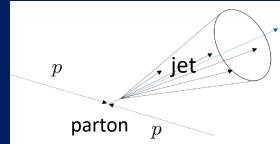


# Jets and Lund plane studies at LHCb

Christine A. Aidala
University of Michigan
On behalf of the LHCb Collaboration



1st Lund Jet Plane Institute July 3, 2023

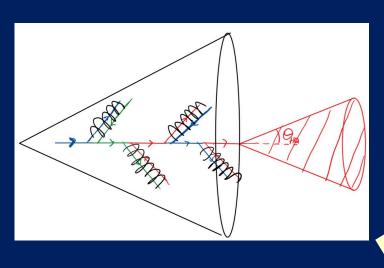




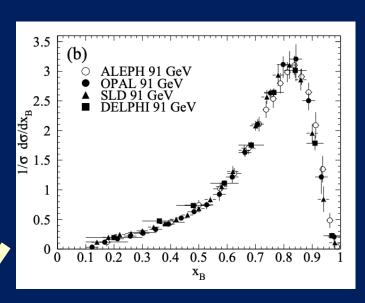


# Heavy quark showering and fragmentation

1. The Dead Cone Effect



2. The Leading Particle Effect



**Lund Jet Plane** 





Dead cone effect

#### Bremsstrahlung off moving charges

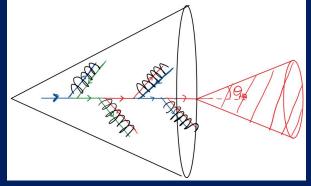
• The relativistic and massless splitting probability in pQCD is given by

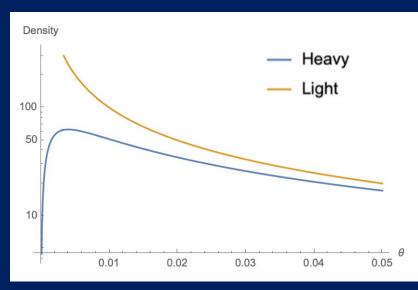
$$dP_{i \to ig} = rac{lpha_s C_i}{\pi} rac{d heta^2}{ heta^2} rac{dz}{z}$$
  $z: ext{Energy Fraction} \ heta: ext{Splitting angle} \ C_i: ext{Color factor}$ 

• For heavy quarks (HQs), a characteristic angle appears in the equation

$$dP_{i\to ig} = \frac{\alpha_s C_i}{\pi} \frac{\theta^2 d\theta^2}{(\theta^2 + \theta_{HQ}^2)^2} \frac{dz}{z}$$

$$\theta_{\rm HQ} = \frac{m_{\rm HQ}}{E}$$





Dokshitzer, Y.L., Khoze, V.A. and Troyan, S.I., 1991. Journal of Physics G: Nuclear and Particle Physics, 17(10), p.1602.



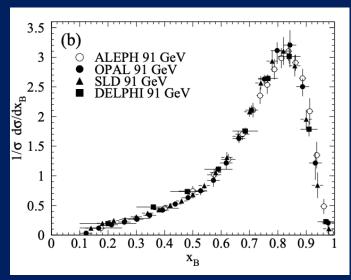


## Heavy quark fragmentation

#### Heavy quarks maintain most of their energy

A STATE OF THE STA

- Light partons lose most of their energy in hard collinear radiation
- The dead cone effect in heavy quarks prevents collinear radiation → very few hard and collinear bremsstrahlung emissions
- Thus, the heavy quark maintains most of its energy



Energy fraction of the jet carried by the b-hadron

(ALEPH), Phys. Lett. B357, 699 (1995) (ALEPH), Phys. Lett. B512, 30 (2001) (DELPHI), Eur. Phys. J. C71, 1557 (2011) (OPAL) Eur. Phys. J. C29, 463 (2003) (SLD), Phys. Rev. D65

(Particle Data Group), Prog. Theor. Exp. Phys. 2022, 083C01 (2022)





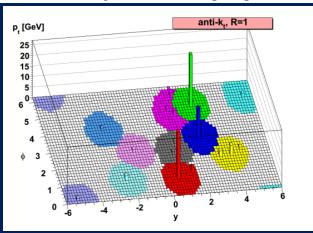
## Jet clustering algorithms

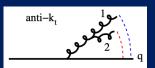
Cacciari, Matteo, Gavin P. Salam, and Gregory Soyez. JHEP 2008.04 (2008): 063.

F. A. Dreyer, G. P. Salam, and G. Soyez, The Lund jet plane, J. High Energy Phys. 12 (2018) 064

#### Anti- $k_T$

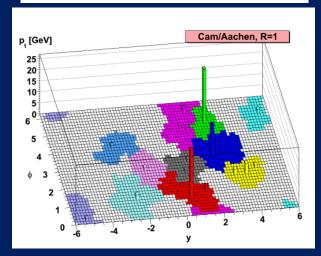
- Infrared and Collinear safe
- Conical jets
- Standard jet clustering algorithm

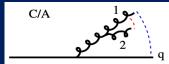




#### Cambridge/Aachen

- Respects angular ordering
- Reconstructs splitting history
- Not infrared safe









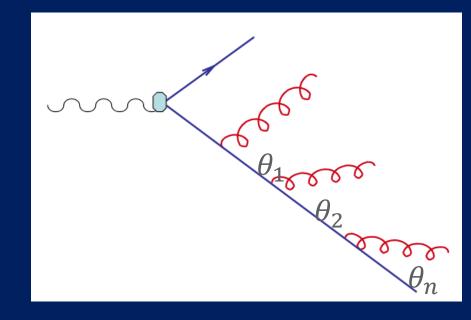
## Angular ordering

## Accessing the splitting history

 Gluon radiation is ordered from larger to smaller angles throughout the showering

$$|\theta_1 > \theta_2 > \ldots > \theta_n|$$

• The C/A algorithm clusters jets based on smallest angles first = respects angular ordering



C/A gives us access to the splitting history of the jet

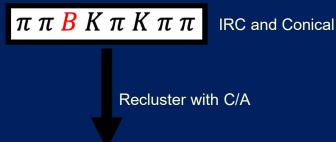
Image: Mangano-Lect3

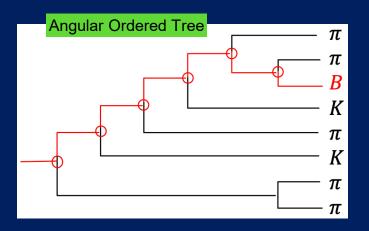


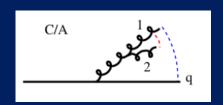
## Iterative declustering

Cunqueiro, Leticia, and Mateusz Płoskoń. PRD 99.7 (2019): 074027

Anti- $k_T$  Jet







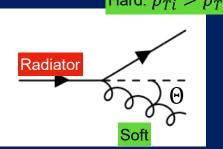
Recluster = combine most collinear particles according to C/A

- 1. Using the FastJet algorithm, cluster jets with the anti- $k_T$  algorithm ("AK5" for R = 0.5) [*EPJC* 72:1 (2012)]
- 2. Recluster jets passing the selection criteria using C/A
- 3. Following the hardest/heavy-flavor branch, at each splitting point record the variables of interest:  $k_T$ , z,  $\Delta R$ ,  $\theta$ ,  $E_{rad}$

## Splitting variables

Hard:  $p_{Ti}>p_{Tj}$ 

We adopt the following definitions for the Lund jet plane variables:



- $\theta_{ij}$ : the angle between the soft daughter and radiator
- $E_{rad}$ : the energy of the radiator

• 
$$\Delta R = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$
 - angular distance

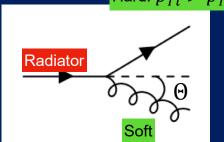
•  $k_T = p_T^{soft} \sin(\Delta R)$  - relative transverse momentum

• 
$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$
 - transverse momentum fraction



## Splitting variables

Hard:  $p_{Ti} > p_{Tj}$ 



#### Focusing on these variables:

- $\theta_{ij}$ : the angle between the soft daughter and radiator
- $E_{rad}$ : the energy of the radiator

Obtain "dead cone plane" in  $E_{rad}$  and  $\theta$ 

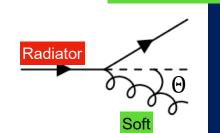
$$\rho(E_{rad}, \theta) = \frac{1}{N_{emissions}} \frac{d^2n}{dE_{rad} d\ln(1/\theta)}$$

$$\theta_{HQ} = \frac{m_{HQ}}{E}$$



## Splitting variables

Hard:  $p_{Ti} > p_{Tj}$ 



#### Focusing instead on these variables:

• 
$$\Delta R = \sqrt{(\eta_i - \eta_j)^2 + (\phi_i - \phi_j)^2}$$
 - angular distance

• 
$$k_T = p_T^{soft} \sin(\Delta R)$$
 - relative transverse momentum

• 
$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$
 - transverse momentum fraction

#### Obtain "standard" versions of Lund jet plane

$$\rho(\Delta R, k_T) = \frac{1}{N_{emissions}} \frac{d^2n}{d\ln(R/\Delta R)d\ln(k_T)} \qquad \rho(\Delta R, \mathbf{z}) = \frac{1}{N_{emissions}} \frac{d^2n}{d\ln(R/\Delta R)d\ln(1/\mathbf{z})}$$

$$\rho(\Delta R, \mathbf{z}) = \frac{1}{N_{emissions}} \frac{d^2n}{d\ln(R/\Delta R)d\ln(1/\mathbf{z})}$$



## Prospects for the LJP at LHCb



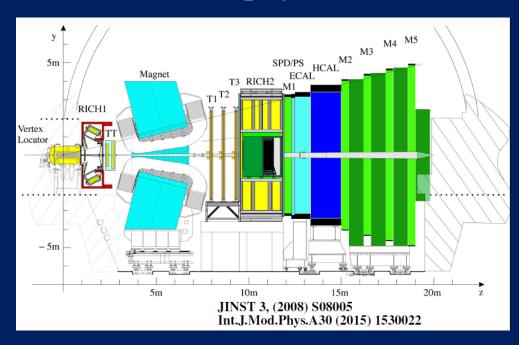
# LHCb: Opportunities for measuring hadron distributions in jets

LHCb is the experiment devoted to flavor physics at the LHC.

Detector design:

• Forward geometry to optimize acceptance for  $b\bar{b}$  pairs:  $2 < \eta < 5$ 

- Tracking: Momentum resolution <1% for p < 200 GeV/c
- Particle ID: Excellent capabilities to select exclusive decays





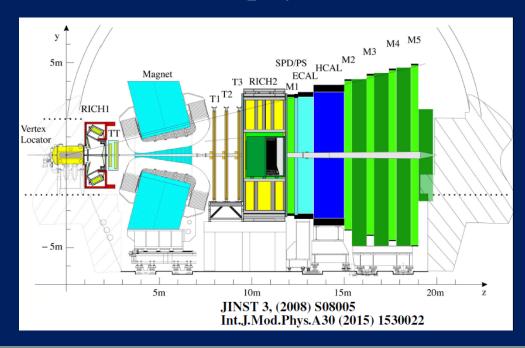
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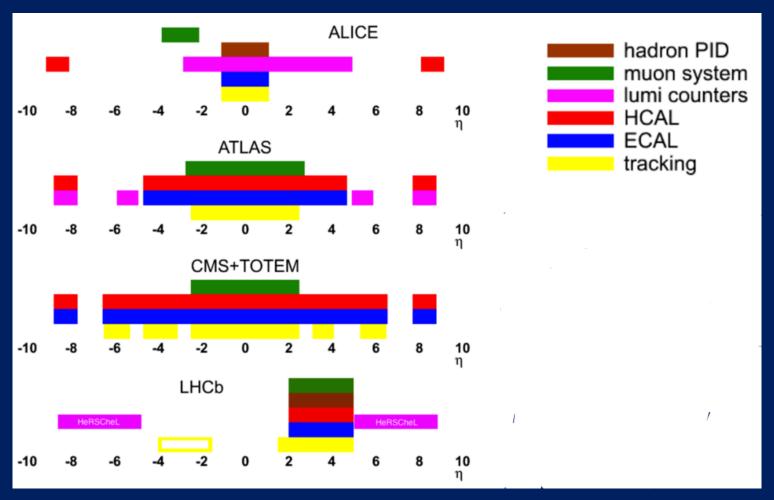
- Tracking: Momentum resolution <1% for p < 200 GeV/c
- Particle ID: Excellent capabilities to select exclusive decays .



- Full jet reconstruction with tracking, ECAL, HCAL
- Heavy flavor tagging of jets
- Charged hadron PID from  $2 \le p \le 100 \text{ GeV}$ 
  - Can study identified particle distributions within jets
- Muon detection



#### Pseudorapidity coverage comparison

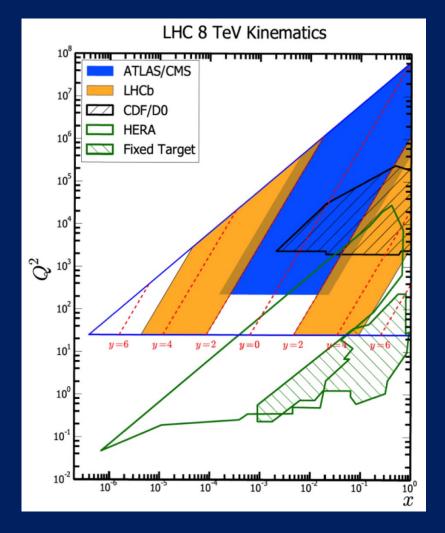






## x-Q² coverage affects parton mix

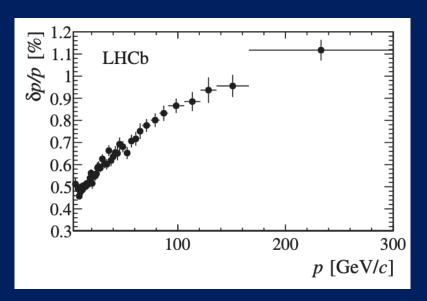
- LHCb also has unique x-Q<sup>2</sup> coverage
  - Enhanced lightquark jet fraction inforward region



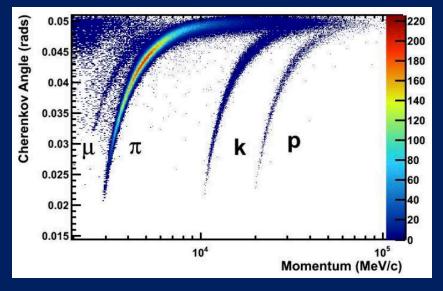


### Tracking and PID

#### Excellent momentum resolution and hadron PID



Resolution <1% up to 200 GeV Int. J. Mod. Phys. A 30, 1530022 (2015)



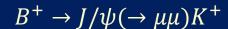
Capability of selecting exclusive decays

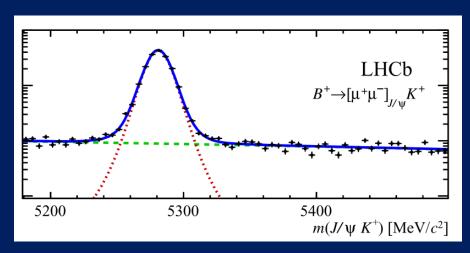
EPJC 73.5 (2013): 1-17



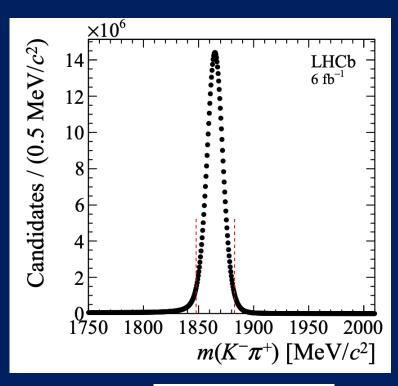
# Excellent reconstruction of exclusive decays

$$D^0 \rightarrow K^-\pi^+$$





PRD 95, 052005 (2017)



Phys. Rev. D 104 (2021) 072010



#### Lund plane at LHCb

#### We plan on

- measuring the LJP for *light*, *charm*, and *beauty* jets,
- measuring the LJP for *track* jets as well as *track* + *neutral* jets,
- and measuring the *dead-cone* effect from the various LJP parametrizations.



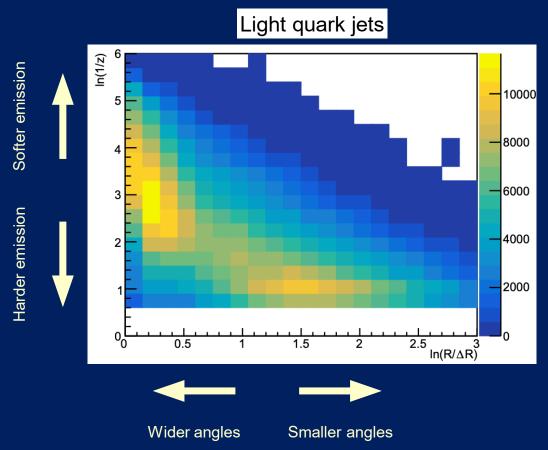
#### Jet samples

Z-tagged jets, jets around  $D^0$ , jets around  $B^{\pm}$ 

- Run 2 pp collisions at  $\sqrt{s} = 13$  TeV data, 2016-2018.
- For light partons (u/d/s/g), jets recoiling off a Z-boson are used to obtain a quark-enriched jet sample.  $pp \to Z(\to \mu\mu) + q(g)$
- For charm-initiated jets, we reconstruct  $D^0 \to K^-\pi^+$  candidates and find jets that contain the  $D^0/\overline{D}^0$  within the jet radius.
- For beauty-initiated jets, we reconstruct  $B^+ \to J/\psi (\to \mu\mu) K^+$  candidates and find jets that contain the  $B^\pm$  within the jet radius.



#### Pythia8 simulations





$$\sqrt{s} = 13 \text{ TeV}$$
 
$$2.5 < \eta_j < 4$$
 
$$p_{T,jet} > 20 \text{ GeV}$$

$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$



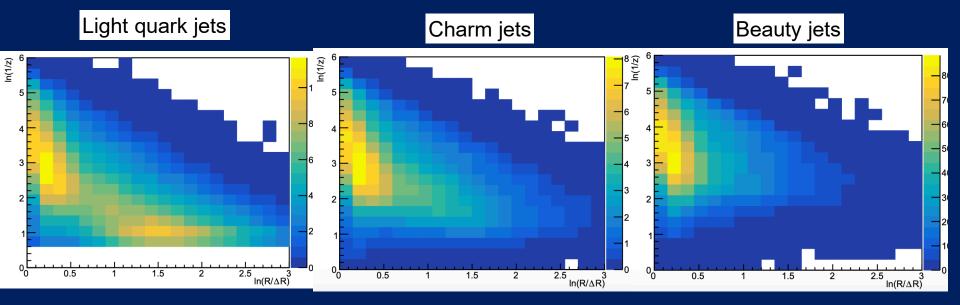
#### Pythia8 simulations

pp collisions

$$\sqrt{s} = 13 \text{ TeV}$$
  
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$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$

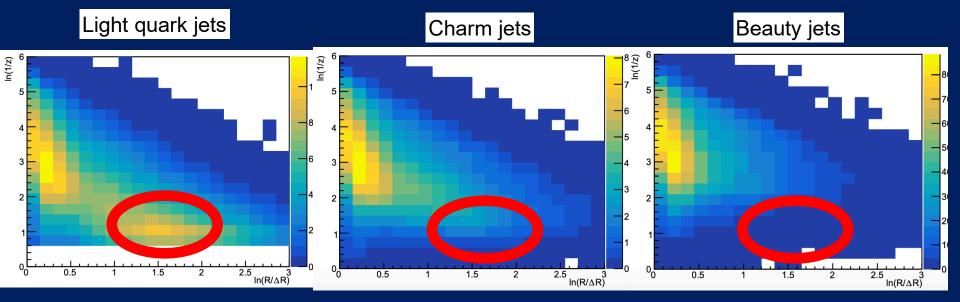




#### Pythia8 simulations

pp collisions  $\sqrt{s} = 13 \text{ TeV}$   $2.5 < \eta_j < 4$   $p_{T,jet} > 20 \text{ GeV}$ 

$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$



Suppression of hard collinear radiation = Heavy quarks maintain most of their energy

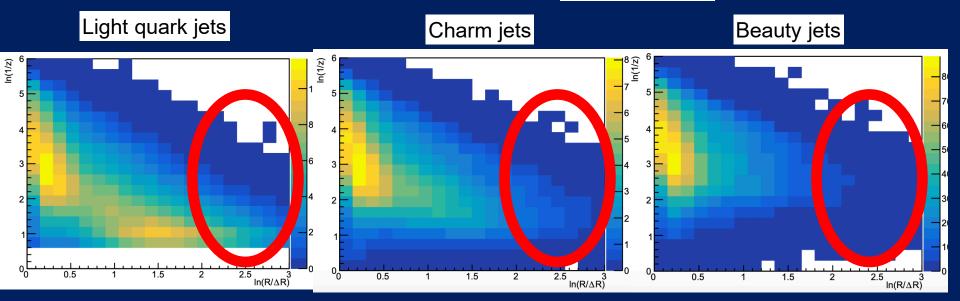


#### Pythia8 simulations

pp collisions

$$\begin{array}{l} \sqrt{s} = 13 \ \mathrm{TeV} \\ 2.5 < \eta_j < 4 \\ p_{T,jet} > 20 \ \mathrm{GeV} \end{array}$$

$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$



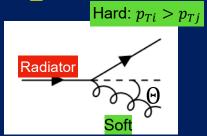
Suppressed collinear radiation = dead cone effect



#### "Dead cone plane" at forward rapidities

Pythia8 simulations

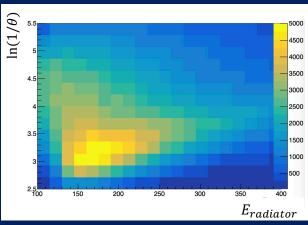
pp collisions  $\sqrt{s} = 13 \text{ TeV}$   $2.5 < \eta_j < 4$   $p_{T,jet} > 20 \text{ GeV}$ 

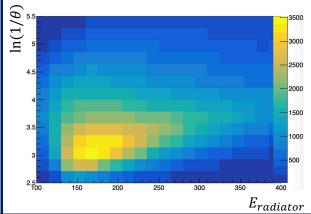


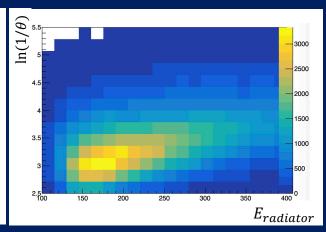
Light quark jets

Charm jets

Beauty jets



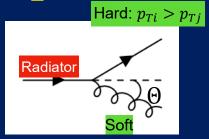




#### "Dead cone plane" at forward rapidities

Pythia8 simulations - ratios

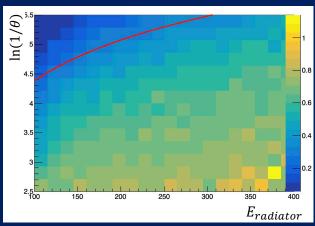
pp collisions  $\sqrt{s} = 13 \text{ TeV}$   $2.5 < \eta_j < 4$   $p_{T,jet} > 20 \text{ GeV}$ 

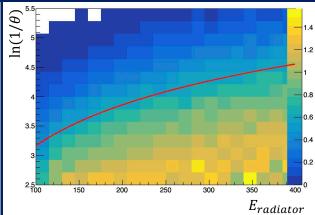


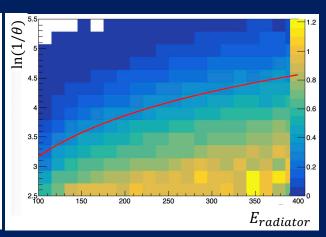
Charm/Light

Beauty/Charm

Beauty/Light







Red line: Dead cone angle as a function of  $E_{radiator}$ 

$$heta_{
m HQ} = rac{m_{
m HQ}}{E}$$

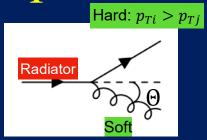




#### "Dead cone plane" at forward rapidities

Pythia8 simulations - ratios

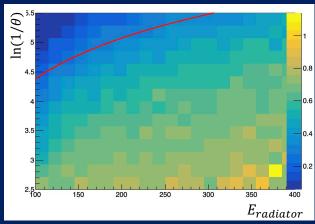
pp collisions  $\sqrt{s} = 13 \text{ TeV}$   $2.5 < \eta_j < 4$   $p_{T,jet} > 20 \text{ GeV}$ 

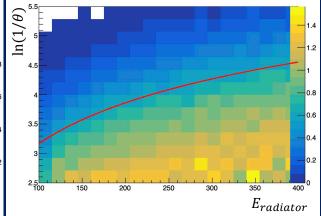


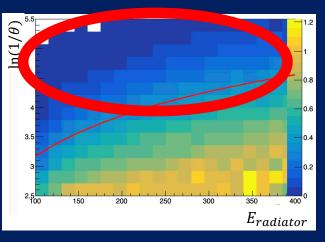
Charm/Light

Beauty/Charm

Beauty/Light







Dead cone effect is most prominent for Beauty/Light ratio

$$heta_{\mathrm{HQ}} = rac{m_{\mathrm{HQ}}}{E}$$



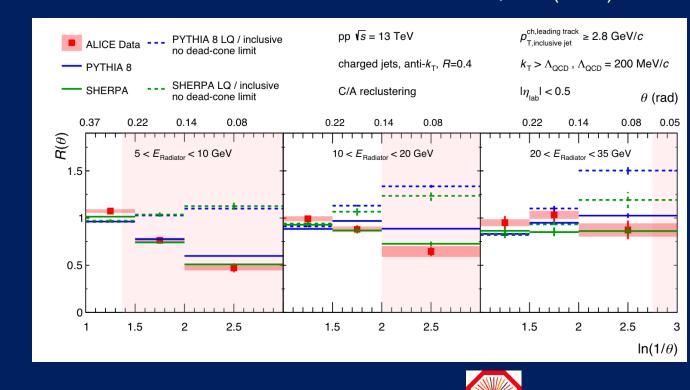


#### Dead cone measurement by ALICE

#### Ratio of charm to inclusive jets

#### Nature 605, 440 (2022)

- ALICE has observed the dead cone in charm jets relative to inclusive jets
- •We would like to measure beauty/light, charm/light, and beauty/charm







#### Recap: Lund jet plane at LHCb

We plan on measuring

- the LJP for *light*, *charm*, and *beauty* jets
- the LJP for track-based and track+neutral jets

• the *dead cone effect* from the various LJP measurements



## Questions for the community (I)

- Our definition of a heavy flavor jet (anti-k<sub>T</sub> containing a HF hadron) is not IRC safe beyond NLO. Would theorists advise using a different definition?
- Our HF LJPs contain gluon splitting events. Would trying to isolate these events also be of interest?
- For HF LJPs, some emissions have z > 0.5 (emission has more energy than the heavy quark). Should we discard these to maintain strict comparison with the light-quark case?



## Questions for the community (II)

- For track-based jets, one does not reconstruct the true kinematics of the radiator and the emission. Does this not lead to a large uncertainty on the LJP?
- Normalizing the dead cone ratio: ALICE measures their significance relative to the "no-dead-cone limit" at R = 1. The ratio of heavy/light emissions can be scaled by a multiplicative factor depending on how one chooses to normalize it. Would the choice of normalization affect the "no-dead-cone limit"? The average number of splittings per jet is different for heavy vs. light quark jets.
  - We tentatively plan to normalize by the number of emissions



## Backup



## Bibliography

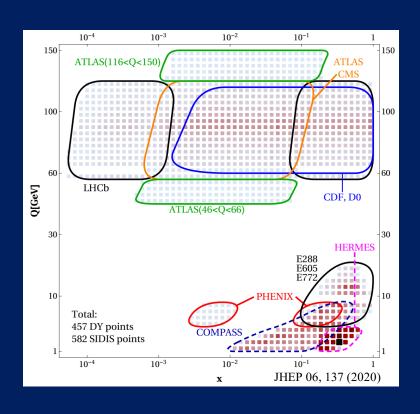
- Dokshitzer, Y.L., Khoze, V.A. and Troyan, S.I., 1991. *Journal of Physics G: Nuclear and Particle Physics*, 17(10), p.1602. [Intro to the dead cone effect and the leading particle effect]
- (Particle Data Group), Prog. Theor. Exp. Phys. 2022, 083C01 (2022) [Fragmentation functions of heavy quarks]
- Cacciari, Matteo, Gavin P. Salam, and Gregory Soyez. JHEP 2008.04 (2008): 063. [anti-kT algorithm]
- F. A. Dreyer, G. P. Salam, and G. Soyez, The Lund jet plane, J. High Energy Phys. 12 (2018) 064 [All the details on the Lund Jet Plane, with theoretical calculations + simulations]
- Cunqueiro, Leticia, and Mateusz Płoskoń. "Searching for the dead cone effects with iterative declustering of heavy-flavor jets." *Physical Review D* 99.7 (2019): 074027. [Exposing the dead cone effect using the Iterative Declustering technique]
- PRL 124.22 (2020): 222002 [ATLAS LJP measurement]
- arXiv:2111.00020v1 [ALICE preliminary measurement]
- *Nature* 605, no. 7910 (2022): 440-446 [ALICE Dead cone measurement]
- <a href="https://cds.cern.ch/record/2853467/files/SMP-22-007-pas.pdf">https://cds.cern.ch/record/2853467/files/SMP-22-007-pas.pdf</a> [CMS LJP Analysis Summary]

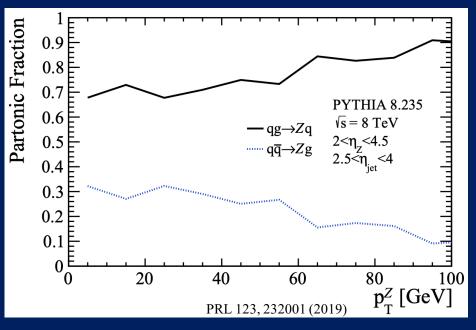
https://indico.cern.ch/event/575526/contributions/2368491/attachments/1426116/2187895/Mang ano-Lect3-print.pdf [Image and explanation of Angular Ordering]



#### Partonic fractions at forward rapidity

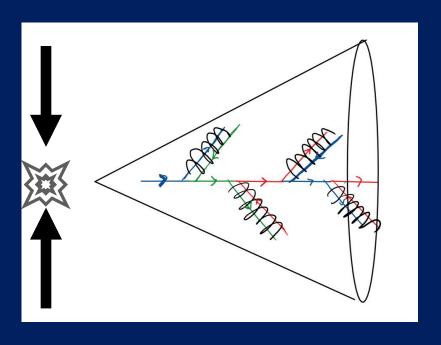
#### High-x enhances the light-quark jet fraction







# Single partons are inaccessible! Only access is to collimated cone of hadrons, i.e. *jets*



Hadronization

α π Β Κ π Κ π π

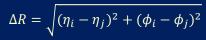


#### Jets and clustering algorithms

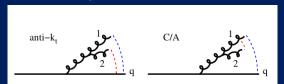
• Given a collection of particles, define a distance as

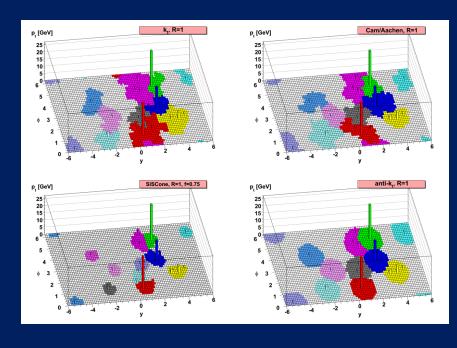
$$d_{ij} = min\left(p_{Ti}^{2p}, p_{Tj}^{2p}\right) \Delta R_{ij}^2 / R^2$$

- $p = 1: k_T$
- p = 0: Cambridge/Aachen (C/A)
- -p=-1: Anti- $k_T$
- Merge the two particles with the lowest distance first, repeat until all particles have been merged/clustered
- Anti-k<sub>T</sub> is infrared and collinear (IRC) safe, and produces conical jets



R: Jet Radius





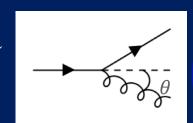
Cacciari, Matteo, Gavin P. Salam, and Gregory Soyez. JHEP 2008.04 (2008): 063.





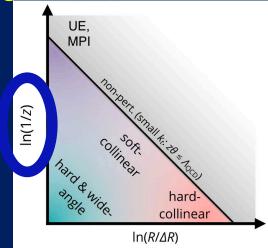
The Lund jet plane

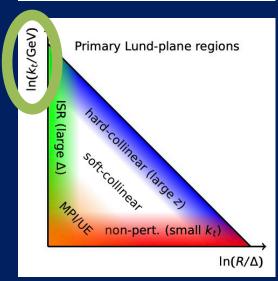
• The Lund jet plane (LJP) is a 2D "image" of parton emissions in jets



- Different representations of the LJP are possible, e.g.  $[\ln(1/z), \ln(R/\Delta R)]$  or  $[\ln(k_t), \ln(R/\Delta R)]$
- The LJP separates various types of emissions into different regions
- The plane is populated uniformly for soft and collinear emissions  $dP_{i\rightarrow ig} = dP_{i\rightarrow ig}$

$$dP_{i \to ig} = \frac{\alpha_s C_i}{\pi} \frac{d\theta^2}{\theta^2} \frac{dz}{z}$$





## Previous measurements of the Lund jet plane

#### arXiv:2111.00020v1

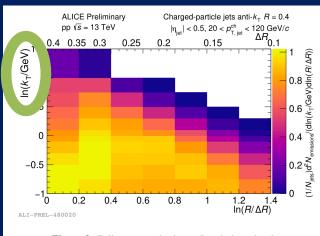
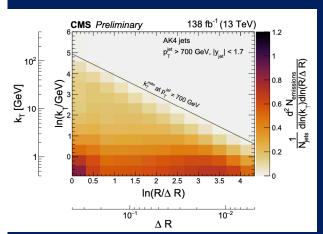


Figure 3: Fully corrected primary Lund plane density.



**ALICE** 

**CMS** 

PRL 124.22 (2020): 222002

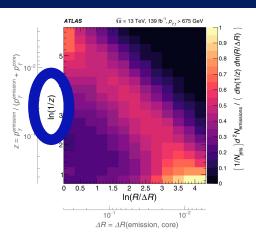


FIG. 2. The LJP measured using jets in 13 TeV pp collision data, corrected to particle level. The inner set of axes indicates the coordinates of the LJP itself, while the outer set indicates corresponding values of z and  $\Delta R$ .

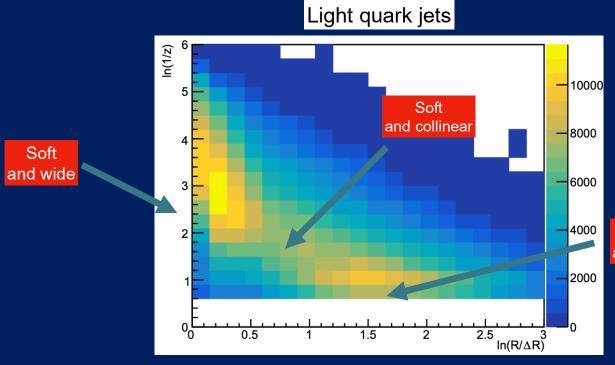
**ATLAS** 





#### LJP at forward rapidities

Pythia8 simulations



pp collisions

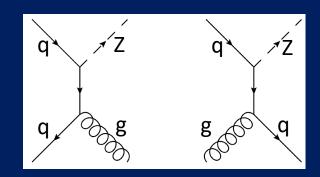
$$\begin{split} \sqrt{s} &= 13 \text{ TeV} \\ 2.5 &< \eta_j < 4 \\ p_{T,jet} &> 20 \text{ GeV} \end{split}$$

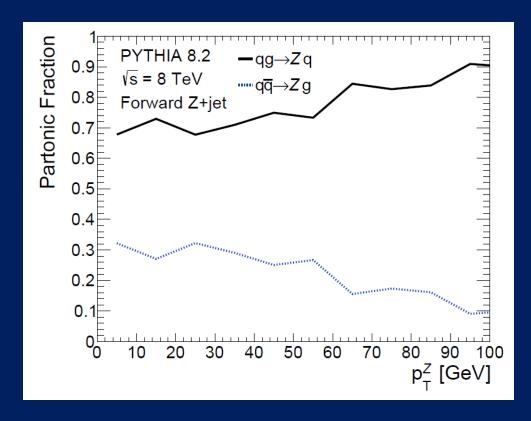
$$z = \frac{p_T^{soft}}{p_T^{hard} + p_T^{soft}}$$

Hard and collinear

#### Forward Z+jet

- Z+jet is predominantly sensitive to quark jets
- Forward
   kinematics
   increases
   fraction of light
   quark jets

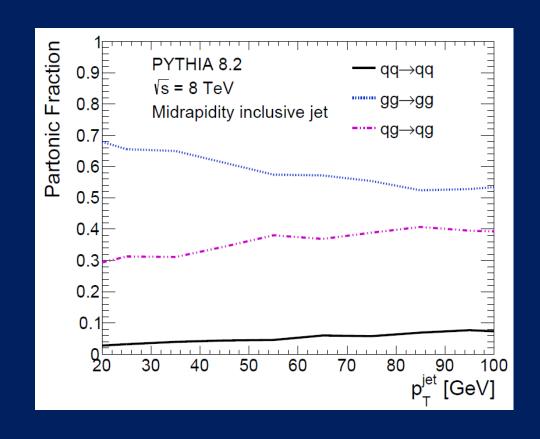






#### Forward Z+jet

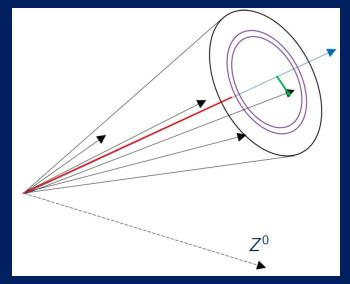
- In contrast to midrapidity inclusive jets, dominated by gluons
- Opportunity to study light quark vs. gluon jets
  - Hadronization dynamics
  - Jet properties





### Charged hadrons in forward Z+jet: Observables measured

- Longitudinal momentum fraction z
- Transverse momentum with respect to jet axis  $j_T$
- Radial profile r



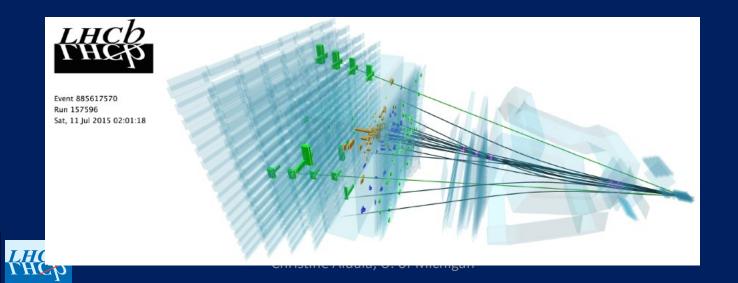
$$z = \frac{p_{jet} \cdot p_h}{|p_{jet}|^2}$$

$$j_T = \frac{|p_h \times p_{jet}|}{|p_{jet}|}$$

$$r = \sqrt{(\phi_h - \phi_{jet})^2 + (y_h - y_{jet})^2}$$

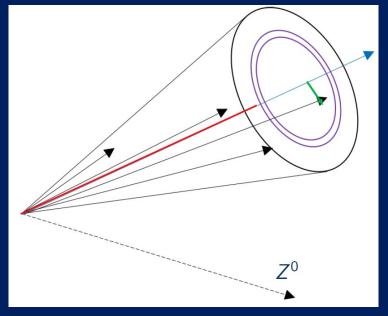
### PRL 123, 232001 (2019) Analysis details

- Follow similar analysis strategy to ATLAS and previous LHCb papers
  - ATLAS: EPJC 71, 1795 (2011), NPA 978, 65 (2018)
  - LHCb: PRL 118, 192001 (2017)
- $Z \rightarrow \mu^+\mu^-$  identified with  $60 < M_{\mu\mu} < 120$  GeV, in  $2 < \eta < 4.5$
- Anti-k<sub>T</sub> jets are measured with R = 0.5,  $p_T^{jet} > 20$  GeV, in  $2 < \eta < 4.5$
- $|\Delta\phi_{Z+jet}| > 7\pi/8$  selects  $2 \rightarrow 2$  event topology
- Charged hadrons selected with  $p_T > 0.25$  GeV, p > 4 GeV,  $\Delta R < 0.5$



### Charged hadrons in forward Z+jet: Observables

- Longitudinal momentum fraction z
- Transverse momentum with respect to jet axis  $j_T$
- Radial profile r



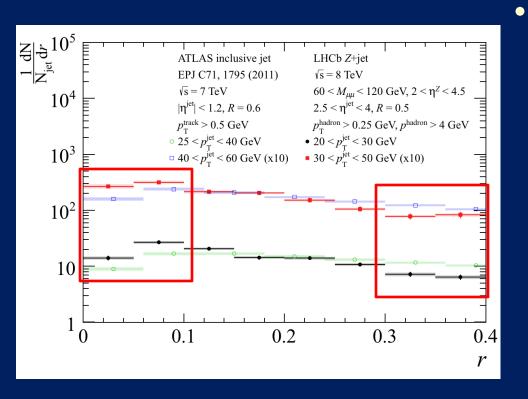
$$z = \frac{p_{jet} \cdot p_h}{|p_{jet}|^2}$$

$$j_T = \frac{|p_h \times p_{jet}|}{|p_{jet}|}$$

$$r = \sqrt{(\phi_h - \phi_{jet})^2 + (y_h - y_{jet})^2}$$



### Differences between quark- and gluondominated jet samples: Radial profile

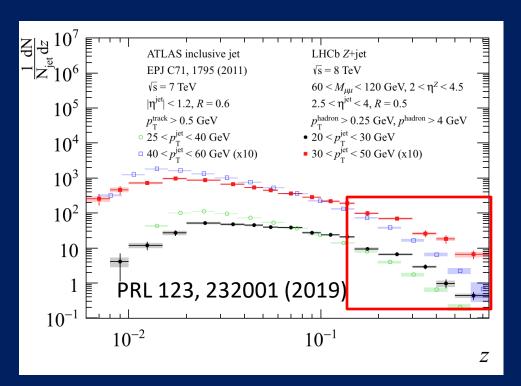


PRL 123, 232001 (2019)

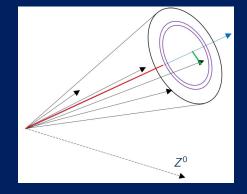
- Quark-dominated jets more collimated than gluon-dominated jets measured by ATLAS
  - I.e. more charged hadrons at small radii, fewer at large radii
  - Qualitatively agrees with conventional expectations, but this shows clear and quantitative evidence from data



### Differences between quark- and gluon-dominated jet samples: Longitudinal profile

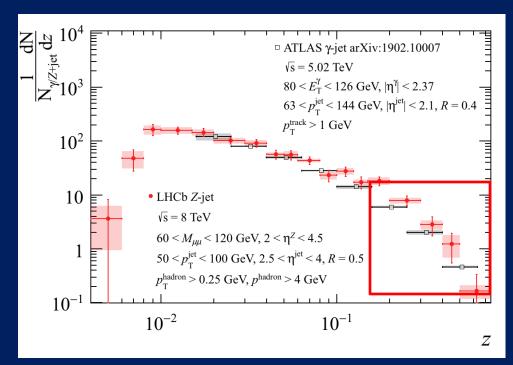


• Quark-dominated jets have relatively more hadrons produced at higher longitudinal momentum fractions than gluon-dominated jets

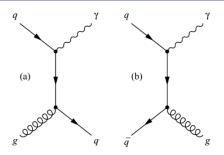




#### Differences between quark- and gluondominated jet samples: Longitudinal profile



PRL 123, 232001 (2019)



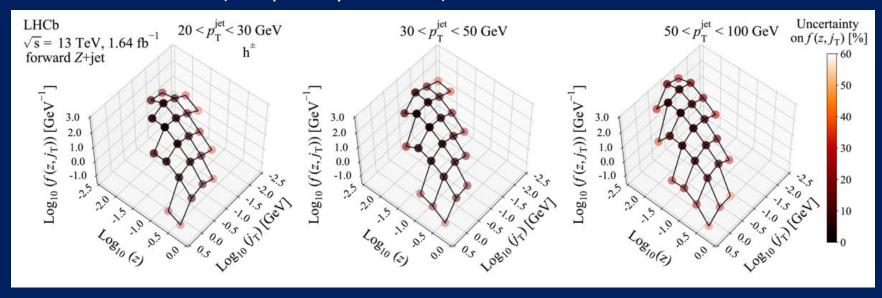
- ATLAS midrapidity γ+jet and LHCb Z+jet longitudinal momentum distributions are more similar
  - γ+jet, like Z+jet, enhances quark jet fraction
  - Further evidence that differences observed between LHCb results and ATLAS gluon-dominated results are due to differences in quark and gluon hadronization





#### First $\underline{multidifferential} z$ - $j_T distributions$

arXiv:2208.11691 (accepted by PRD Lett.)



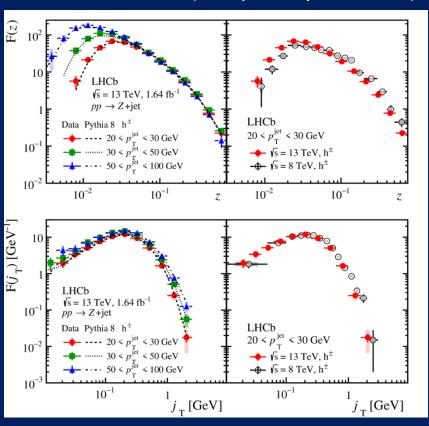
- Larger longitudinal momentum fraction z correlated with larger transverse momentum w.r.t. jet axis  $j_T$  differs from typical phenomenological assumption that they're uncorrelated!
- Larger  $j_T$  for given z in jets with higher  $p_T$ ; consistent with Markov chain fragmentation models, e.g. string or cluster models





### 1D distributions in Z+jet at 8 and 13 TeV

arXiv:2208.11691 (accepted by PRD Lett.)



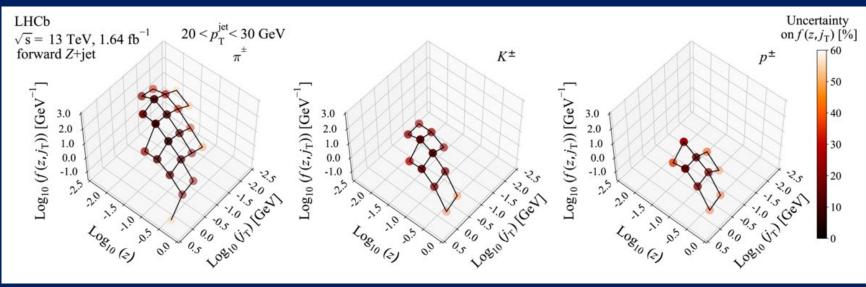
- At small z < 0.02, effects of color coherence as well as kinematic cuts manifest as a humped-back structure
- Harder jets, higher  $p_T$  or higher  $\sqrt{s}$ , produce an excess of soft particles per jet; access smaller z
- Scaling behavior at z > 0.04
- Similar pattern in  $j_T$  between  $\sqrt{s}$  = 8 and 13 TeV





# Multidifferential distributions for identified $\pi^{\pm}$ , $K^{\pm}$ , and $p^{\pm}$

arXiv:2208.11691 (accepted by PRD Lett.)



- Multidifferential distributions for pions, kaons, and protons at  $20 < p_T^{jet} < 30 \text{ GeV/c}$
- Heavier hadrons produced at larger  $j_T$  and z

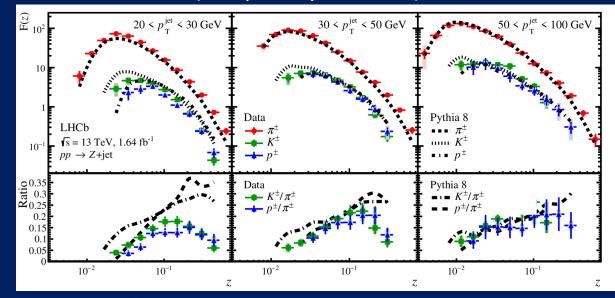




# 1D distributions and ratios for $\pi^{\pm}$ , $K^{\pm}$ , and $p^{\pm}$

- Charged hadron formation within jets predominantly  $\pi^{\pm}$  due to its low mass and flavor content of initial-state protons
- Hadrons with higher mass require a larger z threshold for their formation

arXiv:2208.11691 (accepted by PRD Lett.)



In lowest jet  $p_T$  interval

- Proton production relative to kaons clearly suppressed at lower z
- Pythia 8 overestimates kaon and proton production relative to pions



### 13 TeV identified hadron-in-jet analysis

#### **Dataset & Selections**

- MC : Reco16 Sim09j
  - Generation Code: 42112001
  - Generator level cuts :  $p_T(\mu)$  > 4 GeV/c,  $\eta(\mu)$ > 1.6 and  $m_{\mu\mu}$ >40 GeV/c²
- Data: Run II 2016 p+p data
- Stripping line: 'Z02MuMuLine' in Stripping28r2
- Trigger :
  - LOMuonEWDecision & Hlt1SingleMuonHighPTDecision
     & Hlt2EWSingleMuonVHighPtDecision
- Event requirement :
  - nPV=1

#### • Z selection:

- $p_T(\mu) > 20 \text{ GeV/c}, 2 < \eta(\mu) < 4.5$
- $\frac{\sigma_p}{p}$  < 0.1, P( $\chi^2$ ) > 0.1%, isMuon
- $60 < m_{\mu\mu} < 120 \text{ GeV/c}^2$
- Jet selection:
  - StdJets,  $p_T(\text{jet}) > 20$  [15] GeV/c, 2.5 <  $\eta(\text{jet})$  <4.0, deltaR(jet)=0.5
  - $\Delta \phi$ (jet- $\mu$ ) > 0.4
  - $\Delta \phi$  (Z-jet)> $\frac{7}{8}\pi$
- Track selection
  - Track  $\chi^2$ /ndf < 3
  - 4
  - $p_T > 0.25 \text{ GeV/c}$