

# Higher( $s > 2$ ) spin and parity from galaxies

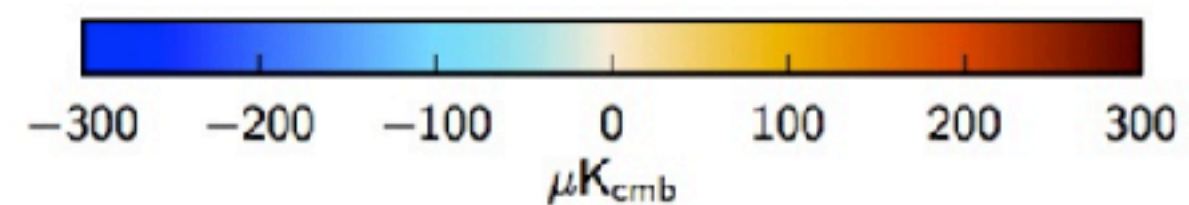
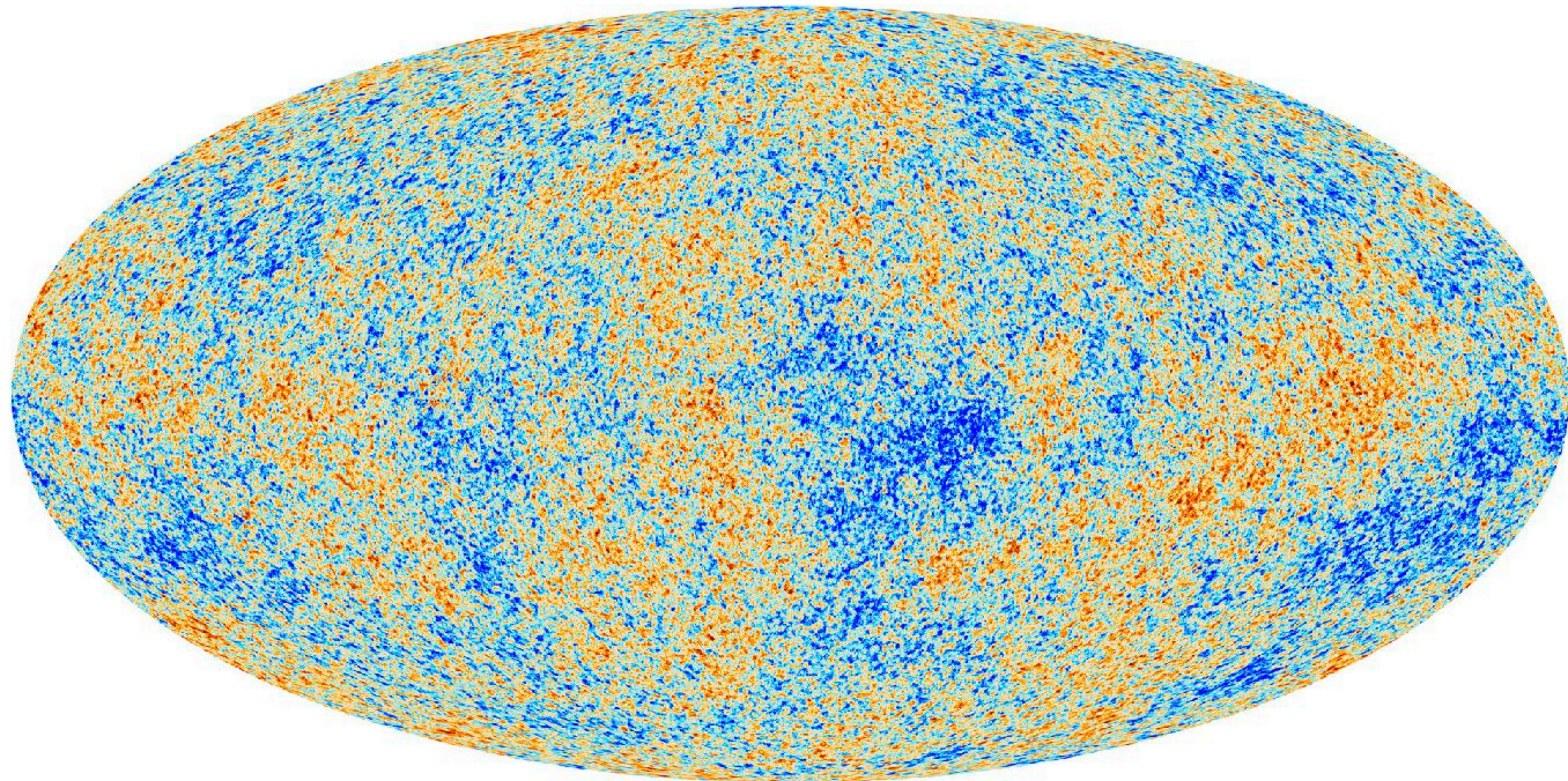
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String Phone 2023

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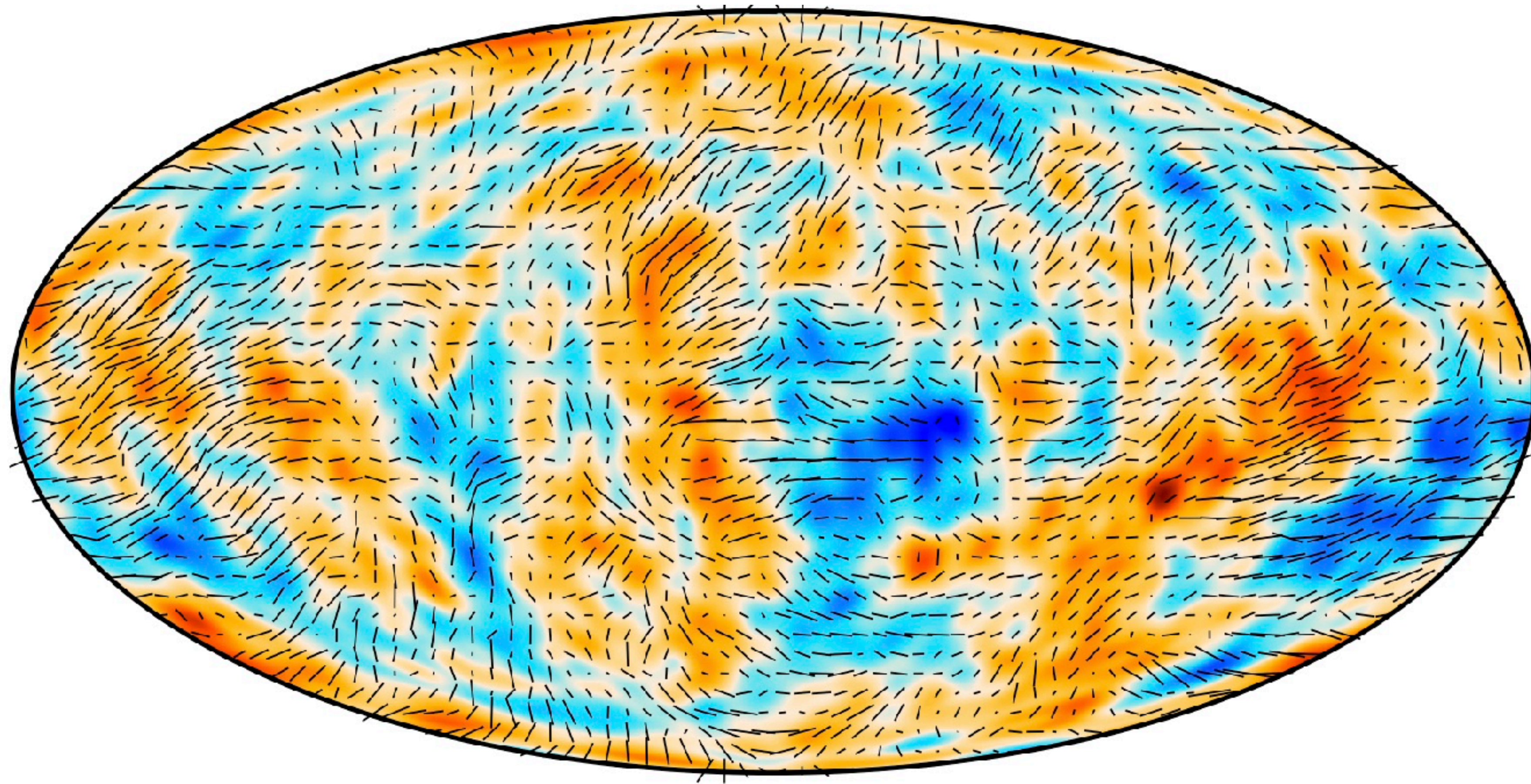
# Temperature map of the CMB



maximum likelihood posterior map  
Planck Collaboration



# Polarization map of the CMB



0.41  $\mu\text{K}$

-160

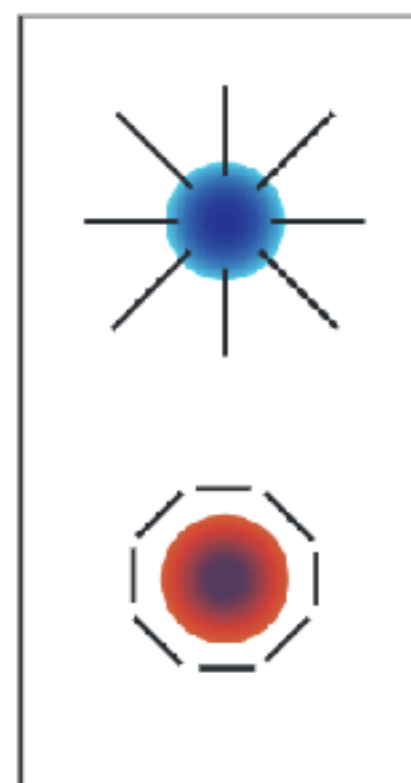
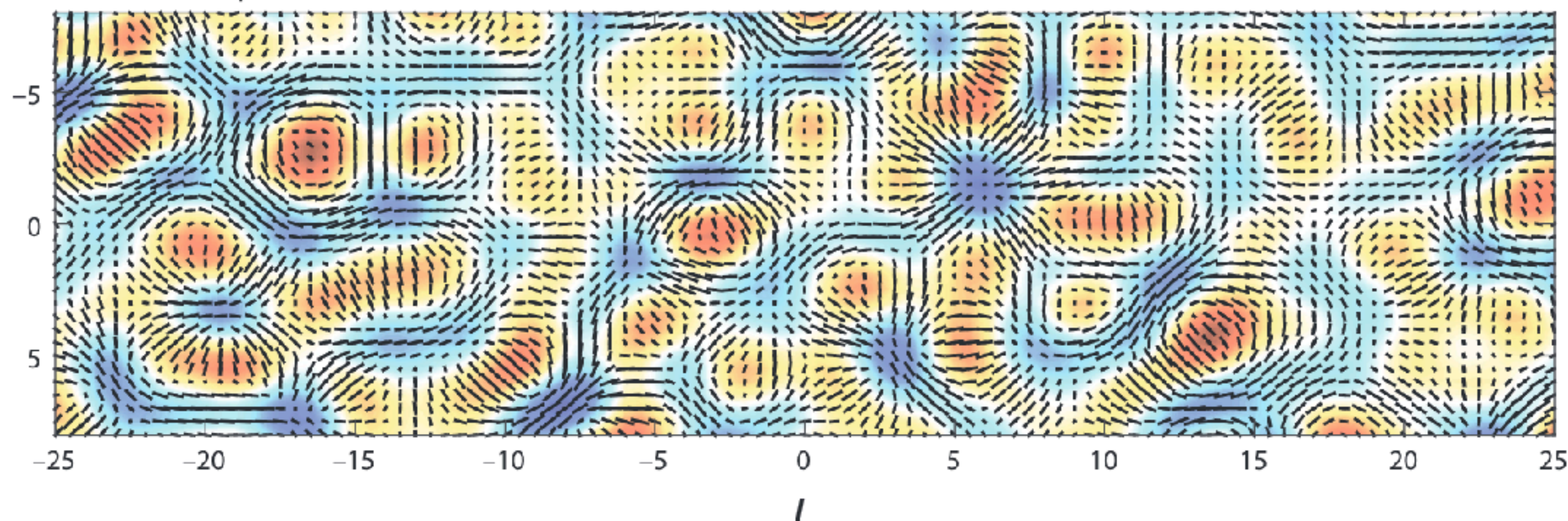
160  $\mu\text{K}$

Planck map smoothed with  $5^\circ$  filter



# E-mode and B-mode

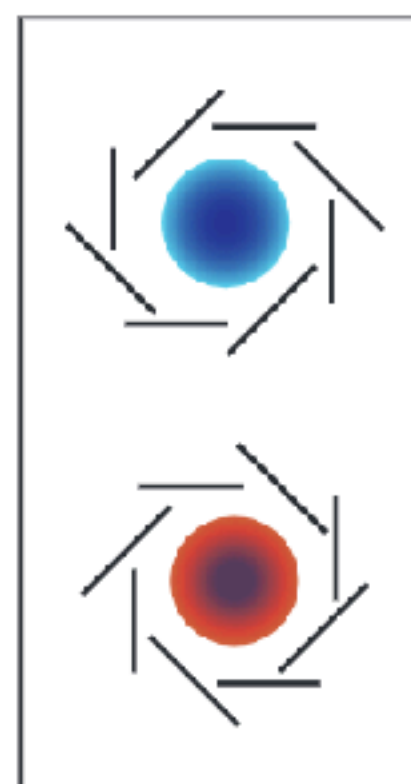
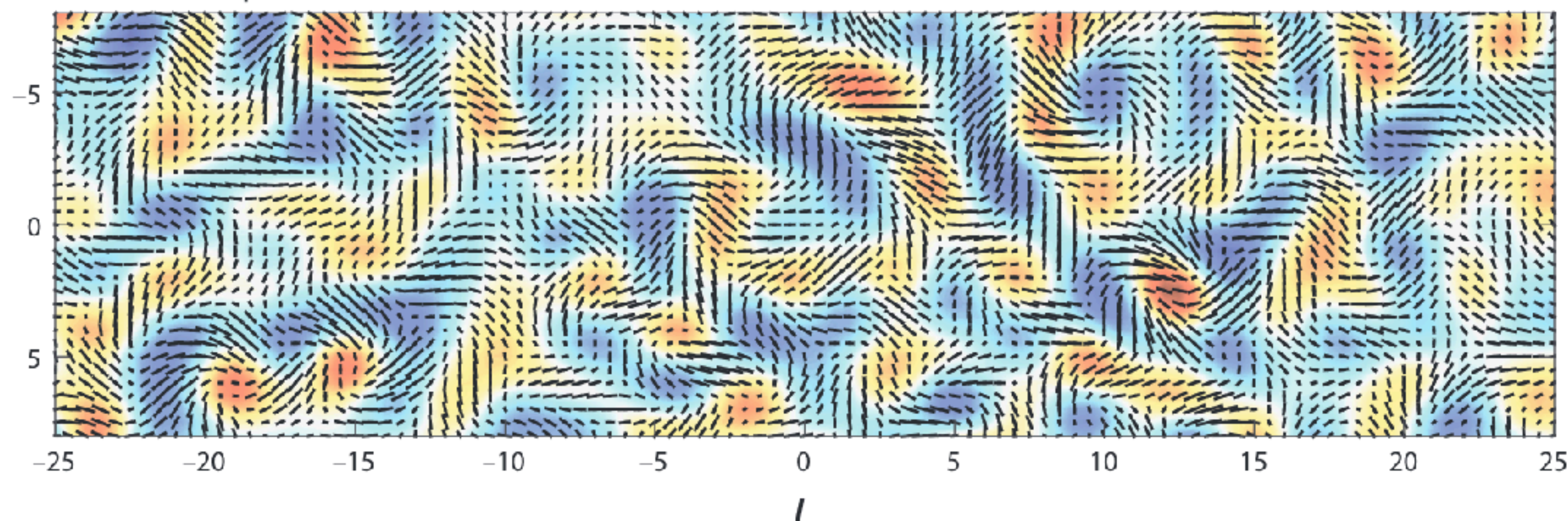
**a** E-mode polarization



*Even* parity

Can be generated from  
scalar (density),  
vector (vorticity),  
tensor (gravitational waves)

**b** B-mode polarization



*Odd* parity

Can be generated from  
vector (vorticity),  
tensor (gravitational waves)

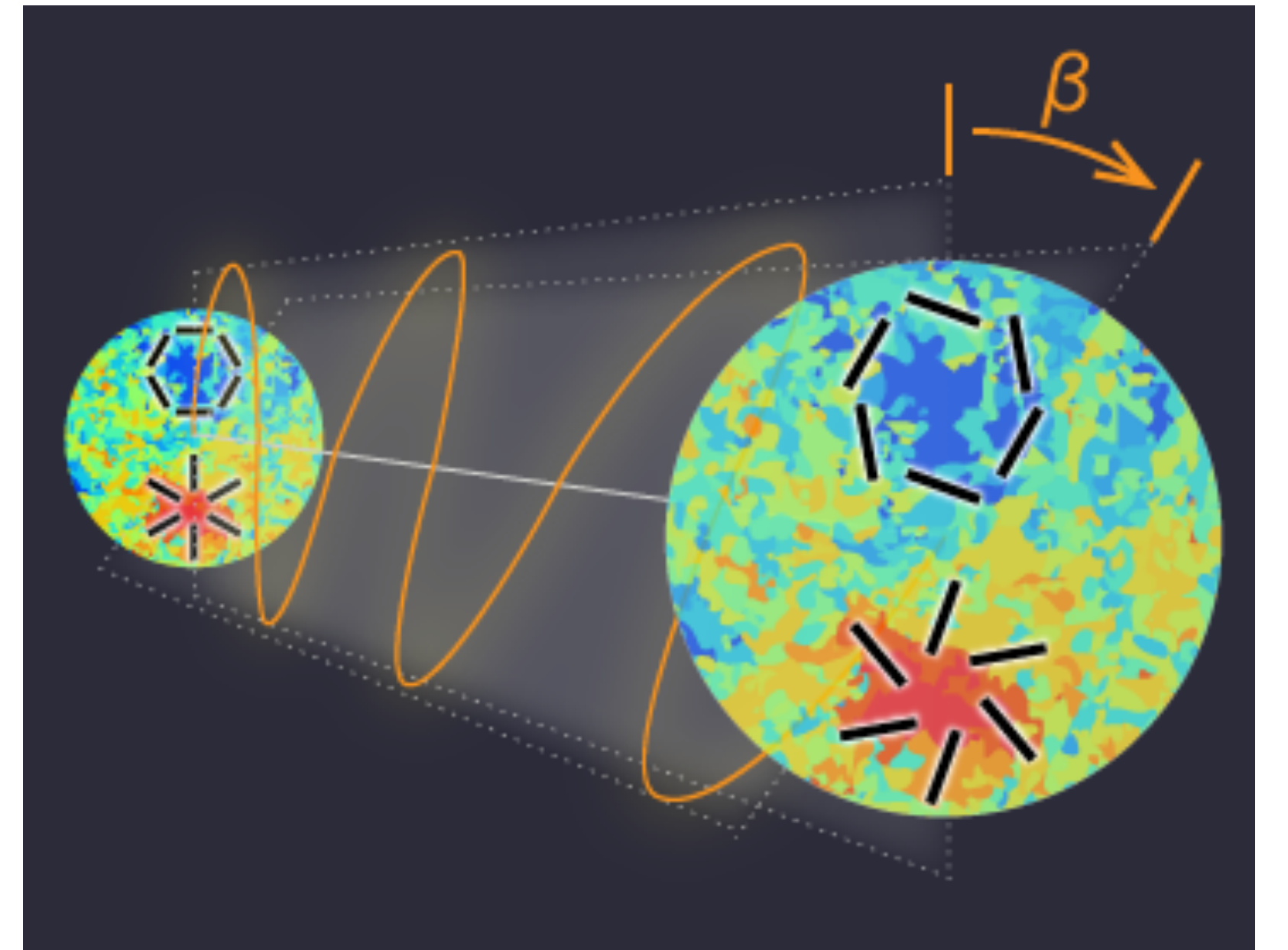


# The Cosmic Birefringence

E  $\leftrightarrow$  B conversion by rotation of the linear polarization plane

- The intrinsic EE, BB, and EB power spectra 13.8 billion years ago would yield the observed EB as

$$C_{\ell}^{EB, \text{obs}} = \frac{1}{2} (C_{\ell}^{EE} - C_{\ell}^{BB}) \sin(4\beta) + C_{\ell}^{EB} \cos(4\beta)$$

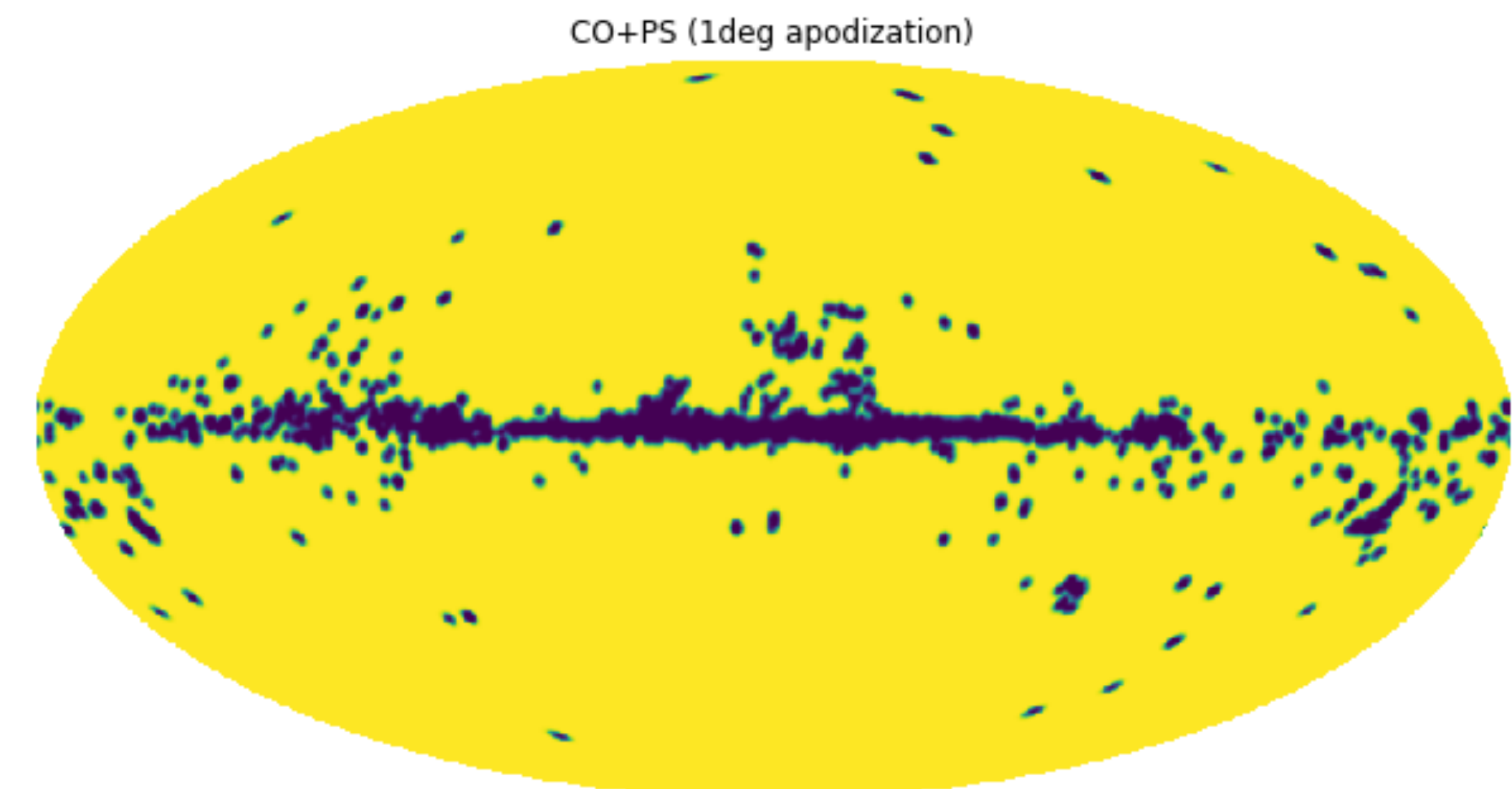
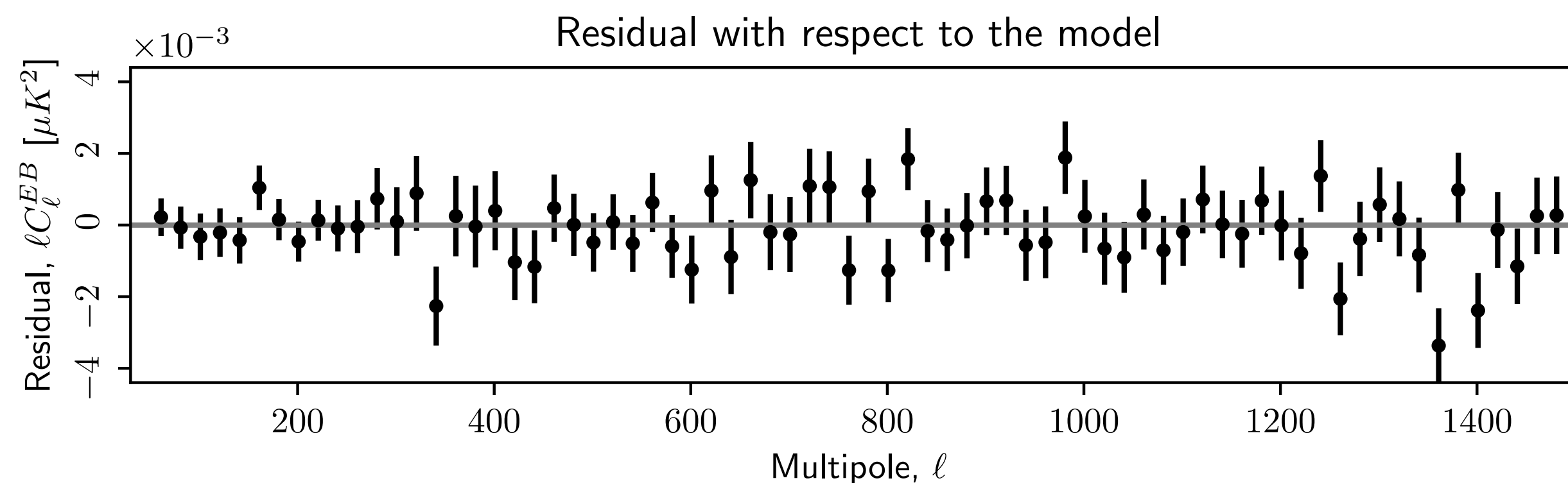
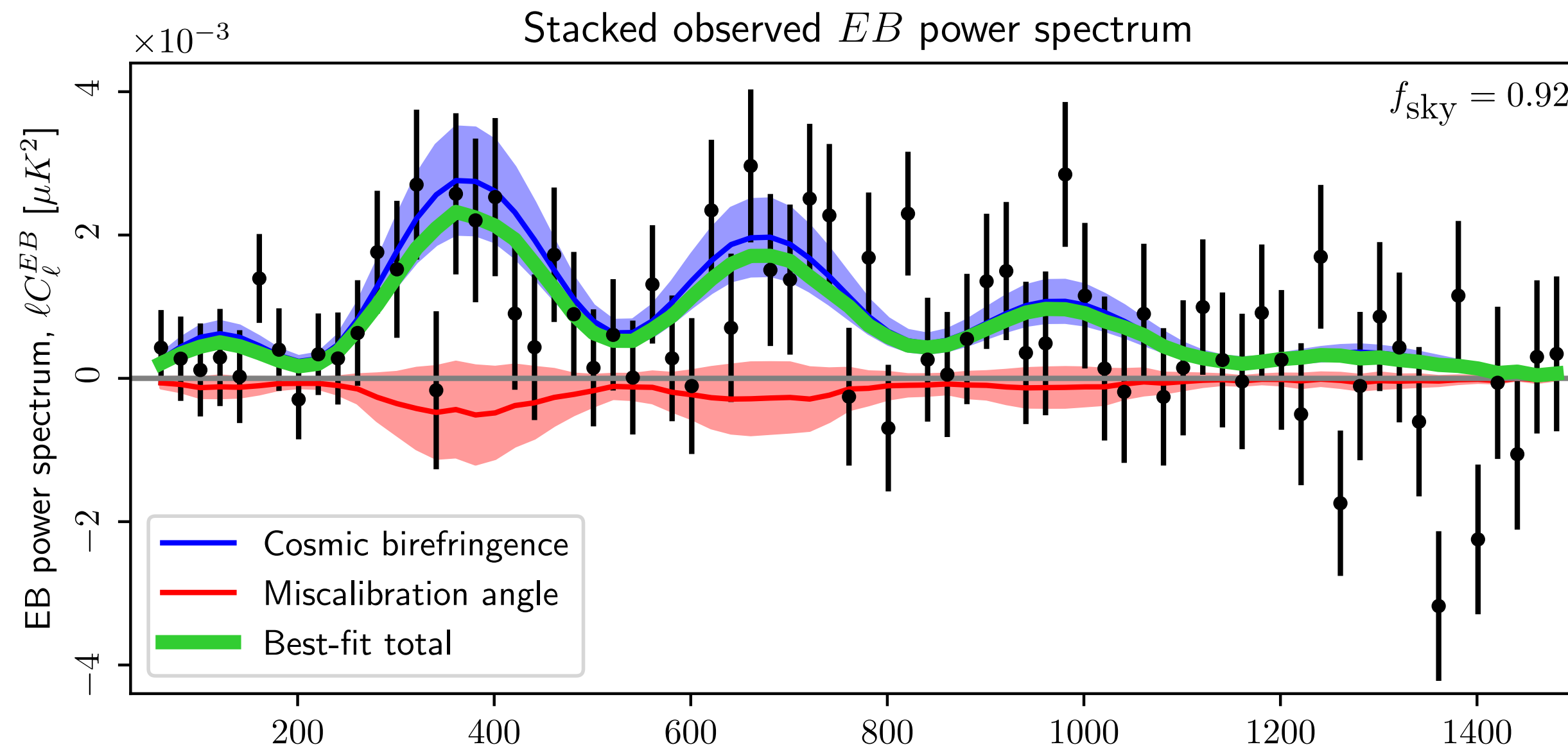


- One would find  $\beta$  by fitting  $C_{\ell}^{EE, \text{CMB}} - C_{\ell}^{BB, \text{CMB}}$  to the observed  $C_{\ell}^{EB, \text{obs}}$  using the best-fitting CMB model, and assuming the intrinsic EB to vanish,  $C_{\ell}^{EB} = 0$ .



# Cosmic Birefringence in WMAP/Planck

Nearly full sky ( $f_{\text{sky}} = 92\%$ ) analysis



- **Mis-calibration angles** make only small contributions thanks to the cancellation.

- $\beta = 0.34 \pm 0.09$  deg

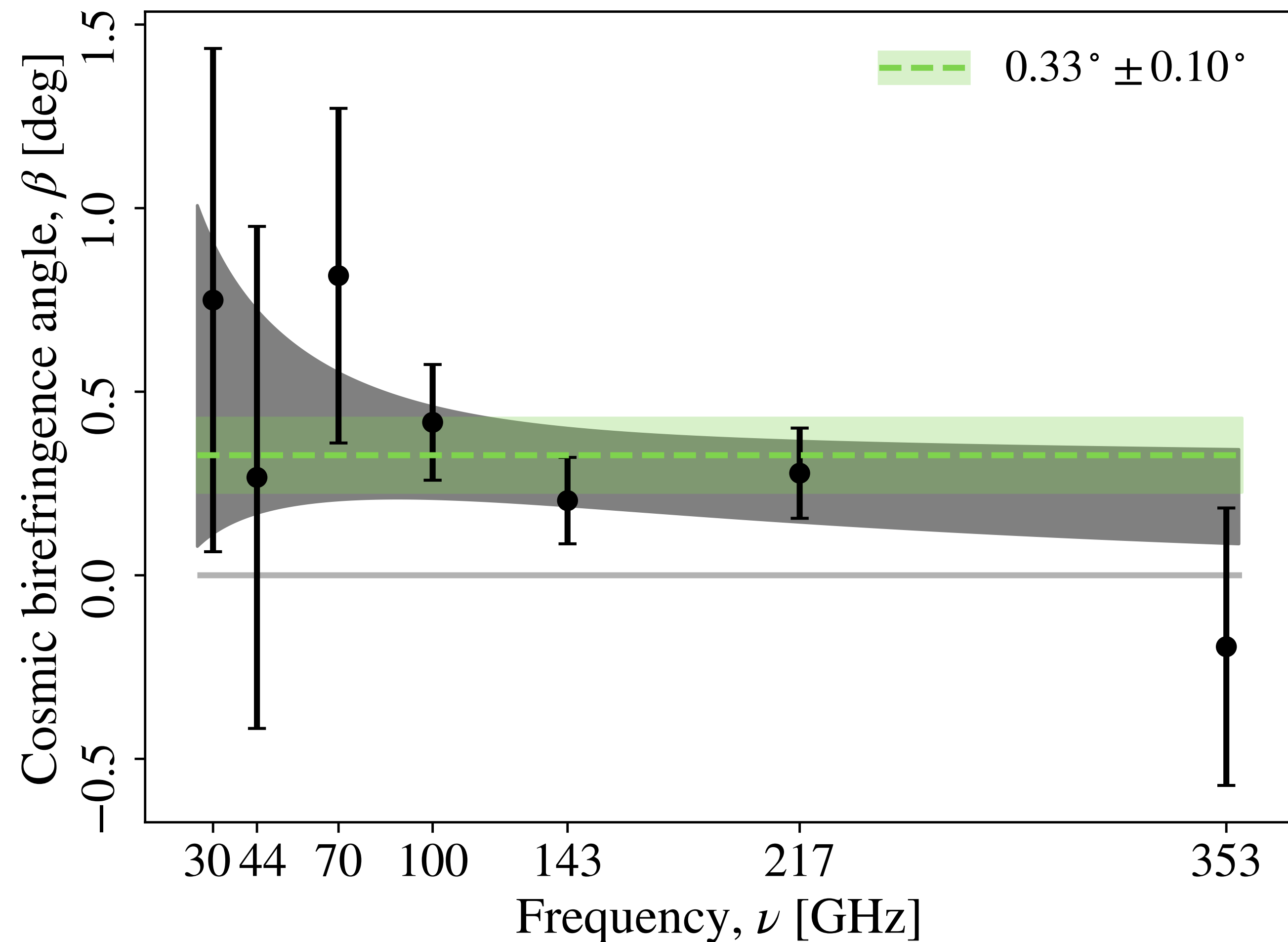
**3.6 $\sigma$ !!**

- $\chi^2 = 65.3$  for DOF=72



# No strong frequency dependence

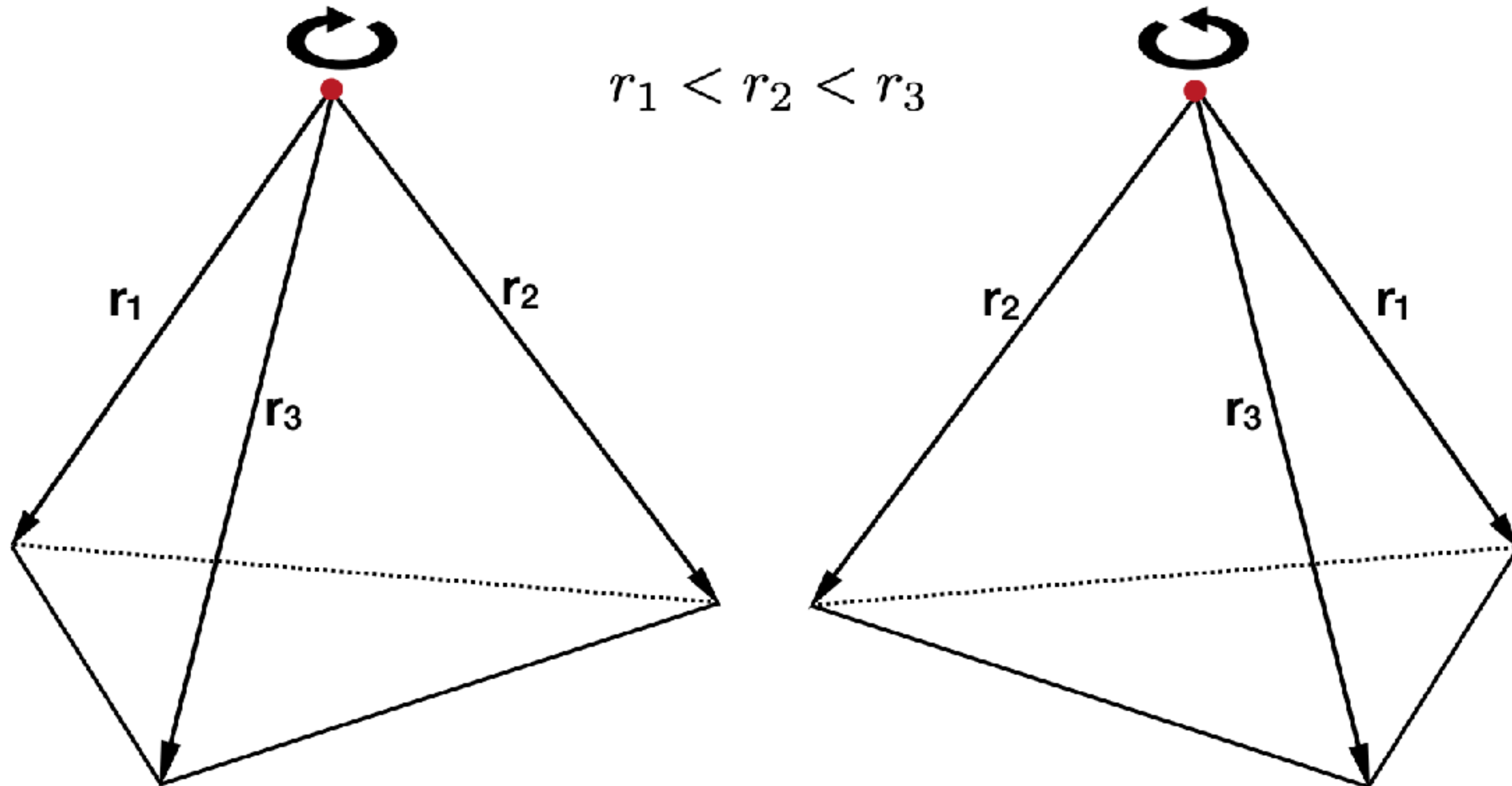
Consistent with cosmic birefringence due to  $\mathcal{L} \ni \theta F\tilde{F}$



- No evidence for frequency dependence:
  - For  $\beta \sim (\nu/150\text{GHz})^n$ ,  
 $\mathbf{n} = -\mathbf{0.20}^{+0.41}_{-0.39}$  (68% CL)
  - Faraday rotation ( $n=-2$ ) is disfavored.



# Parity-violation in galaxies?



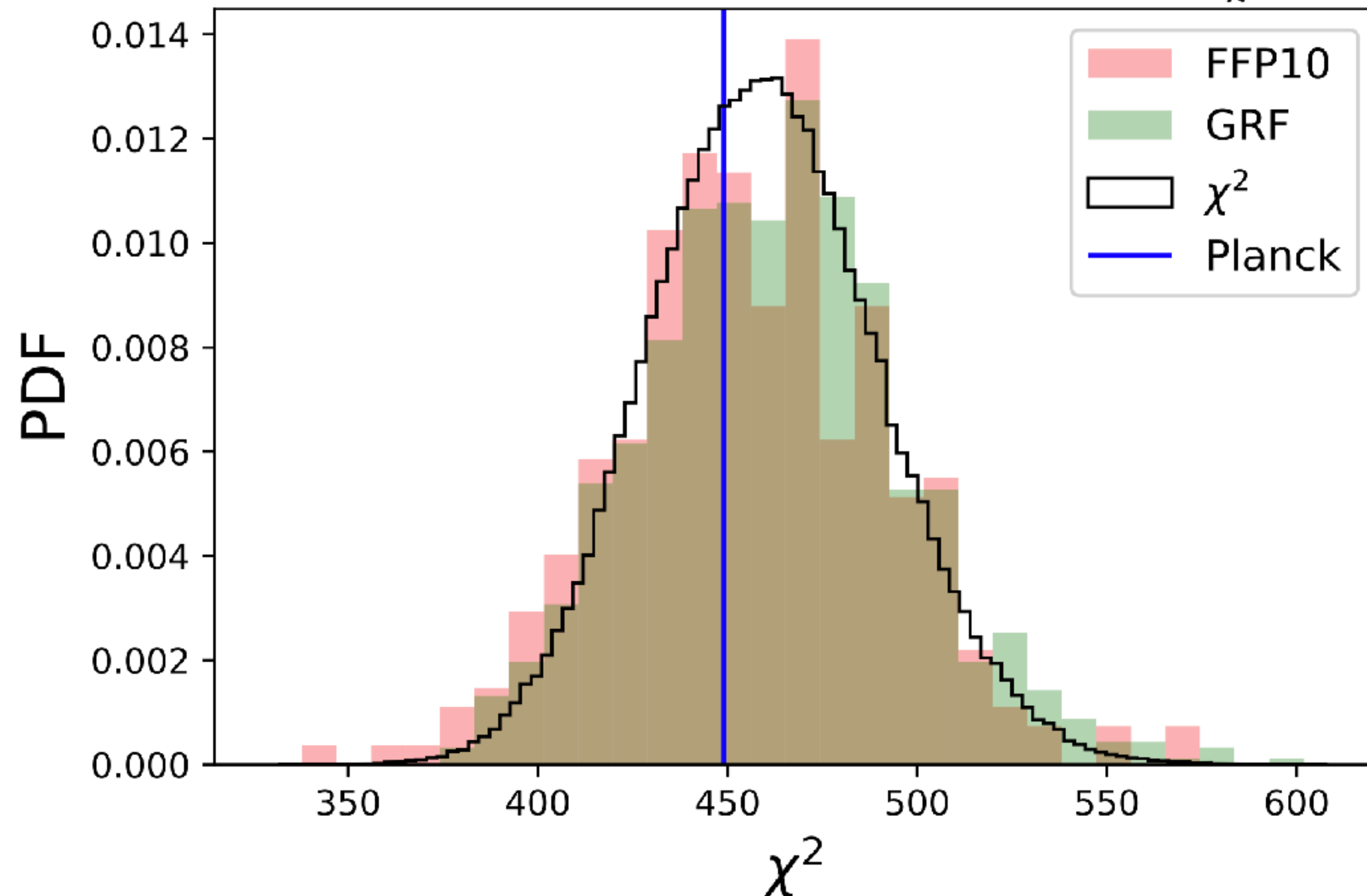
- The 4pt correlation function is *the lowest order statistics sensitive to parity.*
- Hou+ (2022) [2206.03625]  
3.1 $\sigma$  (LOWZ), 7.1 $\sigma$  CMASS
- Philcox (2022)  
[2206.04227]  
2.9 $\sigma$  from CMASS sample



# No parity-violation in the CMB

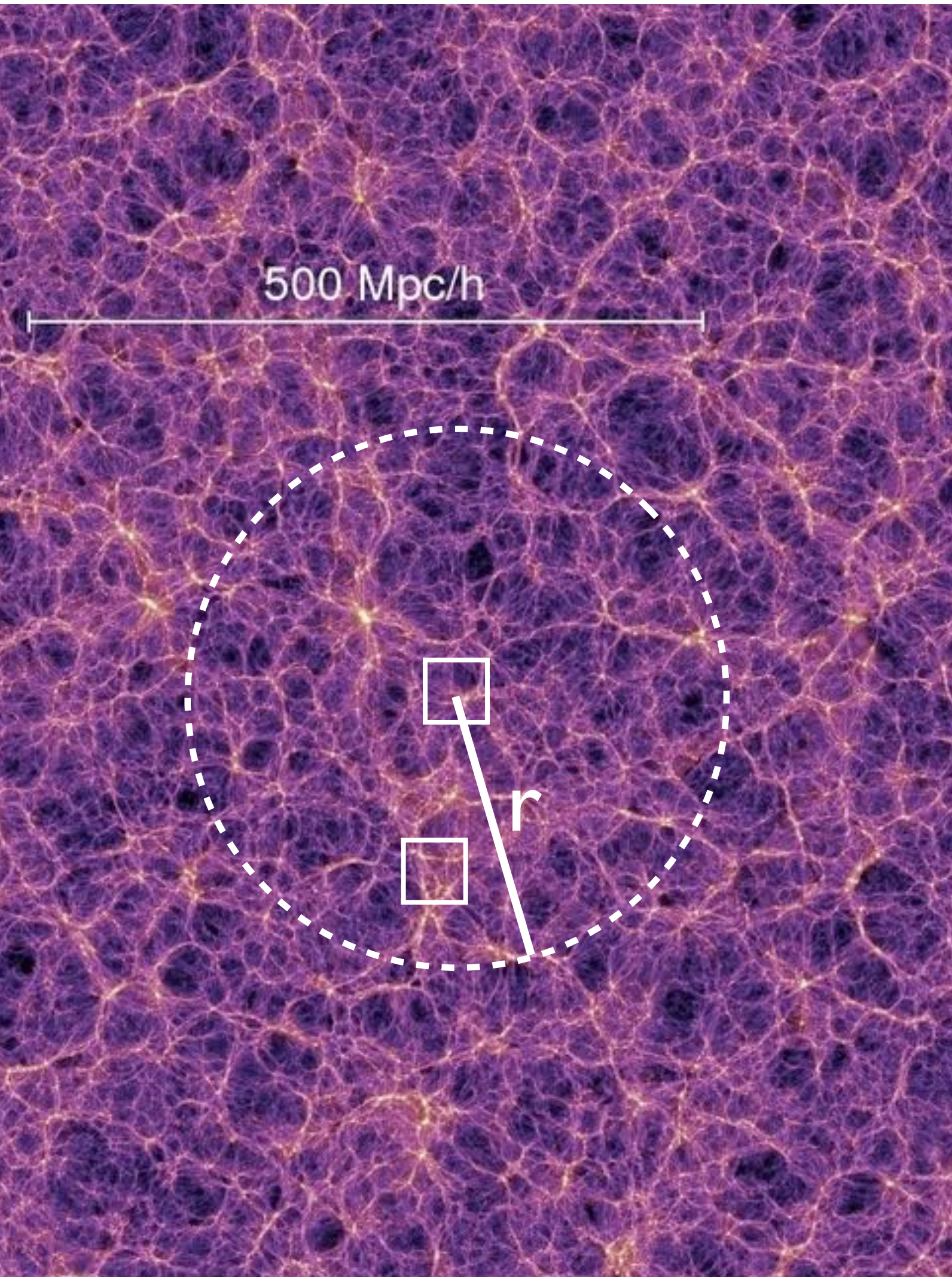
## Measurement from the CMB Trispectrum

Rank = 357/1000 (GRF), 128/300 (FFP10),  $P_{\chi^2} = 0.37$





# Dirac delta and homogeneity



- Two-point correlation function  $\xi(r)$  = excess number of pairs beyond random at separation  $r$

$$\xi(\mathbf{r}) = \langle \delta(\mathbf{x})\delta(\mathbf{x} + \mathbf{r}) \rangle$$

↑  
statistical homogeneity (translational invariance)

where  $\delta(x)$  is the density contrast, excess number density beyond mean:

$$\delta(x) = \text{density}(x)/(\text{mean density}) - 1$$

- Power spectrum is the Fourier transform of it:

$$\langle \delta(\mathbf{k})\delta(\mathbf{k}') \rangle = (2\pi)^3 P(\mathbf{k}) \delta^D(\mathbf{k} + \mathbf{k}')$$



# Parameterizing inhomogeneity

- Deviation from statistical homogeneity in the two-point functions will be evident in the off-diagonal correlation:

$$\langle \delta(\mathbf{k}_1)\delta(\mathbf{k}_2) \rangle |_{\mathbf{k}_1+\mathbf{k}_2 \neq 0} \neq 0$$

- Q: How does the inhomogeneity appear?
  - A way to *organize* the off-diagonal correlations:  $\mathbf{K} = -(\mathbf{k}_1+\mathbf{k}_2)$

$$\langle \delta(\mathbf{k}_1)\delta(\mathbf{k}_2) \rangle = VP(\mathbf{k}_1)\delta_{\mathbf{k}_1+\mathbf{k}_2}^D + \sum_{\mathbf{K}} f(\mathbf{k}_1, \mathbf{k}_2, \mathbf{K})\delta_{\mathbf{k}_1+\mathbf{k}_2+\mathbf{K}}^D$$

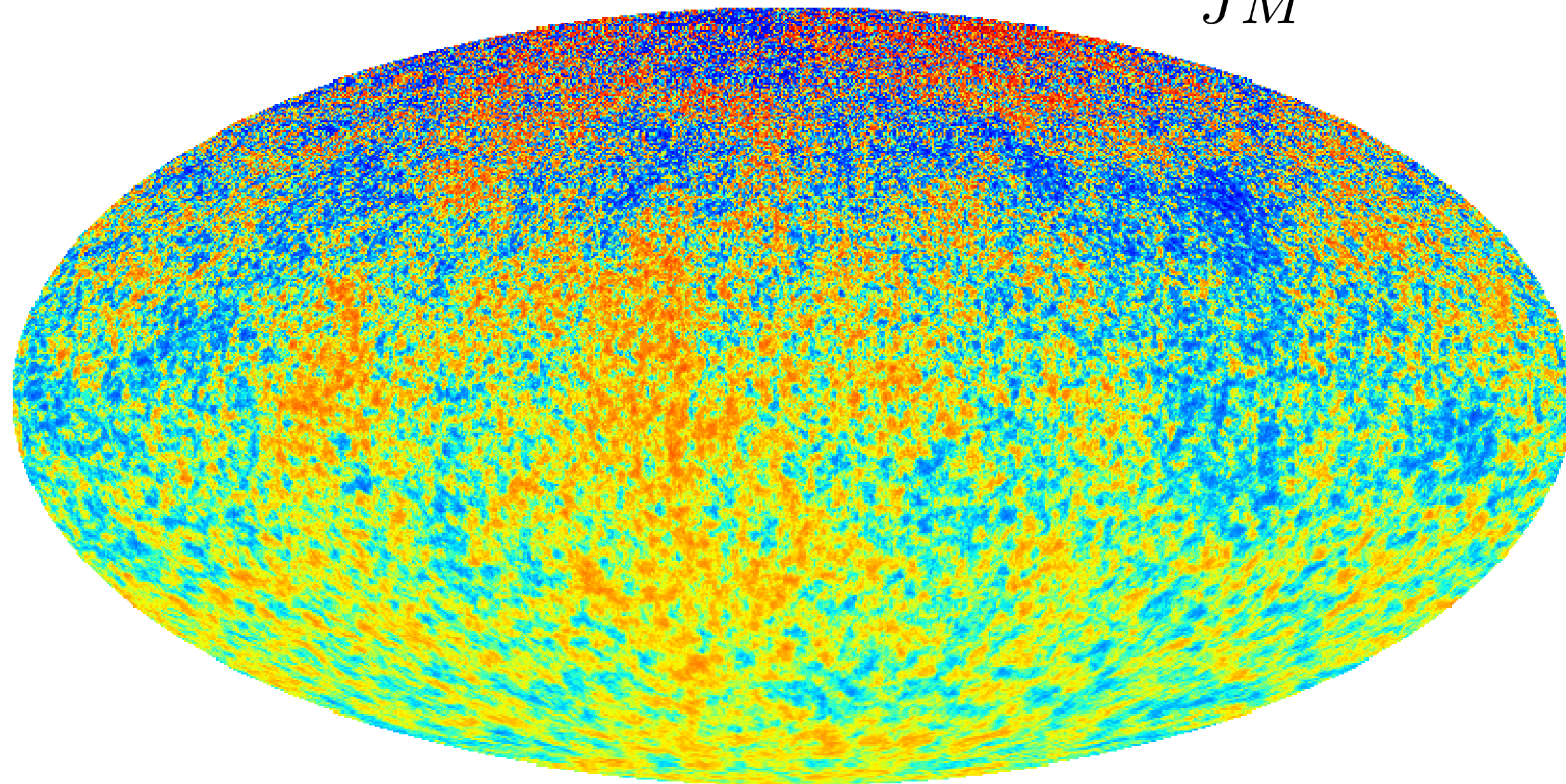
- The pattern of inhomogeneity is encoded in the function  $f$ !



# cf. parameterizing anisotropy

- This is analogous to the BiPoSH (bipolar spherical harmonic) expansion to characterize the statistical anisotropy:

$$\langle a_{\ell m} a_{\ell' m'} \rangle = C_{\ell} \delta_{\ell \ell'} \delta_{m m'} + \sum_{JM} (-1)^{m'} \langle \ell, m; \ell', -m' | J, M \rangle A_{\ell \ell'}^{JM}$$



Example: If we were to move with  $\beta \sim 1$  w.r.t. the CMB rest frame,

CMB would be statistically anisotropic ( $J=1, M=0$ ) with

$$A_{\ell \ell'}^{10} > 0$$



# What makes $\xi(\mathbf{r})$ inhomogeneous?

- Unknown systematics of the survey
  - If something varies over the survey volume and that something modulates the amplitude of clustering
- Our Universe might be intrinsically inhomogeneous
  - No compelling evidence so far, therefore, must be small!
- higher-order correlation functions
  - Non-linearities (e.g. position dependent power spectrum)
  - Primordial three-point function → clustering fossil



(local)

# Non-Gaussianity and ~~homogeneity~~

- **IF** we have a non-linear coupling between primordial density fluctuations and a **spectator field**  $h_p$  (JK coupling):

$$\langle \delta_i(\mathbf{k}_1) \delta_i(\mathbf{k}_2) h_p(\mathbf{K}) \rangle = V P_p(K) f_p(\mathbf{k}_1, \mathbf{k}_2) \epsilon_{ij}^p k_1^i k_2^j \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{K}}^D$$

power spectrum of new field  
 ↓  
 coupling amplitude      polarization basis (scalar, vector, tensor, ...)

- THEN, density power spectrum we observe now has ***non-zero off-diagonal*** components: **Fossil equation**

$$\langle \delta_i(\mathbf{k}_1) \delta_i(\mathbf{k}_2) \rangle |_{h_p(\mathbf{K})} = V P_i(\mathbf{k}_1) \delta_{\mathbf{k}_1 + \mathbf{k}_2}^D + h_p^*(\mathbf{K}) f_p(\mathbf{k}_1, \mathbf{k}_2) \epsilon_{ij}^p k_1^i k_2^j \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{K}}^D$$



# Why call clustering fossils?

- Inflaton(s) : a scalar field(s) responsible for inflation
- But, **inflaton might not be alone**. Many inflationary models need/introduce additional fields. But, direct detection of such fields turns out to be very hard:
  - Additional Scalar: may not contribute seed fluctuations
  - Vector: decays as  $1/[\text{scale factor}]$
  - Tensor: decays after coming inside of comoving horizon
- Clustering fossils may be the only way of detecting them!



# SVT can be distinguished with $\epsilon^p_{ij}$

- In a symmetric 3x3 tensor, we have 6 degrees of freedom, which are further decomposed by Scalar, Vector and Tensor polarization modes.

- They are orthogonal:  $\epsilon^p_{ij} \epsilon^{p',ij} = 2\delta_{pp'}$

- Scalar (p=0,z):  $\epsilon^0_{ij} \propto \delta_{ij}$      $\epsilon^z_{ij}(\mathbf{K}) \propto K_i K_j - K^2/3$

- Vector (p=x,y):  $\epsilon^{x,y}_{ij}(\mathbf{K}) \propto \frac{1}{2} (K_i e_j + K_j e_i)$  where  $K_i e_i = 0$

- Tensor [Gravitational Waves](p=x,+): transverse and traceless

$$K_i \epsilon^{+,\times}_{ij}(\mathbf{K}) = 0 \quad \delta_{ij} \epsilon^{+,\times}_{ij}(\mathbf{K}) = 0$$



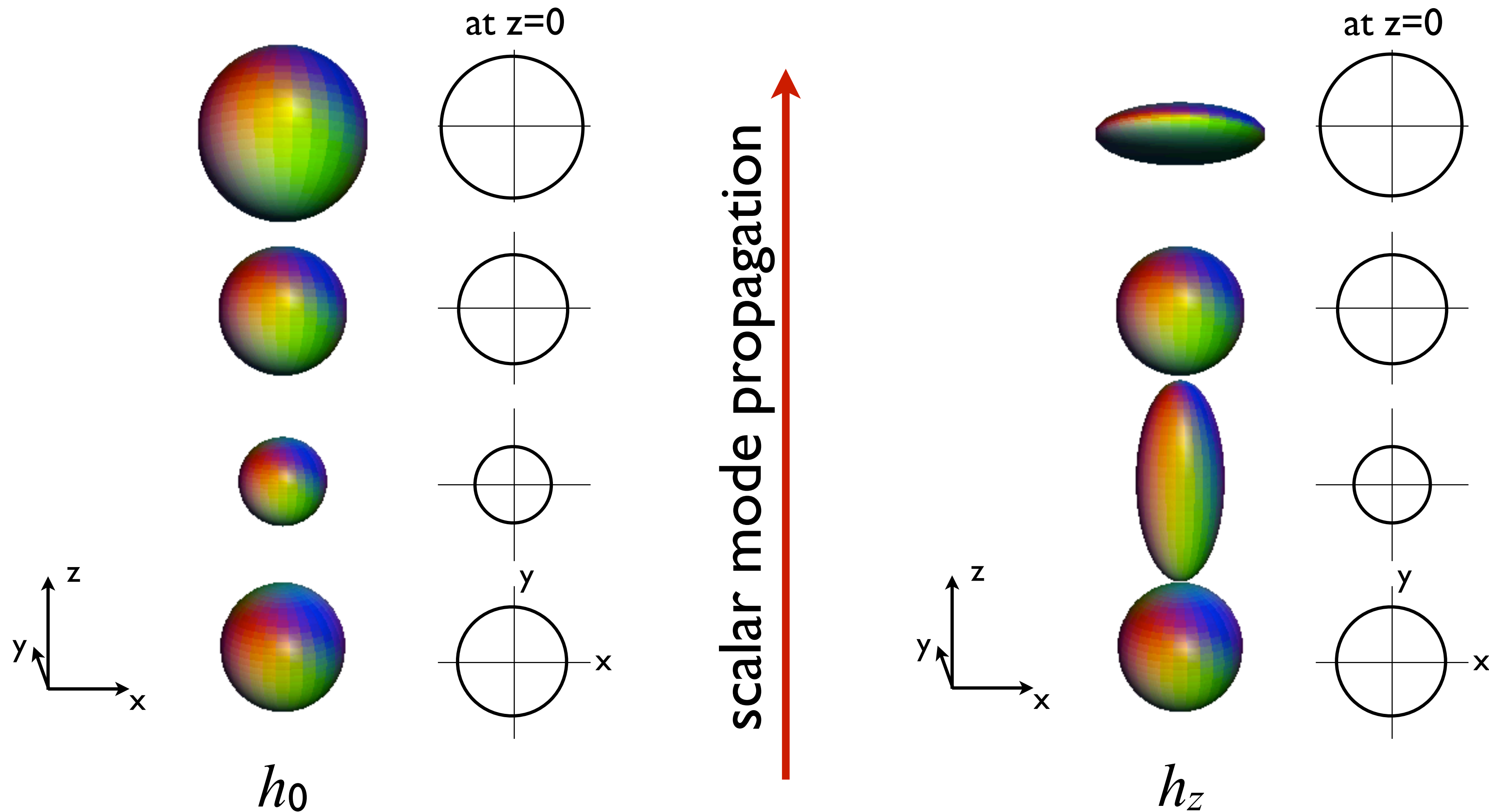
# Effect of fossils on 2PCF

$$\langle \delta_i(\mathbf{k}_1) \delta_i(\mathbf{k}_2) \rangle |_{h_p(\mathbf{K})} = V P_i(\mathbf{k}_1) \delta_{\mathbf{k}_1 + \mathbf{k}_2}^D + h_p^*(\mathbf{K}) f_p(\mathbf{k}_1, \mathbf{k}_2) \varepsilon_{ij}^p k_1^i k_2^j \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{K}}^D$$

- Statistical homogeneity is broken in the presence of the spectator field  $h_p(\mathbf{K})$ .
- Depending on the polarization, the way that the spectator affects clustering is different. How?
  - I will show **equi-correlation-function surfaces** when  $h_p(\mathbf{K})$  propagates upward.
  - Without  $h_p(\mathbf{K})$ , we expect that it should be spherical.

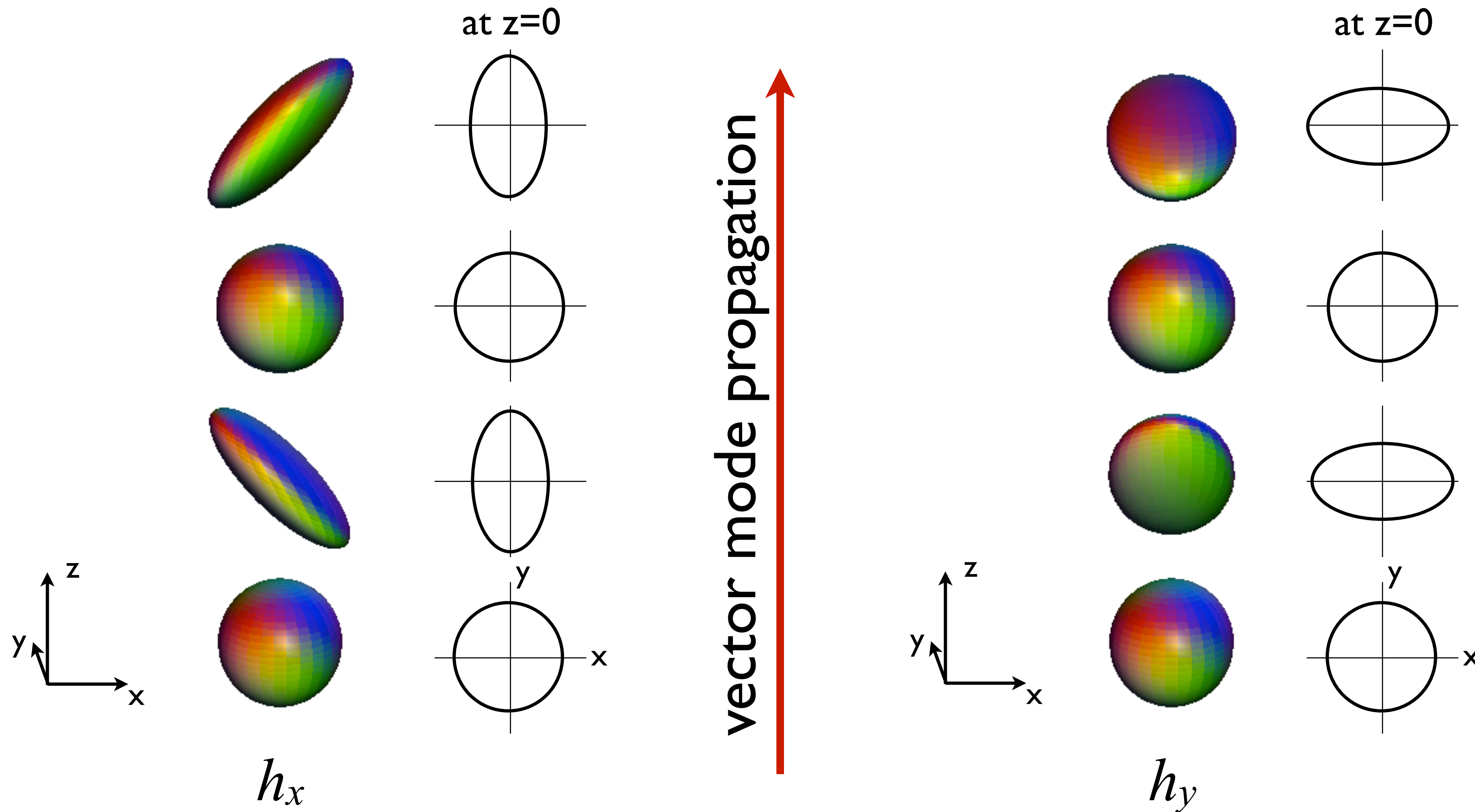


# $\xi(\mathbf{r})$ with single scalar mode ( $p=0, z$ )



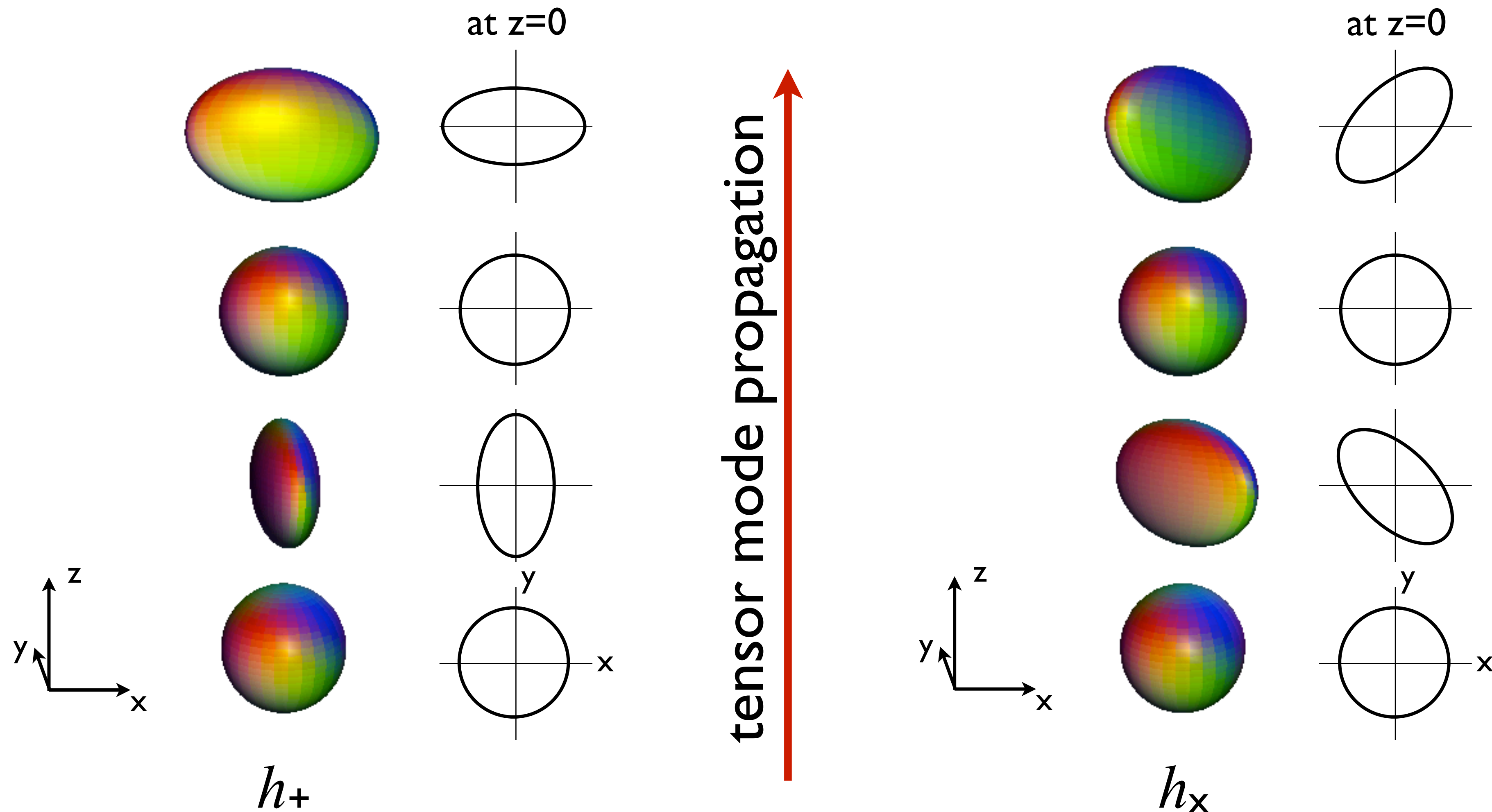


# $\xi(\mathbf{r})$ with single vector mode ( $p=x,y$ )





# $\xi(\mathbf{r})$ with single tensor mode ( $p=+,x$ )





# Example: tensor clustering fossils

- For the *single-field slow-roll inflation* models ( $k_t = k_1 + k_2 + k_3$ ),  
Maldacena (2003)

$$B_{\zeta\zeta h_p}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = \frac{1}{2} \left[ \frac{P_\zeta(k_1)}{k_2^3} + \frac{P_\zeta(k_2)}{k_1^3} \right] P_{h_p}(k_3) \varepsilon_{ij}^p k_1^i k_2^j \left[ -k_t + \frac{k_1 k_2 + k_2 k_3 + k_3 k_1}{k_t} + \frac{k_1 k_2 k_3}{k_t^2} \right]$$

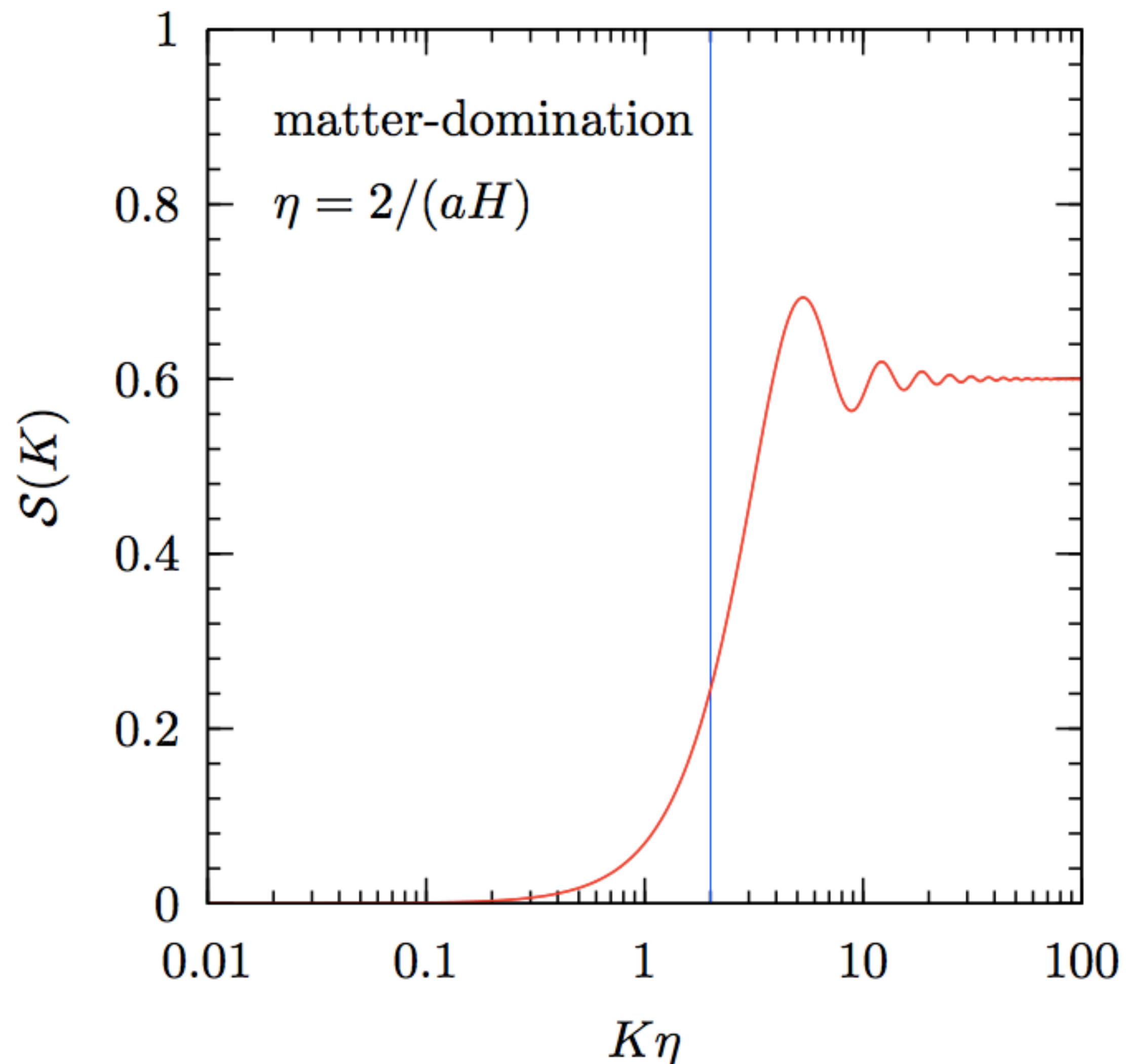
↓ **squeeze limit** ( $k_1 \approx k_2 \gg k_3$ )

$$\left( \frac{4 - n_s}{2} \right) P_\zeta(k_1) P_{h_p}(k_3) \frac{\varepsilon_{ij}^p k_1^i k_1^j}{k_1^2} \equiv -\frac{1}{2} \frac{d \ln P_\zeta(k)}{d \ln k} P_\zeta(k_1) P_{h_p}(k_3) \varepsilon_{ij}^p \hat{k}_1^i \hat{k}_1^j$$

- In the squeeze limit, **long-wavelength tensor field rescales** small scale wave-vector:  $k^2 \rightarrow k^2 - h_{ij} k_i k_j$  (or length  $x^2 \rightarrow x^2 + h_{ij} x_i x_j$ )!
- *Note:* the local observer (use physical ruler, not the coordinate ruler) will not see the effect!



# Interaction @ horizon crossing



- After inflation, tensor (long) modes **re-enters** horizon, and **interact** with density (small) modes:

$$\delta_{\text{int.}}(\mathbf{k}) = -2S(K)h_p(K)\varepsilon_{ij}^p(\hat{\mathbf{K}})\hat{\mathbf{k}}_i\hat{\mathbf{k}}_jT(k)\zeta_p(\mathbf{k})$$

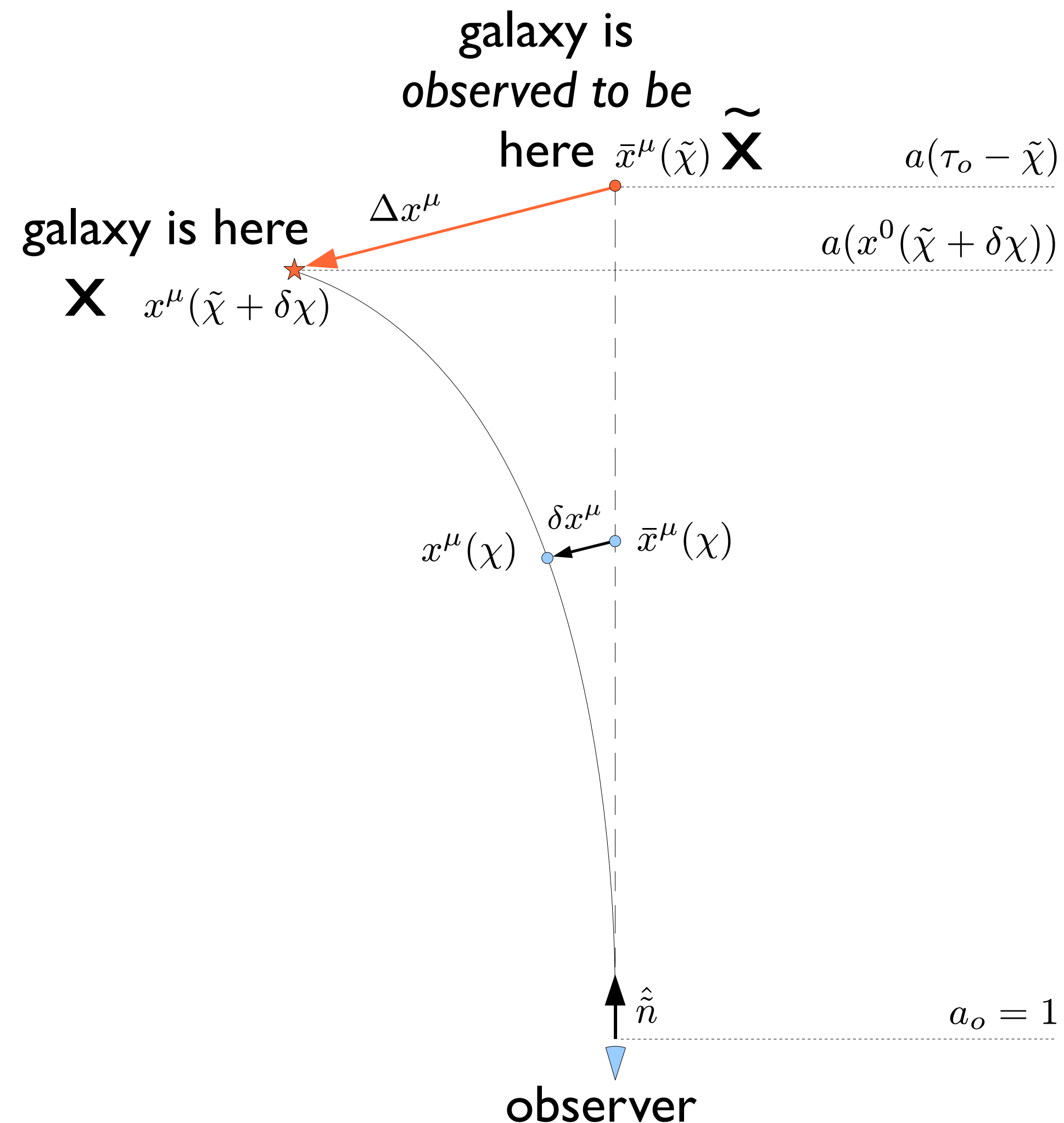
- Note that the influence dies out as tensor mode itself decays after horizon re-entry.

$$S(K) \simeq \frac{3}{5} \left[ 1 - \exp\left(-\frac{5}{42}K^2\eta^2\right) \right]$$



$$ds^2 = a^2(\eta) [-d\eta^2 + (\delta_{ij} + h_{ij})dx^i dx^j]$$

# Light deflection due to GW



- The light deflection changes the observed location of galaxies: the geodesic equation gives  $\Delta x_\mu$
- The large scales ( $K \rightarrow 0$ ) displacement field is

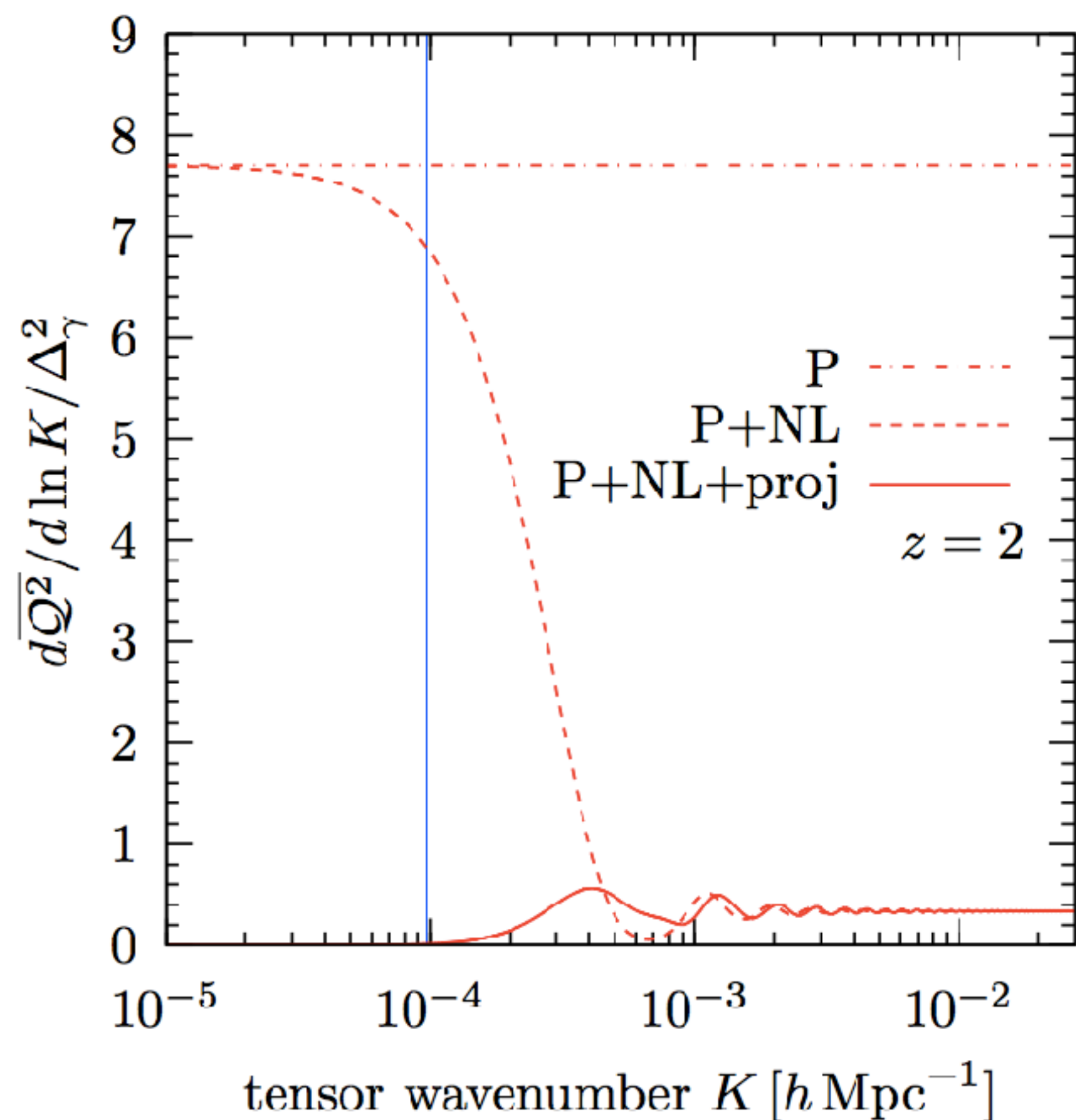
$$\Delta x^i \rightarrow -\frac{1}{2} h_0^{ij} x_j$$

which cancels the super-horizon contributions and (of course) we cannot observe the super horizon modes!



# Observable fossil amplitude

$$\langle \delta_g(\mathbf{k}_1) \delta_g(\mathbf{k}_2) \rangle \simeq P_g(k_1) \delta_{\mathbf{k}_1 + \mathbf{k}_2}^D + \left[ \frac{1}{2} (1 - T_\gamma) \frac{d \ln P_\delta(k_1)}{d \ln k_1} + 2S(K) \right] P_g(k_1) h_p(K) \varepsilon_{ij}^p k_1^i k_1^j \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{K}}^D$$



- Quadrupole power spectrum contribution (when  $K \ll k_F$ ) from single-field slow-roll inflation
- **large-scale** (super-horizon) fossils cancel *completely* with projection
- **small-scale** fossil cancels *partially* with tensor-scalar interaction around horizon crossing

# Fossils from other inflation models

- The large-scale cancelation **happens only for** the SFSR models
  - With scalar-scalar-tensor correlation different from SFSR
    - Power quadrupole can constrain  $k_{\min}$  (beginning of inflation)
    - clustering fossil signal can be big!

- e.g.

Solid inflation

Dimastrogiovanni, Fasiello, Jeong & Kamionkowski (2014)

Quasi-single field inflation

Dimastrogiovanni, Fasiello & Kamionkowski (2015)

$$\mathcal{B}_{\zeta\kappa} = \frac{3}{2} \frac{\mathcal{R}}{\epsilon} P_{\zeta}(k) P_h(K)$$

$$\mathcal{B}_{\zeta\kappa} = -\frac{\pi^2}{2} w(\nu) \frac{\dot{\theta}_0^2}{H^2} P_{\zeta}(k) P_h(K)$$

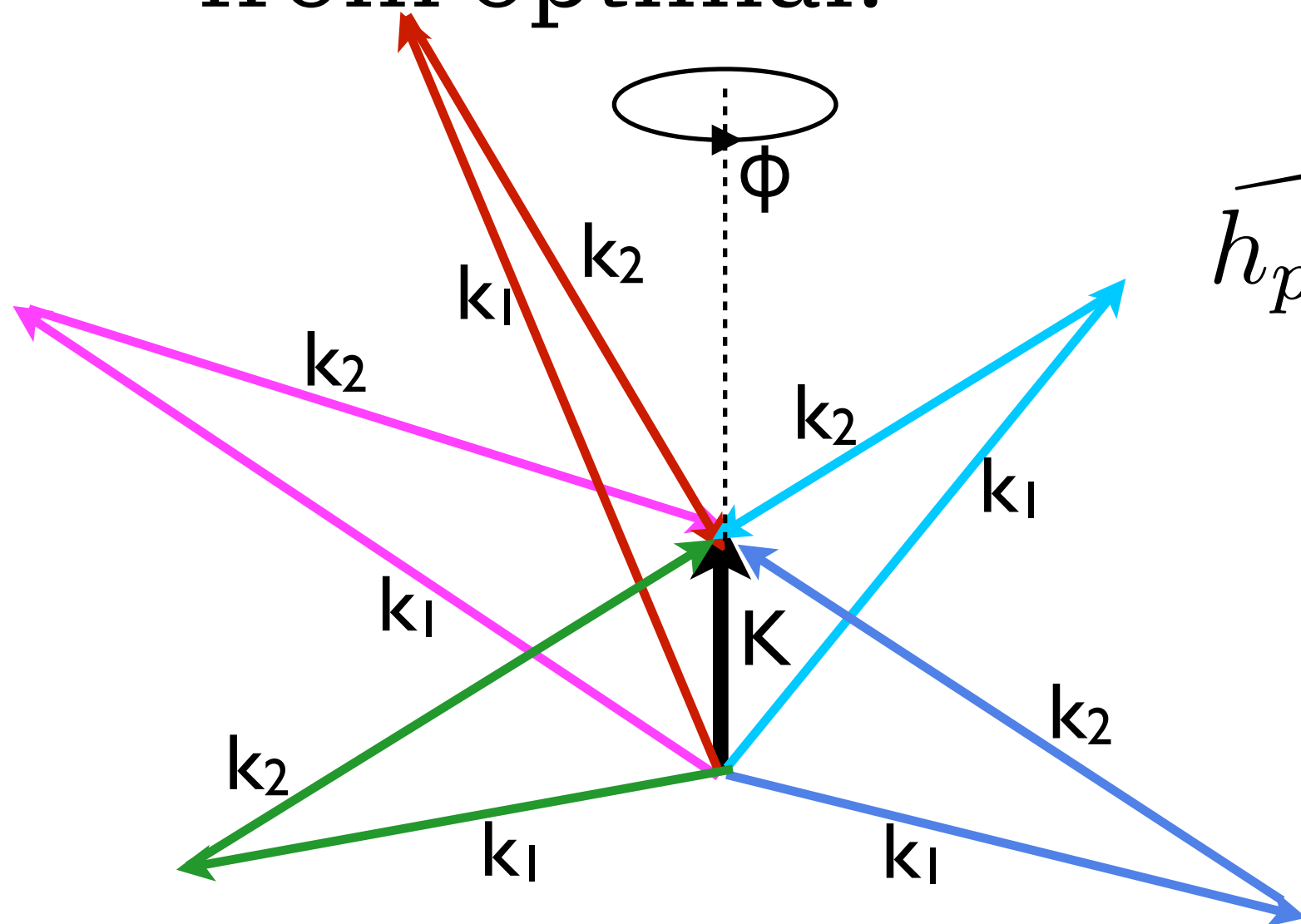


# LSS fossil estimator: naive

- Let's start from Fossil equation

$$\langle \delta(\mathbf{k}_1) \delta(\mathbf{k}_2) \rangle |_{h_p(\mathbf{K})} = h_p(\mathbf{k}_1 + \mathbf{k}_2) f_p(\mathbf{k}_1, \mathbf{k}_2) \epsilon_{ij}^p k_1^i k_2^j \delta_{\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{K}}^D$$

- Rearranging it a bit, we get a naive estimator for the new field, which is far from optimal:



$$\widehat{h_p(\mathbf{K})} = \sum_{\mathbf{k}_1 + \mathbf{k}_2 = \mathbf{K}} \frac{\delta(\mathbf{k}_1) \delta(\mathbf{k}_2)}{f_p(\mathbf{k}_1, \mathbf{k}_2) \epsilon_{ij}^p k_1^i k_2^j}$$

Azimuthal( $\phi$ )-dependence,  $[\cos(s\phi)]$   $s$ =spin, distinguishes scalar from vector from tensor geometrically!

# Optimal estimator (single mode)

- **Inverse-variance weighting** gives an optimal estimator for a single mode

$$\widehat{h_p(\mathbf{K})} = P_p^n(\mathbf{K}) \sum_{\mathbf{k}} \frac{f_p^*(\mathbf{k}, \mathbf{K} - \mathbf{k}) \epsilon_{ij}^p k^i (K - k)^j}{2V P^{\text{tot}}(k) P^{\text{tot}}(|\mathbf{K} - \mathbf{k}|)} \delta(\mathbf{k}) \delta(\mathbf{K} - \mathbf{k})$$

- With a noise power spectrum ( $P_{\text{tot}} = P_{\text{galaxy}} + P_{\text{noise}}$ )

$$P_p^n(K) = \left[ \sum_{\mathbf{k}} \frac{|f_p(\mathbf{k}, \mathbf{K} - \mathbf{k}) \epsilon_{ij}^p k^i (K - k)^j|^2}{2V P^{\text{tot}}(k) P^{\text{tot}}(|\mathbf{K} - \mathbf{k}|)} \right]^{-1}$$



# Optimal estimator for the amplitude $A_h$

- For a stochastic background of new fields with power spectrum  $P_p(K)=A_h P_h^f(K)$ , we **optimally summed over different K-modes** to estimate the amplitude by (w/ NULL hypothesis):

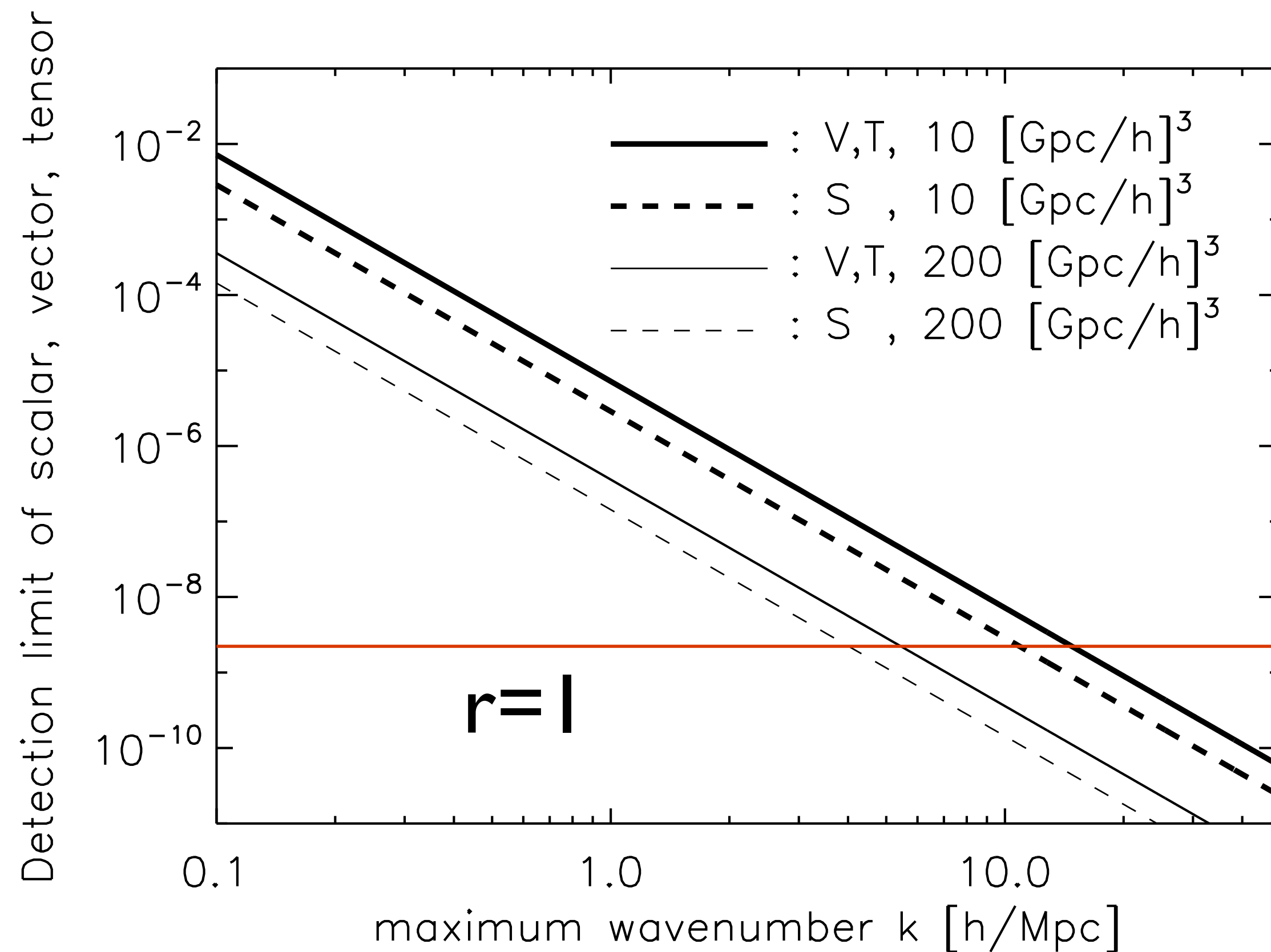
$$\widehat{A}_h = \sigma_h^2 \sum_{\mathbf{K},p} \frac{[P_h^f(K)]^2}{2 [P_p^n(K)]^2} \left( \frac{|\widehat{h_p(\mathbf{K})}|^2}{V} - P_p^n(K) \right)$$

- Here, the minimum uncertainty of measuring amplitude is

$$\sigma_h^{-2} = \sum_{\mathbf{K},p} [P_h^f(K)]^2 / 2 [P_p^n(K)]^2$$

# Order-of-magnitude calculation

- For the SFSR inflation models (Maldacena, 2003)



- projected 3-sigma (99% C.L.) detection limit with galaxy survey parameters
- To detect the gravitational wave, we need a large dynamical range
- Current and future survey should set a limit on primordial V and T (and higher-spin fields)!



# Summary & Conclusion

- Some hints from recent measurements of the parity violation
- Off-diagonal correlators are the place to look at the signature for spatial inhomogeneity.
- “Clustering fossil” is a way to look at primordial spectator fields that existed during the early time.
  - requirement: large dynamical range to beat the small signal (e.g. 21cm). We can distinguish scalar/vector/tensor fossils.
  - *An interesting probe of higher spin field and parity violation.*
- Systematics: survey systematics, non-linearities, non-Gaussianities