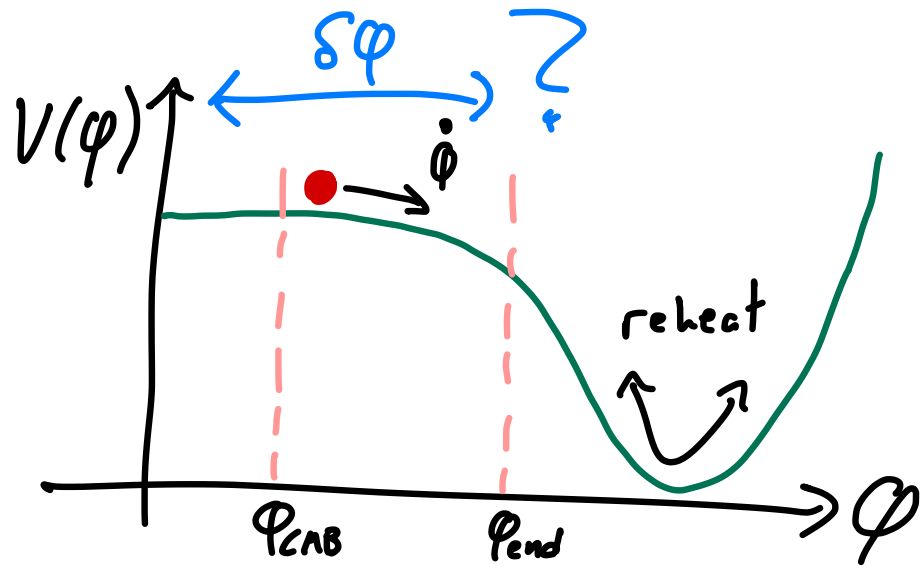


# Large Deviations in the Early Universe

Tim Cohen  
CERN/EPFL/UOregon

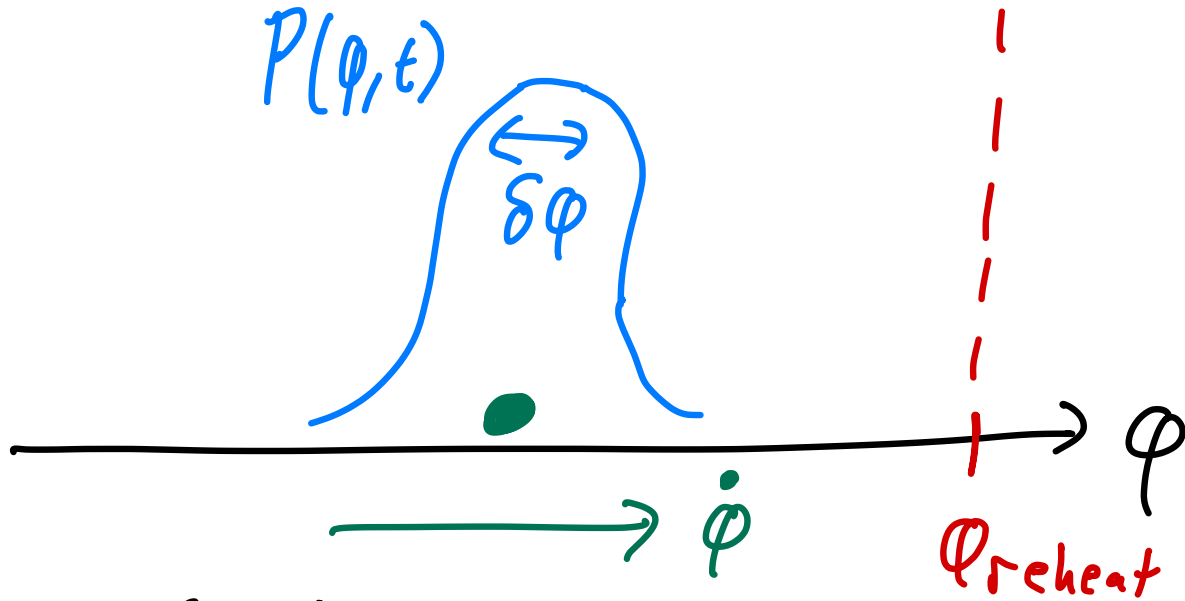
with  
Dan Green  
Akhil Premkumar



CERN

September 4, 2023

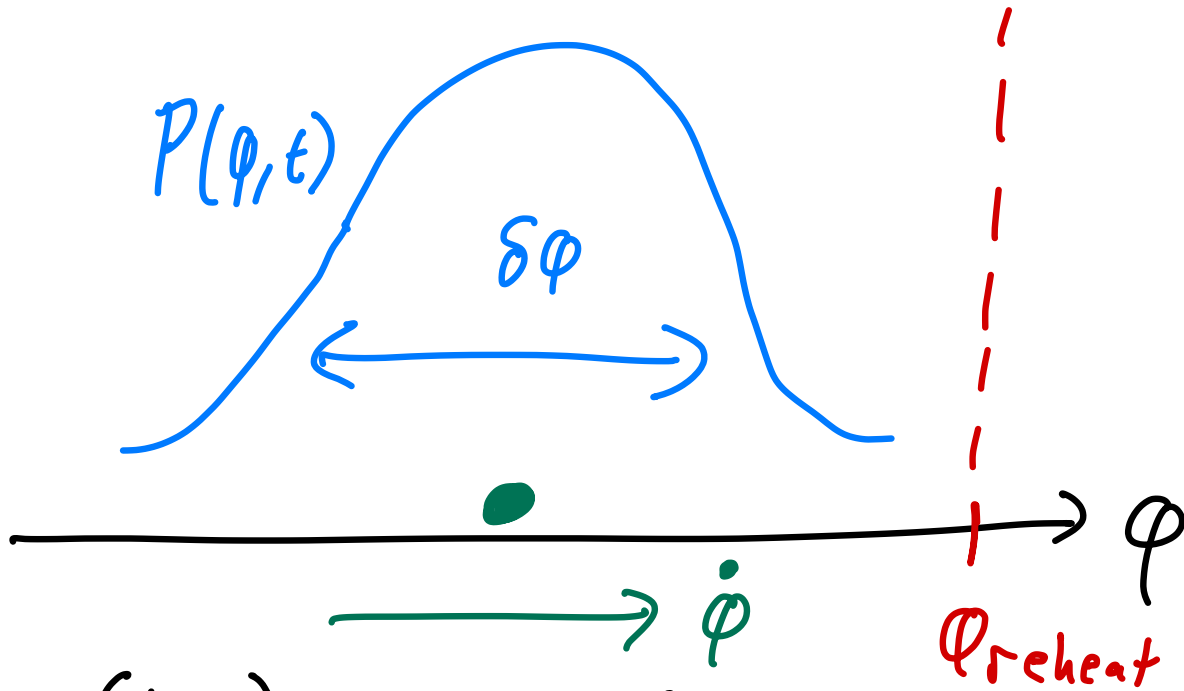
# Inflaton Fluctuations



$$(\Delta\phi)_{\text{classical}} > (\Delta\phi)_{\text{noise}}$$

Small  $\delta\phi \Rightarrow$  universal end to inflation

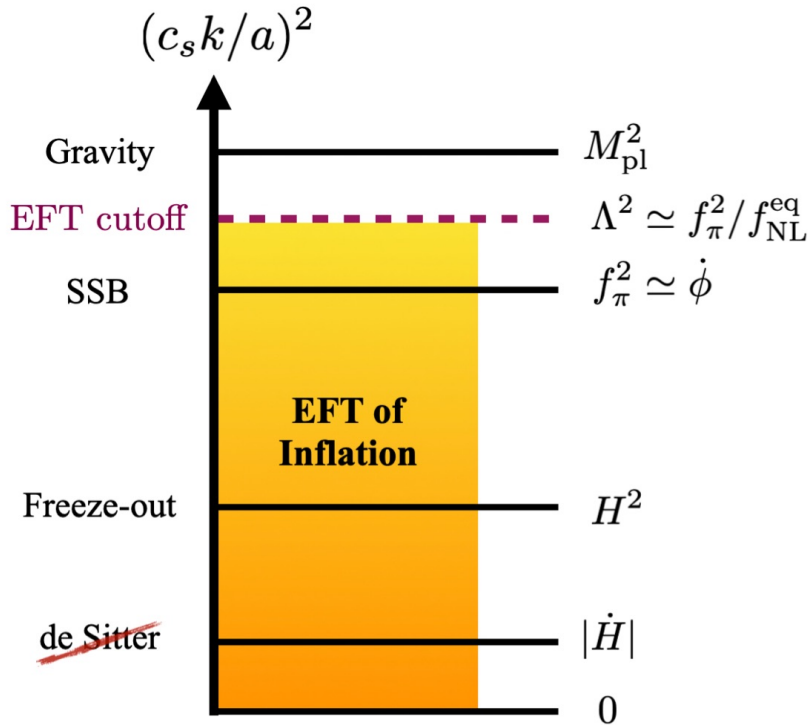
# Eternal Inflation



$$(\Delta\phi)_{\text{classical}} \sim (\Delta\phi)_{\text{noise}}$$

Some patches never reheat!

# EFT of Inflation



Gaussian

$$\Delta t \sim 1/H$$

$$(\Delta\phi)_{\text{cl}} \sim \dot{\phi}/H = f_\pi^2/H$$

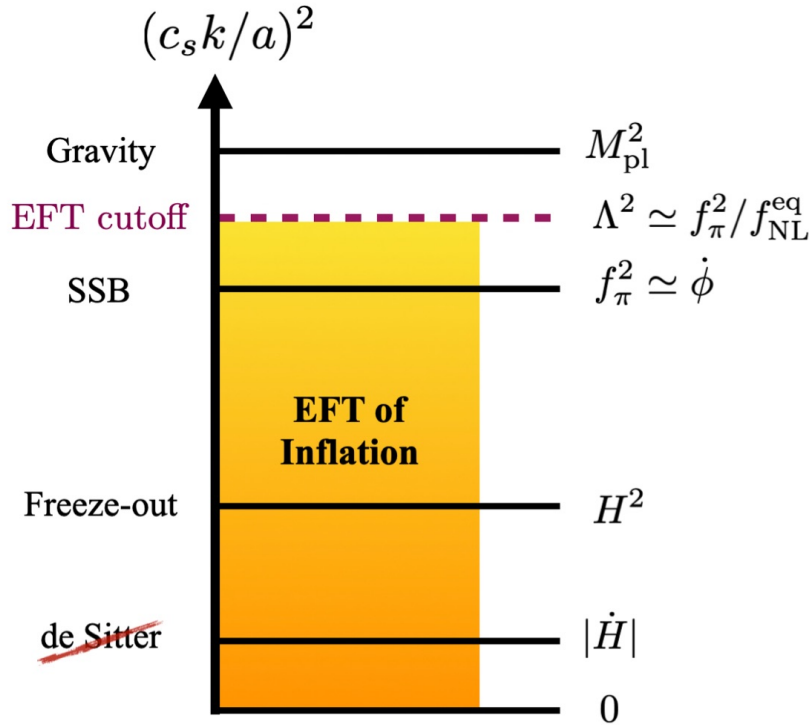
$$(\Delta\phi)_{\text{noise}} \sim H$$

Eternal Inflation

$$\Rightarrow f_\pi \sim H$$

Cheung, Creminelli, Fitzpatrick, Kaplan, Senatore  
 arXiv: 0710.0293

# EFT of Inflation



Non-Gaussian tails

$$\Delta t \sim 1/H$$

$$(\Delta\phi)_{\text{cl}} \sim \dot{\phi}/H \sim f_\pi^2/H$$

$$(\Delta\phi)_{\text{tail}} \sim f_\pi^2/H$$

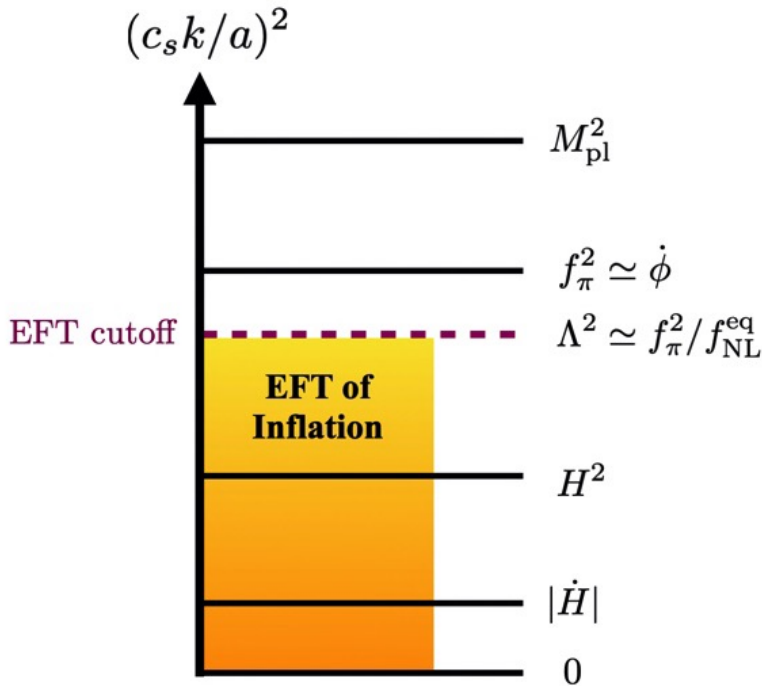
Eternal Inflation

$$\Rightarrow f_\pi \gg H$$

Energy scale associated with tail:

$$(\dot{\phi})_{\text{tail}} \sim H(\Delta\phi)_{\text{tail}} \sim f_\pi^2$$

# EFT of Inflation: $f_\pi < \Lambda$



$$f_{\text{NL}}^{\text{eq}} \sim f_\pi^2 / \Lambda^2$$

Current constraint:

$$f_{\text{NL}}^{\text{eq}} = -26 \pm 47$$

$$\Rightarrow \Lambda^2 \ll f_\pi^2 \text{ allowed}$$

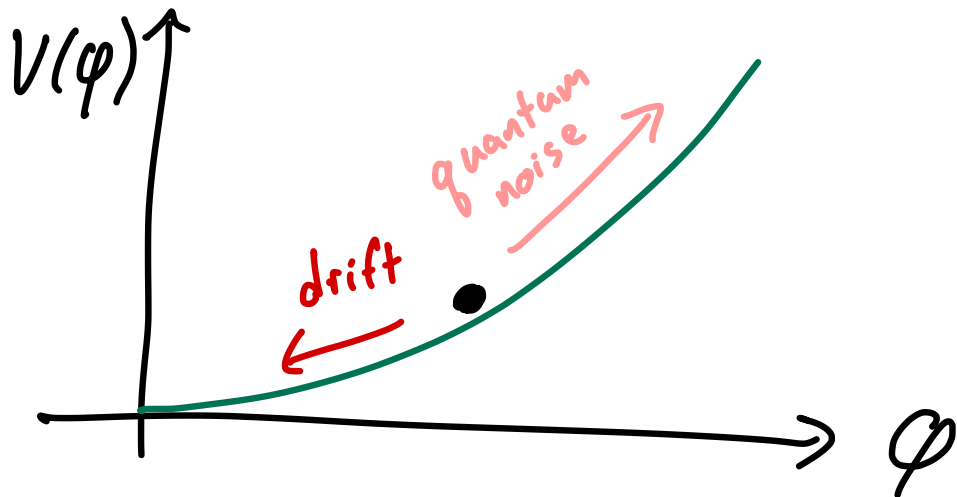
Only need  $\Lambda > H$   
for EFT consistency

Energy scale associated with tail:  
 $(\dot{\phi})_{\text{tail}} \sim H (\Delta\phi)_{\text{tail}} \sim f_\pi^2 \gg \Lambda^2$

Can we reliably  
compute tail  
in these models??

# Starobinsky's Stochastic Inflation

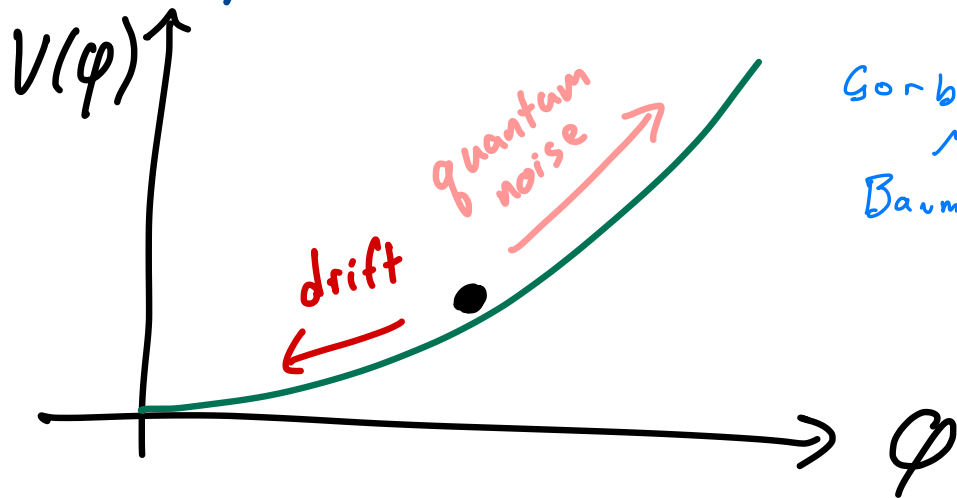
Massless scalar field in dS



⇒ Fokker - Planck equation:

$$\frac{\partial}{\partial t} P(\varphi, t) = \frac{H^3}{8\pi^2} \frac{\partial^2}{\partial \varphi^2} P(\varphi, t) + \frac{1}{3H} \frac{\partial}{\partial \varphi} [V'(\varphi) P(\varphi, t)]$$

# Starobinsky's Stochastic Inflation



see also  
Gorbenko & Senatore  
Mirbabayi  
Baumgardt & Sundrum

Gaussian noise

Tree-level potential

Systematic corrections?



# Leading Order

Probability distribution  $P(\varphi, t)$

$$\frac{\partial}{\partial t} P(\varphi, t) = \underbrace{\frac{H^3}{8\pi^2} \frac{\partial^2}{\partial \varphi^2} P(\varphi, t)}_{\text{noise}} + \underbrace{\frac{1}{3H} \frac{\partial}{\partial \varphi} [V'(\varphi) P(\varphi, t)]}_{\text{drift}}$$

$H = \text{Hubble}$  and  $V' = \frac{\partial V}{\partial \varphi}$

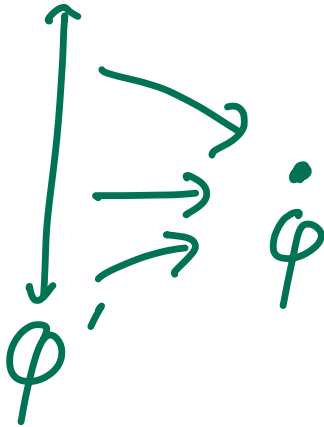
Fixed point solution ( $\partial P / \partial t = 0$ )

$$P_{\text{eq}} \sim \exp(-8\pi U / 3H^4)$$

# Beyond Leading Order

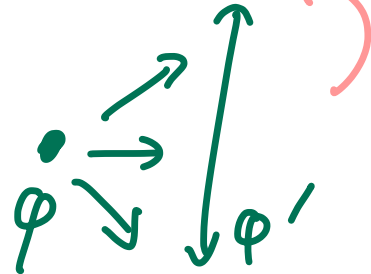
Assume "Markovian" fluctuations (no memory)

$$\frac{\partial}{\partial t} P(\varphi, t) = \int d\varphi' [P(\varphi', t) W(\varphi|\varphi')$$



$W(\varphi|\varphi')$  is transition rate  $\varphi' \rightarrow \varphi$

$$- P(\varphi, t) W(\varphi'|\varphi)]$$



# Beyond Leading Order

Perform Kramers-Moyal "local" expansion

$$\frac{\partial}{\partial t} P(\varphi, t) = \sum_{n=1}^{\infty} \frac{1}{n!} \frac{\partial^n}{\partial \varphi^n} \mathcal{L}_n(\varphi) P(\varphi, t)$$

$$\text{w/ } \mathcal{L}_n(\varphi) = \int d\Delta\varphi (-\Delta\varphi)^n W(\varphi + \Delta\varphi | \Delta\varphi)$$

# Beyond Leading Order

$$\frac{\partial}{\partial t} P(\varphi, t) = \sum_{n=1}^{\infty} \frac{1}{n!} \frac{\partial^n}{\partial \varphi^n} \mathcal{J}_n(\varphi) P(\varphi, t)$$

$\mathcal{J}_n(\varphi)$  has polynomial expansion

$$\mathcal{J}_n(\varphi) = \sum_{m=0}^{\infty} \frac{1}{m!} \mathcal{J}_n^{(m)} \varphi^m$$

LO Stochastic Inflation

$$V = \sum_{\ell} \frac{1}{\ell!} c_{\ell} \varphi^{\ell} \Rightarrow \mathcal{J}_1^{(m)} = \frac{1}{3H} c_{m+1} \quad \Bigg| \quad \mathcal{J}_2^{(0)} = \frac{H^3}{8\pi^2}$$

# Beyond Leading Order

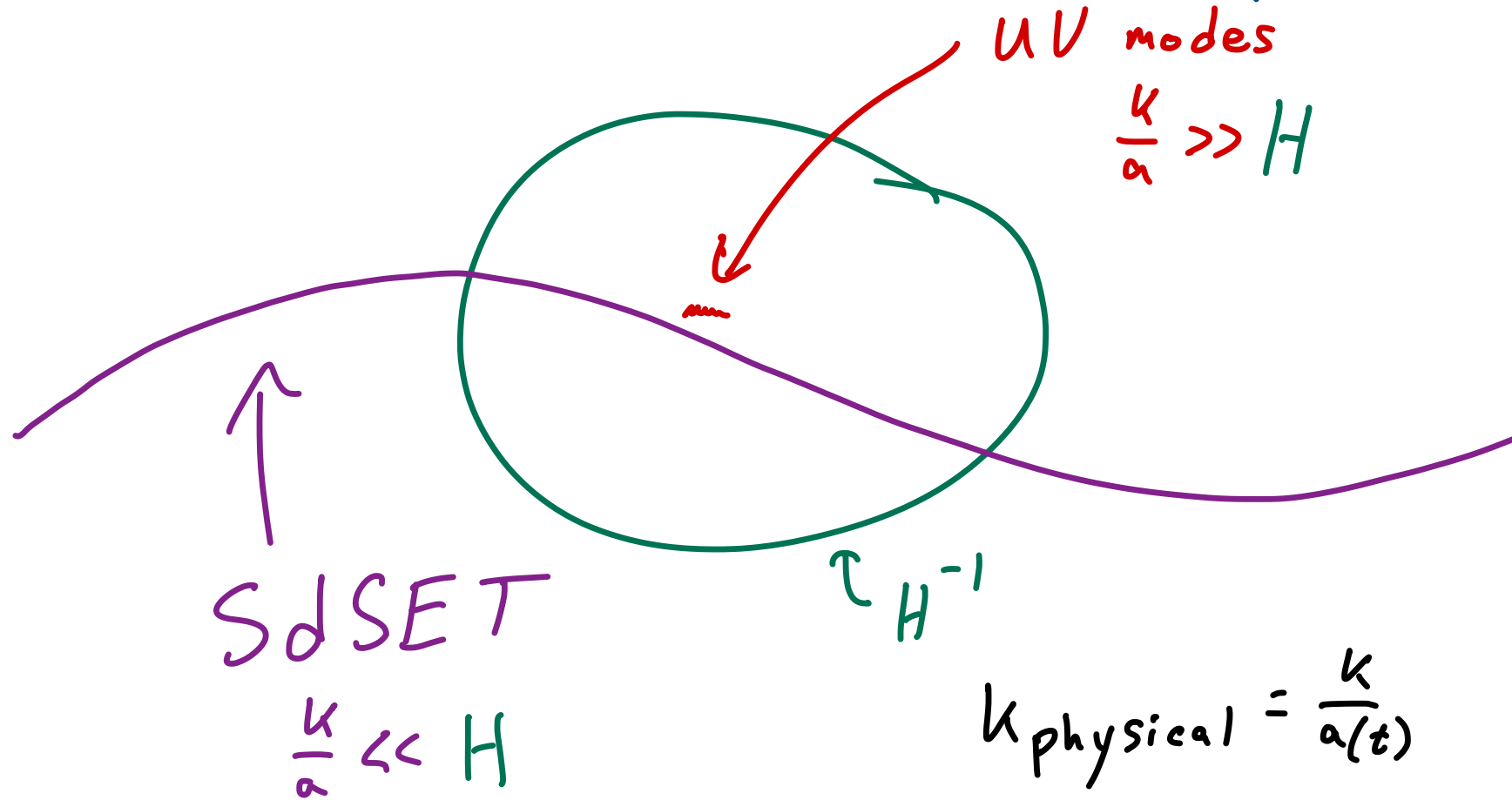
Generic structure

$$\frac{\partial}{\partial t} P(\varphi, t) = \sum_{n=2}^{\infty} \frac{1}{n!} \frac{\partial^n}{\partial \varphi^n} \left[ \sum_{m=0}^{\infty} \frac{1}{m!} \Omega_n^{(m)} \varphi^m P(\varphi, t) \right]$$

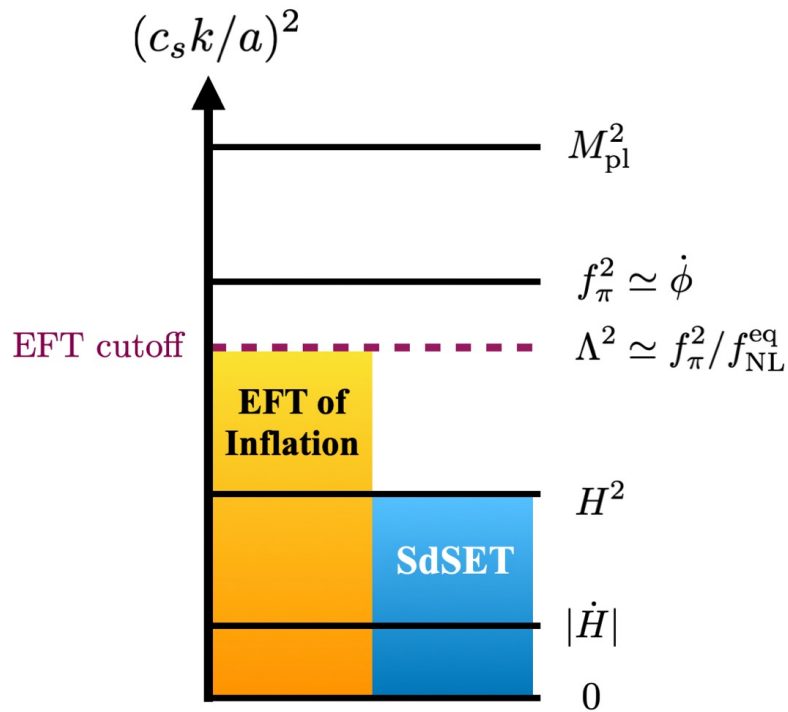
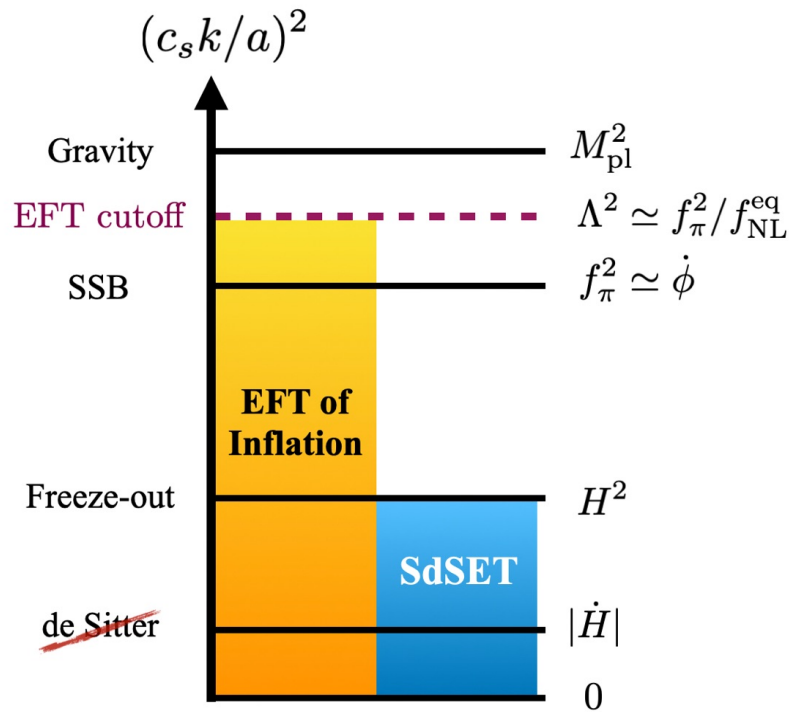
Higher order noise

$$+ \frac{1}{3H} \frac{\partial}{\partial \varphi} [V'(\varphi) P(\varphi, t)]$$

# Soft de Sitter Effective Theory



# Soft de Sitter Effective Theory



# SdSdET Fields

Two IR degrees of freedom

- "Growing" mode  $\varphi_+$  ← Correlators of interest
- "Decaying" mode  $\varphi_-$

$$w/ \phi_s = H \left( (aH)^{-\alpha} \varphi_+ + (aH)^{-\beta} \varphi_- \right)$$

Time dependence factorizes ;)



# Defining $S_{dS}ET$

- DOF  $\varphi_+$  and  $\varphi_-$
  - Power counting  $\sim \frac{k}{\Lambda_{uv}}$  w/  $\Lambda_{uv} = aH$
  - Symmetries
    - (1) "spacetime"
    - (2) "reparametrization"
  - Initial conditions
- \* Very close analogy w/ Heavy Quark EFT

# Light Scalars in dS

Composite operators

$$\mathcal{O}_n = \Phi^n \sim (k/aH)^{n\alpha} \rightarrow \mathcal{O}(1)$$

RG mixing expected

Contract any two legs

$$\langle \mathcal{O}_n \dots \rangle \supset \langle \mathcal{O}_{n-2} \dots \rangle \binom{n}{2} \frac{C_\alpha^2}{2} \int \frac{d^3 p}{(2\pi)^3} \frac{H^{2-2\alpha}}{p^{3-2\alpha}}$$

# Light Scalars in dS

$$\int \frac{d^3 p}{(2\pi)^3} \frac{H^{2-2\alpha}}{p^{3-2\alpha}} \quad \text{is scaleless and diverges as } \alpha \rightarrow 0$$

Isolate UV divergence

$$p^2 \rightarrow p^2 + \overline{k}_{\text{IR}}^2$$

$$\langle \mathcal{O}_n \dots \rangle \supset \langle \mathcal{O}_{n-2} \dots \rangle \binom{n}{2} \frac{C_\alpha^2}{4\pi^2} \left( \frac{-1}{2\alpha} - \gamma_E - \log \frac{aH}{\overline{k}_{\text{IR}}} \right)$$

# Dynamical RG $\Leftrightarrow$ Stochastic Inflation

Resum time dependent logs:

$$\frac{\partial}{\partial t} \langle \sigma_n \dots \rangle = -\frac{n}{3} \sum_{m \geq 1} \frac{c_m}{m!} \langle \sigma_{n-1} \sigma_m \dots \rangle + \frac{n(n-1)}{8\pi^2} \langle \sigma_{n-2} \dots \rangle$$

(Starobinsky; Starobinsky, Yokoyama)

Is equivalent to a Fokker-Planck eq

for  $P(\varphi, t)$  w/  $\langle \varphi^n \rangle = \int d\varphi P(\varphi, t) \varphi^n$  (Baumgart + Sundrum)

Stochastic Inflation for Inflation  
Work with scalar metric fluctuation

$$\zeta \approx H(t - \phi/f_{\pi}^2)$$

Has non-linearly realized shift symmetry

$$\Rightarrow \frac{\partial}{\partial t} P(\zeta, t) = \sum_{n \geq 2} (-1)^n \frac{\gamma_n}{n!} \frac{\partial^n}{\partial \zeta^n} P(\zeta, t)$$

$\uparrow$   
 $H=1$

Determine  $\gamma_n$  by computing operator mixing

$$\frac{\partial}{\partial t} \langle \zeta^N \rangle = \sum_n \gamma_n \binom{N}{n} \langle \zeta^{N-n} \rangle$$

# Non-Gaussian Corrections

$$\gamma_2: \langle \zeta^2 \rangle = \int \frac{d^3k}{(2\pi)^3} \underbrace{\langle \zeta(\vec{k}) \zeta(\vec{k}') \rangle}_{\frac{\Delta \zeta}{k^3} (2\pi)^3 \delta^3(\vec{k} - \vec{k}')} = 2\gamma_2 \log \frac{aH}{k} \quad \begin{matrix} \uparrow \\ \text{IR reg} \end{matrix}$$

$$\gamma_3: \langle \zeta^3 \rangle = \int \frac{d^3k_1 d^3k_2 d^3k_3}{(2\pi)^3} \underbrace{\langle \zeta(k_1) \zeta(k_2) \zeta(k_3) \rangle}_{\text{Two contributions}}$$

$$\gamma_3 = \frac{\Delta \zeta^2}{32\pi^4} \left( \left(1 - \frac{1}{c_s^2}\right) (9 + c_s^2) + \frac{c_3}{c_s^2} \right) \quad \begin{matrix} \zeta^3 & \zeta \partial_i \zeta \partial^i \zeta \end{matrix}$$

# Non-Gaussian Corrections

$$\frac{\partial}{\partial t} P(\zeta, t) = \frac{\gamma_2}{2} \frac{\partial^2}{\partial \zeta^2} P(\zeta, t) - \frac{\gamma_3}{3!} \frac{\partial^3}{\partial \zeta^3} P(\zeta, t)$$

Assuming  $P$  is nearly Gaussian:

$$\langle \zeta \zeta \rangle \sim \Delta_\zeta$$

$$\zeta \sim \Delta_\zeta^{1/2}$$

$$\partial_\zeta \sim \Delta_\zeta^{-1/2}$$

$$\Delta_\zeta \sim \frac{H^4}{f_\pi^4}$$

$\Rightarrow$

$$\gamma_2 \frac{\partial^2}{\partial \zeta^2} \sim \mathcal{O}(1)$$

$$\gamma_3 \frac{\partial^3}{\partial \zeta^3} \sim \frac{\Delta_\zeta^{1/2}}{L_s^2} \sim \frac{H^2}{\Lambda^2} \ll 1$$

$\Lambda = f_\pi L_s$

# Gaussian Distribution

Solve  $\frac{\partial}{\partial t} P_G(\xi, t) = \frac{D\xi}{4\pi^2} \frac{\partial^2}{\partial \xi^2} P_G(\xi, t)$

with boundary condition

$$P_G(\xi, \xi_i; t=0) = \delta(\xi - \xi_i) \quad \text{and} \quad P_G(\varphi_r[\xi]) = 0$$

$$\Rightarrow P_G(\varphi[\xi] < 0, \xi_i; t)$$

$$= \frac{1}{\sqrt{2\pi\sigma^2 t}} \left[ e^{-(\xi - \xi_i)^2 / (2\sigma^2 t)} - e^{-4\xi_i / 2\sigma^2} e^{-(\xi + \xi_i)^2 / (2\sigma^2 t)} \right]$$

$$\sigma^2 = 2\sigma_2 = \frac{D\xi}{2\pi}$$



# Onset of Eternal Inflation

Probability of reheating at time  $t$ :

$$P_{R,G}(t) = -\frac{d}{dt} \int_{-\infty}^0 d\phi P_G(\phi; t) \sim e^{-t/2\sigma^2}$$

Volume of reheating surface:

$$\langle V \rangle_G = L^3 \int_0^{\infty} dt e^{3t} P_{R,G}(t) \approx L^3 \int_0^{\infty} dt e^{t(3 - 1/2\sigma^2)}$$

$$\Rightarrow \langle V \rangle_G \rightarrow \infty \quad \text{when} \quad \sigma^2 = \frac{\Delta_S}{2\pi^2} > \frac{1}{6} \Rightarrow \text{Eternal inflation}$$

# Non-Gaussian Distribution

Solve  $\frac{\partial}{\partial t} P_{NG}(\xi, t) = \left( \frac{D_1}{8\pi^2} \frac{\partial^2}{\partial \xi^2} - \gamma_3 \frac{\partial^3}{\partial \xi^3} \right) P_{NG}(\xi, t)$

Boundary conditions:  $P_{NG}(\xi, \xi_i; t=0) = \delta(\xi - \xi_i)$

$$P_{NG}(\varphi_r[\xi]) = 0$$

Solution:  $P_{NG} = \exp\left(-\frac{\gamma_3 t}{3!} \frac{\partial^3}{\partial \xi^3}\right) P_G + \text{images}$

# Non-Gaussian Onset of Eternal Inflation

Probability of reheating at time  $t$ :

$$P_{R, \nu_6}(t) \sim \exp\left[-t\left(\frac{1}{2\sigma^2} - \frac{\gamma_3}{3!} \frac{1}{\sigma^6}\right)\right]$$

Volume of reheating surface:

$$\langle V \rangle_{\nu_6} = L^3 \int_0^\infty dt e^{3t} P_{R, \nu_6}(t)$$

$$\langle V \rangle_{\nu_6} \rightarrow \infty \quad \text{when} \quad \frac{1}{2\sigma^2} - \frac{\gamma_3}{3!} \frac{1}{\sigma^6} < 3$$

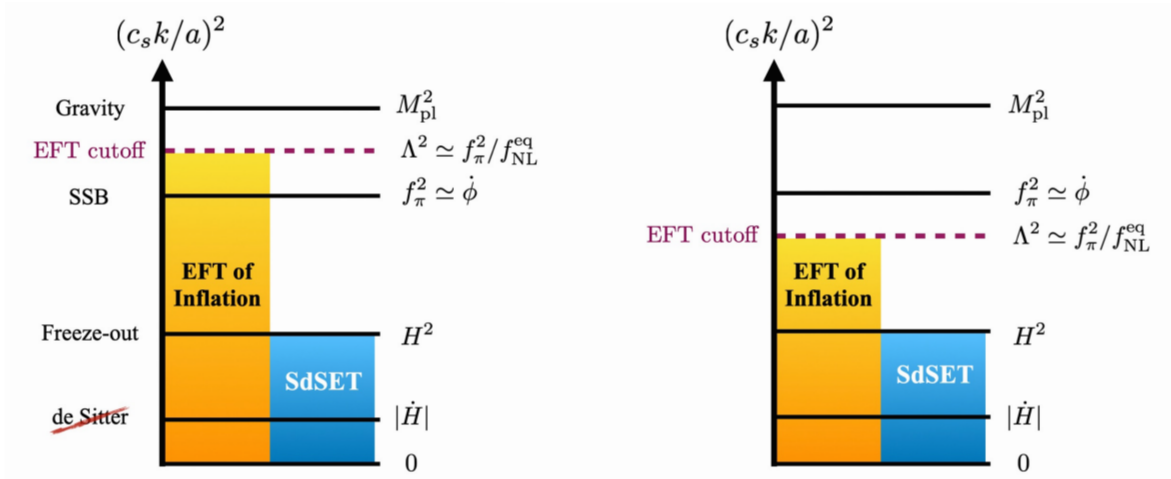
$$\Rightarrow \frac{1}{2} - \frac{1}{48} \frac{f_{\pi}^2}{\Lambda^2} \left( (c_s^2 - 1)(9 + 3c_s^2) + c_3 \right) < \frac{3\Delta\zeta}{2\pi^2}$$

# Interpretation

$$\underbrace{\frac{1}{2}}_{\text{Gaussian}} - \underbrace{\frac{1}{48} \frac{f_\pi^2}{\Lambda^2} \left( (c_s^2 - 1)(9 + 3c_s^2) + c_3 \right)}_{\text{non-Gaussian}} < \frac{3\Delta_\xi}{2\pi^2}$$

Gaussian

non-Gaussian



$\Lambda \gg f_\pi$

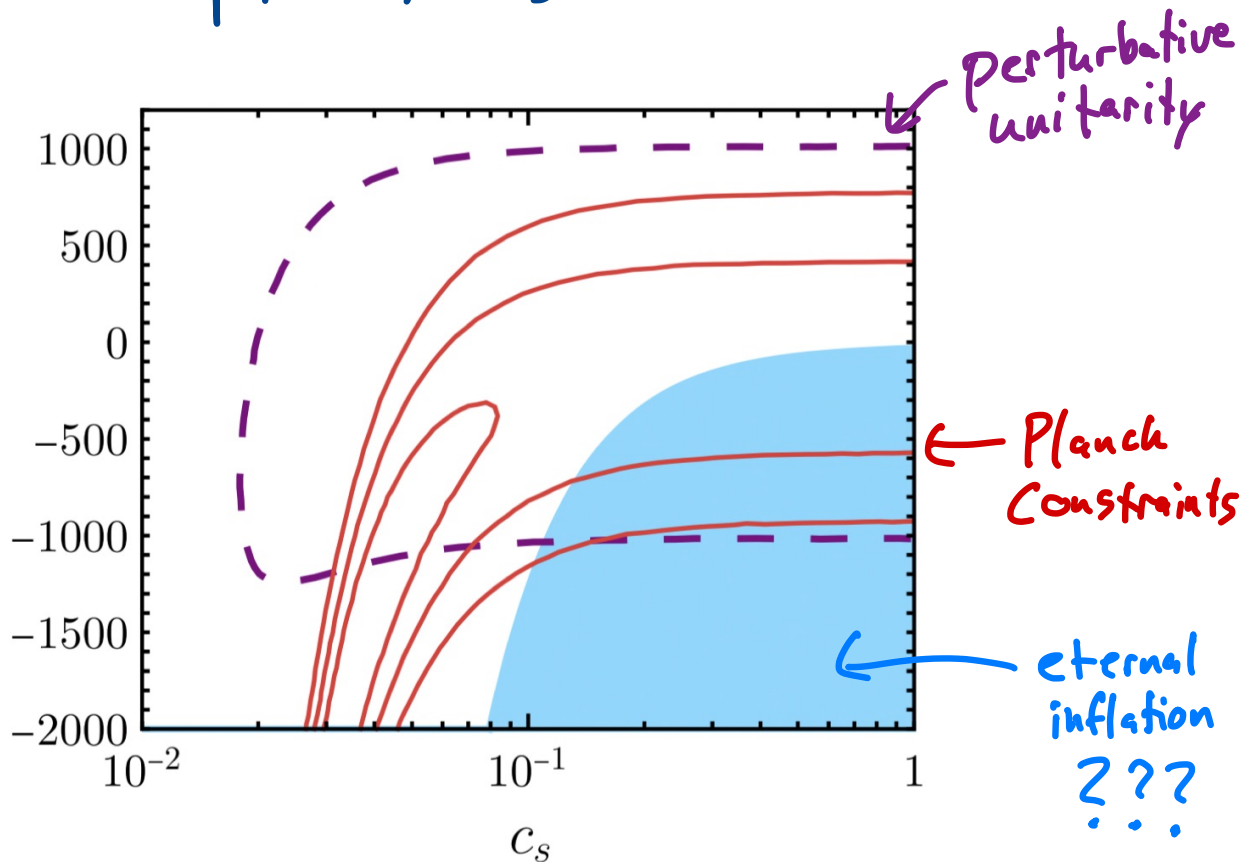
$\Lambda \ll f_\pi$

Correction is out of control

# Implications

$$\frac{1}{3} \frac{4}{C_s^2} - \frac{1}{2} \frac{(1-C_s^2)^2}{C_s^2}$$

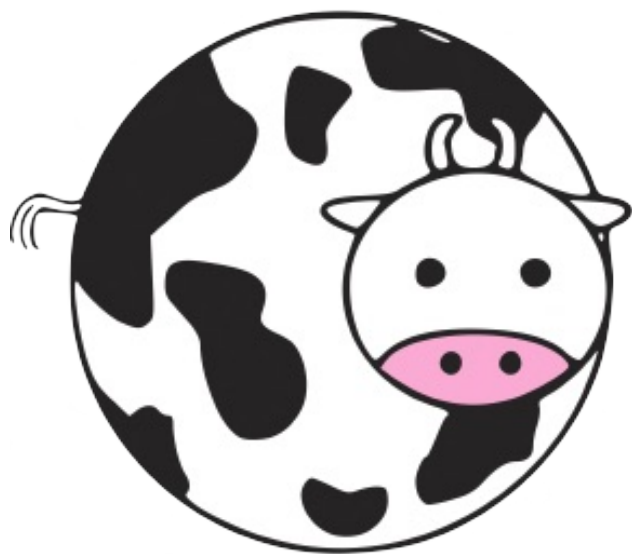
↗  $\bar{\alpha}$



Do these models  
really predict  
eternal inflation??

Or is there  
a surprising  
breakdown of EFT??





# Random Walks and RG

Toy models of fluctuating fields

Independent and identically distributed random variable  $x$ .

1) Gaussian

$$P_G(x) = \frac{1}{\sqrt{2\pi}} \exp(-x^2/2)$$

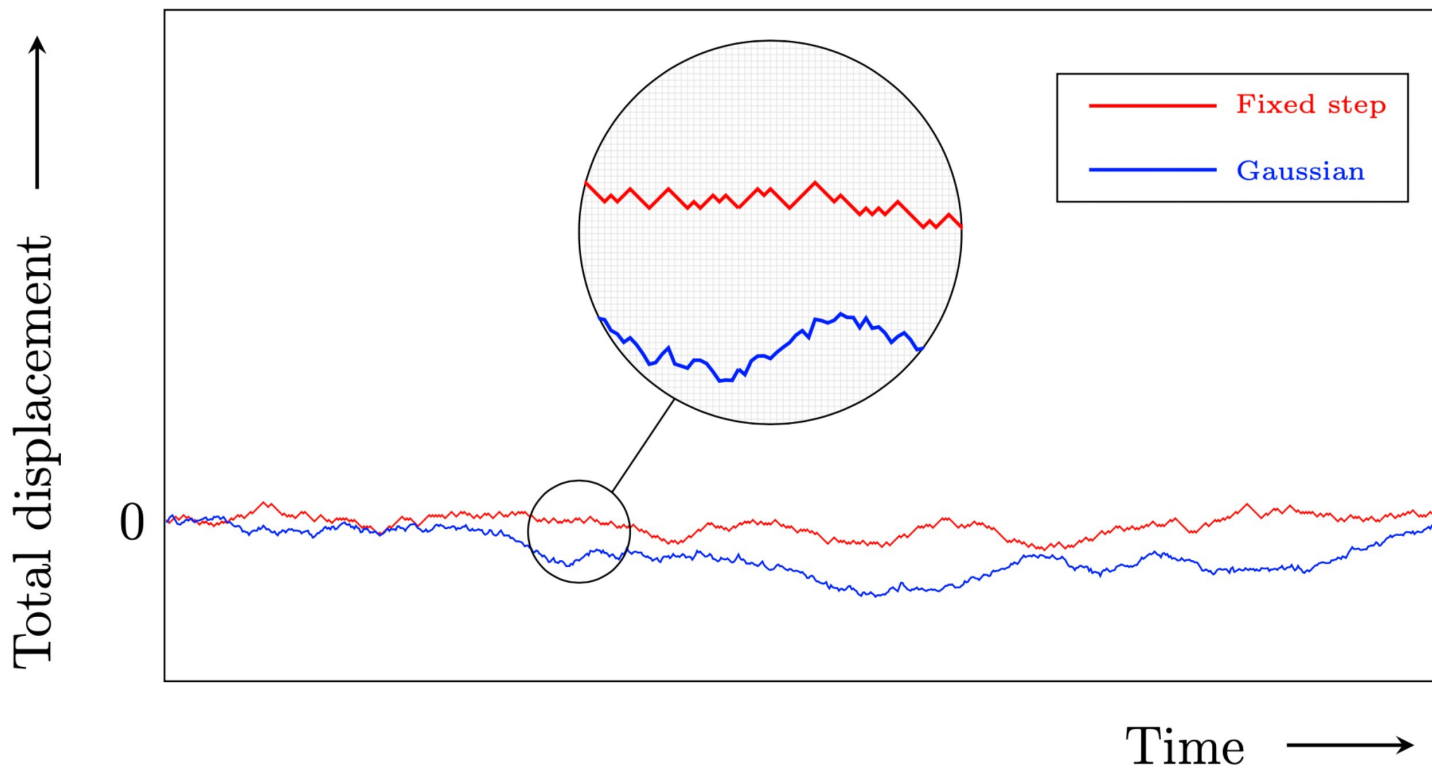
2) Fixed step

$$P_F(x) = \frac{1}{2} \delta(|x| - 1)$$

$$\langle x \rangle = 0 \quad \text{and} \quad \langle x^2 \rangle - \langle x \rangle^2 = 1$$



# Same Coarse Grained Predictions



# Compute Displacement

How far does walker move in  $N$  steps?

$$\mathbb{X} = \sum_{i=1}^N x_i \Rightarrow P(\mathbb{X}) = \int \prod_{i=1}^N dx_i p(x_i) \delta\left(\mathbb{X} - \sum_{i=1}^N x_i\right)$$

$$\int \frac{dk}{2\pi} e^{-ik(\mathbb{X} - \sum_{i=1}^N x_i)}$$

$$\Rightarrow P(\mathbb{X}) = \int \frac{dk}{2\pi} e^{-ik\mathbb{X}} \underbrace{\int \prod_{i=1}^N dx_i p(x_i) e^{ikx_i}}_{\left\langle e^{ikx} \right\rangle^N}$$

# Large Step Limit

1) Gaussian:  $\langle e^{ikx} \rangle_g = e^{-k^2/2}$

$$\Rightarrow P_g(X) = (2\pi N)^{-1/2} \exp(-X^2/2N)$$

2) Fixed step:  $P_f(X) = \frac{N!}{\left(\frac{N-X}{2}\right)! \left(\frac{N+X}{2}\right)!} 2^{-N}$

↑  
Combinatorics

Stirling's approx  $\Rightarrow P_f(X) \approx \exp\left(-X^2/2N - X^4/12N^3 + \dots\right)$

Gaussians!

# Central Limit Theorem

Assume expansion  $\log \langle e^{ikx} \rangle = \sum_{n=1}^{\infty} \frac{(ik)^n}{n!} \langle x^n \rangle_G$

w/  $\langle x \rangle_G = \langle x \rangle$ ,  $\langle x^2 \rangle_G = \langle x^2 \rangle - \langle x \rangle^2 = \sigma_0^2$ , ... ↑  
connected  
correlators

$$P(\Sigma) = \int \frac{dk}{2\pi} e^{-ik\Sigma} \exp\left(ikN - \frac{1}{2}Nk^2\sigma_0^2 + \frac{i^3}{3!}Nk^3\langle x^3 \rangle_G + \dots\right)$$

If integral support dominated by Gaussian:

$$k \lesssim \frac{1}{\sqrt{N}} \sigma_0$$

# Central Limit Theorem

Gaussian support:  $k \lesssim 1/\sqrt{N} \sigma_0$

$$P(\underline{X}) = \int \frac{dk}{2\pi} e^{-ik\underline{X}} \exp\left(\cancel{i k N} - \frac{1}{2} \cancel{N k^2 \sigma_0^2} + \frac{i^3}{3!} \cancel{N k^3} \langle x^3 \rangle_0 + \dots\right)$$

Rescale (coarse grain):  $k \rightarrow k/\sqrt{N}$ ,  $\underline{X} \rightarrow \sqrt{N} \underline{X}$

$$\begin{aligned} \Rightarrow P(\underline{X}) &\rightarrow \frac{1}{\sqrt{N}} \int \frac{dk}{2\pi} \exp\left(ik(\sqrt{N}\langle x \rangle - \underline{X}) - \frac{1}{2} k^2 \sigma_0^2 + O\left(\frac{1}{\sqrt{N}}\right)\right) \\ &\simeq \exp\left(-\underline{X} - \sqrt{N}\langle x \rangle\right)^2 / 2\sigma_0^2 \end{aligned}$$

Central Limit Theorem is RG

"UV insensitive"

In  $N \rightarrow \infty$  limit:

$\langle x \rangle$ : relevant

$\sigma_0$ : marginal

$\langle x^n \rangle_G$  w/  $n > 2$ : irrelevant

# Large Deviation Principle

Consider probability of finding random walker distance beyond  $N$  after  $N$  steps:

$$P(X > N) = ?$$

Expect UV dependence:

Fixed step walker:  $P_f(X > N) = 0$

Gaussian walker:  $P_g(X > N) \neq 0$

# Large Deviation Principle

Compute  $\langle e^{\theta X} \rangle$  w/  $\theta > 0$

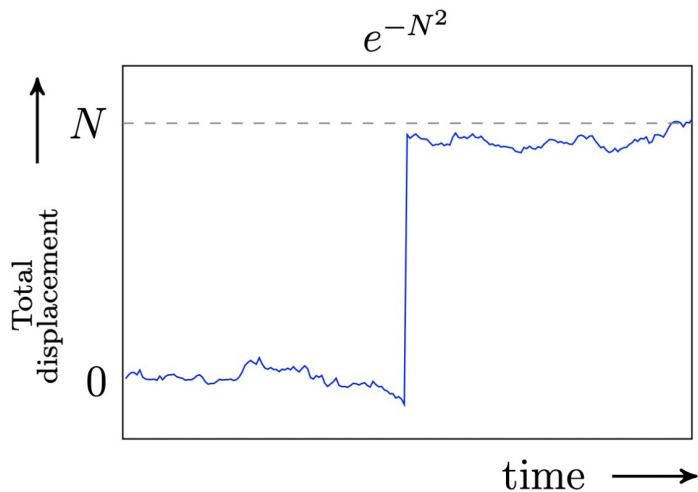
Naively expect  $\langle e^{\theta X} \rangle \sim e^{\theta \theta (\sqrt{N})}$

But  $\langle e^{\theta X} \rangle = \langle e^{\theta x} \rangle^N = e^{N\theta^2/2}$

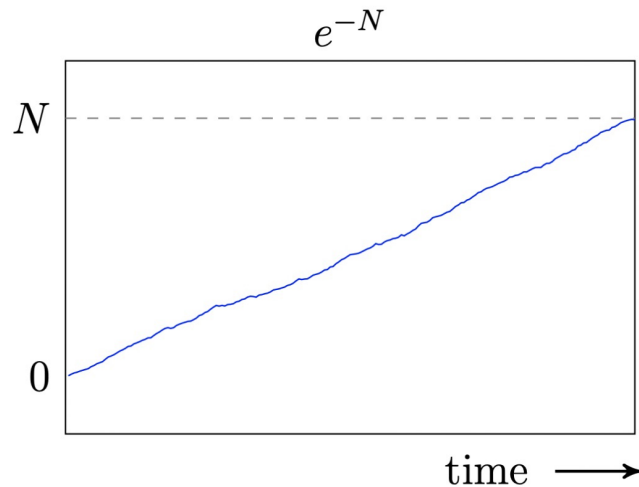
Central limit theorem fails!



# Large Deviation Principle



↑  
CLT



↑  
LDP

# Large Deviation Principle

Define "sample mean"  $\tilde{\bar{X}} = \bar{X}/N$

A distribution satisfies the LDP if

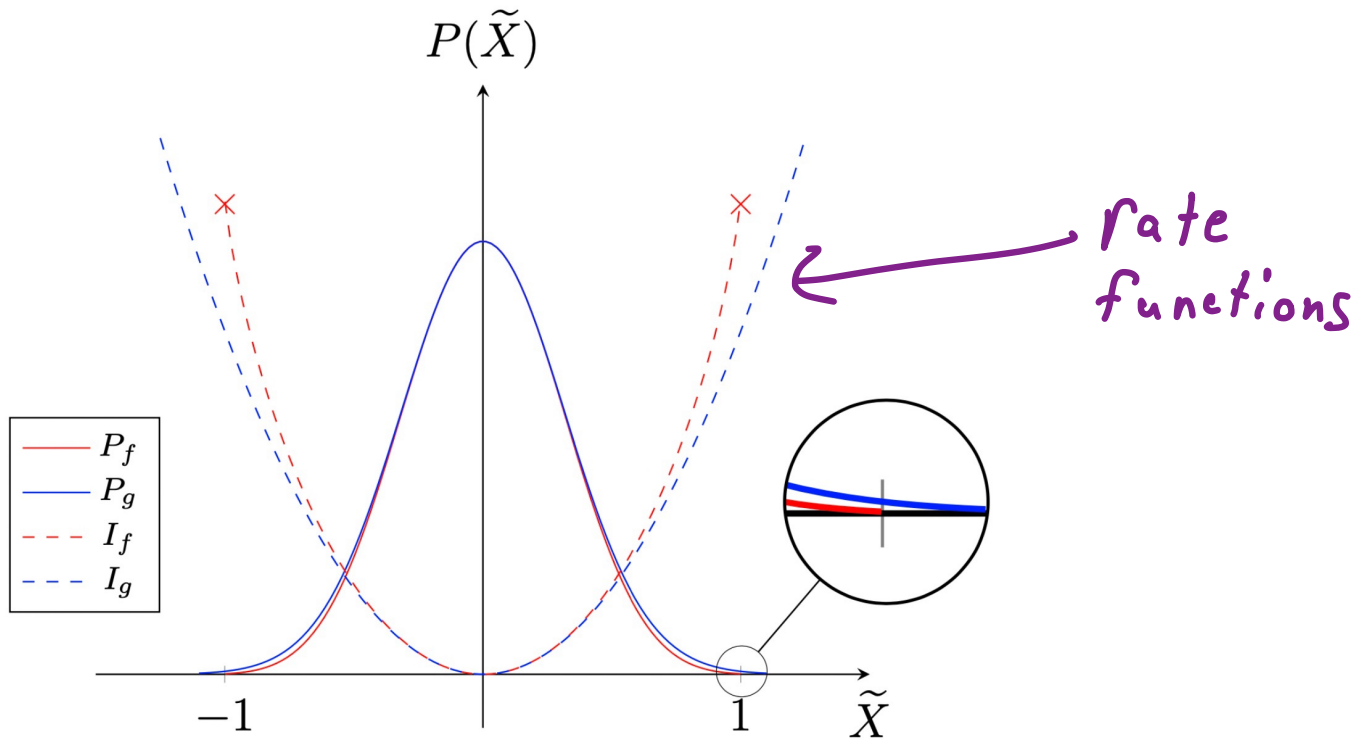
$$P(\bar{X}) \simeq \exp(-N I(\tilde{\bar{X}}))$$

where  $I(\tilde{\bar{X}})$  is the "rate function"

$$I_g(\tilde{\bar{X}}) = \tilde{\bar{X}}^2/2$$

$$I_f(\tilde{\bar{X}}) = \frac{1}{2} \left[ (1-\tilde{\bar{X}}) \ln(1-\tilde{\bar{X}}) + (1+\tilde{\bar{X}}) \ln(1+\tilde{\bar{X}}) \right]$$

# Comparing Tails



# Cramér's Theorem

Distribution of  $\tilde{X}$  satisfies LDP w/

$$I(\tilde{X}) = \sup_{\theta} [\theta \tilde{X} - \lambda(\theta)] \quad \text{w/} \quad \lambda(\theta) = \ln \langle e^{\theta x} \rangle$$

Proof: Assume LDP holds  $P(\tilde{X}) \simeq e^{-N I(\tilde{X})}$

Then  $\langle e^{\theta \tilde{X}} \rangle = \langle e^{N \theta \tilde{X}} \rangle \simeq \int d\tilde{X} e^{N(\theta \tilde{X} - I(\tilde{X}))}$

Saddle point  $\simeq e^{N \sup_{\tilde{X}} [\theta \tilde{X} - I(\tilde{X})]}$

# Cramér's Theorem

So we have  $\langle e^{\theta X} \rangle \simeq e^{N \sup_{\tilde{X}} [\theta \tilde{X} - I(\tilde{X})]}$

Also  $\langle e^{\theta X} \rangle = \langle e^{\theta x} \rangle^N = e^{N \lambda(\theta)}$

$$\Rightarrow \lambda(\theta) = \sup_{\tilde{X}} [\theta \tilde{X} - I(\tilde{X})]$$

Legendre transform:  $I(\tilde{X}) = \sup_{\theta} [\theta \tilde{X} - \lambda(\theta)]$

LDP  $\Rightarrow$  New saddle!

From LDP  $\rightarrow$  CLT

If  $I(\tilde{X})$  is convex and has  
single global minimum  $\tilde{X}_0$

$$\Rightarrow P(\tilde{X}) \approx \exp\left(-\frac{1}{2} N I''(\tilde{X}_0) (\tilde{X} - \tilde{X}_0)^2\right)$$

Good approximation for small deviations

$\Rightarrow$  Central Limit Theorem

# Eternal Inflation and the LPD

Fokker-Planck for Gaussian theory

$$\Rightarrow P_\xi \sim \exp(-\xi^2/2\sigma^2 t)$$

$$\Rightarrow \text{Typical fluctuations } \xi \sim \sqrt{t}$$

Eternal inflation dominated by  $\xi \sim t$

# Eternal Inflation and the LPD

Eternal inflation dominated by  $\xi \sim t$

General solution to F-P eq:

$$P = \exp\left(\dots \frac{\partial^n}{\partial \xi^n}\right) P_S$$

Write  $P = \int \frac{dk}{2\pi} e^{-ik\xi} p(k)$

w/  $p(k) = \left( \exp\left(-k^2 \frac{\sigma^2}{2} t + \sum_{n \geq 2} (ik)^n \frac{\gamma_n}{n!} t\right) \right)$

$$\equiv \langle \exp(ik\xi) \rangle$$



# Eternal Inflation and the LPD

When  $\xi = \alpha t$  for some constant  $\alpha$

as  $t \rightarrow \infty$  steepest descents  $\Rightarrow$

$$P \simeq \exp(-t I(\alpha))$$

$$w/ I(\alpha) = (-i \alpha k_*(\alpha) - k_*^2(\alpha) \frac{\sigma^2}{2}$$

$$+ \sum_{n \geq 2} (i k_*(\alpha))^n \frac{\gamma_n}{n!})$$

$$\text{and } (i \sum_{n \geq 1} (i k_*(\alpha))^n \frac{\gamma_{n+1}}{n!}) - k_* \sigma^2 = i \alpha$$

Cramér's  
Thm!

Eternal Inflation is UV Sensitive

Phase transition to eternal inflation  
probes the tail of the distribution

Sensitive to new saddle of the  
path integral

Breakdown of EFT of Inflation

$$\propto f_\pi^2 > \Lambda^2$$

# Outlook

Fluctuations of fields in  $dS$  governed  
by RG in  $SdSET$

Typical fluctuations governed by  
coarse grained RG  $\Rightarrow$  CLT

Rare fluctuations governed by LDP  
 $\Rightarrow$  UV sensitive