

Non-supersymmetric heterotic strings: gauge symmetry enhancement and one-loop cosmological constant in toroidal compactifications

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Work in collaboration with

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arXiv: 2307.xxxxx

see also [Bernardo's talk on Thursday](#)

String phenomenology 2023, Daejeon

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Alvarez-Gaume, Ginsparg, Moore, Vafa 86
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- Here we'll look at T^d compactifications (and in particular S^1)

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Motivation for T^d compactifications

- Rich phenomenon of gauge symmetry enhancement at special points in mod space

-for SUSY heterotic: full classification of gauge symmetries for $d \leq 4$

full rank ($d + 16$)

Fraiman, M.G., Nuñez 18

De Freitas, Font, Fraiman, M.G., Nuñez 20

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Goddard, Olive 85

Cachazo, Vafa 00

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- Same for **non SUSY**?

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- Local **minima, maxima** or **saddle** points?

Non-susy heterotic string: bosonic formulation

- Start from the $E_8 \times E_8$ (susy) heterotic $\pi \in \Gamma_8 \oplus \Gamma_8$ heterotic momenta

- quotient by $\beta = \pm (-1)^{2\pi \cdot \delta}$
(breaks susy)

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- add twisted sector

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Non-susy heterotic string

- Four sectors

- untwisted sectors $\Gamma_v = \Gamma^+ = \{(0; 0), (s; s)\}$

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- $(8_{vL} \otimes) (8_v, 1; 1)$ metric, B-field, dilaton

- $(8_v, 120; 1)$
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~~SUSY~~

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All 6 non-susy heterotic theories (of rank 16) are dual upon circle compactification!

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$$N = 1, P_L^2 = 0; p_R^2 = 1, \quad \bar{N} = 0 \quad \text{NS sector} \quad P \in \Gamma_0 \quad \text{right-moving vectors}$$

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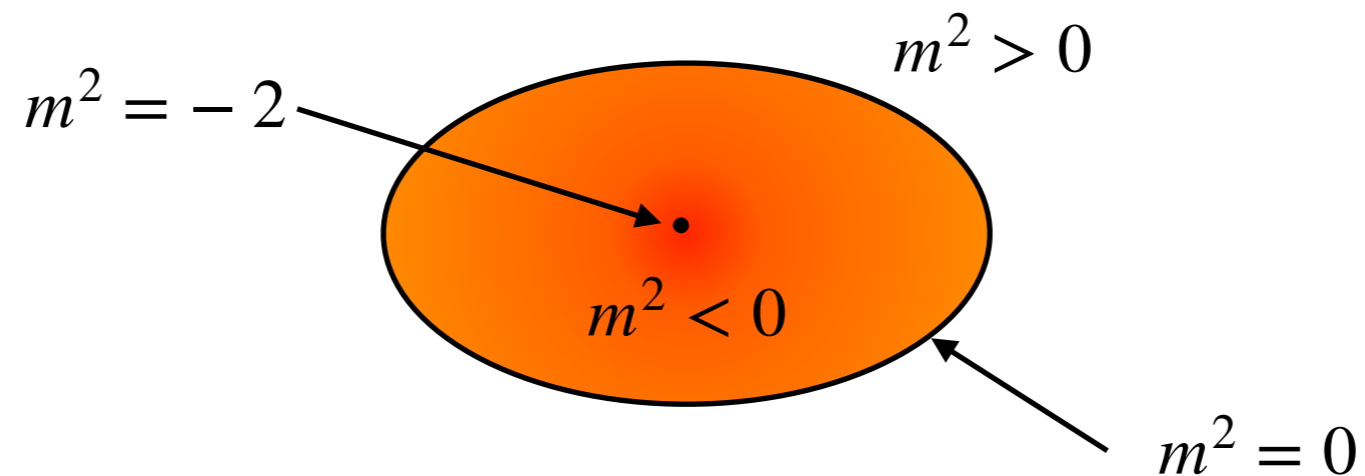
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- Tachyons!

- a region of moduli space has tachyons if there are states in Γ_0 :

$$P_L^2 = 1 + p_R^2 ; \quad 0 \leq p_R^2 < 1 \quad m^2 = -2(1 - p_R^2)$$



Gauge symmetry enhancement

- **Untwisted** + **twisted** massless states

$$p_R = 0 \Rightarrow n = \left(R^2 + \frac{1}{2} A^2 \right) \omega + \pi \cdot A \in \mathbb{Z}$$

generic A

generic R

rational A

generic R

rational A

rational R^2

Gauge symmetry enhancement

- **Untwisted** + **twisted** massless states

$$p_R = 0 \Rightarrow n = \left(R^2 + \frac{1}{2}A^2\right)\omega + \pi \cdot A \in \mathbb{Z}$$

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generic R

$$U(1)_L^8 \times U(1)_L^8 \times U(1)_L \times U(1)_R$$

no spinors (twisted or untwisted), **no massless scalars**

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$$G_1 \times U(1)_L^{8-k_1} \times G_2 \times U(1)_L^{8-k_2} \times U(1)_L \times U(1)_R \quad G_1, G_2 \subseteq SO(16)_{\text{ADE}}$$

maybe $\left\{ \begin{array}{l} \text{pos. chirality spinors in (spinor, 1) of some factor of } G_1, G_2 \\ \text{negative chirality spinors in (fund, spinor)} \end{array} \right.$

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may be: tachyons in all situations

Maximal (G : rank 17) enhancements

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- 107 in total

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- Only 8 without tachyons

L
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$SO(16) \times SO(10) \times SU(5)$
$SO(10) \times SO(10) \times SU(8)$
$SO(16) \times SO(18)$
$SO(16) \times SO(10) \times SO(8)$
$SO(12) \times SO(12) \times SU(4) \times SU(2)^2$
$E_6 \times SU(12)$

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L	R	N_v	N_s	N_c	N_0
$SO(16) \times SO(16) \times SU(2)$	$U(1)$	226	256	256	0
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	$U(1)$	180	192	192	0
$SO(16) \times SO(10) \times SU(5)$	$U(1)$	172	128	160	0
$SO(10) \times SO(10) \times SU(8)$	$U(1)$	136	0	170	0
$SO(16) \times SO(18)$	$U(1)$	256	128	288	256
$SO(16) \times SO(10) \times SO(8)$	$U(1)$	176	208	128	256
$SO(12) \times SO(12) \times SU(4) \times SU(2)^2$	$U(1)$	136	128	168	256
$E_6 \times SU(12)$	$SU(2)$	204	0	0	408

Maximal (G : rank 17) enhancements

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when moving slightly away in mod space
some become tachyonic



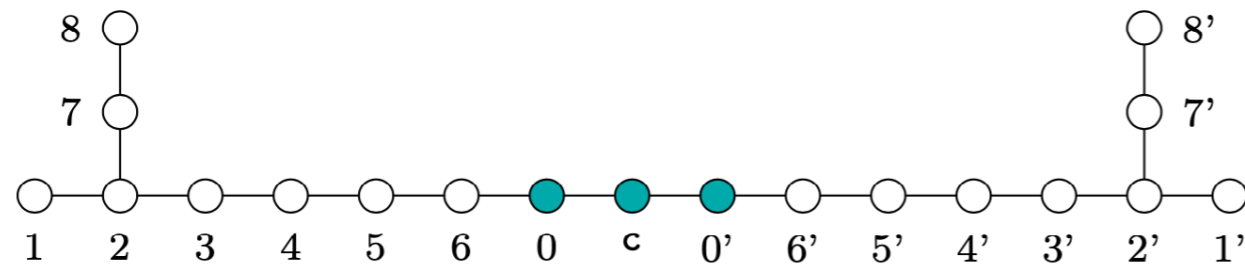
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All (maximal and non-maximal) enhancements from Extended Dynkin Diagram

- In **SUSY** case: all gauge groups, point/region where they occur & fundamental domain of moduli space from Extended Dynkin Diagram

Goddard, Olive 85

Cachazo, Vafa 00

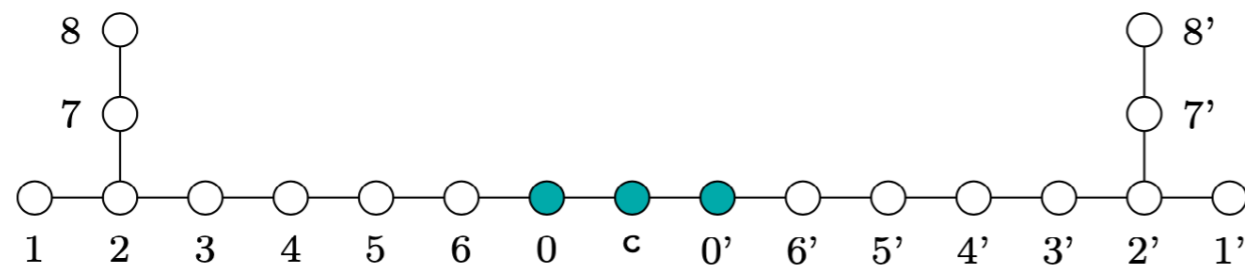


● momentum and/or winding on circle

All (maximal and non-maximal) enhancements from Extended Dynkin Diagram

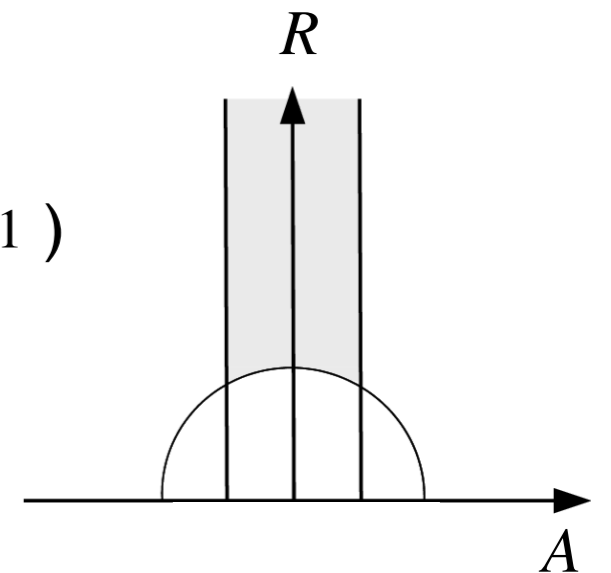
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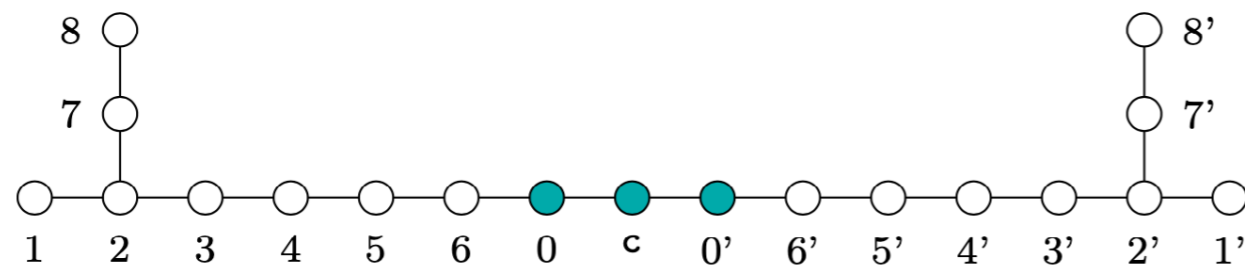
- 19 nodes, associated to 19 Weyl reflections in $\Gamma_{17,1}$
- Each node corresponds to a boundary in mod space (e.g. ●_c : $R^2 + \frac{1}{2}A^2 = 1$)
- Allows to get fundamental region



All (maximal and non-maximal) enhancements from Extended Dynkin Diagram

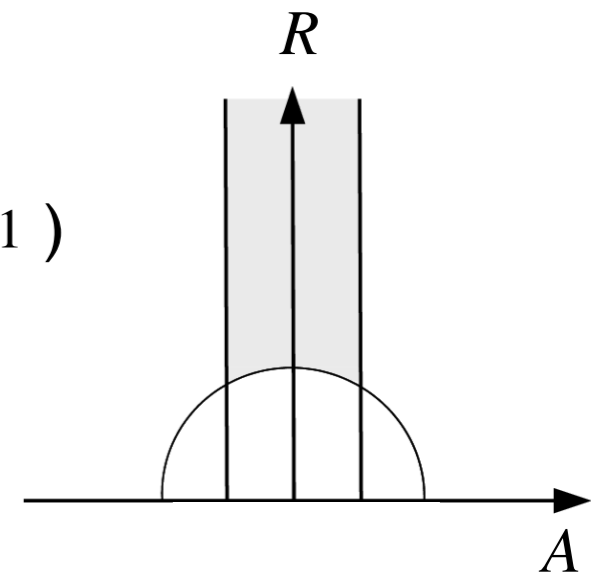
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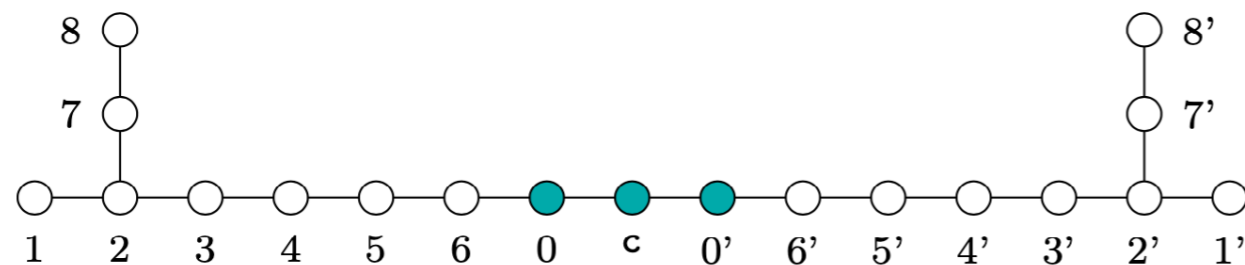


Surface (of codimension k) in mod space: satisfy the k eqs of remaining nodes

All (maximal and non-maximal) enhancements from Extended Dynkin Diagram

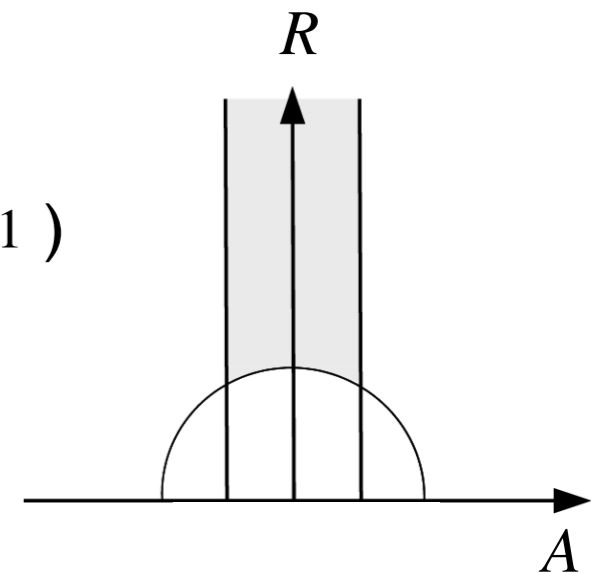
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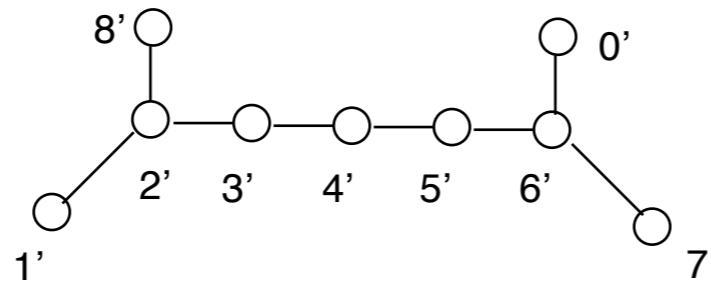
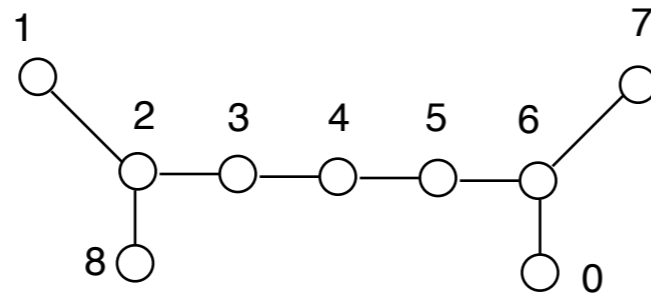


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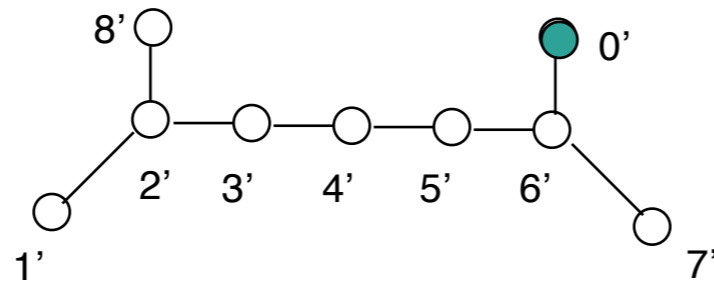
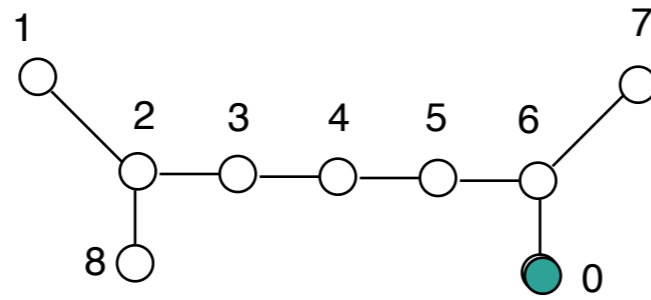
- What about **non-SUSY** case??

- We found an Extended Dynkin Diagram for **non SUSY** heterotic!

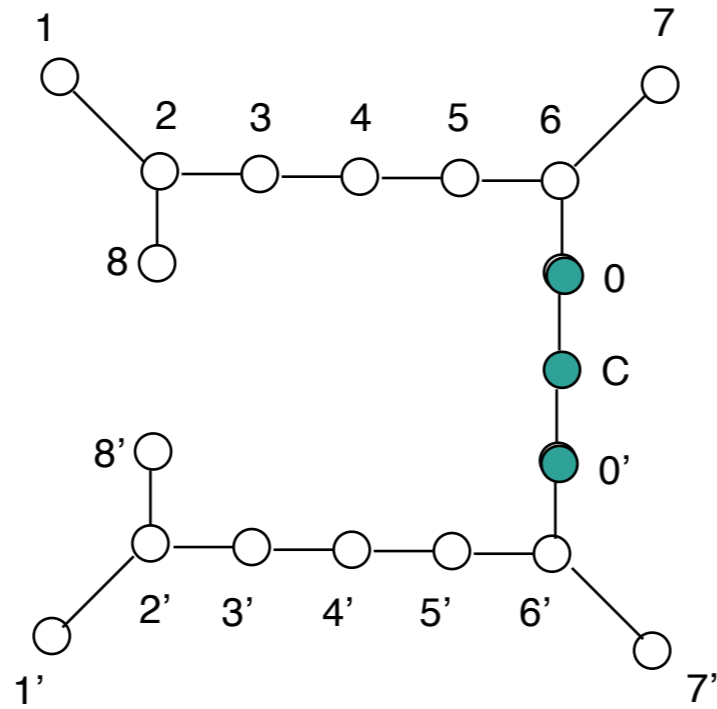
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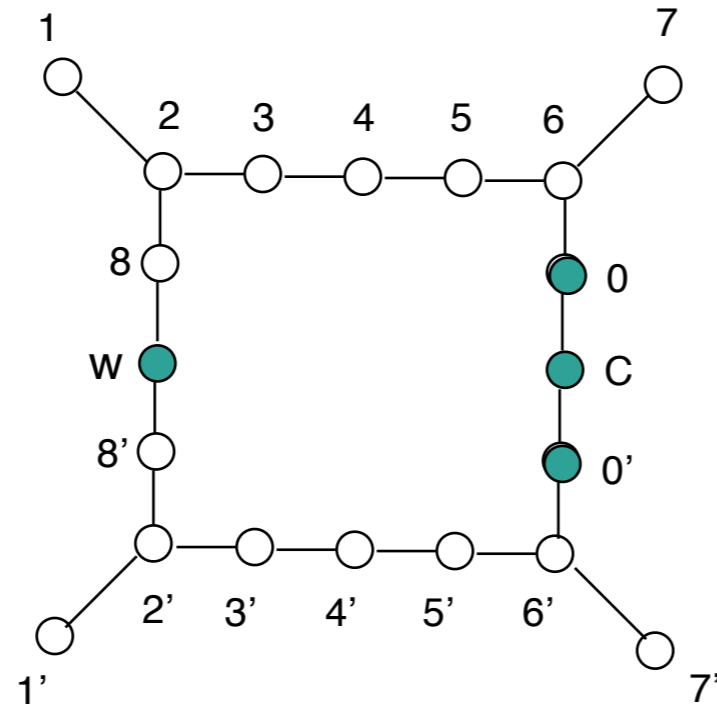
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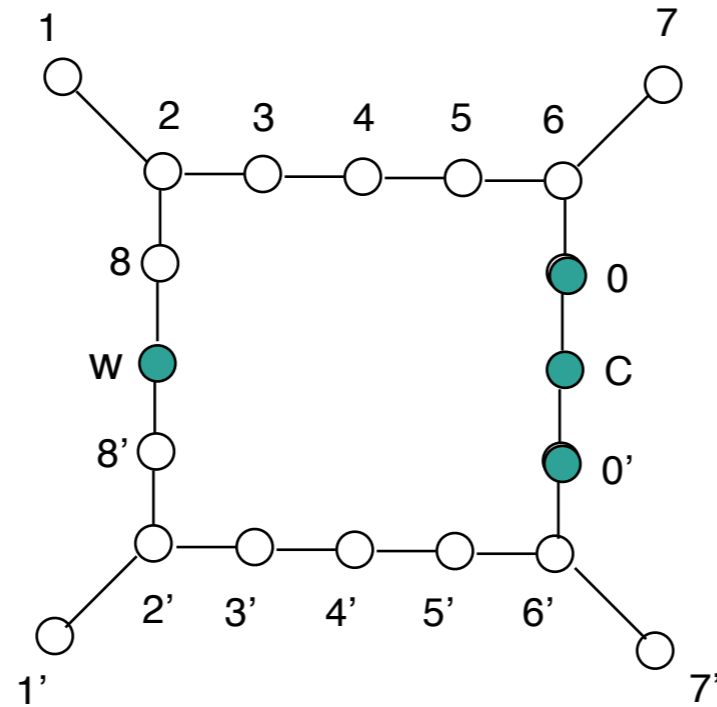
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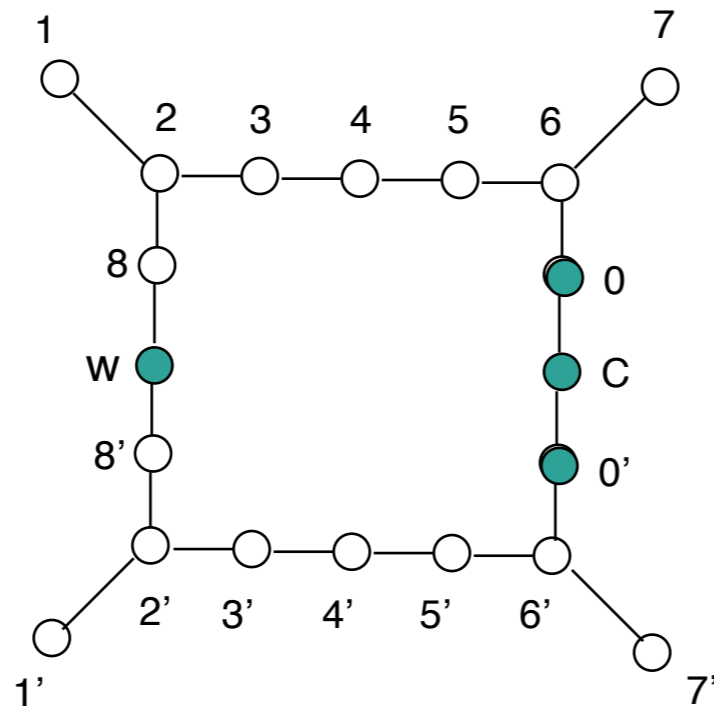


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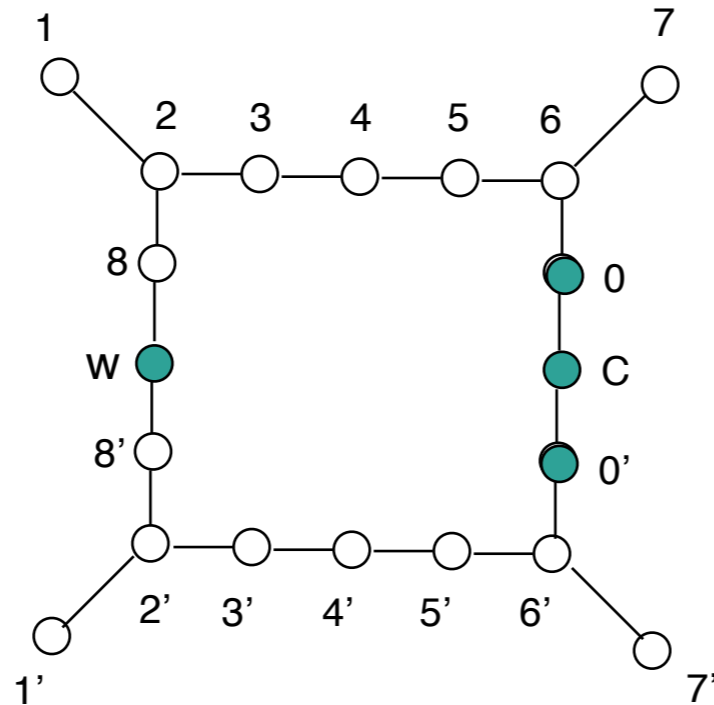


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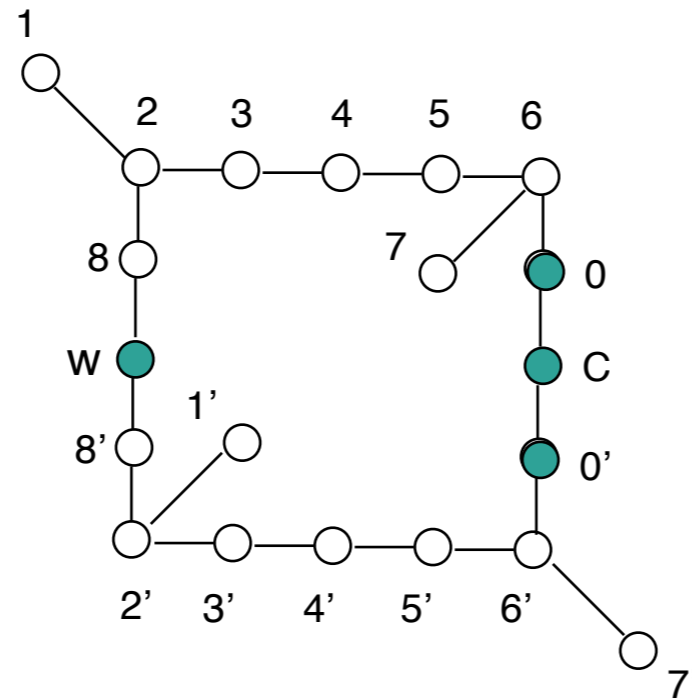


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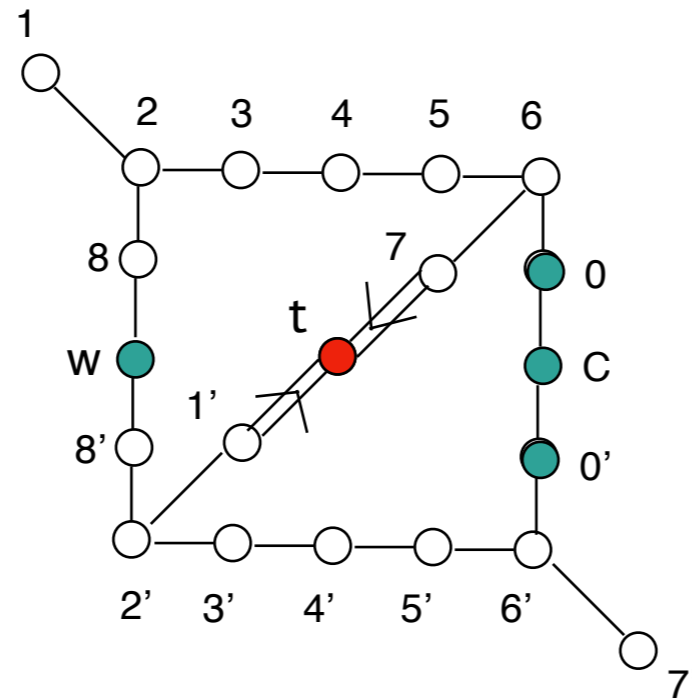


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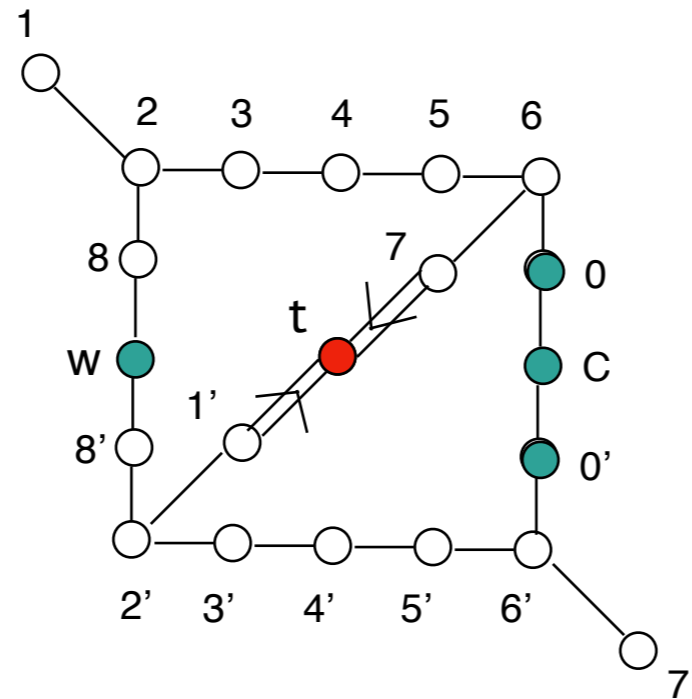


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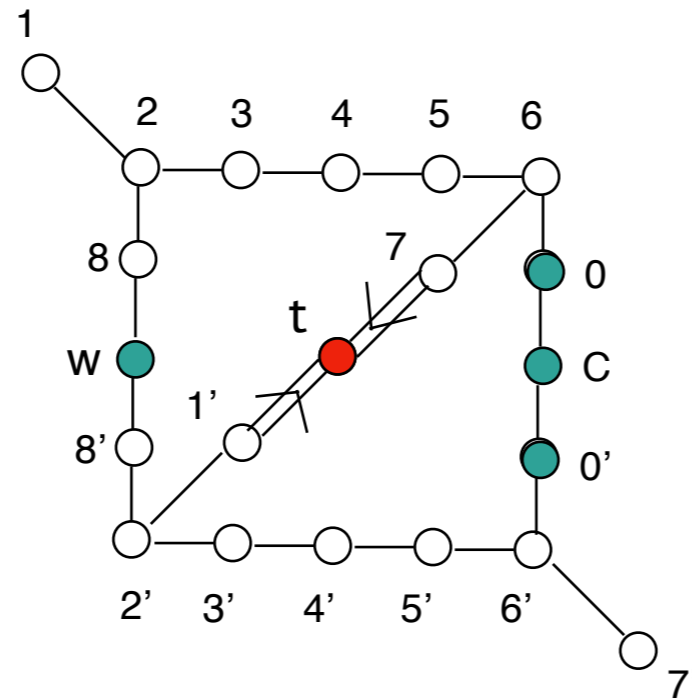


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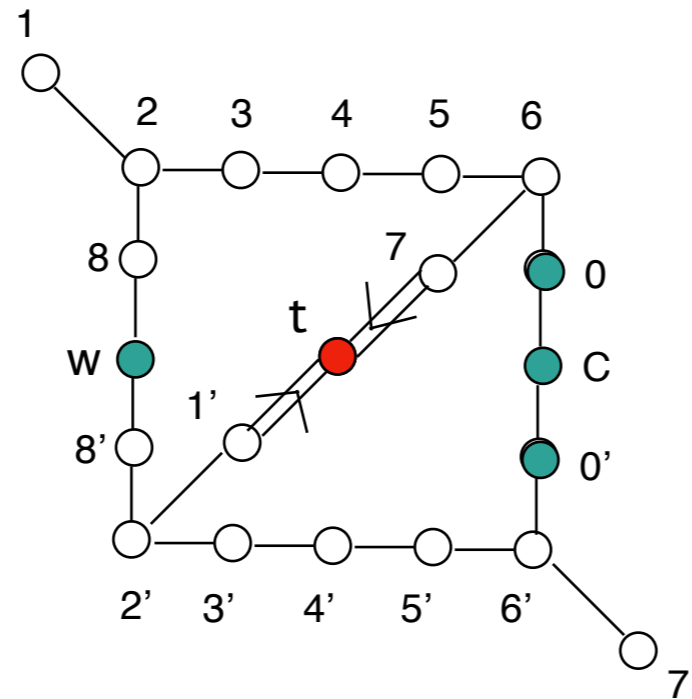


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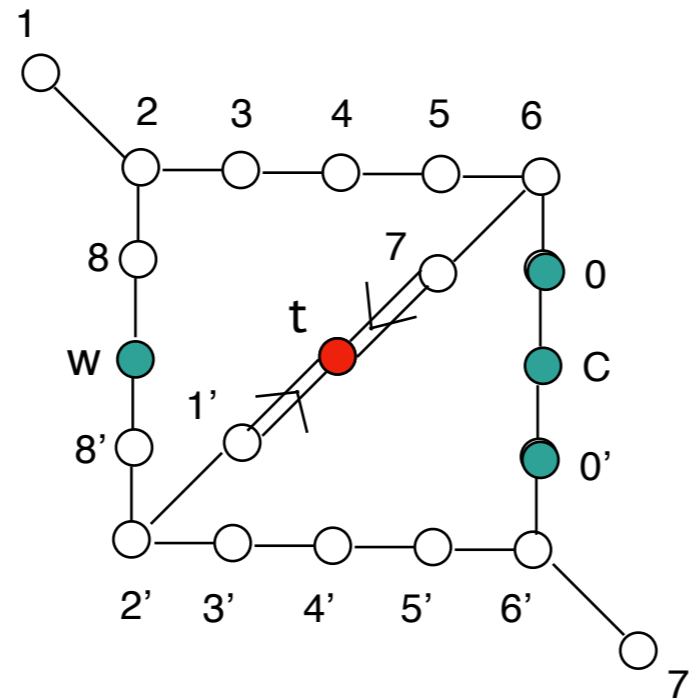
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see Fraiman and Collazuol's talk

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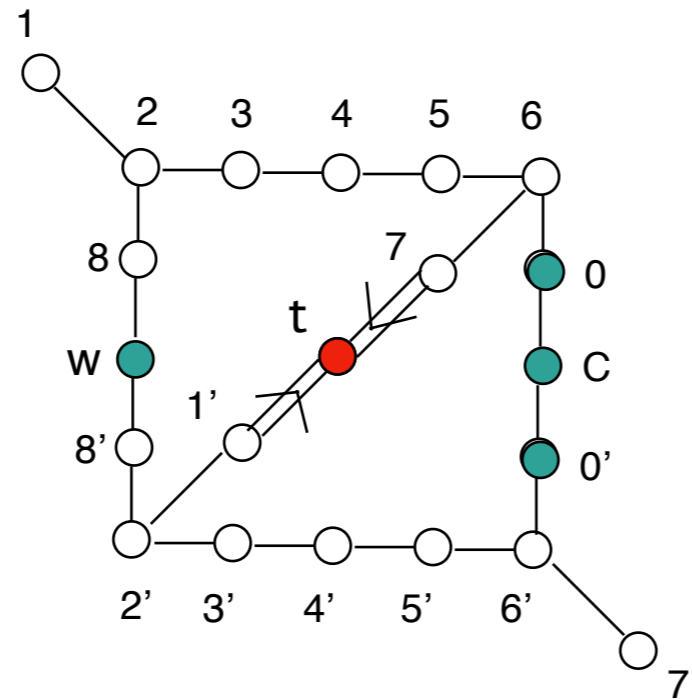
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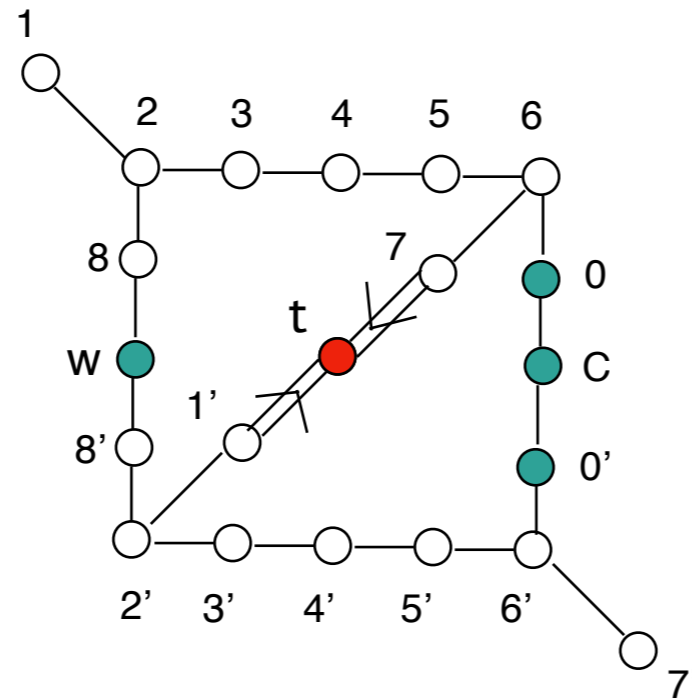
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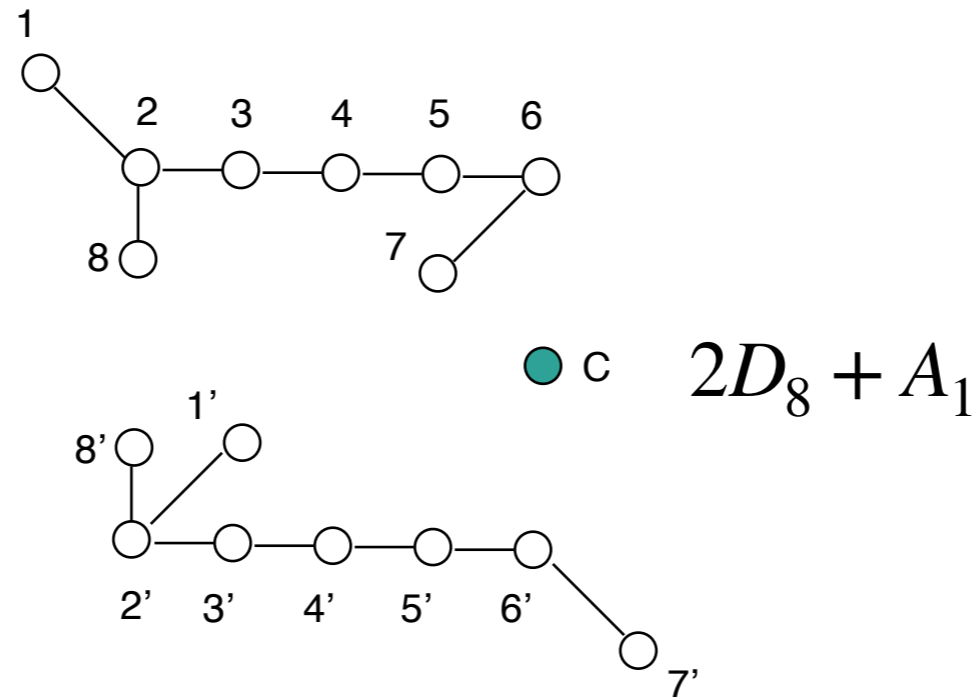
- Not needed for all practical purposes 😊

Classification of all non-Abelian gauge symmetry from EDD



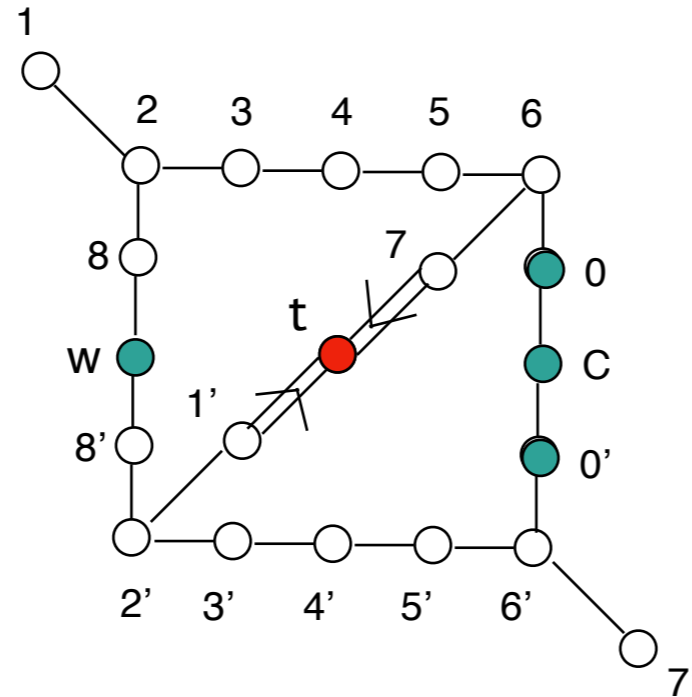
- Every non-Abelian group of rank k from deleting $2l-k$ nodes
- Surface (of codimension k) in mod space where a given group appears
 - require the k eqs of remaining nodes (e.g. if $\underset{c}{\bullet}$ remains $\Rightarrow R^2 + \frac{1}{2}A^2 = 1$)

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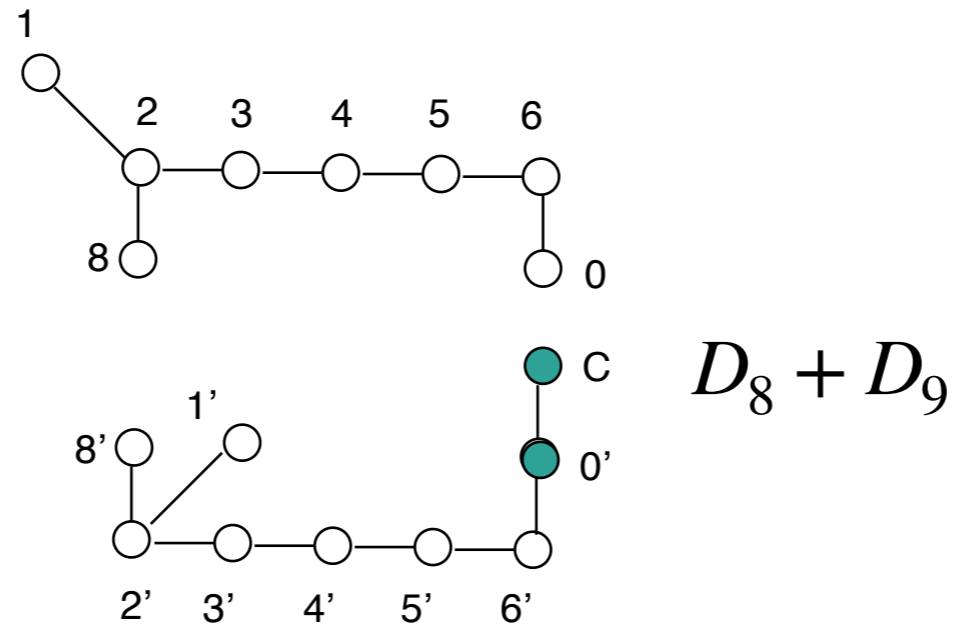
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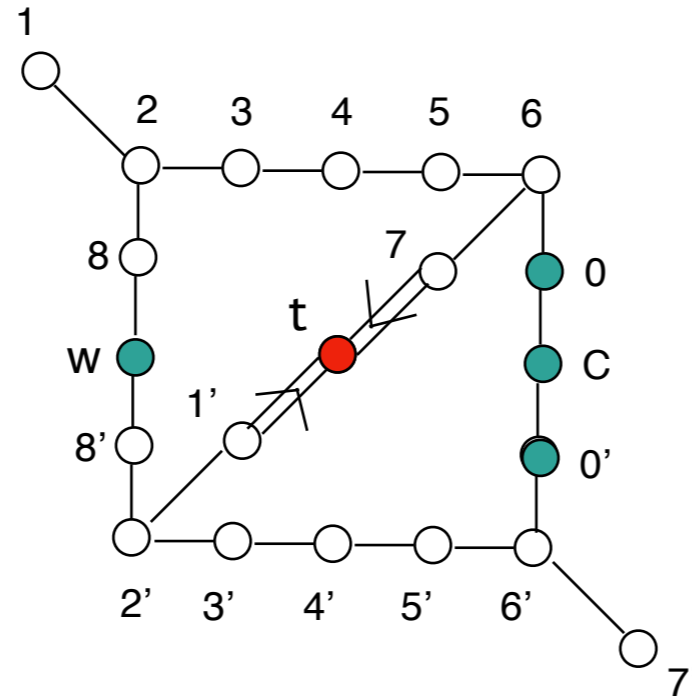
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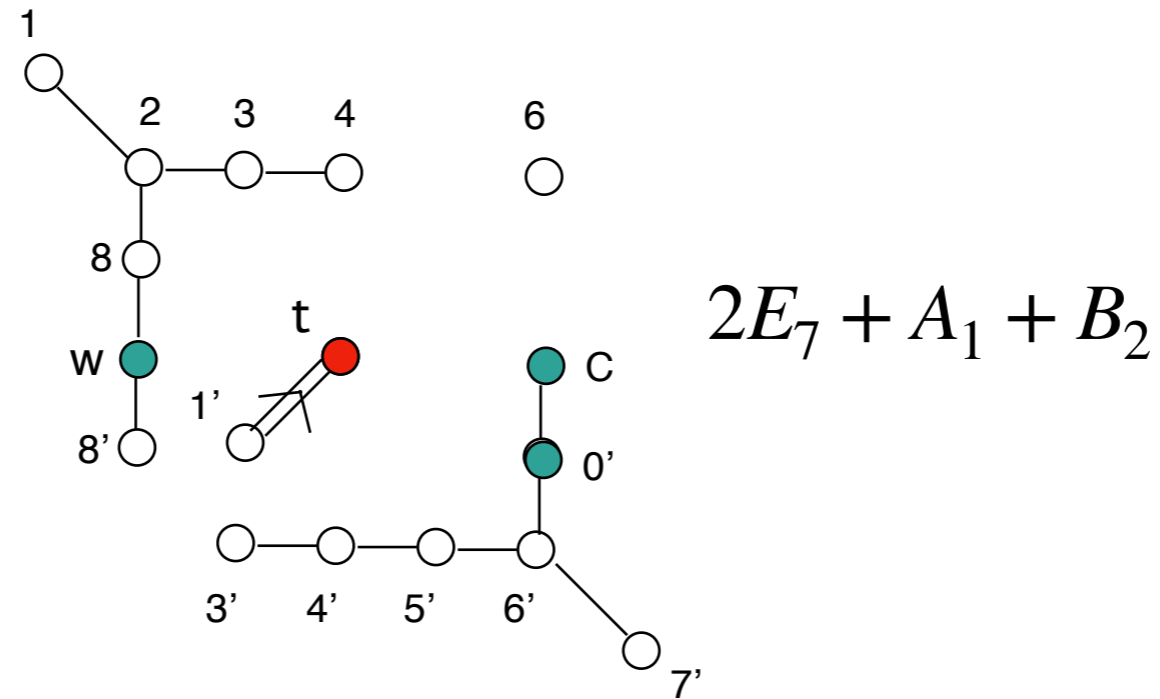
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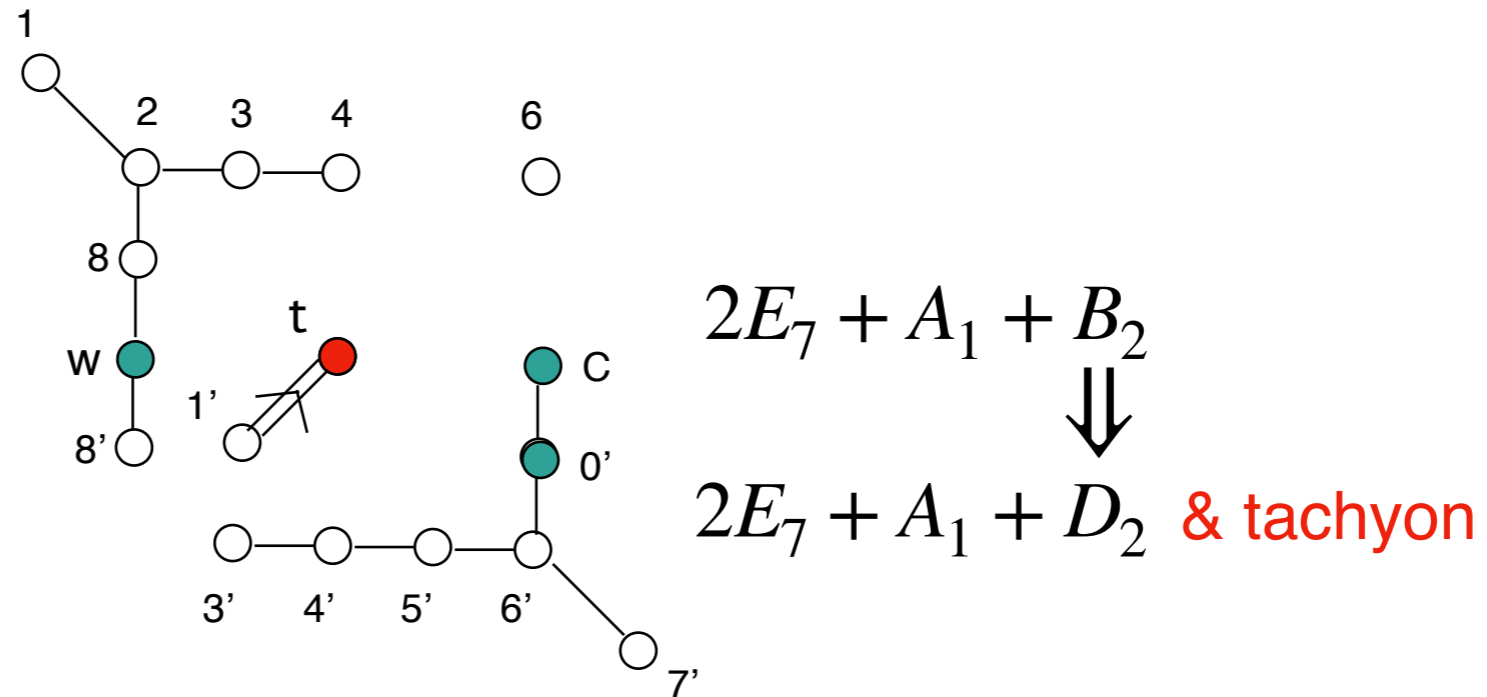
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Cosmological constant

- **Non-SUSY** \Rightarrow quantum potential for the moduli

$$\Lambda_{1\text{-loop}}(R, A) = \int_{F_0} \frac{d^2\tau}{2\tau_2^2} \mathbf{Z}(\tau, R, A)$$

$$\mathbf{Z} \sim \sum_{Z \in \Gamma} q^{\frac{p_L^2}{2}} \bar{q}^{\frac{p_R^2}{2}}$$

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- Before computing it, look at derivatives

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compute & get it's odd in p_R

Cosmological constant

- **Non-SUSY** \Rightarrow quantum potential for the moduli

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- At points in moduli space of maximal (rank $d+16$) enhancement

Weyl reflection

Ginsparg, Vafa 86

$$\forall Z \in \Gamma \quad Z \xrightarrow{\text{Weyl reflection}} Z' \quad \Rightarrow \quad \nabla \mathbf{Z} = 0 \quad \Rightarrow \quad \nabla \Lambda = 0 \quad \text{at ALL loops!}$$

$$p_R(Z) = -p_R(Z')$$

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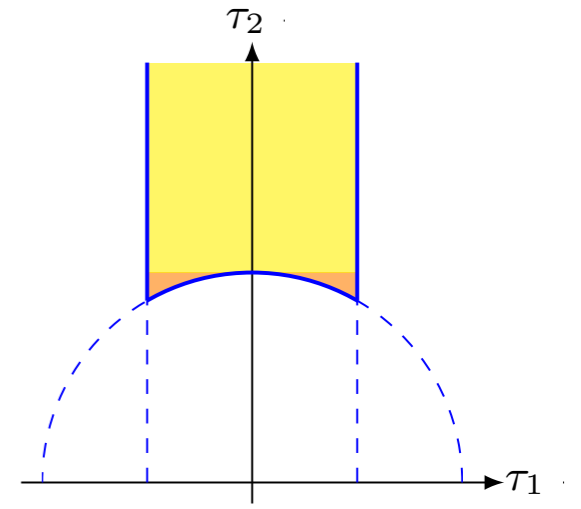
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Ginsparg, Vafa 86

- Points of maximal enhancement $\Rightarrow \nabla \Lambda = 0$ $\nabla^2 \Lambda = 0?$
- ~~\Leftarrow~~ we found counterexamples

Computing cosmological constant

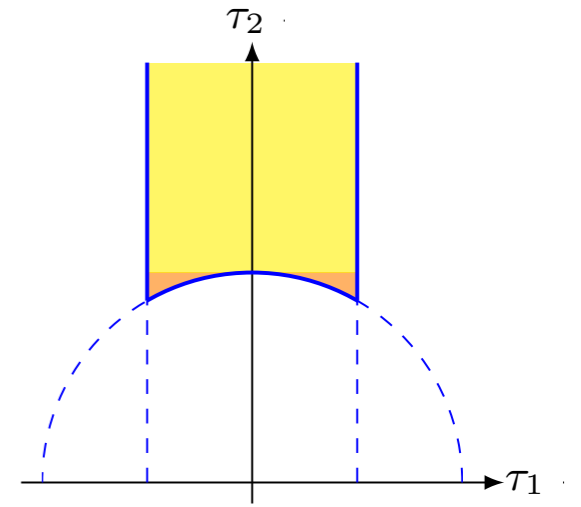
- One-loop cosmological constant for non susy heterotic



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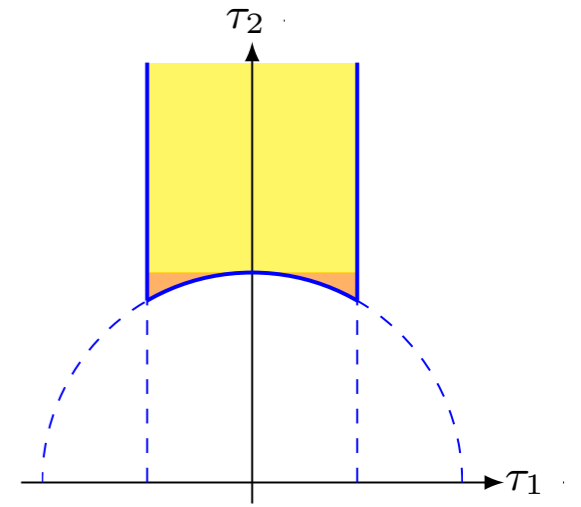
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↑
only positive powers

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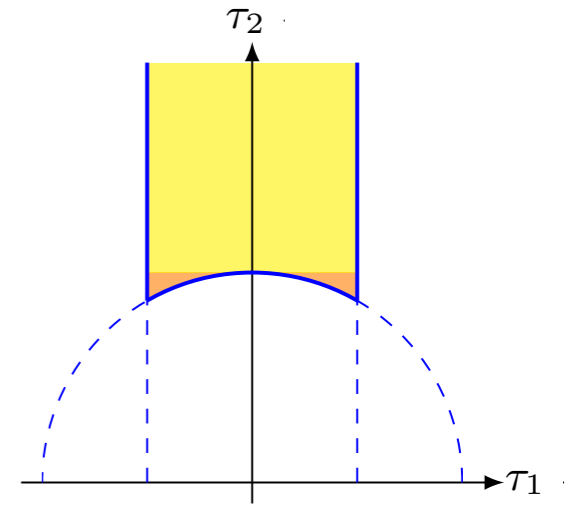
$$P_L^2 + p_R^2 \geq 2 \quad \text{for } P \in \Gamma_{v,s,c}$$

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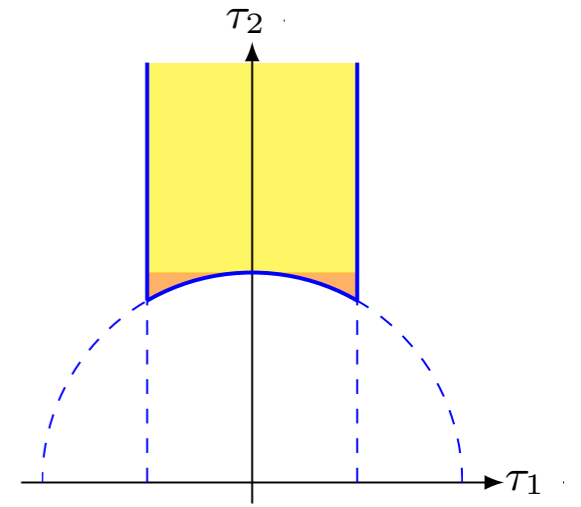
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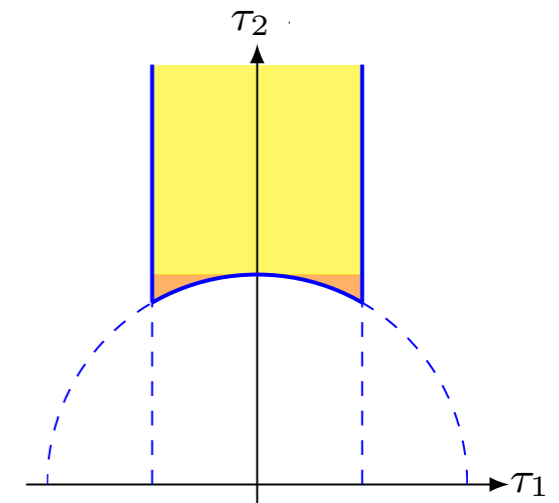
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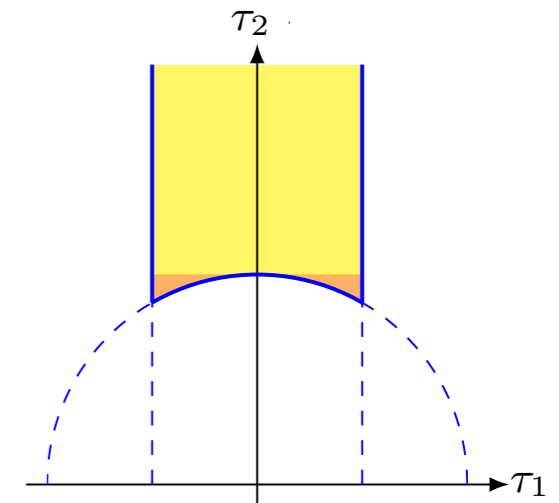
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L	N_v	N_s	N_c	N_0	$\Lambda_{m=0}$
$SO(16) \times SO(16) \times SU(2)$	226	256	256	0	341.6
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	180	192	192	0	251.8
$SO(16) \times SO(10) \times SU(5)$	172	128	160	0	155.4
$SO(10) \times SO(10) \times SU(8)$	136	0	170	0	65.6
$SO(16) \times SO(18)$	256	128	288	256	168.7
$SO(16) \times SO(10) \times SO(8)$	176	208	128	256	168.7
$SO(12) \times SO(12) \times SU(4) \times SU(2)^2$	136	128	168	256	168.7
$E_6 \times SU(12)$	204	0	0	408	-243.7

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- Light states can correct this quite significantly

Cosmological constant: results

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L	N_v	N_s	N_c	N_0	$\Lambda_{m=0}$	Λ
$SO(16) \times SO(16) \times SU(2)$	226	256	256	0	341.6	431.4
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	180	192	192	0	251.8	383.5
$SO(16) \times SO(10) \times SU(5)$	172	128	160	0	155.4	359.2
$SO(10) \times SO(10) \times SU(8)$	136	0	170	0	65.6	303.8
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Cosmological constant at points of tachyon-free maximal enhancement

L	Λ
$SO(16) \times SO(16) \times SU(2)$	431.4
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	383.5
$SO(16) \times SO(10) \times SU(5)$	359.2
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ALL positive!

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$SO(12) \times SO(12) \times SU(4) \times SU(2)^2$	305.0
$E_6 \times SU(12)$	180.4

ALL positive!

- What happens at the vicinity?
- Bernardo Fraiman will show beautiful plots of the cosmological constant for 2d slices in mod space

Cosmological constant at points of tachyon-free maximal enhancement

massless scalars that get tachyonic when
moving in certain directions in mod space



L	Λ	N_0
$SO(16) \times SO(16) \times SU(2)$	431.4	0
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	383.5	0
$SO(16) \times SO(10) \times SU(5)$	359.2	0
$SO(10) \times SO(10) \times SU(8)$	303.8	0
$SO(16) \times SO(18)$	305.0	256
$SO(16) \times SO(10) \times SO(8)$	305.0	256
$SO(12) \times SO(12) \times SU(4) \times SU(2)^2$	305.0	256
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} knife edge



Ginsparg-Vafa
knife edge:
Capitol Peak near Aspen

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L	Λ	N_0	$\nabla^2 \Lambda \times R^2$
$SO(16) \times SO(16) \times SU(2)$	431.4	0	$-306^{16}, 831$
$SO(16) \times SO(12) \times SU(3) \times SU(2)$	383.5	0	$-307^{15}, 544^2$
$SO(16) \times SO(10) \times SU(5)$	359.2	0	$-569^5, -256^8, 355^4$
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$SO(16) \times SO(18)$	305.0	256	} knife edge
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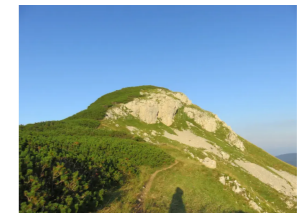
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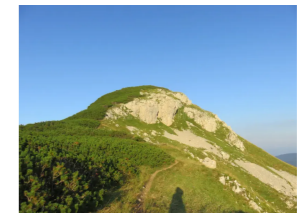
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} saddle points

local maximum



Ginsparg-Vafa
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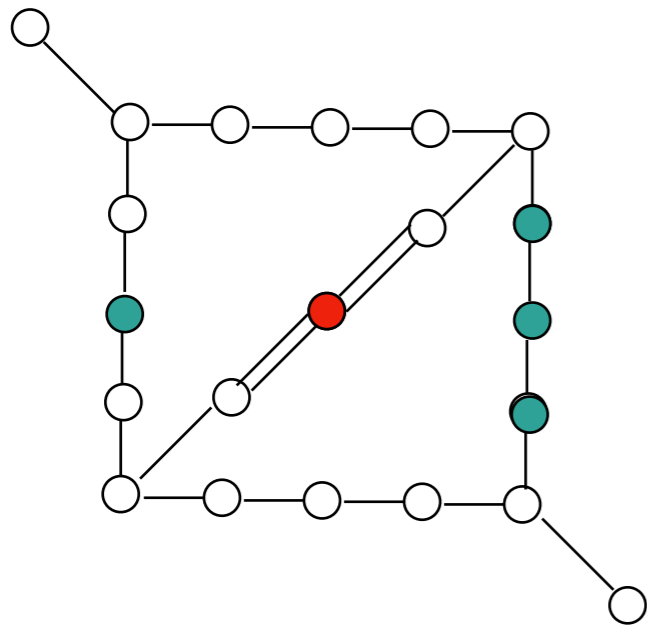
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Summary

- Toroidal compactification of the non-susy heterotic theories give a rich landscape

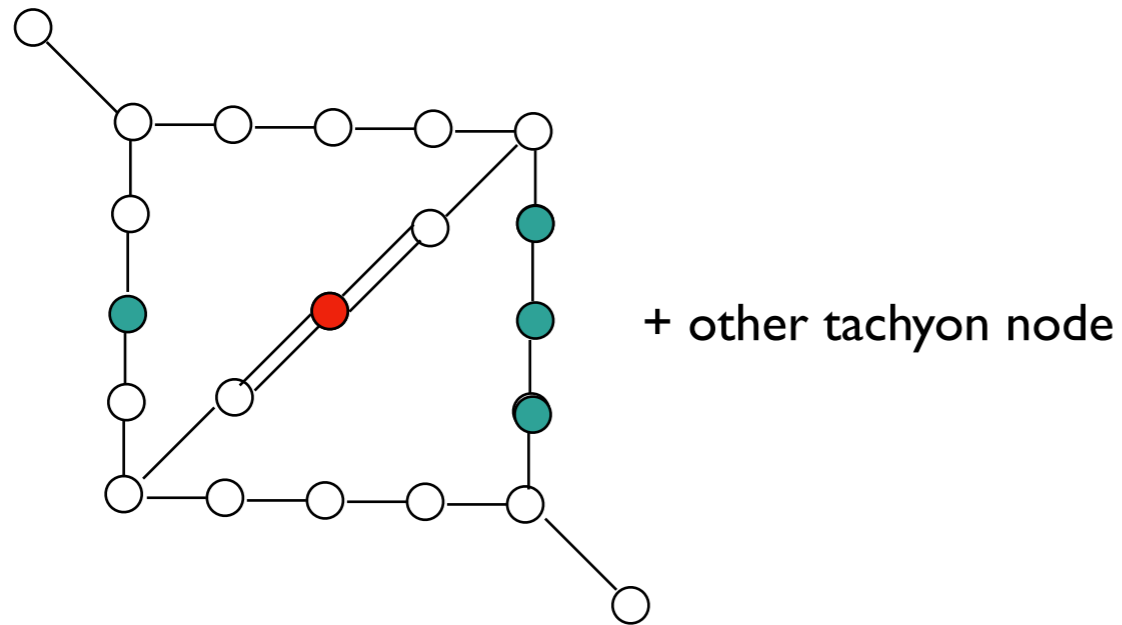
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- Toroidal compactification of the non-susy heterotic theories give a rich landscape
- Phenomena of gauge symmetry enhancement in S^1 : encoded in Extended Dynkin diagram



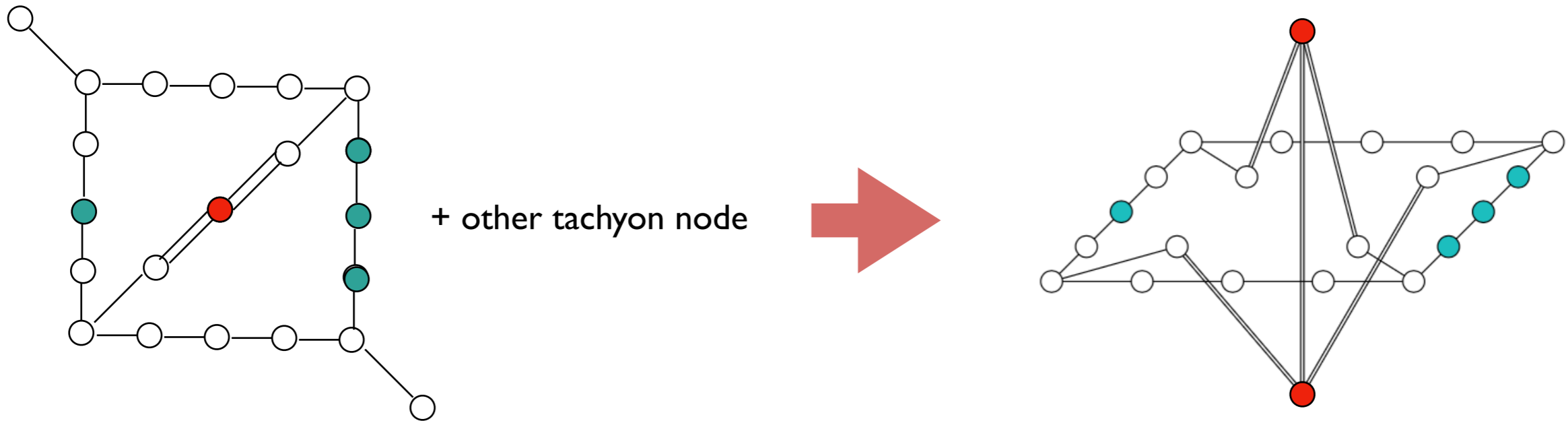
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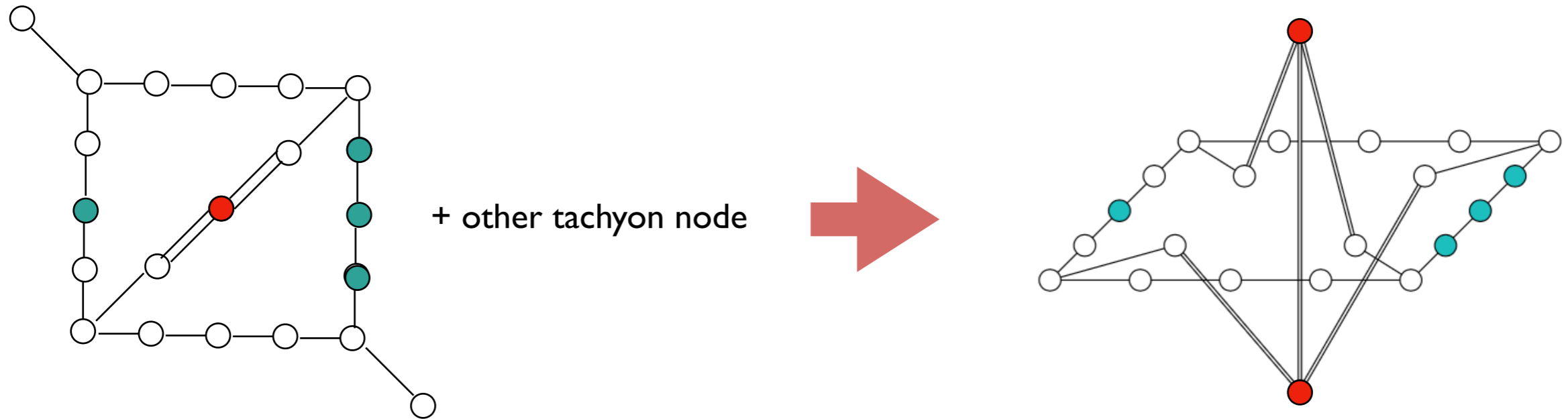
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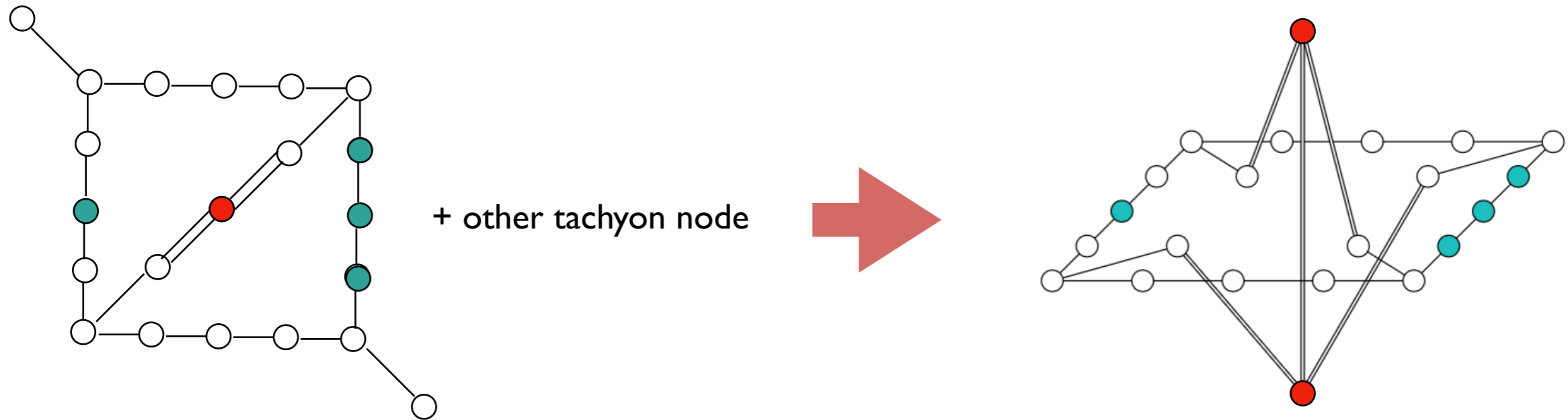
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- 107 maximal enhancements (delete 4 nodes from diagram on the left)

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- 107 maximal enhancements (delete 4 nodes from diagram on the left)
- Only 8 tachyon-free

Summary

- Cosmological constant extremized at points of maximal enhancement (but not only)

see Fraiman's talk

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saddle points $\left\{ \begin{array}{l} SO(16) \times SO(16) \times SU(2) \\ SO(16) \times SO(12) \times SU(3) \times SU(2) \\ SO(16) \times SO(10) \times SU(5) \end{array} \right.$

local maximum $SO(10) \times SO(10) \times SU(8)$

knife edges $\left\{ \begin{array}{l} SO(16) \times SO(18) \\ SO(16) \times SO(10) \times SO(8) \\ SO(12) \times SO(12) \times SU(4) \times SU(2)^2 \\ E_6 \times SU(12) \end{array} \right.$

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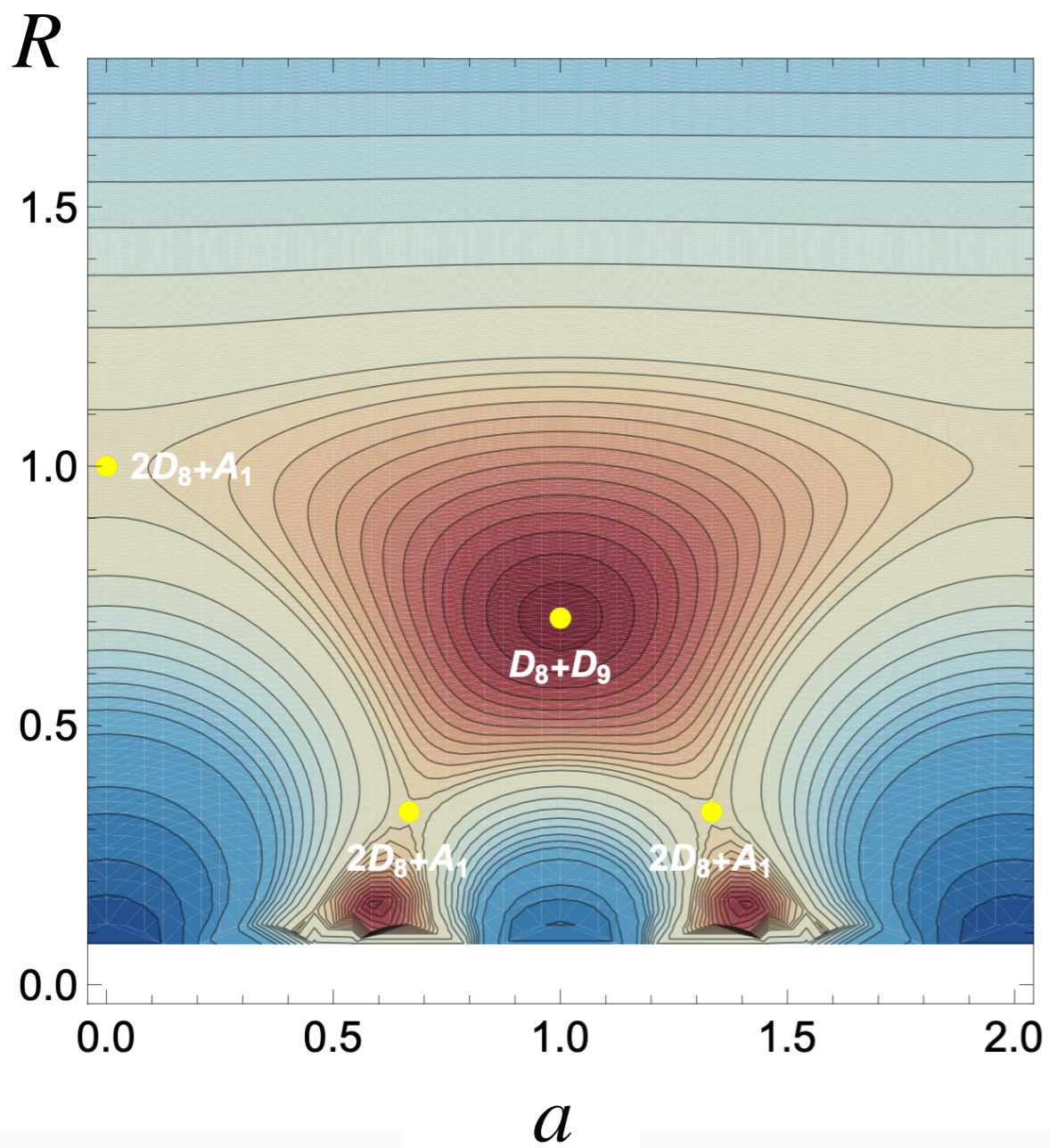
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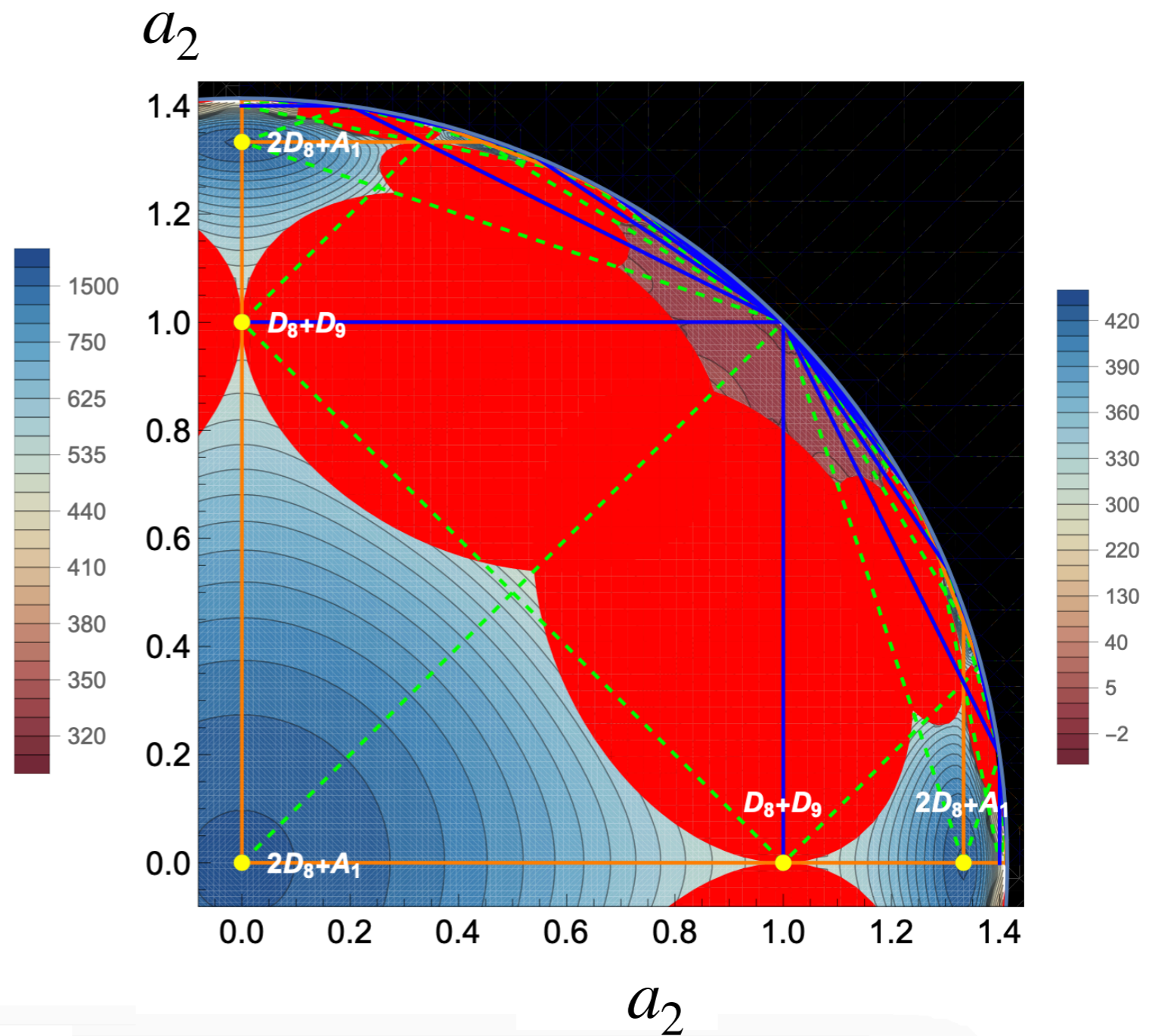
- Does this story change in T^2 compactifications?

To be continued...

Thank you!



$$A = (a, 0^{15})$$



$$A = (a_1, 0^7, a_2, 0^7)$$

$$R^2 = 1 - \frac{1}{2}A^2$$