

Challenges of Stringy de Sitter and Asymptotic Acceleration

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based on work with [Simon Schreyer and Gerben Venken](#)

(cf. also earlier work with [Xin Gao/Junghans](#) and [Xin Gao/Schreyer/Venken](#))

Outline

- **Reminder:** Need for de Sitter / Singular-Bulk Problem of KKLT / LVS Parametric Tadpole Constraint.
- Curvature Corrections for Anti-D3 in Warped Throat: Fundamental Problem or Blessing in Disguise?
- The real thing: Curvature Corrections for NS5.
- Asymptotic Acceleration without de Sitter?

The construction of controlled dS in String Theory remains a key challenge

.....as emphasised e.g. in

... Danielsson/Van Riet; Obied/Ooguri/Spodyneiko/Vafa '18 ...

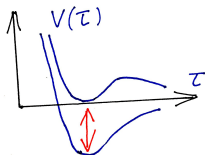
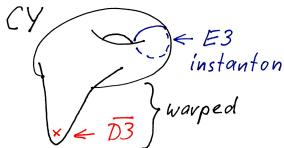
- Quintessence is certainly an alternative, but technically it runs into similar (or worse) problems....

cf. Cicoli/Pedro/Tasinato '12 AH/Skrzypek/Wittner '19

- Thus, the paradigmatic approach of 'AdS-minimum' plus 'Uplift' appears to remain the main road towards controlled dS models.

The former flagship model KKLT appears to be in trouble....

- Reminder:



- The dS vacuum relies on the competition of two small quantities:

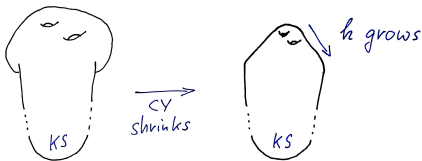
$$V_{AdS} \sim \exp(-\tau) \quad \text{and} \quad V_{up} \sim \exp(-N/g_s M^2)$$

This matching implies that
the throat can not be parametrically smaller than the bulk....

Carta/Moritz/Westphal '19

Control problem of KKLT:

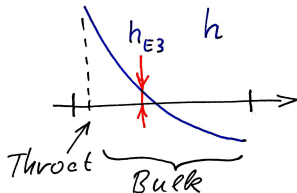
- As a result, strong warping sets in already in the bulk:



- This implies the (potentially deadly) 'singular bulk problem':

Gao/AH/Junghans '20

$$ds_{10}^2 = h(y)^{-1/2} \eta_{\mu\nu} dx^\mu dx^\nu + h(y)^{1/2} \tilde{g}_{mn} dy^m dy^n$$



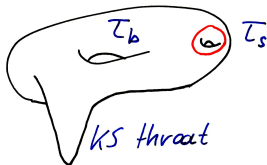
(see however Carta/Moritz, Demirtas et al. '21)

Control problem also for LVS?

- The LVS is naively safe since the volume $\mathcal{V} \sim \tau_b^{3/2}$ is exponentially large:

$$\tau_s \sim \xi^{2/3}/g_s \quad , \quad \mathcal{V} \sim \exp \tau_s$$

- However, the combination of several constraints may nevertheless lead to control problems



Junghans '22

- The key constraint of bulk curvature corrections may be overcome using a large D3-tadpole:

→ LVS Parametric Tadpole Constraint

Gao/AH/Schreyer/Venken '22

The LVS Parametric Tadpole Constraint:

-explicitly, the bound on the required neg. D3-tadpole reads:

$$|Q_3| > N = N_* \left(\frac{1}{3} \ln N_* + \frac{5}{3} \ln c_N + 8.2 + \dots \right),$$

$$\text{with } N_* \equiv \frac{9g_s M^2}{16\pi} \sim \frac{g_s M^2}{5}.$$

and with $c_N \gg 1$ controlling bulk curvature corrections.

(For $g_s M^2$, metastability bounds of $12 \dots 46$ have been discussed. See e.g. KPV, Bena et al., Blumenhagen et al. Scalisi et al., Lüst/Randall '22)

- Optimistically, rather modest bounds of $N \sim 40$ follow. However, things are really more complicated....

Curvature Corrections affecting the $\overline{D3}$

- As correctly emphasised by Junghans, $\overline{D3}$ curvature corrections tend to strengthen the PTC:

$$V_{\overline{D3}} = \frac{\mu_3}{g_s} [1 - R_{10}(\overline{D3})^2] = \frac{\mu_3}{g_s} \left[1 - \frac{c}{(g_s M)^2} \right]$$

with $c = 5.92$.

Junghans '22 (2nd paper), cf. also AH/Schreyer/Venken '22

- To control this corrections, one needs sizeable $g_s M$.

Together with the KPV-bound $1/M < 0.08$, this drives the **key parameter** $g_s M^2$ to larger values.

D3 Curvature Corrections – a Blessing in Disguise?

AH/Schreyer/Venken '22

- However, the uplift potential

$$V_{\text{D3}} h_{\text{tip}}^{-1} \sim \frac{\mu_3}{g_s} \left[1 - \frac{c}{(g_s M)^2} \right] e^{-N/g_s M^2}$$

does not suffer phenomenologically if $[1 - c/(g_s M)^2] \rightarrow 0$.

On the contrary!

- One must only avoid $(g_s M)^2 < c$, since then the uplift is lost.
- Thus, allowing even for all higher-order corrections, i.e.

$$[1 - c/(g_s M)^2] \rightarrow [1 - \Delta_{\text{curv}}(g_s M)],$$

there are two logical possibilities:

Possibility A:

- $[1 - \Delta_{\text{curv}}(g_s M)]$ remains positive even for not so large $g_s M$.
- Then curvature corrections only renormalise the uplift.
- The overall consistency of the LVS (in particular the PTC) is **not affected** significantly.

Possibility B:

- For some $g_s M$, the factor $[1 - \Delta_{\text{curv}}(g_s M)]$ changes sign.
- Then, by continuity, one can find an appropriate (integer) M and some highly tuned value of g_s such that

$[1 - \Delta_{\text{curv}}(g_s M)]$ becomes extremely small.

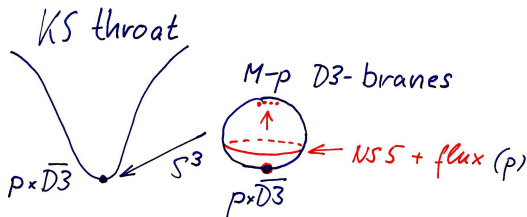
- Thus, trusting the power of landscape tuning of g_s , we can have exponentially small $\overline{D3}$ uplift without deep throats!

...however, the full truth is much more complicated:

NS5-brane curvature corrections

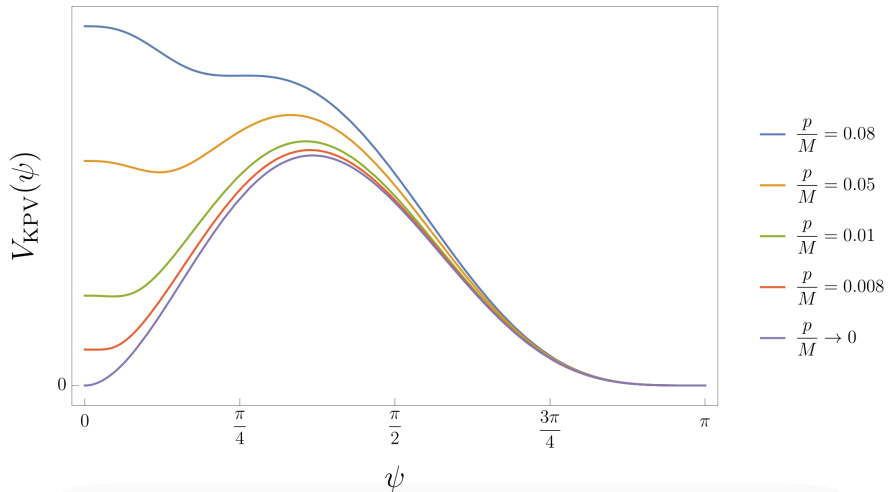
AH/Schreyer/Venken '22; Schreyer/Venken '22

- The $\overline{D3}$ has well-known 'KPV' NS5-brane decay channel:



- The curvature at the tip is controlled by $g_s M$, in particular $R_{S^3} \sim \sqrt{g_s M}$.
- At small $g_s M$, a key concern are NS5-brane curvature corrections and the stability of the KPV-potential!

Reminder of KPV potential (with ψ the NS5-brane altitude)



- Dp curvature corrections known.

Symbolically:

Bachas/Bain/Green '99; Junghans/Shiu '14

$$-\frac{1}{g_s} \int_{Dp} \sqrt{g + \mathcal{F}} (1 - \alpha'^2 R^2)$$

(Here ' R^2 ' stands for various contractions of 10d Riemann tensor and 2nd fundamental form of Dp -hypersurface.)

- For $D3$, which is $SL(2, \mathbb{Z})$ invariant, the all-orders g_s dependence is 'known':

$$\frac{1}{g_s} \alpha'^2 R^2 \rightarrow E_1(S, \bar{S}) \alpha'^2 R^2 \quad (S = C_0 + \frac{i}{g_s})$$

- Based on the fact that a fluxed $D5$ with geometry $\mathbb{R}^{1,3} \times S^2$ gives a $D3$ in the shrinking S^2 -limit, we conjecture:

The $E_1(S, \bar{S})$ prefactor also appears for $D5s$.

- Thus, we write for the D5

$$-\frac{1}{g_s} \int_{D5} \sqrt{g + \mathcal{F}} \left(1 - E_1(S, \bar{S}) \alpha'^2 R^2 \right),$$

and S-dualize ($g_s \rightarrow 1/g_s$),

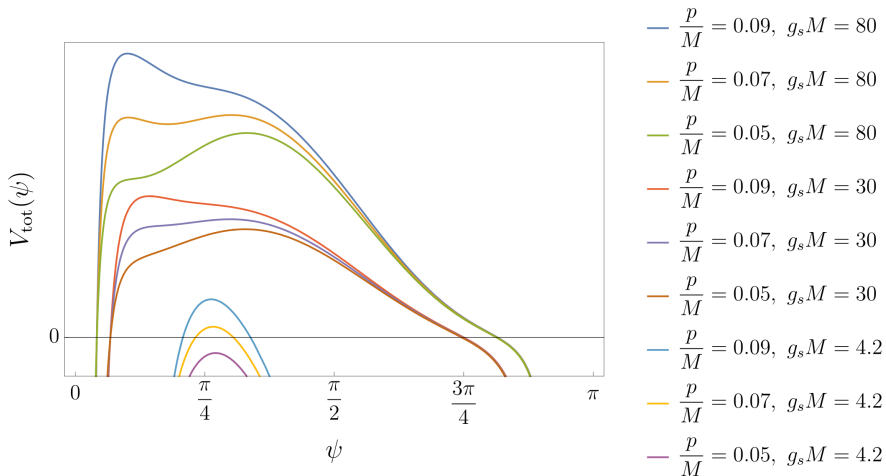
using also $E_1(S, \bar{S}) \sim g_s$ at large g_s , to find:

$$S_{NS5} \sim -\frac{1}{g_s^2} \int_{D5} \sqrt{g + \mathcal{F}} \left(1 - \alpha'^2 R^2 \right)$$

- This result (or conjecture) is consistent with the expectation that, also for a fluxed NS5 on $\mathbb{R}^{1,3} \times S^2$, one expects to get a D3 in the shrinking S^2 -limit.

Note: Could also use S-dual setting and D5 rather than NS5 (cf. Gautason/Schillo/Van Riet '16), but conclusions not better.

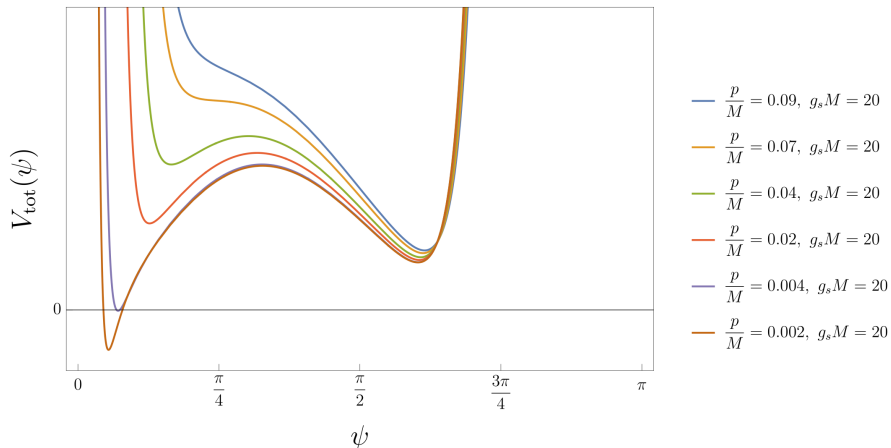
Curvature-corrected KPV potential



Note the **very large** $g_s M$ -value needed for a metastable minimum and the **still large** value needed for a positive barrier!

Curvature and higher-order-flux-corrected KPV potential

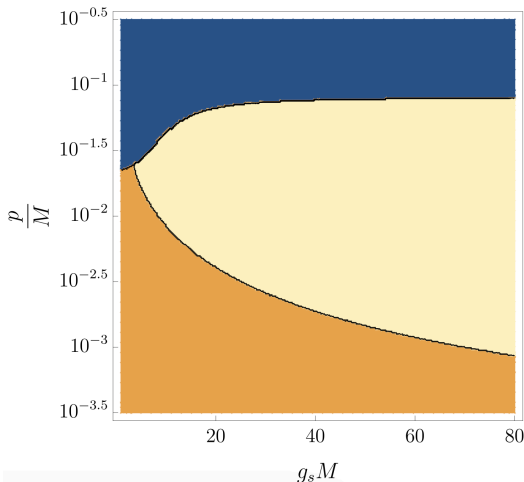
Schreyer/Venken '22 (using results of Robbins/Wang, Garousi, Babaei/Jalali)



Note: One can now actually see, also using the NS5-brane, that the SUSY-breaking minimum falls below zero (\rightarrow weak-warping uplift).

Curvature and higher-order-flux-corrected KPV potential

Schreyer/Venken '22 (using results of Robbins/Wang, Garousi, Babaei/Jalali)



Optimal
(borderline):

$$g_s M \simeq 3.6$$
$$p/M = 1/40$$

Yellow: Metastable minimum exists; Blue: No metastable minimum;
Orange: Metastable minimum at negative energy.

Impact on: LVS parametric tadpole constraint:

- It is now more useful to take $g_s M$ rather than $g_s M^2$ as the basic control parameter of the throat:

$$|Q_3| > N = \frac{2^{8/3} \kappa_s^{2/3} (g_s M)^2}{2\pi^2 \xi^{2/3}} \left(\frac{1}{4} \ln g_s M + \frac{5}{8} \ln c_N + 3.04 + \dots \right)^2.$$

- Choosing $g_s M = 3.8$, $c_N = 5$, $\kappa_s = 0.1$ (this is optimistic!), one finds $N \simeq 560$.
- Recent best value: $Q_3 = -252$. \Rightarrow potential problem!
Crino/Quevedo/Schachner/Valandro '22

(Larger $|Q_3|$ values in models with 'Whitney branes' or generic F-theory geometries have their own control problems.....)

For more see parallel talk by S. Schreyer.

Cosmological Acceleration at the Asymptotics of Field Space

(possibly without de Sitter):

Ooguri/Palti/Shiu/Vafa; AH/Wrase '18; Grimm/Li/Valenzuela '19;
Bedroya/Vafa; Rudelius '21; Shiu/Tonioni/Tran '23;
van de Heisteeg/Vafa/Wiesner/Wu '23

- A key motivation: Possibly, getting metastable de Sitter is so hard because **cosmological horizons** are fundamentally sick.
- So let's focus on getting cosmological horizons in the simplest way, maybe based on

$$V \sim e^{-\gamma\varphi} \quad \text{at} \quad \varphi \rightarrow \infty \quad \text{with} \quad \gamma < \gamma_{\text{acc}} \equiv \frac{2}{\sqrt{d-2}}.$$

- If we succeed, we will earn the right to be more optimistic about **(poorly controlled) metastable dS models**.

Asymptotic Acceleration (continued)

AH/Schreyer/Venken, to appear today!

Conjecture ('Asymptotic Acc. Implies dS' or 'AA \Rightarrow dS'):

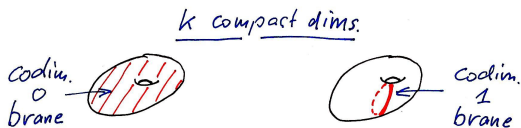
Accelerated expansion at the asymptotics of field space in d dimensions is only possible on the basis of a **compactification of a metastable $(d + k)$ -dimensional dS vacuum.**

Argument:

- All (relevant) asymptotics are decompactification limits.
Based on 'Emergent String', Lee/Lerche/Weigand '18
- Analyse energy sources in k -dimensional compact space.
- Leaders: Branes with **codim. 0** (i.e. C.C.) and **codim. 1**.
- Observe:

$$\gamma_{\text{codim. 0}} < \gamma_{\text{acc}} < \gamma_{\text{codim. 1}} \cdot$$

Asymptotic Acceleration – explicitly....



$$\gamma_{\text{codim. 0}} < \gamma_{\text{acc}} < \gamma_{\text{codim. 1}}$$

$$\frac{\gamma_{\text{codim. 0}}}{\gamma_{\text{acc}}} < 1 < \frac{\gamma_{\text{codim. 1}}}{\gamma_{\text{acc}}}$$

$$\sqrt{\frac{k}{k+d-2}} < 1 < \frac{k+d/2-1}{\sqrt{k(k+d-2)}}$$

For more see parallel talk by G. Venken.

Summary / Conclusions

- KKLT has fundamental problems ('Singular Bulk'); LVS faces quantitative issues ('Parametric Tadp. Constraint').
- Things could be much better if strong curvature drives uplift-energy to zero! (cf. our new, finely tuned uplift.)
- In any case, analysing KPV with NS5-brane curvature corrections appears to be *the* way forward.

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- One may hope to establish asymptotic acceleration rather than dS, to prove that nothing is wrong with cosmic horizons.
 - However, we argue (conjecture) that: 'AA \Rightarrow dS'.

For exciting new results concerning Kinetic Mixing and Cobordism in the Landscape cf. parallel talks by R. Küspert and B. Friedrich.