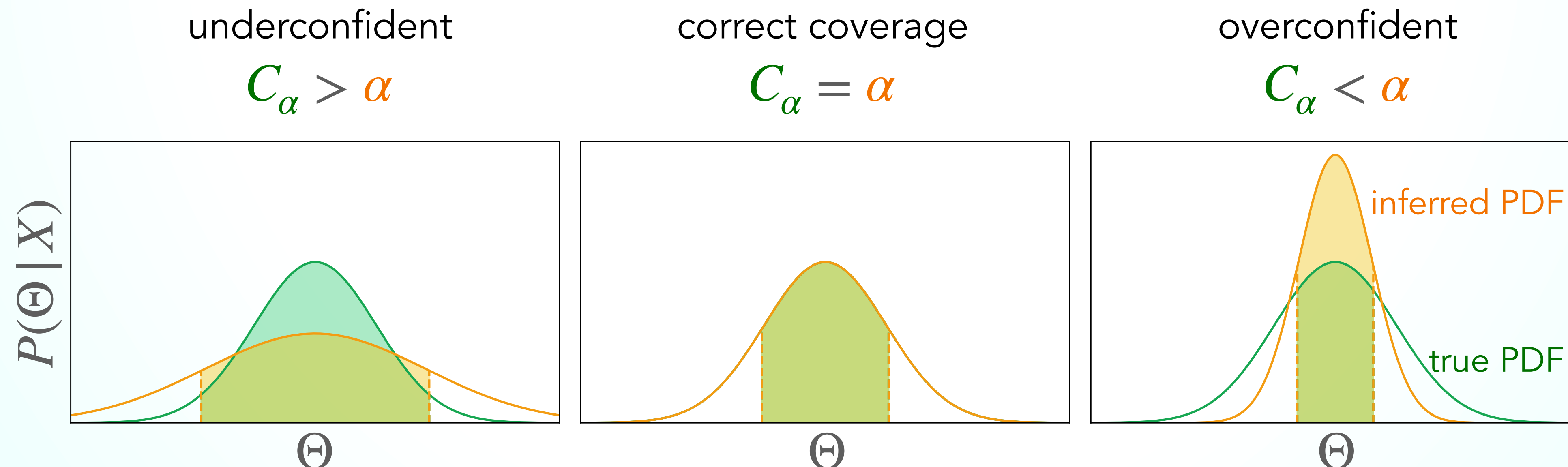
Overall median: 0.54 dex
Fiducial median: 0.71 dex

Overall median: 0.65 dex
Fiducial median: 0.86 dex

Inference Tests

Expected coverage probability

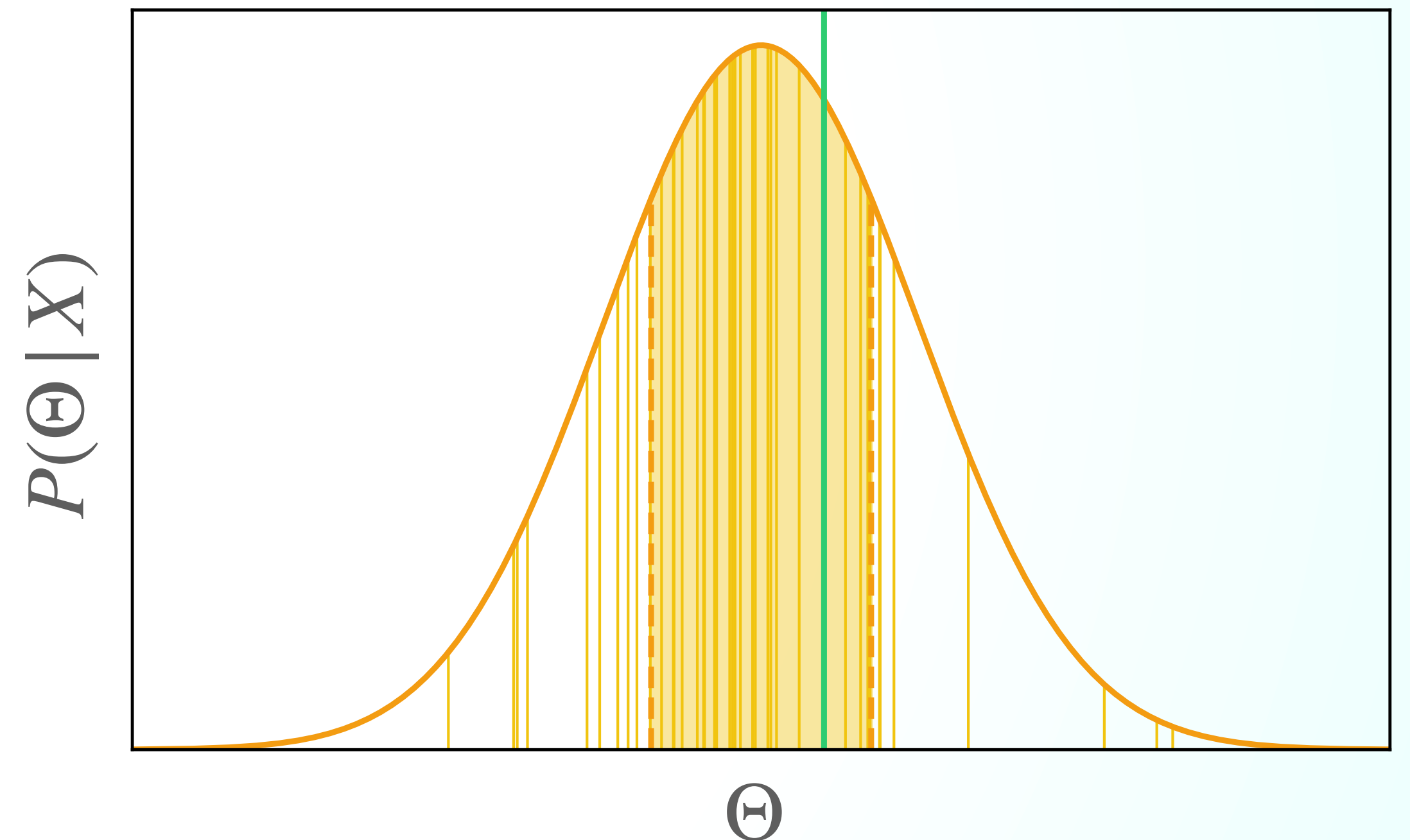
- testing if the inferred posterior represents the true distribution
- select the α -th credibility level of the inferred posterior
- compute the expected coverage probability C_α of the true distribution



Coverage Tests

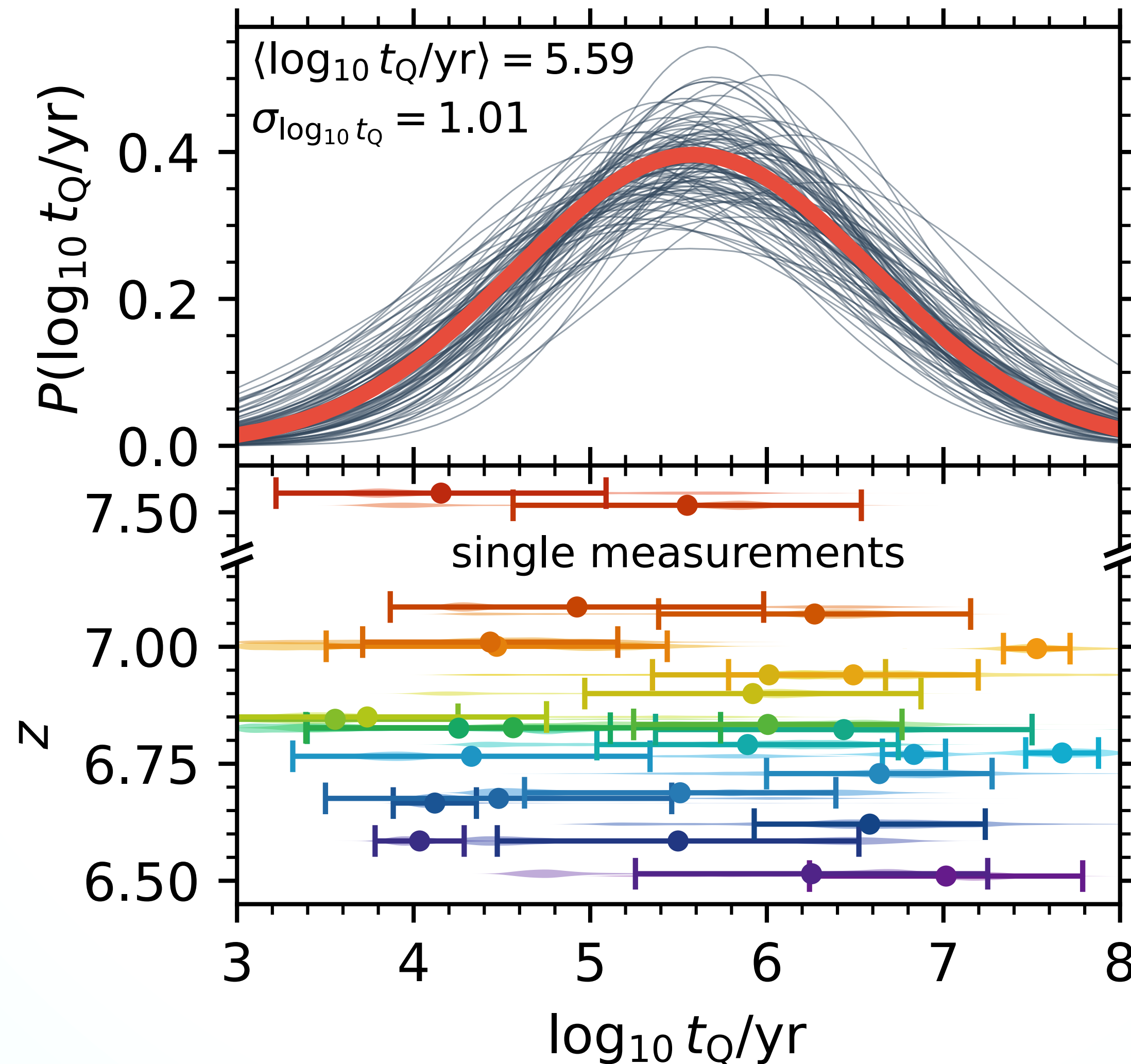
Practical computation

- for each quasar, order the MCMC samples by probability and choose the N highest ones, where $N = \alpha \cdot N_{\text{tot}}$
- test if the true probability is contained inside this region
- for each credibility level α determine the fraction of quasars C_α for which this is the case

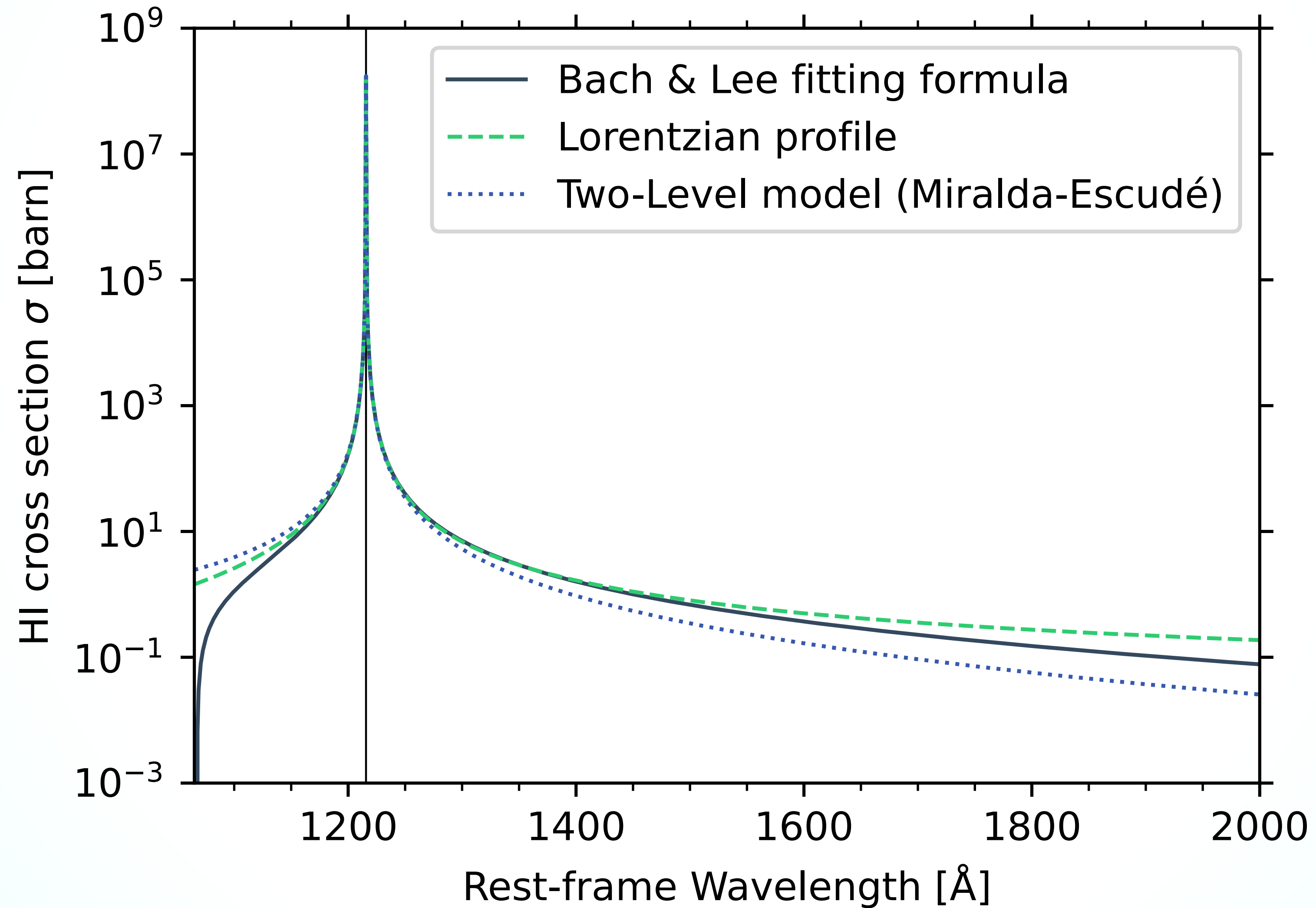


Ensemble inference

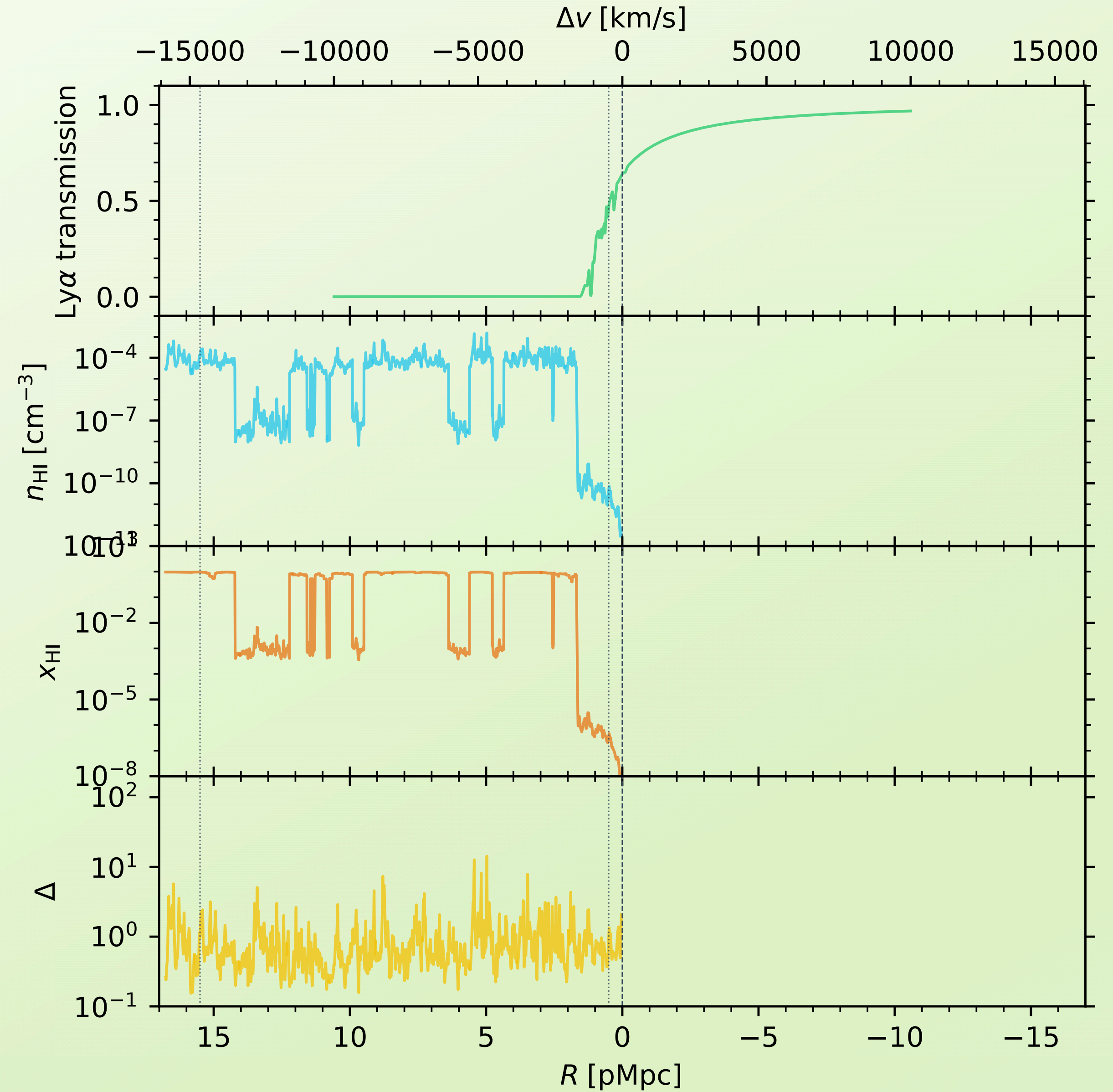
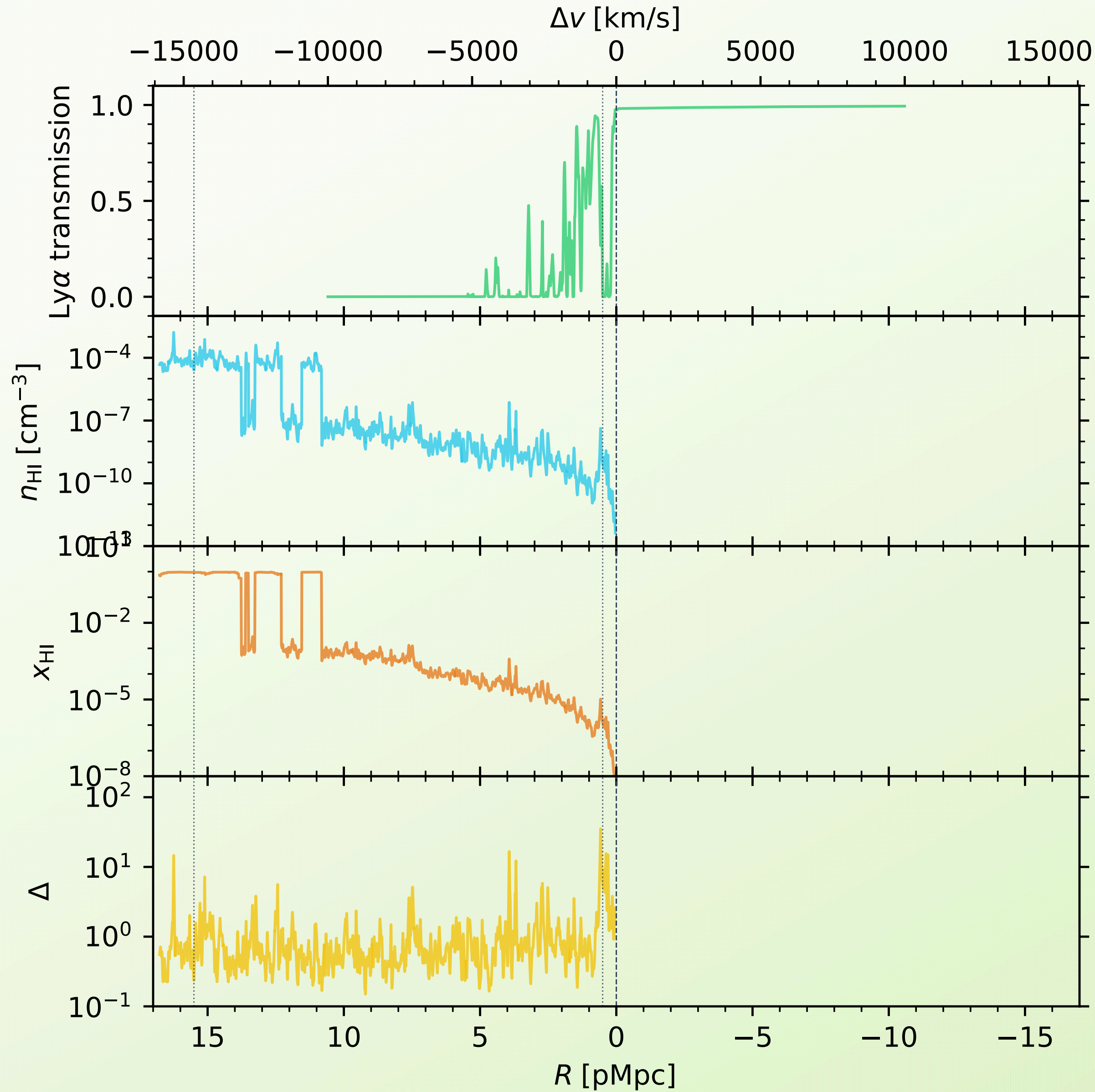
Constraints on the Distribution of Quasar Lifetimes



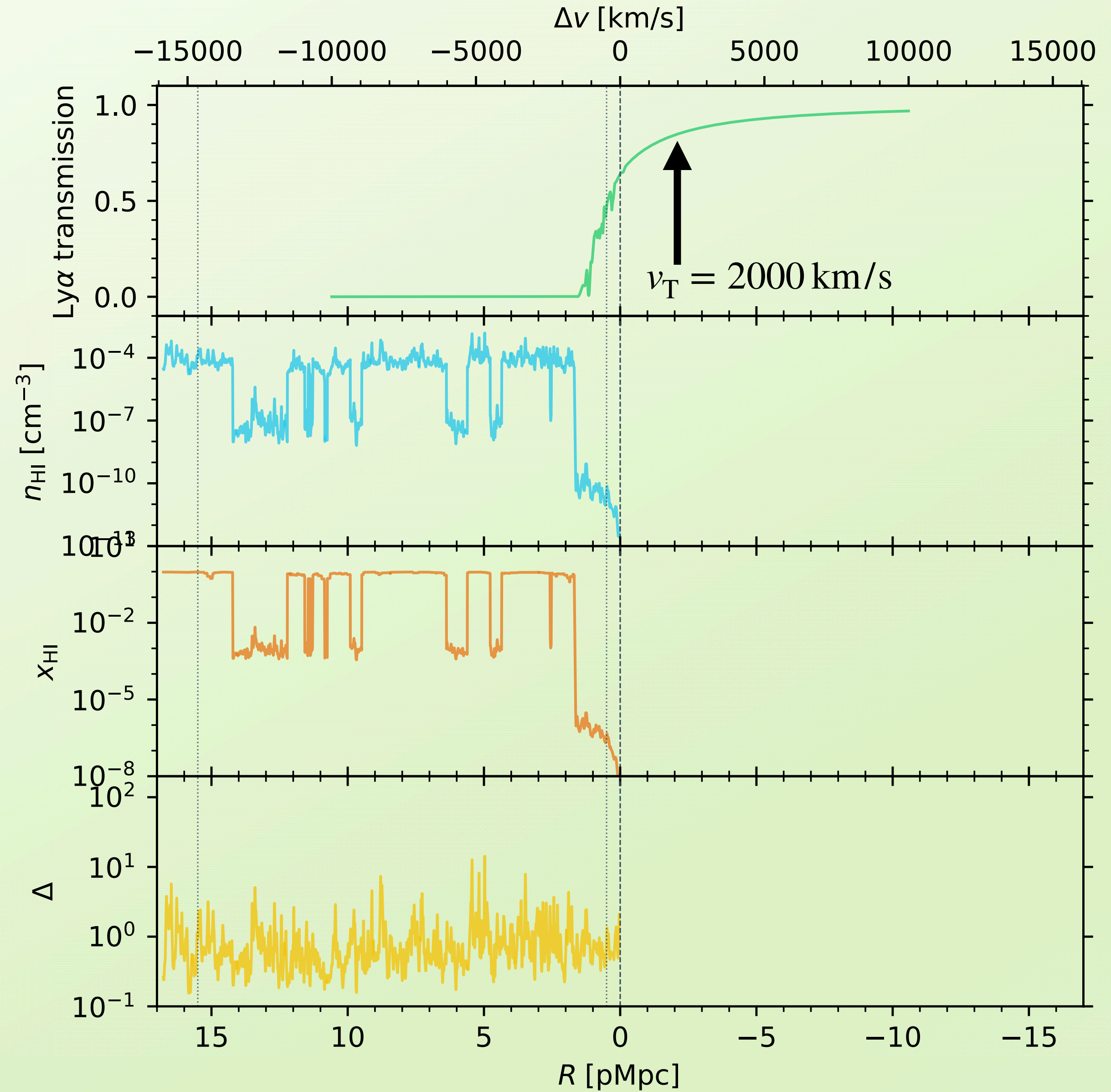
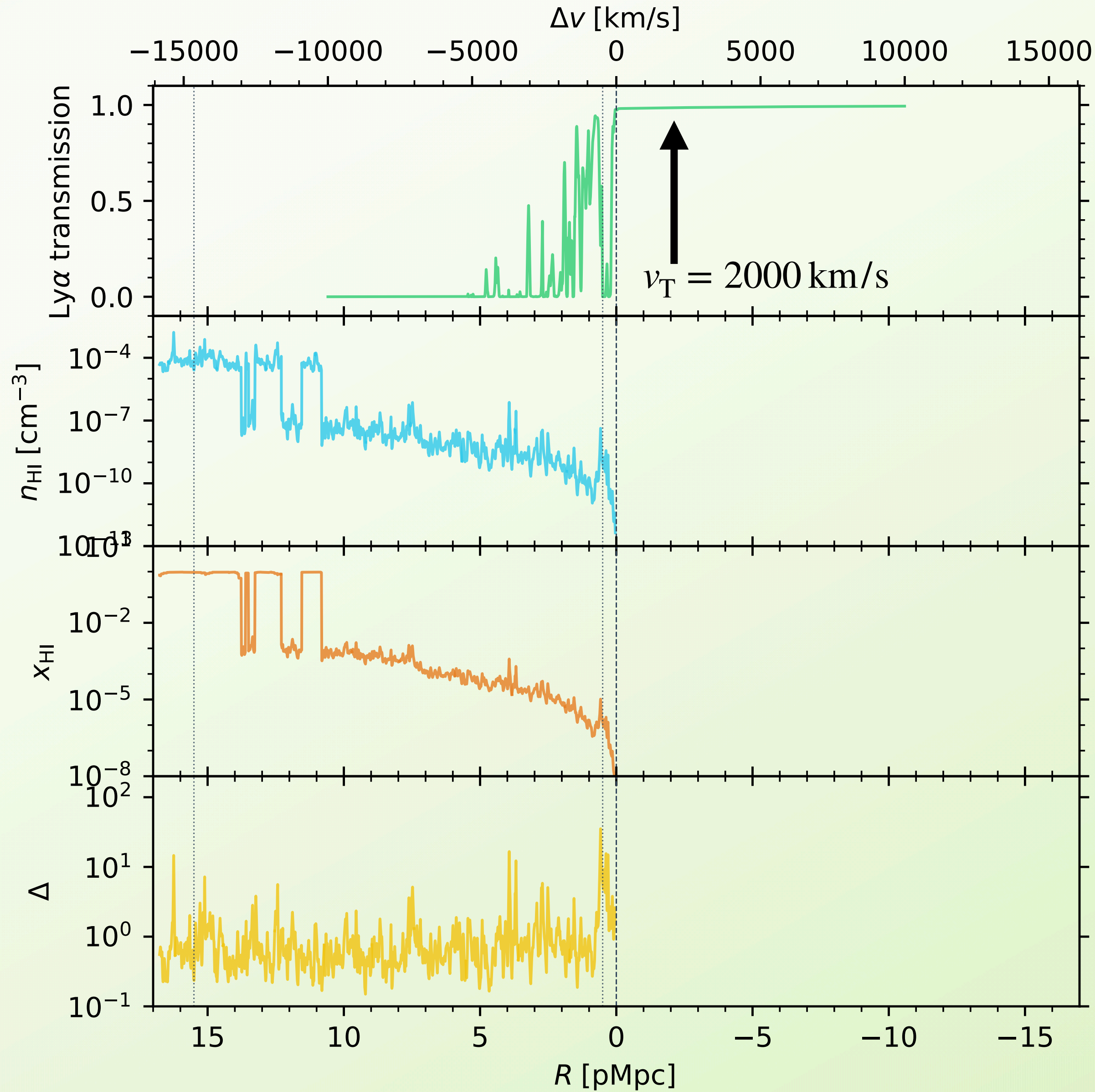
HI absorption cross section



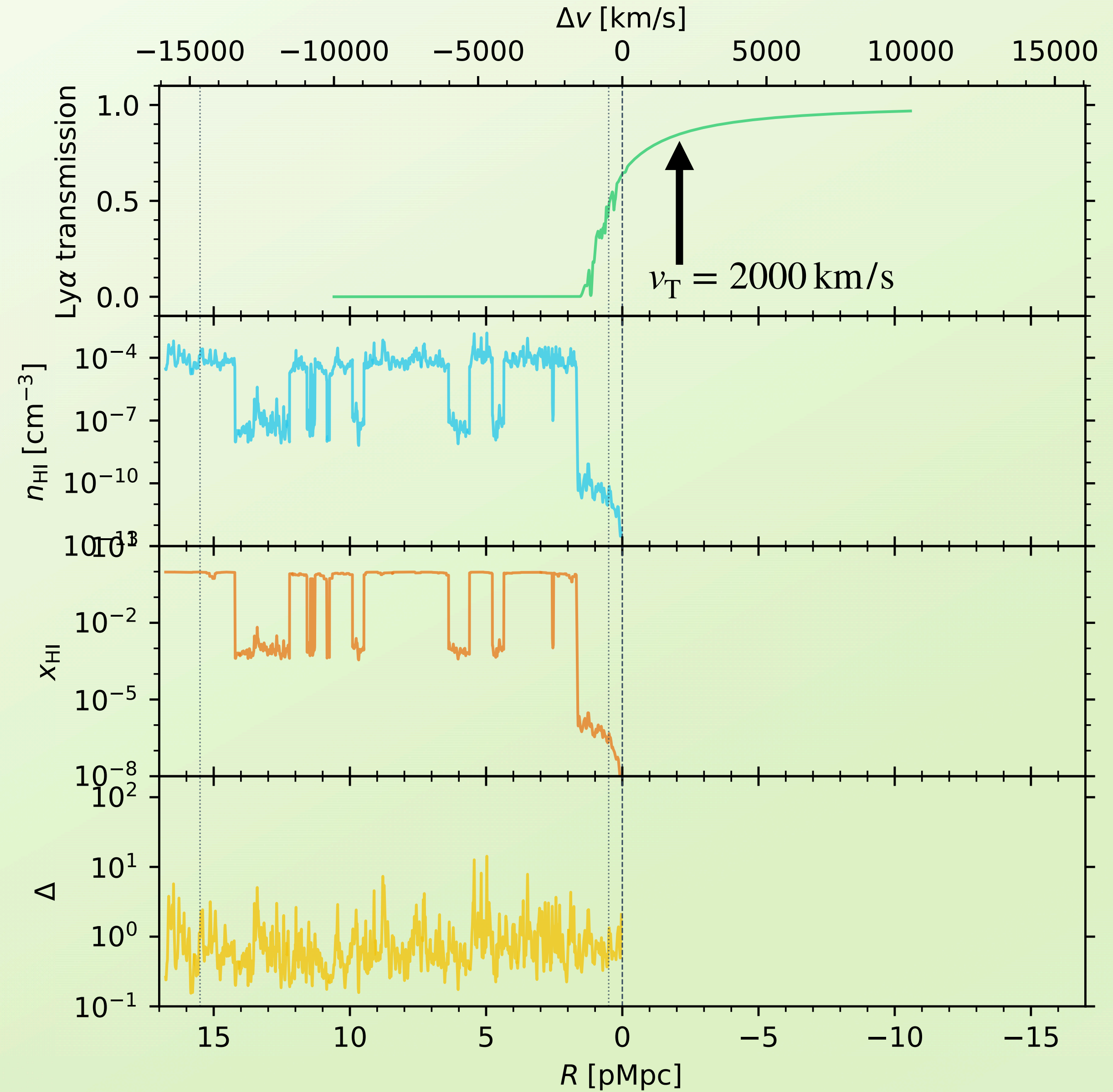
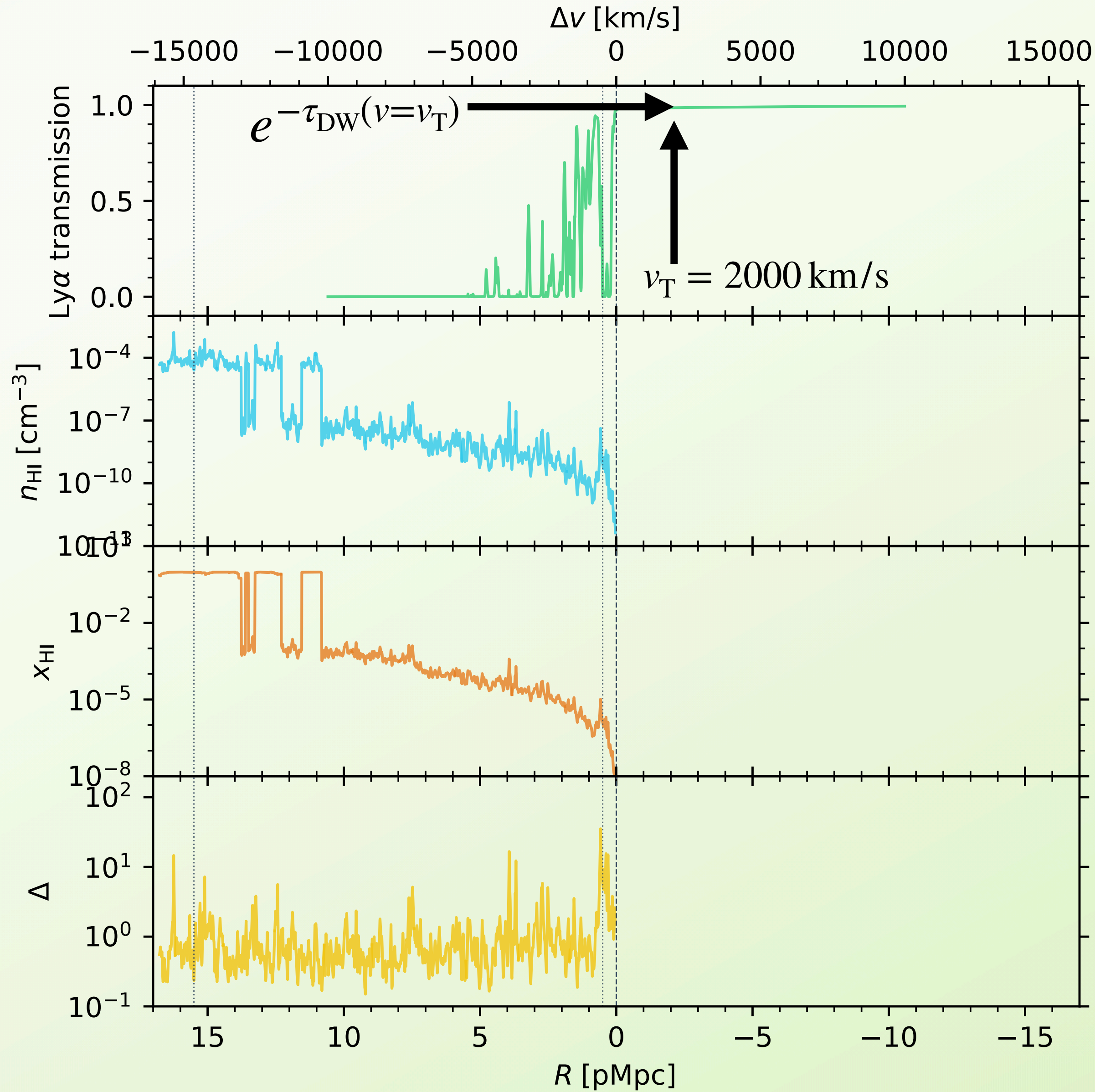
Constructing a new label that minimizes IGM transmission scatter



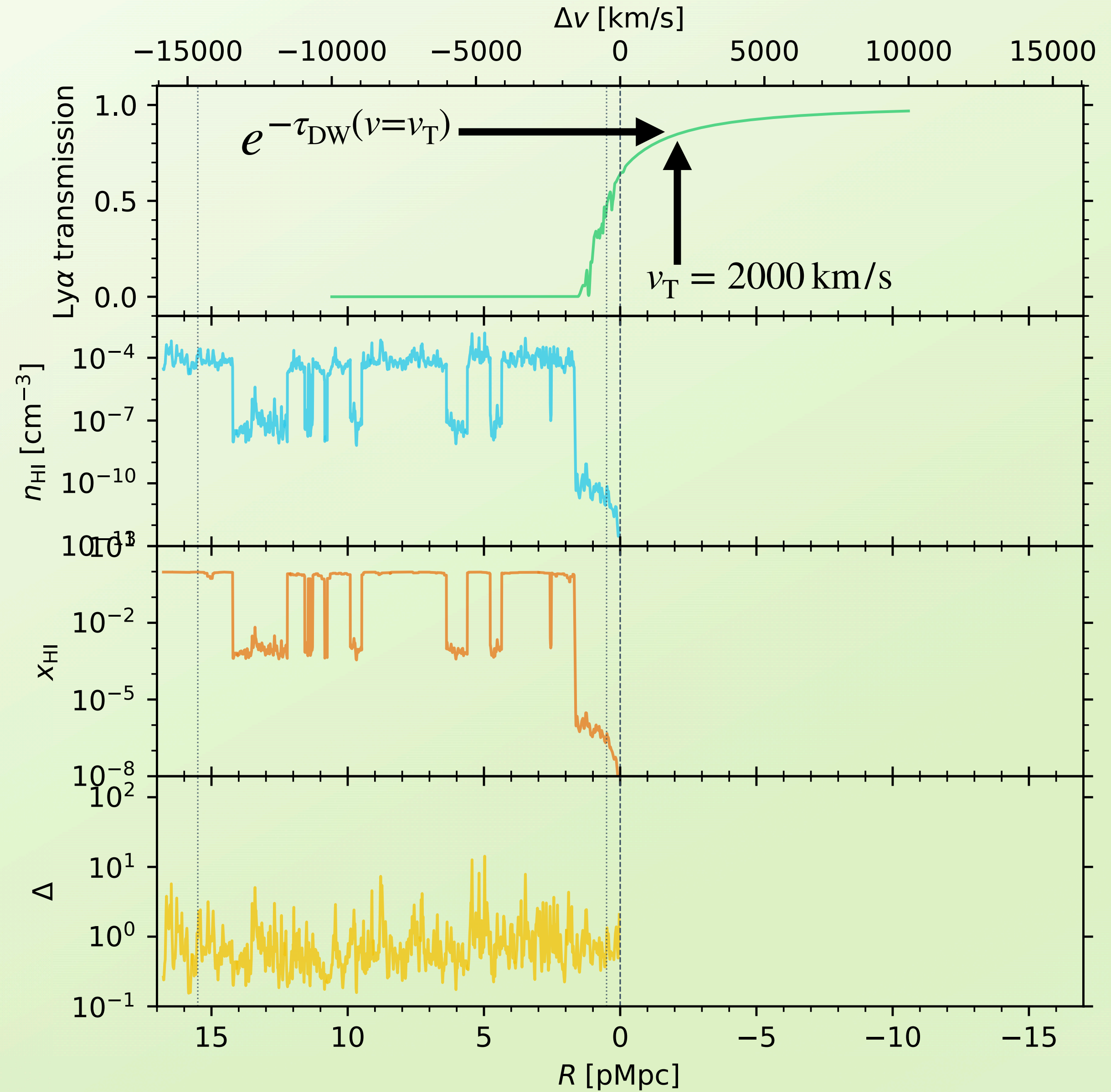
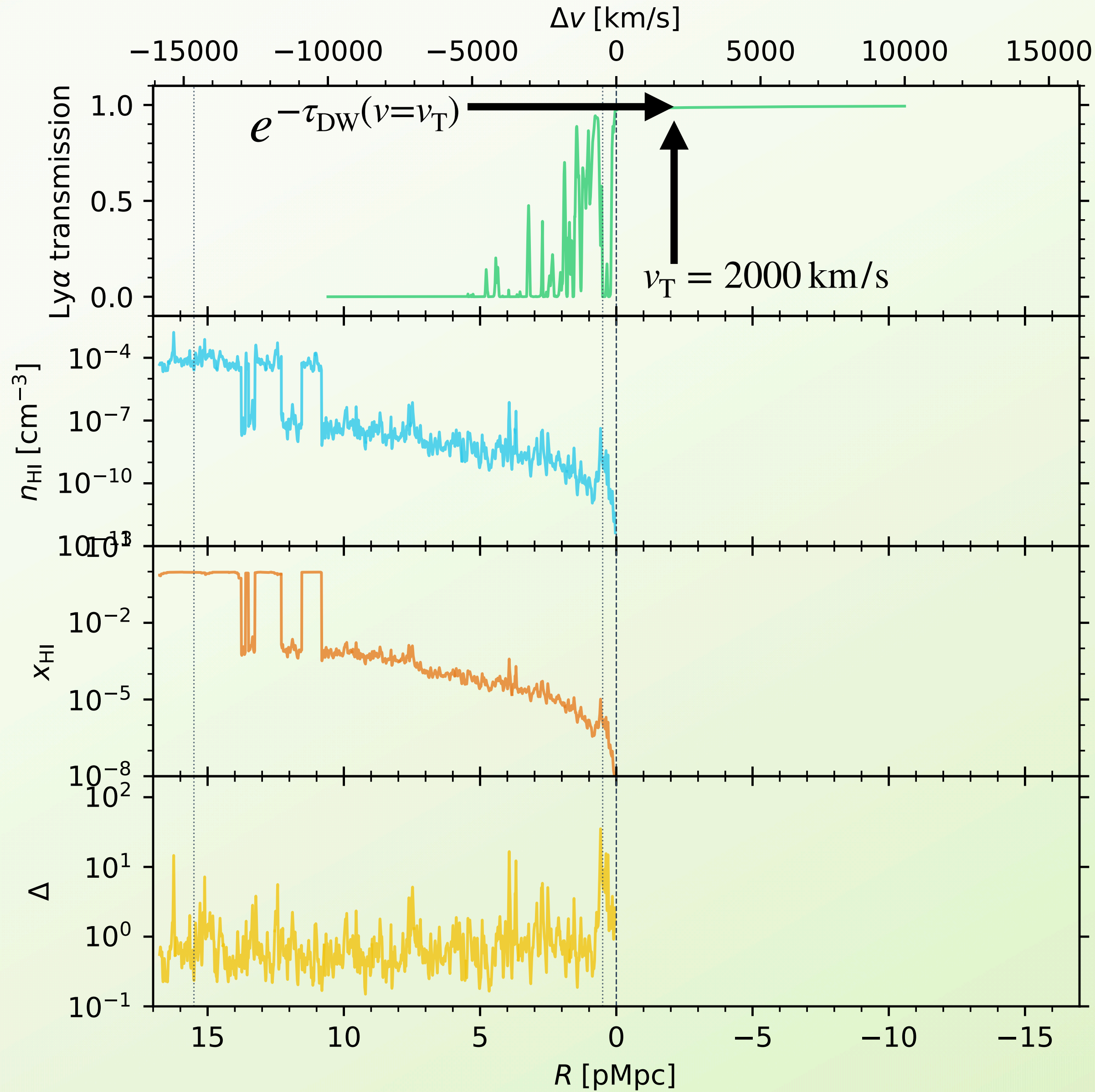
Constructing a new label that minimizes IGM transmission scatter



Constructing a new label that minimizes IGM transmission scatter



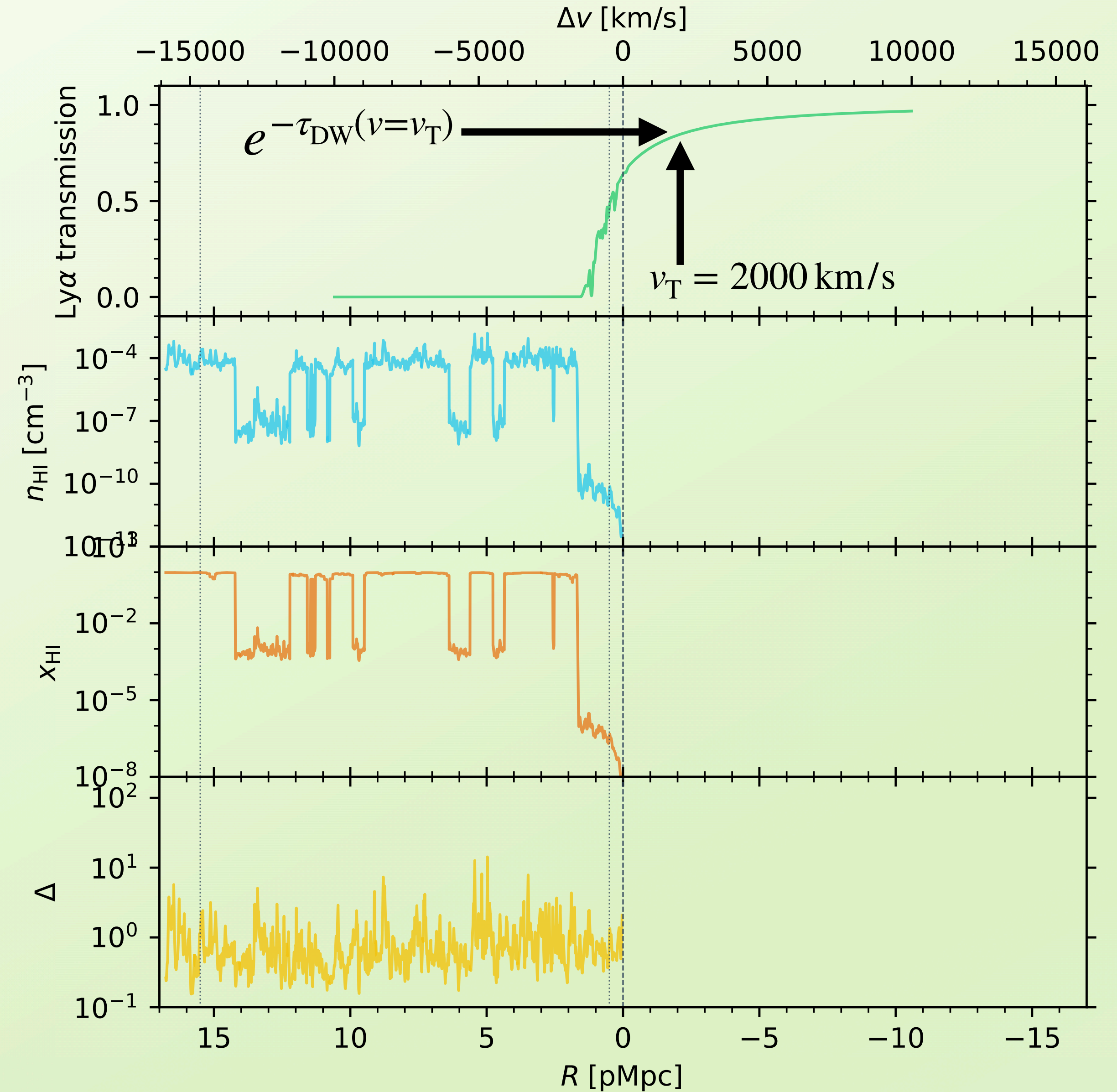
Constructing a new label that minimizes IGM transmission scatter



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

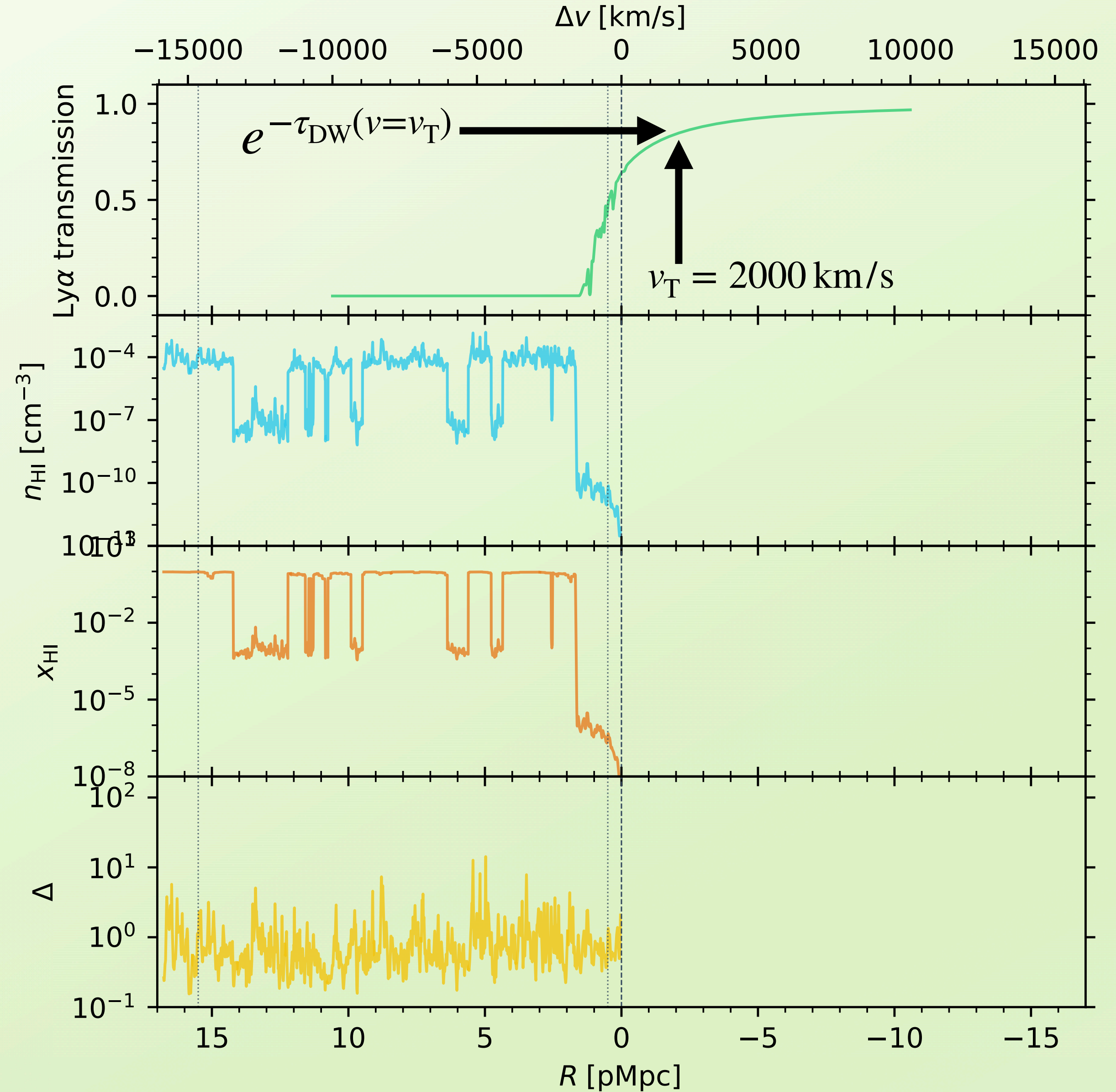


Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field



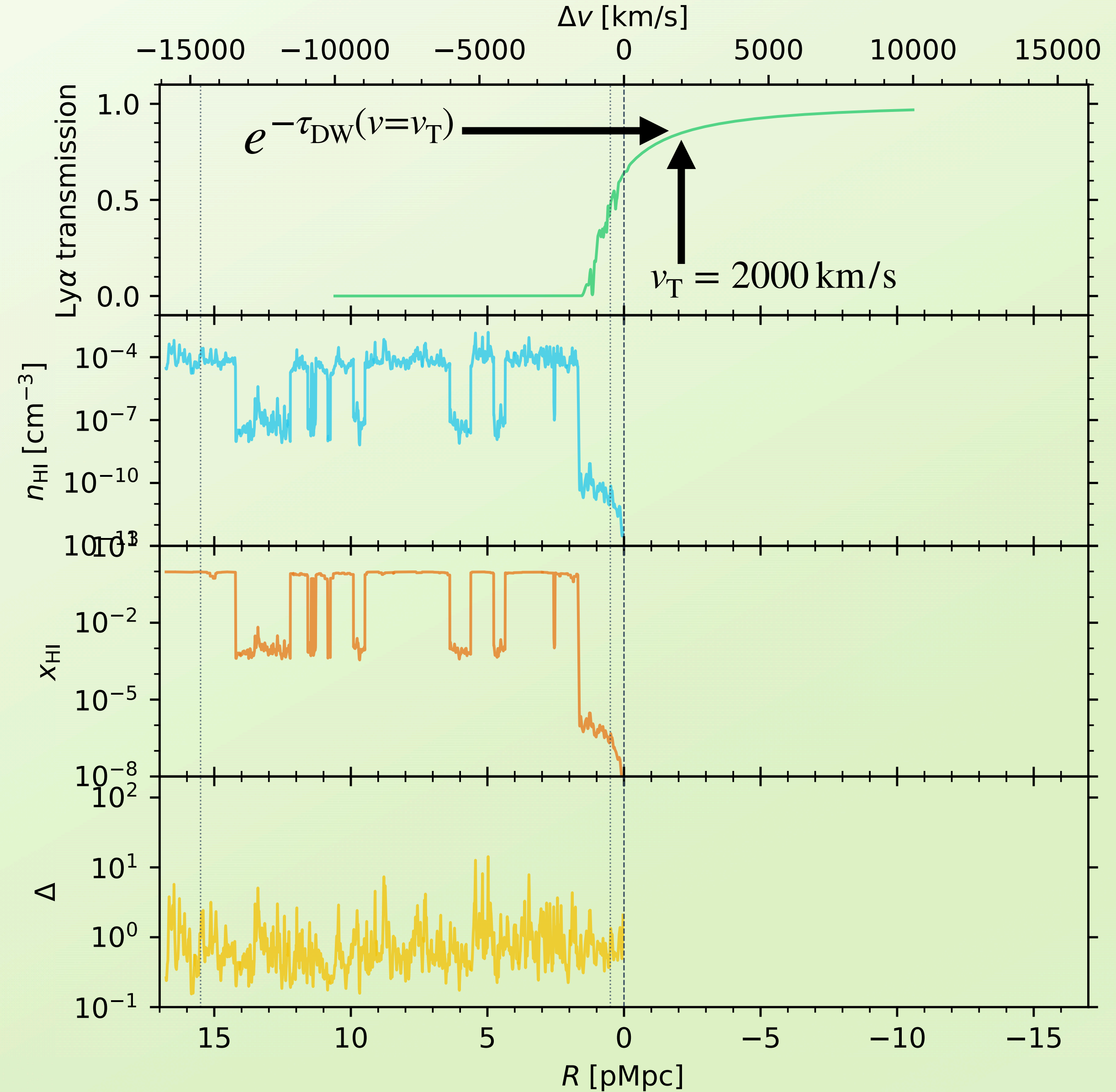
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post-quasar HI density field

Ly α cross section



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

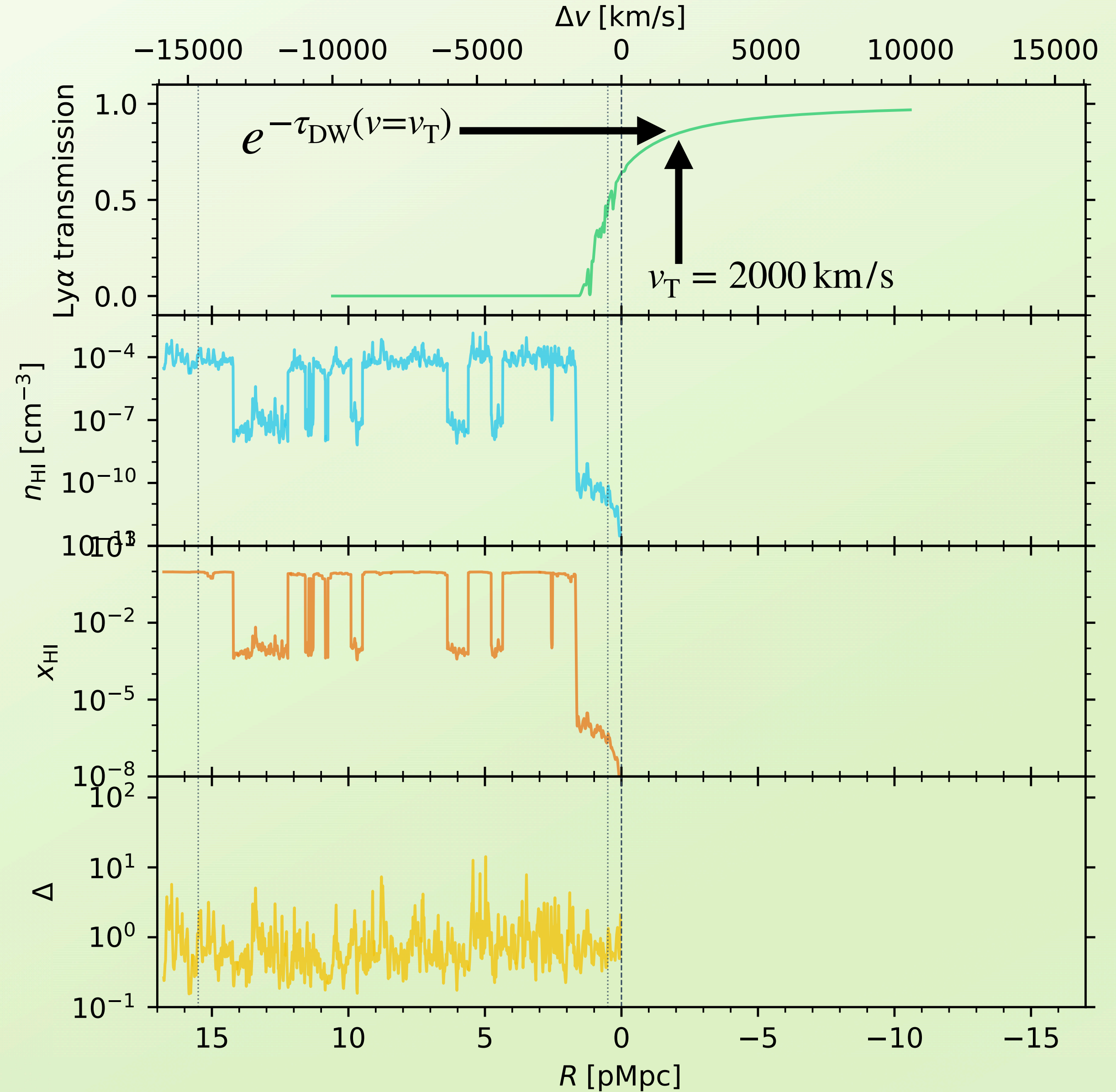
$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field

$\text{Ly}\alpha$ cross section

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

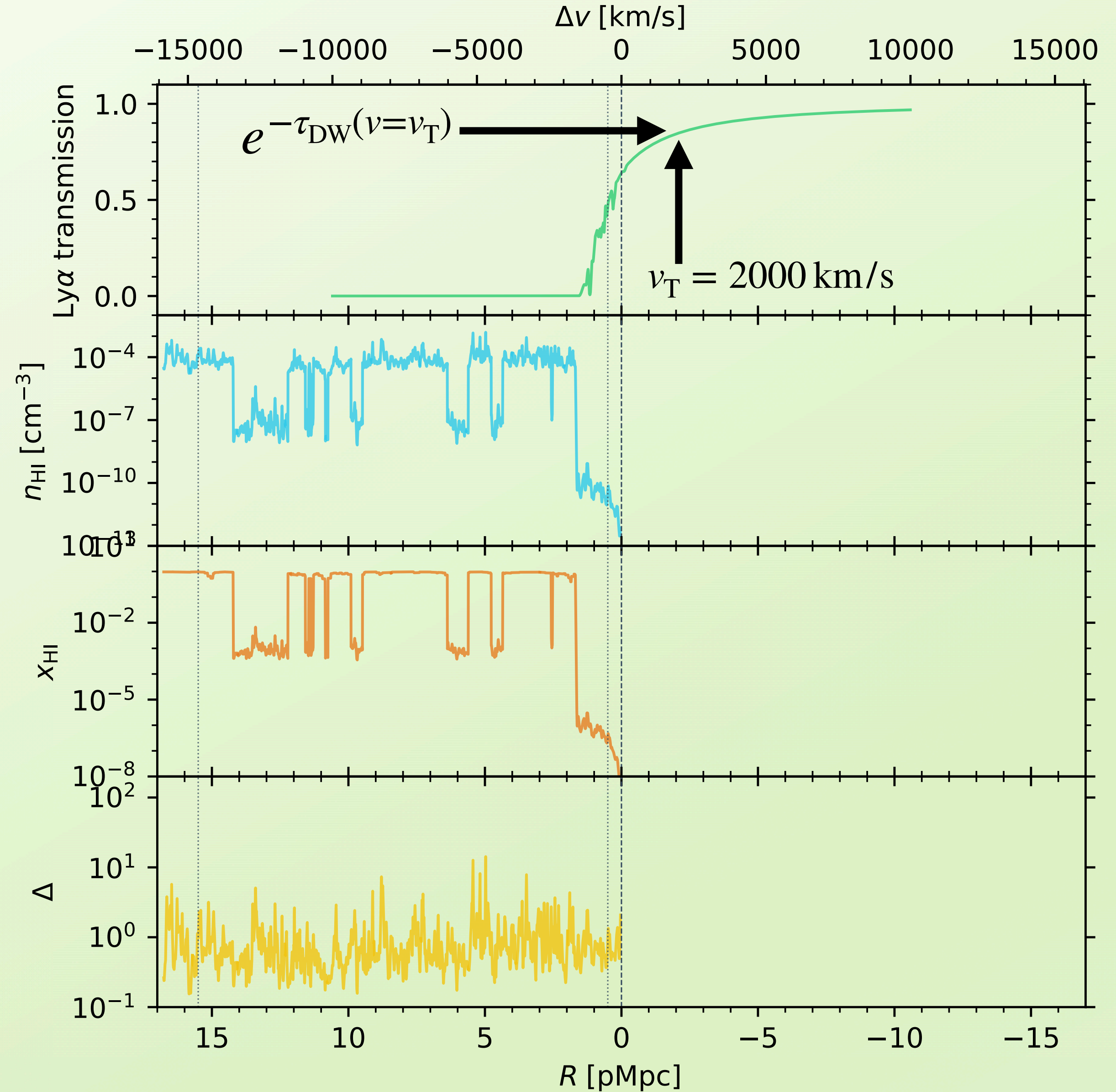
$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field

$\text{Ly}\alpha$ cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

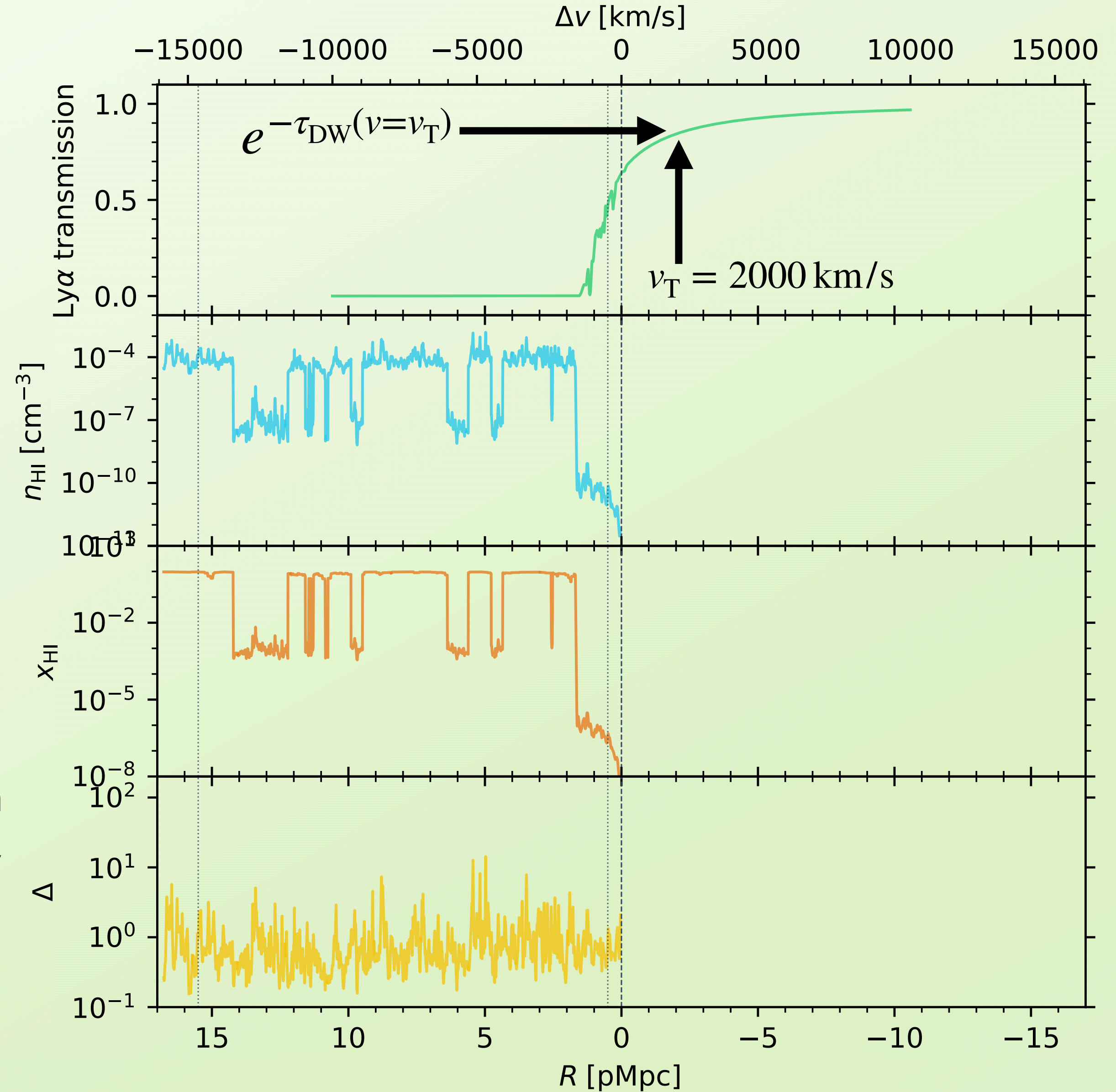
post-quasar HI density field

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 \simeq Lorentzian

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weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field

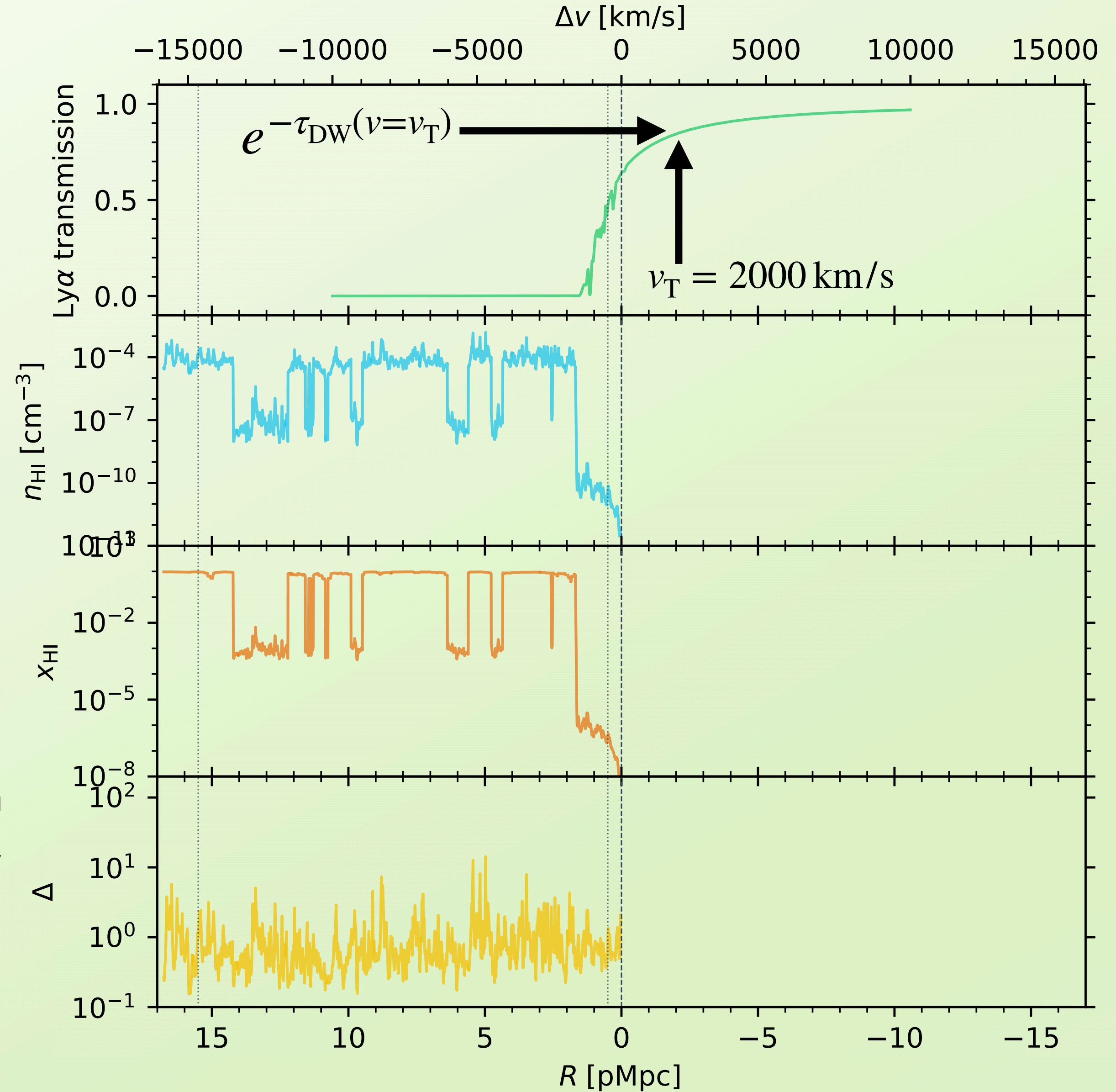
$\text{Ly}\alpha$ cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$

0.5 pMpc

weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field
 \simeq pre-quasar HI density field

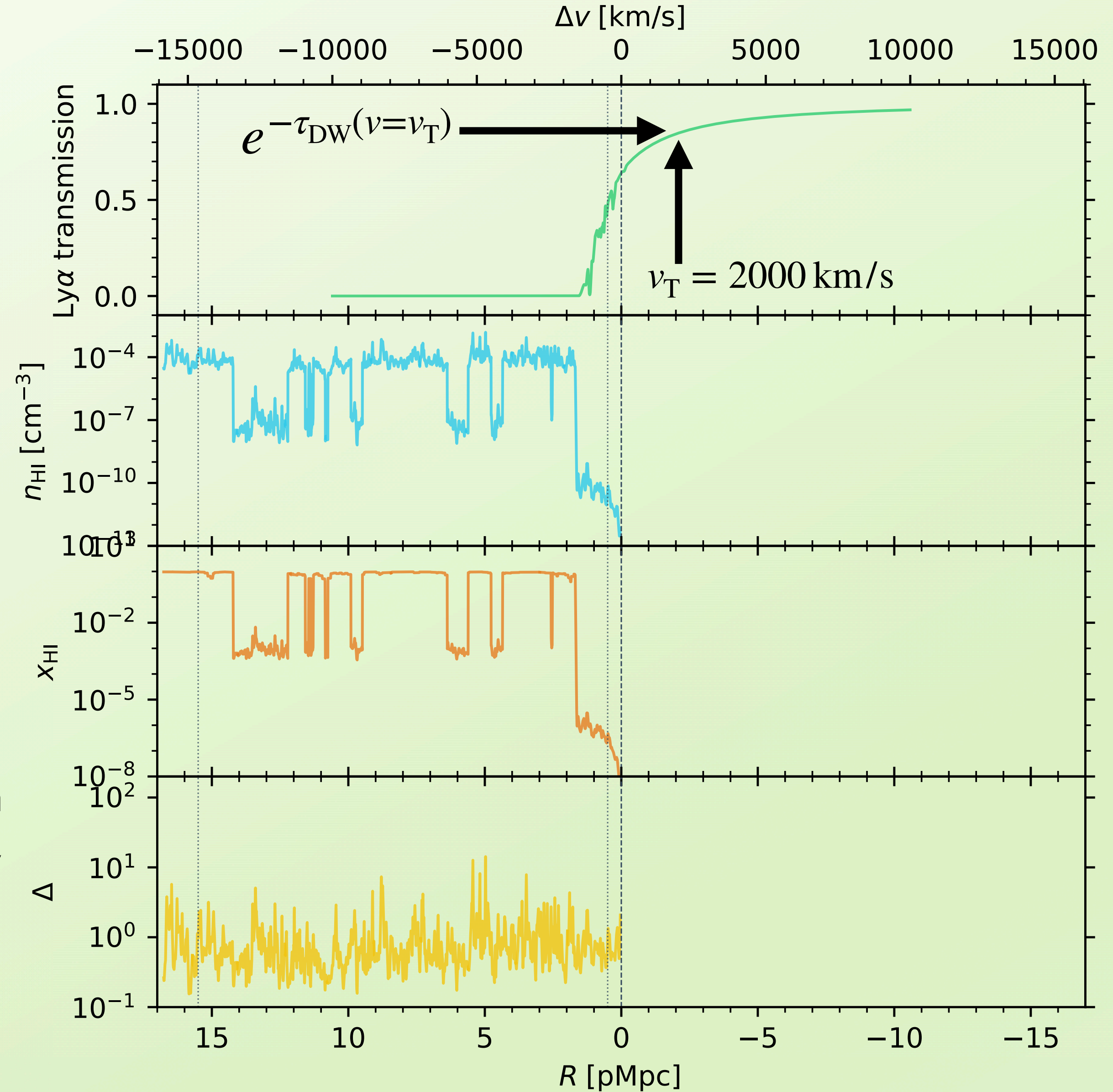
Ly α cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$

15.5 pMpc \rightarrow R_{max}
 0.5 pMpc \rightarrow R_{min}

weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field
 \simeq pre-quasar HI density field

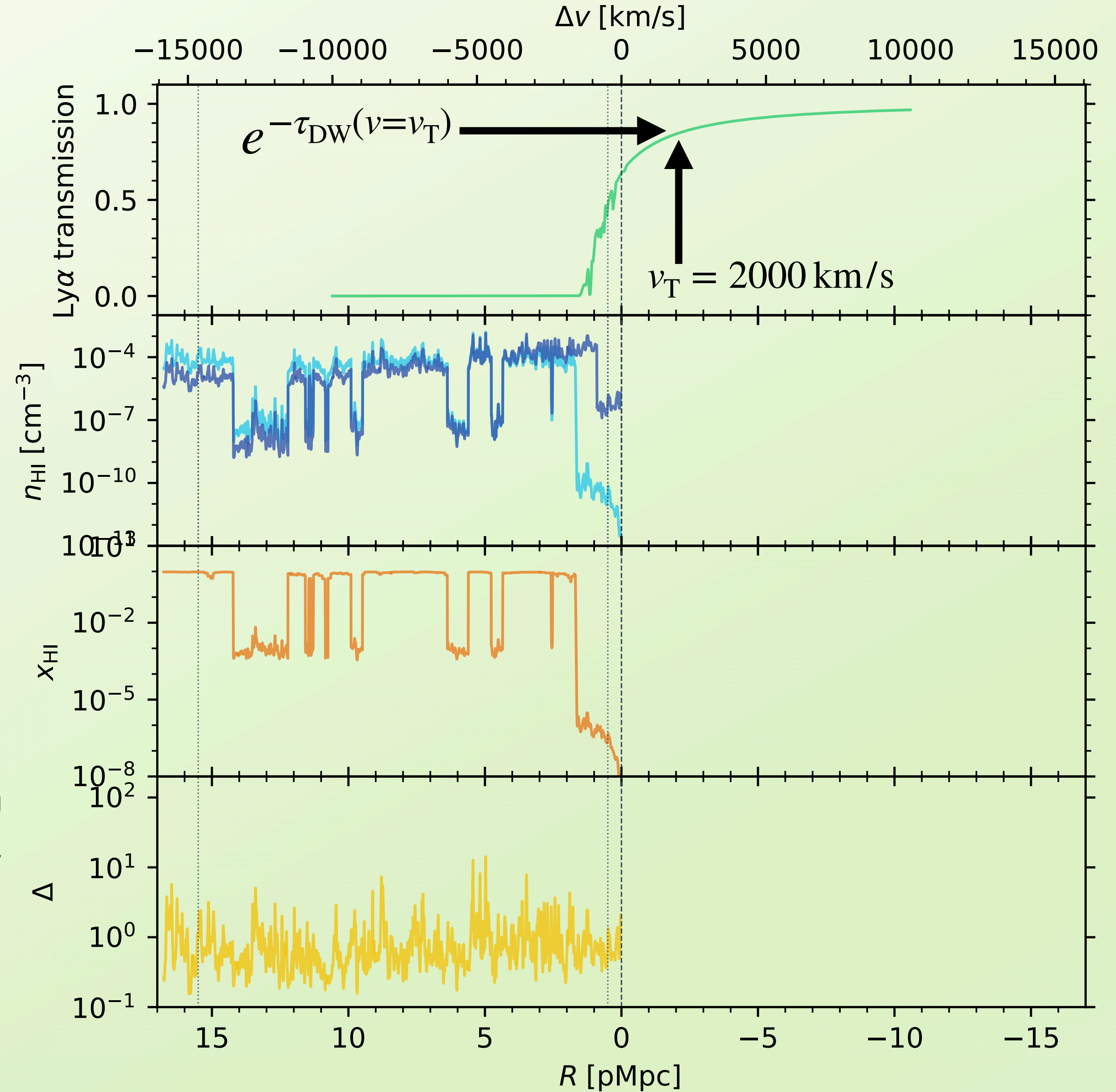
Ly α cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

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Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field
 \simeq pre-quasar HI density field

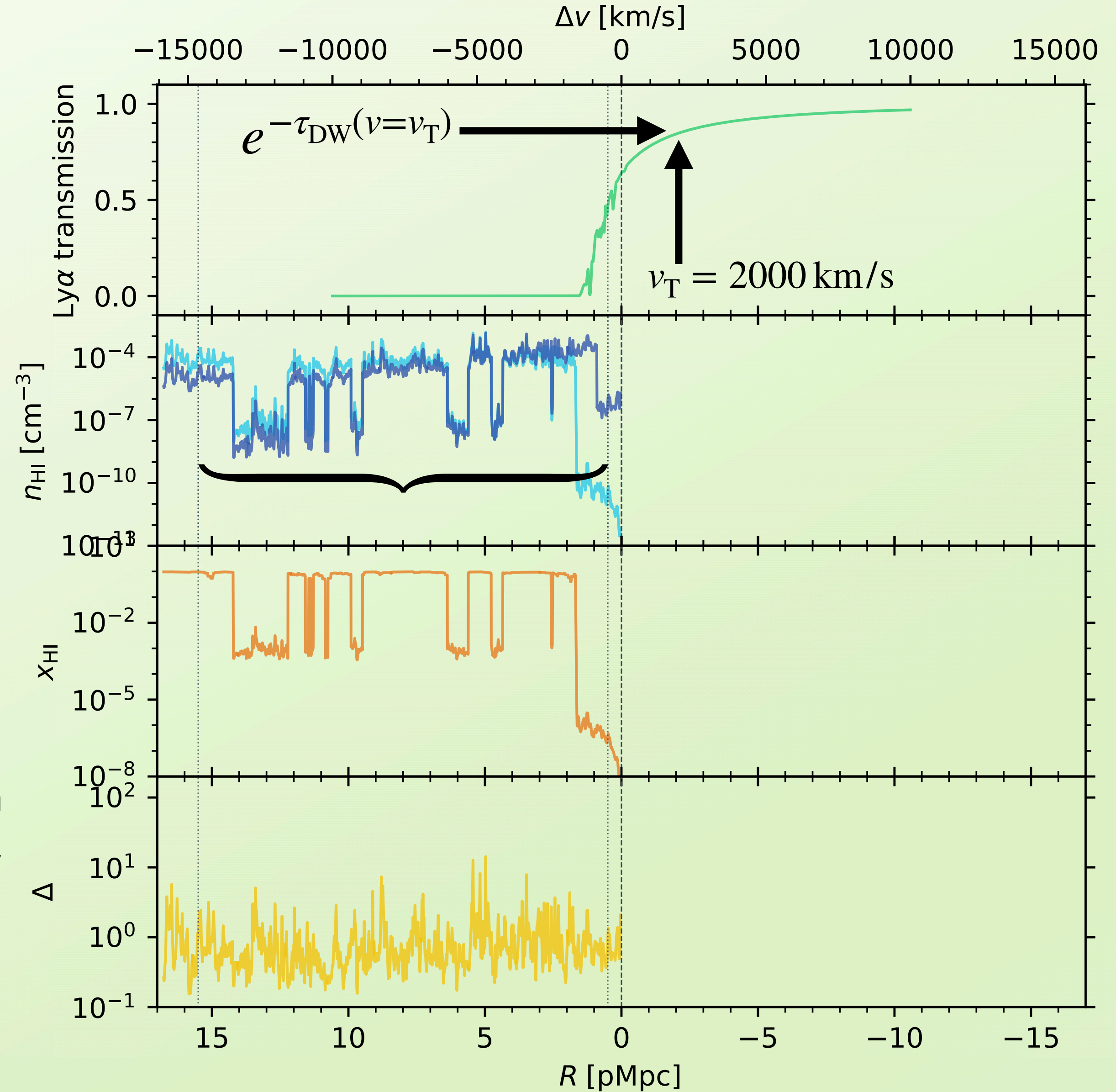
Ly α cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$

15.5 pMpc \rightarrow R_{max}
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weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field
 \simeq pre-quasar HI density field

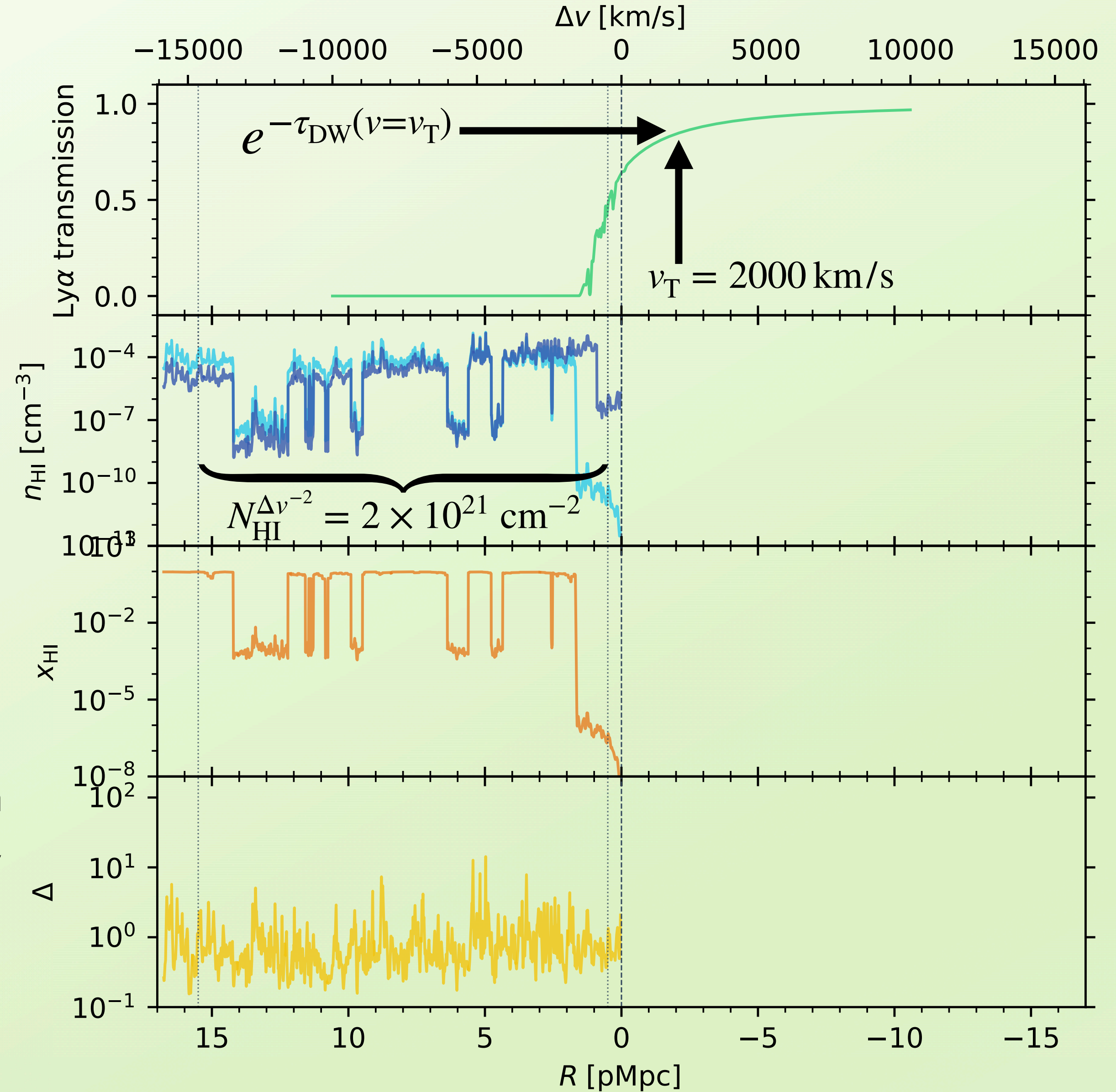
$\text{Ly}\alpha$ cross section
 \simeq Lorentzian

(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$

15.5 pMpc \rightarrow R_{max}
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weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$



Constructing a new label that minimizes IGM transmission scatter

damping wing optical depth

$$\tau_{\text{DW}}(\lambda_{\text{obs}}) = \int_0^{R(z_{\text{QSO}})} n_{\text{HI}}^{\text{QSO}}(R) \times \sigma_{\alpha}(\nu(R)) dR$$

post-quasar HI density field
 \simeq pre-quasar HI density field

Ly α cross section
 \simeq Lorentzian

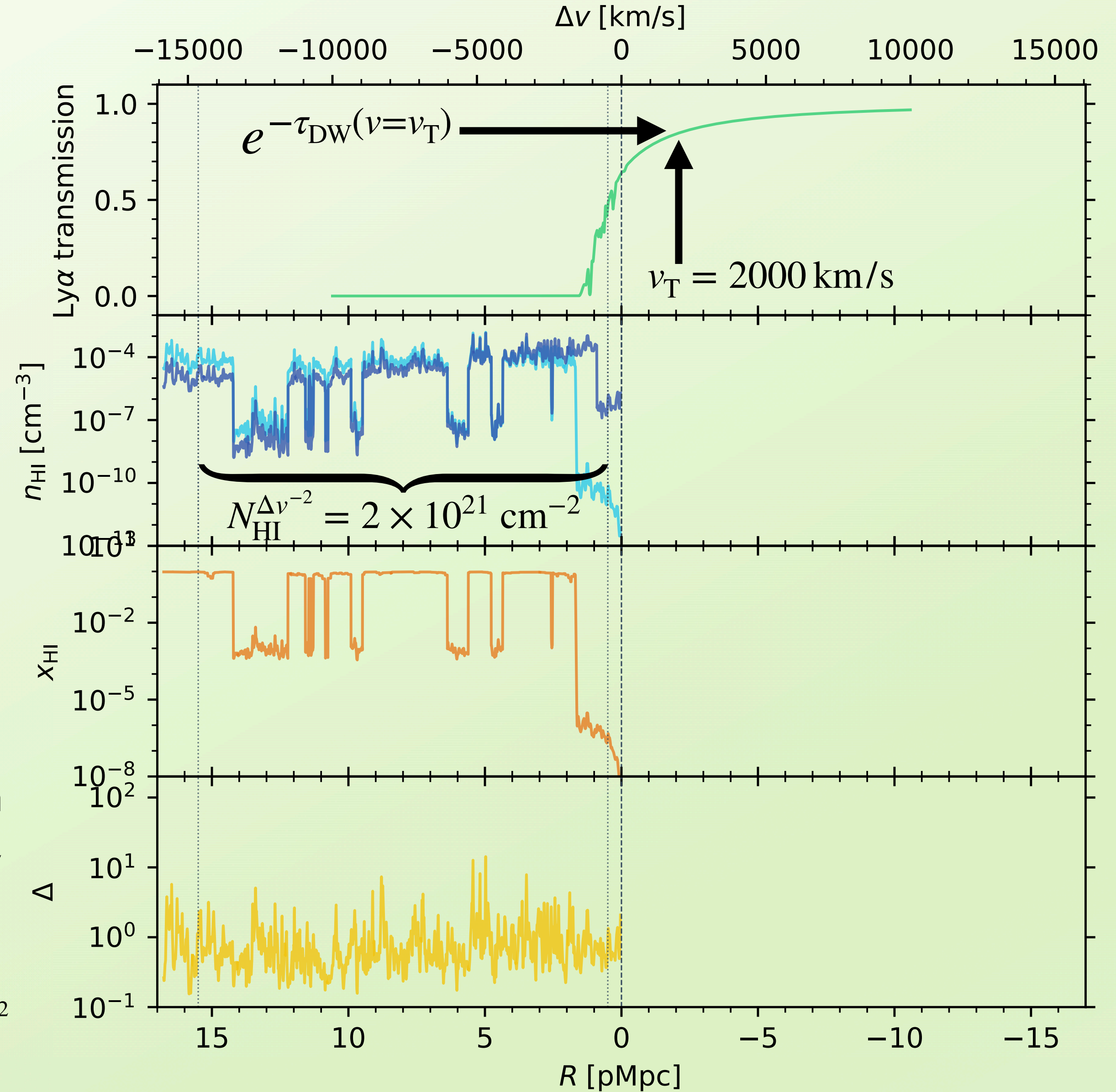
(velocity-weighted) HI column density

$$(N_{\text{HI}})^w = \int_{R_{\text{min}}}^{R_{\text{max}}} n_{\text{HI}}^{\text{gal}}(R) \times w(R) dR$$

15.5 pMpc \rightarrow R_{max}
 0.5 pMpc \rightarrow R_{min}

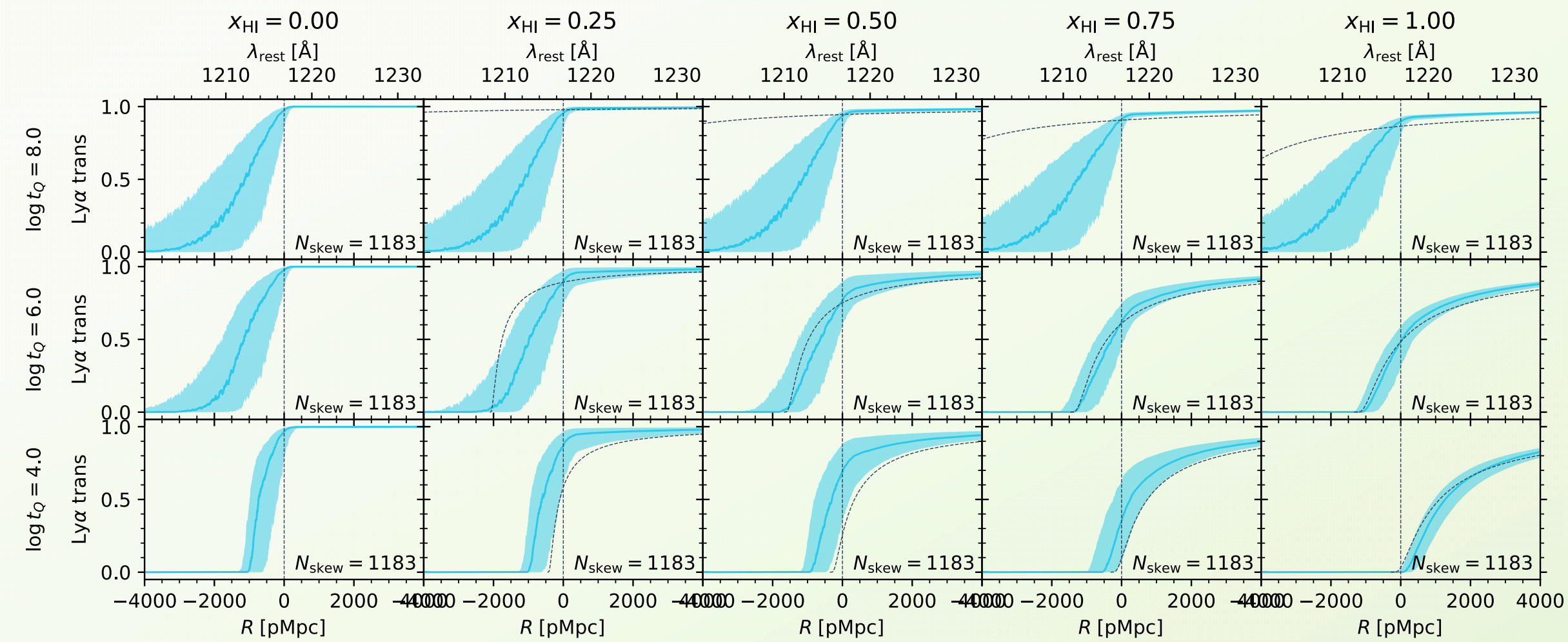
weighting function
 $w(R) \equiv \mathcal{N} \times (v - v_{\text{T}})^{-2}$

$$\tau_{\text{DW}}(v = v_{\text{T}}) = \dots \simeq \frac{e^2}{m_e c} \frac{f_{\alpha} \gamma_{\alpha}}{\nu_{\alpha}} \frac{(c/H(z_{\text{QSO}}) - R_{\text{T}})^2}{(R_{\text{max}} + R_{\text{T}})(R_{\text{min}} + R_{\text{T}})} \times N_{\text{HI}}^{\Delta v^{-2}}$$

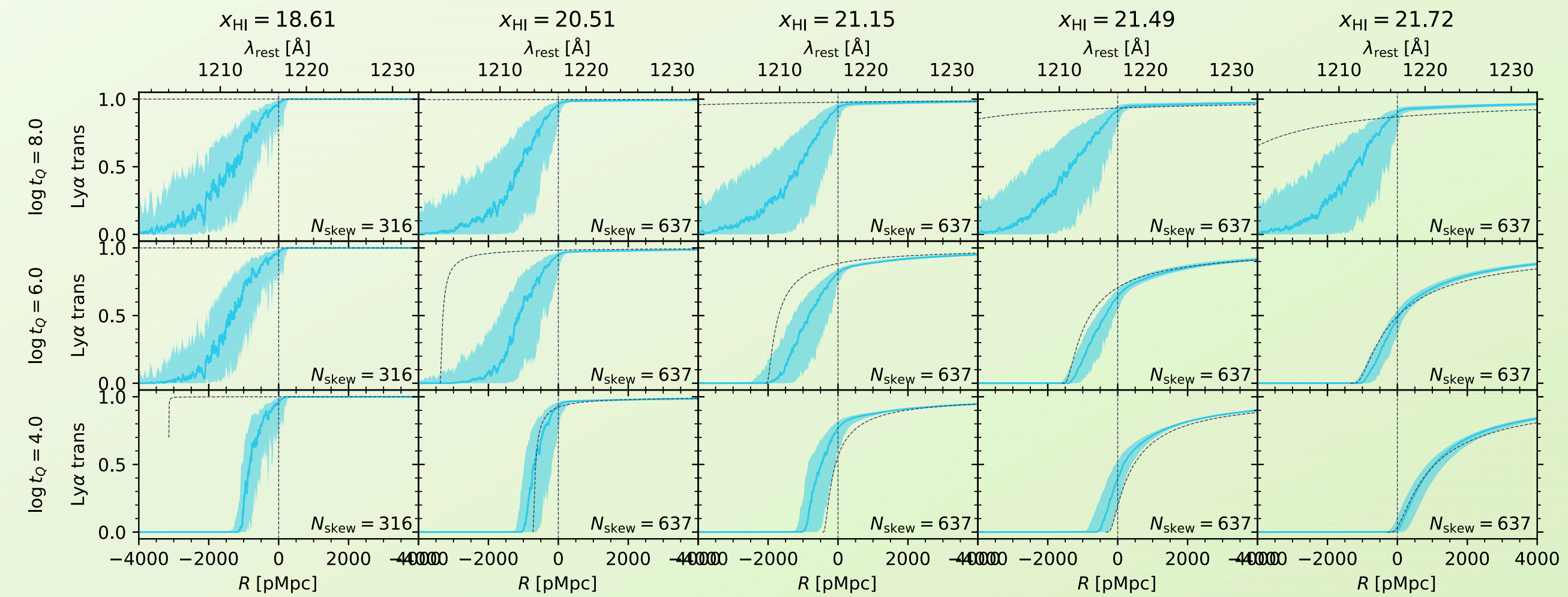


Comparing the old and new labels

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

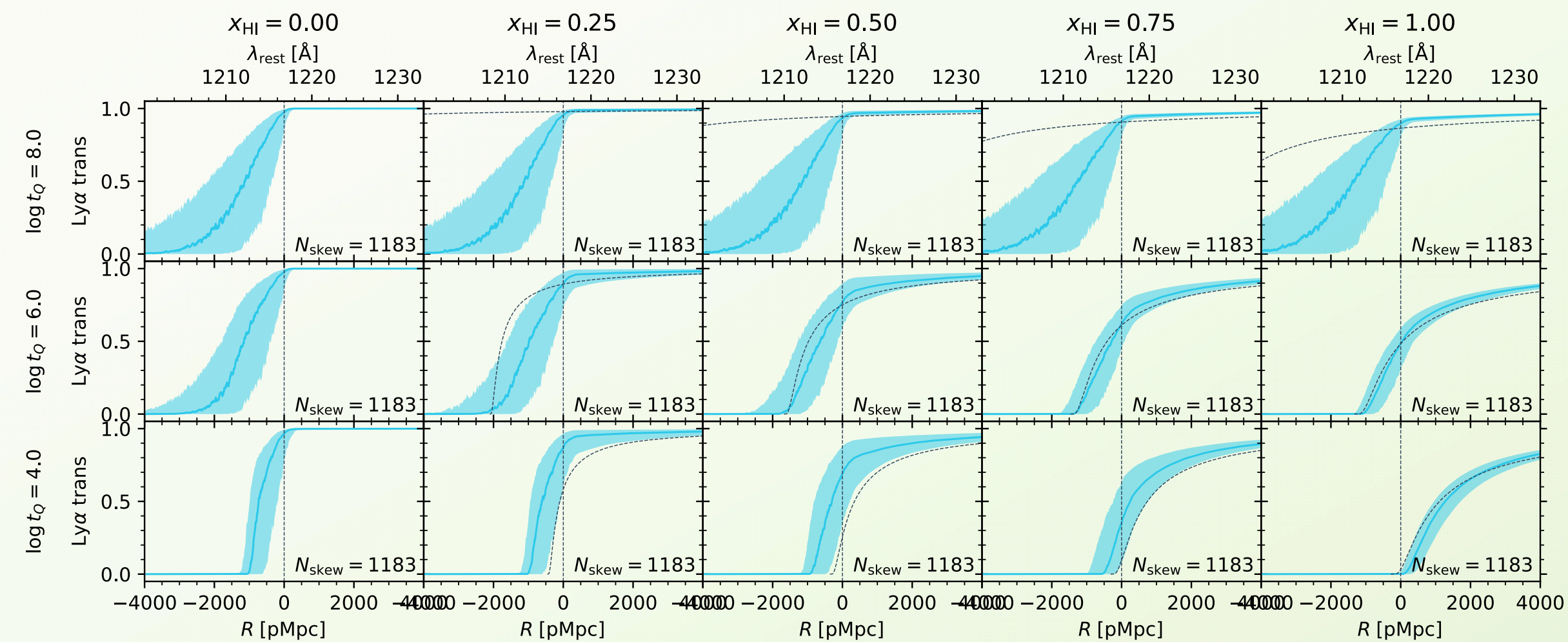


Local HI column density $N_{\text{HI}} \Delta v^{-2}$

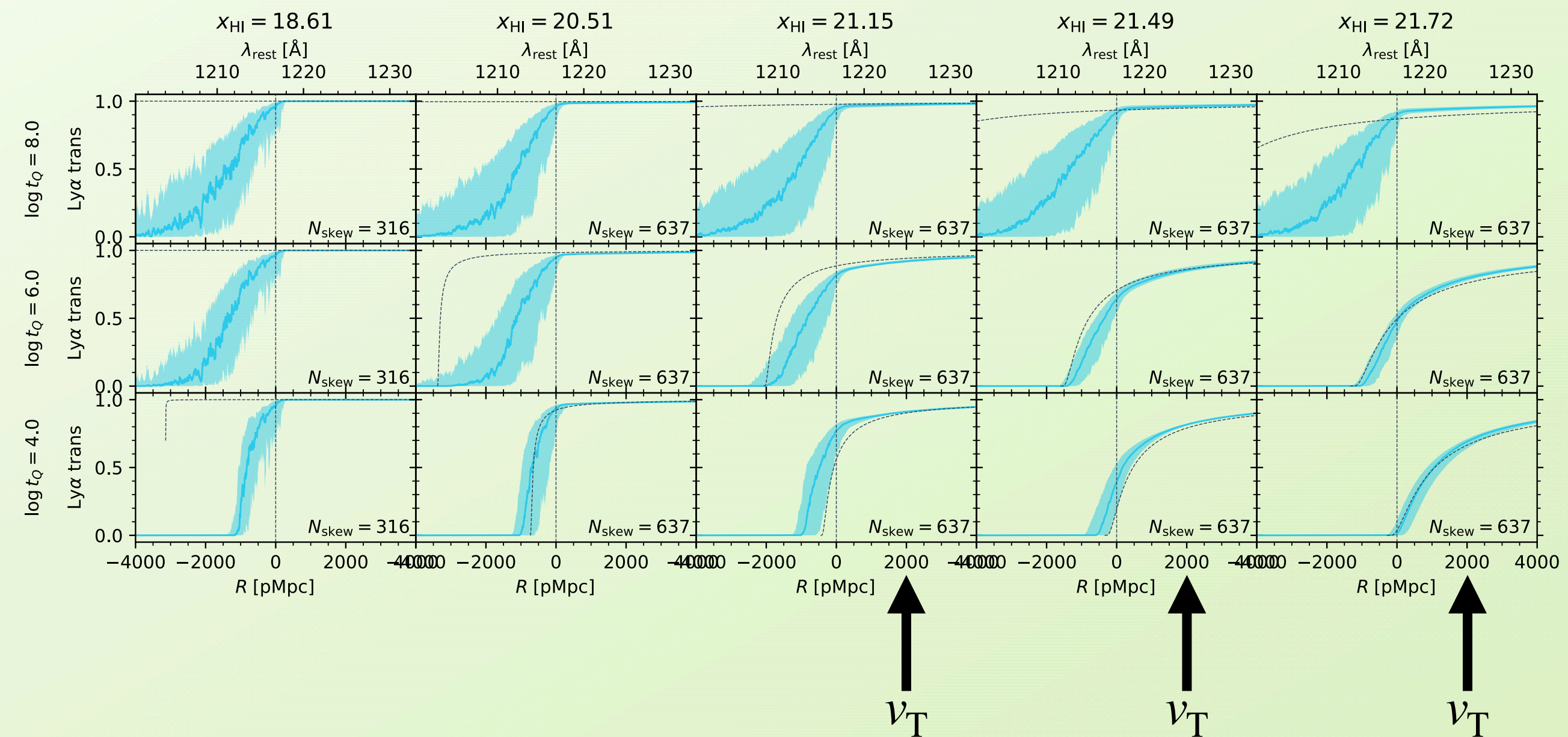


Comparing the old and new labels

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

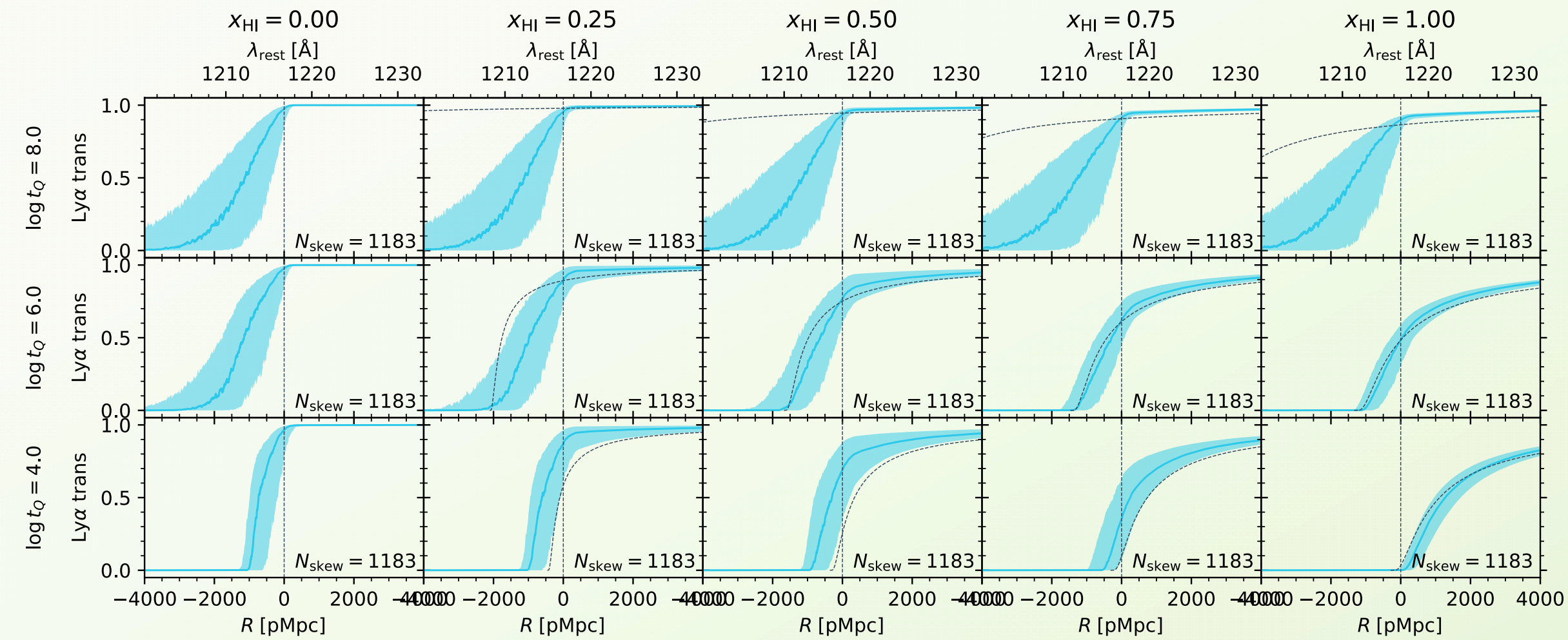


Local HI column density $N_{\text{HI}}^{\Delta v^{-2}}$

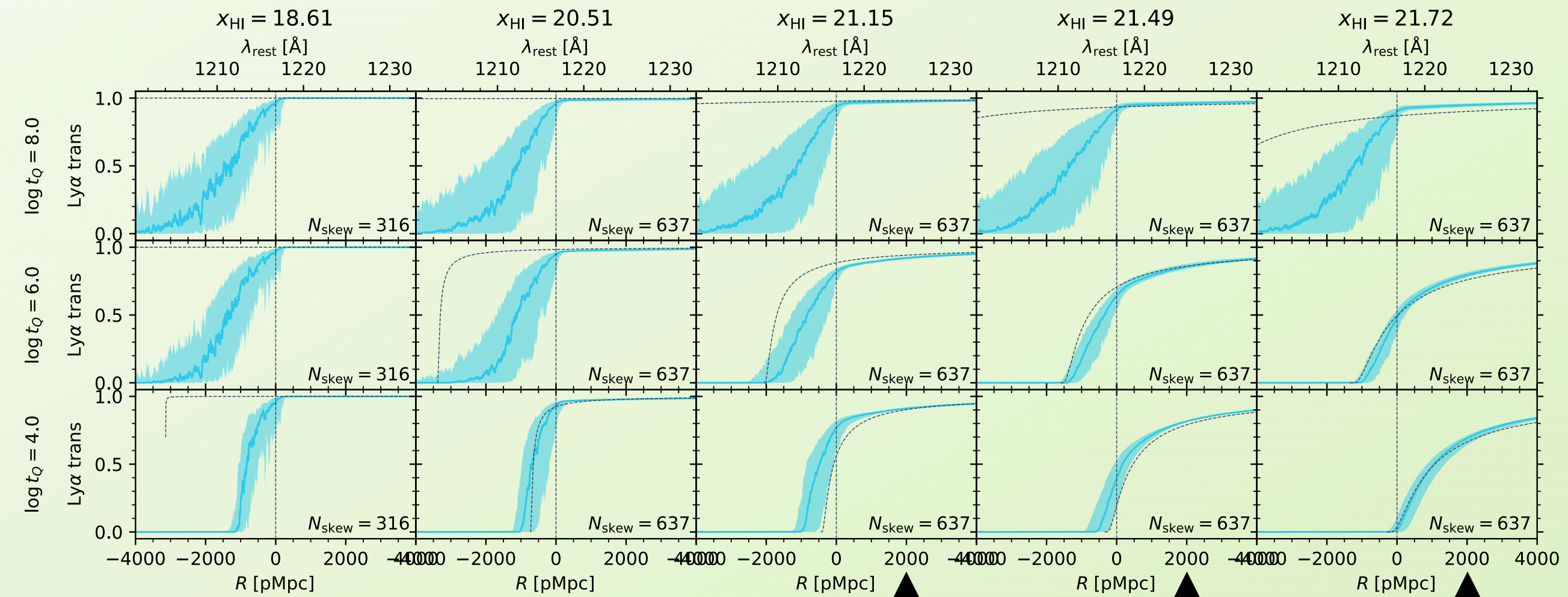


Comparing the old and new labels

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$



Local HI column density $N_{\text{HI}}^{\Delta v^{-2}}$

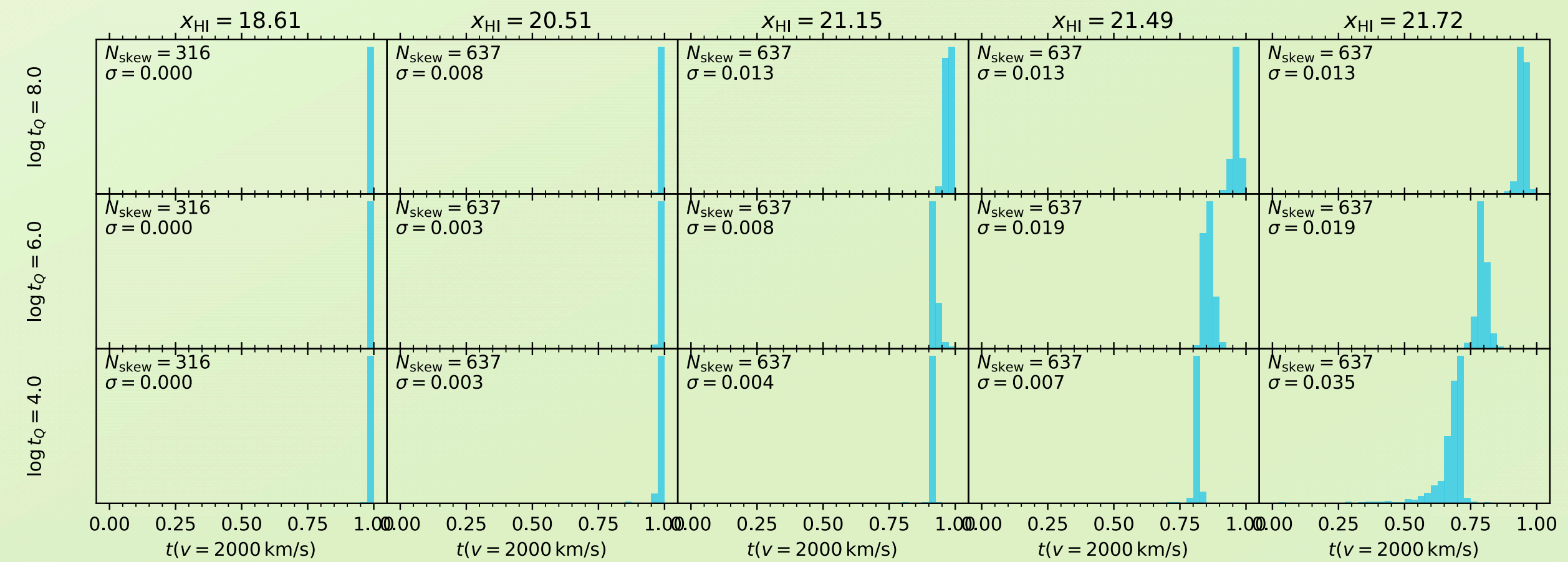
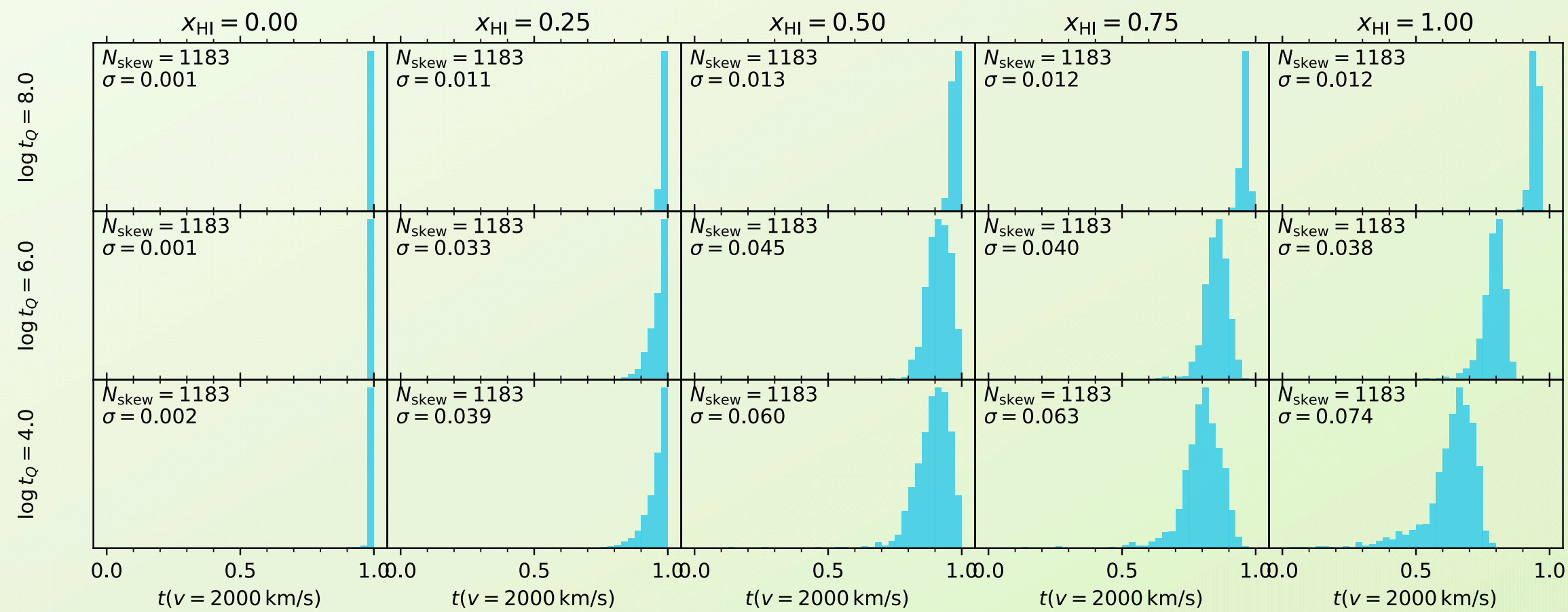


distribution of transmission values at $v_T = 2000 \text{ km/s}$

\uparrow
 v_T

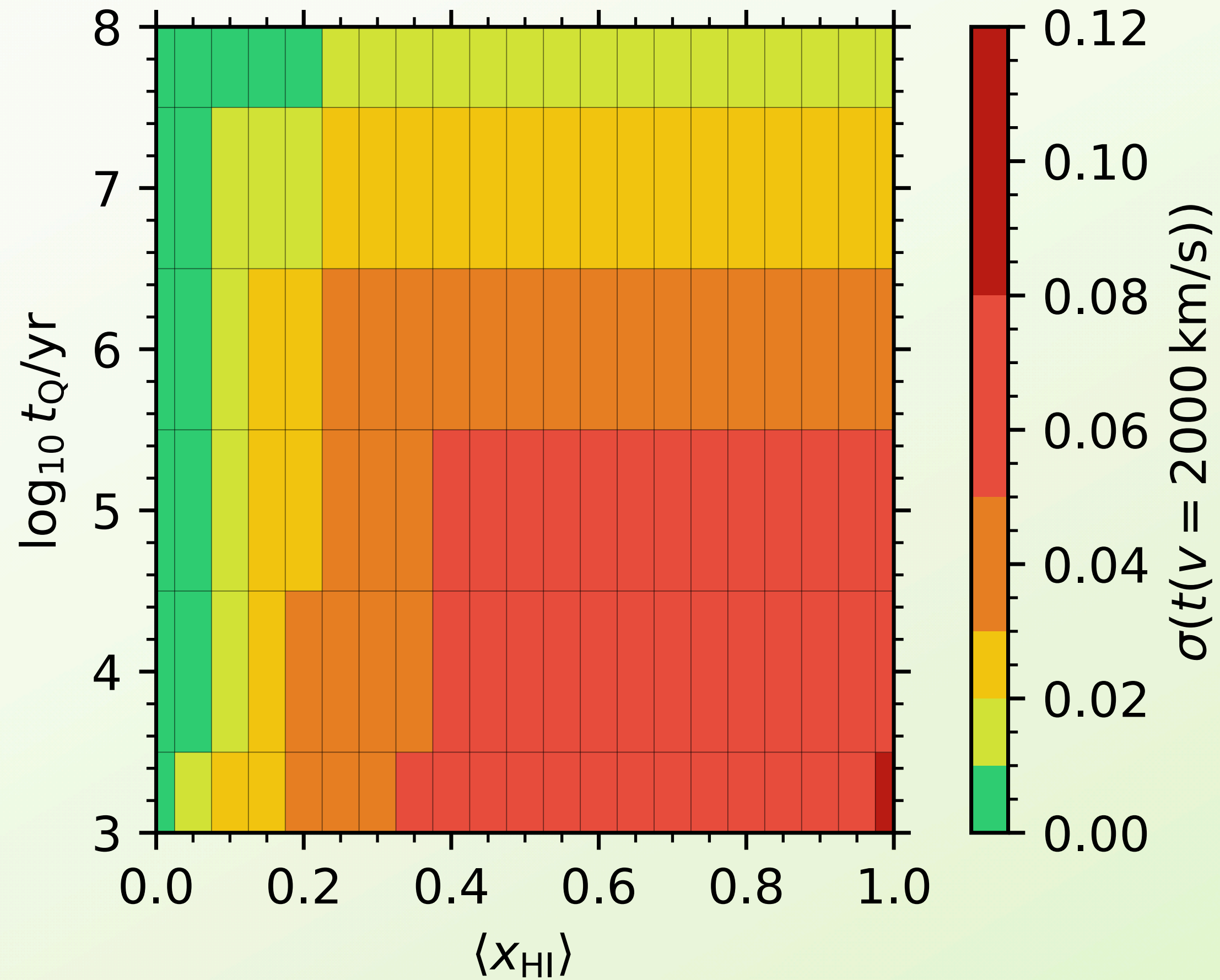
\uparrow
 v_T

\uparrow
 v_T

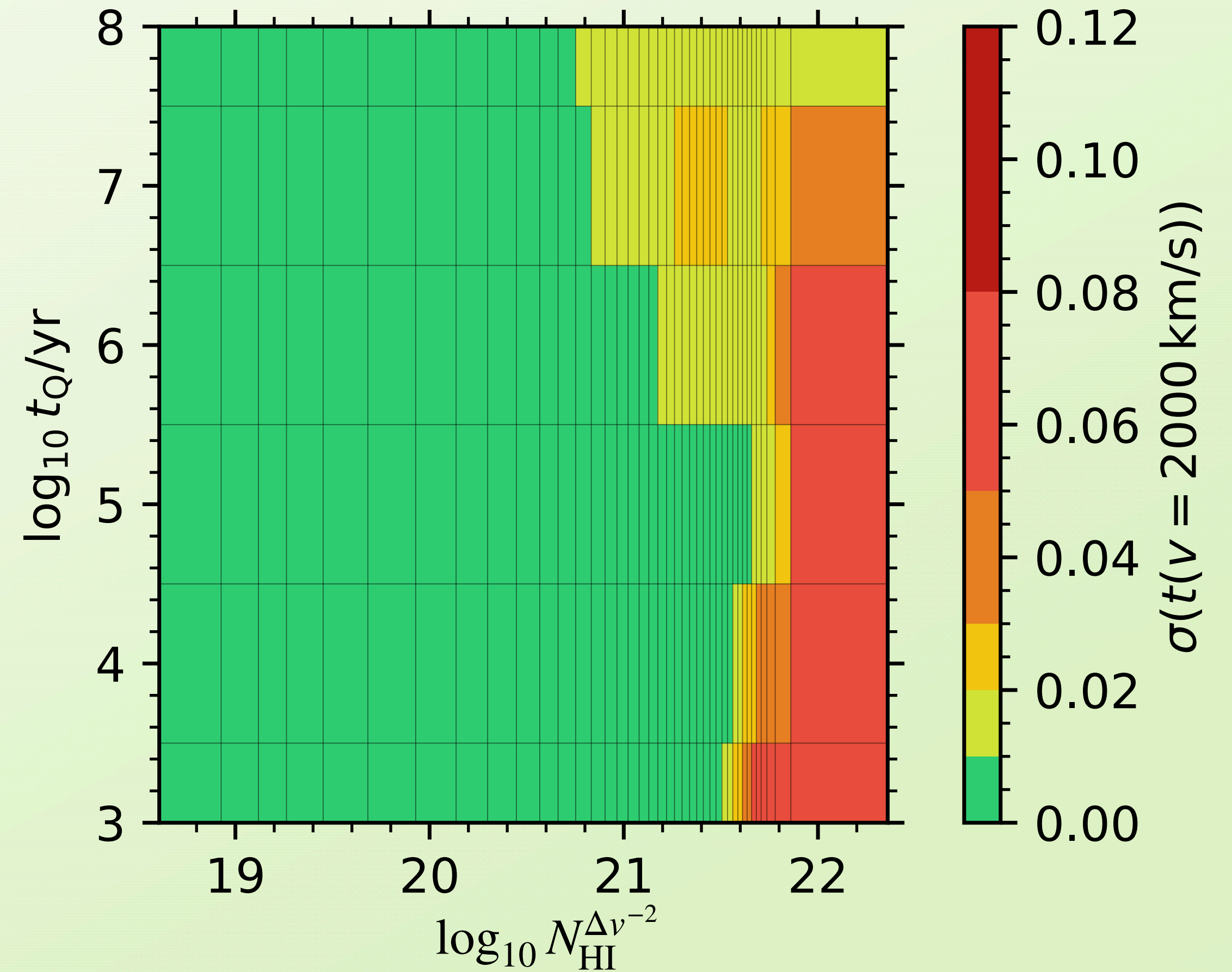


Comparing the old and new labels

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

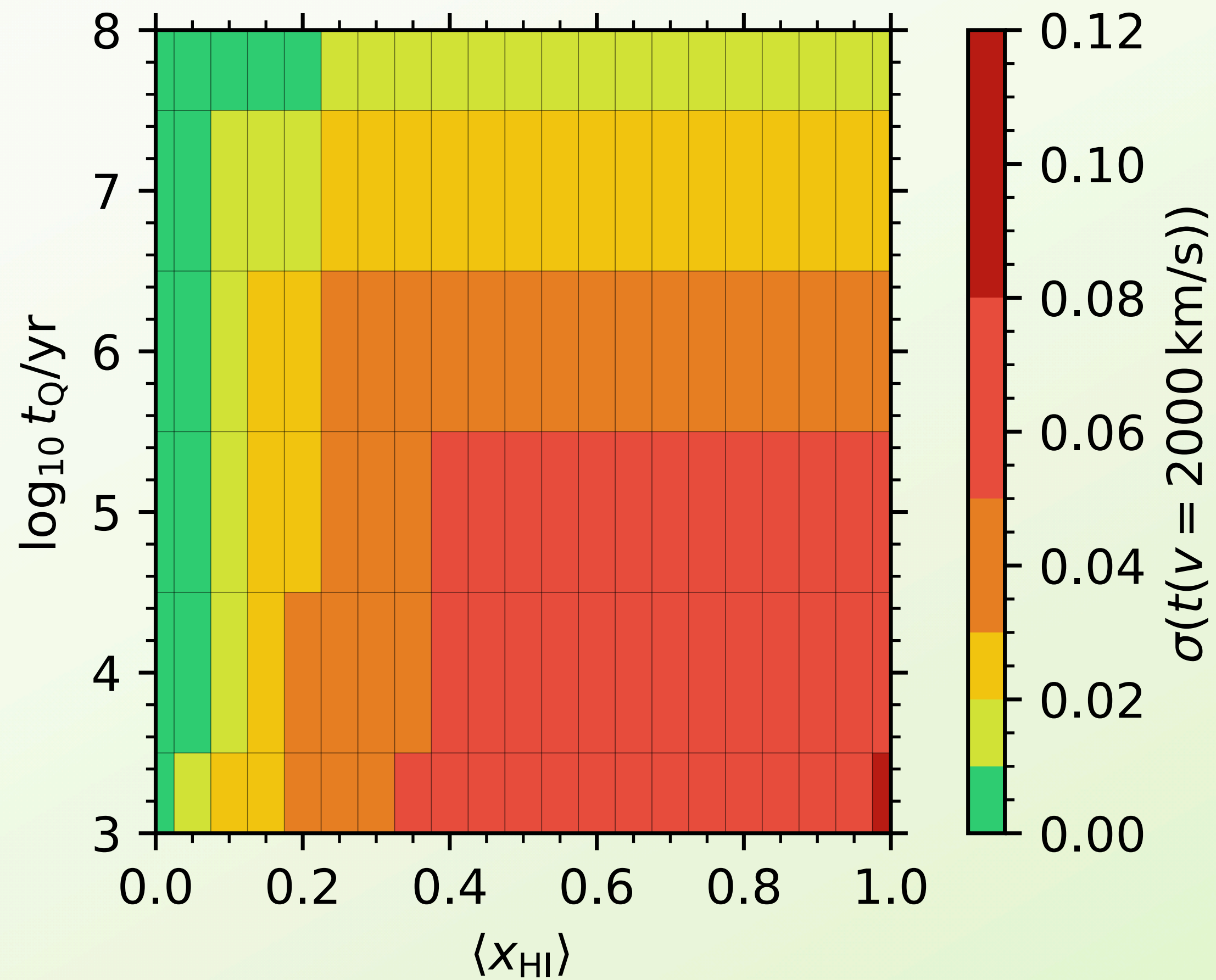


Local HI column density $N_{\text{HI}}^{\Delta v^{-2}}$

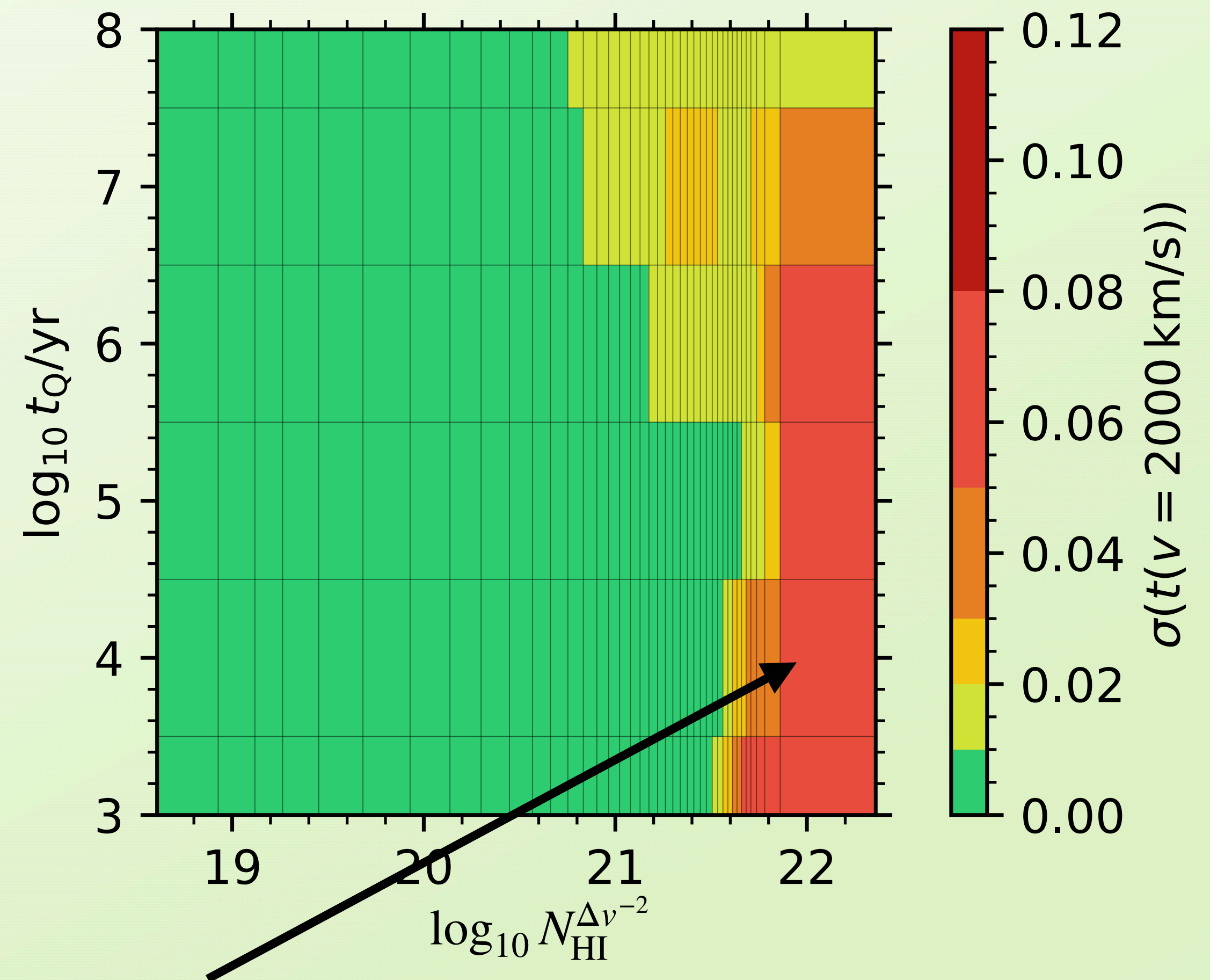


Comparing the old and new labels

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

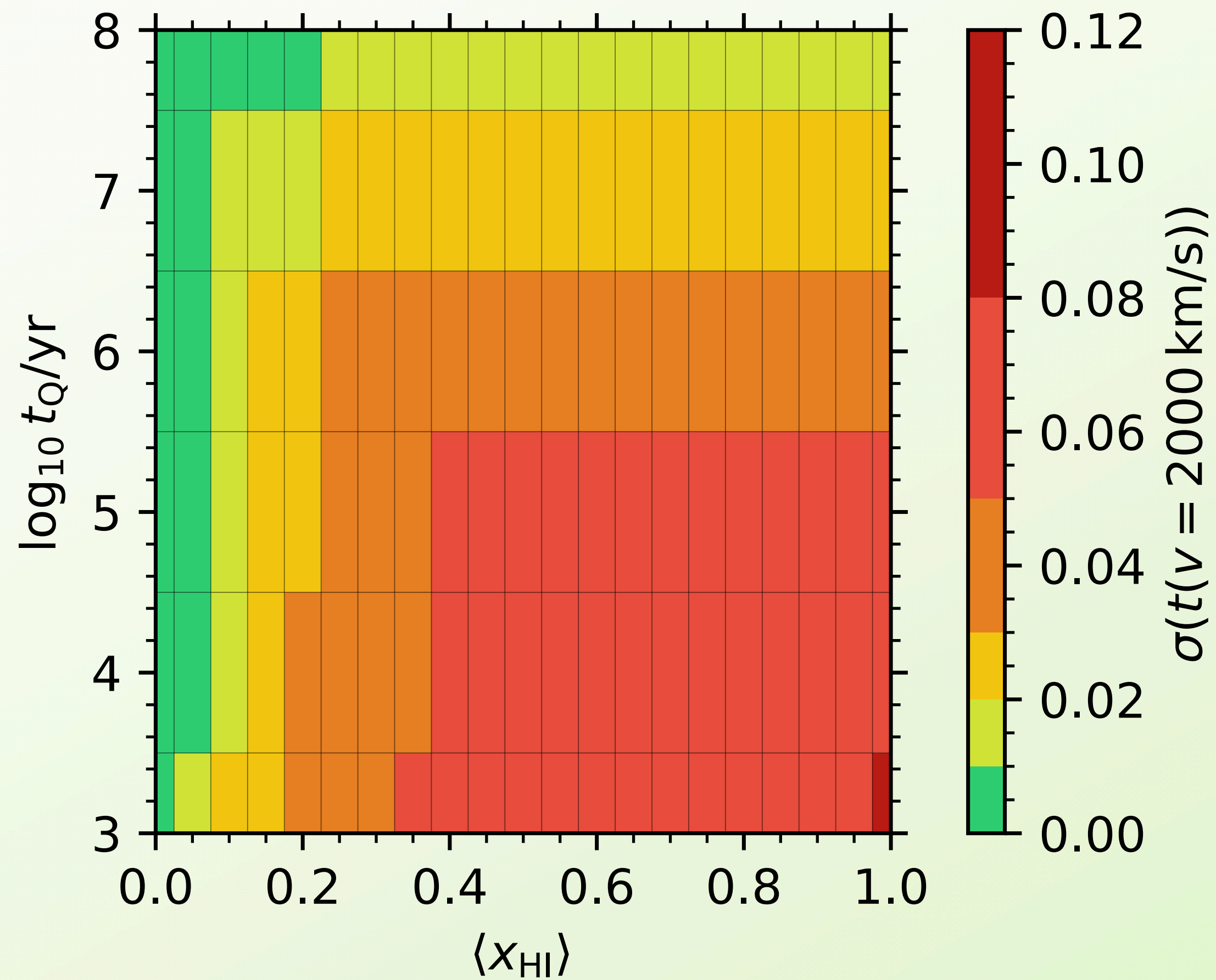


Local HI column density $N_{\text{HI}}^{\Delta v^{-2}}$

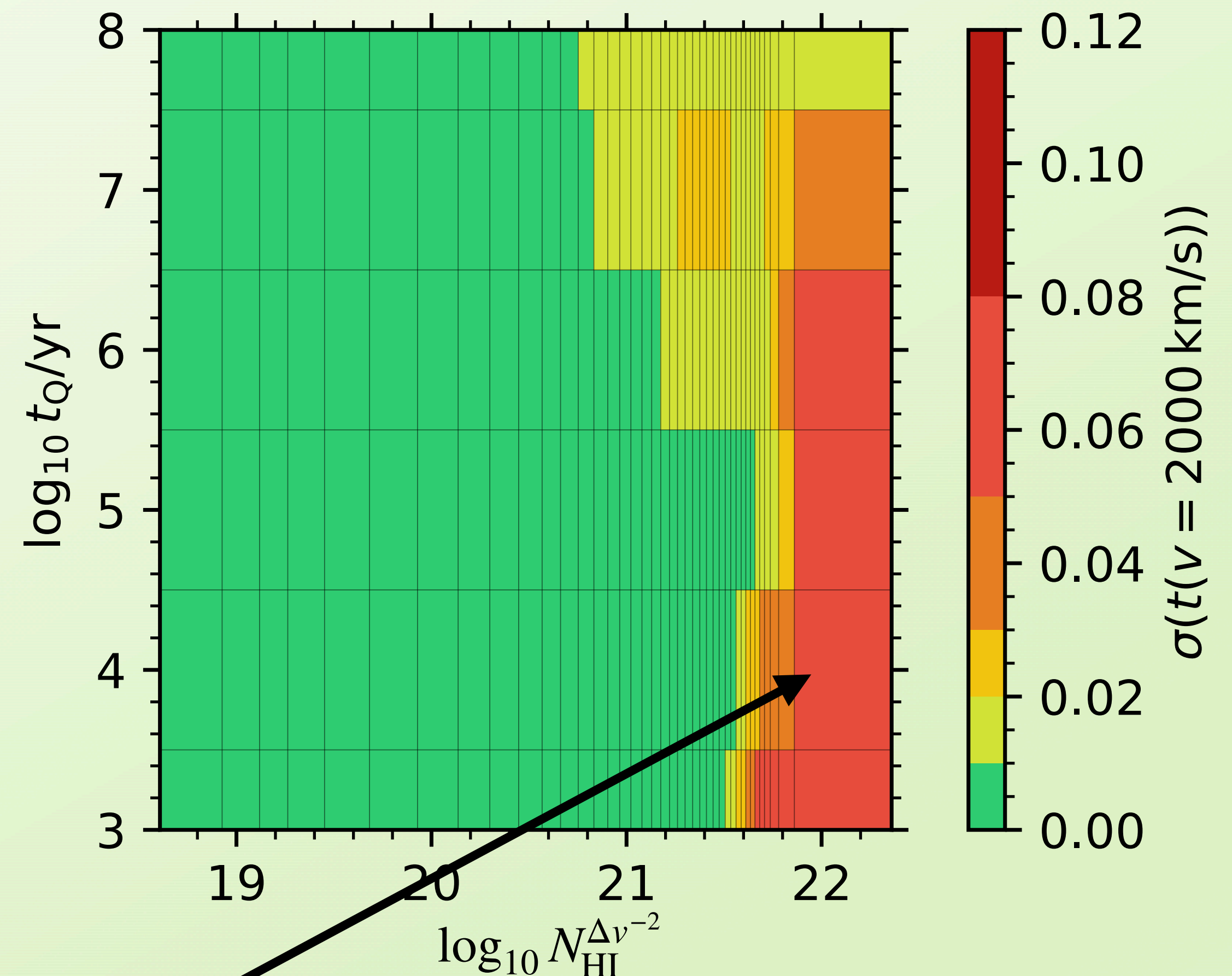


Comparing the old and new labels

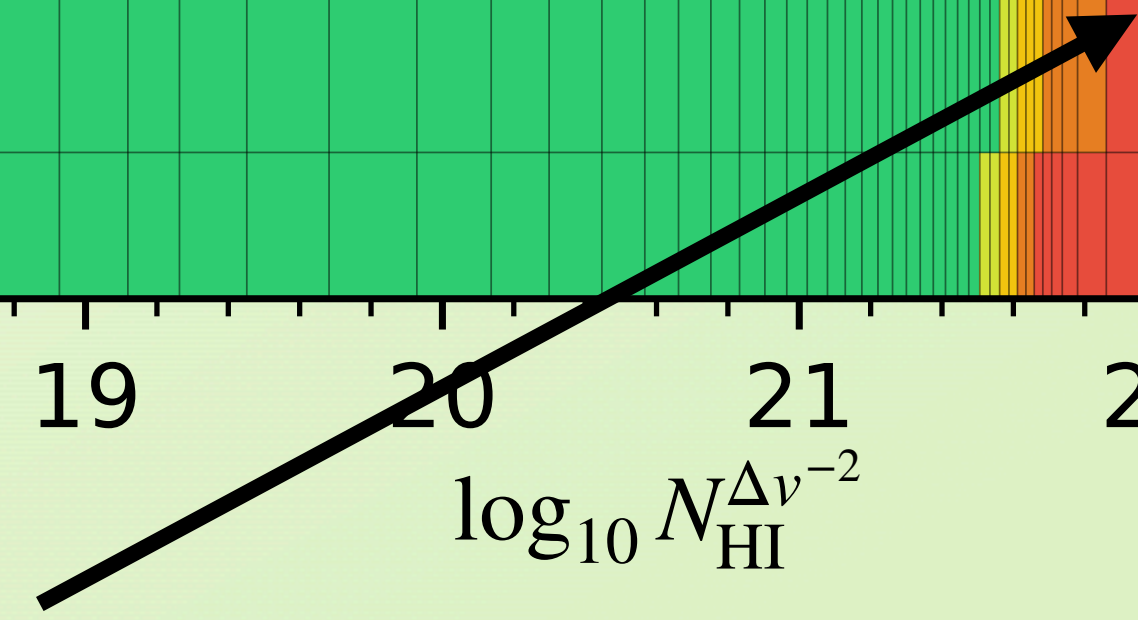
Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$



Local HI column density $N_{\text{HI}}^{\Delta v^{-2}}$

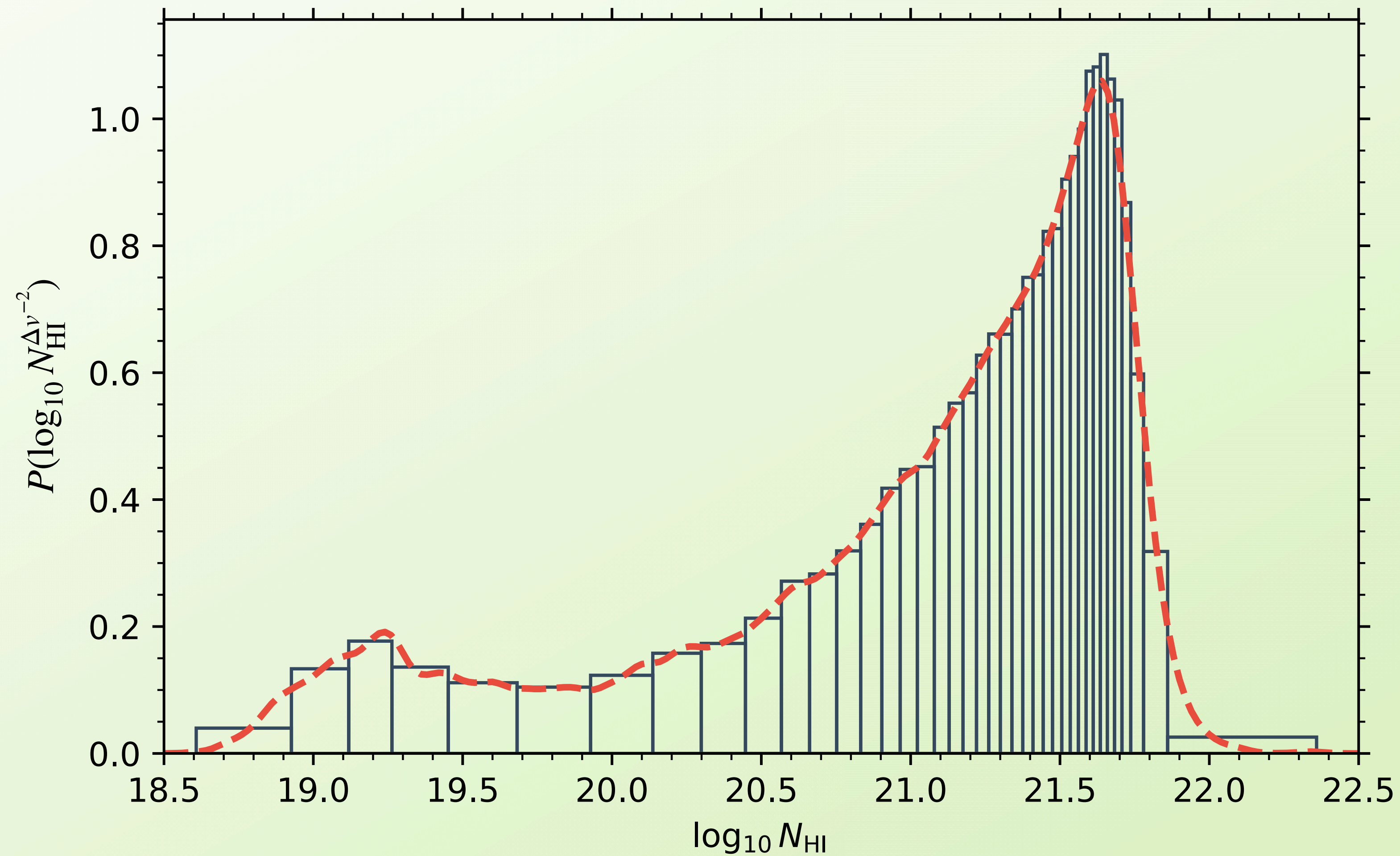


Strongest damping wings
→ impacted by structure at $< 0.5 \text{ pMpc}$



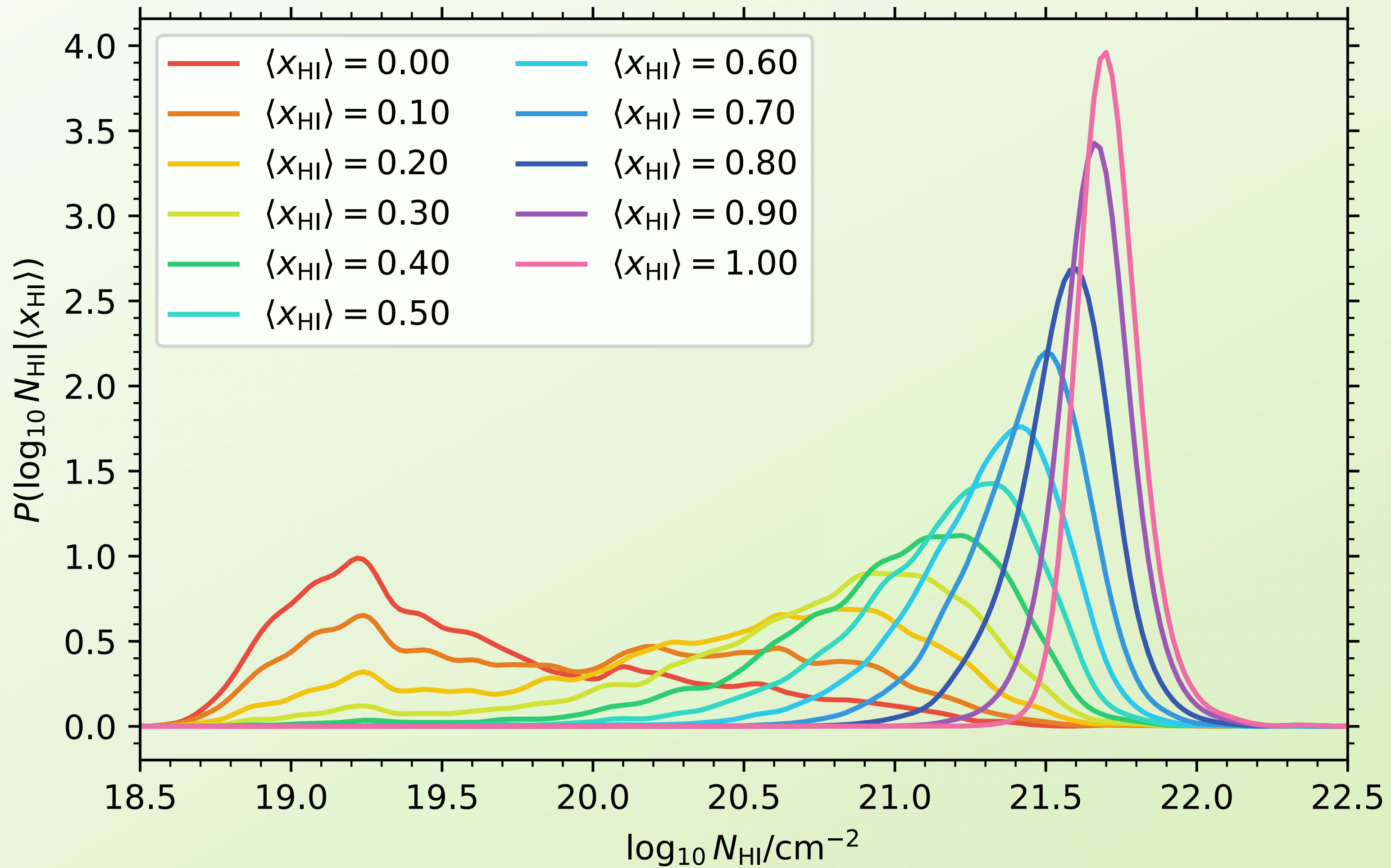
Relating the old and new labels

$N_{\text{HI}}^{\Delta v^{-2}}$ distribution based on skewers extracted from a uniform grid covering $0 \leq \langle x_{\text{HI}} \rangle \leq 1$



Relating the old and new labels

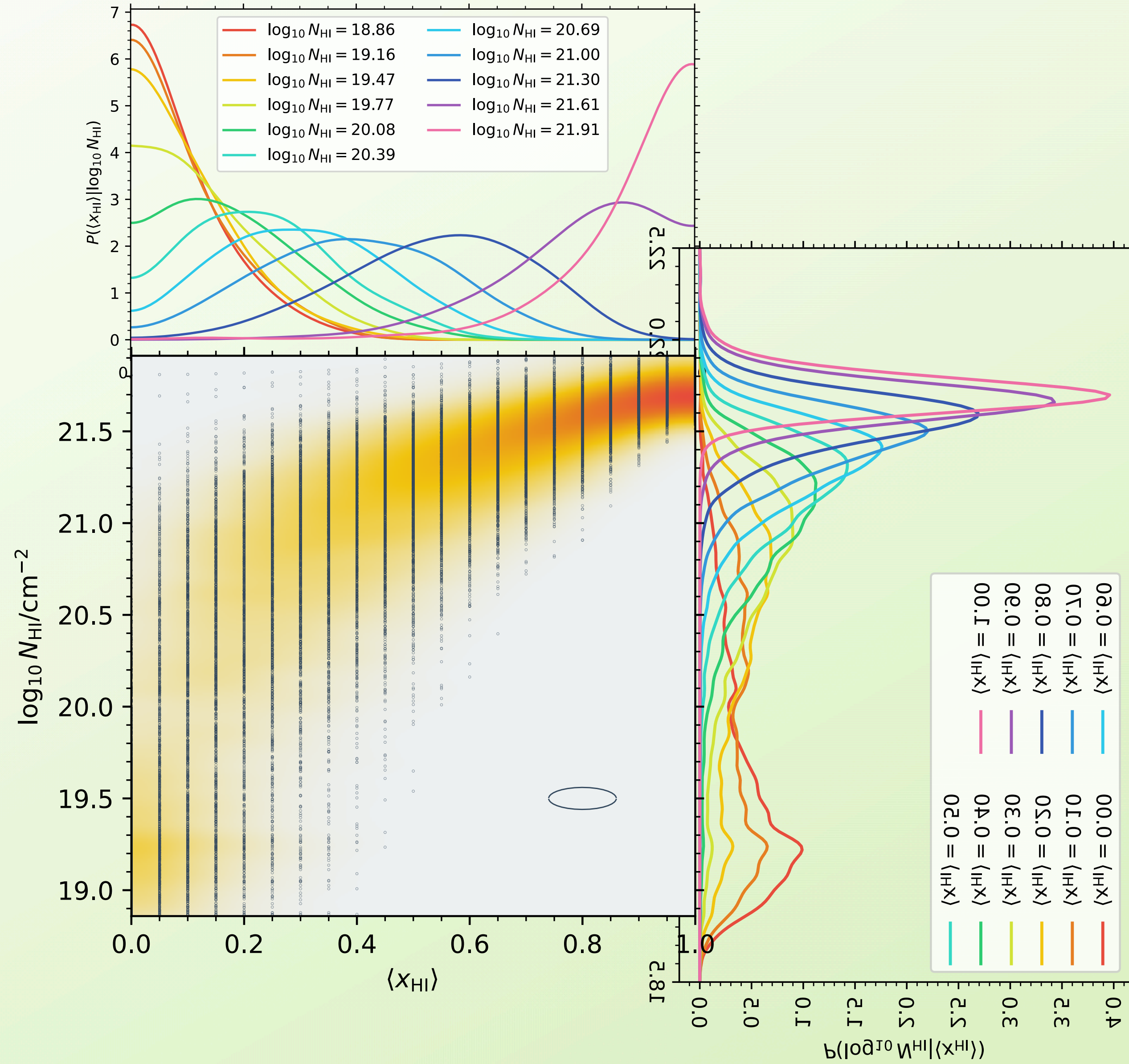
$N_{\text{HI}}^{\Delta y^{-2}}$ distribution at given $\langle x_{\text{HI}} \rangle$ values



Relating the old and new labels

$$P(\langle x_{\text{HI}} \rangle | N_{\text{HI}}^{\Delta v^{-2}})$$

$$P(N_{\text{HI}}^{\Delta v^{-2}}, \langle x_{\text{HI}} \rangle)$$

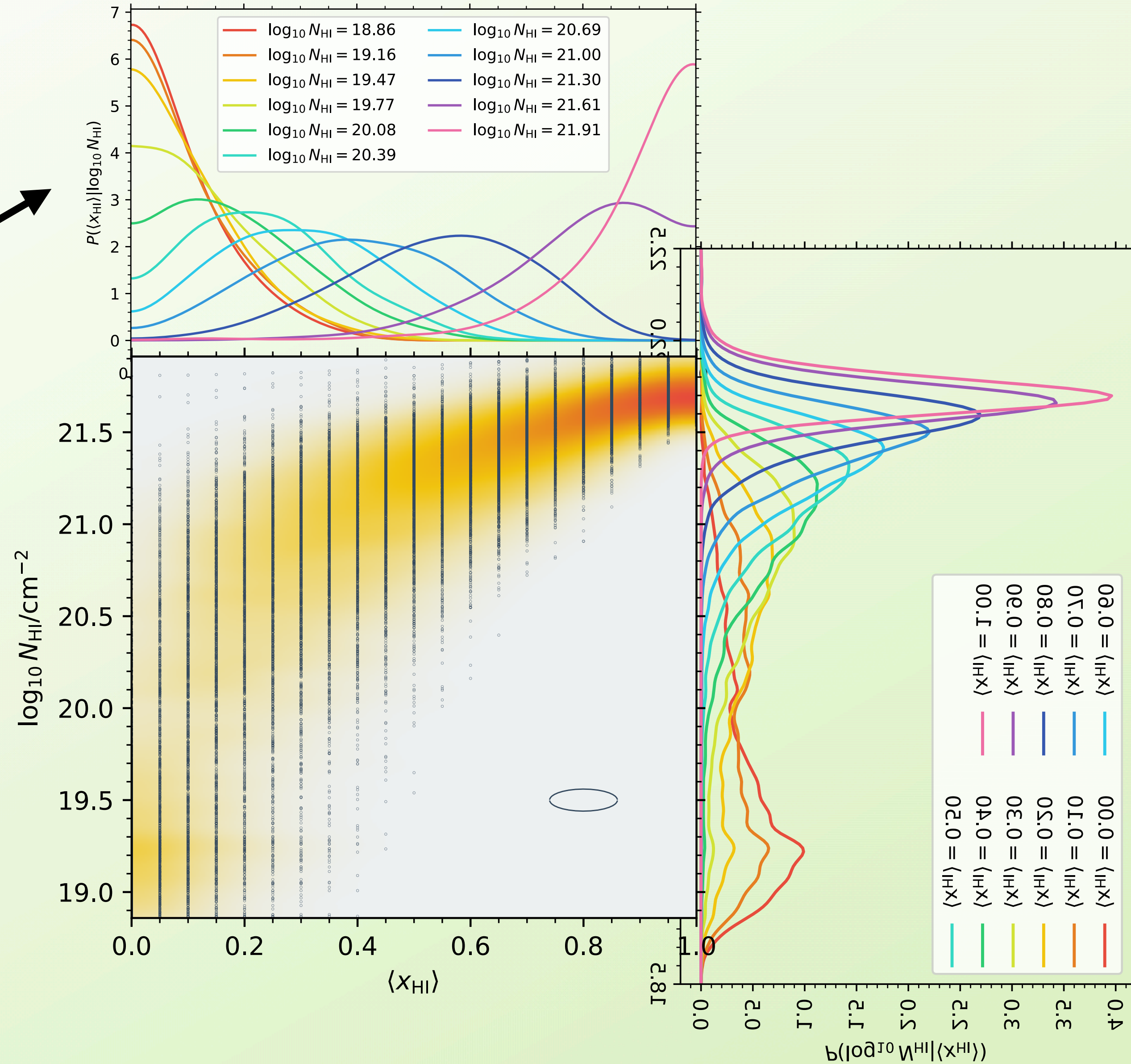


$$P(N_{\text{HI}}^{\Delta v^{-2}} | \langle x_{\text{HI}} \rangle)$$

Relating the old and new labels

$$P(\langle x_{\text{HI}} \rangle | N_{\text{HI}}^{\Delta v^{-2}})$$

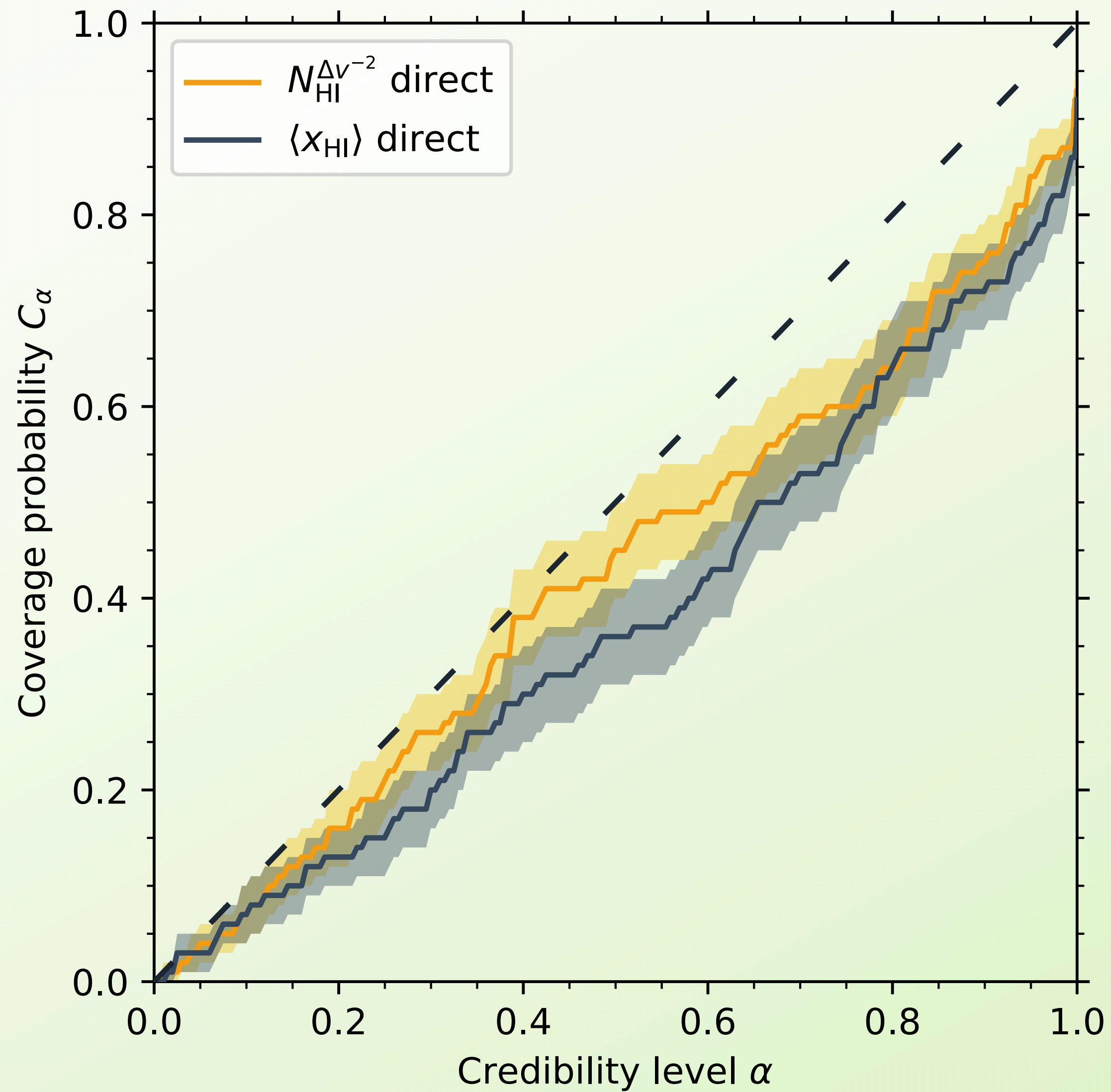
$$P(N_{\text{HI}}^{\Delta v^{-2}}, \langle x_{\text{HI}} \rangle)$$



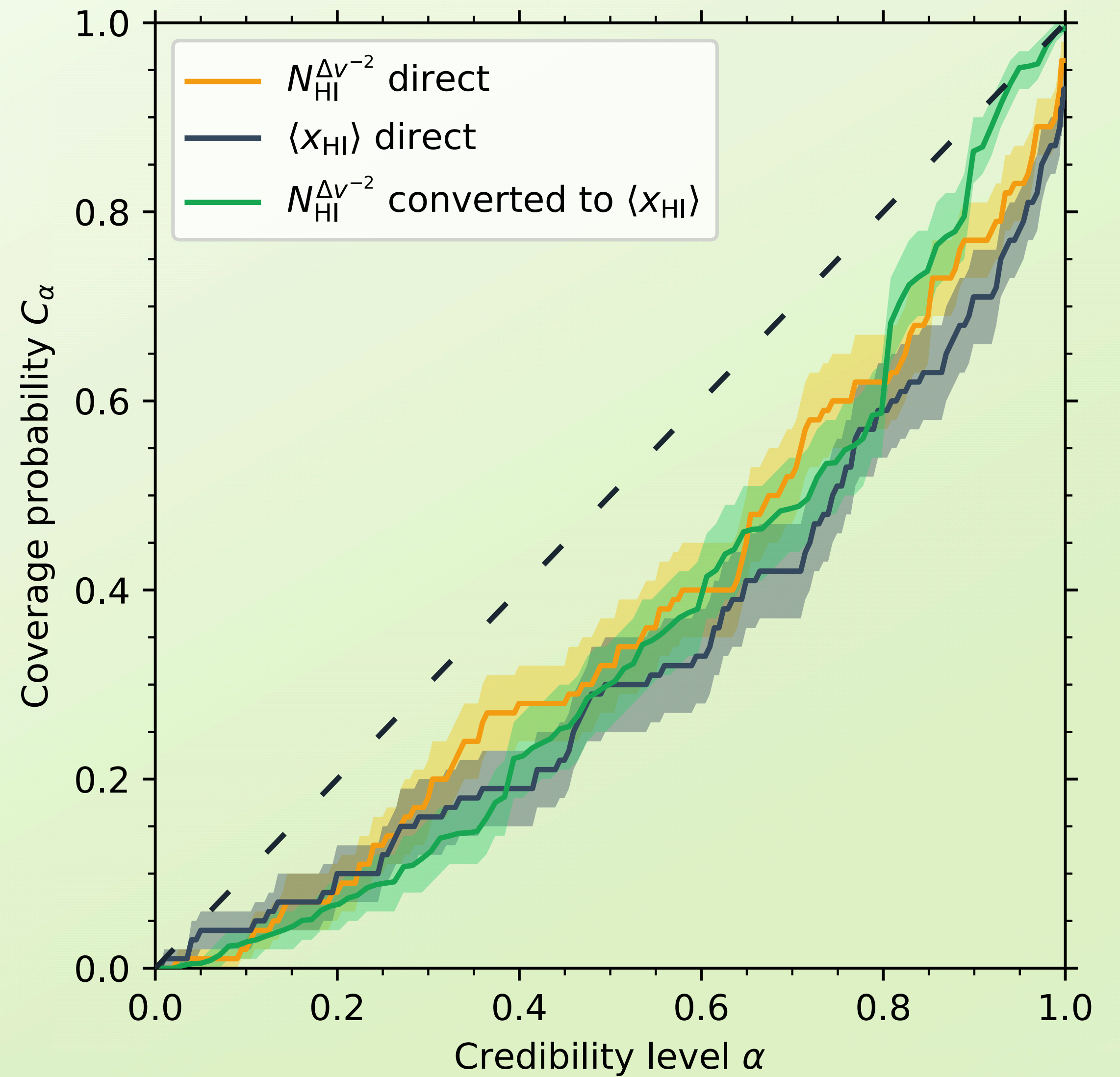
$$P(N_{\text{HI}}^{\Delta v^{-2}} | \langle x_{\text{HI}} \rangle)$$

Inference Tests

Full Coverage



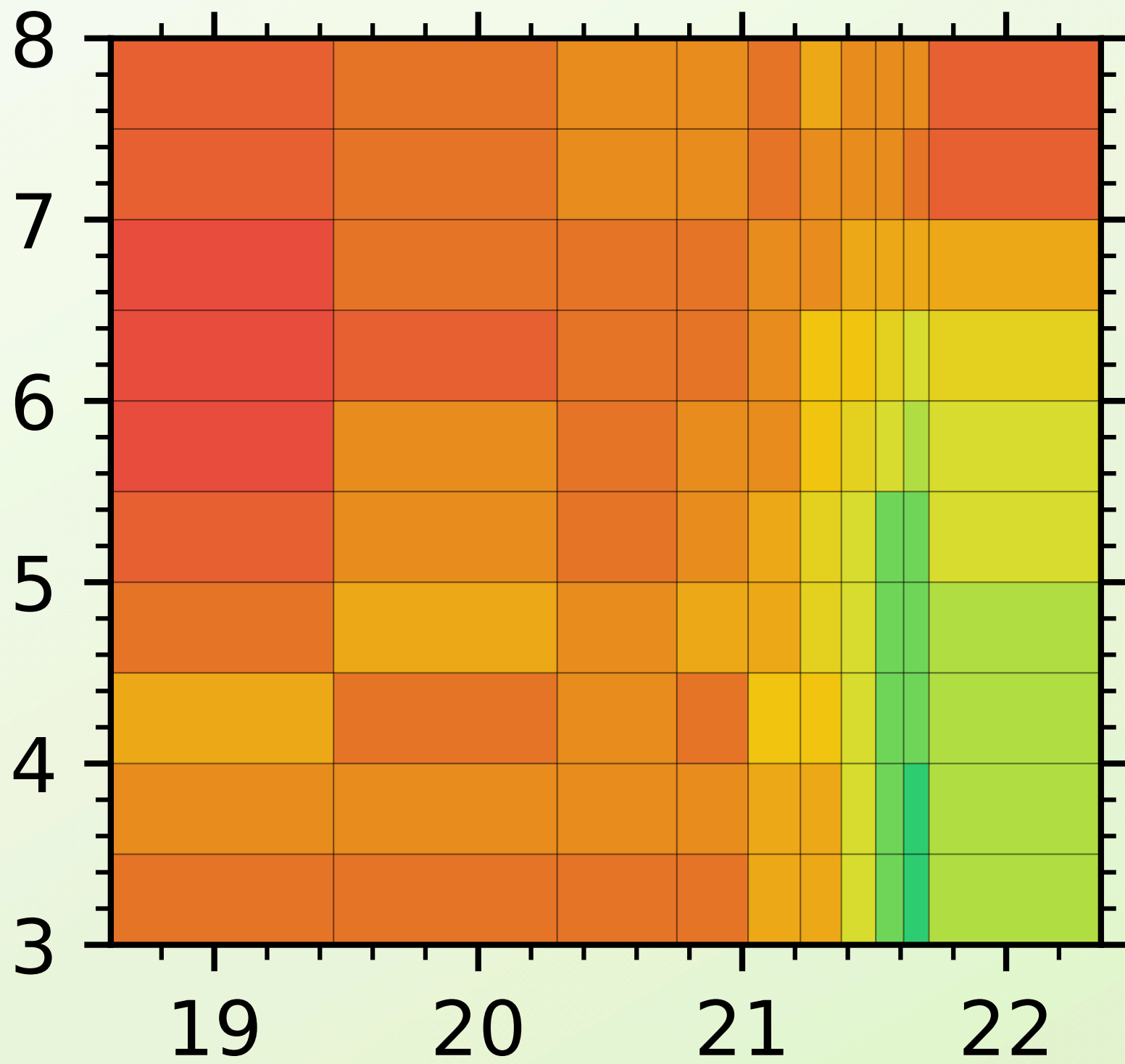
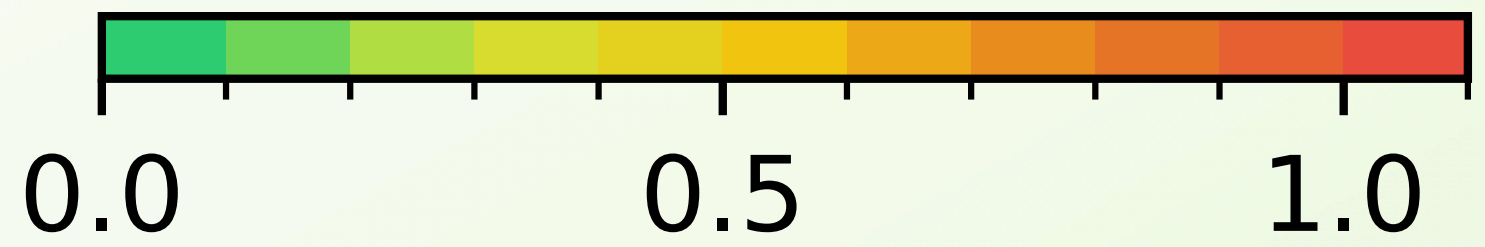
Marginal Coverage



Comparing Inference Precision

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

$\Delta_{68\%}(\log_{10} N_{\text{HI}}^{\Delta v^{-2}})$

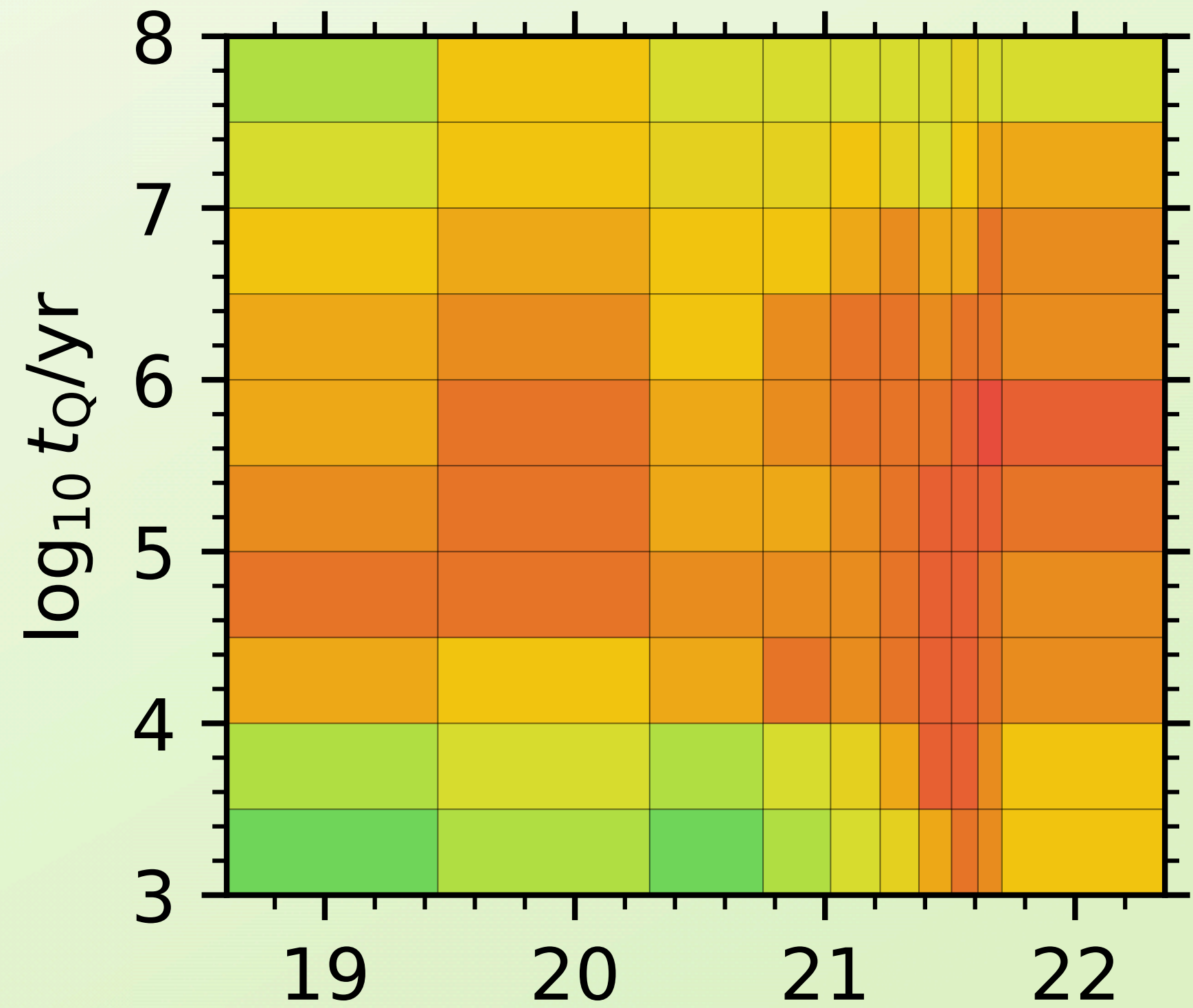
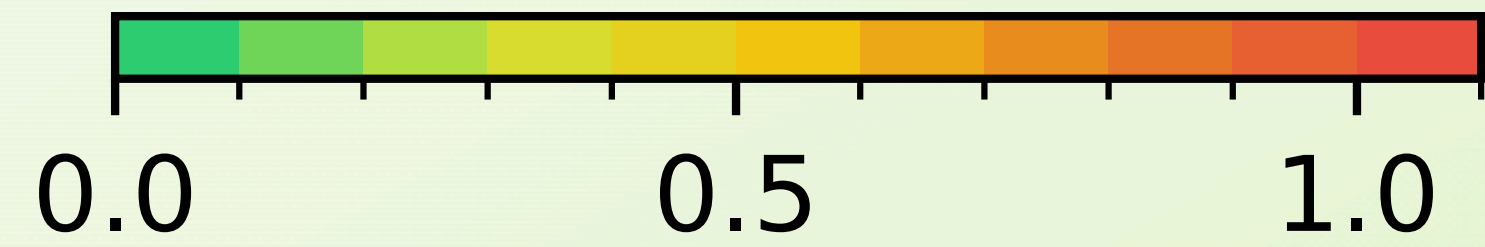


$0.69^{+0.34}_{-0.53}$ dex

$\log_{10} t_{\text{Q}}/\text{yr}$

$\log_{10} N_{\text{HI}}^{\Delta v^{-2}}/\text{cm}^{-2}$

$\Delta_{68\%}(\log_{10} t_{\text{Q}}/\text{yr})$



$0.75^{+0.27}_{-0.52}$ dex

$\log_{10} N_{\text{HI}}^{\Delta v^{-2}}/\text{cm}^{-2}$

Comparing Inference Precision

Global IGM neutral fraction $\langle x_{\text{HI}} \rangle$

$\Delta_{68\%}(\langle x_{\text{HI}} \rangle)$

$\Delta_{68\%}(\log_{10} t_{\text{Q}}/\text{yr})$

