

# Tagging with the Lund Jet Plane

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First Lund Jet Plane Institute - CERN  
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In Collaboration With

L.Cavallini, A.Coccaro, O.Fedkevych, F.Giuli, G.Manco, S.Marzani, F.Parodi,  
D.Rebuzzzi, A.Rescia, F.Sforza And G.Stagnitto

# Outline

- W tagging F.A.Dreyer, G.P.Salam and G.Soyez, [JHEP 12 \(2018\), 064](#)
- Higgs tagging
  - Lund jet plane and jet color ring CKK and S.Marzani, [Phys. Rev. D 104 \(2021\), 055043](#)
  - Lund jet plane and color sensitive observables Cavallini *et al.*, [Eur. Phys. J. C 82 \(2022\) no.5, 493](#)
- B-tagging O.Fedkevych, CKK, S. Marzani and F. Sforza, [Phys. Rev. D 107\(2023\) no.3, 034032](#)
- Top tagging F.A.Dreyer, and H.Qu, [JHEP 03 \(2021\), 052](#)
- Quark-Gluon tagging F.A.Dreyer, G. Soyez and A.Takacs, [JHEP 08 \(2022\), 177](#)

# Boosted Jets

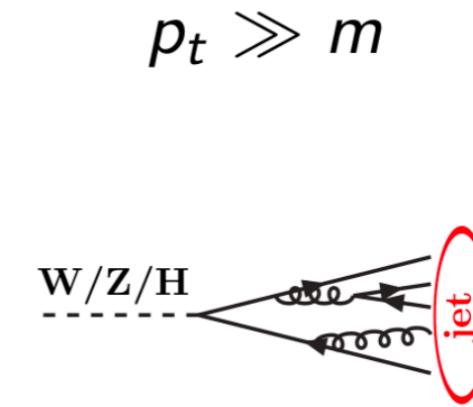
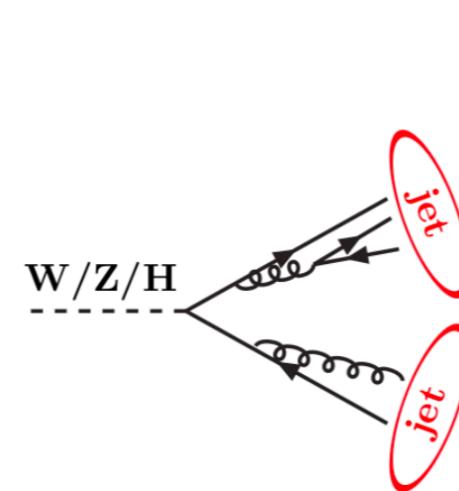
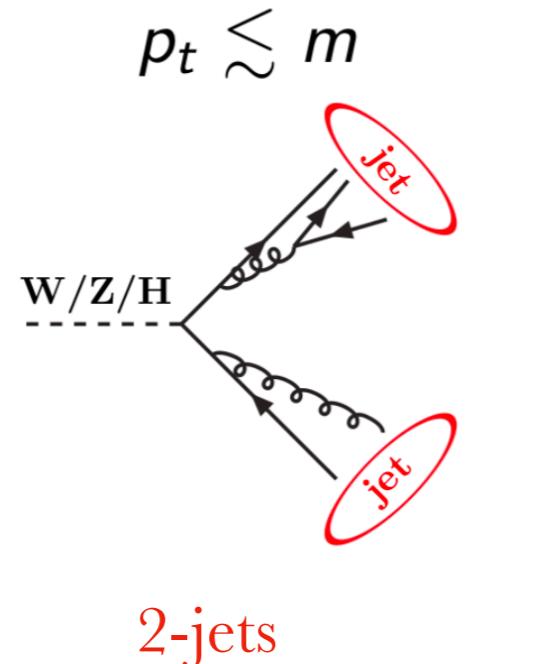
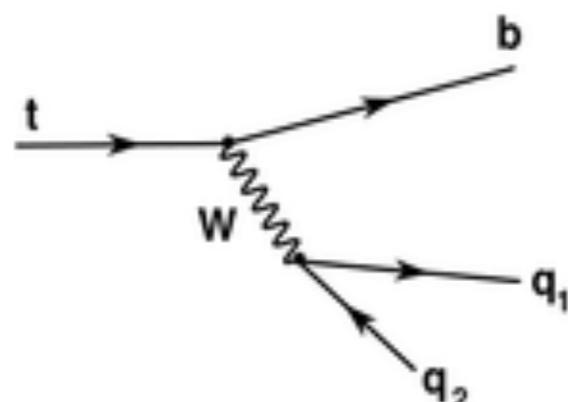
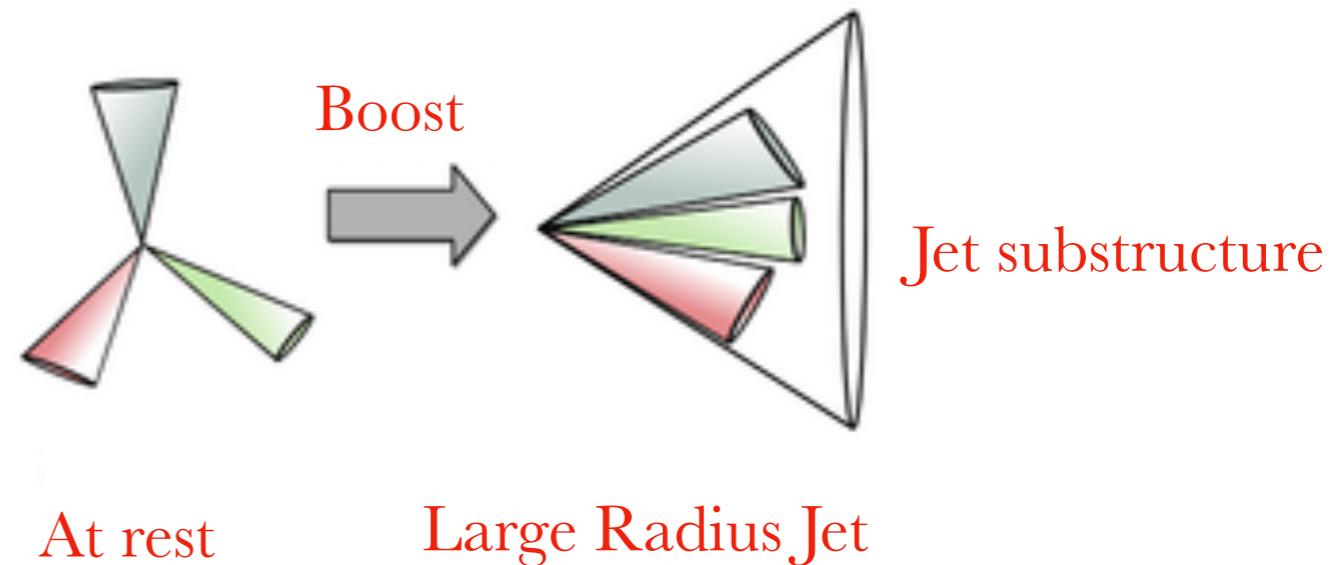


Figure taken from F.Dreyer's slide, original figure credit: G.Soyez

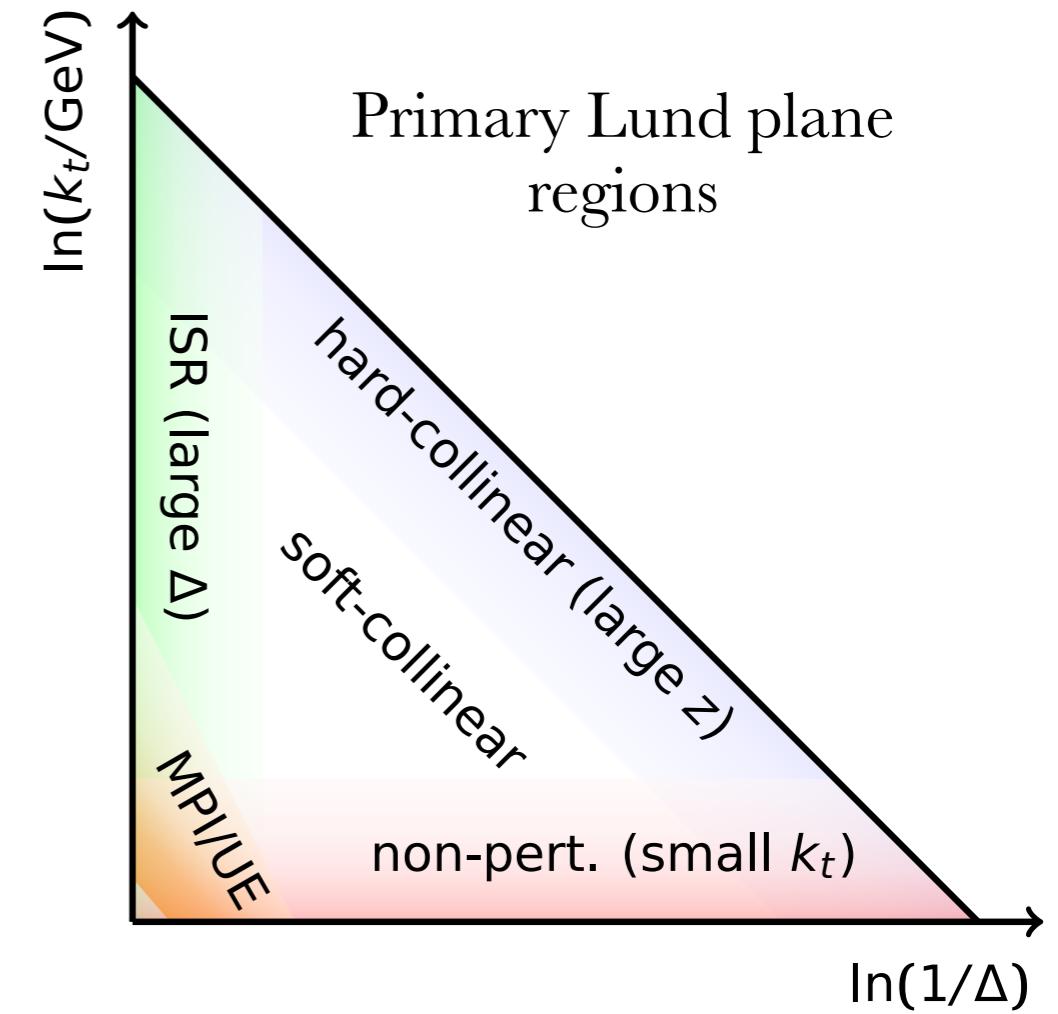
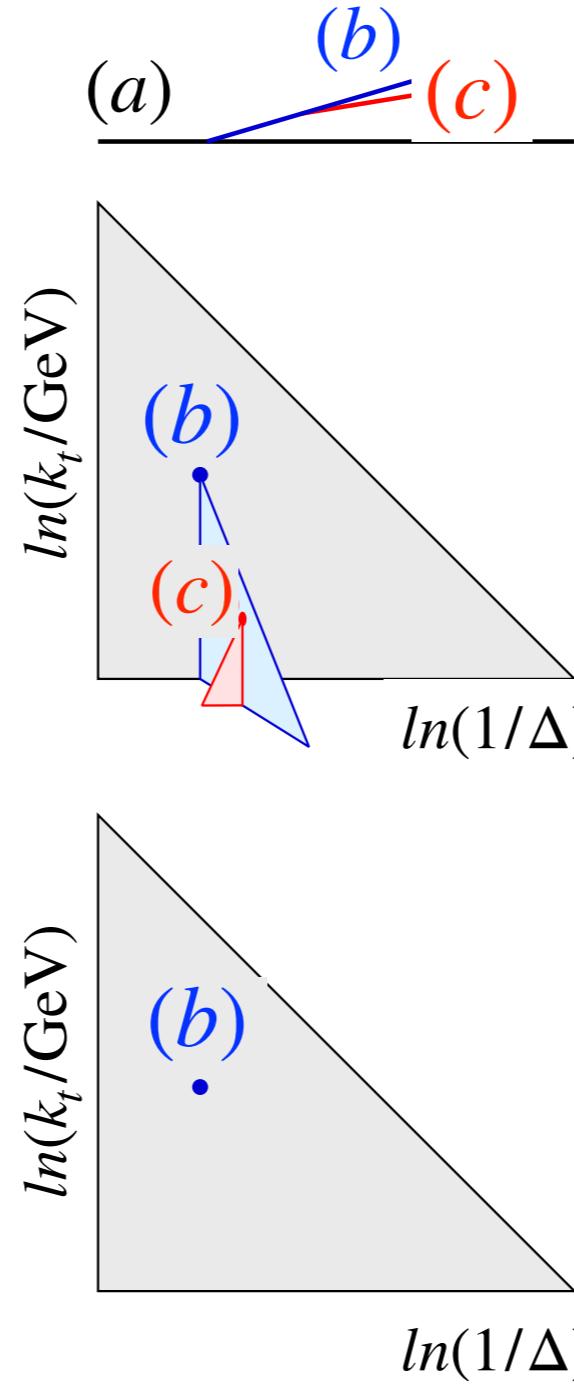
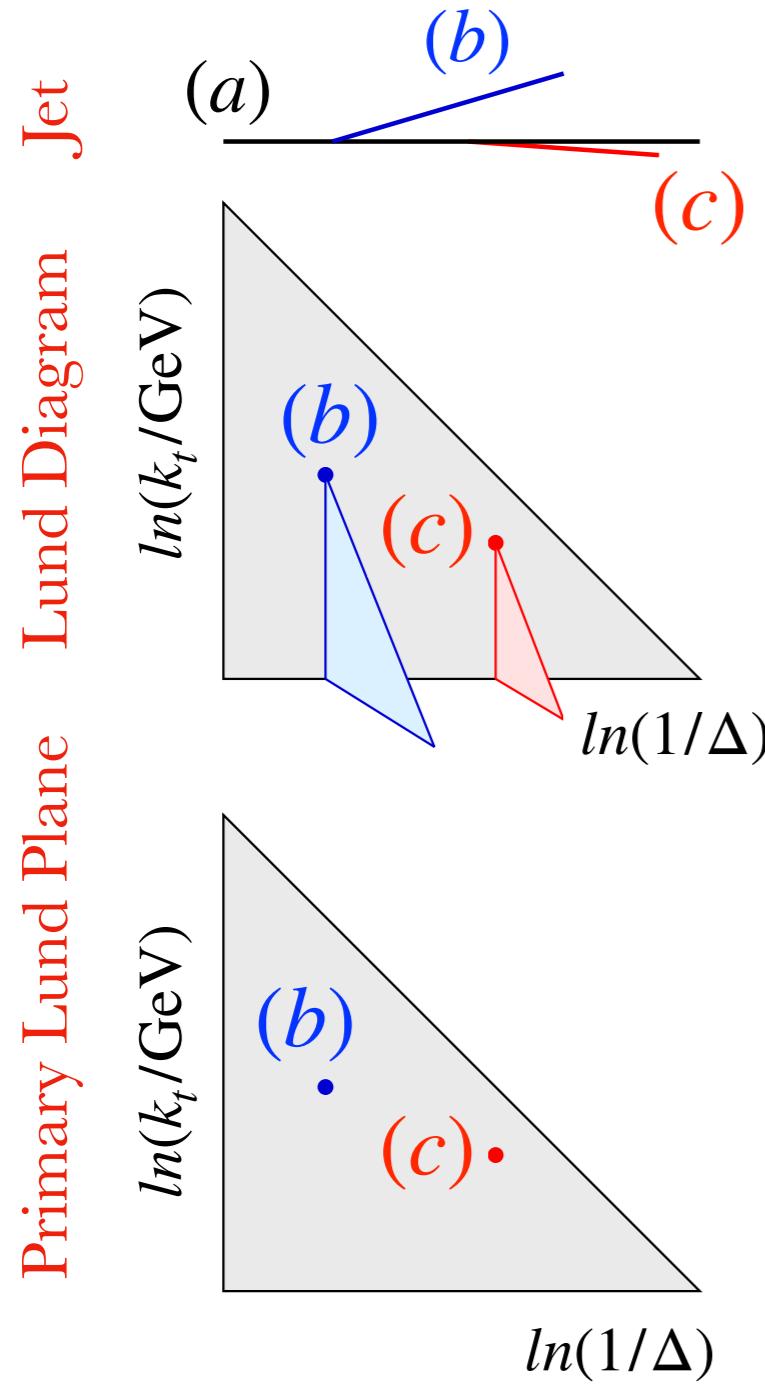
Adapted from:  
<https://www.physi.uni-heidelberg.de>



Top Quark Decay



# Lund Jet Plane



$\Delta$  is the opening angle of the emission.  
 $k_T$  is the transverse momentum w.r.t the jet axis.

# (Primary) Lund Jet Plane

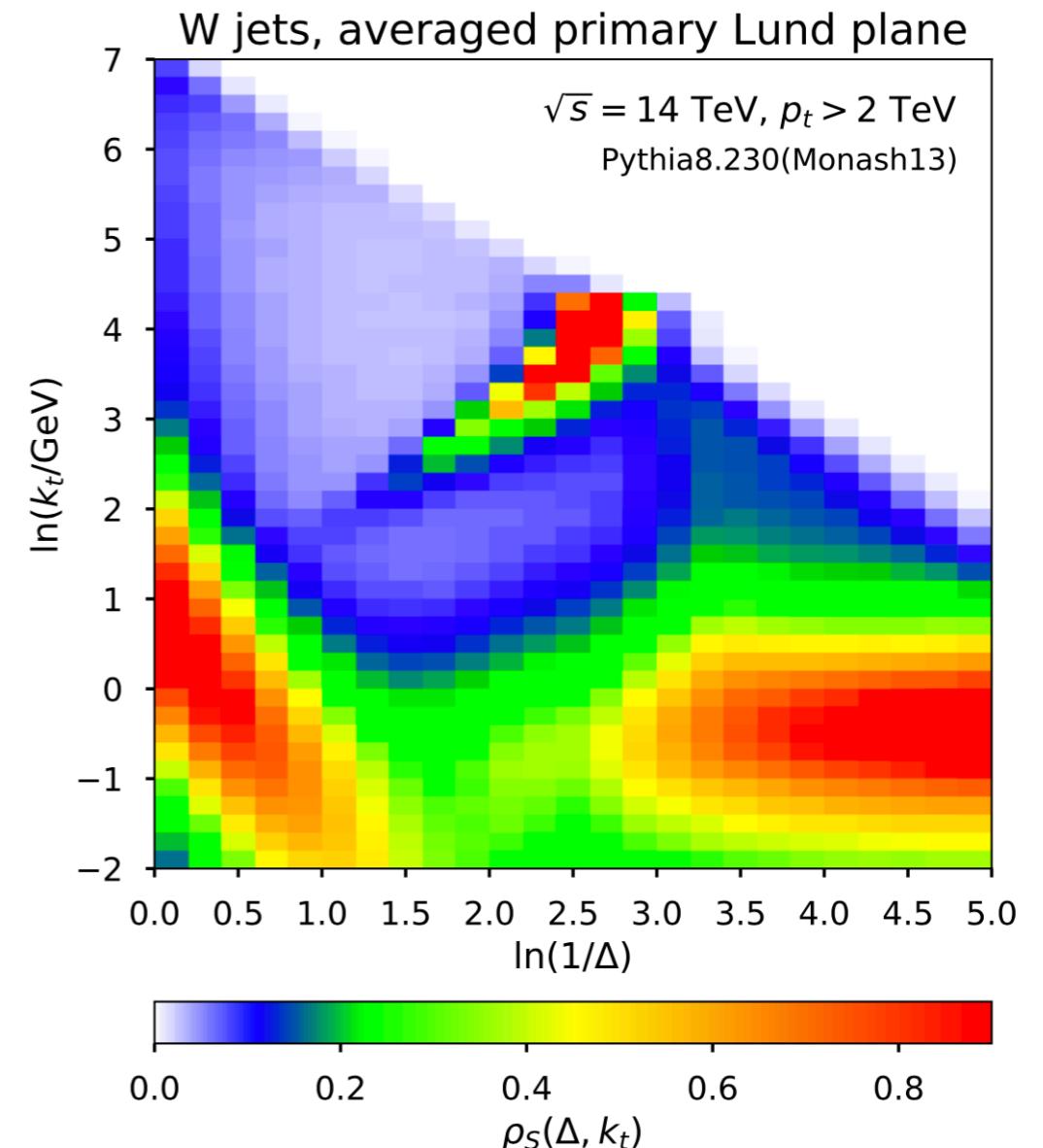
- Re-cluster the constituents using C/A algorithm.
- Start with declustering C/A jet (undo last clustering step) we get two subjects (ordered by momentum).
- Save the kinematic of each declustering step as a tuple  $\mathcal{T} = \{k_t, \Delta, z, m, \psi\}$

$$\Delta^2 \equiv (y_1 - y_2)^2 + (\phi_1 - \phi_2)^2 \quad k_t \equiv p_{t2}\Delta$$

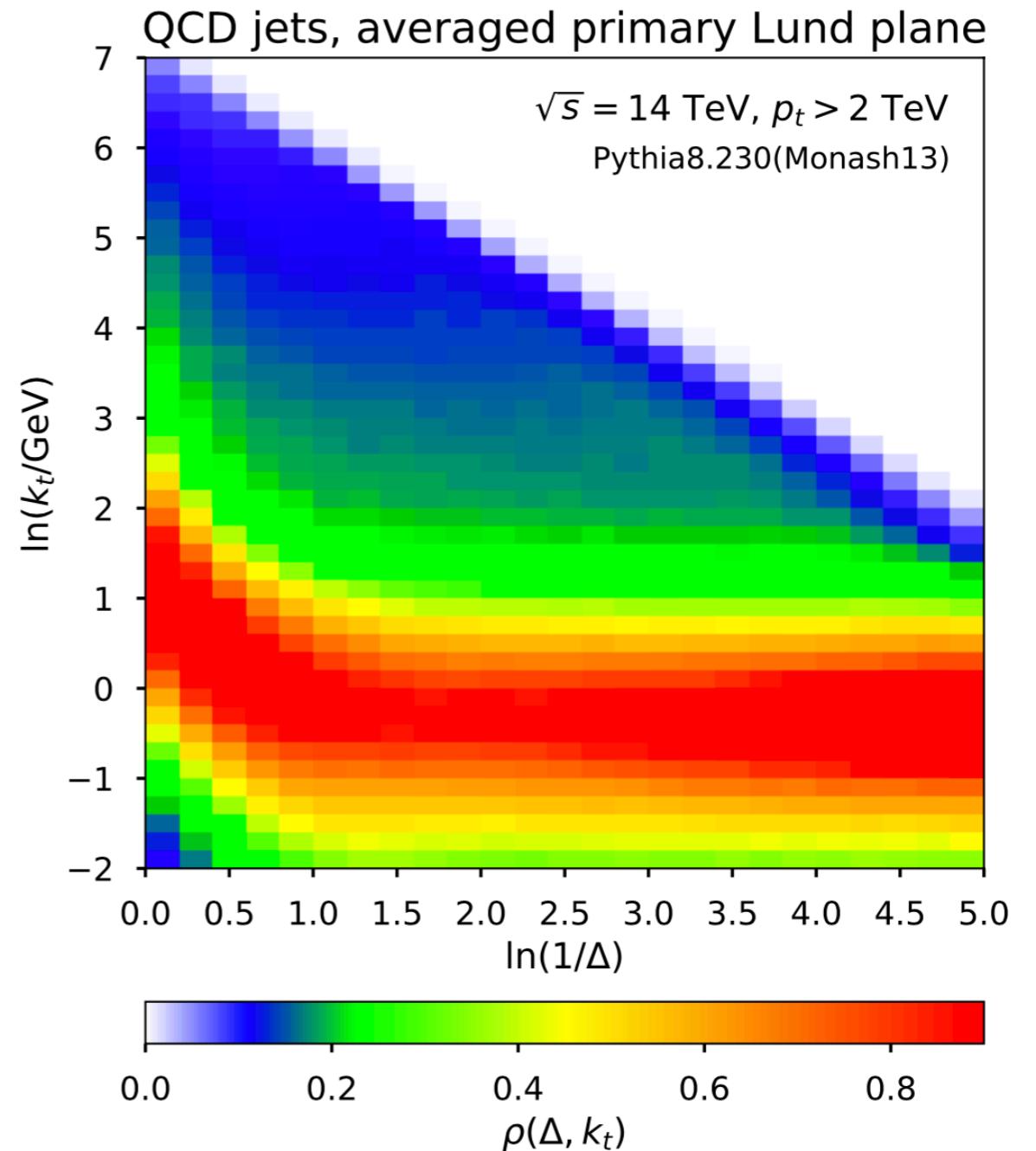
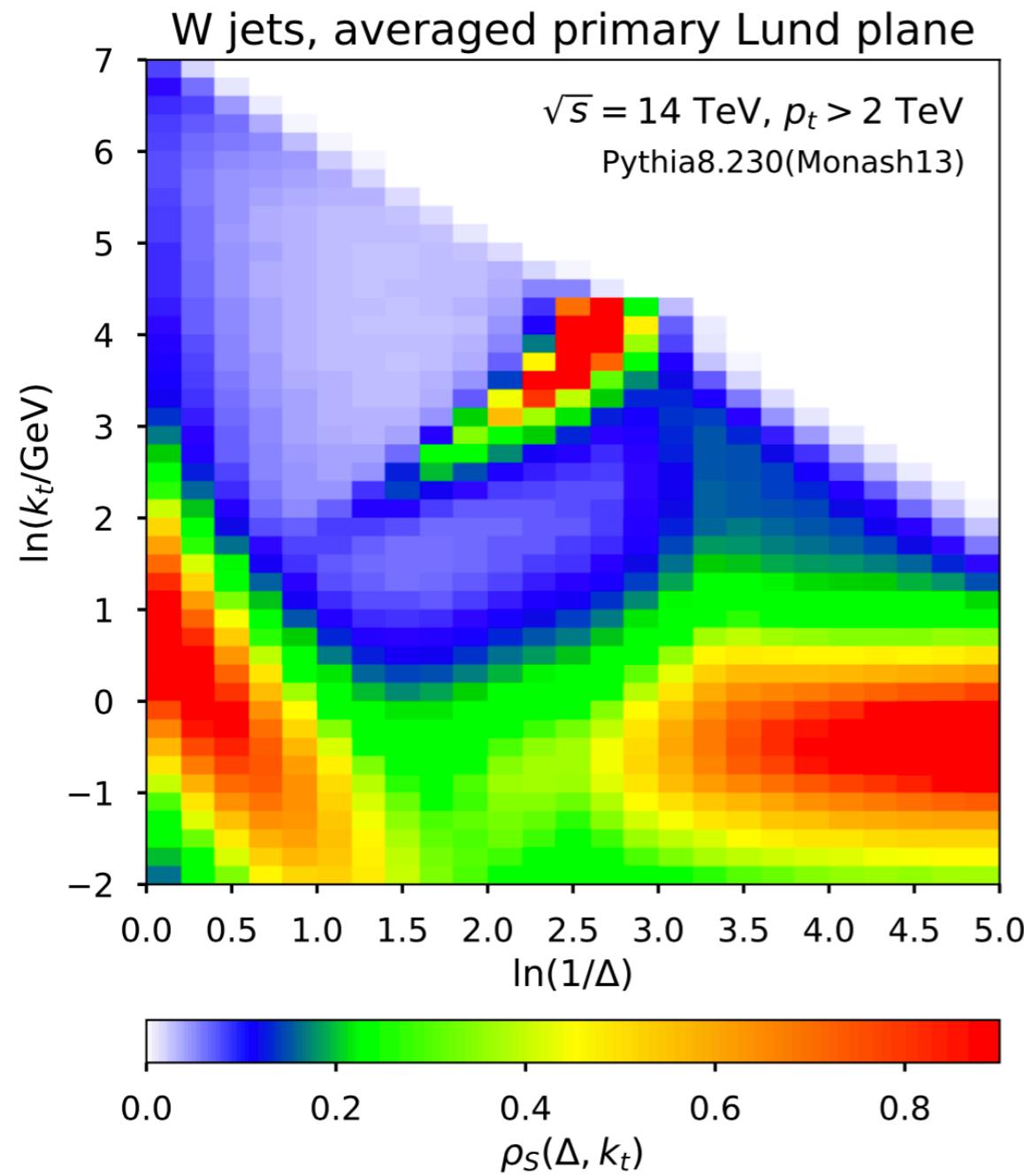
$$z \equiv \frac{p_{t2}}{p_{t1} + p_{t2}} \quad m^2 \equiv (p_1 + p_2)^2 \quad \psi \equiv \tan^{-1} \frac{y_2 - y_1}{\phi_2 - \phi_1}$$

- Following a history of the hardest branch, we get double logarithmic plane  $\left( \ln \frac{1}{\Delta}, \ln \frac{k_t}{\text{GeV}} \right)$ .
- Pixels corresponding to the splitting are turned on.

LundPlane library is publicly available as a part of FastJet contrib package.

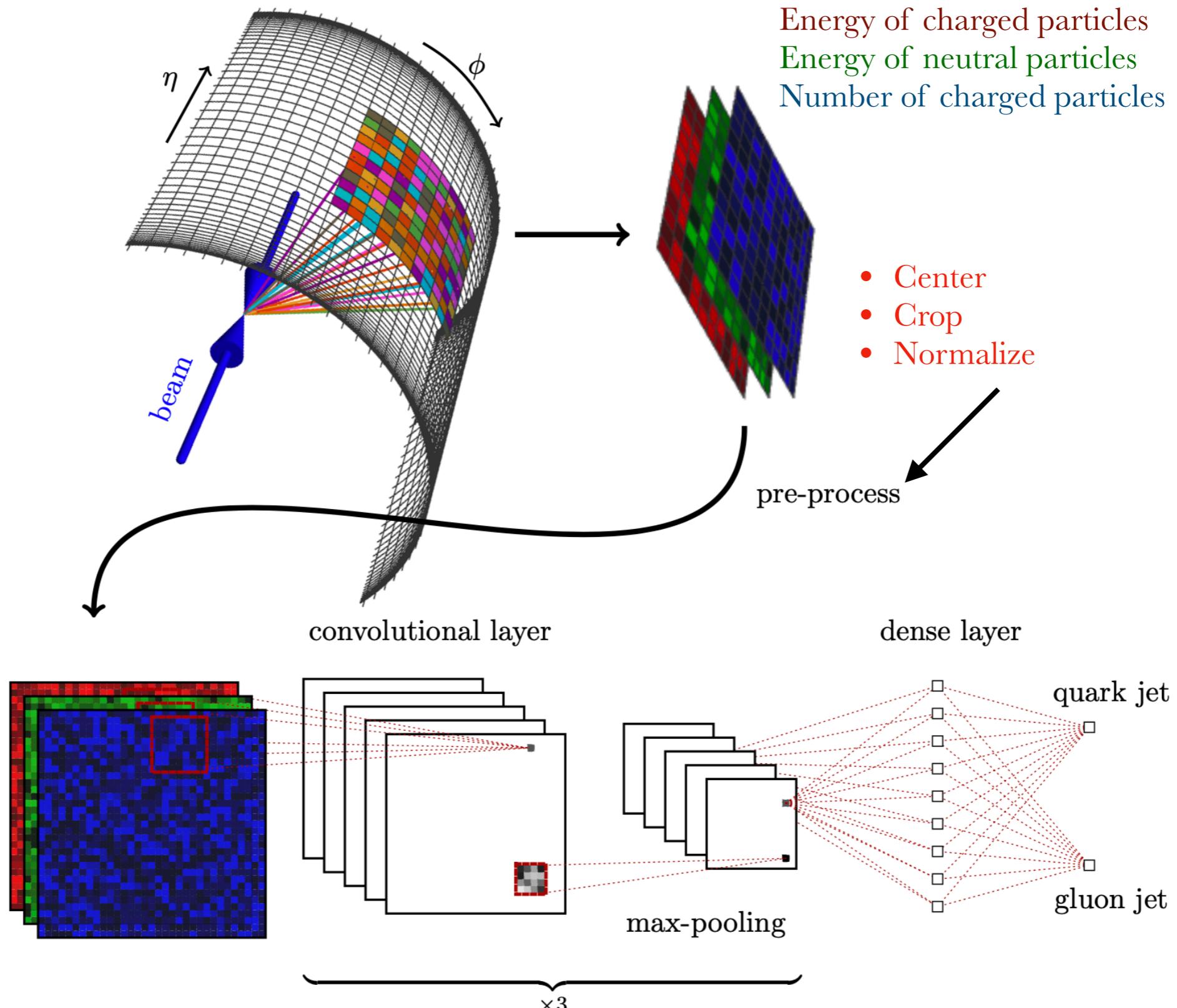


# W and QCD Jets

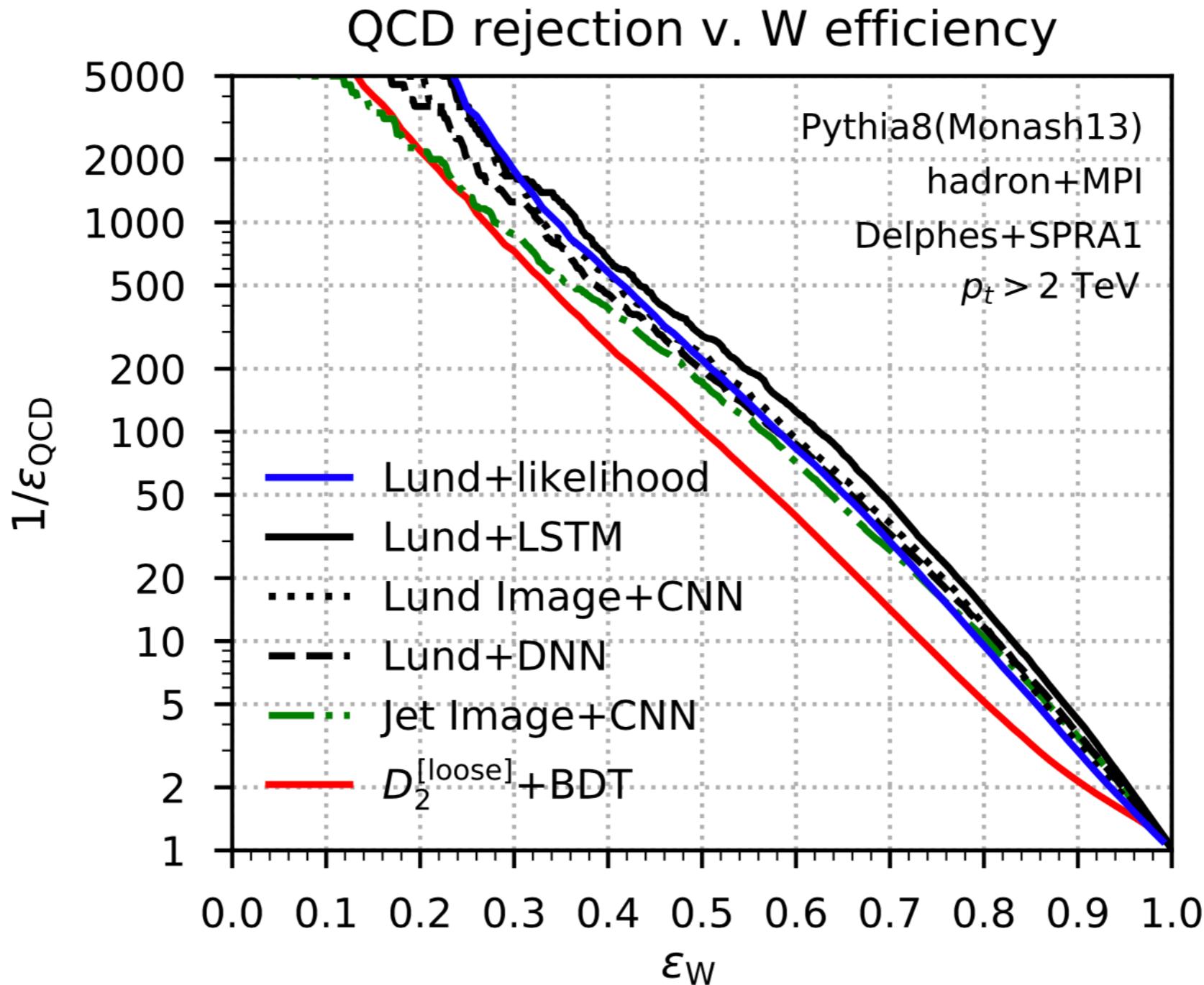


F.A.Dreyer, G.P.Salam and G.Soyez, [JHEP 12 \(2018\), 064](#)

# Example: Jet Images as an input to CNN



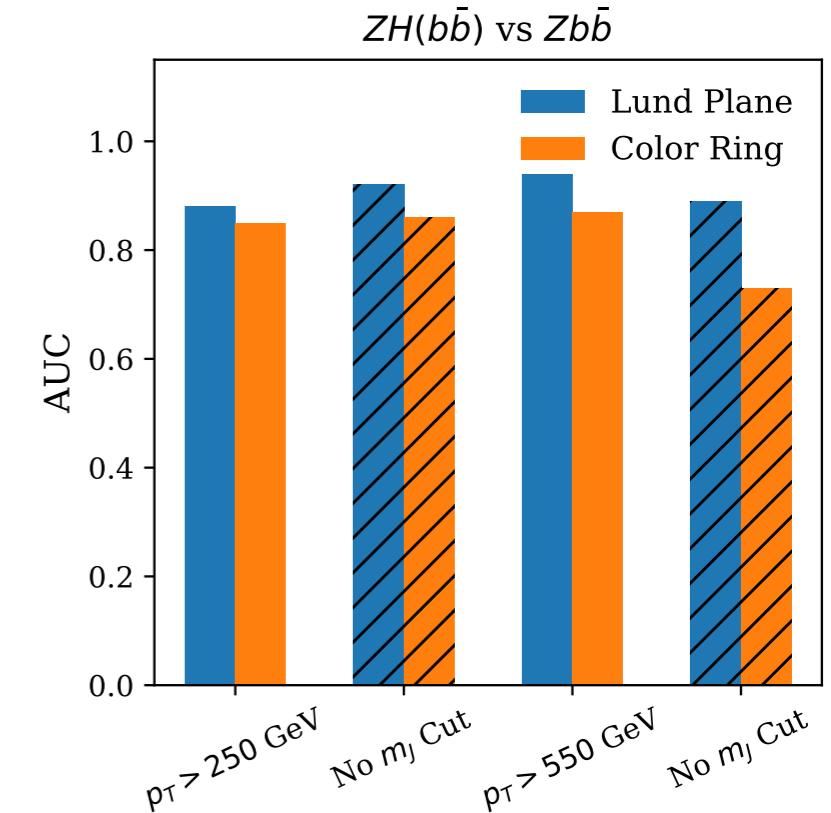
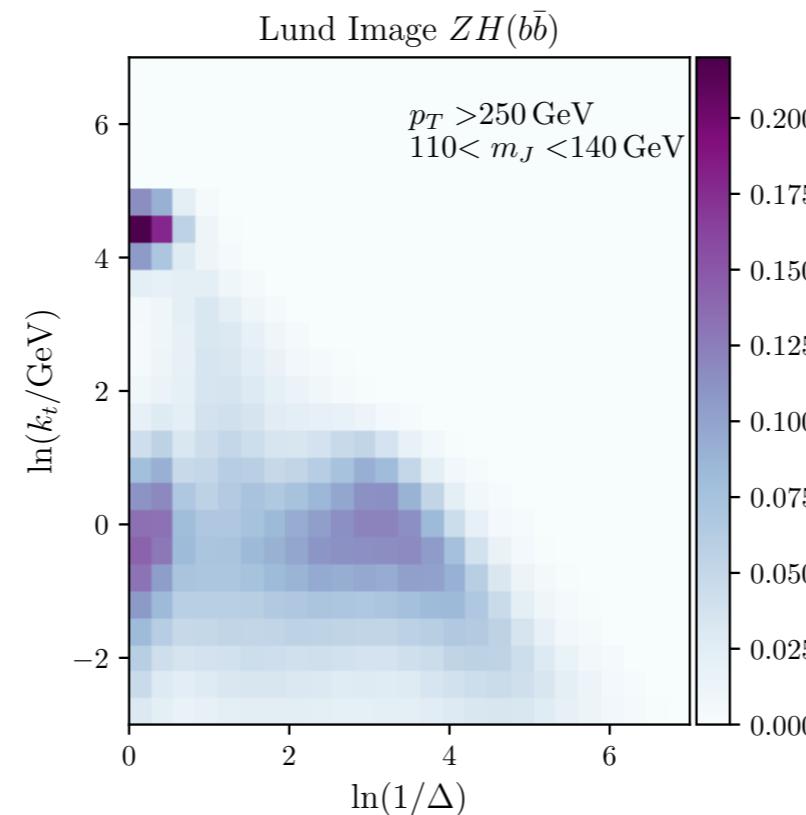
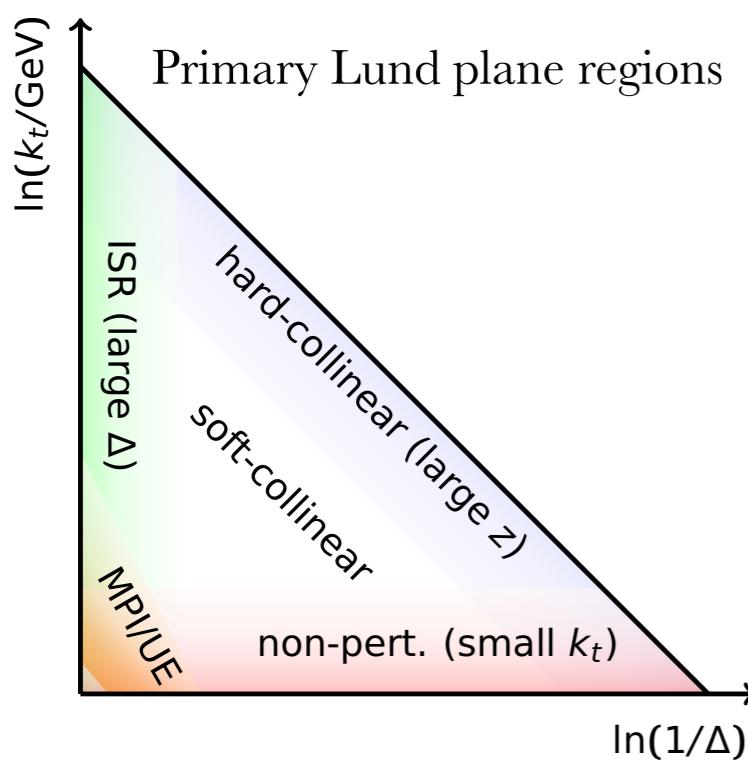
# W Tagging using Lund Jet Plane



F.A.Dreyer, G.P.Salam and G.Soyez, [JHEP 12 \(2018\), 064](#)

# Higgs Tagging using the Lund Jet Plane

CKK and Simone Marzani, Phys. Rev. D 104 (2021) no.5, 055043, arXiv:2105.03989 [hep-ph]



F.A.Dreyer, G.P.Salam and G.Soyez,  
JHEP 12 (2018), 064

Jet color ring  $\mathcal{O} = \frac{\theta_{ka}^2 + \theta_{kb}^2}{\theta_{ab}^2}$

# Simulation Set-up

Tools: Madgraph 2.7.2, Pythia 8 and Fastjet 3.0.

High and moderate  $p_T$  benchmarks:  $p_T > 250$  GeV and  $p_T > 550$  GeV.

Generation level cuts:  $p_T > 200$  GeV and  $p_T > 500$  GeV,  $|\eta_j| < 5.0, |\eta_l| < 2.5$ .

Jet mass cut:  $110 < m_J < 140$  GeV .

$$H \rightarrow b\bar{b}$$

$$pp \rightarrow ZH \text{ (}Z \rightarrow \mu^+\mu^-, H \rightarrow b\bar{b}\text{)}$$

$$pp \rightarrow Zb\bar{b} \text{ (}Z \rightarrow \mu^+\mu^-\text{)}$$

$$H \rightarrow gg$$

$$pp \rightarrow ZH \text{ (}Z \rightarrow \mu^+\mu^-, H \rightarrow gg\text{)}$$

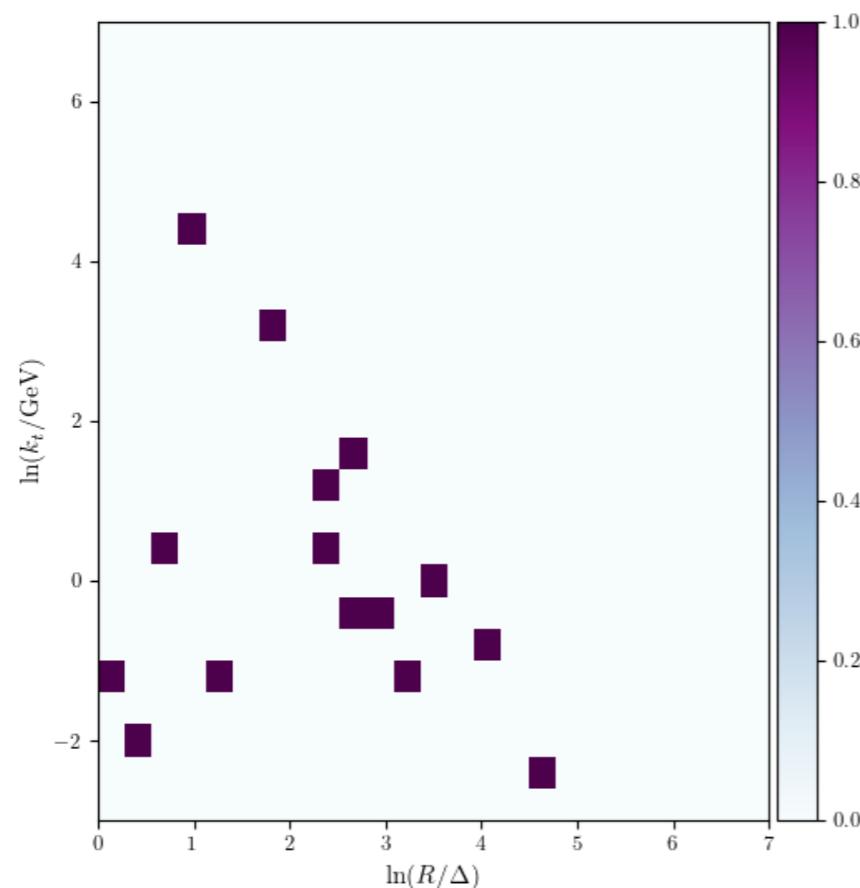
$$pp \rightarrow Zjj \text{ (}Z \rightarrow \mu^+\mu^-\text{)}$$

# Mapping Events to the (primary) Lund Jet Plane

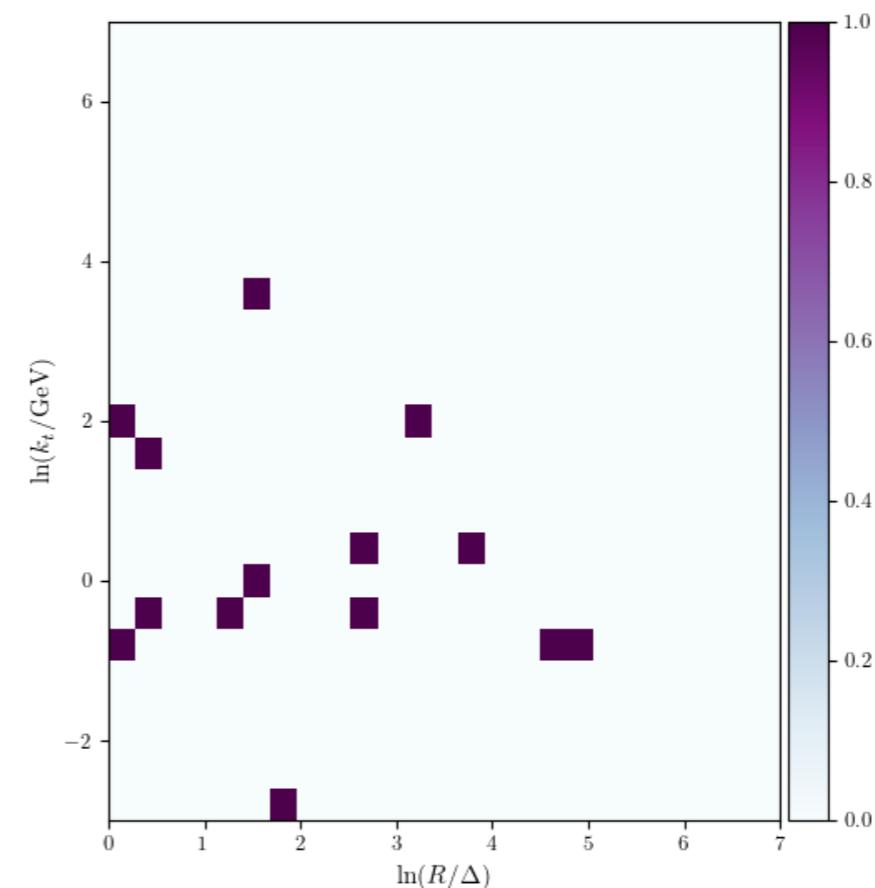
- Consider a list of particles (except the muons from hard scattering).
- Form anti- $k_t R = 1$  jets using Fastjet.
- Cluster the constituents of the leading jet using C/A algorithm with a maximum allowed jet radius.
- Save the Lund coordinates history of the hardest branch.
- Use a double logarithmic plane  $\left( \ln \frac{1}{\Delta}, \ln \frac{k_t}{\text{GeV}} \right)$ .
- Pixels ( $25 \times 25$ ) corresponding to the splitting are turned on.

# Lund Jet Plane

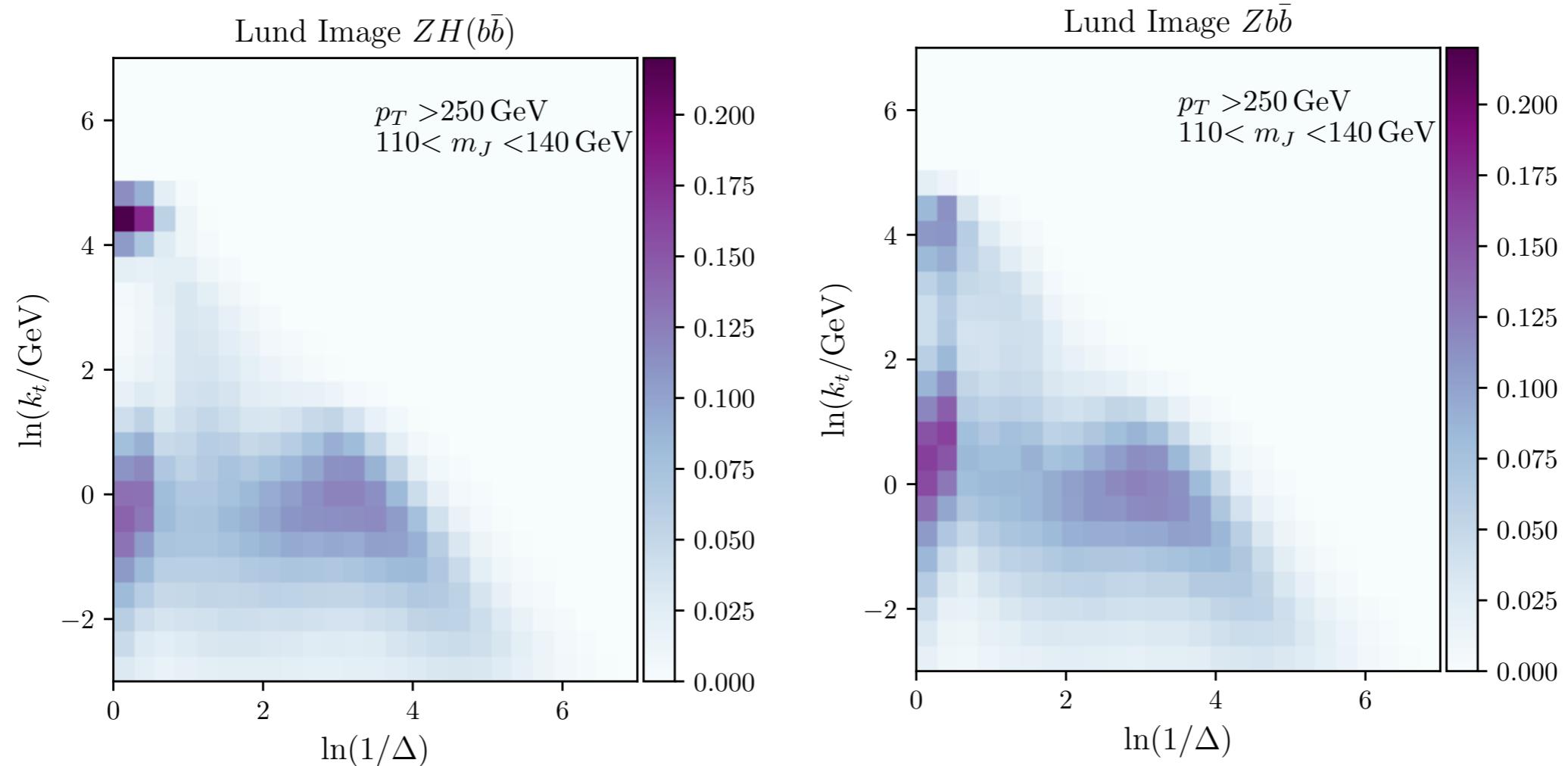
Signal



Background

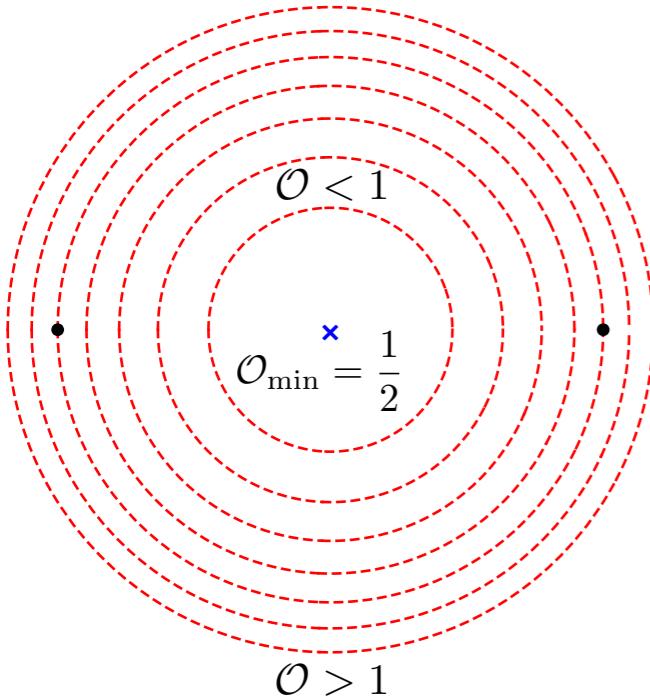


# (Averaged ) Lund Jet Images

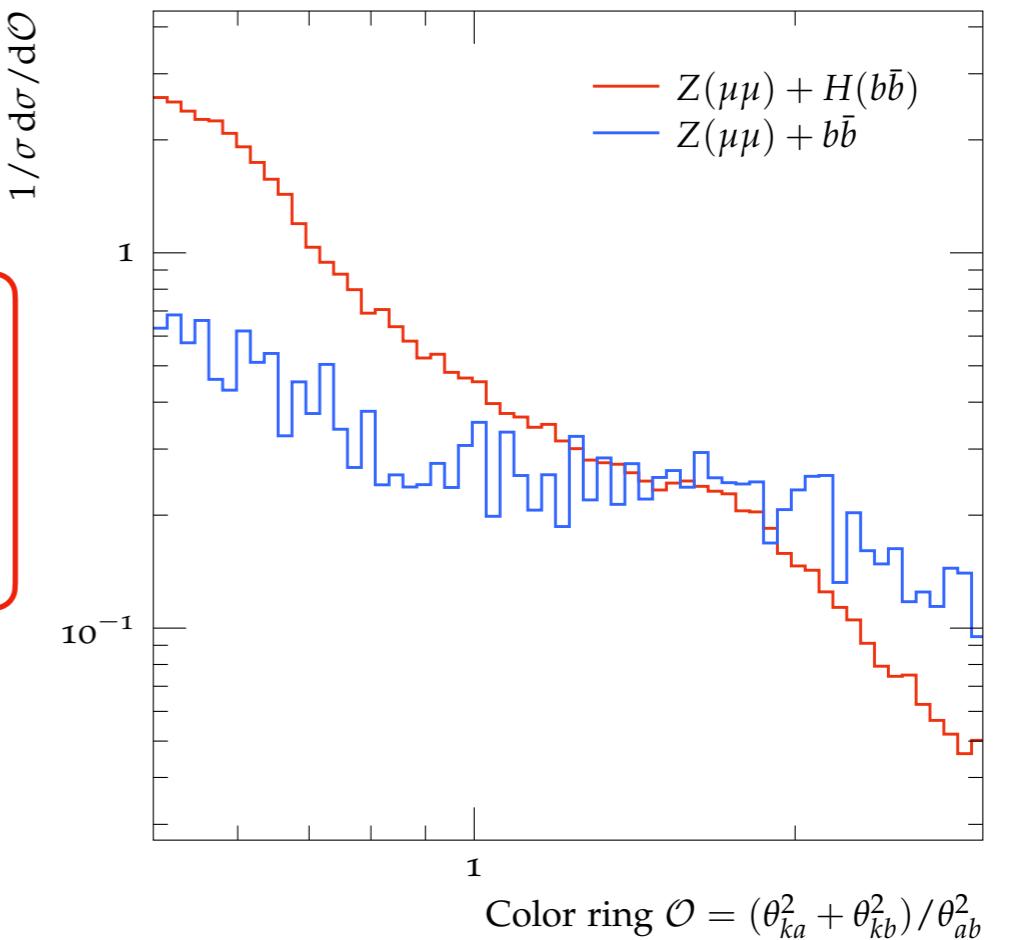


anti- $k_T$  R=1 jets, reclustered the constituents using C/A algorithm

# Color Singlet Tagger: Jet Color Ring



$$\frac{|\mathcal{M}_S|^2}{|\mathcal{M}_B|^2} \simeq \frac{\theta_{ak}^2 + \theta_{bk}^2}{\theta_{ab}^2}$$



# Constructing the Jet Color Ring

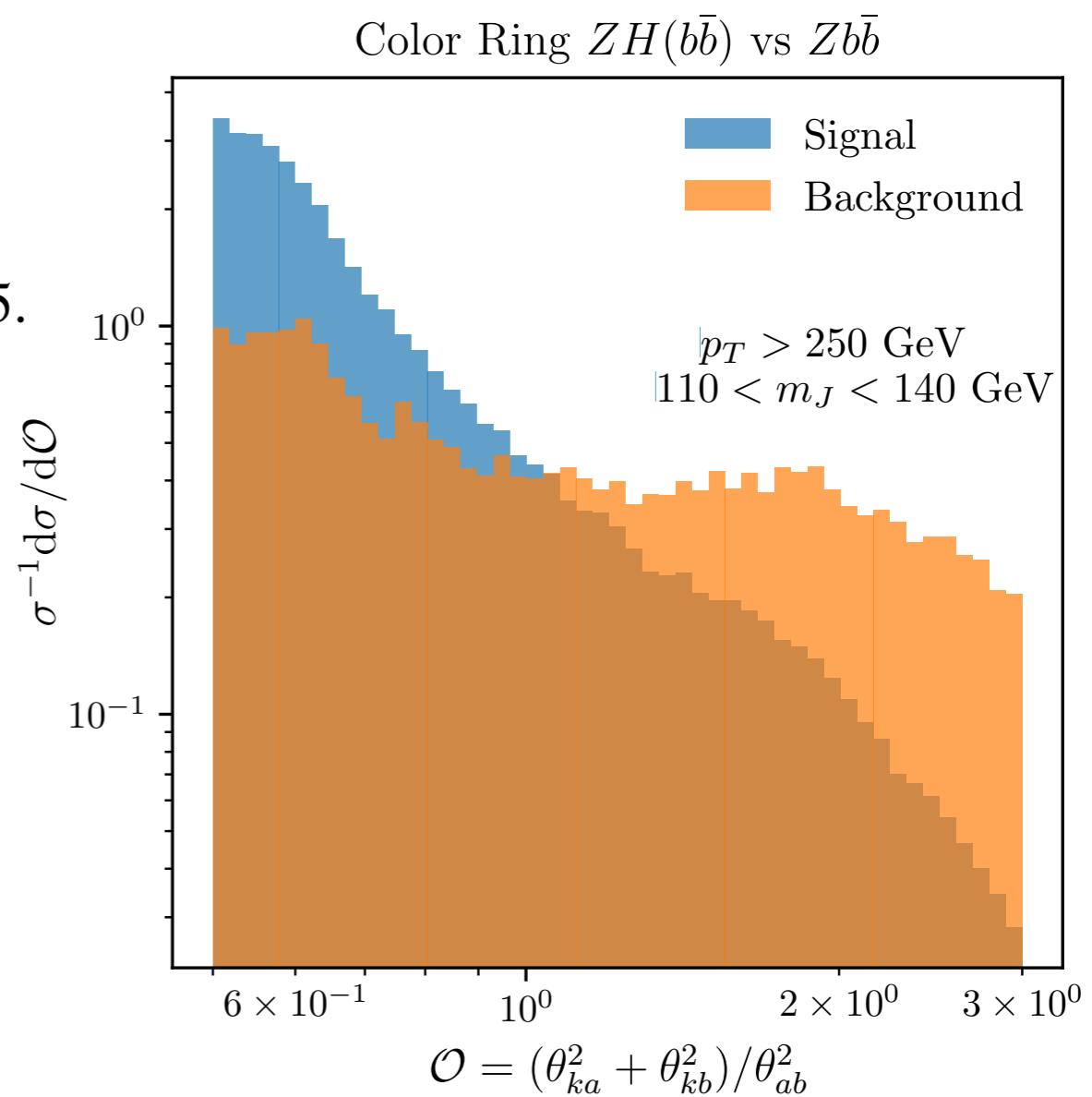
Identify sub-jets within the large  $R$  jet

- Charged particles with  $p_T > 500$  MeV,  $|\eta| < 5$ .
- Construct  $R = 0.2$  track-jets using anti- $k_t$  algorithm.
- Consider track jets with  $p_T > 5$  GeV and  $\Delta_{Jj} < 0.8$ .

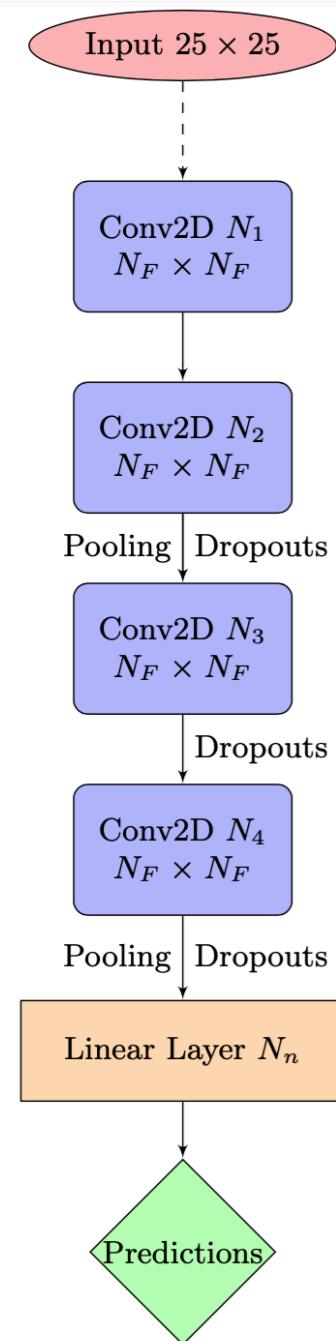
$\Delta_{jb/j\bar{b}} < 0.2$

b-jets      light-jets

$$\mathcal{O} = \frac{\theta_{ka}^2 + \theta_{kb}^2}{\theta_{ab}^2}$$



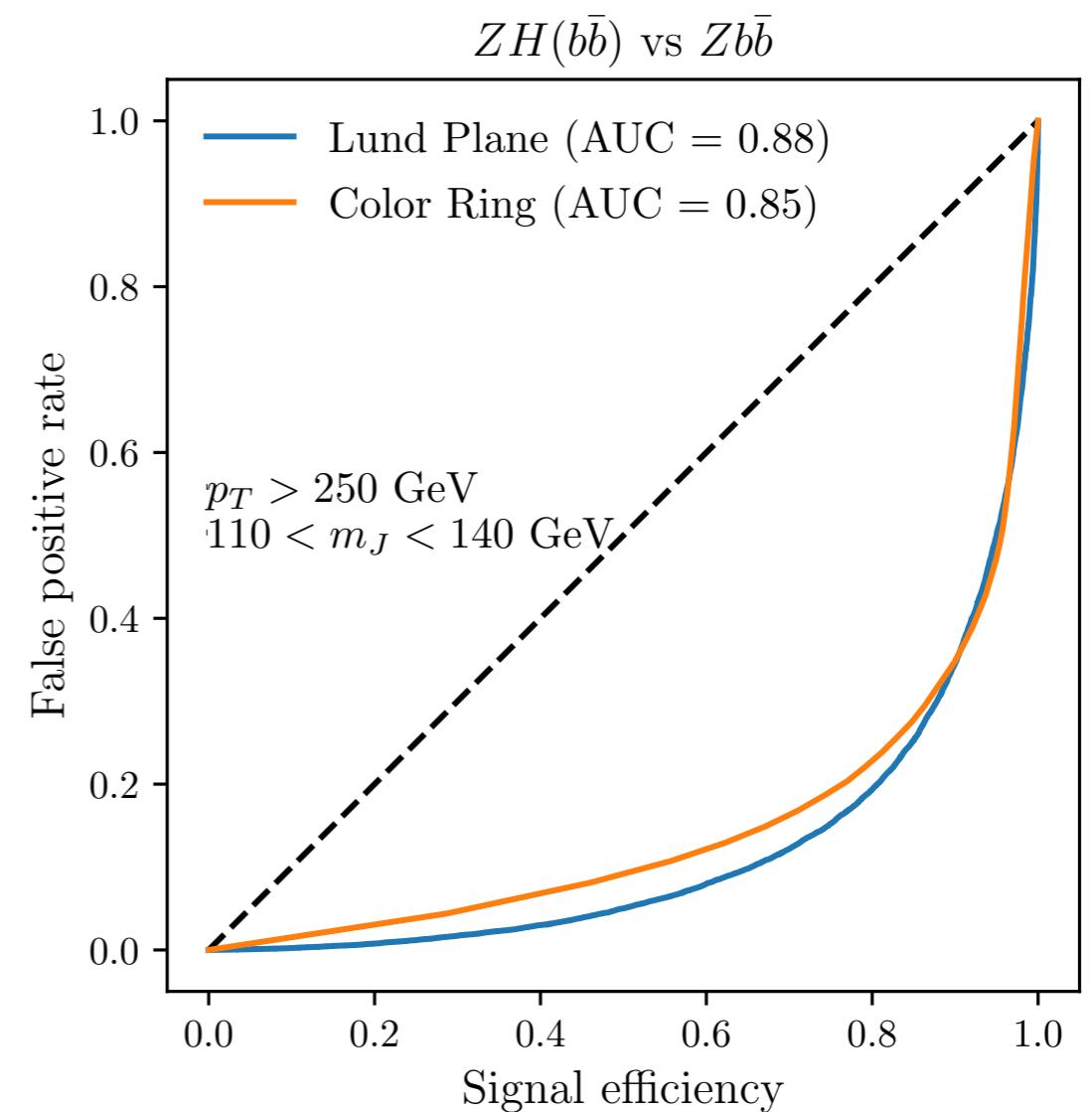
# CNN for Binary Classification



100K Events (balanced data)

Training: Validation:Test data= 60:20:20%

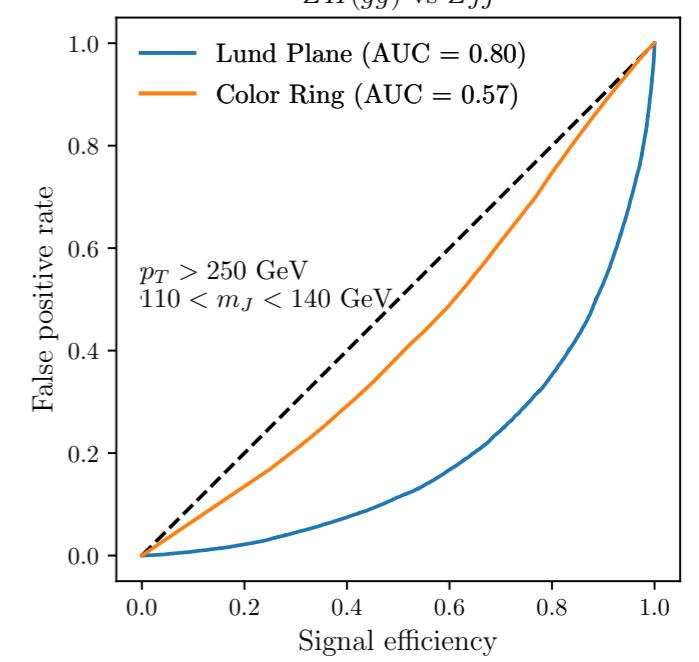
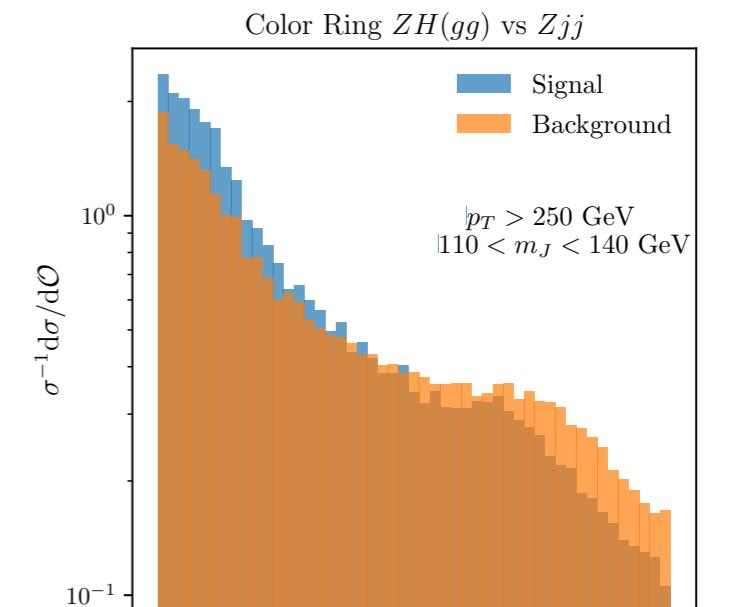
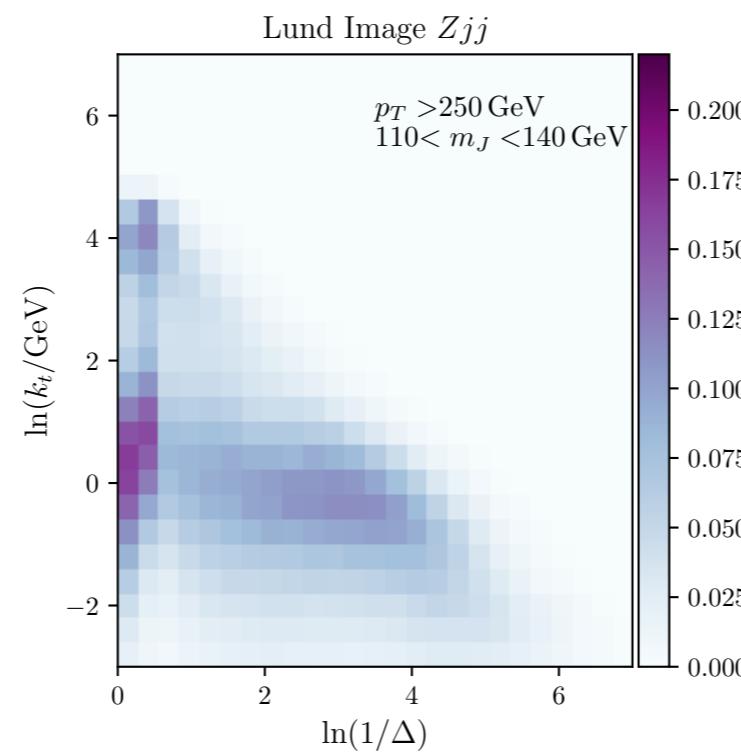
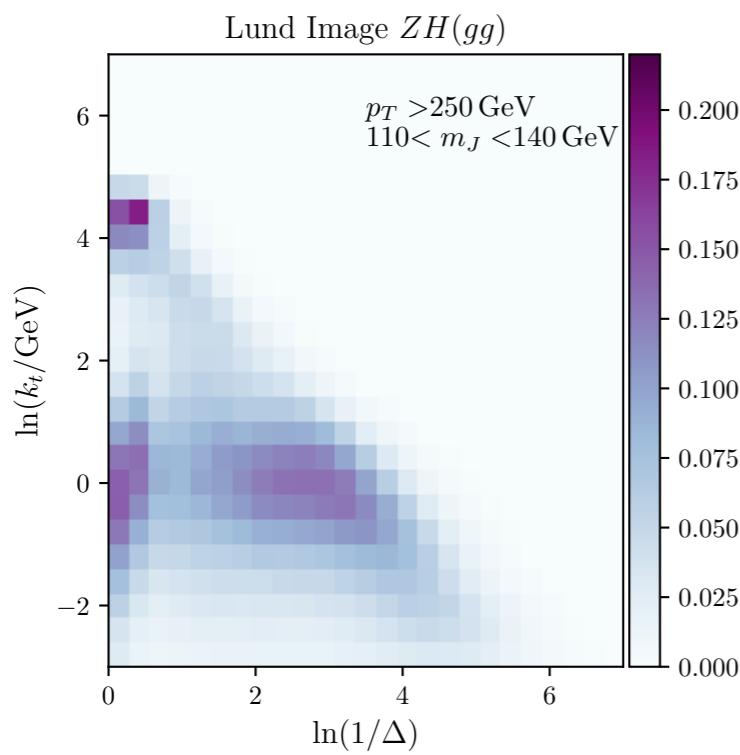
Cross-Entropy Loss function



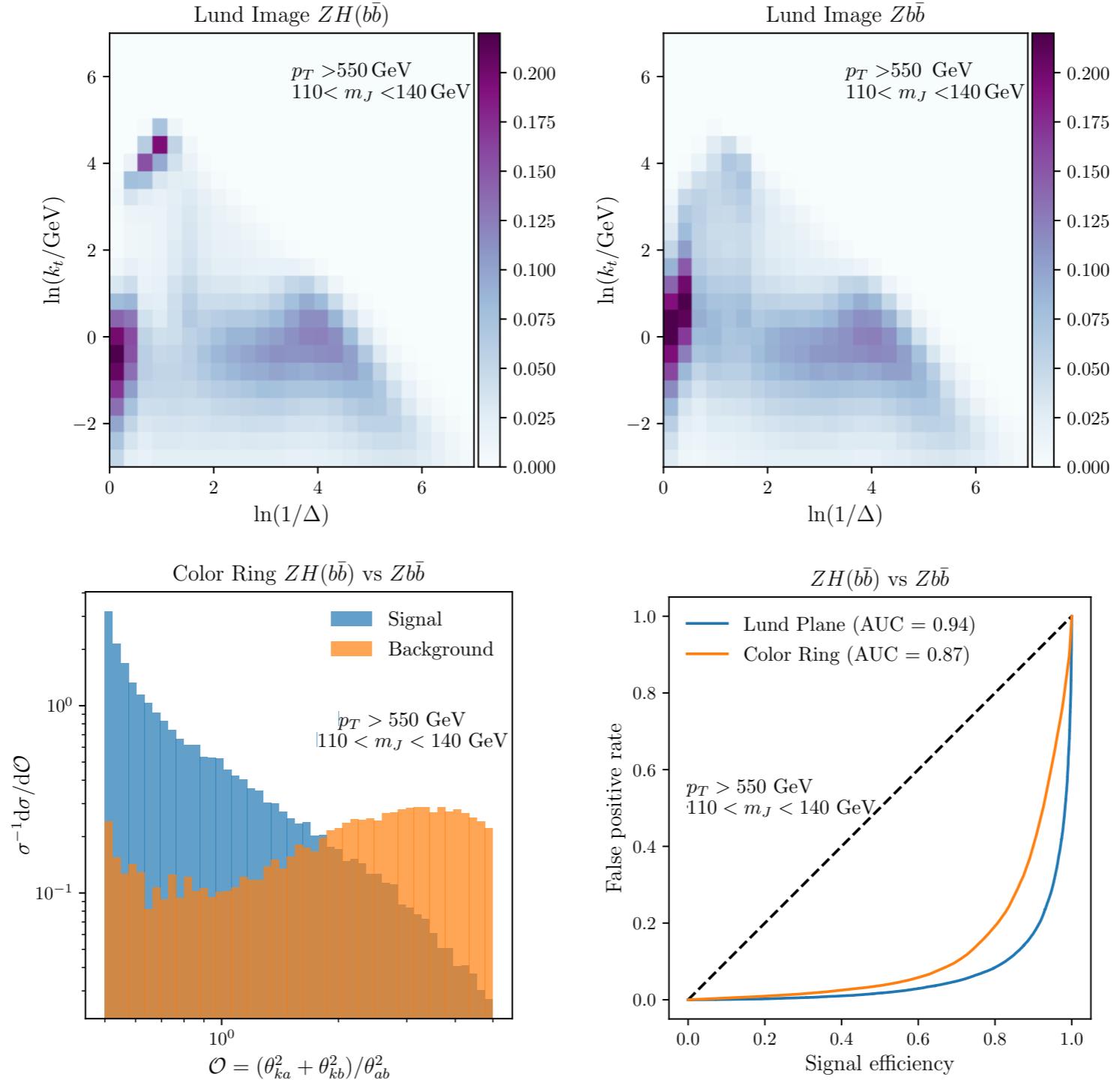
# $H \rightarrow gg$ Analysis

## Jet Color Ring:

- Signal distribution is the same as  $H \rightarrow b\bar{b}$  case.
- Several color configurations are contributing to the background.



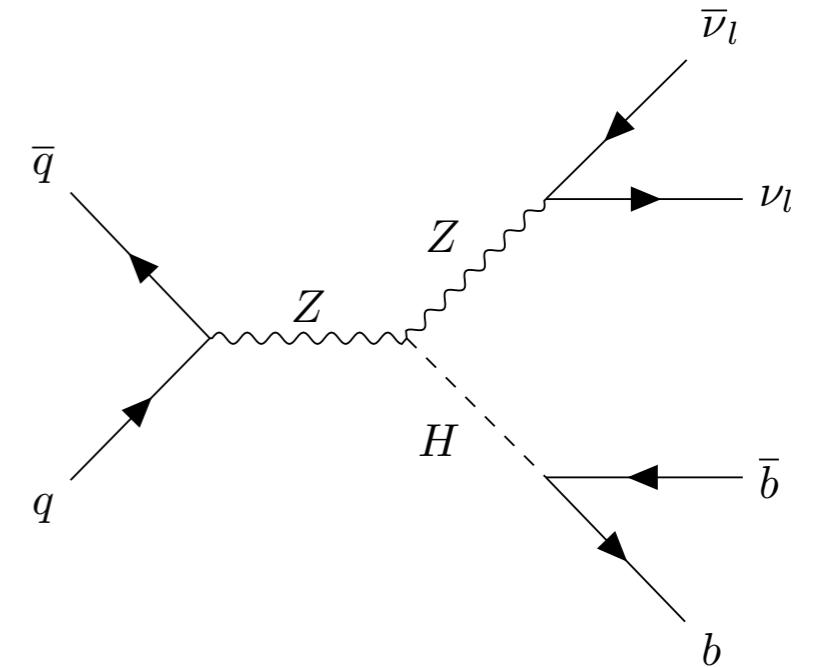
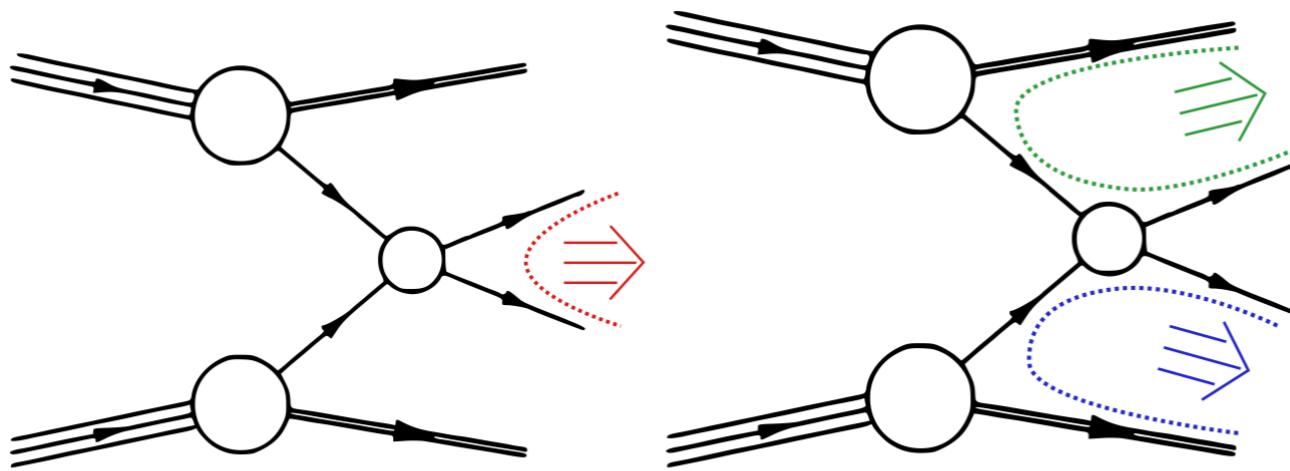
# High $p_T$ Scenario



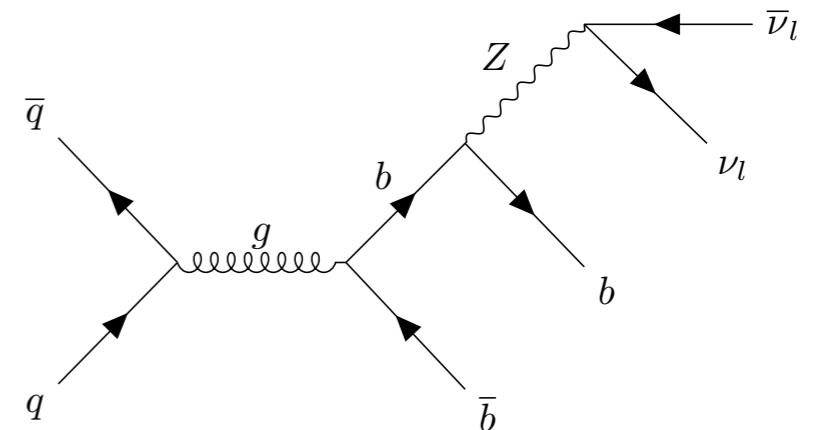
# Color sensitive observable and the Lund Jet Plane

L.Cavallini, A.Coccaro, CKK, G.Manco, S.Marzani, F.Parodi, D.Rebuzzzi, A.Rescia and G.Stagnitto,  
Eur. Phys. J. C 82 (2022) no.5, 493, [arXiv:2112.09650 [hep-ph]]

Jet pull and its projections,  $D_2$ , and color ring, Lund jet plane  
(Including detector effects)



Possible color connections for signal ( $pp \rightarrow H \rightarrow b\bar{b}$ ) and for the background ( $pp \rightarrow g \rightarrow b\bar{b}$ )



J. Gallicchio and M. D. Schwartz, Phys. Rev. Lett. 105 (2010), 022001.

# Jet Pull

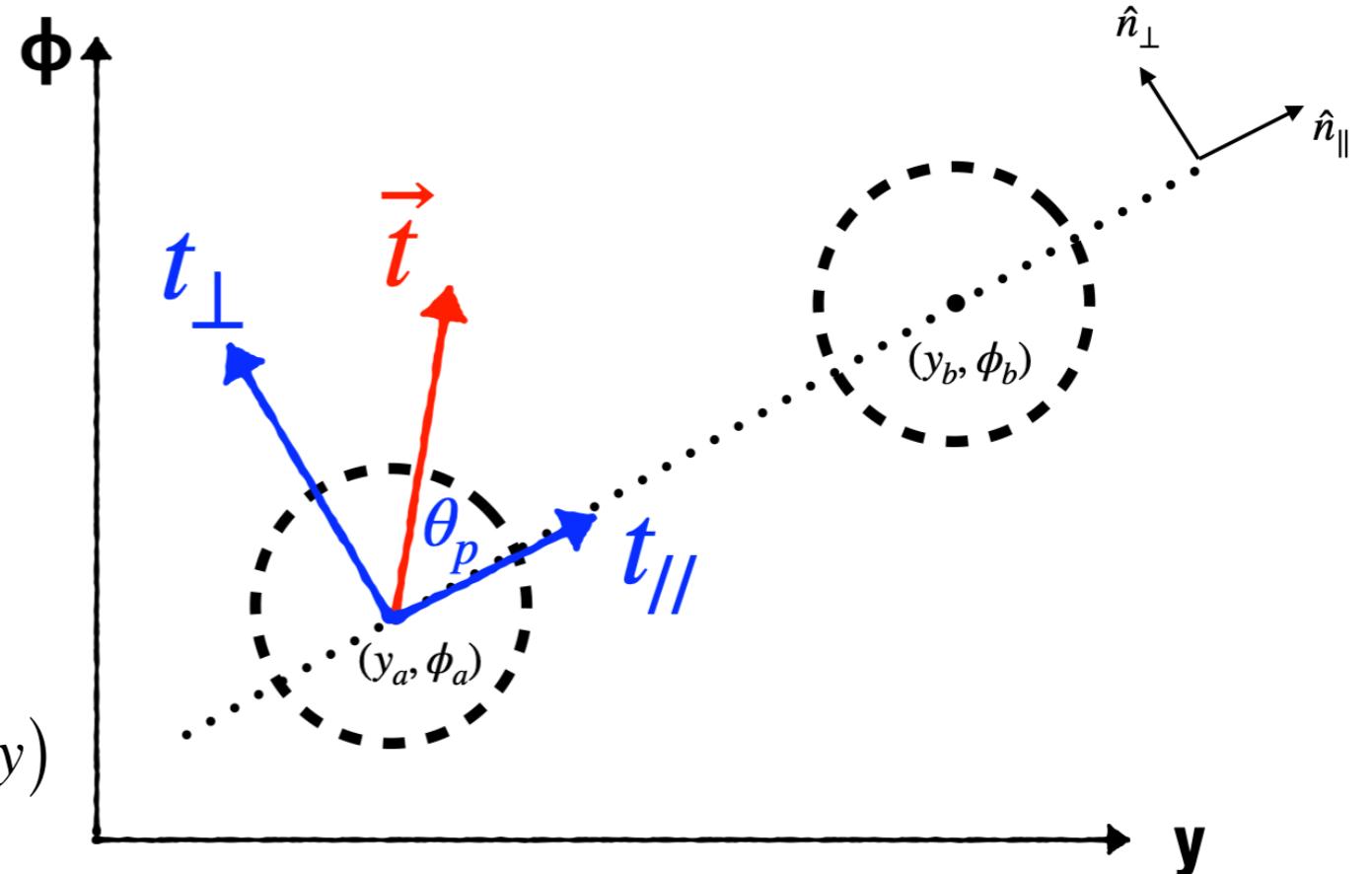
$$\vec{t} = \frac{1}{p_{Ta}} \sum_{i \in J_a} p_{Ti} |\vec{r}_i|^2 \hat{r}_i$$

$$\vec{r}_i = (y_i - y_a, \phi_i - \phi_a)$$

$$t_{\parallel} = \vec{t} \cdot \hat{n}_{\parallel}, \quad \hat{n}_{\parallel} = \frac{1}{\sqrt{\Delta y^2 + \Delta \phi^2}} (\Delta y, \Delta \phi)$$

$$t_{\perp} = \vec{t} \cdot \hat{n}_{\perp}, \quad \hat{n}_{\perp} = \frac{1}{\sqrt{\Delta y^2 + \Delta \phi^2}} (-\Delta \phi, \Delta y)$$

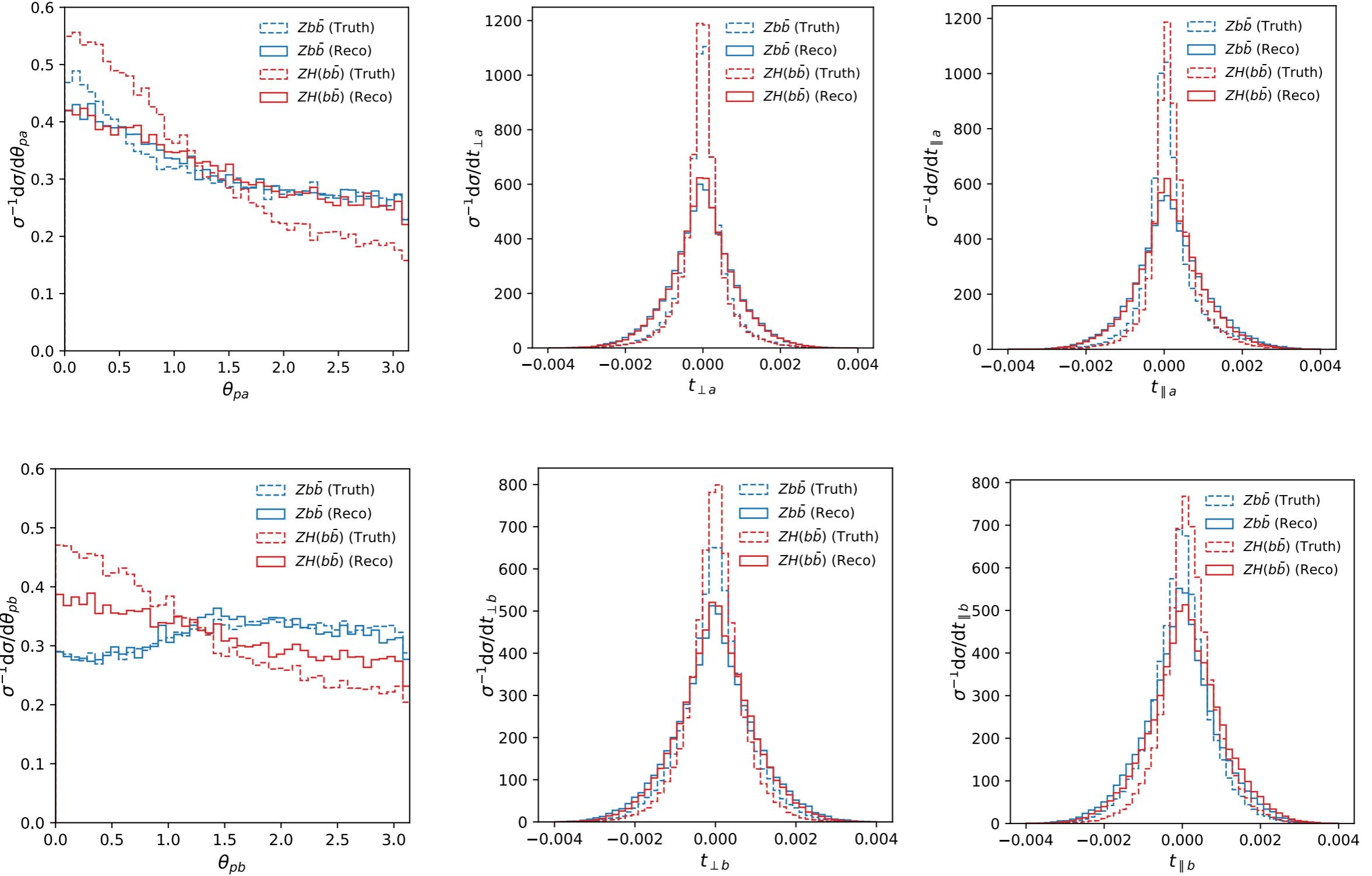
$$\theta_p = \arccos \frac{t_{\parallel}}{|\vec{t}|}$$



Pull vector components of jet  $J_a$

A. Larkoski, S.Marzani and C.Wu, JHEP 01 (2020), 104

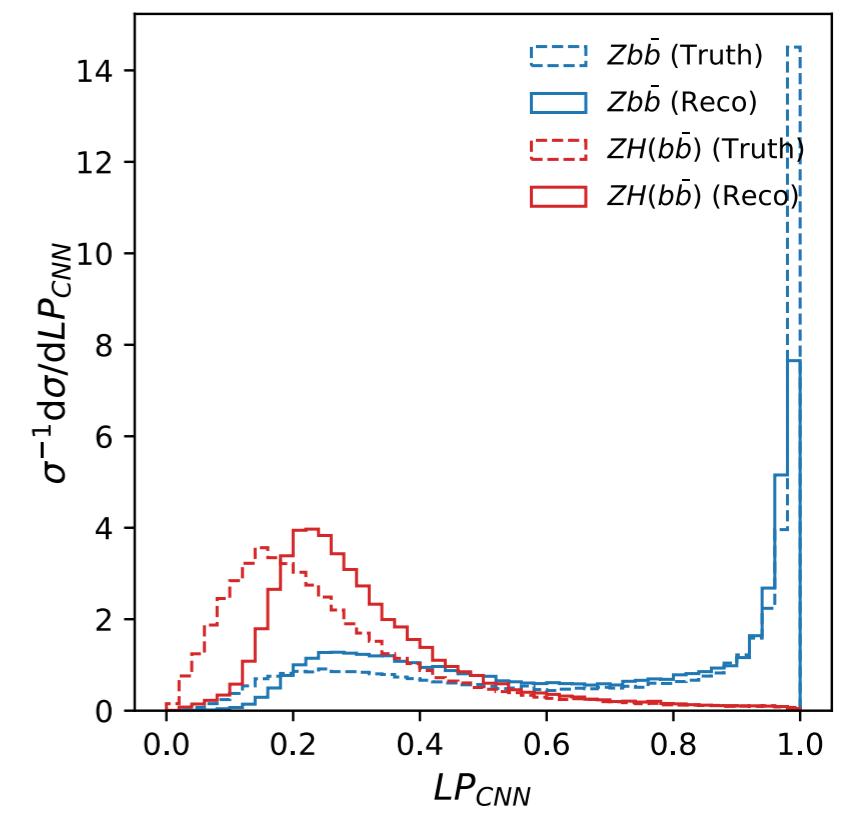
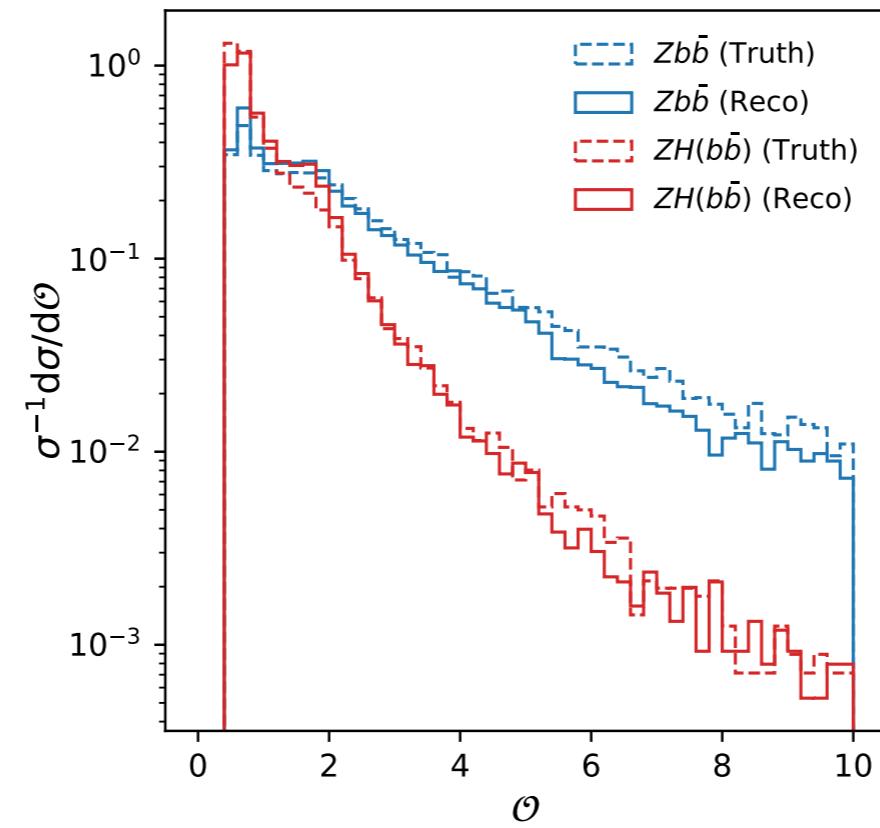
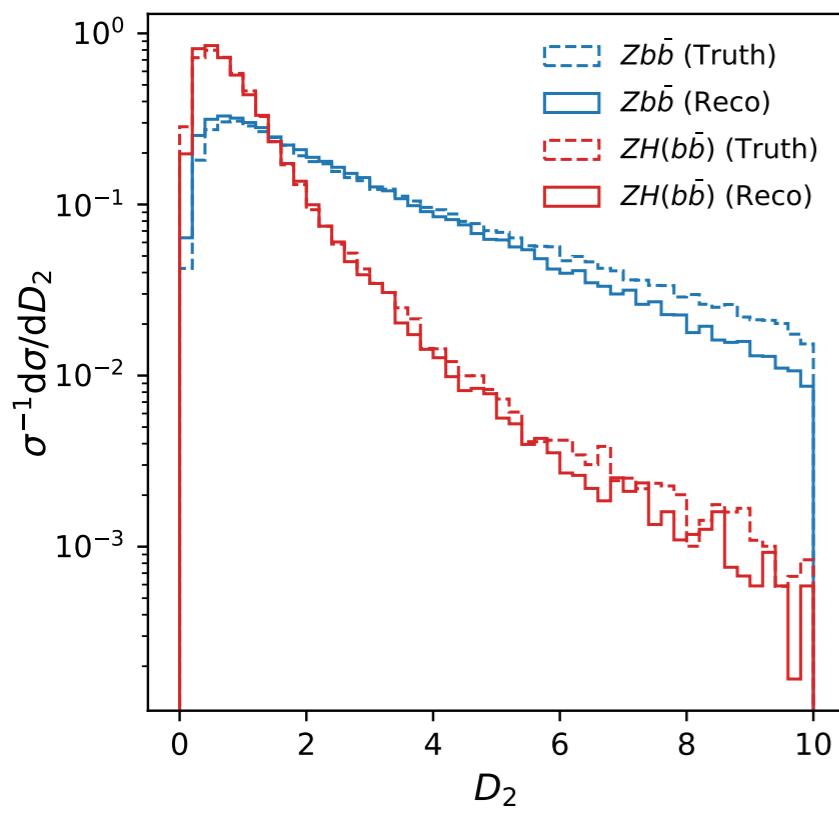
# Jet Pull and its projections



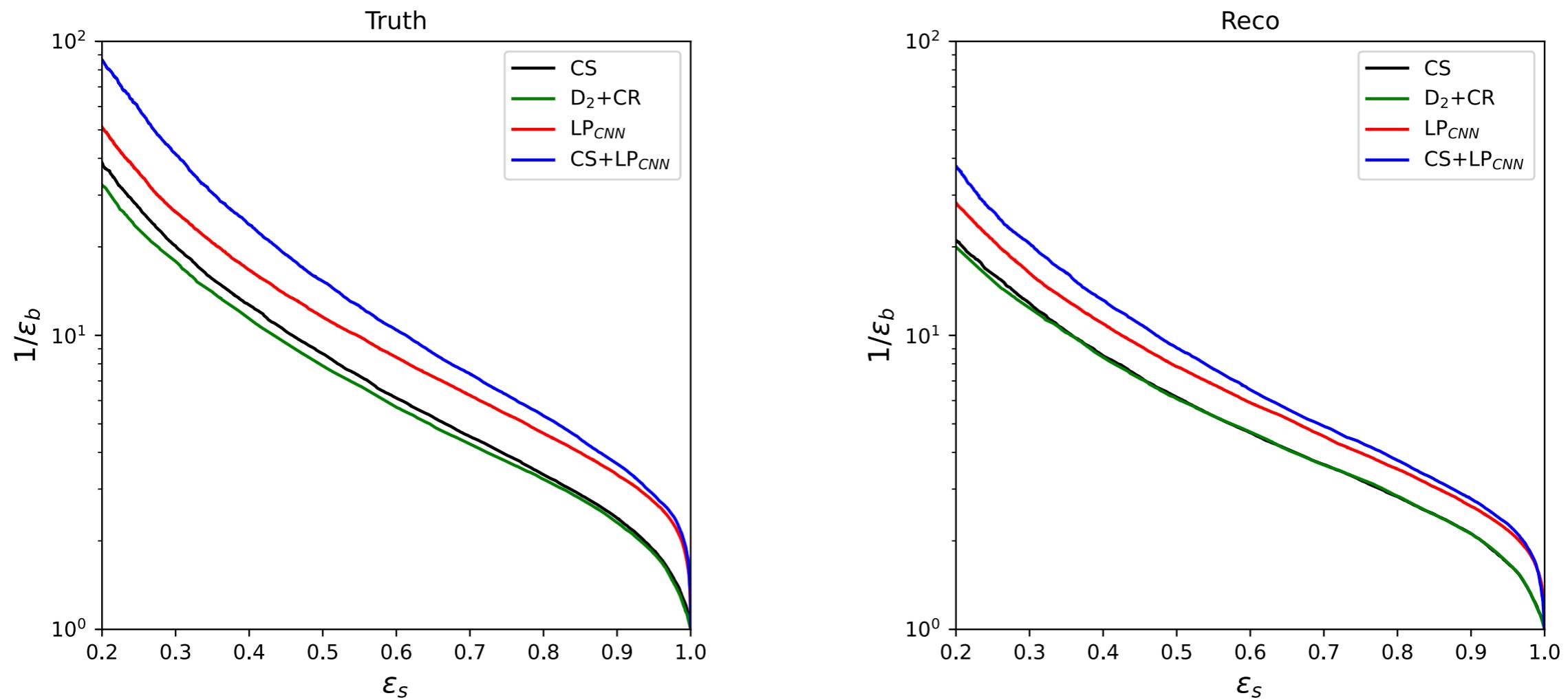
# $D_2$ and Jet Color Ring

$$D_2^{(\beta)} = \frac{e_3^{(\beta)}}{(e_2^{(\beta)})^3}$$

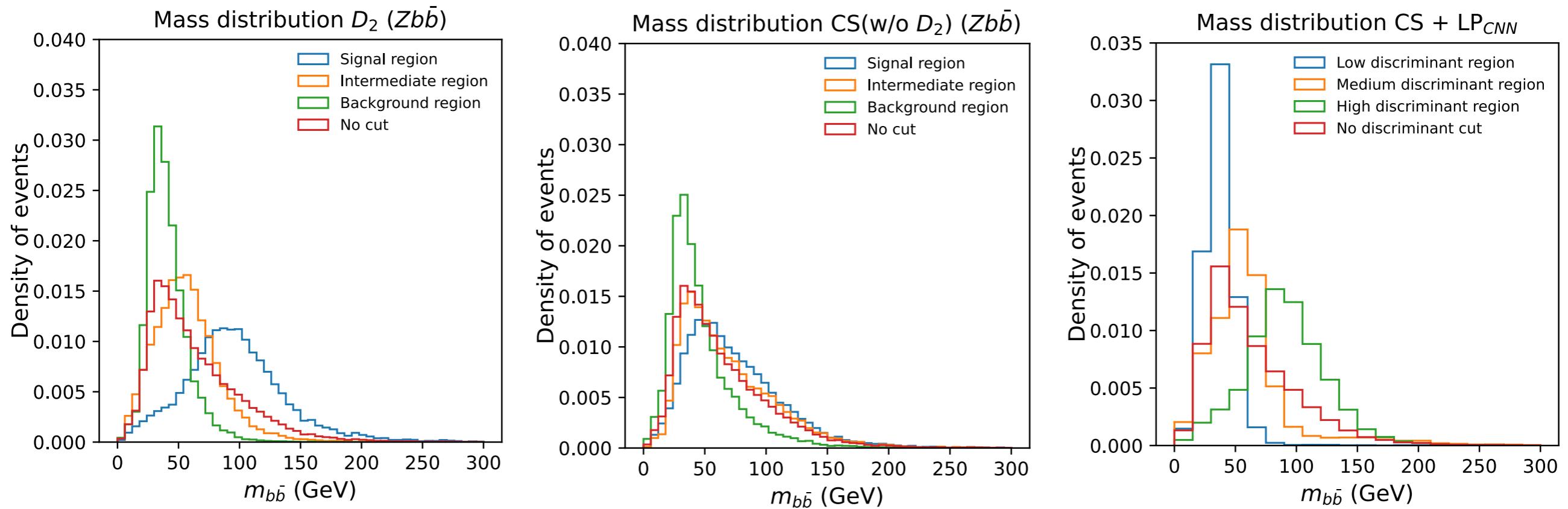
$e_n^{(\beta)}$  is the normalized n-point energy correlation functions



# Discrimination Performance

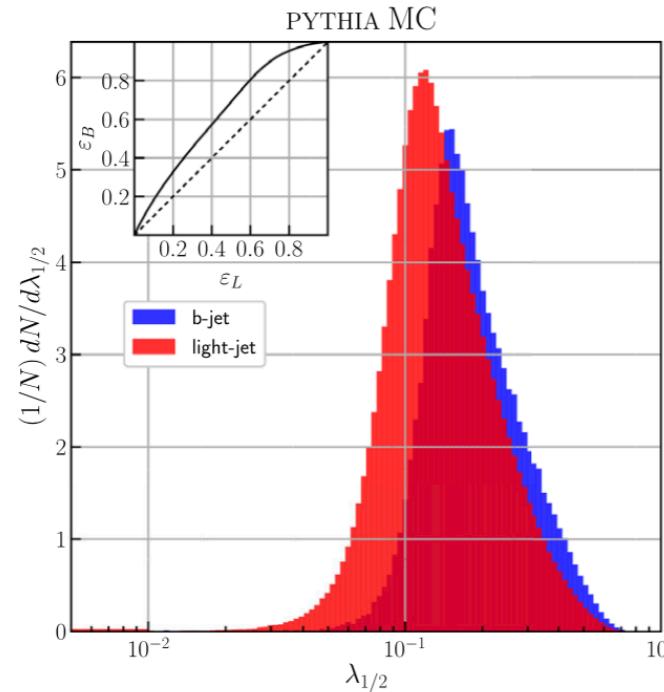


# Invariant Mass Dependence

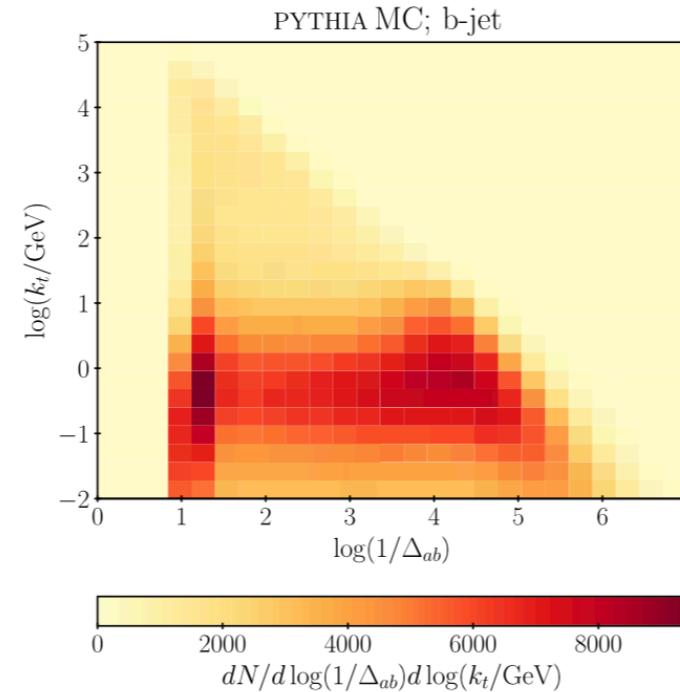


Background distribution of different ranges of classifier output.

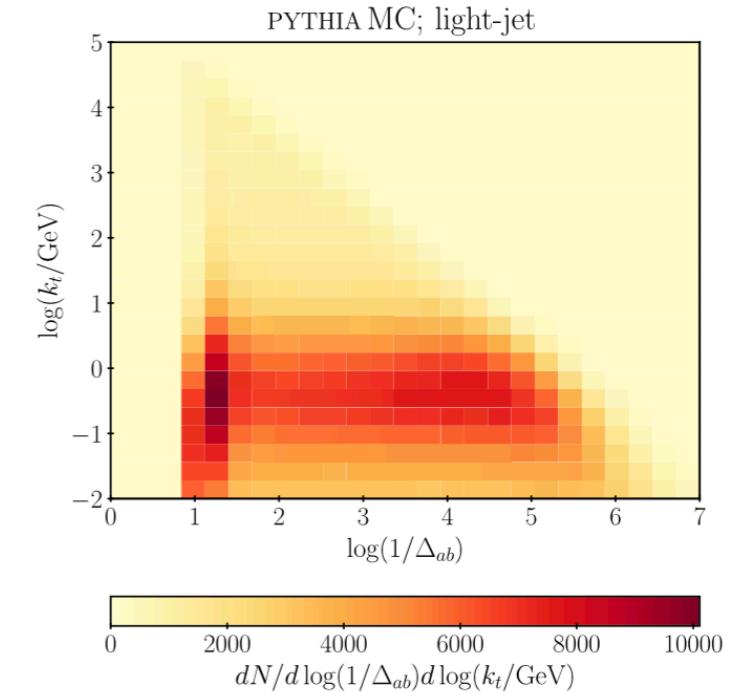
# Identification of b-jets



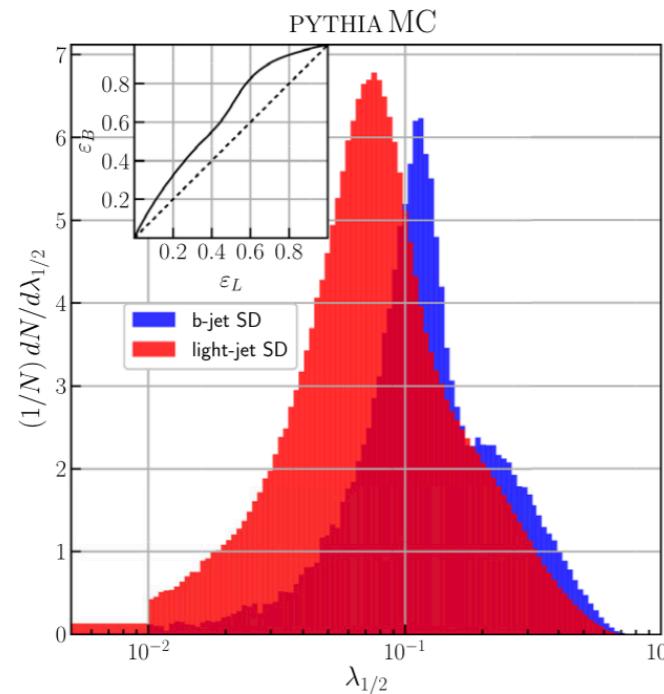
(a)



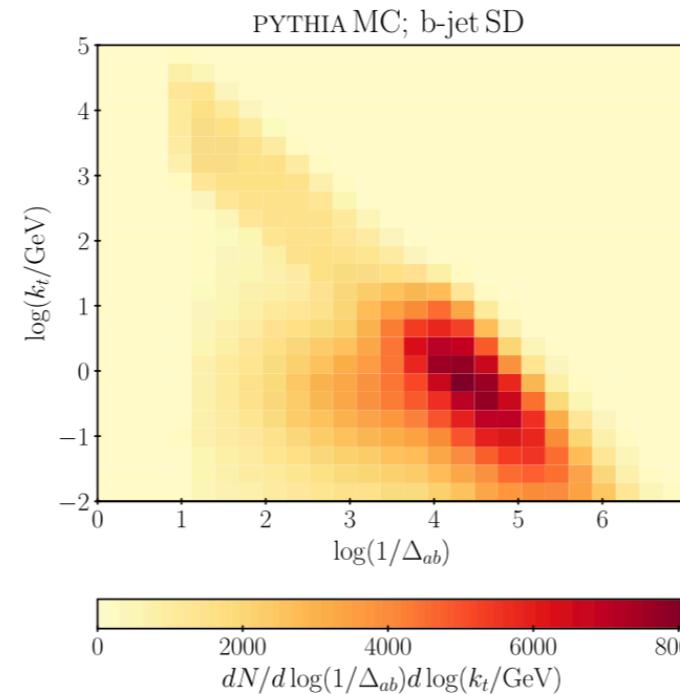
(b)



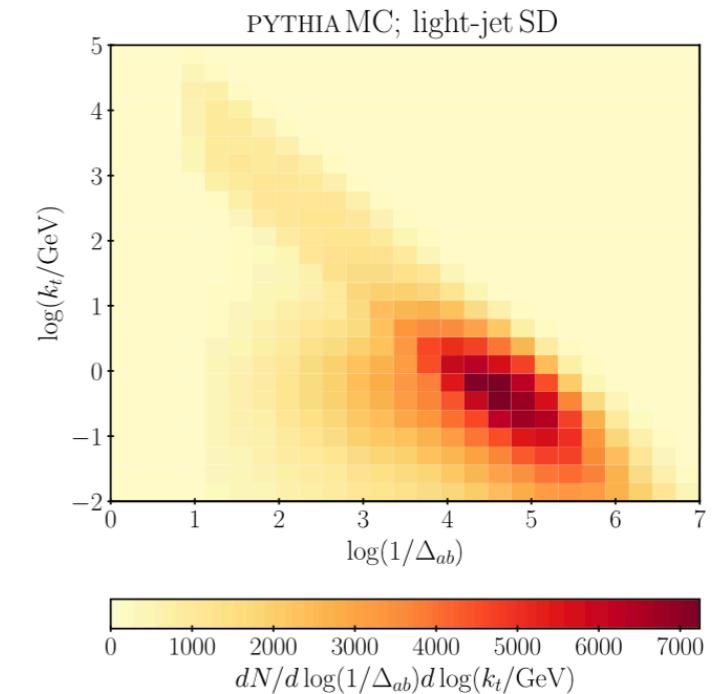
(c)



(d)



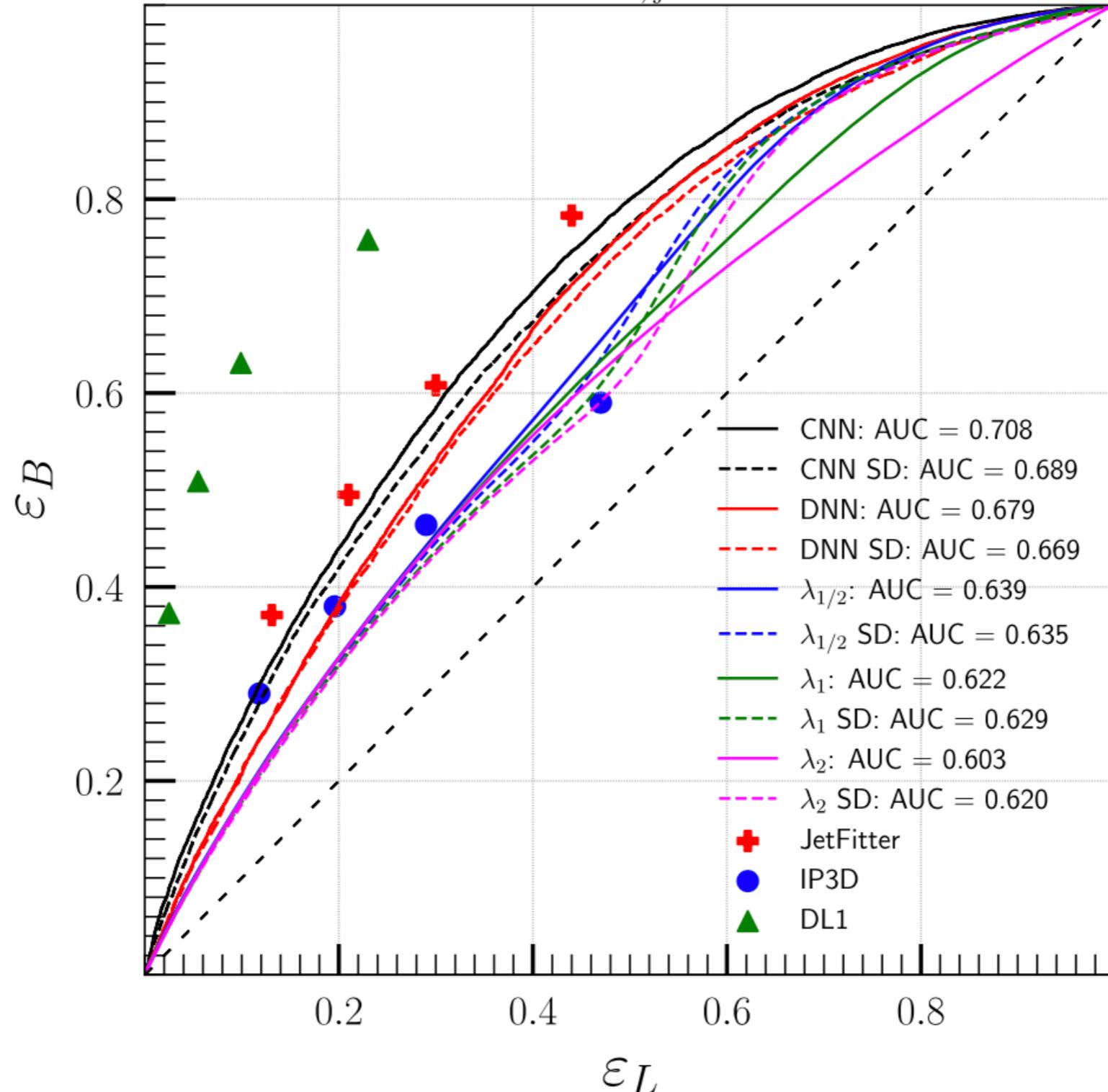
(e)



(f)

# Identification of b-jets

PYTHIA MC;  $p_{T,\text{jet}} > 500 \text{ GeV}$



# Effect of b-mass in the Lund Jet Plane

Ongoing work by

Francesco Giuli, Alberto Rescia, Federico Sforza

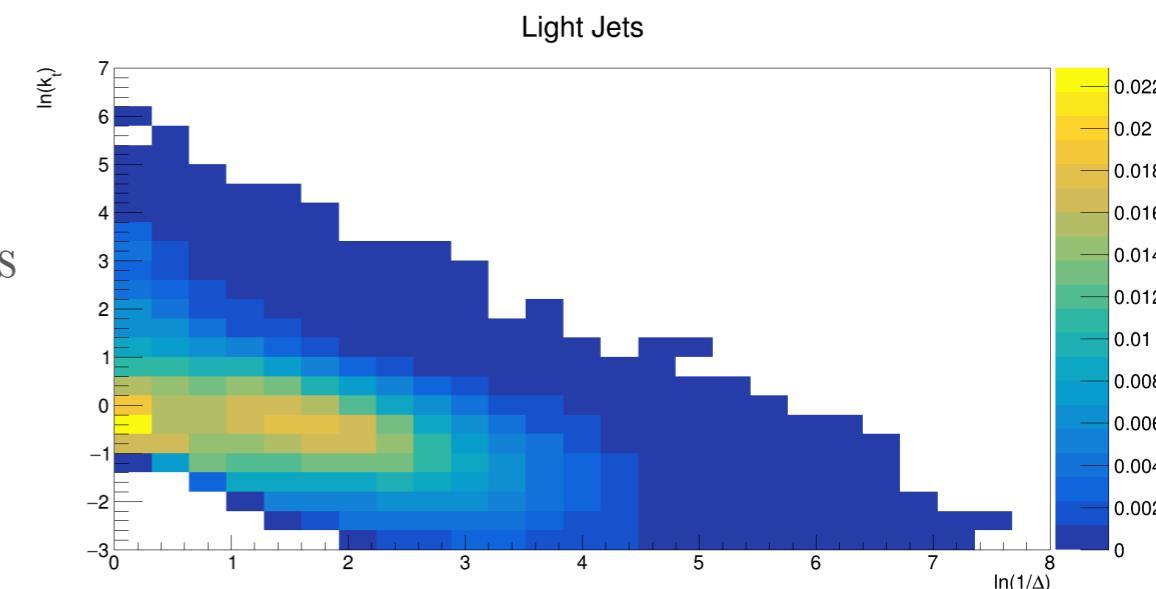
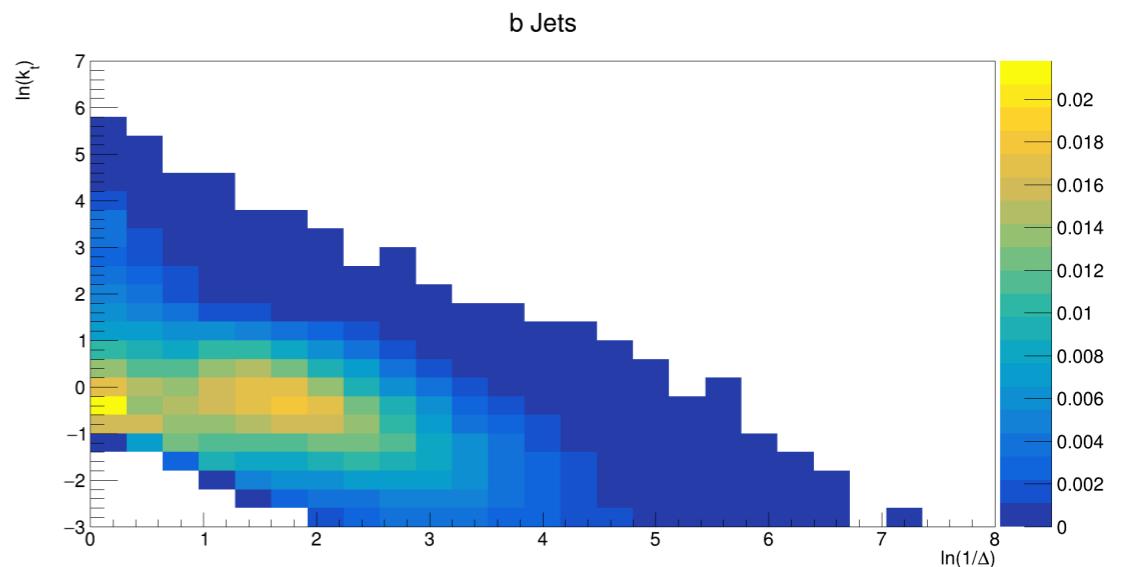
- Generate b & light jet events w/ MG5@NLO-Delta (v3.5.0)
  - $Z(l^+l^-) + j$  final state at NLO in 5FS for light events
  - $Z(l^+l^-) + bb$  with NLO in 4FS for b events
  - No kinematic cuts at generator level
- Shower with Pythia8 v8.309

Analyse at truth-level with a dedicated Rivet routine

- **Lepton cuts:**
  - $p_T > 27 \text{ GeV}$ ,  $|\eta| < 2.5$  and dilepton mass between 76-106 GeV
  - Isolation criterion: discard if  $\Delta R < 0.4$  from jets
- **Jets:**

**Cluster final state hadrons into  $R = 0.4$  jets with  $p_T > 20 \text{ GeV}$  and  $|\eta| < 2.5$**

  - Tag jets as b or light via ghost-matching
  - Require 2 tagged jets in final state

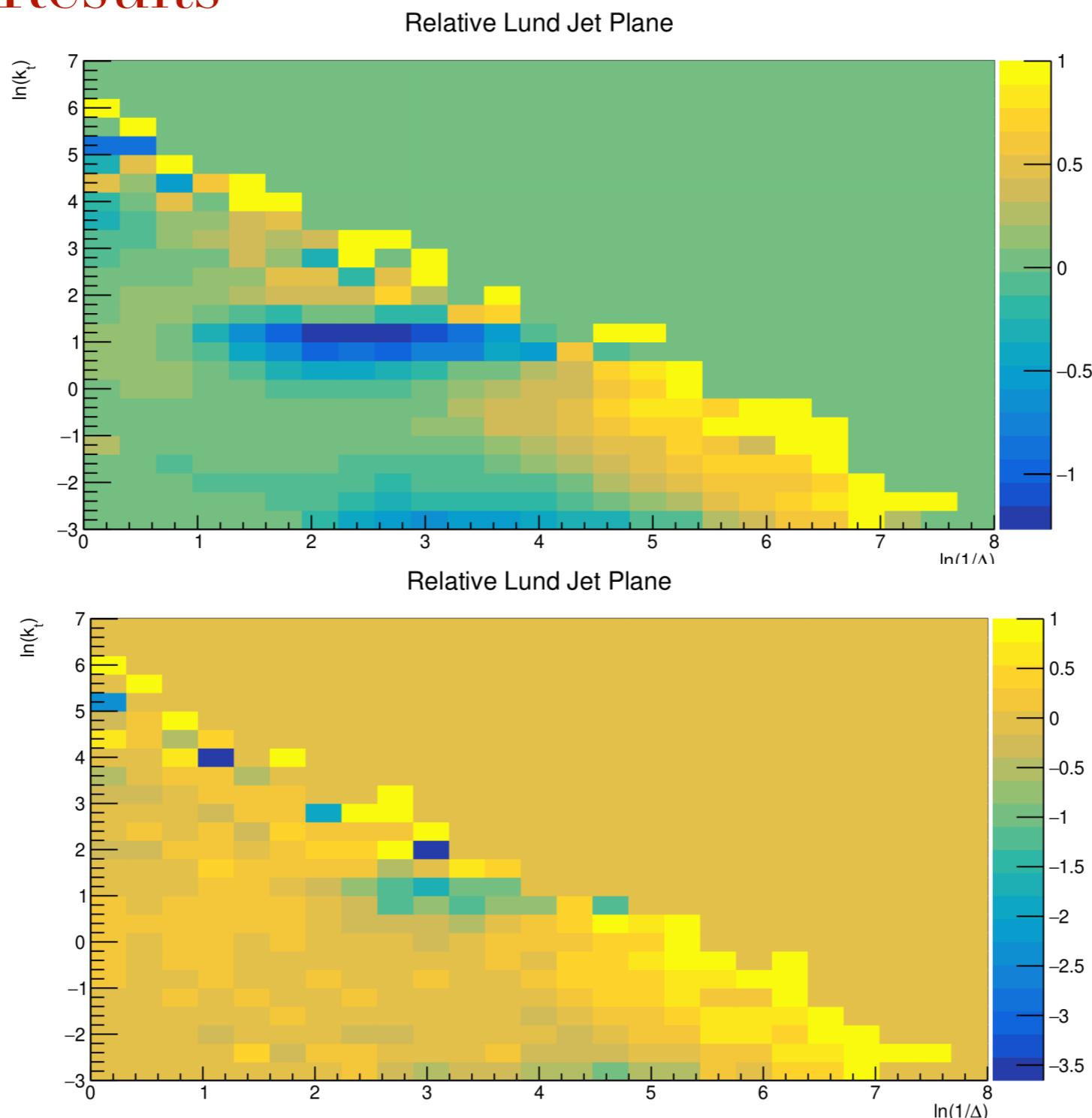


# Effect of b-mass in the Lund Jet Plane

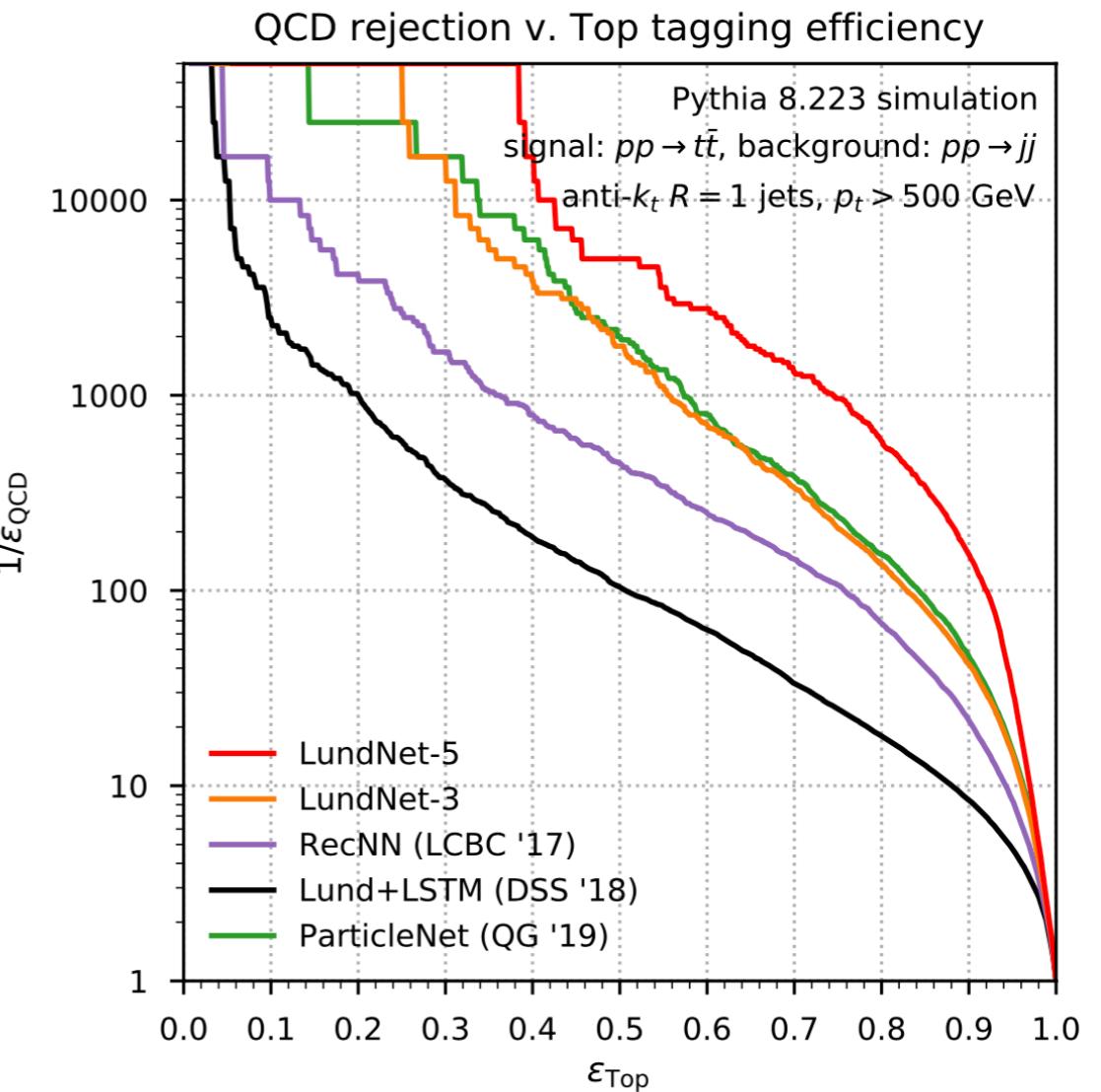
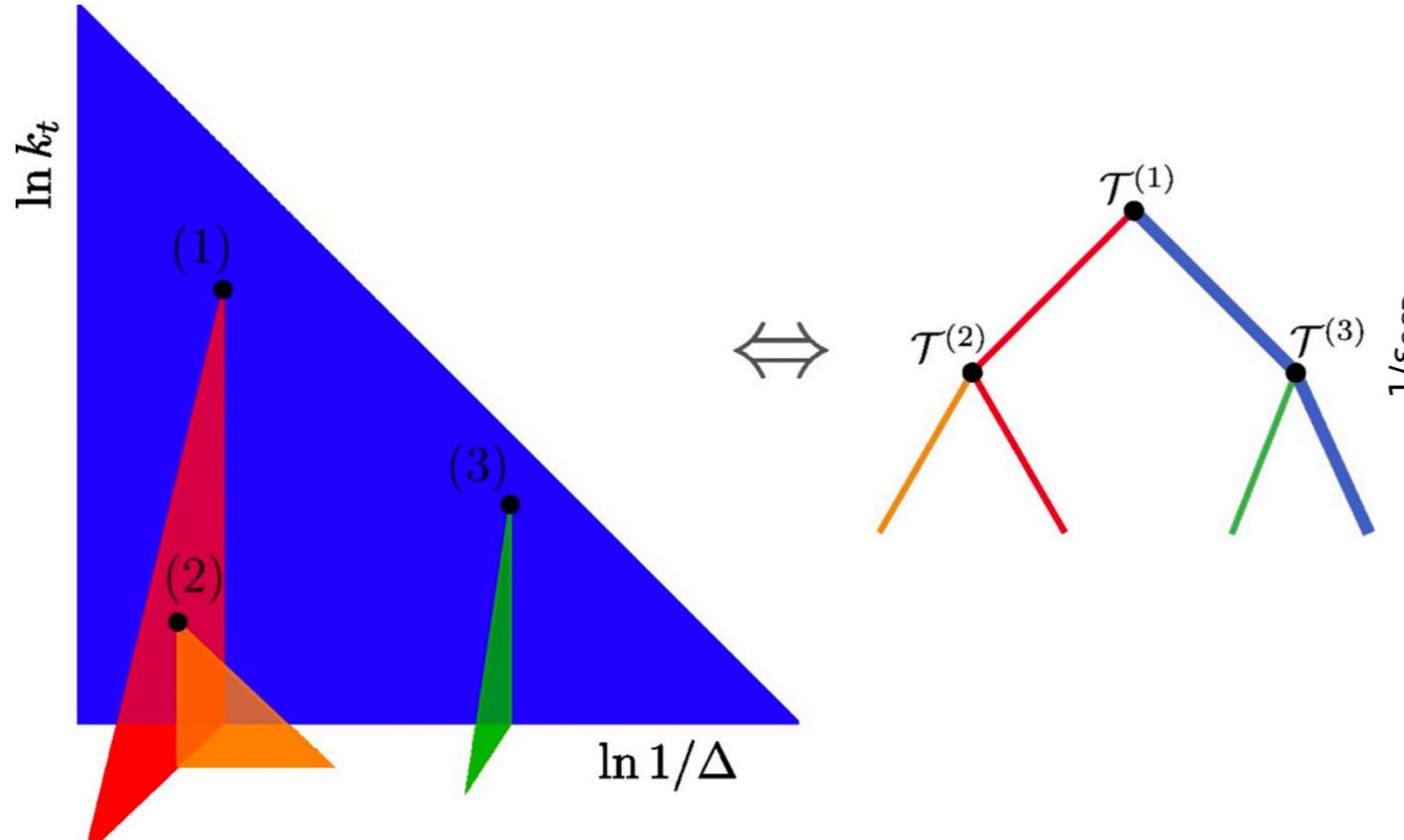
## Ongoing work by

Francesco Giuli, Alberto Rescia, Federico Sforza

## Preliminary Results



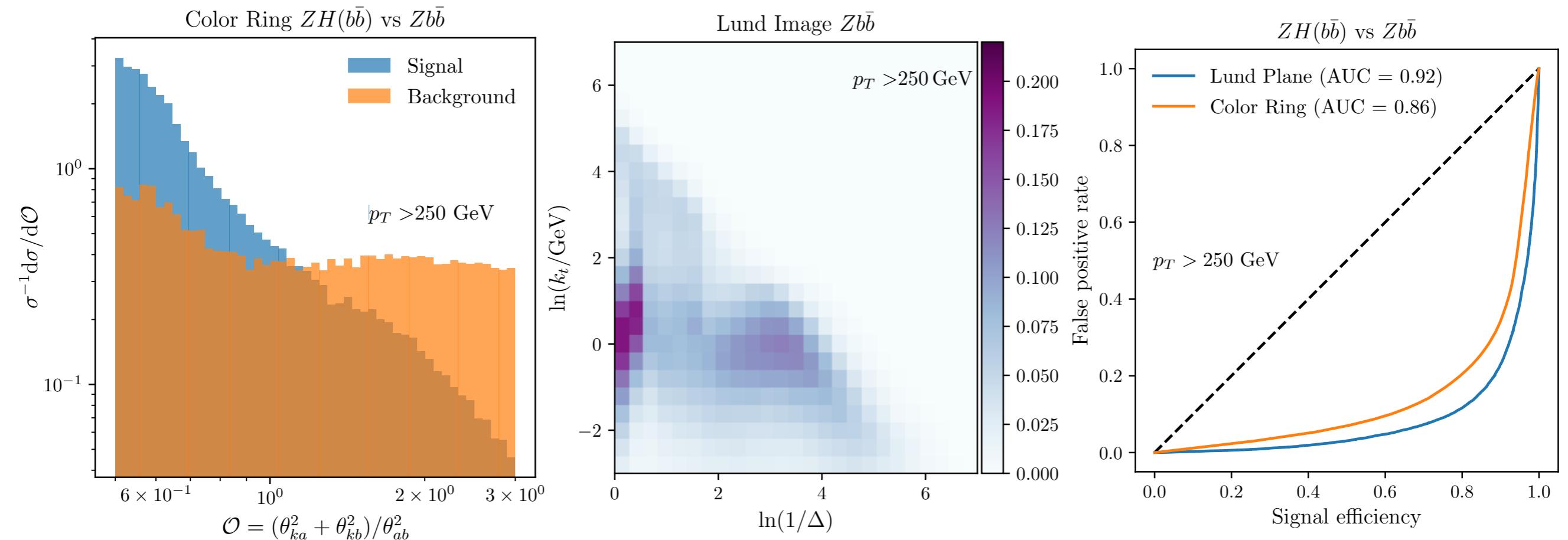
# LundNet for Top Tagging



# Summary and Outlook

- In this talk, we discussed how Lund Jet Plane and machine learning techniques can be used for jet tagging.
- We are using color-sensitive observables and a primary Lund jet plane for the Higgs tagging.
- Other studies also considered more complex architectures like graph neural networks for boosted jet tagging.
- A comparison of these techniques for the same benchmark will be useful for their implementation in the experimental analysis.

# Tagger Without Jet Mass Cut



Mass unspecified tagger using color information rather than prong multiplicities